

Kinetic Memory

Cells -memorize the history of environmental inputs

(1) classic example

When the paramecium is placed in a culture environment with a temperature gradient, it moves toward its original temperature position. Internally, an adaptive process occurs. However, if exposed to a new temperature for a longer period of time, it will remember that temperature as the temperature to which it should return. (cf Fumio Osawa), in Biophysics of Complex Systems). In other words, the adaptation of adaptation process can be regarded as memory.

- Yeast memorizes internal states over 40 generations (Mark Segal)
- Epigenetically Heritable states of Fly (*D. melanogaster*), Stem, Braun, and Yoav Soen
- Unicellular organism: cellular states transferred to next generation. (eg protein abundances)

Still, the information on abundance is reduced by cell division, after 10 division, relaxes 2^{-10}
 $\sim 1/1000$

- * * **epigenetic**—— ‘magic word?’

Methylation, histon modification etc...

Still how such molecular changes are maintained over generations?

Other long-term sustainment in cells

- Dormant state、 spore, seed

Almost closed, but “living state” sustained over years – nonequilibrium states?

Glass?

* * physical viscosity increased, molecules cannot move/react?

Water → trehalose

+ an alternative view before it (-> chemical net glass ?

Biological System:

*Adapt to variety of conditions while preserving its behavior ('homeostasis')

- **Memory** --tendency to stick to a certain state even after the change in external condition

→ Atypical behavior in physico-chemical system

System-level property of catalytic reactions???

Core idea: catalytic reactions → reaction-rate, thus, timescale, depends on catalyst concentration

Autonomous regulation in the concentration of catalysts → autonomous control of state → homeostasis and memory

Genuine Slow relaxation process in catalytic reaction network

external nonequilibrium but internal equilibrium?

inside → different class of nonequilibrium.

Enzyme --- autonomous regulation of time scale
then again sustainment of non-equilibrium
condition distinct from outside

Out-of-equilibrium: usually assumed in models
of cells (cf dissipative structure)

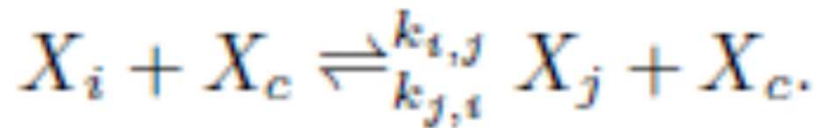
Somehow sustained autonomously? At least
somehow the system is kept off from easily
falling to equilibrium?

Long-term sustainment of non-equilibrium state

Proposal of 'Chemical Reaction Net Glass'

Simple catalytic reaction network **A.Awazu PRE 2009**

CLOSED SYSTEM



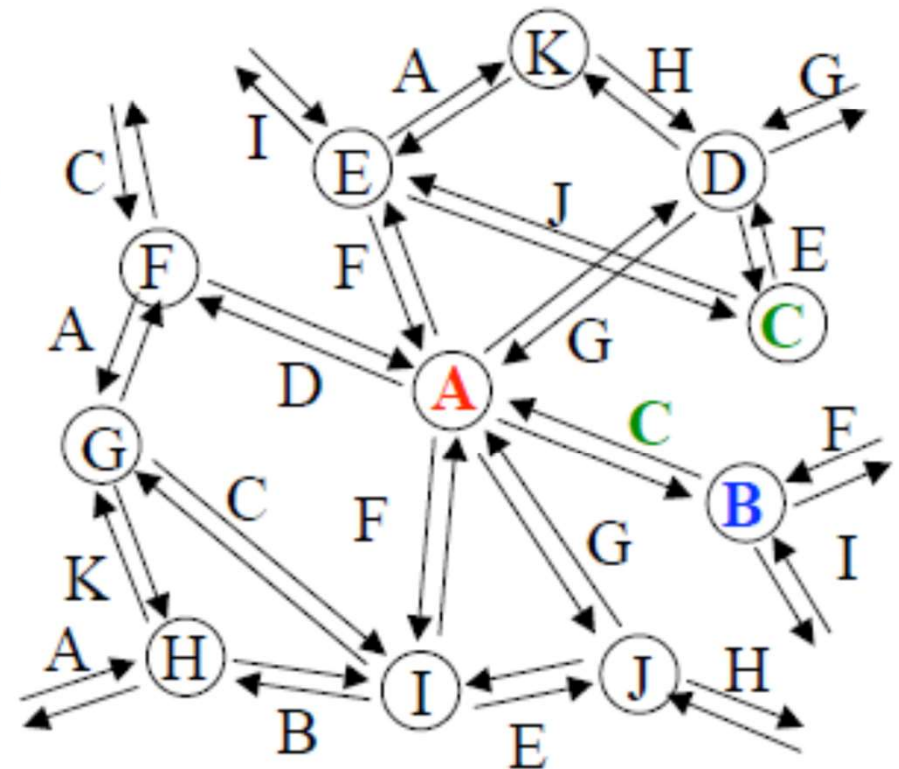
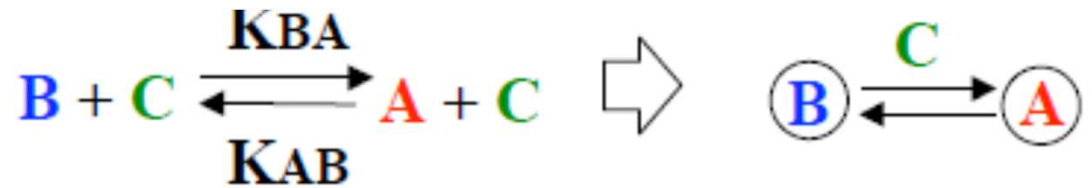
$$\dot{x}_i = \sum_{j,c} \text{Con}(i,j;c) x_c (k_{j,i} x_j - k_{i,j} x_i),$$

$$k_{i,j}/k_{j,i} = \exp(-\beta(E_j - E_i))$$

$$k_{i,j} = \min\{1, \exp(-\beta(E_j - E_i))\}$$

E_i distributed : stnd deviation ε

RELEVANT parameter $\beta\varepsilon$



Equilibrium distribution $\exp(-\beta E_i)$: ($\leftarrow$ detailed balance)

Relaxation process: Initial : $\beta=0$ (high temp) for all species, i.e., equal probability for all chemical species.

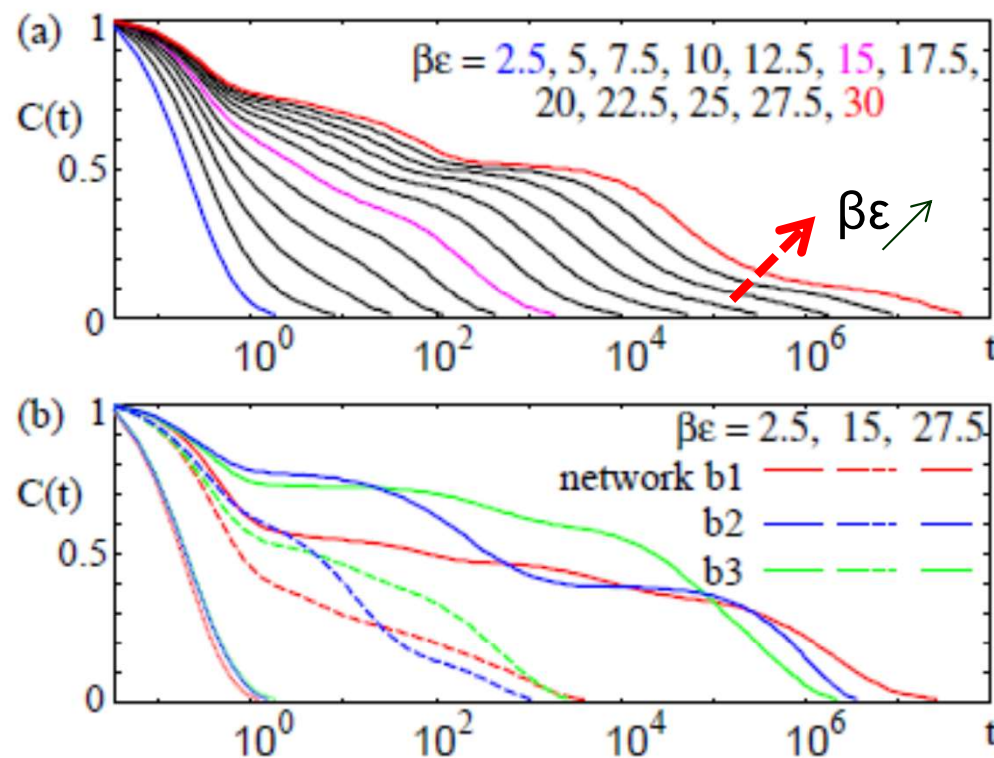


FIG. 1: (a)(b) Relaxation time course for four sets of networks ($M = 24, K = 8$) for several β .

$$C(t) = \frac{\langle (\vec{X}(t) - \vec{X}^{eq})(\vec{X}(0) - \vec{X}^{eq}) \rangle}{\langle (\vec{X}(0) - \vec{X}^{eq})^2 \rangle}$$

Deviation from equilibrium

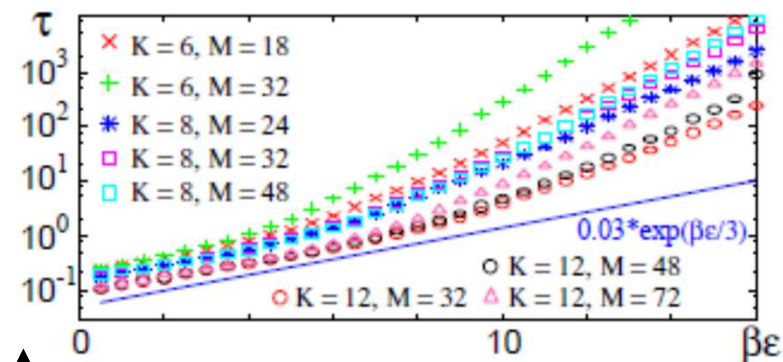


FIG. 2: Relaxation time as a function of β for the sample reaction networks in Fig. 1(a)(b).

$$\tau = \langle \int_0^\infty |C(t)| dt \rangle$$

Two salient features in relaxation analogous to 'glass'

- (1) Log-t slow relaxation (rather than exponential)
- (2) Existence of plateaus

Why Log-t slow relaxation?

