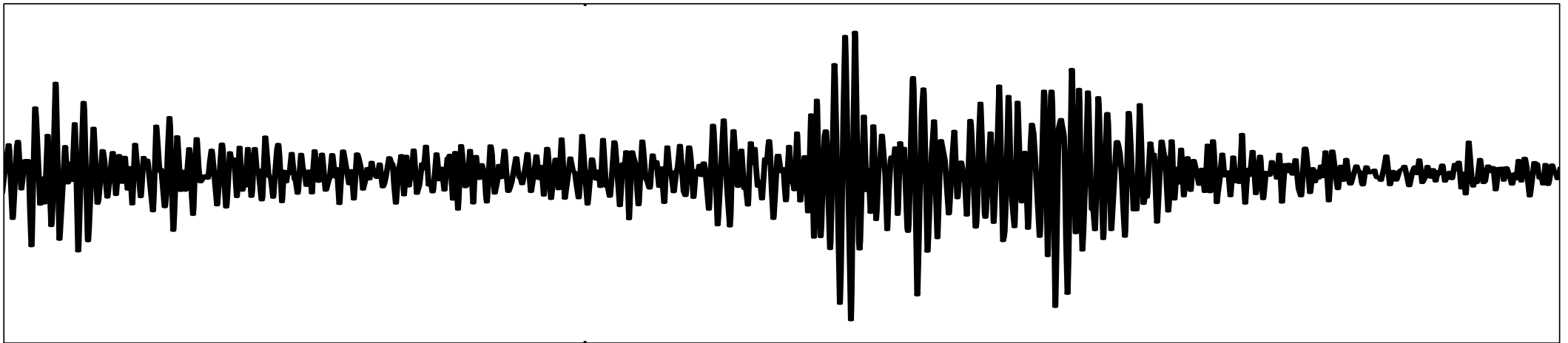


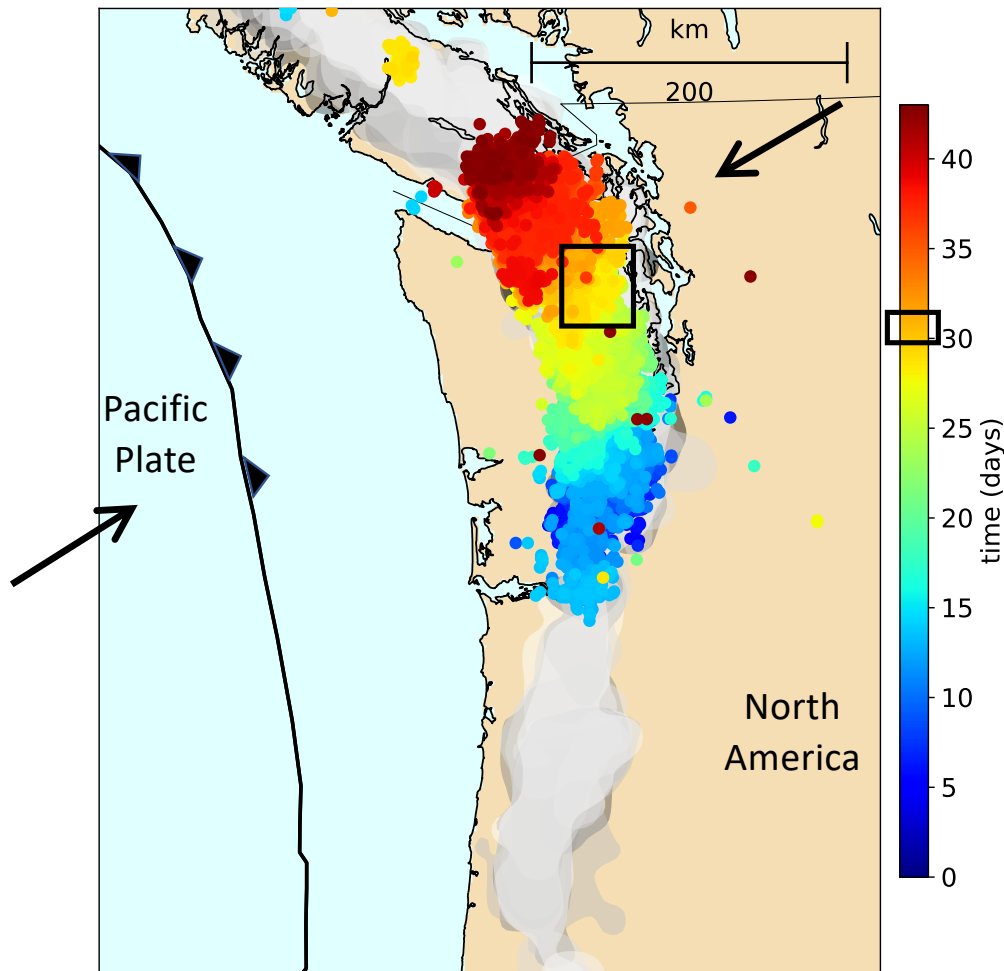
# Probing the properties of seismic tremor

Jessica Hawthorne (Oxford)



10 sec

# Tremor: tracked in real time



Houston et al, 2011;  
Obara et al, 2010

Wech et al, 2009

Millions of tiny earthquakes: LFEs

Ideally, want to

- Use them to learn about subduction
- Use them to learn about hazard

But first, need to

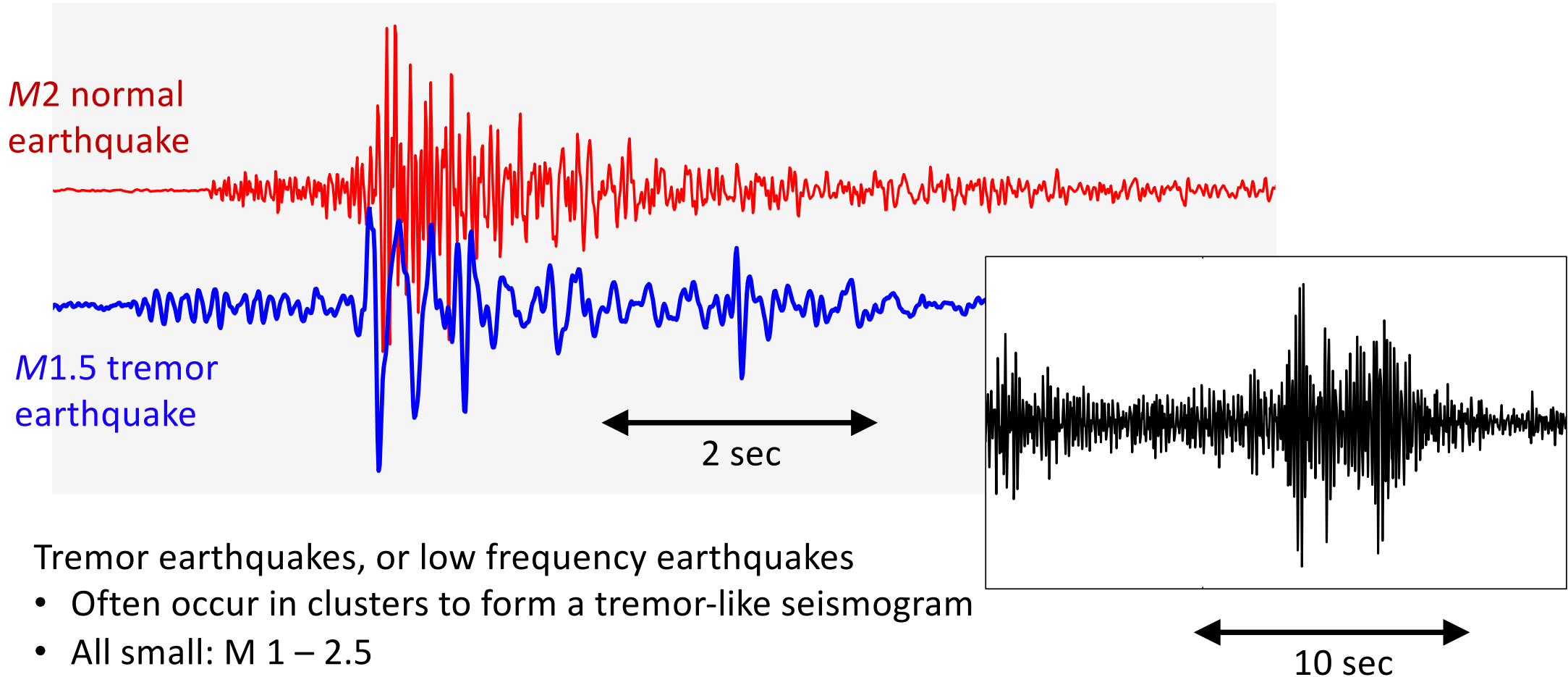
- Understand what LFEs are: why they're slow

*Tremor was first observed >20 years ago*

Obara, 2002

- *Why don't we know what it is yet?*

# Tremor: composed of numerous overlapping low frequency earthquakes



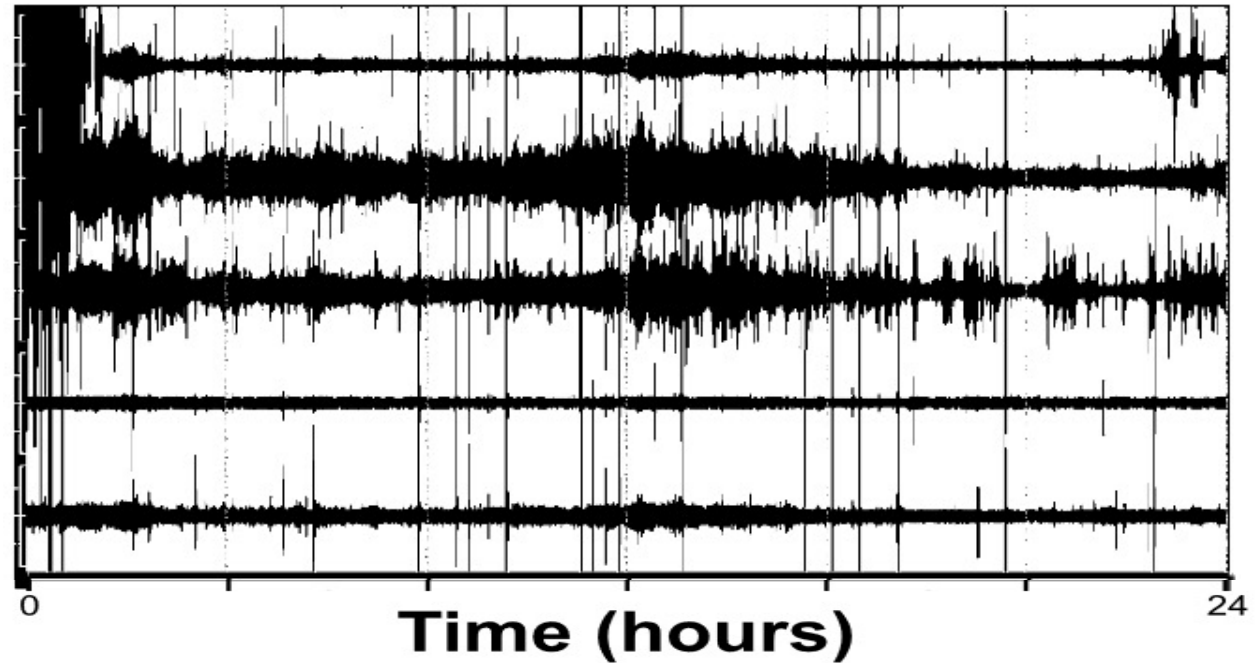
Tremor earthquakes, or low frequency earthquakes

- Often occur in clusters to form a tremor-like seismogram
- All small: M 1 – 2.5
- May be part of a spectrum of slow earthquakes

# Outline

- Detecting and locating tremor
  - Envelopes
  - LFEs
  - Inter-station
  - Coherence
- Tremor energy
- LFE moment and duration
- LFE rupture extent
- More moment-duration scaling
- Focal mechanisms

