

2440-11

**16th International Workshop on Computational Physics and Materials Science:
Total Energy and Force Methods**

10 - 12 January 2013

From transition metal oxides to cosmology with electronic structure calculations

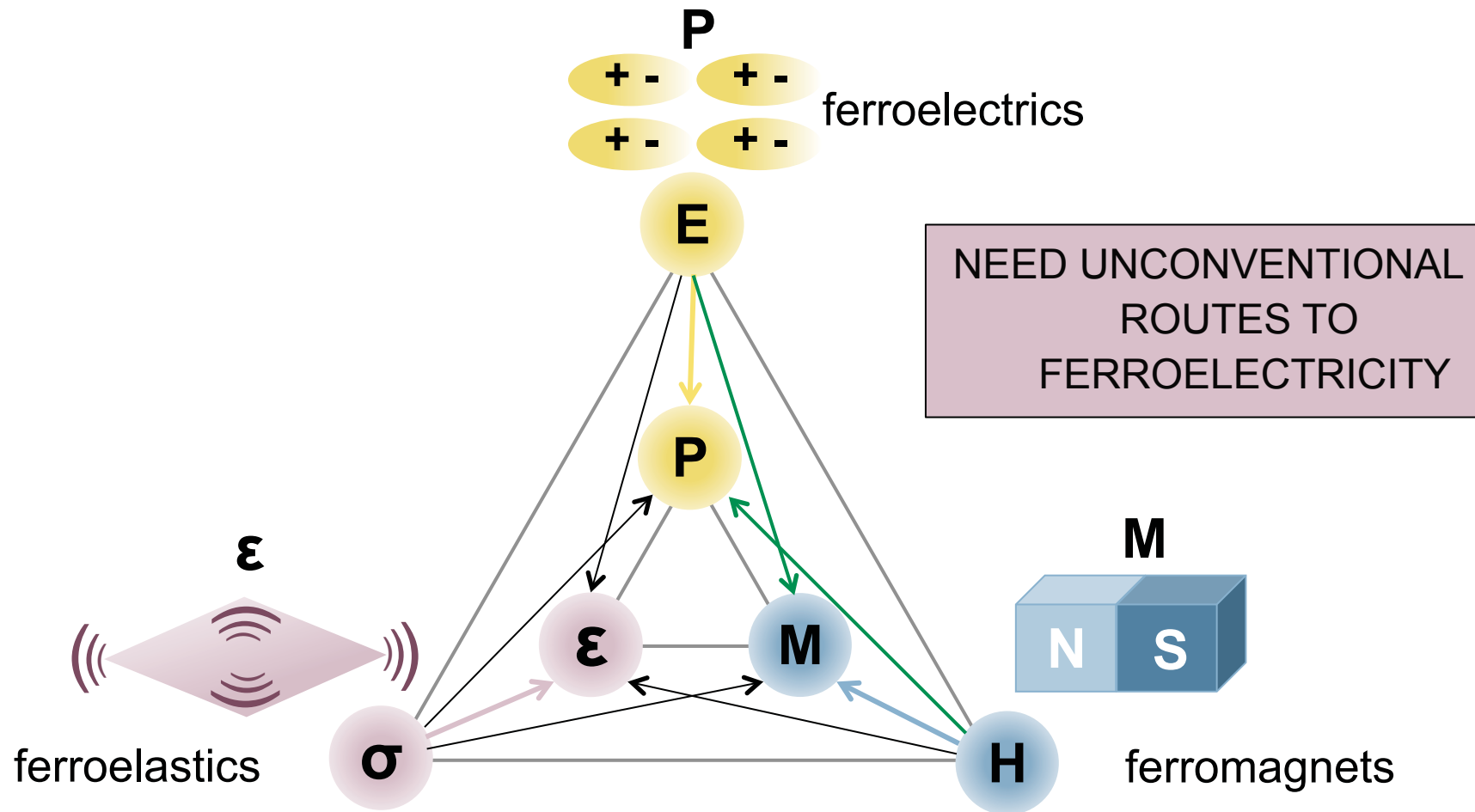
Nicola Spaldin
*ETHZ
Switzerland*

From Multiferroics to Cosmology with Electronic Structure calculations

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Materials Theory
Department of Materials, ETH Zürich



Magnetoelectric multiferroics

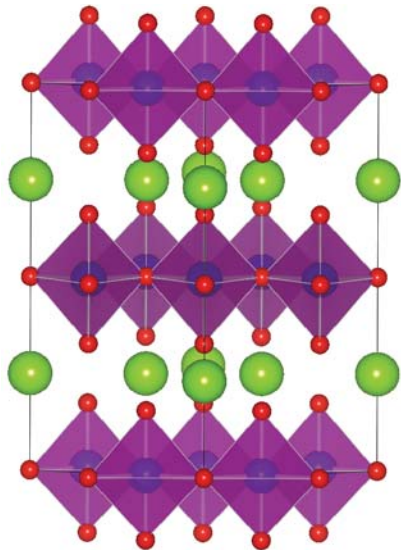


*The renaissance of magnetoelectric multiferroics, N.A. Spaldin and M. Fiebig, Science 15, 5733 (2005)
N.A. Hill, Why are there so few magnetic ferroelectrics? J. Phys. Chem. B 104, 6694 (2000)*

An unconventional ferroelectric: YMnO_3

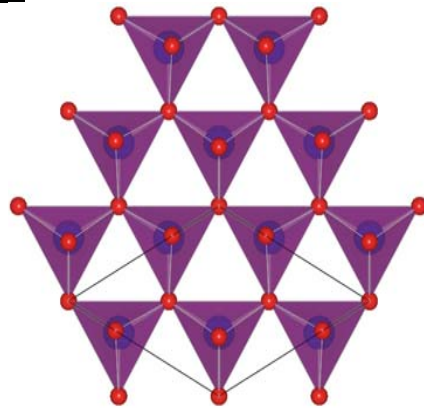
High temperature

$P6_3/mmc$



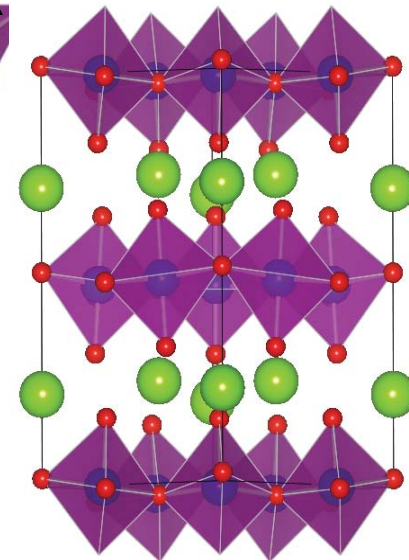
paraelectric

$\sim 1000\text{K}$



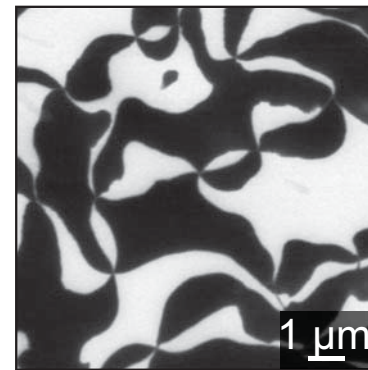
Low temperature

$P6_3cm$



Polarization ($5.6 \mu\text{C}/\text{cm}^2$)

