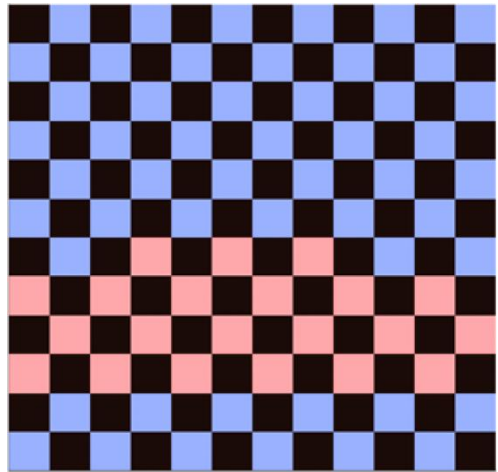
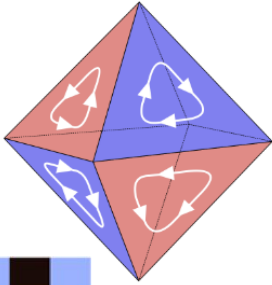


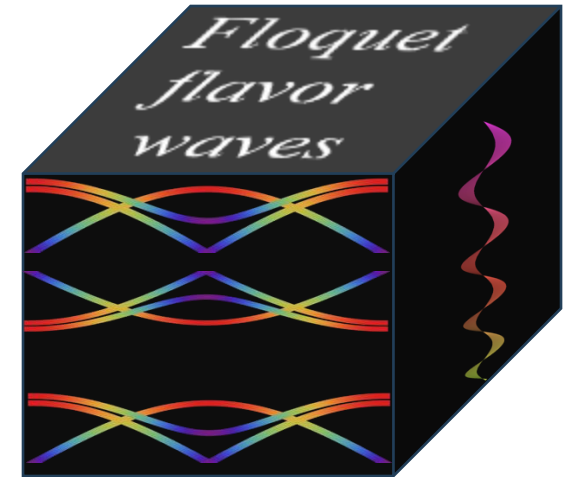
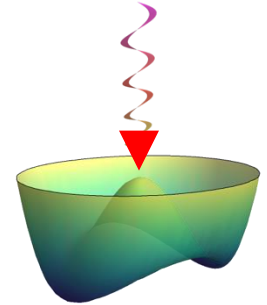
# Phonons as a probe of hidden order in quantum materials

Arun Paramakanti  
(University of Toronto)



Advanced School and Conference on  
Quantum Matter, ICTP Trieste

Dec 01-12, 2025



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**Digital Research  
Alliance** of Canada

# Spin liquid story: Quick summary but not the focus of this talk

## Proximate Dirac spin liquid in the honeycomb lattice $J_1$ - $J_3$ XXZ model: Numerical study and application to cobaltates

[Anjishnu Bose](#)<sup>1,\*</sup>, [Manodip Routh](#)<sup>2,\*</sup>, [Sreekar Voleti](#) <sup>1,\*</sup>, [Sudip Kumar Saha](#)<sup>2</sup>, [Manoranjan Kumar](#) <sup>2</sup>, [Tanusri Saha-Dasgupta](#) <sup>2</sup>, and [Arun Paramekanti](#) <sup>1,2,3</sup>

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Phys. Rev. B **108**, 174422 – Published 16 November, 2023

## Modified large- $N$ approach to gapless spin liquids, magnetic orders, and dynamics: Application to triangular lattice antiferromagnets

[Anjishnu Bose](#) <sup>\*</sup>, [Kathleen Hart](#), [Ruairidh Sutcliffe](#), and [Arun Paramekanti](#)<sup>†</sup>

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more

Phys. Rev. B **111**, 214410 – Published 4 June, 2025

DOI: <https://doi.org/10.1103/PhysRevB.111.214410>

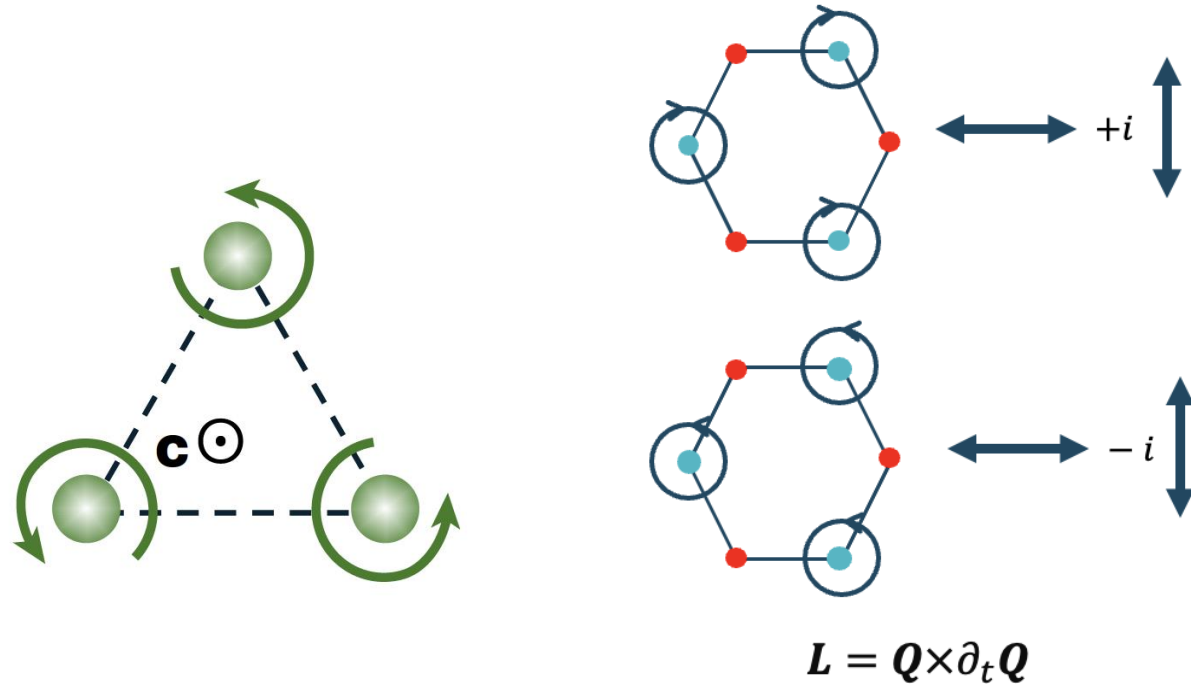
- Study “XY”-type frustrated honeycomb magnets
- Find candidate easy-plane Dirac spin liquid wfn
- Explains THz spectroscopy as function of (B,T)
- Explains “universal” metallic thermal conductivity

- Formulate a distinct large- $N$  approach to QSLs
- Allows access to QSL-Magnetic order transitions
- Parton-parton interactions capture  $S(Q,w)$
- Successfully applied to triangular  $J_1$ - $J_2$  AFM

- A. Bose, K. Hart, R. Sutcliffe, AP, arXiv:2503.09695
- Willsher, J. Knolle, arXiv:2503.13831

# Phonons in solids

# Phonon angular momentum



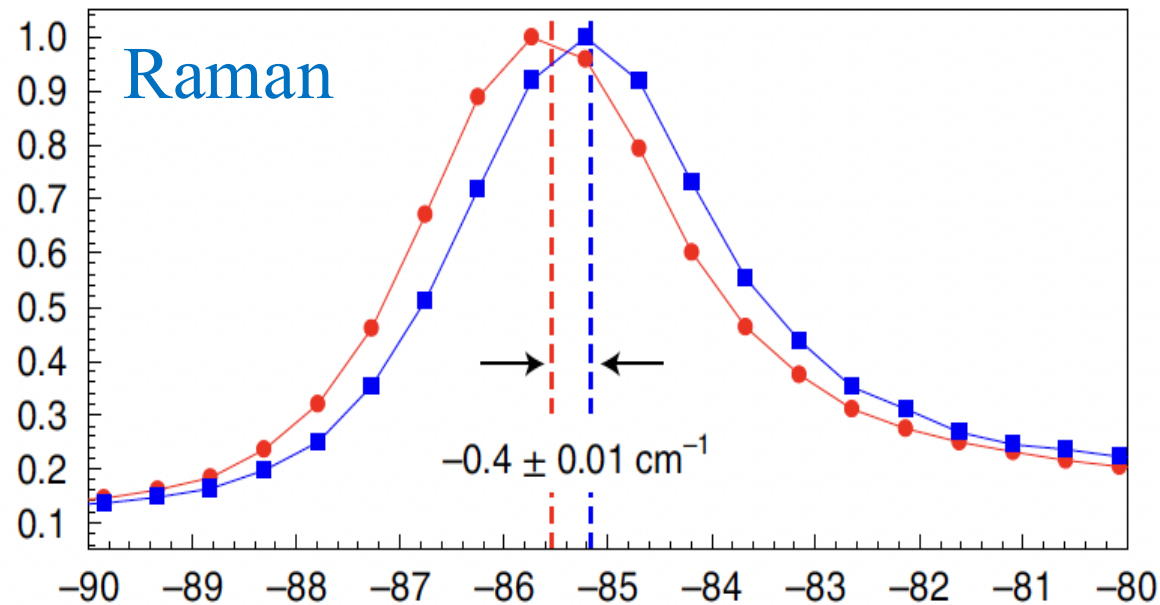
- Phonons: Quantized lattice vibrations
- Atoms in a solid can exhibit circular motion
- Phonons can carry nonzero angular momentum

L. Zhang, Q. Niu, PRL 115, 115502 (2015)

H. Zhang, et al, Nat. Phys. 21, 1387 (2025)

D. Juraschek, et al, Nat. Phys. (Perspective) 21, 1532 (2025)

# Phonon angular momentum in non-centrosymmetric insulators



Phonon mode splitting in a chiral crystal  
 $\alpha$ -HgS: Ishito, et al, Nat. Phys. 19, 35 (2023)

Allowed term:  $\vec{k} \cdot \vec{L}$

- Breaks inversion
- Preserves time-reversal symmetry
- Like a “spin-orbit coupling” for phonons
- Really  $L \sim$  “crystal angular momentum”

Zone center phonon:  $k=0$  (not split)

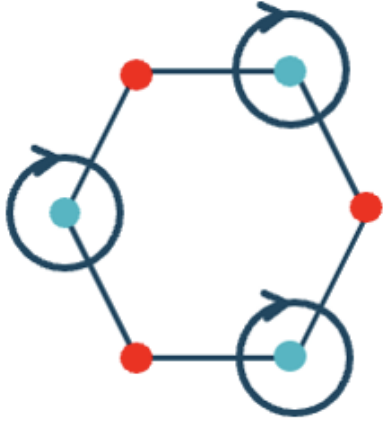
Actually probing small nonzero  $k=2\pi/\lambda$

