

# Introduction to Quantitative XRF analysis

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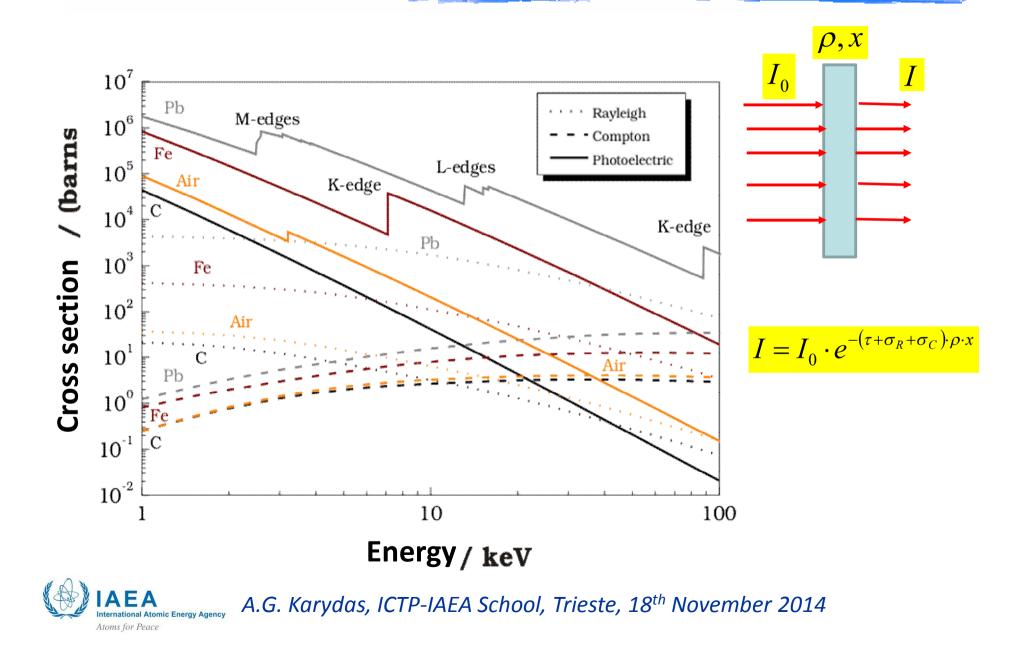


## Outline

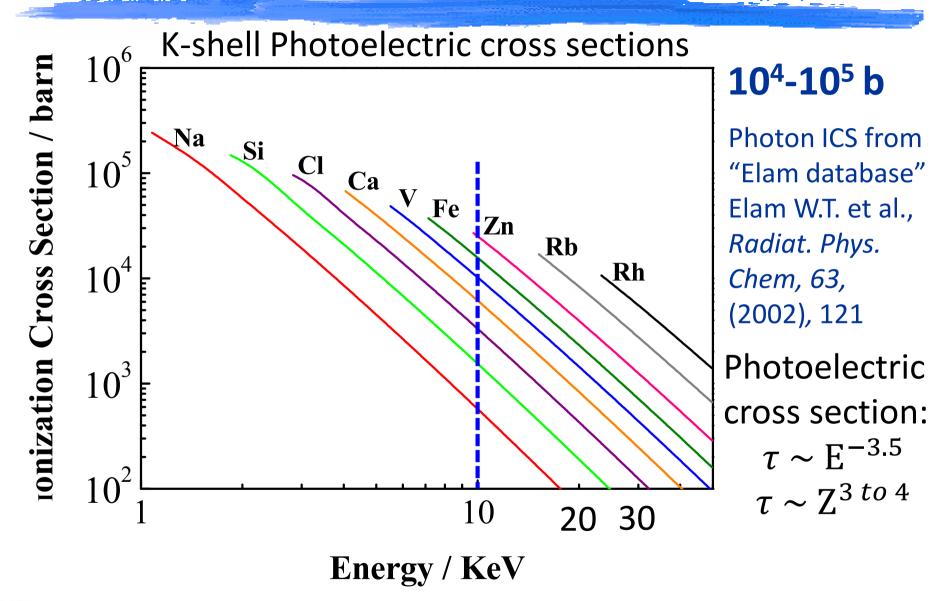
- Basic mechanisms for ionization/fluorescence process
- Primary XRF Intensity
- Indirect enhancement processes of XRF intensity
- XRF analysis in the real world:
  - Non-parallel exciting beams
  - Influence of surface topography
  - Geometrical considerations
  - Particle size effects



#### **Interaction of X-rays with atoms**

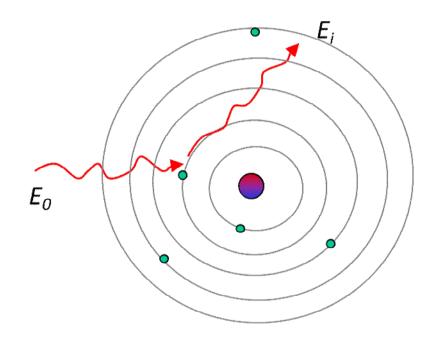


#### **Photoelectric cross sections**





## **X-ray Scattering Interactions with atoms**



#### E<sub>i</sub>=E<sub>0</sub> : Coherent (Rayleigh), mostly with inner atomic electrons

E<sub>i</sub> < E<sub>0</sub>: Incoherent
(Compton), mostly with
outer, less bound
electrons

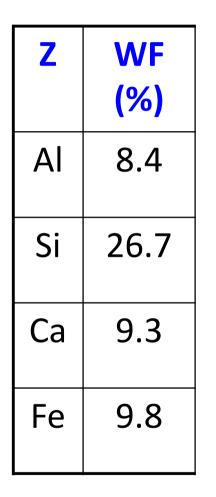
E<sub>0</sub>>>Binding Energy

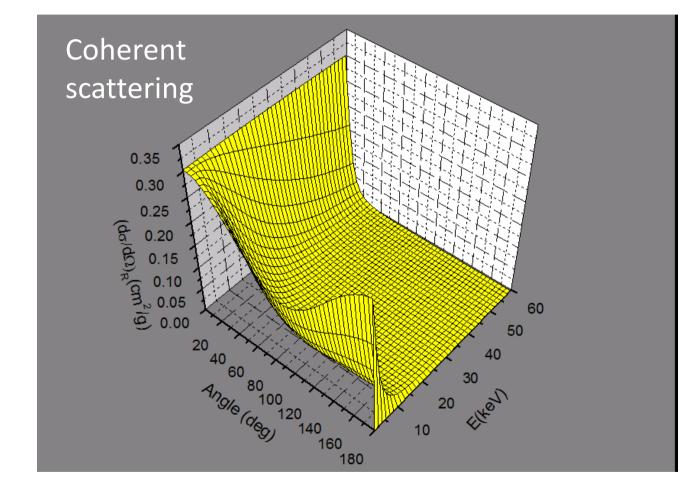
 $E_0$ 

 $E_i$ 



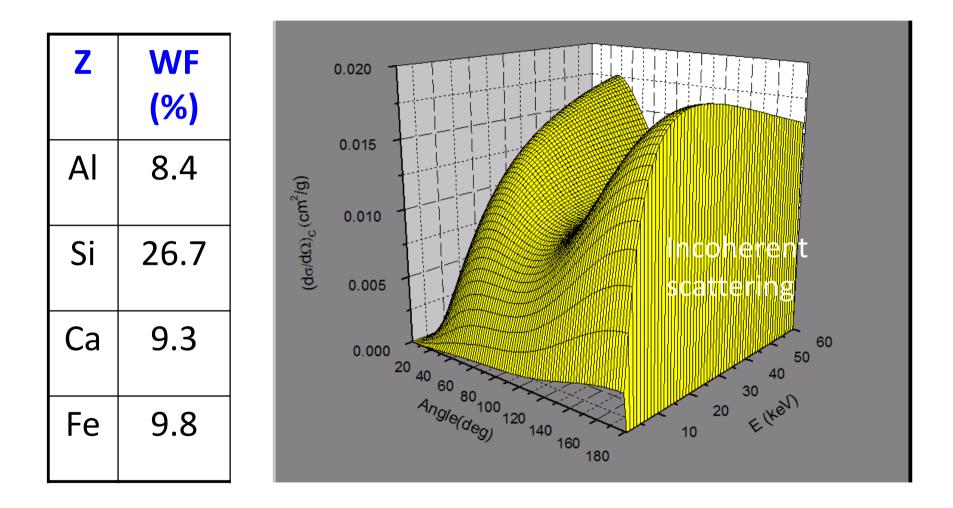
## **Scattering probabilities: Unpolarized excitation**