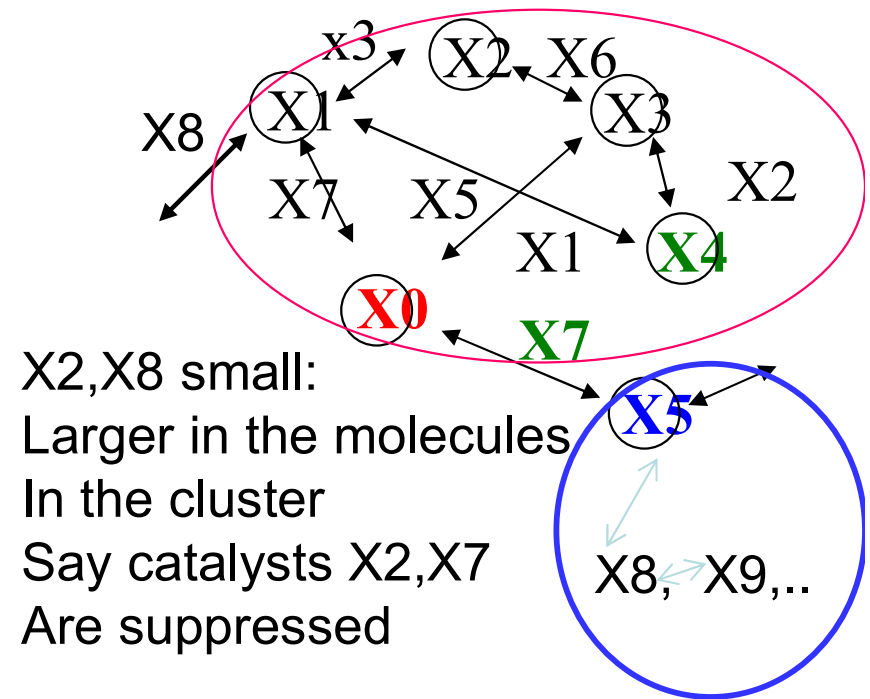
due to energy distribution, the relaxation time
(kinetic coefficients $\exp(-\beta E)$) distribute extensively

$$C(t) \sim \int_0^\infty D(E) a(E) \exp(-e^{-\beta E} t) dE$$

by $u = \exp(-\beta E)t, \quad (1/\beta) \int_{te^{-\beta \epsilon}}^t (1/u) e^{-u} du \rightarrow \log(t)$

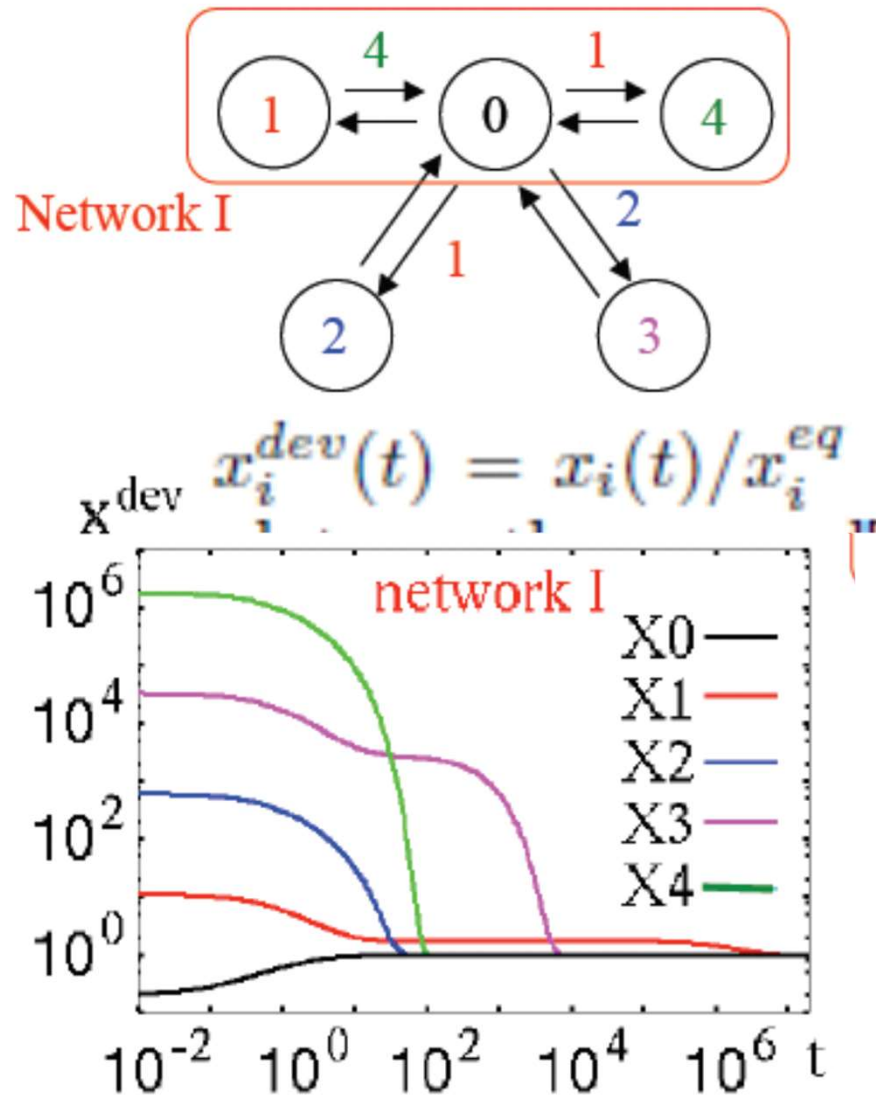
• Why plateaus?

- Local equilibrium within cluster
- Equilibrated with other clusters is suppressed by deficiency of catalytic molecules
- negative-correlation with abundances versus catalysts
- $\Delta X \uparrow \rightarrow \Delta J_{out} \downarrow ?$



General in catalytic networks $\rightarrow$ 'Chemical Net Glass'

A simple example



1 catalyzes decrease of 4 ;
 4 catalyzes decrease of 1
 → mutual competition
 for relaxation

but 4 starts to decrease
 faster as $\exp(-\beta E_4)$ is
 smaller

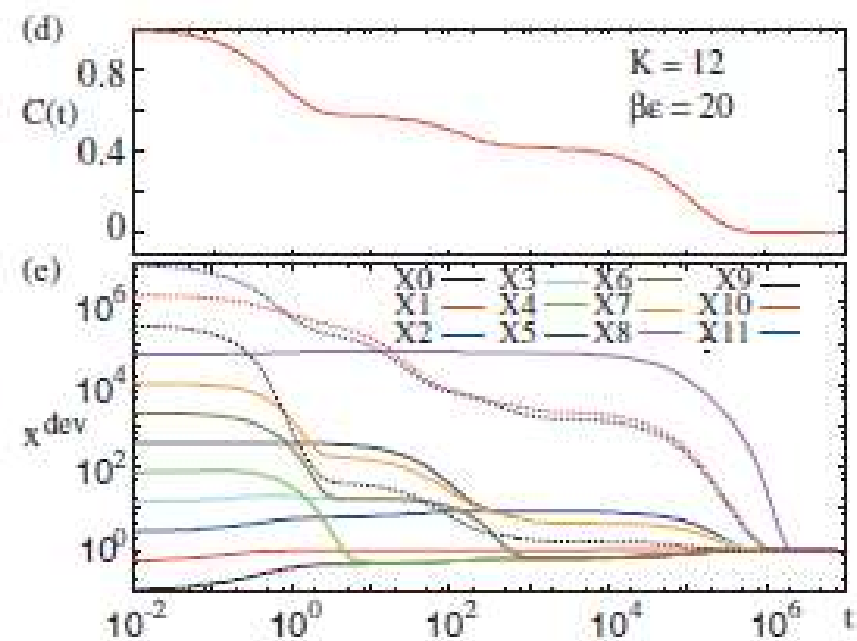
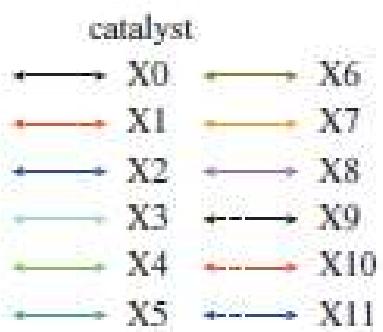
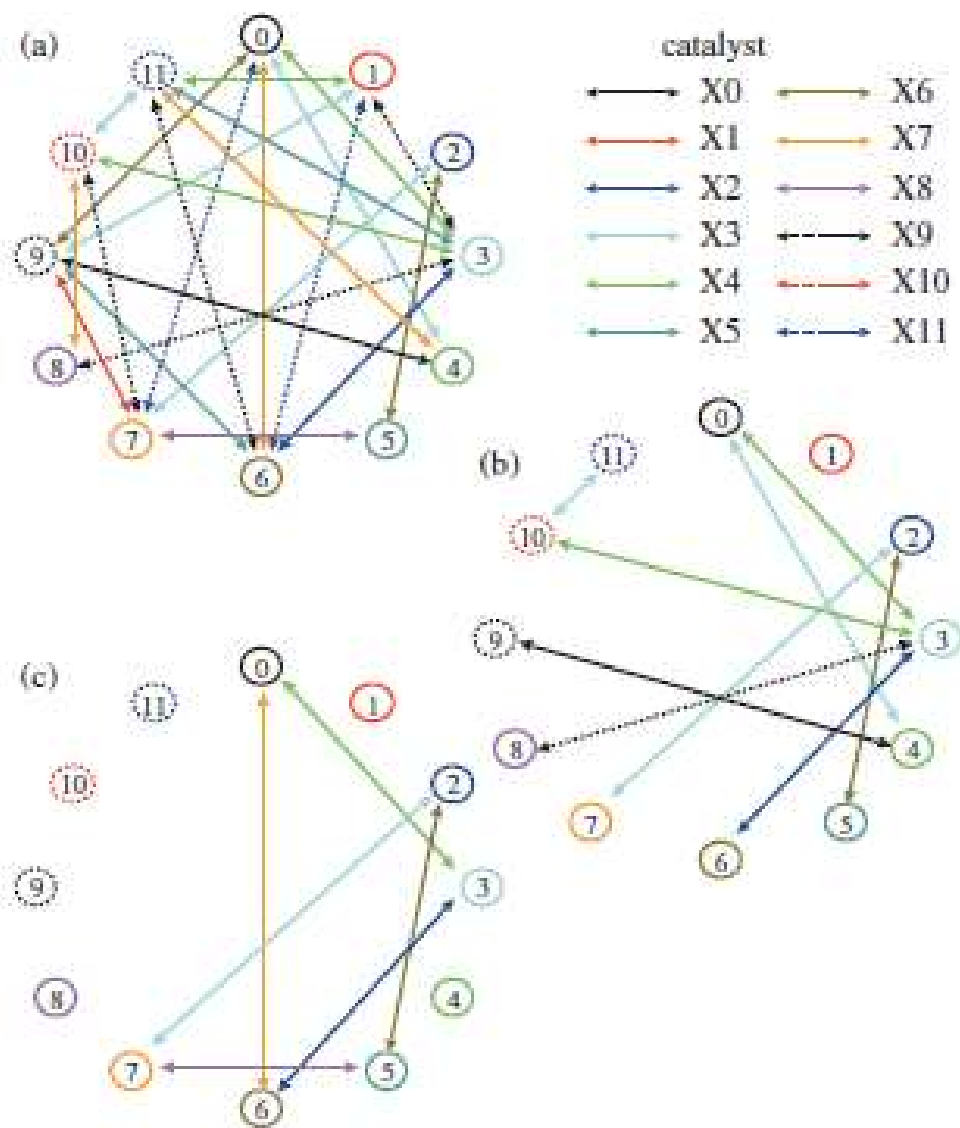
Then relaxation of 1 is
 further hindered