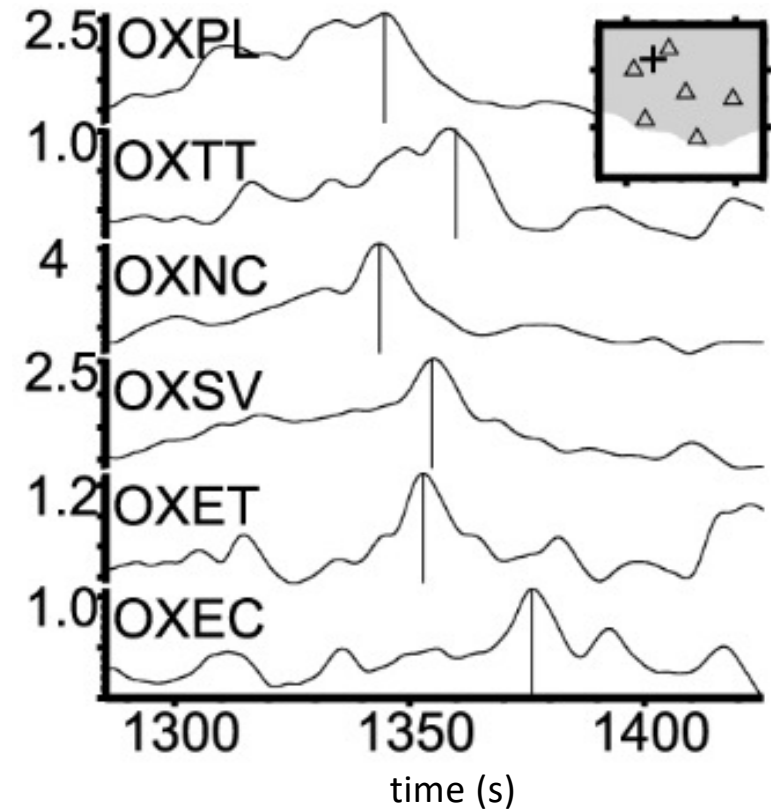
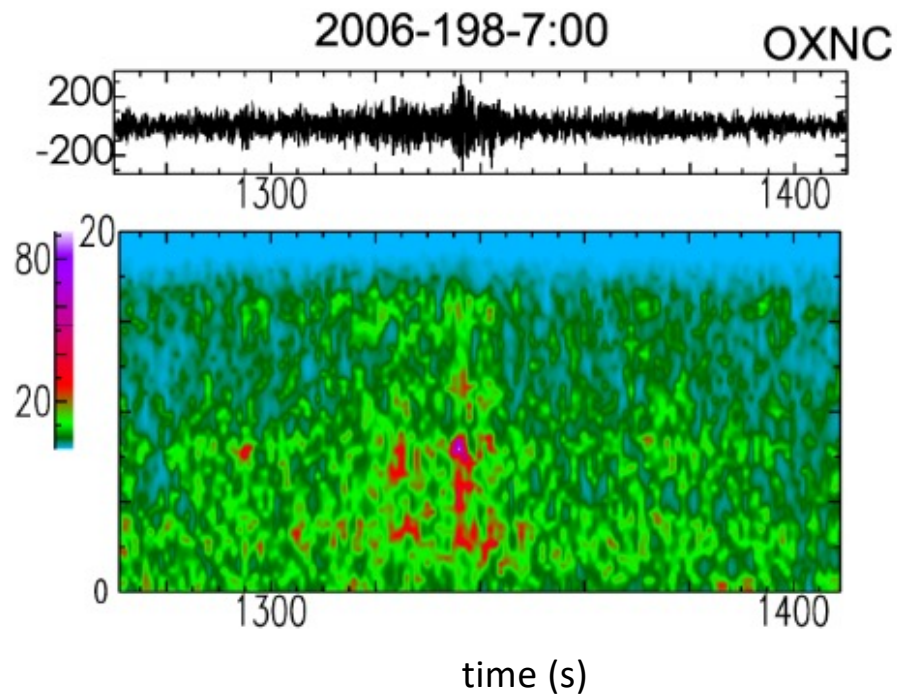
Tremor in Oaxaca, Mexico



Brudzinski et al, 2010

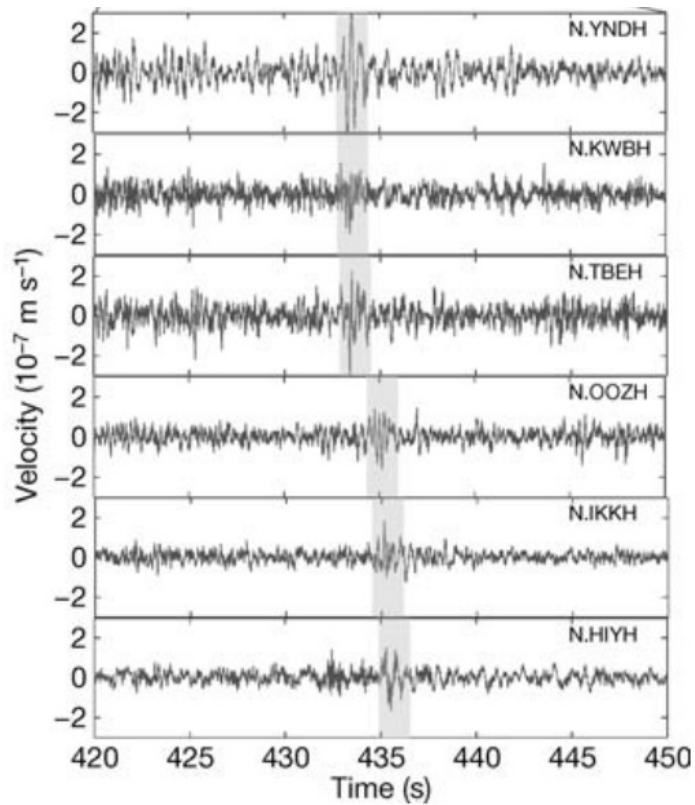
*Motivation: Must understand the nuances of the observations in order to develop (1) testable models and (2) new tests of the models.*

# Envelope correlation

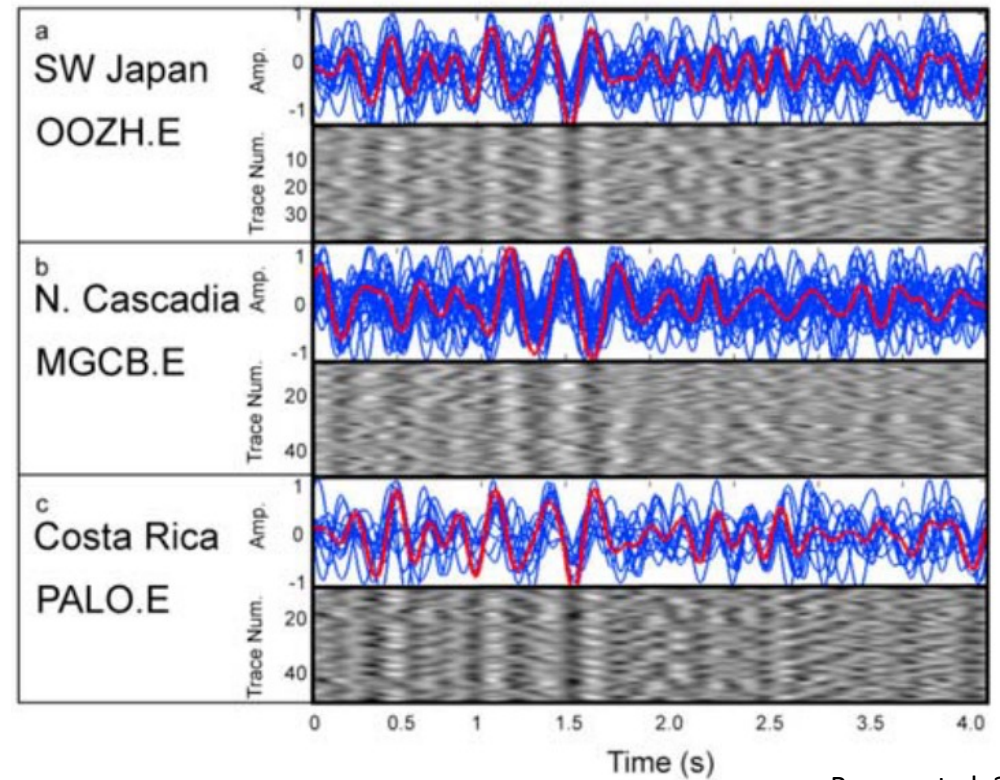


Compute envelope of bandpassed filtered seismograms (here 2-5 Hz).  
Find location required to align envelopes at all stations.

# Low frequency earthquake (LFE) matching



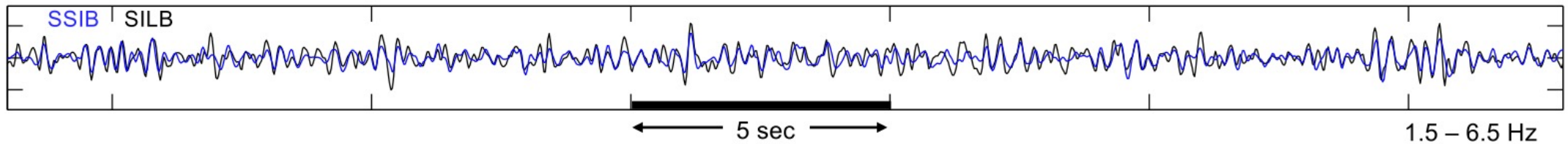
Shelly et al, 2006



Brown et al, 2009

Identify individual LFEs within seismograms and search for more.  
Stack, then search again.

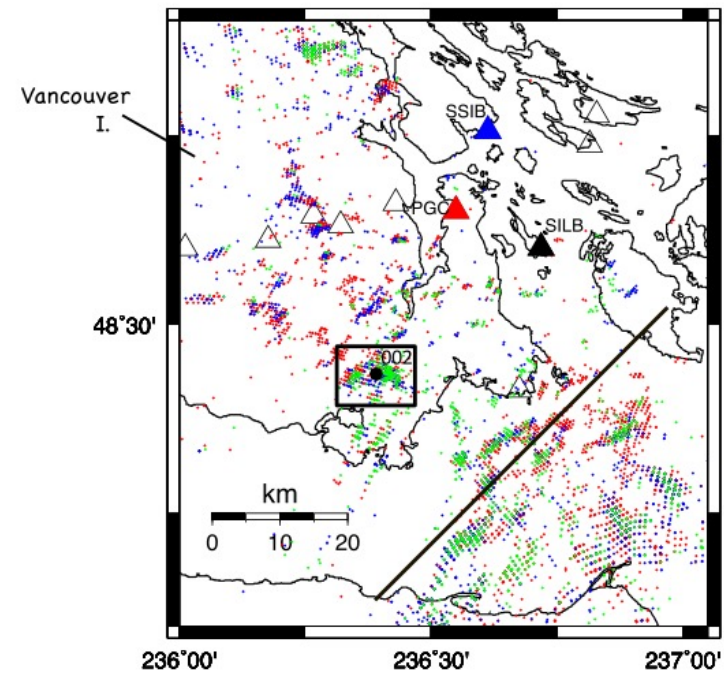
# Cross-station comparison



- Identify intervals with similar signals at several stations
- Determine time shifts and location for each interval

