



# ORBITAL SELECTIVITY AND HUND'S PHYSICS IN IRON-BASED SC

Laura Fanfarillo



# FROM FERMIL LIQUID TO NON-FERMIL LIQUID

Strong  
Correlation



Low  
Temperature



High  
Temperature

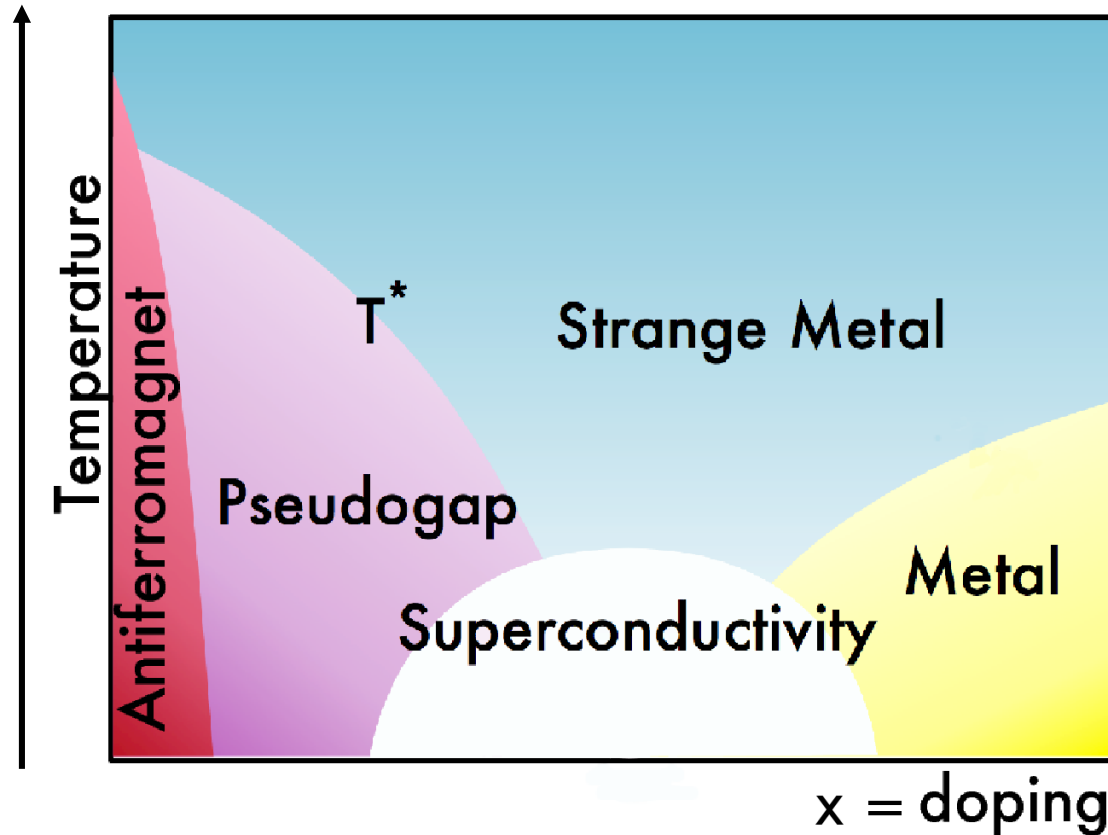
Fermi  
Liquid



Tuning parameter

Unconventional SC emerges at low temperature from a state that is far from an ideal metal

# FROM FERM LIQUID TO NON-FERM LIQUID : CUPRATES

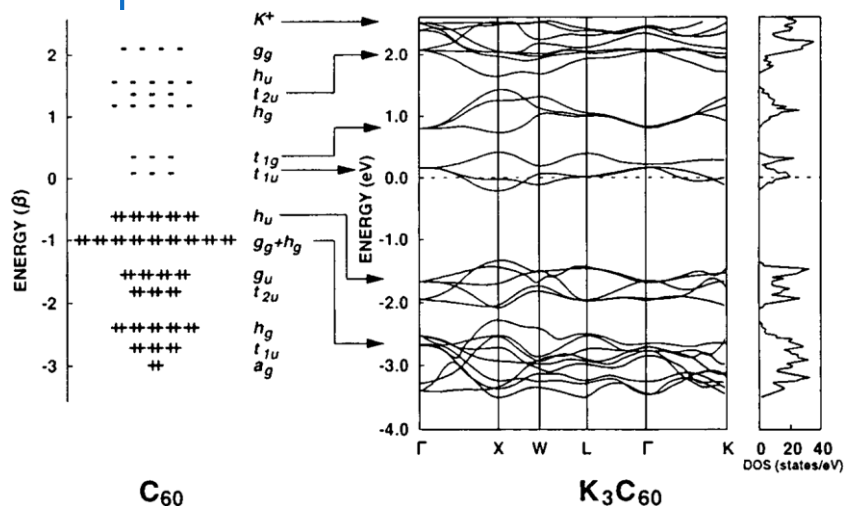


Physics of a doped  
Mott Insulator

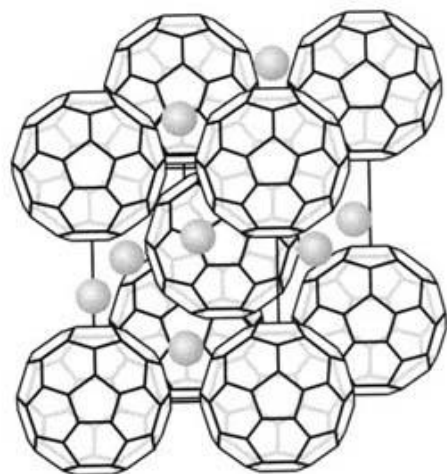
Unconventional SC emerges at low temperature from a state that is  
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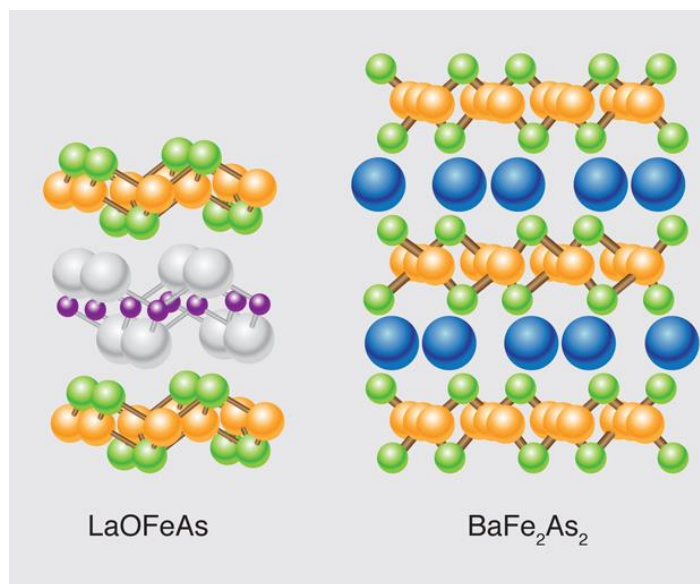
# MULTIORBITAL PHYSICS IN CORRELATED SYSTEMS



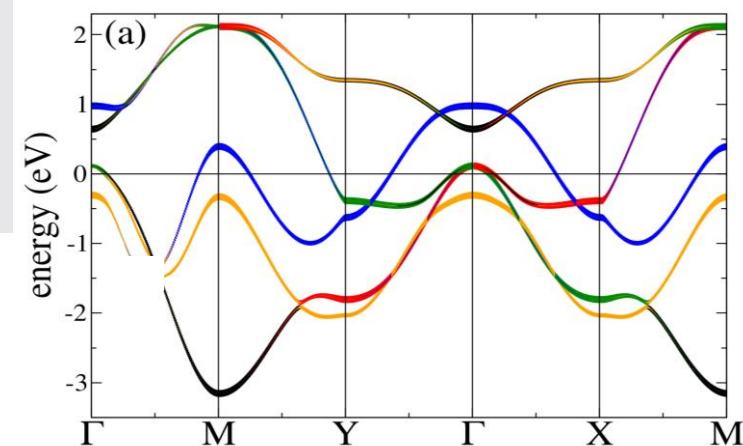
$A_3C_{60}$



Ruthenates, Iridates ...



... and  
Iron based SC



# IRON-BASED MATERIALS: INTERMEDIATE CORRELATED MATERIAL?



Strong  
Correlation



Hund's Physics

Orbital Selective Mott  
Physics

Small Crystal Field Splitting +  
Hund's coupling

DeMedici et al PRL 107 2011,  
DeMedici et al, PRL 112 2014,  
Fanfarillo et al PRB 92 2015 ...

