

# Shaping FEL radiation: from multipulse/multicolor emission to generation of twisted light

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# SOME OF THE PROPERTIES USERS EXPECT FROM A LIGHT SOURCE

- High peak **brilliance** and full **tunability** in the spectral region of interest
- Possibility of controlling **pulse duration**
- Full transverse and longitudinal **coherence** (diffraction imaging, coherent control)
- Variable **polarization** (circular dichroism, surface science)
- **Ultimate feature:** the ability to arbitrarily **shape** the radiation pulse in the temporal and spatial (longitudinal and transverse) domains

## YOU CAN'T ALWAYS GET WHAT YOU WANT?

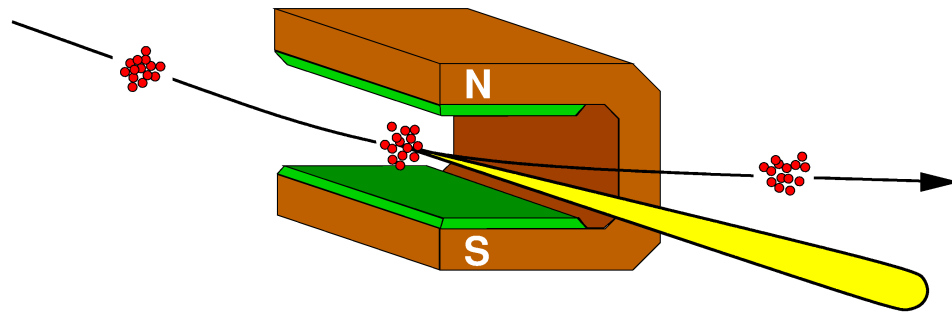
- In the IR to UV spectral region, the **majority** of previously mentioned requirements are met by conventional table-top lasers.
- In the VUV to X-ray spectral domain, different approaches must be used in order to achieve laser-like properties of light. Seeded FELs are currently the most promising candidates for reaching this goal.

# OUTLINE

- quick recap of bending magnet and undulator radiation
- basic principles of FEL operation
- self-amplified spontaneous emission (SASE) vs. seeded FELs
- advanced FEL concepts: longitudinal (temporal) and transverse (spatial) shaping of FEL pulses



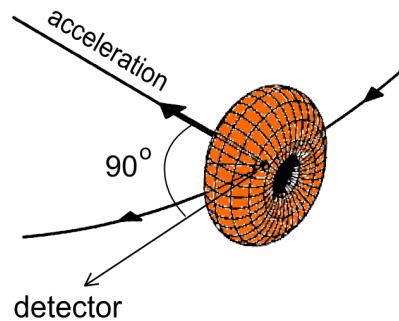
# BENDING MAGNET RADIATION



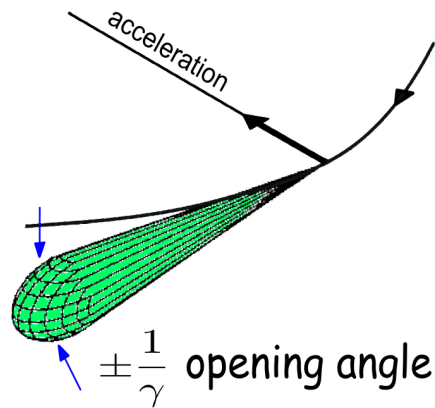
Lorentz-Transformation

Moving frame  
of electron

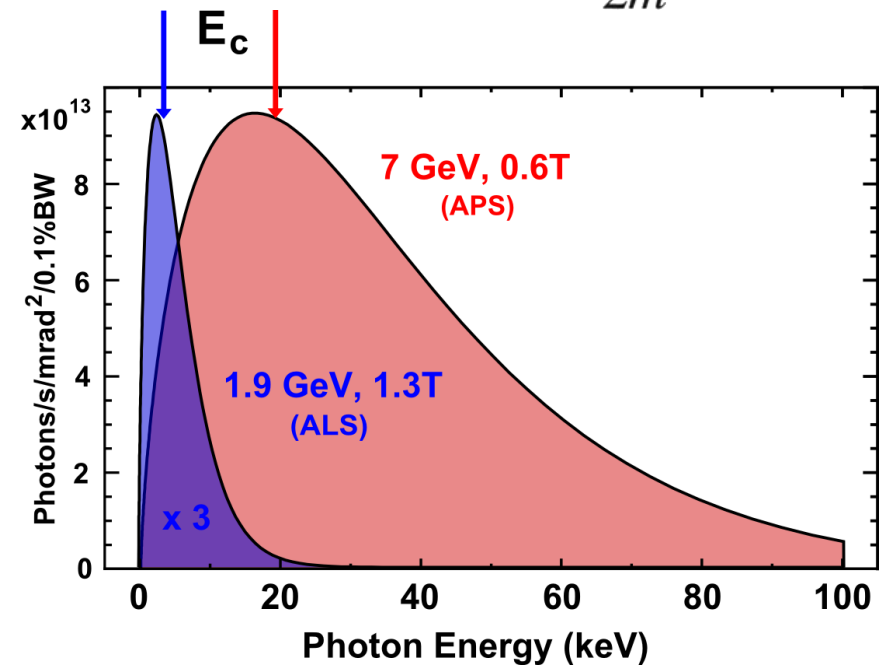
Lab frame



$$\frac{1}{\gamma} = \frac{m_0 c^2}{E} = \sqrt{1 - \left(\frac{v}{c}\right)^2}$$



$$E_c = \hbar \omega_c = \frac{3e \hbar B \gamma^2}{2m}$$



# UNDULATOR RADIATION

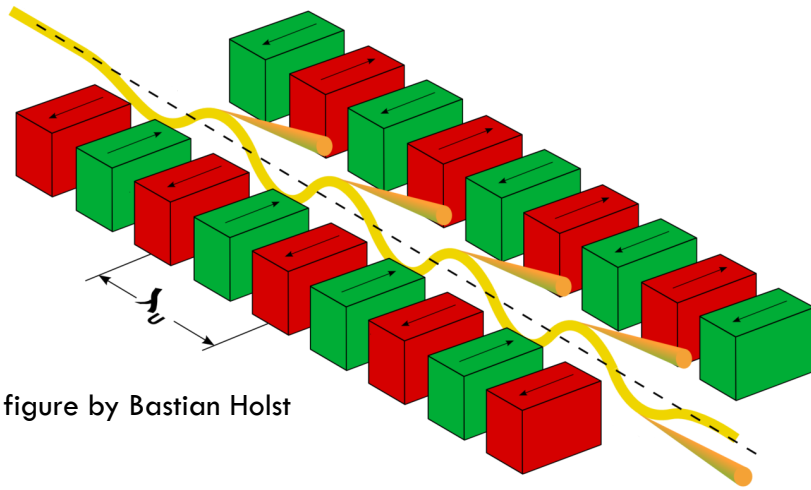
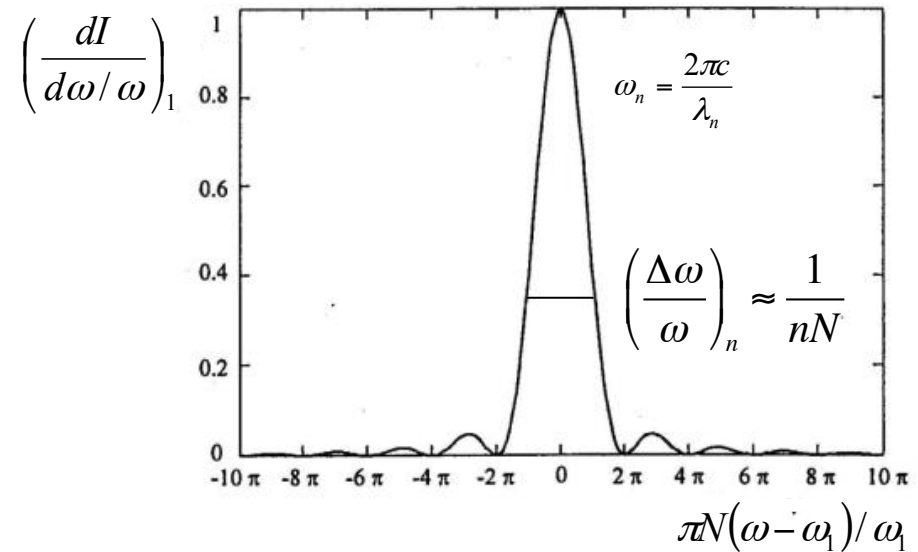


figure by Bastian Holst



$N$  = number of undulator periods

Resonant wavelength:

$$\lambda_n = \frac{\lambda_u}{2n\gamma^2} \left( 1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right),$$

(only odd harmonics on-axis,  
i.e.,  $\theta = 0$ )