*Some highly tremorigenic patches*

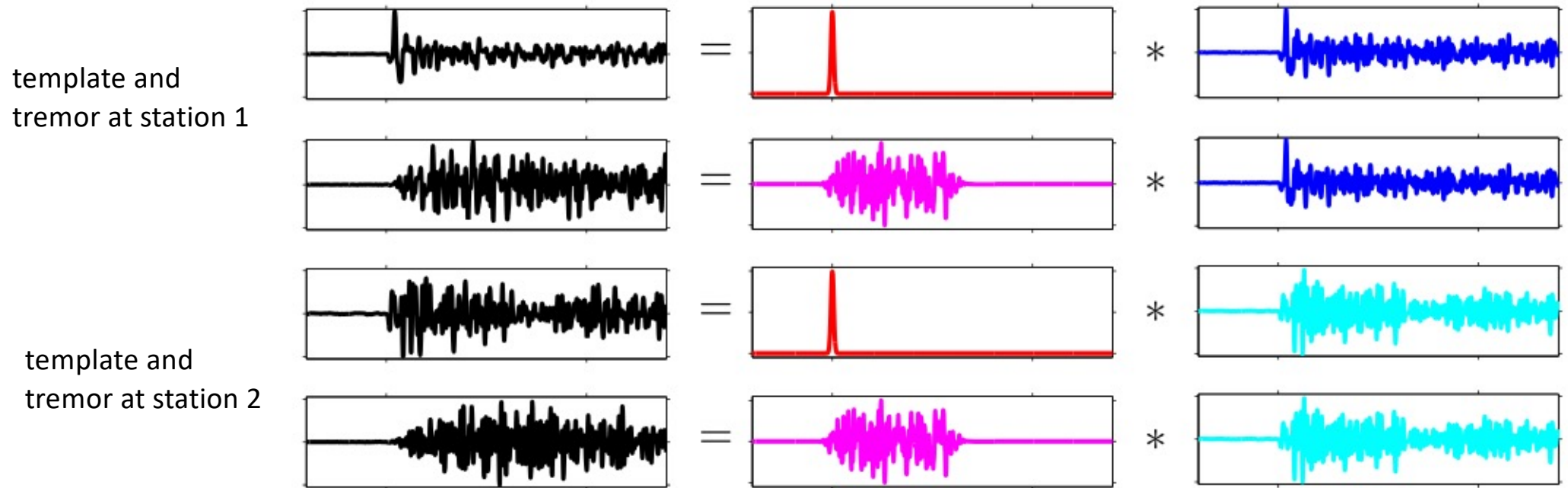
Sept 2005 + July 2004 + March 2003



Armbruster et al, 2014

# Inter-station coherence

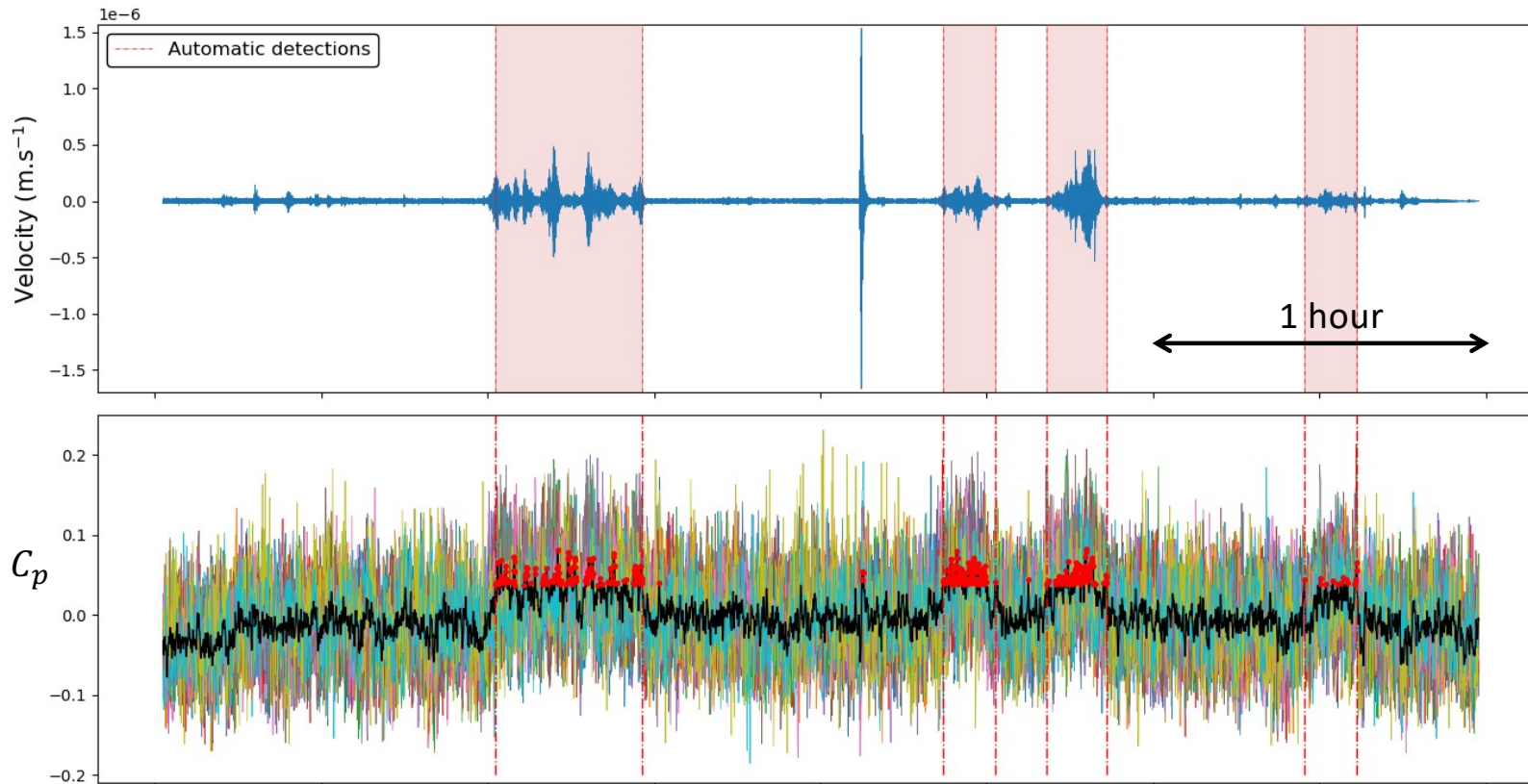
- Compare with a **template** Green's function, as in LFE matching
- But also compare between stations, to compare tremor source time functions



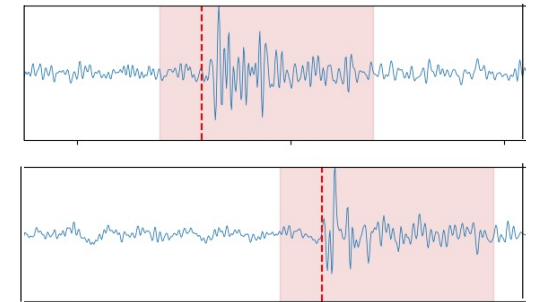
4 observations, 4 unknowns  $\rightarrow$  can identify signals from the same source



# Few-minute tremor bursts offshore Costa Rica



Identify the tremor times using  
local earthquakes as templates.



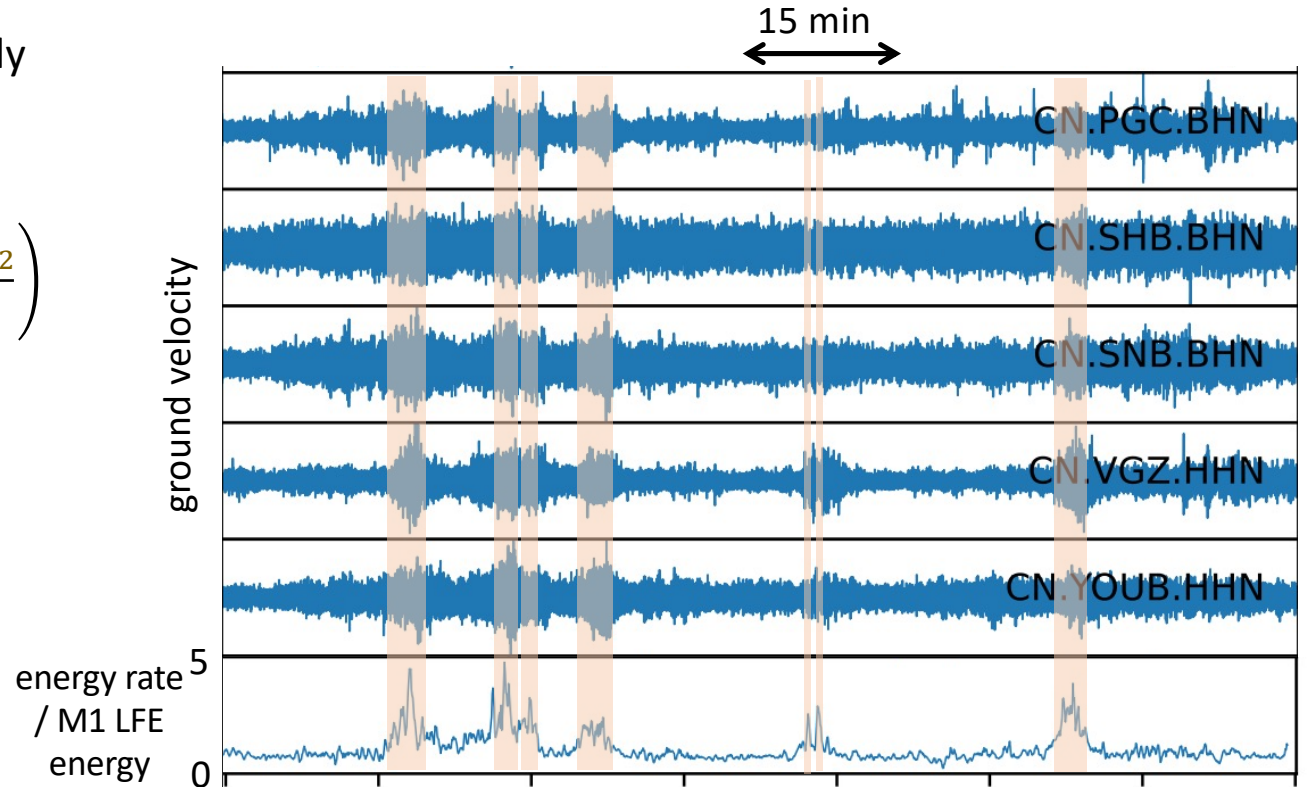
by Julien Renou

$$C_p = \text{Re} \left( \frac{\hat{d}_{\text{template, component 1}} \hat{d}_{\text{tremor, component 1}}^* \hat{d}_{\text{template, component 2}} \hat{d}_{\text{tremor, component 2}}^*}{|\hat{d}_{\text{template, component 1}} \hat{d}_{\text{tremor, component 1}}^* \hat{d}_{\text{template, component 2}} \hat{d}_{\text{tremor, component 2}}^*|} \right)$$

# Tremor energy

Similar approach to coherence, but only normalize by the template

$$\begin{aligned} E_c &= \operatorname{Re} \left( \frac{\hat{d}_{temp,1} \hat{d}_{trem,1}^* \hat{d}_{temp,2} \hat{d}_{trem,2}^*}{|\hat{d}_{temp,1} \hat{d}_{temp,2}|^2} \right) \\ &= \operatorname{Re} \left( \frac{|\hat{s}_{trem,1}^* \hat{s}_{trem,2}^*|}{|\hat{s}_{temp,1} \hat{s}_{temp,2}|} \right) \\ &= \operatorname{Re} \left( \frac{|\hat{s}_{trem,1}^*|^2}{|\hat{s}_{temp,1}|^2} \right) \end{aligned}$$

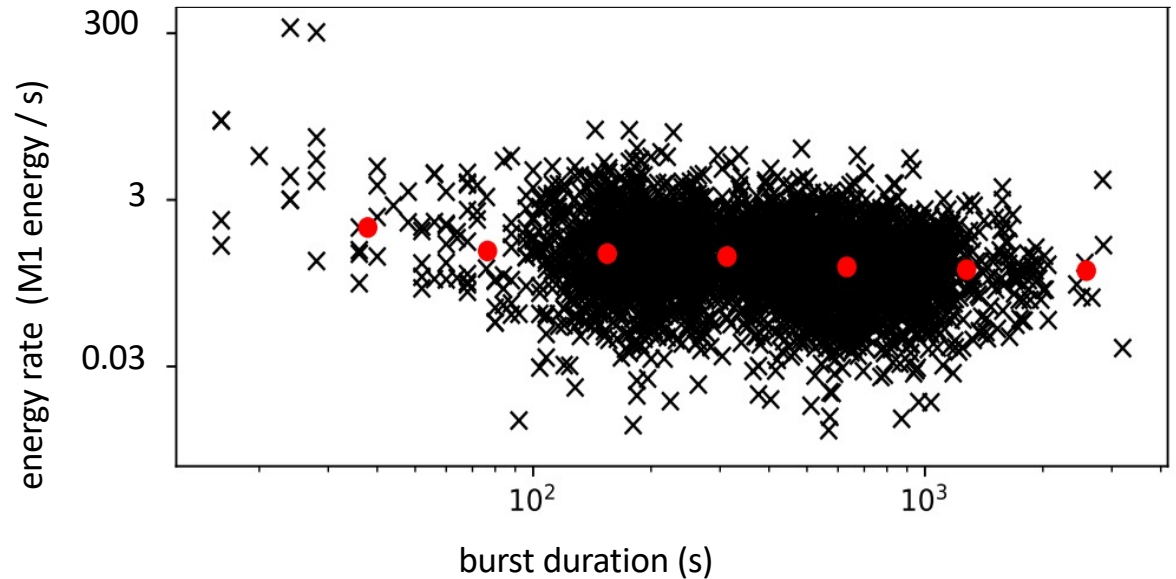


Bottom panel: Seismic energy per second, coming from within 10-20 km of a template, Divided by energy in a M1 LFE

# Tremor energy

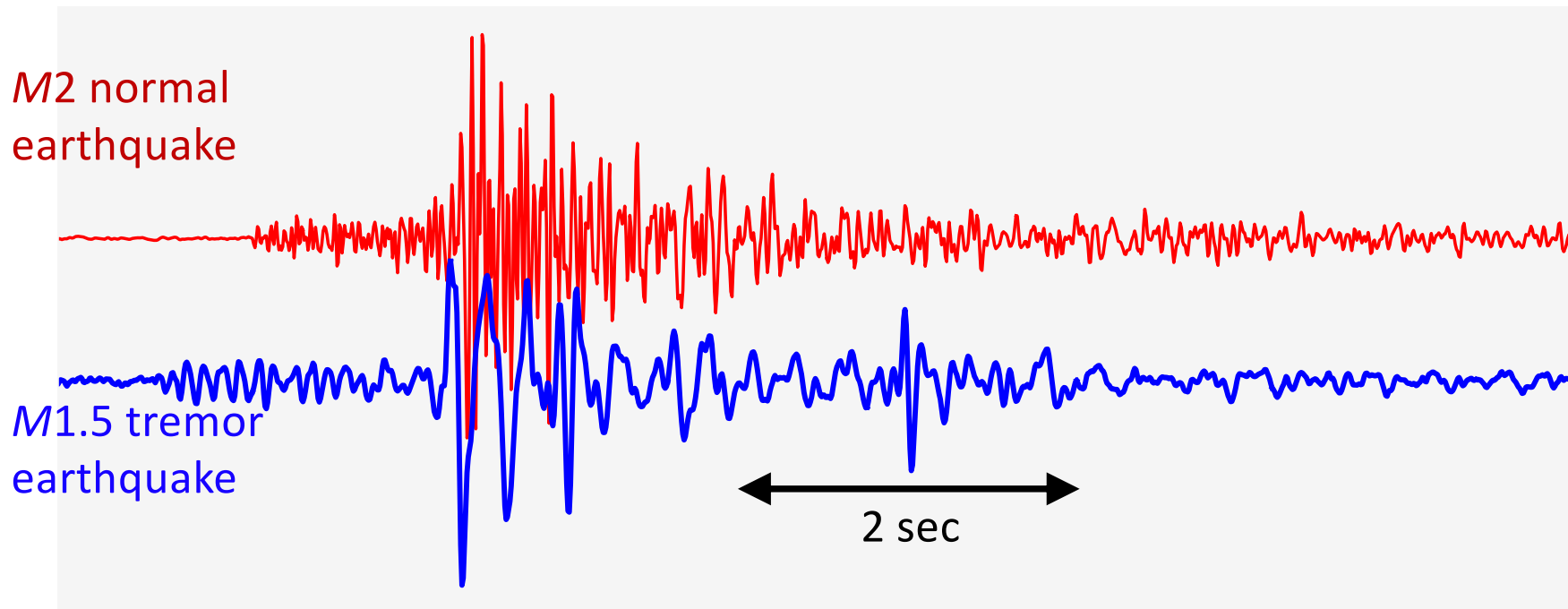
Similar approach to coherence, but only normalize by the template

$$\begin{aligned} E_c &= \operatorname{Re} \left( \frac{\hat{d}_{temp,1} \hat{d}_{trem,1}^* \hat{d}_{temp,2} \hat{d}_{trem,2}^*}{|\hat{d}_{temp,1} \hat{d}_{temp,2}|^2} \right) \\ &= \operatorname{Re} \left( \frac{|\hat{s}_{trem,1}^* \hat{s}_{trem,2}^*|}{|\hat{s}_{temp,1} \hat{s}_{temp,2}|} \right) \\ &= \operatorname{Re} \left( \frac{|\hat{s}_{trem,1}^*|^2}{|\hat{s}_{temp,1}|^2} \right) \end{aligned}$$



