



# Statistical Model Calculations with TALYS for p-induced reactions on Sn isotopes



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Data with the TALYS Code

# Motivation

Sensitivity of element abundance to nuclear reaction rates which in turn depends on the reaction cross section.

The reaction rates determine the balance of feeding and depletion flows for each nucleus.

Puzzling origin of  $p$ -nuclei and their relatively small abundance among other isotopes.

Description of entire synthesis process for  $p$ -nuclei require a comprehensive reaction network involving about 2000 nuclei connected by more than 20000 reactions.

Experimental data are scarce.

Contributions from all branches have to be considered in order to account for correct abundance.

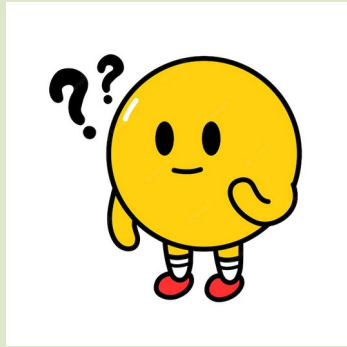
**Most of the involved nuclei are not accessible in the laboratory.**

**Theoretical Models**

**At astrophysical energies, charged particle cross sections are small.**

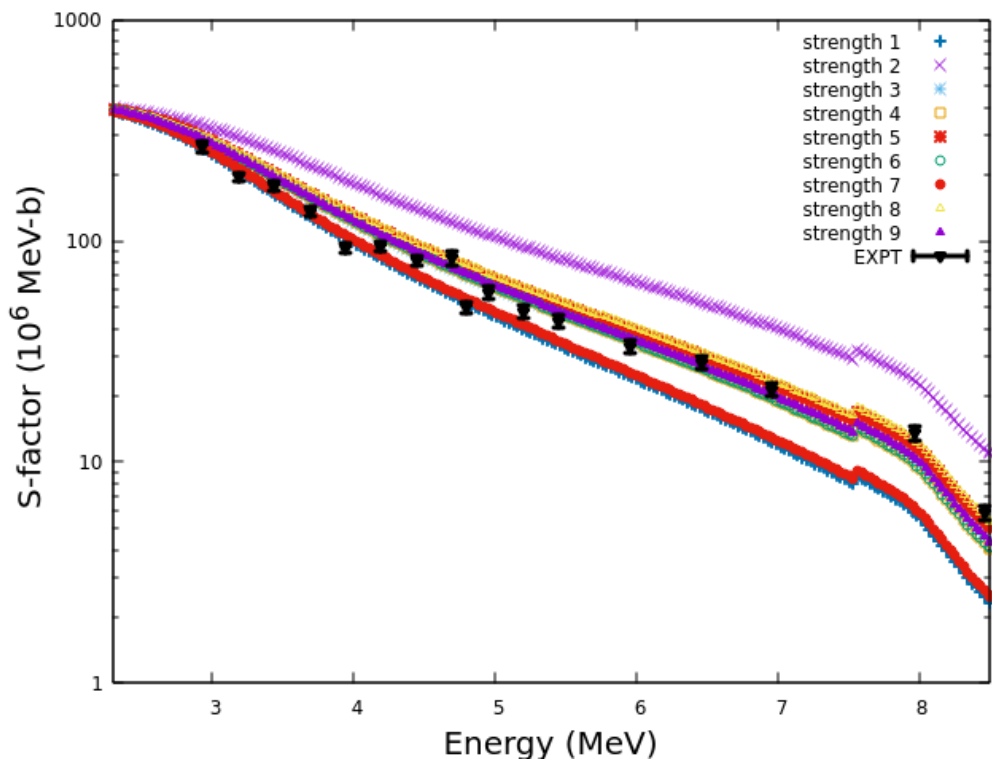
To test the predictive reliability of statistical models in astrophysical scenarios.

# Why Sn

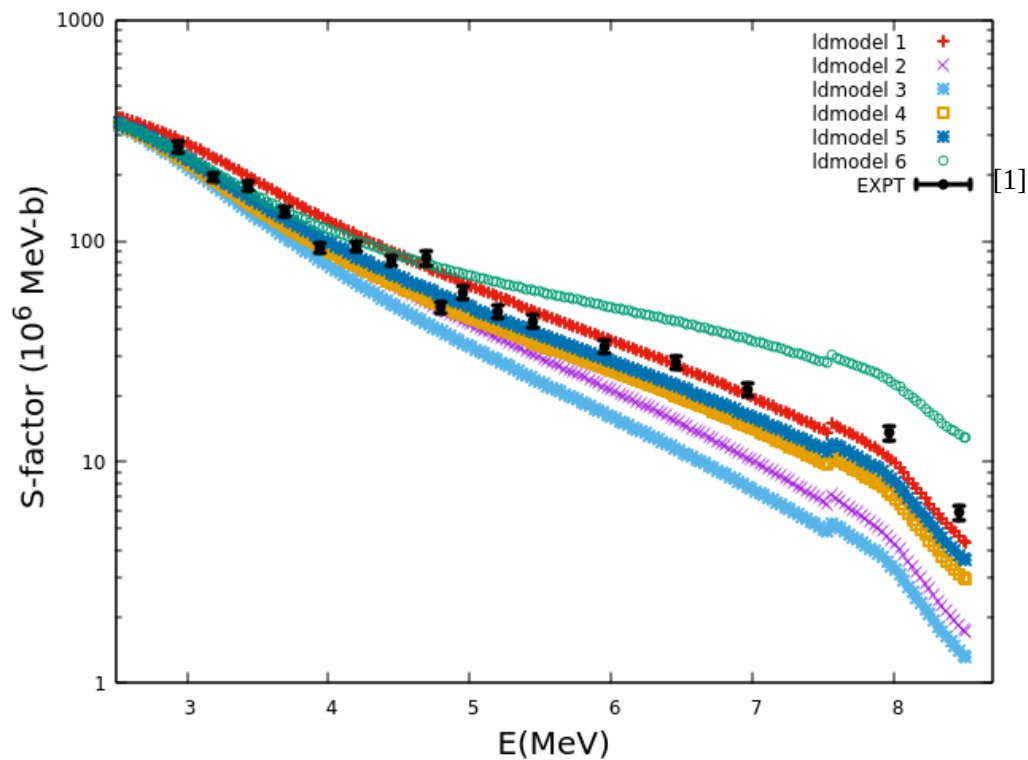


- Tin has large number of isotopes from  $A=112$  to  $124$ .
- Includes a variety of  $r$ -,  $s$ - and  $p$ -process contributions.
  - $^{112}\text{Sn}$  and  $^{114}\text{Sn}$  -  $p$ -process
  - $^{116}\text{Sn}$  -  $s$ -process
  - $^{122}\text{Sn}$  and  $^{124}\text{Sn}$  -  $r$ -process
  - $^{117}, ^{118}, ^{119}, ^{120}\text{Sn}$  – mixture of  $s$ - and  $r$ -process
  - $^{115}\text{Sn}$  – mixture of  $p$ -,  $r$ - and  $s$ -process
- Discrepancy in elemental abundance of tin is still alive.
- A fruitful element for identification of possible isotope anomalies.
- Minor isotopes of tin are used to delineate between various models of  $p$ -process nucleosynthesis.
- Locating astrophysical site of their production.

