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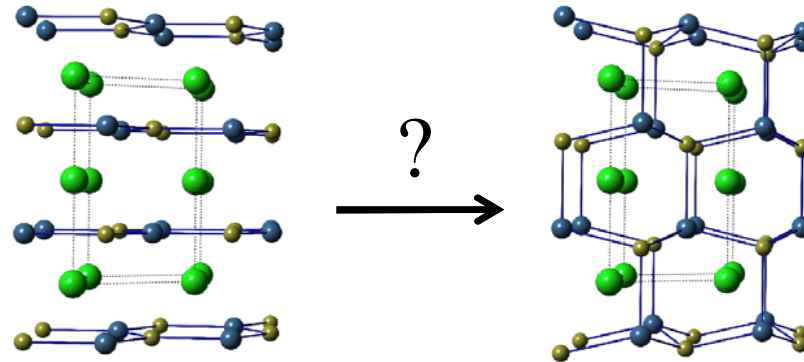
**16th International Workshop on Computational Physics and Materials Science:
Total Energy and Force Methods**

10 - 12 January 2013

**New classes of piezoelectrics, ferroelectrics, and antiferroelectrics by first-
principles high-throughput materials design**

Joseph W. Bennett
*Rutgers University
USA*

New Classes of Piezoelectrics, Ferroelectrics, and Antiferroelectrics by First-Principles High-Throughput Materials Design



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Emerging Technologies...

In order to solve the problems facing us in the 21st century there arises a critical need for new technologies based on multifunctional materials.

High speed, low power computation

Improved communications

High yield energy conversion and storage

Most of the solutions could arise from an improved understanding of **nanoscale phenomena**...

specifically **atomistic interactions** and how they affect the **measurable properties** of a device.

Critical need to successfully couple theoretical modeling and experimental endeavors.

Our Approach

To **design and discover new multifunctional materials** we combine:

1) **Crystallographic database searching**
(Inorganic Crystal Structural Database)

input structural information

and

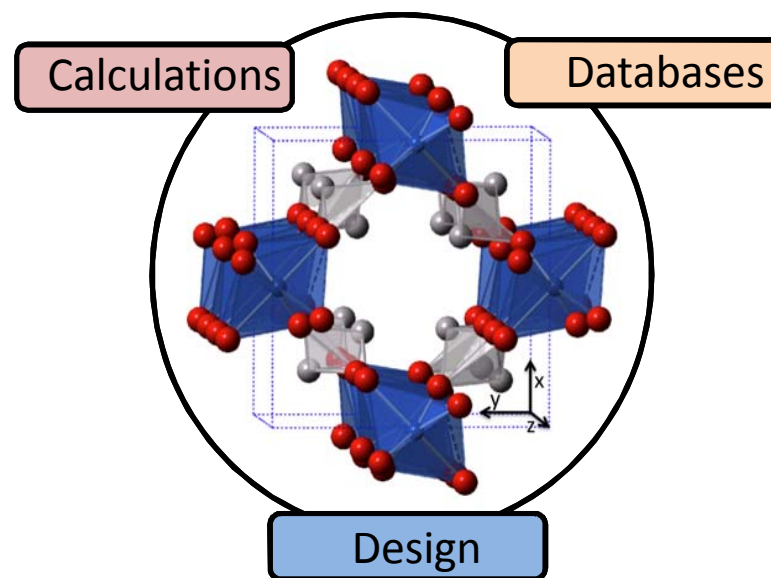
2) **First-principles calculations**

(Density Functional Theory: LDA)

output properties

Structure-property relations...
platforms for functionality

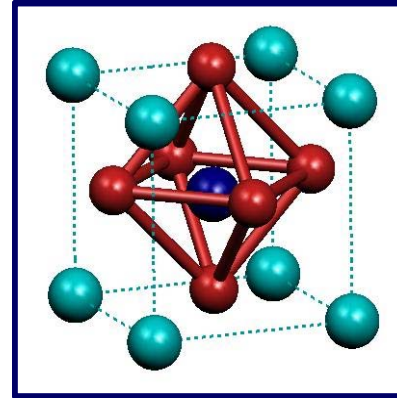
We perform **high-throughput studies** of underdeveloped **families of materials** to screen for **exceptional members** of potentially functional families.



Outline

The ABO_3 Perovskites

A Canonical Family



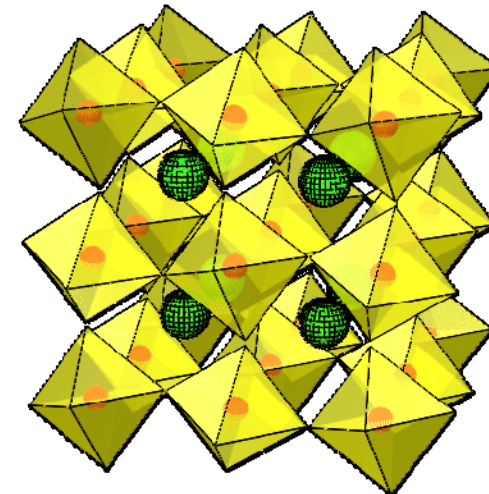
Moving Beyond the Perovskites

A New Class of Piezoelectrics

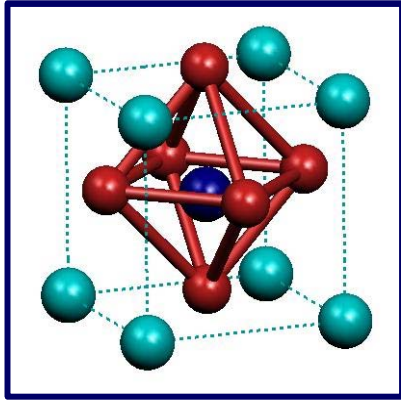
A New Class of Ferroelectrics

A New Class of Antiferroelectrics

Concluding Thoughts



The Perovskites: A Canonical Family



ABO_3 solid oxide perovskites:

A at corners (12-fold coordinate)

B inside of O octahedron
(6-fold coordinate)

O octahedron are **corner-sharing**

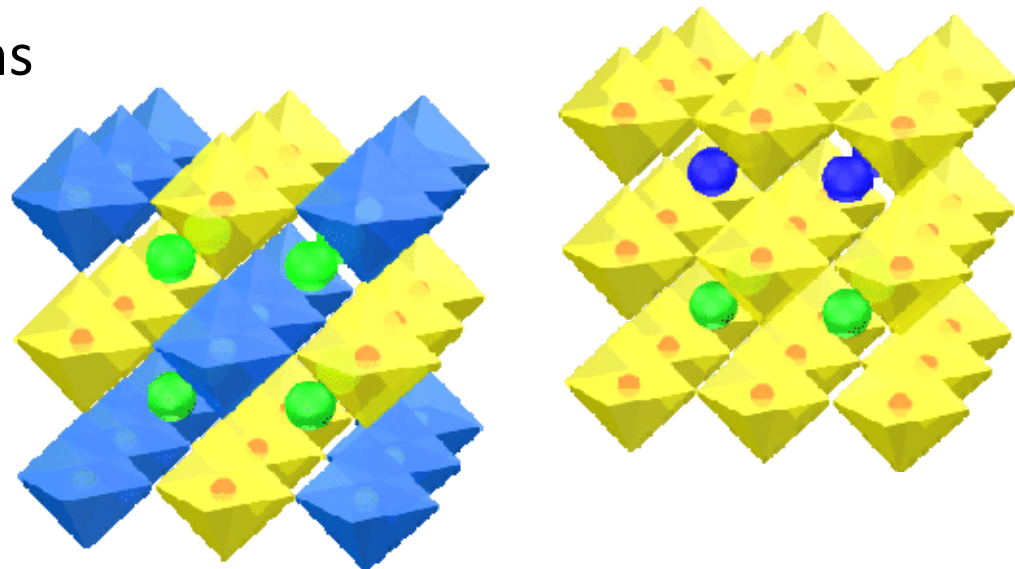
Flexible structure with choice
of *A* and *B* sites combinations
almost unlimited

$PbTiO_3$, $BaZrO_3$, $LiNbO_3$

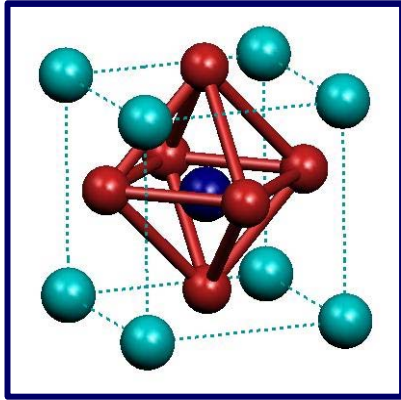
Solid solutions as well

$AA'BB'O_3$

$Pb(Zr,Ti)O_3$



The Perovskites: A Functional Family



ABO_3 solid oxide perovskites:

A at corners (12-fold coordinate)

B inside of O octahedron
(6-fold coordinate)

O octahedron are **corner-sharing**

Flexible structure with choice
of *A* and *B* sites combinations
almost unlimited

$PbTiO_3$, $BaZrO_3$, $LiNbO_3$

Solid solutions as well

$AA'BB'O_3$

$Pb(Zr,Ti)O_3$

**A piezoelectric used in a
variety of applications!**

SONAR

ultrasound

positioning

sensors and actuators

BiFeO₃: A Multifunctional Perovskite

Bi distort **along (111)** as O₆ tilt to generate **R_{3c}** symmetry, a **polar** space group.

This polarization is reversible: **ferroelectric**.

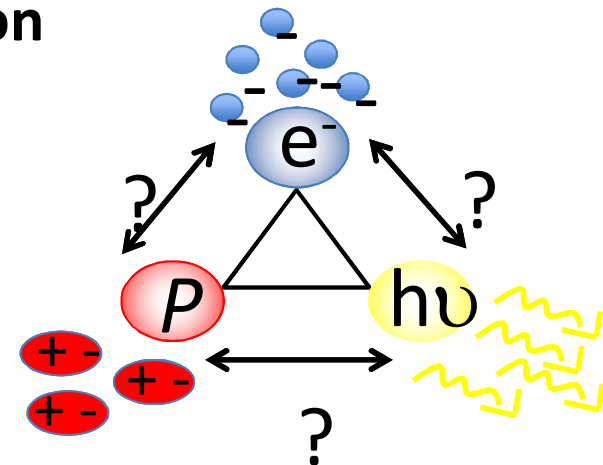
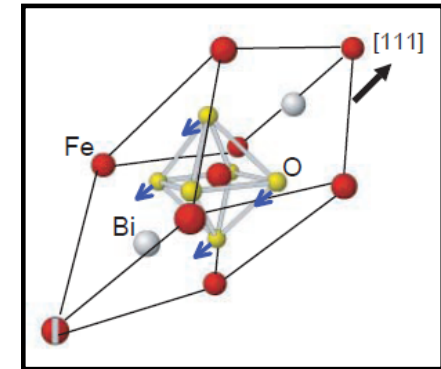
AND...Fe³⁺ is **magnetic**

We can **couple polarization and magnetization** in one material!

AND...BiFeO₃ shows BPVE with **visible light!**

AND...it's been incorporated as a diode!

We want more materials like BiFeO₃!

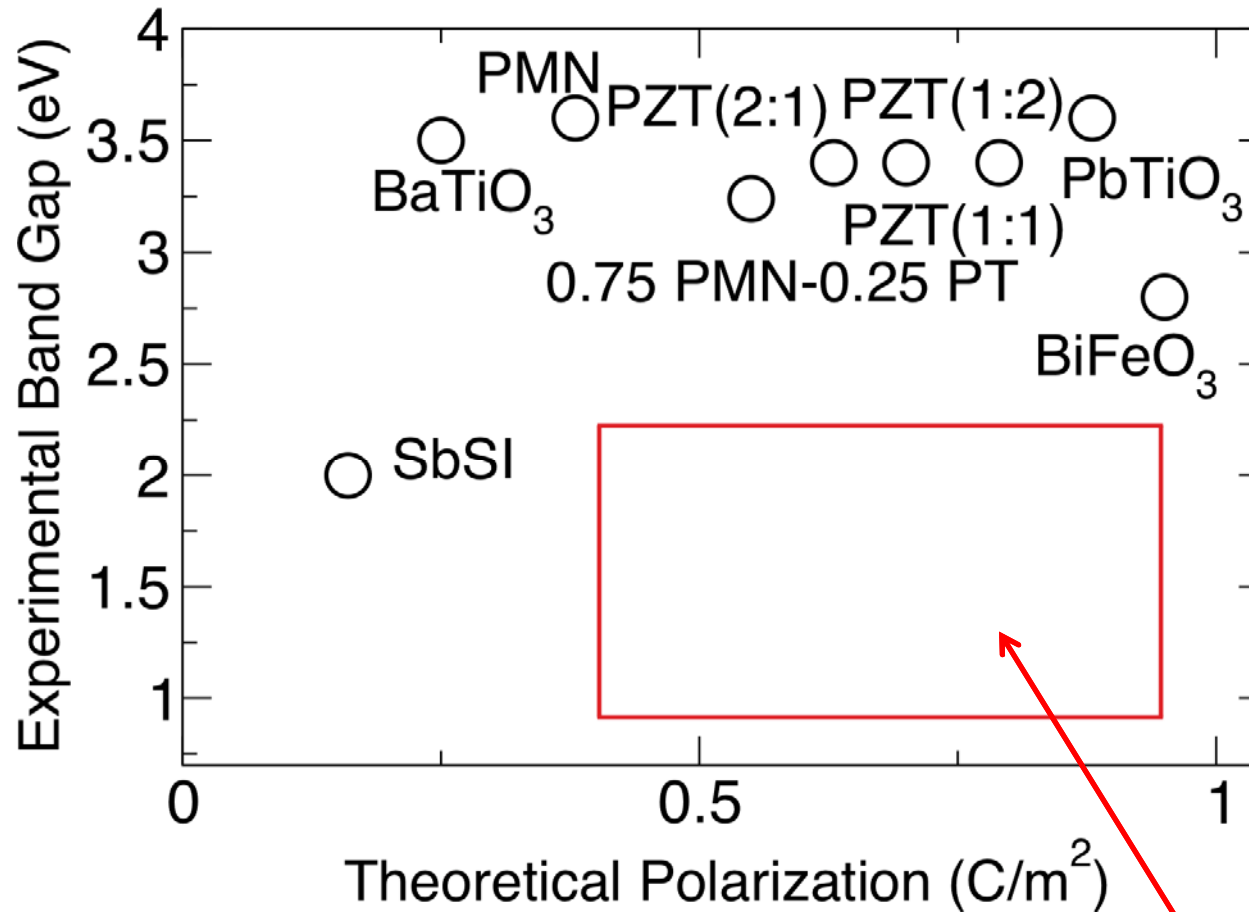


Wang *et al.*, Science 2003, 1719

Choi *et al.*, Science 2009, 63

Katiyar & Scott, 2011

What About the Band Gap?

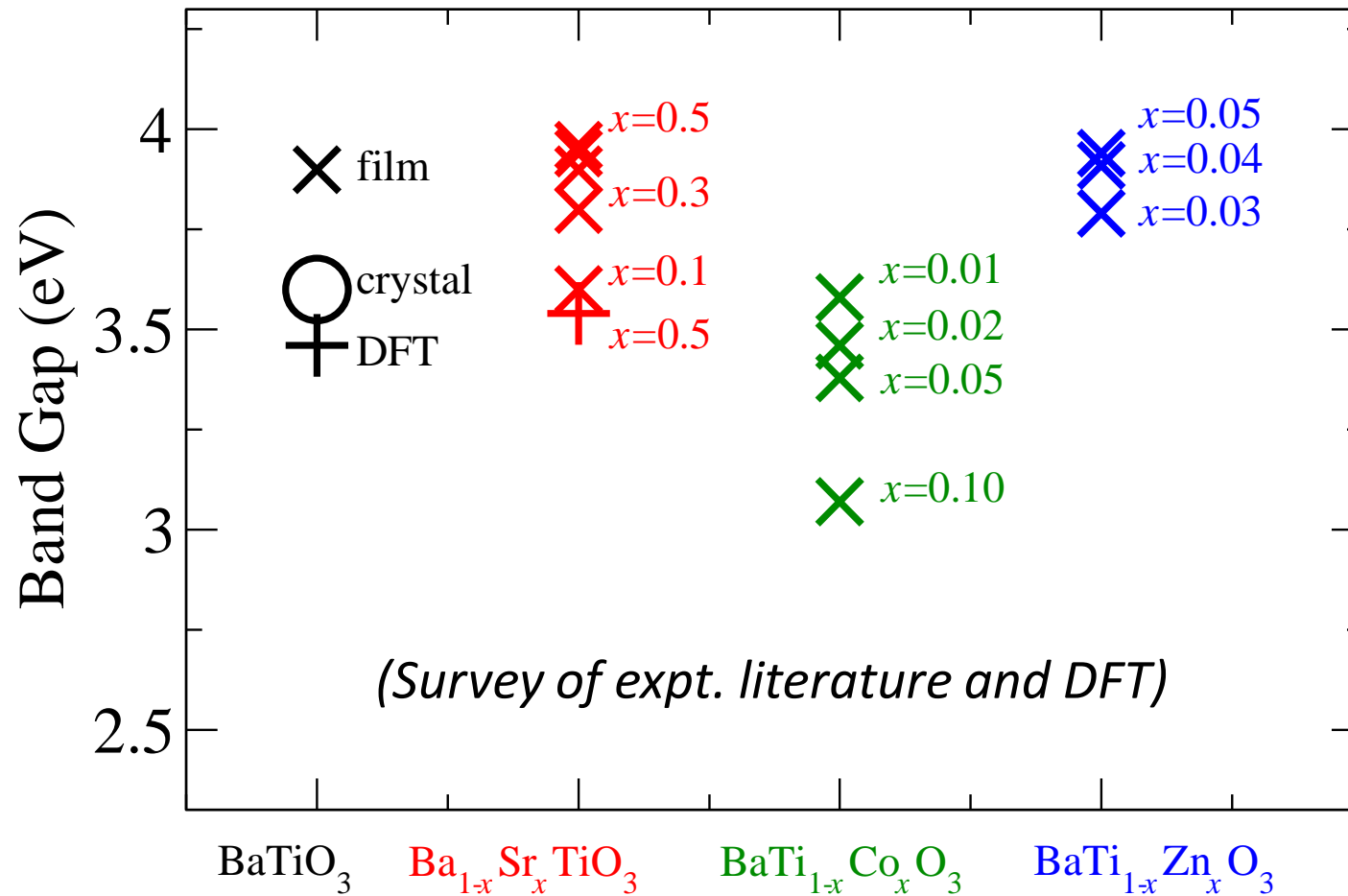


Interesting phase space to explore.