$\lambda_u$  = undulator period

$\gamma$  = electron energy

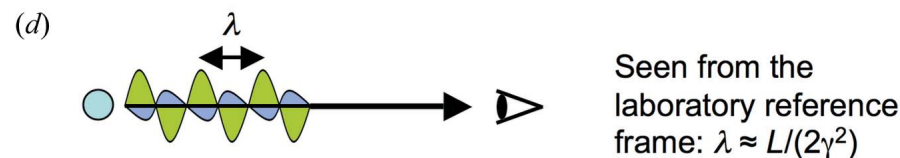
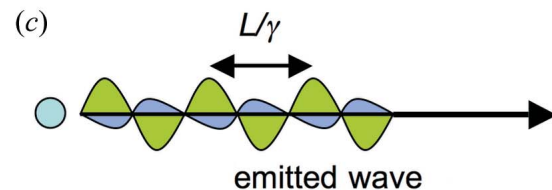
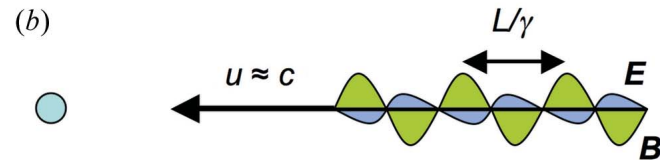
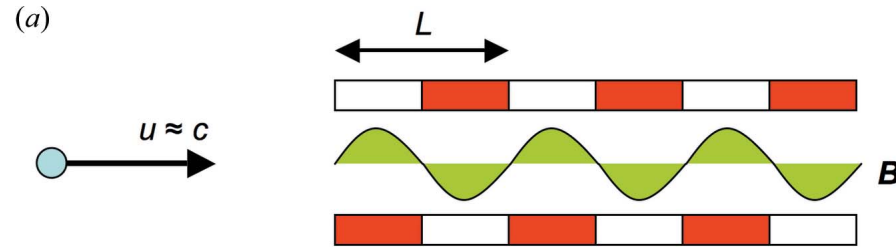
$K \propto \lambda_u B_0$  = undulator parameter

$B_0$  = peak undulator field

$n$  = harmonic number

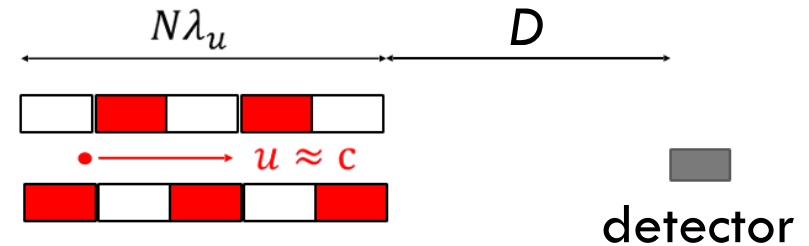
# UNDULATOR RADIATION „EXPLAINED“

Resonant wavelength:



$$\lambda = \frac{L}{2\gamma^2} \left( 1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

Pulse properties:



Frist photons detected at  $t_1 = \frac{N\lambda_u + D}{c}$

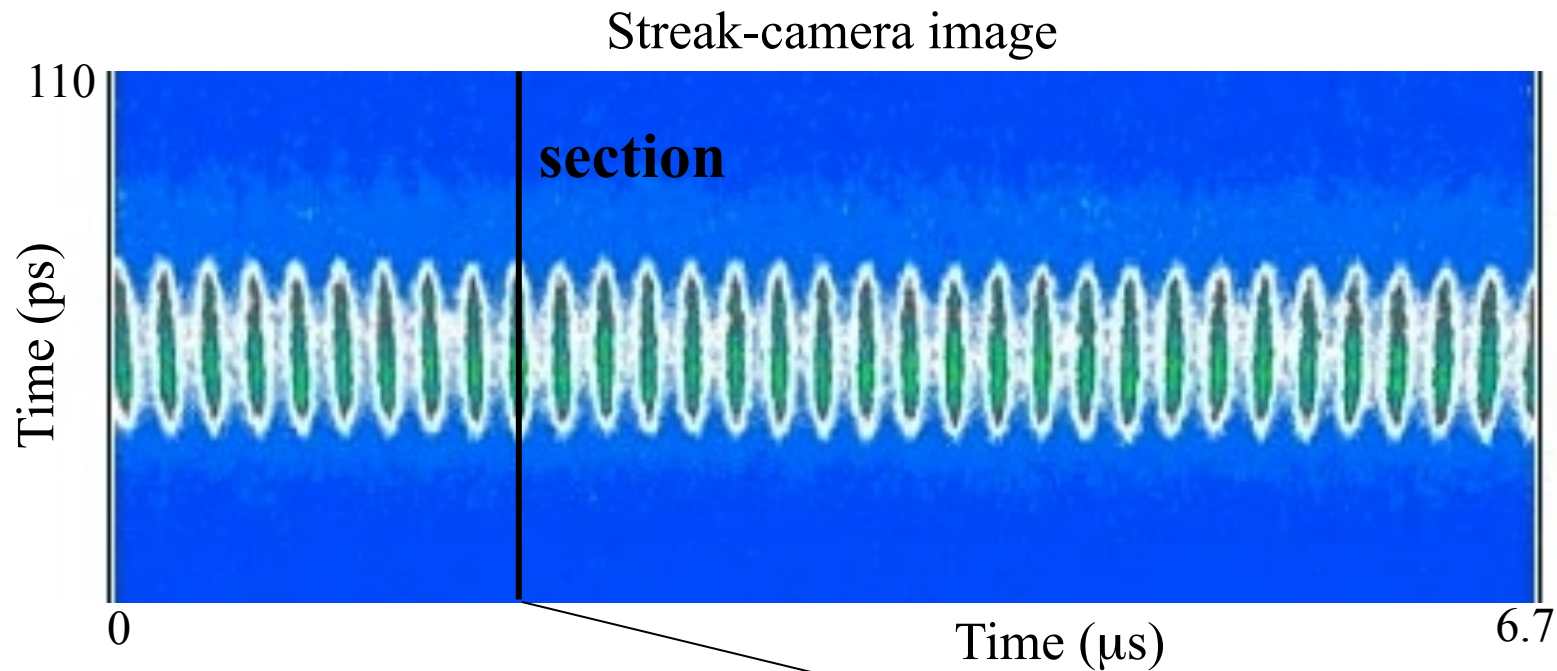
Detection ends at  $t_2 = \frac{N\lambda_u}{u} + \frac{D}{c}$

Pulse duration =  $t_2 - t_1 \approx \frac{N\lambda_u}{2c\gamma^2} \approx \frac{N\lambda}{c}$

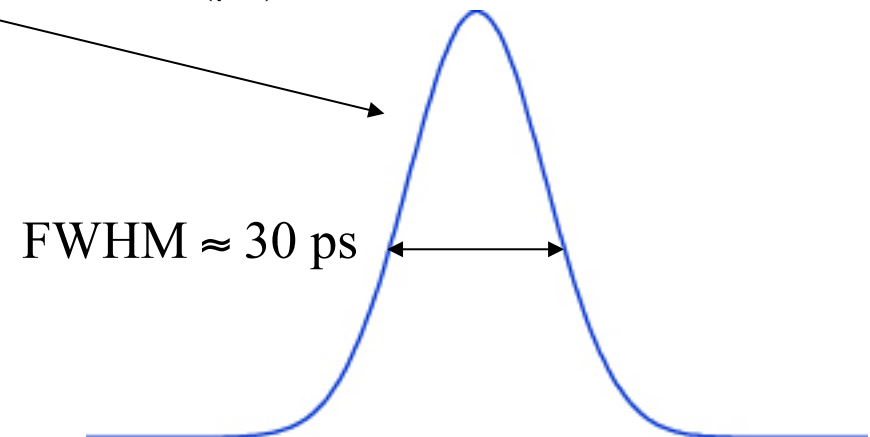
Characteristic frequency  $\propto 1/\Delta t \propto \frac{c}{N\lambda}$

Bandwidth  $\frac{\Delta\omega}{\omega} \propto \frac{1}{N}$

# TIME STRUCTURE OF SYNCHROTRON RADIATION

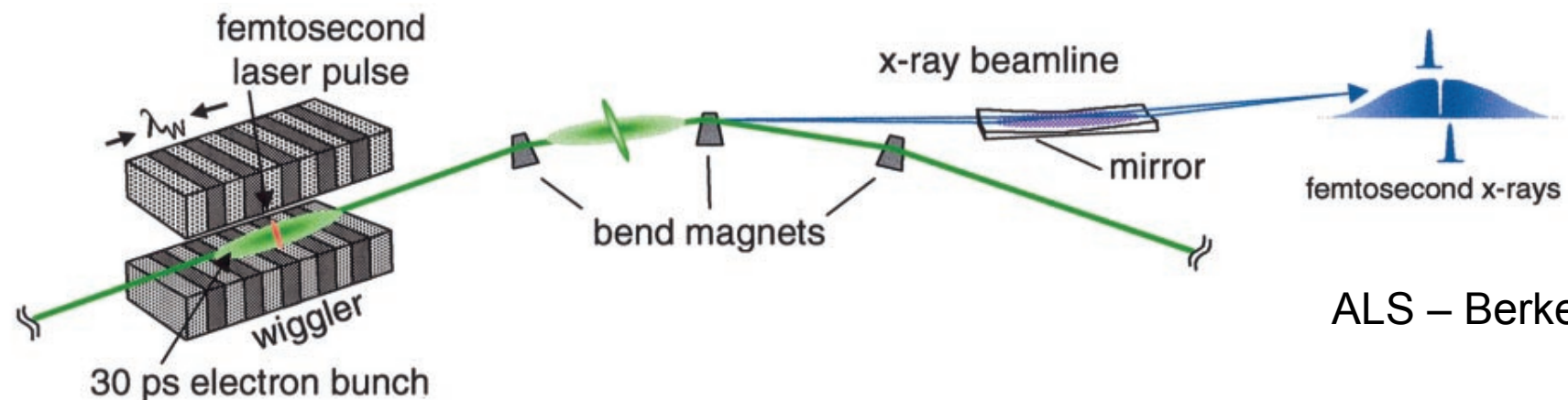


Time structure of synchrotron radiation is a replica of that of the electron bunch, and is invariant over the entire spectrum.



# DECREASING THE PULSE DURATION

A femtosecond laser is used to imprint **an energy modulation** onto a long electron bunch (femtosing).



Drawback: strong reduction of photon flux (by a factor of 1000).

