

Quantum Computing Architectures with Superconducting Circuits

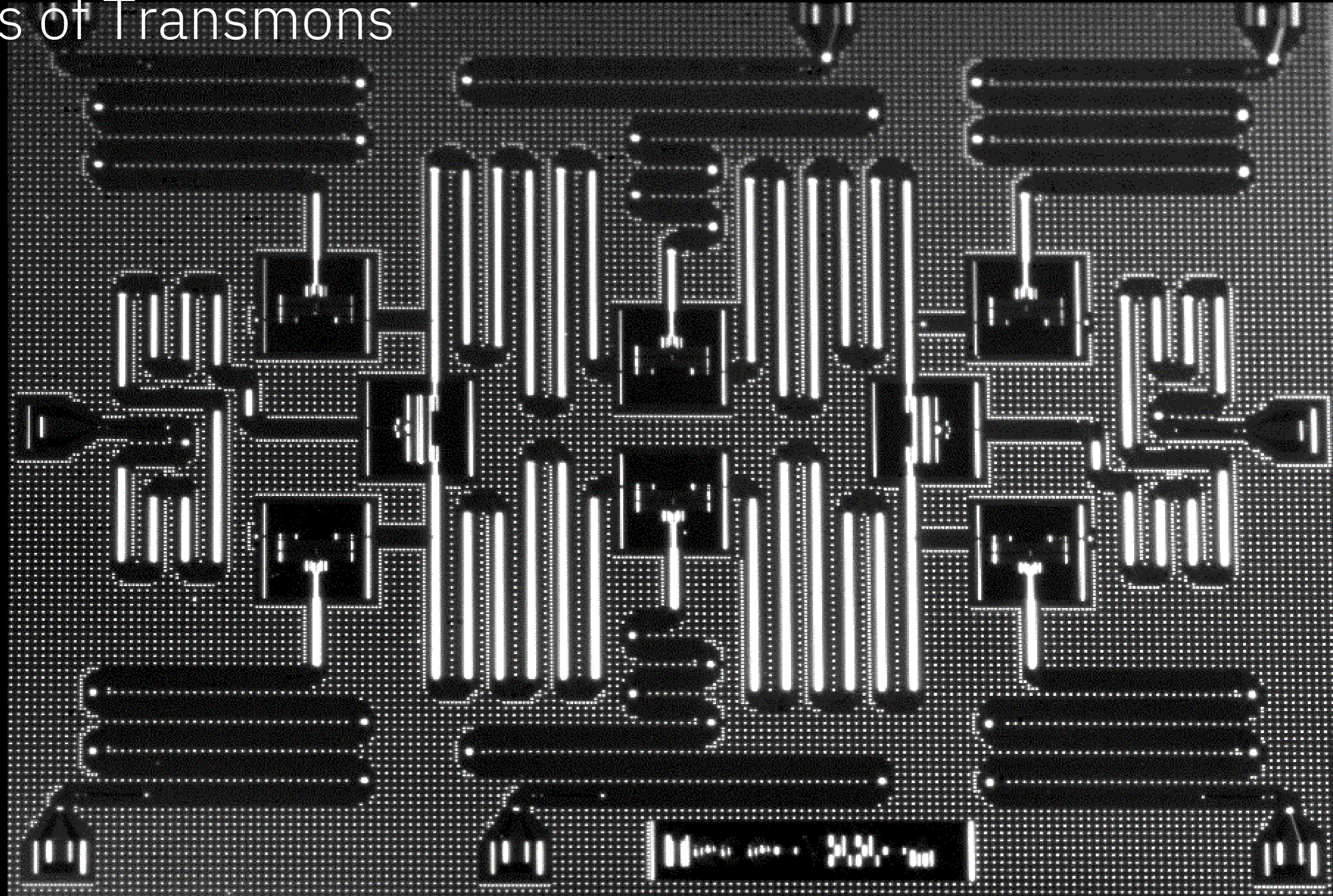
Oliver Dial

IBM Quantum mission

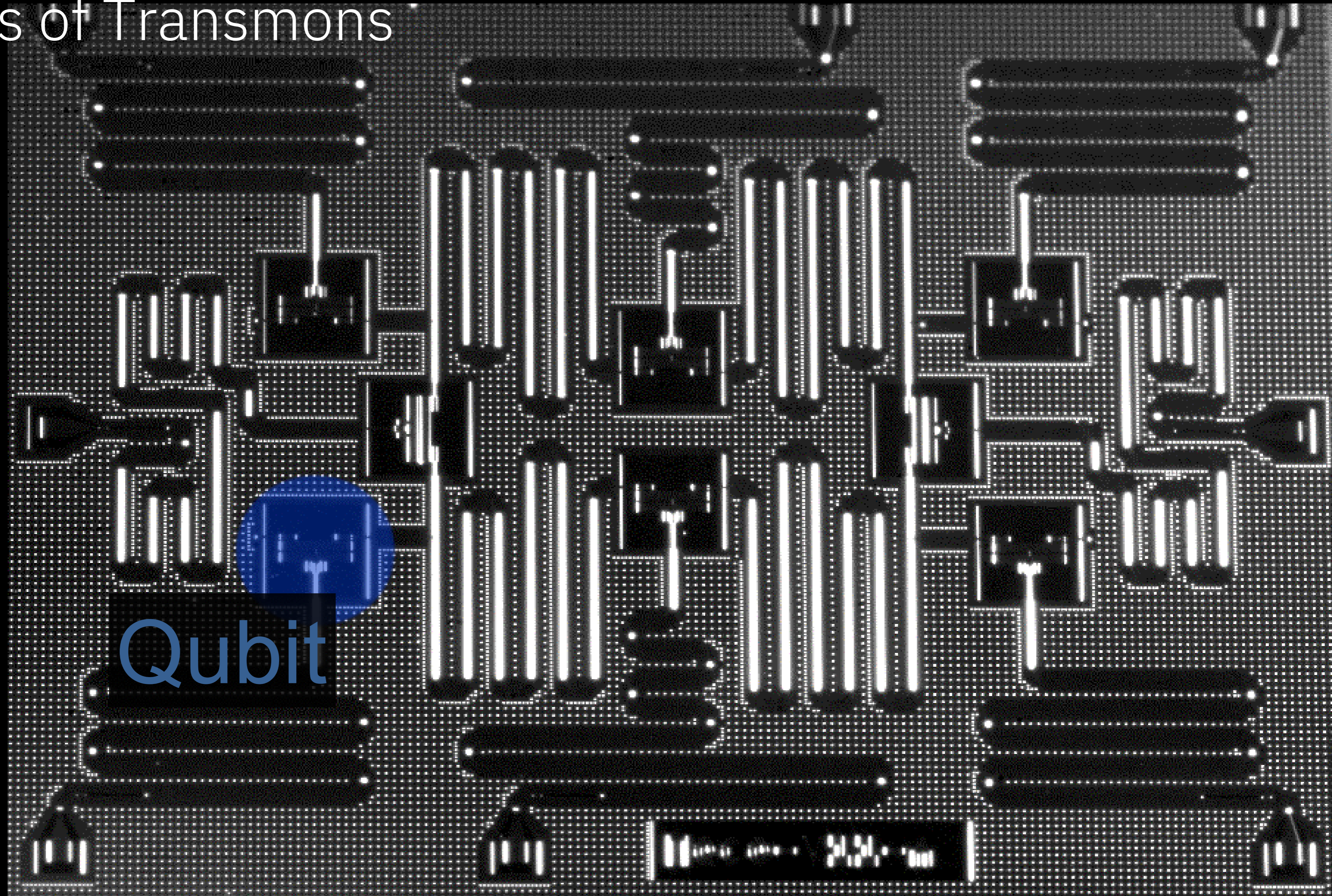
Bring useful
quantum
computing to
the world



Circuits of Transmons

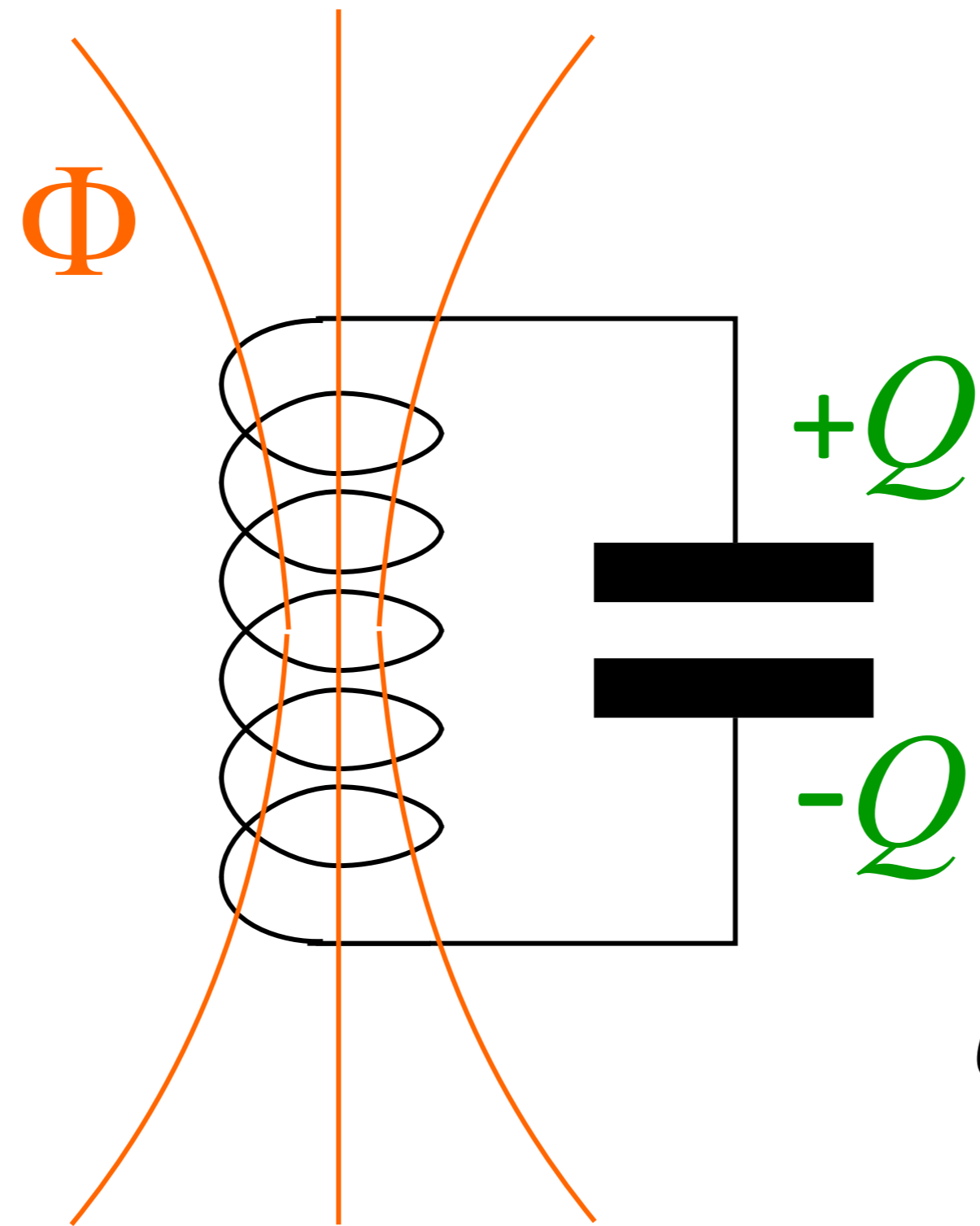


Circuits of Transmons



Qubit

Quantum linear circuits



$$L \sim 0.1 \text{ nH}$$
$$C \sim 10 \text{ pF}$$

$$1 \text{ K} \approx 20 \text{ GHz}$$

$$\omega_0/2\pi = 1/2\pi\sqrt{LC} \sim 5 \text{ GHz}$$

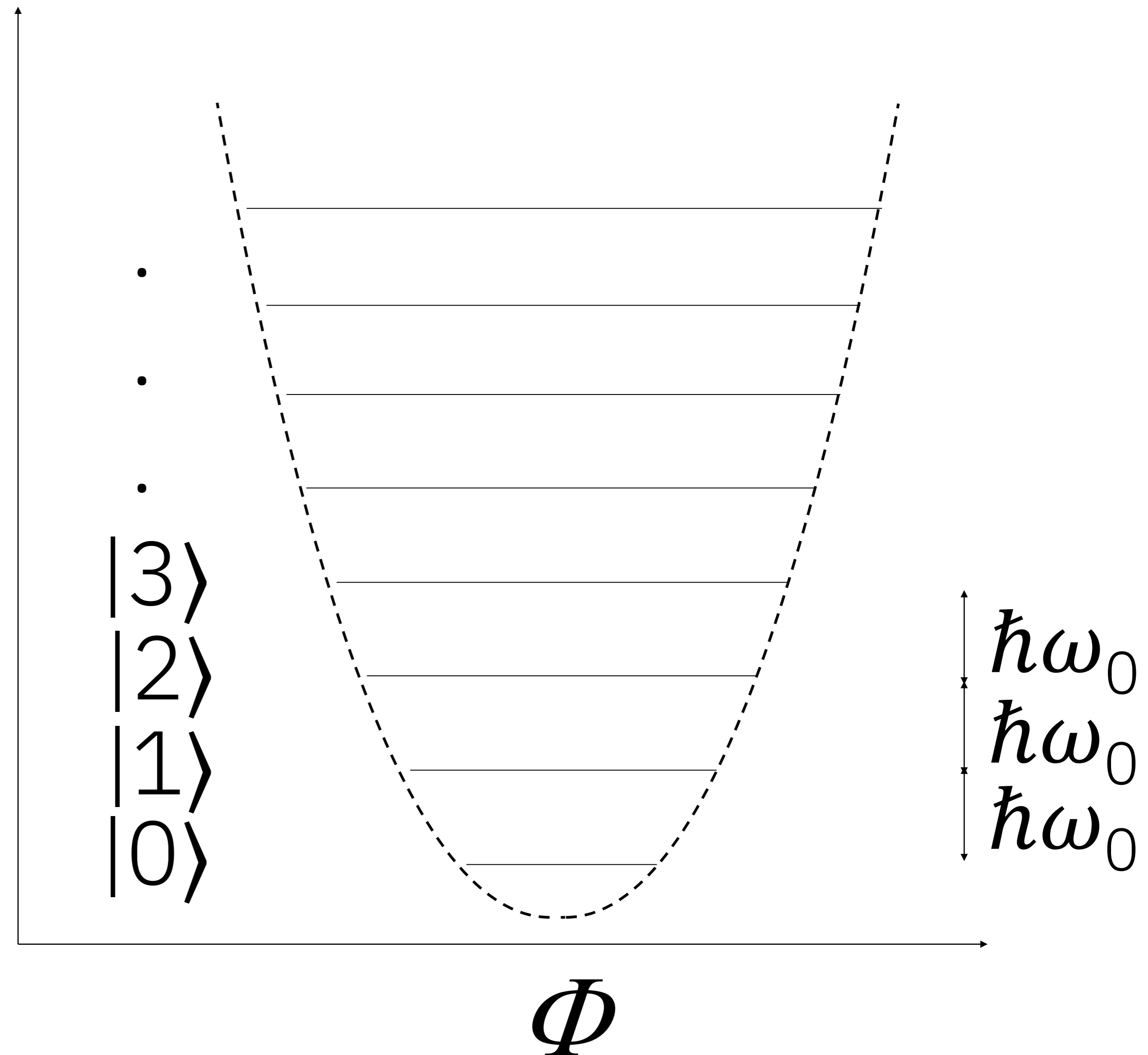
Quantum linear circuits

Quantum Hamiltonian

$$\hat{H} = \frac{1}{2C} \hat{Q}^2 + \frac{1}{2L} \hat{\Phi}^2$$

$$\hat{H} = \hbar\omega_0 \left(\hat{n} + \frac{1}{2} \right) \quad E$$

Need unique addressability for use as a qubit

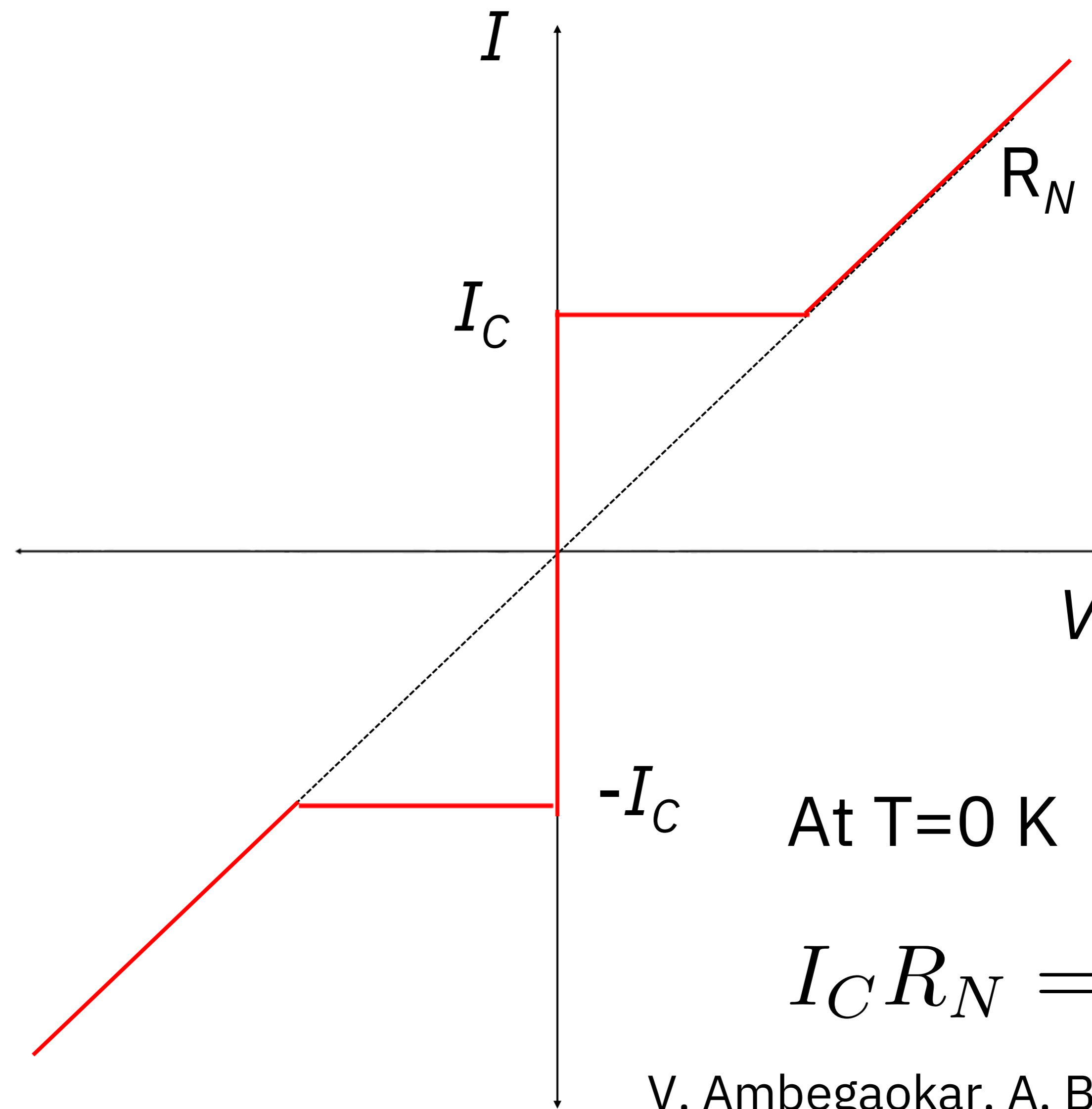


Quantum non-linear circuits: Josephson junction

SC $\Psi_1 = \sqrt{\rho_1} e^{i\phi_1}$

Insulator

SC $\Psi_2 = \sqrt{\rho_2} e^{i\phi_2}$



$$I_C R_N = \frac{\pi}{2e} \Delta$$

V. Ambegaokar, A. Baratoff, PRL 10, 486-489 (1963)

Al

Al₂O₃

Al

JAP, 125(16), 165301, 2019

Quantum non-linear circuits: Josephson junction

$$\text{SC} \quad \Psi_1 = \sqrt{\rho_1} e^{i\phi_1}$$

Insulator

$$\text{SC} \quad \Psi_2 = \sqrt{\rho_2} e^{i\phi_2}$$

Josephson phase

$$\delta = \phi_1 - \phi_2 = 2\pi\Phi/\Phi_0$$

$$I = I_c \sin(2\pi\Phi/\Phi_0)$$

$$V = \dot{\Phi}$$

$$\text{Josephson Energy} \quad U = \int V I dt$$

$$U = \frac{I_c \Phi_0}{2\pi} (1 - \cos(2\pi\Phi/\Phi_0))$$

$$U = E_J (1 - \cos(2\pi\Phi/\Phi_0))$$

Quantum non-linear circuits: Josephson junction

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Insulator

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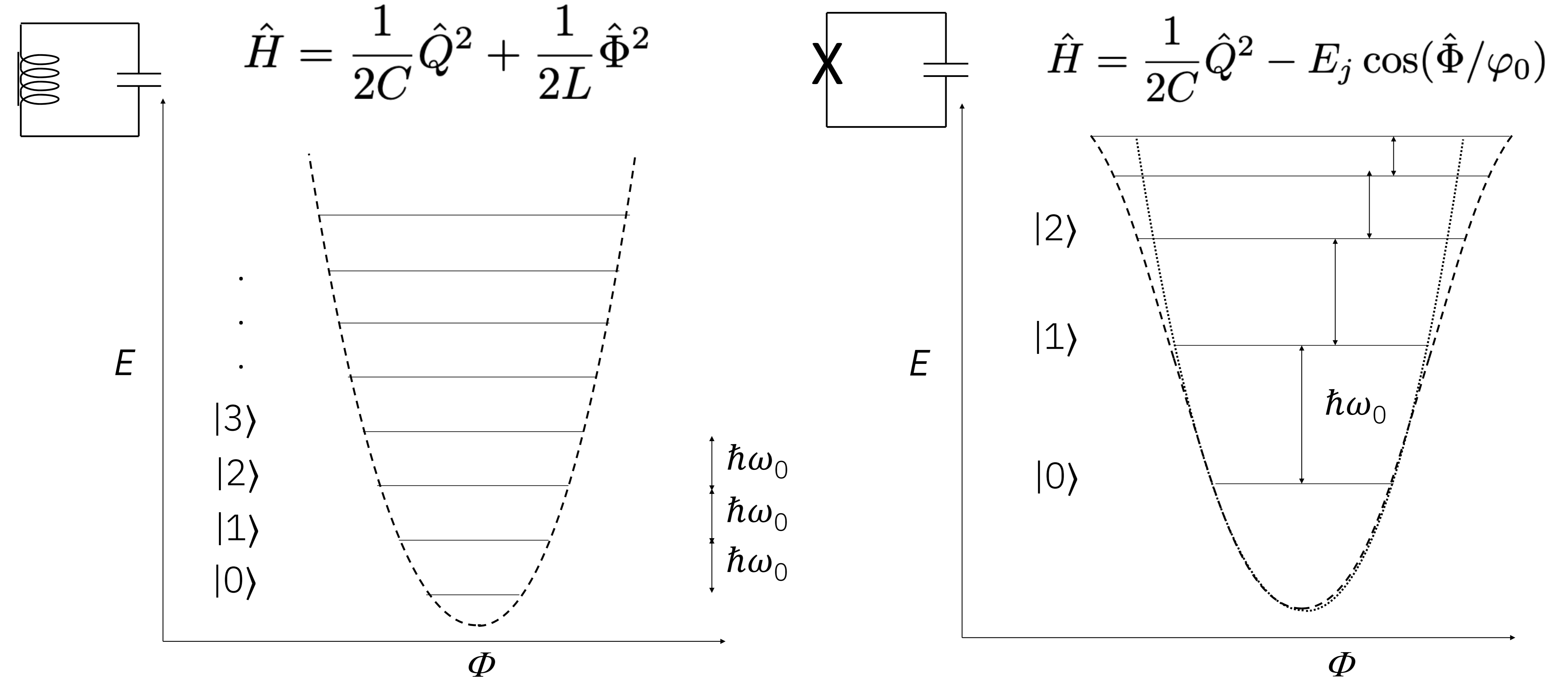
$$U = \frac{I_c \Phi_0}{2\pi} (1 - \cos(2\pi\Phi/\Phi_0))$$

$$U = E_J (1 - \cos(2\pi\Phi/\Phi_0))$$

$$\text{Inductance} \quad \frac{dI}{dt} = \frac{1}{L} V(t)$$

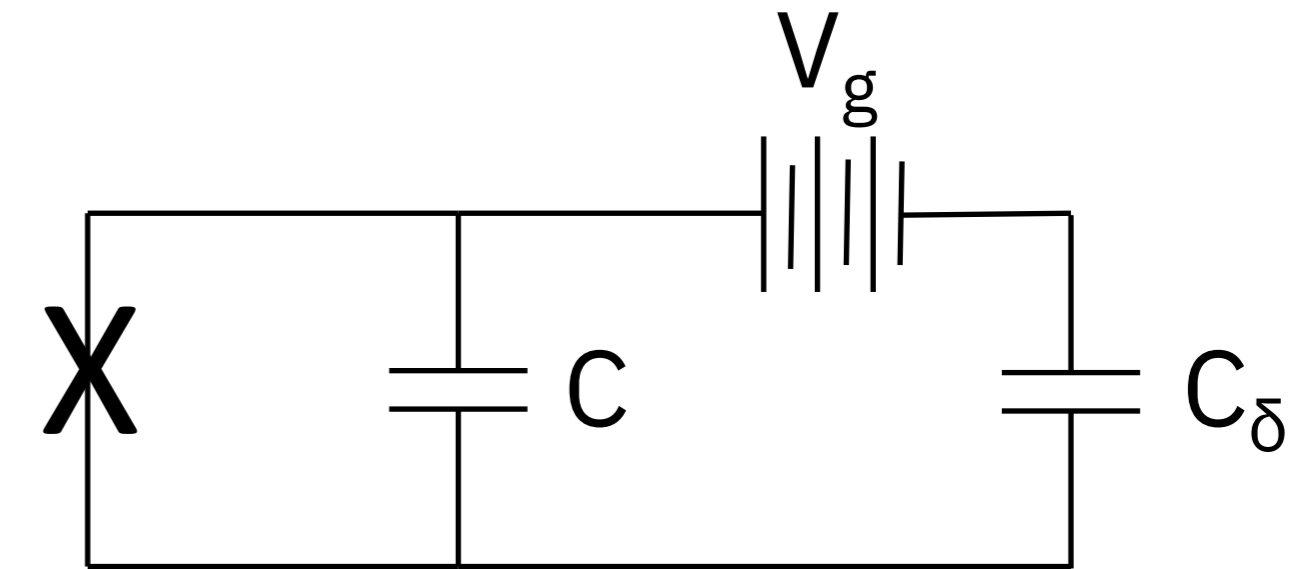
$$L = \frac{\Phi_0}{2\pi I_c \cos(2\pi\Phi/\Phi_0)}$$

Quantum non-linear circuits: Josephson junction



Quantum non-linear circuits: Josephson junction

$$\hat{H} = \frac{1}{2C} \left(\hat{Q} - V_g C_\delta \right)^2 - E_j \cos(\hat{\Phi} / \varphi_0)$$



$$E_C = \frac{e^2}{2C} \quad n_g = \frac{V_g C_\delta}{4e^2} \quad n = \text{number of Cooper pairs}$$

$$\hat{H} = 4E_C (\hat{n} - n_g)^2 - E_j \cos(\hat{\Phi} / \varphi_0)$$

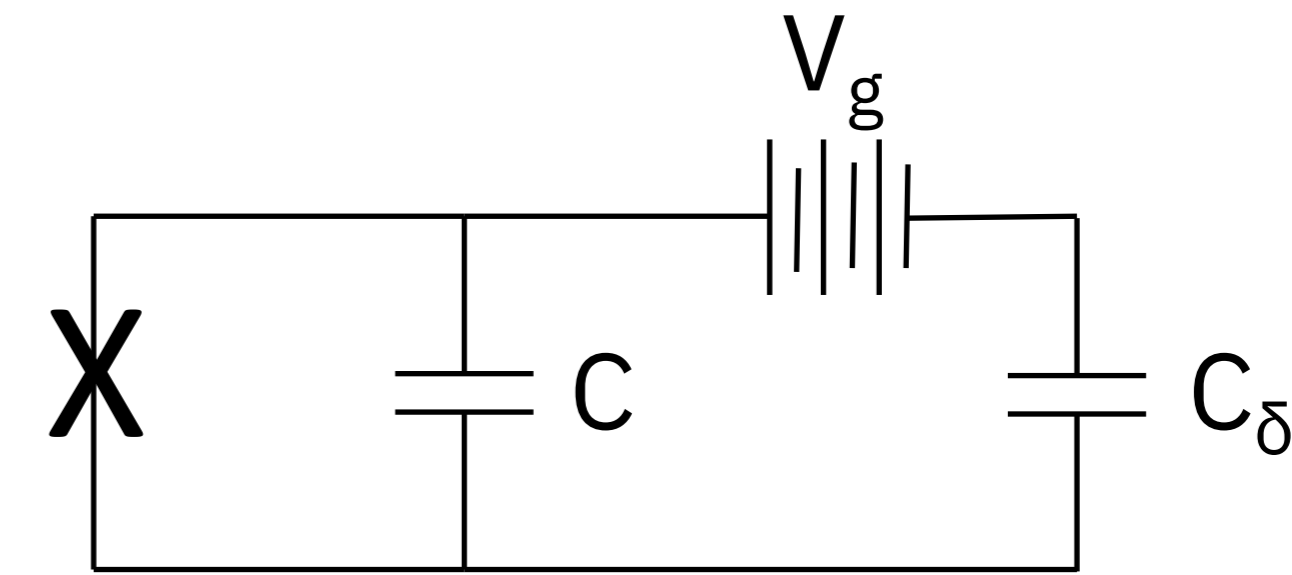
$$e^{-ip\hat{\Phi}} |n\rangle = |n + p\rangle \quad (n \text{ and } \phi \text{ are conjugate variables})$$

Quantum non-linear circuits: Josephson junction

$$E_j \gg E_c$$

$$\hat{H} = 4E_c (\hat{n} - n_g)^2 - E_j \cos(\hat{\Phi}/\varphi_0)$$

$$\hat{H} = 4E_c (\hat{n} - n_g)^2 + \frac{E_j}{2} \left(\frac{\hat{\Phi}}{\varphi_0} \right)^2 - \frac{E_j}{24} \left(\frac{\hat{\Phi}}{\varphi_0} \right)^4$$



“Duffing Oscillator”

$$Z_{tr} = \sqrt{L_j/C}$$

$$\hat{x} = \sqrt{\frac{1}{\hbar Z_{tr}}} \hat{\Phi}$$

$$\hat{y} = \sqrt{\frac{Z_{tr}}{\hbar}} \hat{Q}$$

$$\hbar\omega_0 = \sqrt{8E_j E_c}$$

$$\hat{H} = \frac{\hbar\omega_0}{2} (\hat{x}^2 + \hat{y}^2) - \frac{E_c \hat{x}^4}{3}$$

$$\hat{H} = \frac{\hbar\omega_0}{2} (\hat{x}^2 + \hat{y}^2) - \frac{E_c \hat{x}^4}{3}$$

“Normal” SHO stuff

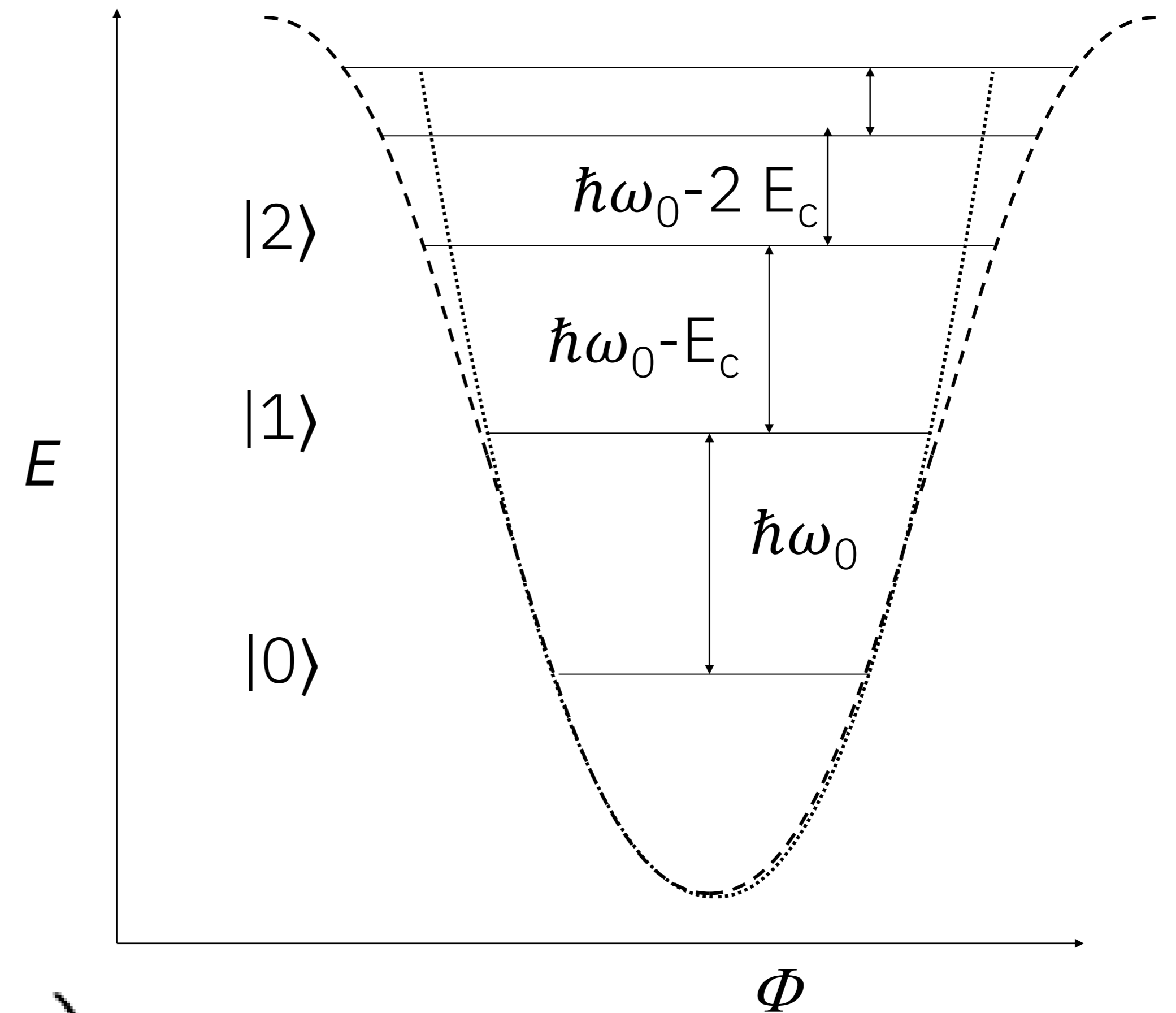
Quantum non-linear circuits: Josephson junction

$$E_j \gg E_c$$

$$\hat{H} = \frac{\hbar\omega_0}{2} (\hat{x}^2 + \hat{y}^2) - \frac{E_c \hat{x}^4}{3}$$

$$\hat{x} = \frac{1}{\sqrt{2}} (\hat{a} + \hat{a}^\dagger)$$

$$\hat{y} = \frac{1}{\sqrt{2}} (\hat{a} - \hat{a}^\dagger)$$



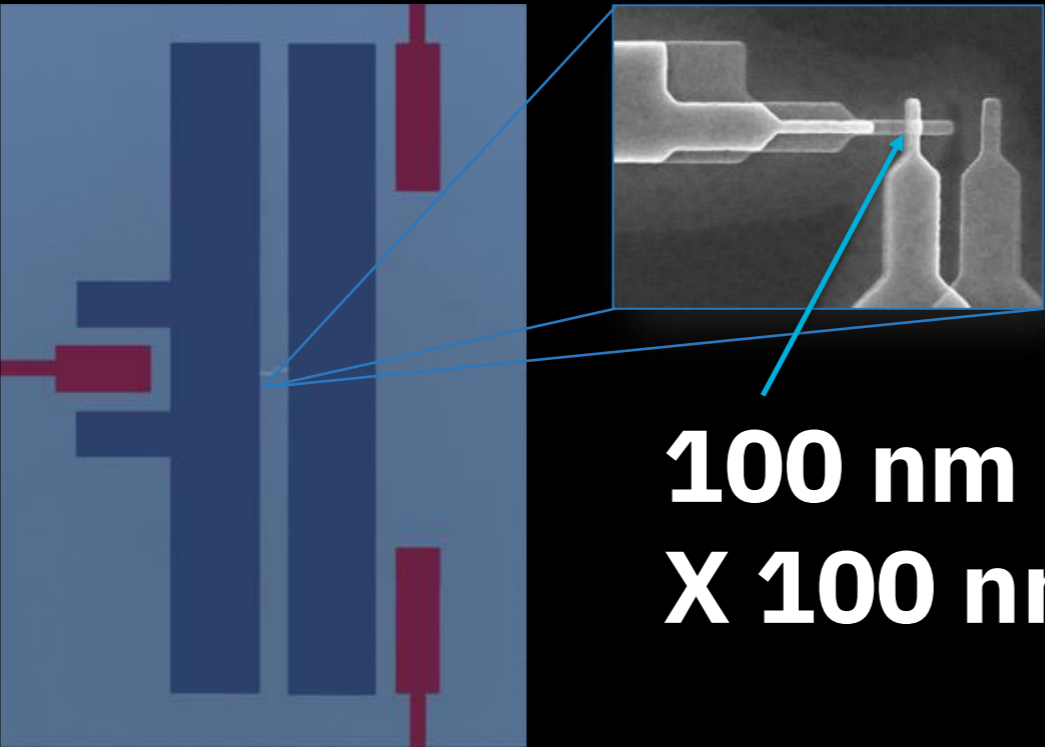
$$\hat{H} = \hbar\omega_0 \hat{a}^\dagger \hat{a} - \frac{E_c}{2} \left((\hat{a}^\dagger \hat{a})^2 - \hat{a}^\dagger \hat{a} \right) + \text{Non-RWA terms}$$

A Transmon

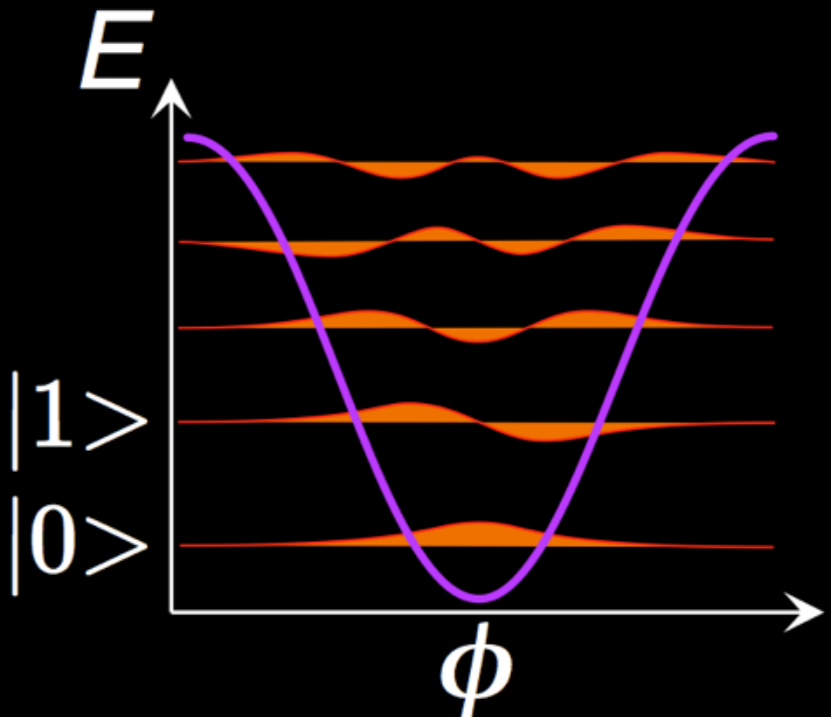
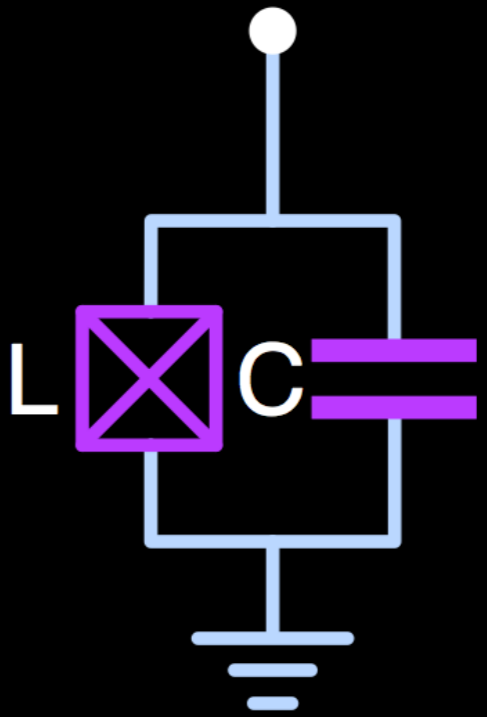


Superconducting Qubit:

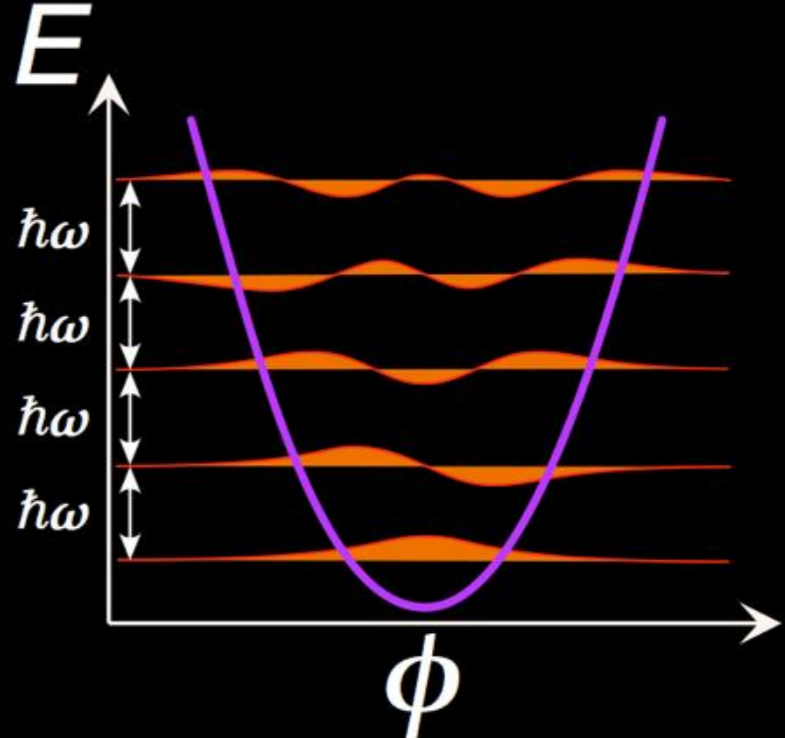
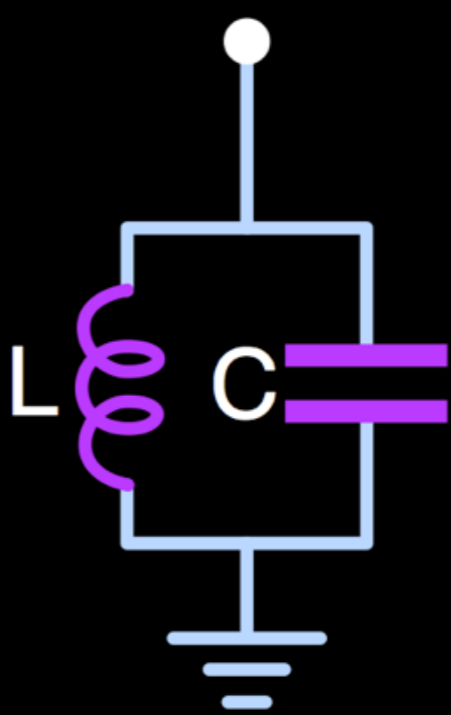
- Josephson Junction as a non-linear inductor



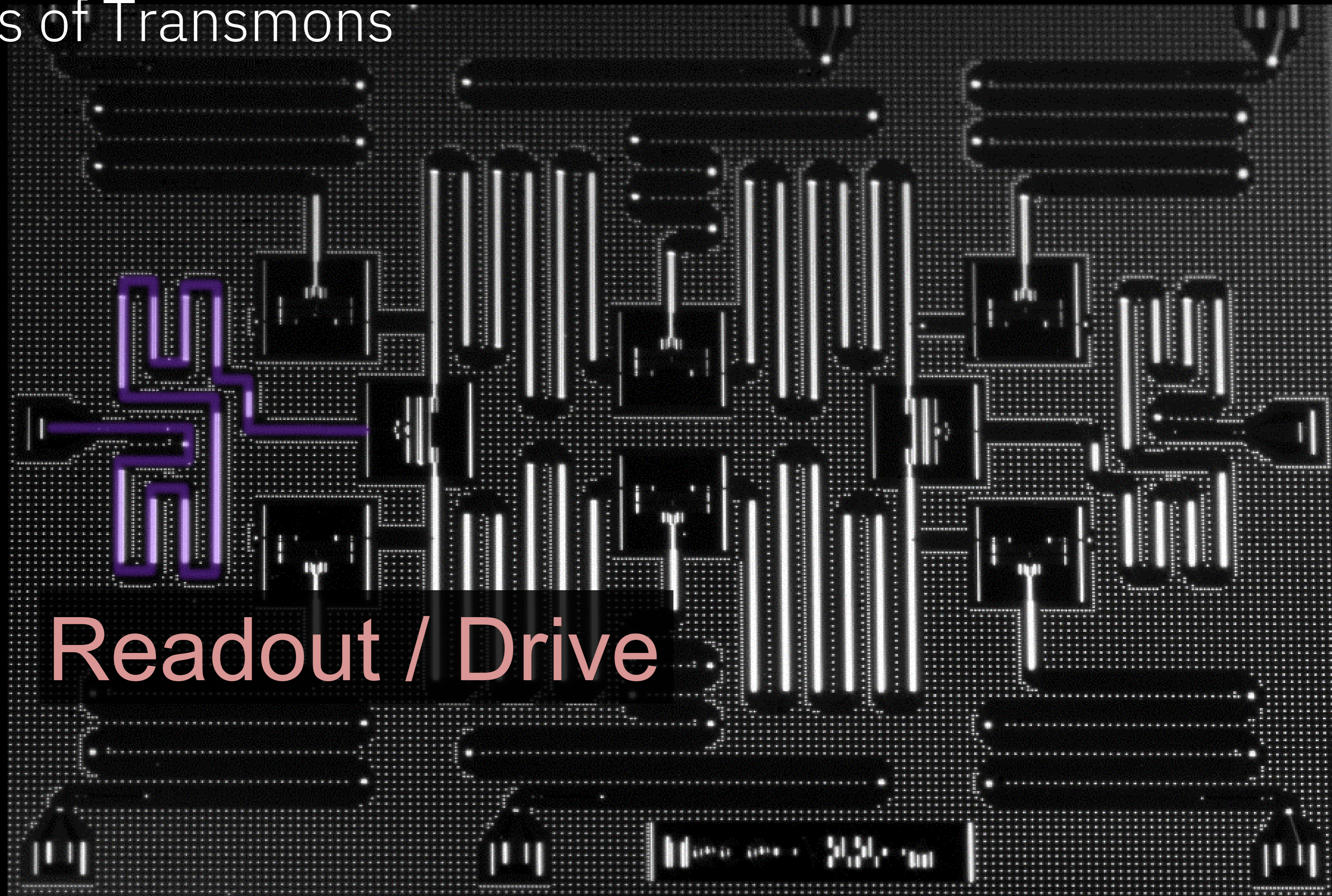
100 nm
X 100 nm



$$E_{01} \approx 5 \text{ GHz} \approx 240 \text{ mK}$$

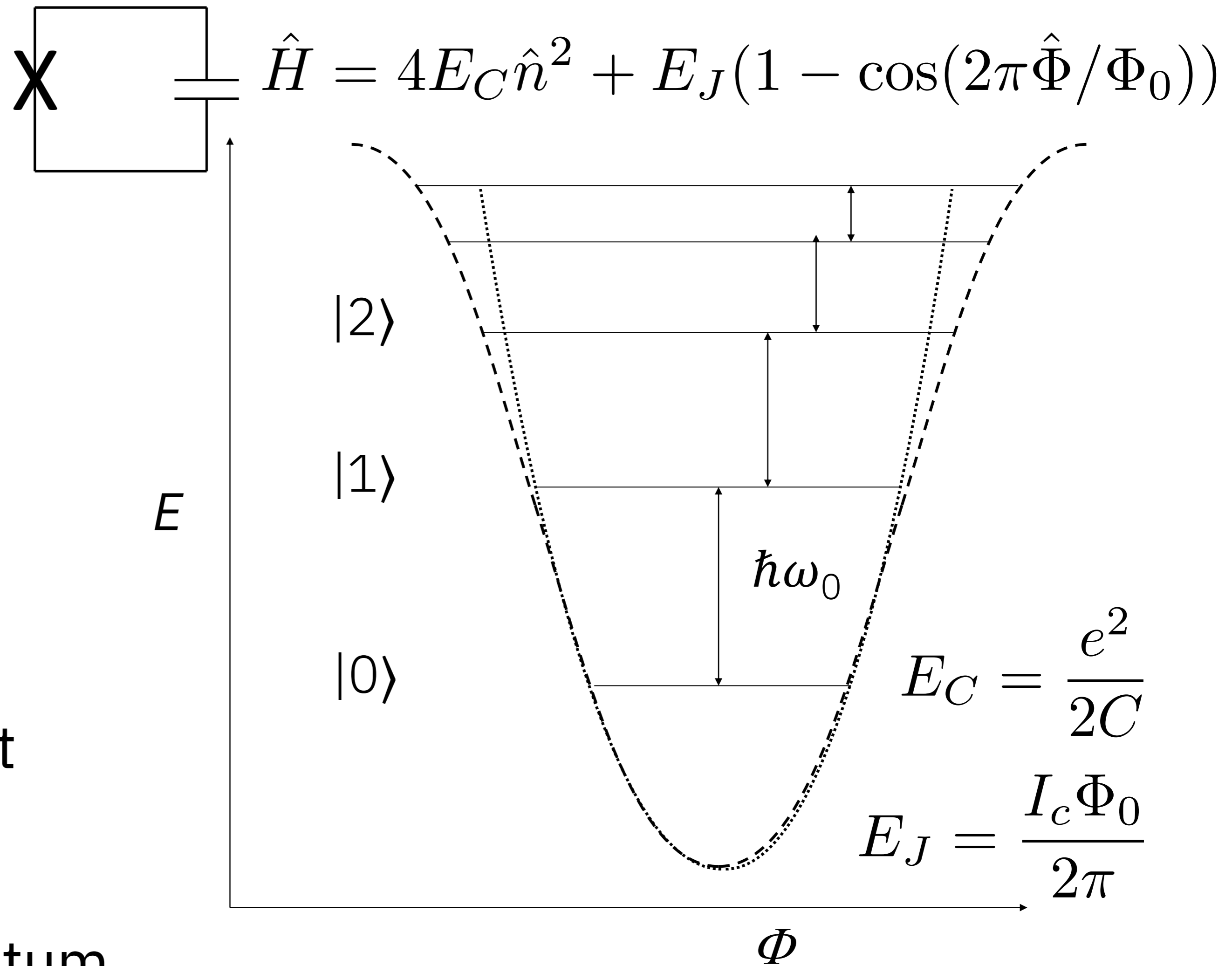
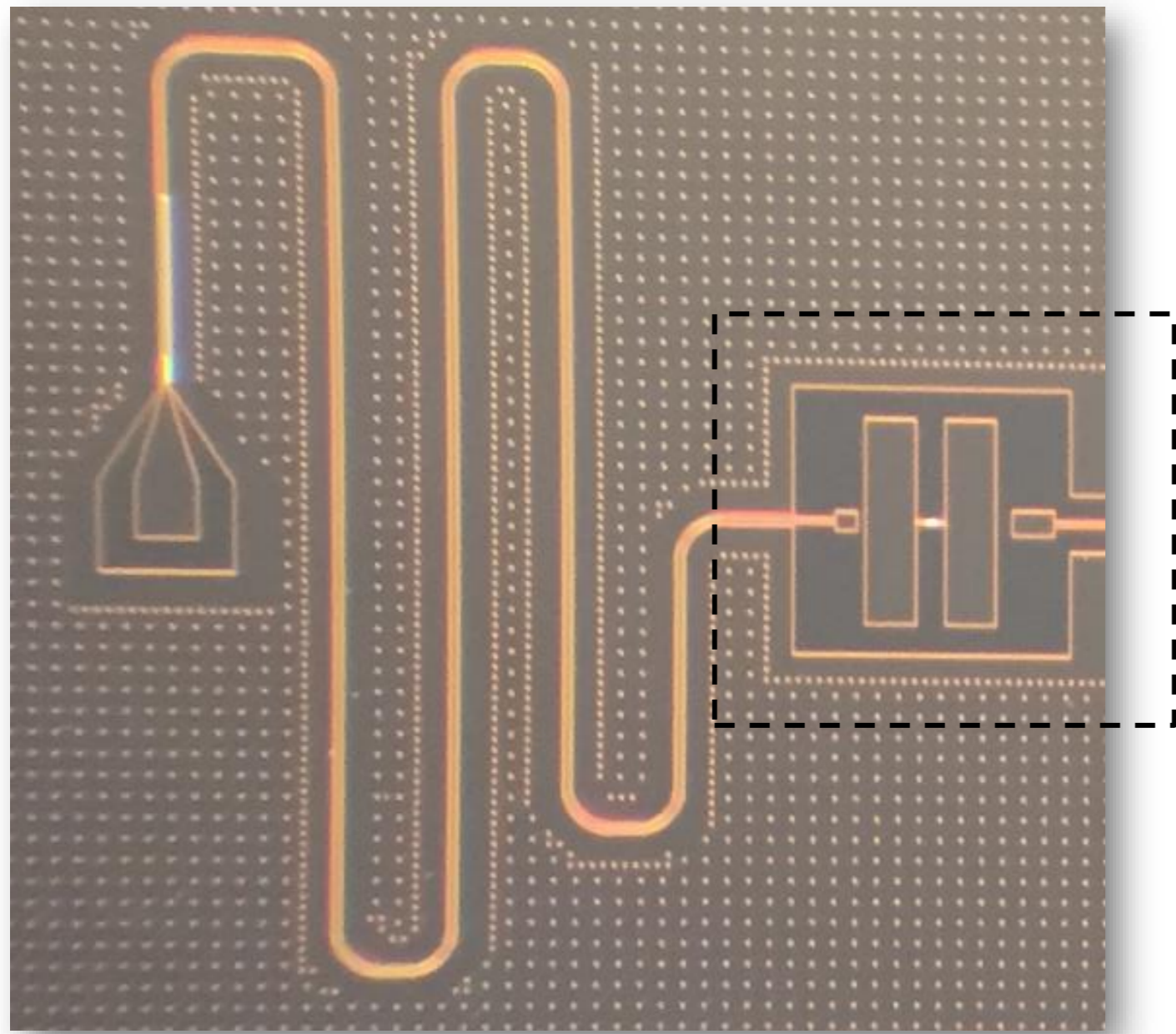


Circuits of Transmons



Readout / Drive

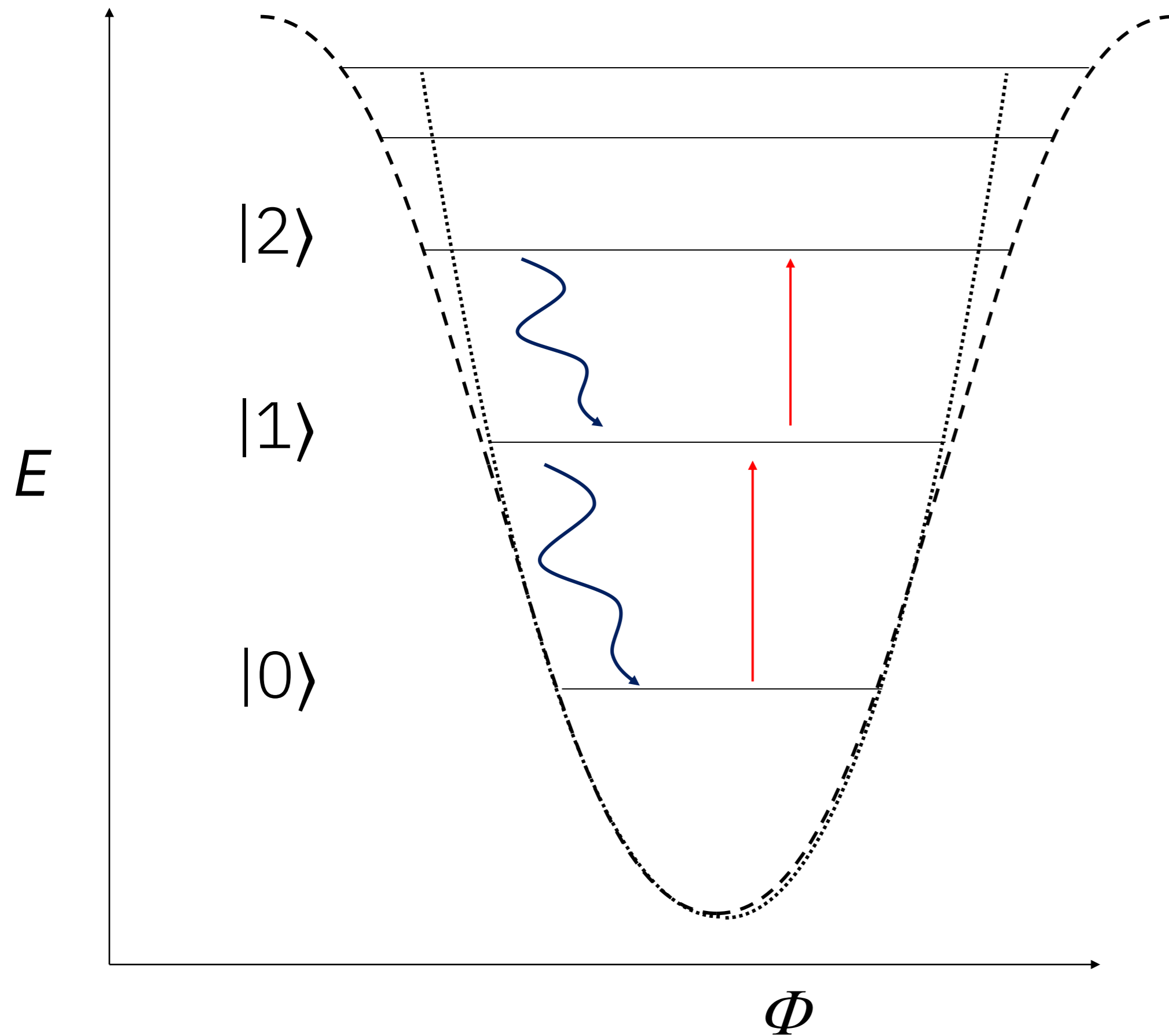
Single Qubit Control



As discussed, we have a quantum object with a ladder of energy states:

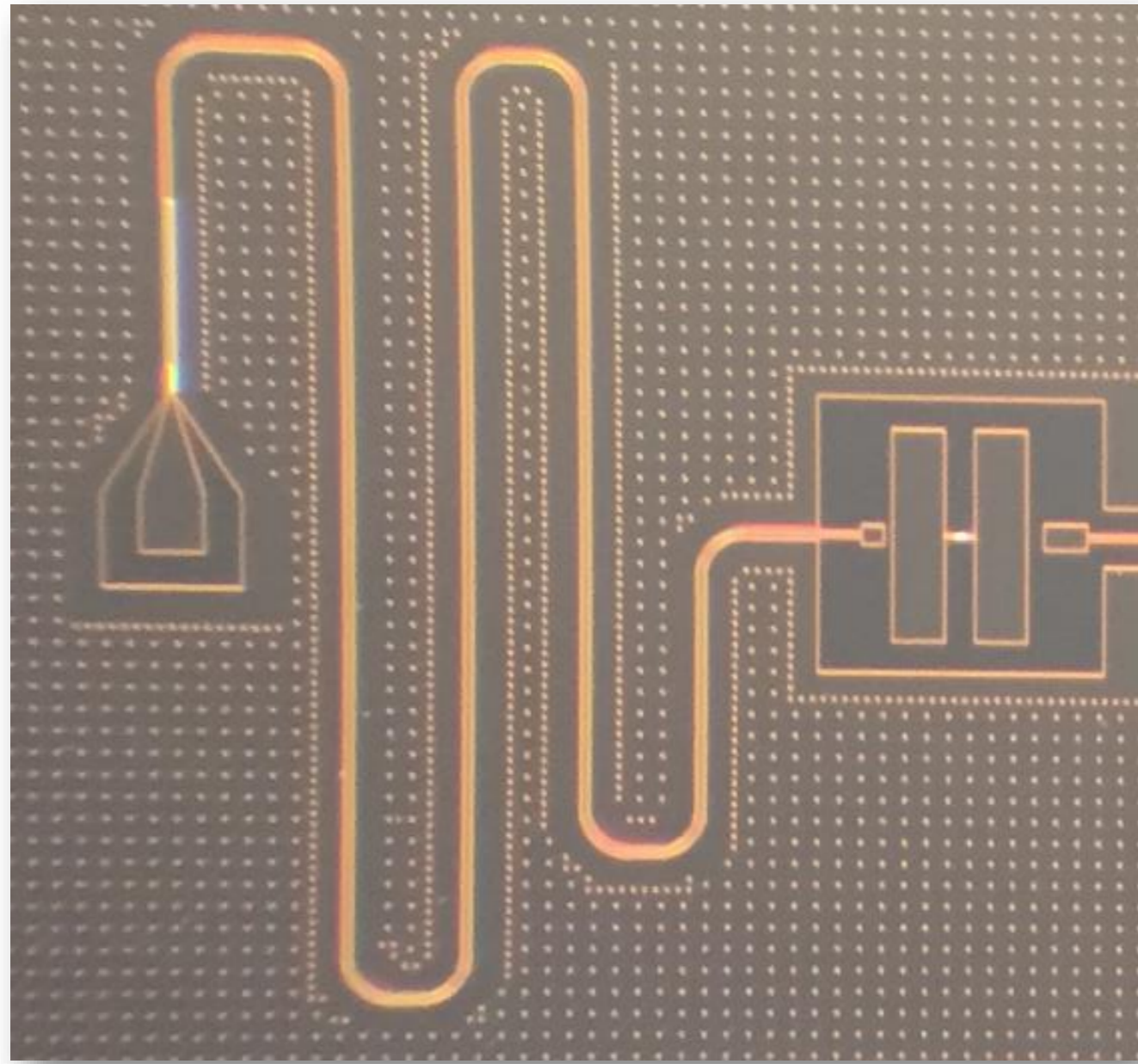
- How do we start in the ground state?
- How do we prepare an arbitrary quantum state?

