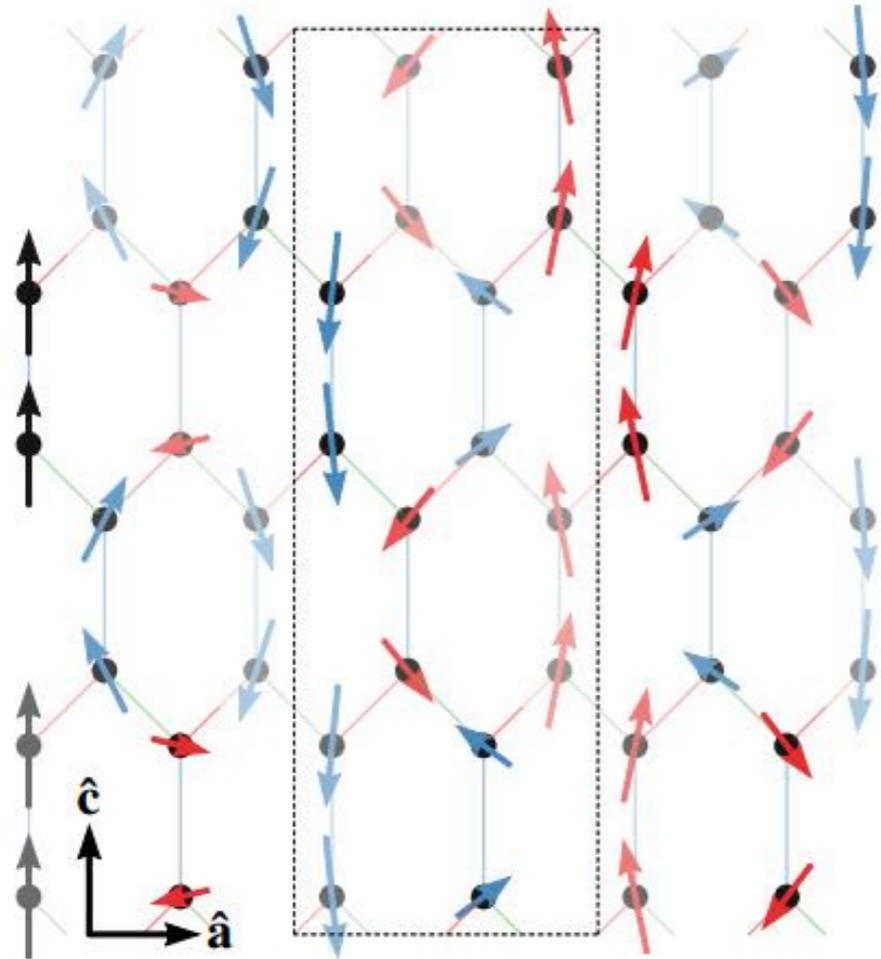


$\beta\text{-Li}_2\text{IrO}_3$

# Counter-rotating Incommensurate Non-Coplanar Spiral Orders

Radu Coldea,  
P. Gegenwart (2014)

EXPERIMENT



$$F = [+ , + , + , +]$$

$$C = [+ , + , - , -]$$

$$G = [+ , - , + , -]$$

$$A = [+ , - , - , +]$$

$$\mathbf{Q}_{\text{exp}} = (0.57, 0, 0)$$

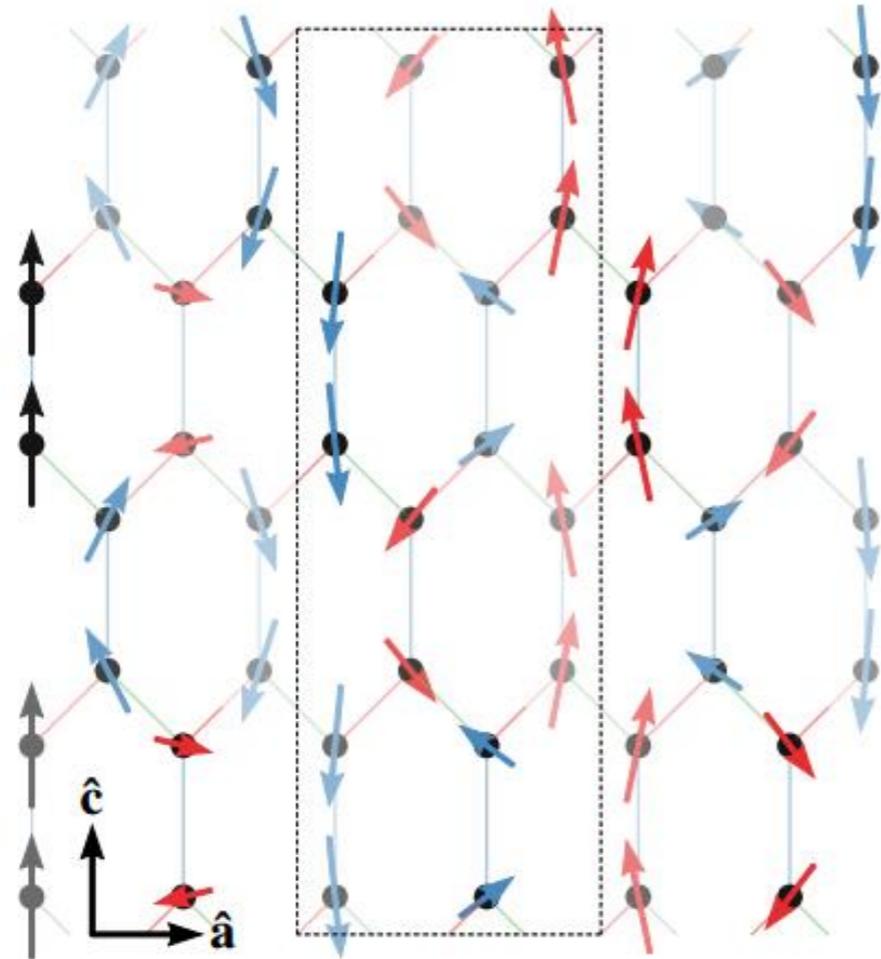
$$(iA_a, iC_b, F_c)$$

$\beta\text{-Li}_2\text{IrO}_3$

# Counter-rotating Incommensurate Non-Coplanar Spiral Orders

Radu Coldea,  
P. Gegenwart (2014)