Can we go **beyond BiFeO₃**?

How do we do that? Solid solutions?

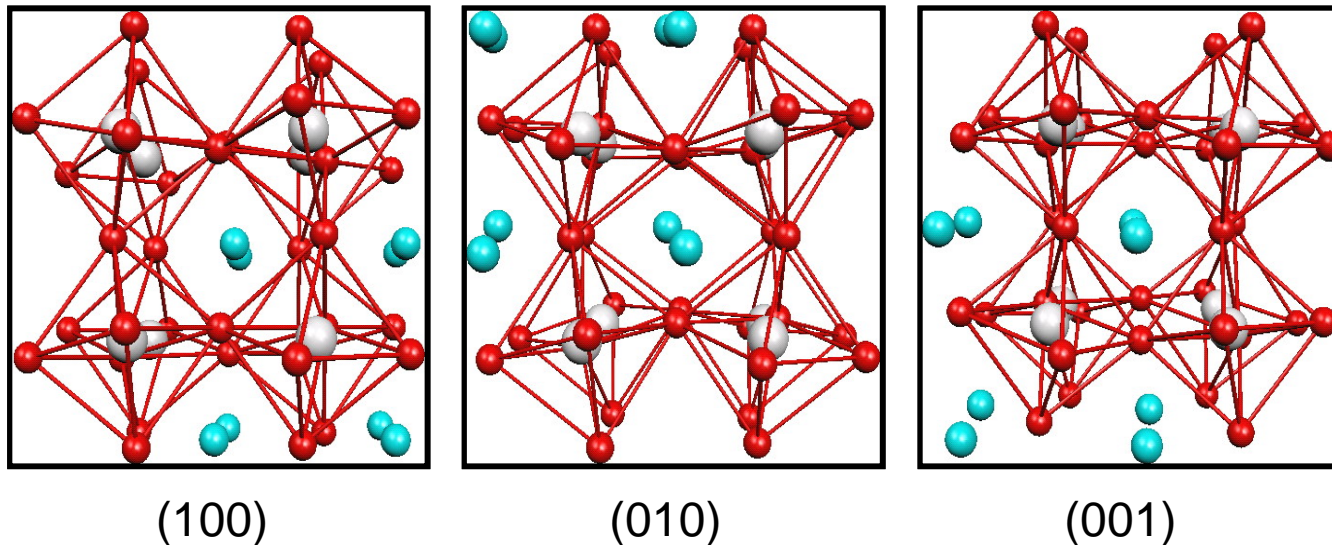
Band Gaps of Solid Solutions of BaTiO₃



Sulfide Perovskites?

BaZrS₃: DFT **band gap decreases**
from 3.9 to 1.7 eV relative to BaZrO₃

Non-polar -- **Pnma** symmetry:
rotations hinder concerted displacements...
Most are non-polar orthorhombic or
hexagonal...**no ferroelectric effect!**



High-Throughput Search: New Perovskites

So far, we've only discussed studying a few materials at one time...
but what about many at once?

Since 2005, the **Ceder group at MIT** has published extensively on a combination of adapted machine learning, database mining and first-principles screening to search for new materials.

Morgan et al., *Mat. Sci. Tech.* 296 (2005)

Fischer et al., *Nature Mater.* 641 (2006)

Hautier et al., *Chem. Mater.* 3762 (2010)

Armiento et al., *Phys. Rev. B.* 014103 (2011)

Jain et al., *Comp. Mat. Sci.* 2295 (2011)

They've uncovered about **50 candidate ABO_3** compounds as targets for materials realization...**most of which are as yet to be synthesized!**

Outline

The ABO_3 Perovskites

Moving Beyond the Perovskites

We need to create a road map!

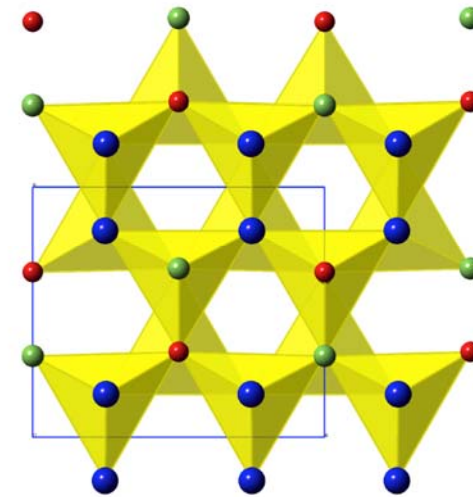
J. Solid State Chem. (2012) 195, 21

A New Class of Piezoelectrics

A New Class of Ferroelectrics

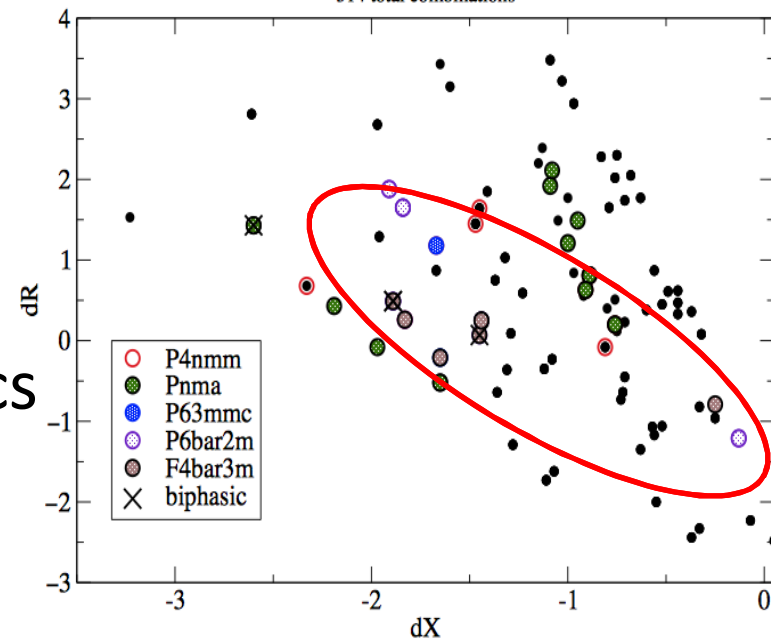
A New Class of Antiferroelectrics

Concluding Thoughts



8Ve Structure Forming Map

314 total combinations



Inorganic Crystal Structural Database

Database of completely identified inorganic structures.
150,000 peer-reviewed entries, dating back to 1913.
7,000 added annually, in conjunction with NIST databases

Structural Information:

Each entry is **assigned to one of the 230 space groups**
Lattice constants, Wyckoff parameters, occupancies

Structure types:

Currently **6,250 structure types**
Over **70% of the structures** have been **assigned** a structure type

Other search fields include:

Quality of refinement data, warnings/comments...

<http://www.fiz-karlsruhe.de/icsd.html>

Related Functions in Materials

piezoelectric-polar-**ferroelectric**

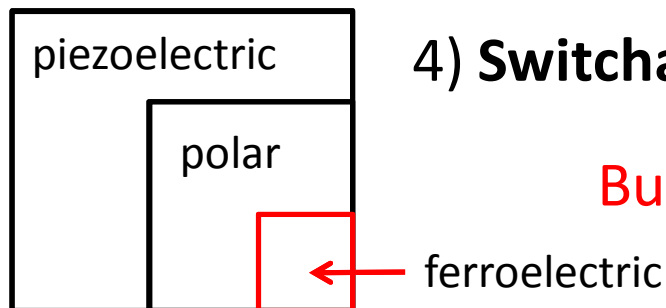
The **piezoelectric effect** is an electromechanical interaction
(this means that electricity is generated by a mechanical force)

- 1) The material needs to be **insulating**
- 2) The material has **no inversion center**

Relative displacement between positive and negative ions

- 3) Measurable **macroscopic polarization**

- 4) **Switchable polarization**



But we can't just search ICSD for ferroelectrics.

How Many Polar Materials Are Known?

Of the 230 crystallographic space groups, 68 are polar (**30%**).
As of this year, 12,553 total polar entries (**less than 10% total**)

- 1) **hexagonal** ($6mm$ and 6 , with 2264 compounds, **18.0%**)
- 2) **rhombohedral** ($3mm$ and 3 , with 2411 compounds at **19.2%**)
- 3) **tetragonal** ($4mm$ and 4 with 851 compounds, **6.8%**)
- 4) **orthorhombic** ($mm2$ with 4033 compounds, **32.1%**)
- 5) **monoclinic** (2 and m with 2534 compounds, **20.2%**)
- 6) **triclinic** (1 with 460 compounds, **3.7%**)

How Many Polar Materials Are Known?

Of the 230 crystallographic space groups, 68 are polar (30%).
As of this year, 12,553 total polar entries (less than 10% total)

This is an interesting result!

Most familiar ferroelectric materials are
rhombohedral (LiNbO_3 perovskite), hexagonal (YMnO_3)
or tetragonal (PbTiO_3 and BaTiO_3 perovskites)....

**Could there be exotic new ferroelectrics
that we don't know about, simply
because we haven't yet looked?**

How Many Polar Materials Are Known?

Of the 230 crystallographic space groups, 68 are polar (30%).
As of this year, 12,553 total polar entries (less than 10% total)

This is an interesting result!

Most familiar ferroelectric materials are
rhombohedral (LiNbO_3 perovskite), hexagonal (YMnO_3)
or tetragonal (PbTiO_3 and BaTiO_3 perovskites)....

2x as many polar orthorhombic entries as
there are either rhombohedral or hexagonal

3x as many monoclinic entries as 2500
there are tetragonal entries! vs. 800

5x as many polar orthorhombic entries 4000
than there are tetragonal entries! vs. 800

What Are They?

How many unique chemical elements per polar entry?

1 (0.3%), 2 (14.3%), 3 (29.9%), 4 (30.4%) or 5+ (25.1%)

Less than 1% are “polar elements” (A)

14.3% are **binary** compositions (*AB*)

29.9% are **tertiary** compositions (*ABC*)

30.4% are **quaternary** compositions (*ABCD*)

This is 3/4
of the polar
entries.

5+ elements are mostly solid solutions with fractional occupations (alloys, dopants, etc. based on *AB*, *ABC* or *ABCD*)

Structure Types

Common polar structure types:

In 186: ZnS with 445 entries and LiGaGe with 139 entries
(or 44.0% of the 1327 total entries).

In 99: PbTiO_3 (210 entries), KNbO_3 (17 entries) and PbVO_3 (12 entries)
...all related to the perovskite structure
and account for 79.3% of the 299 entries.

At the other extreme:

there are 12 polar space groups with no familiar structure types!

183, 172, 171, 158, 106, 105, 101, 80, 78, 37, 35 and 3
total number of entries in these groups is only 196, or 1.6%

For Our Initial ICSD Search(es)

Two strategies for the **discovery of novel functional materials**:

- 1) identify previously-overlooked systems in a familiar structure type
- 2) identify unfamiliar structure types

Want to find **families** of **intermetallic semiconductors**
with potentially **untapped functional behavior**

Need a **simple chemical formula** that involves three atoms: **ABC**

Most functional materials have **three types of atoms**
(two types form a rigid crystal structure, the third adds flexibility)

Keeping in mind that:

- we do not want corner-sharing octahedra
- we do not want hundreds of oxides

Outline

The ABO_3 Perovskites

Moving Beyond the Perovskites

A New Class of Piezoelectrics

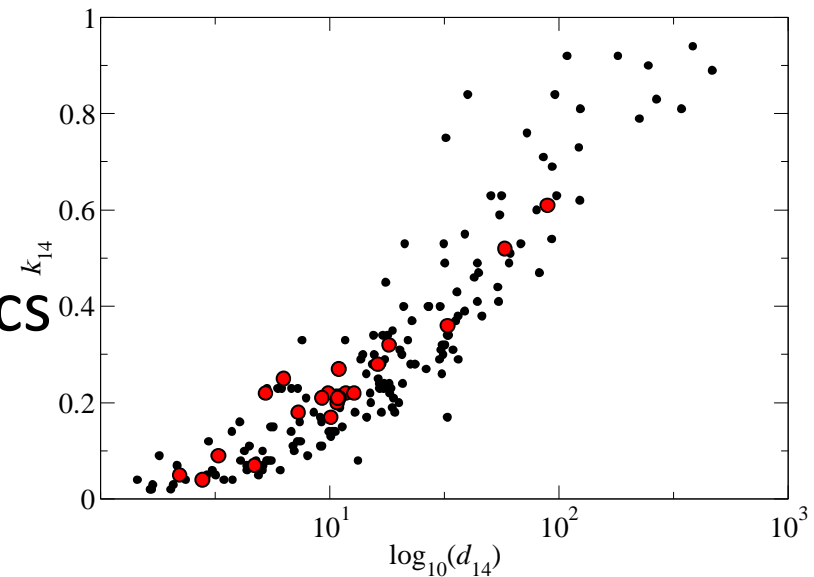
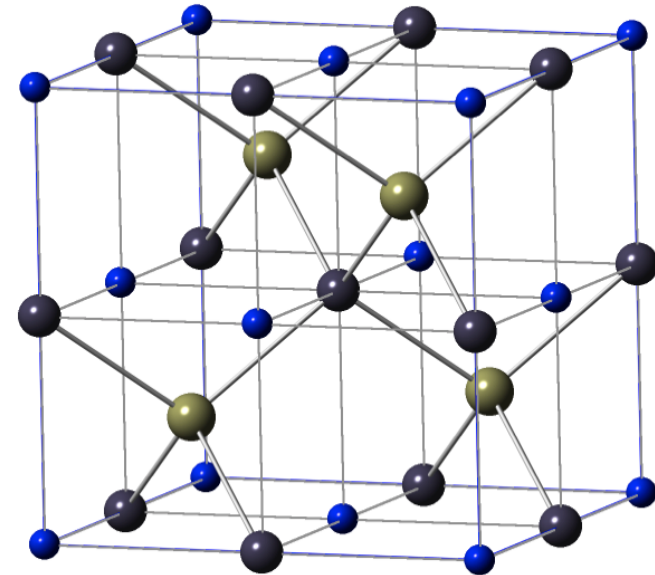
The Cubic LiAlSi Family

Phys. Rev. Lett. (2012) 109, 037602

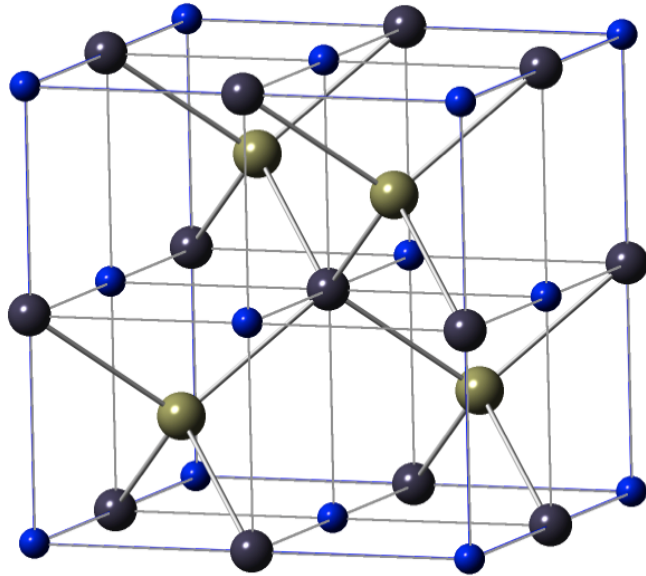
A New Class of Ferroelectrics

A New Class of Antiferroelectrics

Concluding Thoughts



LiAlSi: Target For a High-Throughput Study



A (black) and B (blue) rocksalt
C (gold) tetrahedrally bound

Half-Heusler: three atoms, *ABC*:

A and B form a rocksalt lattice

C occupies 1/2 of the the
tetrahedral sites...
most electronegative element?

Have three different variations

Gaining popularity as multifunctional materials!

F4bar3m space group means piezoelectricity!

But no mention of this in the literature!

How many LiAlSi are known? **Go to the ICSD!**

With Regards to Database Searching

Warnings and Comments:

These are a must-read.

Some combinations are reported in more than one similar structure:

This is a great use of theoretical modeling!

Some entries could be assigned to more than one structure type:

Another great use of theoretical modeling! Phase transitions?

Some entries could be misassigned:

Check nonpolar structures for polar instabilities with ISOTROPY

A new way to obtain improper ferroelectrics.

Some entries are simply missing information:

Missing 1 of 3 elements: where's the C in ABC?

Searching the ICSD for *ABC*

F4bar3m (#216), cubic nonpolar: 269 total (260 LiAlSi)

Number of entries **without magnetic cations: 49**

Basic search for platform to support functionality

(We can add these back in later)

Searching the ICSD for *ABC*

F4bar3m (#216), cubic nonpolar: 269 total (260 LiAlSi)

Number of entries **without magnetic cations: 49**

Number of entries with **8 or 18 valence electrons: 38**

Want to promote a band gap

(Insulating intermetallics usually require a filled octet)

Searching the ICSD for *ABC*

F4bar3m (#216), cubic nonpolar: 269 total (260 LiAlSi)

Number of entries **without magnetic cations: 49**

Number of entries with **8 or 18 valence electrons: 38**

Examples, divided into families

I-II-V: LiMgP, LiMgAs

X-III-V: PdYSb, PtYSb

X-IV-IV: NiTiSn, PdHfSn

XI-III-IV: AuScSn

I-XII-V: LiCdP

Searching the ICSD for *ABC*

F4bar3m (#216), cubic nonpolar: 269 total (260 LiAlSi)

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Examples, divided into families

I-II-V: LiMgP, LiMgAs, **NaBeAs, KMgSb...**

X-III-V: PdYSb, PtYSb, **NiAlAs, PtScBi...**

X-IV-IV: NiTiSn, PdHfSn, **NiZrGe, NiSiSn...**

XI-III-IV: AuScSn, **CuYPb, AgAlGe...**

I-XII-V: LiCdP, **NaZnBi, KZnP...**

But couldn't there be more? Like hundreds or thousands more?

