

2458-13

Workshop on GNSS Data Application to Low Latitude Ionospheric Research

6 - 17 May 2013

**Satellite Navigation for Guidance of Aircraft
(Part 2)**

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Satellite Navigation for Guidance of Aircraft

The seal of Stanford University is a circular emblem. It features a central green tree with a brown trunk and roots, set against a light blue background. The tree is surrounded by a landscape of rolling hills in shades of brown and tan. The entire scene is enclosed within a red circular border with a diamond-shaped pattern. The text "LEND STANFORD JUNIOR UNIVERSITY" is written in red along the top inner edge of the border. The German motto "DIE LIT DER FREIHEIT" is written in white along the top inner edge. The year "1891" is written in red at the bottom center of the seal.

Todd Walter
Stanford University

<http://waas.stanford.edu>



Outline

- ➔ **Ionospheric Modeling**
- ➔ Ionospheric Threats
- ➔ Next Generation Satellite Navigation
- ➔ Future Signals
- ➔ Conclusions



How Are Measurements Correlated Over Distance?

- Translate Our Measurements of the Ionosphere Into User Corrections
- How Does the Ionosphere Behave Spatially?
 - *What is the underlying structure?*
 - *What does one measurement tell us about the nearby ionosphere?*
 - *How should we combine multiple samples?*
 - *What confidence can we have in our prediction?*
- We Need to Determine the Ionospheric Decorrelation Function



“Supertruth” Data

- Raw Data Collected From Each WRS
 - *3 independent receivers per WRS*
- Postprocessed to Create “Supertruth”
 - *Carrier tracks “leveled” to reduce multipath*
 - *Interfrequency biases estimated and removed for satellites and receivers*
 - *Comparisons made between co-located receivers (voting to remove artifacts)*
- Multipath and Bias Residuals are ~50 cm
- Without Voting, Receiver Artifacts Cloud Results and Make It Impossible to See Tails of the Distribution



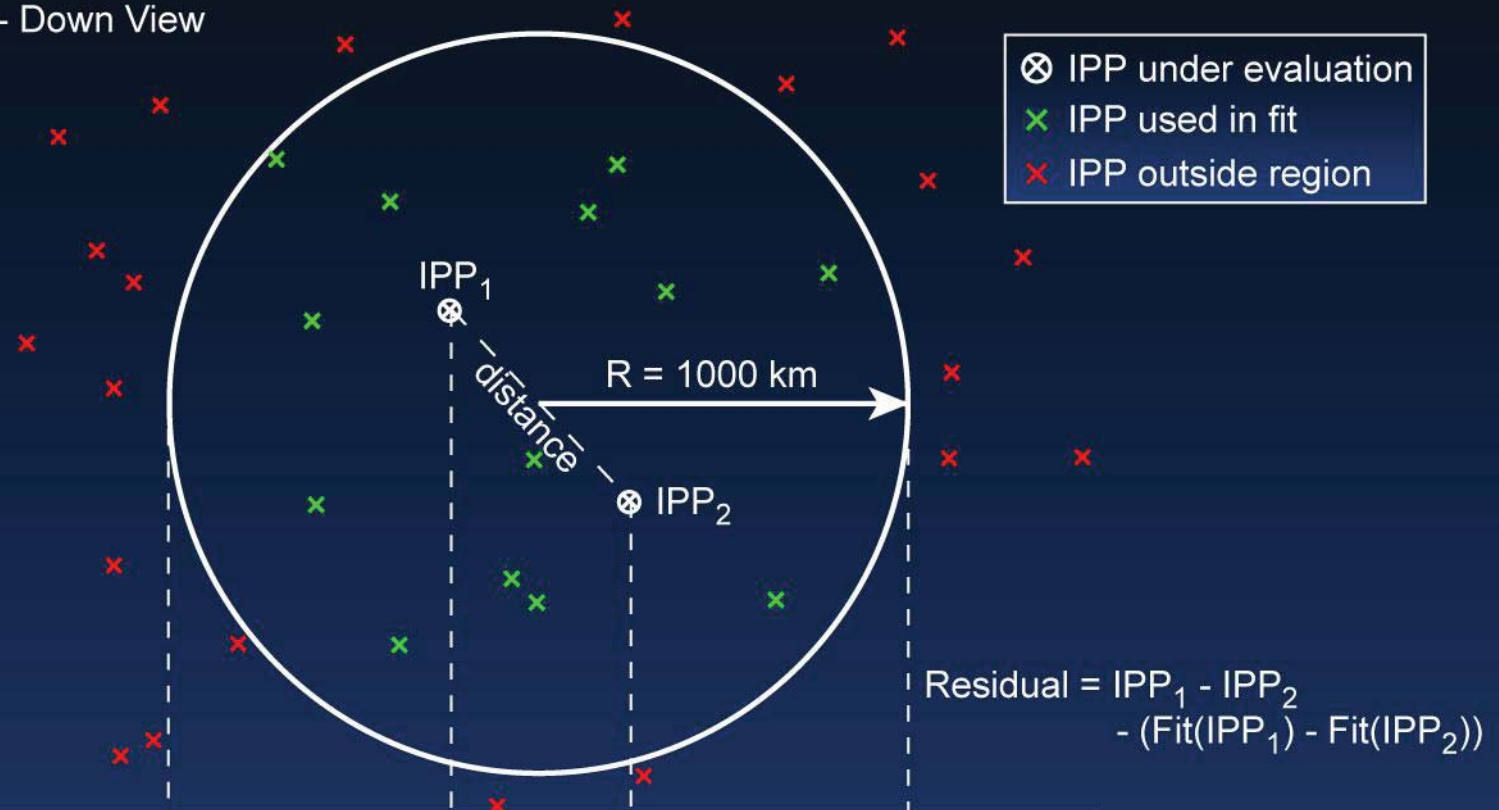
Decorrelation Estimation

- Every Supertruth IPP Is Compared to All Others
- The Great Circle Distance Between the IPPs Is Calculated
- The Difference in Vertical Ionosphere Is Calculated
- A Two-dimensional Histogram Is Formed: Each Bin Corresponds to a Distance Range and a Vertical Difference Range
- Histogram Contains the Counts for Each Time an IPP Pair Fell in a Particular Bin



Correlation Estimation Process

Top - Down View



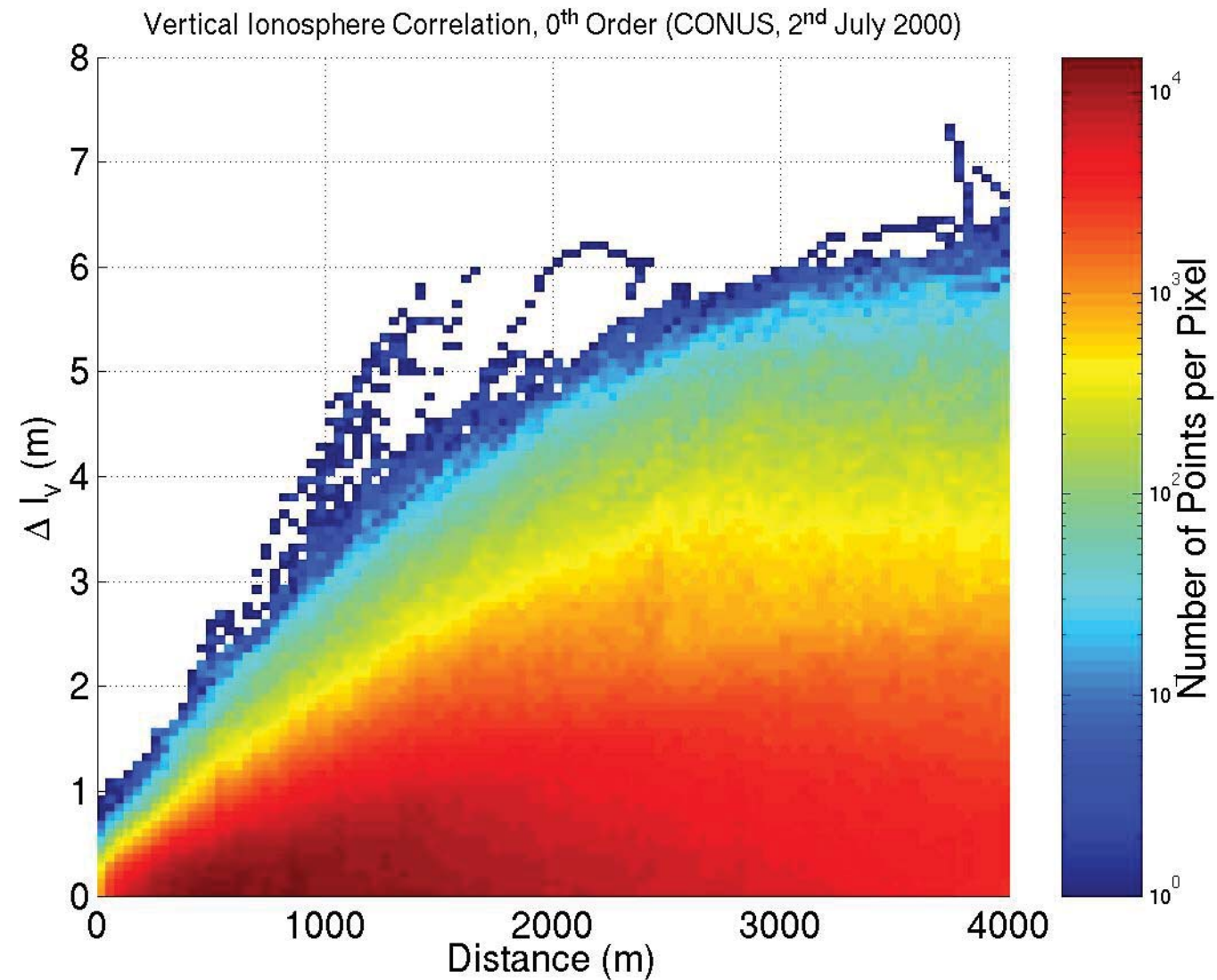
Side View



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Ionospheric Decorrelation (0th Order)

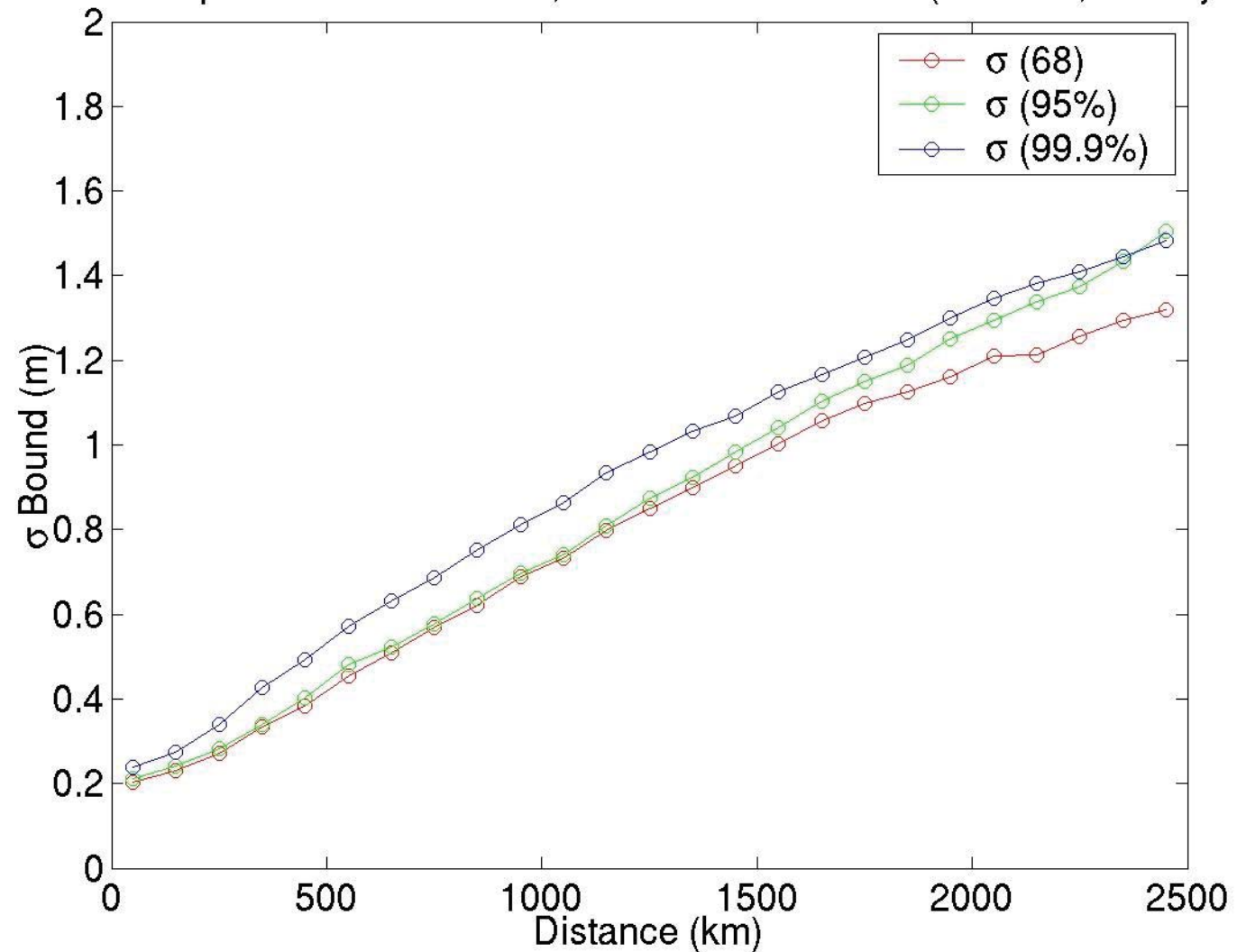


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Ionospheric Decorrelation Function (0th Order)

Vertical Ionosphere Containment σ , 0th Order Correlation (CONUS, 2nd July 2000)



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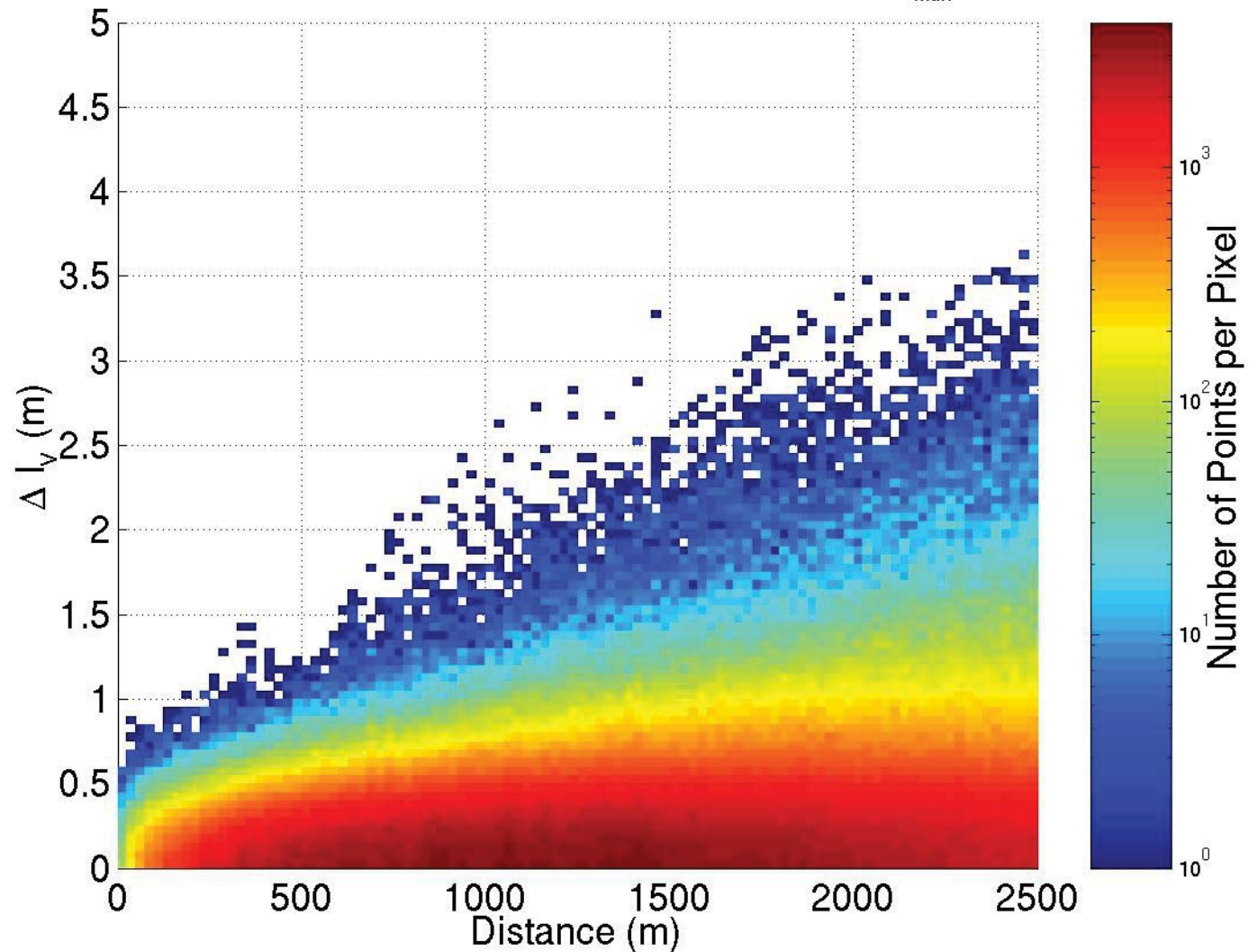
Preliminary Decorrelation Findings

- Nominal Ionosphere is Relatively Smooth
 - *Nearby IPPs Well Correlated*
- Confidence About a Single Measurement Can Be Described As:
$$\sigma^2 = \sigma_m^2 + (0.3 m + d*0.5 m/1000km)^2$$
- There Appears to Be a Deterministic Component
- Next Try Removing a Planar Fit



Ionospheric Decorrelation About a Planar Fit (1st Order)

Vertical Ionosphere Correlation, 1st Order (CONUS, 2nd July 2000, $R_{\max} = 1500\text{km}$)

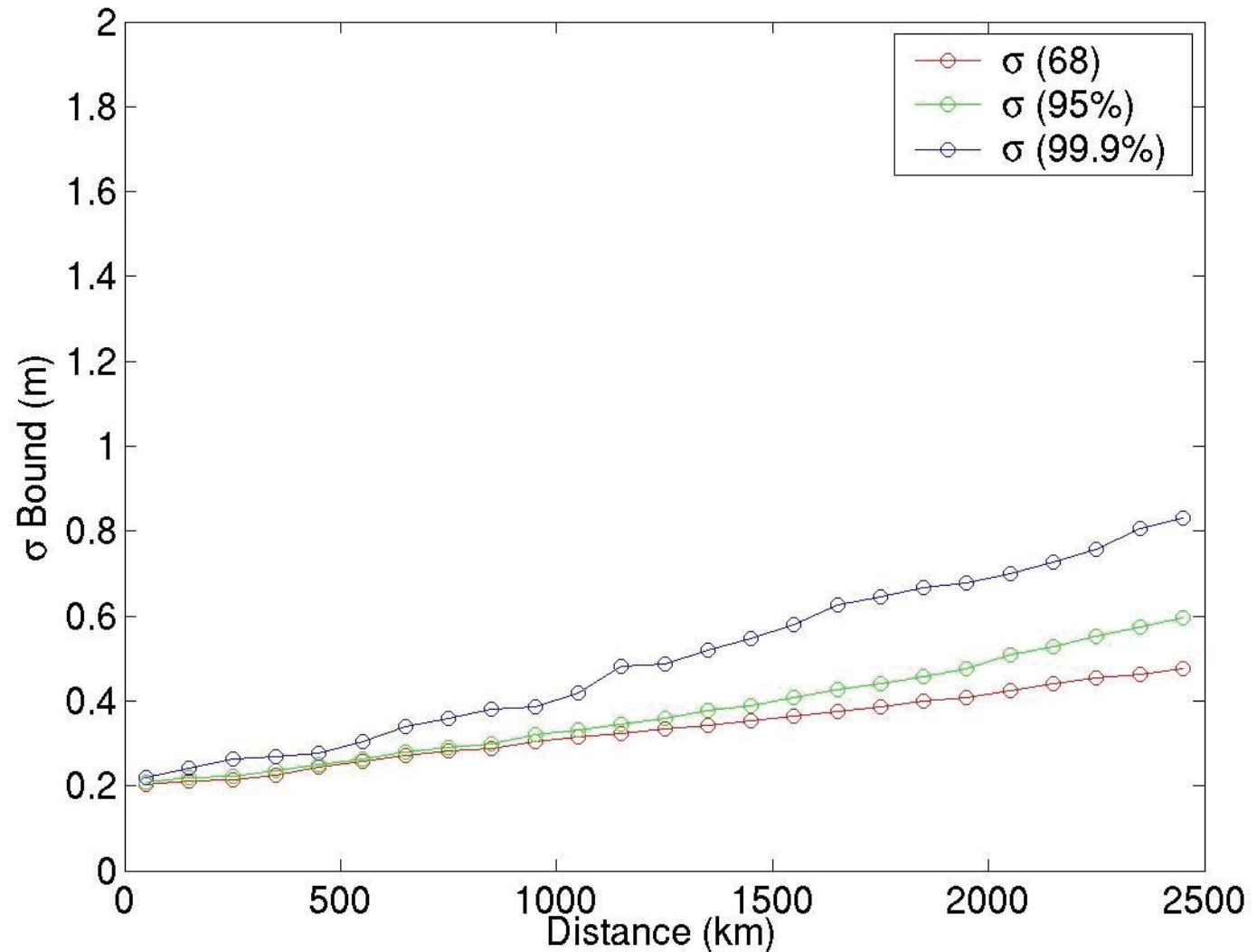


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Ionospheric Decorrelation Function (1st Order)

Vertical Ionosphere Containment σ , 1st Order Correlation (CONUS, 2nd July 2000)

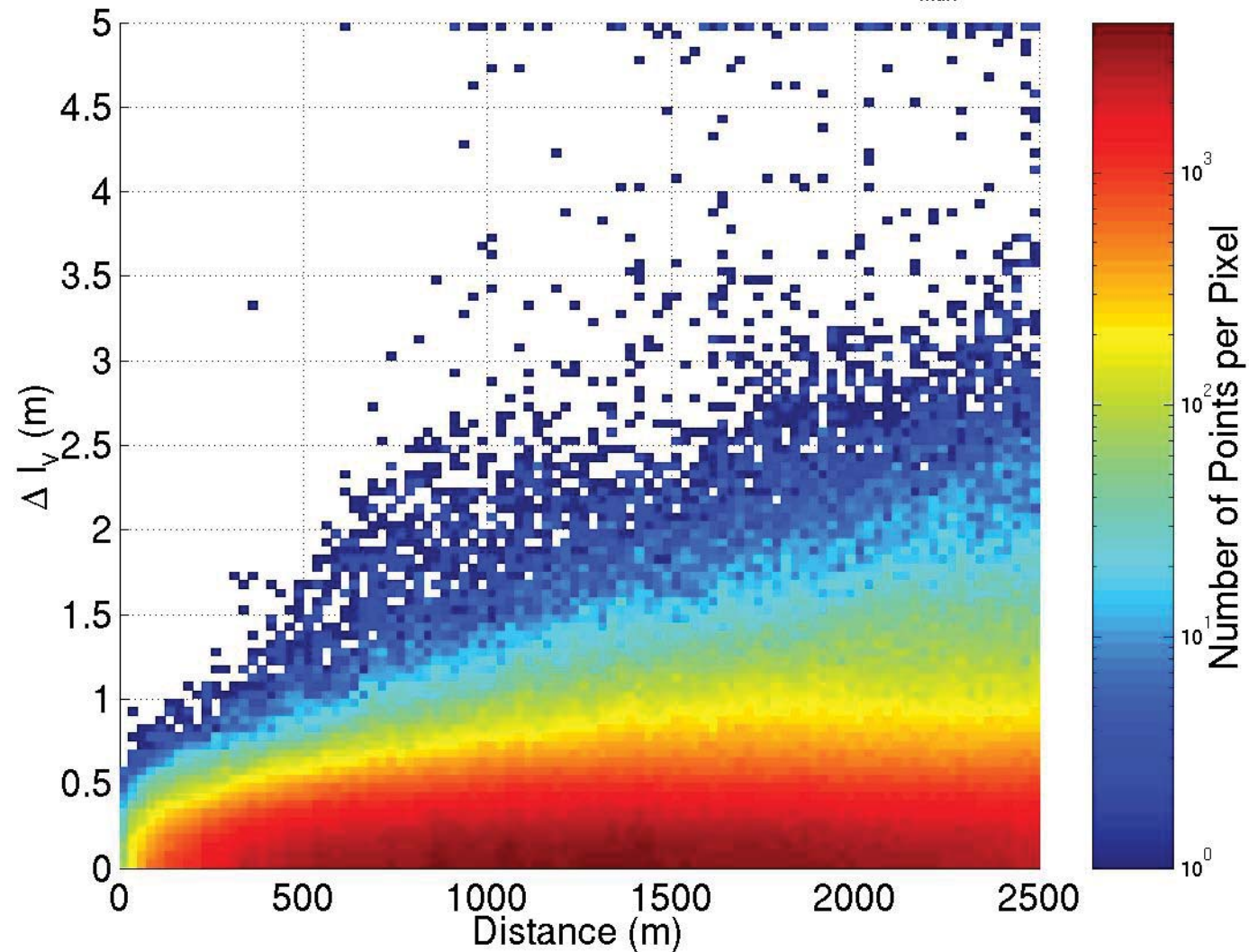


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Ionospheric Decorrelation About a Quadratic Fit

Vertical Ionosphere Correlation, 2nd Order (CONUS, 2nd July 2000, $R_{\max} = 1500\text{km}$)