Light wavelength  $\lambda \sim 7000\text{\AA}$

Lattice spacing  $a \sim 10\text{\AA}$

$k.a \sim 1/100$

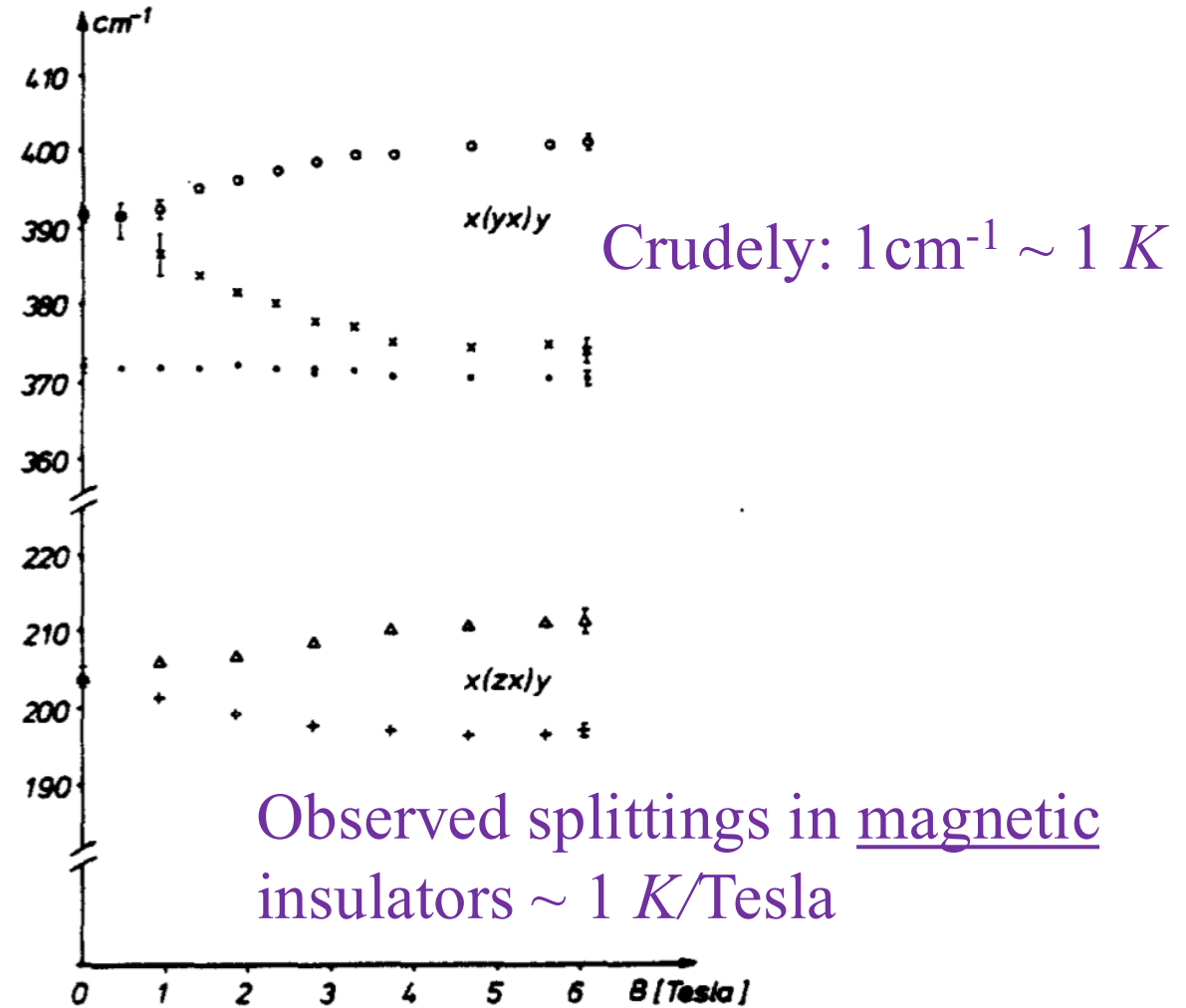
# Magnetic moment of phonons



Expectation:

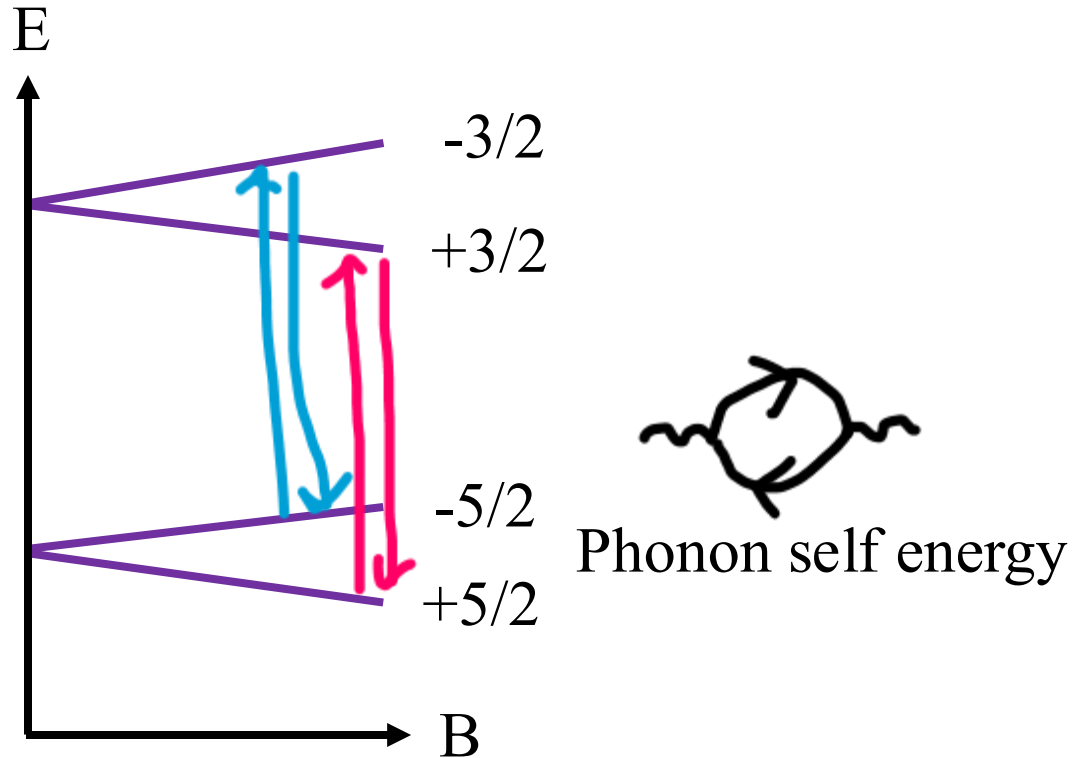
$$\mu_{\text{ph}} = \frac{Q\hbar}{2M} \sim \mu_B \frac{m_e}{M}$$

Zeeman splitting  $\sim 1 \text{ mK/Tesla}$

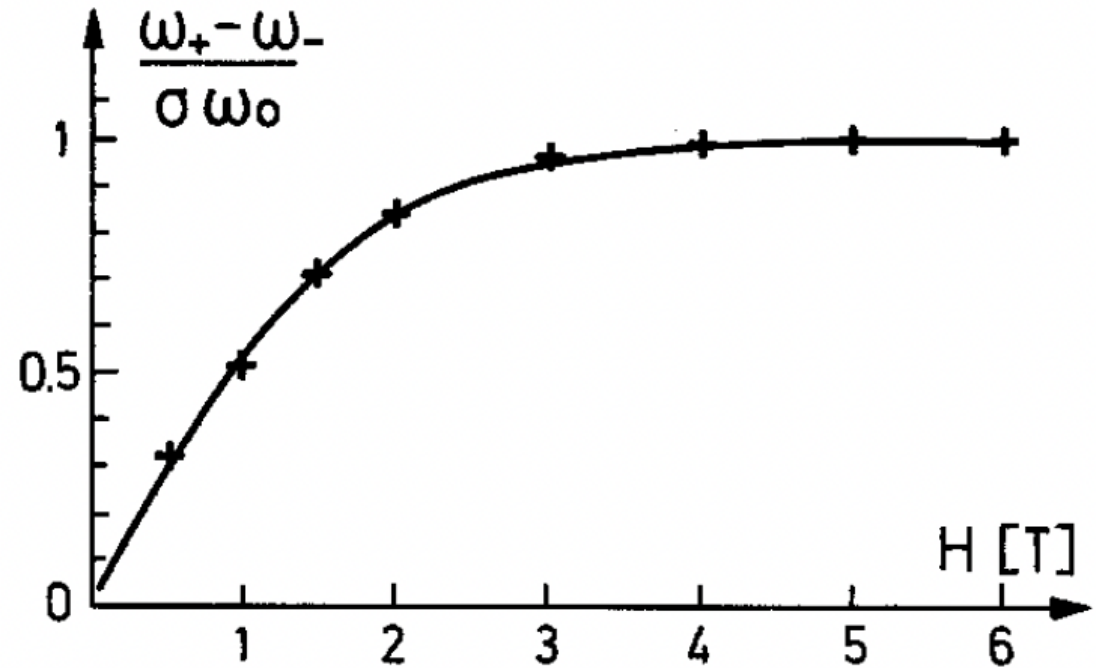


Raman scattering on  $\text{CeF}_3$   
G. Schaack, Sol. State Comm. 15, 505 (1975)

# Magnetic moment of phonons



Crystal field Kramers doublets  
split by B-field



P. Thalmeier and P. Fulde, Z. Physik B 26, 323 (1977)

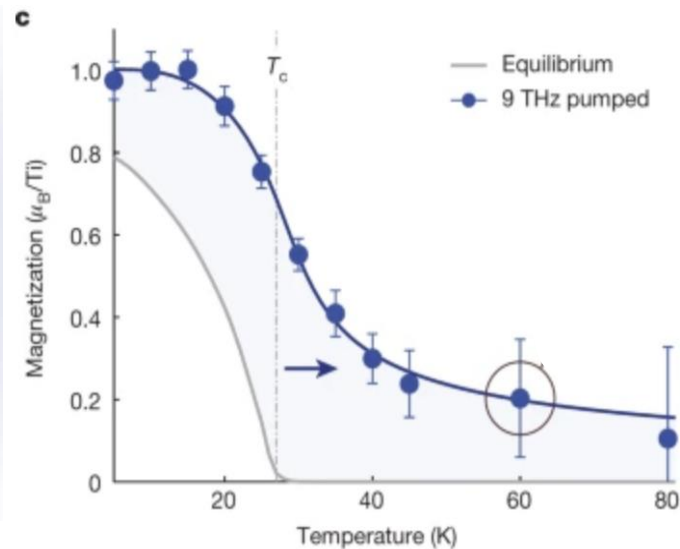
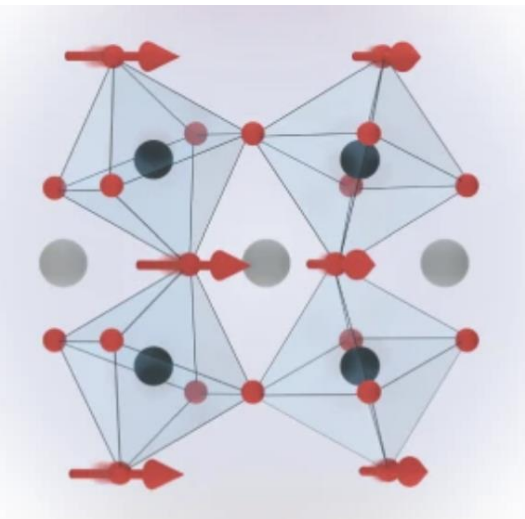
Fully microscopic theory + d-orbital materials  
S. Chaudhary, D. Juraschek, M. Rodriguez-Vega, G. Fiete, PRB (2024)

# Magnetization induced by driven phonons

## Photo-induced high-temperature ferromagnetism in $\text{YTiO}_3$

A. S. Disa<sup>1,2</sup>✉, J. Curtis<sup>3,4</sup>, M. Fechner<sup>1</sup>, A. Liu<sup>1</sup>, A. von Hoegen<sup>1</sup>, M. Först<sup>1</sup>, T. F. Nova<sup>1</sup>, P. Narang<sup>3,4</sup>, A. Maljuk<sup>5</sup>, A. V. Boris<sup>6</sup>, B. Keimer<sup>6</sup> & A. Cavalleri<sup>1,7</sup>✉

Nature 617, 73 (2023)