*R. W. Schoenlien et al., Science, 2000*

# SYNCHROTRON RADIATION: TYPICAL PERFORMANCE

**Tunability:** Full (between IR and X-rays)

**Shot-to-shot reproducibility:** Very good

**Polarization:** Fully adjustable

**Repetition rate:** hundreds of MHz

**Peak brilliance:**  $\approx 10^{21}$  ph/s/0.1%BW/mm<sup>2</sup>/mrad<sup>2</sup> (at 10 keV)

**Pulse duration:** tens of picoseconds

**Natural spectral resolution:**  $\approx$  few percent

**Coherence:** good transverse, poor longitudinal

# INCREASING THE BRILLIANCE

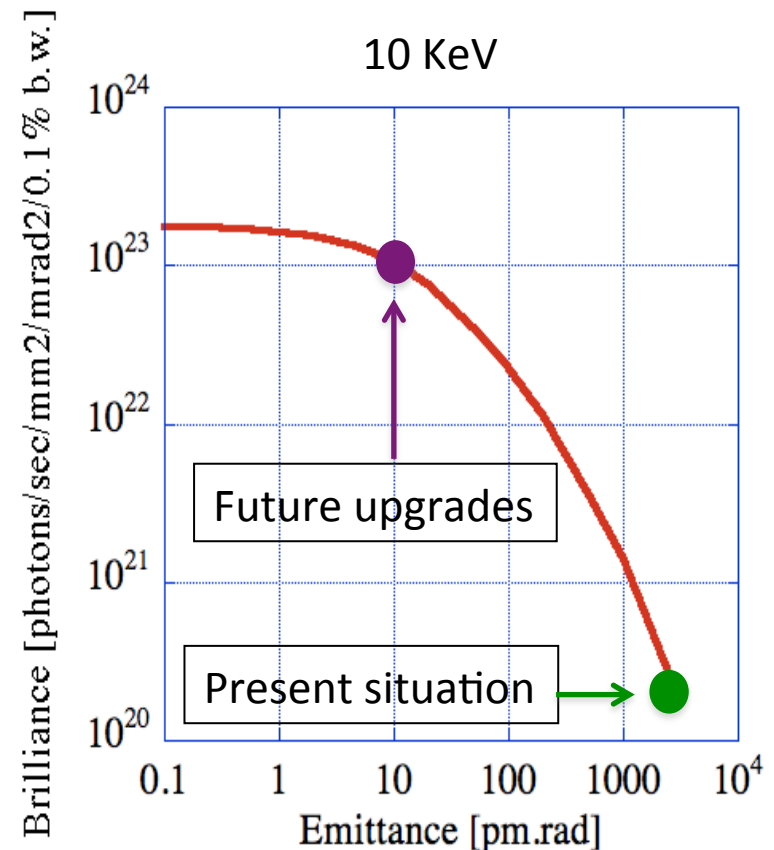
$$\text{brilliance (or brightness)} \propto \frac{\text{photon flux}}{\text{unit area} \times \text{unit solid angle}}$$

Limited by *wake field instabilities*

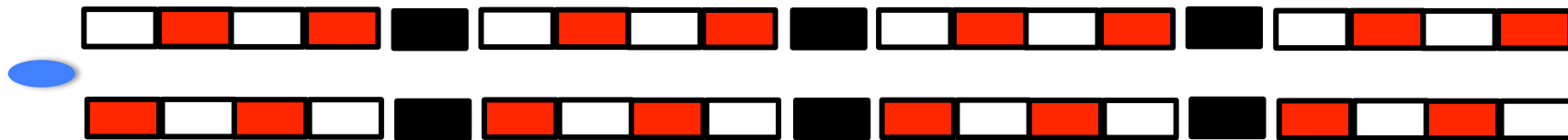
$$\text{brilliance} \propto \frac{I_{\text{beam}}}{\epsilon_x \epsilon_y}$$

Limited by diffraction

*Low Emittance Rings Workshop, Crete, 2011*



## INCREASING THE BRILLIANCE, TRY NO. 2

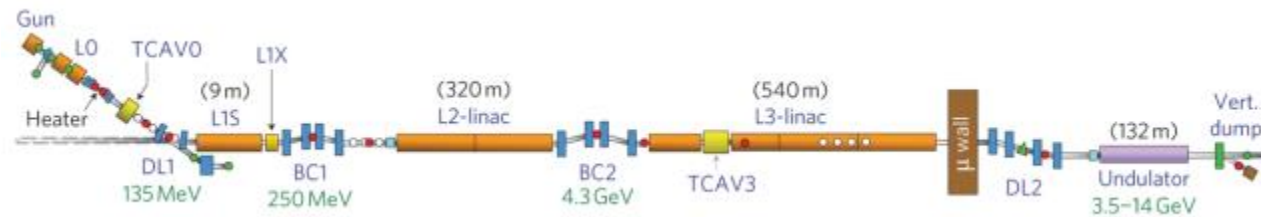


Is this a brute force approach? Yes and no...

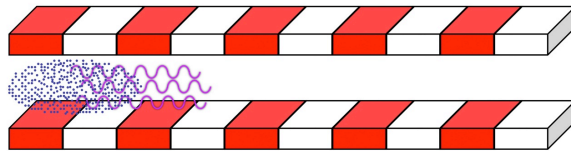


# WHAT IS A FEL ?

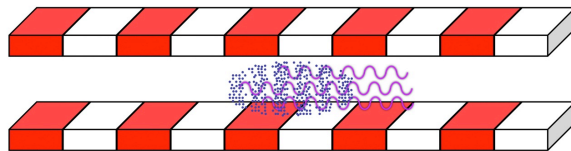
- electrons are accelerated in a high-energy linear accelerator to a speed close to  $c$  (speed of light)



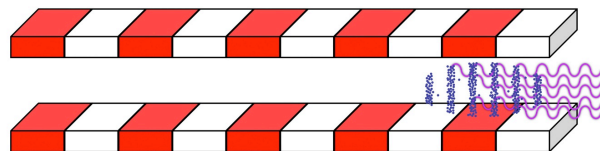
P. Emma *et al.*, *Nat. Photonics* (2010) **4**, 641



- electron bunch enters the undulator  
→ (uncorrelated) emission of radiation by individual electrons

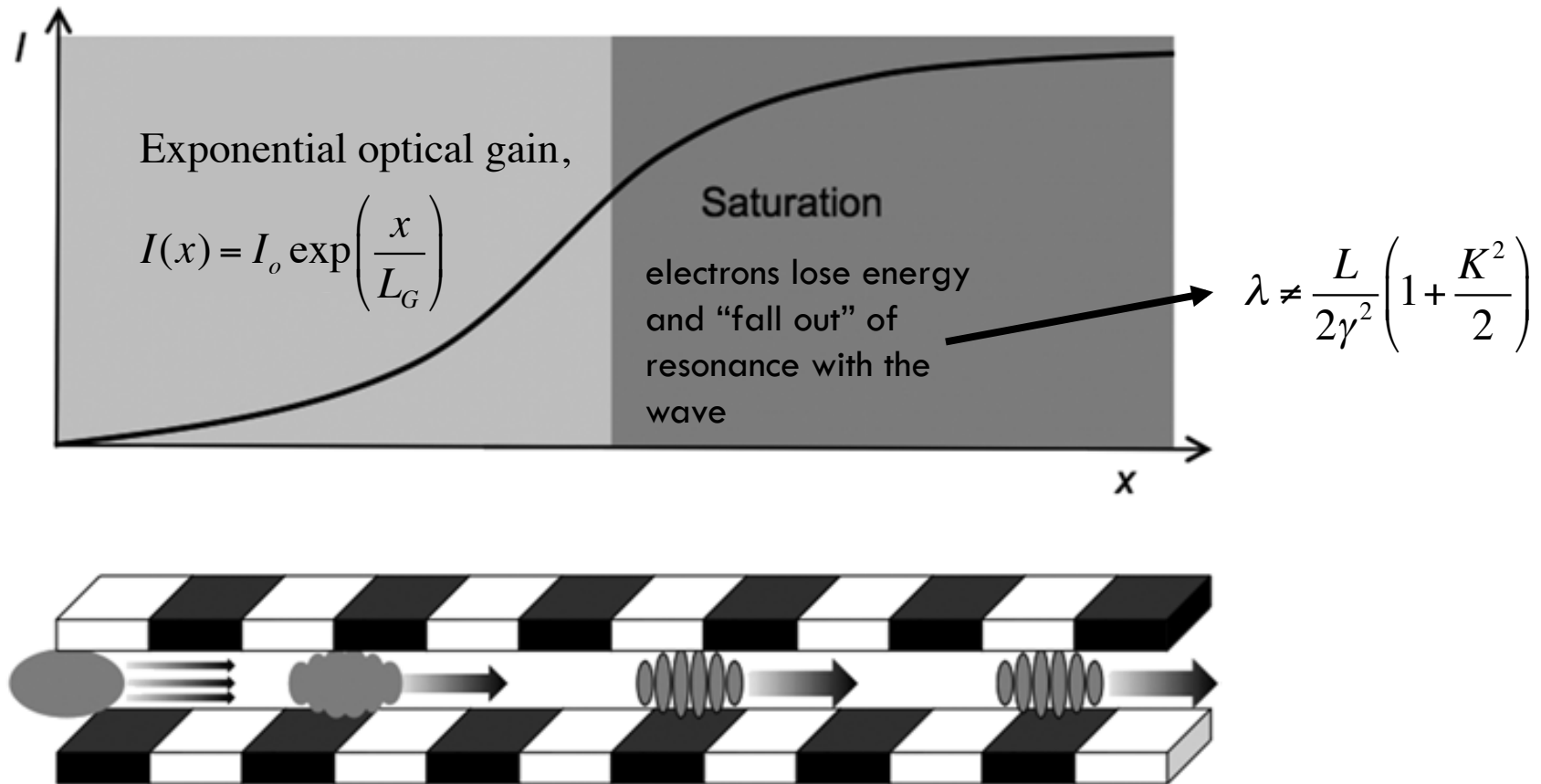


- interaction of electrons with previously emitted waves leads to microbunching  
→ partly correlated emission



