Molecular Dynamics Optimization and Parallelization Case Study

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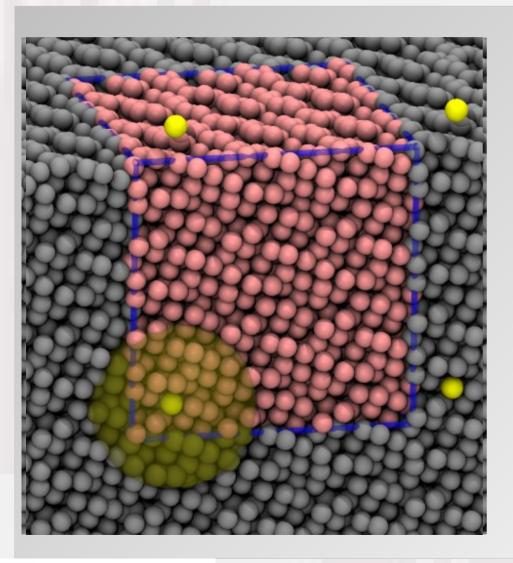


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0) The Model for Liquid Argon



 Cubic box of particles with a Lennard-Jones type pairwise additive interaction potential

$$U(r) = \sum_{i,j} \left\{ 4 \in \left[\left(\frac{\sigma}{r_{ij}} \right)^{12} - \left(\frac{\sigma}{r_{ij}} \right)^{6} \right], \quad r_{ij} < r_{c} \\ 0, \quad r_{ij} \ge r_{c} \right\}$$

 Periodic boundary conditions to avoid surface effects



Newton's Laws of Motion

- We consider our particles to be classical objects so Newton's laws of motion apply:
 - 1. In absence of a force a body rests or moves in a straight line with constant velocity
 - 2. A body experiencing a force \mathbf{F} experiences an acceleration \mathbf{a} related to \mathbf{F} by $\mathbf{F} = m\mathbf{a}$, where m is the mass of the body.
 - 3. Whenever a first body exerts a force **F** on a second body, the second body exerts a force **-F** on the first body (*Bonus Law*)



Velocity-Verlet Algorithm

 The Velocity-Verlet algorithm is used to propagate positions and velocities of the atoms

$$\vec{x} \overrightarrow{v_{i}}(t + \frac{\Delta t}{2}) = \vec{x_{i}}(\vec{v_{i}}(t)) \vec{v_{i}}(t) \vec{v_{i}}(t)$$

L. Verlet, Phys. Rev. 159, 98 (1967); Phys. Rev. 165, 201 (1967).



What Do We Need to Program?

- 1. Read in parameters and initial status and compute what is missing (e.g. accelerations)
- 2. Integrate Equations of motion with Velocity Verlet for a given number of steps
 - a) Propagate all velocities for half a step
 - b) Propagate all positions for a full step
 - c) Compute forces on all atoms to get accelerations
 - d) Propagate all velocities for half a step
 - e) Output intermediate results, if needed



1) Initial Serial Code: Velocity Verlet

```
void velverlet(mdsys_t *sys) {
  for (int i=0; i < sys > natoms; ++i) {
     sys->vx[i] += 0.5*sys->dt / mvsq2e * sys->fx[i] / sys->mass;
     sys->vy[i] += 0.5*sys->dt / mvsq2e * sys->fy[i] / sys->mass;
     sys->vz[i] += 0.5*sys->dt / mvsq2e * sys->fz[i] / sys->mass;
    sys->rx[i] += sys->dt*sys->vx[i];
     sys->ry[i] += sys->dt*sys->vy[i];
    sys->rz[i] += sys->dt*sys->vz[i];
  force(sys);
  for (int i=0; i < sys > natoms; ++i) {
     sys->vx[i] += 0.5*sys->dt / mvsq2e * sys->fx[i] / sys->mass;
     sys->vy[i] += 0.5*sys->dt / mvsq2e * sys->fy[i] / sys->mass;
    sys->vz[i] += 0.5*sys->dt / mvsq2e * sys->fz[i] / sys->mass;
```