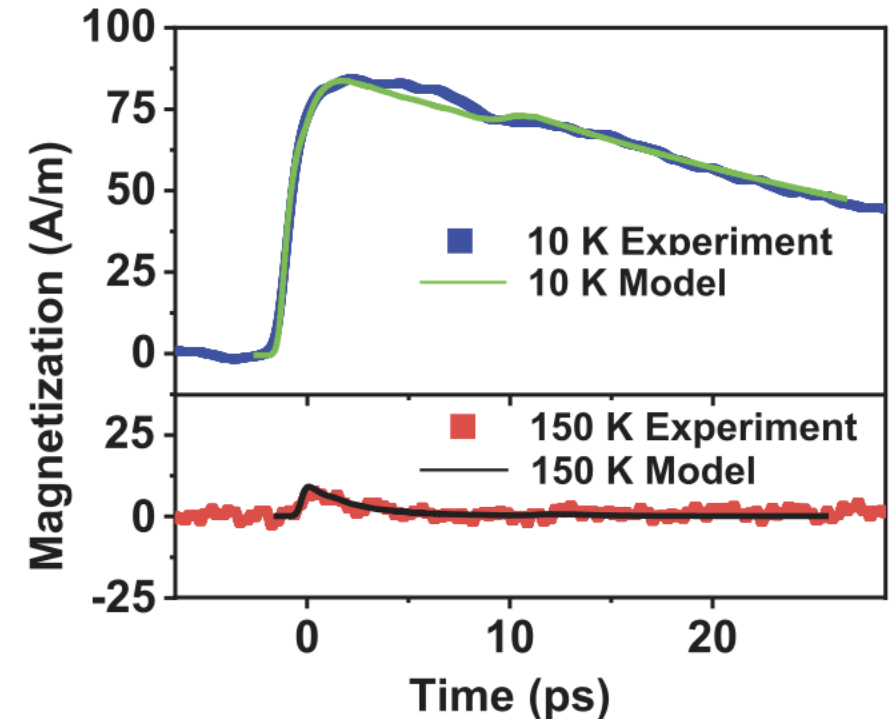


Phonon drive controls distortions in the crystal

## Large effective magnetic fields from chiral phonons in rare-earth halides

Jiaming Luo<sup>1,2</sup>, Tong Lin<sup>1</sup>, Junjie Zhang<sup>1</sup>, Xiaotong Chen<sup>1</sup>, Elizabeth R. Blackert<sup>1</sup>, Rui Xu<sup>1</sup>, Boris I. Yakobson<sup>1</sup>, Hanyu Zhu<sup>1\*</sup>

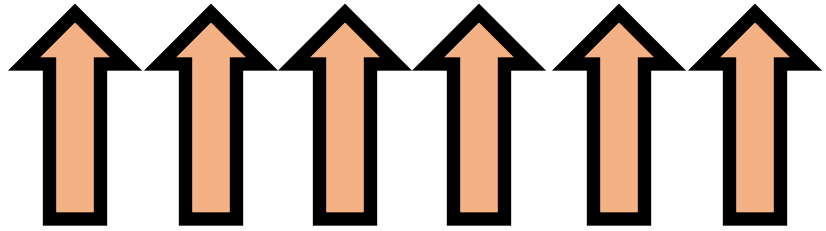
Luo *et al.*, *Science* **382**, 698–702 (2023)



Theory: D. Juraschek, T. Neuman, P. Narang, Phys. Rev. Res. 4, 013129 (2022)

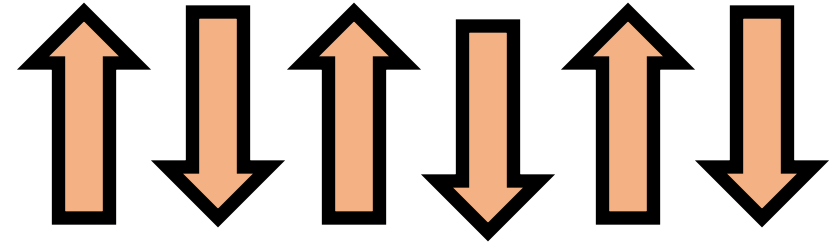
# Hidden orders in solids

# Quantum materials: Simple orders



Ferromagnetism ~ 600 BC

Easily observable  
(lodestone, fridge magnets)

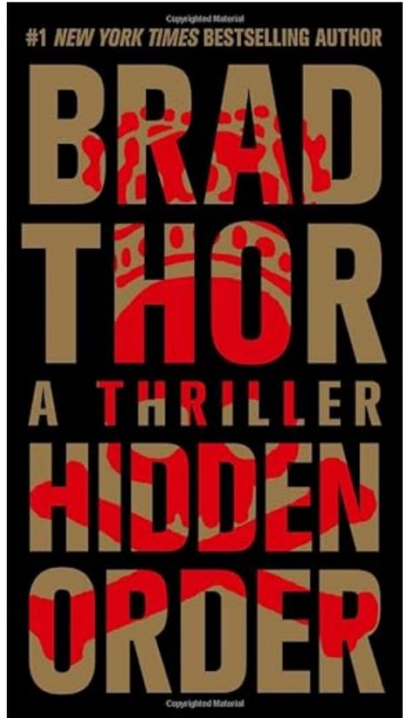


Antiferromagnetism

Neutron diffraction (1940s)

- Simple patterns of symmetry breaking
- Well developed experimental probes
- Even AFM is “hidden” until we can “see” the pattern

# What is hidden order?



## Hidden Order: A Thriller (12) (The Scot Harvath Series)



Mass Market Paperback – May 20, 2014

by [Brad Thor](#) (Author)

4.4 ★★★★★ 9,858 ratings 4.2 on Goodreads 17,203 ratings

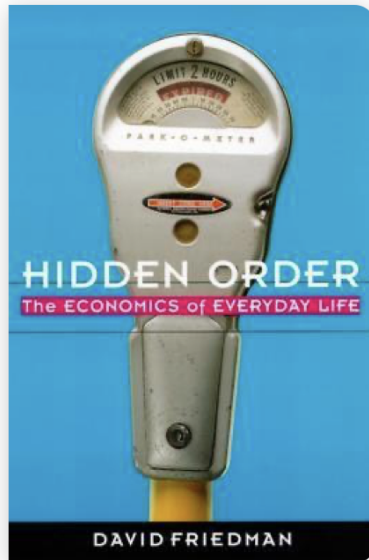
[Book 12 of 23: The Scot Harvath](#)

[See all formats and editions](#)

**#1 *New York Times* and #1 *Wall Street Journal* bestselling author Brad Thor returns with his hottest and most action-packed thriller yet!**

The most secretive organization in America operates without accountability to the American people. Hiding in the shadows, pretending to be part of the United States Government, its power is beyond measure.

Control of this organization has just been lost and the future of the nation has been thrust into peril.



## Hidden Order: The Economics of Everyday Life

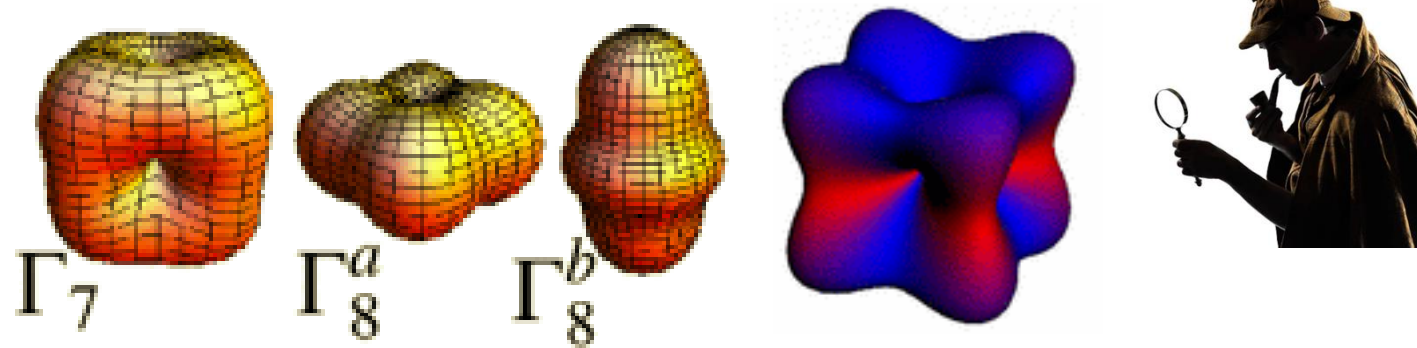
David D. Friedman

★★★★★ 3.74 505 ratings · 32 reviews

David Friedman has never taken an economics class in his life. Sure, he's taught economics at UCLA, Chicago, Tulane, Cornell, and Santa Clara, but don't hold that against him. After all, everyone's an economist. We all make daily decisions that rely, consciously or not, on an acute understanding of economic theory—from picking the fastest checkout time at the supermarket to voting or not voting, from negotiating the best job offer to finding the right person to marry. *Hidden Order* is an essential guide to rational living, revealing all you need to know to get through each day

# Hidden order in quantum materials

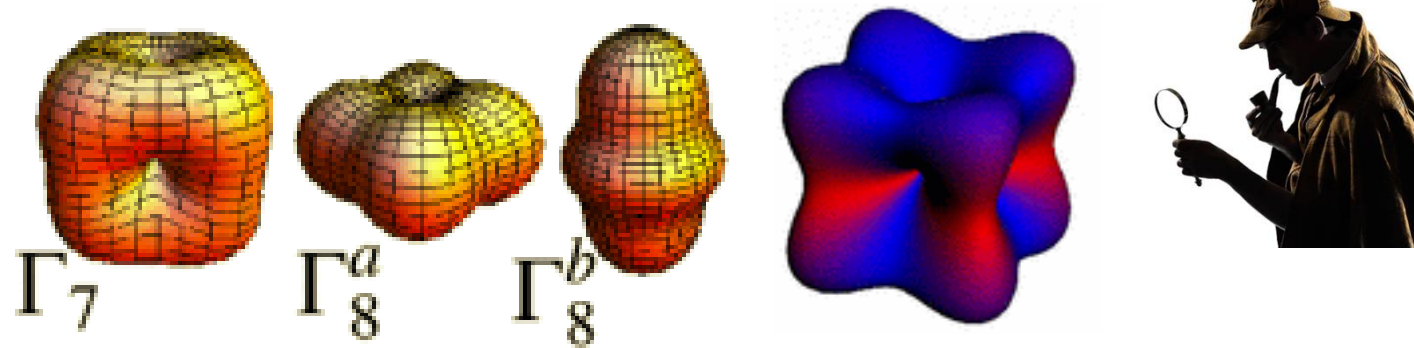
## Multipolar magnetism in spin-orbit coupled materials



Strong local entanglement of spins and orbital degrees of freedom

# Hidden order in quantum materials

## Multipolar magnetism in spin-orbit coupled materials



- Phase transition easily seen in thermodynamics (e.g., specific heat)
- Precise nature of hidden order: Very hard to unravel
- Many examples:  $\text{URu}_2\text{Si}_2$ ,  $\text{NpO}_2$ ,  $\text{PrV}_2\text{Al}_{20}$ , 5d transition metal oxides
- Similar difficulties arise in probing quantum spin liquids but with spatially extended entanglement – here it is “local entanglement” of many degrees of freedom (like “synthetic dimension”)

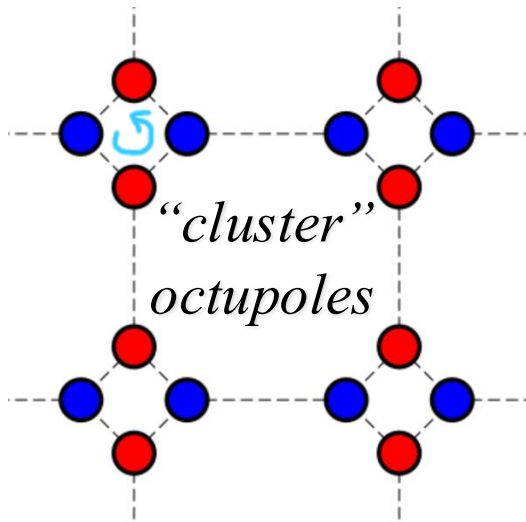
# “Cluster multipoles” in quantum materials

## Spin Altermagnets

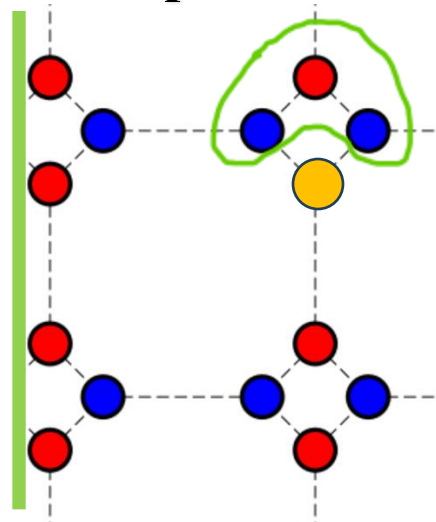
- Ferro-spin order (translationally invariant)
- Zero net magnetization (protected by point group symmetry)
- Spin-split electronic bands of interest for spintronics