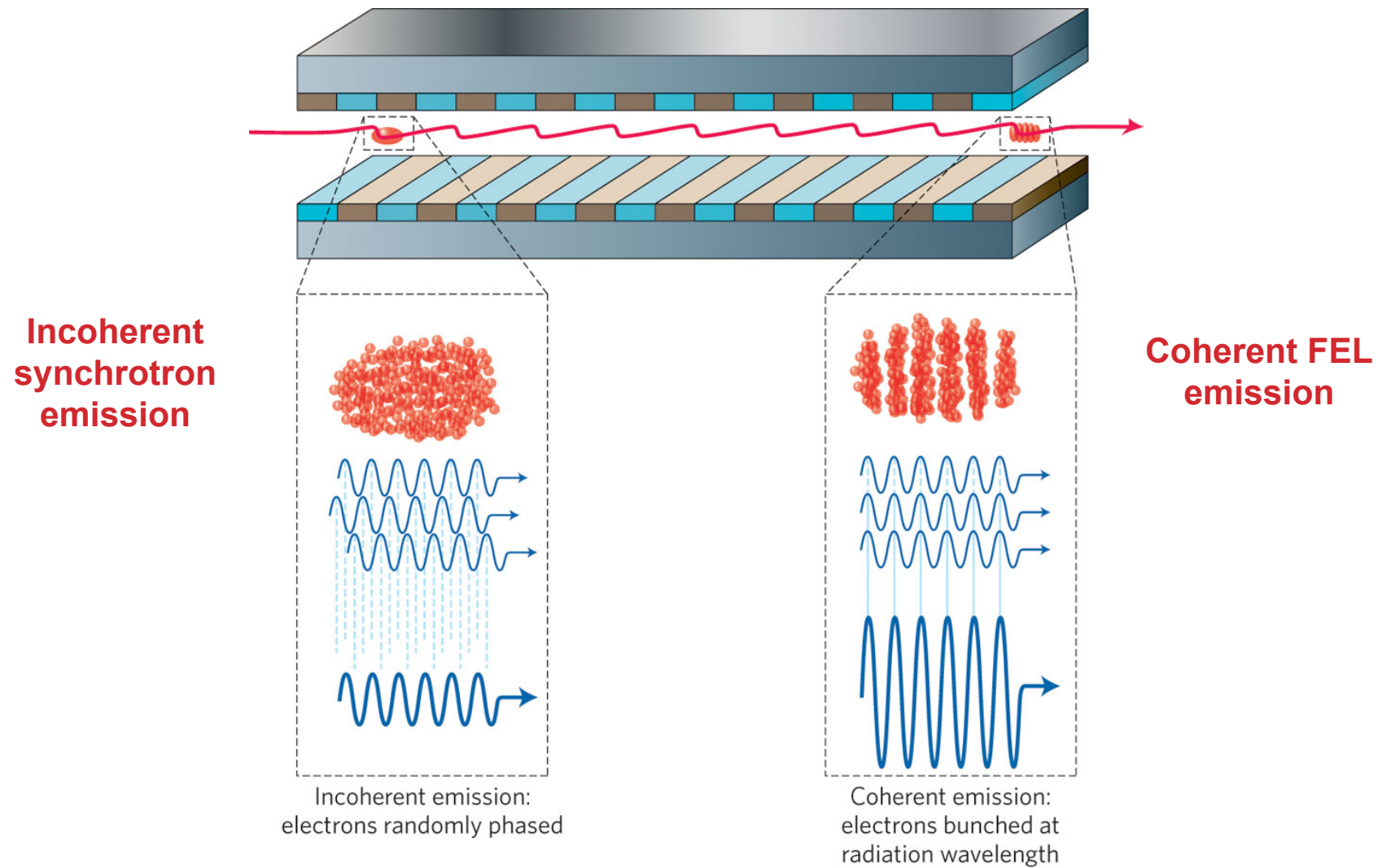
- complete microbunching → the emission is fully correlated

# FEL GAIN



The electron beam and the emitted electromagnetic wave co-propagate in a long undulator. Electrons couple with spontaneous emission, resulting in exponential amplification (gain) of the intensity until saturation is reached.

# A QUESTION OF COHERENCE



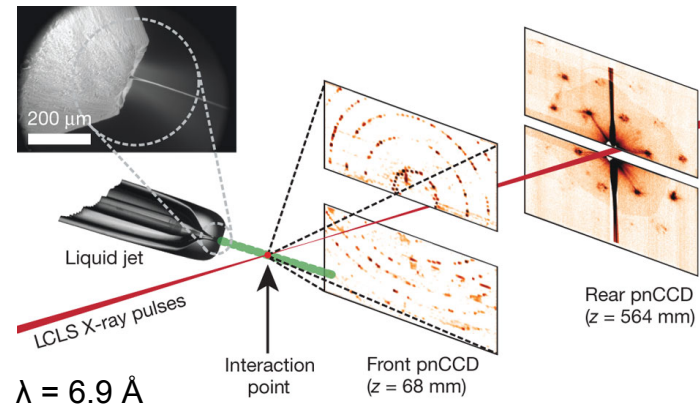
$$\text{brilliance} \propto I_{\text{beam}}$$

$$\text{brilliance} \propto I_{\text{beam}}^2$$

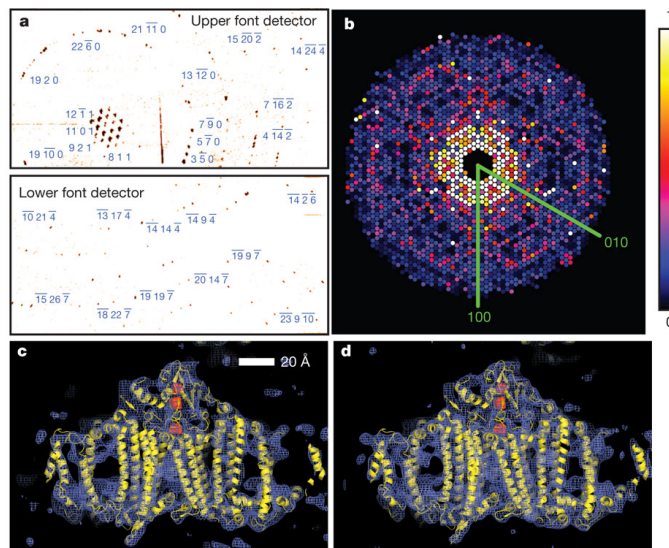
B.W.J. McNeil, N. R. Thompson, *Nature Photonics*, 2010