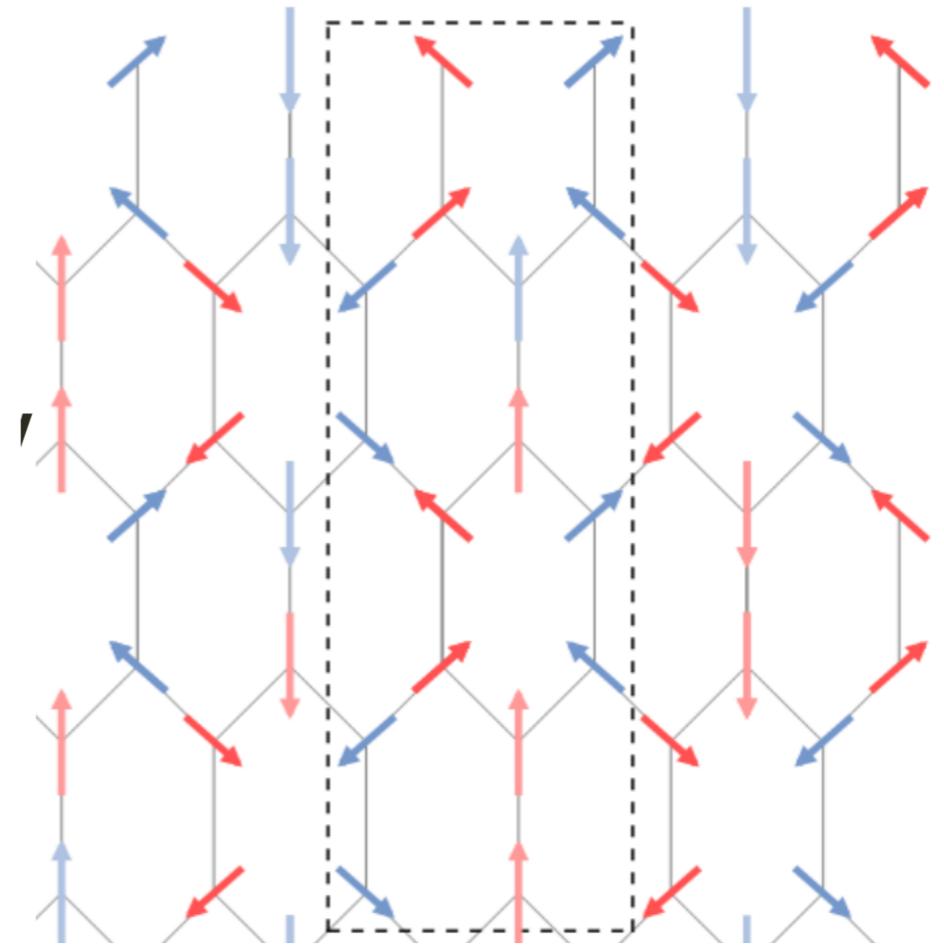
EXPERIMENT



$$\mathbf{Q}_{\text{exp}} = (0.57, 0, 0)$$

$$(iA_a, iC_b, F_c)$$

THEORY



SYMMETRY  
AGREES

$$\mathbf{Q} = (h'00) \quad 0.53 \lesssim h' \lesssim 0.80$$

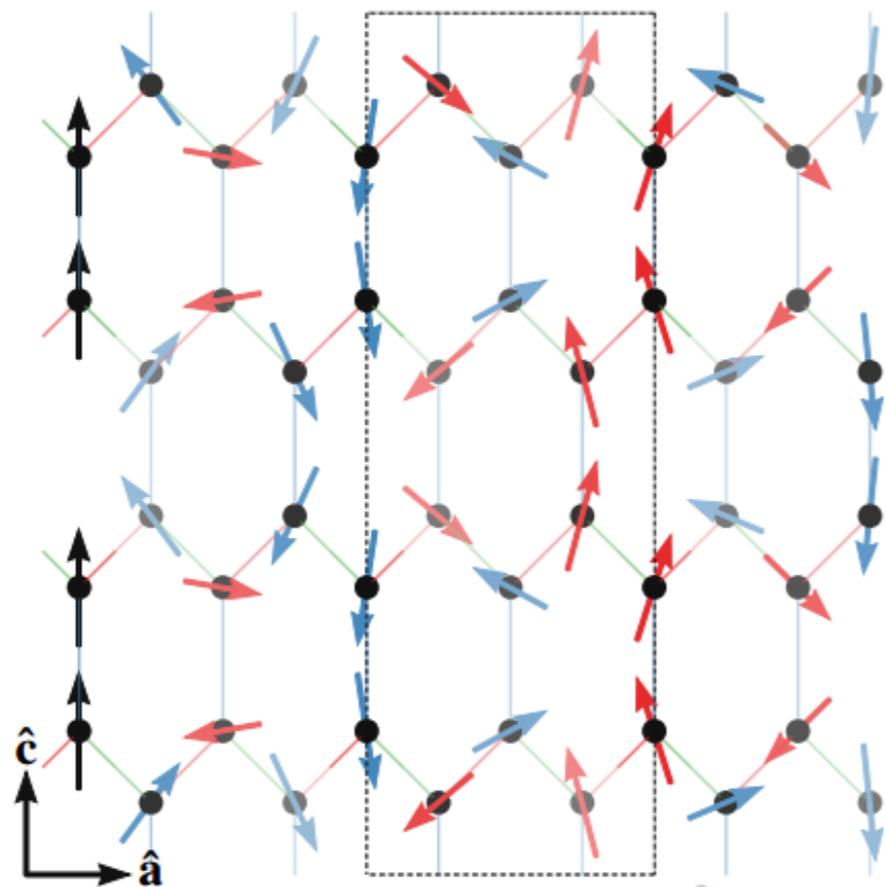
$$(iA_a, iC_b, F_c)$$

$\gamma$ -Li<sub>2</sub>IrO<sub>3</sub>

# Counter-rotating Incommensurate Non-Coplanar Spiral Orders

Radu Coldea,  
James Analytis  
(2014)

