
Measurement of (n,xn) reactions

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OUTLINE

Introduction

1. Applications
2. Facilities
3. Cross-section measurements
 1. Activation technique
 2. $n, xn\gamma$ gamma
 3. Direct measurement of secondary neutrons
4. Double differential measurements
5. Examples of experiments

n,xn reactions



□ Production of an isotope

- Same element (no chemical separation)
- Can decay on other element (β decay....)

□ Threshold

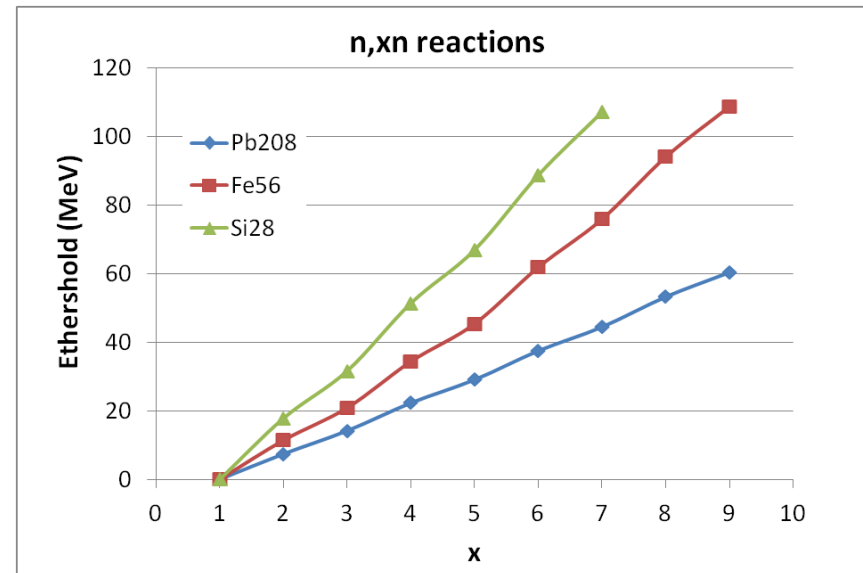
- n,n' the energy of the first excited level
- n,xn depends on the Q-value

$$Q = {}^{A-x+1}_Z M + x M_n - ({}^A_Z M + M_n)$$

$$Q = \Delta(A-1, Z) + (x-1)\Delta n - \Delta(A, Z)$$

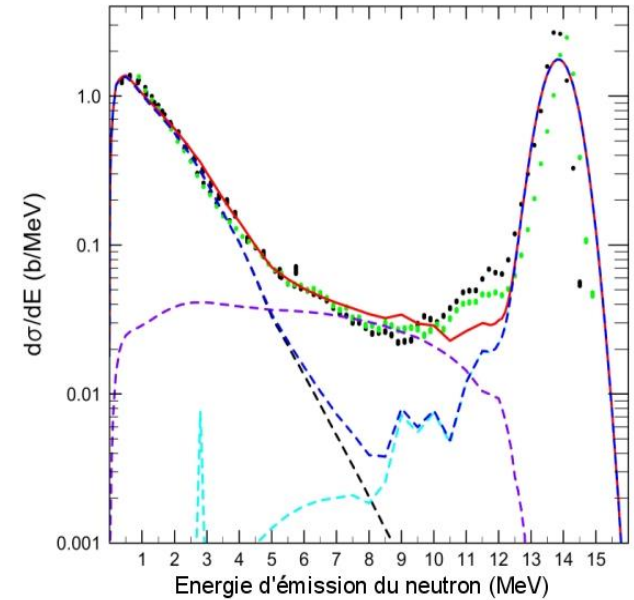
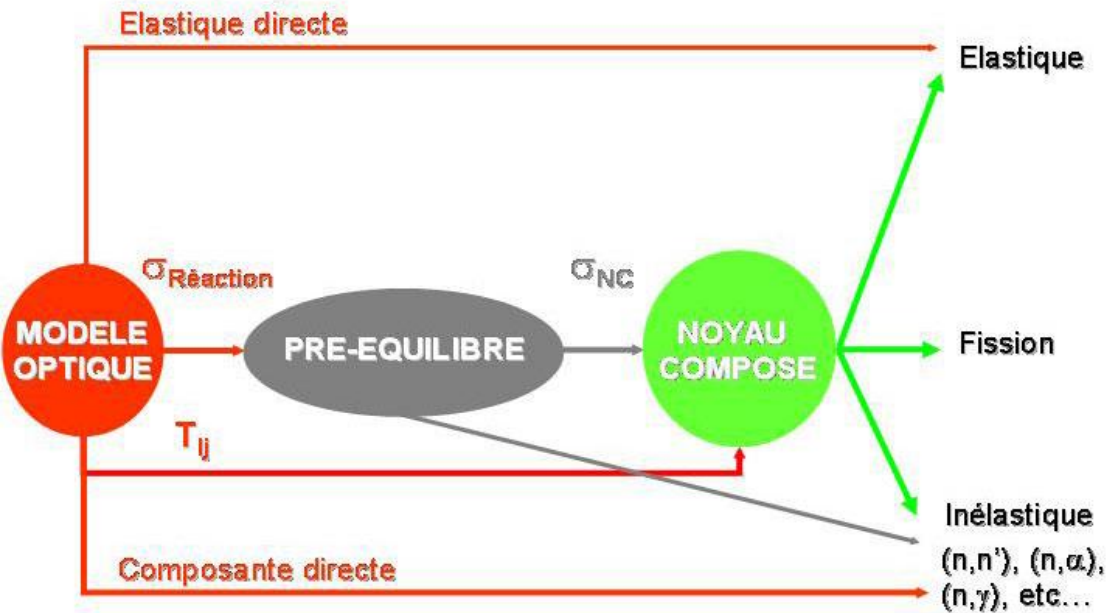
$$E_{th} = -Q \frac{M_n + M_x}{M_x} \cong -Q \frac{A+1}{A}$$

$\Delta(A, Z)$ The mass excess of nuclei A,Z



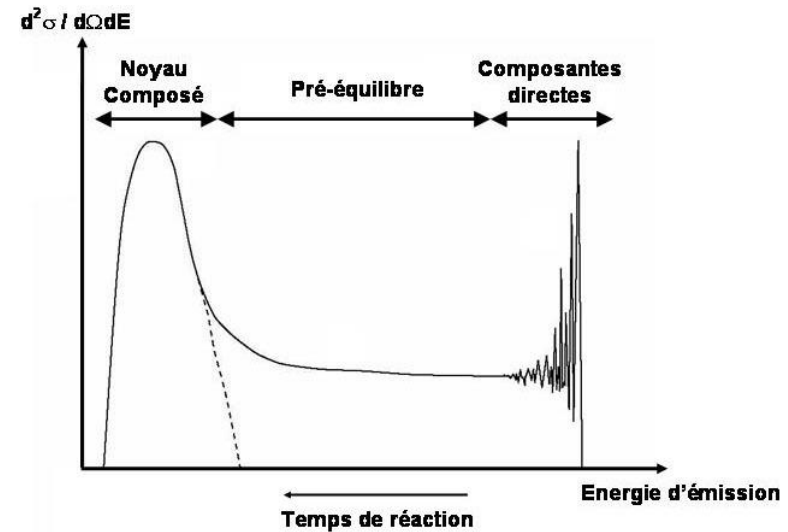
	Ethres	Q
${}^{208}\text{Pb}(n,2n){}^{207}\text{Pb}$	7,403	-7,367
${}^{208}\text{Pb}(n,3n){}^{206}\text{Pb}$	14,174	-14,105
${}^{208}\text{Pb}(n,4n){}^{208}\text{Pb}$	22,299	-22,192

Reaction process



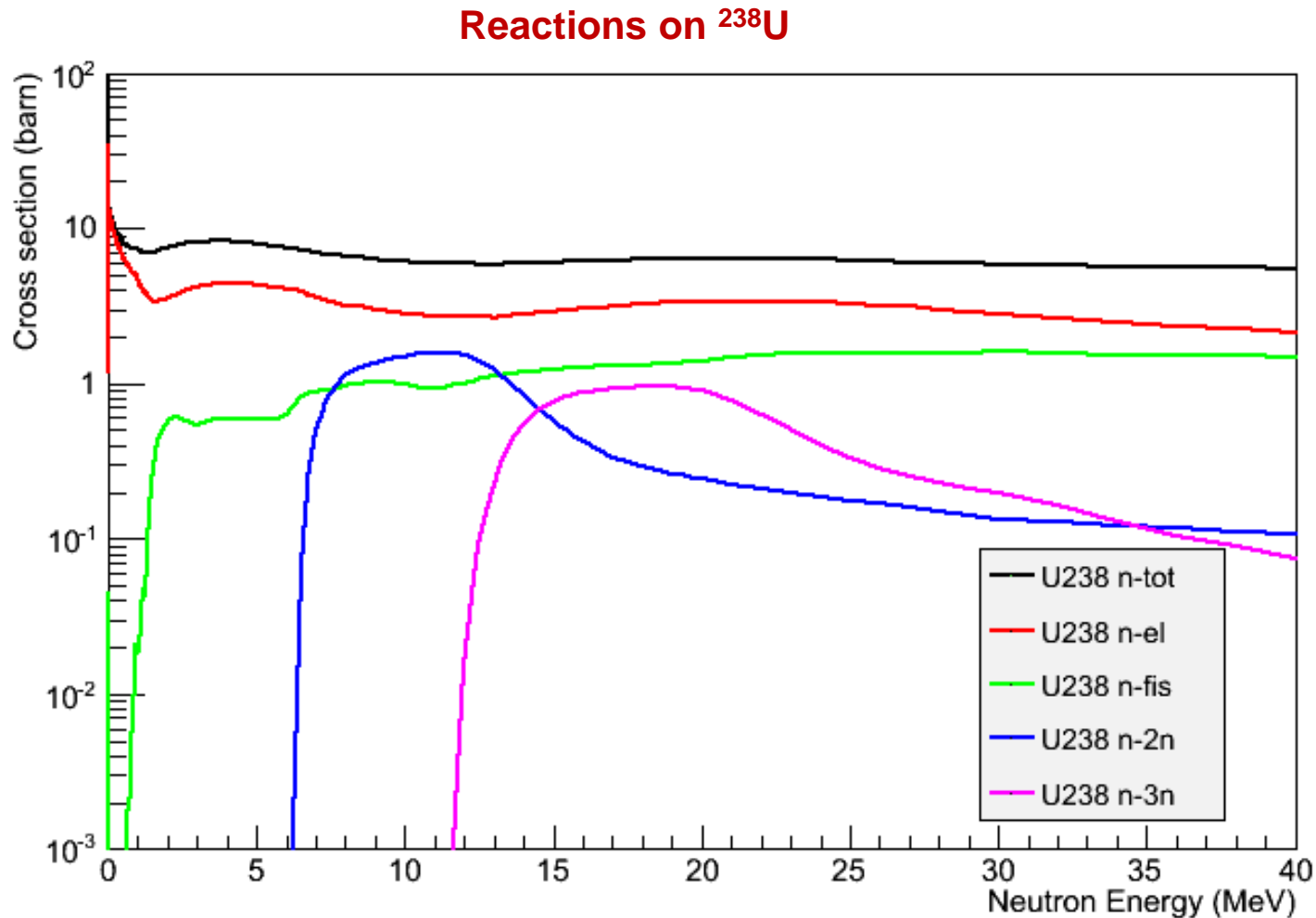
Neutrons are emitted during:

- Direct component : elastic component
- The evaporation of compound nuclei
- During the pre-equilibrium intermediate energy



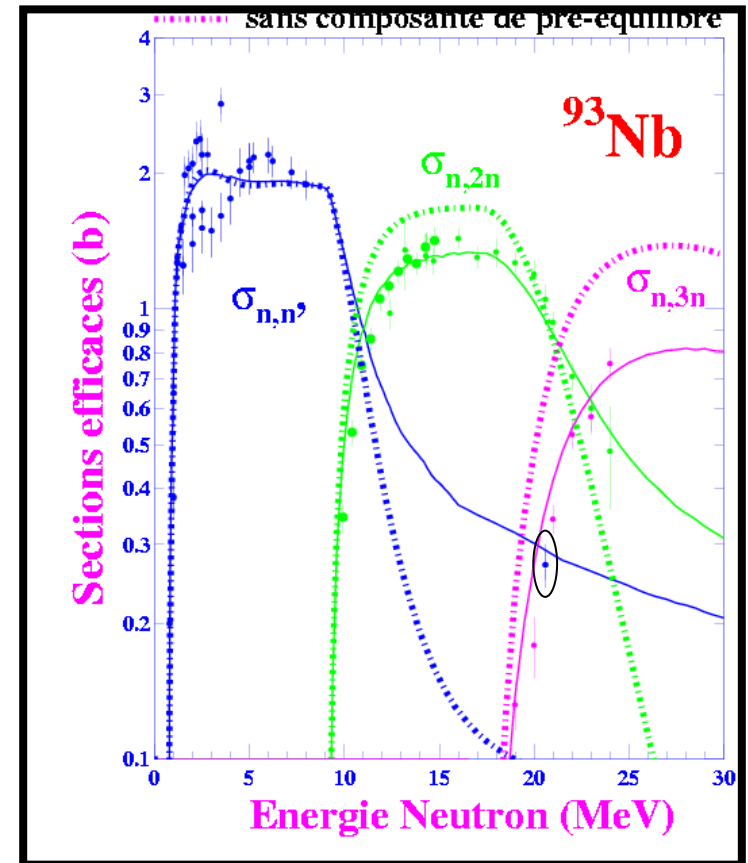
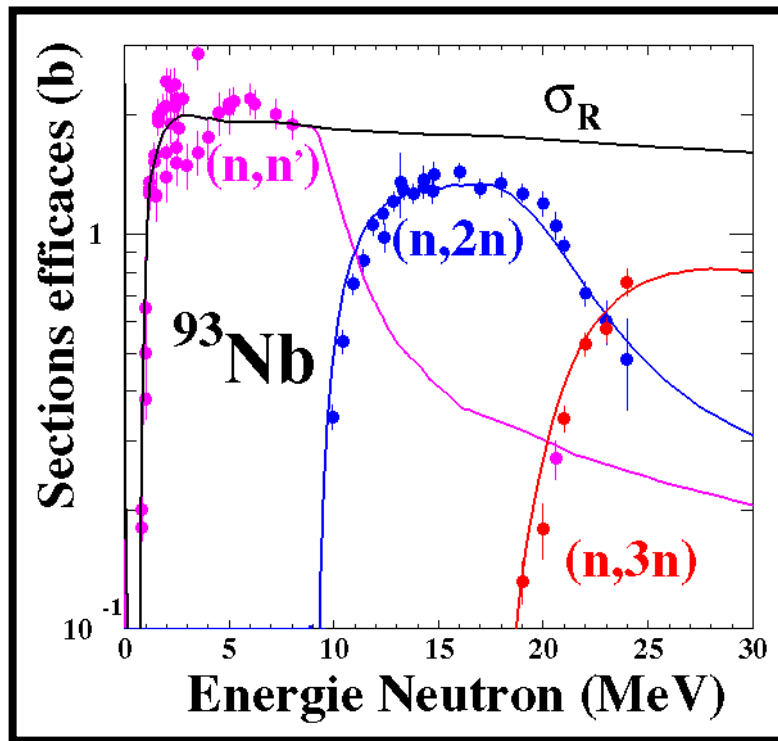
Importance of (n,xn) reactions

(n,xn) reactions represent the main part of the reaction cross-section above MeV



Role of the pre-equilibrium process in (n,xn) reaction

The pre-equilibrium process is an important process of the n,xn reactions



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Applications

- ❑ **Reactor and accelerator driven systems:** n, xn contributes to
 - Energy loss mechanism
 - Neutron multiplication
 - Production of radioactive isotopes
- ❑ **Production of nuclear waste** (fusion technology)
- ❑ **Nuclear data evaluation** (all the channels have to be studied)
- ❑ **Neutron field characterization**
 - Fluence
 - Energy and angular distribution

Reliable evaluated data bases are request → accurate measurements

Neutron field characterization

Threshold reactions including (n,n') and (n,xn) reactions are used for determining the differential flux from neutron sources by activation techniques.

❑ Irradiation of a set of material i in a flux Φ :

❑ Measurement of the activity of each sample i :
$$A_i^{mes} = k \int_{E_s}^{E_m} \frac{d\Phi}{dE}(E_n) \sigma_i(E_n) dE_n$$

❑ Use a simulated neutron spectrum: $\psi(E)$ to calculate A_i^{sim}
$$A_i^{sim} = k \int_{E_s}^{E_m} \frac{d\Psi}{dE}(E_n) \sigma_i(E_n) dE_n$$

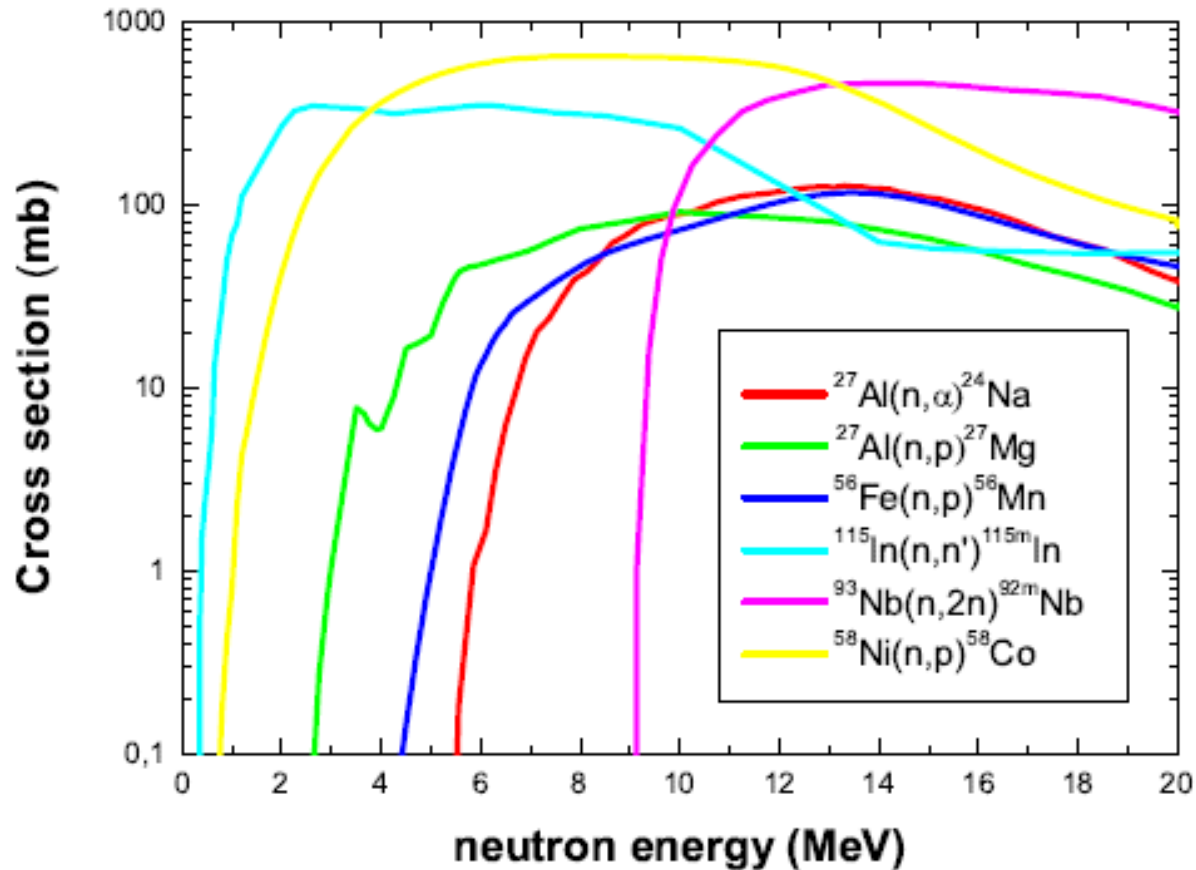
❑ Adjust $\psi(E)$ in order to minimize
$$\chi^2 = \frac{1}{m} \sum_i \frac{(A_i^{mes} - A_i^{sim})^2}{\varepsilon_i^2}$$

The choice of the reactions depends on:

- Energy threshold in order to cover the energy range of interest
- Product of reaction measurable (radioactive, period, decay mode)
- Reaction (n,p), (n, α), (n,n'), (n,xn)

Accurate knowledge of the cross-section reactions is required

Usable Reactions up to 20 MeV



N. Jovančević* et al., Physics Procedia 59 (2014) 154 – 159
Göran Lövestam et al., Radiation Measurements 44 (2009) 72–79

Above 20 MeV

Experimental determination of neutron spectra produced by bombarding thick targets:
(100 MeV/u) D + ^9Be , ^{238}U and (95 MeV/u) ^{36}Ar + ^{12}C

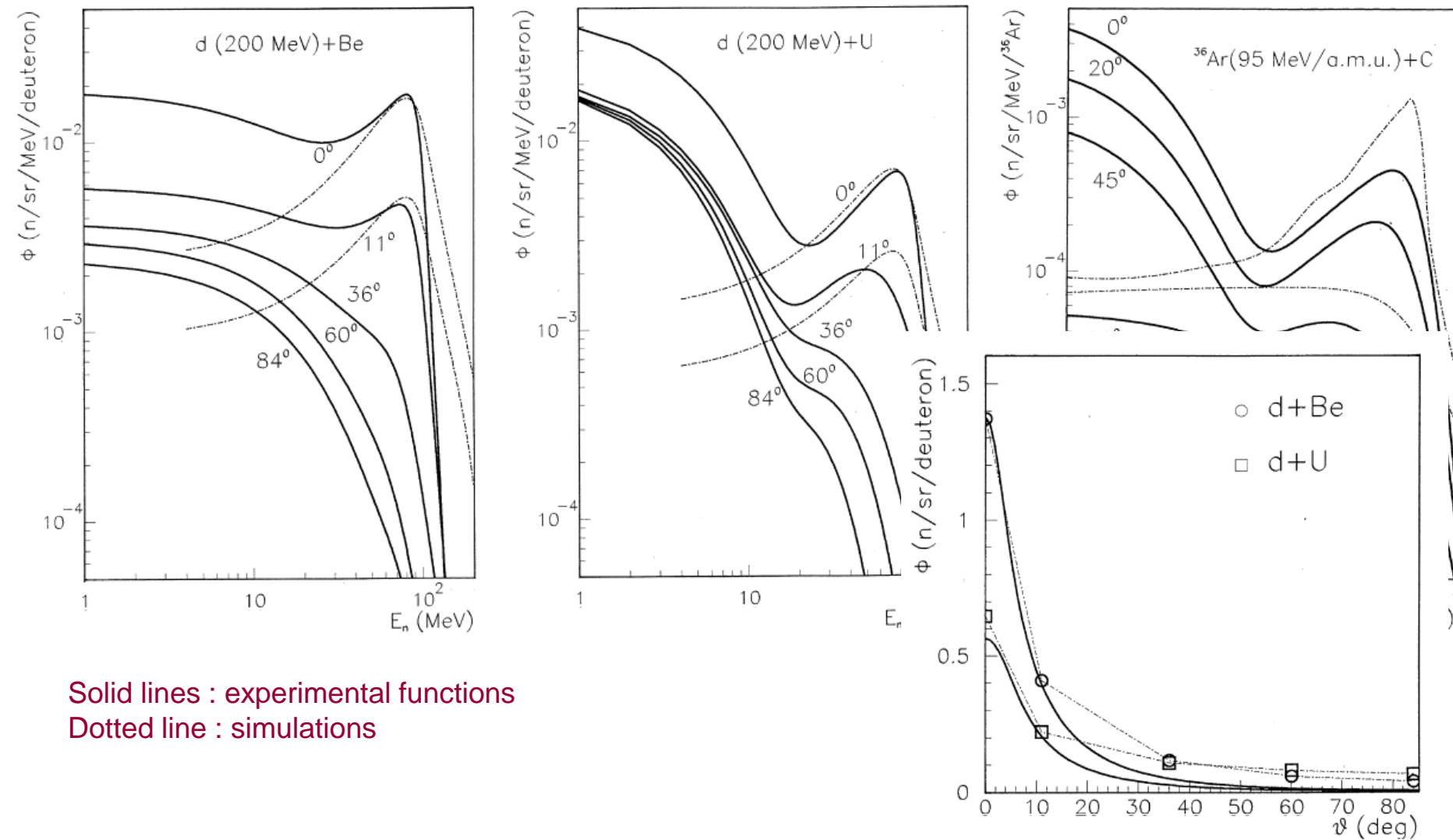
Experimental set-up

Incident beam	Energy (MeV/u)	Intensity (p.p.s)	Target	Irradiation time (min)	Activation detectors	Detector position
^{36}Ar	95	6.42×10^{11}	Carbon	88	Al, Ni, Bi	0°, 20°, 45°, 90°
Deuterons	100	6.72×10^{10}	Beryllium	373	Al, Ni, Co, Bi	0°, 11°, 36°, 60°, 84°
Deuterons	100	6.47×10^{10}	Uranium	376	Al, Ni, Co, Bi	0°, 11°, 36°, 60°, 84°