Kivelson, et al Rev. Mod. Phys. (2003)  
Naka, et al, Nat Comm (2019)  
Smejkal, Sinova, Jungwirth PRX (2022)

**d-wave ferromagnet**

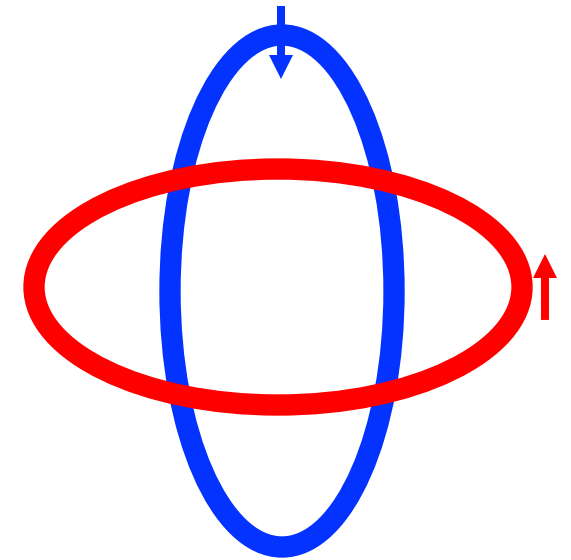
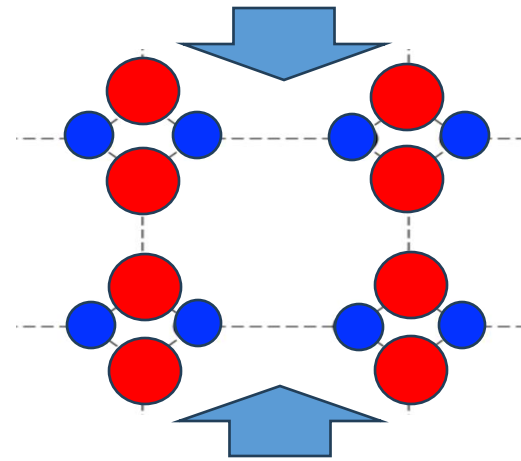


**Bulk impurity  
dipole moments**



**Surface  
magnetization**

**Piezomagnetism**



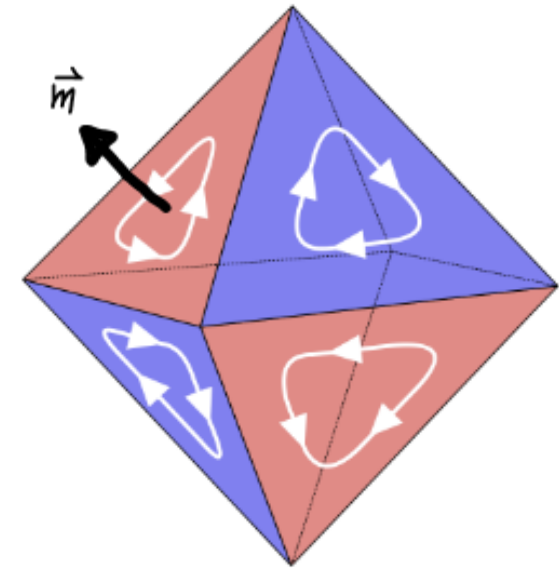
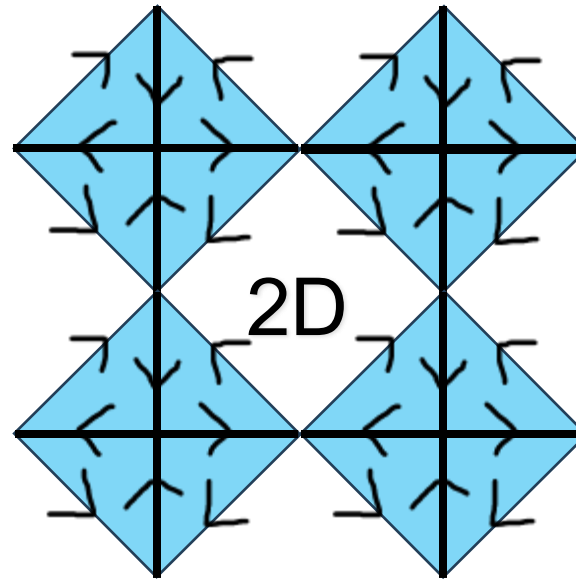
**Metallic regime**

# “Cluster multipoles” in quantum materials

## “Orbital” Altermagnets

## Loop current orders

Q=0 orbital magnetism



3D

(111) Surface

- orbital magnetization
- Kerr effect?

e.g., Loop currents in cuprates

Simon and Varma, PRL 2002

Varma, PRB 2006

Bourges, Bounoua, Sidis, Comptes Rendus 2021

# Toy example of “atomic multipoles”

Consider spin  $S=1$  at each site: three-level system

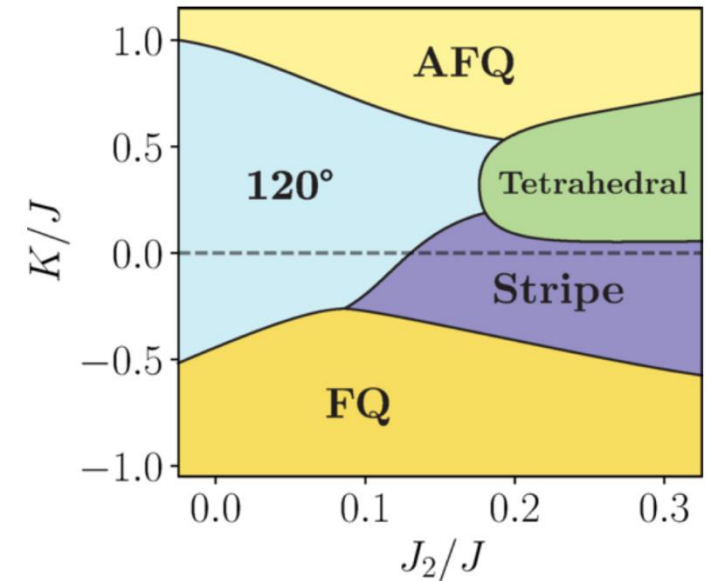
Local  $3 \times 3$  Hermitian operators: 9 observables

- Identity
- 3 Dipoles:  $S_x, S_y, S_z$
- 5 Quadrupoles:  $Q_{ab} = S_a S_b + S_b S_a$

**Moral:**

Bigger angular momentum  $\Rightarrow$  More multipoles ( $s=3/2$  allows octupoles, etc)

$(2S+1) = N \Rightarrow$  Nontrivial Hermitian matrices =  $N^2-1$  [SU(N) generators]



Triangular lattice

A. Szasz, C. Wang, Y.C. He (PRB 2022)

$$H = \sum_{i,j} \left[ J_{ij} \vec{S}_i \cdot \vec{S}_j + K_{ij} (\vec{S}_i \cdot \vec{S}_j)^2 \right]$$

# “Atomic multipoles” in rare-earth quantum materials

$\text{PrTi}_2\text{Al}_{20}$ ,  $\text{PrV}_2\text{Al}_{20}$

Diamond Lattice

$\text{Pr}^{3+} : J = 4$

$T_d$  crystal field splitting

$$|\Gamma_3^{(1)}\rangle = \frac{1}{2}\sqrt{\frac{7}{6}}|4\rangle - \frac{1}{2}\sqrt{\frac{5}{3}}|0\rangle + \frac{1}{2}\sqrt{\frac{7}{6}}|-4\rangle$$

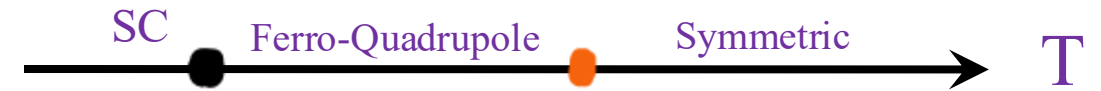
$$|\Gamma_3^{(2)}\rangle = \frac{1}{\sqrt{2}}|2\rangle + \frac{1}{\sqrt{2}}|-2\rangle.$$

$$\tau_x \propto J_x^2 - J_y^2 \quad \rightarrow \quad \text{Quadrupolar charge density}$$

$$\tau_z \propto 3J_z^2 - J^2$$

$$\tau_y \propto \text{Sym} [J_x J_y J_z] \quad \rightarrow \quad \text{Ising magnetic octupole}$$

$\text{PrTi}_2\text{Al}_{20}$



Recent work: A. Sakai, et al, Nat. Comm 16:2114 (2025)

$\text{PrV}_2\text{Al}_{20}$



M. Tsujimoto, et al, PRL 113, 267001 (2014)

*Multipolar orders*

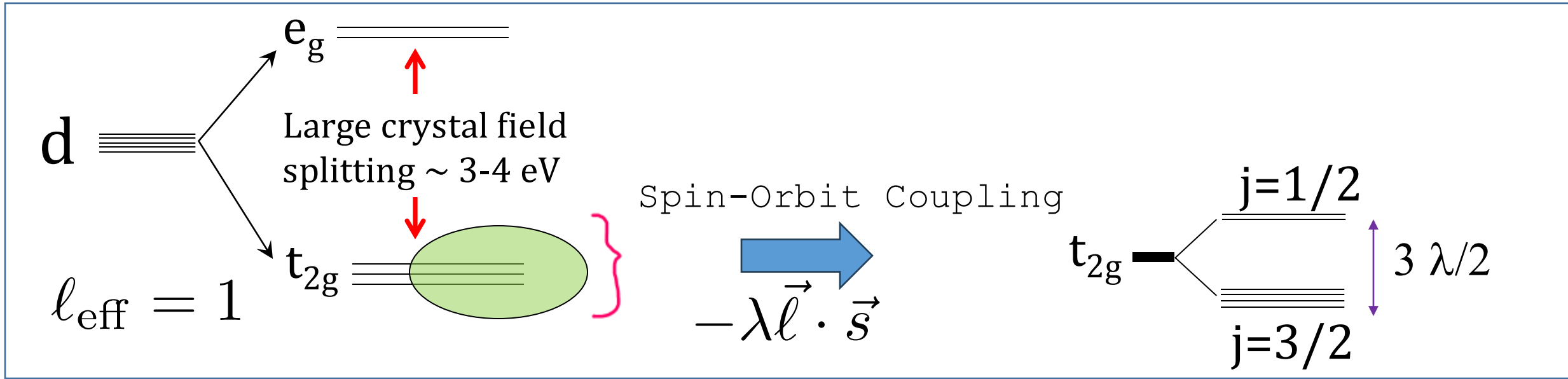
F. Freyer, J. Attig, S.B. Lee, **AP**, S. Trebst, Y.B. Kim (PRB 2017)

S. B. Lee, S. Trebst, Y. B. Kim, **AP** (PRB 2018)

A. Patri, A. Sakai, S B Lee, **AP** S. Nakatsuji, Y B Kim, Nat. Comm. (2019)

F. Freyer, S.B. Lee, Y B Kim, S Trebst, **AP**, PRR (2020)

# “Atomic multipoles” in d-orbital quantum materials

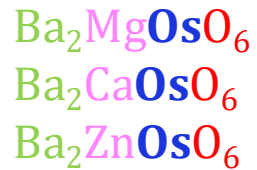
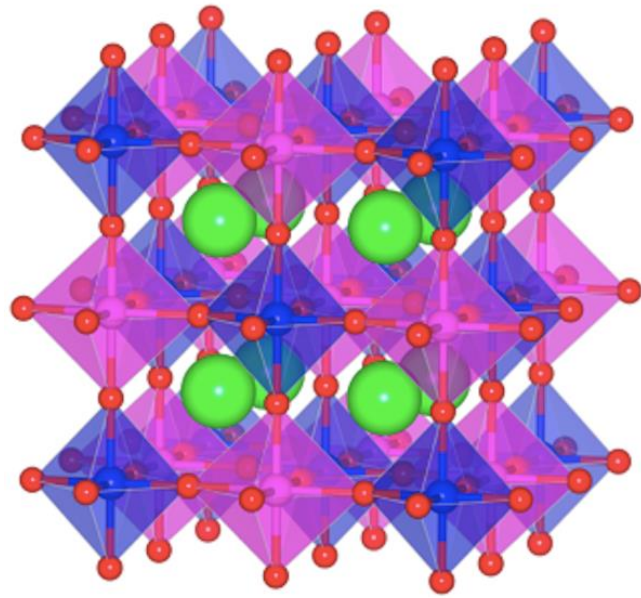


