

Kagome Quantum Spin Liquids: the case of herbertsmithite (and beyond?)

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Spectroscopies of Quantum Materials
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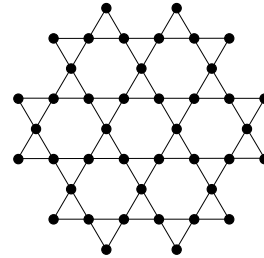
Kagome materials: QSL candidates

Kagome materials (Heisenberg, Quantum)

- Good realizations (+ small perturbations)

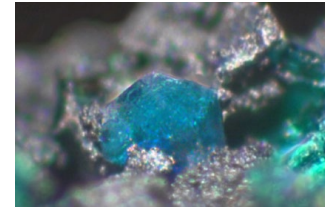
herbertsmithite $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

Zn-barlowite $\text{ZnCu}_3(\text{OH})_6\text{FBr}$



Herbertsmithite

Shores et al, JACS, 2005



Barlowite

Han et al, PRL 2014

-> Signature of QSL : no LRO, continuum of excitations ...

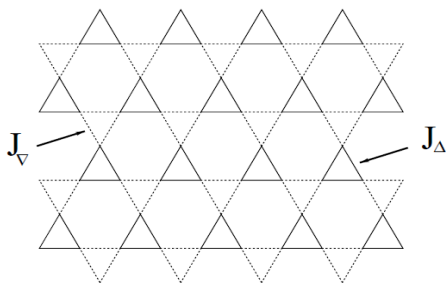
-> Type of QSL (gapped, gapless..), nature of the excitations remains challenging

- **Modified kagome lattice** : a side view, extending the phase diagram

-> new (quantum) states

-> feedback on the kagome problem ?

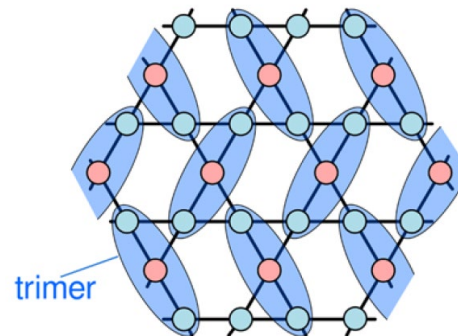
Breathing kagome



$[\text{NH}_4]_2[\text{C}_7\text{H}_{14}\text{N}][\text{V}_7\text{O}_6\text{F}_{18}]$: Orain, PRL (2017)

Repellin, PRB (2017); Iqbal PRB (2018) ..

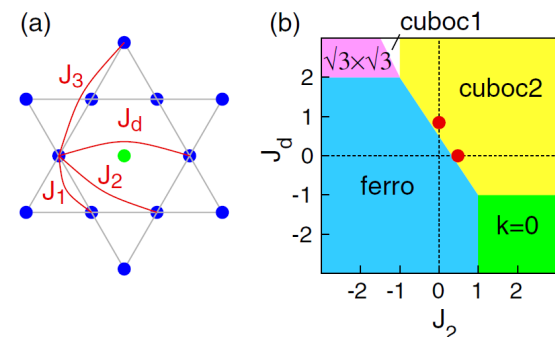
Exchange anisotropy



Volborthite $\text{Cu}_3\text{V}_2\text{O}_7(\text{OH})_2 \cdot 2\text{H}_2\text{O}$: Hiroi, JPSJ (2001)

Janson PRL (2016), Yoshida PRB (2017)..

Competing exchange interactions



Zn-Kapellasite $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$: Fak, PRL (2012)

Bieri, PRB (2016)...

Herbertsmithite, a spin liquid: no order, which is it?

J|A|C|S
COMMUNICATIONS

Published on Web 09/09/2005

M.R. Norman, RMP (2016)
Exp Reviews
C. Broholm et al. Science (2020)

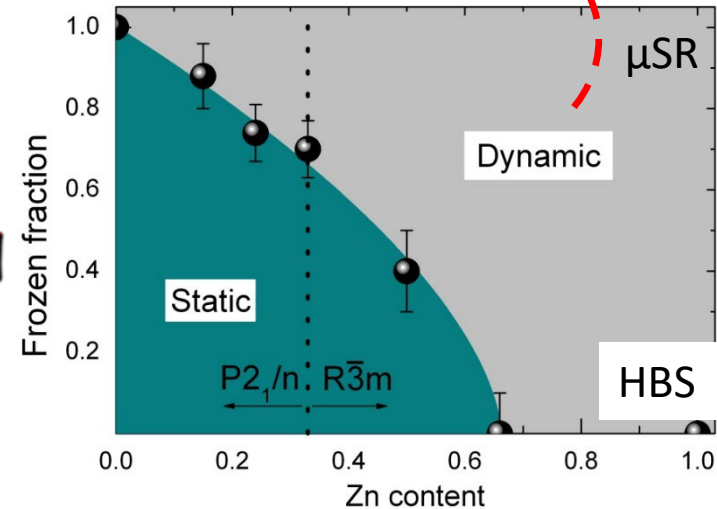
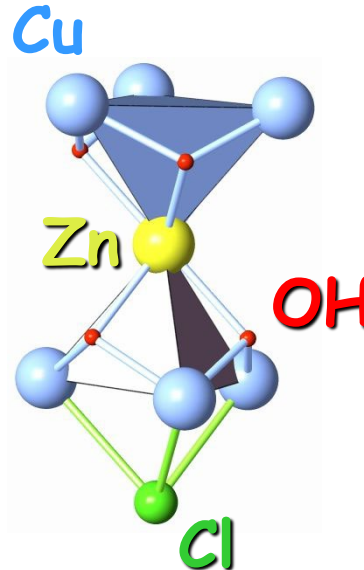
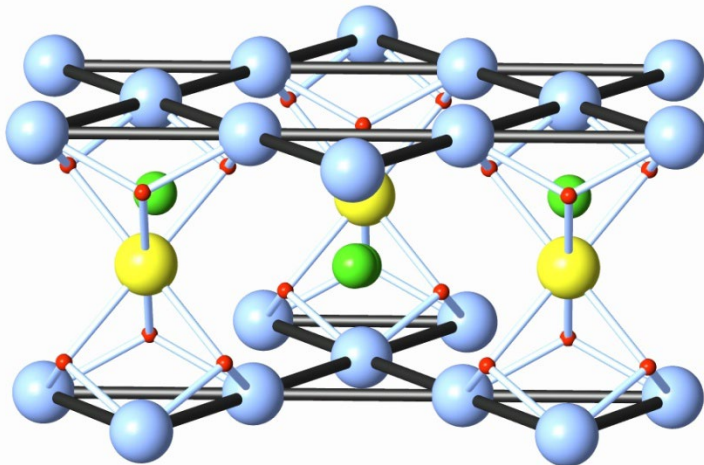
A Structurally Perfect $S = 1/2$ Kagomé Antiferromagnet

Matthew P. Shores, Emily A. Nytko, Bart M. Bartlett, and Daniel G. Nocera*

*Department of Chemistry, 6-335, Massachusetts Institute of Technology, 77 Massachusetts Avenue,
Cambridge, Massachusetts 02139-4307*

Herbertsmithite (HS): $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ Cu^{2+} , $S=1/2$; $J=190$ K (AF)

No freezing (at $\pm 6 \times 10^{-4} \mu_B$) down to 20 mK ($J/9000$) !



P. Mendels et al, PRL 98 (2007)

Interlayer, n.n. 2^{nd} , 3^{rd} n.n. couplings < 5 K (H. Jeschke, Phys. Rev. B 2013)

A spin liquid: no order. 15 years later: which is it?

J|A|C|S
COMMUNICATIONS

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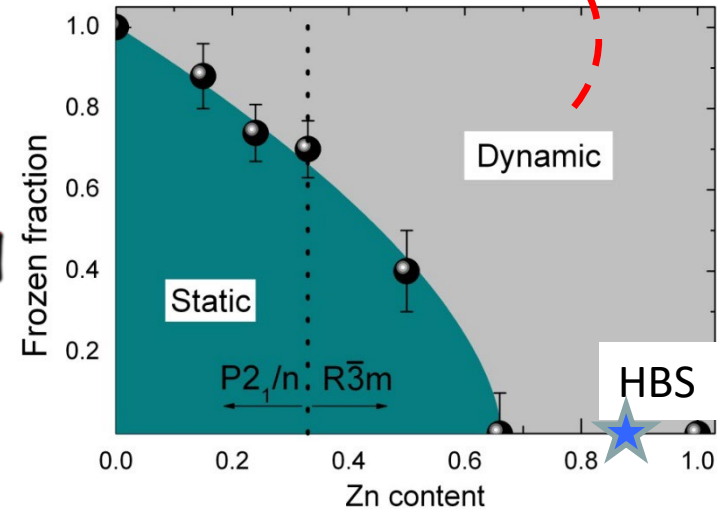
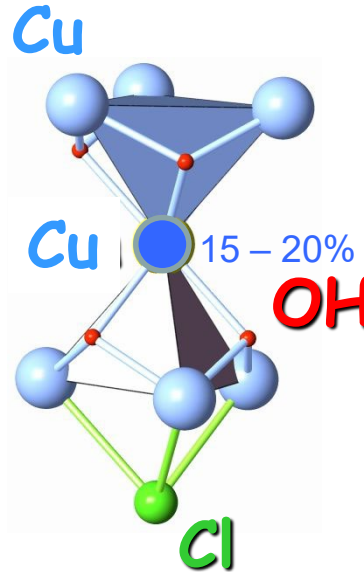
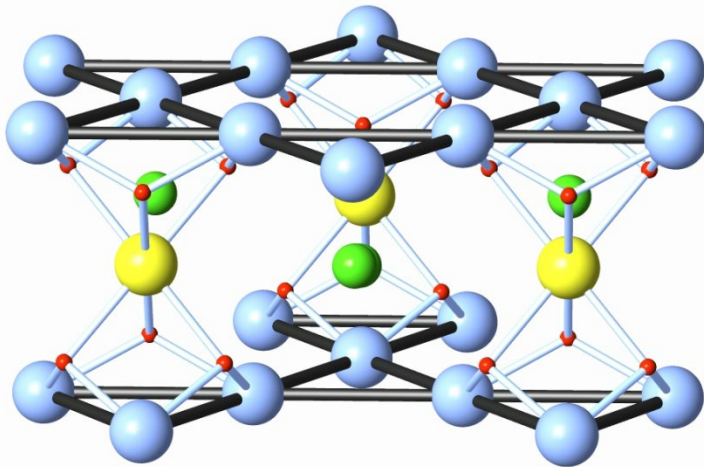
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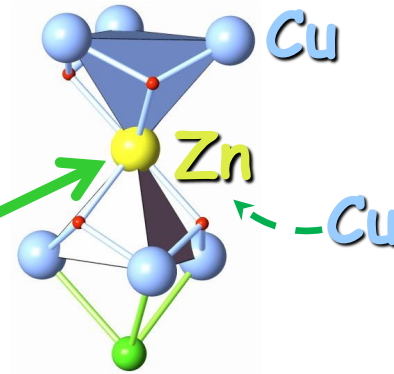


P. Mendels et al, PRL 98 (2007)

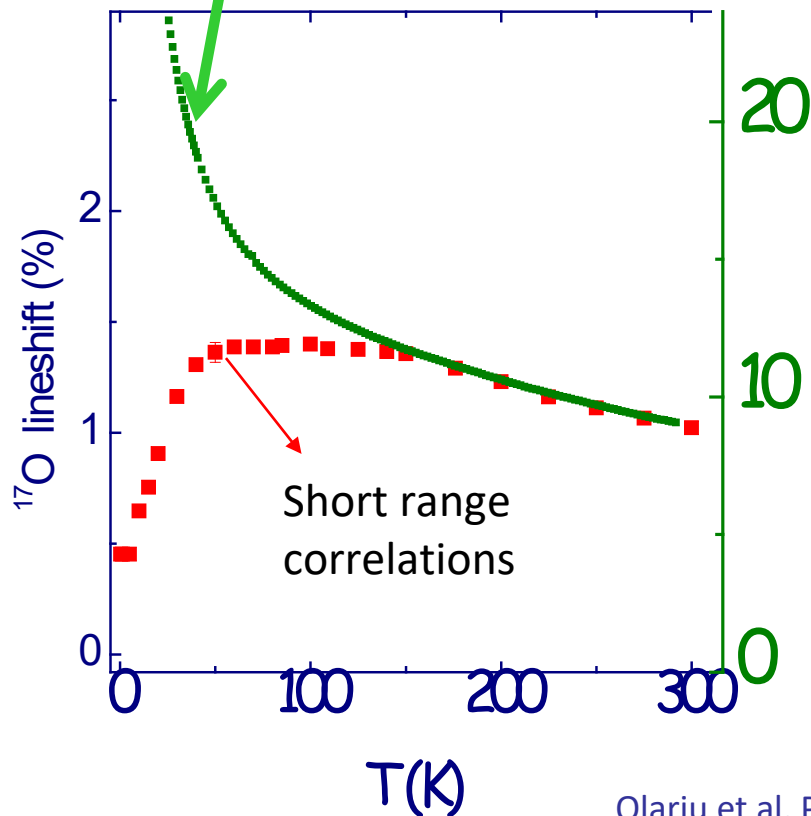
No Zn on kagome site (Smaha, Phys. Rev. Materials 2020)

Site selective spectroscopy: ^{17}O NMR

- Nuclei: ● Cl, H, D are dominantly coupled to Cu@Zn
● O dominantly coupled to Cu_{kago}, less to Cu@Zn



~15% Cu on the Zn site
Nearly free $\frac{1}{2}$ spins






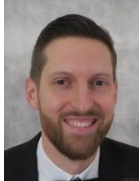

Low-T NMR and C_p investigations of kagome herbertsmithite crystals


Nature Physics 16, 469-474 (2020)
Phys Rev X, 12, 011014 (2022)

P. Mendels, Lab. Physique des Solides, Univ. Paris-Saclay
Spectroscopies of Quantum Materials

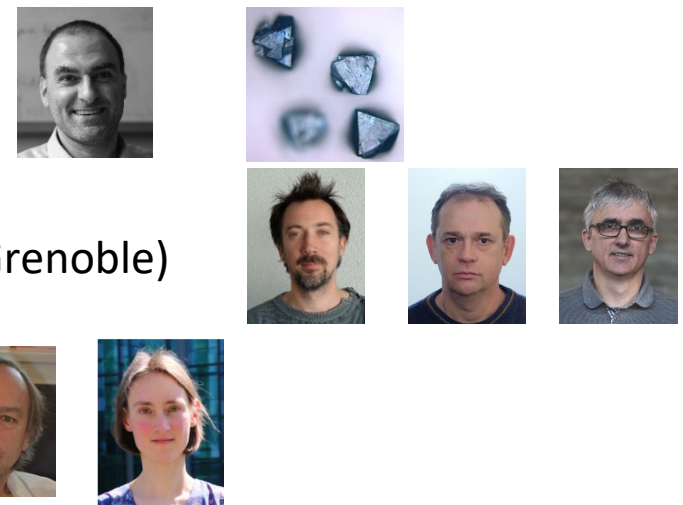
P. Khuntia, F. Bert, E. Kermarrec, Q. Barthélemy

Now IIT Madras   Post-doc

   PhD

Now IQ Sherbrooke 

- ✓ M. Velazquez (crystals): ICMCB, INP Grenoble (France)
- ✓ A. DeMuer, C. Marcenat, T. Klein (C_p): LNCMI & Néel (Grenoble)
- ✓ B. Bernu, L. Messio (Theory): LPTMC, (Paris)



A spin liquid : yes, but gapped or gapless?

SCIENCE sciencemag.org

FRUSTRATED MAGNETISM

Evidence for a gapped spin-liquid ground state in a kagome Heisenberg antiferromagnet

2015

Imai's group

Mingxuan Fu,¹ Takashi Imai,^{1,2*} Tian-Heng Han,^{3,4} Young S. Lee^{5,6}



Mendels' group

Gapless ground state in the archetypal quantum kagome antiferromagnet $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

2020

P. Khuntia^{1,2}, M. Velazquez^{3,4}, Q. Barthélemy¹, F. Bert¹, E. Kermarrec¹, A. Legros¹, B. Bernu⁵, L. Messio^{5,6}, A. Zorko^{7,8} and P. Mendels¹✉



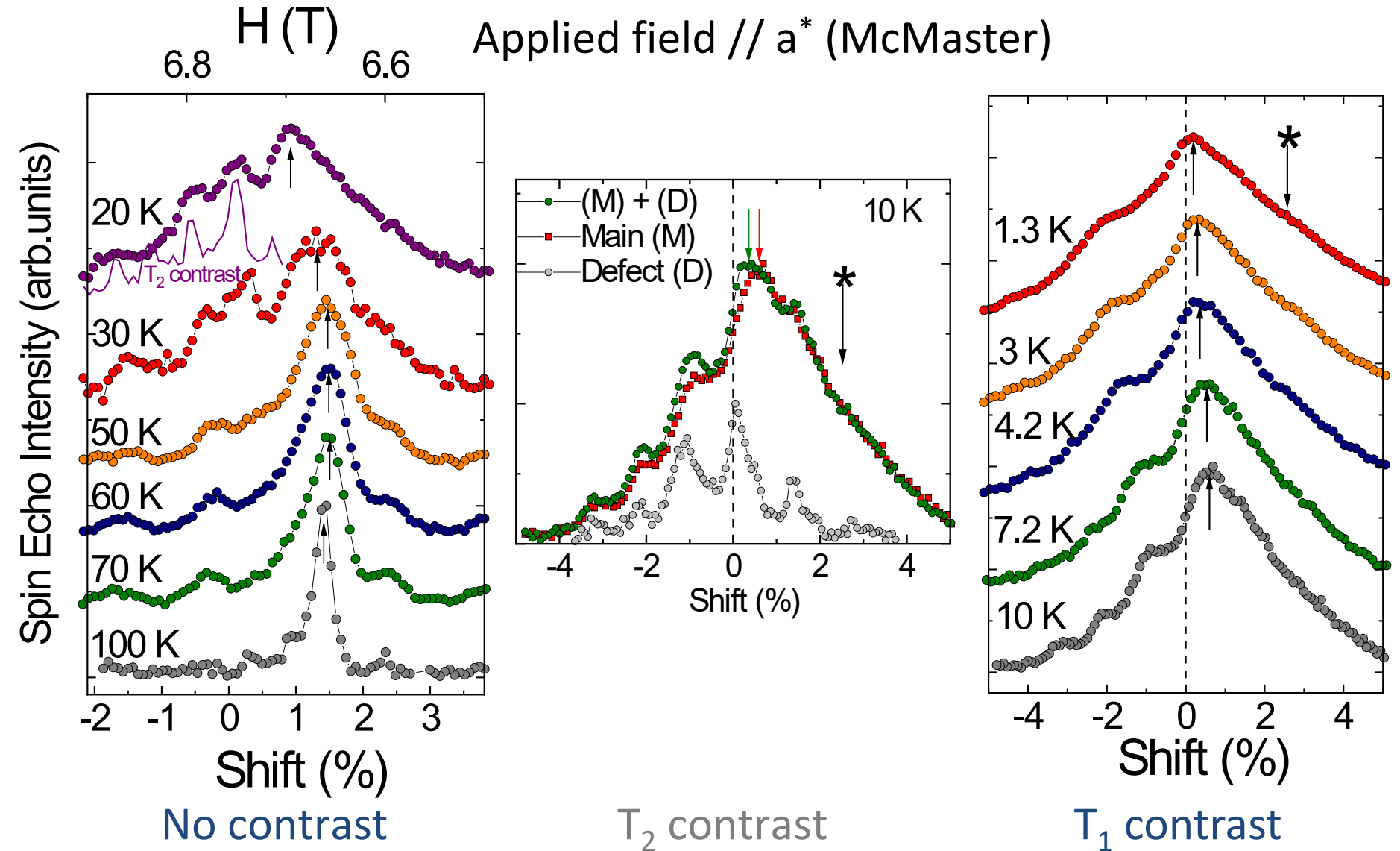
Imai's group

Emergence of spin singlets with inhomogeneous gaps in the kagome lattice Heisenberg antiferromagnets Zn-barlowite and herbertsmithite

2021

Jiaming Wang¹, Weishi Yuan¹, Philip M. Singer², Rebecca W. Smaha^{3,4}, Wei He^{3,5}, Jiajia Wen³, Young S. Lee^{3,6} and Takashi Imai^{1,7}✉

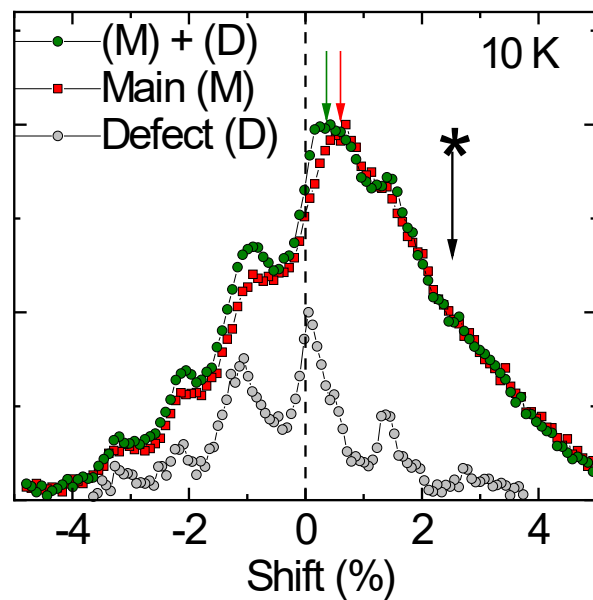
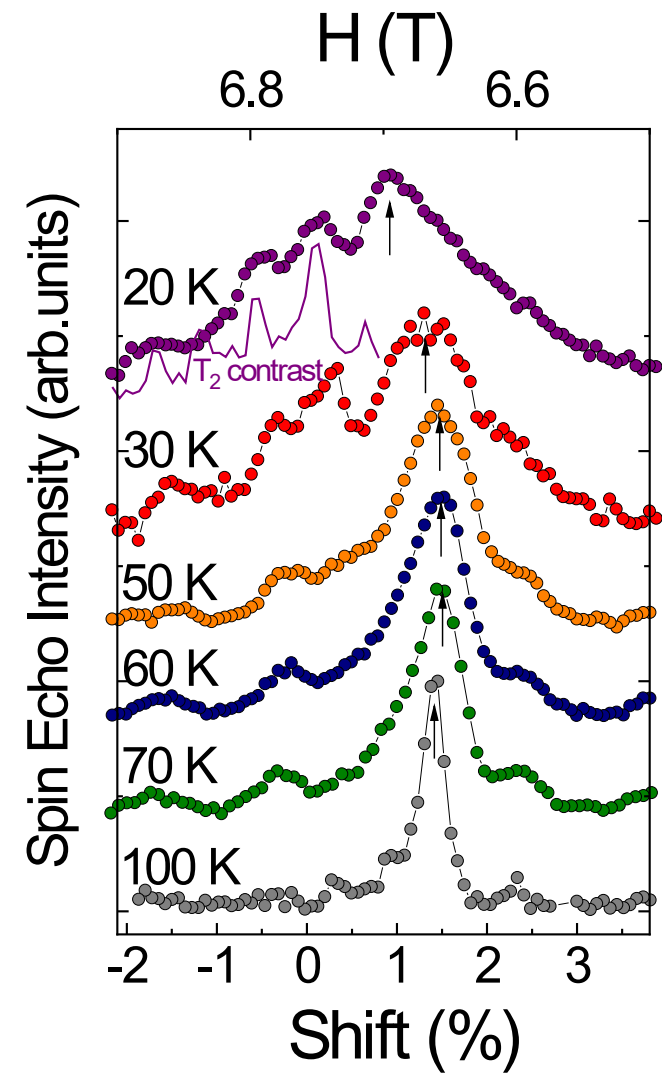
Two (or more) spectral components → deconvolution



$T=1.2$ K

From long T_2 , short T_2 component & spectral integration ~ 45% (D) weight
 From smoothing out singularities of (M) + (D) spectrum ~ 39(4)% (D) weight

