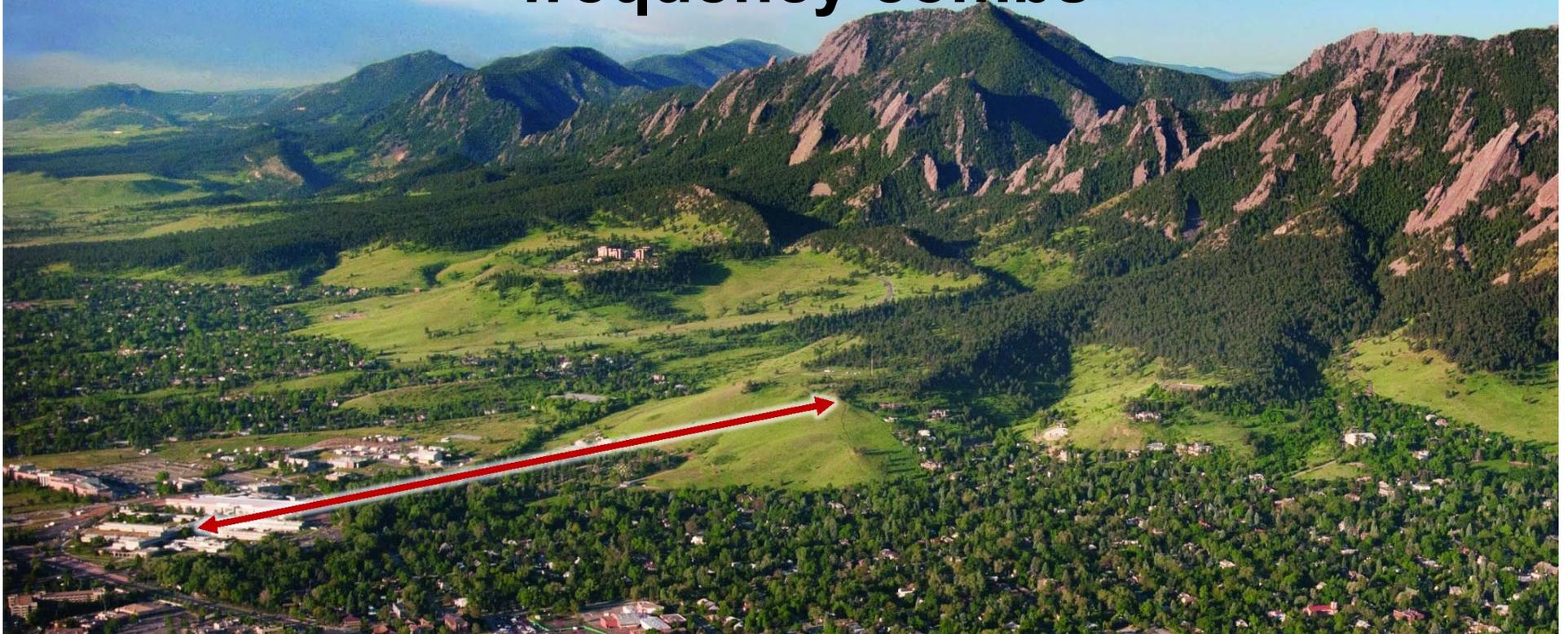


# Noise sources and stabilization strategies in frequency combs



ICTP Winter College on Optics  
Trieste, Italy  
February 17, 2015

*Nathan Newbury*  
*National Institute of Standards and Technology, Boulder, CO*  
*nnewbury@boulder.nist.gov*

# Outline

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- Motivation for frequency combs
- Frequency comb
- Noise in fiber-based frequency combs
  - Fixed point
- Making a quiet frequency comb
- Fiber frequency combs at NIST
  - Overview of different designs since 2003
  - Current “robust” NIST frequency comb
- Conclusion

# People



**Esther Baumann**  
**Hugo Bergeron**  
**Mick Cermak**  
**Ian Coddington**  
**Kevin Cossel**  
**Stefan Droste**  
**Fabrizio Giorgetta**  
**Dan Herman**  
**Nathan Newbury**  
**Laura Sinclair**  
**Bill Swann**  
**Gar-Wing Truong**  
**Eleanor Waxman**  
**Gabe Ycas**

## **Other non-NIST collaborators:**

**Brian Washburn (Kansas State)**  
**Jean Daniel Deschenes (U of Laval)**  
**Greg Rieker (CU)**

## **NIST collaborators:**

**Scott Diddams, Dave Leibrandt, Craig Nelson, Scott Papp, Frank Quinlan, Kevin Silverman, Jeff Shainline, Rich Mirin, ...**

# Recent review articles

---

RSI Review article on current NIST comb design:

L.C. Sinclair, J.-D. Deschênes, L. Sonderhouse, W. C. Swann, I.H. Khader, E. Baumann, N. R. Newbury, and I. Coddington, **Invited Article: A Compact Optically-Coherent Fiber Frequency Comb**, Review of Scientific Instruments 86, 081301 (2015);

See also: <http://www.nist.gov/pml/div686/grp07/fpga-based-digital-control-box-phase-stablization-frequency-comb.cfm>

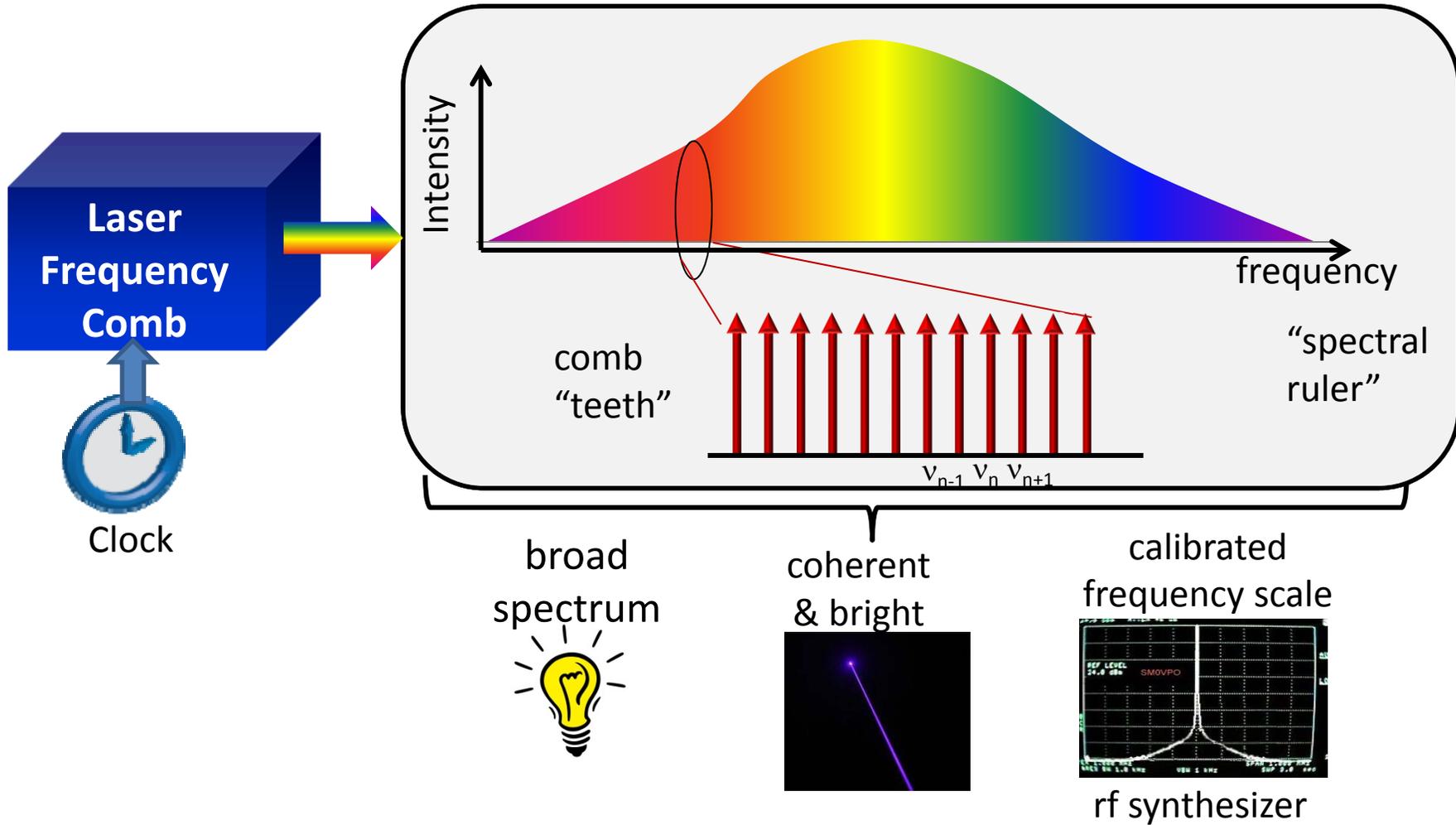
Nanophotonics upcoming review on fiber combs:

S. Droste, G. Ycas, B. R. Washburn, I. Coddington, NRN, **Optical Frequency Comb Generation based on Erbium Fiber Lasers**, Nanophotonics, to be published

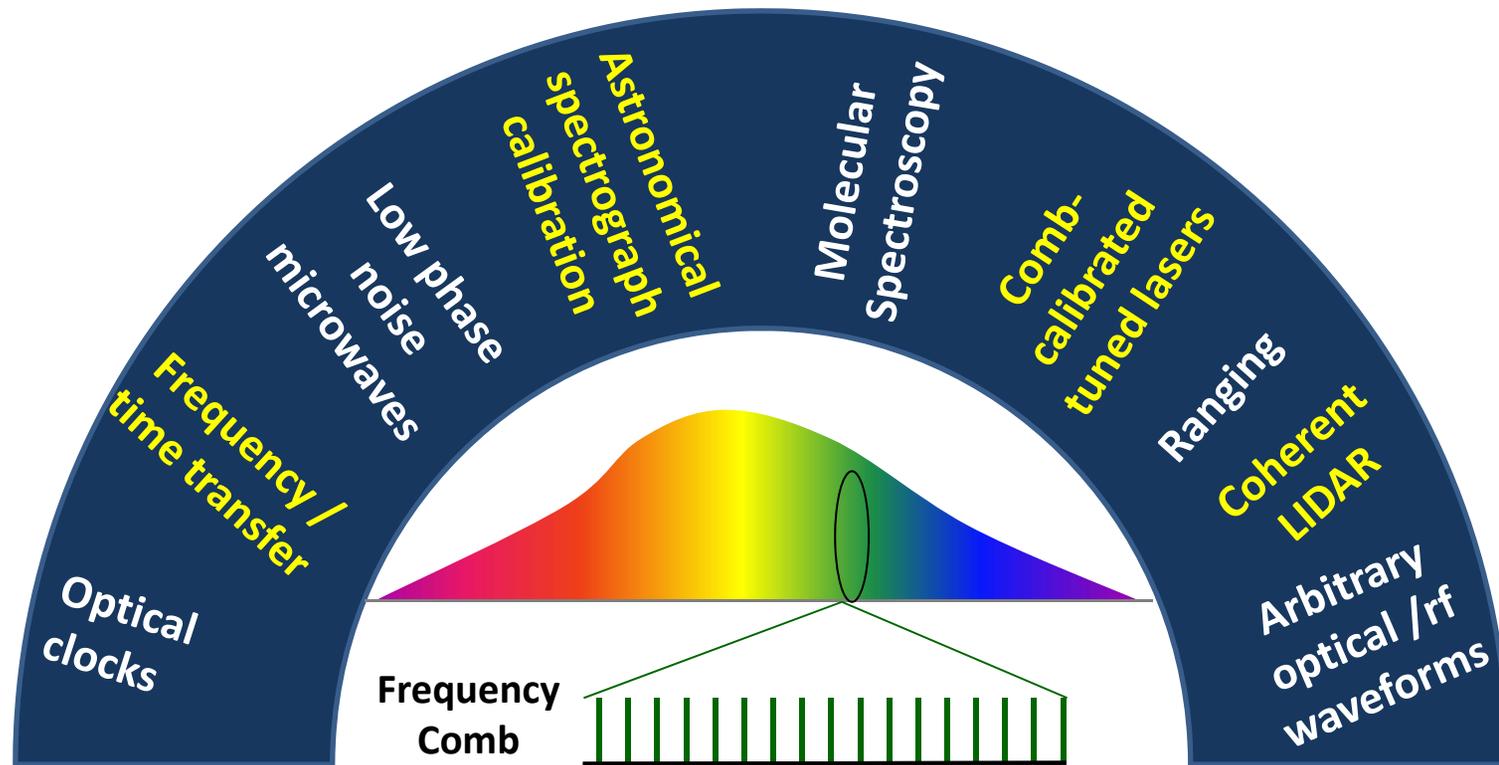
Fiber frequency Comb noise

N. Newbury, W. Swann, J. Opt. Soc. Am. B, **Low-noise fiber-laser frequency combs**, 24, (2007)

# Frequency Combs: Why are they special?



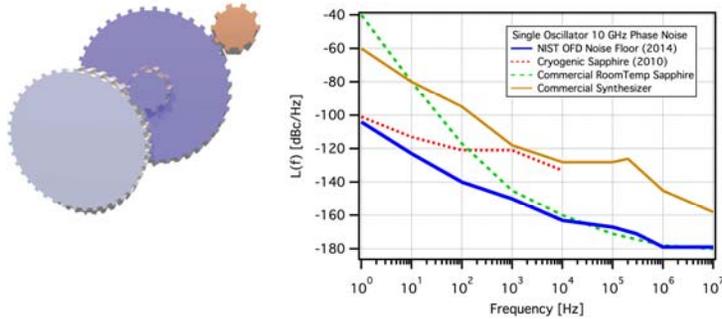
# Applications of Frequency Combs



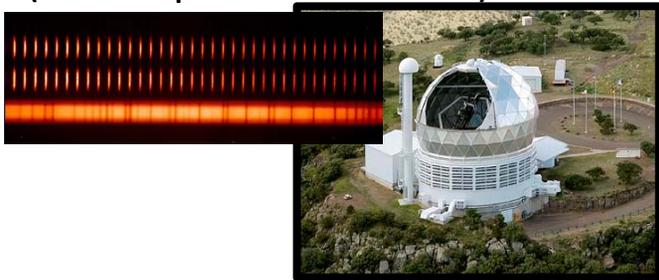
- **Applied to laser-based metrology/sensing systems**
  - As a spectral ruler
  - As a “time” ruler
  - As a frequency divider
  - As a calibrated broadband source

# Example applications

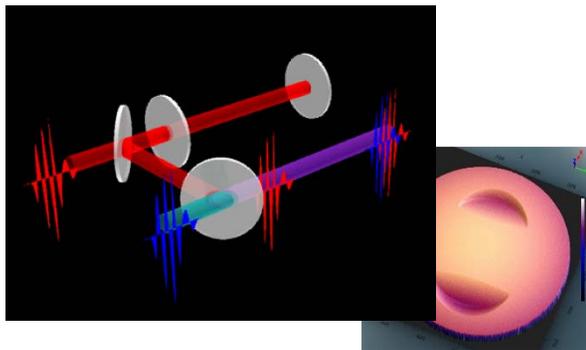
## Precision microwave generation (for RADAR)



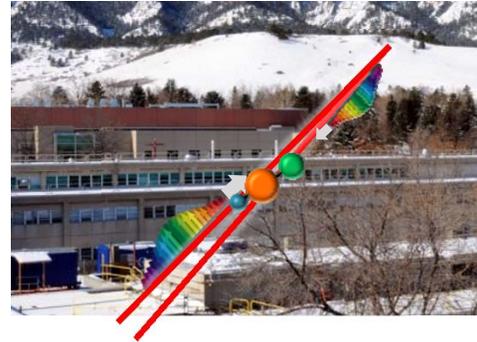
## Precision spectroscopy (for exoplanet searches)



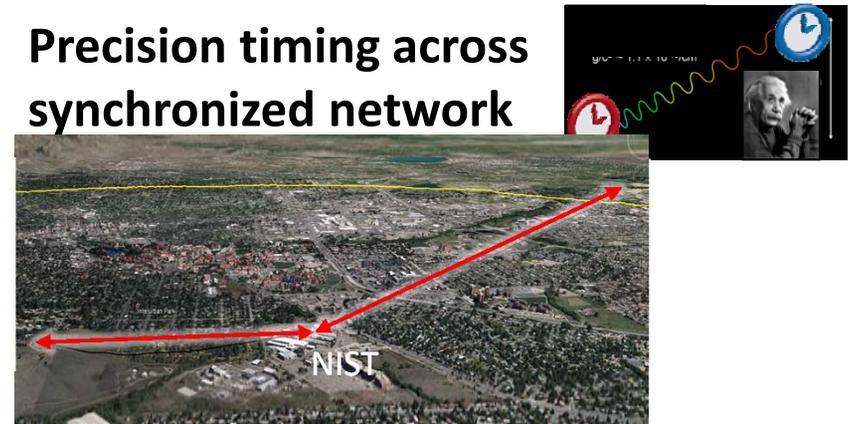
## Precision Ranging



## Precision molecular spectroscopy (for greenhouse gases)



## Precision timing across synchronized network



*Others:  
Advanced communications  
Fundamental scientific tests*

...

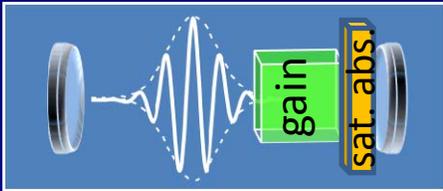
# Outline

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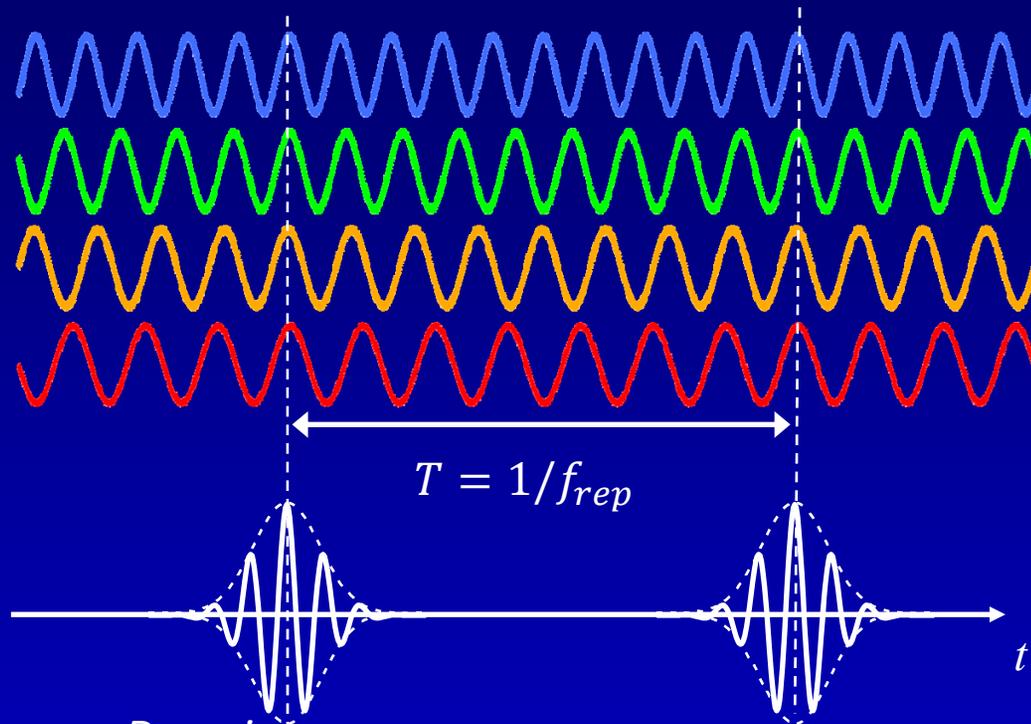
- Motivation for frequency combs
- ▪ Frequency comb
  - Basic picture
  - Types of Frequency combs
- Noise in fiber-based frequency combs
  - Fixed point
  - Noise sources
  - Actuators
- Making a quiet frequency comb
- Fiber frequency combs at NIST
  - Overview of different designs since 2003
  - Current “robust” NIST frequency comb
- Conclusion

# A Mode-Locked Laser

Passively  
Modelocked Laser

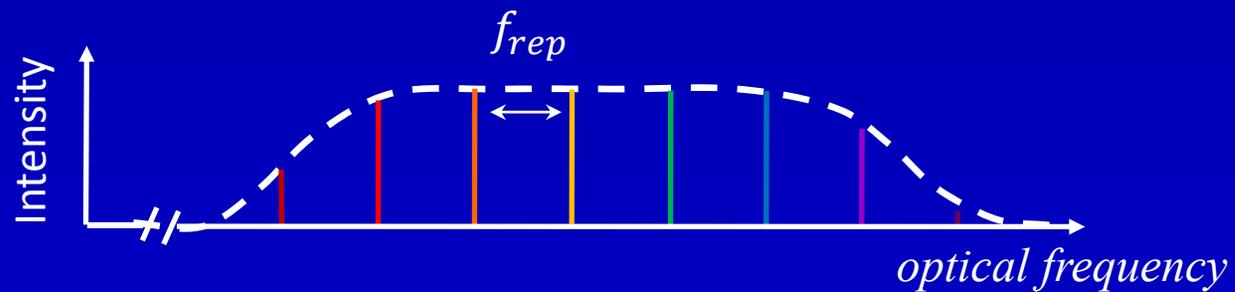


Time domain



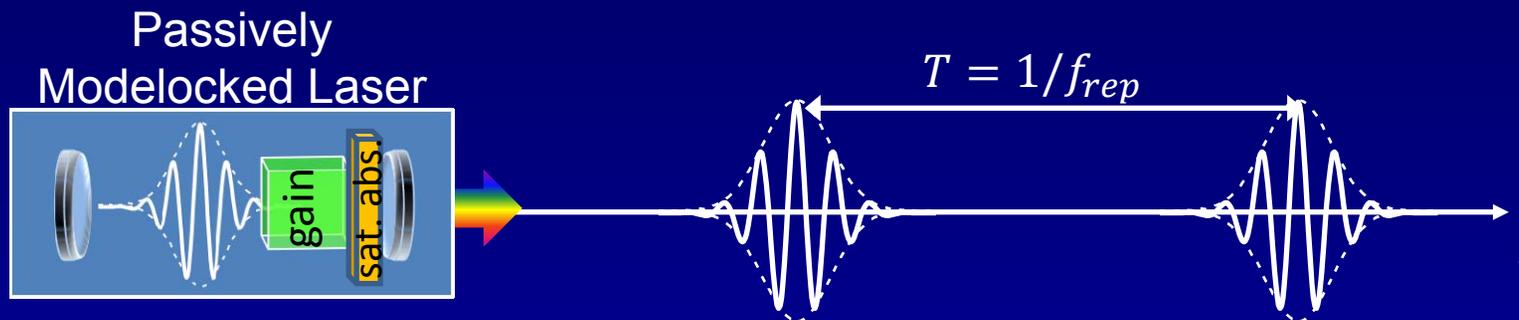
Outputs  
light at  
equally  
spaced  
modes of  
the laser