Preparing the Ground State



- The system has a natural decay from higher to lower levels (the “T1” time, which we will discuss in more detail later)
- There are competing heating processes, but given the temperature of the system is cold compared to the energy levels the final state should be well into the ground state
- Typical procedure is to allow the system to relax back to the ground state (see the problem set)
- “Active Reset” (some references):
 - <https://arxiv.org/abs/1802.08980>,
 - <https://arxiv.org/abs/1801.07689>,
 - <https://arxiv.org/abs/1508.01385>

Single Qubit Control

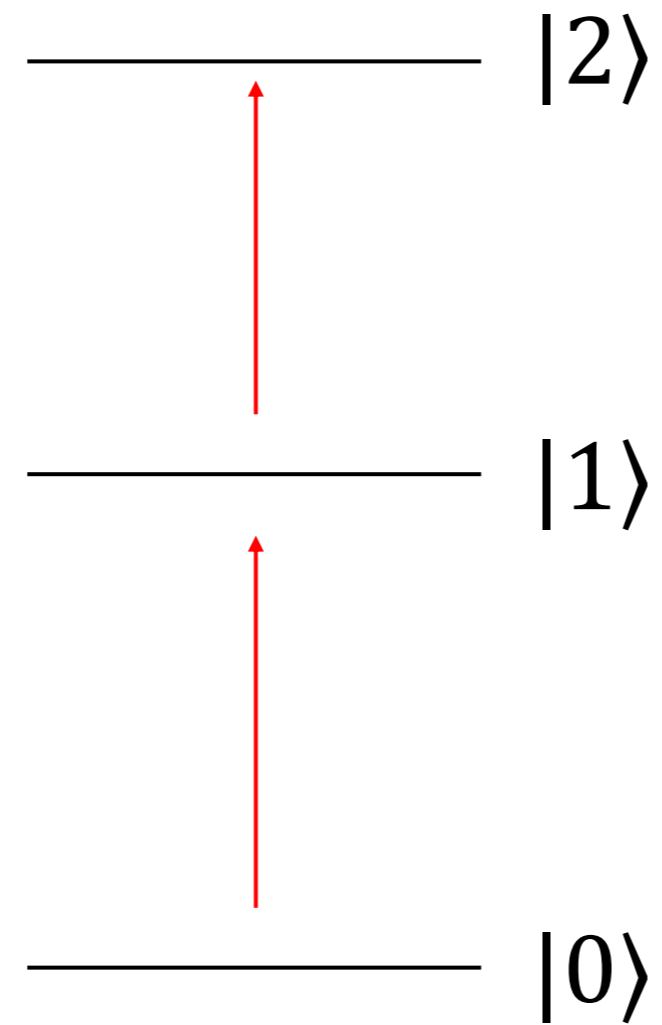


$$\langle n | \hat{a} | n + 1 \rangle = \sqrt{n}$$

Transmon (Duffing model approximation)

$$H = \omega_Q \hat{a}^\dagger \hat{a} + \frac{\alpha}{2} \hat{a}^\dagger \hat{a} (\hat{a}^\dagger \hat{a} - 1) + \Omega (\hat{a}^\dagger + \hat{a}) \cos(\omega_D t + \phi)$$

Coupling term

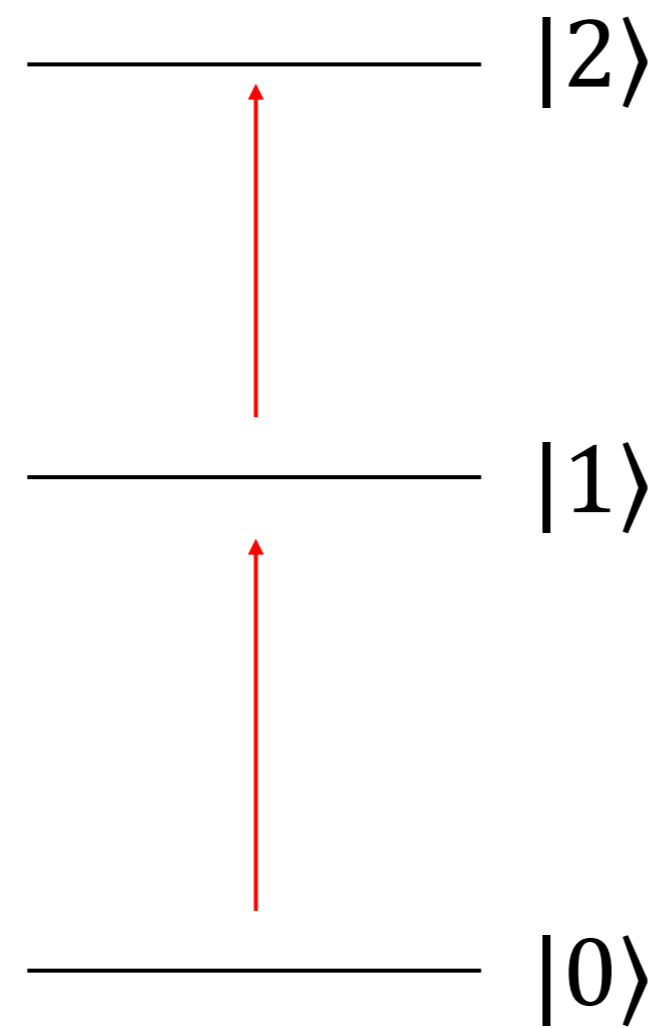
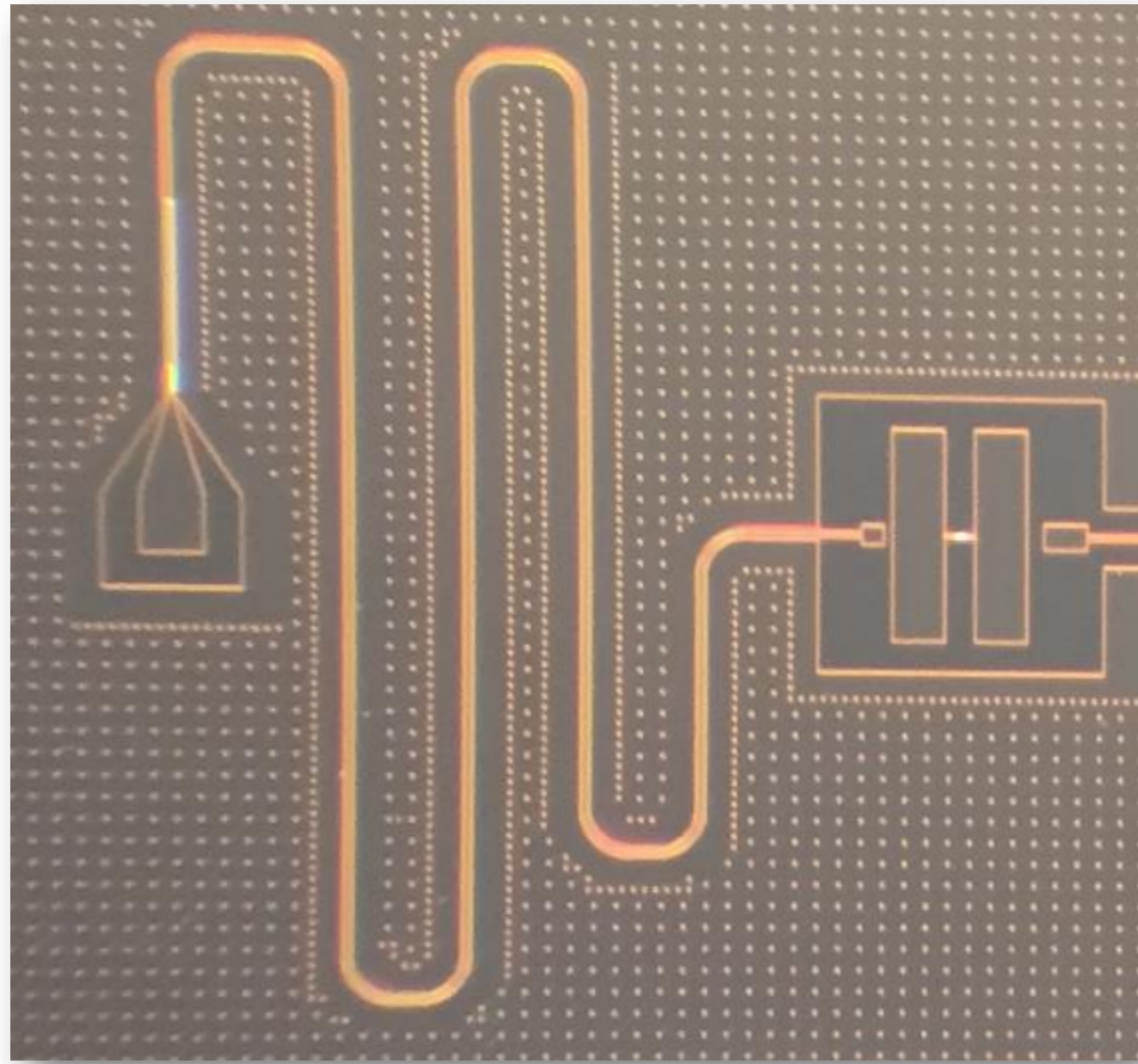


$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & \omega_Q & 0 \\ 0 & 0 & 2\omega_Q + \alpha \end{bmatrix}$$

$$\begin{bmatrix} 0 & \Omega \cos(\omega_D t + \phi) & 0 \\ \Omega \cos(\omega_D t + \phi) & \omega_Q & \sqrt{2}\Omega \cos(\omega_D t + \phi) \\ 0 & \sqrt{2}\Omega \cos(\omega_D t + \phi) & 2\omega_Q + \alpha \end{bmatrix}$$

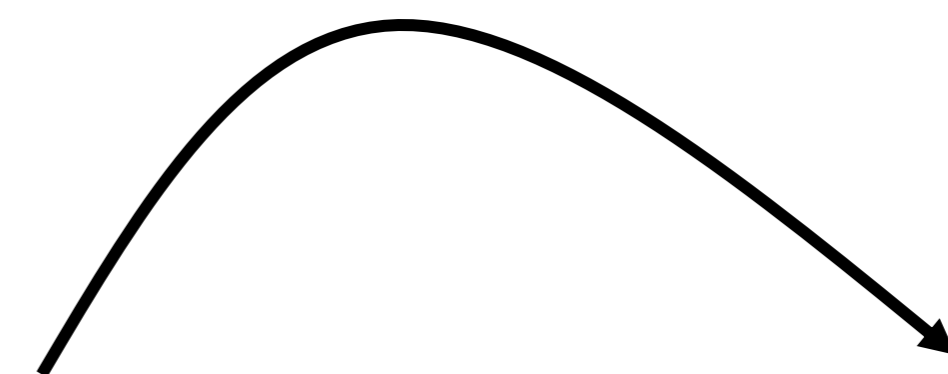
RWA

Go to a rotating frame at the drive frequency and assume the drive frequency and qubit frequency are similar



$$H = (\omega_Q - \omega_D) \hat{a}^\dagger \hat{a} + \frac{\alpha}{2} \hat{a}^\dagger \hat{a} (\hat{a}^\dagger \hat{a} - 1) + \frac{\Omega}{2} [\cos(\phi) (\hat{a}^\dagger + \hat{a}) + i \sin(\phi) (\hat{a}^\dagger - \hat{a})]$$

On resonance, $\phi = 0$

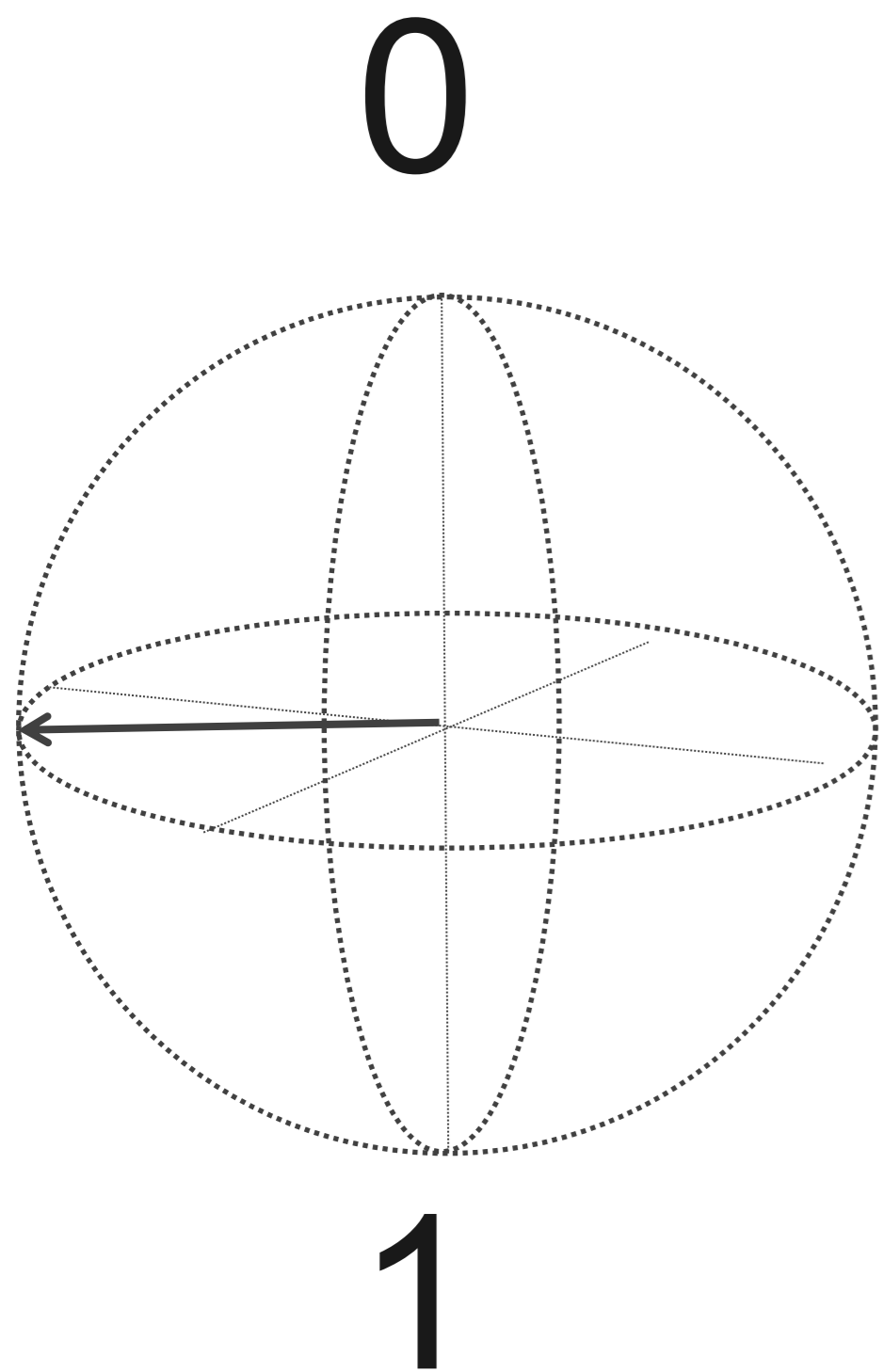


$$\begin{bmatrix} 0 & \frac{\Omega}{2} [\cos(\phi) + i \sin(\phi)] & 0 \\ \frac{\Omega}{2} [\cos(\phi) - i \sin(\phi)] & \omega_Q - \omega_D & \sqrt{2} \frac{\Omega}{2} [\cos(\phi) - i \sin(\phi)] \\ 0 & \sqrt{2} \frac{\Omega}{2} [\cos(\phi) - i \sin(\phi)] & 2\omega_Q - 2\omega_D + \alpha \end{bmatrix} \quad \begin{bmatrix} 0 & \frac{\Omega}{2} & 0 \\ \frac{\Omega}{2} & 0 & \sqrt{2} \frac{\Omega}{2} \\ 0 & \sqrt{2} \frac{\Omega}{2} & \alpha \end{bmatrix}$$

RWA

Restricted to two-levels:

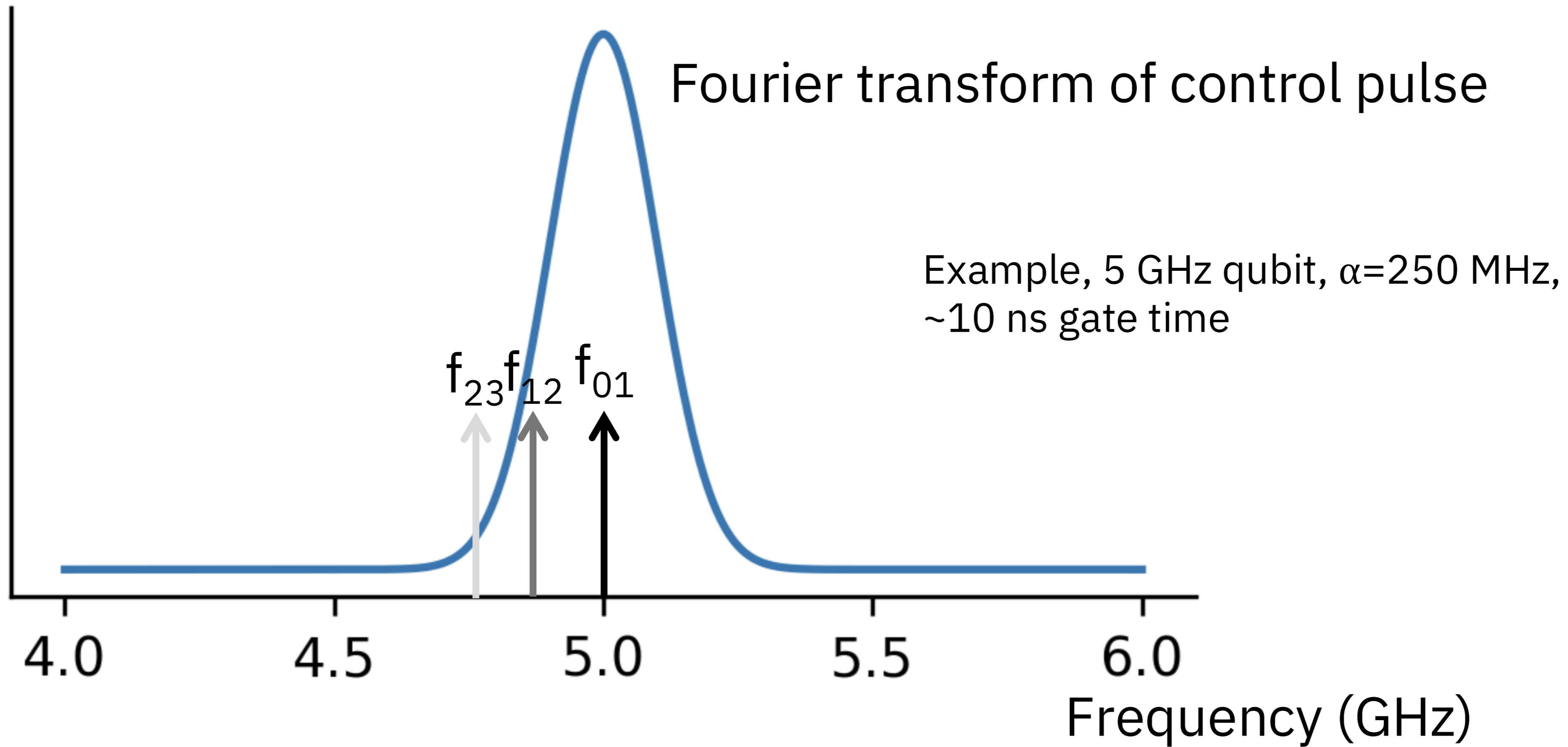
$$\begin{bmatrix} 0 & \frac{\Omega}{2} [\cos(\phi) + i \sin(\phi)] \\ \frac{\Omega}{2} [\cos(\phi) - i \sin(\phi)] & 0 \end{bmatrix} = \underbrace{\frac{\Omega}{2} \cos(\phi) \sigma_X + \frac{\Omega}{2} \sin(\phi) \sigma_Y}$$



Apply for a time $t = \frac{\theta}{2\omega}$ to get the unitary

$$R(\theta, \phi) = \begin{bmatrix} \cos\left(\frac{\theta}{2}\right) & -ie^{-i\phi} \sin\left(\frac{\theta}{2}\right) \\ -ie^{i\phi} \sin\left(\frac{\theta}{2}\right) & \cos\left(\frac{\theta}{2}\right) \end{bmatrix}$$

Limitations on gate times



Qubits and Errors

A qubit is a quantum two-level system

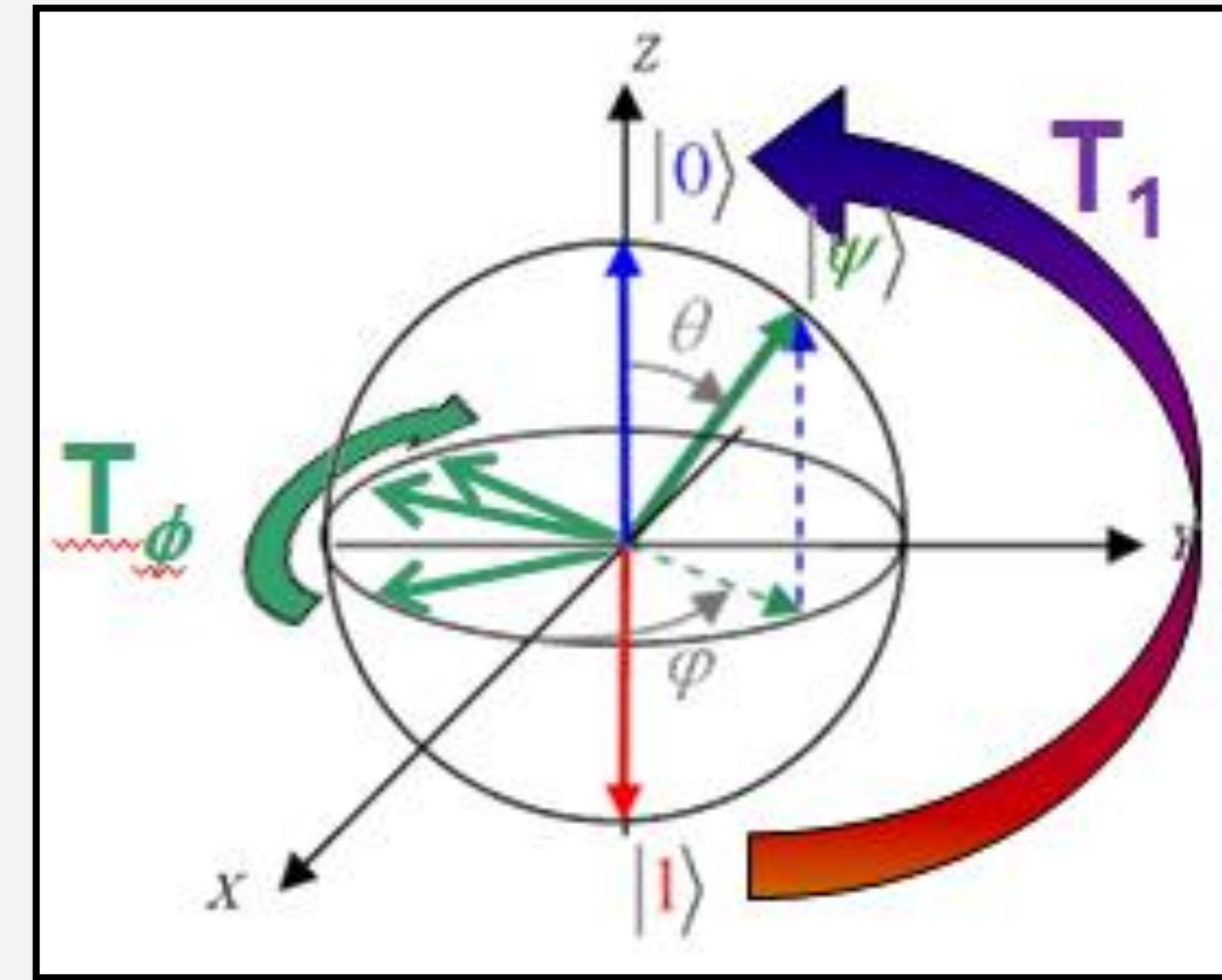
Finite qubit coherence times

- T_1 : relaxation (dissipation - think resistor)
- T_ϕ : dephasing (randomization of ϕ)
 - Results from measurement (intentional or not)
- T_2 : parallel combination of above,

Imperfect control pulses

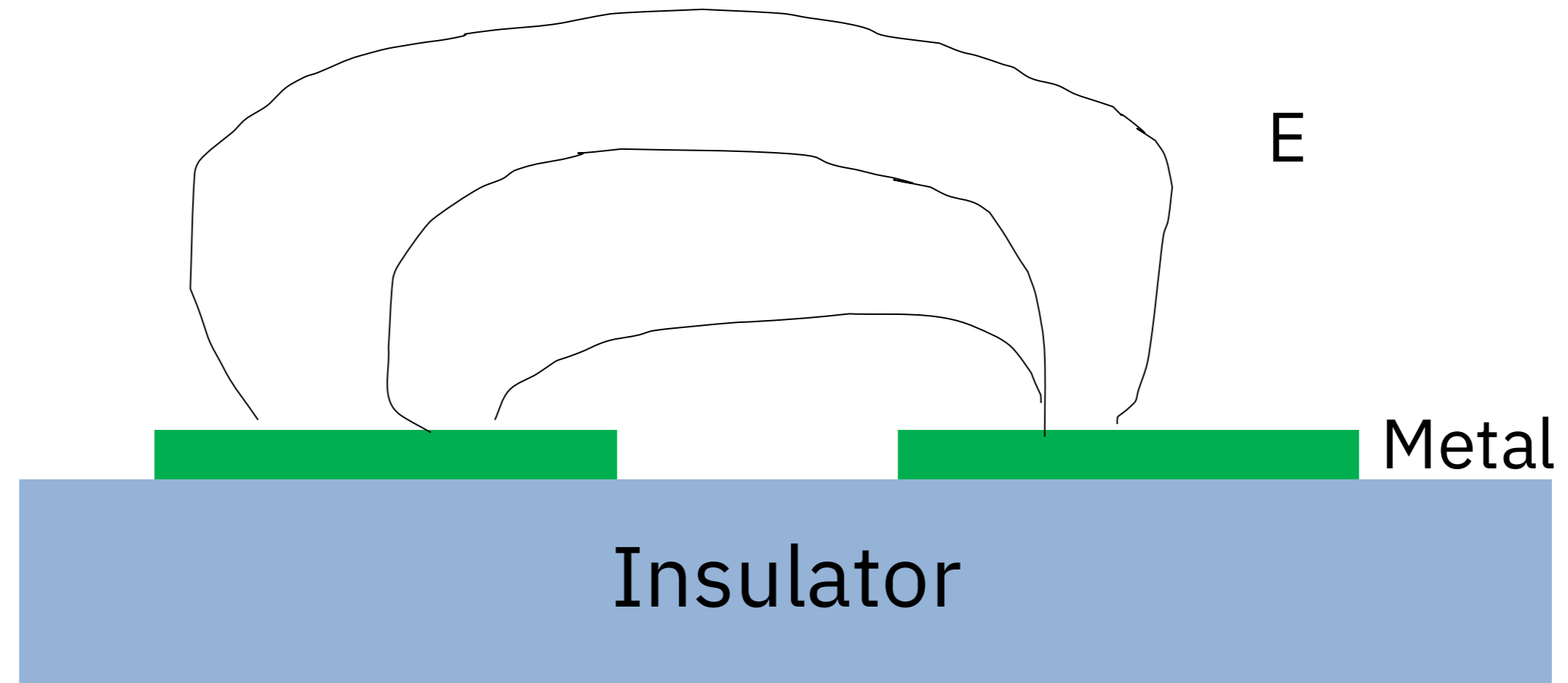
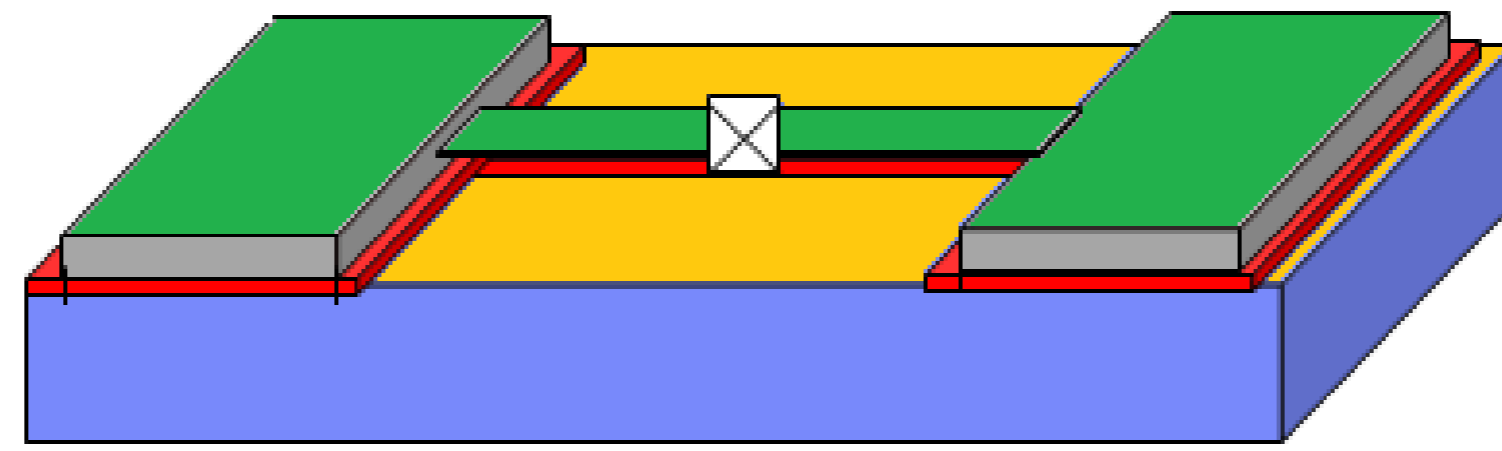
Spurious inter-qubit couplings

Imperfect qubit state measurements

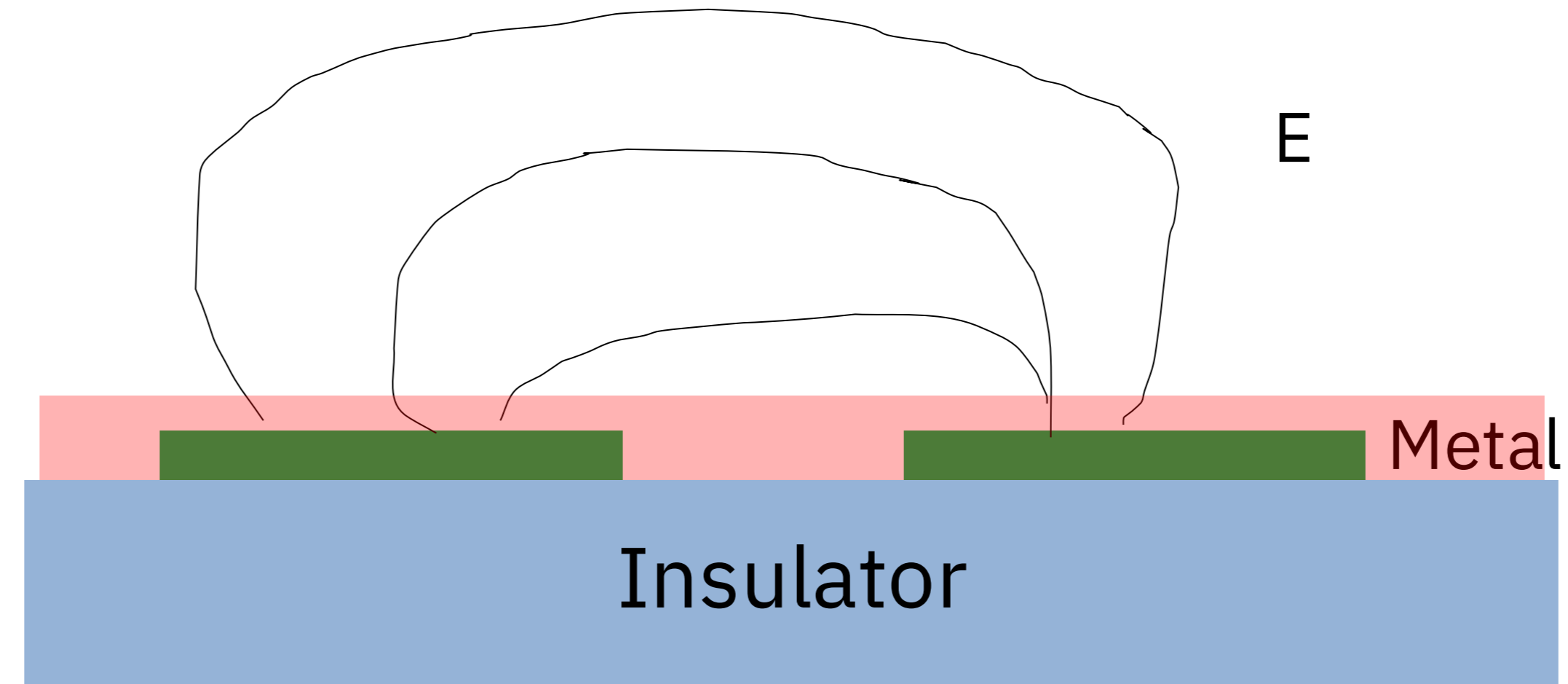
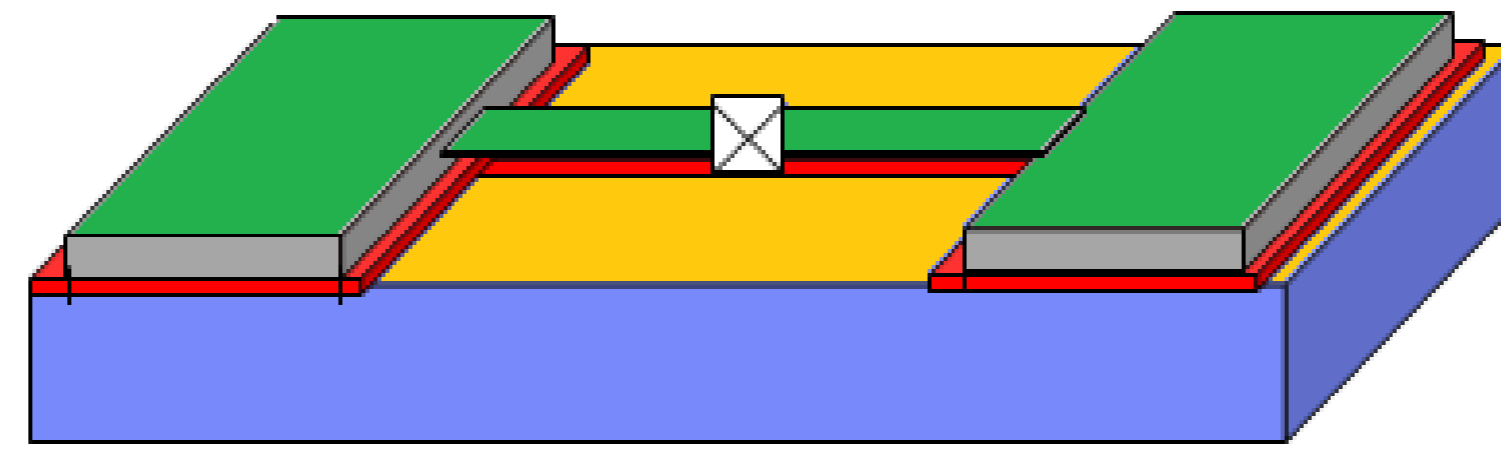


$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{1}{T_\phi}$$

T_1 and qubit size

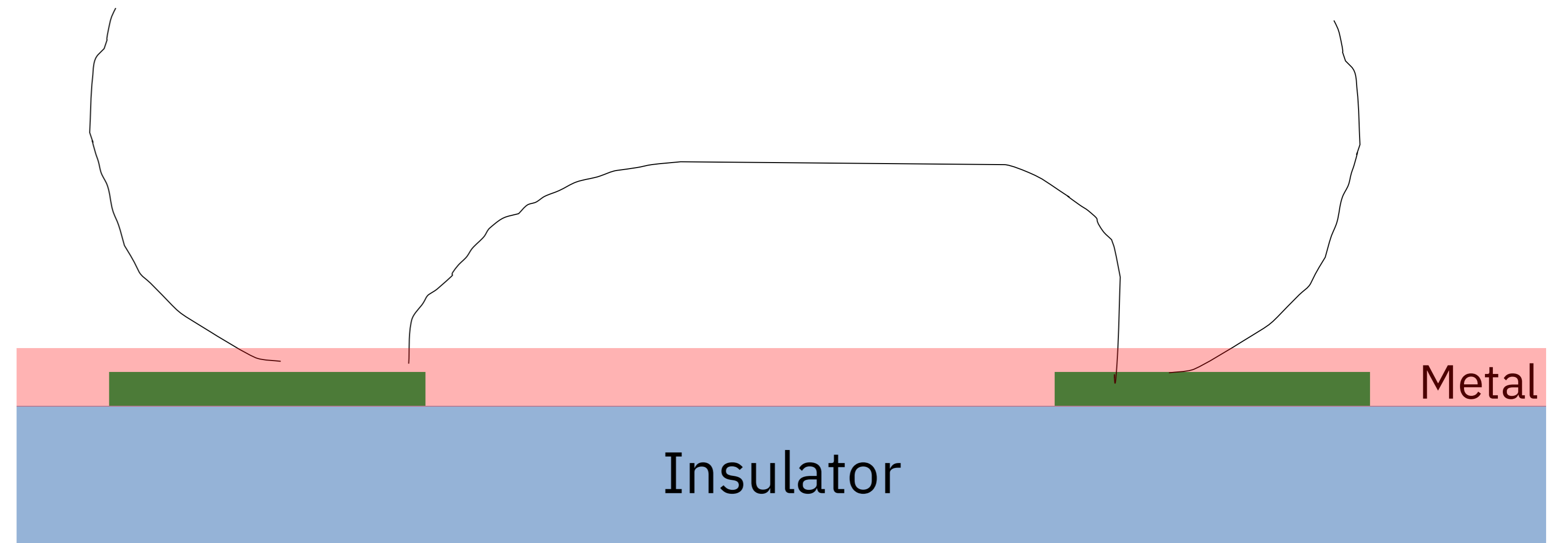
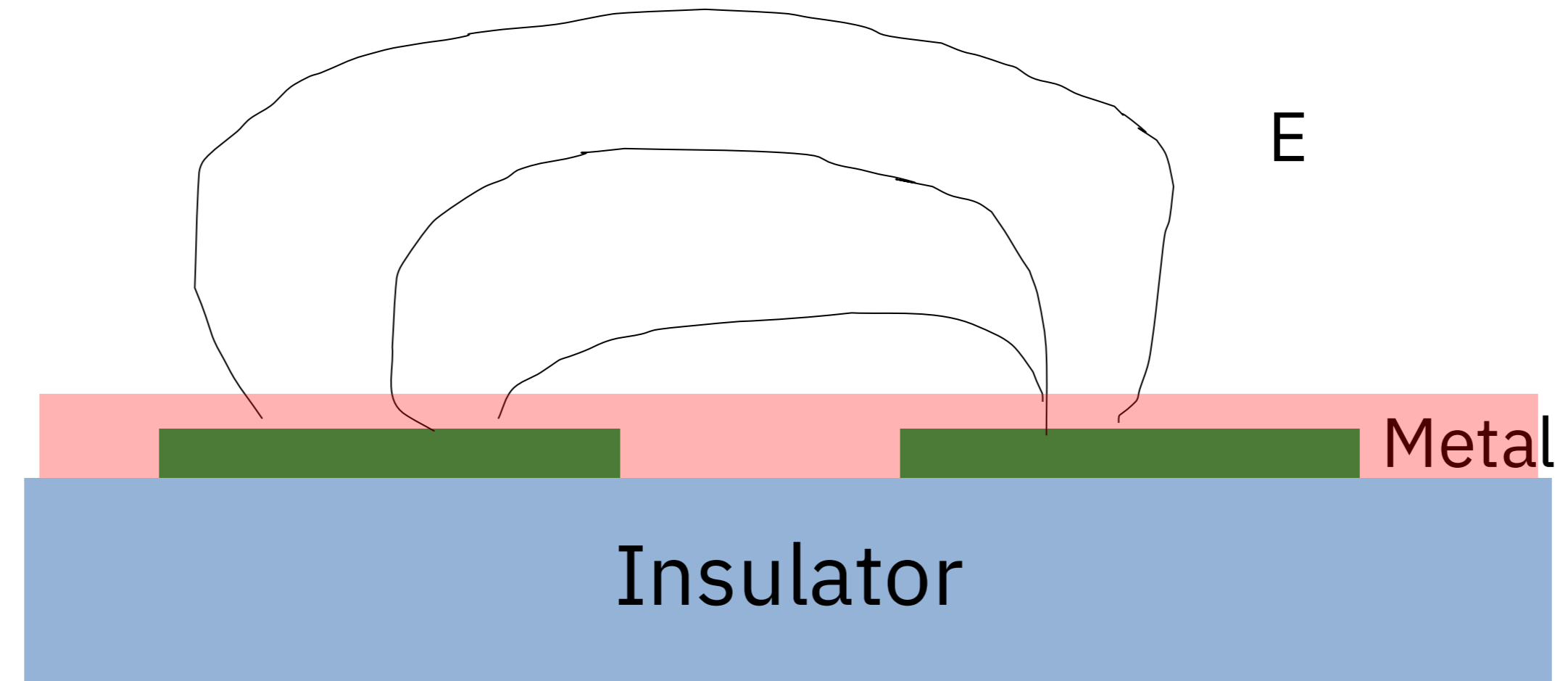
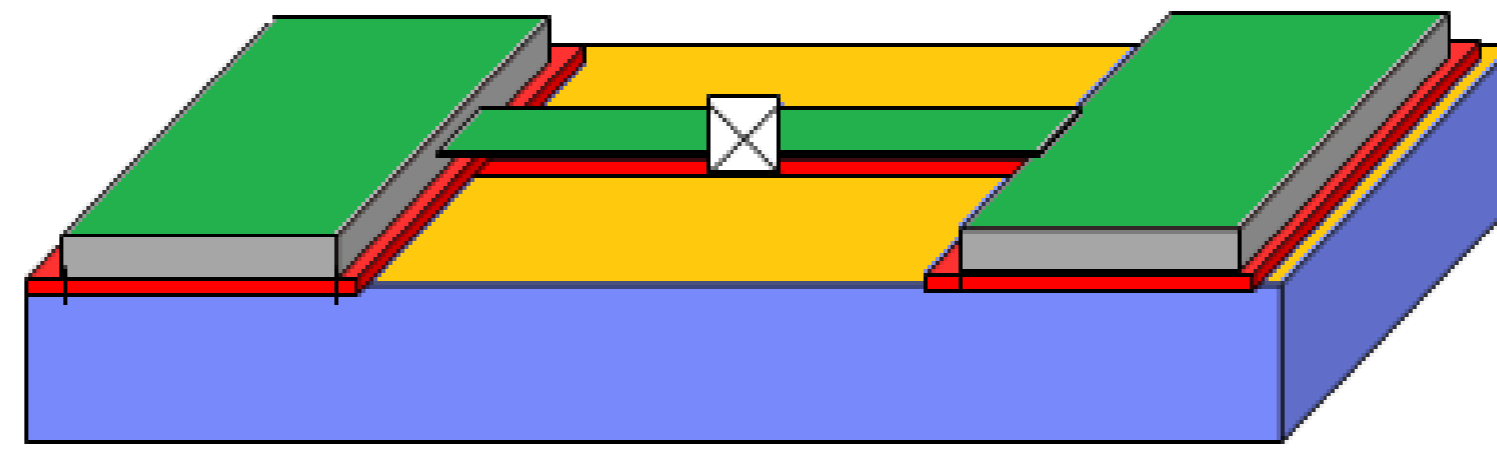


T_1 and qubit size

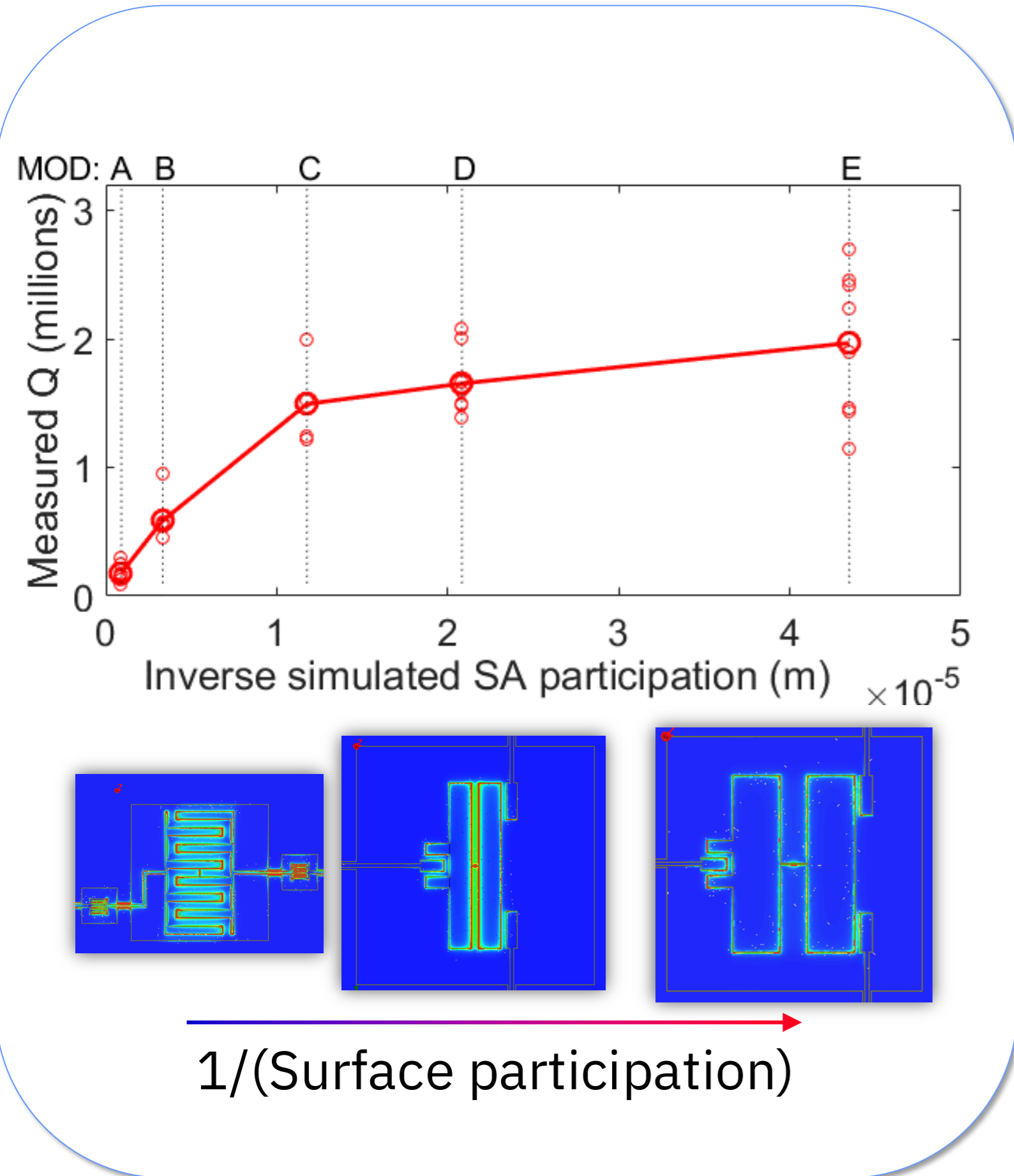


If there is a thin lossy interfacial layer, the loss from it will depend on how much electrical energy is stored in it

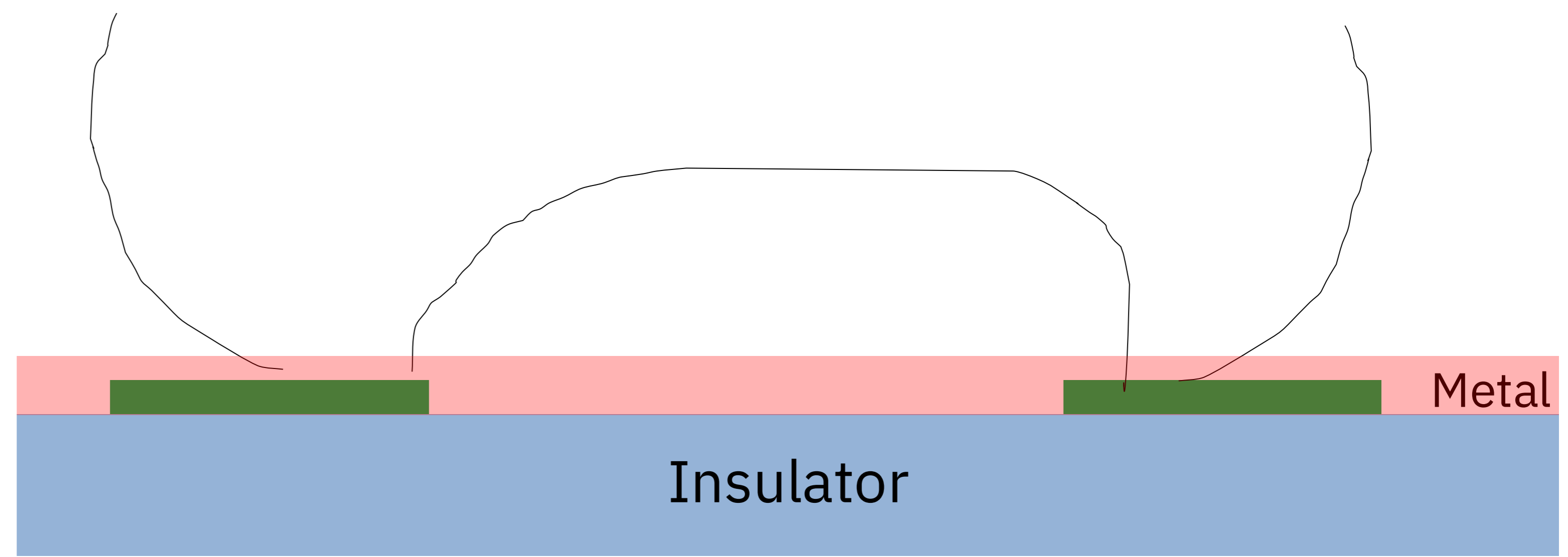
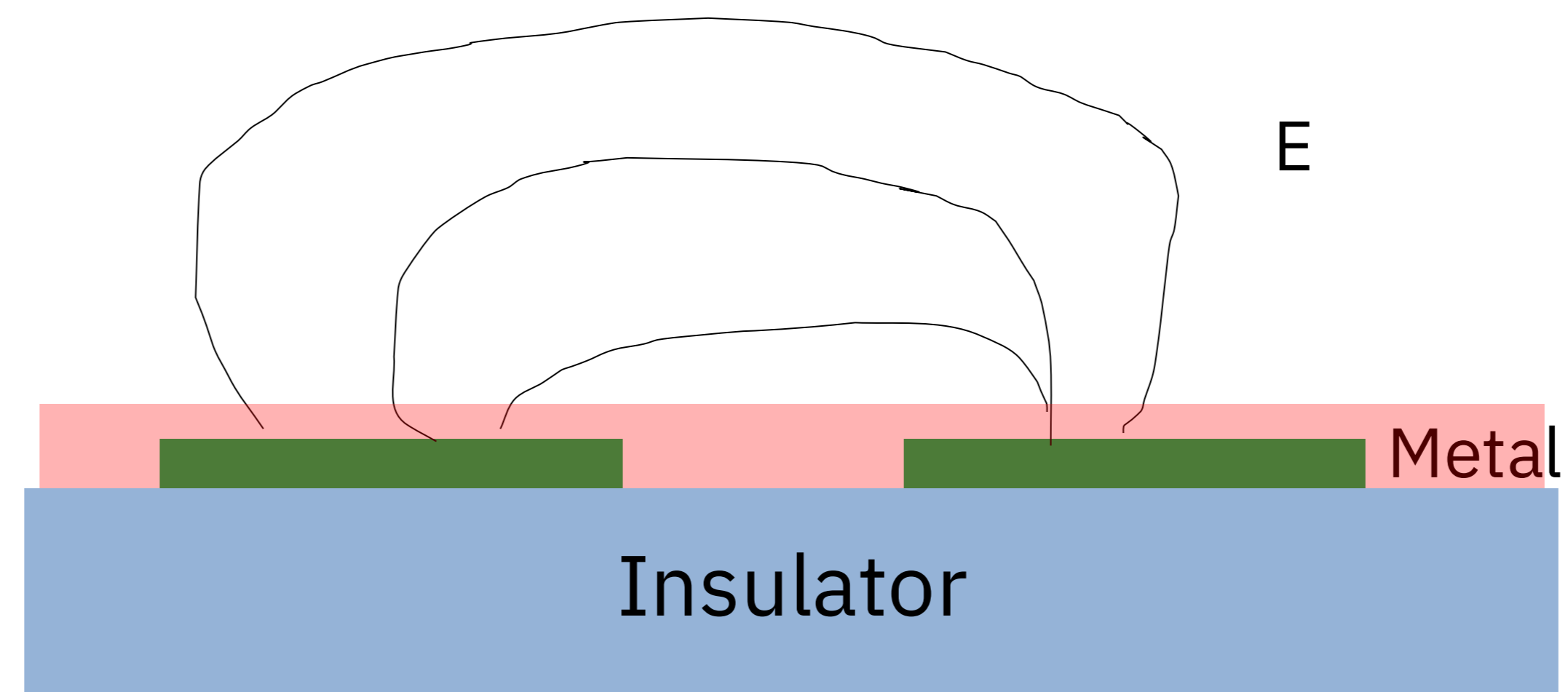
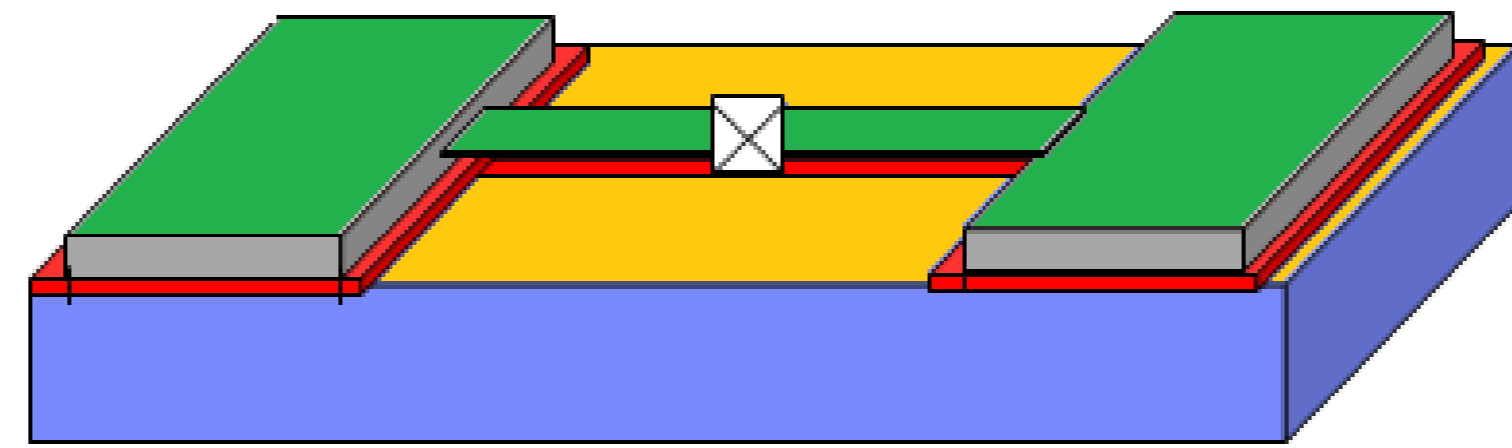
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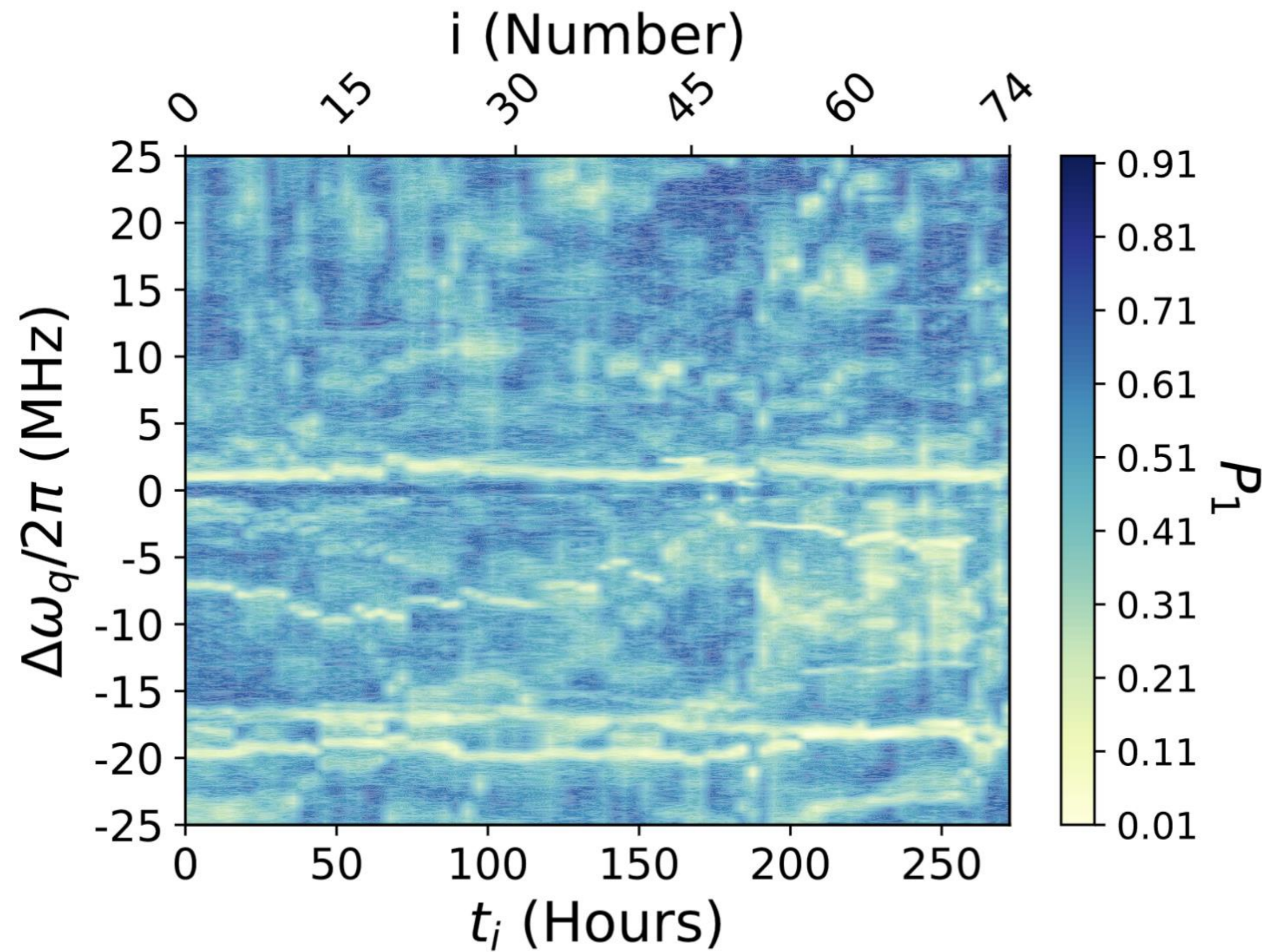


T_1 and qubit size



Gambetta et al, EEE Trans. on App. Superconductivity 27 1 (2017)



Variability of T_1 

T_1 is highly variable from qubit to qubit and over time

Two Level Systems (TLS)

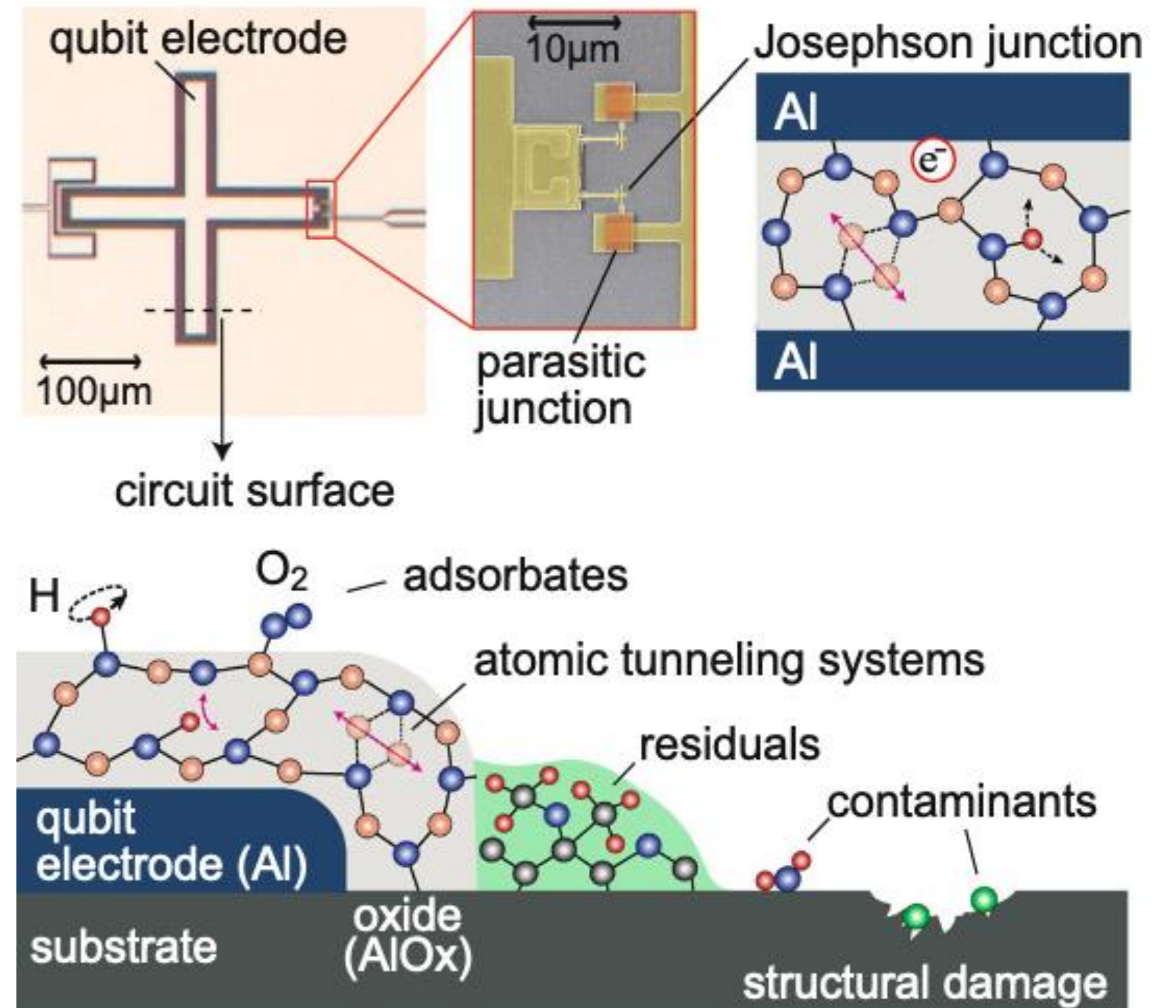
Atomic-scale defects that may reside in a number of places within the qubit environment

First detected as anomalous heat capacity in glasses at low temp (Zeller & Pohl)

Described by Standard tunneling Model (Phillips/Anderson 1972) w/ refinements (Burin+others 1990s, Ioffe+Faoro 2010s)

Shown to affect qubits (Martinis) and resonators (Gao)

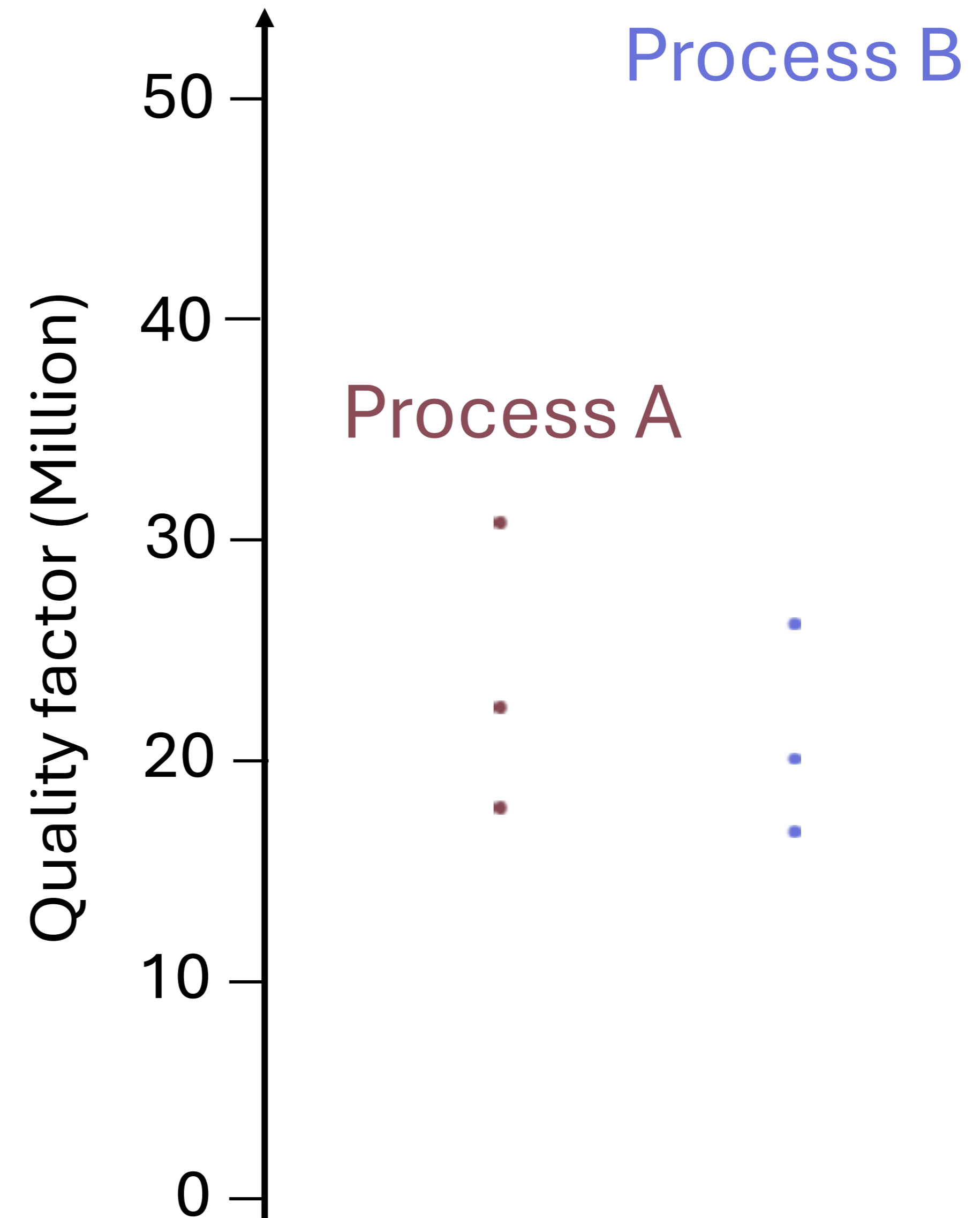
Zeller and Pohl, *PRB* 4, 2029 (1971)
Phillips, *JLTP* 7 351 (1972)
Anderson, Halperin, & Varma, *Phil. Mag.* 25, 1 (1972)
W. Phillips, *Rep. Prog. Phys.* 50, 1657 (1987)
Burin & Kagan, *ZETF* 106, 633 (1994)
Gao et al, *Appl. Phys. Lett.* 92, 152505 (2008).
Faoro & Ioffe, *PRL* 109, 157005 (2012)
Martinis et al, *PRL* 95, 210503 (2005)



Lisenfeld et al., *npj Quant. Info.*, 5 105 (2019)

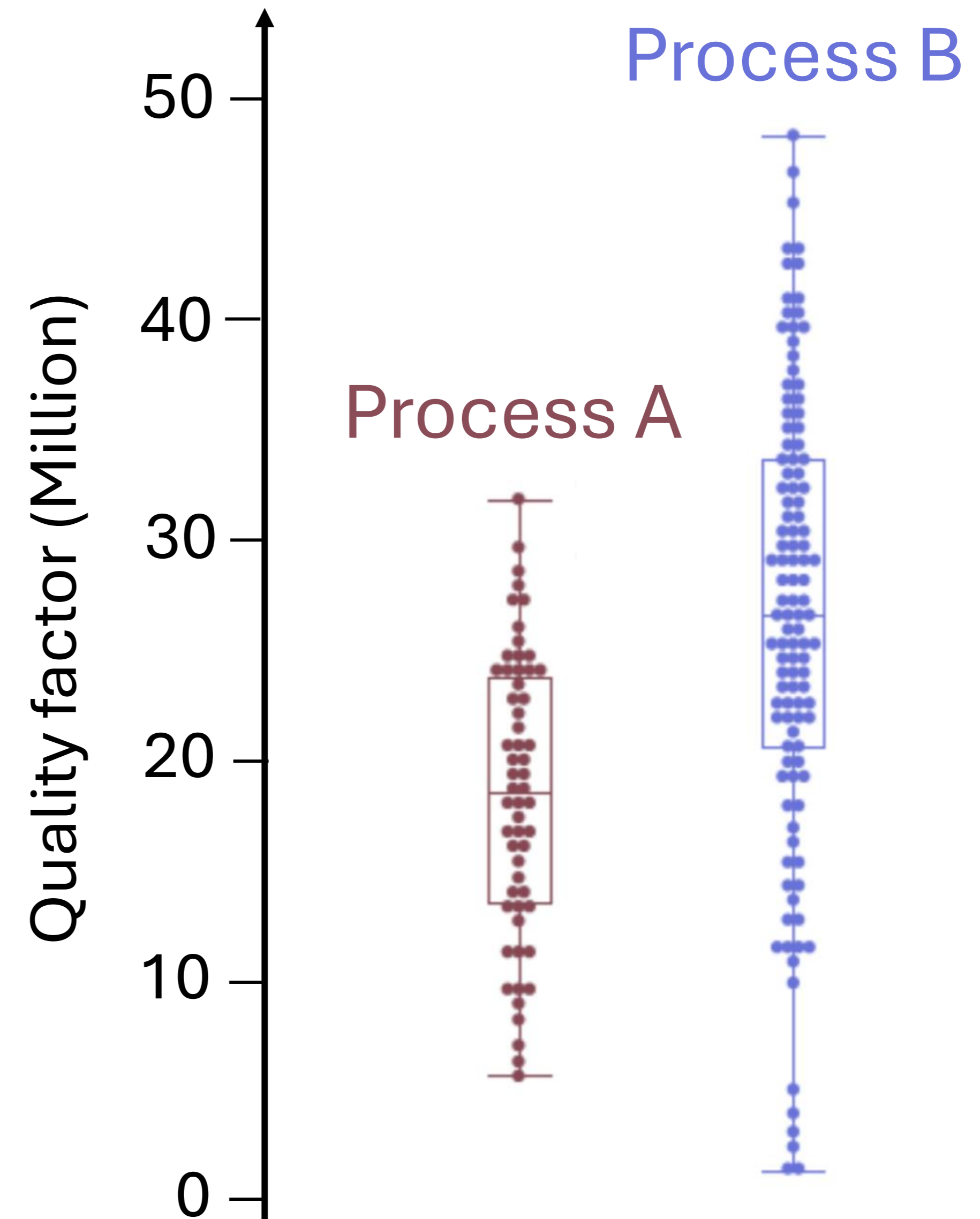
Doing research on T_1

- Is Process B better than process A?
- As T_1 improves:
 - Measure more qubits
 - Measure each longer
- Open questions about how many and how long



Doing research on T_1

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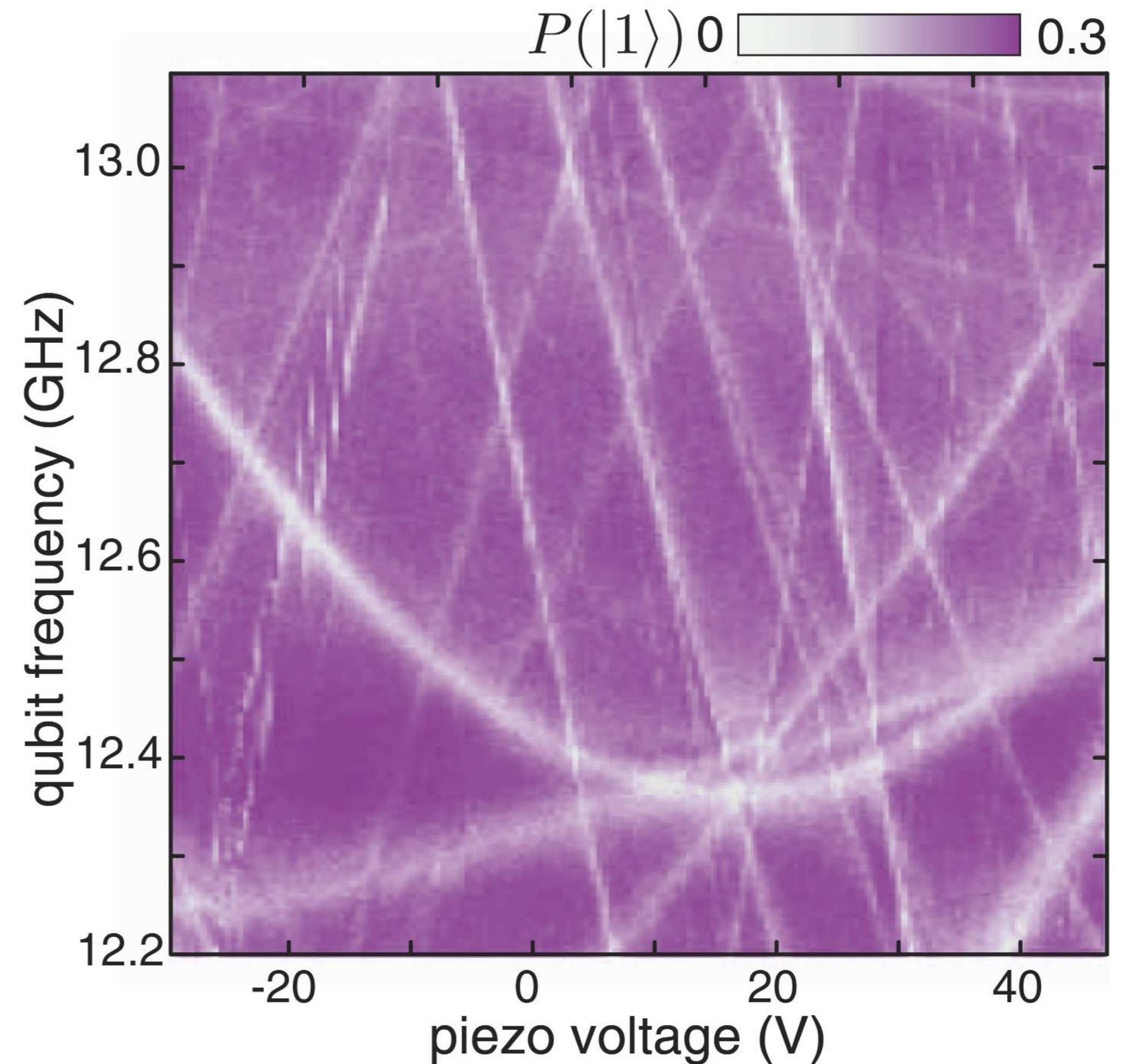
TLS Manipulation

