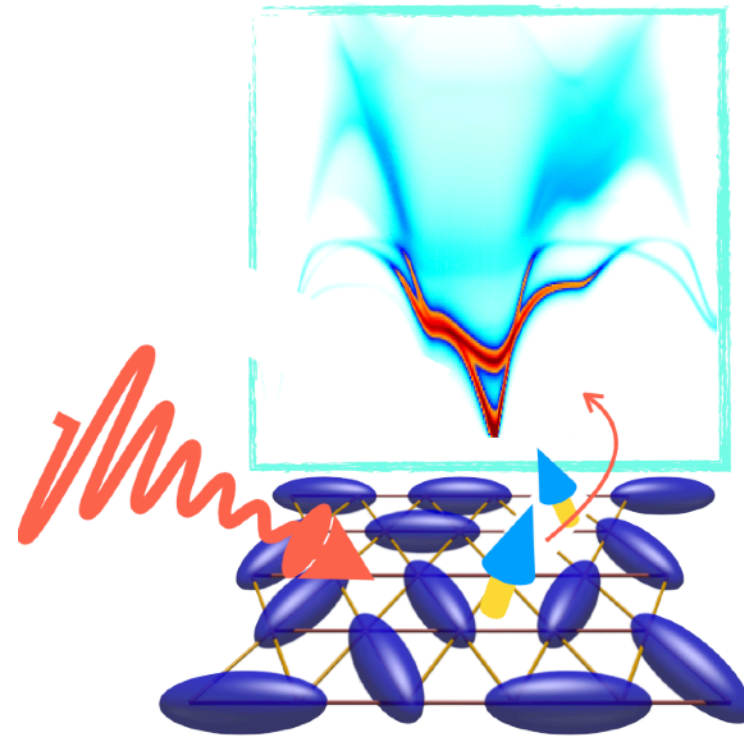


Dynamical response of magnetized spin liquids

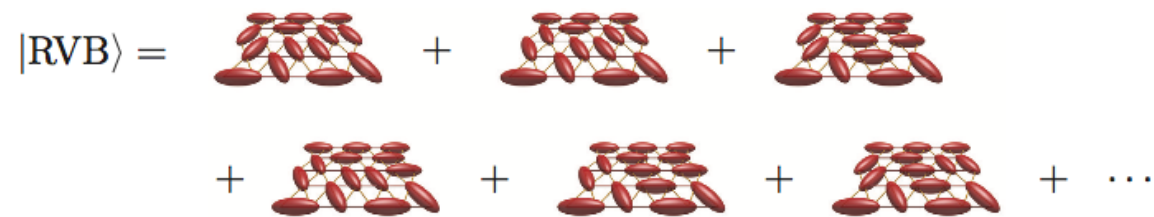


Oleg Starykh, University of Utah

ICTP, December 2023, Trieste



Probing fractionalized excitations *and* their interactions



No broken symmetries.
Quantum entangled state:
fractionalized excitations = spinons
+ emergent gauge fields

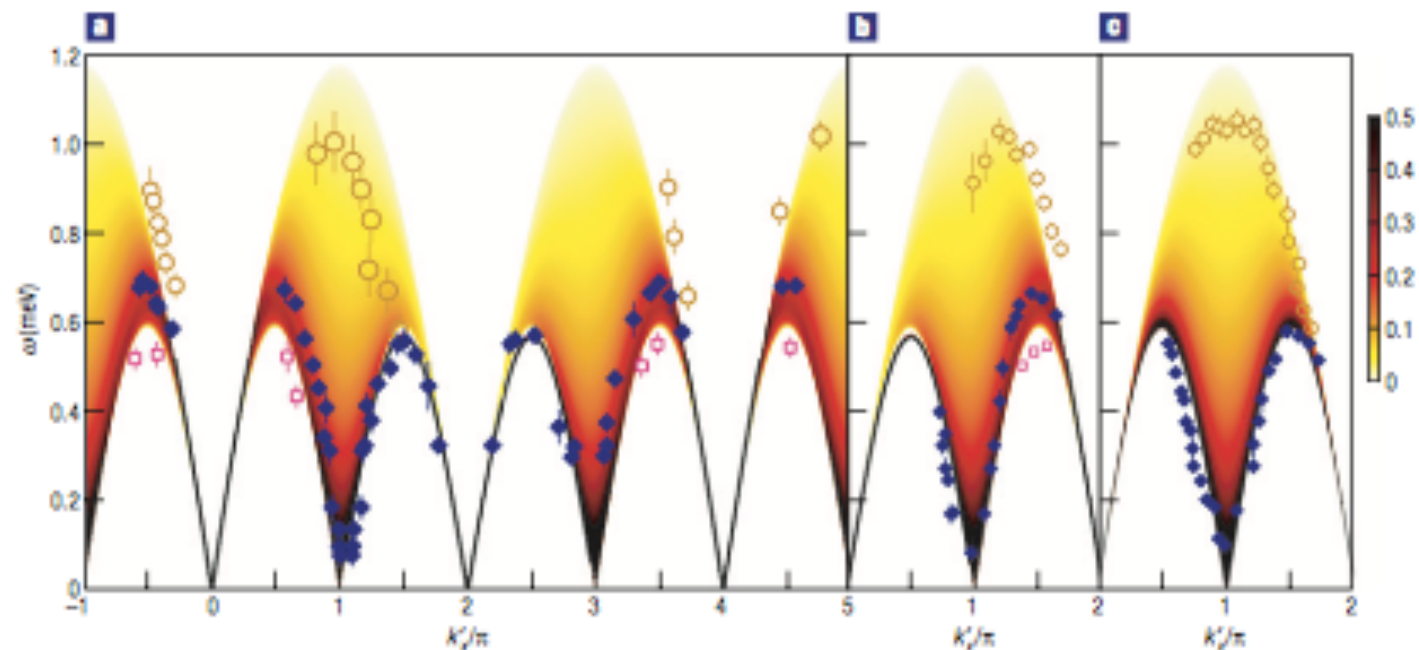
Figure 1. A 'resonating valence bond' (RVB) state. Ellipsoids indicate spin-zero singlet states of two $S = 1/2$ spins.

Savary, Balents 2017

How to detect/observe it?

Neutrons, RIXS, NMR, thermal transport, terahertz optics, ESR, quantum spintronics

Dynamics in magnetic field!



Outline

Probing fractionalized excitations *and* their collective modes.



Spinon Fermi surface spin liquid in magnetic field. Spinon spin wave.

New take on the magnetized Heisenberg spin chain.

Interacting Dirac fermions in magnetic field.

Spin liquid (?) in magnetic field

What is $S(k, \omega)$
for a spinon FS QSL?

Article | OPEN | Published: 08 October 2018

Fractionalized excitations in the partially magnetized spin liquid candidate YbMgGaO_4

Yao Shen, Yao-Dong Li, H. C. Walker, P. Steffens, M. Boehm, Xiaowen Zhang, Shoudong Shen, Hongliang Wo, Gang Chen & Jun Zhao

Nature Communications 9, Article number: 4138 (2018) | Download Citation

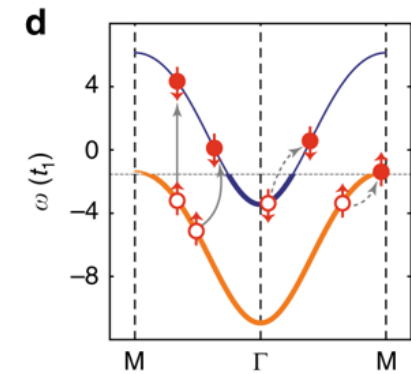
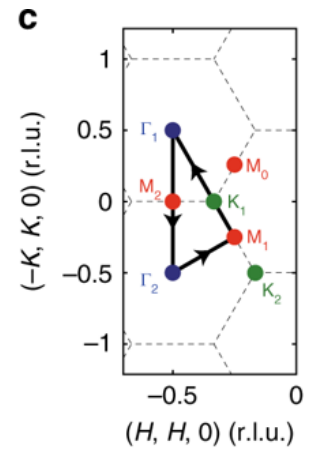
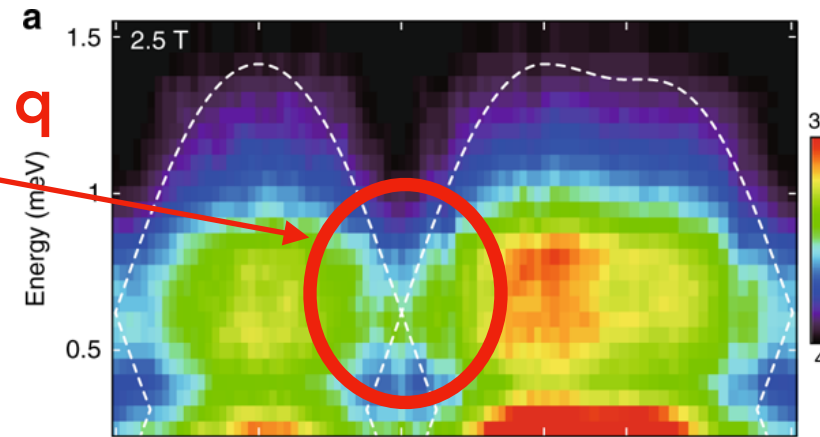
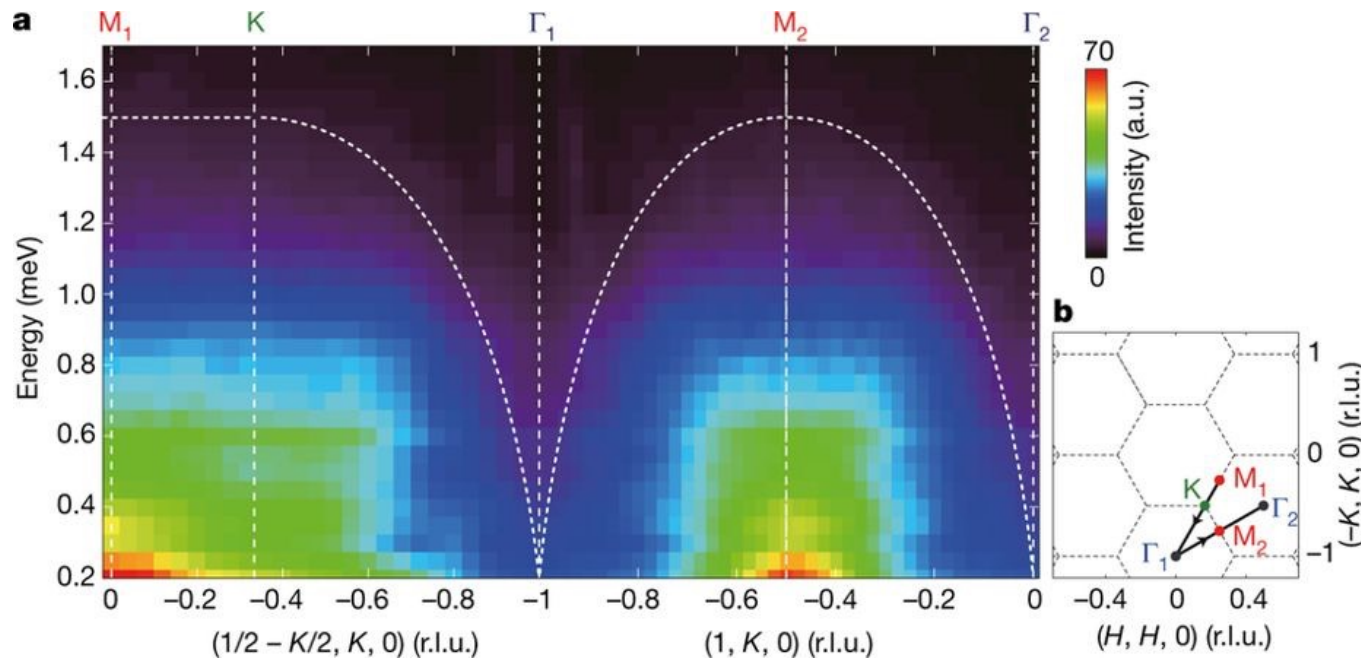
Letter | Published: 05 December 2016

Evidence for a spinon Fermi surface in a triangular-lattice quantum-spin-liquid candidate

Yao Shen, Yao-Dong Li, Hongliang Wo, Yuesheng Li, Shoudong Shen, Bingying Pan, Qisi Wang, H. C. Walker, P. Steffens, M. Boehm, Yiqing Hao, D. L. Quintero-Castro, L. W. Harriger, M. D. Frontzek, Lijie Hao, Siqin Meng, Qingming Zhang, Gang Chen & Jun Zhao

Nature 540, 559–562 (22 December 2016) | Download Citation

Small momentum q
structure



Sketch of U(1) gauge theory

1) $S_{\mathbf{r}}^a = \frac{1}{2} \psi_{\mathbf{r},\alpha}^\dagger \sigma_{\alpha\beta}^a \psi_{\mathbf{r},\beta}$ provided $\sum_{\alpha} \psi_{\mathbf{r},\alpha}^\dagger \psi_{\mathbf{r},\alpha} = 1$ enforced by \mathbf{A}_0

2) $\vec{S}_{\mathbf{r}} \cdot \vec{S}_{\mathbf{r}'} \rightarrow |\Delta_{\mathbf{r}\mathbf{r}'}| e^{iA_{\mathbf{r}\mathbf{r}'}} \psi_{\mathbf{r}\alpha}^\dagger \psi_{\mathbf{r}'\alpha} \rightarrow A_{\mathbf{r}\mathbf{r}'} \rightarrow (\mathbf{r} - \mathbf{r}') \cdot \mathbf{A} \left(\frac{\mathbf{r} + \mathbf{r}'}{2} \right)$

3) $S_{\psi} = \int d\tau d^2\mathbf{r} \psi_{\alpha}^\dagger \left([\partial_{\tau} - iA_0 - \mu - \frac{(\nabla_{\mathbf{r}} - i\mathbf{A})^2}{2m}] \delta_{\alpha\beta} - \omega_B \sigma_{\alpha\beta}^3 \right) \psi_{\beta}$

Gauge field
External magnetic field
Spinon

Gauge theory of high-temperature superconductors and strongly correlated Fermi systems

G. Baskaran and P. W. Anderson

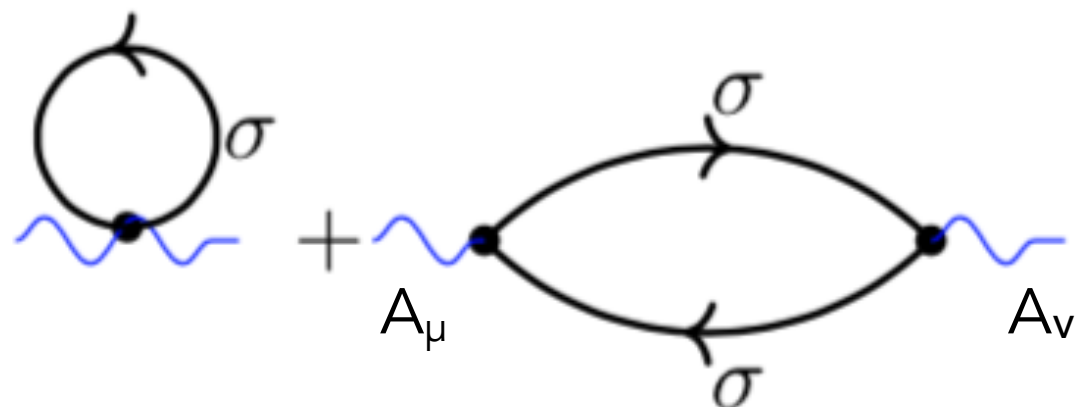
Gapless fermions and gauge fields in dielectrics

L. B. Ioffe and A. I. Larkin
Phys. Rev. B **39**, 8988 – Published 1 May 1989

Gauge theory of the normal state of high- T_c superconductors

Patrick A. Lee and Naoto Nagaosa
Phys. Rev. B **46**, 5621 – Published 1 September 1992

4) Gauge dynamics generated by spinons



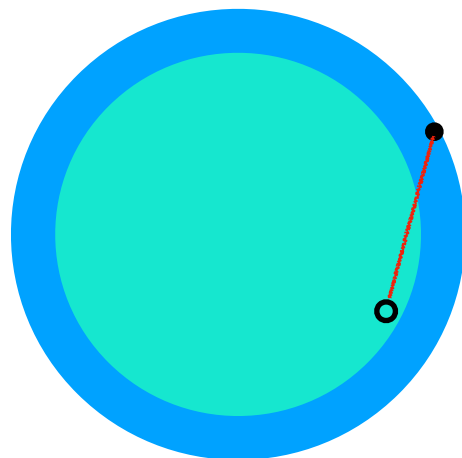
Interactions

- Longitudinal

$$A_0 \psi^\dagger \psi \rightarrow u \psi_\uparrow^\dagger \psi_\uparrow \psi_\downarrow^\dagger \psi_\downarrow$$

screened Coulomb
interaction

Short-ranged

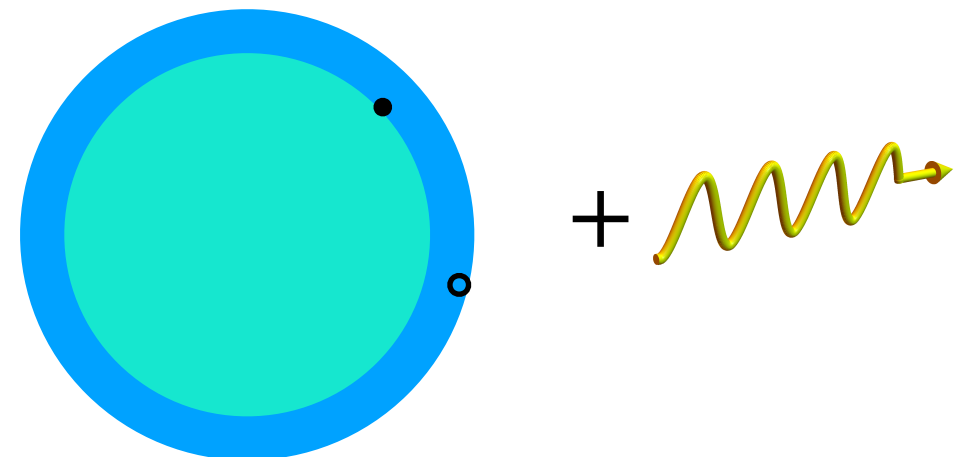


- Transverse

$$i\mathbf{A} \cdot (\psi^\dagger \nabla \psi - \nabla \psi^\dagger \psi)$$

coupling to dynamical
photons

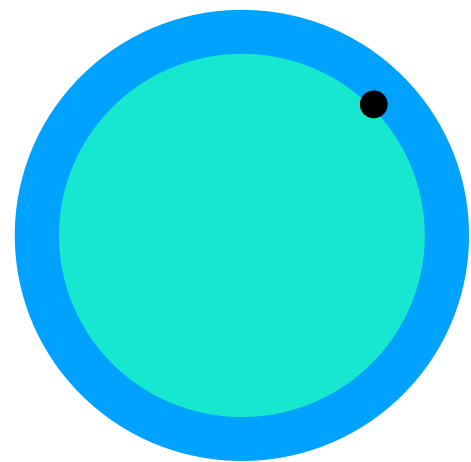
**Source of non-analytical
behaviors $\omega^{2/3}$, etc**



