

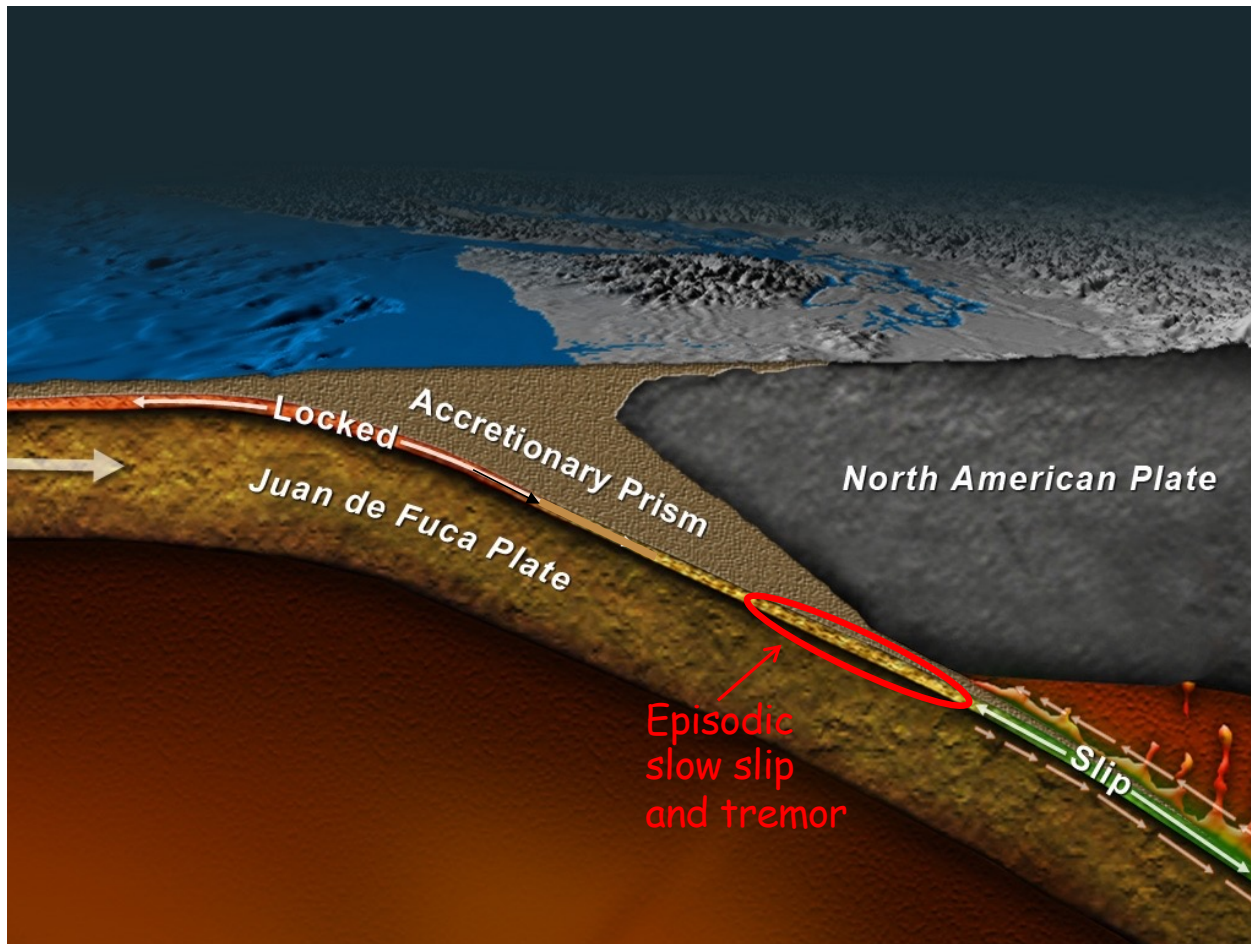
# Workshop on Mechanics of the Earthquake Cycle

ICTP, Trieste, 16-27 October, 2023

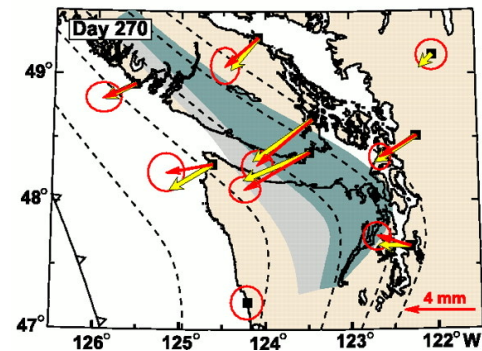
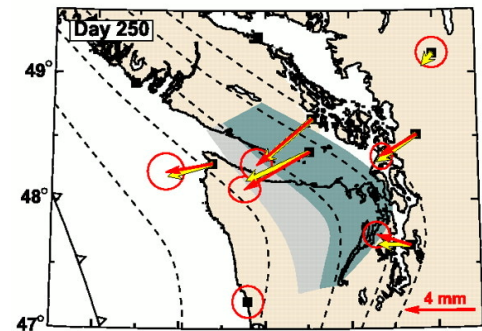
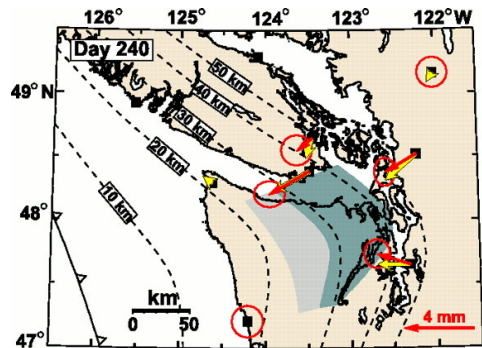
Wednesday October 18, Lecture 2:

## Episodic slow slip and tremor in subduction zones: Some observations, some models

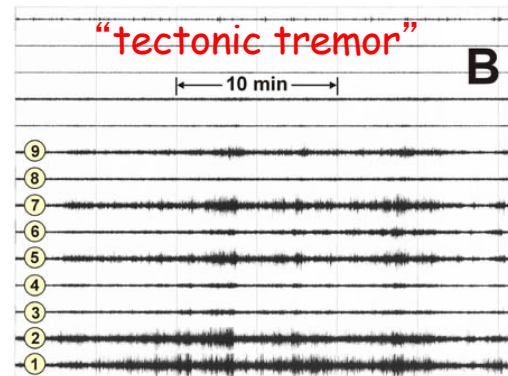
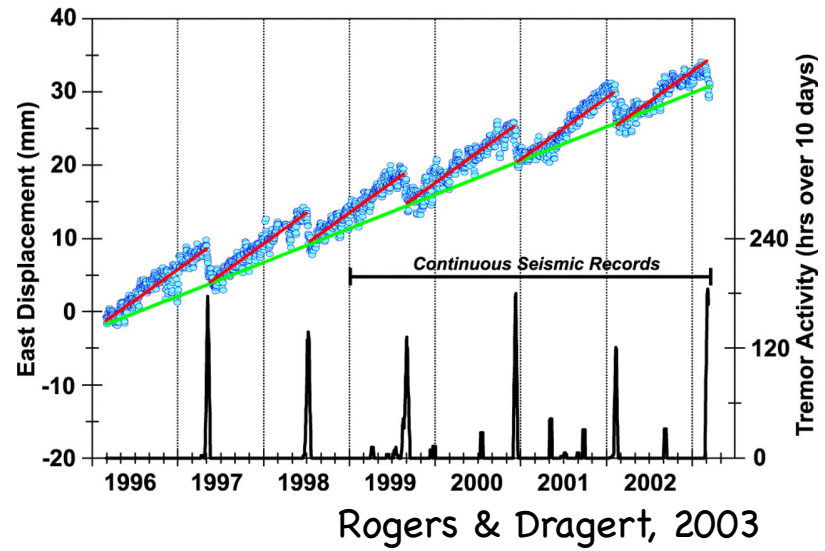
Allan Rubin, Princeton University



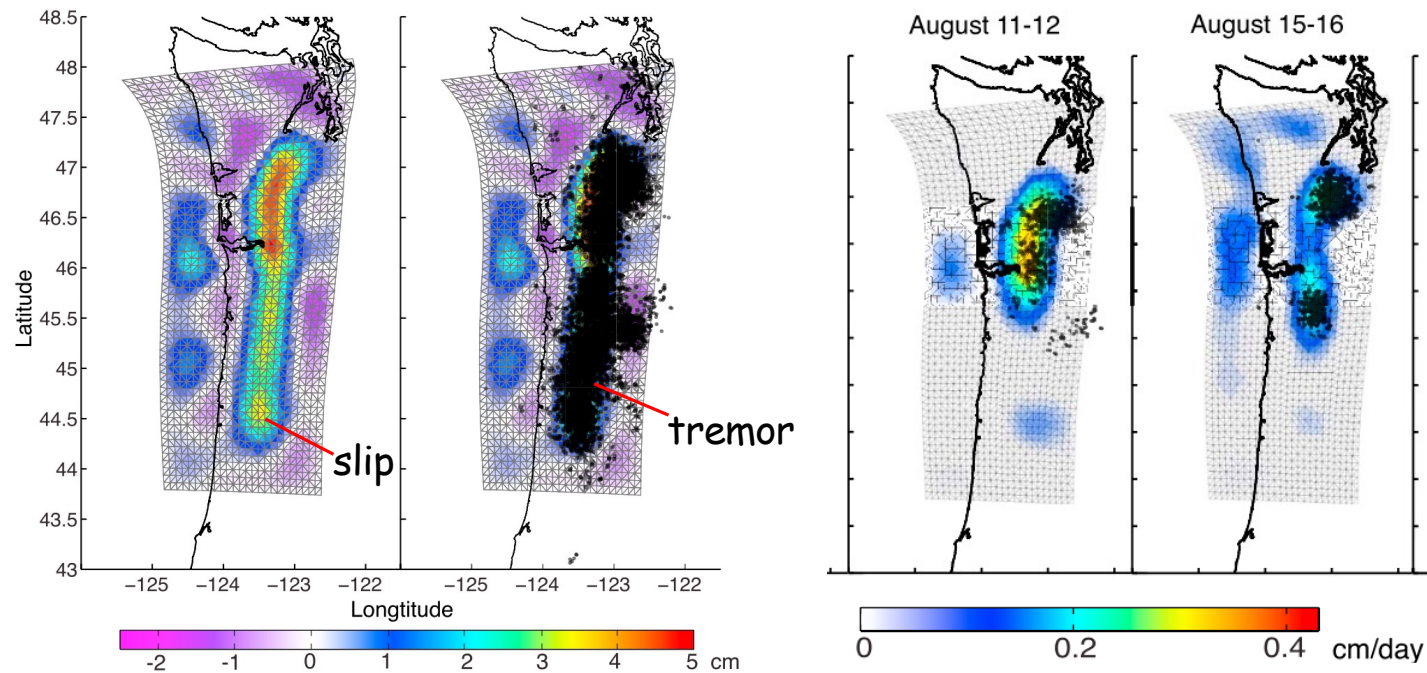
(from Steve Malone via the Central Wash. U. Geodesy website)



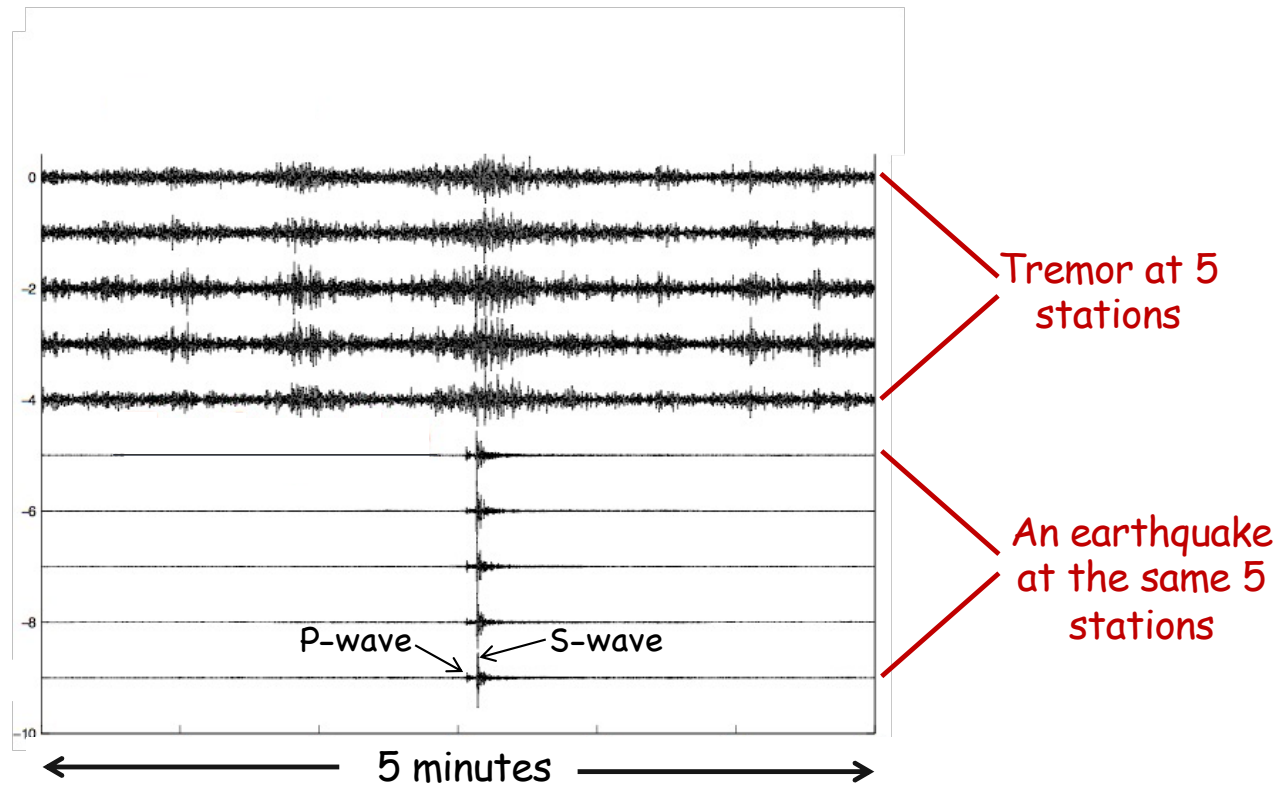
Dragert et al., 2001  
(summer 1999 event)



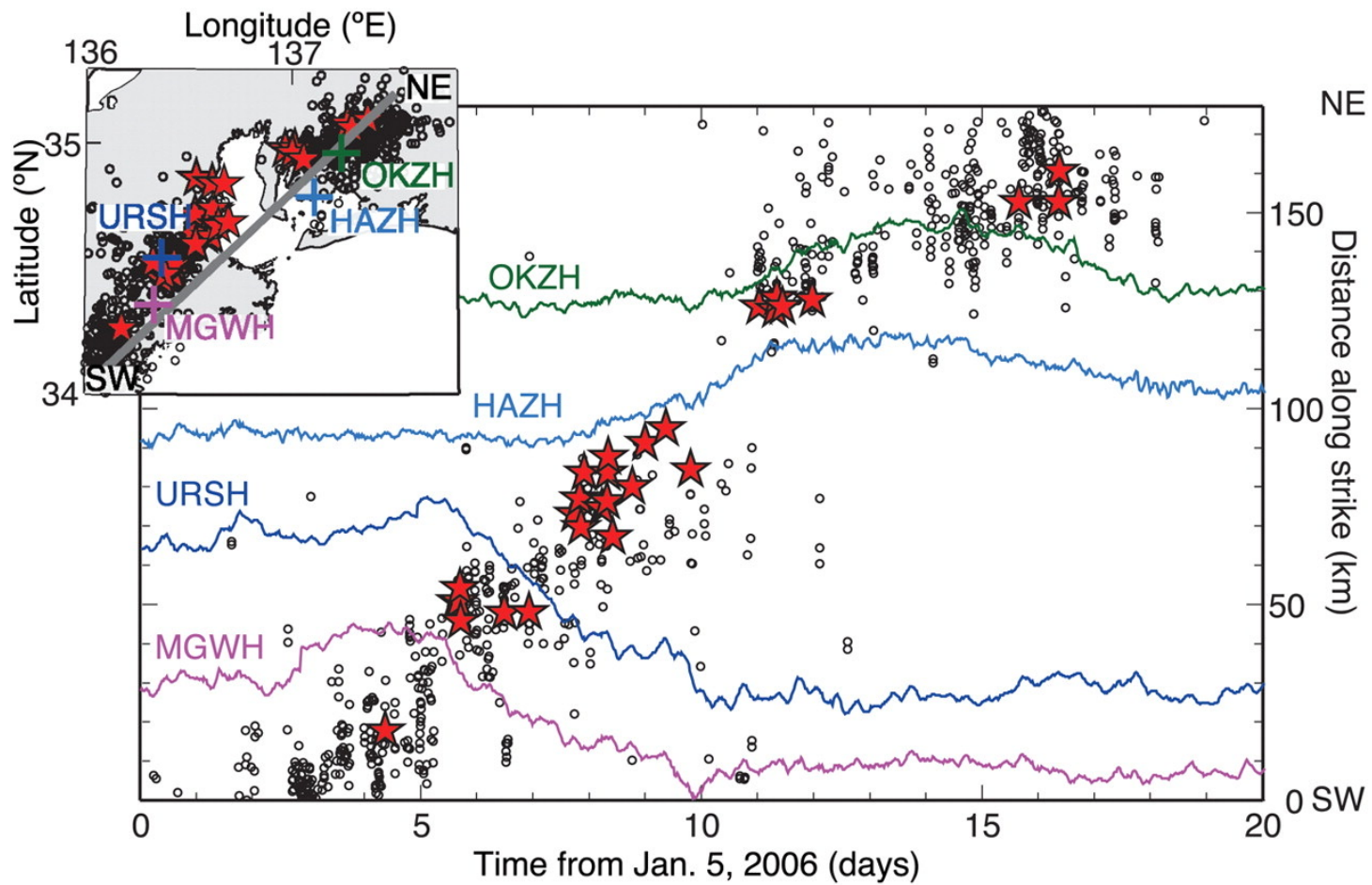
## August 2009 slow slip event



Bartlow et al., 2011  
Tremor closely tracks slip in space and time

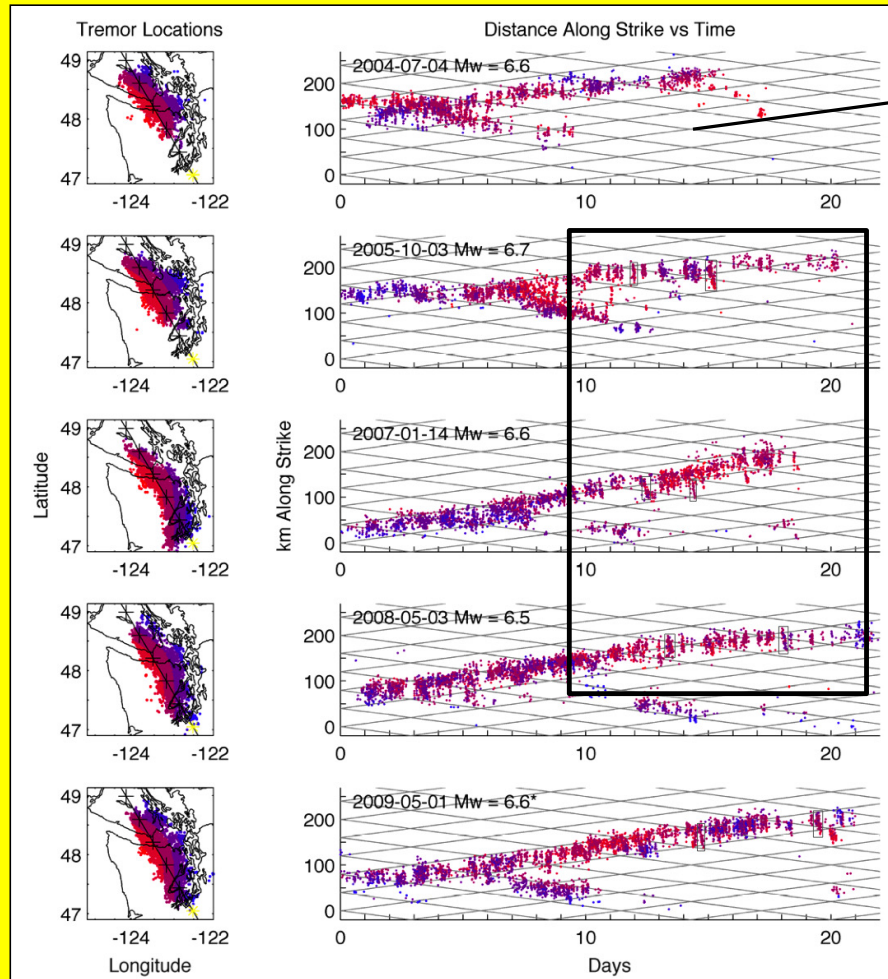


Courtesy of John Vidale



Kii Peninsula, Jan. 2006

Ito et al., 2007



7 km/day

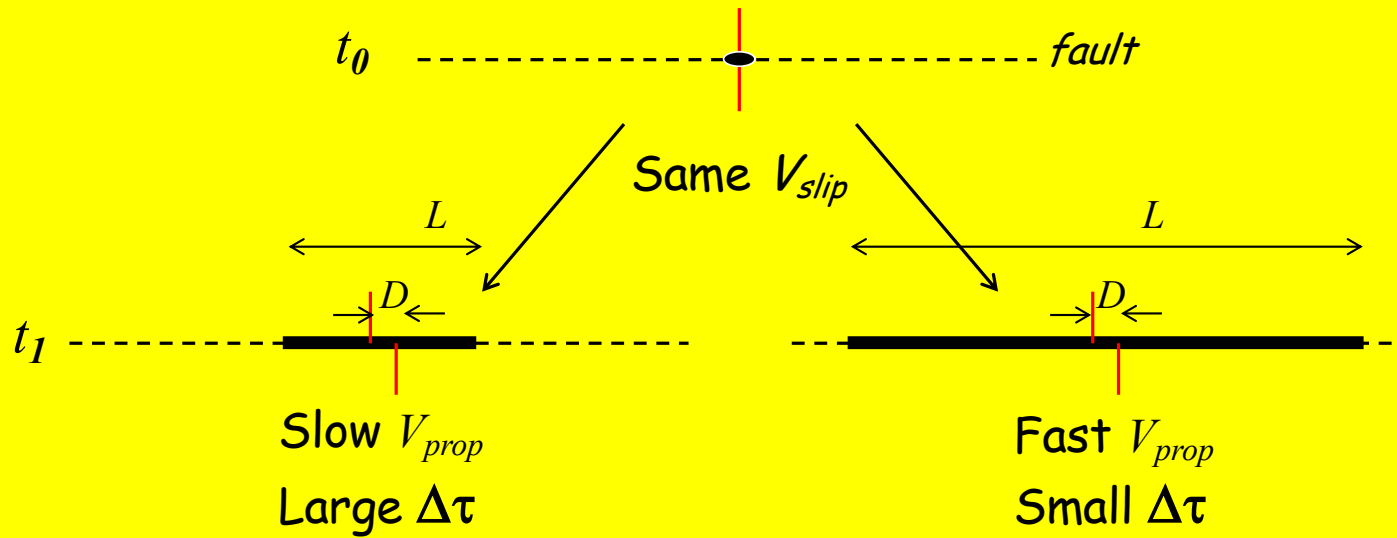
Houston et al.,  
2011

## Summary of (early) slow slip observations:

1. Stress drop is low ( $\sim 10\text{-}30$  kPa vs.  $1\text{-}10$  MPa: 2+ orders of magnitude lower than for "normal" earthquakes). From the small slip:length ratio (2 cm/50 km vs. 1 m/10 km)
2. Propagation speed is low ( $\sim 10$  km/day vs.  $\sim 3$  km/s: 4.5 orders of magnitude low).
3. Slip speed is low (2 cm/2days =  $0.1 \mu\text{m/s}$  vs. 1 m/s: 7 orders of magnitude low).
4. Triggerable by small stress perturbations (slow slip by typhoons & tides; tremor by tides & teleseismic surface waves). Seems qualitatively consistent with small stress drops and inferences of high pore fluid pressure in source region.  
[shear stress = (coeff. friction)(normal stress - pore pressure)]



## SLOW SLIP PROPAGATION SPEEDS:



Elasticity:

$$\frac{D}{L} \approx \frac{\Delta\tau}{G}$$

Kinematically,

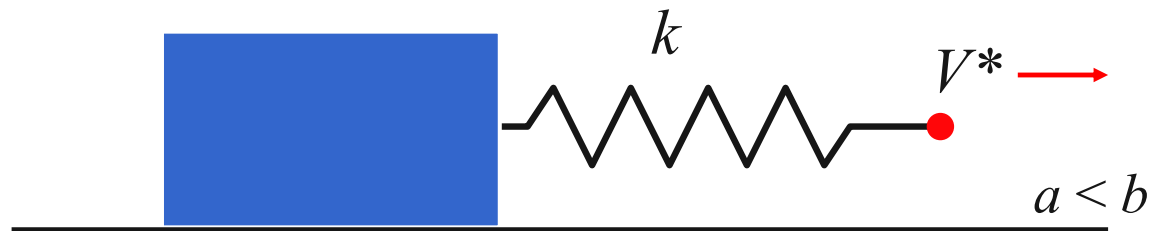
$$\frac{V_{prop}}{V_{slip}} = \frac{L}{D} \approx \frac{G}{\Delta\tau}$$

$$V_{prop} = V_{slip} \frac{G}{\Delta\tau}$$

$$V_{slip} = V_{prop} \frac{\Delta\tau}{G}$$

## Instability:

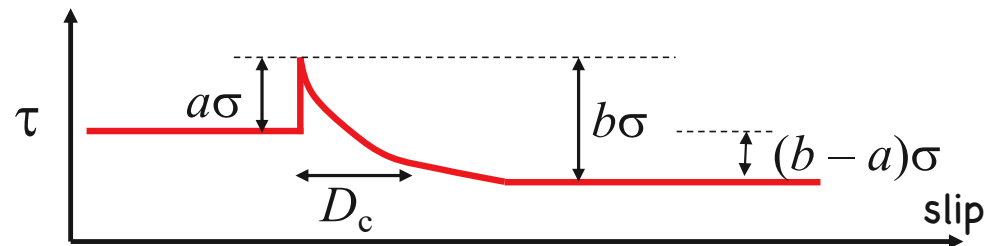
Surface must weaken faster than driving stress decreases



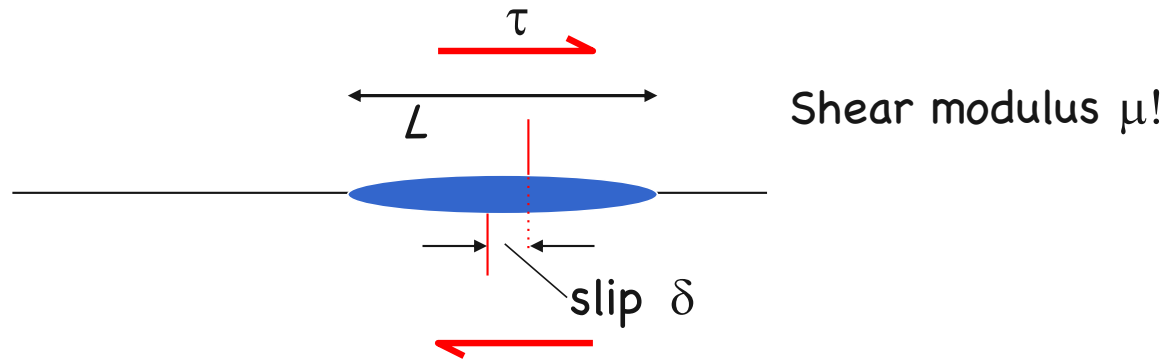
For a spring-block slider, instability requires (from a linear stability analysis in the vicinity of steady state)

$$k < k_{crit} = \frac{(b - a)\sigma}{D_c}$$

(Ruina, Rice, 1983)



What about a nucleating patch on a fault ?



At the center of  
a crack in an  
elastic solid,

$$\frac{\delta}{L} \approx \frac{\Delta\tau}{\mu}$$

$$\left( \frac{\text{slip}}{\text{length}} = \frac{\text{stress drop}}{\text{shear modulus}} \right)$$

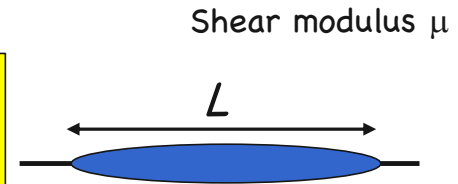
Patch stiffness  
(stress drop  
per unit slip)

$$k_{\text{patch}} \equiv \frac{\Delta\tau}{\delta} \approx \frac{\mu}{L}$$

(larger patches are less stiff; easier  
for them to accelerate because stress  
decays only slowly with slip.)

