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Preparatory School to the Winter College on Optics: Fundamentals of Photonics - Theory, Devices and

3 - 7 February 2014

Introduction to nonlinear optics

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In general ∞ $(3\pi v) \times (3\pi v) \times (3\pi$ $S(X) \longrightarrow V(X)$ $\widehat{S}(X) \longrightarrow \widehat{V}(X) = \widehat{S}(X) + (X)$ On the other hand: $S(x) = \int S(x') S(x-x') dx' - B > V(x) = \int S(x') G(x-x') dx$ = 5 + 6 (x)S(x) + G(x) Impulse response So the effect of a LSI system is always a convolution, Which in Fourier space 15 a product. Therefore \$xxx G(X)=H(1)/ The system acts as a blur, or equivalently, as a Fourier filter. Examples: { Low pass | High pass | DC removal | derivatives (including fractional") | combination of images

n(x) HAMAMA Noise · Fourier transform $f_{\text{vail}}(x) = \widetilde{N}(v)$ often, we do not know in, but we do know voughly how it behaves $\langle |\tilde{n}(v)| \rangle = S_n(v)$ power spectrum of the noise. average over many "realizations" $= \left(\left(\left(N^*(x') \hat{N}(V) e^{i 2\pi V(x+x')} \right) dV dx' \right)^*$ $= \left(\left(N^*(x) \right) \left(\hat{n}(v) e^{i 2 \pi i v (x + x')} dv dx' \right) = \left(\left(N^*(x) n \left(x' + x' \right) dx' \right) \right)$ $f_{x \rightarrow v} A_n(x) = S_n(v)$ Wiener-Khinchin theorem. Examples of $A_n(x) \approx \delta(x)$, $S_n(V) \approx constant$

If Sn(V) xi 1 , o(x < 2 usually x≈1.

Noise filtering & deconvolution Consider a noisy system, where

$$V(x) = G * S(x) + N(x)$$

Vesponse | Signal noise | Impulse response

we measure V(x), we know G(x) (system). We do not know n(x) but know its statistics $A_n(x)$. We want to estimate S(x)

In Former space: $\tilde{r}(V) = H(V)\tilde{s}(V) + \tilde{n}(V)$

Propose estimate Ŝ(V) = W(V) r(V) filter.

The total error is
$$\mathcal{E} = \left(|\hat{S}(v) - \tilde{S}(v)|^2 dv = \left(|WH\tilde{S} + W\tilde{n} - \tilde{S}|^2 dv \right) \right) \\
= \left(|(WH - 1)\tilde{S} + W\tilde{n}|^2 dv \right)$$