Initial Code: Force Calculation

```
double pbc(double x, const double boxby2) {
for(i=0; i < (sys->natoms); ++i) {
                                        while (x > boxby2) x = boxby2 + boxby2;
  for(j=0; j < (sys->natoms); ++j) {
                                        while (x < -boxby2) x += boxby2 + boxby2;
    if (i==j) continue;
                                        return x;
    rx = pbc(sys - rx[i] - sys - rx[j], 0.5*sys - box);
                                                     Compute distance
    ry=pbc(sys->ry[i] - sys->ry[j], 0.5*sys->box);
                                                     between atoms i & j
    rz=pbc(sys->rz[i] - sys->rz[j], 0.5*sys->box);
    r = sqrt(rx*rx + ry*ry + rz*rz);
                                            Compute energy and force
    if (r < sys -> rcut) {
       ffac = -4.0*sys->epsilon*(-12.0*pow(sys->sigma/r,12.0)/r
                       +6*pow(sys->sigma/r,6.0)/r);
       sys->epot += \underline{0.5}*4.0*sys->epsilon*(pow(sys->sigma/r,12.0)
                          -pow(sys->sigma/r,6.0));
       sys->fx[i] += rx/r*ffac;
                                       Add force contribution
       sys->fy[i] += ry/r*ffac;
                                       of atom j on atom i
       sys->fz[i] += rz/r*ffac;
```



How Well Does it Work?

Compiled with:
 gcc -o ljmd.x -pg ljmd.c -lm
 Test input: 108 atoms, 10000 steps: 49s
 Let us get a profile (using gprof):

9	cumulative	self		self	total	
time	seconds	seconds	calls	ms/call	ms/call	name
73.70	13.87	13.87	10001	1.39	1.86	force
24.97	18.57	4.70	346714668	0.00	0.00	pbc
0.96	18.75	0.18				main
0.37	18.82	0.07	10001	0.01	0.01	ekin
0.00	18.82	0.00	30006	0.00	0.00	azzero
0.00	18.82	0.00	101	0.00	0.00	output
0.00	18.82	0.00	12	0.00	0.00	getline



Step One: Compiler Optimization

- Use of pbc() is convenient, but costs 25% time
 => compiling with -O3 should inline it
- Loops should be unrolled for superscalar CPUs => compiling with -O2 or -O3 should do it for us
 Time now: 39s (1.3x faster) Only a bit faster than 49s
- Now try more aggressive optimization options:
 -ffast-math -fexpensive-optimizations -msse3
 Time now: 10s (4.9x faster) Much better!
- Compare to LAMMPS: 3.6s => need to do more



Now Modify the Code

• Use physics! Newton's 3^{rd} law: $F_{ij} = -F_{ji}$

```
for (i=0; i < (sys->natoms)-1; ++i) {
  for (j=i+1; j < (sys->natoms); ++j) {
    rx=pbc(sys->rx[i] - sys->rx[j], 0.5*sys->box);
    ry=pbc(sys->ry[i] - sys->ry[j], 0.5*sys->box);
    rz=pbc(sys->rz[i] - sys->rz[j], 0.5*sys->box);
    r = sqrt(rx*rx + ry*ry + rz*rz);
    if (r < sys->rcut) {
      ffac = -4.0*sys->epsilon*(-12.0*pow(sys->sigma/r,12.0)/r
                                 +6*pow(sys->sigma/r,6.0)/r);
                       4.0*sys->epsilon*(pow(sys->sigma/r,12.0)
      sys->epot +=
                                 -pow(sys->sigma/r,6.0));
      sys->fx[i] += rx/r*ffac;
                                     sys->fx[j] -= rx/r*ffac;
      sys \rightarrow fy[i] += ry/r*ffac; sys \rightarrow fy[j] -= ry/r*ffac;
      sys->fz[i] += rz/r*ffac; sys->fz[j] -= rz/r*ffac;
} } }
```