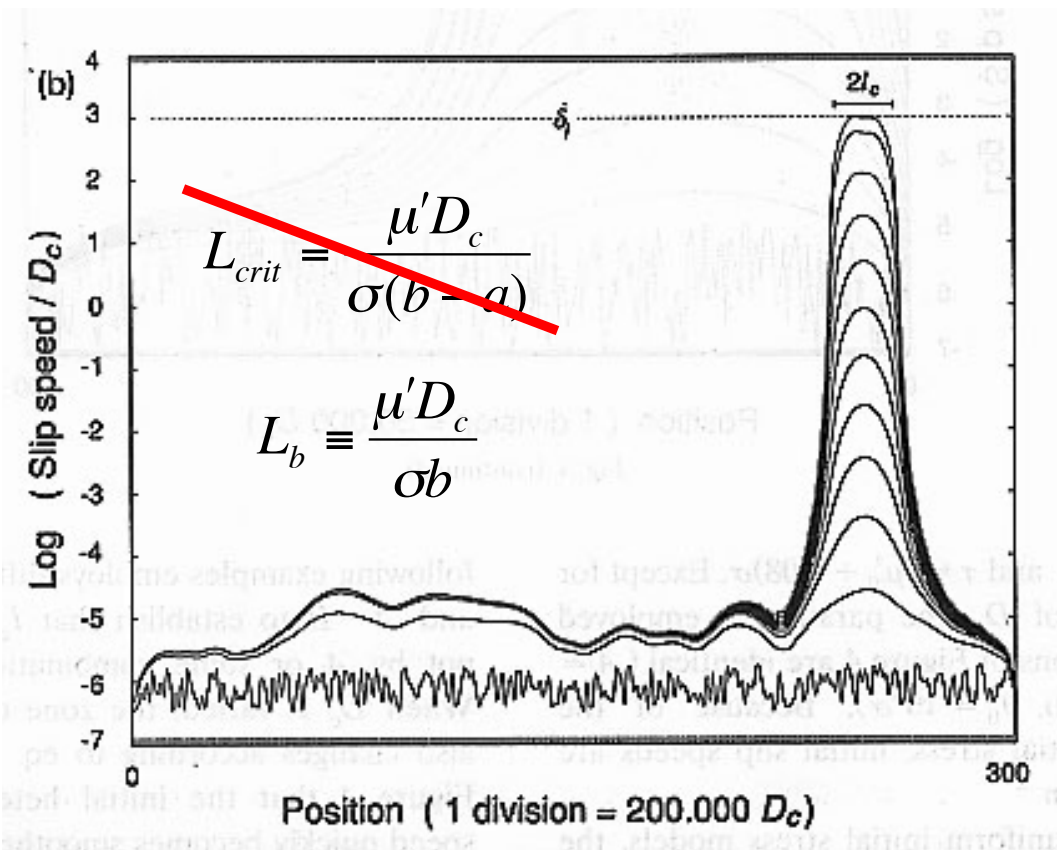
For instability,

$$k_{crack} = \frac{\mu}{L} < k_{crit} = \frac{\sigma(b-a)}{D_c}$$

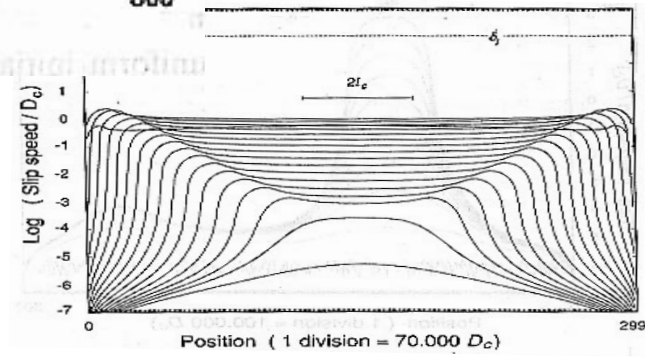


$$L > L_{crit} = \frac{\mu D_c}{\sigma(b-a)}$$

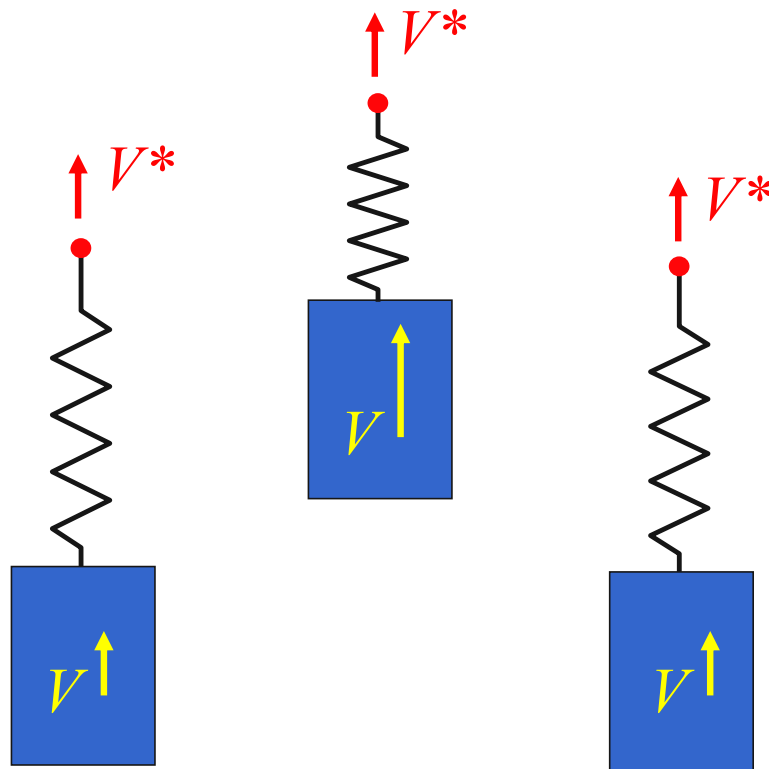
Or so it was thought...



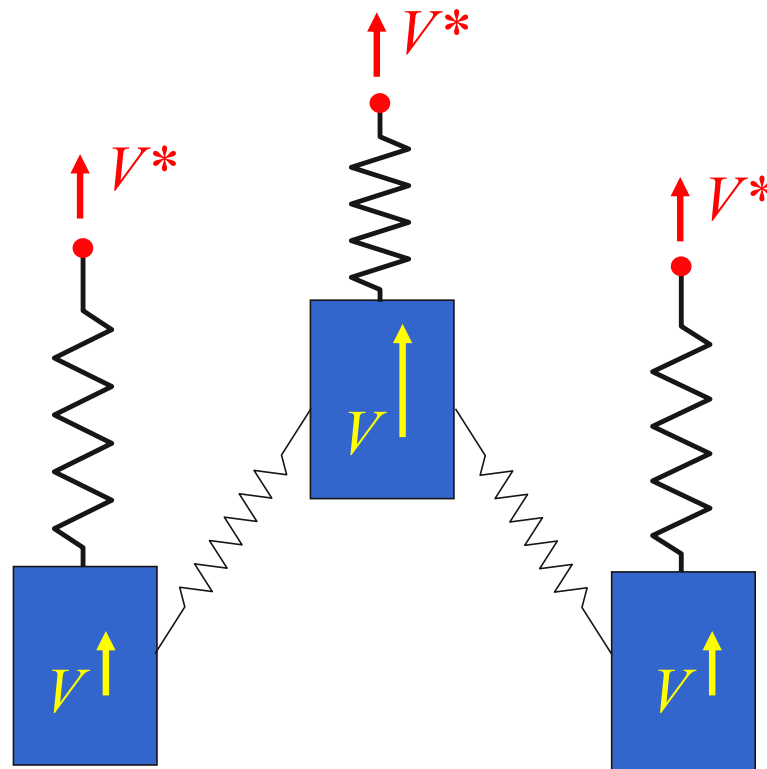
Dieterich, 1992



Instability: Surface must weaken faster than driving stress decreases



Instability: Surface must weaken faster than driving stress decreases



## Three length scales:

$$L_b = \frac{\mu' D_c}{b \sigma} \quad (\text{Dieterich 1992. Generic value of 1 m for } \sigma = 100 \text{ MPa})$$

Appropriate well above steady state (**Aging law**)

$$L_{b-a} = \frac{\mu' D_c}{\sigma(b-a)} = \frac{b}{(b-a)} L_b \quad (\text{Ruina 1983; Rice 1993})$$

In the vicinity of steady state

$$L_\infty = \frac{2}{\pi} \frac{b}{b-a} L_{crit} = \frac{2}{\pi} \left( \frac{b}{b-a} \right)^2 L_b \quad (\text{Rubin \& Ampuero 2005})$$

(full length)  
(**Aging law**)

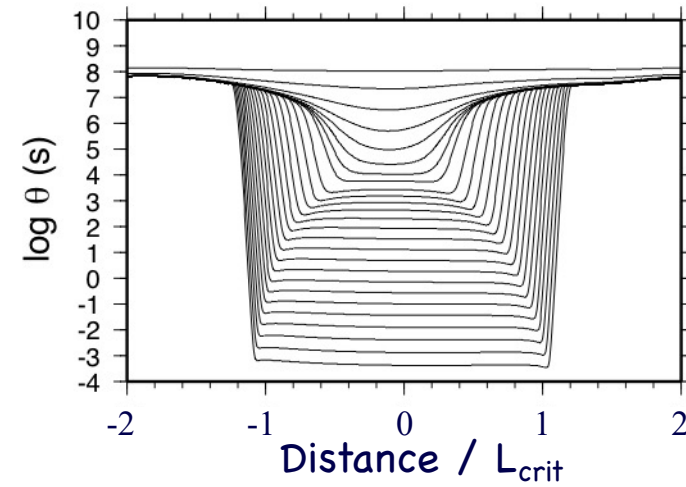
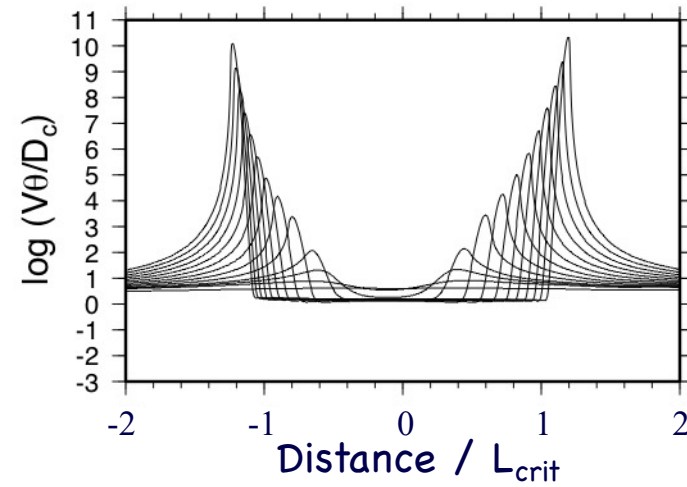
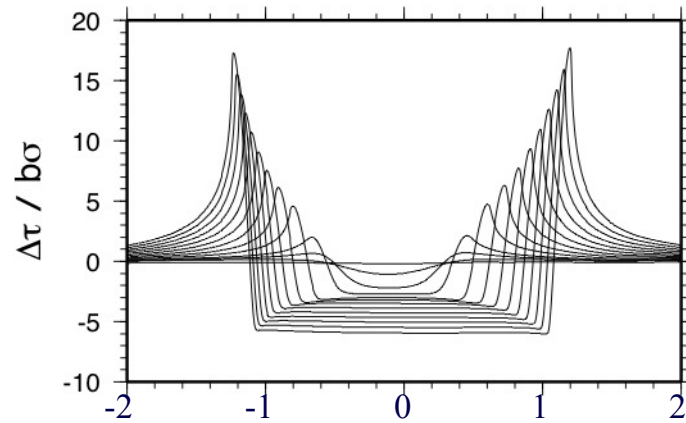
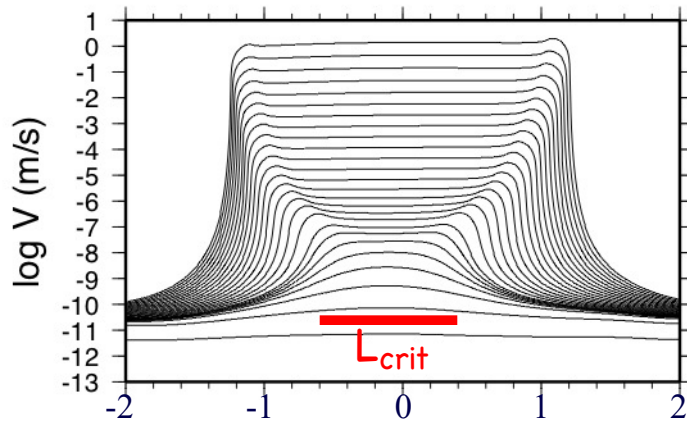


Why all these length scales, if a spring-slider has only a single critical stiffness?

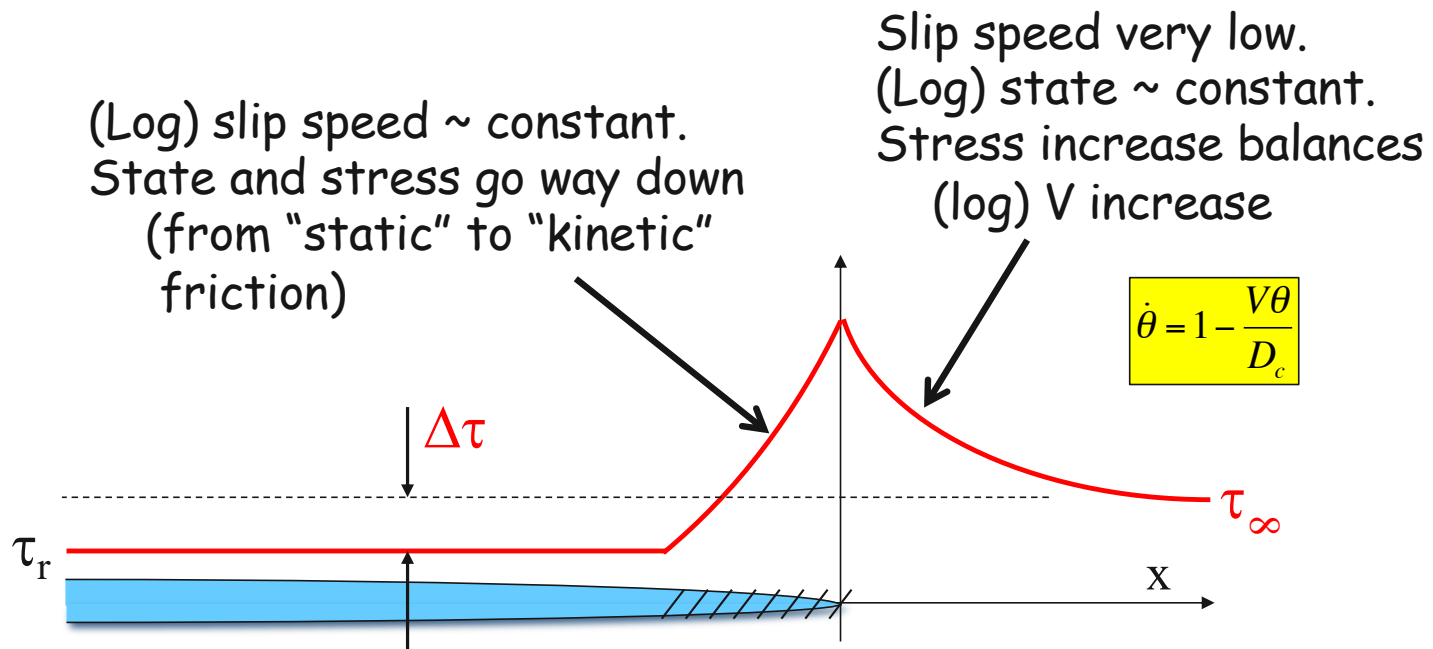
An important difference between  
spring-sliders and faults:

Unlike a spring, a fault patch does not have a single stiffness. Its stiffness varies in space (it has a larger stress drop for a given slip distance near the patch ends than in the center), and its stiffness varies in time as the patch expands or shrinks. The portion of the fault accelerating to instability gets to choose its own stiffness.

## Aging law, $a/b=0.8$

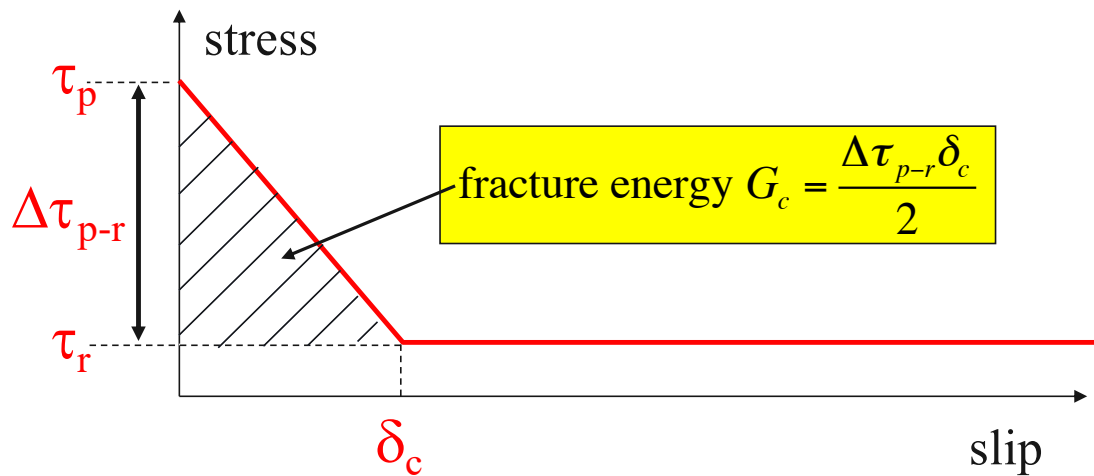
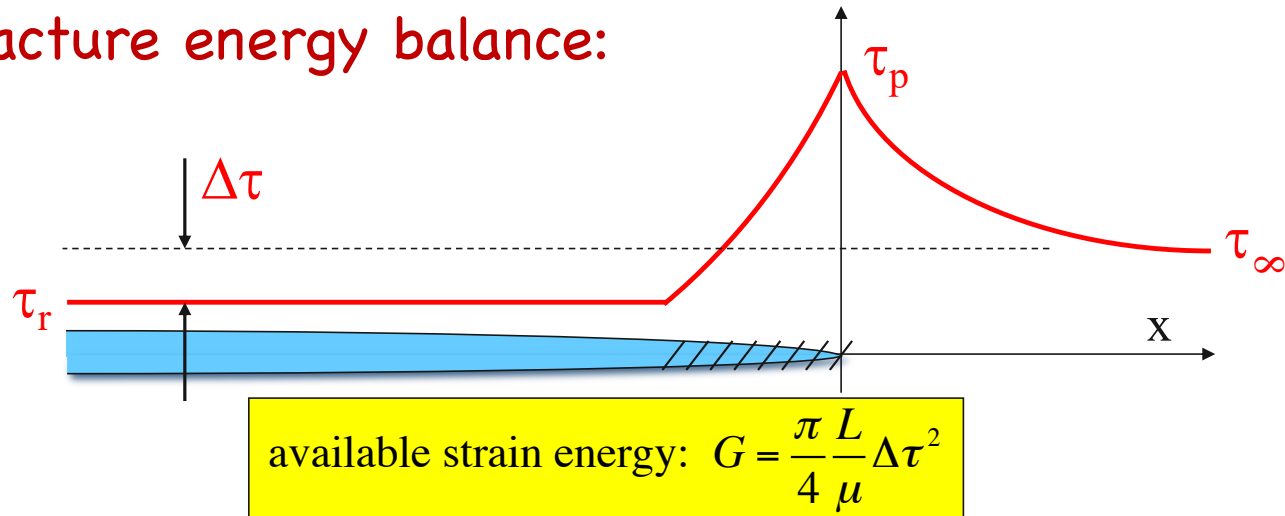


## Rate-State model:



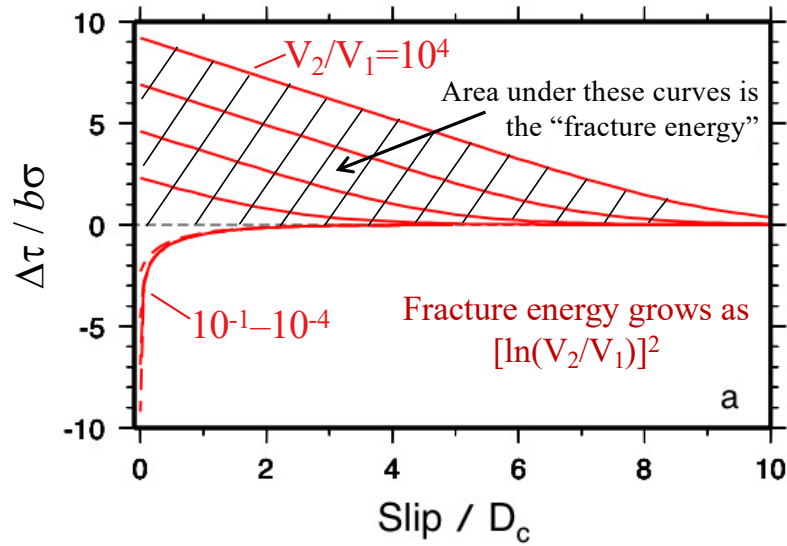
$$\tau = \tau^* + a\sigma \ln \frac{V}{V^*} + b\sigma \ln \frac{\theta}{\theta^*}$$

## Fracture energy balance:



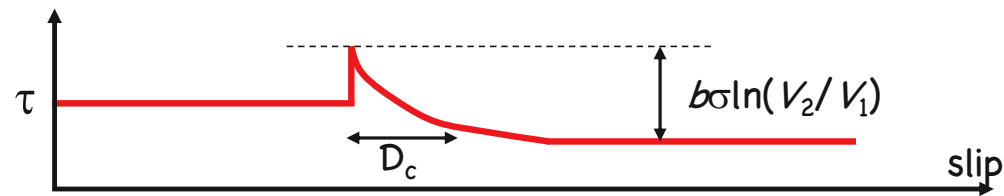
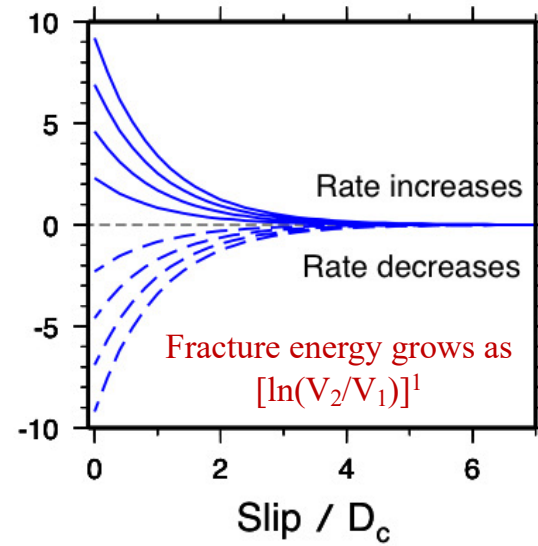
## Aging law evolution

$$\dot{\theta} = 1 - \frac{V\theta}{D_c}$$

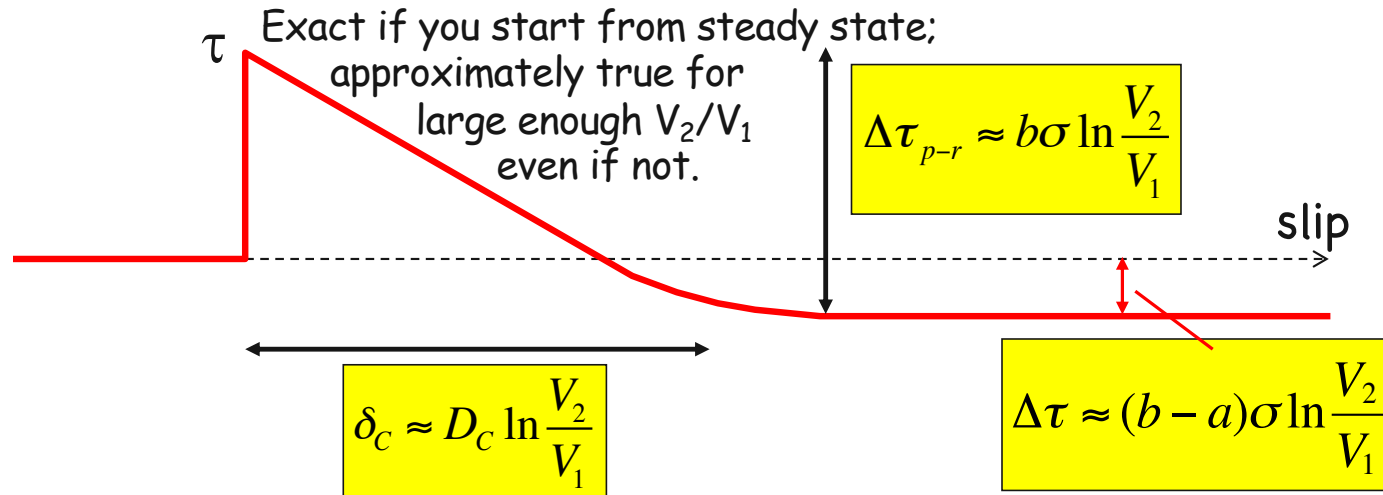


## Slip law evolution

$$\dot{\theta} = -\frac{V\theta}{D_c} \ln \frac{V\theta}{D_c}$$



Aging law:



Fracture energy:

$$G_c \approx \frac{\Delta\tau_{p-r} \delta_c}{2} = \frac{D_c b \sigma}{2} \ln^2 \frac{V_2}{V_1}$$

Strain energy release rate:

$$G \approx \frac{\pi L}{4 \mu} \Delta\tau^2 = \frac{\pi L}{4 \mu} (b-a)^2 \sigma^2 \ln^2 \frac{V_2}{V_1}$$

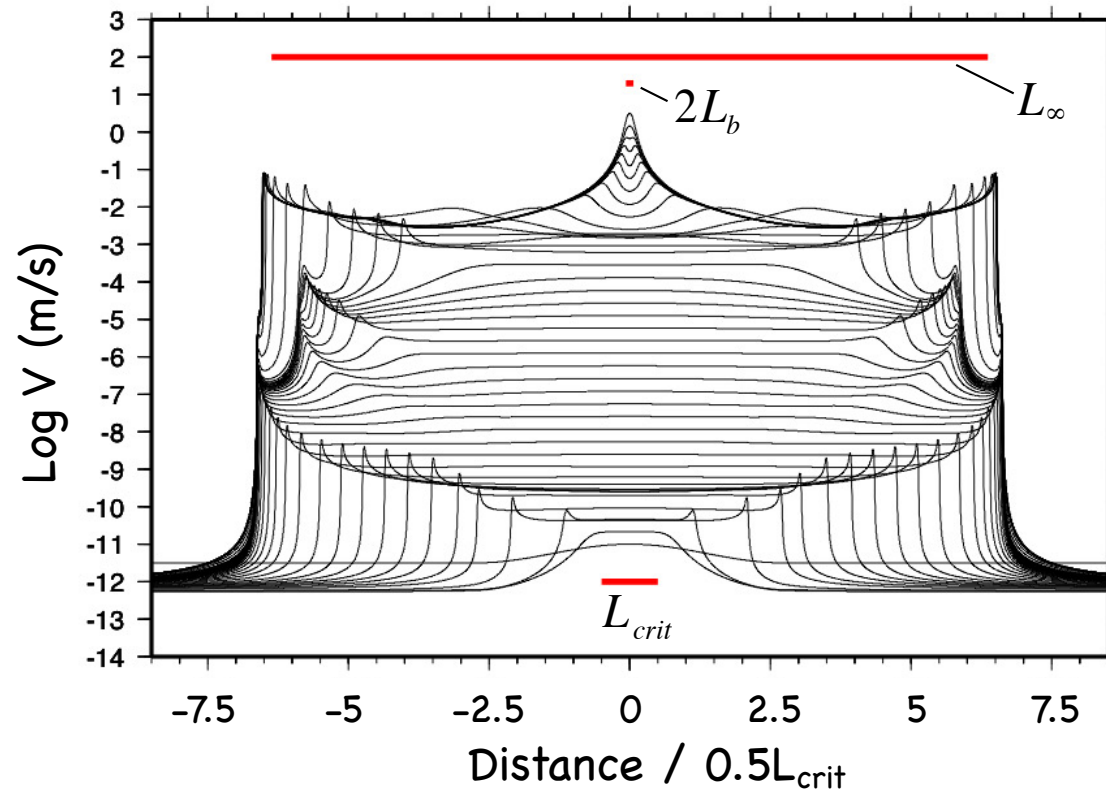
$G = G_c :$

}

$$L_\infty = \frac{2}{\pi} \left( \frac{b}{b-a} \right) L_{crit}$$

(in the limit of large slip speeds)

Aging law,  $a/b=0.95$

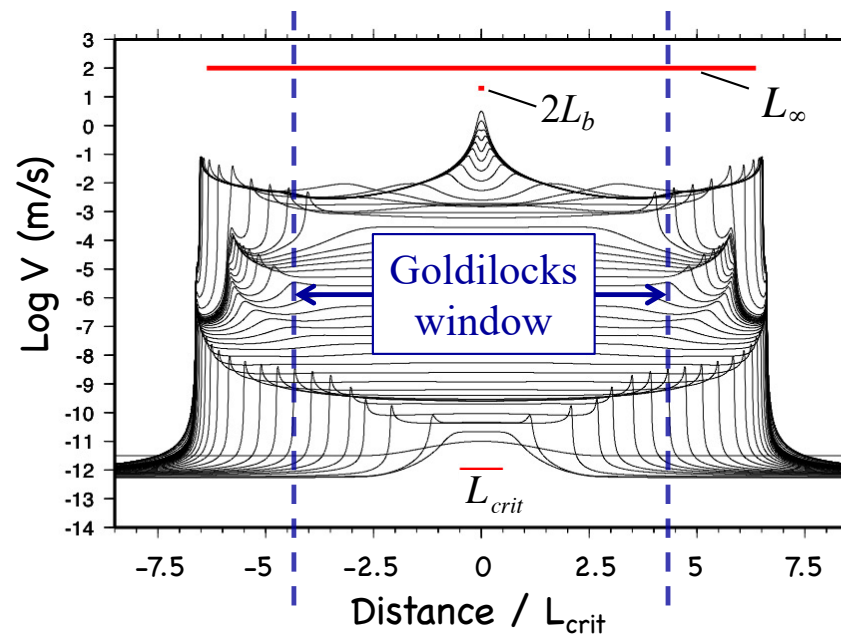


## Slow Slip Explanation #1: The “Goldilocks hypothesis”

(a fault that is neither too large nor too small but just right...)

[Yoshida and Kato, 2003; Kuroki et al. 2004;

Liu and Rice, 2005, 2007, 2009; Rubin, 2008]





## Liu and Rice, 2007

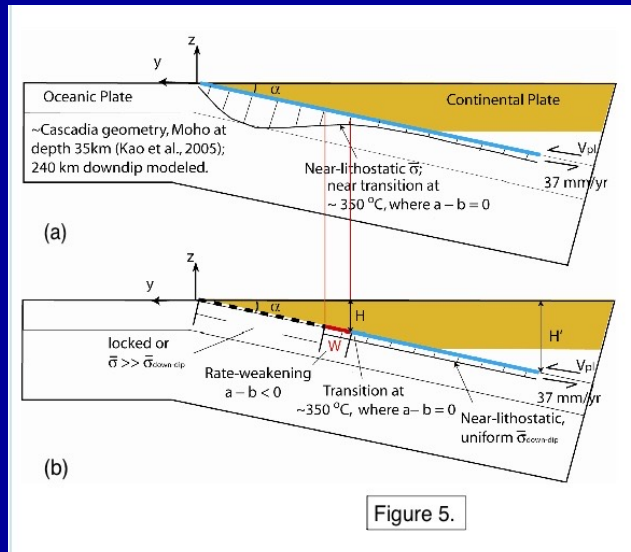
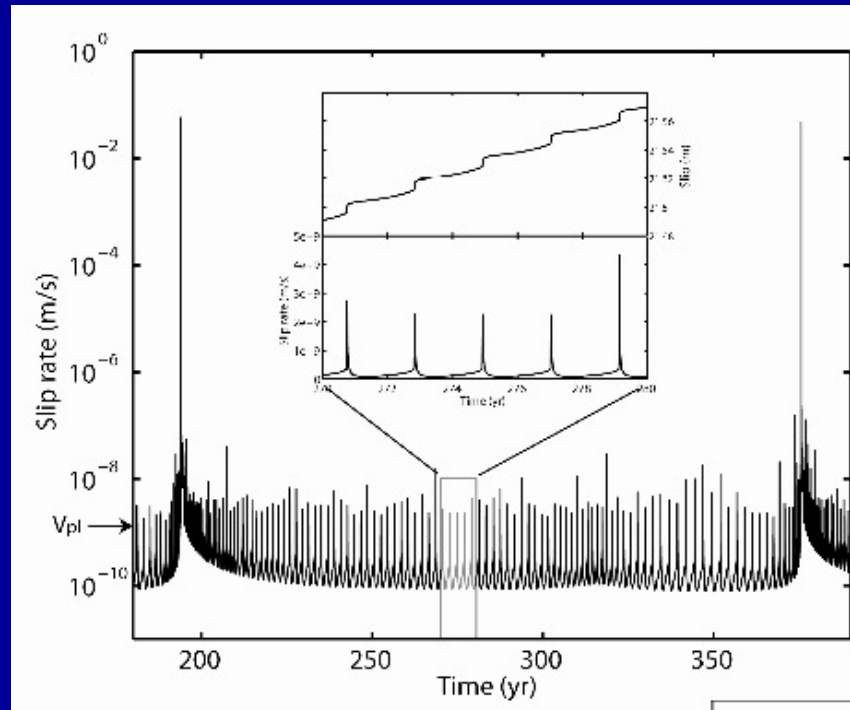


Figure 5.