Adding local Coulomb interaction:

| $d^1$   | $d^2$ | $d^3$   | $d^4$ | $d^5$   |
|---------|-------|---------|-------|---------|
| $j=3/2$ | $J=2$ | $J=3/2$ | $J=0$ | $j=1/2$ |

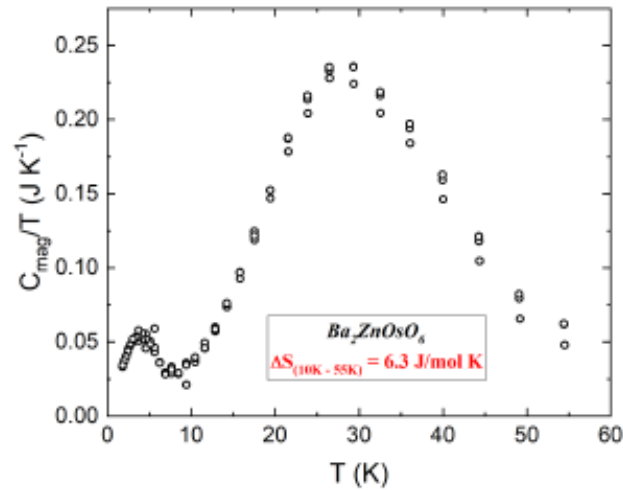
Candidates for “atomic multipolar” order: Quadrupoles, Octupoles, etc.

# 5d<sup>2</sup> Double Perovskites: Puzzles around hidden J=2 magnetism

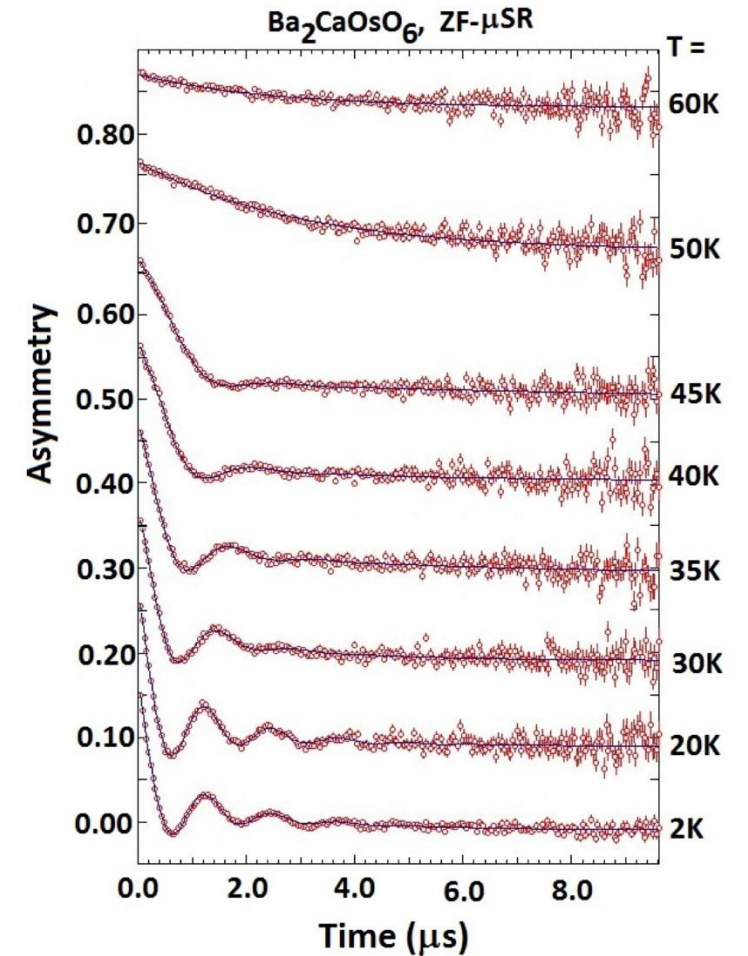


*C. M. Thompson, et al, JPCM 2014*  
*C. A. Marjerrison, et al, PRB 2016*

**Measured Entropy  $\sim R \ln 2$**   
**Not  $2J+1 \Rightarrow R \ln 5$**



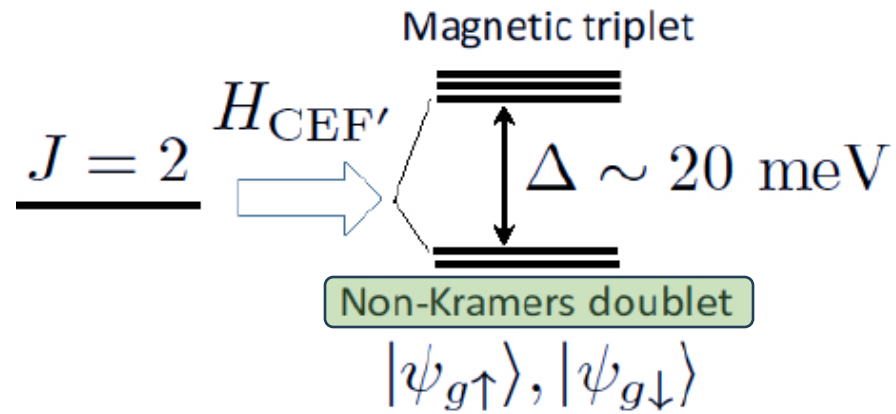
**$\mu$ SR: Time reversal broken**  
**Very weak internal field**



**Robust  $T_c$ , yet no sign of magnetic order in neutron diffraction**

| System                      | $T^*$ | $\theta_{CW}$ | $a$ (Å) | Ref. | $\mu_{ord}$   |
|-----------------------------|-------|---------------|---------|------|---------------|
| $\text{Ba}_2\text{CaOsO}_6$ | 49    | $-156.2(3)$   | 8.3456  | [13] | $< 0.11\mu_B$ |
| $\text{Ba}_2\text{MgOsO}_6$ | 51    | $-120(1)$     | 8.0586  | [15] | $< 0.13\mu_B$ |
| $\text{Ba}_2\text{ZnOsO}_6$ | 30    | $-149.0(4)$   | 8.0786  | [15] | $< 0.06\mu_B$ |

# 5d<sup>2</sup> Double Perovskites: Potential resolution of puzzles



$$|\psi_{g,\uparrow}\rangle = |0\rangle$$

$$|\psi_{g,\downarrow}\rangle = \frac{1}{\sqrt{2}}(|2\rangle + |-2\rangle)$$

$$\begin{aligned} \tau_x &\propto J_x^2 - J_y^2 \\ \tau_z &\propto 3J_z^2 - J^2 \\ \tau_y &\propto \text{Sym} [J_x J_y J_z] \end{aligned}$$

Quadrupolar charge density  $\sim E_g$

Ising magnetic octupole

- ✓ Entropy:  $R \ln 2$  (unless very high T)
- ✓ No dipole order: No dipole matrix elements
- ✓ Spin gap: Doublet-Triplet gap
- ✓ T-breaking order: Hidden octupolar order!

First example of d-orbital octupolar order

## Phenomenology and microscopics

Data: D. D. Maharaj, et al PRL 124, 087206 (2020)

Proposal: Paramakanti, et al, PRB 101, 054439 (2020)

muSR: S. Voleti, et al, AP, PRB 101, 155118 (2020)

LDA+DMFT: Pourovskii, Mosca, Franchini, PRL (2021)

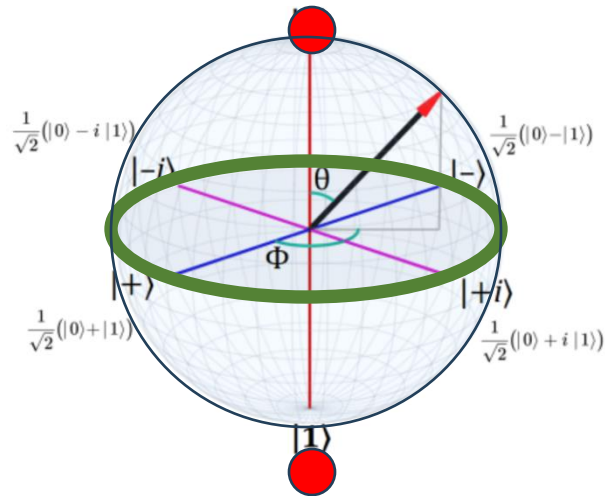
Tight binding + ED: Voleti, Haldar, Paramakanti, PRB (2021)

Tight binding + ED: Churchill, Kee, PRB (2022)

NMR: S. Voleti, et al, AP, npjQM (2023)

Can we use phonons to probe and control hidden orders?

# Non-Kramers doublet on the Bloch sphere



- Poles: Octupolar +/-
- Equator: Quadrupolar states

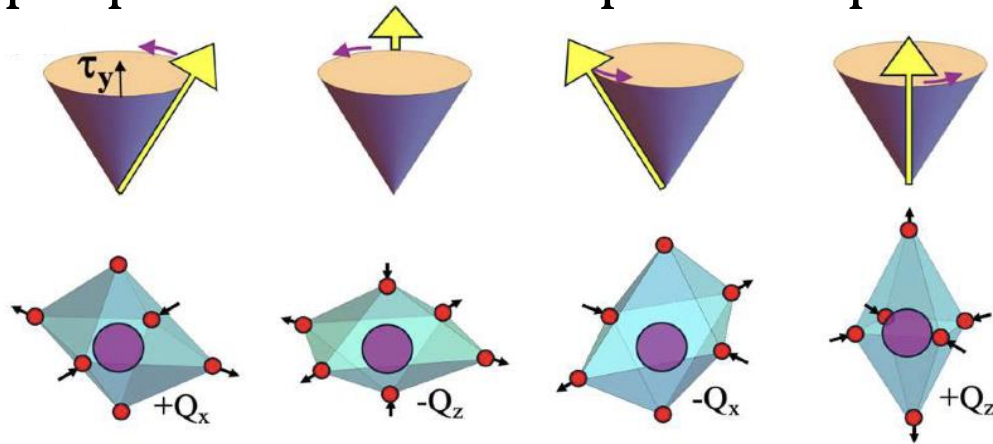
- Eg phonons linearly couple to quadrupole moment

$$H_{\text{sp-ph}} = -\lambda \sum_{\mathbf{r}} [Q_x(\mathbf{r})\tau_{\mathbf{r}x} + Q_z(\mathbf{r})\tau_{\mathbf{r}z}] \quad \begin{cases} x \equiv x^2 - y^2 \\ z \equiv 3z^2 - r^2 \end{cases}$$

- Can we use phonons as a fictitious “field” to probe and manipulate the state (like NMR)?