A New T-scale : $T < 30$ K

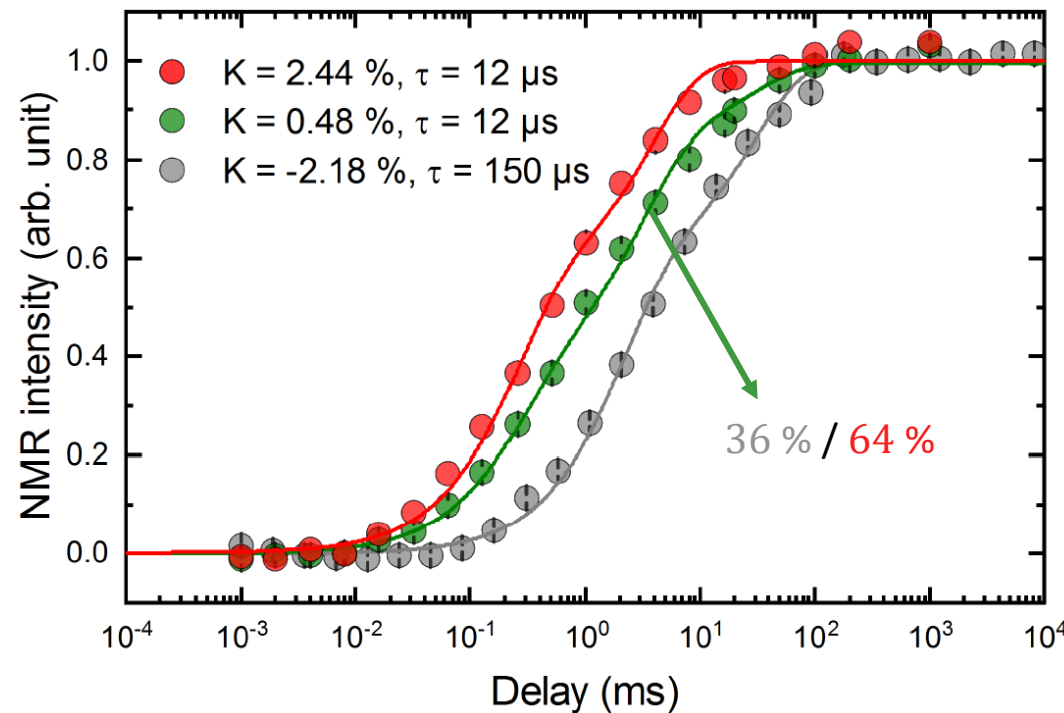
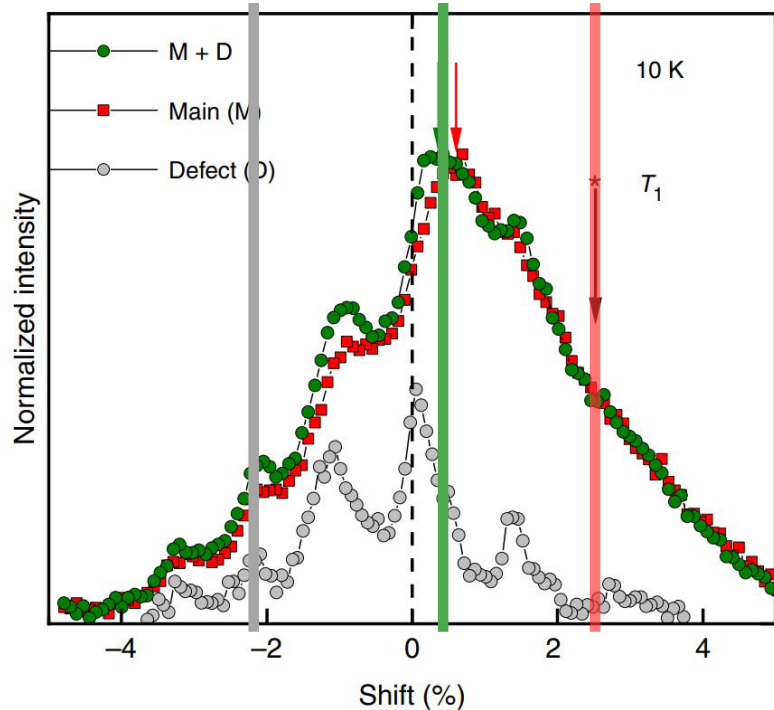


Spectrum with narrower peaks only resolved **below 30 K**
Typical of the spin liquid state?

Low-T Spin Dynamics T_1 : 2 components spectrally resolved

$B//a^*$ 6.6 T

$$\frac{1}{T_1} = \frac{1}{\hbar^2} \frac{k_B T}{(g\mu_B)^2} \sum_q |A(q)|^2 \frac{\chi_t''(q, \omega_n)}{\omega_n}$$



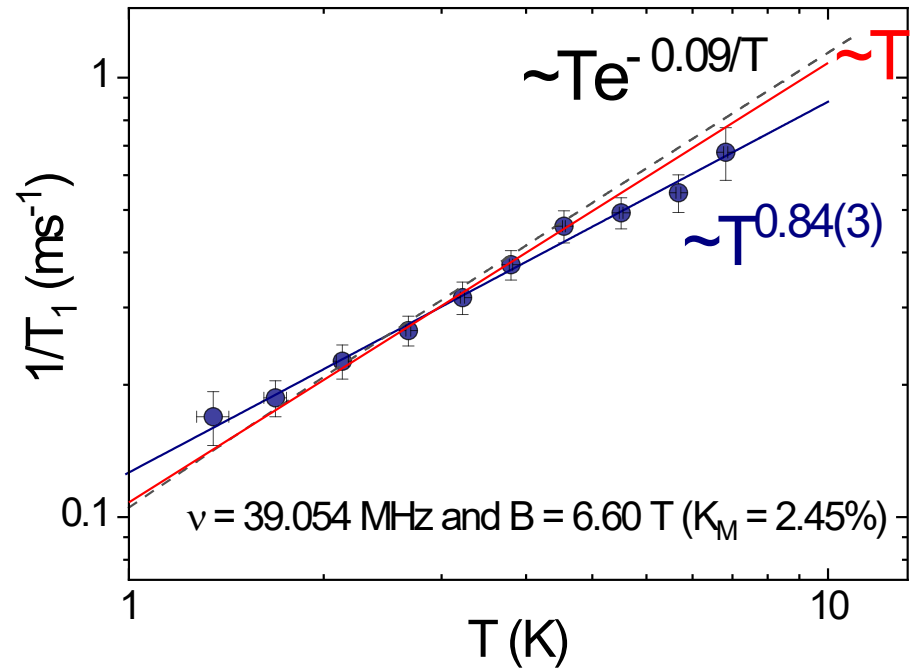
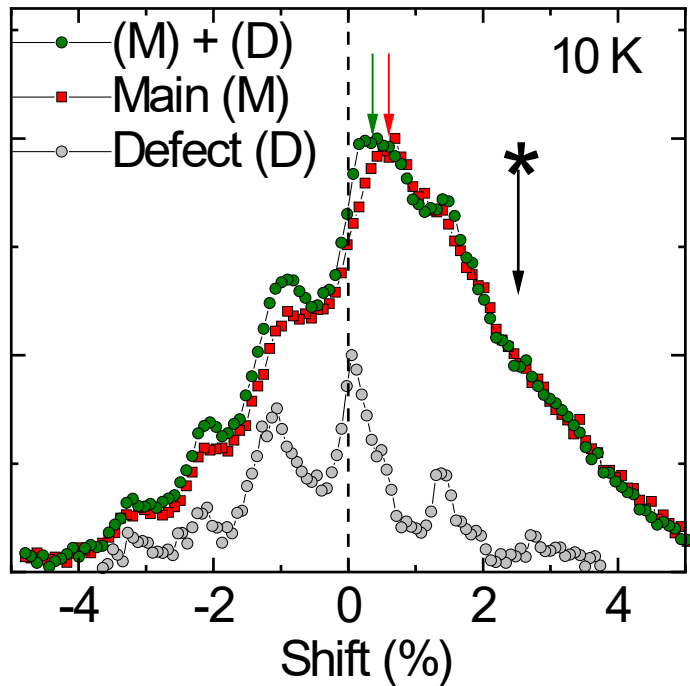
P. Khuntia et al. Nat. Phys. 2020

dominantly gapless

From long T_2 , short T_2 component & spectral integration $\sim 45\%$ (D) weight)
 From smoothing out singularities of (M) + (D) spectrum $\sim 39(4)\%$ (D) weight
 From T_1 (amplitude) $\sim 36\%$ (D) weight

Low-T Spin Dynamics T_1

$B//a^*$ 6.6 T $\frac{1}{T_1} \sim \int_{-\infty}^{\infty} \langle B_L^+(t) B_L^-(0) \rangle \exp(-i\omega_{RMN} t) dt$

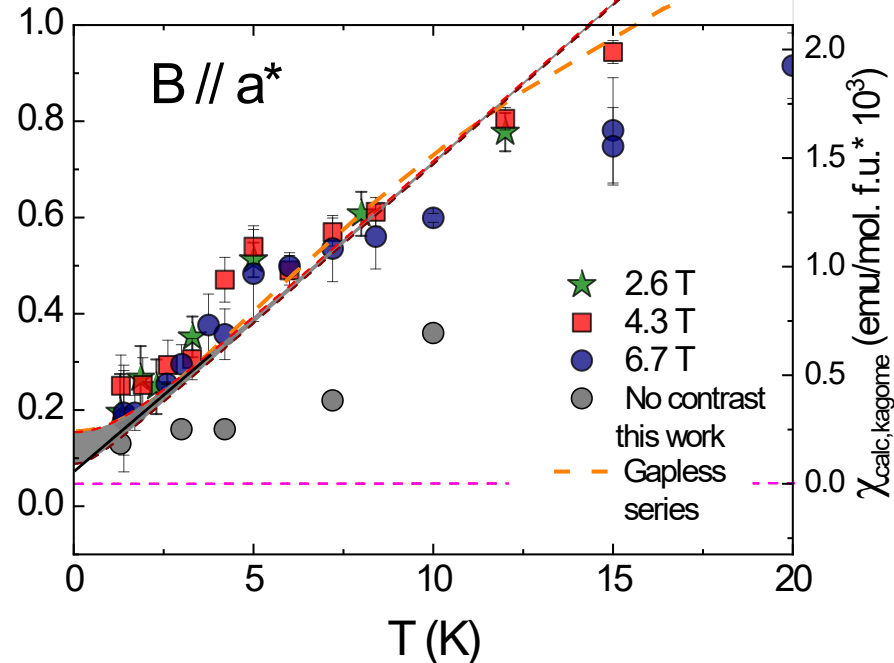
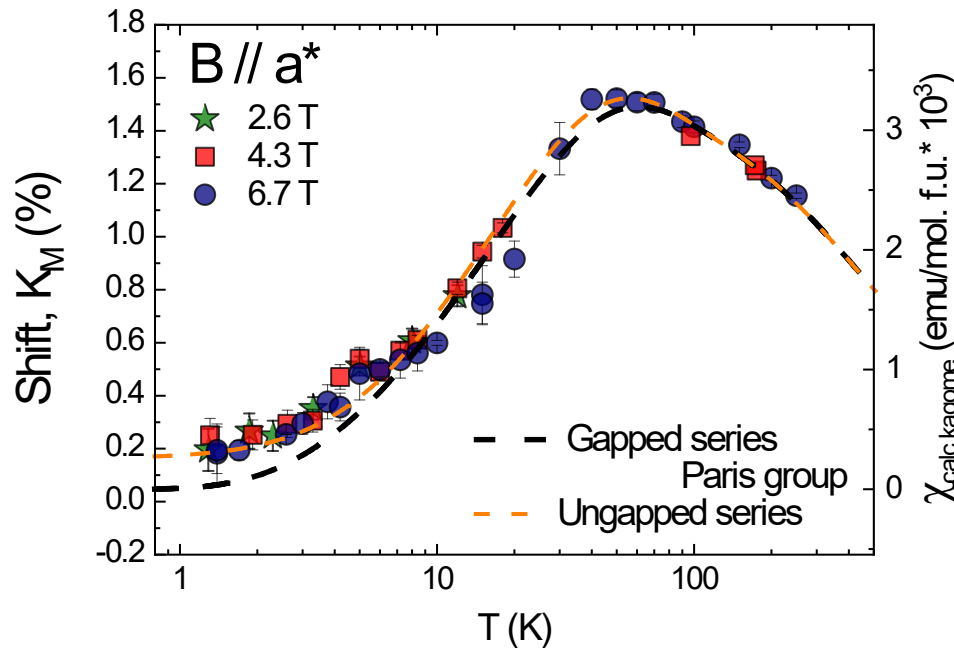


P. Khuntia et al. Nat. Phys. 2020
Q. Barthélemy, PhD :3.1 Tesla

- No spin gap behavior (conservative < 0.02 J)
- power law dependence $1/T_1 \sim T^{0.84(3)}$
- defect : 10 times lower relaxation rate (no gap)

Shift of the main line (intrinsic)

$J = 190 \text{ K}$



- ✓ Fu et al (Science 2015) : gap $\sim 9\text{K}$ (closing with applied field)
- P. Khuntia et al (Nat. Phys. 2019) : no gap, $\chi \sim T$, field independent**

- ✓ Series expansion for the kagome susceptibility

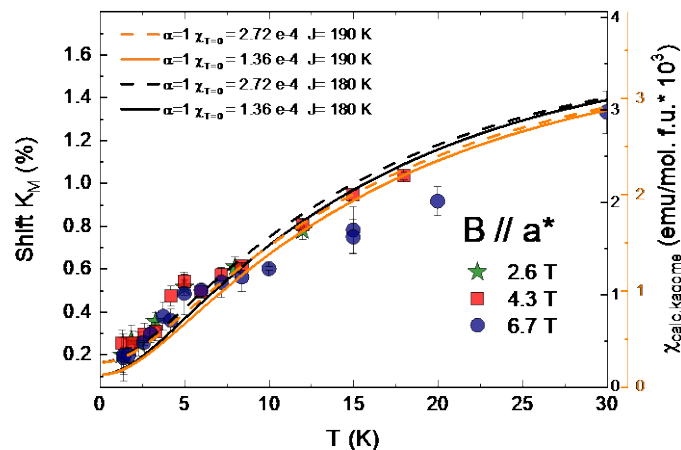
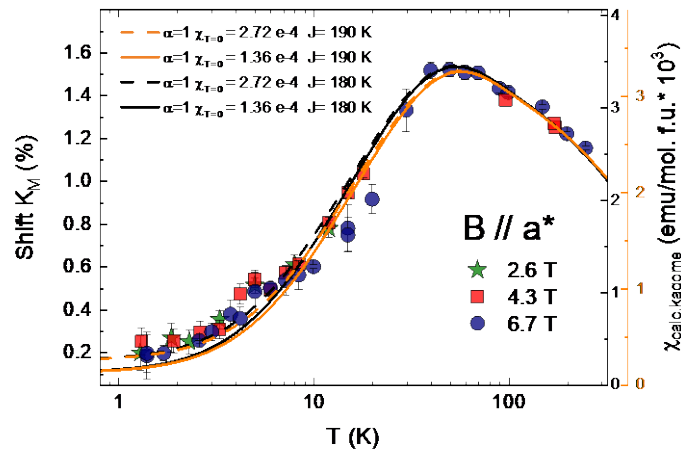
Expansion of $S(E)$ + assume asymptotic behavior of C and $\chi(T=0)$ gapped or gapless

Two boundary conditions: e_0 ground state energy and high T expansions

Comparison to series

(b) $K_{\text{chem}}(T=0) = 0.05\%$ $C \sim T$

(Also compatible with $C \sim T^2$)



✓ Series expansion for the kagome susceptibility

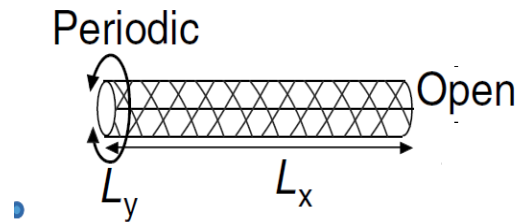
Expansion of $S(E)$ + assume asymptotic behavior of C and $\chi(T=0)$ gapped or gapless

Two boundary conditions: e_0 ground state energy and high T expansions

A gapless Dirac model ?

Gapped

The ground-state of QKHA would be a gapped spin-liquid (short-range RVB)



Yan et al Science (2011): first DMRG, Depenbrock et al PRL (2012)

. Z_2 from correlations

. Gap $0.13 \text{ J} \rightarrow 0.05 \text{ J}$

Gapless

He et al, PRX (2017) DMRG (revisited)

. DMRG in infinite system: a Dirac SL would be gapped

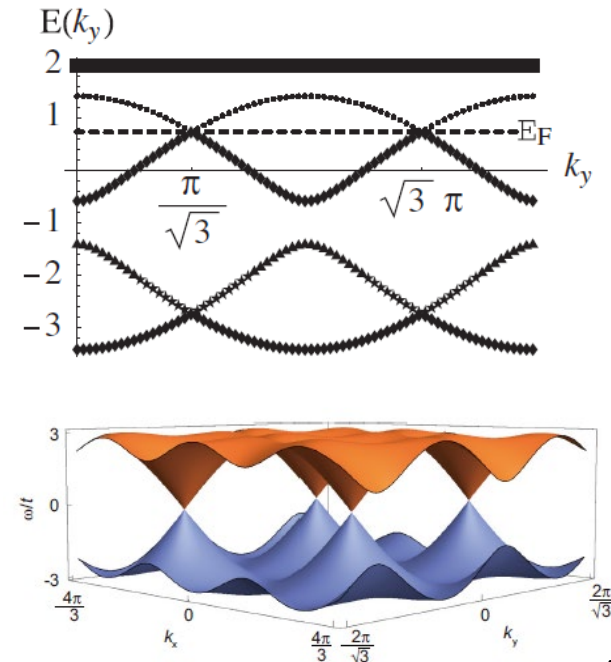
. Momentum dependent excitation spectrum

\Rightarrow Dirac Spin Liquid favoured

Iqbal, Poilblanc, Becca (2011 – 2015) Variational MC

Hotta et al, PRB (2018) Exact Diagonalization (+SSD) ...

Liao et al, PRL (2017) Tensor network states



A gapless Dirac model ?

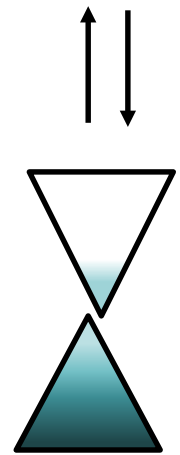
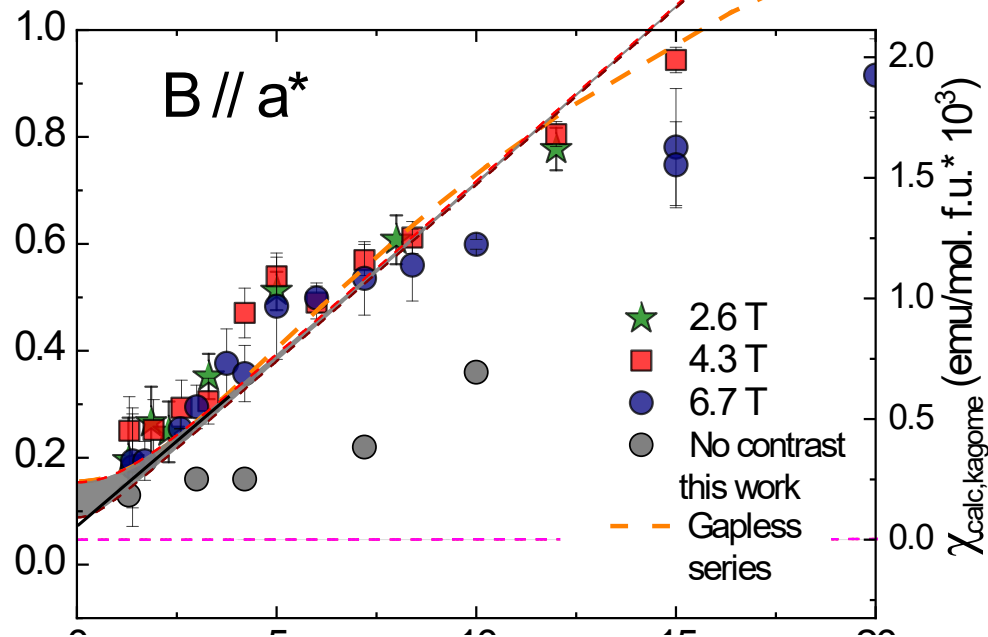
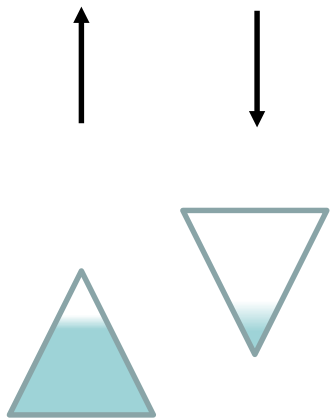
Two energy scales: kT vs $\mu_B B$

$kT \ll \mu_B B$ (spinon pockets)

1. finite $\chi \sim B$ at $T=0$
2. $C \sim T$ for $T \rightarrow 0$
3. $1/T_1$ algebraic in T

$kT \gg \mu_B B$ (Dirac cones)

1. Susceptibility : χ linear in T
2. Specific heat $\sim T^2$
3. $1/T_1$ algebraic in T



A gapless Dirac model ?

Two energy scales: kT vs $\mu_B B$

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1. finite χ at $T=0$
2. $C \propto T$ for $T \rightarrow 0$
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$kT \gg \mu_B B$ (Dirac cones)

1. Susceptibility : χ linear in T
2. Specific heat $\sim T^2$
3. $1/T_1$ algebraic in T

Ran et al, PRL 98, 2007; Hermele et al. PRB 2008 ; Ran et al PRL 2009

1. Yes
$$\chi(T) = \frac{3.2\mu_B^2}{J^2}(k_B T)$$

(Slope) $^{0.5} \sim v_F = 4.8 \times 10^3$ m/s \leftrightarrow only factor 1.2 off

2. Yes, Series consistent with $C(T \rightarrow 0) \sim T$... valid for $\mu_B B \gg kT$ or $C(T \rightarrow 0) \sim T^2$
3. Yes

Consistency with Dirac cone of spinon excitations

but

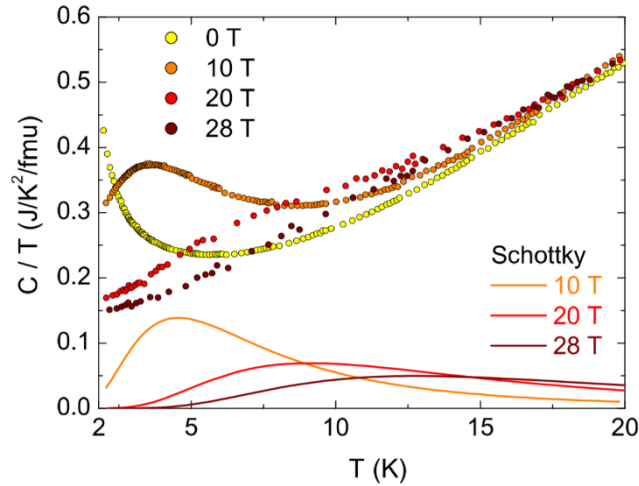
U(1) Dirac spin liquid is unstable (anisotropy DM, field) any similar model stable???