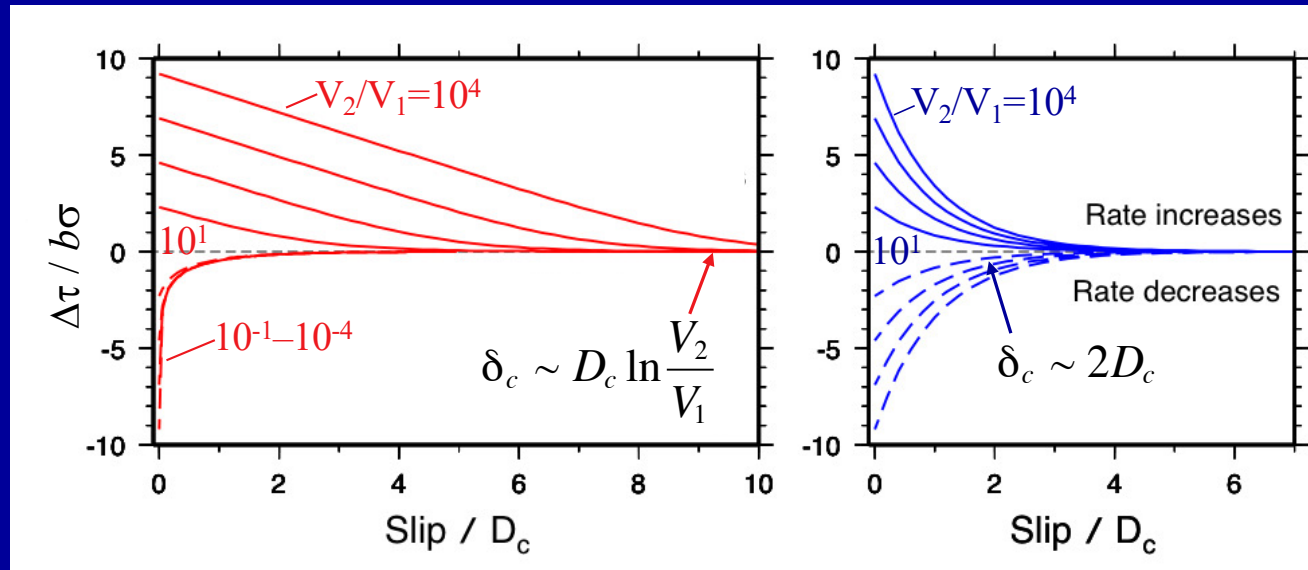
$$L_b = \frac{\mu' D_c}{b \sigma}$$

(30 GPa, 10  $\mu\text{m}$ , 0.01, 30 MPa  $\Rightarrow$  1 m)

(30 GPa, 100  $\mu\text{m}$ , 0.01, 3 MPa  $\Rightarrow$  100 m  $\Rightarrow 2L_{\text{inf}} = 25$  km,  $a/b=0.95$ )

What about the slip law?

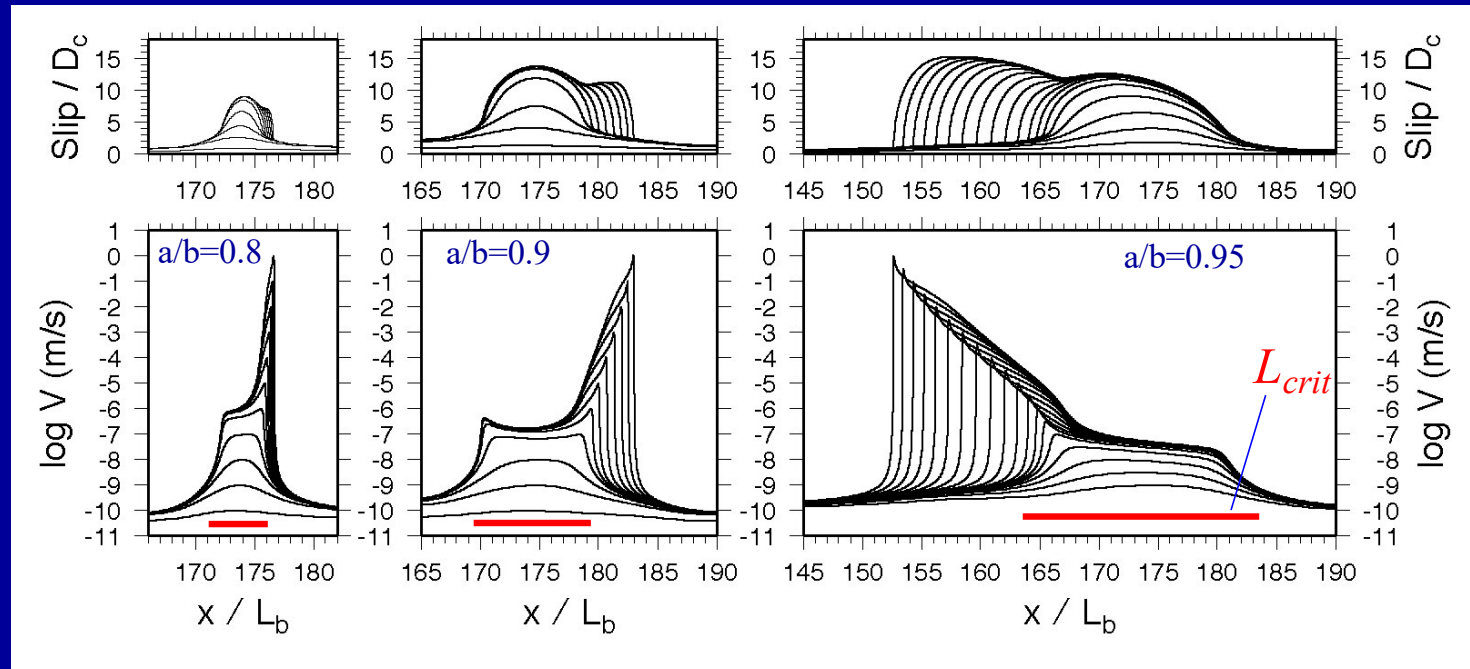
## Aging law



Fracture energy:  $G_c \sim \left( \ln \frac{V_2}{V_1} \right)^2$

$G_c \sim \left( \ln \frac{V_2}{V_1} \right)^1$

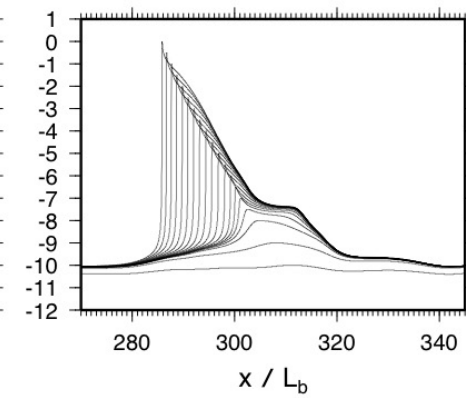
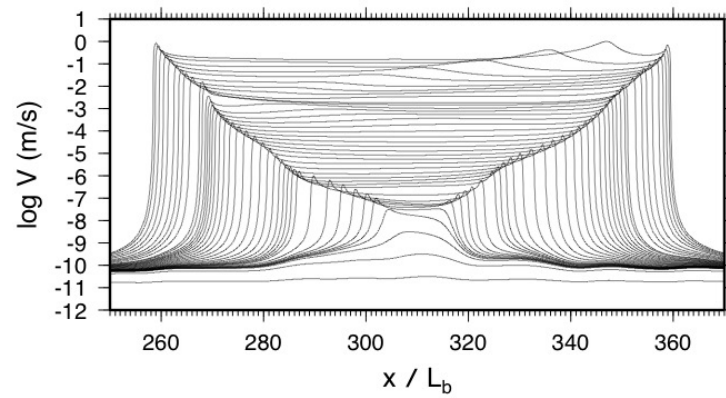
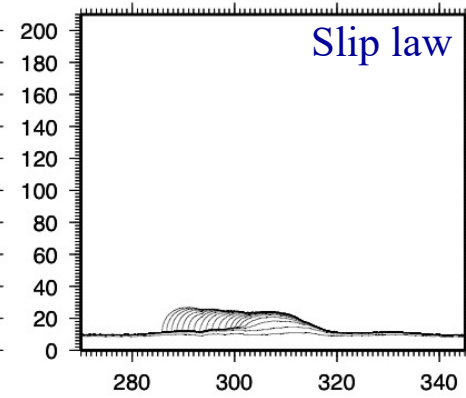
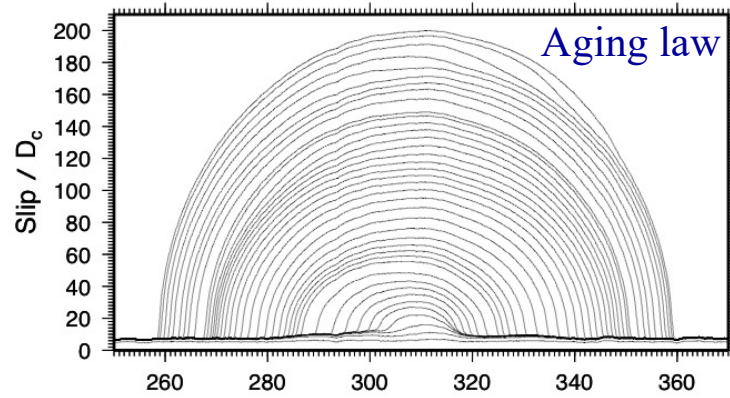
## Slip law, $V\theta/D_c \sim 1$

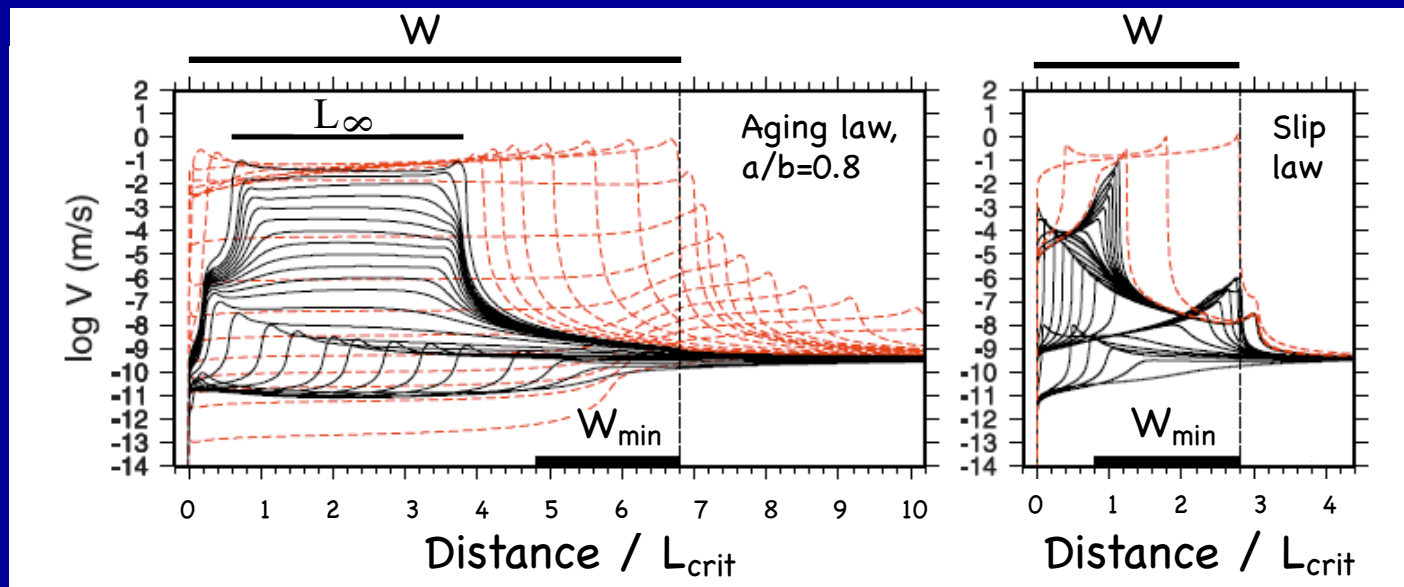
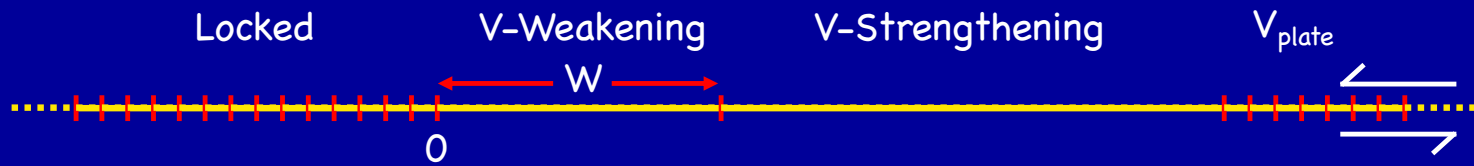


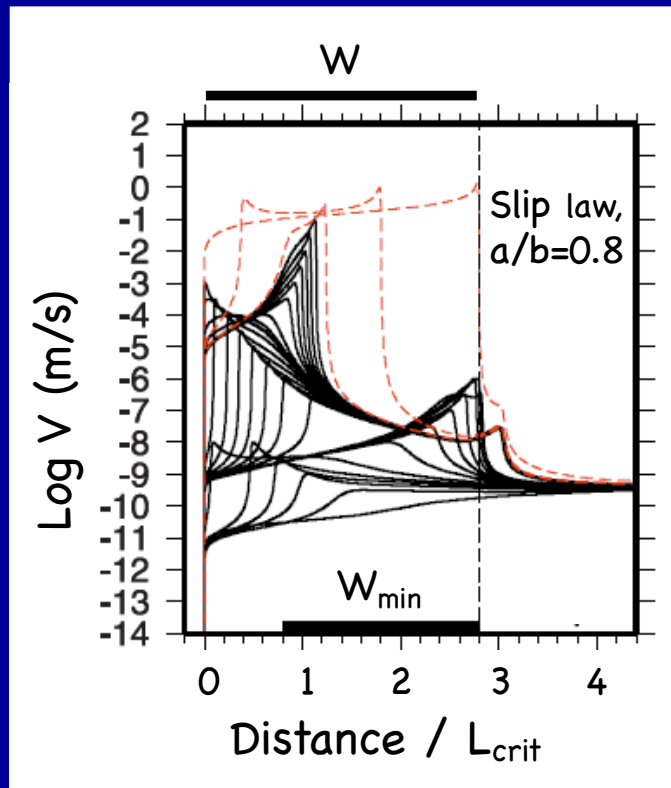
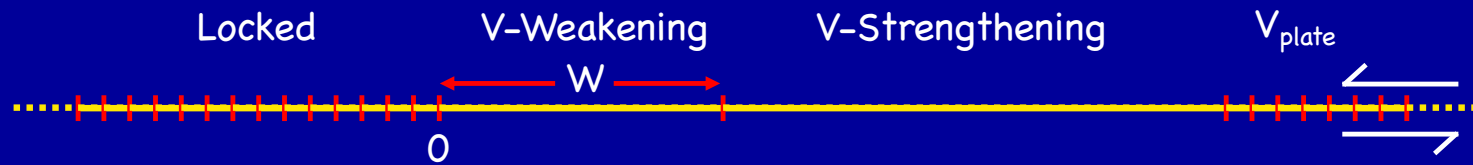
$$G^{crack} \propto L \left( \ln \frac{V_2}{V_1} \right)^2, \quad \text{but} \quad G_c^{SLIP} \propto \left( \ln \frac{V_2}{V_1} \right)^1$$

Crack-like growth not possible!

$$a/b = 0.95$$

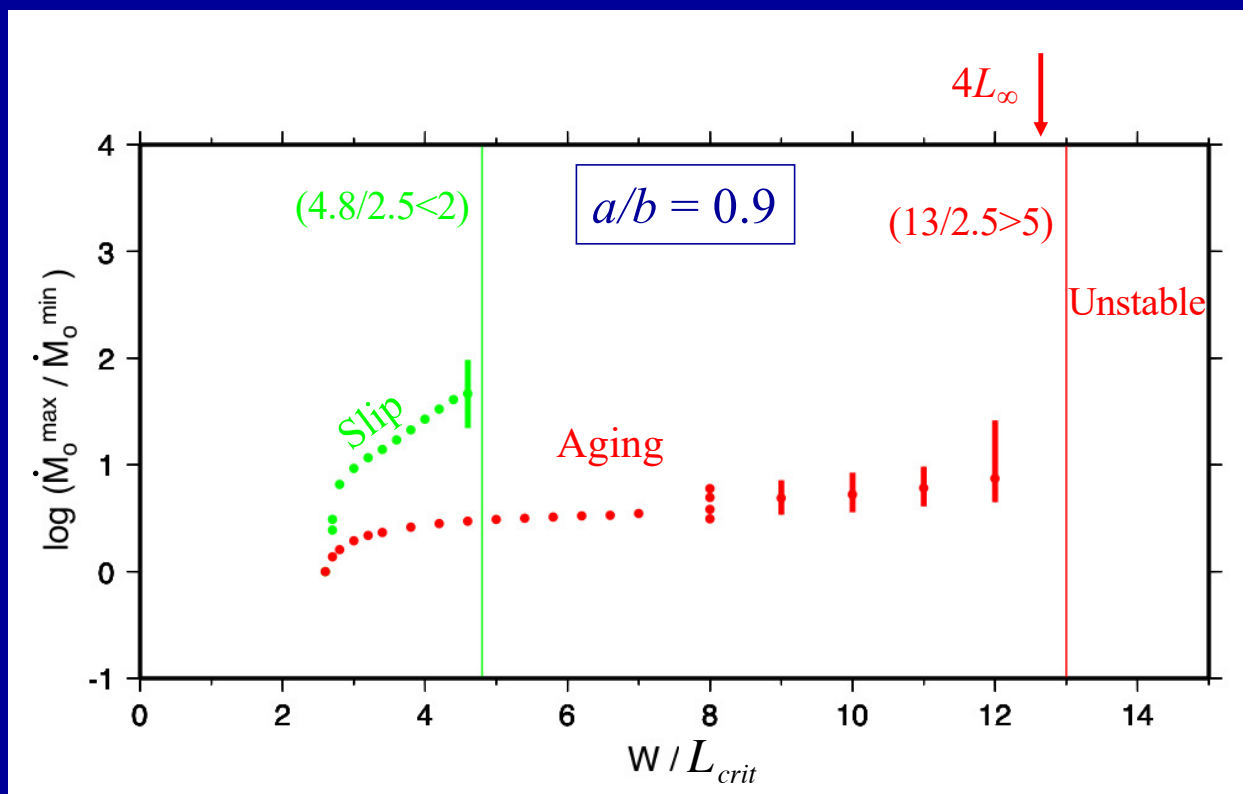
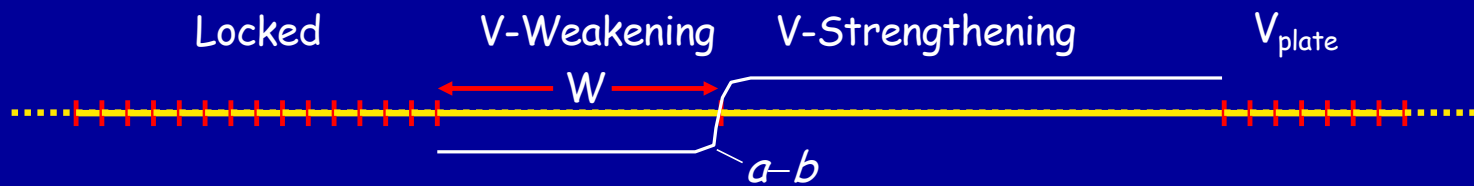






For the Slip law, fracture energy increases much less rapidly with slip speed.

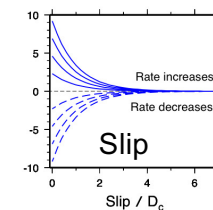
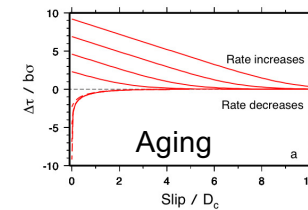
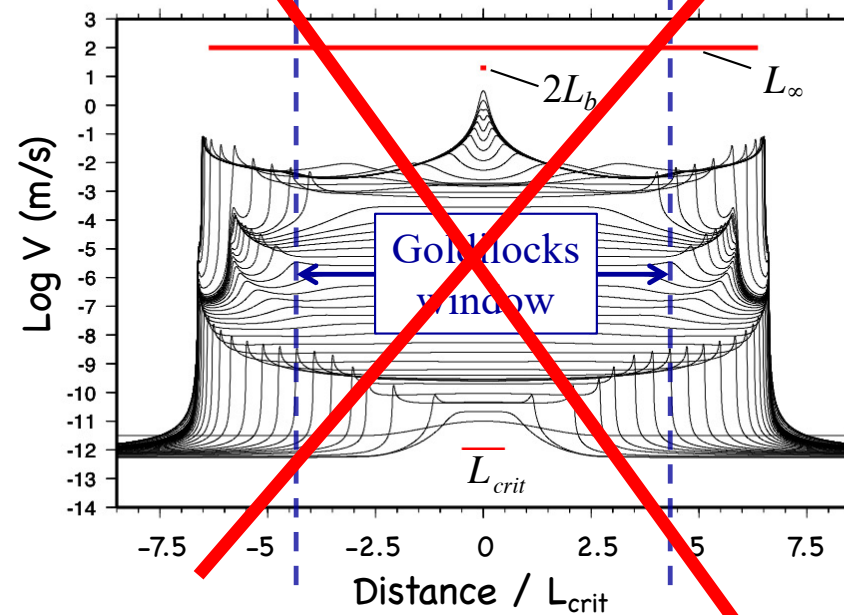
Much less expansion is required to reach elastodynamic speeds





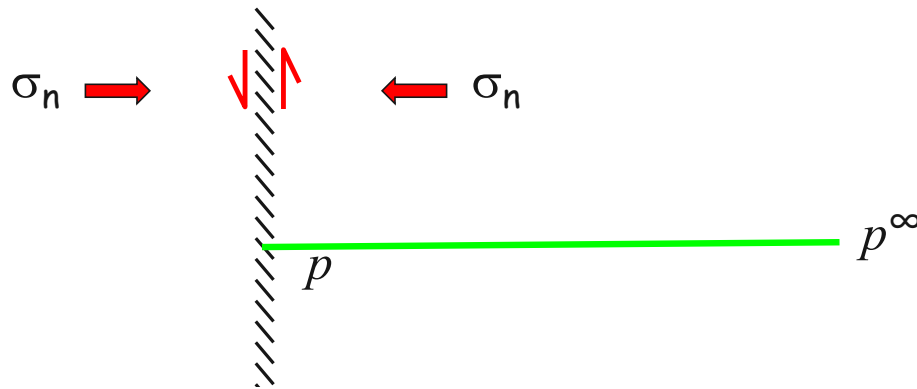
## Slow Slip Explanation #1: The “Goldilocks hypothesis”

If you use the (Slip) state evolution law that properly captures the laboratory response to rapid velocity increases, the range of fault lengths hosting episodic slow slip is too narrow to credibly explain why it is common to so many subduction zones.



## Slow Slip Explanation #2:

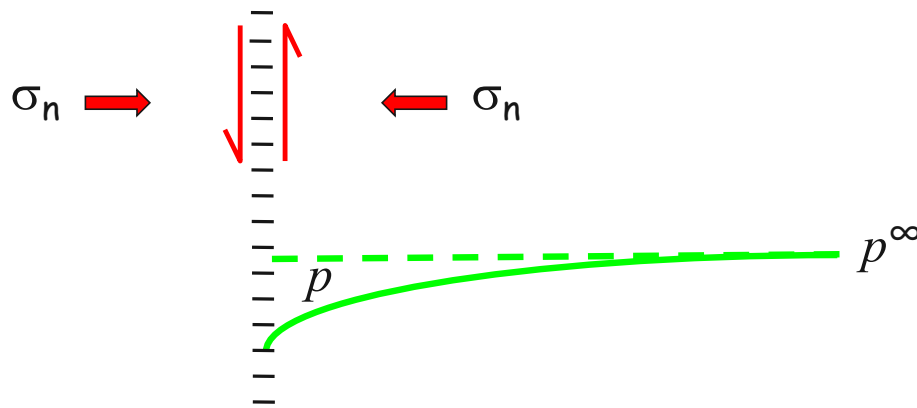
Stabilization due to pore dilatancy/pore pressure reduction during accelerating slip. Expected to dominate over standard rate-and-state strength changes at low effective normal stress [Suzuki and Yamashita (2009); Liu and Rubin (2010); Segall et al., 2010; Yamashita, 2013].



$$\text{Shear strength} = \text{friction} * (\sigma_n - p)$$

## Slow Slip Explanation #2:

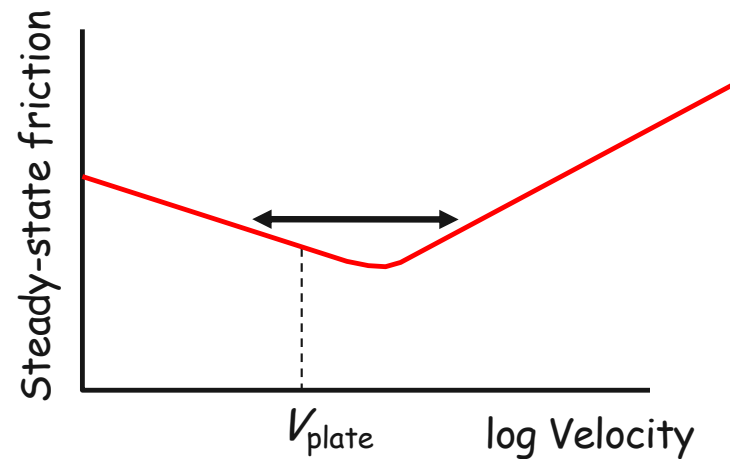
Stabilization due to pore dilatancy/pore pressure reduction during accelerating slip. Expected to dominate over standard rate-and-state strength changes at low effective normal stress [Suzuki and Yamashita (2009); Liu and Rubin (2010); Segall et al., 2010; Yamashita, 2013].



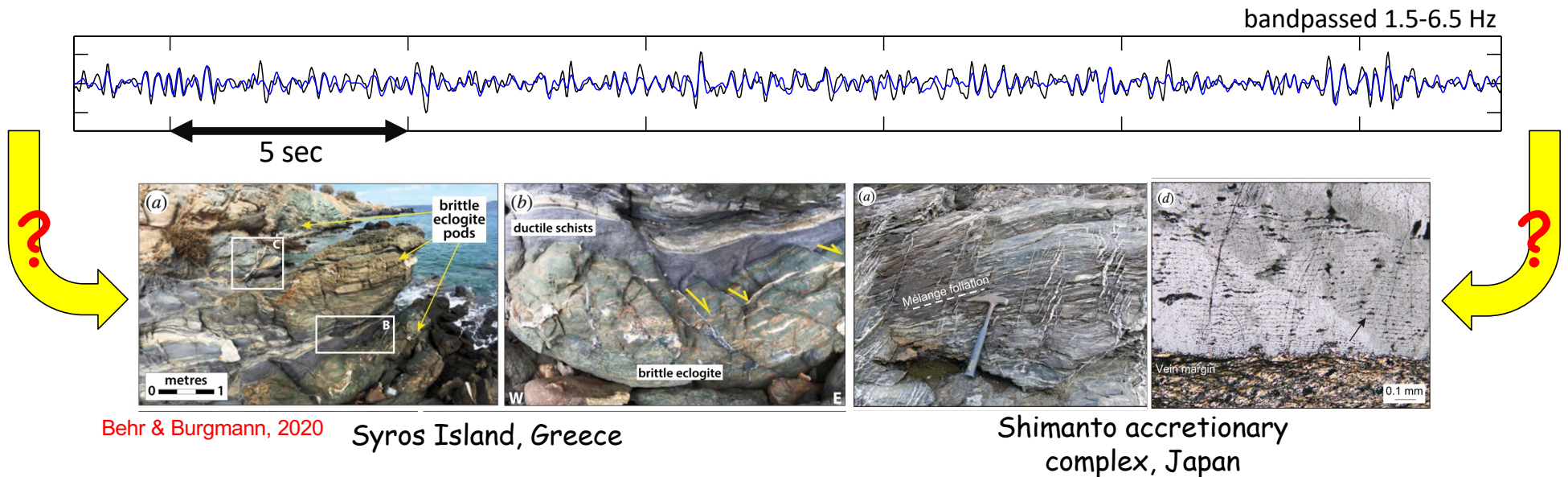
$$\text{Shear strength} = \text{friction} * (\sigma_n - p)$$

### Slow Slip Explanation #3:

A transition from steady-state velocity-weakening to velocity-strengthening behavior in the appropriate range of slip speeds  
[e.g. Kato, 2003; Shibazaki and Iio, 2003; Shibazaki and Shimamoto, 2007; Hawthorne and Rubin, 2013].