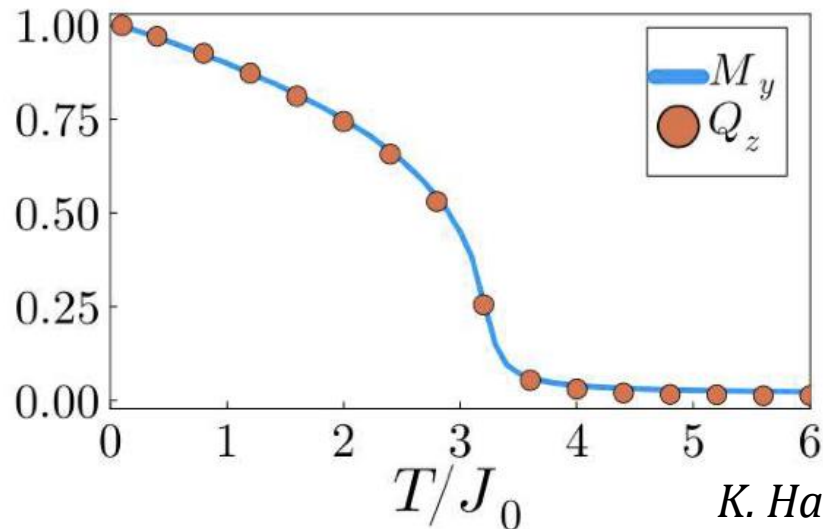
# Pump-probe: Kick X-mode, track Z-mode

Pseudospin precession drives phonon “precession”

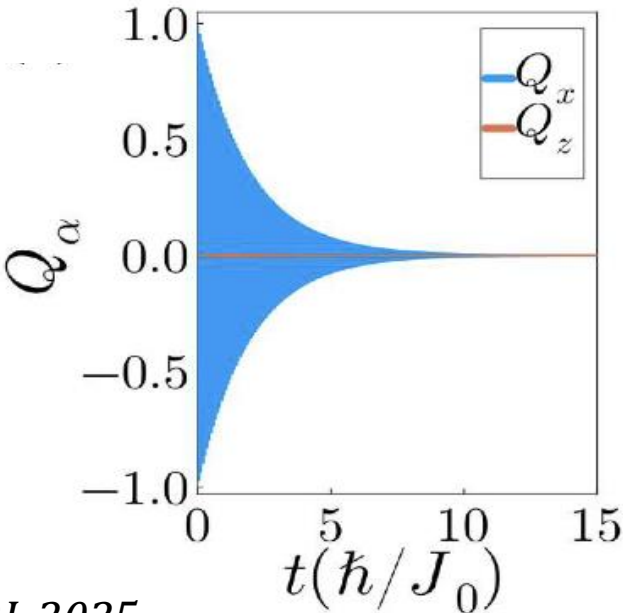
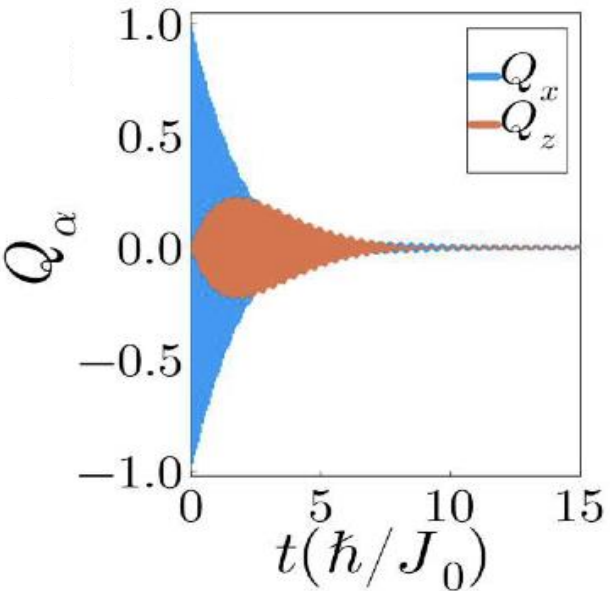


$$H_{\text{sp-ph}} = -\lambda \sum_{\mathbf{r}} [Q_x(\mathbf{r})\tau_{\mathbf{r}x} + Q_z(\mathbf{r})\tau_{\mathbf{r}z}]$$

Computed cross-response tracks octupolar order



# Spin-Phonon Molecular Dynamics Simulations



# Phonon Green function

- Eg phonon frequency  $\gg$  spin oscillations
- Phonons see “frozen” spin configuration
- Average phonon Green function over instantaneous spin configs (Monte Carlo) after integrating out spin-wave fluctuations at  $\mathcal{O}(1/S)$ .

$$\mathcal{G}_{xx}^{-1}(\mathbf{r}, i\nu_n) = -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\Delta_{\mathbf{r}}^x}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

$$\mathcal{G}_{zx}^{-1}(\mathbf{r}, i\nu_n) = \mathcal{G}_{xz}^{-1}(\mathbf{r}, -i\nu_n) = -4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\chi_{\mathbf{r}} + i\nu_n\gamma_{\mathbf{r}}}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

$$\mathcal{G}_{zz}^{-1}(\mathbf{r}, i\nu_n) = -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\Delta_{\mathbf{r}}^z}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

# Phonon Green function

- Eg phonon frequency  $\gg$  spin oscillations
- Phonons see “frozen” spin configuration
- Average phonon Green function over instantaneous spin configs (Monte Carlo) after integrating out spin-wave fluctuations at  $\mathcal{O}(1/S)$ .

$$\begin{aligned}\mathcal{G}_{xx}^{-1}(\mathbf{r}, i\nu_n) &= -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}} \overset{\text{↙}}{\Delta_{\mathbf{r}}^x}}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right] \\ \mathcal{G}_{zx}^{-1}(\mathbf{r}, i\nu_n) &= \mathcal{G}_{xz}^{-1}(\mathbf{r}, -i\nu_n) = -4S\lambda^2 \left[ \frac{2h_{\mathbf{r}} \overset{\text{↘}}{\chi_{\mathbf{r}}} + i\nu_n \overset{\text{↘}}{\gamma_{\mathbf{r}}}}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right] \\ \mathcal{G}_{zz}^{-1}(\mathbf{r}, i\nu_n) &= -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}} \overset{\text{↖}}{\Delta_{\mathbf{r}}^z}}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]\end{aligned}$$

Information about local  
Weiss field strength and  
orientation

# Phonon Green function

- Eg phonon frequency  $\gg$  spin oscillations
- Phonons see “frozen” spin configuration
- Average phonon Green function over instantaneous spin configs (Monte Carlo) after integrating out spin-wave fluctuations at  $\mathcal{O}(1/S)$ .

$$\mathcal{G}_{xx}^{-1}(\mathbf{r}, i\nu_n) = -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\Delta_{\mathbf{r}}^x}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

$$\mathcal{G}_{zx}^{-1}(\mathbf{r}, i\nu_n) = \mathcal{G}_{xz}^{-1}(\mathbf{r}, -i\nu_n) = -4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\chi_{\mathbf{r}} + i\nu_n\gamma_{\mathbf{r}}}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

$$\mathcal{G}_{zz}^{-1}(\mathbf{r}, i\nu_n) = -i\nu_n + \Omega_0 - 4S\lambda^2 \left[ \frac{2h_{\mathbf{r}}\Delta_{\mathbf{r}}^z}{(i\nu_n)^2 - 4h_{\mathbf{r}}^2} \right]$$

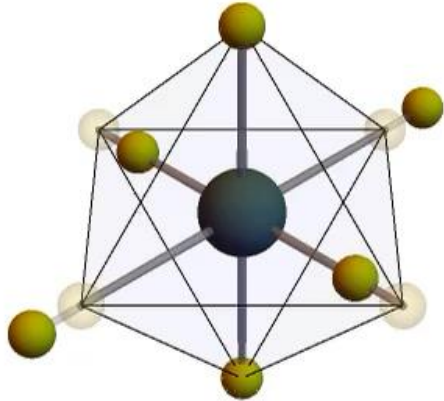
- Octupolar order leads to off-diagonal Green function coupling Eg modes  $\sim$  “Hall effect”

$$\begin{pmatrix} -i\nu_n + \Omega_0 + \delta\Omega & i\Phi \\ -i\Phi & -i\nu_n + \Omega_0 + \delta\Omega \end{pmatrix}$$

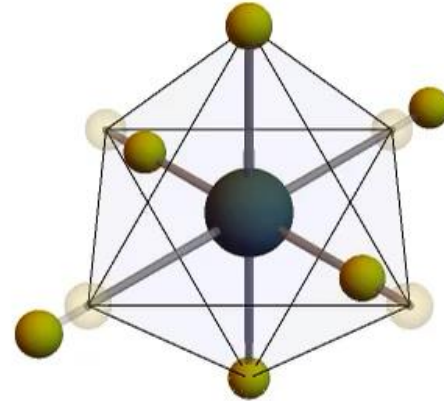
# Pseudochiral phonons peering down [111] axis

$\omega t/2\pi=0.$

$\omega t/2\pi=0.$



$Q^+$



$Q^-$

$$R'(Q^+) = \begin{pmatrix} -i a^+ & a^+ & \sqrt{2} a^+ \\ a^+ & i a^+ & -i \sqrt{2} a^+ \\ \sqrt{2} a^+ & -i \sqrt{2} a^+ & 0 \end{pmatrix}$$

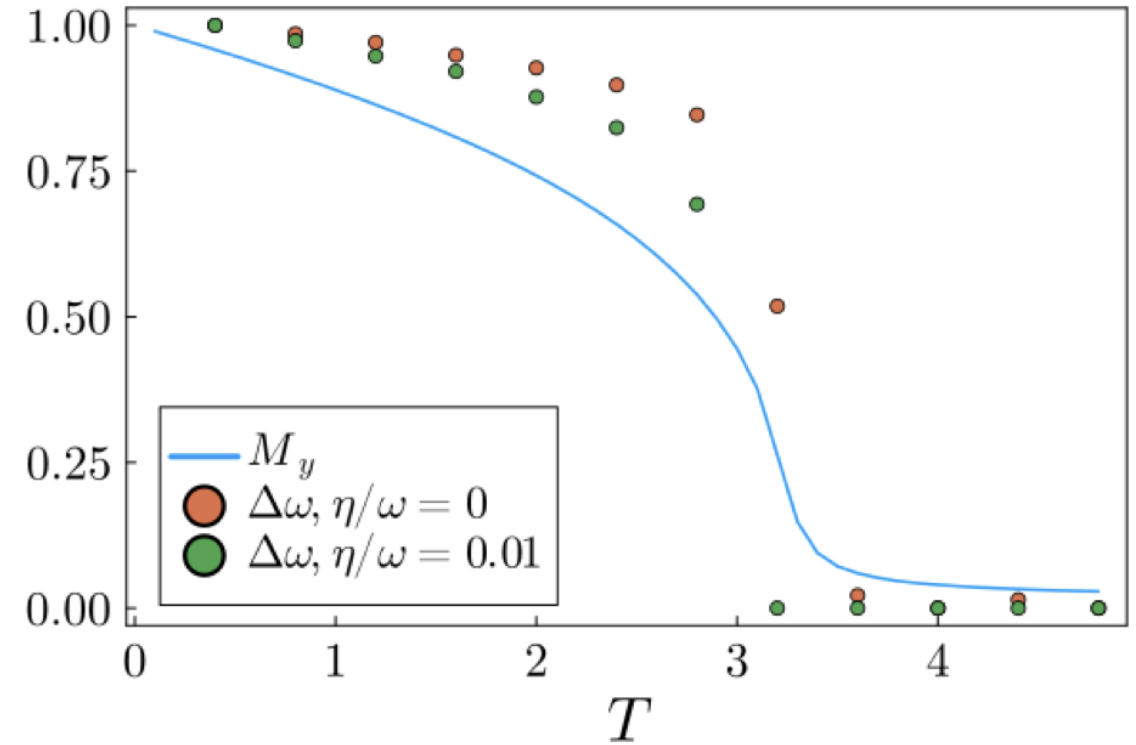
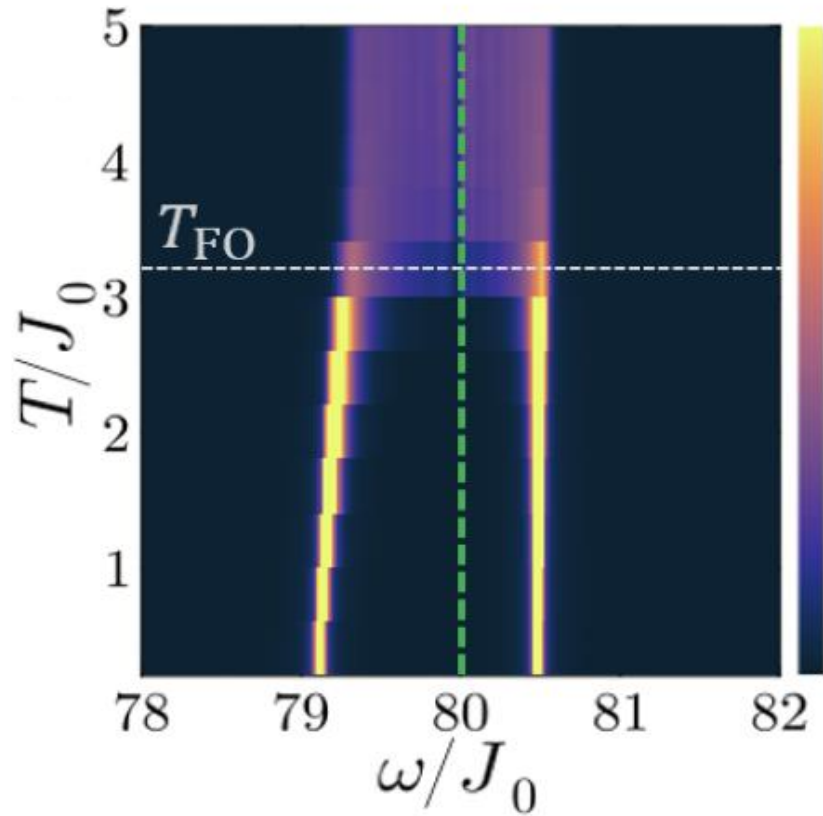
$$R'(Q^-) = \begin{pmatrix} i a^- & 0 & \sqrt{2} a^- \\ 0 & -i a^- & i \sqrt{2} a^- \\ \sqrt{2} a^- & i \sqrt{2} a^- & 0 \end{pmatrix}$$