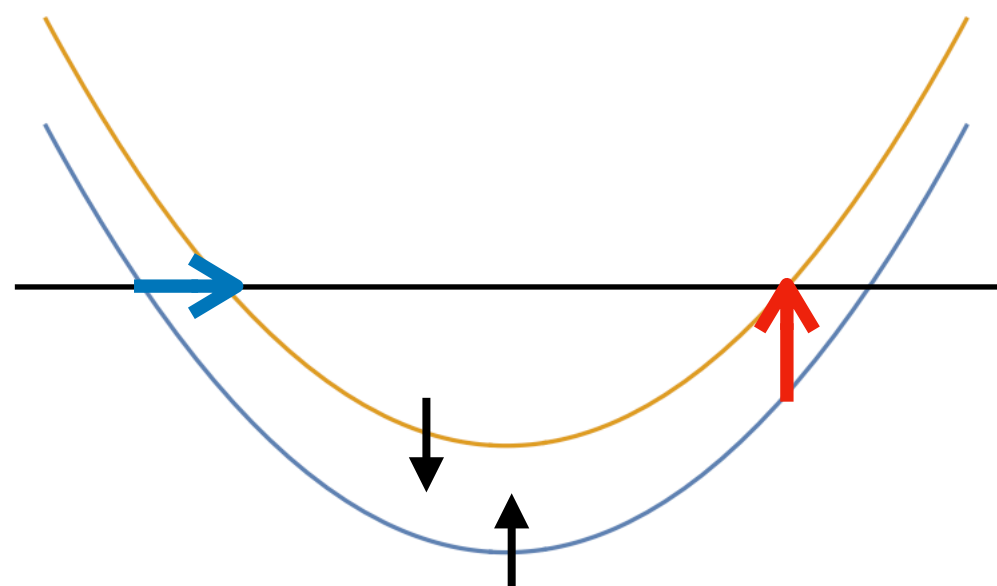
Spinon particle-hole continuum

+ Zeeman field

$$\chi_{\pm}(\mathbf{q}, \omega) = i \int_0^{\infty} dt \langle [S_{\mathbf{q}}^{\dagger}(t), S_{-\mathbf{q}}(0)] \rangle e^{i\omega t}$$

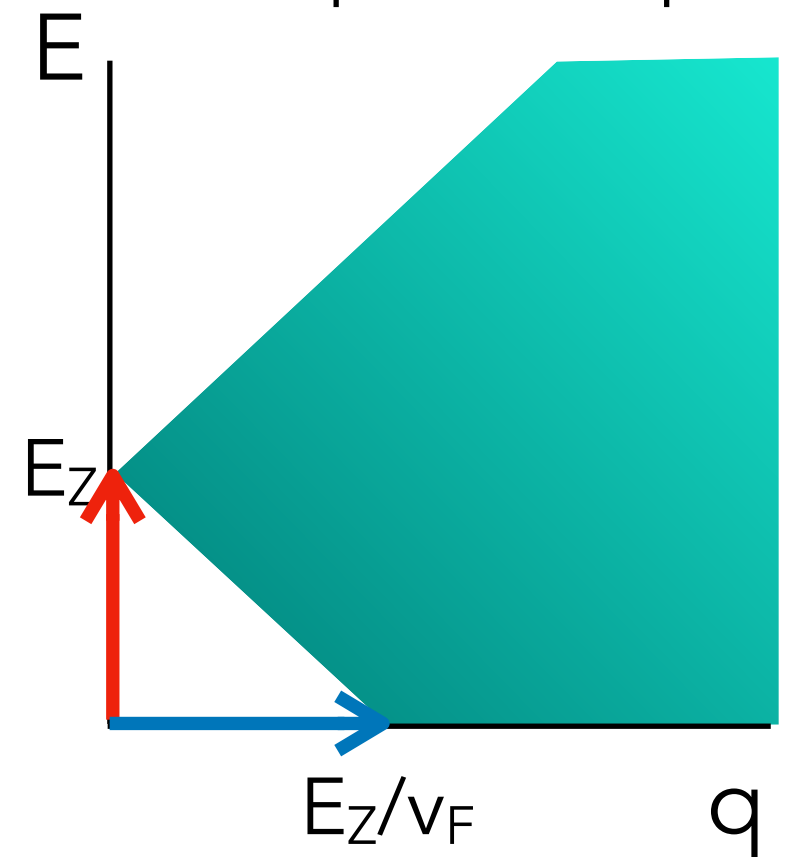


$q=0$ costs Zeeman energy



zero energy when $v_F q$
= Zeeman

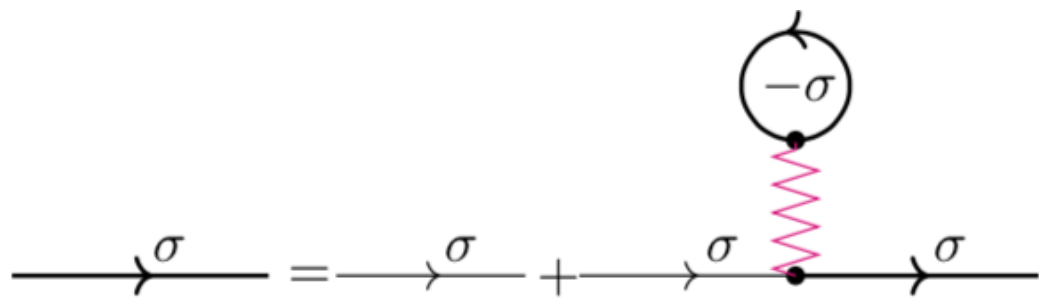
Transverse spin susceptibility



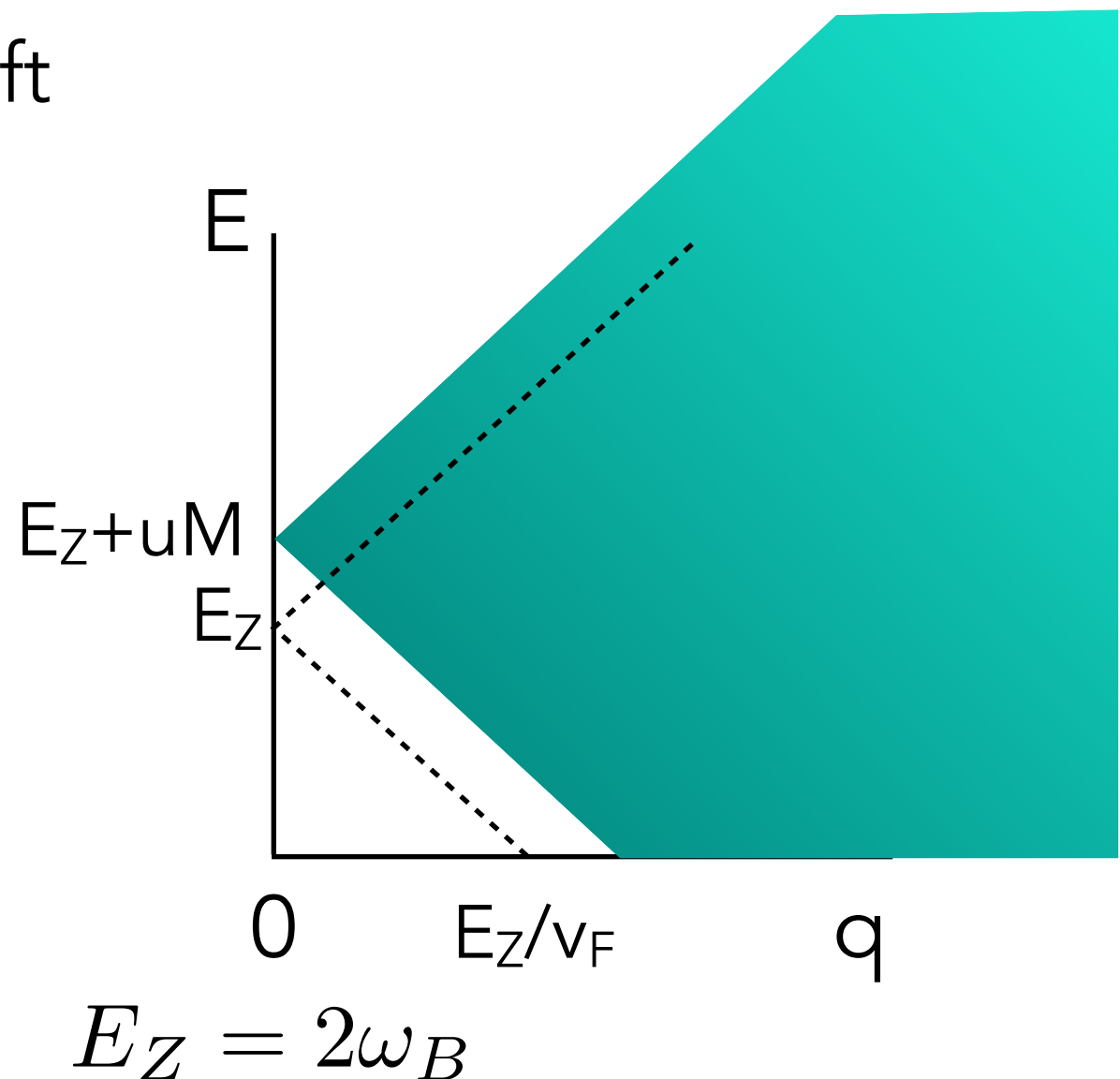
Short-range interaction + Zeeman magnetic field

$$u\psi_{\uparrow}^{\dagger}\psi_{\uparrow}\psi_{\downarrow}^{\dagger}\psi_{\downarrow} \longrightarrow = -\frac{1}{2}uM(\psi_{\uparrow}^{\dagger}\psi_{\uparrow} - \psi_{\downarrow}^{\dagger}\psi_{\downarrow})$$

Self-energy = mean field shift



PH continuum shifts
up in energy by **uM**



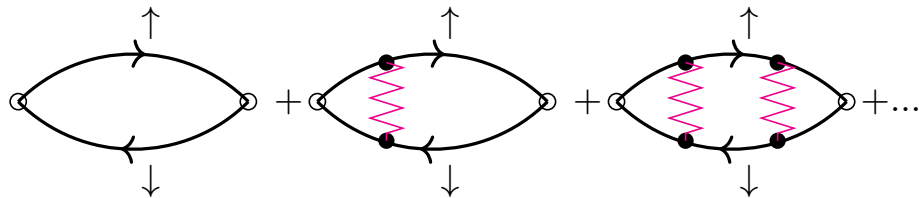
Silin spin wave

Larmor theorem: $\mathbf{q}=0$

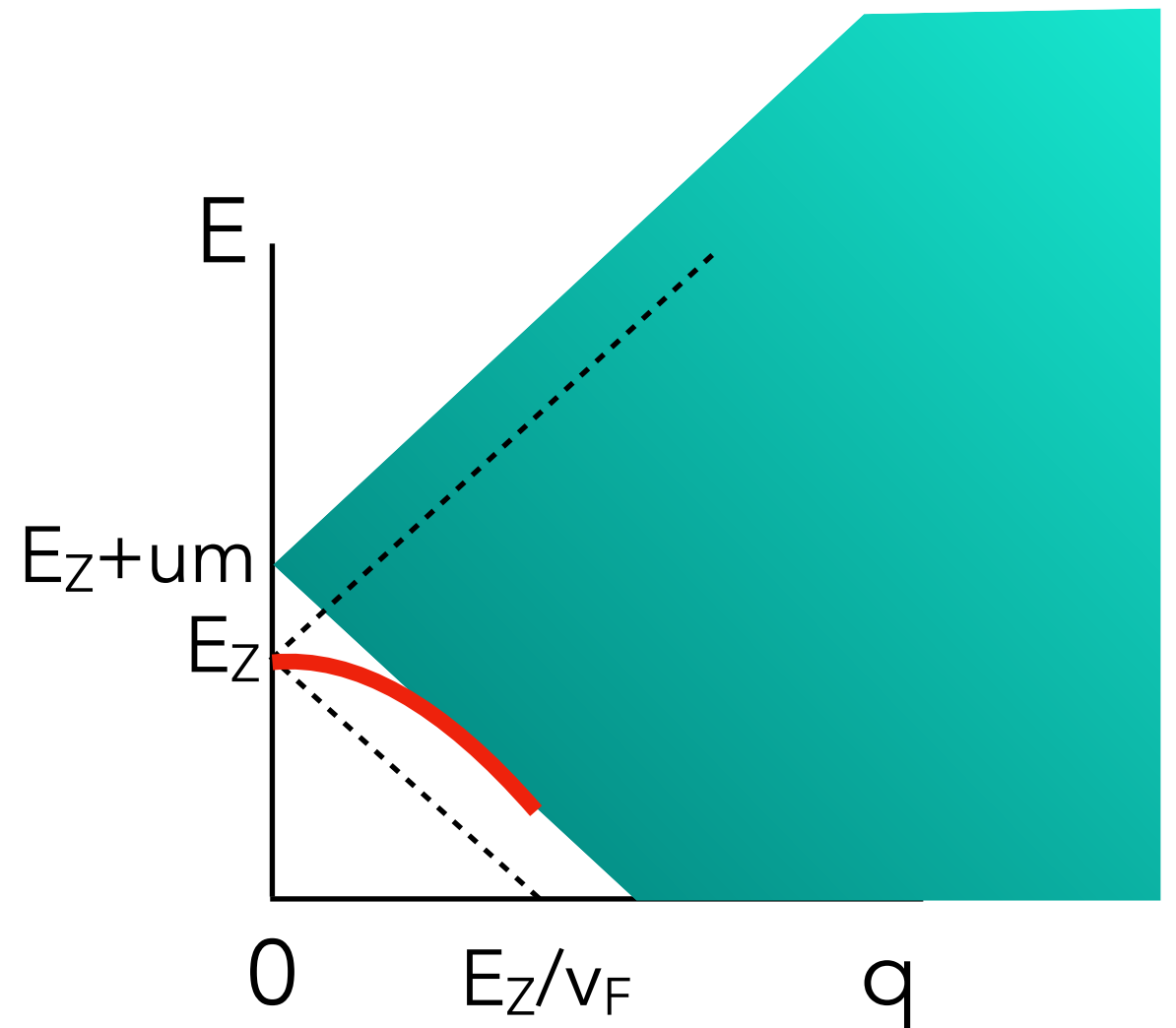
excitation *must* be at E_Z

$$\frac{dS_{\text{tot}}^+}{dt} = -iBS_{\text{tot}}^+$$

RPA: ladder series



$$\chi(\mathbf{q}, i\omega_n) = \frac{\chi^0(\mathbf{q}, i\omega_n)}{1 + u\chi^0(\mathbf{q}, i\omega_n)}$$



“Silin spin wave”

Theory: V.P. Silin, JETP 6, 945 (1958);

Platzman, Wolf, PRL 18, 280 (1967);

Exp: Schultz, Dunifer, PRL 18, 283 (1967).

pole: collective mode

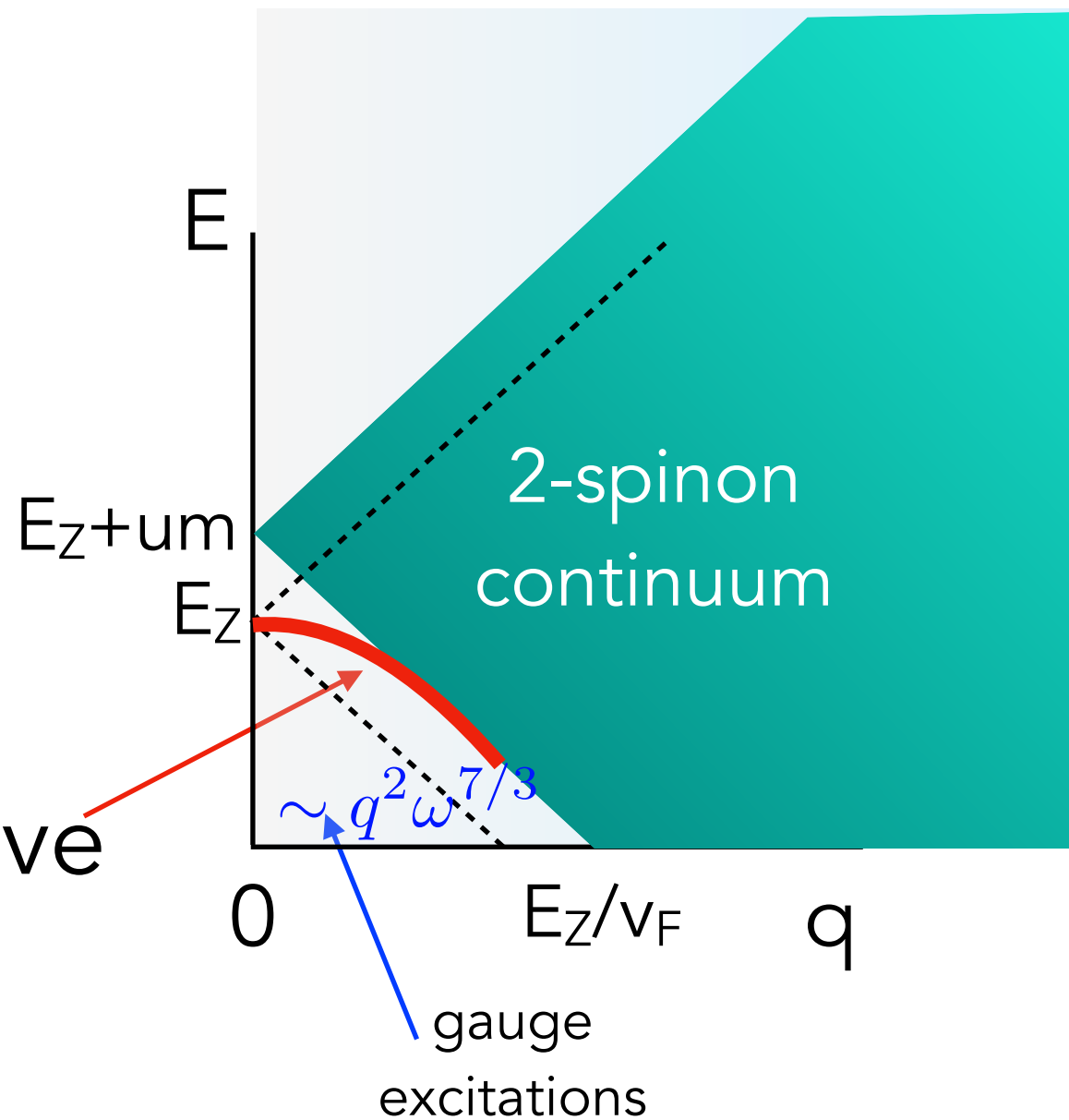
$$\omega = E_Z + um - \sqrt{u^2 m^2 + v_F^2 q^2}$$

Collective spinon spin wave in a magnetized U(1) spin liquid

Leon Balents and Oleg A. Starykh
 Phys. Rev. B **101**, 020401(R)

Distinct signature of spinons, interactions, and gauge fields

Transverse collective spin wave is dressed by gauge fluctuations, acquires finite lifetime.