Time now: 5.4s (9.0x faster) Another big improvement



More Modifications

Avoid expensive math: pow(), sqrt(), division

```
c12=4.0*sys->epsilon*pow(sys->sigma, 12.0);
c6 = 4.0 \text{ sys} - \text{sepsilon*pow} (\text{sys} - \text{sigma, } 6.0);
rcsq = sys->rcut * sys->rcut;
for (i=0; i < (sys->natoms)-1; ++i) {
  for (j=i+1; j < (sys->natoms); ++j) {
    rx=pbc(sys->rx[i] - sys->rx[j], 0.5*sys->box);
    ry=pbc(sys->ry[i] - sys->ry[j], 0.5*sys->box);
    rz=pbc(sys->rz[i] - sys->rz[j], 0.5*sys->box);
    rsq = rx*rx + ry*ry + rz*rz;
    if (rsq < rcsq) {
      double r6, rinv; rinv=1.0/rsq; r6=rinv*rinv*rinv;
      ffac = (12.0*c12*r6 - 6.0*c6)*r6*rinv;
      svs - > epot + = r6*(c12*r6 - c6);
       sys \rightarrow fx[i] += rx*ffac; sys \rightarrow fx[j] -= rx*ffac;
      sys->fy[i] += ry*ffac; sys->fy[j] -= ry*ffac;
       sys \rightarrow fz[i] += rz*ffac; sys \rightarrow fz[j] -= rz*ffac;
} } }
```

=> 108 atoms: 4.0s (12.2x faster) still worth it



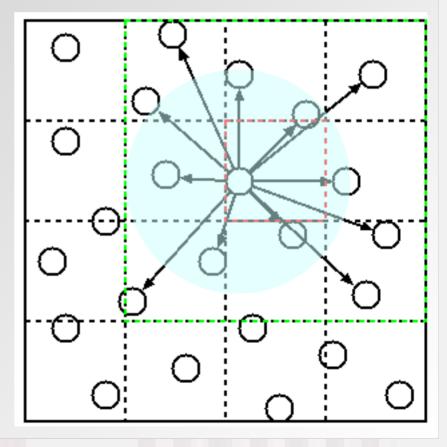
Improvements So Far

- Use the optimal compiler flags => ~5x faster but some of it: inlining, unrolling could be coded
- Use our knowledge of physics => ~2x faster since we need to compute only half the data.
- Use our knowledge of computer hardware => 1.35x faster. (could be more: SSE/AVX)
 We are within 10% (4s vs. 3.6s) of LAMMPS.
- Try a bigger system: 2916 atoms, 100 steps
 Our code: 13.3s LAMMPS: 2.7s => Bad scaling with system size



2) Making it Scale with System Size

- Lets look at the algorithm again:
 We compute all distances between pairs
- But for larger systems not all pairs contribute and our effort is O(N²)
- So we need a way to avoid looking at pairs that are too far away
 - => Sort atoms into cell lists, which is O(N)





The Cell-List Variant

- At startup build a list of lists to store atom indices for atoms that "belong" to a cell
- Compute a list of pairs between cells which contain atoms within cutoff. Doesn't change!
- During MD sort atoms into cells
- Then loop over list of "close" pairs of cells i and j
- For pair of cells loop over pairs of atoms in them
- Now we have linear scaling with system size at the cost of using more memory and an O(N) sort



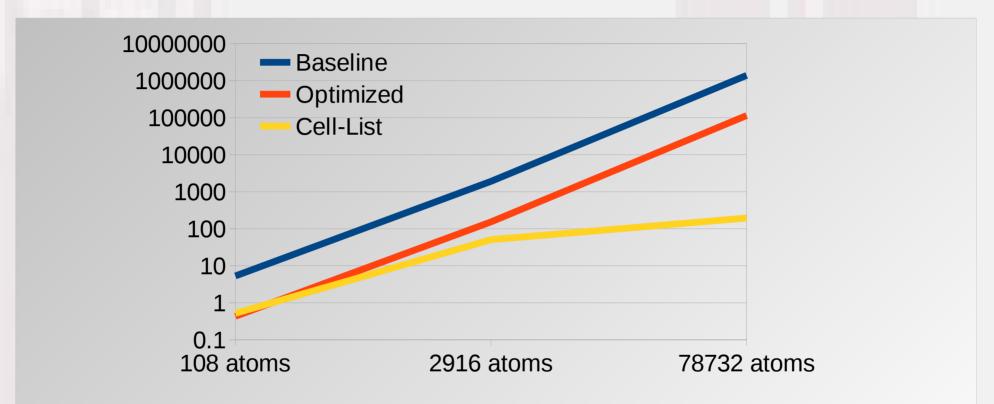
Cell List Loop

```
for(i=0; i < sys->npair; ++i) {
    cell t *c1, *c2;
    c1=sys->clist + sys->plist[2*i];
    c2=sys->clist + sys->plist[2*i+1];
        for (int j=0; j < c1->natoms; ++j) {
            int ii=c1->idxlist[j];
            double rx1=sys->rx[ii];
            double ry1=sys->ry[ii];
            double rz1=sys->rz[ii];
            for (int k=0; k < c2->natoms; ++k) {
                double rx, ry, rz, rsq;
                int jj=c2->idxlist[k];
                rx=pbc(rx1 - sys->rx[jj], boxby2, sys->box);
                ry=pbc(ry1 - sys->ry[jj], boxby2, sys->box);
```