High Field specific heat data invalidate the Dirac cone model

Q. Barthélemy et al., Phys. Rev. X (2022)

High-Field, Low-T specific heat: not a Dirac SL

Q. Barthélemy et al., Phys. Rev. X (2022)

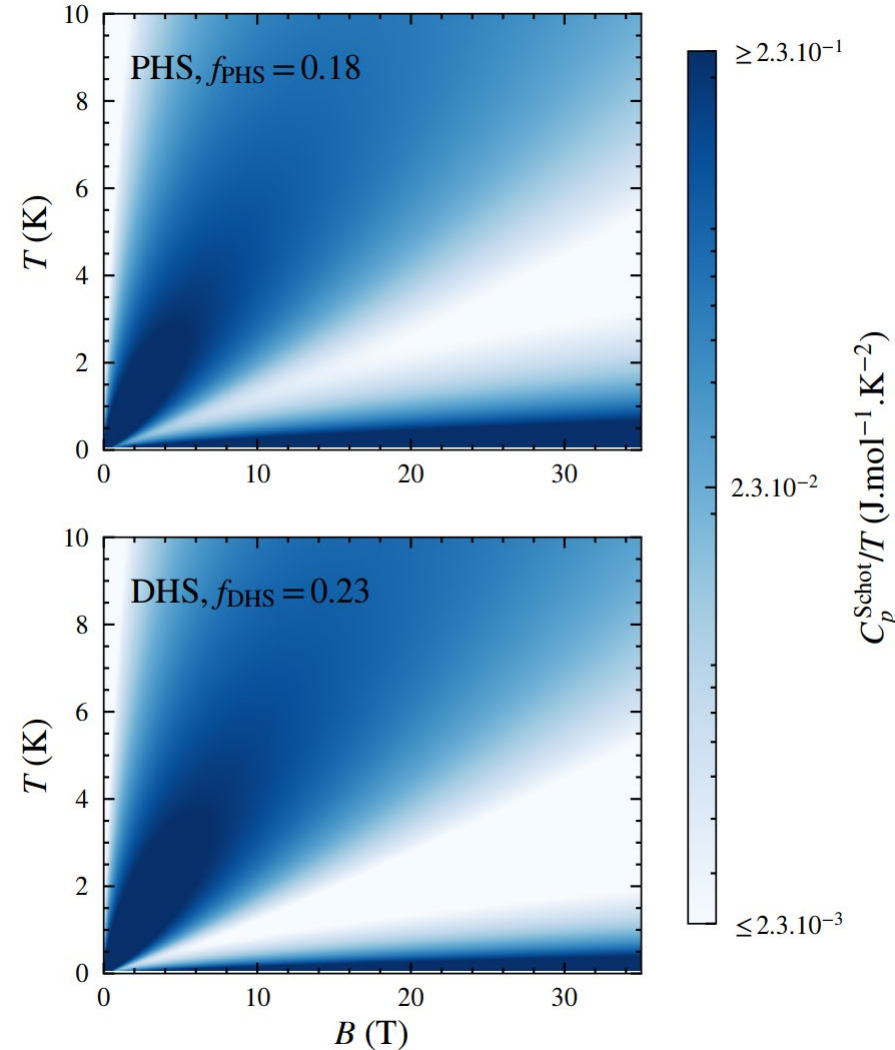


$$C_p = C_p^{\text{kago}} + C_p^{\text{imp}} + C_p^{\text{phon}}, \text{ where } C_p^{\text{imp}} \approx C_p^{\text{Schot}}.$$

$$C_p^{\text{Schot}}(T, \Delta) = f \frac{N_A k_B \Delta^2 \exp(\Delta/T)}{T^2 [1 + \exp(\Delta/T)]^2},$$

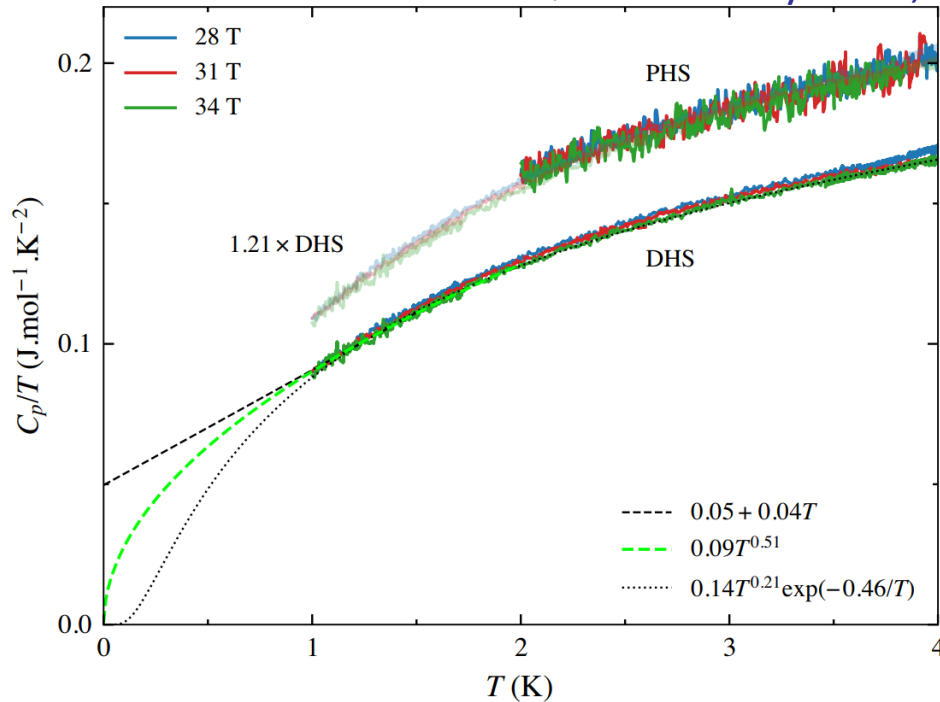
with

$$\Delta = g \mu_B B / k_B \text{ (Zeeman gap, } g \approx 2.2).$$

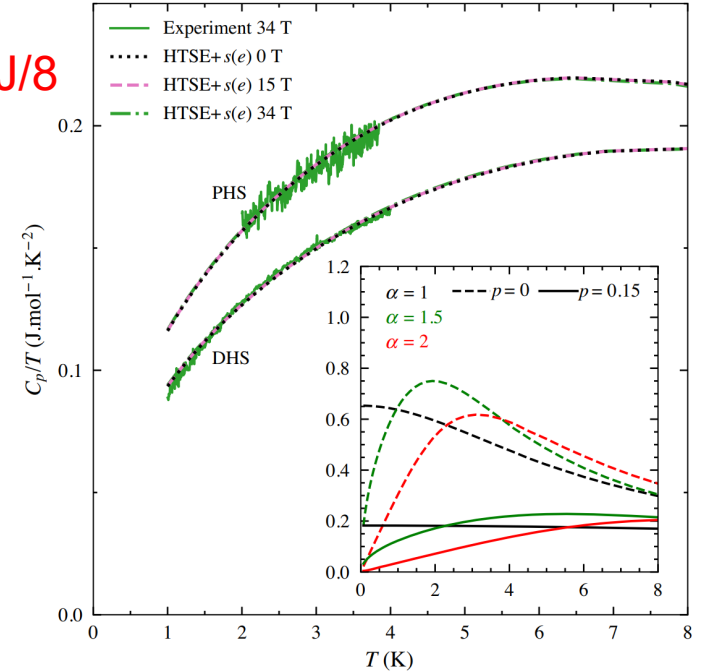


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Q. Barthélemy et al., Phys. Rev. X (2022)

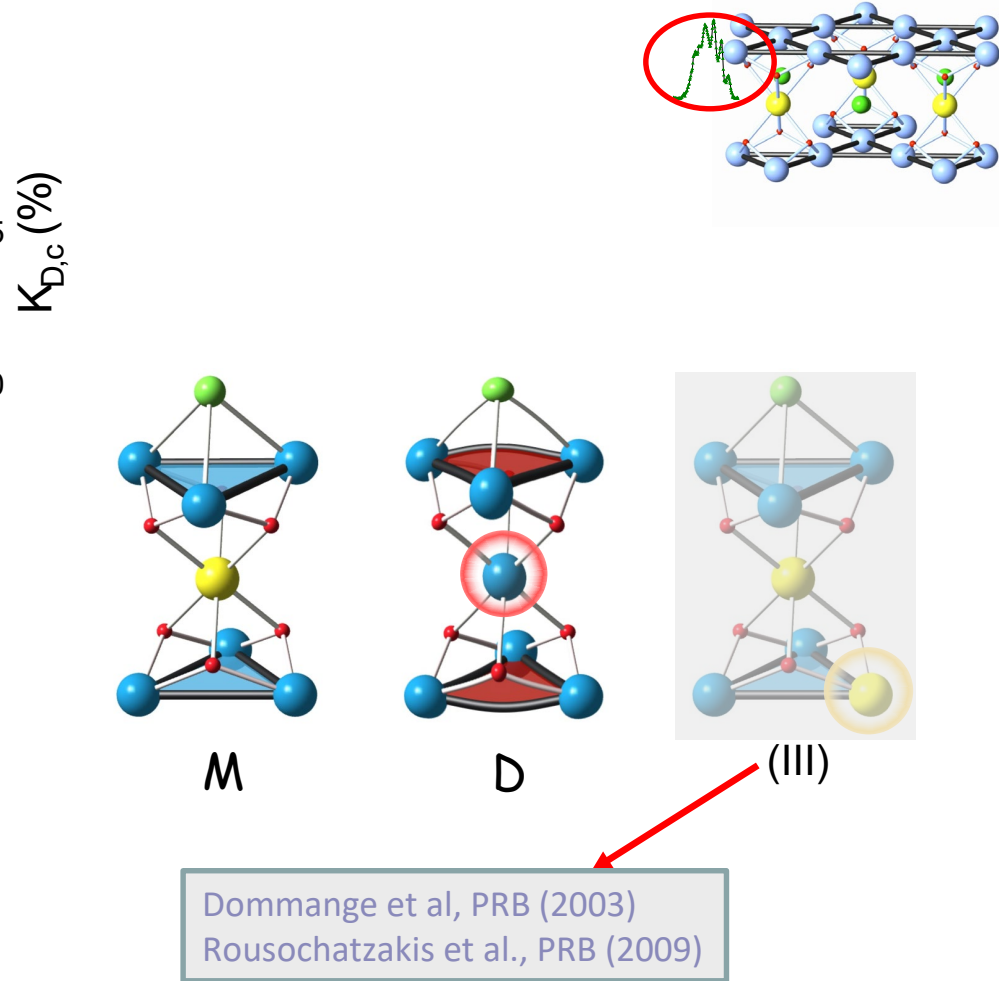
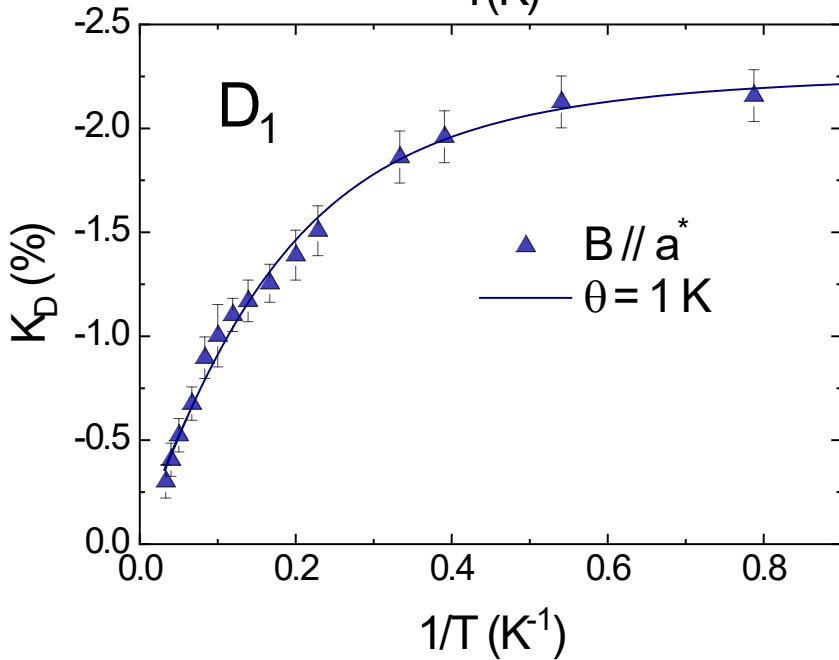
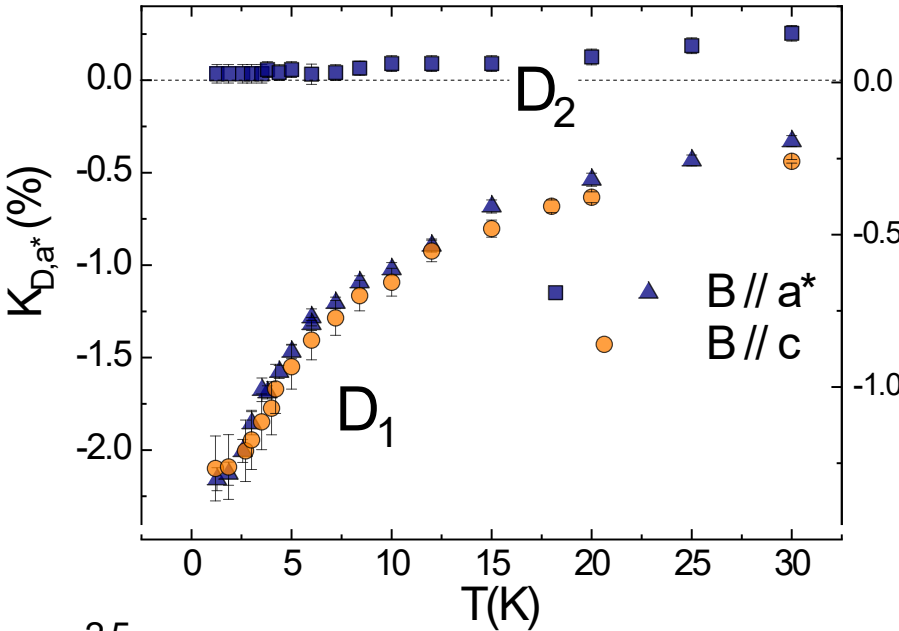


$$\mu_B B < J/8$$



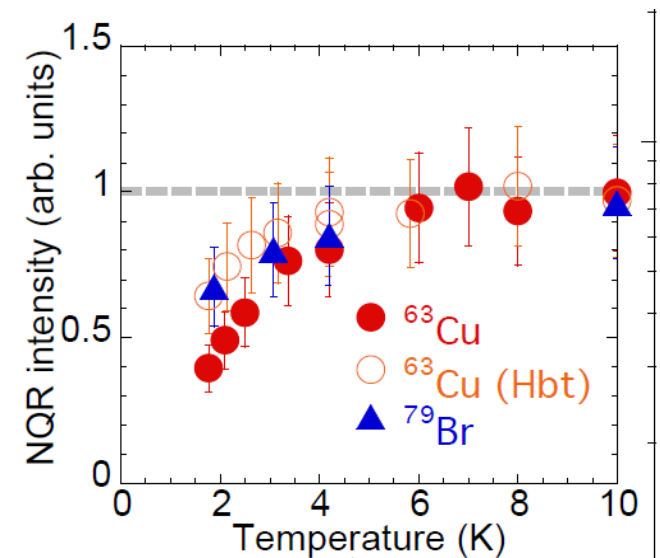
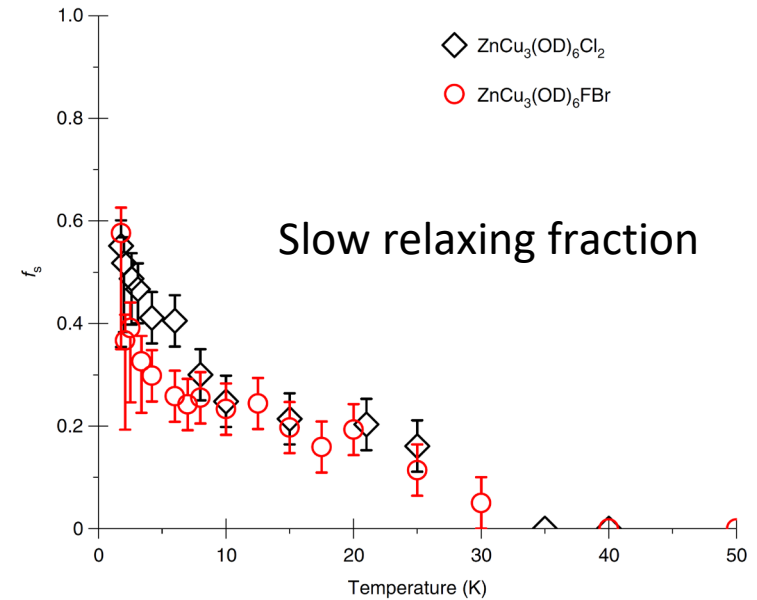
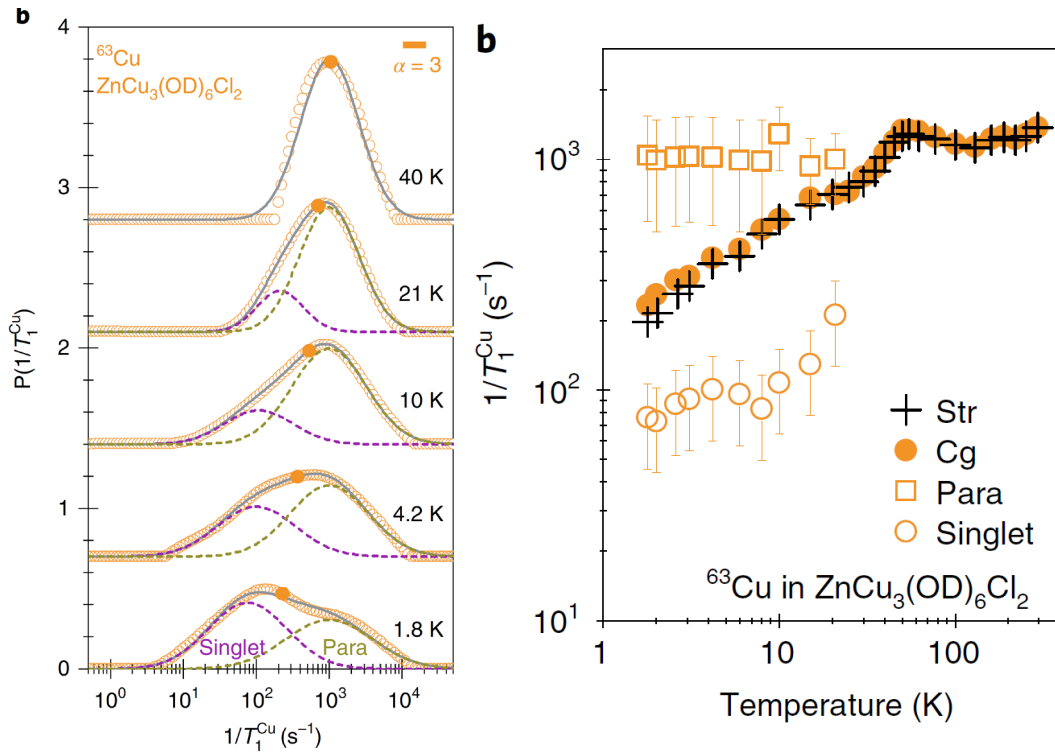
- ✓ **Field independent** C_p for $1 \leq T \leq 4$ K and $28 \leq B \leq 34$ T: not a Dirac SL.
- ✓ **Spinon**: v_F from NMR too small to explain the magnitude of C_p
- ✓ **If any gap**, it would be less than $J/500$ (models give $\Delta > J/20$)
- ✓ **Power law**: $C_p \sim T^{1.51}$
- ✓ Fit to series are severely constrained \rightarrow **effective dilution** of kagome planes 11% to 13.5%.
 $\rightarrow C_p \sim T^{1.5}$
- ✓ Consistency of $C_p \sim T^{1.5}$ with low-field data + Schottky \rightarrow **field-invariant down to $B \rightarrow 0$.**

Shift of the defect lines



Cu NQR ($T < 30$ K): McMaster's group

Emergence of spin singlets with inhomogeneous gaps in the kagome lattice Heisenberg antiferromagnets Zn-barlowite and herbertsmithite



Comparison ^{17}O NMR and Cu NQR ($T < 30\text{ K}$)

^{17}O NMR $T = 1.2\text{ K}$

P. Khuntia et al. Nat. Phys. (2019)

(M) Line

Weight 60%

No gap

« Fast » relaxing site

(D) Lines

Weight 40%

« Slow » relaxing sites

P. Khuntia et al. Nat. Phys. 2020

Cu NQR, T decreasing

J. Wang et al. Nat. Phys. (2021)

Two components of T_1

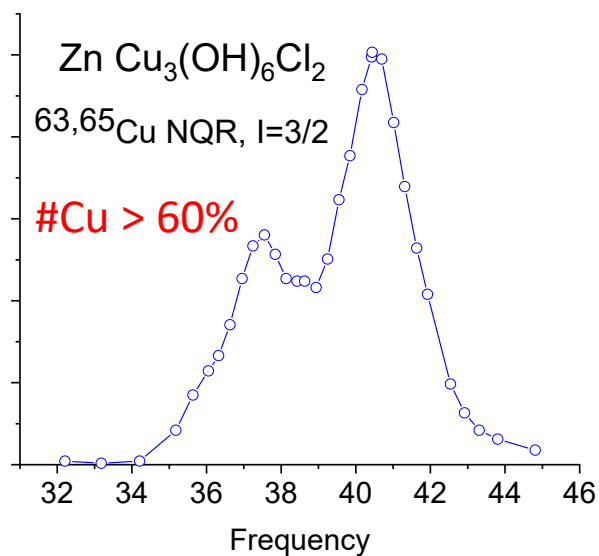
Fast, Slow

Fraction Slow / Fast \uparrow

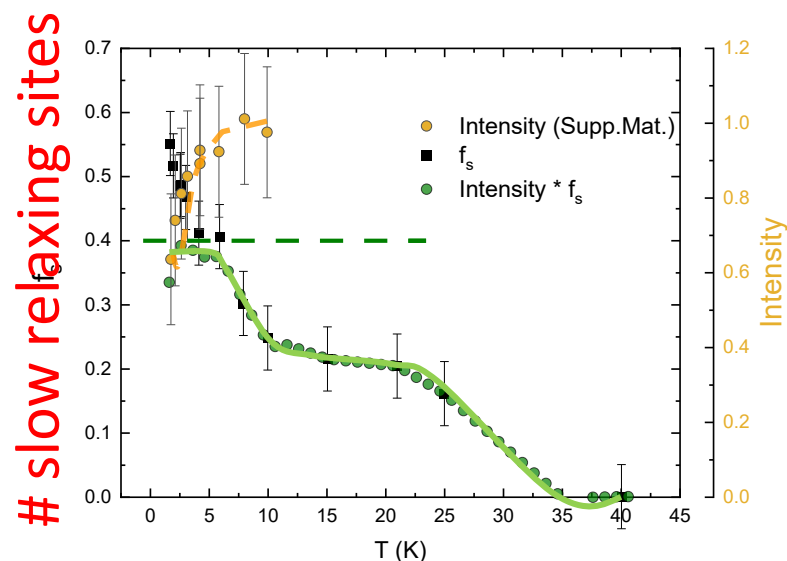
Intensity \downarrow

Fast/Slow $\sim 60\%/40\%$?

J. Wang et al., Nat. Phys (2021)



P. Mendels, unpublished

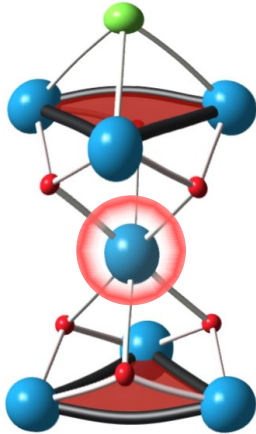


Adapted from J. Wang et al.

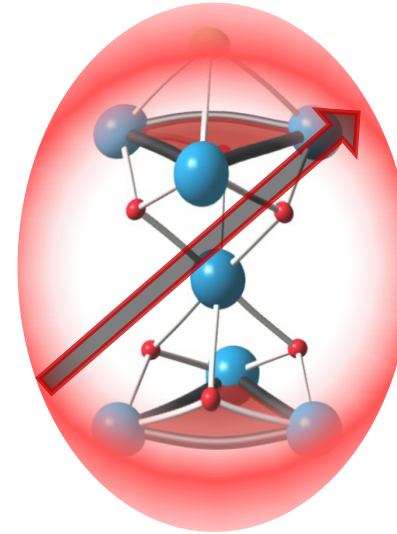
Nature of the defect : Two scenarios ?