# WHY MORE BRILLIANCE? AREN'T SYNCHROTRONS POWERFUL ENOUGH?

## protein nanocrystallography



## measurements on photosystem I

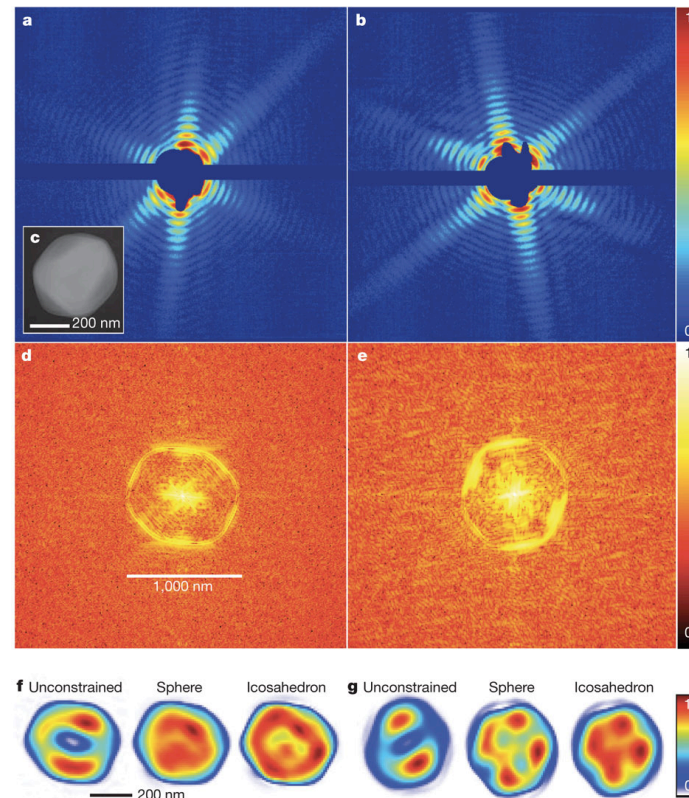


H. N. Chapman *et al.*, *Nature*, 2011

## coherent X-ray diffraction imaging (CXDI)

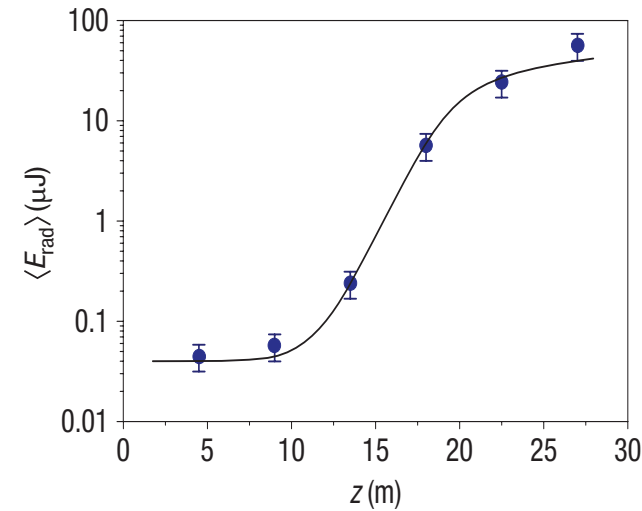
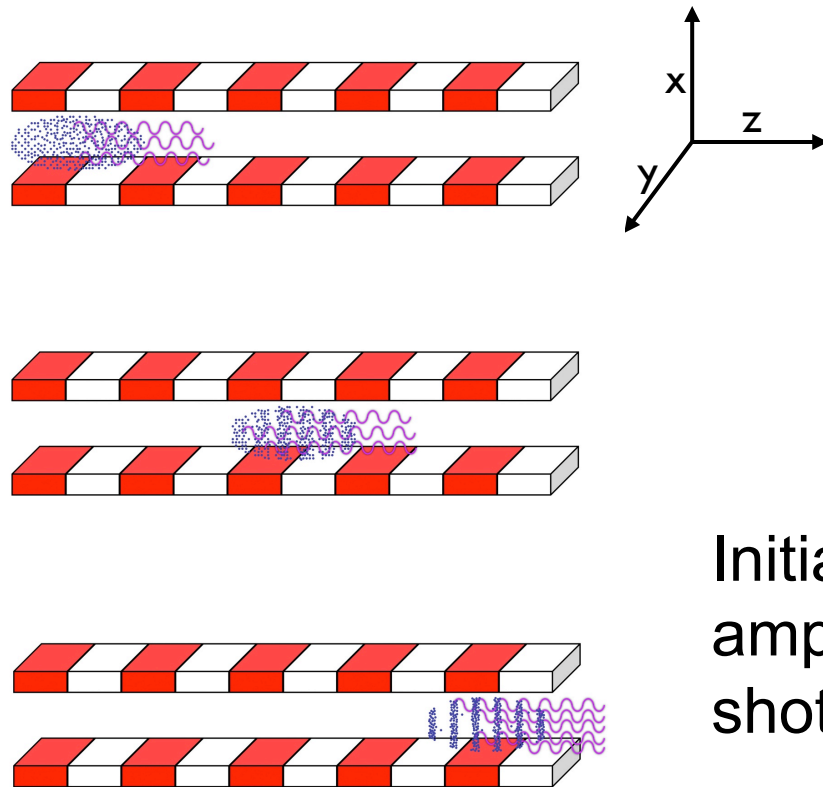
non-periodic objects  $\rightarrow$  continuous diffraction pattern  $\rightarrow$  oversampling  $\rightarrow$  phase retrieval  $\rightarrow$  image reconstruction

## CXDI of single mimivirus particles



M. M. Seibert *et al.*, *Nature*, 2011

# SELF-AMPLIFIED SPONTANEOUS EMISSION (SASE) FEL

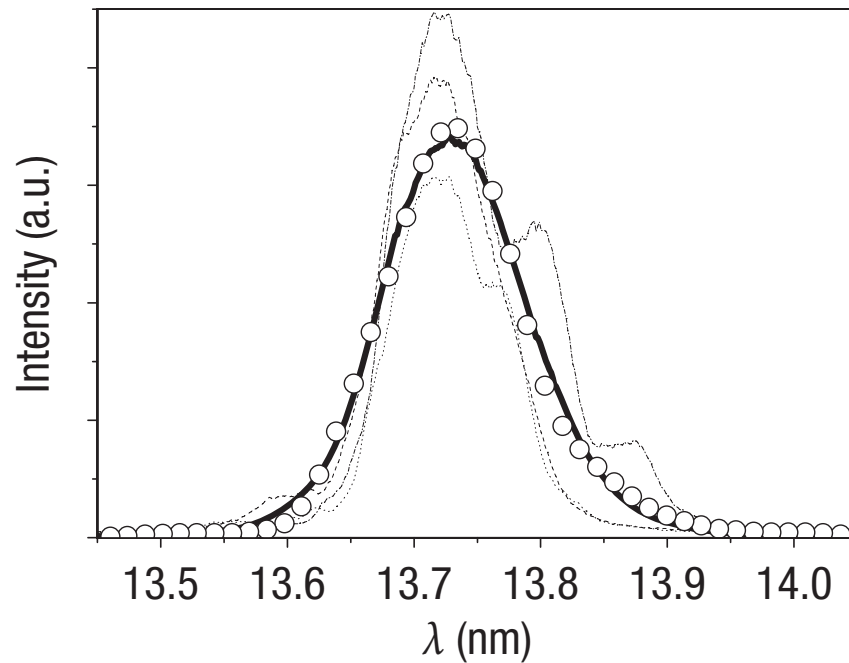


Initial emission that is being amplified originates from electron shot-noise:

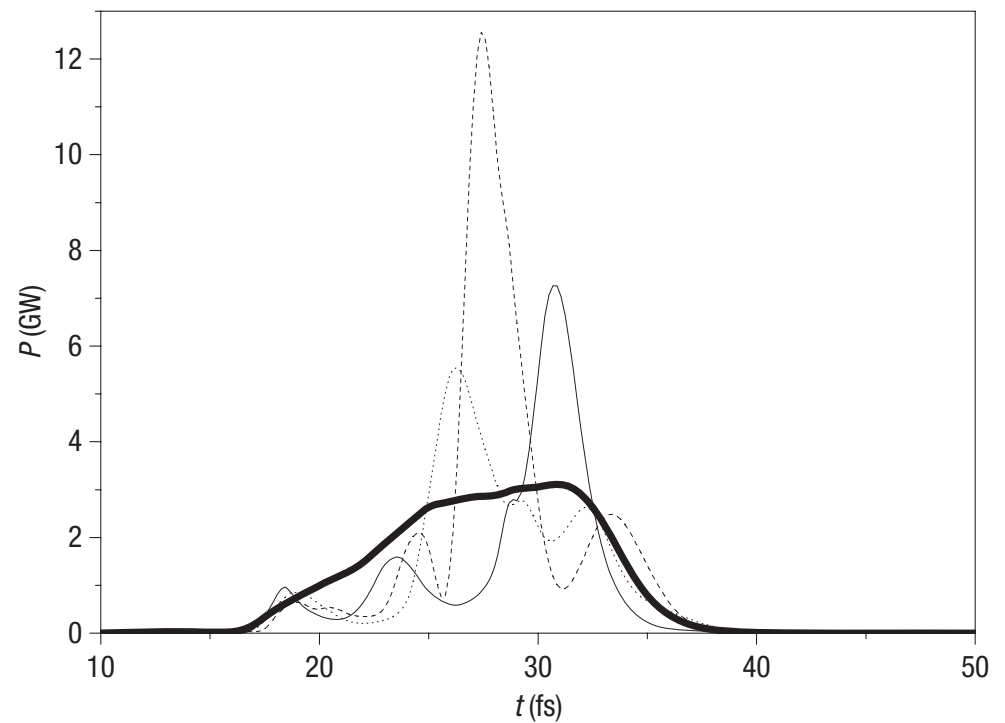
$$j_e = eK \cos\left(\frac{2\pi}{L} z\right) \sum_{j=1}^N \frac{1}{\gamma_j} \delta[\bar{x} - \bar{x}_j(z)] \delta[t - t_j(z)]$$

# SASE SPECTRAL AND TEMPORAL CHARACTERISTICS (FLASH)

Spectral profile



Temporal profile (simulation)