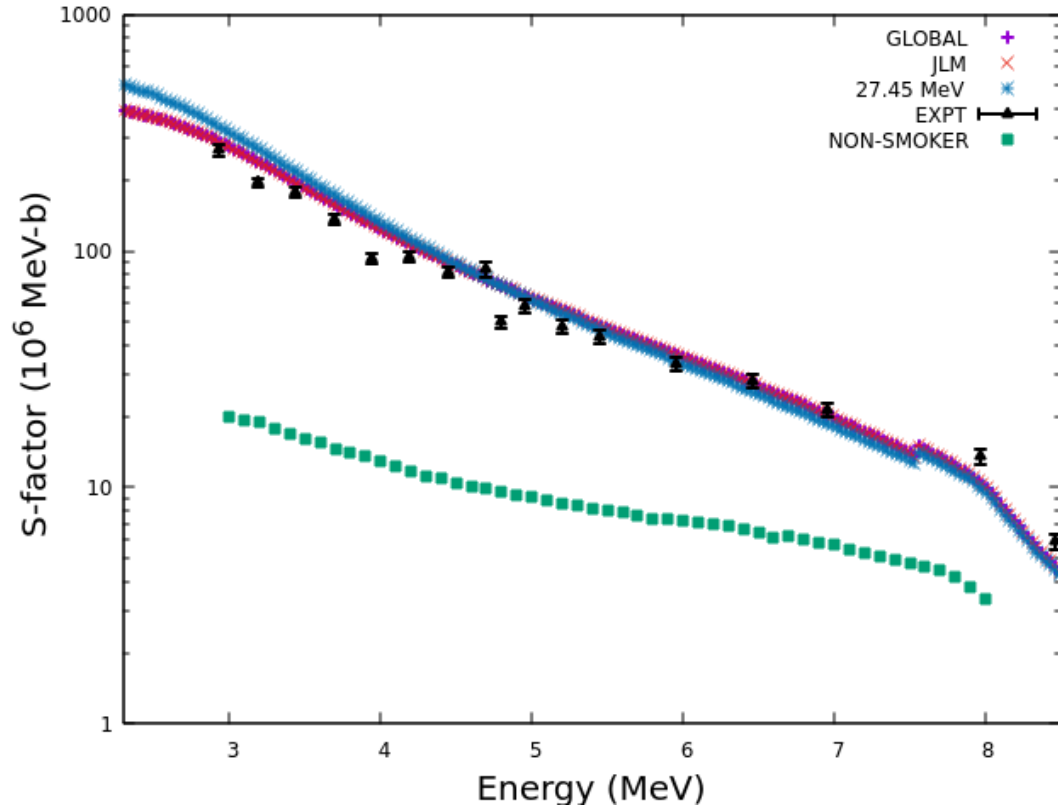
# TALYS Calculations for $^{112}\text{Sn}(p,\gamma)^{113}\text{Sb}$



With different Gamma Strength Function models



With different Nuclear Level density models



[2]  
[3]

**With different Optical Potential models :**

-> **Global**

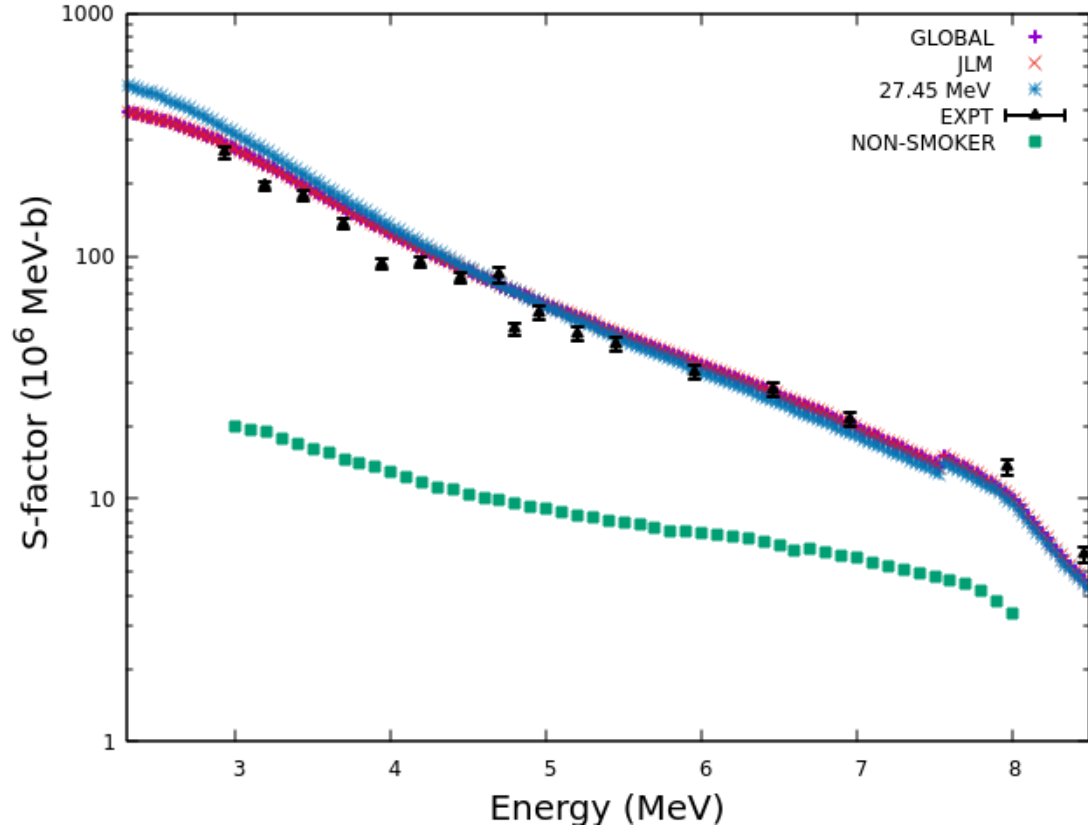
-> **Semimicroscopic JLM potential**

-> **Local Potential parameters fitted with elastic scattering of proton on  $^{112}\text{Sn}$  at 27.45 MeV.**

$E_{\text{lab}}$	$V_o$	$r_v$	$a_v$	$W$	$r_w$	$a_w$
27.45	51.92	1.17	0.75	7.5	1.32	0.51

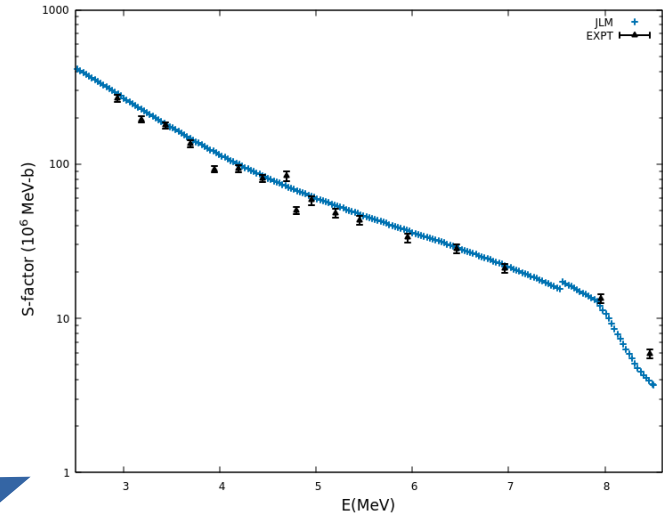
[2] P.J.Biankert et al., Nuclear Physics A356, 74-96 (1981).

[3] W. Makofske et al., Physical Review , Vol 174, No. 4 (1968).



With different Optical Potential models :

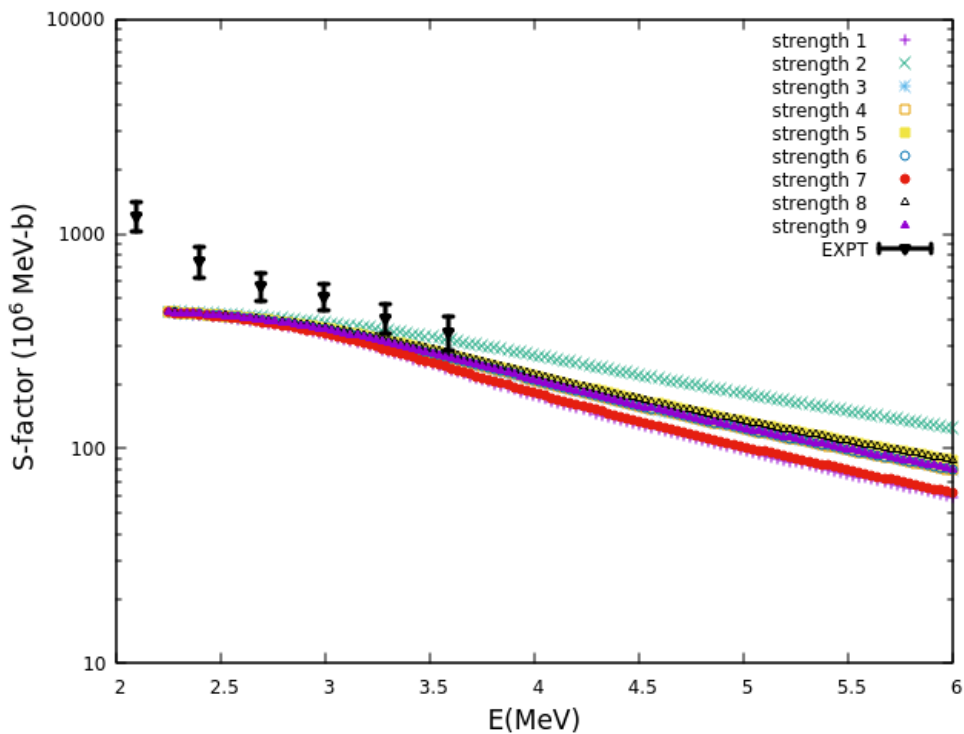
- [2] -> Global
- [3] -> Semimicroscopic JLM potential
- > Local Potential parameters fitted with elastic scattering of proton on  $^{112}\text{Sn}$  at 27.45 MeV.