EXPERIMENT



$$\mathbf{Q}_{\text{exp}} = (0.57, 0, 0)$$

$$F = [+ , + , + , +]$$

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$$G = [+ , - , + , -]$$

$$A = [+ , - , - , +]$$

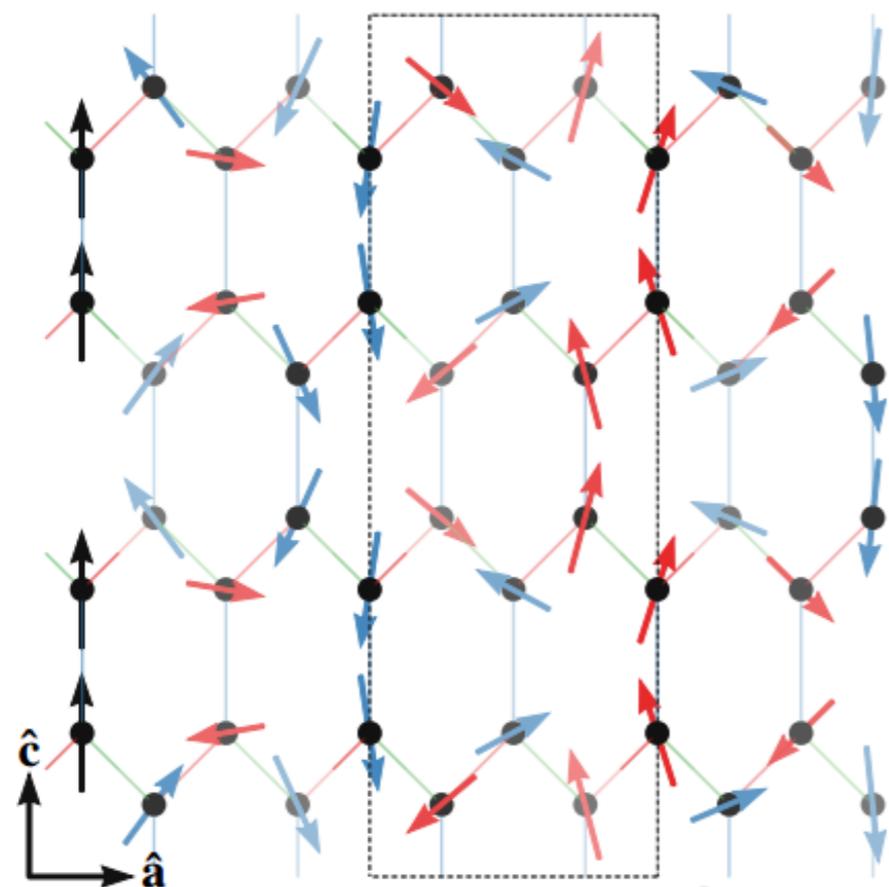
$$[i(A, -A)_a, (-1)^m i(F, -F)_b, (\bar{F}, F)_c]$$

$\gamma$ -Li<sub>2</sub>IrO<sub>3</sub>

# Counter-rotating Incommensurate Non-Coplanar Spiral Orders

Radu Coldea,  
James Analytis  
(2014)