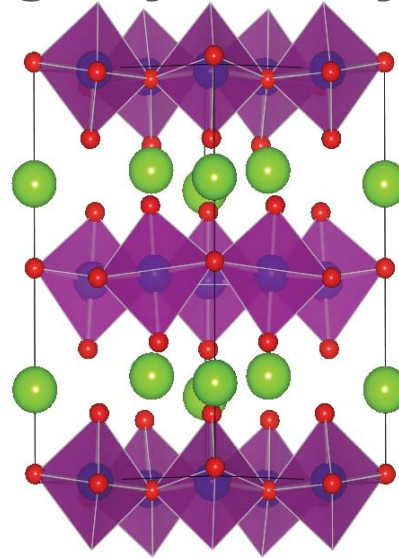
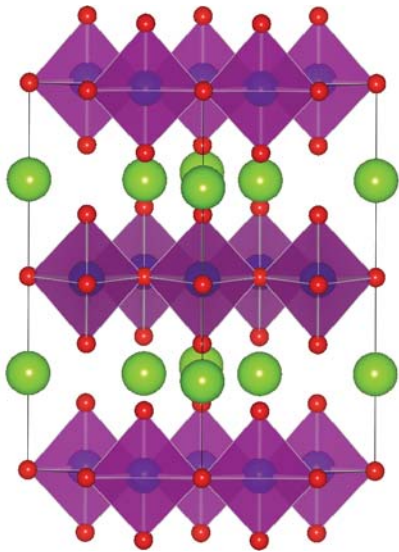
ferroelectric



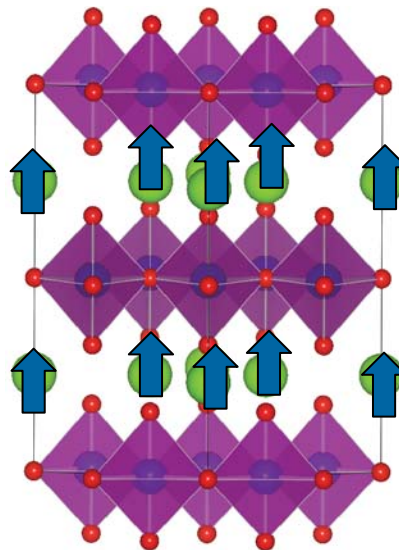
0 2 4 6 8 10
Relative PFM contrast (%)

Calculate phonons for high symmetry structure

We find that 2 phonon modes of the high symmetry structure take us to the low symmetry structure



Trimerization (K_3)



Y displacements (Γ_2)

We can then map out the energy surface for these phonons

DFT calculations show us that the ferroelectricity is *improper*.

The trimerization (K3) mode is the energy-lowering primary order parameter

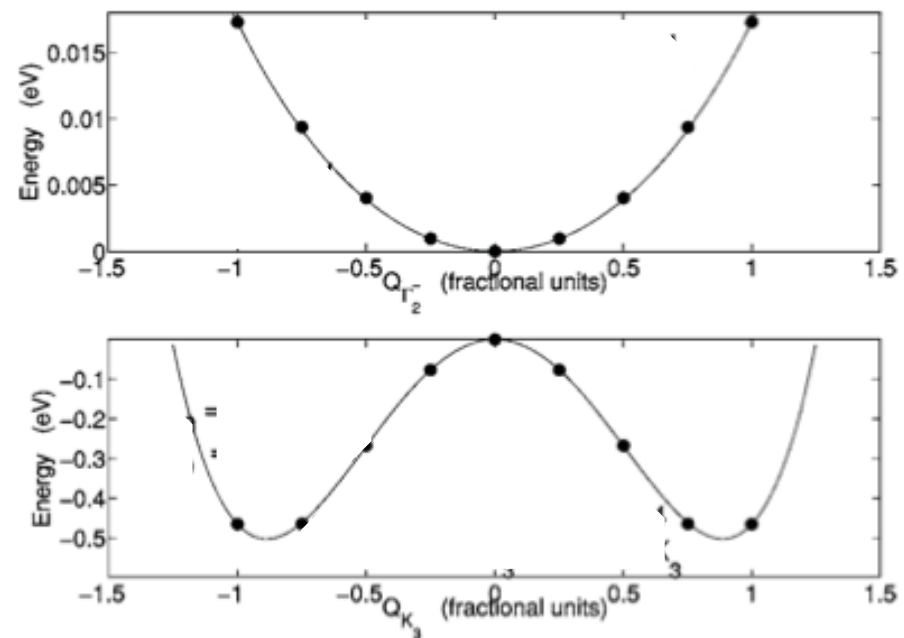
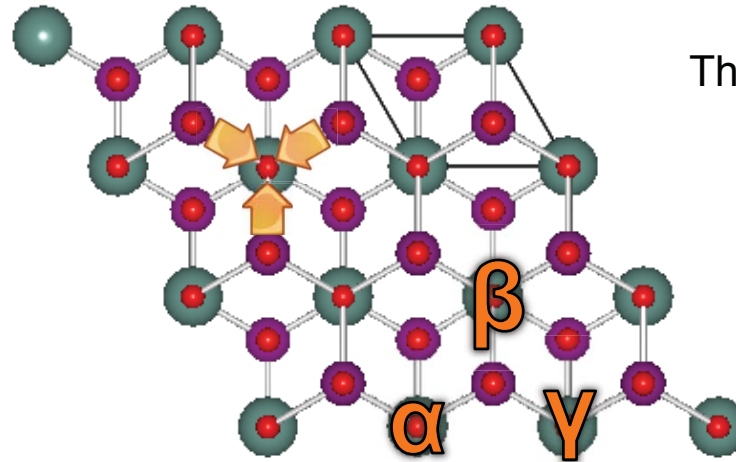
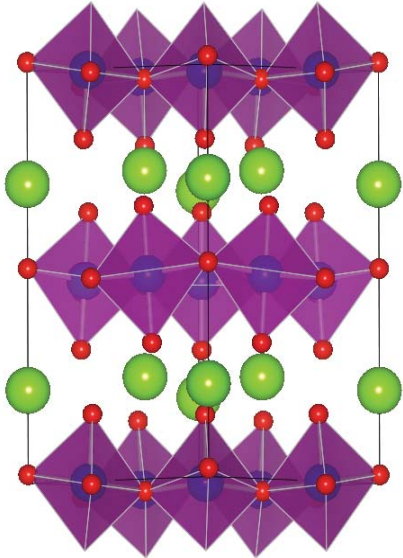


FIG. 2. Energy as a function of (top) $Q_{\Gamma_2^-}$ and (bottom) Q_{K_3} .