1 is not easily equilibrated
 1—4 negative correlation

$$E_0 < E_1 < E_2 < E_3 < E_4$$

→ x_1, x_2, x_3, x_4 decreases to increase x_0

$$X_i \sim \exp(-\beta E_i)$$



Relevance of autonomous
regulation of enzyme abundances
to long-term dynamics

A proposal for kinetic memory
based on enzyme-limited
competition

Tetsuhiro S. Hatakeyama & KK
PLoS Comp Biol 2014

Cellular memory

Epigenetic Memory --- over dozens of generations
(yeast, E Coli)

Memorization of cultured temperature
(Oosawa, Nakaoka)

Origin? Molecular? How preserved?

Standard Picture --- multiple attractors --OK?

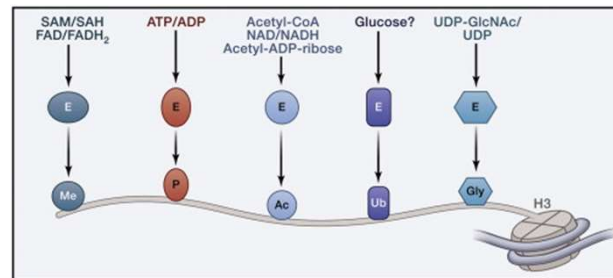
1) continuous states are not memorized

2) dynamic processing for stimuli?

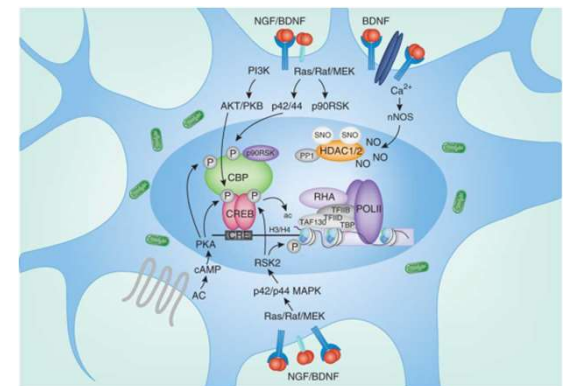
3) storage needs costs,

Phosphorylation of signaling molecule

Chromatin modifications



Kotada S, et al., Cell (2012)



Riccio A, Nat. Neurosci. (2010)

An Alternative: Proposal of Kinetic memory **not** stored at attractors, stored in a relaxation process

- Keeping memory for a long time
 - Slow relaxation dynamics
- Memorize history of continuous environment
- No cost, simple

← Autonomous change in time scale by
Enzyme-limited Competition

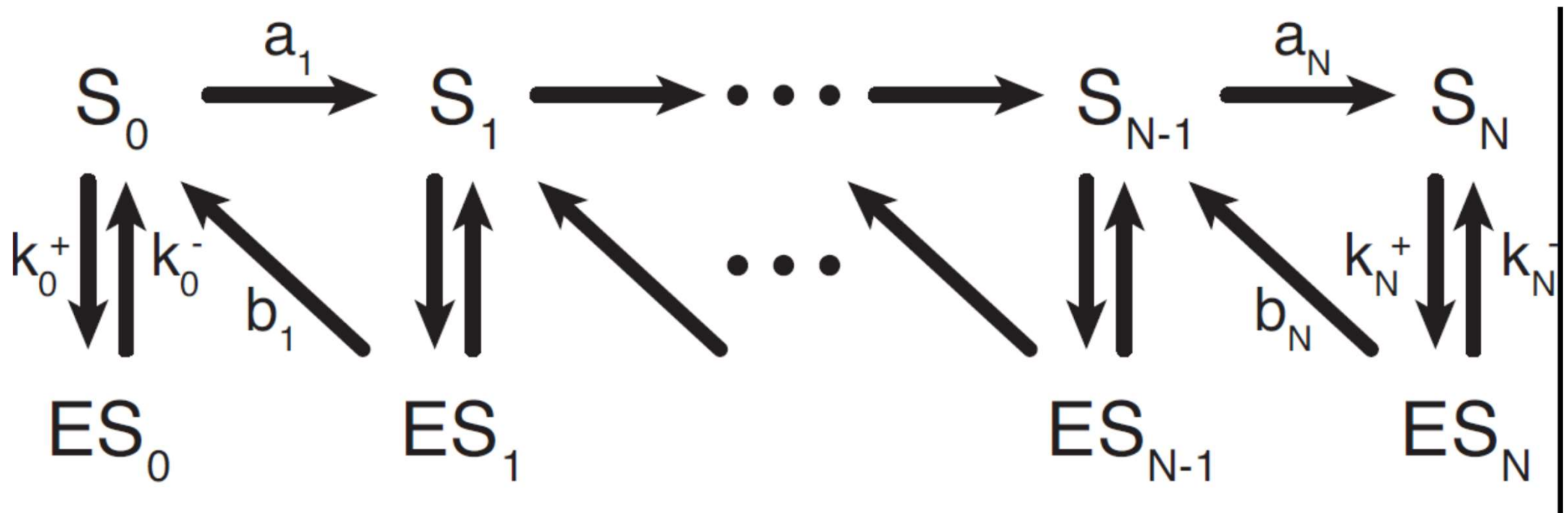
Kinetic memory by ELC?

Hatakeyama, KK

Consider adaptation dynamics +ELC, instead of oscillation

E : Enzyme or Cofactor for site modification
(e.g., methylation etc)

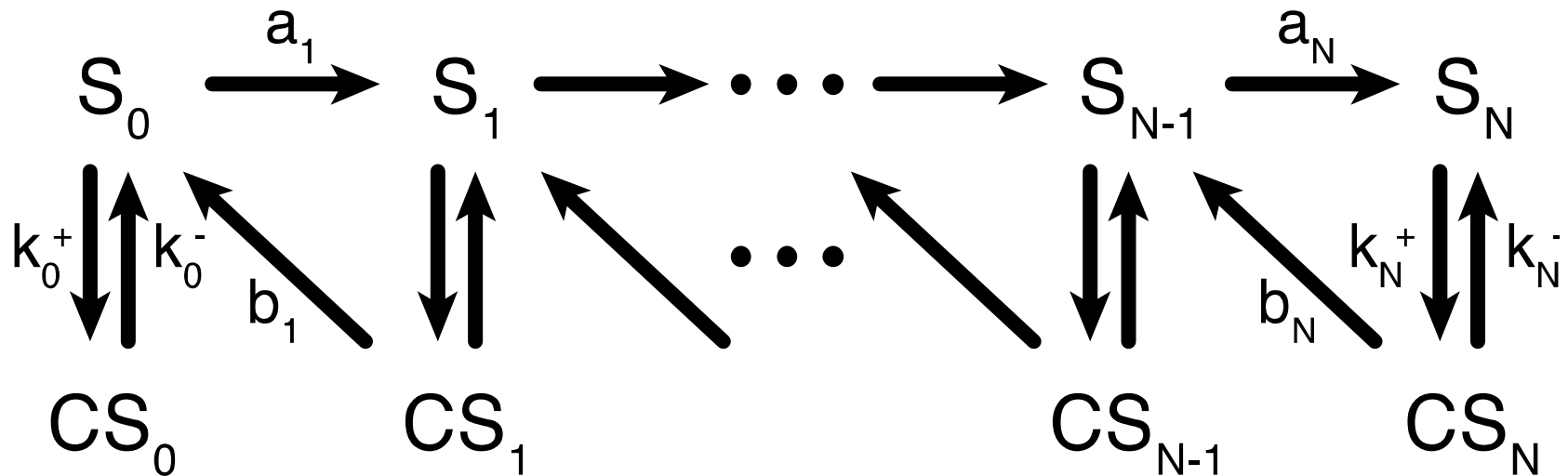
Each substrate competes for E



S_i : S form substrate with i modified sites

ES_i : S form substrate binding cofactor

Chained modification model



Stimulus $a_i = a(t)$
:

$$K_i = k_i^- / k_i^+ = K_o \times \gamma^i \quad \text{Heterogeneity of affinity}$$