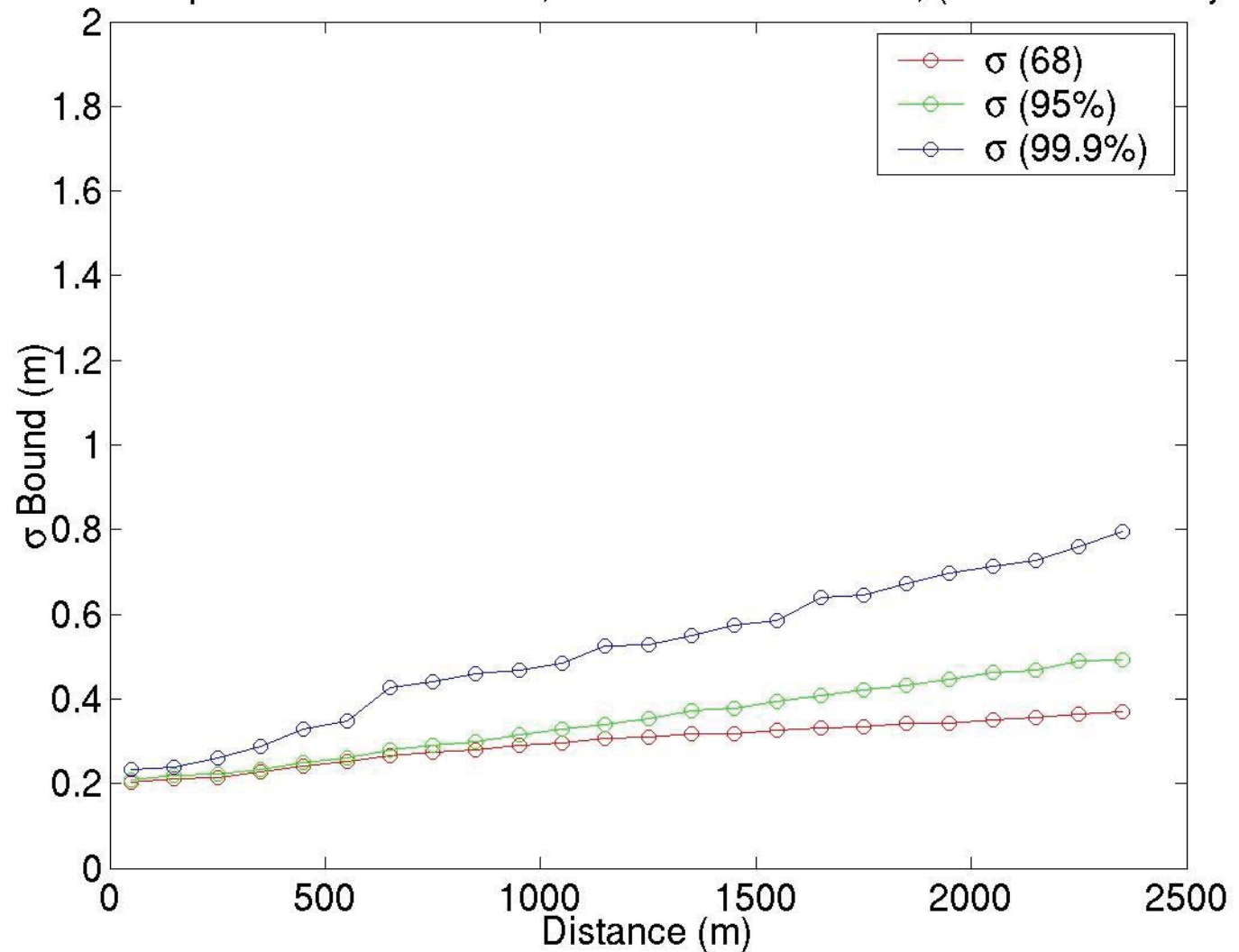


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Ionospheric Decorrelation Function (2nd Order)

Vertical Ionosphere Containment σ , 2nd Order Correlation, (CONUS 2nd July 2000)



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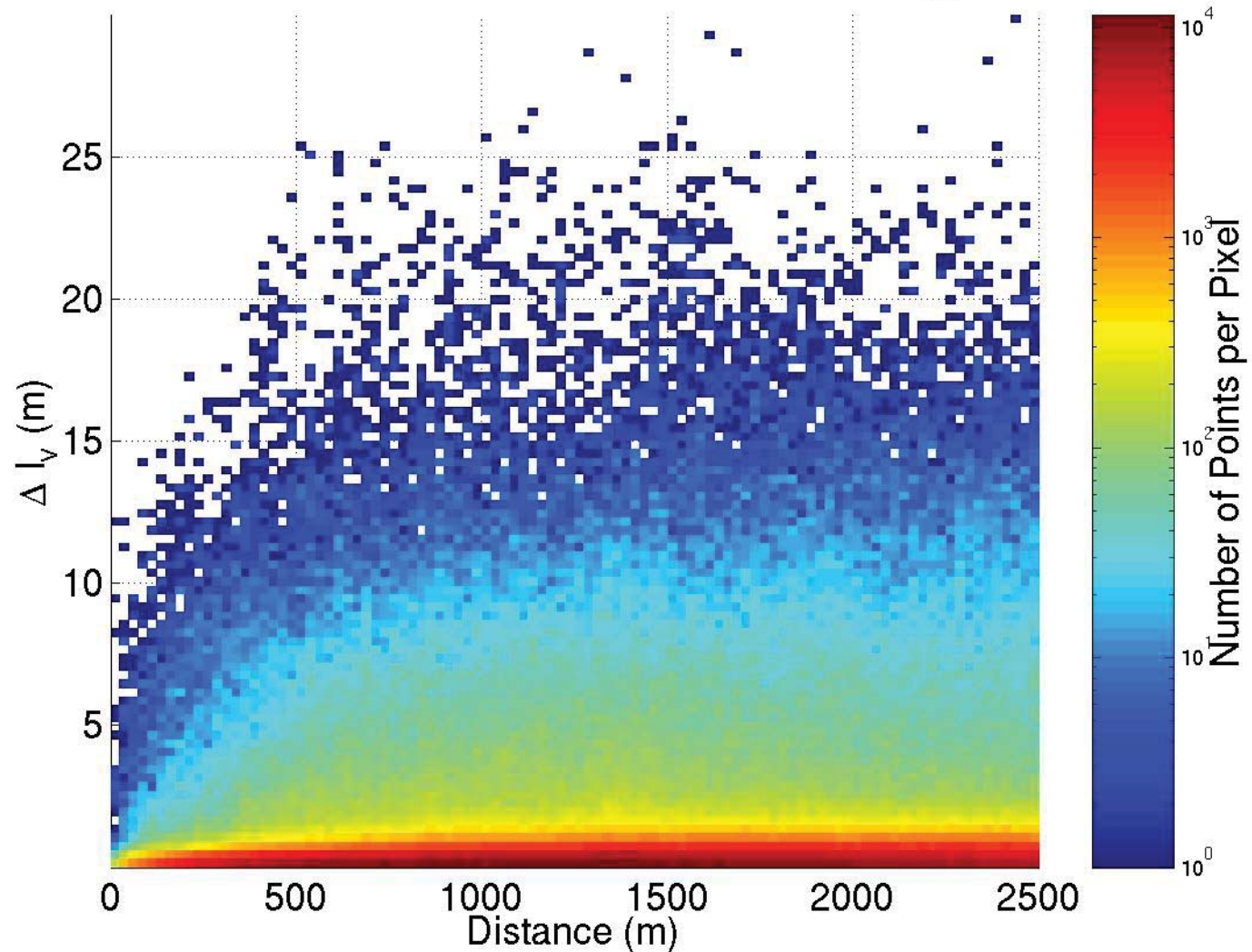
Initial Decorrelation Summary

- Planar Fit Appears to Remove Nearly All Deterministic Elements
- No Decorrelation Variation With Elevation Angle or vs Day/Night
 - *Decorrelation appears to result from residual error in supertruth data*
- 35 cm Valid for Mid-Latitude Nominal Decorrelation ($R < \sim 1000$ km)
- Decorrelation at Lower Latitudes Is Likely Different (larger, more orders?)



Disturbed Ionosphere

Vertical Ionosphere Correlation, 1st Order (CONUS, 15th July 2000, $R_{\max} = 1500\text{km}$)

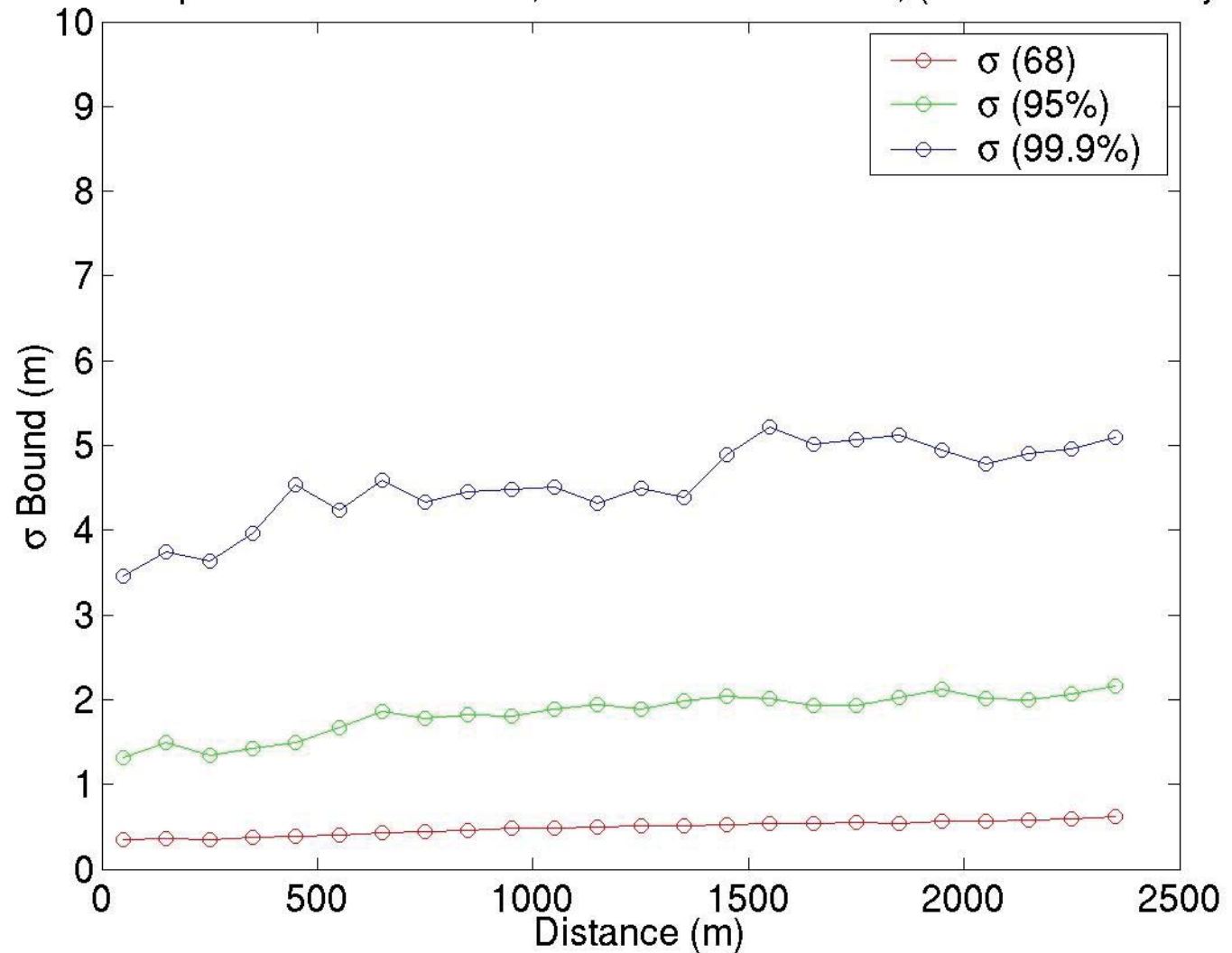


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Disturbed Ionosphere

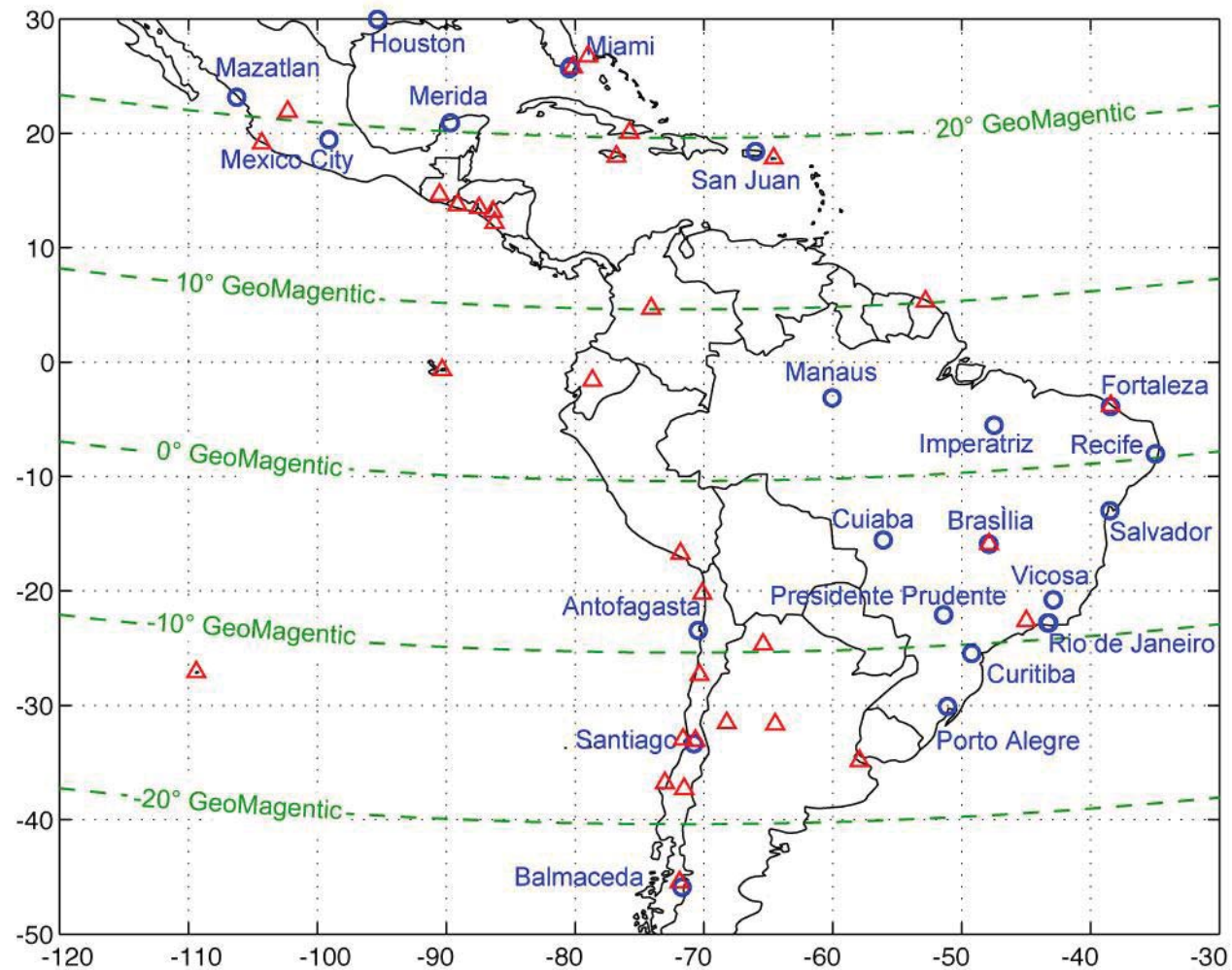
Vertical Ionosphere Containment σ , 1st Order Correlation, (CONUS 15th July 2000)



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Map of South American Stations



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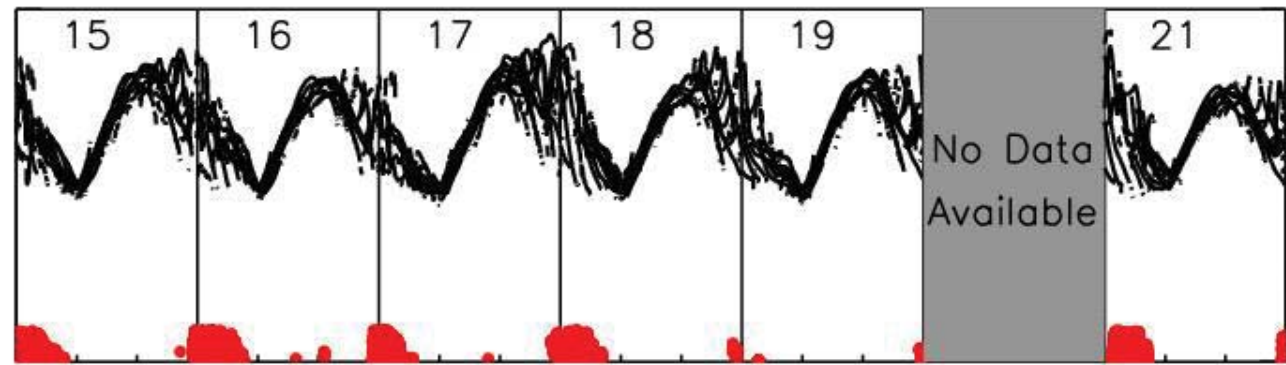
Determination of Quiet Days

- First wish to identify “undisturbed” days to use as basis for “nominal” model
 - *Want a day free of depletions and scintillation*

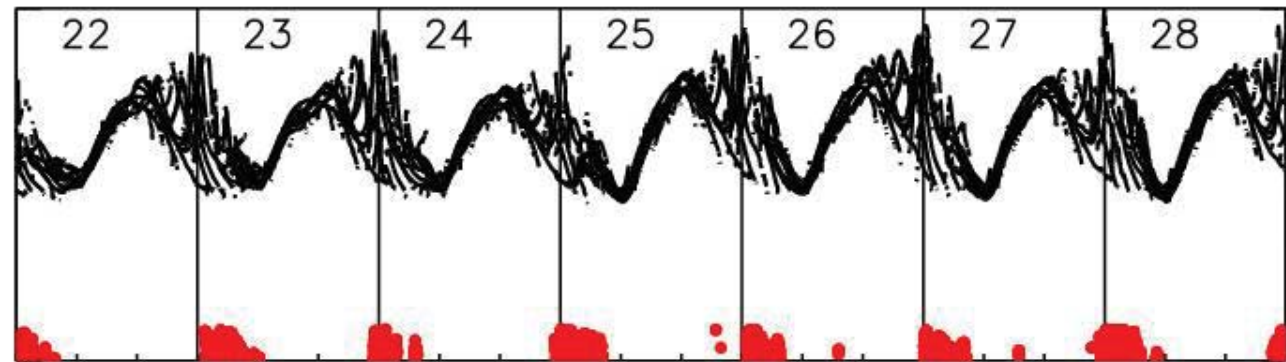


Daily Observations of TEC and S4

S4, Range Delay (m)



S4, Range Delay (m)

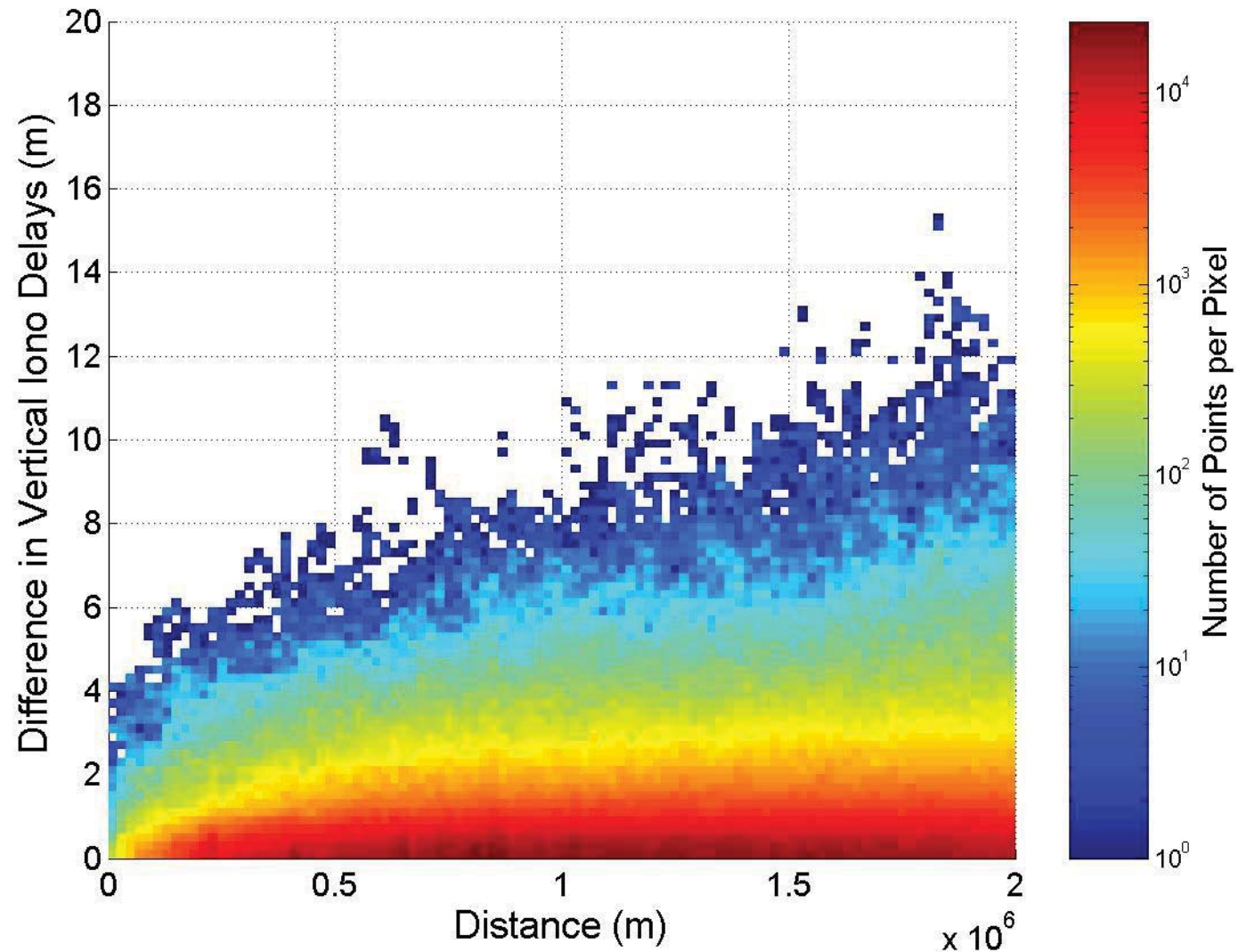


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Two-D Histogram 1st Order

Residues of Planar Fit, $R_{\max} = 1000$ km, JPL Processed, 19th Feb 2002

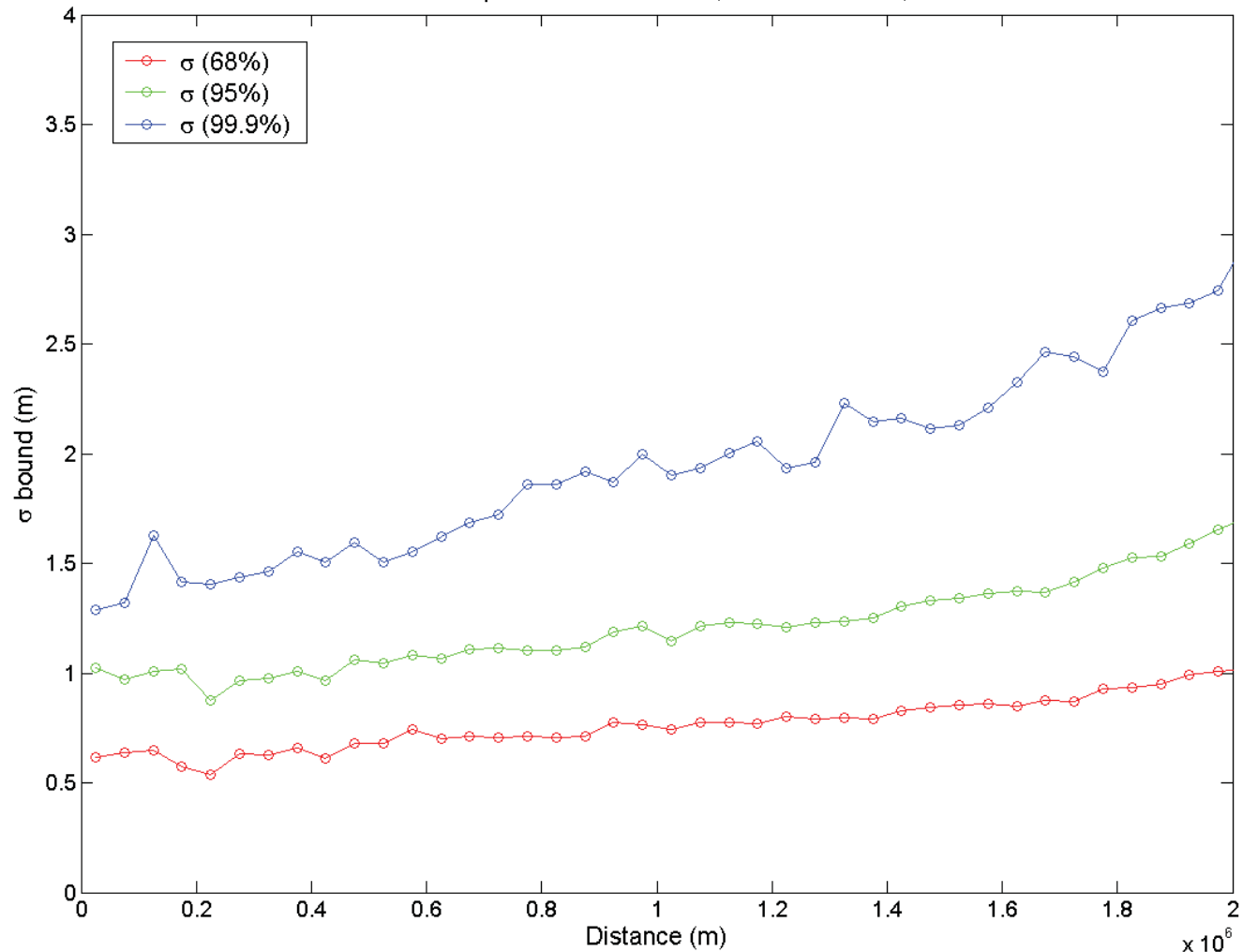


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Sigma Estimate 1st Order

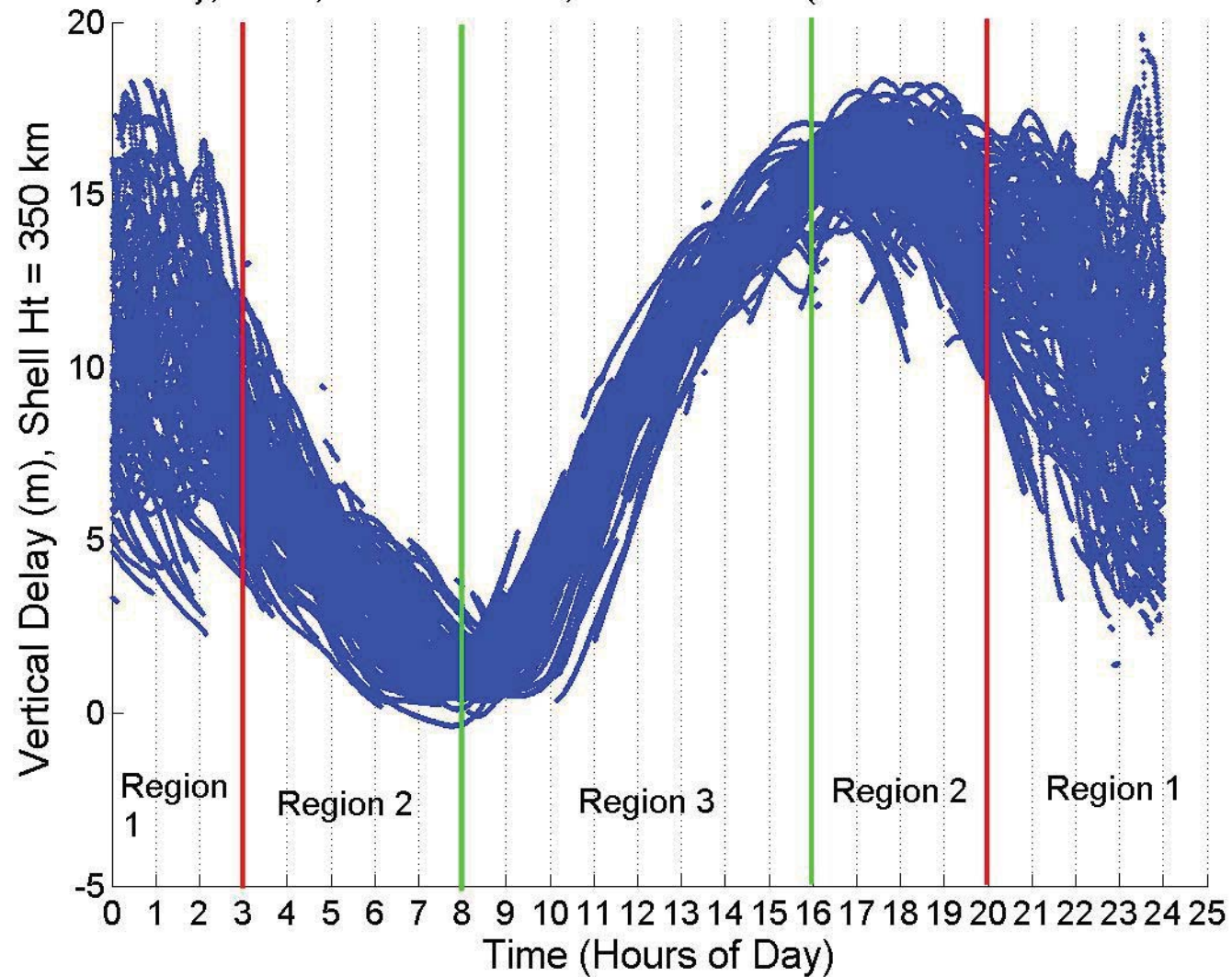
Planar Residual Ionosphere Containment σ , JPL Processed, 19th Feb 2002