We can directly control TLS energy by:

- 1) altering local **strain**
- 2) altering **E-field** at TLS

$$\hbar\omega_{TLS} = \sqrt{\Delta_0^2 + \varepsilon^2}$$

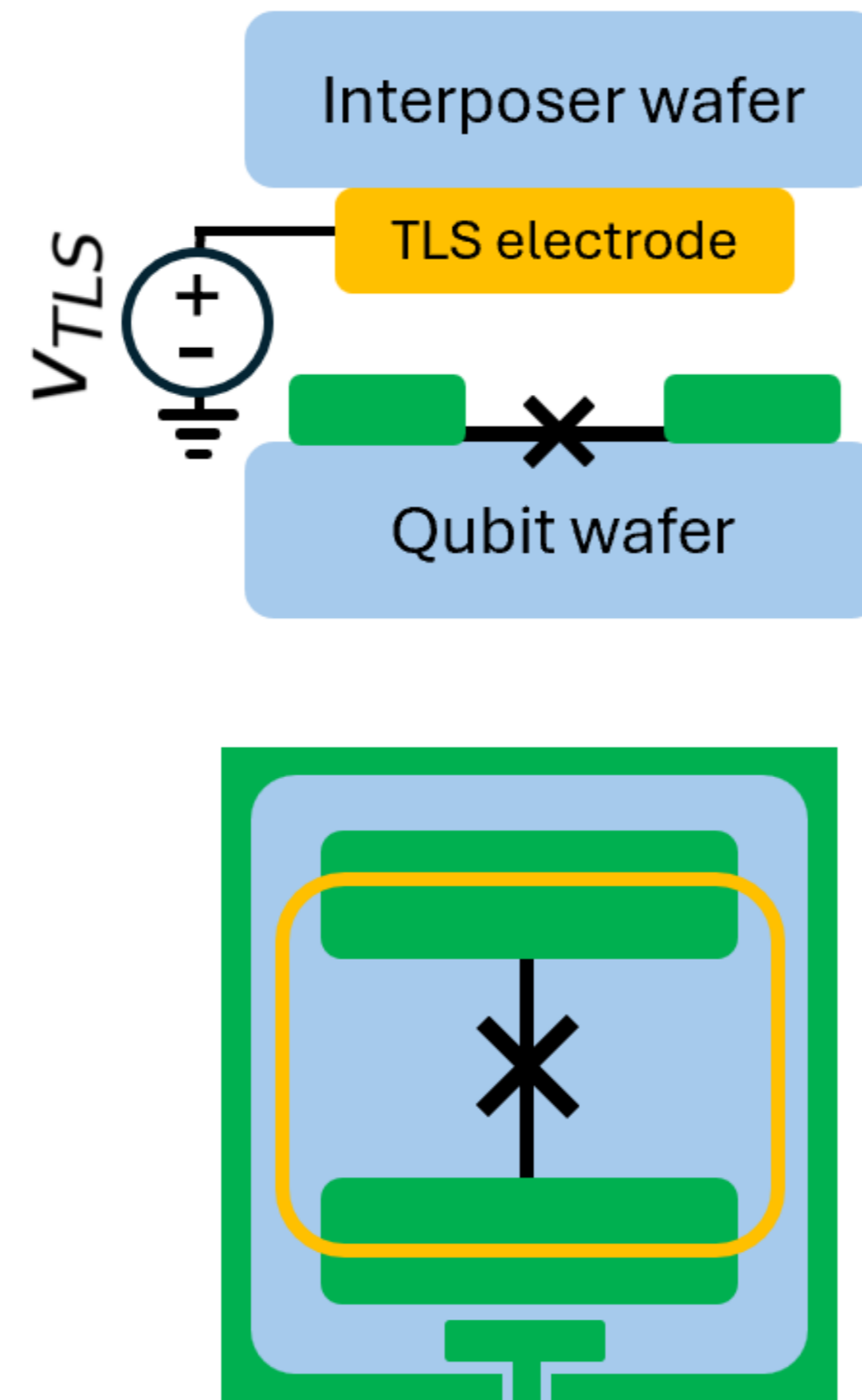
$$\varepsilon = 2\boldsymbol{\gamma} \cdot \boldsymbol{S} + 2\boldsymbol{p} \cdot \boldsymbol{E} + \varepsilon_0$$



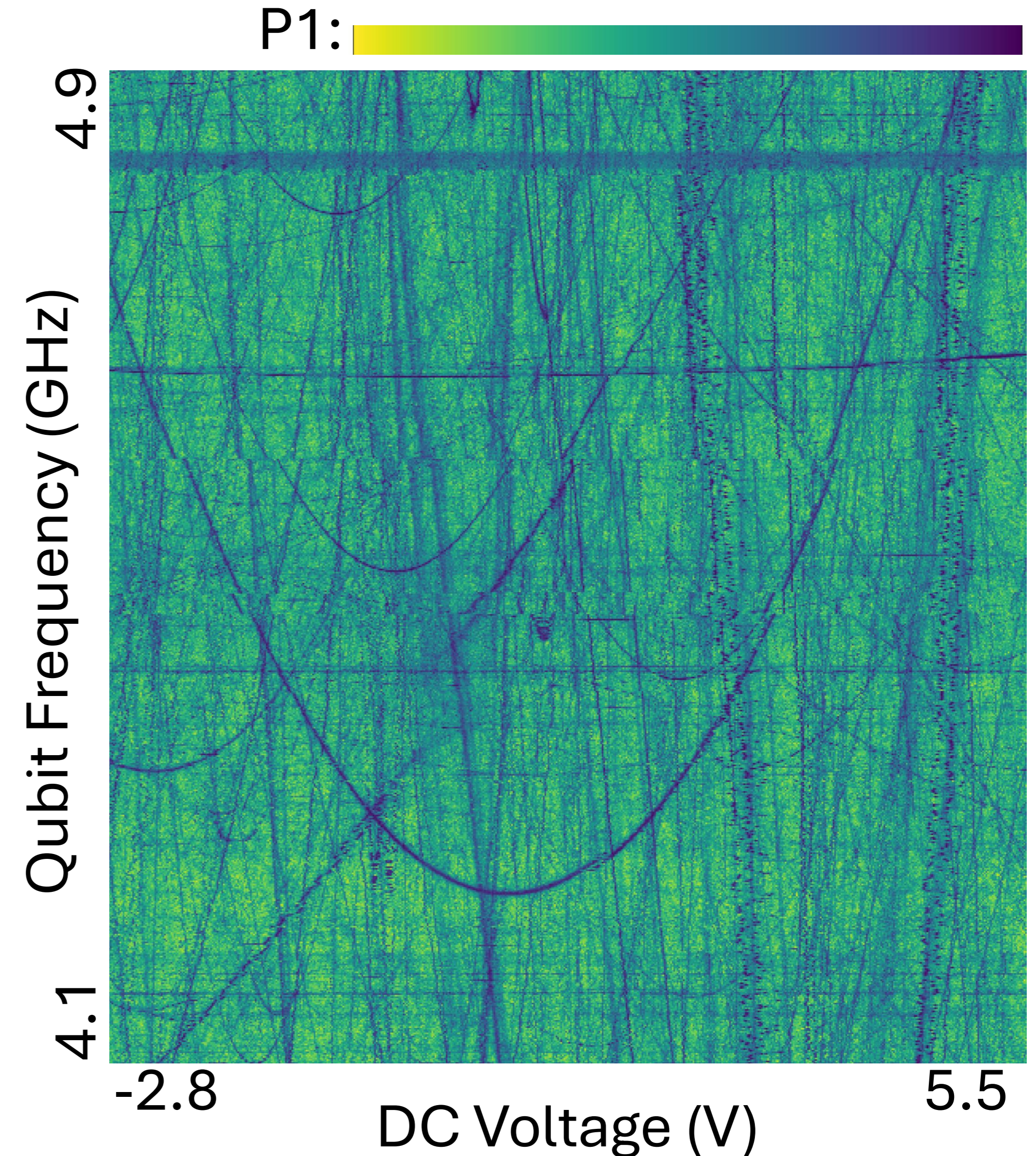
Grabovski et al, *Science* 338 (2012)

Local TLS Manipulation

- Transmon qubits
- Weakly coupled to RO resonator
- Electrode centered above qubit paddles on interposer wafer

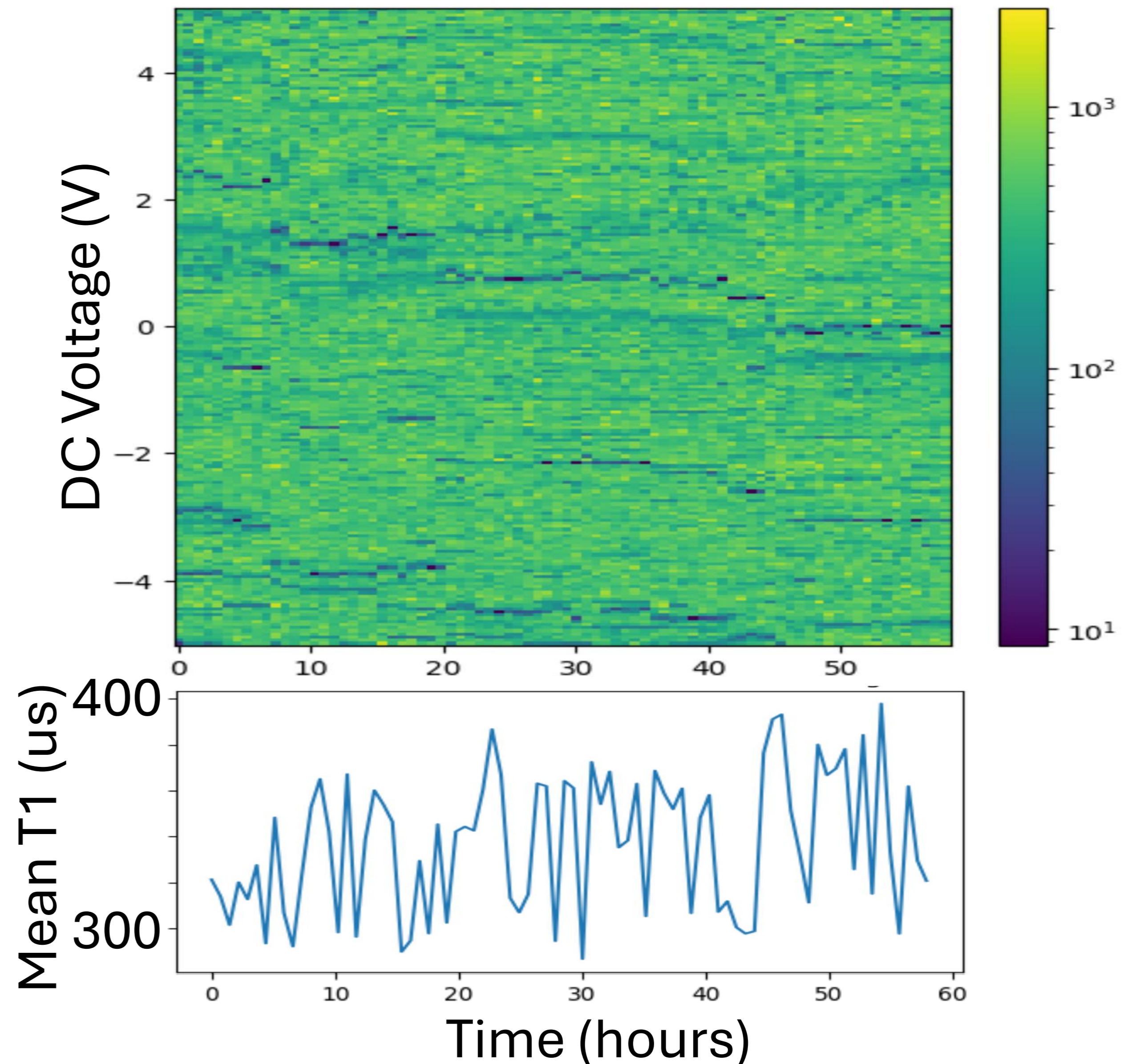


Dane et al., npj Quant. Info, 2026

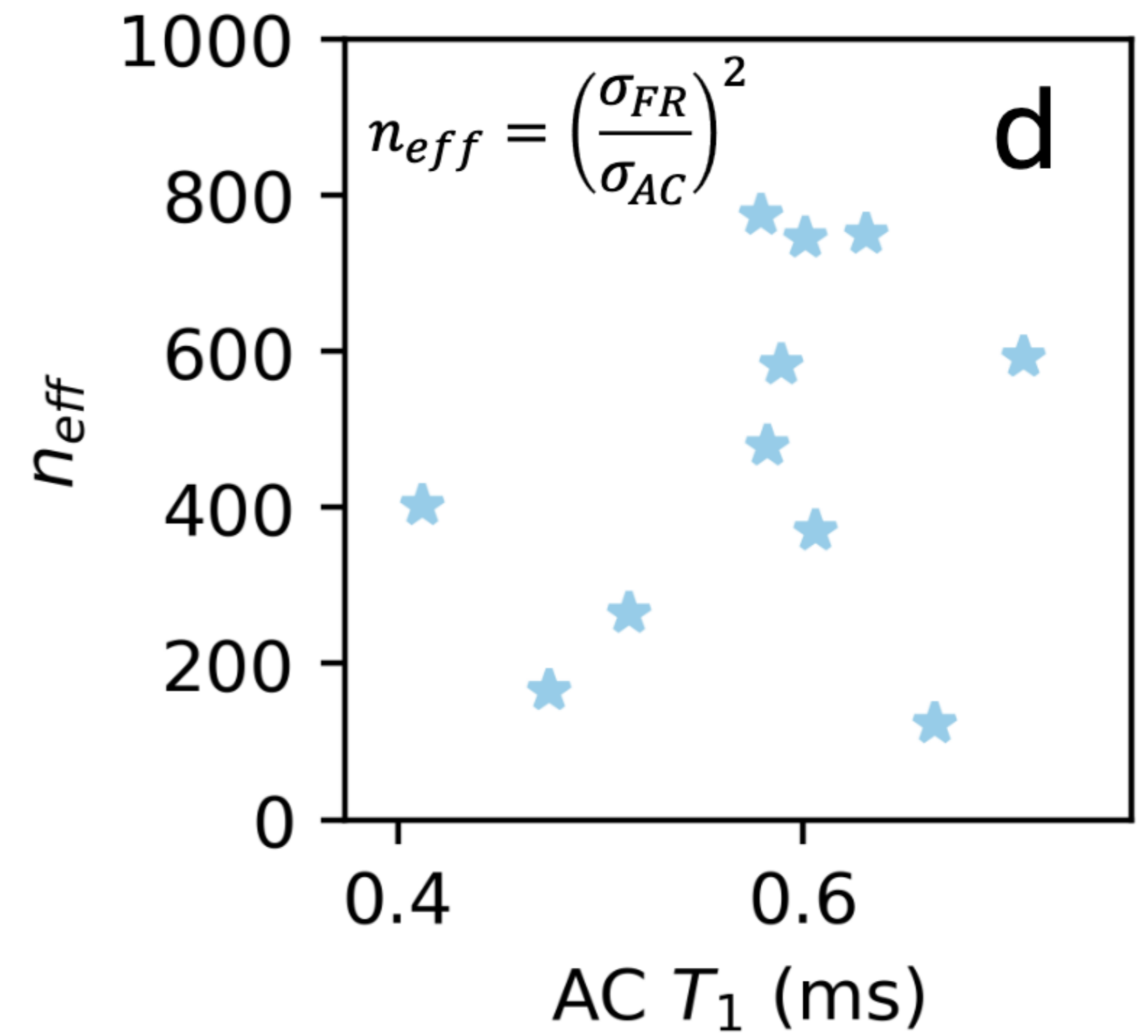
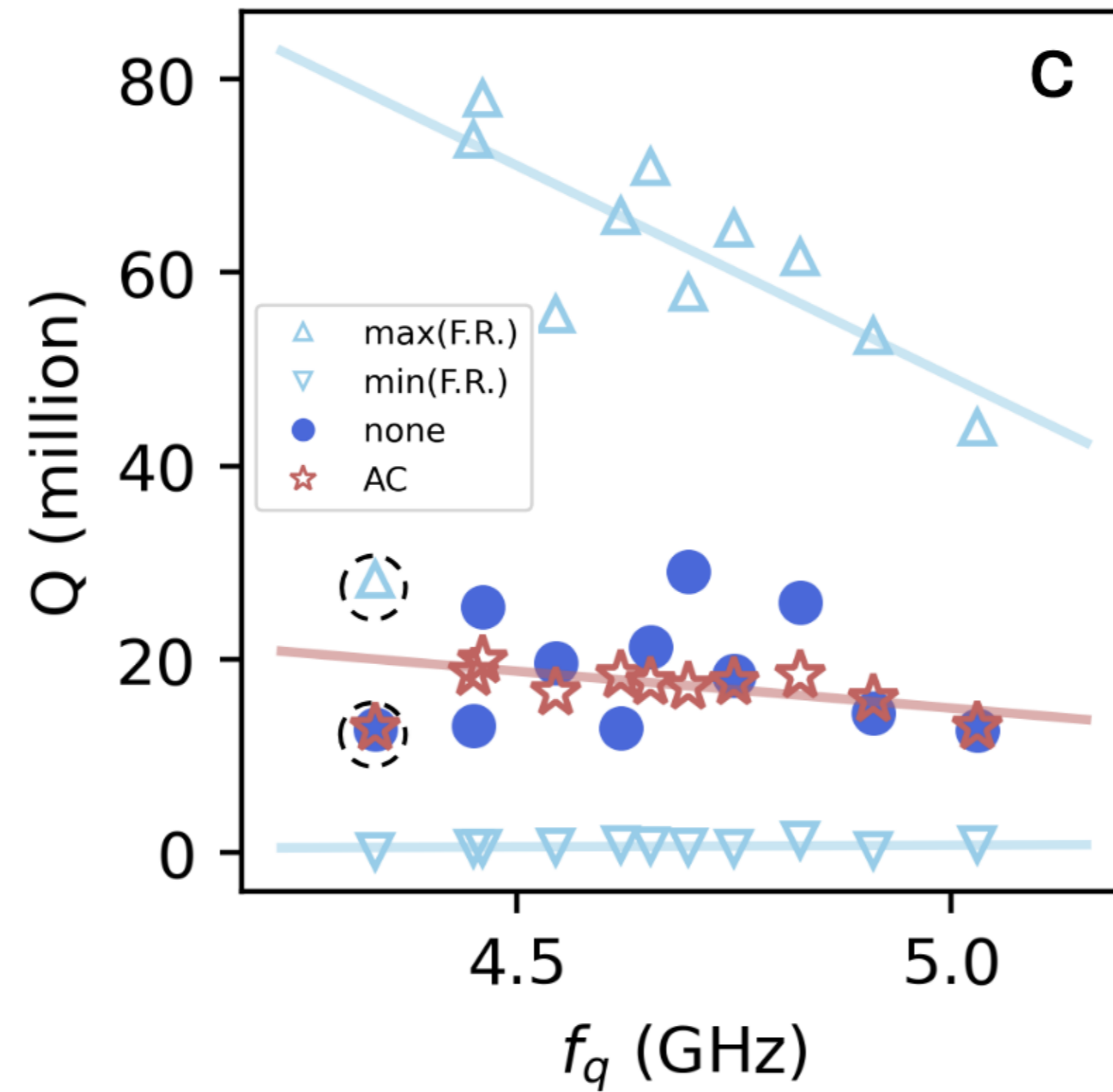
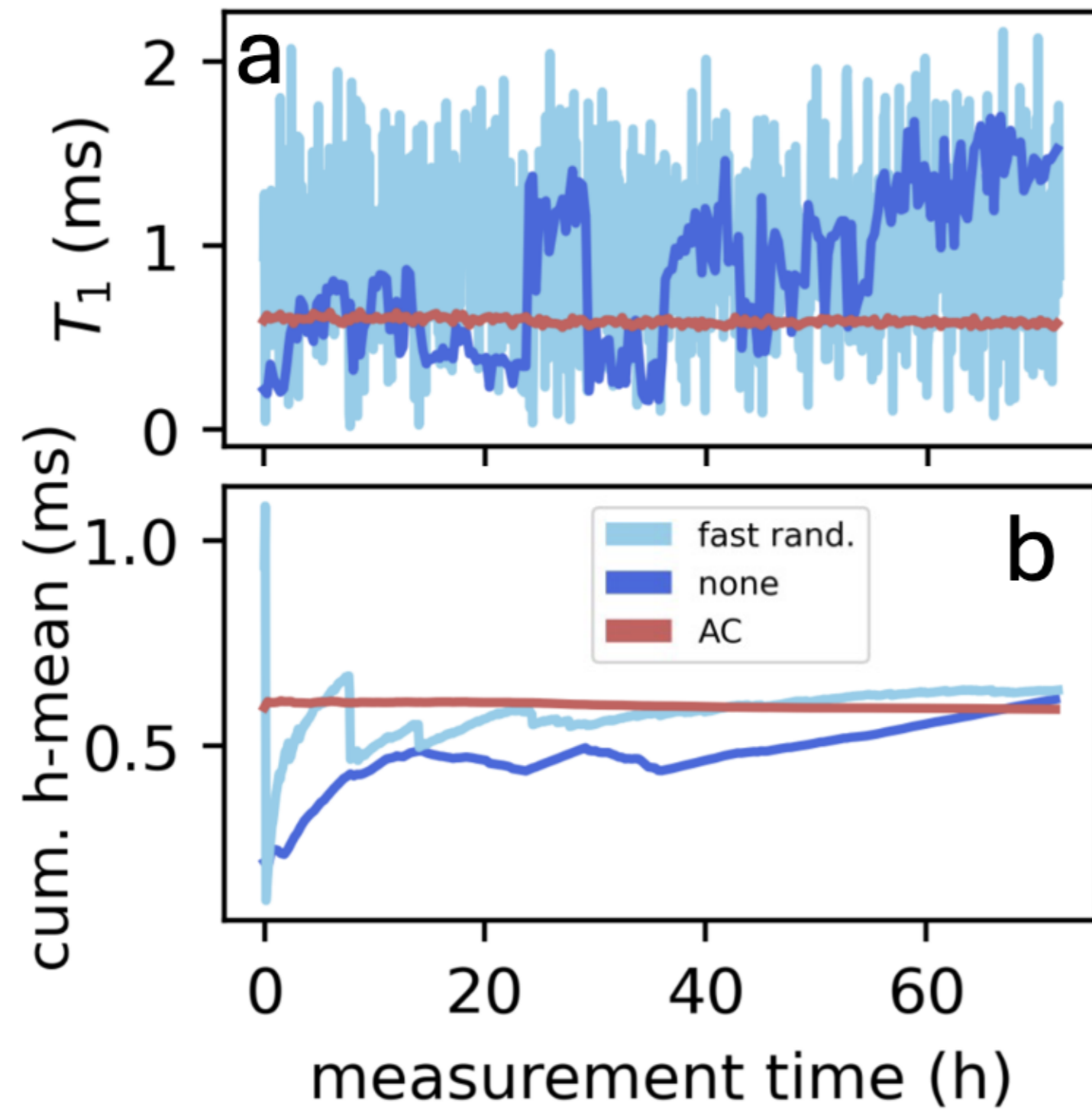


Evolution vs. voltage and time

- Sweep DCV, measure P1 -> T1
- TLS losses (dark blue)
- Two major observations:
 - The vast majority of the voltage space has T1 100s of us
 - TLSes move around more than appear/disappear.
- T1 averaged over voltage is very stable (337 us \pm 29 us)

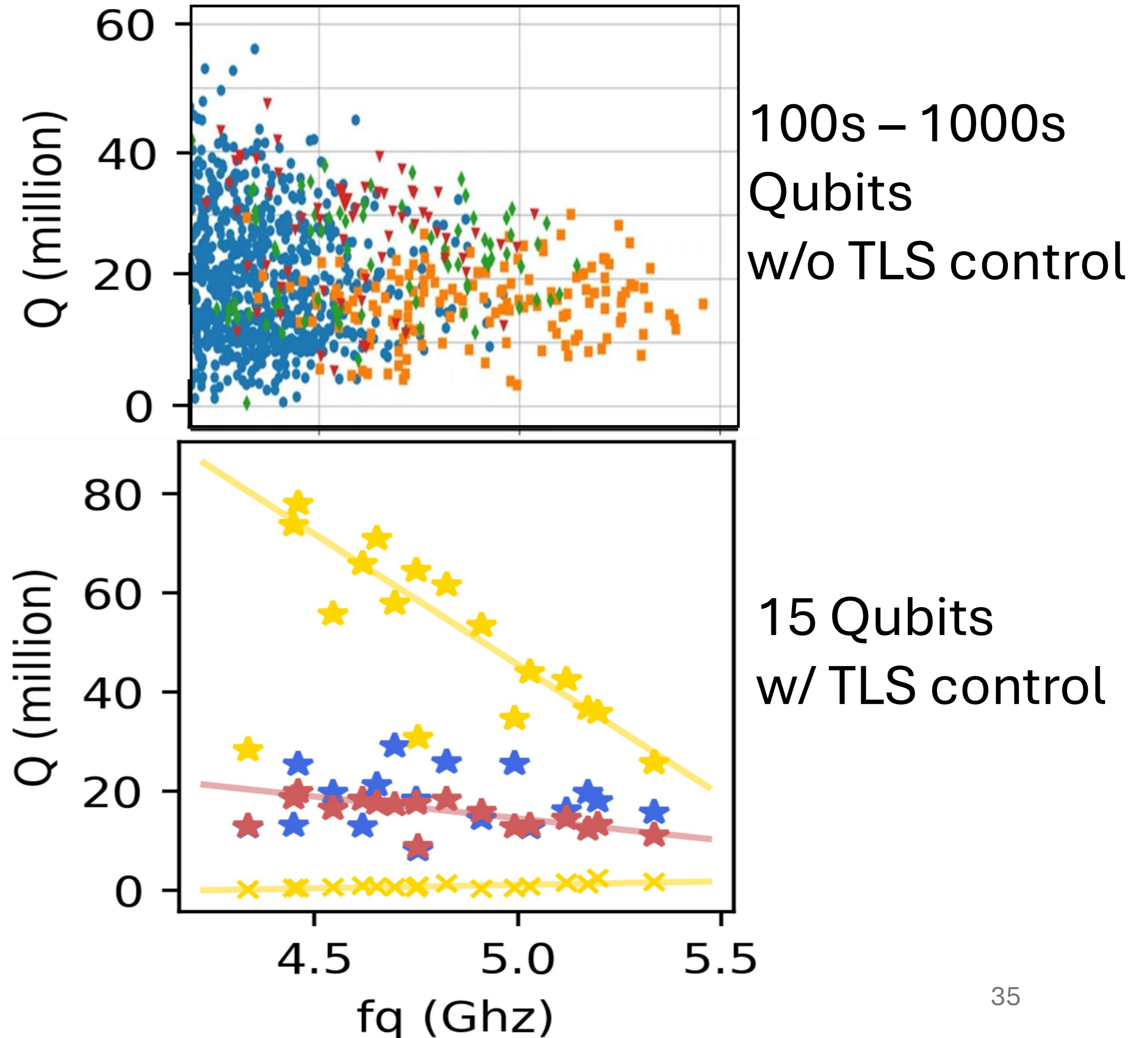


Better statistics with less data



Seeing trends with T_1 control

- Top: portion of Q vs frequency collected over thousands of qubits, many builds
- Bottom: Qs accessed using the TLS voltage pad.
- TLS control allows us to observe subtle trends with orders of magnitude fewer qubits

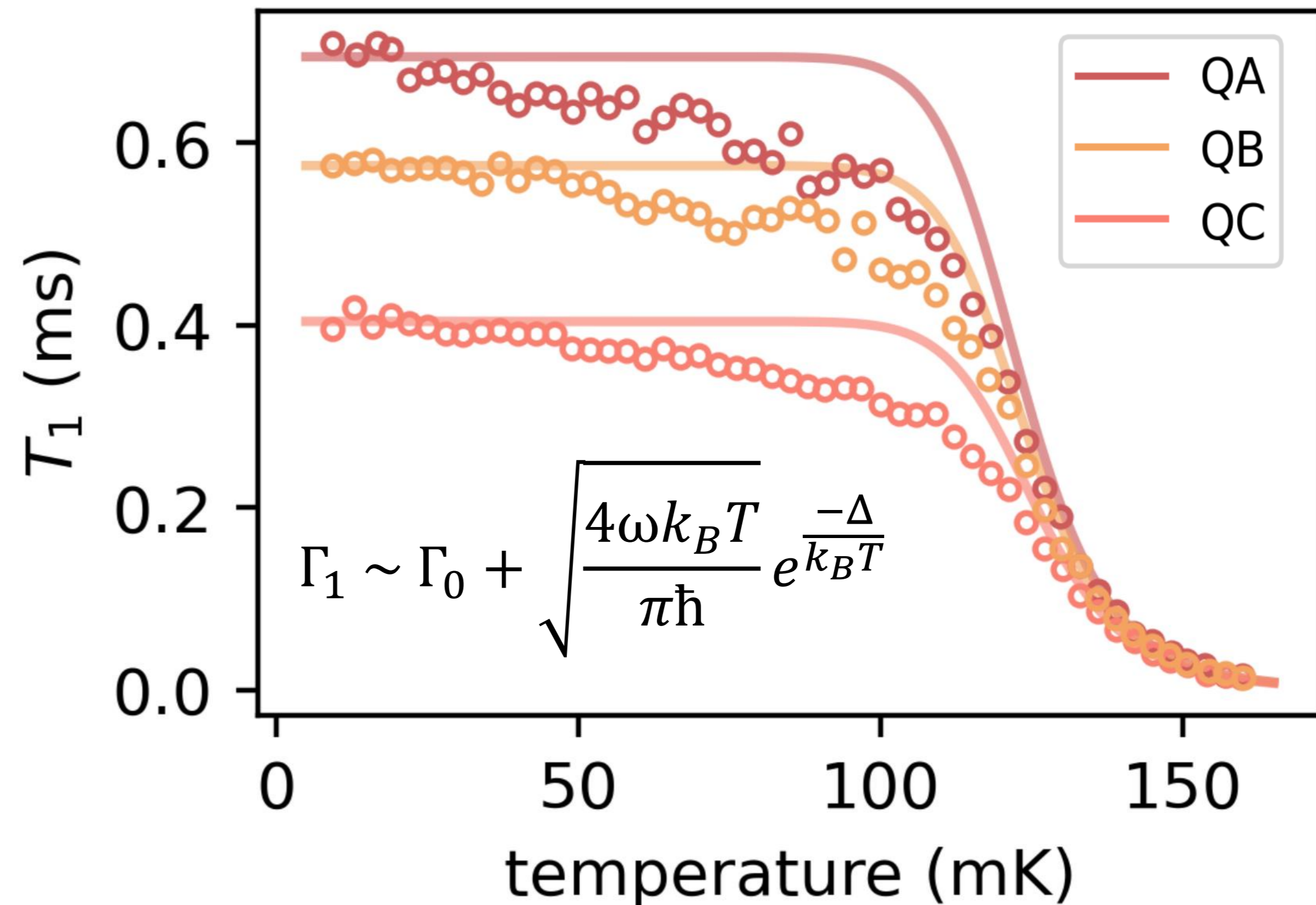


Seeing trends with T_1 control

- Measure T_1 with AC bias as a function of mixing plate temperature
- Functional form of T_1 well explained by thermal QPs $T > 100$ mK
- Quasi-linear regime not understood
- Quasi-linear regime also seen when averaging together large # of qubits

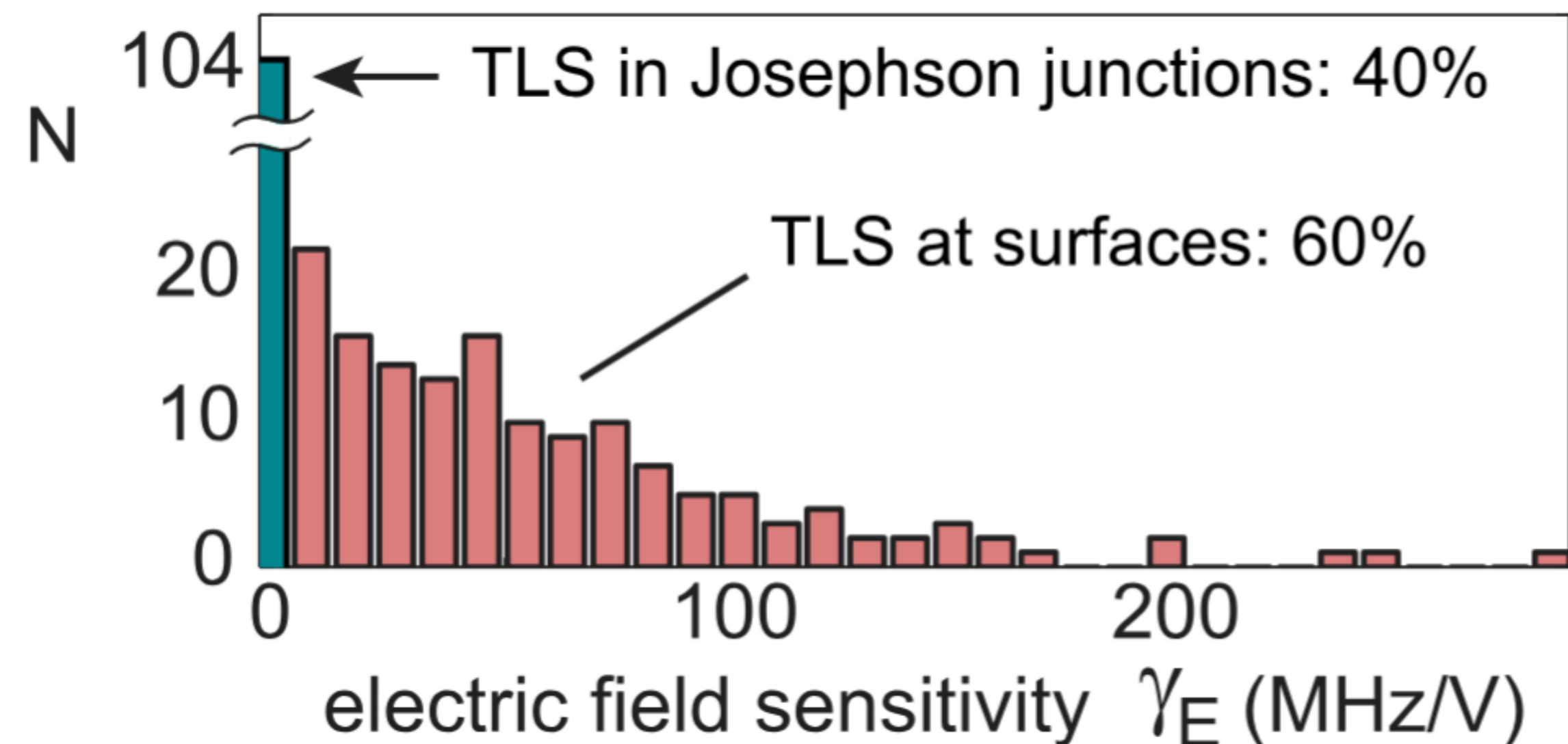
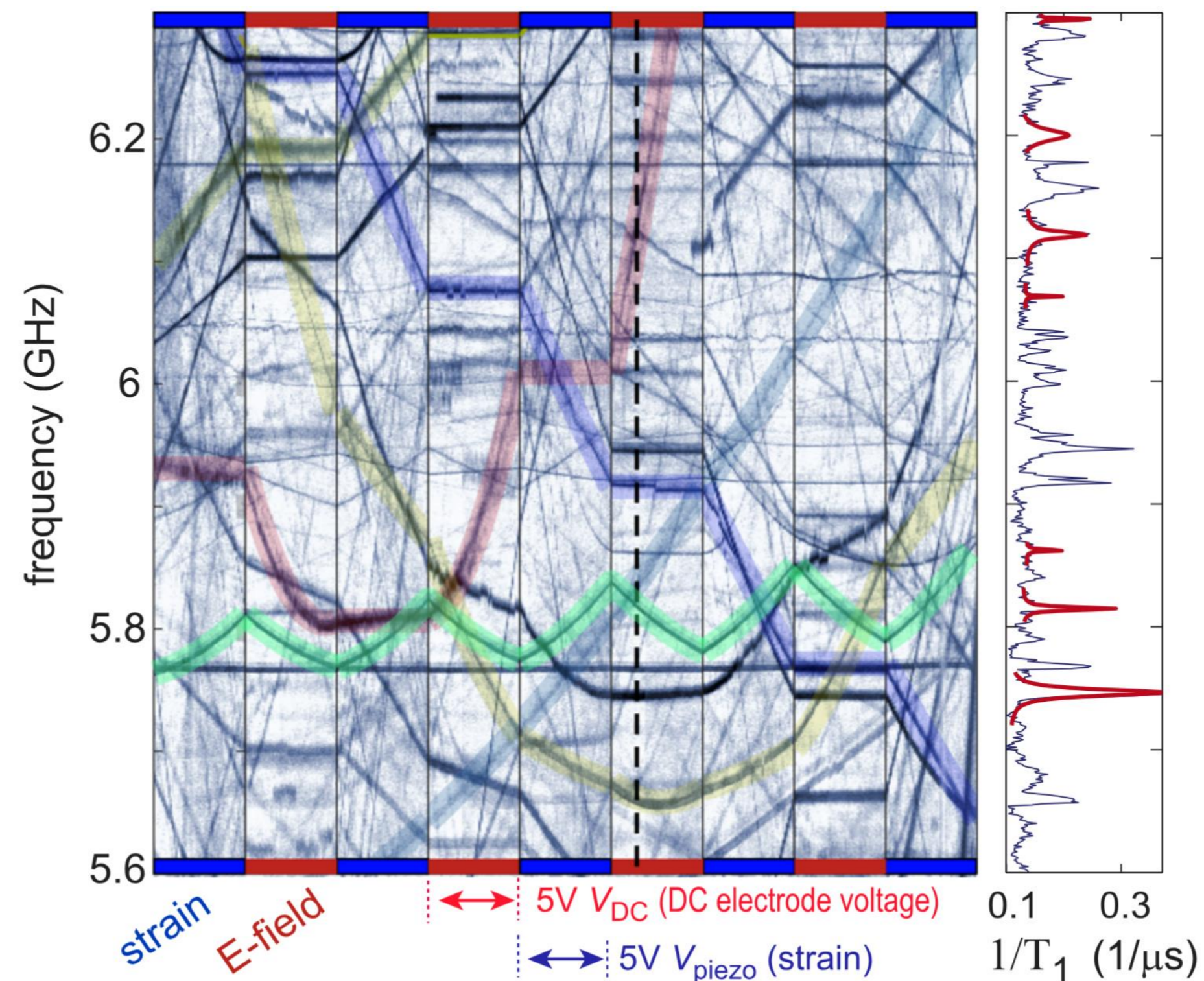
Dominant loss mechanism:

← TLS | Thermal QPs →



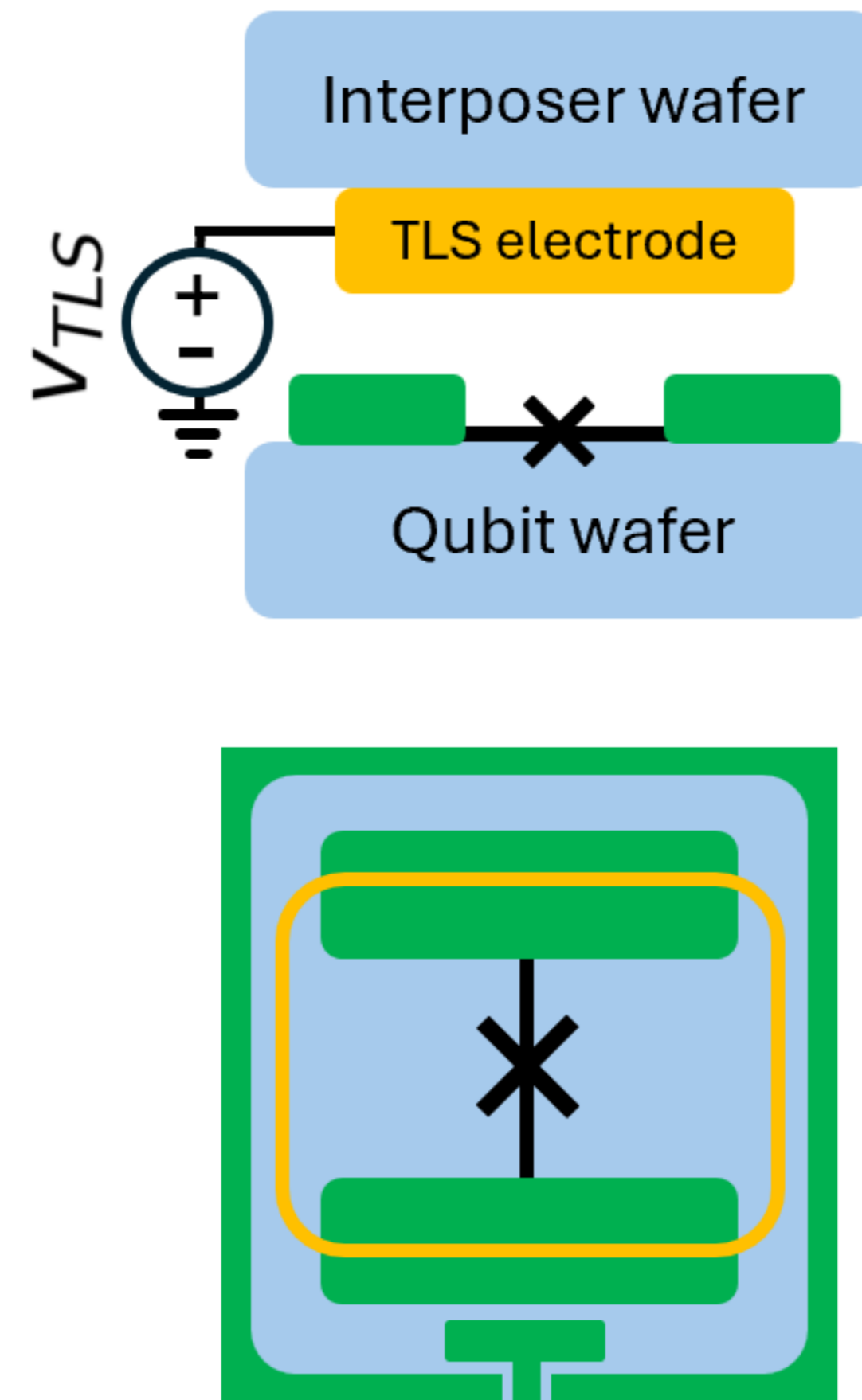
Non-tunable TLS's

- TLS only change frequency if the applied field reaches them
- Literature suggests ~40% of TLS do not respond to applied field
- These non-tunable TLS can't be moved by our AC fields

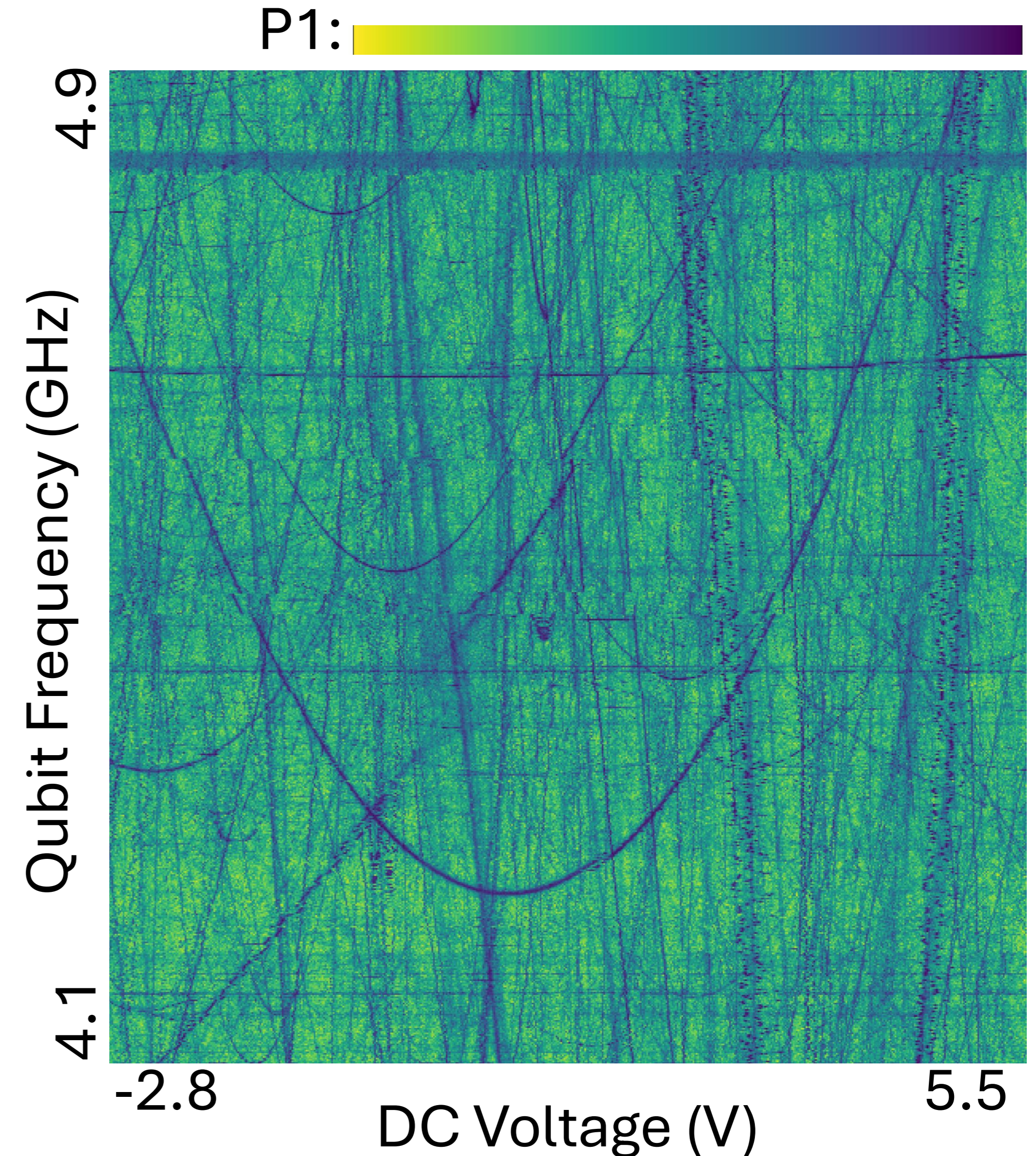


Local TLS Manipulation

- Transmon qubits
- Weakly coupled to RO resonator
- Electrode centered above qubit paddles on interposer wafer

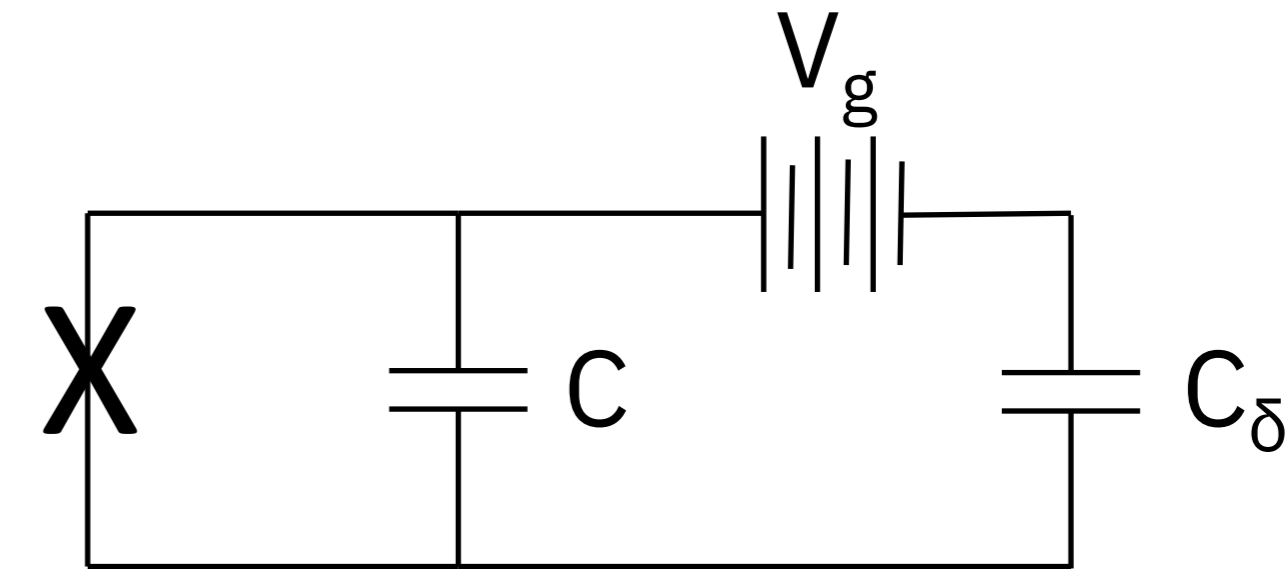


Dane et al., npj Quant. Info, 2026



Quantum non-linear circuits: Josephson junction

$$\hat{H} = \frac{1}{2C} \left(\hat{Q} - V_g C_\delta \right)^2 - E_j \cos(\hat{\Phi} / \varphi_0)$$



$$E_C = \frac{e^2}{2C} \quad n_g = \frac{V_g C_\delta}{4e^2} \quad n = \text{number of Cooper pairs}$$

$$\hat{H} = 4E_C (\hat{n} - n_g)^2 - E_j \cos(\hat{\Phi} / \varphi_0)$$

$$e^{-ip\hat{\Phi}} |n\rangle = |n + p\rangle \quad (n \text{ and } \phi \text{ are conjugate variables})$$

Charge qubit: The cooper pair box

$$\hat{H} = 4E_C (\hat{n} - n_g)^2 - E_J \cos(\hat{\Phi})$$

Define charge basis

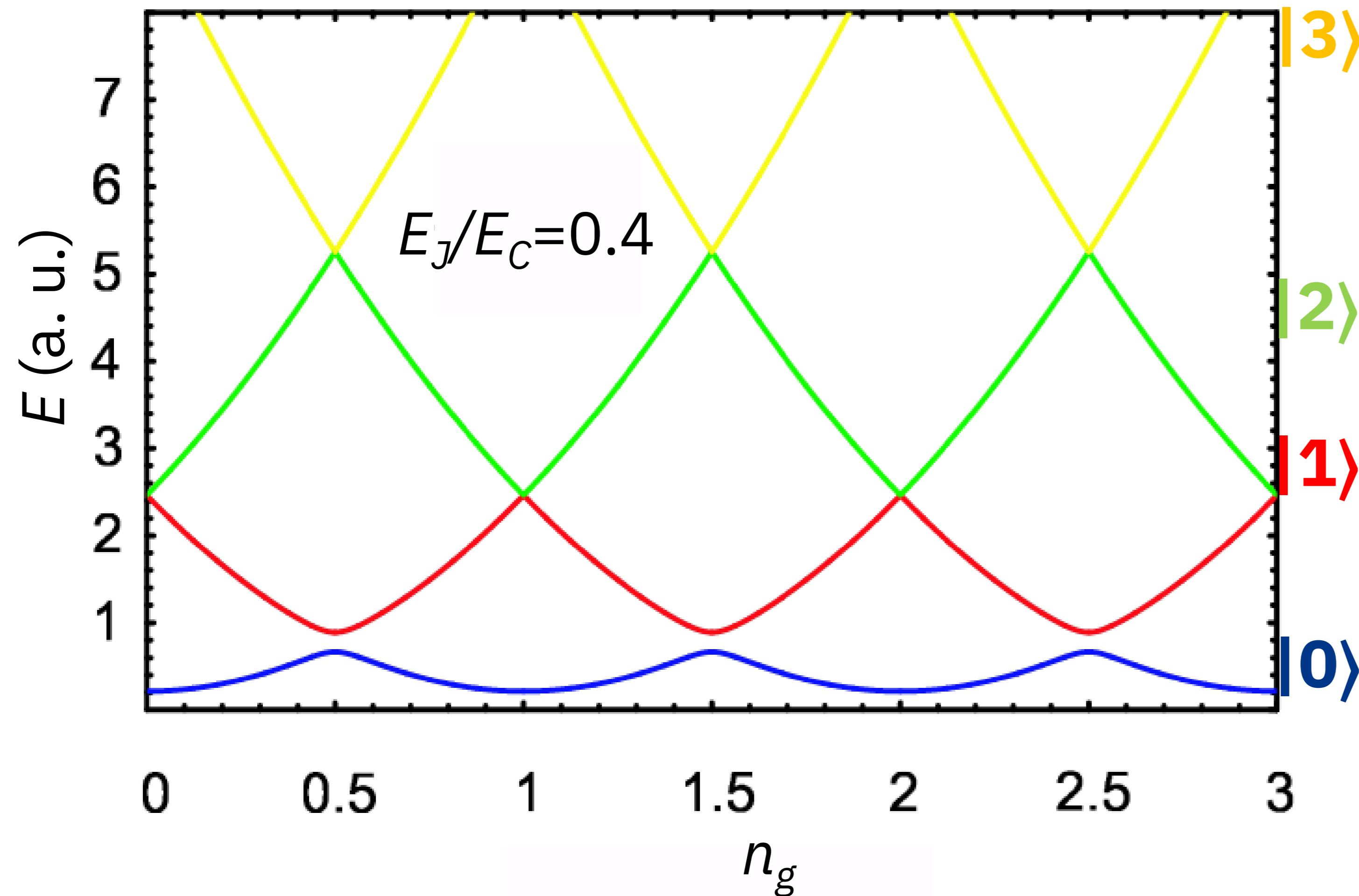
$$\hat{n}|n\rangle = n|n\rangle$$

Conjugate variables

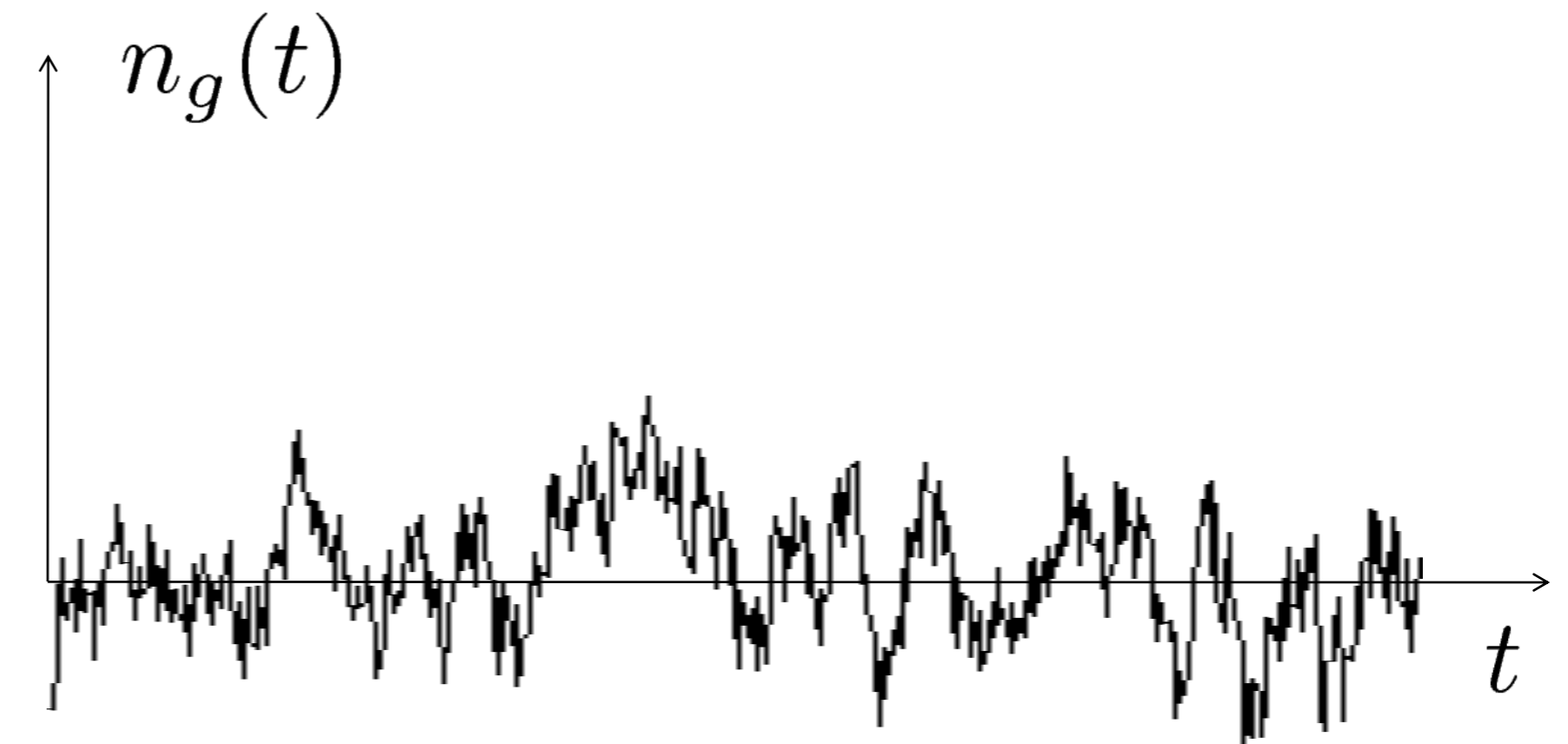
$$e^{-ip\hat{\Phi}}|n\rangle = |n+p\rangle$$

$$\hat{H} = \sum_n 4E_C (n - n_g)^2 |n\rangle \langle n| - \frac{E_J}{2} (|n+1\rangle \langle n| + |n\rangle \langle n+1|)$$

Charge qubit: The cooper pair box



Charge fluctuations



First experiment in 1999: $T_2 \sim 1$ ns
 Sweet spot operation in 2002
 $T_2 \sim 500$ ns Nakamura, Nature 1999

$$\hat{H} = \sum_n 4E_C (n - n_g)^2 |n\rangle \langle n| - \frac{E_J}{2} (|n+1\rangle \langle n| + |n\rangle \langle n+1|)$$

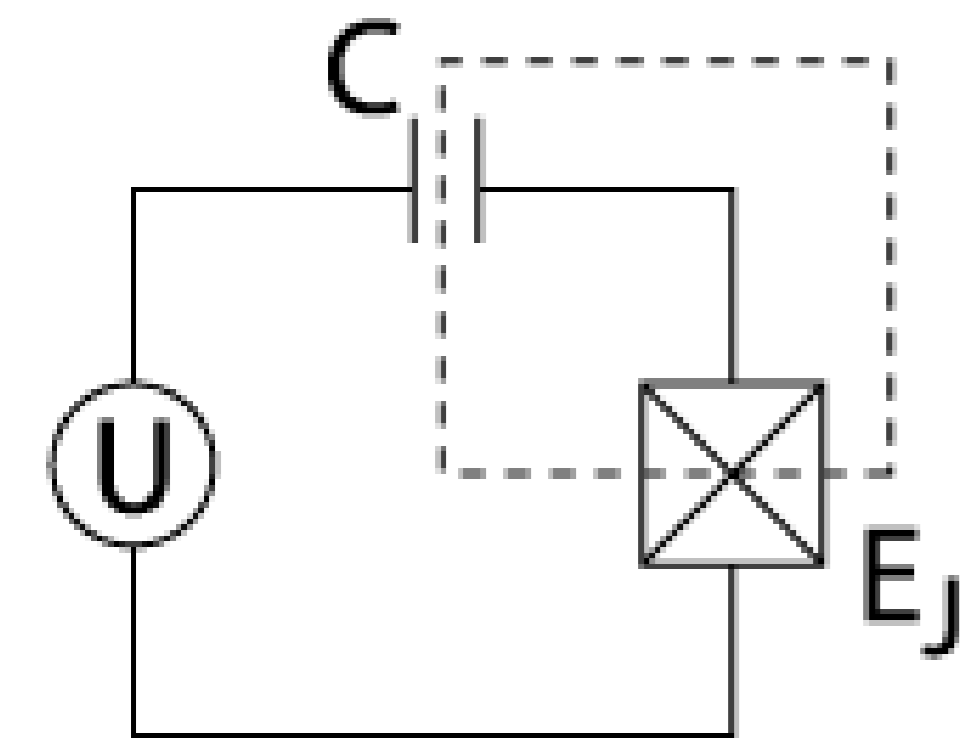
The tale of two energies

J. Koch et al, Phys. Rev. A 76, 042319 (2007)

IBM Quantum

L. Bishop. PhD Thesis

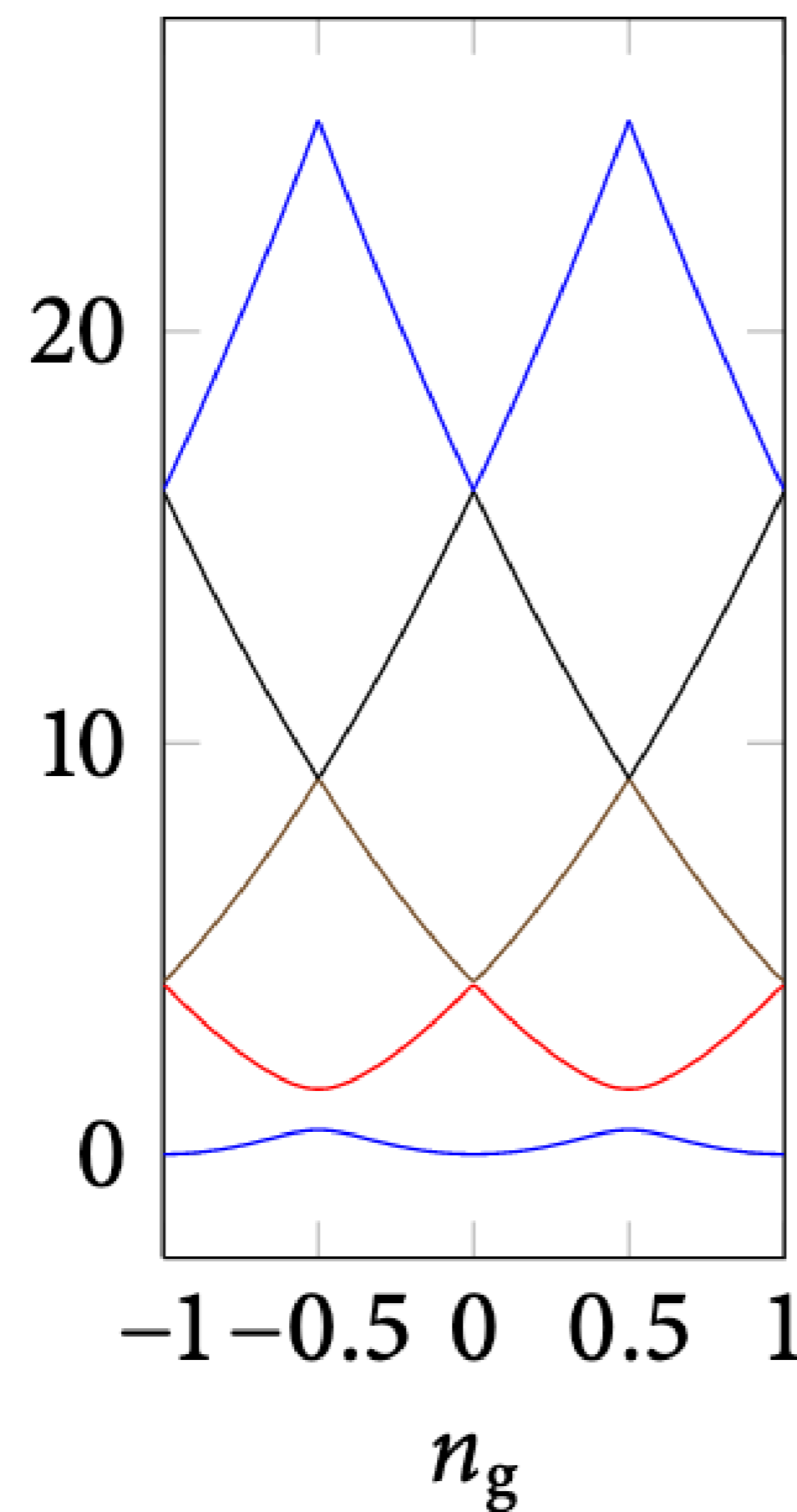
Charge dispersion suppressed faster than anharmonicity