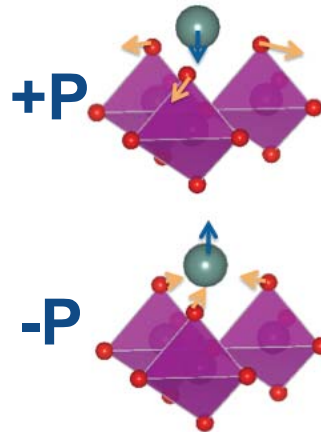
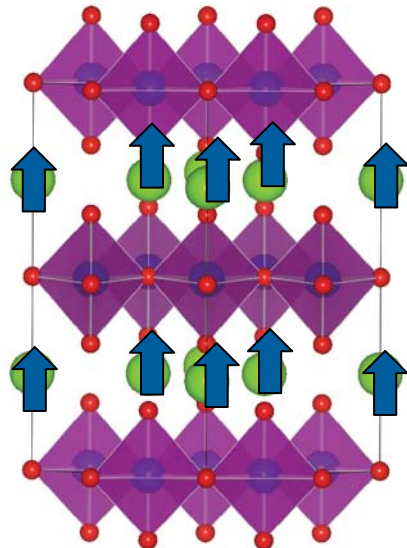
An improper geometric ferroelectric

Look at these distortions in more detail:

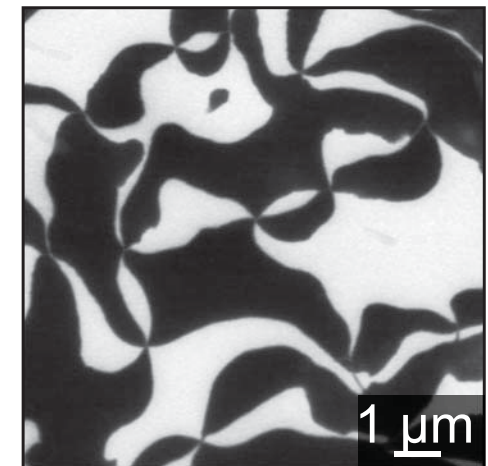


Three possible origins

Expect six domains!



Two possible orientations



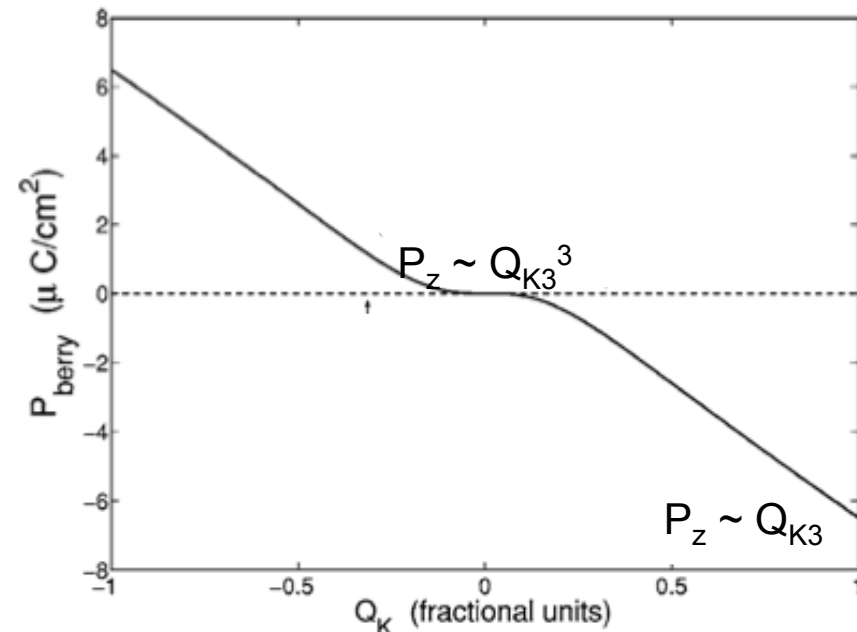
0 2 4 6 8 10
Relative PFM contrast (%)

We can calculate how the polarization depends on the trimerization amplitude:

Near the phase transition the ferroelectric polarization is effectively zero

Landau free energy

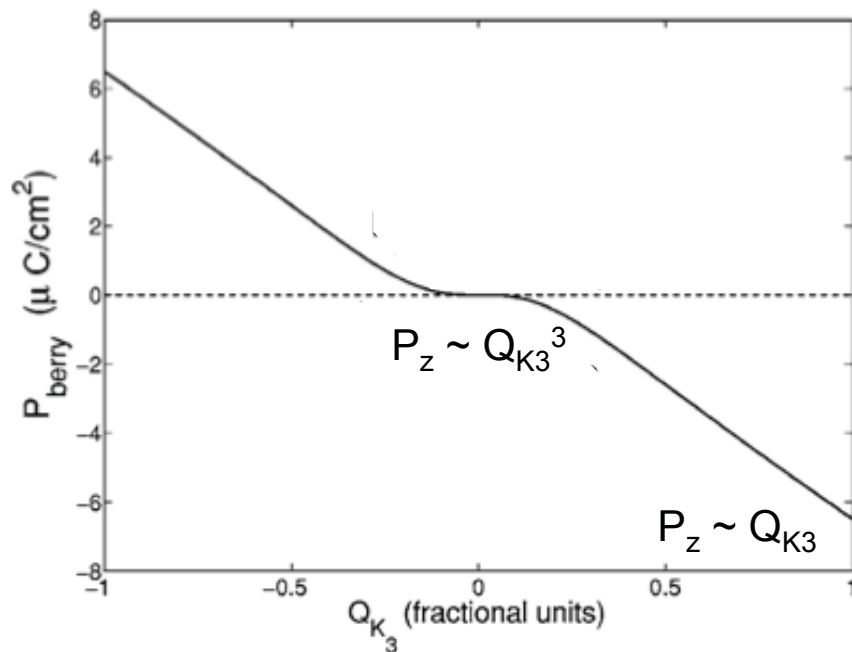
$$f_u = \frac{a}{2}Q^2 + \frac{b}{4}Q^4 + \frac{Q^6}{6}(c + c' \cos 6\Phi) - gQ^3 P_z \cos 3\Phi \\ + \frac{g'}{2}Q^2 P_z^2 + \frac{P_z^2}{2\chi_0}$$



S. Artyukhin, K.T. Delaney, NAS and M. Mostovoy, *Landau theory of topological defects in multiferroic hexagonal manganites*, arXiv:1204.4126

C.J. Fennie and K.M. Rabe, *Ferroelectric phase transition in YMnO3 from first principles* Phys. Rev. B 72, 100103 (2005)

Consequences of “zero” polarization at small trimerization amplitude:



1) Domain formation at the transition is not dominated by minimization of the depolarizing field

2) Effective continuous symmetry at the phase transition

Combine to allow application of YMnO_3 to cosmological problems

S. Artyukhin, K.T. Delaney, NAS and M. Mostovoy, *Landau theory of topological defects in multiferroic hexagonal manganites*, arXiv:1204.4126

C.J. Fennie and K.M. Rabe, *Ferroelectric phase transition in YMnO_3 from first principles* Phys. Rev. B 72, 100103 (2005)

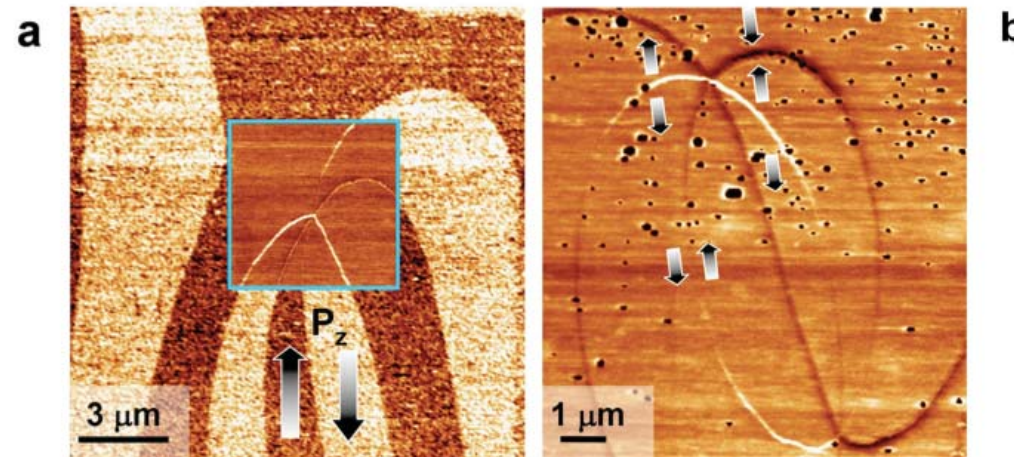
Outline

Analogy between the structural phase transition in YMnO_3 and the Grand Unification Transition

