





Outline

- Optical fibers
- Fiber modes
- Fiber lasers
- Spatial nonlinear effects
- Experiments with multicore fibers
- Coherent combining





Total internal reflection

• On the interface of two media, light refracts according to the Snell's law

$$rac{\sin heta_1}{\sin heta_2} = rac{n_2}{n_1}$$

- When n₁>n₂, above the critical angle, there is no solution
- Total internal reflection captures the light in medium with higher refraction index







Simple optical fibers – total internal reflection

- Total internal reflection captures the light in medium with higher refraction index
- The refraction index of silica glass is around 1.4 – 1.5, of air is 1
- Thin fibers of glass are flexible and can deliver light







images from Wikipedia



Optical fibers – structure

- Modern optical fibers do not rely on air, but instead have two or more layers with different refraction index
- The cladding diameter usually ranges between 100 and 500 µm
- Core diameter can be as small as a few wavelengths in singlemode fibers
- Modern fibers are cheap and have extremely low losses (0.2 dB/km)





Fibers in the lab



Optical fibers – types

- Multimode fibers have larger core size, different field patterns (modes) can propagate through the fiber
- In singlemode fibers, the core is thin, fields can only take a specific shape inside the fiber
- Multimode fibers handle much higher power, while singlemode fibers guarantee good beam quality





Fiber modes

- Helmholtz equation governs linear light propagation in a fiber
- Look for z-independent solution for E by separation of the variables
- For the shape *F* we get a boundary value problem, solvable in Bessel functions

$$\nabla^2 \tilde{\mathbf{E}} + n^2(\omega) \frac{\omega^2}{c^2} \tilde{\mathbf{E}} = 0$$

$$\tilde{E}_z(r,\omega) = A(\omega)F(\rho)e^{il\phi}e^{i\beta z}$$

$$\frac{d^2F}{d\rho^2} + \frac{1}{\rho} \frac{dF}{d\rho} + \left(n^2 k_0^2 - \beta^2 - \frac{l^2}{\rho^2}\right)F = 0$$



image from G. P. Agrawal, Nonlinear Fiber Optics



Fiber modes

- The parameter V shows the number of modes
- When V is below the critical value, the fiber is singlemode
- For singlemode: $a < \frac{2.405\lambda_0}{2\pi\sqrt{n_1^2 n_c^2}}$
- Example: 1550 nm

a < ???

$$n_1 - n_c = 0.005$$
$$n_c = 1.5$$

$$V = k_0 a \sqrt{n_1^2 - n_c^2} \qquad k_0 = \frac{2\pi}{\lambda_0}$$

 $V_c \approx 2.405$



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$$n_1 - n_c = 0.005$$

 $n_c = 1.5$
a < 4.8 µm

2009 Nobel Prize for groundbreaking achievements concerning the transmission of light in fibers for optical communication

$$= k_0 a \sqrt{n_1^2 - n_c^2}$$

 $V_c \approx 2.405$

V



Sir Charles Kao Kuen

Fiber lasers

- Three main parts of a laser are
 - Gain medium
 - Resonator
 - Pump
- Fibers can be doped to create gain medium
 - Er for 1550 nm
 - Yb for 1030 nm, etc
- Loop the fiber to create feedback
- Pumping can be done with laser diodes





Fiber lasers

- Simple, small, and robust
- Provide good beam quality
- High pumping efficiency
- Easy to cool down
- Easy to deliver the beam
- Typically, low peak power



Fluorescence of Er-doped fiber laser



Fiber lasers



10 kW ytterbium-doped fiber laser system

Nikolay Kalinin | EASSOL | Nairobi, Kenya | 08.05.2024



Fluorescence of Yb-doped fiber amplifier through IR viewer



Fluorescence of Er-doped fiber laser



High-power fiber lasers

- Master oscillator, power amplifier scheme (MOPA)
- CW fiber lasers reach 10-100 kW

- In pulsed regime, peak power is limited by nonlinear effects
- Chirped-pulse amplification (CPA) is useful
 - stretching and amplifying in the fiber
 - compressing in free space



Progress of CW fiber lasers

image from M. N. Zervas, C. A. Codemard, IEEE J. Sel. Top. Quantum Electron., 20(5), 219, 2014 13