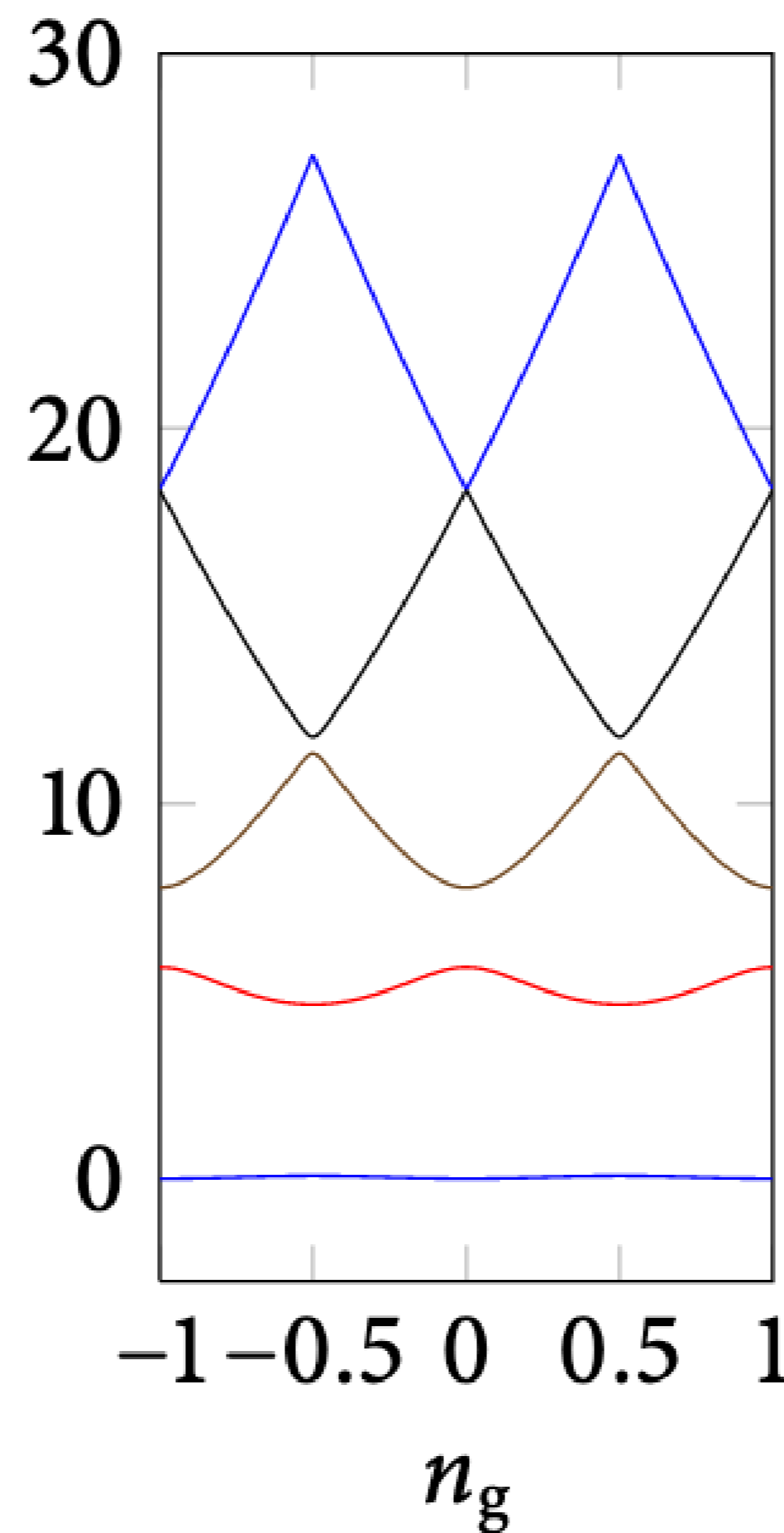
$$E_J = \frac{I_c \Phi_0}{2\pi}$$

$$E_C = \frac{e^2}{2C}$$

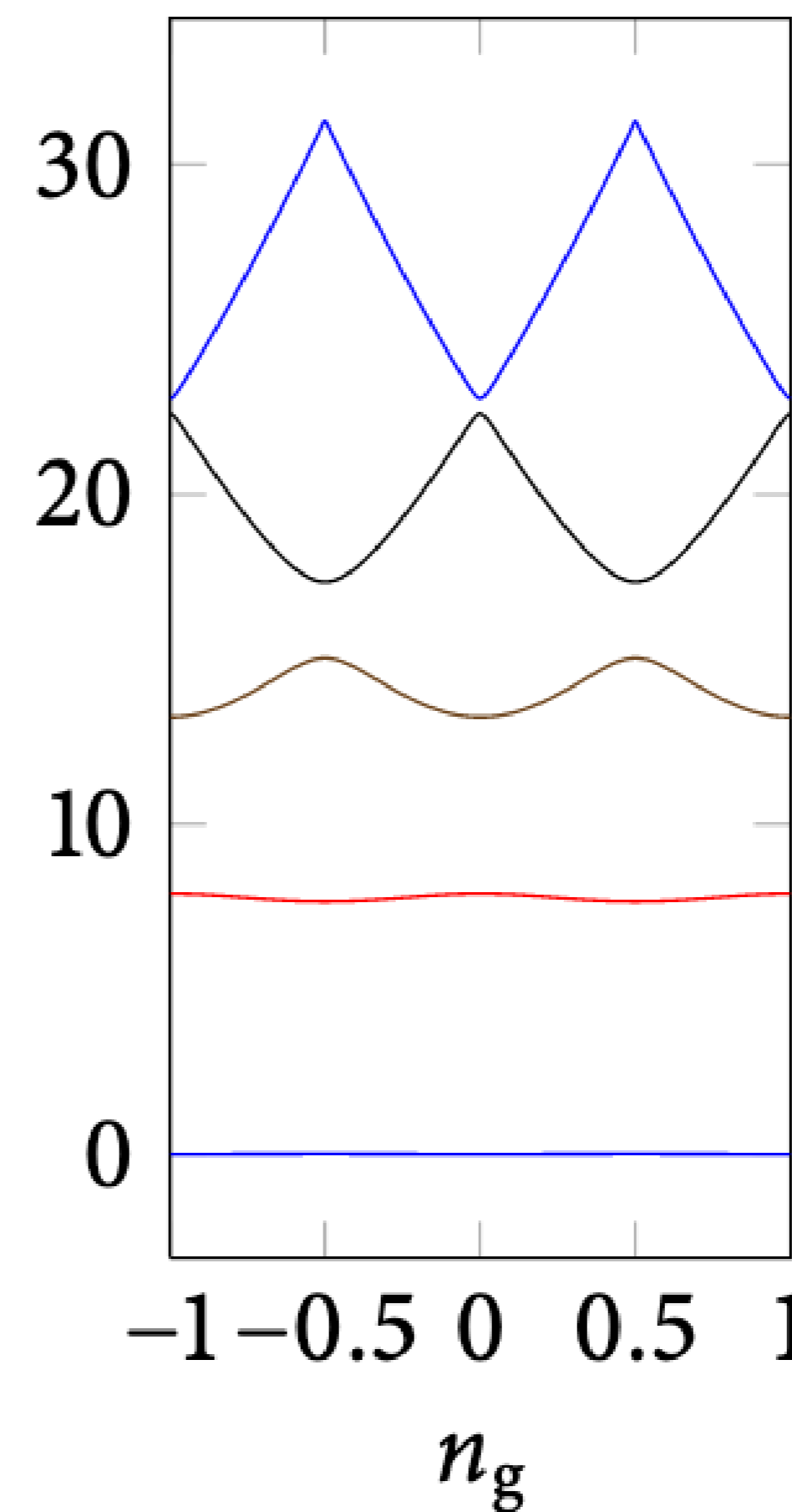
$E_J/E_C = 1$



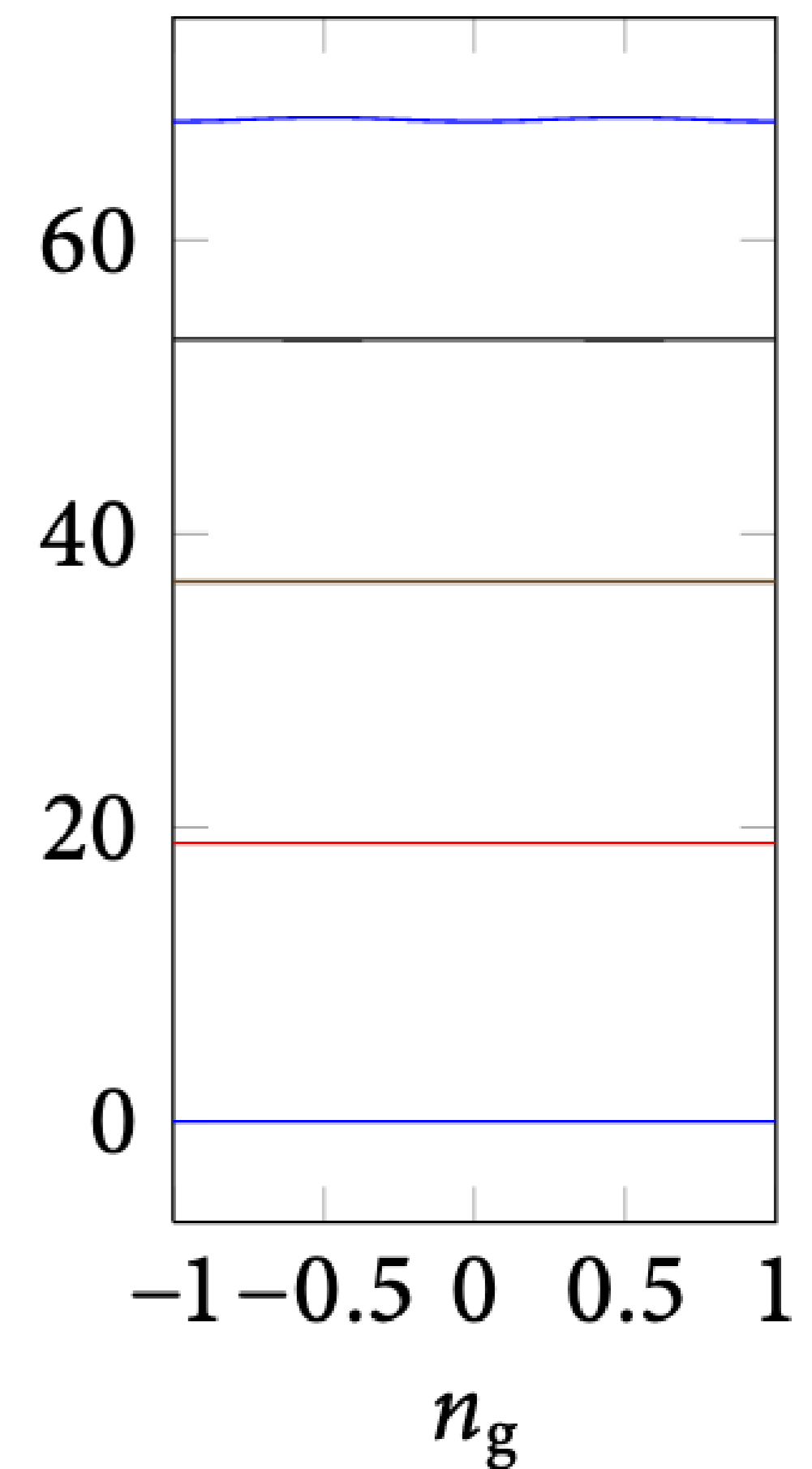
$E_J/E_C = 5$



$E_J/E_C = 10$



$E_J/E_C = 50$



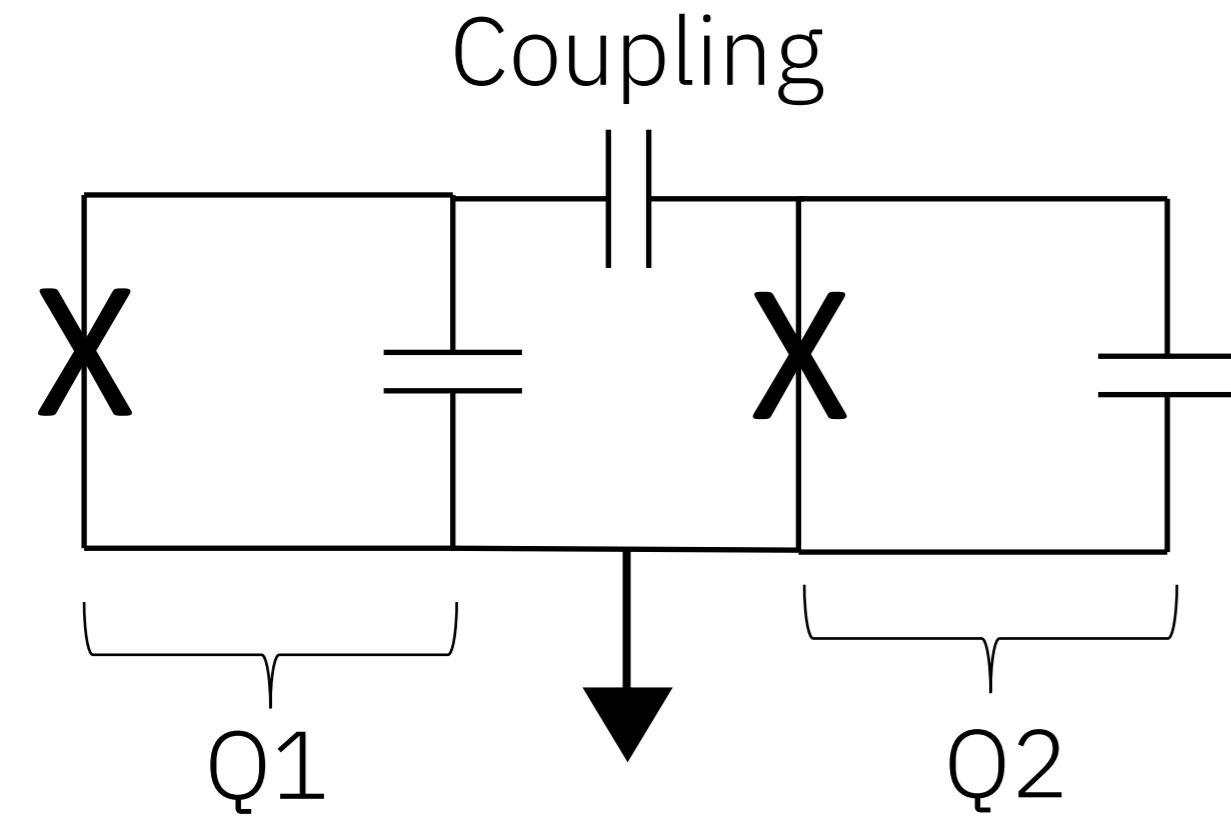
Introduction to Quantum Electromagnetic Circuits

Uri Vool* and Michel Devoret†

Department of Applied Physics,
Yale University, New Haven, CT 06520

arXiv:1610.03438v2

This is how to write these
Hamiltonians down correctly!



$$\hat{H} = \underbrace{\hbar\omega_1 \hat{a}^\dagger \hat{a} - \frac{\alpha_1}{2} \left((\hat{a}^\dagger \hat{a})^2 - \hat{a}^\dagger \hat{a} \right)}_{H_{Q1}} + \underbrace{\hbar\omega_2 \hat{b}^\dagger \hat{b} - \frac{\alpha_2}{2} \left((\hat{b}^\dagger \hat{b})^2 - \hat{b}^\dagger \hat{b} \right)}_{H_{Q2}} + \underbrace{C_c (\hat{Q}_1 \hat{Q}_2)}_{H_{\text{couple}}}$$

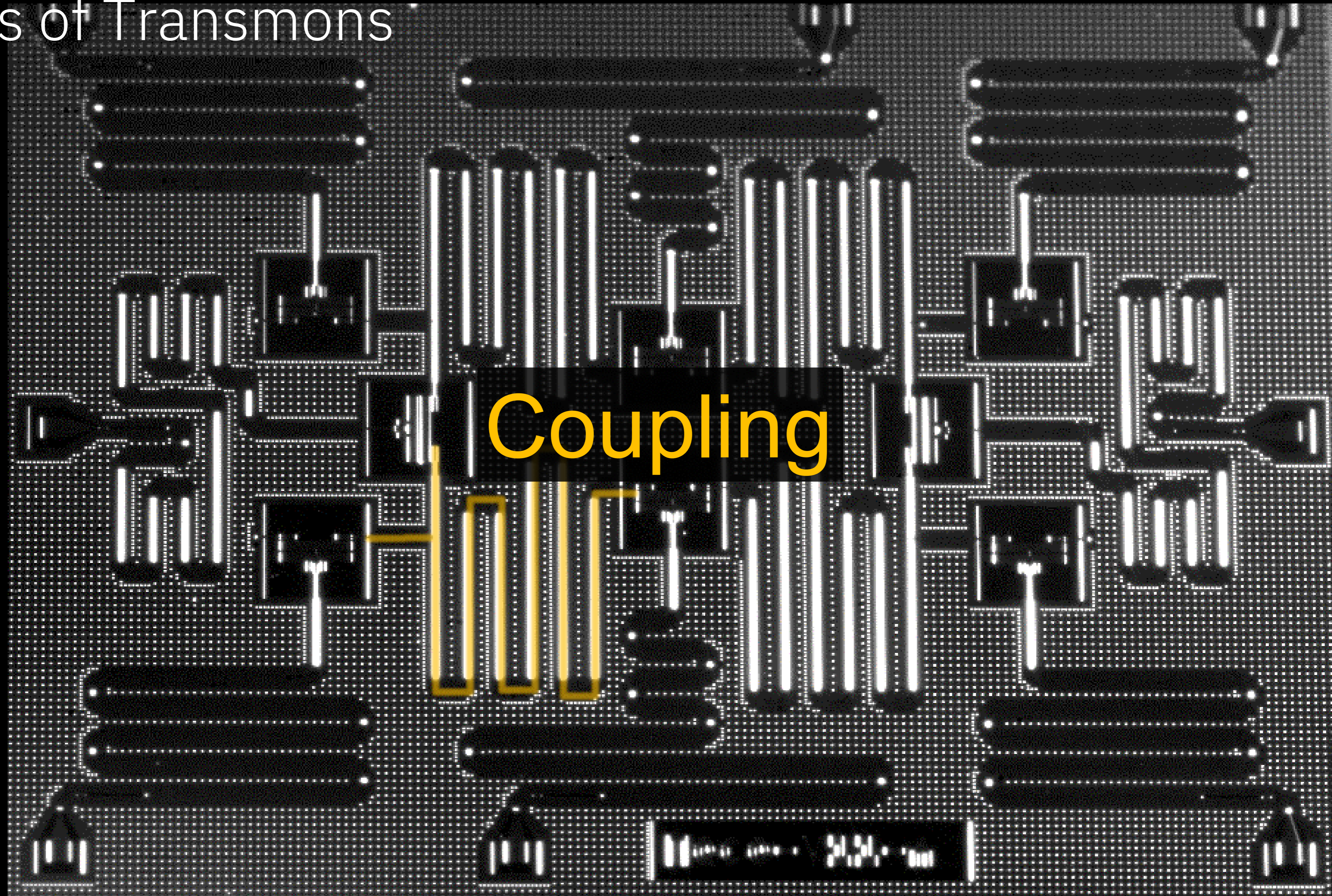
$$H_{\text{couple}} = J (\hat{a}^\dagger + \hat{a}) (\hat{b}^\dagger + \hat{b}) = J (\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms})$$

We call this exchange coupling because, in the RWA, it allows excitations to swap between the qubits.

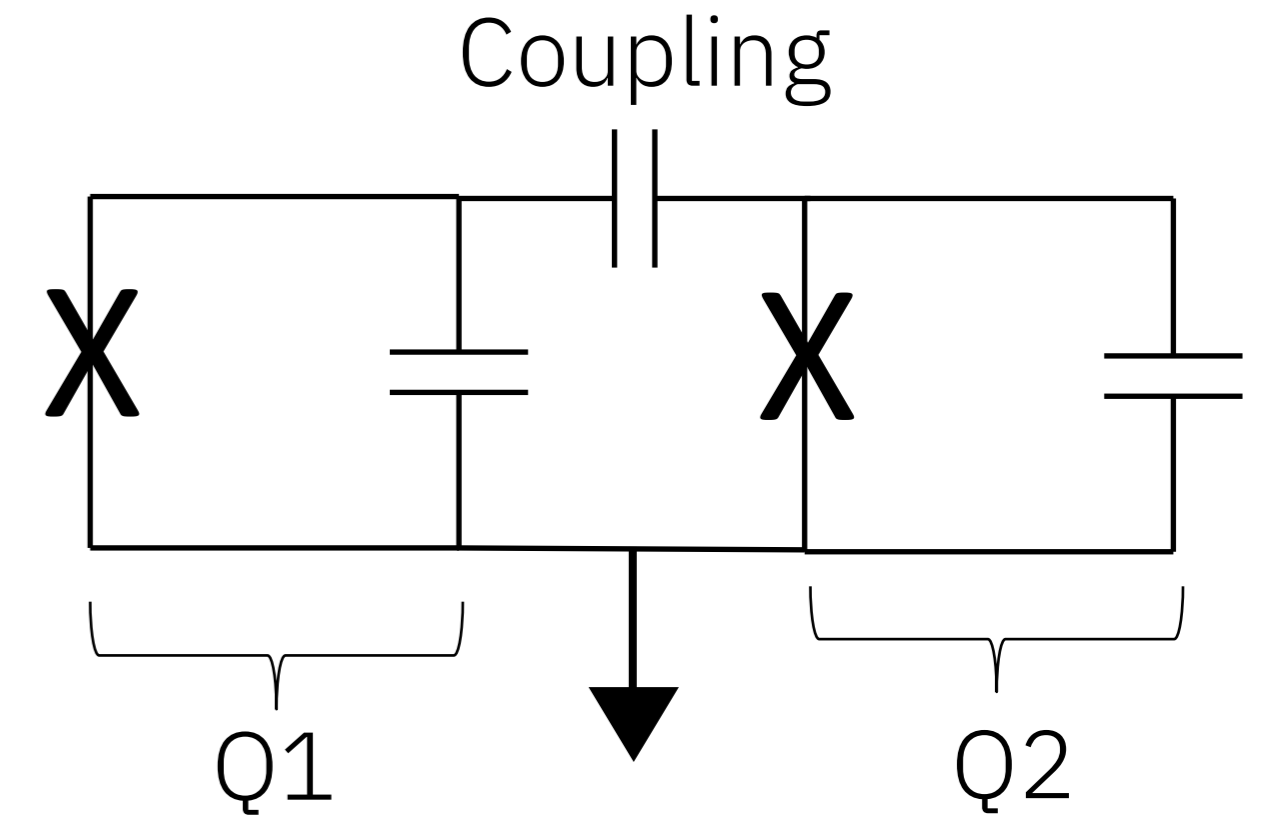
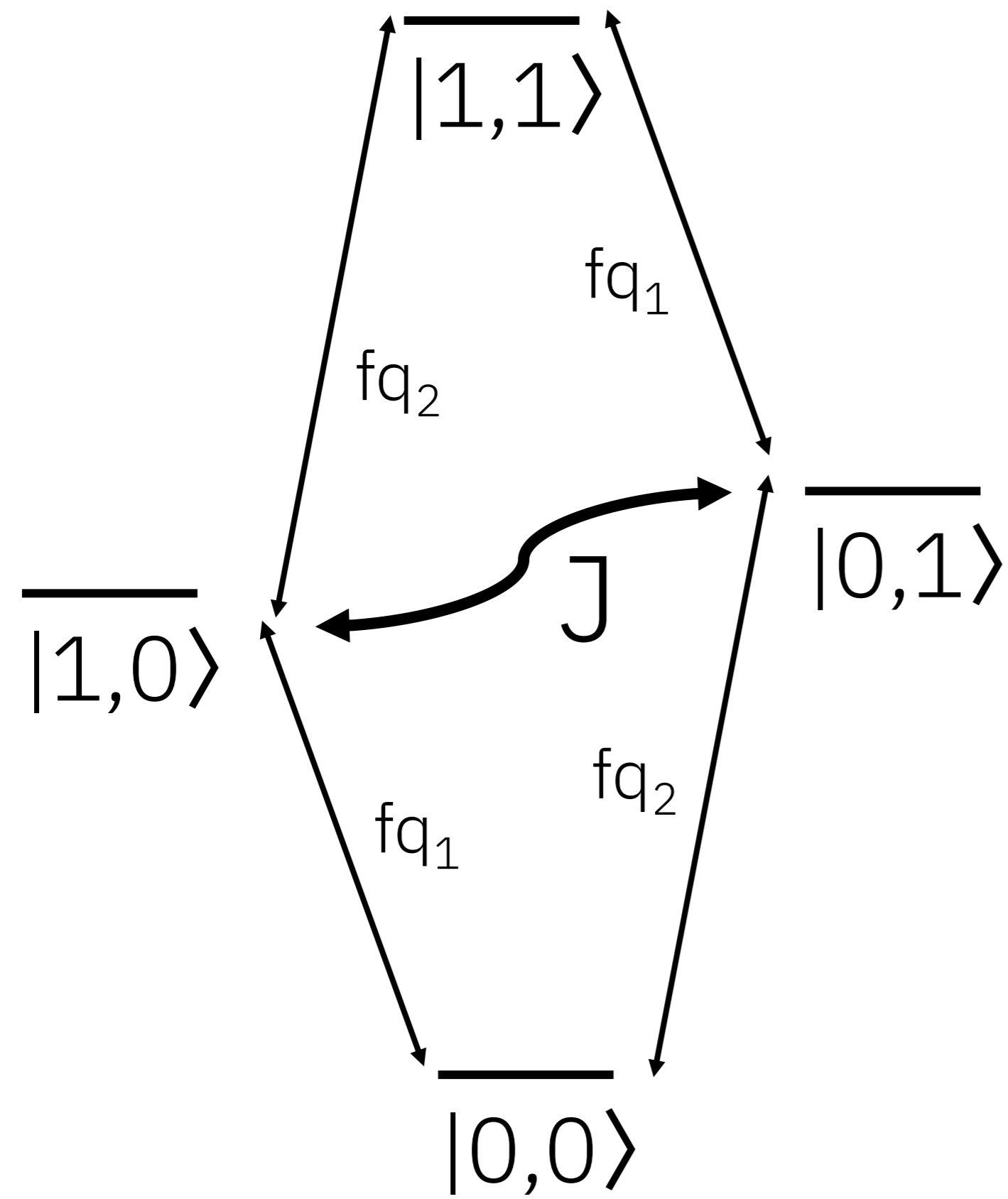
You can also get inductive exchange couplings, if, unlike this circuit, you have inductances.

α is the anharmonicity of the qubits; in the large E_j/E_c limit it is given by E_c

Circuits of Transmons

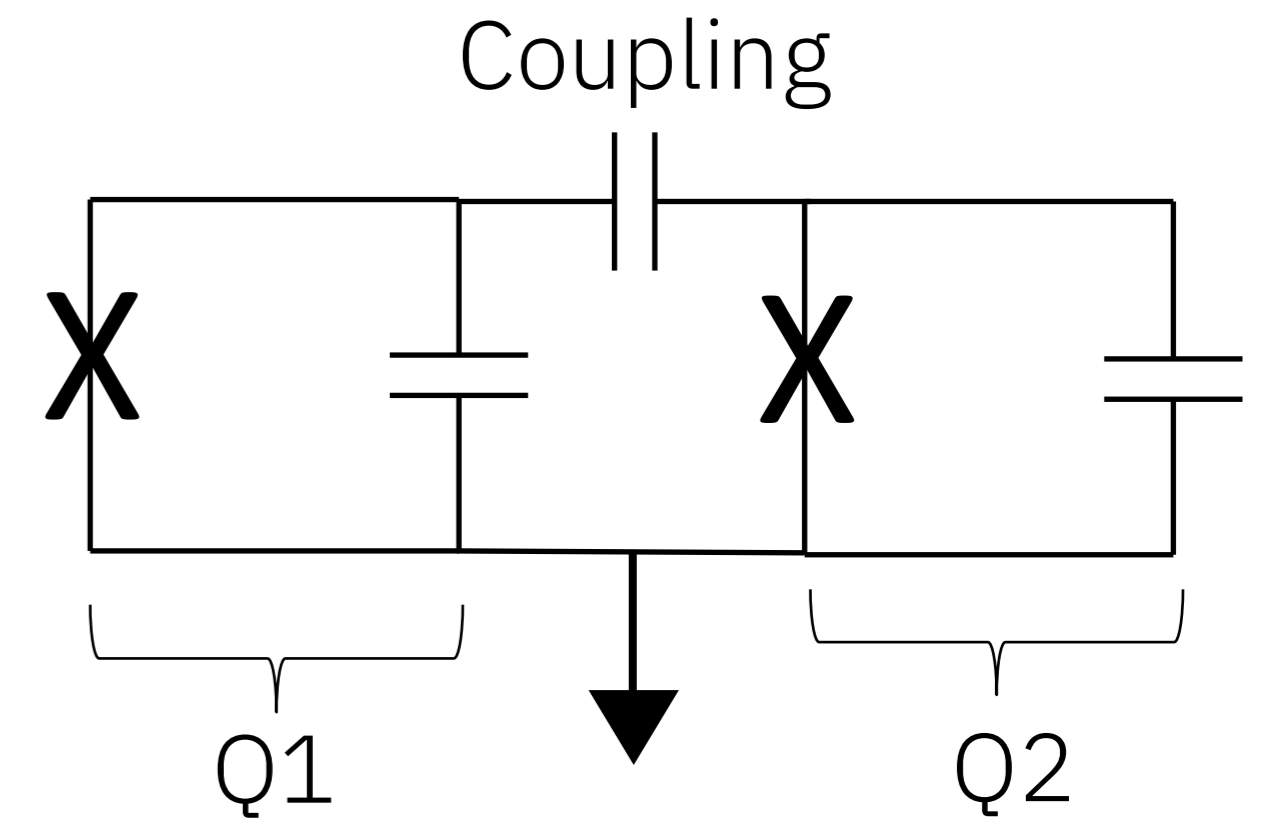
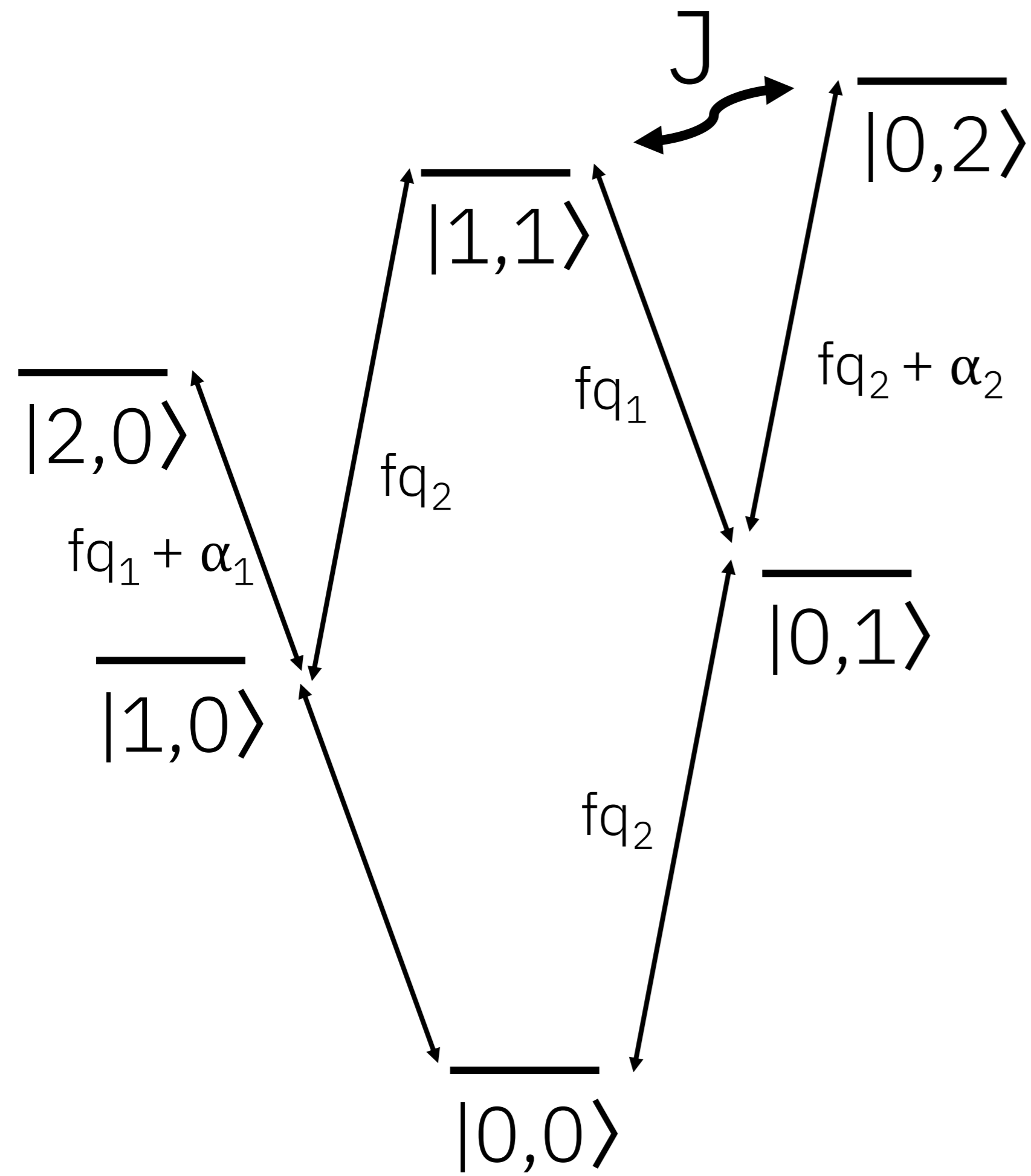


Two qubit gates: idle ZZ



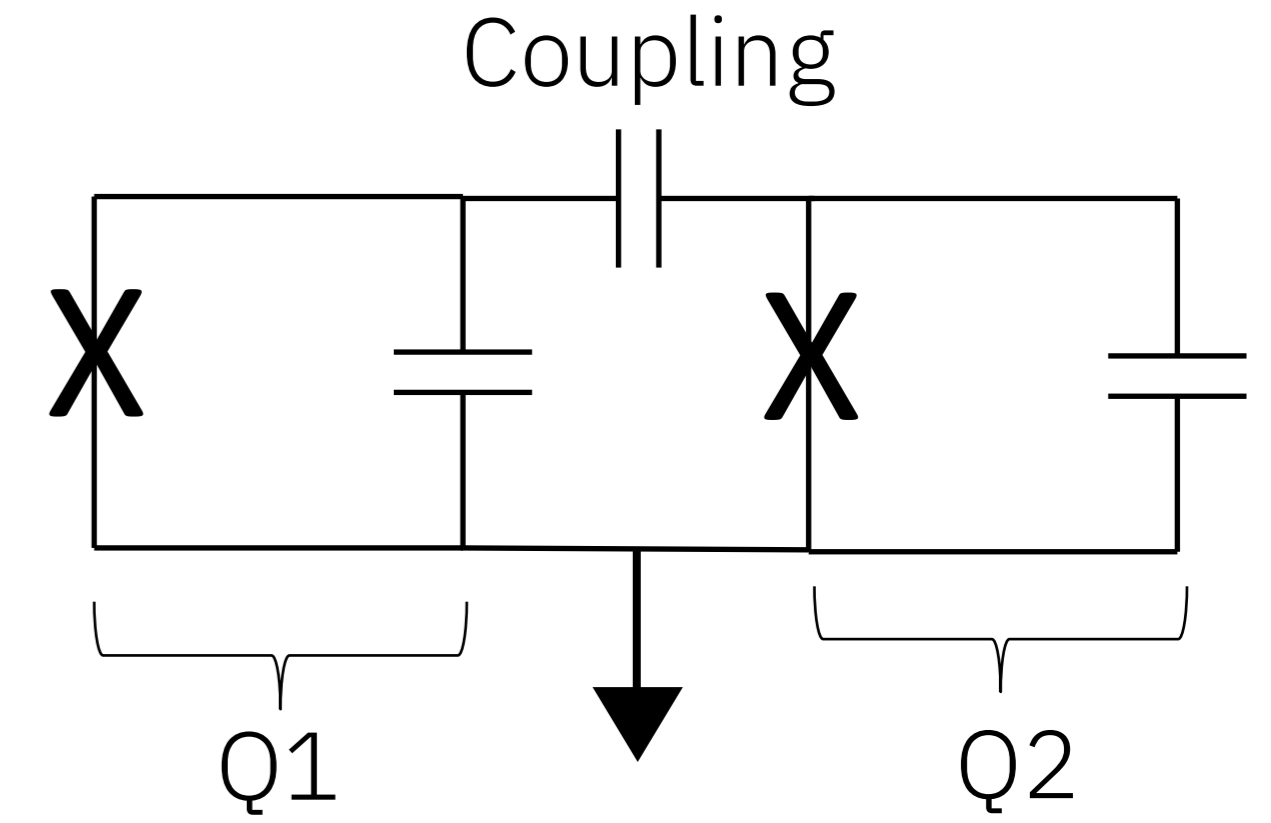
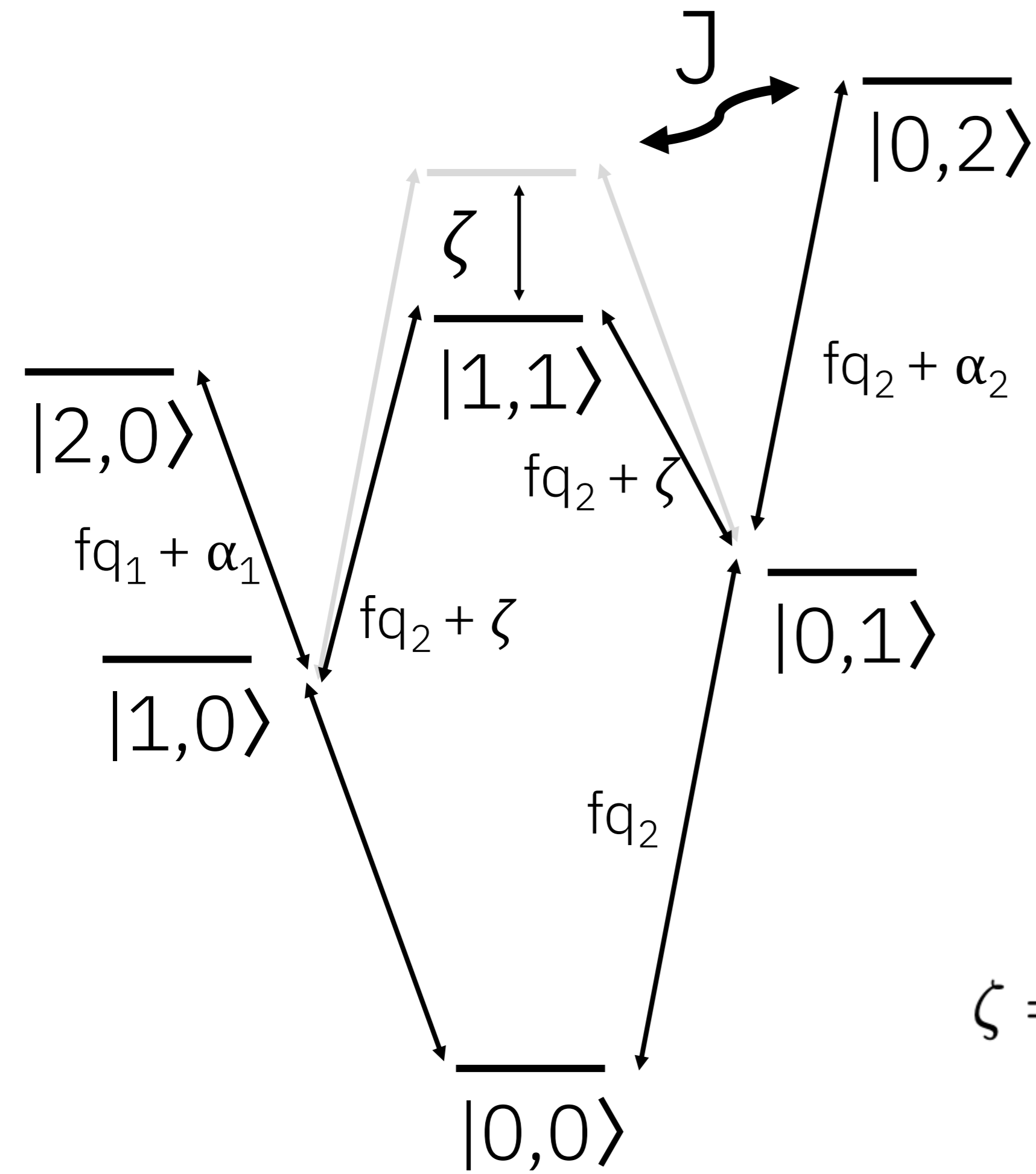
$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

Two qubit gates: idle ZZ



$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

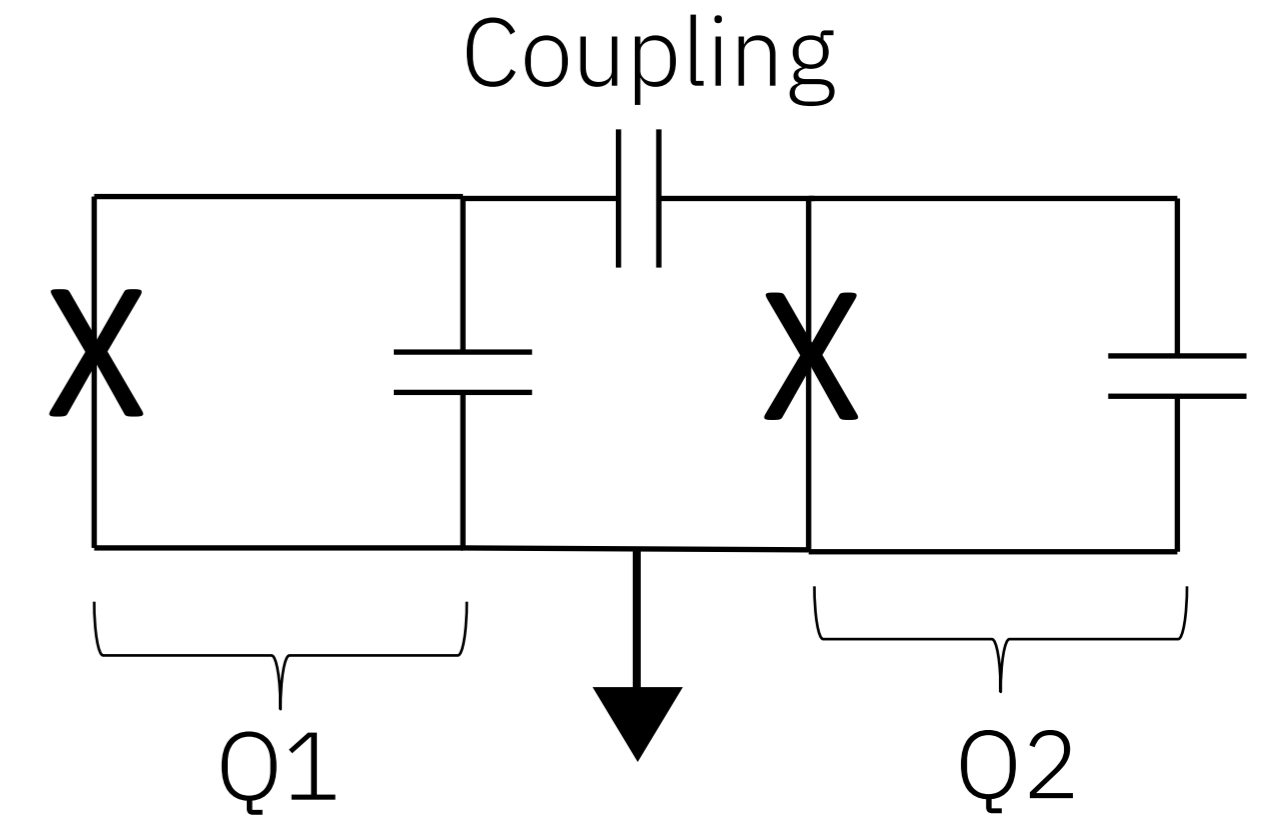
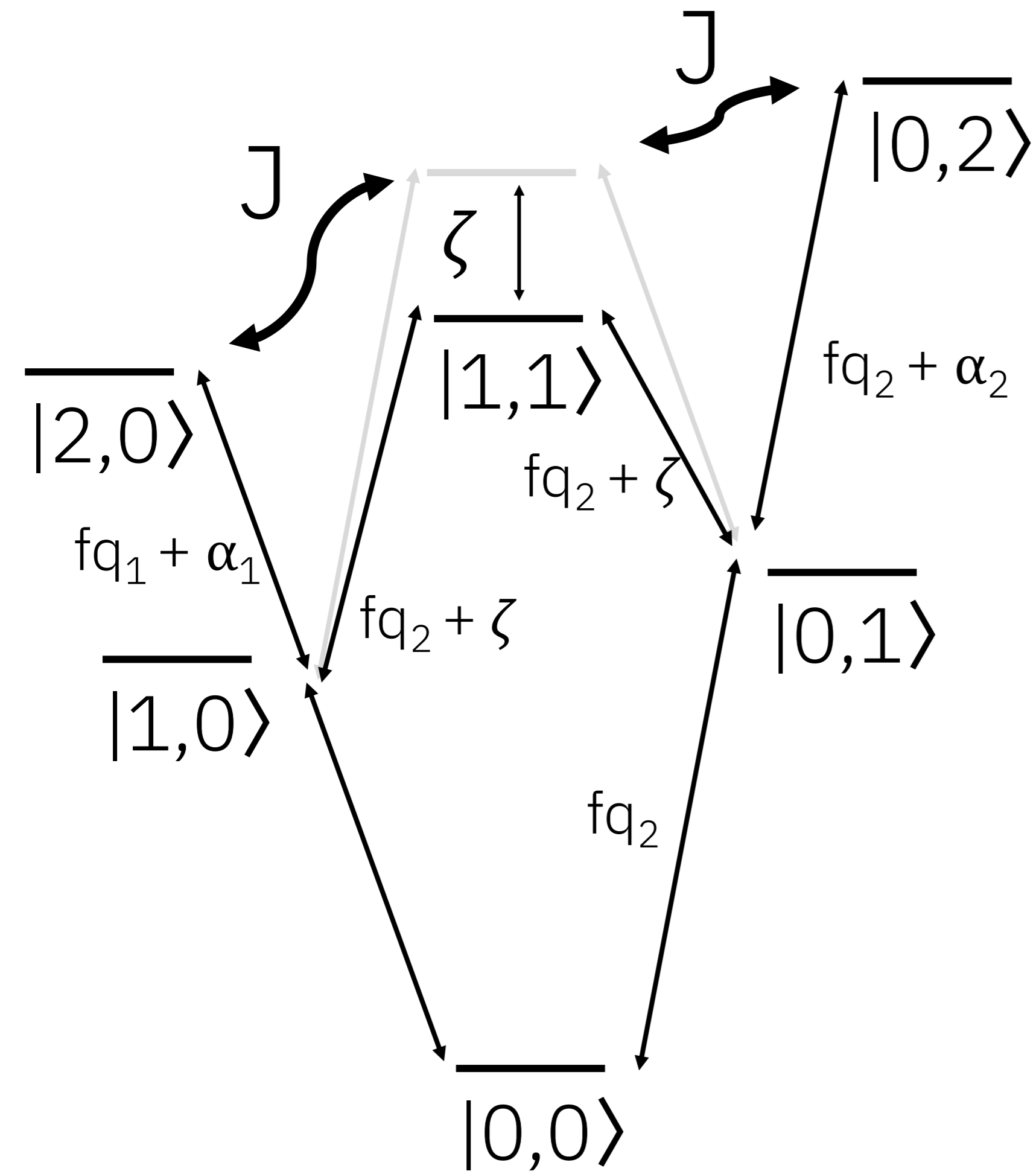
Two qubit gates: idle ZZ



Two qubit gates: idle ZZ

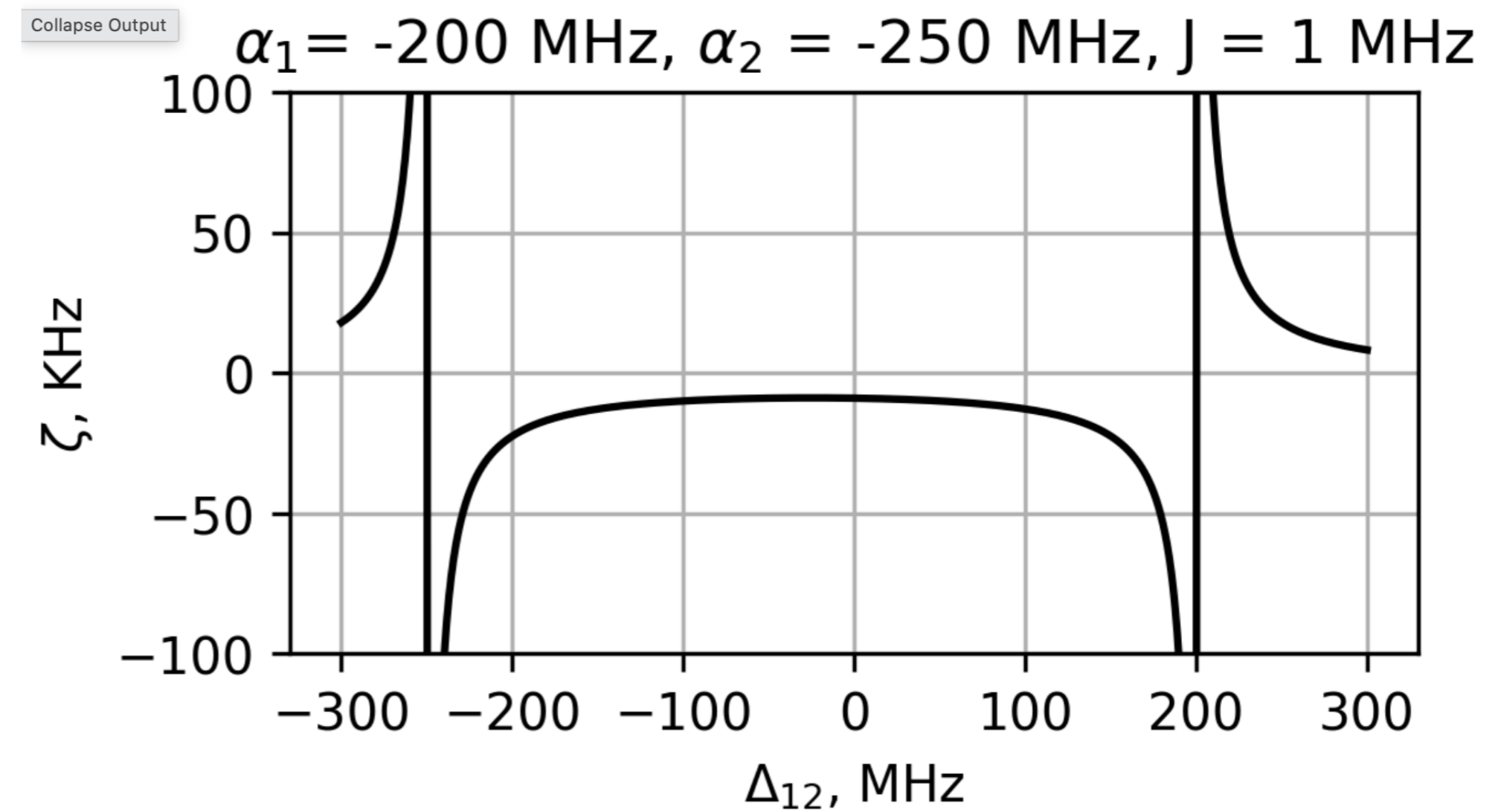
$$\zeta = \frac{|\langle 0, 2 | H_{couple} | 1, 1 \rangle|^2}{E_{11} - E_{02}} = \frac{J^2}{\omega_1 + \omega_2 - 2\omega_2 - E_{c,b}} \equiv \frac{J^2}{\Delta_{12} - \alpha_2}$$

Two qubit gates: idle ZZ

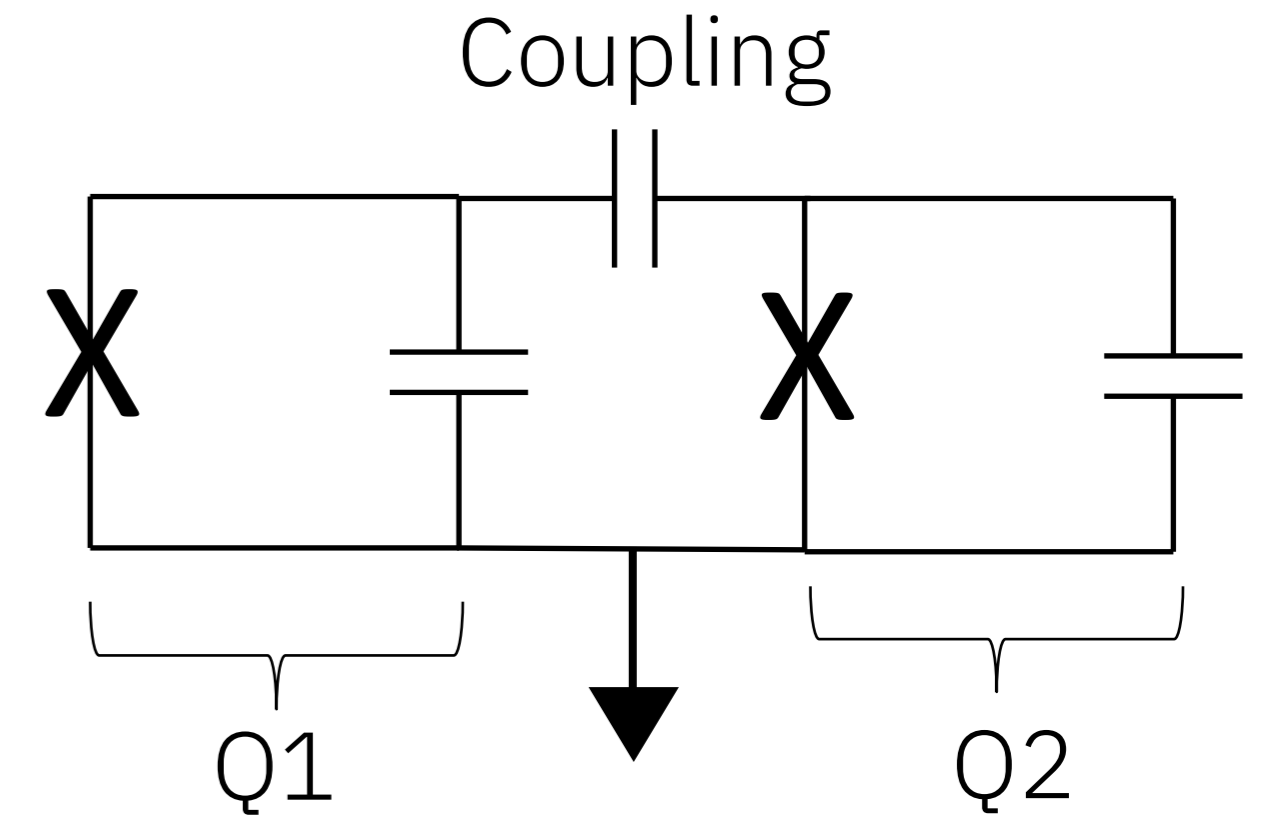
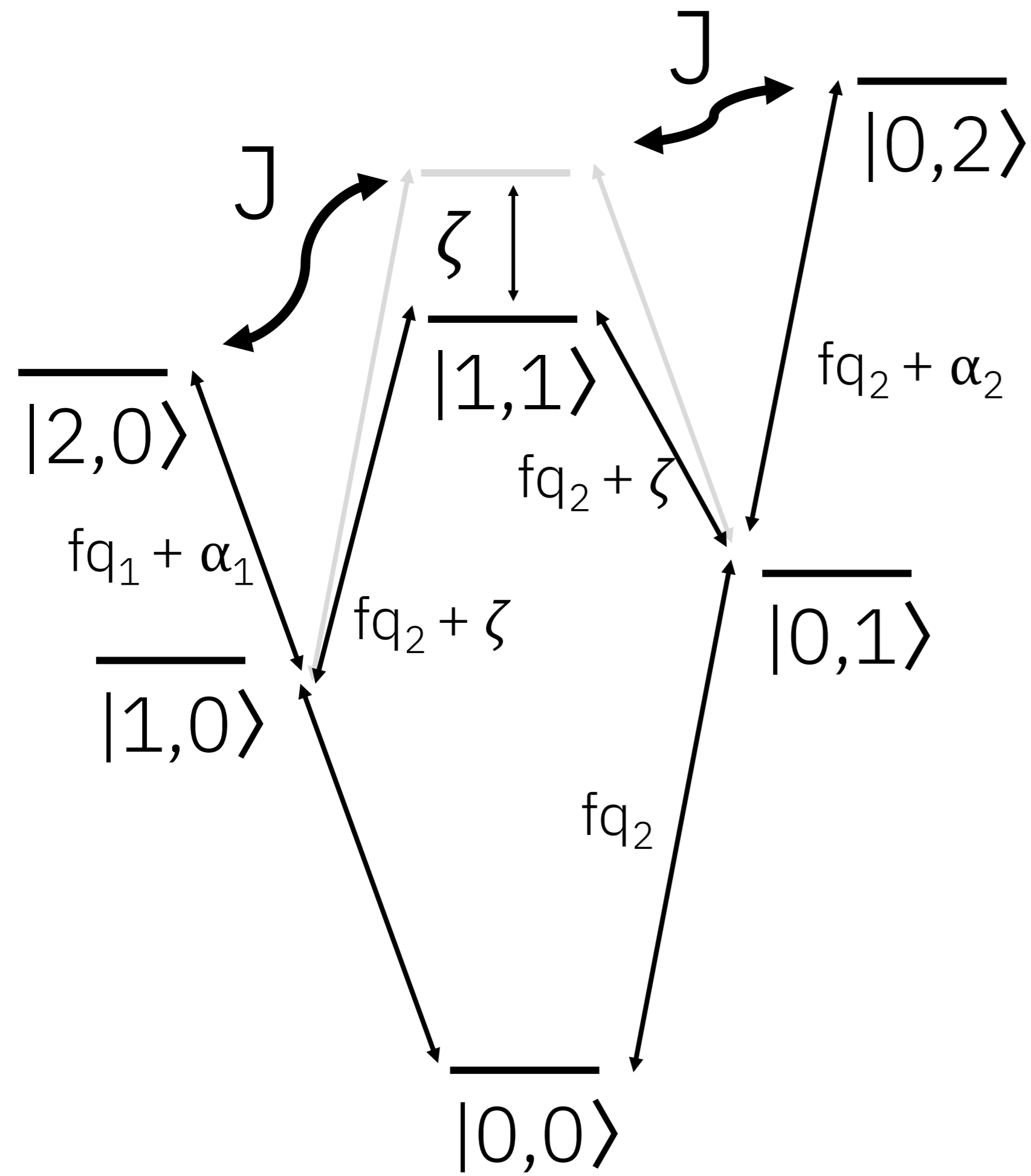


$$\zeta = \frac{J^2}{\Delta_{12} - \alpha_2} + \frac{J^2}{-\Delta_{12} - \alpha_1} = \frac{J^2 (\alpha_1 + \alpha_2)}{(\alpha_2 - \Delta_{12})(\alpha_1 + \Delta_{12})}$$

Two qubit gates: idle ZZ



Two qubit gates: idle ZZ



$$H = (\omega_1 - \zeta/2) [\hat{\sigma}_z \otimes \hat{I}] + (\omega_2 - \zeta/2) [\hat{I} \otimes \hat{\sigma}_z] + \frac{\zeta}{2} [\hat{\sigma}_z \otimes \hat{\sigma}_z]$$

$$H = \frac{\zeta}{2} [\hat{\sigma}_z \otimes \hat{\sigma}_z] \text{ co-rotating frame}$$

Two qubit gates: idle ZZ

$$H = \frac{\zeta}{2} [\hat{\sigma}_z \otimes \hat{\sigma}_z] \text{ co-rotating frame}$$

$$e^{-iHt} = \begin{bmatrix} e^{-i\zeta t/2} & 0 & 0 & 0 \\ 0 & e^{i\zeta t/2} & 0 & 0 \\ 0 & 0 & e^{i\zeta t/2} & 0 \\ 0 & 0 & 0 & e^{-i\zeta t/2} \end{bmatrix}$$

$$\text{at } t = \frac{\theta}{2\zeta}$$

$$e^{-i\frac{\theta H}{2\zeta}} = \begin{bmatrix} e^{-i\theta/2} & 0 & 0 & 0 \\ 0 & e^{i\theta/2} & 0 & 0 \\ 0 & 0 & e^{i\theta/2} & 0 \\ 0 & 0 & 0 & e^{-i\theta/2} \end{bmatrix} \equiv R_{zz}(\theta)$$

Recall: single qubit Z rotations

$$Z(\phi) \otimes I = \begin{bmatrix} e^{i\phi/2} & 0 & 0 & 0 \\ 0 & e^{i\phi/2} & 0 & 0 \\ 0 & 0 & e^{-i\phi/2} & 0 \\ 0 & 0 & 0 & e^{-i\phi/2} \end{bmatrix}$$

$$I \otimes Z(\gamma) = \begin{bmatrix} e^{i\gamma/2} & 0 & 0 & 0 \\ 0 & e^{-i\gamma/2} & 0 & 0 \\ 0 & 0 & e^{i\gamma/2} & 0 \\ 0 & 0 & 0 & e^{-i\gamma/2} \end{bmatrix}$$

This is an entangling gate!

Two qubit gates: idle ZZ

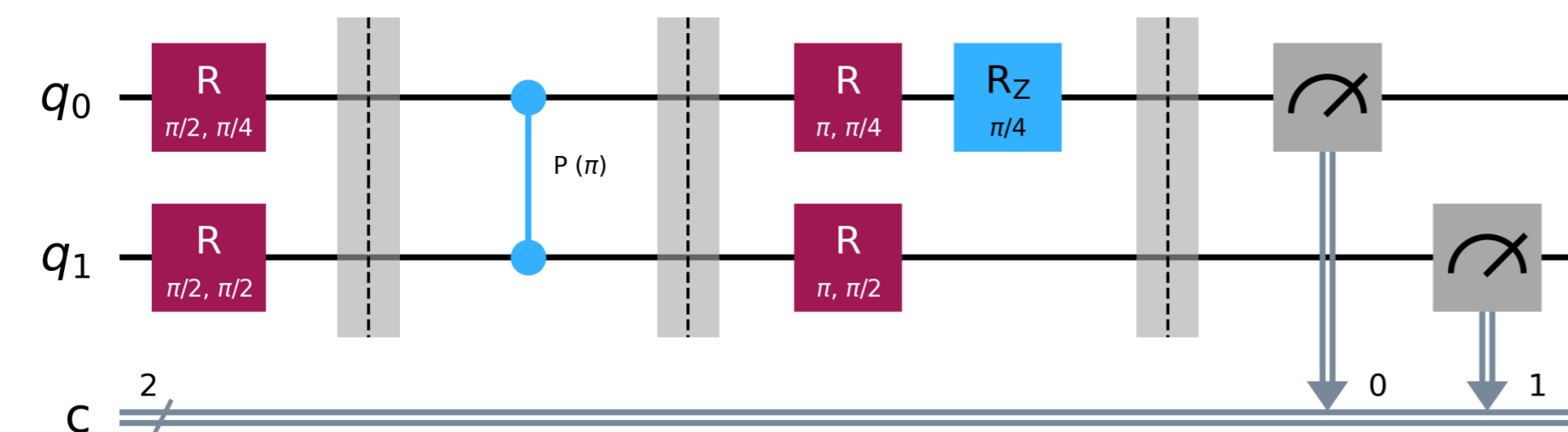
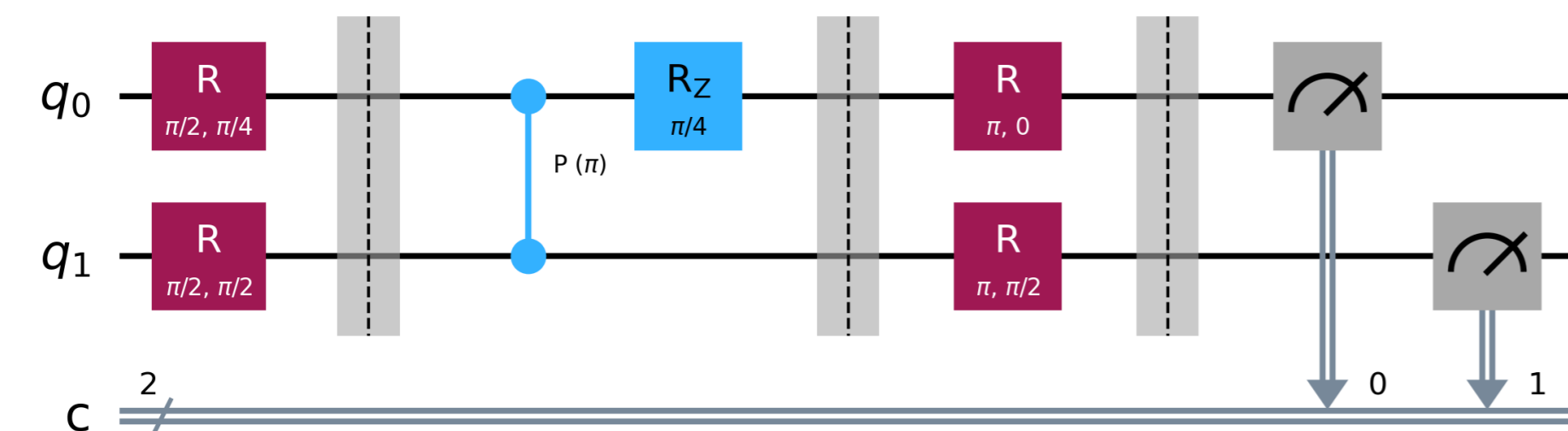
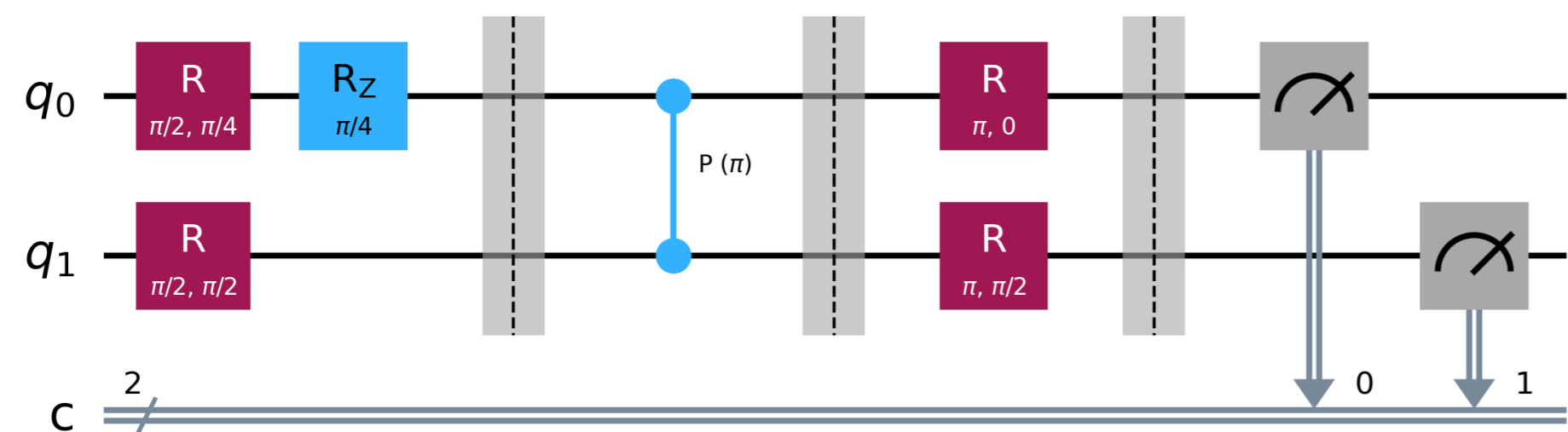
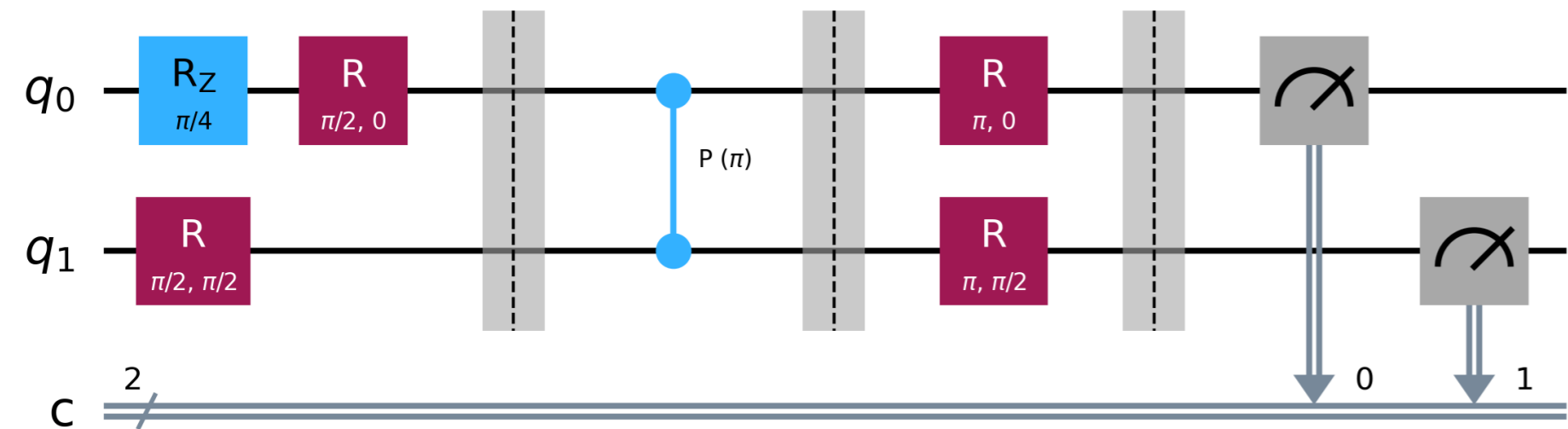
Recall: single qubit Z rotations

$$Z(\phi) \otimes I = \begin{bmatrix} e^{i\phi/2} & 0 & 0 & 0 \\ 0 & e^{i\phi/2} & 0 & 0 \\ 0 & 0 & e^{-i\phi/2} & 0 \\ 0 & 0 & 0 & e^{-i\phi/2} \end{bmatrix} \quad Z(\phi) \otimes I = \begin{bmatrix} e^{i\phi/2} & 0 & 0 & 0 \\ 0 & e^{i\phi/2} & 0 & 0 \\ 0 & 0 & e^{-i\phi/2} & 0 \\ 0 & 0 & 0 & e^{-i\phi/2} \end{bmatrix}$$

$$R_{zz}(\theta) [I \otimes Z(\gamma)] [Z(\phi) \otimes I] = \text{diag}\left(e^{i(\theta+\phi+\gamma)}, e^{i(-\theta+\phi-\gamma)}, e^{i(-\theta-\phi+\gamma)}, e^{i(\theta-\phi-\gamma)}\right)$$

With a little algebra, for $\theta = -\phi = -\gamma = \frac{\pi}{4}$ this is a CPHASE gate

Virtual z-gates



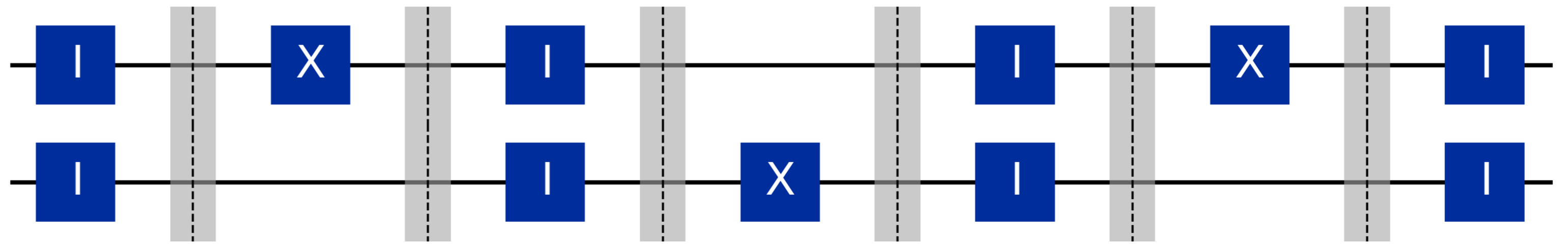
As long as the Z-gates commute with our physical basis gates, or map them to other basis gates *without spreading to other qubits*, we can apply them virtually just by modifying remaining gates in the circuit, with *constant overhead book-keeping*. This is true even real-time!