Vertical TEC

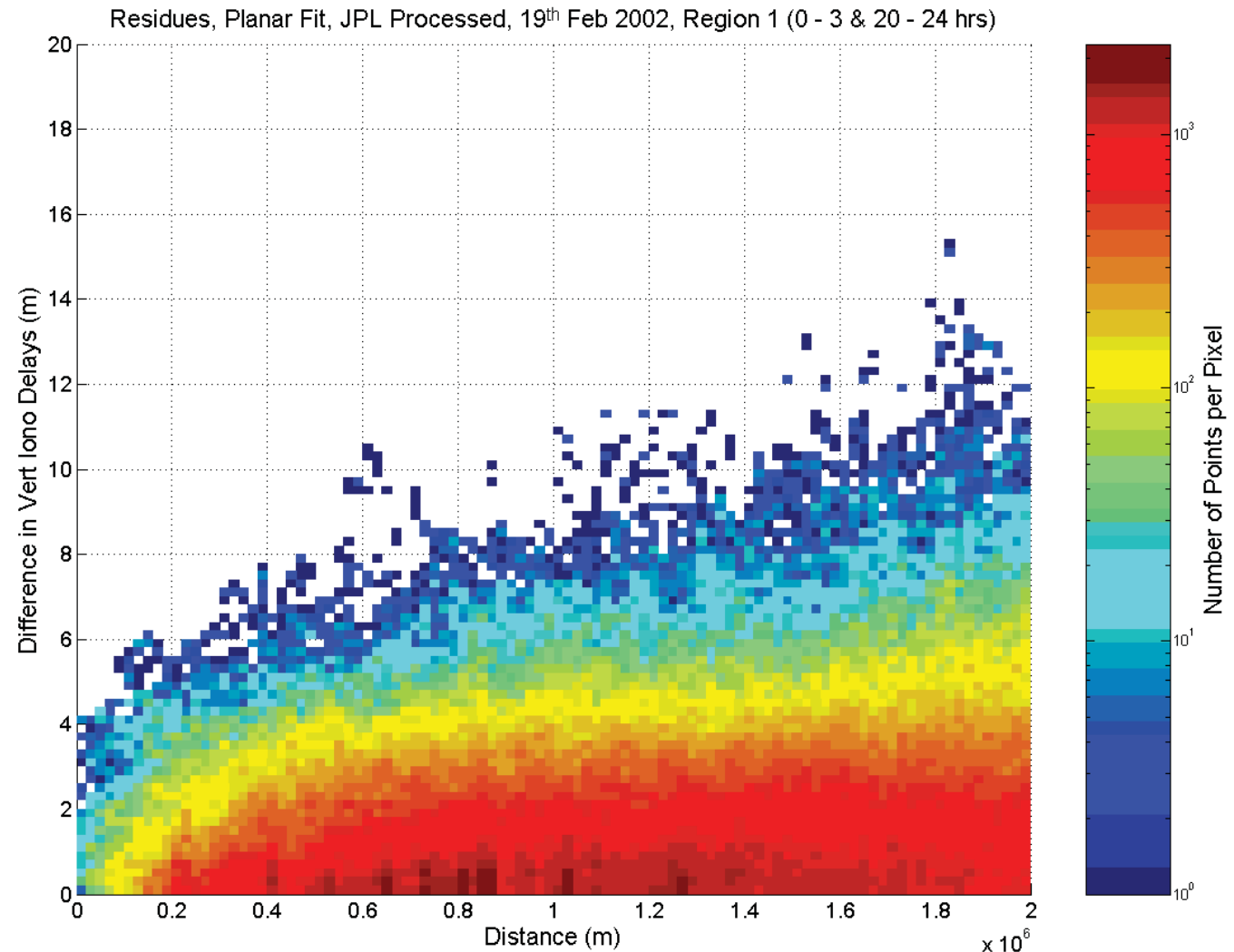
Vertical Delay, Brazil, JPL Processed, 19th Feb 2002 (UTC Start time = 698112000sec)



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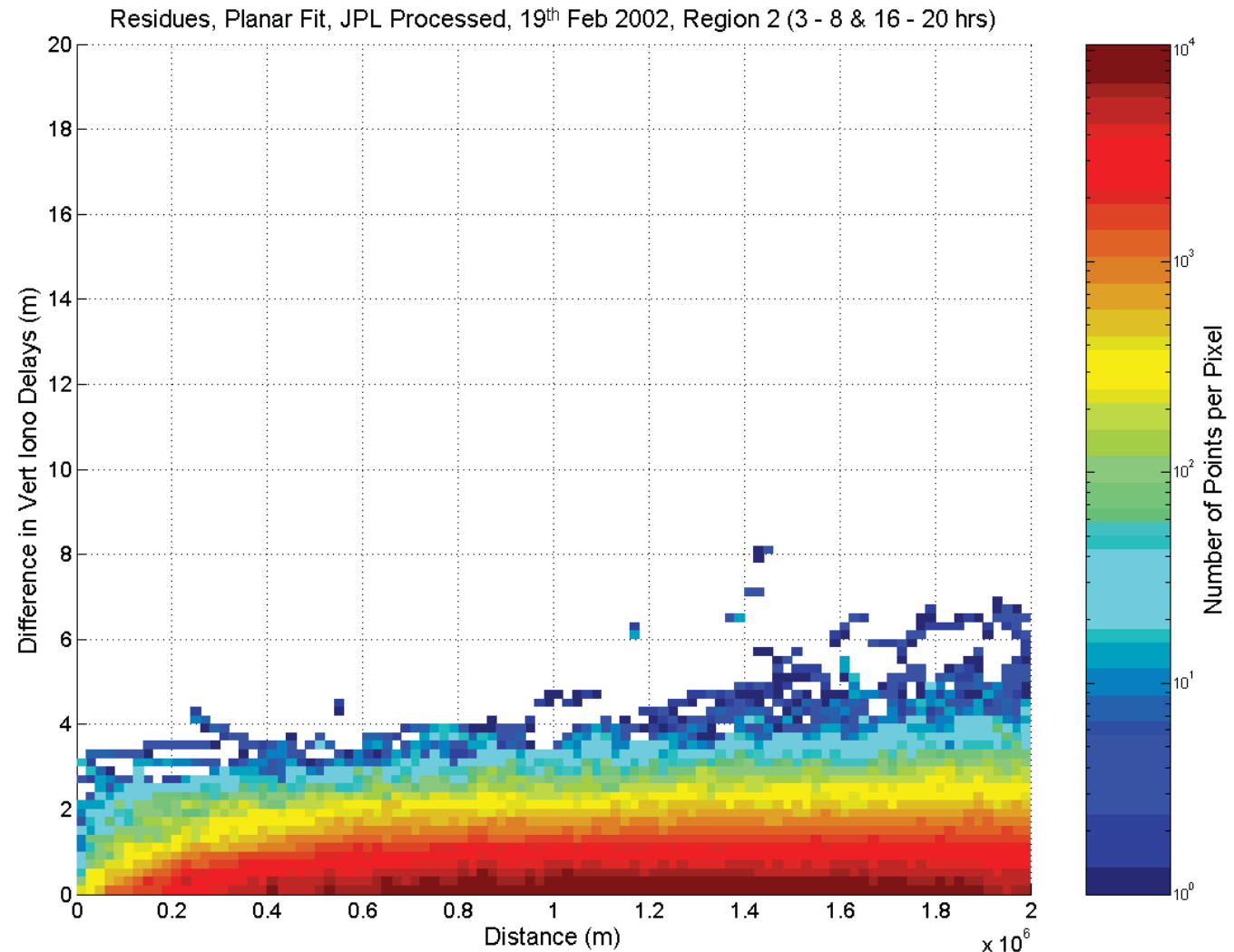
Two-D Histogram 1st Order (Region 1)



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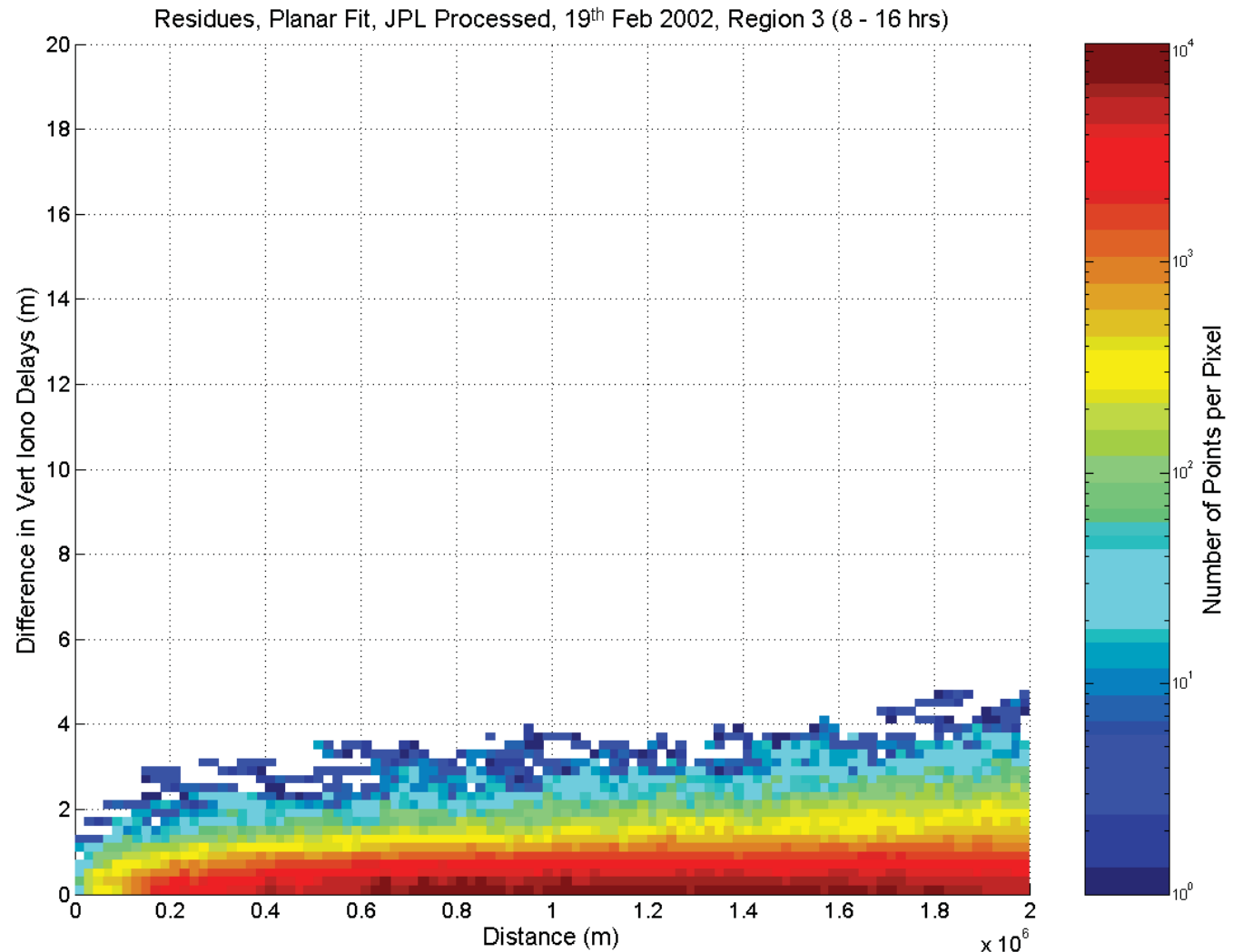
Two-D Histogram 1st Order (Region 2)



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Two-D Histogram 1st Order (Region 3)

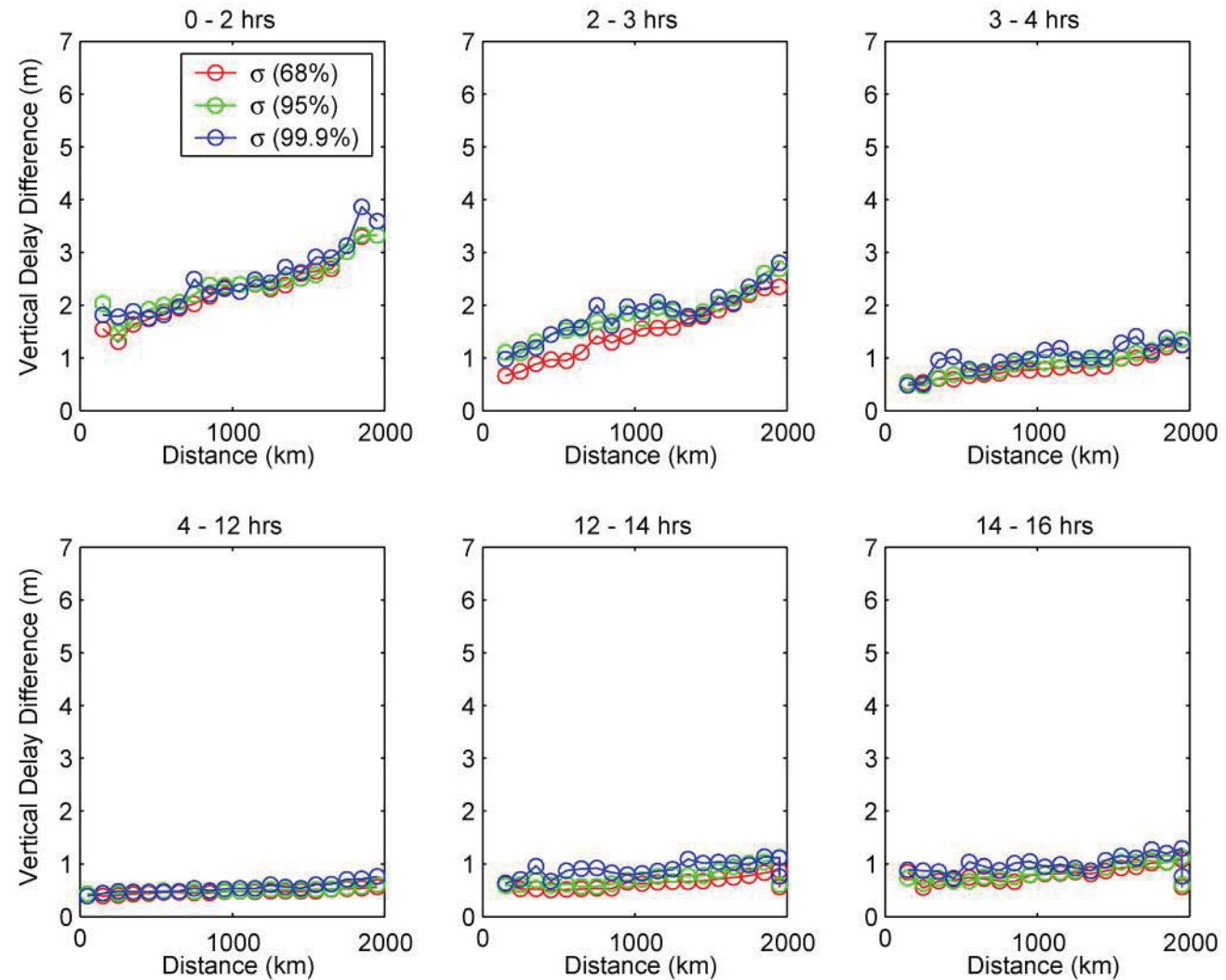


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Sigma Estimate 1st Order (Sliced by Time)

Planar Fit 19th Feb 2002

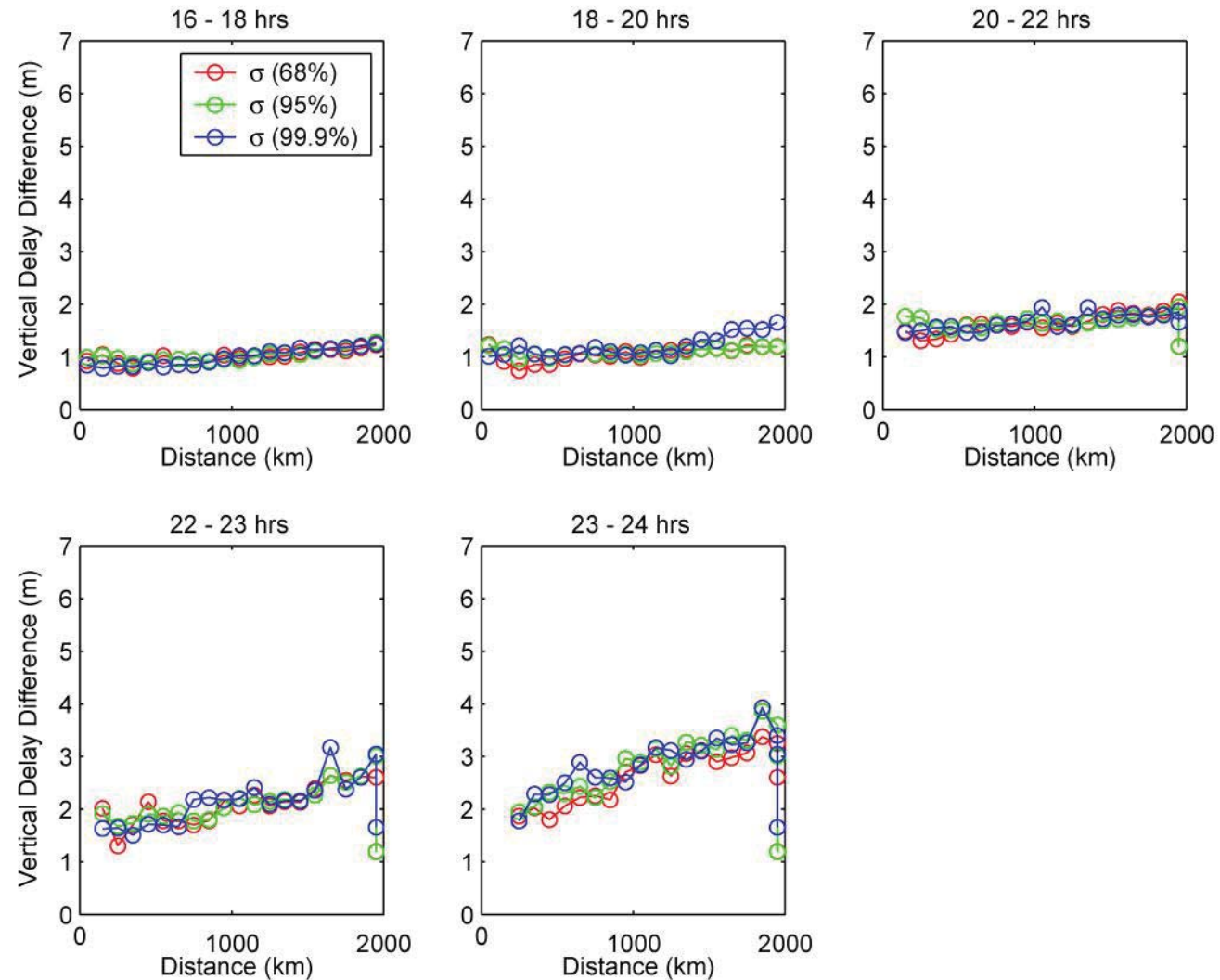


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Sigma Estimate 1st Order (Sliced by Time)

Planar Fit 19th Feb 2002



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Correlation Observations

- Clear temporal dependencies in the variogram (σ_{decorr} term)
 - *Evening into nighttime is worst*
 - *Daytime more easily modeled*
- Clear spatial trends in the data
 - *1st and 2nd order model the trend about equally well, both better than 0th order*
- Random Component significantly larger than mid-latitude
 - *Gaussian over short times*



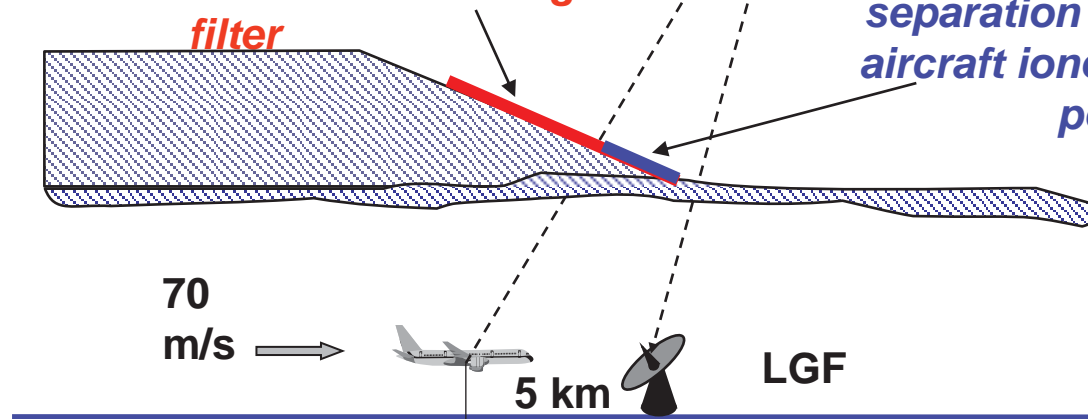
Contributors to Differential Ionosphere Error

Simplified Ionosphere Wave Front Model:
a ramp defined by constant **slope** and **width**

Error due to code-carrier divergence experienced by 100-second aircraft carrier-smoothing filter

GPS Satellite

Error due to physical separation of ground and aircraft ionosphere pierce points



$$\text{Diff. Iono Range Error} = \text{gradient slope} \times \min\{ (x + 2 \tau v_{air}), \text{gradient width} \}$$

For 5 km ground-to-air separation at CAT I DH: $x = 5 \text{ km}$; $\tau = 100 \text{ sec}$; $v_{air} = 70 \text{ m/s}$

$$\Rightarrow \text{"virtual baseline" at DH} = x + 2 \tau v_{air} = 5 + 14 = 19$$

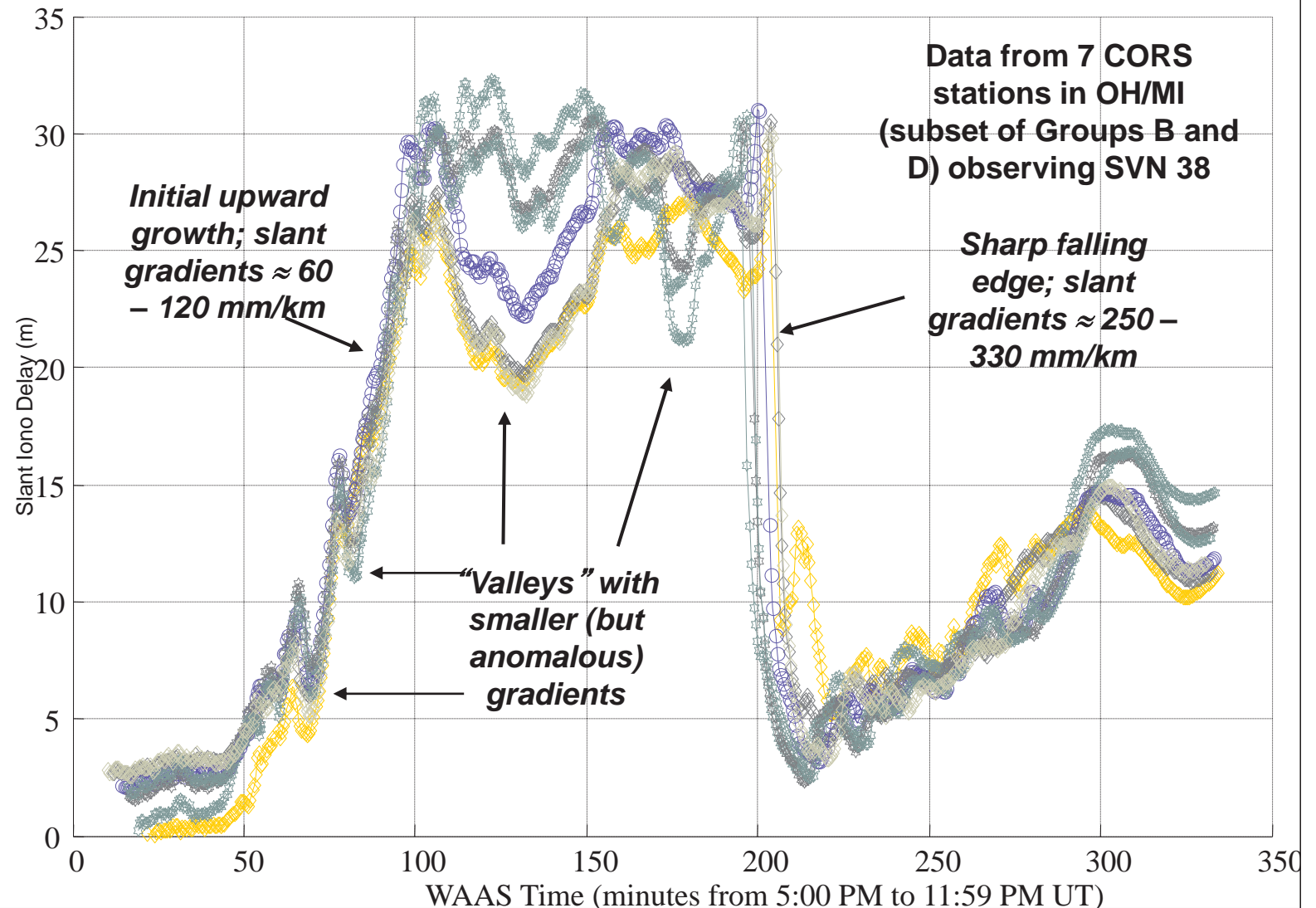
Courtesy:
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Ionosphere Delay Gradients