Frequency Domain

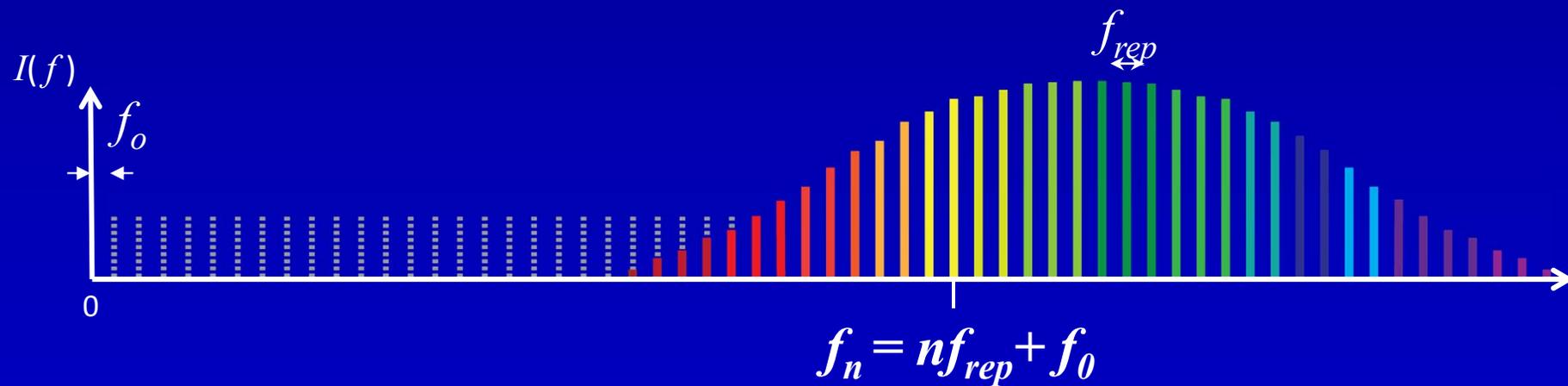


# A Free-Running Mode-Locked Laser

Time domain

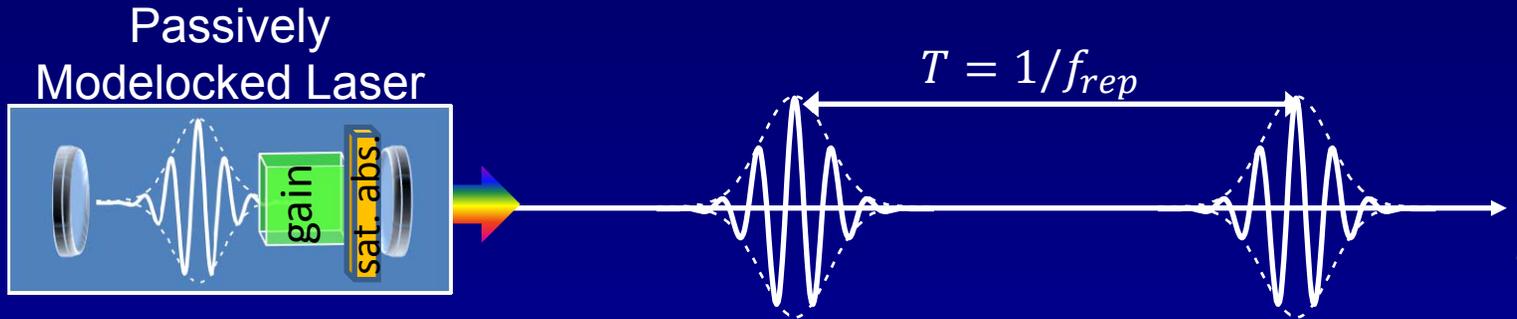


Frequency domain

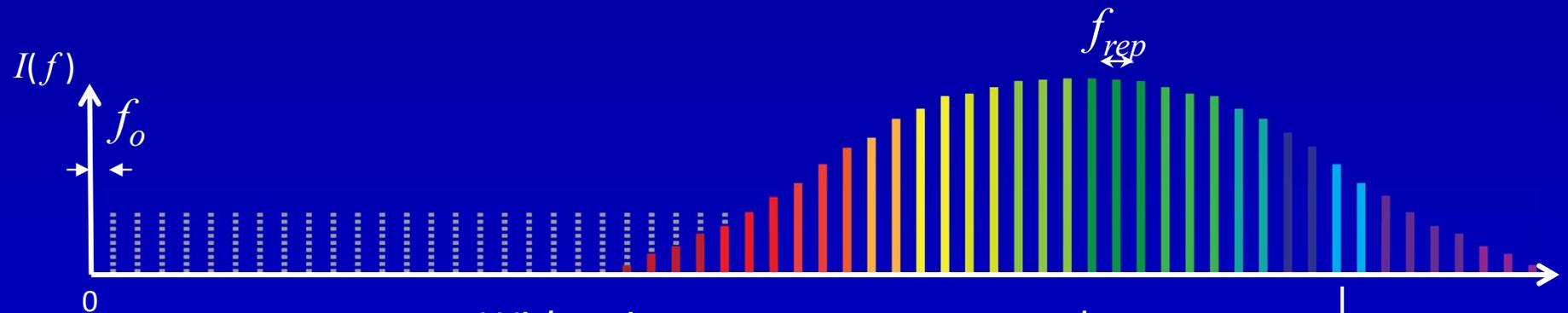


# A Free-Running Mode-Locked Laser

Time domain



Frequency domain



With noise, output moves around...  
but basic comb structure is preserved.  
Comb can only "translate" and "breathe"

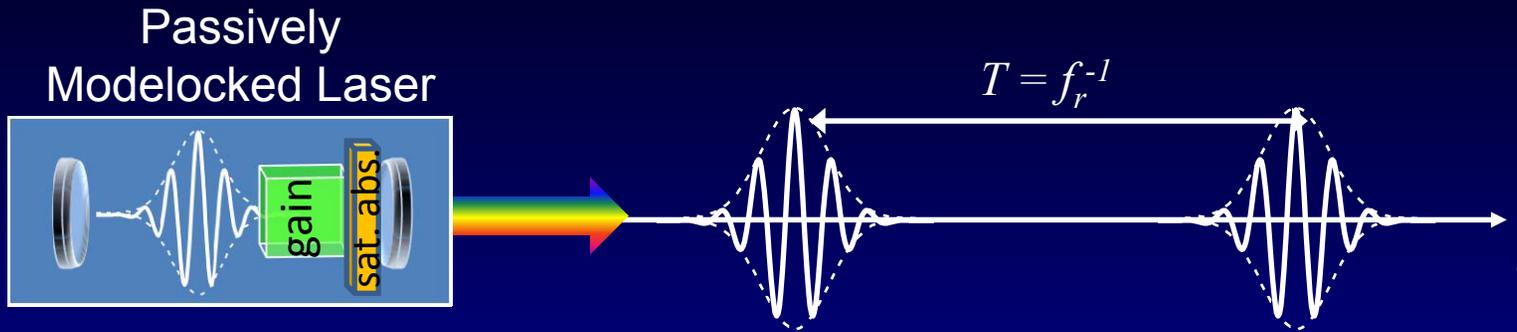
$$f_n = nf_{rep} + f_0$$

# Offset Frequency Stabilization

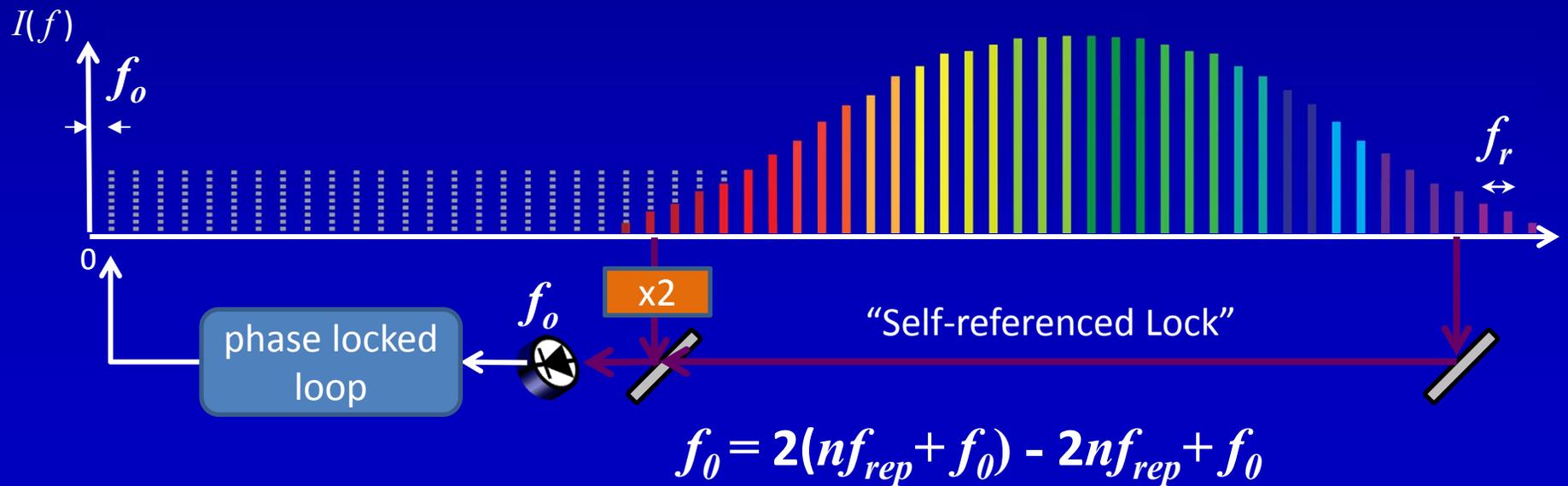
Jones, et al. *Science* **288**, 635 (2000)



J. Hall  
T. Hänsch



→ Spectrally broaden to an octave ←

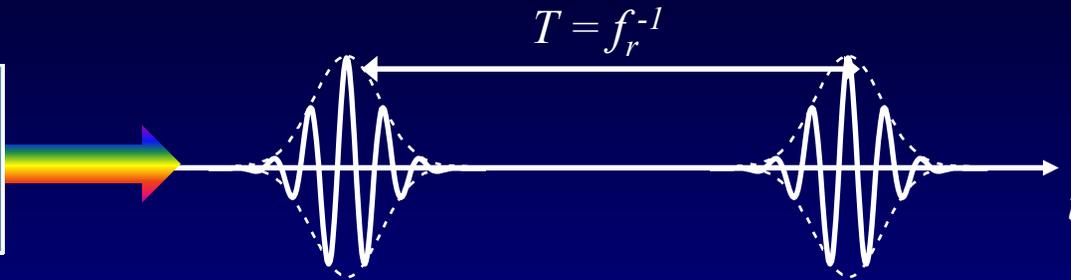
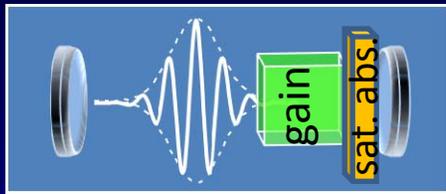


# Stabilization of the Second Degree of Freedom

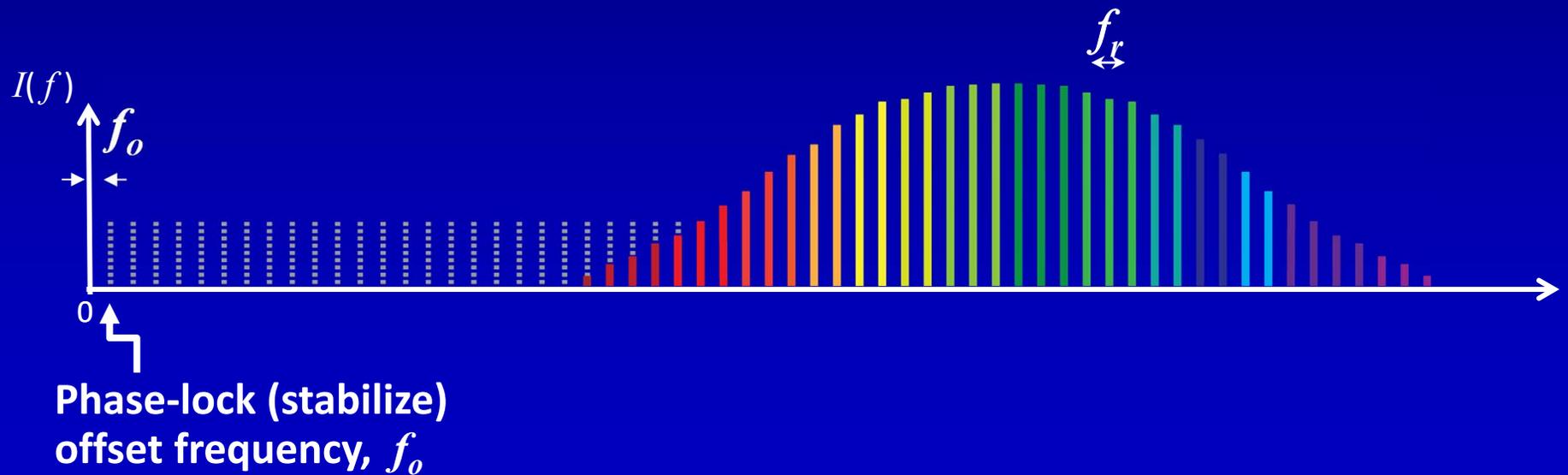


J. Hall  
T. Hänsch

Passively  
Modelocked Laser



A choice: Stabilize to an Optical or RF oscillator



# Frequency Comb needs a Reference Oscillator

## RF oscillator

(Quartz / DRO / H-maser)

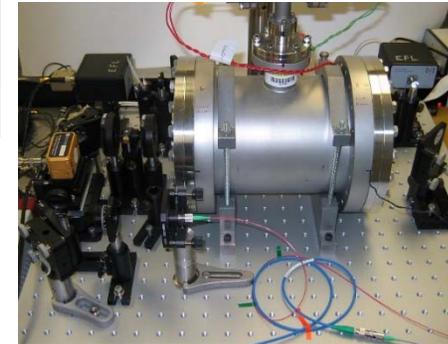
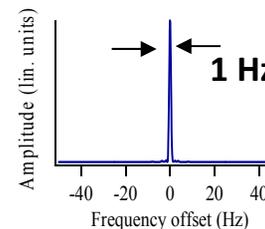
Signal @ 10 MHz – 10 GHz



- Quartz/DRO: small, compact, cheap
- RF comb stabilization easy
- No optical coherence in comb
- Broad optical teeth

## Optical Oscillator (cavity-stabilized Laser)

Signal @ 200 THz



***Pound-Drever-Hall Cavity Lock***

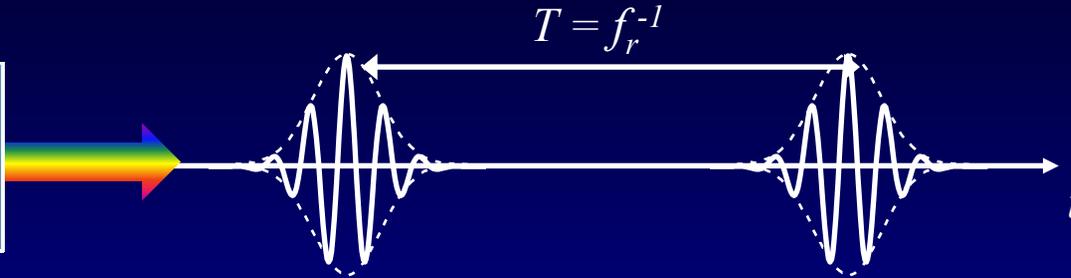
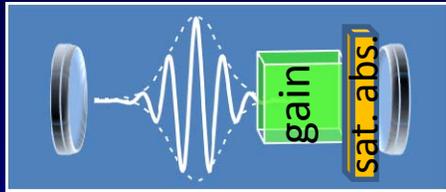
- Not small, not compact, not cheap
- Optical comb stabilization hard
- Optically coherent comb
- “Delta function teeth”

# RF Stabilization

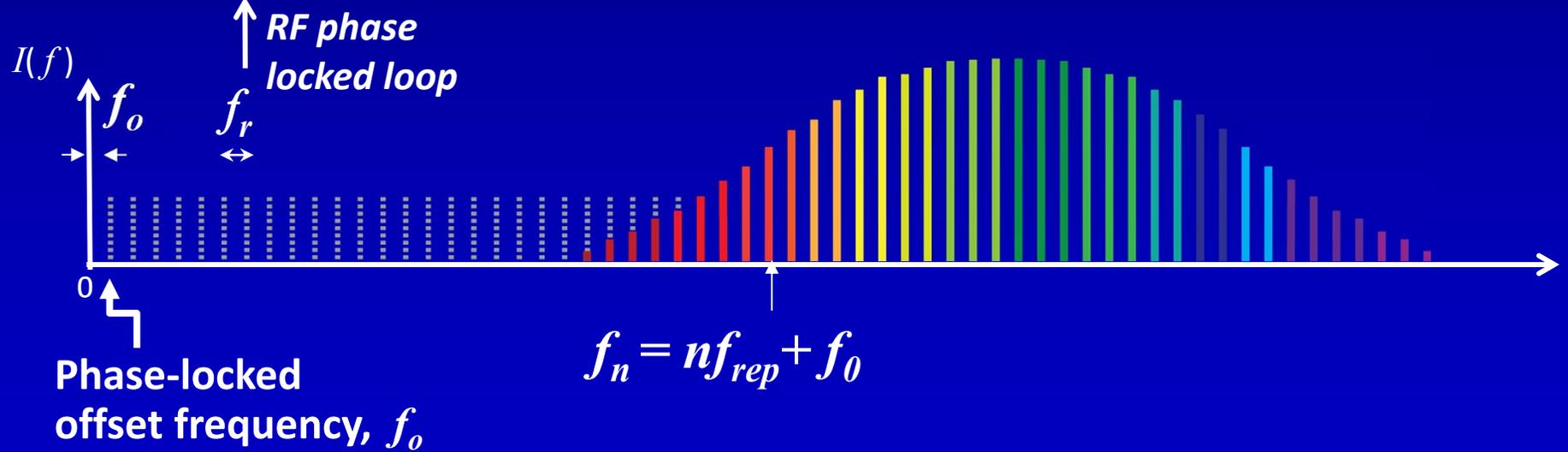


J. Hall  
T. Hänsch

Passively  
Modelocked Laser



RF oscillator

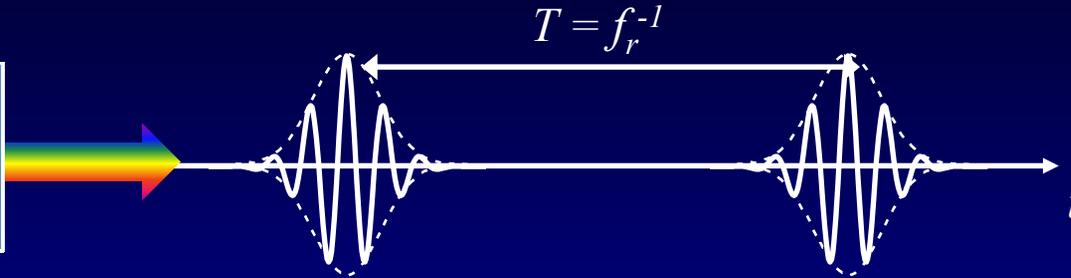
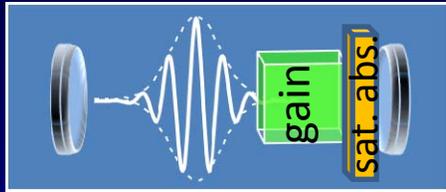


# Optical Stabilization



J. Hall  
T. Hänsch

Passively  
Modelocked Laser

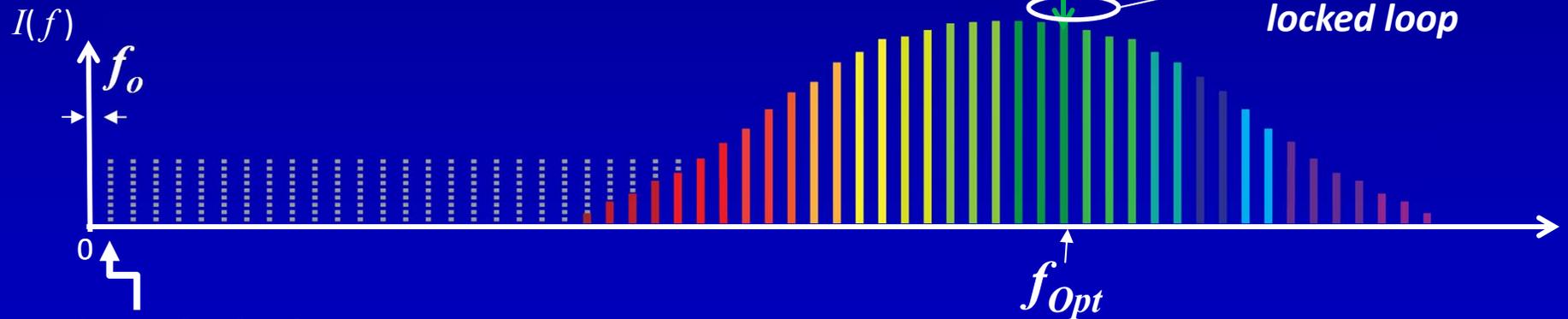


Optical "Clock" = Narrow linewidth laser



Laser

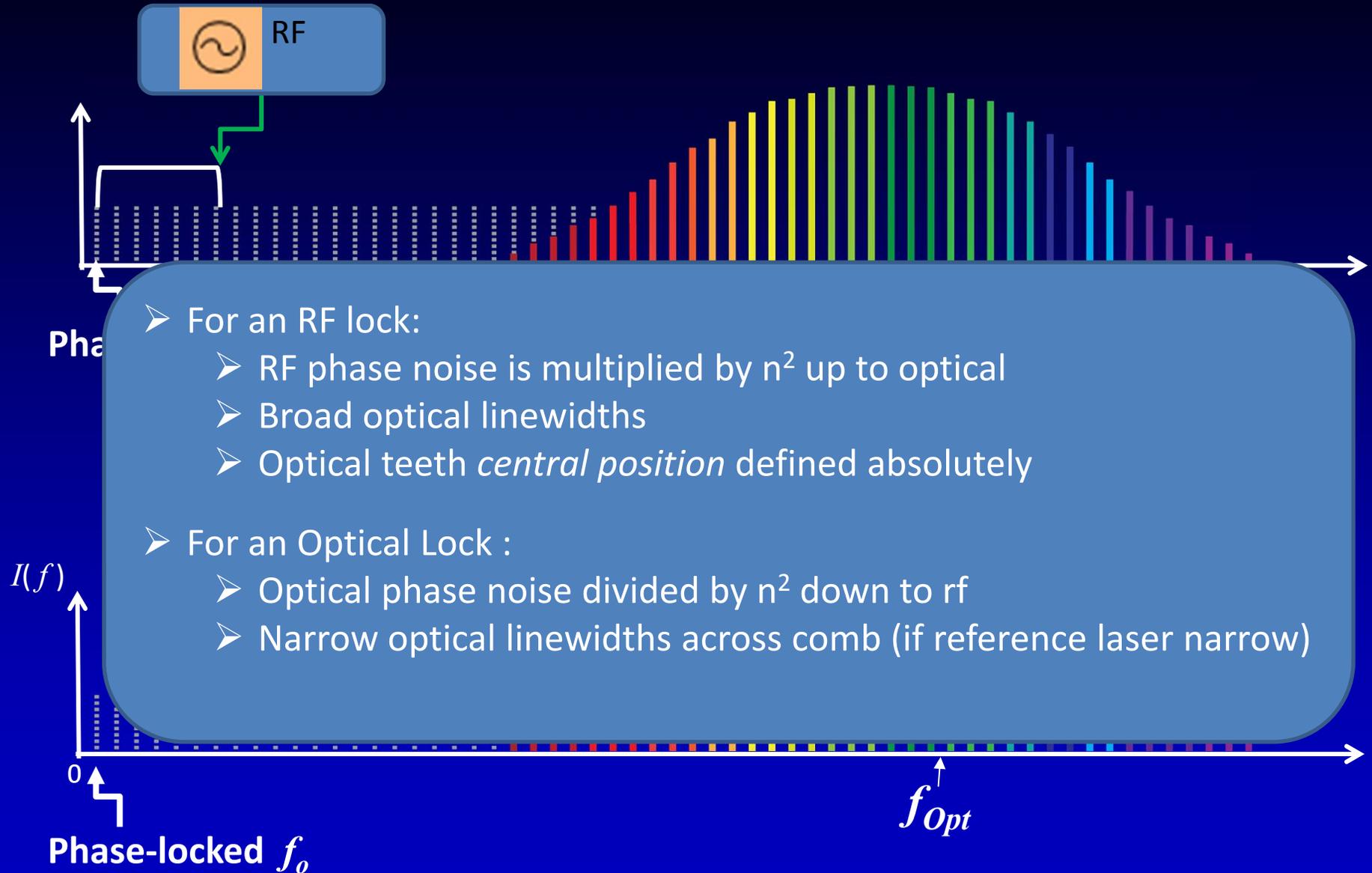
Optical phase  
locked loop



Phase-locked  
offset frequency,  $f_0$



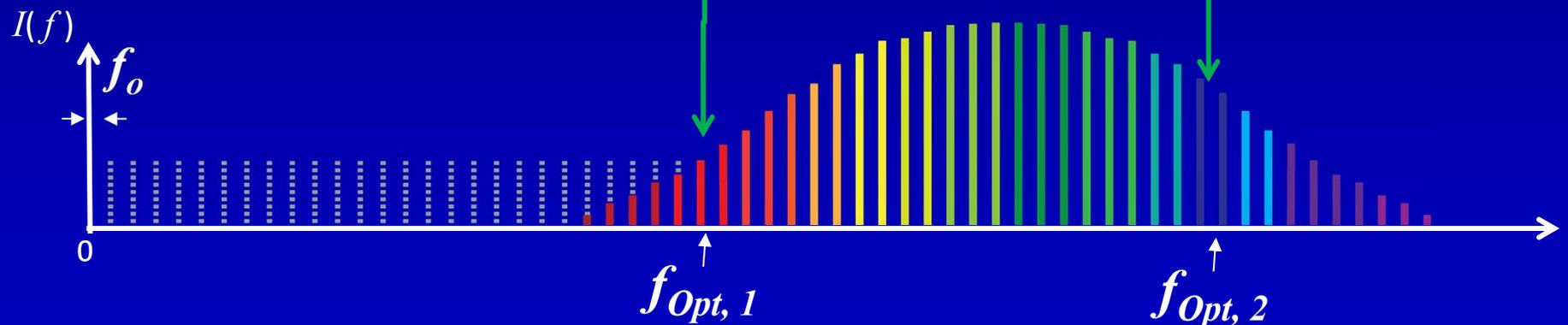
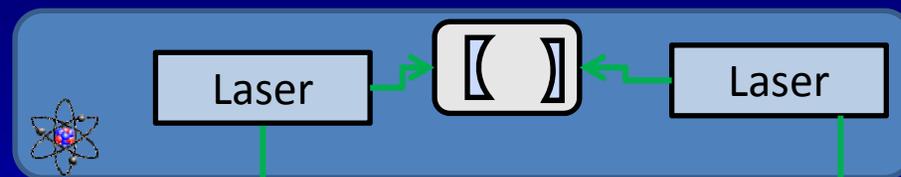
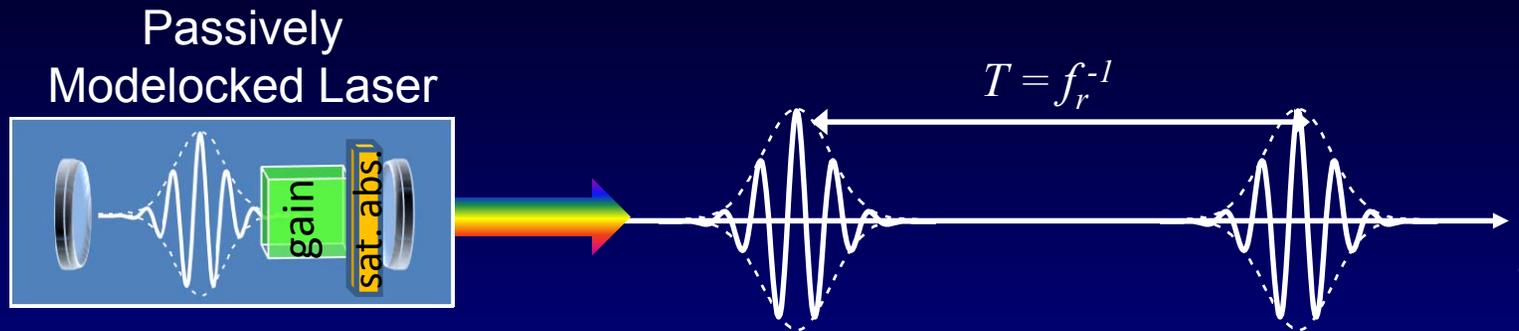
# RF vs Optical Stabilization: Lever Arm Difference