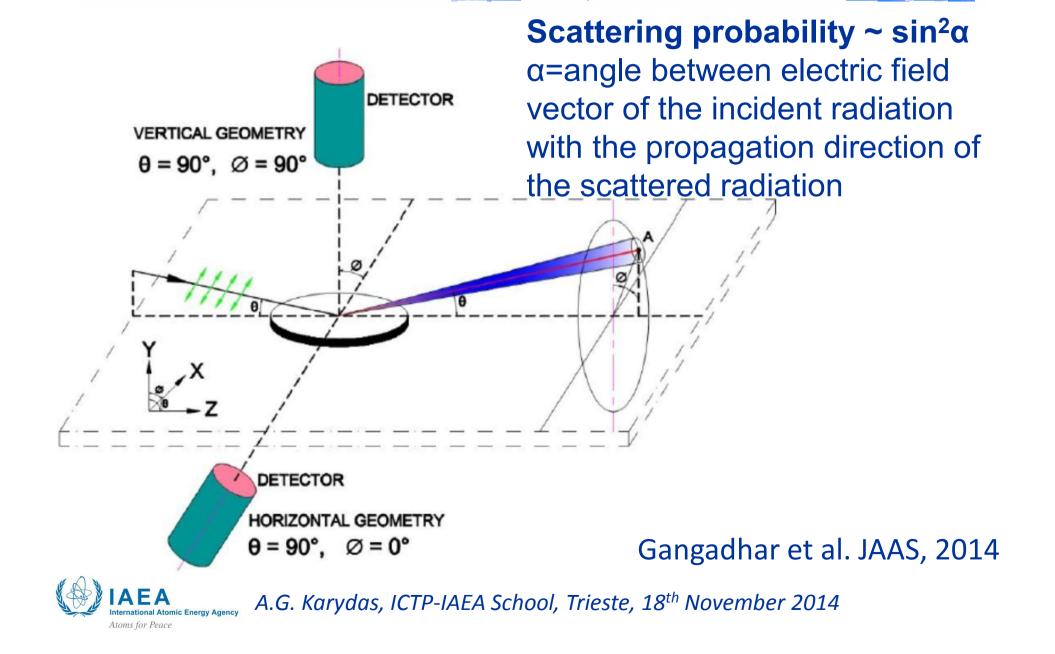


#### **Scattering probabilities: Unpolarized excitation**

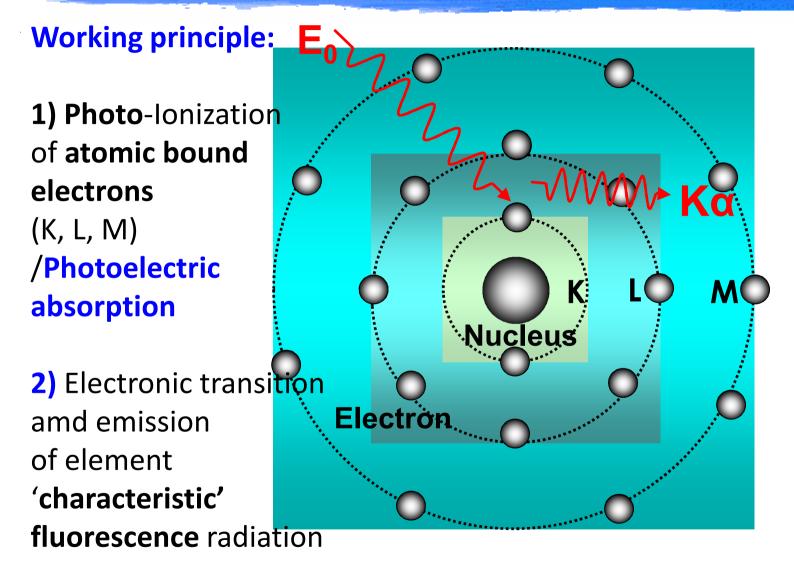




#### **Scattering probabilities: Polarized radiation**



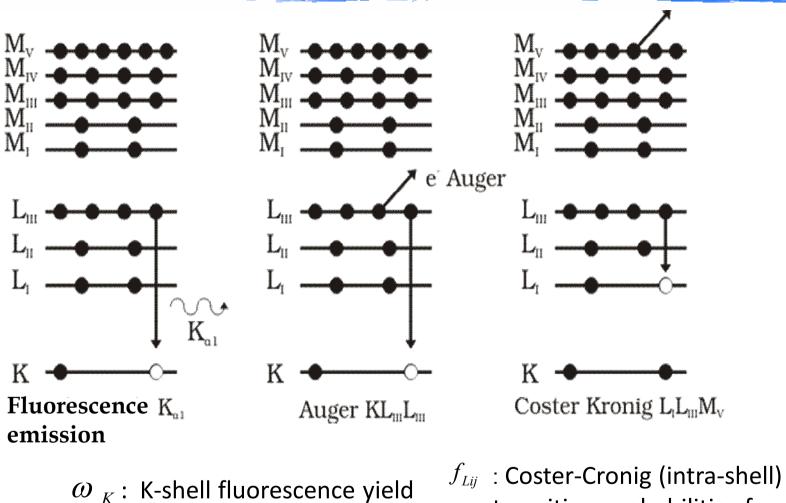
# Working principle: X-Ray Fluorescence Analysis



Incident photon **Energy E**<sub>0</sub> should be adequate to ionize the atomic bound electrons >= **Atomic shell Binding** energy



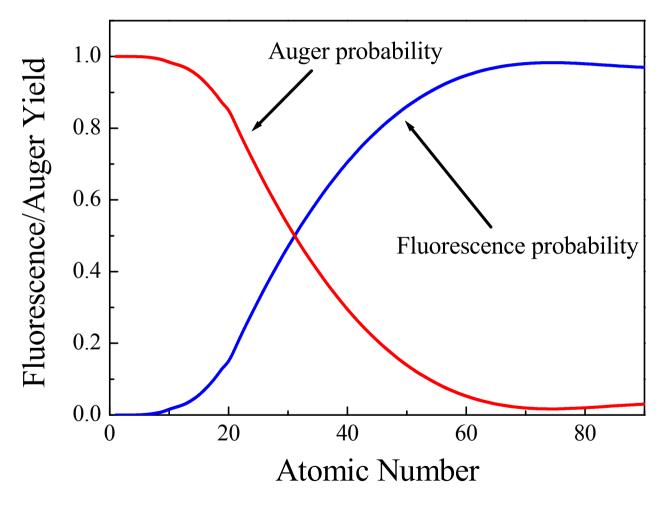
#### **De-excitation of atoms: Competitive processes**



*t<sub>Lij</sub>*: Coster-Cronig (intra-shell)
 transition probabilities from
 the *i* to the *j* L subshell



## **De-excitation: Fluorescence/Auger yield**

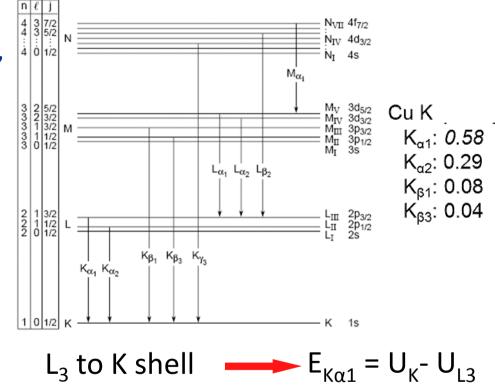




# **Emission of element 'characteristic' x-rays**

- K alpha lines: L shell etransition to fill vacancy in K shell. Most frequent transition, hence most intense peak
- K beta lines: M shell etransitions to fill vacancy in K shell.
- L alpha lines: M shell etransition to fill vacancy in L shell.
- L beta lines: N shell e- transition to fill vacancy in L shell.

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#### Each element has a unique set of emission energies

## **XRF cross sections: K- Emission**

XRF K-shell fluorescence cross section,  $\sigma_{KX}(E_o)$ 

$$\sigma_{KX}(E_o) = \tau_K(E_o) \cdot \omega_K \cdot F_{KX}$$

 $au_{K}(E_{o})$ : K-shell photoelectric cross section (*cm<sup>2</sup>/g or barns/atom*)

- $\omega_{K}$  : K-shell fluorescence yield
- $f_{KX}$  : Transition probability for K $\alpha$  emission



#### **XRF cross sections: L- Emission**

**Example: Incident energy E<sub>o</sub>>U<sub>L1</sub>** 

$$\sigma_{L1X}(E_o) = \tau_{L1}(E_o) \cdot \omega_{L1}(Z_i) \cdot f_{L1X}(Z_i)$$

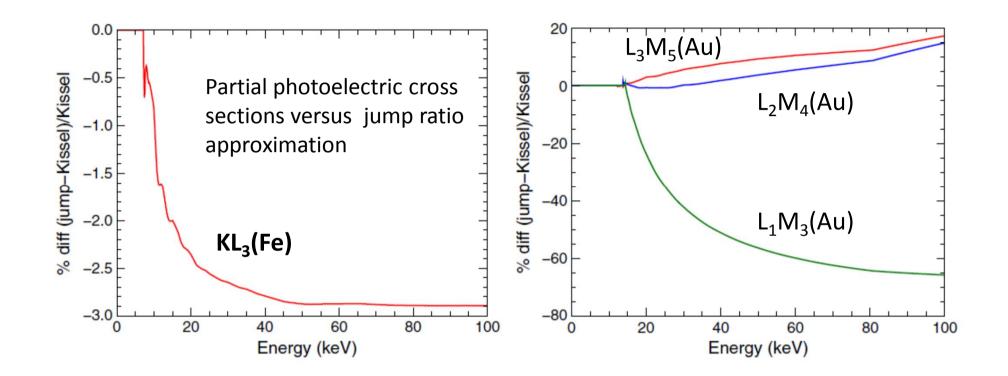
$$\sigma_{L2X}(E_o) = (\tau_{L2} + \tau_{L1} \cdot f_{L12}) \cdot \omega_{L1}(Z_i) \cdot f_{L2X}(Z_i)$$

$$\sigma_{L3X}(E_o) = (\tau_{L3} + \tau_{L2} \cdot f_{L23} \cdot f_{L12} + \tau_{L1} \cdot f_{L13}) \cdot \omega_{L3}(Z_i) \cdot f_{L3X}(Z_i)$$

 $f_{Lij}$ : Coster-Cronig (intra-shell) transition probabilities from the *i* to the *j* L subshell

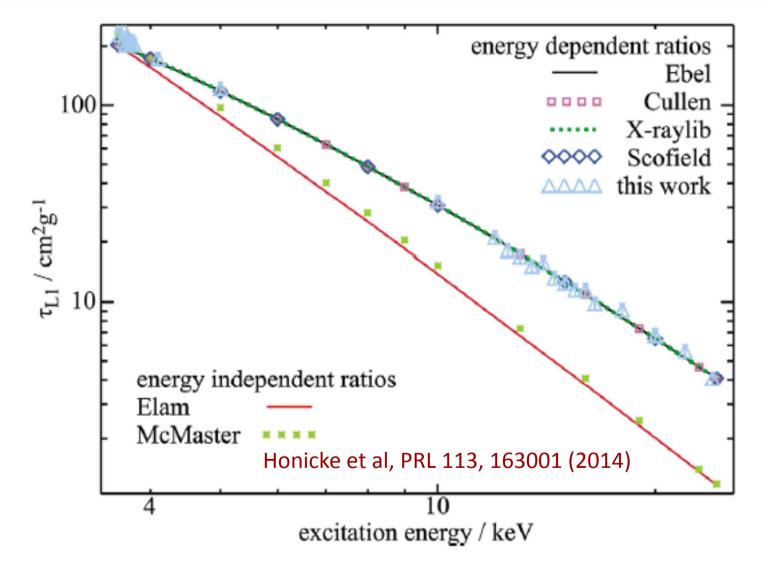


#### **XRF cross sections: L- Emission**



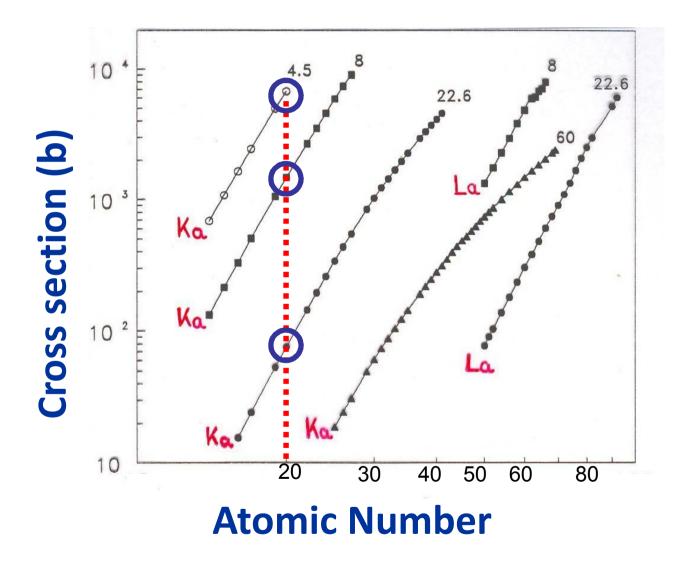


#### **XRF cross sections: L- Emission**





#### Fluorescence Ka, La cross sections



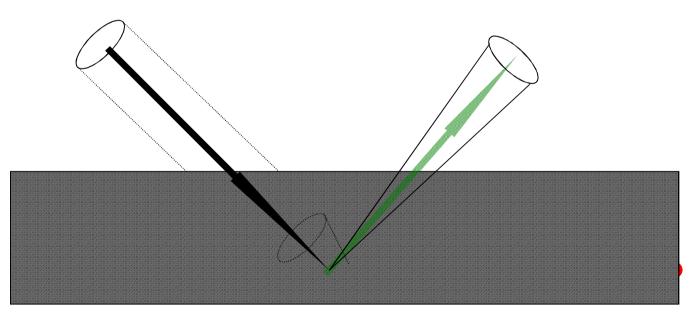
Optimization of the exciting beam energy for maximizing the characteristic Xray intensity



#### **Primary Fluorescence intensity: Assumptions**

- Parallel incident beam
- Infinite surface for sample
- Beam cross section infinite
- Homogenous sample
- Flat surface of the sample

- D.K.G. de Boer, XRS, 19(1990) 145
- M. Mantler, in Handbook of Practical XRFA, Edited by B. Beckhoff et *al*.