$$|\sigma^+ \cdot R'(Q^+) \cdot \sigma^-|^2 = |a^+|^2$$

$$|\sigma^- \cdot R'(Q^-) \cdot \sigma^+|^2 = |a^-|^2$$

Detect using Raman scattering  
in cross-circular channel

# Phonon spectral function



Probe using cross-circular Raman scattering

# Controlling hidden order via phonons

Chiral phonon drive

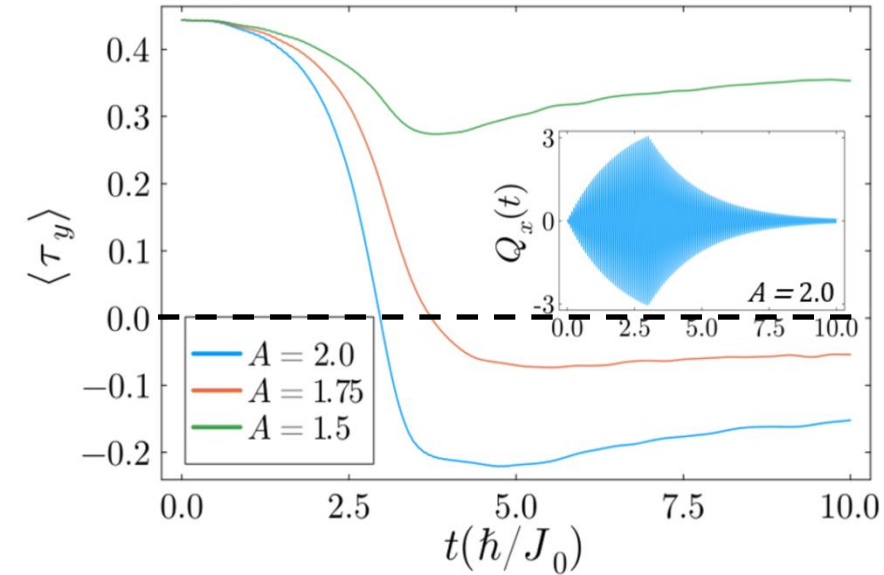
$$H_{\text{drive}}^{\text{ph}} = -A \sum_{\mathbf{r}} [Q_x(\mathbf{r}) \cos(\Omega t) + Q_z(\mathbf{r}) \cos(\Omega t - \phi)]$$

Floquet  
analysis

$$H_{\text{drive},0}^{\text{sp}} = 0; \quad H_{\text{drive},\pm}^{\text{sp}} = -\frac{\lambda Q_0}{2} \sum_{\mathbf{r}} (\tau_{\mathbf{r}x} + e^{\mp i\phi} \tau_{\mathbf{r}z})$$

$$H_{\text{drive}}^{\text{sp,eff}} = \frac{1}{\Omega} [H_{\text{drive},+}^{\text{sp}}, H_{\text{drive},-}^{\text{sp}}] = \frac{\lambda^2 Q_0^2}{\Omega} \sin \phi \sum_{\mathbf{r}} \tau_{\mathbf{r}y}$$

Chiral phonon driven growth of octupolar domains



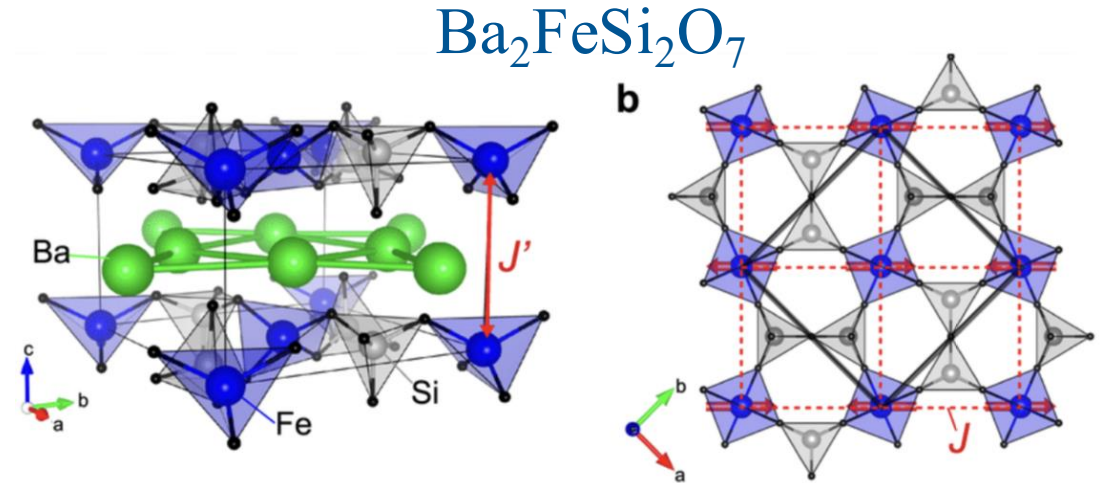
Phonon driven switching  
of octupolar order

# Spin-1 coupled to phonons: SU(3) Monte Carlo and Dynamics

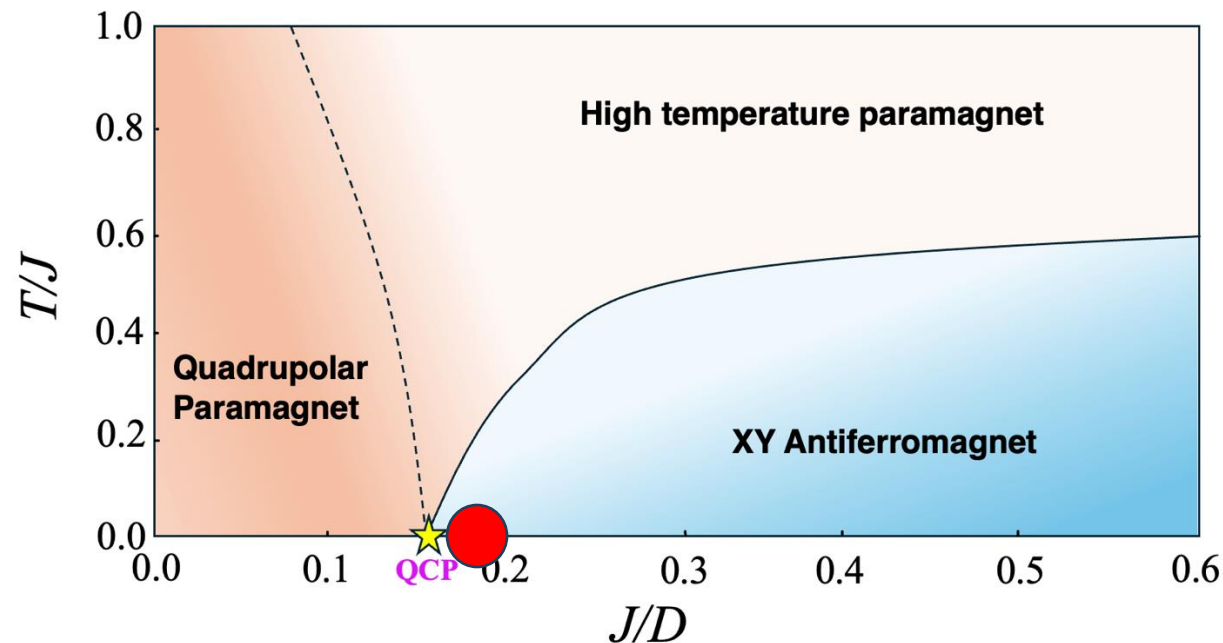
$$S_z = \pm 1 \quad \text{Exciton}$$

$$S_z = 0 \quad \text{Ground state}$$

$$H = DS_z^2$$



$$H_{\text{sp}} = \sum_{\langle \mathbf{r}, \mathbf{r}' \rangle} J_{\mathbf{r}\mathbf{r}'} \mathbf{S}(\mathbf{r}) \cdot \mathbf{S}(\mathbf{r}') + D \sum_{\mathbf{r}} S_z^2(\mathbf{r})$$



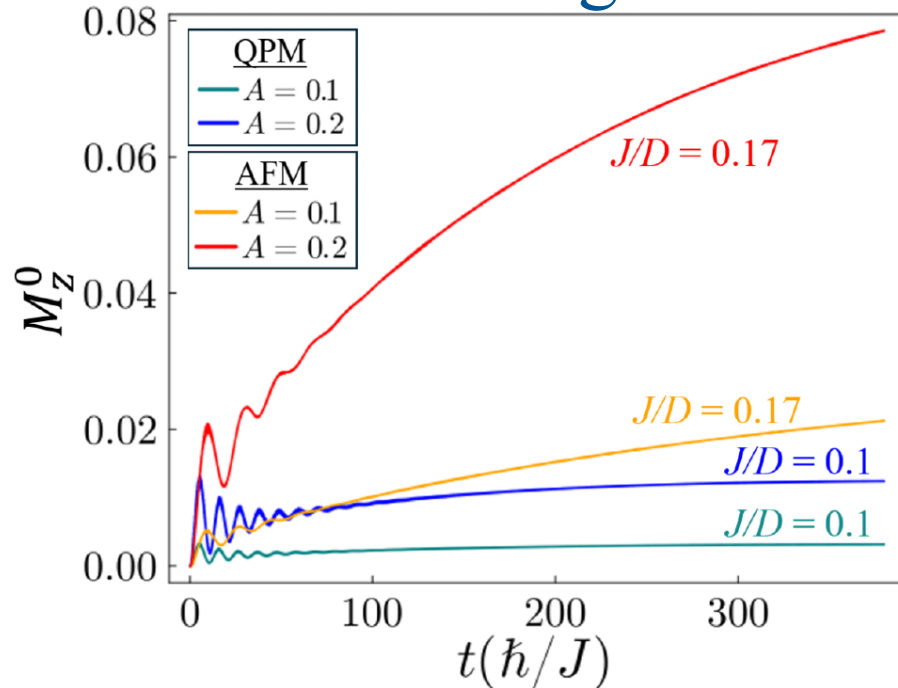
Consider phonons:  $(Q_{xz}, Q_{yz})$

Couple to  $\begin{cases} T_{xz} = S_x S_z + S_z S_x \\ T_{yz} = S_y S_z + S_z S_y \end{cases}$