Fermi  
Liquid



Localized Electrons Picture

Magnetic SuperExchange

Itinerant Electrons Picture

Fermi-Surface Instabilities  
(Nesting)

# HUND'S PHYSICS CONCEPTS

High spin  
atomic  
configuration

Bad  
Metal

Itinerant but  
heavy  
quasiparticles

Orbital  
Selective Mott  
physics

Orbital  
Decoupling

# MOTT-HUBBARD INSULATOR: SINGLE ORBITAL CASE HALF FILLING

Despite the conduction band is half-filled the system is insulating because of the strong Coulomb repulsion

Quasiparticle Spectral Weight Suppressed

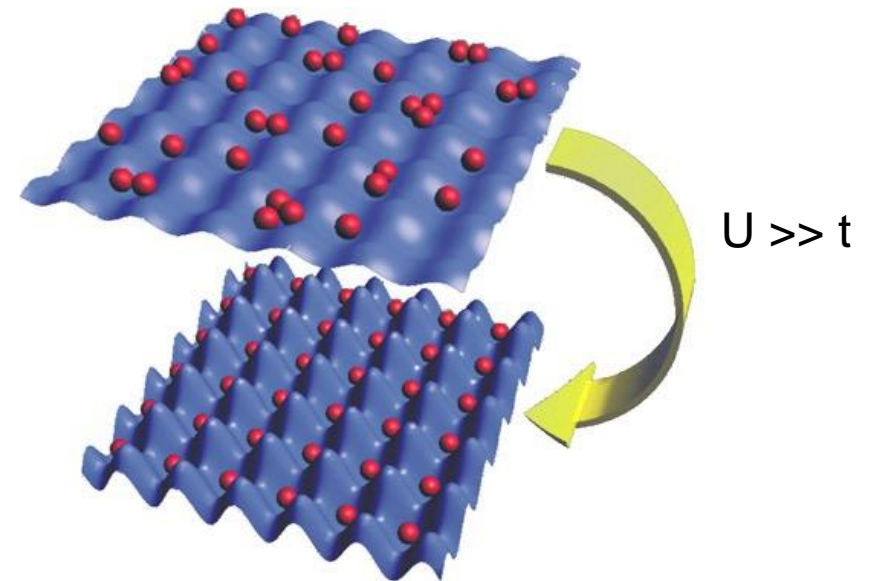
$Z \sim 1/m^*$  **increasing of correlation**

Charge Fluctuations Suppressed:

**localization of the electrons**

Spin Fluctuations Enhanced

**atoms are locally spin polarized**

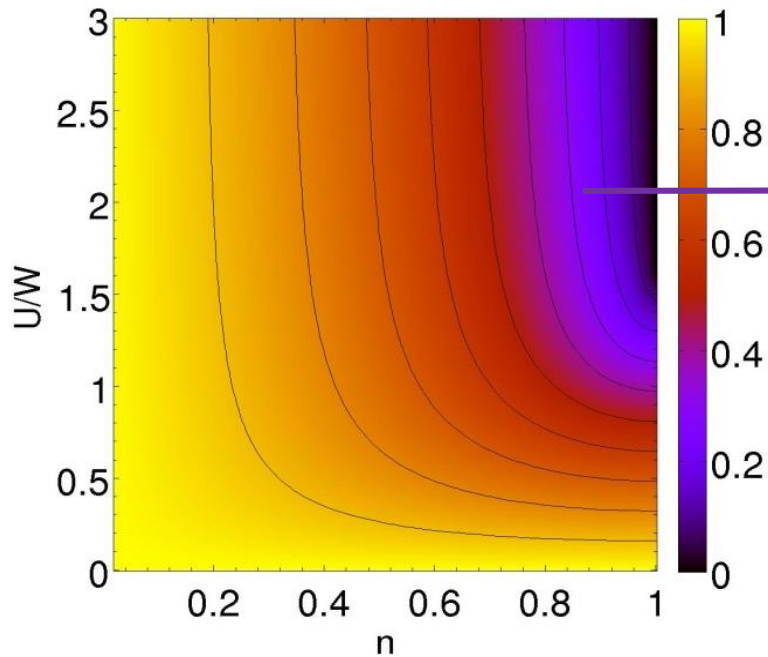


$Z=1$  FL - Metal

$Z=0$  Correlated electrons - Insulator

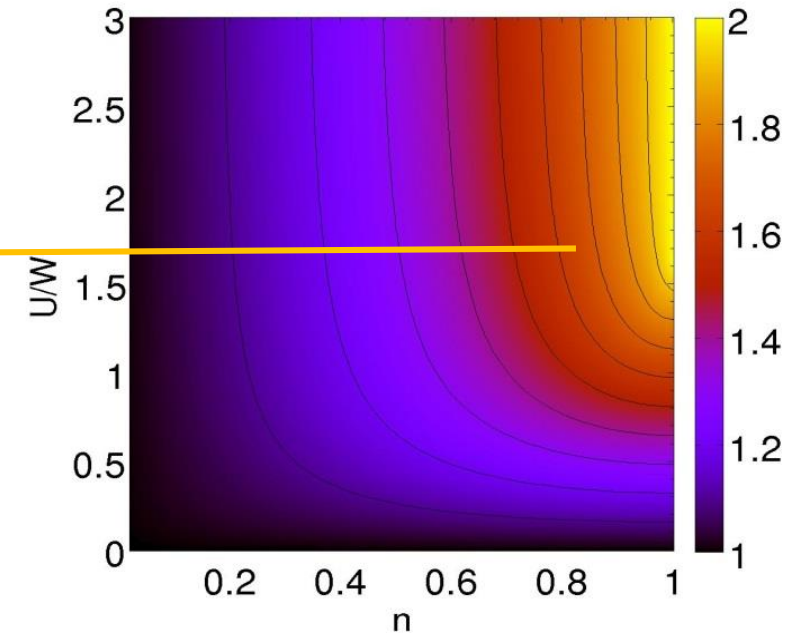
# MOTT-HUBBARD INSULATOR: SINGLE ORBITAL CASE IN DOPING

Far from half-filling ( $n \neq 1$ ) :



Correlated bad metal close to the Mott insulator

High Spin Phase





# MULTIORBITAL MODEL: U, JH

$$\begin{aligned} H = & \sum_{i,j,\gamma,\beta,\sigma} t_{i,j}^{\gamma,\beta} c_{i,\gamma,\sigma}^\dagger c_{j,\beta,\sigma} + h.c. + U \sum_{j,\gamma} n_{j,\gamma,\uparrow} n_{j,\gamma,\downarrow} \\ & + (U' - \frac{J_H}{2}) \sum_{j,\gamma > \beta, \sigma, \tilde{\sigma}} n_{j,\gamma,\sigma} n_{j,\beta,\tilde{\sigma}} - 2J_H \sum_{j,\gamma > \beta} \vec{S}_{j,\gamma} \vec{S}_{j,\beta} \\ & + J' \sum_{j,\gamma \neq \beta} c_{j,\gamma,\uparrow}^\dagger c_{j,\gamma,\downarrow}^\dagger c_{j,\beta,\downarrow} c_{j,\beta,\uparrow} + \sum_{j,\gamma,\sigma} \epsilon_\gamma n_{j,\gamma,\sigma} . \end{aligned}$$