Show that the symmetry of the phase transition in YMnO_3 results in one-dimensional “topologically protected” defects (Kibble)

Test whether the formation of these defects follows the so-called “Kibble-Zurek” scaling (number of defects as a function of cooling rate) proposed for such a transition

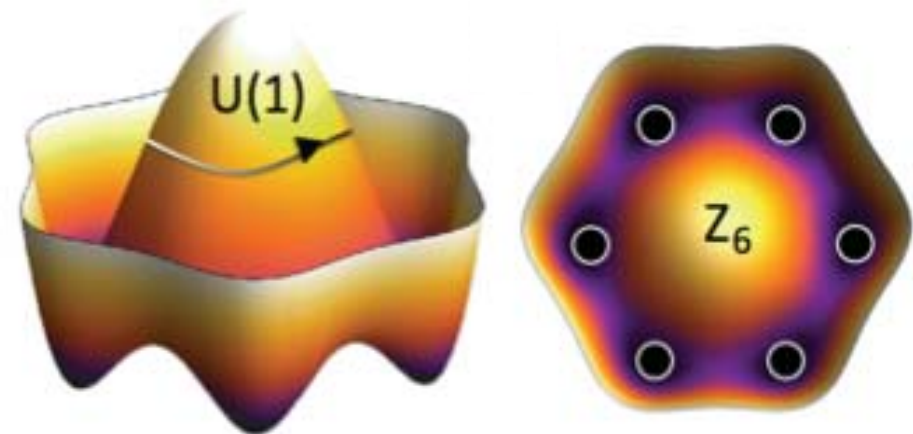
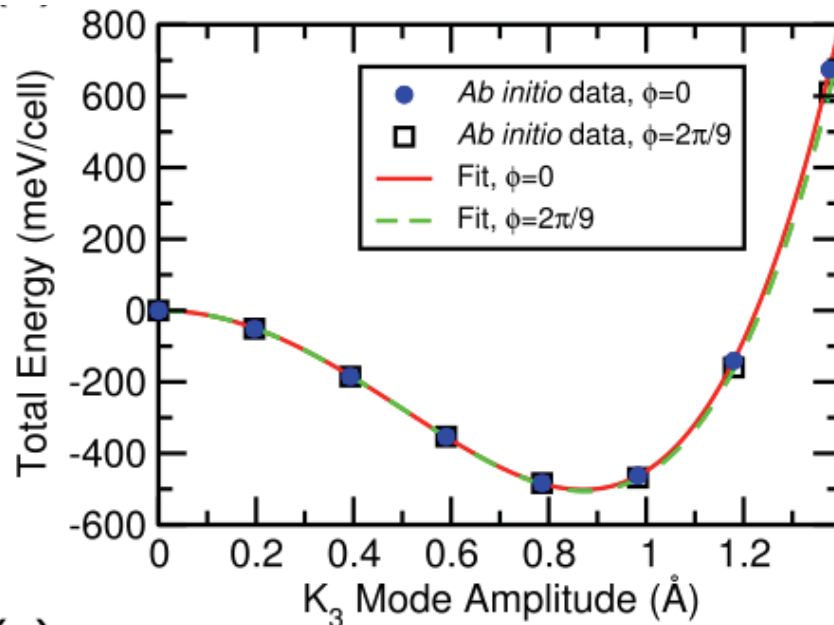
Ferroelectric polarization does not determine domain structure: Formation of head-to-head and tail-to-tail domain walls



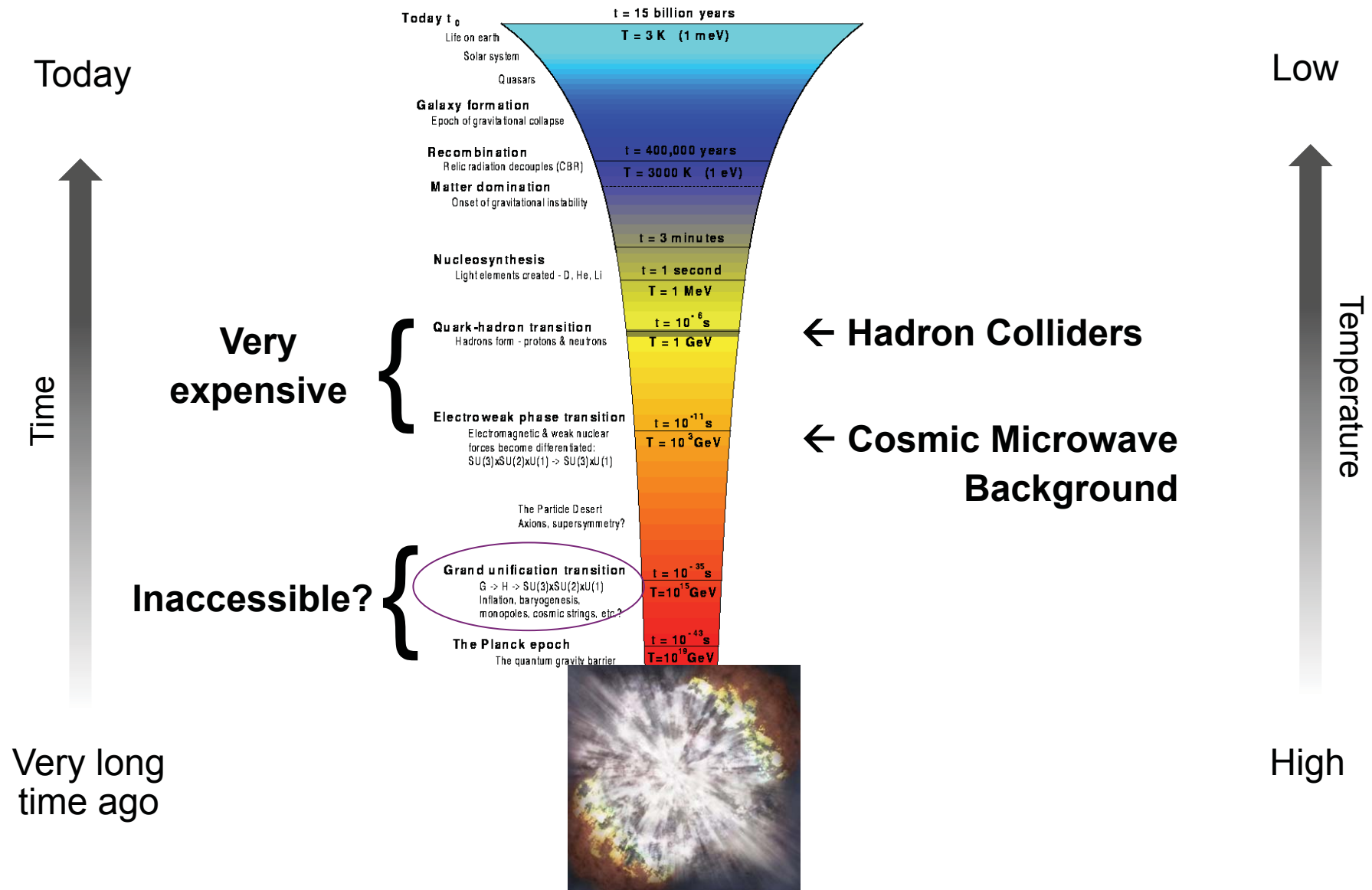
Effective continuous symmetry at the phase transition:

When $P=0$, the energy is (surprisingly) independent of the trimerization angle:

And the potential is a Mexican hat with a smooth peak and six minima in the brim:



Early universe processes

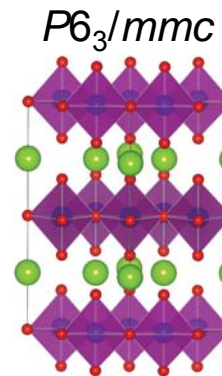
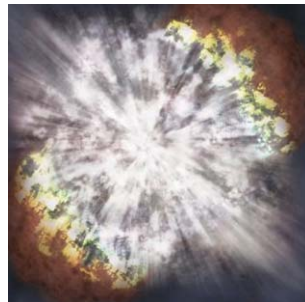
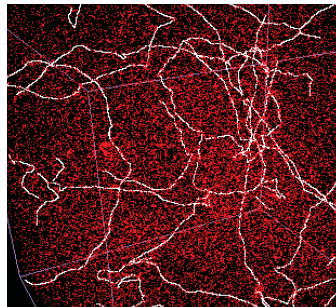


Analogy between YMnO_3 and the physics proposed for the GUT?

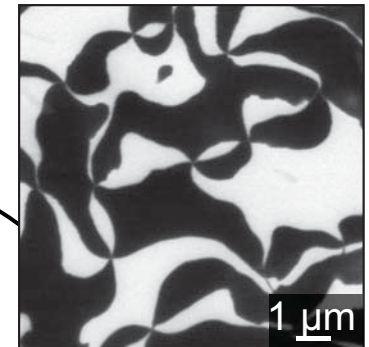
spontaneous symmetry breaking described by a non-trivial homotopy group

Results in formation of *topological defects* (Kibble)

Universe



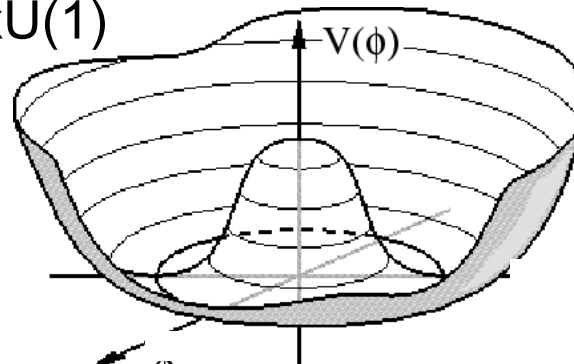
YMnO_3



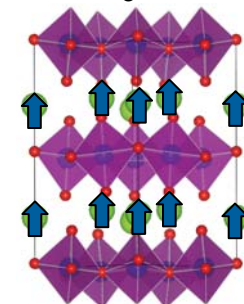
$U(1)$

$SU(3) \times SU(2) \times U(1)$

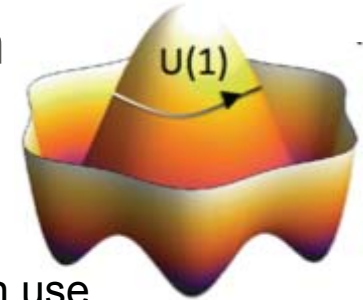
The Particle Desert



$P6_3cm$



We can show formally that the YMnO_3 phase transition produces one-dimensional topological defects:

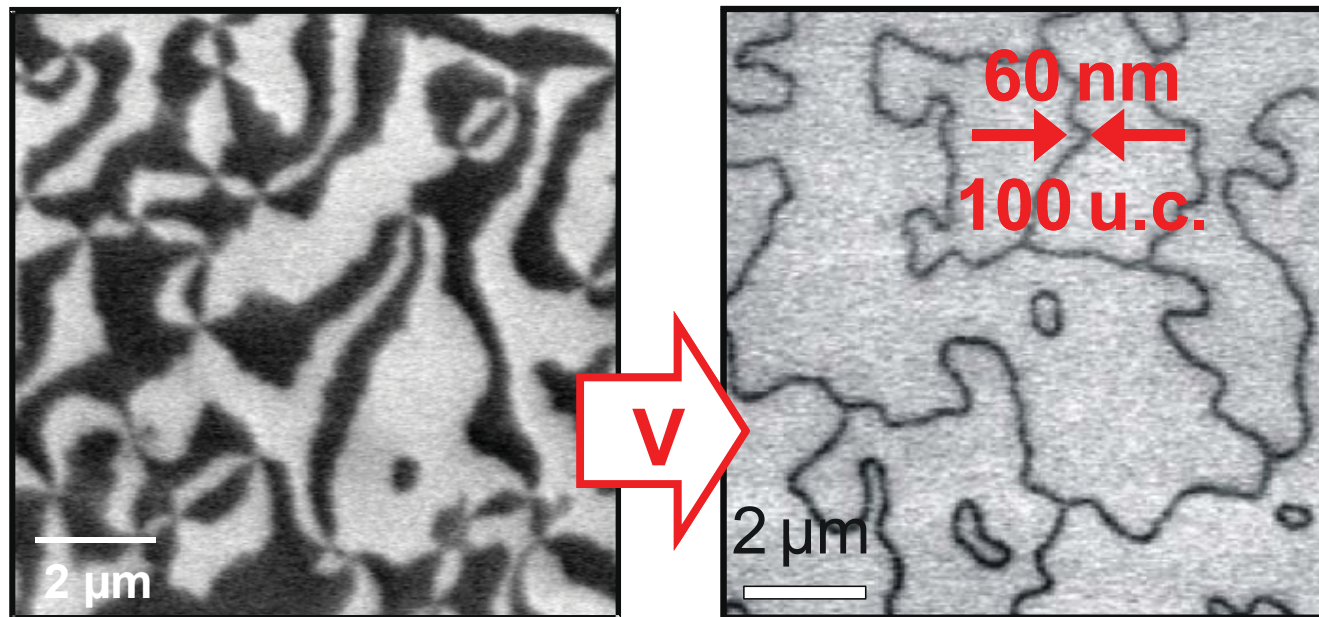


Since the symmetry near the phase transition is effectively continuous, we can use established results of homotopy theory to assess the topology of transition:

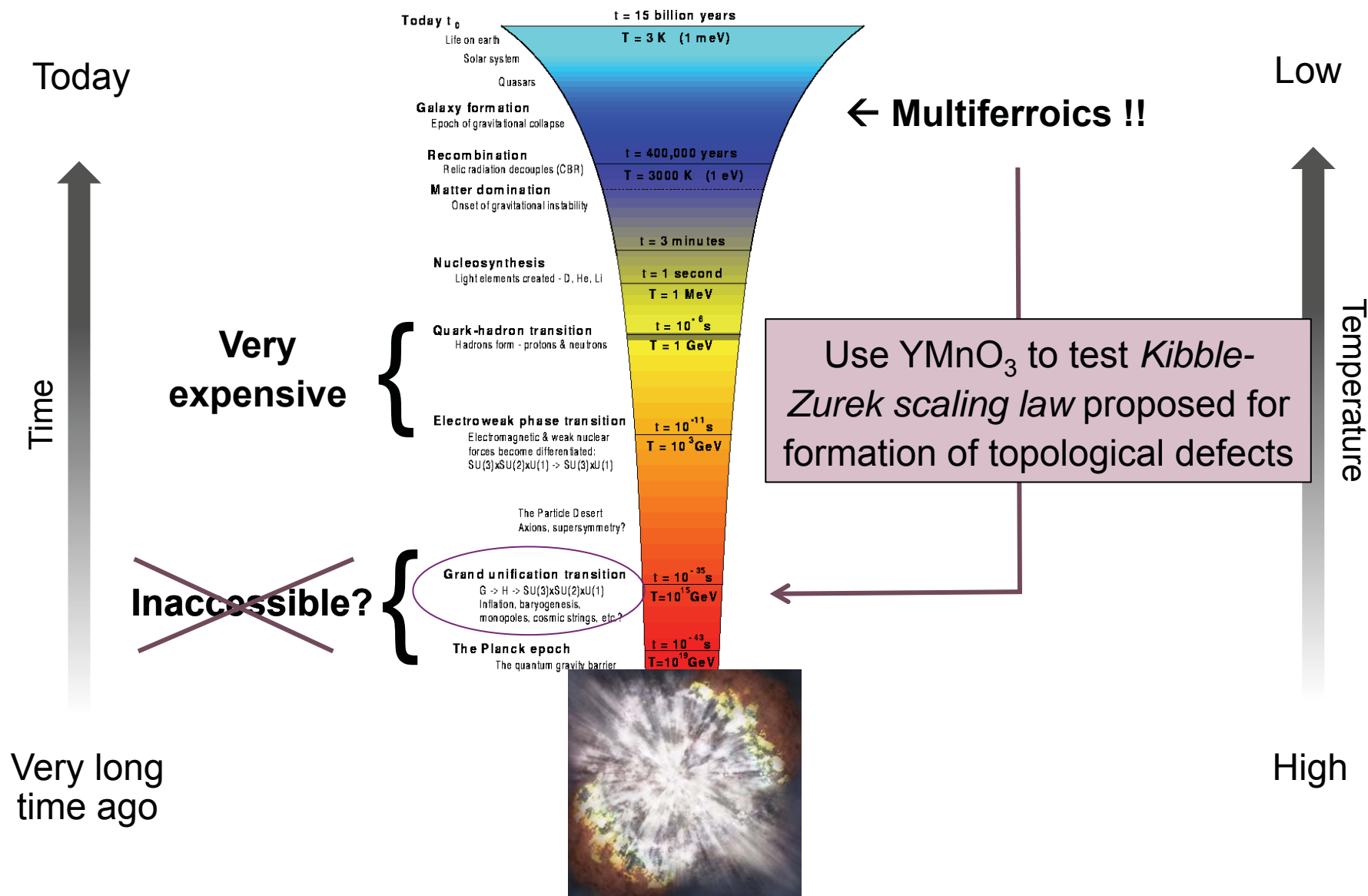
- 1) Map the symmetry characteristic of the order parameter – $U(1)$ – onto an n -dimensional sphere: one-dimensional circle S^1
- 2) Look up in a topology textbook whether the homotopy group π of S^1 is non-trivial or not
- 3) In fact $\pi_1(S^1)$ is non-trivial and produces 1-dimensional topologically protected singularities!

The domain intersections in YMnO_3 are formally mathematically topologically protected

“Protected” domain structure can’t be poled:



Early universe processes

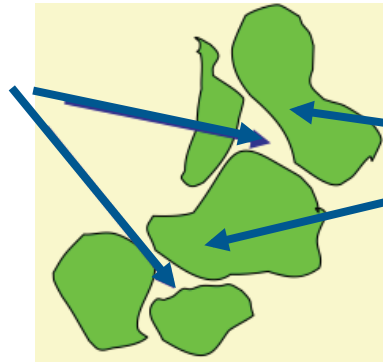


Kibble-Zurek scenario

Kibble: Spontaneous symmetry breaking described by non-trivial homotopy group yields topologically-protected defects

Zurek:

defects form when
they meet



isolated low-symmetry
regions fluctuate

How many defects depends on time spent at the transition temperature

Cool slowly: Different regions can communicate their choice of phase

→ **Large regions of the same choice**

→ **Low density of defects**

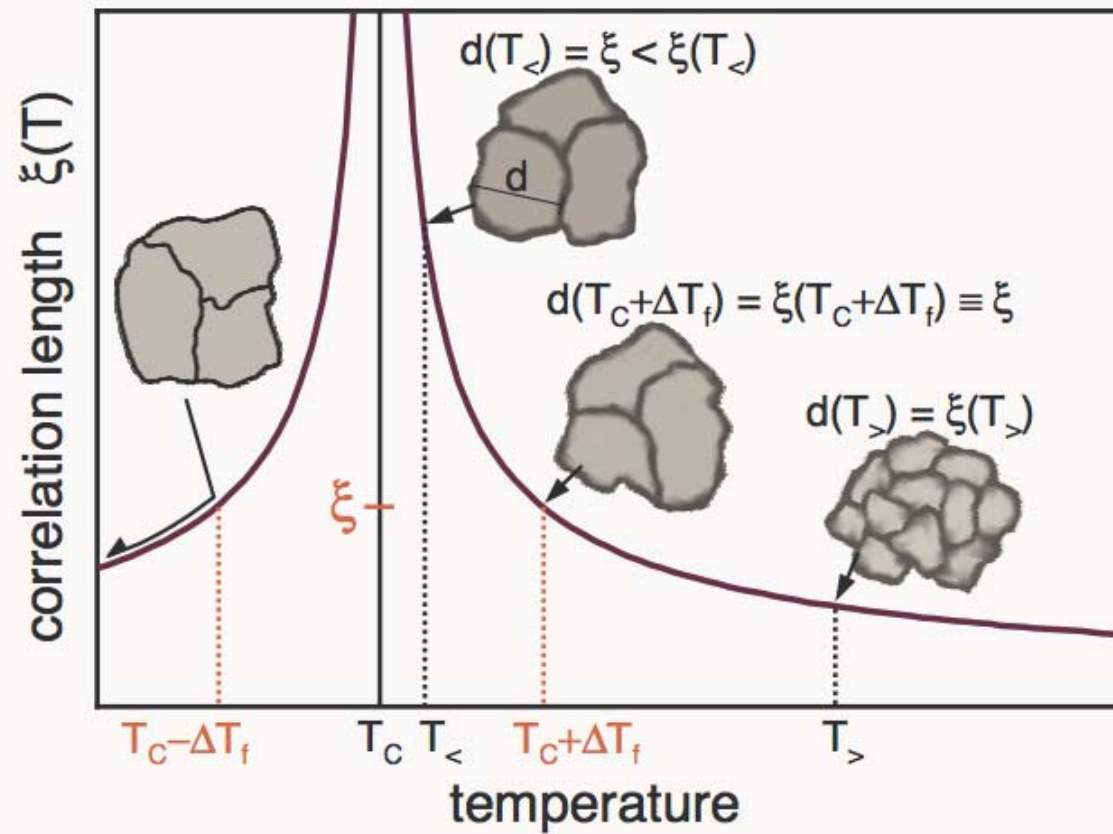
Cool quickly: Not much time to communicate choice of phase