If we had, for example a two-qubit SWAP gate, this would no longer be true.

McKay et al, Phys. Rev. A **96**, 022330 (2017)

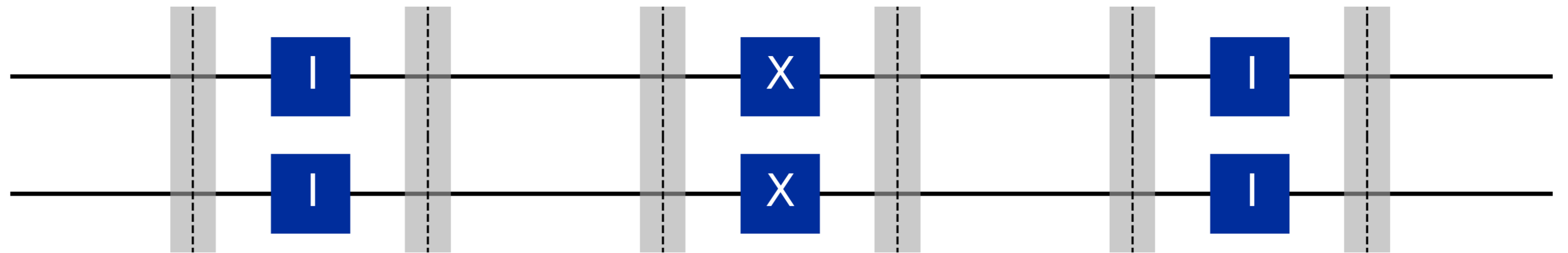
In practice...

Leaves no Z rotations

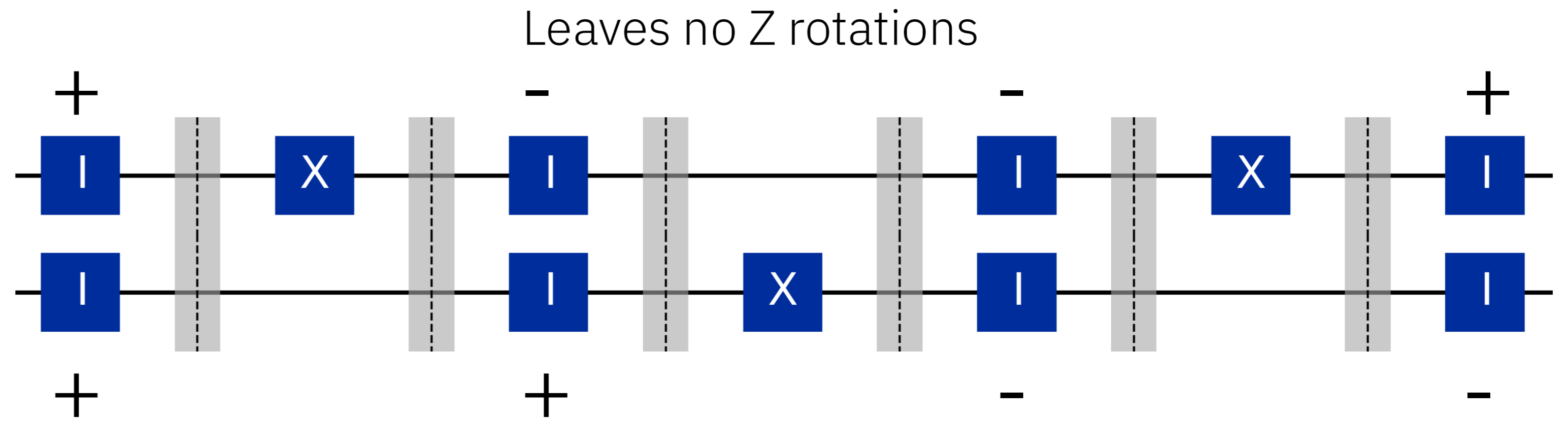


In principle, if single qubit gates are very fast compared to ζ , we can selectively turn on or off this gate with refocusing sequences

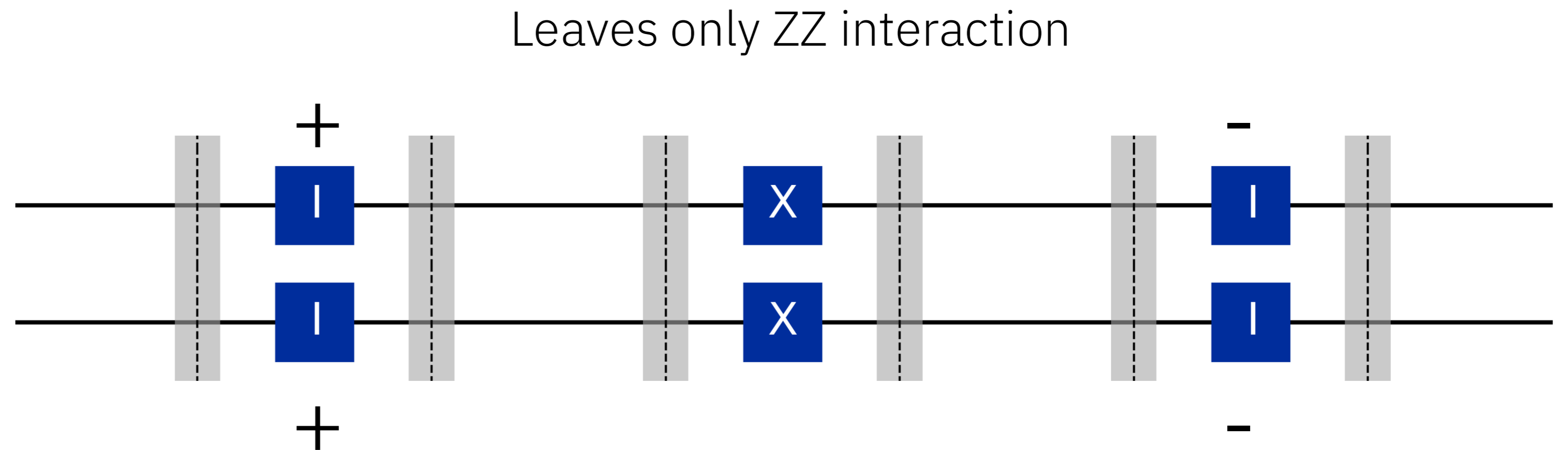
Leaves only ZZ interaction



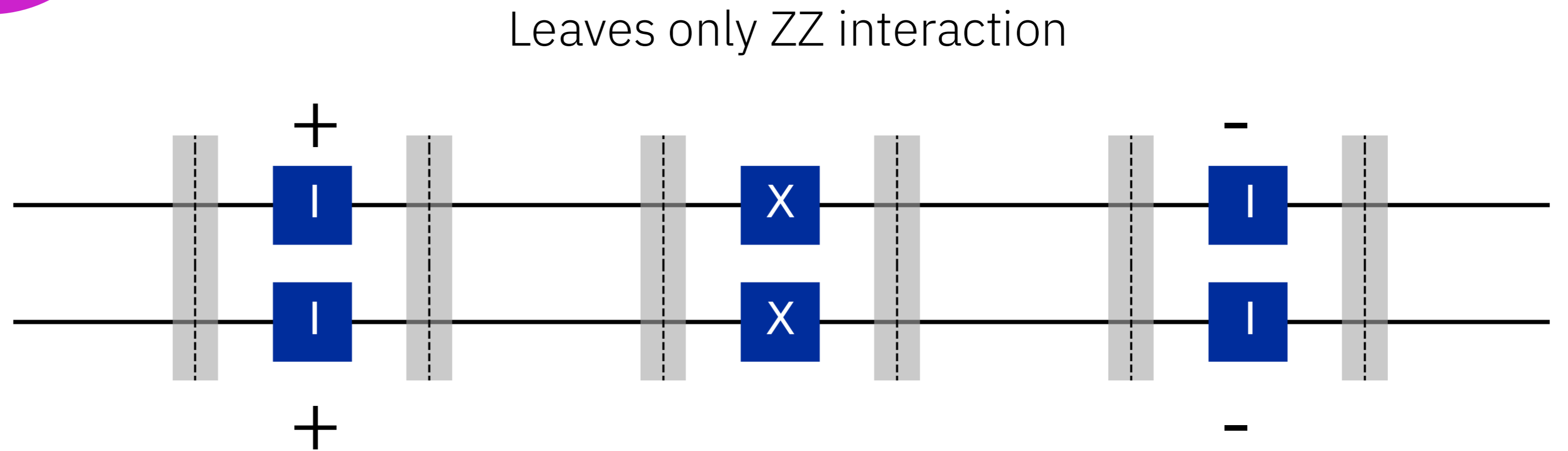
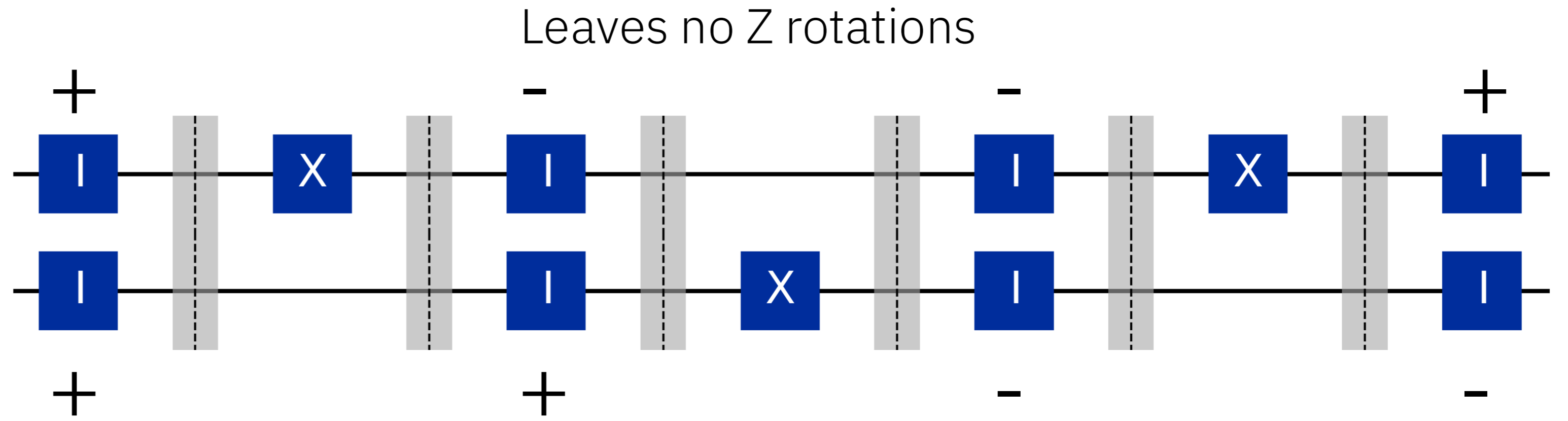
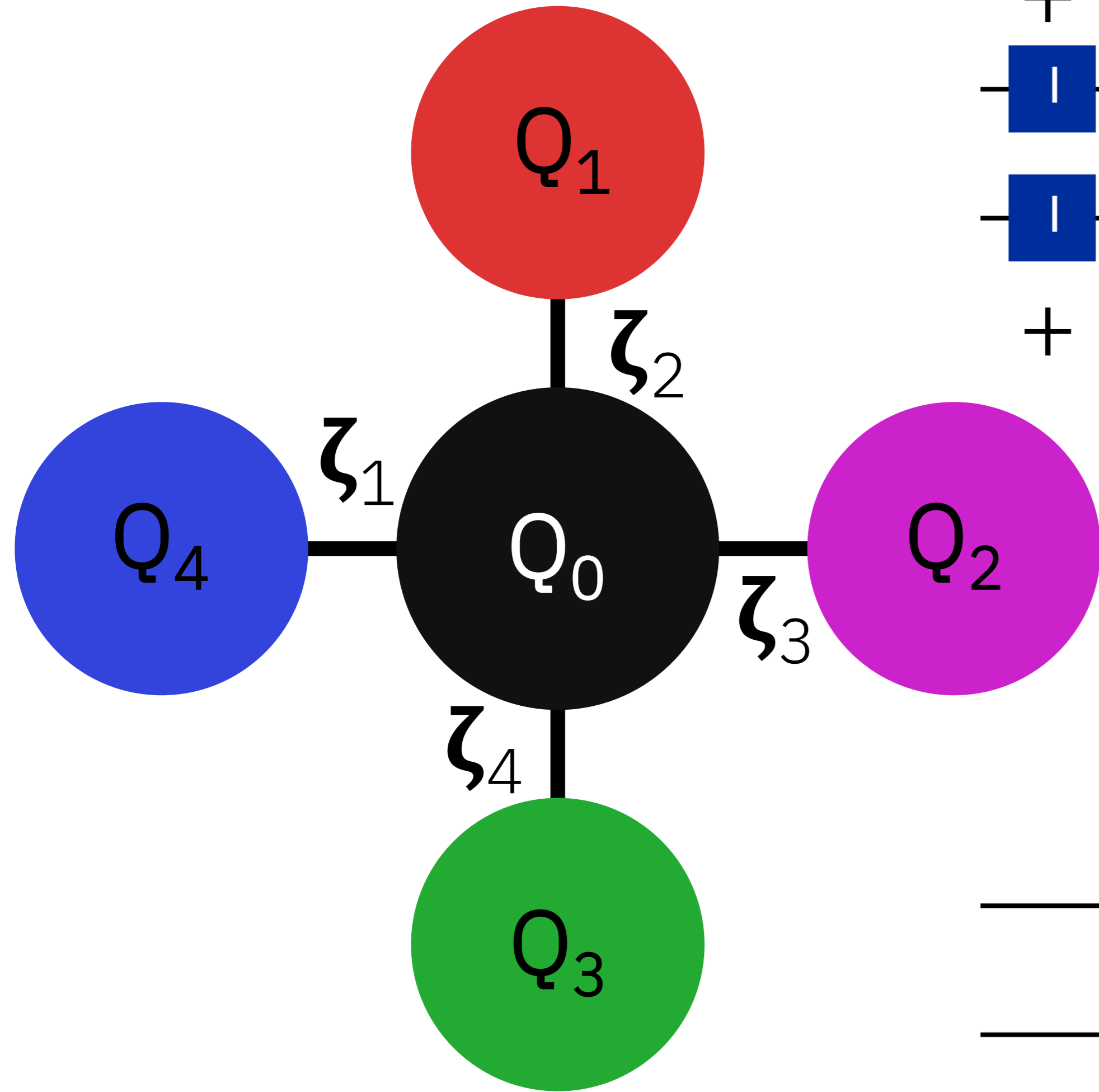
In practice...



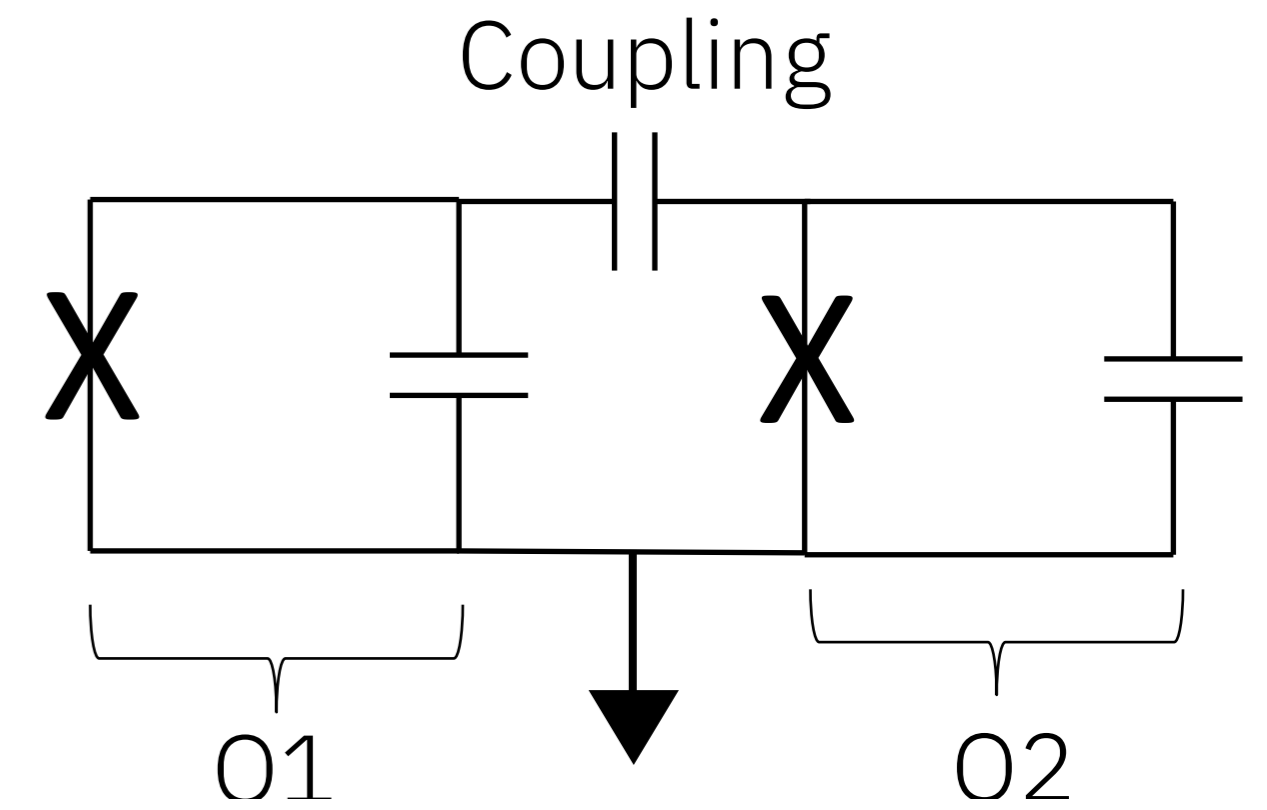
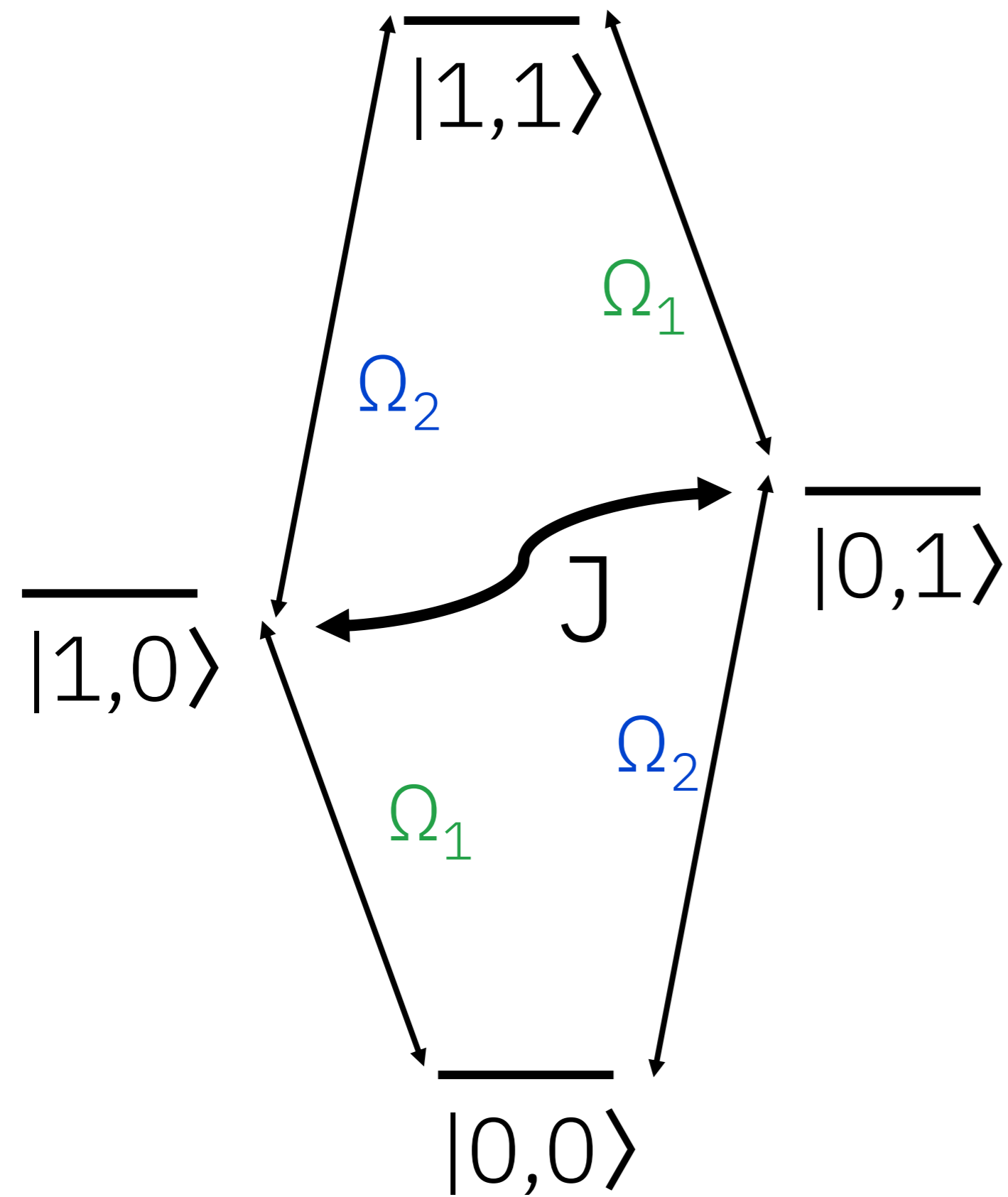
In principle, if single qubit gates are very fast compared to ζ , we can selectively turn on or off this gate with refocusing sequences



In practice...



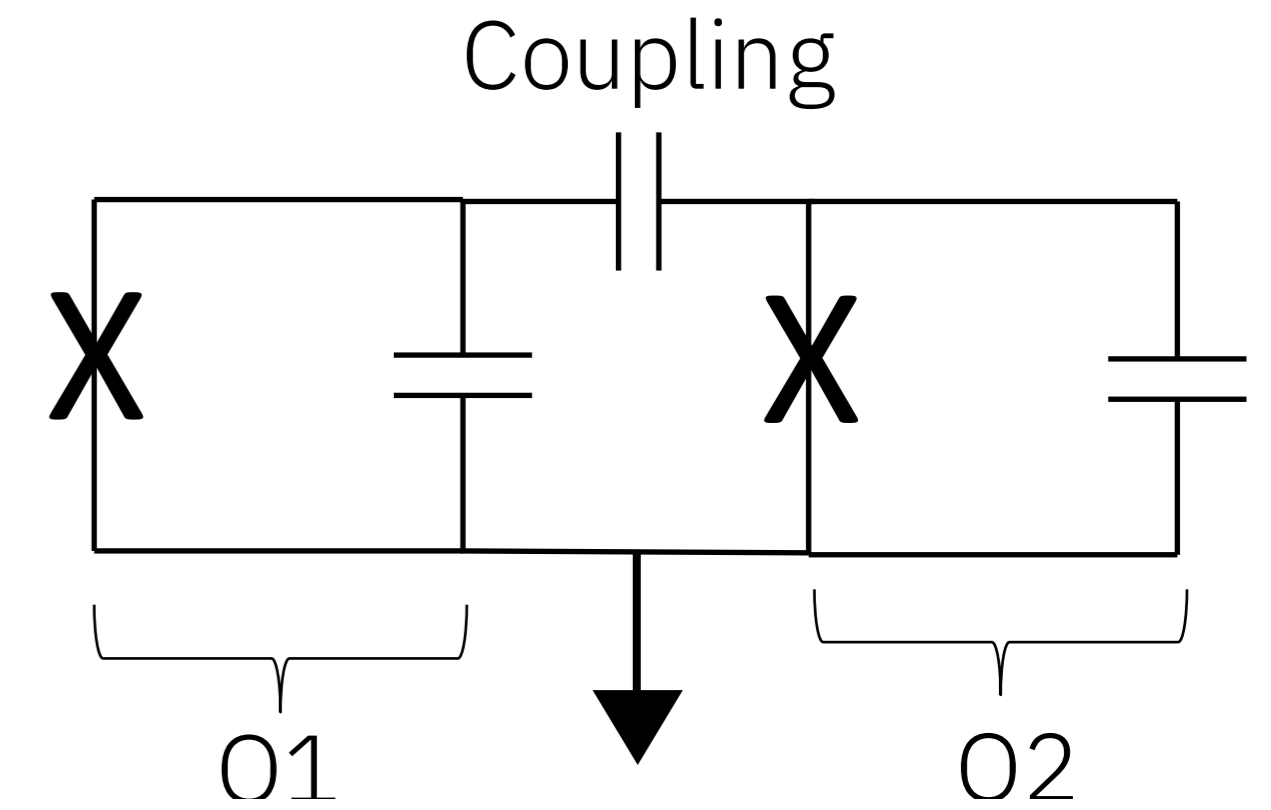
Two qubit gates: cross-resonance



$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

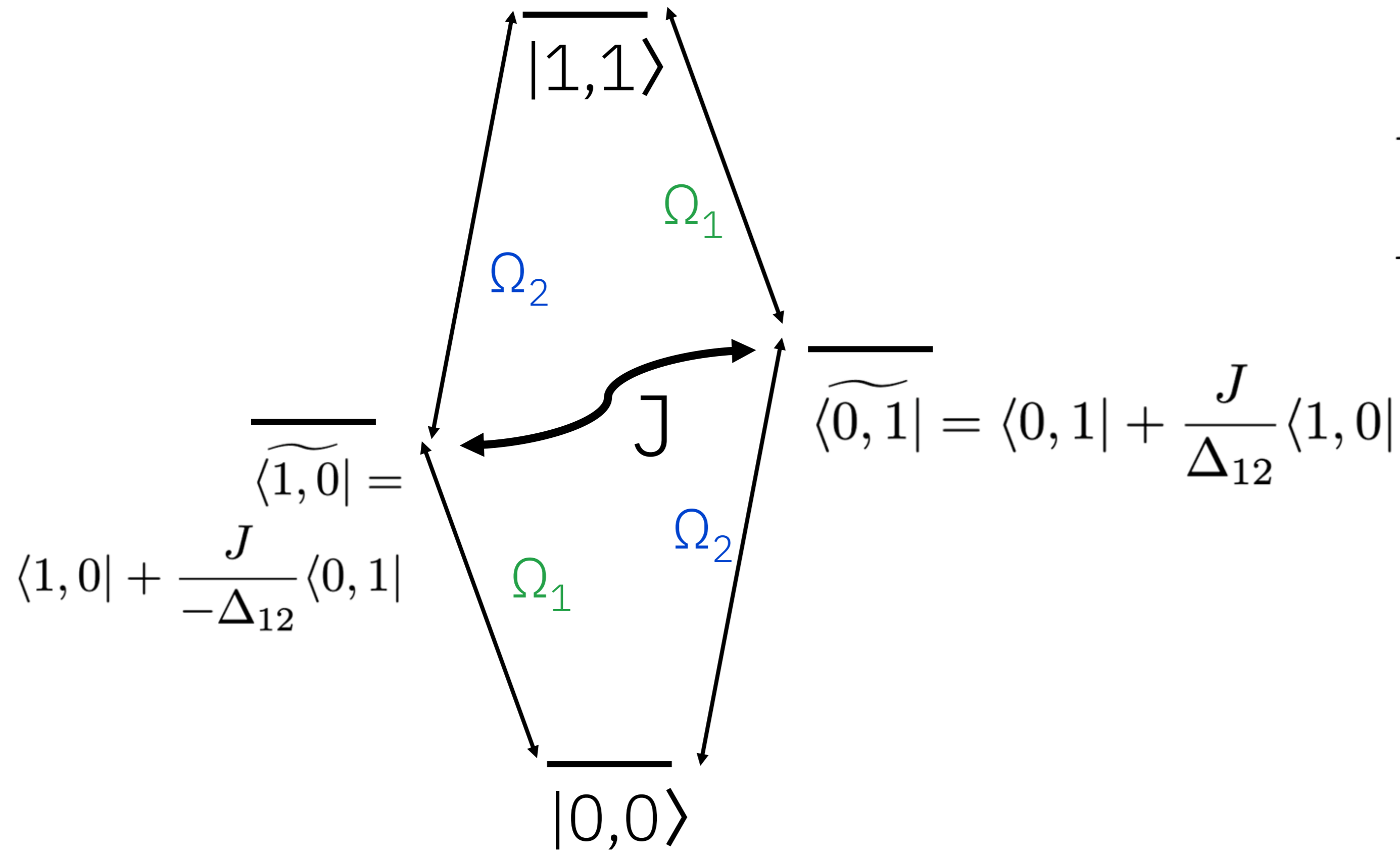
$$H_{dr} = \Omega_1(t) (\hat{a}^\dagger + \hat{a}) + \Omega_2(t) (\hat{b}^\dagger + \hat{b})$$

Two qubit gates: cross-resonance

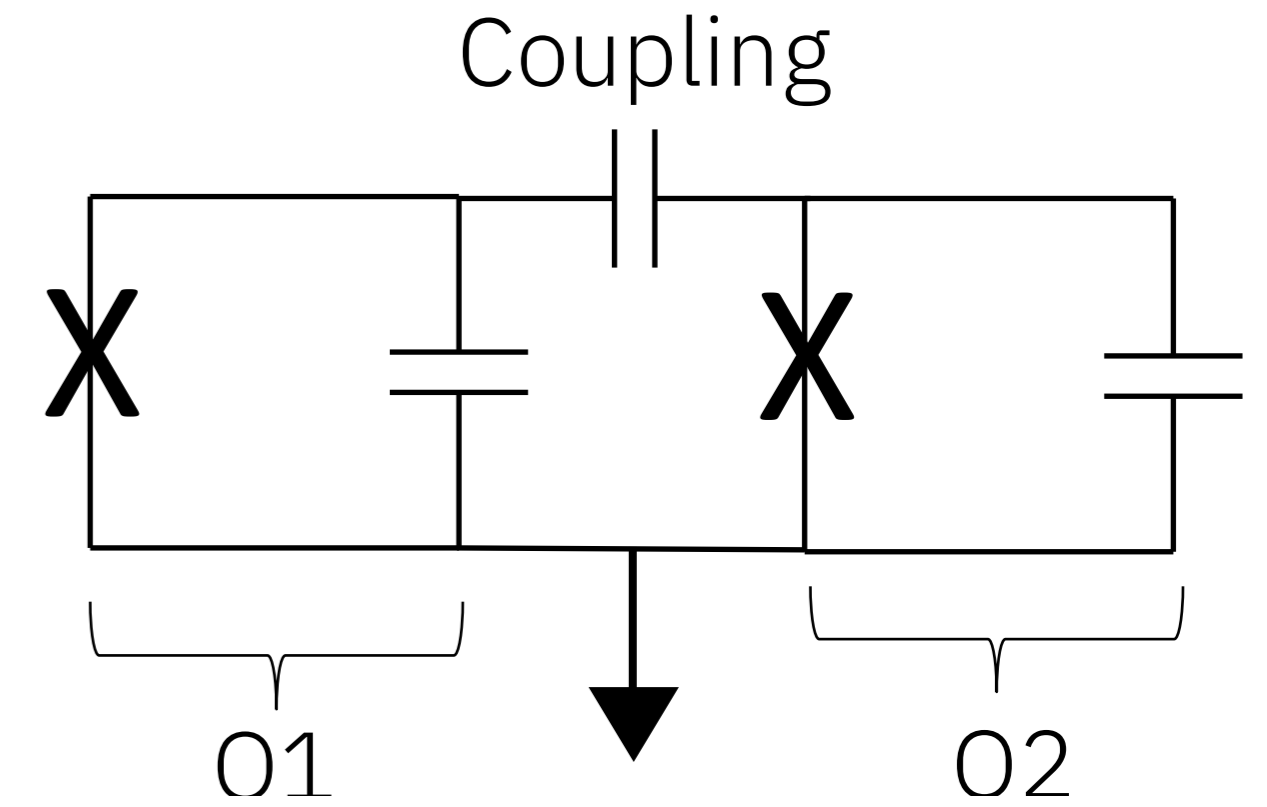


$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

$$H_{dr} = \Omega_1(t)(\hat{a}^\dagger + \hat{a}) + \Omega_2(t)(\hat{b}^\dagger + \hat{b})$$

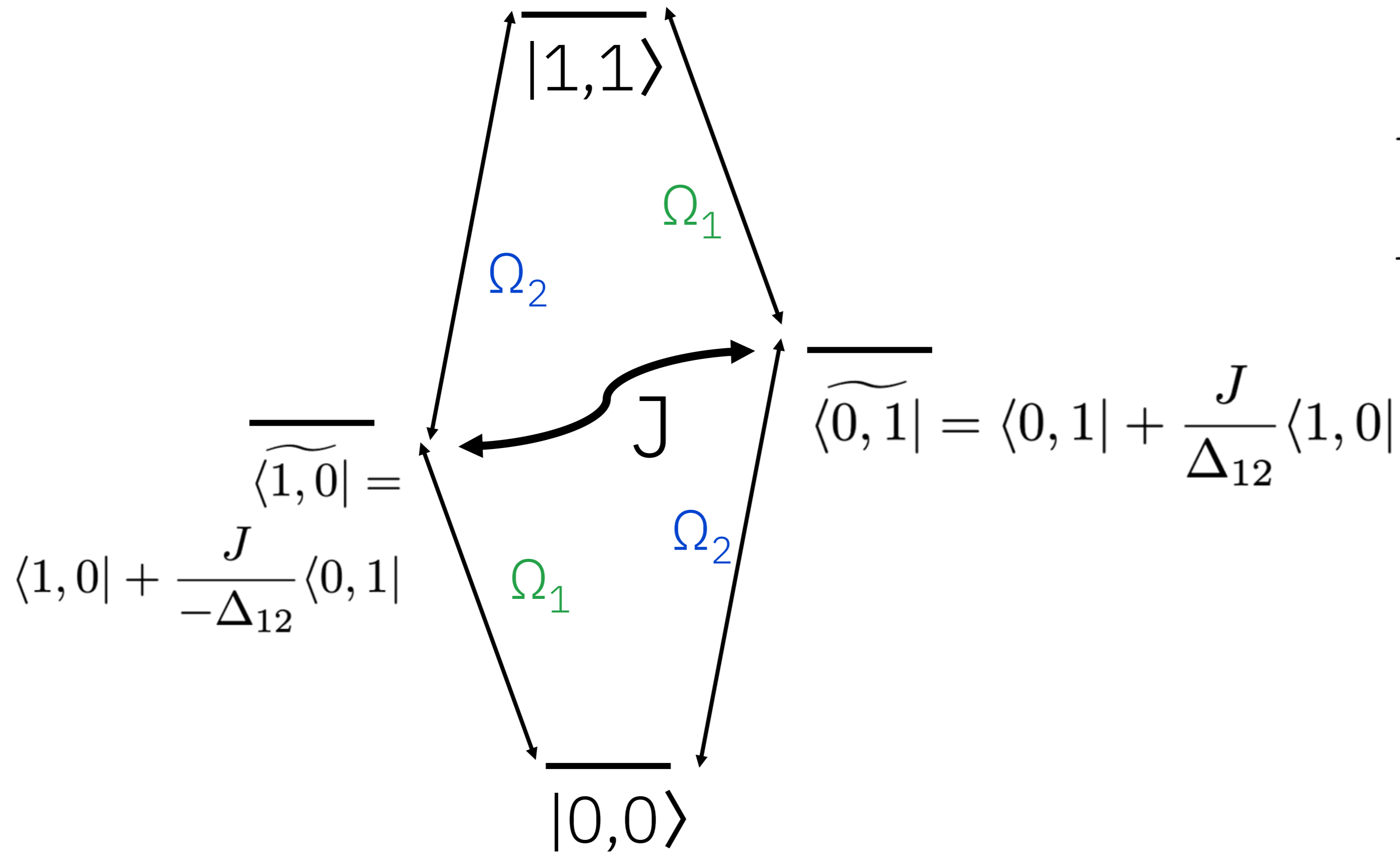


Two qubit gates: cross-resonance

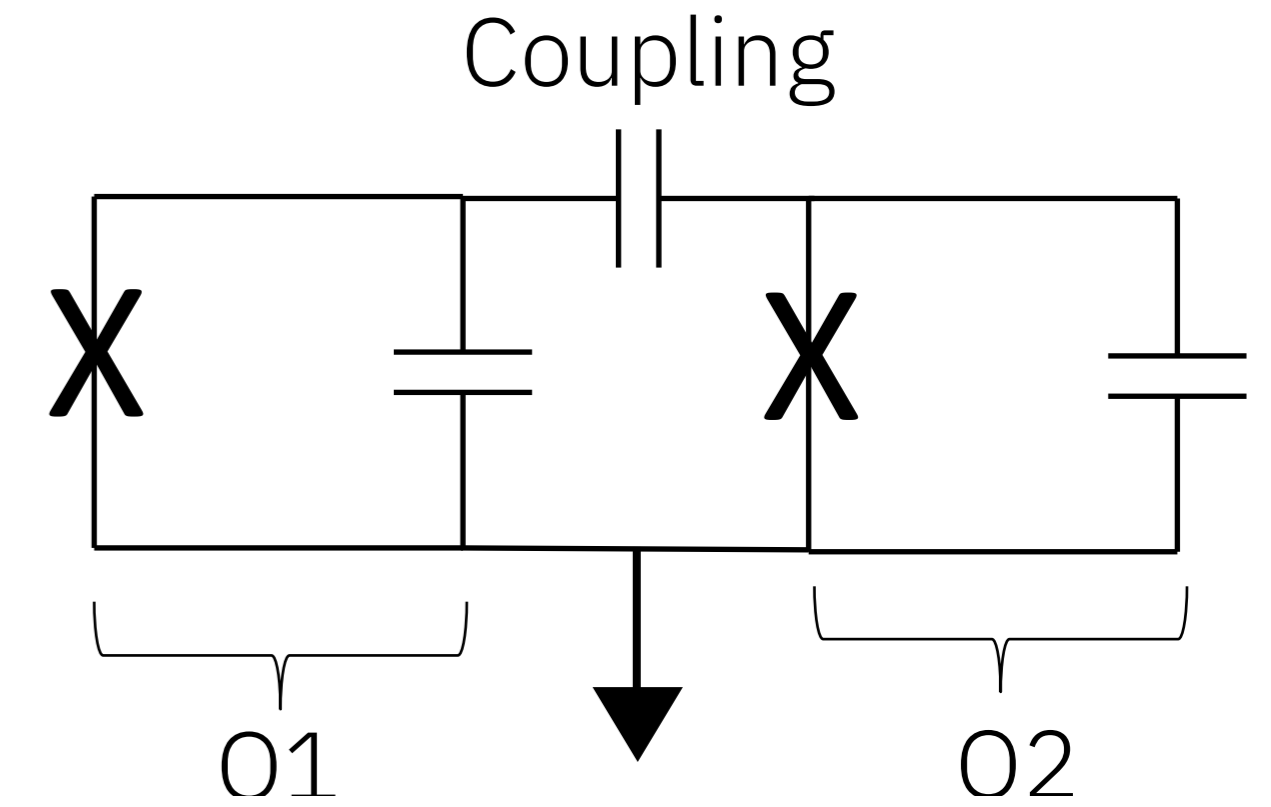


$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

$$H_{dr} = \Omega_1(t)(\hat{a}^\dagger + \hat{a}) + \Omega_2(t)(\hat{b}^\dagger + \hat{b})$$

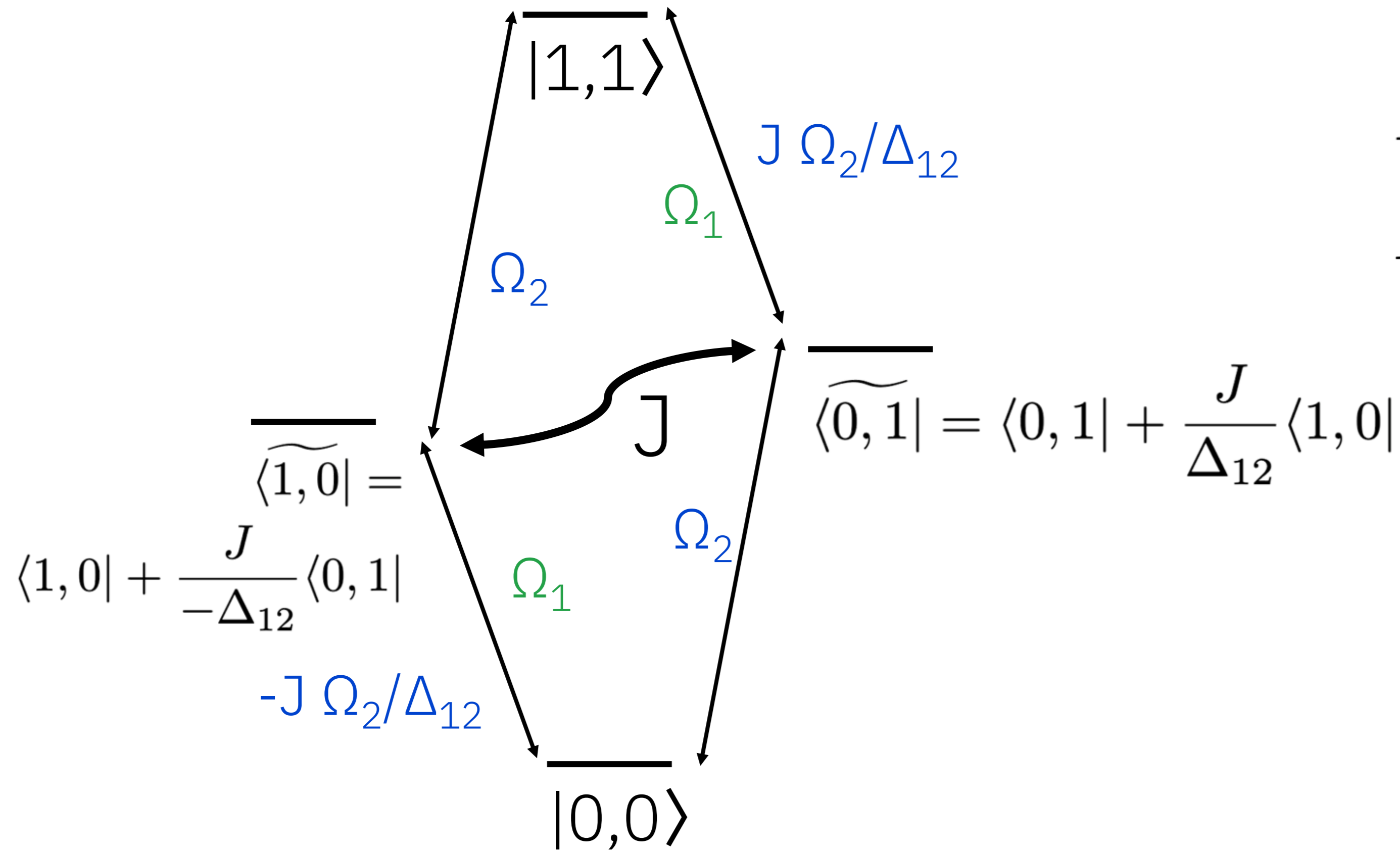


Two qubit gates: cross-resonance

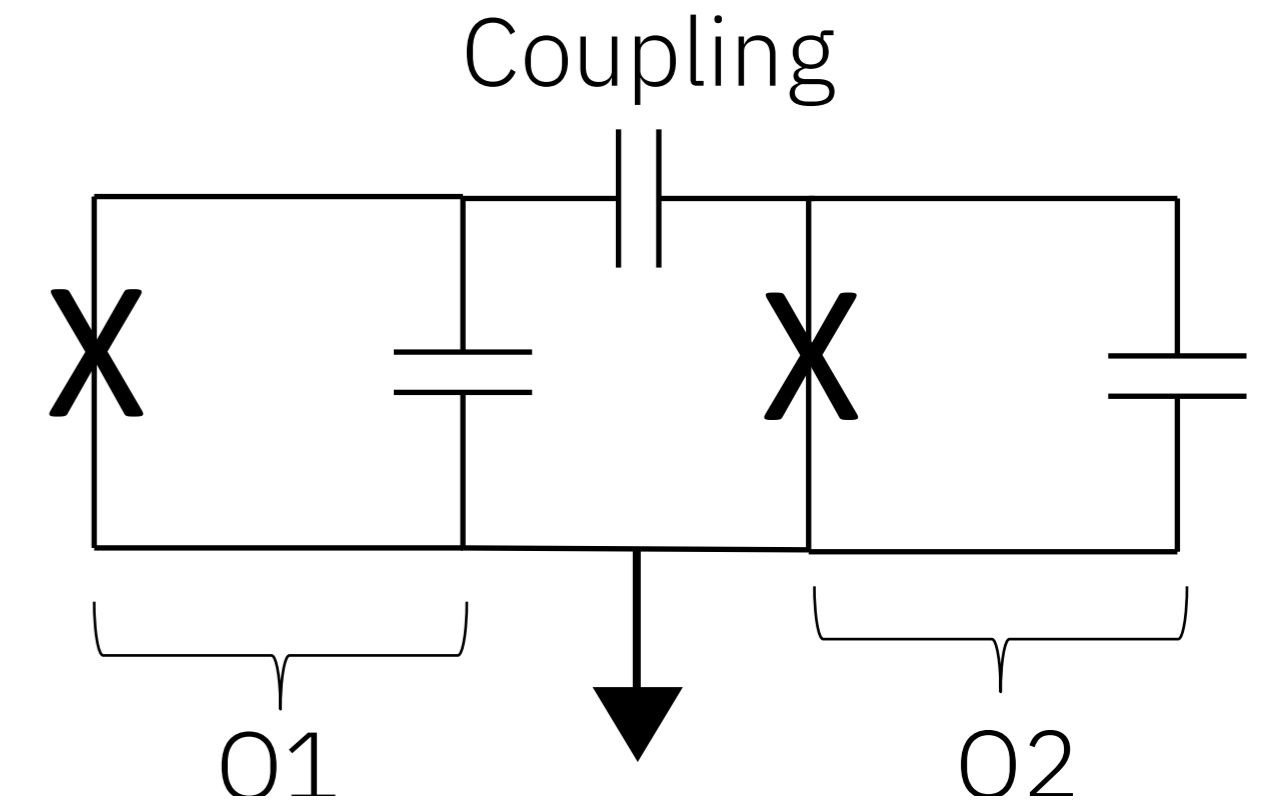


$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

$$H_{dr} = \Omega_1(t)(\hat{a}^\dagger + \hat{a}) + \Omega_2(t)(\hat{b}^\dagger + \hat{b})$$

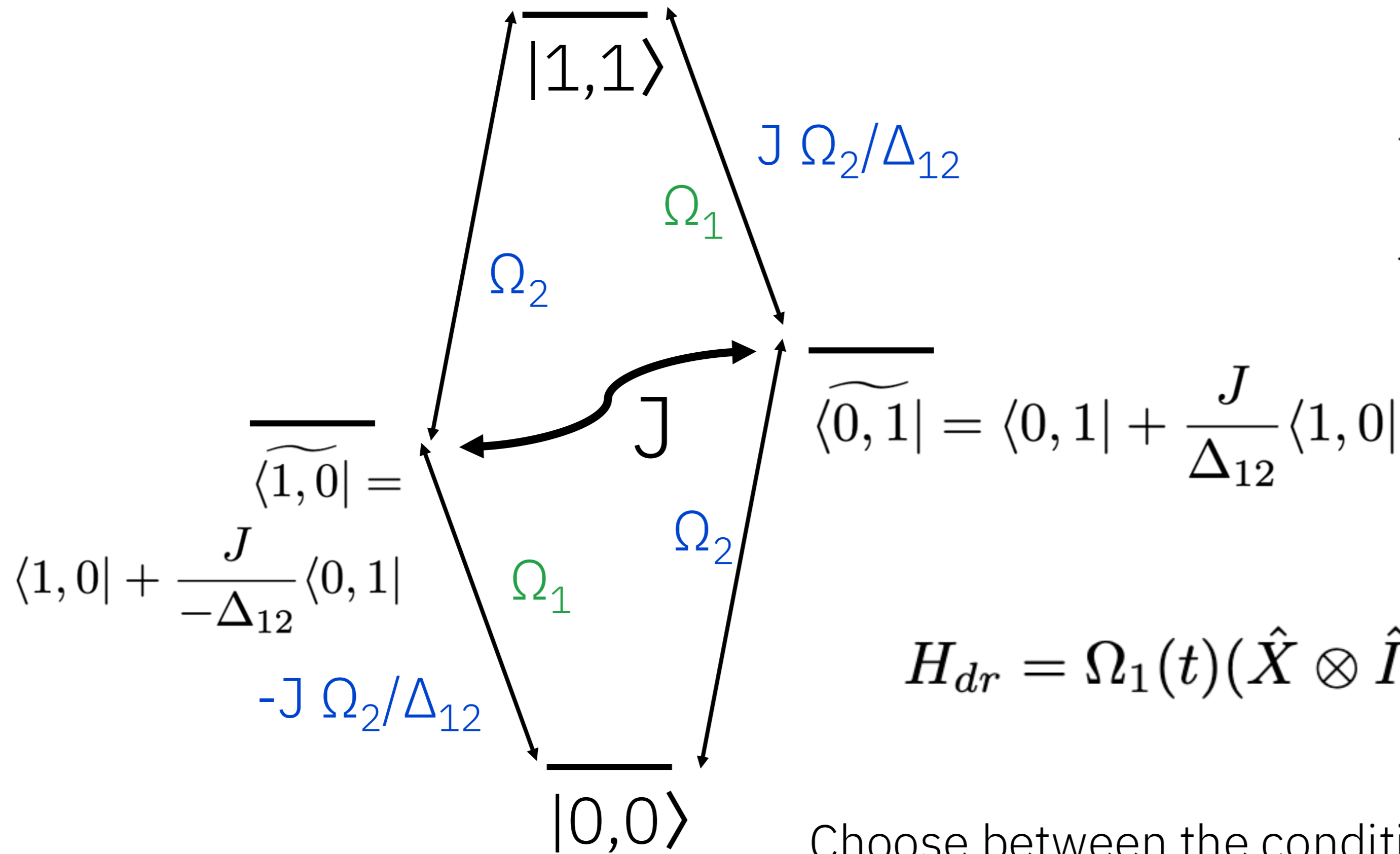


Two qubit gates: cross-resonance



$$H_{couple} = J \left(\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a} + \text{Non-RWA terms} \right)$$

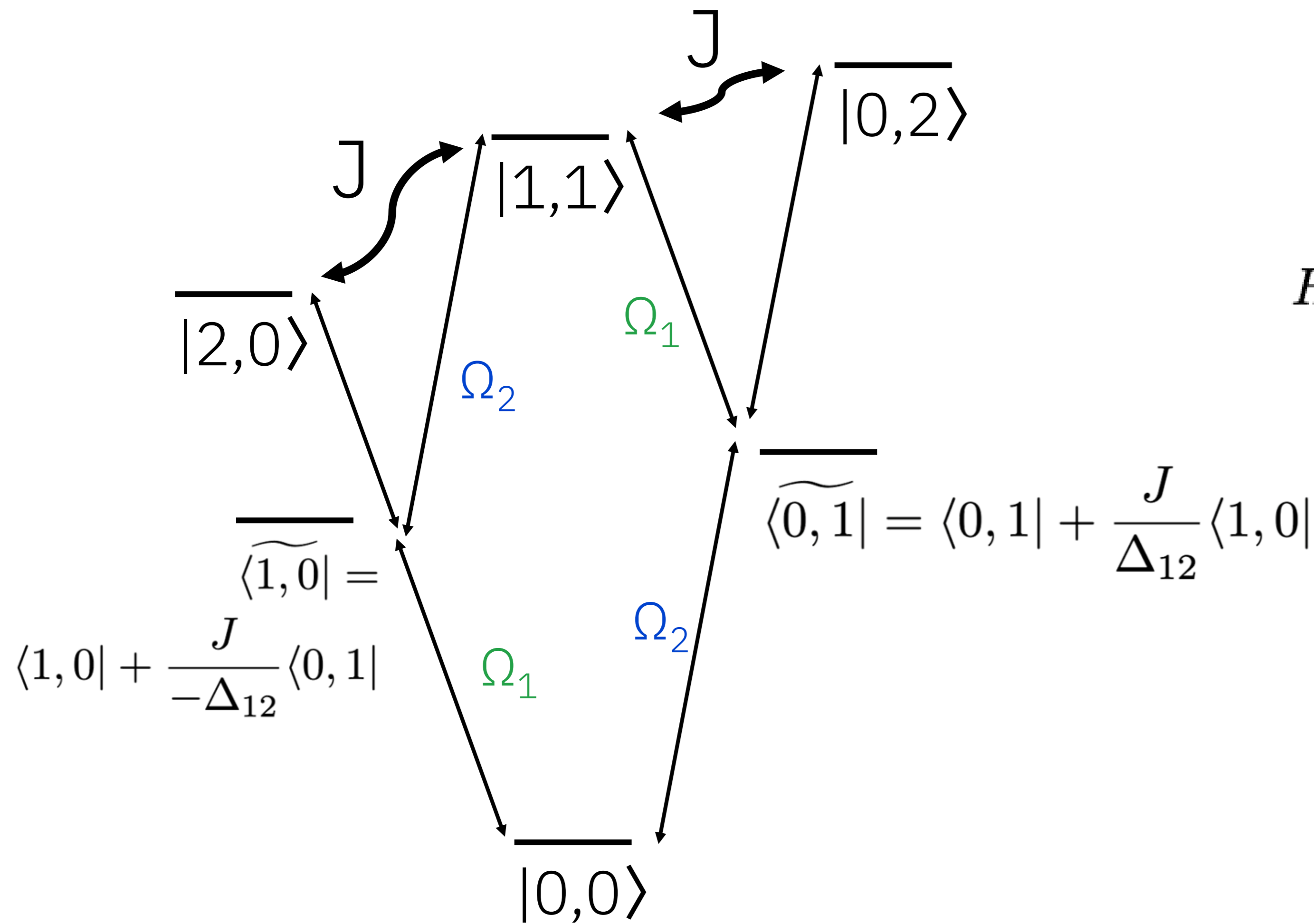
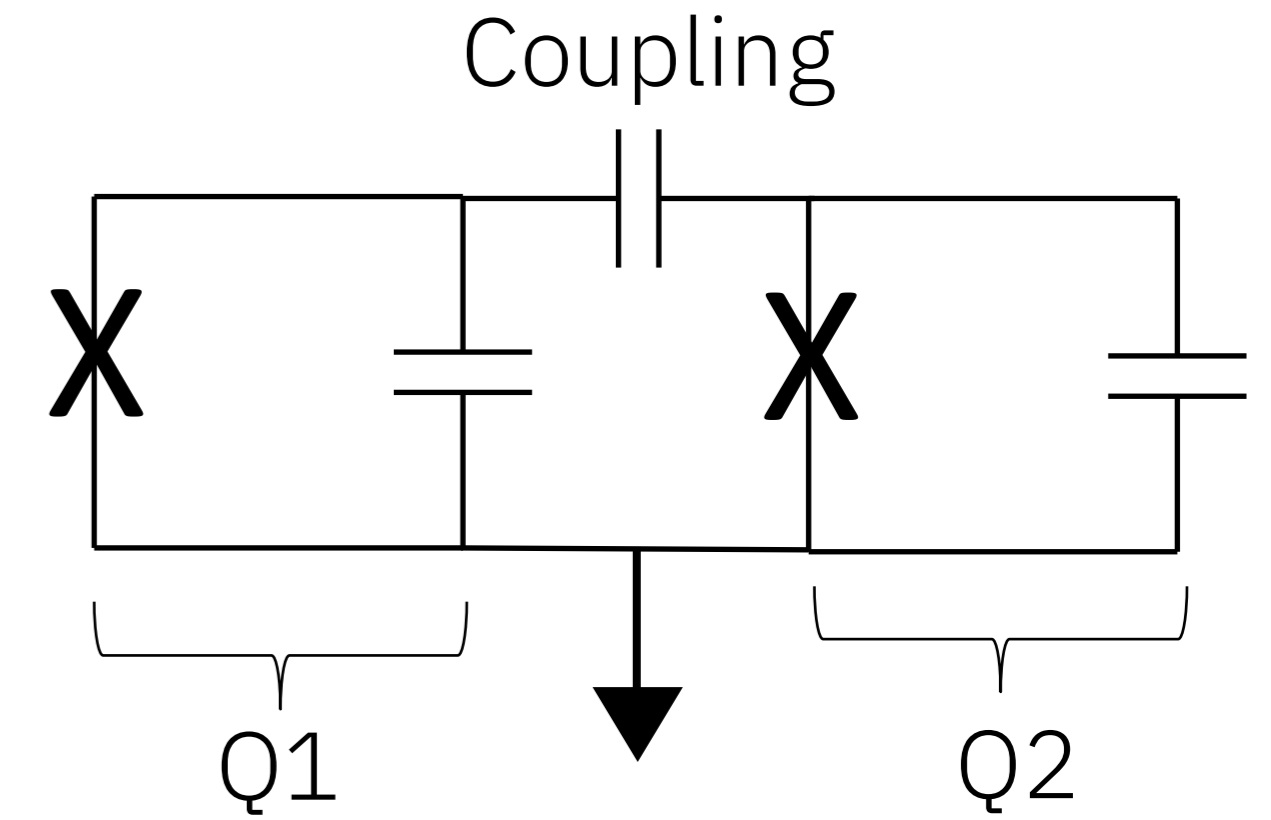
$$H_{dr} = \Omega_1(t)(\hat{a}^\dagger + \hat{a}) + \Omega_2(t)(\hat{b}^\dagger + \hat{b})$$



$$H_{dr} = \Omega_1(t)(\hat{X} \otimes \hat{I} - \frac{J}{\Delta} \hat{X} \otimes \hat{Z}) + \Omega_2(t)(\hat{I} \otimes \hat{X} + \frac{J}{\Delta} \hat{Z} \otimes \hat{X})$$

Choose between the conditional and unconditional drives with the drive frequency, provided the qubits are at different frequencies

Two qubit gates: cross-resonance



$$H_{dr} = \Omega_1(t)(\hat{X} \otimes \hat{I} - \nu_1 \hat{I} \otimes \hat{X} - \mu_1 \hat{Z} \otimes \hat{X}) + \Omega_2(t)(\hat{I} \otimes \hat{X} + \nu_2 \hat{X} \otimes \hat{I} + \mu_2 \hat{X} \otimes \hat{Z})$$

$$\nu_1 = \frac{J}{\delta_1 + \Delta_{12}} \quad \mu_1 = \frac{J\delta_1}{\Delta_{12}(\delta_1 + \Delta_{12})}$$

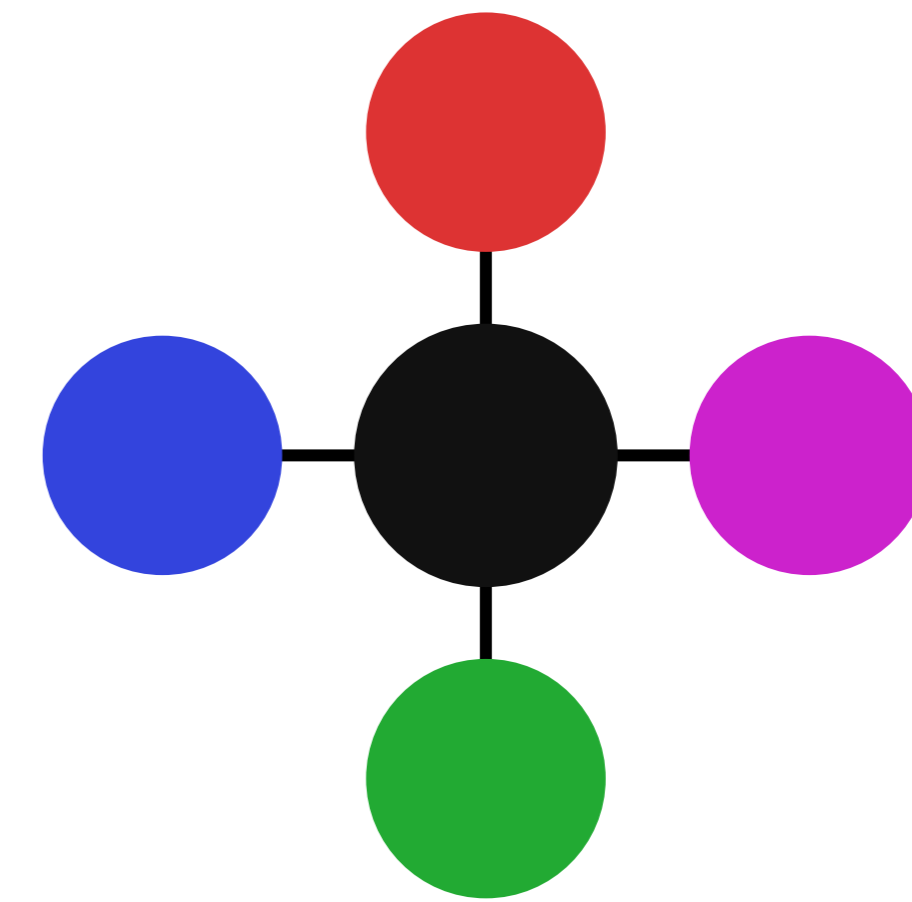
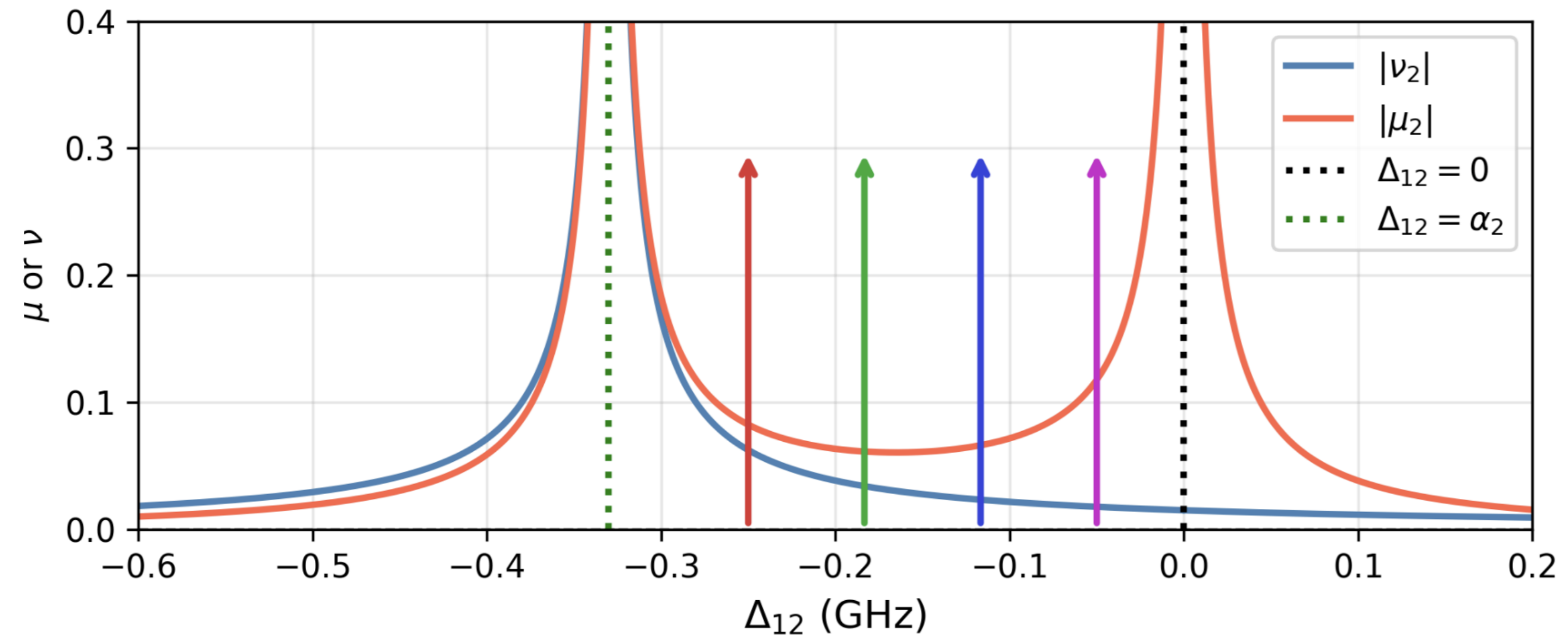
$$\nu_2 = \frac{-J}{\delta_2 - \Delta_{12}} \quad \mu_2 = \frac{J\delta_2}{\Delta_{12}(\delta_2 - \Delta_{12})}$$

“Exercise for the reader”

The 1,1 state also hybridizes with the 0,2 and 2,0 states, which gives two more transitions you can drive!