# Other Stabilization Options: double pinning



J. Hall  
T. Hänsch



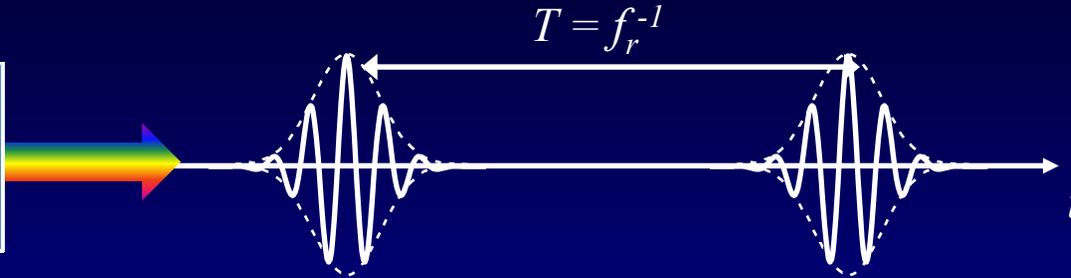
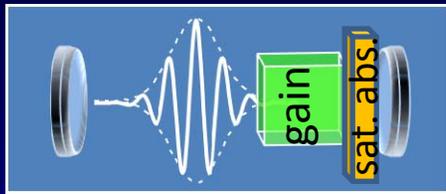
NO Offset frequency stabilization -> no need for octave supercontinuum  
But no absolute frequency knowledge (unless cavity separately measured)

# Other Stabilization Options: free running laser

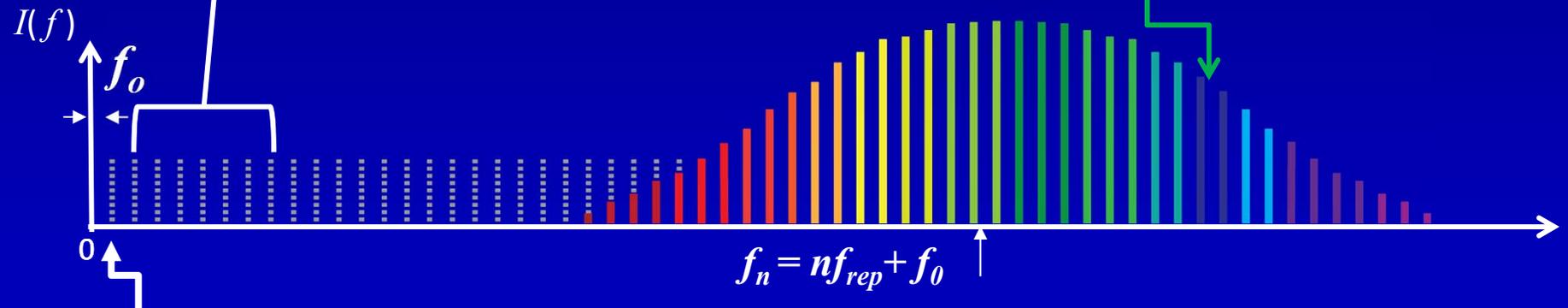


J. Hall  
T. Hänsch

Passively  
Modelocked Laser



RF frequency  
counter  
( $nf_{rep}$ )



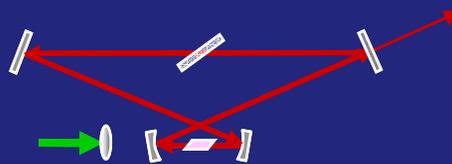
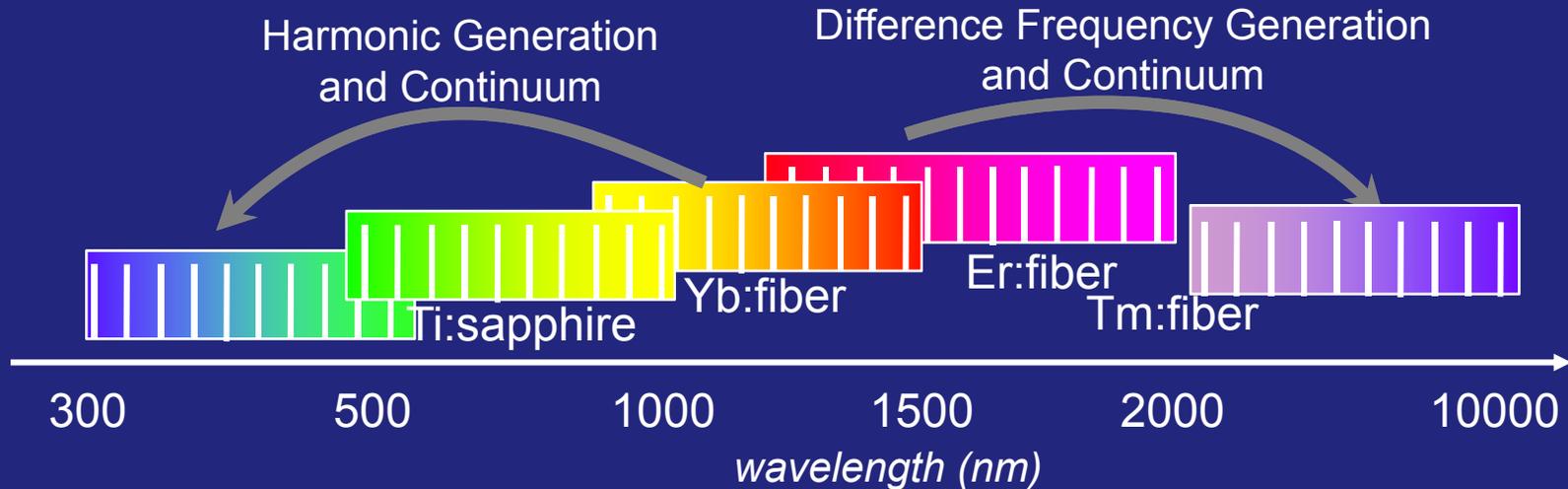
Phase-locked  
offset frequency,  $f_0$

Avoids need for cavity-stabilized laser  
Retains absolute frequency knowledge

# Femtosecond Laser Frequency Combs

A unique source for sensing and spectroscopy

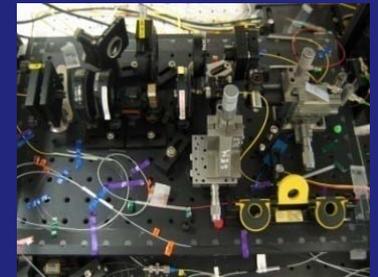
- an array of millions of phase-coherent CW oscillators
- large spectral coverage: 300 nm - 10 microns
- precisely known frequencies ( $\sim 1$  Hz resolution)
- high peak power for efficient nonlinear optics



Ti:Sapphire  
laser



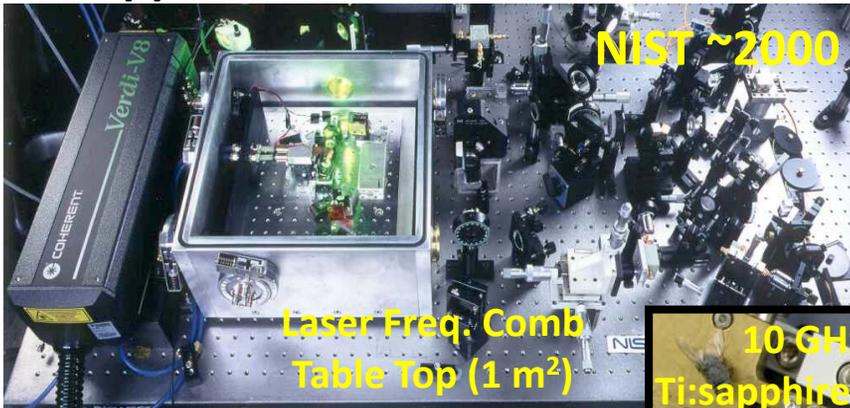
Er: fiber laser



courtesy of S. Diddams et al.

# Some Frequency Combs

## Ti:Sapphire Combs

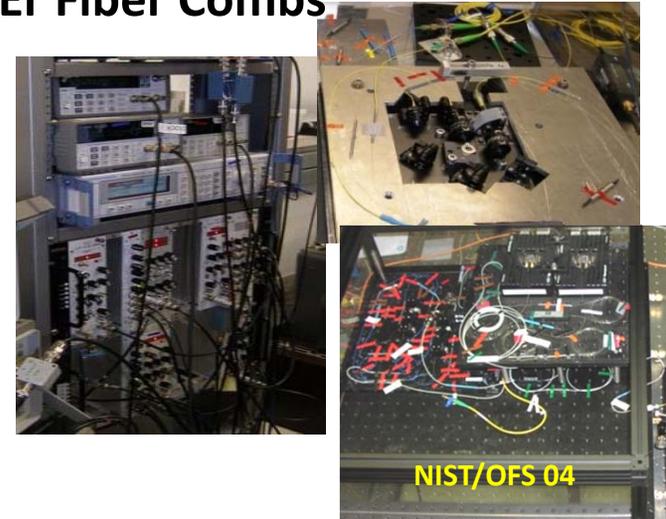


Courtesy S. Diddams

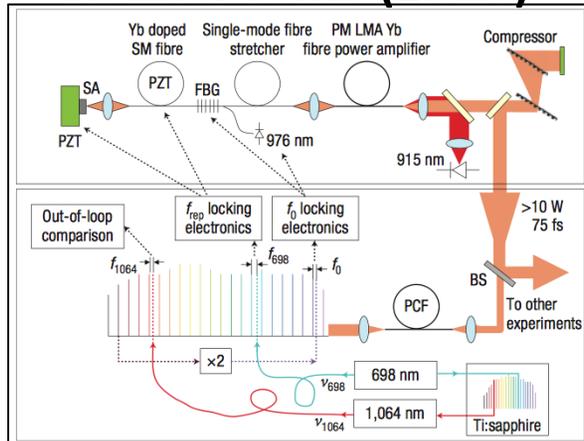


A. Bartels,, *Science* **326**, 681 (2009).

## Er Fiber Combs

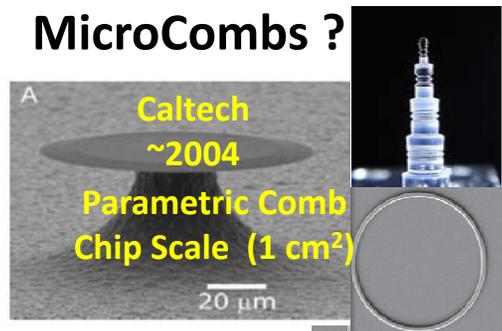


## Yb fiber comb (10W!)



Schibli, et al. *Nature Photonics* **2**, 355 - 359 (2008) (IMRA America & JILA)

## MicroCombs ?



Del'Haye, *Nature*, **450**, 1214, 2007;  
Levy, *Nat. Phot.* **4**, 32 (2010), Papp,  
Diddams, *PR A* **84**, 053833 (2011),  
EPFL, OE waves, Cornell, CalTech,  
MPQ, NIST....



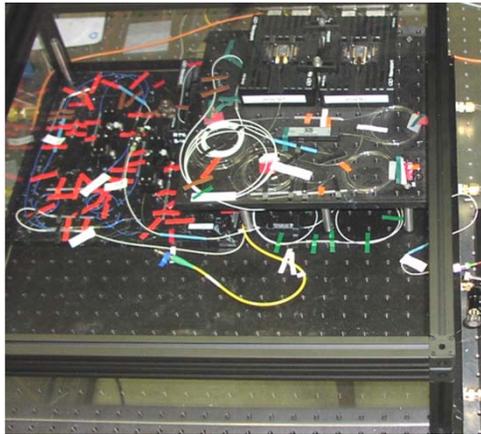
Many others  
Er:Yb glass  
Thulium Fiber combs  
Cr:Forsterite

# Most “universal” solution: Fiber Laser Based Combs

---

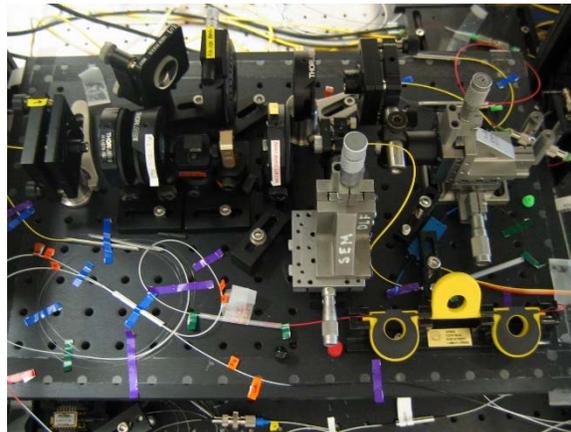
- Advantages of fiber frequency comb
  - Compact, inexpensive design
  - Potential for stable “hands-free” operation
  - Compatible with highly reliable telecommunication components
  - Covers the Infrared region of the spectrum
  - Under development at: Menlo, Toptica, MPQ, PTB, AIST, IMRA, OFS, U. Konstanz, Kansas State, Arizona, NIST, etc. etc.
- Rest of talk will focus on fiber frequency combs but many of the results/analysis are general and apply to other frequency combs as well .

# Some Different NIST Fiber Combs



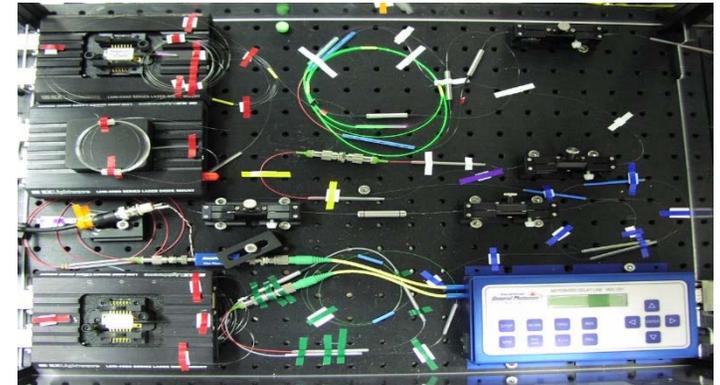
**NIST/OFS Figure-8  
Fiber Frequency Comb**

Washburn et al., Opt. Lett. **29**, 250 (2004)



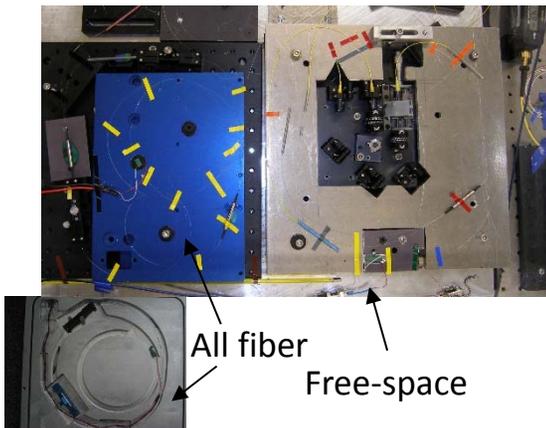
**stretched-pulse ring laser  
Fiber Frequency Comb**

McFerran et al., Opt. Lett. **31**, 1997 (2006)  
Swann, Opt. Lett. **31**, 3046 (2006).



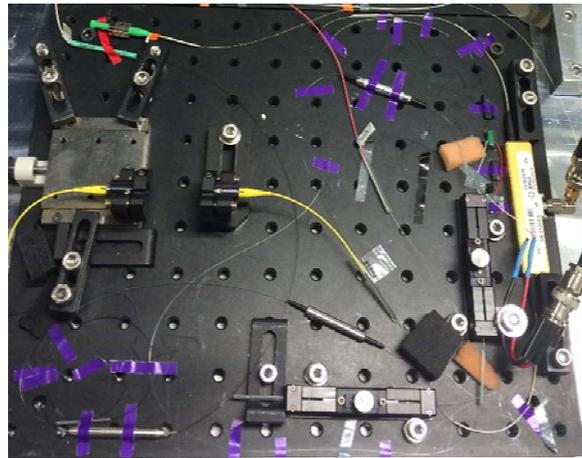
**stretched-pulse ring laser with variable  
rep rate  
Fiber Frequency Comb**

Washburn et al, OE, **12**, 4999 (2004)



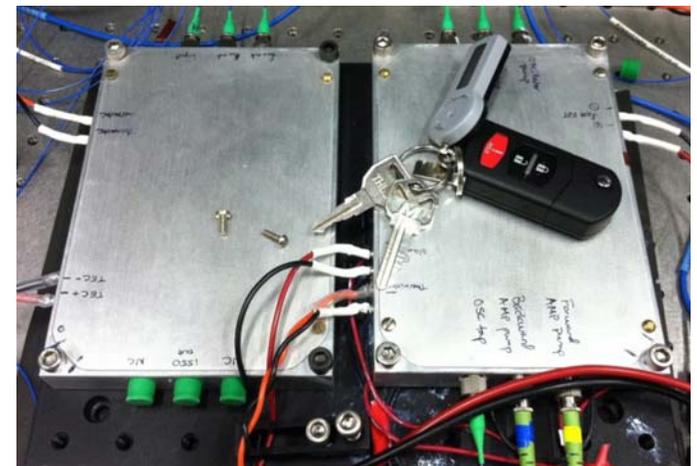
**Stretched-pulse ring lasers  
Fiber Frequency Combs**

Coddington et al, PRA, **81**,  
043817 (2010)



**Ring laser with intracavity EOM**

Swann et al. OE, **19**, 243817(2011)

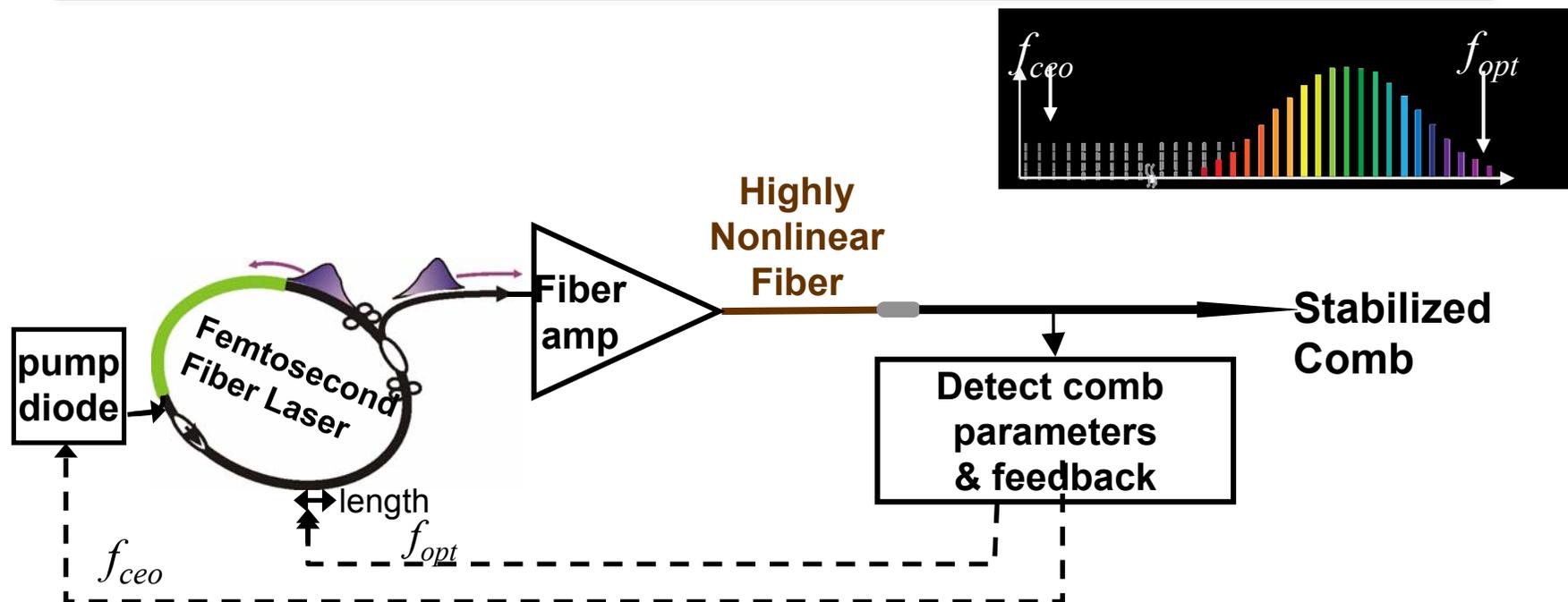


**Linear SESAM Linear cavity Fiber  
Frequency Comb**

Sinclair, OE, **22**, 6996 (2014)  
Sinclair, RSI, **86**, 081301 (2015);

# Fiber Laser Frequency Comb

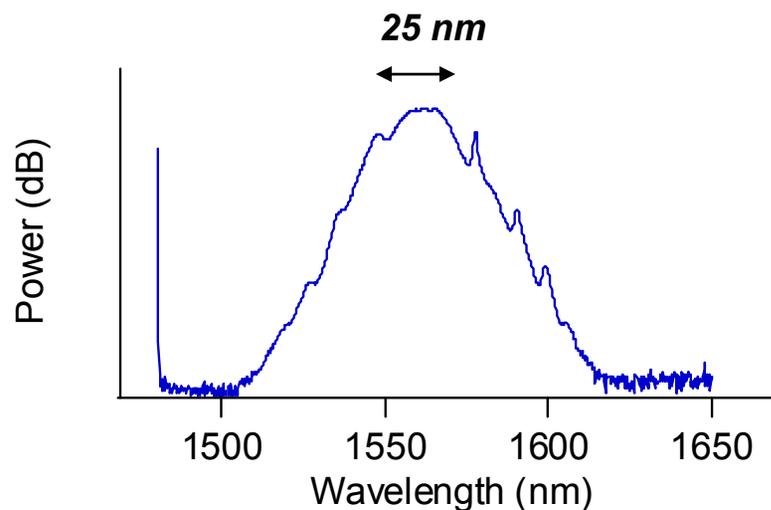
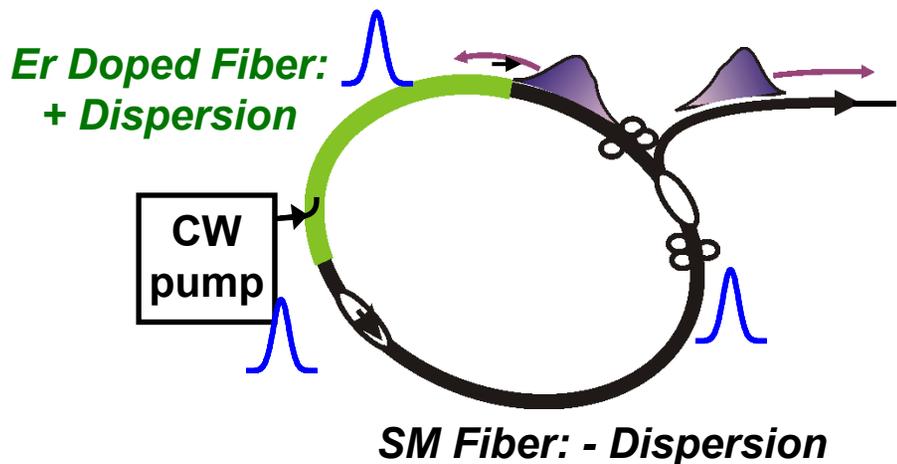
NIST



