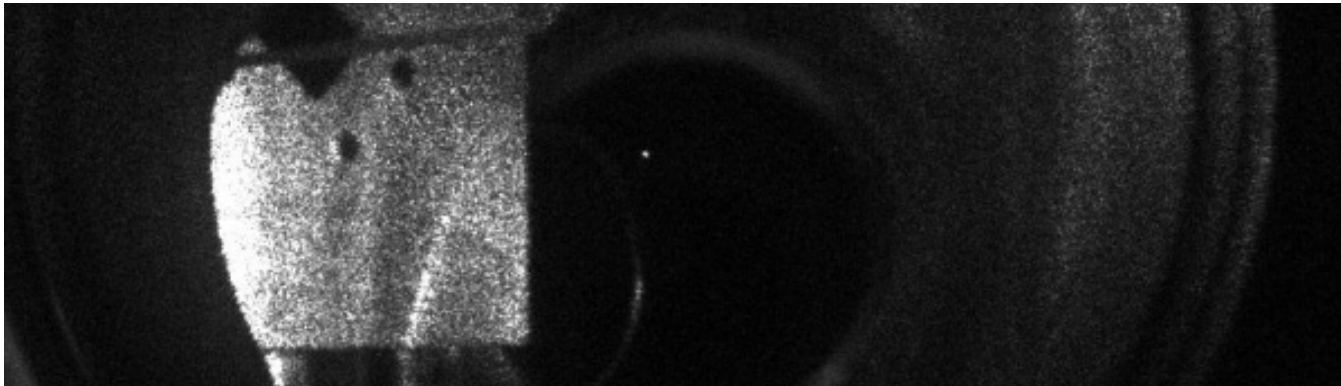


Detecting short-range forces and gravitational waves using resonant sensors

A. Geraci, University of Nevada, Reno



Frontiers of New Physics:
Colliders and Beyond
ICTP
June 27, 2014



Resonant Sensors

Techniques

Mechanical sensors

High Q Mechanical Oscillators
-Cantilevers
-Optically trapped dielectrics

Spin Resonance

Nuclear Magnetic Resonance
-Hyperpolarized gases or liquids

New Physics

Gravitational Inverse Square Law violations

- Moduli
- Large Extra Dimensions
- Dilatons

Gravitational Waves

Spin-dependent forces

- Axions

Outline

- Testing gravity at the micron length scale

A. Geraci, S. Papp, and J. Kitching, Phys. Rev. Lett. 105, 101101 (2010).

- Detecting high frequency gravitational waves

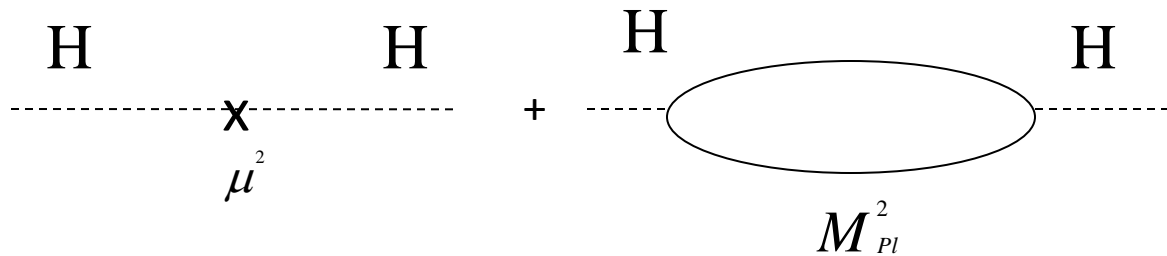
A. Arvanitaki and A. Geraci, Phys. Rev. Lett. 110, 071105 (2013).

- Searching for axion-mediated short range forces by NMR

A. Arvanitaki and A. Geraci, arxiv: 1403.1290

Physics beyond the Standard Model

- One reason to expect: **hierarchy problem**
Standard Model, as is, requires extreme fine tuning



Possible Solutions:

1) **Supersymmetry (4-d)**

2) **Large Extra Dimensions**

Exotic particles e.g.
(gravitationally coupled
light moduli from string theory)

Particles (vectors or scalars)
residing in the bulk of large
extra dimensions

Either case \rightarrow New physics below a millimeter

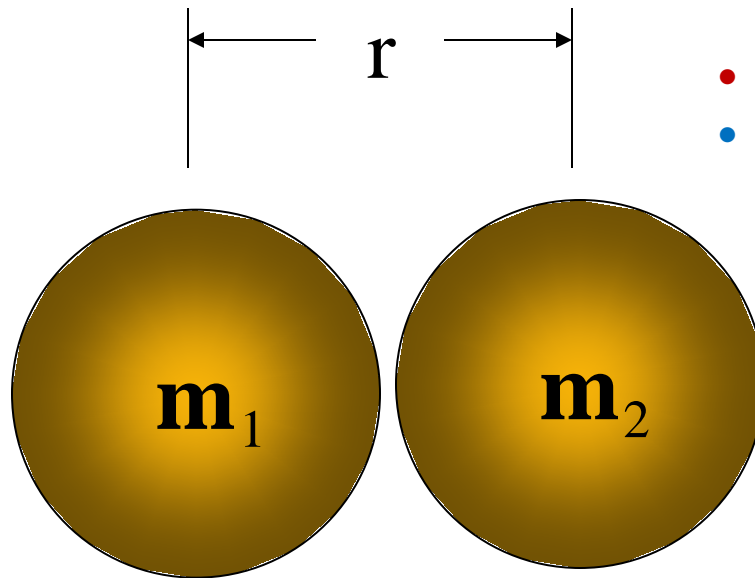
Testing gravity at short range

$$V_N = -G \frac{m_1 m_2}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$

Exotic particles (new physics)

$$\lambda < 1 \text{ mm}$$

- Supersymmetry
- Large extra dimensions

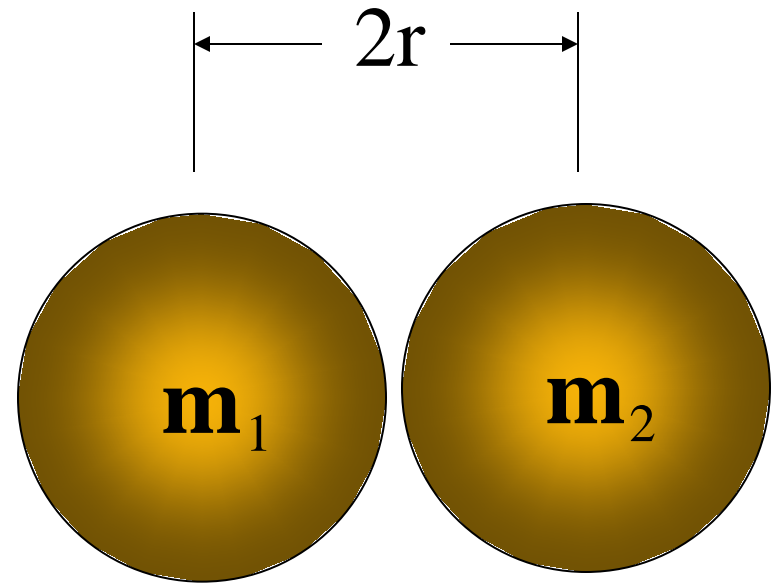


Experimental challenge: scaling of gravitational force

$$V_N = -G \frac{m_1 m_2}{r}$$

$$F_N = G_N \frac{\rho^2 (4\pi r^3 / 3)^2}{4r^2} \sim G_N \rho^2 r^4$$

$$F_N \cong 0.1 r^4 \quad \text{for } \rho \sim 20 \text{ gr/cm}^3$$



In the range of experimental interest:

$$r \sim 10 \mu\text{m} ;$$

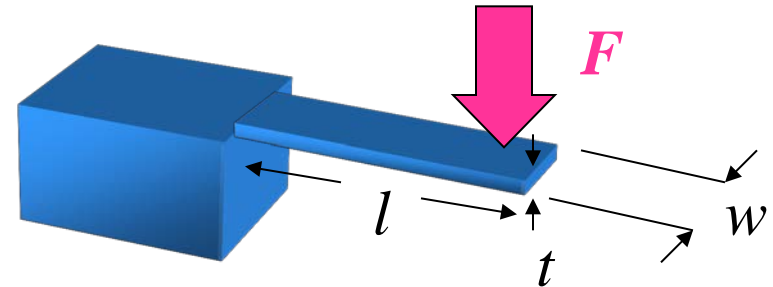
$$F_N \sim 10^{-21} \text{ N}$$

Resonant force detection

- Cantilever is like a spring:

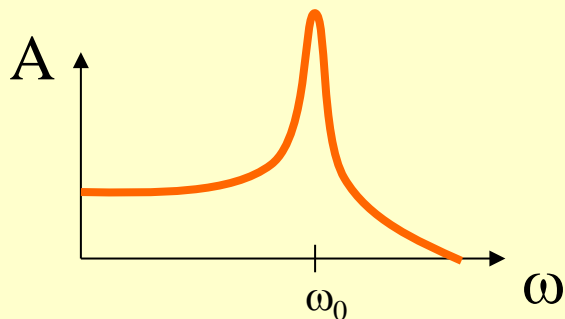
$$F = -Kx$$

$$\omega_0 = \sqrt{\frac{K}{m}}$$



Sinusoidal driving force

Amplitude:



$$A_{(\omega=0)} = \frac{F}{k}$$

Constant force

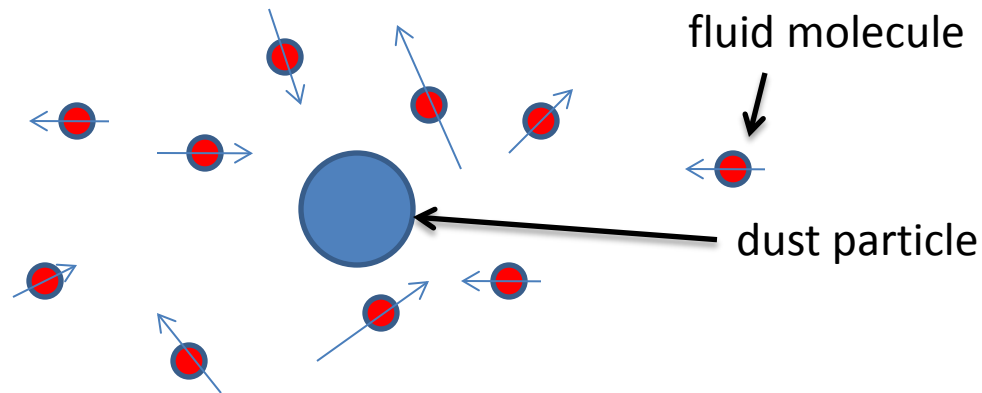
$$A_{(\omega=\omega_0)} = \frac{F}{k} Q$$

Driving force on resonance of cantilever ω_0

Q can be very large >100,000

Fundamental limitation: thermal noise

Brownian motion – random “kicks” given to particle due to thermal bath



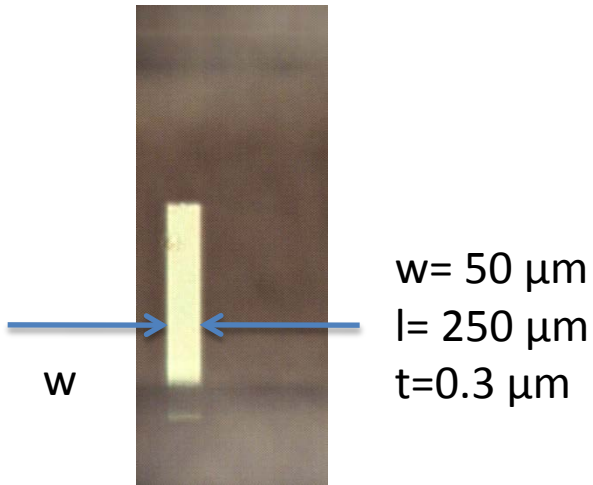
- Random “kicks” are given to cantilever due to finite T of oscillator

$$\frac{1}{2}k\langle x^2 \rangle = \frac{1}{2}k_B T$$



$$F_{\min} = \left(\frac{4kk_B T b}{Q\omega_0} \right)^{1/2}$$

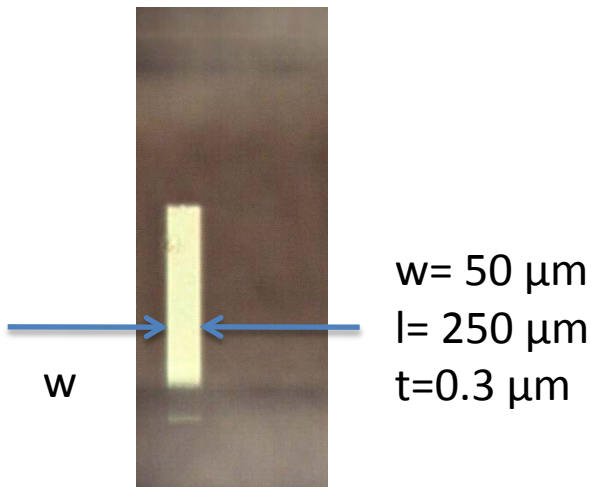
Fundamental limitation: thermal noise



Silicon Cantilevers:

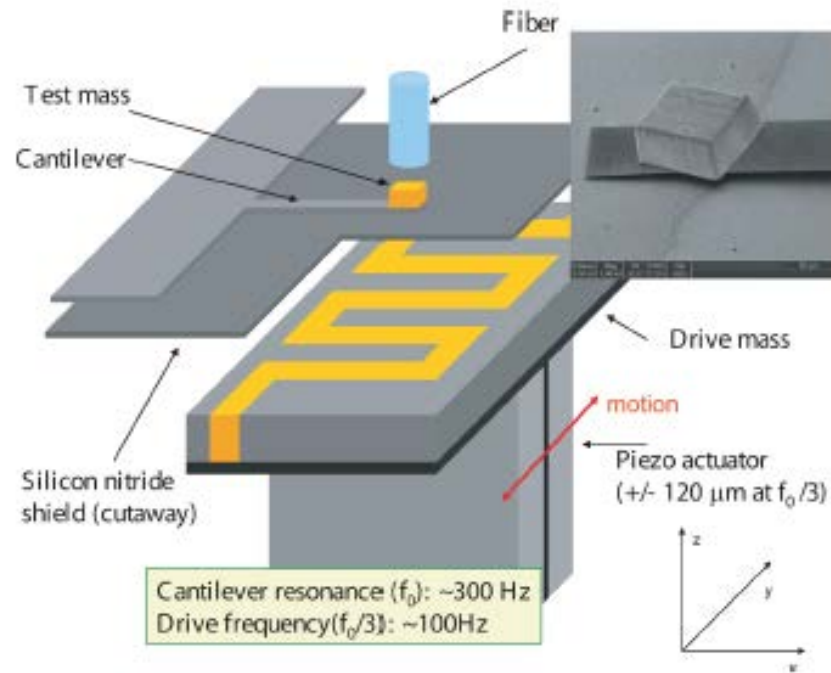
$F_{min} \sim 10 \times 10^{-18} \text{ N}/\sqrt{\text{Hz}}$
at 4 K at $Q=10^5$

Fundamental limitation: thermal noise



Silicon Cantilevers:

$F_{\min} \sim 10 \times 10^{-18} \text{ N}/\sqrt{\text{Hz}}$
 at 4 K at $Q = 10^5$



Best Yukawa constraints at $\sim 10 \mu\text{m}$ range:

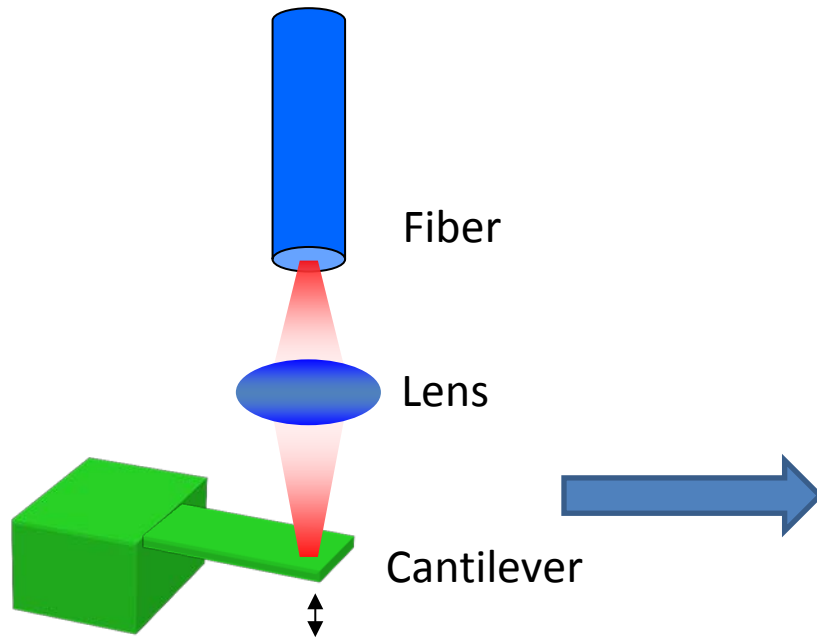
A.A. Geraci, S.J. Smullin, D. M. Weld, J. Chiaverini, and A. Kapitulnik, *Phys. Rev. D* 78, 022002 (2008).

$$F_{\min} = \sqrt{\frac{4k k_B T b}{\omega_0 Q}}$$

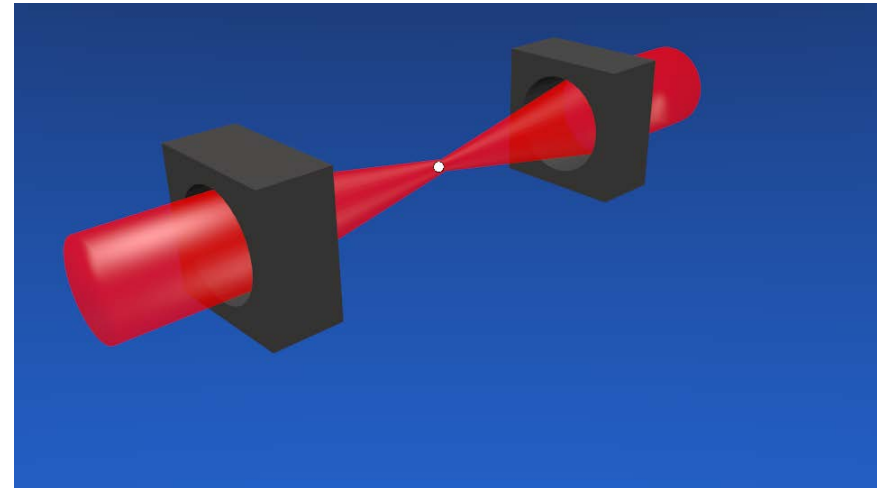
To improve sensitivity:

- Make cantilever small
- Lower temperature
- Raise the quality factor

Improving Q?



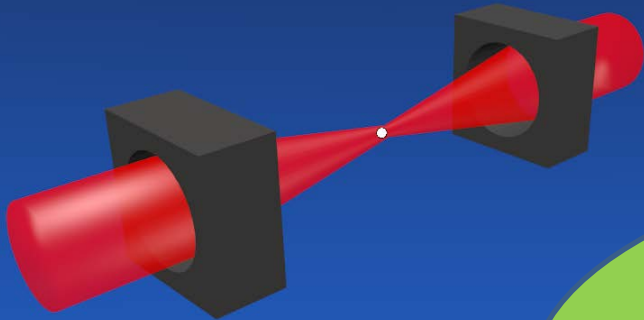
Levitate the force sensor!



Limitations on Q: Clamping, surface imperfections, internal materials losses

CM motion decoupled from environment –
no clamping, materials losses

Optically-levitated sensors



Pressure-limited damping

$$\frac{dp}{dt} = -\gamma_g \frac{p}{2} \qquad \frac{\gamma_g}{2} = \left(\frac{8}{\pi} \right) \frac{P}{\bar{v} r \rho}$$

$P=10^{-10}$ Torr, $r=0.15 \mu\text{m}$, $\omega/2\pi=10$ kHz, $Q=10^{12}$!

$$F_{\min} = \left(\frac{4kk_B T b}{Q\omega_0} \right)^{1/2}$$

$$Q \sim 10^{12}$$

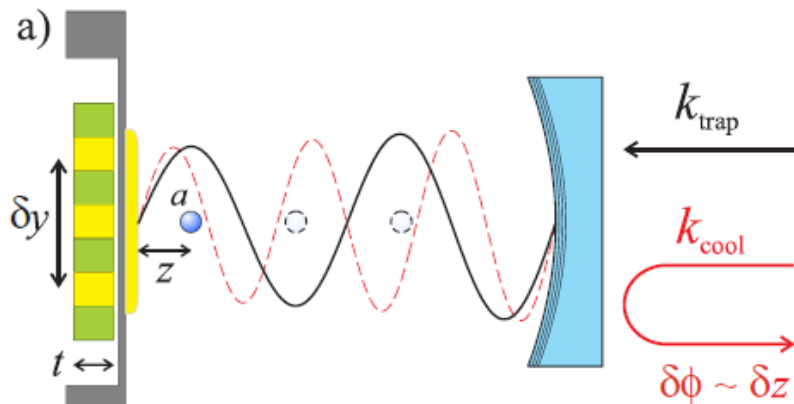
$$T \sim 300$$

$$\omega_0/2\pi \sim 10^5$$

$$m \sim 10^{-(14-17)} \text{ kg}$$

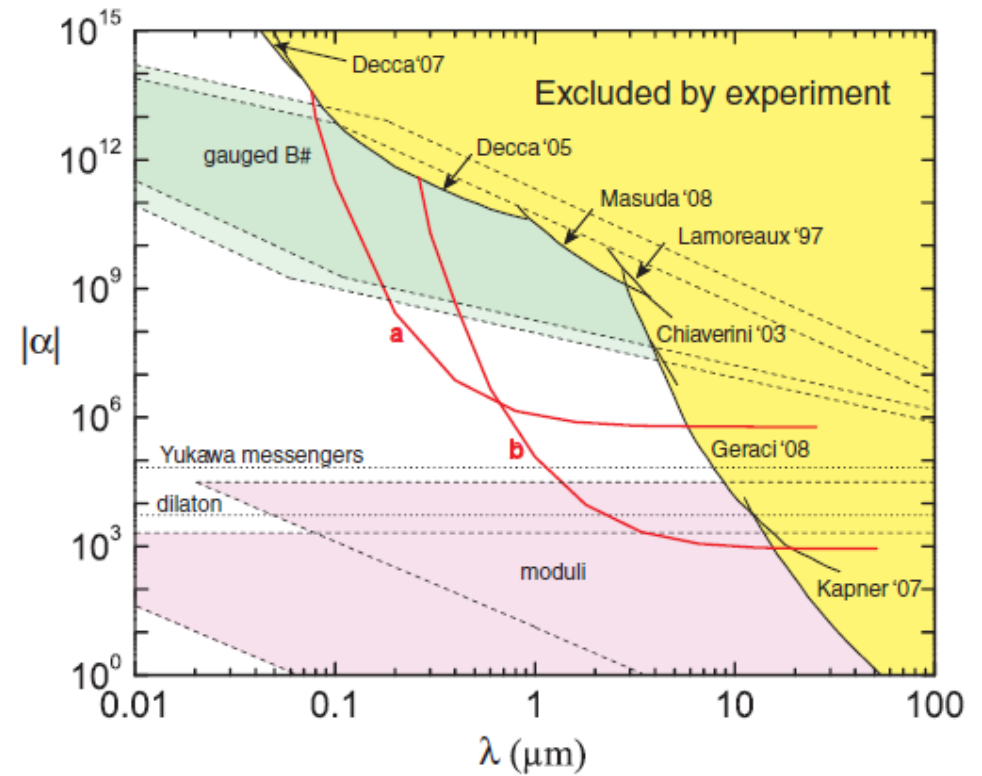
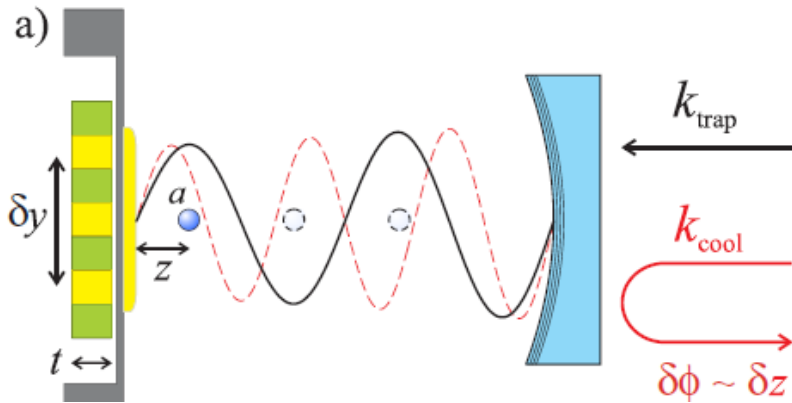
$$\rightarrow F \sim 10^{-21} \text{ N/Hz}^{1/2}$$