→ **Many smaller regions with different choice of phase**

→ **High density of defects**



A bit more rigorously



Quantitatively

domain size,

defined as T_c (1400K) / cooling rate

$$d = \xi_0 \left(\frac{\tau_q}{\tau_0} \right)^{\frac{\nu}{1+\mu}}$$

Critical exponents: $\nu = 0.6717$

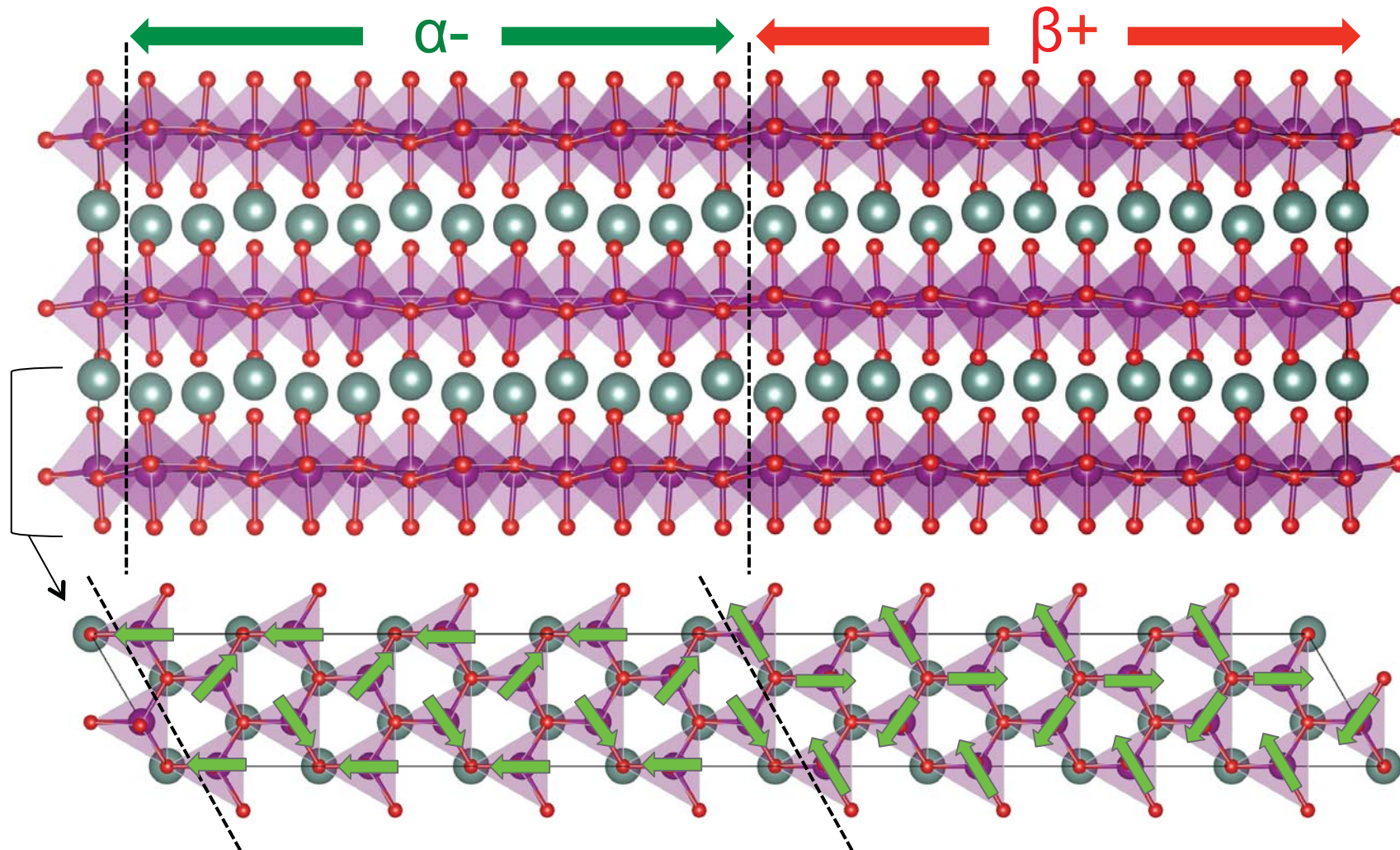
$\mu = 1.3132$

from MC simulations for 3D XY model

M. Campostrini et al., Phys.
Rev. B **74**, 144506 (2006)

zero-temperature correlation length
~ domain wall width in ferroelectrics
(DFT)

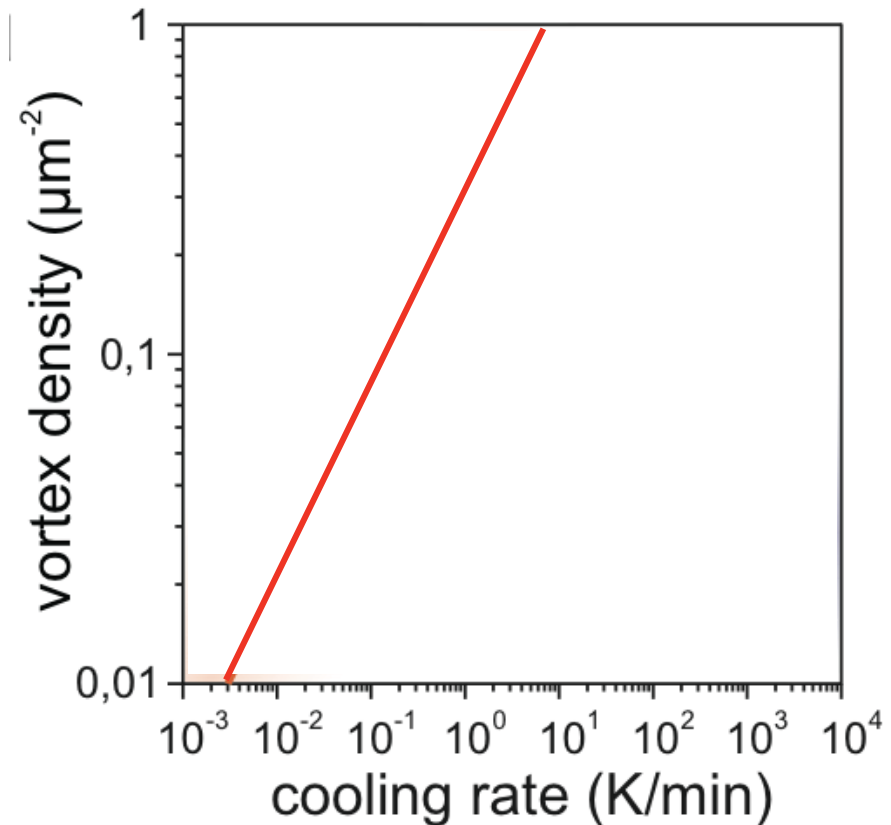
zero-temperature relaxation time
= ξ_0 / speed of sound
speed of sound = 640 m/s (DFT)

DFT calculations of domain walls in YMnO_3 

Domain wall width effectively zero!