Reaction and isotopes characteristics

Detector	Reaction	Radionuclide	Half-life	Threshold energy (MeV)	γ -ray (keV)
Al	(n, α)	^{24}Na	15 h	6	1368.6
Al	(n, spall)	^{22}Na	2.6 yr	30	1274.5
Ni	(n, p)	^{58}Co	70.78 d	1	810.75
Co	(n, 2n)	^{58}Co	70.78 d	11	810.75
Co	(n, 3n)	^{57}Co	270 d	20	122.07
Co	(n, p)	^{59}Fe	45.1 d	4	1099.22
Bi	(n, 3n)	^{207}Bi	31.55 yr	14.42	1063.6
Bi	(n, 4n)	^{206}Bi	6.24 d	22.55	803
Bi	(n, 5n)	^{205}Bi	15.31 d	29.62	703.3
Bi	(n, 6n)	^{204}Bi	11.3 h	38.13	984
Bi	(n, 7n)	^{203}Bi	11.8 h	45.37	820.2
Bi	(n, 8n)	^{202}Bi	1.8 h	54.24	960.7
Bi	(n, 9n)	^{201}Bi	1.85 h	61.69	629.1
Bi	(n, 10n)	^{200}Bi	36 min	70.89	1026.5

Neutron spectra produced by bombarding thick targets:
 (100 MeV/u) D + ^9Be , ^{238}U and (95 MeV/u) ^{36}Ar + ^{12}C



Solid lines : experimental functions
 Dotted line : simulations

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5. Double differential measurements
6. Particular cases

Facilities

□ Neutron production

- Nuclear reaction → accelerator
- Photofission → e^- accelerator + converter
- Nuclear fission → Reactor

□ Parameters

- Energy range 5-50 MeV for (n,xn) reactions
- Energy distribution mono-kinetic or white spectrum
- Fluence
- Time structure pulsed beam for tof measurement

□ Types of facilities

- Open field
- Collimated beam

Reactor

- Neutron fission
- High flux
- No time spectrum
- Energy limited to 10 MeV
- Energy spectrum (fast neutrons for n,xn)

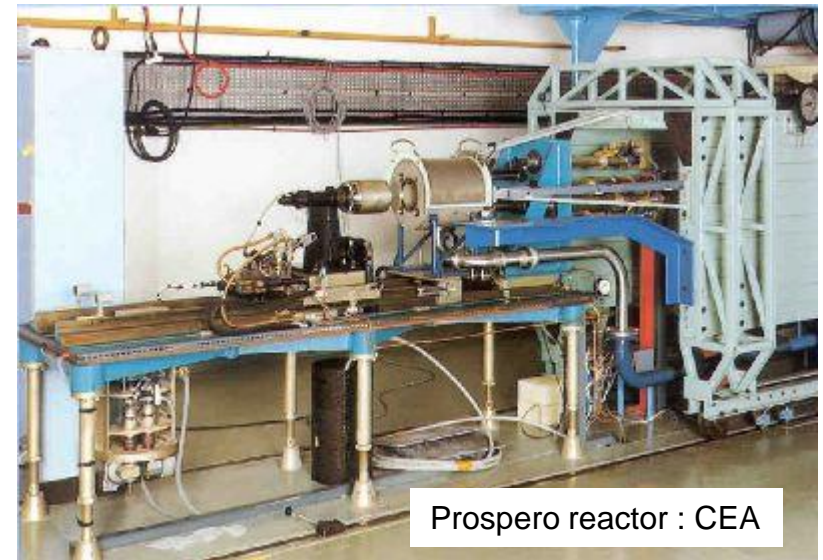
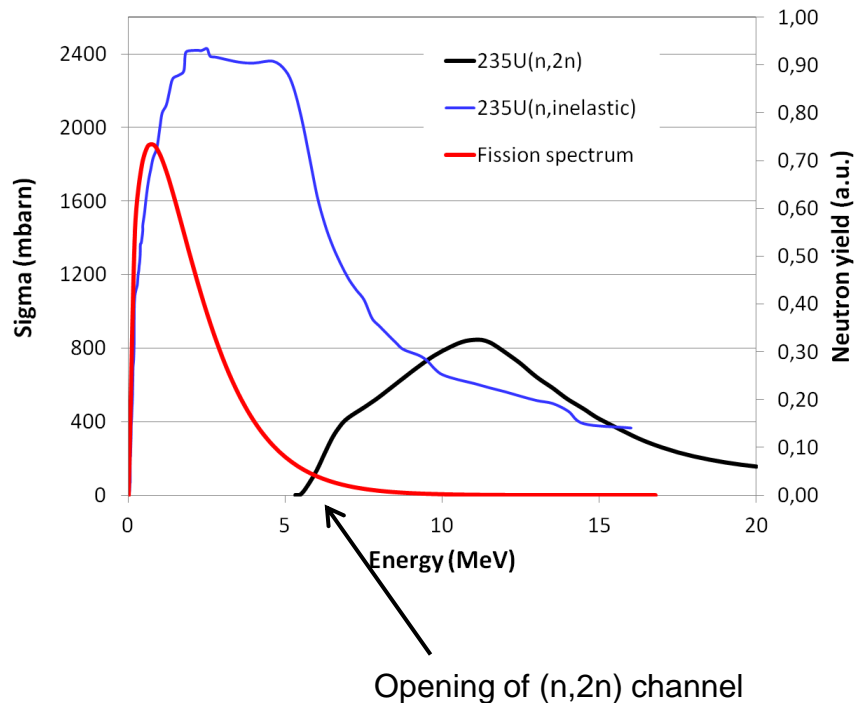
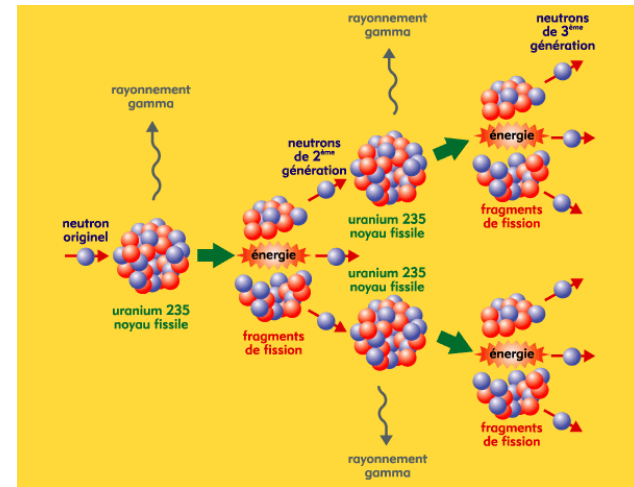
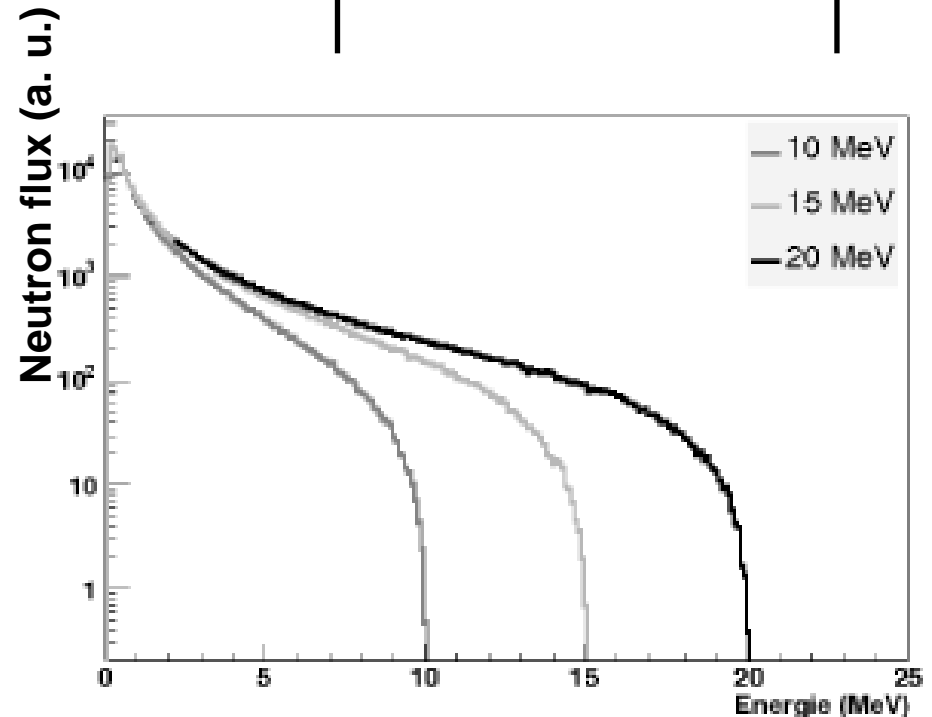
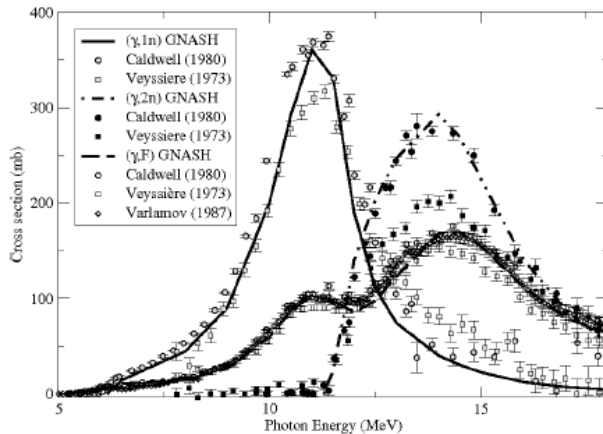
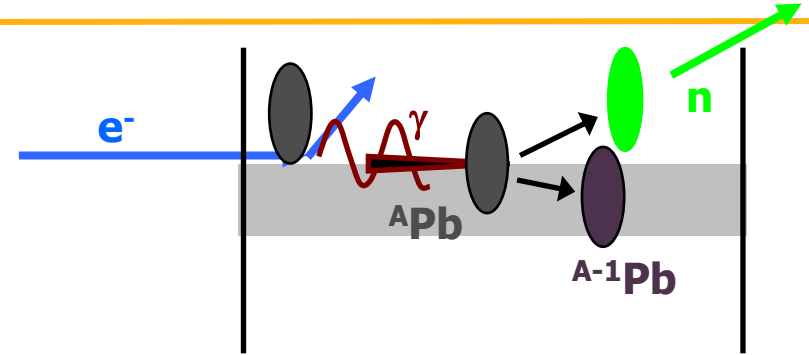


Photo-production of neutrons with bremsstrahlung

- **Electron beam**
- Photon production by Bremsstrahlung
- Neutron production by (γ, xn) or (γ, f) reaction



- **Continuous neutron energy spectrum**
- “Low cost” accelerator
- High power Accelerator

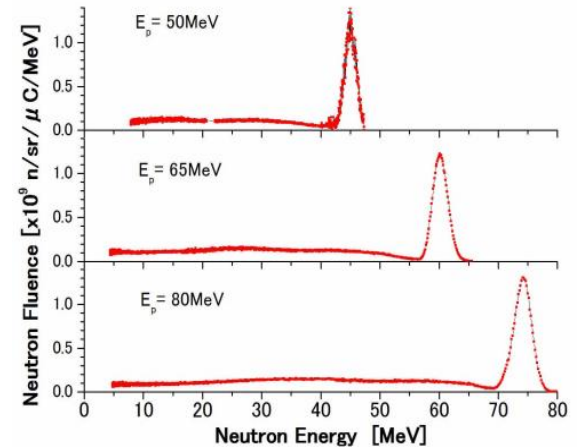
nELBE yield: $3 \cdot 10^{11}$ n/s with 30 MeV 15 μA (Target: Pb, liquid) 200 kHz

GELINA yield: $3 \cdot 10^{13}$ n/s with 100 MeV 96 μA (Target: U(Hg cooled)) 800 Hz

Intermediate energy 20-200MeV

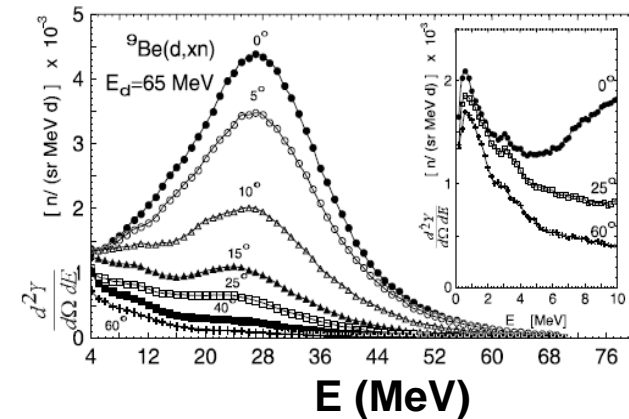
□ Quasi-mono-energetic spectrum:

- Proton beam on thin ${}^7\text{Li}$ converter
- ${}^7\text{Li}(p,n){}^7\text{Be}$ reaction $Q = -1,64 \text{ MeV} \rightarrow$ at 0° $E_n \approx E_p - 2 \text{ MeV}$
- Forward peak
- Limitations :
 - Spectrum not purely mono-energetic \rightarrow pulsed beam
 - Low melting point of Lithium (limited intensity) \rightarrow liquid target
 - Target highly activated (${}^7\text{Be}$)



□ Continuous spectrum:

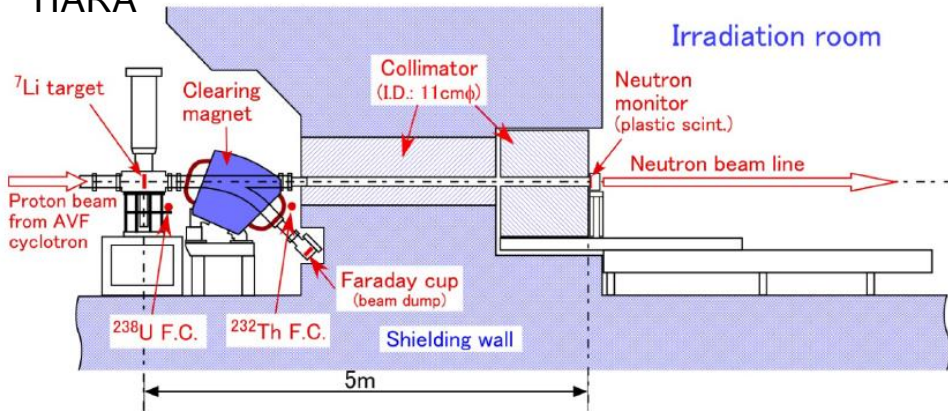
- Proton or deuteron beam on thick converter Be or C
- Continuous spectrum up to beam energy
- Flux increasing with energy
 - The beam stops in the converter
 - Large power deposition \rightarrow cooling is challenging



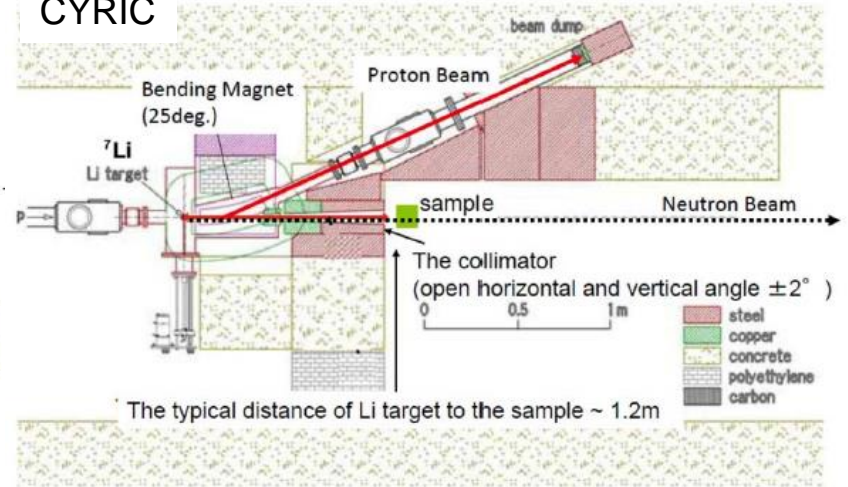
Several facilities proposes both types of spectra

Some Quasi-Monoenergetic facilities

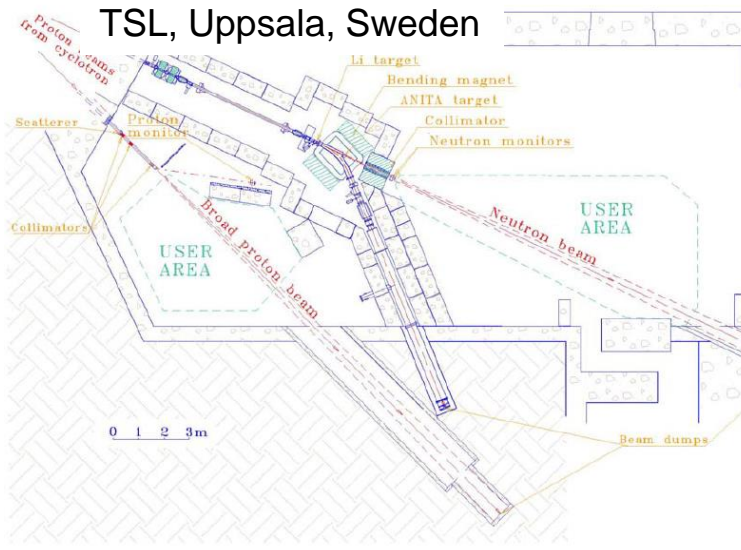
TIARA



CYRIC



TSL, Uppsala, Sweden



EURADOS
European Radiation Dosimetry Group e.V.

EURADOS Report 2013-02
Braunschweig, May 2013

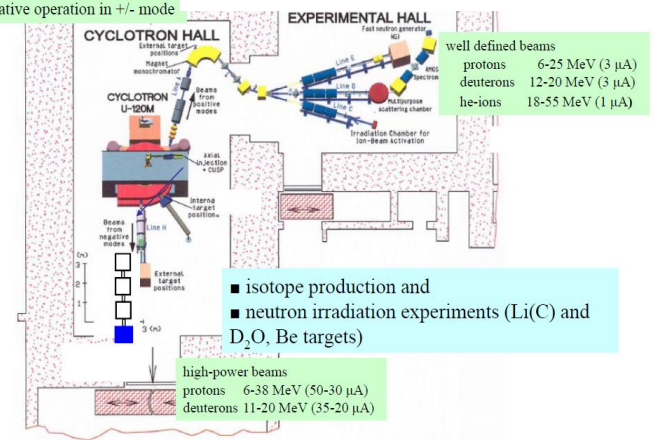
High-energy quasi-monoenergetic neutron fields: existing facilities and future needs

Pomp S., Bartlett D.T., Mayer S., Reitz G., Röttger S., Silari, M., Smit F.D., Vincke H., and Yasuda H.

ISSN 2226-8057
ISBN 978-3-943701-04-3

-120 (1960) upgrade to isochronous regime (1975) to alternative operation in +/- mode

NPI, Rez, Czech Republic



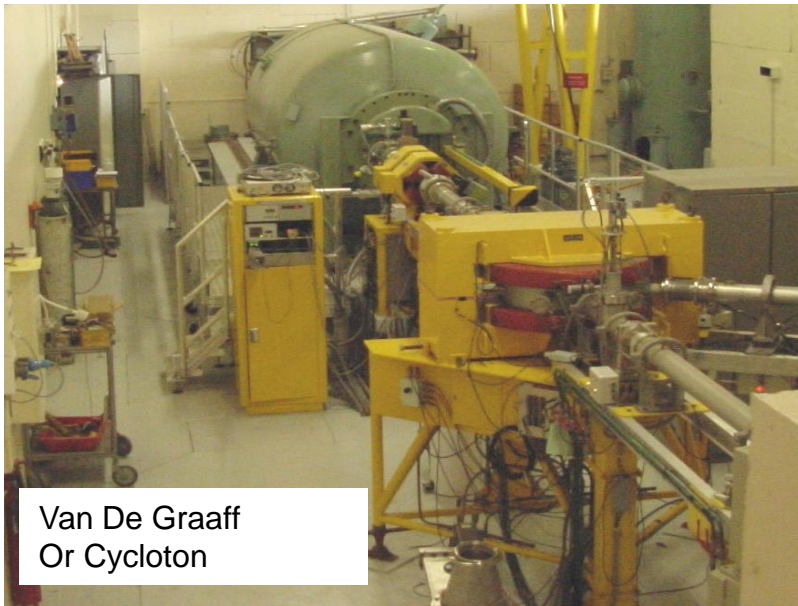
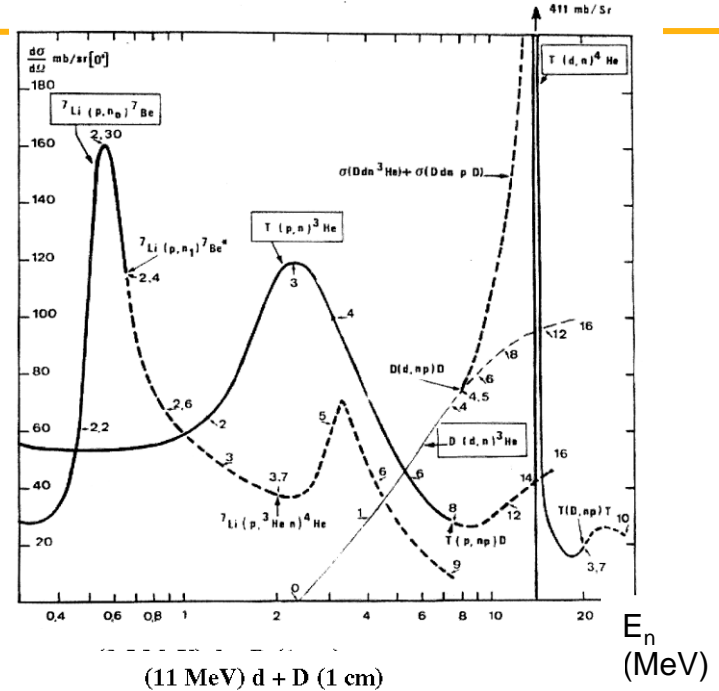
neutron flux up to $3 \cdot 10^8$ n/cm²/s

Mono-kinetic neutron sources

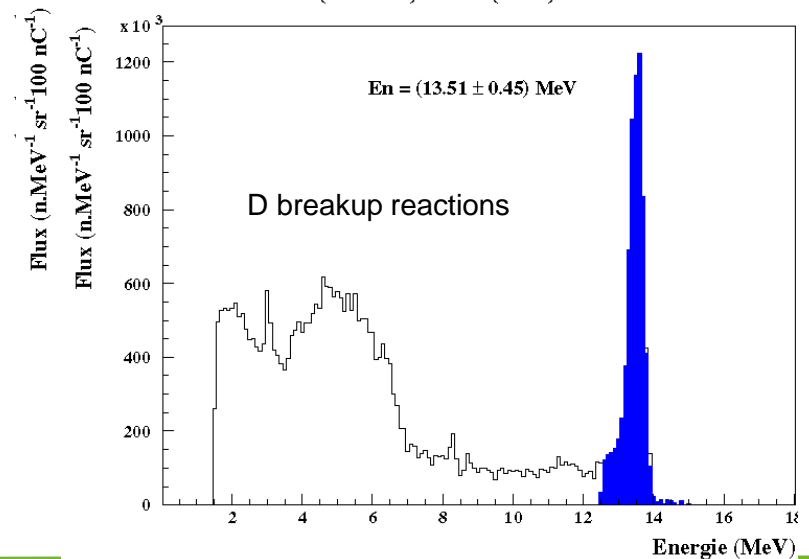
Nuclear reactions (The big four)



- Proton and deuteron beams with $E < 4$ MeV
- **Purely mono-energetic** neutrons for $E < 7$ MeV and $14 < E < 17$ MeV