Kerr effect

- When the electric field is strong enough, the induced polarization in the medium is no longer proportional to the electric field
- In isotropic media such as glasses, the thirdorder nonlinearity is the lowest
- The change can be induced both by external electric field and by self-action (optical Kerr effect)
- Effectively, the refraction index is changed proportionally to the intensity
- Kerr effect leads to a number of effects in time and space

$$\mathbf{P}(t) = arepsilon_0 \left(\chi^{(1)} \mathbf{E}(t) + \chi^{(2)} \mathbf{E}^2(t) + \chi^{(3)} \mathbf{E}^3(t) + \ldots
ight),$$

$$\tilde{n} = n + \bar{n}_2 |E|^2$$



Self-focusing

- Kerr effect leads to self-focusing in fibers
 - Refraction index in the center is increased due to the Kerr effect
 - Light is more tightly focused due to the changes in refraction index
 - Positive feedback is created
- At low power, diffraction is stronger
- Above critical power, the beam collapses
- Critical power is at the order of MW for silica fibers

- Example:
 - 400 fs sech-shaped pulses
 - Average power 400 mW
 - Repetition rate 0.5 MHz
 - Peak power 1.7 MW
- Possible solutions:
 - coherent combining
 - special fibers



Multicore fibers

- It is possible to create fibers with more than one core
- If the cores are far apart, light propagates in each core independently
 - Effectively, N individual fibers in a single bundle
 - Allows for power scaling, but phase stabilization is required
- If the cores are close to each other, light propagates coherently in all cores
 - Phase is stable
 - Nonlinear effects on a larger scale







Supermodes in coupled-core MCFs

- In weakly coupled MCFs, fields can be approximated by the sum of fields of modes in each core, with some coefficients
- Due to overlap, the equations for the envelope in each mode are coupled

$$\frac{dA_i(z)}{dz} = i\Delta\beta_i A_i(z) + \sum_{j\neq i} ic_{ij}A_j$$

• In matrix form,

$$\frac{dA}{dz} = iCA, \quad C = \begin{pmatrix} \Delta\beta_1 & c_{12} & \cdots & c_{1N} \\ c_{21} & \Delta\beta_2 & \cdots & c_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ c_{N1} & c_{N2} & \cdots & \Delta\beta_N \end{pmatrix}$$



Supermodes in coupled-core MCFs

• The eigenvalues of A are called supermodes

$$\frac{dA}{dz} = iCA$$

• In MCF with N single-mode cores there are N supermodes





Excitation and analysis of supermodes in an MCF



25-core MCF





Excitation and analysis of supermodes in an MCF



6-core MCF







Excitation and analysis of supermodes in an MCF

- We used stochastic gradient descent to find an SLM phase mask to maximize selectivity of out-of-phase and in-phase supermodes excitation
- 90% of pulse energy in the out-ofphase supermode achieved





N. A. Kalinin, et al. Photonics, 8, 314, 2021



2x critical power

High-power stability

- Discrete self-focusing effect can limit total power in MCF, as in the in-phase supermode regime.
- However, in nonlinear regime of the out-of-phase supermode power in cores equalizes, allowing for high peak power.





Out-of-phase supermode amplification, 6-core MCF

- Pulse energy up to ~0.9 μJ
- Pulse duration ~50 ps
- Estimated peak power ~18 kW



A. V. Andrianov, et al. J. Light. Technol., 38(8), 2464, 2020







Coherent beam combining (CBC)

• Another approach for high power lasers is to combine many beams into a single one





Coherent beam combining (CBC)

• Most versatile approach is tiled aperture





Coherent beam combining (CBC)

- The channels need to be in phase
- Phase stabilization system up to 10 kHz bandwidth is needed



7-core Yb-doped independent-core MCF: near field, far field no phase control, in-phase far field

image from Ramirez L P et al 2015, Opt. Exp. 23 5406–16



Out-of-phase tiled aperture CBC

• Flipping the phase of every second beam is more efficient





Coherent combining of the out-of-phase supermode

- Use the out-of-phase regime of tiled aperture scheme
- No lens array is needed because of high fill factor
- Combining efficiency 93%, M²=1.09 (simulation)





Coherent combining of the out-of-phase supermode

- Two steps of combining, a delay line to match group delay, and a wedge to match phase in each step
- Combining efficiency 73%, M² = 1.3 (experiment)





N. A. Kalinin, et al. Opt. Express, 30, 1013, 2022



Thank you!

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