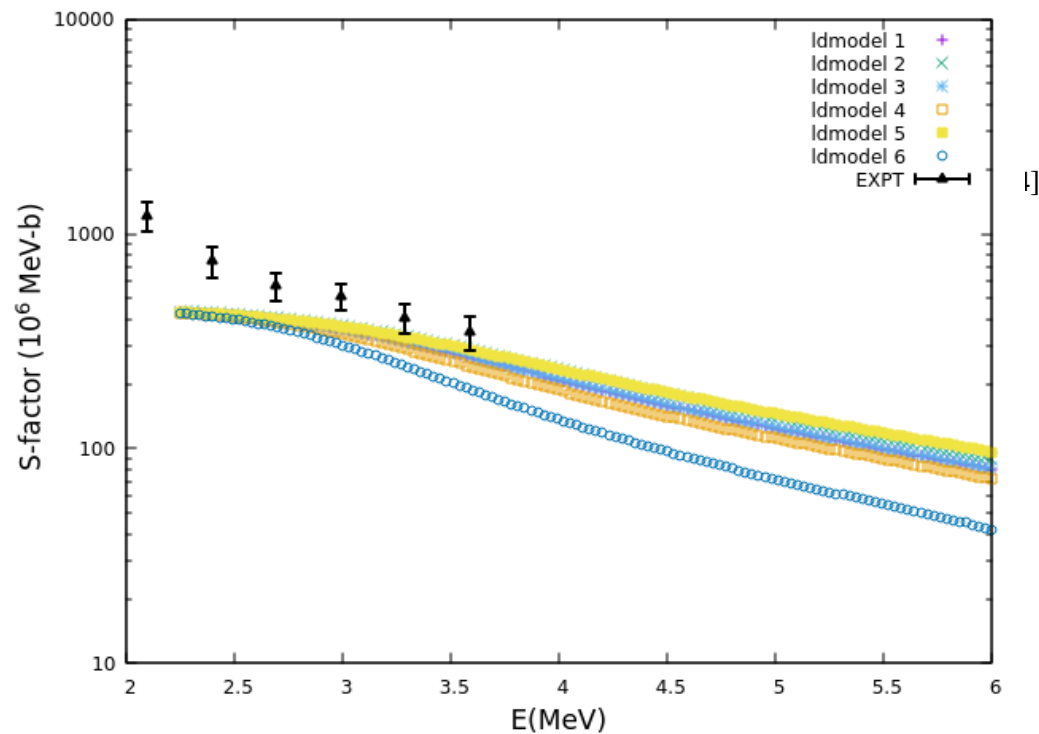
With semi microscopic JLM potential



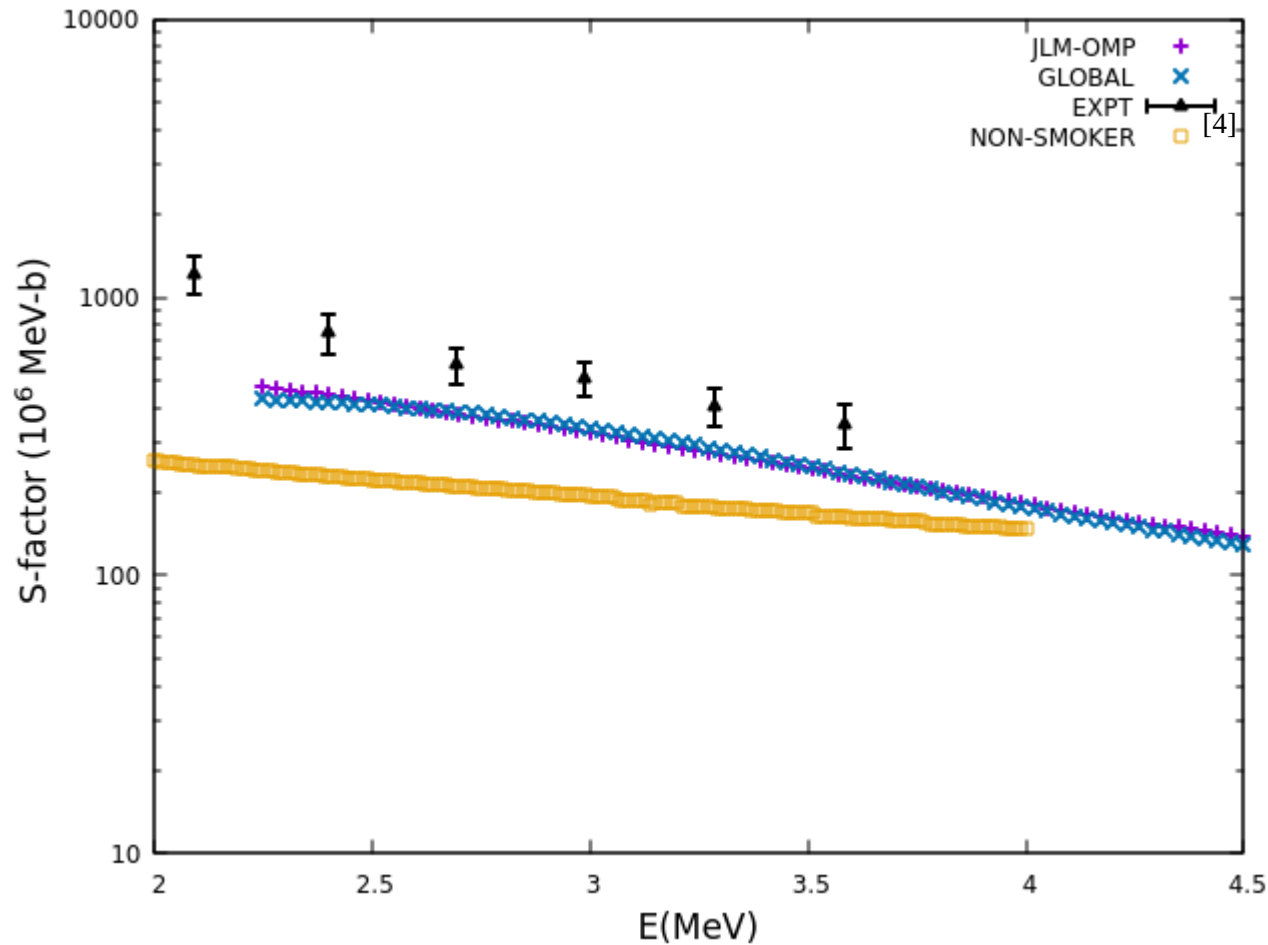
# TALYS Calculations for $^{114}\text{Sn}(p,\gamma)^{115}\text{Sb}$