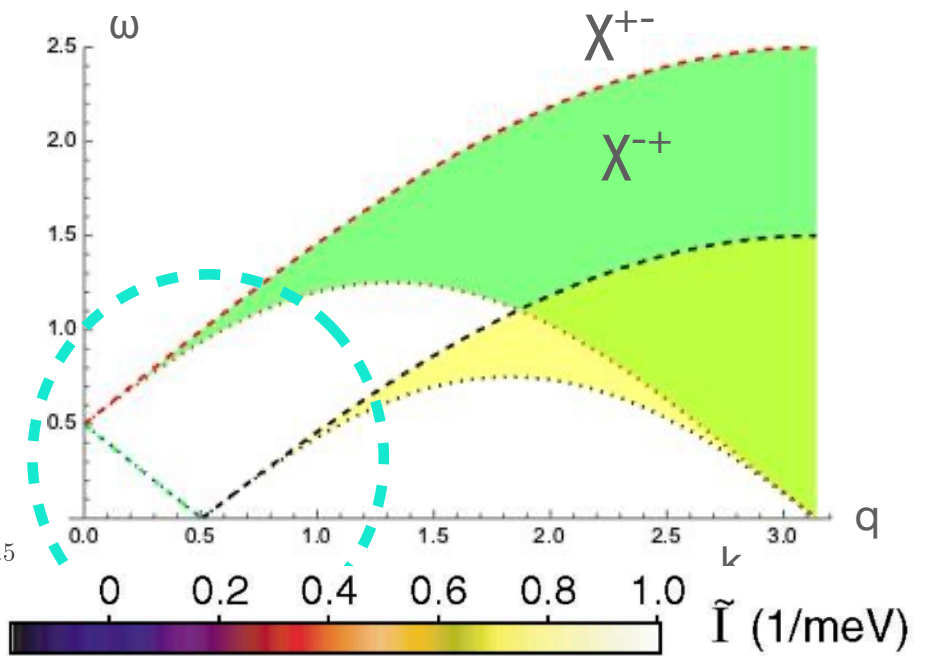
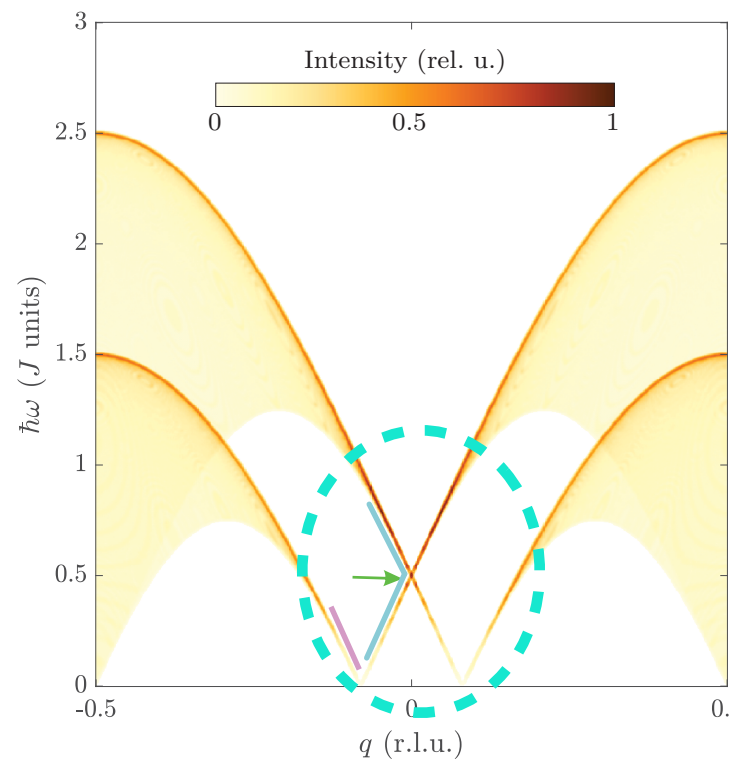
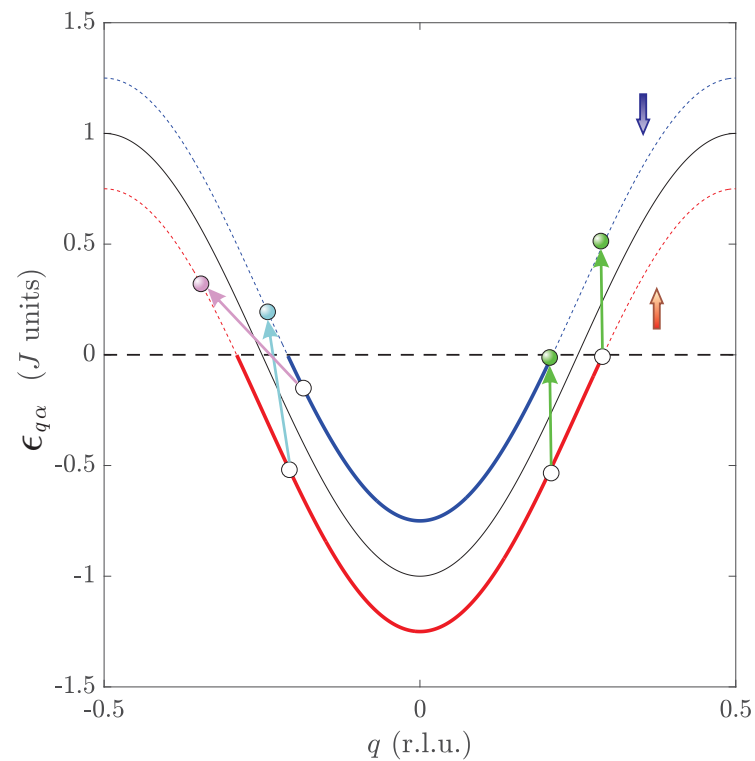


$$\frac{E_Z}{v_F} \sim \sqrt{m E_Z} \sqrt{\frac{E_Z}{E_F}}$$

conductors $\frac{E_Z}{E_F} \rightarrow 0$
 QSL $\frac{E_Z}{E_F} \sim 1$

Check the best-known spin liquid: spin-1/2 chain in a magnetic field

Non-interacting limit ($g=0$) - field splits spin up/down bands $H = H_0 - B \int dx \left[\underbrace{J_R^z(x) + J_L^z(x)}_{\text{Magnetization}} \right]$



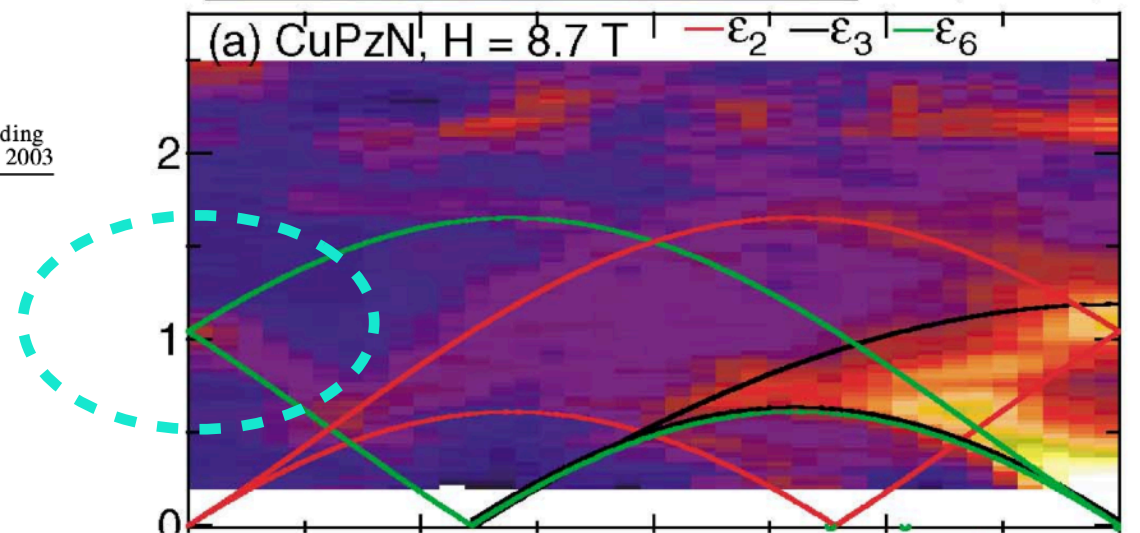
VOLUME 91, NUMBER 3

PHYSICAL REVIEW LETTERS

week ending
18 JULY 2003

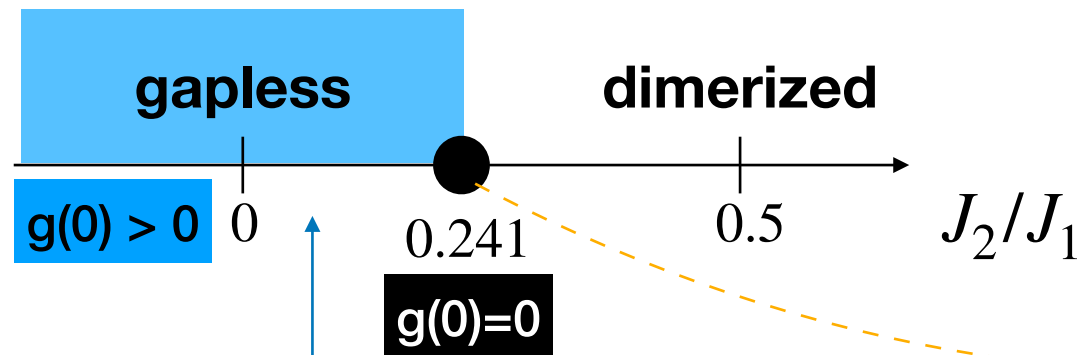
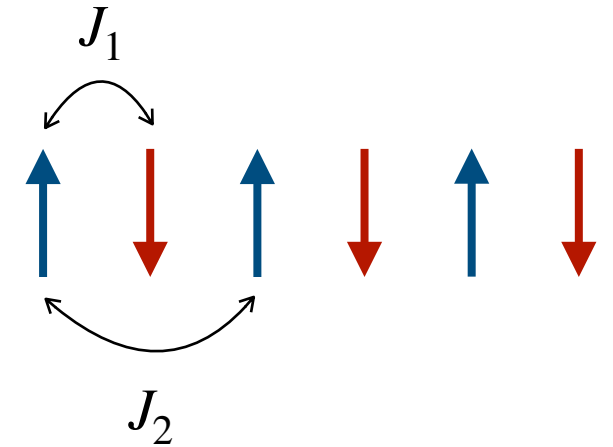
Extended Quantum Critical Phase in a Magnetized Spin- $\frac{1}{2}$ Antiferromagnetic Chain

M. B. Stone,^{1,*} D. H. Reich,¹ C. Broholm,^{1,2} K. Lefmann,³ C. Rischel,⁴ C. P. Landee,⁵ and M. M. Turnbull⁵



Spin-1/2 antiferromagnetic chain

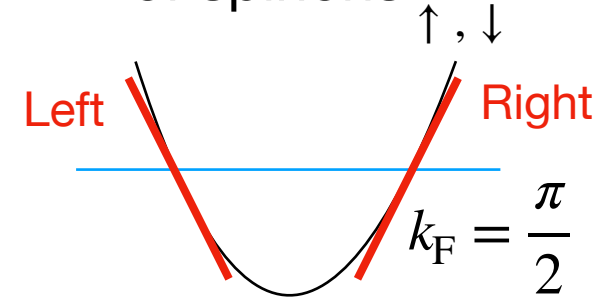
$$H = \sum_n J_1 \vec{S}_n \cdot \vec{S}_{n+1} + J_2 \vec{S}_n \cdot \vec{S}_{n+2} - BS_n^z$$



backscattering is marginally irrelevant!

half-filled band of spinons

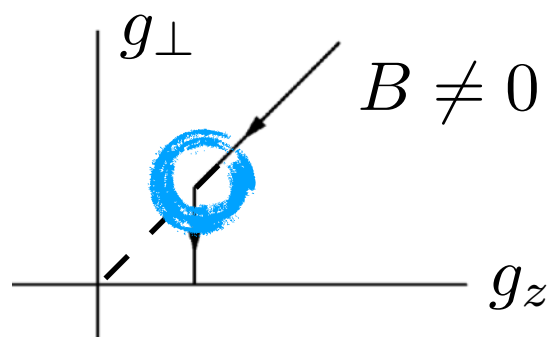
$$H = \int dx \left(\underbrace{\psi_R^\dagger (-iv_F \partial_x) \psi_R + \psi_L^\dagger (iv_F \partial_x) \psi_L}_{H_0} - \underbrace{g \vec{J}_R \cdot \vec{J}_L}_{H_{\text{int}}} \right)$$



Free fermions

Spin current $\vec{J}_{R/L} = \frac{1}{2} \psi_{R/L}^\dagger \vec{\sigma} \psi_{R/L}$

$$\vec{S}(x_i) \rightarrow \vec{J}_R + \vec{J}_L + \frac{(-1)^{x_i}}{2} \left(\psi_R^\dagger \vec{\sigma} \psi_L + \psi_L^\dagger \vec{\sigma} \psi_R \right)$$



$g > 0$: marginally irrelevant interaction of spin currents (spin backscattering $\sim g \cos[\sqrt{8\pi}\varphi_\sigma]$)

$$g(\ell) = \frac{g(0)}{1 + g(0)\ell}, \quad \ell = \ln(J/E) \longrightarrow g(E \rightarrow 0) \rightarrow 1/\ln(J/E)$$

Spin-1/2 Heisenberg chain in magnetic field

PHYSICAL REVIEW B, VOLUME 65, 134410

Electron spin resonance in $S = \frac{1}{2}$ antiferromagnetic chains

Masaki Oshikawa¹ and Ian Affleck^{2,*}

¹Department of Physics, Tokyo Institute of Technology, Oh-okayama, Meguro-ku, Tokyo 152-8551, Japan

²Department of Physics, Boston University, Boston, Massachusetts 02215

(Received 13 August 2001; published 19 March 2002)

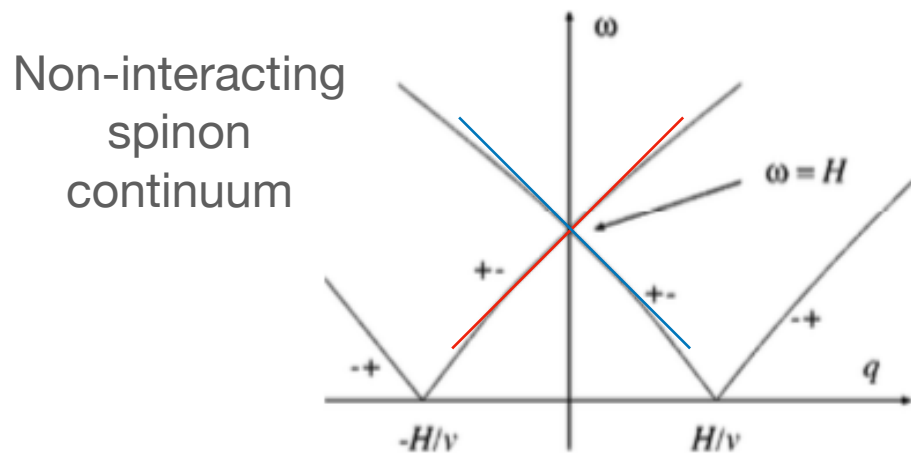


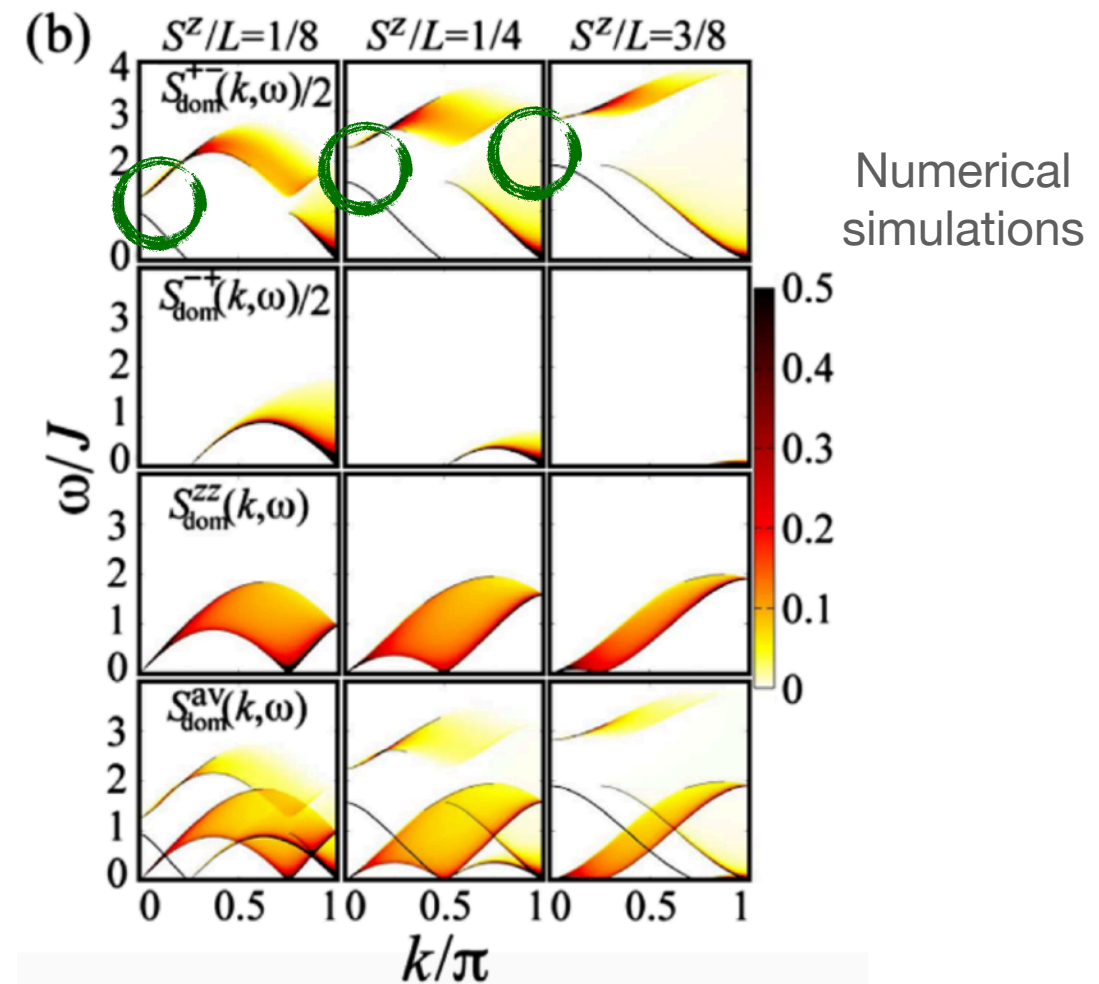
FIG. 2. The zero temperature transverse spin structure factor $S_{xx}(\omega, q) = S_{yy}(\omega, q)$ of the $S = 1/2$ Heisenberg antiferromagnetic chain under an applied field H , near $q = 0$. It is approximately proportional to $\omega[\delta(\omega - |q - H|) + \delta(\omega - |q + H|)]$, giving the resonance at $q = 0, \omega = H$. This consists of two branches coming from S_{+-} and S_{-+} , which are marked by $+-$ and $-+$ in the graph. In fact, there is a small spreading of the spectrum and the structure factor is generally not a perfect delta function. However, it is exactly the delta function $\delta(\omega - H)$ at $q = 0$, as explained in the text.

$$S_{xx}(\omega, q) = S_{yy}(\omega, q) \propto \omega[\delta(\omega - |q + H|) + \delta(\omega - |q - H|)].$$

BUT
 ???
 Splitting
 between
 two
 branches;
 increases
 with M

Dynamically Dominant Excitations of String Solutions in the Spin-1/2 Antiferromagnetic Heisenberg Chain in a Magnetic Field

Masanori Kohno
 Phys. Rev. Lett. **102**, 037203 – Published 22 January 2009



Spin backscattering is finite at energy $E = B$

$$H = H_0 - g \int dx \left[J_R^z J_L^z + \frac{1}{2} J_R^+ J_L^- + \frac{1}{2} J_R^- J_L^+ \right] - B \int dx \left[J_R^z(x) + J_L^z(x) \right]$$

Transverse interaction
must restore Larmor Th

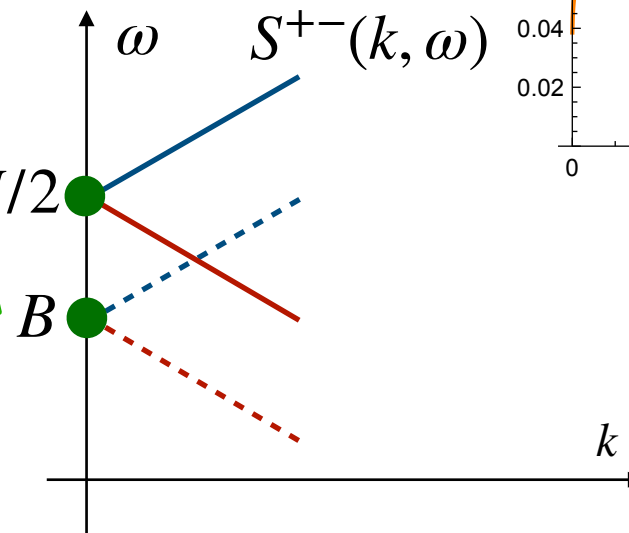
Self energy

$$-g \int dx \left[\langle J_L^z \rangle J_R^z + J_L^z \langle J_R^z \rangle \right]$$

