



Next-generation climate modeling with new tools: leveraging the AI revolution



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Outline

1. Introduction: climate uncertainties and the role of subgrid processes
2. AI: from climate process emulation
to new discoveries
3. Solutions and challenges for next-generation climate models
4. A vision for next-generation climate models



Current gap: Climate Adaptation is Needed



But adaptation requires:

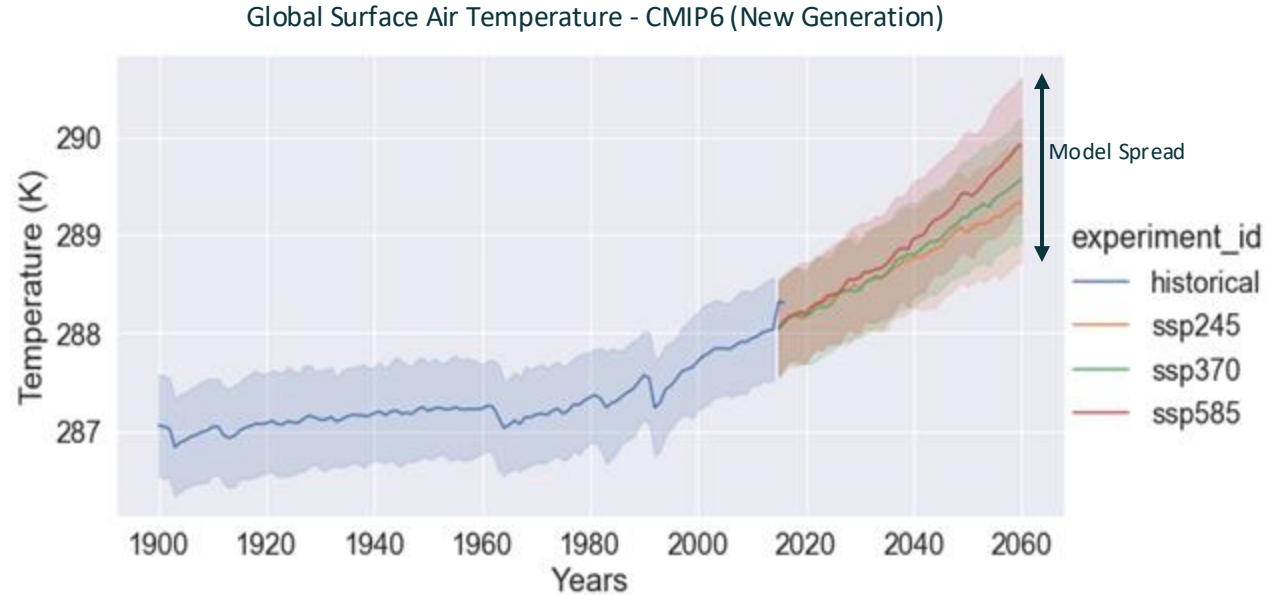
- Accurate information (projection) about the future using climate models
- Broadly and easily accessible climate projection information (outreach, LEAP-Pangeo platform not covered today)





Yet, current projections are still too uncertain

Even for (simple) global metrics such as surface temperature

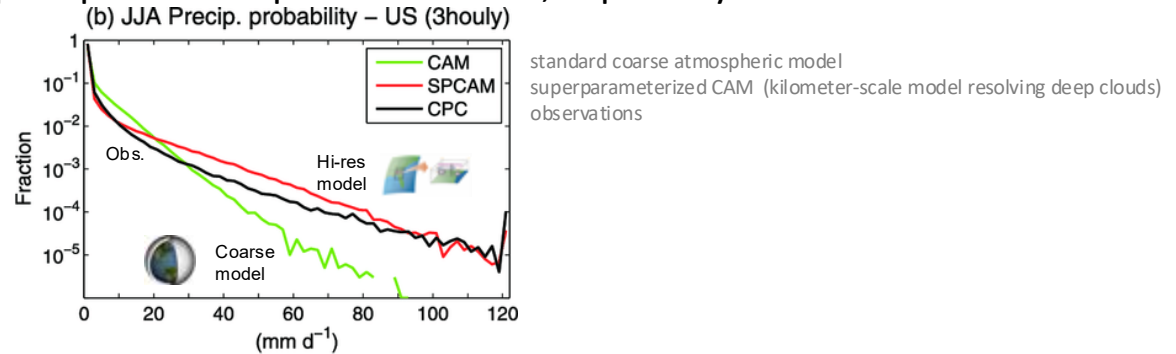


*note it takes 5 minutes to plot this with modern cloud data infrastructure (LEAP-Pangeo)

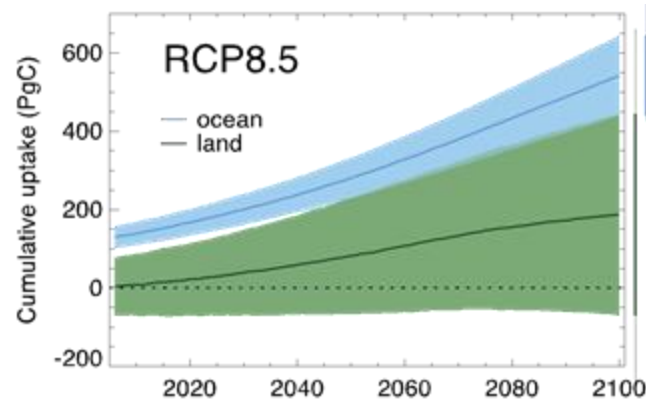


Regional climate and carbon cycles are even more uncertain

- Regional precipitation is quite inaccurate, especially for extremes

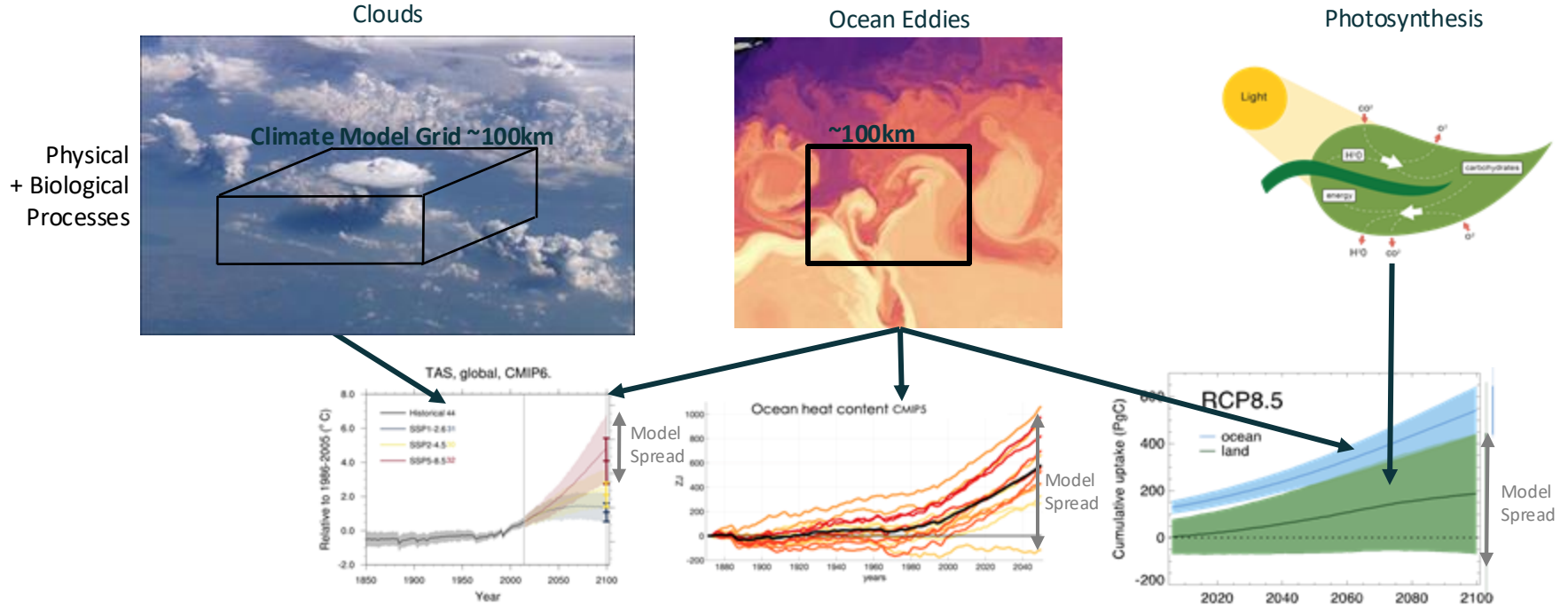


- Future of carbon cycle





Unresolved or Unknown processes Require “Parameterizations” Causing Projection Uncertainties



- Model errors dominate (>50%) uncertainties <50 years

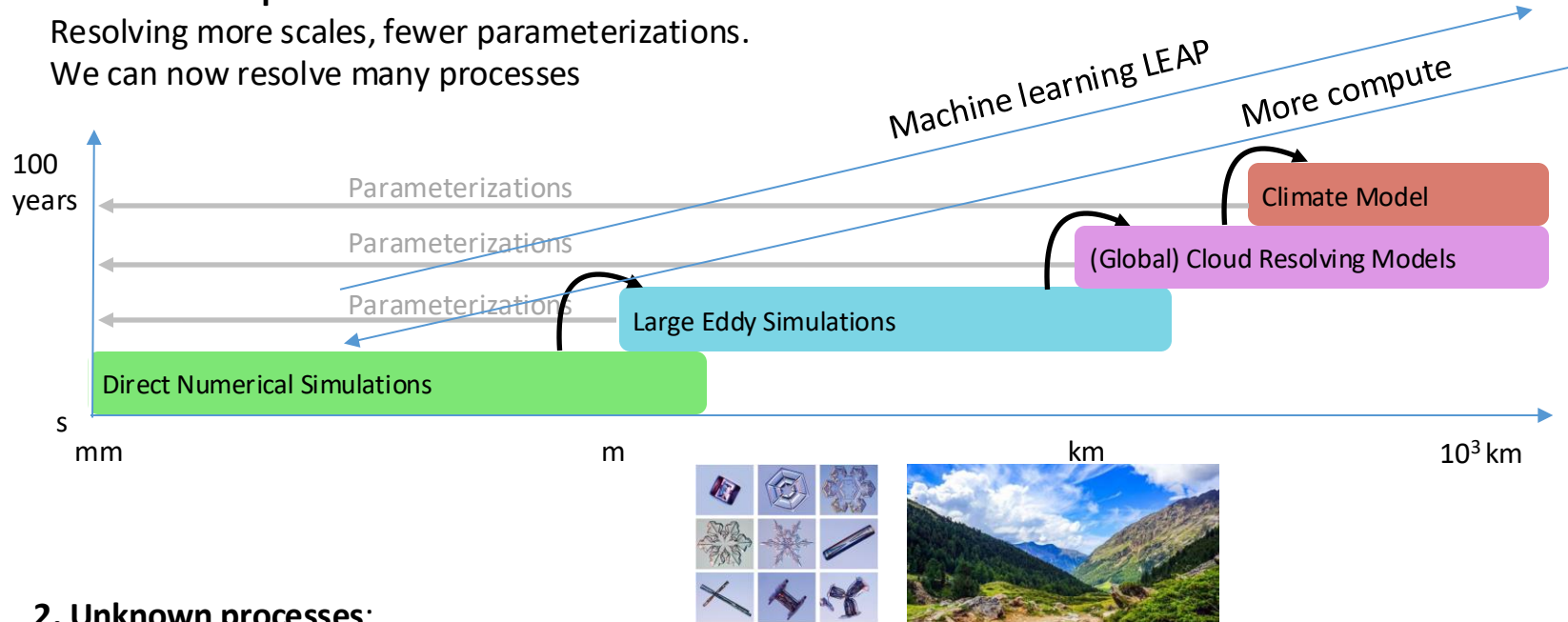


Strategies to improve climate modeling

1. Unresolved processes:

Resolving more scales, fewer parameterizations.

We can now resolve many processes



2. Unknown processes:

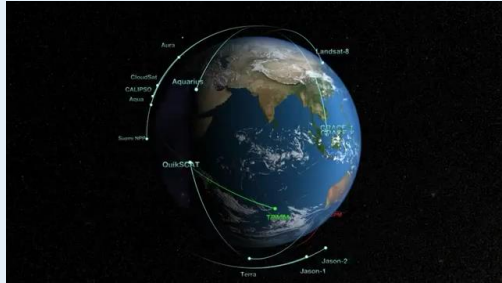
Many processes cannot be simulated: microphysics, biogeochemistry

→ Use observations (in situ, remote sensing) to learn processes

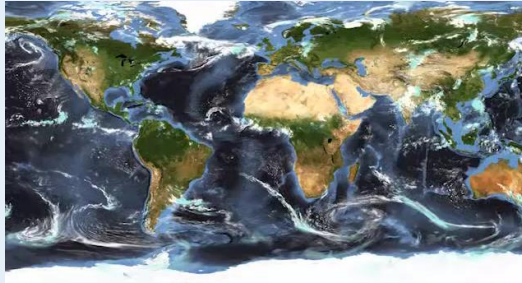


Harvesting the Data Revolution to improve parameterizations

1. Massive data from Earth observation



2. High-resolution simulations



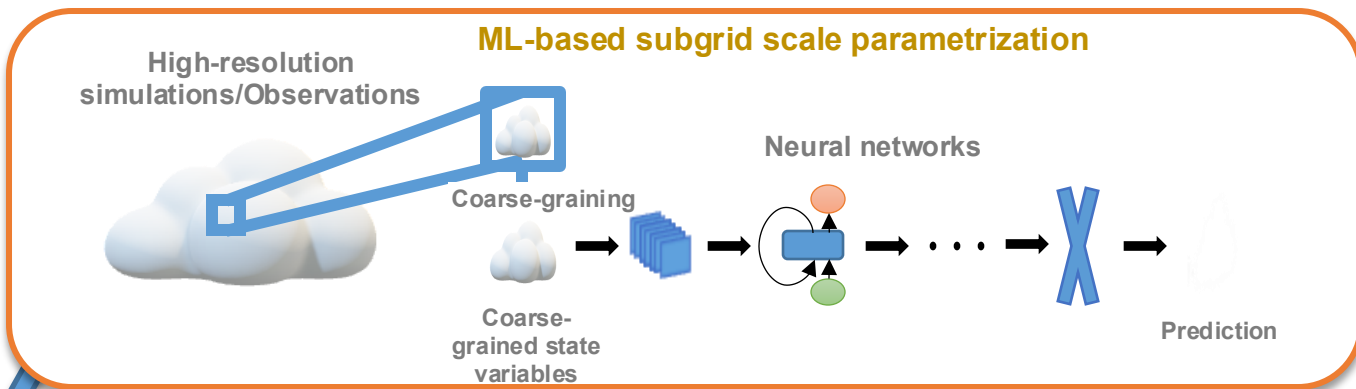
3. Progress in machine learning



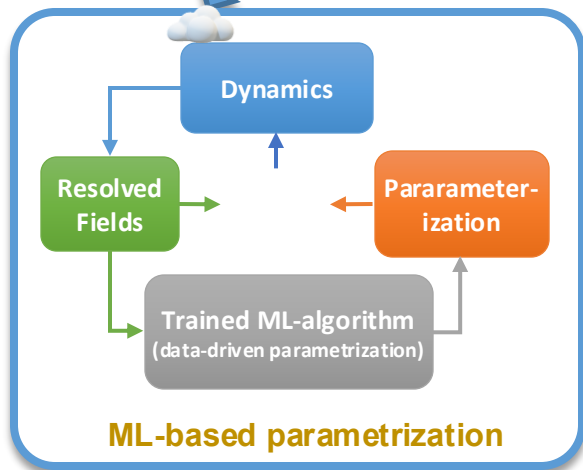


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Improved climate projections



Phenology

Modeling the Climate System

Radiation

Land-atmosphere exchange

Clouds

Turbulence

Snow water equivalent forecast

Wildfire risk and impacts

Burned area

Fire hazard

None of those processes (besides deep convection) are resolved in high-resolution cloud-resolving models!