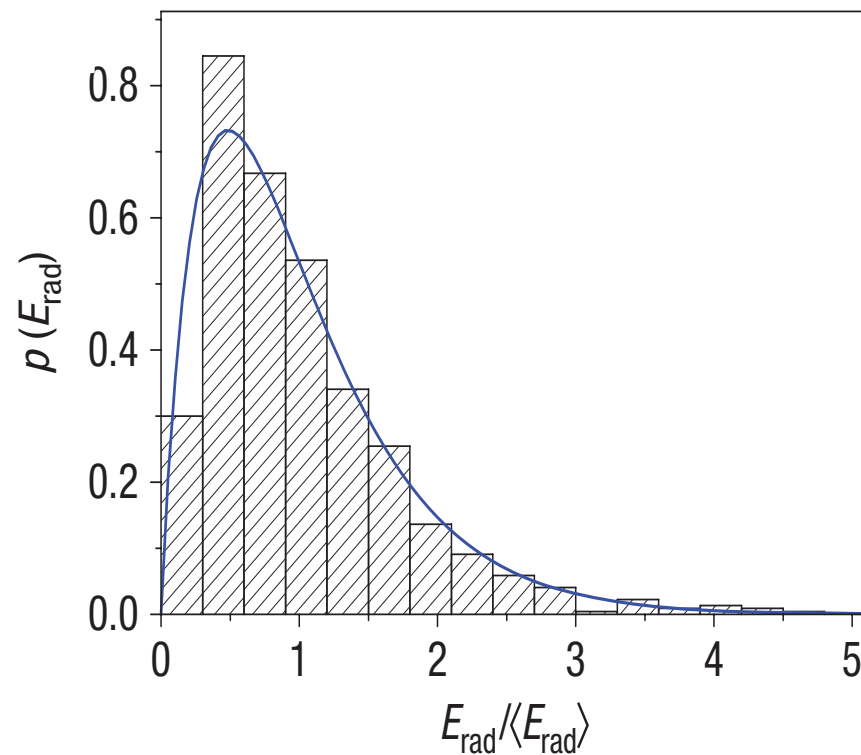


W. Ackermann *et al.*, *Nature*, 2007

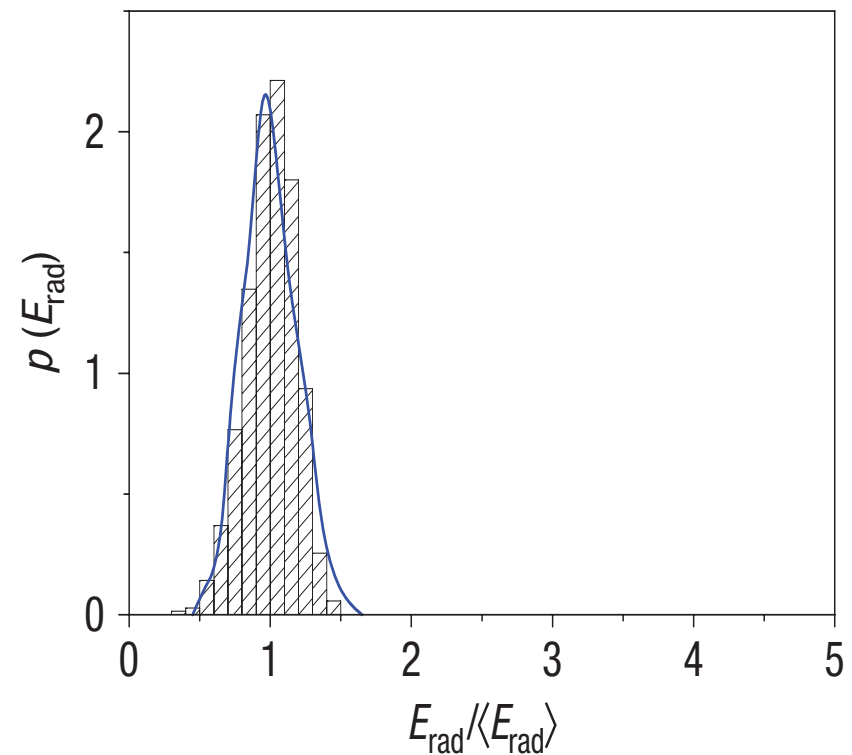
# SASE PULSE ENERGY STABILITY (FLASH)

Probability distribution for the energy of FLASH radiation pulses

End of exponential growth

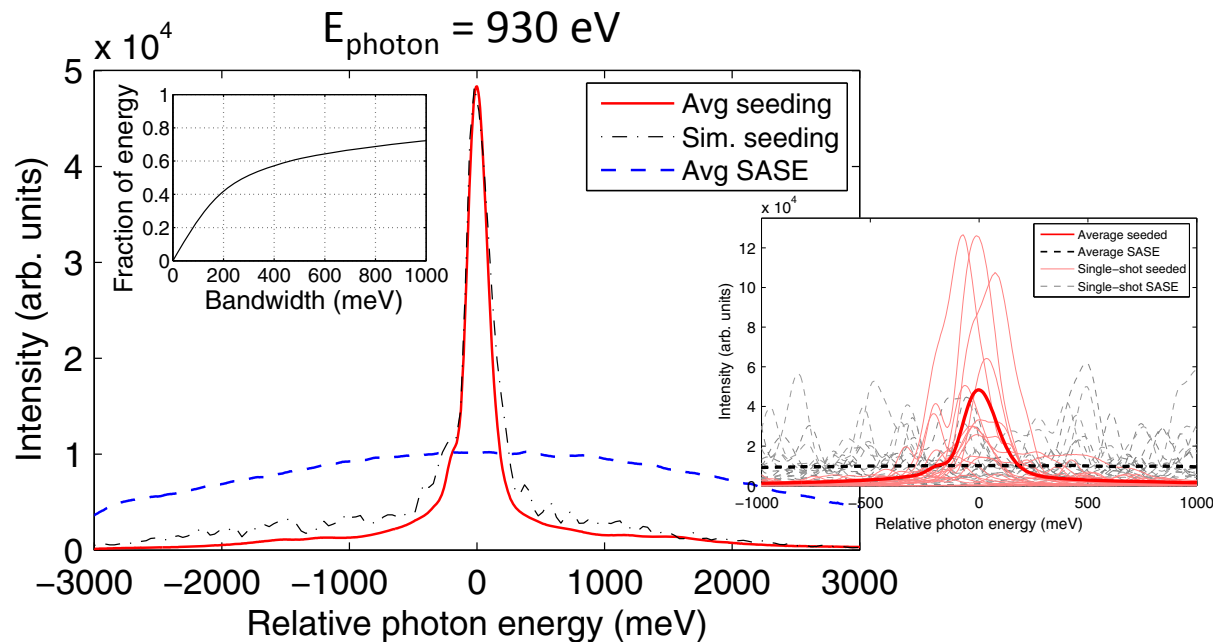
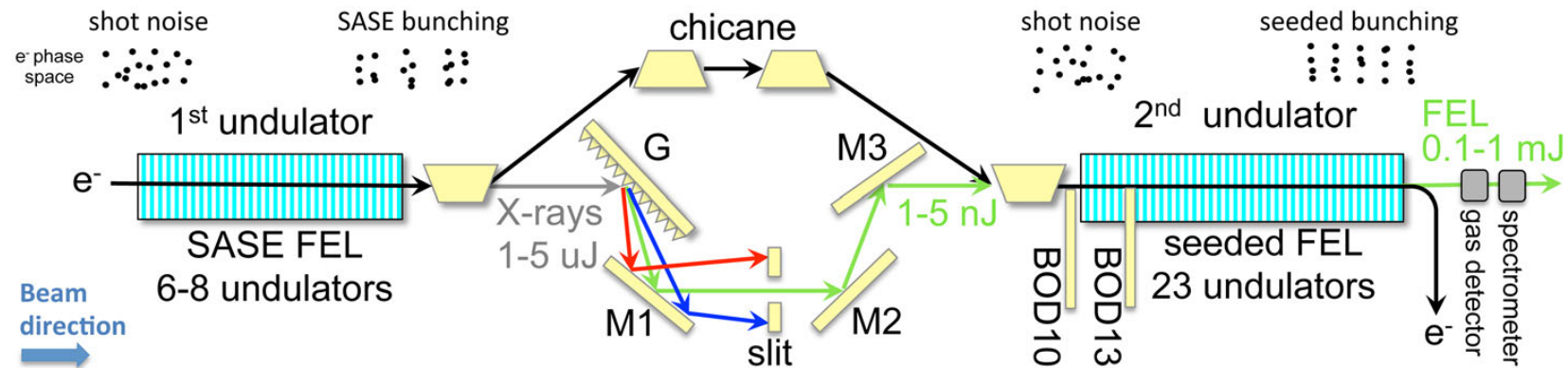


Saturation





# OVERCOMING SASE LIMITS 1 – SELF SEEDING

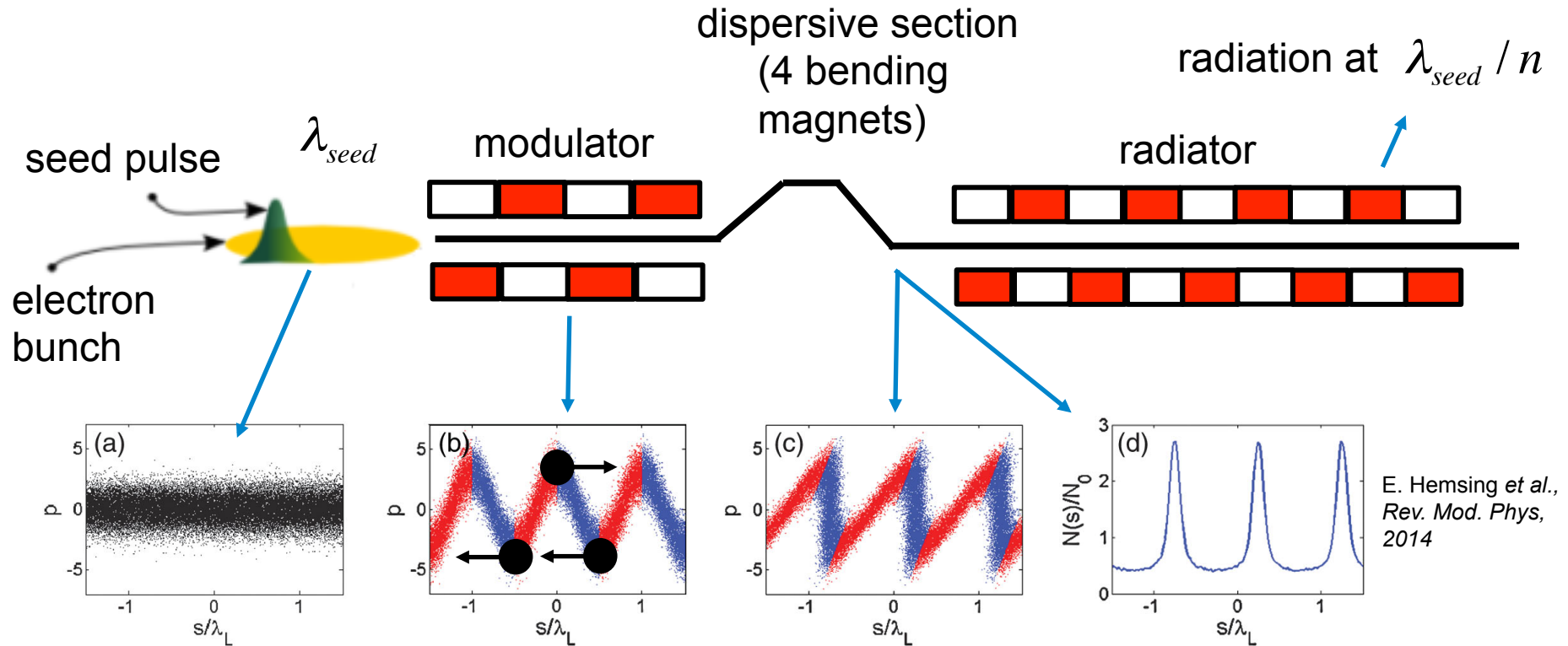


- improved central wavelength stability
- narrower bandwidth (increased brightness)
- limited ability to shape the radiation pulse