#### **Primary Fluorescence intensity: Assumptions**

Spectrochimica Acta, 1955, Vol 7, pp 288 to 806. Pergamon Press Ltd., London

#### The theoretical derivation of fluorescent X-ray intensities from mixtures\*

JACOB SHERMAN Philadelphia Naval Shipyard, Philadelphia 12, Pennsylvania

(Received 4 August 1955)

JAPANESE JOURNAL OF APPLIED PHYSICS

Vol. 5, No. 10, October, 19

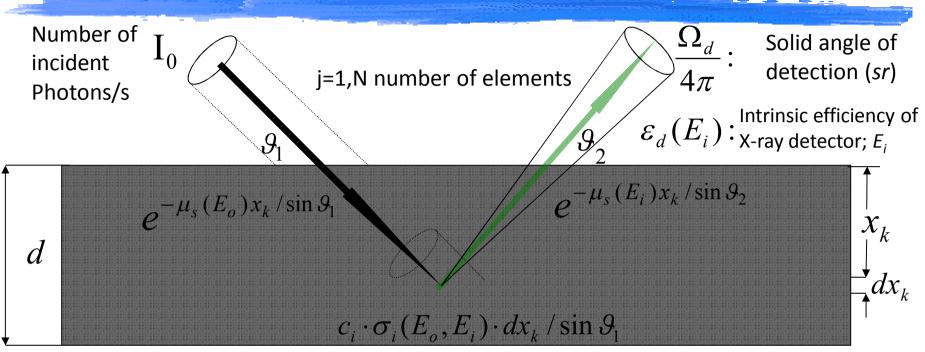
#### Theoretical Calculation of Fluorescent X-Ray Intensities in Fluorescent X-Ray Spectrochemical Analysis.

Toshio Shiraiwa and Nobukatsu Fujino Physics Section, Central Research Laboratories, Sumitomo Metal Industries, Amagasaki, Hyogo.

(Received April 15, 1966)



#### Primary Fluorescence intensity



(Concentration of *i* element) X (Fluorescence cross section; cm<sup>2</sup>/g) X (areal density; g/cm<sup>2</sup>)

$$\mu_{s}(E_{o}): \text{ Sample mass attenuation coefficient for energy Eo} \equiv \sum_{j=1,N} c_{j} \mu_{j}(E_{o})$$

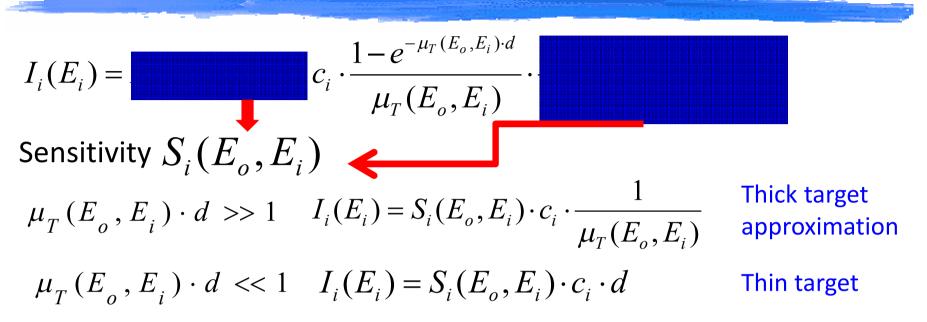
$$dI_{i}(E_{i}) = I_{o} \cdot e^{-\mu_{s}(E_{o}) \cdot x_{k} / \sin \theta_{1}} c_{i} \cdot \sigma_{i}(E_{o}, E_{i}) \cdot \frac{dx_{k}}{\sin \theta_{1}} \cdot e^{-\mu_{s}(E_{i}) \cdot x_{k} / \sin \theta_{2}} \frac{\Omega_{d}}{4 \cdot \pi} \cdot \mathcal{E}_{d}(E_{i})$$

$$\mu_{T}(E_{o}, E)_{i} = \mu_{s}(E_{o}) / \sin \theta_{1} + \mu_{s}(E_{i}) / \sin \theta_{2}$$

$$A.G. Karydas, ICTP-IAEA School, Trieste, 18th November 2014$$

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# **Primary Fluorescence intensity: Calibration**

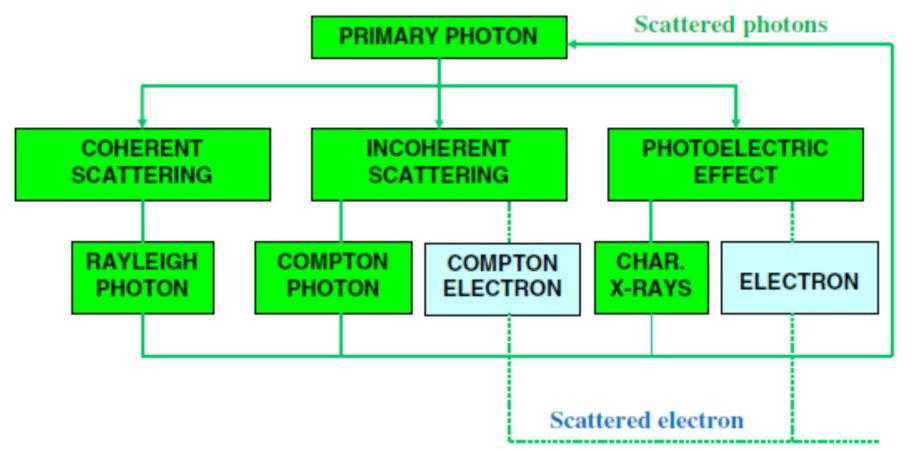


Different approaches are followed depending on how well the set-up geometry and incident beam intensity are characterized:

- Sensitivity calibration: certified pure element/compound targets
- Solid angle calibration: Normalized beam intensity, detector efficiency known, well certified pure element/compound targets
- Standard-less XRFA: Calibrated apertures, distances, detector response function versus energy, incident beam intensity

## **Indirect Enhancement Processes in**

#### **Fluorescence Emission**

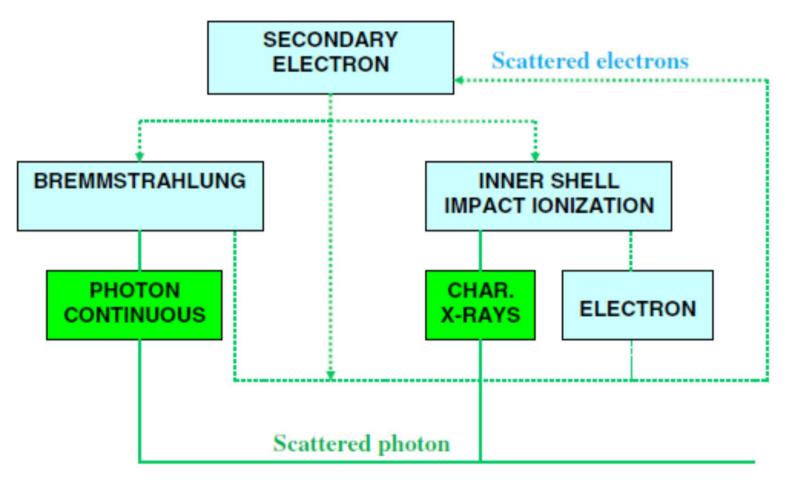


J. Fernandez et *al.*, X-Ray Spectrom. 2013, 42, 189–196



#### **Indirect Enhancement Processes in**

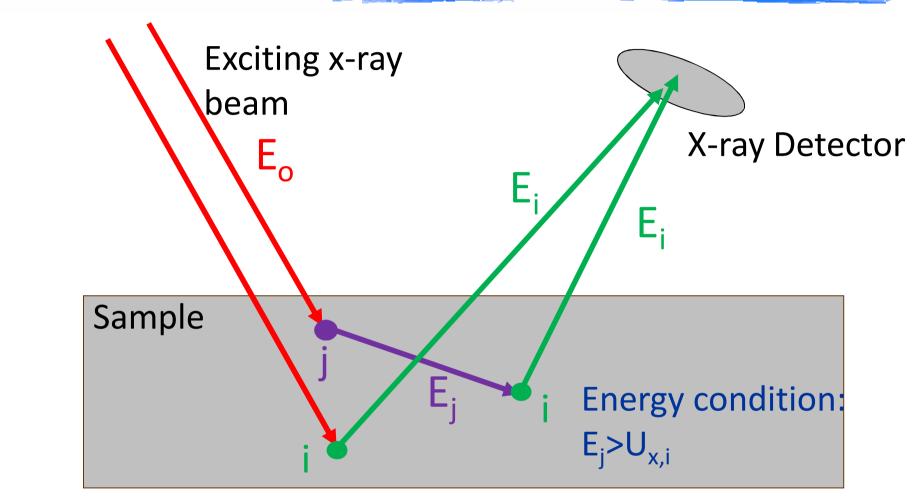
#### **Fluorescence Emission**



J. Fernandez et *al.*, X-Ray Spectrom. 2013, 42, 189–196



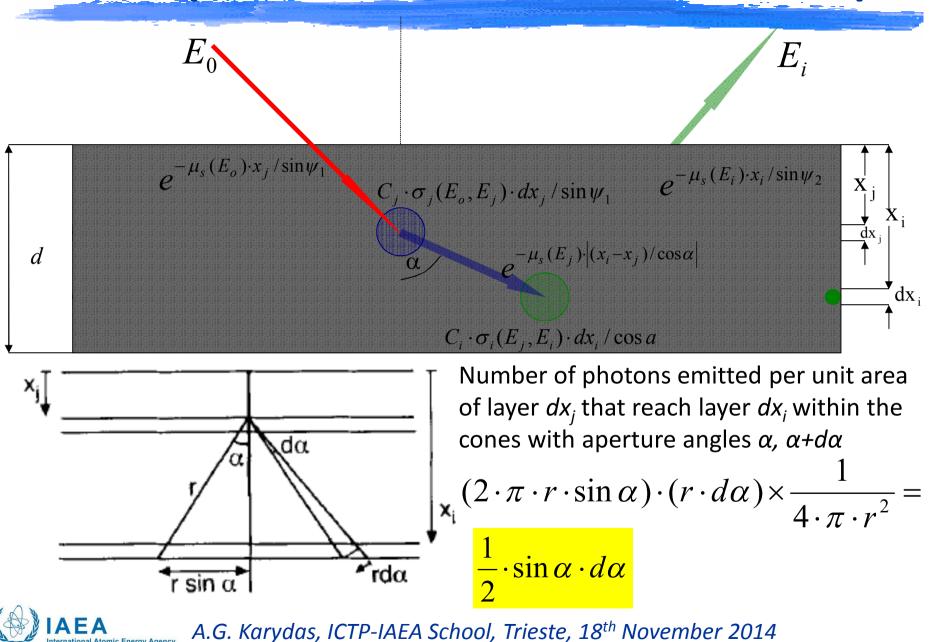
#### **Secondary Fluorescence Enhancement**



Element *j* characteristic x-ray(s) can excite element *i* characteristic x-rays within the sample volume