Van De Graaff
Or Cyclotron



Spallation reaction

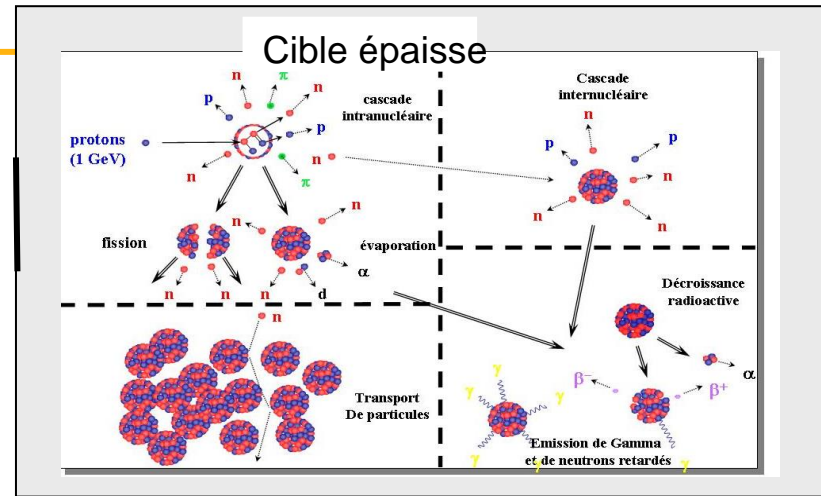
Proton beam with energy $> 800\text{MeV}$

Very intense neutrons source

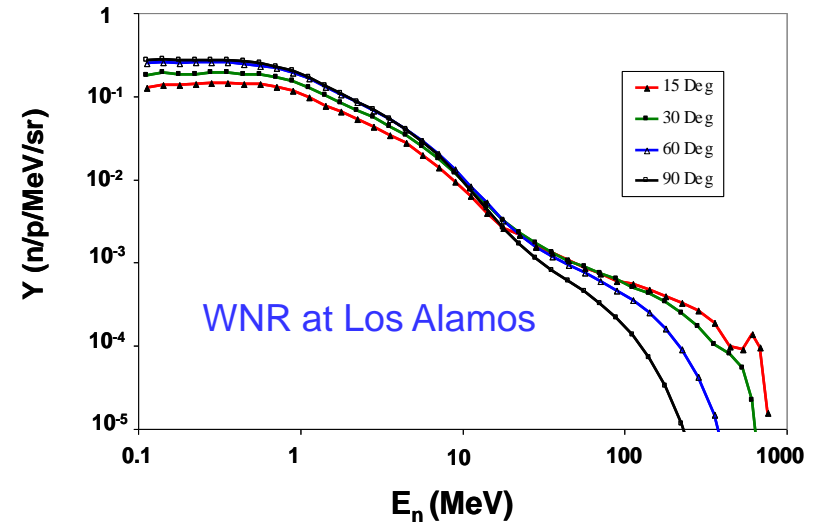
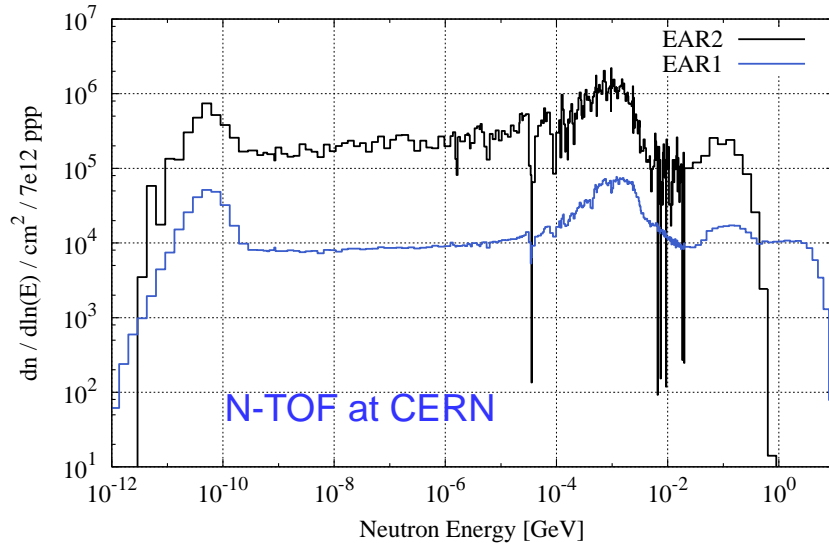
Proton accelerator $1\text{ GeV} \times 1\text{ mA} = 1\text{ MW}$

$\Rightarrow 10^{17}\text{ n/s}$

- Neutron production up to the proton energy
- Use of moderator to increase neutrons flux at low energy thermal or cold
- N-tof, WNR, SNS, ESS, JPARC



Comparison of the Neutron Fluence in EAR1 and EAR2



Type of beam

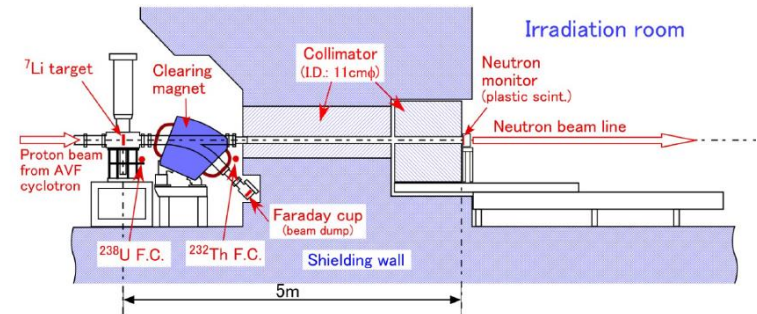
□ Open field

- Neutron emission in 4π
- Background in the experimental area
- The sample can be placed very close to the source
- VdG, PTB



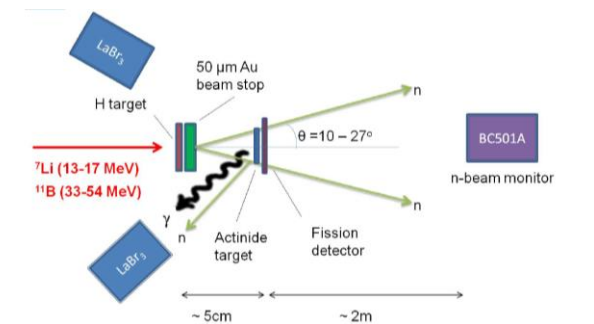
□ Collimated beam

- The detectors can be placed close to the sample
- Low flux because of the distance source-sample
- WNR, N-TOF, NFS



□ “Conical” beam

- Kinematic effect
- Neutrons are emitted in a cone in the forward direction
- LICORNE, FRANZ



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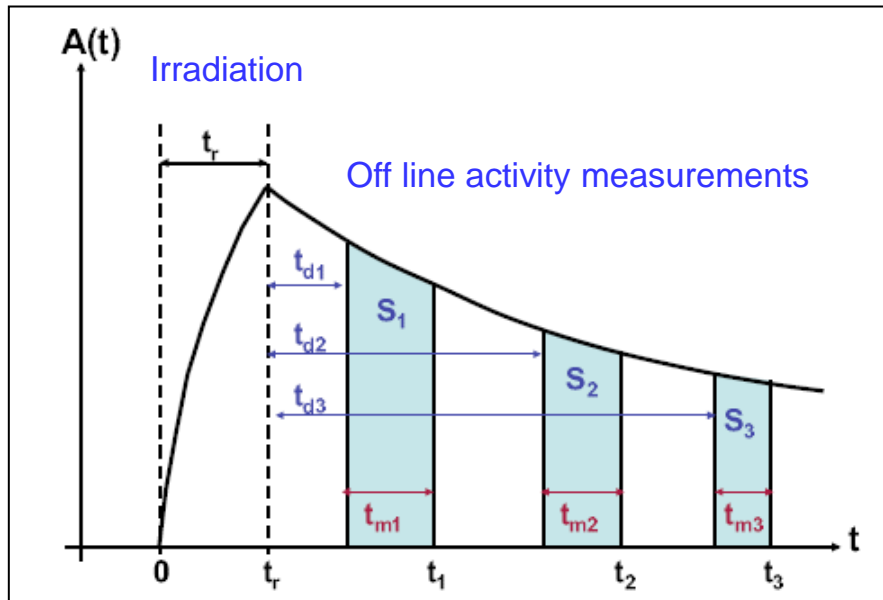
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Activation technique

Also called radiochemical technique

Activation and off-line gamma ray spectrometric technique



Only if ${}^{A-x+1}_Z X$ radioactive

→ Period

Decay mode (γ , α , e)

Feeding ratio

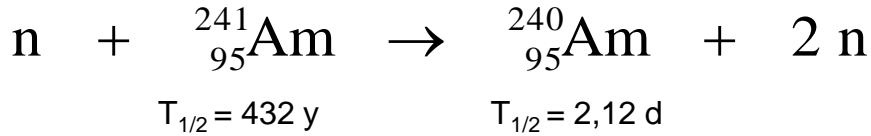
Advantages:

- Target do not need to be isotopic if $E_n < B_n (A+1)$
- No need of pulsed beam

Drawbacks :

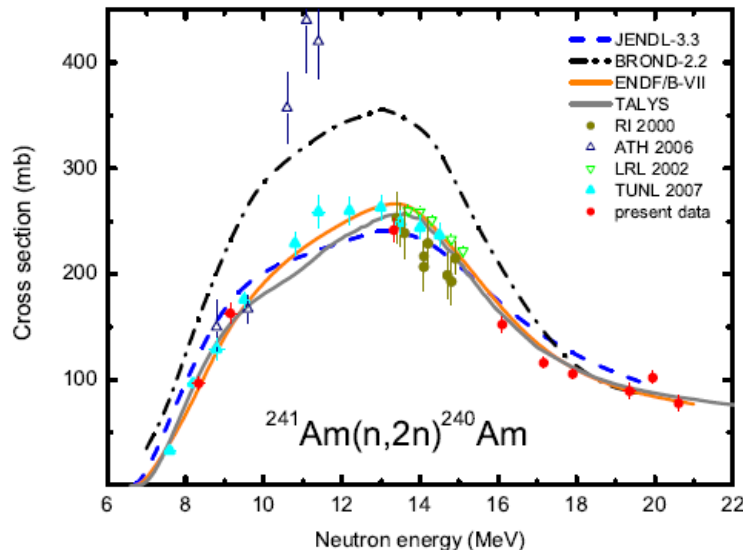
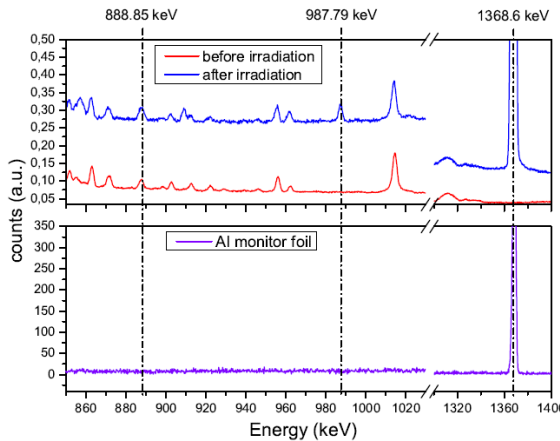
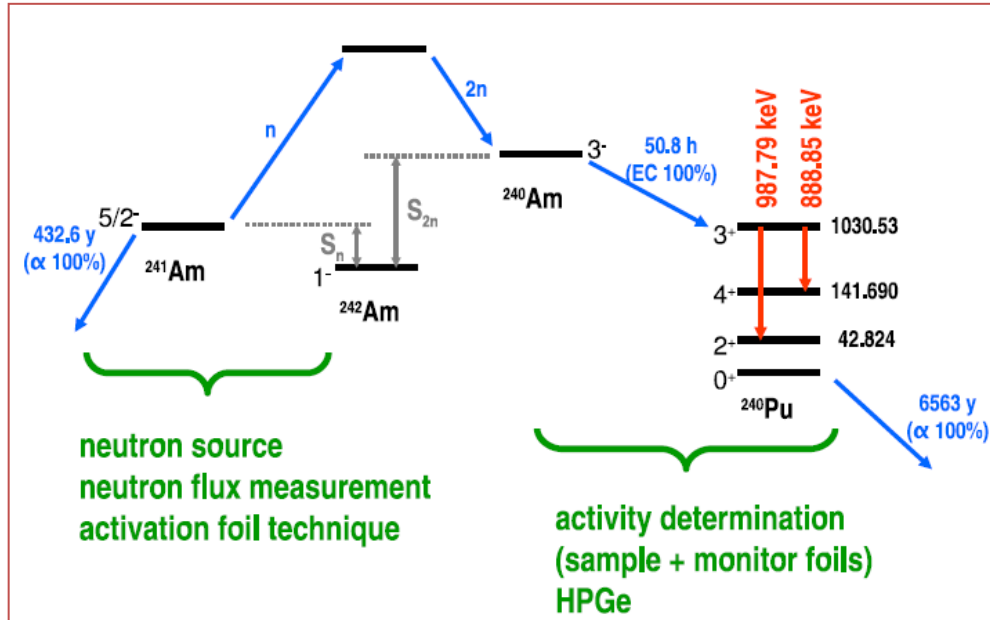
- Incident energy is not measured → need mono-energetic beam
- One measurement for each energy
- One target for each energy

Cross-section of the $^{241}\text{Am}(n,2n)$ reaction



IRMM Van de Graaff accelerator
Monitoring by activation of foils
Radioactive target

Targets
30-40 mg of ^{241}Am



C. Sage, PhD thesis

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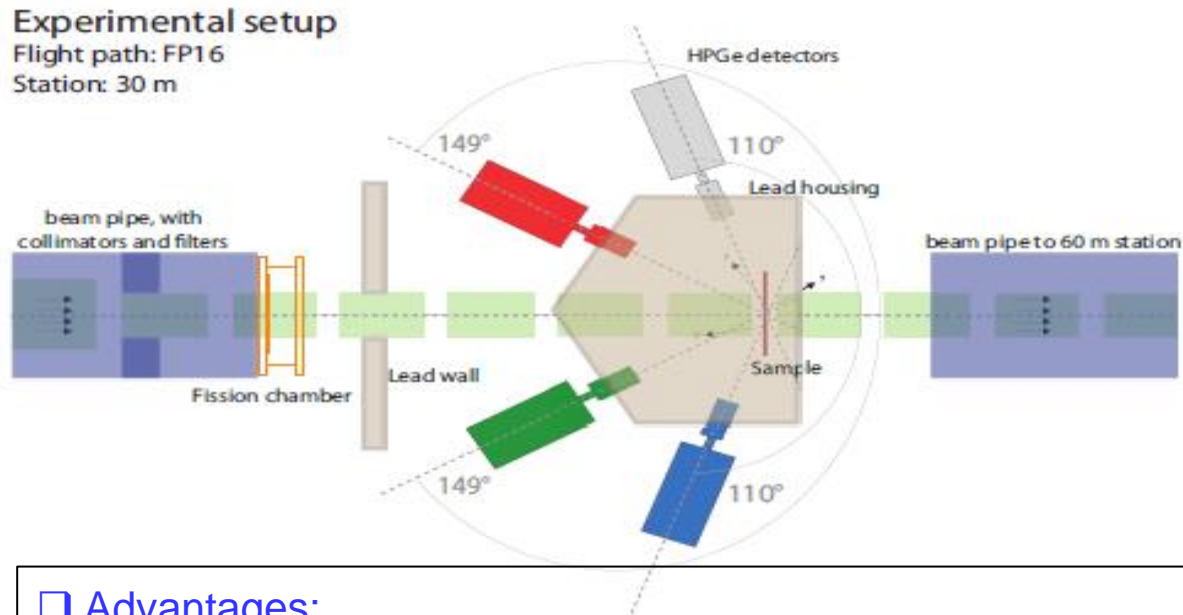
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Prompt γ -ray spectroscopy

Detection of the γ -rays stemming from the decay of excited states of nucleus created by the (n,xn) reaction.

Measure on line of prompt gamma spectroscopy of the ${}^{A-x+1}_{Z}X$



□ Advantages:

- The incident energy can be measured if the beam is pulsed
- On-line measurement of several energies during the same run
- **Several isotopes** can be measured simultaneously

□ Drawbacks :

- (n,xn γ) cross-section is measured
- **Calculations** are required to determine the (n,xn) cross-section

Inelastic scattering and (n,xn) experimental studies

4 HPGe Planar
(110°,150°)
Actinides
samples
 $\Delta E_n = 10 \text{ keV}$ @
 $E_n = 1 \text{ MeV}$

GRAPhEME @ FP16/30 m



Neutron Time of flight facility

GELINA@IRMM(Geel)

^{52}Cr : L.C. Mihailescu *et al.* **NPA786(2007)1**
 ^{209}Bi : L.C. Mihailescu *et al.* **NPA799(2008)1**
 ^{208}Pb : L.C. Mihailescu *et al.* **NPA811(2008)1**
 ^{23}Na : C. Rouki *et al.* **NIMA672(2012)82**
 ^{235}U : M. Kerveno *et al.* **PRC87(2013)024609**
 $0\nu 2\beta$: A. Negret *et al.* **PRC88(2013)027601**
 ^{28}Si : A. Negret *et al.* **PRC88(2013)034604**
 ^{76}Ge : C. Rouki *et al.* **PRC88(2013)054613**
 ^{56}Fe : A. Negret *et al.* **PRC90(2014)034602**
 ^{24}Mg : A. Olacel *et al.* **PRC90(2014)034603**
 ^{232}Th : M. Kerveno *et al.* **EPJA(2014) accepted**
 ^7Li , ^{12}C , ^{58}Ni , $^{\text{nat}},^{184},^{186}\text{W}$, $^{206},^{207}\text{Pb}$, ^{232}Th , ^{238}U : conf.

Pulsed white neutron beam
10 meV - 20 MeV
Multi-users facility
10 m to 400 m



GAINS @ FP3/200 m

12 HPGe \varnothing 80 mm x L 80 mm
(110°,150°)
 $\Delta E_n = 1 \text{ keV}$ @ $E_n = 1 \text{ MeV}$

^{12}C , ^{23}Na , ^{24}Mg , ^{28}Si , ^{52}Cr , ^{56}Fe , ^{58}Ni , ^{76}Ge , $^{\text{nat}}\text{Zr}$,
 $^{\text{nat}},^{182},^{183},^{184},^{186}\text{W}$, $^{206},^{207},^{208}\text{Pb}$, ^{209}Bi , ^{232}Th , $^{235},^{238}\text{U}$

Measurement of $^{235}\text{U}(n,n'\gamma)$ and $^{235}\text{U}(n,2n\gamma)$ cross-section

M. Kerveno, WONDER 2012, Sept 25-28, 2012, Aix en Provence

☐ Beam time : 1466 hours

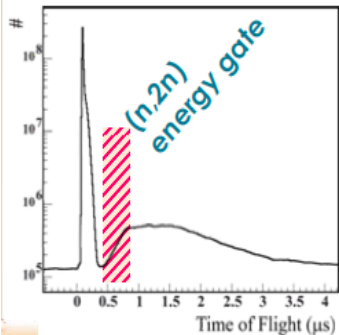
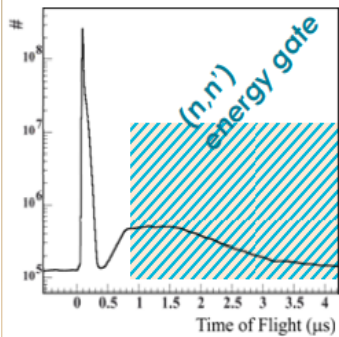
☐ Sample :

- enrichment ^{235}U 93,2%
- m= 37,43 g
- $\Phi= 12,00$ cm
- thickness 0,21 mm

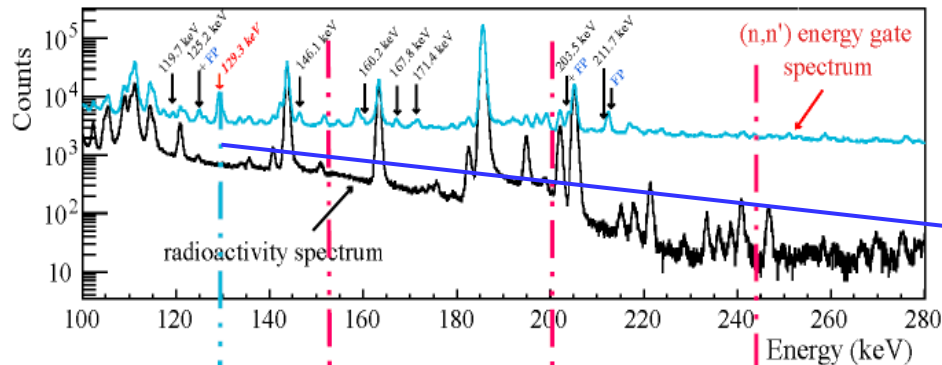
1 γ transition in ^{235}U \rightarrow $^{235}\text{U}(n,n'\gamma)$

3 γ transitions in ^{234}U \rightarrow $^{235}\text{U}(n,2n\gamma)$

TOF spectra

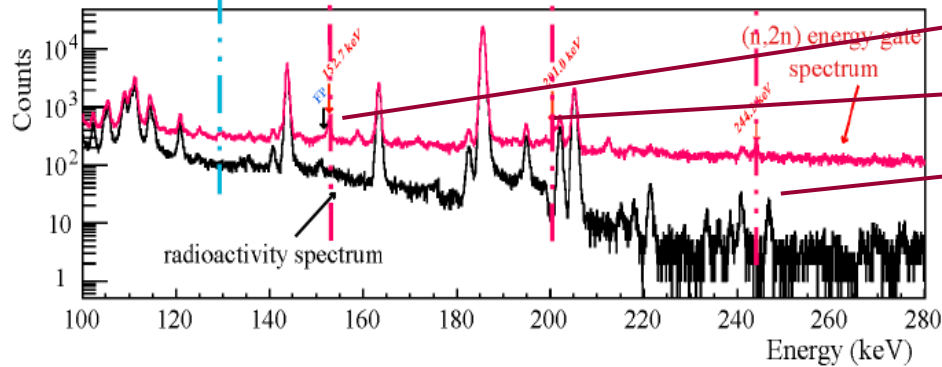


Gamma spectra



$^{235}\text{U}(n,n'\gamma)$

129,3 keV $5/2^- \rightarrow 7/2^-$



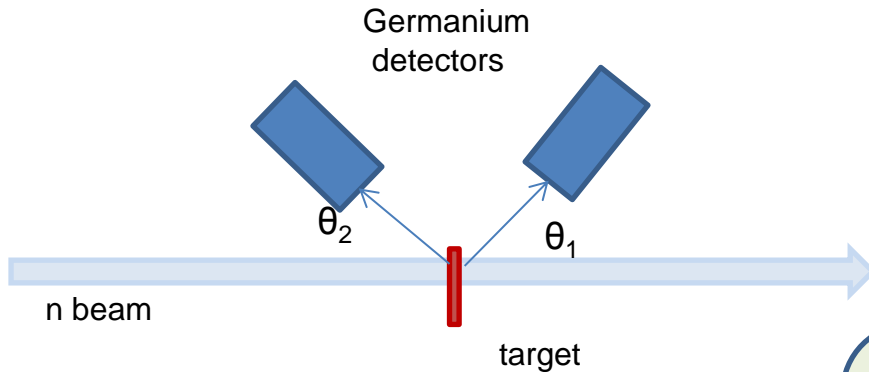
152,72 keV $6^+ \rightarrow 4^+$

200,96 keV $8^+ \rightarrow 6^+$

244,2 keV $10^+ \rightarrow 8^+$

$^{235}\text{U}(n,2n\gamma)$

Measurement of $\sigma(n,xn\gamma)$



$$\frac{d\sigma^{(n,xn\gamma)}}{d\Omega}(\theta) = \frac{n_{\text{det}}}{N_{\text{at}} \cdot \phi_n \cdot \varepsilon \cdot t}$$

n_{det} : number of detected γ
 N_{at} : number of atoms
 in the sample
 ϕ_n : neutron flux
 ε : HPGe efficiency
 t : measurement time

$$\sigma^{(n,xn\gamma)} = \int_{4\pi} \frac{d\sigma^{(n,xn\gamma)}}{d\Omega} d\Omega = 2\pi \int_{-1}^1 \frac{d\sigma^{(n,xn\gamma)}}{d\Omega} d(\cos(\theta))$$

Gaussian quadrature Approximation $\rightarrow \sigma^{(n,xn\gamma)} \approx 2\pi \sum_{i=1}^N w_i \frac{d\sigma^{(n,xn\gamma)}}{d\Omega}(\theta_i)$