20 Nov. 2003



Courtesy:
Sam Pullen

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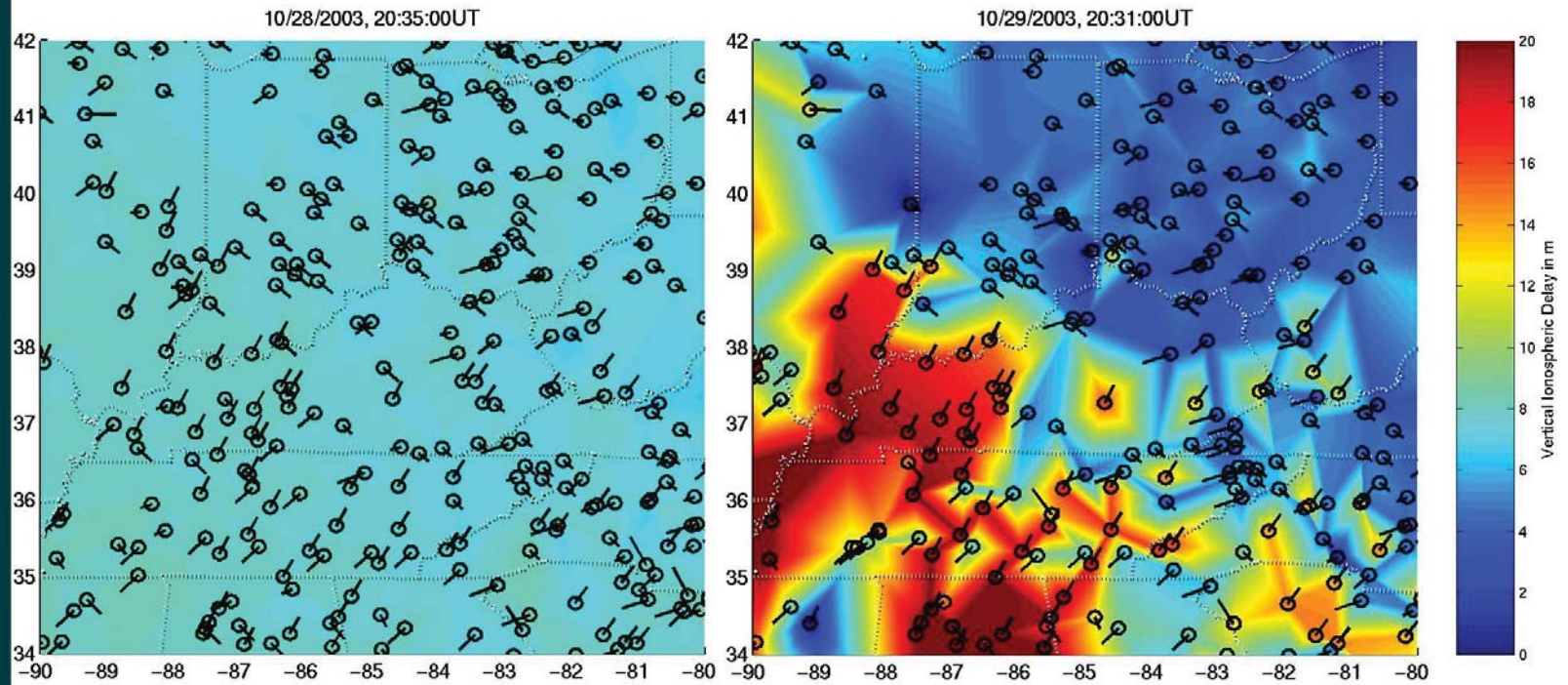


SBAS Ionospheric Threats

- WAAS Was Commissioned on 10 July 2003
 - *Availability > 99% for first 3 months*
- October 29-31 Two Large Disturbances Each Cause the Storm Detectors to Trip for Hours
 - *Protection factor set to ~15 m 1-sigma*
- November 20-21 Another Large Disturbance Limits Vertical Guidance for Several Hours



Failure of Thin Shell Model



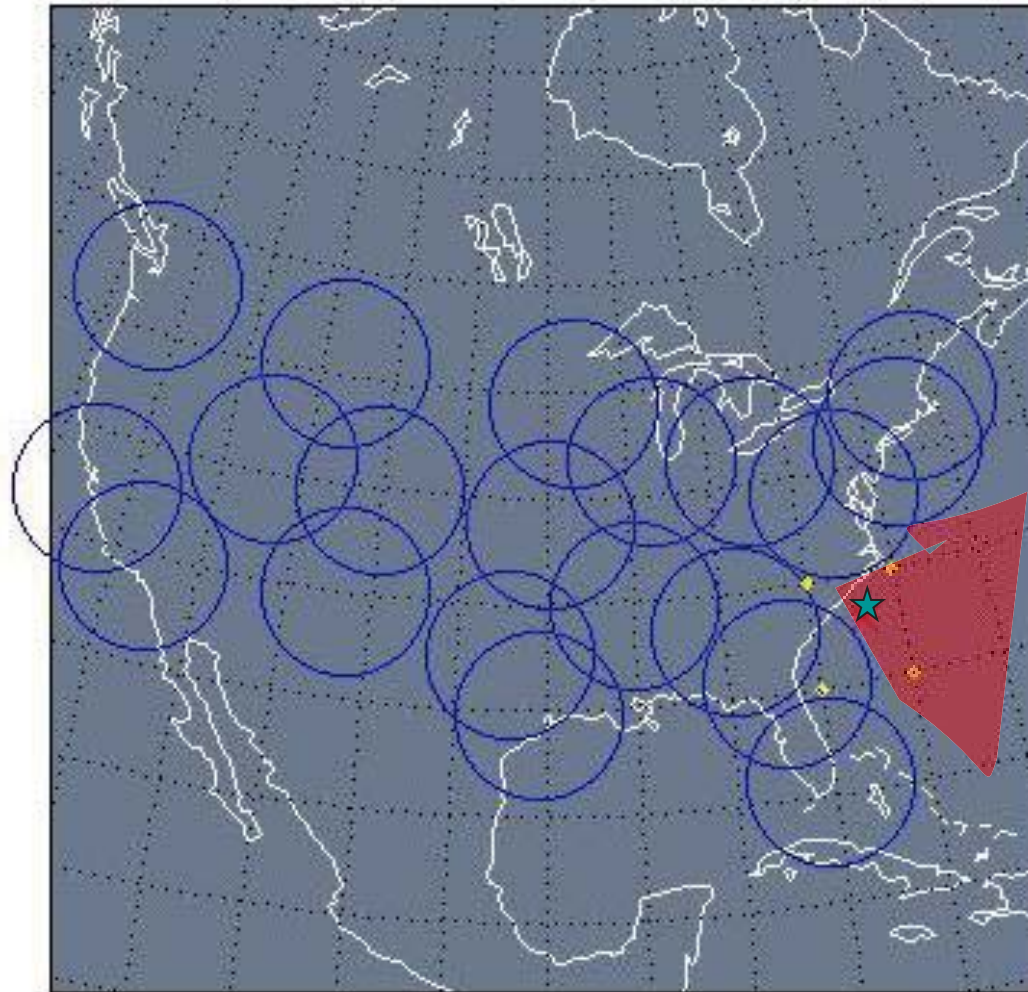
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Quiet Day

Disturbed Day



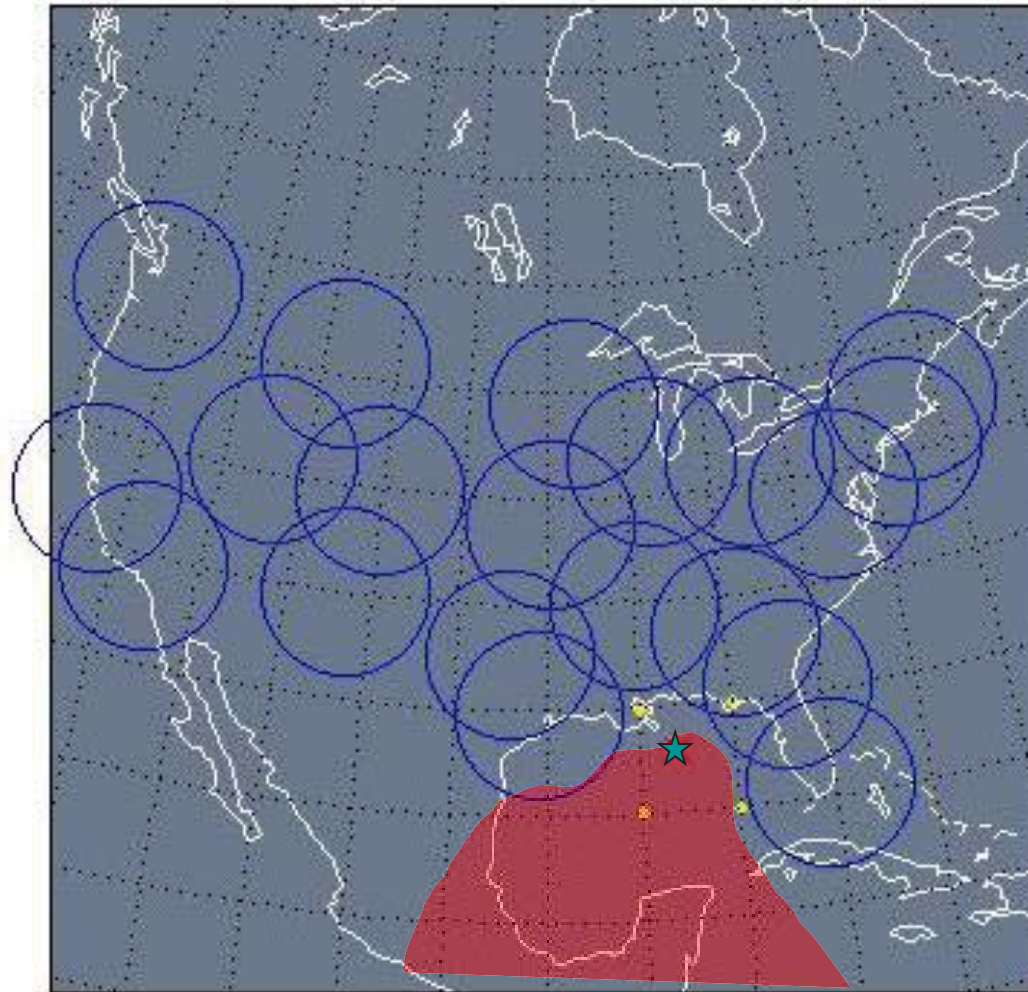
Threats at the Edge of Coverage



Courtesy:
Seebany
Datta-Barua



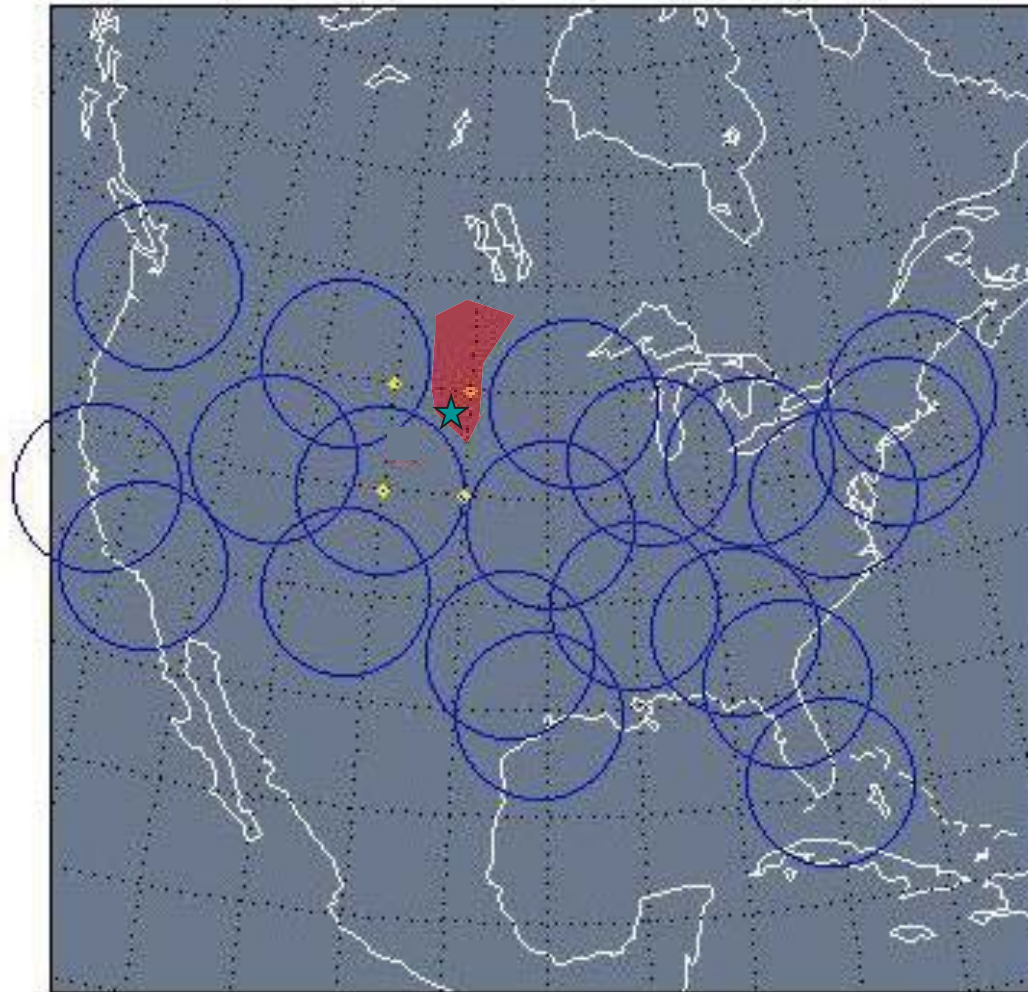
Edge of Coverage 2



Courtesy:
Seebany
Datta-Barua



Undersampling Within CONUS



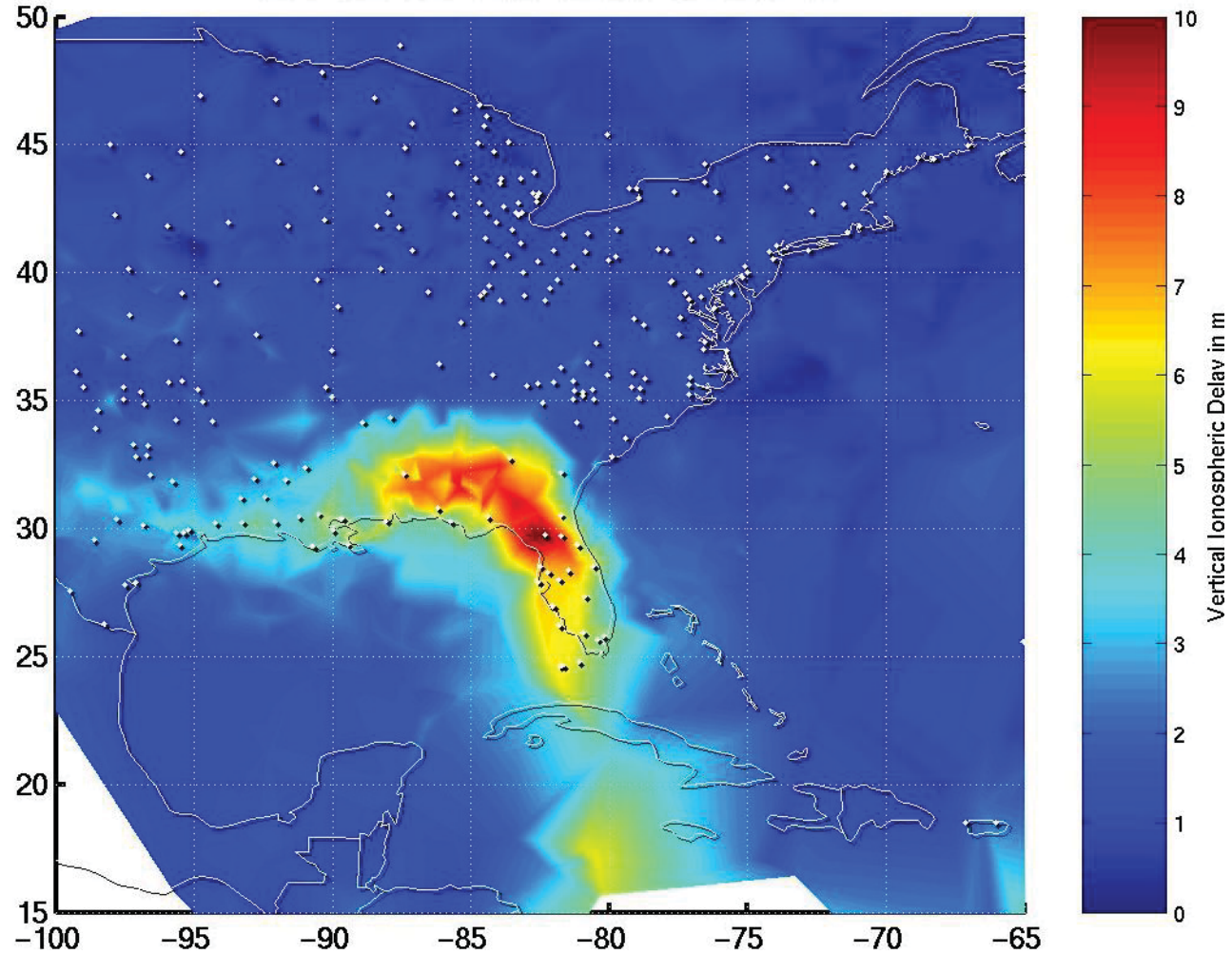
Courtesy:
Seebany
Datta-Barua



Small-scale Irregularity



10/31/2003, 05:00:00UT, CORS 400 Stations



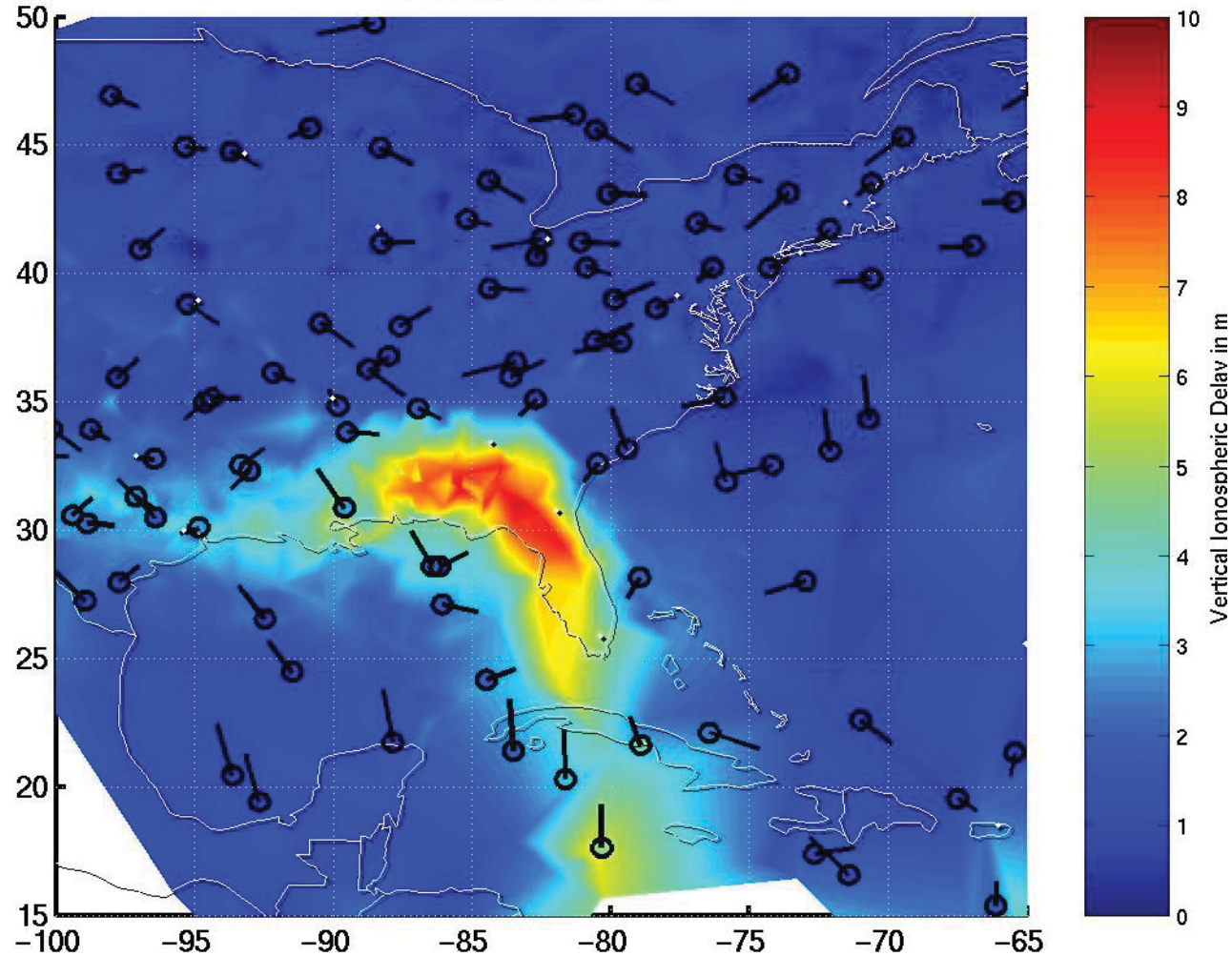
Courtesy:
Seebany
Datta-Barua



Artificial Undersampled Scenario



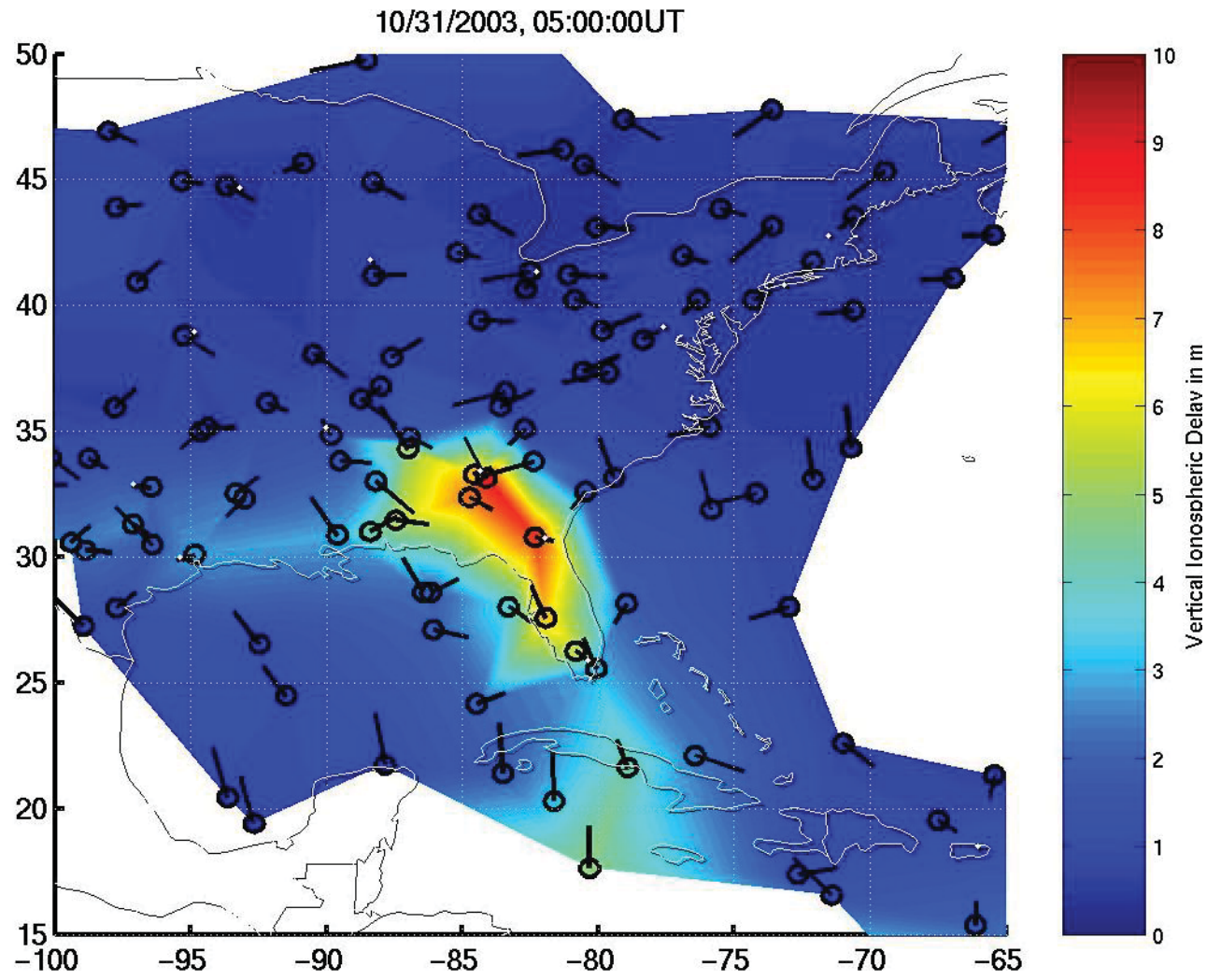
10/31/2003, 05:00:00UT



Courtesy:
Seebany
Datta-Barua



WAAS Measurements



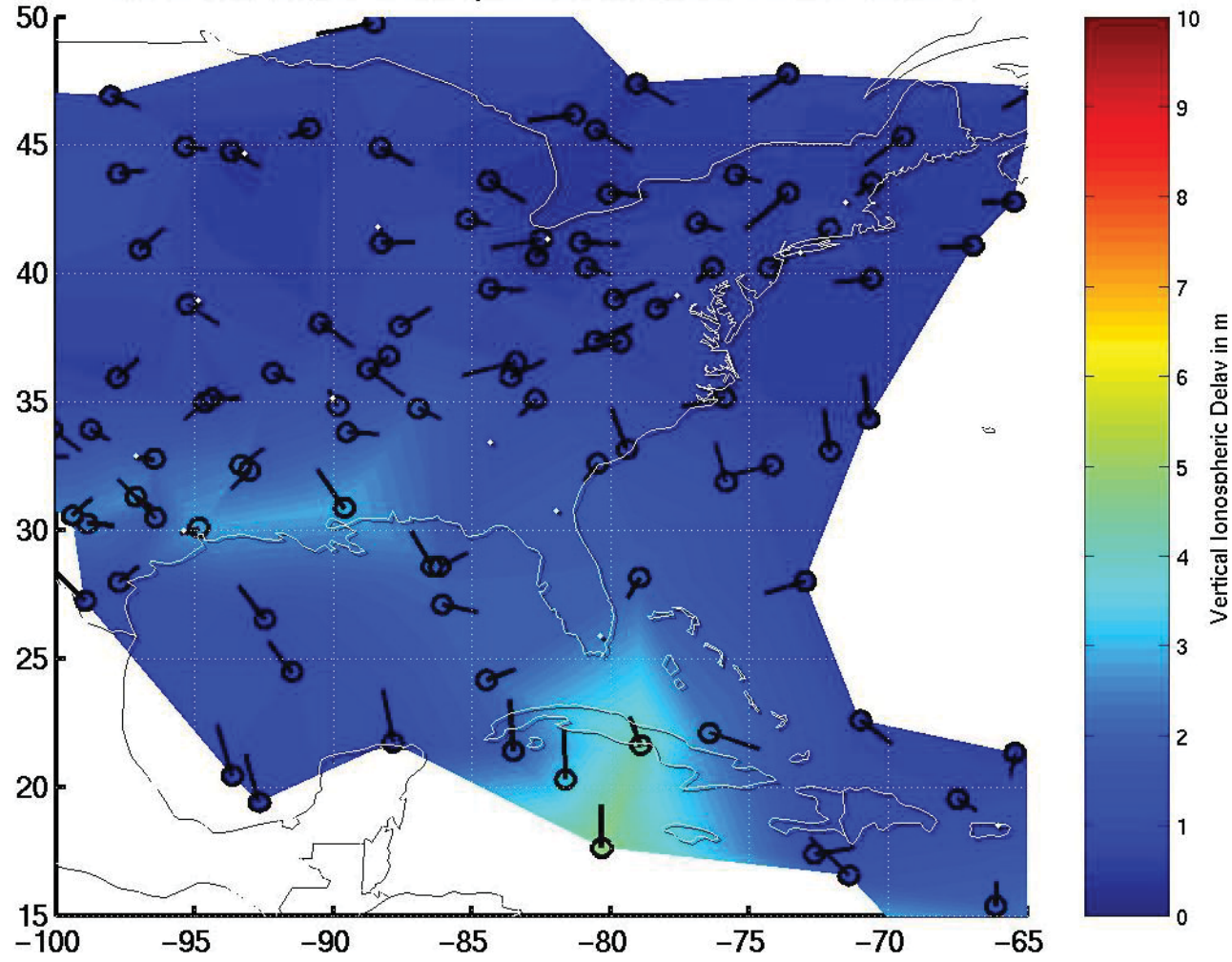
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Seebany
Datta-Barua