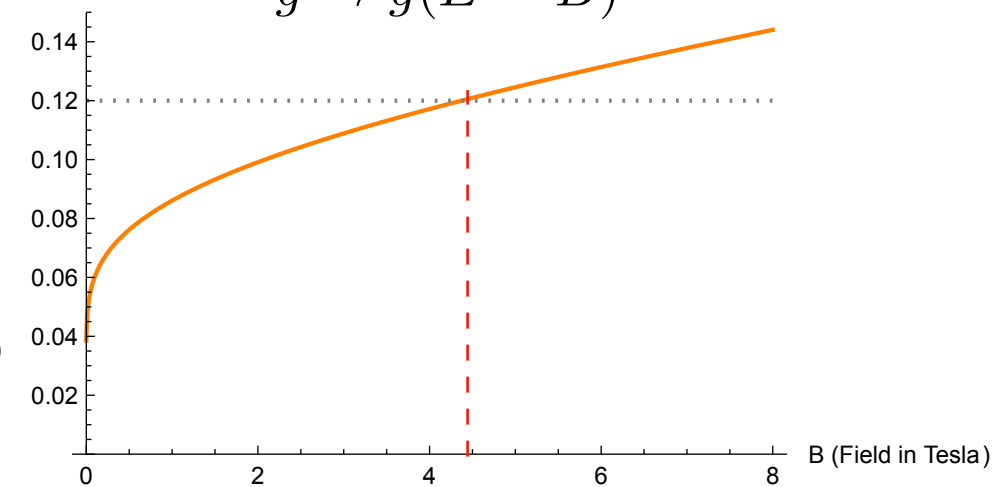
$$\langle J_{L,R}^z \rangle = M/2 \quad \longrightarrow \quad B + gM/2$$

(magnetization)

shifts the mode at $k=0$: $B \rightarrow B + gM/2$



$$\delta = g/(4\pi v)$$



$$g \approx \frac{\pi^2 J}{\ln \left(\frac{\sqrt{2\pi^3} e^\gamma J}{B} \right)}$$



Nuclear Physics B 522 [FS] (1998) 533-549



Theoretical problem: need to calculate dynamical spin susceptibility with the finite backscattering interaction between spinons

Low energy effective Hamiltonian for the XXZ spin chain

Sergei Lukyanov¹

Department of Physics and Astronomy, Rutgers University, Piscataway, NJ 08855-0849, USA
L.D. Landau Institute for Theoretical Physics, Kosygina 2, Moscow, Russia

(approximate) hydrodynamics: Dynamical susceptibility of interacting spinon liquid

Spin currents obey (level 1) Kac-Moody algebra: $[\hat{J}_{R/L}^a(x), \hat{J}_{R/L}^b(x')] = \frac{\mp i}{4\pi} \delta^{ab} \partial_x \delta(x-x') + i\epsilon^{abc} \hat{J}_{R/L}^c(x) \delta(x-x')$

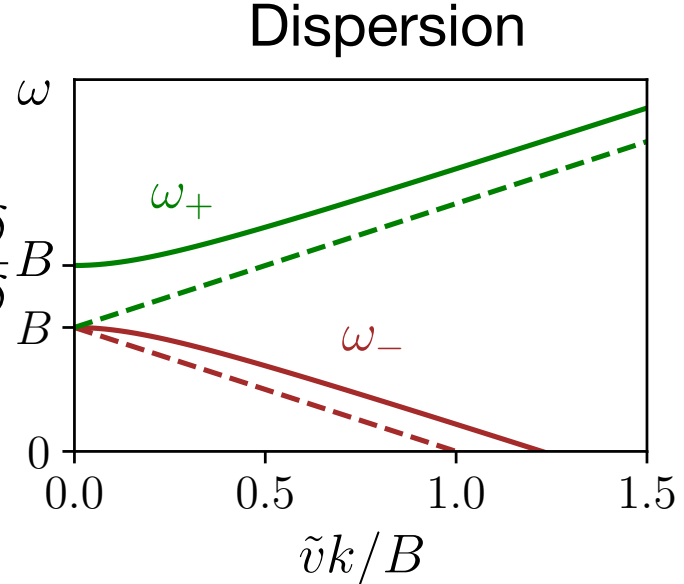
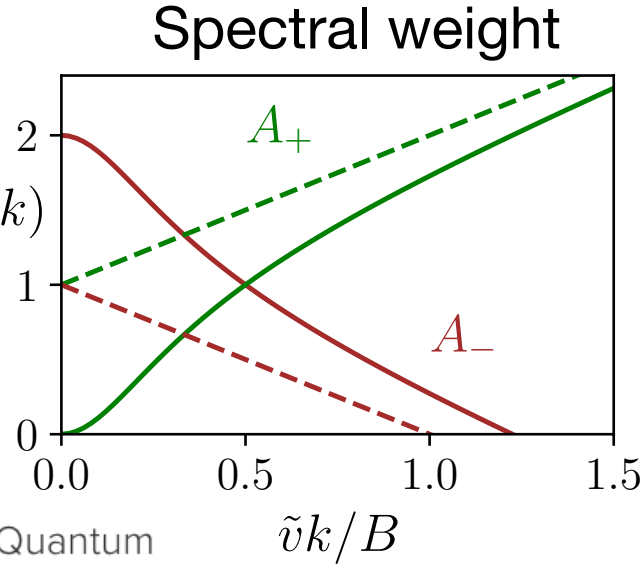
Equations of motion for right/left spin currents lead to the **hydrodynamic** description of the small- k response: $\mathbf{M} = \mathbf{J}_R + \mathbf{J}_L, \mathbf{L} = \mathbf{J}_R - \mathbf{J}_L$

$$\begin{aligned} \partial_t \mathbf{M} &= -v(1+\delta) \partial_x \mathbf{L} - \mathbf{B} \times \mathbf{M} \\ \partial_t \mathbf{L} &= -v(1-\delta) \partial_x \mathbf{M} - \mathbf{B} \times \mathbf{L} - \underbrace{g \mathbf{M} \times \mathbf{L}}_{\text{interaction!}} \end{aligned} \quad \dashrightarrow \quad \underbrace{\mathbf{M} \rightarrow \langle \mathbf{M} \rangle = \frac{\chi_0}{1-\delta} \mathbf{B}}_{\text{approximation}} \rightarrow \partial_t \mathbf{L} = -v(1-\delta) \partial_x \mathbf{M} - \frac{1+\delta}{1-\delta} \mathbf{B} \times \mathbf{L}$$

The result: $\chi^\pm(k, \omega) = M \left(\frac{A_+(k)}{\omega - \omega_+(k)} + \frac{A_-(k)}{\omega - \omega_-(k)} \right)$ $\omega_\pm(k) = B + \frac{\delta B}{1-\delta} \pm \sqrt{\left(\frac{\delta B}{1-\delta}\right)^2 + v^2(1-\delta^2)k^2}$

$$\delta = \frac{g}{4\pi v} = \frac{g}{2\pi^2 J}$$

$$A_\pm(k) = 1 \pm \frac{v^2(1-\delta^2)k^2 - \frac{\delta}{1-\delta} B^2}{B \sqrt{\left(\frac{\delta B}{1-\delta}\right)^2 + v^2(1-\delta^2)k^2}}$$



spin current (L-mode) $\frac{1+\delta}{1-\delta} B$
Larmor \rightarrow

Dashed lines: free spinon gas ($g=0$)

$$\tilde{v} = v\sqrt{1-\delta^2}$$

Dynamical Signatures of Quasiparticle Interactions in Quantum Spin Chains

Anna Keselman, Leon Balents, and Oleg A. Starykh
Phys. Rev. Lett. **125**, 187201 – Published 27 October 2020

Hydrodynamics of interacting spinons in the magnetized spin- $\frac{1}{2}$ chain with a uniform Dzyaloshinskii-Moriya interaction

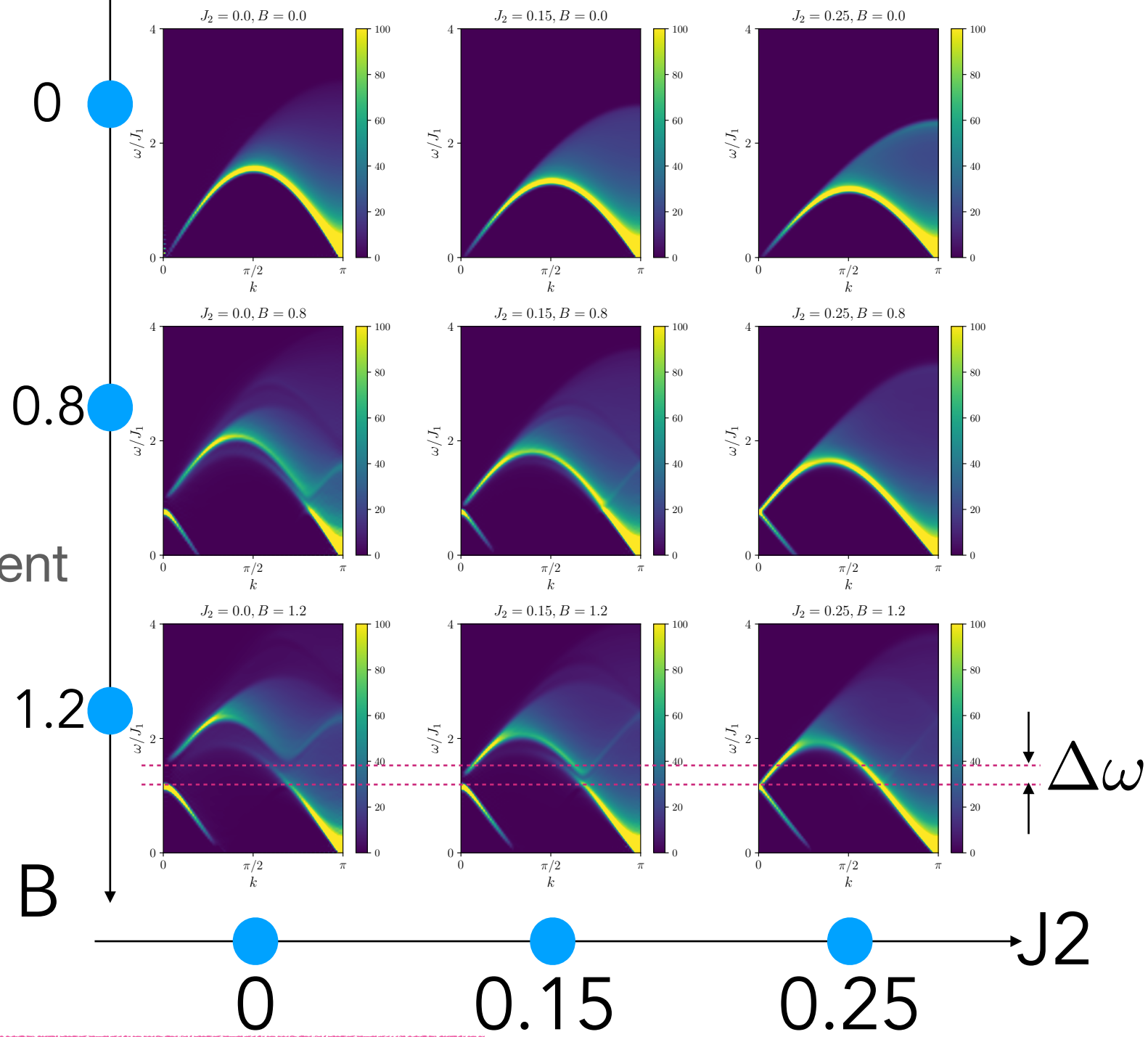
Ren-Bo Wang, Anna Keselman, and Oleg A. Starykh
Phys. Rev. B **105**, 184429 – Published 27 May 2022

Numerical confirmation

$$S^{+-}(\vec{k}, \omega) = \int_{-\infty}^{\infty} dt e^{i\omega t} \int d\vec{r} e^{-i\vec{k}\cdot\vec{r}} \langle 0 | S_r^+(t) S_0^-(0) | 0 \rangle \longrightarrow \langle 0 | e^{iHt} S_r^+ e^{-iHt} S_0^- | 0 \rangle = e^{iE_0 t} \langle 0 | S_r^+ e^{-iHt} S_0^- | 0 \rangle$$

It works!

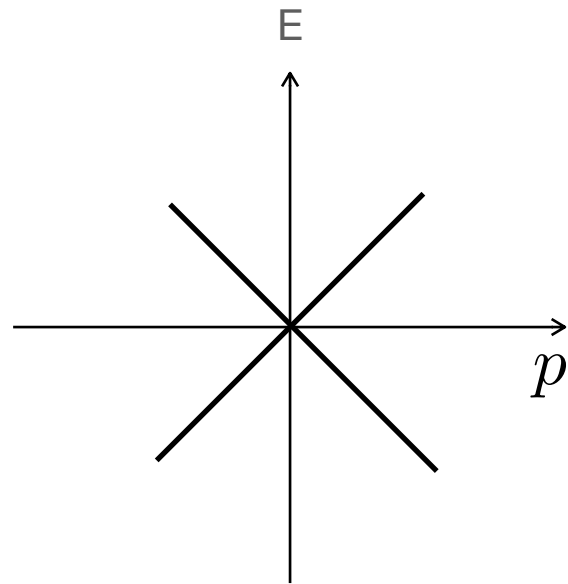
Explains ESR experiment
in $K_2CuSO_4Br_2$



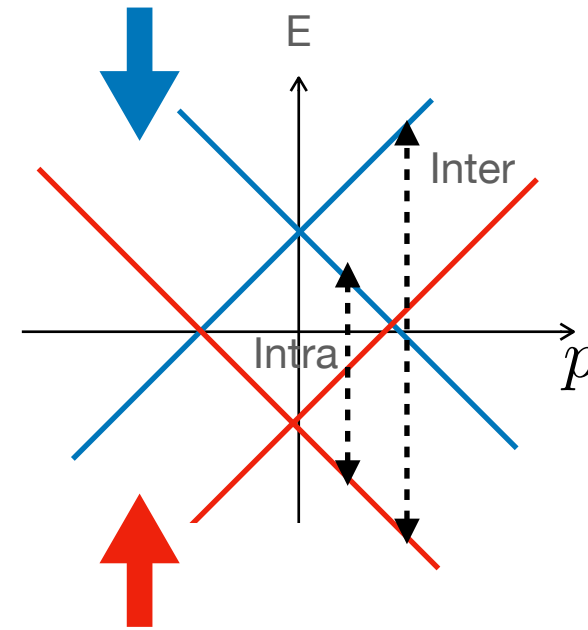
Heisenberg chain
interacting spinon liquid

Haldane-Shastry chain
spinon gas

Dirac fermions -> Graphene



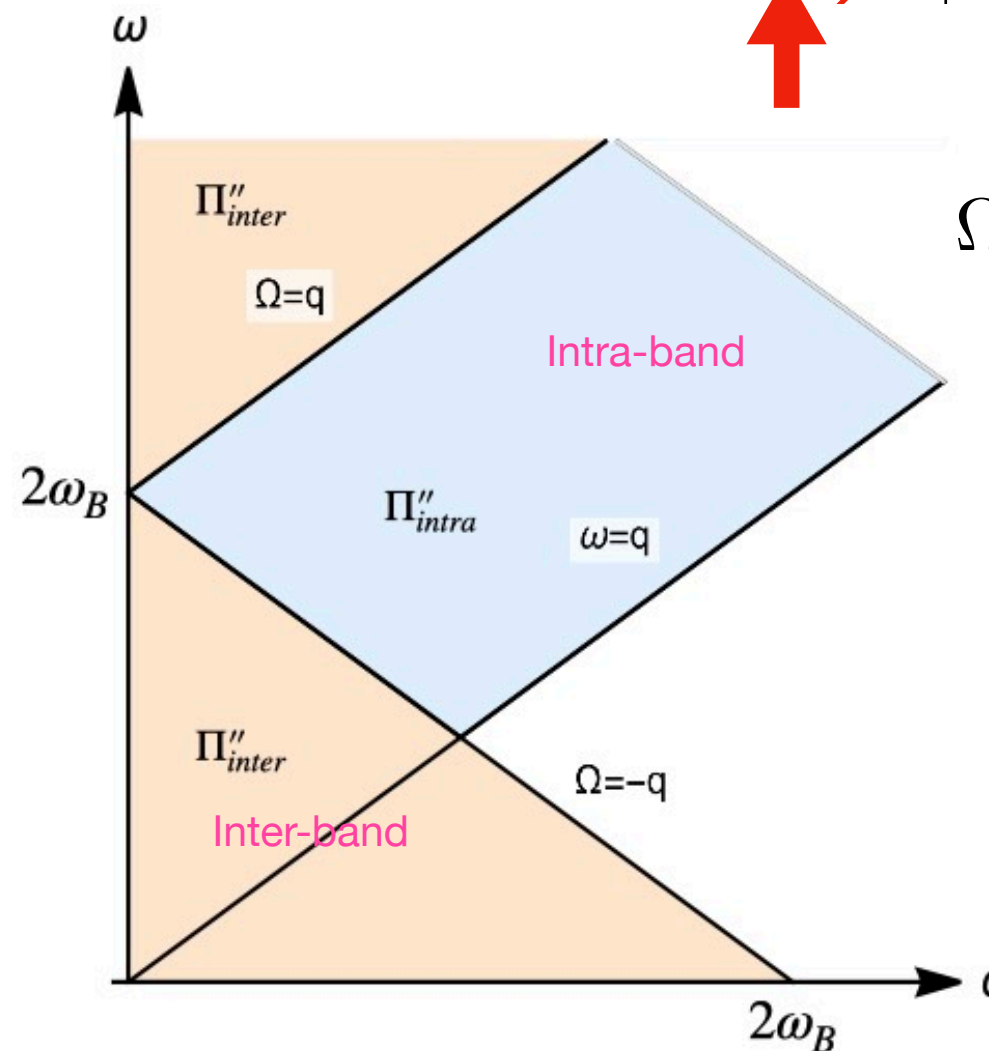
B →



Non-interacting fermions

$$H = H_0 + H_{\text{zeeman}}$$

$$H_0 = \sum_{\mathbf{p}} \Psi^\dagger \vec{\sigma} \cdot \vec{p} \Psi$$



$$\Omega = \omega - 2\omega_B$$

Interacting (short-ranged) Dirac fermions

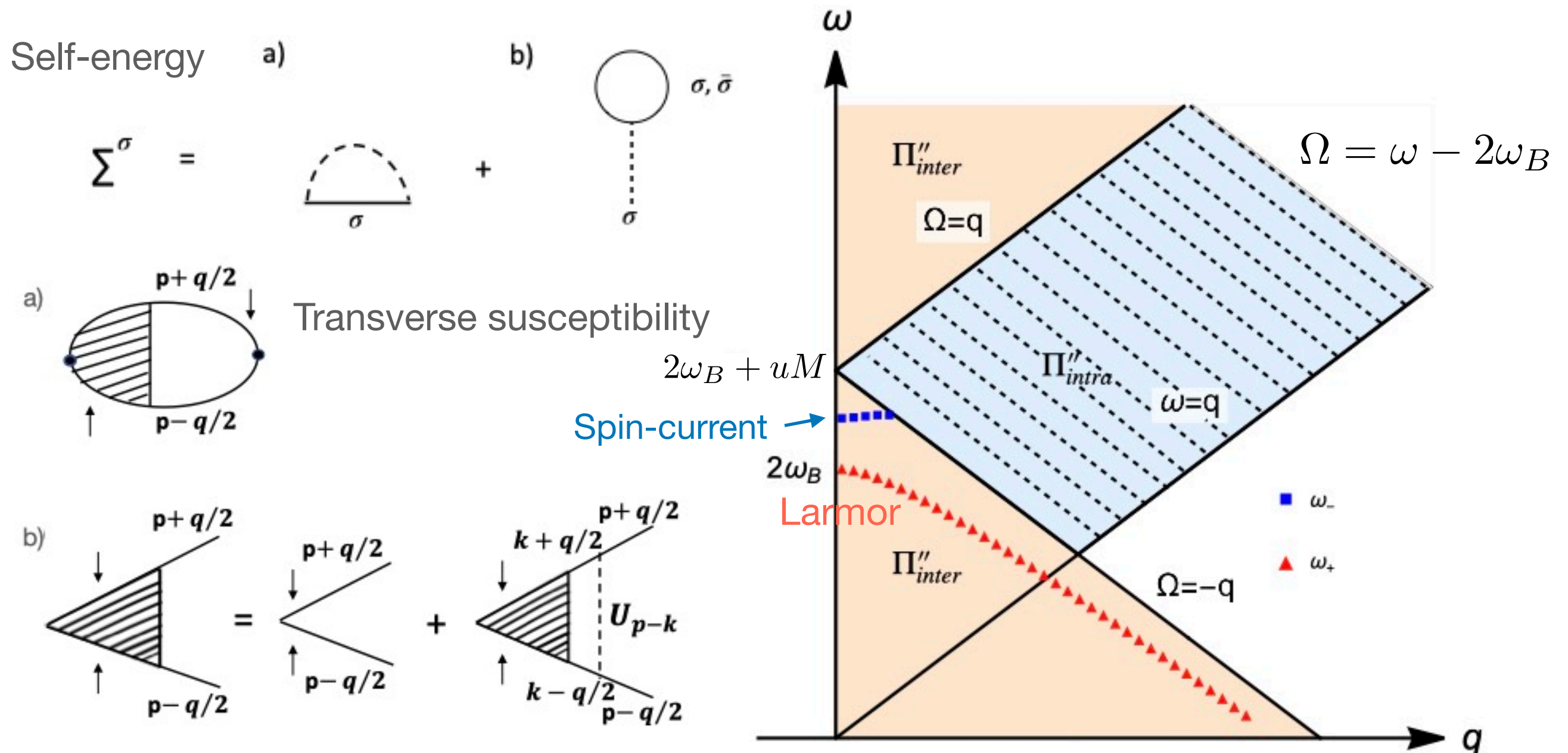
$$H = H_0 + H_{\text{zeeman}} + H_{\text{int}}$$