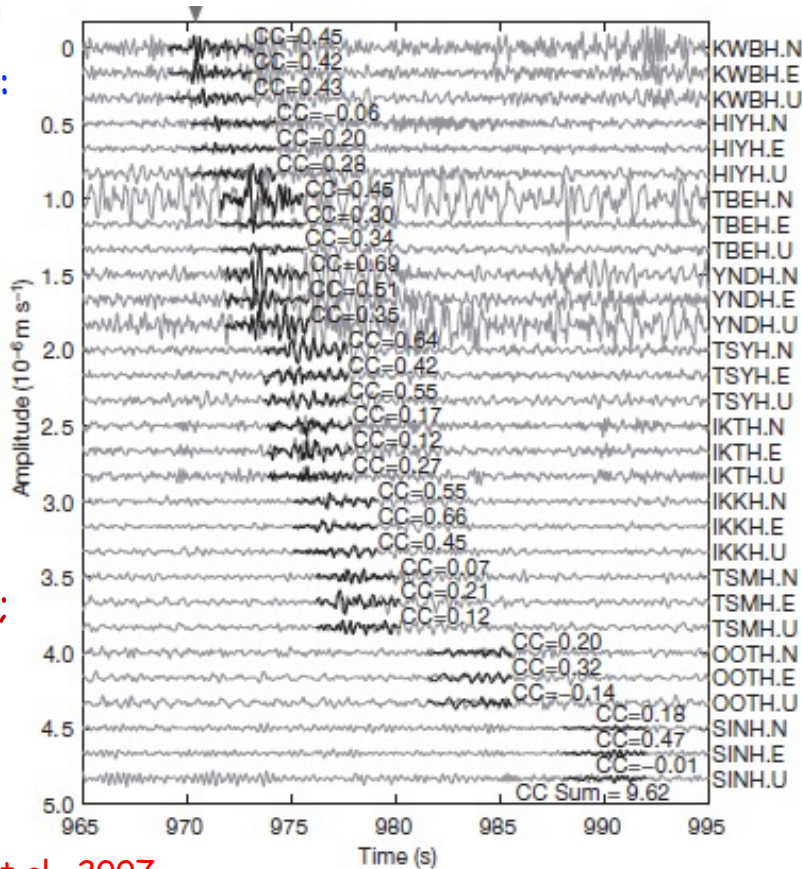
# Toward a physical interpretation of Low Frequency Earthquakes (LFEs)



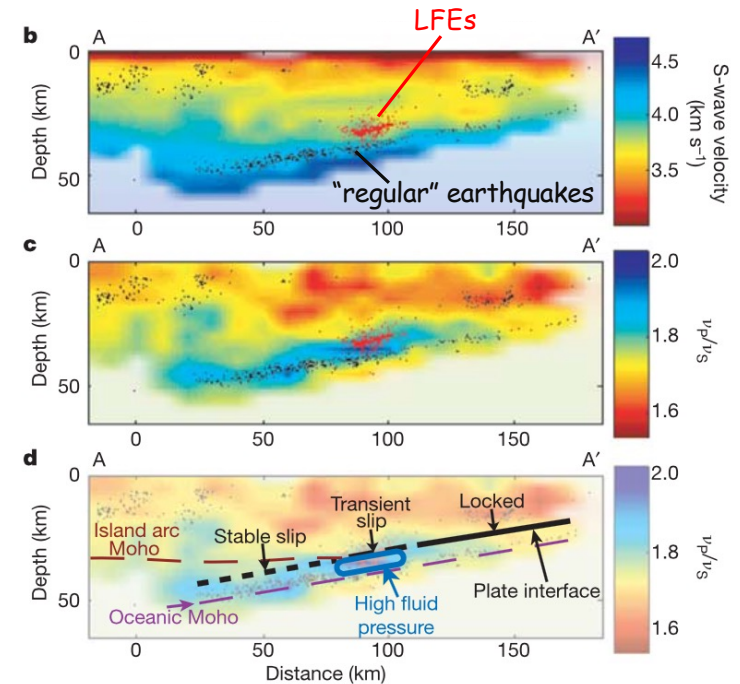
One Low Frequency Earthquake (LFE) cross-correlated with continuous tremor seismograms in Japan: Tremor is comprised of myriad LFEs.

Gives you "families" of LFEs: Anything with waveforms and moveouts similar enough to your template event.

(10 stations; 3 channels)



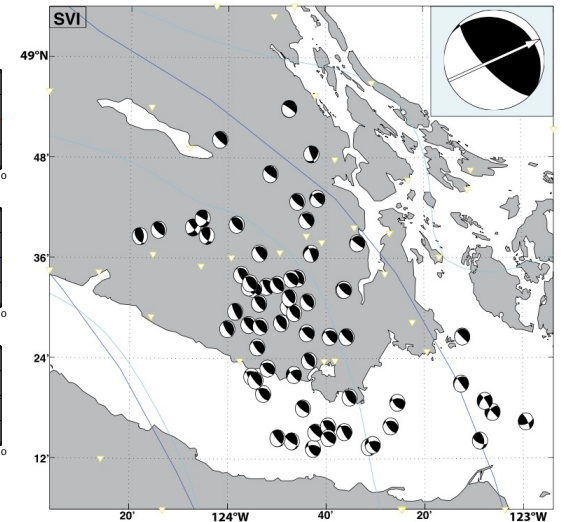
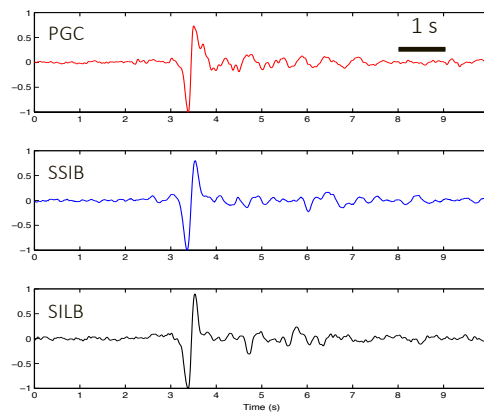
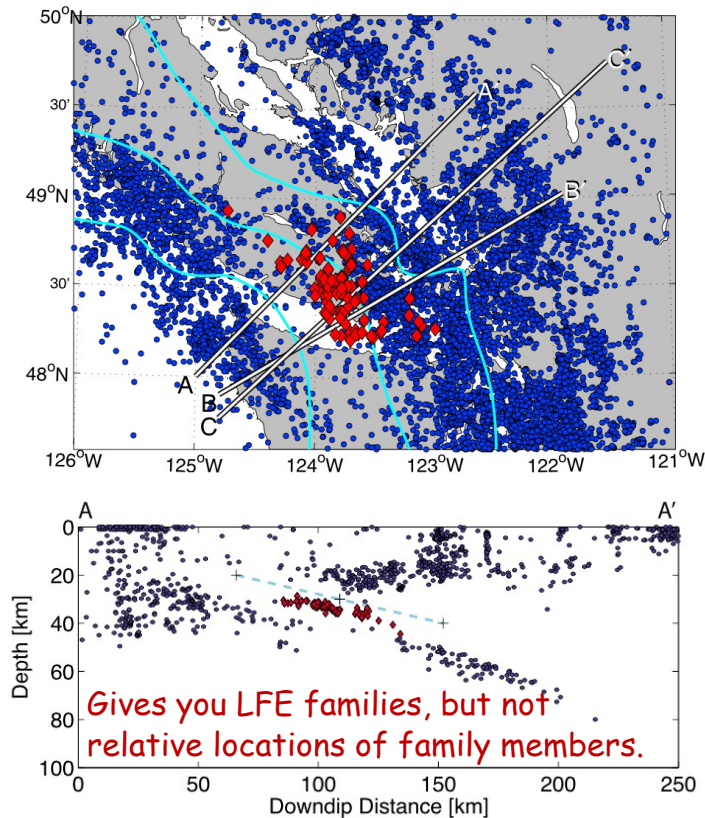
Shelly et al., 2007



Shelly et al., 2006

Bostock et al. 2012: LFE families in Cascadia from cross-correlating each time window with all other time windows (following Brown and Beroza).

**“CROSS-TIME” DETECTIONS**



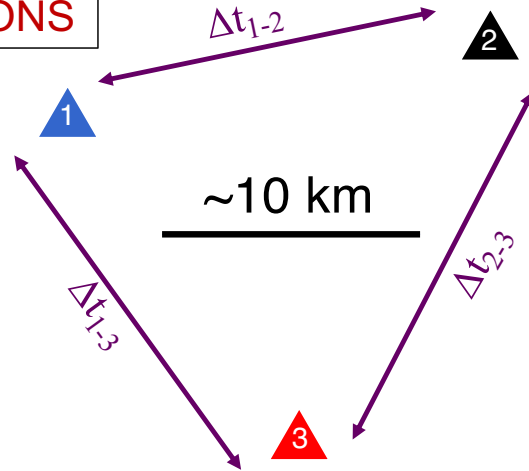
Stacking of LFEs w/in families gives good focal mechanisms - Royer & Bostock 2014 (also Ide et al. 2007 for Japan):  
 LFEs represent slip on the plate interface, in the direction of relative plate motion.

# “CROSS-STATION” DETECTIONS

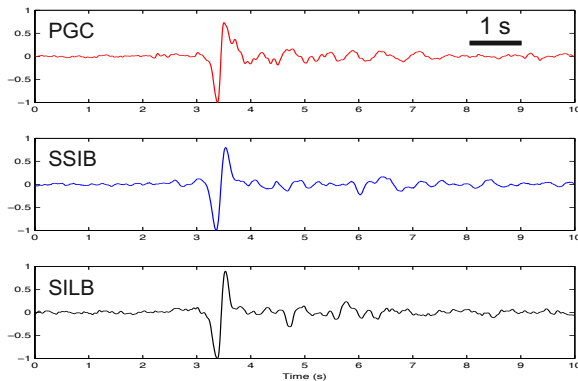
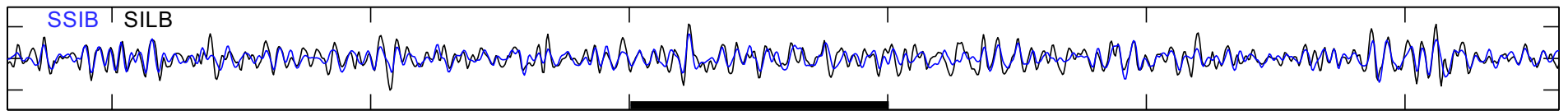


source

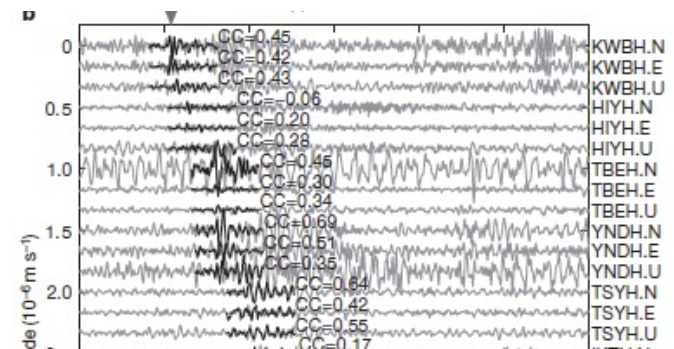
Armbruster et al., 2014



1. Rotate the horizontal components at 3 stations into the particle motion direction.
2. Cross-correlate the 3 station-station pairs.
3. Average CC value > threshold and “loop of time offsets” < threshold gives a detection.
4. Two independent time offsets give a map location, assuming the source to lie on the plate interface.



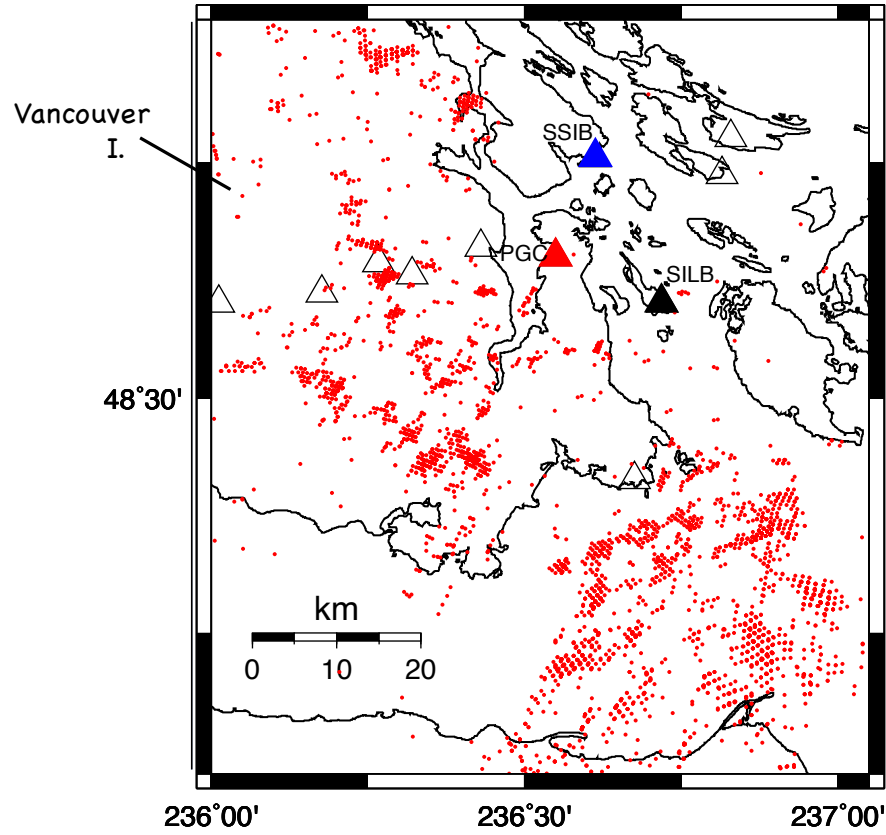
stacks of ~2000 LFEs in Bostock’s Family #002





# Slow slip episodes:

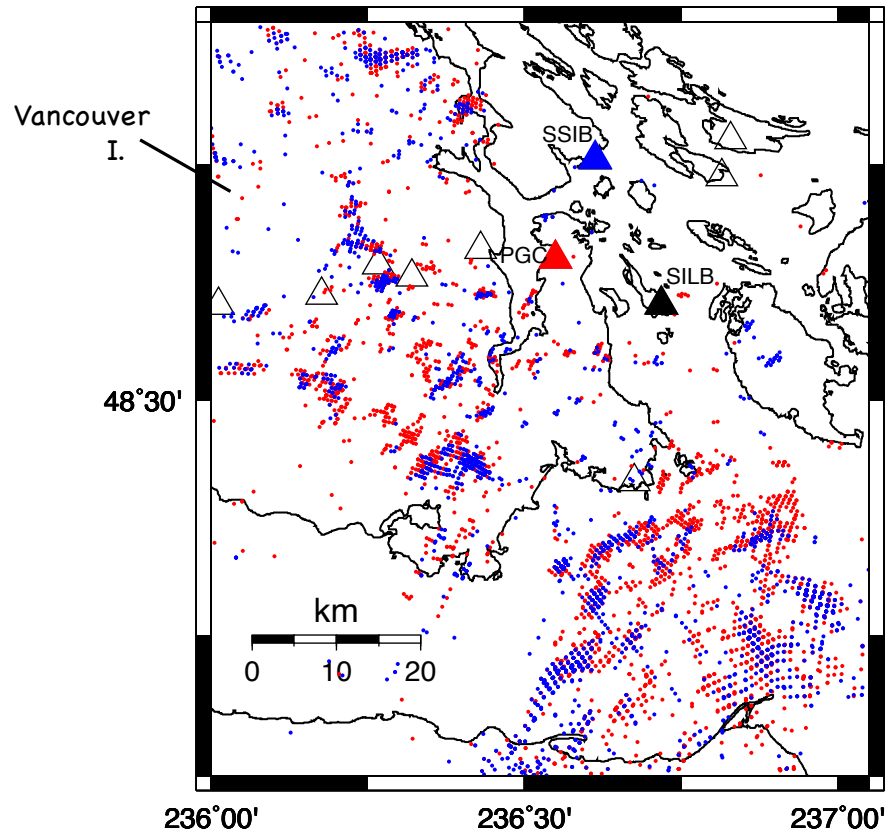
Sept 2005



Arnbruster et al., 2014 (150 s windows)

## Slow slip episodes:

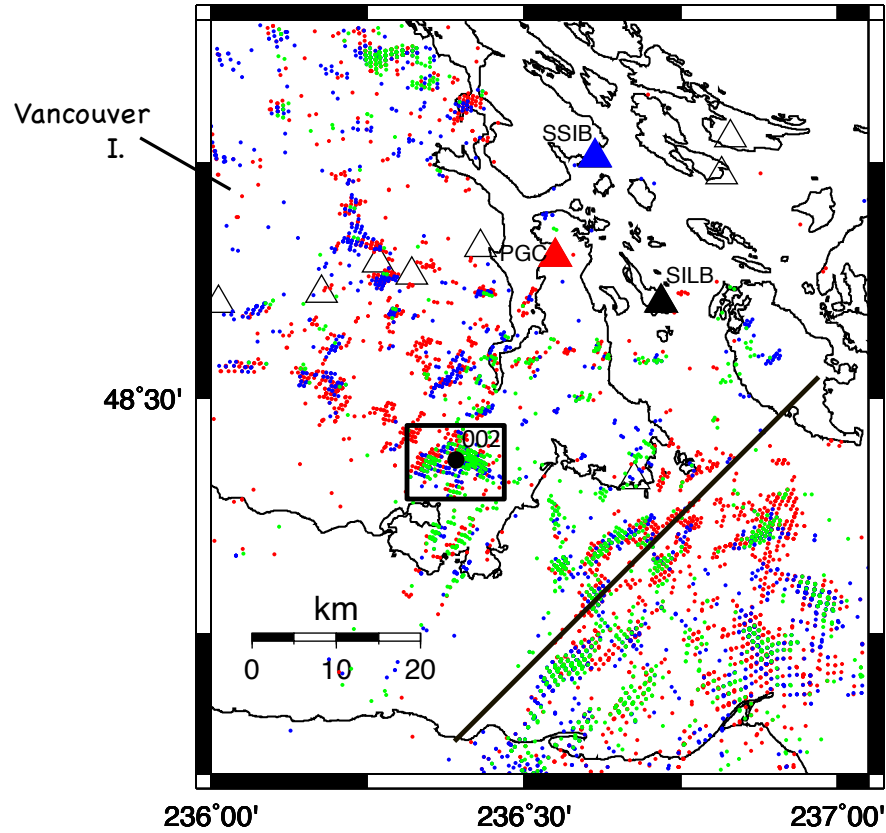
Sept 2005 + July 2004



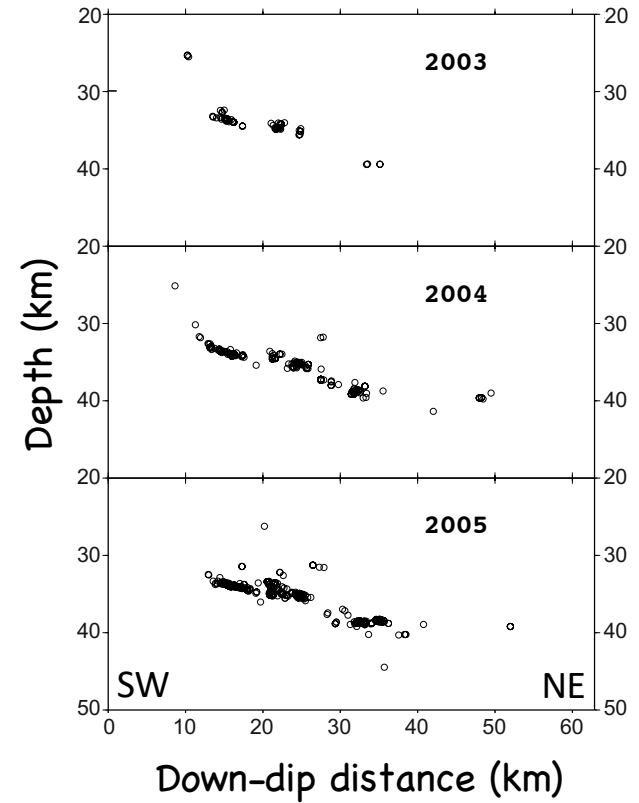
Arnbruster et al., 2014 (150 s windows)

## Slow slip episodes:

Sept 2005 + July 2004 + March 2003



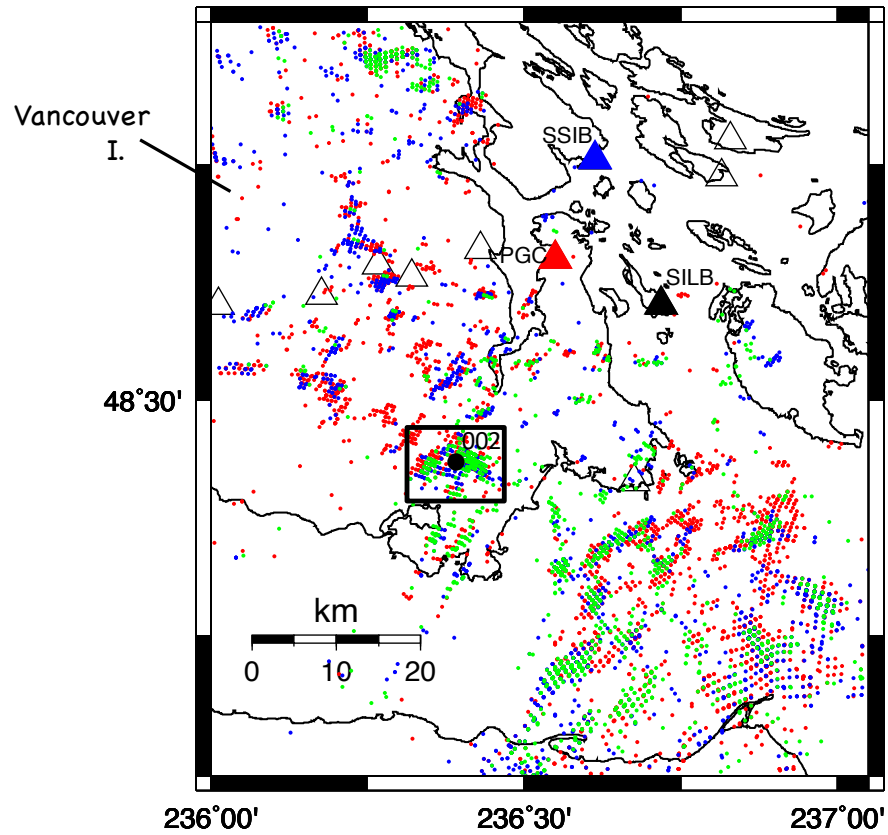
"Four S plus one P" catalog  
(753 detections vs 22,000)



Armbruster et al., 2014 (150 s windows)

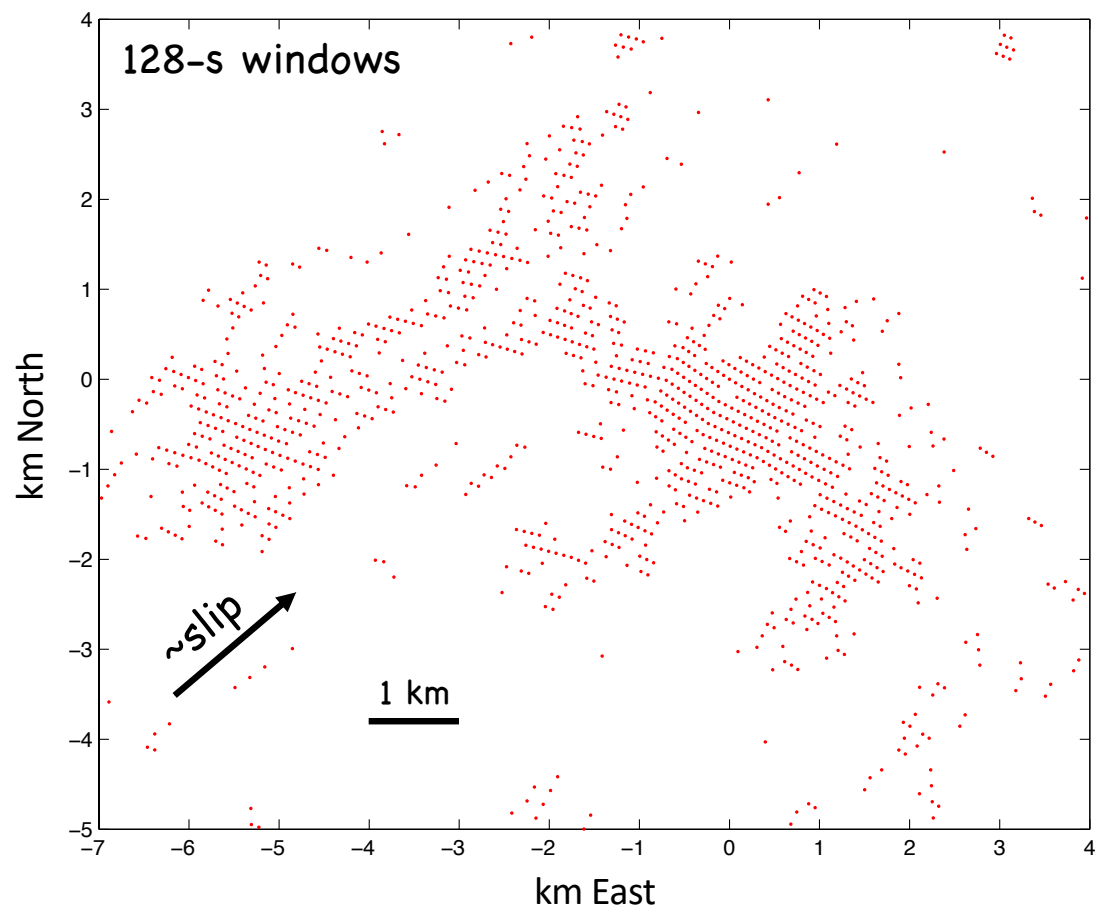
## Slow slip episodes:

Sept 2005 + July 2004 + March 2003

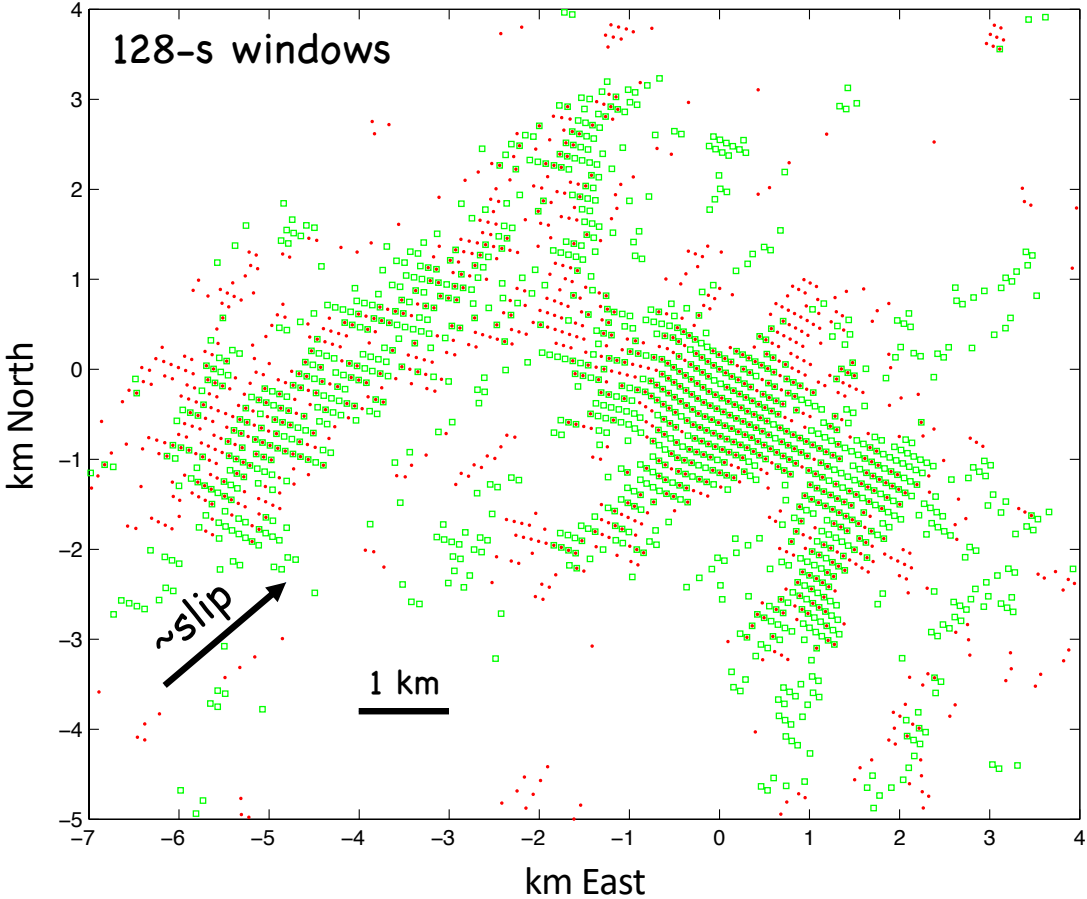


Arnbruster et al., 2014 (150 s windows)