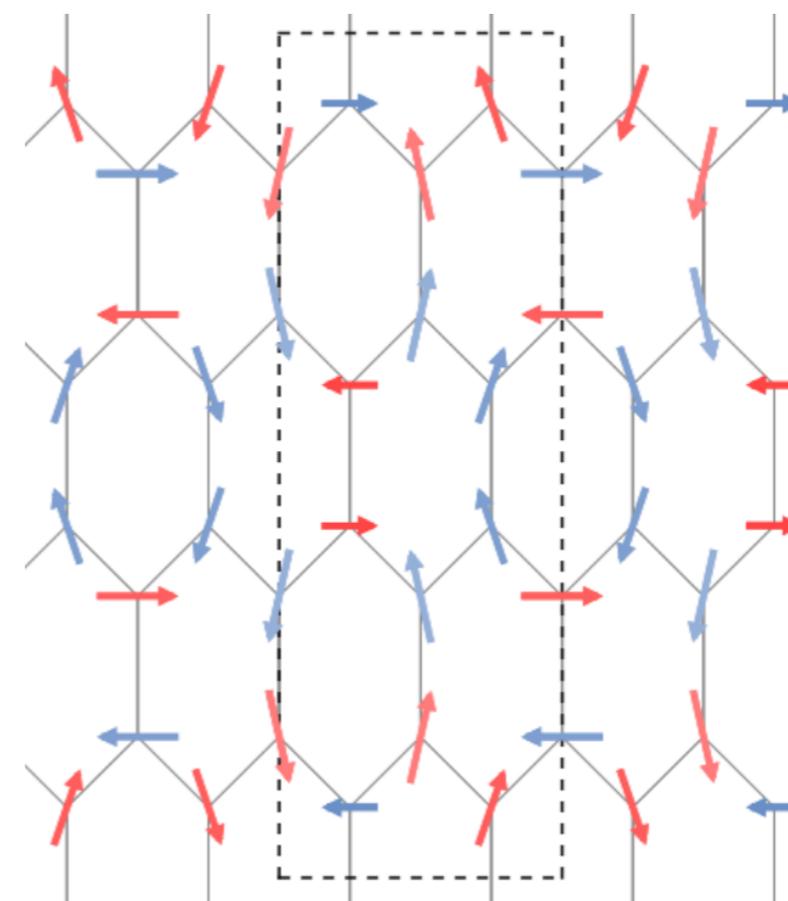
EXPERIMENT



$$\mathbf{Q}_{\text{exp}} = (0.57, 0, 0)$$

$$[i(A, -A)_a, (-1)^m i(F, -F)_b, (\bar{F}, F)_c]$$

THEORY

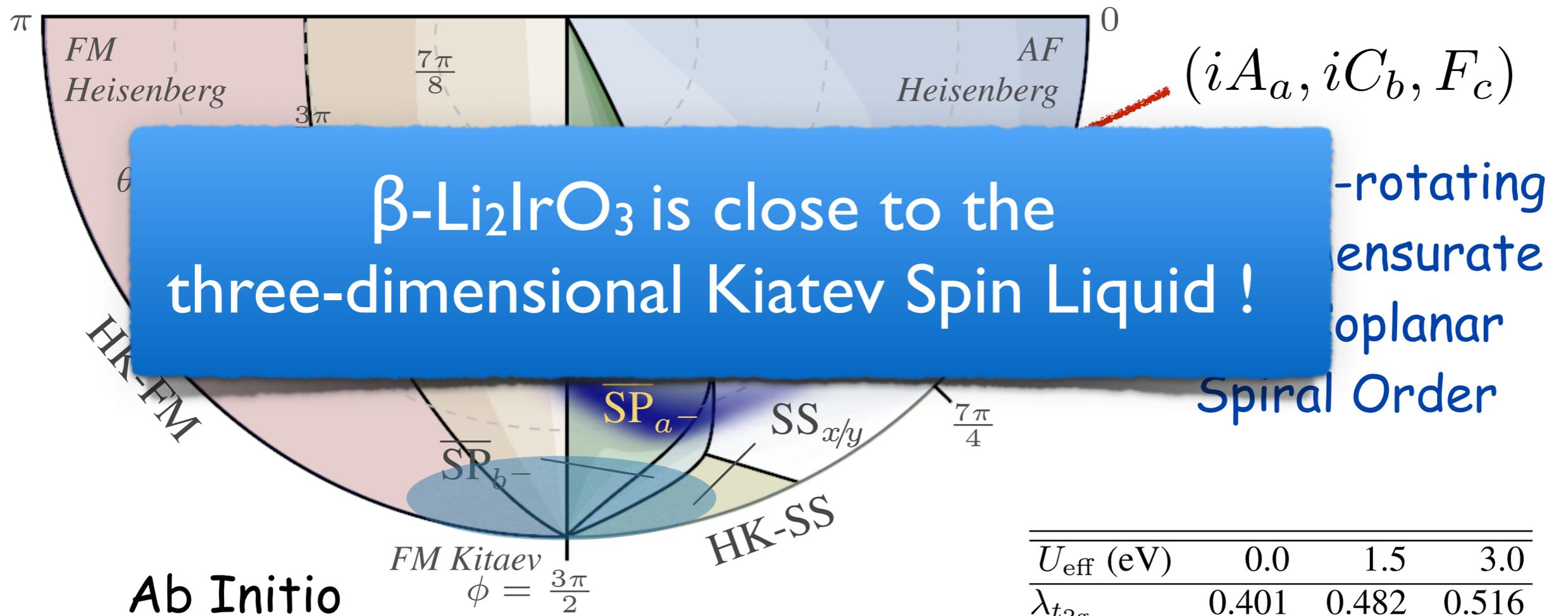


$$\mathbf{Q} = (h'00) \quad 0.53 \lesssim h' \lesssim 0.80$$

$$[i(A, -A)_a, -i(C, -C)_b, (F, F)_c]$$

SYMMETRY  
DISAGREES  
IN  $b$  COMP

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} \left[ J \vec{S}_i \cdot \vec{S}_j + K S_i^\gamma S_j^\gamma + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha) \right]$$



$U_{\text{eff}}$ (eV)	0.0	1.5	3.0
$\lambda_{t_{2g}}$	0.401	0.482	0.516
$t_1$ Z	+0.085	+0.077	+0.064
X	+0.083	+0.074	+0.058
$ t_2 $ Z	0.238	0.255	0.270
X	0.260	0.276	0.289
$t_3$ Z	-0.162	-0.119	-0.060
X	-0.153	-0.110	-0.055