1) Collisionless kinetic equation for the single-particle density matrix

$$\partial_t f^{\downarrow\uparrow}(\mathbf{p}, \mathbf{x}, t) + \frac{1}{2} \{ \nabla_{\mathbf{x}}^a f^{\downarrow\uparrow}(\mathbf{p}, \mathbf{x}, t), \partial_{p_a} H \} - i [f^{\downarrow\uparrow}(\mathbf{p}, \mathbf{x}, t), H + \epsilon^{\text{HF}}] - \frac{1}{2} \{ \nabla_{\mathbf{x}}^a \epsilon^{\text{HF}}, \partial_{p_a} f^{\downarrow\uparrow}(\mathbf{p}, \mathbf{x}, t) \} = 0$$

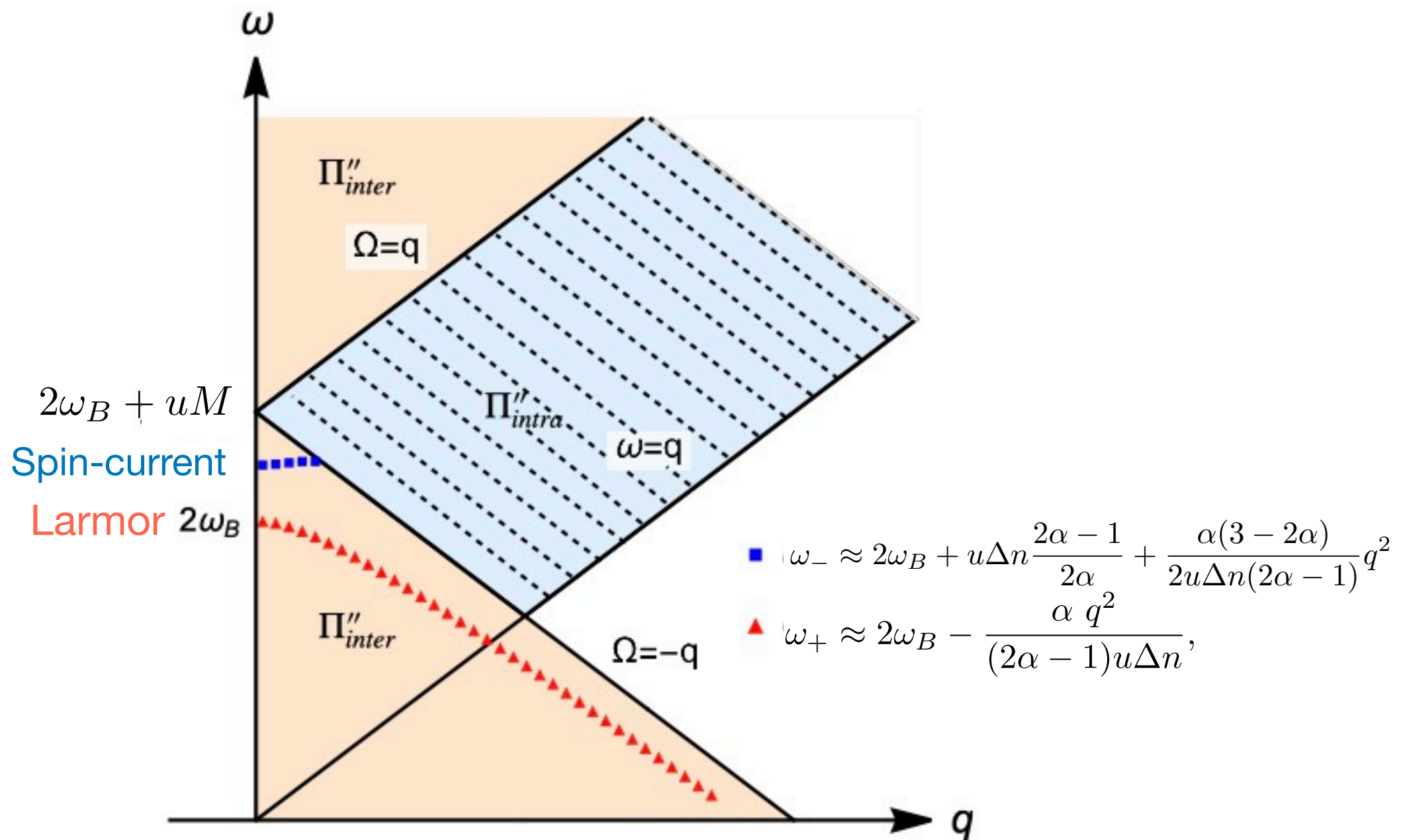
1) = 2)

2) Diagrammatic calculation



$$\Pi_{\uparrow\downarrow}(\omega, q) = \frac{2\Delta n}{\omega - \omega_+ + i \frac{u\alpha^2 q^2}{4(2\alpha-1)^2}} + \frac{2(3-2\alpha)\alpha^2 q^2}{u^2 \Delta n (2\alpha-1)^2 \left[\omega - \omega_- + i \frac{u^3 \Delta n^2 (1-2\alpha)^2}{64\alpha^3} \right]}$$

$$\alpha = 1 - u\Lambda$$



Conclusions

Probing fractionalized excitations *and* their collective modes.

Spinon Fermi surface spin liquid in magnetic field. Spinon spin wave.

New take on the magnetized Heisenberg spin chain.

Interacting Dirac fermions in magnetic field.

Dynamical response of the quantum spin liquid in magnetic field is very informative!

ESR: Spin chain with **uniform** Dzyaloshinskii - Moriya (DM) interaction

PHYSICAL REVIEW LETTERS **128**, 187202 (2022)

Editors' Suggestion

Featured in Physics

Electron Spin Resonance of the Interacting Spinon Liquid

Kirill Yu. Povarov^{1,*}, Timofei A. Soldatov^{2,†}, Ren-Bo Wang³, Andrey Zheludev,¹
Alexander I. Smirnov^{2,†} and Oleg A. Starykh^{3,‡}

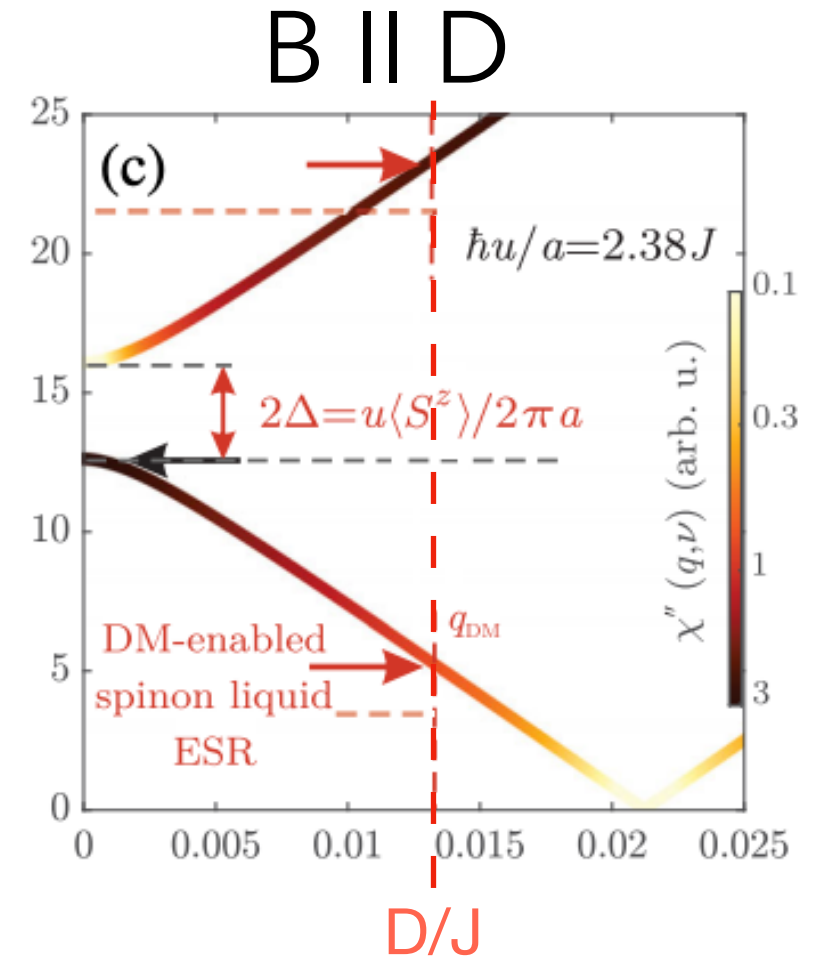
¹Laboratory for Solid State Physics, ETH Zürich, 8093 Zürich, Switzerland

²P. L. Kapitza Institute for Physical Problems RAS, 119334 Moscow, Russia

³Department of Physics and Astronomy, University of Utah, Salt Lake City, Utah 84112, USA

(Received 17 January 2022; accepted 25 March 2022; published 6 May 2022)

We report experimental verification of the recently predicted collective modes of spinons, stabilized by backscattering interaction, in a model quantum spin chain material. We exploit the unique geometry of uniform Dzyaloshinskii-Moriya interactions in $K_2CuSO_4Br_2$ to measure the interaction-induced splitting between the two components of the electron spin resonance (ESR) response doublet. From that we directly determine the magnitude of the “marginally irrelevant” backscattering interaction between spinons for the first time.



Heisenberg chain with **uniform** DM

$$\mathcal{H} = \sum_n J \vec{S}_n \cdot \vec{S}_{n+1} - \vec{D} \cdot \vec{S}_n \times \vec{S}_{n+1} - B S_n^z$$

Unitary rotation for **B || D**: $(S_n^+ = \tilde{S}_n^+ e^{iQn}, Q = \tan^{-1}(D/J), S_n^z = \tilde{S}_n^z)$ maps onto

$$\tilde{\mathcal{H}} = \sum_n \sqrt{J^2 + D^2} (\tilde{S}_n^x \tilde{S}_{n+1}^x + \tilde{S}_n^y \tilde{S}_{n+1}^y) + J \tilde{S}_n^z \tilde{S}_{n+1}^z - B \tilde{S}_n^z \approx \sum_n J \tilde{S}_n^a \tilde{S}_{n+1}^a - B \tilde{S}_n^z$$

Momentum boost $k \rightarrow k + D/J$

Structure factor $\mathcal{S}(k=0, \omega)|_{DM} = \tilde{\mathcal{S}}(D/J, \omega)|_{no DM}$

DM allows ESR to probe upper (forbidden) branch at $Q = D/J$.



- Similar materials: $Na_2CuSO_4Cl_2$ [Ohta et al. PRB 105, 144410 (2022)] and $Ca_3ReO_5Cl_2$ [Nawa et al. PR Research 2, 043121 (2020)]

Electron Spin Resonance in $\text{K}_2\text{CuSO}_4\text{Br}_2$

PHYSICAL REVIEW B **90**, 174413 (2014)

PHYSICAL REVIEW B **92**, 134417 (2015)

Quantum spin chains with frustration due to Dzyaloshinskii-Moriya interactions

Electron spin resonance in a model $S = \frac{1}{2}$ chain antiferromagnet with a uniform Dzyaloshinskii-Moriya interaction

M. Hälg,^{1,*} W. E. A. Lorenz,¹ K. Yu. Povarov,^{1,2} M. Månsson,^{1,3} Y. Skourski,⁴ and A. Zheludev¹

¹Neutron Scattering and Magnetism, Laboratory for Solid State Physics, ETH Zürich, CH-8093 Zürich, Switzerland

²P. L. Kapitza Institute for Physical Problems, RAS, 119334 Moscow, Russia

³Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institut, CH-5232 Villigen, Switzerland

⁴Hochfeld-Magnetlabor Dresden, Helmholtz-Zentrum Dresden-Rossendorf, D-01314 Dresden, Germany

(Received 25 August 2014; revised manuscript received 22 October 2014; published 12 November 2014)

A. I. Smirnov,¹ T. A. Soldatov,^{1,2} K. Yu. Povarov,^{3,*} M. Hälg,³ W. E. A. Lorenz,³ and A. Zheludev³

¹P. L. Kapitza Institute for Physical Problems, RAS, 119334 Moscow, Russia

²Moscow Institute for Physics and Technology, 141700 Dolgoprudny, Russia

³Neutron Scattering and Magnetism, Laboratory for Solid State Physics, ETH Zürich, Switzerland

(Received 27 July 2015; revised manuscript received 6 October 2015; published 22 October 2015)

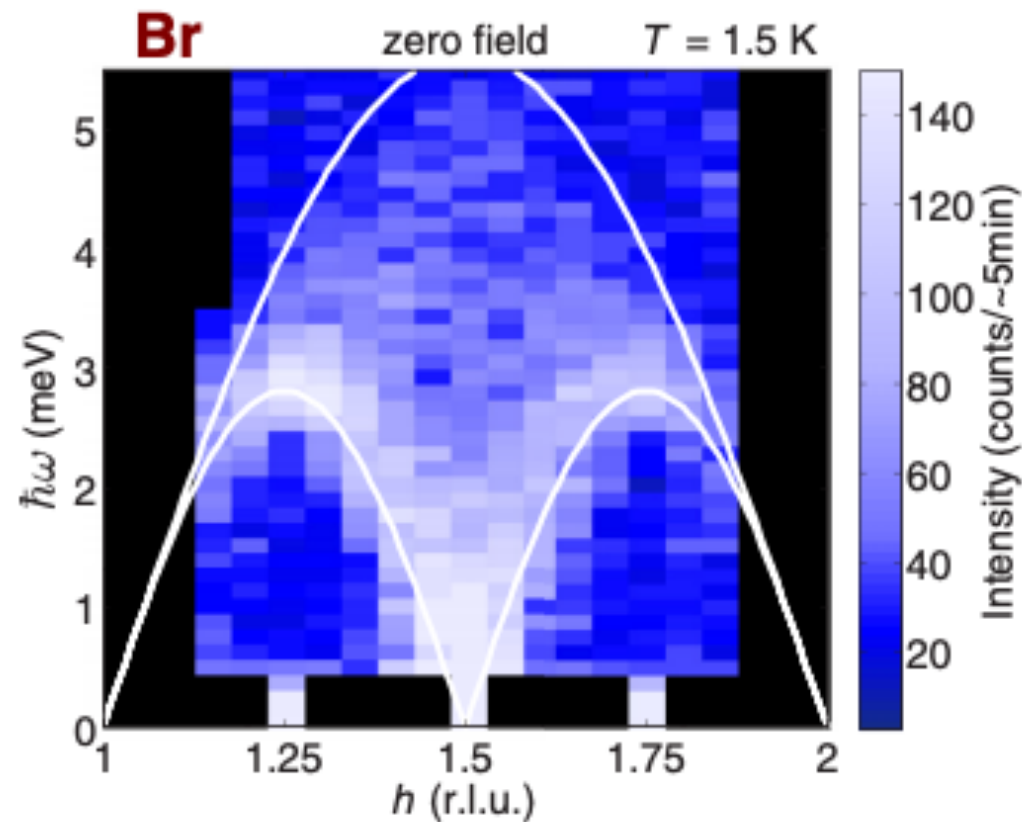


FIG. 7. (Color online) Neutron scattering intensity map of the two-spinon continuum along the a^* axis [$\mathbf{q} = (h, 0, 0)$] for $\text{K}_2\text{CuSO}_4\text{Br}_2$ in zero magnetic field. Raw data are shown in Fig. 8. The white line indicates the lower and upper boundary of the continuum following Eqs. (4) and (5) with $J_{\text{Br},a} = 20.7$ K.

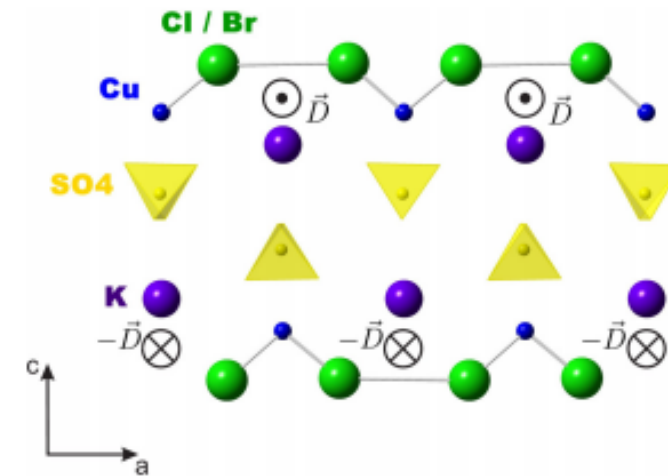


FIG. 9. (Color online) The antisymmetric contribution \mathbf{D} to J_a points along the b axis, is uniform along the chain, and antiparallel in adjacent chains.