2916 atom time: 3.4s (4x faster), LAMMPS 2.7s



Scaling with System Size



 Cell list does not help (or hurt) much for small inputs, but is a huge win for larger problems
 Lesson: always pay attention to scaling



3) What if optimization is not enough?

- Having linear scaling is nice, but twice the system size is <u>still</u> twice the work and takes twice the time. => Parallelization
- Simple MPI parallelization first
 - MPI is "share nothing" (<u>replicated</u> or distributed data)
 - Run the same code path with the same data but insert a few MPI calls
 - Broadcast positions from rank 0 to all before force()
 - Compute forces on different atoms for each rank
 - Collect (reduce) forces from all to rank 0 after force()



Replicated Data MPI Version

```
static void force(mdsys_t *sys) {
                               cx/cy/cz on all nodes; fx/fy/fz on master only
  double epot=0.0;
  azzero(sys->cx,sys->natoms); azzero(sys->cy,sys->natoms); azzero(sys->cz,sys->natoms);
  MPI_Bcast(sys->rx, sys->natoms, MPI_DOUBLE, 0, sys->mpicomm);
  MPI_Bcast(sys->ry, sys->natoms, MPI_DOUBLE, 0, sys->mpicomm);
  MPI_Bcast(sys->rz, sys->natoms, MPI_DOUBLE, 0, sys->mpicomm);
  for (i=0; i < sys->natoms-1; i += sys->nsize) {
    ii = i + sys->mpirank;
    if (ii \geq (sys-\geqnatoms - 1)) break;
    for (j=i+1; i < sys->natoms; ++j) {
   [...]
         sys->cy[j] -= ry*ffac;
         sys->cz[j] -= rz*ffac;
  MPI_Reduce(sys->cx, sys->fx, sys->natoms, MPI_DOUBLE, MPI_SUM, 0, sys->mpicomm);
  MPI_Reduce(sys->cy, sys->fy, sys->natoms, MPI_DOUBLE, MPI_SUM, 0, sys->mpicomm);
  MPI_Reduce(sys->cz, sys->fz, sys->natoms, MPI_DOUBLE, MPI_SUM, 0, sys->mpicomm);
  MPI_Reduce(&epot, &sys->epot, 1, MPI_DOUBLE, MPI_SUM, 0, sys->mpicomm);
```

Easy to implement, but lots of communication



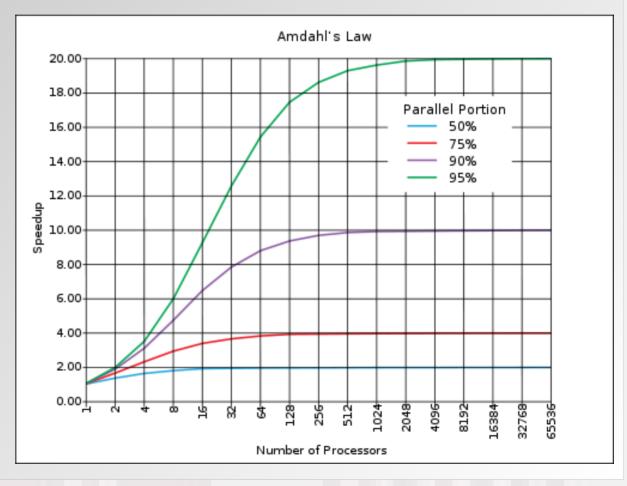
Replicated Data Limitations

Amdahl's Law (we only parallelized the force

computation)