Includes the Atmosphere, Land, Oceans, Ice, and Biosphere

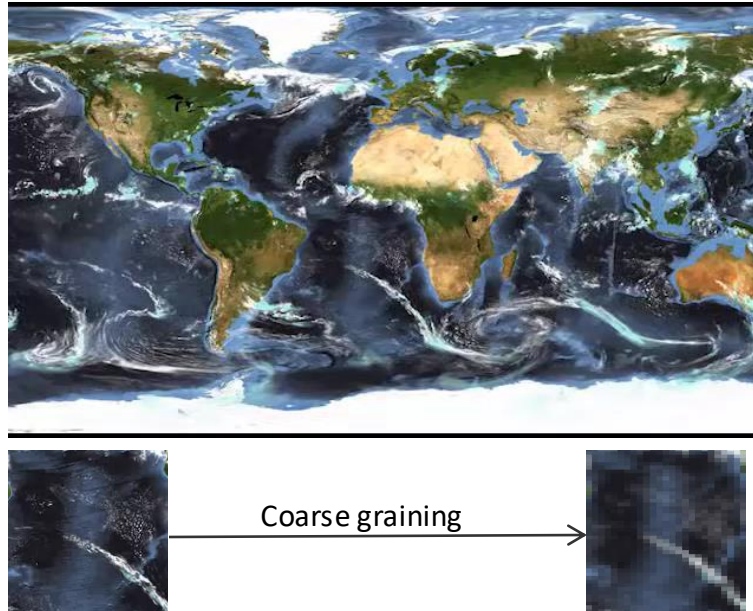
Zhao et al. 2019 GRL; El Ghawi et al 2023 ERL; Buch et al. 2023 GMD; Shamekh et al; JAMES in review; Lahlou et al. in prep

**None of those processes
(besides deep convection)
are resolved in high-resolution cloud-resolving models!**



Learn subgrid convection parameterization with machine learning

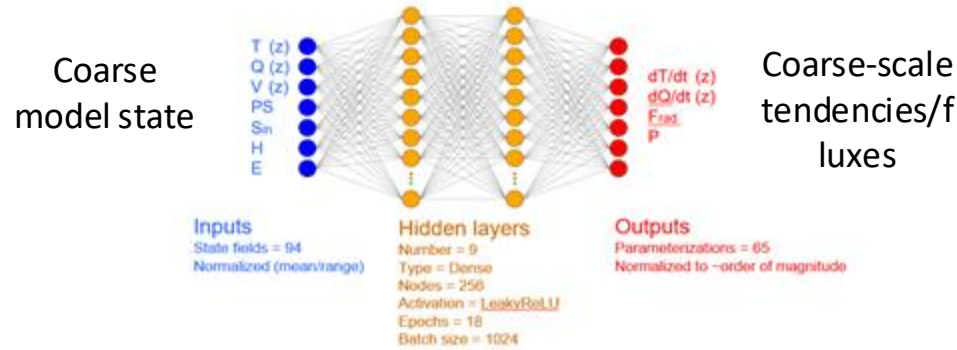
- Main strategy: use high-resolution cloud-resolving model (few kms) data as “training” for closure development (supervised learning) at coarse resolution
- Multi-institution, inter-disciplinary, international efforts: LEAP/USMILE ERC/M²LinES



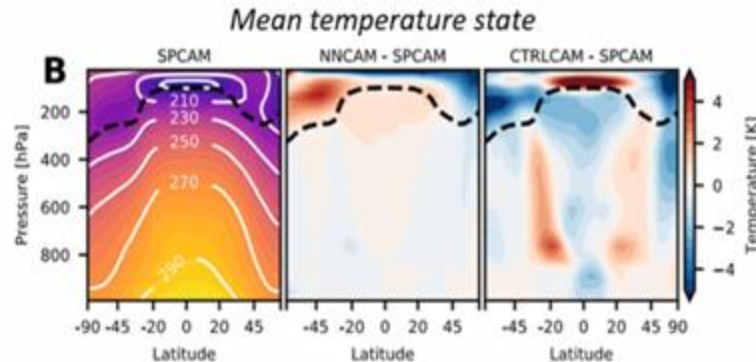


Learn subgrid convection closures with machine learning

- Main strategy: use high-resolution cloud-resolving model (few kms) data as “training” for closure development (supervised learning) at coarse resolution



Online
Aquaplanet
(NCAR CAM)



Temperature
profiles



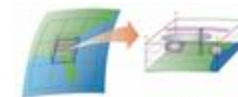
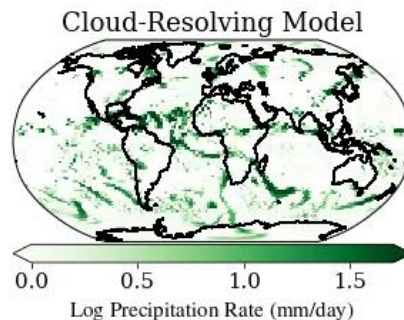
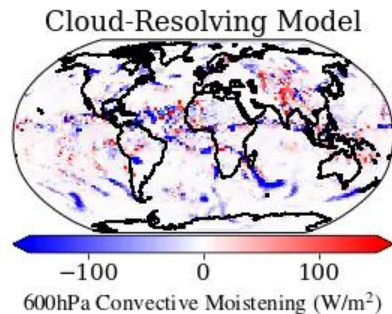
Successful Emulation of Convection on “real geography”

Real geography results in *Offline* Community Atmosphere Model (CAM)

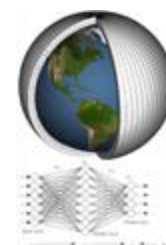
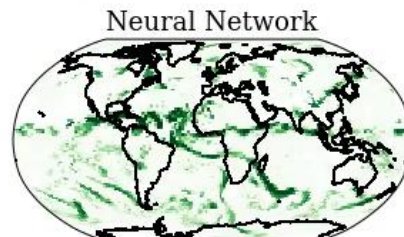
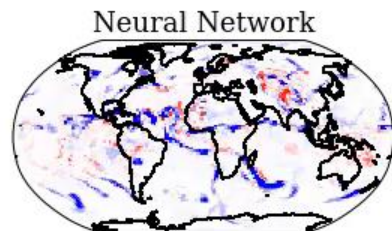
Online in ICON with Max Planck/DLR



Truth
Super-param.
(SPCAM)
simulation



Prediction
NN



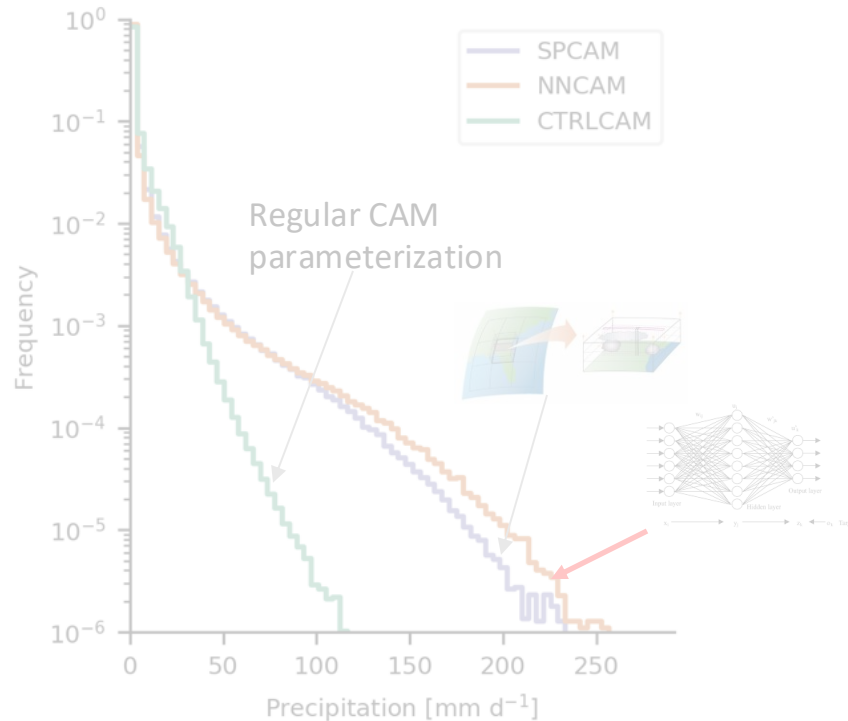
Skillful convection emulation with continents



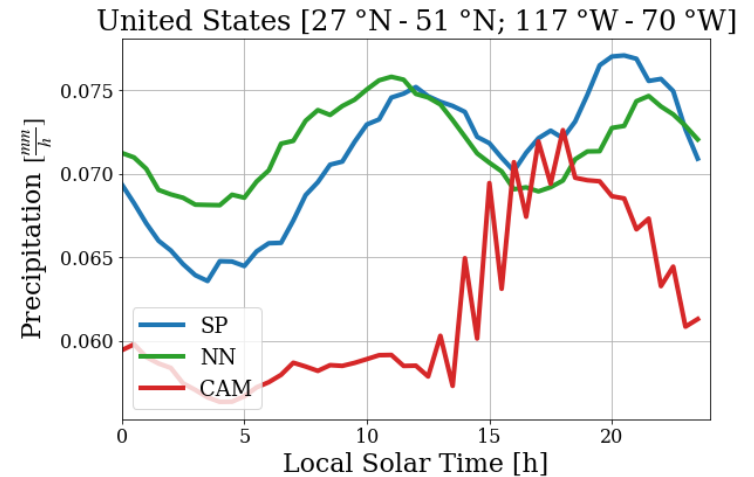
Inclusion of ML parameterizations leads to **Step-change** in climate model quality

Online global simulations 

Precipitation distribution (CAM)

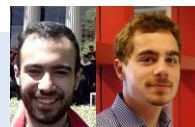


Precipitation diurnal cycle (CAM+ICON)

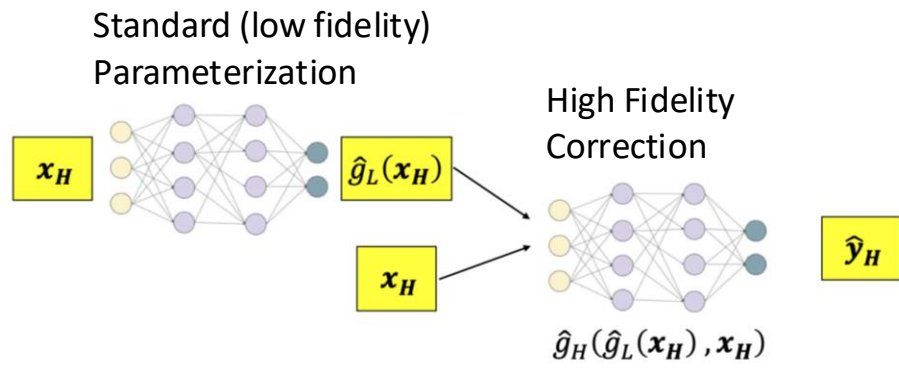




Main Challenge for ML: Generalization



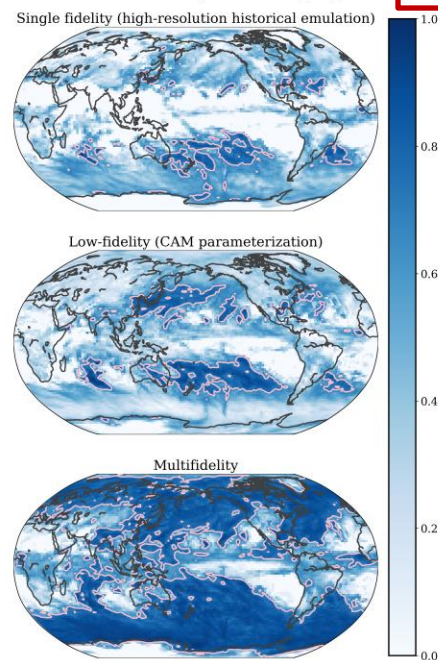
- Challenge: out-of-distribution prediction: climate change
 - Solution: **Hybrid Multifidelity approach**: merges physics with ML to extrapolate (online with MeteoFrance to improve subseasonal/seasonal forecast)
- Best of both worlds



Other strategies:

- embedding physical invariances
- merging causality & ML

R^2 of moisture tendency on future projection (+4K)

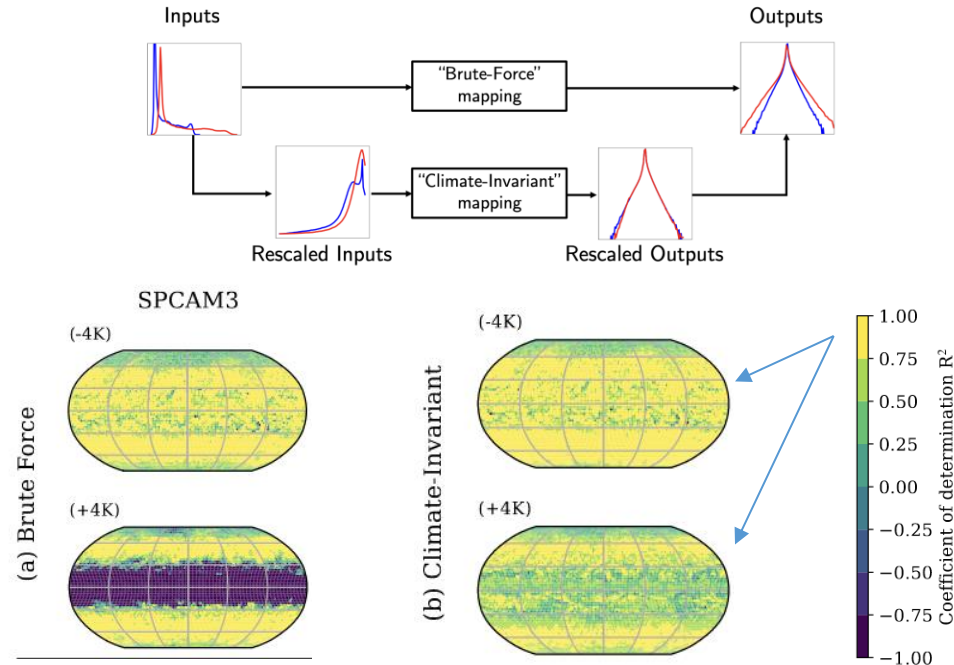




Trust, interpretability, generalization

Challenge 1: Generalization

- Challenge: out-of-sample, out-of-distribution prediction/sampling bias
- Solution: **embed physical invariances/equivariance** along Lie groups in ML (e.g., dimensionless numbers or rotational equivariance to collapse distributions)



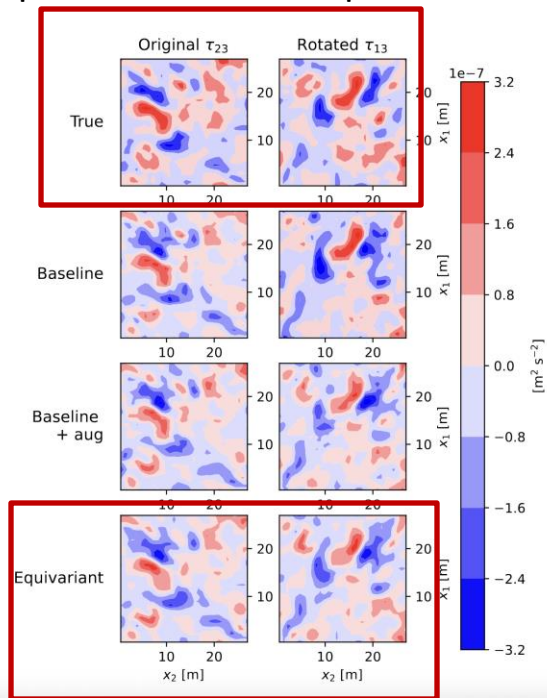


Trust, interpretability, generalization

Challenge 1: Generalization

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$$f(\rho_{\text{in}}(g)x^*) = f(x^*)$$



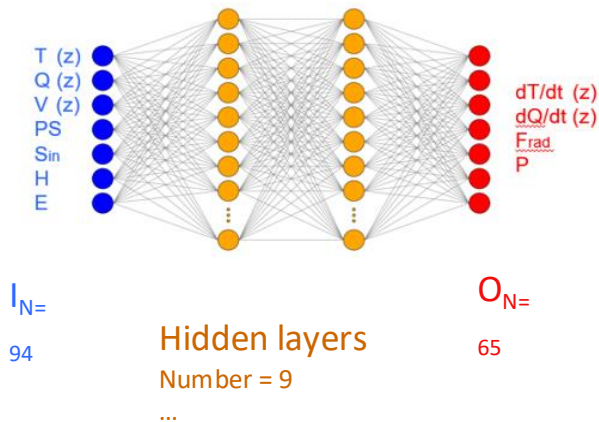


Trust, interpretability, generalization

Challenge 2: Trust + interpretability

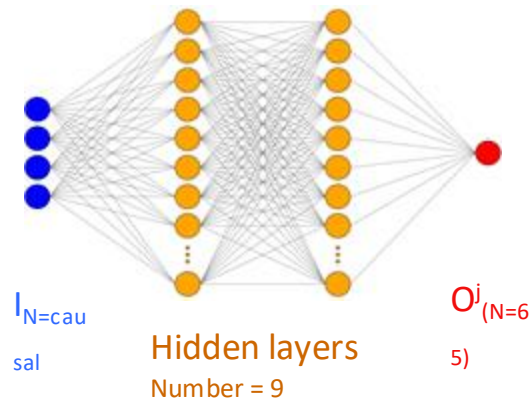
- Challenge: cross-correlations can fool ML
- Solution: merge **causal discovery with ML**
→ more interpretable, more trustworthy

NN (Rasp et al., 2018)