Artificial WAAS Undersampling Scenario



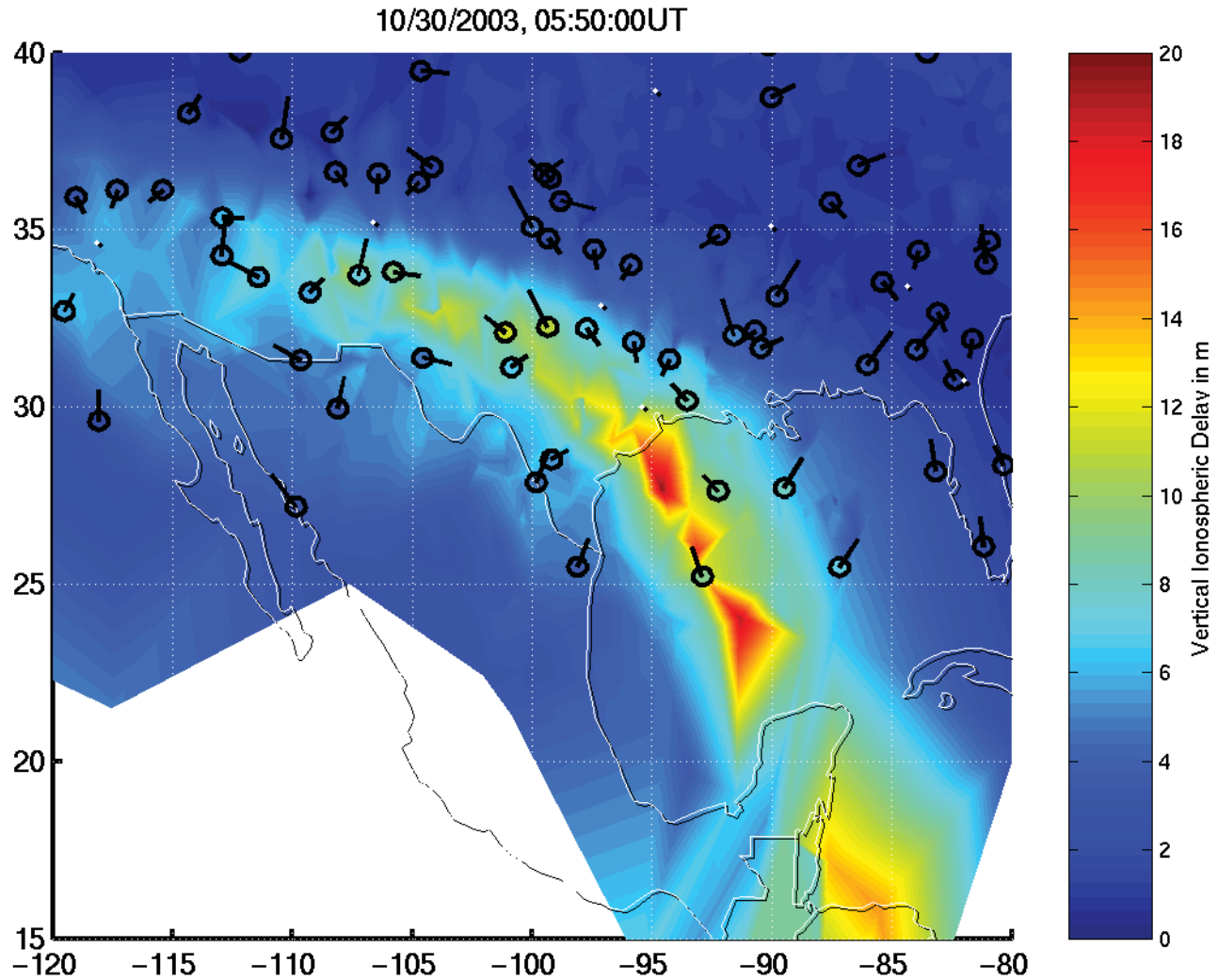
10/31/2003, 05:00:00UT, Supertruth Malicious Threat Removed



Courtesy:
Seebany
Datta-Barua



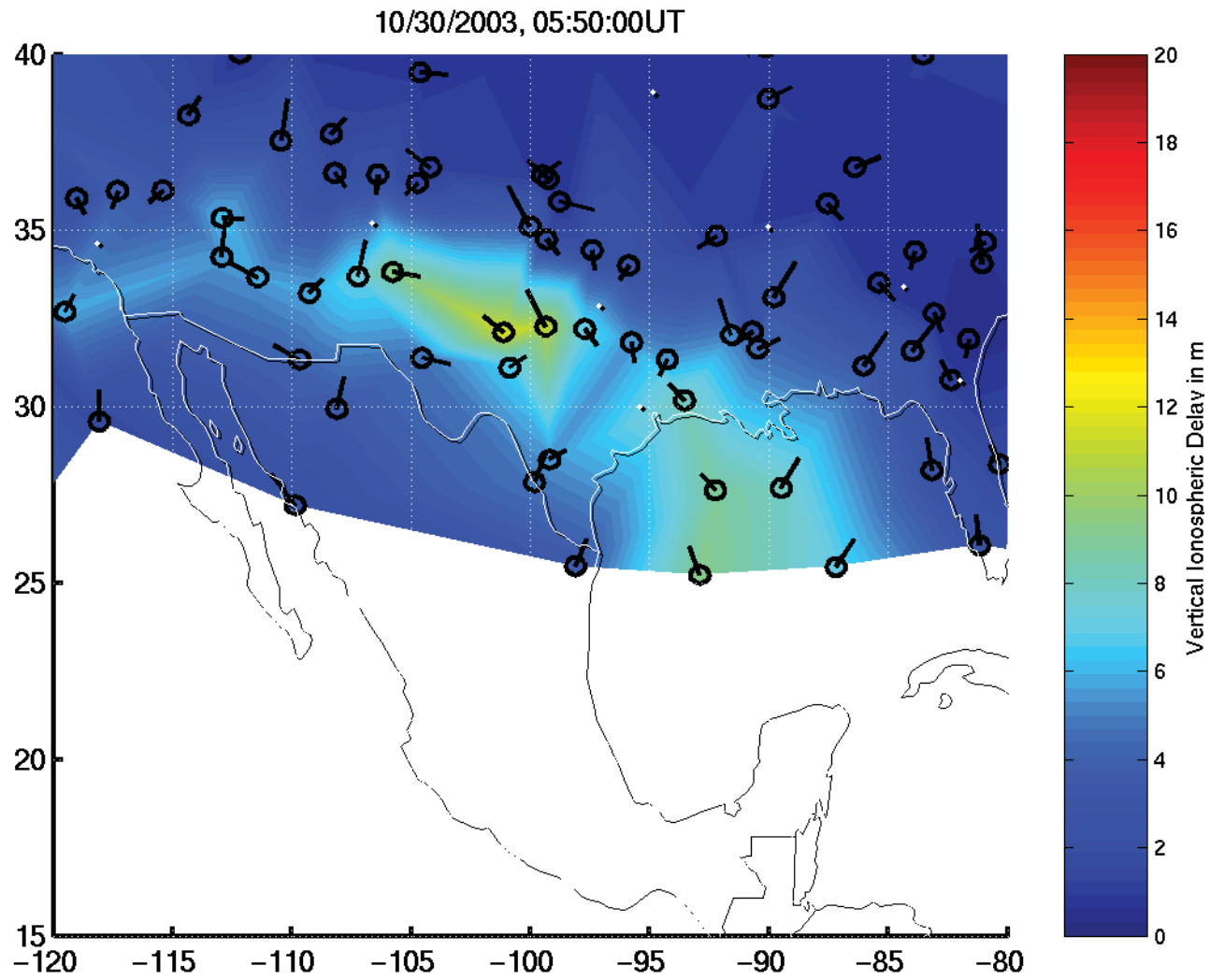
Real Undersampled Condition



Courtesy:
Seebany
Datta-Barua



WAAS Measurements



Courtesy:
Seebany
Datta-Barua



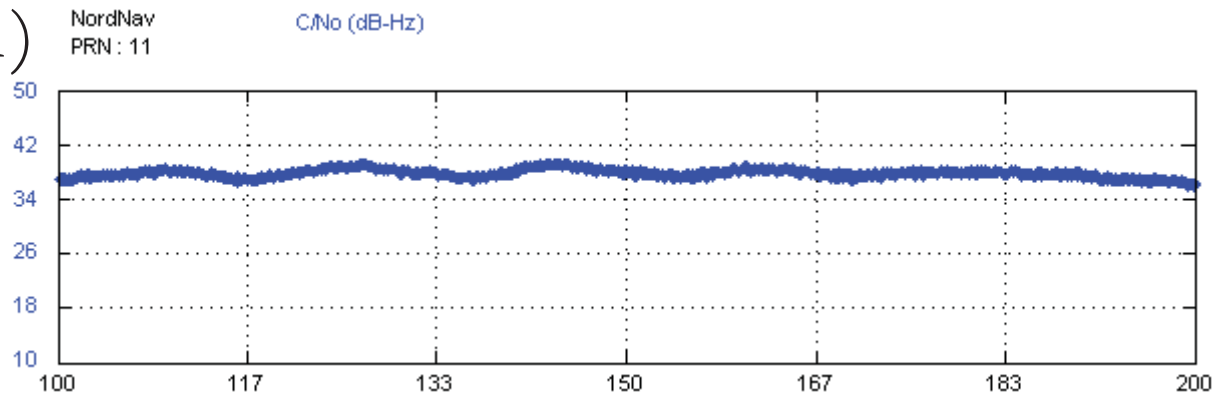
Scintillation and Deep Signal Fading



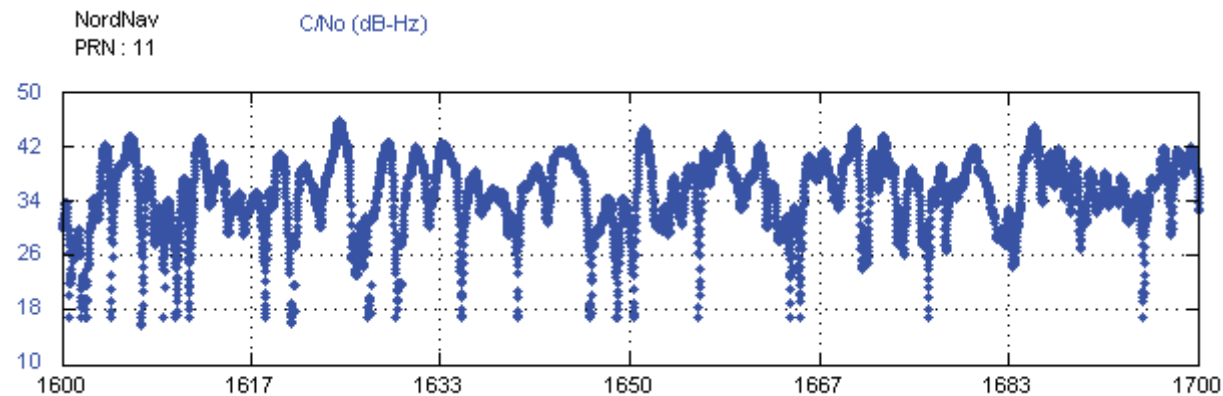
- Signal to noise ratio (C/No) of PRN 11 (Mar. 18, 2001)

C/No

Nominal



Scintillation
(equatorial &
solar max)



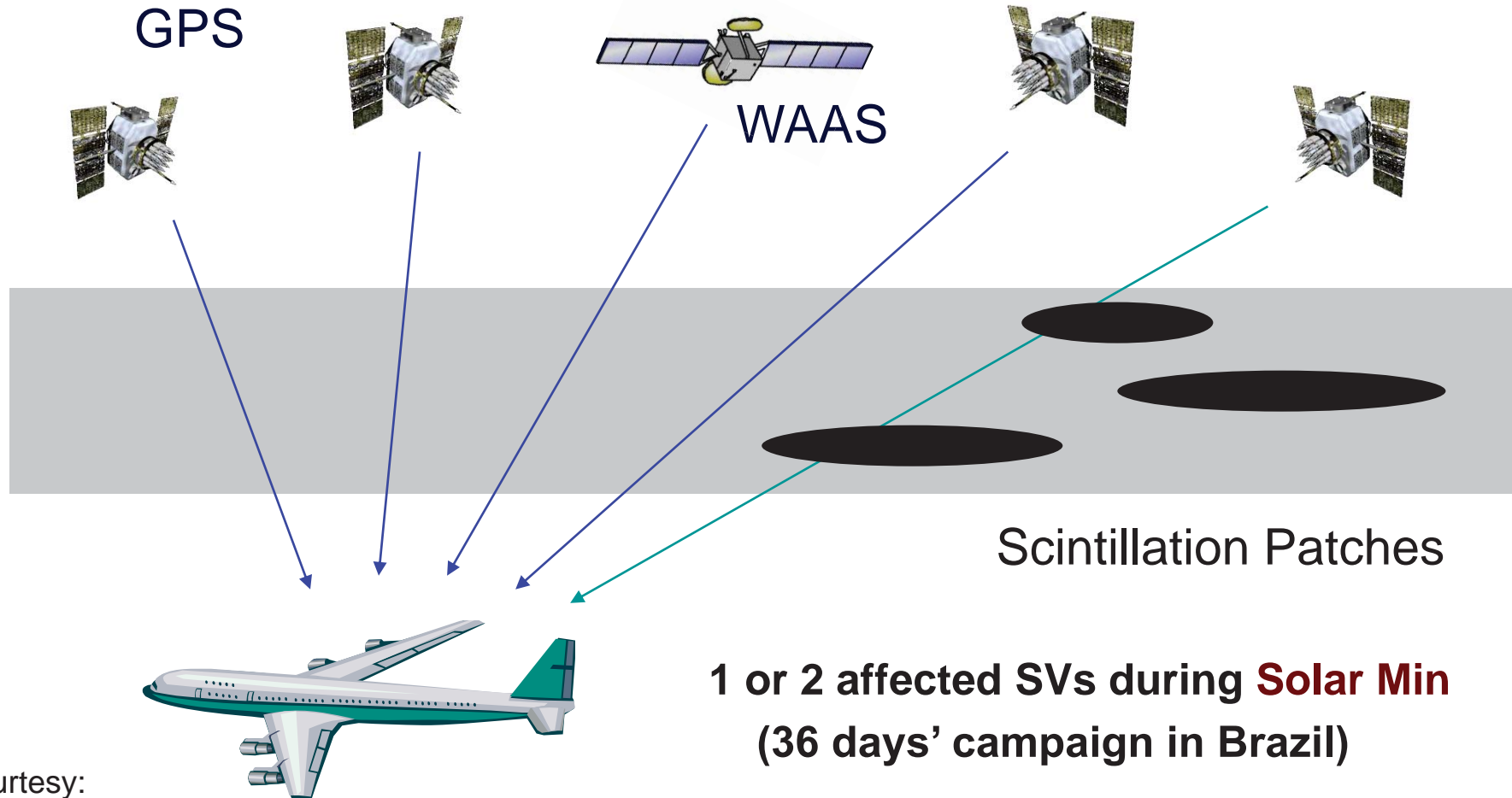
25 dB

Courtesy:
Jiwon Seo

← 100 sec →



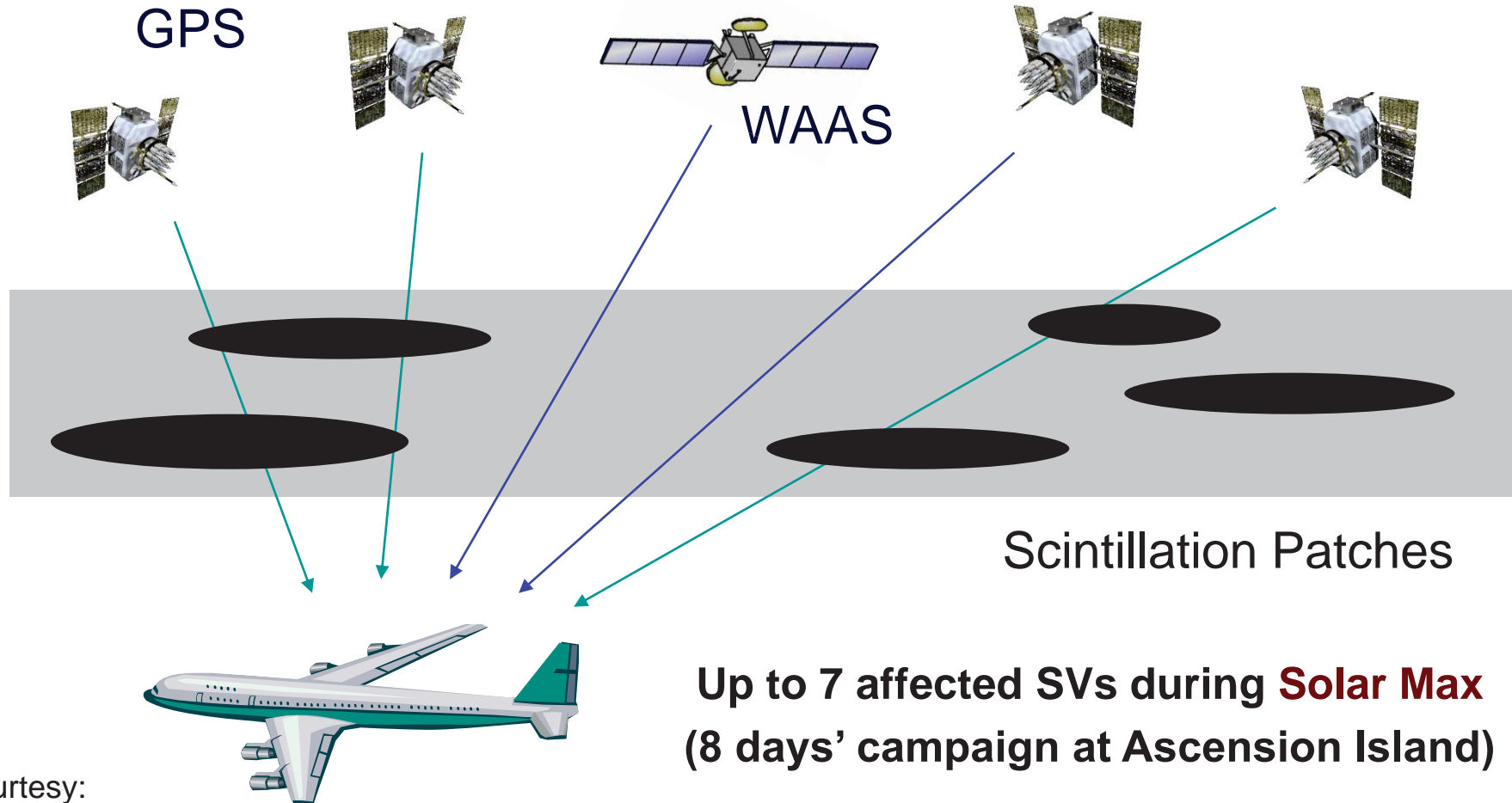
Scintillation and Navigation



Courtesy:
Jiwon Seo



Scintillation and Navigation



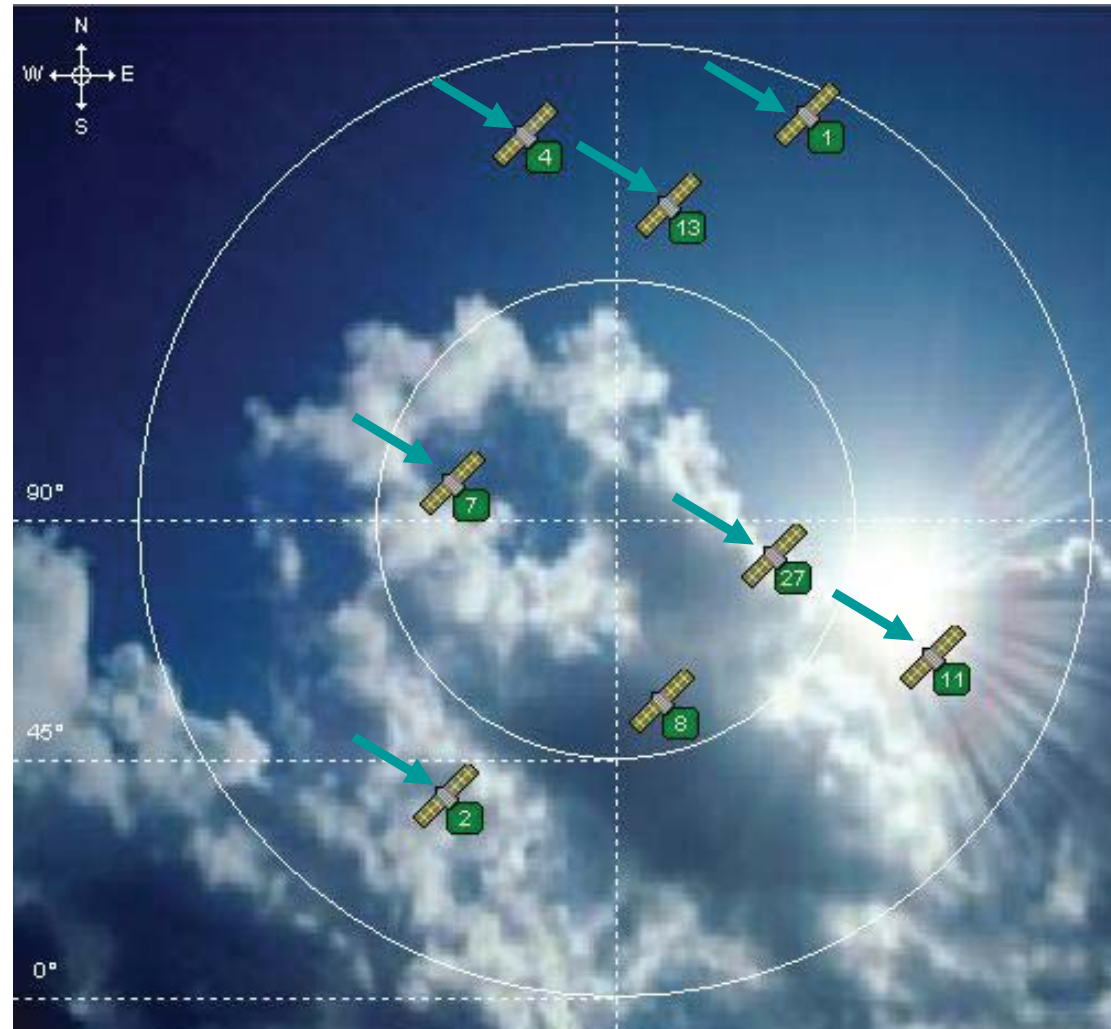
Courtesy:
Jiwon Seo



Severe Scintillation Data



Solar Max
(worst 45 min
in 8 days)