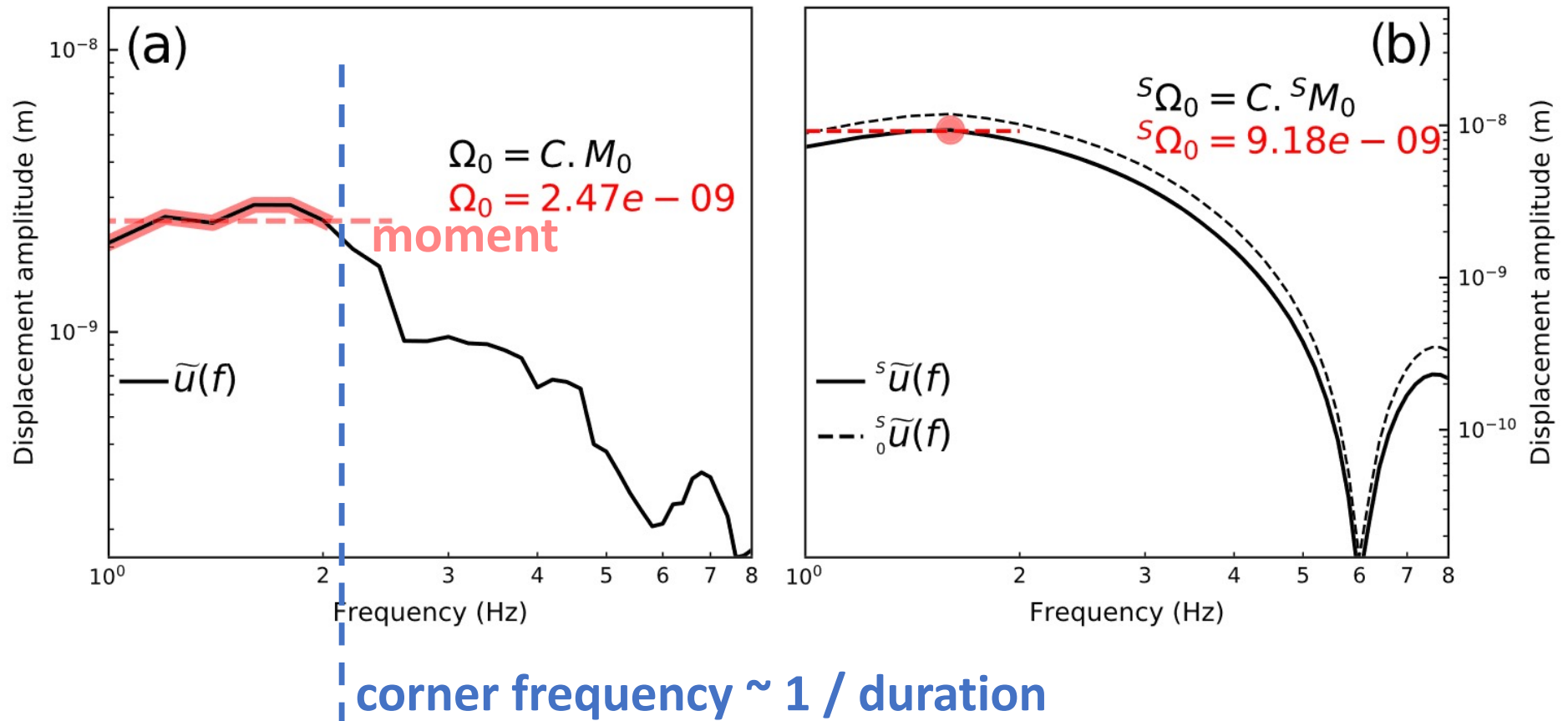
- Estimate coherent energy in thousands of few-minute tremor bursts
- If we assume that tremor is composed mostly of M1 LFEs, appear to be about 0.5 LFEs per second
- *Only a few percent of the moment in few-minute slow earthquakes is seismic*

# LFE durations and moments

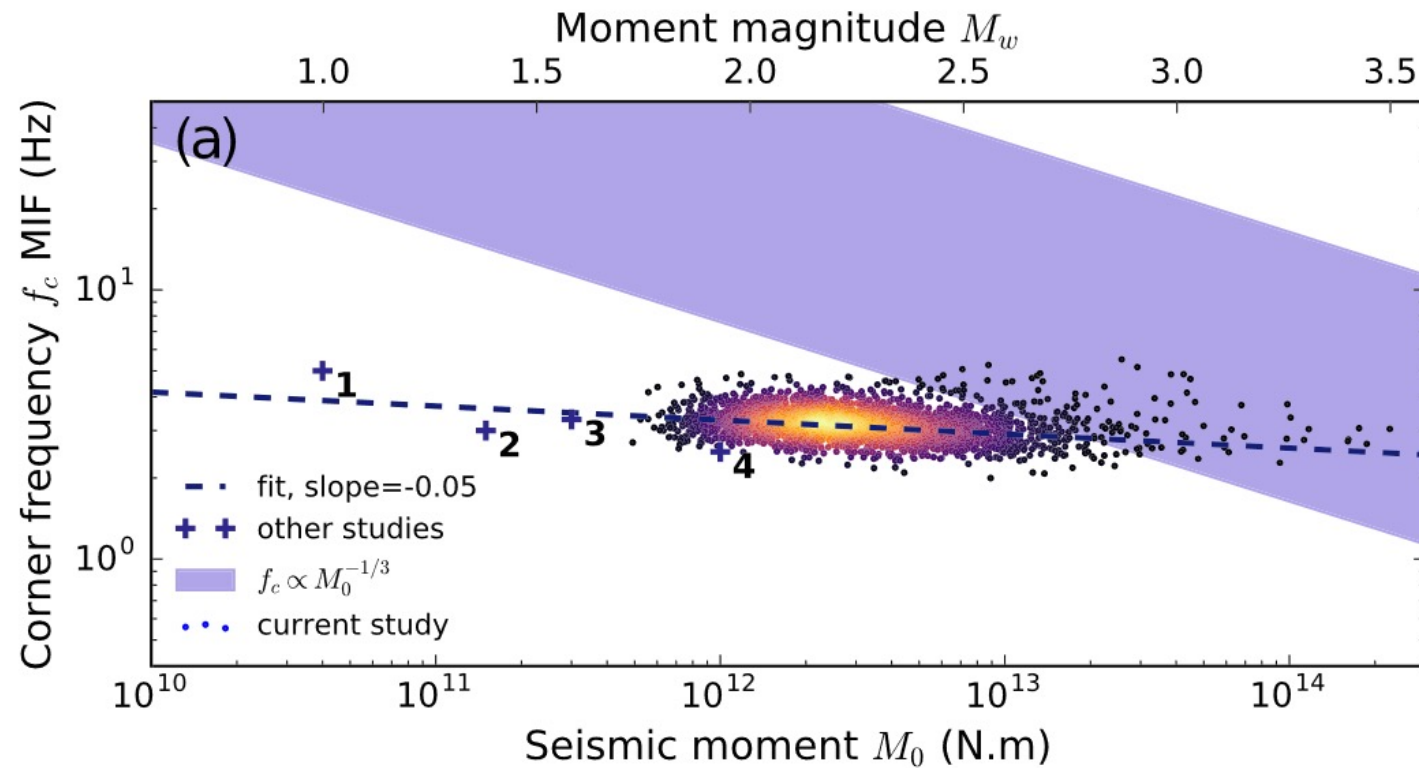


Which event lasts longer?

# Moments and durations from spectra



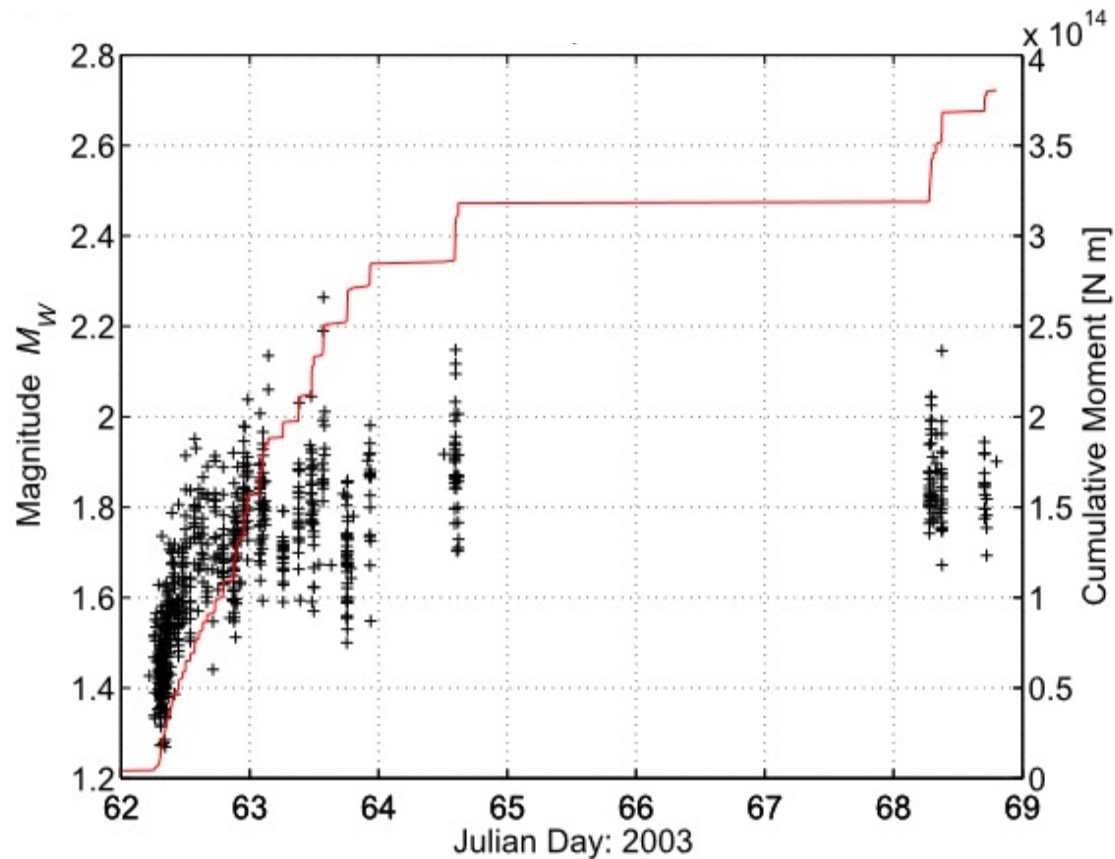
# Moments and durations from spectra



Moment is independent of duration?