High-Throughput: Over 900 Combinations!

THE PERIODIC TABLE

Legend:
H — SYMBOL
 1 — ATOMIC NUMBER
 1.008 — ATOMIC WEIGHT
 Hydrogen — NAME
 () = ESTIMATES

Legend:
 ALKALI METALS
 ALKALI EARTH METALS
 LANTHANIDES
 ACTINIDES
 HALOGENS
 NOBLE GASES

Legend:
 HAYDEN
 M
 McNEIL
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How do we get over 900?
 Investigate all of these triplets:

- I-II-V, I-III-IV, I-I-VI
- II-II-IV, II-III-III
- X-III-V, X-IV-IV
- XI-II-V, XI-III-IV
- XII-II-IV, XII-I-V

Total is 8 or 18 Ve.

I=Li, Na, K; II=Be, Mg, Ca, Sr, Ba; III=Sc, Y, B, Al, Ga;
 IV=Ti, Zr, Hf, C-Pb; V=N-Bi; VI=O-Te
 X=Ni, Pd, Pt; XI=Cu, Ag, Au; XII=Zn, Cd

A Word of Caution

High throughput studies:

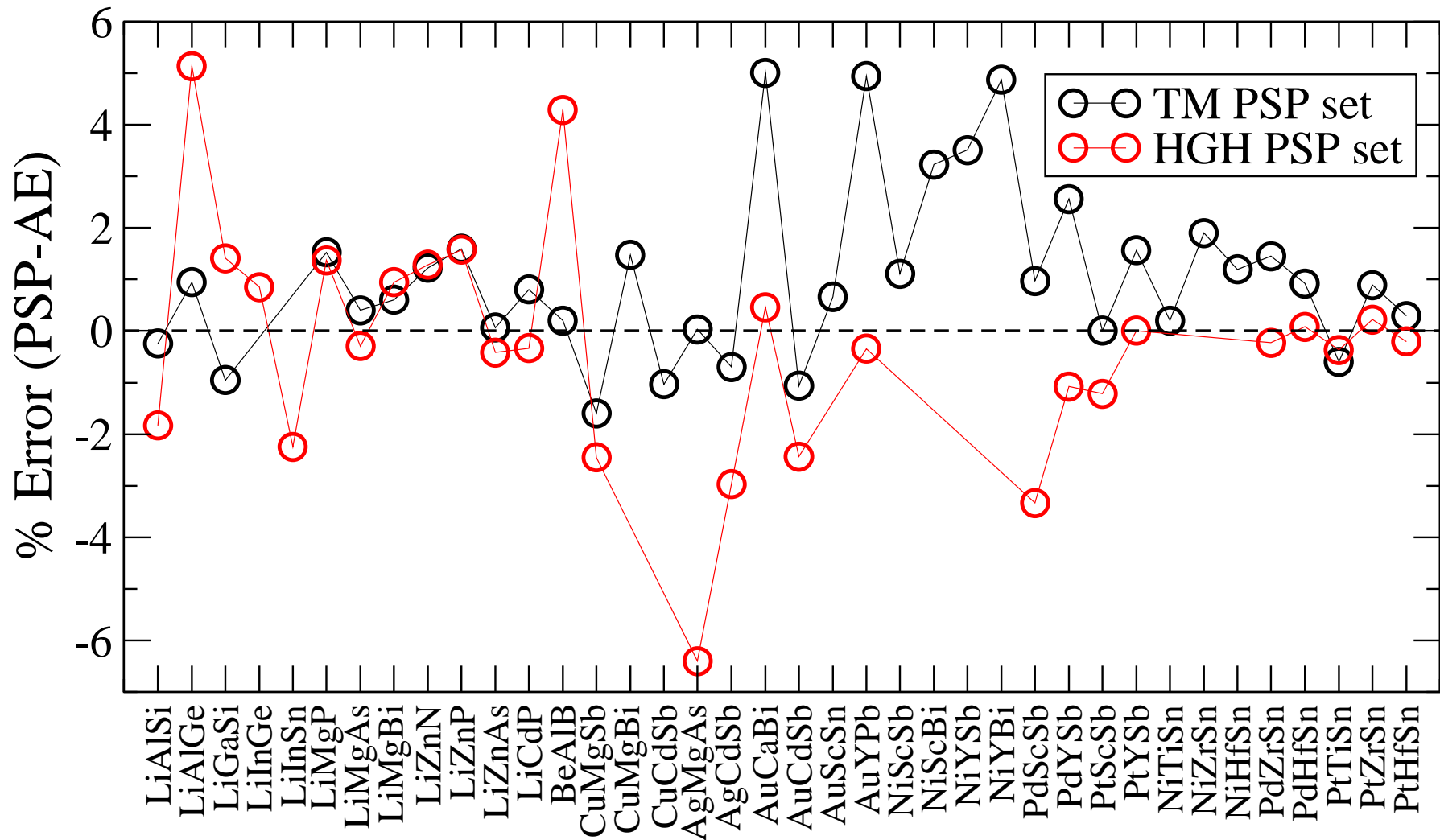
Pseudopotential testing is a must!

Do they match all electron (AE) DFT calculations? I used **Wien2k**.

Set up a few test calculations before your high-throughput study!

Obtain (at least) the lattice parameters from AE and PSP to see how well they agree, or disagree...

PSP Test of Known *ABC* Lattice Constants



38 Known Half-Heuslers

THE PERIODIC TABLE

	1 <i>IA</i>																	18 <i>VIIIA</i>	
1	H 1 1.008 Hydrogen																		He 2 4.00 Helium
2	Li 3 6.94 Lithium	Be 4 9.01 Beryllium										B 5 10.81 Boron	C 6 12.01 Carbon	N 7 14.01 Nitrogen	O 8 16.00 Oxygen	F 9 19.00 Fluorine	Ne 10 20.18 Neon		
3	Na 11 22.99 Sodium	Mg 12 24.31 Magnesium										Al 13 26.98 Aluminum	Si 14 28.09 Silicon	P 15 30.97 Phosphorus	S 16 32.07 Sulfur	Cl 17 35.45 Chlorine	Ar 18 39.95 Argon		
4	K 19 39.10 Potassium	Ca 20 40.08 Calcium	Sc 21 44.96 Scandium	Ti 22 47.88 Titanium	V 23 50.94 Vanadium	Cr 24 52.00 Chromium	Mn 25 54.94 Manganese	Fe 26 55.85 Iron	Co 27 58.93 Cobalt	Ni 28 58.69 Nickel	Cu 29 63.55 Copper	Zn 30 65.39 Zinc	Ga 31 69.72 Gallium	Ge 32 72.61 Germanium	As 33 74.92 Arsenic	Se 34 78.96 Selenium	Br 35 79.90 Bromine	Kr 36 83.80 Krypton	
5	Rb 37 85.47 Rubidium	Sr 38 87.62 Strontium	Y 39 88.91 Yttrium	Zr 40 91.22 Zirconium	Nb 41 92.91 Niobium	Mo 42 95.94 Molybdenum	Tc 43 (97.9) Technetium	Ru 44 101.07 Ruthenium	Rh 45 102.91 Rhodium	Pd 46 106.42 Palladium	Ag 47 107.87 Silver	Cd 48 112.41 Cadmium	In 49 114.82 Indium	Sn 50 118.71 Tin	Sb 51 121.76 Antimony	Te 52 127.60 Tellurium	I 53 126.90 Iodine	Xe 54 131.29 Xenon	
6	Cs 55 132.91 Cesium	Ba 56 137.33 Barium	La 57 138.91 Lanthanum	Hf 72 178.49 Hafnium	Ta 73 180.95 Tantalum	W 74 183.85 Tungsten	Re 75 186.21 Rhenium	Os 76 190.2 Osmium	Ir 77 192.22 Iridium	Pt 78 195.08 Platinum	Au 79 196.97 Gold	Hg 80 200.59 Mercury	Tl 81 204.38 Thallium	Pb 82 207.2 Lead	Bi 83 208.98 Bismuth	Po 84 (209) Polonium	At 85 (210) Astatine	Rn 86 (222) Radon	
7	Fr 87 223.02 Francium	Ra 88 226.03 Radium	Ac 89 227.03 Actinium	Rf 104 (261) Rutherfordium	Db 105 (262) Dubnium	Sg 106 (263) Seaborgium	Bh 107 (262) Bohrium	Hs 108 (265) Hassium	Mt 109 (266) Meitnerium	Unnamed Discovery 110 Nov. 1994	Unnamed Discovery 111 Nov. 1994	Unnamed Discovery 112 1996		Unnamed Discovery 114 1999		Unnamed Discovery 116 1999		Unnamed Discovery 118 1999	
	ALKALI METALS	ALKALI EARTH METALS															HALOGENS	NOBLE GASES	

H — SYMBOL
1 — ATOMIC NUMBER
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() = ESTIMATES

8 9 10
VIII B

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Ce 58 140.12 Cerium	Pr 59 140.91 Praseodymium	Nd 60 144.24 Neodymium	Pm 61 (145) Promethium	Sm 62 150.36 Samarium	Eu 63 152.07 Europium	Gd 64 157.25 Gadolinium	Tb 65 158.93 Terbium	Dy 66 162.50 Dysprosium	Ho 67 164.93 Holmium	Er 68 167.26 Erbium	Tm 69 168.93 Thulium	Yb 70 173.04 Ytterbium	Lu 71 174.97 Lutetium
Th 90 232.04 Thorium	Pa 91 231.04 Protactinium	U 92 238.03 Uranium	Np 93 237.05 Neptunium	Pu 94 (240) Plutonium	Am 95 243.06 Americium	Cm 96 (247) Curium	Bk 97 (248) Berkelium	Cf 98 (251) Californium	Es 99 252.08 Einsteinium	Fm 100 257.10 Fermium	Md 101 (257) Mendelevium	No 102 259.10 Nobelium	Lr 103 262.11 Lawrencium

THE PERIODIC TABLE

The Bennett-Rappe library
of OPIUM constructed
designed non-local
optimized norm-conserving
pseudopotentials

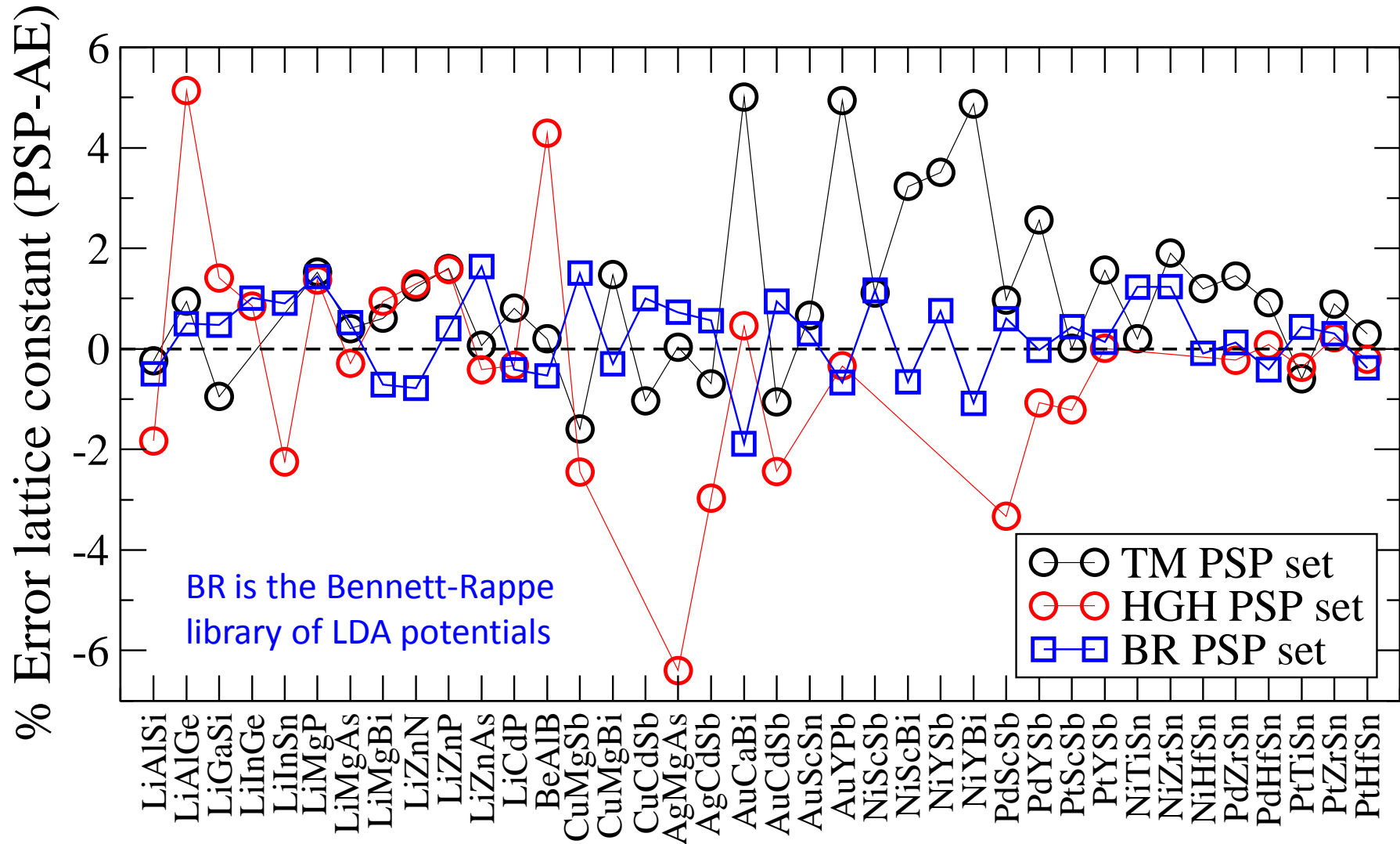
J. W. Bennett

Dept. of Physics and Astronomy,

Rutgers, The State University of New Jersey

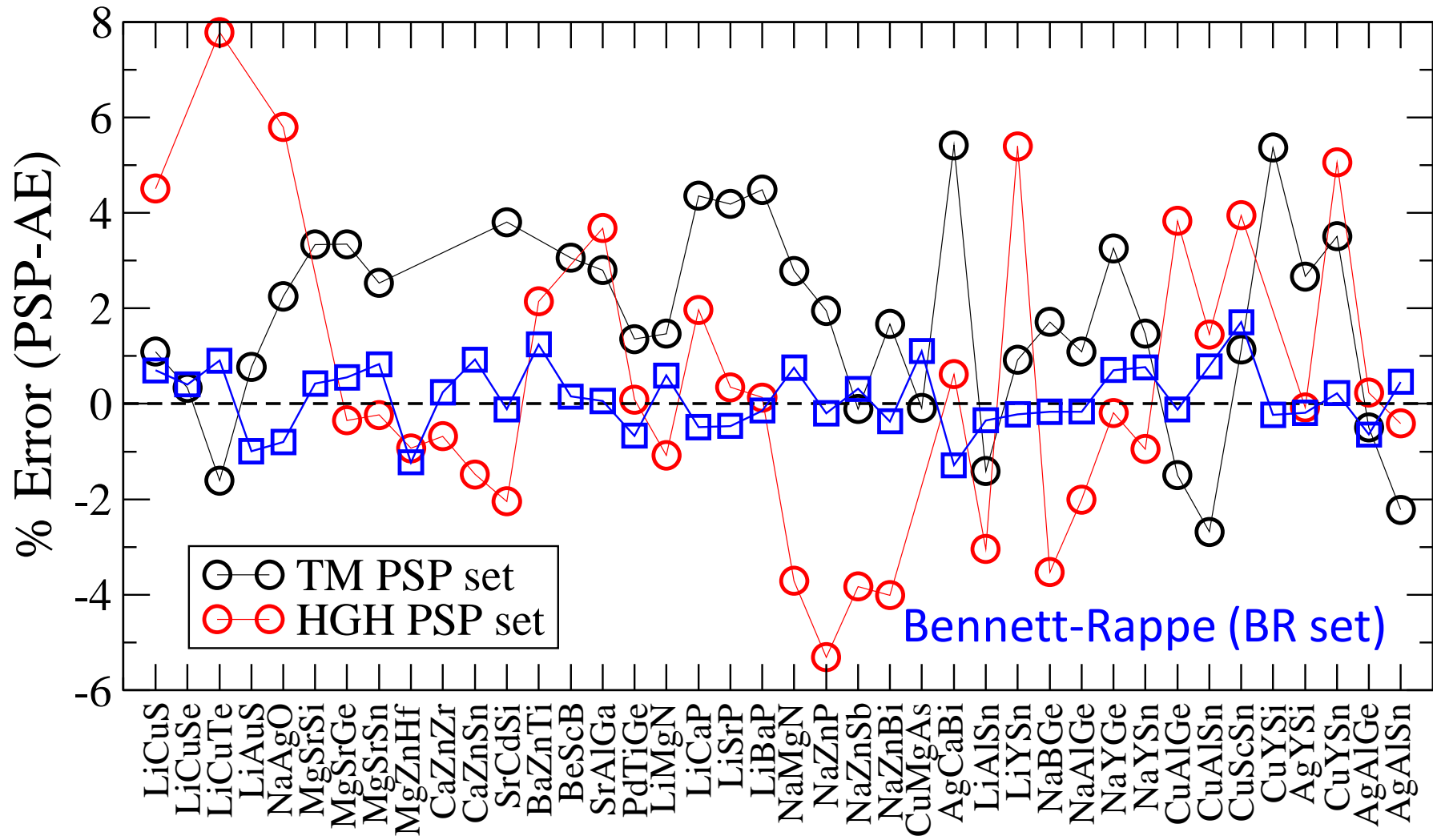
http://physics.rutgers.edu/~bennett/PSP_v2.pdf

PSP Test of Known *ABC* Lattice Constants



38 Known Half-Heuslers

What About the Hypothetical *ABC*?