Micron-scale gravity test experiment



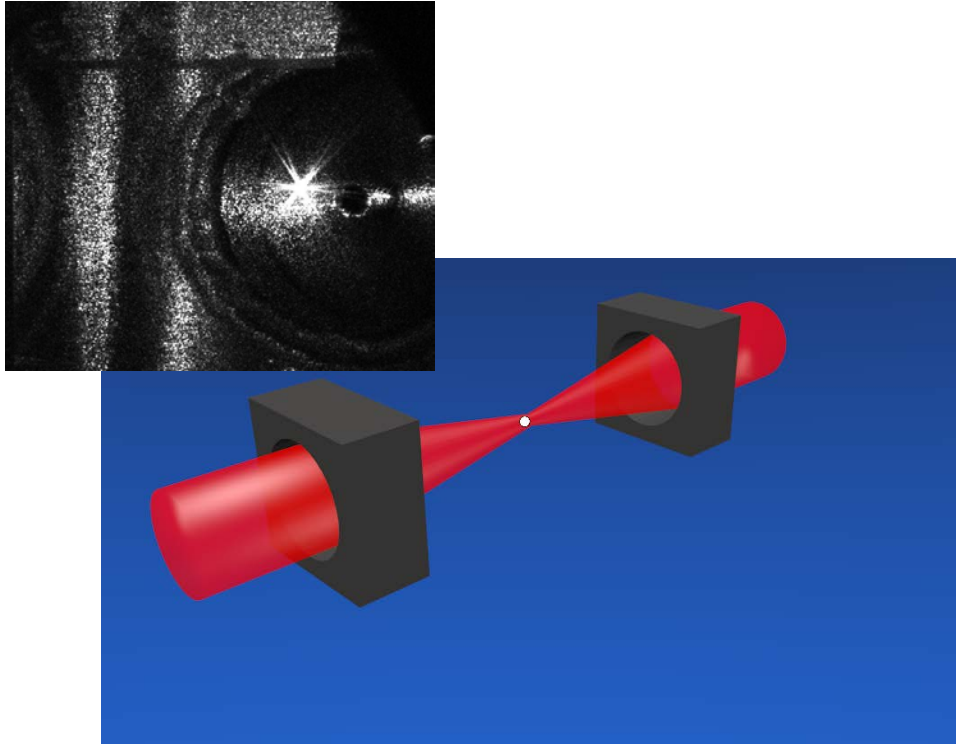
Micron-scale gravity test experiment

$$V_N = -G \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$

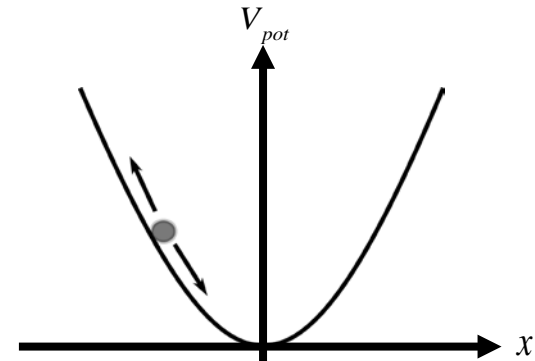
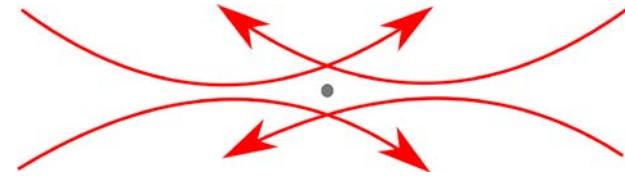


10^6 improvement possible at $1\mu\text{m}$ length scale

Dual beam dipole trap

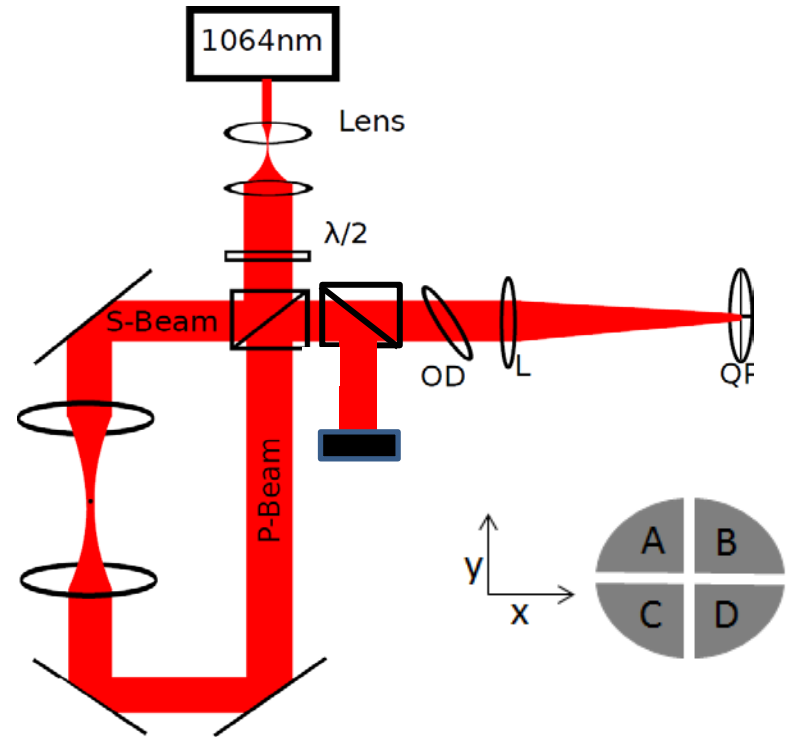
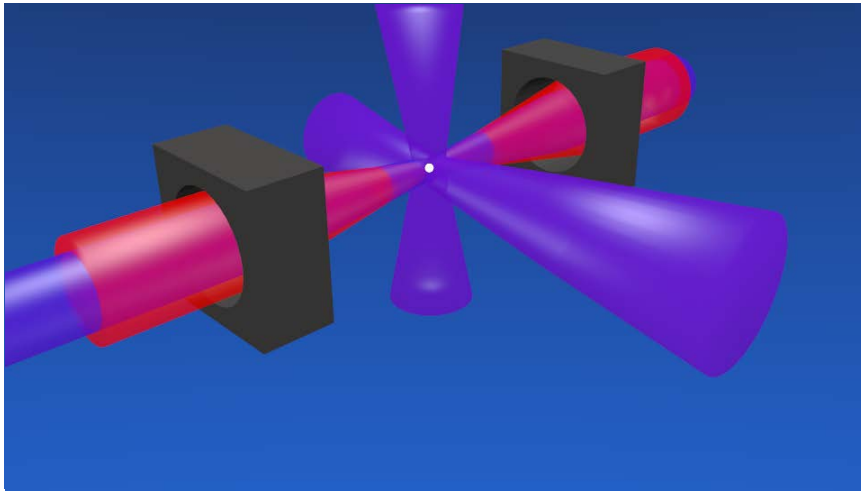


Our Trap Configurations



- Trap frequency ~ 10 kHz
- High Q-factor $> 10^{12}$
- Need cooling!

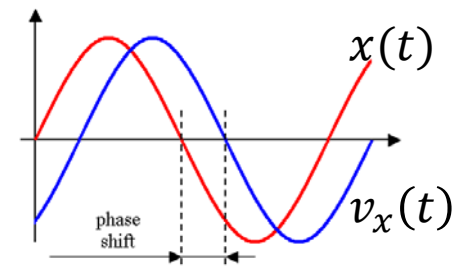
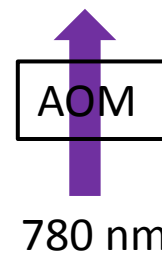
Laser cooling of a microsphere



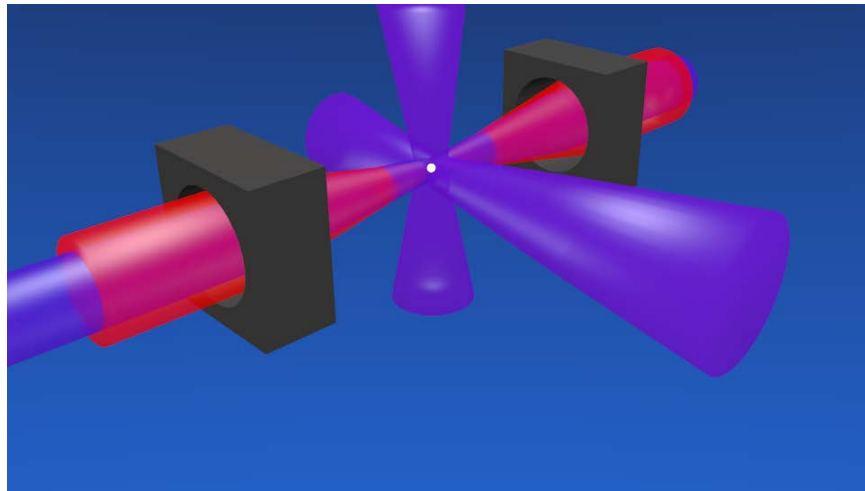
$$F_{\min} = \sqrt{\frac{4kK_B T B}{\omega_0 Q}}$$