Drop connections based on causality: a very sparse NN

Causal-NNs

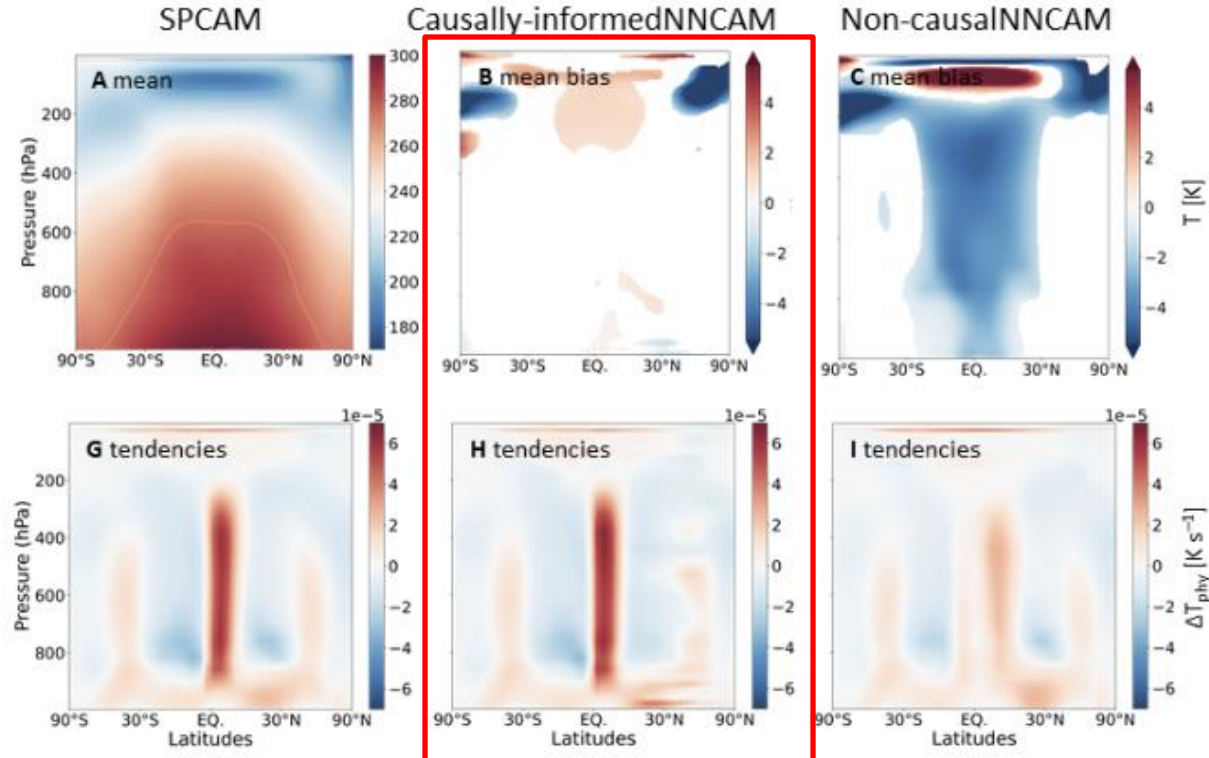


$$I_{causal}^i \rightarrow O_j \in P(O_j)$$



Causality: going beyond correlations

Online global simulations





Journey through the use of ML in climate science

Journey through ML use: a roller coaster 🎢

Initial work:

- Correct emulation of convection 🙌 🍷 🍌
- But cannot generalize, may lack stability, misses physical invariances 🐒 😬 😞

Recent work focusing on:

- Embedding physical invariances improves model stability, including causality and generalization 👍

More fundamentally, what did we (really) learn? 🧐 ♂

- Using machine learning for new **discoveries** 🌟



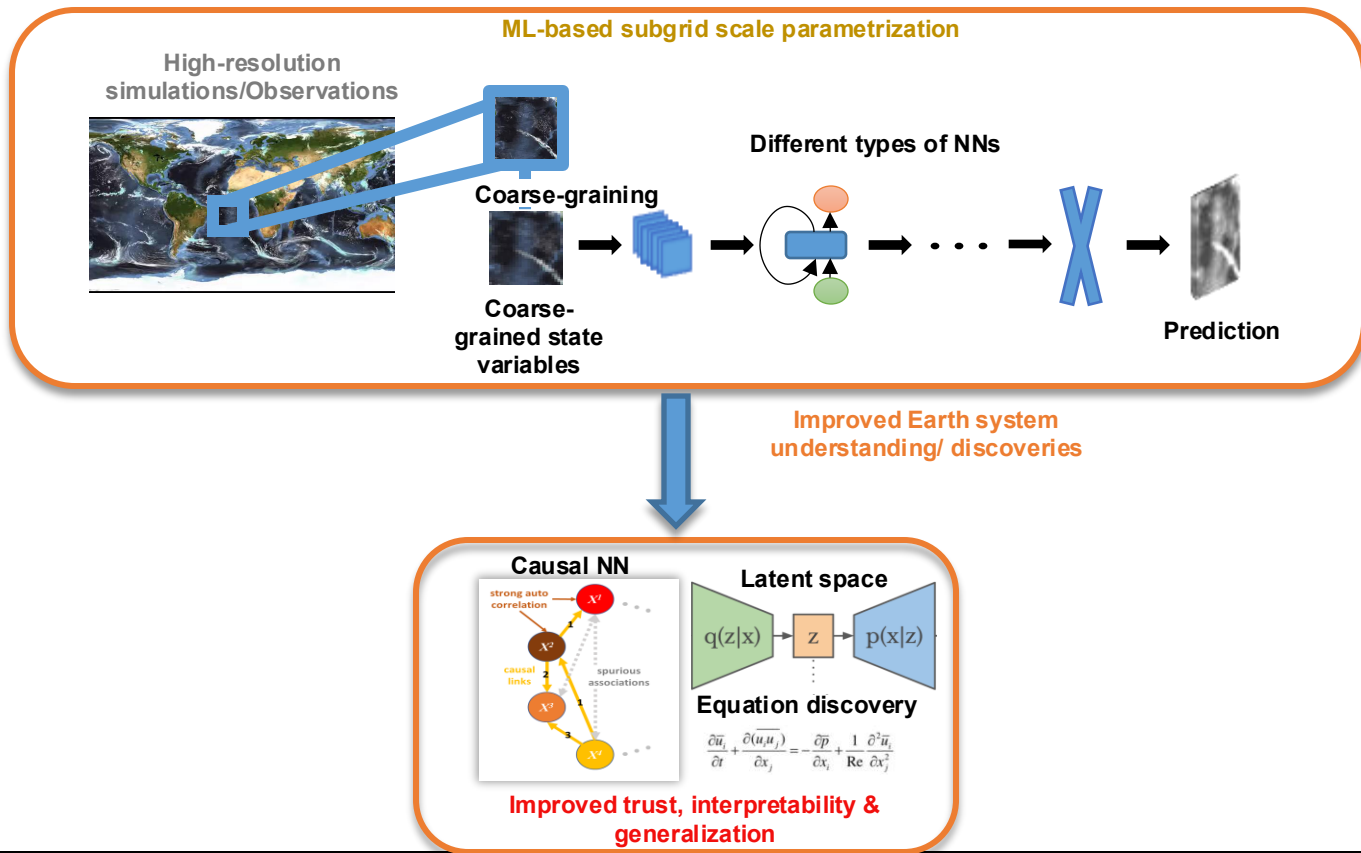
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From emulation to understanding

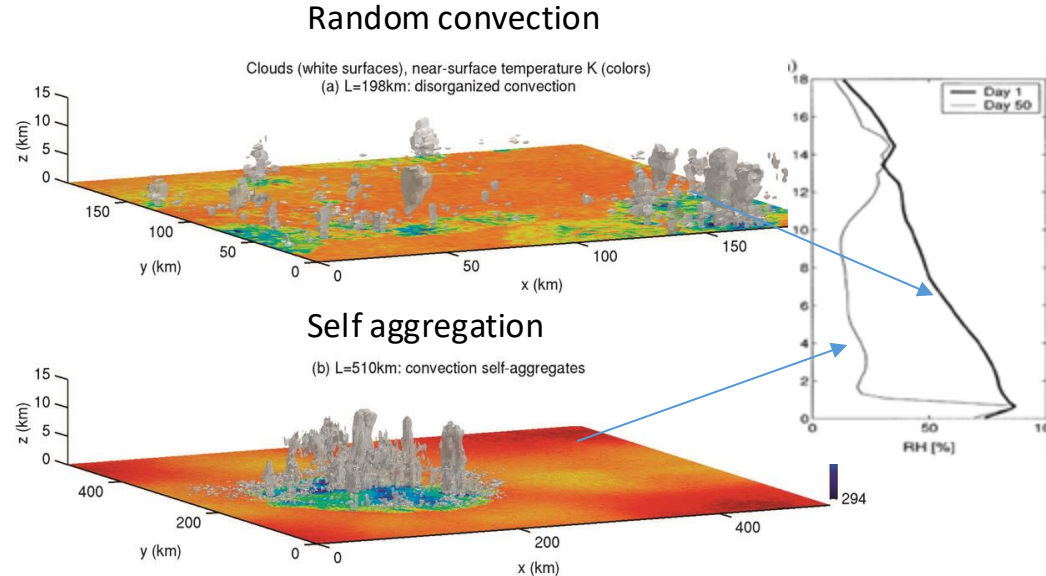
Data analysis is extremely challenging in high-res simulations and remote sensing (size)





New discoveries 1: Cloud organization

- Convection can **aggregate**
- Aggregation has a large impact on:
 - Humidity
 - Enhances radiative cooling
 - Potentially impacts climate sensitivity
 - Precipitation
 - Increases accumulated precipitation





Can we learn the implicit role of subgrid (micro) scale on precipitation?

- Science questions:
 - Does $P = F(X \text{ coarse-scale, } \text{microscale subgrid scale stuff})$ improve prediction?
 - Can we explain (some of) the **stochasticity**? Still unclear how to model it.

STOCHASTIC PARAMETERIZATION

Toward a New View of Weather and Climate Models

JUDITH BERNER, ULRICH ACHATZ, LAURIANE BATTÉ, LISA BENGTTSSON, ALVARO DE LA CÁMARA,
HANNAH M. CHRISTENSEN, MATTEO COLANGELI, DANIELLE R. B. COLEMAN, DAAN CROMMELIN,
STAMEN I. DOLAPTCHIEV, CHRISTIAN L. E. FRANZKE, PETRA FRIEDERICH, PETER IMKELLER, HEIKKI JÄRVINEN,
STEPHAN JURICKE, VASSILI KITSIOS, FRANÇOIS LOTT, VALERIO LUCARINI, SALIL MAHAJAN, TIMOTHY N. PALMER,
CÉCILE PENLAND, MIRJANA SAKRADZIJA, JIN-SONG VON STORCH, ANTJE WEISHEIMER,
MICHAEL WENIGER, PAUL D. WILLIAMS, AND JUN-ICHI YANO

Stochastic parameterizations—empirically derived or based on rigorous mathematical and statistical concepts—have great potential to increase the predictive capability of next-generation weather and climate models.



Using high-res models to learn the role of subgrid microscale on P

- Data:
DYAMOND Storm-resolving model experiment
Tropical band (20S-20N), ~2.5km resolution,
10 days of simulations
 10^8 data points

→ Predicting precipitation



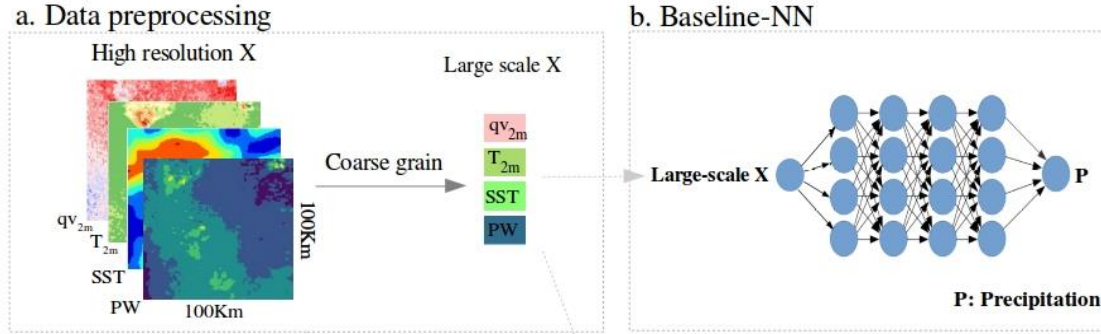
Coarse graining





The inner gut: learning organization end-to-end

- Strategy: Learning precipitation and organization (implicitly) in tandem





Learnt organization dramatically improves precipitation predictions

- Precipitation and its stochasticity are very well predicted with org



What did we learn?

- ✓ Organization regulates precipitation extremes and their prediction
- ✓ Precipitation stochasticity is mainly due to convective aggregation



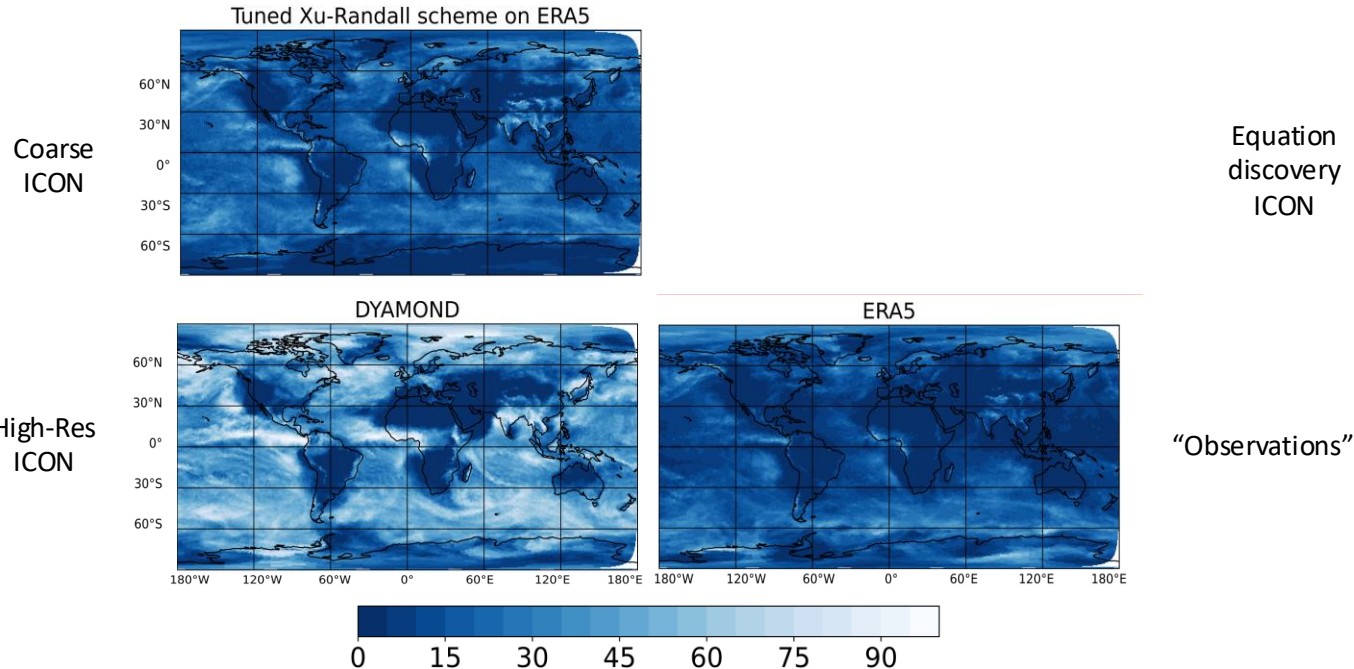
New discoveries 2: Symbolic regression – equation discovery

- Example for ICON (offline) **cloud cover**
- Projection on library of functions

More interpretable, more trustworthy. Improve upon high-res ICON model.

$$C = P_3(RH, T) + (c_1 \partial_z RH + c_2)(\partial_z RH)^2 - \frac{1}{c_3 q_c + c_4 q_i + \varepsilon}$$

Cloud cover [%]





Machine learning improves climate model processes and understanding

Machine learning can improve the representation of subgrid processes in climate models and **leap across scales**

ML closures are *working now* in full climate models (CAM/ICON) with leap in accuracy and major reduction in biases (implementation at a pace faster than climate change).

→ Not a hypothesis anymore.

Still some challenges – several of them discussed in this talk.

Machine learning can be used for **new discoveries** on big data.



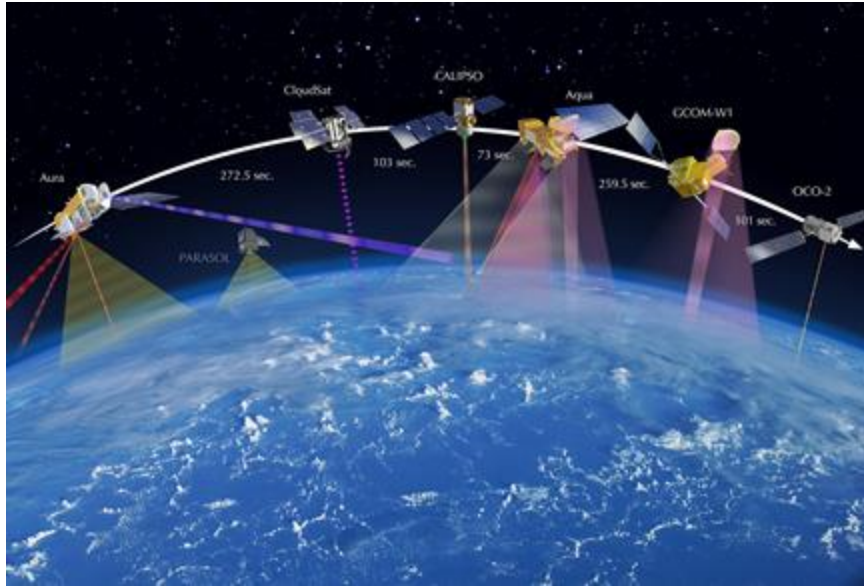
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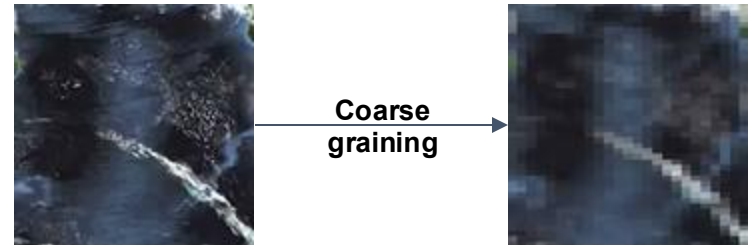


How can we improve climate projections?