With θ_i such that for $P_n(\cos \theta)=0$

Legendre polynomial of order N=4

$\sqrt{\frac{15+2\sqrt{30}}{35}} = 0.8611$	30.6°	$\frac{-\sqrt{30}+18}{36} = 0.3479$
$\sqrt{\frac{15-2\sqrt{30}}{35}} = 0.3400$	70.1°	$\frac{\sqrt{30}+18}{36} = 0.6521$
$-\sqrt{\frac{15-2\sqrt{30}}{35}} = -0.3400$	109.9°	$\frac{\sqrt{30}+18}{36} = 0.6521$
$-\sqrt{\frac{15+2\sqrt{30}}{35}} = -0.8611$	149.4°	$\frac{-\sqrt{30}+18}{36} = 0.3479$

$$P_N(-x) = (-1)^N P_N(x),$$

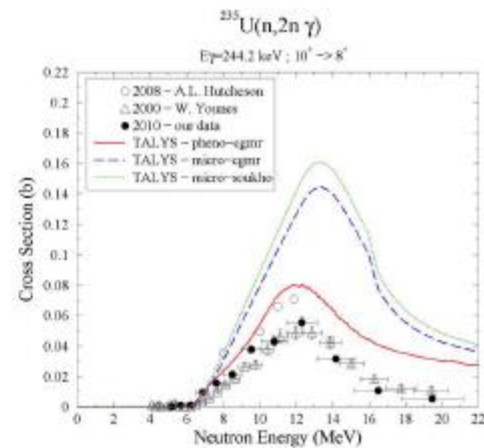
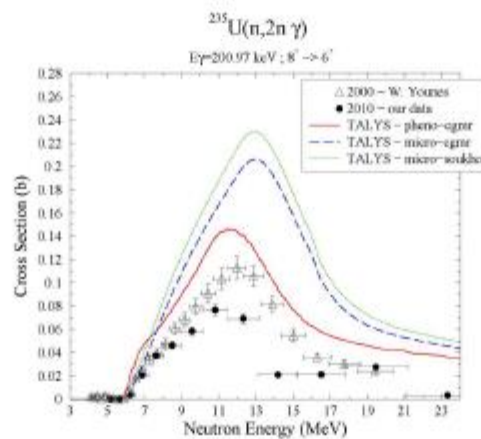
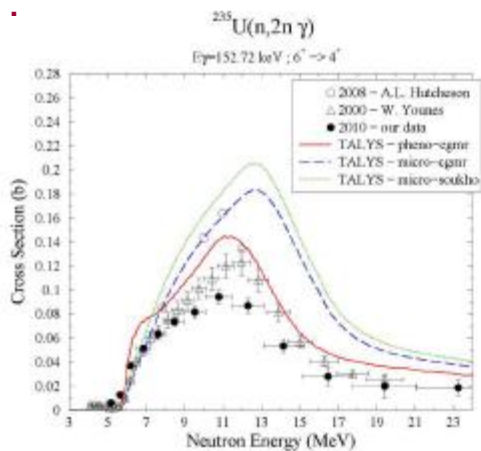
$\sigma(n,xn\gamma)$ can be deduced with 2 detectors

$$\sigma_{\text{tot}}^{(n,xn\gamma)} = 4\pi \left[w_1^* \frac{d\sigma}{d\Omega}(\theta_1^*) + w_2^* \frac{d\sigma}{d\Omega}(\theta_2^*) \right]$$

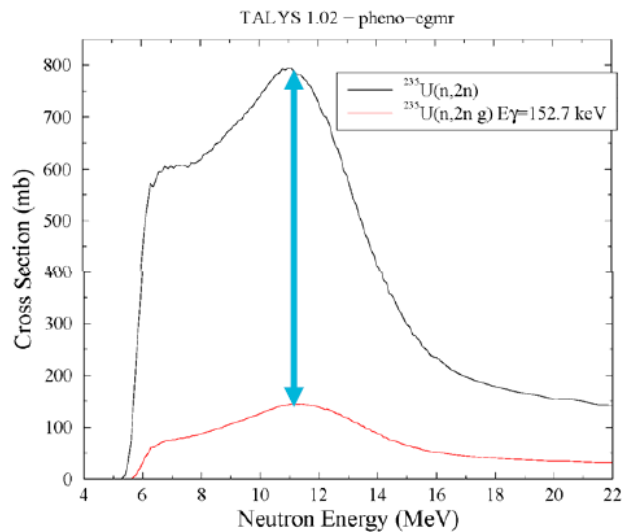
$w_1 = 0.3479$ for $\theta_1 = 30.56^\circ$ or 149.44° and
 $w_2 = 0.6571$ for $\theta_2 = 70.12^\circ$ or 109.88°

From (n,2n γ) to (n,2n) cross-section

Measurements :



Theoretical model :

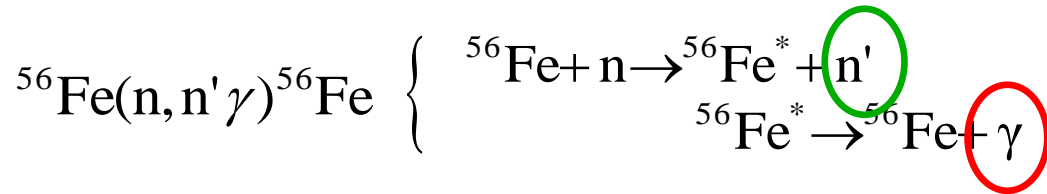


Only one part of the (n,2n) cross-section is measured



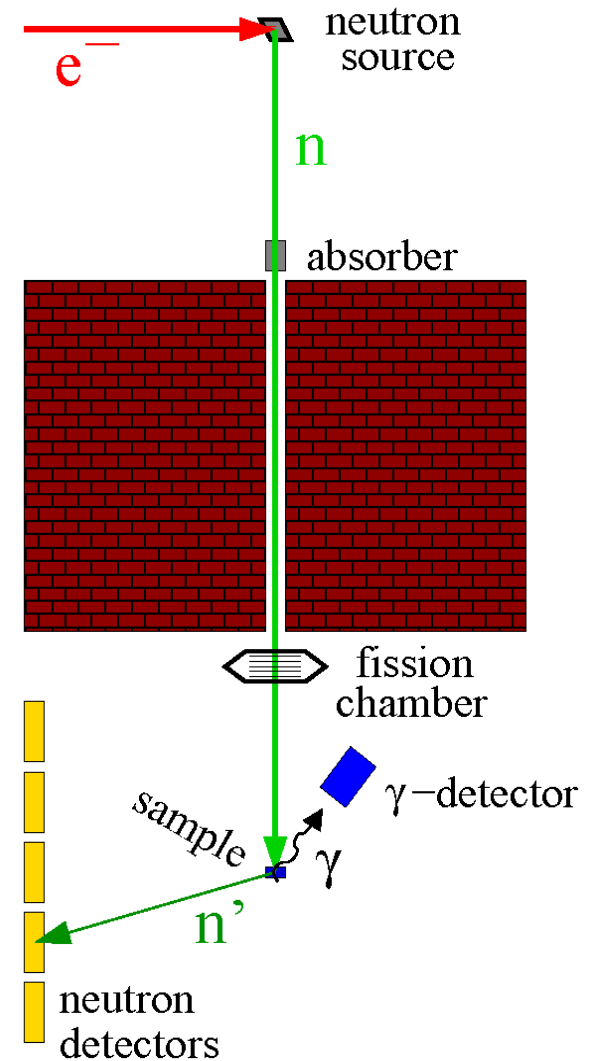
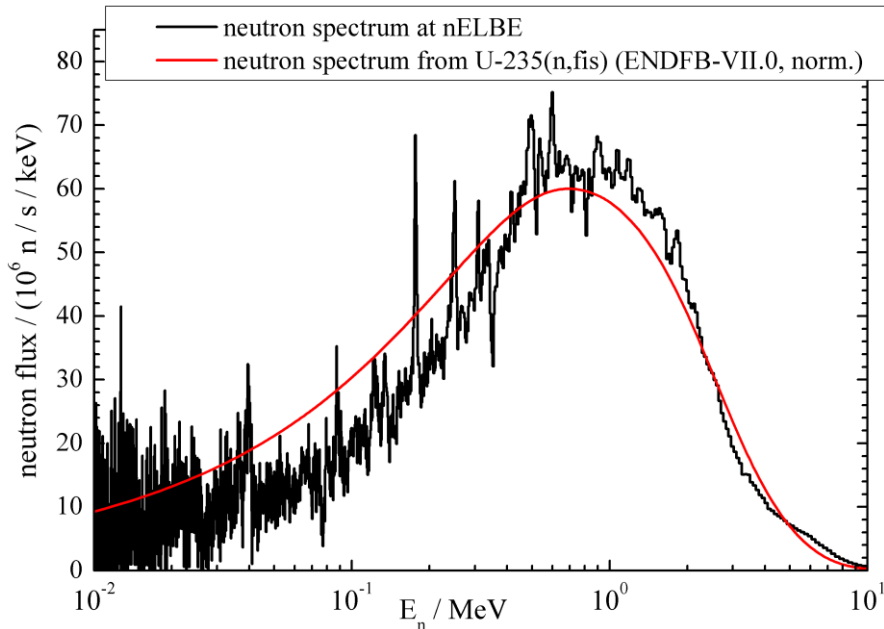
$\sigma(n,2n)$

(n,xn γ) measurement at nELBE

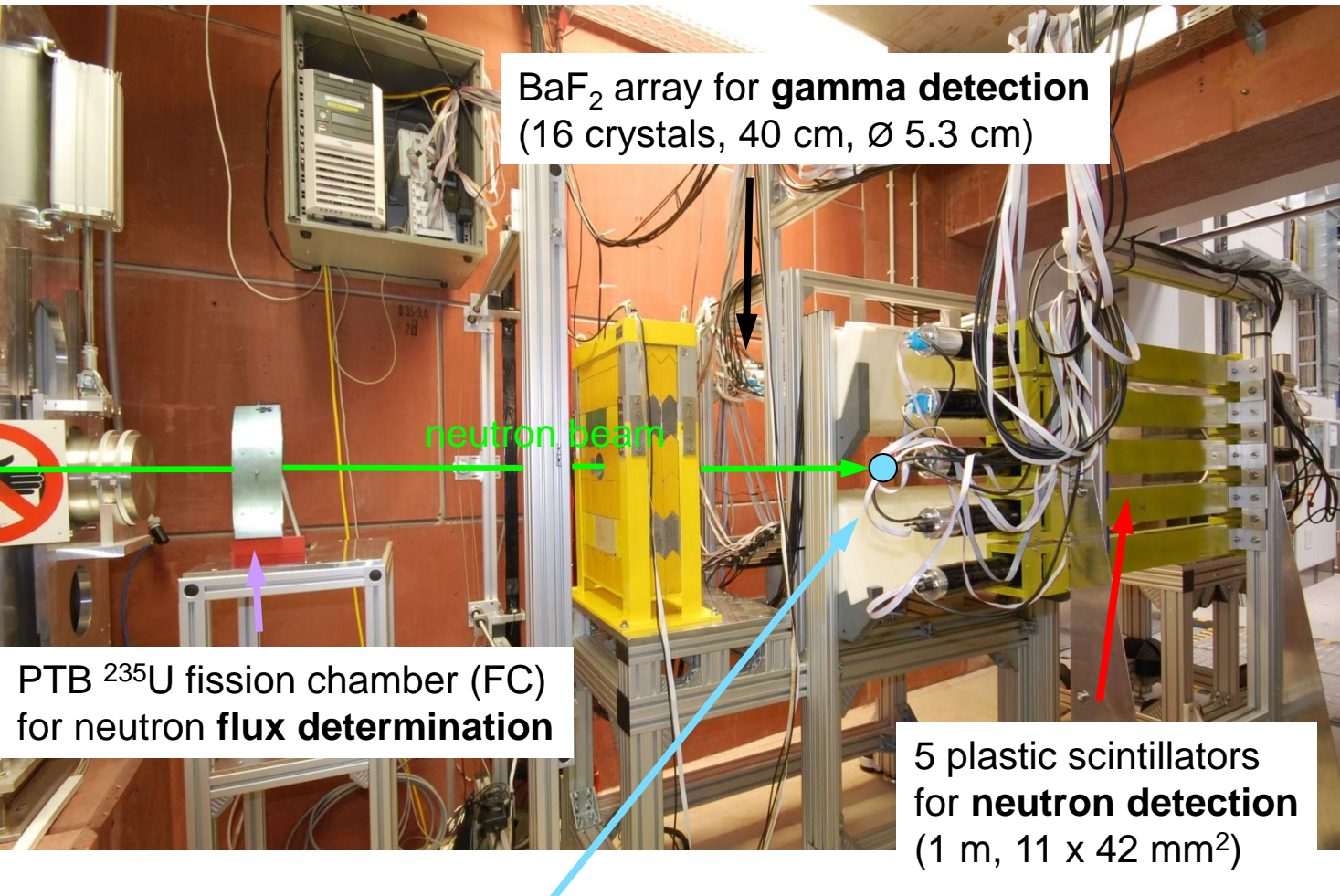


Neutron production : photo reaction

- $E < 10\text{MeV}$
- Collimated beam
- Pulsed beam



nELBE – double ToF detector setup



BaF₂ array for **gamma detection**
(16 crystals, 40 cm, Ø 5.3 cm)

neutron beam

PTB ²³⁵U fission chamber (FC)
for neutron **flux determination**

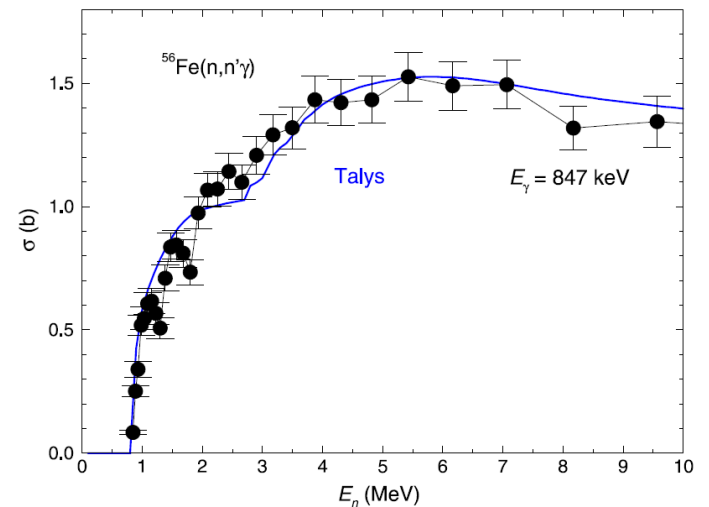
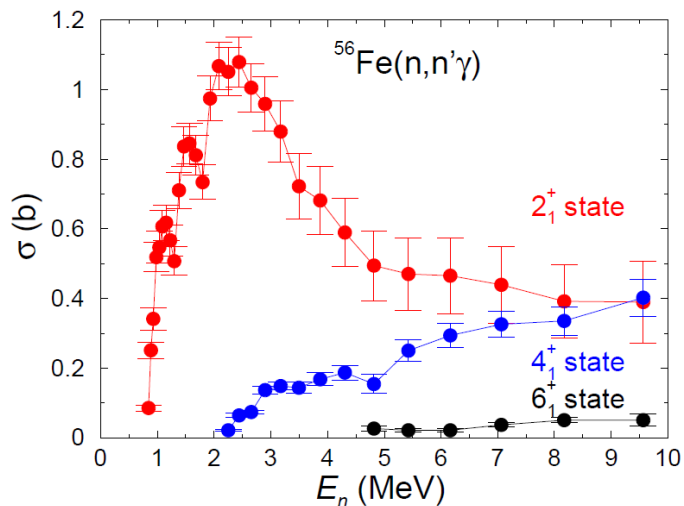
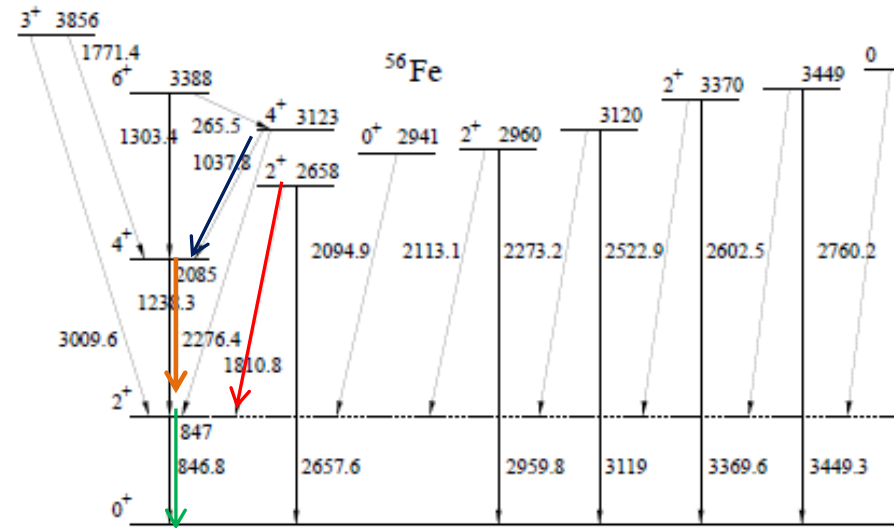
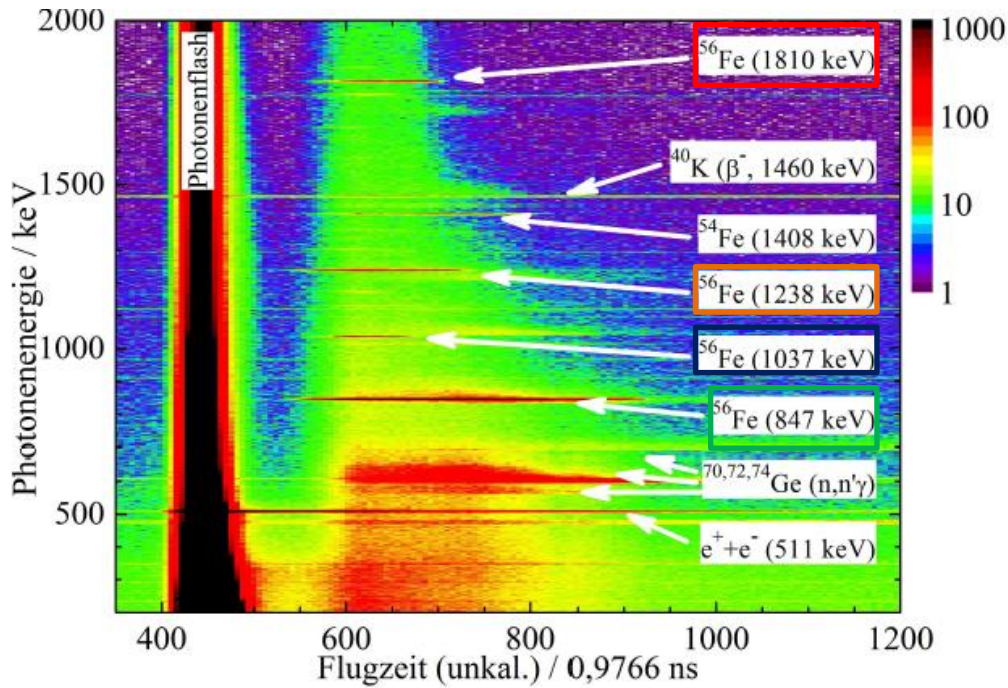
5 plastic scintillators
for **neutron detection**
(1 m, 11 x 42 mm²)

sample: ^{nat}Fe (99.8%) → 91.754% ⁵⁶Fe
mass: 19.82 g → 18.15 g ⁵⁶Fe

flight paths:
source - FC:
400 cm
source - sample:
600 cm
sample - BaF₂:
30 cm
sample - plastics:
100 cm

R. Beyer, PhD Thesis

$^{56}\text{Fe}(n,xn\gamma)$ measurement at nELBE



OUTLINE

Introduction

1. Applications
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- 3. Cross-section measurements**
 1. Activation technique
 2. $n, xn\gamma$ gamma
 - 3. Direct measurement of secondary neutrons**
4. Double differential measurements
5. Examples of experiments

Direct measurement of secondary neutrons

Measure the x neutrons emitted in the reaction

□ Advantages :

- Direct measurement
- Applicable to all nuclei

□ Drawbacks:

- Need a mono-isotopic target
- Neutron detector of high efficiency

□ Detector type :

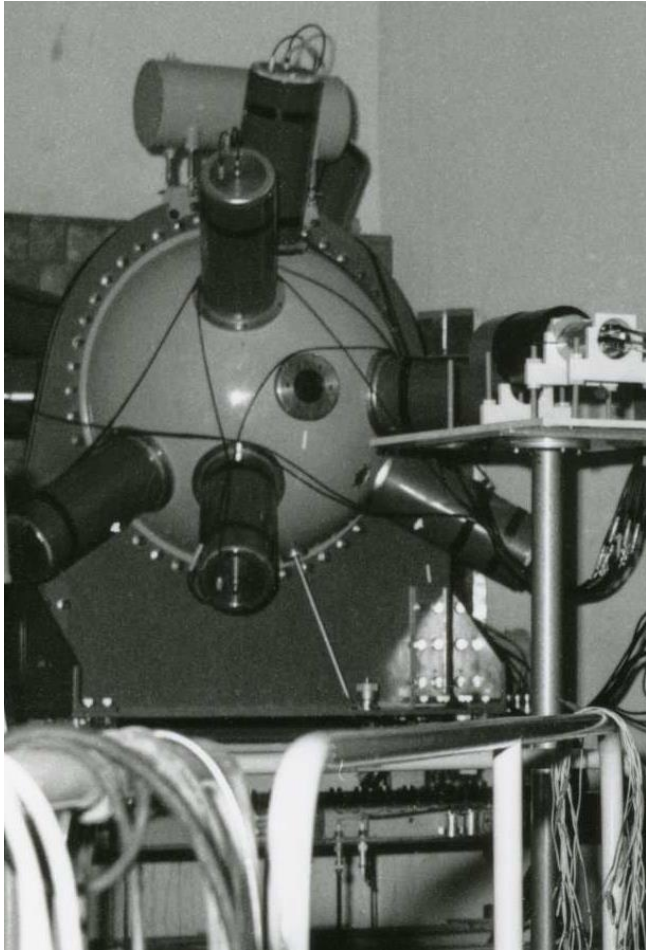
- Neutron balls
- Neutron spectrometer

The neutron balls

- Measurement of neutron multiplicity event by event
- Composed of a tank filled by liquid scintillator
- Phototubes detected the prompt and delayed signal

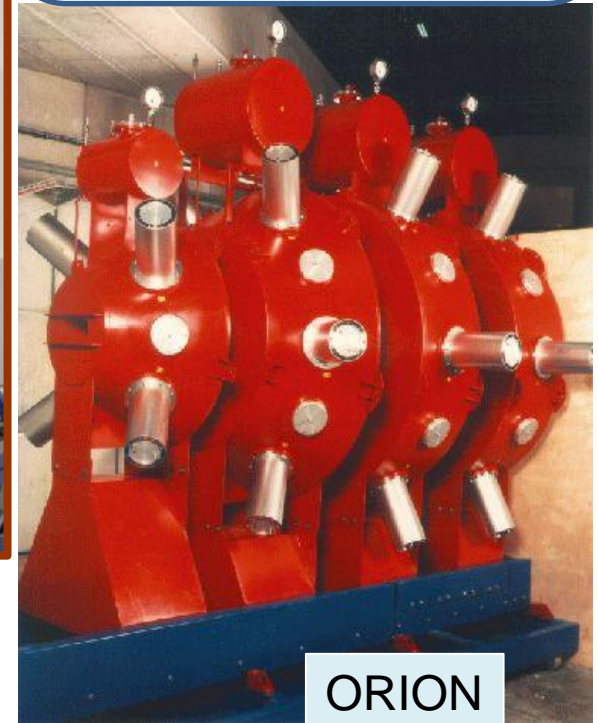
4π , high efficiency
High sensitivity to background

Application:
n,xn cross-section measurements
Nubar measurements
Hot nuclei studies