$$Q_{\text{eff}} = \frac{Q_0 \Gamma_0}{\Gamma_0 + \Gamma_{\text{cool}}}$$

$$T_{\text{eff}} = \frac{T_0 \Gamma_0}{\Gamma_0 + \Gamma_{\text{cool}}}$$



Laser cooling of a microsphere



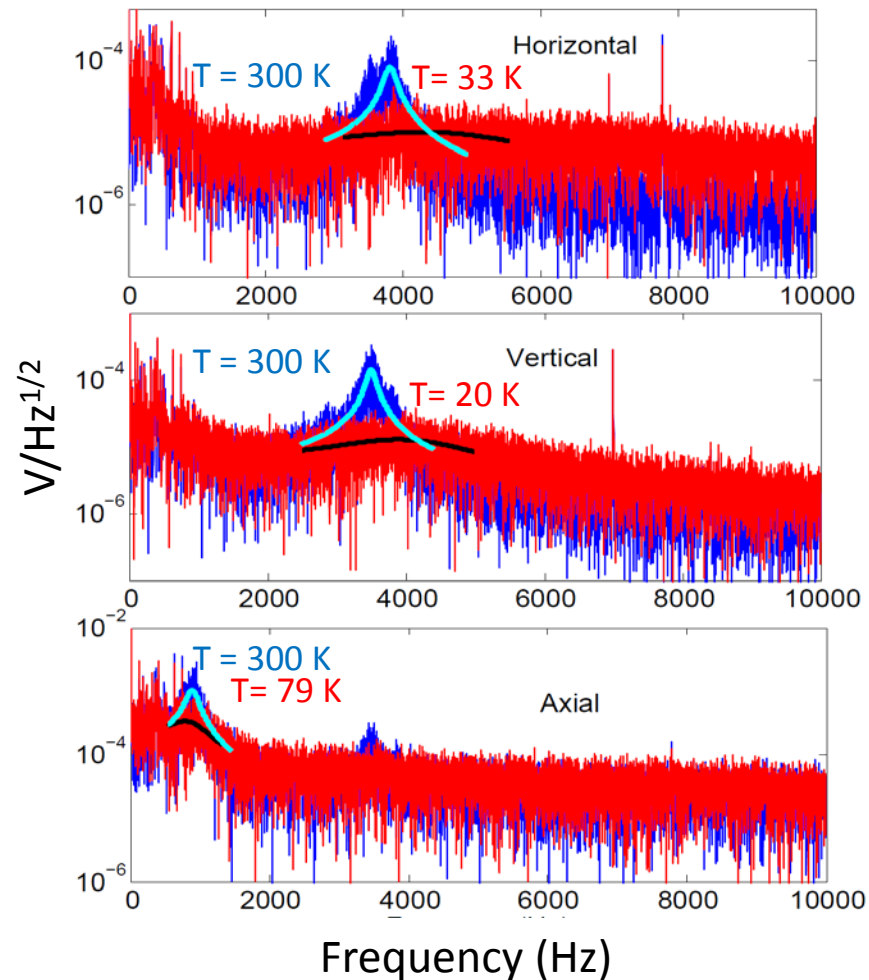
$Q = 38$
 $T = 300\text{K}$

$\Rightarrow F_{\min} \sim 50 \times 10^{-17} \text{ N} / \sqrt{\text{Hz}}$

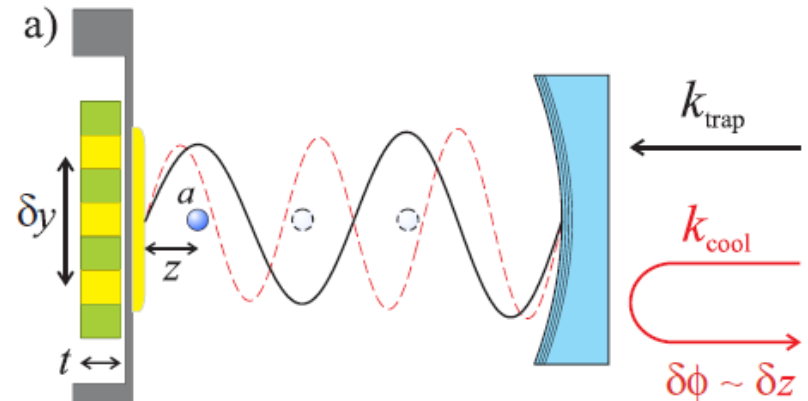
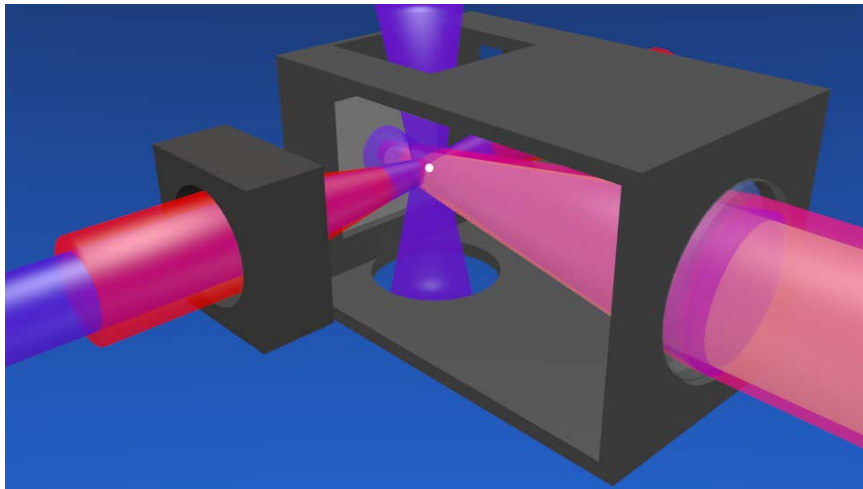
Goal at UHV: $F_{\min} \sim 10^{-21} \text{ N} / \sqrt{\text{Hz}}$

Preliminary

3D Feedback cooling at 2 mbar

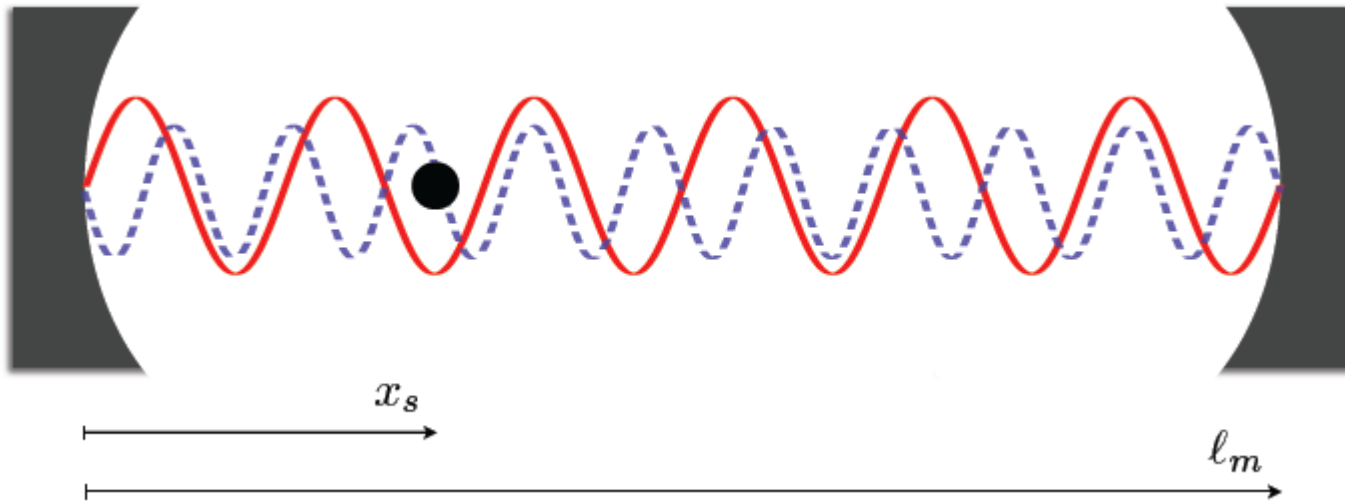


Cavity Trapping and cooling



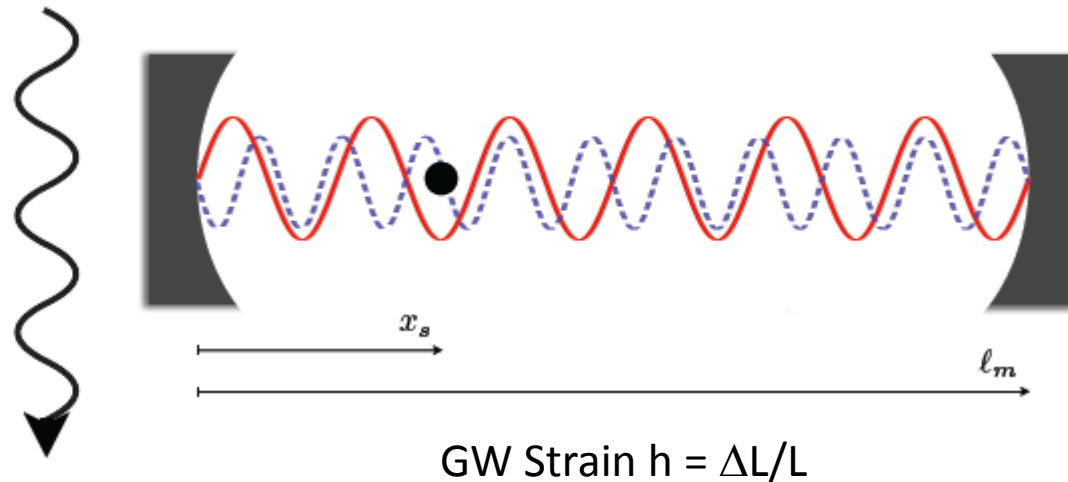
1596nm beam to trap a bead at its antinode
1064nm beam to cavity cool the CM of bead

Gravitational Wave Detection



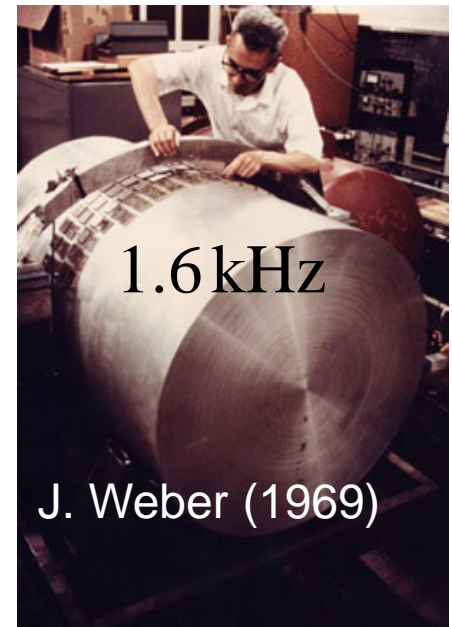
- Fused silica sphere ($r = 150\text{nm}$) or disc ($t = 500\text{nm}$, $r = 75\ \mu\text{m}$)
In an optical cavity of size 10-100 m
- One laser to **trap**, one to **cool** and measure sensor position

Gravitational Wave Detection

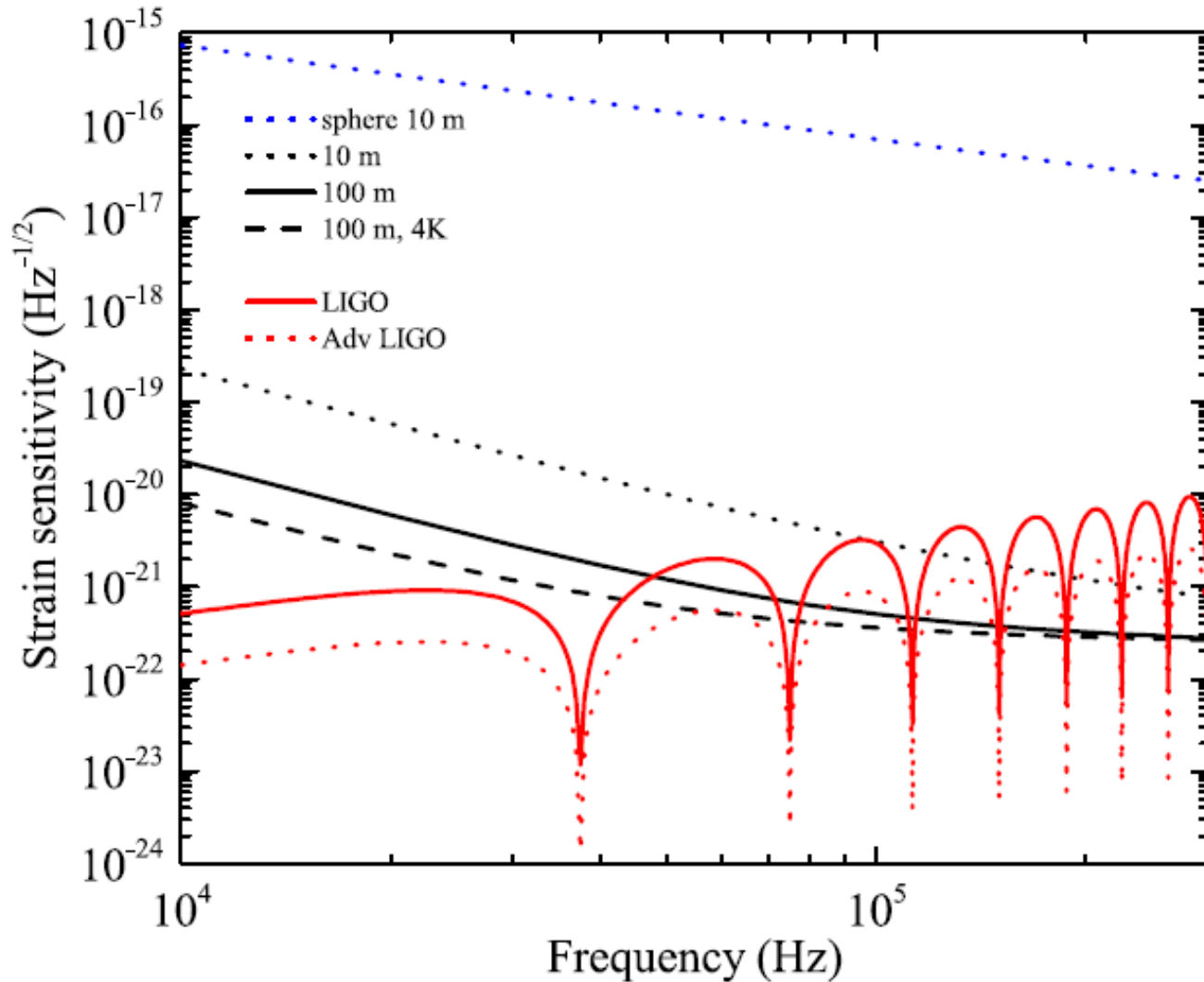


- Laser intensity changed to match trap frequency to GW frequency
- For a 100m cavity, $h \sim 10^{-22} \text{ Hz}^{-1/2}$ at high frequency (100kHz) ($a = 75 \text{ } \mu\text{m}$, $d = 500 \text{ nm}$ disc)
- Limited by thermal noise in sensor (not laser shot noise)

Position measurement \rightarrow force measurement



GW Strain Sensitivity



— 100 m

Size scale:



LIGO

GW sources at high-frequency

- Astrophysical Sources

Natural upper bound on GW frequency
inverse BH size ~ 30 kHz

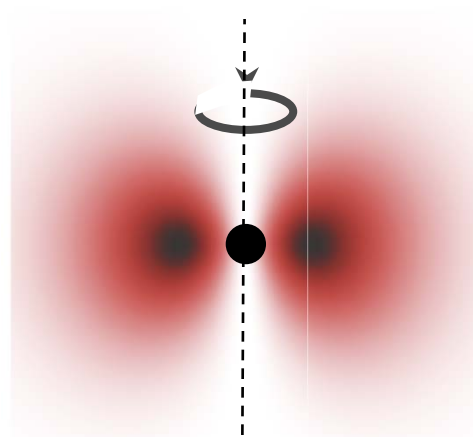
- Beyond standard model physics

- QCD Axion \rightarrow Annihilation to gravitons in
cloud around Black holes

A. Arvanitaki *et al.*, PRD, 81, 123530 (2010)

A. Arvanitaki *et al.*, PRD 83, 044026 (2011)

Black hole superradiance



- String cosmology

R. Brustein *et al.*, Phys. Lett. B, 361, 45 (1995)

- The unknown?