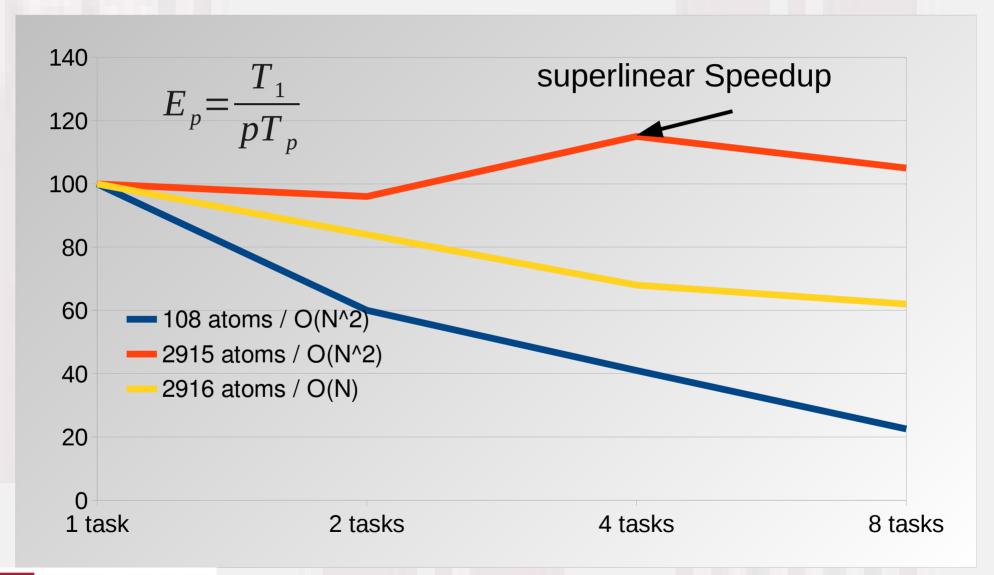
Parallel
 overhead
 (grows with
 system size):

- Broadcast
- Reduction
- Limited scaling



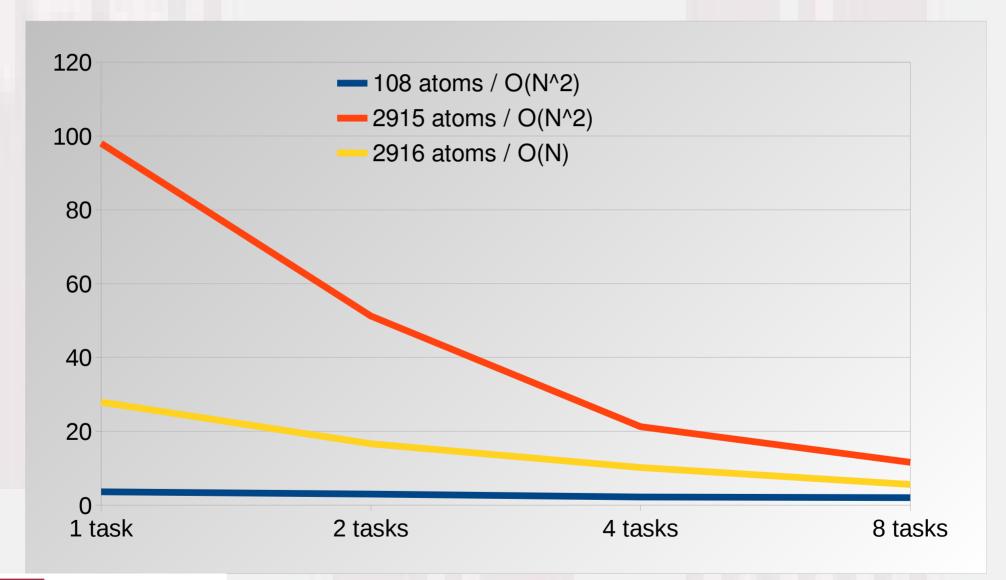


MPI Parallel Efficiency





MPI Parallel Execution Times





4) OpenMP Parallelization

- OpenMP is directive based
 => code (can) work without them
- OpenMP can be added incrementally
- OpenMP only works in shared memory
 => multi-socket nodes, multi-core processors
- OpenMP hides the calls to a threads library
 => less flexible, but much less programming
- Caution: write access to shared data can easily lead to race conditions