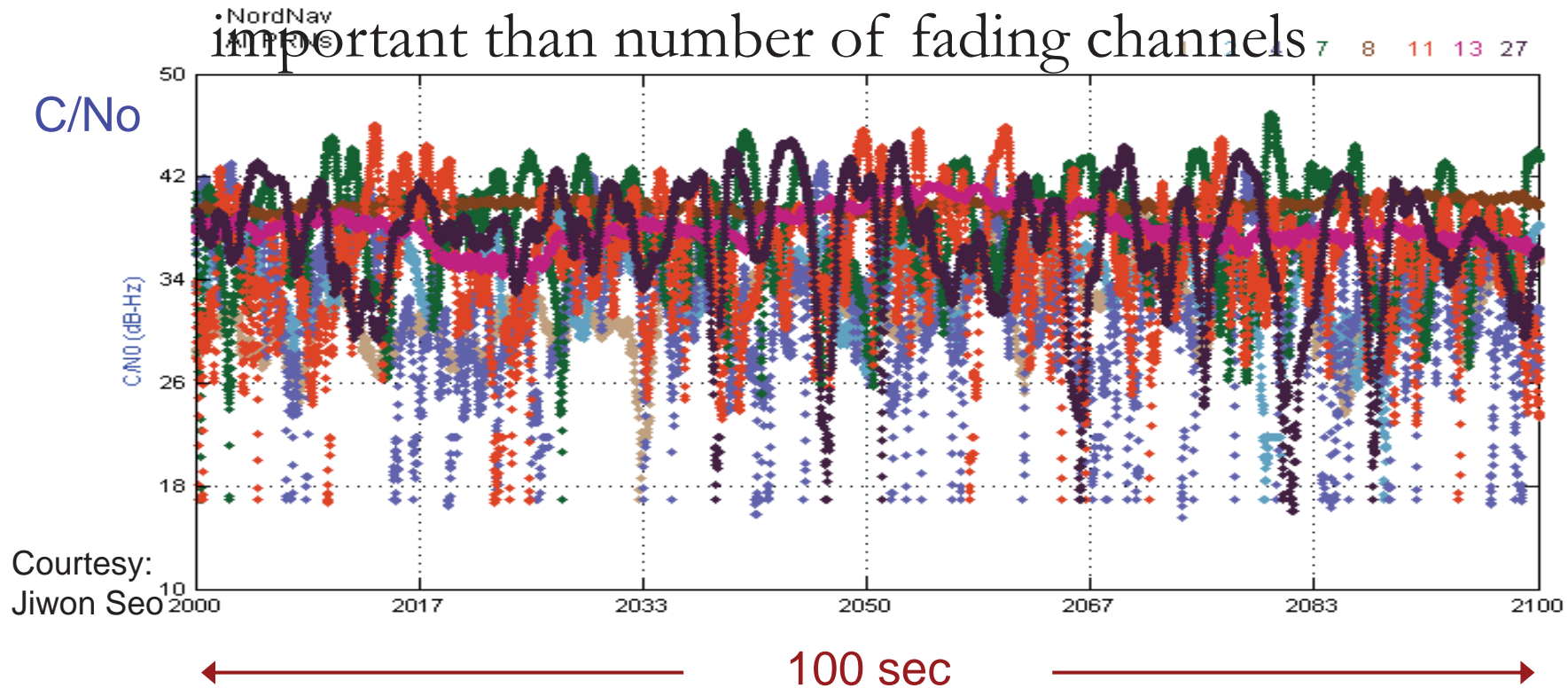
Courtesy:
Jiwon Seo



Severe Scintillation (example)



- 50 Hz C/No outputs of all 8 satellites on sky (100 sec out of 45 min data as an example)
- Number of **simultaneous loss** of satellites is more important than number of fading channels



Courtesy:
Jiwon Seo



Hatch Filter Model



50 dB-Hz

C/No

10 dB-Hz

10

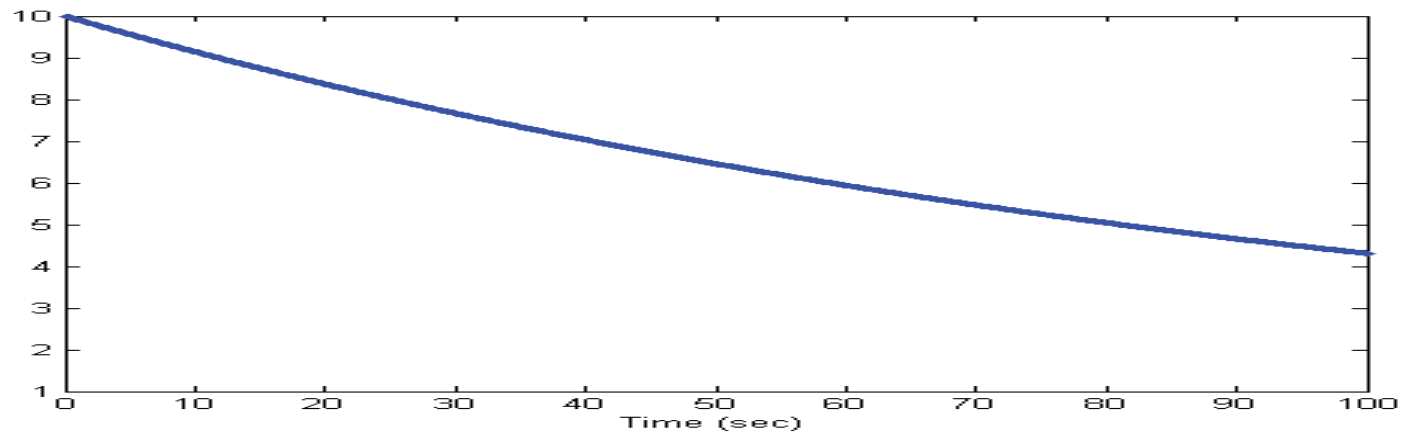
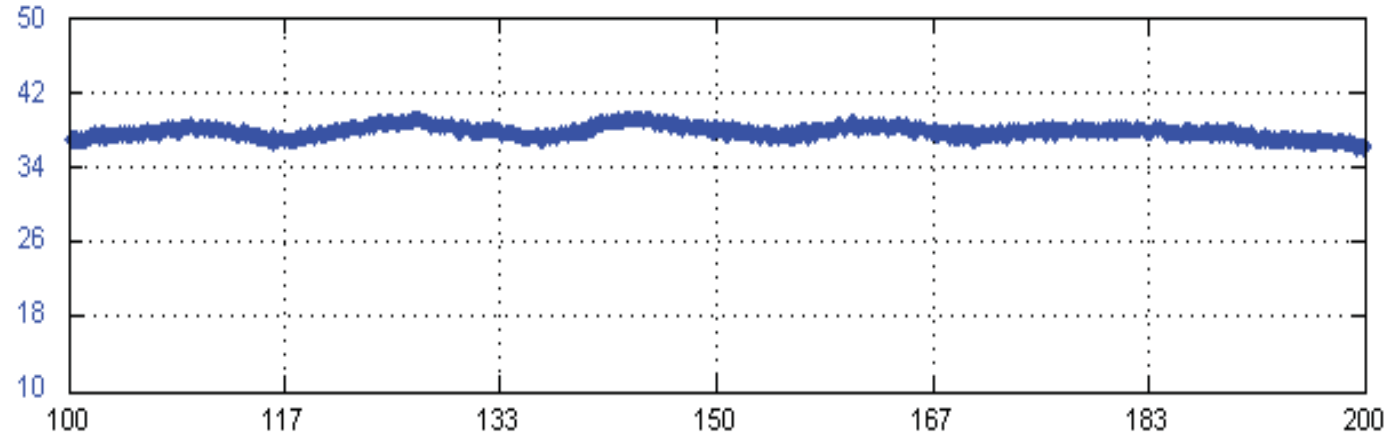
Relative
Noise
Level

1

Courtesy:
Jiwon Seo

NordNav
PRN : 11

C/No (dB-Hz)



← 100 sec →



Hatch Filter Model



50 dB-Hz

C/No

10 dB-Hz

10

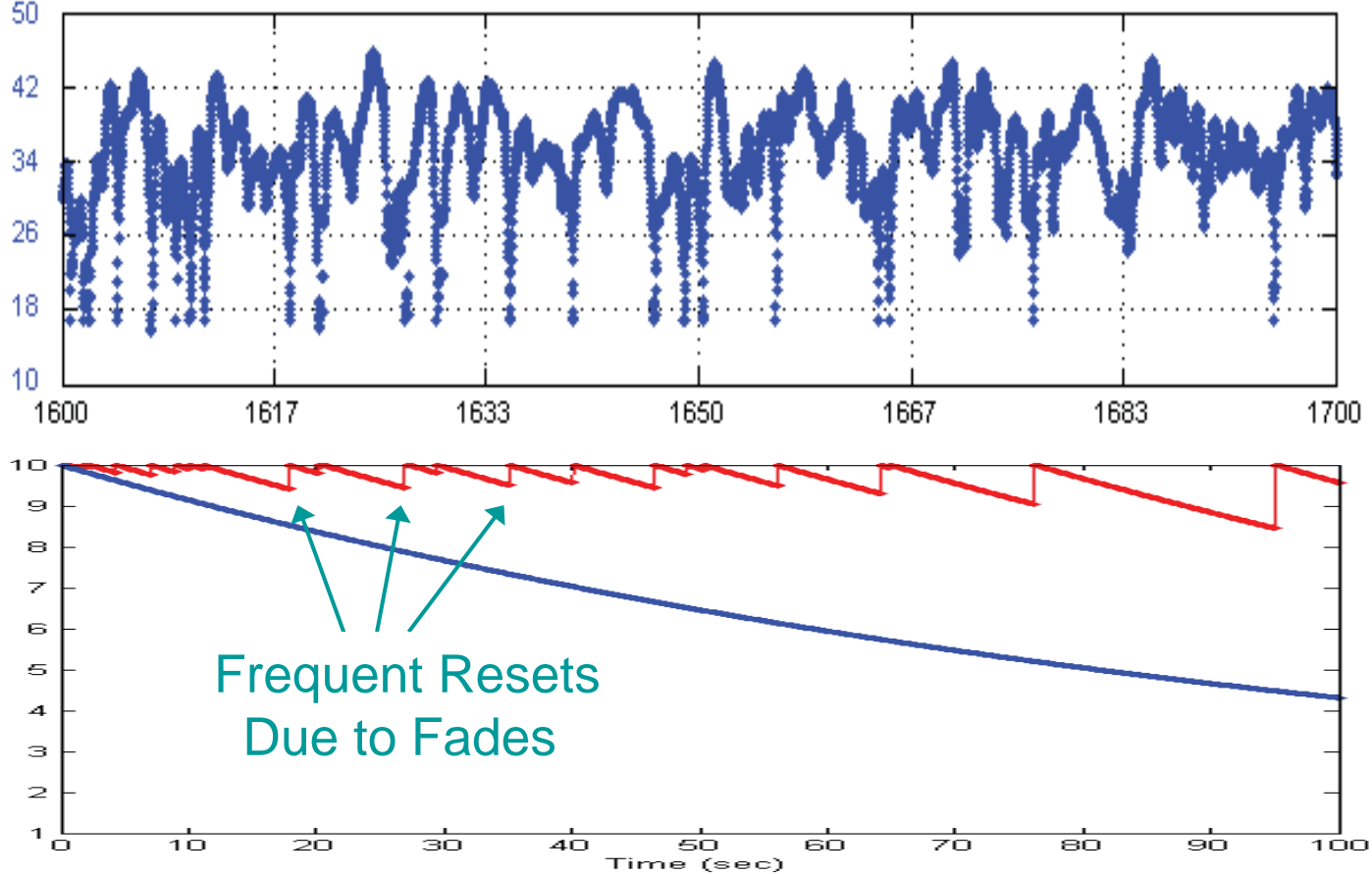
Relative
Noise
Level

1

Courtesy:
Jiwon Seo

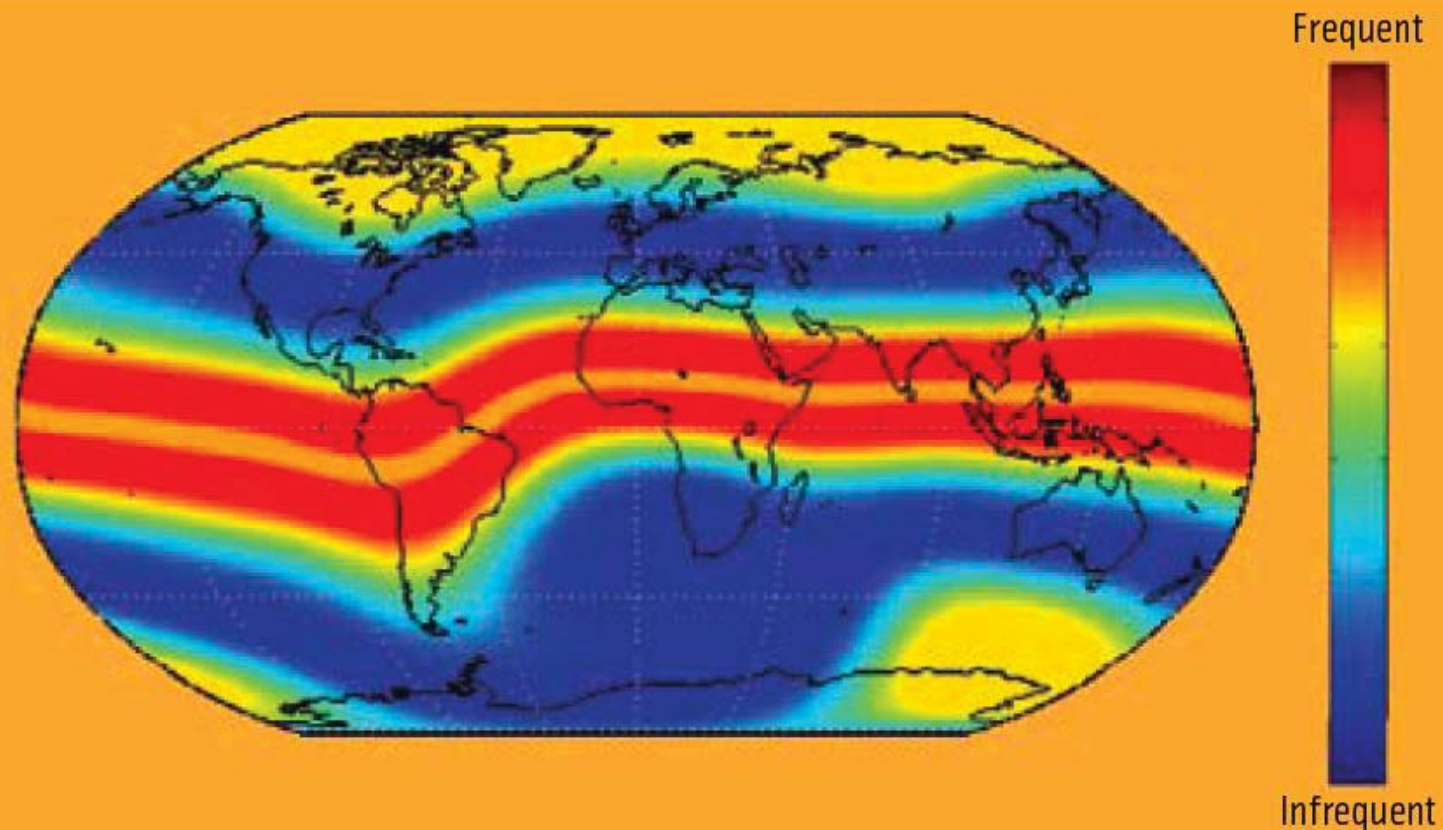
NordNav
PRN : 11

C/No (dB-Hz)





Regions with Scintillation



Courtesy: Paul Kintner

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FIGURE 1 Scintillation map showing the frequency of disturbances at solar maximum. Scintillation is most intense and most frequent in two bands surrounding the magnetic equator, up to 100 days per year. At poleward latitudes, it is less frequent and it is least frequent at mid-latitude, a few to ten days per year.



Outline

- Ionospheric Modeling
- Ionospheric Threats
- **Next Generation Satellite Navigation**
- Future Signals
- Conclusions

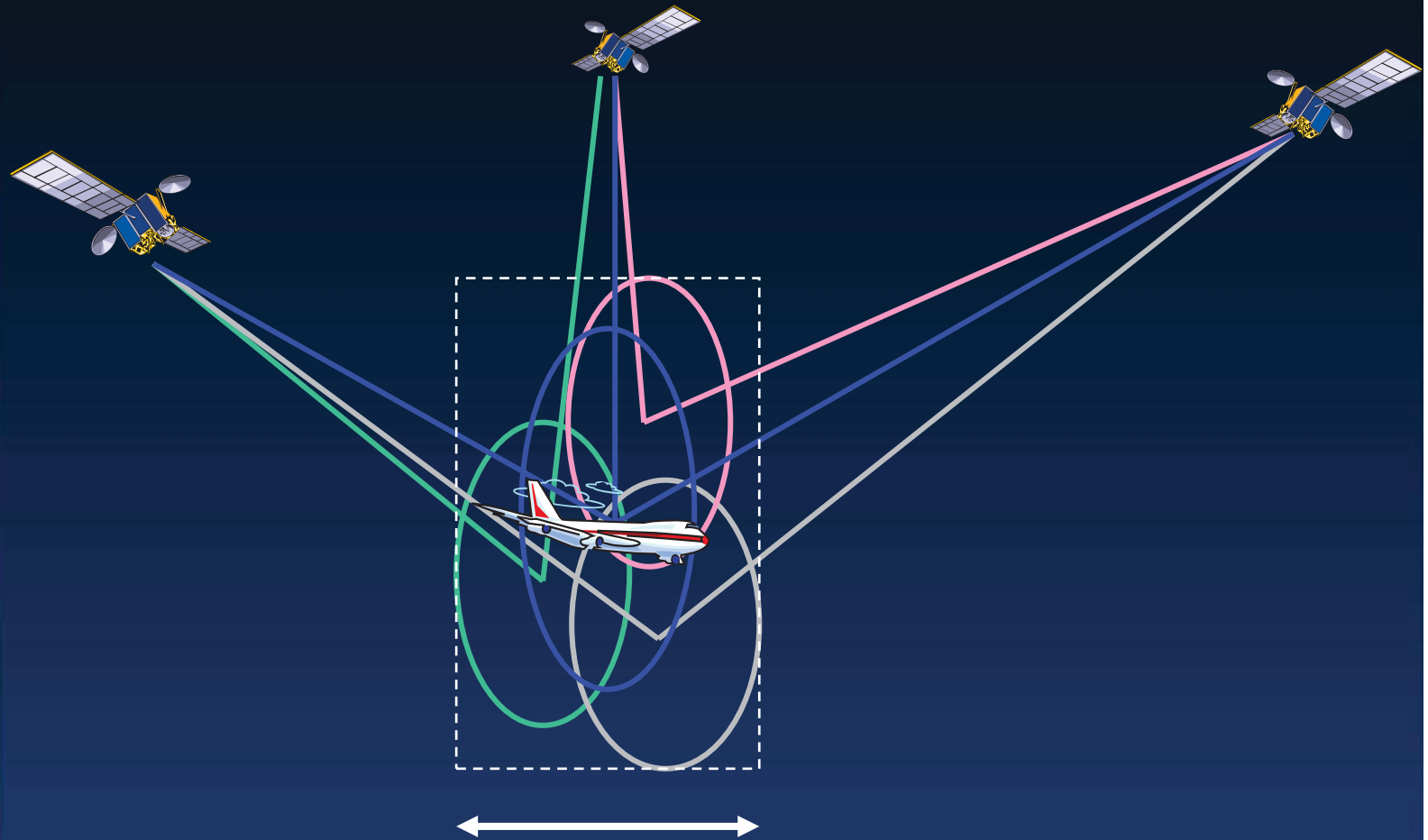


Looking Ahead

- Next generation of satellite navigation will exploit new signals and new systems
 - *GPS is being modernized*
 - *Other nations developing SatNav*
- It is time to plan ahead
 - *What new capabilities can we provide?*
 - *Are there more efficient ways to provide them?*



RAIM Protection



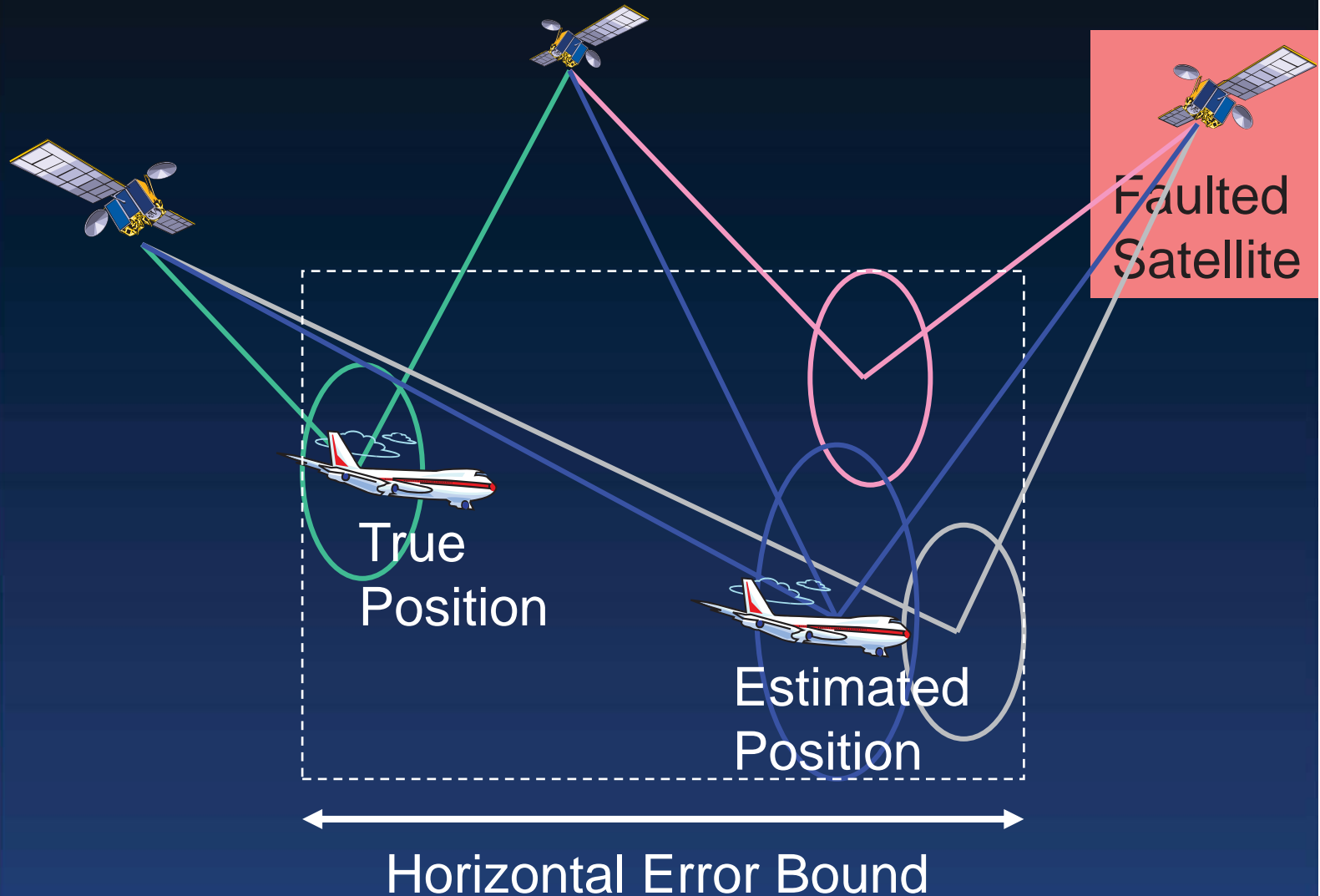
Horizontal Error Bound

Courtesy:
Juan Blanch

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RAIM Protection



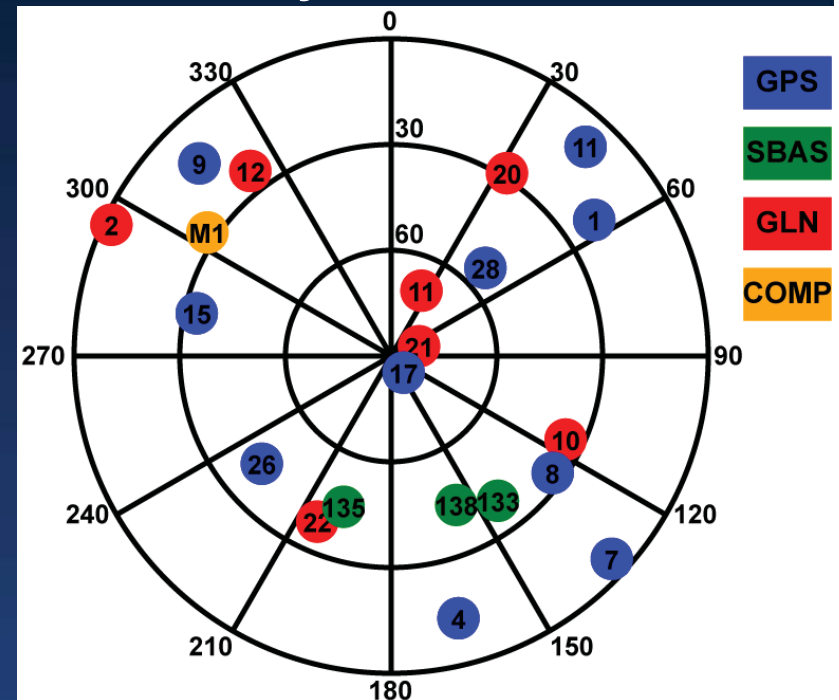
Courtesy:
Juan Blanch

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New GNSS Constellations

- A solution to constellation weakness
 - Many more ranging sources
 - Fills in gaps
 - Provides extra redundancy
 - Averages down uncertainty