# Coupled Zig-Zag Chain (CZC) Model

**FM KITAEV**, HIGHLY BOND ANISOTROPIC

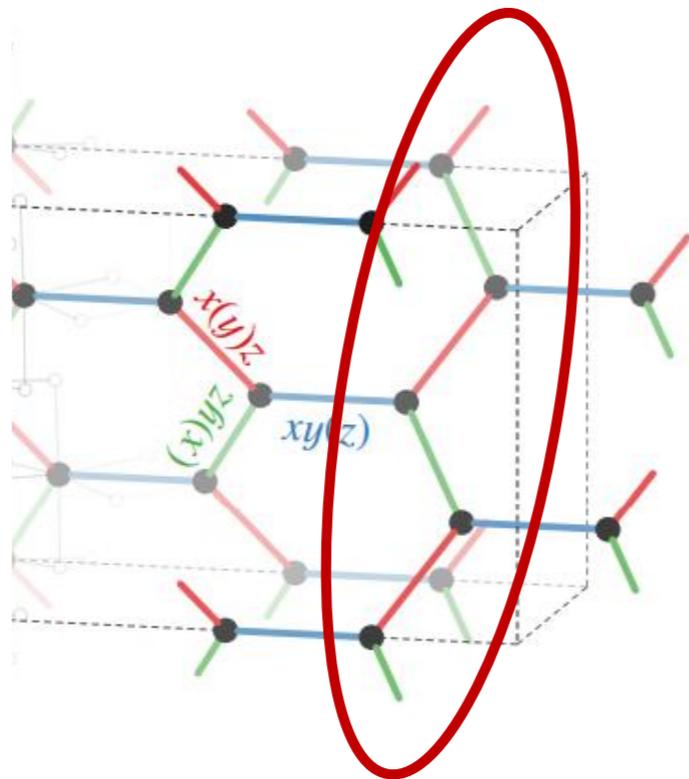
$$H = \sum_{\langle ij \rangle \in \gamma} [J \vec{S}_i \cdot \vec{S}_j + K S_i^\gamma S_j^\gamma] + \sum_{\langle ij \rangle \in Z} I_c (\hat{r}_{ij} \cdot \vec{S}_i) (\hat{r}_{ij} \cdot \vec{S}_j)$$

$$J_Z = J + \frac{1}{2} I_c \quad K_Z = K - \frac{1}{2} I_c$$

$$J_{X/Y} = J \quad K_{X/Y} = K$$

$$\Gamma_Z = \frac{1}{2} I_c$$

$$\Gamma_{X/Y} = 0$$



I KIMCHI, R COLDEA, A VISHWANATH  
PRB 91, 245134 (2015)

# Comparison Study

## MODELS

JK $\Gamma$  TORONTO      CZC BERKELEY

## METHODS

CLASSICAL (SIM ANNEALING)

E. K.-H. Lee, Y. B. Kim,  
PRB 91, 064407 (2015)

SOFT-SPIN (MIX BY HAND)

I KIMCHI, R COLDEA, A VISHWANATH  
PRB 91, 245134 (2015)

# Comparison Study

CLASSICAL (SIM ANN)

SOFT-SPIN

No Mix

Mix

---

JKΓ  
TORONTO

$\beta$

same as exp

$\gamma$

Non-coplanar  
(a, wrong, c)

---

CZC  
BERKELEY

$\beta$

co-planar  
(a, zero, c)

same as exp

$\gamma$

co-planar  
(a, zero, c)

same as exp

# Comparison Study

CLASSICAL (SIM ANN)

SOFT-SPIN

No Mix

Mix

---

JK $\Gamma$   
TORONTO

$\beta$  same as exp

$\gamma$  Non-coplanar  
(a, wrong, c)

---

CZC  
BERKELEY

$\beta$  Commensurate

$\gamma$  Commensurate

co-planar  
(a, zero, c)

co-planar  
(a, zero, c)

same as exp

same as exp

# Comparison Study

CLASSICAL (SIM ANN)

SOFT-SPIN

No Mix

Mix

JKΓ  
TORONTO

$\beta$

same as exp

same as exp

No need

$\gamma$

Non-coplanar  
(a, wrong, c)

Non-coplanar  
(a, wrong, c)

same as exp

CZC  
BERKELEY

$\beta$

Commensurate

co-planar  
(a, zero, c)