tb (hopping term)      Intra-orbital repulsion

Inter-orbital repulsion      Hund's coupling

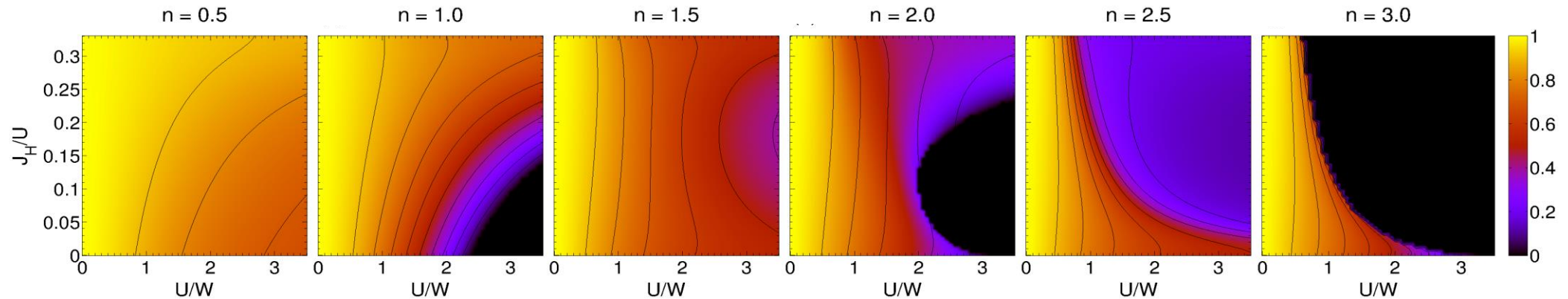
Pair hopping

Interactions are local and satisfy rotational invariance:  $U' = U - 2J_H$

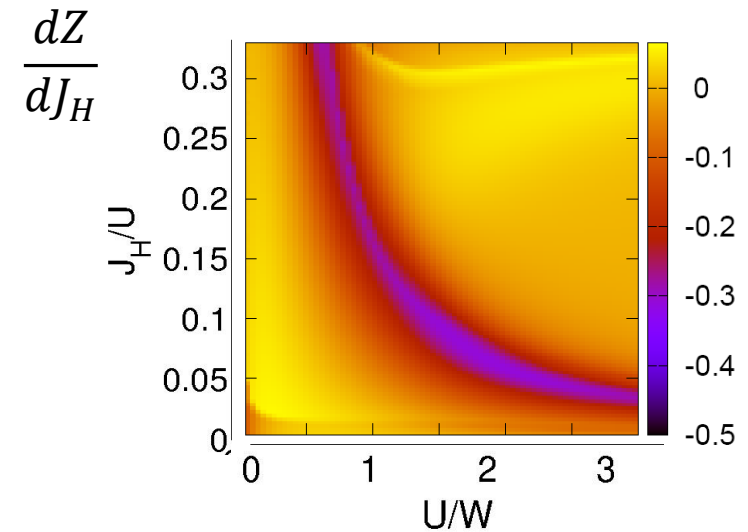
$U$  and  $J_H$  are free parameters

# MORE IS DIFFERENT: 3 ORBITALS

Quasiparticle  
Spectral Weight  
 $Z(U, J_H)$

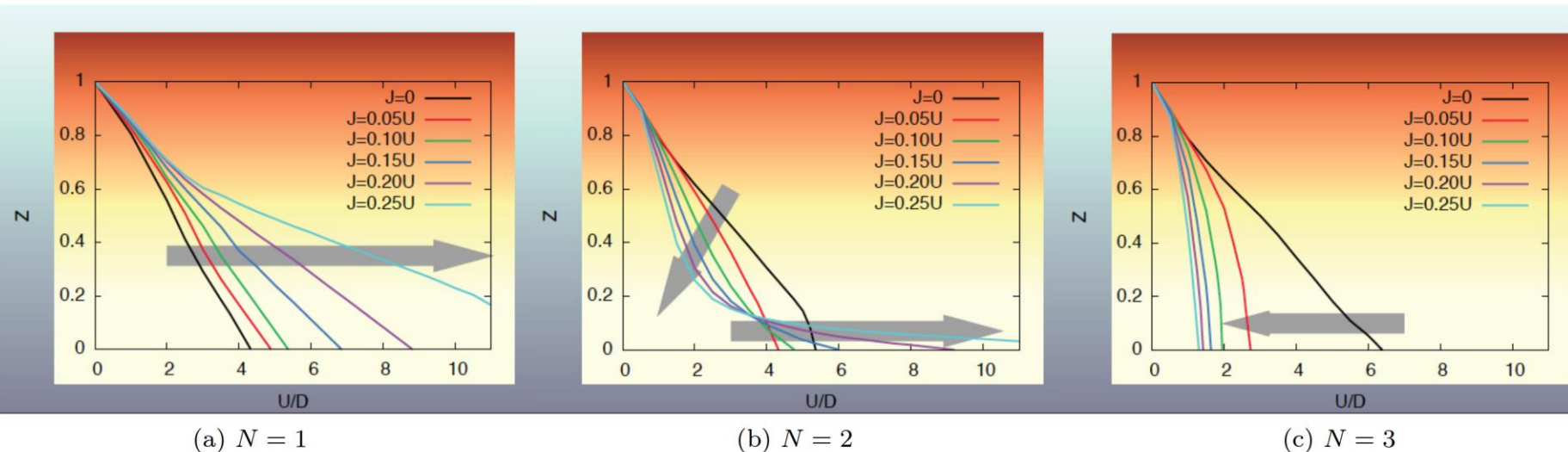
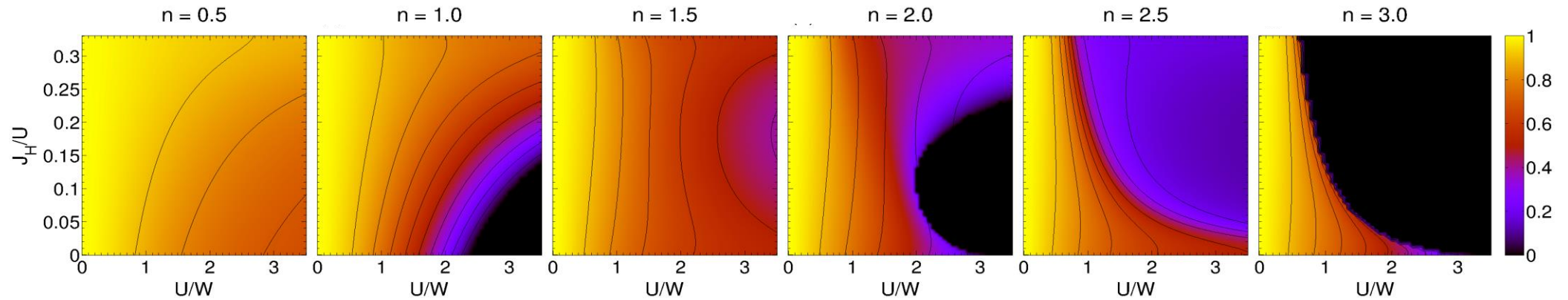


- Bad metals close to HF Mott Insulator
- Hund's metal boundary follows the MI transition line
  - Strong doping dependence:  
2(4) el/3orb Hund induces correlated metal state



# MORE IS DIFFERENT: 3 ORBITALS

Quasiparticle  
Spectral Weight  
 $Z(U, J_H)$

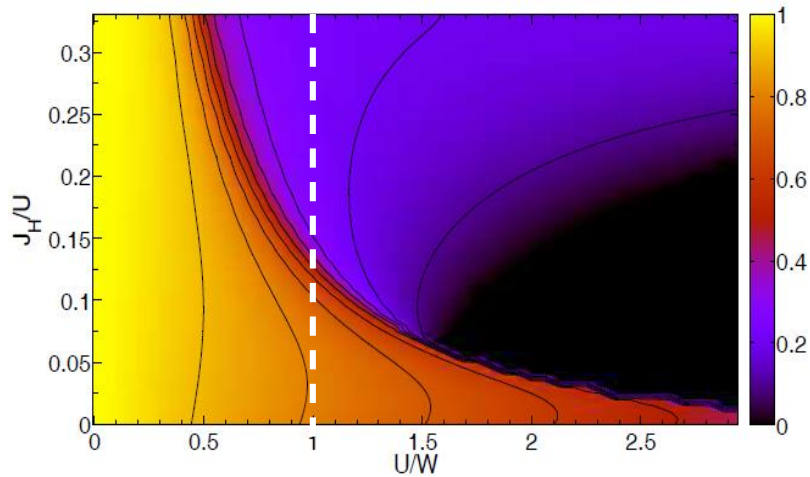


Strong doping dependence:  
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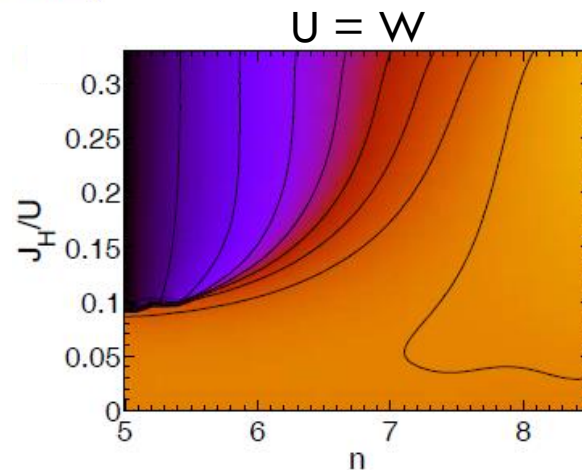
DeMedici et al PRL 107 (2011)

# THE IBS CASE: 6 ELECTRONS IN 5 ORBITALS

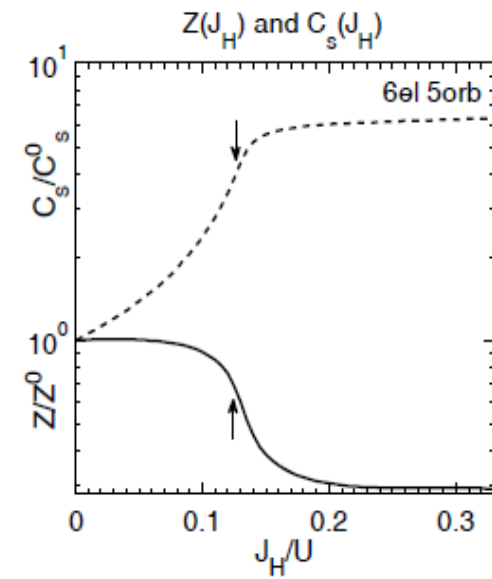
6 el in 5 orb



Hund'metal linked to the  
half-filled  $n=5$  Mott insulator  
*doping asymmetry around  $n=6$*