40 Unknown Half-Heuslers

High-Throughput Study of Half-Heuslers

1) **Ground state DFT-LDA calculation.**

over **900** combinations

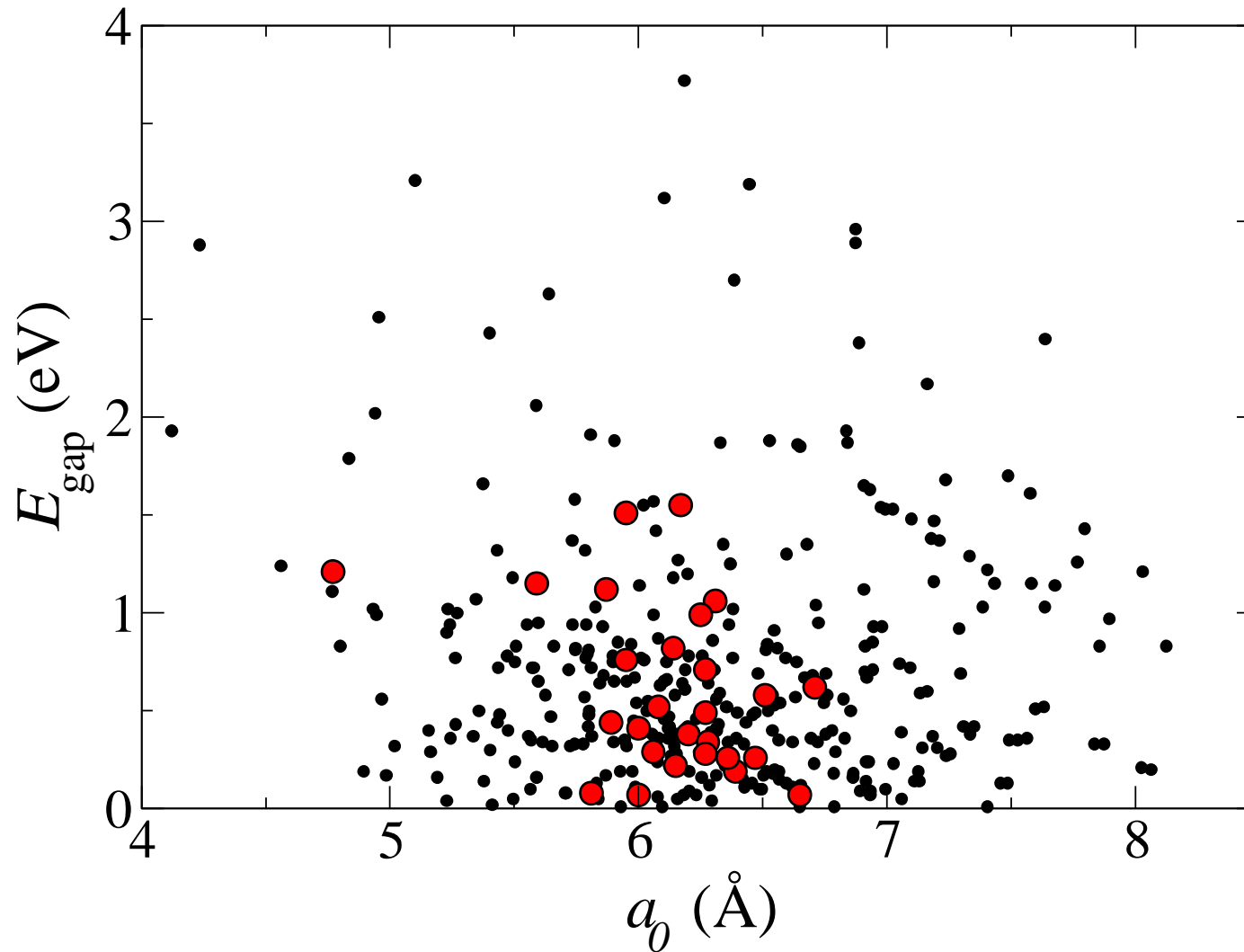
3 possible structural variants (**2700 calc.!**).

Which atom sits in the tetrahedral site?

Calculate the differences in total energy

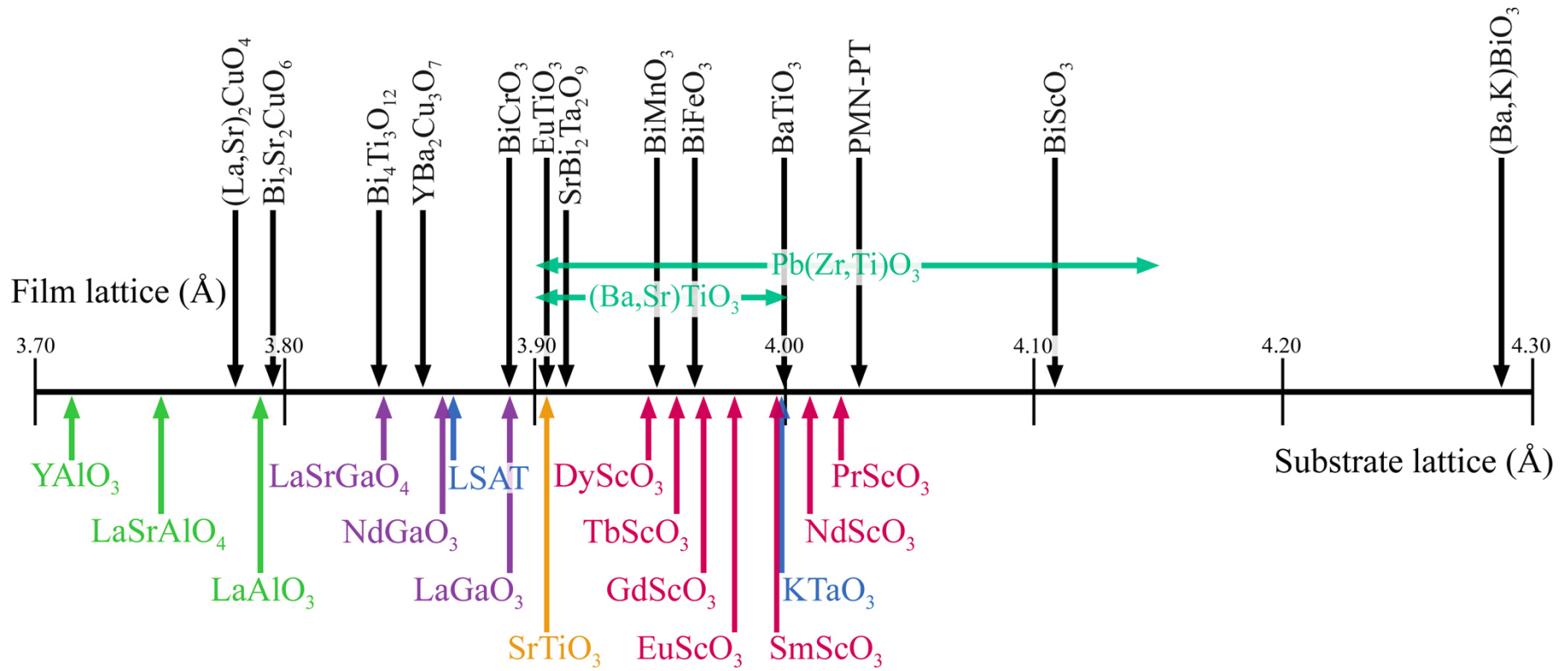
2) **Insulating or metallic?**

What Do We Find?



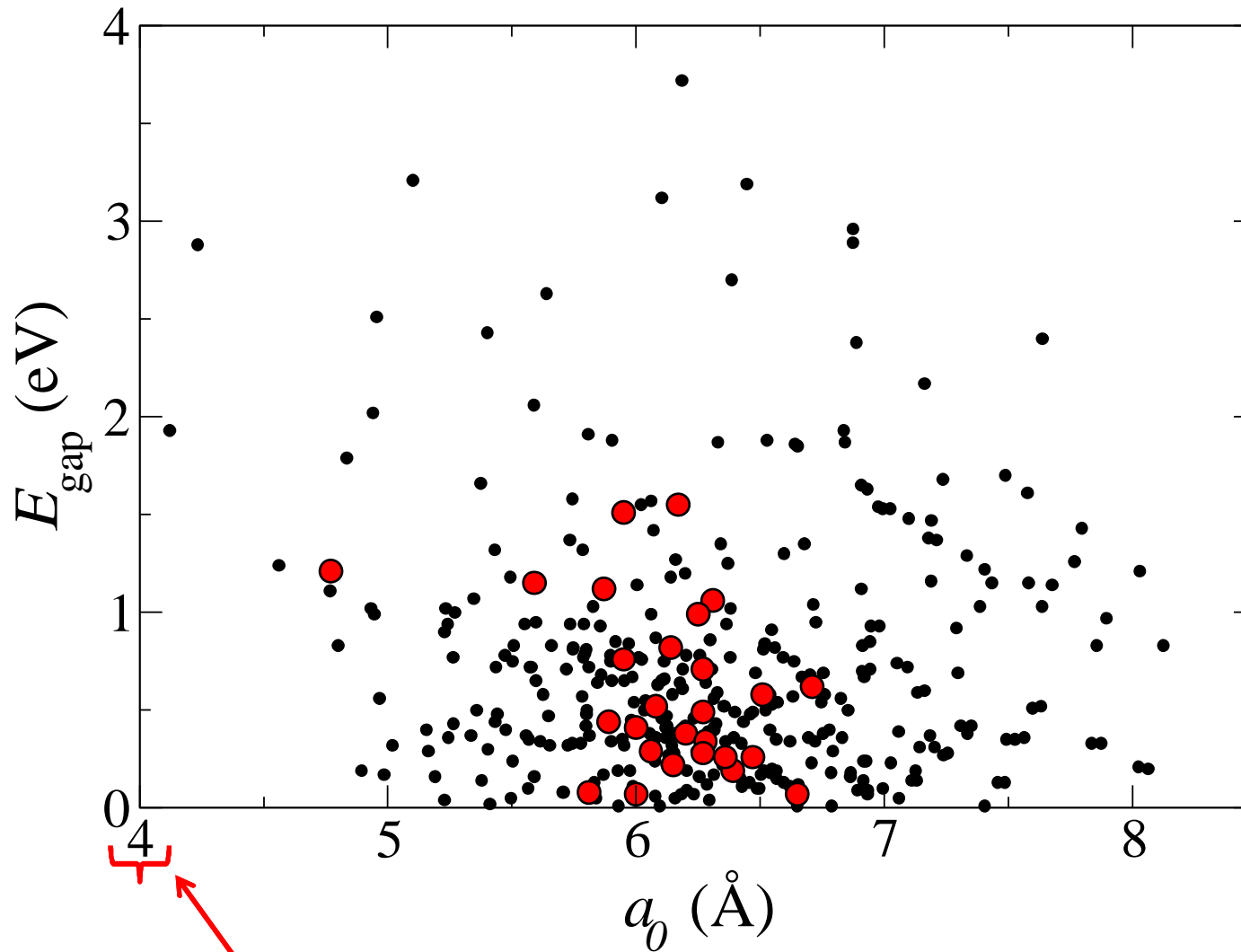
Choice of **band gap and lattice constant**
match for **many applications** is very large!

Perovskite Substrates



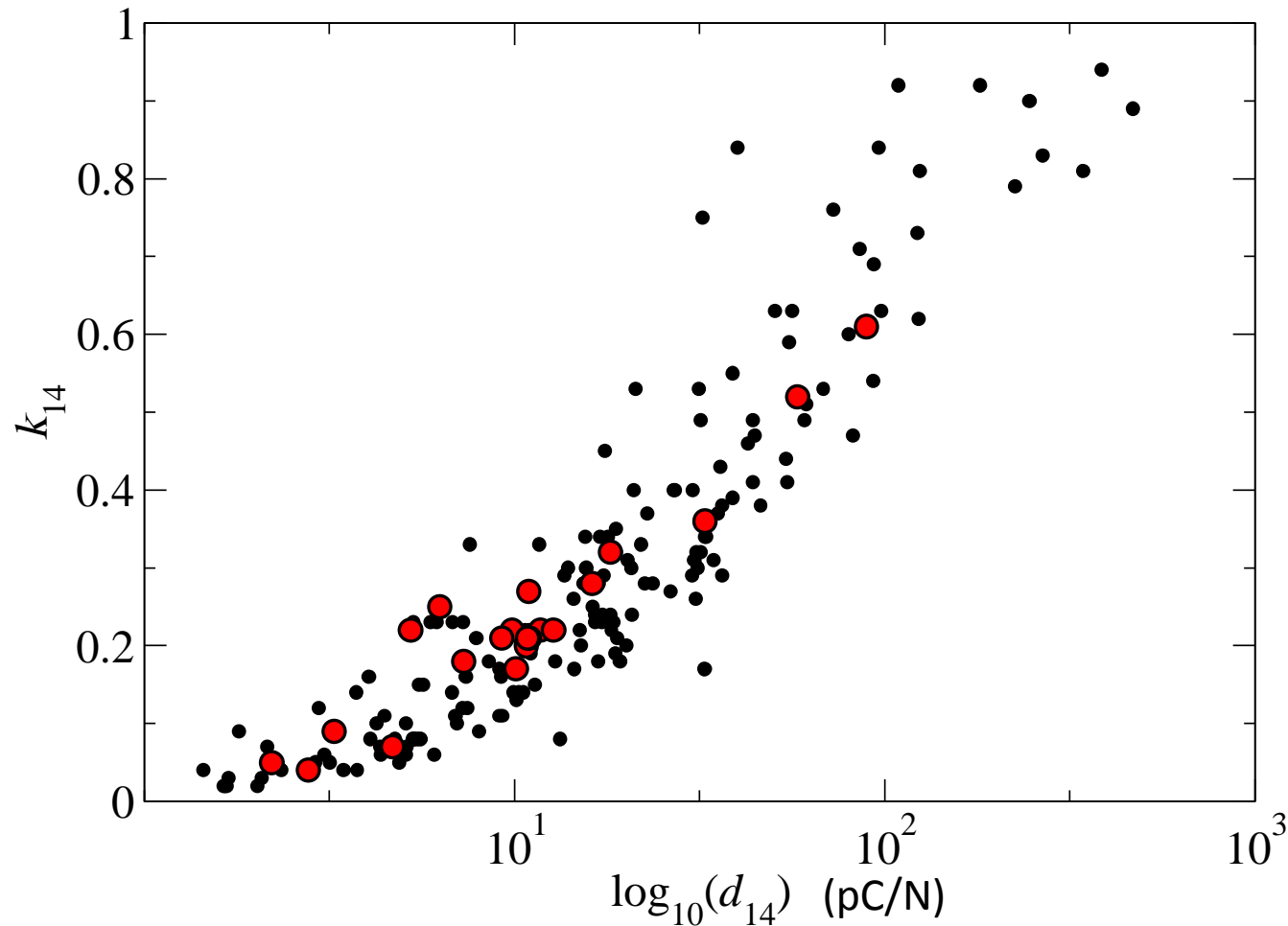
D.G. Schlom, L.Q. Chen,
X.Q. Pan, A. Schmehl, and
M.A. Zurbuchen, *Journal of
the American Ceramic
Society* 91 (2008) 2429-2454.

Why Is This Important?



The range of the perovskites!

And The Piezoelectric Coefficients?



Electromechanical coupling (k_{14}) vs. **piezoelectric constant** (d_{14}) is on a **logarithmic scale**orders of magnitude to choose from!

Top Half-Heuslers

ABC	a	E_{gap}	e_{14}	d_{14}	C_{44}	k_{14}	ϵ_0
KMgP	6.71	1.04	1.19	346.28	0.03	0.89	13
LiNaS	6.10	3.12	0.92	208.22	0.04	0.86	8
LiSrAs	6.84	1.93	0.79	286.27	0.03	0.85	10
LiNaSe	6.39	2.70	0.75	227.09	0.03	0.84	8
NaMgN	5.43	0.72	1.50	165.23	0.09	0.83	13
NaBeP	5.59	2.06	1.02	192.98	0.05	0.82	11
KMgAs	6.92	0.67	1.06	205.75	0.05	0.81	13
KScPb	7.35	0.42	1.21	330.83	0.04	0.80	25
MgBaSi	7.18	0.37	1.13	290.51	0.04	0.80	21
BeBaSn	6.86	0.16	0.49	1036.54	0.01	0.80	33
KScSn	7.31	0.42	1.19	294.69	0.04	0.79	24

These are all **WAY better piezoelectrics** than those listed for $F4bar3m$ in Landolt-Bornstein database!

(**Best known member** in LB database is Tl_3TaS_4 with $d_{14}=58$ pC/N)

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Moving Beyond the Perovskites

A New Class of Piezoelectrics

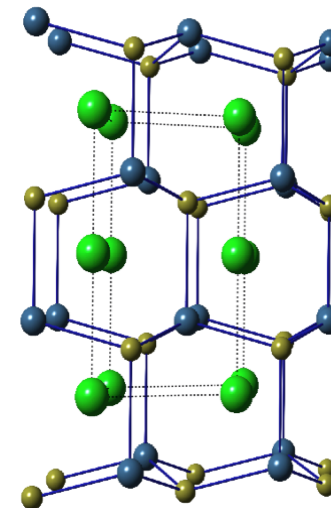
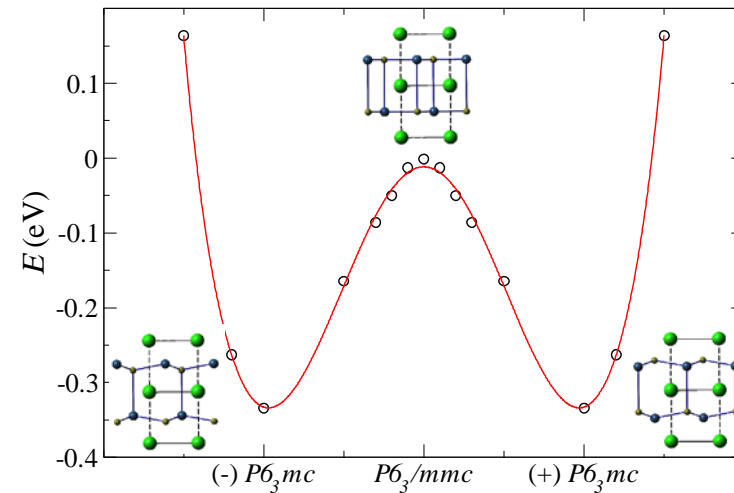
A New Class of Ferroelectrics

The Hexagonal LiGaGe family

Phys. Rev. Lett. (2012) 109, 167602

A New Class of Antiferroelectrics

Concluding Thoughts



Revisiting the ICSD: the ABC's

Listed in the database, we find:

51,000 entries with three unique chemical elements!