Solution 1. Using AI to harvest the data revolution: high-resolution simulations or Earth's observations to better emulate processes



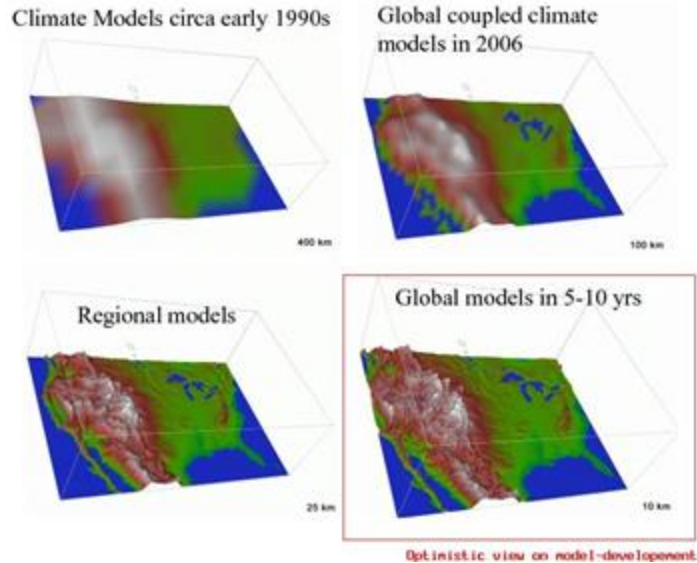
Challenge: Climate models cannot easily integrate AI (old languages like Fortran) and assimilate data
→ Difficult to harvest the data revolution



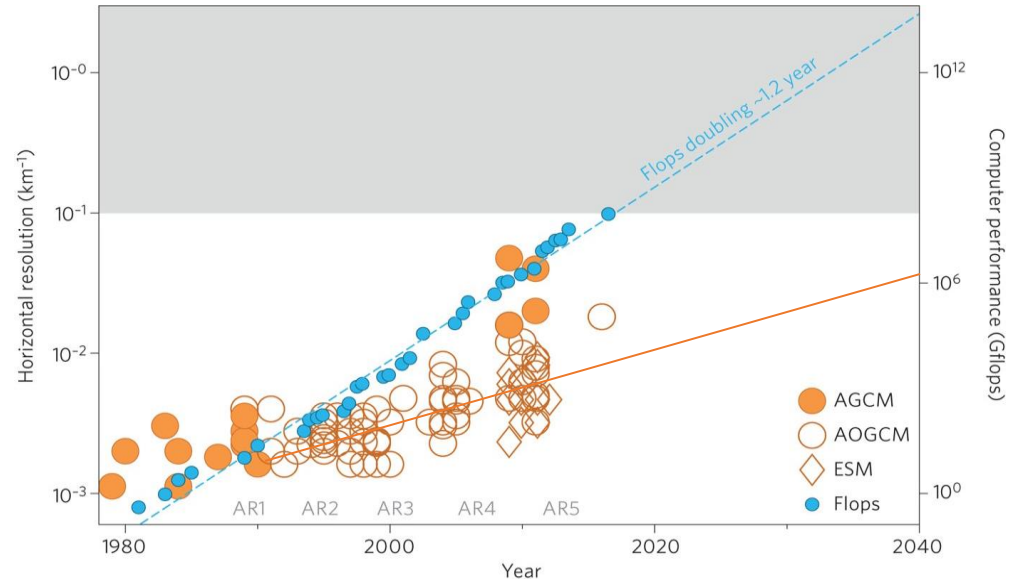


How can we improve climate projections?

Solution 2. Increasing compute to better resolve processes: Exponential cost with resolution



Challenge: Climate models do not leverage modern hardware GPUs or TPUs and are based on old hardware infrastructure (CPUs). Legacy of low-level Fortran code, not agile to different hardware, plateauing performance



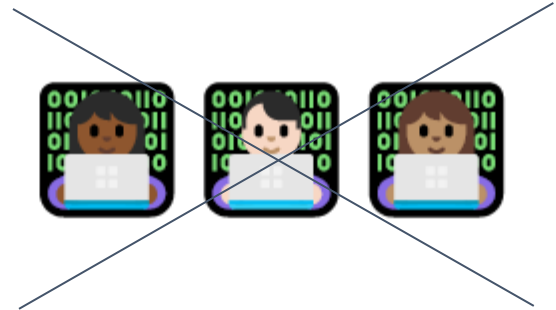


How can we improve climate projections?

Solution 3. Accelerate progress on climate model developments and theories

$$\frac{\partial \vec{v}_h}{\partial t} + (\vec{v} \cdot \nabla) \vec{v}_h + f \hat{k} \times \vec{v}_h + \frac{1}{\rho_0} \nabla_h p' = \vec{F}$$
$$\nabla_h \cdot \vec{v}_h + \frac{\partial w}{\partial z} = 0$$

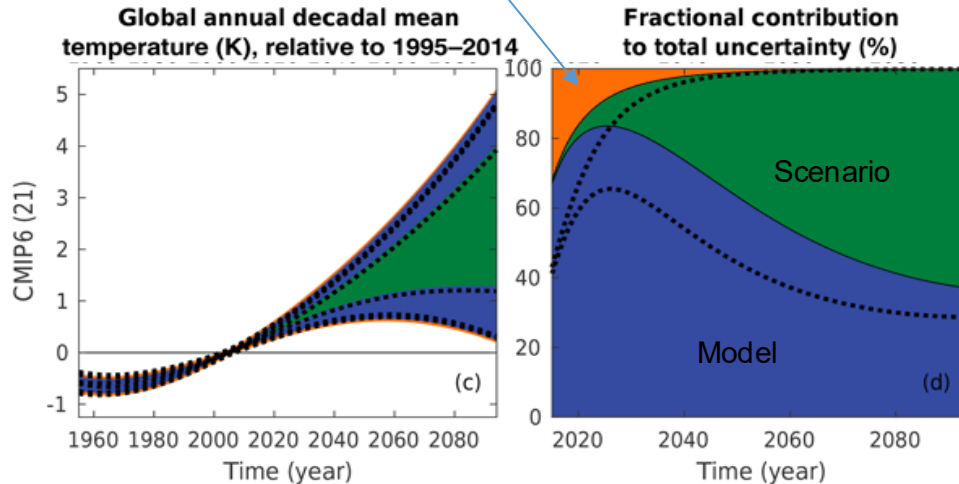
Challenge: Climate models are based on old programming languages and are very difficult to use → **not inclusive:** huge barrier to progress



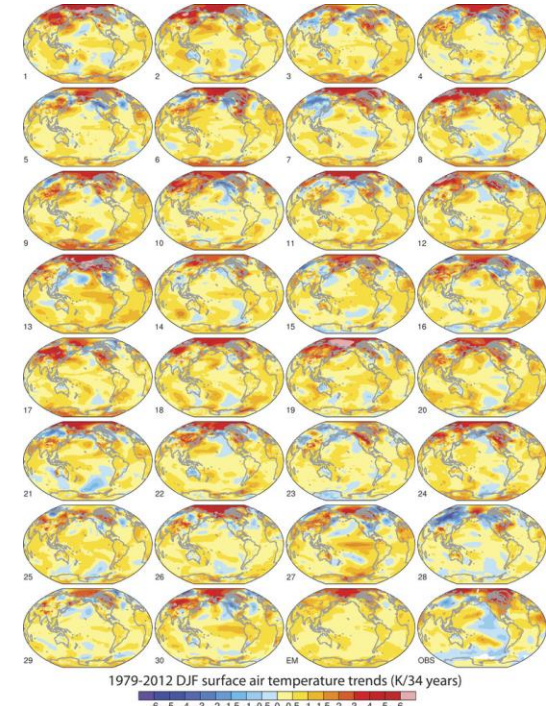


How can we improve climate projections?

Solution 4. Accurate quantification of internal variability (and extremes)



Challenge: Computationally expensive – tradeoff between resolution and ensemble members





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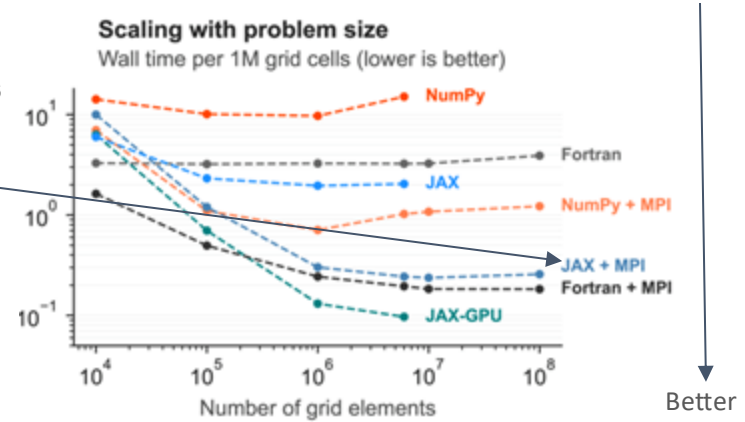


A vision for next-generation climate modeling

THREE PILLARS

1. Modern code & compute:

Python-based: more inclusive
+ JAX /GT4Py for fast compute (GPUs)





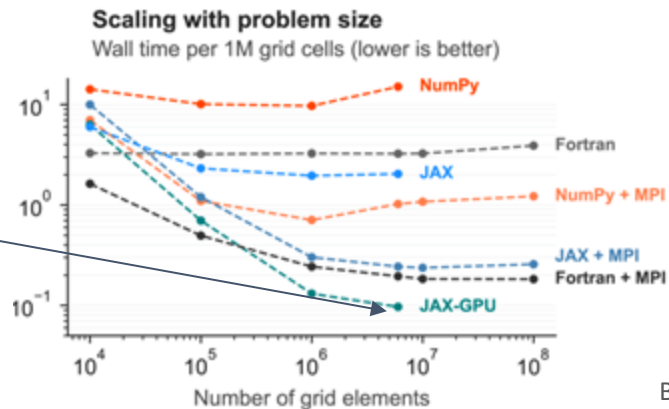
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Better



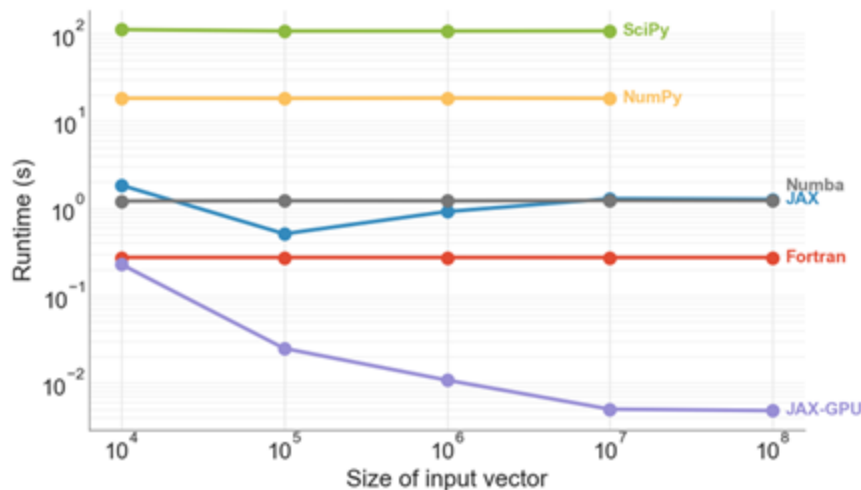
How can we convert codes (faster)?

Generative AI with human-in-the-loop can help translate code faster: test on Community Land Model

```
1 subroutine ci_func(ci, fval, p, iv, c, gb_mol, je, cair, oair, lmr_z, par_z,  
2 rh_can, gs_mol)  
3  
4 !! DESCRIPTION:  
5 ! evaluate the function  
6 ! f(ci)=ci - (ca - (1.37rb+1.65rs))+patmean  
7  
8 !! ARGUMENTS:  
9 real(r8), intent(in) :: ci ! Intracellular leaf CO2  
10 (Pa)  
11 real(r8), intent(in) :: lmr_z ! canopy layer: leaf  
12 maintenance respiration rate (umol CO2/m**2/s)  
13 real(r8), intent(in) :: par_z ! par absorbed per unit  
14 lai for canopy layer (w/m**2)  
15 real(r8), intent(in) :: gb_mol ! leaf boundary layer  
16 conductance (umol H2O/m**2/s)  
17 real(r8), intent(in) :: je ! electron transport rate  
18 (umol electrons/m**2/s)  
19 real(r8), intent(in) :: cair ! Atmospheric CO2 partial  
20 pressure (Pa)  
21 real(r8), intent(in) :: oair ! Atmospheric O2 partial  
22 pressure (Pa)  
23 real(r8), intent(in) :: rh_can ! canopy air relative  
24 humidity  
25 integer, intent(in) :: p, iv, c ! pft, vegetation type and  
26 column indexes  
27 real(r8), intent(out) :: fval ! return function of the  
28 value f(ci)  
29 real(r8), intent(out) :: gs_mol ! leaf stomatal  
30 conductance (umol H2O/m**2/s)  
31 !type(atm2lnd_type), intent(in) :: atm2lnd_inst  
32 !type(photosyns_type), intent(inout) :: photosyns_inst  
33  
34 !local variables  
35 real(r8) :: ai ! intermediate co-limited photosynthesis  
36 (umol CO2/m**2/s)  
37 real(r8) :: cs ! CO2 partial pressure at leaf surface (Pa)
```



Scaling with problem size
Runtime per 1M computations





A vision for next-generation climate modeling

THREE PILLARS

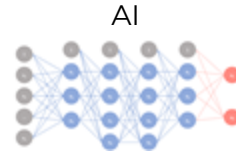
1. Modern code & compute:

Python-based: more inclusive
+ JAX /GT4Py for fast compute (GPUs)



2. Seamless AI-integration:

hybrid Earth system model: unify physics and AI



Physics

$$\begin{aligned}\frac{Du}{Dt} &= \frac{uv \tan \phi}{r} - \frac{uw}{r} + fv - f'w - \frac{c_p \theta}{r \cos \phi} \frac{\partial \Pi}{\partial \lambda} + D(u) \\ \frac{Dv}{Dt} &= -\frac{u^2 \tan \phi}{r} - \frac{vw}{r} - uf - \frac{c_p \theta}{r} \frac{\partial \Pi}{\partial \phi} + D(v), \\ \frac{\delta Dw}{\delta r} &= \frac{u^2 + v^2}{r} + uf' - g(r) - c_p \theta \frac{\partial \Pi}{\partial r},\end{aligned}$$



A vision for next-generation climate modeling

THREE PILLARS

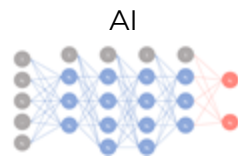
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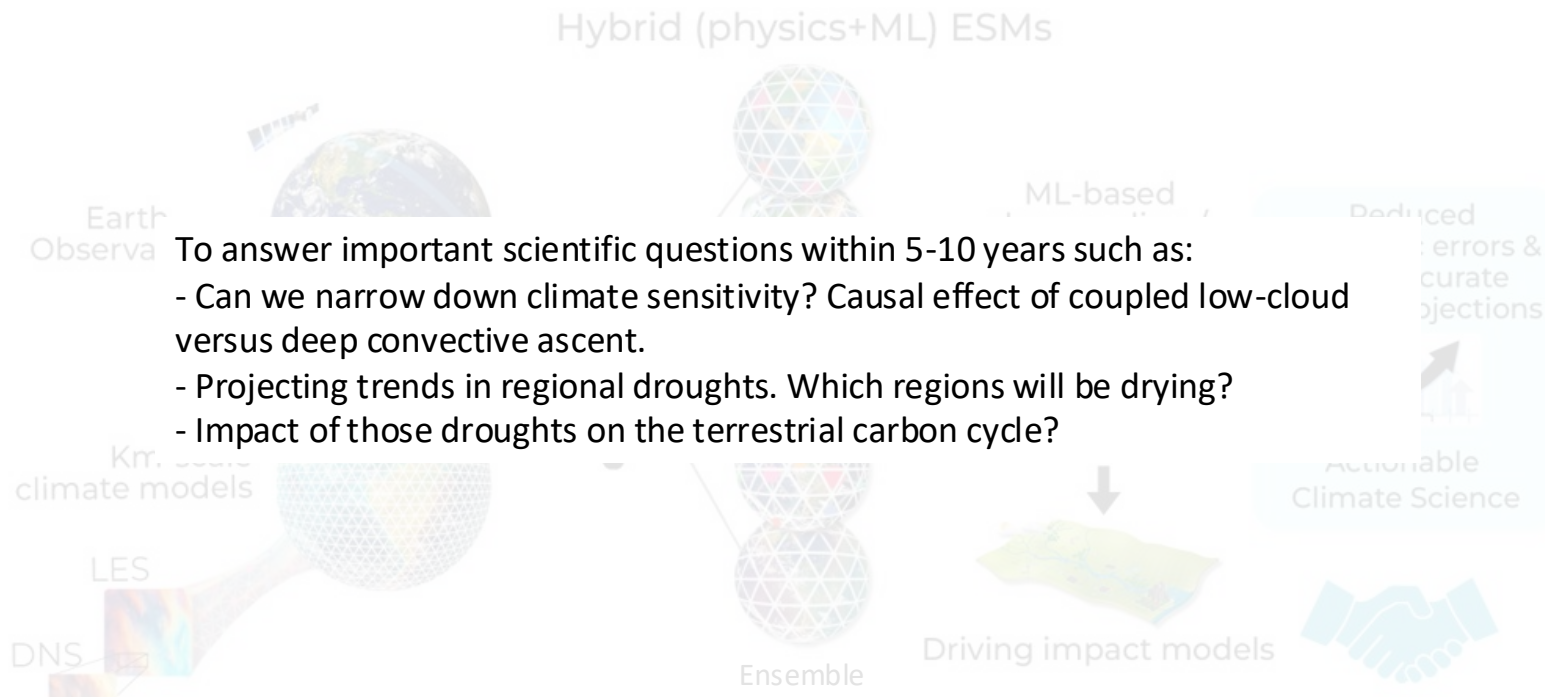
3. Harnessing global observations:

with new data assimilation
- targeting statistics (e.g. precipitation distribution)
- even high-res models are imperfect