same as exp

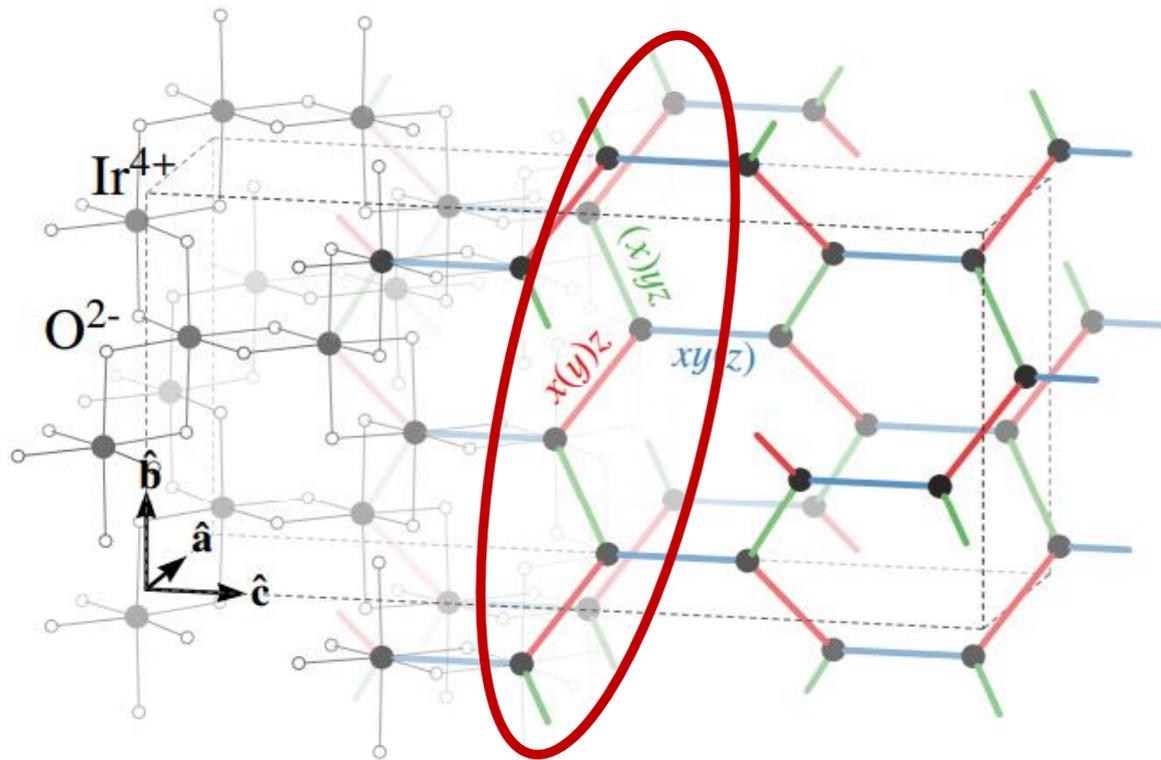
$\gamma$

Commensurate

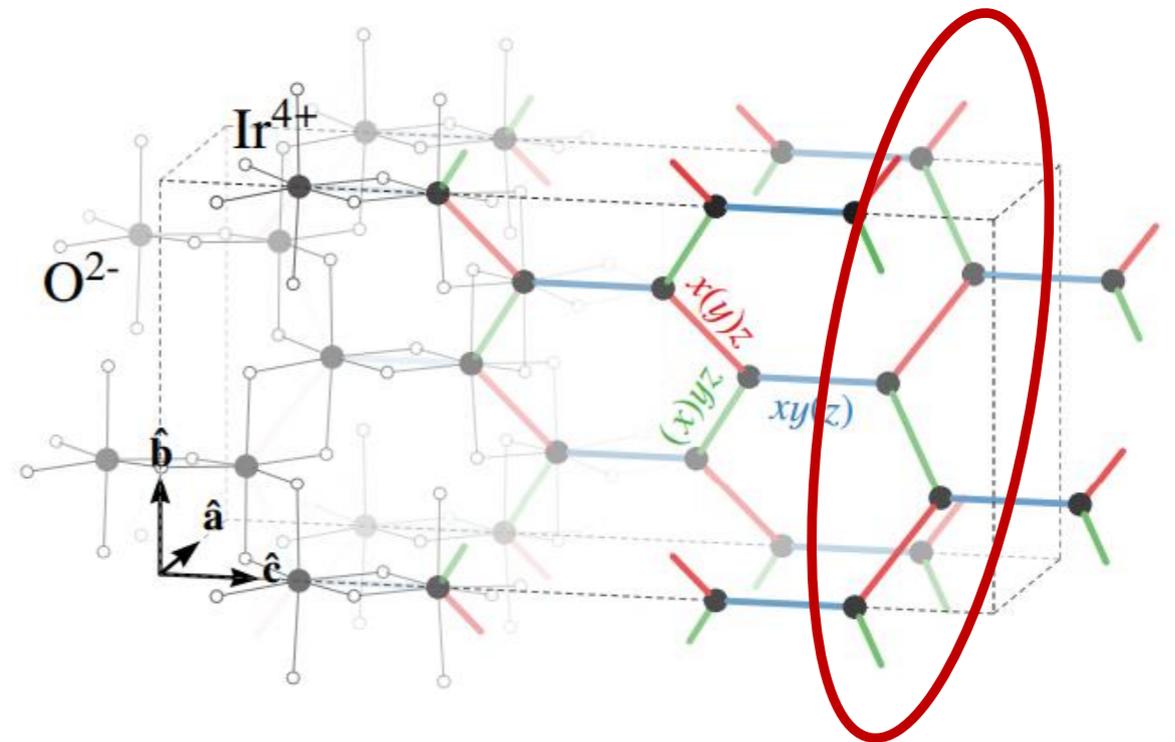
co-planar  
(a, zero, c)