Of these, **3700 have the chemical formula ABC.**

F4bar3m (#216), cubic nonpolar: **269** total (260 LiAlSi)

This is less than 10% of the known entries.

Revisiting the ICSD: the ABC's

Listed in the database, we find:

51,000 entries with three unique chemical elements!

Of these, **3700 have the chemical formula ABC.**

F4bar3m (#216), cubic nonpolar: 269 total (260 LiAlSi)

P6₃/mmc (#194), hexagonal nonpolar: 297 total (200 ZrBeSi)

P6bar2m (#189), hexagonal nonpolar: 712 total (680 Fe₂P)

P6barm2 (#187), hexagonal nonpolar: 47 total (40 BaPtSb)

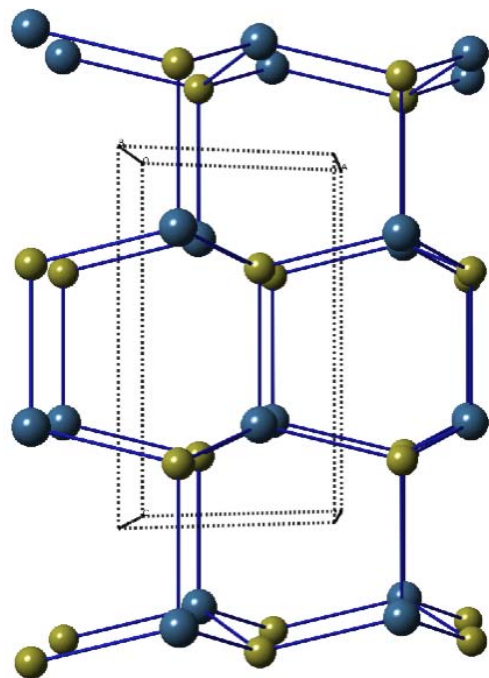
P6₃mc (#186), hexagonal polar: 153 total (120 LiGaGe)

P4/nmm (#129), tetragonal nonpolar: 613 total (450 PbClF)

Pnma (#62), orthorhombic nonpolar: 548 total (450 MgSrSi)

P6₃mc is one of the **polar space groups** that we **identified** in our **database search as well-known**. Common structure types included LiGaGe and **wurtzite**, which is not ferroelectric.

Wurtzite



Our DFT results

$a=3.19$ Ang. (3.21 Ang)

$c=5.15$ Ang. (5.25 Ang)

$u=0.379$ (0.375)

Polar hexagonal $P6_3mc$ structure

Each Zn is tetrahedrally bound to 4 O

Each O is tetrahedrally bound to 4 Zn

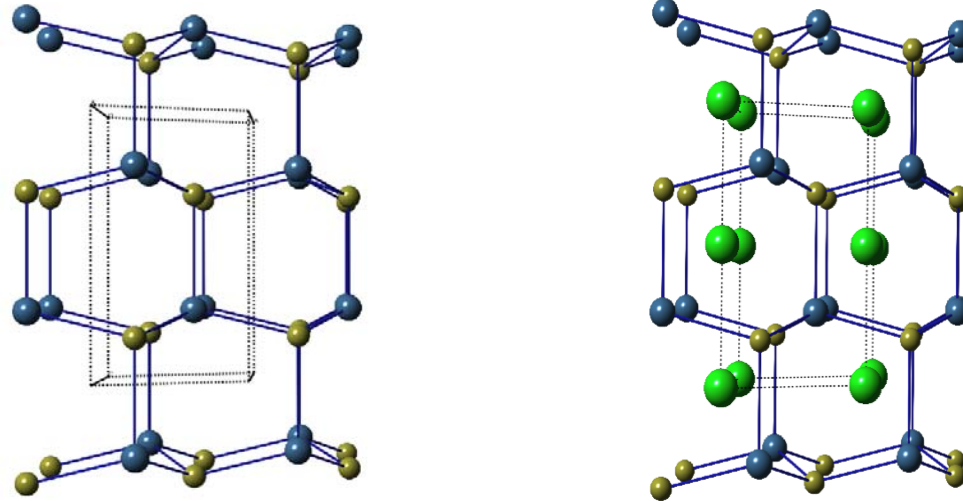
Strong sp^3 bond formation is driving force for formation...rigid structure!

Switching would have to include:

- 1) breaking sp^3 bonds
- 2) high-symmetry planar structure ($P6_3/mmc$)
- 3) re-forming sp^3 bonds

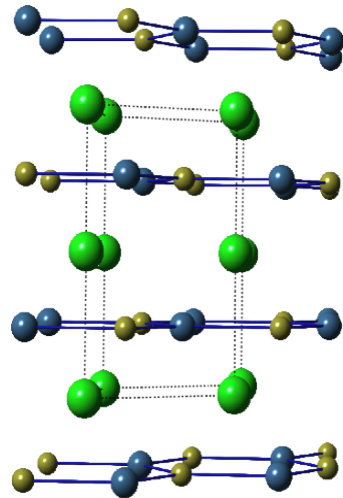
This is more than 0.6 eV by DFT!

LiGaGe is “Stuffed Wurtzite”



LiGaGe, or “**stuffed wurtzite**” is the polar $P6_3mc$ phase

ZrBeSi: A Non-Polar Structure

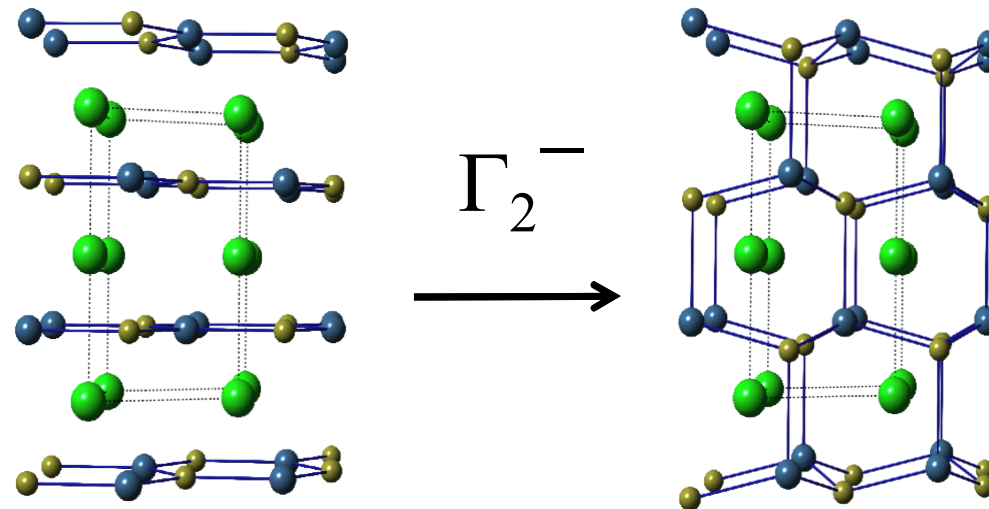


LiGaGe, or “stuffed wurtzite” is the polar $P6_3mc$ phase

ZrBeSi in the **layered non-polar $P6_3/mmc$** phase...

There's at least **6 combinations reported in both** space groups.

A Polar Distortion!



LiGaGe, or “stuffed wurtzite” is the polar $P6_3mc$ phase
ZrBeSi in the layered non-polar $P6_3/mmc$ phase...

There’s at least 6 combinations reported in both space groups.

ISOTROPY shows that a **Gamma mode relates the two phases**

Unlike Perovskites: **No competing octahedral rotations!**

Use first-principles to screen this family (6 atoms/cell).

Can we make wurtzite ferroelectric?

Known LiGaGe Compounds

		a		c		z_{2b}		z'_{2b}		E_{gap}	ΔE
I-II-IV	<u>Li</u> GaGe	4.139	(4.175)	6.713	(6.783)	0.314	(0.312)	0.698	(0.700)	0	0.80
	Cu <u>Sc</u> Sn	4.351	(4.388)	6.795	(6.830)	0.330	(0.326)	0.729	(0.229)	0	0.45
	Cu <u>Y</u> Sn	4.475	(4.543)	7.148	(7.274)	0.320	(0.316)	0.728	(0.733)	0	0.32
	Cu <u>Y</u> Pb	4.512	(4.559)	7.191	(7.334)	0.321	(0.323)	0.729	(0.729)	0	0.34
	Ag <u>Y</u> Sn	4.634	(4.683)	7.240	(7.372)	0.314	(0.308)	0.702	(0.719)	0	0.39
	Au <u>Sc</u> Ge	4.263	(4.308)	6.679	(6.846)	0.196	(0.200)	0.793	(0.798)	0	0.61
	Au <u>Sc</u> Sn	4.507	(4.593)	7.066	(7.202)	0.348	(0.340)	0.730	(0.731)	0	0.75
	Au <u>Y</u> Si	4.247	(4.288)	7.358	(7.546)	0.228	(0.234)	0.780	(0.775)	0	0.05
	Au <u>Y</u> Ge	4.364	(4.410)	7.084	(7.309)	0.219	(0.216)	0.789	(0.791)	0	0.26
	Au <u>Y</u> Sn	4.614	(4.636)	7.293	(7.373)	0.173	(0.194)	0.774	(0.821)	0	0.70
I-II-V	<u>Li</u> BeSb	4.091	(4.152)	6.636	(6.738)	0.350	(0.341)	0.733	(0.732)	1.45	0.79
	<u>Li</u> ZnSb	4.327	(4.431)	7.024	(7.157)	0.290	(0.304)	0.668	(0.689)	0.99	0.93
	<u>Ca</u> AgBi	4.730	(4.811)	7.564	(7.827)	0.318	(0.312)	0.715	(0.721)	0	0.36
II-II-IV	<u>Ca</u> ZnSn	4.595	(4.655)	7.331	(7.628)	0.218	(0.220)	0.813	(0.805)	0	0.32
	<u>Ca</u> HgSn	4.754	(4.800)	7.547	(7.760)	0.289	(0.310)	0.686	(0.720)	0	0.53
	<u>Sr</u> HgSn	4.878	(4.893)	7.801	(8.217)	0.305	(0.300)	0.712	(0.720)	0	0.36
	<u>Sr</u> HgPb	4.894	(4.995)	8.054	(8.172)	0.311	(0.300)	0.719	(0.720)	0	0.19

We have 17 combinations with reliable structural data

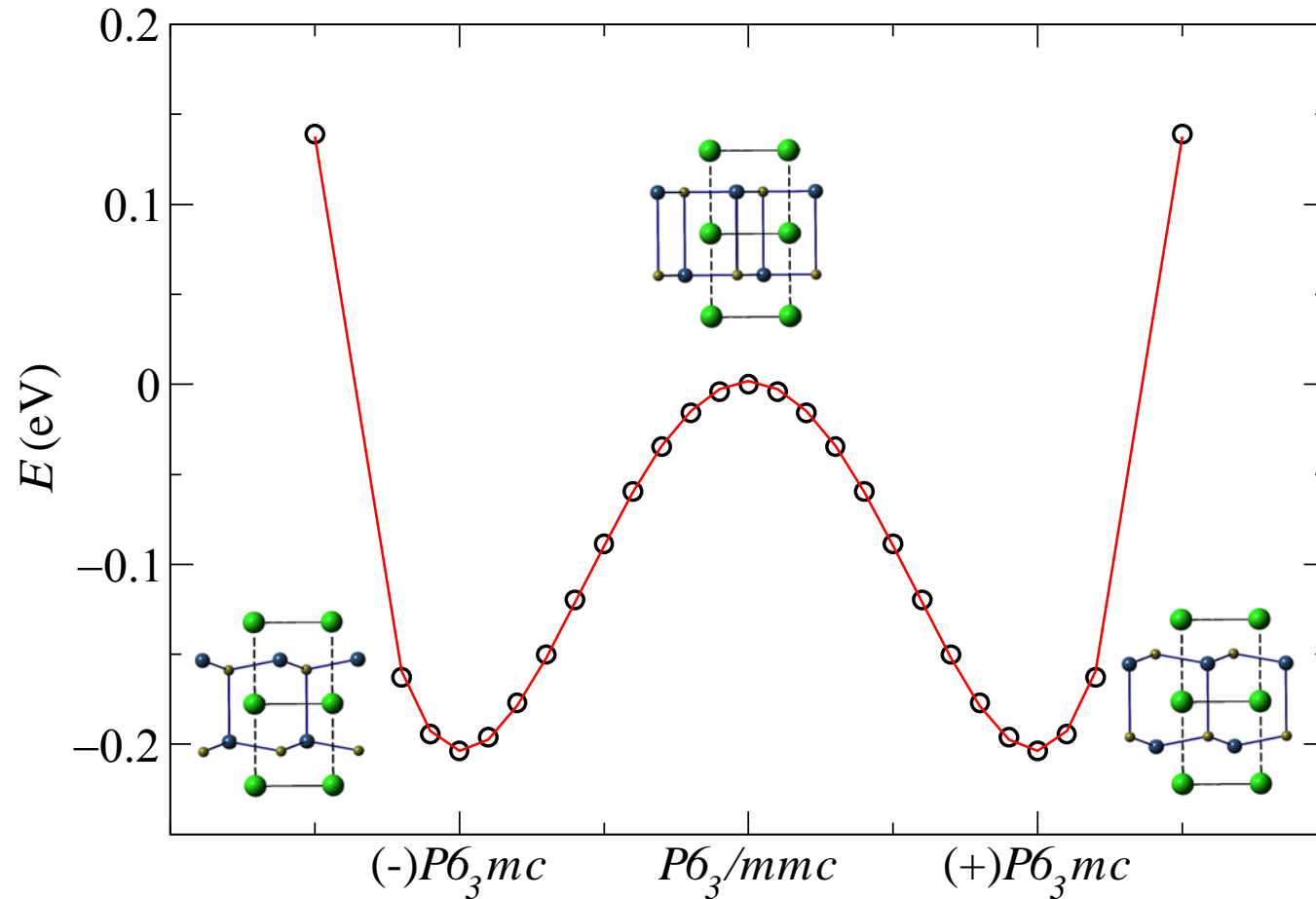
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Two are insulators of the I-II-V type...we can expand the set to 72!

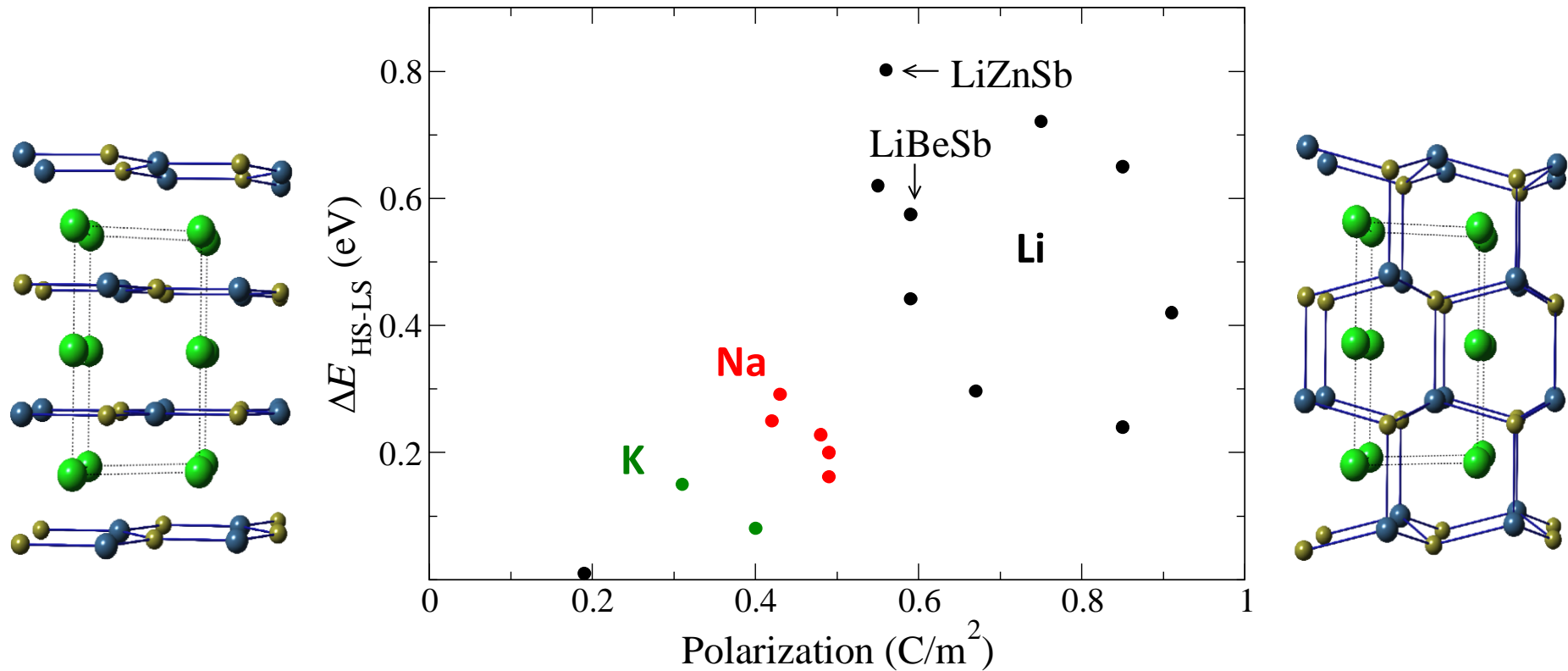
We choose I=Li, Na, K; II=Be, Mg, Ca, Sr, Ba, Zn; and V=P, As, Sb, Bi.

A Double Well!



The **difference in energy** between $P6_3/mmc$ and either polar phase for **NaMgP is 0.21 eV... barrier for $PbTiO_3$ is 0.2 eV.** This is reminiscent of switchability observed in the perovskites!