Chained modification model

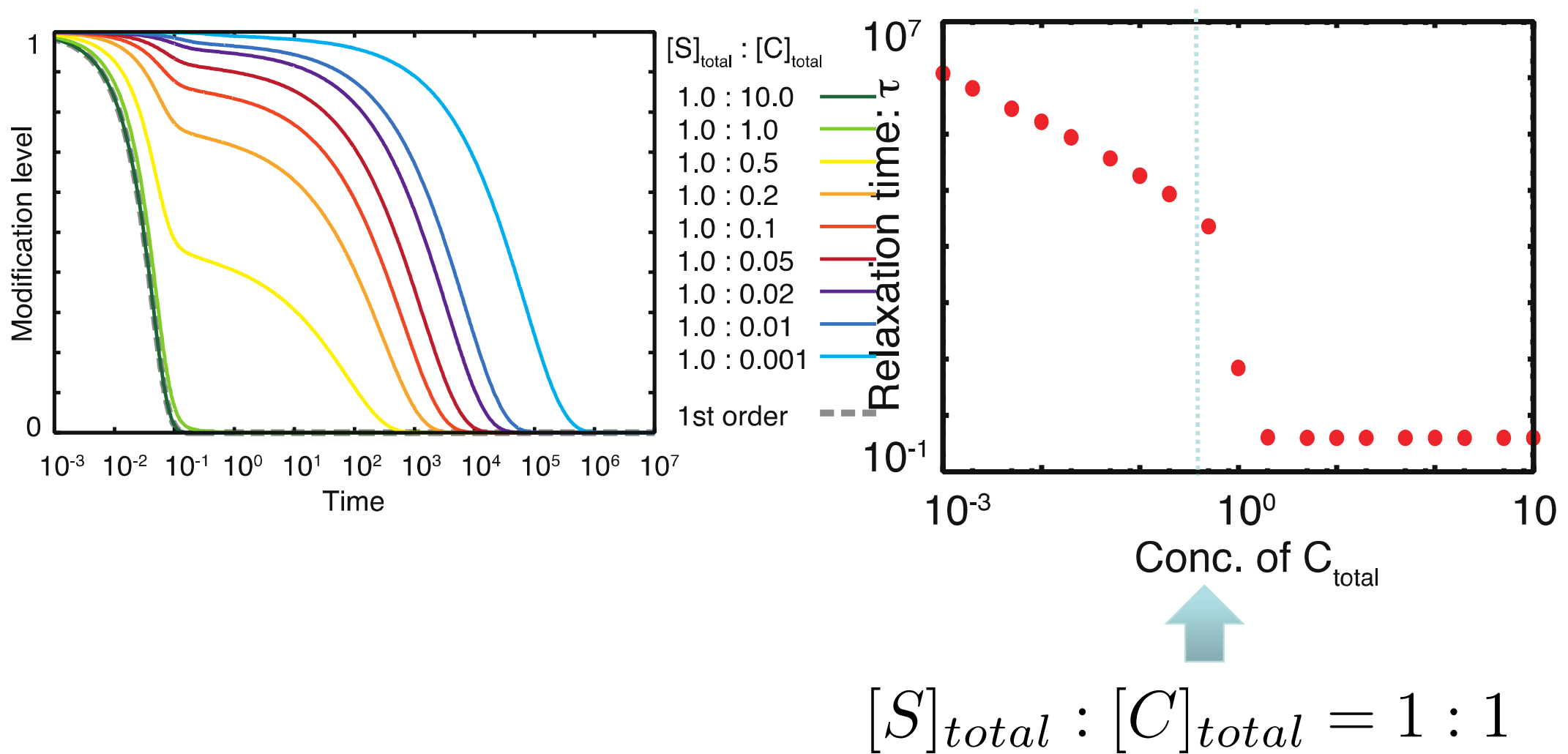
$$\begin{aligned} [\dot{S}_i] = & -a_{i+1}[S_i] + b_{i+1} \frac{[C]_{free}[S_{i+1}]}{K_{i+1} + [C]_{free}} \\ & + a_i[S_{i-1}] - b_i \frac{[C]_{free}[S_i]}{K_i + [C]_{free}} \end{aligned}$$

$$[C]_{total} = \sum_{i=0}^N \frac{[C]_{free}[S_i]}{K_i + [C]_{free}} + [C]_{free} \text{Enzyme competition}$$

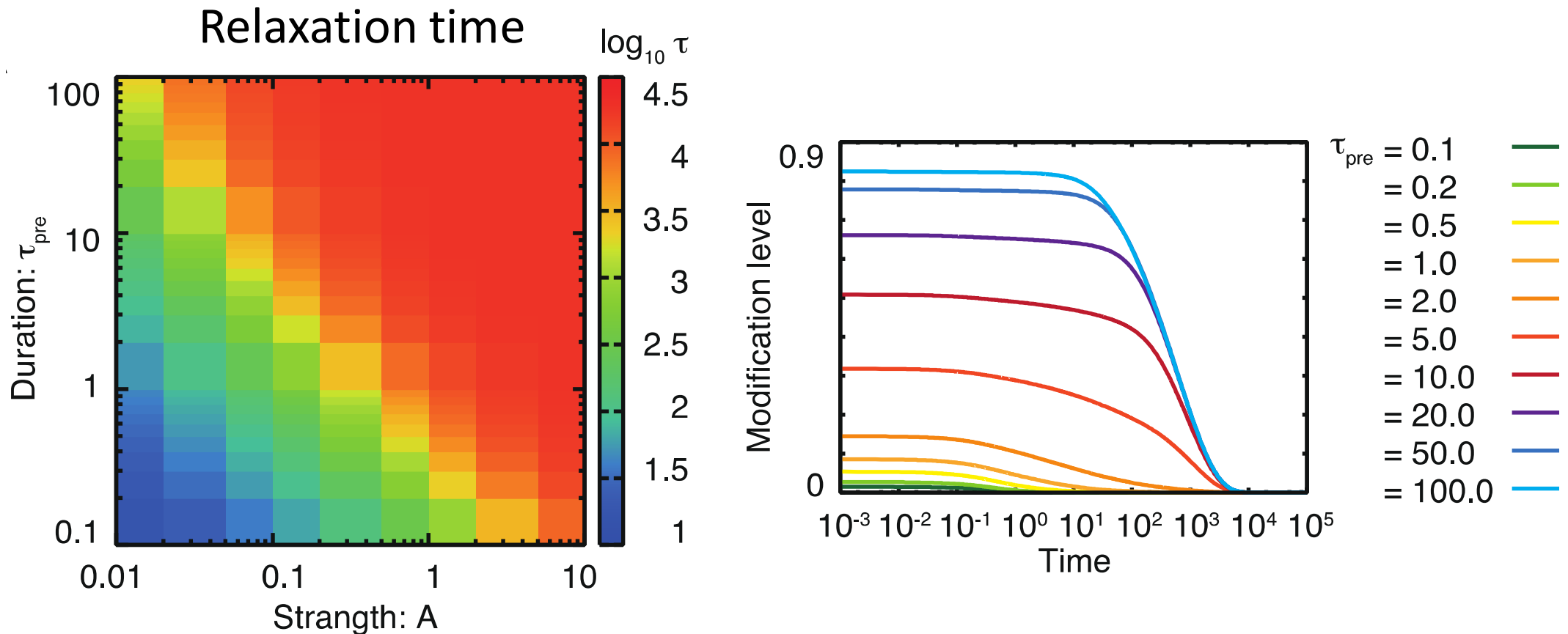
$$K_i = k_i^- / k_i^+ = K_0 \times \gamma^i$$