Note that in the limit $\delta \rightarrow 0$, this effect vanishes, and in the limit $\delta \rightarrow \infty$ we recover our previous expression

Two qubit gates: cross-resonance



Transmon fabrication (Dolan bridge)

1. Clean wafer
2. Sputter superconductor



3. Pattern resonators and capacitors using photolithography



Superconductor

Substrate

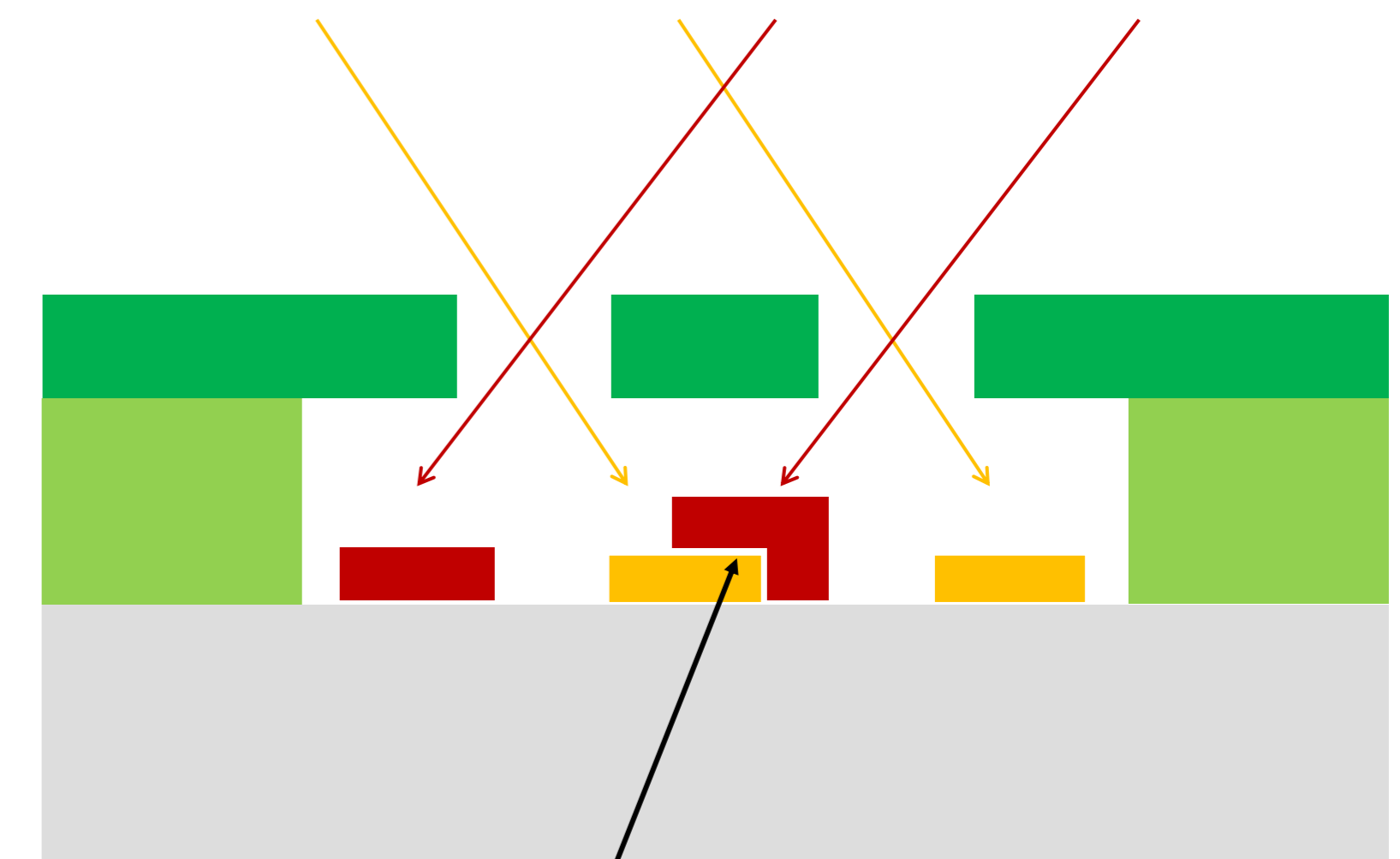
MMA / PMMA

1st Al evaporation

Al oxide

2nd Al evaporation

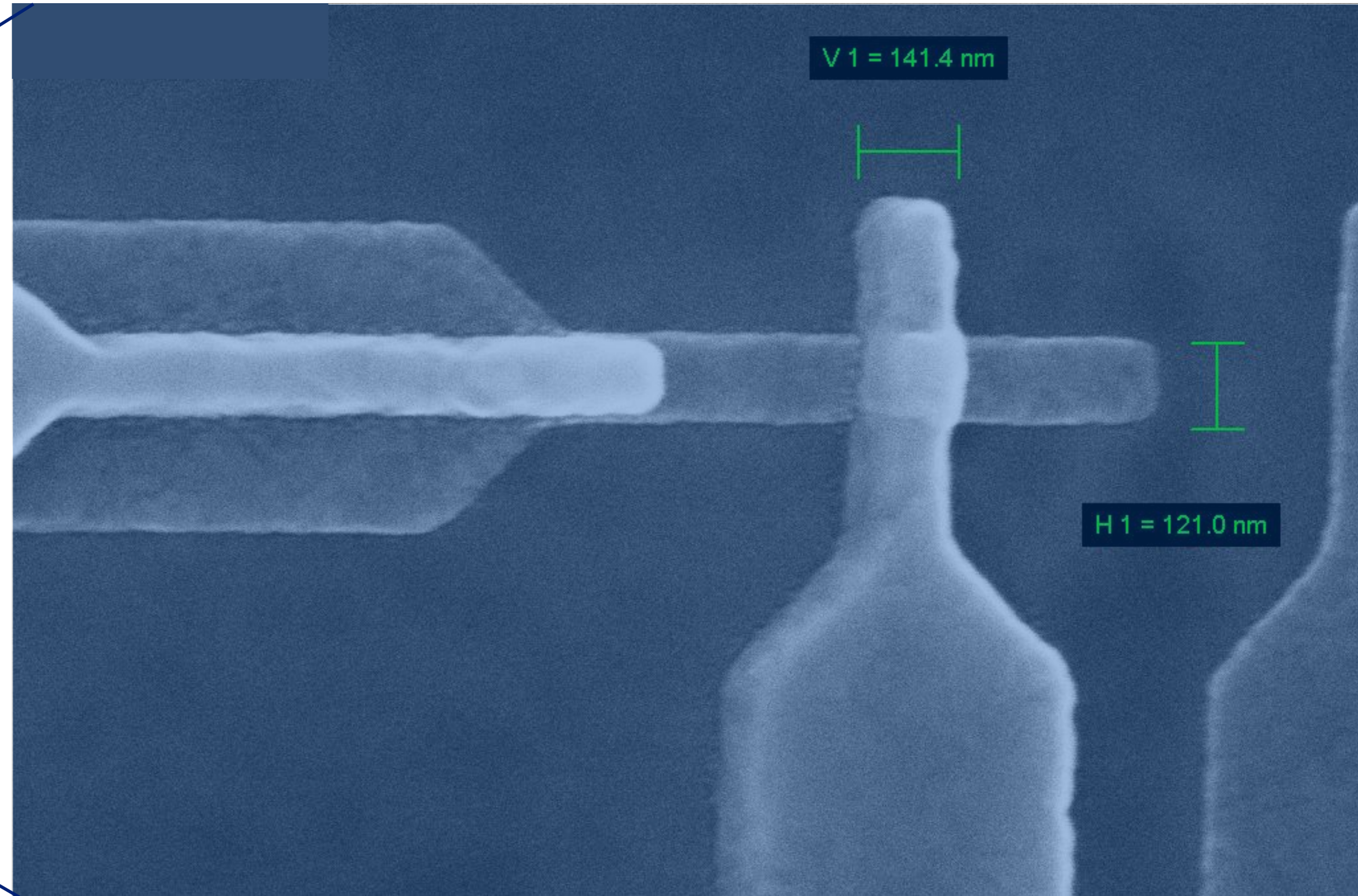
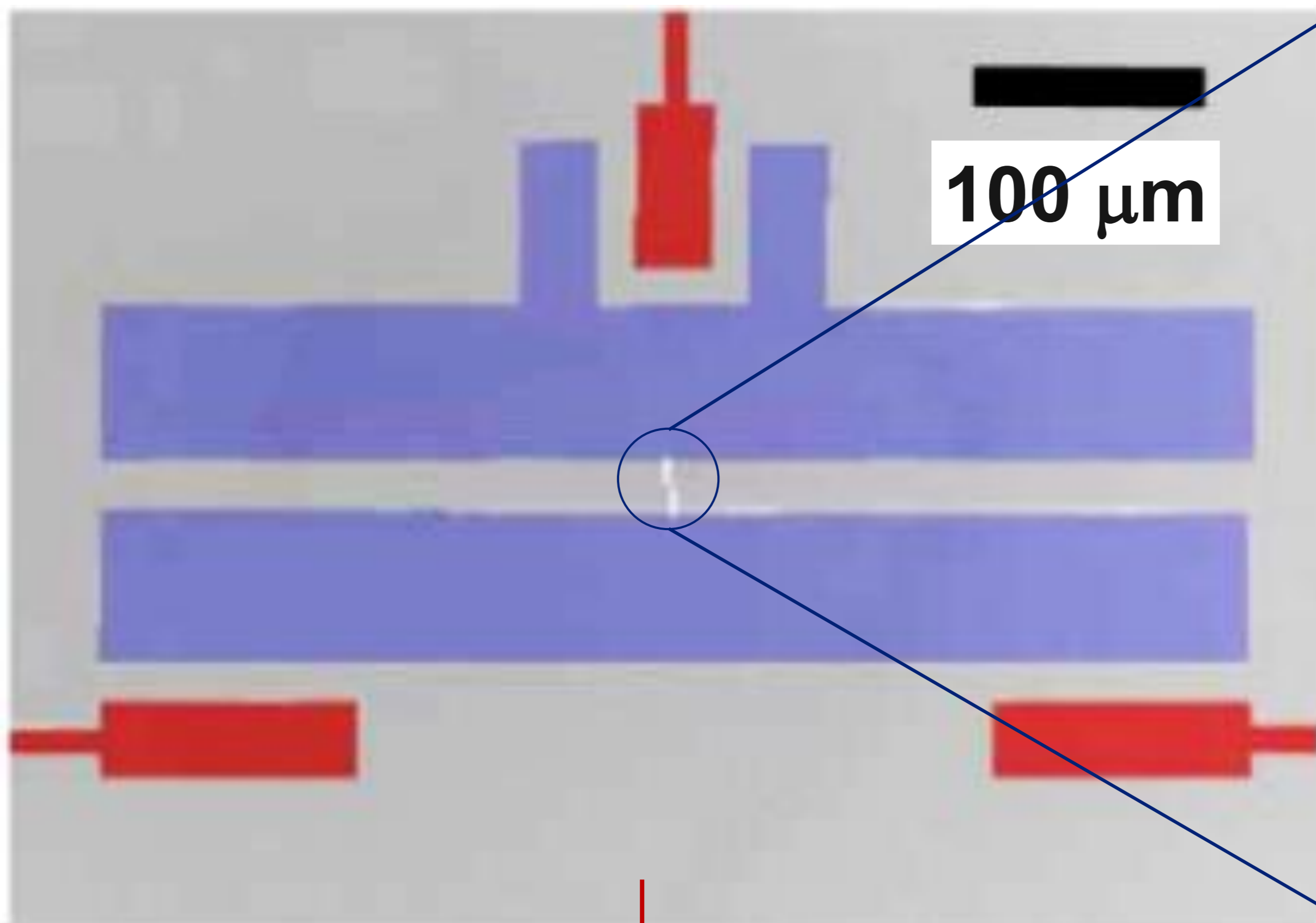
1. Form Dolan bridge structure in MMA/PMMA resist stack using e-beam lithography
2. Deposit Al/AlOx/Al Josephson junction using double-angle evaporation, in-situ oxidation and liftoff



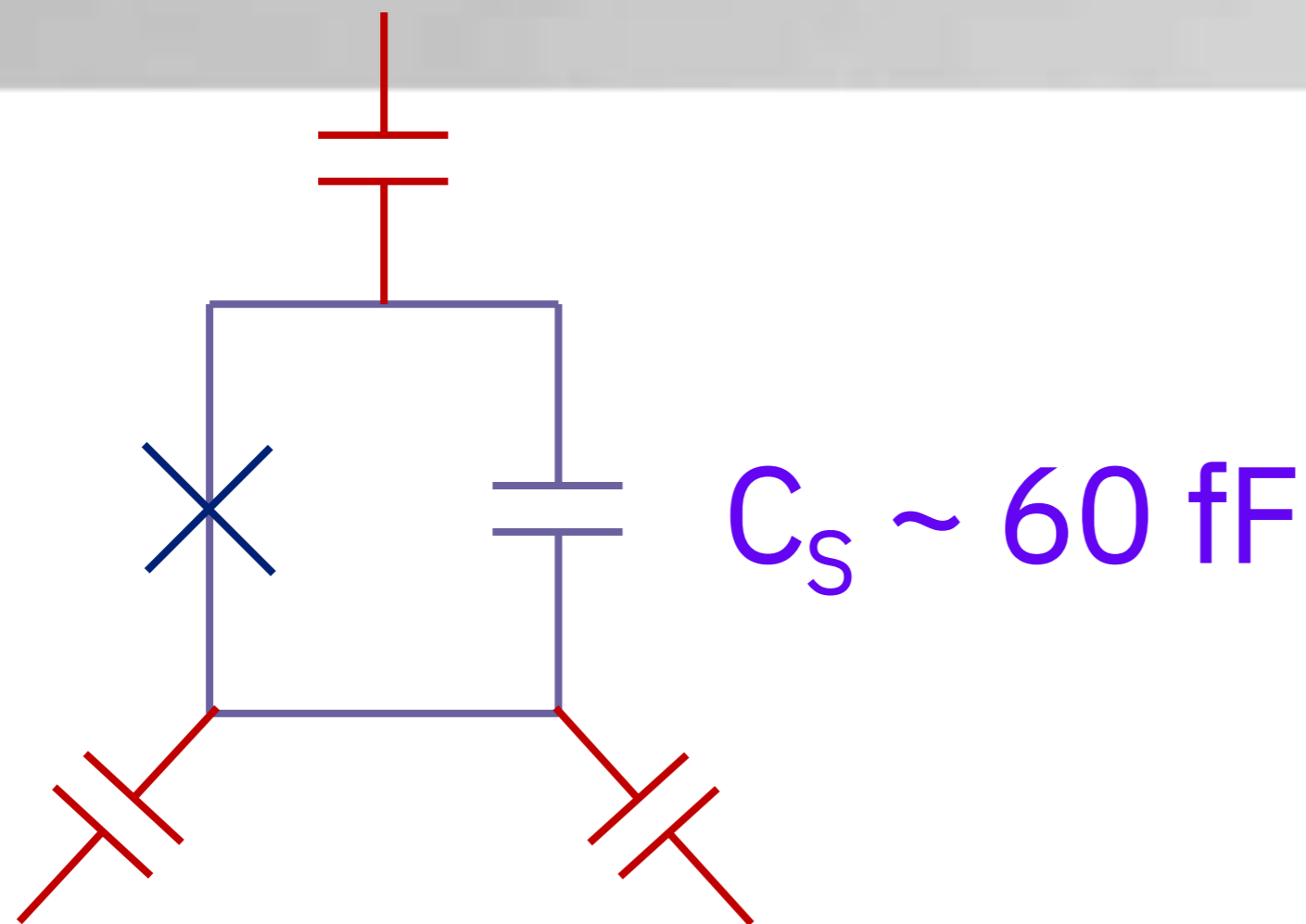
**Josephson
Junction**

Transmon fabrication (Dolan bridge)

IBM Quantum



$L_J \sim 20 \text{ nH}$
 $C_J \sim 1 \text{ fF}$



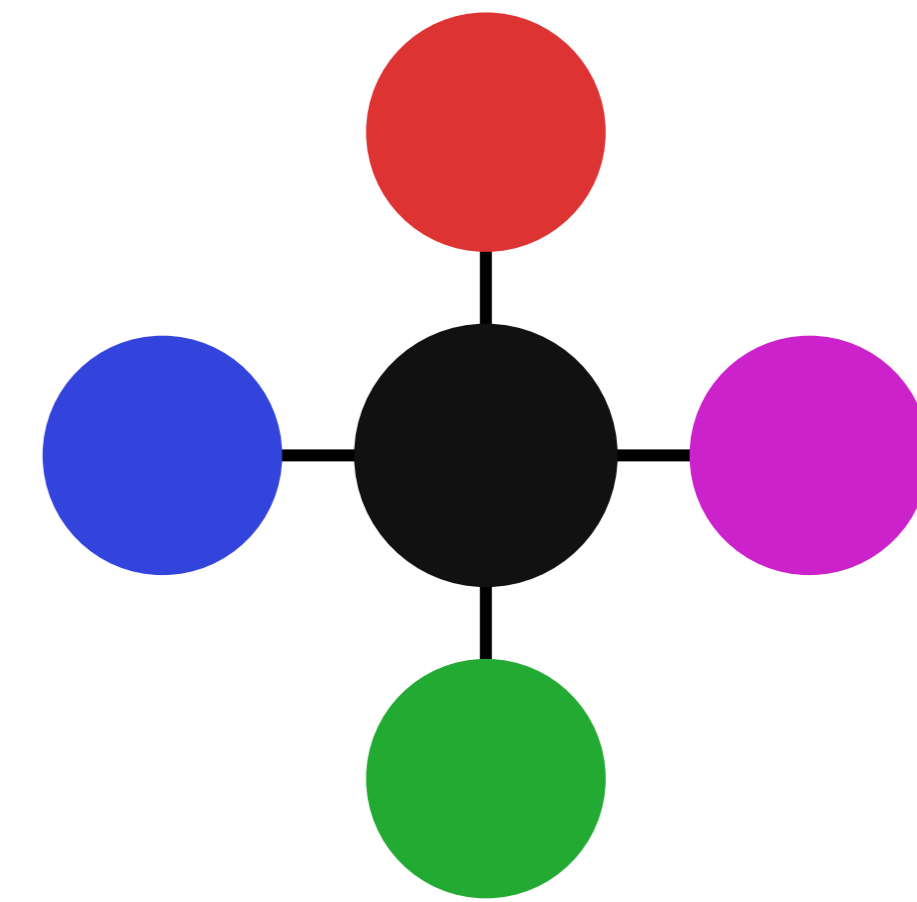
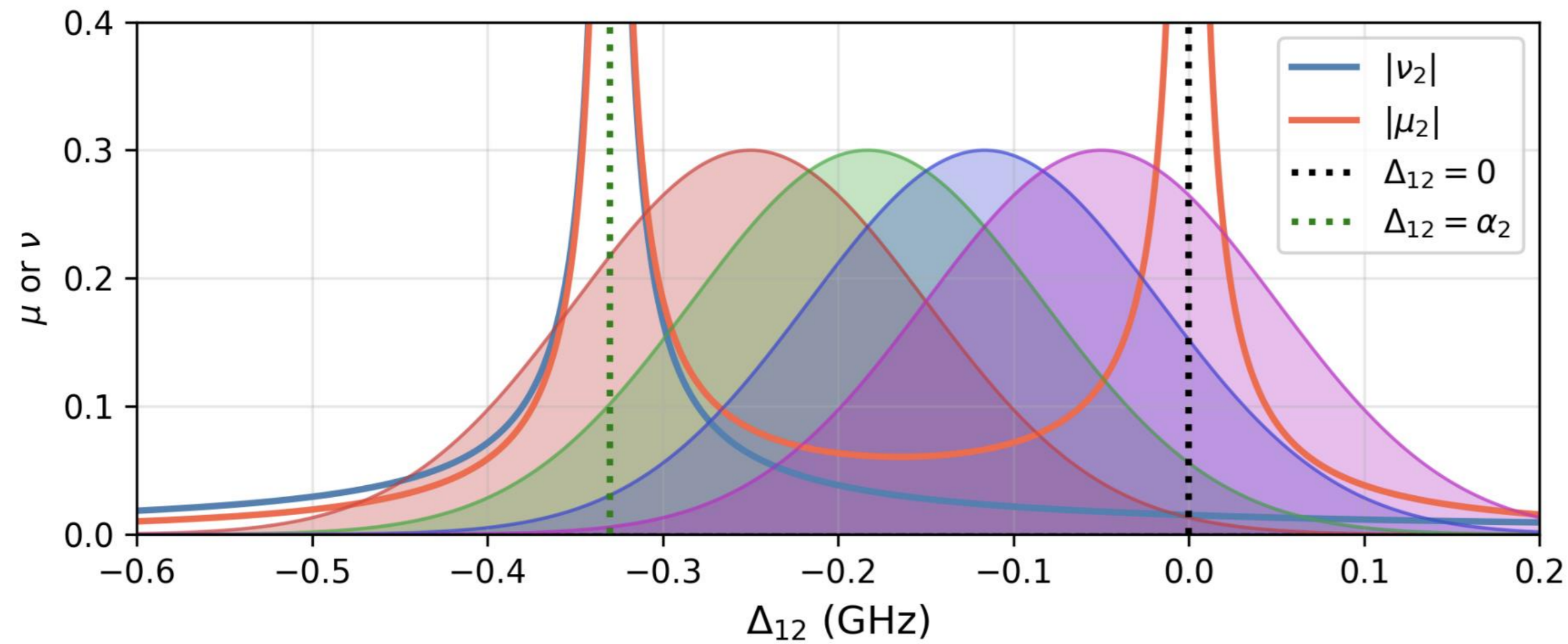
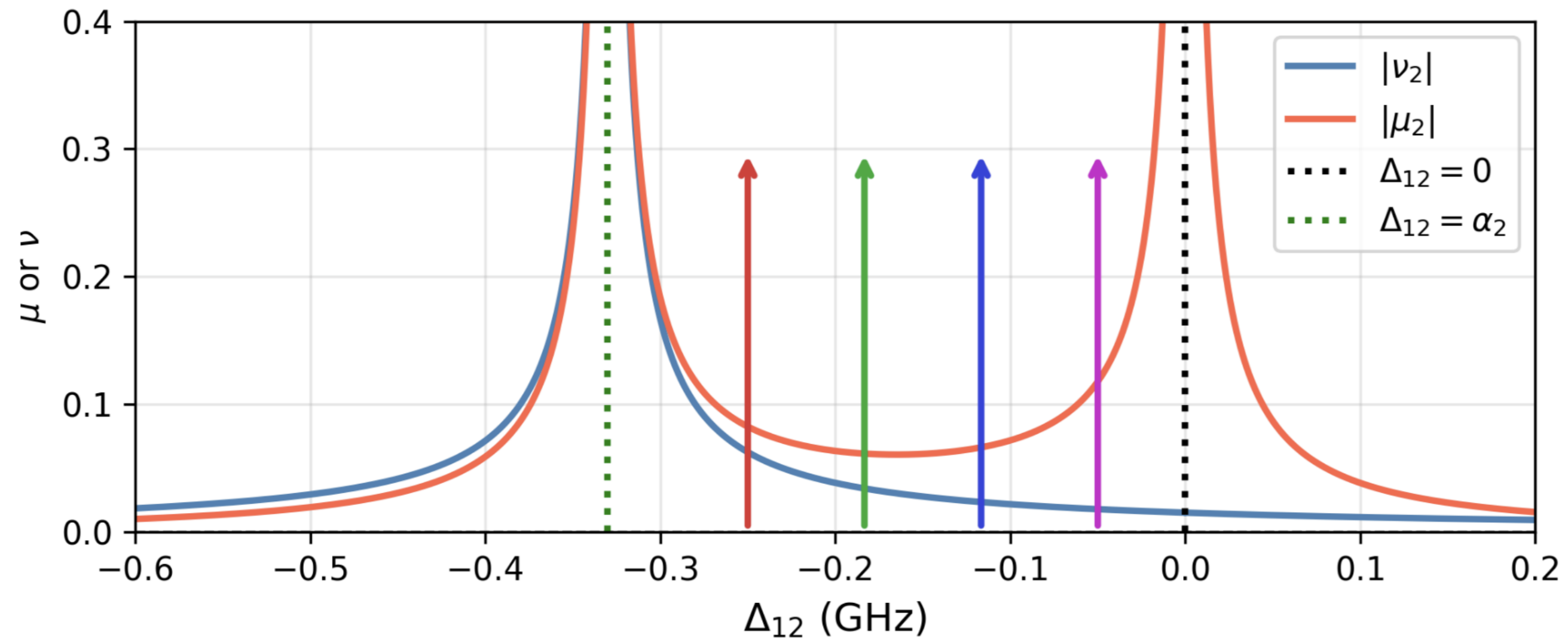
Nb pads

Al - Al₂O₃ - Al JJ

$\omega_{01} \sim 5 \text{ GHz}$

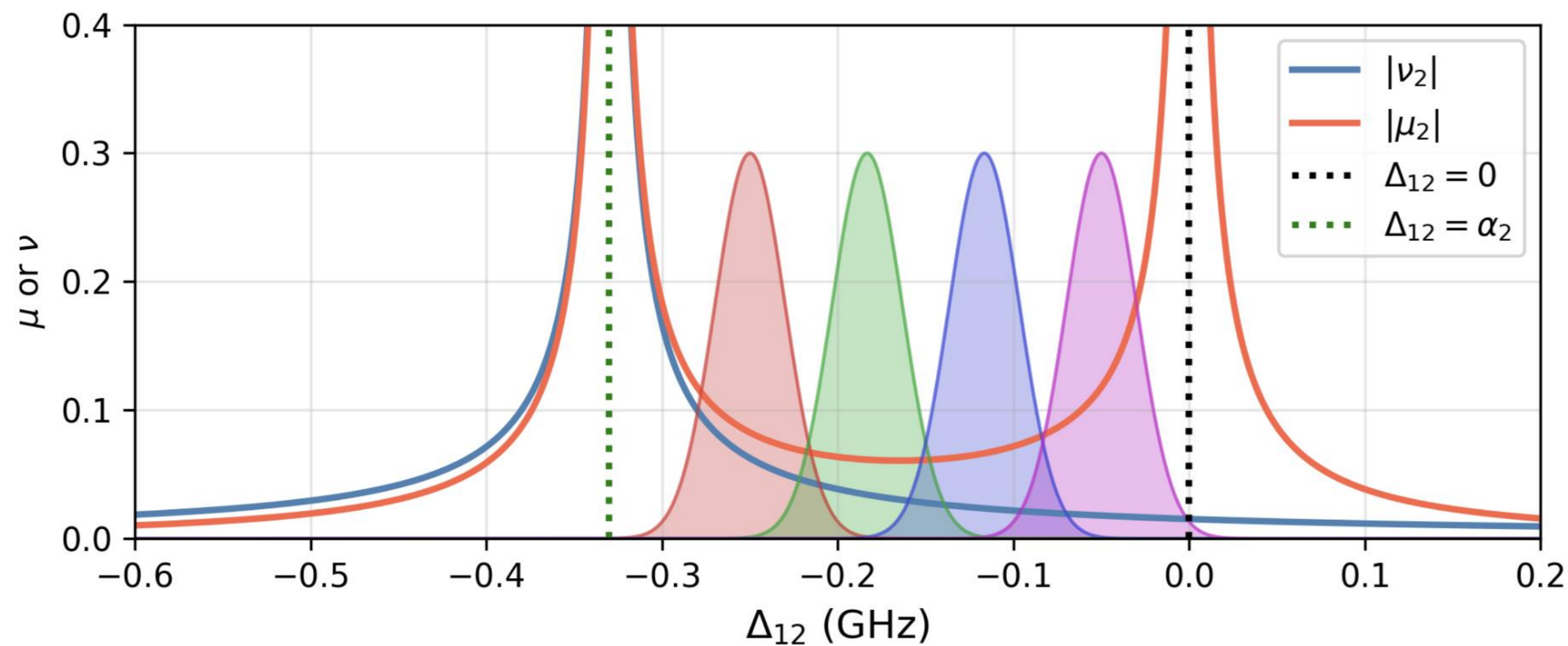
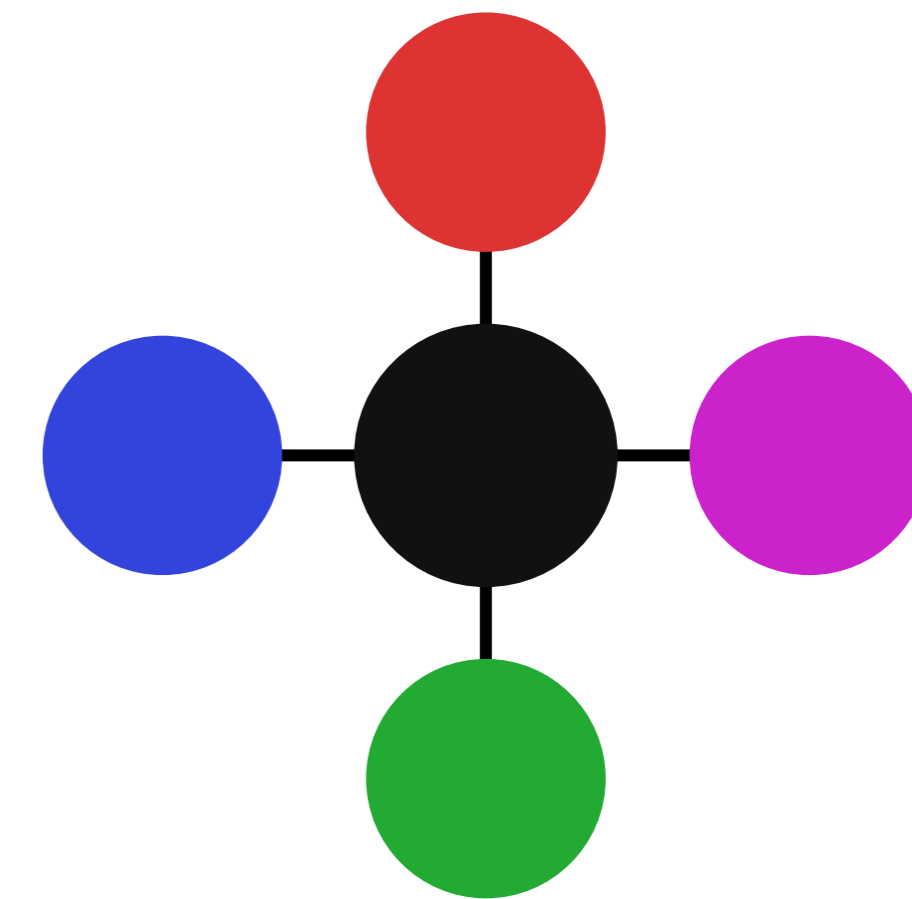
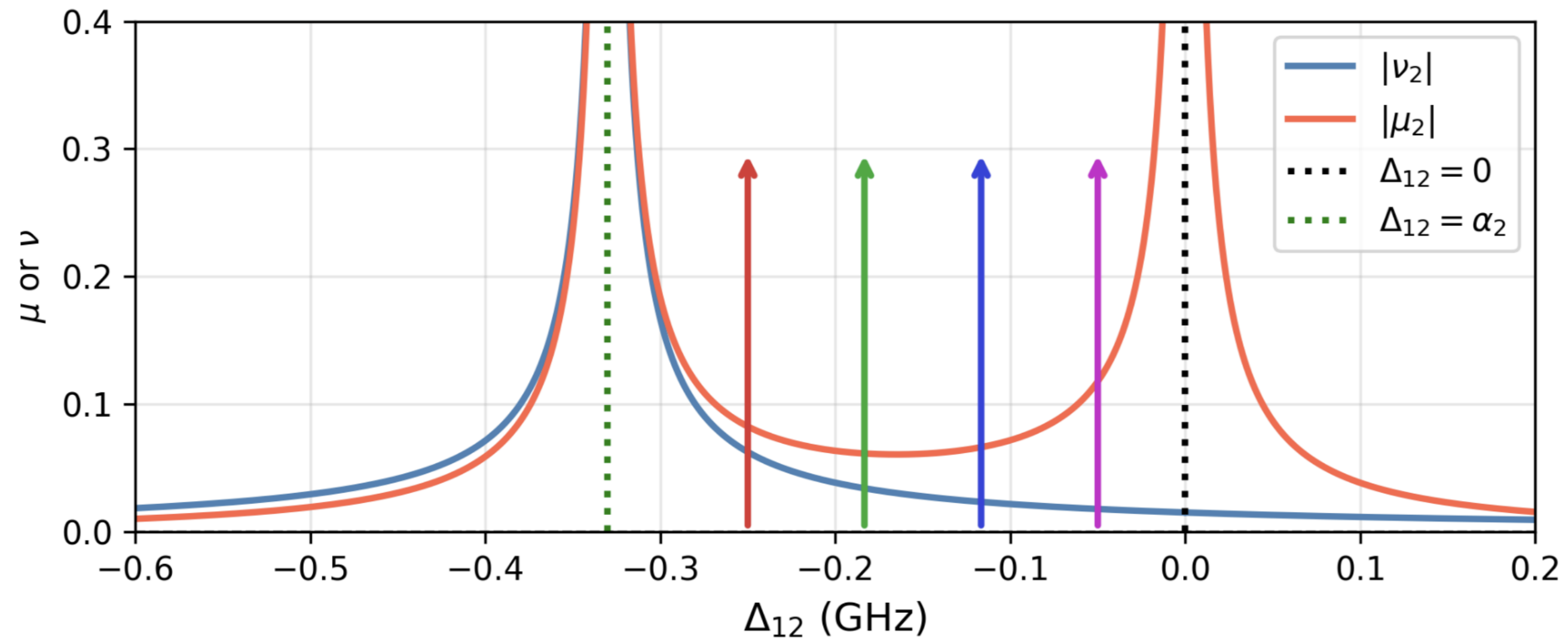
$\omega_{01} - \omega_{12} \sim 0.330 \text{ GHz}$

Two qubit gates: cross-resonance



Fabrication spread makes frequency collisions certain in large devices

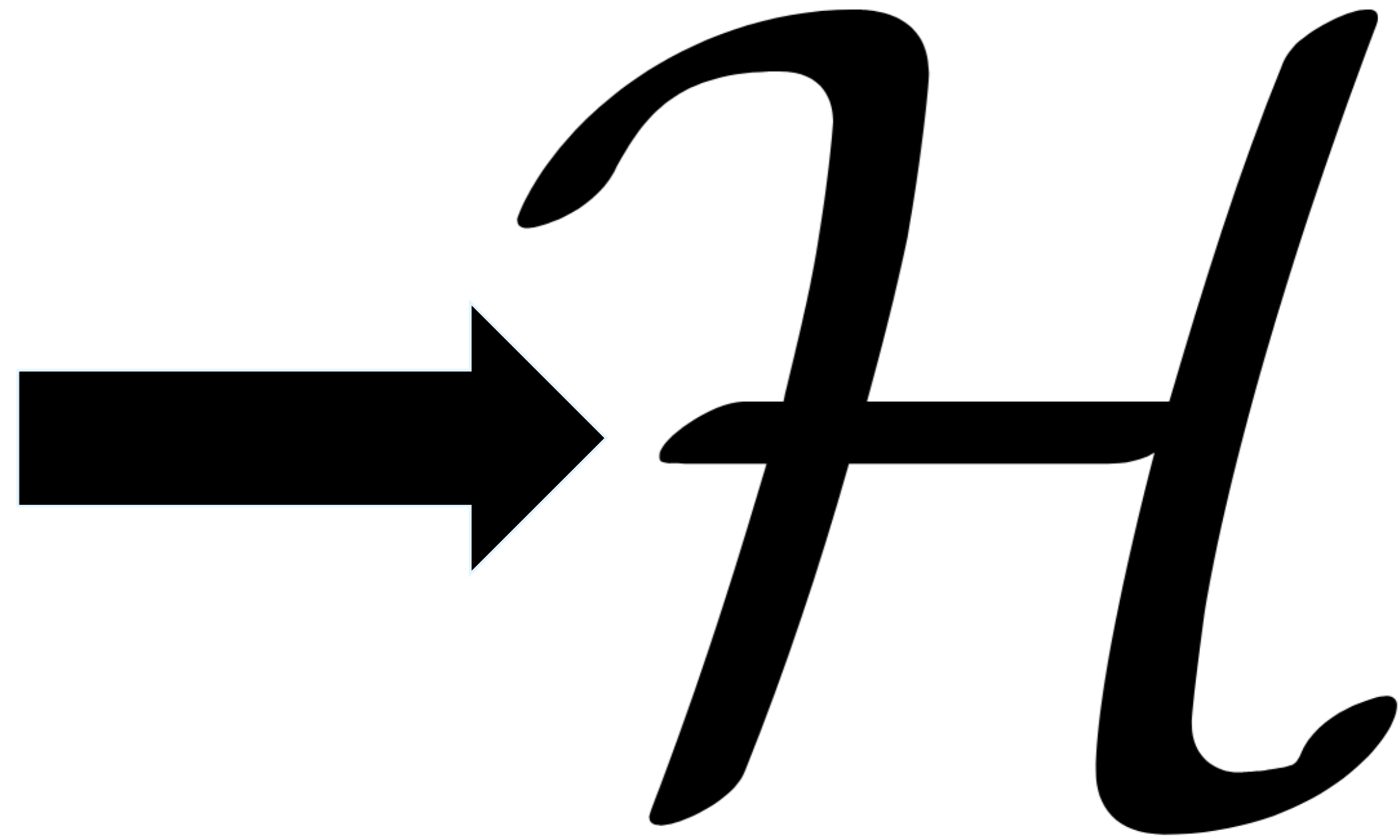
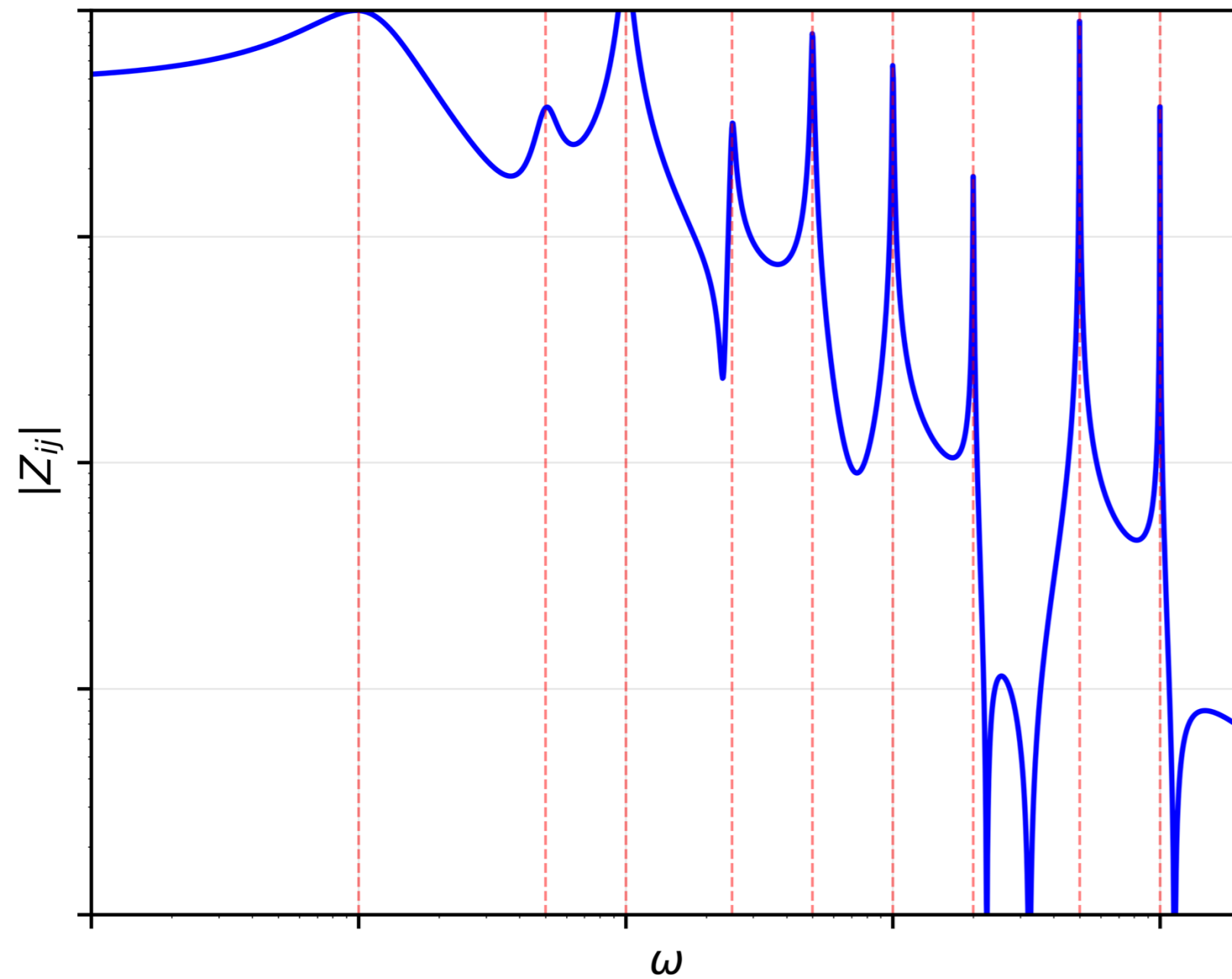
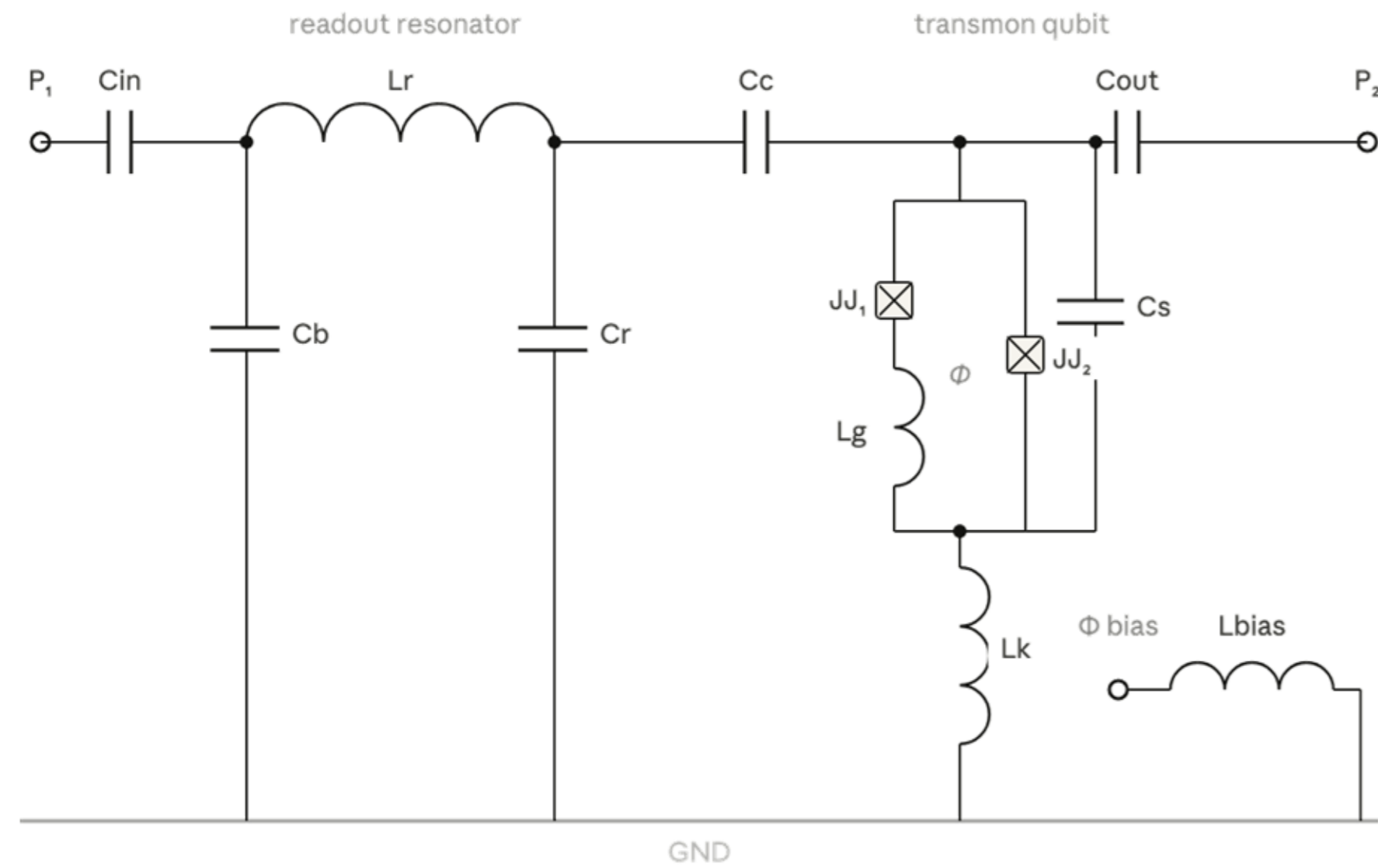
Two qubit gates: cross-resonance



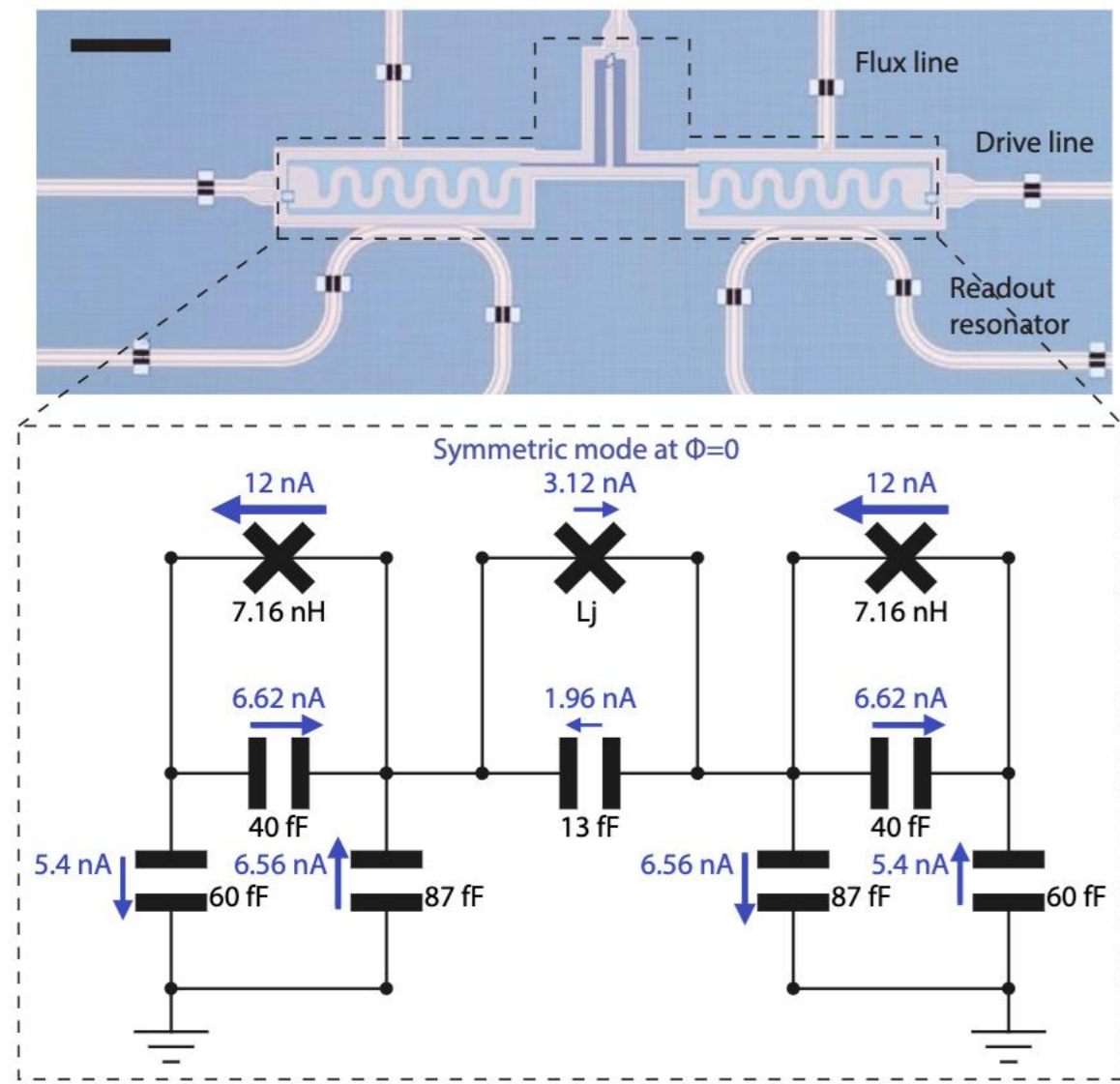
Fabrication spread makes frequency collisions certain in large devices

Even with laser tuning of junctions

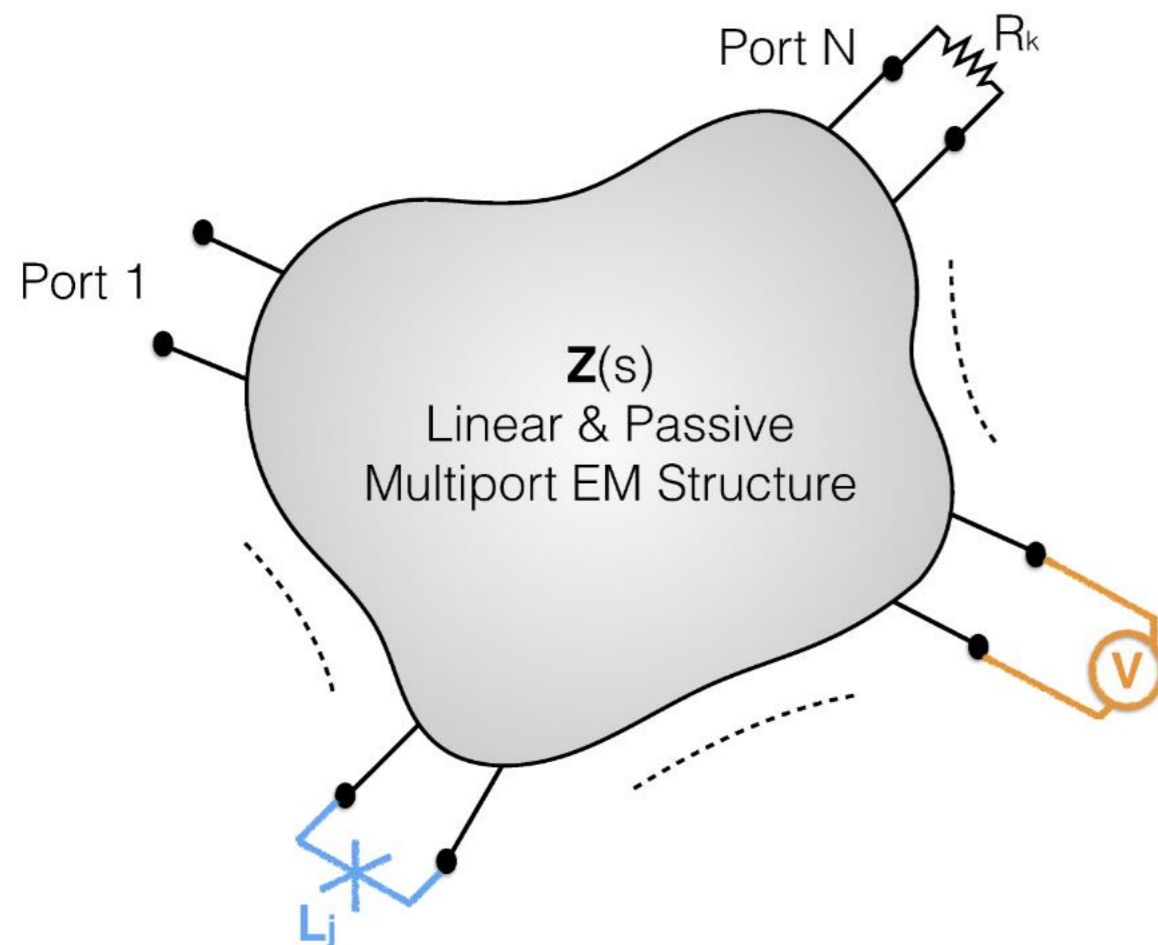
Circuit models to Hamiltonians



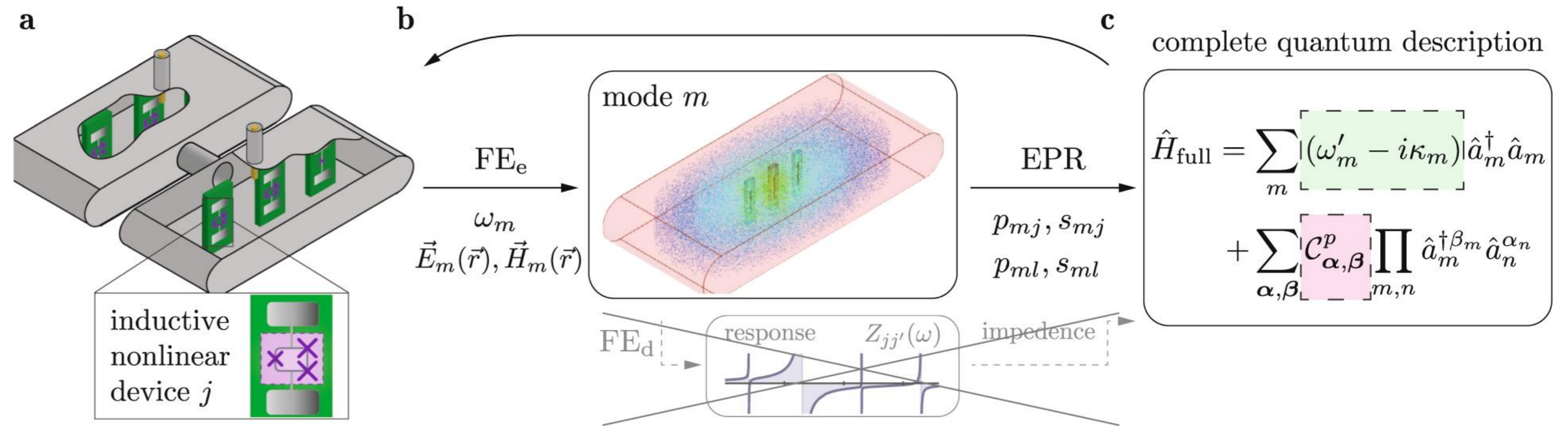
Circuit models to Hamiltonians



From [3]



From [2]



From [4]

[1] S. Nigg et al. “Black-Box Superconducting Circuit Quantization.” *Phys. Rev. Lett.* **108**, 240502 (2012).

[2] F. Solgun and D. DiVincenzo, “Mutliport Impedance Quantization.” *Annals of Physics*, Volume 361, (2015).

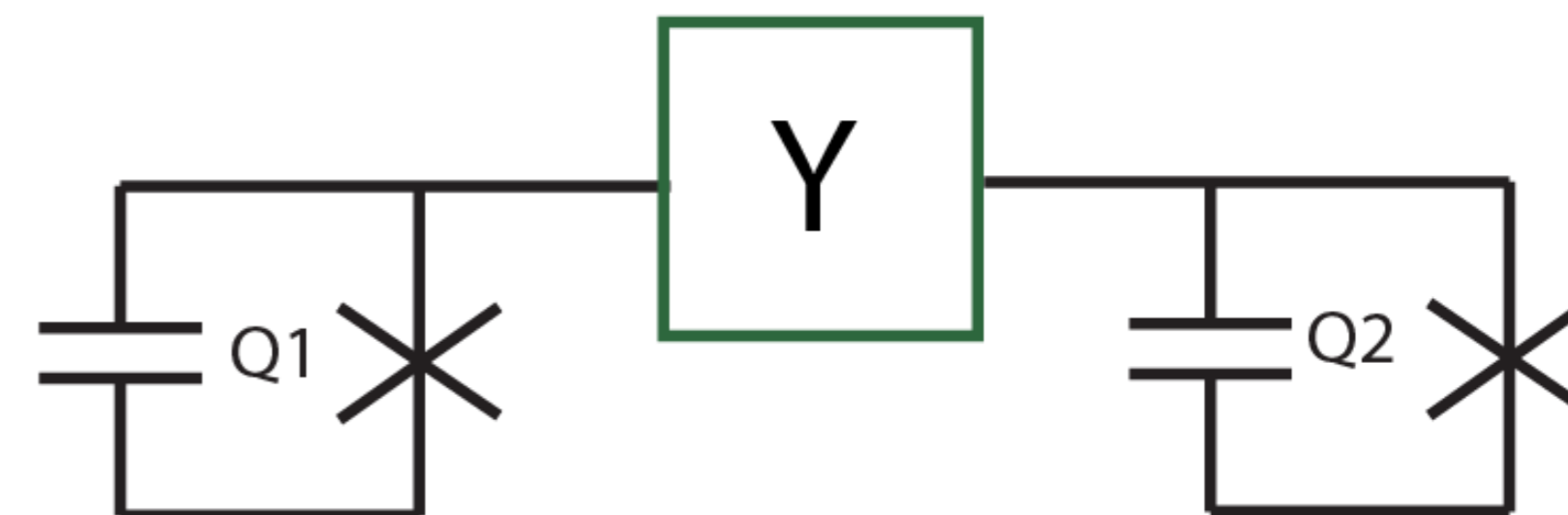
[3] Mario F. Gely and Gary A. Steele. “QuCAT: quantum circuit analyzer tool in Python.” *New Journal of Physics* **22.1** (2020).

[4] Zlatko Mineev et al. ”Energy-participation quantization of Josephson circuit.” *npj Quantum Inf* **7**, 131 (2021).

Approximate impedance methods

Weakly coupled, weakly anharmonic oscillators

$$J_{ij} = -\frac{1}{4} \sqrt{\frac{\omega_i \omega_j}{L_i L_j}} \operatorname{Im} \left[\frac{Z_{ij}(\omega_i)}{\omega_i} + \frac{Z_{ij}(\omega_j)}{\omega_j} \right]$$

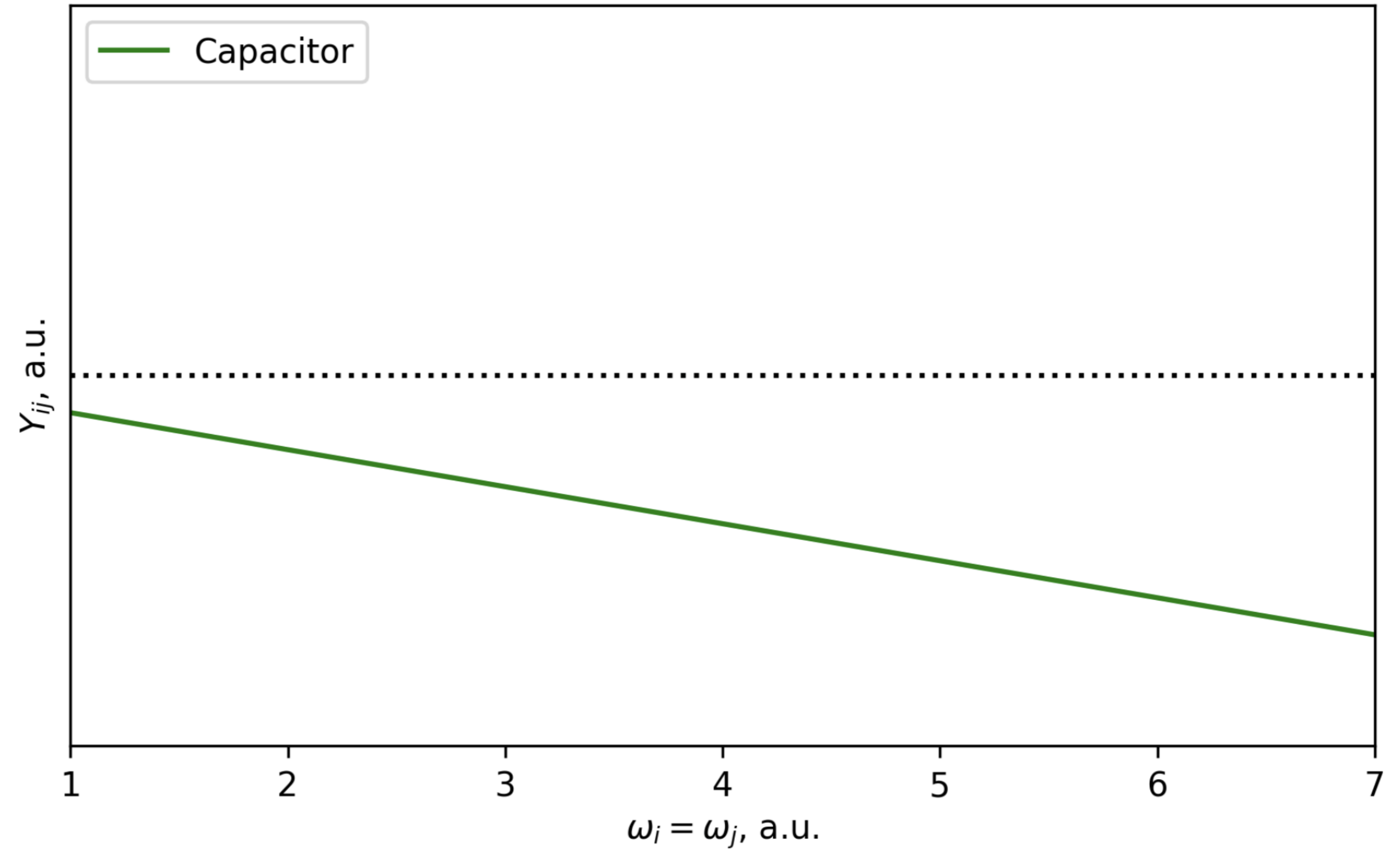


$$Y_{ii} \ll Y_{ij}$$

$$J_{ij} = -\frac{(\omega_i \omega_j)^{3/2}}{4 \sqrt{C_i C_j}} \left[\frac{Y_{ij}(\omega_i)}{\omega_i^3} + \frac{Y_{ij}(\omega_j)}{\omega_j^3} \right]$$

F. Solgun, D. DiVincenzo, J. Gambetta, “Simple Impedance Response Formulas for the Dispersive Interaction Rates in the Effective Hamiltonians of Low Anharmonicity Superconducting Qubits.” *IEEE Transactions on Microwave Theory and Techniques* **67**(3) (2019).

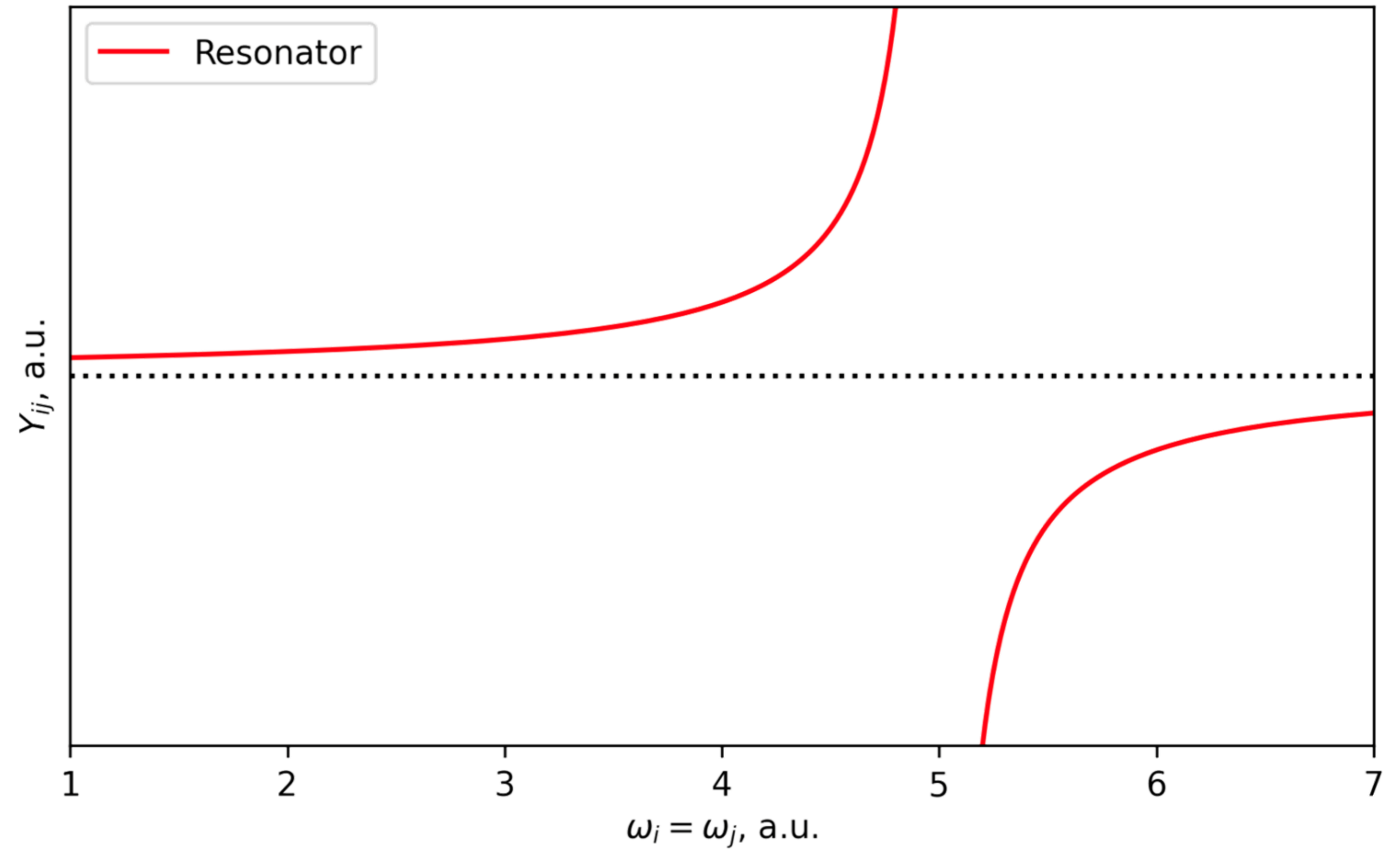
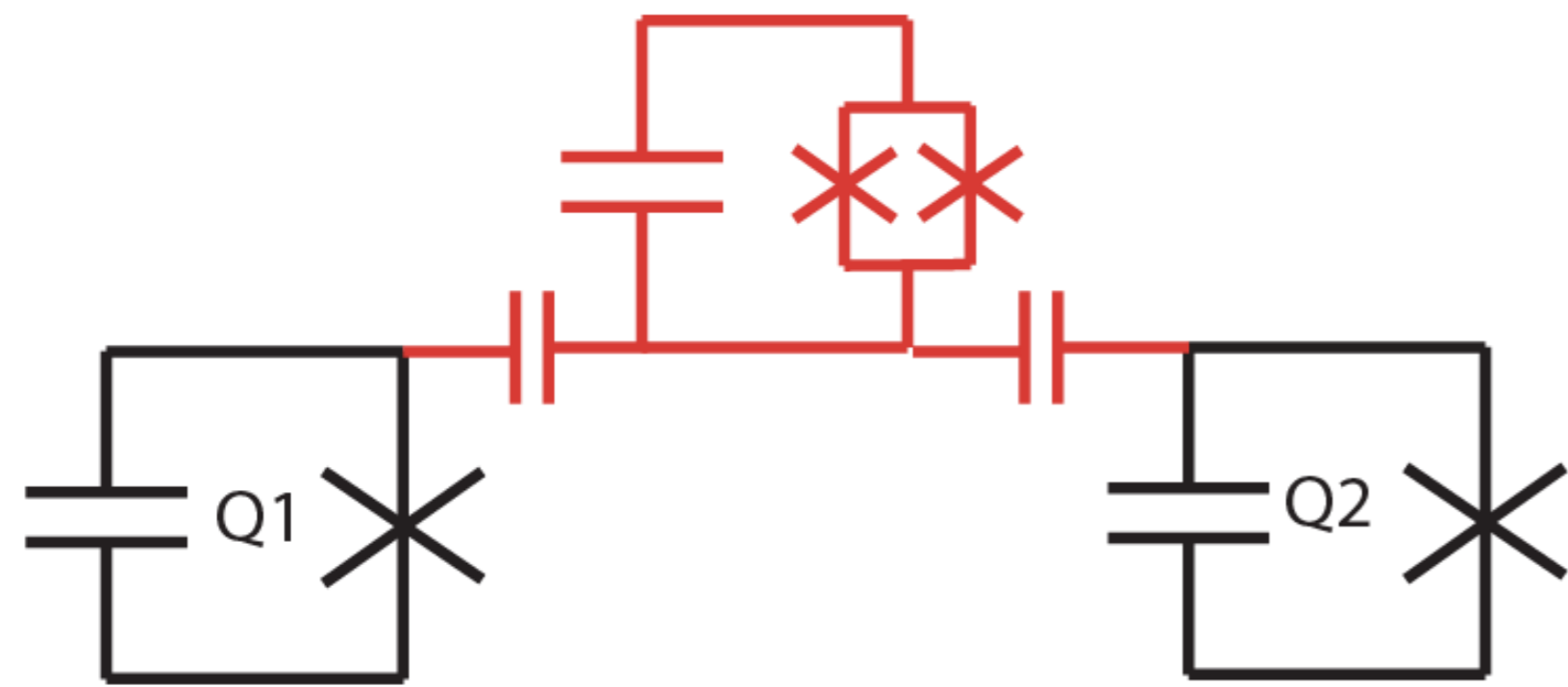
Flux Tunable Couplers



[1] F. Yan et al. "Tunable Coupling Scheme for Implementing High-Fidelity Two-Qubit Gates." Phys. Rev. Applied 10, 054062 (2018).

With techniques of F. Solgun et al., IEEE Transactions on Microwave Theory and Techniques 67(3) (2019).