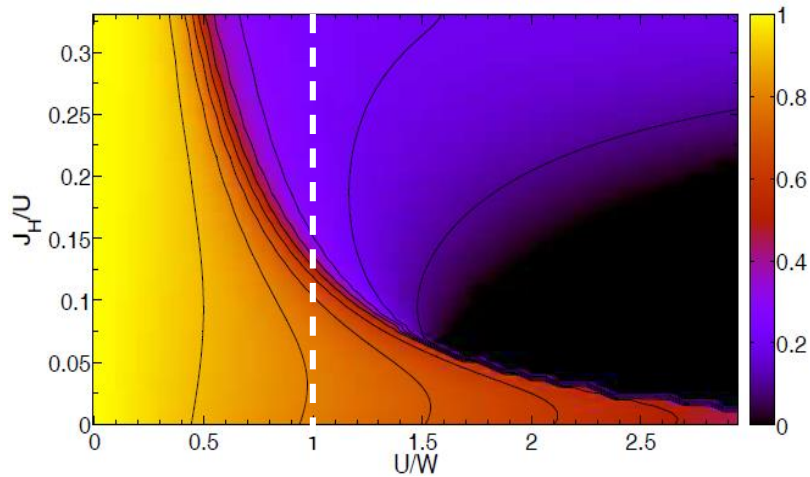


Hund's coupling induced  
high spin configuration

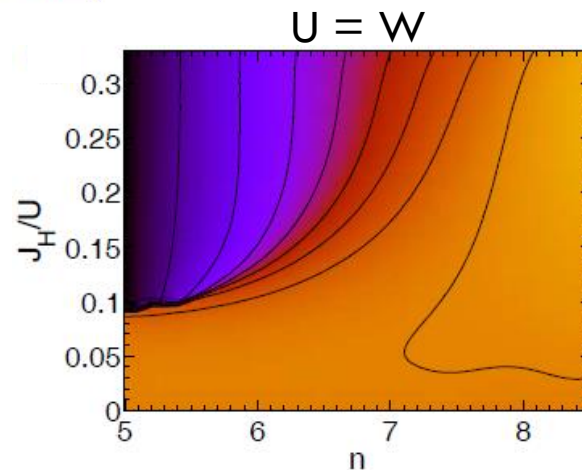


# THE IBS CASE: 6 ELECTRONS IN 5 ORBITALS

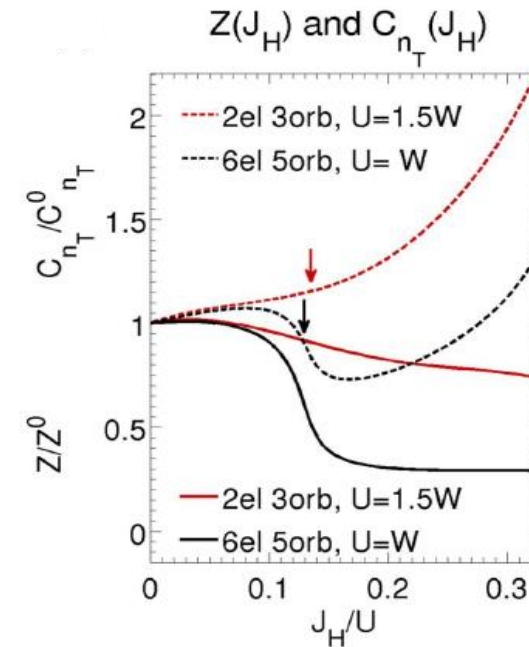
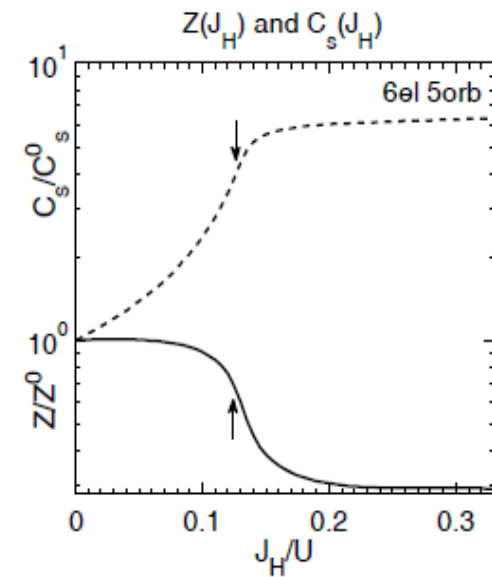
6 el in 5 orb



Hund'metal linked to the  
half-filled  $n=5$  Mott insulator  
*doping asymmetry around  $n=6$*



Hund's coupling induced  
high spin configuration



Quasiparticle weight  
and charge fluctuations:

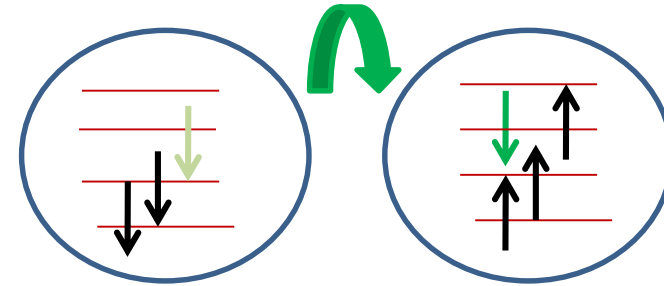
Correlation vs  
Localization





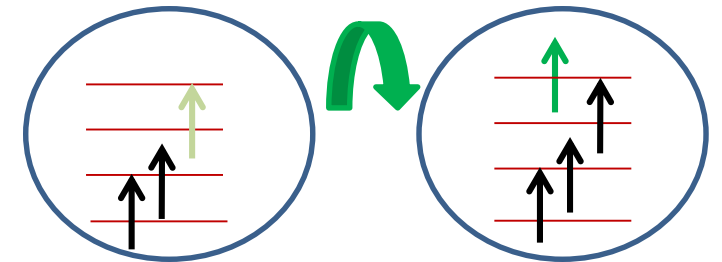
# HUND'S METAL: LINK TO HF MOTT TRANSITION

- ❑ Suppression of coherence due to suppression of hopping processes which involve **intraorbital double occupancy**



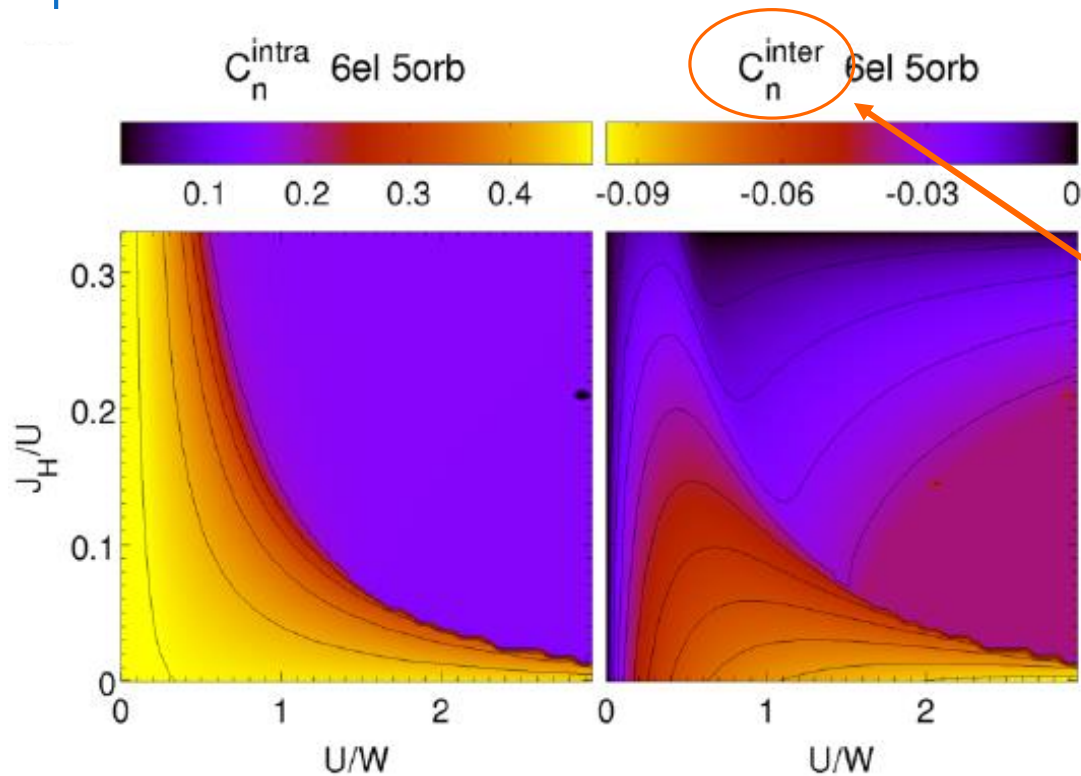
$$E^{intra\uparrow\downarrow} = U + (n - 1)J_H$$

- ❑ Enhancement of charge fluctuations due to hopping processes which involve parallel spins to an empty orbital



$$E^{\uparrow\uparrow} = U - 3J_H$$

# HUND'S METAL: LINK TO HF MOTT TRANSITION



As the double occupancies are suppressed:

- atoms becomes *spin polarized*

- *orbitals decoupled*

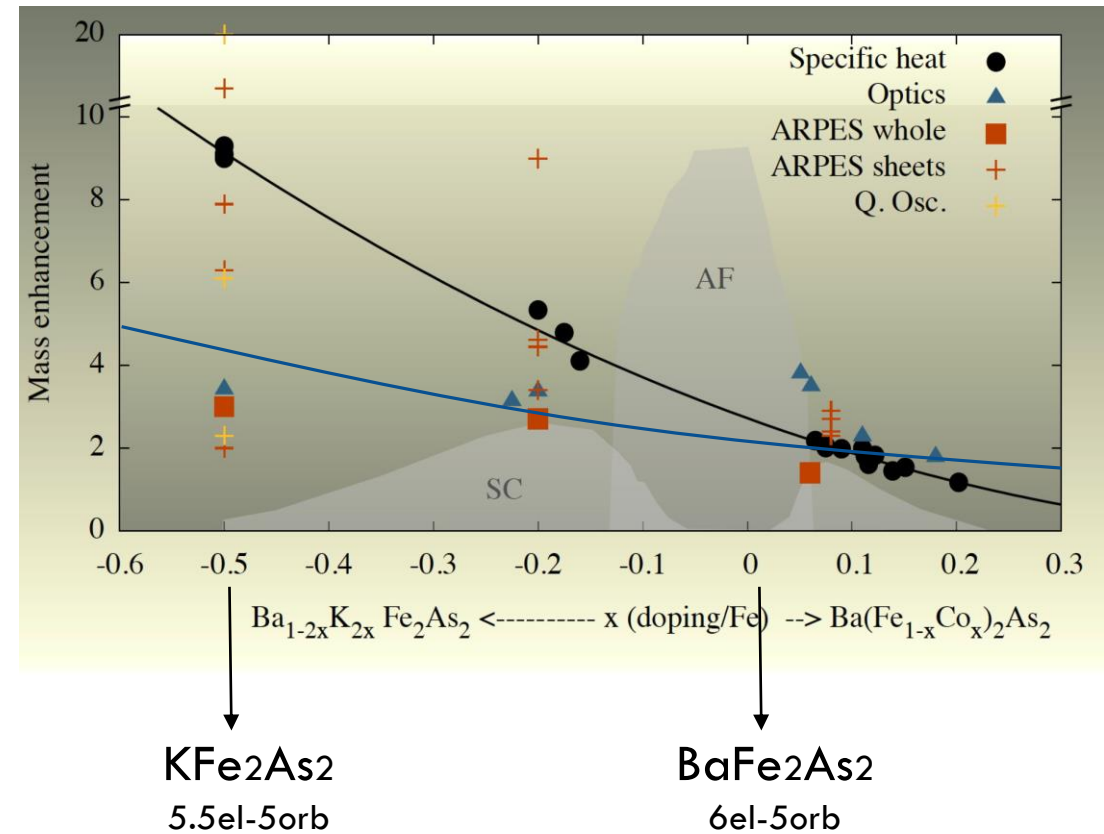
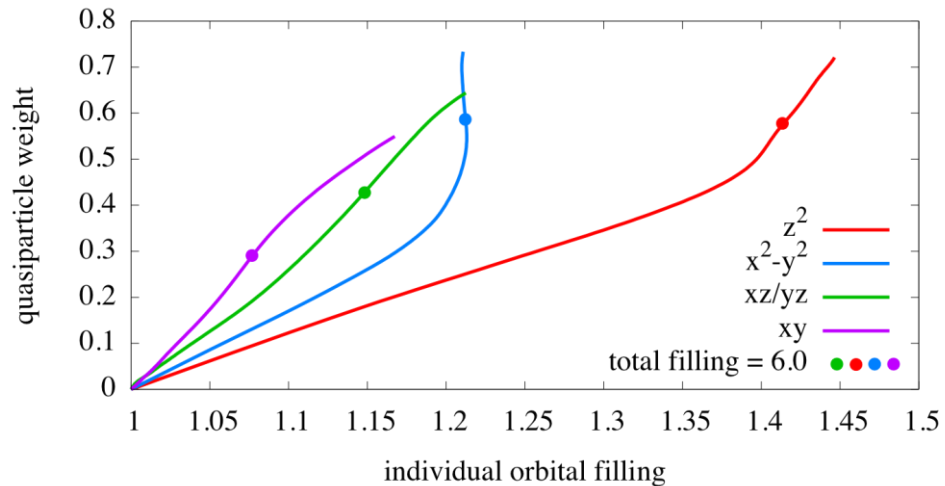
In the polarized state the effective interorbital interaction between the electrons decreases.

It vanishes at  $J_H = U/3$ .

# HUND'S PHYSICS IN IBS: EFFECTIVE MASS

- $m^*$  increases reducing the # of electrons
- $m^*$  strongly orbital selective

BaFe<sub>2</sub>As<sub>2</sub> - total filling from 6.25 to 5.0



- Each orbital has a different  $Z_\alpha \sim 1/m_\alpha^*$  proportional to the orbital filling

***Each orbital behaves as a doped Mott insulator***

# CONCLUSIONS: HUND'S PHYSICS IN IBS

- More is different:

- The degree of correlation is **complicated by the multiorbital physics**
- The entrance at the Hund's metal is due to the **suppression of the double occupancies**

Consequences: local spin polarization and orbital decoupling

- Correlation **is not** a good measure of localization

- IBS (parent compound 6 el/5 orb)

IBS collection of five decoupled single-band doped Mott insulator

Correlations increase reducing the number of electrons in d-bands:

$\text{KFe}_2\text{As}_2$  is much more correlated than  $\text{BaFe}_2\text{As}_2$

# CAN WE GO FURTHER?

## ORBITAL SELECTIVITY AND HUND'S PHYSICS IN THE PHASE DIAGRAM OF IBS

- *From the strong correlated side*

Try to figure out if local correlations can explain the phase diagram of IBS

Orbital selective SC ...

DeMedici et al arXiv 1609.01303

Fanfarillo et al arXiv 1609.06672 ...

- *From the FL side*

Project interacting multiorbital Hamiltonian into low-energy model for IBS

Orbital selective character of spin fluctuations

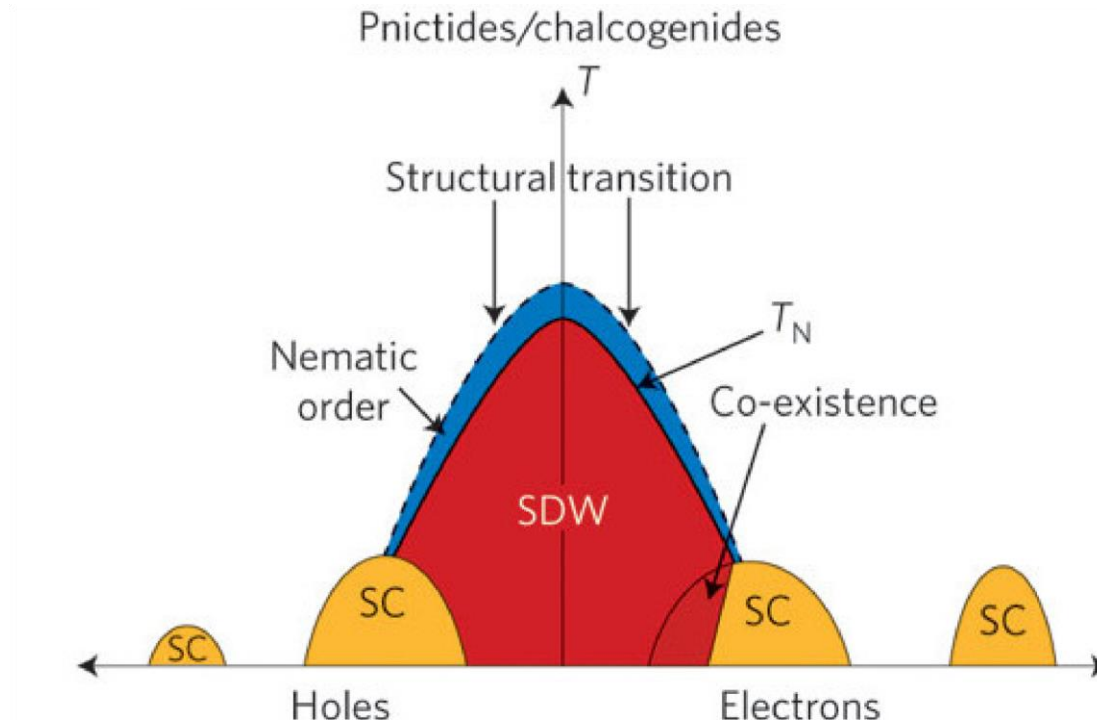
Fanfarillo et al. PRB 91 (2015),

Christenses et al. PRB 93 (2016)

Fanfarillo et al arXiv 1605.02482 ...