Memory maintenance and erasure

Maintenance erasure
Slow log relaxation fast exp relaxation

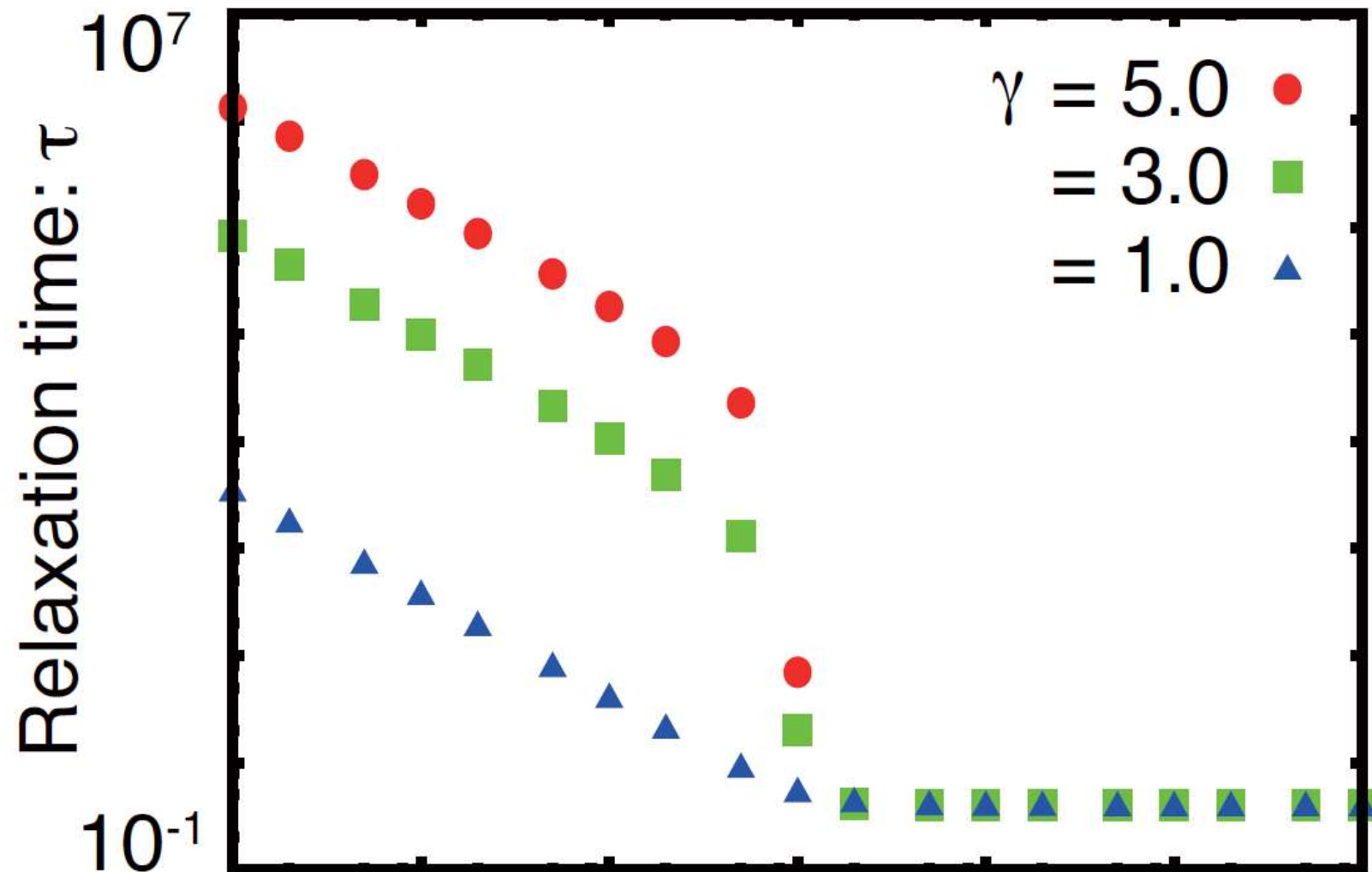


Continuous Memory

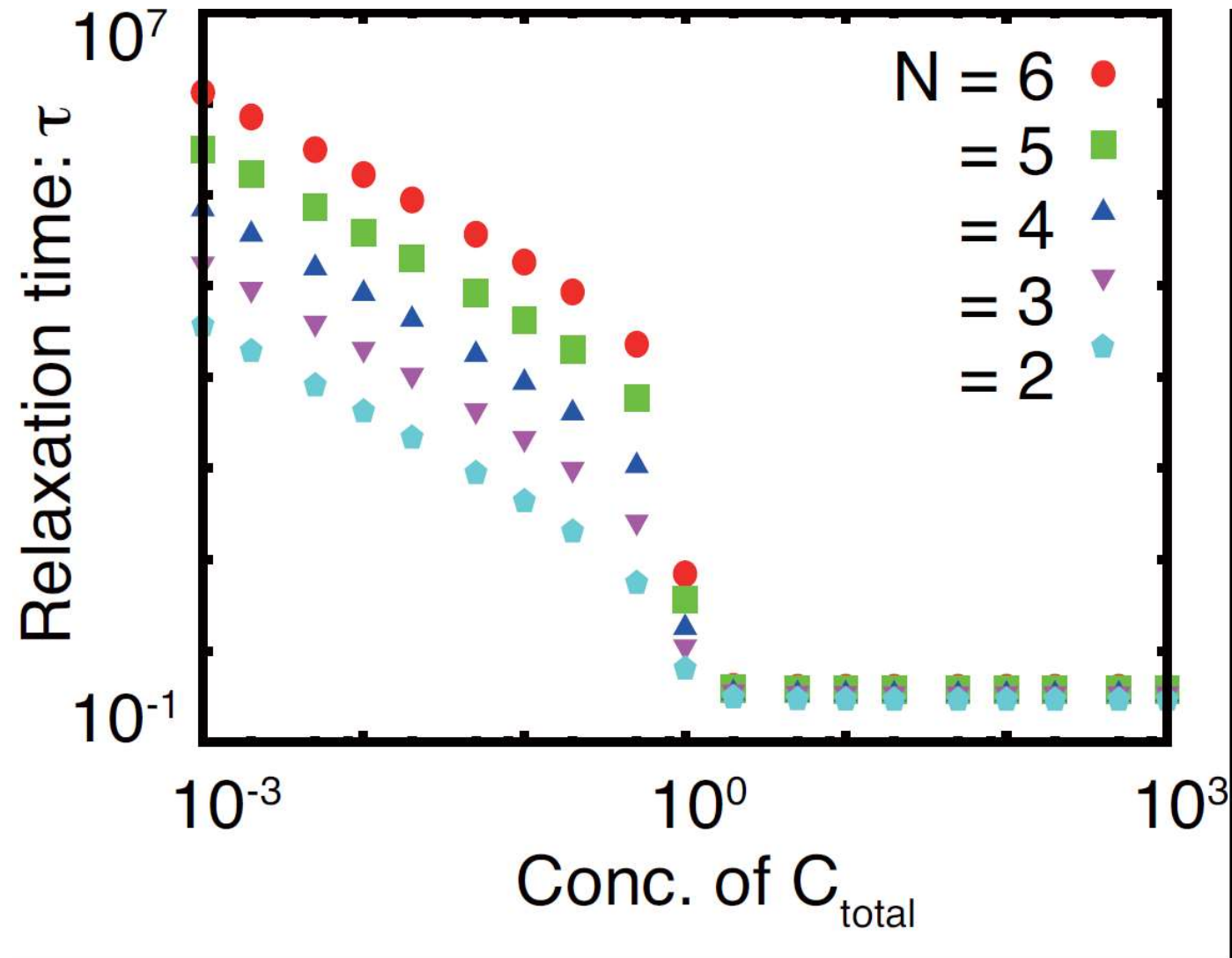


Modification level and relaxation time continuously changes with the stimulus strength and lenbth

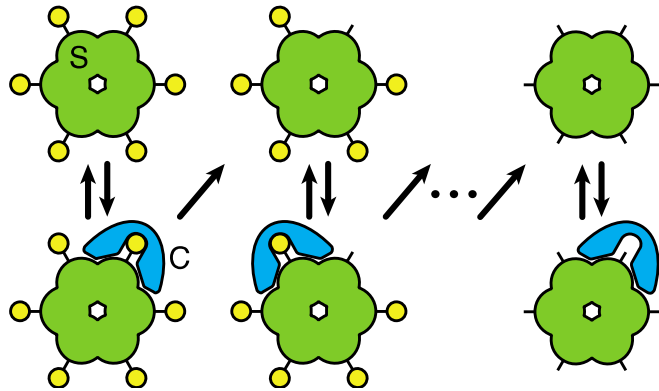
Condition: affinity depends on sites



Enhanced as the number of
sites is larger

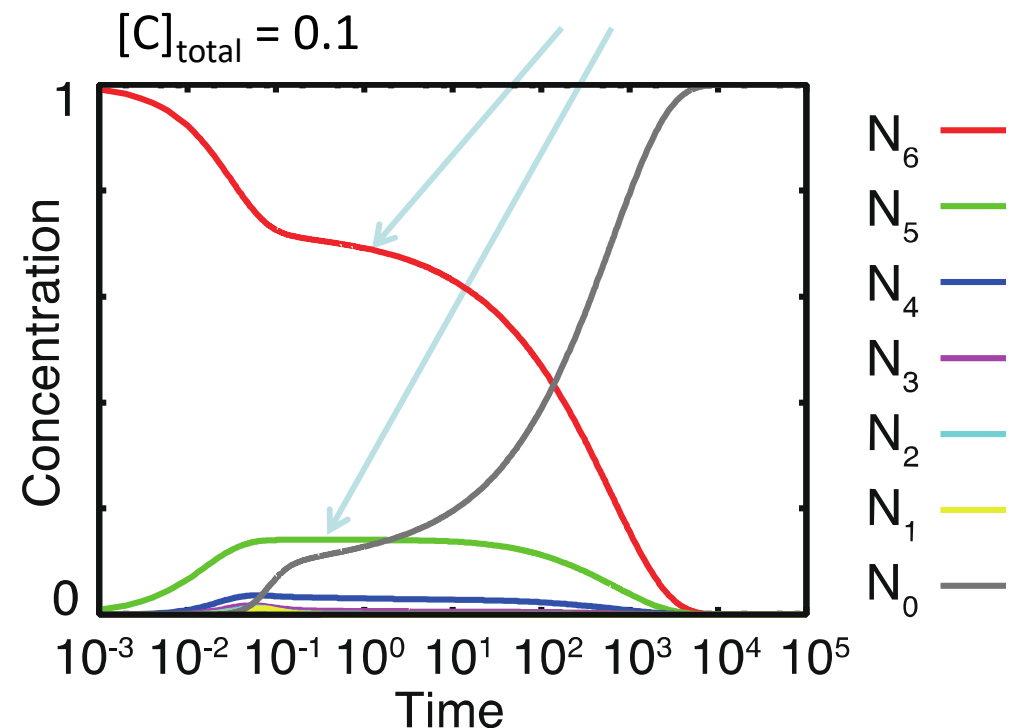
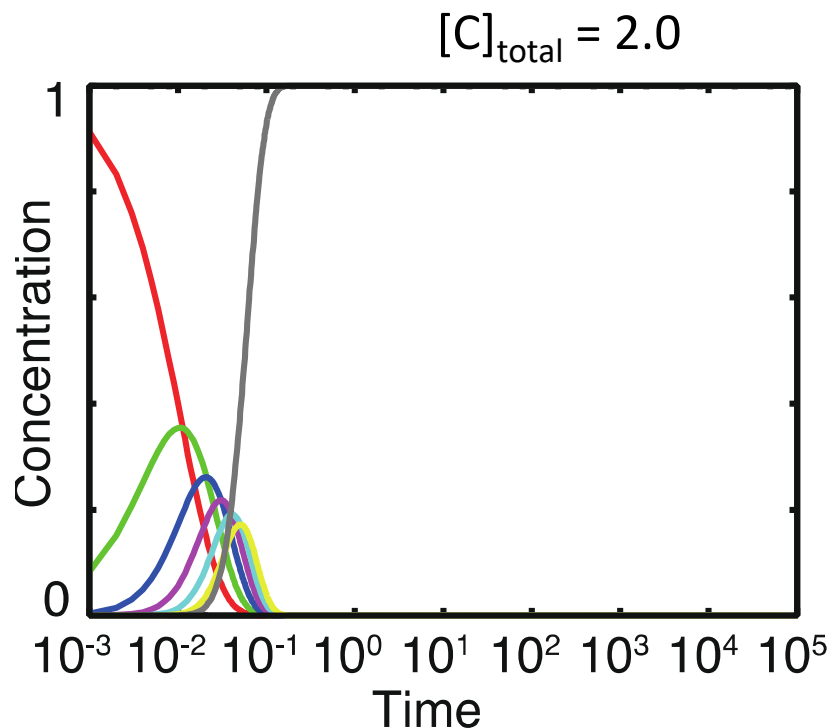