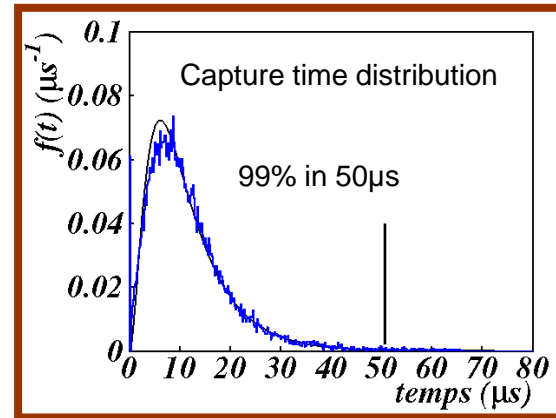
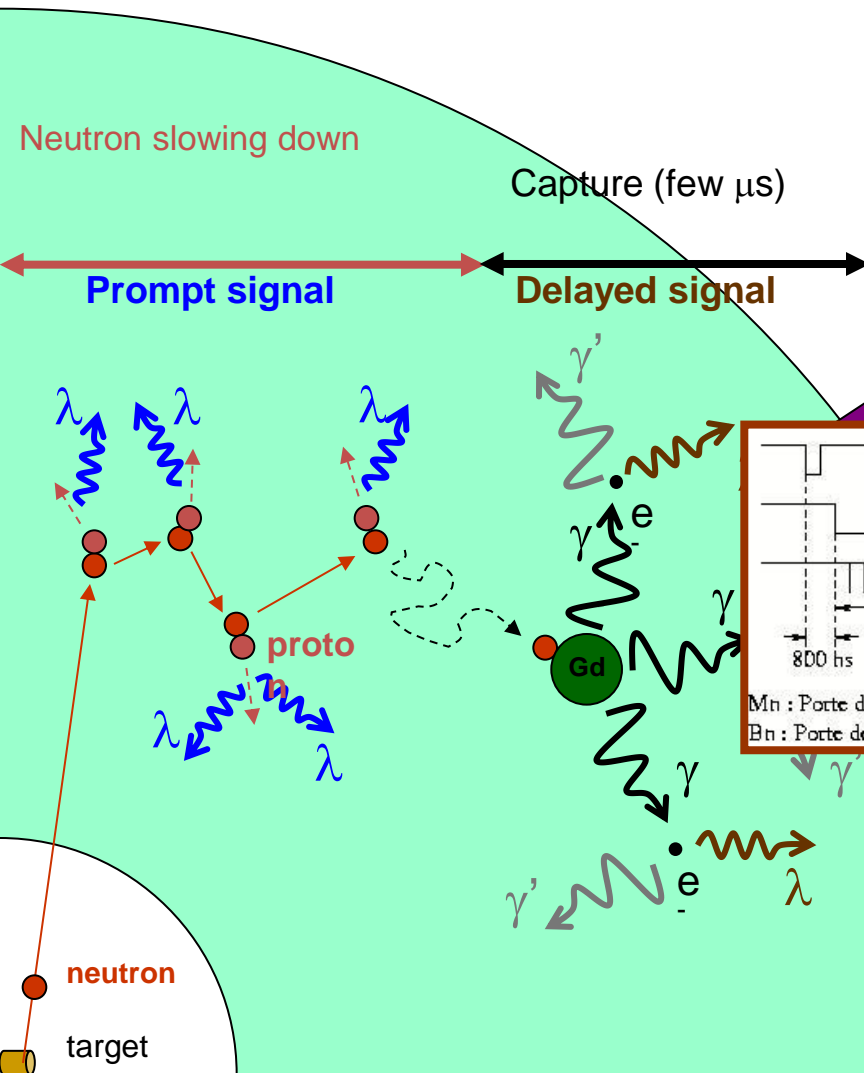
CARMEN

Measurement of neutron
Multiplicity distribution

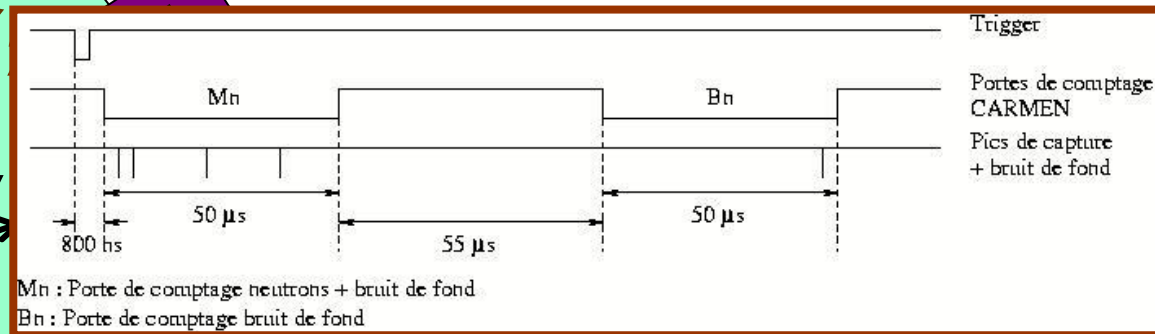


ORION

The neutron balls : working process



2 counting gates of 50 μs long



Efficiency

$$\varepsilon = \varepsilon_{\text{capt}} \cdot \varepsilon_{\text{lum}} \cdot \varepsilon_{\text{coll}}$$

Size of detector, E_n

Number of PM

□ The efficiency decreases when E_n increases :

- escape probability
- reactions on C

□ Increase the thickness r would increase the efficiency but :

- volume increases as r^3
- increase the background sensitivity

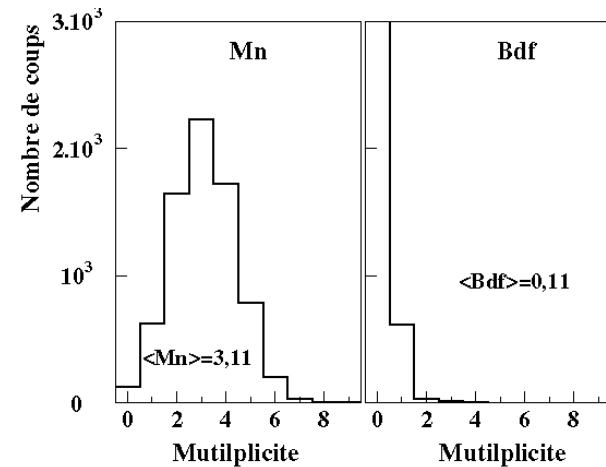
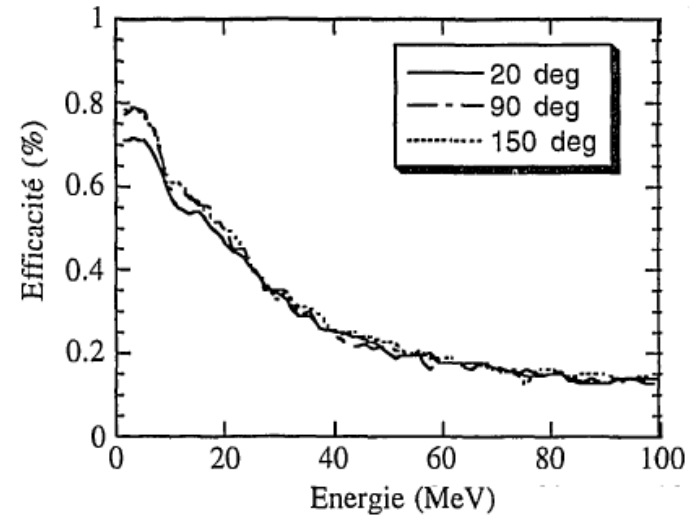
Efficiency determination :

- Monte-Carlo Simulations
- Measurement

- ^{252}Cf source ($\langle v \rangle = 3,78$)

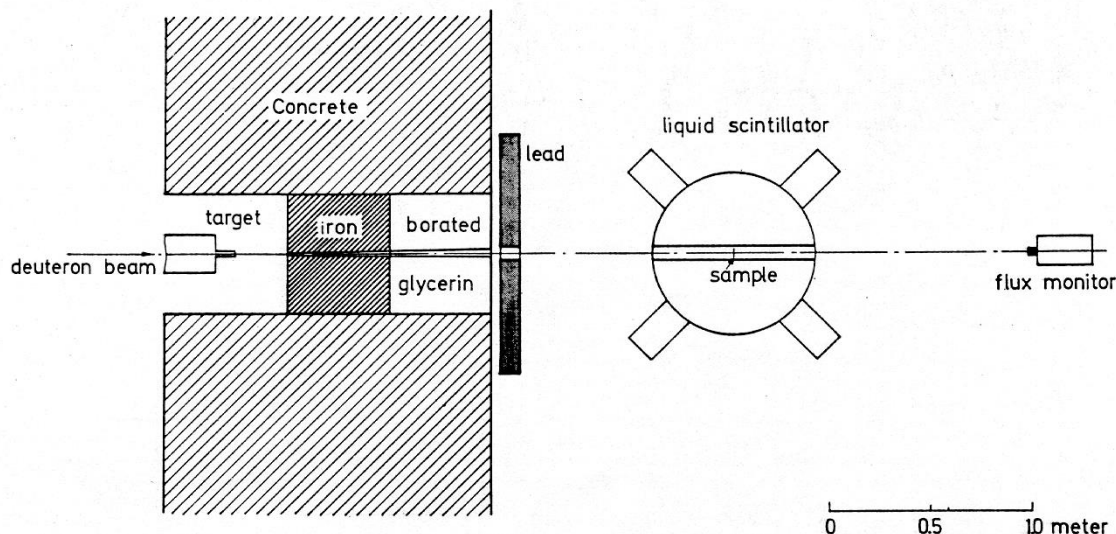
- Mn distribution in coincidence with the detection of fission fragment

Efficiency $\approx 85\%$ to fission neutrons



n,xn cross section measurement

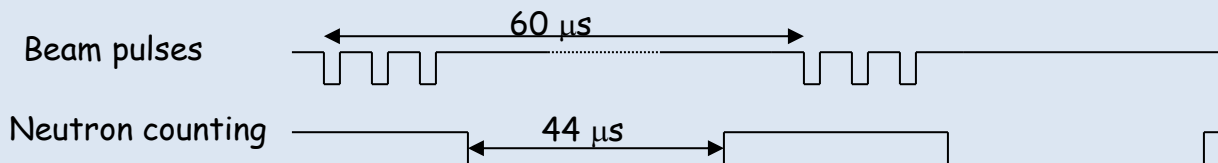
Measurement of $M_n(x)$: number of reactions with neutron multiplicity x



$$\sigma_{n,xn} = \frac{M_n(x)}{\Phi N_{at} \varepsilon}$$

Φ = flux (cm^{-2})
 $N_{at} = m N_{av} / A$
 ε = efficiency

Background : 2 gates and deconvolution



Trigger: prompt peak

Passive target :
 Mono-energetic neutrons

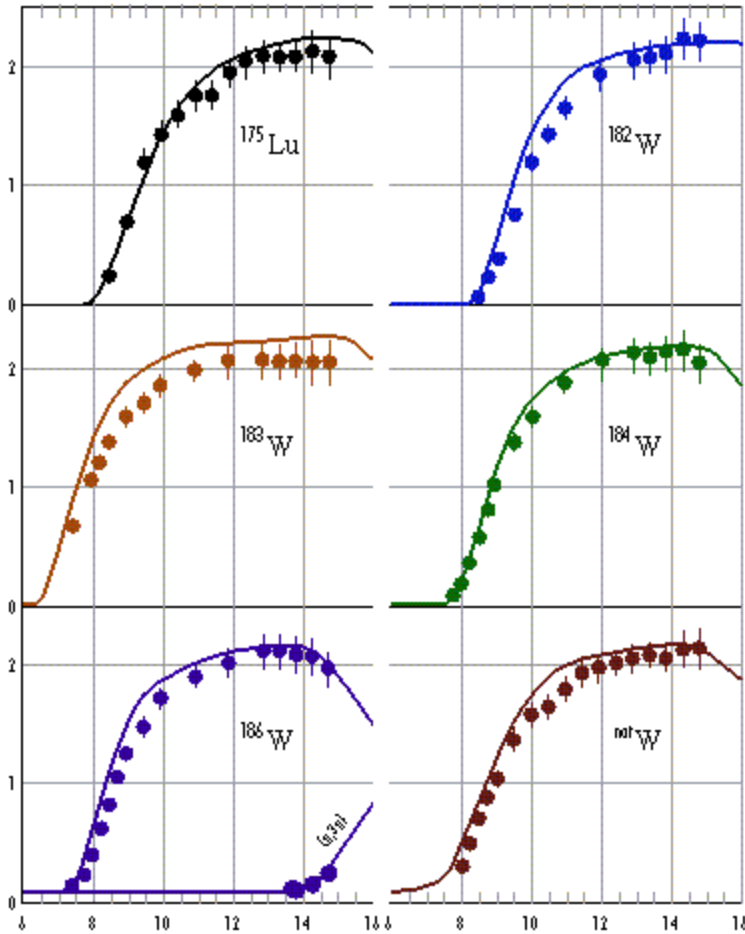
Efficiency : Cf source

simulations to take into account the energy and angular distributions

J. Fréhaut, Nuclear Instruments and Methods 135 (1976) 511-518

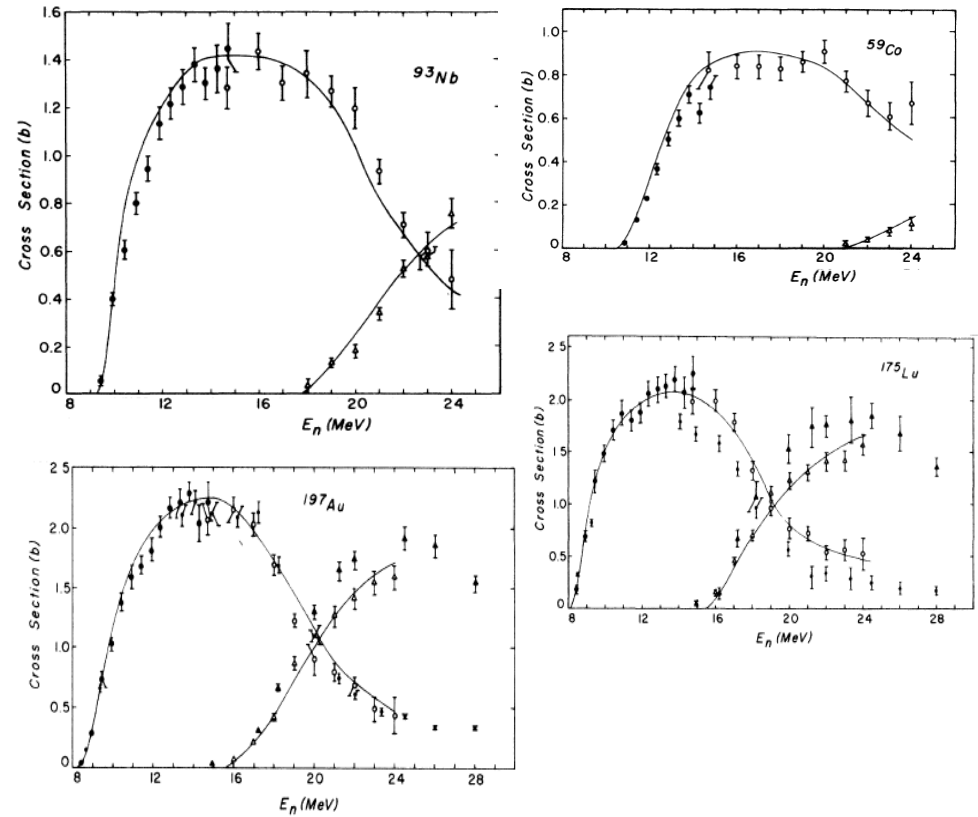
Some $\sigma(n,2n)$ and $\sigma(n,3n)$ measured with neutron balls

Fréhaut et al.



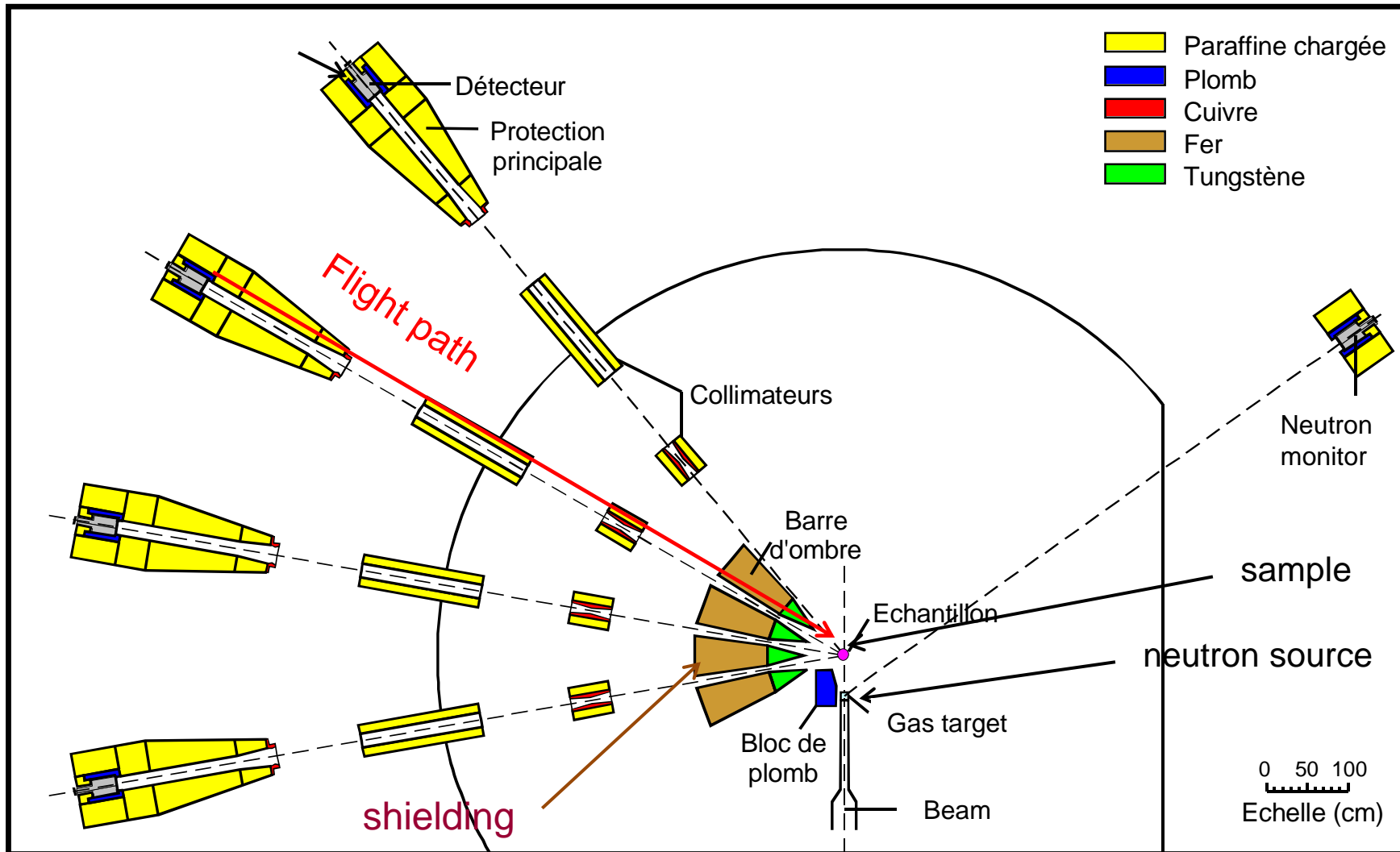
L. R. Veaser et al., PRC 16, num 5 (1977) p 1792

Comparison with radiochemical measurements



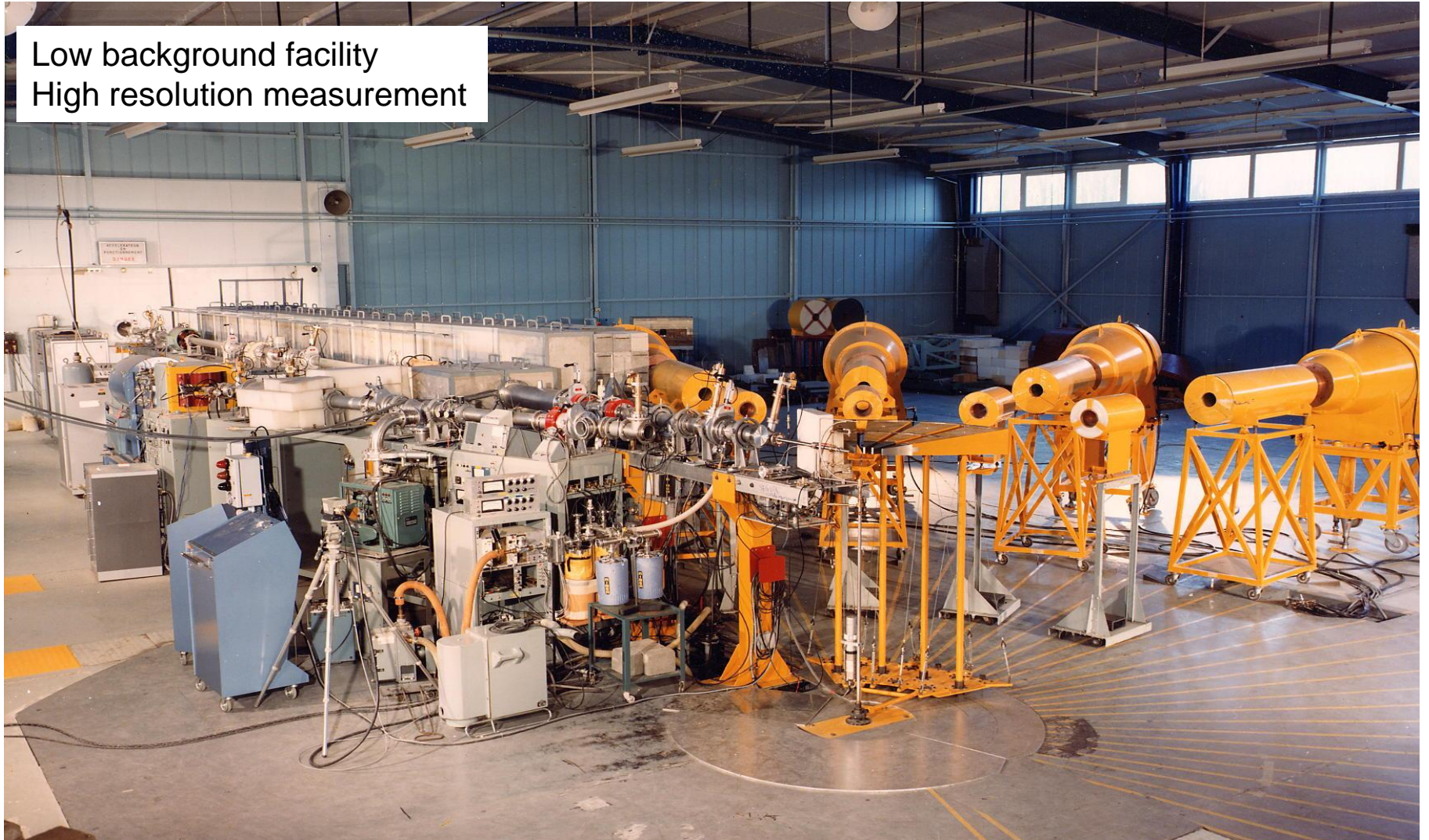
Neutron spectrometer

Elastic and inelastic cross-section measurements



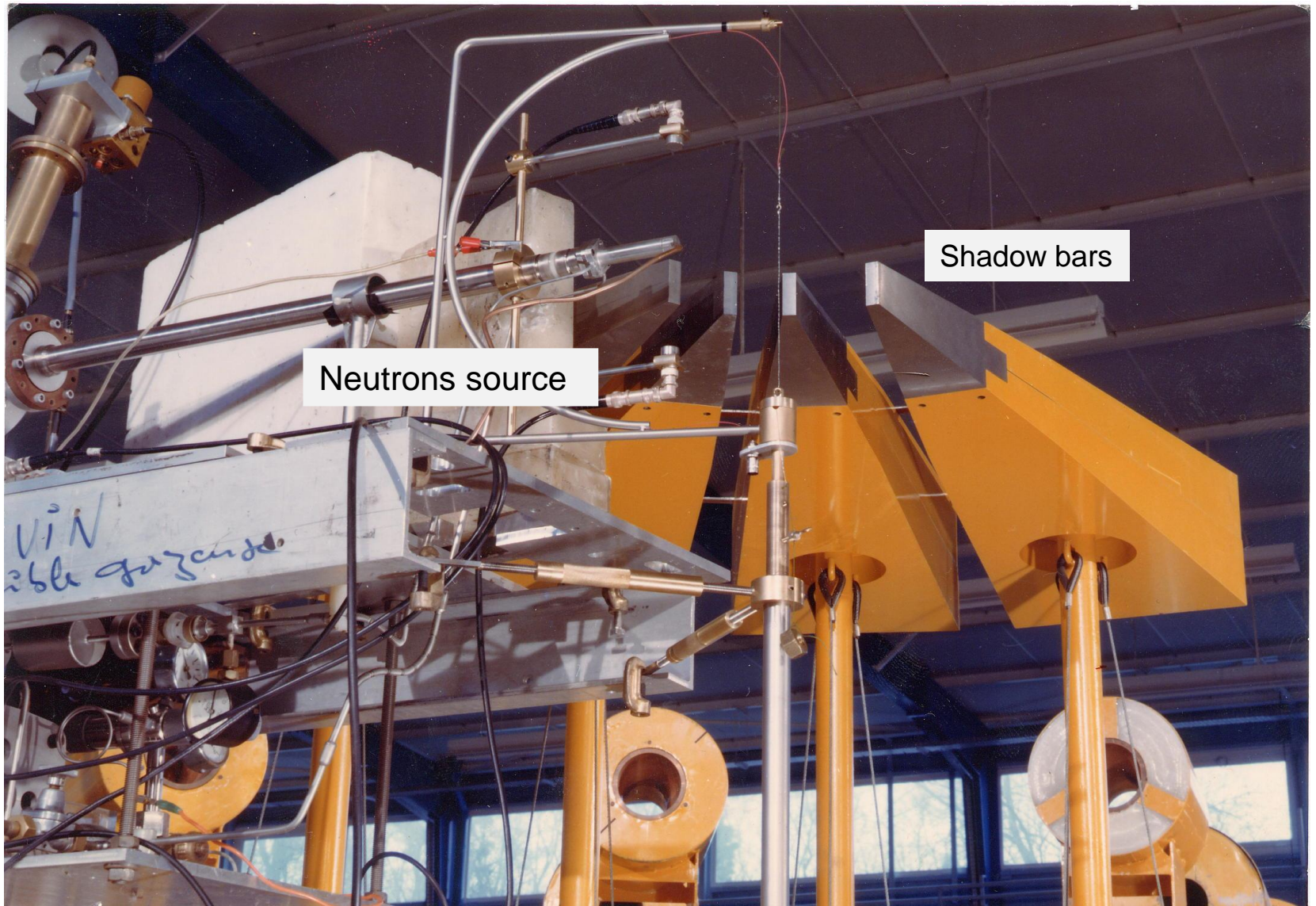
Spectrometer of CEA/Bruyères-le-Châtel

Low background facility
High resolution measurement



J. Lachkar, M. T. Mc Ellistrem, G. Haouat, Y. Patin, J. Sigaud and F. Coçu, *Phys. Rev. C* **14**, 933 (1976)
G. Haouat, J. Lachkar, J. Sigaud, Y. Patin and F. Coçu, *Nucl. Sci. Eng.* **65**, 331-346 (1978)
G. Haouat, J. Lachkar, Ch. Lagrange, J. Jary, J. Sigaud, and Y. Patin, *Nucl. Sci. Eng.* **81**, 491-511 (1982)