A New Class of Ferroelectrics Based on Wurtzite!



Difference in energy between paraelectric and ferroelectric structures for all **17 polar combinations**.

10 are below 0.3 eV and potentially switchable.

The larger the stuffing cation, the smaller the barrier to switch polarization...**This is a new class of ferroelectrics!**

Outline

The ABO_3 Perovskites

Moving Beyond the Perovskites

A New Class of Piezoelectrics

A New Class of Ferroelectrics

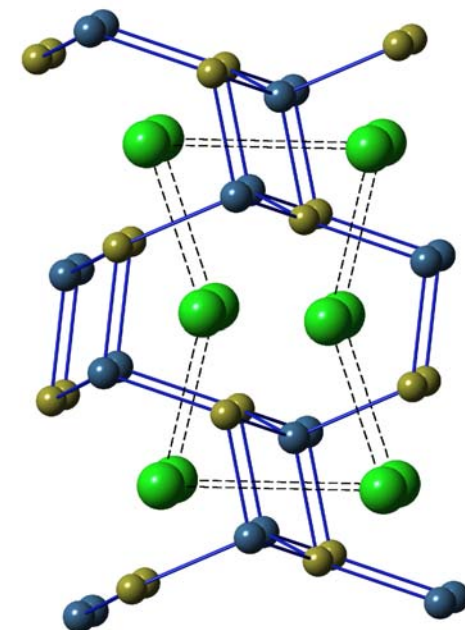
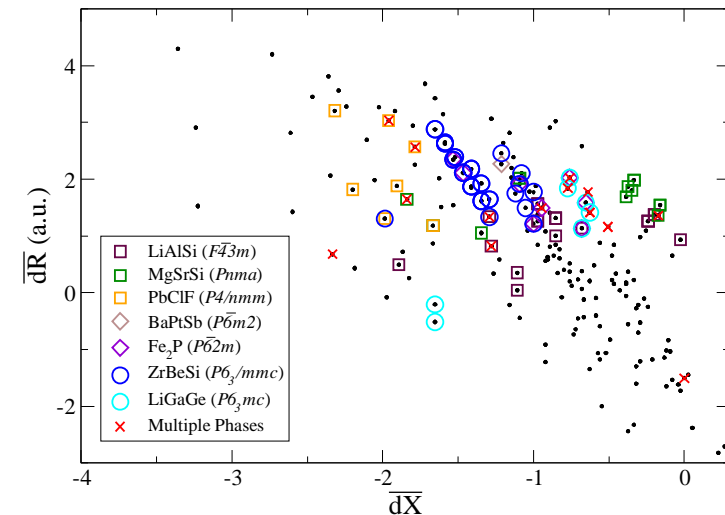
A New Class of Antiferroelectrics

The Orthorhombic MgSrSi Family

Phys. Rev. Lett. (2013) 110, 017603

Concluding Thoughts

Structure Forming 18Ve



What is an antiferroelectric?

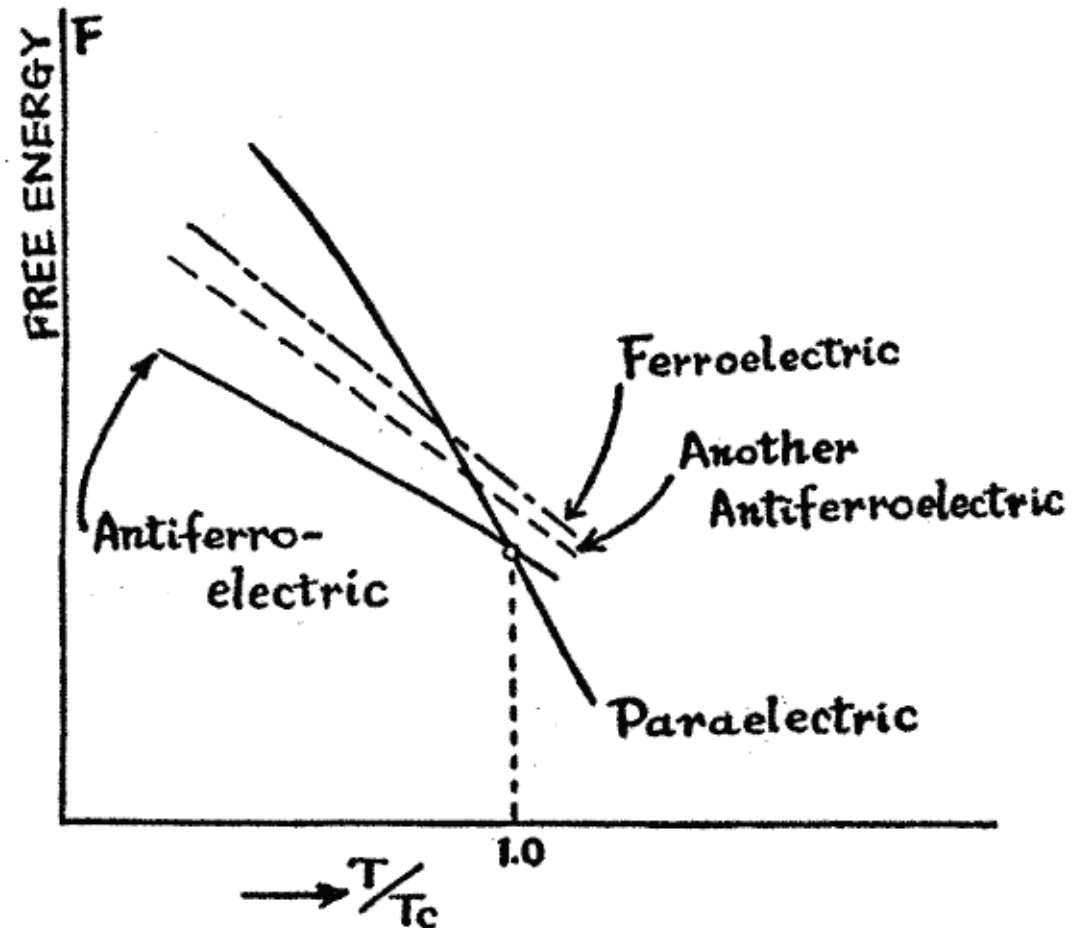
Two important criteria:

1) Structure

Antipolar ground state
crystal structure
(Kittel, 1951)

2) Energy

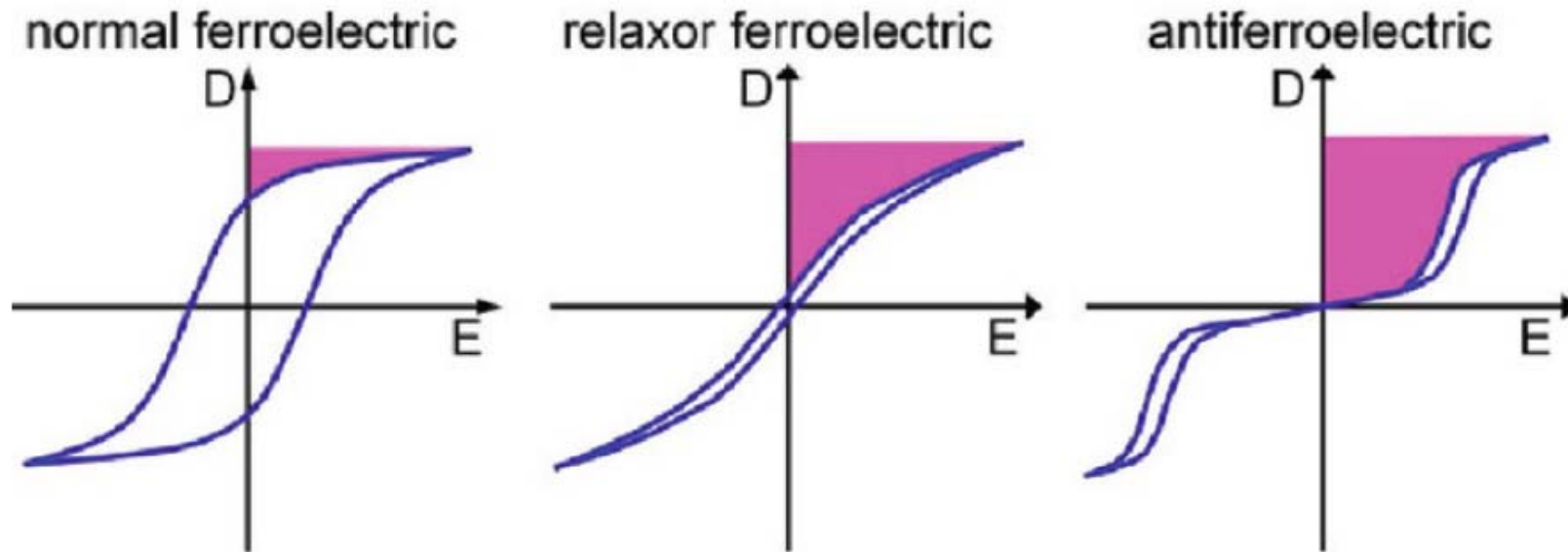
Competition with a polar
ferroelectric phase
(Shirane, 1952)
electric-field induced
first-order phase transition



K. M. Rabe: Antiferroelectricity in oxides: A reexamination
Functional Metal Oxides: New Science and Novel Applications (2012)

So, why are antiferroelectrics important?

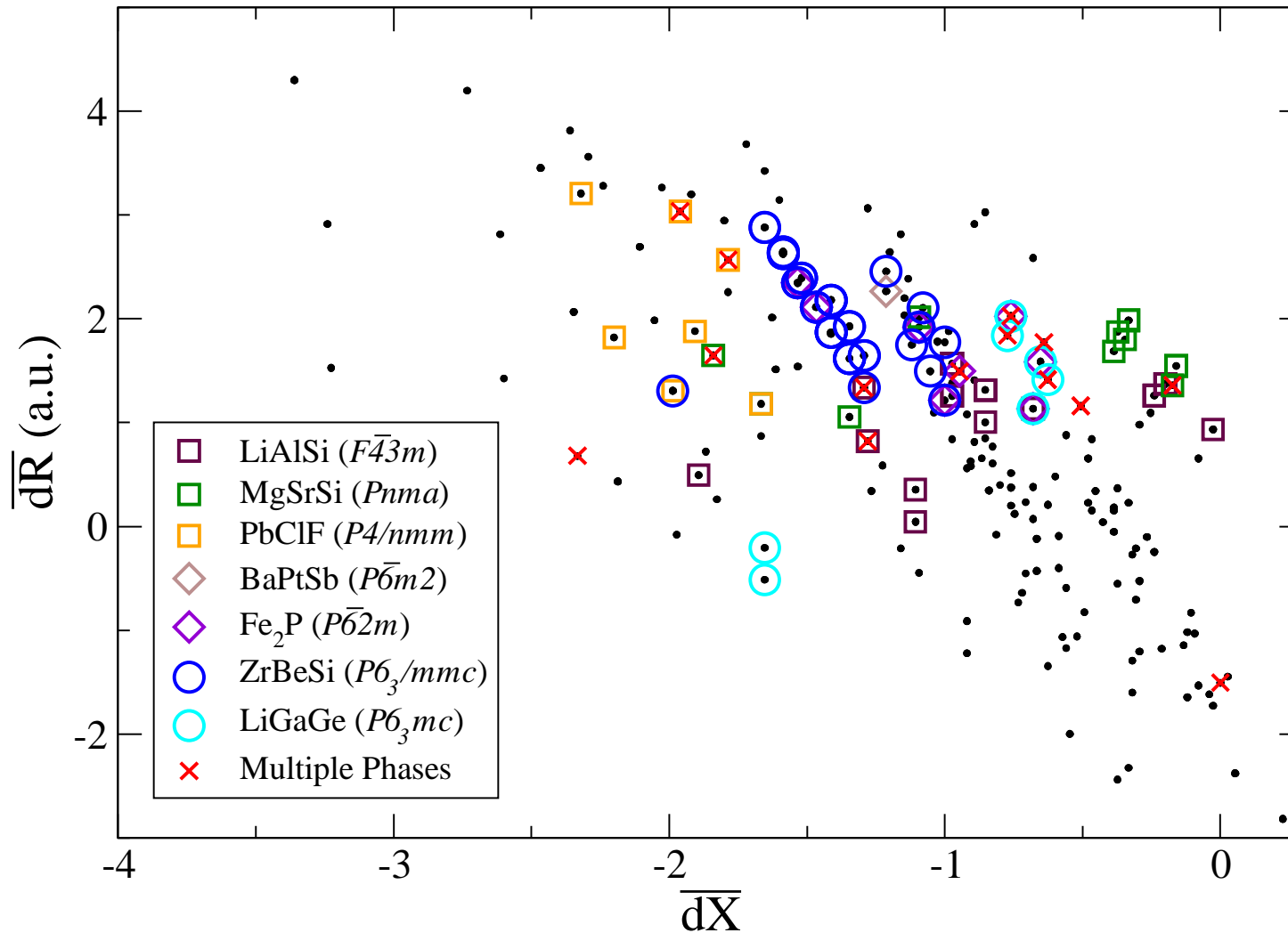
Increased Capacitance: Energy Storage!



The double hysteresis loop of the antiferroelectric has a much greater capacity to store and release energy. Can we find any with the chemical formula *ABC*?