With different Gamma Strength Function models

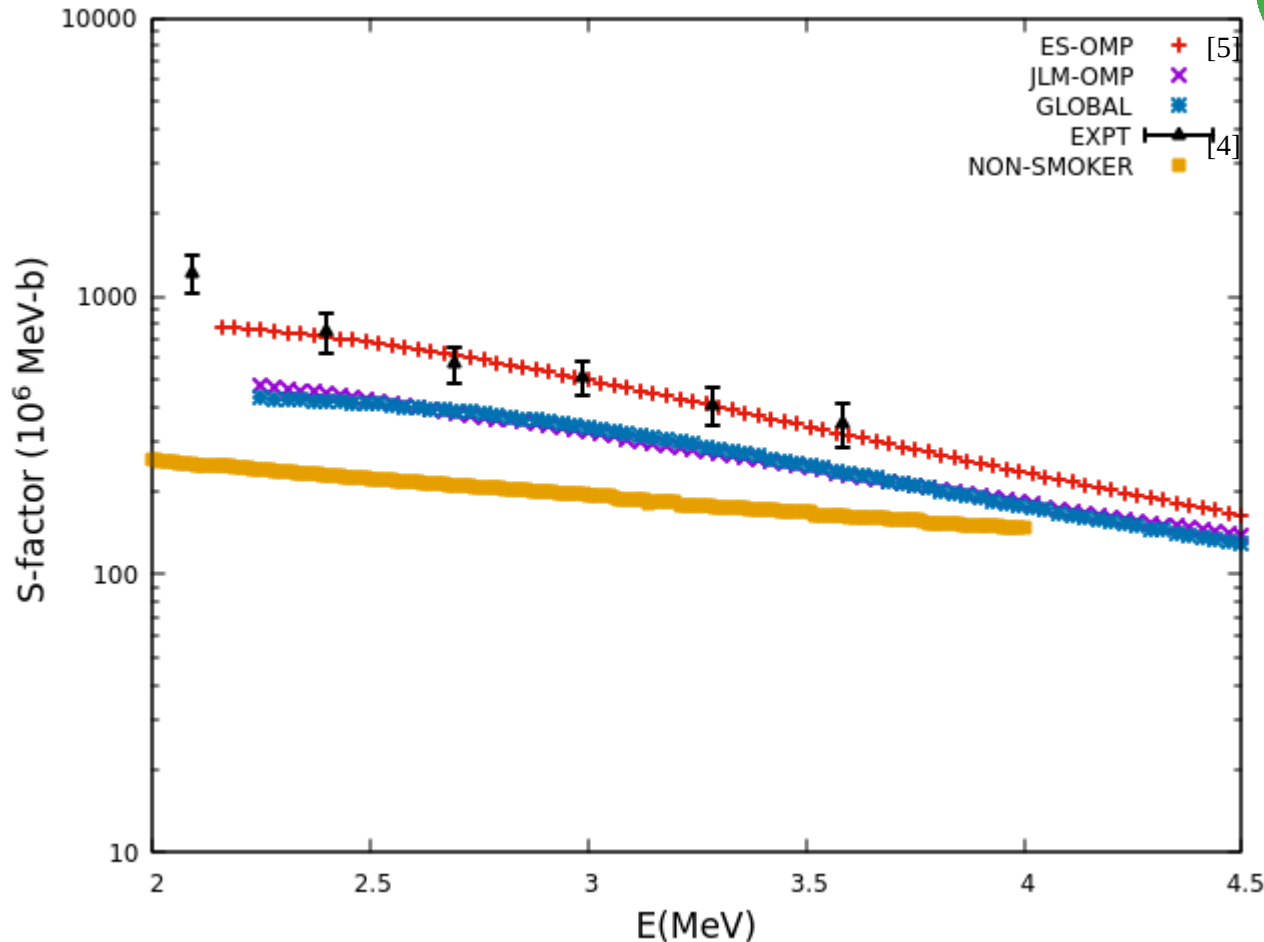


With different Nuclear Level density models



**Comparison of  
Experimental data with the  
default Optical Potentials :  
Global and Semi  
microscopic JLM potential  
and NON-SMOKER  
predictions.**





*Explains the experimental data much better*



Optical Model Parameters by fitting proton elastic scattering data on  $^{114}\text{Sn}$ :

$E_{\text{lab}} = 22.00 \text{ MeV}$

$V_o = 50.0 \text{ MeV}$

$r = 1.25 \text{ fm}$

$a = 0.65 \text{ fm}$

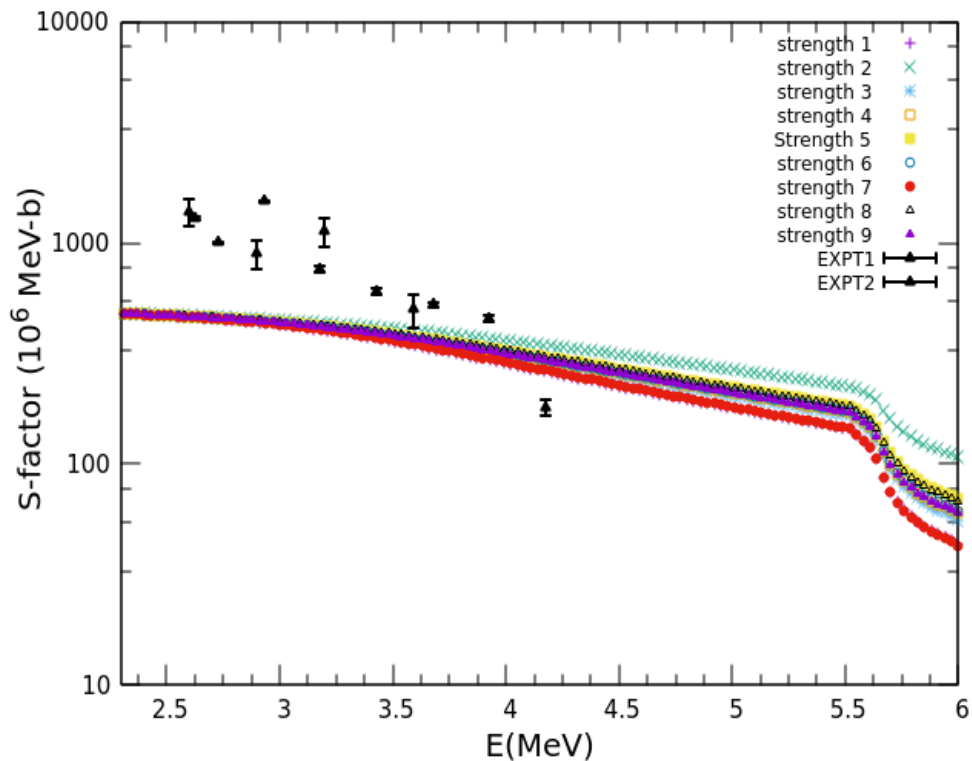
$W_D = 10.0 \text{ MeV}$

$r' = 1.30 \text{ fm}$

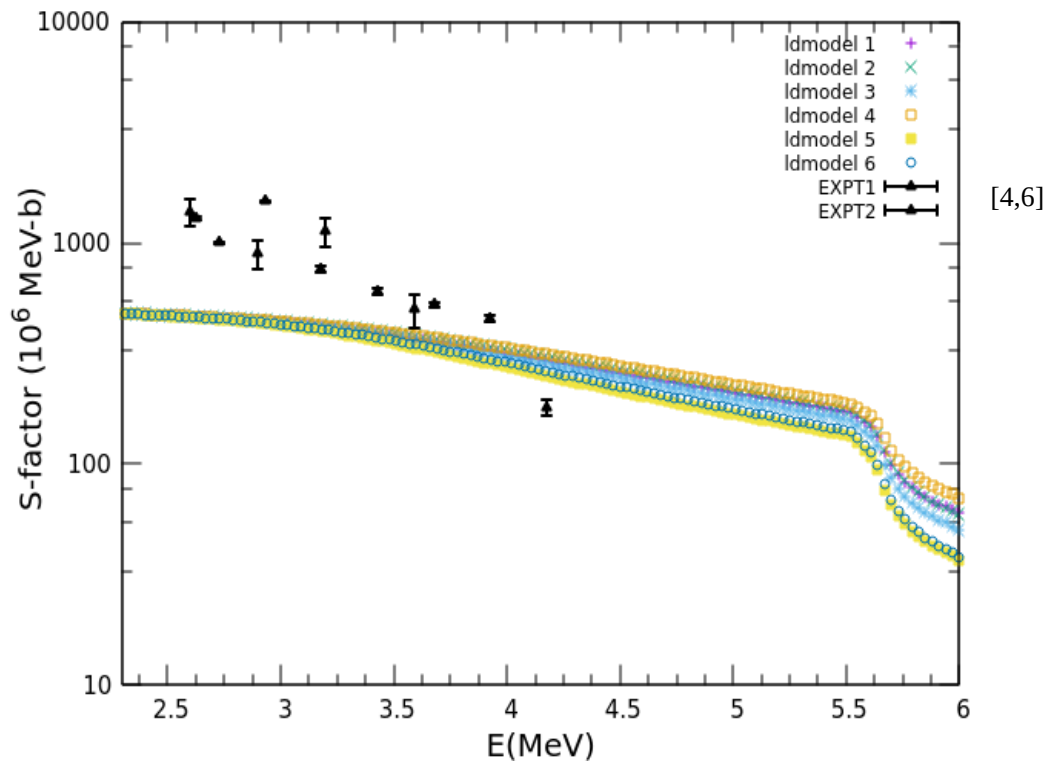
$a' = 0.6 \text{ fm}$

[5] P. Guazzoni et al., *Physical Review C* 85, 054609 (2012).