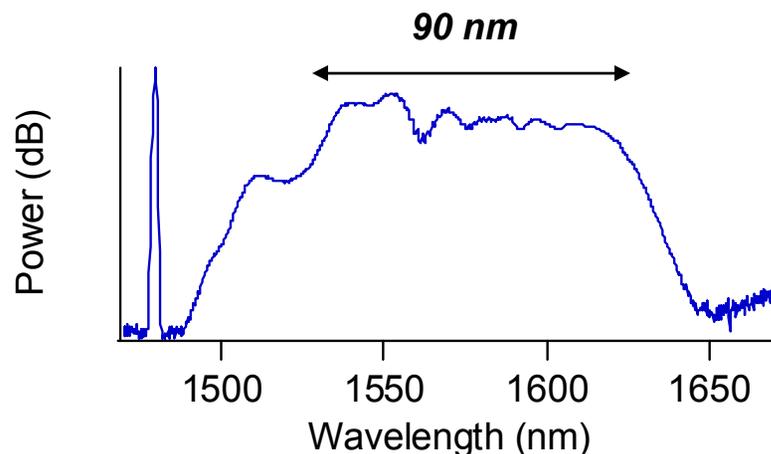
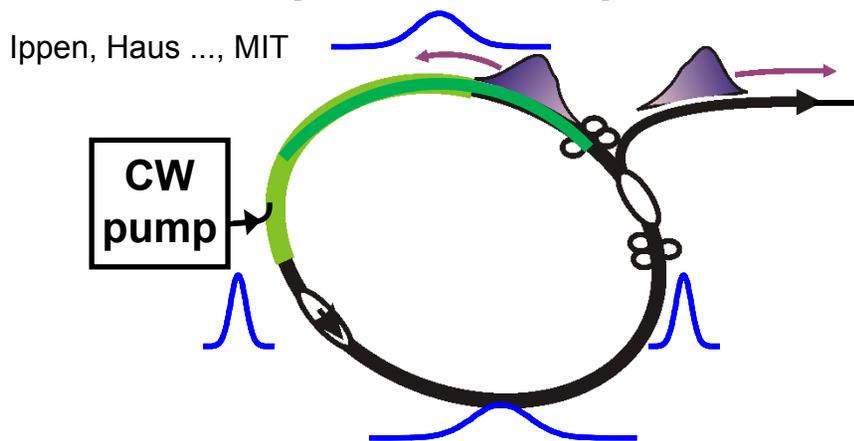
- Stabilize offset frequency by feeding back to pump power
- Stabilize  $f_{rep}$  (or optical tooth) by feeding back to cavity length

# Ring Laser: “Soliton” vs. Stretched pulse mode

Soliton-mode: net dispersion  $< 0$

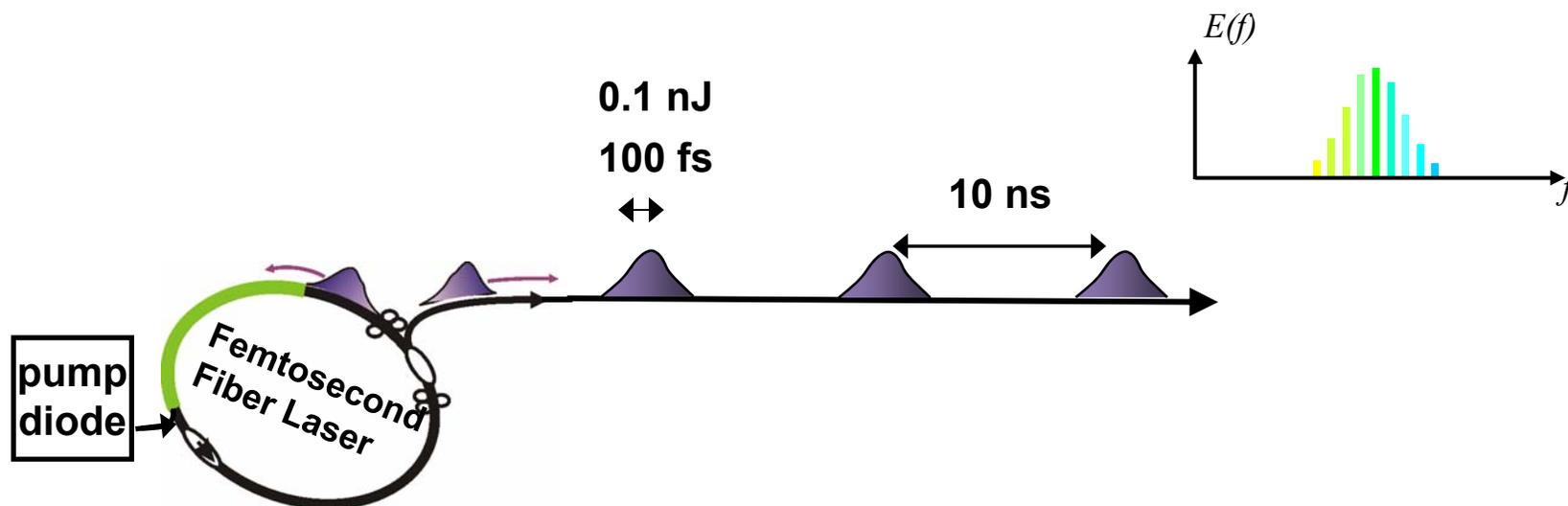


Stretched-pulse: net dispersion  $> 0$



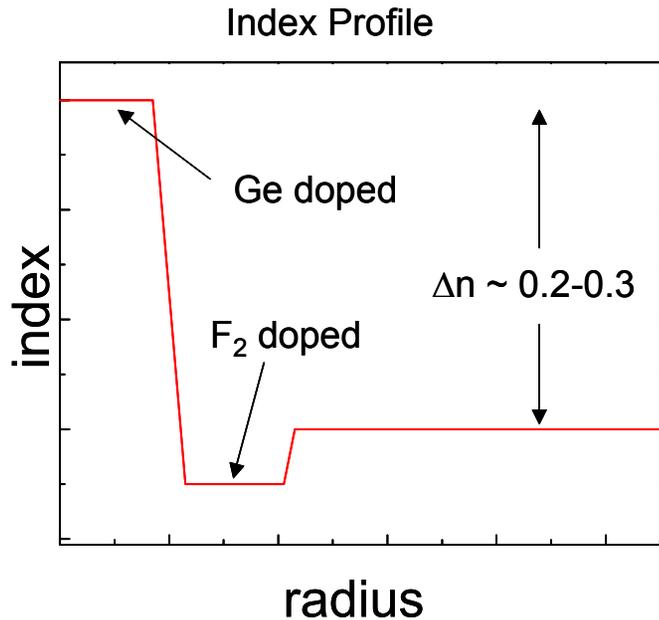
*Either works for a frequency comb: low dispersion better for noise*

# Free-running Mode-locked laser



- A free-running frequency comb .
- Now need to broaden to octave-spanning supercontinuum

# Highly Nonlinear Fiber (HNLf) for Er fiber combs



nonlinearity : 8 to 15 1/W-km

Effective Area : 13  $\mu\text{m}^2$

loss : 0.7 to 1 dB/km

dispersion (1550 nm) :

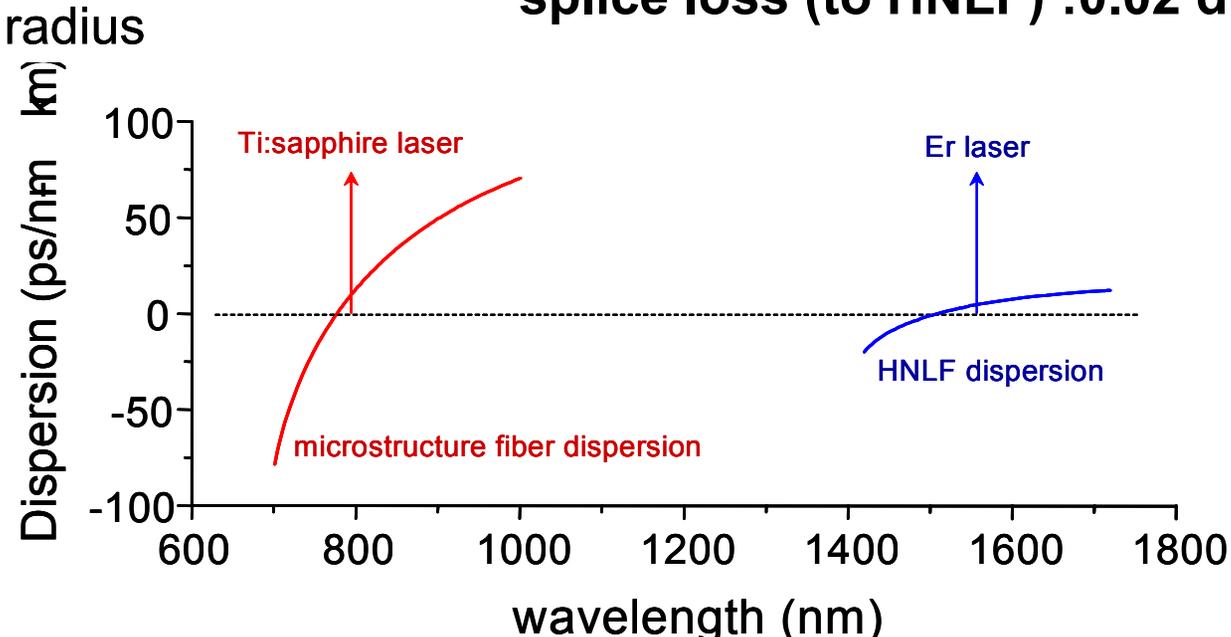
-10 to +10 ps/nm-km

dispersion slope (1550 nm) :

0.024 ps/nm<sup>2</sup>-km

splice loss (to SMF) : 0.18 dB

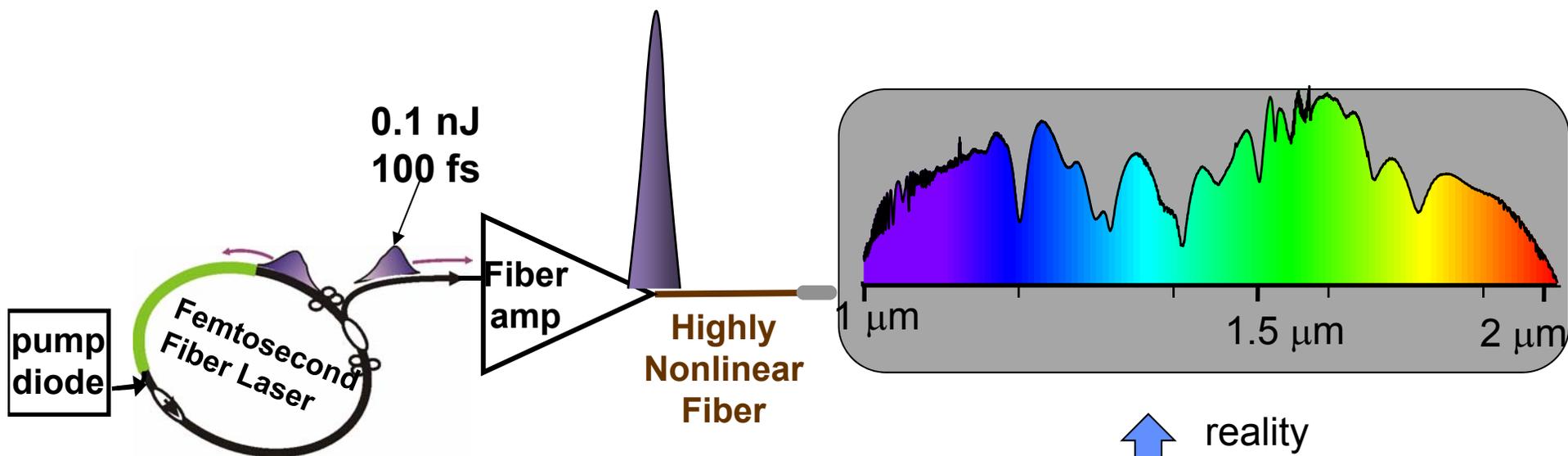
splice loss (to HNLf) : 0.02 dB



# Fiber Laser Frequency Comb

## Octave Spanning Comb

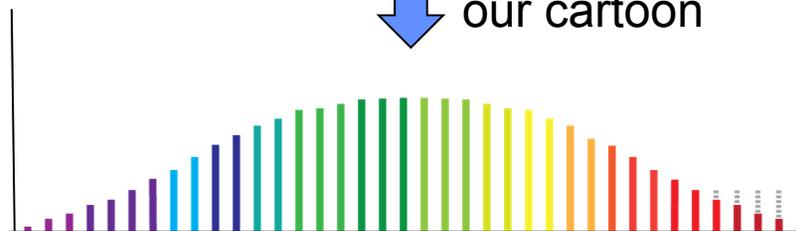
NIST



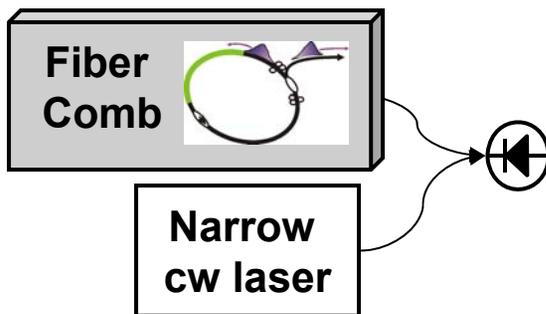
reality

our cartoon

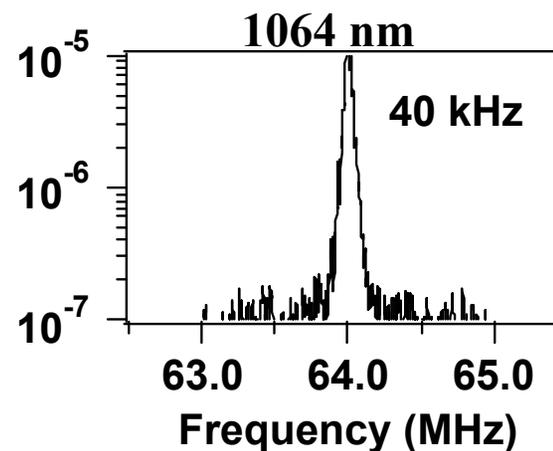
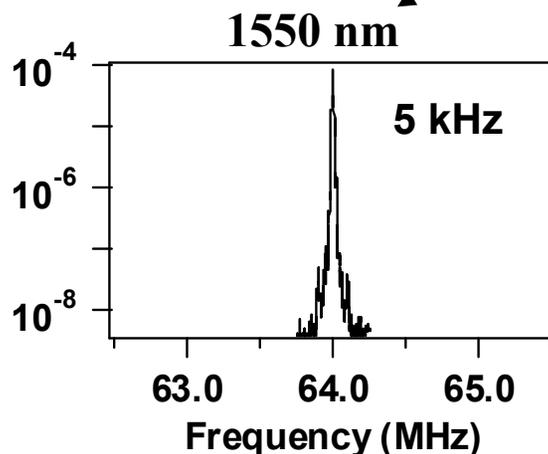
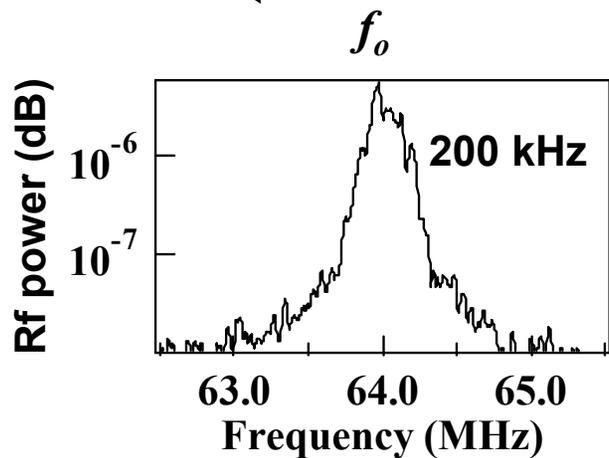
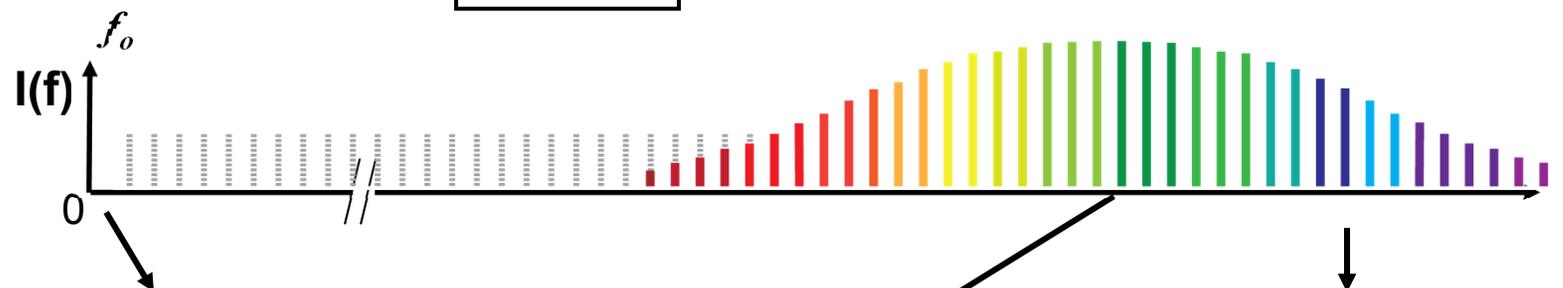
How noisy is the free-running comb?  
What causes this noise?  
How do we feedback against it?



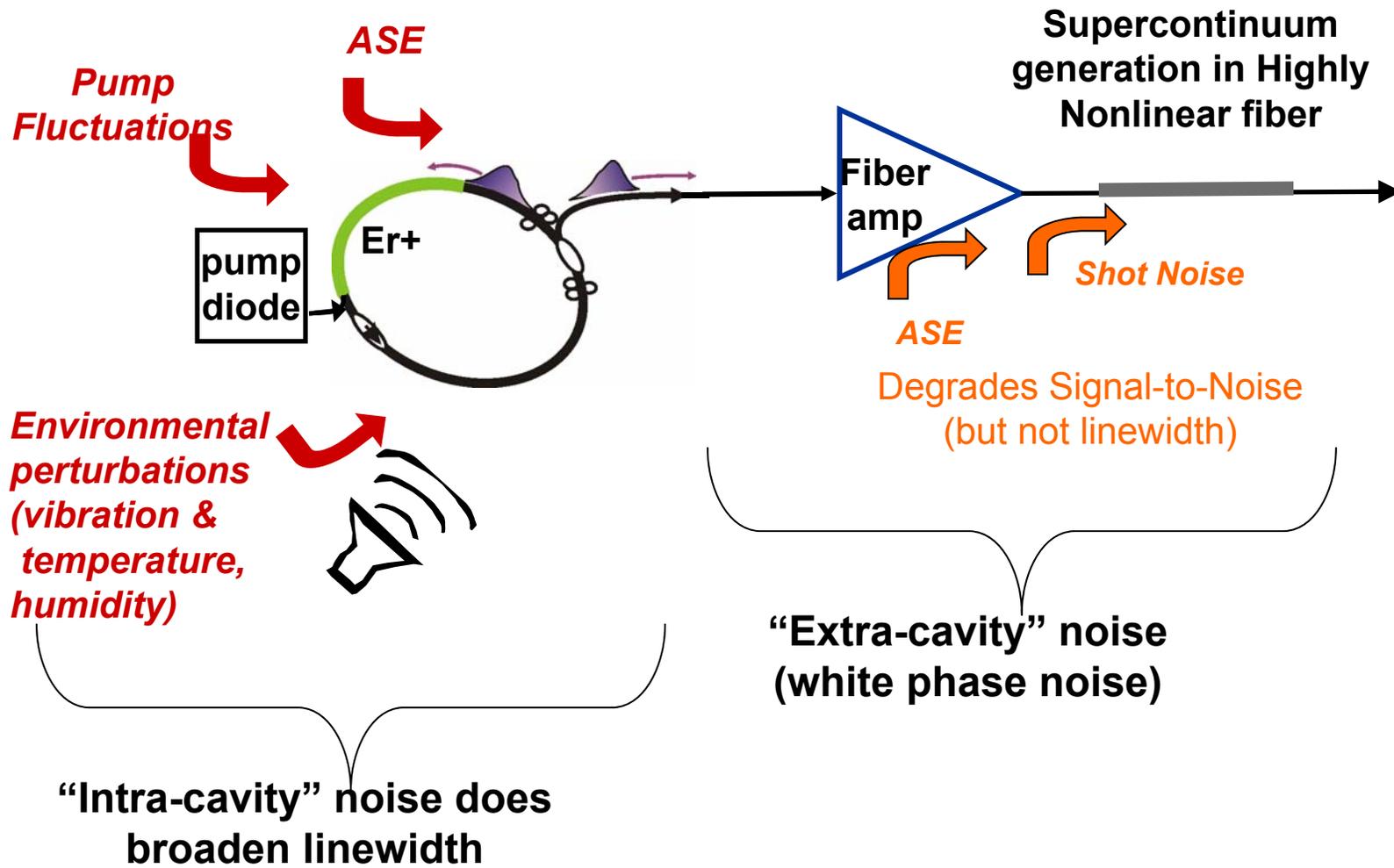
# Free-running Linewidths



**We would like 1 Hz linewidths (or rather sub-radian phase noise)**



# Noise Sources



# How to characterize the frequency comb response to noise (and actuators)? NIST

---

## 1. Use Fixed Point

- $f_n = nf_r + f_{ceo}$  → tempting to characterize noise by effect on  $f_r$  and  $f_{ceo}$  → **Don't!**
- All\* noise/actuators change  $f_r$
- But differ in their “Fixed point”

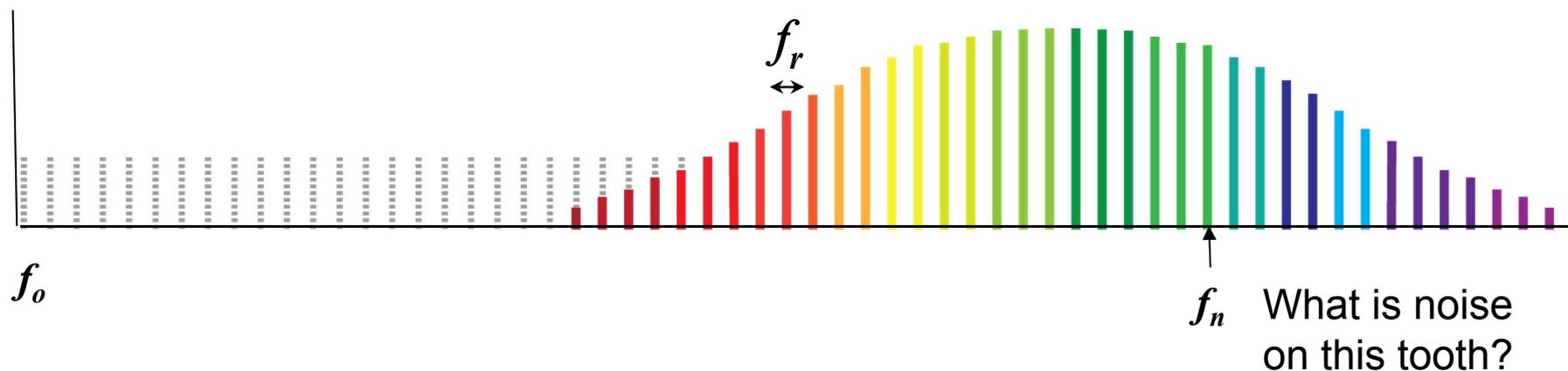
## 2. Use Frequency noise PSD

- Always characterize by frequency (or phase) noise power spectral density
- Linewidth is a (misleading) convenience

(\* except self phase modulation or external AOM)

# Perturbation -> Comb Noise Must be “accordion like”

From H. Telle and coworkers: H. R. Telle, B. Lipphart, and J. Stenger, APB, 74, 1 (2002)

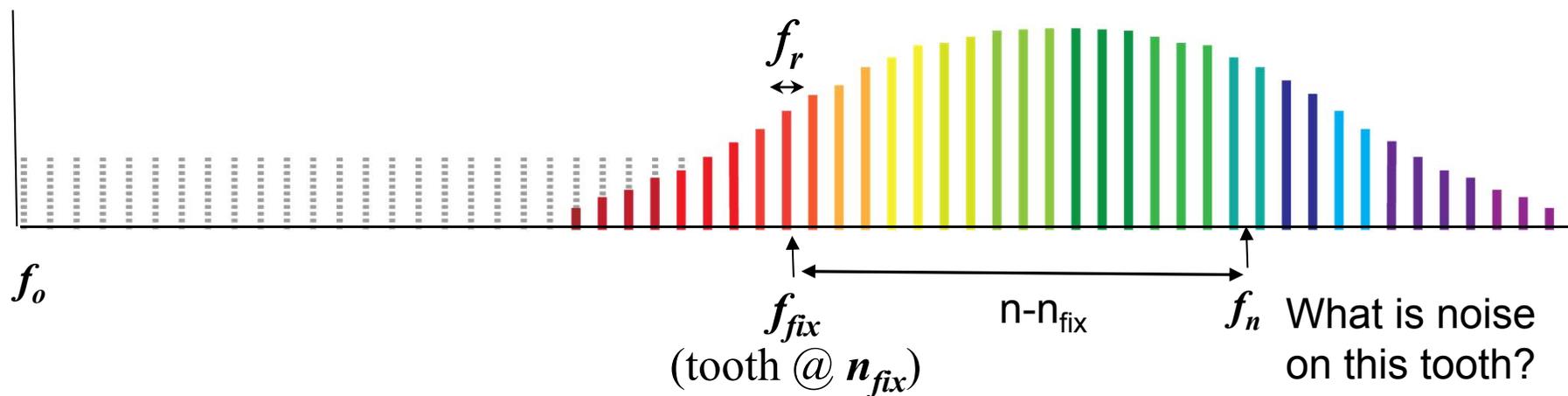


$$\delta f_n = n\delta f_{rep} + \delta f_o$$

Correlated!!