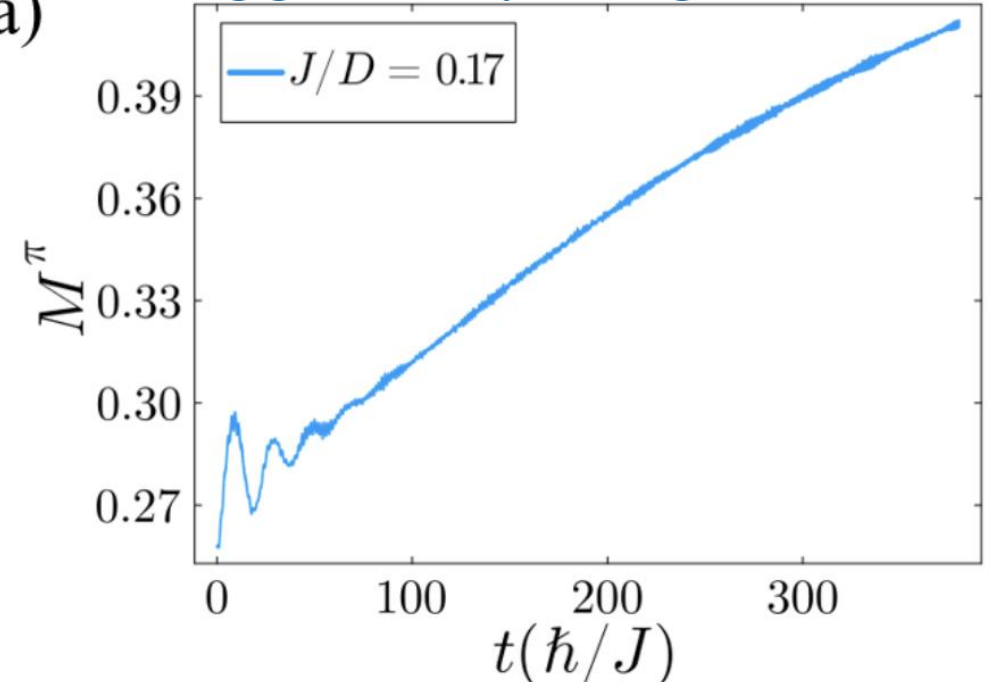
# Impact of Chiral Phonon Drive

$$H_{\text{drive}}^{\text{ph}} = -A \sum_{\mathbf{r}} (Q_{xz}(\mathbf{r}) \cos \Omega t + Q_{yz}(\mathbf{r}) \sin \Omega t)$$

## Uniform z-magnetization



## (a) Staggered xy-magnetization



Creates a nonzero  $S_z$  magnetization, strengthens AFM order  
Phonon induced  $\langle S_z \rangle$  could be potentially detected via Kerr rotation

# Chiral Phonon Drive: High Frequency Magnus Expansion

$$\begin{bmatrix} H_0 - \Omega & H_{\text{drive}} \\ H_{\text{drive}} & H_0 \end{bmatrix} \begin{matrix} H_{\text{drive}} \\ H_{\text{drive}} \end{matrix}$$

The diagram shows a 2x2 matrix with elements  $H_0 - \Omega$ ,  $H_{\text{drive}}$ ,  $H_{\text{drive}}$ , and  $H_0$ . To the right of the matrix, the terms  $H_{\text{drive}}$  and  $H_{\text{drive}}$  are listed. Pink arrows indicate the sequence of terms in the Magnus expansion: from the top-right  $H_{\text{drive}}$  to the bottom-right  $H_{\text{drive}}$ , and from the bottom-right  $H_{\text{drive}}$  to the bottom-left  $H_{\text{drive}}$ .

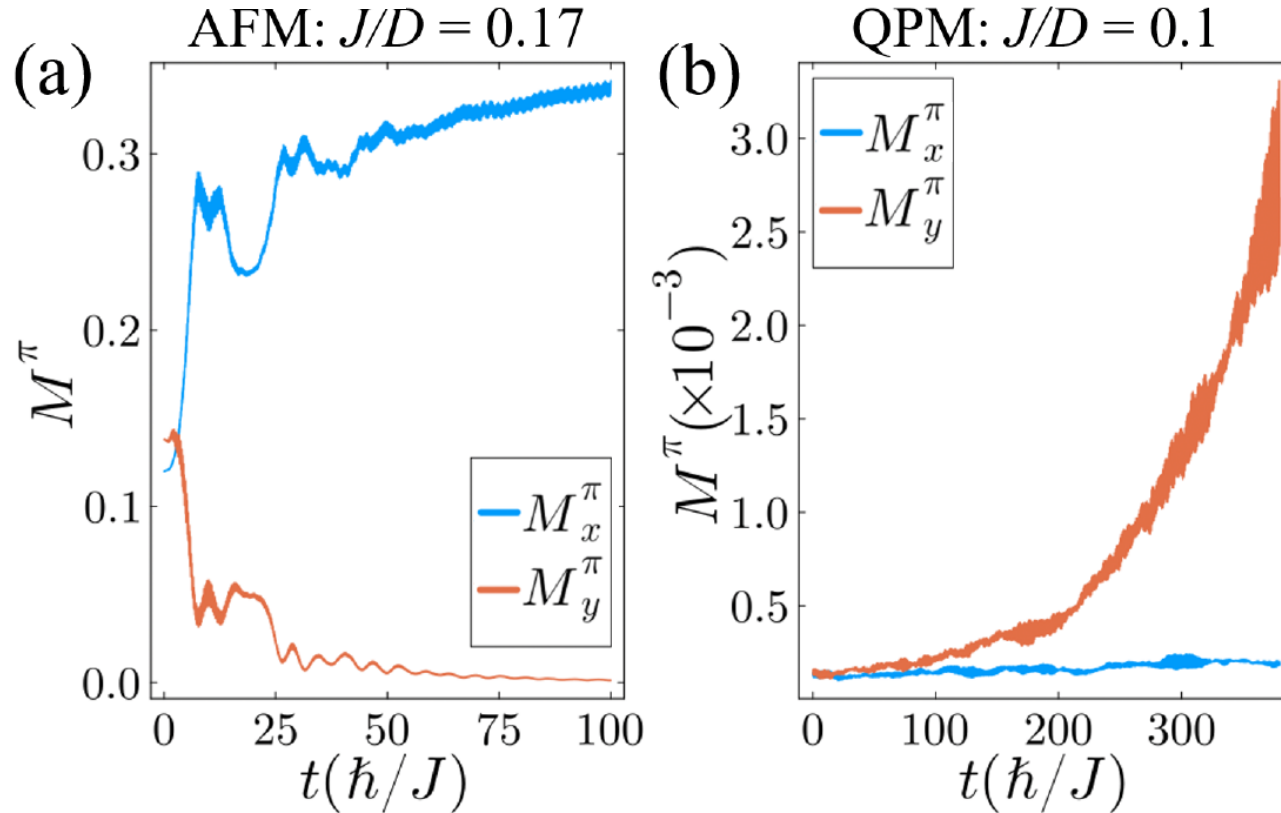
$$H_{\text{drive},0}^{\text{sp}} = 0; \quad H_{\text{drive},\pm}^{\text{sp}} = -\frac{\lambda Q_0}{2} \sum_{\mathbf{r}} (T_{xz}(\mathbf{r}) \mp iT_{yz}(\mathbf{r}))$$

$$H_{\text{drive}}^{\text{sp,eff}} = \frac{1}{\Omega} [H_{\text{drive},+}^{\text{sp}}, H_{\text{drive},-}^{\text{sp}}] = -\frac{\lambda^2 Q_0^2}{2\Omega} \sum_{\mathbf{r}} S_z(\mathbf{r})$$

- Chiral phonon drive generates an effective Floquet magnetic field
- Lowers Heisenberg symmetry to XY symmetry suppressing AFM fluctuations

# Impact of Single Phonon Drive

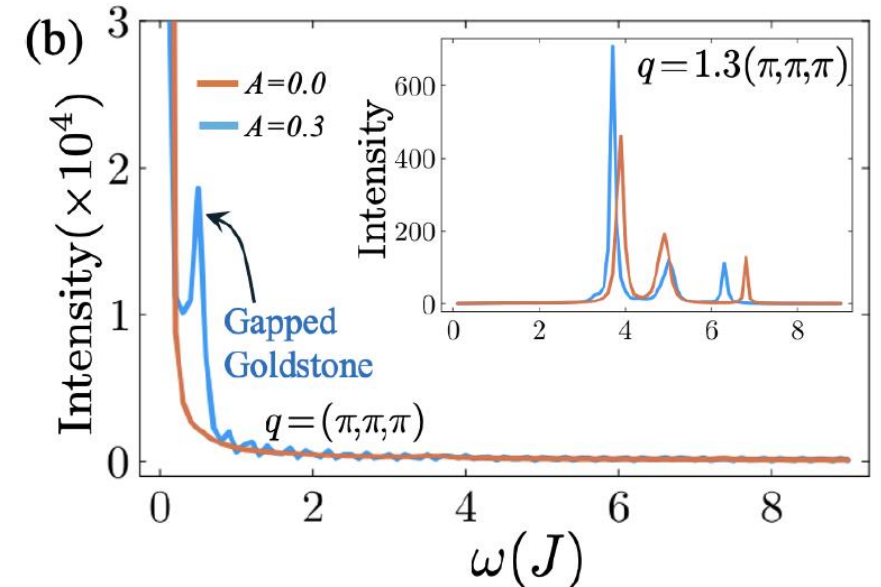
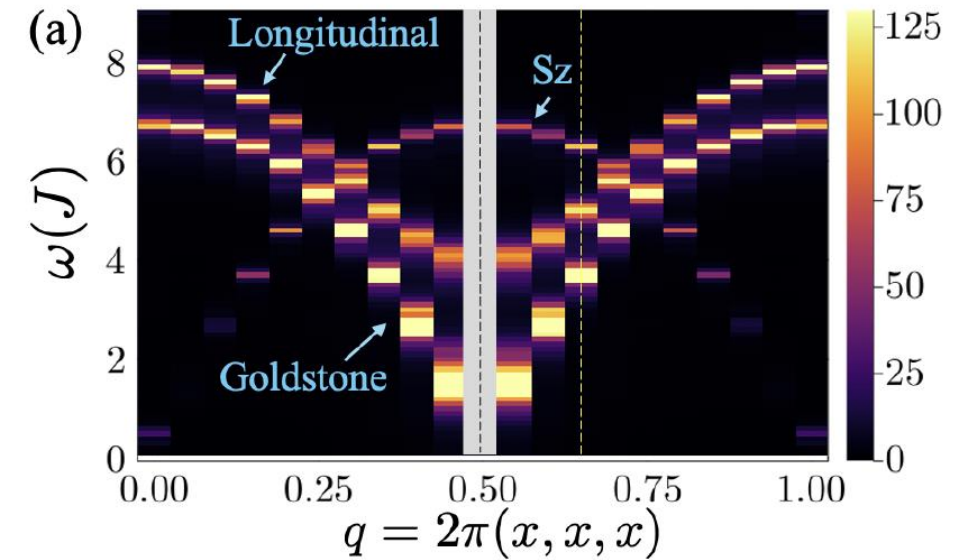
$$H_{\text{drive}}^{\text{ph}} = -A \sum_{\mathbf{r}} \cos(\Omega t) Q_{xz}(\mathbf{r})$$



- Creates uniaxial strengthening of AFM order, breaking XY symmetry
- Creates weak Ising AFM order in the quadrupolar paramagnet

# Single Phonon Drive: Gapping the Nambu-Goldstone mode

- Compute  $S(q, \omega)$  in the full driven system on large lattice sizes
- Phonon drive renormalizes all branches
- Emergence of a gapped NG mode reflects weak drive-induced Ising anisotropy



# Collaborators

## PhD students



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Pradhan



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Swati Chaudhary



Bruce Gaulin



Dalini Maharaj

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Edwin Kermarrec, Clemens Ritter,  
Francois Fauth, Casey Marjerrison,  
John Greedan, Graeme Luke

## Caltech



Gil Refael

# Summary

1. Phonons: Can carry angular momentum and show chiral splittings
2. Multipolar Order: Serves to synthesize various forms of hidden order
  - Spin altermagnets
  - Loop current orders
  - Octupolar order
3. Phonons can serve to probe, drive, and switch multipolar orders