→ Tremor has a characteristic duration

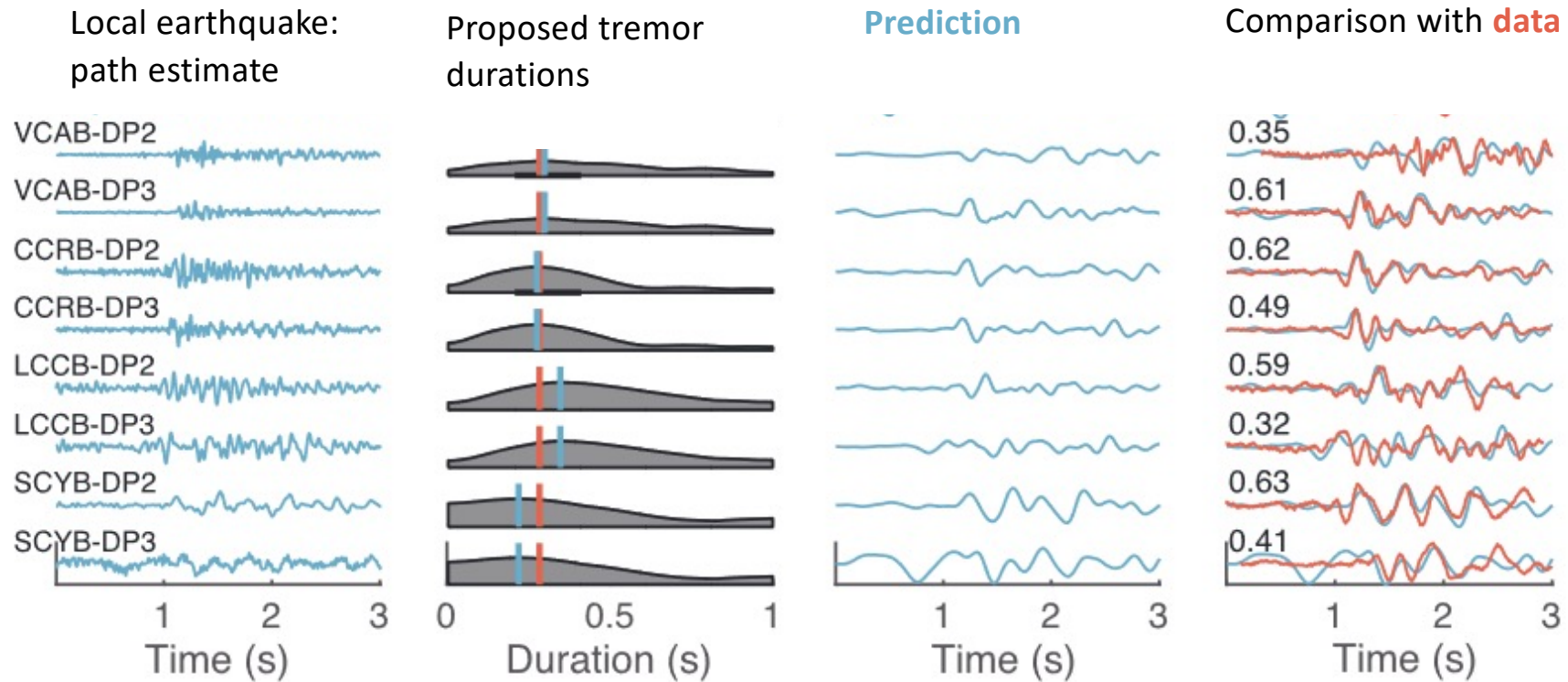
# LFE moments through time



Moments at one location through time

- Start small
  - But increase as the main front moves farther ahead
- A change in smoothness or permeability through time?

# Durations from grid search with path effect corrections

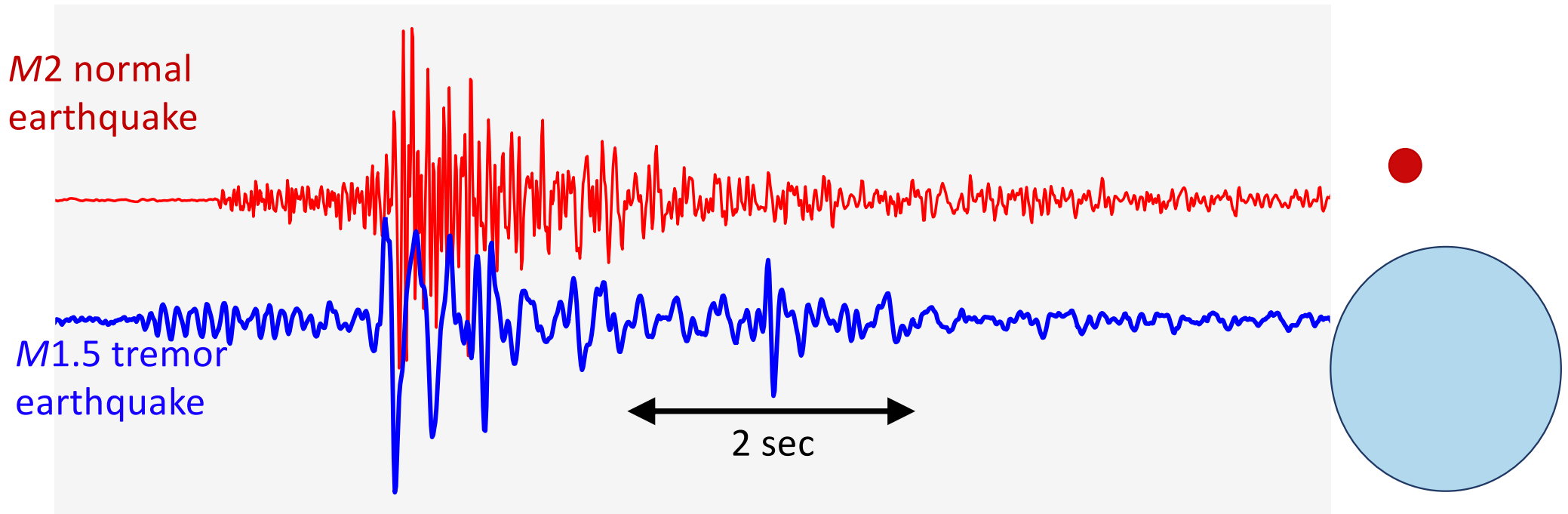


- Use a local earthquake as an estimate of the path effect
- Convolve with proposed source time functions
- Determine which one matches the data

*Best-fitting duration here and elsewhere: 0.2 – 0.5 s*



# LFE spatial extents and rupture speeds

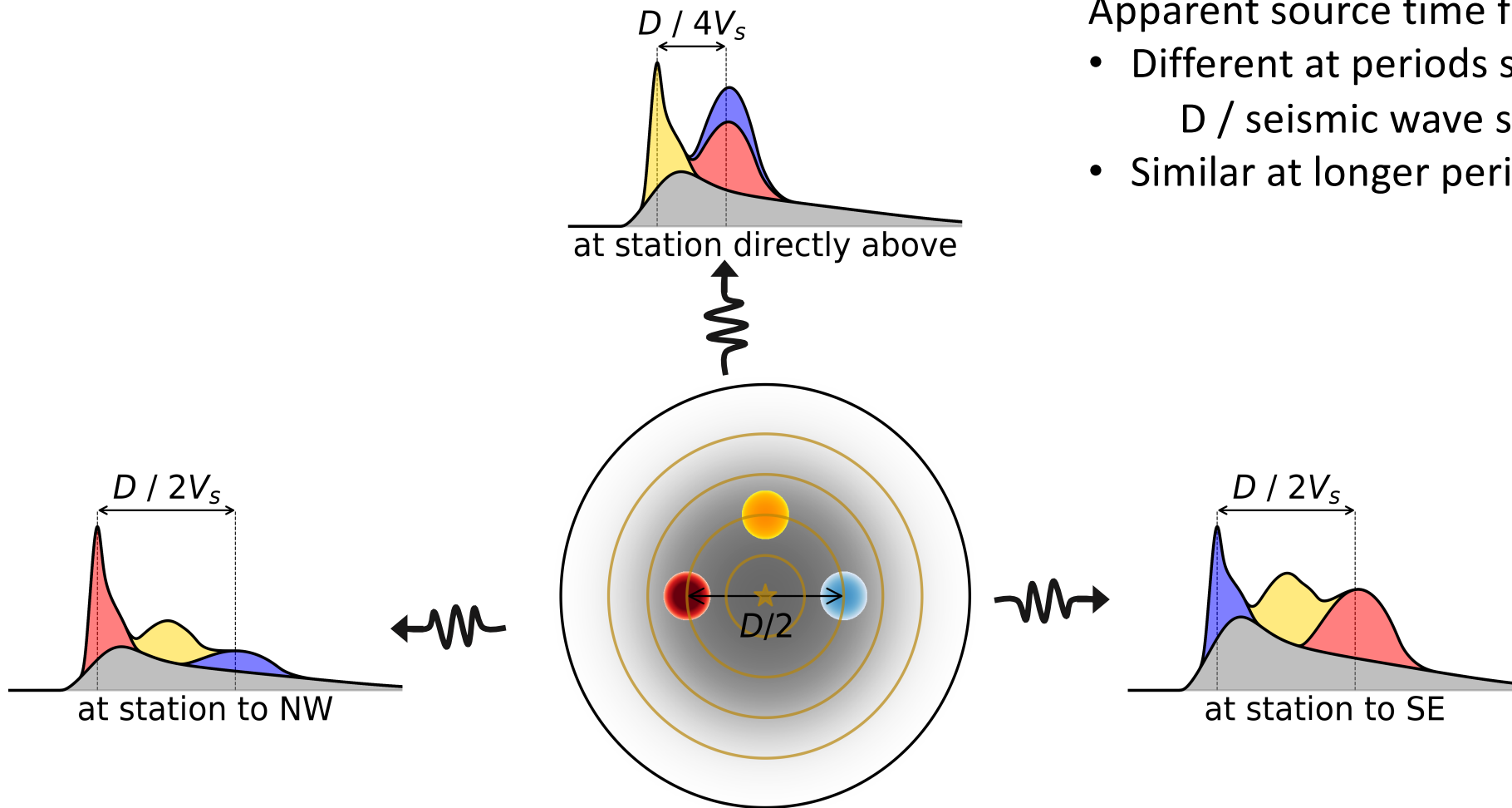


Tremor's earthquakes are long, and create low frequency signals

But are we sure they're slow? Maybe the slip is just spread out.

- Ruptures limited by seismic wave radiation propagate at near shear wave speeds.
- Rupture duration = Width / Propagation speed

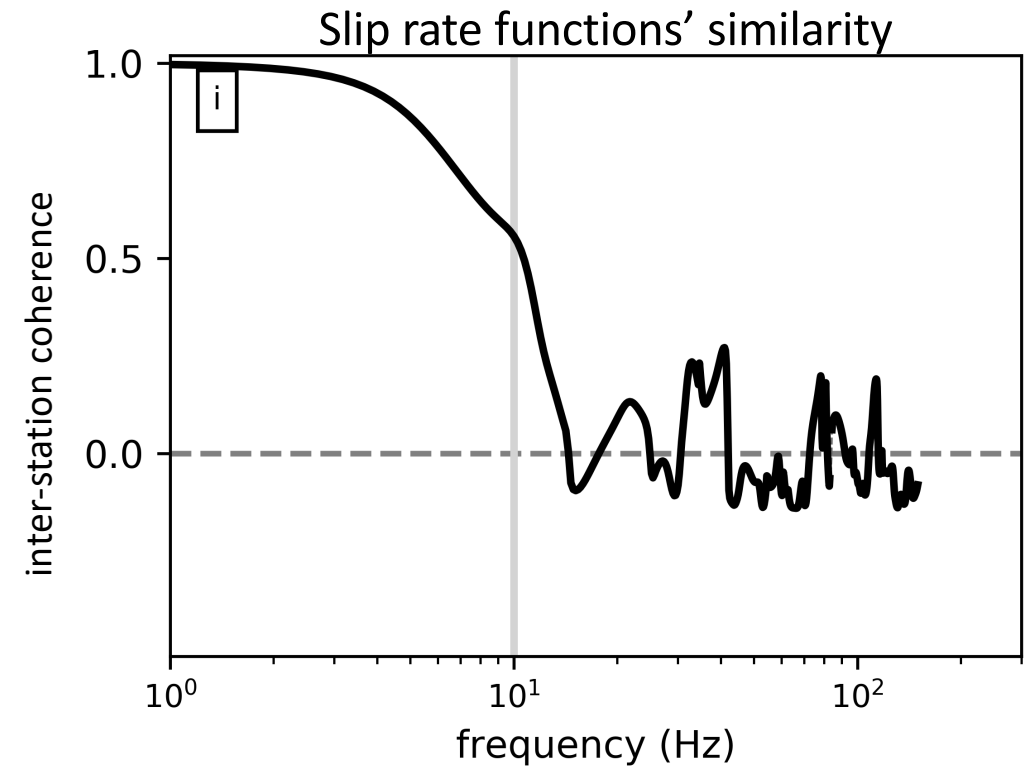
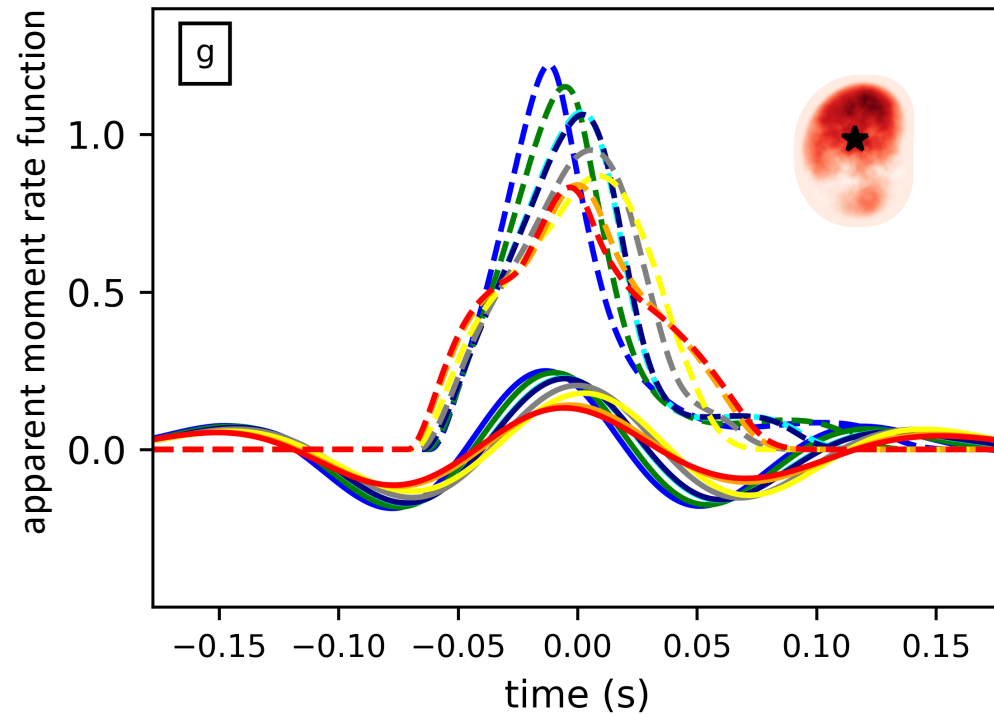
To measure the width, look for inter-station differences