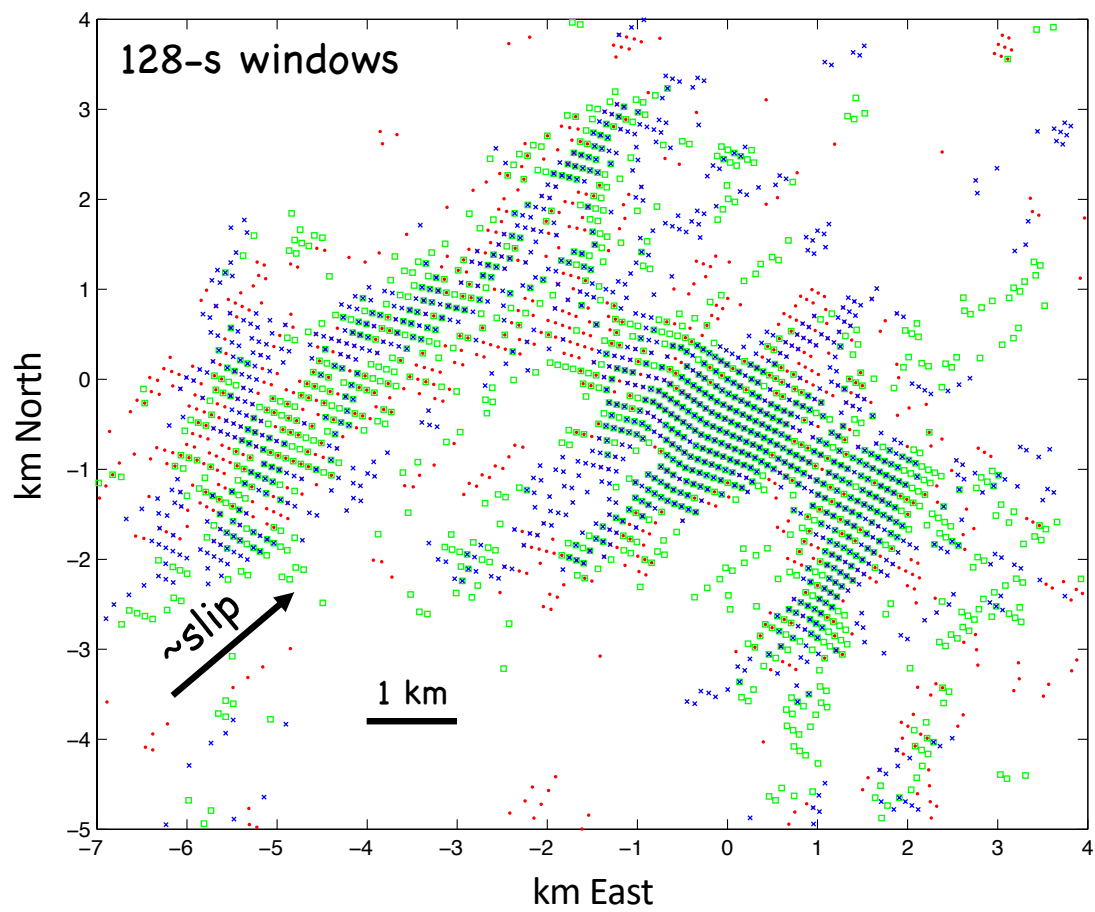
September 2005



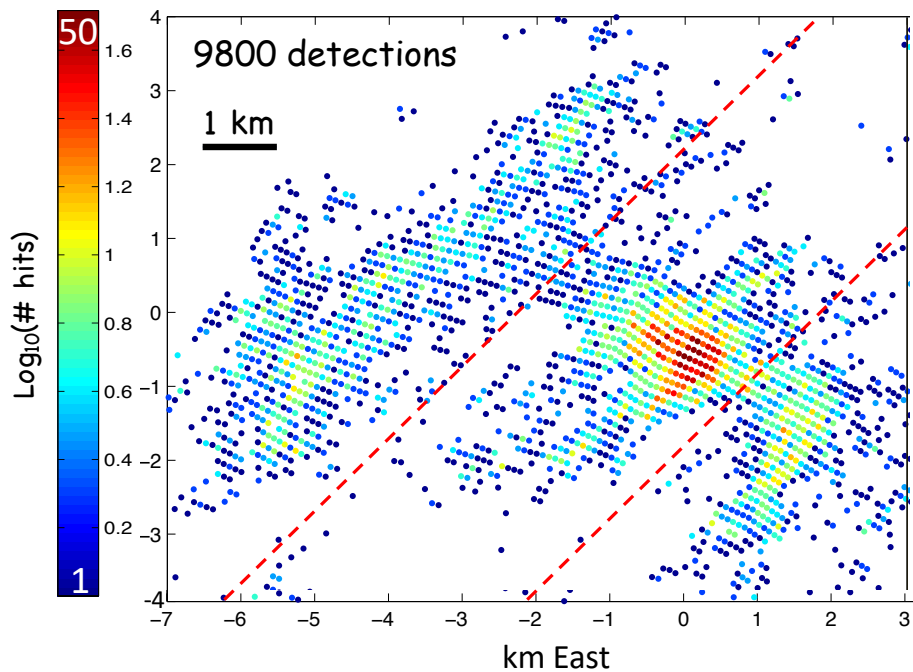
Sept 2005; July 2004



Sept 2005; July 2004; March 2003

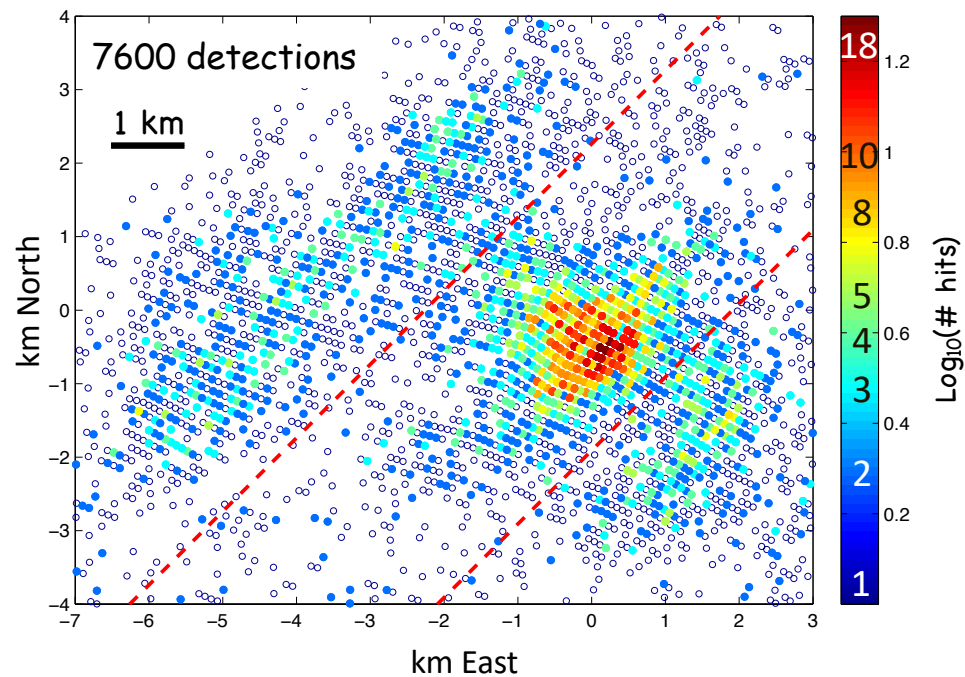


Sept 2005; July 2004; March 2003

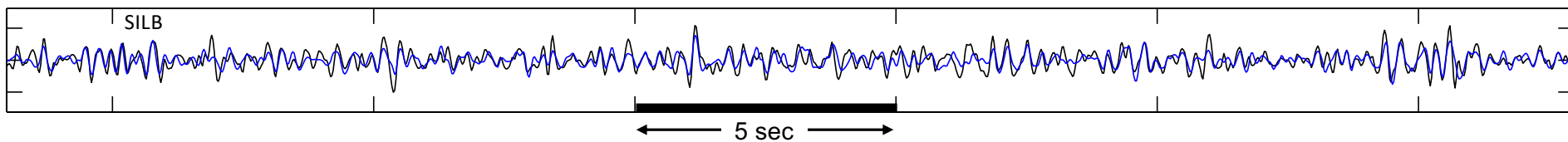


128-s windows

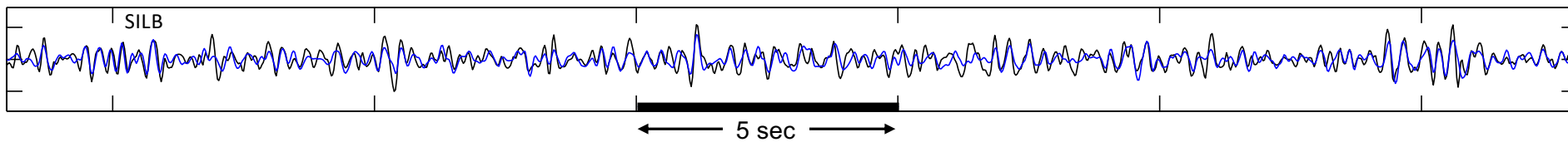
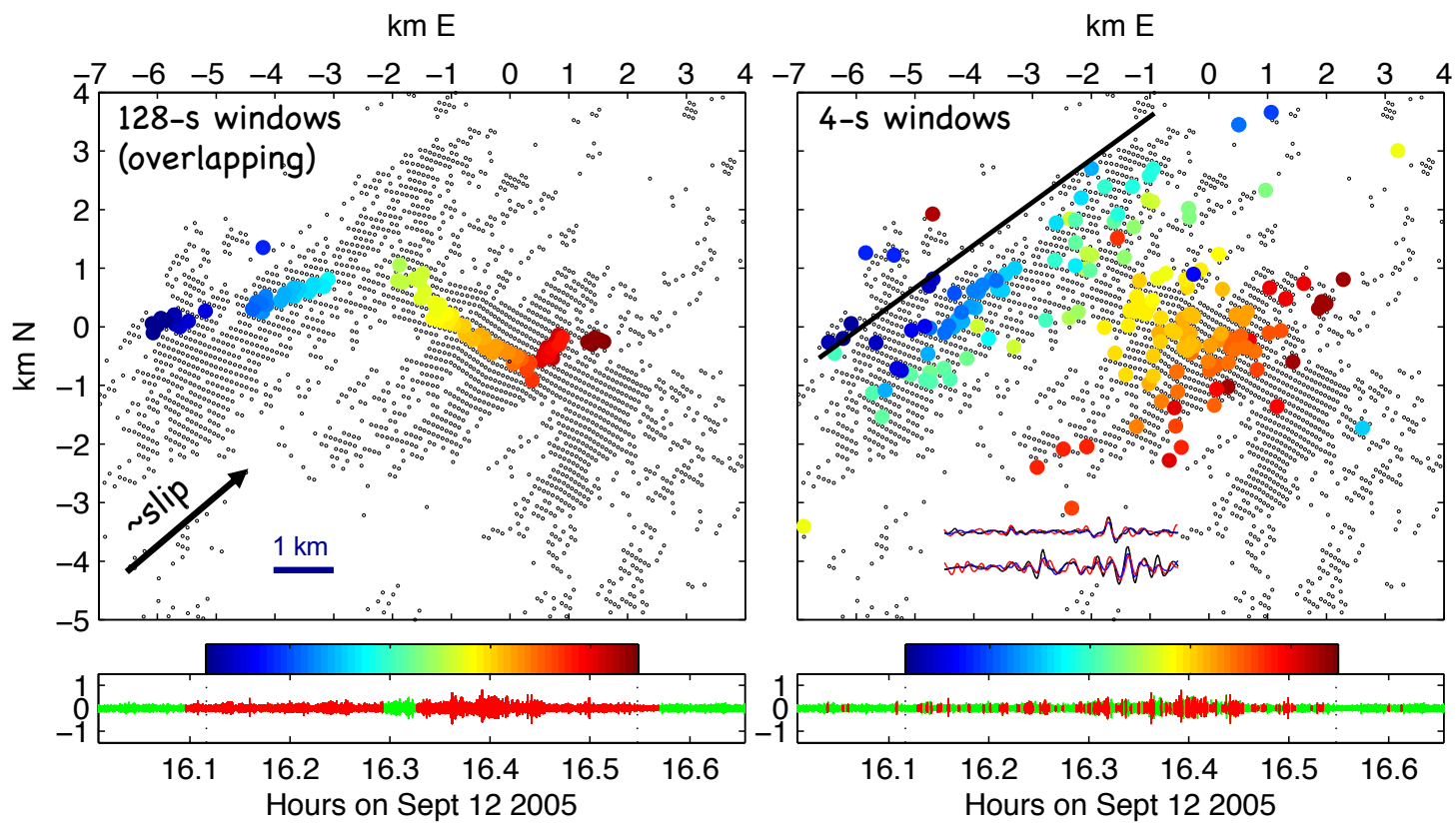
Sept 2005; July 2004; March 2003

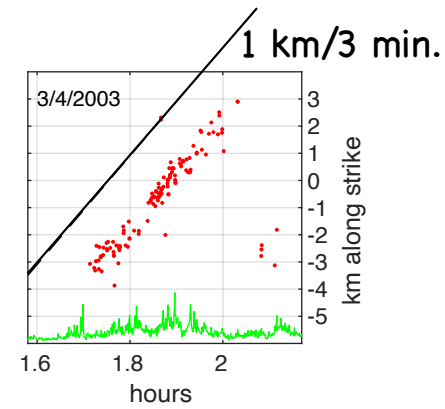
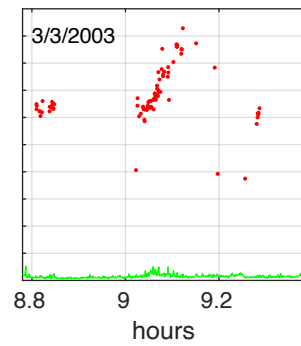
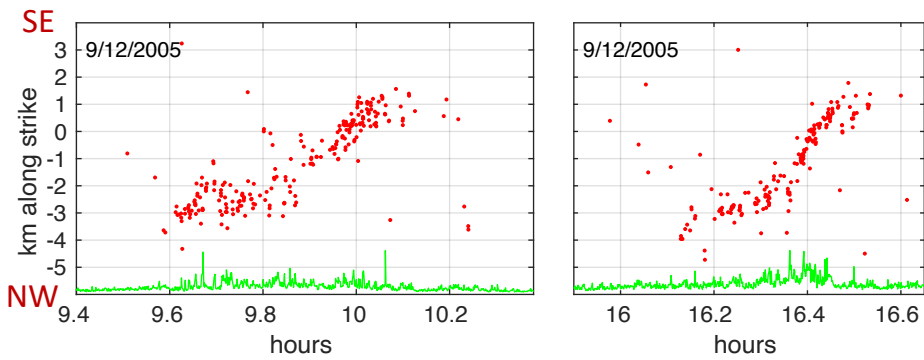
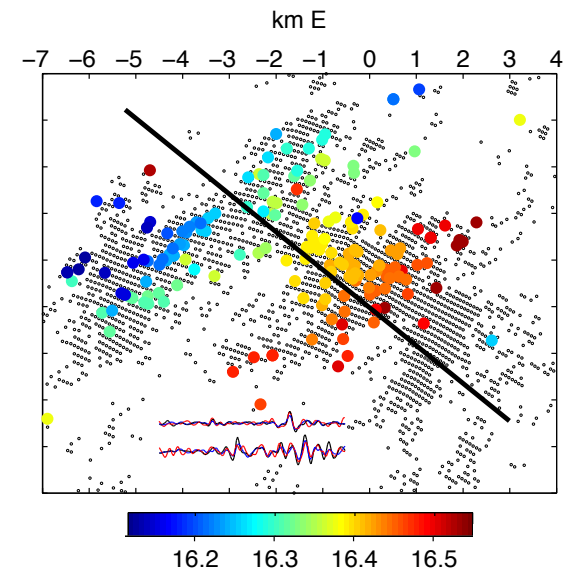
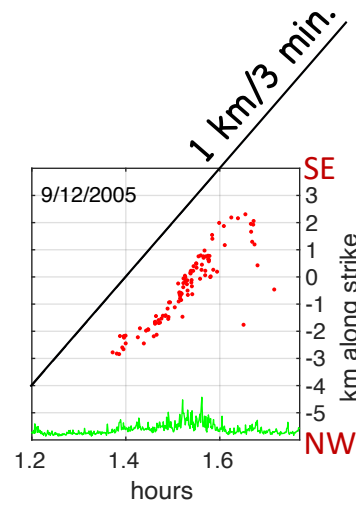
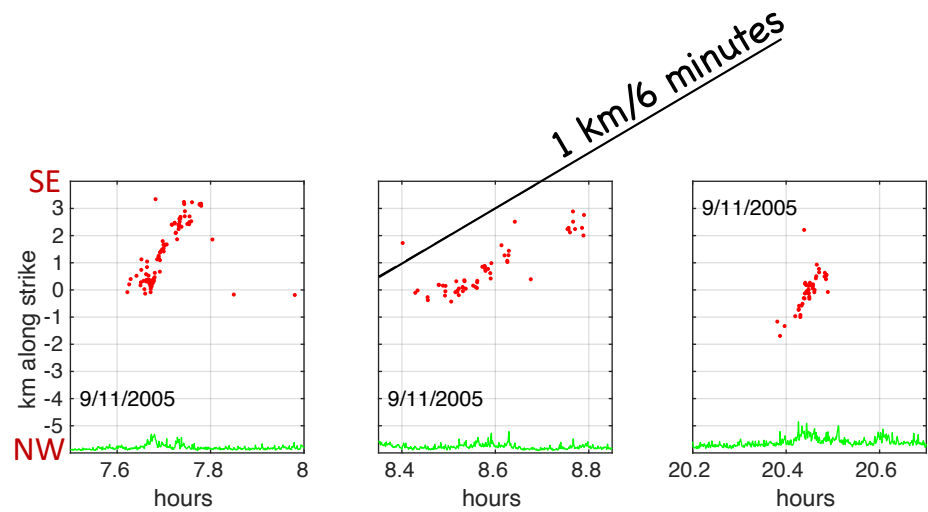


4-s windows

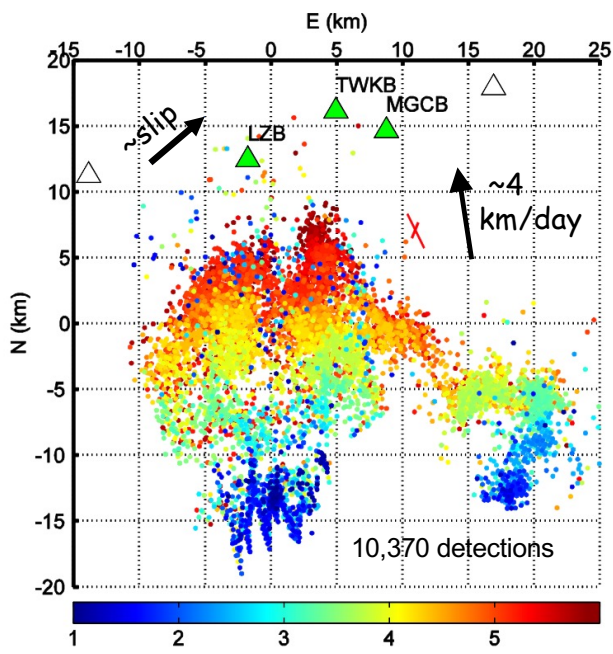




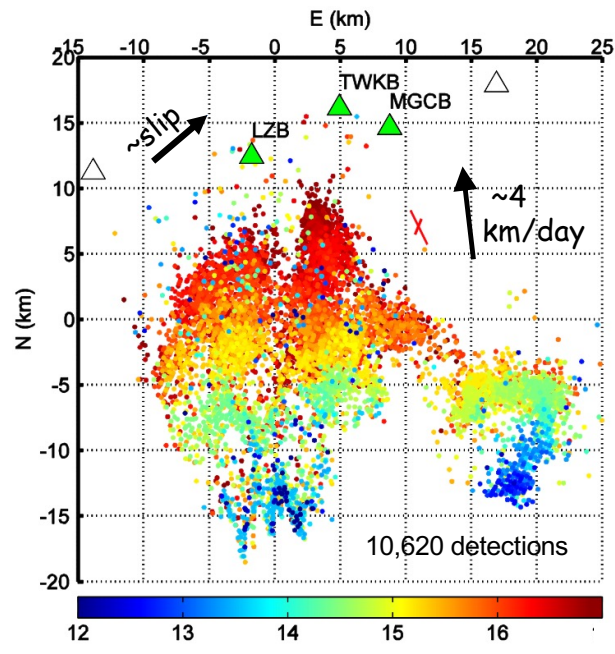




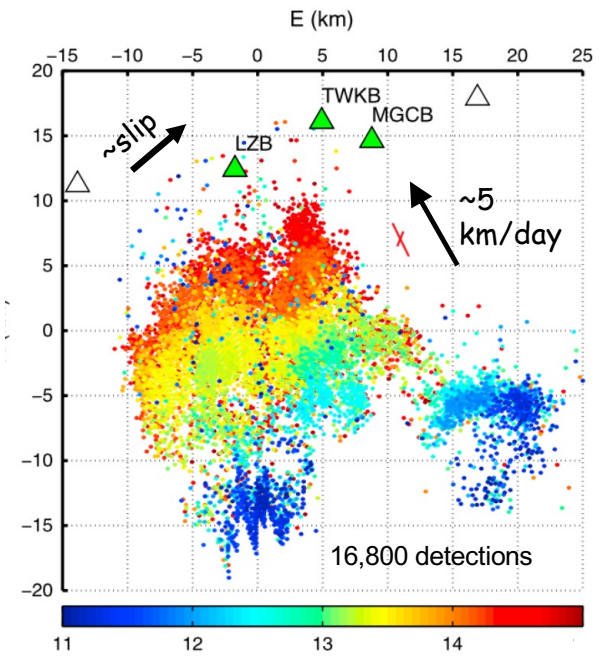
The "apparent" width of the slipping front tends to be 1 - 1.5 km. Each accumulates about 1-2 mm of slip. In roughly 200 s (1 km/[1 km/200 s]). Average slip speed 5-10  $\mu\text{m/s}$ .



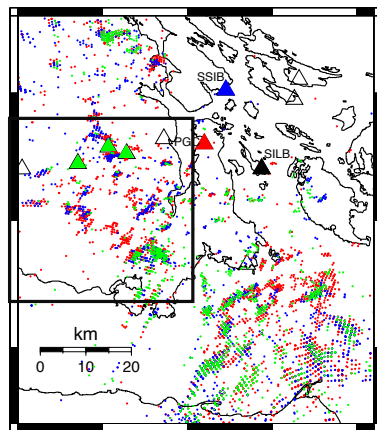
March 2003

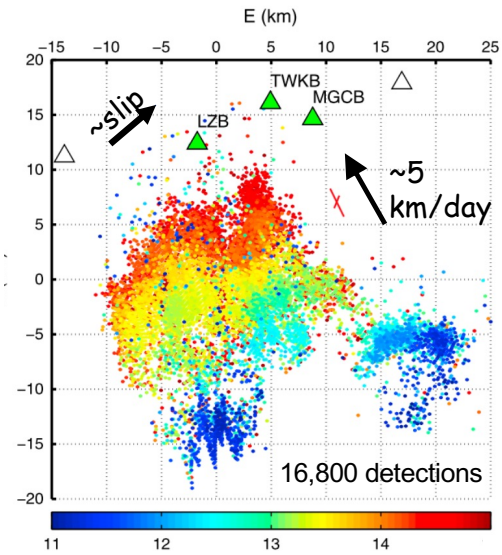
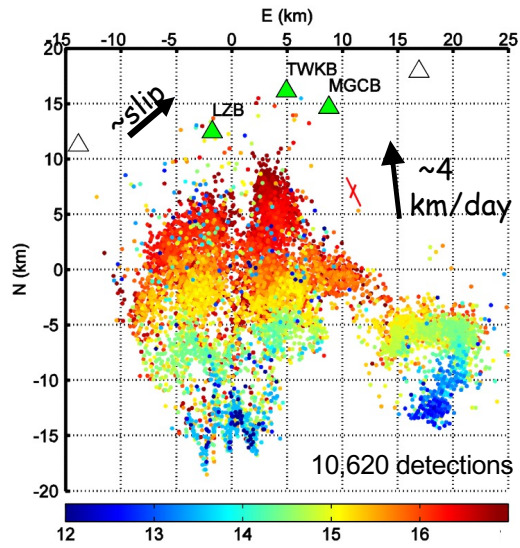
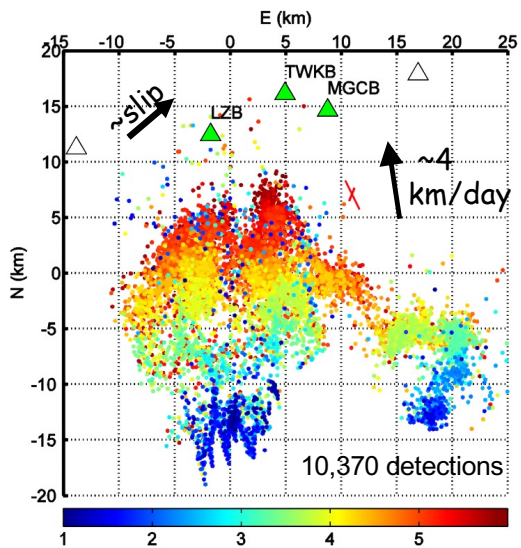


July 2004

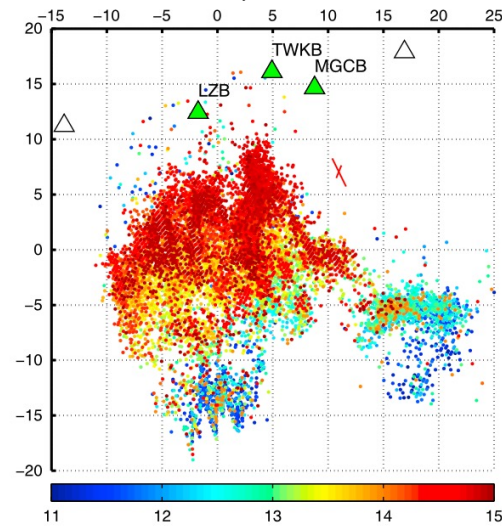
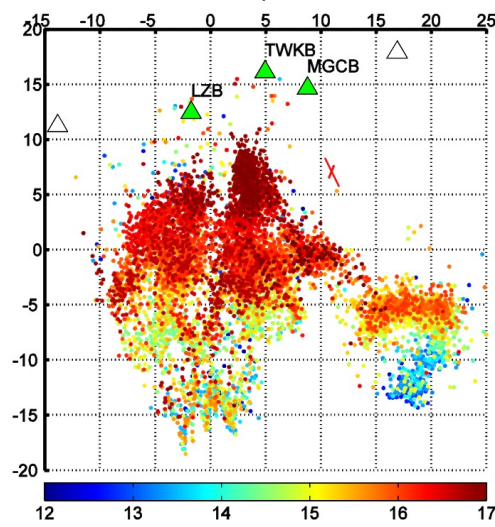
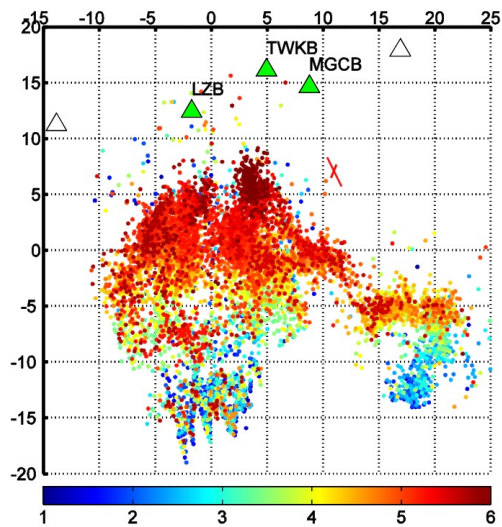


Sept 2005





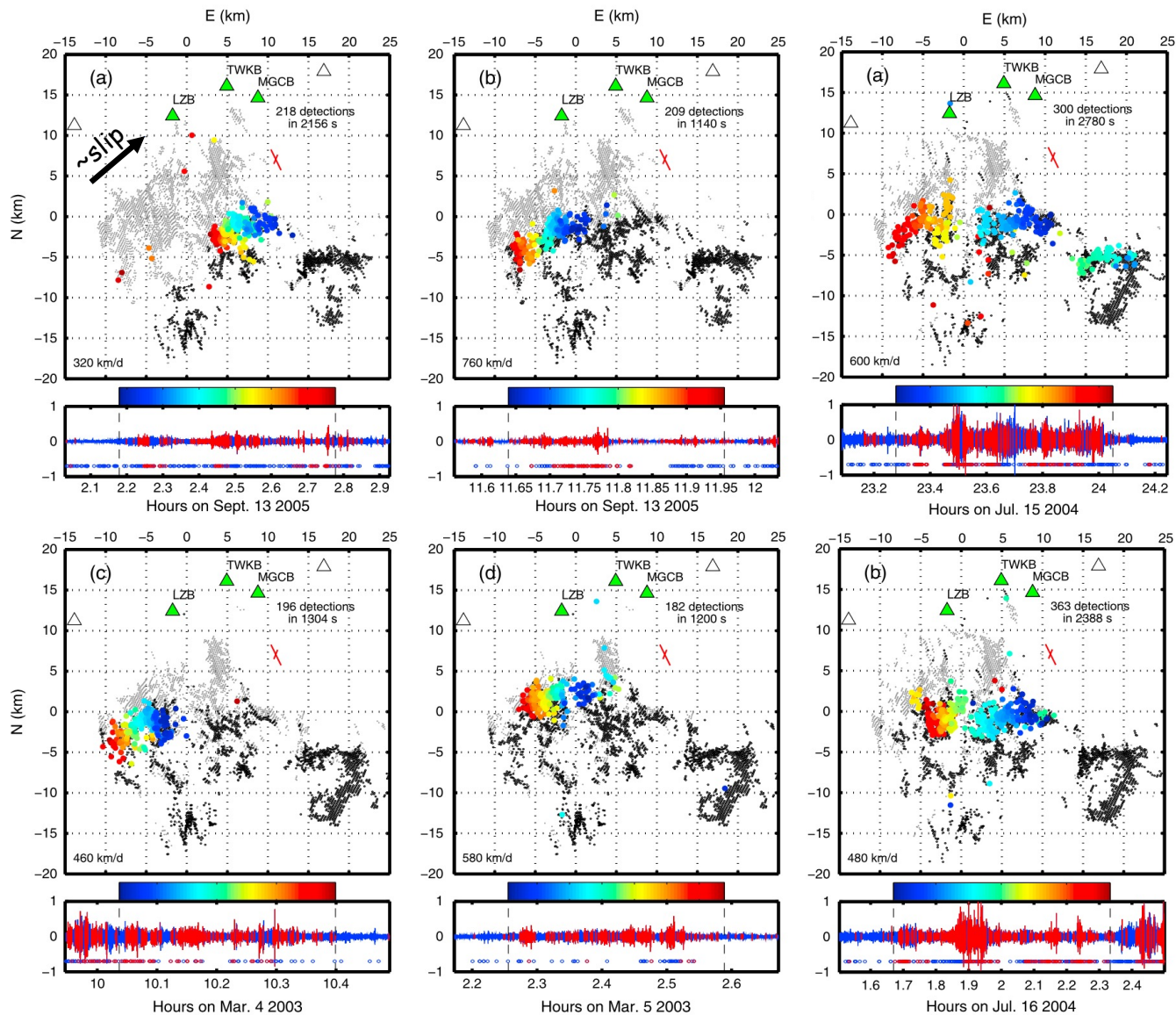
Earliest (blue)  
on top



Latest (red)  
on top

Gray dots: All detections  
 Black dots: Detections  
 thus far in this SSE

Migrations are along the  
 main front, 50 - 150 times  
 faster than the main front  
 propagation rate  
 (hundreds of km/day).