In-plane spin-texture: indirectly induced by out of plane defects

$J_{\perp} = 0$ (?? many rivals)



J_{\perp} sizeable



$$S_{\text{eff}} = 1/2$$

Structural distortion around interlayer Cu
→ Impacts adjacent Cu's triangles @ kagome
→ Effective in-plane defect
→ Local and long-distance response

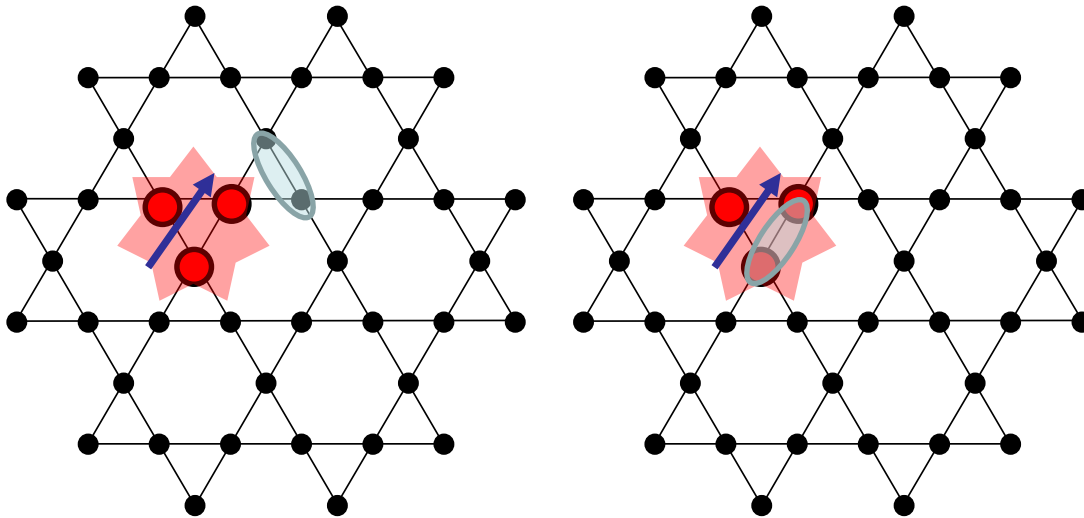
Coupling of inter-and intra- layer Cu spins
→ Effective spin $\frac{1}{2}$ defect
→ Coupling to the kagome plane
→ Local and long-distance response

↓ Our proposal

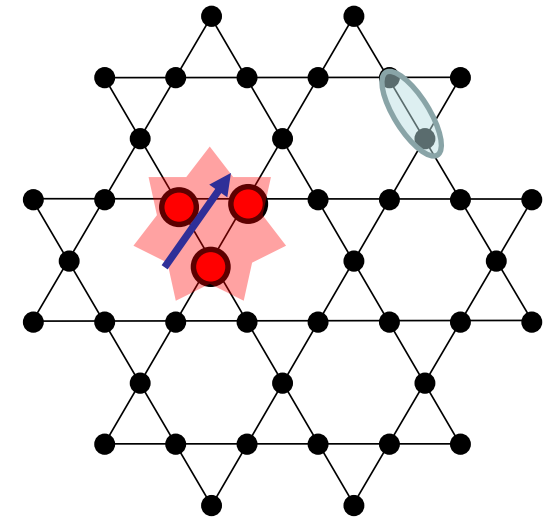
- ✓ NN O to a « defect »: **not feeling** the long distance response (Sachdev, Mila,...)
- ✓ Spin texture around the defect: **staggered** response (M line progressively broadening)
- ✓ **Quenching of the dynamics** for NN O to a « defect »: release of frustration

Which picture for the low-T « defect-induced physics »?

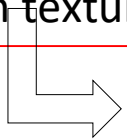
Orsay interpretation



McMaster interpretation



- ✓ 40 % slow relaxing of very specific sites
(*well resolved, protected, quenching of dynamics*)
- ✓ Spin texture for 60% fast relaxing, gapless sites



Need for understanding the nature of the defect
induced by Cu on interlayer site: $J_{\text{interlayer}}$

Summary for NMR and C_p

- ✓ Herbertsmithite is clearly an ABCA-stacked QSL kagome antiferromagnet, with the largest amount of data available to-date and a clean equilateral geometry.
- ✓ Not all excitation channels are gapped : T1, shift, specific heat (**conservative**)
- ✓ $T < J/10$: gapless susceptibility for main site : zero or finite $\chi_0 < 0.07 \chi_{\max}$
- ✓ Relaxing components
 - $1/T_1 \sim T^{0.84}$ (3) for fast relaxing component ~60% of total
 - Two slow relaxing components, protected against disorder **singled out below 30 K: an energy scale for the spin liquid phase?**
Huang et al., Phys. Rev. Lett. 127 (2021)
- ✓ $C_p \sim T^{1.5}$, field independent up to J/12; thermal conductivity: no deconfined spinon

Murayama et al., arXiv 2106.07223 (2021)
- ✓ **Theoretical** scenario still open for herbertsmithite and for the pure KHAF
We know what it is not: **not Z2 short range RVB**, “not just a soup of featureless singlets: a large number of possible Q many body states (Lauchli et al PRB 2019)”, **Dirac in the pure case ? But not with defects, another kind of defect-induced QSL?**

Collaboration



P. Pupal
MPI Stuttgart



Q. Barthélemy
U. Sherbrooke



D. Chatterjee
phD SQM/LPS



F. Bert
SQM/LPS



E. Kermarrec
SQM/LPS

M. Parzer, A. Riss, F. Garmroudi, A. Pustogow
K.M. Zoch, C. Krellner
Sylvain Petit,
J. Willwater, S. Süllow
C. Baines
E. Ressouches, J. Ollivier



Theory:

M. Hering, J. Reuther
F. Ferrari, A. Razpopov,, R. Valentí,
H.O. Jeschke
I. Mazin

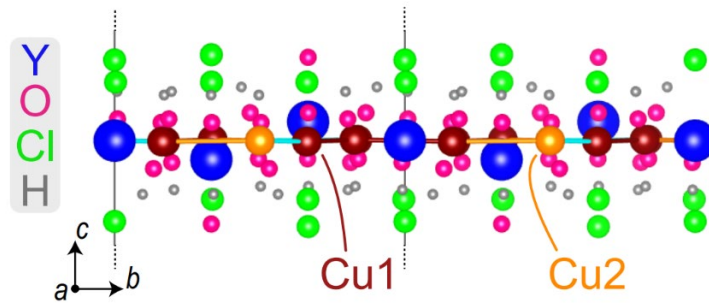
Chatterjee et al, PRB 107, 125156 (2023)

Y-Kapellasite, a new distorted kagome model



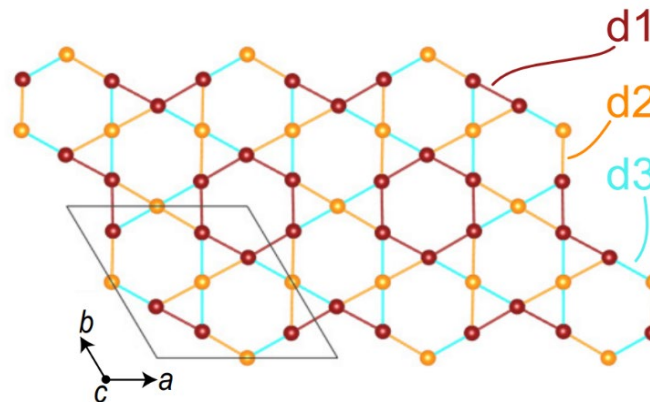
Charge doping herbertsmithite $\text{Zn}^{2+} \leftrightarrow \text{Y}^{3+}$? fails ☹️

-> new (anisotropic) kagome $\text{Y}_3\text{Cu}_9(\text{OH})_{19}\text{Cl}_8$ 😊

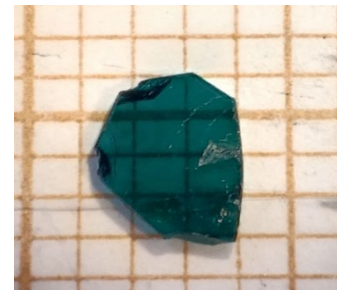

$$R\bar{3}$$

kapellasite-like AA stacking
No $\text{Cu}^{2+} \leftrightarrow \text{Y}^{3+}$ intersite mixing

Anisotropic kagome:
2 Cu sites
9 times larger unit cell



Puphal, J.Mat.Chem C (2017)
Sun, PRM (2021)
Barthélemy PRM (2019)



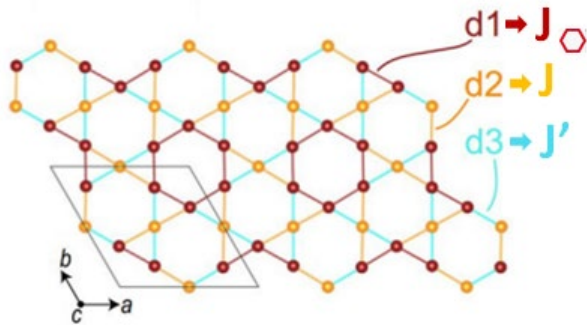
Y-Kapellasite, a new distorted kagome model



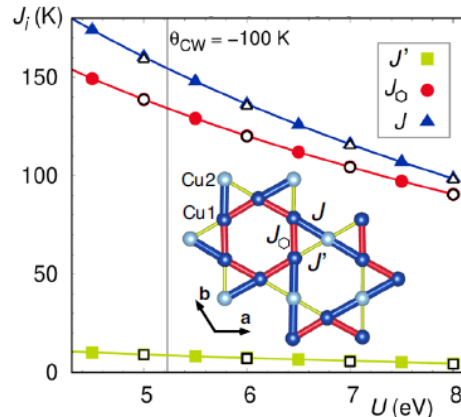
Phase diagram of a distorted kagome antiferromagnet and application to Y-kapellasite

Max Hering^{1,2}, Francesco Ferrari³, Aleksandar Razpopov³, Igor I. Mazin⁴, Roser Valenti³, Harald O. Jeschke⁵ and Johannes Reuther^{1,2}

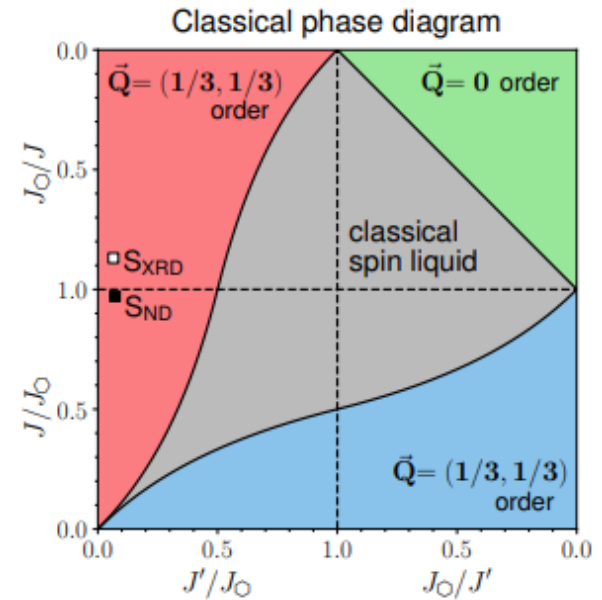
npj | Computational Materials 2022



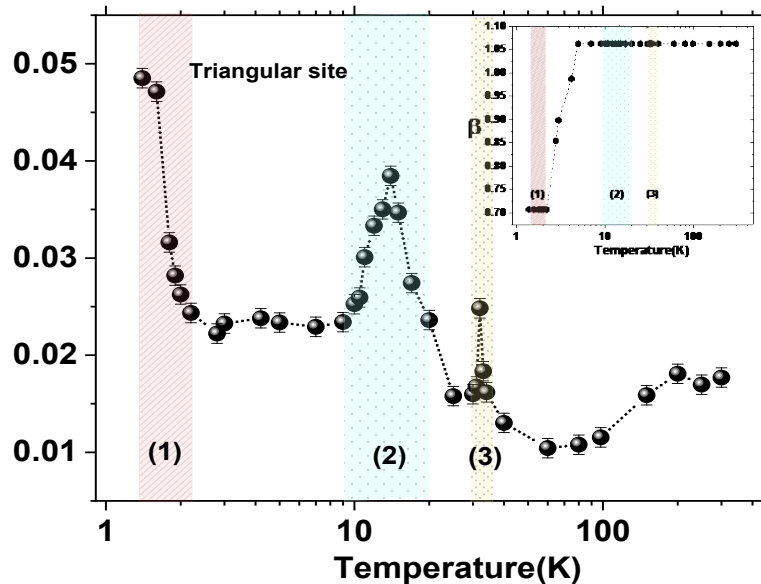
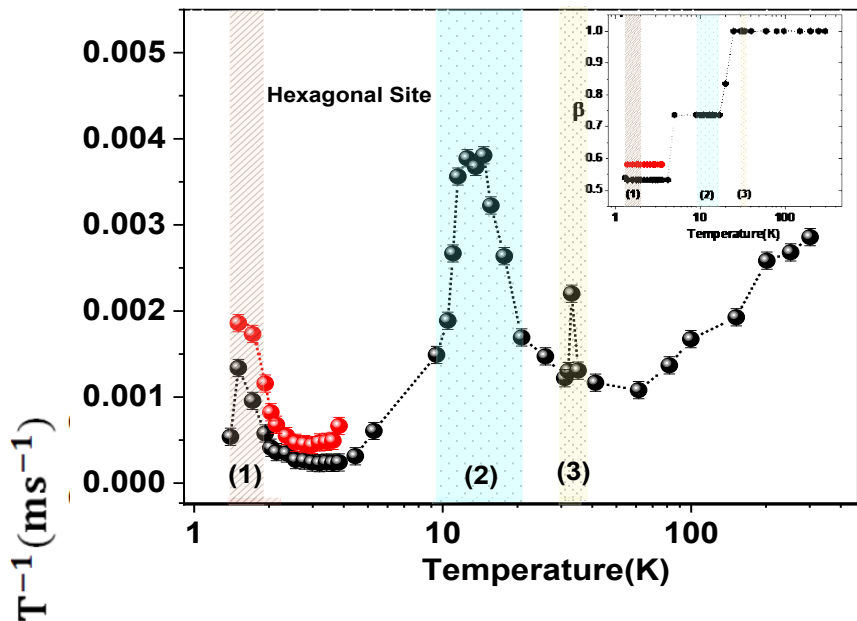
$d_1 = 3.353(8)$ ($Cu_1-O_2-Cu_1$) = 117.7°
 $d_2 = 3.328(11)$ ($Cu_2-O_4-Cu_1$) = 116.6°
 $d_3 = 3.314(8)$ ($Cu_1-O_3-Cu_2$) = 113.1°
 (In Zn-Kapellasite $105^\circ \rightarrow J = -15K$)



All other $J_i < J / 50$
 -1st nn model
 -strongly 2D
 -retains 6 fold rotation symmetry

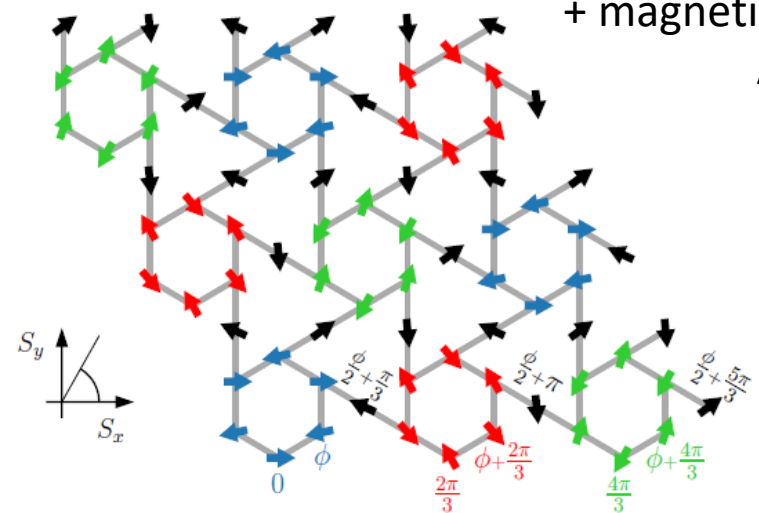


Transitions from CI NMR relaxation



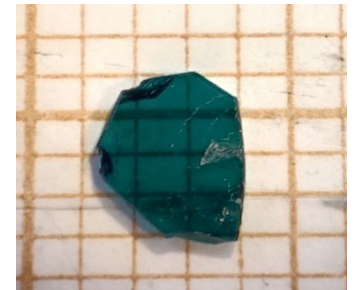
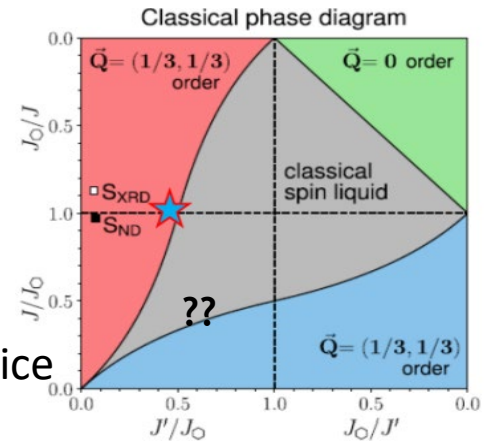
Structural transitions at 33K and around 12K
 + magnetic transition below 2K (also from μSR)
 All detected at both CI sites

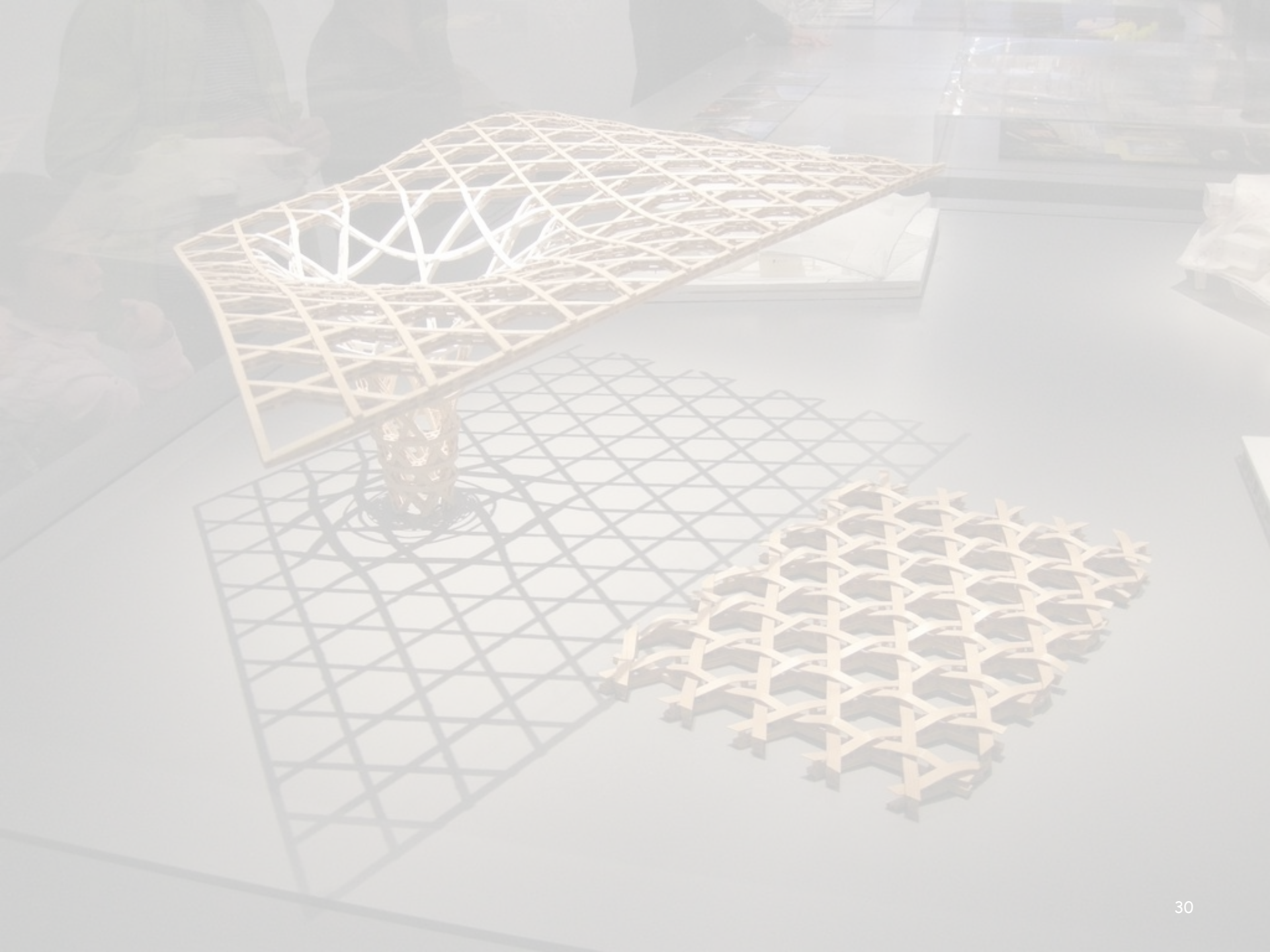
100% transition from μSR
 NMR consistent with predicted $Q=1/3, 1/3$ order
 Small moment $1/30 \mu_B$
 Fit of spin waves \rightarrow new estimate of the couplings



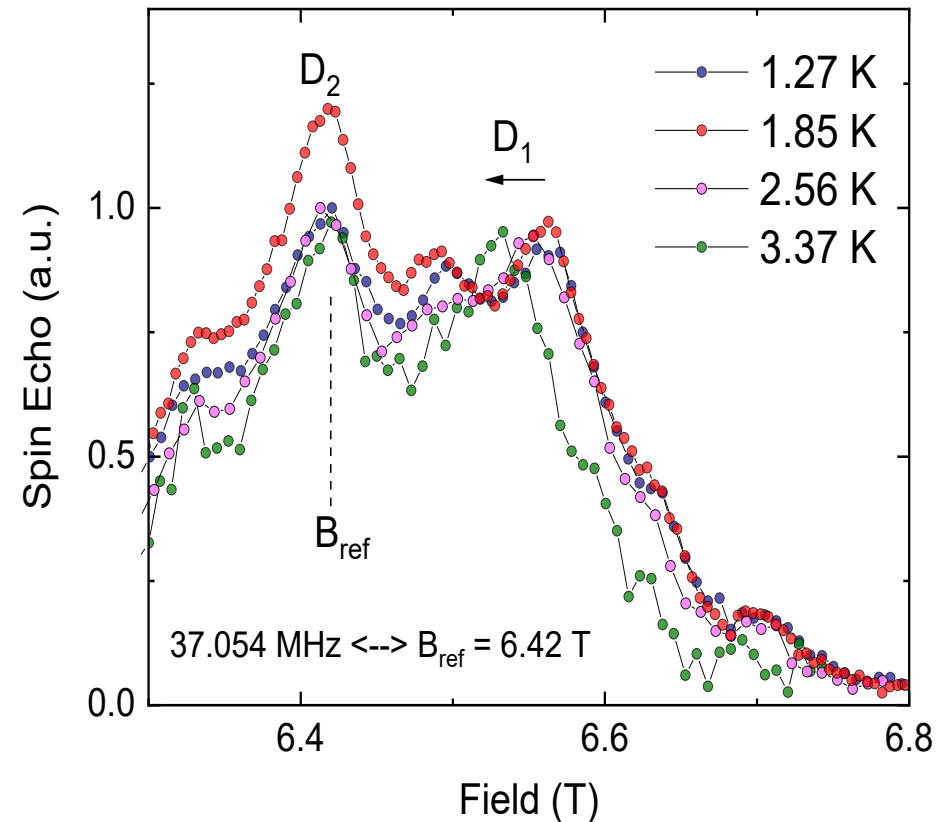
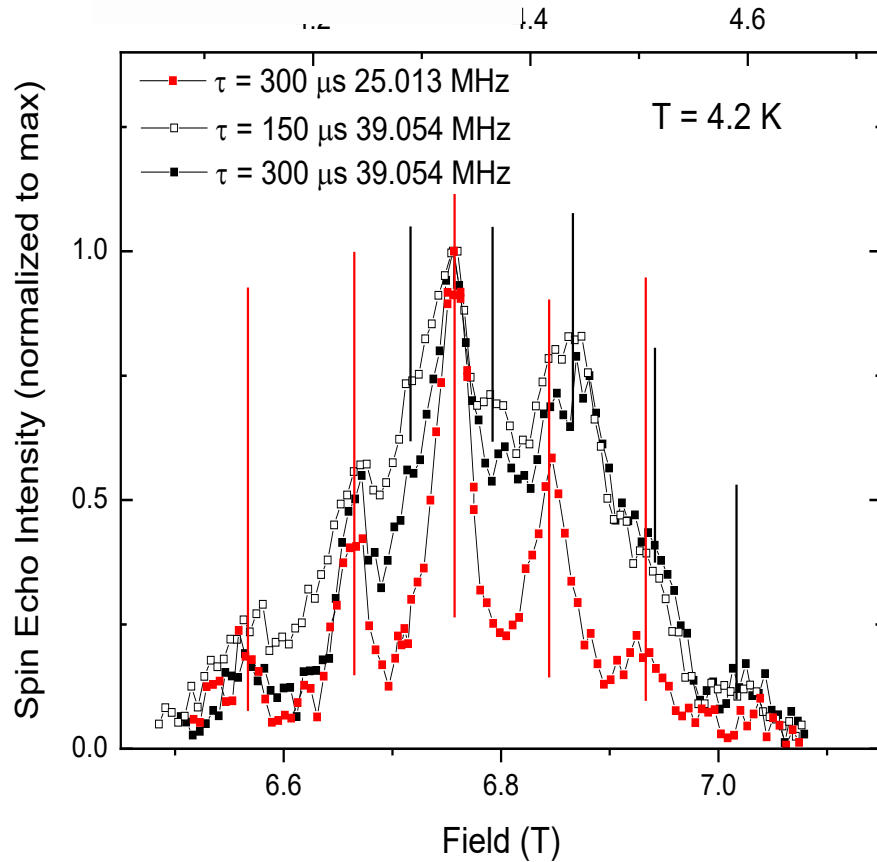
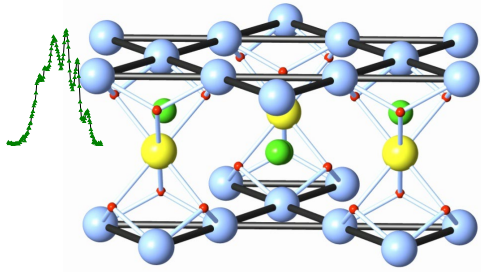
Conclusion Y-Kapellasite (single crystal)

- Y-Kapellasite features a new interesting magnetic model
- Long ranged magnetic $(1/3, 1/3)$ ordering at 2.1 K
+ Spin texture compatible with theory
but $J' \sim 0.45J_0$ and distributed,
locating Y-Kapellasite close to the 'classical spin liquid' phase
- Low value of magnetic moment $< 0.1 \mu_B$
- Role of 'disorder'/perturbation
 - 2 structural transitions (33K, 13K), not affecting the magnetic lattice
 - anisotropy DM ? (large in $x=0$)
- Strain releases frustration (J. Wang et al, arXiv:2209.08613)
- Spanning phase diagram $Y_3Cu_9(OH)_{19}Br_8$ (Zengh et al PRB 2022) ?
- Classical spin liquid phase? (Jammed SL, Bilitewski et al, PRL 2017)
Quantum fluctuations close to CSL phase (or in)?