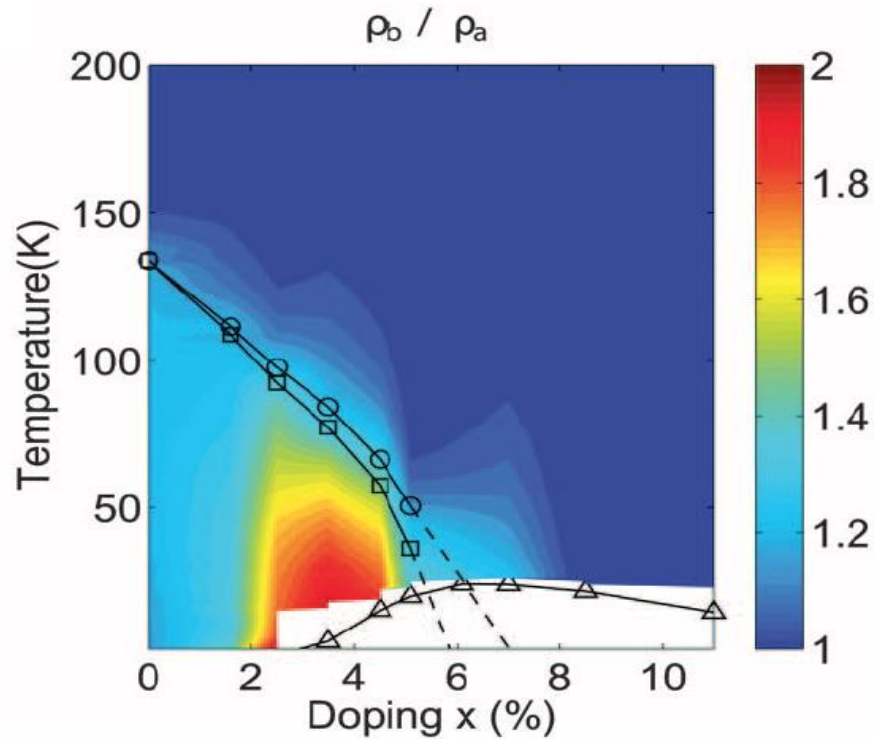
# NEMATIC PHASE OF IBS



Structural transition takes place before/simultaneously to the magnetic one:

Several experimental probes revealed  $x,y$  anisotropy above the magnetic transition not only in the lattice parameter but also in the electronic properties: [NEMATIC PHASE](#)

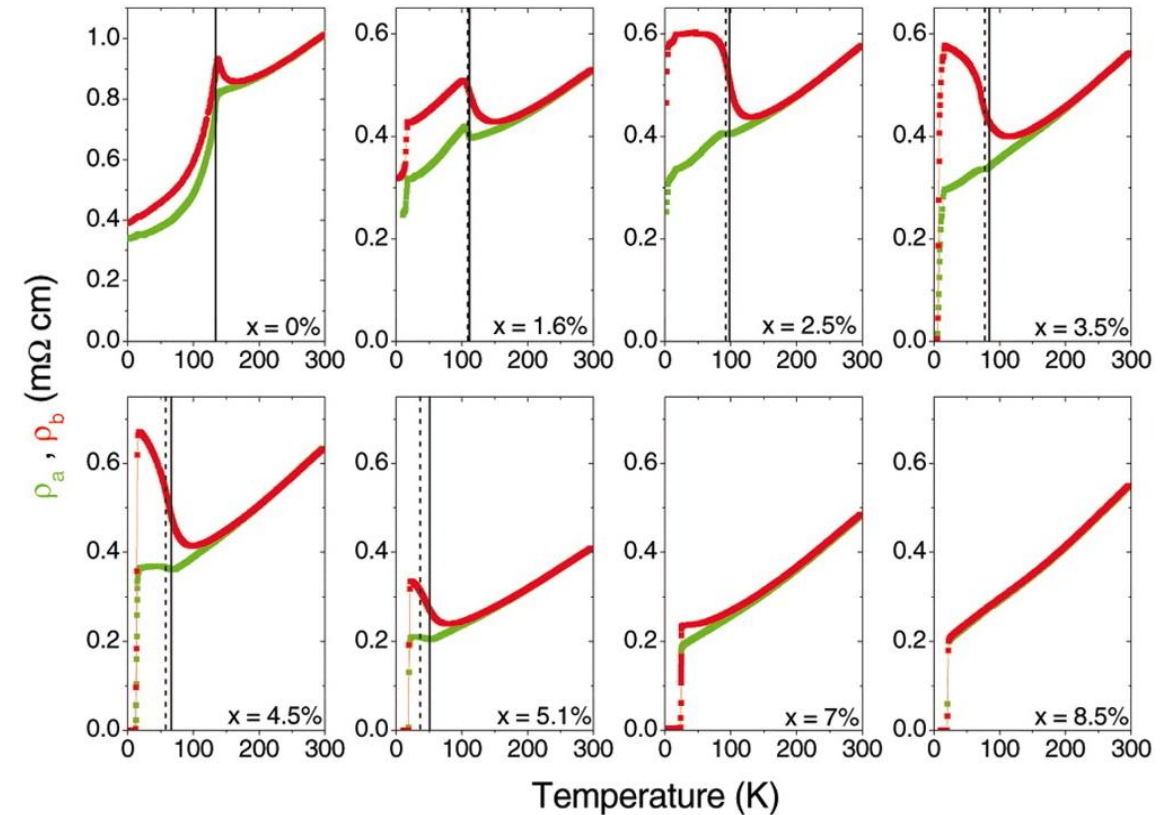
# NEMATIC PHASE OF IBS



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## Resistivity anisotropy measurements



J-H Chu et al. Science 329 (2010)

# MATTER OF ANISOTROPY

Possible origin of “nematic phase”:

- Structural distortion → Anisotropy from the lattice parameters (odd!)
- Orbital/Charge order → Anisotropy from the orbital filling
- Spin order → Anisotropy from spin fluctuations along  $x,y$

Classical “*chicken and egg problem*”

All three types of order (structural, orbital and spin-driven nematic) are very entangled  
no matter which drives the nematic instability.

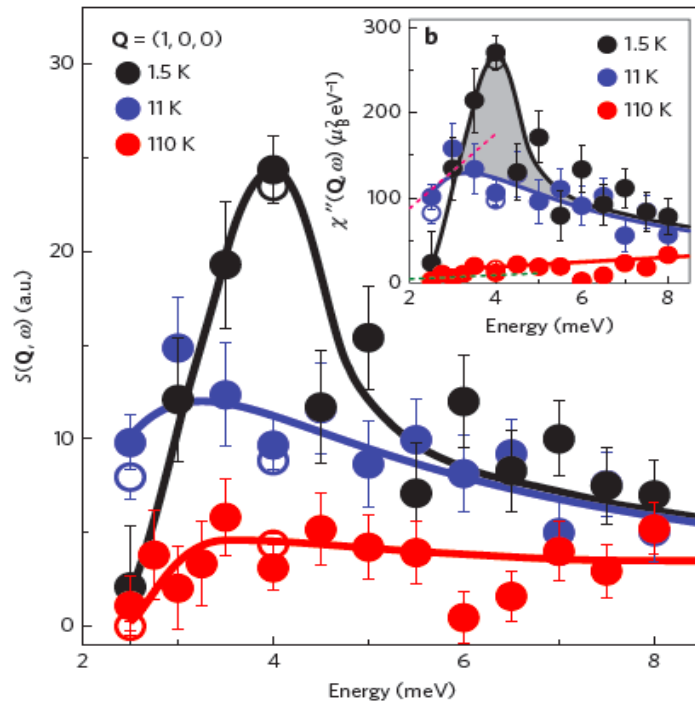
*What drives nematic order in iron-based superconductors?*