# TALYS Calculations for $^{116}\text{Sn}(p,\gamma)^{117}\text{Sb}$



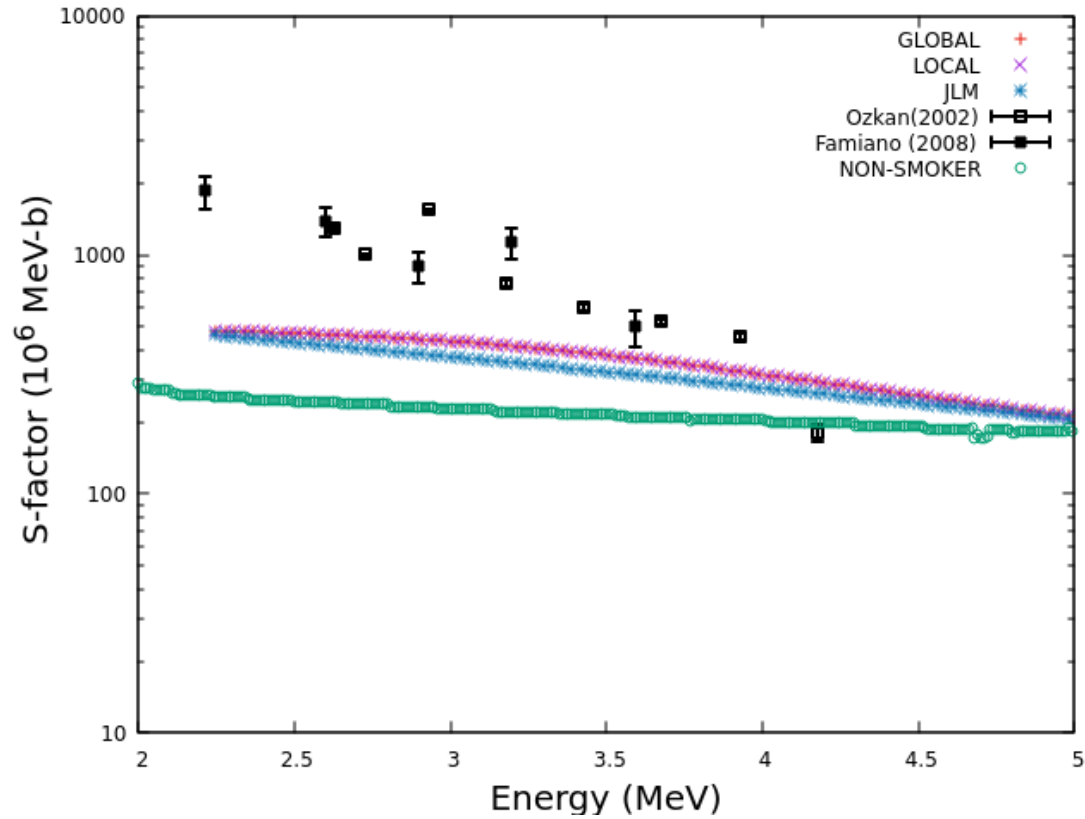
With different Gamma Strength Function models



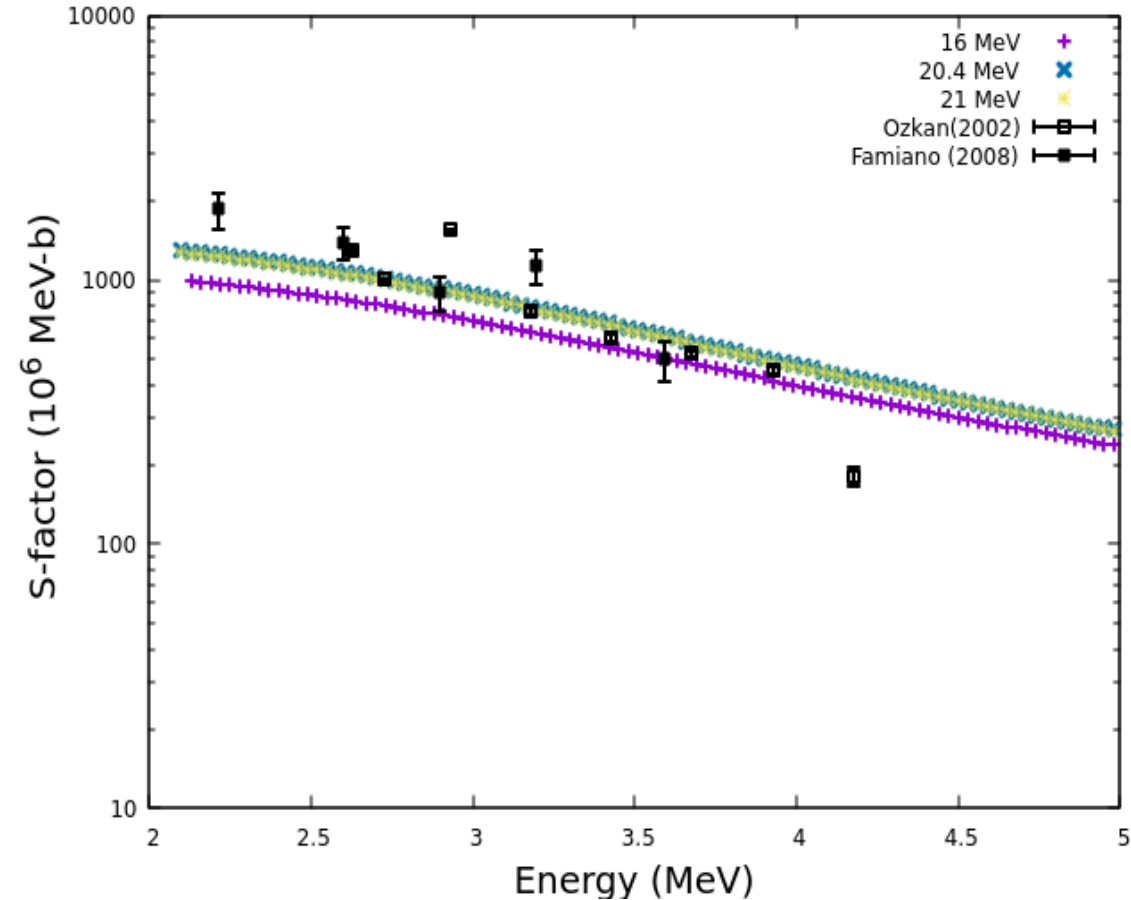
With different Nuclear Level density models

[4] Michael A. Famiano et al., *Nuclear Physics A*802, 26-44 (2008).

[6] N.Ozkan et al., *Nuclear Physics A*710, 469-485 (2002).