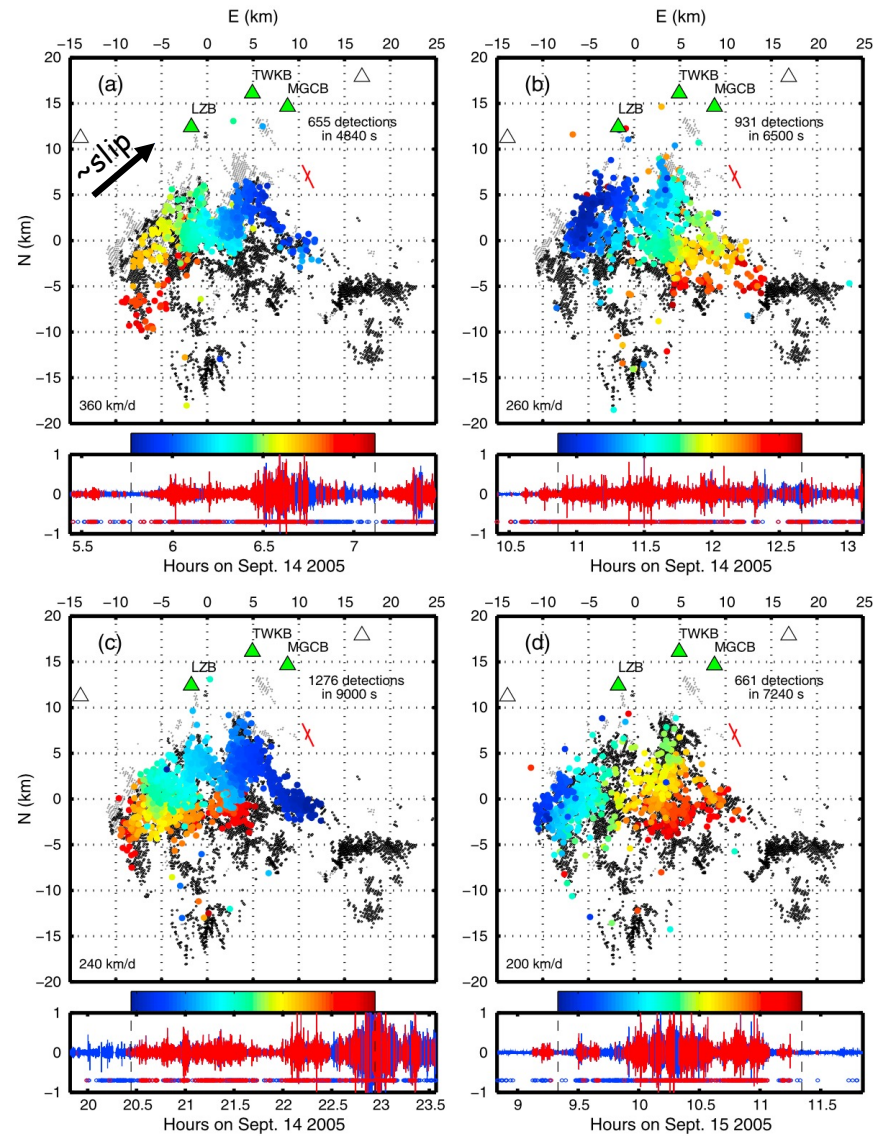


Gray dots: All detections

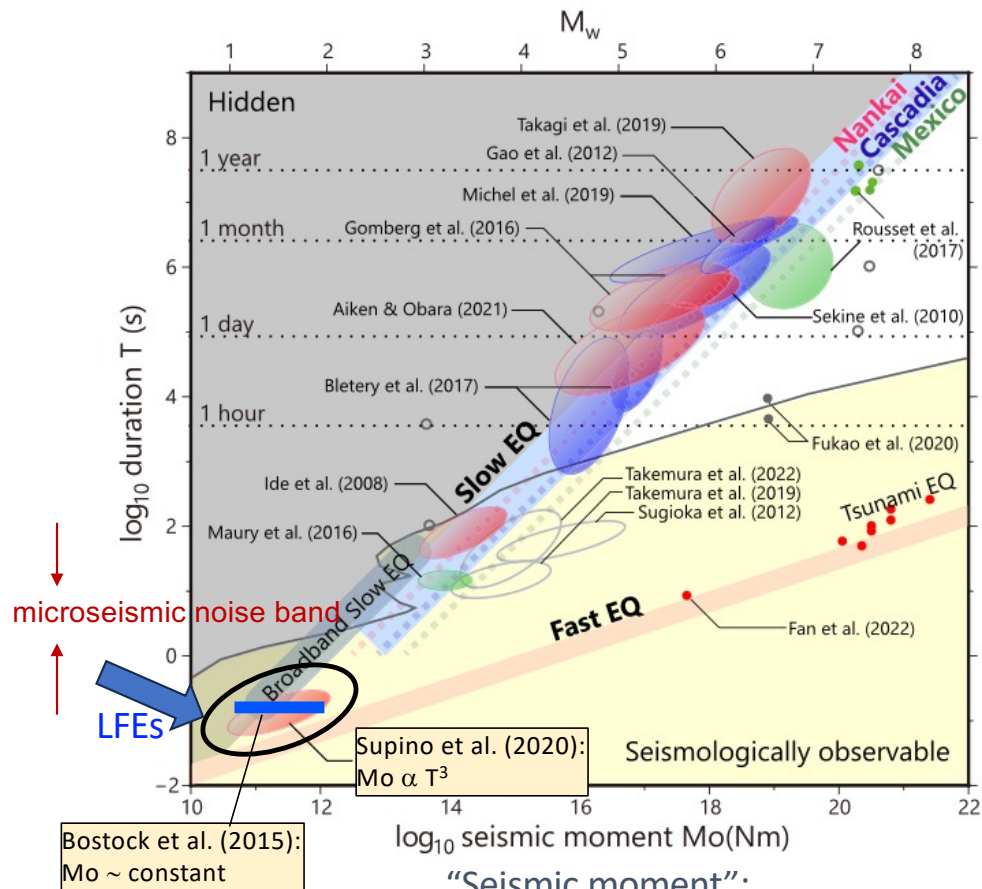
Black dots: Detections  
thus far in this SSE

4 migrations in 30 hours.  
Propagation speeds  
1 km/4-6 minutes.

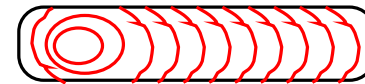
>3500 detections in 460  
minutes (4-s windows).  
On average, one 4-s  
detection every 7-8 s.



# So what are Low Frequency Earthquakes?



$M_o \propto T$  ( $T = \text{duration}$ )



$M_o \propto T^3$ :

Area  $\propto R^2$  (geometry)

Slip  $\propto R$  (elasticity & uniform stress drop)

$\Rightarrow M_o \propto R^3$

$T \propto R$  (uniform rupture velocity)

$\Rightarrow M_o \propto T^3$

“Seismic moment”:  
(slip area) x (slip distance) x (shear modulus)

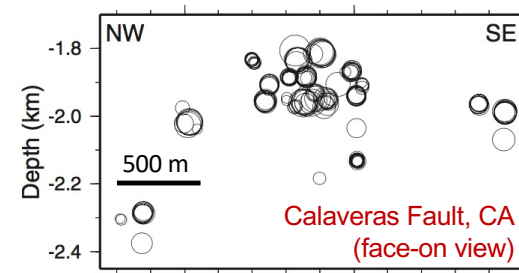
Ide & Beroza, 2023

# What are Low-Frequency Earthquakes?

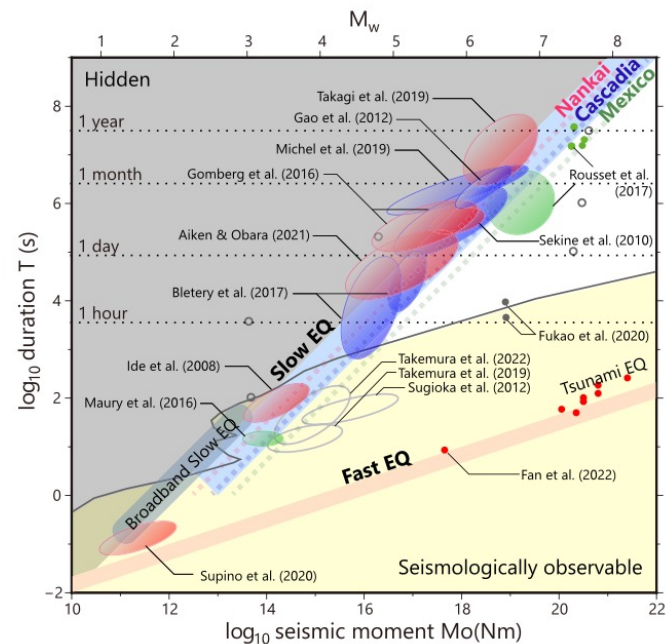
Two (somewhat) different views:

1. The "Slow earthquake trend" just links two familiar end-members: LFEs are stick-slipping brittle asperities embedded in an otherwise creeping fault zone; that creep gives rise to slow slip. 50-second "VLFs" are just a bunch of LFEs concentrated in space and time (Ando et al, 2010; Gomberg et al., 2016).

2. "LFEs" occupy the high-frequency limit of a continuous spectrum extending from periods <1 sec to several weeks or more ("slow slip events"). "LFEs" are just what we see of this continuum when we look in the frequency band 1-8 Hz (Ide). (Think stochastic fluctuations of fault slipping area and/or sliding speed.)



Each LFE is an acceleration followed by a deceleration. Each LFE source is mechanically distinct from its surroundings.



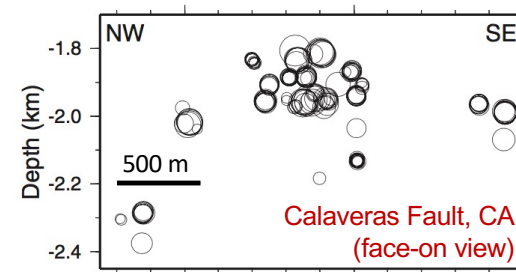


## What are Low-Frequency Earthquakes?

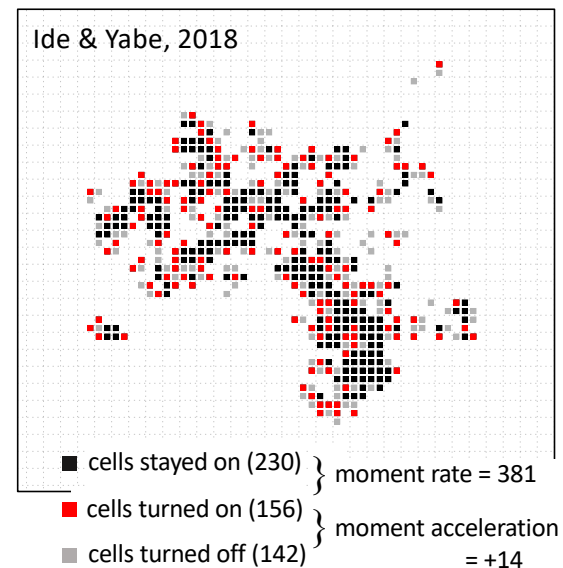
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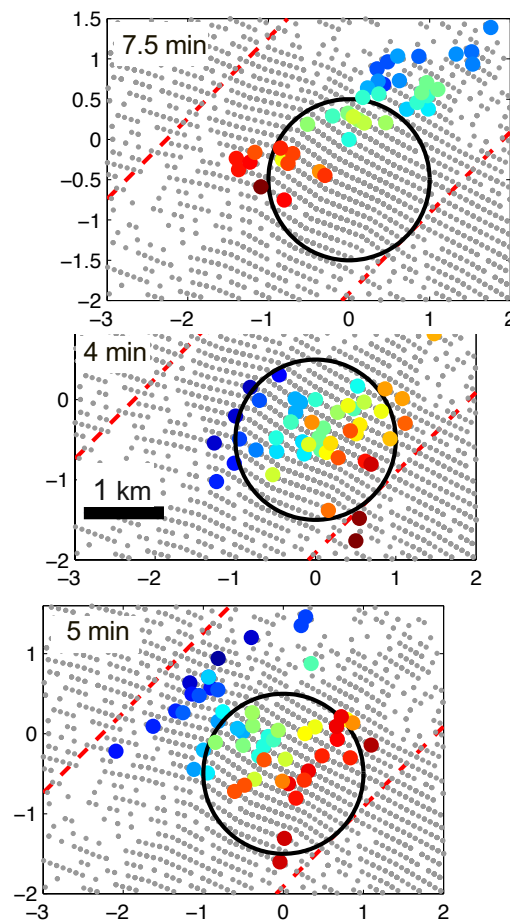
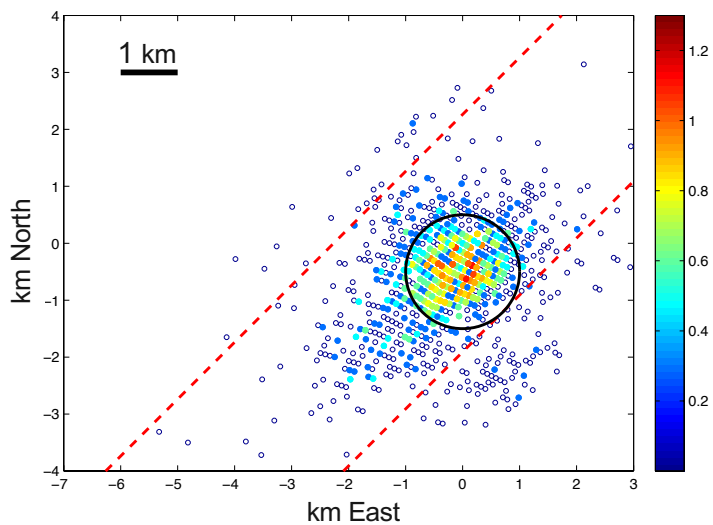
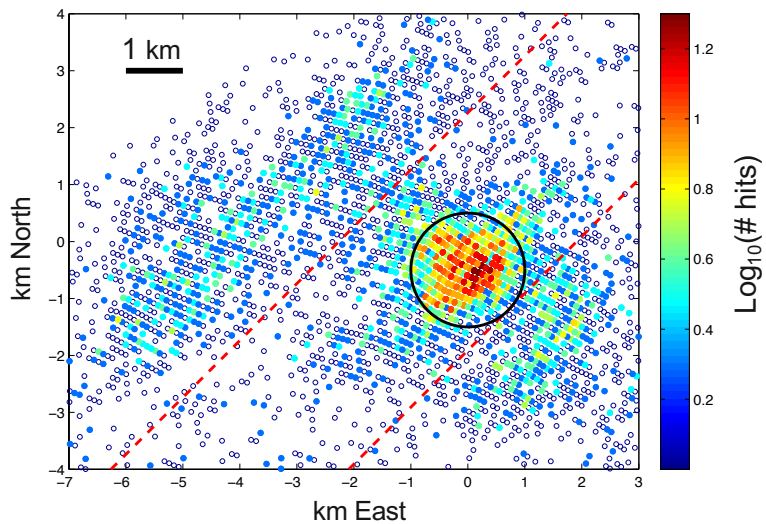


Accelerations and decelerations need not come from the same spot. "An LFE" is inherently a composite of many events, not necessarily mechanically distinct from their surroundings.

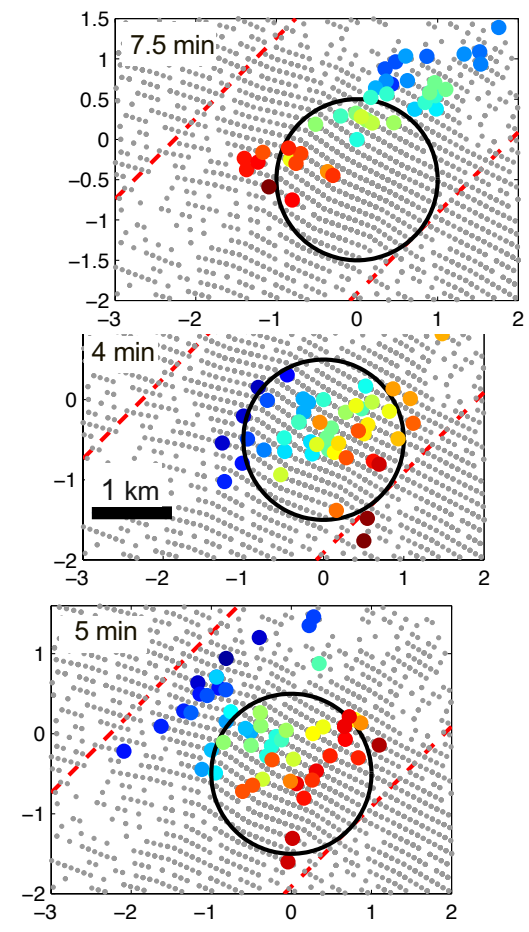
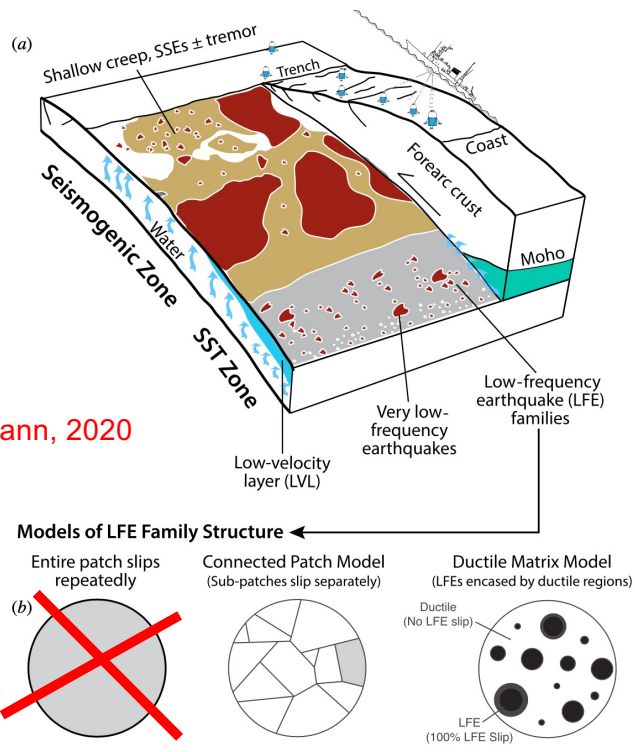
Our 4-second-window locations (7800)

SO – What can we learn from good tremor locations?

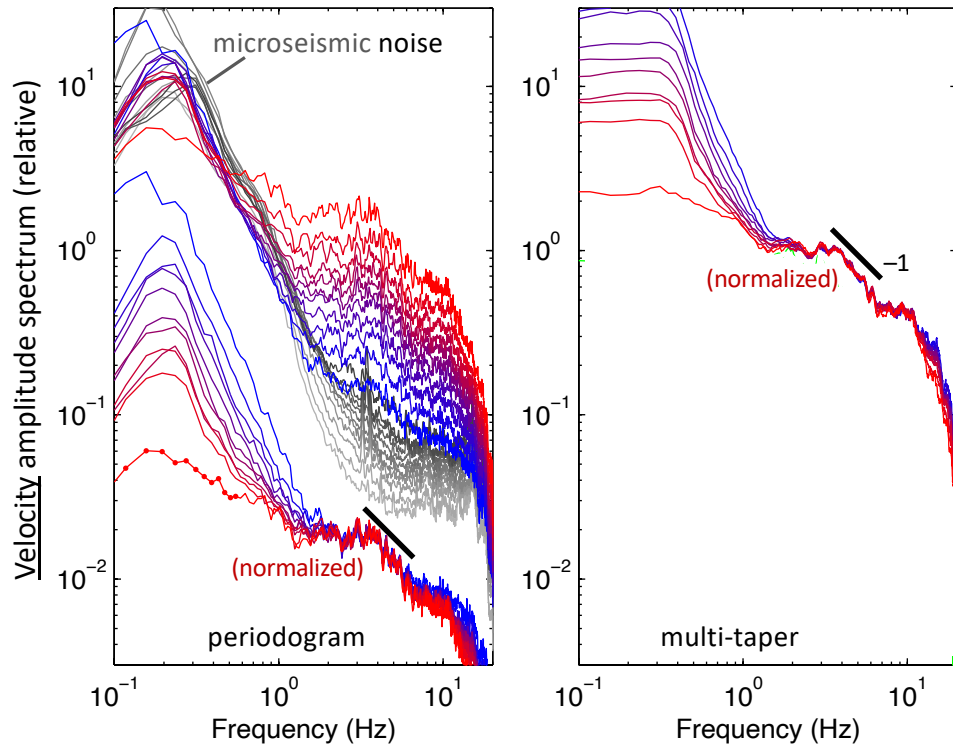
Our 4-second locations of Bostock LFE family #002 (~2/3 of them; 1472/2287)



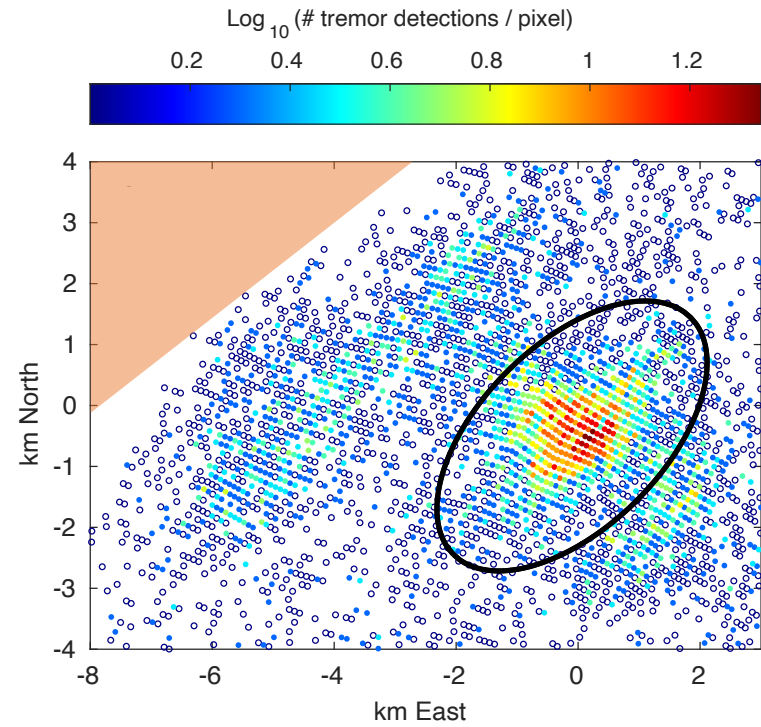
Behr & Burgmann, 2020



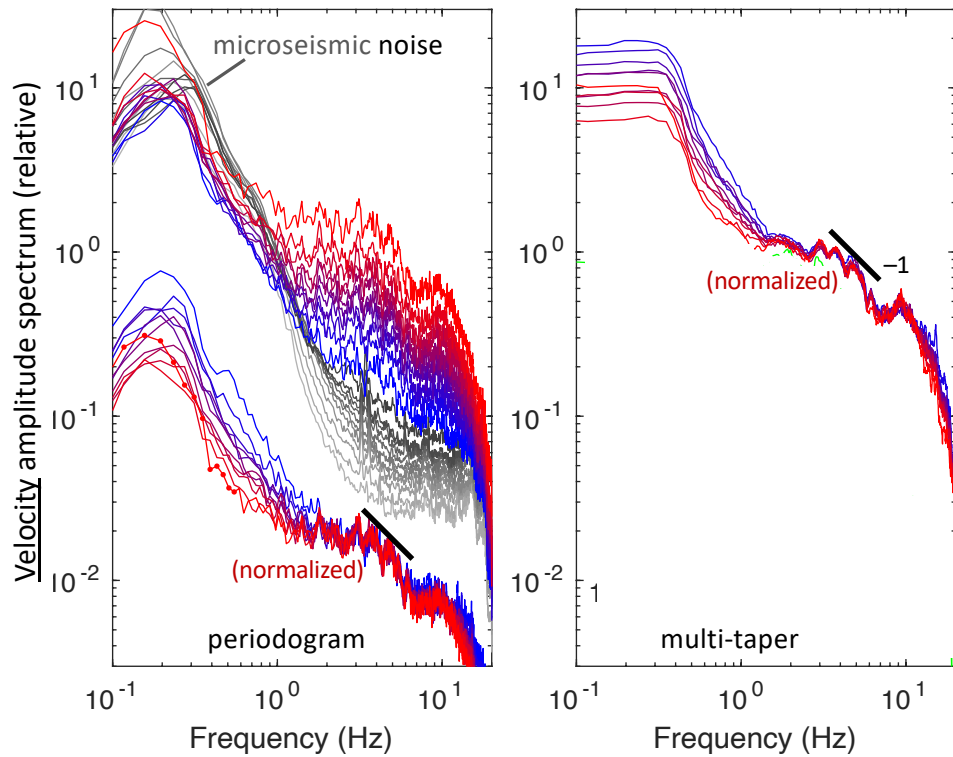
LFE "families" are an observational convenience; they don't reflect the distribution of seismic sources on the fault.



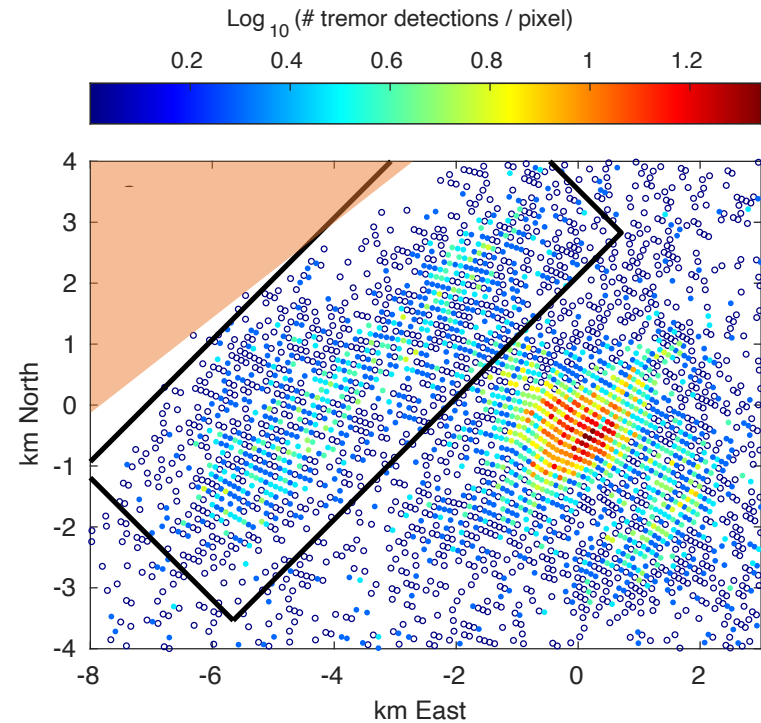
Tremor spectra are independent of tremor amplitude!