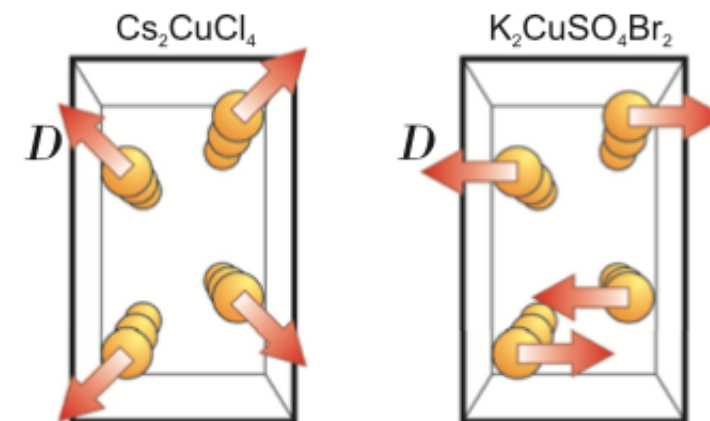
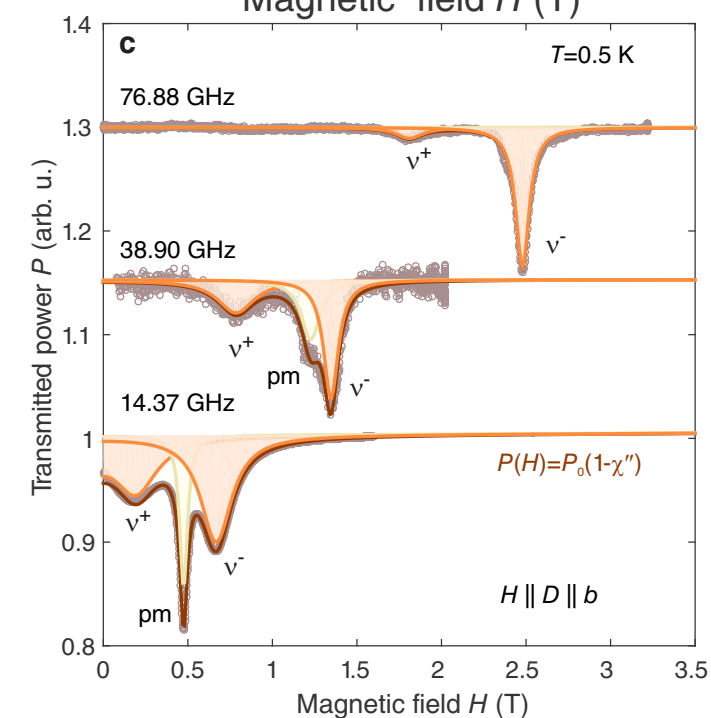
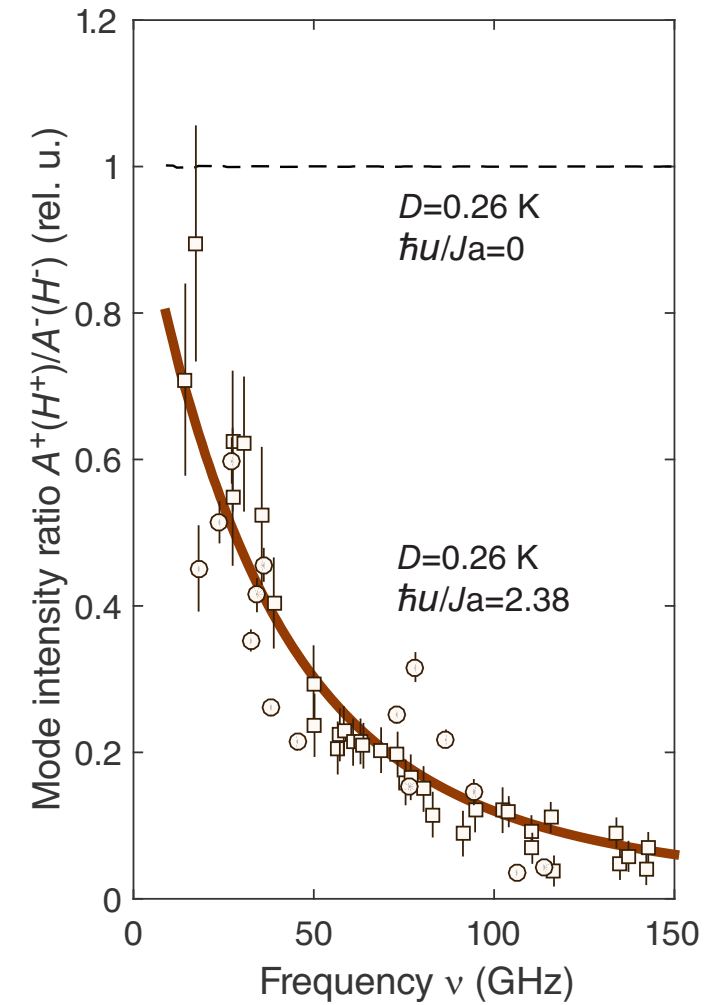
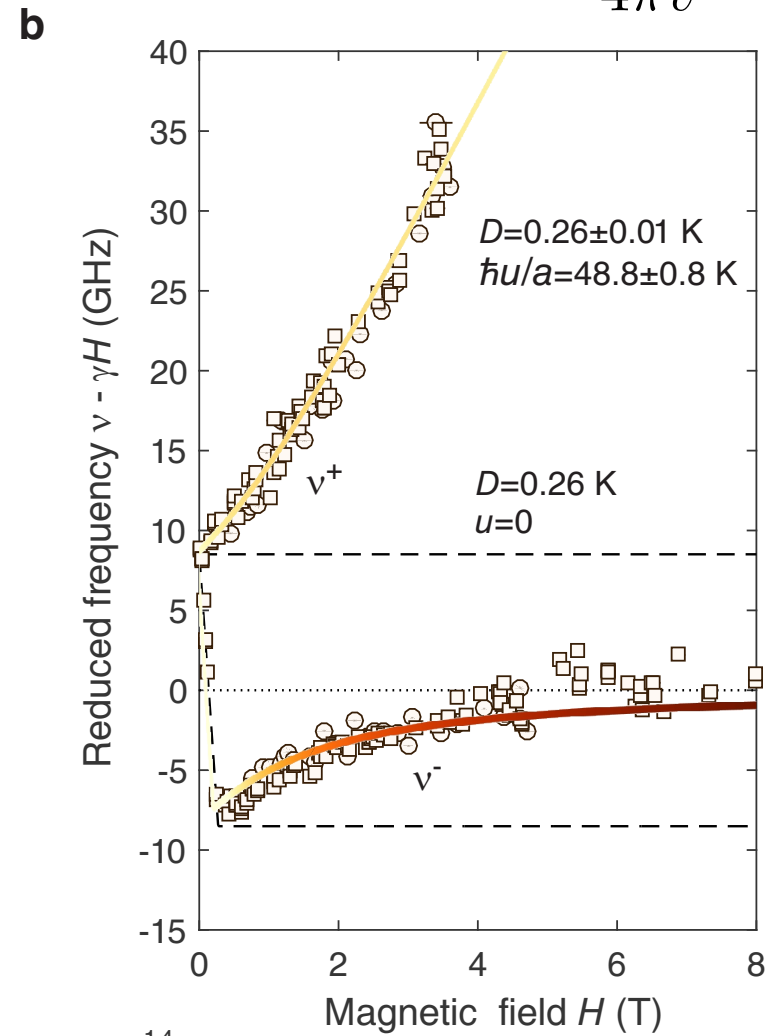
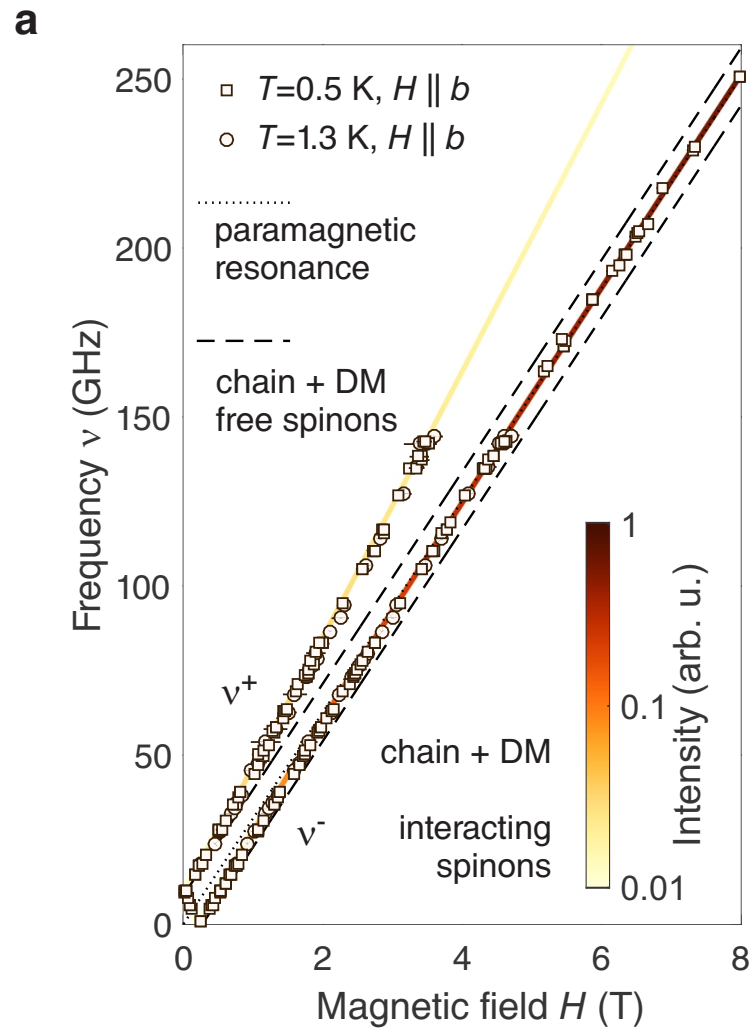


FIG. 2. (Color online) Comparison of the Dzyaloshinskii-Moriya vectors in Cs_2CuCl_4 and $\text{K}_2\text{CuSO}_4\text{Br}_2$. Perspective view along the spin chains.

Qualitative difference between (strongly) interacting spinons and the non-interacting approximation!

Notation change: $g = u \rightarrow \delta = \frac{u}{4\pi v} = \frac{u}{2\pi^2 J} = 0.12$



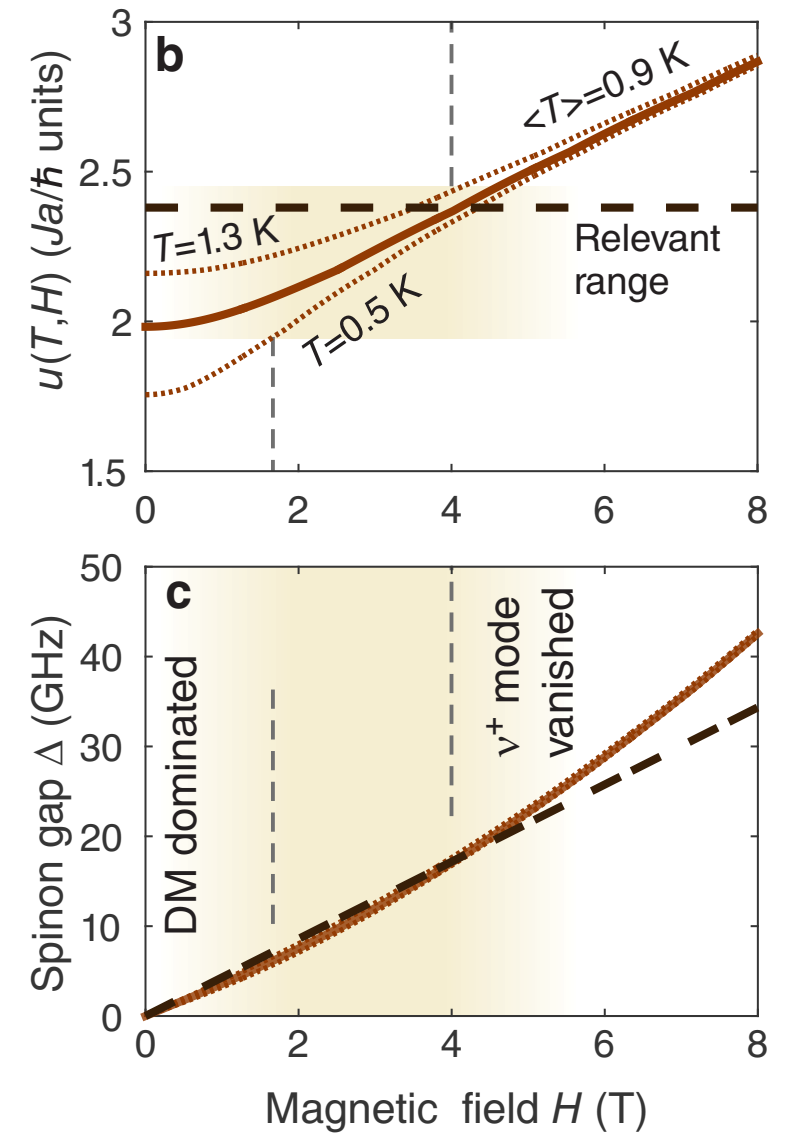
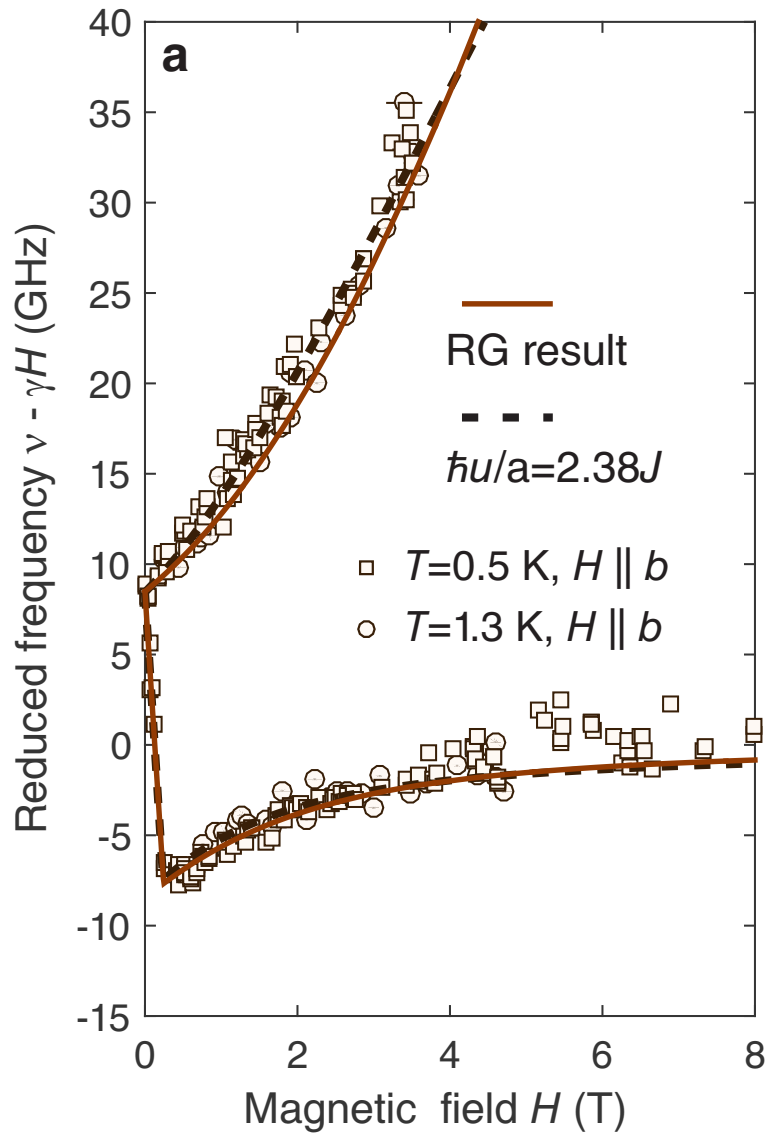
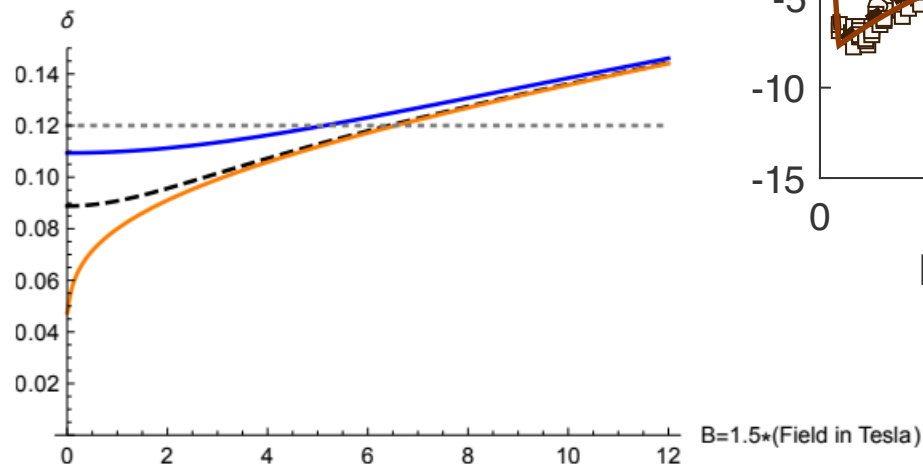
----- non-interacting spinon gas

————— interacting spinon liquid

Comparison with the Renormalization Group approach

$$\frac{1}{2\delta} + \frac{\ln 2\delta}{2} = \ln \left(\sqrt{\frac{\pi}{2}} e^{1/4} \frac{J}{T} \right) - \text{Re} \left[\psi \left(1 + i \frac{g\mu_B H}{2\pi T} \right) \right]$$

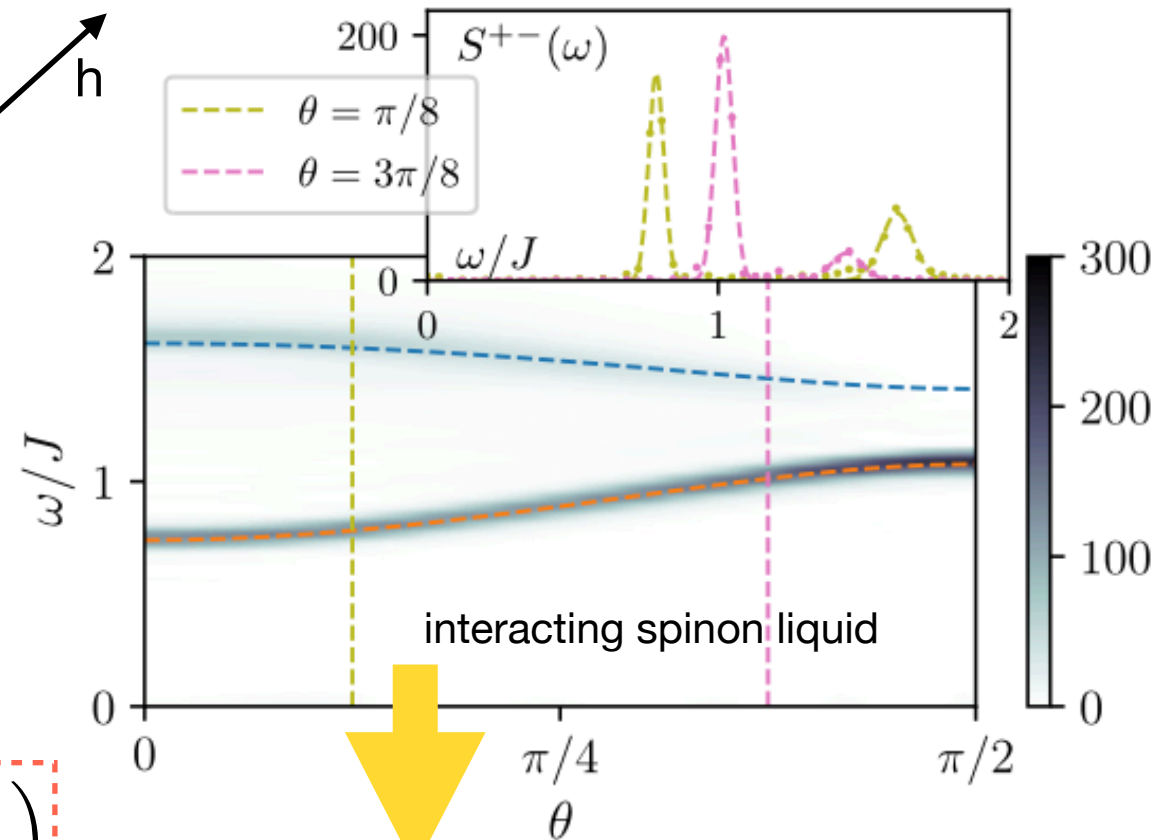
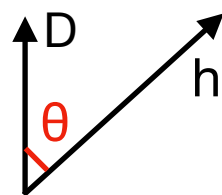
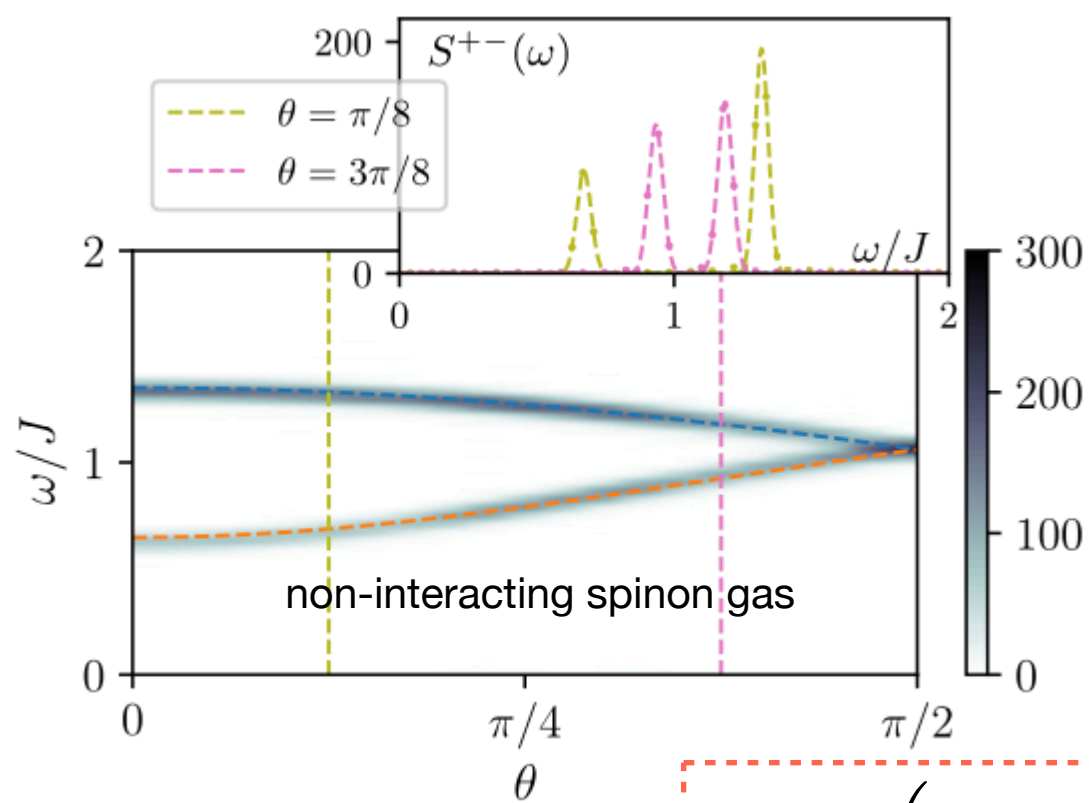
$$\delta = \frac{u}{4\pi v}$$



SUPP. FIG. 3. Solution of Eq.(S.65) for $T = 1.3\text{K}$ (solid blue line), $T = 0.5\text{K}$ (dashed black line) and $T = 0.0005\text{K}$ (solid orange line) as a function of field B from 0 to 8 T. The field is converted into Kelvins by $B = 1.5 \times (\text{field in Tesla})\text{K}$. Dotted gray line shows $\delta = 0.12$.