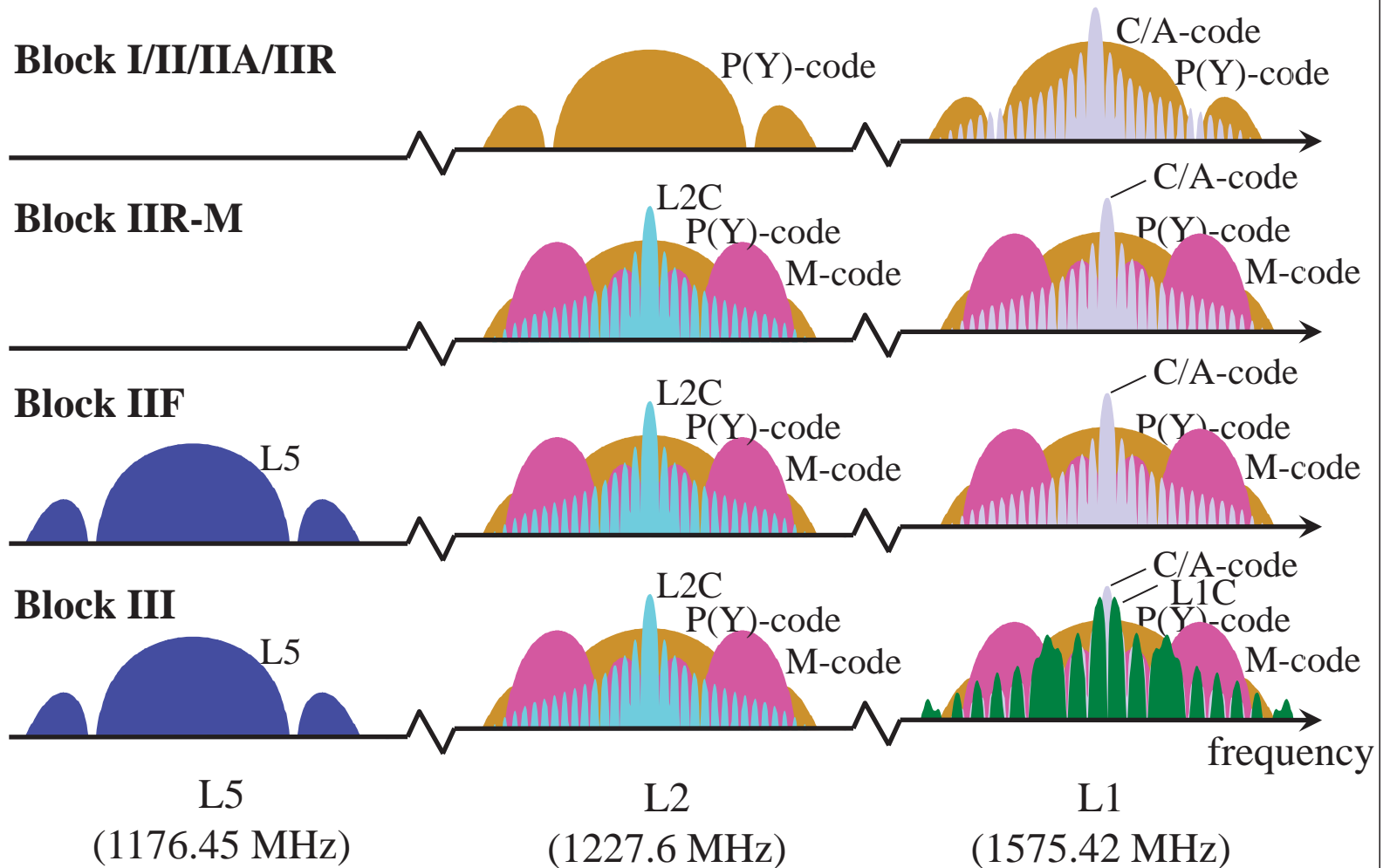


Advanced RAIM (ARAIM)

- Dual Frequency - Multi-constellation
 - *Eliminates multiple SV iono threat*
 - *Strong geometries*
- Support for vertical guidance
 - *Requires a more stringent level of certification than RAIM for lateral*
 - *May require ground monitoring by approving agency*
- Potential for near global coverage
 - *Modest infrastructure requirements*



GPS Signals



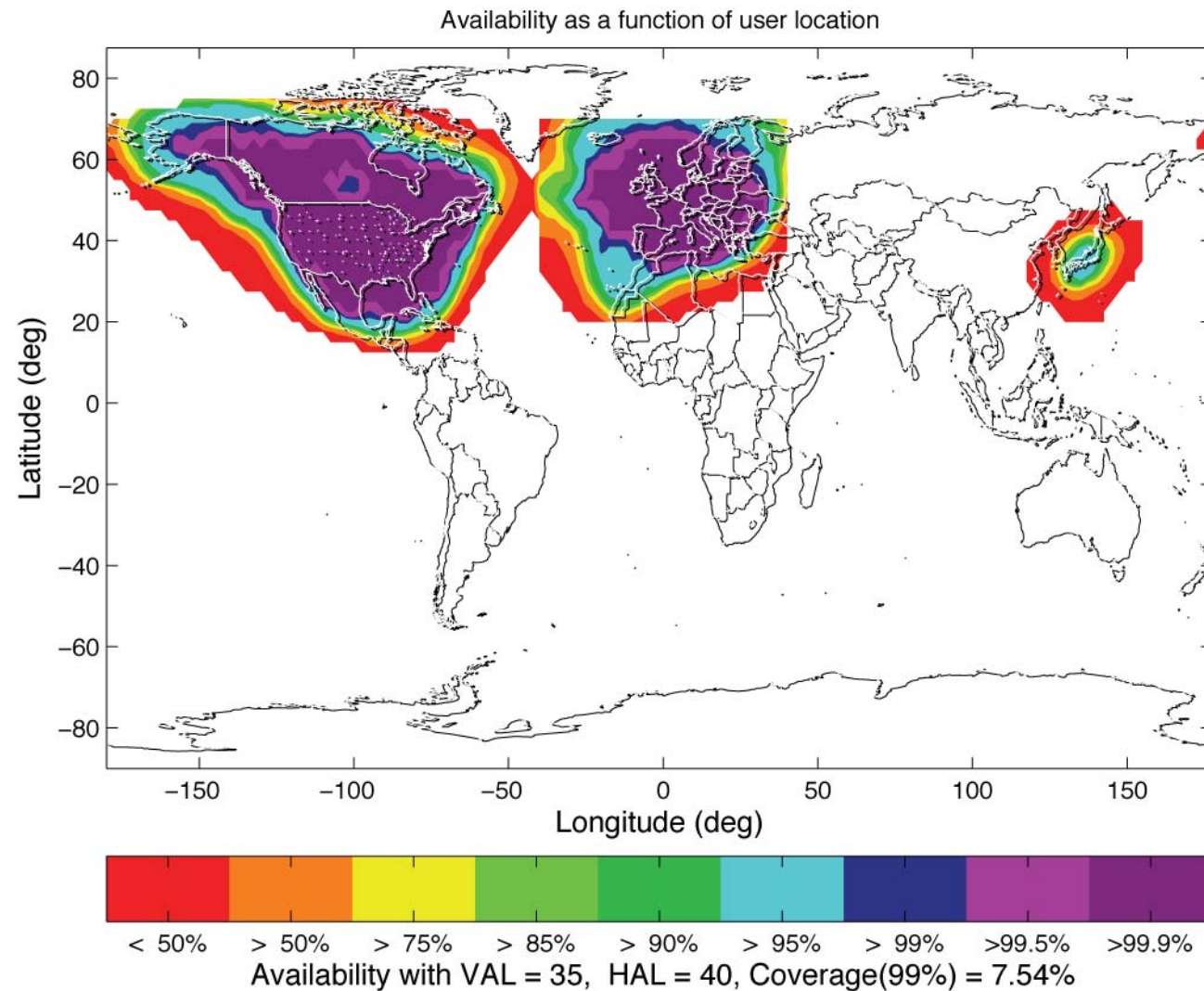
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WAAS
EGNOS
MSAS

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Current SBAS Coverage

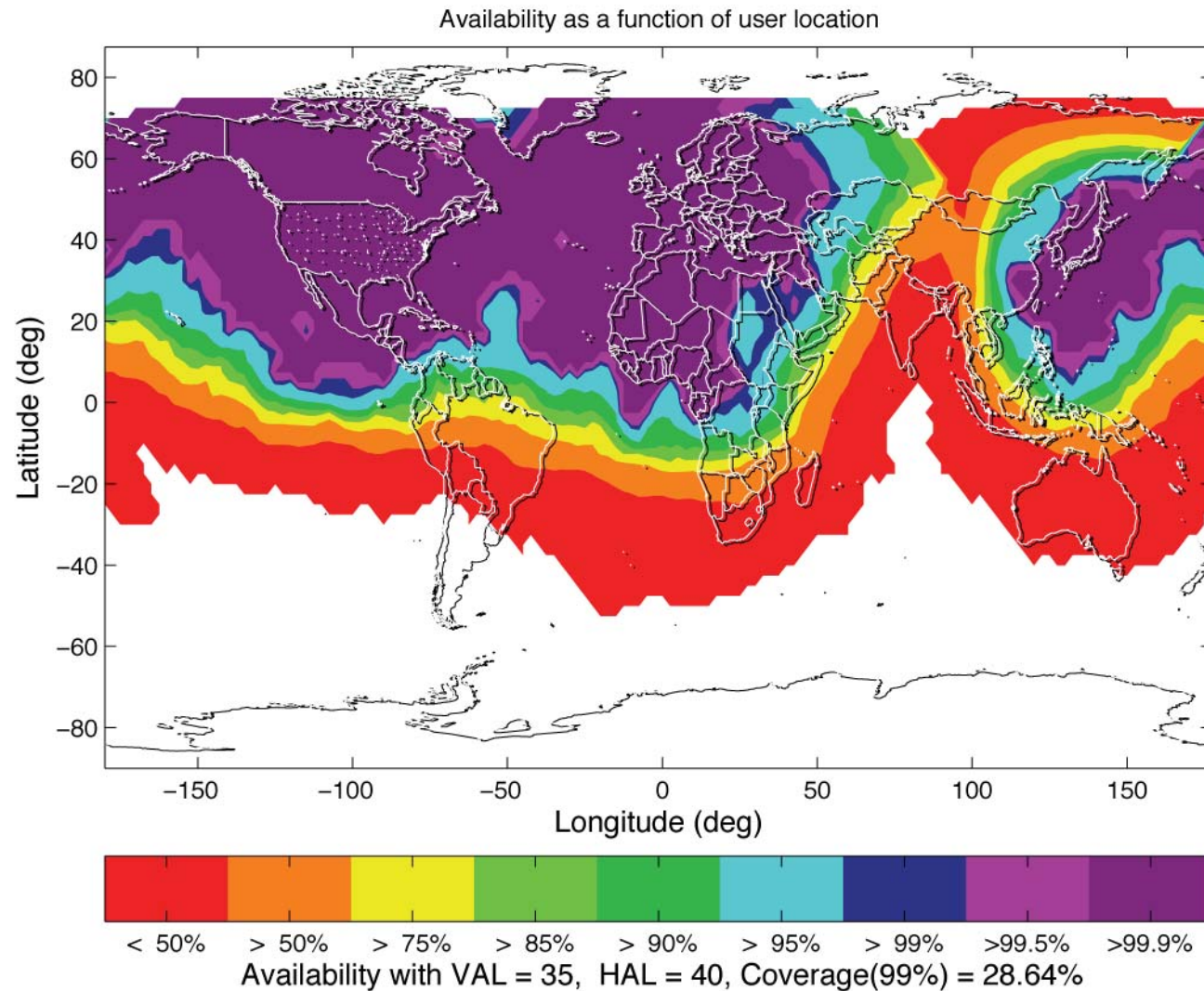




WAAS
EGNOS
MSAS

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Dual Frequency Coverage (WAAS, EGNOS, MSAS)

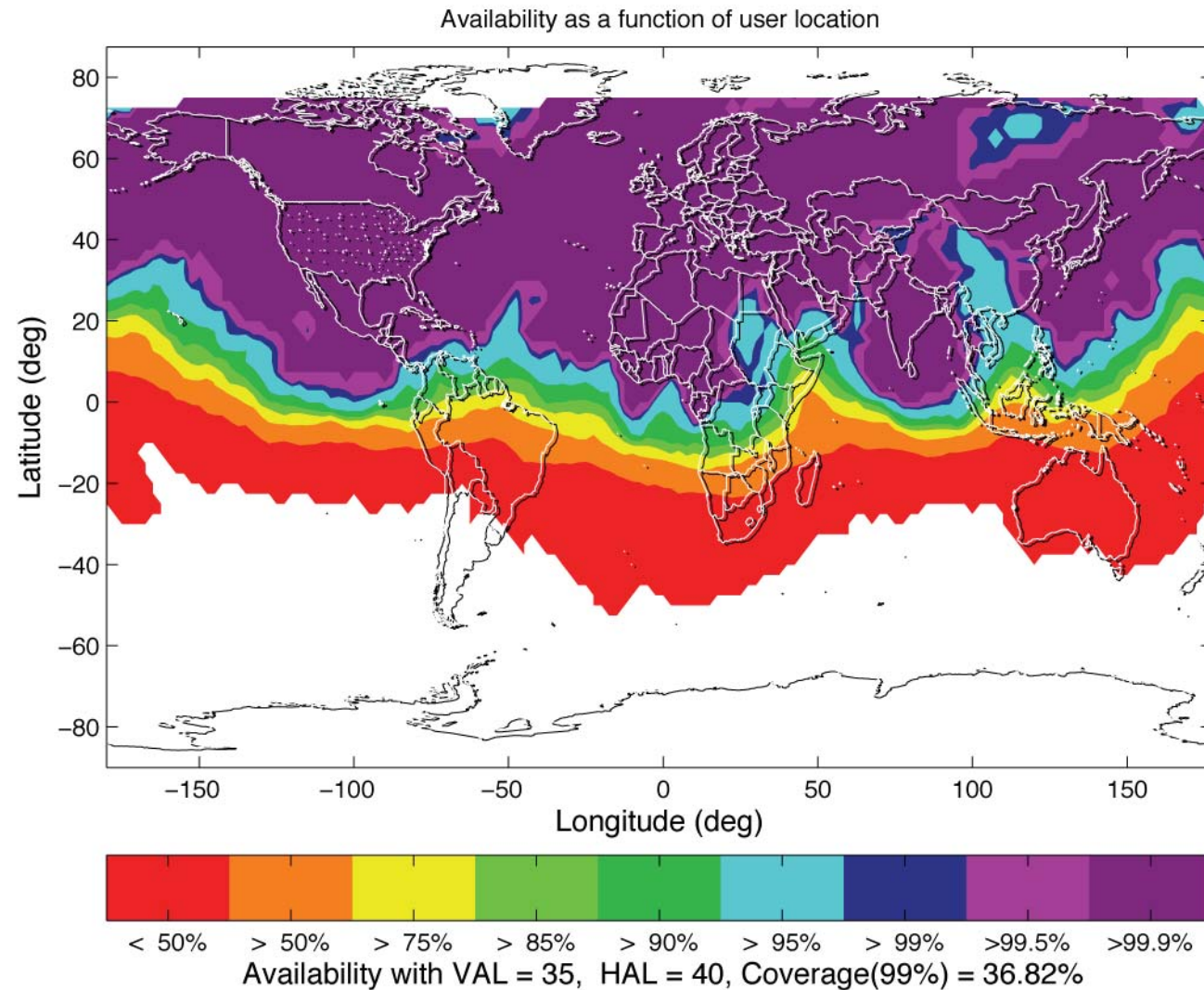




Dual Frequency Coverage (with GAGAN + Russia)

WAAS
EGNOS
MSAS
GAGAN
SDCM

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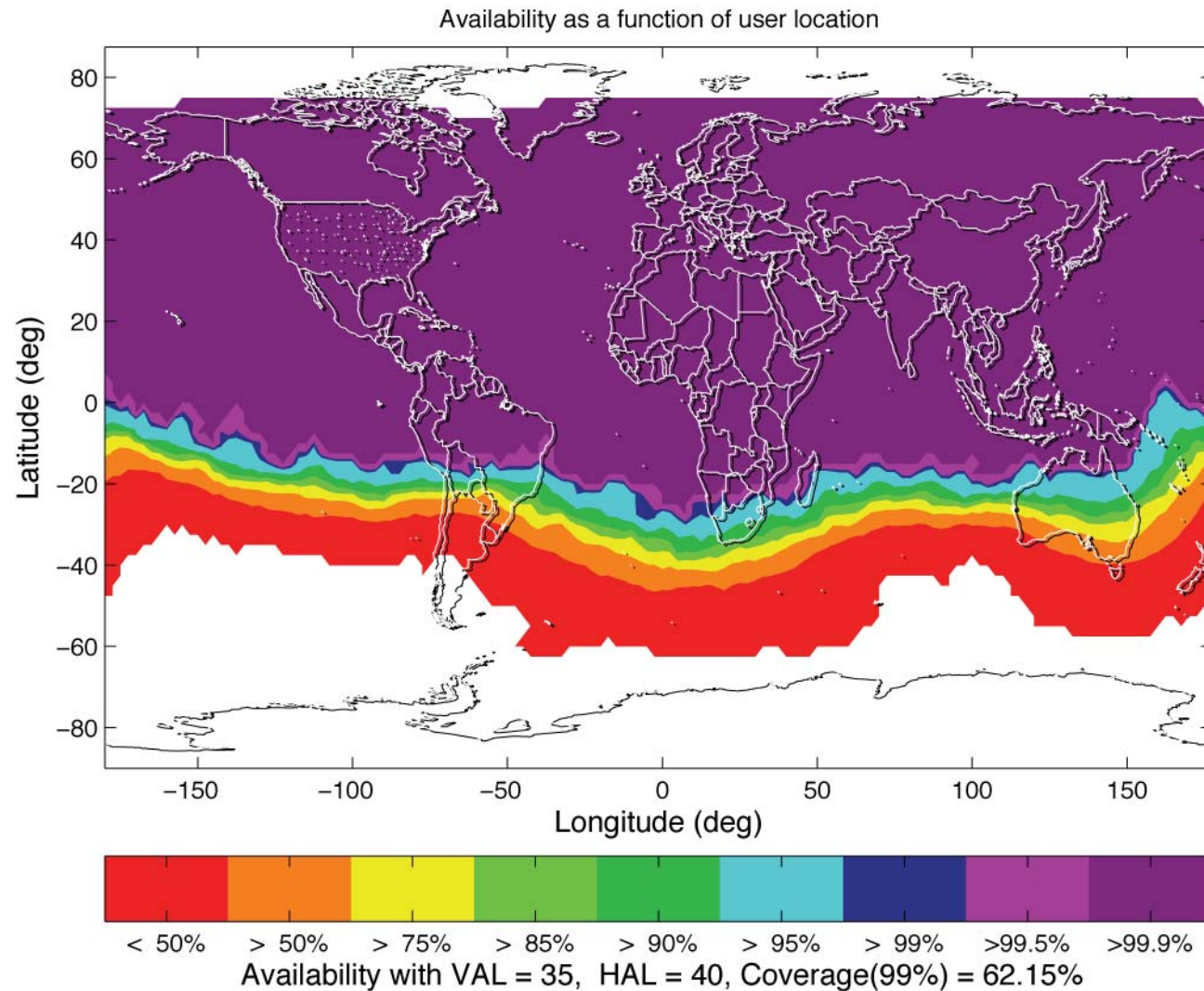




Dual Frequency + Second Constellation (Galileo)

WAAS
EGNOS
MSAS
GAGAN
SDCM

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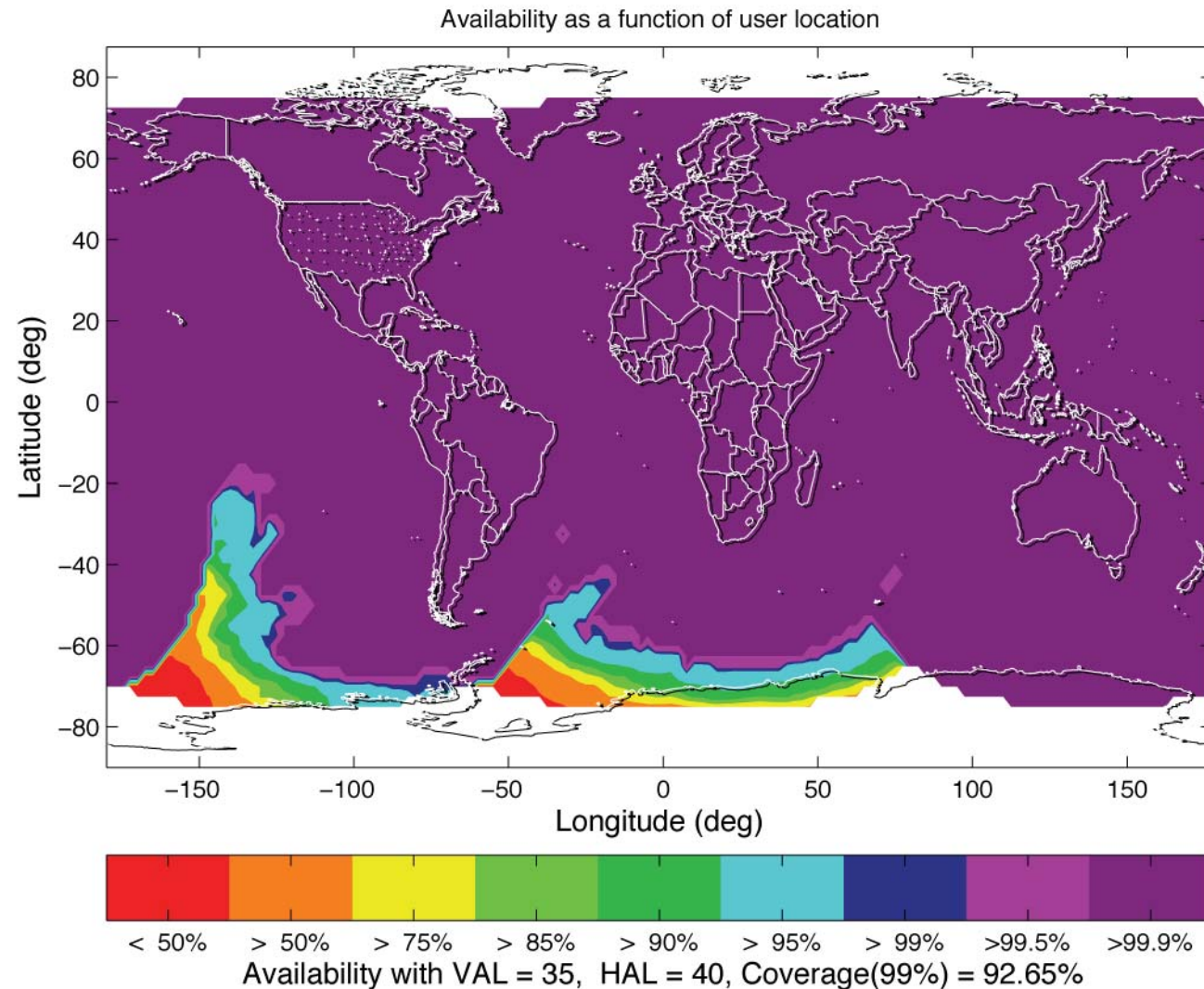




Dual Frequency, Dual GNSS, Expanded Networks

WAAS
EGNOS
MSAS
GAGAN
SDCM

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Conclusions

- GNSS can be used to provide aircraft navigation for all levels of service
- Integrity is a key concern
 - *Important to understand what can go wrong and how to protect users*
- Observation and data collection are key to understanding behavior
 - *A long history of careful and consistent data monitoring are required*
 - *Practical experience leads to trust and acceptance*



Outline

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- Ionospheric Threats
- **Other Integrity Threats**
- Integrity Methodology
- Next Generation Satellite Navigation
- Future Signals
- Conclusions

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Integrity

- Monitor network or signal redundancy identifies observable threats
 - *Protection against satellite failures*
 - Ephemeris errors
 - Clock errors
 - Signal errors
 - *Protection against ionospheric errors*

- Design assumes worst credible values for all unobservable threats



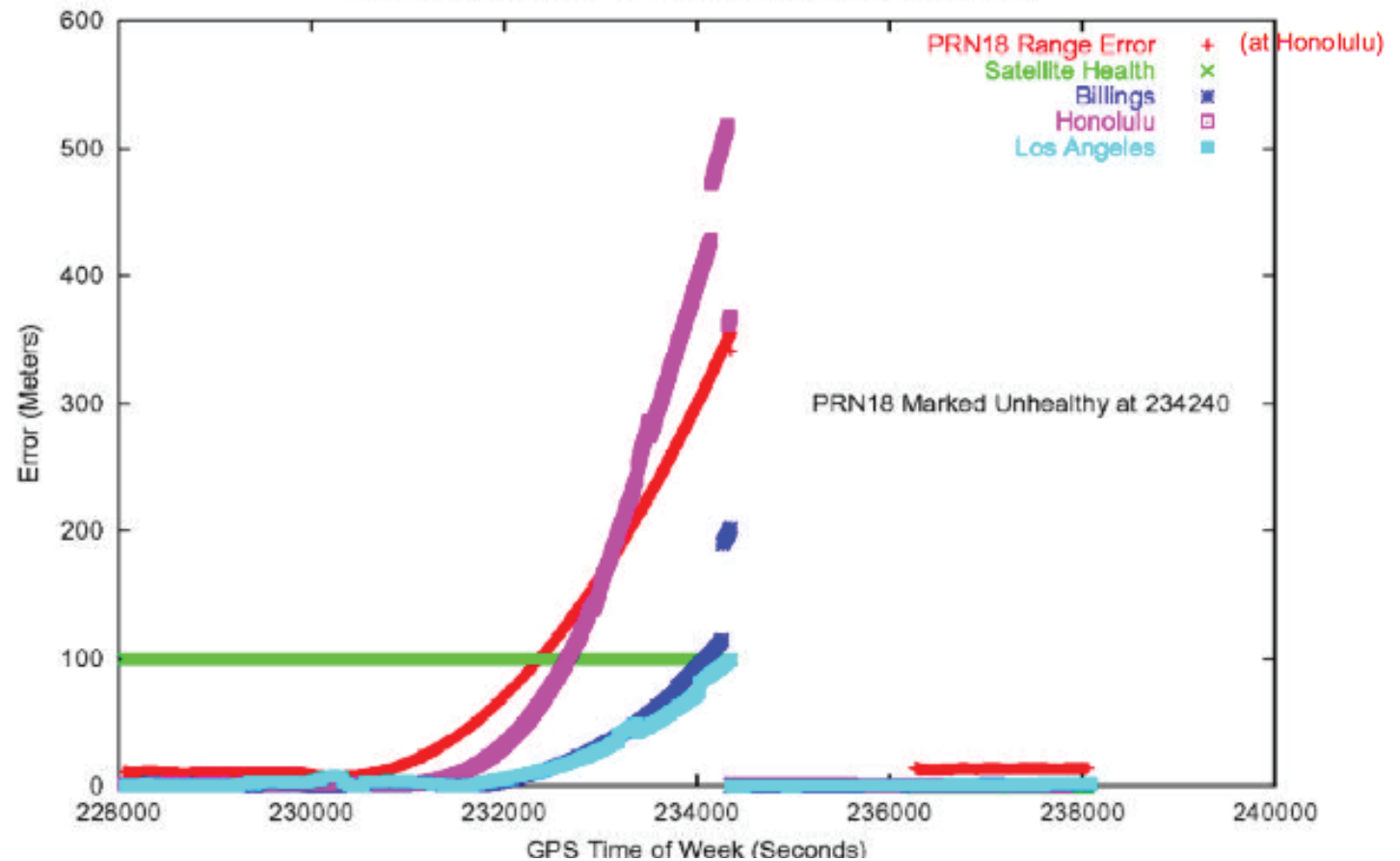
Satellite Ephemeris Anomaly



Observed GPS SPS 3-D Position Errors on April 10, 2007

Source: FAATC GPS SPS PAN Report #58, 31 July 2007.