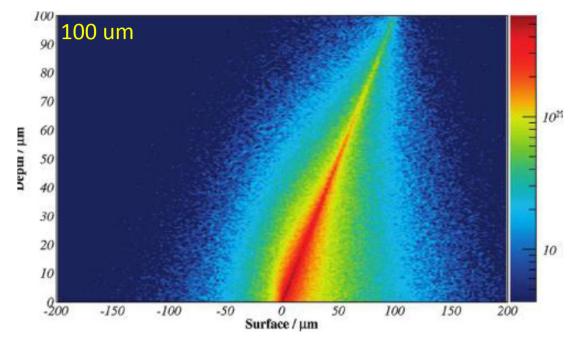


## **Secondary enhancement calculation: Example**



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## **Topology of secondary fluorescence**

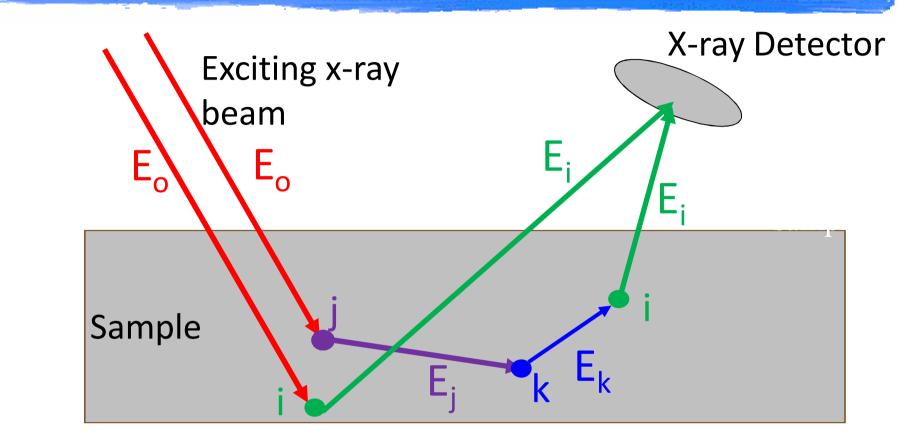


13 keV, excitation, SiO<sub>2</sub> matrix, 5% Cu, 5% Fe

#### Sokaras et al, Anal. Chem. 2009, 81, 4946



## **Tertiary Fluorescence Enhancement**



The element *j* characteristic x-ray(s) can excite element's *k* characteristic x-ray(s) which consequently can also excite element's *i* characteristic x-rays

**Energy conditions:** E<sub>j</sub>>U<sub>x,k</sub> and E<sub>k</sub>>U<sub>x,i</sub>

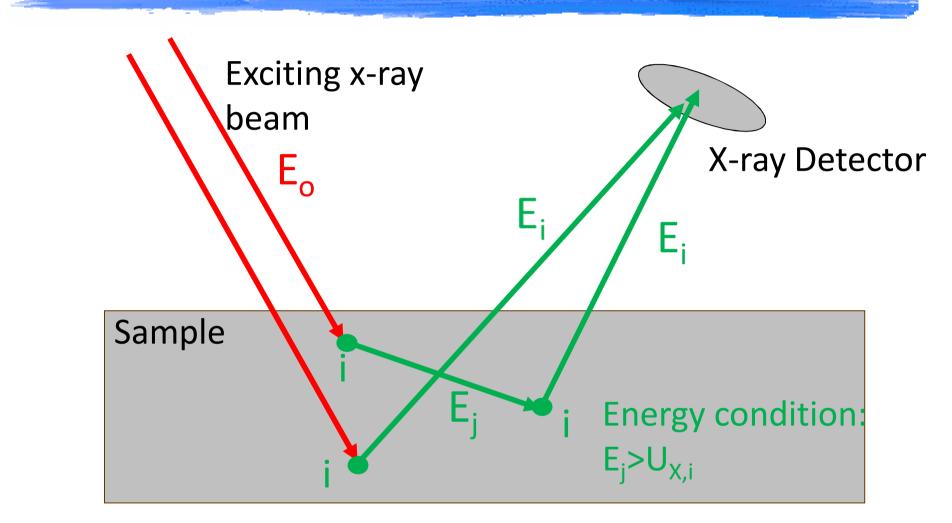


# **SF Enhancement in Poly-Energetic excitation**

Type of Sample	Secondary Fluorescence Mechanism	Am-241 (59.6 keV) Source*	Filtered Rh- tube excitation*
Ag: 92.5% Cu: 7.5%	Ag-K to Cu		0.29
Au: 88.3 % Ag: 8.5 %	(Ag-K+Au-L) to Cu	0.82	0.55
Cu: 3.1 %	Ag-K to Au	6.6e-2	1.4e-2
Cu: 80 %	(Sn-K + Pb-L) to Cu	0.22	7.8e-2
Pb: 10 % Sn: 10 %	Sn-K to Pb	0.11	1.6e-2

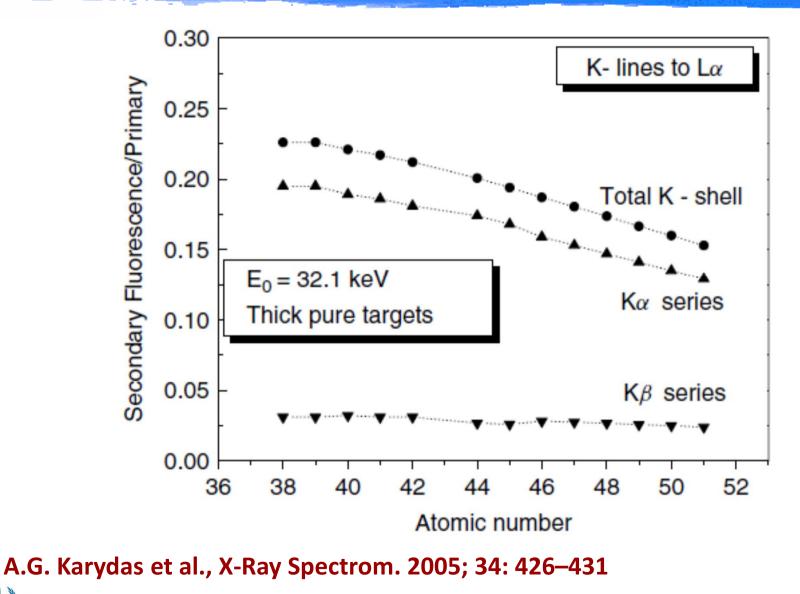
\* Including ternary contribution



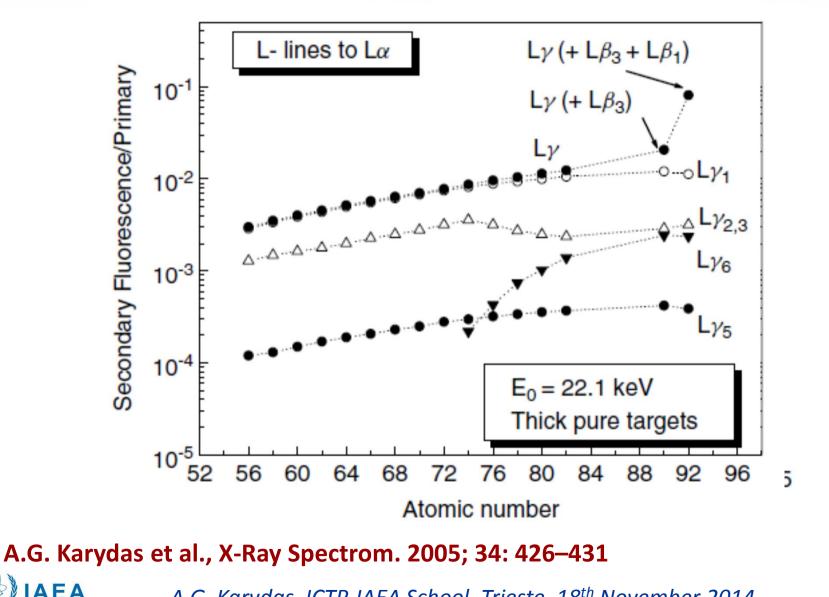


Element *i* characteristic x-ray(s) can excite different series of characteristic X-rays of the same element *i* within the sample volume; for example K to L, L to M lines

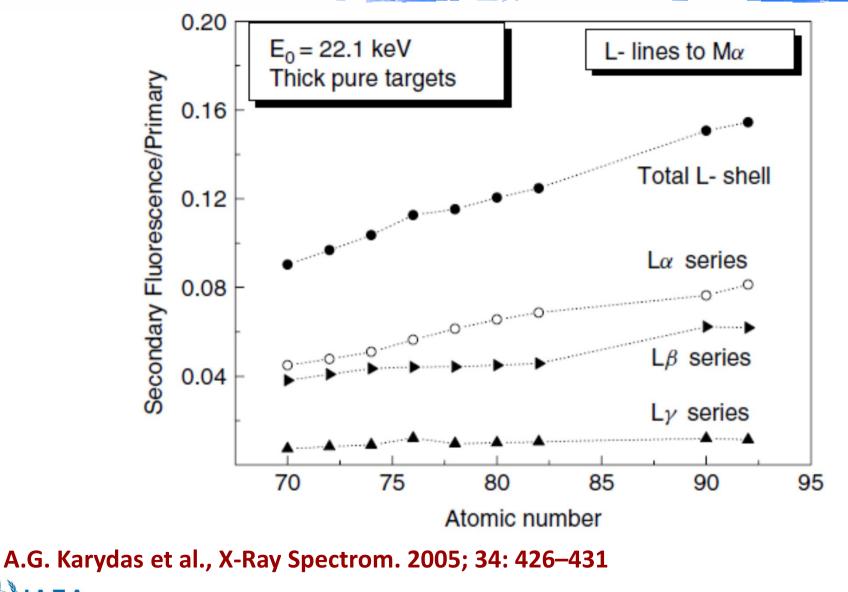
A.G. Karydas, ICTP-IAEA School, Trieste, 18th November 2014