R.M. Fernandes et al. NATURE PHYSICS | VOL 10 | FEBRUARY 2014

*Enigmatic nematic*

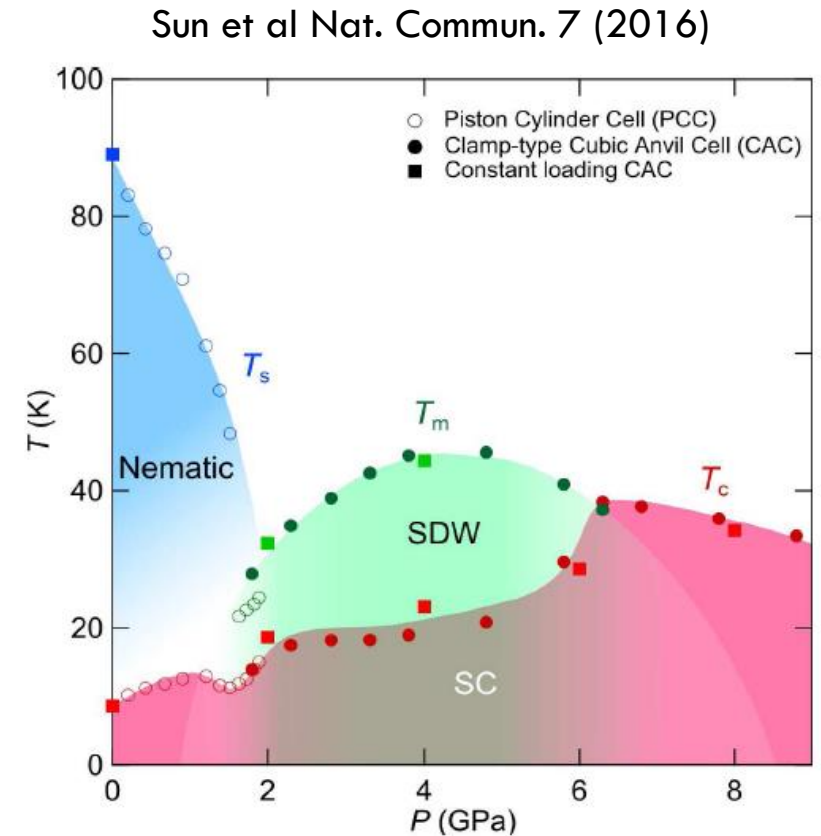
J. C. Davis and P. J. Hirschfeld NATURE PHYSICS | ADVANCE ONLINE PUBLICATION 2014

# THE CASE OF FESE: NEMATIC PHASE NOT FOLLOWED BY THE MAGNETIC ONE



Q. Wang et al. Nat. Mat. (2015)

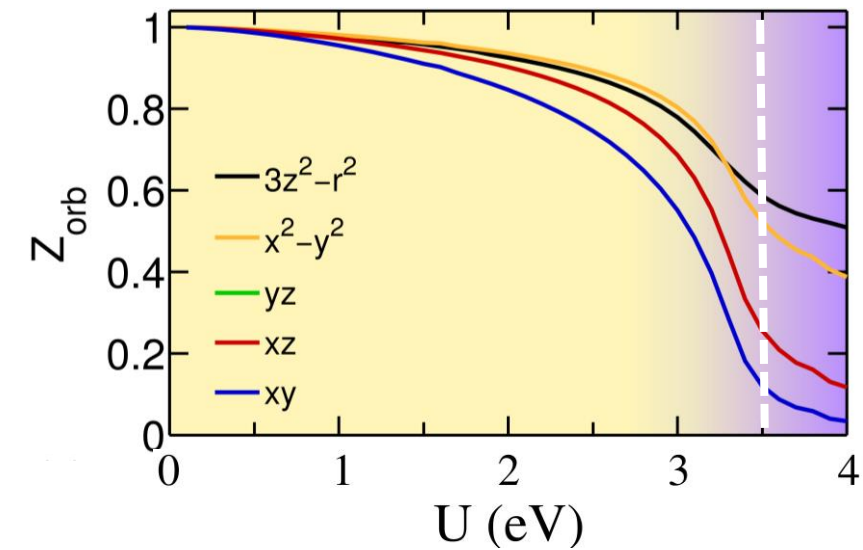
Sizeable SDW fluctuations  
but NO magnetic long  
range ordered phase



*Is the charge degree of freedom the driver?*

*Can local correlations induce a nematic phase transition?*

# ORBITAL NEMATIC PERTURBATION



From ARPES, Quantum oscillations, X ray  
FeSe  $\sim U = 3.5$  eV and  $J_H/U = 0.20$

Compute the Response of the system to **orbital perturbations modulated in k-space**:

$$\delta H_{A_{1g}/B_{1g}}^m = \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) h_m$$

Orbital Nematic Parameter:

$$\Delta_m = -\langle \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) \rangle$$

Linear response:

$$\chi_m = \frac{\delta \Delta_m}{\delta h_m}$$



# ORBITAL NEMATIC PERTURBATION

$$\delta H_{A_{1g}/B_{1g}}^m = \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) h_m$$

$$\Delta_m = -\langle \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) \rangle$$

**Onsite ferro-orbital**

$$h_{OFO} = \delta\epsilon \quad f_{OFO}(\mathbf{k}) = 1$$

$$\begin{array}{c} \epsilon_{zx} \\ \epsilon_{yz} \end{array} \begin{array}{c} \text{---} \\ \text{---} \end{array} \updownarrow \delta\epsilon$$

3 Orbital Orders considered in literature:

**Sign-change orbital order**

$$h_{SCO} = \delta t' \quad f_{SCO}(\mathbf{k}) = \cos k_x \cos k_y$$

Lift the degeneracy of the second neighbor hopping

**d-wave bond order**

$$h_{DBO} = \delta t \quad f_{DBO}(\mathbf{k}) = (\cos k_x - \cos k_y)/2.$$

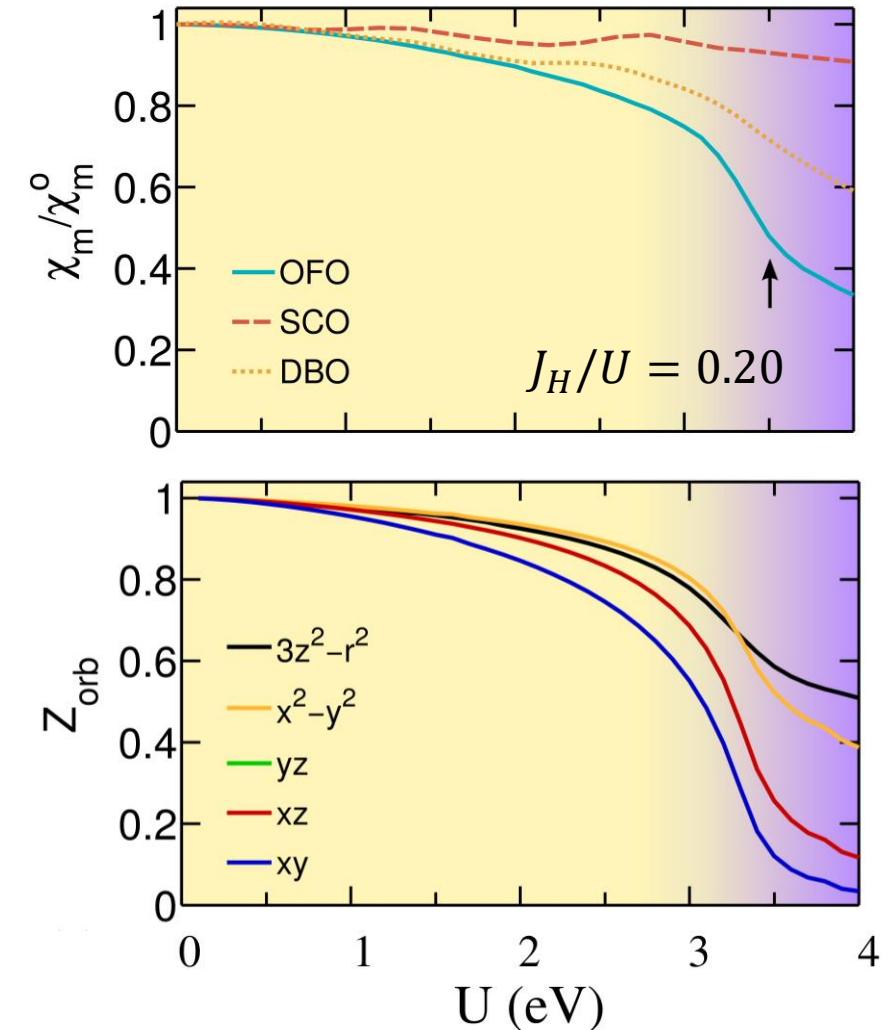
Lift the degeneracy of the nn hopping

# ORBITAL RESPONSE FUNCTIONS

No divergence = no phase transition

Interactions strongly suppress OFO order:  
*Suppression in correspondence of the entrance in  
the Hund Metal region.*