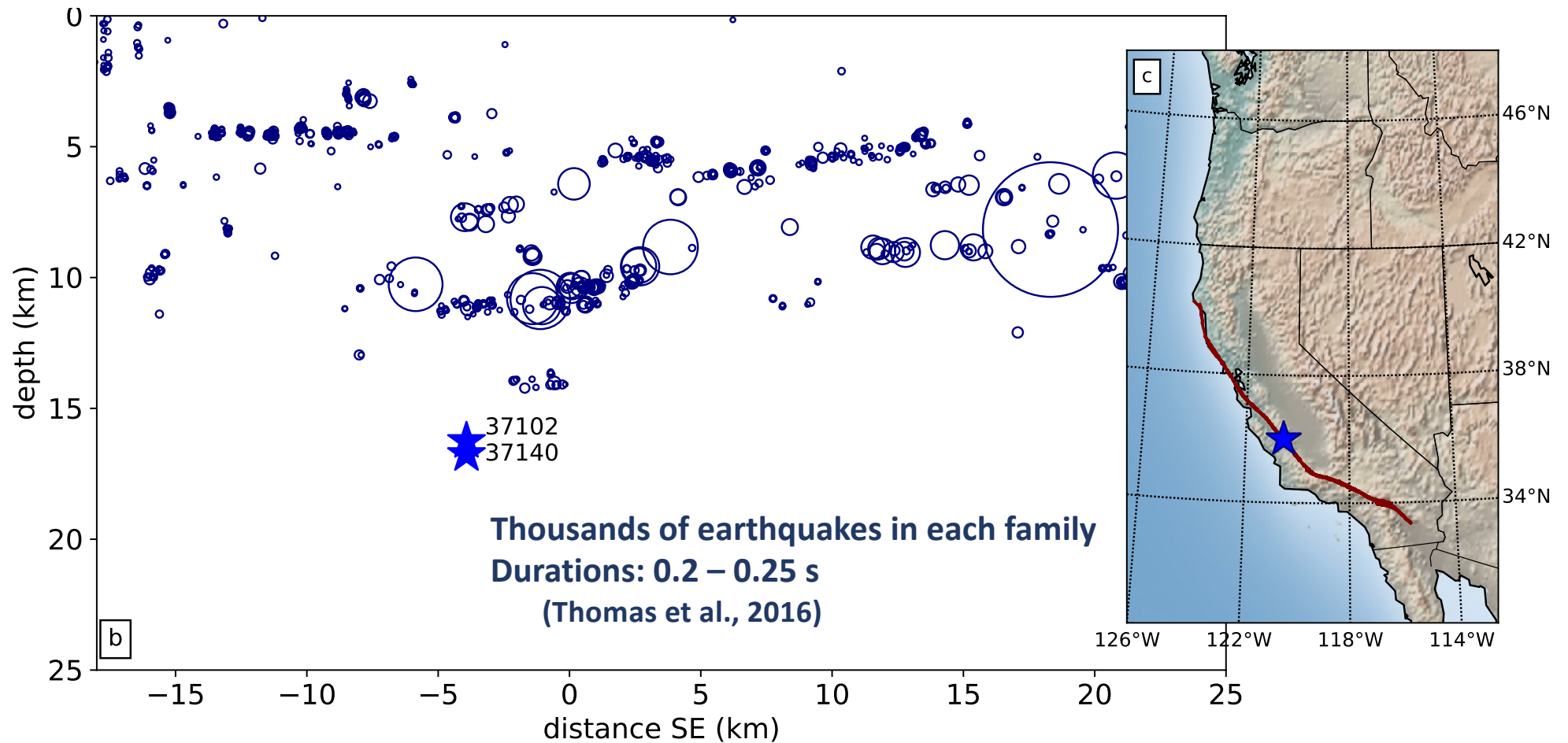
- Apparent source time functions  $s_k$
- Different at periods shorter than  $D / \text{seismic wave speed}$
  - Similar at longer periods

# Synthetics for a 600-m wide earthquake

Apparent slip rate functions recorded at 7 stations, as shifted to account for source-station travel times



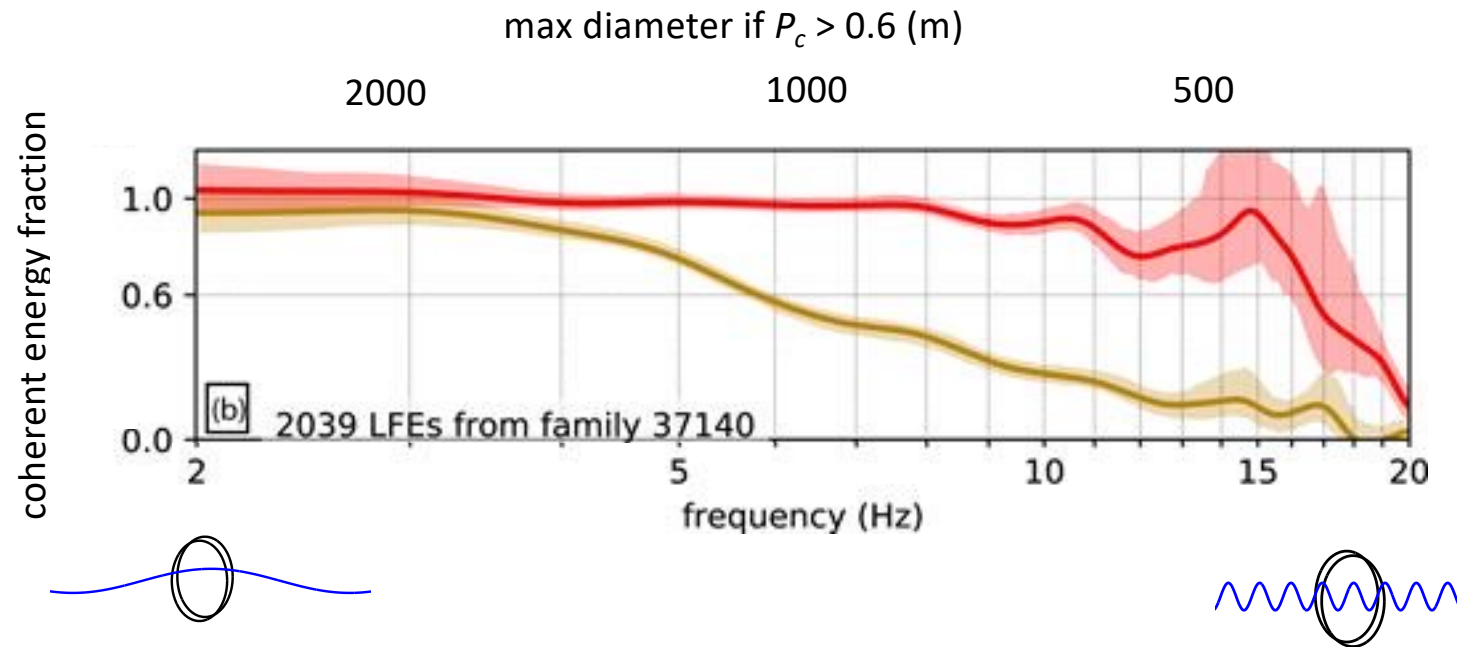
# Tremor earthquakes near Parkfield, CA



# Coherent energy in one LFE family

Similar energy calculation to that used previously, compared with total energy

Most energy at frequencies less than 15 Hz is coherent across stations (red)  
→ Diameter < 400 m



Combine with duration  $\approx 0.2$  s (Thomas et al, 2016)

→ Rupture speed < 0.6 (400 m) / (0.2 s) = 1200 m/s  $\lesssim 0.3 \times$  shear wave speed

→ Tremor less limited by seismic wave radiation than most earthquakes?

# LFE and tremor properties so far

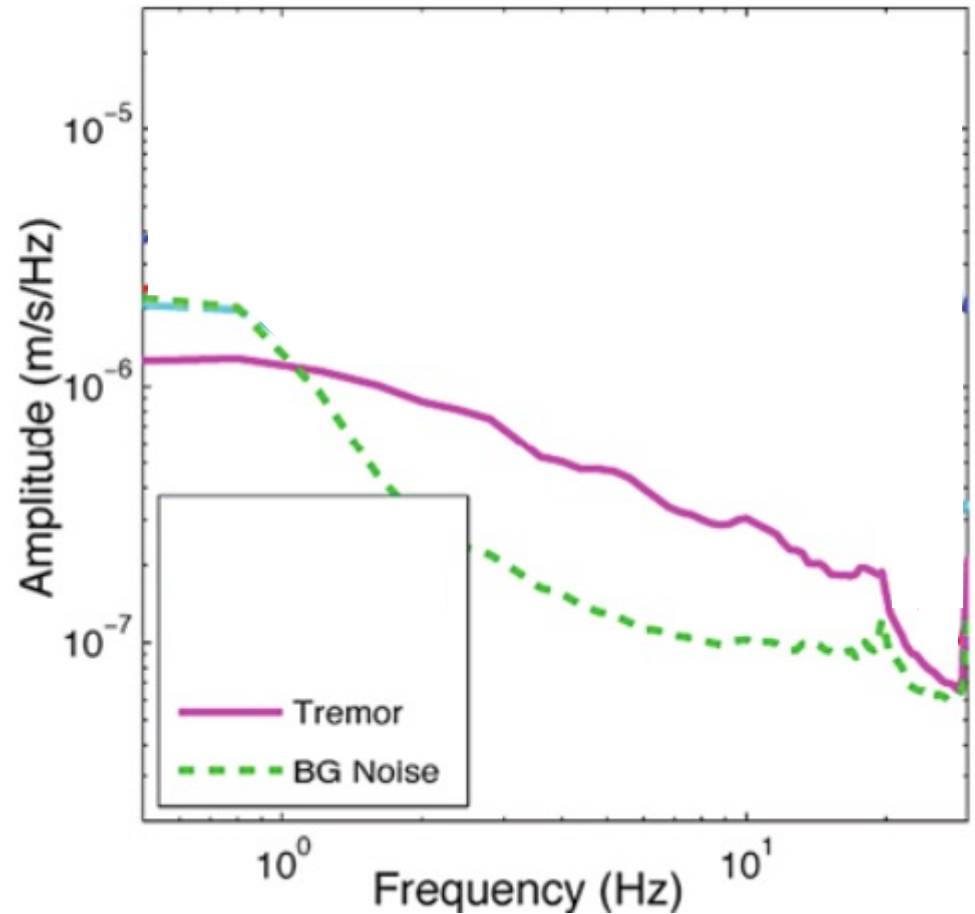
- *Dominantly in 1-10 Hz band*
- *M1 – 2.5*
- *0.2 – 0.5 s long*
- *Some < 400 m wide*
- *Some rupture at < 0.5 times shear wave speed*

Need precise, careful, and creative analysis

So what are LFEs?

- Low stress drop earthquakes?
- Resonance in fault zone?
- Short slow slip events?