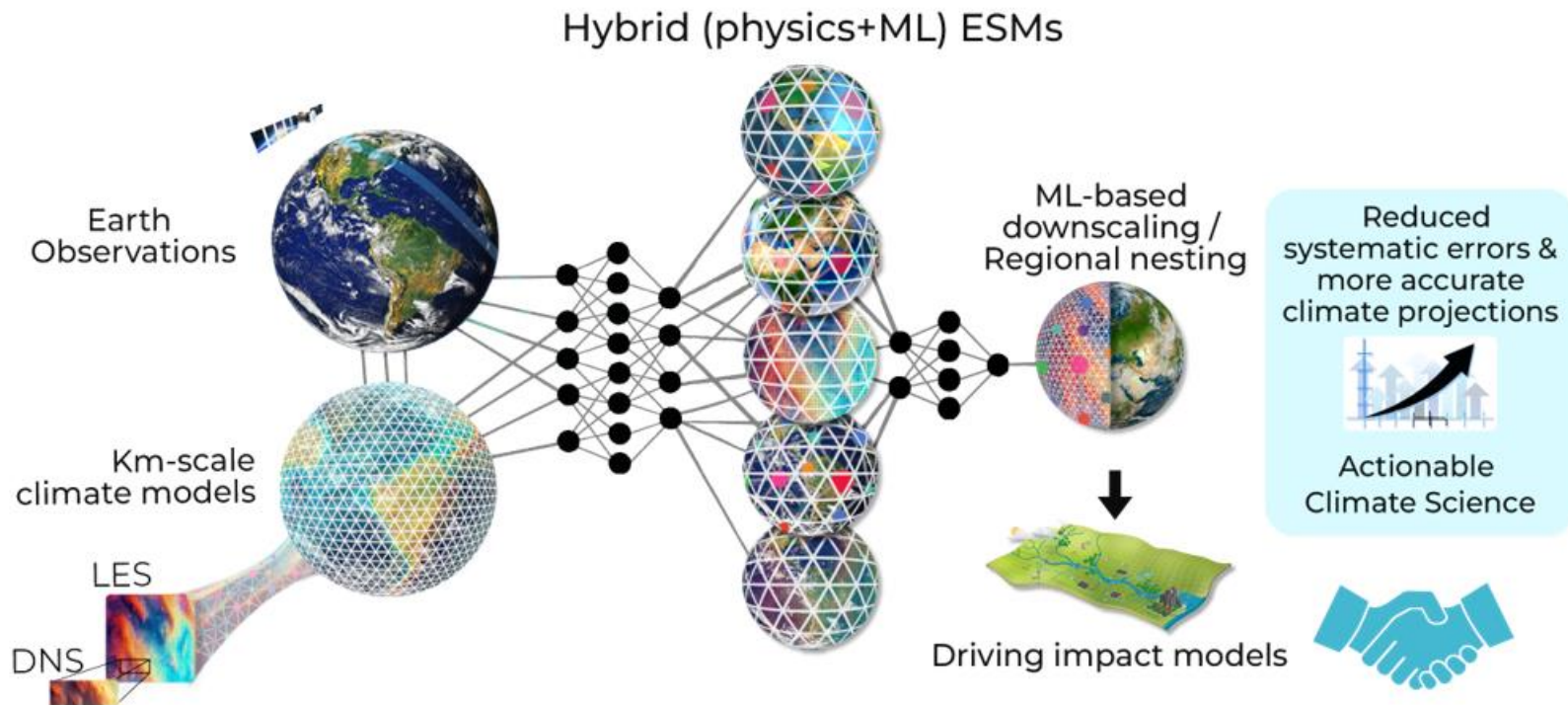
A vision for next-generation climate model



With focus on land and atmosphere in my group



Questions and Answers





Supplementary slides

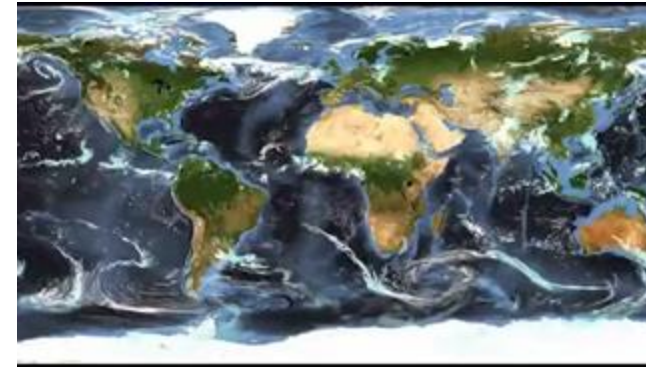


Summary

A vision for next generation climate model to address societal needs

Goal: build the first full climate model based on:

- modern language (Python)
- scalable + flexible hardware (GPUs)
- seamless integration of AI to harvest global data





Summary

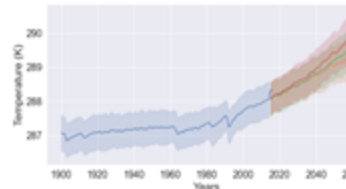
A vision for next-generation climate model to address societal needs

Goal: build the first full climate model (starting with atmosphere and land) based on:

- modern language (Python)
- scalable + flexible hardware (GPUs)
- seamless integration of AI to harvest global data



to provide more accurate climate projections, support global climate adaptation and make new discoveries





A vision for next-generation climate modeling

Can we replicate the machine learning revolution in physical/climate modeling?

Backbones of the ML revolution:

- Data
- Efficient hardware use
- Algorithms for optimization (backpropagation, automatic differentiation)
- Under-appreciated: high-level programming with expressive, flexible and optimized low-level operations (few lines of codes)

```
model_vanilla = Sequential()

model_vanilla.add(Dense(n_neuron, activation=activation, input_shape=(X_train.shape[1],))) # the 1st hidden layer
model_vanilla.add(Dense(n_neuron, activation=activation)) # the 2nd hidden layer
model_vanilla.add(Dense(n_neuron, activation=activation)) # the 3rd hidden layer
model_vanilla.add(Dense(y_train.shape[1], activation='linear')) # the output layer

model_vanilla.compile(loss='mse', optimizer=tf.keras.optimizers.Adam(learning_rate=learning_rate))

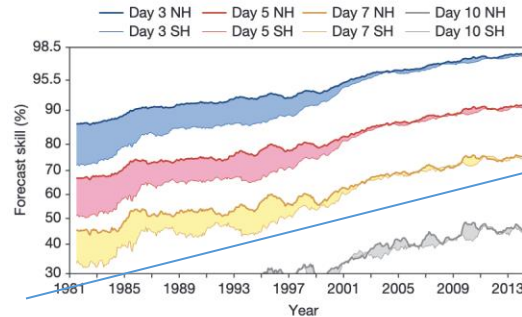
early_stop = keras.callbacks.EarlyStopping(monitor='val_loss', patience=20)

history = model_vanilla.fit(X_train, y_train,
                           batch_size = minibatch_size,
                           epochs = num_epochs,
                           validation_split= 0.2,
                           verbose = 1,
                           callbacks = [early_stop])
```



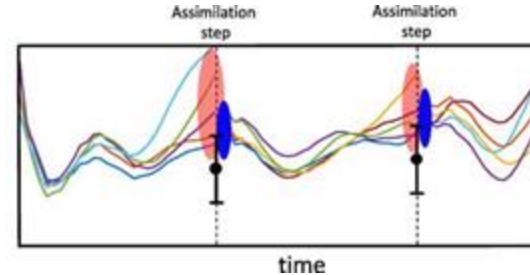
Bringing observational data into climate model development core

- No perfect model, even at high-resolution (e.g high-res ICON $\sim 10W/m^2$ bias or cloud cover)
- Data assimilation led to weather quiet revolution due to increasing data (\sim like AI)



More data

Traditional data assimilation



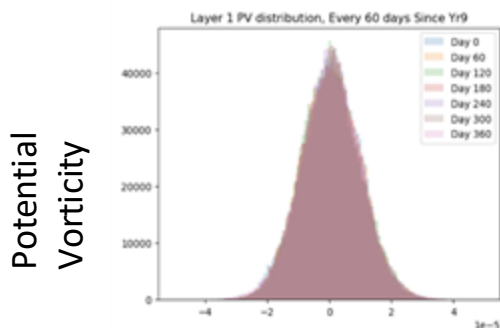
- Traditional data assimilation focuses on trajectory correction - **initial conditions**

→ Not applicable to climate: need excellent future model

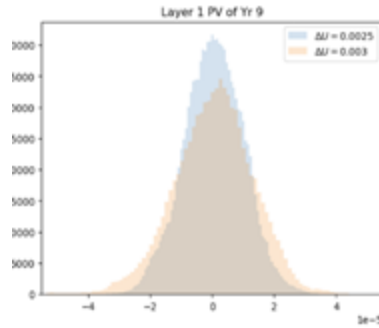


New data assimilation for climate

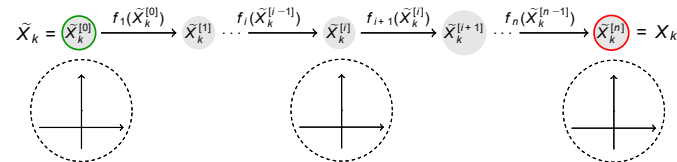
- Key differences with traditional techniques:
 - Does not correct trajectories but **corrects the model parameters/structure** (predicting into the future)
 - Does not consider individual realizations but **statistics**



Statistically steady state



Parameter dependence of distribution

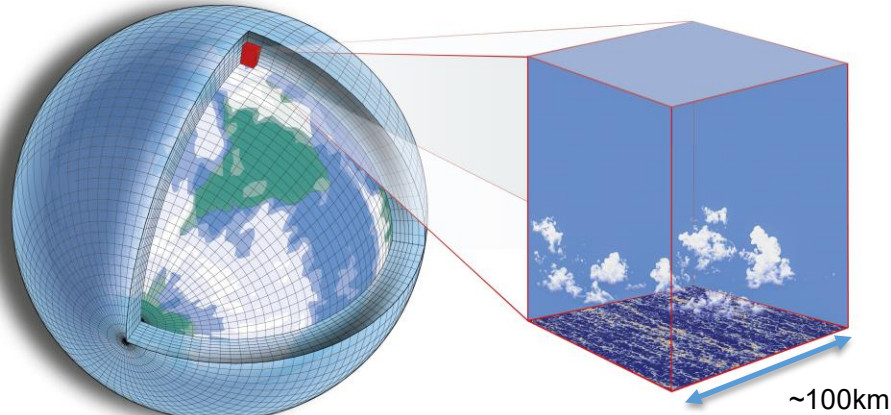


- Merges Machine Learning with Data Assimilation techniques:
harvest data at scale + uncertainty quantification + indirect observations



Climate models use parameterizations of subgrid processes

Parameterization: represents (physically or statistically)
a physical process that cannot be resolved (e.g. clouds).
Typically physically based.

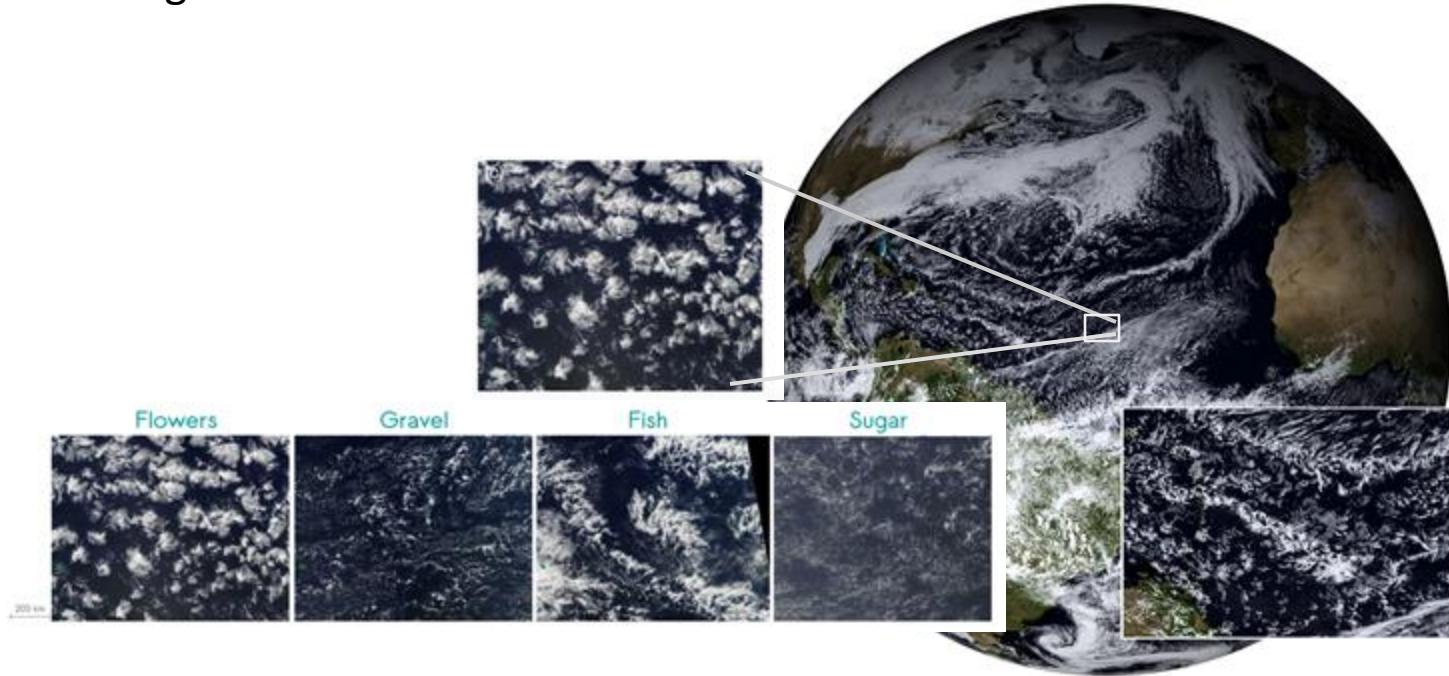


However: it has failed for ~40 years
This largely **explains inter-model spread in climate projection**



Understanding: Cloud organization

- Clouds organize in observations

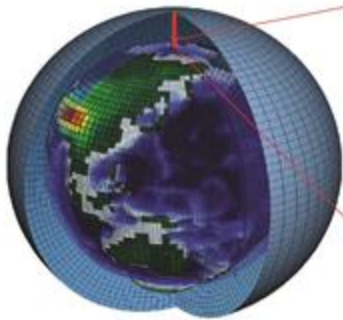




More reliable predictions is one problem ...

effective climate action is another problem altogether

Climate
Prediction Data



Goal



Knowledge Transfer

+

Diversity, Equity,
Inclusion



Effective
Climate
Action

Modern cloud infrastructure to empower climate action with an ecosystem of local partners, especially in Global South (with Climatesmatch Academy)

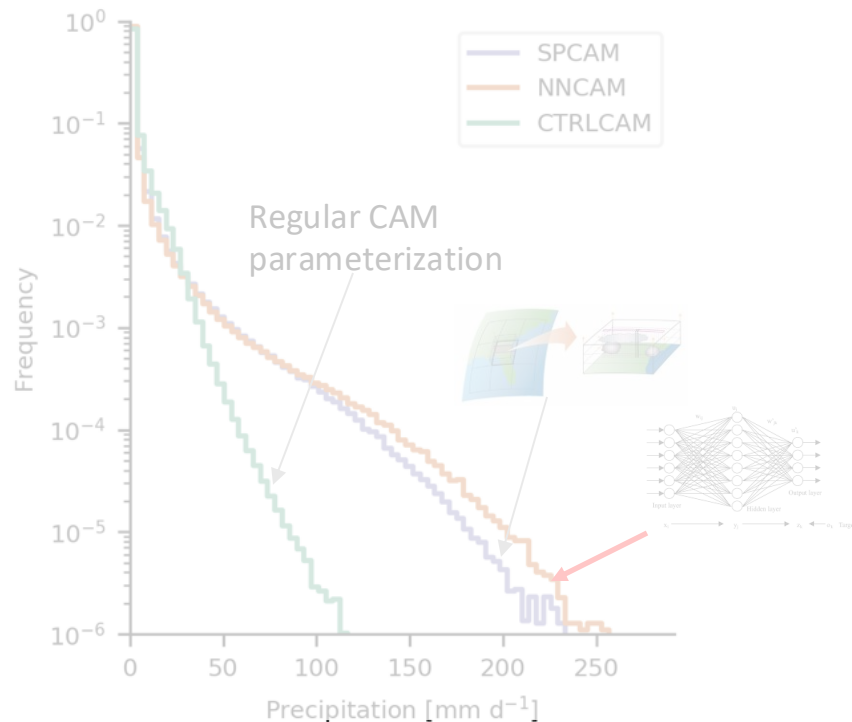
*Transparent, inclusive and ethical:
same climate data accessible
by anyone across the globe*