same as exp

# Decoupled Chain Limit



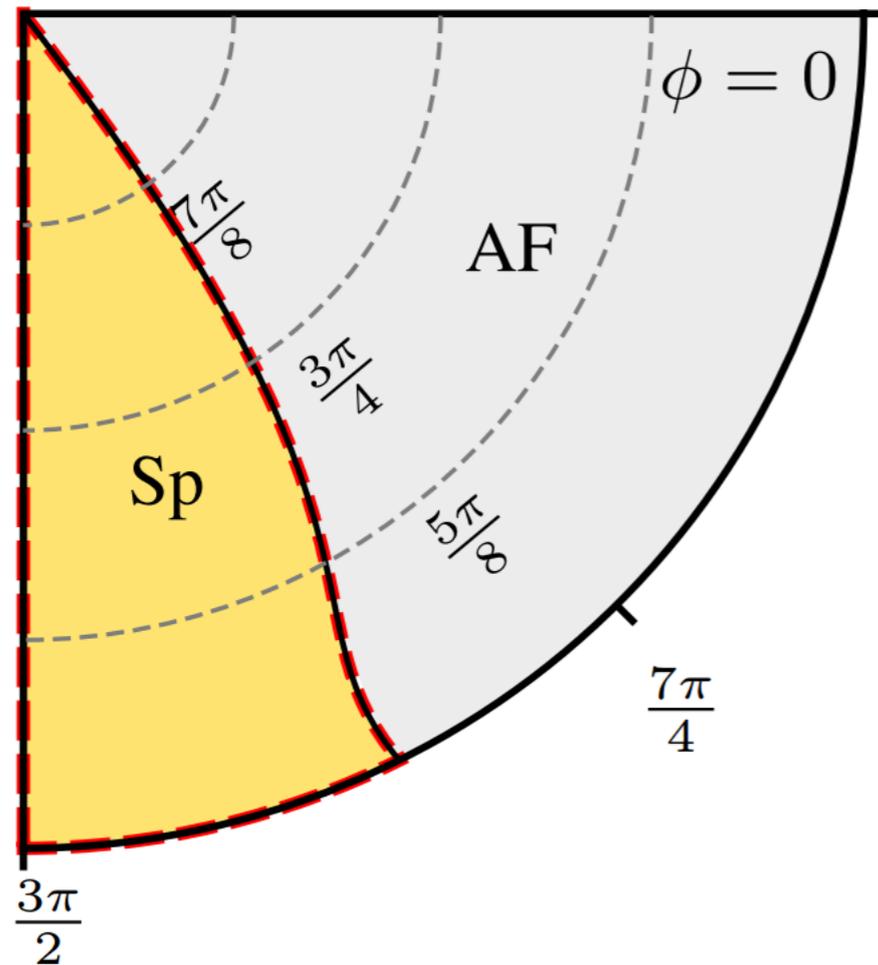
HYPERHONEYCOMB



STRIPYHONEYCOMB

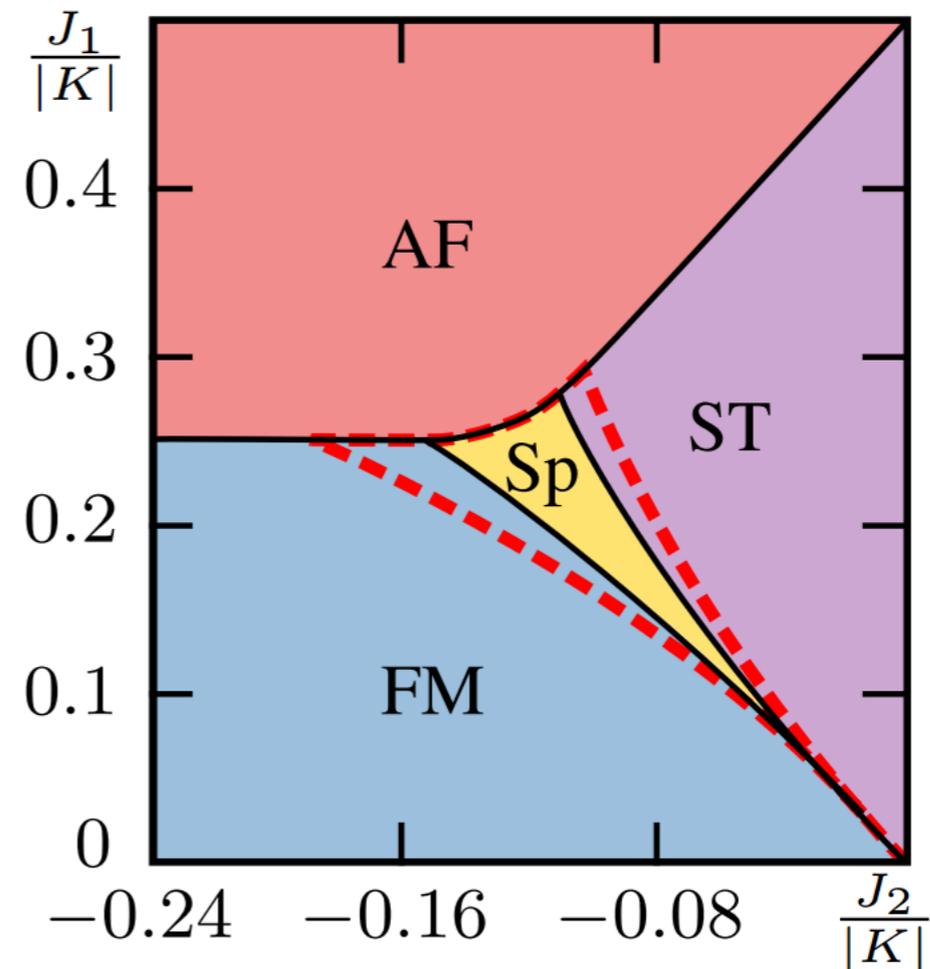
EKH LEE, J RAU, YB KIM  
arXiv:150606746 (2015)