How Slow relaxation occurs



S_{i-1} has higher affinity than S_i
 $\rightarrow S_i$ cannot get the enzyme successively

For relaxation of each component
 There emerges a plateau



Enzyme limit competition is a key

Requirements for kinetic memory

- Enzyme-limited competition by multiple modification sites
- Different affinity among substrate states

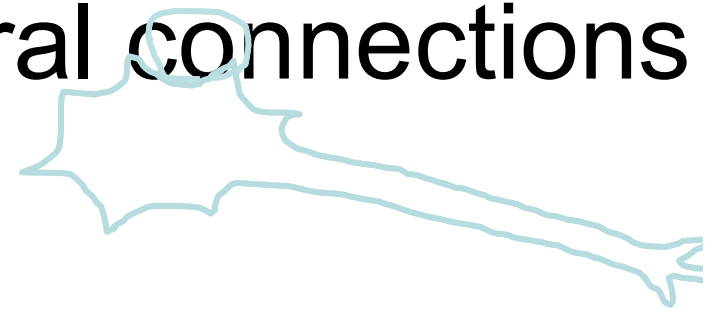
–Leading to glassy relaxation

By decreasing the concentration of catalysts, current state is memorized, while, memory is erased by increasing the concentration

Relevance of ‘kinetic memory’

Long term potentiation in neural connections

Molecules concerning LTP

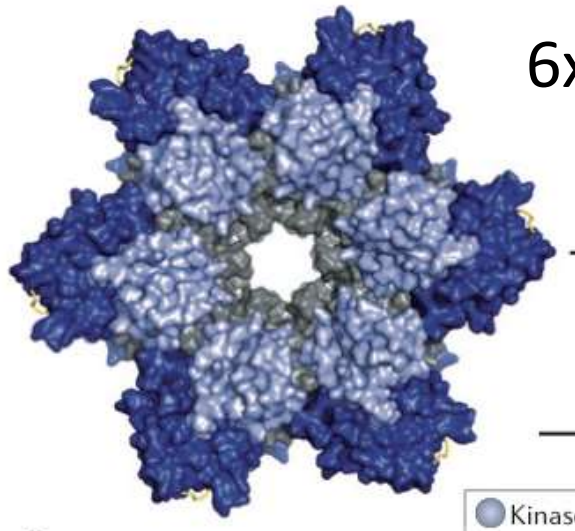


- Early LTP (without protein synthesis)
 - Ca^{2+} /calmodulin-dependent kinase II (CaMKII)
 - Protein Kinase C (PKC)
- Late LTP (with protein synthesis)
 - cAMP-responsive element-binding protein (CREB)

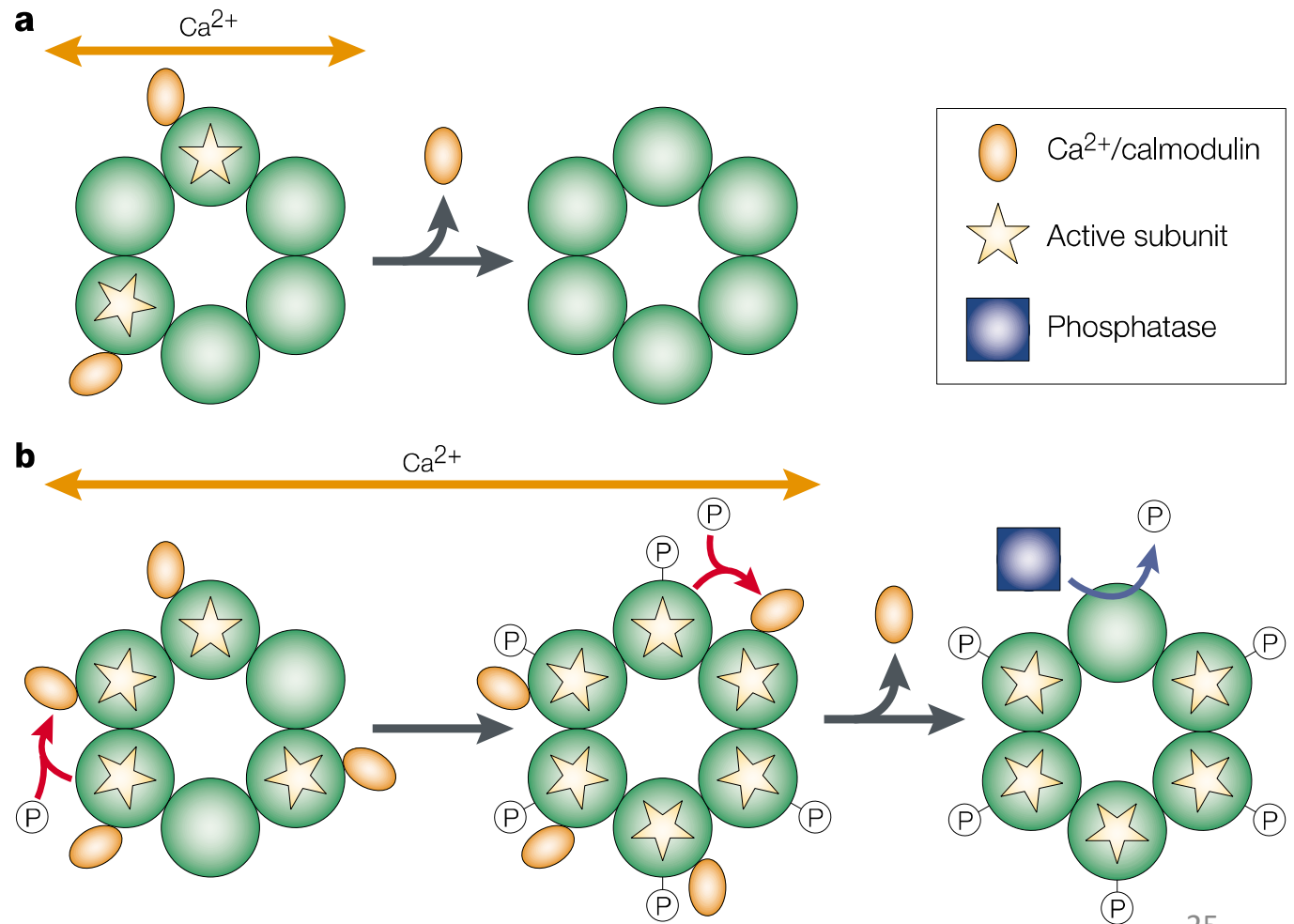
With multiple phosphorylation sites
(eg, CaMKII CREB)

Long-term phosphorylation needed

CaMKII



6x2 mer



Lisman et al.,
Nat Rev Neurosci (2012)

Lisman et al., Nat Rev Neurosci (2002)

Attractor memory: limitation?

- Memory in multiple-attractor system
 - requires a number of modification sites
(e.g., memory $\propto n$ or less)
 - Need to isolated each site (then read/write has difficulty?)
 - Erasure needs cost?
 - or need to design complex network structure
 - hard to store the memories against various stimuli
- Some form of 'Kinetic memory '
preferable to adapt to a various dynamic stimuli?
Also low cost to read/write/ erase?

Relevance of continuous, kinetic memory?

Flexibility?