Sample and shadow bars



Neutron energy measurement

Energy measurement:

$$\text{Flight path : } d \xrightarrow{\text{tof}_n} v = \frac{d}{\text{tof}_n} \xrightarrow{\beta = \frac{v}{c}} \gamma = \frac{1}{\sqrt{1 - \beta^2}} \xrightarrow{E = (\gamma - 1) m c^2}$$

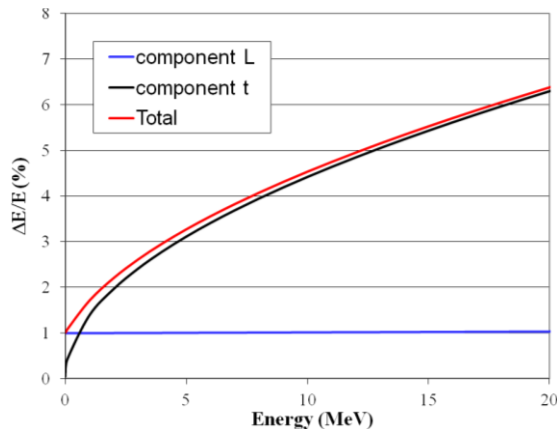
Start and stop signals : detector + accelerator or active target

Energy resolution:

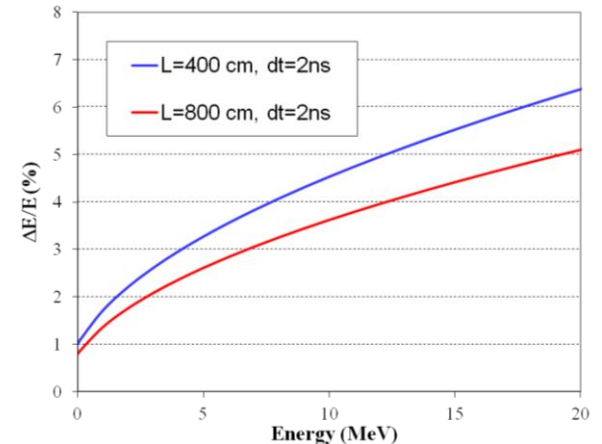
$$\frac{\Delta E}{E} = \gamma(\gamma + 1) \sqrt{\left(\frac{\Delta t}{t}\right)^2 + \left(\frac{\Delta d}{d}\right)^2}$$

Δt time resolution detector + accelerator ≈ 1 ns

ΔL flight path uncertainty



The Flight path is a compromise
between
The energy resolution
The efficiency

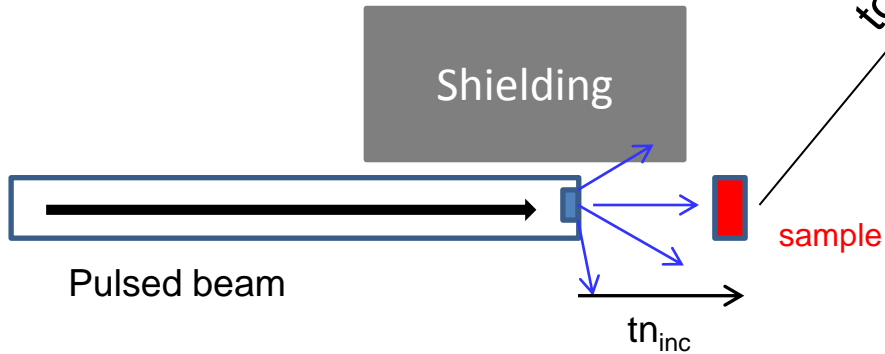


TOF technique

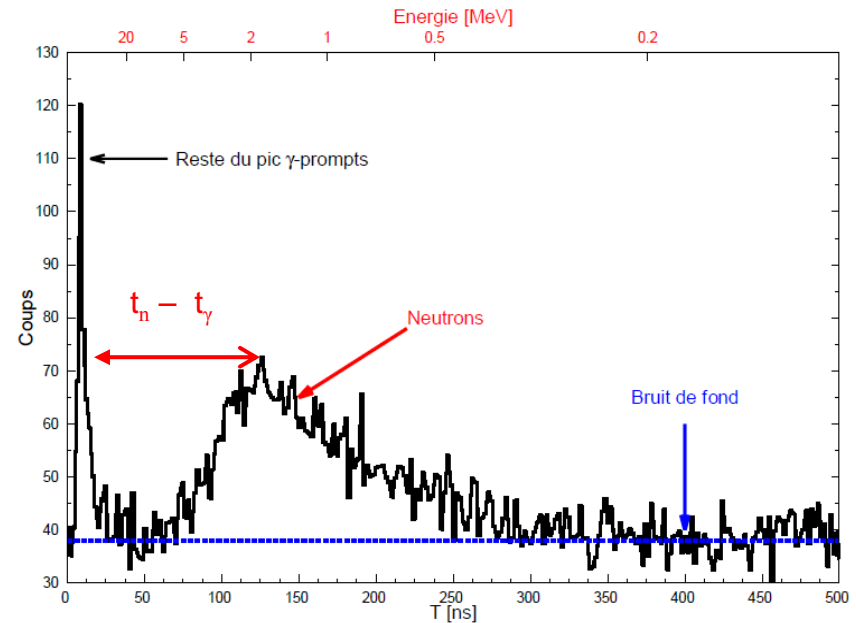
t_{mes} = time between detector and accelerator HF
 $tof = t_{mes} - cst - tn_{inc} = t_{mes} - K$
 tn_{inc} must be constant -> **mono-energetic neutrons**



tof



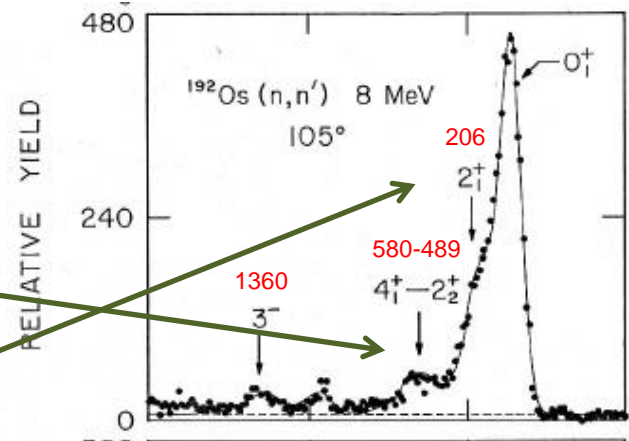
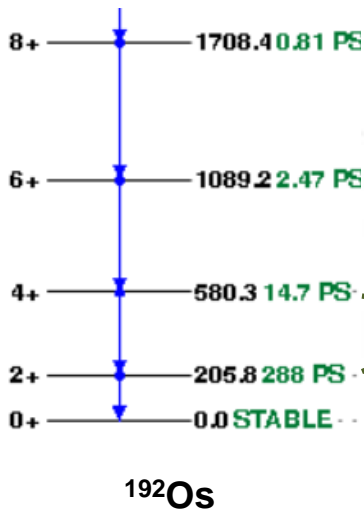
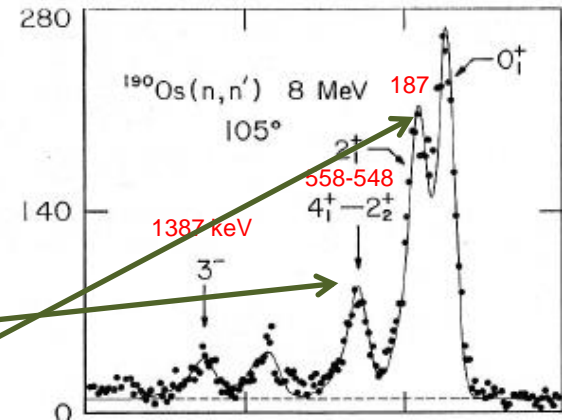
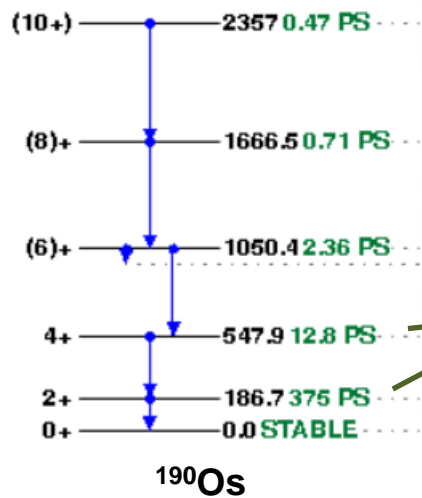
- tof is not a absolute measurement
- use of gamma to calibrate tof
- $tof_{\gamma} = t_{\gamma} - K = d/c$
- $K = t_{\gamma} - d/c$
- $tof_n = t_n - K = t_n - t_{\gamma} + d/c$



$^{190}\text{Os}(n,n')^{190}\text{Os}$

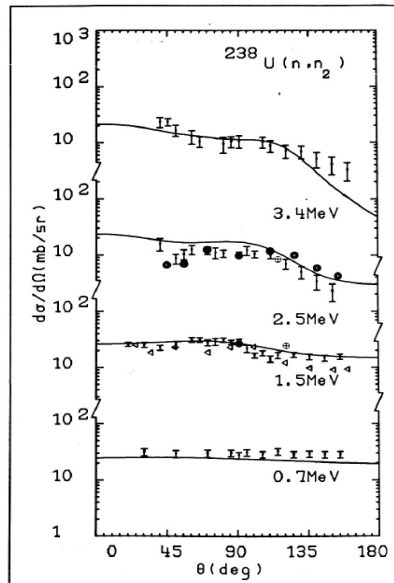
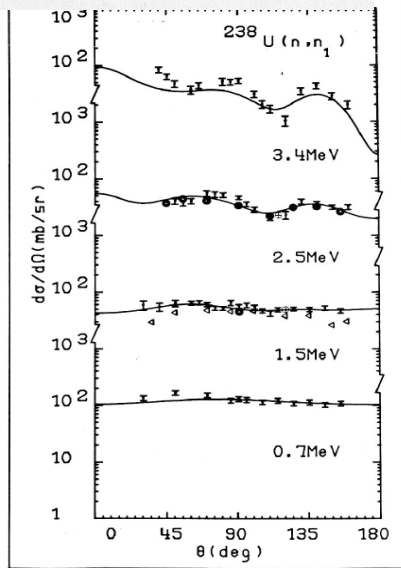
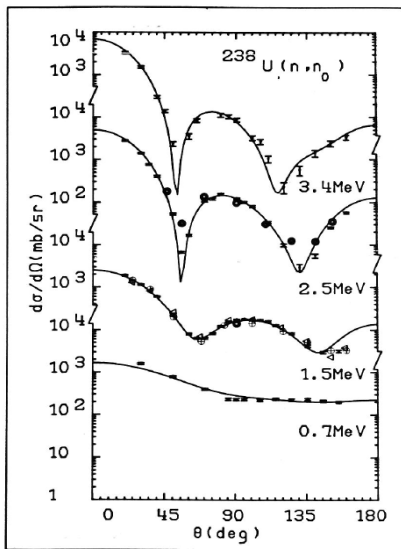
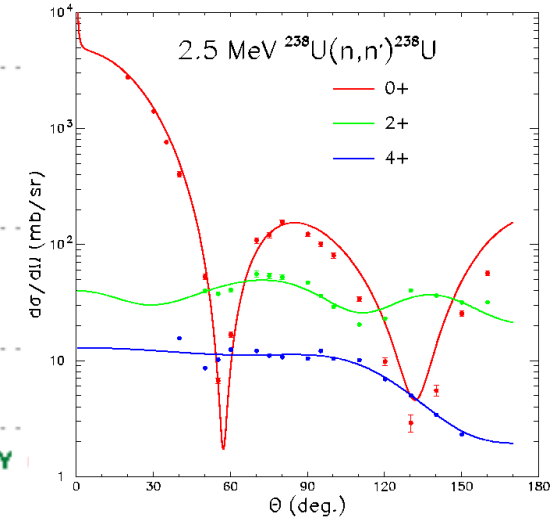
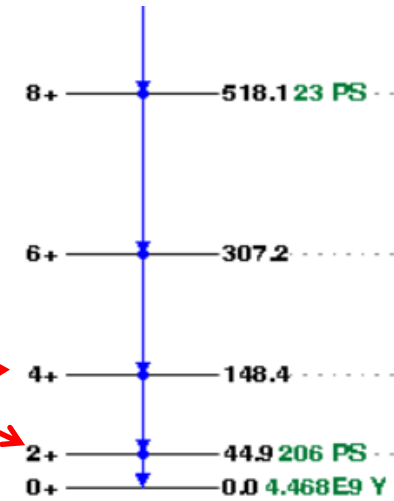
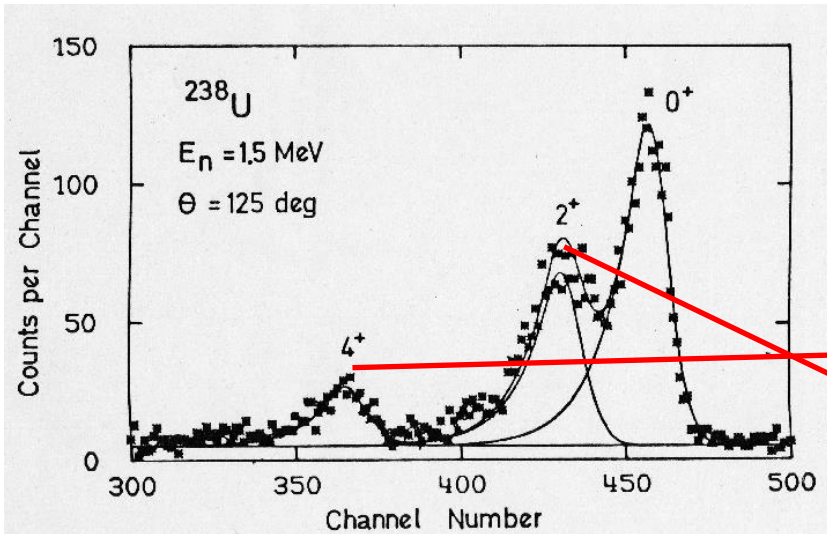
- $E_n = 8,0 \text{ MeV}$
- $L = 8,0 \text{ m}$
- $\theta = 105^\circ$
- Samples (Cylinders of metal)

Noyau	m(g)
^{190}Os	38,82
^{192}Os	66,63



Time-of-flight (channel)

$^{238}\text{U}(n,n')^{238}\text{U}$



The first excited state 45 keV requires a very good energy resolution

E (MeV)	TOF (ns)
1,5	295
1,455	300
1,355	311

Counting rate estimation

▪ Neutron source

- $I = 3$ to $5 \mu\text{A}$
- Tritium target

$$\text{Flux : } \Phi = 3 \cdot 10^8 \text{ n} \cdot \text{sr}^{-1} \cdot \text{s}^{-1}$$

▪ Sample

- $m = 30 \text{ g}$
- $A = 190$
- Distance source sample $d = 7 \text{ cm}$

$$d\sigma/d\Omega = 10 \text{ mb} \cdot \text{sr}^{-1}$$

▪ Detector:

- Surface detector = $\pi * r^2 = 122 \text{ cm}^2$
- Intrinsic efficiency = 10%
- Distance from sample $L = 800 \text{ cm}$

Number of neutrons detected by second :

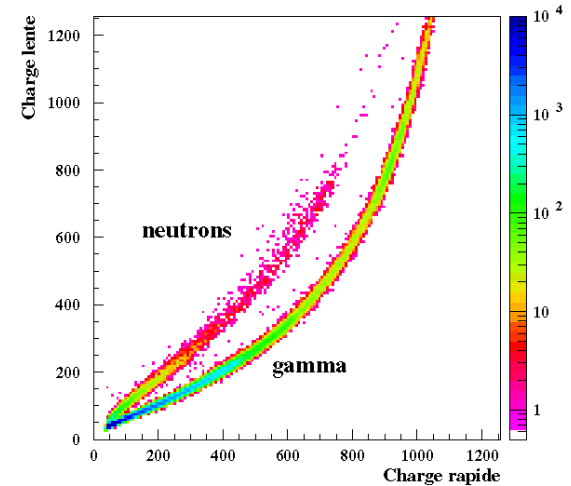
$$N_{\text{det}} = \frac{\Phi}{d^2} \frac{m N_{\text{avo}}}{A} \frac{d\sigma}{d\Omega} \frac{S}{L^2} \varepsilon$$

$$N_{\text{det}} \approx 1 \text{ counts/s}$$

Multicells detectors

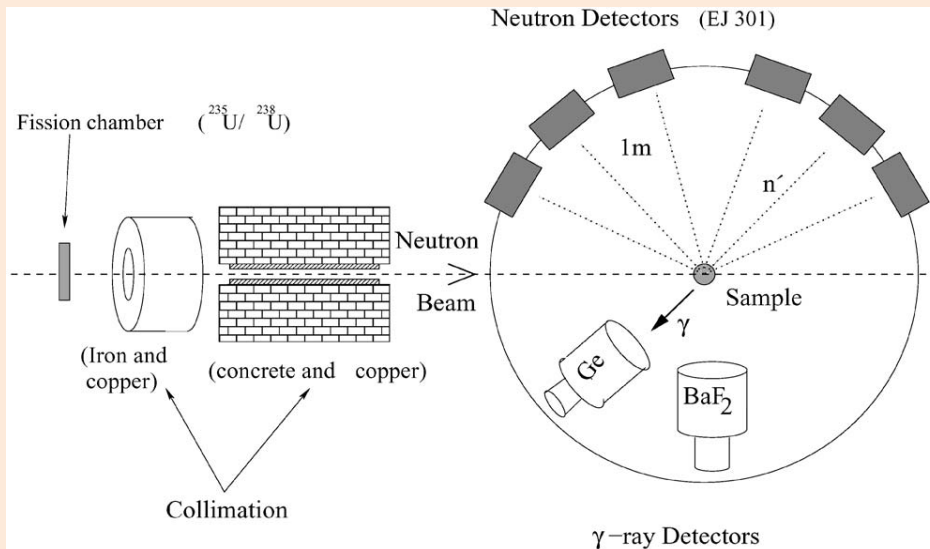
- ❑ Array of neutrons detector cells
- ❑ Low efficiency:
 - Geometrical effect
 - Intrinsic efficiency $\approx 20\%$
- ❑ Measurement of average neutron multiplicity
- ❑ Measurement of energy and angular distributions

need a trigger signal



The FIGARO facility

(n, xn') measurements



20 EJ301 liquid scintillator
45 to 135°
1m of flight path

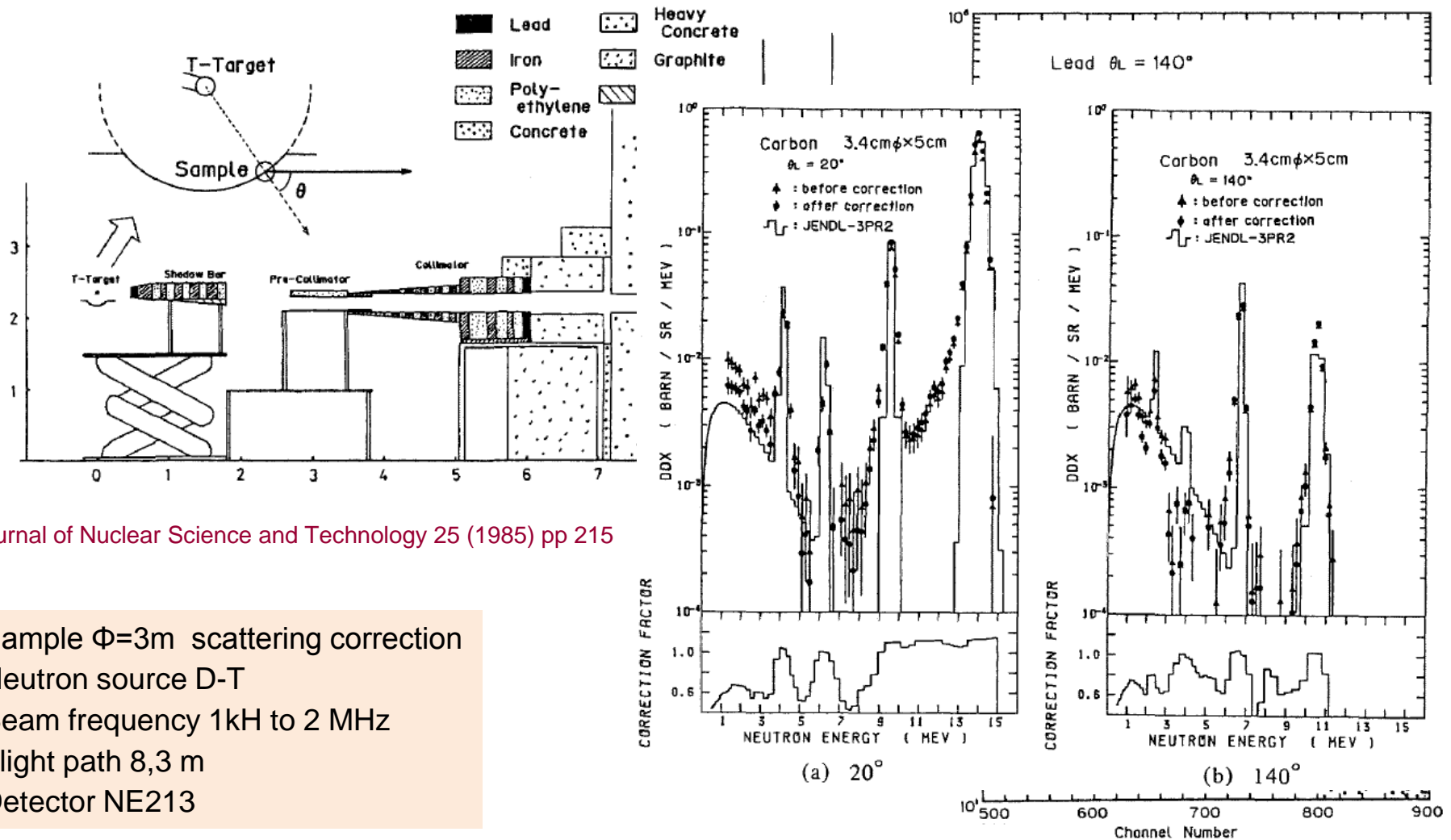


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5. Examples of experiments

Measurement of double differential emission cross-section for incident neutrons of 14,1 MeV