A.G. Karydas, ICTP-IAEA School, Trieste, 18<sup>th</sup> November 2014

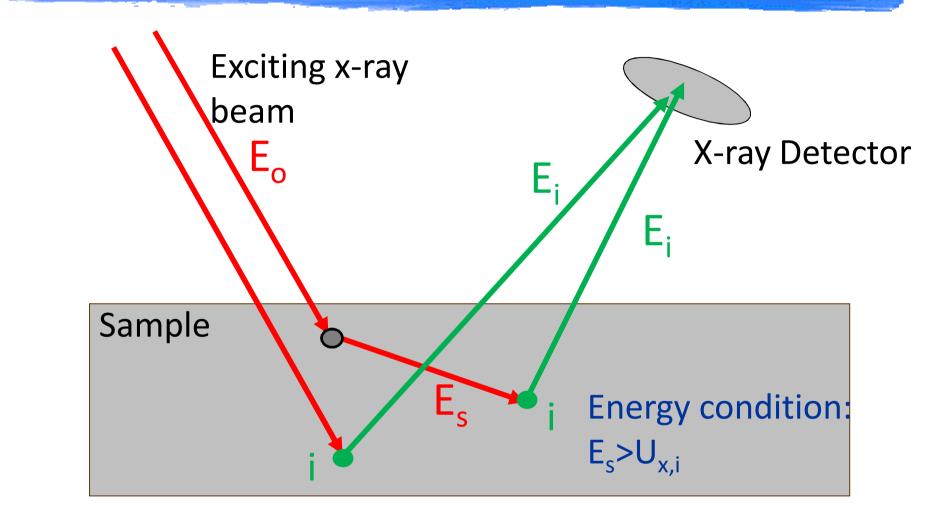


A.G. Karydas, ICTP-IAEA School, Trieste, 18th November 2014



A.G. Karydas, ICTP-IAEA School, Trieste, 18th November 2014

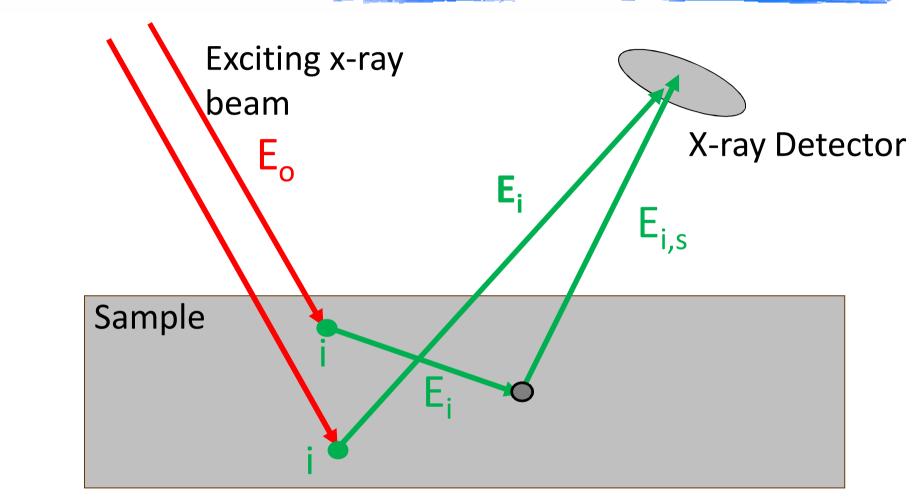
## **Secondary Scattering Enhancement (Beam)**



Incident beam after encountering elastic/inelastic scattering at one produces photoionization of an element *i* in another sample position volume



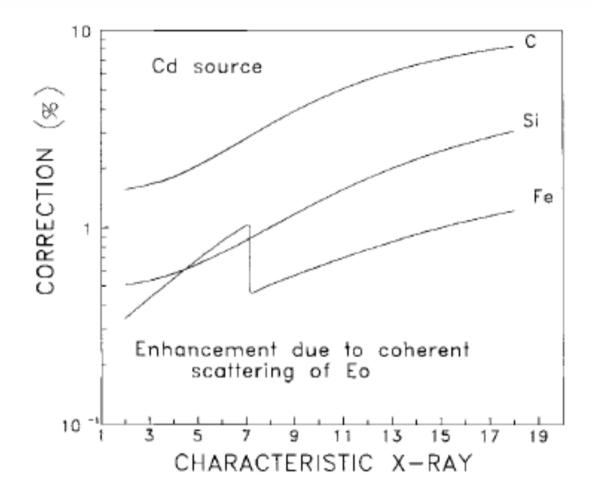
## **Secondary Scattering Enhancement (Fluo)**



Element a characteristic x-ray after elastic/inelastic scattering within the sample volume are directed to the detector

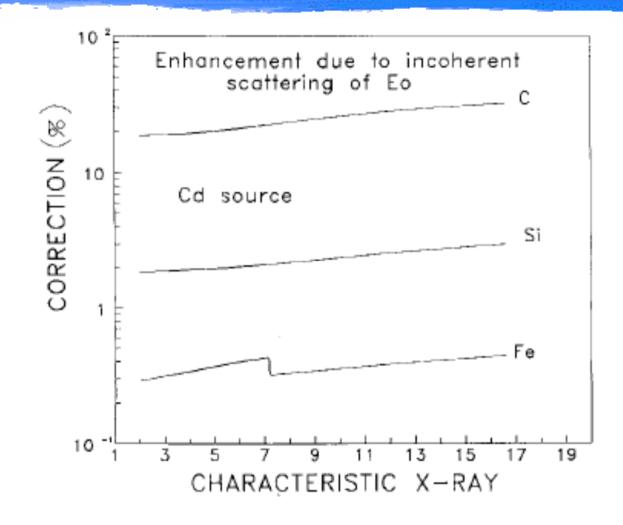


## Secondary Enhancement due to Scattering



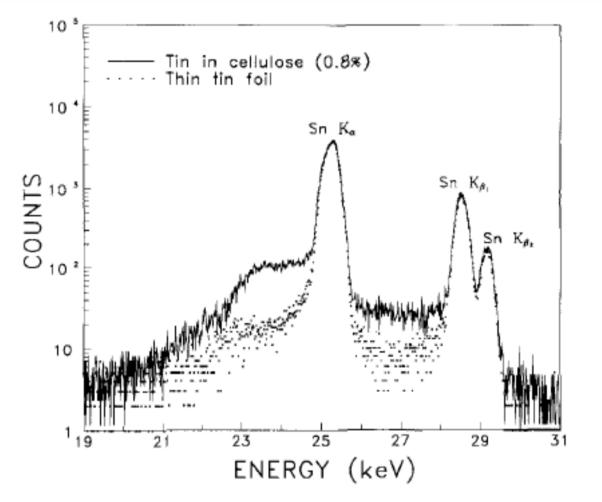
Karydas, Paradellis, X-Ray Spectrom. 1993; 22: 208 Tirao, Stutz, X-Ray Spectrom. 2003; 32: 13–24 MARKA ALEXANDER ALEXANDER ALCONDUCTOR ALEXANDER AND ALEXA

## Secondary Enhancement due to Scattering



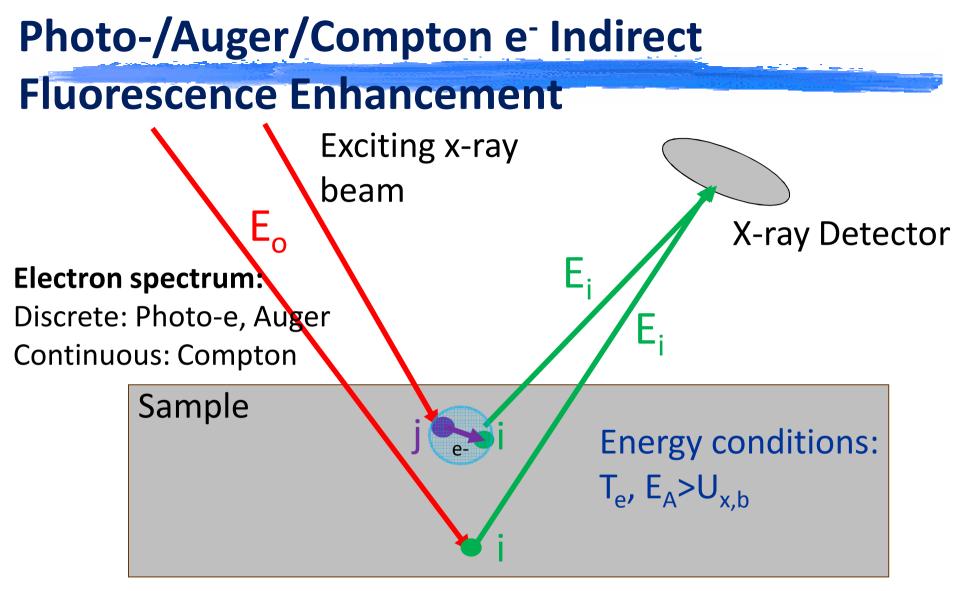
Karydas, Paradellis, X-Ray Spectrom. 1993; 22: 208 Tirao, Stutz, X-Ray Spectrom. 2003; 32: 13–24 IAEA IAEA INFINITION ALCON KARYDAS, ICTP-IAEA School, Trieste, 18<sup>th</sup> November 2014 A.G. Karydas, ICTP-IAEA School, Trieste, 18<sup>th</sup> November 2014

### Secondary Enhancement due to Scattering



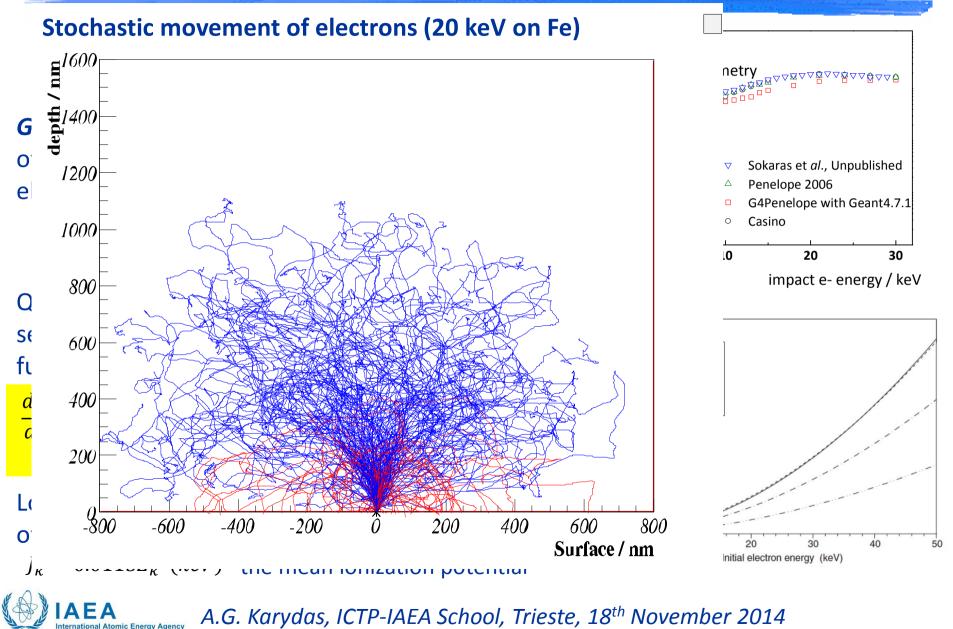
# Effect on spectrum!