Outline

- Testing gravity at the micron length scale

A. Geraci, S. Papp, and J. Kitching, Phys. Rev. Lett. 105, 101101 (2010).

- Detecting high frequency gravitational waves

A. Arvanitaki and A. Geraci, Phys. Rev. Lett. 110, 071105 (2013).

- Searching for axion-mediated short range forces by NMR

A. Arvanitaki and A. Geraci, arxiv: 1403.1290

Axions

- Light pseudoscalar particles in many theories Beyond Standard model
- Peccei-Quinn Axion (QCD) solves strong CP-problem
- Dark matter candidate

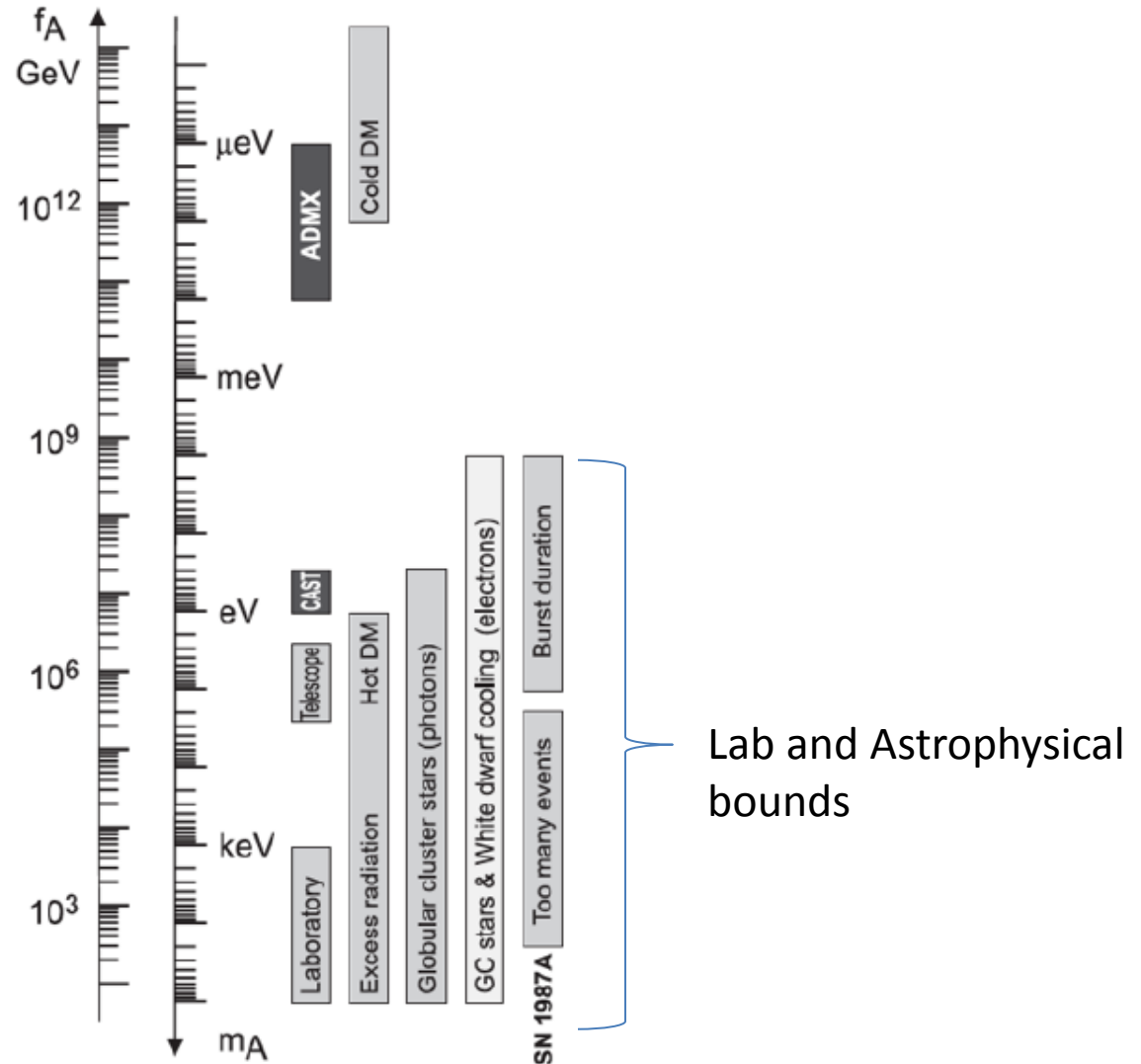


- Also mediates spin-dependent forces between matter objects at short range (down to $30 \mu\text{m}$)

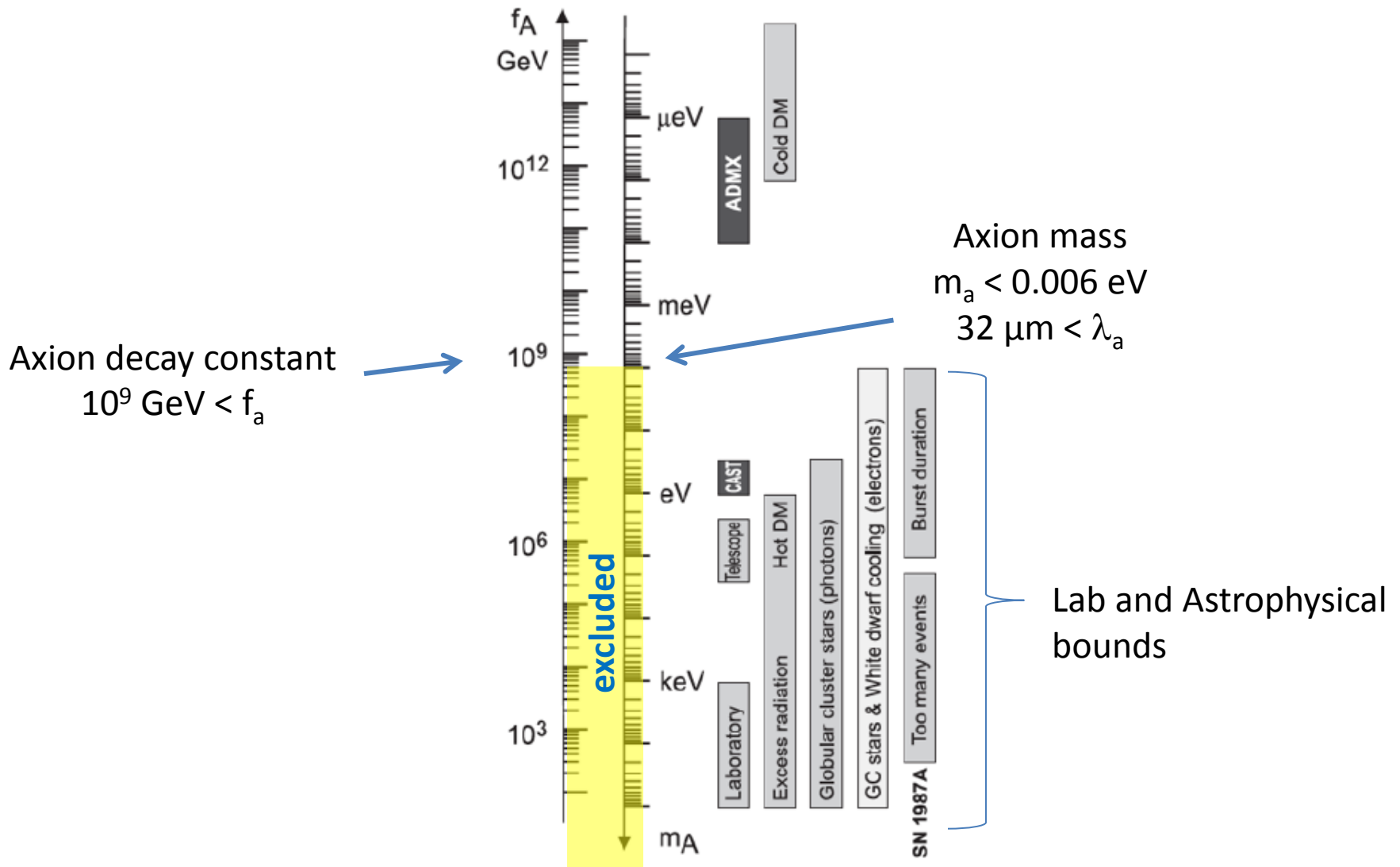
→ Can be sourced locally

- R. D. Peccei and H. R. Quinn, Phys. Rev. Lett. 38, 1440 (1977);
- S. Weinberg, Phys. Rev. Lett. 40, 223 (1978);
- F. Wilczek, Phys. Rev. Lett. 40, 279 (1978).
- J. E. Moody and F. Wilczek, Phys. Rev. D 30, 130 (1984).