Journal of Nuclear Science and Technology 25 (1985) pp 215

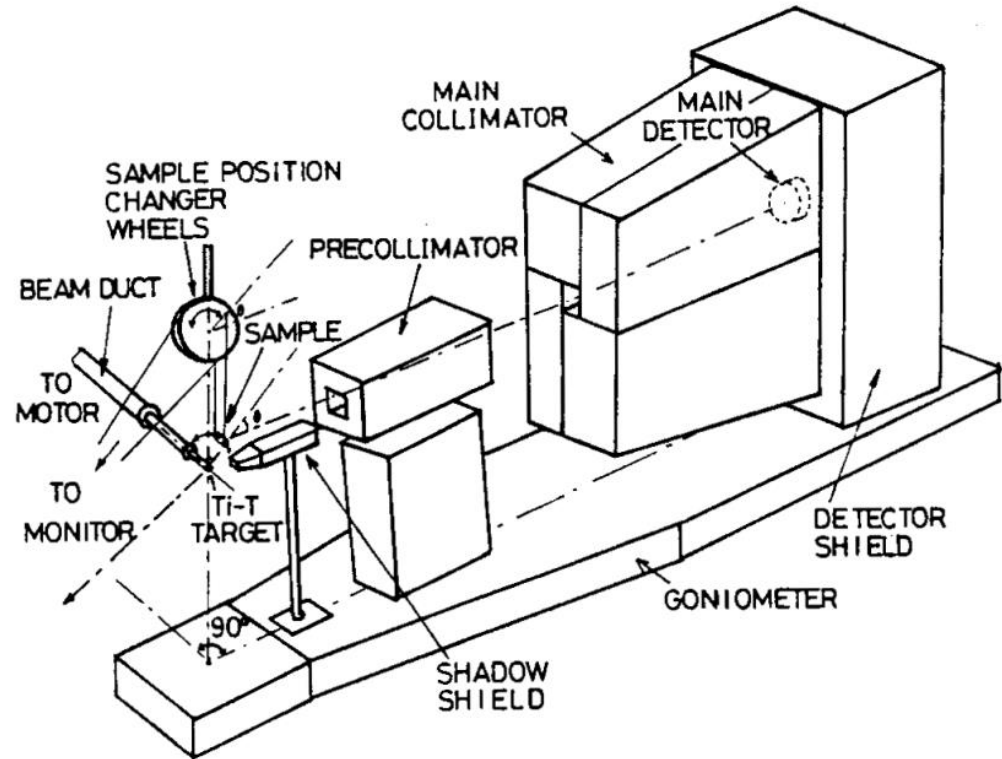
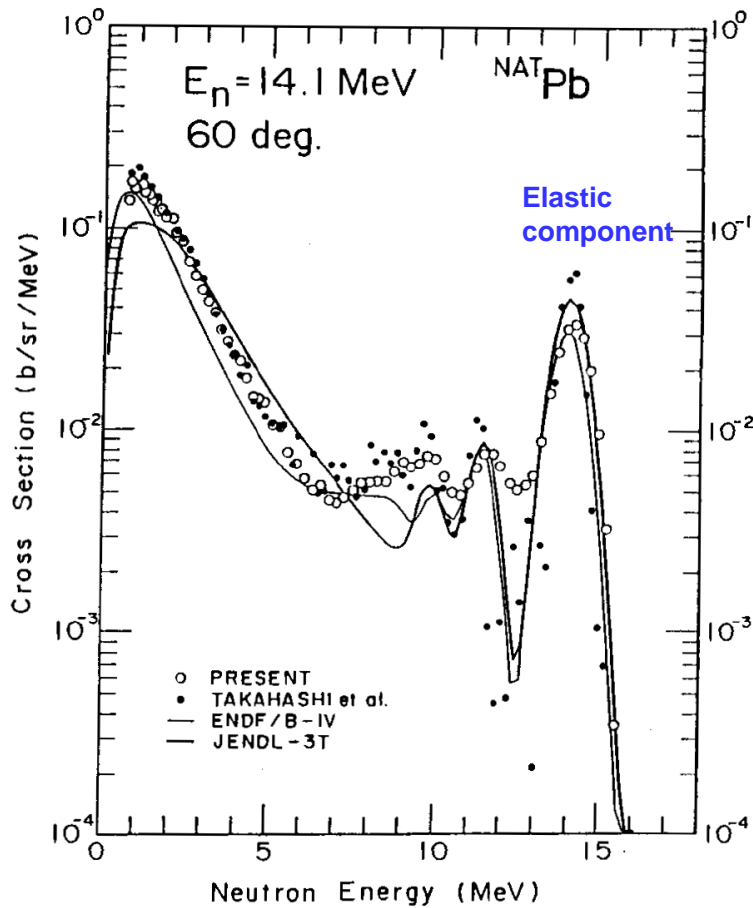
Sample $\Phi=3\text{m}$ scattering correction
 Neutron source D-T
 Beam frequency 1kHz to 2 MHz
 Flight path 8,3 m
 Detector NE213

The neutron spectrum is the sum of all the channels where at least one neutron is emitted

Pb(n,2n)

Nuclear Data for Science and Technology(1988 MITO), 229- 232, Copyright © 1988 JAERI.

Sample $\Phi=3\text{cm}$, $h=4\text{cm}$
Source d+T
Pulsed beam



S. Iwasaki, N. Odano, S. Tanaka, J.R. Dumais
and
K. Sugiyama

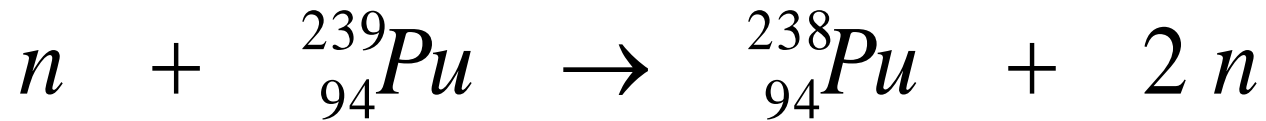
Department of Nuclear Engineering, Tohoku University
Aramaki-Aoba, Sendai 980, Japan

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$^{239}\text{Pu}(n,2n)$ reaction cross-section measurement



$T_{1/2} = 24110 \text{ y}$

$T_{1/2} = 87,7 \text{ y}$

α emitter 5456 keV
5499 keV

- Activation technique
- Measurement of direct neutrons
- n,xn γ measurement

$^{239}\text{Pu}(n,2n)^{238}\text{Pu}$ cross-section by Activation technique

$^{239}\text{Pu}(n,2n)$ cross-section measurement near $E_n=14\text{MeV}$, R. W. Lougheed, Radiochim. Acta 90, 833-843 (2002)

□ Irradiation :

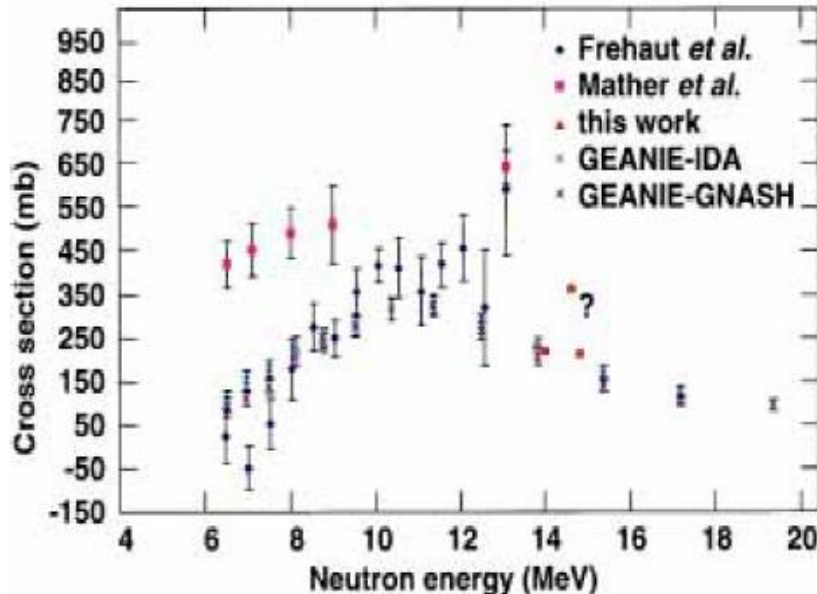
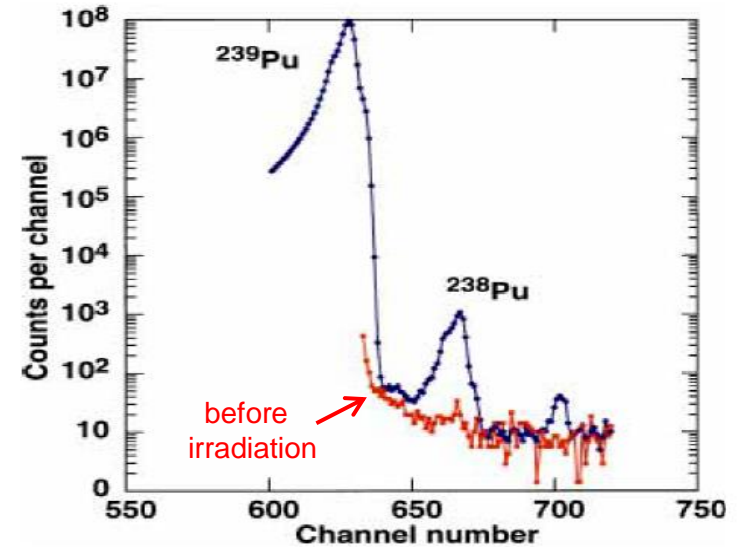
- Neutrons produced by d+T reaction
- Flux : $5,5 \cdot 10^{11} \text{ n.cm}^{-2} \cdot \text{s}^{-1}$
- Integrated fluence : $8,98 \cdot 10^{17} \text{ n}$ in 4π

□ Sample :

- $130\mu\text{g.cm}^{-2}$, $\Phi=3 \text{ mm}$ → $10\mu\text{g}$
- $^{238}\text{Pu}/^{239}\text{Pu} \approx 6 \cdot 10^{-10}$ before irradiation
- Distance source sample 4mm

□ Monitoring : Au(n,2n) cross-section

^{238}Pu Activity → alpha spectroscopy



Before irradiation: $A(^{238}\text{Pu}) \approx 0,004 \text{ Bq}$
 Integrated fluence = $8,98 \cdot 10^{17} \text{ n.cm}^{-2}$
 After irradiation of
 $m = 10\mu\text{g}$
 $\sigma = 0,3 \text{ barn}$
 $N_{\text{at}} ^{238}\text{Pu} = 10^9$
 $A(^{238}\text{Pu}) \approx 2 \text{ Bq}$

$^{239}\text{Pu}(n,2n)^{238}\text{Pu}$ cross-section from partial γ -ray cross-sections (1)

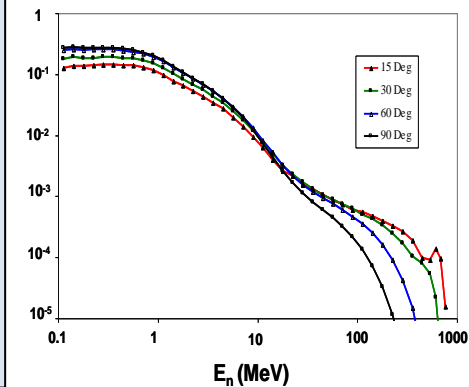
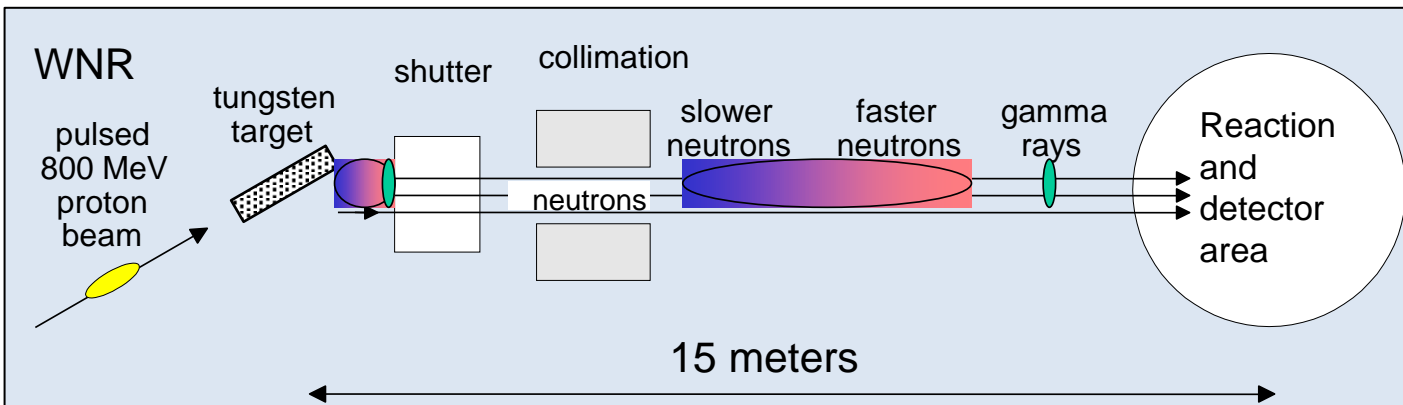
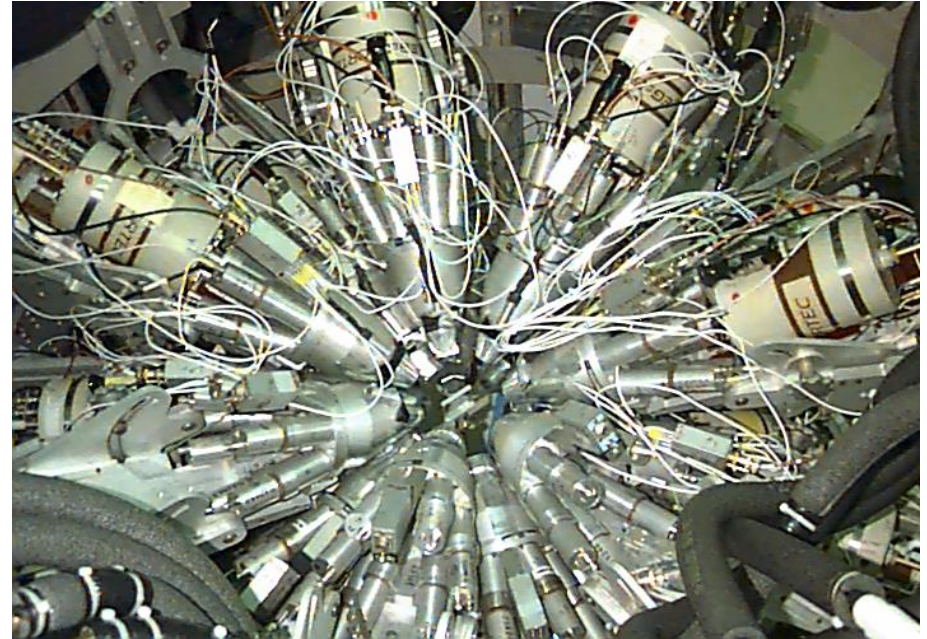
GERmanium Array for Neutron Induced Excitations

□ LANSCE (Los Alamos Neutron Science Center)

- Spallation source
- White neutron beam
- Pulsed beam

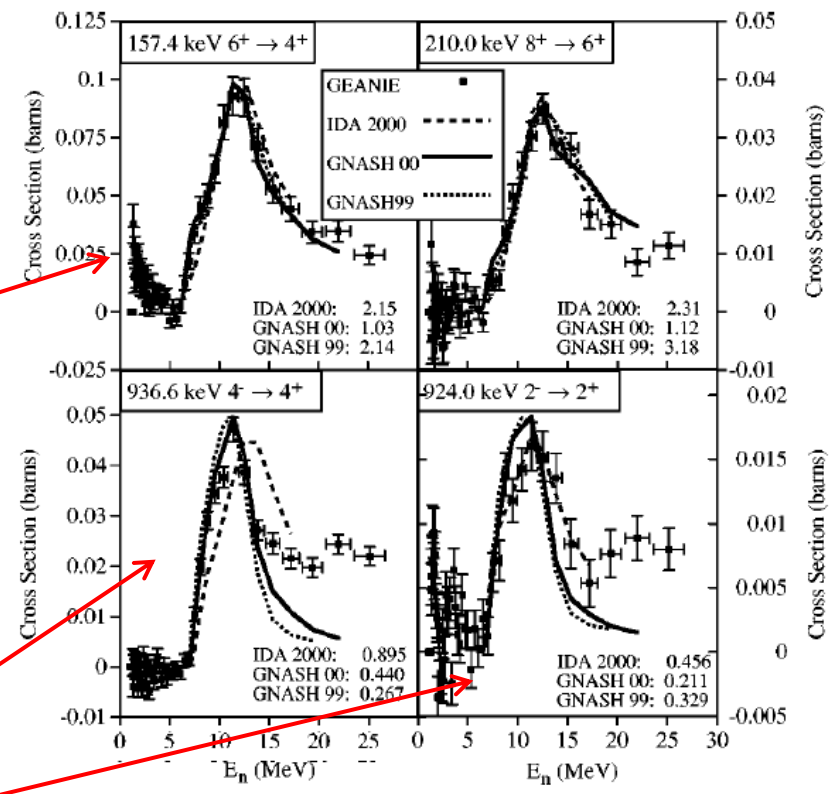
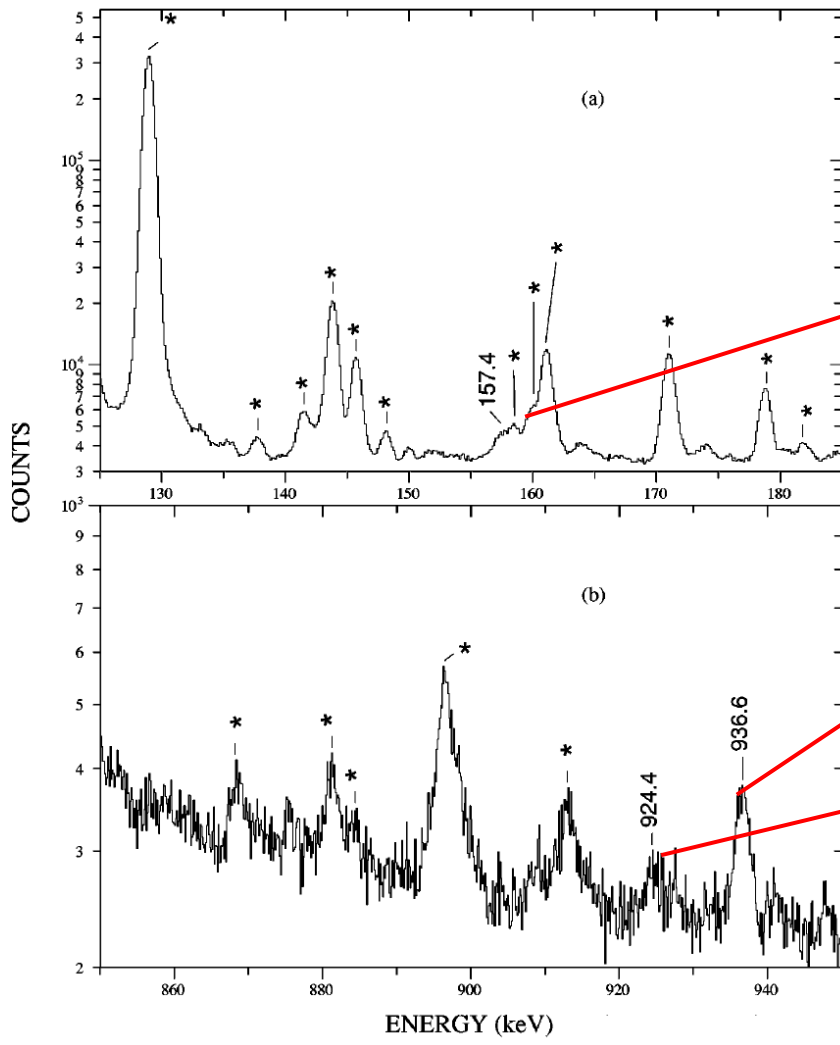
□ GEANIE

- 26 high-resolution Ge detectors
- BGO escape-suppression shields.



$^{239}\text{Pu}(n,2n)^{238}\text{Pu}$ cross-section from partial γ -ray cross-sections (2)

En=11,37 MeV



Use of theoretical calculations to deduce (n,2n) cross-section

L. A. Bernstein et al., PHYSICAL REVIEW C 65 021601(R)

Direct measurement of secondary neutrons

Difficulty : distinguishing fission neutrons from (n,2n)

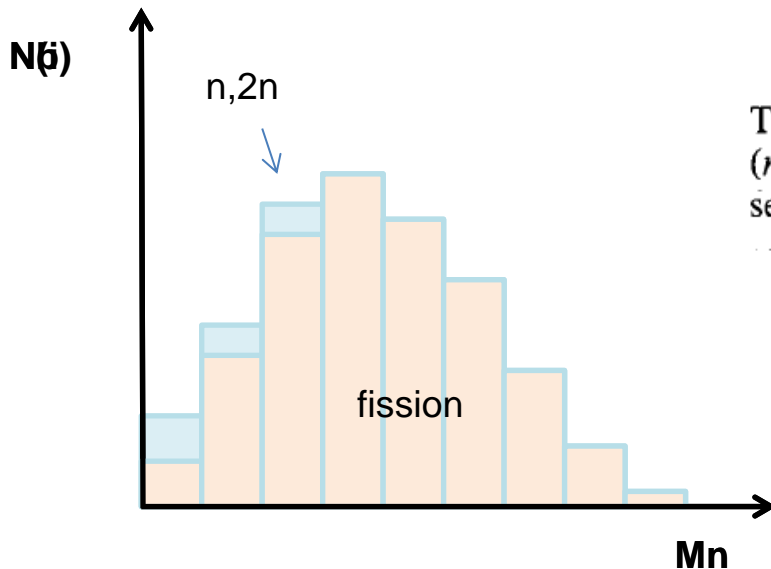
❑ Total neutrons multiplicity measurement (n,fis) + (n,2n) + (n,n')

- Neutron ball
- Thick target
- Trigger on prompt peak

❑ For Mn ≥ 4 only fission contribution

❑ Mn=2

$$N_F = \frac{\sum_{i \geq 4} N(i)}{\sum_{\nu \geq 4} P(\nu)} \quad . \quad P(i) \text{ fission multiplicity probability}$$



$$N_2 = N(2) - N_F P(2) \quad ,$$

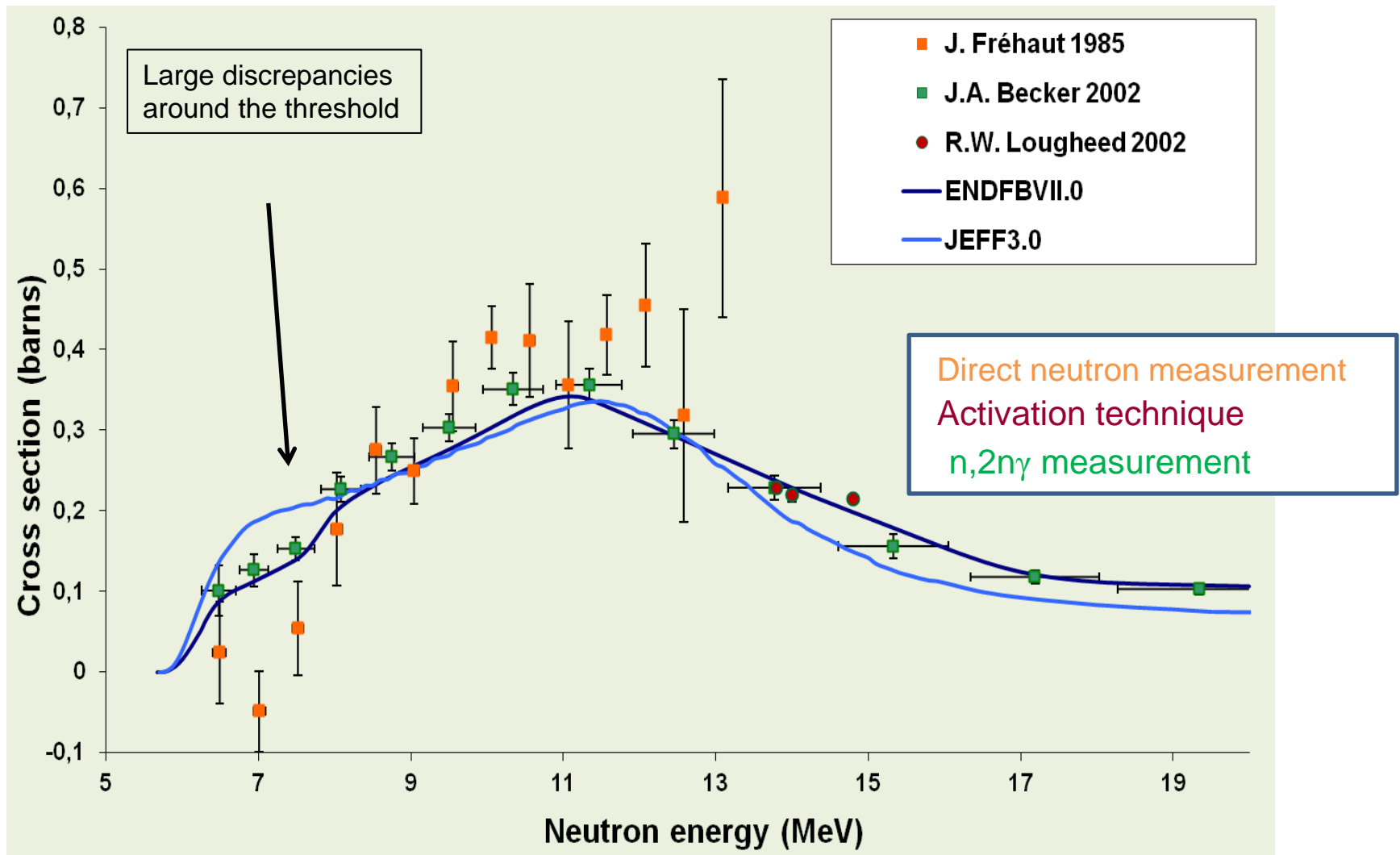
$$N_3 = N(3) - N_F P(3) \quad . \quad (2)$$