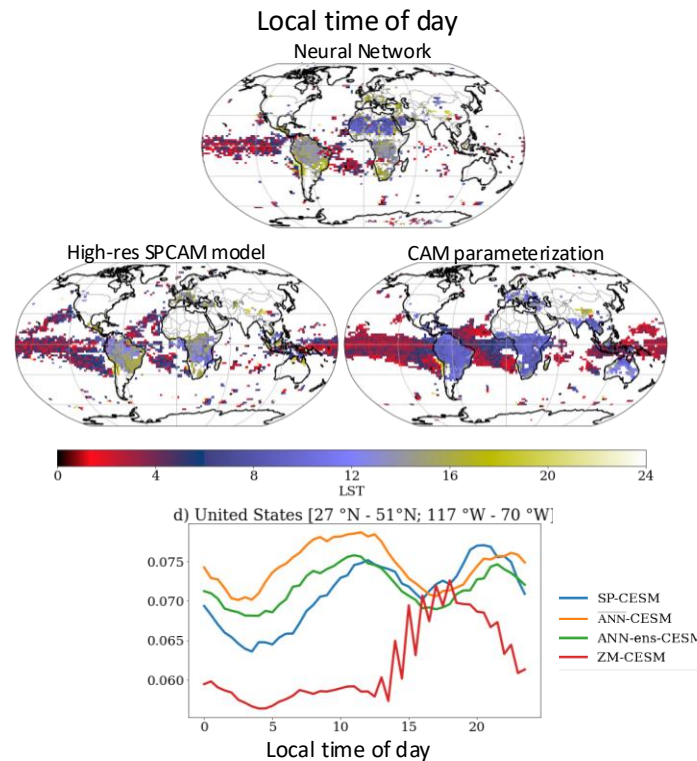
Inclusion of ML closure leads to **Step-change** in climate model quality

Online global simulations 

Precipitation distribution (CAM)

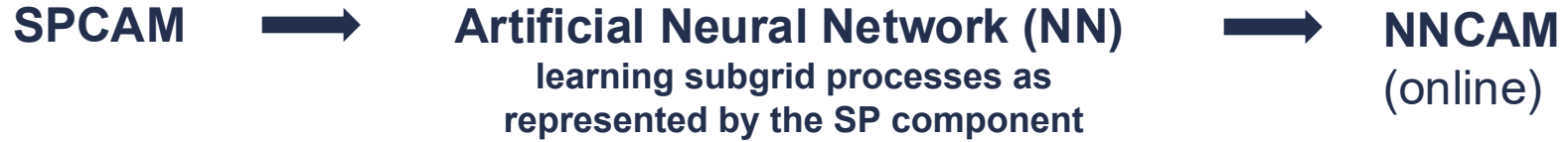


Precipitation diurnal cycle (CAM+ICON)

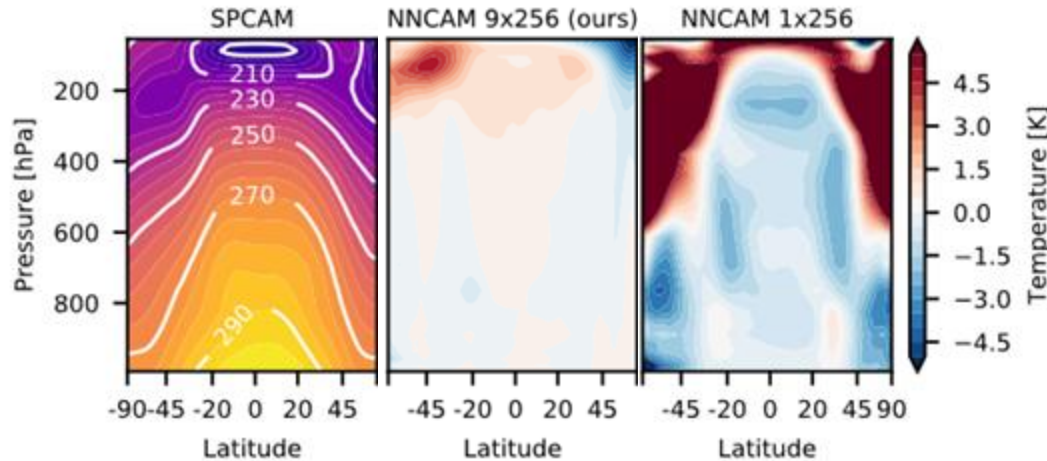




Issues: Convection – DL instabilities & spurious correlations



Zonal-mean temperature



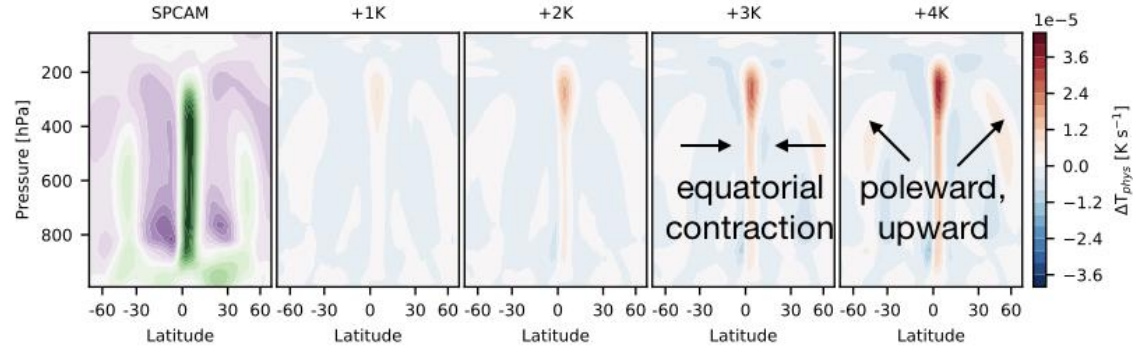
NN-parametrizations can capture many aspects of CRMs

Issues

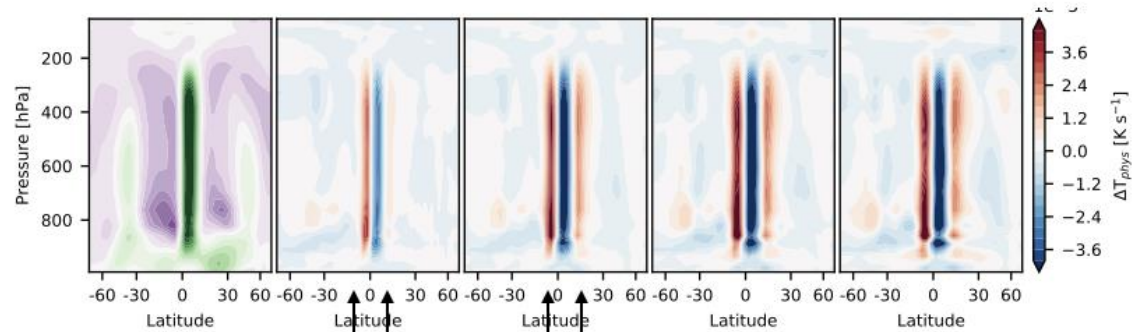
- Spurious correlations between stratosphere and boundary layer
- Instabilities in the coupled runs (NNCAM) under a number of setups
- Generalization: Limitations with out-of-sample temperatures
- Does not conserve energy



SP-CAM



NN-CAM



**ITCZ shift
failure mode**

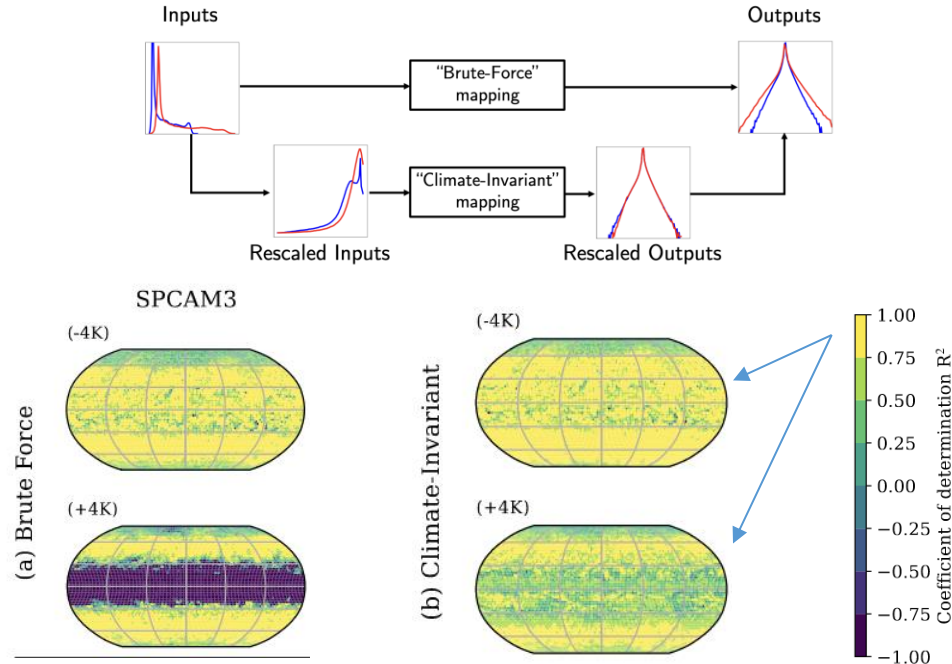
**double ITCZ
failure mode**



Trust, interpretability, generalization

Challenge 1: Generalization

- Challenge: out-of-sample, out-of-distribution prediction/sampling bias
- Solution: **embed physical invariances/equivariance** along Lie groups in ML (e.g., dimensionless numbers or rotational equivariance to collapse distributions)



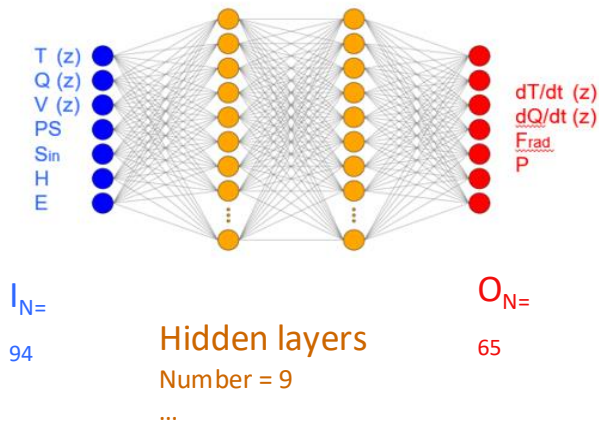


Trust, interpretability, generalization

Challenge 2: Trust + interpretability

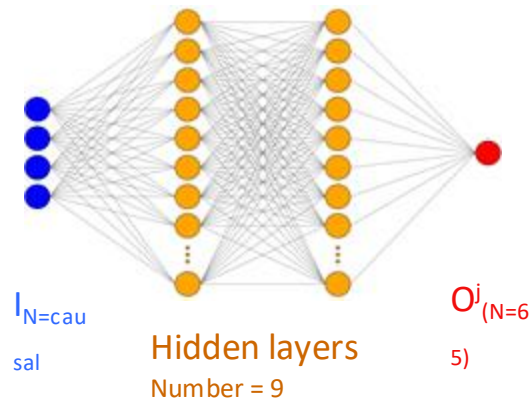
- Challenge: cross-correlations can fool ML
- Solution: merge **causal discovery with ML**
→ more interpretable, more trustworthy

NN (Rasp et al., 2018)



Drop connections based on causality: a very sparse NN

Causal-NNs

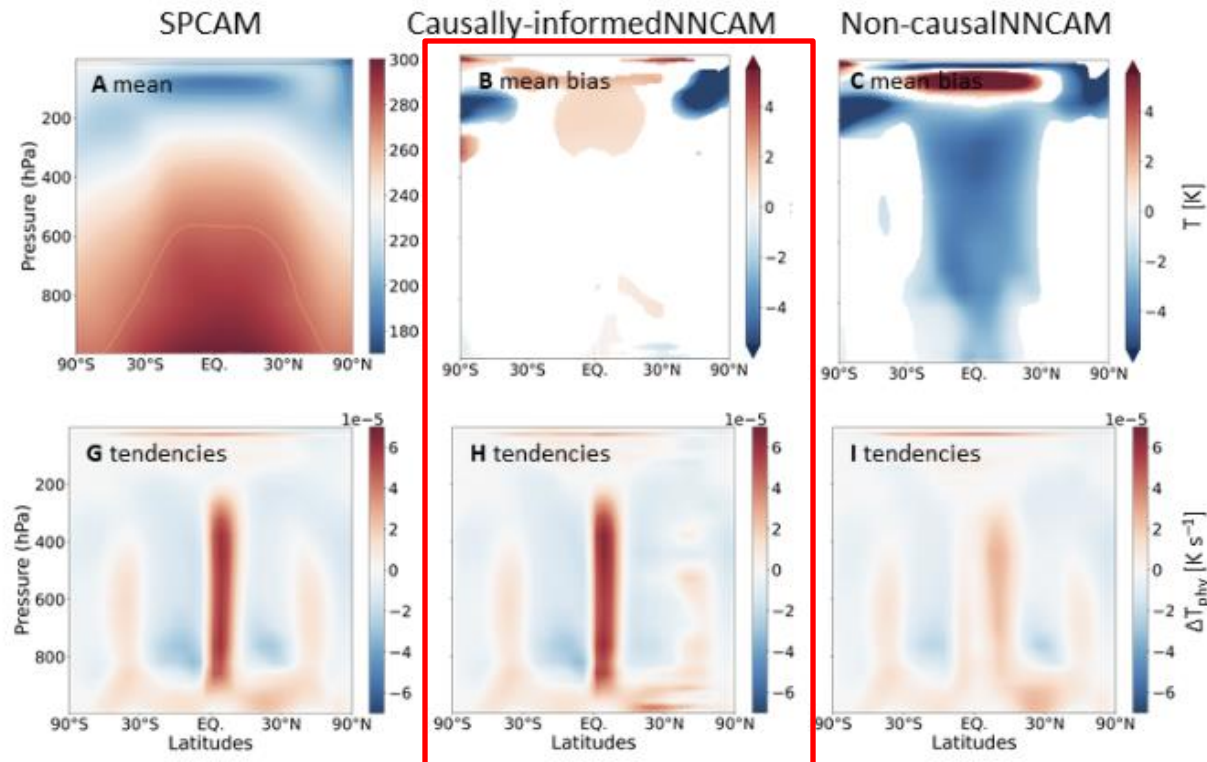


$$I_{causal}^i \rightarrow O^j \in P(O^j)$$



Causality: going beyond correlations

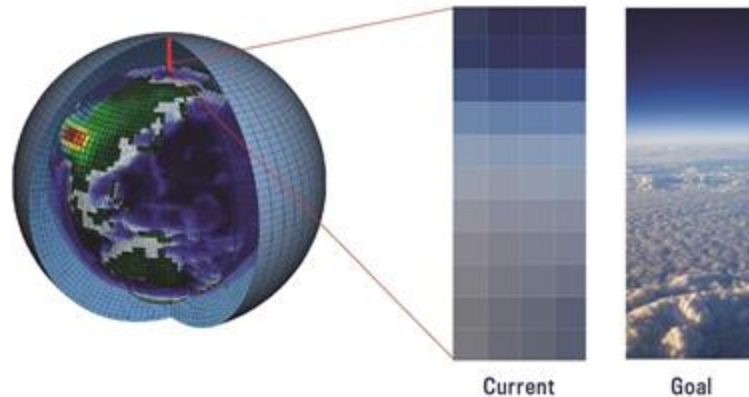
Online global simulations





Why ETH

- ICON ongoing work
- Aligned vision on high-level code and high compute (MeteoSwiss-ETH)
- Continued collaboration on land (MPI)
- Strong climate group (including impact), who would be using new model outputs
- Strong CS group, plus interested in climate and climate modeling
- Key partnership with MeteoSwiss, pioneer in the use of GPUs



A realistic Earth's Twin



Model tuning

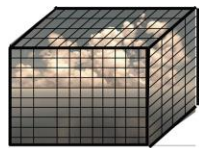
Other strategy

Use physical insights to improve (phenomenological) subgrid models

+ **systematic model tuning**

(with statistical emulation for speedup)

e.g., IPSL (France), NASA GISS (US), NCAR (US), Clima (US)