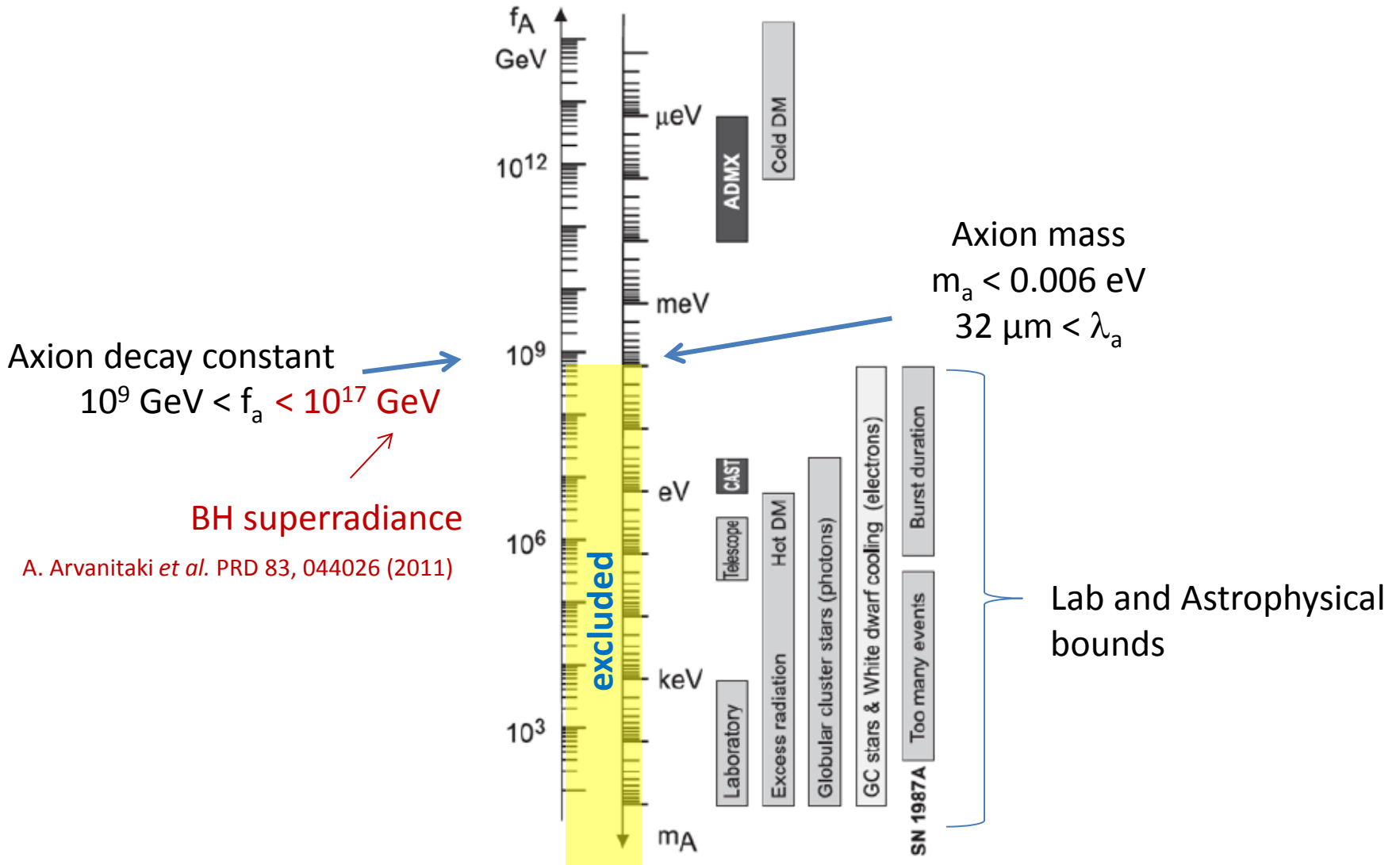
QCD Axion parameter space



QCD Axion parameter space

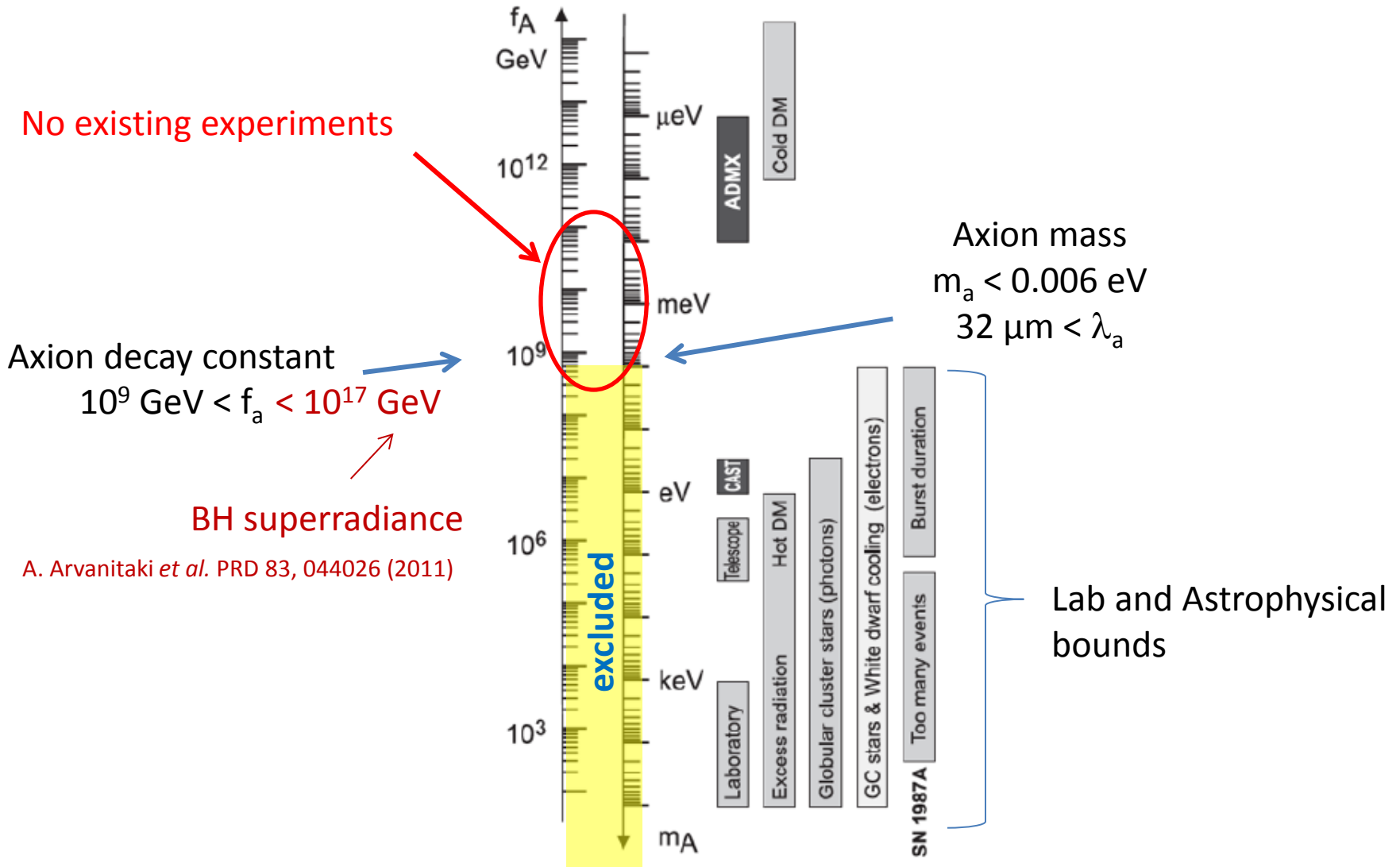


QCD Axion parameter space

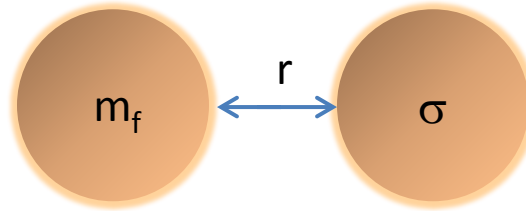


QCD Axion parameter space

- No existing experiments



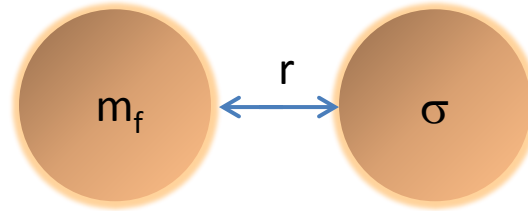
Spin-dependent forces



Monopole-Dipole axion exchange

$$U(r) = \frac{\hbar^2 g_s g_p}{8\pi m_f} \left(\frac{1}{r\lambda_a} + \frac{1}{r^2} \right) e^{-r/\lambda_a} (\hat{\sigma} \cdot \hat{r})$$

Spin-dependent forces



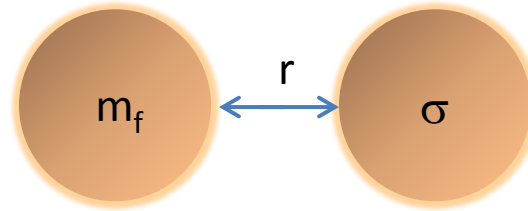
Monopole-Dipole axion exchange

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$$B_{\text{eff}} = \frac{1}{\gamma_f} \frac{\hbar g_s g_p}{4\pi m_f} \left(\frac{1}{r\lambda_a} + \frac{1}{r^2} \right) e^{-r/\lambda_a}$$

gyromagnetic ratio

Spin-dependent forces



Monopole-Dipole axion exchange

$$U(r) = \frac{\hbar^2 g_s g_p}{8\pi m_f} \left(\frac{1}{r\lambda_a} + \frac{1}{r^2} \right) e^{-r/\lambda_a} (\hat{\sigma} \cdot \hat{r}) \quad \equiv \mu \cdot B_{\text{eff}}$$

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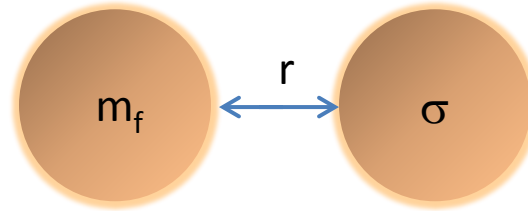
gyromagnetic ratio

Coupling constants

$$6 \times 10^{-27} \left(\frac{10^9 \text{ GeV}}{f_a} \right) < g_s < 10^{-21} \left(\frac{10^9 \text{ GeV}}{f_a} \right)$$

$$g_p = \frac{C_f m_f}{f_a} = C_f 10^{-9} \left(\frac{m_f}{1 \text{ GeV}} \right) \left(\frac{10^9 \text{ GeV}}{f_a} \right)$$

Spin-dependent forces



Monopole-Dipole axion exchange

$$U(r) = \frac{\hbar^2 g_s g_p}{8\pi m_f} \left(\frac{1}{r\lambda_a} + \frac{1}{r^2} \right) e^{-r/\lambda_a} (\hat{\sigma} \cdot \hat{r}) \quad \equiv \quad \mu \cdot B_{\text{eff}}$$

$$B_{\text{eff}} = \frac{1}{\gamma_f} \frac{\hbar g_s g_p}{4\pi m_f} \left(\frac{1}{r\lambda_a} + \frac{1}{r^2} \right) e^{-r/\lambda_a}$$

Coupling constants

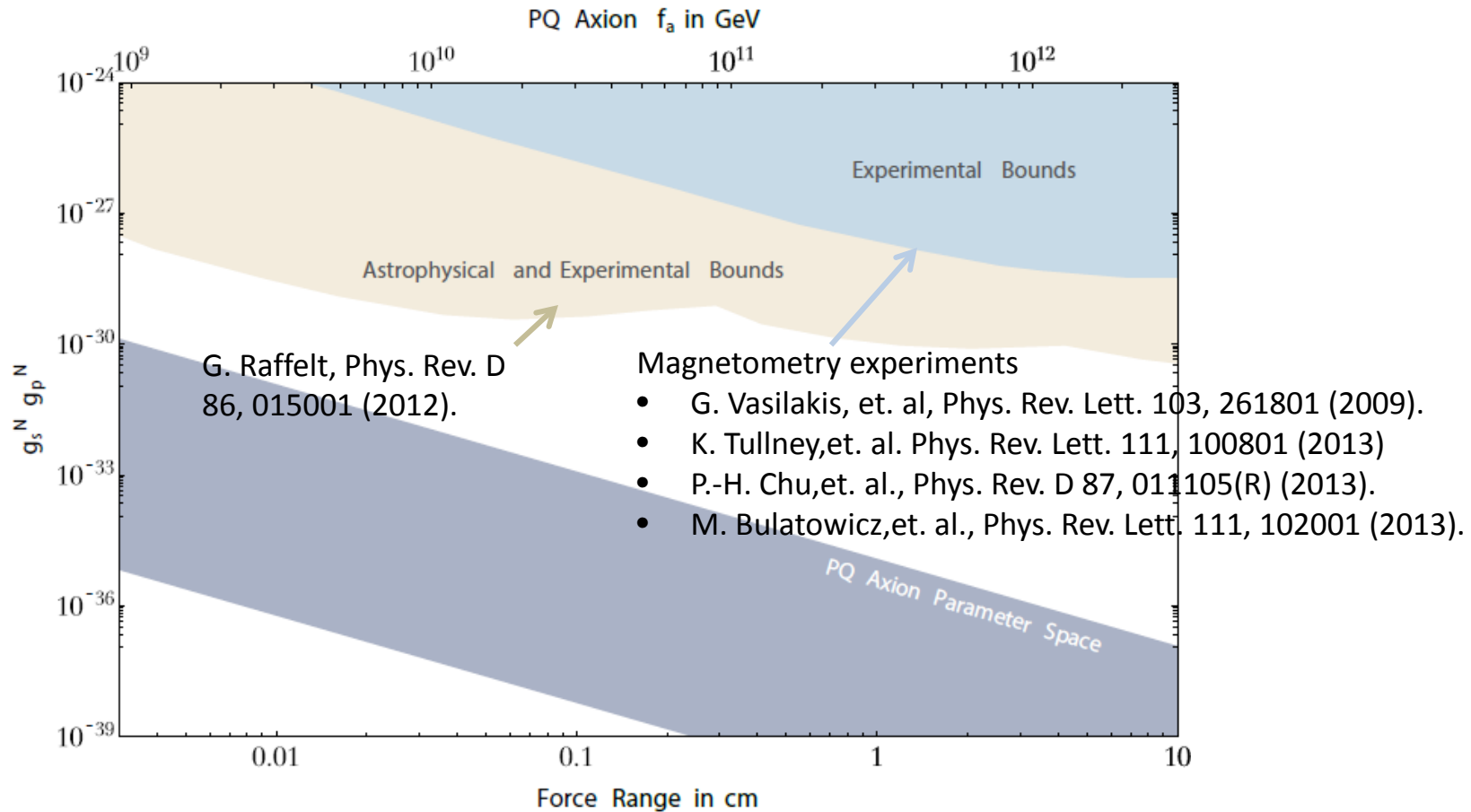
$$6 \times 10^{-27} \left(\frac{10^9 \text{ GeV}}{f_a} \right) < g_s < 10^{-21} \left(\frac{10^9 \text{ GeV}}{f_a} \right)$$