# Decoupled Chain Limit - Classical



**JKG TORONTO**

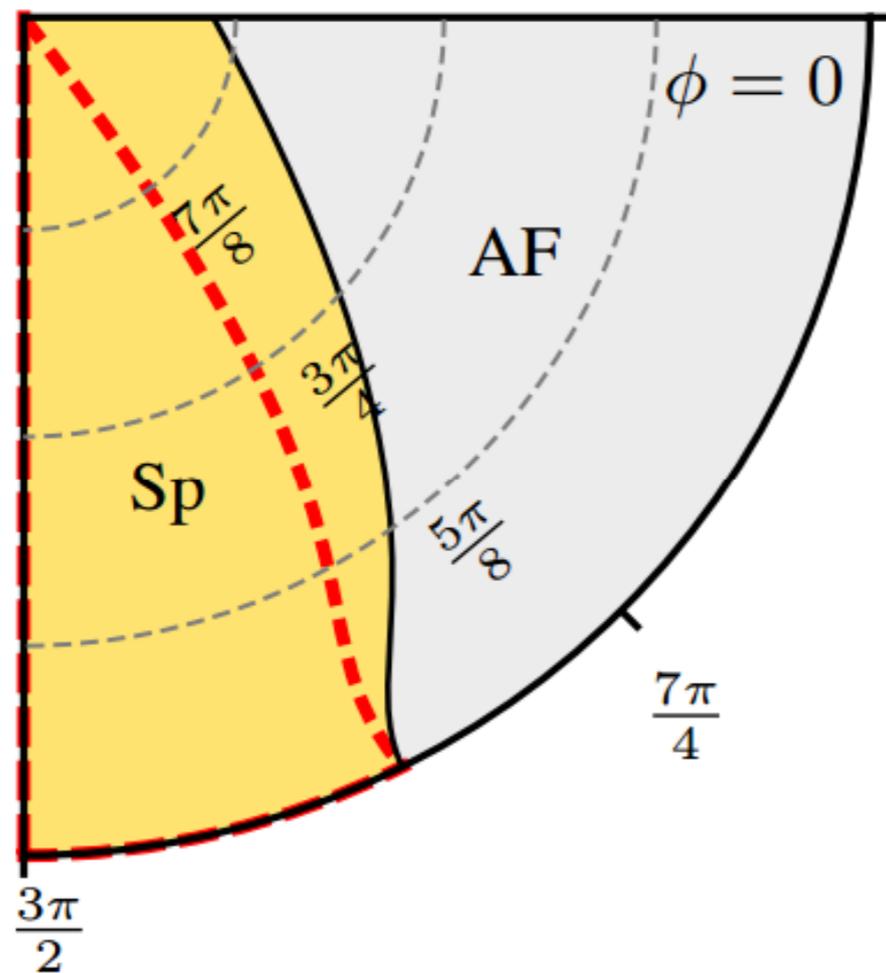
EKH LEE, J RAU, YB KIM  
arXiv:150606746 (2015)



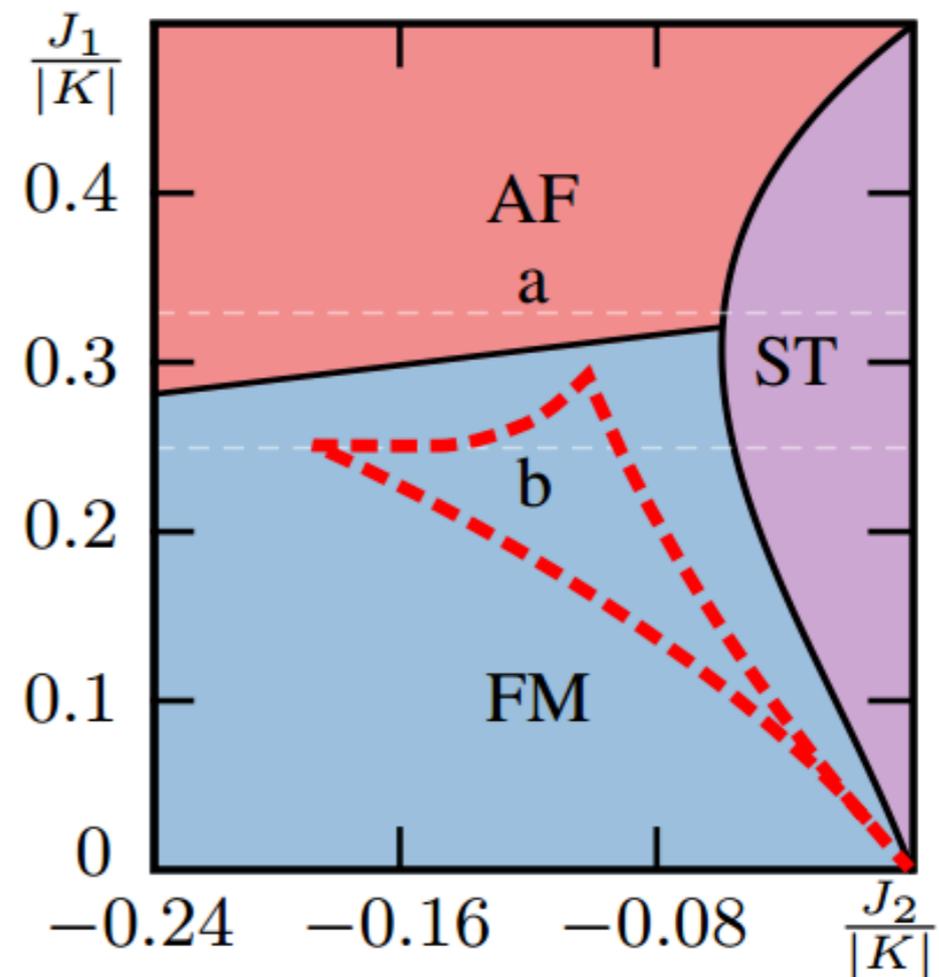
**CZC+J2 BERKELEY**

I KIMCHI, R COLDEA, A VISHWANATH  
PRB 91, 245134 (2015)

# Decoupled Chain Limit - DMRG



JKG TORONTO



CZC+J2 BERKELEY

EKH LEE, J RAU, YB KIM  
arXiv:150606746 (2015)

# Decoupled Chain Limit - DMRG

Intra-chain  $\Gamma$  interaction is important for the stabilization of incommensurate spiral order in the 1D quantum model

Inter-chain  $\Gamma$  interaction may be important for CZC (coupled zig-zag chain) model in 3D ?  
will need 3D quantum model

# Why do we care (no spin liquid) ?

This is a benchmark for Kitaev interaction

Engineering Kitaev limit (relative strength of Ir-Ir and Ir-O-Ir exchanges)

The Kitaev interaction may be dominant in the 3D materials, irrespective of details  
Pressure exp (Takagi); gapless spin liquid ?

Finite temperature signatures

Need understanding of Quantum Model