Controllability, continuous

by inputs/ enzyme abundances

continuous dependence on inputs

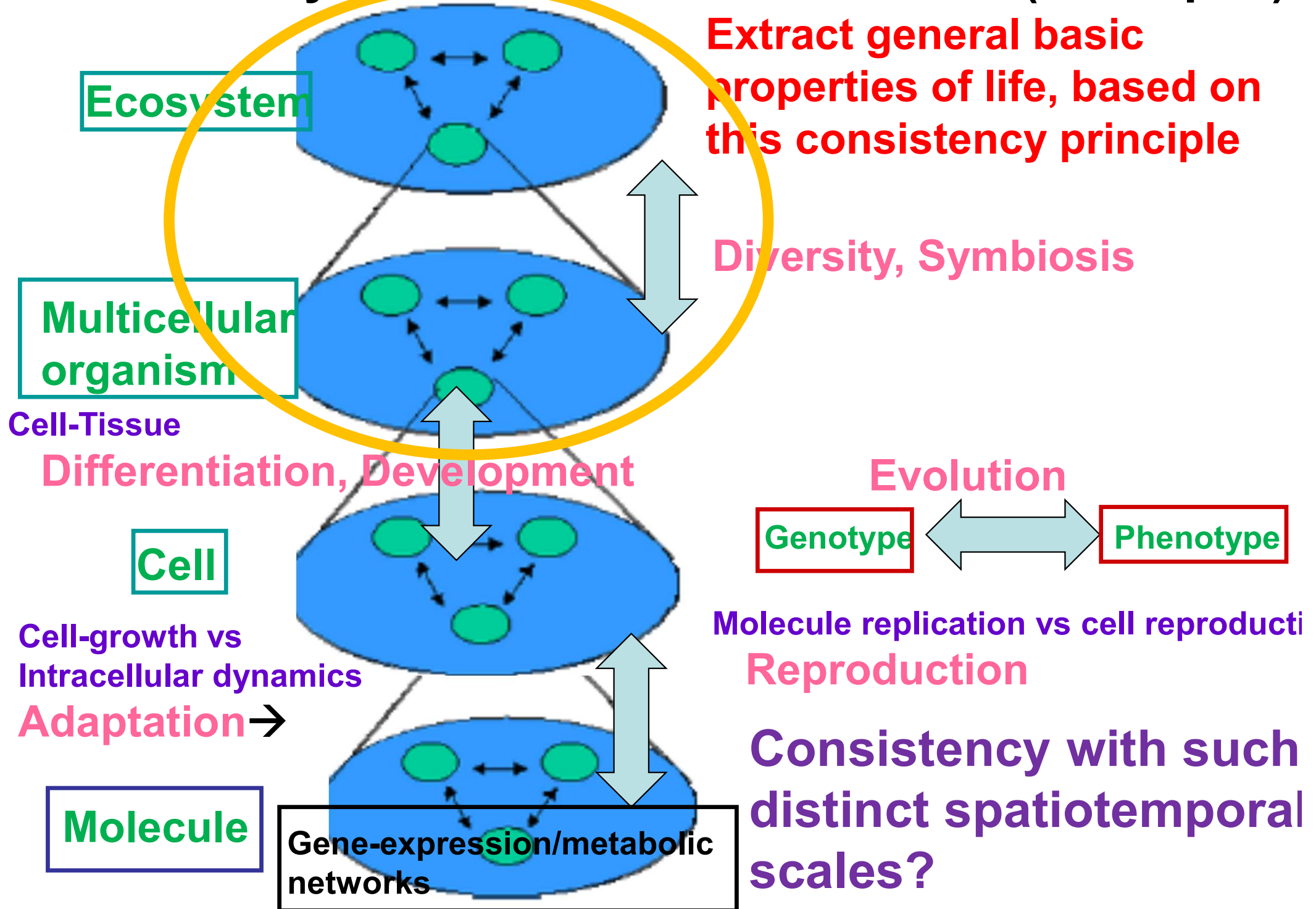
→ LTP/LDP, Hebb/antiHebb

Erasable without thermodynamic costs?

- Processing of temporal information
- Memory in Synapse (continuous /by number ?)
metaplasticity?
- Epigenetic Memory on DNA?
(copy? Feedback?)

- OtherTopics that I have no time to talk this time...

Consistency between hierarchical levels (+collapse)



○ Ecosystem: further hierarchy -- Theory for interaction-induced diversity

traditional studies -- population dynamics

In reality (eg microbial ecosystem such as biofilm)

intracellular dynamics + interaction

-- multi-level dynamics (eg Yamagishi Saito, KK PLoSCB2021)

Growth rate μ -- as a function of

intra-cellular components $\{X^*\}$ as $\mu = g(\{X_j\})$

Balance condition among types

KK,2015

$$\frac{dX_i(\alpha)}{dt} = F_i^\alpha(\{X_j(\alpha)\}) + H_i([X_i(\alpha), \rho^\beta]) - \mu^\alpha$$

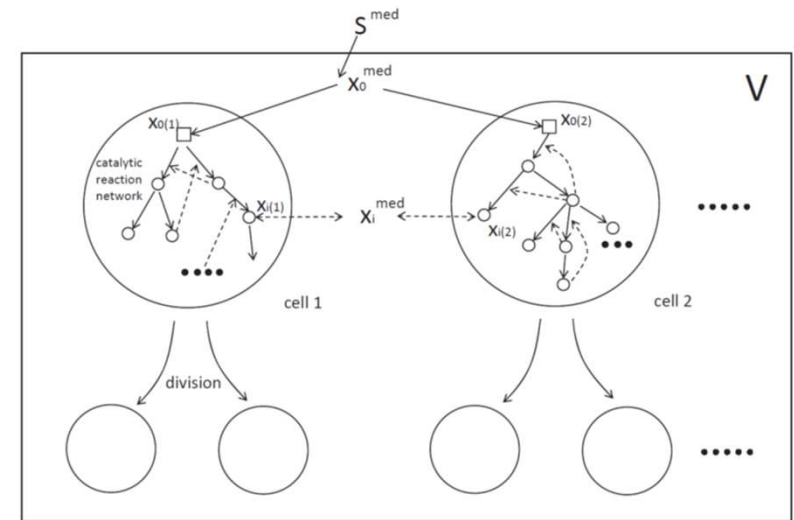
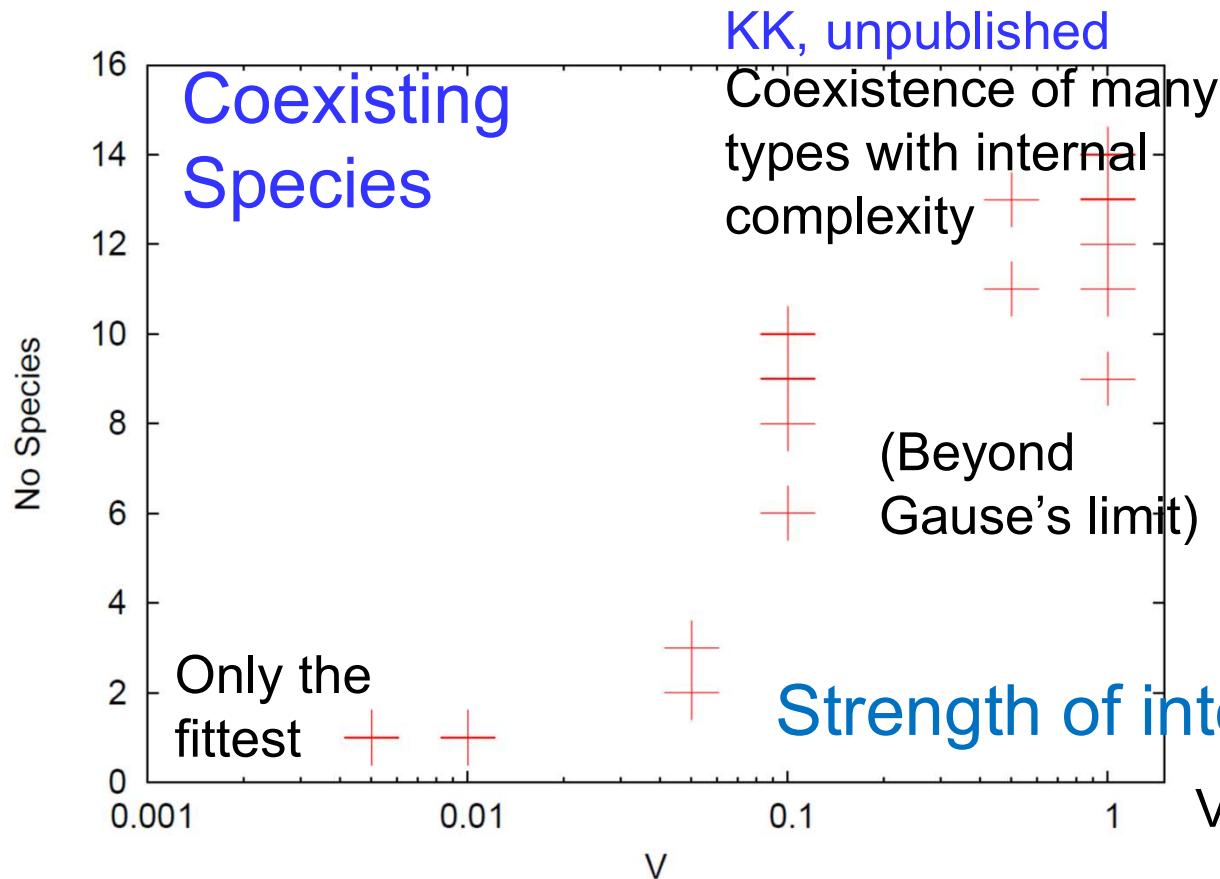
$$\rho^\alpha = N^\alpha / N_{tot}$$

$$\mu^\alpha = \mu^\beta$$

$$\frac{d\rho^\alpha}{dt} = (g^\alpha(\{X_j^*(\alpha)\}) - \bar{\mu})\rho^\alpha \quad g^\alpha(\{X_j(\alpha)\}) = g^\alpha(\{X_j(\beta)\})$$

Resource-limitation+ Strong Interaction (Exchange of chemicals)

- Coexistence of diverse celltypes



V = cell volume / medium volume

“Strong cell type in isolation” secrets out useful chemical → Coexistence of diverse species

Cf Kashiwahi,..., Yomo coexistence of multiple E Coli types
J Mol Ev 2001

* * Theory for interaction-induced diversity

traditional studies --population dynamics
(random matrix+ α)