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gyromagnetic ratio

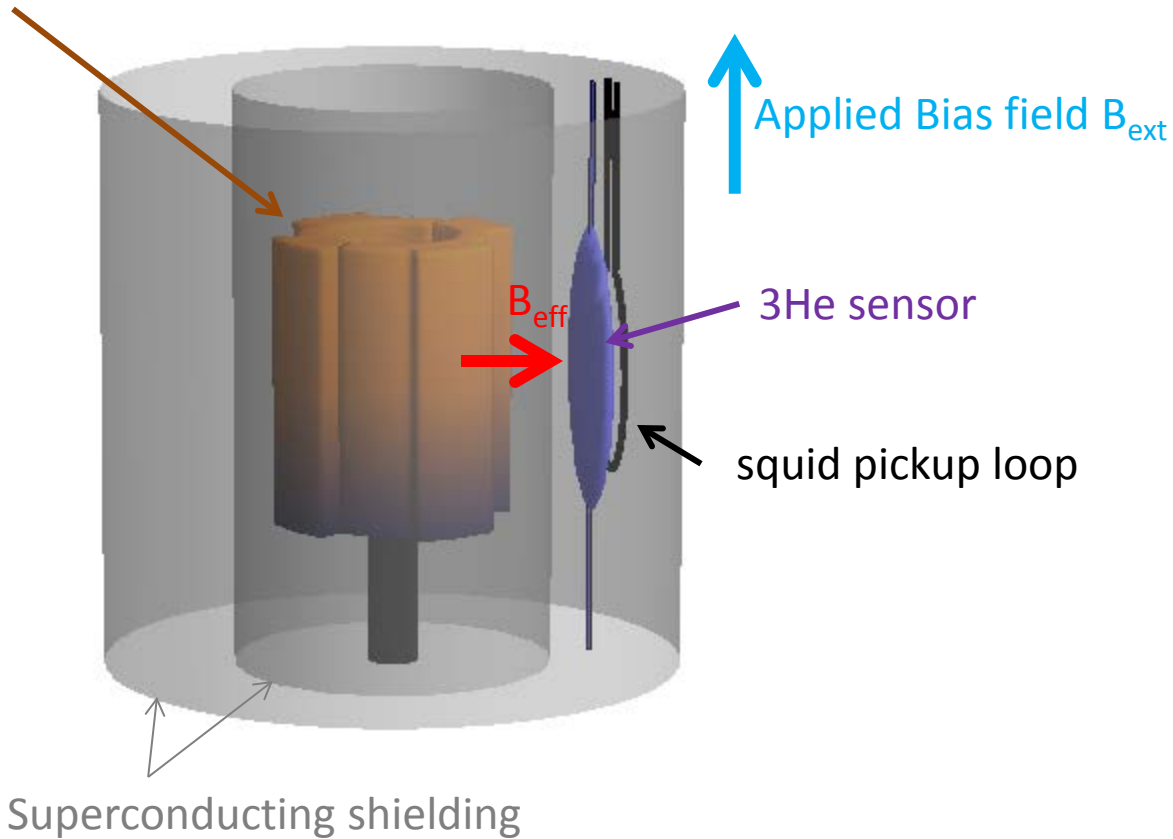
- Different than ordinary B field
- Does not couple to angular momentum
- Unaffected by magnetic shielding

Constraints on spin dependent forces



Concept for new experiment

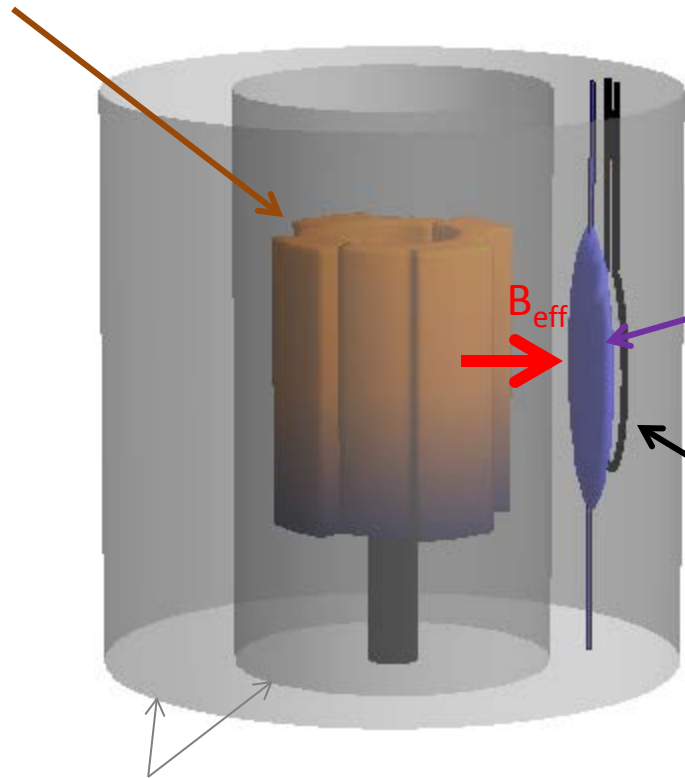
Rotating segmented cylinder sources B_{eff}



$$\omega = \frac{2\mu_N \cdot B_{\text{ext}}}{\hbar}$$

Concept for new experiment

Rotating segmented cylinder sources B_{eff}



Applied Bias field B_{ext}

$$\omega = \frac{2\mu_N \cdot B_{\text{ext}}}{\hbar}$$

3He sensor

$$M_x(t) \approx \frac{\hbar}{2} n_s \mu_N \gamma_N B_{\text{eff}} t \cos[\omega t]$$

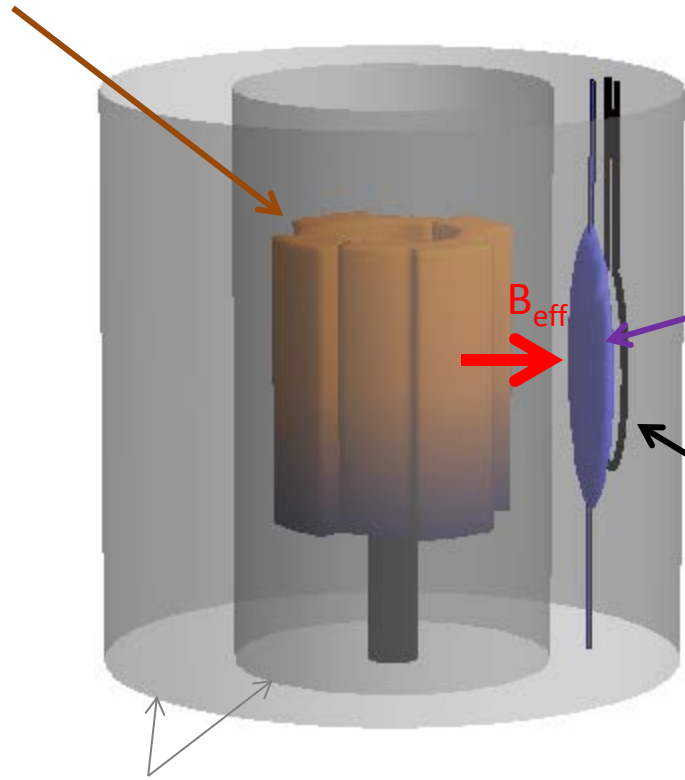
squid pickup loop

Spin density

Superconducting shielding

Concept for new experiment

Rotating segmented cylinder sources B_{eff}



Superconducting shielding

Applied Bias field B_{ext}

$$\omega = \frac{2\mu_N \cdot B_{\text{ext}}}{\hbar}$$

^3He sensor

$$M_x(t) \approx \frac{\hbar}{2} n_s \mu_N \gamma_N B_{\text{eff}} t \cos[\omega t]$$

squid pickup loop

Spin density

Limit: Transverse spin projection noise

$$B_{\text{min}} \approx p^{-1} \sqrt{\frac{2\hbar}{n_s \mu^3 \text{He} \gamma V T_2}} = 10^{-20} \frac{T}{\sqrt{\text{Hz}}} \times \left(\frac{1}{p}\right) \left(\frac{1 \text{ cm}^3}{V}\right)^{1/2} \left(\frac{10^{21} \text{ cm}^{-3}}{n_s}\right)^{1/2} \left(\frac{1000 \text{ sec}}{T_2}\right)^{1/2}$$

Sensitivity

Experimental parameters:

10 segments

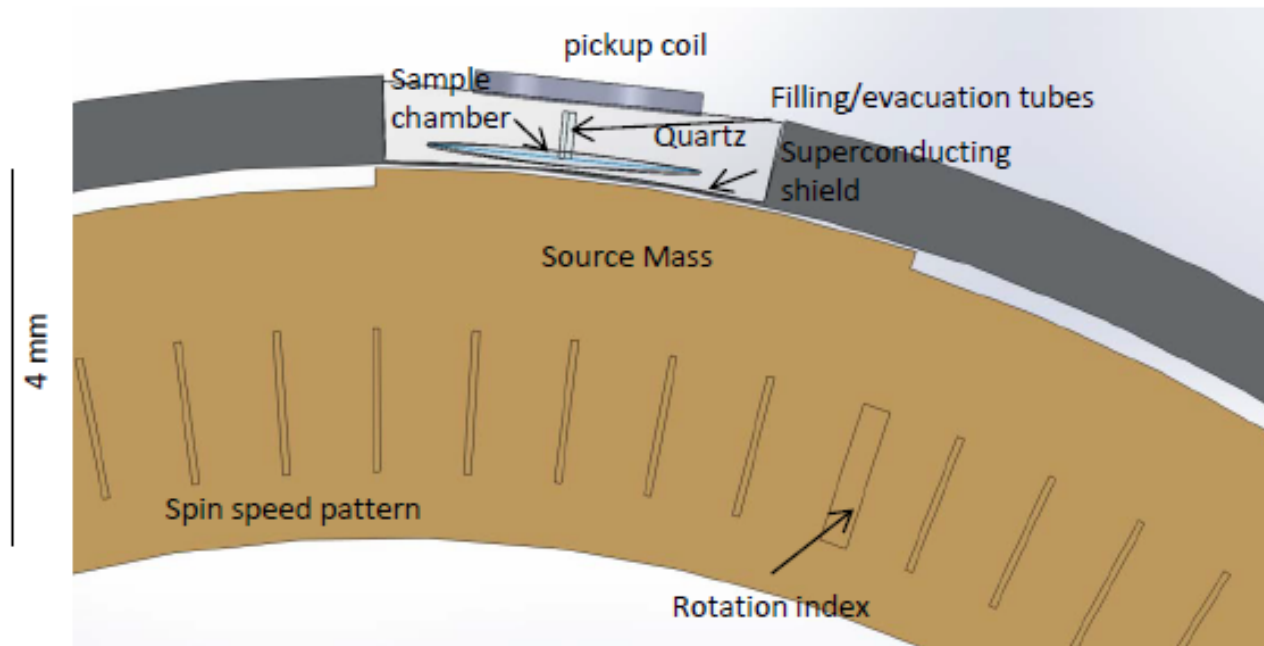
100 Hz nuclear spin precession frequency