SPS 3D Position Error During PRN18 Anomaly: 10 April 2007



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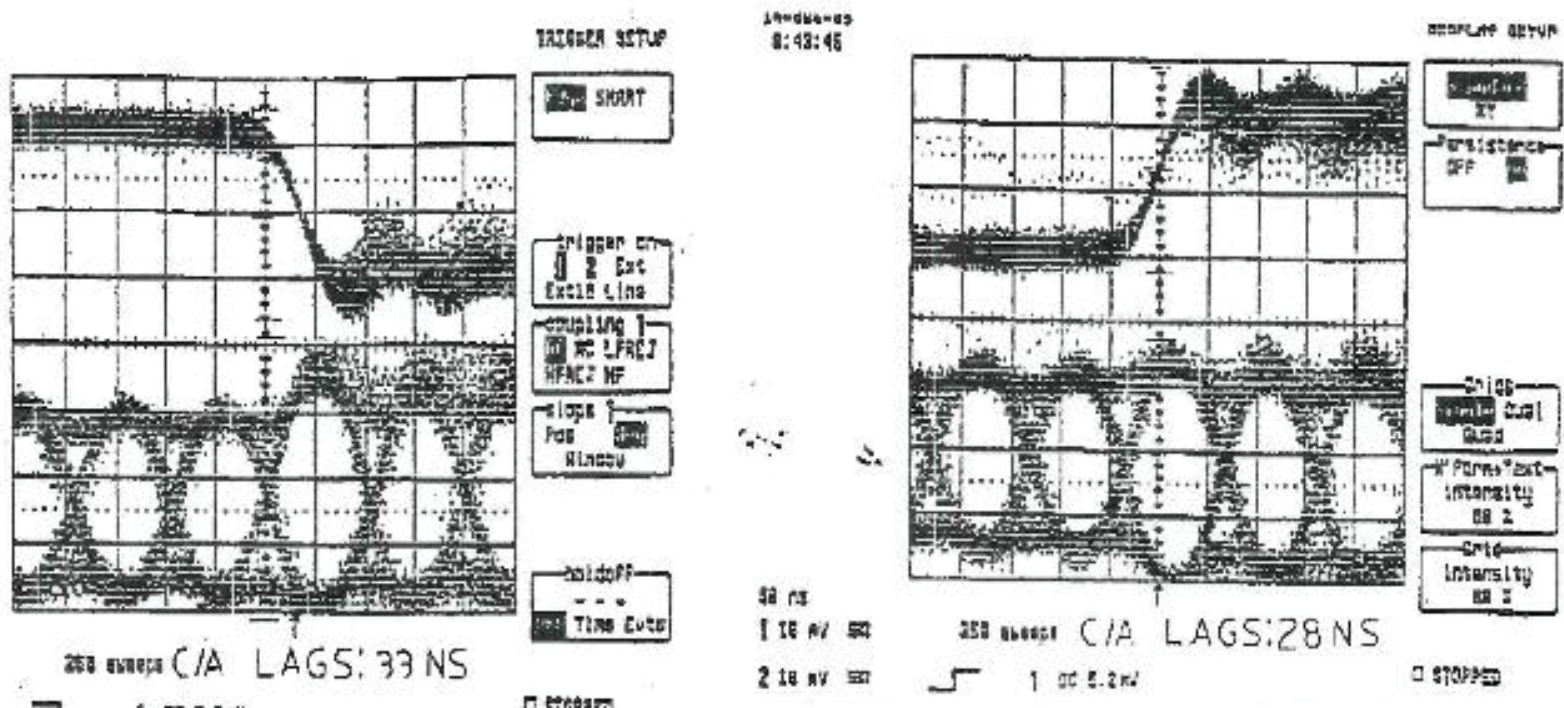


Satellite Signal Anomaly

L1 C/A Lags L1 P Code Falling Edge or Leading Edge

Oct 13, 1993, 23:45

Oct 14, 1993, 08:43



Courtesy:
Per Enge

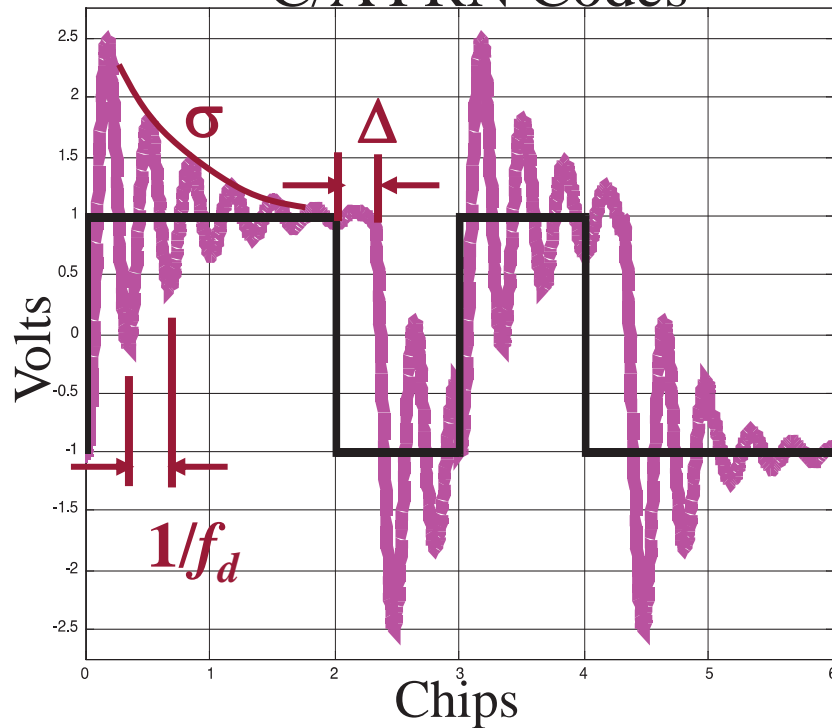
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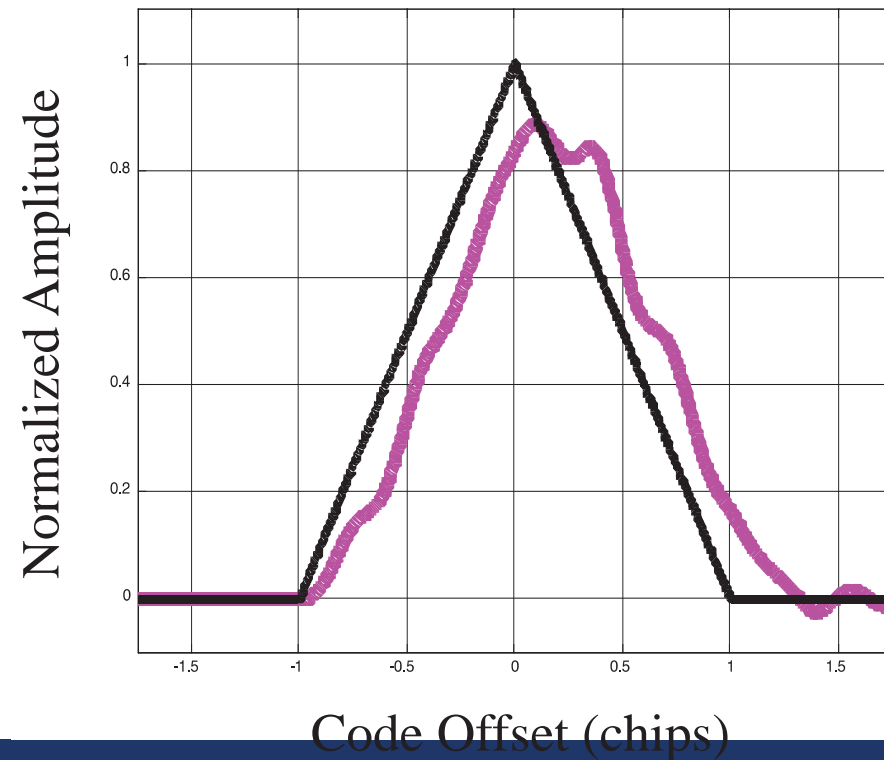
“Evil Waveform” Failure Mode Example

Comparison of Ideal and “Evil Waveform” Signals for Threat Model C

C/A PRN Codes



Correlation Peaks



Todd Walter

Note:

Threat Model A: Digital Failure Mode (Lead/Lad Only: Δ)

Threat Model B: Analog Failure Mode (“Ringing” Only: $f_d\sigma$)



Outline

- Ionospheric Modeling
- Ionospheric Threats
- Other Integrity Threats
- **Integrity Methodology**
- Next Generation Satellite Navigation
- Future Signals
- Conclusions



Overall Integrity Approach

- Conventional Differential GPS Systems Rely on Lack of Disproof
 - *“I’ve been using it for N years and I’ve never had a problem”*
- 10^{-7} Integrity Requires Active Proof
- Analysis, Simulation, and Data Must Each Support Each Other
 - *None sufficient by themselves*
- Clear Documentation of Safety Rationale is Essential



Interpretation of “Probability of HMI $< 10^{-7}$ Per Approach”

→ Possible Interpretations

- *Ensemble Average of All Approaches Over Space and Time*
- *Ensemble Average of All Approaches Over Time for the Worst Location*
- *Previous Plus No Discernable Pattern (Rare & No Correlation With User Behavior)*
- *Worst Time and Location*



Probability of Integrity Failure

→ Average Risk

$$\square \int P(\text{fault} \mid \text{condition}) \square P(\text{condition})$$

all conditions

→ Specific Risk

$$P(\text{fault} \mid \text{condition})$$

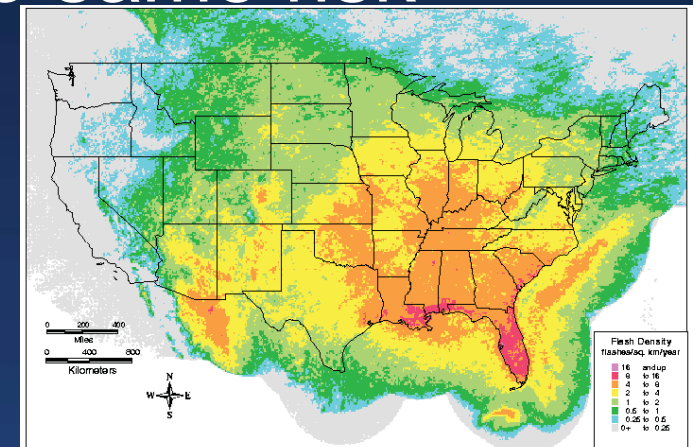


Probability of Being Struck by Lightning

- From the Lightning Safety Institute
 - USA population = 280,000,000
 - 1000 lightning victims/year/average
 - Odds = 1 : 280,000 of being struck by lightning
- Not everyone has the same risk

One person struck 7 times

Naïve calculation:
< 1e-38 probability





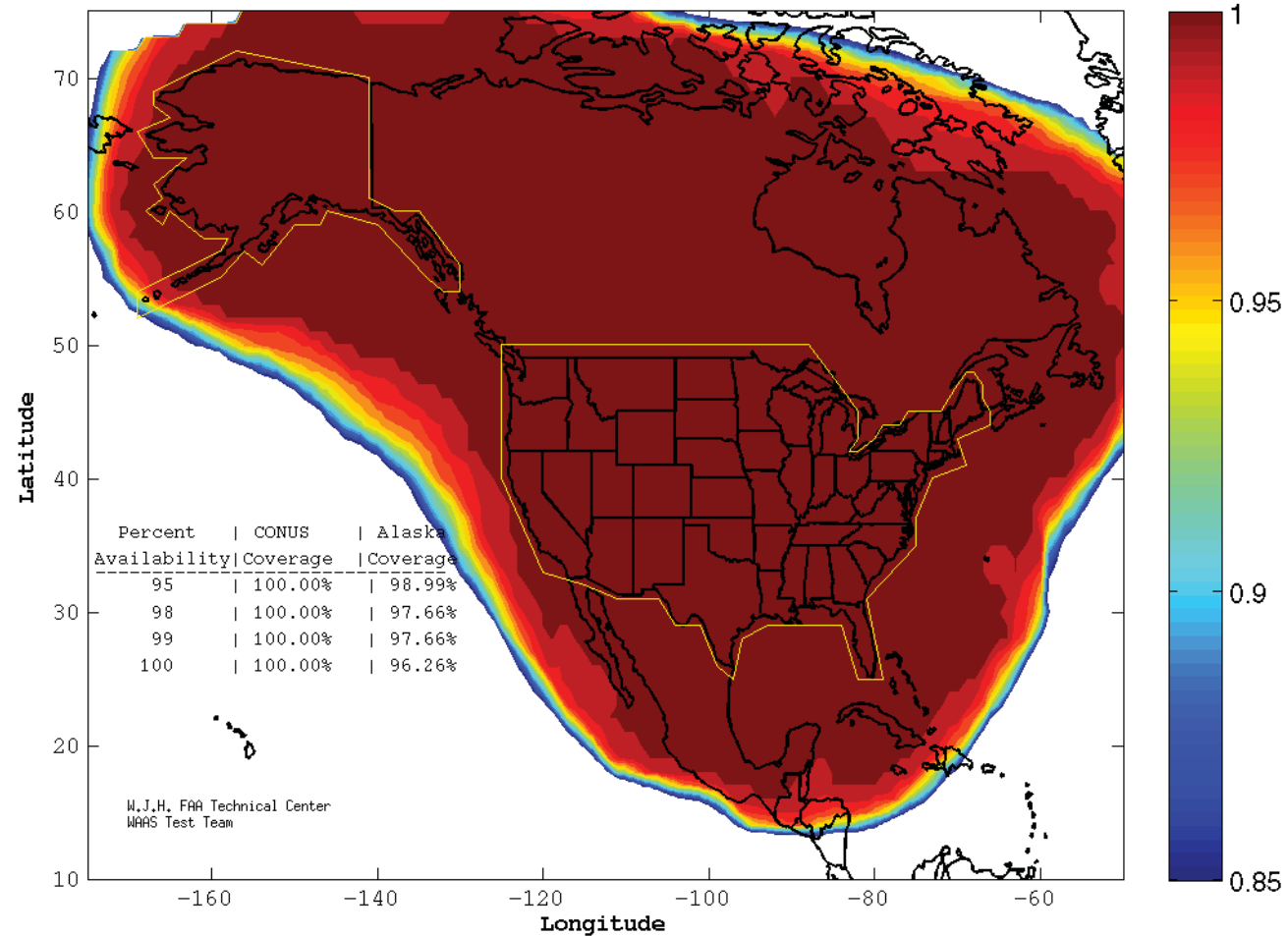
WAAS Interpretation

- Events handled case by case
- Events that are rare and random may take advantage of an *a priori*
- Deterministic events must be monitored or treated as worst-case
- Events that are observable must be detected (if risk $> 10^{-7}$)
- Must account for worst-case undetected events



Nominal WAAS Vertical Guidance Performance

WAAS LPV Coverage Contours
 04/22/11
 Week 1632 Day 5



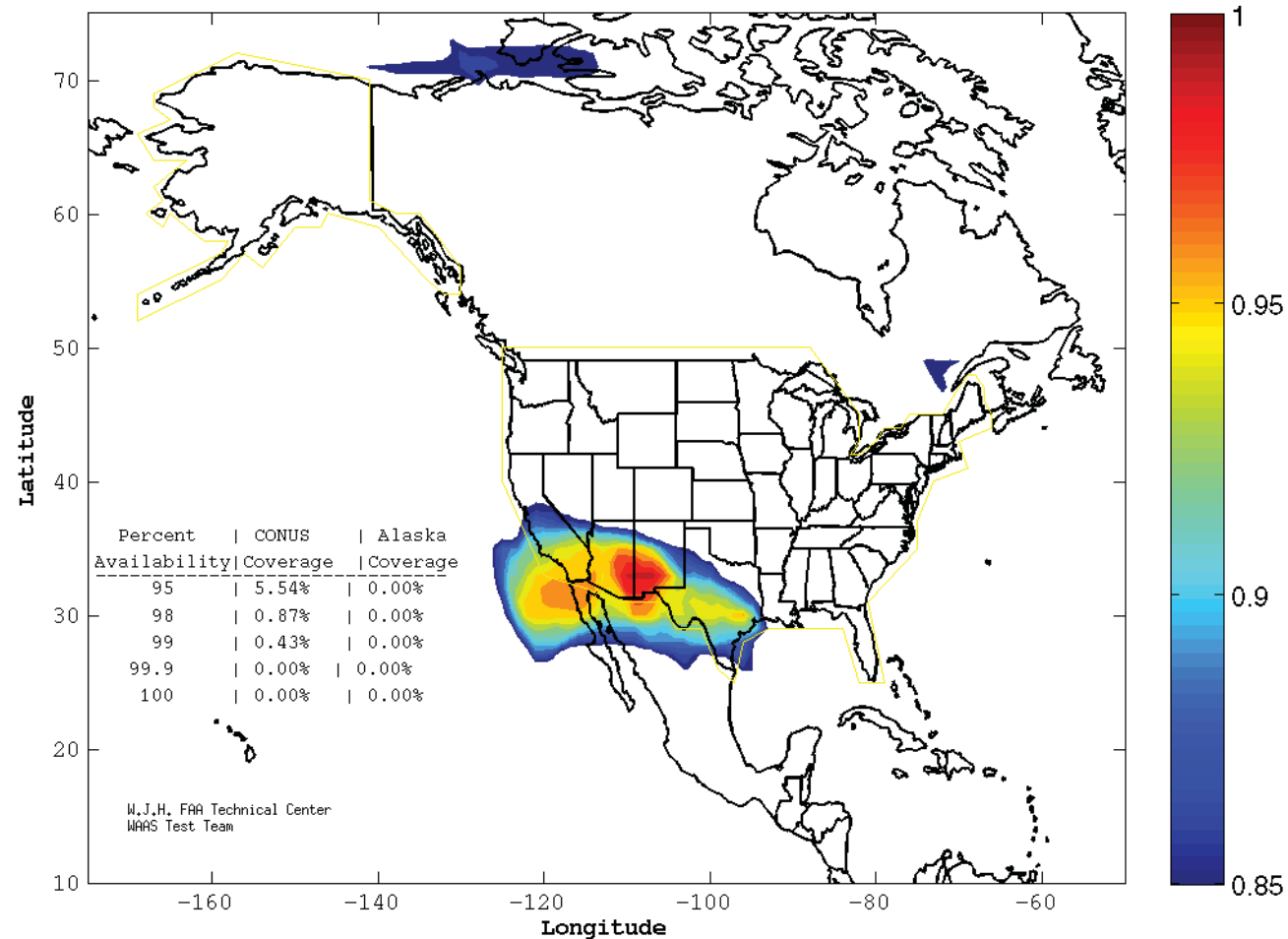
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Vertical Guidance with Major Ionospheric Disturbance

WAAS LPV Coverage Contours
10/25/11
Week 1659 Day 2



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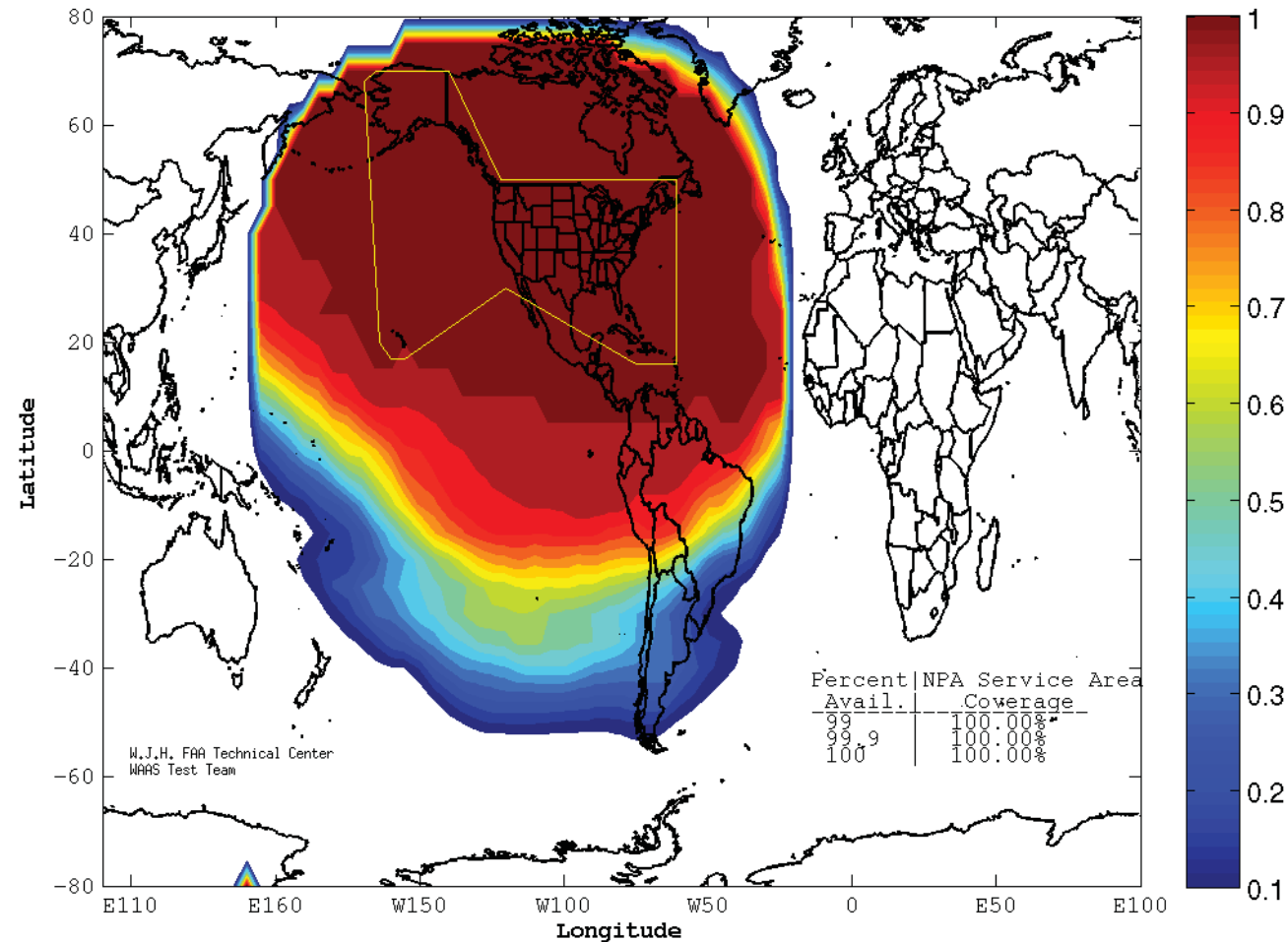


Nominal WAAS Horizontal Guidance Performance

WAAS RNP 0.1 Coverage Contours

04/22/11

Week 1632 Day 5



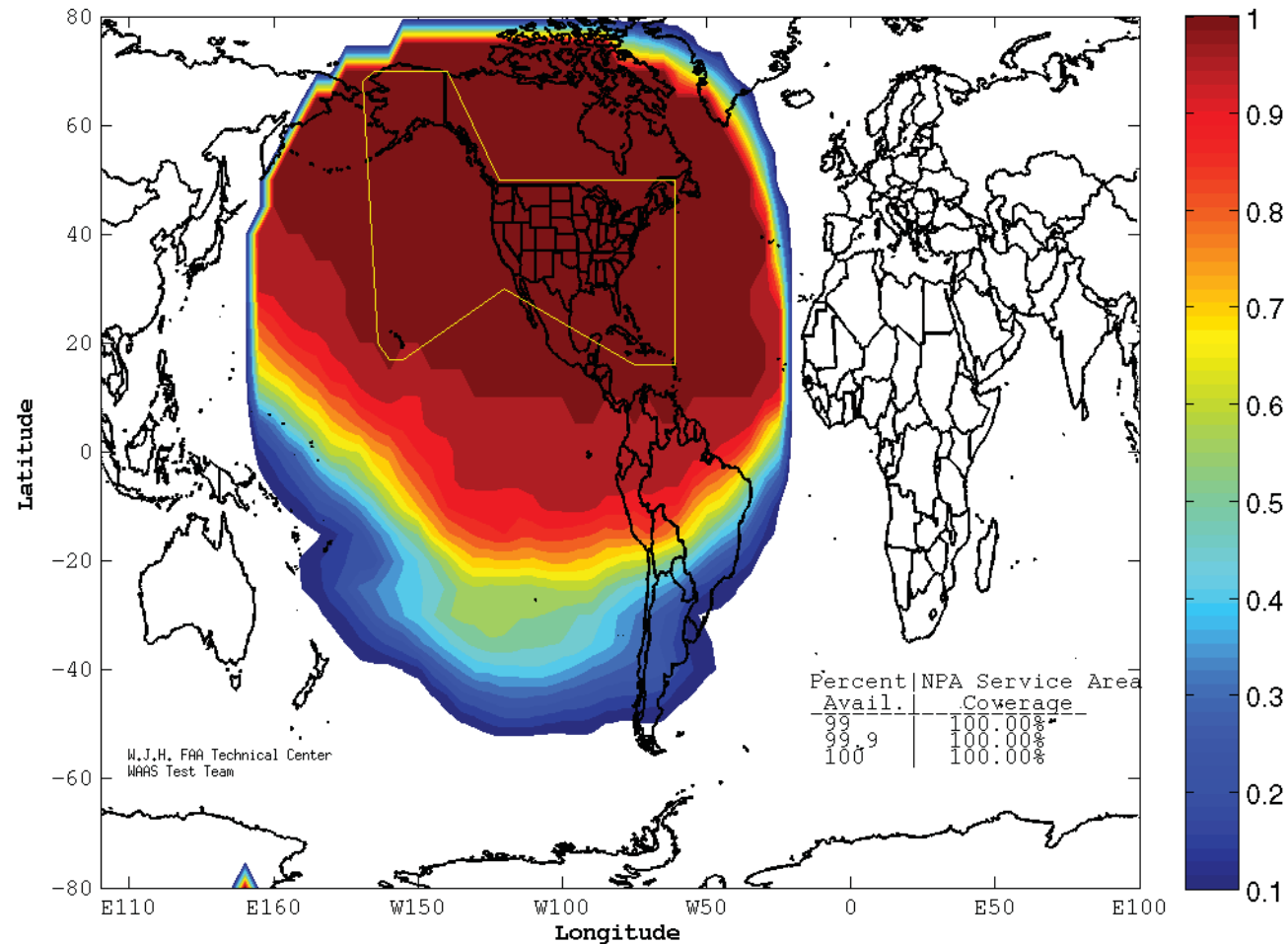
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Horizontal Guidance in Major Ionospheric Disturbance

WAAS RNP 0.1 Coverage Contours
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