#### Karydas, Paradellis, X-Ray Spectrom. 1993; 22: 208 Tirao, Stutz, X-Ray Spectrom. 2003; 32: 13–24 (IAEA International Atomic Energy Agency Atoms for Peace



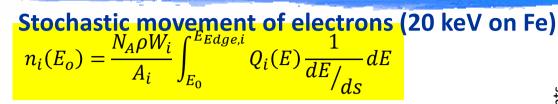
Ejected electrons from the atoms of element *j* can ionize an inner shell of element *i* 

### **Ionization induced by electrons**



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### **Ionization induced by electrons**



*Green and Cosslett* expression for the number of photons emitted by interaction with a single electron of initial kinetic energy Eo

$$Q_{ip}(E) = 6.51 \times 10^{-20} \frac{Z_{subshell,i}}{E_{Edge,i}^2} b \frac{ln(cU)}{U} (cm^2)$$

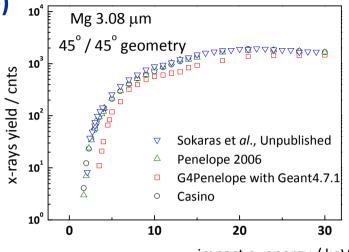
Q<sub>i</sub>(E) and dE/ds are the inner shell ionization crosssection and the stopping power (energy loss function), respectively, of electrons in a material

$$\frac{dE}{ds} = -\frac{\rho}{J'} \sum_{k} \frac{W_k Z_k}{A_k} \frac{1}{1.18 \times 10^{-5} \sqrt{E/J'}} + 1.47 \times 10^{-6} \left(\frac{E}{J'}\right)$$

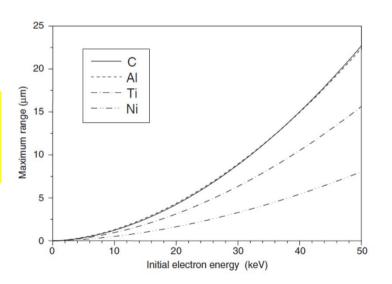
Love et al. expression for stopping power of electrons

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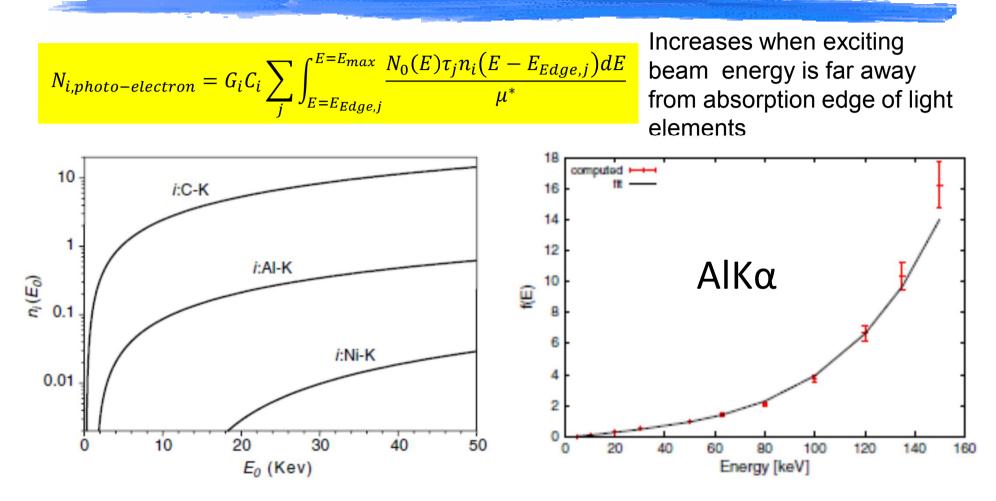
 $J_k = 0.0115Z_k$  (keV) the mean ionization potential



impact e- energy / keV



### Photo e<sup>-</sup> Fluorescence Enhancement

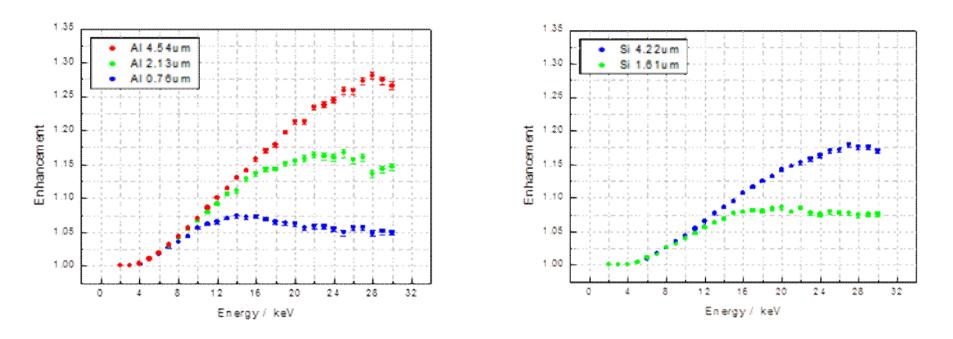


N. Kawahara in Handbook of Practical X-Ray Fluorescence Analysis, by B. Beckhoff B. Kanngiesser, N. Langhoff, R.Wedell, H.Wolff, (Eds.)

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J. Fernandez et *al.*, X-Ray Spectrometry 2013, 42, 189–196

### Photo e<sup>-</sup> Fluorescence Enhancement

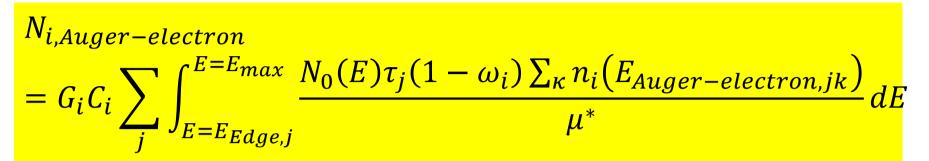


Monte Carlo calculations of phot-e enhancement: Al (4.54μm, 2.13μm, 0.76μm) and Si (4.22μm, 1.61μm) Casnati parameterization for electron ionization cross sections

#### D. Sokaras et al., unpublished

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### Auger e<sup>-</sup> Fluorescence Enhancement

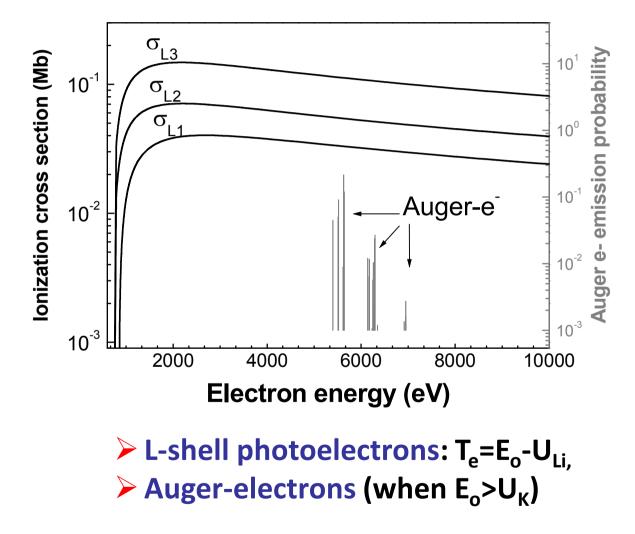


- **Important:** When a light element analyte is embedded in a heavy element matrix.
- The Auger-electrons from the matrix elements can excite light element fluorescence.
- Example: When carbon in steel is analyzed, a Fe KLL Auger-electron with a kinetic energy of 6.3 keV can excite multiple carbon K-shells



# Secondary electron induced ionizations

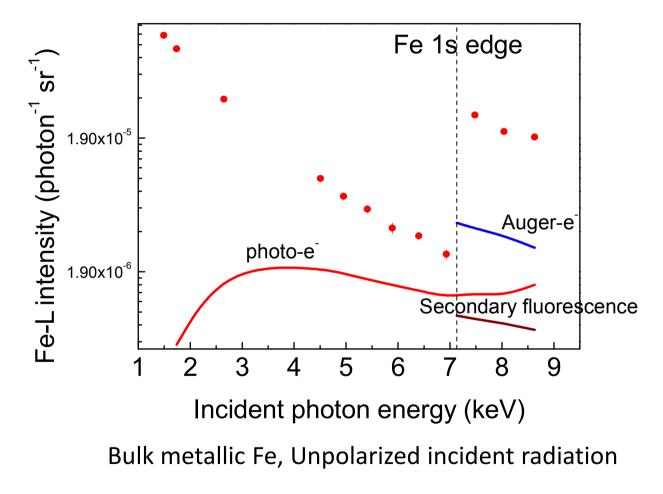
### **Example: Thick Fe target**





# **Relative e- enhancement to Fe-Lα excitation**

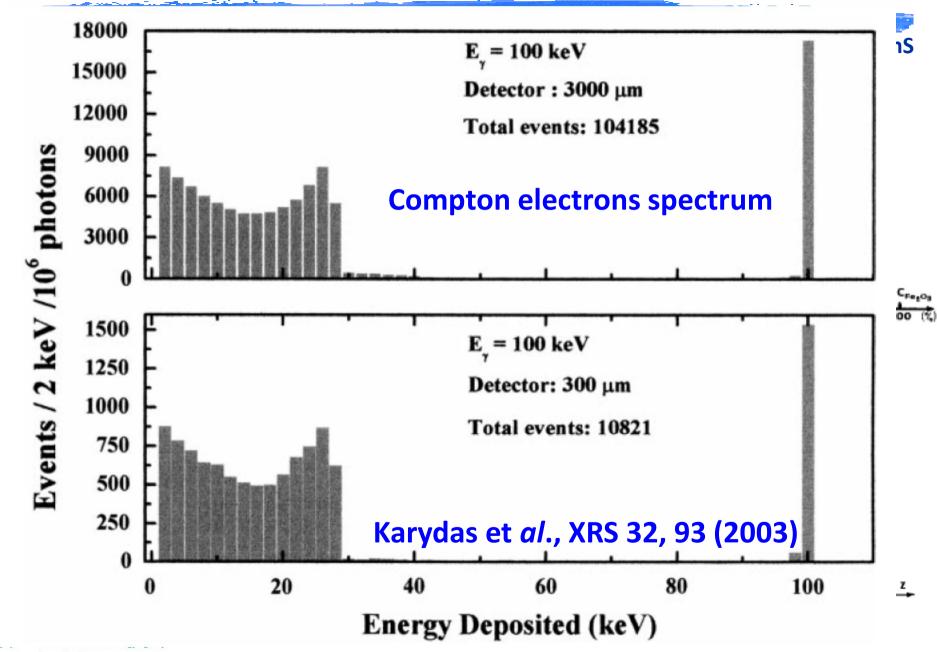
### in the case of a Fe pure target



Sokaras et *al.*, Phys. Review A 83, 052511 (2011)



### **Compton electrons Fluorescence Enhancement**



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### **Compton electrons Fluorescence Enhancement**

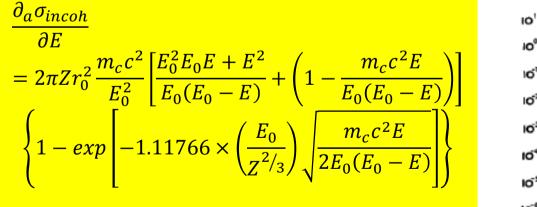
Thomas-Fermi model for the incoherent scattering function

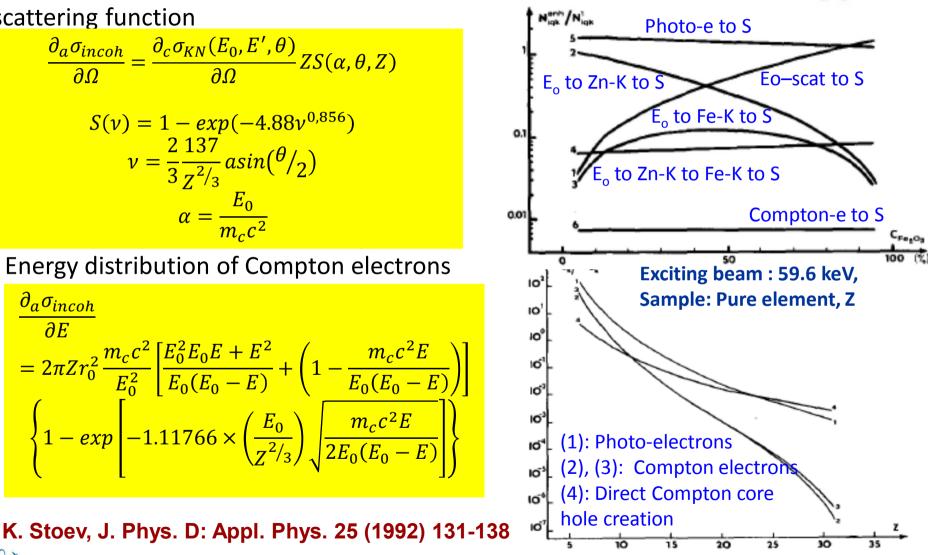
$$\frac{\partial_a \sigma_{incoh}}{\partial \Omega} = \frac{\partial_c \sigma_{KN}(E_0, E', \theta)}{\partial \Omega} ZS(\alpha, \theta, Z)$$
$$S(\nu) = 1 - exp(-4.88\nu^{0.856})$$

$$\nu = \frac{2}{3} \frac{137}{Z^{2/3}} asin(\theta/2)$$
$$\alpha = \frac{E_0}{m_c c^2}$$