# “Fixed-Point” picture for Noise

From H. Telle and coworkers: H. R. Telle, B. Lipphart, and J. Stenger, APB, 74, 1 (2002)



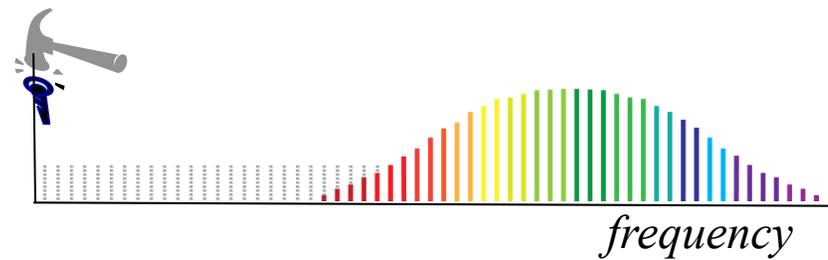
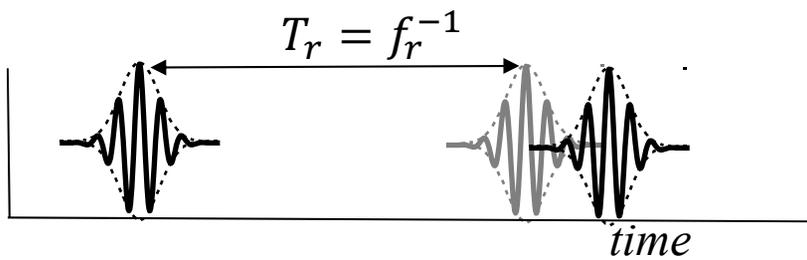
$$\delta f_n = (n - n_{fix}) \delta f_{rep}$$

Any noise described by:

1. Fixed tooth that does not move
2. Repetition rate change about that point

# Where is the fixed point? Three important cases

Round trip & Carrier Phase shift together

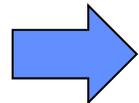


# How to characterize the frequency comb response to noise (and actuators)? NIST

---

## 1. Use Fixed Point

- $f_n = nf_r + f_{ceo}$  → tempting to characterize noise by effect on  $f_r$  and  $f_{ceo}$  → **Don't!**
- All\* noise/actuators change  $f_r$
- But differ in their “Fixed point”



## 2. Use Frequency noise PSD

- Always characterize by frequency (or phase) noise power spectral density
- Linewidth is a (misleading) convenience

(\* except self phase modulation or external AOM)

# Frequency Noise PSD

- Can use phase noise PSD to by just dividing by  $f^2$

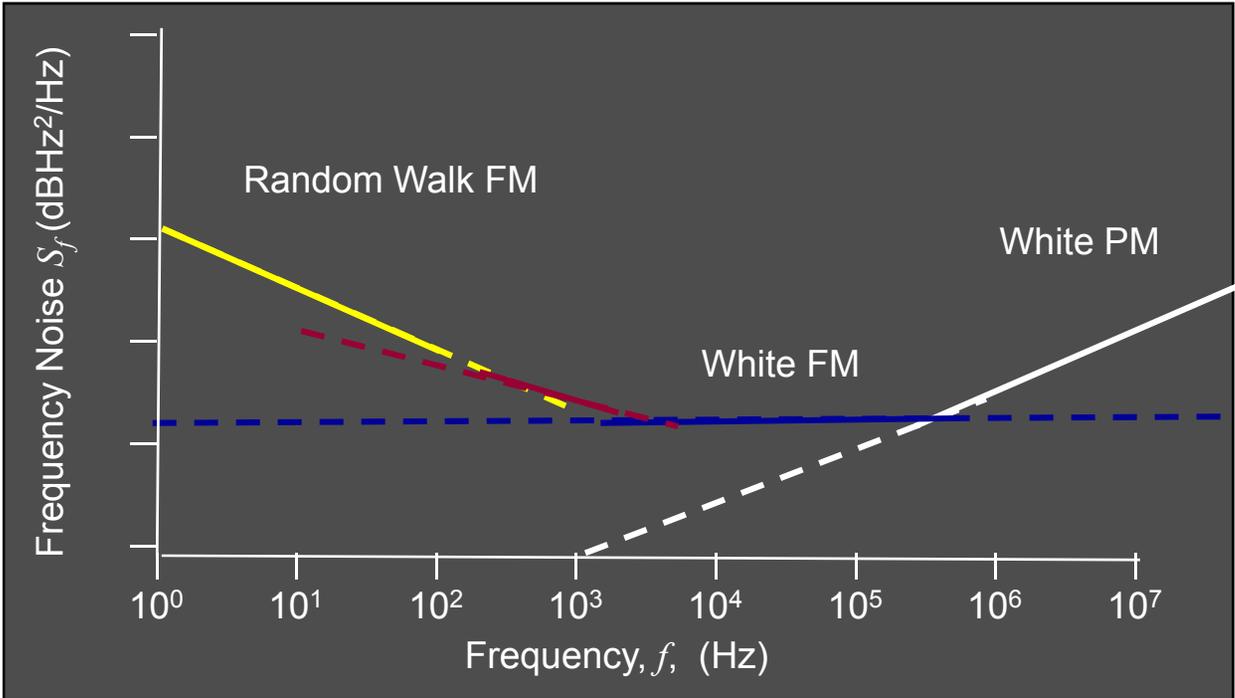


$$\langle \delta f_n^2 \rangle$$

FFT

## Frequency Noise PSD: $S_n$

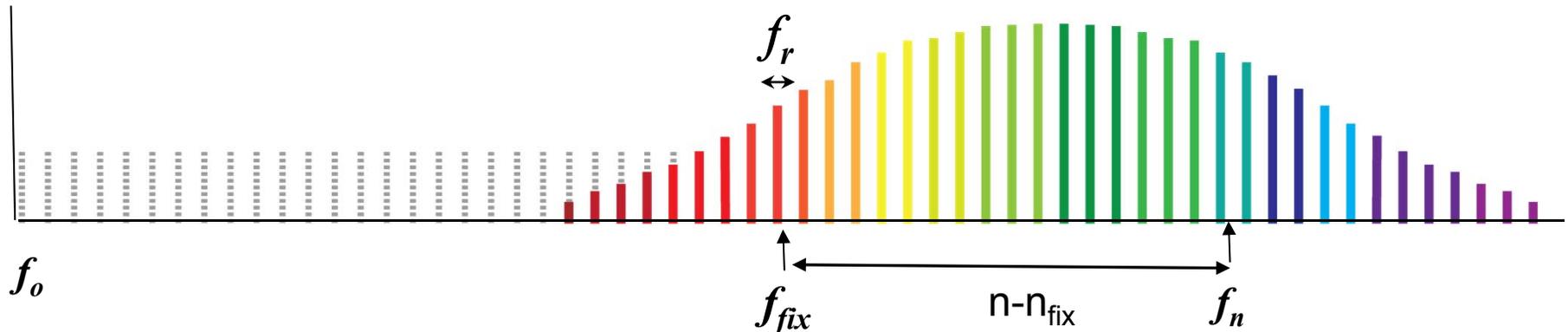
*How far tooth moves*



*How fast tooth moves*

# “Fixed-Point” picture for Noise

From H. Telle and coworkers: H. R. Telle, B. Lipphart, and J. Stenger, APB, 74, 1 (2002)



(tooth @  $n_{fix}$ )

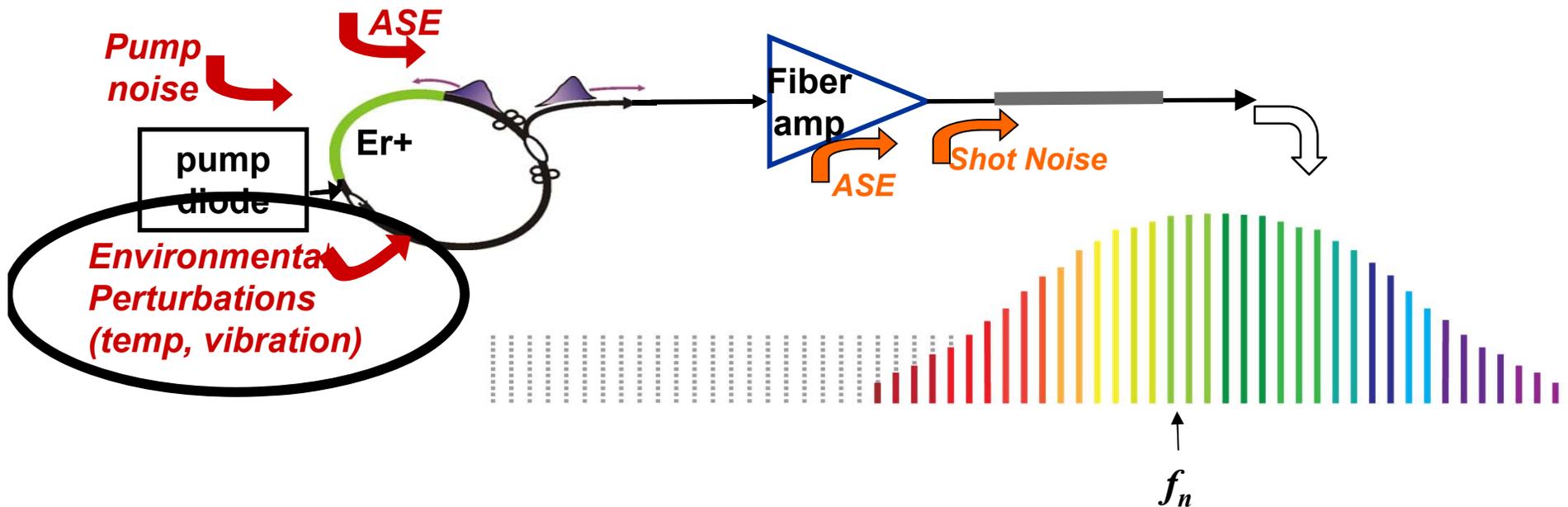
What is noise on this tooth?

Frequency Noise PSD

$$\langle \widetilde{\delta f_n^2} \rangle = S_n = (n - n_{fix})^2 S_{frep}$$

Noise on any tooth is just “scaled” repetition rate noise

# Quantifying the Noise on the Comb Summing Frequency Noise PSD



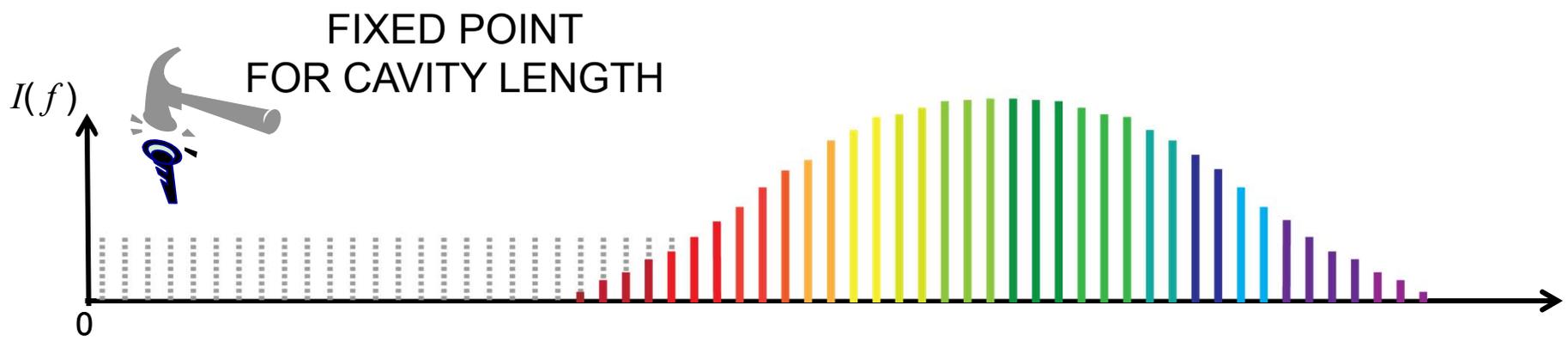
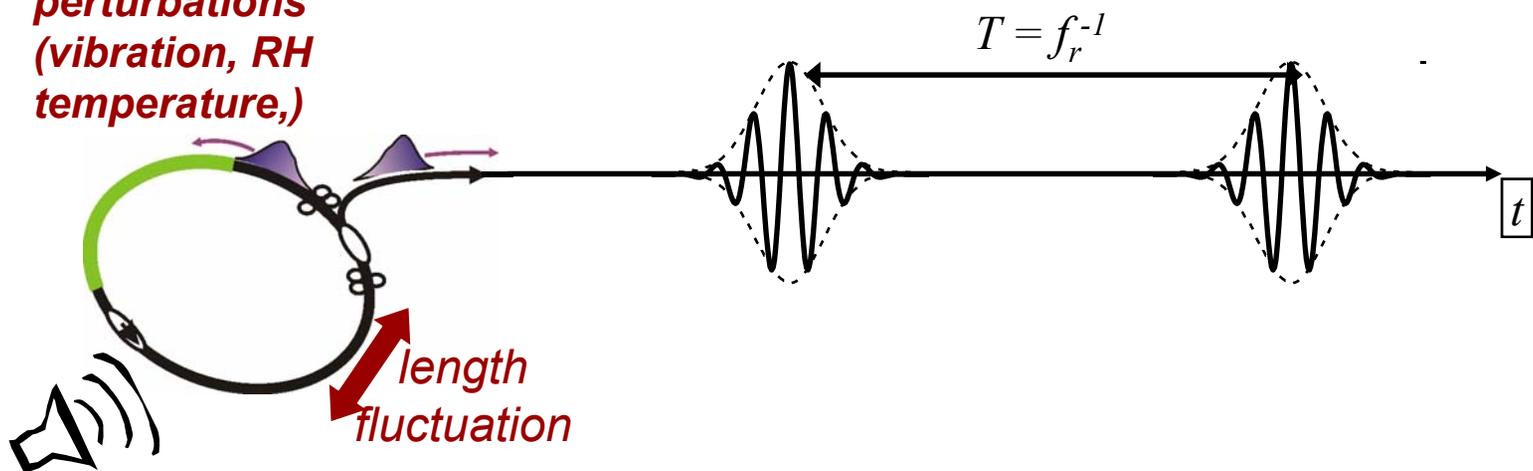
What is noise on the  $n$ th tooth? Sum of noise from each effect

$$S_n = \left( n - n_{fix}^{temp} \right)^2 S_{temp} + \left( n - n_{fix}^{vib} \right)^2 S_{vib} + \left( n - n_{fix}^{ASE} \right)^2 S_{ASE} + \left( n - n_{fix}^{pump} \right)^2 S_{pump} + \dots$$

$$\langle \delta f_n^2 \rangle = \langle \delta f_n^2 \rangle \text{ from temperature} + \langle \delta f_n^2 \rangle \text{ from vibrations} + \langle \delta f_n^2 \rangle \text{ from amplified spontaneous emission} + \langle \delta f_n^2 \rangle \text{ from pump noise}$$

# Environmental Perturbations -> Cavity length

**Environmental perturbations (vibration, RH temperature,)**

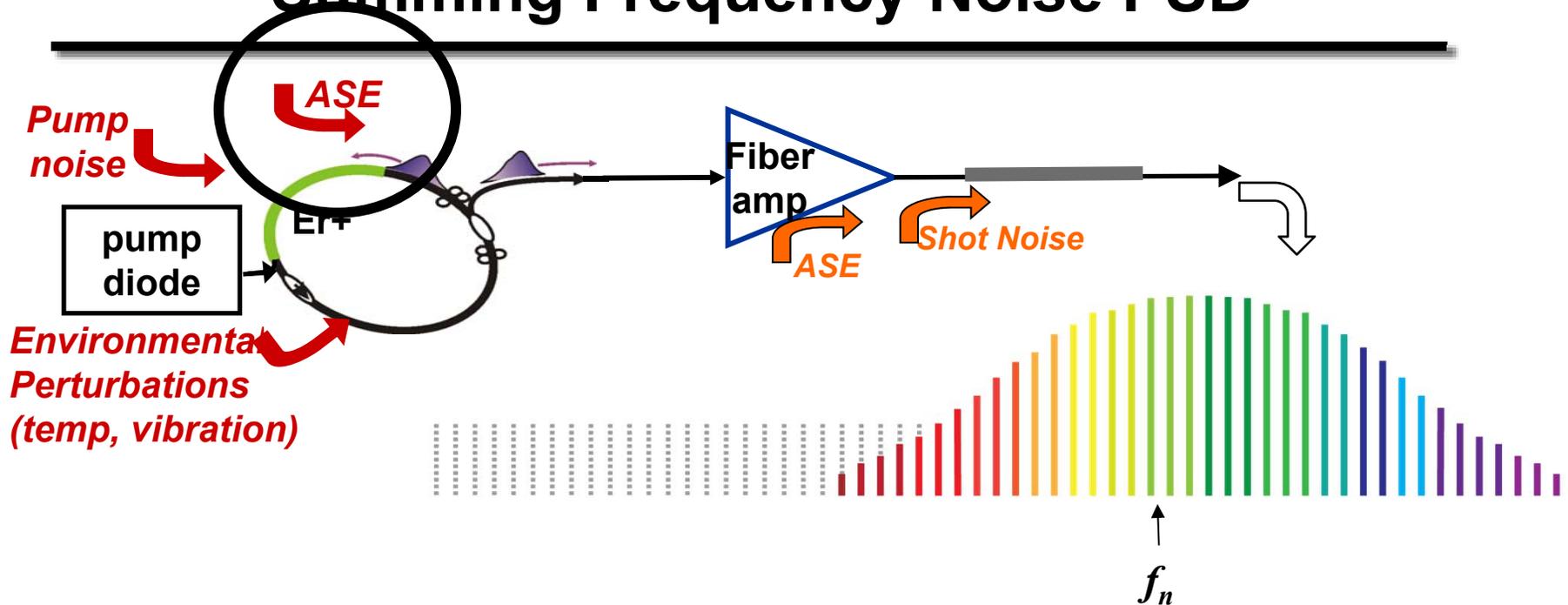


$f_0$

Temperature:  $10^{-5}$  per degree C (very sensitive)  
Vibration/Humidity: very sensitive  
 $S \sim 1/f$  behavior

# Quantifying the Noise on the Comb Summing Frequency Noise PSD

NIST



What is noise on the nth tooth? Sum of noise from each effect

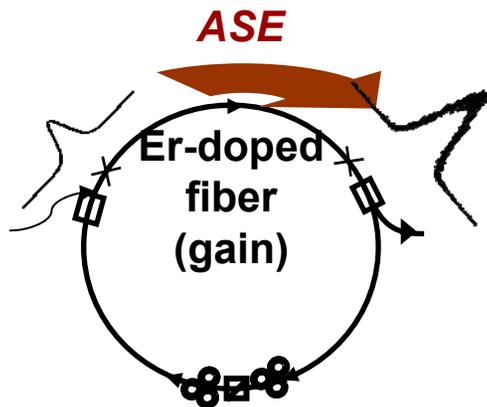
$$S_n = (n - n_{fix}^{temp})^2 S_{temp} + (n - n_{fix}^{vib})^2 S_{vib} + (n - n_{fix}^{ASE})^2 S_{ASE} + (n - n_{fix}^{pump})^2 S_{pump} + \dots$$

$$\langle \delta f_n^2 \rangle = \langle \delta f_n^2 \rangle \text{ from temperature} + \langle \delta f_n^2 \rangle \text{ from vibrations} + \langle \delta f_n^2 \rangle \text{ from amplified spontaneous emission} + \langle \delta f_n^2 \rangle \text{ from pump noise}$$

# Effect of Amplified Spontaneous Emission Direct Timing Jitter

Often called Quantum Limit for mode-locked lasers

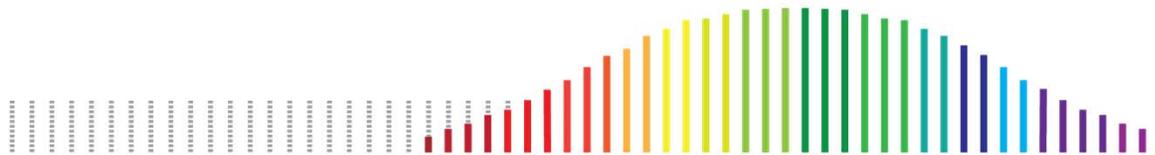
- H. A. Haus and A. Mecozzi, IEEE J. Quantum Electron. 29, 983 (1993).
- R. Paschotta, Appl Phys. B 79, 163 (2004).



$$\text{Pulse at } t_{arrival} + \text{ASE} = \text{Pulse at } t_{arrival} \pm \delta t = \text{Round Trip Timing Shift}$$



Comb expands/contracts about center of spectrum

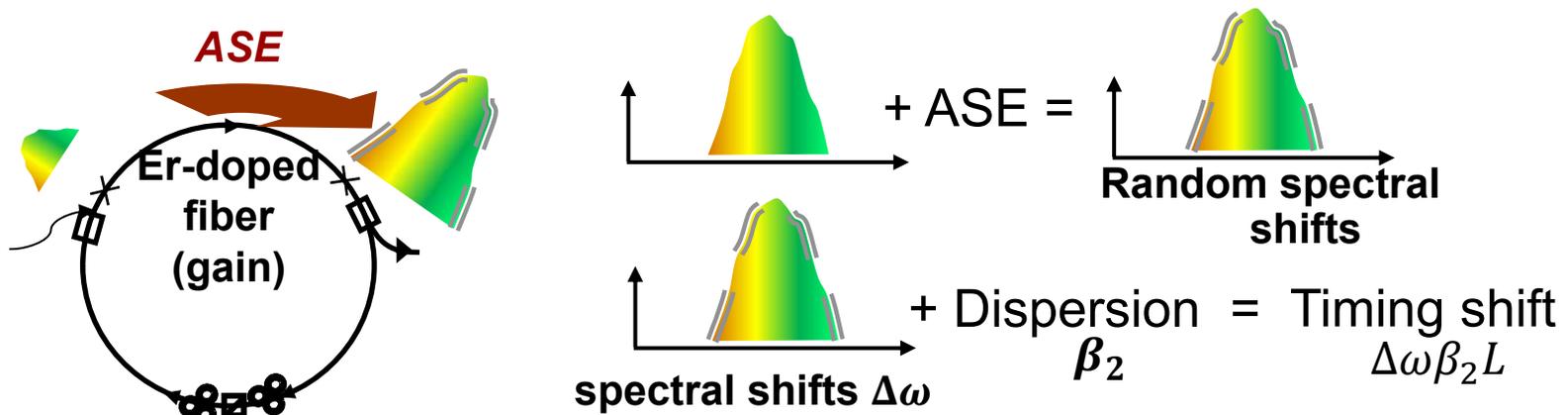


$S_{ASE} \sim$  white noise (broadband)

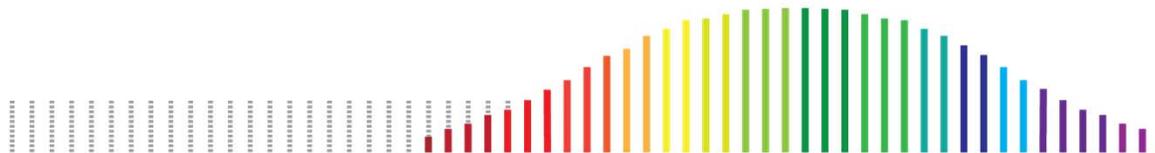
\* phase jitter gives  
S-T linewidth

# Effect of Amplified Spontaneous Emission Indirect Timing Jitter

- H. A. Haus and A. Mecozzi, IEEE J. Quantum Electron. 29, 983 (1993).
- R. Paschotta, Appl Phys. B 79, 163 (2004).