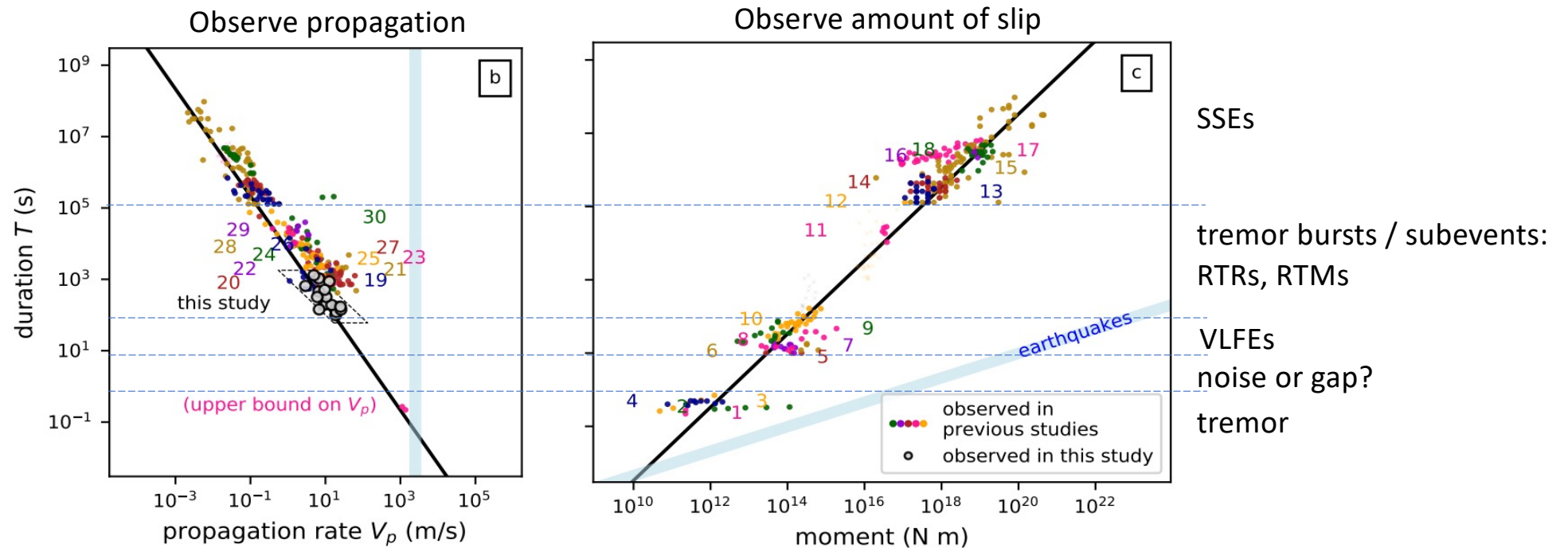
modified from Rubinstein et al, 2009



# Are slow slip and tremor the same process?

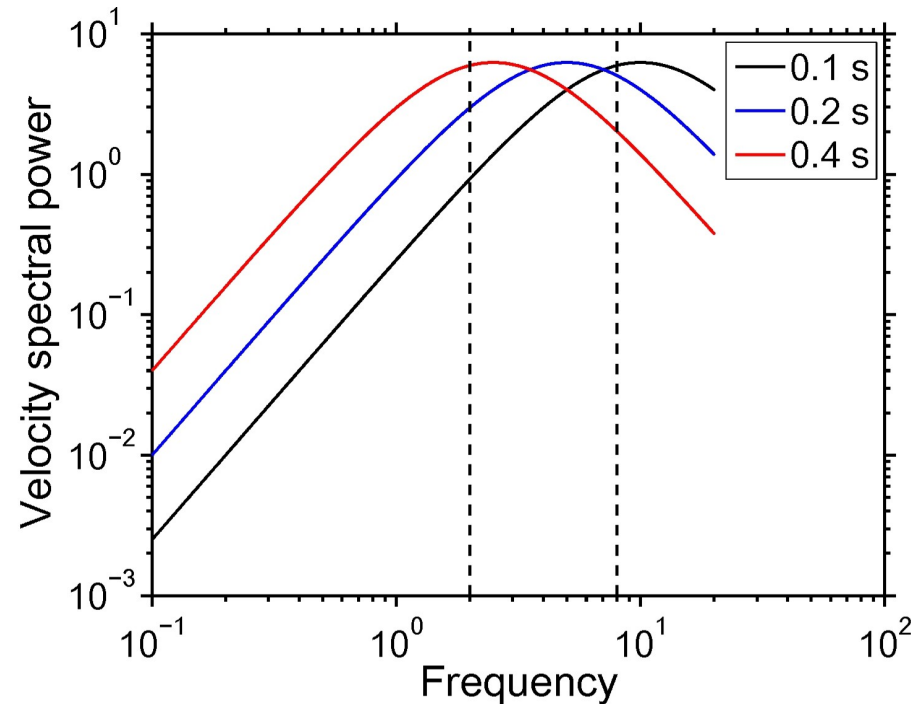
No: There's a gap between VLFs and tremor. And **tremor's LFEs seem to have a characteristic moment and duration** in some observations.

Yes: They're on the right trend, and they're slow for some reason. Why not the same reason as slow slip? The gap is just because the ocean generates lots of 1-s seismic noise.



# Or maybe longer events are just harder to find?

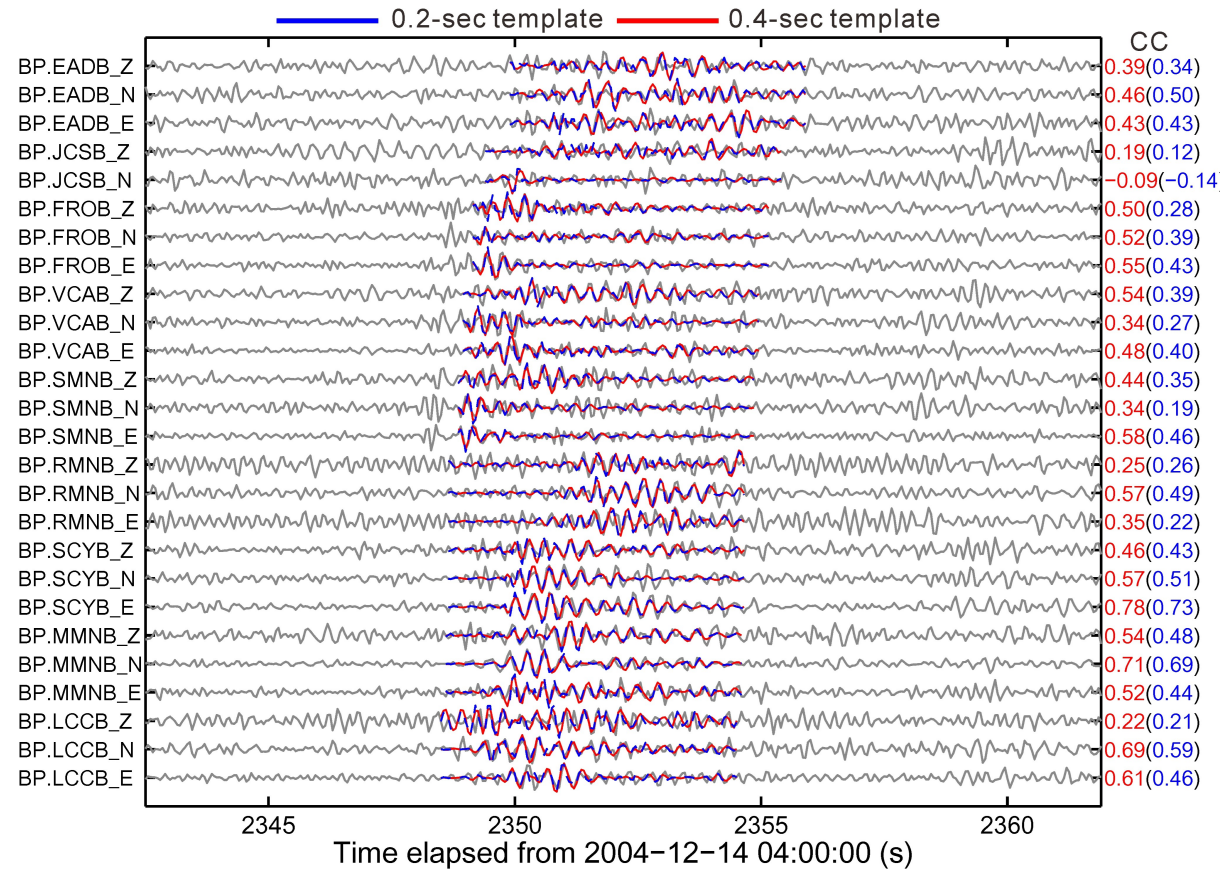
Work by Hui Huang:  
Huang and Hawthorne,  
submitted



- Tend to work at 2-8 Hz frequencies because of noise at lower frequencies
- In that band, 0.2-s-long earthquakes are easiest to find

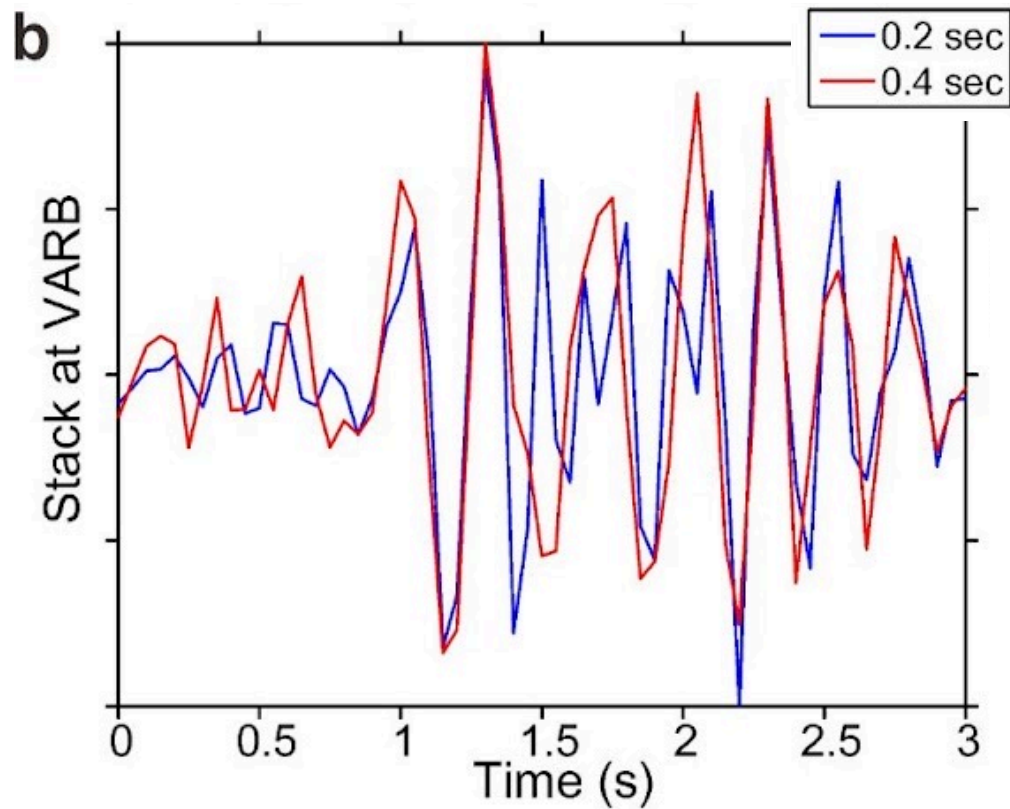


# So let's look for longer events



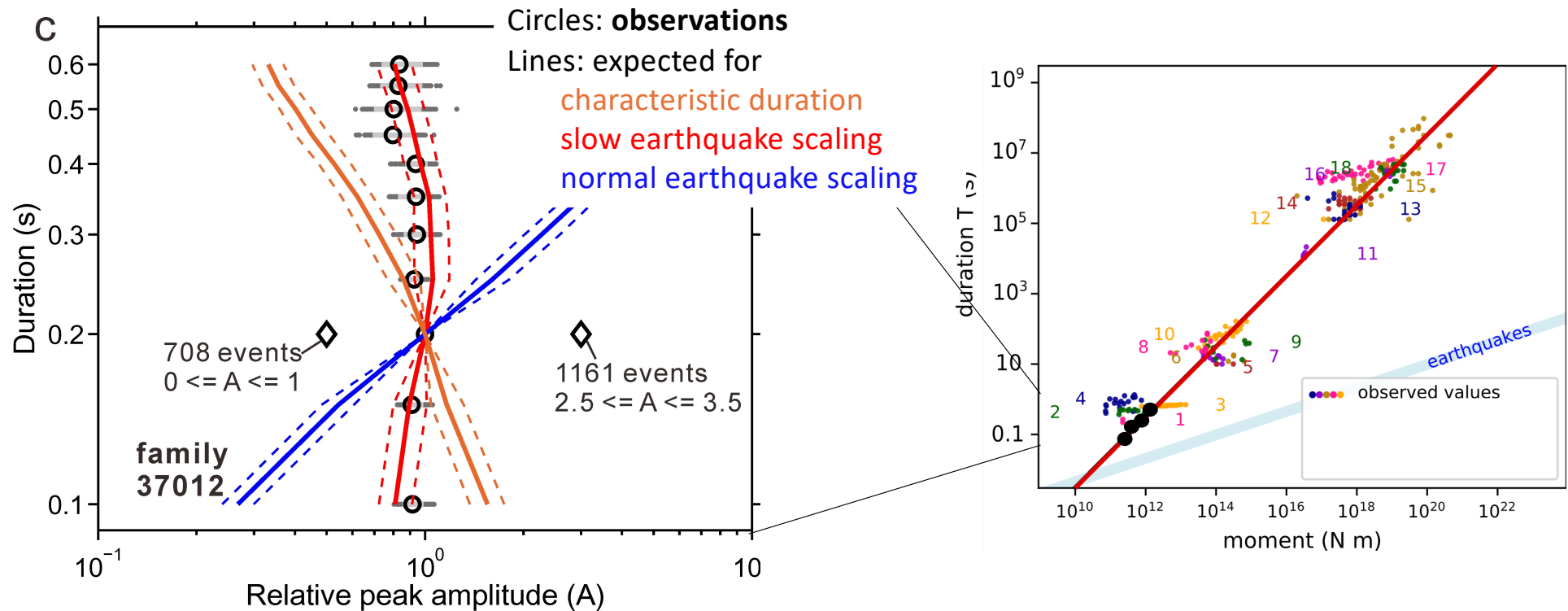
Create templates for 0.2-s and 0.4-s events and search through continuous seismic data  
Stack identified events and estimate their amplitudes and durations