**With different Optical Potential models inherent to TALYS and a comparison with NON-SMOKER results**



[7]

[8]

[9]

[4,6]

Optical Model Parameters by fitting experimental data of elastic scattering of proton on  $^{116}\text{Sn}$ :

$E_{\text{lab}}$	$V_o$	$r_v$	$a_v$	$W$	$r_w$	$a_w$
16	55.25	1.2	0.7	10.73	1.25	0.65
20.4	53.71	1.194	0.713	8.85	1.265	0.675
21	53.9	1.18	0.71	10.6	1.26	0.66

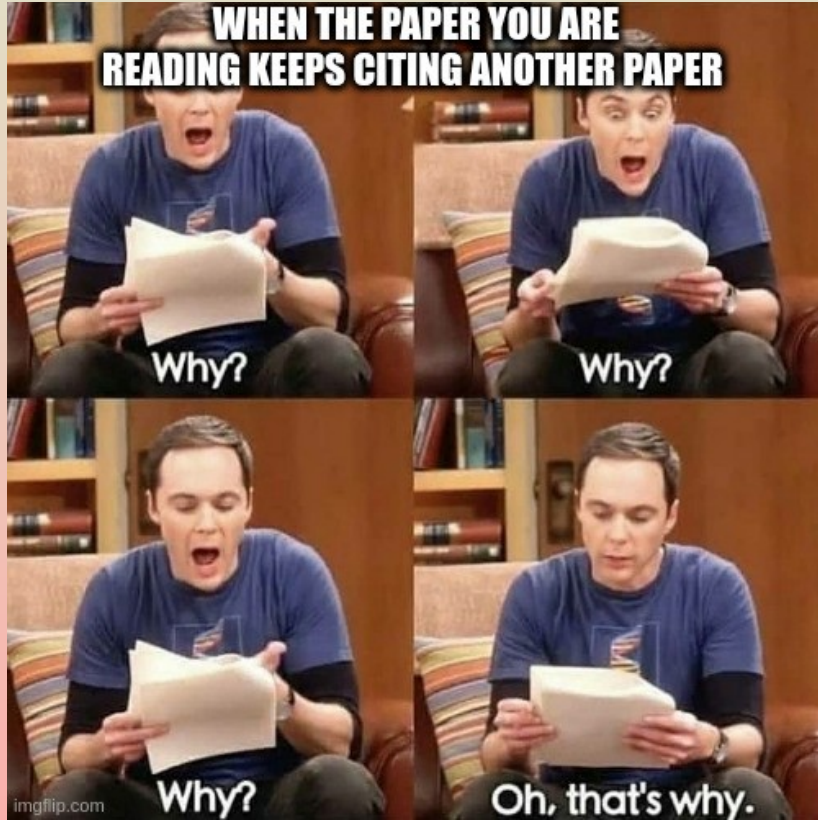
[7] W. Makofske et al., *Physical Review*, Vol 174, No. 4 (1968).

[8] S.D.Wassenaar et al., *J. Phys. G: Nucl. Part. Phys.* 15 181 (1989)

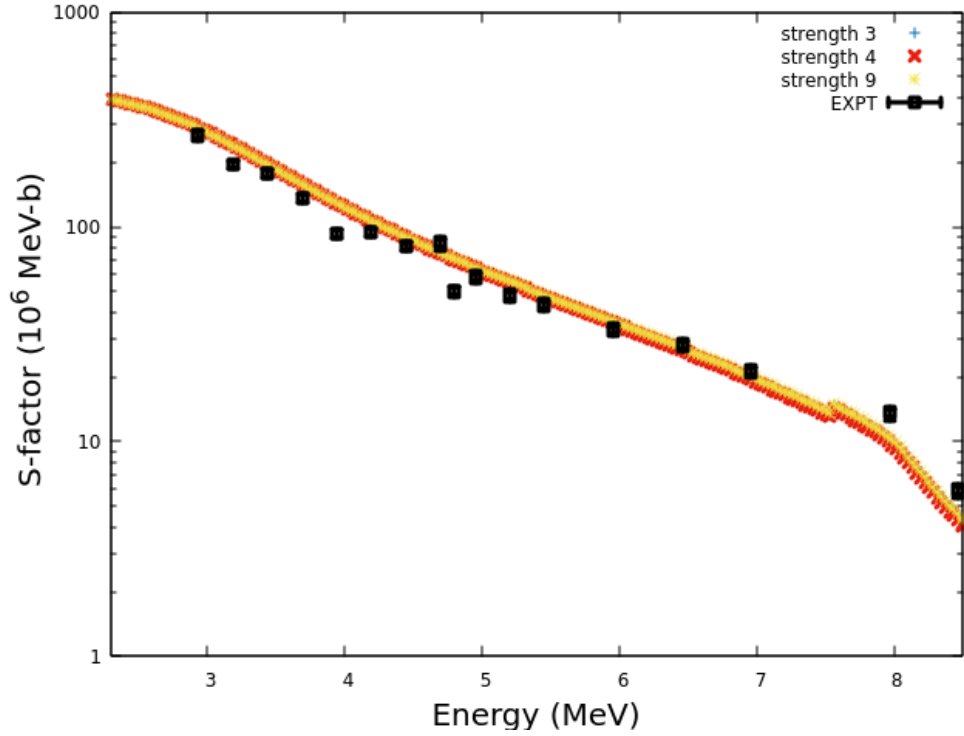
[9] Norton baron et al., *Physical Review*, Vol 180, No. 4 (1969)

# SUMMARY

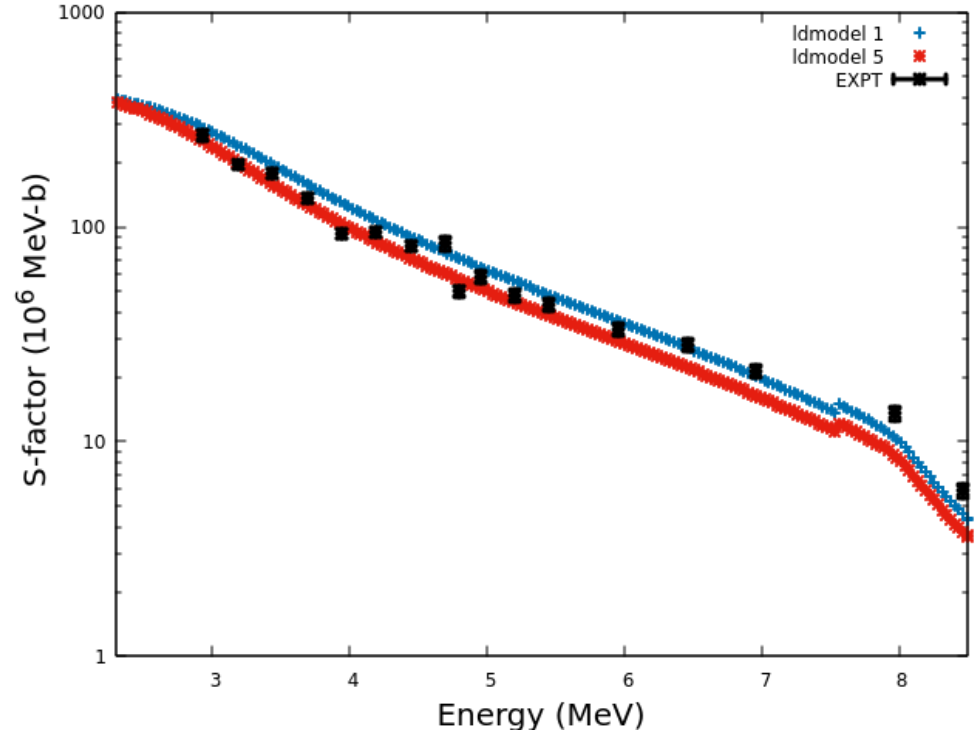
- Hauser Feshbach statistical model calculations were performed to describe the experimental cross sections of  $^{112}\text{Sn}(p,\gamma)^{113}\text{Sb}$ ,  $^{114}\text{Sn}(p,\gamma)^{115}\text{Sb}$  and  $^{116}\text{Sn}(p,\gamma)^{117}\text{Sb}$  using TALYS.
- Effect of different models for GSF, NLD and various sets of OMP parameters in the energy domain of the present study, namely 2-9 MeV for all three reactions were studied.
- Several OMP parameter sets optimized with proton elastic scattering data were used to calculate cross sections.
- Astrophysical S-Factor was plotted against proton lab energy and compared with literature data.