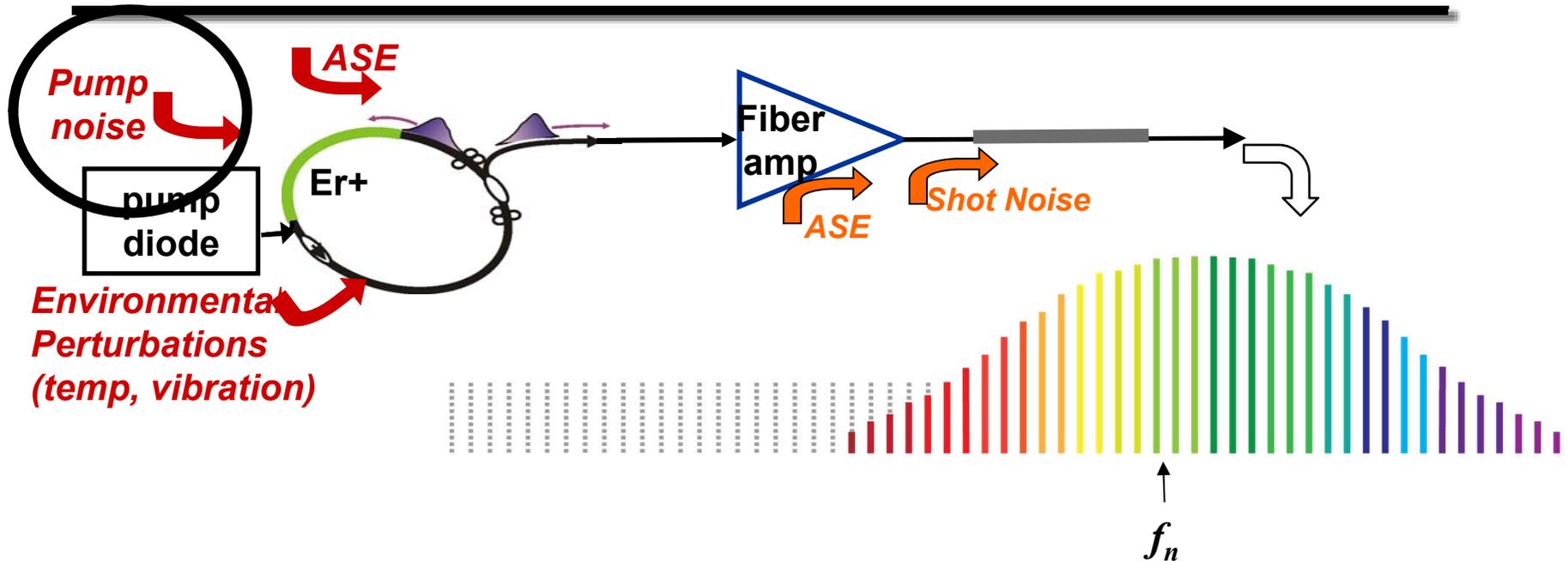
Comb expands/contracts about center of spectrum



***This effect dominates ASE timing jitter at high cavity dispersion***

# Quantifying the Noise on the Comb Summing Frequency Noise PSD

NIST



What is noise on the nth tooth? Sum of noise from each effect

$$S_n = (n - n_{fix}^{temp})^2 S_{temp} + (n - n_{fix}^{vib})^2 S_{vib} + (n - n_{fix}^{ASE})^2 S_{ASE} + (n - n_{fix}^{pump})^2 S_{pump} + \dots$$

$$\langle \delta f_n^2 \rangle = \langle \delta f_n^2 \rangle \text{ from temperature} + \langle \delta f_n^2 \rangle \text{ from vibrations} + \langle \delta f_n^2 \rangle \text{ from amplified spontaneous emission} + \langle \delta f_n^2 \rangle \text{ from pump noise}$$

# How to solve for the Response of the Fiber-Laser Frequency Comb

NIST

## Three Options

(1) ✓

### Heuristic derivation

- **Physical insight**
- **Ad hoc**
- **Numerical factors sometimes obscure**
- **Implementation:**
  - L. Xu, et al. *Opt. Lett.*, vol. 21, 1996, Haverkamp, *APB* 78, 2004, etc.

(2) ✓

### Master Equation & Perturbation Theory

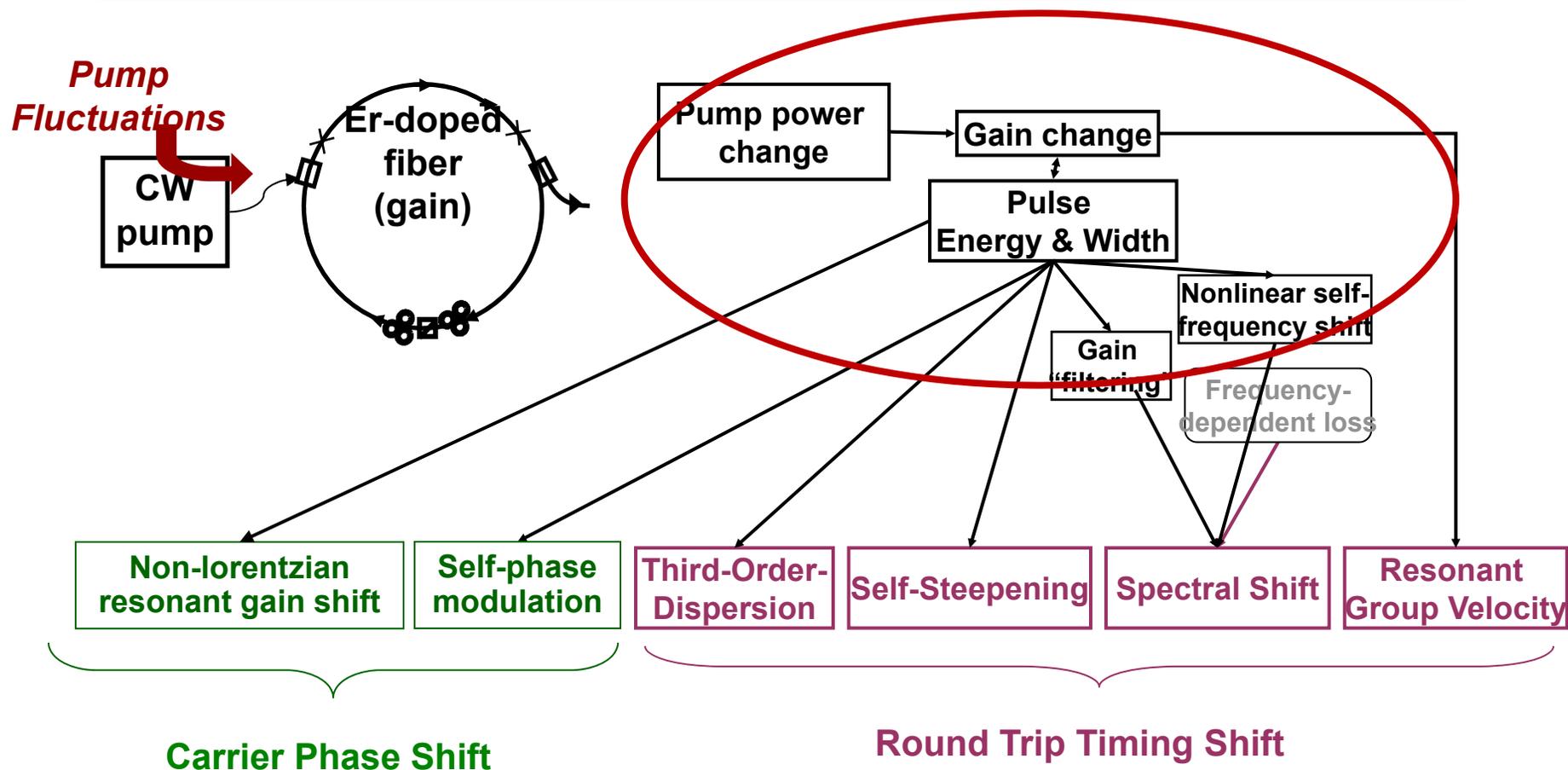
- **Analytic, self-consistent treatment**
- **Rigorous bookkeeping**
- **Requires analytic perturbations (e.g. Lorentzian gain .)**
- **Master equation is an approximation**
- **Implementation:**
  - Haus and Mecozzi, *JQE.*, vol. 29, 1993.
  - But add chirp, gain dynamics, all perturbations

(3)

### Numerical integration of Nonlinear Schrödinger Eq.

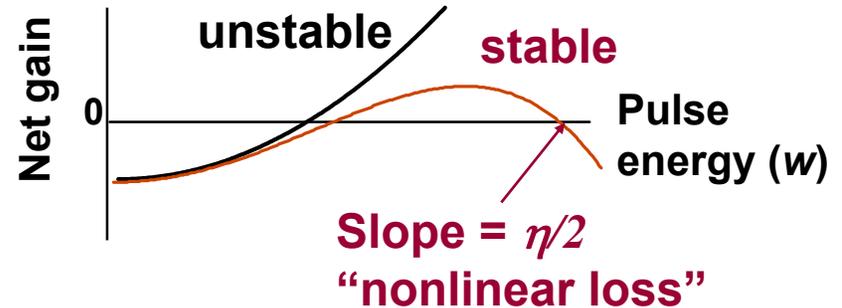
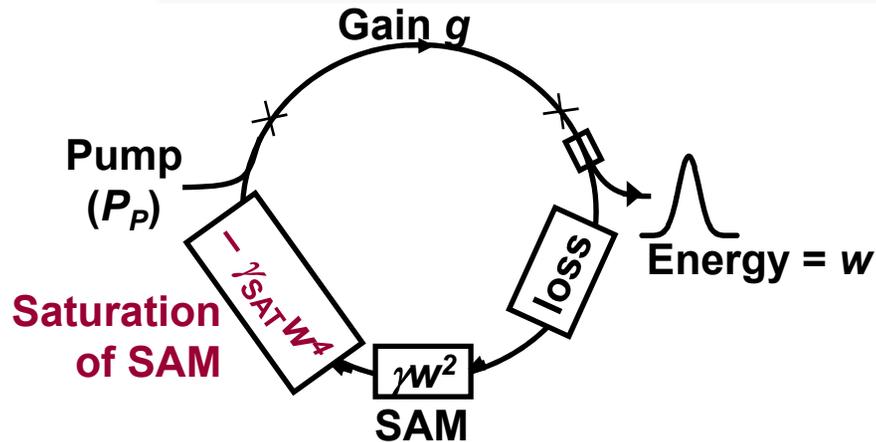
- **Full solution of NLSE**
- **Include all effects**
- **Significant computation (pulse width vs round trip vs response time)**
- **Potential loss of physical insight**
- **Implementation:**
  - Paschotta, *Appl. Phys. B*, vol. 79, 2004.

# Effect of Pump Power Noise on Comb



# Response Bandwidth and Laser Stability NIST

## (Gain-Pulse Energy Coupling)



### Coupled differential equations

$$\text{Energy round trip } \partial_T \Delta w = -\frac{1}{T_r} [\eta \Delta w - 2 \Delta g w]$$

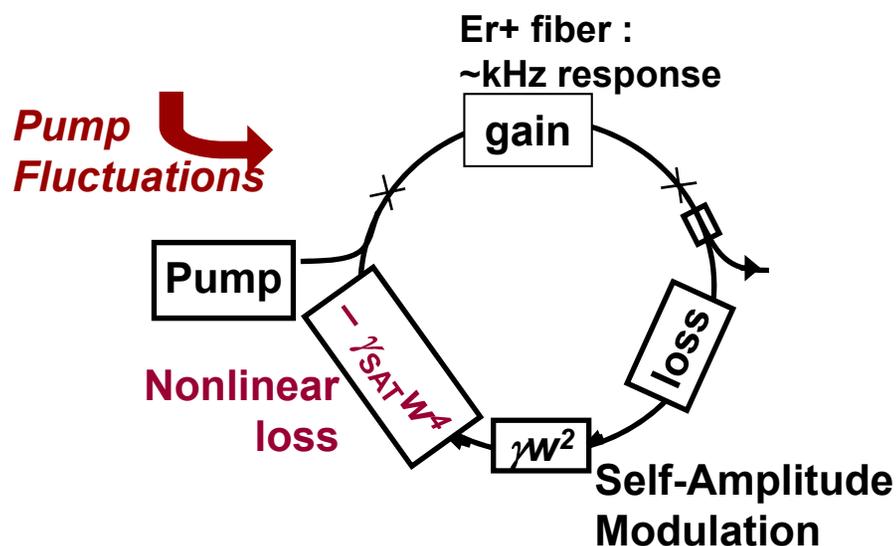
$$\text{Gain round trip } \partial_T \Delta g = -\frac{1}{T_g} \left[ \Delta g + g_w \frac{\Delta w}{w} - g_p \frac{\Delta P_p}{P_p} \right]$$

Eigenvalues:  
Time constants

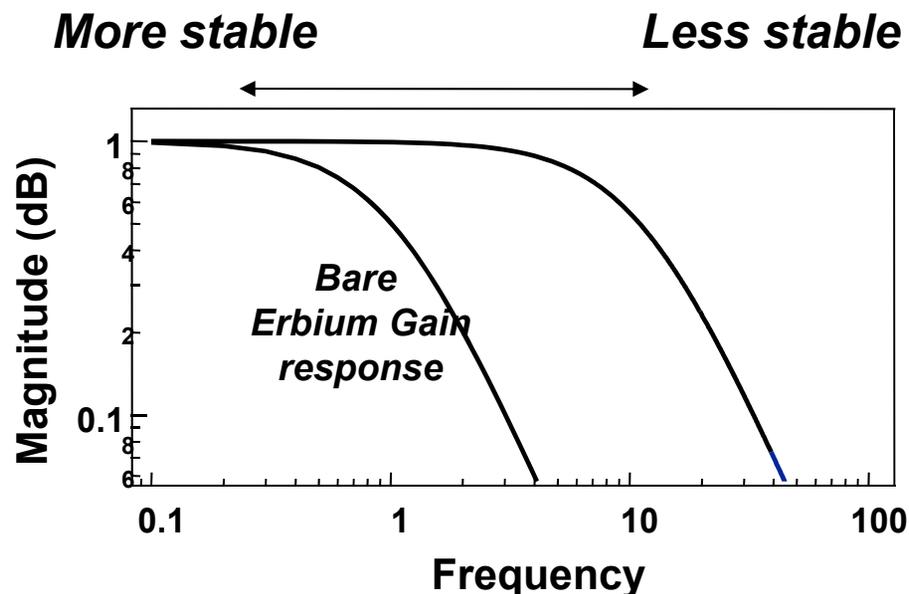
$$v_{3dB} = \left( 1 + \frac{1}{\eta} \right) v_{3dB}^{Erbium}$$

- System is unstable without extra nonlinear loss
  - Gain saturation too slow to counteract SAM
- Parameters support simple exponential decay
  - No relaxation oscillations (see Namiki et al, APL, 69,3969 (1996))

# Dynamics Pump Power Noise on Comb Responds as a Low-Pass Filter

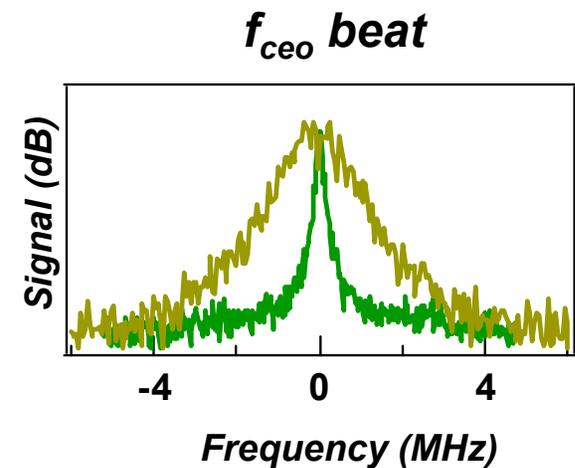
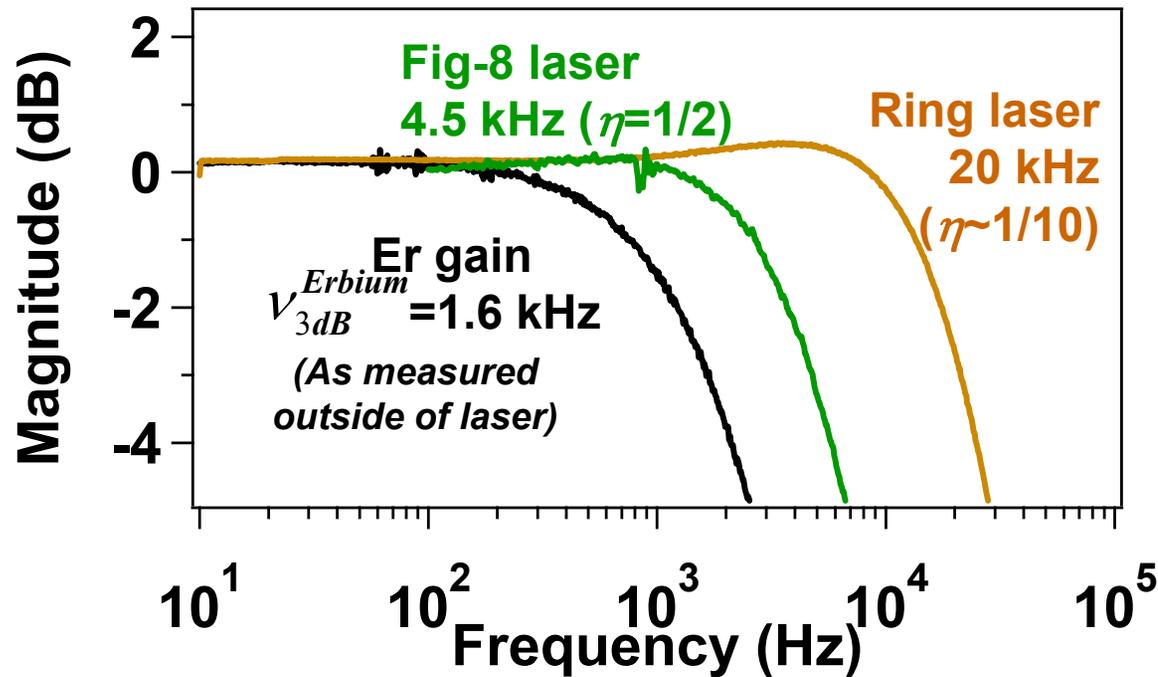
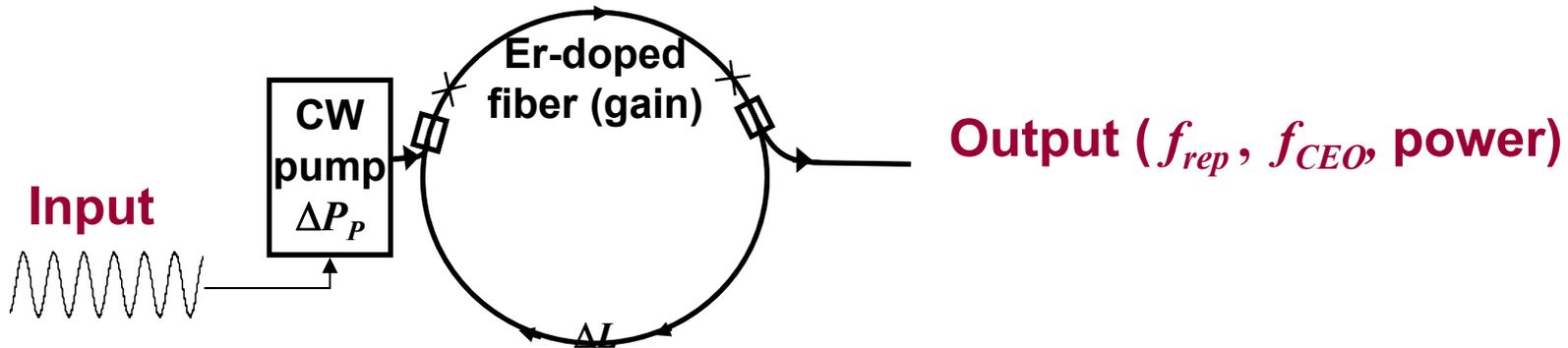


## Response to Pump Power change

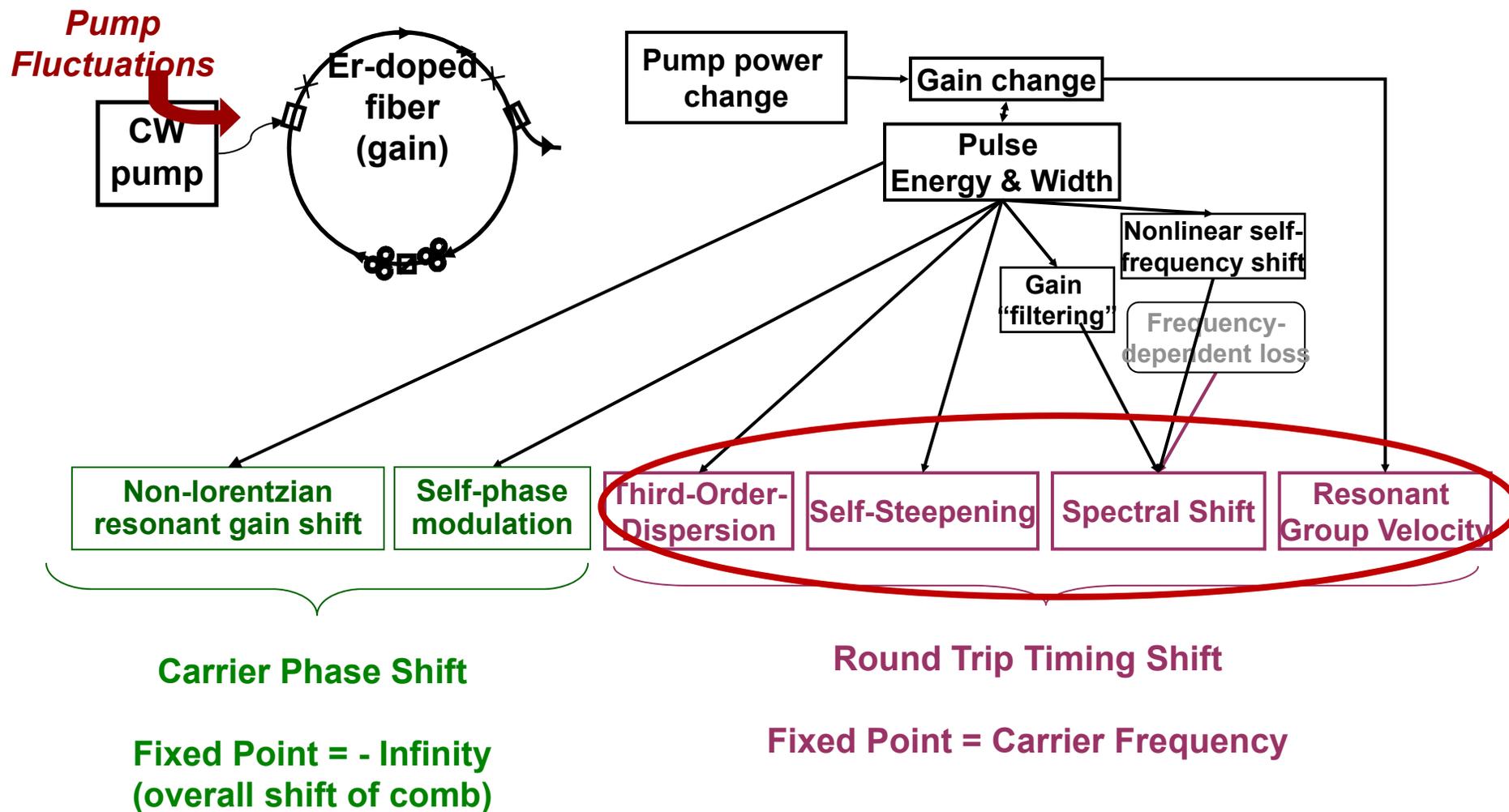


- **Overdamped system -> No Relaxation Oscillations!!**
- **Consequences:**
  - **Finite response to pump fluctuations**
  - **“Slows” laser response to pump power feedback**
  - **But can phase compensate for a simple rolloff with a capacitor!**

# Response Bandwidth: Experiment



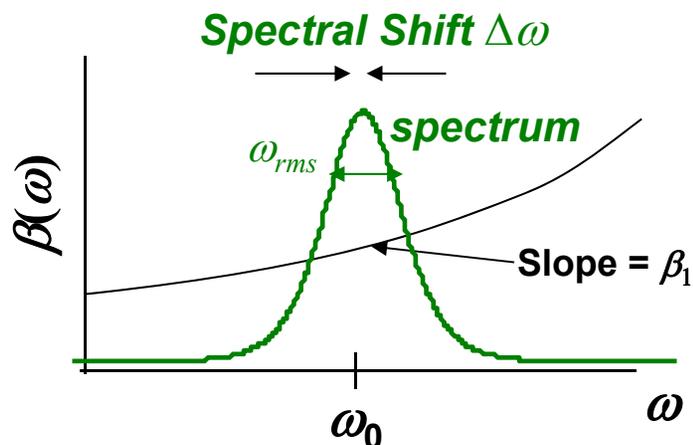
# Effect of Pump Power Noise on Comb



# Change in $f_{rep}$ : Theory (Part I)

## Spectral Shifts & Third-Order Dispersion Contributions

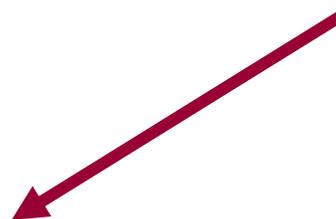
Effective Group Velocity depends on spectrum center and width