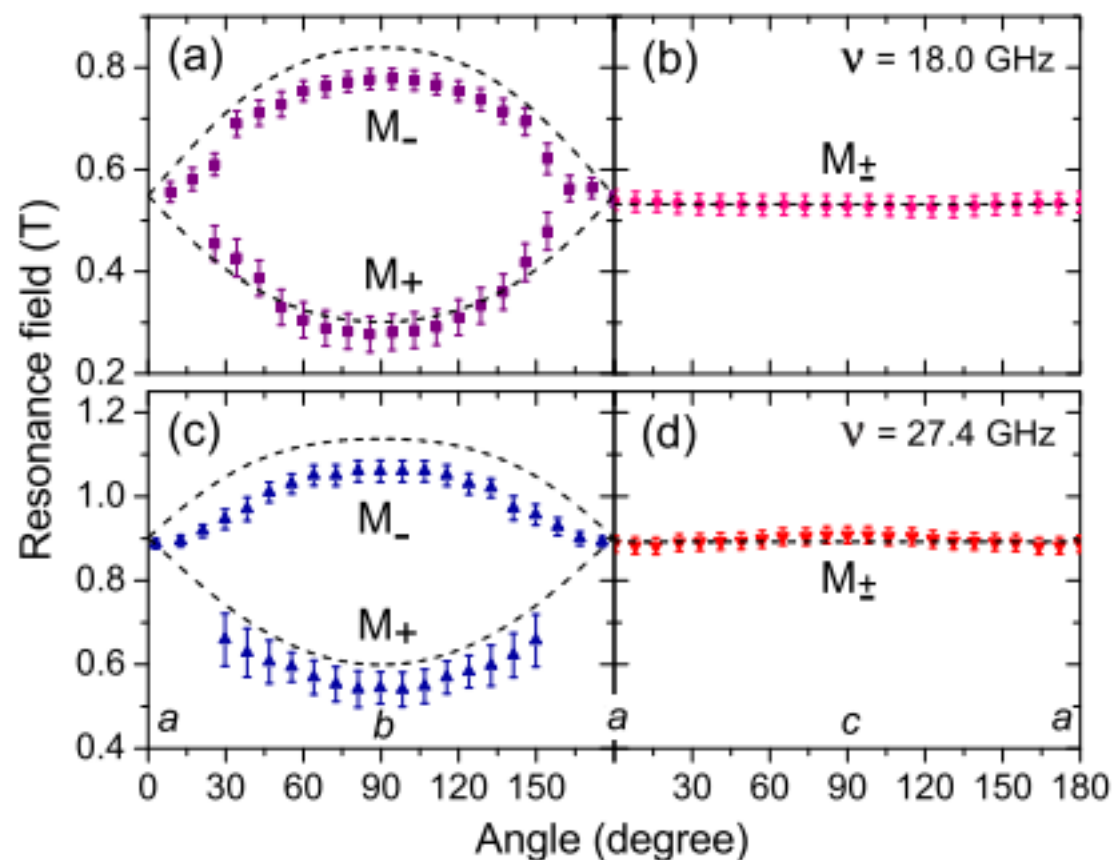
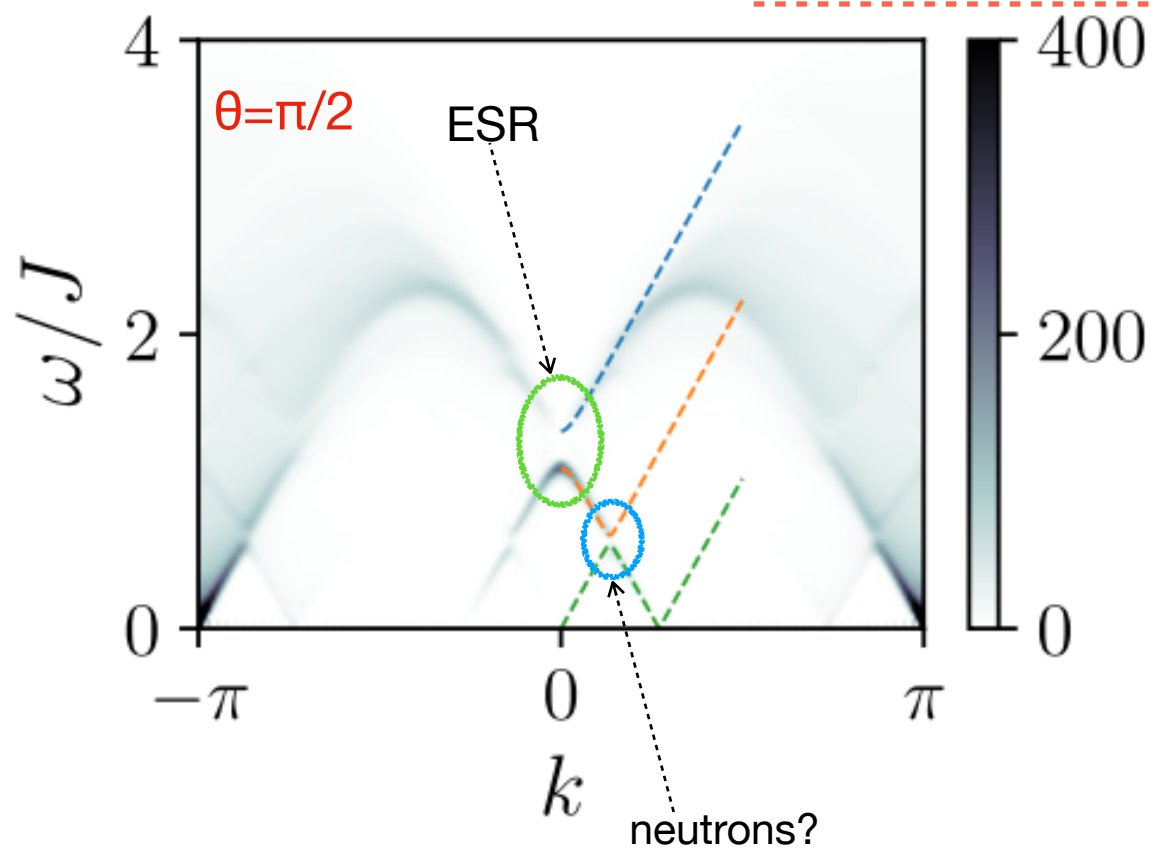
First ever spectroscopic measurement
of the backscattering spinon interaction u (=g)

Angular dependence of the ESR response



$$\partial_x \rightarrow \left(\partial_x + \mathbf{D} \times \right)$$

Smirnov et al PHYSICAL REVIEW B 92, 134417 (2015)





Quantum spintronics

LETTERS

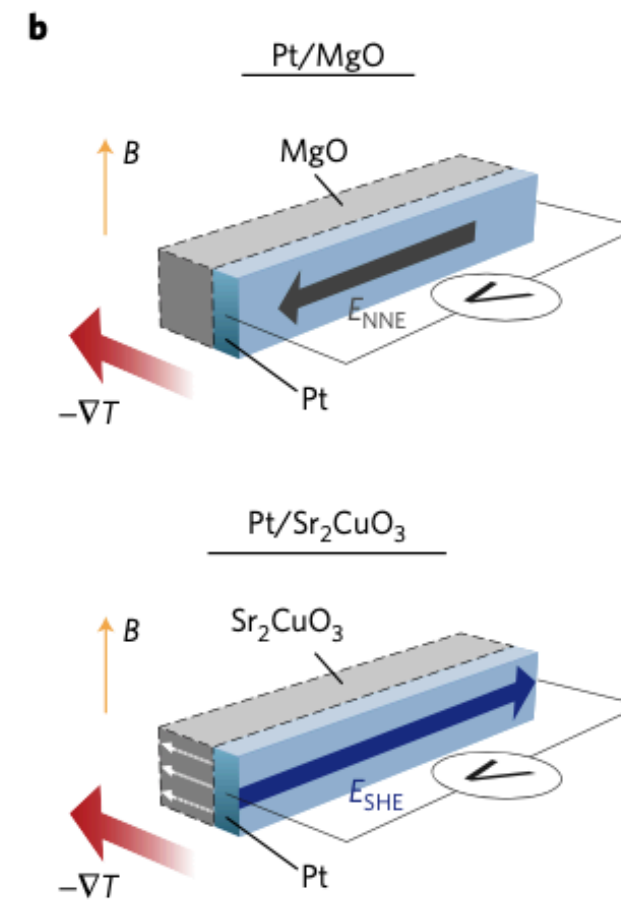
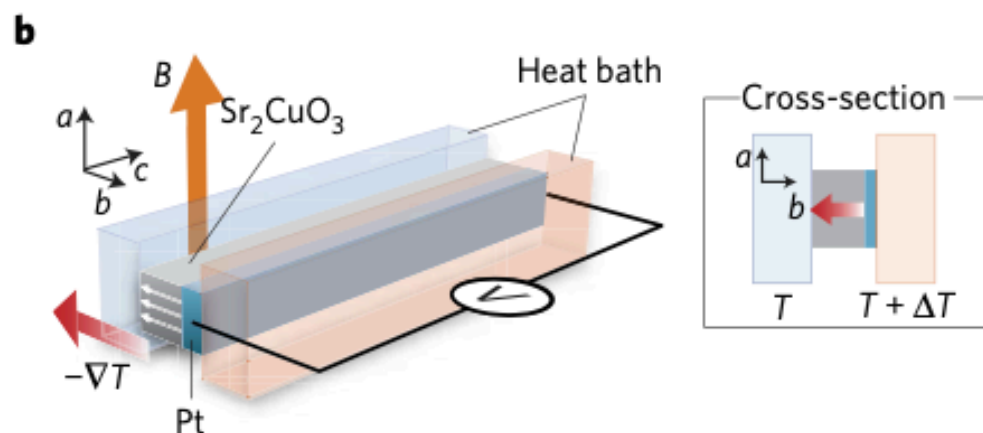
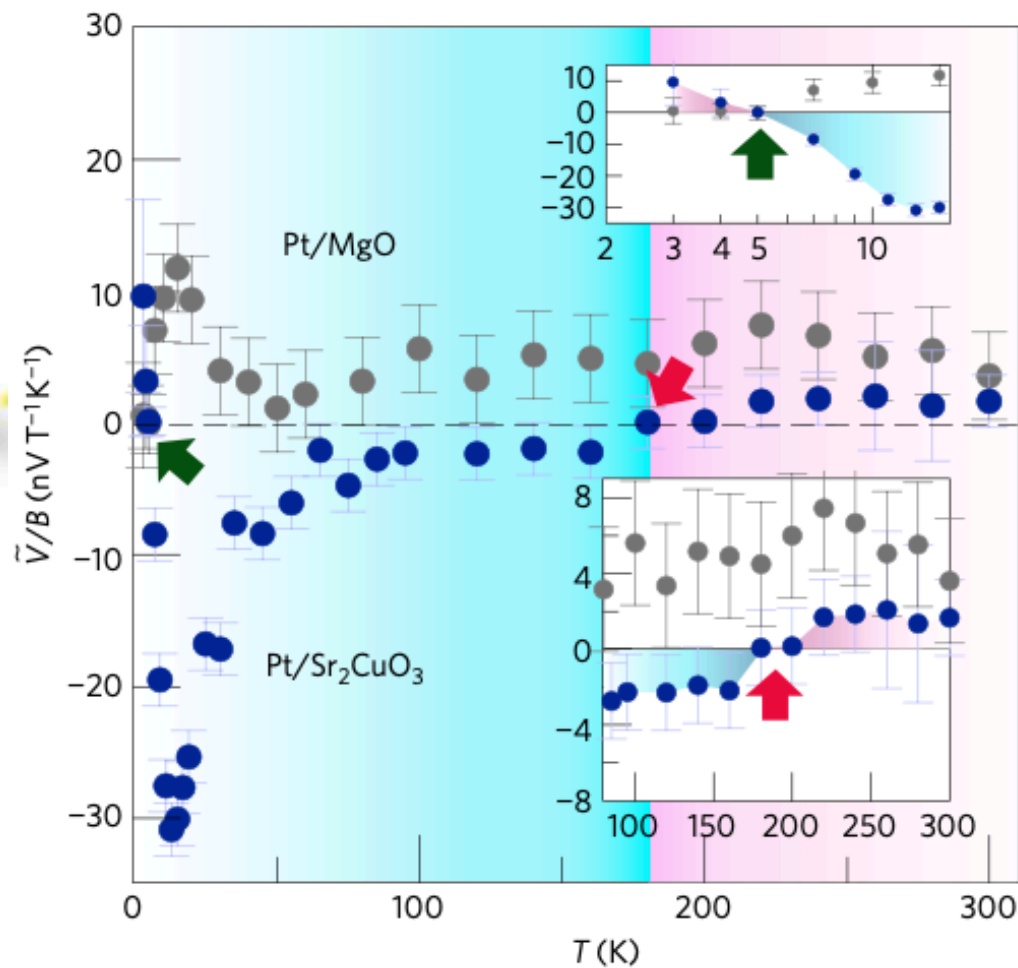
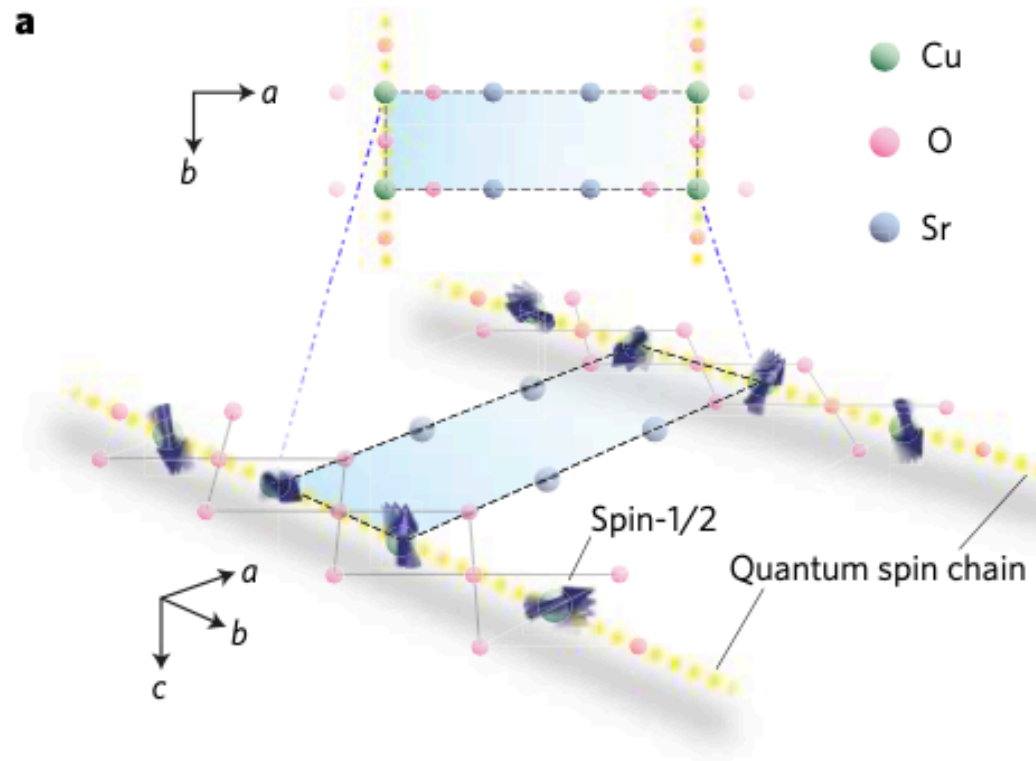
PUBLISHED ONLINE: 26 SEPTEMBER 2016 | DOI: 10.1038/NPHYS3895

nature
physics

The essence: spin current across the tunneling barrier between different magnetic materials due to the finite temperature gradient δT

One-dimensional spinon spin currents

Daichi Hirobe^{1*}, Masahiro Sato^{2,3†}, Takayuki Kawamata⁴, Yuki Shiomi^{1,2}, Ken-ichi Uchida^{1,5}, Ryo Iguchi^{1,2}, Yoji Koike⁴, Sadamichi Maekawa^{2,3} and Eiji Saitoh^{1,2,3,6*}



Quantum spintronics

The essence: spin current across the tunneling barrier between different magnetic materials due to the finite temperature gradient δT

$$1. \quad \vec{S}(x_i) \rightarrow \vec{J}_R + \vec{J}_L + \frac{(-1)^{x_i}}{2} \left(\psi_R^\dagger \vec{\sigma} \psi_L + \psi_L^\dagger \vec{\sigma} \psi_R \right)$$

Interface = tunneling contact = open boundary condition for the spin chain

$$\psi(x=0, t) = 0 \rightarrow \psi_L(x=0, t) = -\psi_R(x=0, t)$$

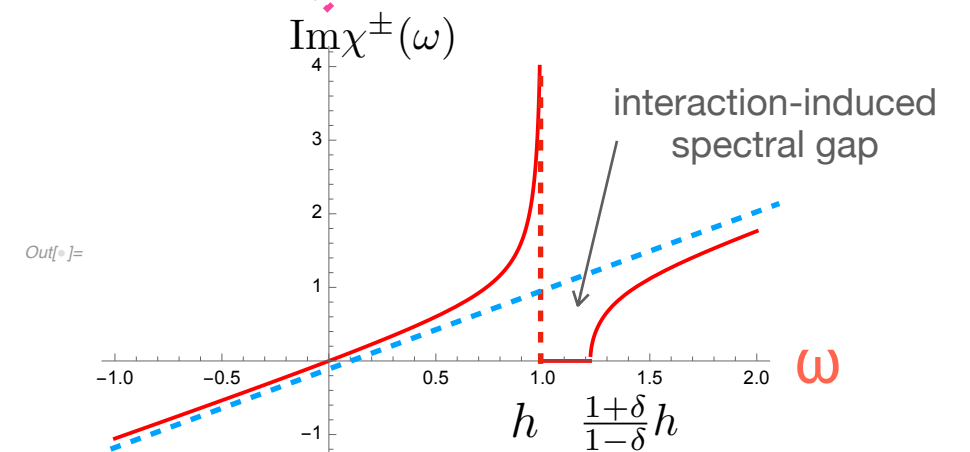
$$\rightarrow \vec{S}(x=0, t) = 0 \text{ and } \vec{S}(x=1, t) \approx 2 \left(\vec{J}_R + \vec{J}_L \right)$$

$$2. \quad I_{\text{spin}} \propto \frac{J_{\text{interface}}^2}{T^2} \int_{-\infty}^{+\infty} d\omega \underbrace{\text{Im}\chi_{\text{Pt}}^{\pm}(\omega)}_{\omega} \underbrace{\text{Im}\chi_{\text{chain}}^{\pm}(\omega)}_{\text{local susceptibility}} \frac{\omega \delta T}{\sinh^2[\omega/2T]}$$

$\rightarrow I_{\text{spin}} = 0$ if $\text{Im}\chi_{\text{chain}}^{\pm}(\omega)$ is odd.