#### **Energy distribution of Compton electrons**

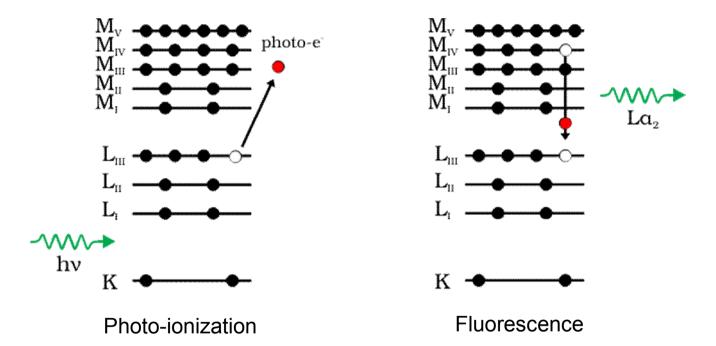
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Exciting beam : 59.6 keV, Sample: Fe<sub>2</sub>O<sub>3</sub> + ZnS

# **De-excitation processes for inner-shell ionized atoms. Diagram L-emission**

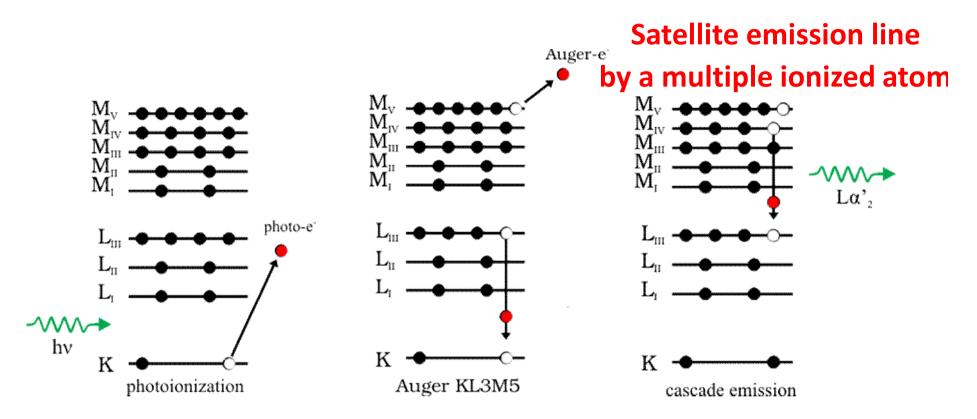


### Emission of a diagram line



### **Cascade L X-ray emission**

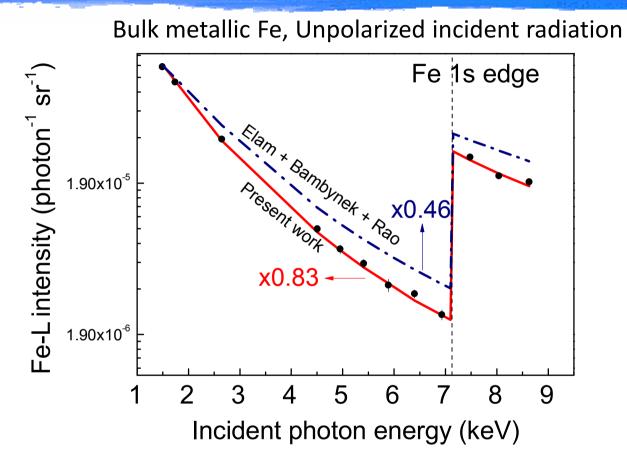
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**Cascade Emission**: X-ray emission due to relaxation of an **indirectly** vacancy created by the relaxation of innermost shell and **not** due to a direct ionization.

# **Fe-L cascade effect**

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Sokaras et *al.*, Phys. Review A 83, 052511 (2011) T. Schoonjans et *al*, SAB, B66, (2011) 776

Fluorescence cross sections include full cascade effect due to radiative and non radiative probabilities



# Secondary fluorescence enhancement

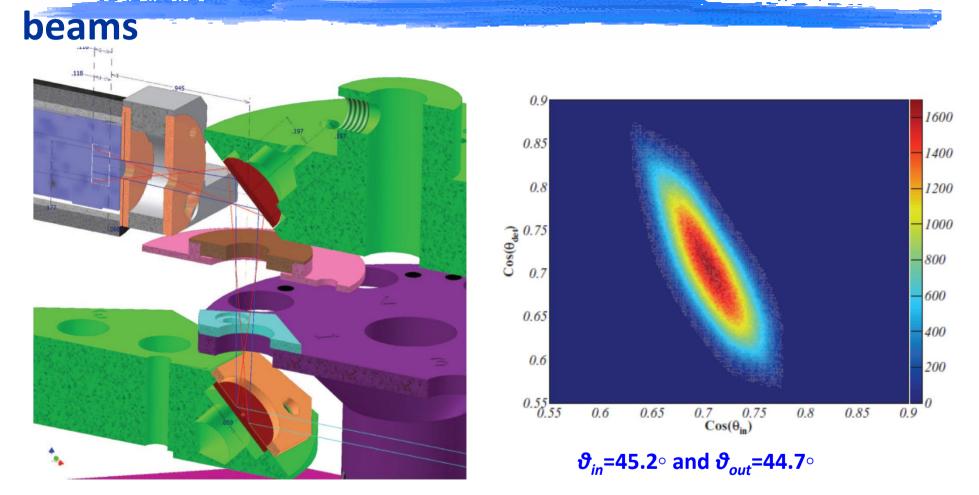
Z	WF	lpr	lsec	lter	lscat
	(%)	(%)	(%)	(%)	(%)
AI	8.4	1	21.2	1.17	1.2
Si	26.7	1	18.1	0.64	1.23
Са	9.3	1	13.8	-	1.64
Fe	9.8	1	-	-	2.44

$$\psi_1 = \psi_2 = 45^\circ$$

$$E_0 = 17.44 keV$$
$$(Mo - K_a)$$



### **Geometrical considerations: Non-parallel x-ray**

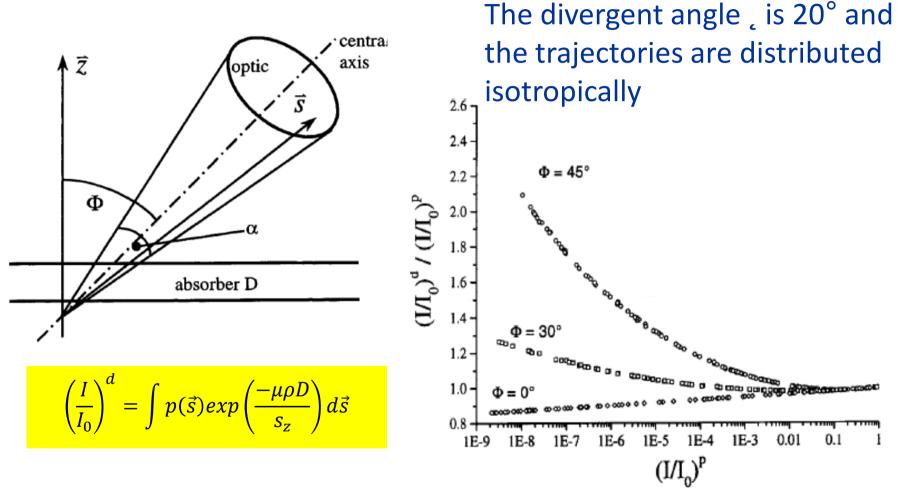


#### Sokaras et al., Review of Scientific Instruments 83, 123102 (2012);



# Fluorescence intensities for non-parallel x-ray

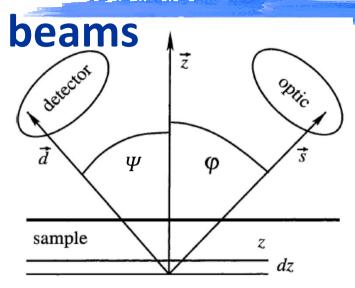
beams



Malzer, Kanngiesser, X-Ray Spectrom. 2003; 32: 106–112



### Fluorescence intensities for non-parallel x-ray



$$I_i^d = \frac{I_0 K_i c_i}{\mu} \int p(\vec{s}) p(\vec{d}) \frac{1 - exp\left[-\mu \rho D\left(\frac{k}{d_z} + \frac{1-k}{s_x}\right)\right]}{k\frac{s_z}{d_z} + (1-k)} d\vec{s} d\vec{d}$$

$$\cos = s_z$$
 and  $\cos \Psi = d_z$ 

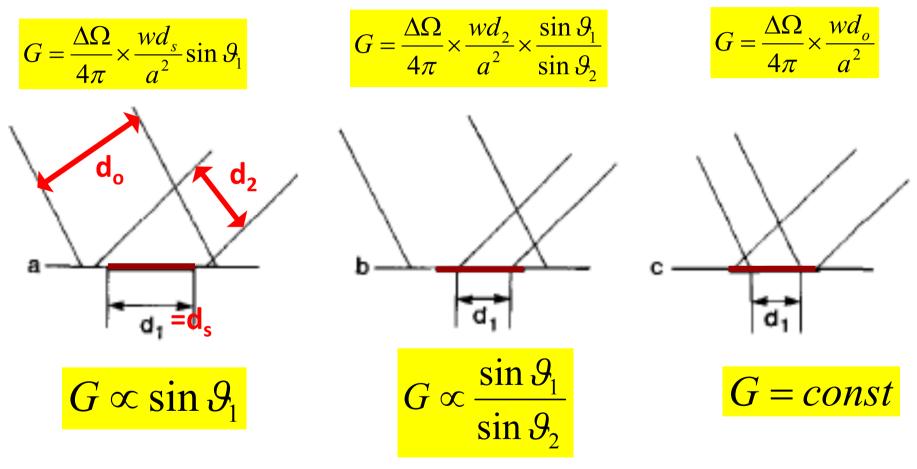
$$\mu = \mu_0 + \mu_i \qquad k = \frac{\mu_i}{\mu}$$

The divergent angle of the excitation is 60° Aipolipes that of the excitation is coverse 20° of 100° point in 20° point and the additular mictor & Brass gletors 20°.