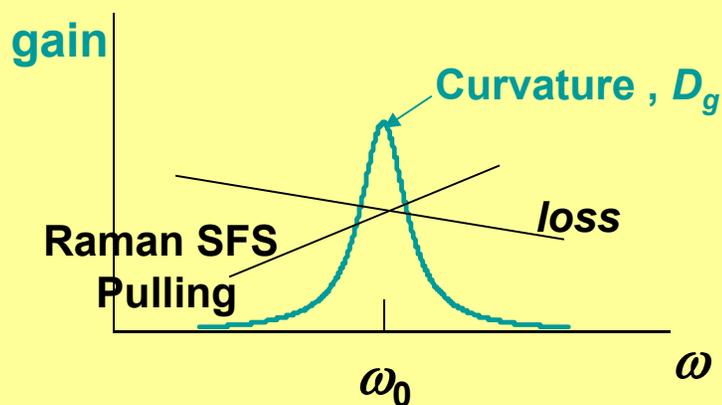
Round Trip Time Shift

$$\Delta T_r = \Delta\omega\beta_2L + \frac{1}{2}\omega_{rms}^2\beta_3L$$

Spectral Shifts      Third-order dispersion



### Cause of Spectral Shifts :

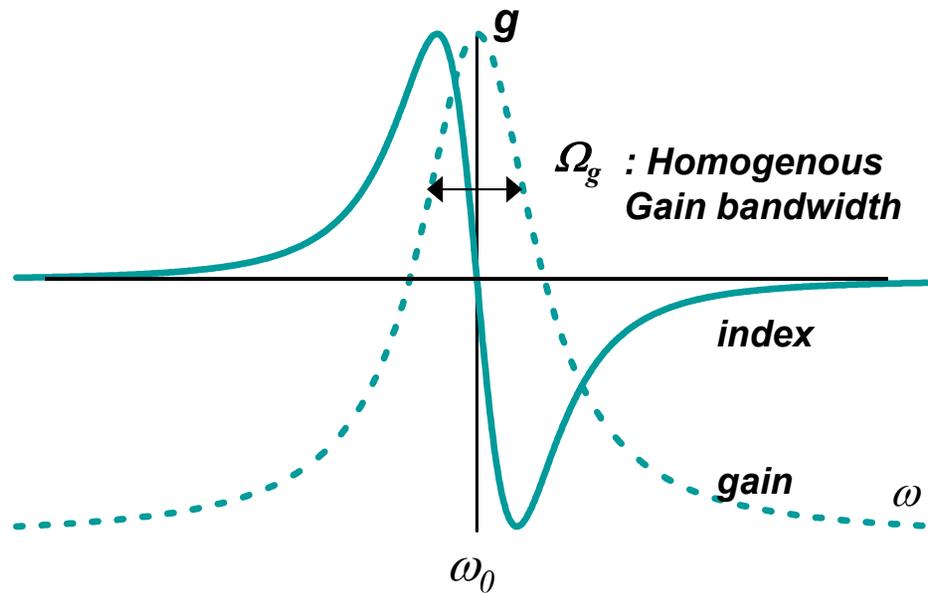


- 1.) Gain pulls frequency toward gain peak
- 2.) Loss pushes frequency up or down
- 3.) Raman SFS pushes frequency down

$$\Delta\omega = \frac{-1}{2D_g} (l_{\omega,NL} + l_{\omega})$$

# Changes in $f_{\text{rep}}$ : Theory (Part II)

## Resonant Gain Contribution



Round Trip  
Time Shift

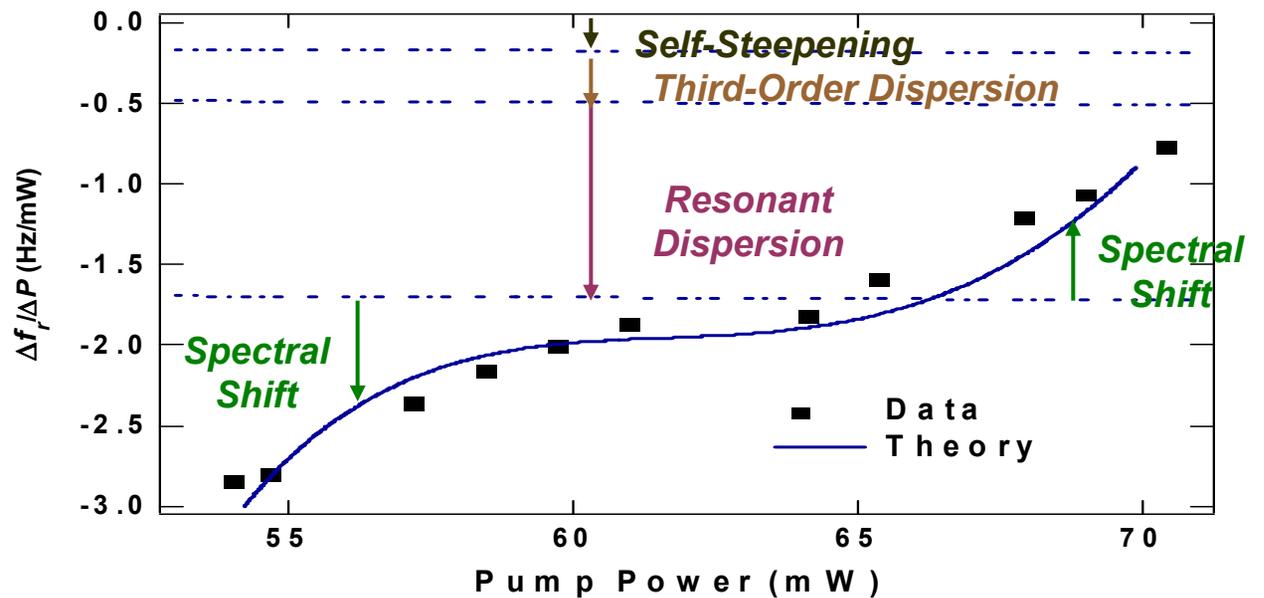
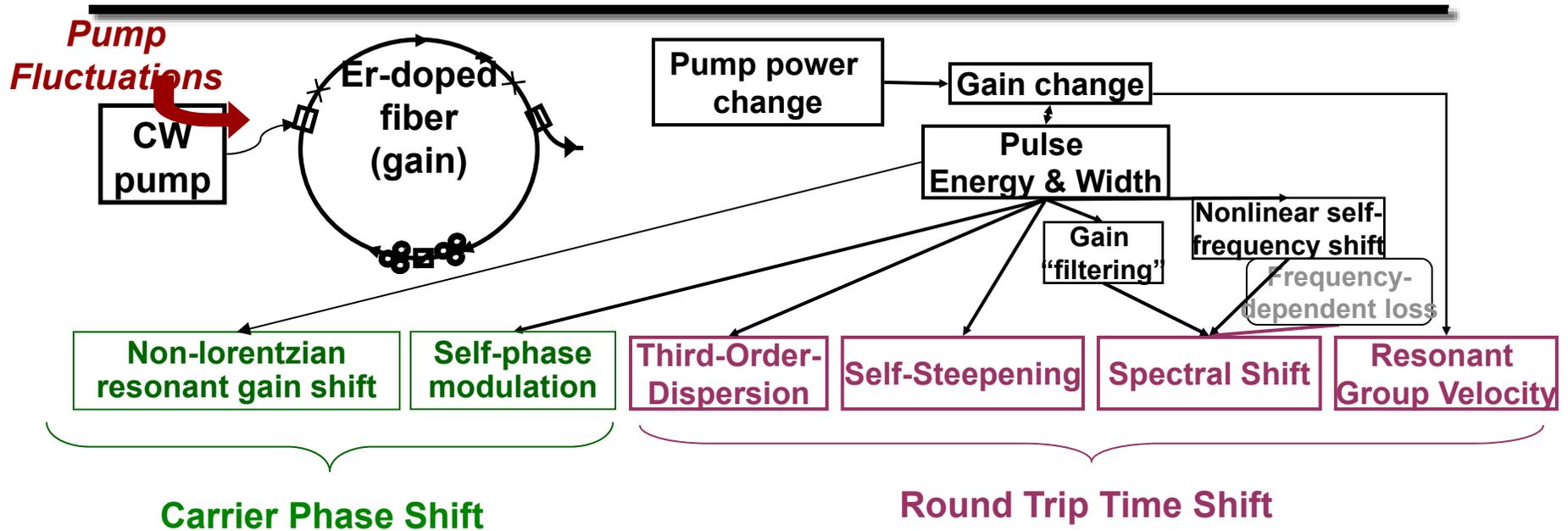
$$\Delta T_r = \frac{\Delta g L}{\Omega_g} +$$

Resonant gain  
dispersion

- Group index of the Er gain fiber depends on the Er gain inversion
- For Lorentzian gain with gain bandwidth 5 nm, maximum shift:
  - 10 ppm or 500 Hz out of 50 MHz rep. rate

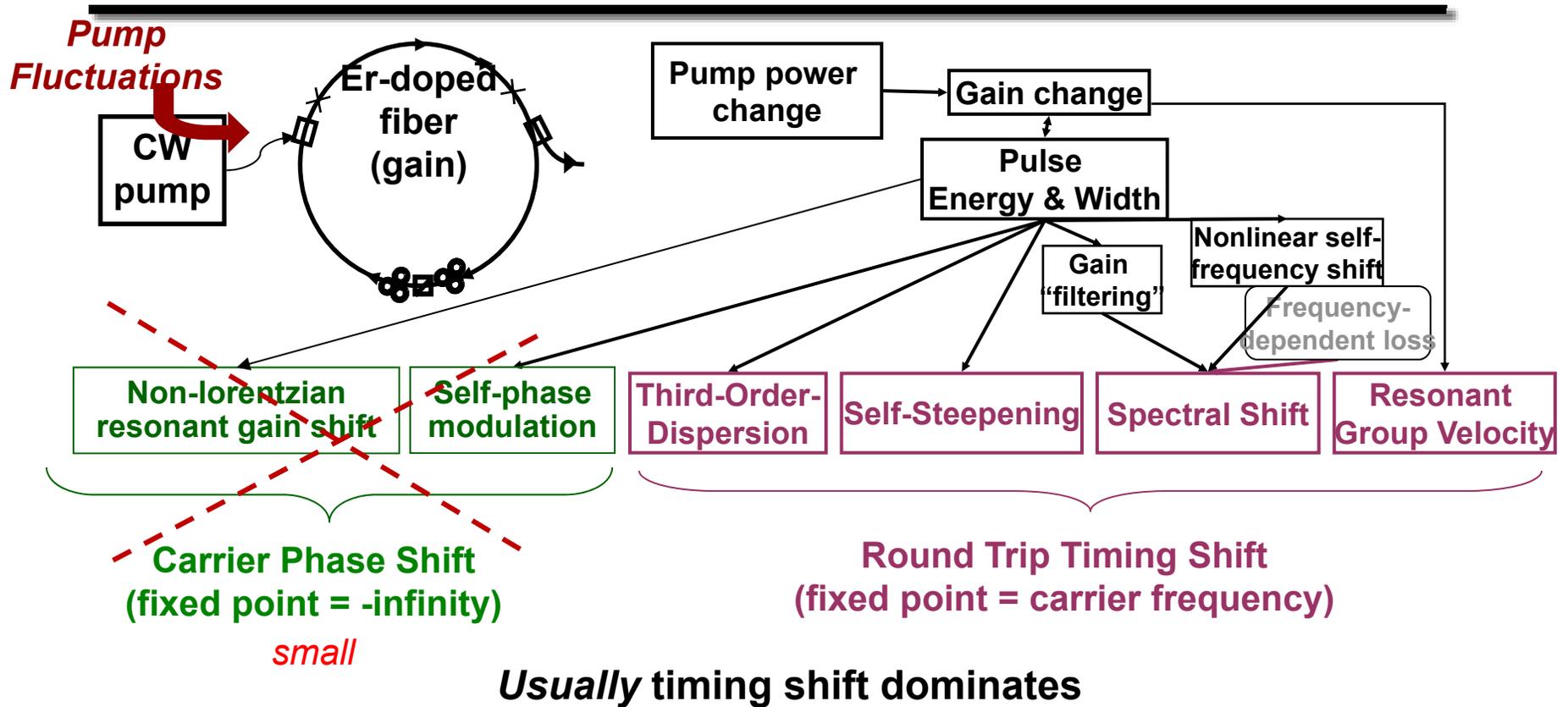
# Effect of Pump Power Noise on Comb NIST

## Summary



# Effect of Pump Power Noise on Comb NIST

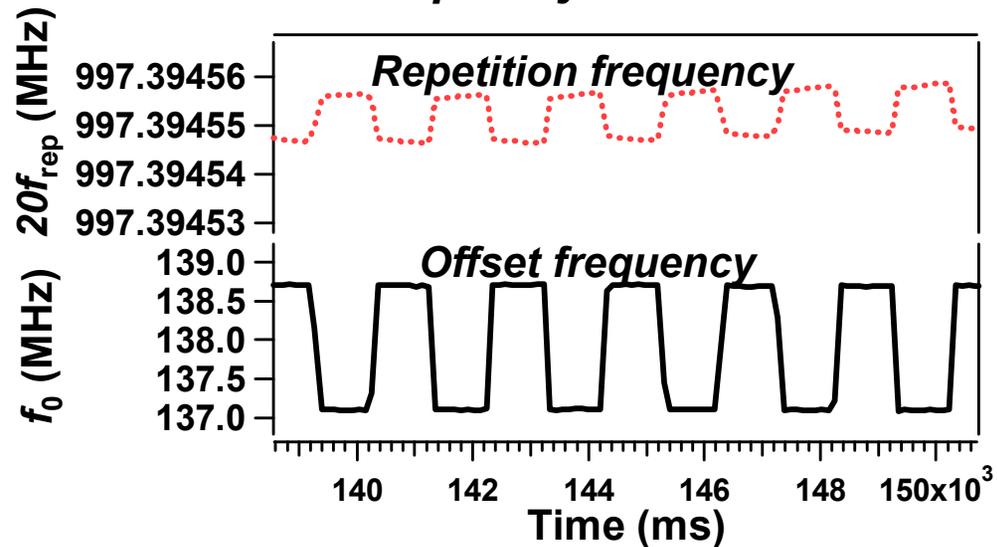
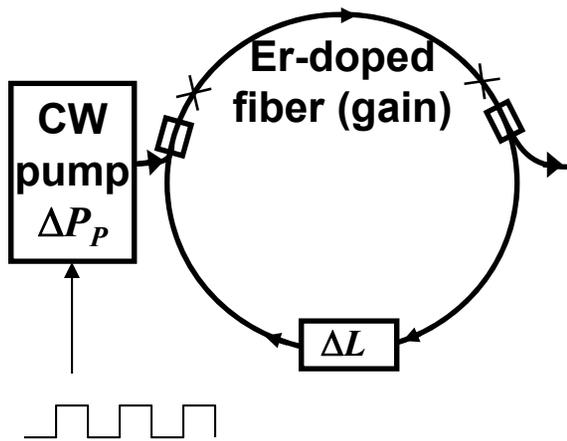
## Summary



# Experimental Data for Comb Response to Pump Power

Not hard to measure the fixed point  
Stimulate comb & measure response!

*Frequency Counter Data*



$$f_{fix} = 0 = n_{fix} \delta f_{rep} + \delta f_0$$

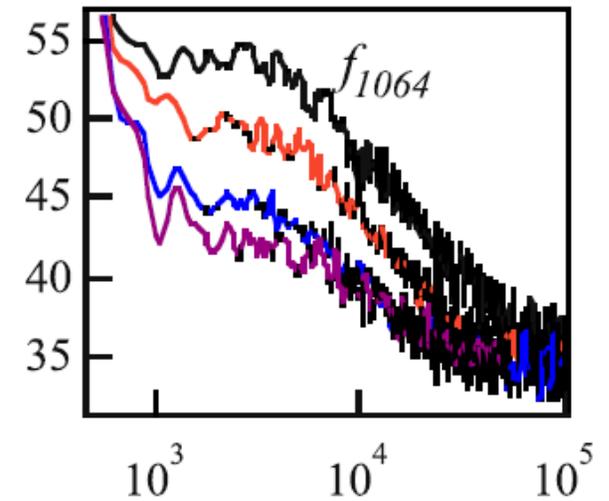
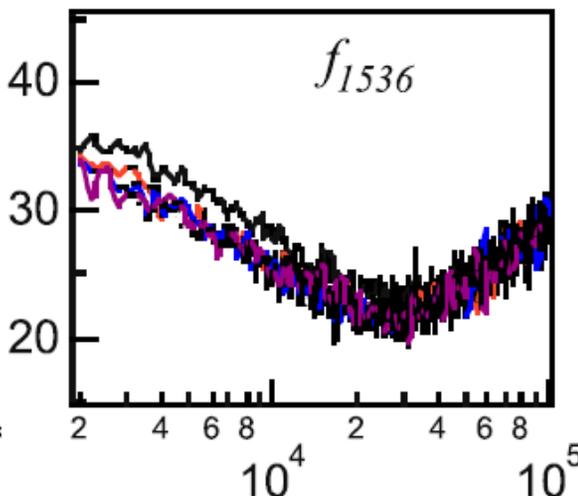
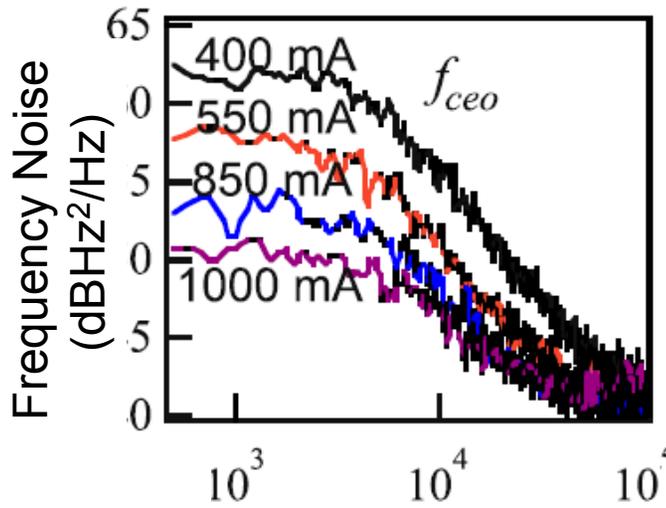
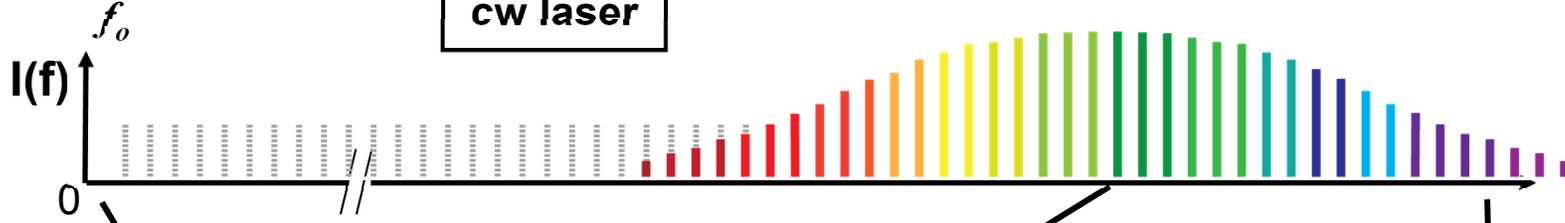
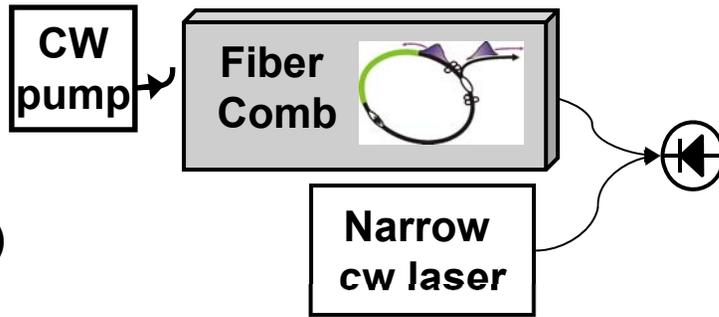
$$n_{fix} = -\frac{\delta f_0}{\delta f_{rep}}$$

Here fixed point = 150 THz fixed point

# Frequency Noise PSDs vs Pump Noise

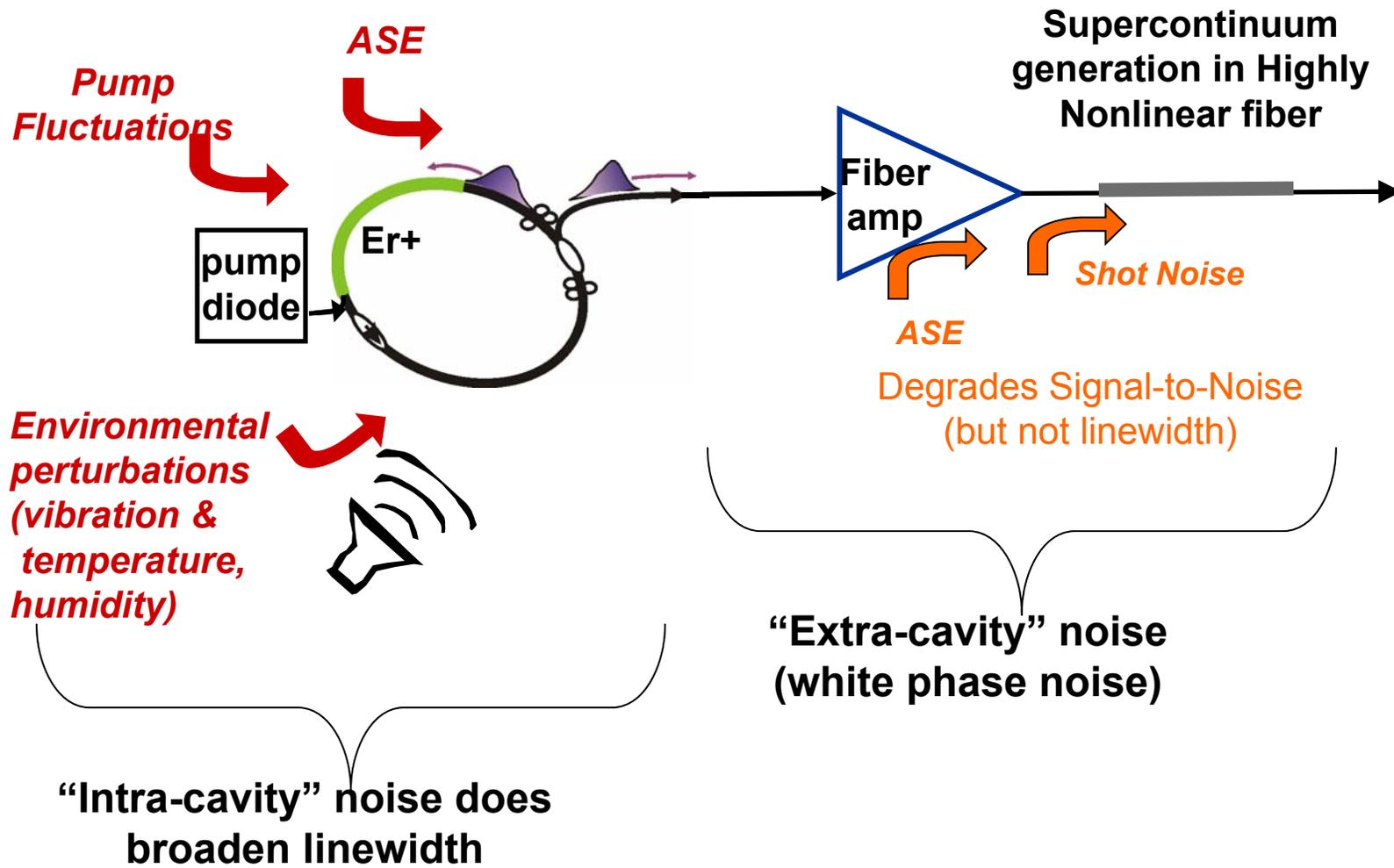
John McFerran, APB 86, 219 (2006)

Vary Pump RIN (pump current dependent)