- 154 time windows with:
  - a minimum of five 4-s detections
  - a maximum gap of 30 s
- 14,300 s (4 hours) of data
- 1288 half-overlapping 18-s windows
- 3-station median
- binned by amplitude 2.4-4 Hz



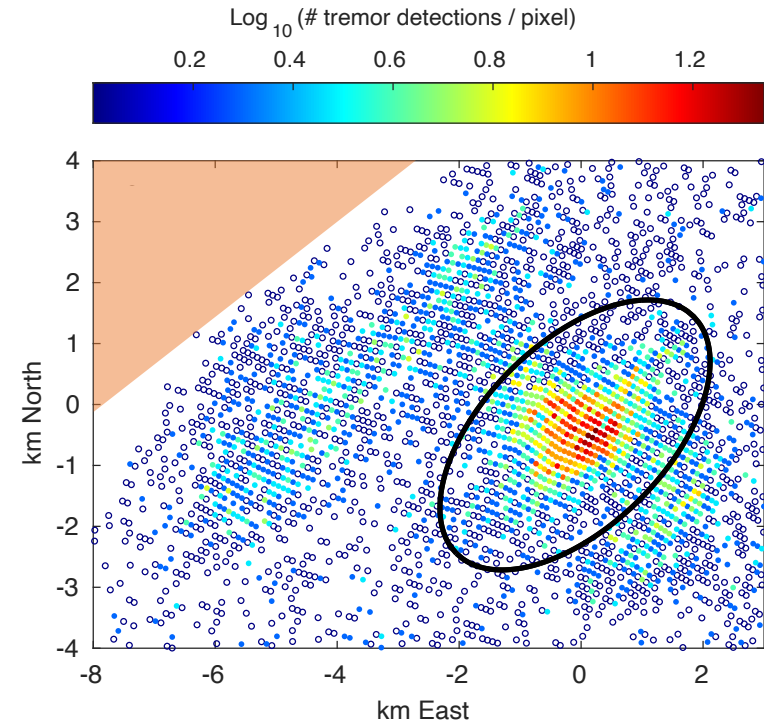
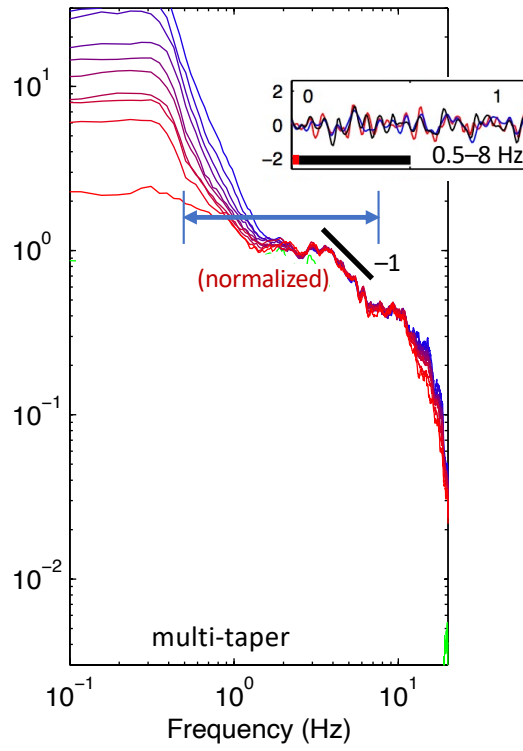
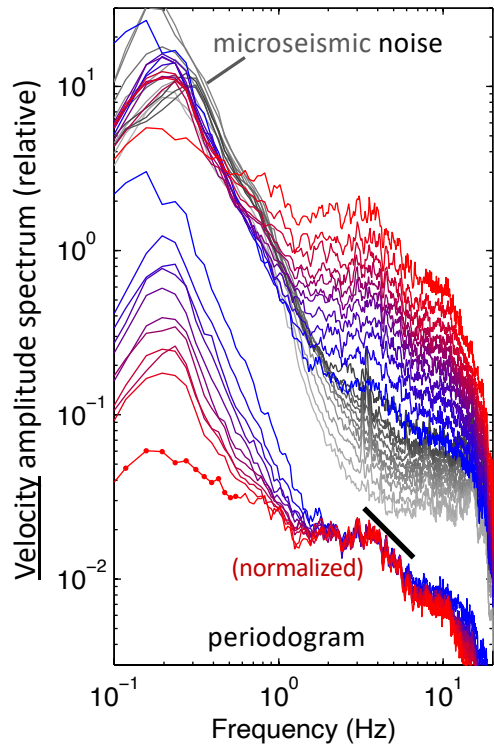
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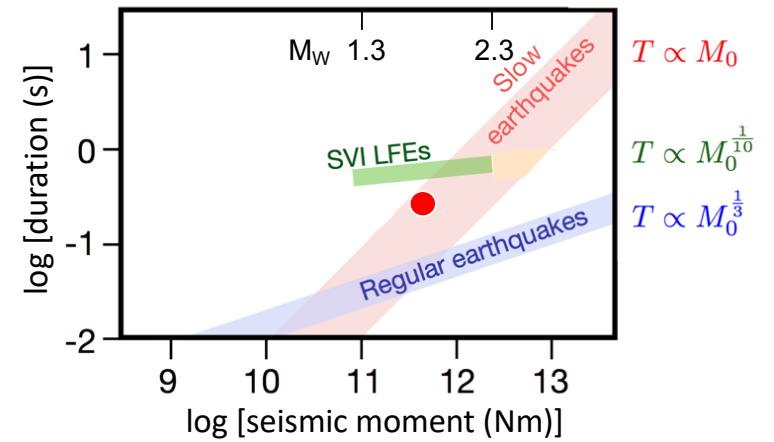
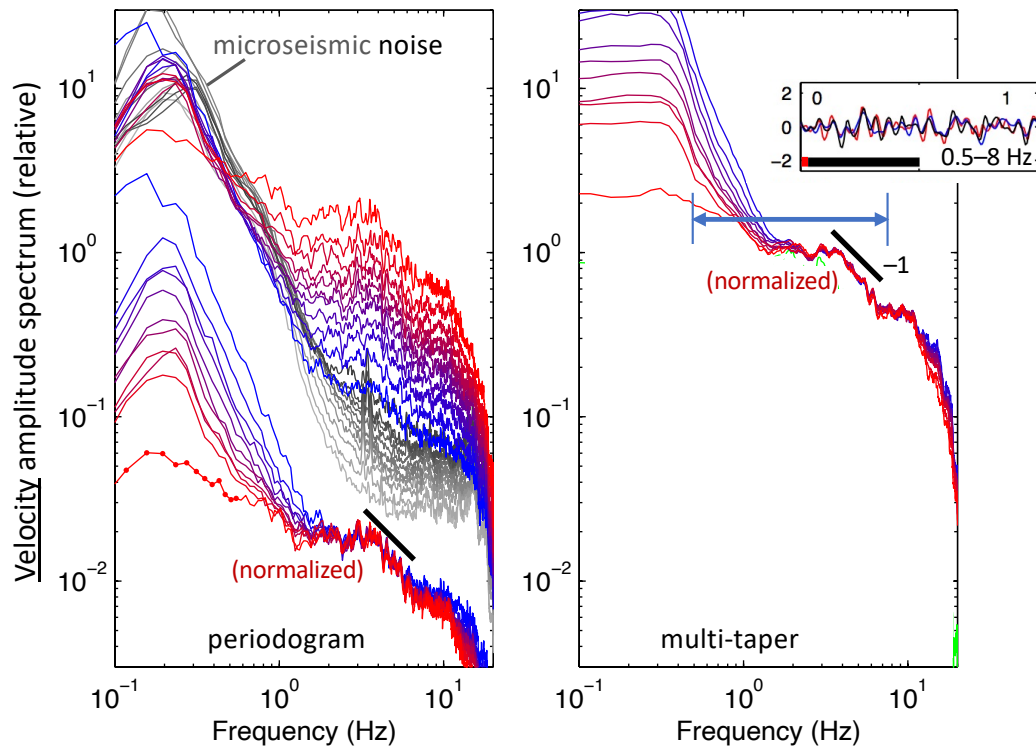
- 101 time windows with:

  - a minimum of five 4-s detections
  - a maximum gap of 30 s

- 9270 s (2.6 hours) of data
- 833 half-overlapping 18-s windows
- 3-station median
- binned by amplitude 2.4-4 Hz

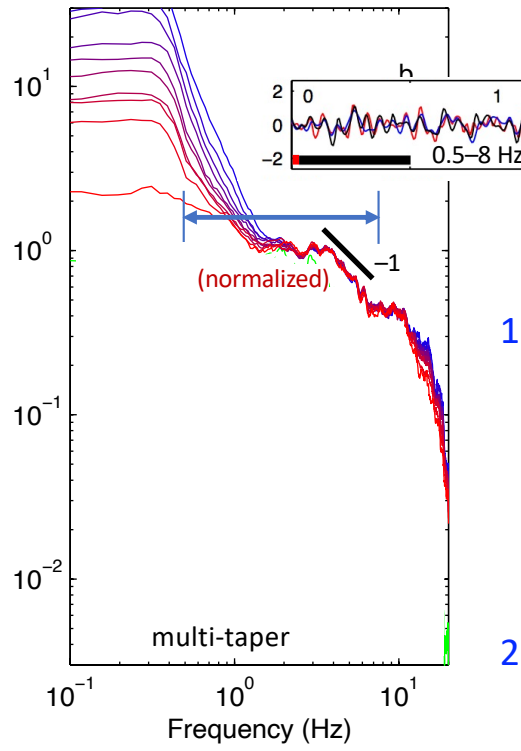
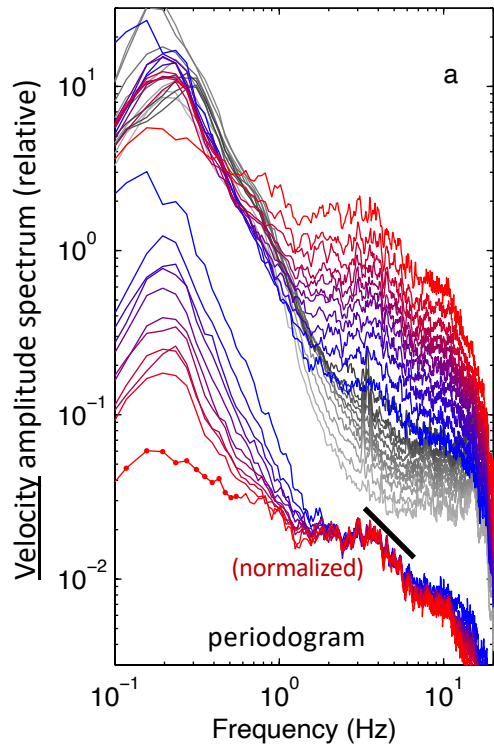


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(courtesy M. Bostock)

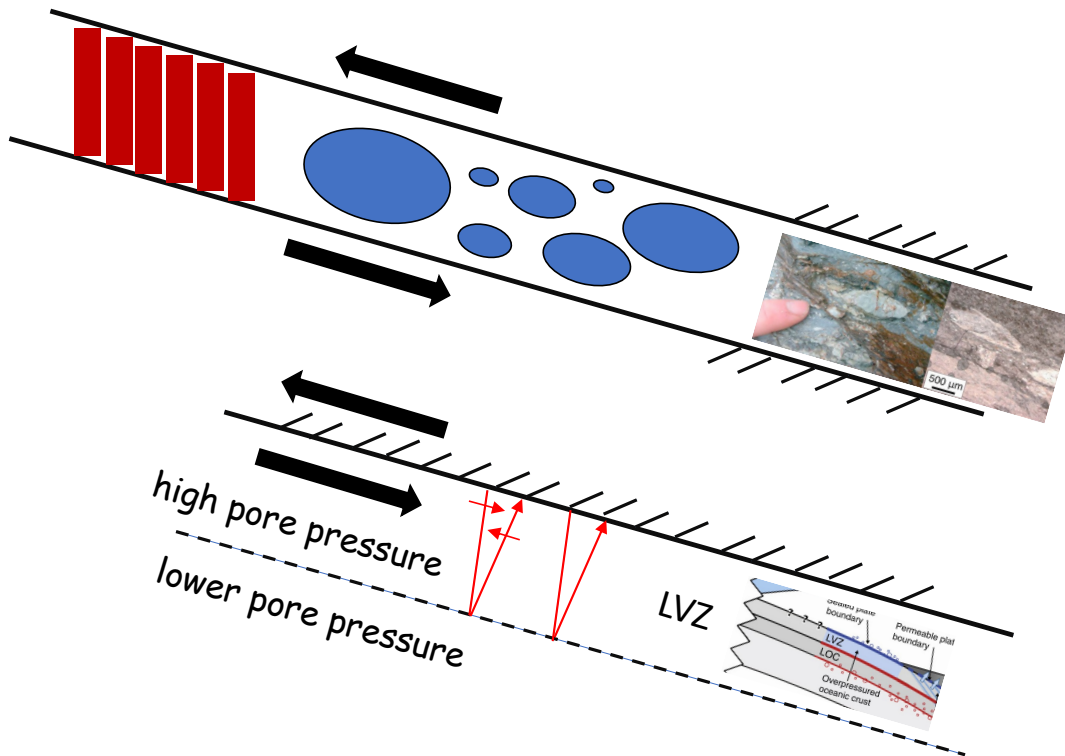
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- 3-station median
- binned by amplitude 2.4-4 Hz



1. LFEs are more than just what one sees of tremor in the  $\sim 2\text{--}8$  Hz passband of good signal-to-noise ratio. (If not due to attenuation) the 4-Hz “corner” represents a fundamental time scale of the tremor source region. Whatever process sets that time scale defines the basic building block of tremor.
2. The characteristic duration of  $\sim 1/4$  s is independent of tremor amplitude, and is most plausibly a characteristic length scale divided by a characteristic velocity, for example a fault-zone thickness or largest clast size divided by a shear wave speed.

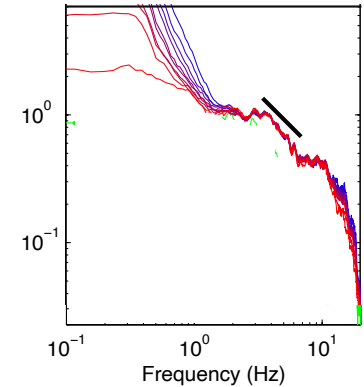


## Mechanisms for generating a characteristic time scale:



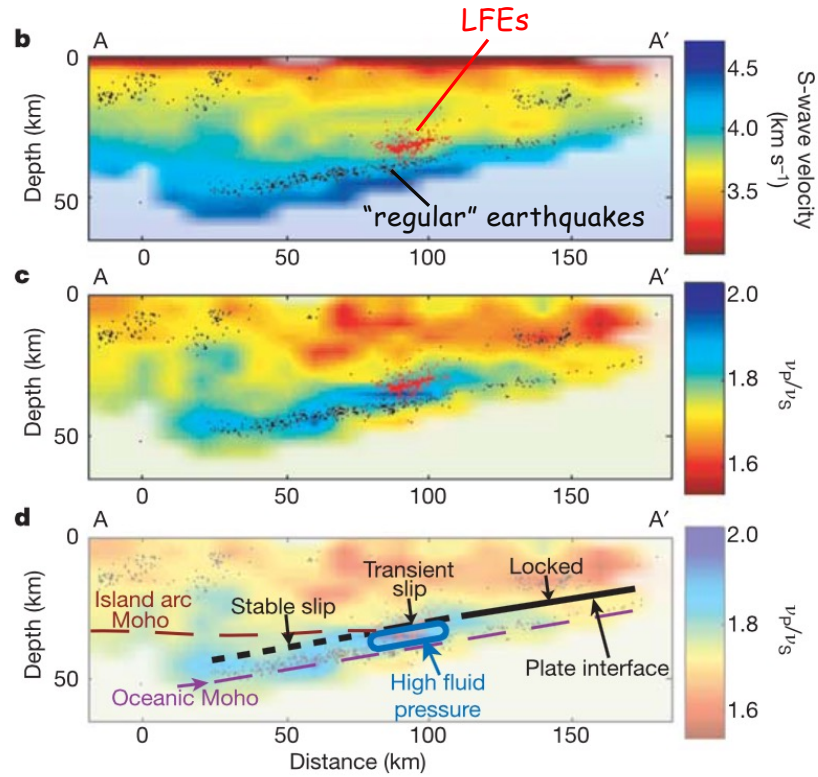
Busted-up eclogite blocks;  
bookshelf faulting; etc.

Reflected waves in a  
compliant fault zone

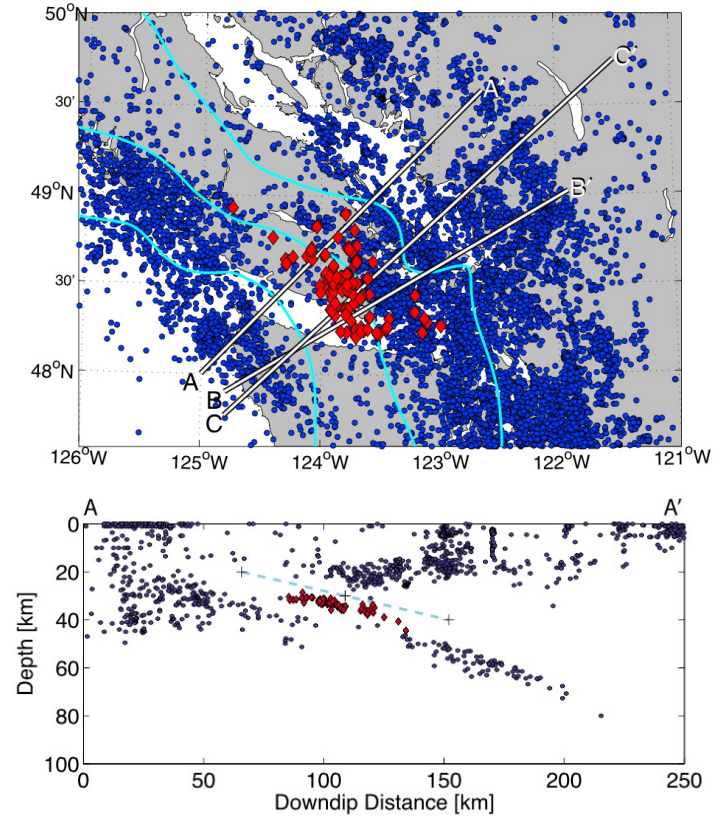


(all of these rely on the fault zone thickness plus a wave speed)  
(or maybe a fault zone thickness plus a reduced propagation speed)

Some consensus that the corner is not due to attenuation...

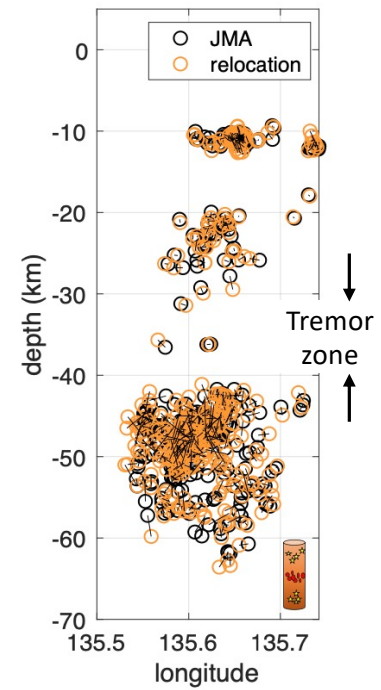
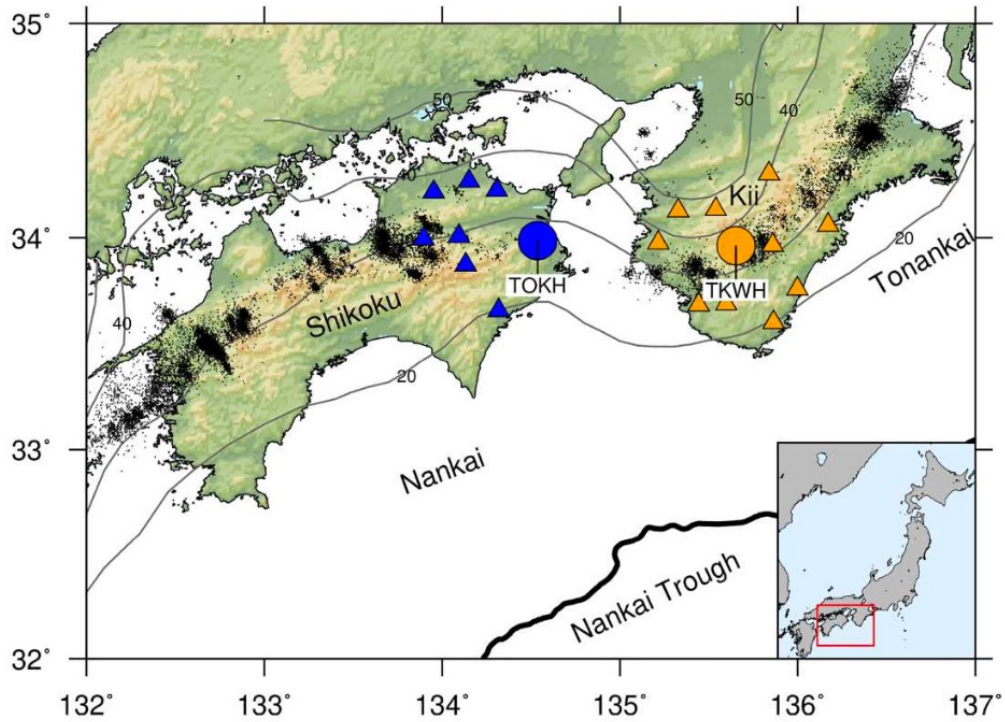


Shelly et al., 2006

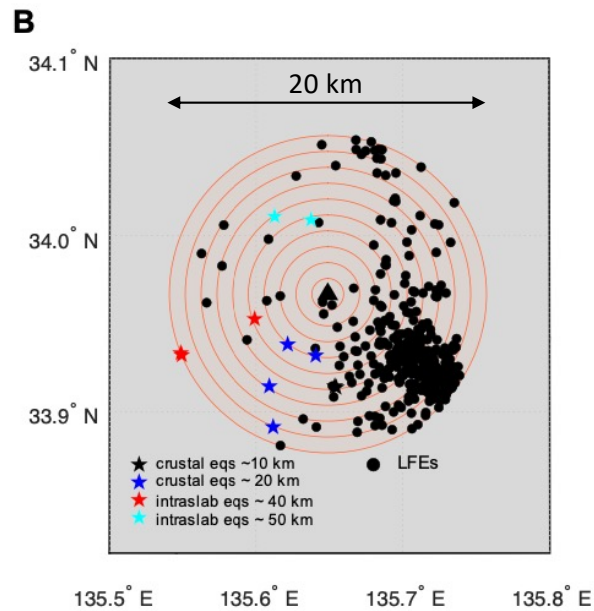


Bostock et al., 2012

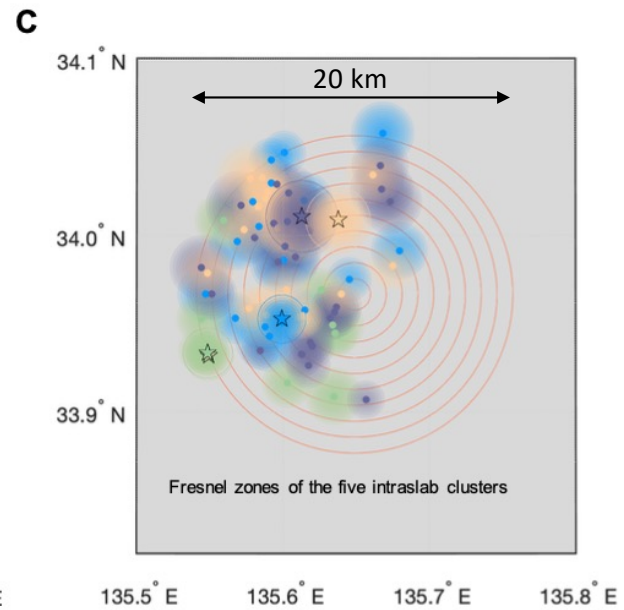
This was also the conclusion of Wang et al. (2023):



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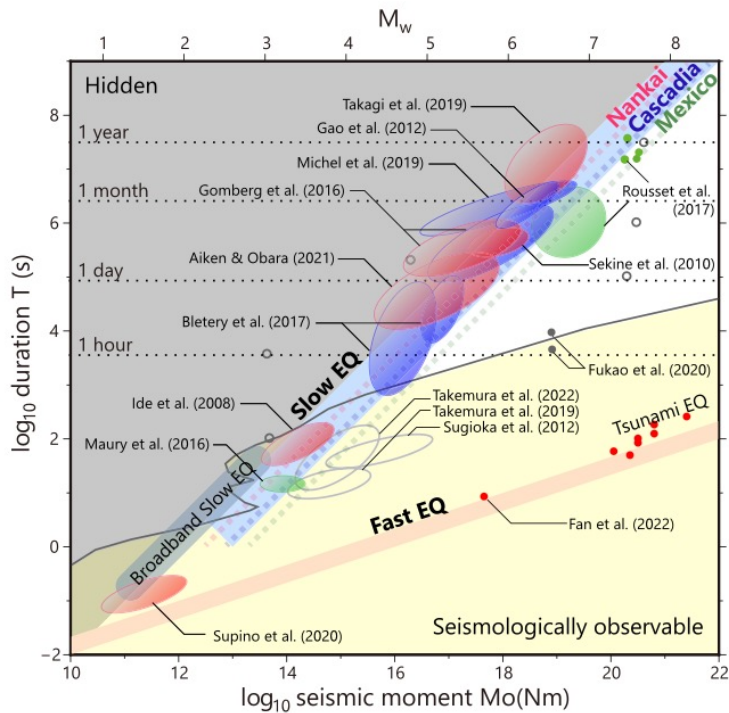


Map view of tremor locations

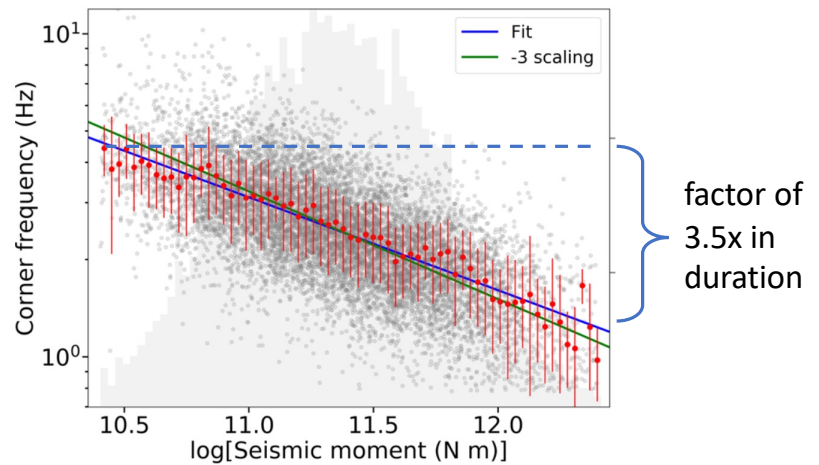


Map view of the “Fresnel zones”  
of deeper earthquakes as they  
pass through the tremor zone

Is it good enough?



Ide and Beroza, 2023

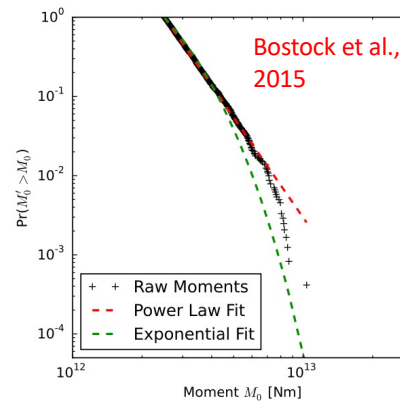
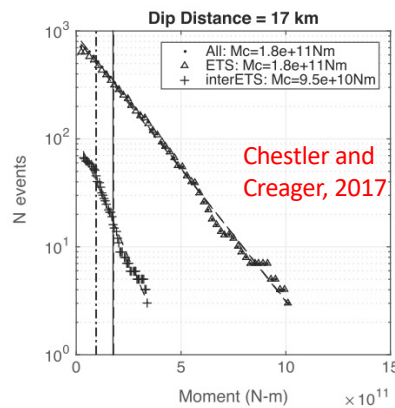


Supino et al., 2022

So how to interpret the Supino et al. result that LFE moment in Shikoku is proportional to duration<sup>3</sup>, in light of the Bostock/Farge result that LFE duration is ~independent of moment, and the result that tremor corner frequency is independent of amplitude?

An observation related(?) to the "characteristic duration" observation:

Bostock's SVI catalog has 160,000 LFE's with  $M > 1.6$ , and 0 with  $M > 2.6$ :  
LFEs have a well-defined average, or "characteristic", moment  
(e.g., exponential distribution; power-law with  $b$ -values in the range 6-8; etc.)  
Due to a characteristic (well-defined average) length scale in the source region?

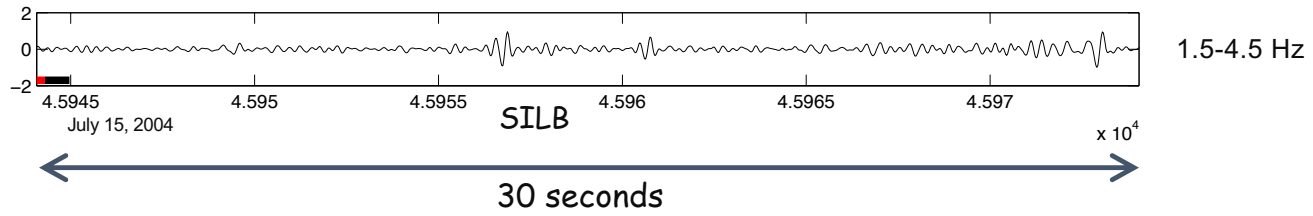


A characteristic moment implies that if tremor is the superposition of myriad LFEs, the seismogram is dominated by the sum of the little ones, not the occasional big ones (unlike regular earthquakes).

### Saturated (in time) seismogram:

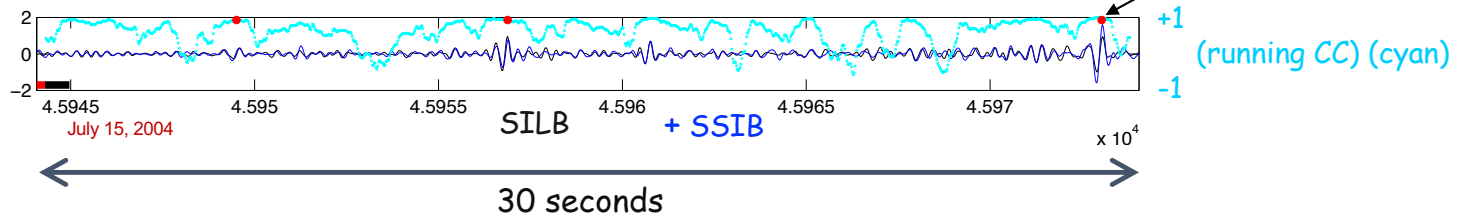
A seismogram for which, on average, the time lag between the direct wave arrivals of different events is shorter than the typical event duration.