D. Ratner *et al.*, PRL, 2015



# OVERCOMING SASE LIMITS 2 – SEEDING BY AN EXTERNAL COHERENT SIGNAL (HIGH GAIN HARMONIC GENERATION - HHG)



$$b_n \sim \exp[-n^2 B^2 / 2] J_n[-nAB]$$

$$\text{max : } AB \approx 1 \Rightarrow b_n \sim \exp[-n^2 / 2A^2]$$

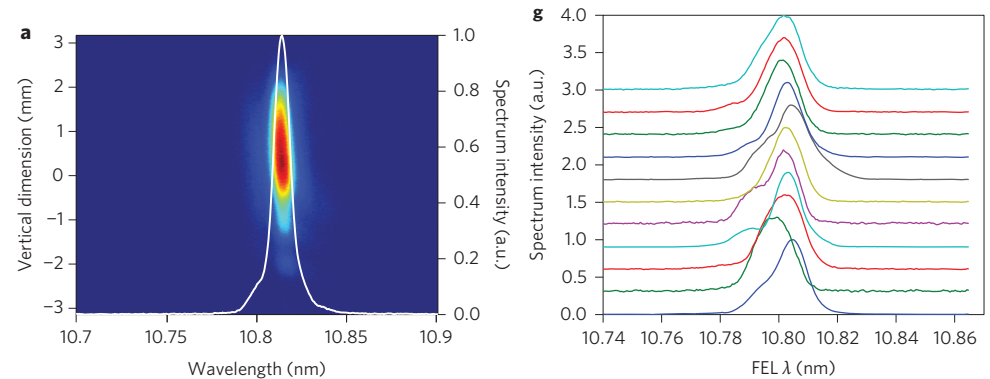
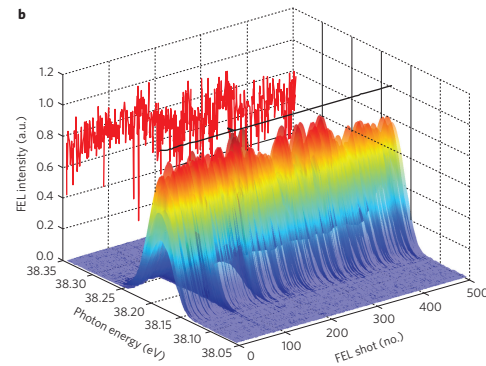
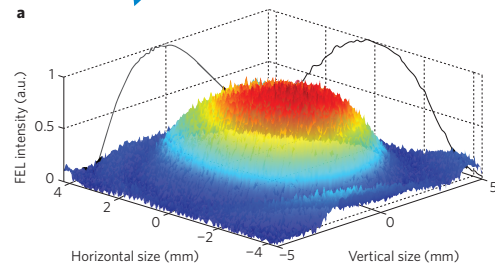
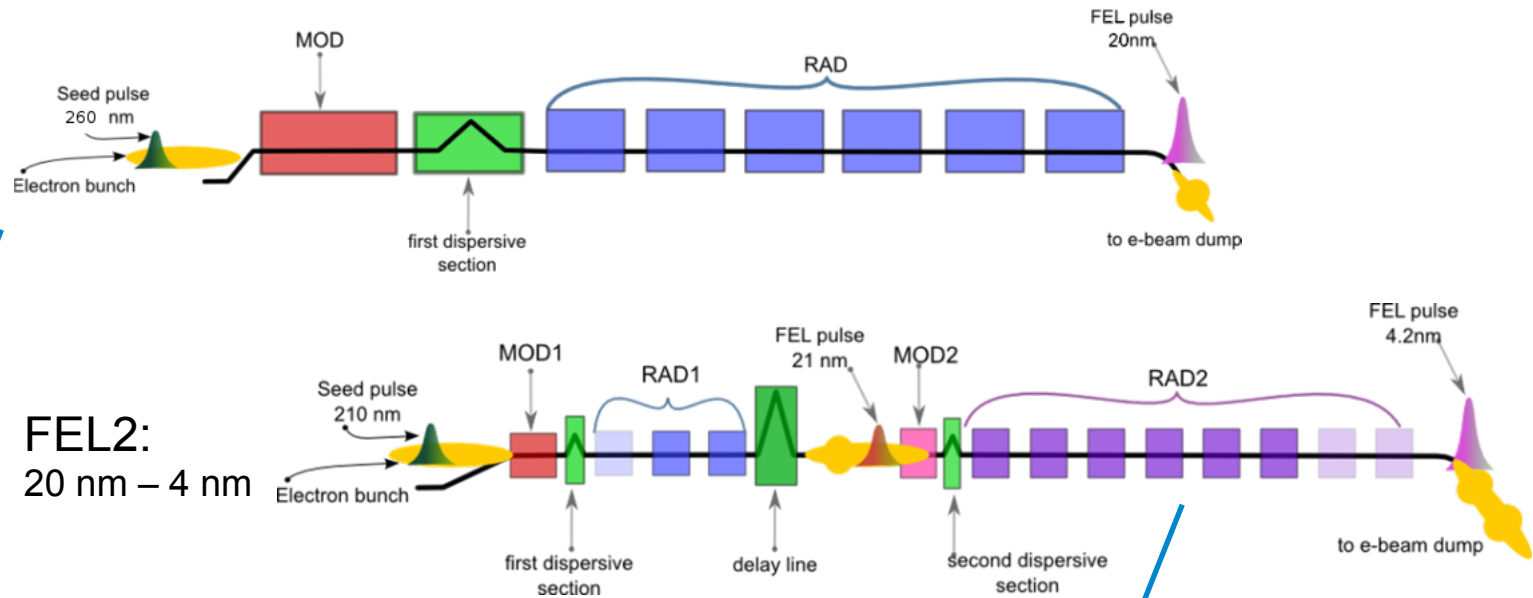
A = energy modulation normalized to the initial energy spread

B = (dimensionless) dispersive strength

FEL radiation properties are governed by the seed laser => PULSE SHAPING!

# FERMI SEEDED FEL

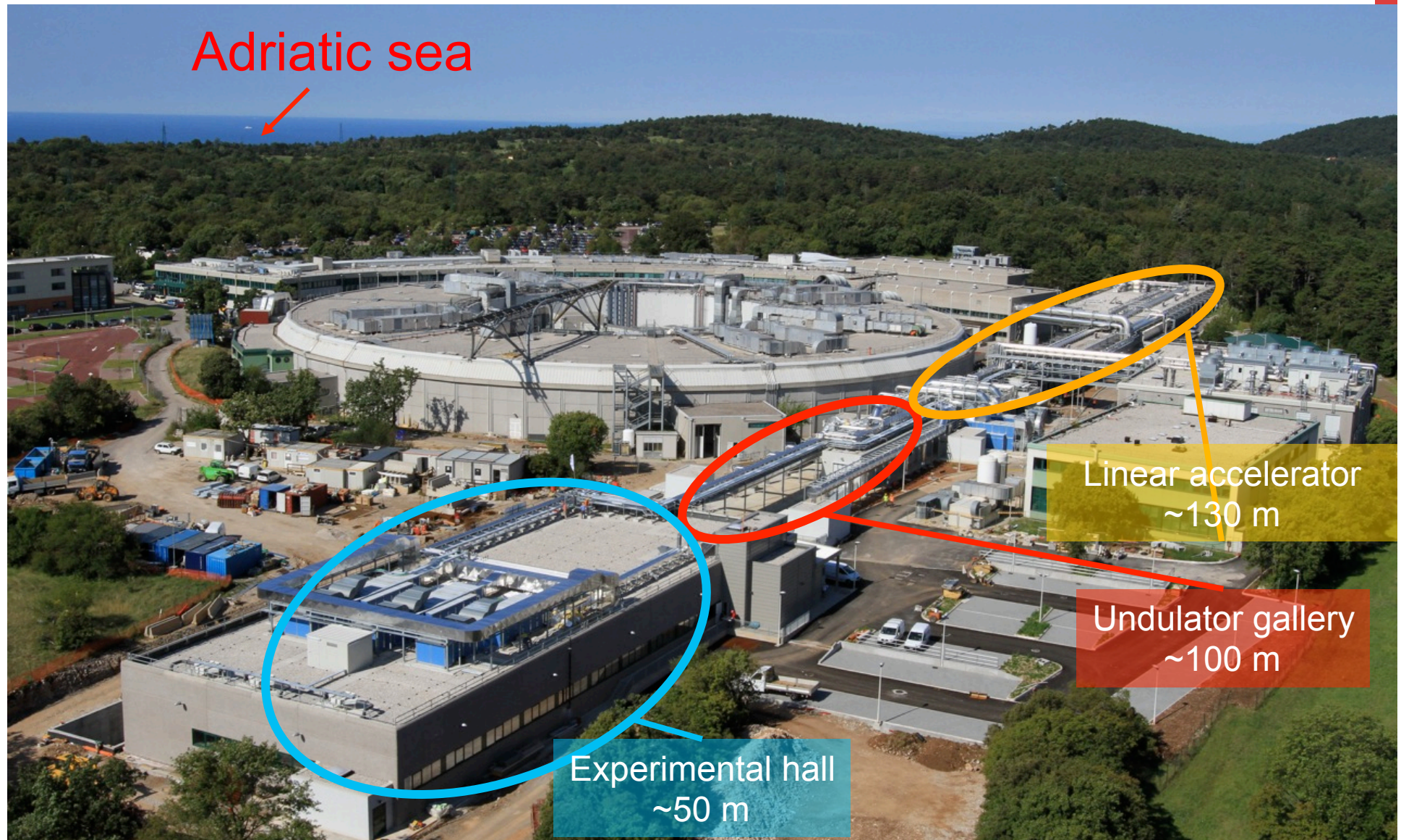
FEL1:  
100 nm – 20 nm



Allaria *et al.*, *Nature Photonics*, 2012 and 2013



# FERMI SEEDED FEL



SHAPING FEL LIGHT:  
TWO COLOR FEL SCHEMES  
(FOR X-RAY PUMP-X-RAY PROBE  
EXPERIMENTS)