Two O sites -> two types of defects; T_2 contrast



Exchange constants: n.n. Heisenberg model

First-principles determination of Heisenberg Hamiltonian parameters for the spin-1/2 kagomé antiferromagnet $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

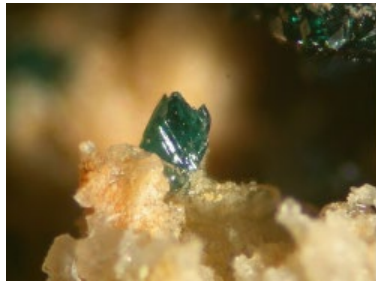
Harald O. Jeschke,* Francesc Salvat-Pujol, and Roser Valentí
*Institut für Theoretische Physik, Goethe-Universität Frankfurt,
Max-von-Laue-Strasse 1, 60438 Frankfurt am Main, Germany*
(Dated: February 5, 2018)

TABLE V: Exchange coupling constants for $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ (herbertsmithite) determined from total energies of nine different spin configurations. Energies were calculated with GGA+U functionals at $J = 1$ eV with different values of U and with atomic limit double counting correction.

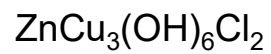
name	d_{Cu-Cu}	type	J_i (K)	J_i (K)	J_i (K)
			$U = 6$ eV	$U = 7$ eV	$U = 8$ eV
kagomé layer couplings					
J_1	3.4171	kagomé nn	182.4	155.4	131.8
J_3	5.91859	kagomé 2nd nn	3.4	2.9	2.3
J_5	6.8342	kagomé 3rd nn	-0.4	-0.5	-0.4
interlayer couplings					
J_2	5.07638	interlayer 1st nn	5.3	4.5	3.7
J_4	6.11933	interlayer 2nd nn	-1.5	-1.1	-0.8
J_6	7.00876	interlayer 3rd nn	-6.4	-5.4	-4.4
J_7	8.51328	interlayer 4th nn	3.0	2.5	2.1
J_9	9.17347	interlayer 6th nn	2.5	2.1	1.7

Materials are mostly existing minerals

all based on Cu^{2+} $S=1/2$



Herbertsmithite



MP Shores et al, JACS, 2005



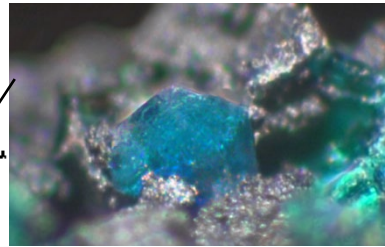
Völborthite

Z. Hiroi et al, JPSJ
2001



Brochantite,

Y. Li et al, New J. Phys. 2014



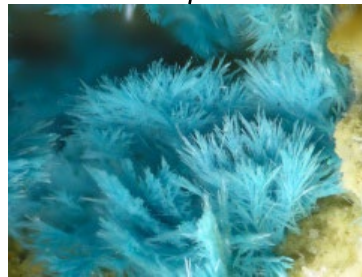
Barlowite

Han et al, PRL 2014



Haydeeite

R. Colman et al, Chem. Mater. 2010



Kapellasite

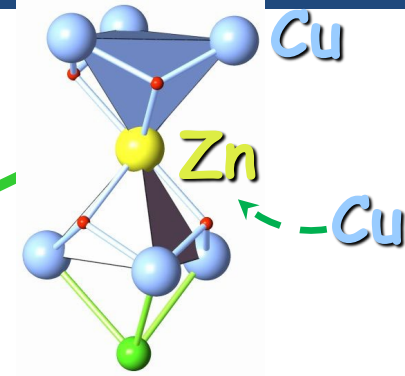
R. Colman et al, Chem. Mater. 2008



Vesignieite

Y. Okamoto et al, JPSJ 2009

Site selective spectroscopy: ^{17}O NMR



~15% Cu on the Zn site
Nearly free $\frac{1}{2}$ spins

✓ Low-T NMR ($7 \cdot 10^{-3} \text{ J} - 0.1 \text{ J}$):

$$K_{\text{spin}} = A_{\text{hf}} \chi_{\text{loc}}(q=0, \omega=0)$$

$K \rightarrow \chi$ defect contribution

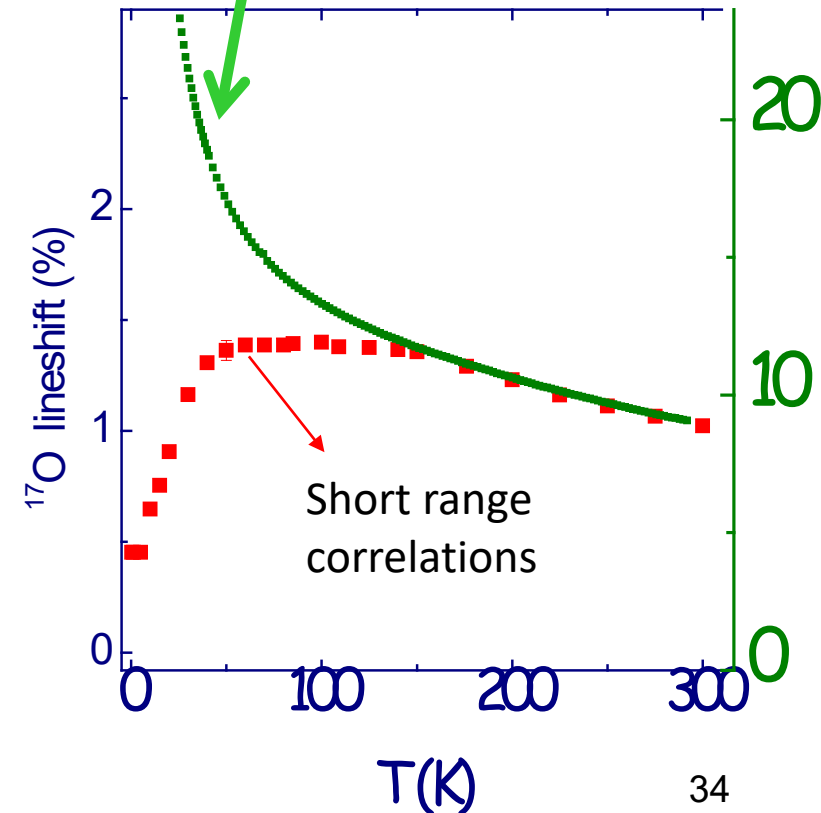
intrinsic contribution: analysis

T_1 dynamics

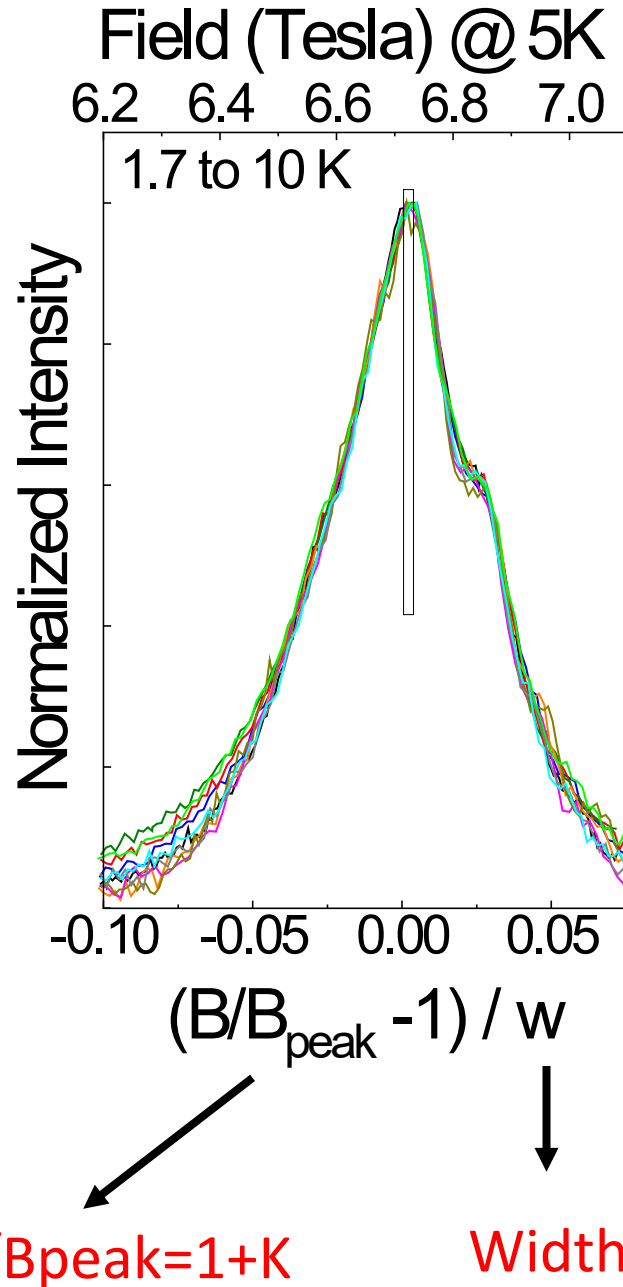
$$\frac{1}{T_1} = \frac{1}{\hbar^2} \frac{k_B T}{(g\mu_B)^2} \sum_q |A(q)|^2 \frac{\chi''(q, \omega_n)}{\omega_n}$$

✓ Issue: what is the so-called « defect »

✓ What is the « defect » impact on the pure kagome physics



Shift: T1 contrast and scaling



A gapless Dirac model ?

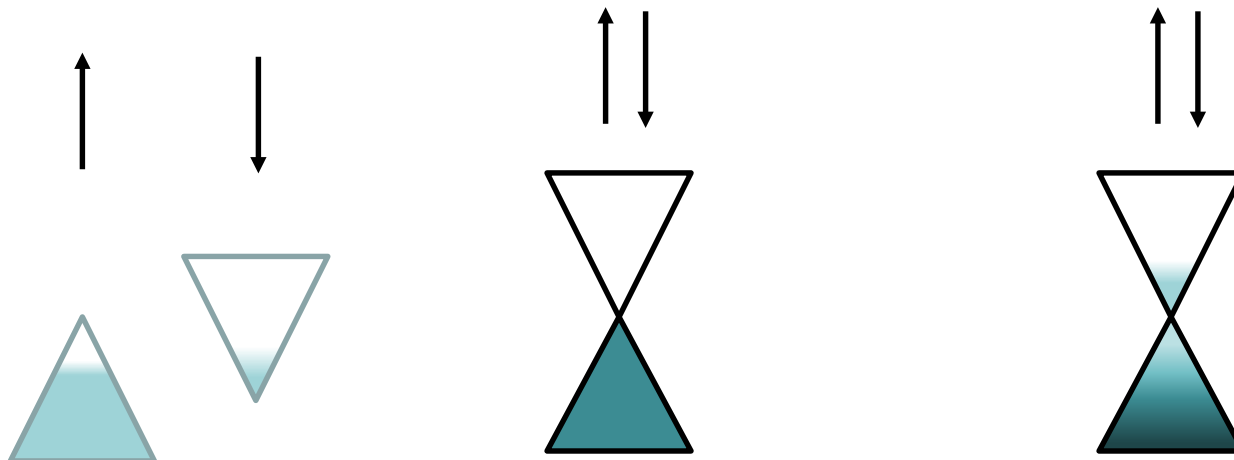
Two energy scales: kT vs $\mu_B B$

$kT \ll \mu_B B$ (spinon pockets)

1. finite χ B at $T=0$
2. $C \propto T$ for $T \rightarrow 0$
3. $1/T_1$ algebraic in T

$kT \gg \mu_B B$ (Dirac cones)

1. Susceptibility : χ linear in T
2. Specific heat $\sim T^2$
3. $1/T_1$ algebraic in T



$T = 0$ and $B = 0$

A gapless Dirac model ?

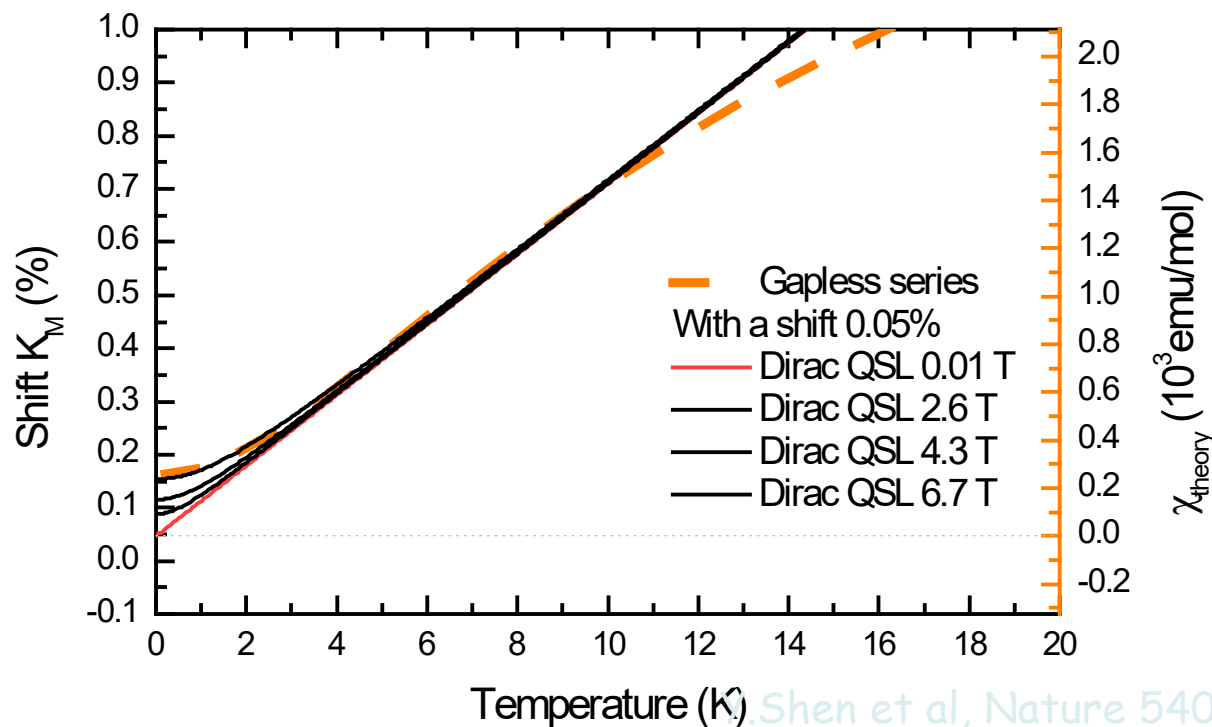
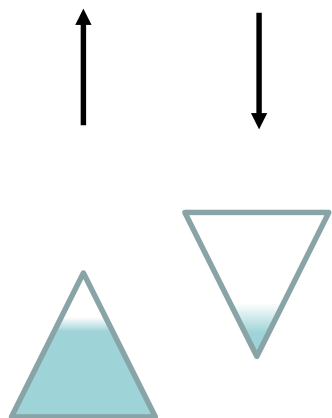
Two energy scales: kT vs $\mu_B B$

$kT \ll \mu_B B$ (spinon pockets)

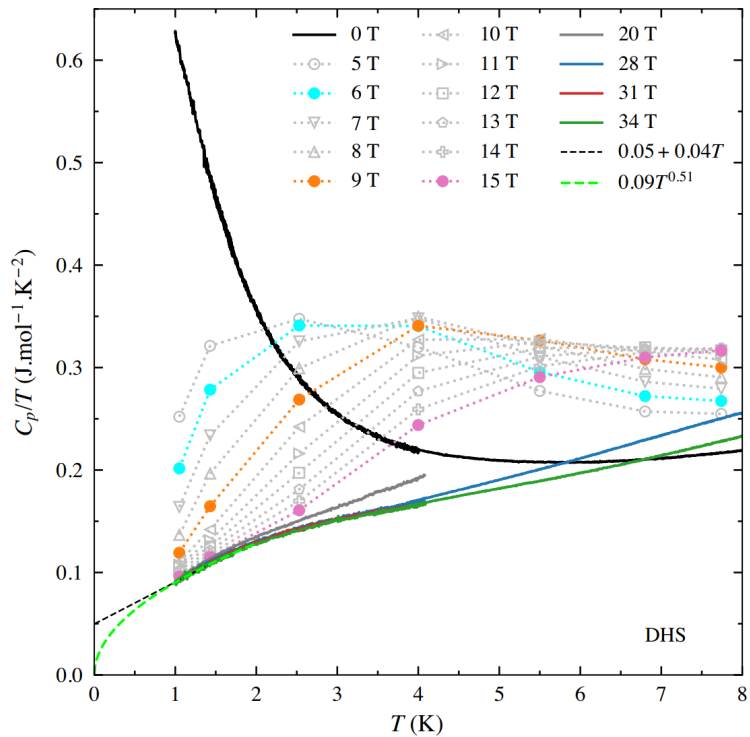
1. finite χ at $T=0$
2. $C \propto T$ for $T \rightarrow 0$
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$kT \gg \mu_B B$ (Dirac cones)

1. Susceptibility : χ linear in T
2. Specific heat $\sim T^2$
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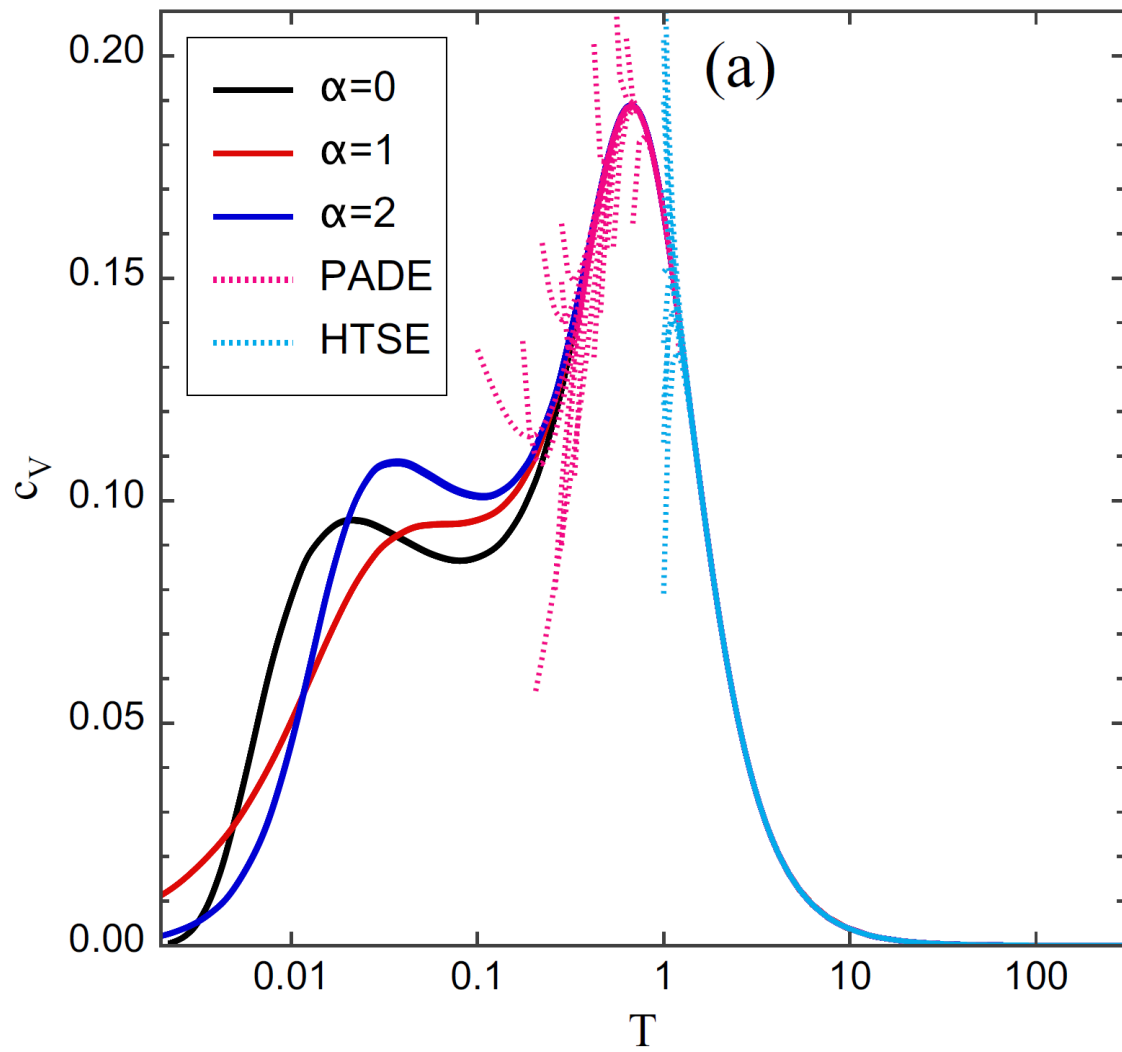
Direct measurement of C^{kago}