T H A N K  
Y O U

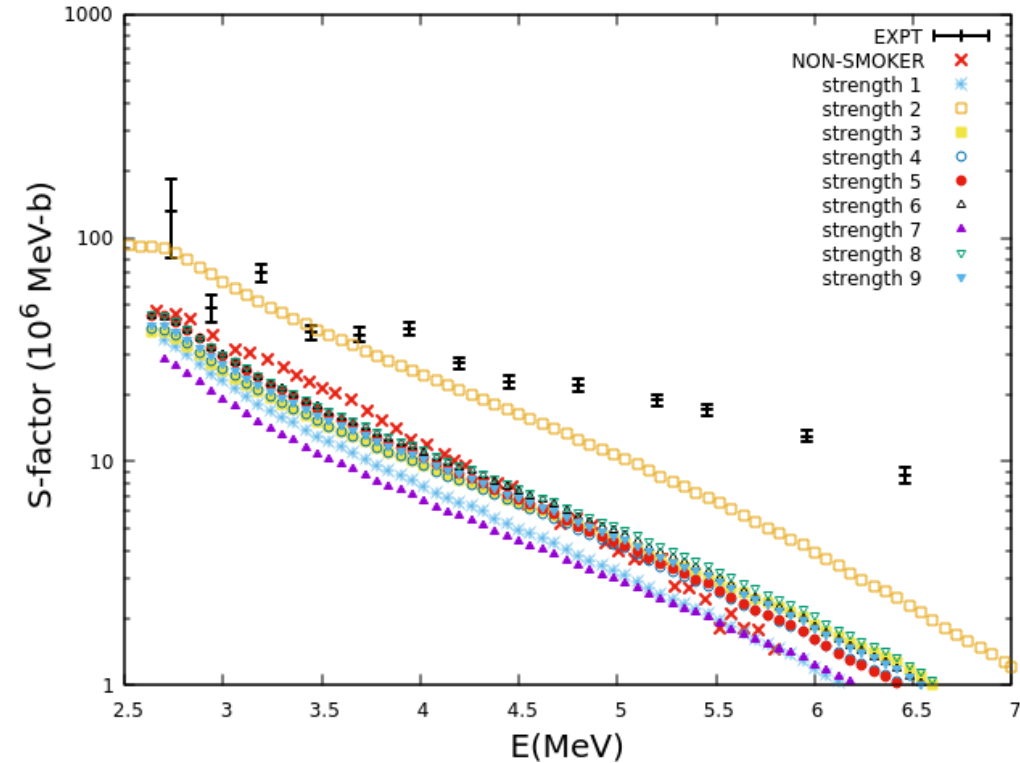


$^{112}\text{Sn}$  Sfactors with GSF models, S3,4,9  
 Default model - S9



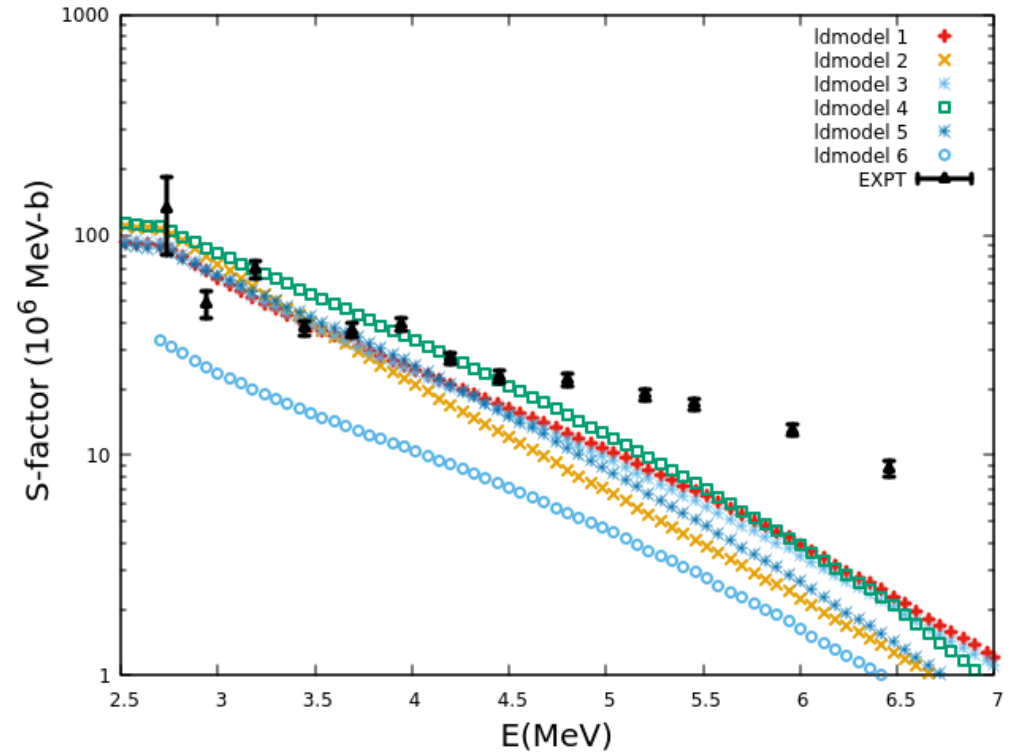
$^{112}\text{Sn}$  Sfactors with NLD models, LD 1 and 5  
 Default model – LD1

# TALYS Calculations for $^{119}\text{Sn}(p,\gamma)^{120}\text{Sb}$

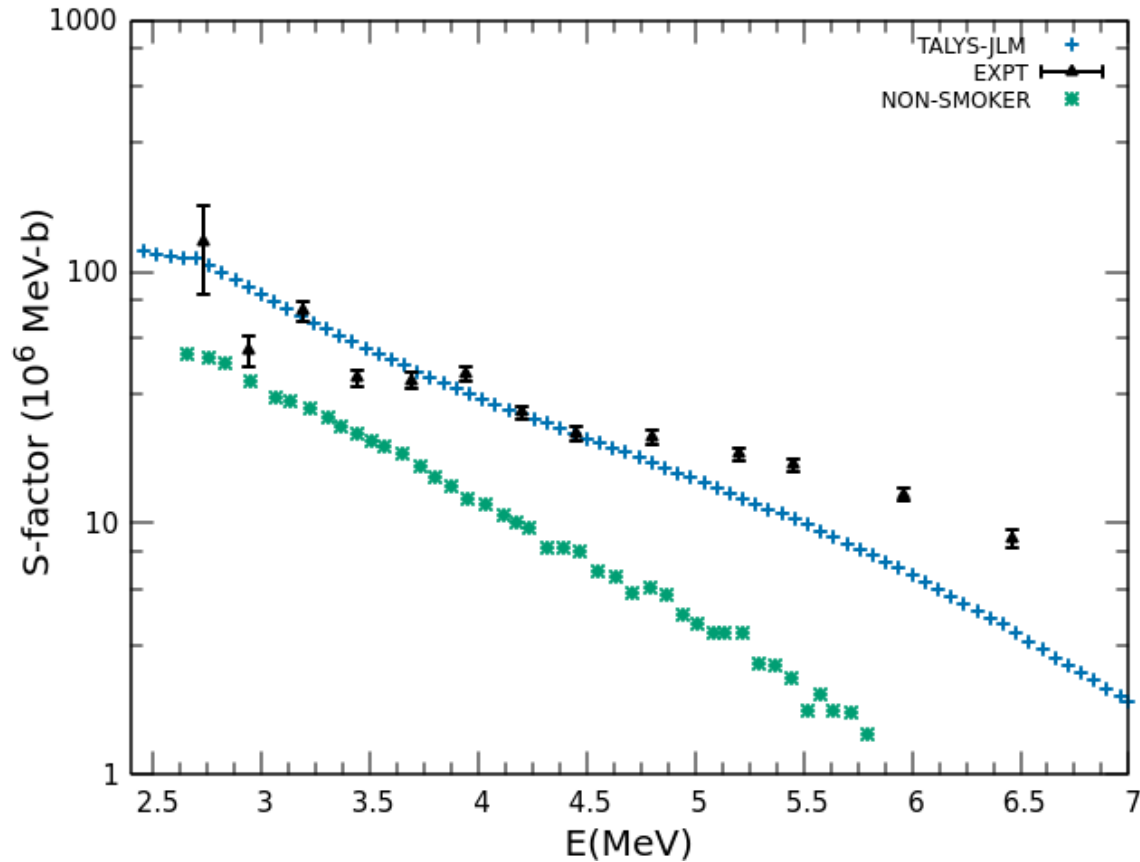


With different Gamma Strength Function models

With different Nuclear Level density models







**Comparison of  
Experimental data with the  
default Optical Potentials :  
Global and Semi  
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predictions.**