(Most? All?) SVI tremor seismograms are "saturated" in time:

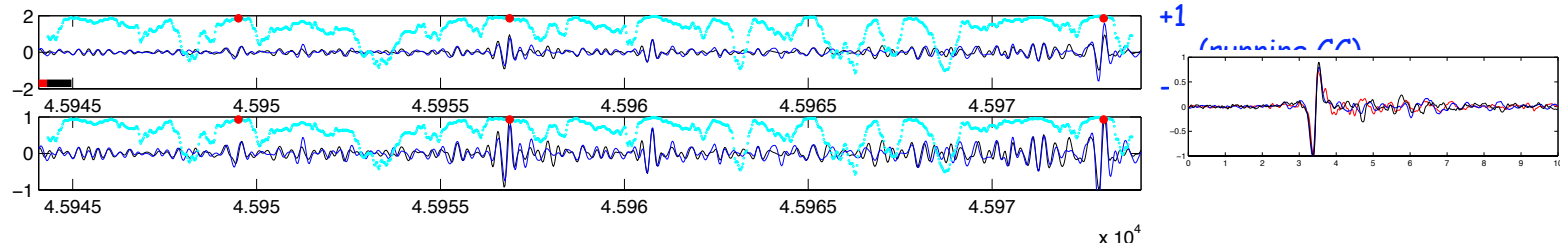




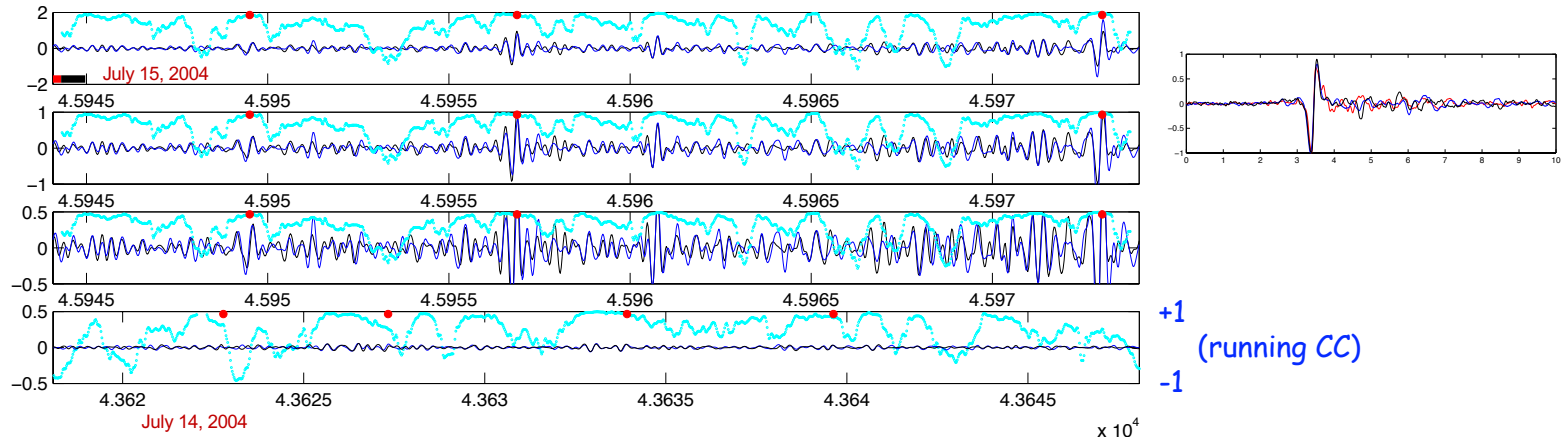
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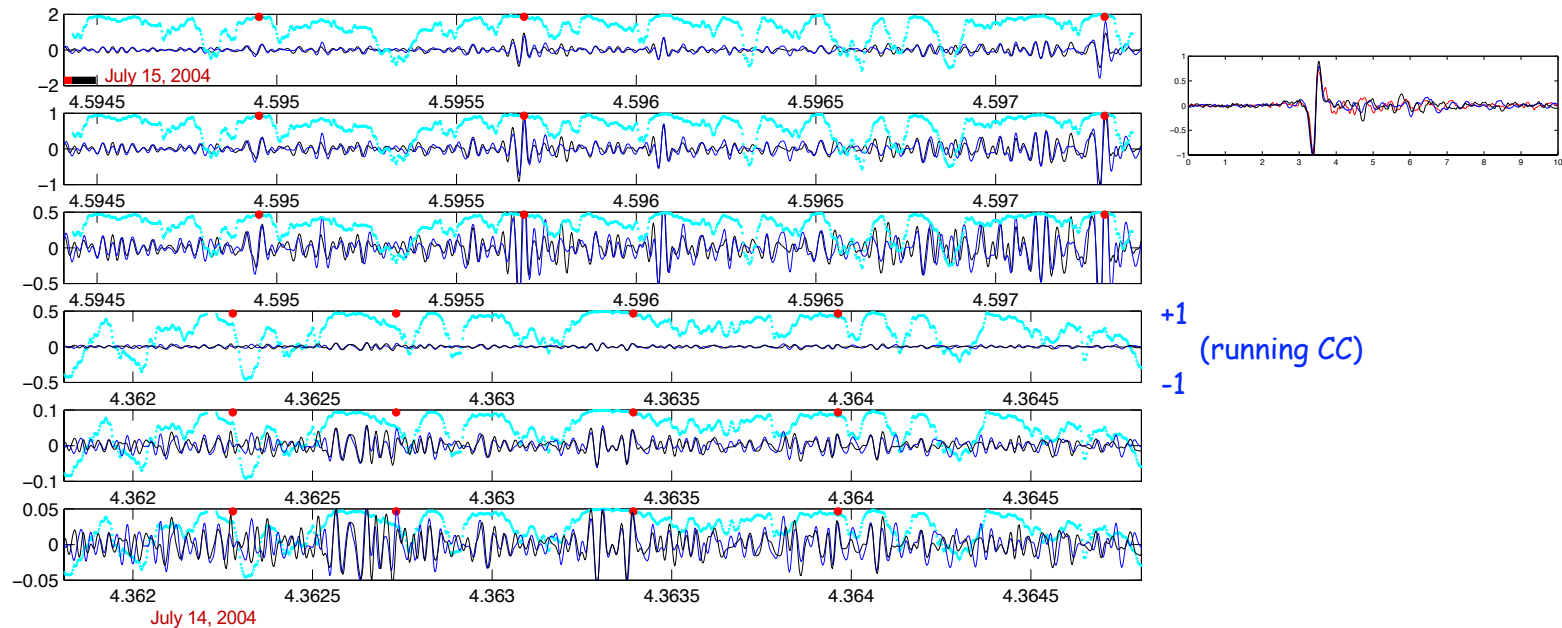
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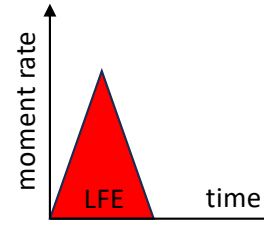
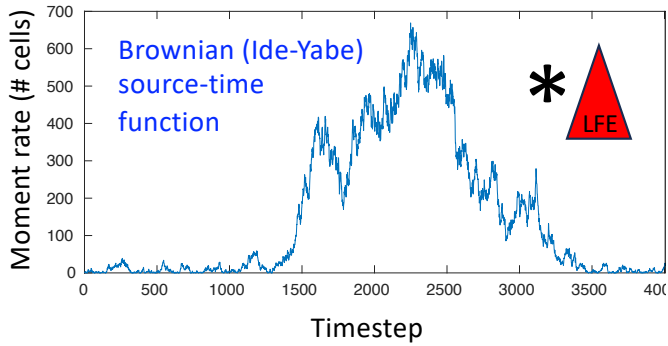


If the LFEs that make up tremor are drawn from a time-independent magnitude-frequency distribution, the tremor amplitude increases only as the square-root of the event rate.

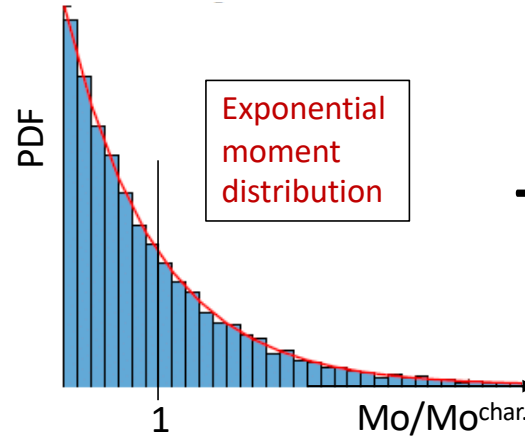
e.g., if 5 consecutive peaks at the lowest amplitude represent at least 5 LFEs, then at the largest amplitude 5 consecutive peaks represent at least 500 LFEs. We can't count them. This is built into the Ide-Yabe (2018) model.

Alternatively, 10x louder tremor could be comprised of 10x larger (in Moment) LFEs (e.g., same source duration; seismogram amplitude proportional to driving slip rate).

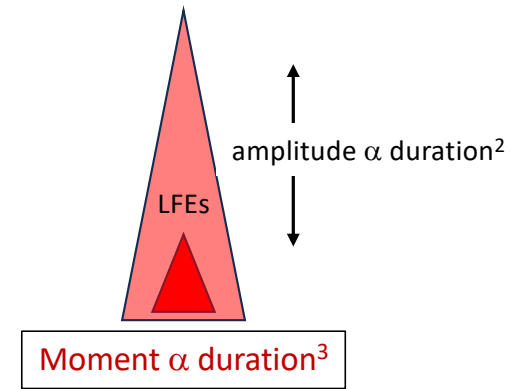
What does this mean for estimates of the moment-duration and magnitude-frequency distributions?

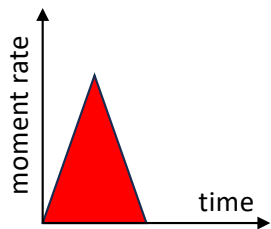


Uniform moment and duration

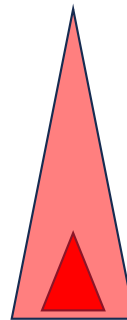


+

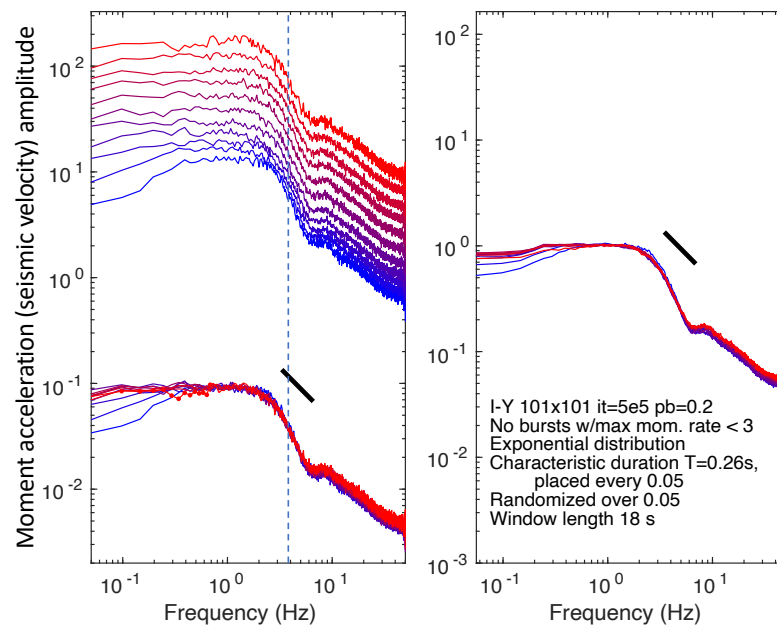
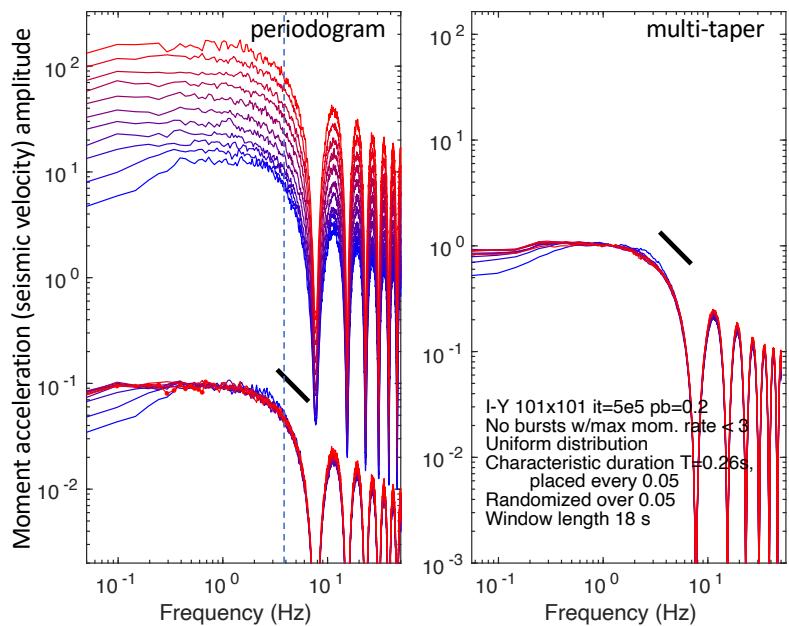
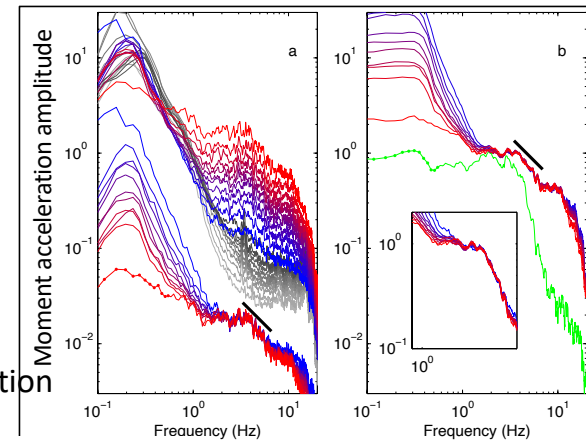




Uniform moment and duration

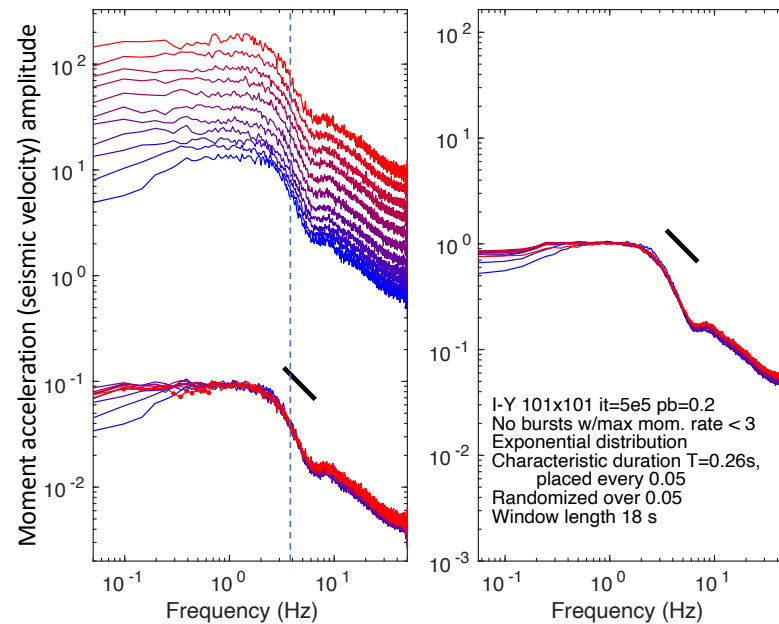
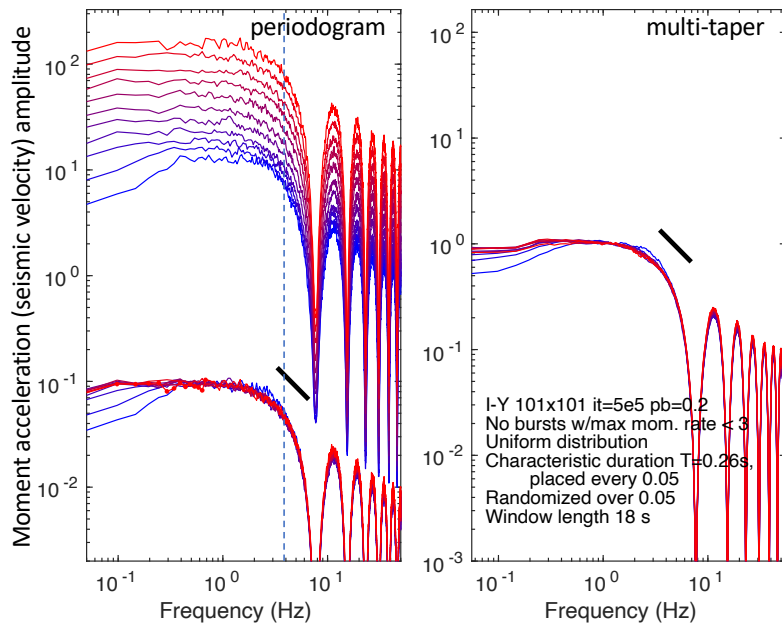
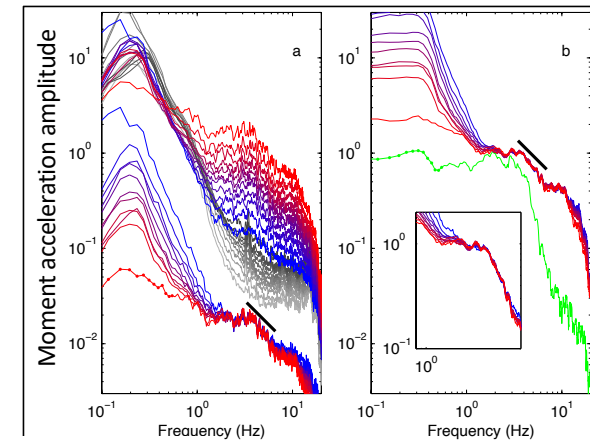


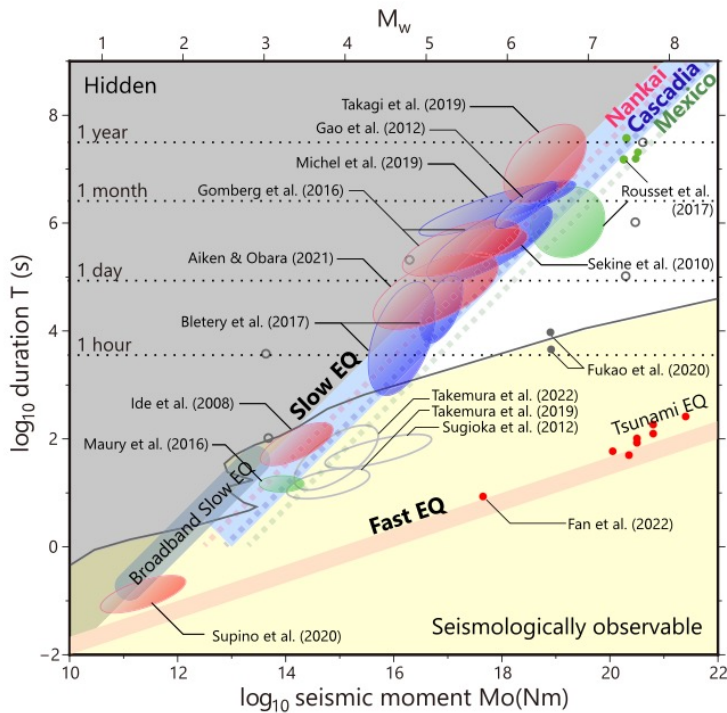
Exponential moment distribution  
 $\text{Moment} \propto \text{duration}^3$



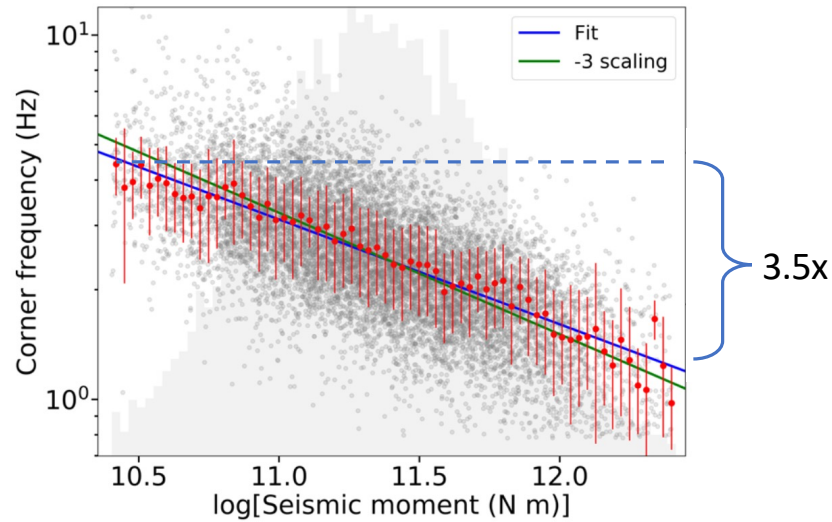
If you are drawing LFEs from a size distribution that has a well-defined average\*, and if your tremor seismogram is saturated in time, then larger tremor amplitudes do not result from larger LFEs (with possibly longer durations), they result from more frequent LFEs of the same average duration. Unlike regular earthquakes.

(\*and if, in addition, that average is not varying with time)





Ide, 2023

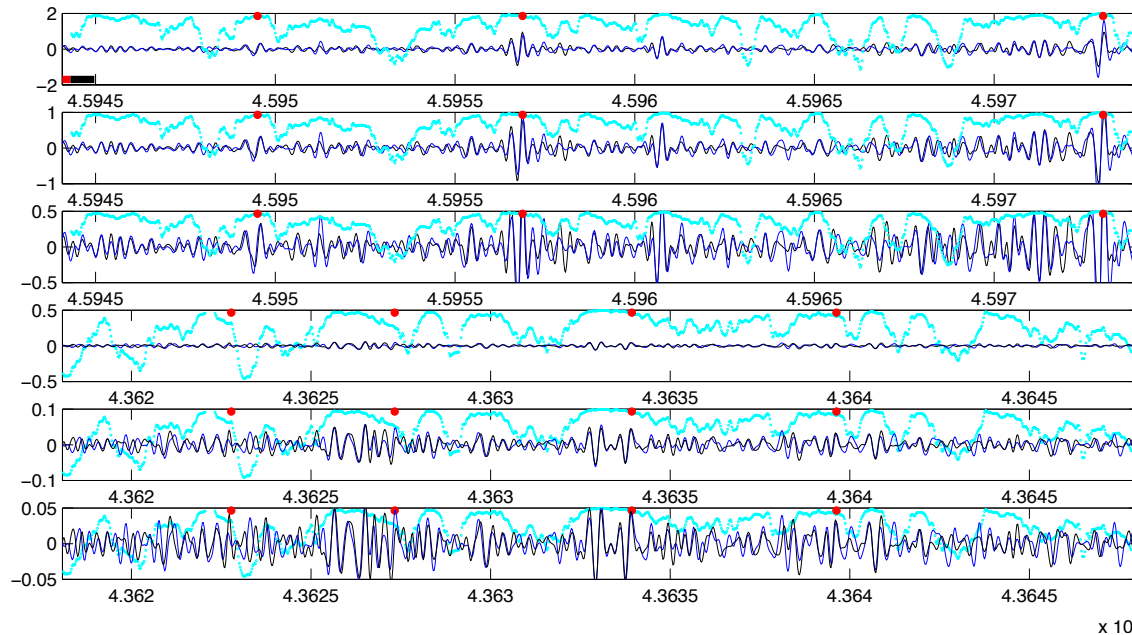


Supino et al., 2022

- Either:** Supino et al. managed to find LFEs in seismograms that were not saturated in time (but with a narrow, log-normal moment-frequency distribution, over a moment range very similar to that in Cascadia),
- Or:** Their catalog mixes saturated seismograms from regions with characteristic durations that differ by a factor of 3 to 4.



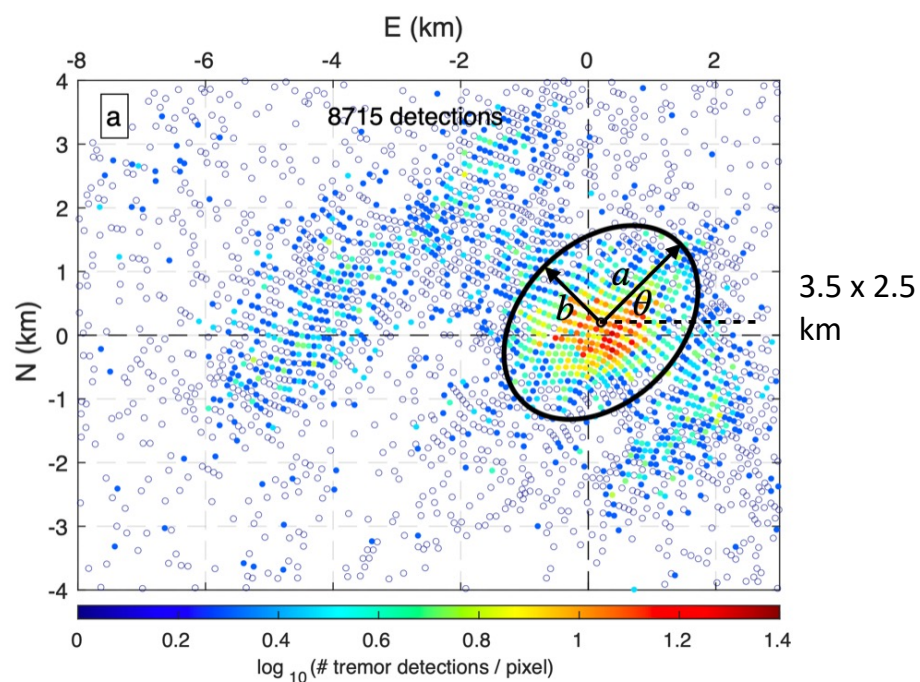
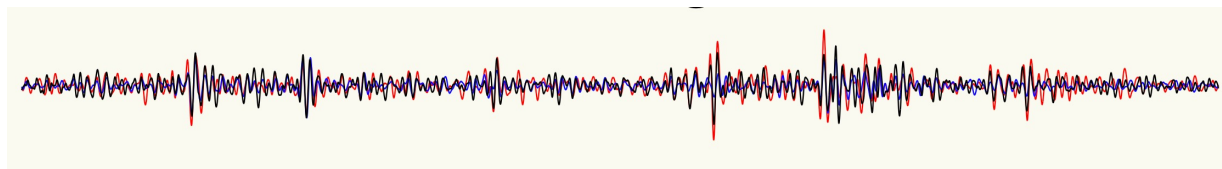
Many (many) SVI tremor seismograms are saturated.  
Are all SVI tremor seismograms saturated?



This is not a trivial question to answer, given the presence  
of noise (mostly tremor from elsewhere)

## Time-domain deconvolution (trying to locate every coherent wiggle in tremor)

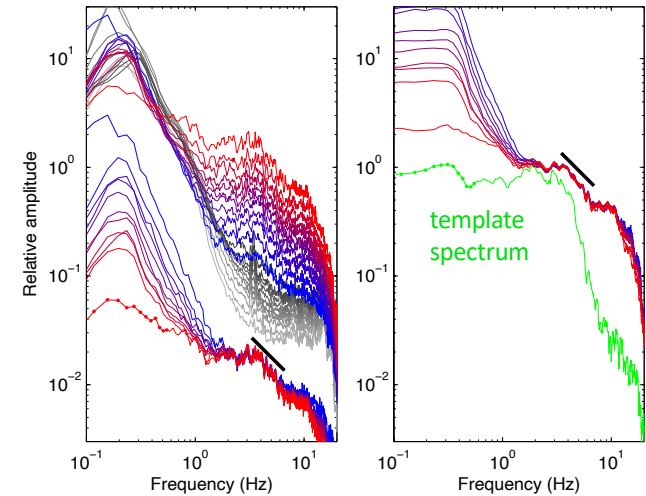
1. Identify tremor bursts in Bostock's 002 region using our 4-s catalog.
2. Cross-correlate the seismogram at each station with the template for that station.
3. Rank the resulting CC peaks at each station by their amplitude, weighted by the running CC between the stations.
4. Run the time-domain deconvolution.
5. Starting from the highest-ranked impulse at one station, find at the other two stations the nearest impulse in time to form a triplet.
6. Reject the impulse if the triplet spans too long a time.
7. Identify and remove "secondary sources".



## Conclusions

LFEs are the “quantum event” of tremor (i.e., they are more than just what we see of tremor in the narrow passband of 2-8 Hz).

Tremor has a well-defined “corner frequency” that is independent of tremor amplitude. This reflects a characteristic time scale in the source region. The simplest interpretation would be a characteristic length scale (e.g., the fault zone thickness; largest clast size; etc.) divided by a significant fraction of the shear wave speed.

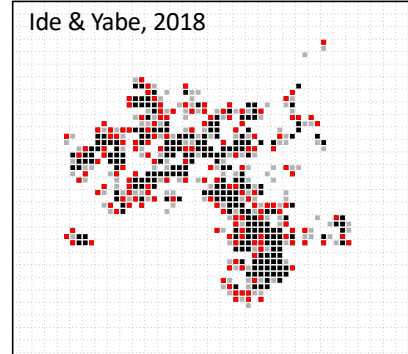
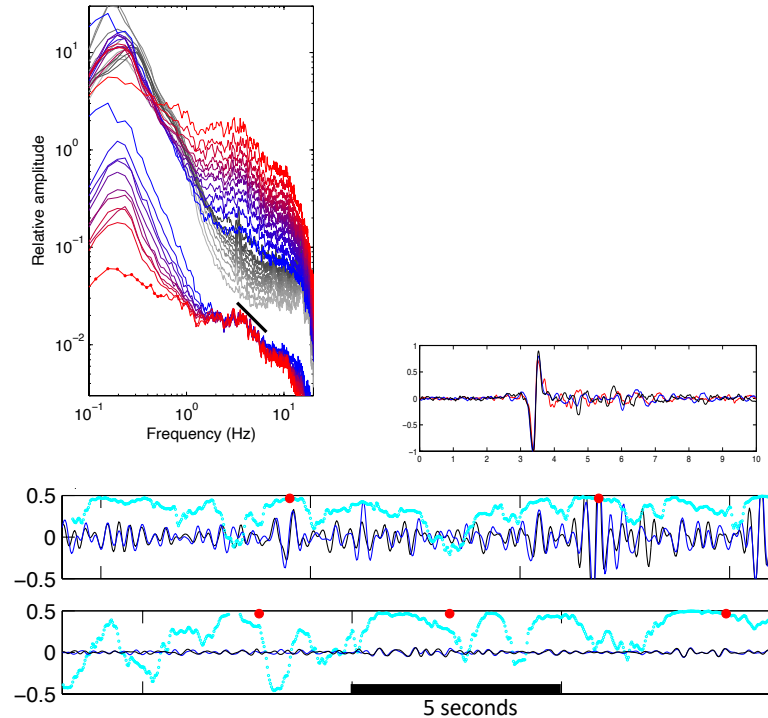


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From the loudest to the quietest, the tremor seismograms we have examined are “saturated in time”, in that the typical interval between LFE arrivals is smaller than the characteristic LFE duration. This is consistent with Ide’s stochastic model of tremor generation.



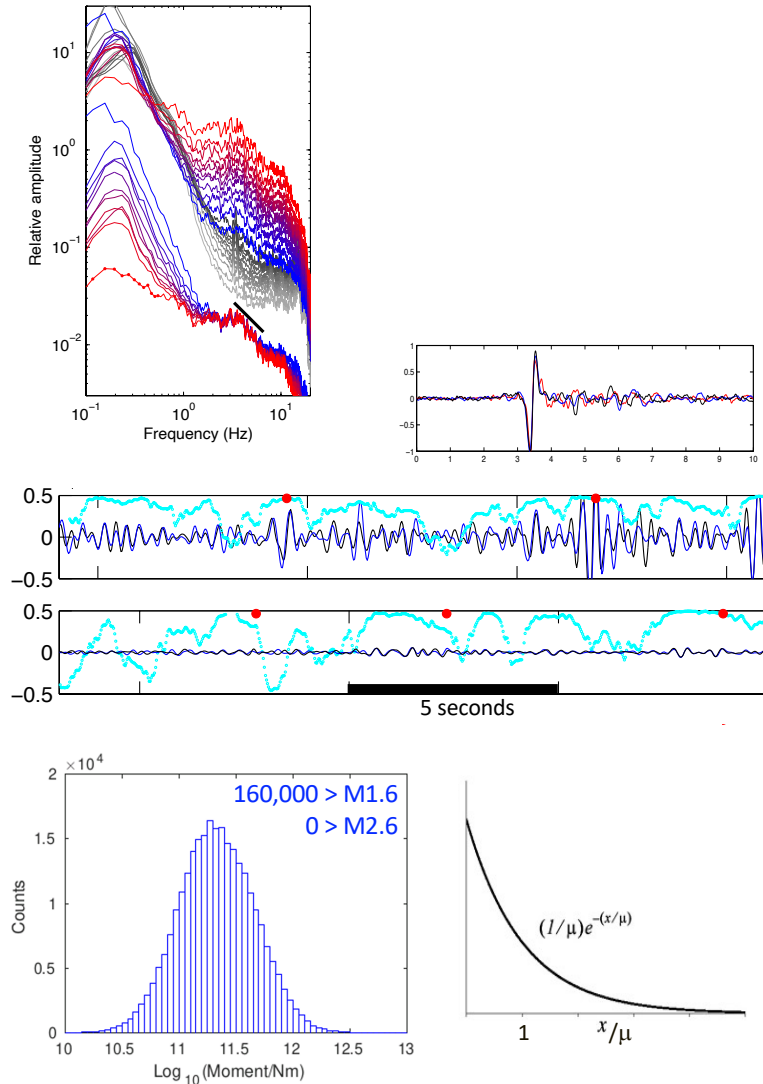
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Given a characteristic LFE size, seismograms that are saturated in time hide BOTH the underlying moment-duration distribution AND the underlying magnitude-frequency distribution of the LFEs that make up tremor. Assuming that LFE moment varies as duration<sup>3</sup> provides a possible mechanism for reconciling the observations of Supino and Bostock/Farge.