### **Geometrical considerations in XRF intensities**

#### Incident flux I<sub>o</sub> is expressed in number of photons/s/cm<sup>2</sup>

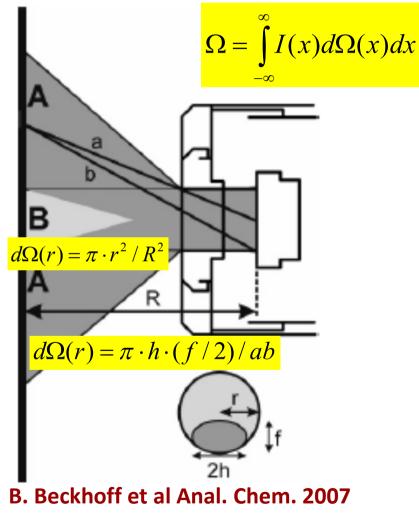


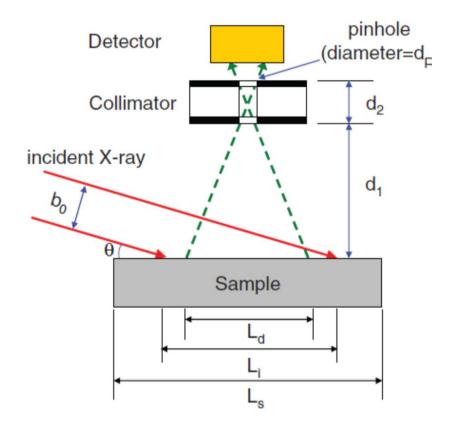
De Boer, XRS, 18, 119, 1989



### **Geometrical considerations in XRF intensities**

### Geometry under GI conditions



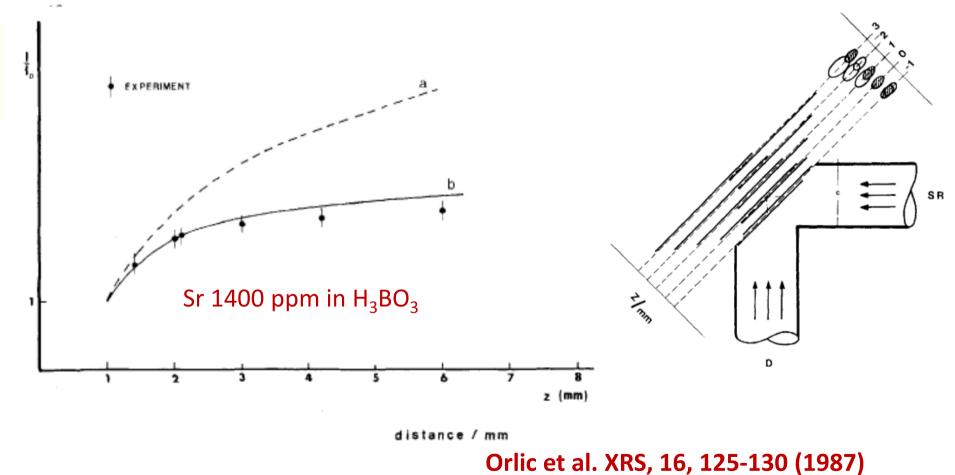


Weblin Ll, Rev. Sci. Instrum. 83, 053114 (2012); doi: 10.1063/1.4722495

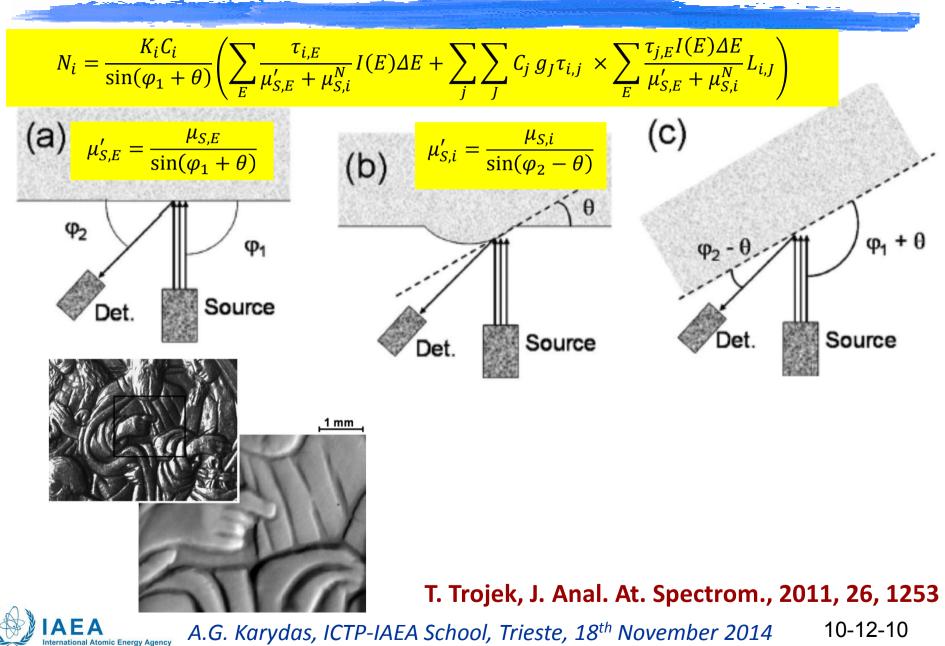


### **Geometrical considerations in XRF intensities**

### Sample Volume effect in millibeam size XRF set-ups







Atoms for Peace

$$\hat{n} \cdot (s_i \hat{b} + s_f \hat{d}) = 0$$

$$s_f = -\frac{\hat{b} \cdot \hat{n}}{\hat{d} \cdot \hat{n}} s_i \equiv k \cdot s_i$$

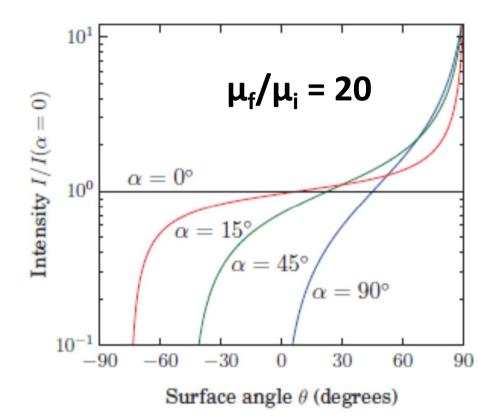
$$k = (\cos a + \tan \theta \sin \alpha)^{-1}$$

$$incident \qquad \theta \quad z \quad b \quad y \quad y \quad s_i = s_i \quad b \quad y \quad s_i = s_i \quad s_i \quad s_i \quad s_i \quad s_i \quad b \quad s_i \quad$$

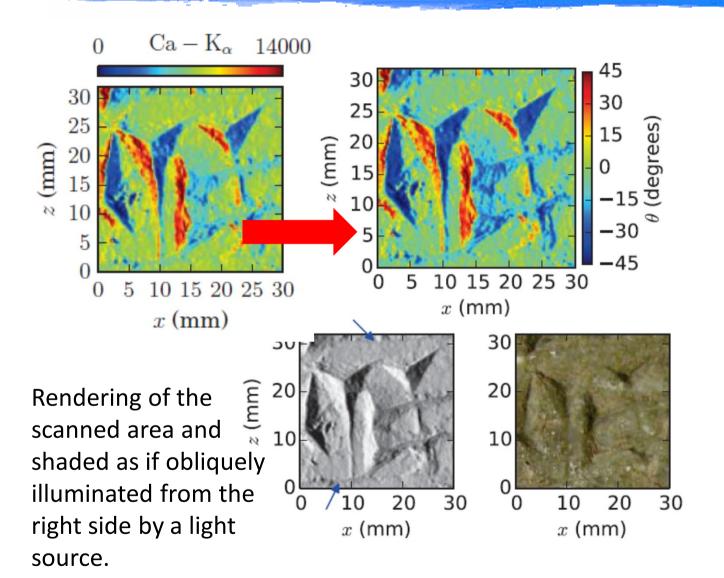
E. C. Geil and R. E. Thorne, J. Synchrotron Rad. (2014), 21, 1358-1363

#### Hints:

The objects should be mounted so that their dominant surface curvature runs perpendicular to the detector—incident beam (x-y) plane



The angle effect vanishes as the detector position approaches the incident beam, and it is maximal when the detector is perpendicular to the beam. CaCO3 matrix, with incident beam energy 16.5keV



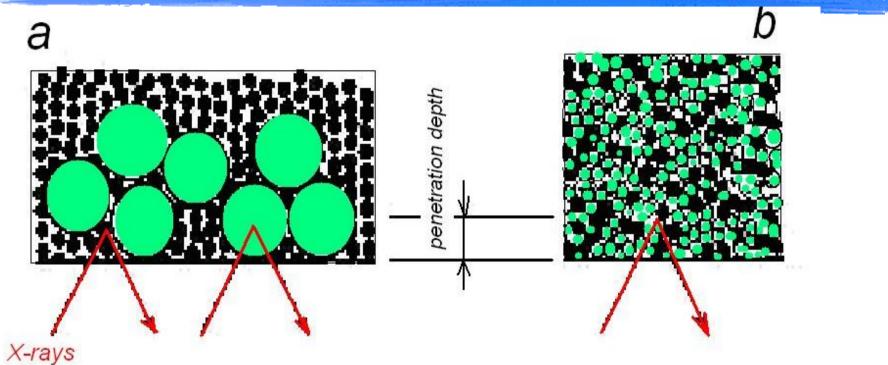
Map of surface angle θ computed from the Ca – Kα fluorescence

Photograph of the scanned area, adjusted to enhance contrast and brightness.



A.G. Karydas, ICTP-IAEA School, Trieste, 18<sup>th</sup> November 2014 10-12-10

### Sample effects – Particle size



Example: Fe2O3

50% of 8 -12 keV from 30µm – 60µm

90% of 8 -12 keV from 100 $\mu$ m – 200 $\mu$ m

Information originates only from the first two layers



### Particle size correction models

Berry et al (Adv. X-ray Anal. 12, 612 1969)

- o Dependence of fluorescence intensity on:
  - $\overline{d} = 2/3$  diameter of sphere •  $\eta = \text{packing ratio}, \quad m = \frac{c_{nf}}{c_f} \qquad D \approx 10nm$

$$P_{ja} = \frac{1 - \exp\left[(\mu_f + \mu_f') \cdot \rho_f \cdot \overline{d}\right]}{1 - \exp\left[(\mu_f + \mu_f') \cdot \rho_f \cdot D\right]} \cdot \frac{\left\{1 - \eta + \eta \cdot \exp(-\mu_f \cdot \rho_f \cdot D) + \eta \cdot m \cdot \exp(-\mu_{nf} \cdot \rho_{nf} \cdot D)\right\}}{\left\{1 - \eta + \eta \cdot \exp(-\mu_f \cdot \rho_f \cdot \overline{d}) + \eta \cdot m \cdot \exp(-\mu_{nf} \cdot \rho_{nf} \cdot \overline{d})\right\}}$$

$$\mu_f = \sum_f c_f \frac{\mu_f(E_0)}{\sin \psi_1} \qquad \qquad \mu_{nf} = \sum_{nf} c_{nf} \frac{\mu_{nf}(E_0)}{\sin \psi_1}$$

$$\mu'_{f} = \sum_{f} c_{f} \frac{\mu_{f}(E_{j})}{\sin \psi_{2}} \qquad \qquad \mu'_{nf} = \sum_{nf} c_{nf} \frac{\mu_{nf}(E_{j})}{\sin \psi_{2}}$$



# **Overview - Conclusions**

- The quantitative XRF analysis is currently supported by a well-defined mathematical formalism based on the so-called fundamental parameters approach
- The majority of second/third order phenomena that affect the analyte fluorescence intensity are described by analytical formulas
  Obstacles:
- Enhancement due to electrons ionization requires verification and currently is not taken into account routinely
- Accuracy of fundamental parameters (soft energy region) and for L, M characteristic X-rays

#### Perspectives

Monte Caro methods it is the most comprehensive tool to account for all high-order phenomena and assess their contribution in fluorescence intensities

A.G. Karydas, ICTP-IAEA School, Trieste, 18th November 2014

□ FP re-evaluation by means of metrological SR experiments

IAEA International Atomic Energy Ag

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