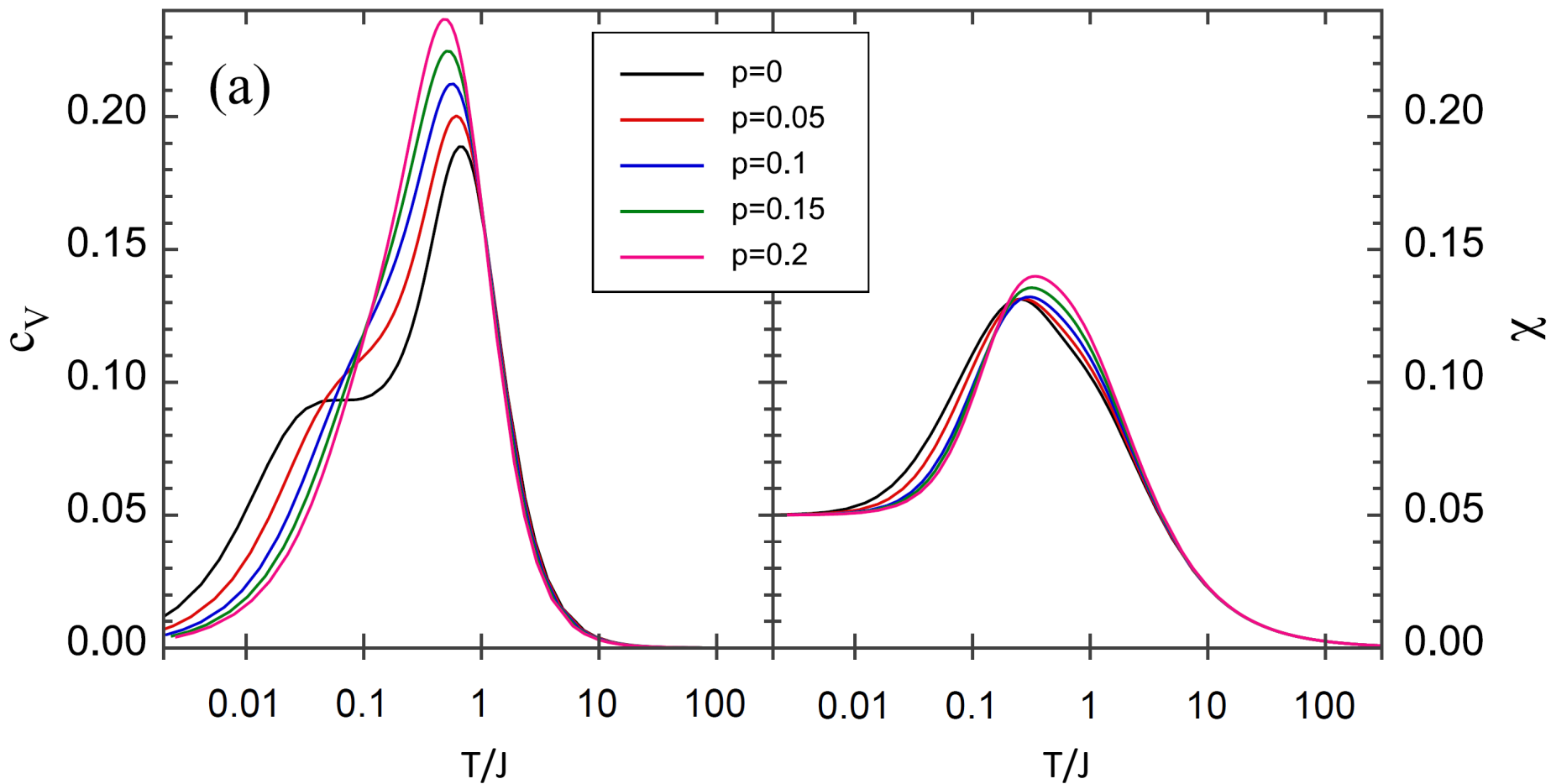


Field-independent for $1 \leq T \leq 4$ K and $28 \leq B \leq 34$ T

$1.21 \sim q = 1.3(1)$: effective (impurity-induced) dilution of the kagome planes

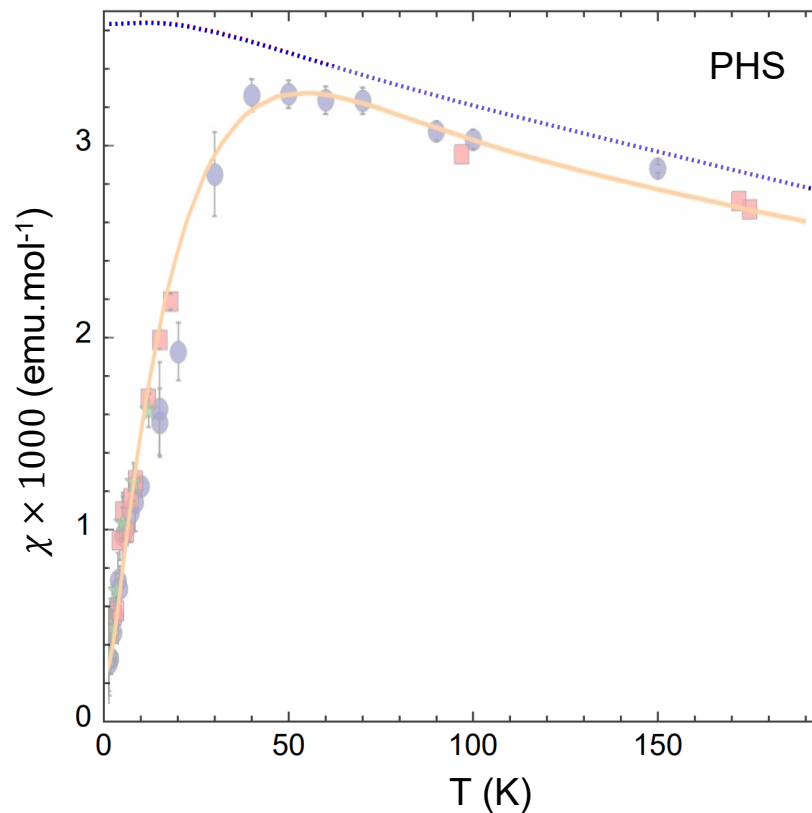
Tentative extrapolation: unusual power law $C_p(T \rightarrow 0) \propto T^\alpha$ with $\alpha \sim 1.5$





Fitting series for C_p does not match NMR susceptibility

Q. Barthélemy et al., Phys. Rev. X (2022)



- ✓ Susceptibility deduced from series inconsistent with NMR (too large / more dependent on B)
- ✓ **But** susceptibility deduced from ^{17}O NMR is for 60% of the fast relaxing sites «far from defects»

Analysis with the HTSE+s(e) Method

Khuntia et al., Nat. Phys. 16 (2020)
 Bernu et al., Phys. Rev. B 101 (2020)
 Barthélemy et al., Phys. Rev. X 12 (2022)



B. Bernu
LPTMC Paris

L. Messio
LPTMC Paris

HTSE+s(e):
 extrapolations of high- T series expansions
 with the entropy method.

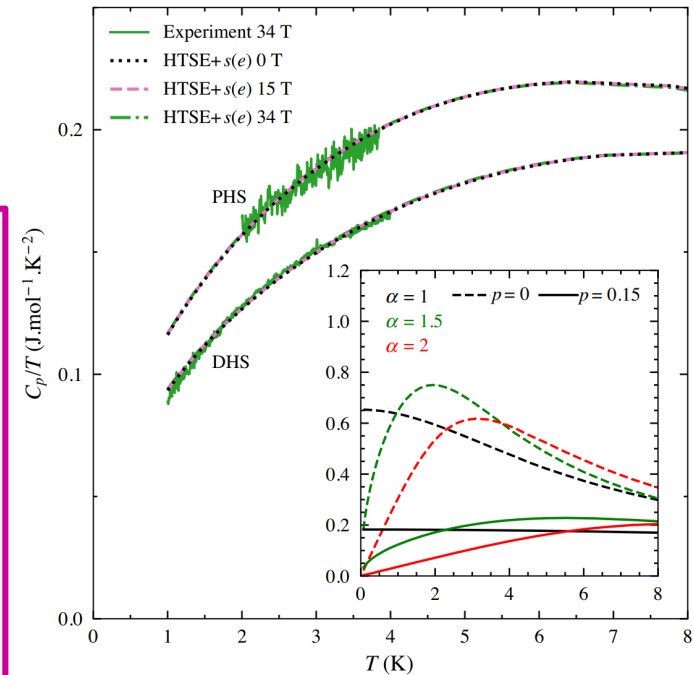
→ The HTSE+s(e) computations fit the experimental data if and only if:

1. We set a **nontrivial power law** $C_p(T \rightarrow 0) \propto T^\alpha$ with $\alpha \approx 1.45$.
2. We set a **dilution of the kagome planes**: random vacancies with concentration p .
 $p \sim 13.5\%$ for DHS and $p \sim 11\%$ for PHS.
Note that the p ratio matches the low- T Curie constants ratio $q = 1.3(1)$.

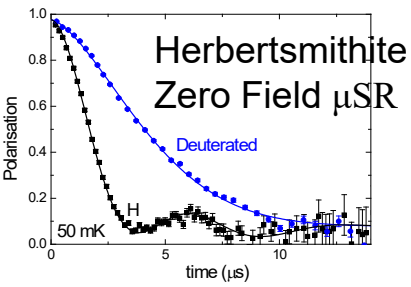
→ The optimized ground state energy follows $e_0(B, p) = e_{00}(p) - A(p)B^2$.

→ The optimized C_p is **field-independent** on a large field range up to about 150 T.

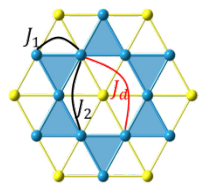
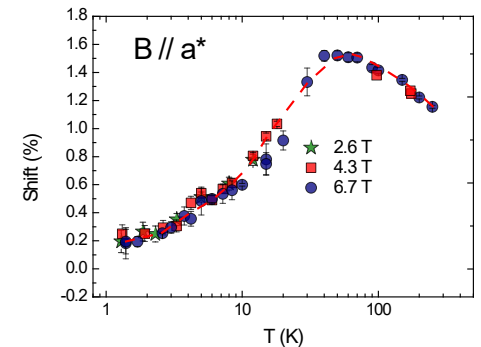
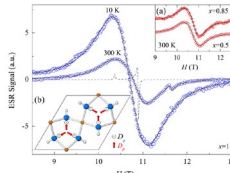
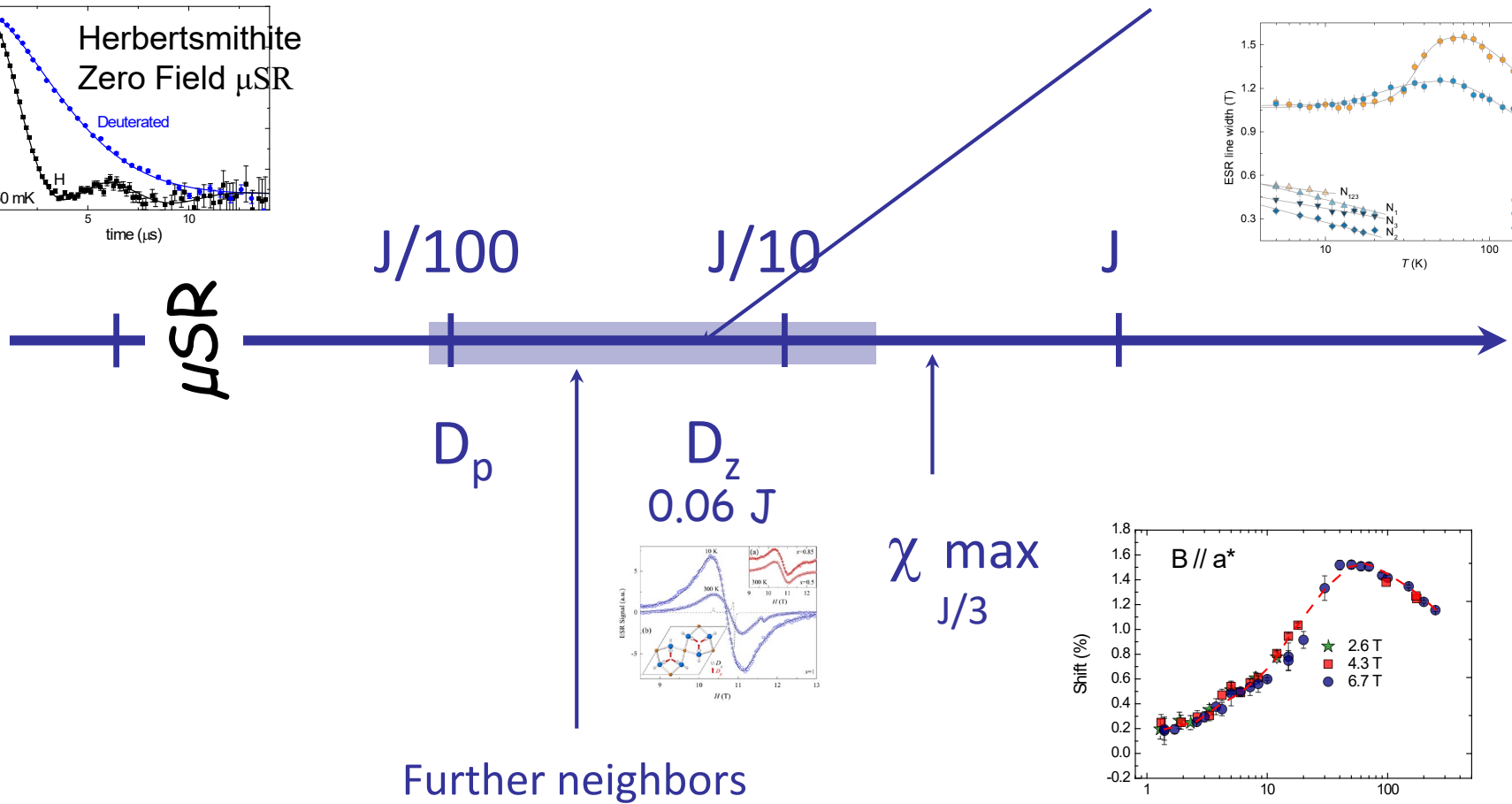
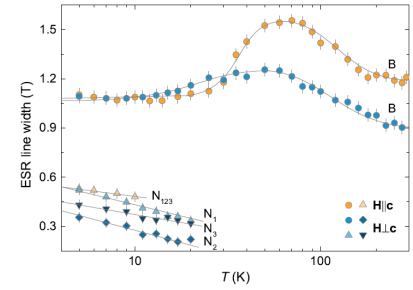
→ With the C_p parameters, the optimized χ_0 is about **10 times larger than the NMR χ_0** .



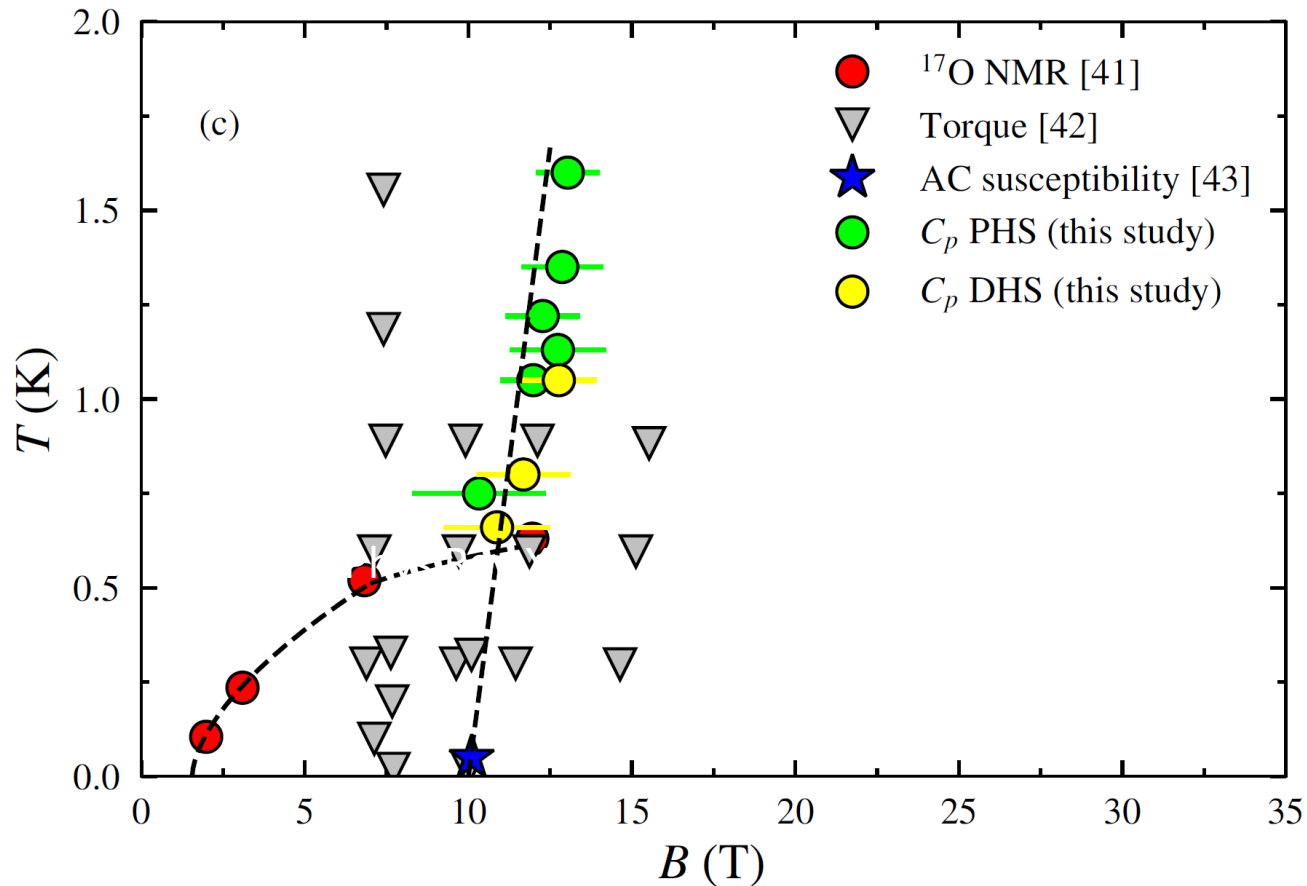
Energy scales (J = 190 K)



Exchange anisotropy



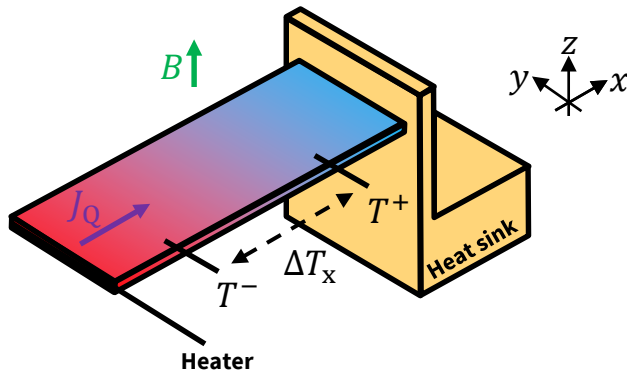
Field- induced crossover from QSL to ???



- M. Jeong et al, PRL 107, 237201 (2011): frozen moments $\sim 0.1 \mu_B$
- ▼ T. Asaba et al, PRB 90, 64417 (2014)
- ★ J. Helton, PhD (2009)
- Q. Barthélemy, PRX (2022)
-

(No?) Mobile Spin Excitations

Huang et al., *Phys. Rev. Lett.* 127 (2021)
Murayama et al., *arXiv* 2106.07223 (2021)

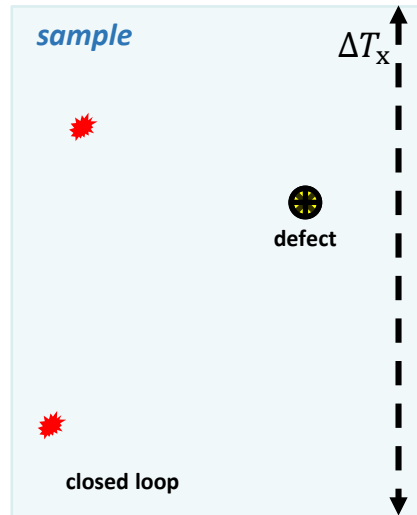


Longitudinal thermal conductivity:

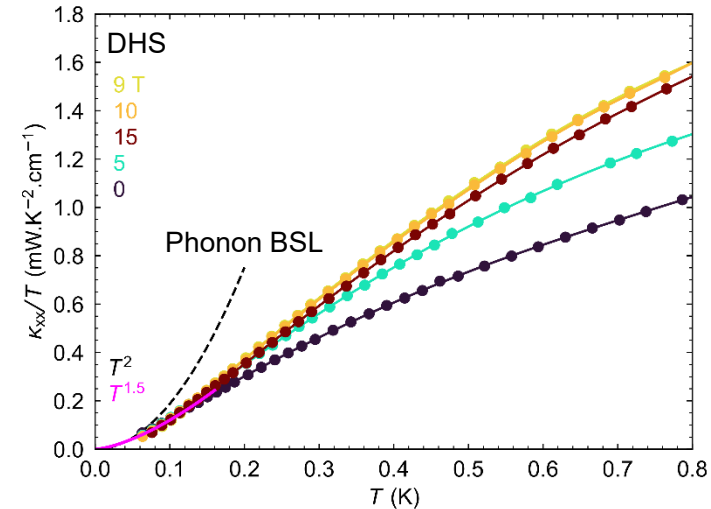
$$\kappa_{xx} \propto \frac{J_Q}{\Delta T_x}$$

It probes the **mobile heat carriers**: phonons +

...



Thermal transport: is it really conclusive?

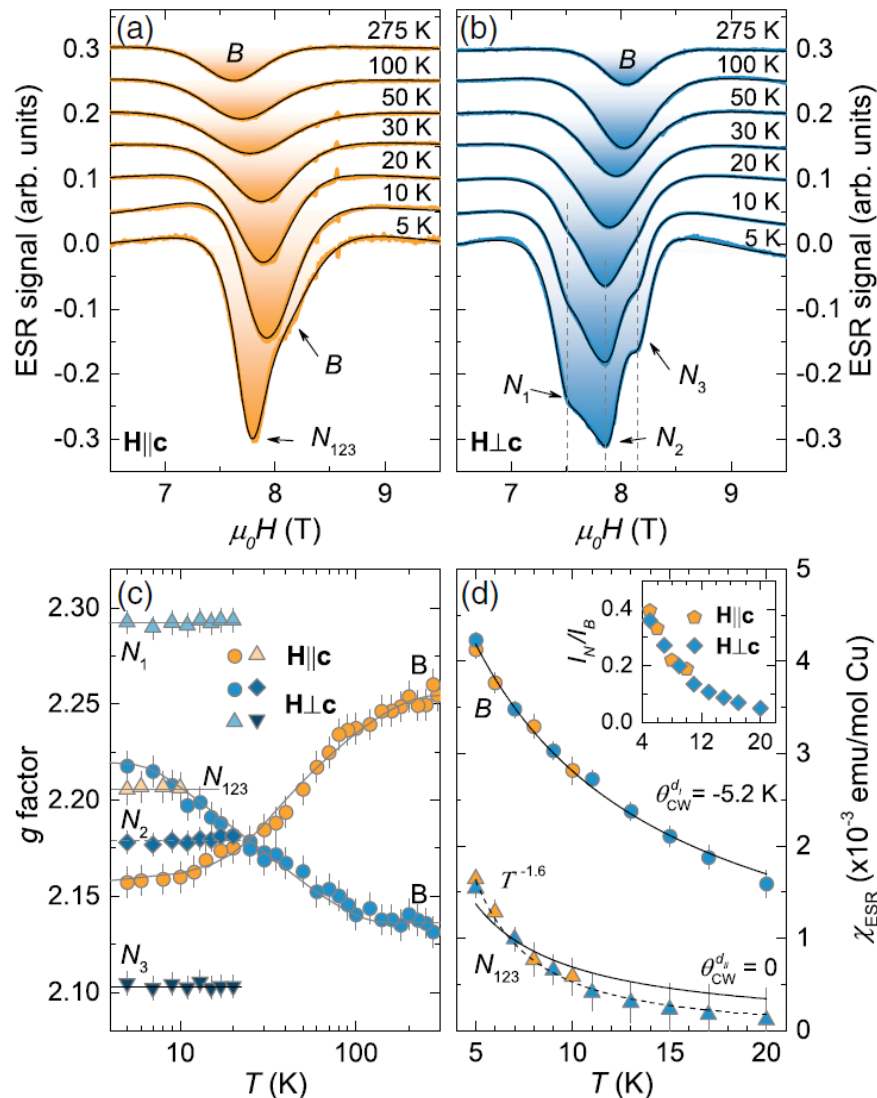


→ In zero field, **no sizeable residual term** in the $T \rightarrow 0$ limit \Rightarrow **phonons are the main heat carriers**. Compatible with recent reports.

→ **Low magnitude & field dependence** \Rightarrow phonons are **strongly scattered by some magnetic degrees of freedom**.

→ Scattering centers: **the (localized?) QSL excitations** and the **defects**.