# And we find longer LFEs!



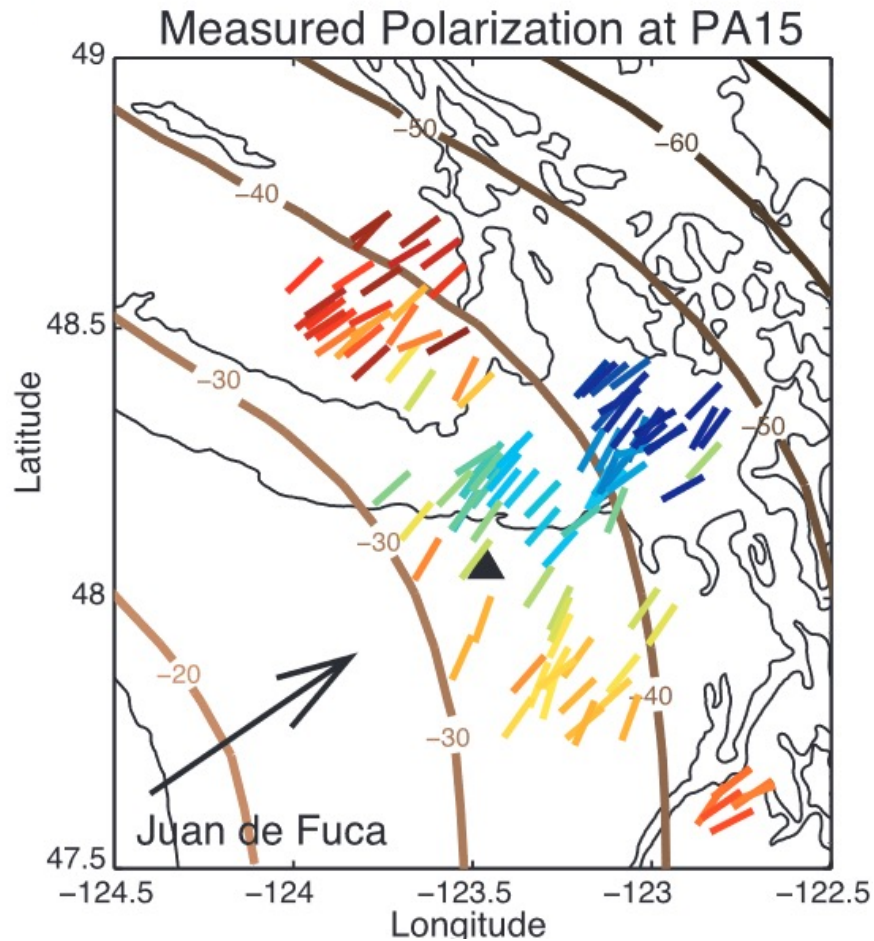
- Differences are subtle but significant
- Detect at some stations, stack at others to be sure we're not biasing our result

# LFE moment-duration scaling



Observed scaling is the same as seen for longer slow earthquakes  
 → Tremor earthquakes are short slow slip events?

# LFEs are mostly shear slip: polarization analysis

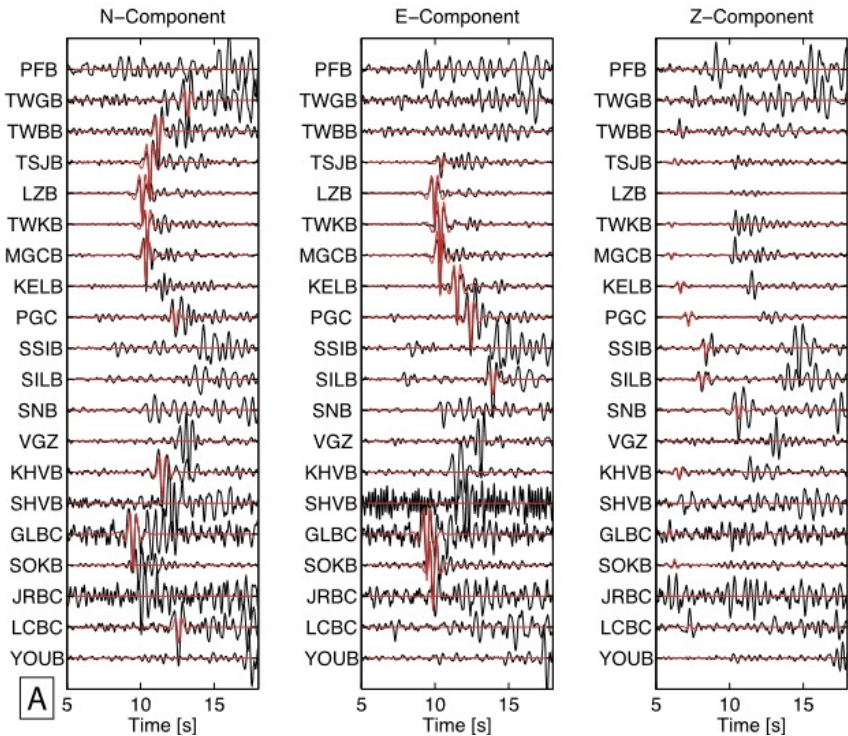
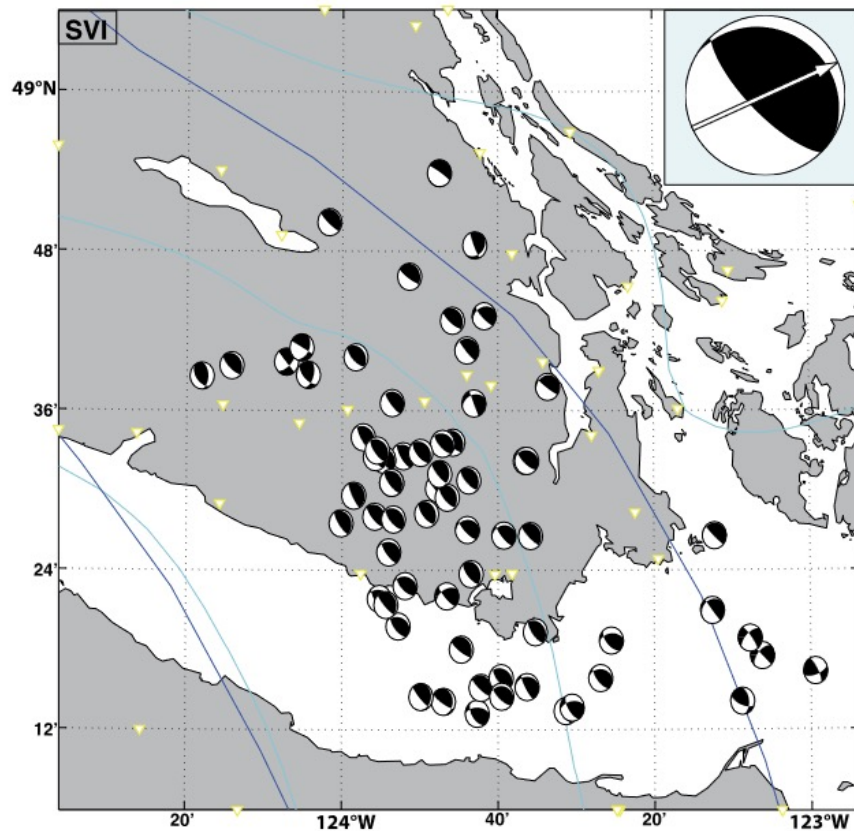


Measure orientation of S wave observed at the array (triangle) due to tremor centred on each of the lines.

All NE-SW, parallel to slip direction.

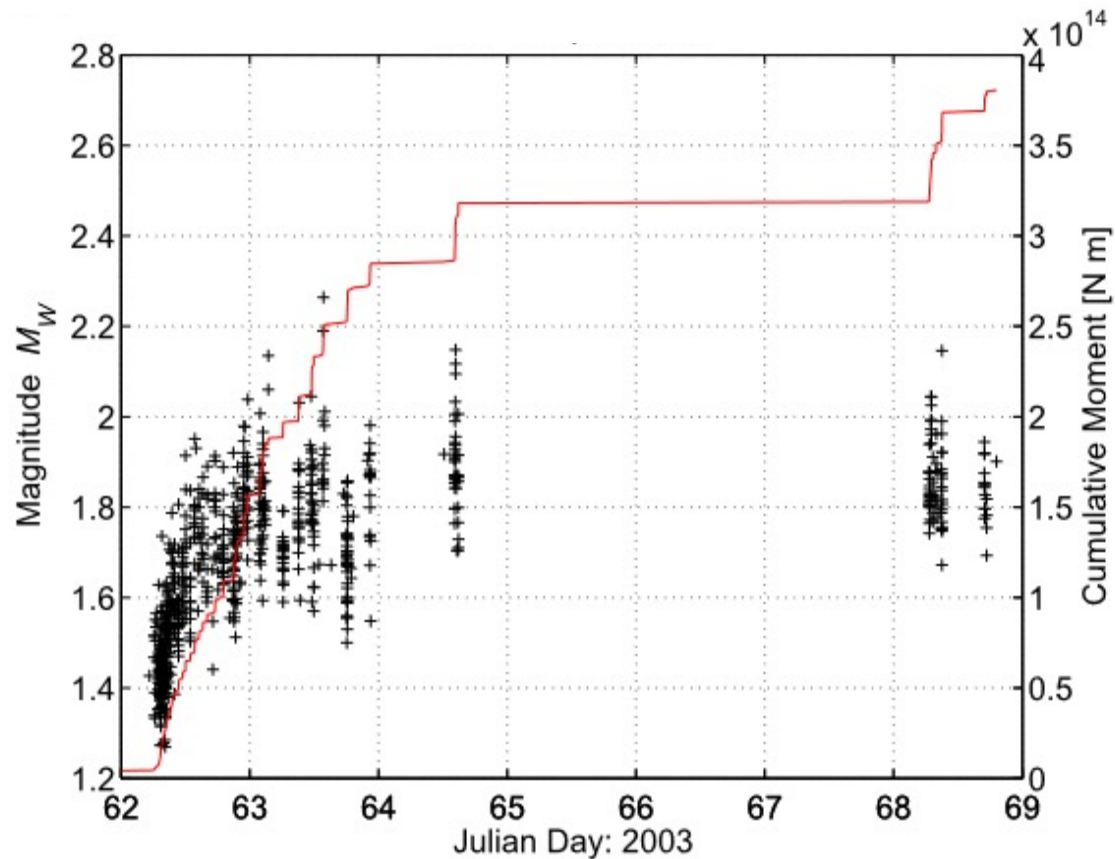
Wech and Creager, 2007

# LFEs are mostly shear slip: focal mechanisms



Compare observed waveforms to synthetics for a range of focal mechanisms

# What about dilation?



Bostock et al, 2015

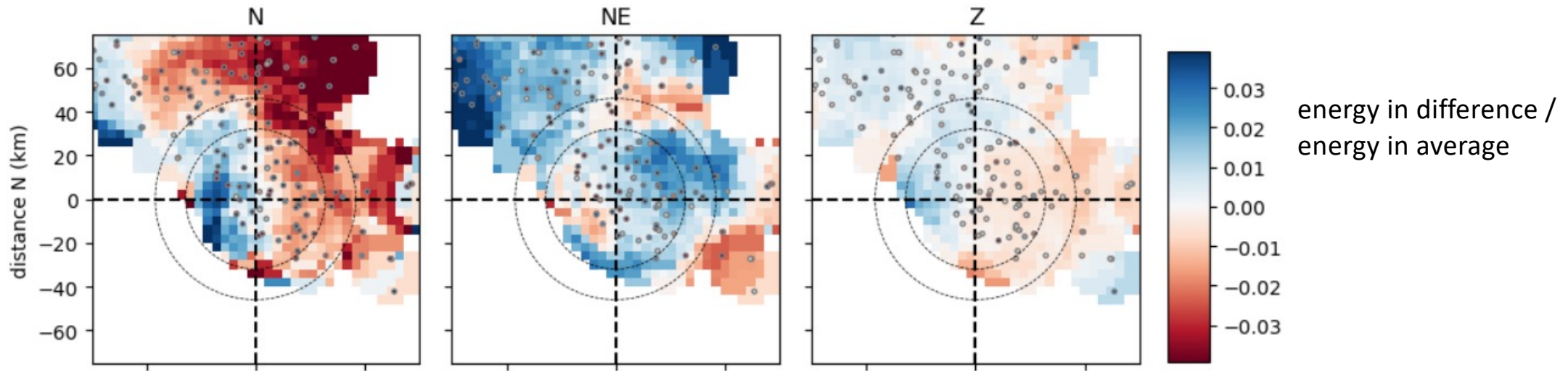
Moments at one location through time

- Start small
- But increase as the main front moves farther ahead  
→ A change in smoothness or permeability through time?

*Maybe the later, bigger LFEs have less dilation because the permeability is higher?*

*Can we see a difference in the focal mechanisms of early and late LFEs?*

# Energy in the difference



- Stack early LFEs (more dilation expected) and late LFEs (less dilation expected)
- Subtract the two stacks
- Examine the polarization of the difference: mostly N-S, NE-SW, vertical?

- Difference is less than a few percent of the total energy
- No obvious patterns

*But just a few percent dilation is plausible; Need to try harder?*

# Tremor summary

- *Dominantly in 1-10 Hz band*
- *M1 – 2.5*
- *0.2 – 0.5 s long*
- *Some < 400 m wide*
- *Some rupture at < 0.5 times shear wave speed*
- *Possible detection bias, some longer LFEs*
- *Mostly shear slip*

Need more precise, careful, and creative analysis to determine what causes LFEs.

modified from Rubinstein et al, 2009