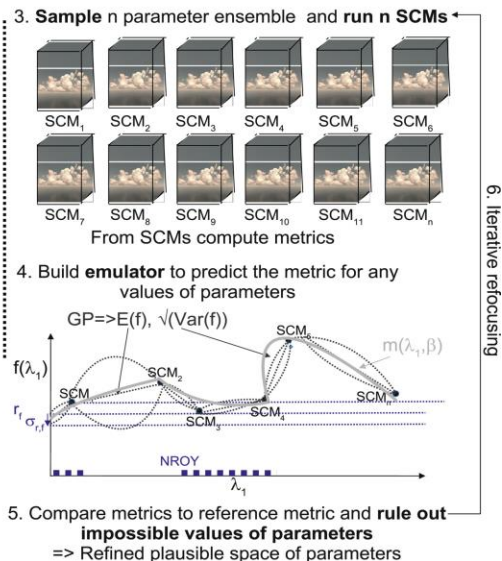


Reference
LES

High-resolution
Simulation as truth

**Goal: Estimate
parameterization
parameters Θ**

e.g. clouds



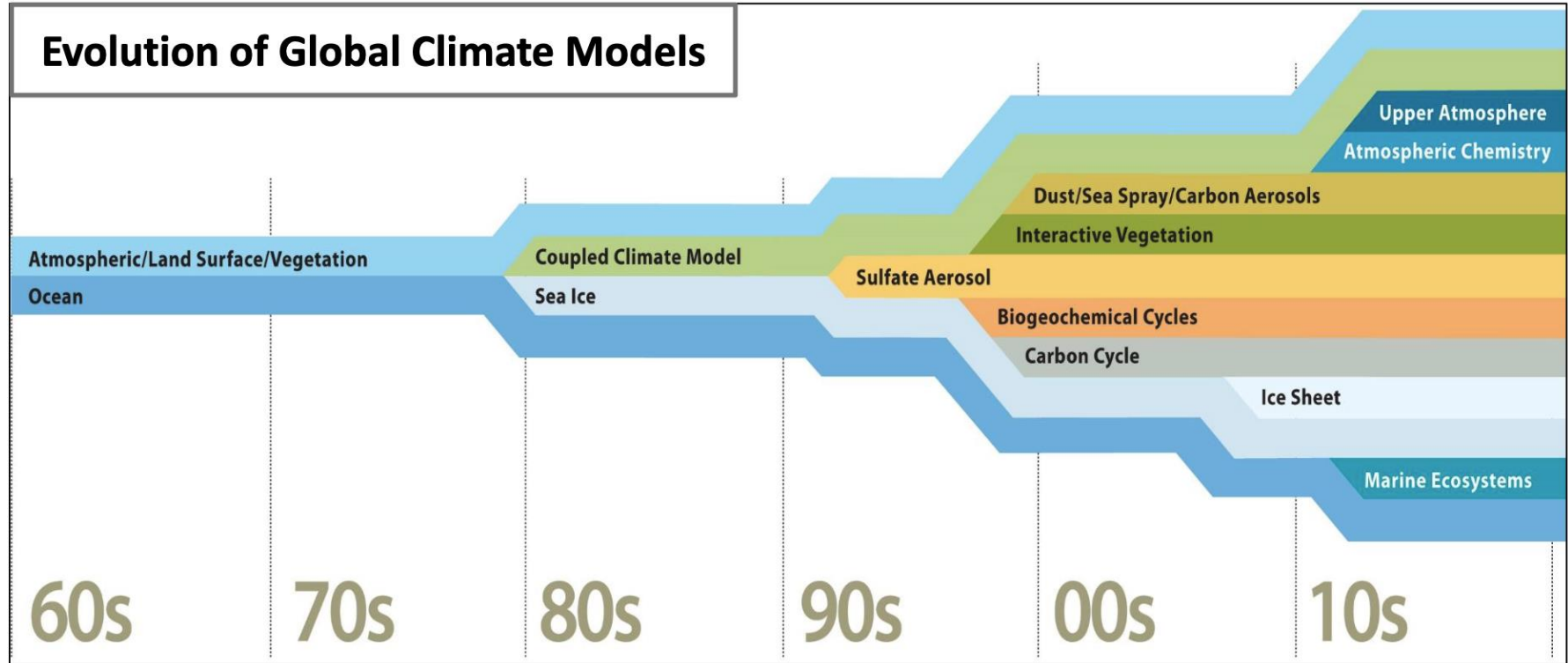
Sample: Coarse-resolution model MCMC on Θ

Emulator on Θ

Calibrate Θ



From climate models to Earth system models

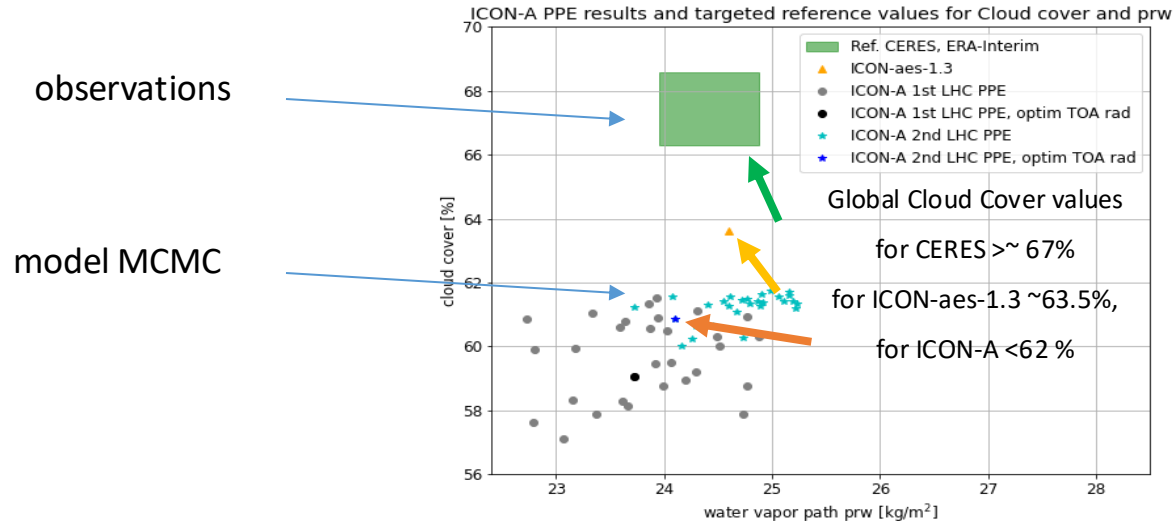


Simple climate models have evolved into complex Earth System models
to **answer many questions** (not just climate projections)



Caveat: parameterizations can have large structural errors

- Parameter tuning might be **impossible**



- Structural errors dominate many processes**
→ traditional data assimilation may not be feasible for climate



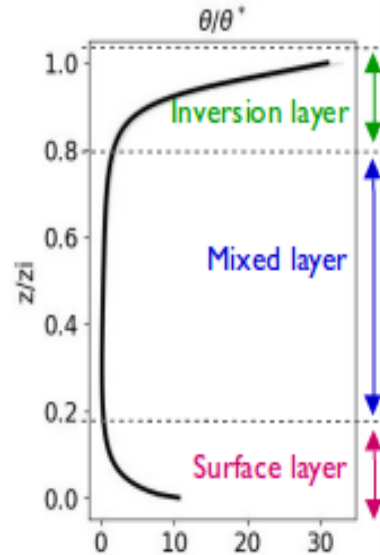
Caveat: parameterizations can have large structural errors

- Example of dry turbulence with state-of-the-art model:

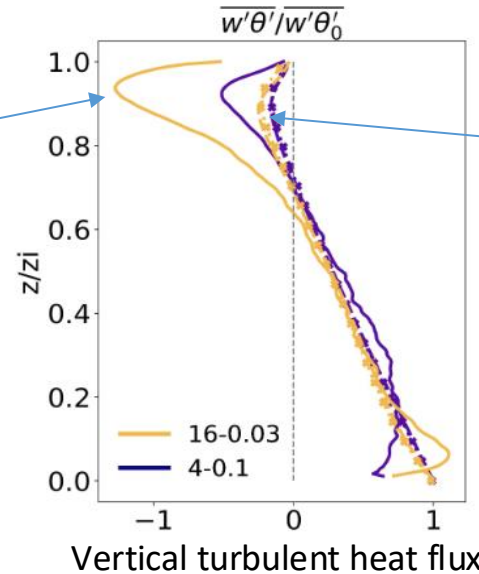
Eddy-diffusion mass-flux model

(ECMWF, IPSL, Clima...)

$$\overline{w'\theta'} = -K \frac{\partial \bar{\theta}}{\partial z} + M_u(\theta_u - \bar{\theta})$$



Best fit
coarsem
odel



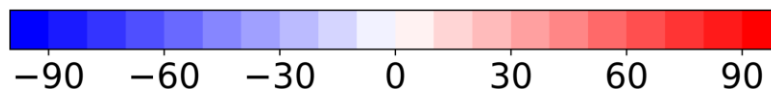
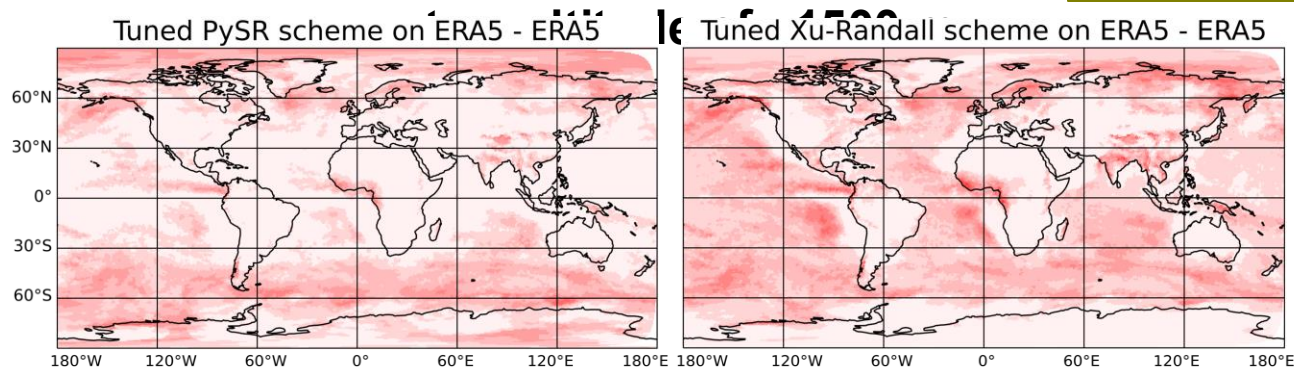
High-
resolution
truth

- Even the best set of parameters still has substantial deficiencies

Bias of averaged cloud cover (area fraction) of 3-hourly data from 20160811 to 20160820

$$C_{\text{Xu-Randall}}^{\text{def}} = \min\{\text{RH}^\beta(1 - \exp(-\alpha(q_c + q_i))), 1\}$$

(multiplied by 100)



Cloud cover bias [%]

The data-driven analytical PySR equation

$$f(RH, T, \partial_z RH, q_c, q_i) = I_1(RH, T) + I_2(\partial_z RH) + I_3(q_c, q_i),$$

$$I_1(RH, T) \stackrel{\text{def}}{=} a_1 + a_2(RH - \overline{RH}) + a_3(T - \overline{T}) + \frac{a_4}{2}(RH - \overline{RH})^2 + \frac{a_5}{2}(T - \overline{T})^2(RH - \overline{RH})$$

$$I_2(\partial_z RH) \stackrel{\text{def}}{=} a_6^3 \left(\partial_z RH + \frac{3a_7}{2} \right) (\partial_z RH)^2$$

$$I_3(q_c, q_i) \stackrel{\text{def}}{=} \frac{-1}{q_c/a_8 + q_i/a_9 + \epsilon}.$$

$$\{a_1, \dots, a_9, \epsilon\} = \{0.4435, 1.1593, -0.0145 \text{ K}^{-1}, 4.06, 1.3176 \cdot 10^{-3} \text{ K}^{-2}, \\ 584.8036 \text{ m}, 2 \text{ km}^{-1}, 1.1573 \text{ mg/kg}, 0.3073 \text{ mg/kg}, 1.06\}$$

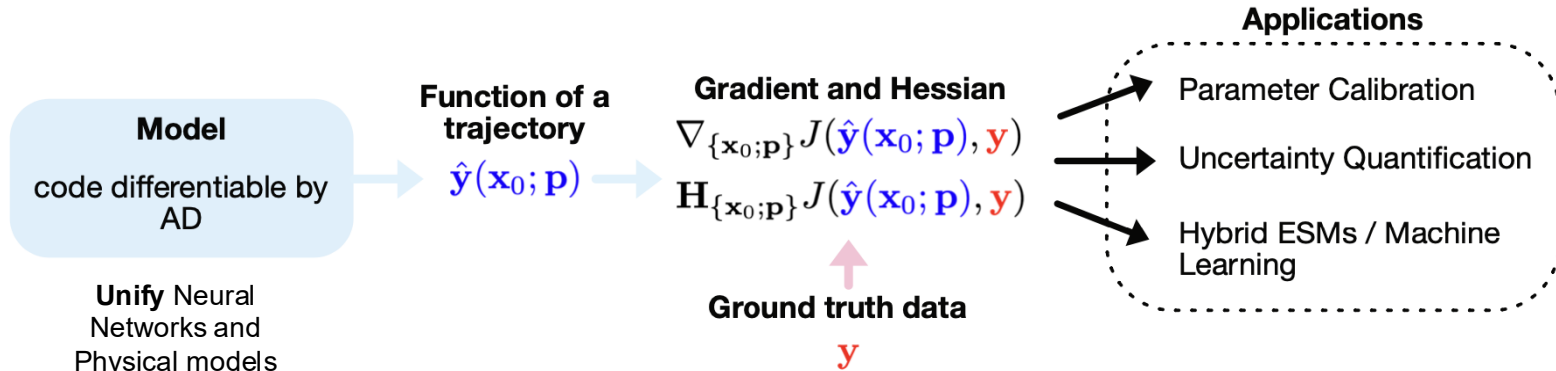
$$C(X) = \max\{\min\{100 f(X), 100\}, 0\}$$

Abbreviated form:

$$C = P_3(RH, T) + (c_1 \partial_z RH + c_2)(\partial_z RH)^2 - \frac{1}{c_3 q_c + c_4 q_i + \epsilon}$$



- From weather to climate



Bhouri et al., 2022 *arxiv*; Gelbrecht et al. 2022 *arxiv*; Shen, Gentine et al, 2023 *Nat Comm*

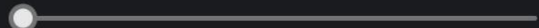
(carbon)plan

DATASET

<https://carbonplan-data-viewer.s3.amazonaws.com/d>

VARIABLE tasmax ⓘ

TIME ⓘ



Jan 01 2015 (0 / 84)

DISPLAY

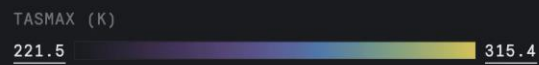
PROJECTION mercator

BASEMAPS Land boundaries ☒

Land mask ☐

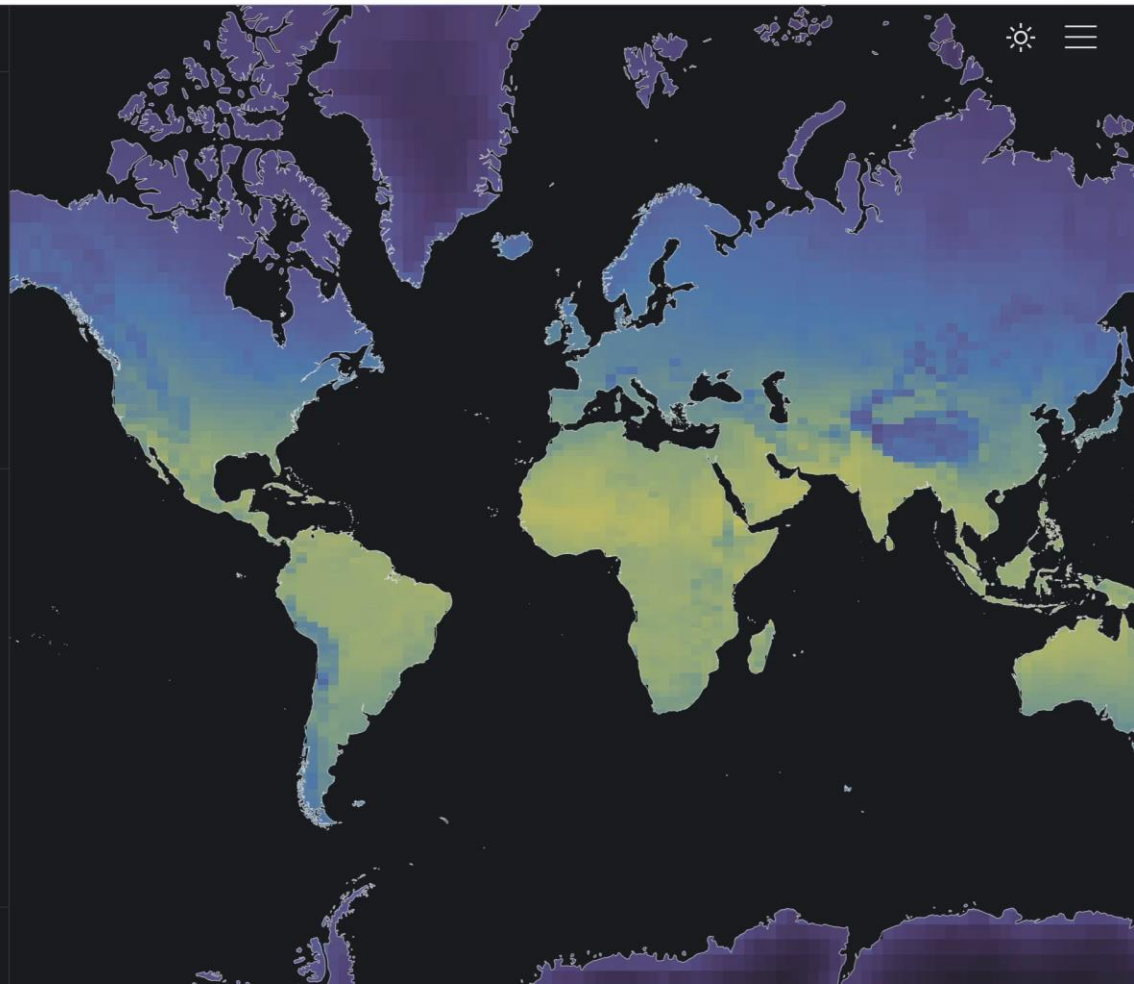
Ocean mask ☒

COLORMAP cool



Reset color range

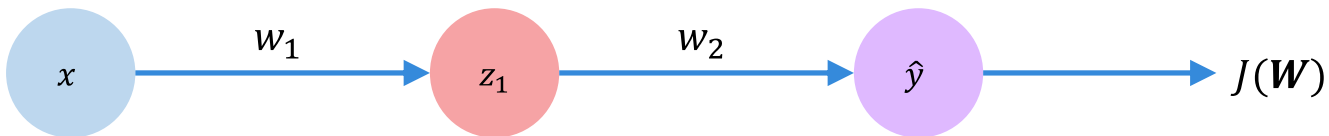
PLOTS





Intermission 1: Advances in Machine Learning: *backpropagation*

- *Backpropagation*
- Chain's rule



$$\frac{\partial J(W)}{\partial w_1} = \underbrace{\frac{\partial J(W)}{\partial \hat{y}}}_{\text{purple bar}} * \frac{\partial \hat{y}}{\partial z_1} * \underbrace{\frac{\partial z_1}{\partial w_1}}_{\text{blue bar}}$$