In reality (eg microbial ecosystem such as biofilm)
intracellular dynamics + interaction

-- multi-level dynamics model (eg Yamagishi Saito, KK

PLoSCB2021), not a single layer) Species other than the fittest
at a single-level coexist due to interaction

NEED

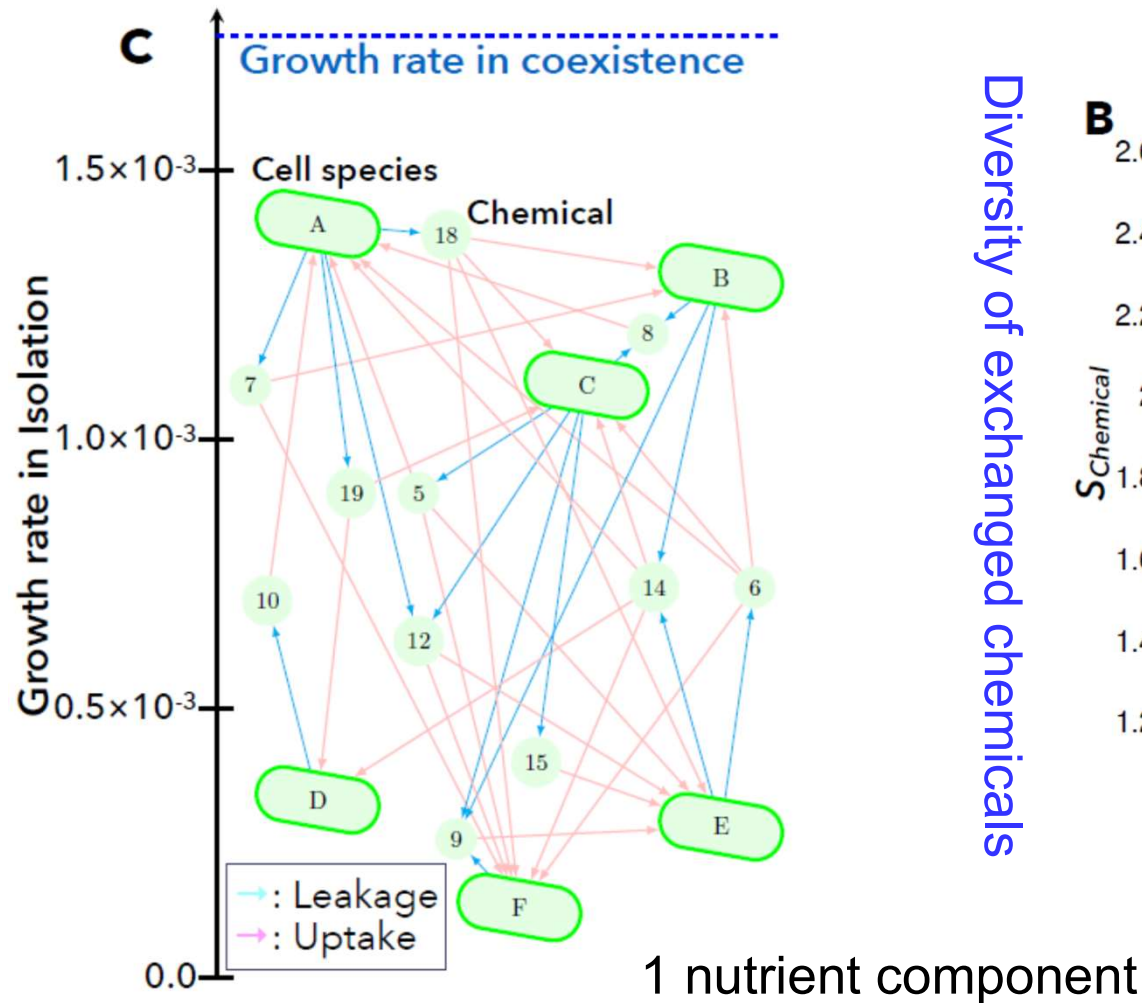
Simple model with internal states + interaction

e.g., spin model + interaction

Statistical-physics Theory?

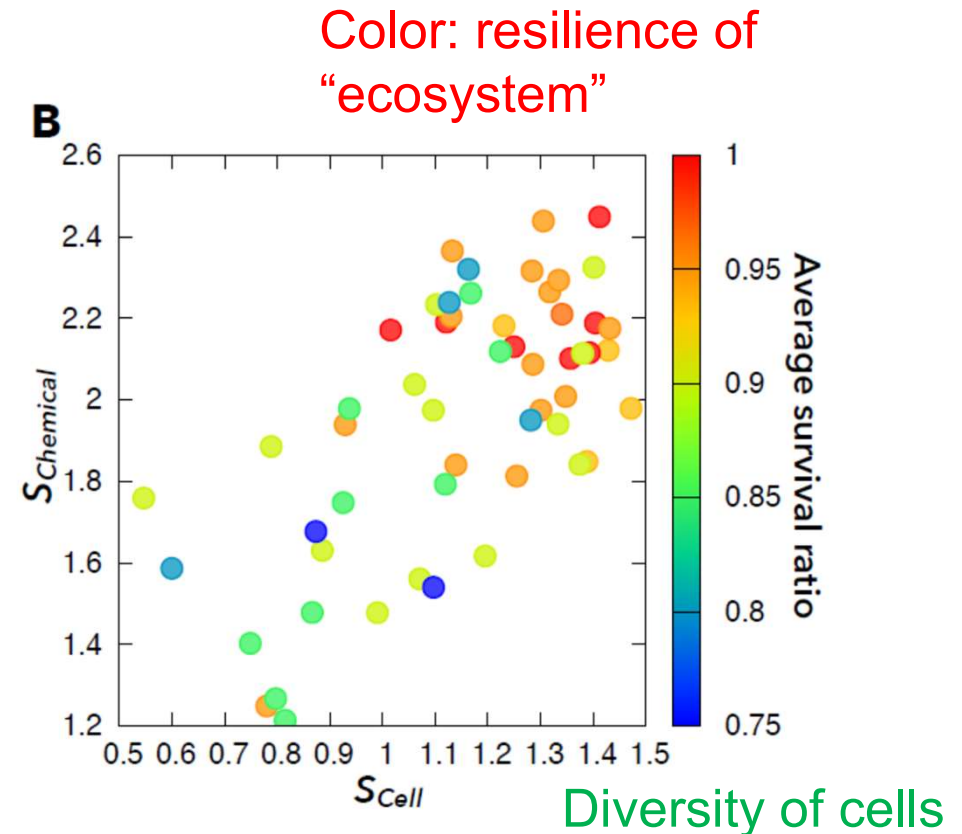
for each unit + population dynamics

Multiple Species Interaction → Intra-Inter Dynamics (Exchange of Chemicals) → Coexistence of multiple species (Macro-micro-consistency) → Each cell-types increase the growth-speed by interaction → Resilient “ecosystem”



A-E: different celltypes with reaction nets

Yamagishi, Saito, KK, PLoS CB 2021.



Diversity enhances Resilience
(no trophic level,
entangled)

○Neural Dynamics: from dynamics to symbol

Chaotic Itinerancy in layered coupled map (KK unpub 90's, 2017)

i) "?" state → slow-fast interfere → slow-mode control: Fast changes are successively embedded into slower (to generate prior) :

←Brain as Timescale Machine

Fast input –Embed by Slow Learning →Output (Kurikawa, KK 2011..., 21; Ichikawa, KK) --memory dynamics

ii) Learning ←recent view of phenotypic evolution (constraint, dim-reduction, fluctuation-response)

iii) Revisit to MagicNo7??

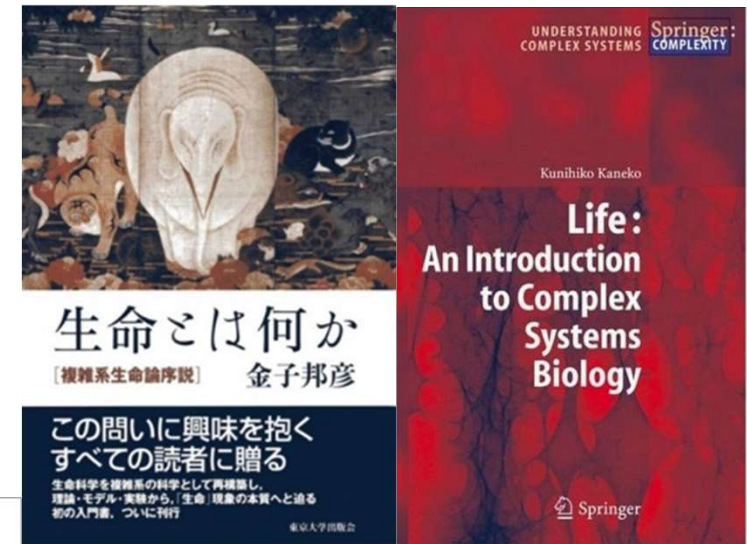
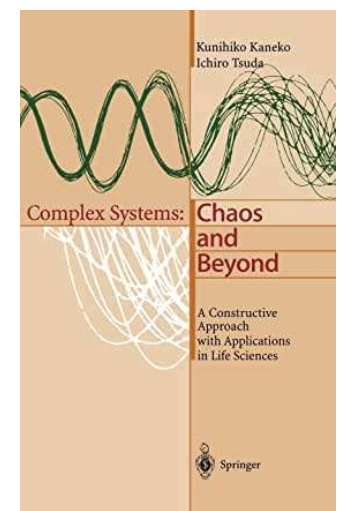
(cf Ishihara, KK 2005)

etcetc.....

Complex Systems; High-dimensional Dynamical Systems

→ Complex-systems Biology

→ Universal Biology



Translation
in Progress