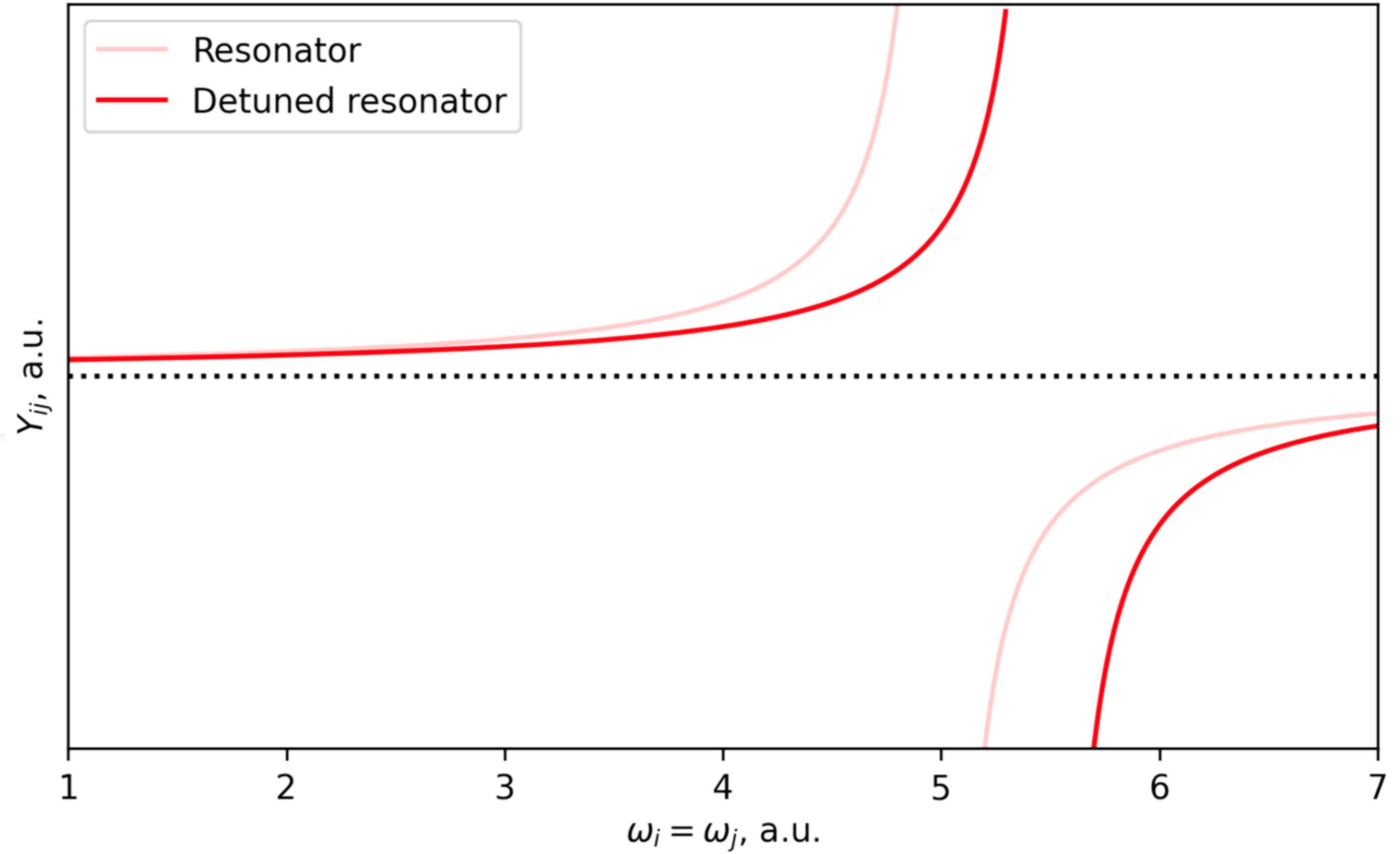
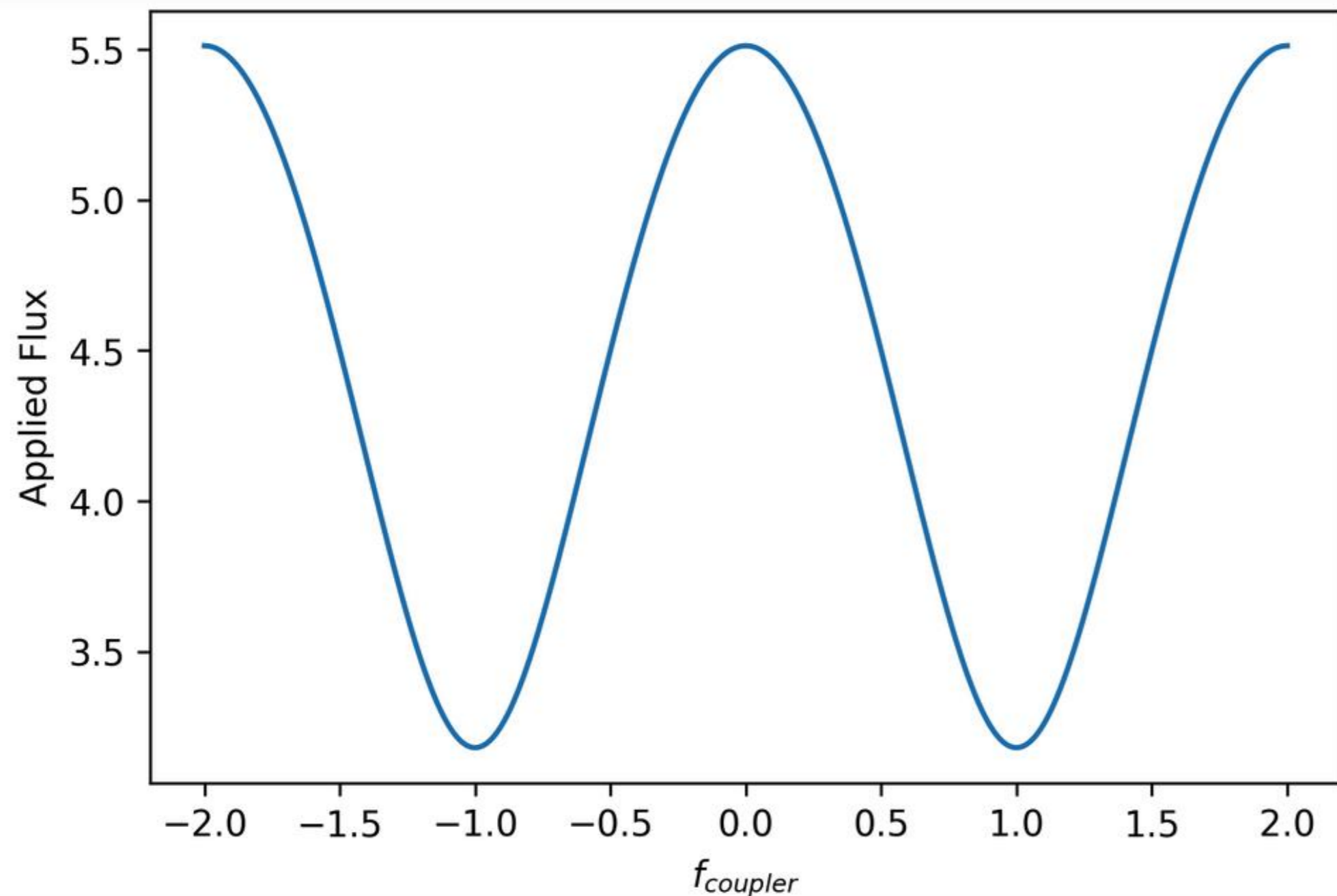
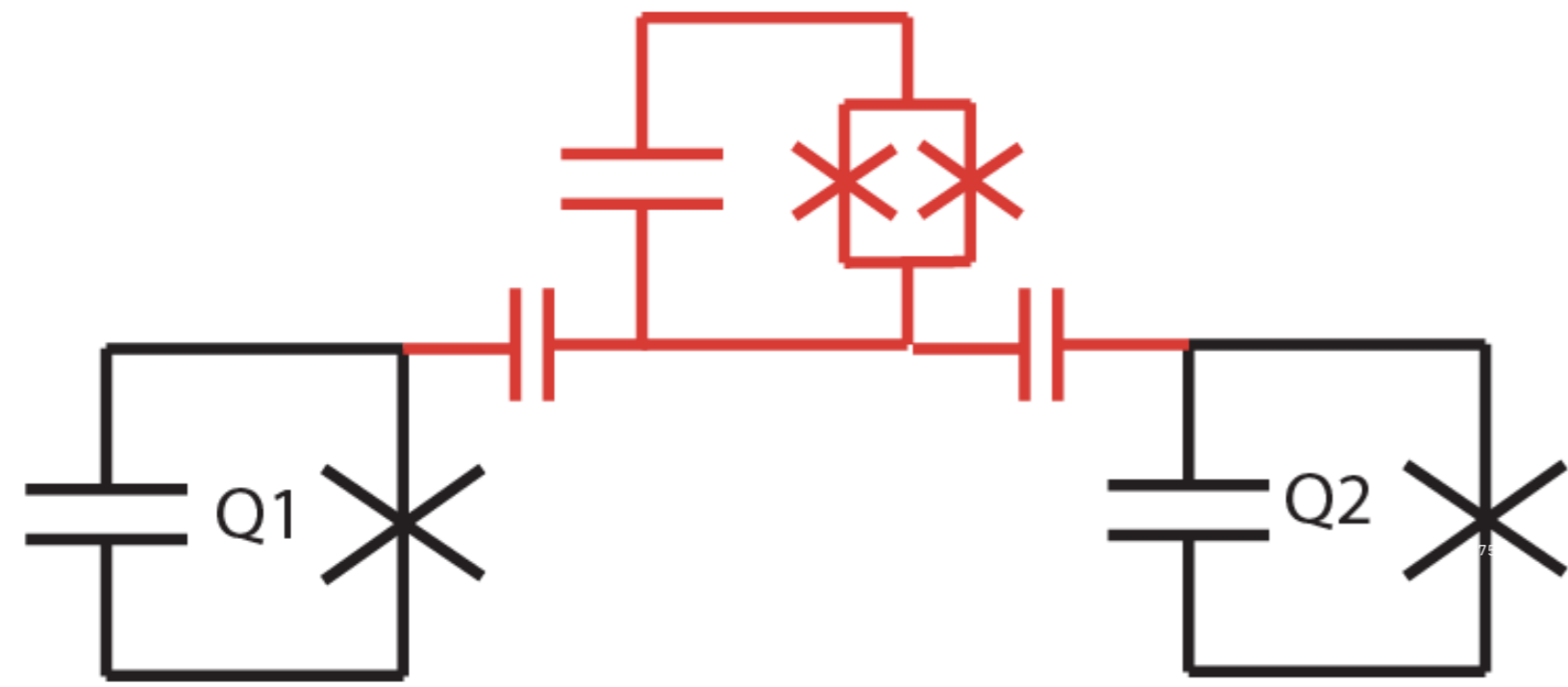
Coupling qubits 101



[1] F. Yan et al. "Tunable Coupling Scheme for Implementing High-Fidelity Two-Qubit Gates." *Phys. Rev. Applied* 10, 054062 (2018).

With techniques of F. Solgun et al., *IEEE Transactions on Microwave Theory and Techniques* 67(3) (2019).

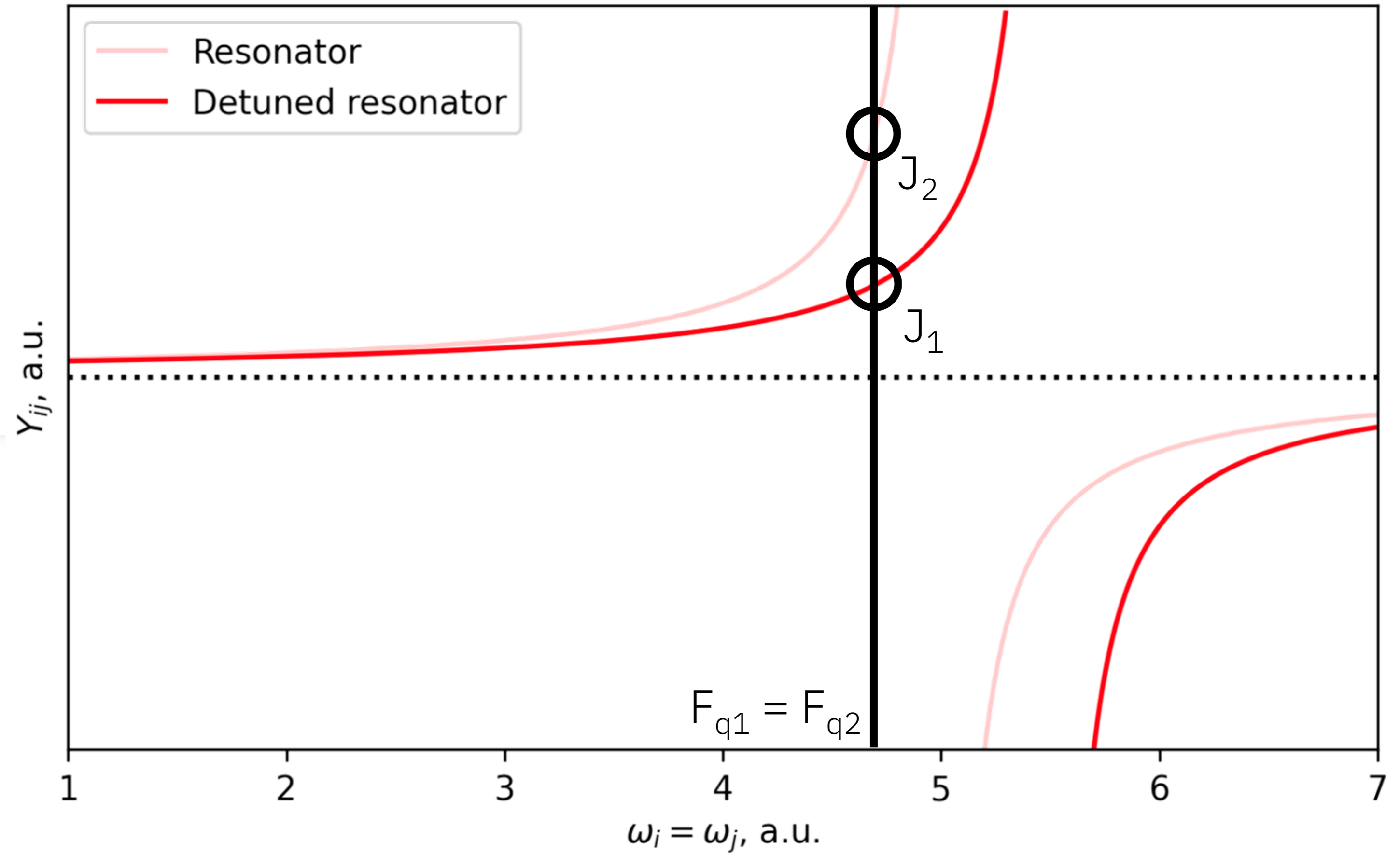
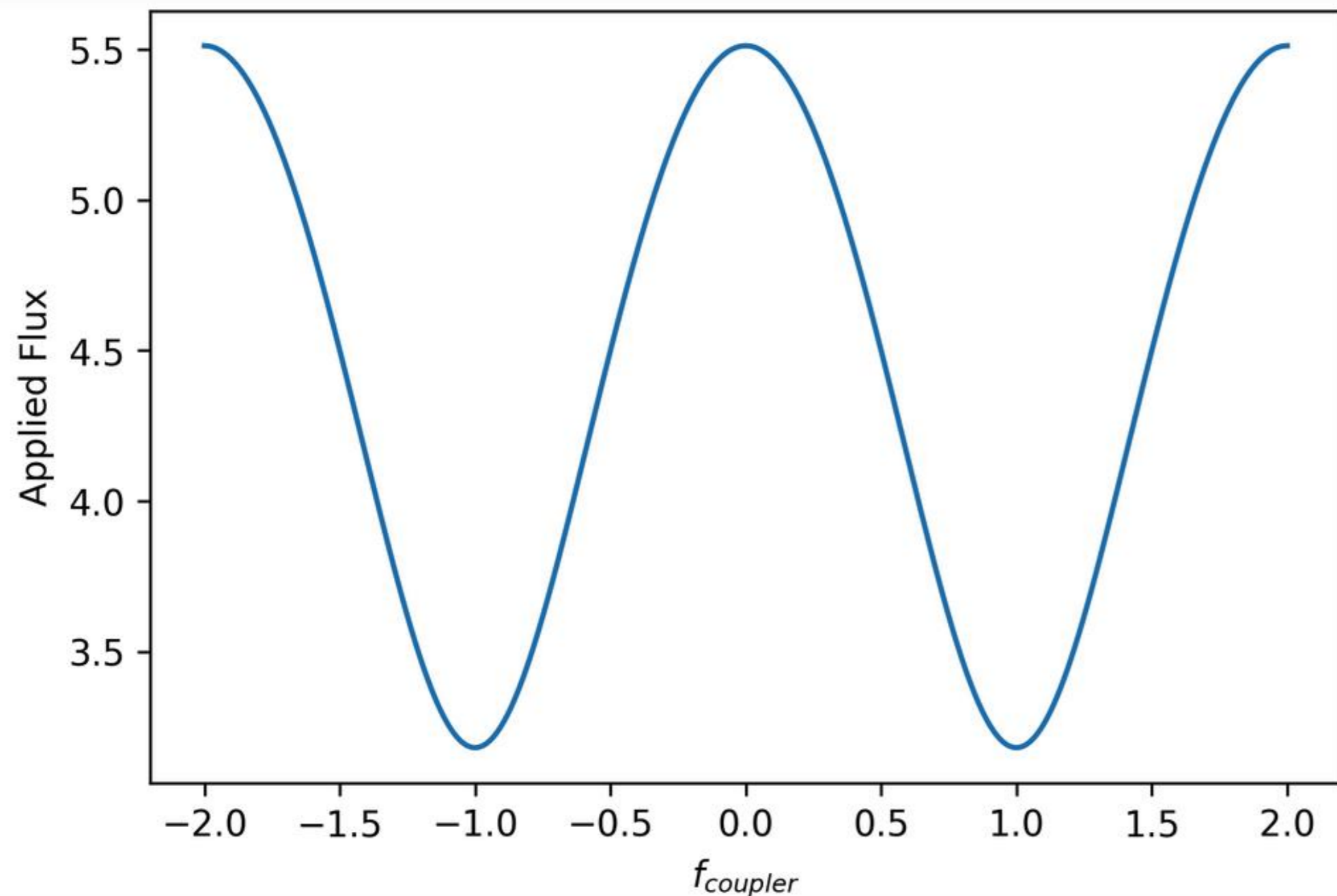
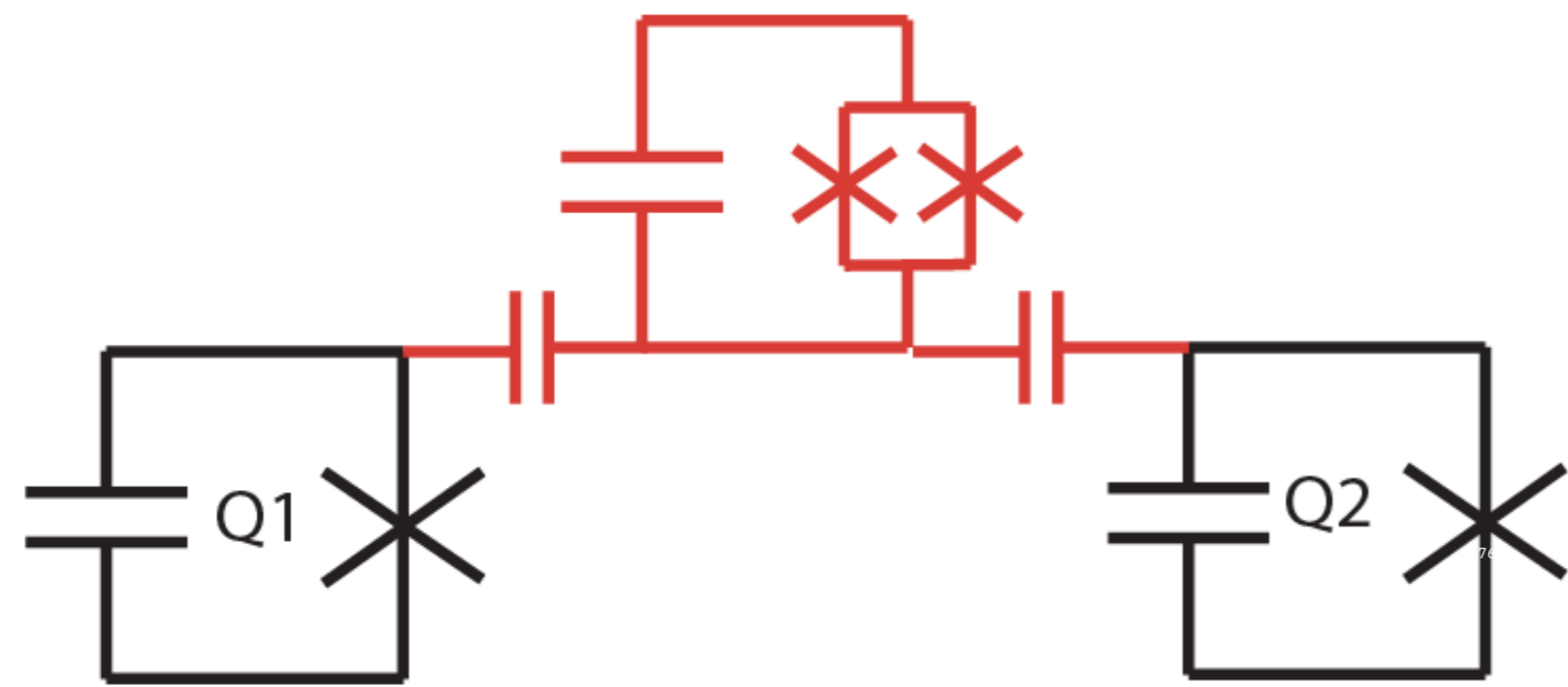
Coupling qubits 101



[1] F. Yan et al. "Tunable Coupling Scheme for Implementing High-Fidelity Two-Qubit Gates." Phys. Rev. Applied 10, 054062 (2018).

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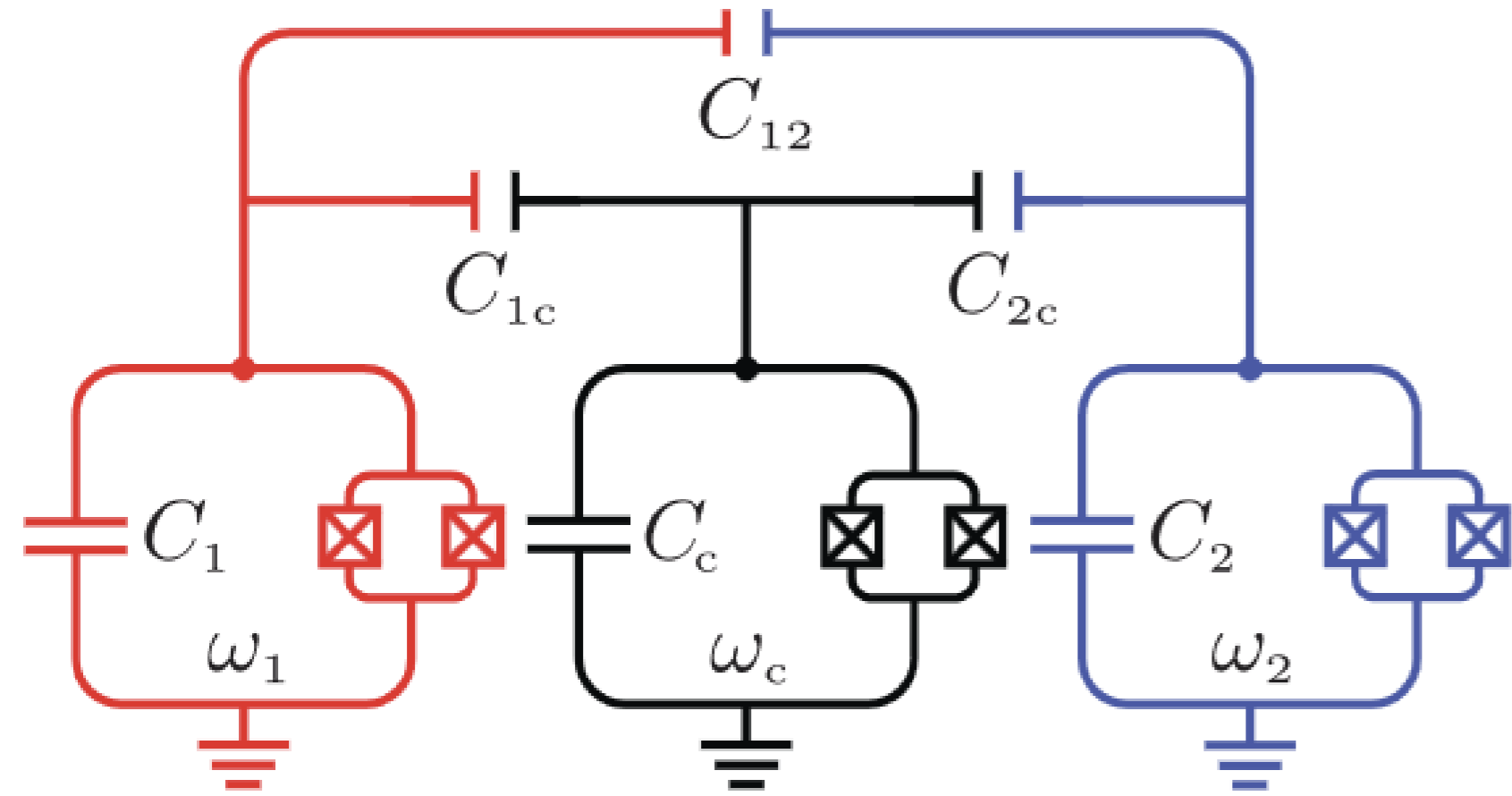
Coupling qubits 101



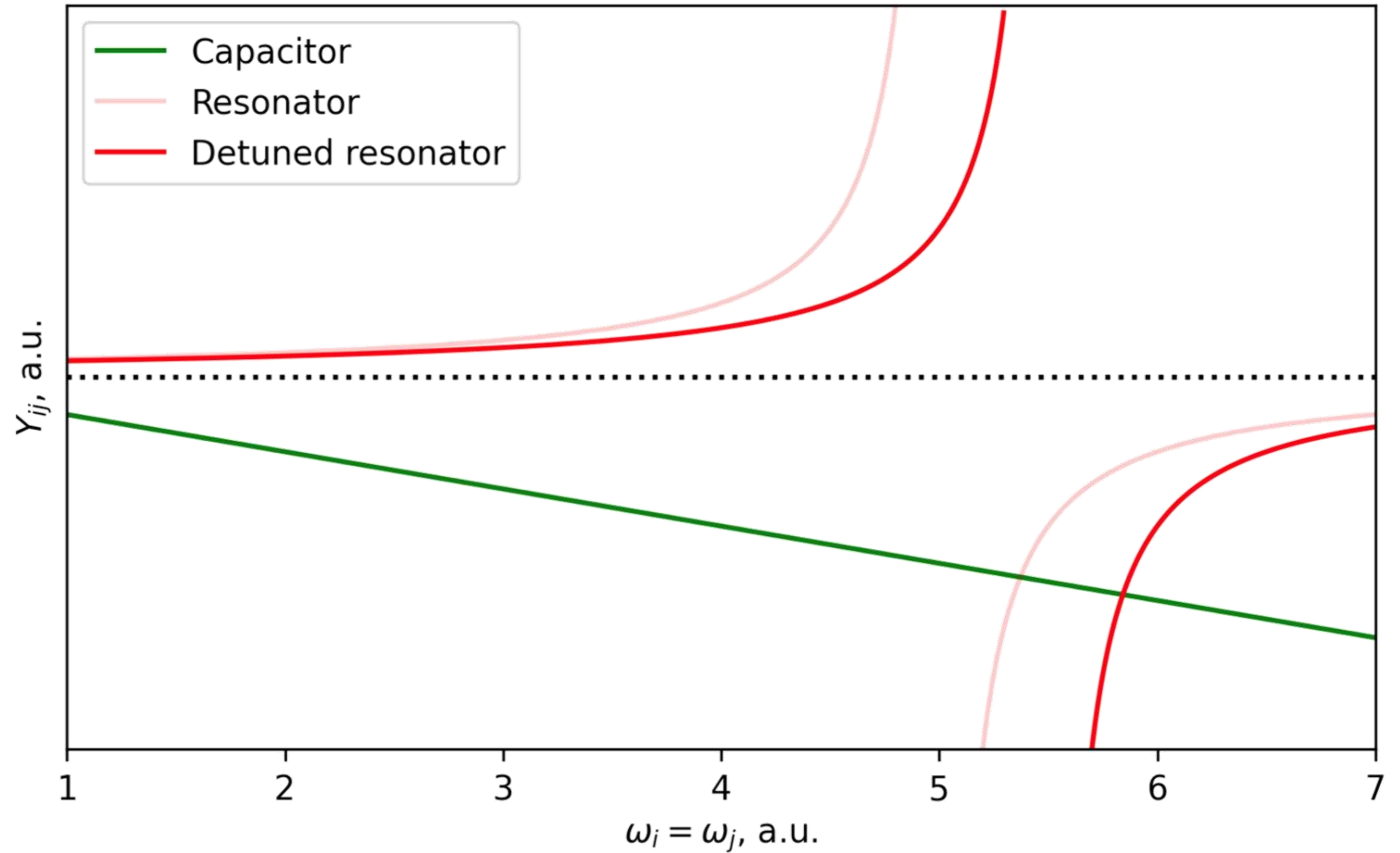
[1] F. Yan et al. "Tunable Coupling Scheme for Implementing High-Fidelity Two-Qubit Gates." Phys. Rev. Applied 10, 054062 (2018).

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Coupling qubits 101



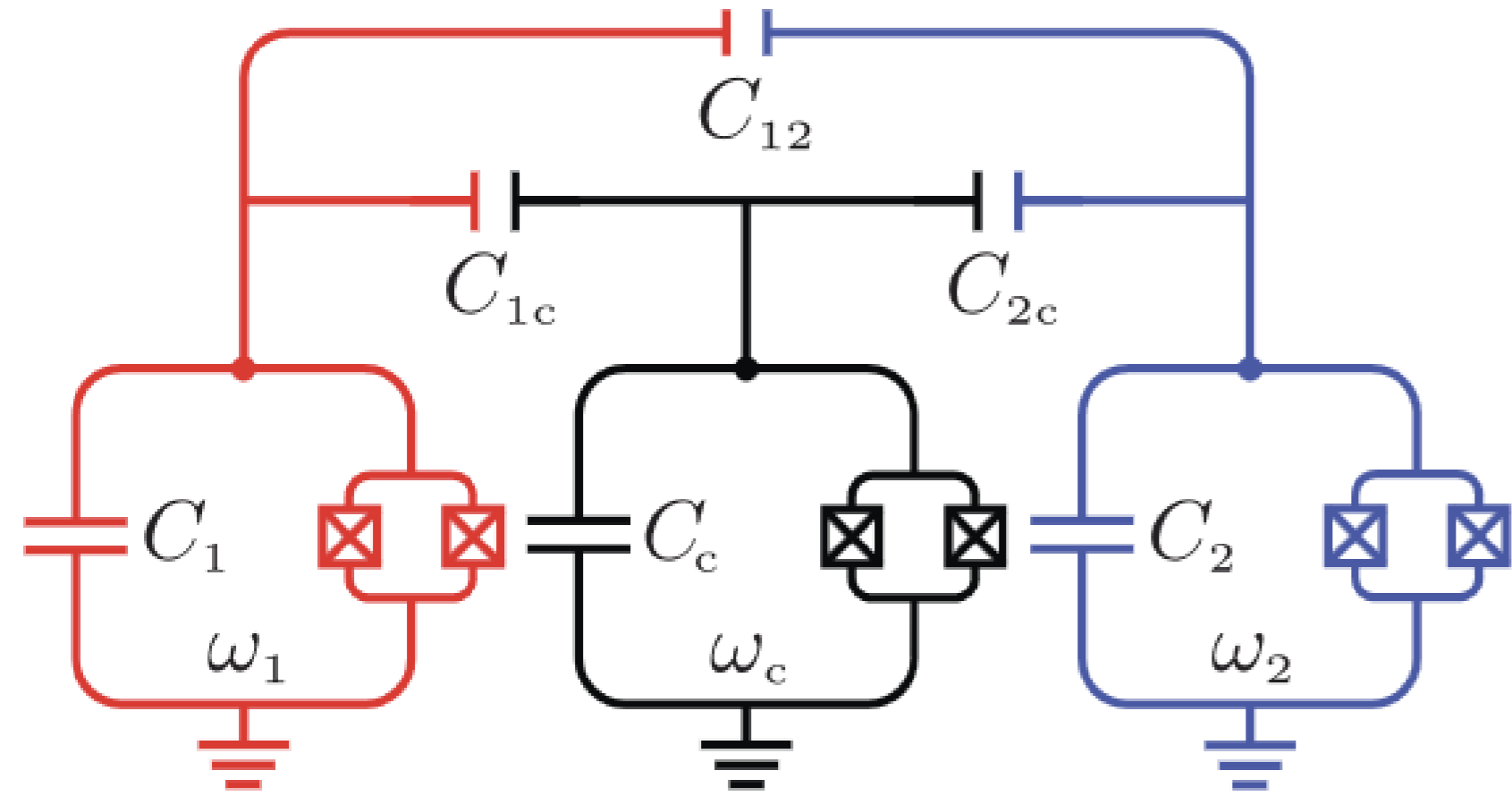
From [1]



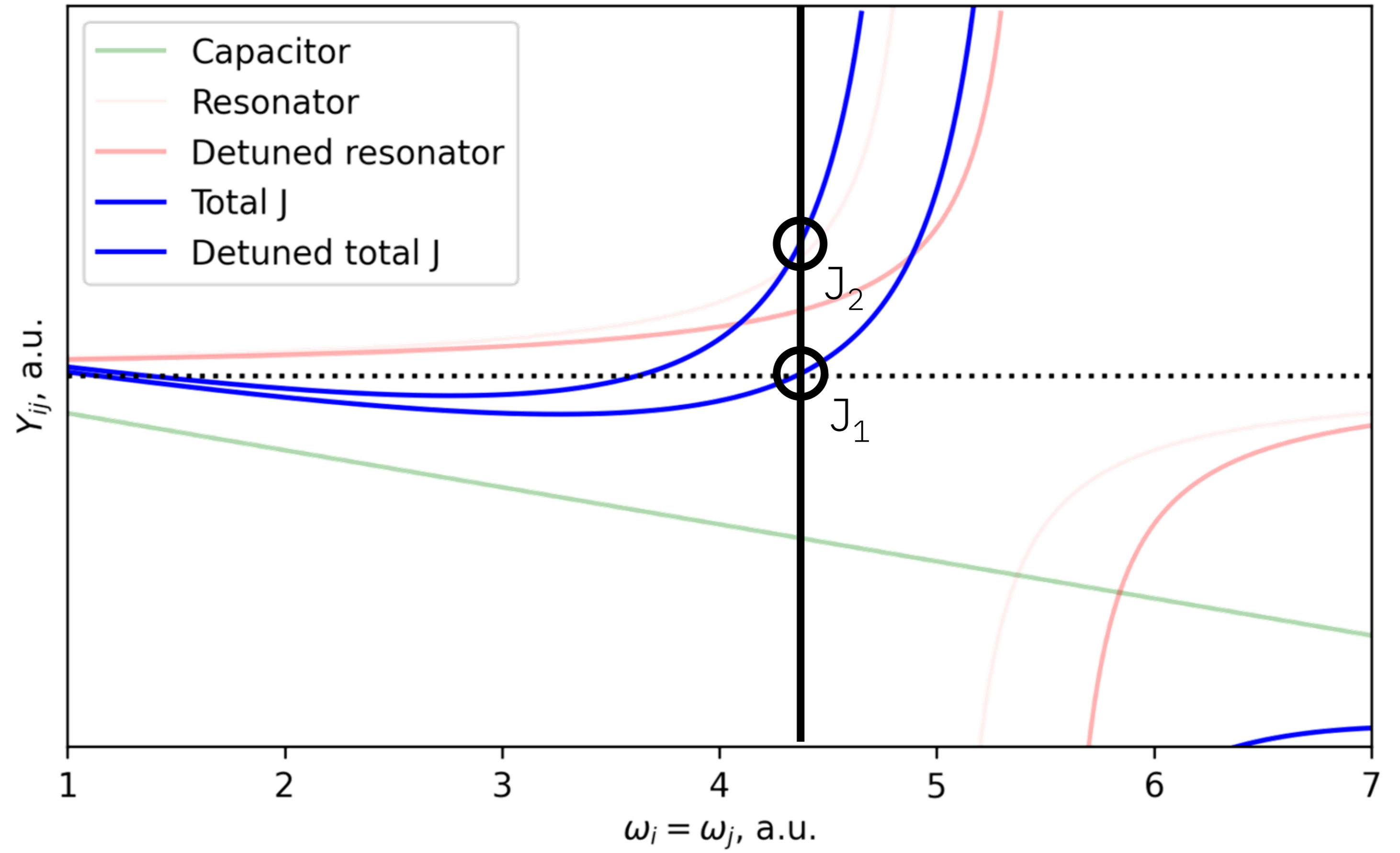
[1] F. Yan et al. "Tunable Coupling Scheme for Implementing High-Fidelity Two-Qubit Gates." Phys. Rev. Applied 10, 054062 (2018).

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Coupling qubits 101



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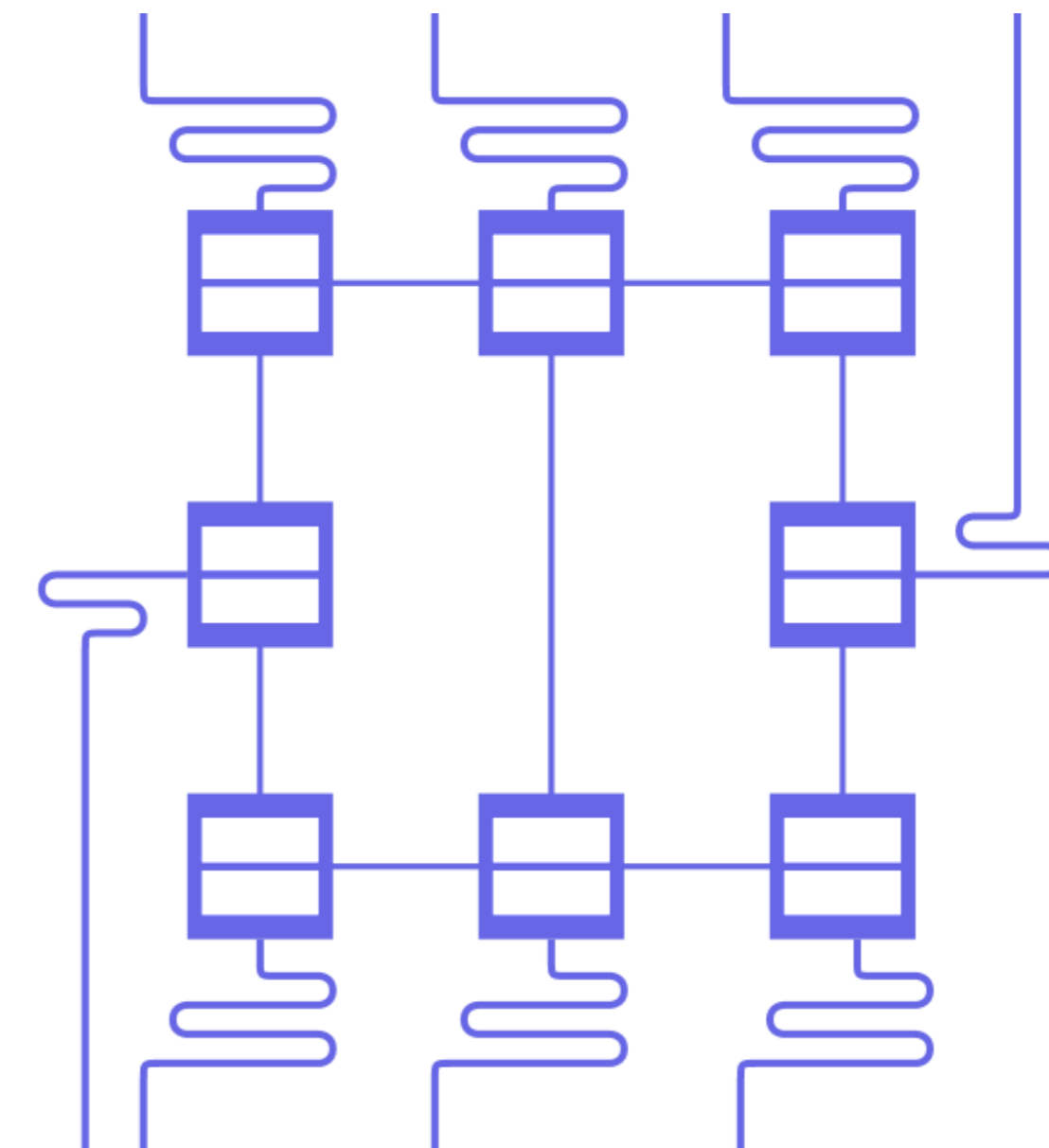
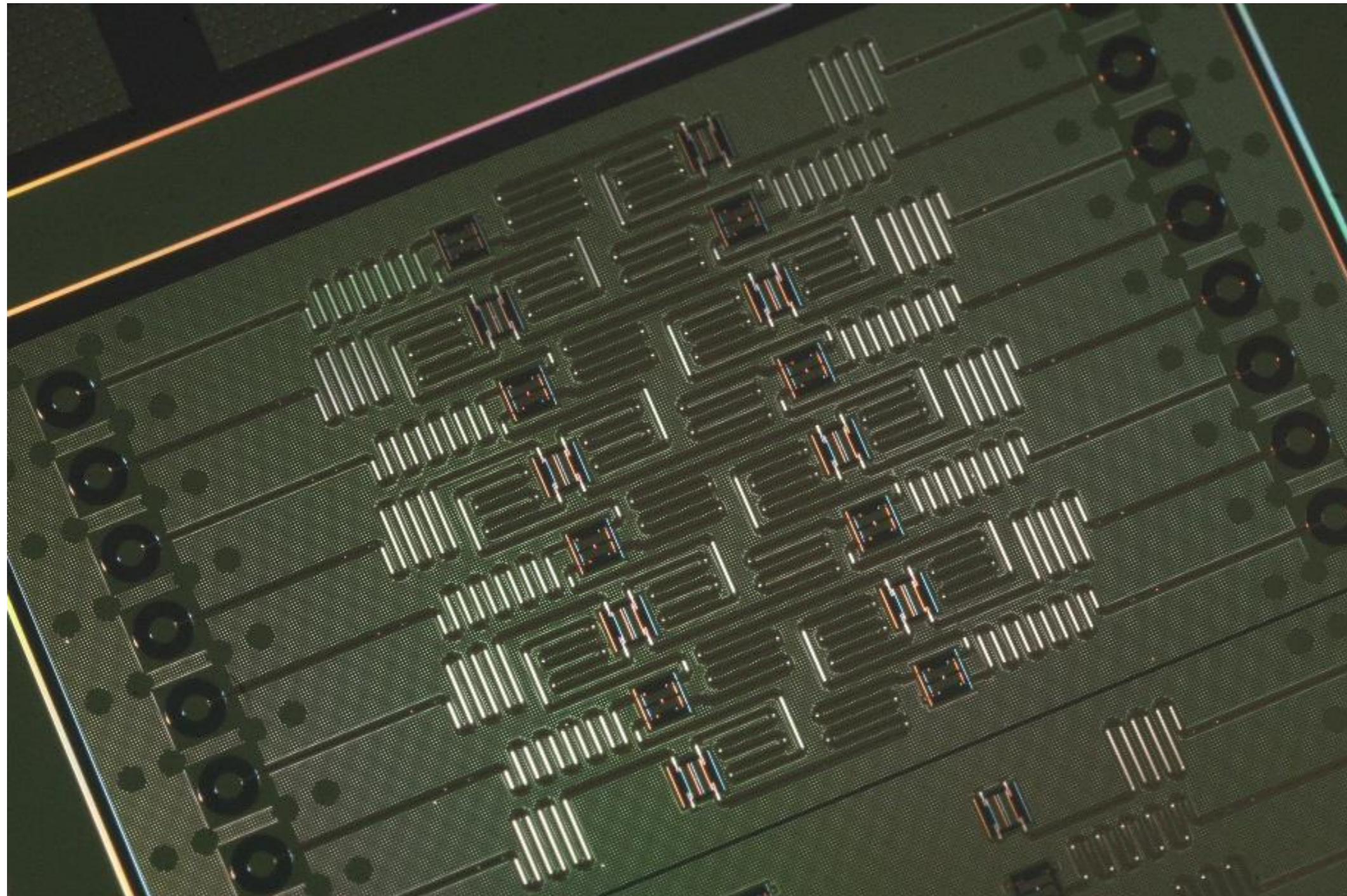
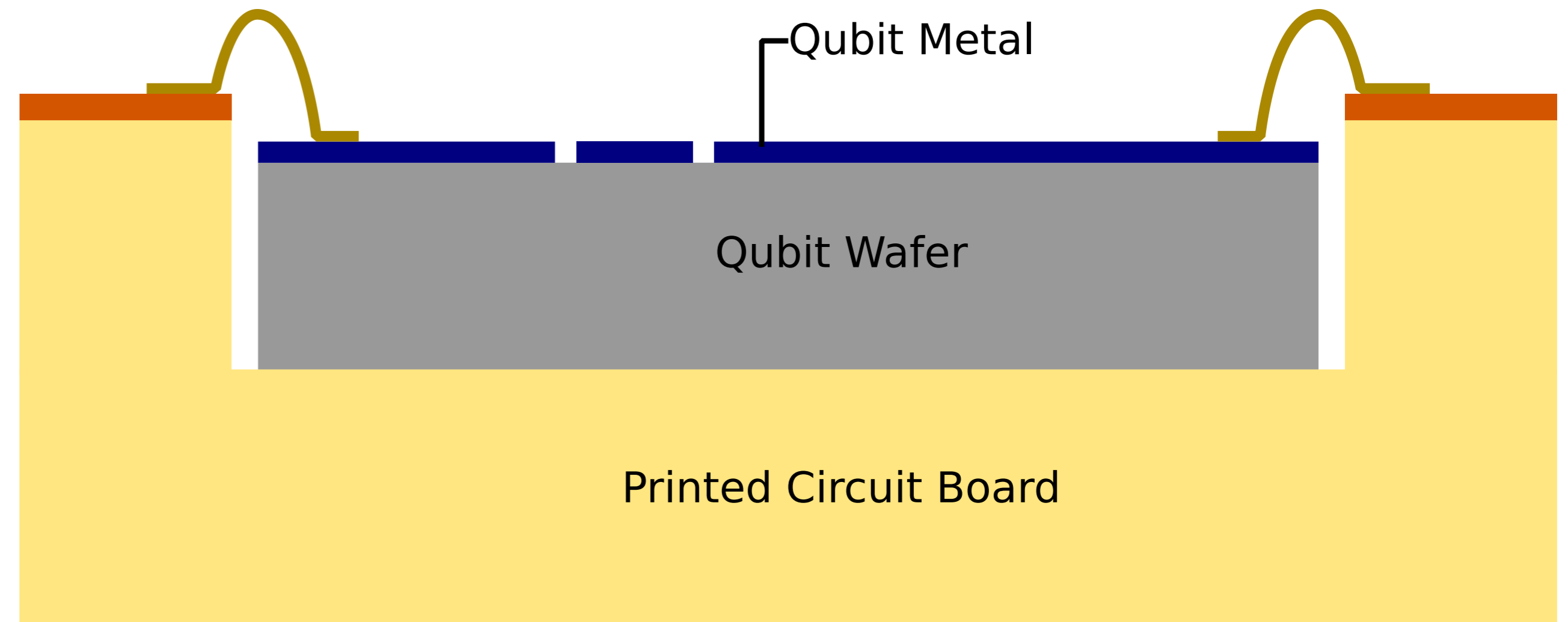
With techniques of F. Solgun et al., IEEE Transactions on Microwave Theory and Techniques 67(3) (2019).

Architecture



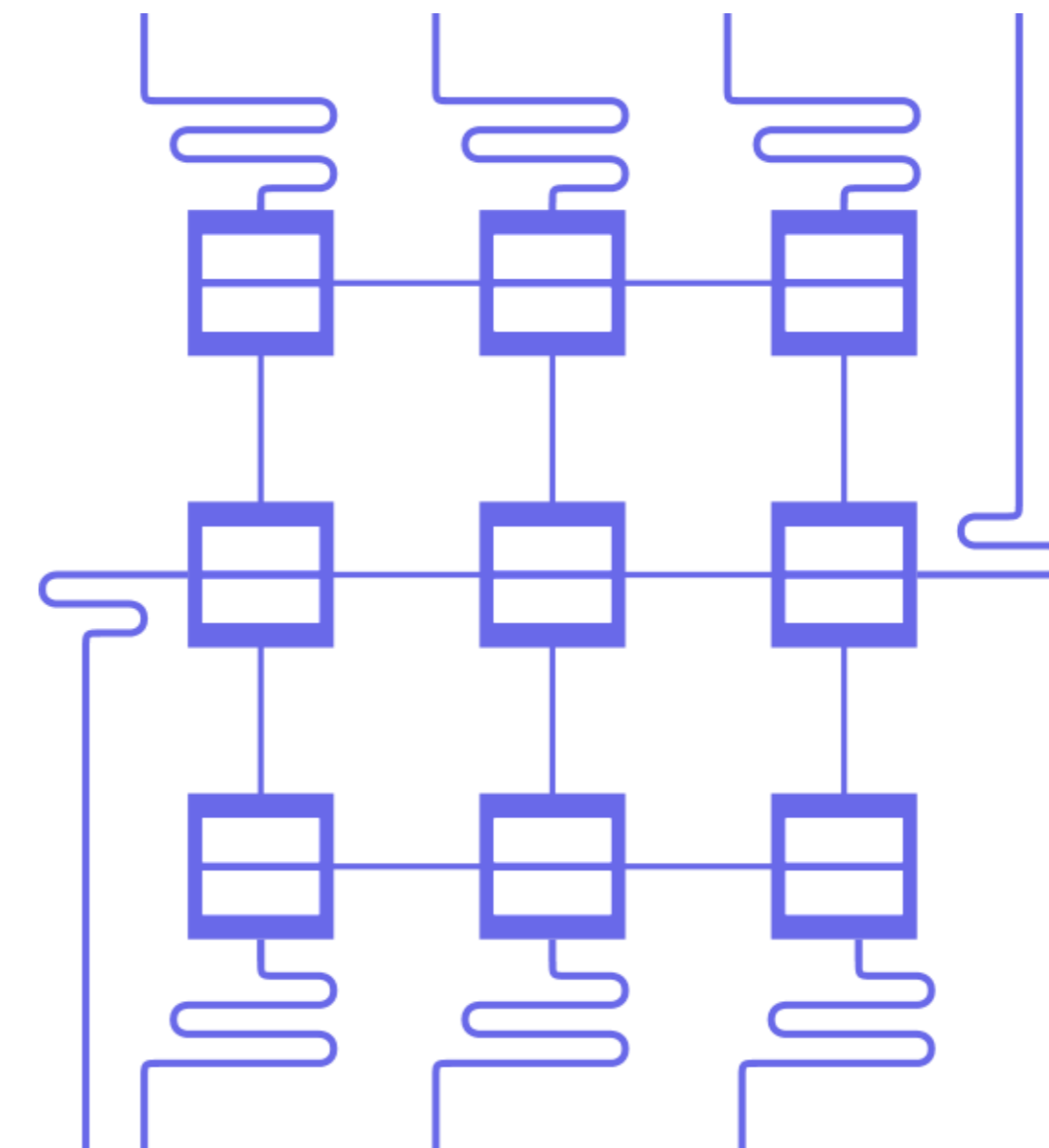
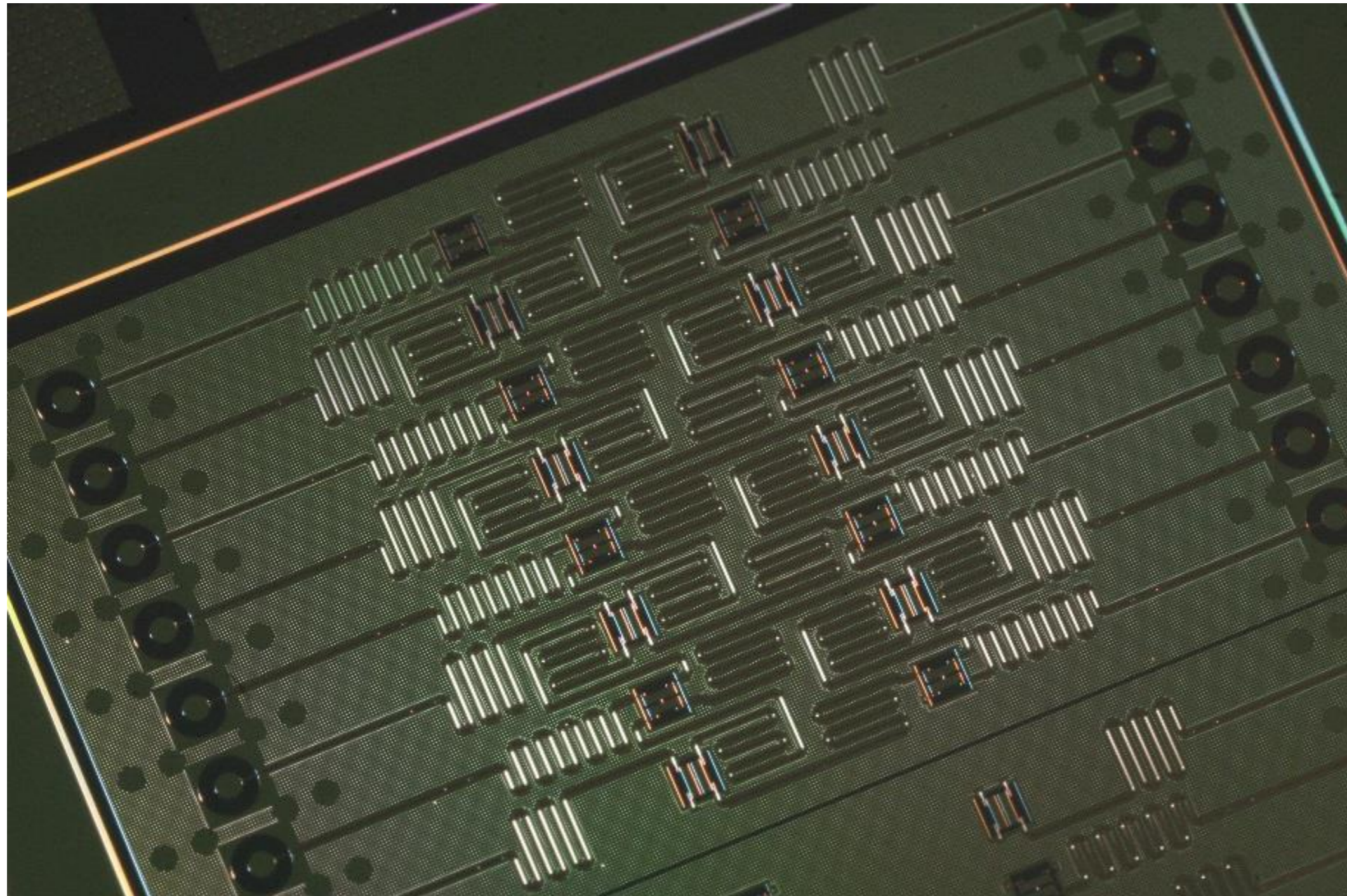
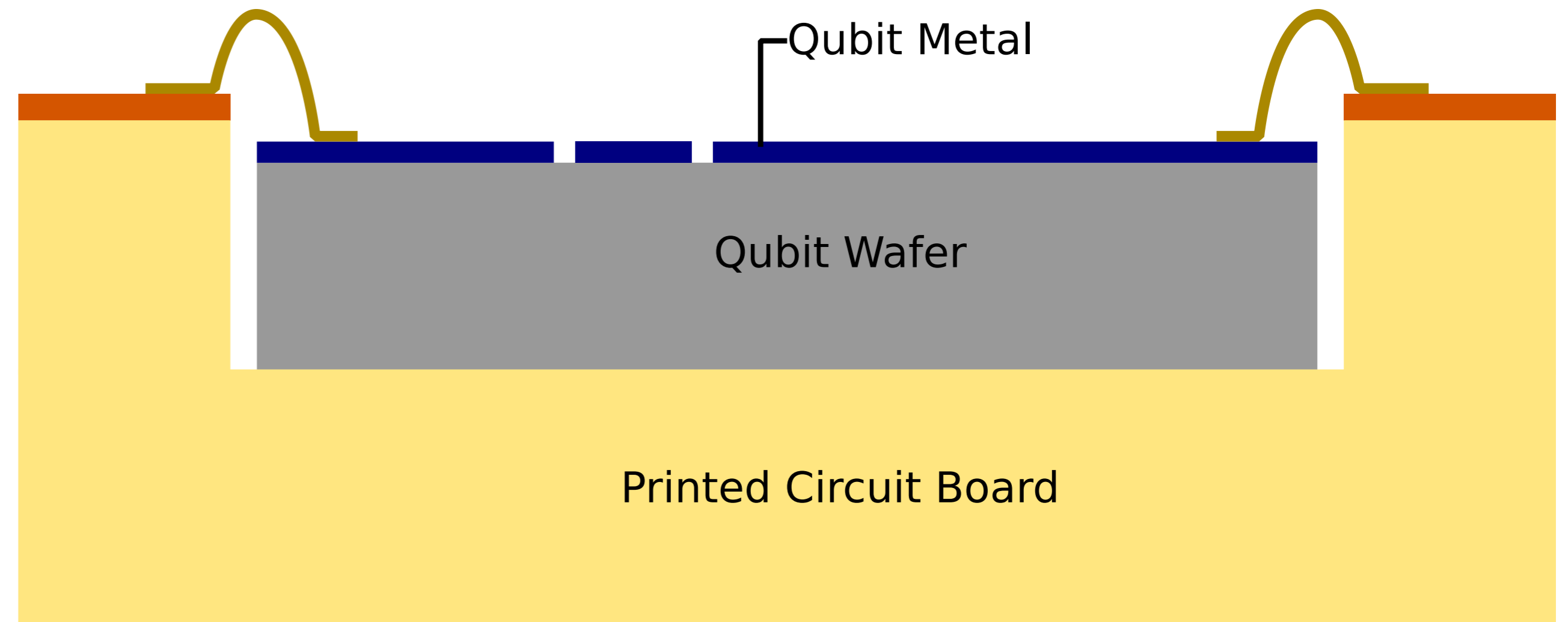
Evolution of Packaging Schemes: Generation 1

- Single layer of metal
 - Works fine for “Ring” topologies
 - Breaks down if there are any qubits inside ring



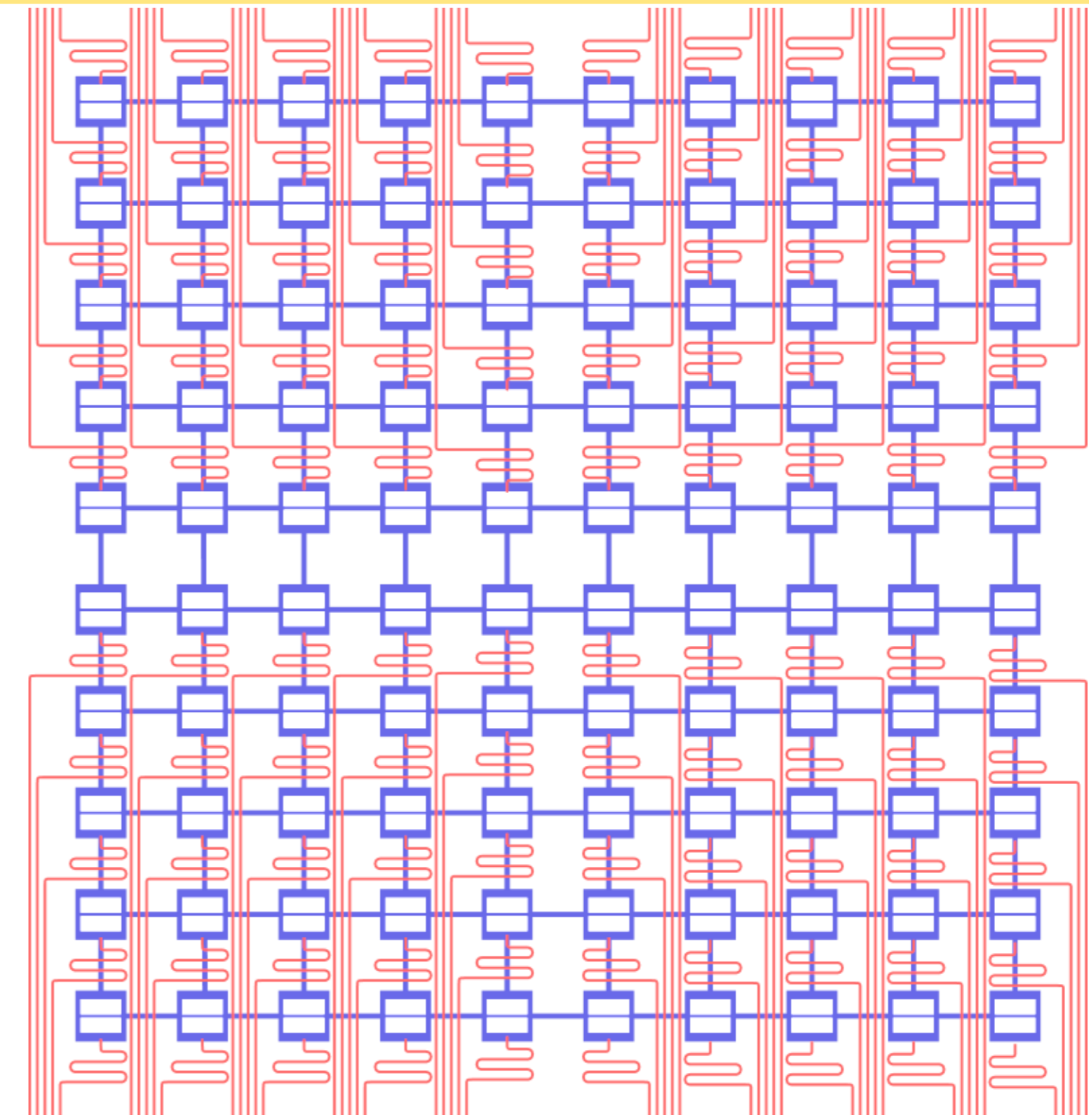
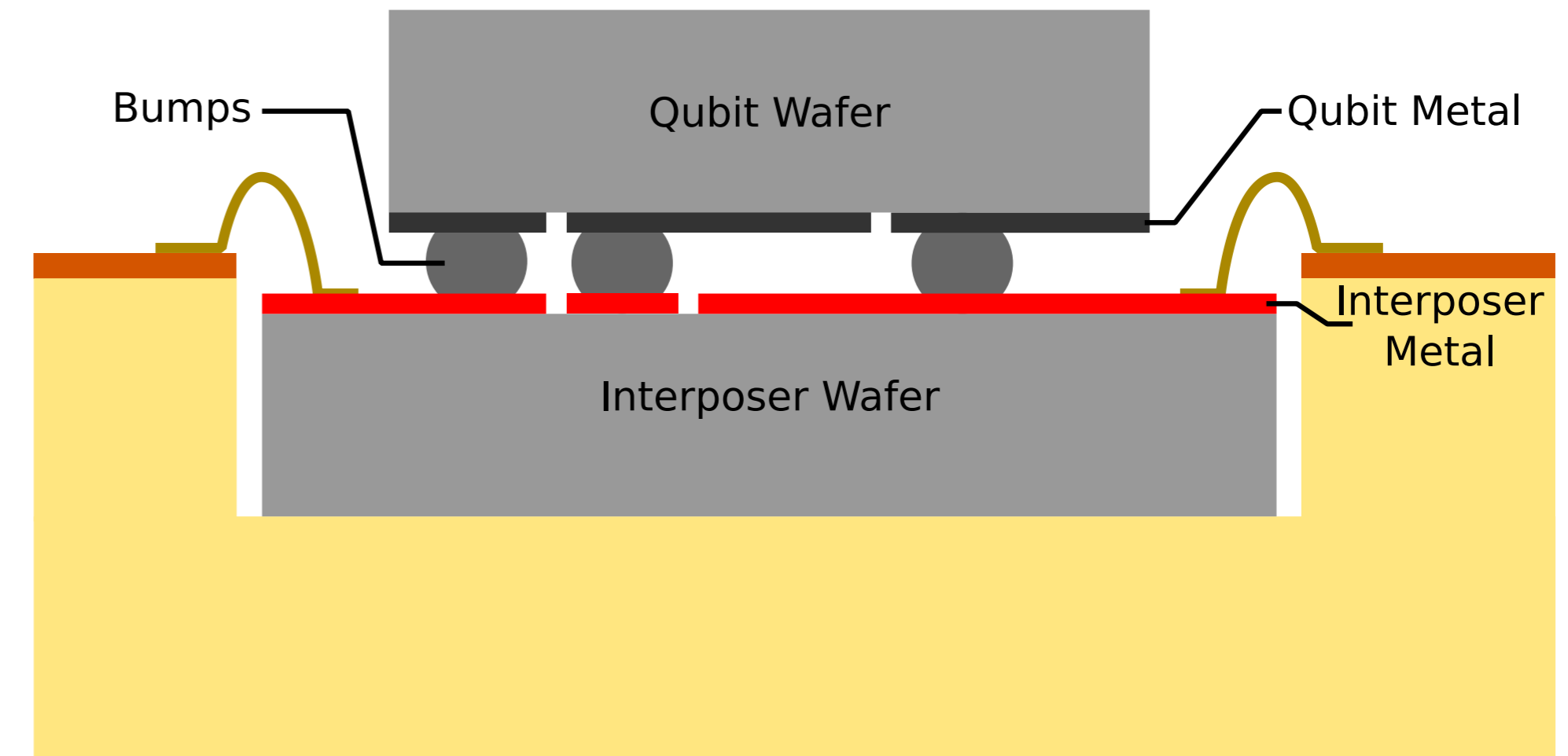
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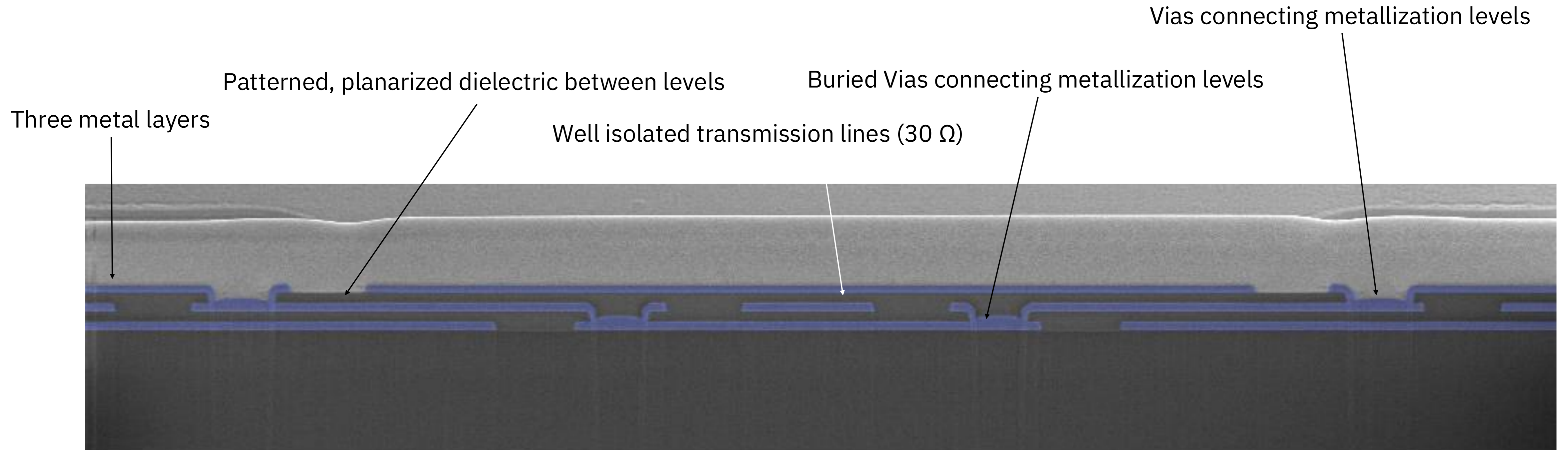


Evolution of Packaging Schemes: Generation 2

- Two separate chips, each with one layer of patterned metal
 - Joined via superconducting bump bonds
 - Allows nearest-neighbor qubit coupling
 - All control and readout lines must be routed to periphery of chip
 - Metal layers are not isolated from each other