## List of 35 *p*-nuclei

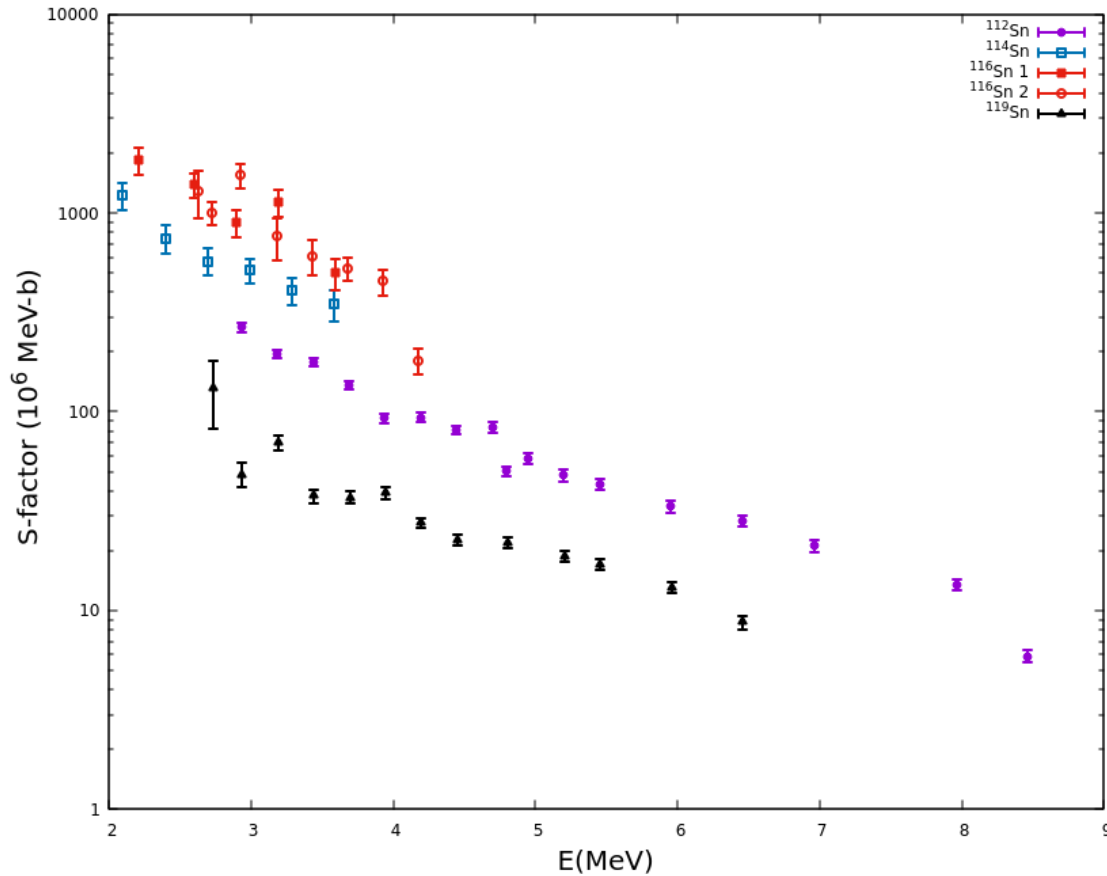
$^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ ,  $^{92}\text{Mo}$ ,  $^{94}\text{Mo}$ ,  $^{96}\text{Ru}$ ,  $^{98}\text{Ru}$ ,  $^{102}\text{Pd}$ ,  $^{106}\text{Cd}$ ,  $^{108}\text{Cd}$ ,  $^{112}\text{Sn}$ ,  $^{113}\text{In}$ ,  $^{114}\text{Sn}$ ,  
 $^{115}\text{Sn}$ ,  $^{120}\text{Te}$ ,  $^{124}\text{Xe}$ ,  $^{126}\text{Xe}$ ,  $^{130}\text{Ba}$ ,  $^{132}\text{Ba}$ ,  $^{136}\text{Ce}$ ,  $^{138}\text{La}$ ,  $^{138}\text{Ce}$ ,  $^{144}\text{Sm}$ ,  $^{152}\text{Gd}$ ,  $^{156}\text{Dy}$ ,  
 $^{158}\text{Dy}$ ,  $^{162}\text{Er}$ ,  $^{164}\text{Er}$ ,  $^{168}\text{Yb}$ ,  $^{174}\text{Hf}$ ,  $^{180}\text{Ta}$ ,  $^{180}\text{W}$ ,  $^{184}\text{Os}$ ,  $^{190}\text{Pt}$ , and  $^{196}\text{Hg}$

TABLE IX. Maxwellian averaged neutron capture cross sections of  $^{114}\text{Sn}$ ,  $^{115}\text{Sn}$ ,  $^{116}\text{Sn}$ ,  $^{117}\text{Sn}$ ,  $^{118}\text{Sn}$ , and  $^{120}\text{Sn}$  for thermal energies from 10 to 100 keV (the 1.5% uncertainty of the gold standard is not included here since it cancels out in most applications of relevance for nuclear astrophysics).

$kT$ (keV)	$^{114}\text{Sn}$ (mb)	$^{115}\text{Sn}$ (mb)	$^{116}\text{Sn}$ (mb)	$^{117}\text{Sn}$ (mb)	$^{118}\text{Sn}$ (mb)	$^{120}\text{Sn}$ (mb)
10	$249.2 \pm 8.4$	$550.7 \pm 42$	$171.6 \pm 2.6$	$549.4 \pm 13$	$126.6 \pm 3.1$	$73.2 \pm 1.7$
12	$226.2 \pm 6.3$	$512.4 \pm 33$	$155.4 \pm 2.1$	$506.6 \pm 10$	$112.4 \pm 2.3$	$65.1 \pm 1.3$
20	$169.9 \pm 3.0$	$413.2 \pm 16$	$116.1 \pm 1.3$	$395.5 \pm 6.5$	$80.3 \pm 1.1$	$46.7 \pm 0.7$
25	$149.3 \pm 2.2$	$373.2 \pm 11$	$102.1 \pm 1.1$	$351.8 \pm 5.5$	$69.7 \pm 0.8$	$40.5 \pm 0.6$
30	$134.4 \pm 1.8$	$342.4 \pm 8.7$	$91.9 \pm 0.9$	$318.8 \pm 4.8$	$62.6 \pm 0.6$	$36.4 \pm 0.5$
40	$114.6 \pm 1.4$	$298.5 \pm 6.3$	$78.6 \pm 0.7$	$271.4 \pm 4.0$	$53.3 \pm 0.6$	$31.1 \pm 0.4$
50	$102.3 \pm 1.2$	$268.8 \pm 5.2$	$70.5 \pm 0.7$	$239.1 \pm 3.5$	$47.8 \pm 0.4$	$27.9 \pm 0.3$
52	$100.4 \pm 1.2$	$263.9 \pm 5.0$	$69.2 \pm 0.6$	$233.7 \pm 3.4$	$46.9 \pm 0.4$	$27.5 \pm 0.3$
60	$94.1 \pm 1.1$	$247.4 \pm 4.5$	$65.1 \pm 0.6$	$215.0 \pm 3.1$	$44.1 \pm 0.4$	$25.9 \pm 0.3$
70	$88.4 \pm 1.1$	$231.3 \pm 4.0$	$61.2 \pm 0.6$	$196.4 \pm 2.8$	$41.7 \pm 0.4$	$24.5 \pm 0.3$
80	$84.3 \pm 1.1$	$218.5 \pm 3.8$	$58.4 \pm 0.6$	$181.5 \pm 2.7$	$39.9 \pm 0.5$	$23.4 \pm 0.4$
90	$81.0 \pm 1.1$	$208.0 \pm 3.4$	$56.5 \pm 0.6$	$169.3 \pm 2.5$	$38.5 \pm 0.5$	$22.6 \pm 0.3$
100	$78.6 \pm 1.3$	$198.9 \pm 3.3$	$54.7 \pm 0.7$	$159.1 \pm 2.6$	$37.5 \pm 0.5$	$22.0 \pm 0.4$

## ISOTOPIC ABUNDANCES OF TIN

Isotope	Absolute Abundance (atom percent)	Solar Abundance (atoms per $10^6$ Si)	Solar Abundance (ppm)
112 .....	0.973	0.0372	0.0163
114 .....	0.659	0.0252	0.0107
115 .....	0.339	0.0129	0.0057
116 .....	14.538	0.555	0.244
117 .....	7.672	0.293	0.129
118 .....	24.217	0.925	0.407
119 .....	8.587	0.328	0.144
120 .....	32.596	1.245	0.548
122 .....	4.632	0.177	0.0778
124 .....	5.787	0.221	0.0972
Total .....	100.00	3.82	1.68



*Systematic study of proton capture on Sn isotopes in the astrophysical energy range*

*Experimental cross sections available at energies from 2 – 9 MeV*

*$^{119}\text{Sn}$  shows a peculiar trend*