ESR at low T, dominated by defects: 2 types

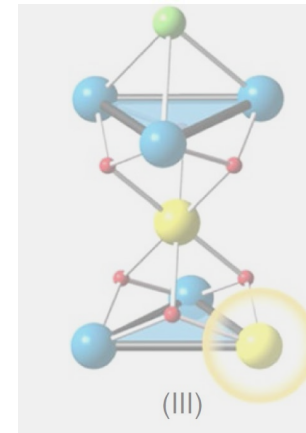
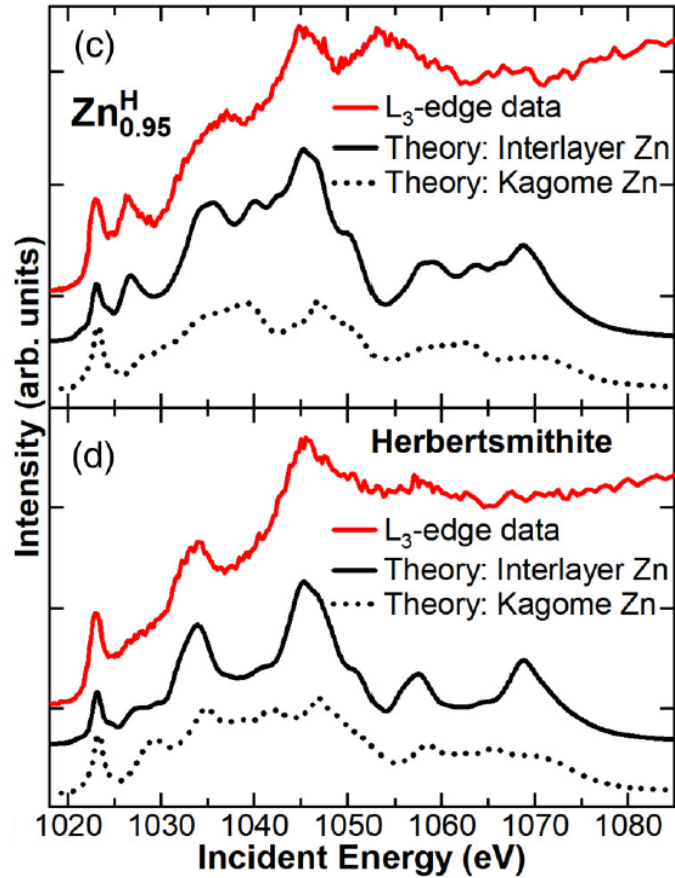


(B) Coupled defect to kagome
 (N) weakly coupled defects,
 In plane defect or induced effect in
 the plane!

Lowering of symmetry: tiny effect

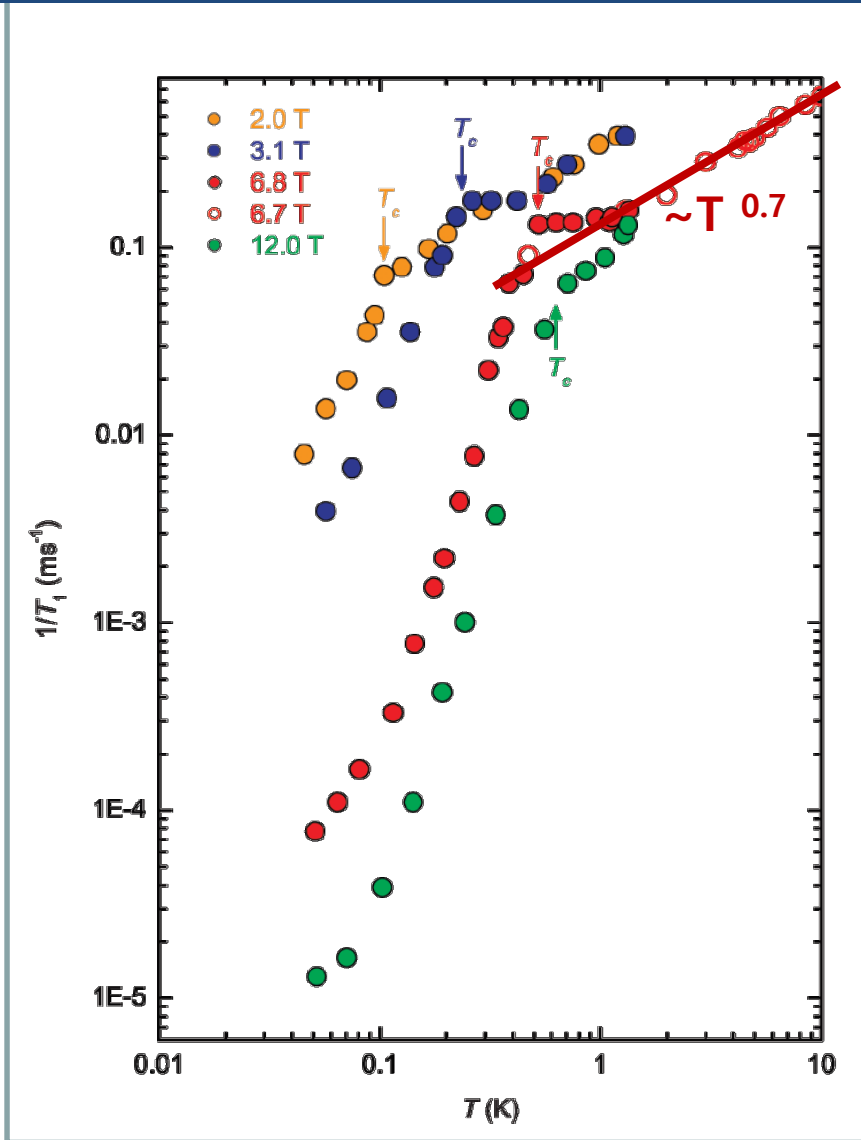
ESR, Torque, Zorko et al., PRL (2017)
 ^{17}O NMR, M. Fu et al., Science (2015)
 2nd harmonic, N.J. Laurita, ArXiv (2019)
 CI NMR ?, T. Imai et al., PRL (2008)
 Infrared, A.B. Sushkov, JPCM (2017)

X-ray absorption near edge spectroscopy

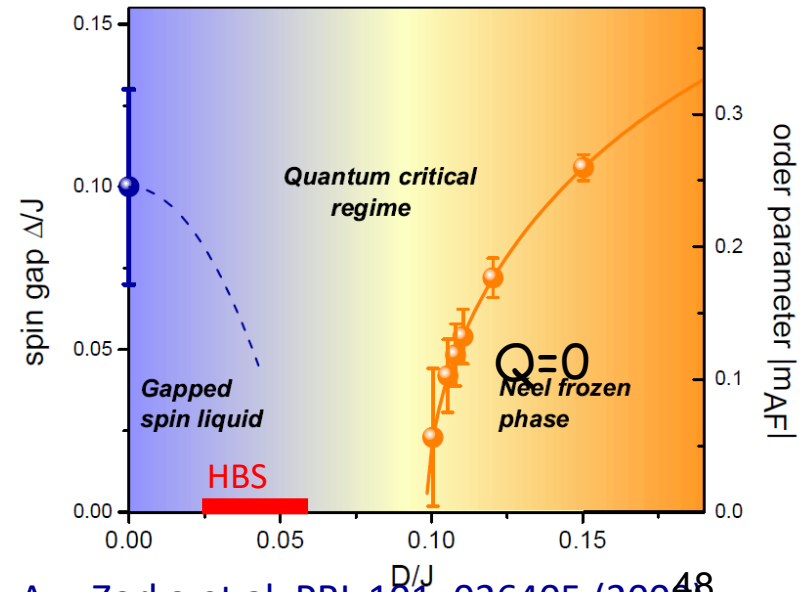
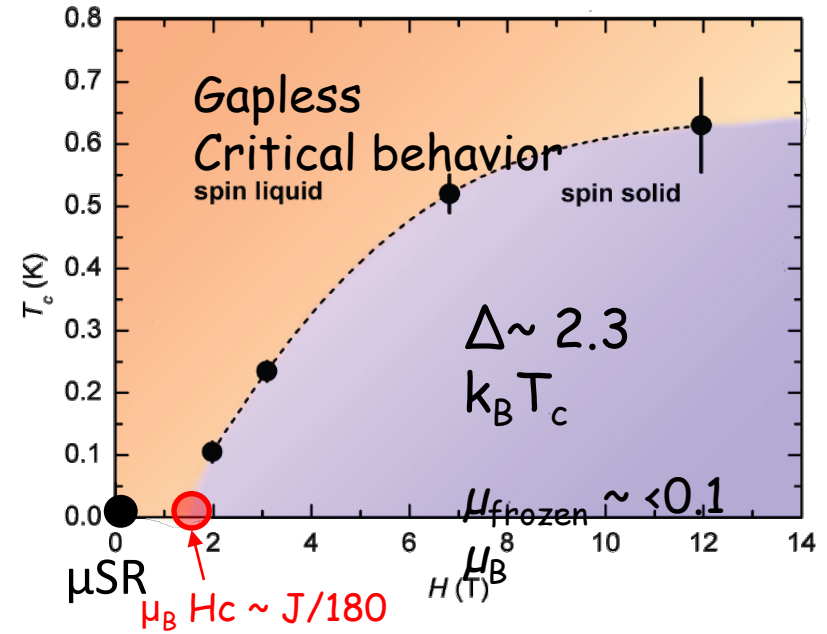


Smaha et al. PhysRevMaterials.4.124406

Evading the QSL phase : $T \sim 1K$ under applied field

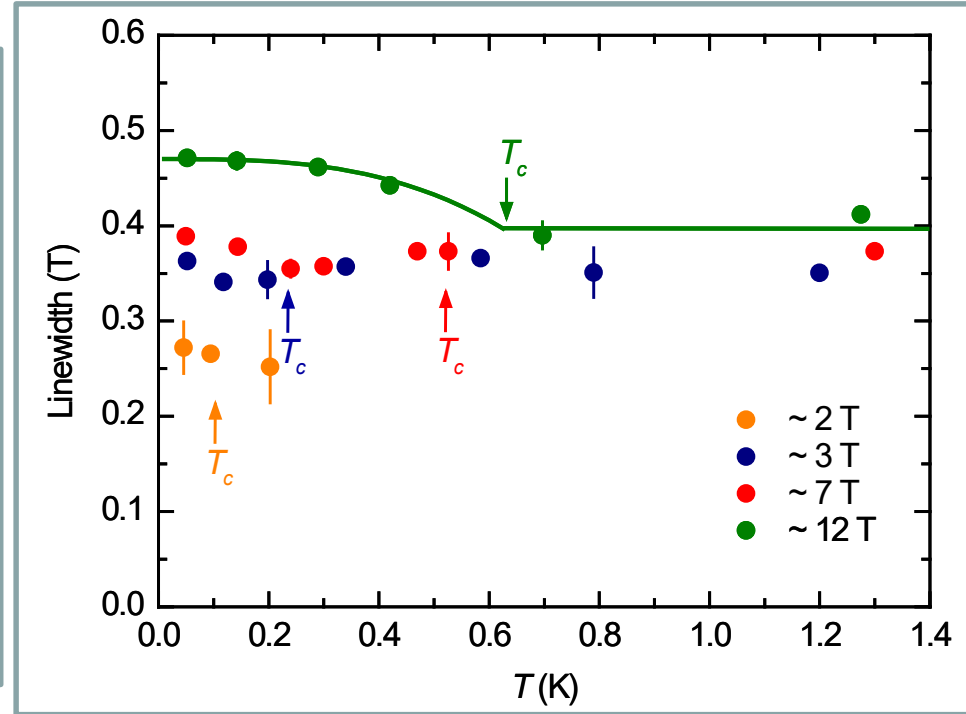
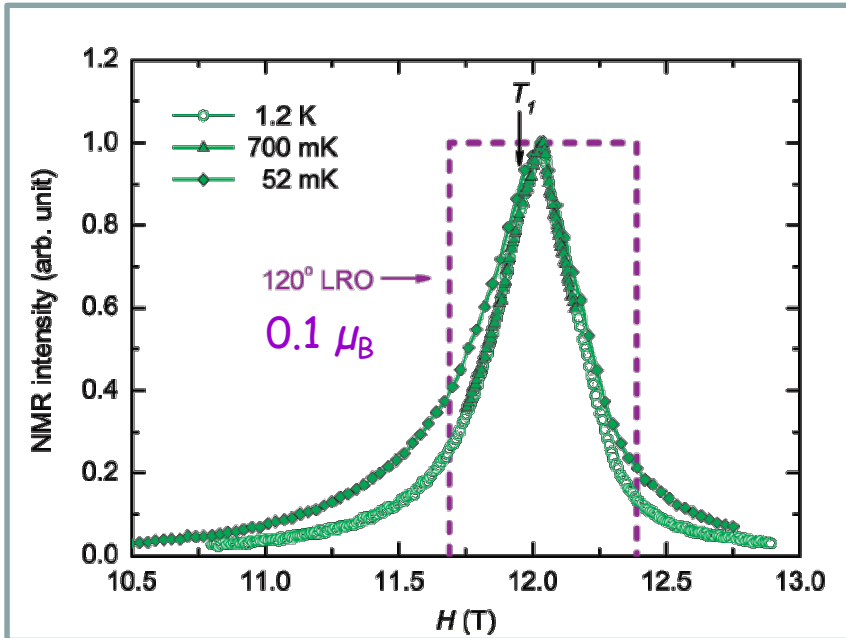


M. Jeong et al, PRL 107, 237201 (2011)
 Q. Barthélemy, PhD



A. Zorko et al, PRL 101, 026405 (2008)
 S. El Shawish et al, PRB 81, 224421 (2010)

Very Small frozen moment



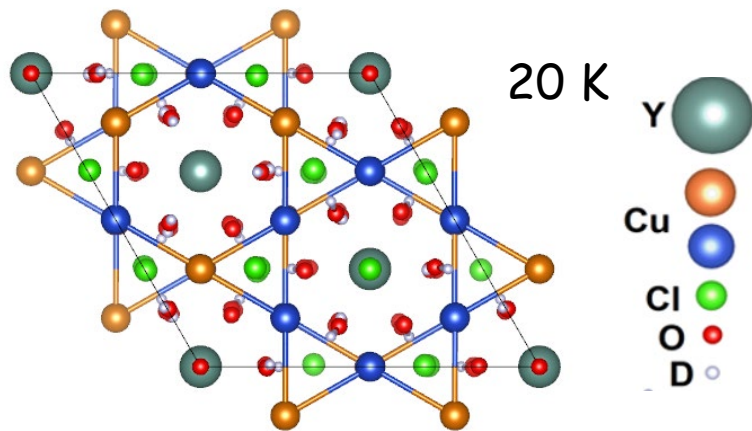
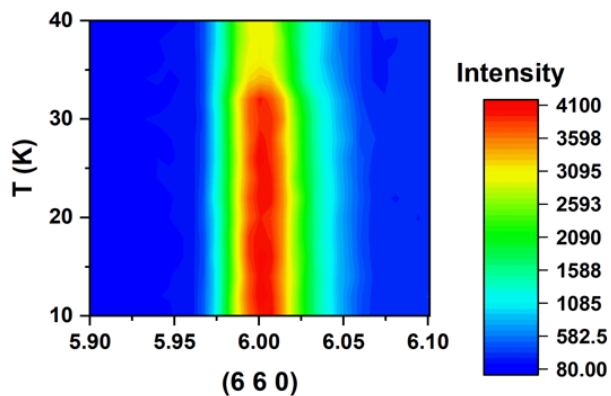
-No long range order but frozen state

-Hyperfine constant: $3.5 \text{ T}/\mu_B$

$\mu_{\text{frozen}} \sim 0.1 \mu_B$ @ 12 T

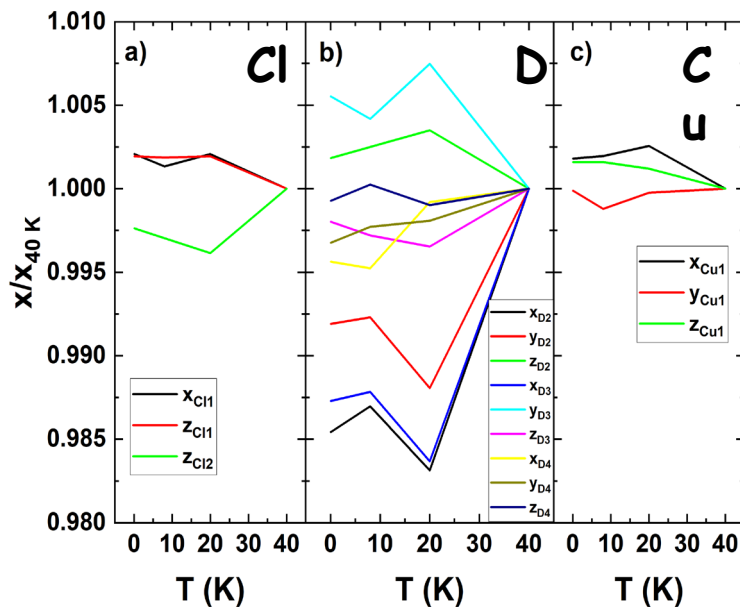
μ_{frozen} even smaller for smaller H

Neutron diffraction measurements

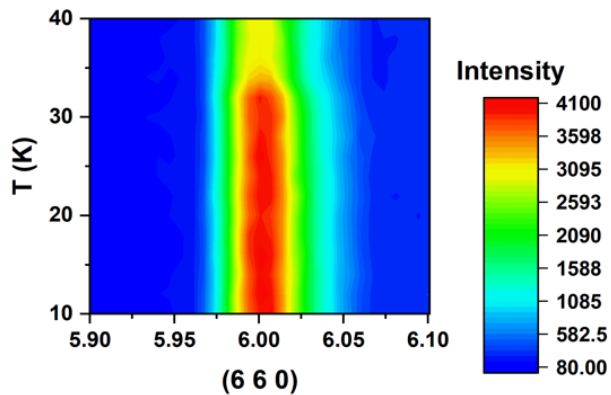


No additional Bragg peaks down to 65mK
but intensities change at **33 K**

Transition preserves the crystal symmetry (on average)
involves mostly small changes in the hydrogen positions.

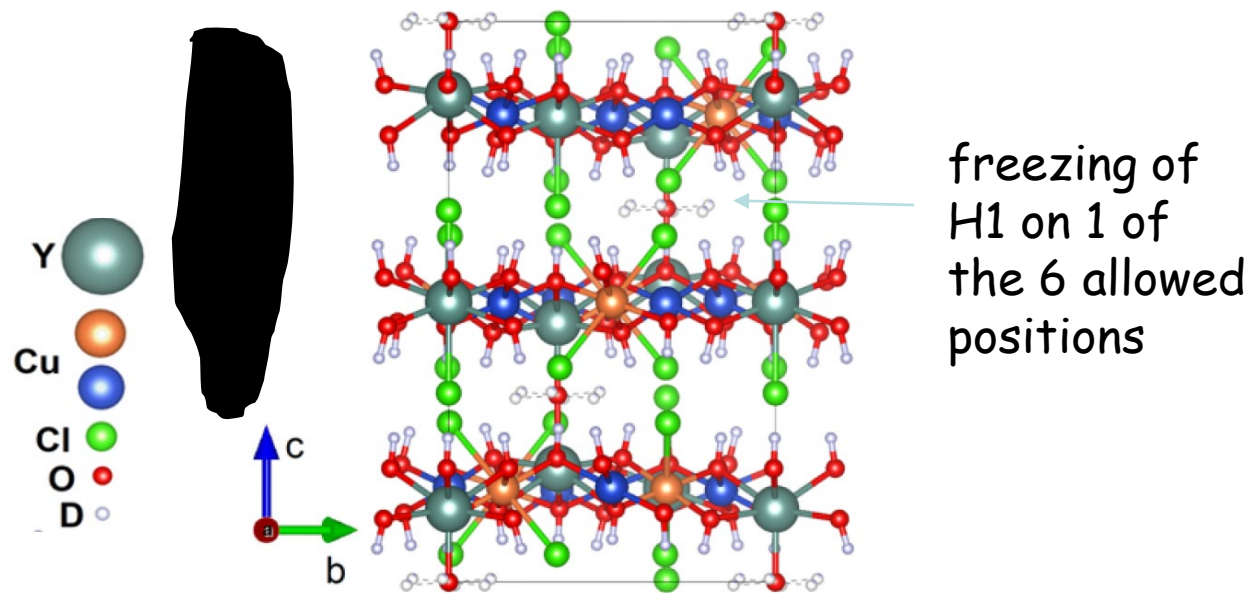


Neutron diffraction measurements

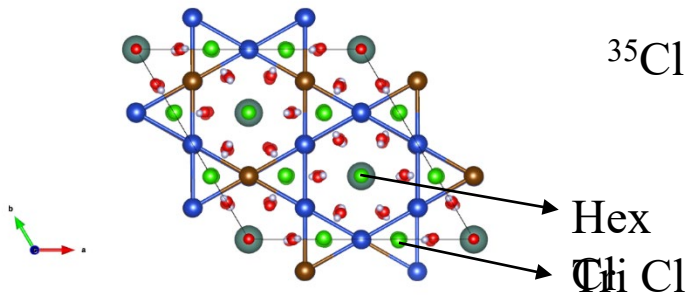


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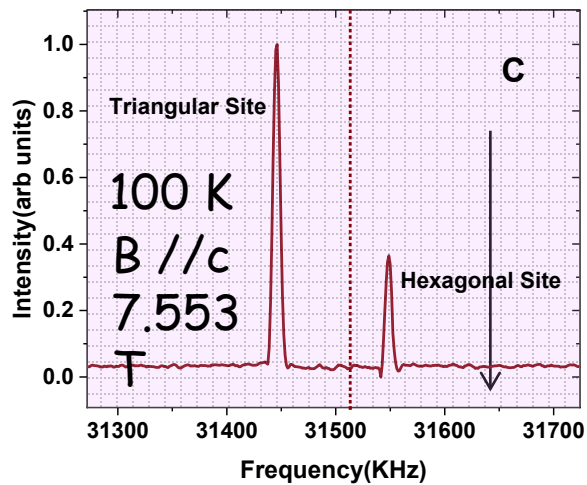
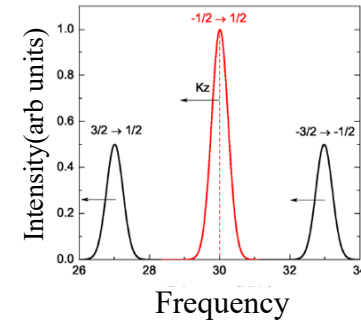
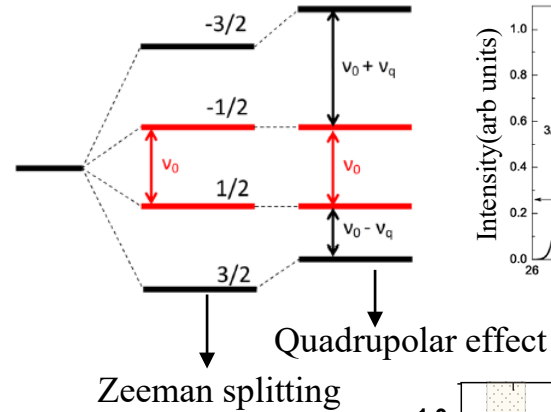
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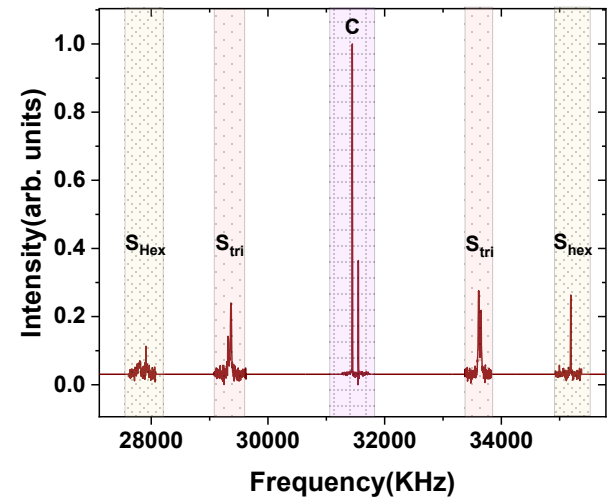
^{35}Cl NMR in structurally distorted kagome lattice