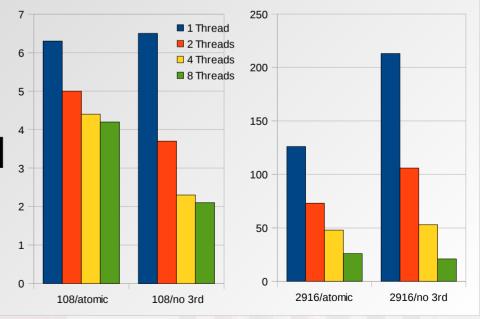
Naive OpenMP Version

```
#if defined(OPENMP)
  #pragma omp parallel for default(shared) \
      private(i) reduction(+:epot)
                                              Each thread will
  #endif
      for(i=0; i < (sys->natoms)-1; ++i) { work on different
          double rx1=sys->rx[i];
                                              values of "i"
          double ry1=sys->ry[i];
          double rz1=sys->rz[i];
           [\ldots]
                             The "critical" directive will let only
  #if defined(_OPENMP)
  #pragma omp critica
                       sys->oneithreachexecute this delochattorime
  #endif
                       sys->fy[i] += ry*ffac;
                                                 "i" will be unique for
                       sys->fz[i] += rz*ffac;
                                                each thread, but not "j"
                       sys->fx[j] -= rx*ffac;
Timings (108 atoms):
                       sys->fy[j] -= ry*ffac;
                                                => multiple threads may
1 thread: 4.2s
                       sys->fz[j] -= rz*ffac;
                                                 write to the same location
2 threads: 7.1s
                       sys->fx[j] -= rx*ffac;
                                                concurrently
                       sys->fy[j] -= ry*ffac;
4 threads: 7.7s
                       sys->fz[j] -= rz*ffac;
8 threads: 8.6s
```



OpenMP Improvements

- Use omp atomic to protect one instruction
 - => faster, but requires hardware support
 - => some speedup, but serial is faster for 108, at 2916 atoms we are often beyond cutoff
- No Newton's 3rd Law:
 - => no race condition
 - => better scaling, but we lose 2x serial speed
 - => need 8 threads to be faster than **atomic**





MPI-like Approach with OpenMP

```
#if defined(OPENMP)
#pragma omp parallel reduction(+:epot)
#endif
    { double *fx, *fy, *fz;
#if defined(OPENMP)
        int tid=omp_get_thread_num(); Thread Id is like MPI rank
#else
                     sys->fx holds storage for one full fx array for
        int tid=0;
                     each thread => race condition is eliminated.
#endif
        fx=sys->fx + (tid*sys->natoms); azzero(fx,sys->natoms);
        fy=sys->fy + (tid*sys->natoms); azzero(fy,sys->natoms);
        fz=sys->fz + (tid*sys->natoms); azzero(fz,sys->natoms);
        for (int i=0; i < (sys->natoms -1); i += sys->nthreads) {
            int ii = i + tid;
            if (ii >= (sys->natoms -1)) break;
            rx1=sys->rx[ii];
            ry1=sys->ry[ii];
            rz1=sys->rz[ii];
```



MPI-like Approach with OpenMP (2)

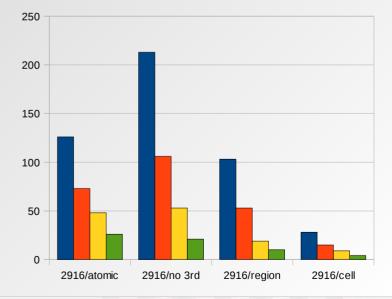
We need to write our own reduction:

```
#if defined ( OPENMP)
                            Need to make certain, all threads
#pragma omp barrier
                            are done with computing forces
#endif
    i = 1 + (sys->natoms / sys->nthreads);
    fromidx = tid * i;
    toidx = fromidx + i;
    if (toidx > sys->natoms) toidx = sys->natoms;
    for (i=1; i < sys->nthreads; ++i) {
         int offs = i*sys->natoms;
         for (int j=fromidx; j < toidx; ++j) {</pre>
                                                        Use threads to
              sys \rightarrow fx[j] += sys \rightarrow fx[offs+j];
                                                        parallelize the
              sys \rightarrow fy[j] += sys \rightarrow fy[offs+j];
                                                        reductions
              sys \rightarrow fz[j] += sys \rightarrow fz[offs+j];
```



More OpenMP Timings

- The omp parallel region timings
 2916: 1T: 103s, 2T: 53s, 4T: 19s, 8T: 10s
 => better speedup, but serial is faster for 108, at 2916 atoms we are often beyond cutoff
- This approach also works with cell lists
 - => with 8 threads:
 - 4.1s = 6.8x speedup vs. serial cell list version (28s). That is <u>62x</u> faster than the first naive serial version