Non-interacting spinon gas: $\text{Im}\chi_{\text{chain}}^{\pm}(\omega) \propto \omega$

Interacting spinon liquid: finite spin current for $\delta > 0$, $I_{\text{spin}} \neq 0$



$$\text{Im}\chi_{\text{chain}}^{\pm}(\omega) \propto \omega \sqrt{\frac{\omega - (1+\delta)h/(1-\delta)}{\omega - h}} \left[\Theta(h - \omega) + \Theta(\omega - (1+\delta)h/(1-\delta)) \right]$$

Experiment

Extended Quantum Critical Phase in a Magnetized Spin- $\frac{1}{2}$ Antiferromagnetic Chain

M. B. Stone,^{1,*} D. H. Reich,¹ C. Broholm,^{1,2} K. Lefmann,³ C. Rischel,⁴ C. P. Landee,⁵ and M. M. Turnbull⁵

¹Department of Physics and Astronomy, Johns Hopkins University, Baltimore, Maryland 21218, USA

²National Institute of Standards and Technology, Gaithersburg, Maryland 20899, USA

³Materials Research Department, Risø National Laboratory, DK-4000 Roskilde, Denmark

⁴Ørsted Laboratory, Niels Bohr Institute, University of Copenhagen, DK-2100, København Ø, Denmark

⁵Carlson School of Chemistry and Department of Physics, Clark University, Worcester, Massachusetts 01610, USA
(Received 18 March 2003; published 17 July 2003)

Measurements are reported of the magnetic field dependence of excitations in the quantum critical state of the spin $S = 1/2$ linear chain Heisenberg antiferromagnet copper pyrazine dinitrate (CuPzN). The complete spectrum was measured at $k_B T/J \leq 0.025$ for $H = 0$ and $H = 8.7$ T, where the system is $\sim 30\%$ magnetized. At $H = 0$, the results are in agreement with exact calculations of the dynamic spin correlation function for a two-spinon continuum. At $H = 8.7$ T, there are multiple overlapping continua with incommensurate soft modes. The boundaries of these continua confirm long-standing predictions, and the intensities are consistent with exact diagonalization and Bethe ansatz calculations.

DOI: 10.1103/PhysRevLett.91.037205

PACS numbers: 75.10.Jm, 75.40.Gb, 75.50.Ec

Finally, we note that Fig. 4(a) shows some evidence of weak scattering intensity for $\hbar\omega > 2$ meV. This could be due to the presence of short chains resulting from impurities, or to higher-order processes not included in the spinon/psinon picture. However, we note that our error bars are much larger here than at lower energy due to shorter counting times (see Fig. 2), and so a definitive statement on the existence of excitations in this energy range cannot be made at this time.

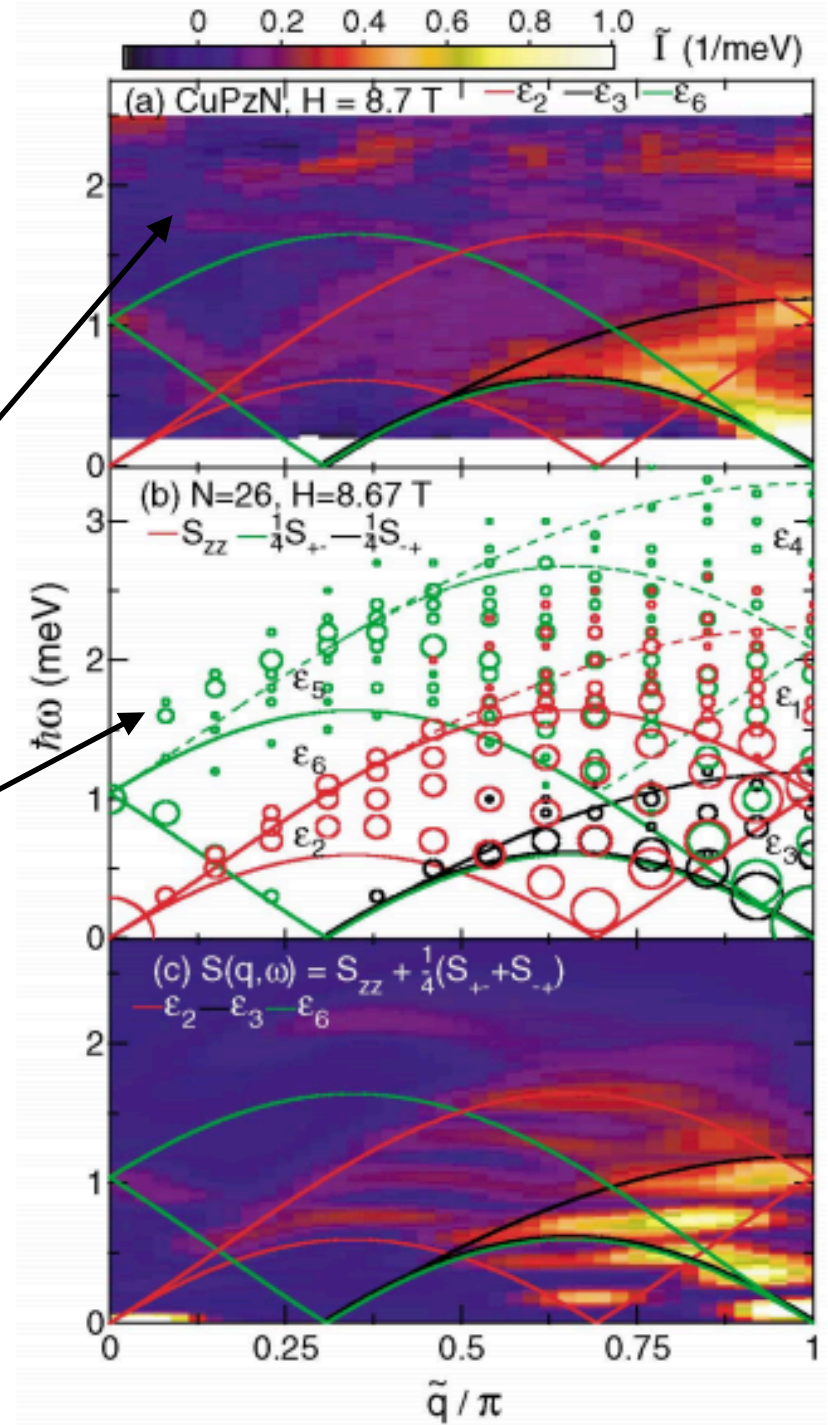


FIG. 4 (color). (a) Inelastic neutron scattering intensity $\tilde{I}_m(\tilde{q}, \omega)$ for CuPzN at $T = 0.25$ K and $H = 8.7$ T. (b) Calculations of the different components of $S(\tilde{q}, \omega)$ for $N = 26$ spins and $m = 2/13$. The area of each circle is proportional to $S(\tilde{q}, \omega)$. (c) $\tilde{I}_m(\tilde{q}, \omega)$ calculated for ensemble of chains with $N = 24, 26,$ and 28 . The curves in (a)–(c) show the bounds of the excitation continua ϵ_1 – ϵ_6 . Solid lines: Continua predicted to predominate as $N \rightarrow \infty$. In (b), ϵ_2 (upper) = ϵ_1 (lower).

Dynamical correlation functions of the $S=1/2$ nearest-neighbor and Haldane-Shastry Heisenberg antiferromagnetic chains in zero and applied fields

Kim Lefmann*

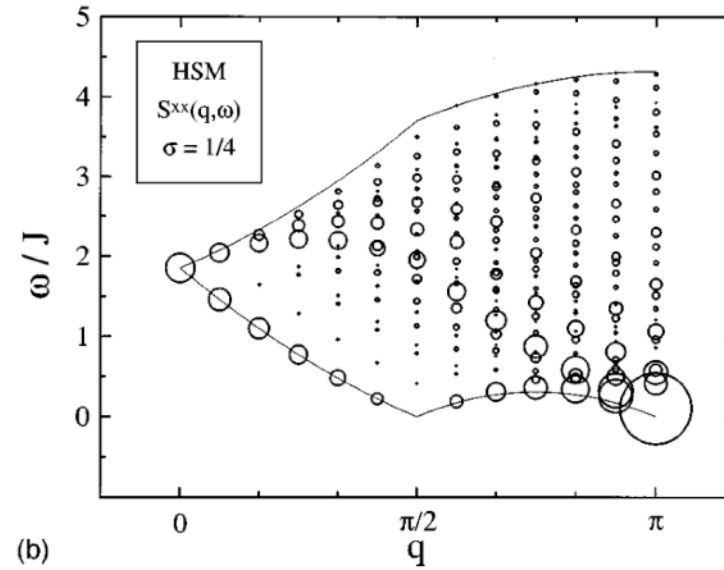
Department of Solid State Physics, Risø National Laboratory, DK-4000 Roskilde, Denmark

Christian Rischel†

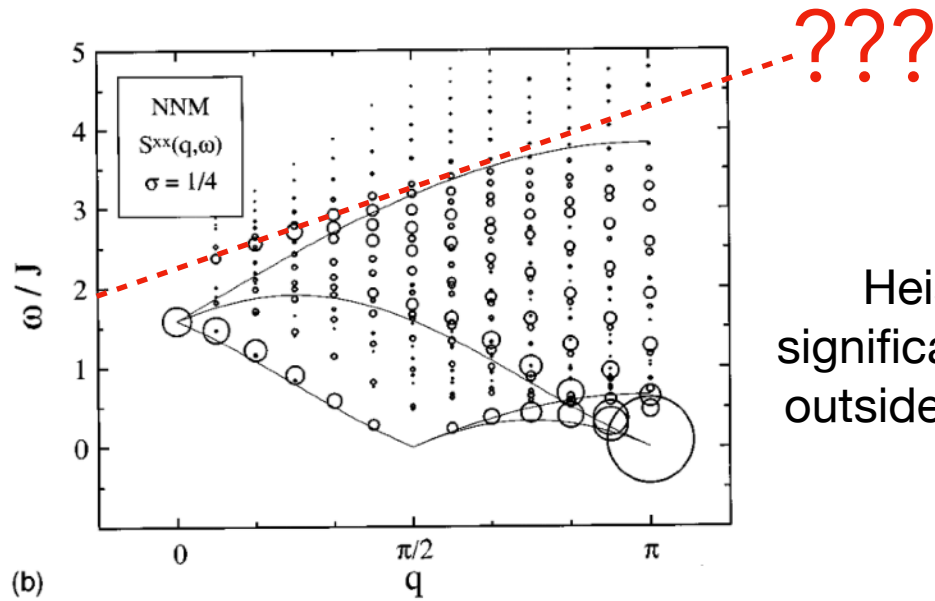
Ørsted Laboratory, Niels Bohr Institute, University of Copenhagen, DK-2100 København Ø, Denmark

(Received 12 February 1996)

We present a numerical diagonalization study of two one-dimensional $S=1/2$ antiferromagnetic Heisenberg chains, having nearest-neighbor and Haldane-Shastry ($1/r^2$) interactions, respectively. We have obtained the $T=0$ dynamical correlation function, $S^{\alpha\alpha}(q, \omega)$, for chains of length $N=8-28$. We have studied $S^{zz}(q, \omega)$ for the Heisenberg chain in zero field, and from finite-size scaling we have obtained a limiting behavior that for large ω deviates from the conjecture proposed earlier by Müller *et al.* For both chains we describe the behavior of $S^{zz}(q, \omega)$ and $S^{xx}(q, \omega)$ for selected values of the applied field, and compare with previous work by Müller *et al.* and Talstra and Haldane. Suggestions for future finite-field neutron scattering experiments are made. [S0163-1829(96)00733-3]



(b) Haldane-Shastry chain: non-interacting 2-spinon continuum

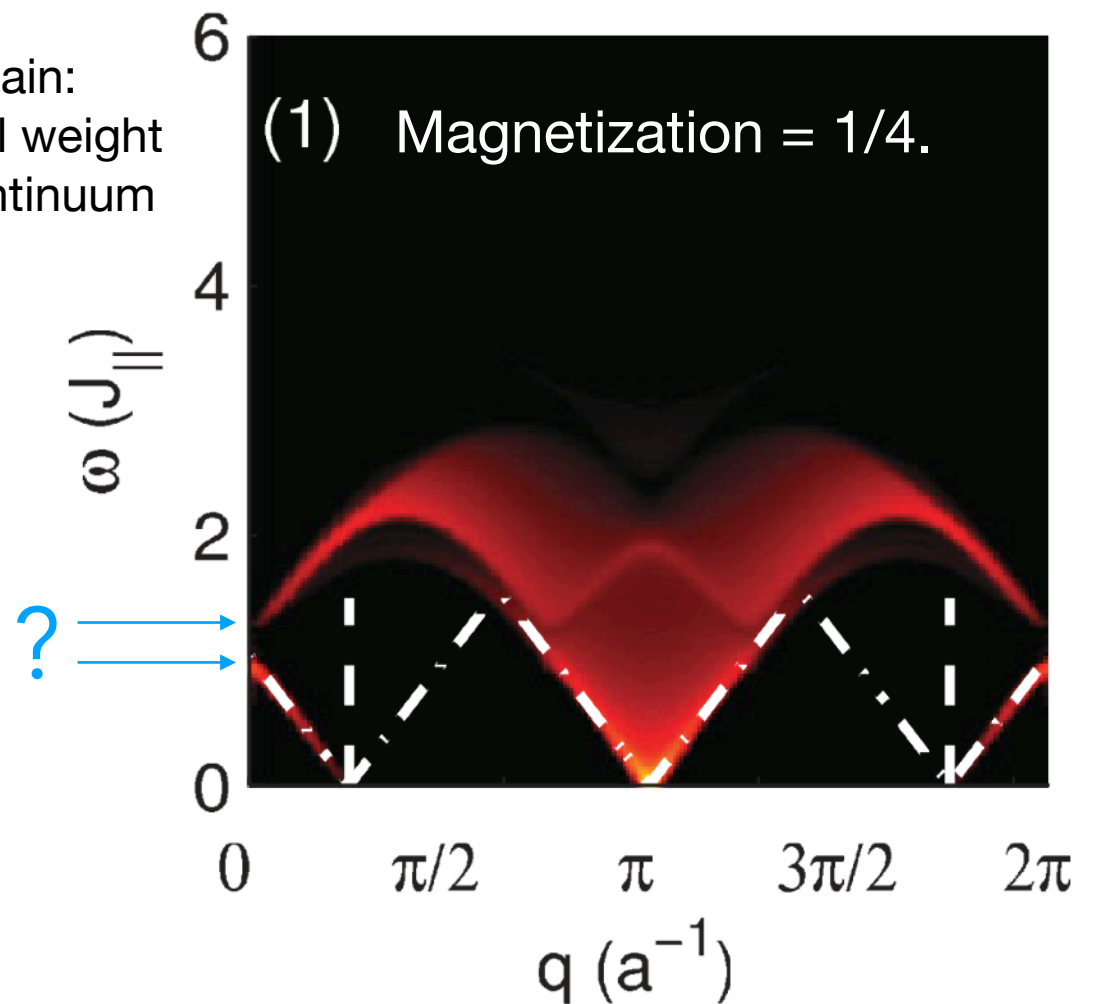


Heisenberg chain: significant spectral weight outside Muller continuum

Clearly, looks more like an interacting Fermi liquid than a non-interacting Fermi gas...

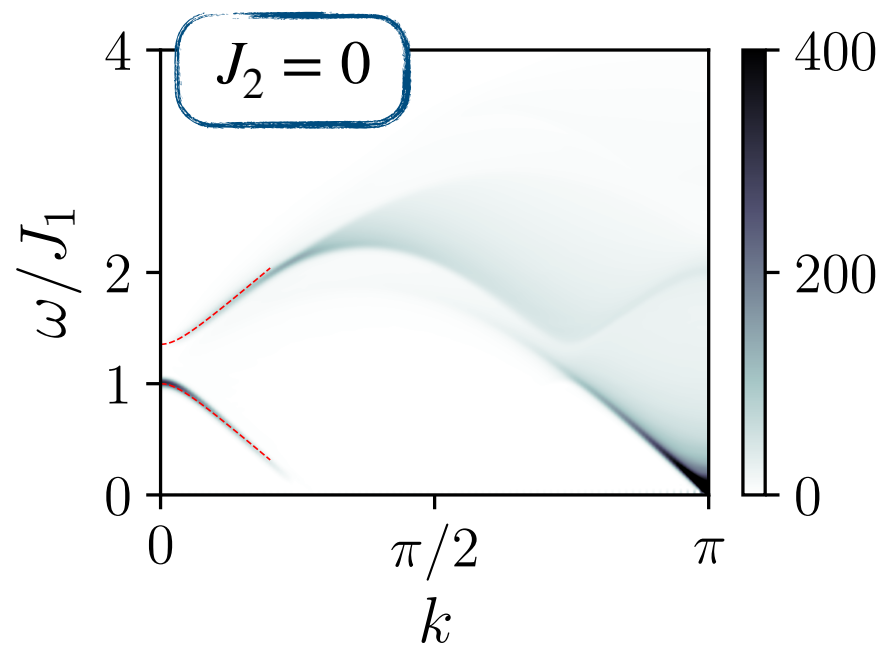
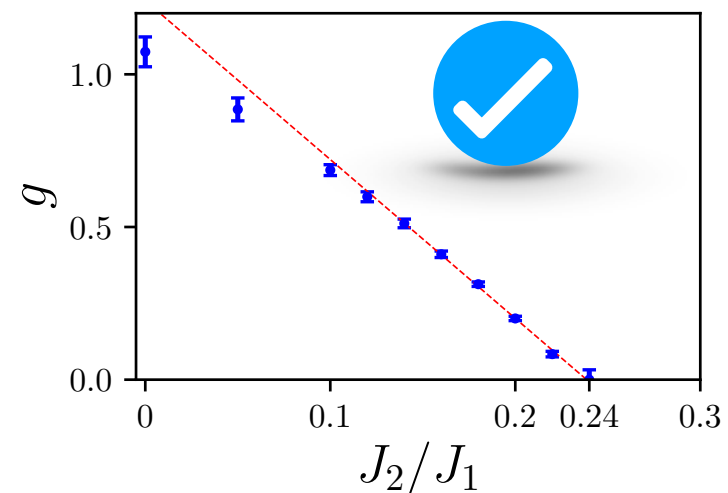
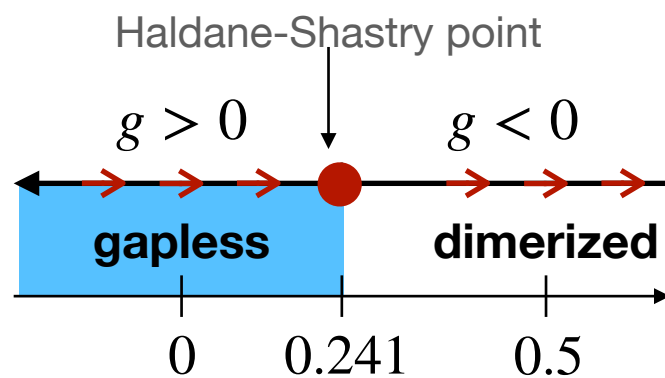
Statics and dynamics of weakly coupled antiferromagnetic spin- $1/2$ ladders in a magnetic field

Pierre Bouillot, Corinna Kollath, Andreas M. Läuchli, Mikhail Zvonarev, Benedikt Thielemann, Christian Rüegg, Edmond Orignac, Roberta Citro, Martin Klanjšek, Claude Berthier, Mladen Horvatić, and Thierry Giamarchi
Phys. Rev. B **83**, 054407 – Published 9 February 2011



Numerical results

$$B/J_1 = 1$$



interacting spinon liquid