- Efficient computation of gradients is key (analytical or automatic differentiation)



Intermission 2: Advances in Machine Learning: *automatic differentiation*

- What is **automatic differentiation**?
- Propagate ϵ differential throughout code $f(x + \epsilon)$ with property: $\epsilon^2 = 0$

- Taylor series:

$$f(x + \epsilon) = f(x) + \epsilon f'(x) + \epsilon^2/2 f''(x) + O(\epsilon^2)$$

0

Efficient computation of gradients ~ almost free

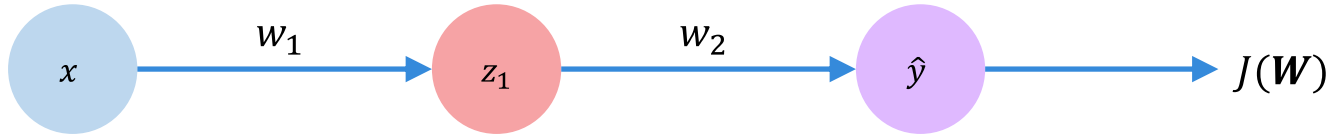
- Used in many modern ML toolboxes:
Pytorch, JAX or modern computing languages: Julia





Differentiable codes unify physical and machine learning models

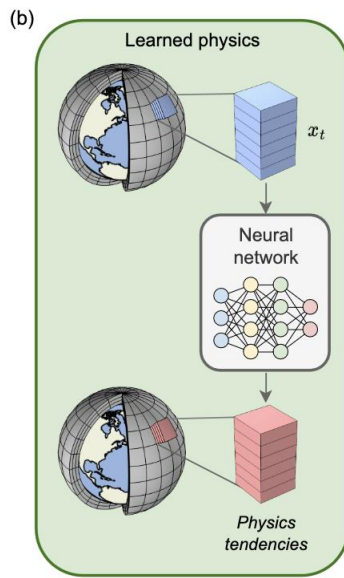
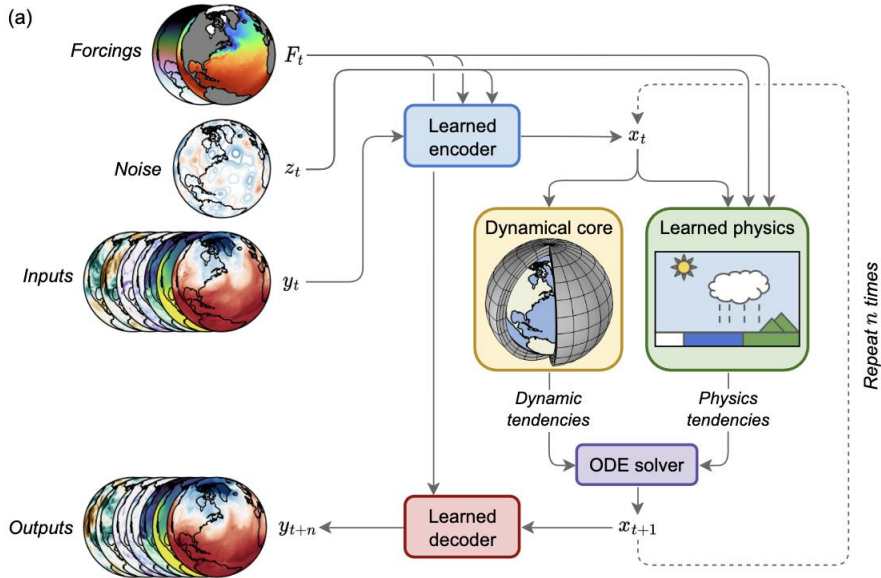
- Dependence of neural network weights, physical parameters or initial conditions is the same!



NN weight,
initial
condition
(x_0),
physical
parameter
 θ



Differentiable model



Neural General Circulation Models

Dmitrii Kochkov^{1†}, Janni Yuval^{1†}, Ian Langmore^{1†},
 Peter Norgaard^{1†}, Jamie Smith^{1†}, Griffin Mooers¹,
 James Lottes¹, Stephan Rasp¹, Peter Düben³, Milan Klöwer⁴,
 Sam Hatfield³, Peter Battaglia², Alvaro Sanchez-Gonzalez²,
 Matthew Willson², Michael P. Brenner^{1,5}, Stephan Hoyer^{1†}

¹Google Research, Mountain View, CA.

²Google DeepMind, London, UK.

³European Centre for Medium-Range Weather Forecasts, Reading, UK.

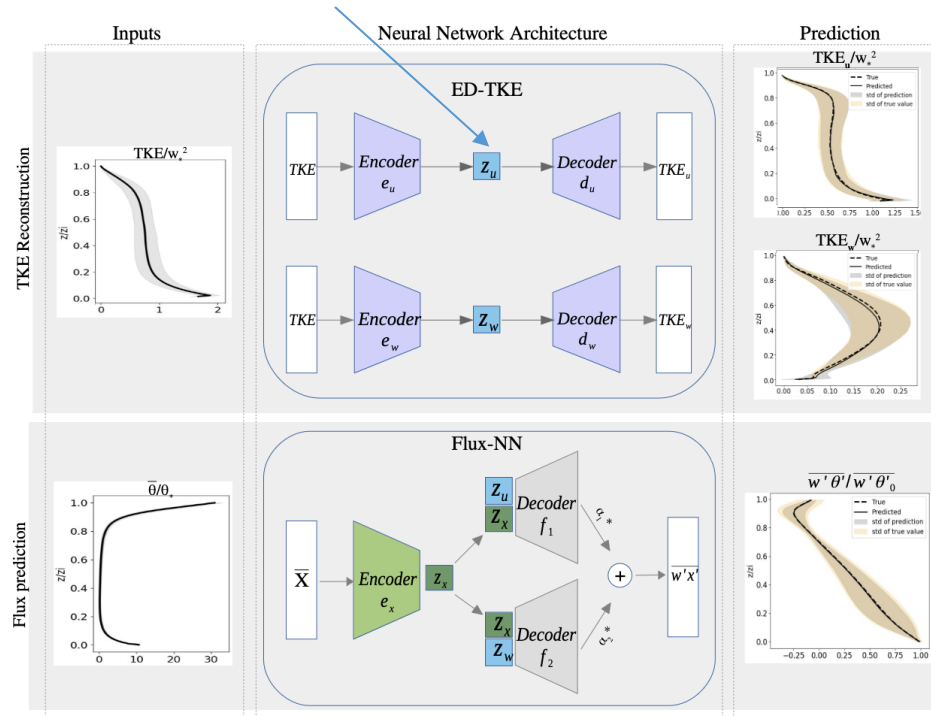
⁴Earth, Atmospheric and Planetary Sciences, Massachusetts Institute of Technology.

⁵School of Engineering and Applied Sciences, Harvard University.



Scientific discovery: latent models

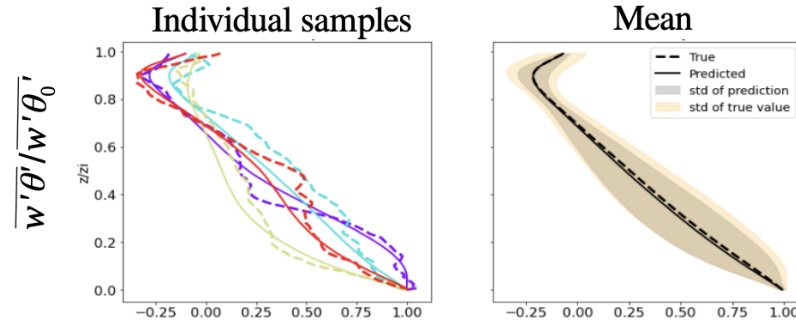
- Example to dry atmospheric turbulence using ML:
latent representation of turbulence



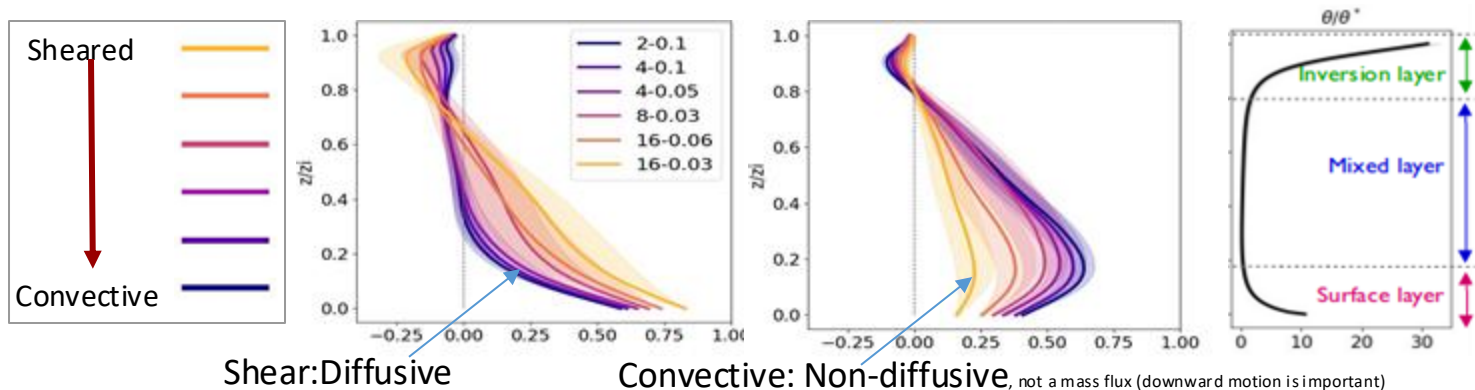


Latent model for dry atmospheric turbulence

- Great at **prediction**



- Can be used for **understanding** (2D only)



Shear:Diffusive Convective: Non-diffusive, not a mass flux (downward motion is important)



Supplementary: ML-accelerated dynamical core

There are now methods to also accelerate PDE resolution (here JAX-based again)



Machine learning–accelerated computational fluid dynamics

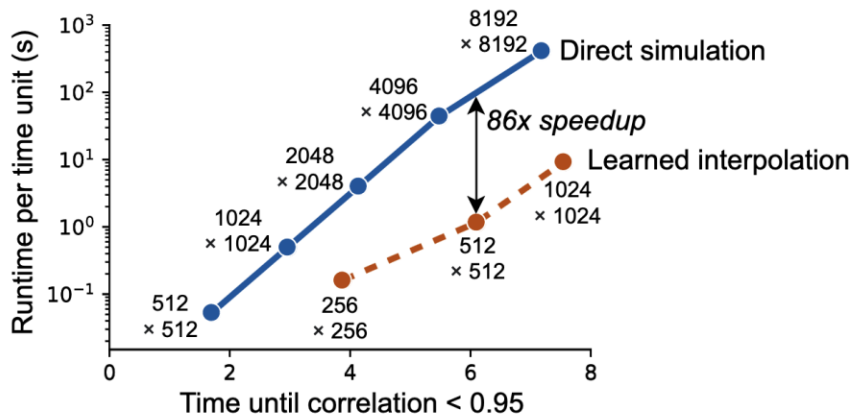
Dmitrii Kochkov^{a,1,2}, Jamie A. Smith^{a,1,2} , Ayya Alieva^a, Qing Wang^a, Michael P. Brenner^{a,b,2} , and Stephan Hoyer^{a,2} 

^aGoogle Research, Mountain View, CA 94043; and ^bSchool of Engineering and Applied Sciences, Harvard University, Cambridge, MA 02138

Edited by Andrea L. Bertozzi, University of California, Los Angeles, CA, and approved March 25, 2021 (received for review January 29, 2021)

Numerical simulation of fluids plays an essential role in modeling many physical phenomena, such as weather, climate, aerodynamics, and plasma physics. Fluids are well described by the Navier-Stokes equations, but solving these equations at scale remains daunting, limited by the computational cost of resolving the smallest spatiotemporal features. This leads to unfavorable trade-offs between accuracy and tractability. Here we use end-to-end deep learning to improve approximations inside computational fluid dynamics for modeling two-dimensional turbulent flows. For both direct numerical simulation of turbulence and large-eddy simulation, our results are as accurate as baseline solvers with 8 to 10 \times finer resolution in each spatial dimension, resulting in 40- to 80-fold computational speedups. Our method remains stable during long simulations and generalizes to forcing functions and Reynolds numbers outside of the flows where it is trained, in contrast to black-box machine-learning approaches. Our approach exemplifies how scientific computing can leverage machine learning and hardware accelerators to improve simulations without sacrificing accuracy or generalization.

machine learning | turbulence | computational physics | nonlinear partial differential equations





- **Data assimilation**
- Objective: find **state** that minimizes a cost function $J(\mathbf{x})$
- *3D Var*

$$J(\mathbf{x}) = (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + (\mathbf{y} - H[\mathbf{x}])^T \mathbf{R}^{-1} (\mathbf{y} - H[\mathbf{x}])$$

$$J(\mathbf{x}) = \|\mathbf{x} - \mathbf{x}_b\|_{\mathbf{B}}^2 + \|\mathbf{y} - H[\mathbf{x}]\|_{\mathbf{R}}^2$$

4D Var

$$J(\mathbf{x}) = \|\mathbf{x} - \mathbf{x}_b\|_{\mathbf{B}}^2 + \sum_i \|\mathbf{y}_i - H[\mathbf{x}_i]\|_{\mathbf{R}_i}^2$$



- **Data assimilation**
- Extension to update *parameters*
- Objective: find **state + parameters** that minimize a cost function $J(\mathbf{x})$

$$J(\mathbf{x}; \mathbf{p}) = \|\mathbf{x} - \mathbf{x}_b\|_{\mathbf{B}_x}^2 + \|\mathbf{p} - \mathbf{p}_b\|_{\mathbf{B}_p}^2 + \|\mathbf{y} - H[\mathbf{x}]\|_{\mathbf{R}}^2$$

- Caveat: underlying dynamics is *modeled*: $\frac{d\mathbf{x}}{dt} = g(\mathbf{x}, \mathbf{p}, t)$

But only an *ansatz* of the world

For weather: even a deficient model can work well because of frequent assimilation

For climate: cannot have a deficient model+DA → diverging



- **Machine learning**
- Objective: find (neural network) **parameters \mathbf{p}** that minimize a cost function $J(\mathbf{p}; \mathbf{x})$

$$J(\mathbf{p}; \mathbf{x}) = \|\mathbf{y} - f(\mathbf{p}; \mathbf{x})\|_{\mathbf{I}}^2$$

- Parameters are estimated over a set $\{\mathbf{x}_i\}$
- Clear similarities with Data Assimilation (DA)
- Caveats: no observational errors + assumes *direct* observations

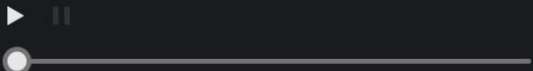
(carbon)plan

DATASET

<https://carbonplan-data-viewer.s3.amazonaws.com/d>

VARIABLE tasmax ⓘ

TIME ⓘ



Jan 01 2015 (0 / 84)

DISPLAY

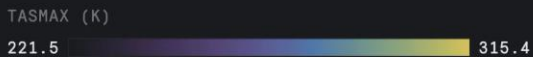
PROJECTION mercator

BASEMAPS Land boundaries ☒

Land mask ☐

Ocean mask ☒

COLORMAP cool



Reset color range

PLOTS