My secret weapon...Villars maps

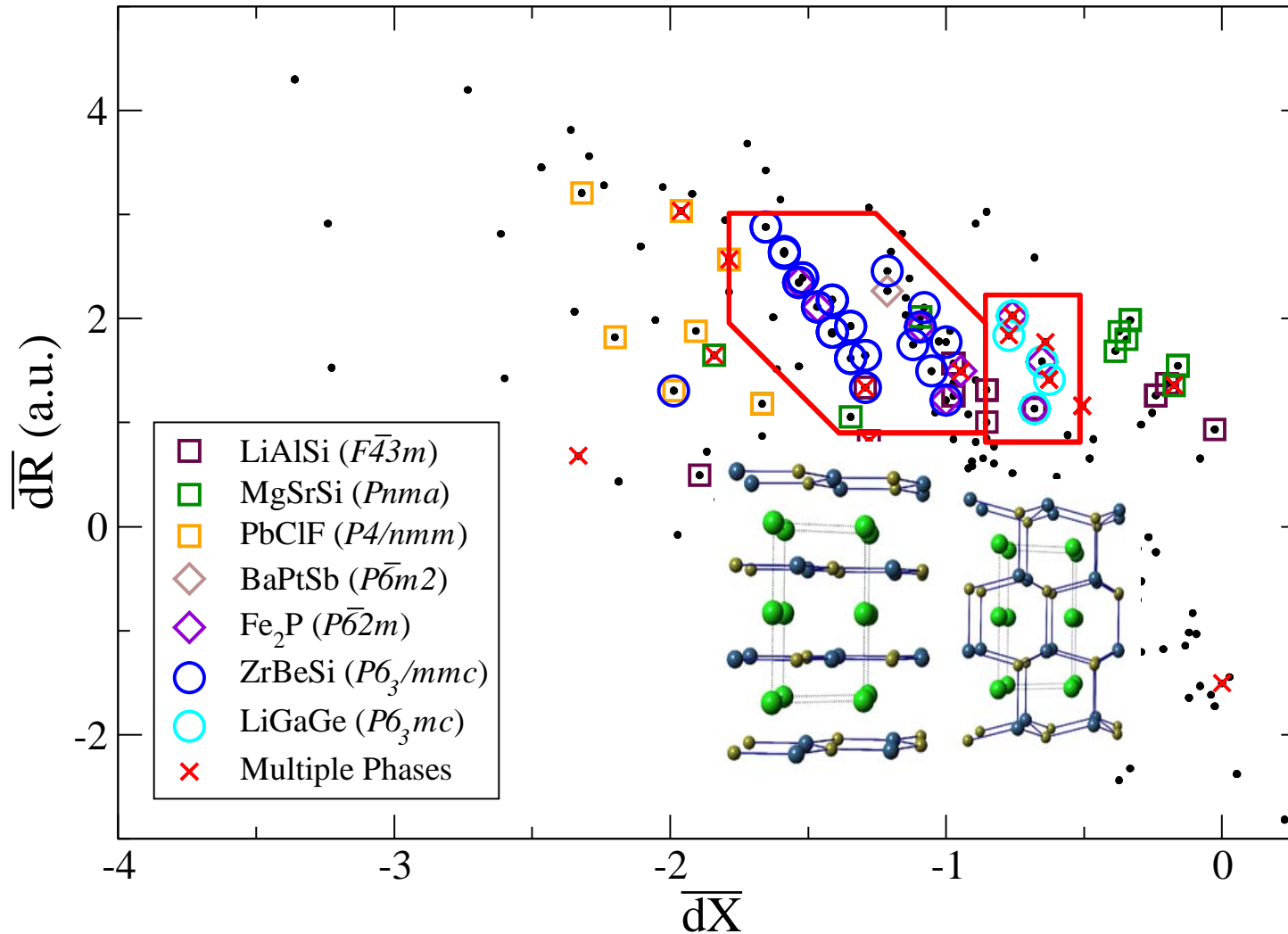
Structure Forming 18Ve



Villars et al., *J. Less Common Metals* (1986) 175, (1987) 289

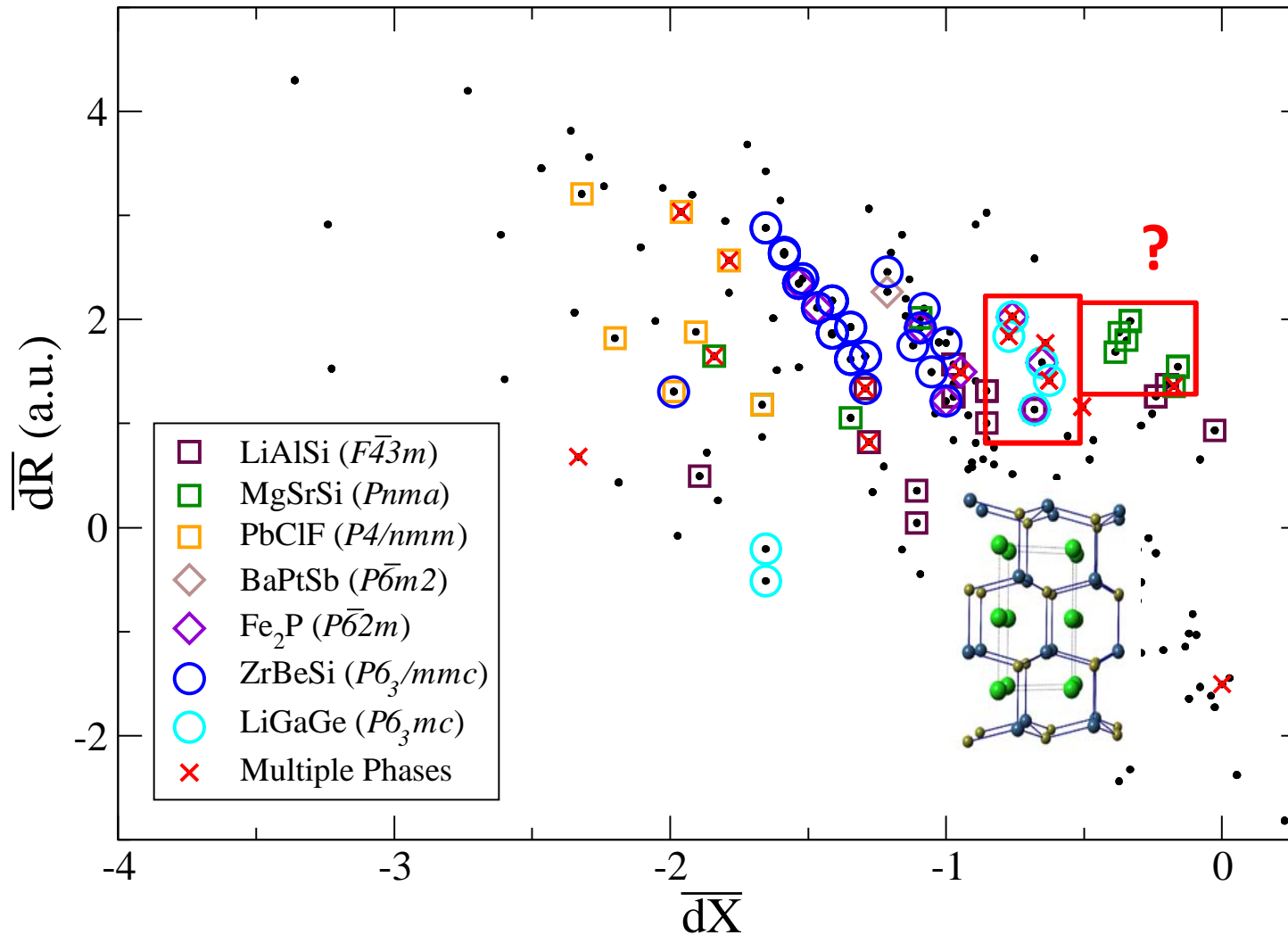
We know about this transition...

Structure Forming 18Ve

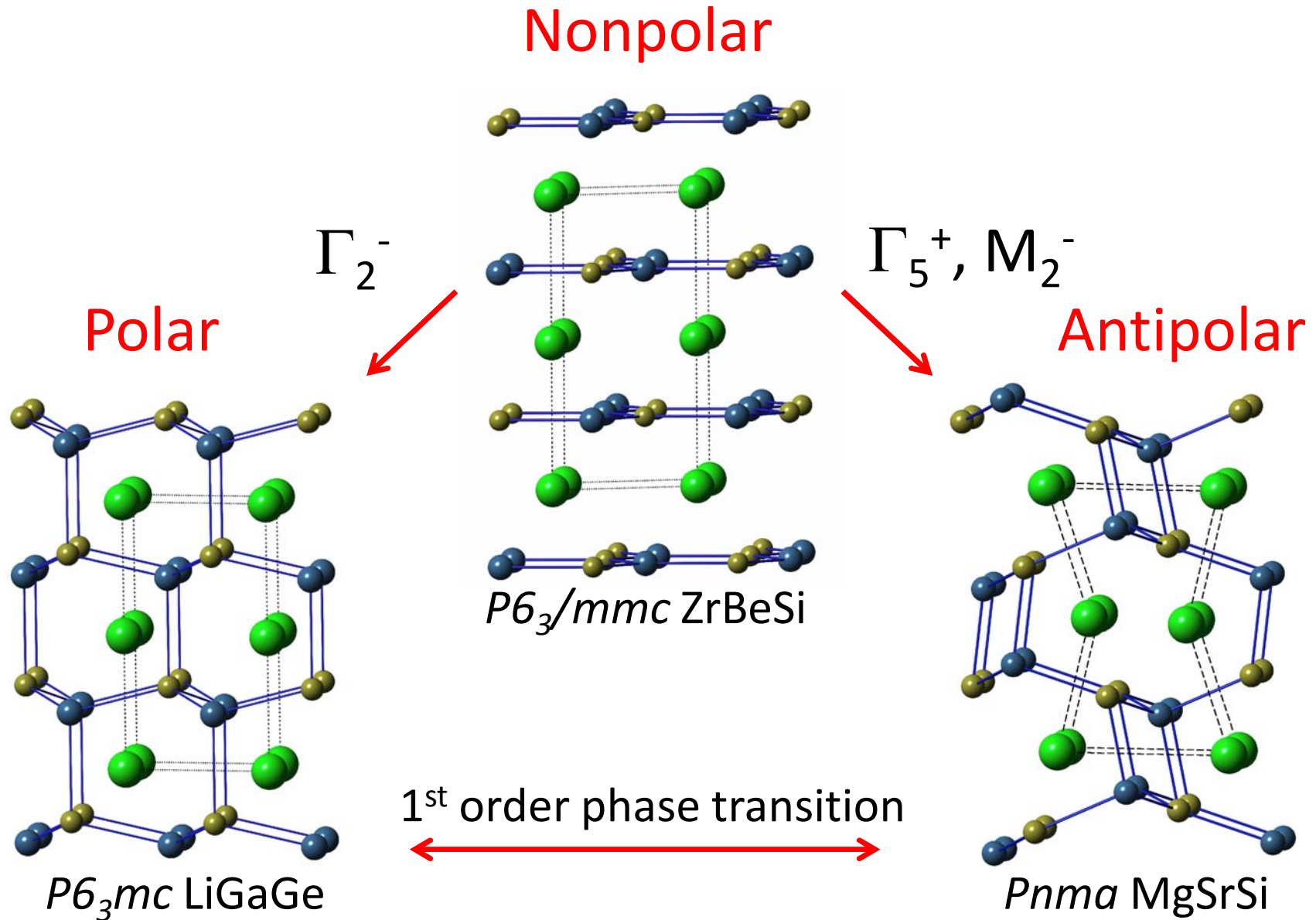


... are other transitions possible?

Structure Forming 18Ve



Orthorhombic *ABC* as antiferroelectrics



Orthorhombic ABC as antiferroelectrics

Our search set is composed of **three subsets**:

- 1) The compounds **in ICSD** in the **MgSrSi structure type**
- 2) The compounds we **previously identified as polar $P6_3mc$** .
- 3) The compounds **predicted to be $Pnma$** in a high-throughput study by Zhang et al., *Adv. Funct. Mater.* (2012)

This gives us **70 total combinations**, for which we need to calculate $P6_3/mmc$, $P6_3mc$ and $Pnma$ (12 atom/cell) symmetries.

We also need to calculate the three possible structural variants.
 $70 \times 3 \times 3 = \mathbf{630 \text{ calculations}}$

Orthorhombic ABC as antiferroelectrics

ABC	ΔE_{sw} (meV)	P (C/m ²)	Γ_5^+	M_2^-	ΔE (meV)	ΔV (Å ³)	$\Delta V/V$ (%)
<u>Li</u> BeP	119	0.85	0.26	1.26	18	1.23	3.7
<u>Mg</u> LiP	20	0.38	0.41	1.28	230	0.49	1.1
<u>Mg</u> LiAs	30	0.39	0.42	1.35	207	0.12	0.2
<u>Ca</u>LiSb	7	0.18	0.19	1.17	79	0.09	0.1
<u>Ca</u>LiBi	7	0.19	0.20	1.16	80	-0.10	-0.1
<u>Na</u> MgP	102	0.49	0.31	1.43	275	1.88	3.2
<u>Na</u> MgAs	114	0.48	0.34	1.44	232	1.65	2.5
<u>Na</u> MgSb	146	0.43	0.40	1.51	154	0.93	1.2
<u>Na</u> MgBi	127	0.42	0.44	1.51	143	1.14	1.4
<u>K</u> MgSb	41	0.40	0.33	1.77	254	2.17	2.6
<u>K</u> MgBi	73	0.31	0.34	1.78	227	1.65	1.8
<u>Na</u> ZnSb	81	0.49	0.18	1.48	42	2.68	4.1
<u>Na</u>LiTe	23	0.20	0.30	1.41	114	0.96	1.4
<u>K</u>NaS	12	0.17	0.32	1.36	149	1.60	2.3
<u>K</u>NaSe	13	0.15	0.33	1.38	131	2.09	2.7
<u>K</u>NaTe	14	0.13	0.38	1.42	96	2.81	2.9
<u>Na</u> AgSe	51	0.65	0.62	1.63	134	0.11	0.2
<u>Ba</u>CaSi	11	0.34	0.35	1.62	310	0.37	0.4

Outline

The ABO_3 Perovskites

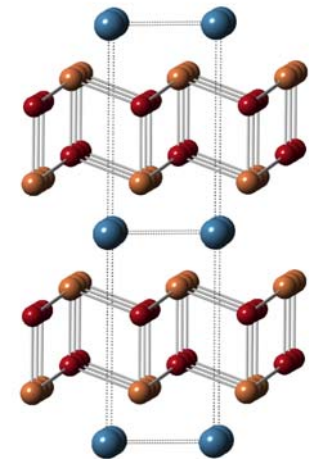
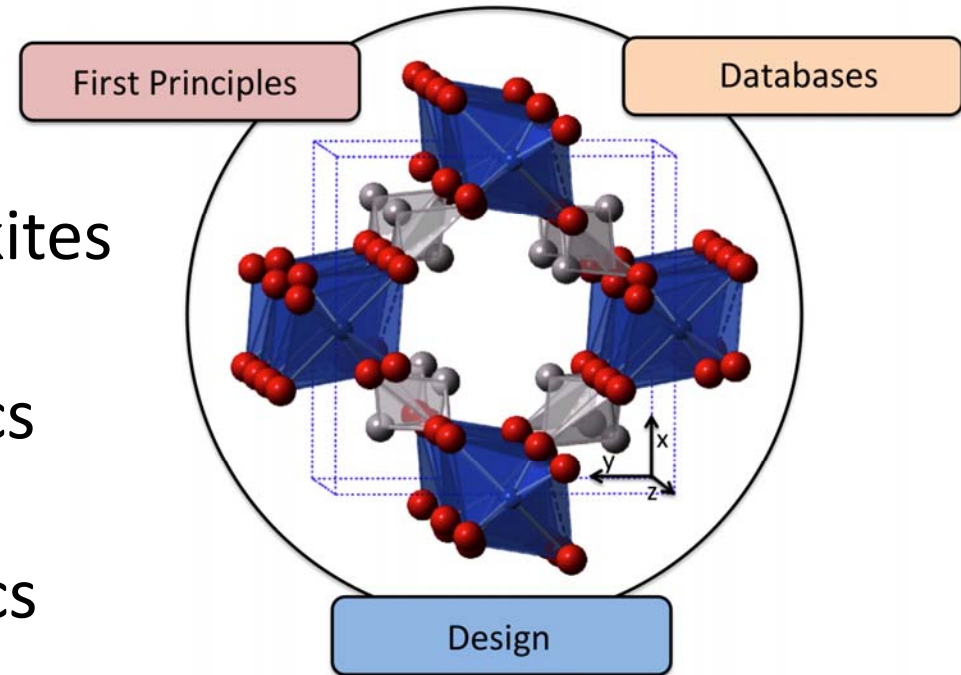
Moving Beyond the Perovskites

A New Class of Piezoelectrics

A New Class of Ferroelectrics

A New Class of Antiferroelectrics

Concluding Thoughts



New Platforms for Functionality

The **half-Heuslers** have **piezoelectric** properties comparable to the perovskites and a **range of lattice constants** and **band gaps**

The **hexagonal ferroelectrics** have a **different shape...**
wurtzite, which is used in many commercial technologies

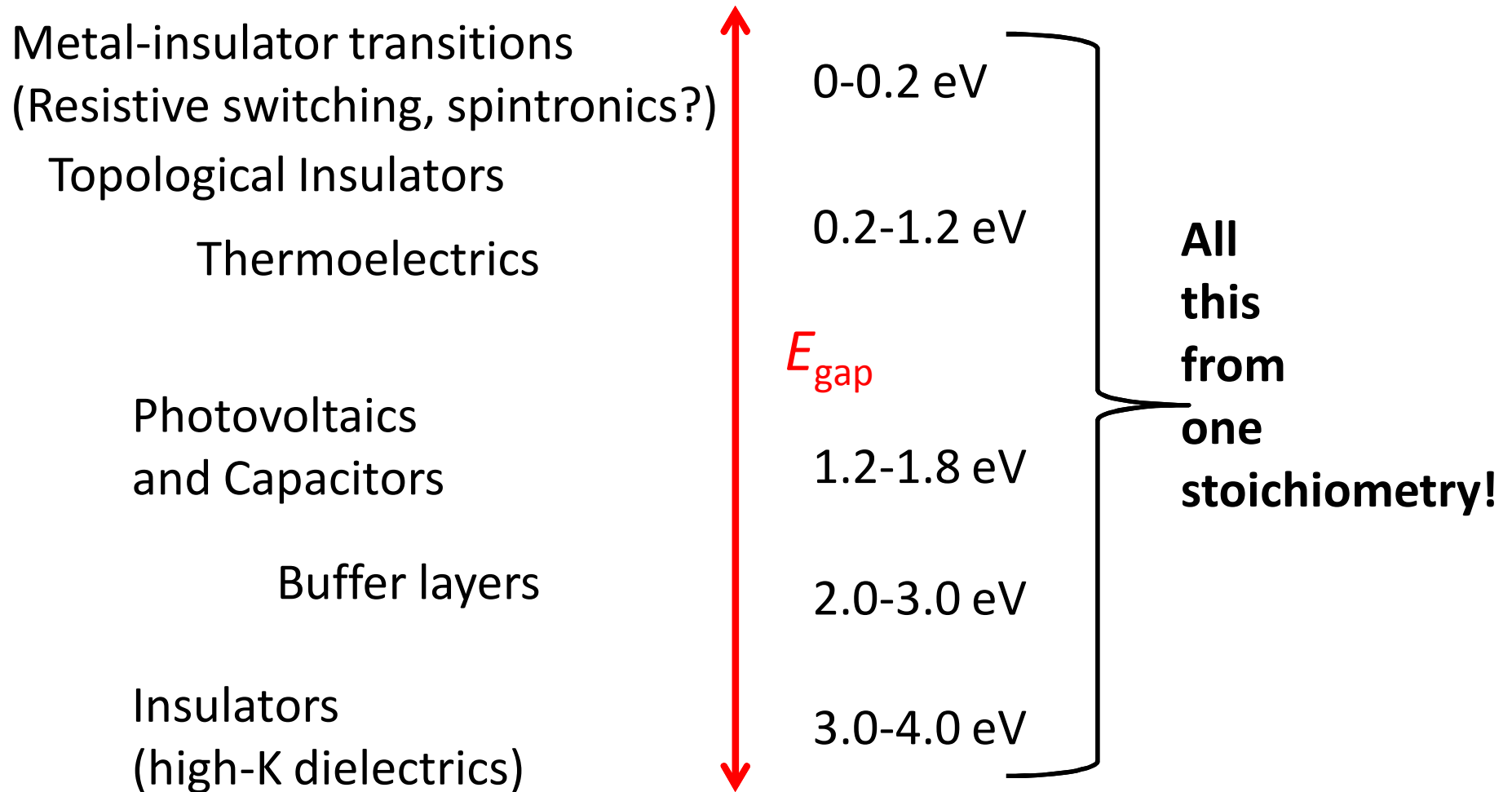
Some of the *ABC* **orthorhombic** variants are **antiferroelectrics**.
(energy storage! metal-insulator transitions? optics?)

Additional database searching shows that there's **more than one way to stuff wurtzite and make it functional!**

Could we think of ways to **replace the materials** in **current devices**?

What do I mean?

We now have intermetallic semiconductors in which a variety of functional properties that can potentially be coupled to:



Acknowledgements

At Rutgers University:

Dr. Anindya Roy (currently at UCSB)

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Dr. Don Hamann

Prof. David Vanderbilt

Prof. Karin Rabe

At Univ. Penn.:

Prof. Sara E. Mason (UI)

Dr. Valentino Cooper (ORNL)

Dr. Eric J. Walter (William and Mary)

Dr. David Stein, **Dr. Ilya Grinberg**,

Prof. Peter Davies

Prof. Andrew M. Rappe

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Prof. Jim Scott

At UCSB:

Prof. Ram Seshadri

At Cornell Univ.:

Prof. Craig Fennie

Dr. Derek Stewart

At UGA:

Prof. Steve Lewis

At Univ. Houston:

Prof. P Shiv Halasyamani

With Regards to the Calculations

High throughput studies:

Pseudopotential testing is a must!

Set up a few test calculations before your high-throughput study!

Converged data for functional property of interest:

d_{14} vs. e_{14} and k_{14} , need to increase k-point sampling, E_{cut} , etc.