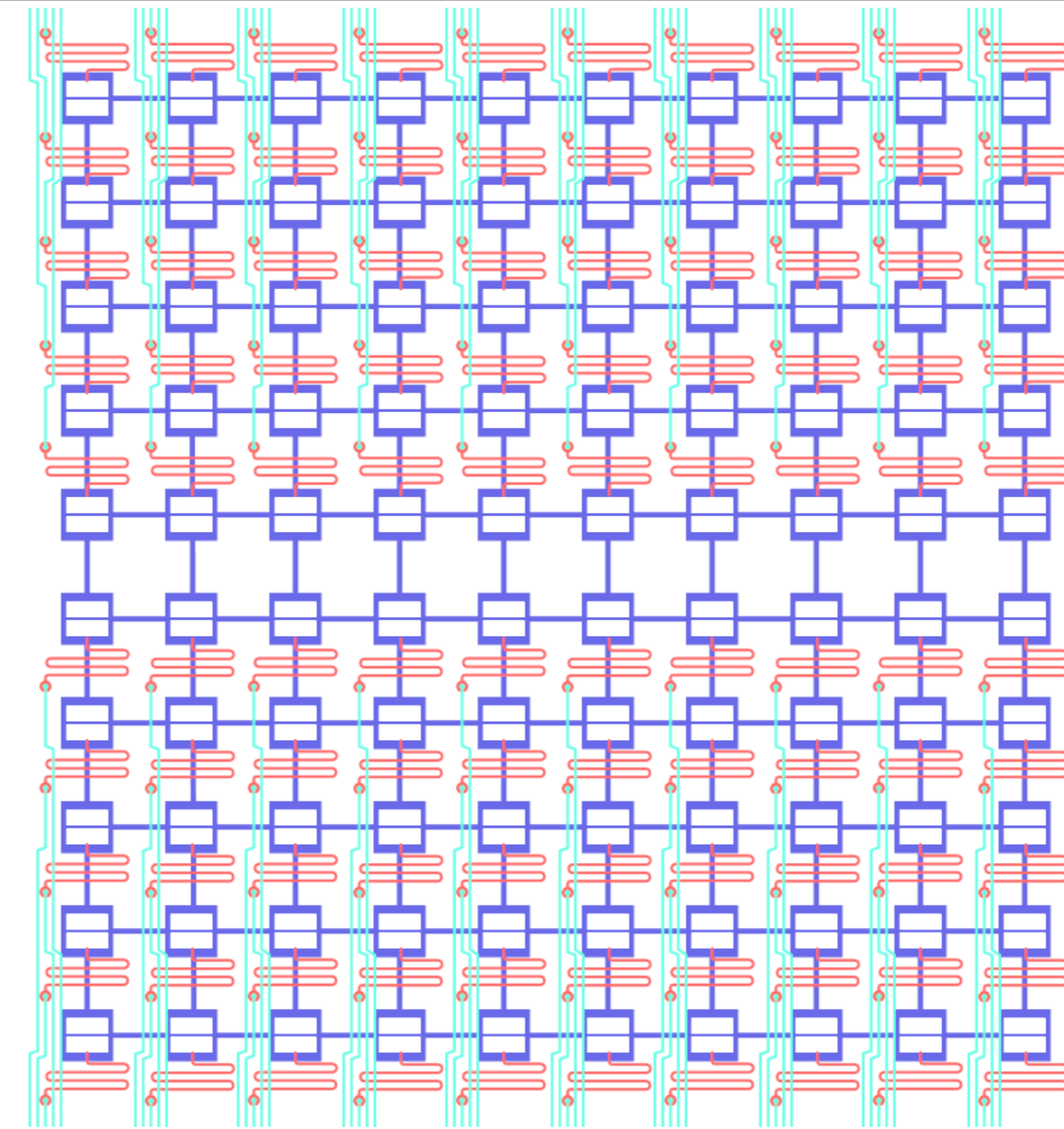
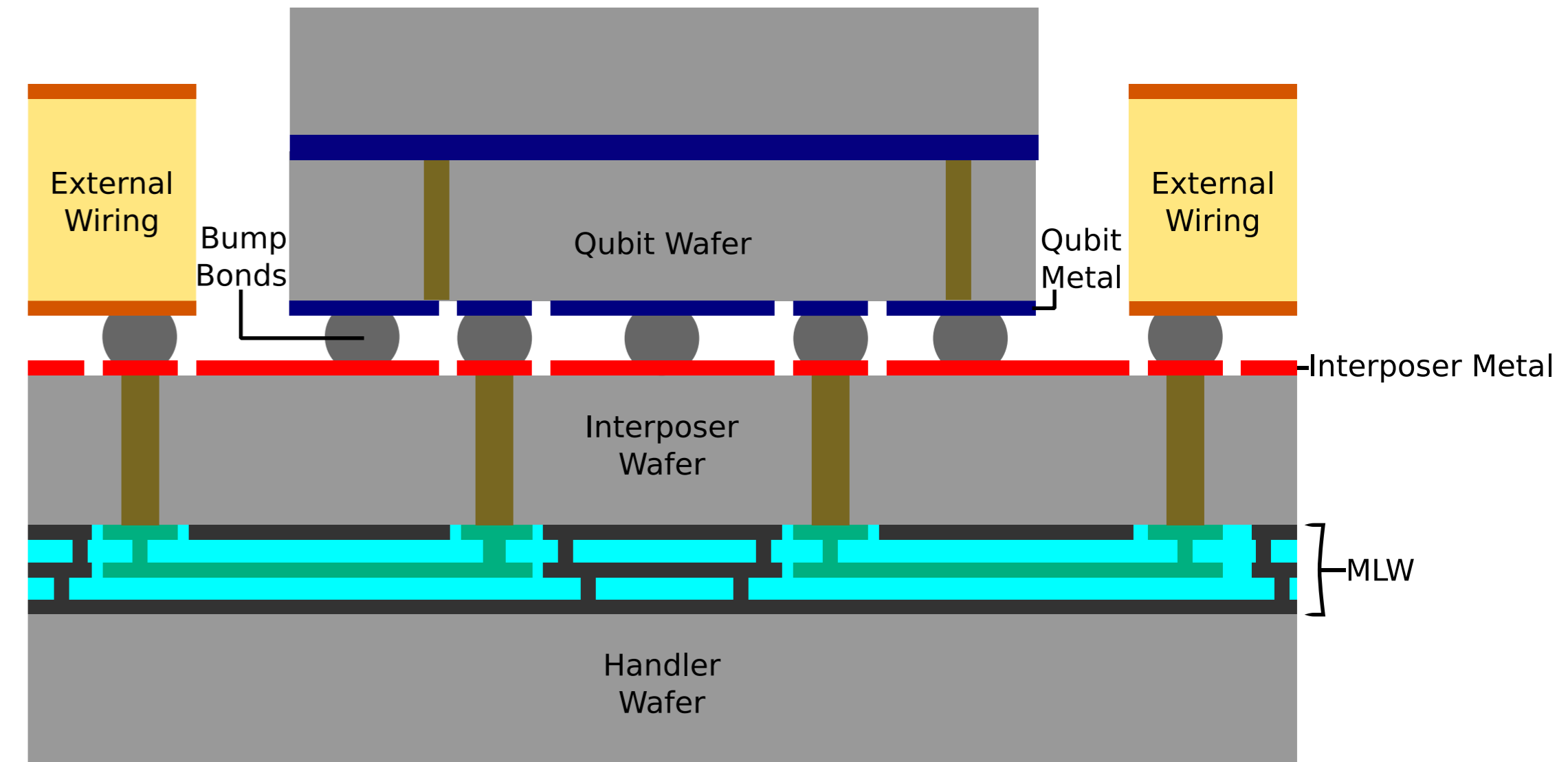


Beyond breaking the plane: Superconducting Multi-Layer Wiring



Evolution of Packaging Schemes: Generation 3

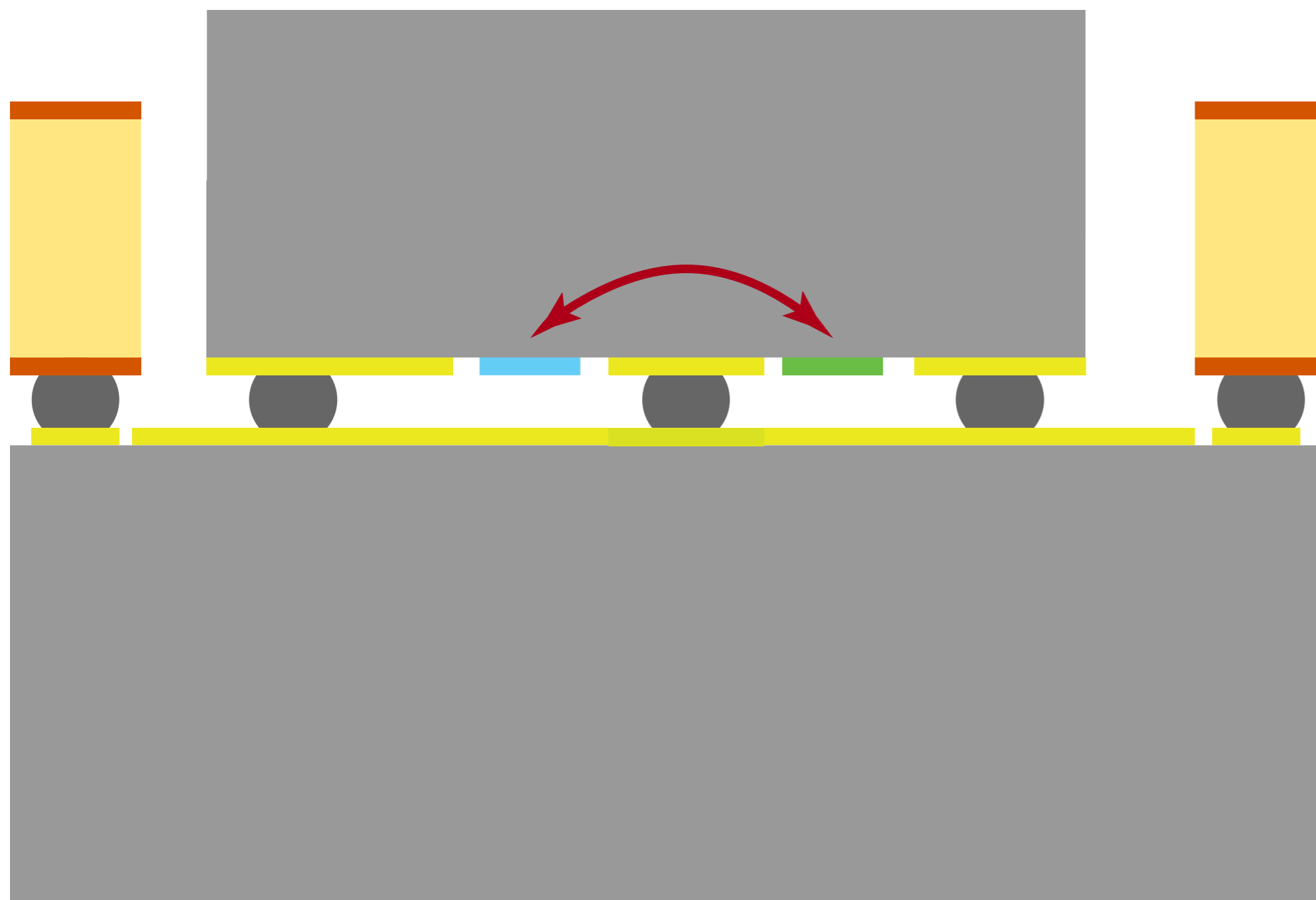
- Two chips, as before
 - Add “Multi-level Wiring” (MLW) level formed on backside of interposer
 - Control and readout signals routed as striplines in the MLW
 - Well isolated from Interposer and Qubit metal levels
 - Connect to MLW via superconducting Through-Substrate-Vias (TSVs)



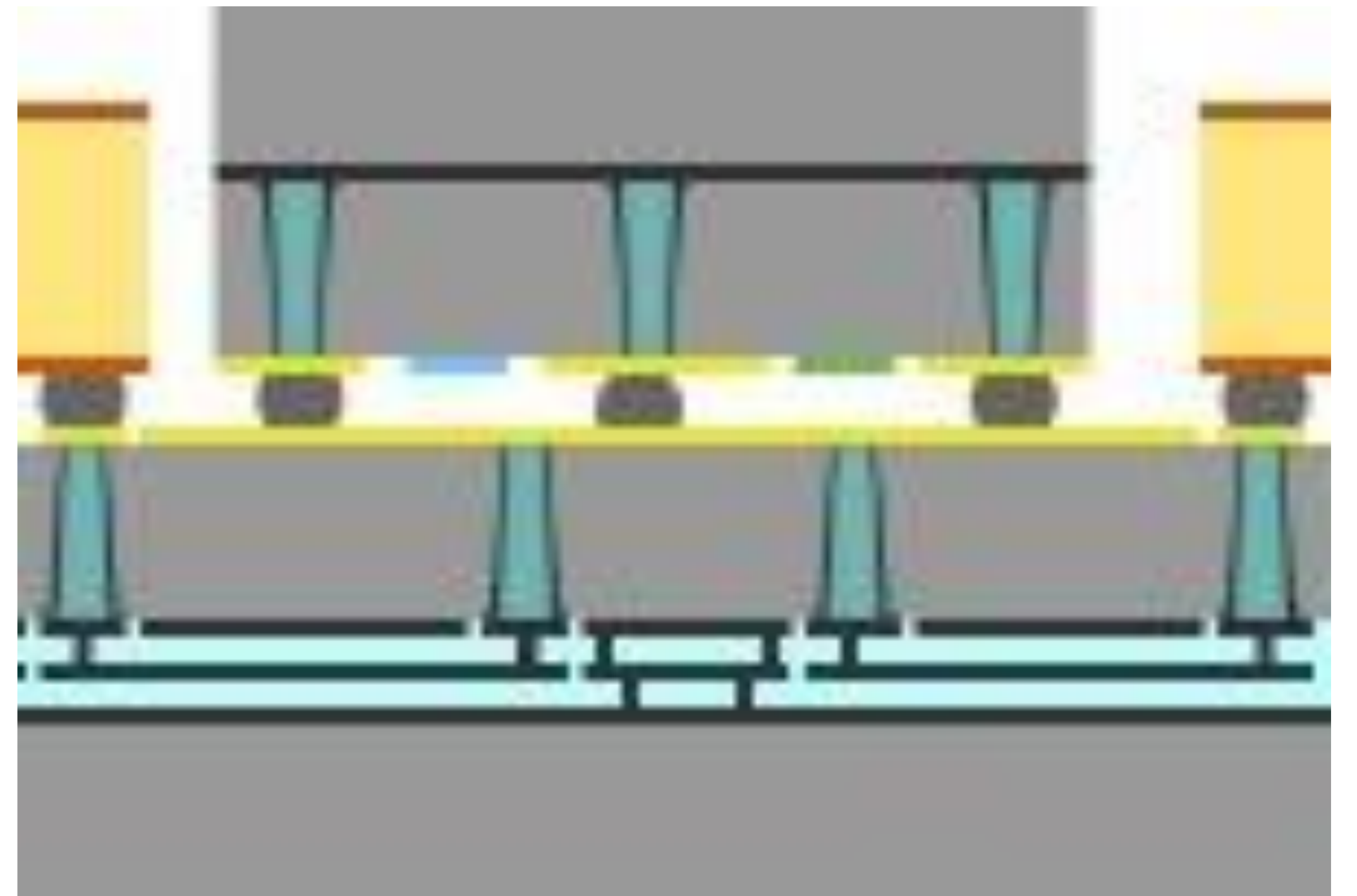
[1] Licata, T.J. et al. IBM Journal of R&D **39**. (1995)

[2] Edelstein, D. et al. International Electron Devices Meeting. IEDM Technical Digest (1997)

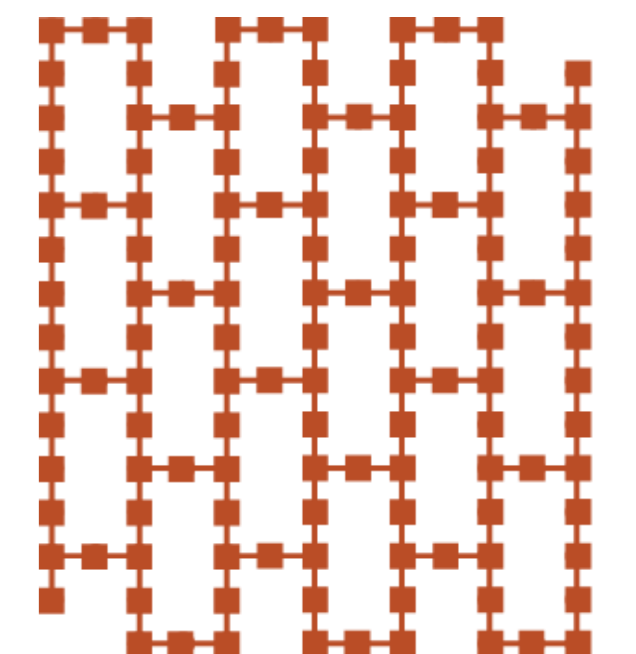
Crosstalk



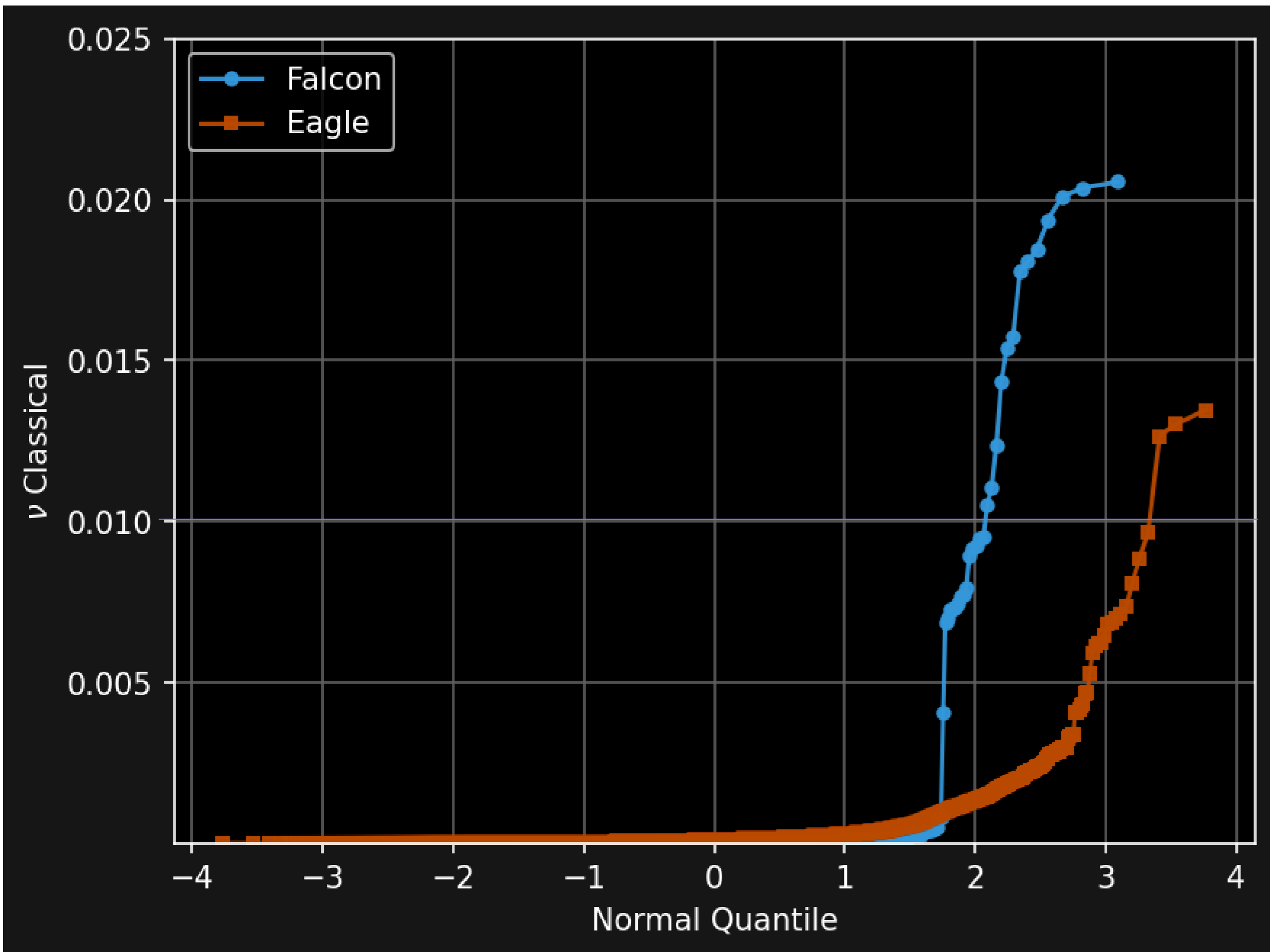
Generation 2 = Falcon
(via fencing impossible)



Generation 3 = Eagle
(via fencing possible)



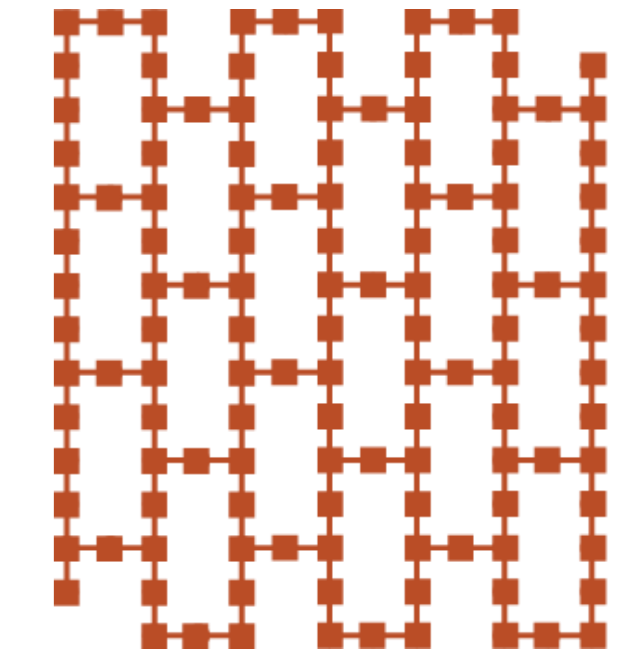
Crosstalk



Falcon



Eagle



Many fewer (as a fraction) high fliers in crosstalk on Eagle

Which pairs of qubits have high crosstalk is consistent from chip-to-chip in both instances

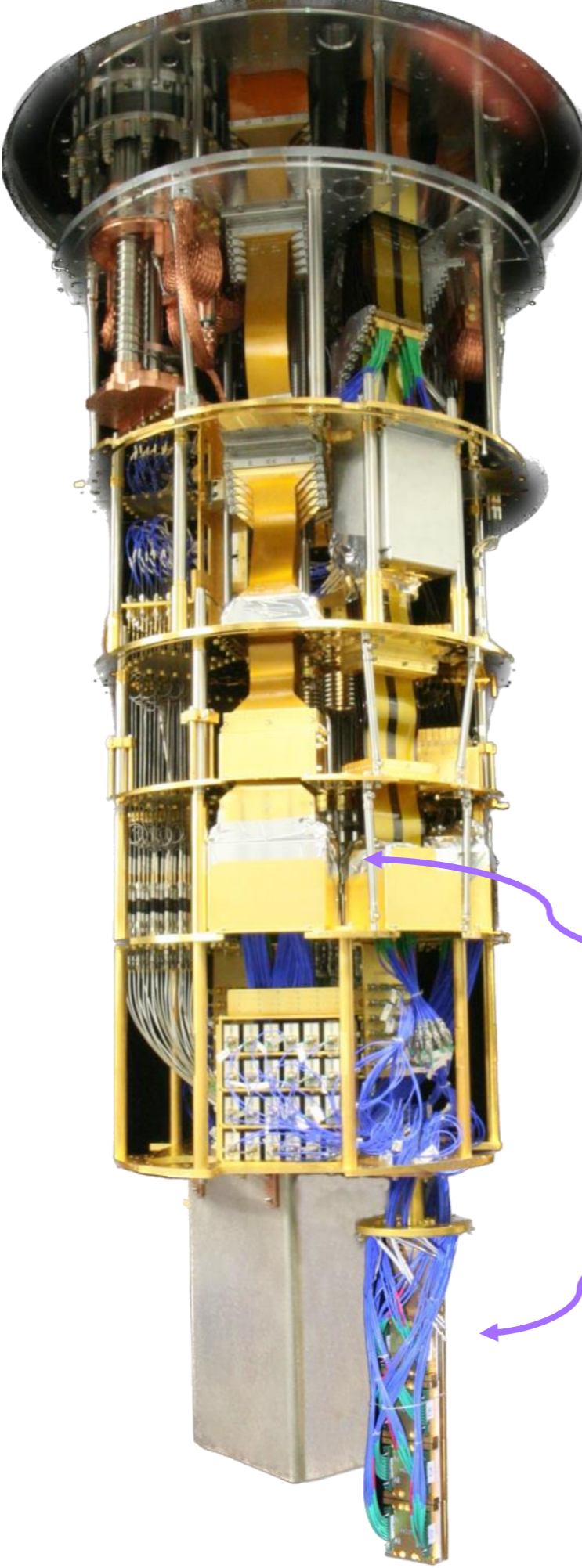
Eagle has 16,000 pairs of qubits! If measured 1 by 1, finding the 3 qubits with >1% crosstalk would take 11 days...



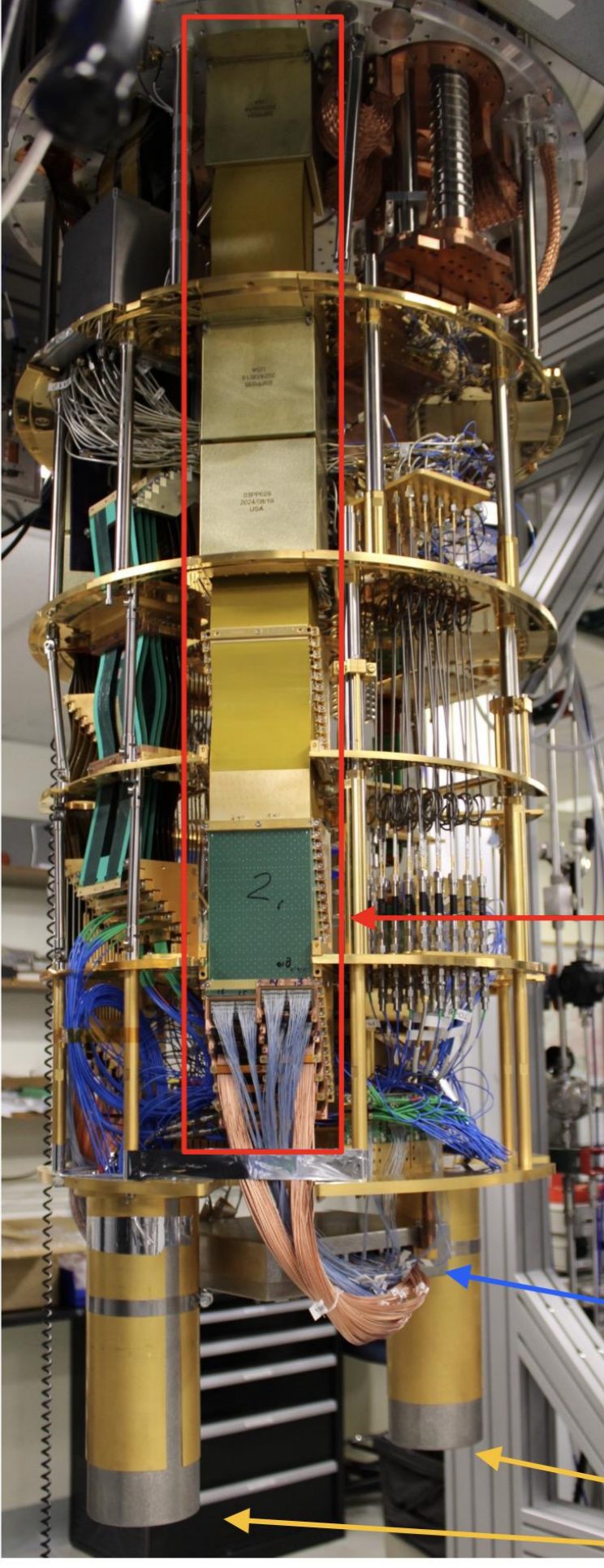
Scaling number of qubits in a single cryogenic fridge with better signal lines (Flex)



10x increase
→



4x increase
→



Configuration for 50 cross-resonance qubits

Configuration for 500 cross-resonance qubits

Configuration for 1000 tunable coupler qubits (additional signal lines per qubit)

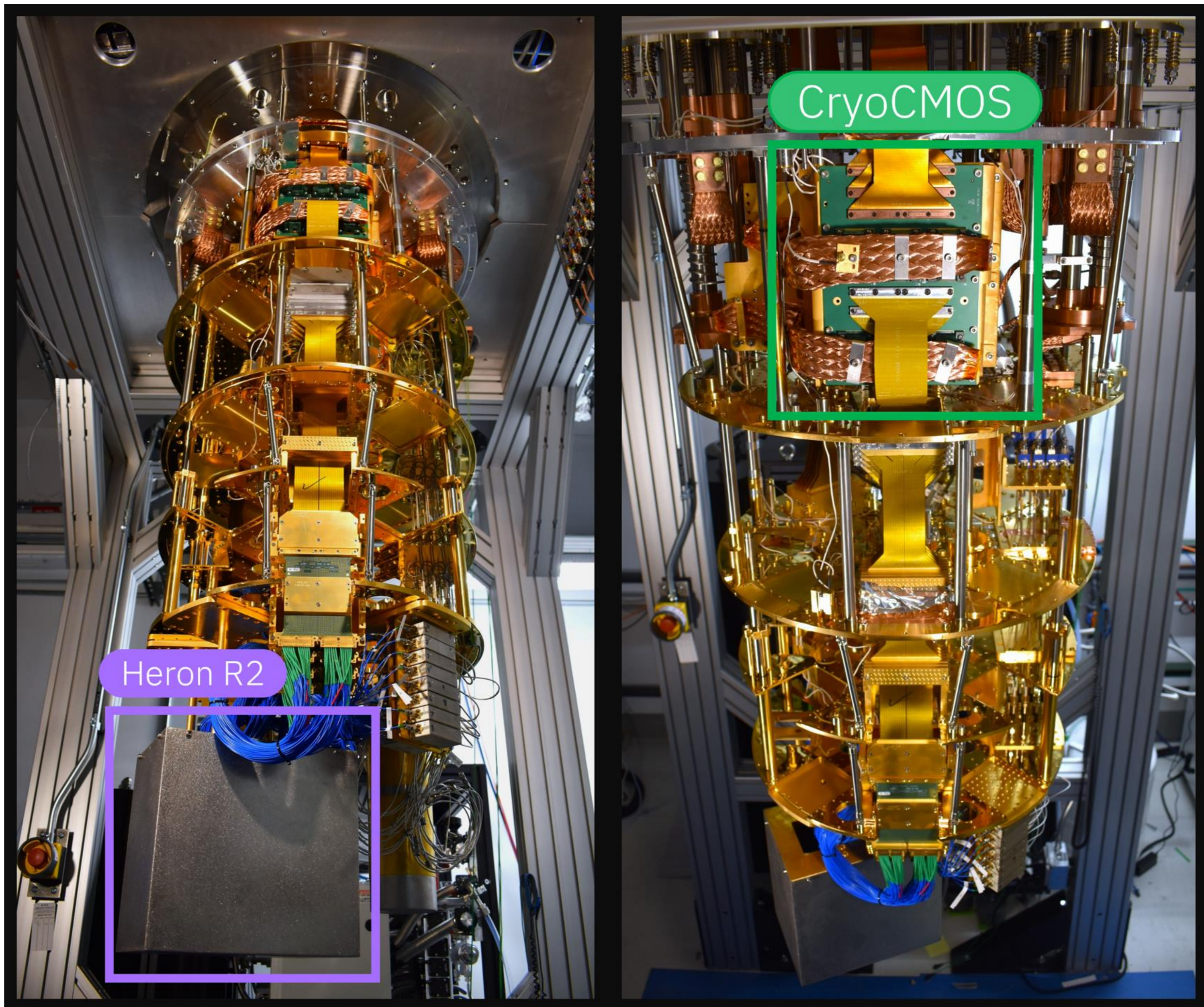
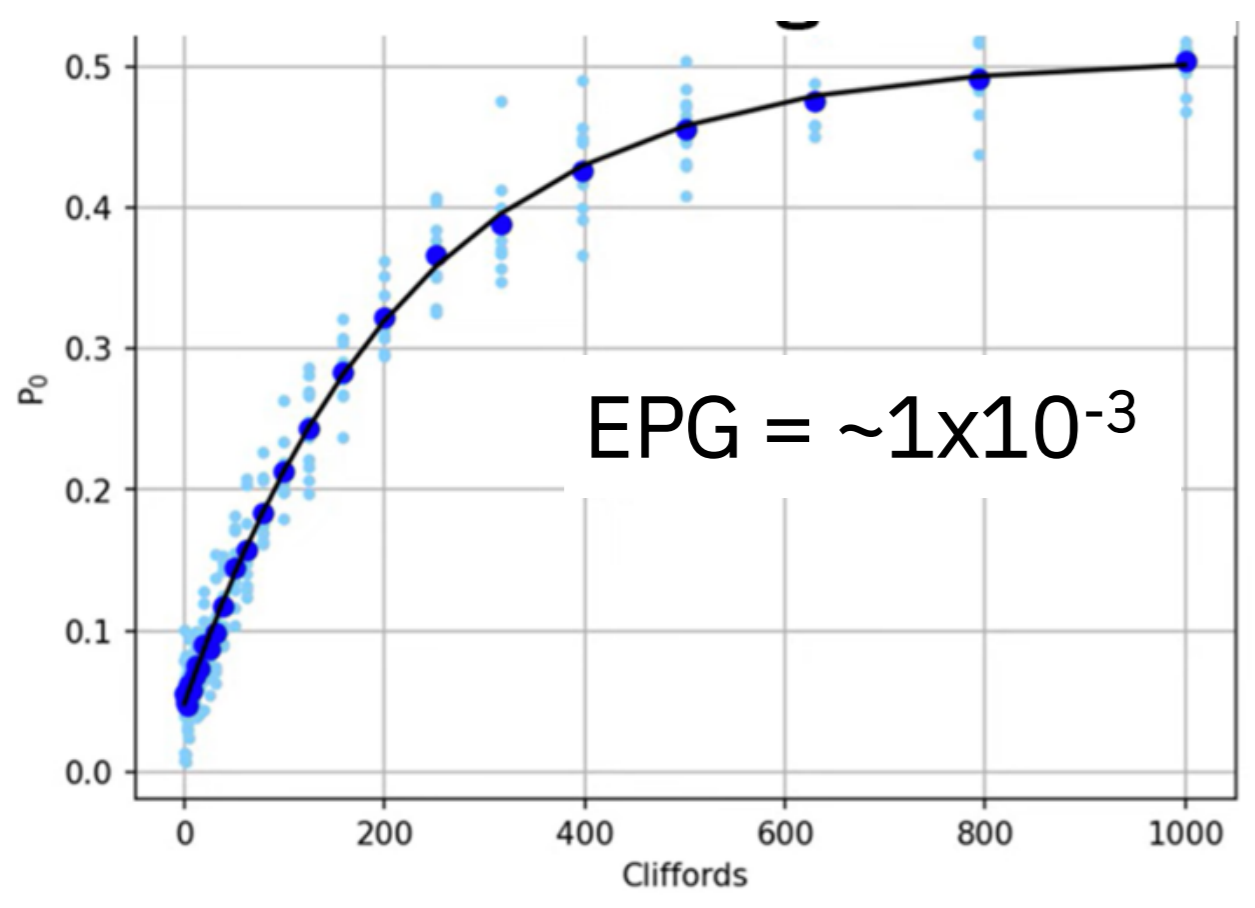
Coaxial cables
attenuation

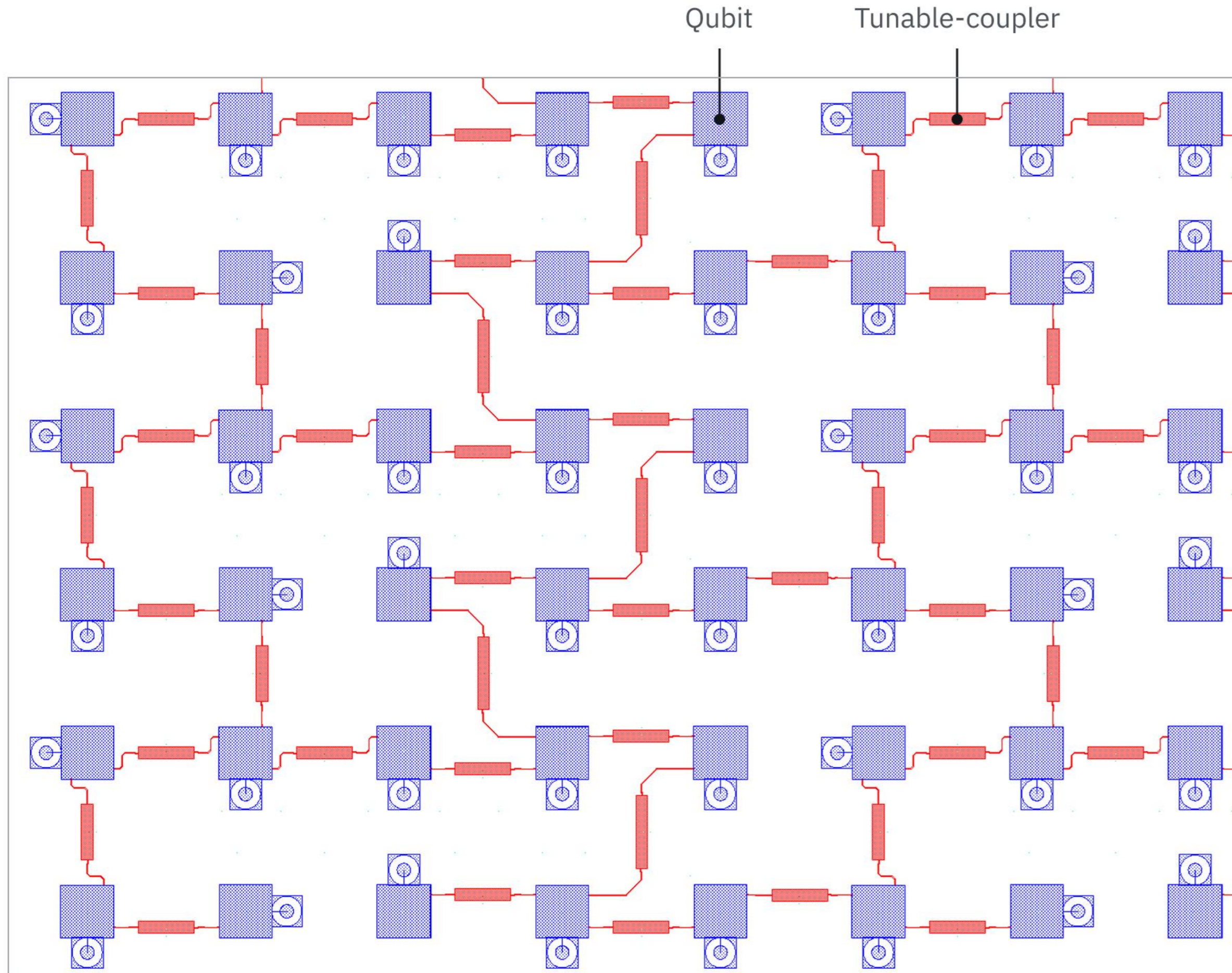
Modular I/O wiring and space transformers
Modular amplifiers and other microwave components

Gen3 flex bay
Crossbill payload
TWPA cans

Cryo-CMOS for scalable control

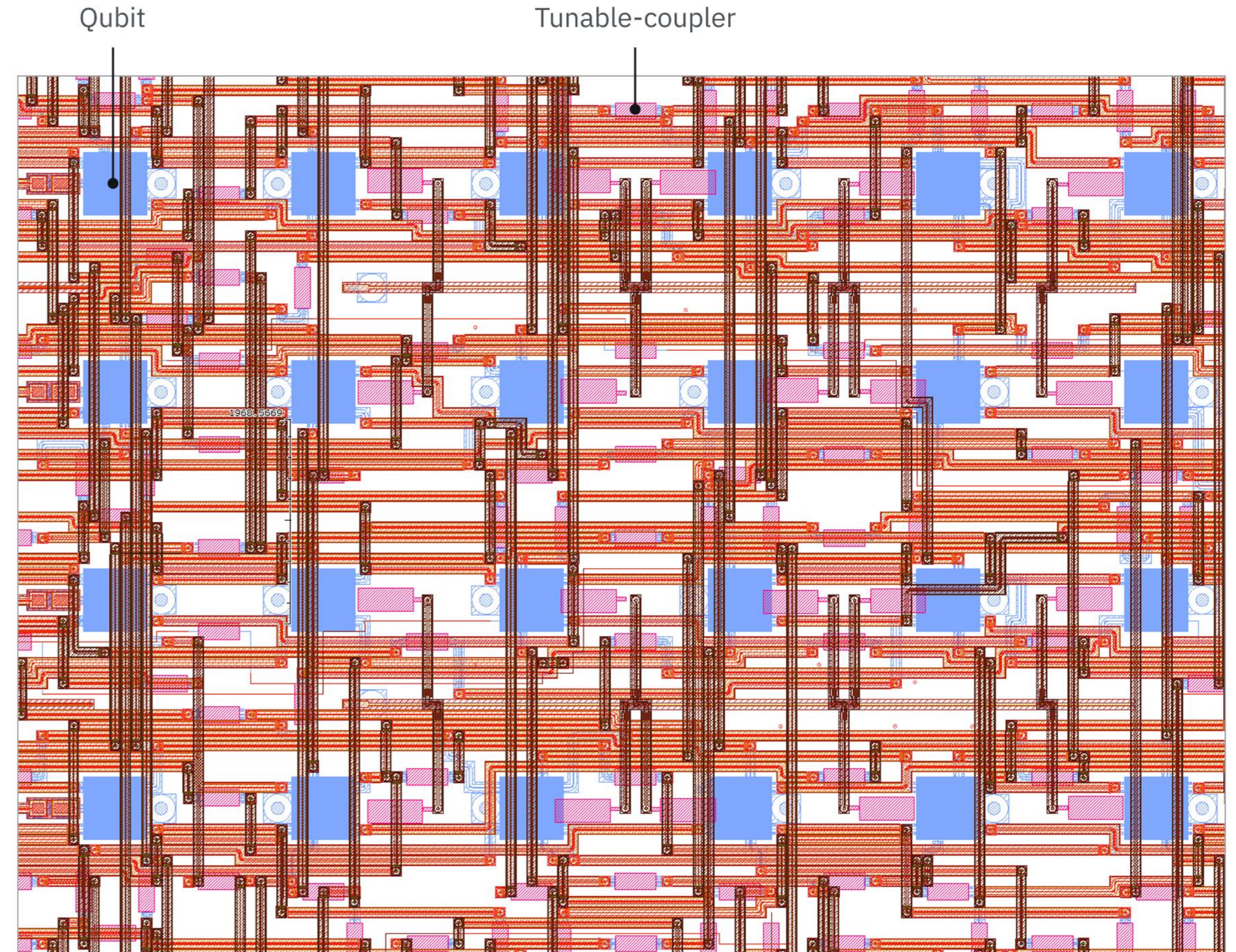
- Overcome control bottlenecks into and out of cryostat
- 94 tunable couplers on a Heron device controlled with 12 “Cedar” cryo-CMOS AWGs on two printed circuit boards
- Gate fidelities as high as 99.9%
- Integrated with conventional RF control and readout hardware as well as software stack.





Heron architecture

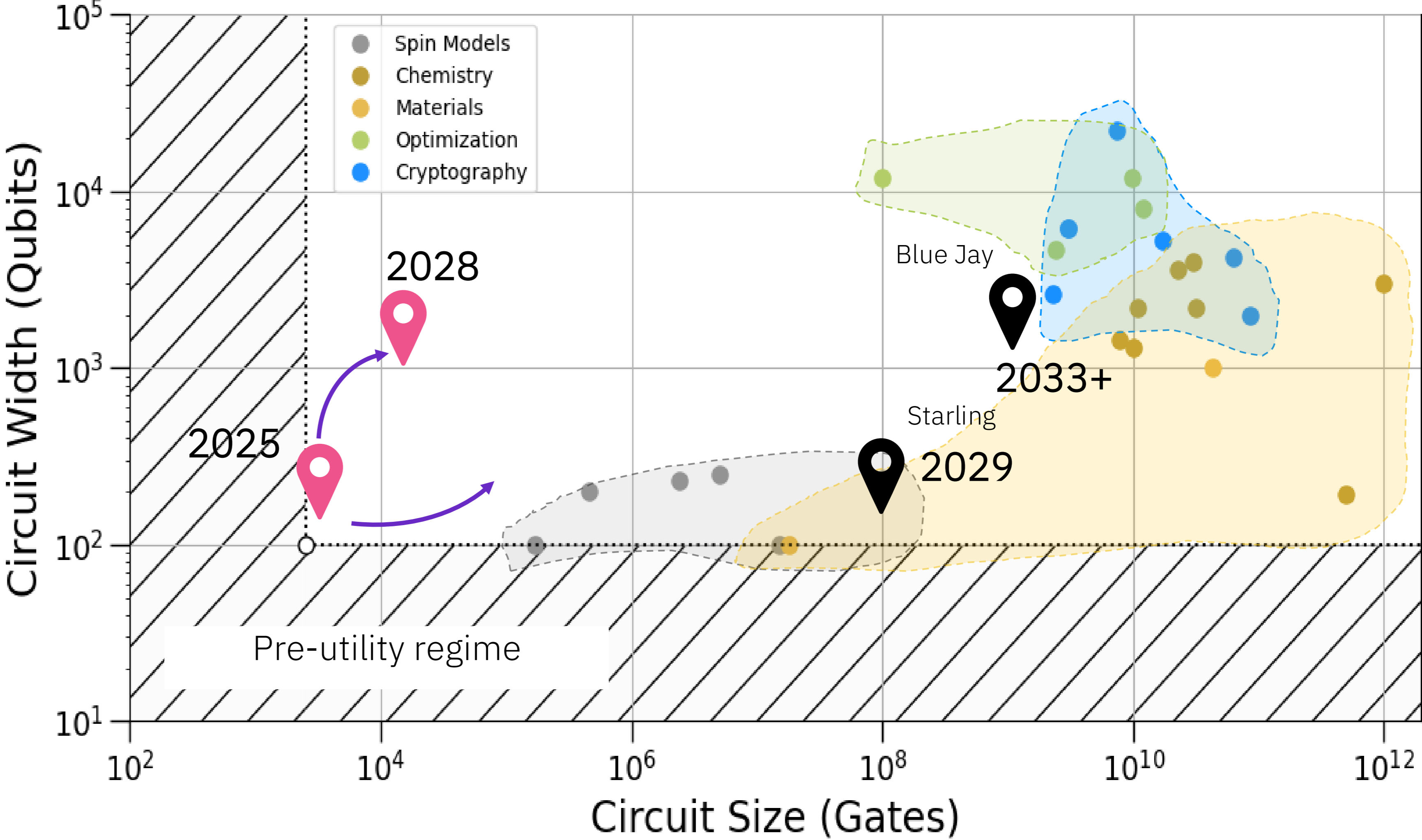
Above is a schematic of IBM's lattice for connecting qubits within its IBM Quantum Heron processor, in which the blue boxes represent qubits and the red lines and boxes represent connectors, or couplers.



Loon architecture

Above is a schematic of IBM's forthcoming quantum processor architecture, beginning to be developed in 2025 with the IBM Quantum Loon processor, which depicts a more complex lattice to allow a vastly increased number of connections between the qubits.

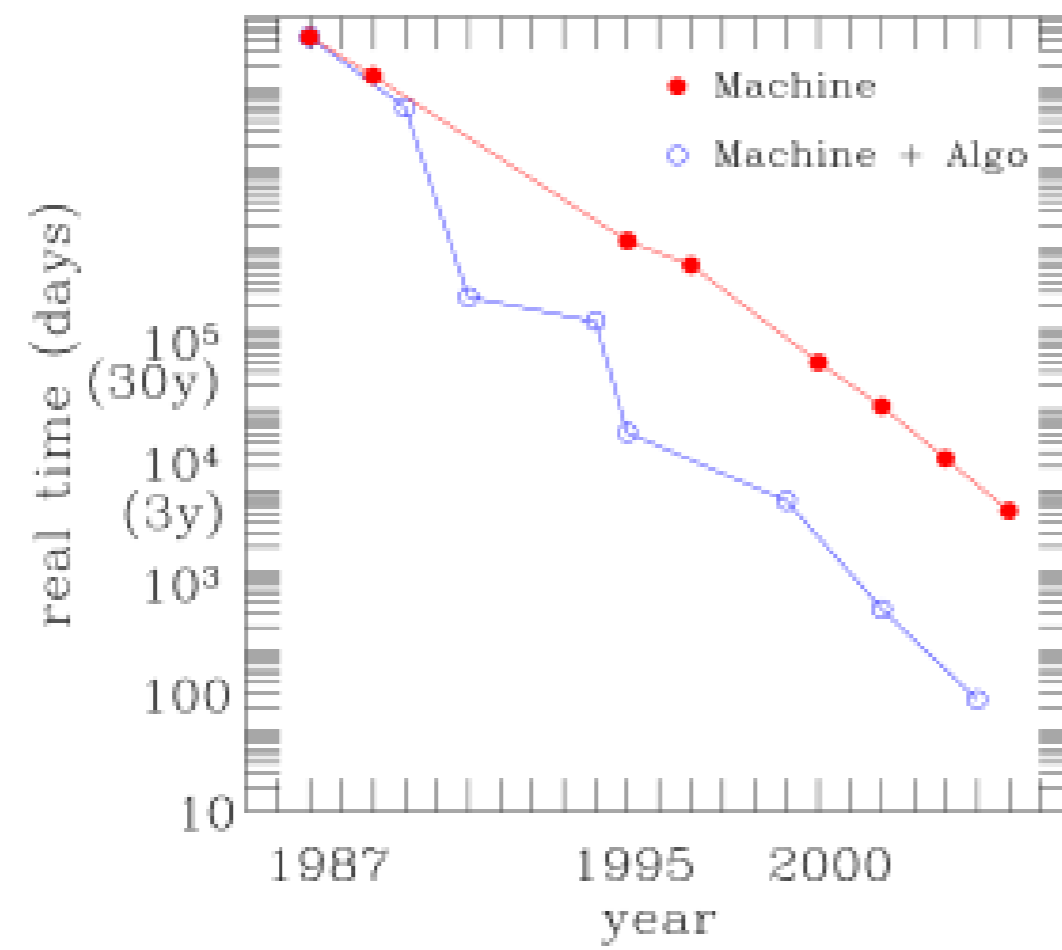
What can you do with a large-scale, fault-tolerant quantum computer?



Algorithmic advances..

Computer and algorithm development over the years

time estimates for simulating $32^3 \cdot 64$ lattice, 5000 configurations



→ O(few months) nowadays with a typical collaboration
supercomputer contingent

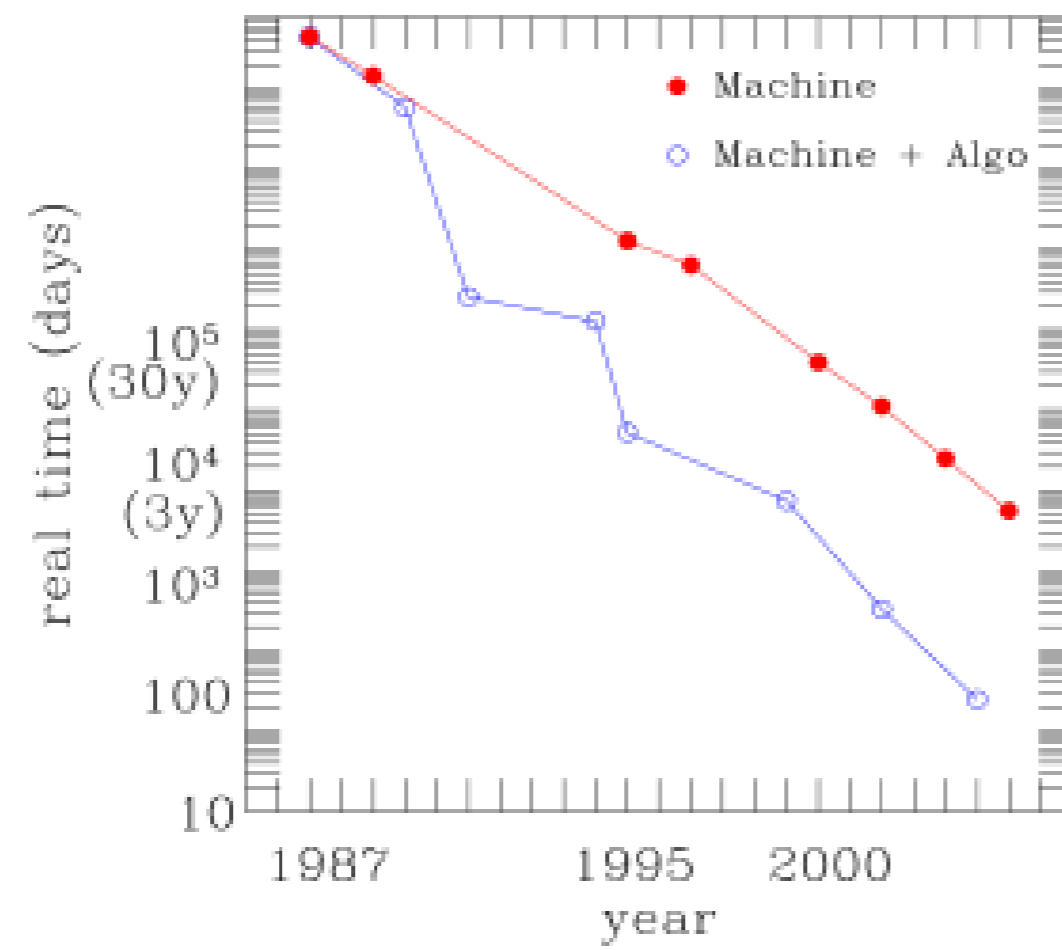
Courtesy Karl Jansen, CQTA DESY

Algorithmic vs. compute improvements in simulating a lattice gauge theory

And discovery

Computer and algorithm development over the years

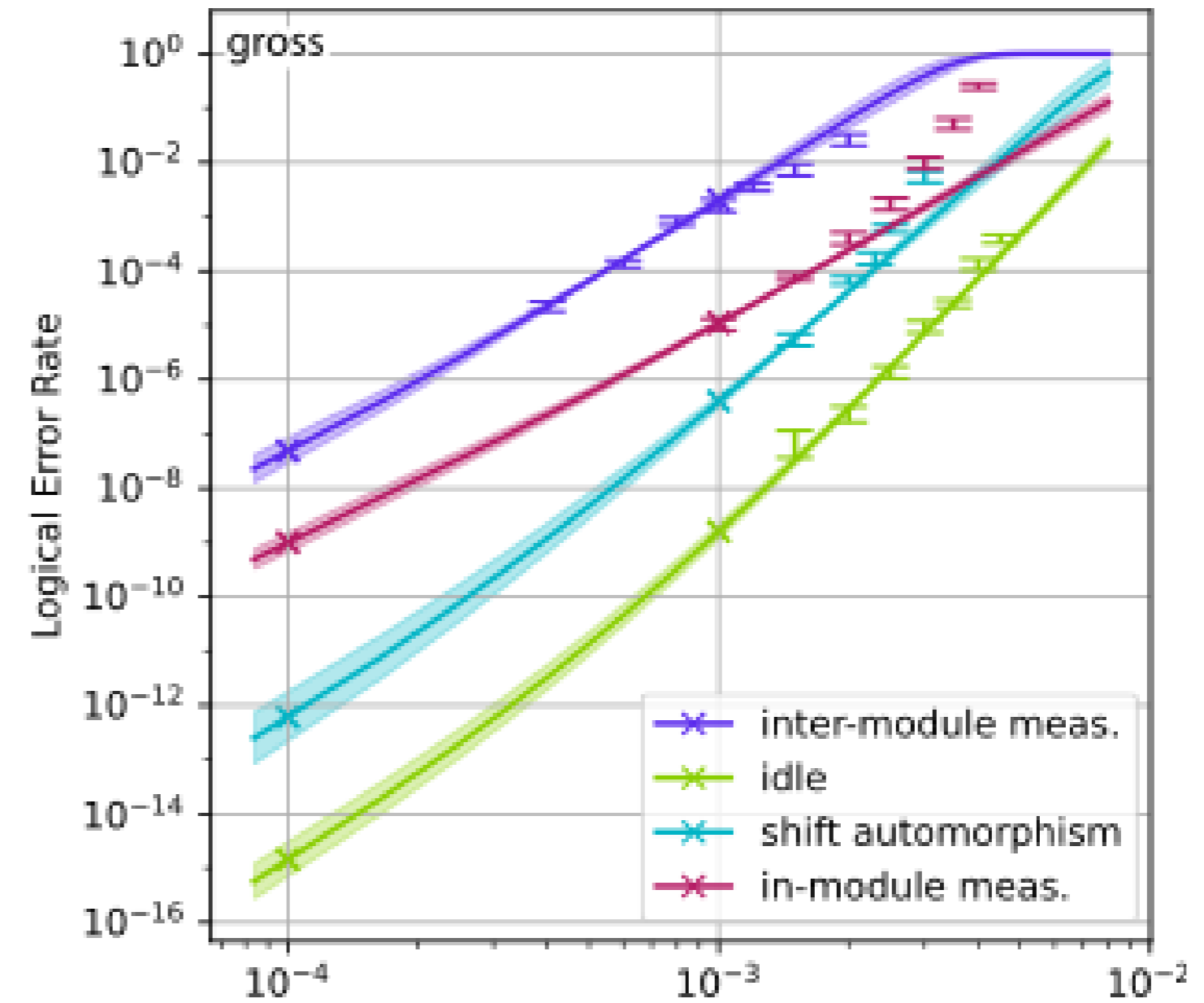
time estimates for simulating $32^3 \cdot 64$ lattice, 5000 configurations



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Courtesy Karl Jansen, CQTA DESY

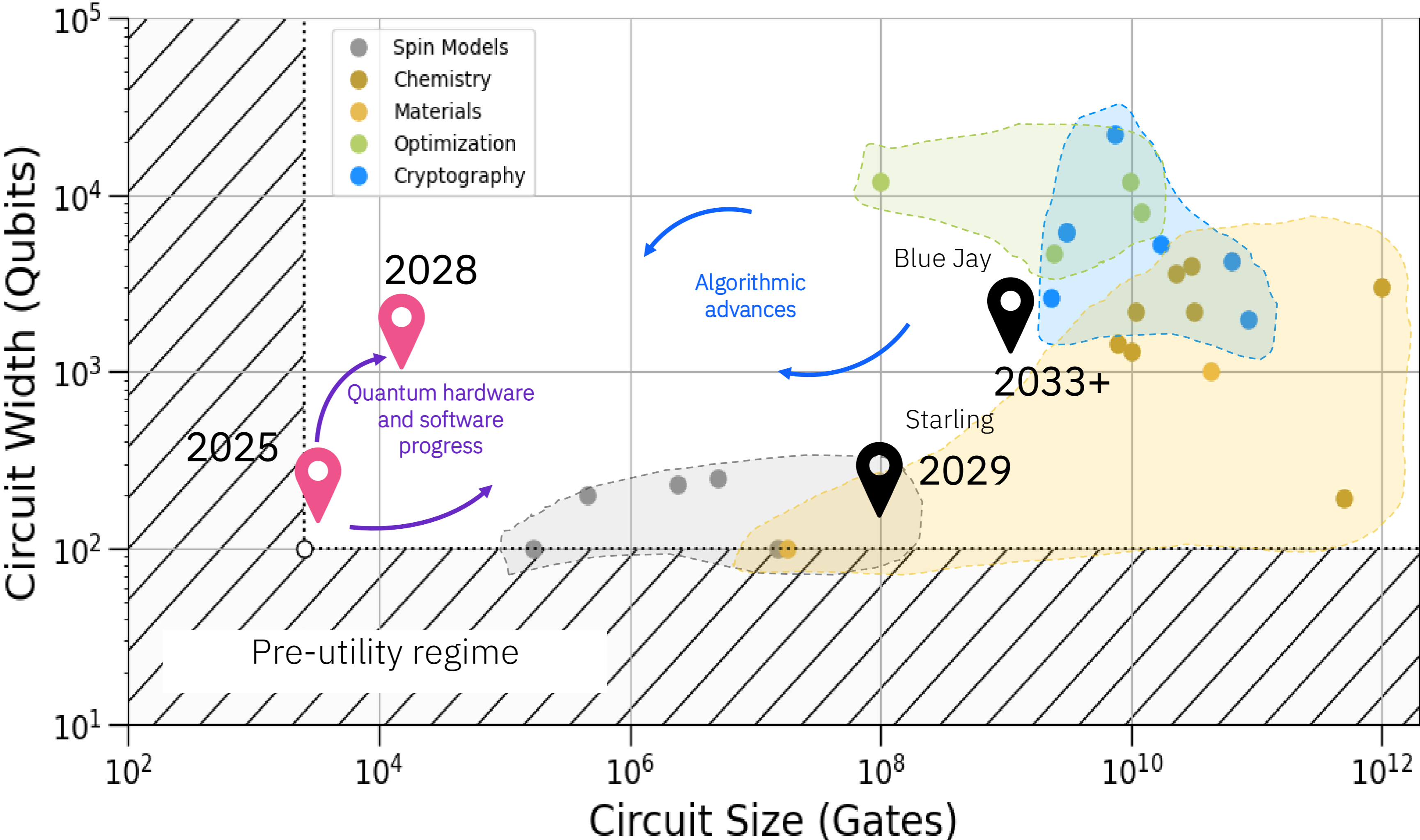
Algorithmic vs. compute improvements in simulating a lattice gauge theory



Tour de gross: A modular quantum computer based on bivariate bicycle codes

Theodore J. Yoder¹, Eddie Schoute¹, Patrick Rall¹, Emily Pritchett¹, Jay M. Gambetta¹, Andrew W. Cross¹, Malcolm Carroll¹, and Michael E. Beverland^{*1}

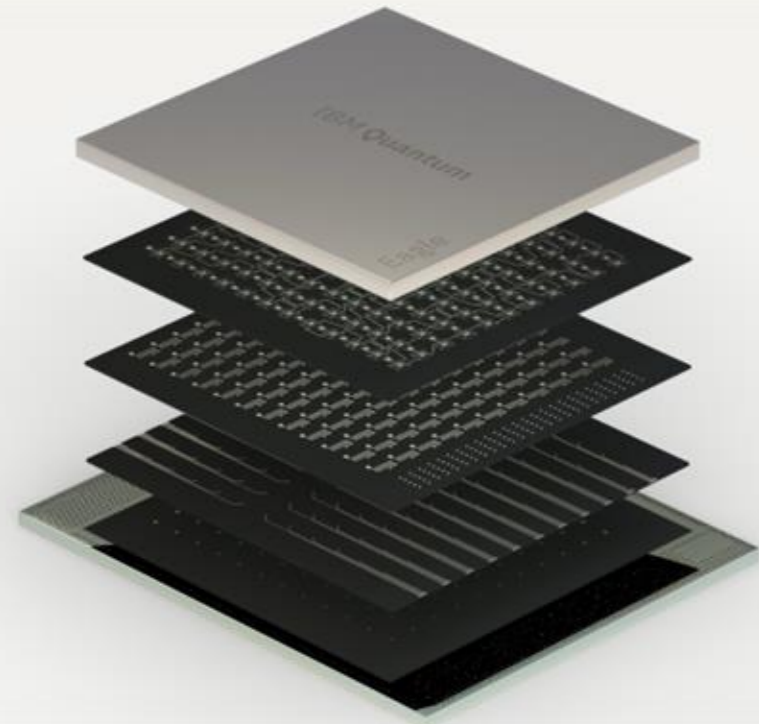
What can you do with a large-scale, fault-tolerant quantum computer?



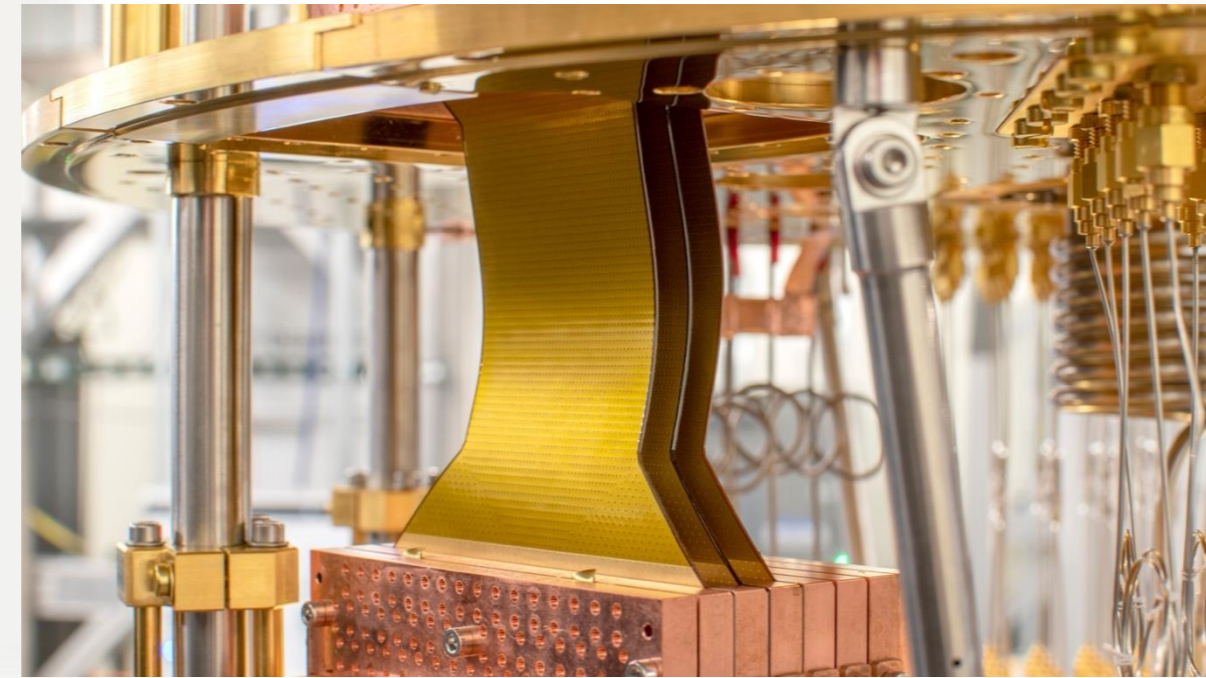
Scaling

IBM Quantum

Processors



I/O wiring and space transformers



Control electronics



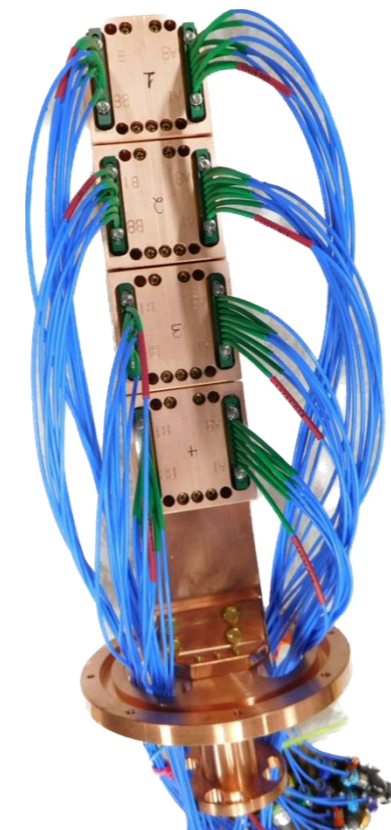
Runtime Infrastructure



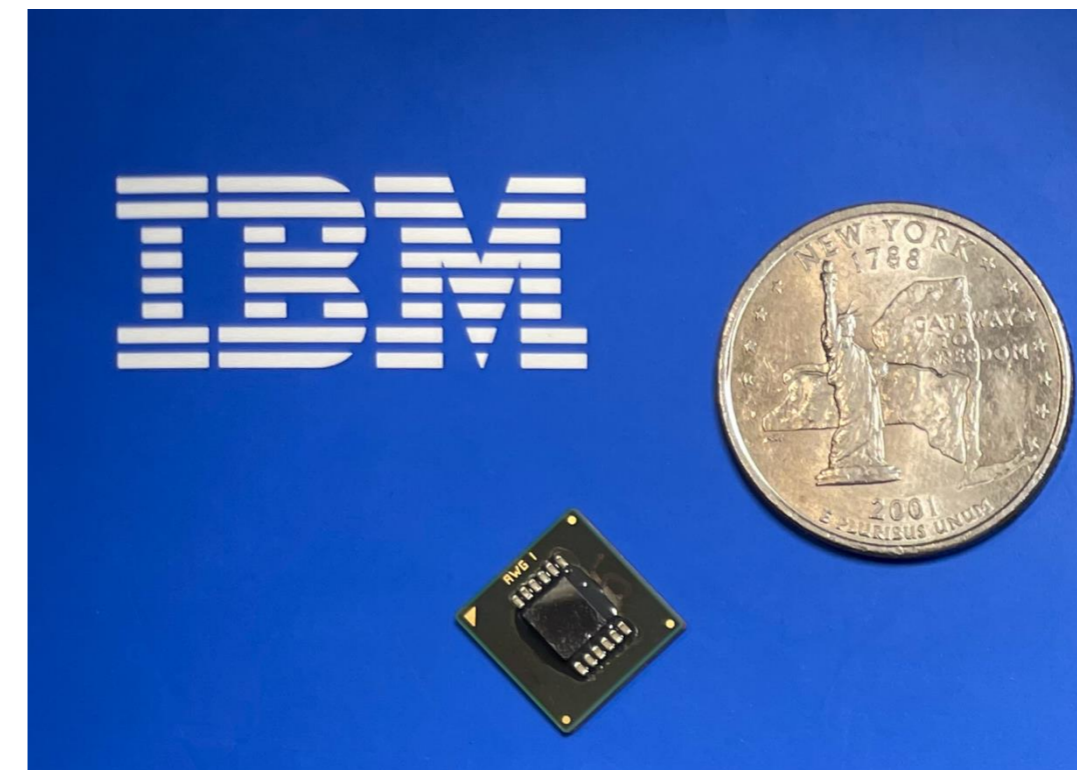
Software



Amplifiers and other microwave components



Full-featured 4K cryo-CMOS qubit controller



Cryo Infrastructure





RTE 02

RTE 01

CRYOGENIC ENCLOSURE

RTE 01

RTE 02

IBM Quantum
System Two

IBM

UTILITY

CRS 01

CRS 02

Wrapping it up

Superconducting qubits in isolation are misleadingly easy

Progress will be faster than we expect

We want to build large systems – statistics matter

This talk only went down one path! [P. Krantz et al., Appl. Phys. Rev. 6, 021318 \(2019\)](#). is a nice review to learn on devices

Similarly, [Bravyi et al, J. Appl. Phys. 132, 160902 \(2022\)](#) for architecture.

BACKUPS