2×10^{21} / cc ^3He density

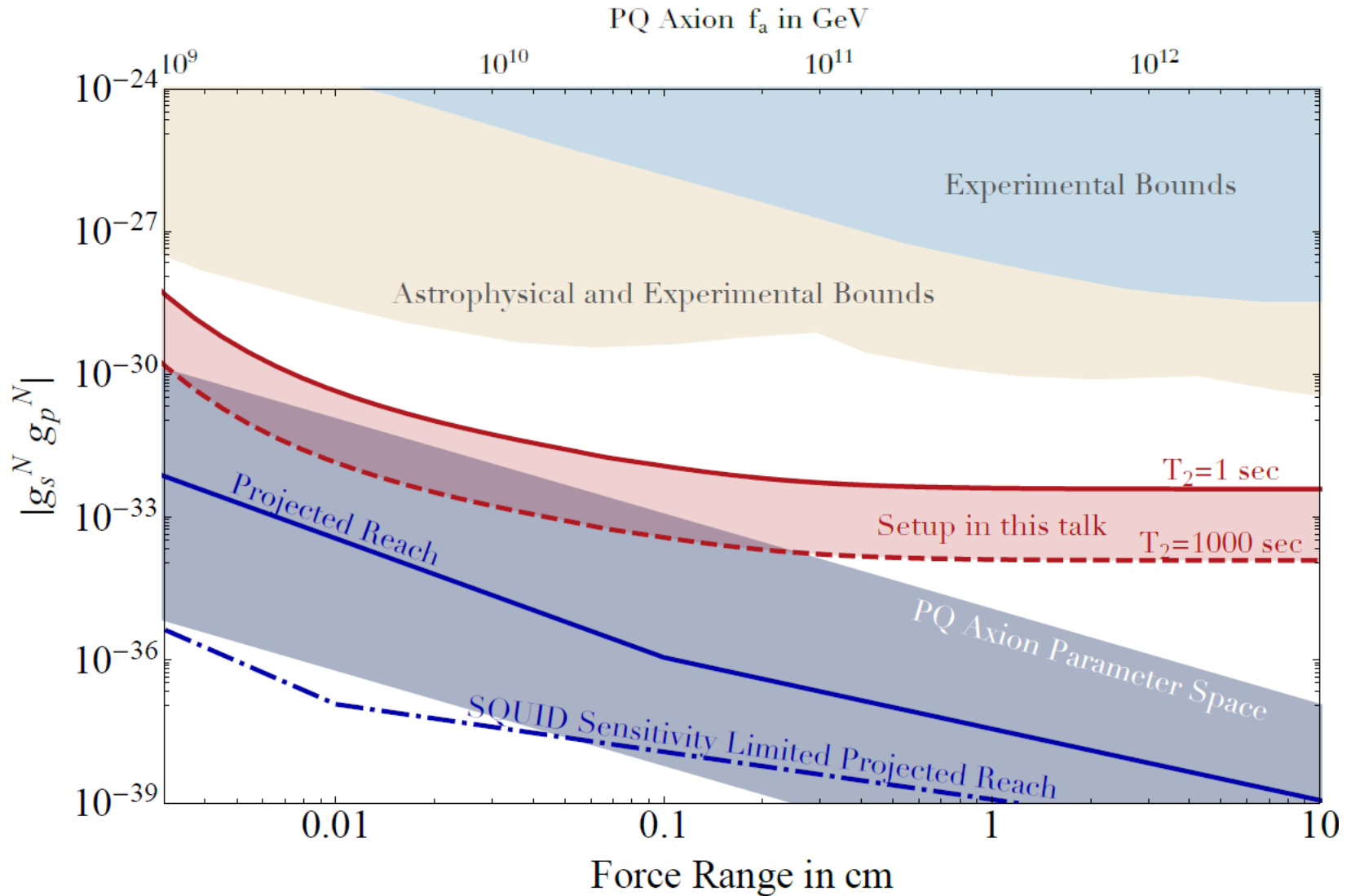
10 mm x 3 mm x 150 μm volume

Separation 200 μm

Tungsten source mass (high nucleon density)



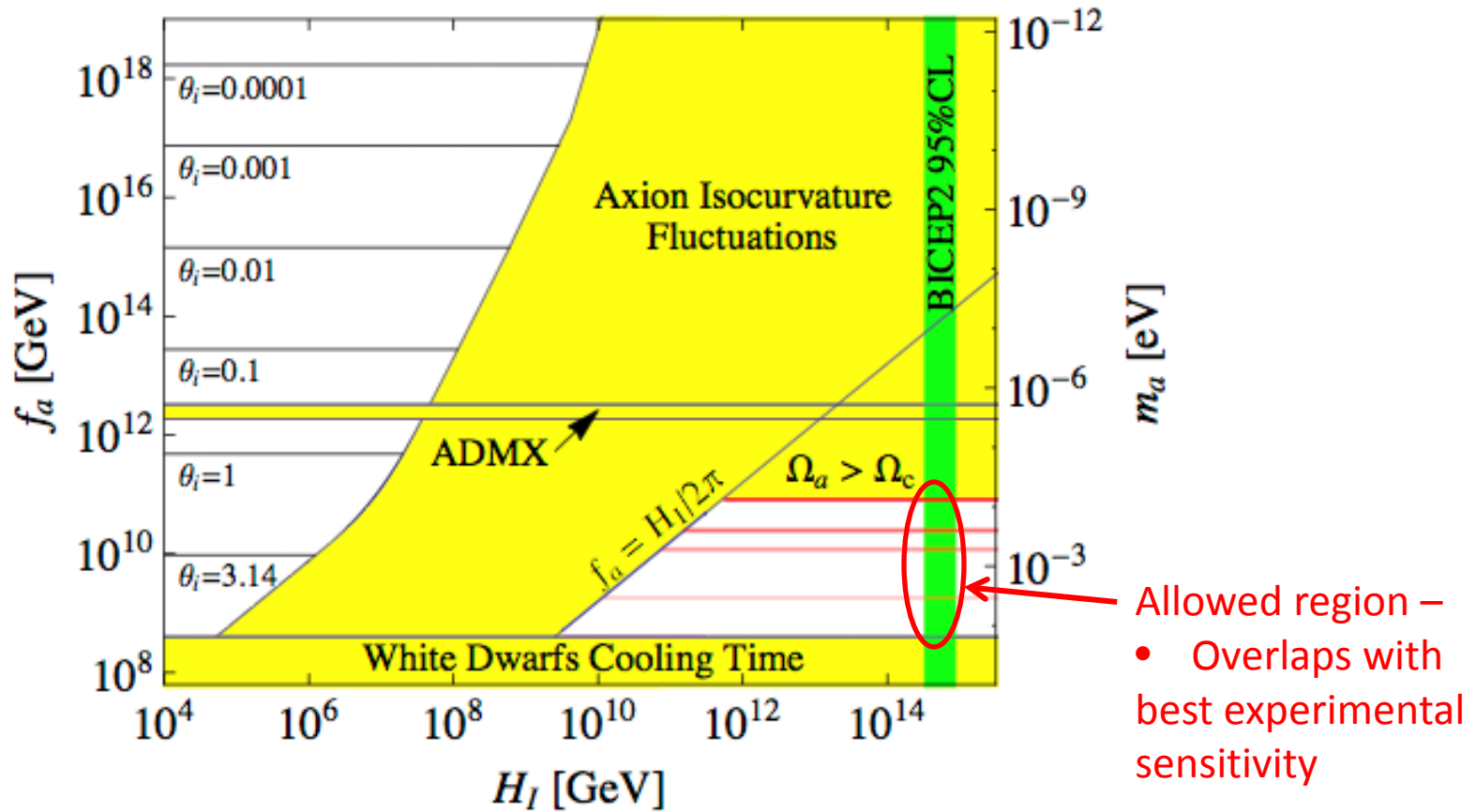
Sensitivity



Experimental challenges

- Magnetic gradients
- Nonlinearities
- Barnett Effect
- Trapped magnetic flux
- Vibration isolation
- Magnetic noise from thermal currents

Axion Cosmology in light of Inflationary scale

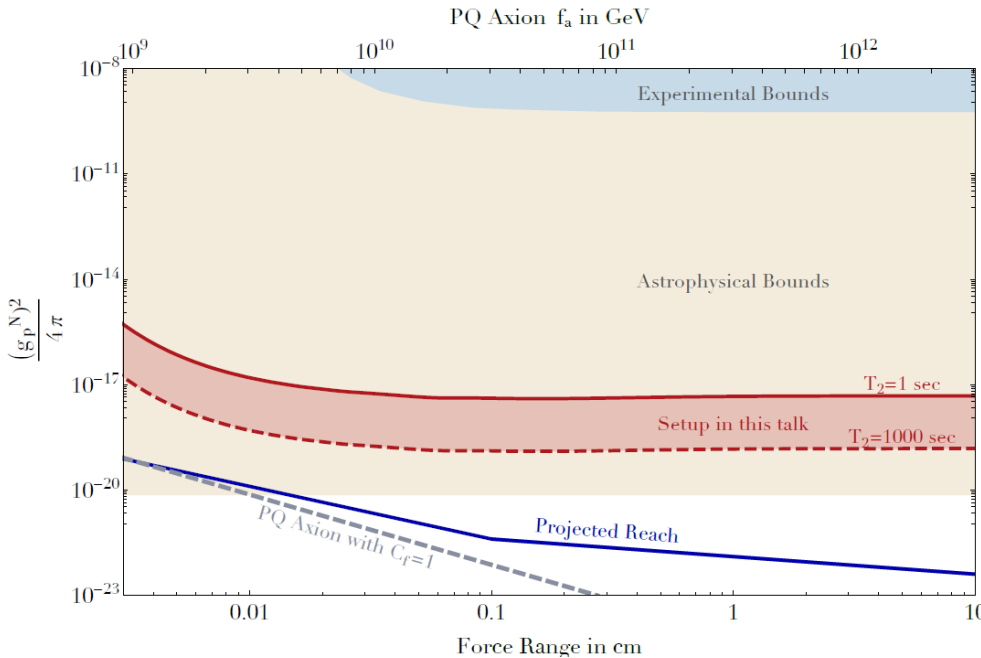


from: Luca Visinelli and Paolo Gondolo, arxiv: 1403.4594v2

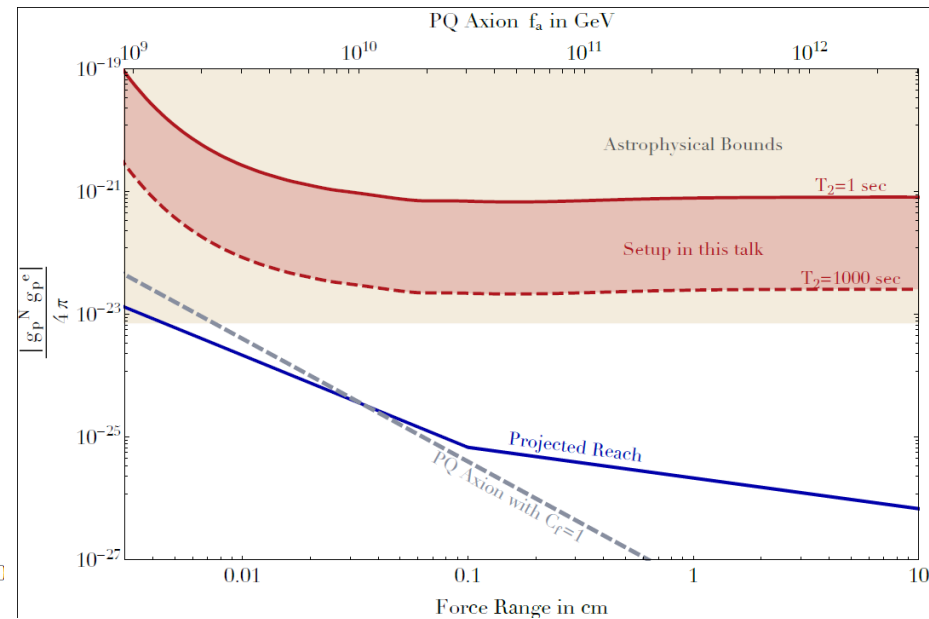
Dipole-Dipole axion forces

- Spin-polarized source mass
- May be competitive with astrophysical bounds
- Magnetic shielding requirements more stringent

Nuclear spin



Electron spin



Summary

- Microspheres as ultrasensitive mechanical force sensors
 - Micron-distance gravity tests
 - High frequency gravitational waves?
- Gap in experimental PQ axion searches $10^9 \text{ GeV} < f_a < 10^{11} \text{ GeV}$
- New resonant NMR method could probe into PQ axion parameter space, $\sim 10^8$ improvement over previous techniques (even if axion is not dark matter)
- Plans for Experiment: Axion Resonant InterAction Detection Experiment (ARIADNE)



Acknowledgements

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John Kitching (NIST)
Mike Snow (Indiana)
Aharon Kapitulnik (Stanford)
Eli Levenson-Falk (Stanford)
Josh Long (Indiana)
Chen-Yu Liu (Indiana)

Funding:

University of Nevada
National Science Foundation



University of Nevada, Reno



PHY-1205994