6) Hybrid OpenMP/MPI Version

- With multi-core nodes, communication between MPI tasks becomes a problem
 - => all communication has to us2 one link
 - => reduced bandwidth, increased latency
- OpenMP and MPI parallelization are orthogonal and can be used at the same time Caution: don't call MPI from threaded region!
- Parallel region OpenMP version is very similar to MPI version, so that would be easy to merge



Hybrid OpenMP/MPI Kernel

- MPI tasks are like GPU thread blocks
- Need to reduce forces/energies first across threads and then across all MPI tasks

```
incr = sys->mpisize * sys->nthreads;
/* self interaction of atoms in cell */
for(n=0; n < sys->ncell; n += incr) {
    int i, j;
    const cell_t *c1;

    i = n + sys->mpirank*sys->nthreads + tid;
    if (i >= sys->ncell) break;
    c1=sys->clist + i;

for (j=0; j < c1->natoms-1; ++j) {
[...]
```

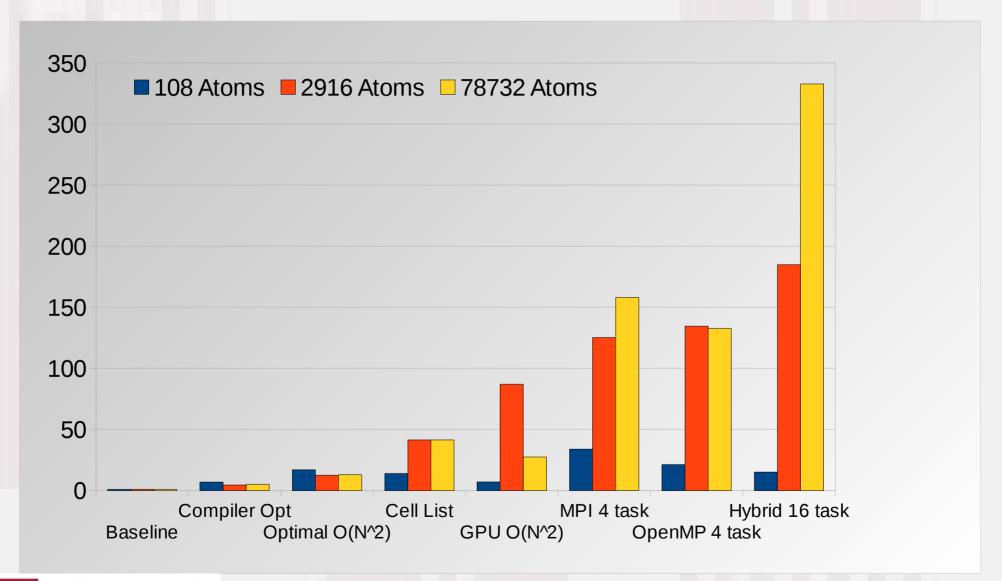


Hybrid OpenMP/MPI Timings

Cell list serial code:	18s	50.1s	Tw
16 MPI x 1 Threads:	14s	19.8s	Two nodes with
8 MPI x 2 Threads:	5.5s	8.9s	des
4 MPI x 4 Threads:	4.3s	8.2s	with
2 MPI x 8 Threads:	4.0s	7.3s	2 _X
=> Best speedup: =>Total speedup:	4.5x 185 x	6.9x 333x	quad-core



Total Speedup Comparison





What about GPUs?

- GPUs are threading taken to the extreme
- Programming models: CUDA (like C), OpenCL (more explicit but portable across hardware), OpenACC (like OpenMP)
- Need to generate >1000 work units:
 - => One (or more) thread(s) per "i atom"
 - => good weak scaling, limited strong scaling
- Offload only some kernels (GPU=accelerator)
 vs. moving entire calculation (CPU=decelerator)
 => depends on problem size, choice of hardware



Conclusions

- Make sure that you exploit the physics of your problem well => Newton's 3rd law gives a 2x speedup for free (but interferes with threading!)
- Let the compiler help you (more readable code), but also make it easy to the compiler
 => unrolling, inlining can be offloaded
- Understand the properties of your hardware and adjust your code to match it
- Best strong scaling on current hardware with hybrid parallelization, e.g. MPI+OpenMP