This method therefore provided the ratio of the (n,2n) or the (n,3n) cross section to the fission cross section:

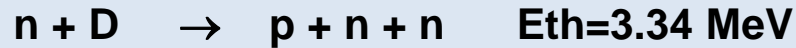
$$\frac{\sigma_2}{\sigma_F} = \frac{N_2}{N_F} \quad \text{and} \quad \frac{\sigma_3}{\sigma_F} = \frac{N_3}{N_F} \quad . \quad (3)$$

J. Fréhaut et al. NUCLEAR SCIENCE AND ENGINEERING: 74, 29-33 (1980)

Results on the $^{239}\text{Pu}(n,2n)^{238}\text{Pu}$ cross-section measurements

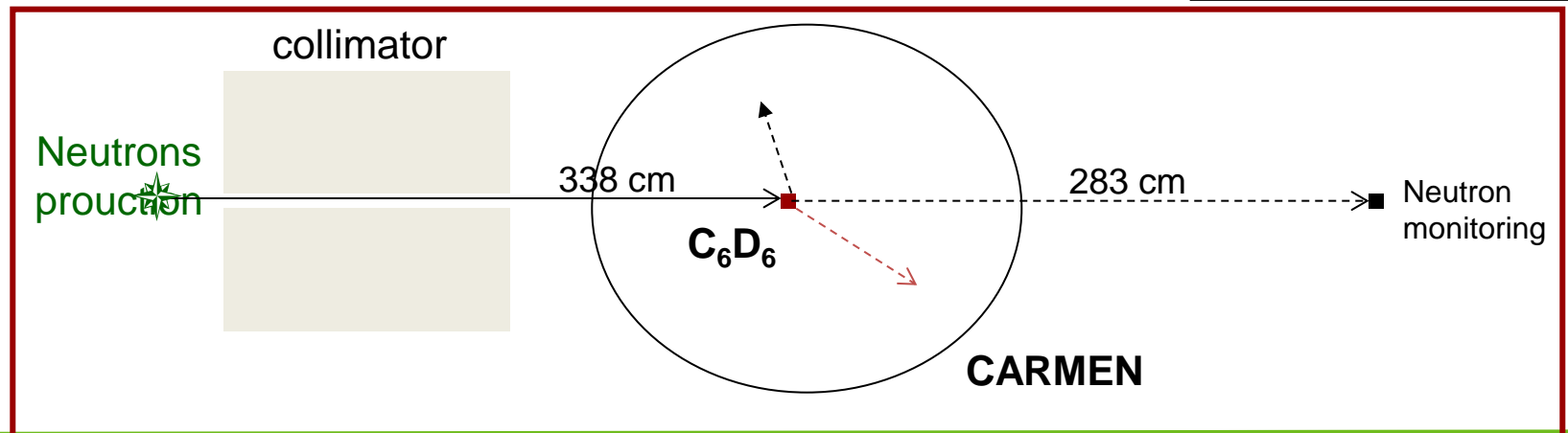
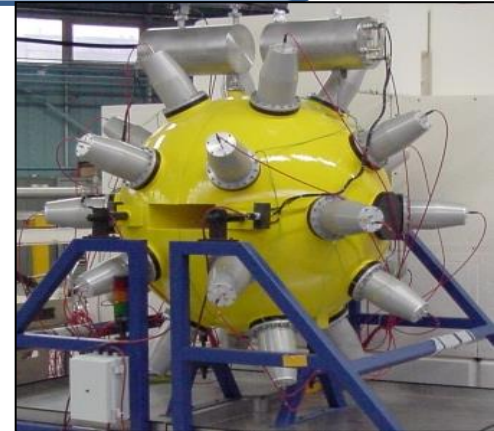


Cross-section measurement of the D(n,2n) reaction (1)

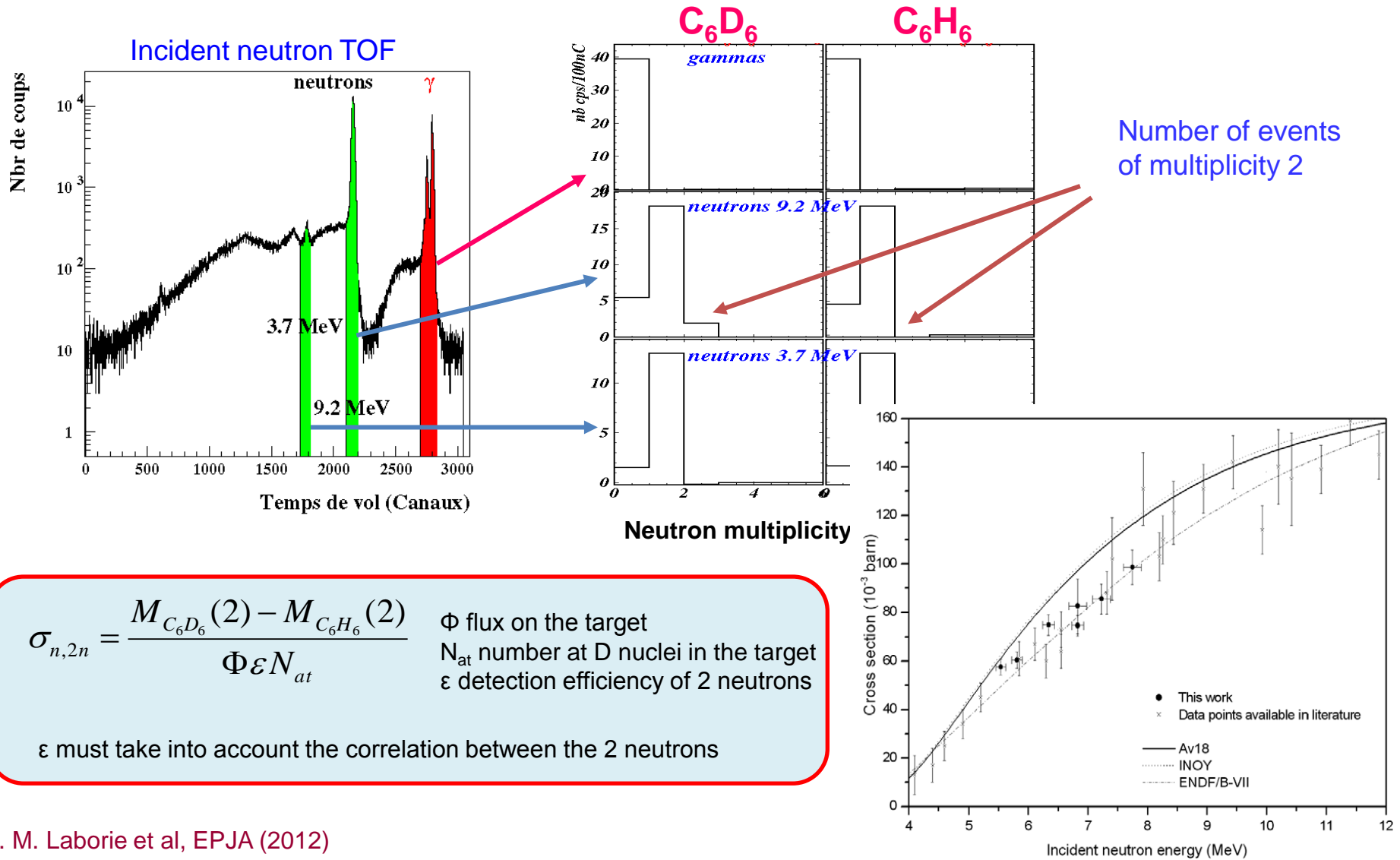


- Three bodies system in the exit channel
- The emission of the 2 neutrons cannot be treated like evaporated neutrons
- Theoretical model based on the resolution of the Faddeev equations (J. Carbonell et B. Morillon)

- Measurement of the 2 neutrons emitted -> Neutron ball
- Active target made of C_6D_6 :
 - reaction tagged by the recoil of the proton
 - incident neutron energy measured by time of flight
- Measurement with C_6H_6 target to subtract the carbon contribution



Cross-section measurement of the D(n,2n) reaction (2)

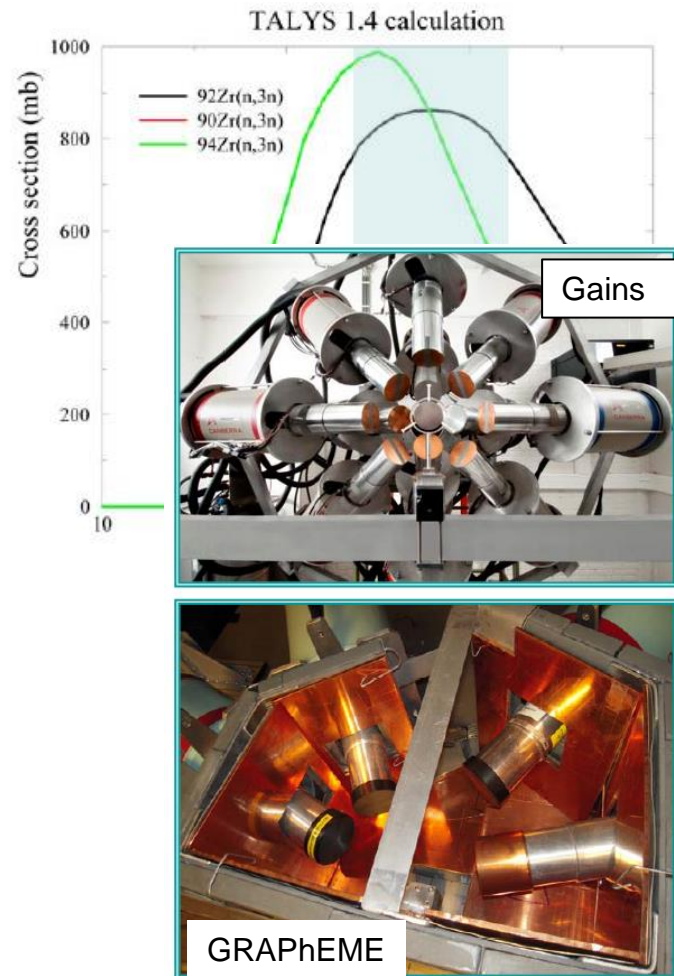
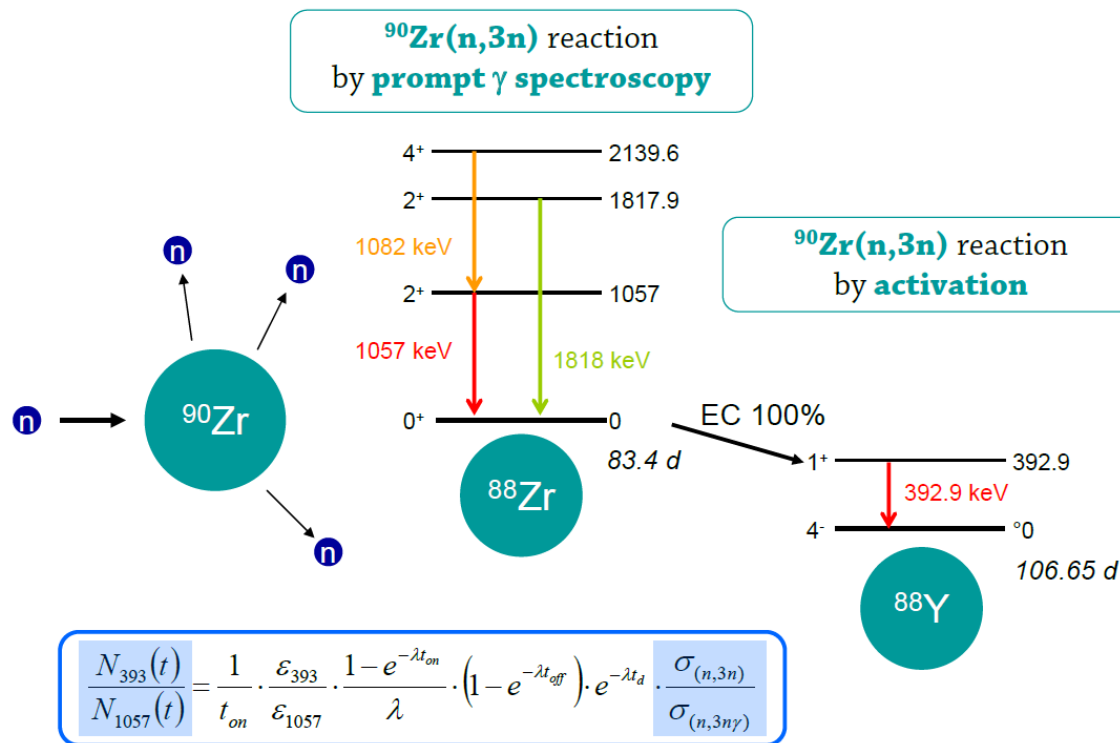


J. M. Laborie et al, EPJA (2012)

(n,3n) cross section measurement by two techniques

The (n,xny) cross-section measurements are used to extract (n,xn) cross section-> need of theoretical model

At NFS the $^{90}\text{Zr}(n,3n)$ cross-section can be measured by prompt γ spectroscopy and by activation technique **at the same time**
 →validation of the theoretical models



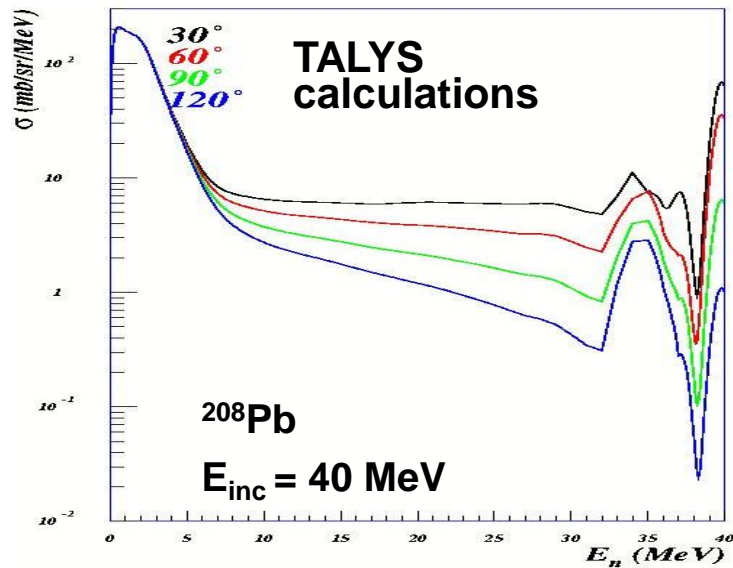
Quasi-mono-energetic neutrons from 26 to 32 MeV

M. Kerveno et al., Letter of Intents for NFS facility

Study of pre-equilibrium process in (n,xn) reaction

Measurement of (n,xn) double differential cross section in coincidence with neutron multiplicity.

Validation of pre-equilibrium models



Method :

- measurement of energy and angle of one neutron
- count of the (x-1) neutrons emitted simultaneously.

Experimental set-up :

- NE213 detectors
- CARMEN detector



Beam request:

- Quasi-monokinetic beam
- Pulsed
- Well collimated

X. Ledoux et al., Letter of Intents for NFS facility

Summary

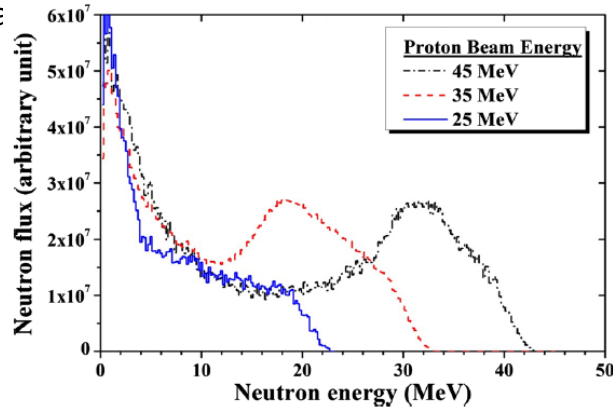
- n, xn reactions play an important role in the 1 MeV – 50 MeV range
 - Reactor
 - Waste production in high neutron flux
 - Accurate library of nuclear data
- Several techniques exist
 - Activation
 - $n, xn\gamma$ reactions
 - Direct outgoing neutron measurement
- All the techniques cannot be used in all cases
 - Specific detection set-up
 - Specific neutron facilities

Yttrium

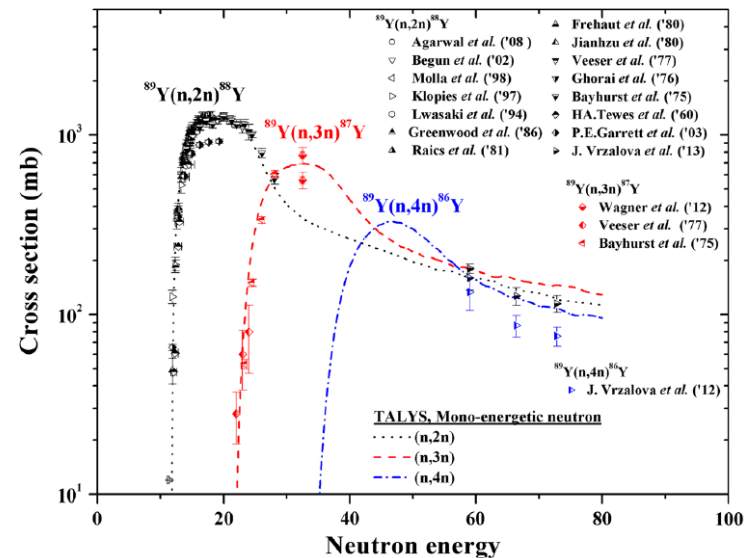
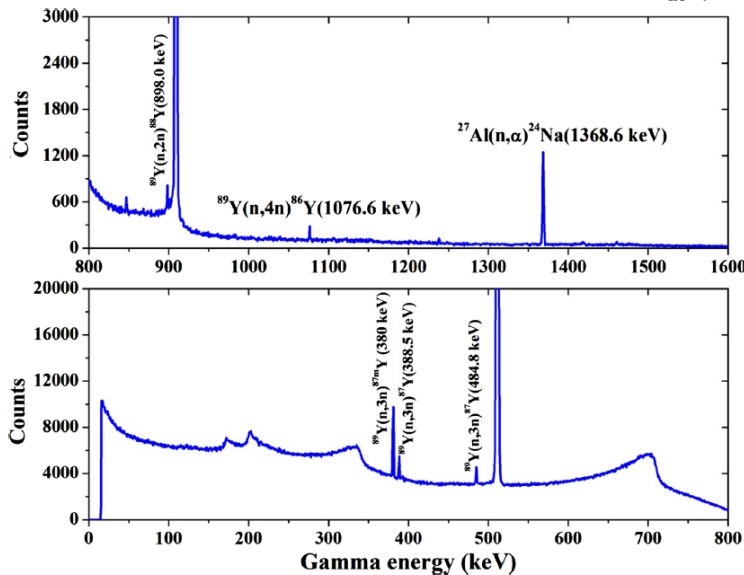
Thus the (n, xn) reaction of ^{89}Y is important, when the superconductor is used in the neutron field of higher energy such as in the fast reactor and accelerated driven sub-critical system (ADSs).

Measurement of cross-sections for $^{89}\text{Y}(n, xn)$ reaction at average neutron energies of 15–36 MeV

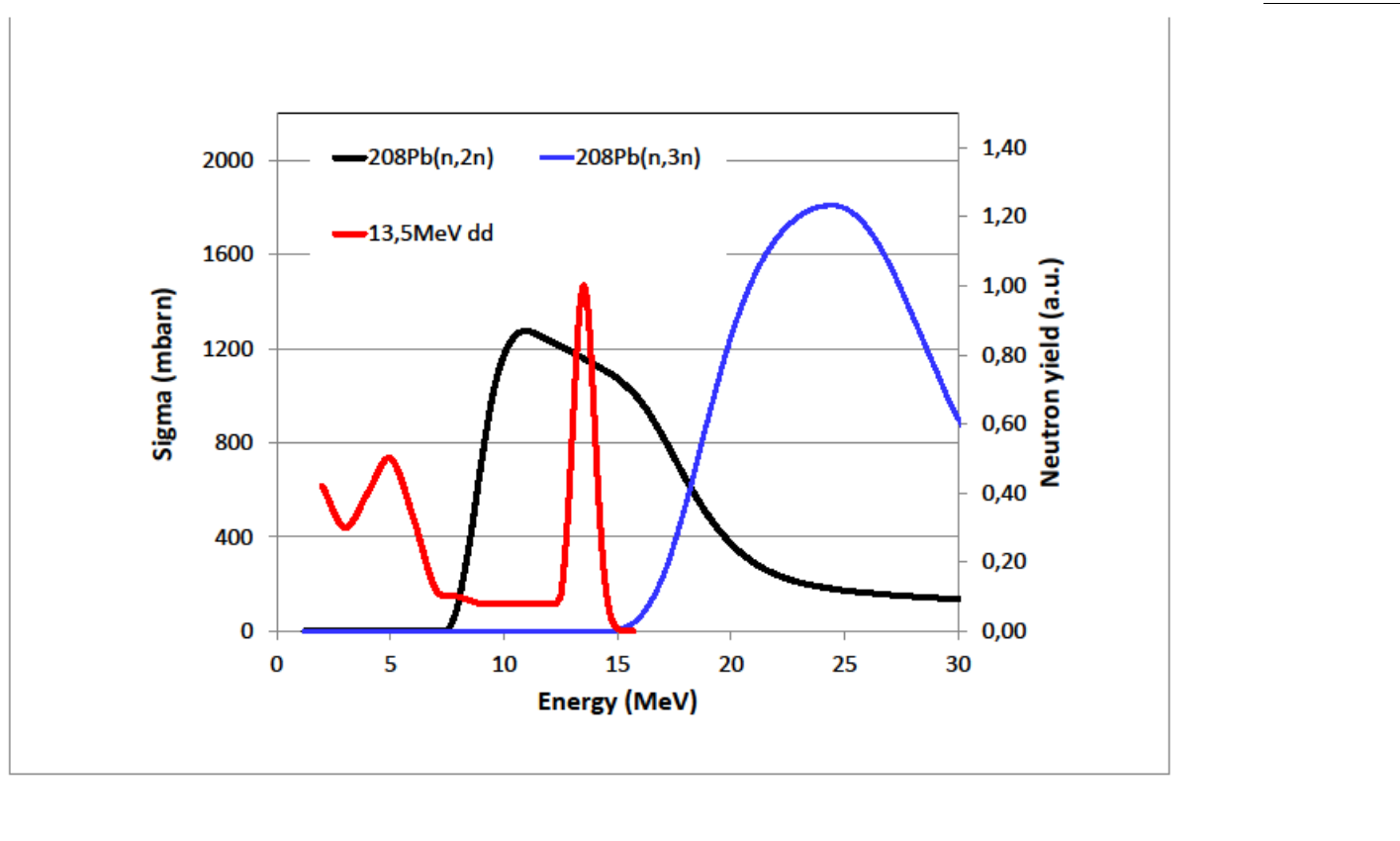
Monitoring : active



$$\langle \sigma \rangle = \frac{N_{obs}(CL/LT)\lambda}{n \Phi_n I_\gamma \varepsilon (1 - e^{-\lambda T_i}) e^{-\lambda T_c} (1 - e^{-\lambda CL})}$$



(n,2n) and (n,3n) measurements



D(d,n) ^3He produces purely mono-energetic neutrons up to 7 MeV
But The low energy component is below the (n,2n) threshold
D(d,n) ^3He can be used up 10 MeV

Numerical application

Measurement on Carbon sample

Flux : Φ (n.cm⁻².s⁻¹)

Differential cross section : $d\sigma/d\Omega$ (barn.sr⁻¹)

Intrinsic efficiency : 20%

Sample : A=12, $\Phi=3$ cm, h=3cm, m=15g

$$N_{\text{det}} (s^{-1}) = \Phi \left(\frac{m}{A} N_{\text{avo}} \right) \epsilon \frac{d\sigma}{d\Omega} d\Omega$$

$$\Phi = 10^6 \text{ n.cm}^{-2}.\text{s}^{-1}$$

$$d\sigma/d\Omega = 0,001 \text{ barn.sr}^{-1}$$

$$N_{\text{det}} = 0,02 \text{ count.s}^{-1}$$