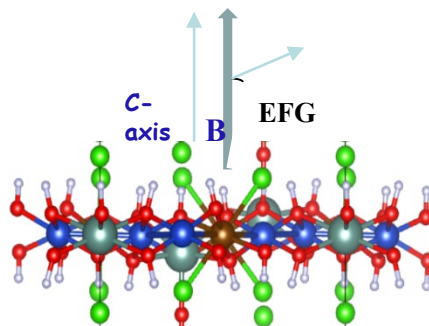
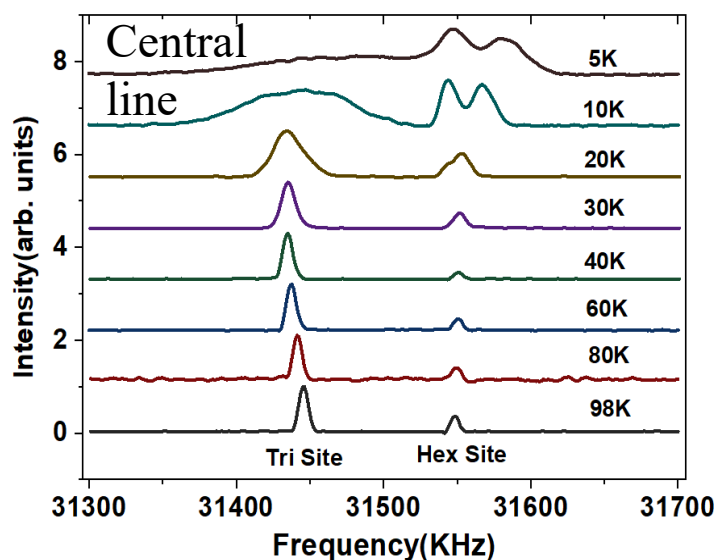
^{35}Cl $I=3/2$



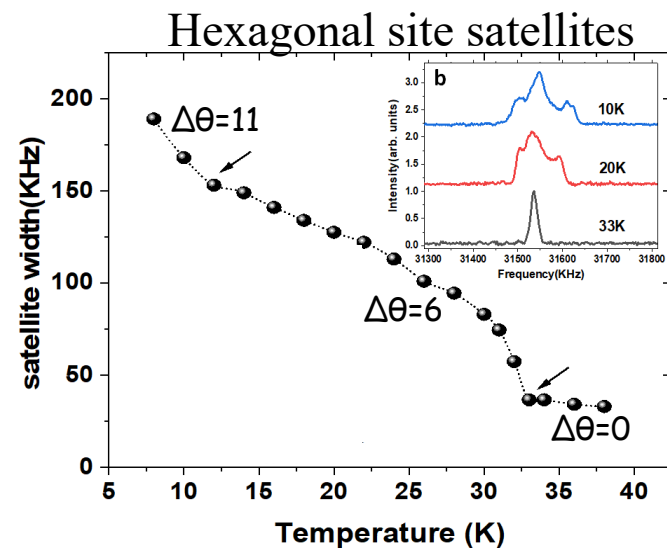
2 sites ✓
Intensity ratio 3:1 ✓



Structural transition from NMR local probe

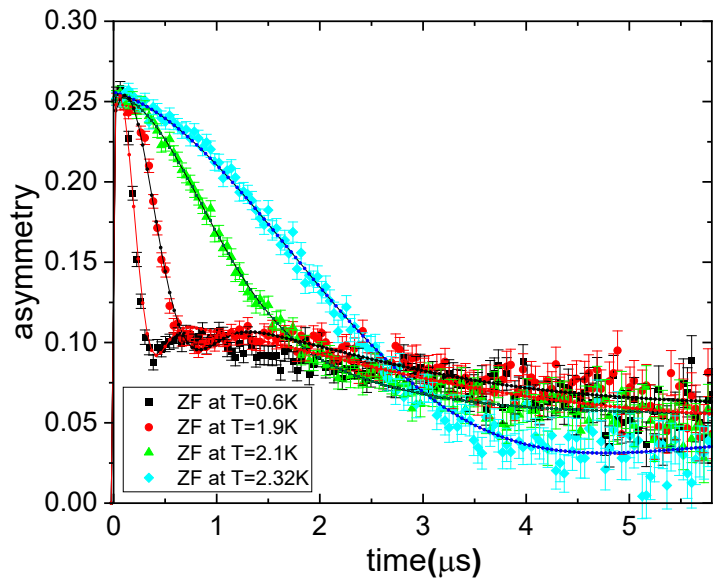


$\Delta\theta \sim 5^\circ$ at 20 K
and around $\sim 10^\circ$
at 10 K



Marked changes at 33K and around 12K
Multiple Cl sites with rotated local EFG
 \neq average structure from neutron

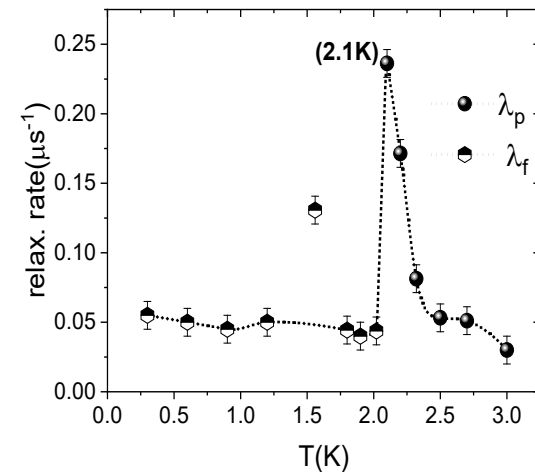
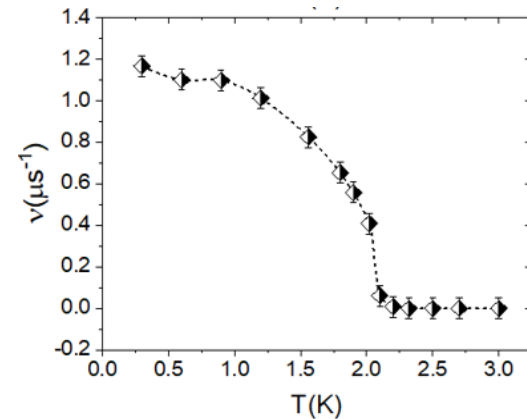
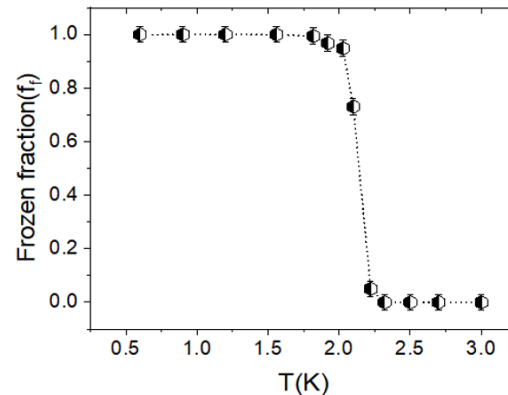
Muon spin relaxation measurements



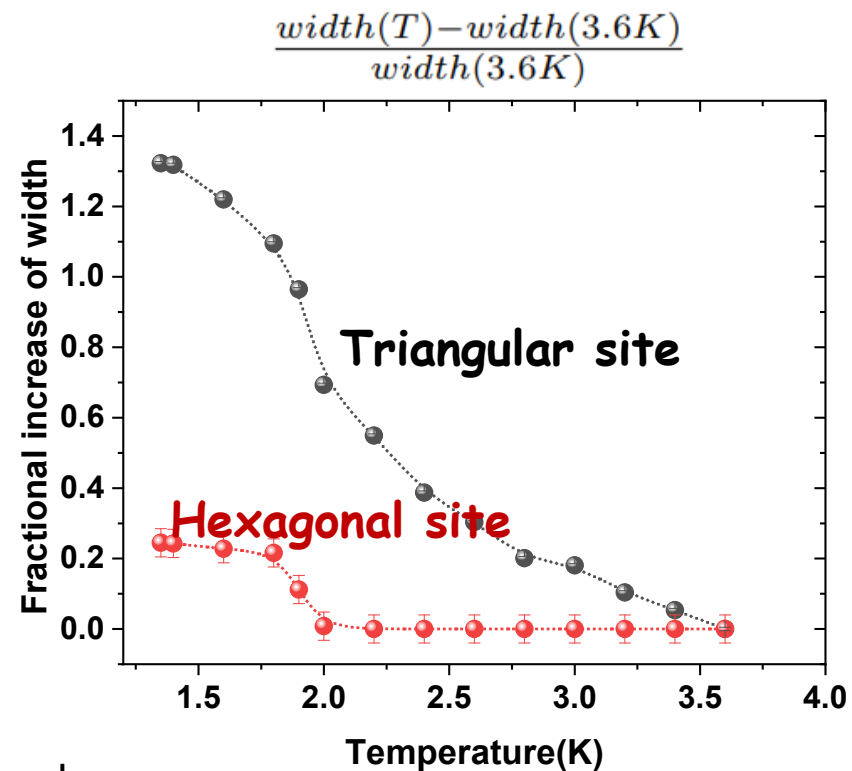
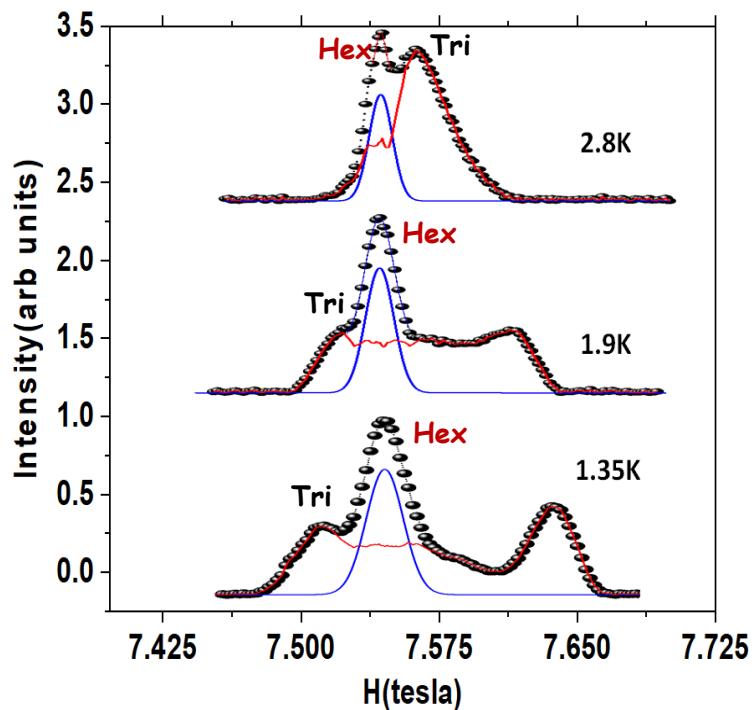
Complete transition at 2.1 K

Frozen moment $\sim 0.03 \mu_B$

Strongly damped oscillations, SRO //c?, multiple stopping sites...)



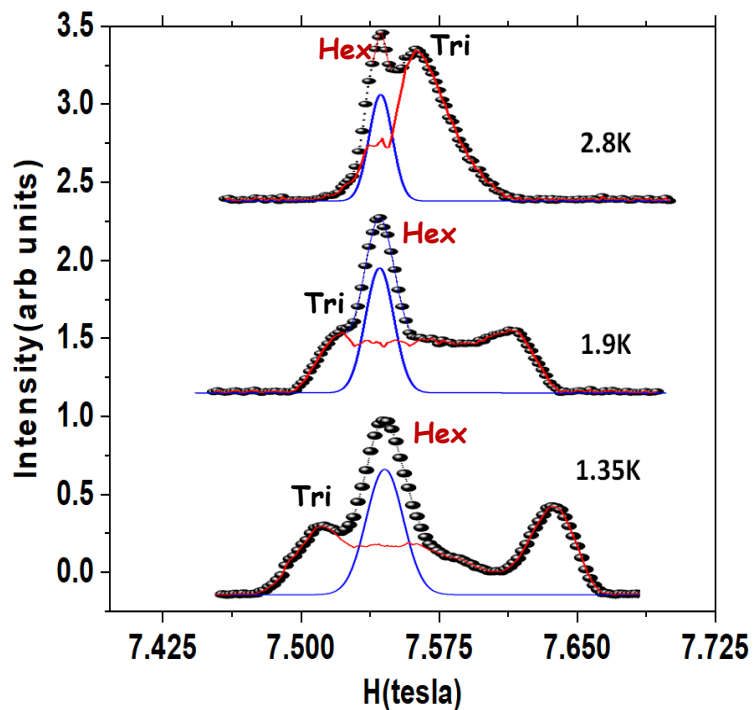
Magnetic ordering at low temperature



Hexagonal Cl hardly broadens

Triangular Cl line broadens/splits at the magnetic transition

Magnetic ordering at low temperature

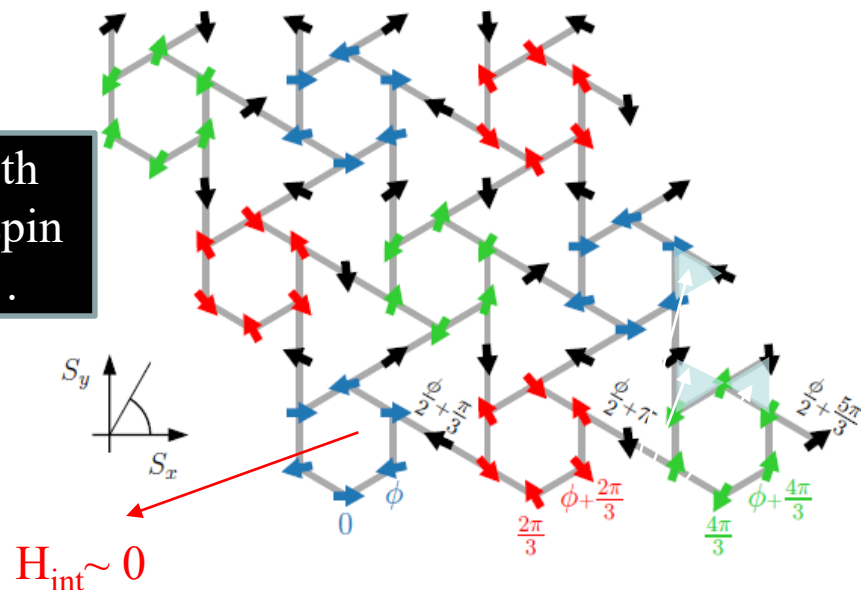


Hexagonal CI hardly broadens
 Triangular CI line broadens/splits at the magnetic transition

Proposed $(1/3, 1/3)$ ordering

Hering et al, npj Comput Mater 8, 10 (2022)

in line with
 proposed spin
 texture...



Finite H_{int} , 3
 configurations

Magnetic ordering of the distorted kagome antiferromagnet $\text{Y}_3\text{Cu}_9(\text{OH})_{18}[\text{Cl}_8(\text{OH})]$ prepared via optimal synthesis

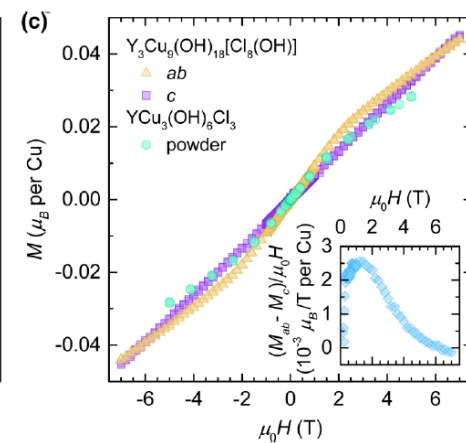
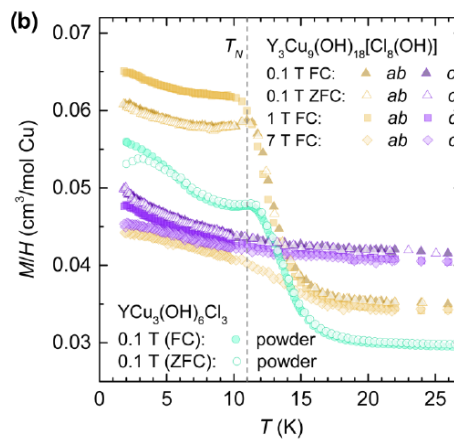
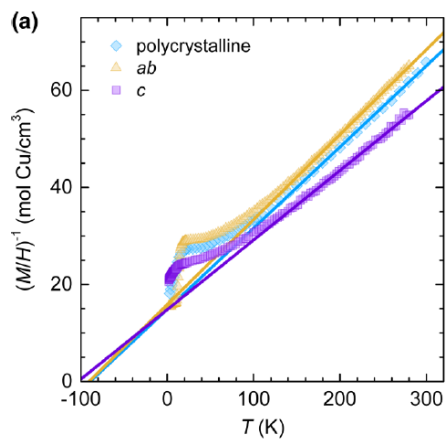
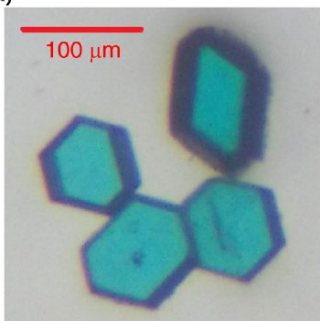
W. Sun,¹ T. Arh,^{2,3} M. Gomilšek,² P. Koželj,^{2,3} S. Vrtnik,² M. Herak,⁴ J.-X. Mi,¹ and A. Zorko^{2,3,*}

(¹Fujian Provincial Key Laboratory of Advanced Materials, Department of Materials Science and Engineering, College of Materials, Xiamen University, Xiamen 361005, Fujian Province, People's Republic of China

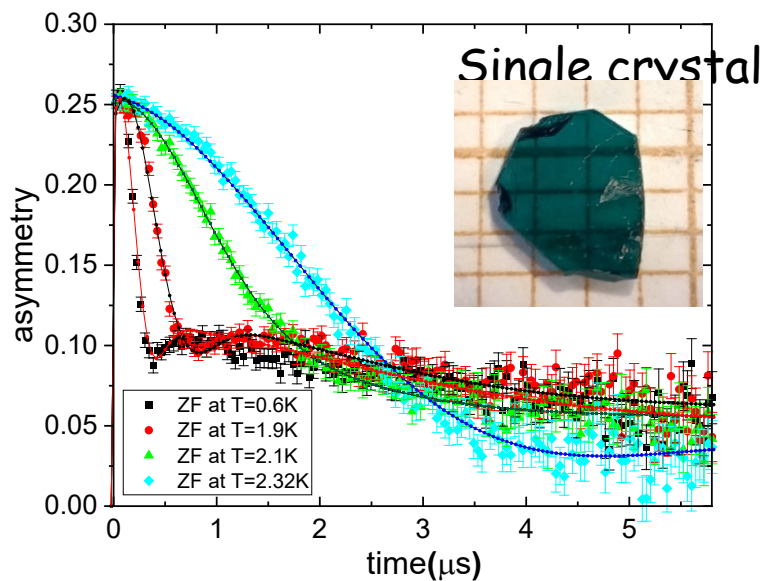
²Jožef Stefan Institute, Jamova cesta 39, SI-1000 Ljubljana, Slovenia

³Faculty of Mathematics and Physics, University of Ljubljana, Jadranska ulica 19, SI-1000 Ljubljana, Slovenia

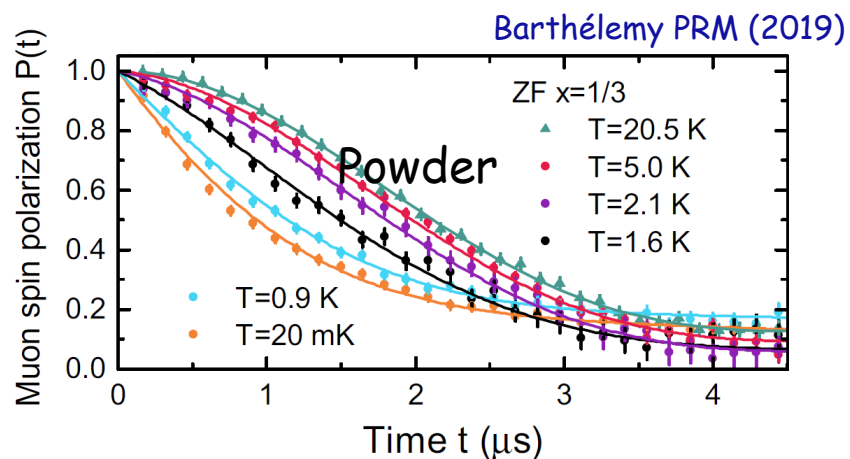
⁴Institute of Physics, Bijenička cesta 46, HR-10000 Zagreb, Croatia



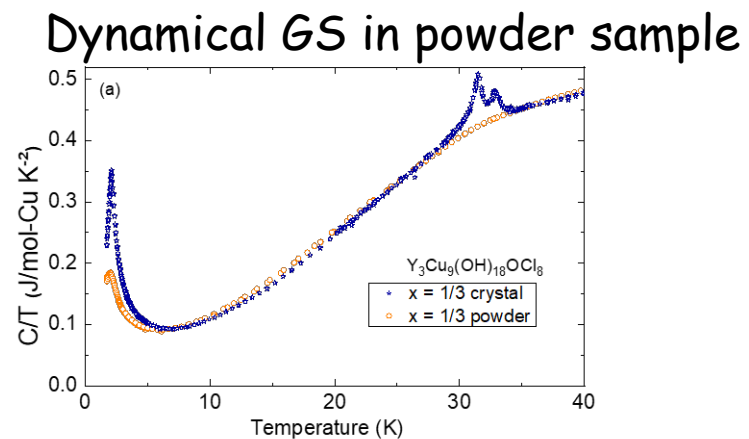
Muon spin relaxation measurements



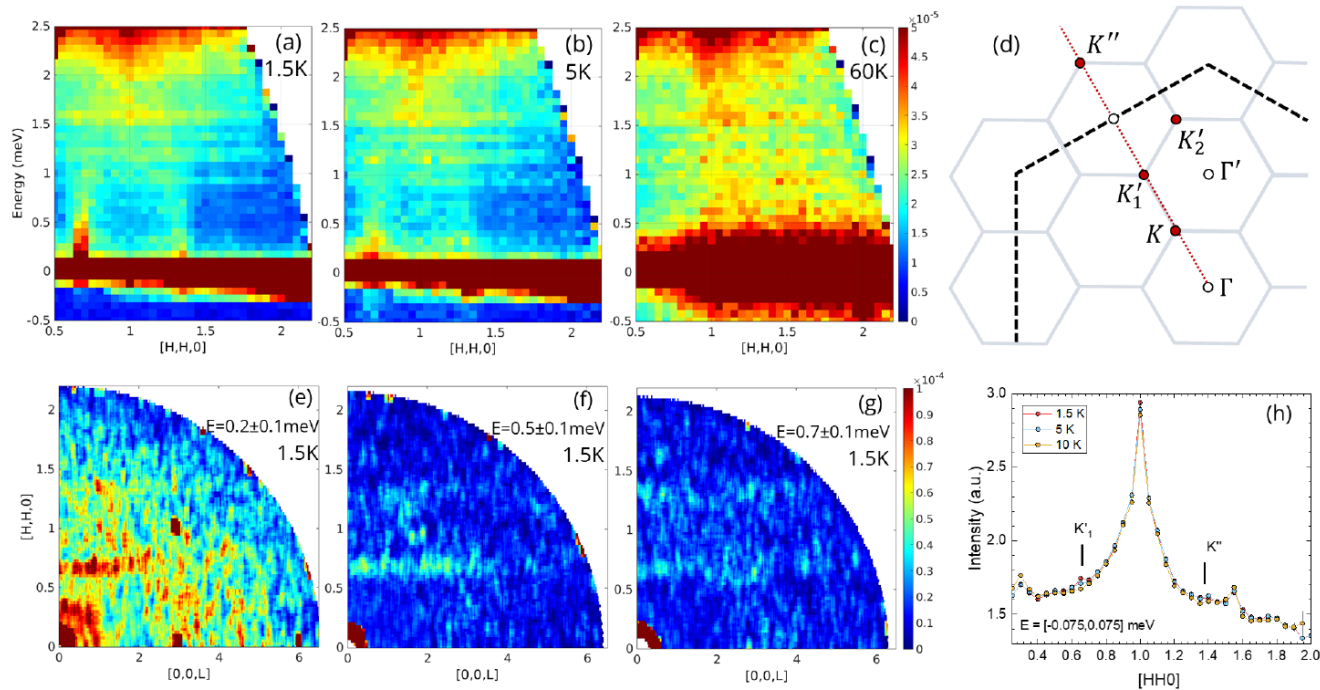
\neq



Complete transition at 2.1 K
Frozen moment $\sim 0.1\mu_B$



Long range magnetic order (INS)



Spin waves dispersion emerging from K points at 1.5K inline with $(1/3, 1/3)$ LRO
 No dispersion along (00L), strongly 2D
 Very weak static moment