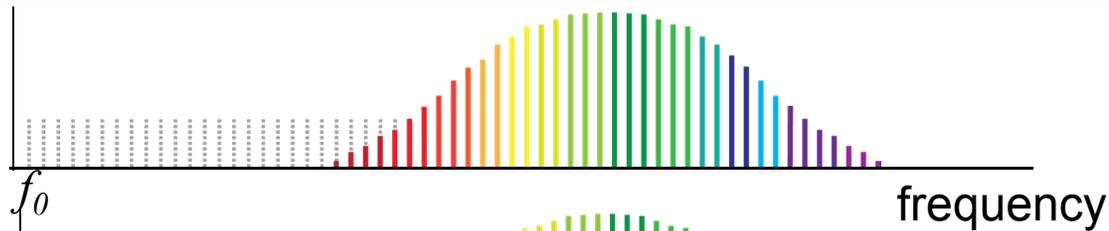
Frequency (Hz)

# Noise Sources

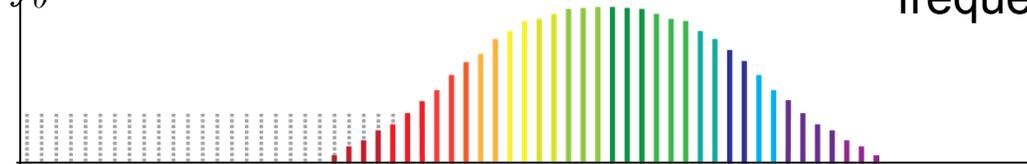


# Effect of Different Noise Source on Frequency Comb

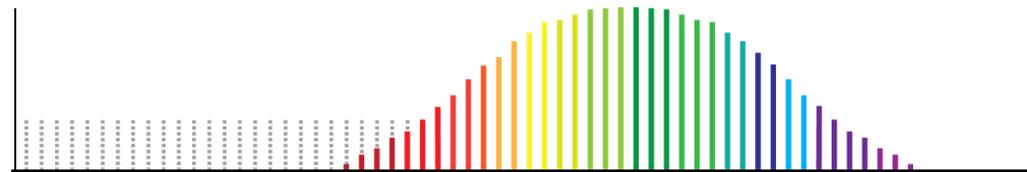
NIST



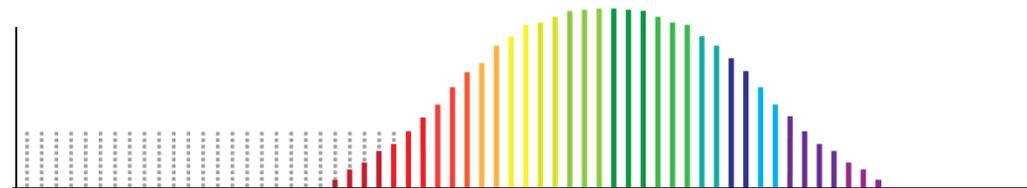
Ideal  
Output



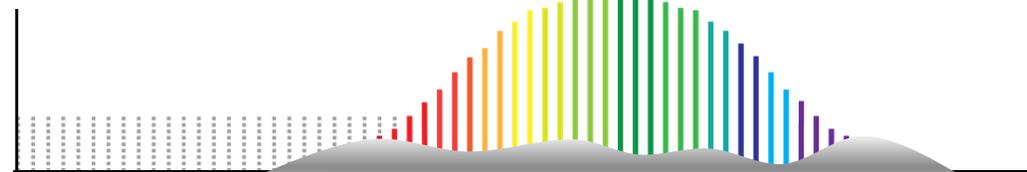
Environmental Effects  
PSD  $\sim 1/f$



Pump Noise  
PSD  $\sim$  low pass filter

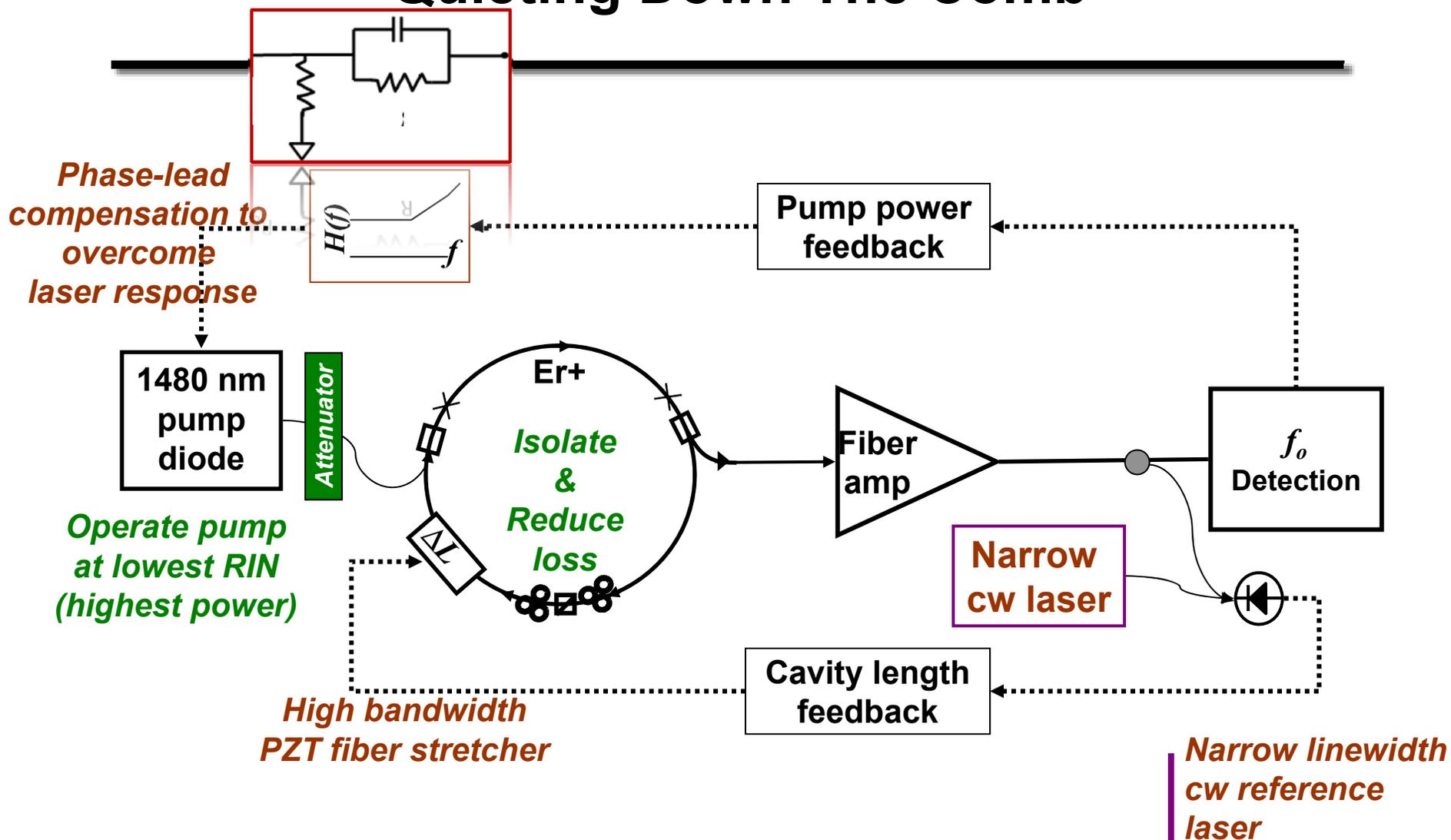


ASE-induced  
Quantum Noise  
PSD  $\sim$  white noise

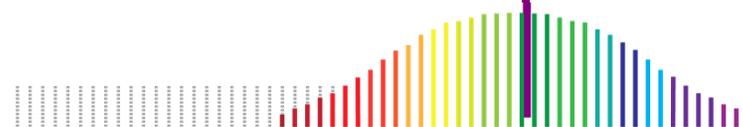


“Extra-cavity noise”  
(ASE, shot noise)

# Quieting Down The Comb

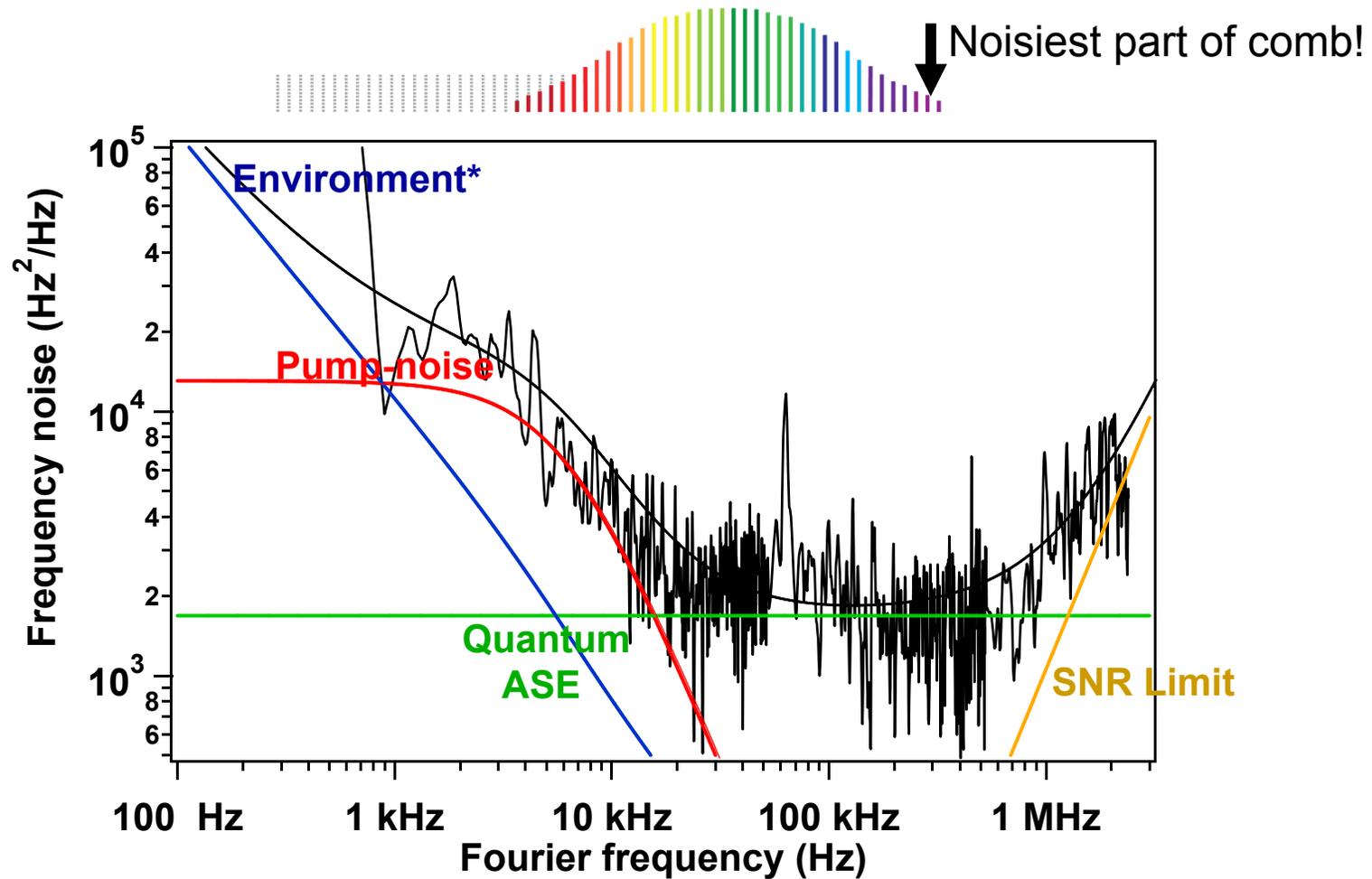


McFerran et al, Opt. Lett., 31, 1997 (2006)  
 N. R. Newbury and B. Washburn, IEEE JQE, 41, 1388 (2005)  
 Swann et al., Opt. Lett. **31**, 3046 (2006).



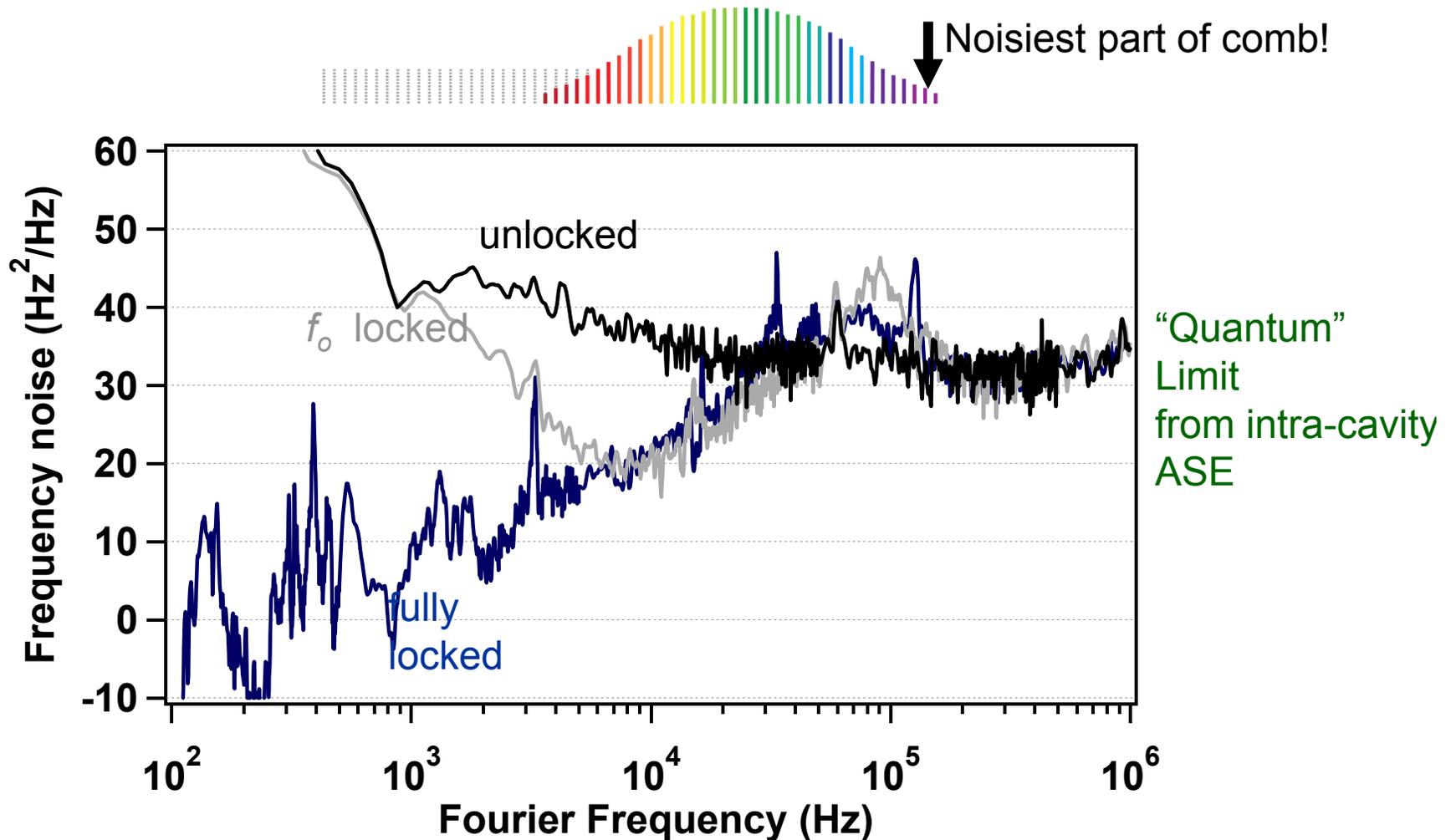
# Free-running Frequency Noise at 1 $\mu\text{m}$ (far edge of comb)

NIST



(Corresponding Linewidth is  $\sim 10$ 's of kHz)

# Phase-Locked Frequency Noise at 1 $\mu\text{m}$ <sup>NIST</sup> (far edge of comb)

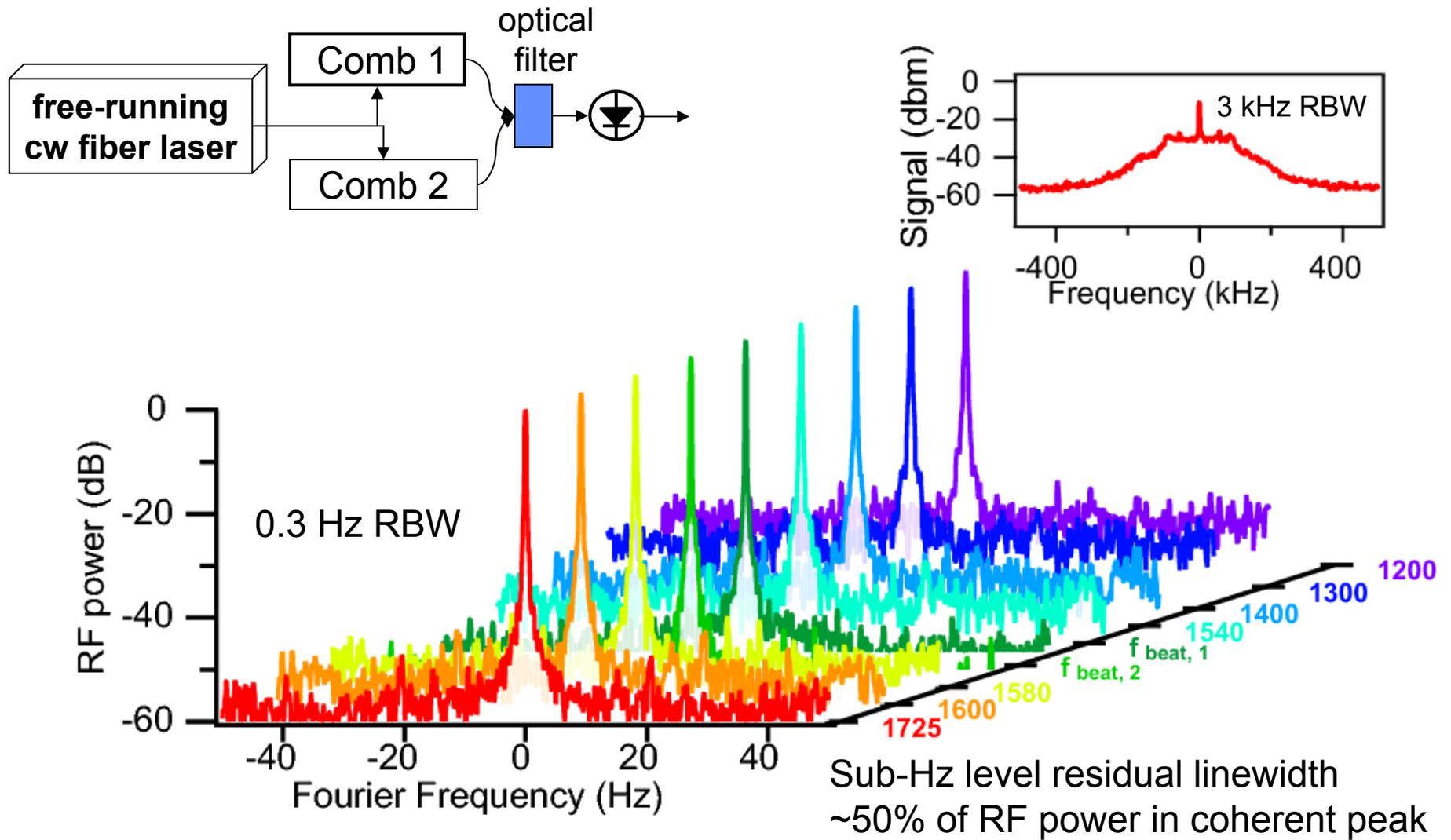


*Unlocked phase noise  $\sim 200$  radians*  
*Locked phase noise  $\sim 0.6$  radians*

# Optical Coherence Between Combs with IMRA America

NIST

Swann, I Hartl, M. Fermann, Opt. Lett. **31**, 3046 (2006).

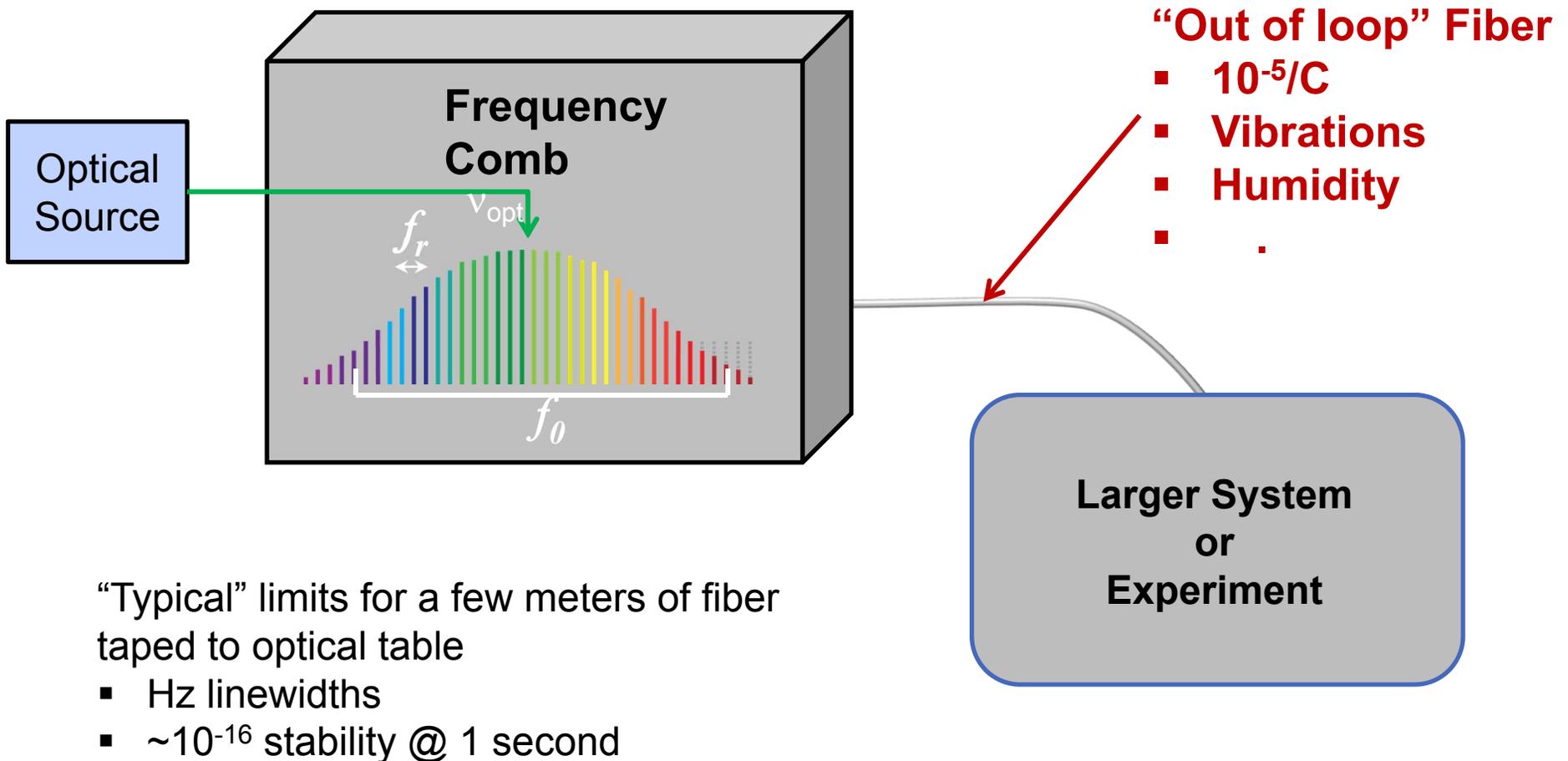


## Prescription for using a stabilized Frequency Comb

1. Measure the offset frequency
  - Hard to do - requires octave spanning continuum
2. Detect either an optical beat or high harmonic of the repetition rate (optical vs rf stabilization)
3. Understand and minimize noise
  - Check fixed point of pump power modulation if low dispersion cavity!
4. “Feedback” to actively cancel leftover noise
  - High bandwidth feedback
  - Two or more actuators (or signal processing on comb)
5. Design the rest of the experiment to not re-introduce noise we just cancelled
  - Minimize out-of-loop paths.

# Limits to Comb Performance

For frequency stability or linewidth:  
Limit is set by “out of loop fiber/free-space” and not comb



## A Few General Rules of Thumb for Frequency combs

- Comb has no intrinsic accuracy -> needs an external reference
- “Flat” supercontinuum not achievable
  - Challenge for spectroscopy
  - Sometimes solved with multiple supercontinuum branches
- Hard to detect offset frequency ( $f_{\text{ceo}}$ ) with enough SNR!
  - $f$ - $2f$  requires octave spanning continuum
  - $2f$ - $3f$  requires less bandwidths but more power
- The “Fixed Point” picture is the best way to analyze the noise and the stabilization....
- Coherent narrow linewidth comb requires careful design & high bandwidth feedback.
- Frequency stability (Allan deviation) depends on more experiment than the comb
  - “Out-of-Loop” paths almost always dominate frequency stability