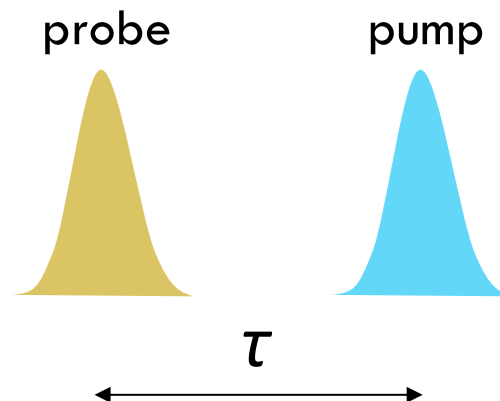


# TWO COLOR FEL SCHEMES

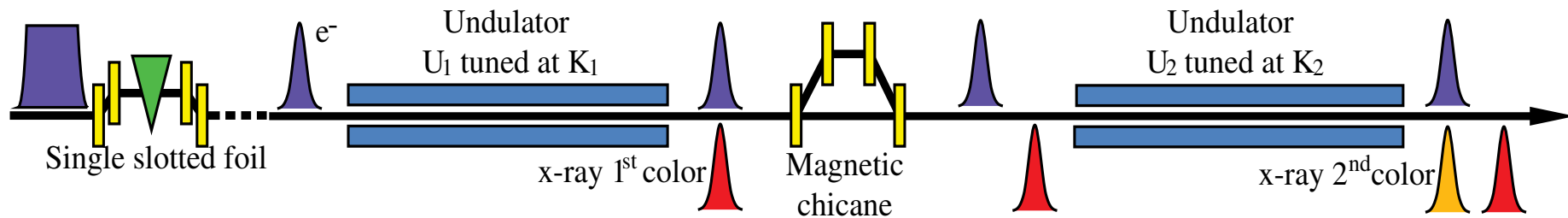
How can we generate two FEL pulses with different wavelengths?

$$\lambda = \lambda_u \frac{1 + K^2}{2\gamma^2} \begin{cases} \nearrow \lambda_{1,2} = \lambda_u \frac{1 + K_{1,2}^2}{2\gamma^2} & \text{split undulator scheme} \\ \searrow \lambda_{1,2} = \lambda_u \frac{1 + K^2}{2\gamma_{1,2}^2} & \text{twin-bunch scheme} \end{cases}$$

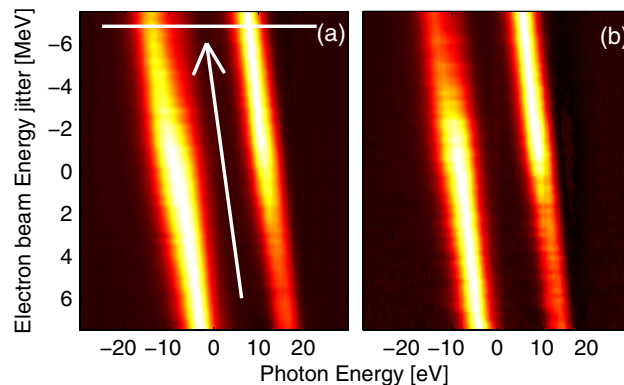
two colors + delay =



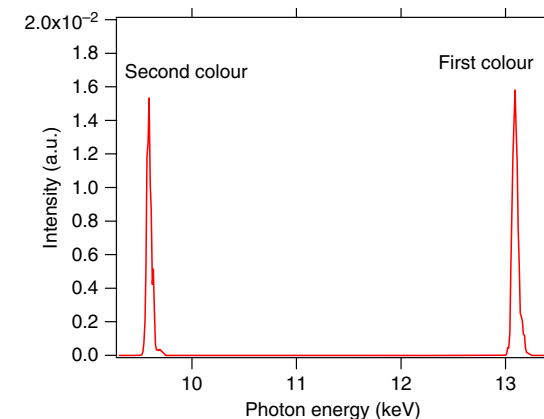
# TWO COLOR SASE FEL: SPLIT UNDULATOR SCHEME



- Advantage: easy to tune
- Drawback: reduced power due shorter undulator length available for one color (1/20 to 1/5 of one color SASE power)
- Max delay limited by chicane magnets: typically from ~50 fs to hundreds of fs
- Min delay: below 1 fs
- Time delay jitter: ~ 0.1%
- Energy separation of two colors: 0 to several 10%



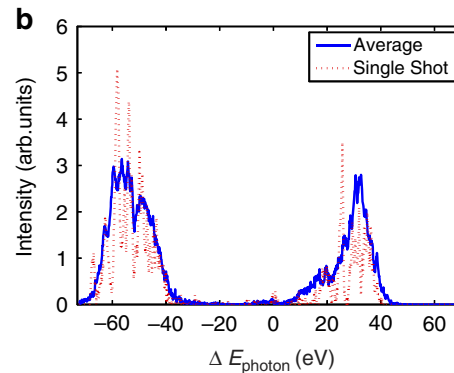
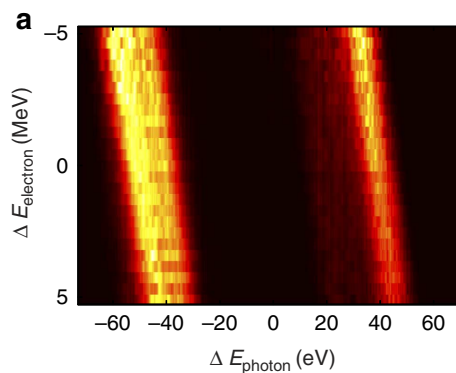
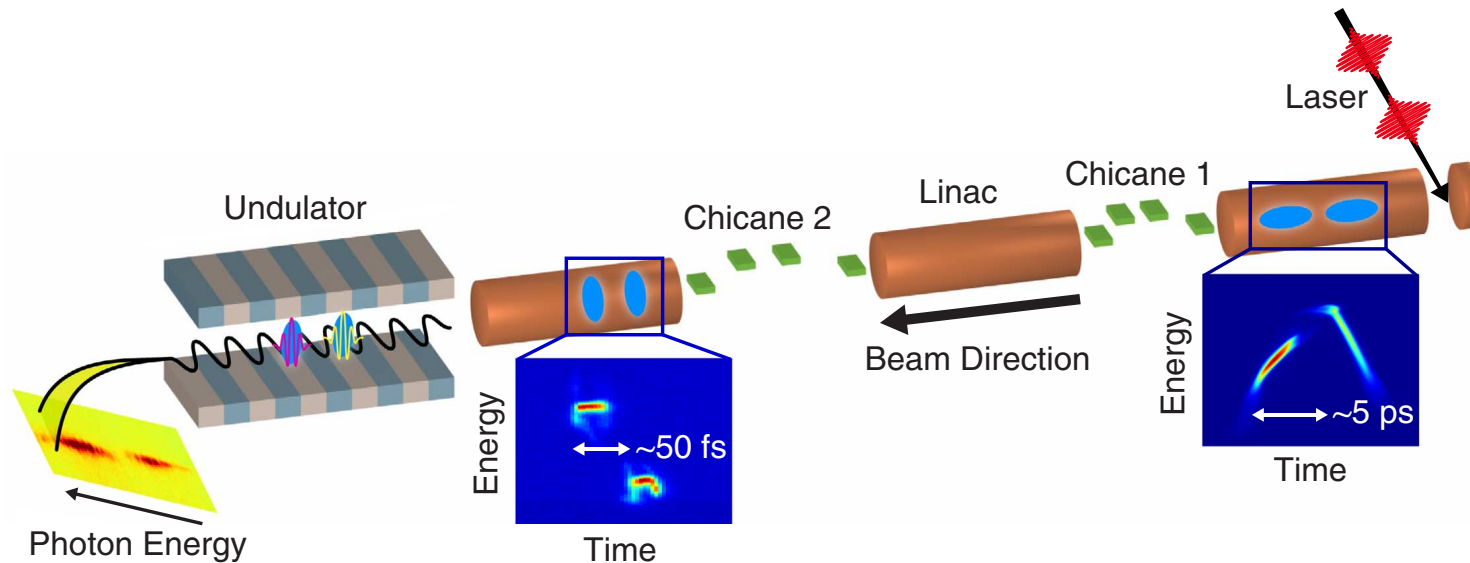
A. A. Lutman *et al.*, PRL, 2013



T. Hara *et al.*, Nat. Commun., 2013



# TWO COLOR SASE FEL: TWIN-BUNCH SCHEME



A. Marinelli *et al.*, *Nat. Commun.*, 2015

- Advantage: full undulator available for both colors  $\rightarrow$  more power
- Maximum energy separation:  $\sim 1\%$ , tuned by compression in Chicane 1
- Maximum delay:  $\sim 100$  fs, tuned by cathode delay and compression in Chicane 2
- Time delay jitter:  $\sim 5$  fs