Post-DFT methods may be necessary:

Looking for semiconductive materials, want an accurate band gap

LDA+U, PBE0, or GW for the exceptional candidates

See both G. Gou *et al.*, PRB (2011) 205115, and *our JSSC paper*

Some Calculations Simply Fail:

This is most times a hardware issue, sometimes software (dilatomx)

No One Wants HgPbAs In Their Cell Phone

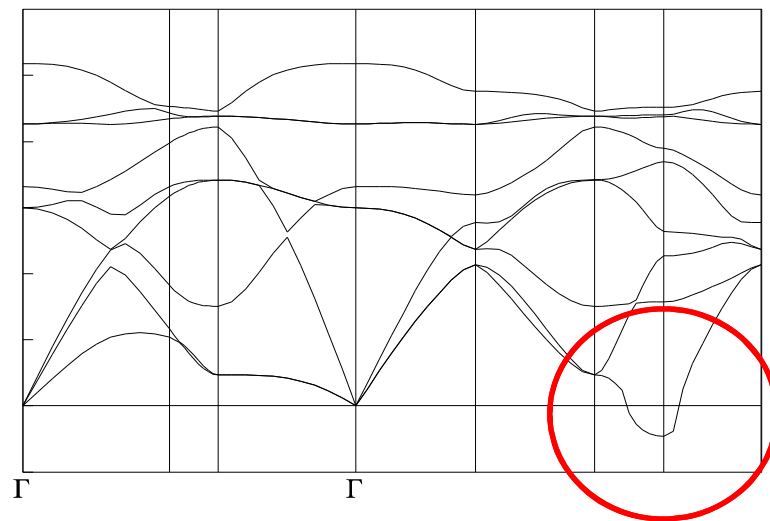
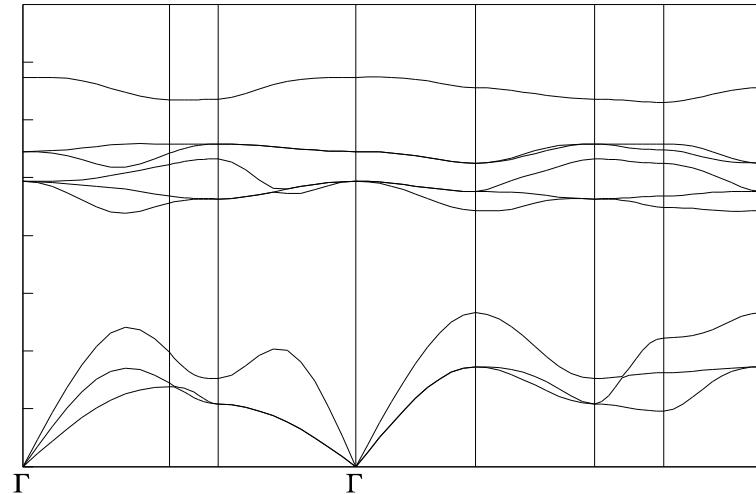
Apply these criteria:

1) Must not contain toxic or expensive elements

2) DFT band gap > 0.4 eV
(experimental leakage)

3) $dE > 0.15$ eV
(difference between
2 lowest configurations)

4) Instabilities at some point in the BZ?



High-Throughput Study of Half-Heuslers

1) Ground state DFT-LDA calculation.

3 possible structural variants (**2700 calc.!**).
Which atom sits in the tetrahedral site?
Calculate the differences in total energy

2) Insulating or metallic?

3) Phonon response calculation.

Unstable at Gamma?
(won't form half-Heusler...
not dynamically stable)

4) Toxic or expensive elements, dE, etc.

over **900** combinations



over **400** combinations



over **300** combinations



over **100** combinations

High-Throughput Study of Half-Heuslers

Sorting Stable vs. Unstable Hypothetical Compounds:
The case of multifunctional *ABX* half-Heusler
filled tetrahedral structures

by Zhang, Yu, Zakuthayev and Zunger (2012)

Considered stability with regards to binary compositions
(thermodynamic stability wrt decomposition)
and alternative structures. Used GW to predict band gap.

Of the 488 *ABC* not yet reported, predicted 235 to be stable.

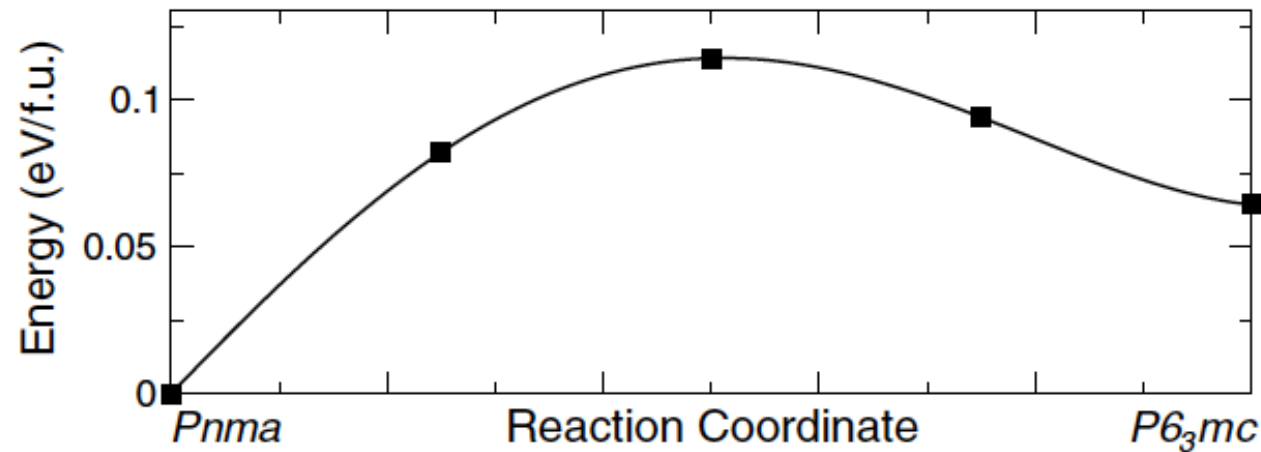
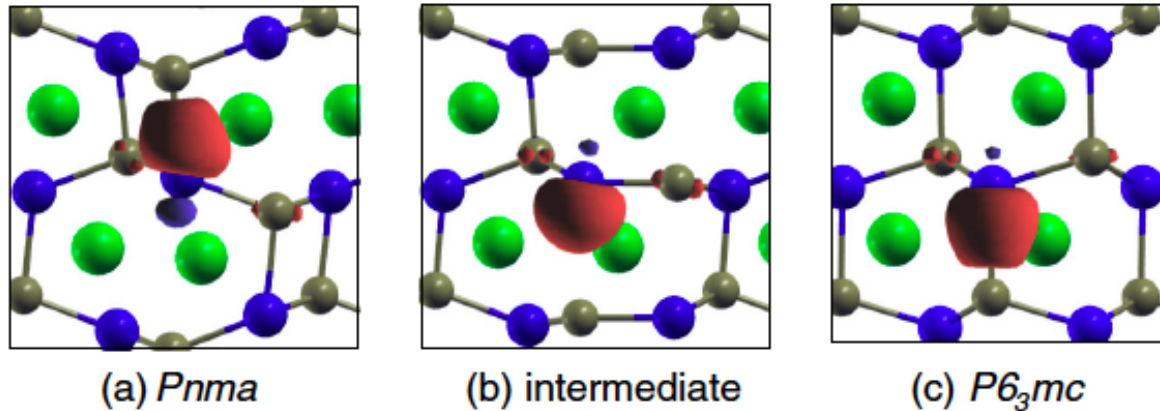
Our approach assumes that if we could potentially stabilize
an *ABC* combination in an insulating half-Heusler structure,
then we could measure their piezoelectric properties

AFEs metal/insulator

TABLE II. Same as Table I, but for compounds in the search set for which either the $Pnma$ state or the $P6_3mc$ state is metallic in our discrete Fourier transform (DFT) calculation. A dash in the polarization (P) column indicates that the $P6_3mc$ state is metallic.

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<u>MgLiBi</u>	41	...	0.52	1.45	126	1.52	2.4
<u>MgCuP</u>	1	0.36	0.42	1.43	174	-0.58	-1.3
<u>NaZnBi</u>	328	...	0.18	1.28	18	2.50	3.6
<u>NaCdAs</u>	199	0.40	0.31	1.44	50	1.54	2.4
<u>SrCaGe</u>	2	0.04	0.27	1.36	186	3.72	4.6
<u>BaCaGe</u>	11	0.26	0.37	1.59	289	1.04	1.1

AFE Wannier Functions: NaCdAs NEB path



Solid State Testing

What is your project?

Simple binary oxide (MO, MO₂, M₂O₃, etc.)

tertiary oxide (ABO₃)

III-V semiconductor (GaAs, InN, etc.)

Use ICSD for structural parameters

Find other DFT references

(Run AE calculations?)

AIP *F4bar3m* a=5.398 Ang. (-0.59 %)

YN *F4bar3m* a=5.192 Ang. (-0.09 %)

BaO *Fm3barm* a=5.539 Ang. (-1.51 %)

PbS *Fm3barm* a=5.842 Ang. (-1.54 %)

TiO₂ *hex.* a=4.549 Ang. (-0.98 %); c=2.958 Ang. (-1.05 %)

Calculation of Properties

Use **Landolt Bornstein** (LB) for properties like **piezoelectric response**.
Find **other DFT references**. What do they report?

Set up a **phonon response** calculation.

In **ABINIT**, there are **tutorials** that will guide you through this.

For example, results of my potentials using telast tutorials:

InSb

$$d_{14} = -2.29 \text{ pC/N } (-2.35 \text{ pC/N LB})$$

$$e_{14} = -0.066 \text{ C/m}^2 \text{ } (-0.07 \text{ C/m}^2 \text{ LB})$$

While this is in good agreement,
it is not an indication
that the potential is perfect...
but it is promising.

GaAs

$$d_{14} = -2.89 \text{ pC/N } (-2.60 \text{ pC/N LB})$$

$$e_{14} = -0.15 \text{ C/m}^2 \text{ } (-0.16-0.21 \text{ C/m}^2 \text{ LB})$$

Hexagonal and Trigonal Polar Groups

Crystal Class	Space Group	Total	1	2	3	4	5+	Most Common Structure Types	No Type
<i>6mm</i>	186	1327	6	374	551	248	148	GaGeLi (139), ZnS (445)	118 (8.9%)
	185	169	0	32	67	52	18	LuMnO ₃ (54), LaF ₃ (25)	46 (27.2%)
	184	15	0	0	5	2	8	zeolite (9)	5 (33.3%)
	183	19	0	1	7	9	2	none	19 (100%)
6	173	681	0	29	125	304	223	Apatite (39), La ₃ CuSiS ₇ (177)	145 (21.3%)
	172	1	0	0	0	1	0	none	1 (100%)
	171	5	0	3	0	1	1	none	5 (100%)
	170	13	0	1	0	7	5	Ba(NO ₂) ₂ *2H ₂ O (5)	7 (53.9%)
	169	33	0	6	9	6	12	Al ₂ S ₃ (11)	16 (48.5%)
	168	1	0	0	0	1	0	none	0 (0.0%)
<i>3mm</i>	161	587	0	22	212	221	132	LiNbO ₃ (287), whitlockite (61)	118 (20.1%)
	160	798	0	276	215	102	205	ZnS (123), FeBiO ₃ (79)	216 (27.1%)
	159	168	2	27	22	57	60	Si ₃ N ₄ (18)	80 (47.6%)
	158	22	0	5	3	7	7	none	22 (100%)
	157	72	0	3	28	26	15	Mg ₃ Si ₂ O ₅ (OH) (19)	30 (41.7%)
	156	347	0	259	29	53	6	CdI ₂ (137)	116 (33.4%)
3	146	214	1	12	76	76	49	Ni ₃ TeO ₆ (12)	131 (61.2%)
	145	22	0	1	7	6	8	RbNO ₃ (2)	19 (86.4%)
	144	82	0	16	23	32	11	RbNO ₃ (16)	42 (51.2%)
	143	99	1	13	33	21	31	NiTi (6)	86 (86.9%)

Tetragonal Polar Groups

<i>4mm</i>	110	51	0 4	28 10	9	Li ₂ B ₄ O ₇ (22)	11 (21.6%)
	109	50	0 11	30 6	3	LaPtSi (16)	19 (38.0%)
	108	29	0 1	21 5	2	Pb ₅ Cr ₃ F ₁₉ (4)	25 (86.2%)
	107	121	0 13	69 17	22	BaNiSn ₃ (43)	44 (36.4%)
	106	5	0 0	2 3	0	none	5 (100%)
	105	5	0 0	4 1	0	none	5 (100%)
	104	9	0 0	5 0	4	Tl ₄ HgI ₆ (4)	5 (55.6%)
	103	8	0 6	2 0	0	NbTe ₄ (7)	1 (12.5%)
	102	23	4 6	5 4	4	Al ₂ Gd ₃ (4)	12 (52.2%)
	101	3	0 0	3 0	0	none	3 (100%)
	100	97	0 1	16 57	23	BSN (21), Ba ₂ TiOSi ₂ O ₇ (23)	20 (20.6%)
	99	299	0 6	104 82	107	PbTiO ₃ (210), PbVO ₃ (12)	32 (10.7%)
	4	80	16	0 3	6 5	2	none
79		42	0 5	20 7	10	U ₃ Al ₂ Si ₃ (6)	29 (69.1%)
78		12	1 0	6 1	4	none	12 (100%)
77		10	0 4	4 2	0	H ₂ S (3)	7 (70.0%)
76		48	2 5	22 4	15	Ca ₂ P ₂ O ₇ (16)	23 (47.9%)
75		23	0 7	4 6	6	K ₄ CuV ₅ O ₁₅ Cl (4)	19 (82.6%)

Orthorhombic Polar Groups

Crystal Class	Space Group	Total	1	2	3	4	5+	Most Common Structure Types	No Type
<i>mm2</i>	46	179	0	4	52	52	71	Ca ₂ AlFeO ₅ (79), ErSr ₂ GaCu ₂ O ₇ (27)	53 (29.6%)
	45	33	0	0	15	8	10	Ca ₁₁ InSb ₉ (5), Sr ₄ Fe ₆ O ₁₃ (15)	17 (51.5%)
	44	153	0	25	78	31	19	NaNO ₂ (13)	74 (48.4%)
	43	287	0	43	44	87	113	Natrolite (61)	111 (38.7%)
	42	69	1	23	21	16	8	NbS ₂ (10)	47 (68.1%)
	41	117	0	18	24	54	21	Bi ₄ Ti ₃ O ₁₂ (15)	71 (60.7%)
	40	107	0	15	16	58	18	NaCu ₂ NbS ₄ (14)	55 (51.4%)
	39	42	0	14	15	7	6	LaS (5)	31 (73.8%)
	38	186	2	51	86	37	10	CeNiC ₂ (29)	108 (58.1%)
	37	22	0	0	6	4	12	none	22 (100%)
	36	691	1	65	268	214	143	Bi ₃ TiNbO ₉ (87)	249 (36.0%)
	35	41	0	1	6	16	18	none	41 (100%)
	34	55	0	5	8	25	17	Ca ₂ B ₅ O ₉ Br (12)	35 (63.6%)
	33	1087	2	68	300	377	340	Cu ₂ Sc ₂ O ₅ (18), NaFeO ₂ (56)	258 (23.7%)
	32	48	0	5	15	10	18	K _{1-x} FeF ₃ (4)	33 (68.8%)
	31	376	0	16	136	114	110	Cu ₃ AsS ₄ (56)	157 (41.8%)
	30	20	0	2	3	5	9	Fe ₃ (PO ₄) ₂ *H ₂ O	19 (95.0%)
	29	305	1	11	83	124	86	boracite (16)	184 (60.3%)
	28	30	0	6	12	2	10	AuTe ₂ (5)	20 (66.7%)
	27	5	0	1	3	1	0	V ₄ H ₃ (1)	4 (80.0%)
26	133	0	9	37	59	28	NaNbO ₃ (5)	88 (66.2%)	
25	47	0	17	12	12	6	GaAs (7)	29 (61.7%)	

Mono and Triclinic Polar Groups

<i>m</i>	9	621	0	40	159	215	207	Pb(Ti,Zr)O ₃ (14)	339 (54.6%)
	8	350	0	30	103	116	101	Ca ₅ (BO ₃) ₃ F (17), Pb ₂ FeNbO ₆ (48)	199 (56.9%)
	7	307	0	51	68	108	80	WO ₃ (32)	189 (61.6%)
	6	59	0	7	13	22	17	PMN-PT and (Na,K)NbO ₃ (17)	42 (71.2%)
2	5	430	1	30	123	152	124	many	292 (67.9%)
	4	722	10	35	151	282	244	many	415 (57.5%)
	3	45	2	4	11	13	15	none	45 (100%)
1	1	460	6	52	118	150	134	many	324 (70.4%)

Landolt-Bornstein database

Some materials are very well characterized! **And decent!**

Class 3m ($C3v$)	k_{31}	k_{33}	k_{15}	d_{31}	d_{33}	d_{15}	e_{31}	e_{33}	e_{15}
Ag_3SbS_3	0.17	0.4	0.3	23	35	32	0.2	1.1	0.4
LiNbO_3	0.02	0.2	0.6	1	18	75	0.7	1.8	3.8

But most really aren't

Class 622 ($D6$)	k_{14}	d_{14}	e_{14}
CsCuCl_3	0.12	7.2	0.04
SiO_2	?	2	?

Class 3 ($C3$)	k_{31}	k_{33}	e_{31}	e_{33}
$\text{Pb}_5\text{Ge}_3\text{O}_{11}$	0.08	0.13	0.61	0.77

Class 4bar3m	k_{14}	d_{14}	e_{14}
AlSb	0.10	1.6	0.07
CdTe	0.03	1.7	0.04
GaAs	0.09	2.6	0.16
Tl_3TaS_4	0.55	58	0.32
ZnS	0.09	3.2	0.15
ZnSe	0.03	1.1	0.05
ZnTe	0.02	0.9	0.03

where's the d_{ij} values?

What is a piezoelectric?

- 1) A material that needs to be **insulating**
- 2) A material that has **no inversion center**

The **piezoelectric effect** is an electromechanical interaction
(this means that electricity is generated by a mechanical force)

We **measure** how great this effect is
(via response to a deformation)
with **tensors** e_{ij} and d_{ij}

$$e_{i\alpha} = \frac{\partial P'_i}{\partial \eta_\alpha} \quad d_{i\alpha} = S_{\alpha\beta} e_{i\beta}$$

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$$k_{i\alpha} = \frac{|d_{i\alpha}|}{\sqrt{\epsilon_{ii}^{\sigma} S_{\alpha\alpha}}}$$

However, the **figure of merit** is k_{14} !