Comparison of KZ theory (DFT parameters) with experiment

Red line: our calculations
with $\xi_0 = 0.06 \text{ A}$



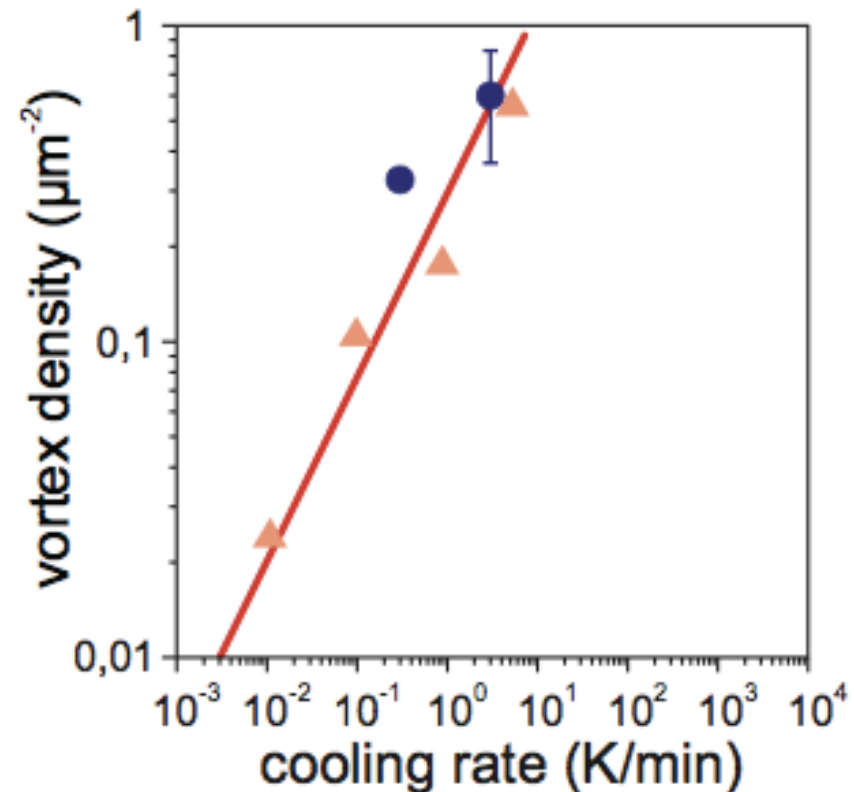
Comparison of KZ theory (DFT parameters) with experiment

Red line: our calculations
with $\xi_0 = 0.06 \text{ \AA}$

Red circles: measured by Chae et al.

Blue circles: measured by Fiebig et al.

REMARKABLE AGREEMENT!



S. C.. Chae et al., *Direct observation of the proliferation of ferroelectric loop domains and vortex-antivortex pairs*, PRL **108**, 167603 (2012)

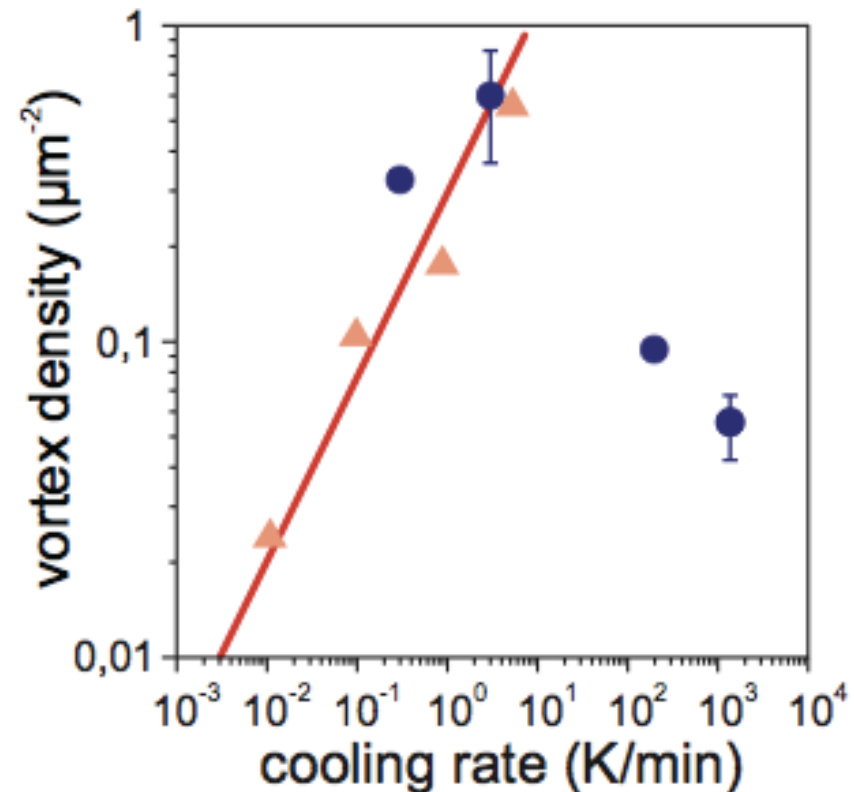
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Red circles: measured by Chae et al.

Blue circles: measured by Fiebig et al.

REMARKABLE AGREEMENT
AT SLOW COOLING RATES!



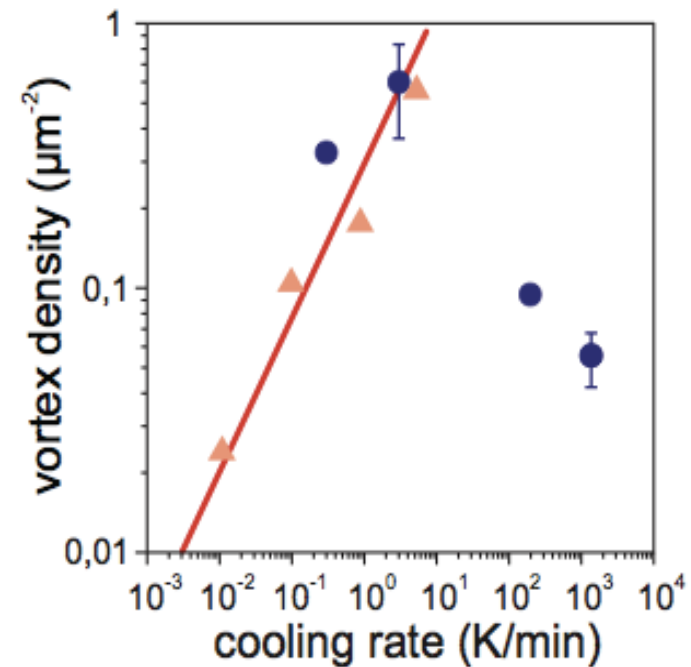
S. Griffin, M. Lilienblum, K. Delaney, Y. Kumagai, M. Fiebig and N. A. Spaldin, *Scaling behaviour and beyond equilibrium in the hexagonal manganites*, PRX **2**, 041022 (2012)

Open questions:

Are we now able to explore the “beyond-Kibble-Zurek” regime?

If so, what is the origin of the turnaround?

Or do we not have K-Z behavior at all?



S. Griffin, M. Lilienblum, K. Delaney, Y. Kumagai, M. Fiebig and N. A. Spaldin, *Scaling behaviour and beyond equilibrium in the hexagonal manganites*, PRX 2, 041022 (2012)

The Materials Theory group

Yu Kumagai



Sinead Griffin

The Multifunctional Ferroic Materials group

Manfred Fiebig and Martin Lilienblum

Kris Delaney, UC Santa Barbara



Summary

YMnO₃ displays rich physics beyond its multiferroism

Electronic structure calculations are helpful in unraveling some of this physics

YMnO₃ seems to provide the first example of Kibble-Zurek scaling in a condensed matter system

Use of condensed matter systems to explore questions in other areas of physics is a lot of fun

K. Rushchanskii, NAS et al., *A multiferroic material to search for the permanent electric dipole moment of the electron*, Nature Materials 9, 649 (2010)

Universe's Existence May Be Explained by New Material

2010-08-05 12:17

NATIONAL GEOGRAPHIC Daily News

Universe's Existence May Be Explained by New Material



A new material could help physicists explain the existence of matter, such as this astronaut seen above Earth.

Photograph courtesy NASA