SCO order independent by U



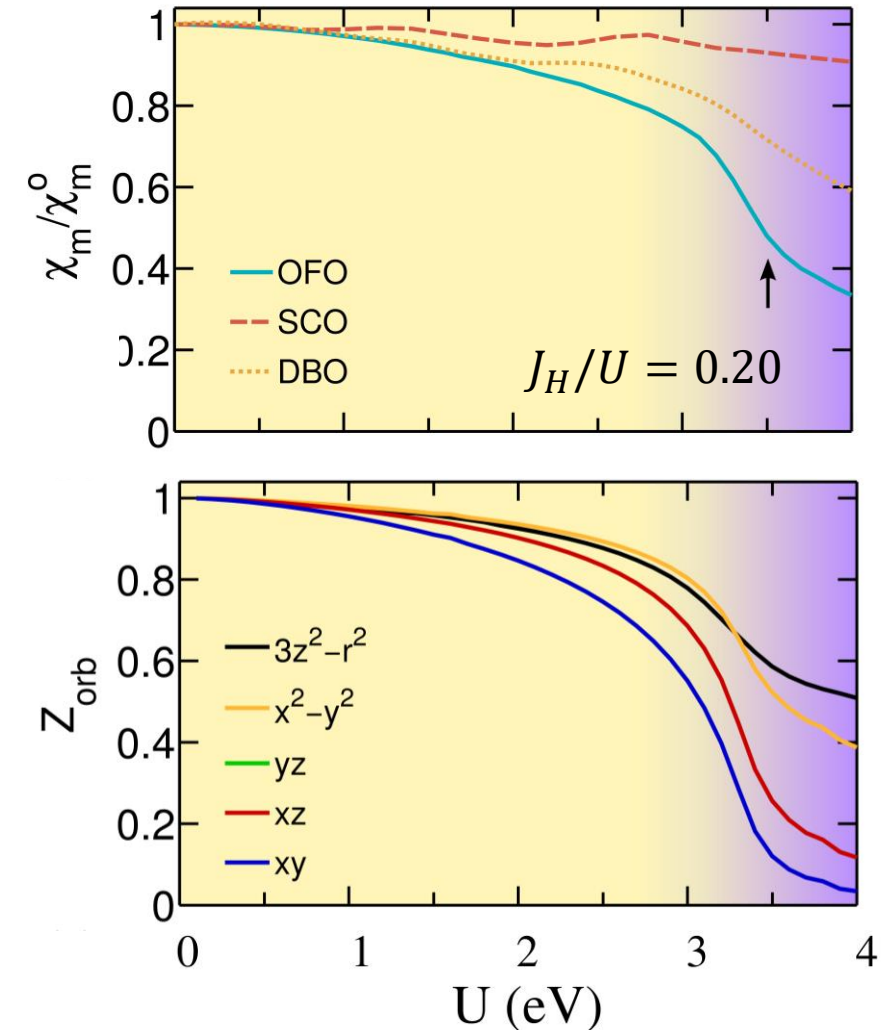
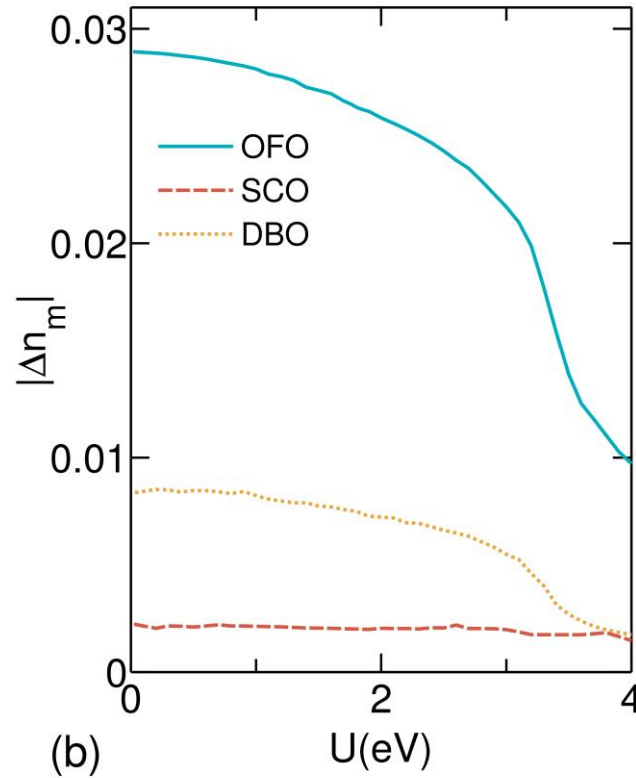
# ORBITAL RESPONSE FUNCTIONS

Sign-changing orbital order

small occupation imbalance  
between  $zx$  and  $yz$  orbitals



not suppressed by interactions!



# ORBITAL RESPONSE FUNCTIONS

- ✓ Local correlations cannot drive alone nematic transition
  - ✓ Correlations constrain possible orbital orders

Onsite ferro-orbital ordering strongly suppressed by interactions

Sign-changing orbital order = small occupation imbalance between  $z_x$  and  $yz$  orbitals = not suppressed by Hund's coupling.

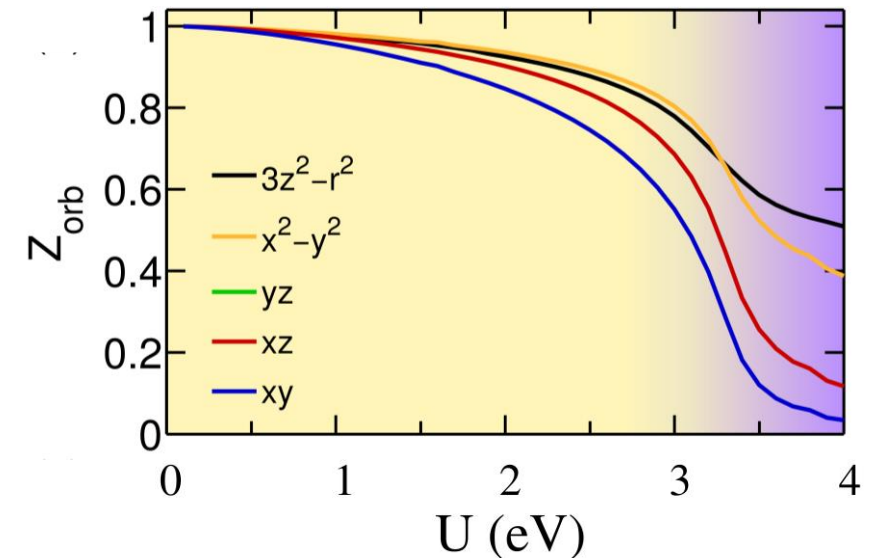
From RG Analysis:

Nematicity in the Pomeranchuk d-wave assisted by spin fluctuations

# ENHANCED NEMATICITY & HUND METAL PHASE

New route to nematicity:  
anisotropy in the orbital effective mass

$$\chi_Z^m(U) = \frac{\delta(Z_{zx} - Z_{yz})}{\delta h_m}$$





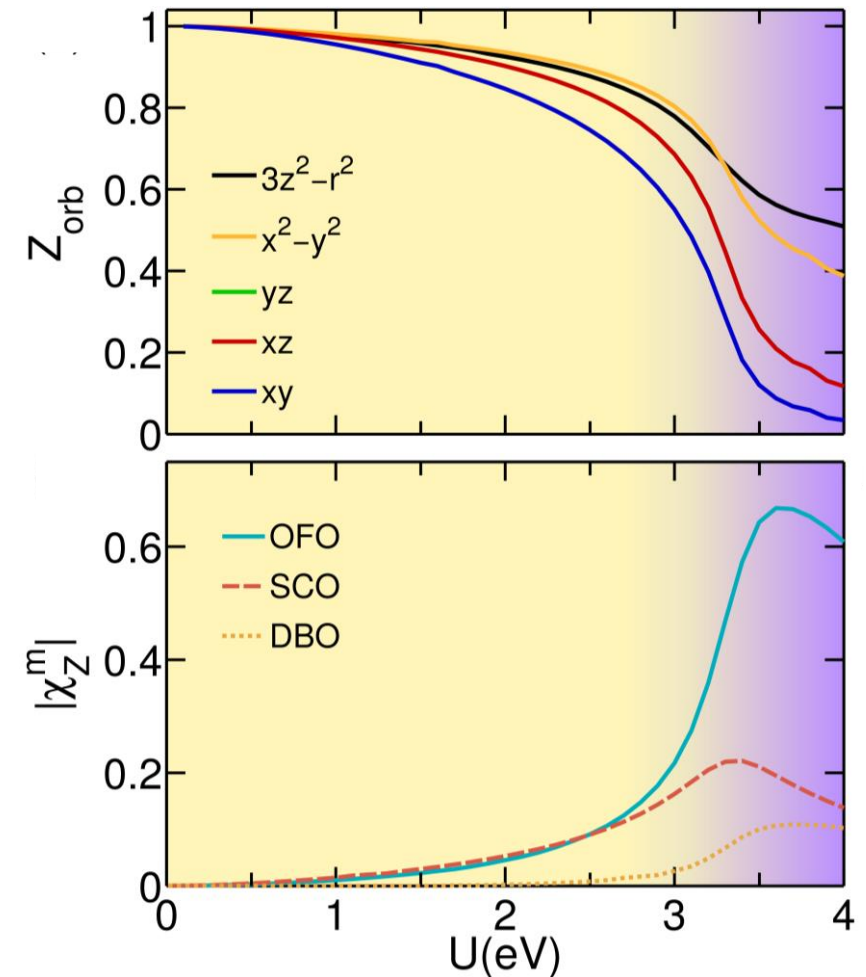
# ENHANCED NEMATICITY & HUND METAL PHASE

New route to nematicity:  
anisotropy in the orbital effective mass

$$\chi_Z^m(U) = \frac{\delta(Z_{zx} - Z_{yz})}{\delta h_m}$$

Anisotropy in the orbital mass is induced by  
the orbital order perturbation.

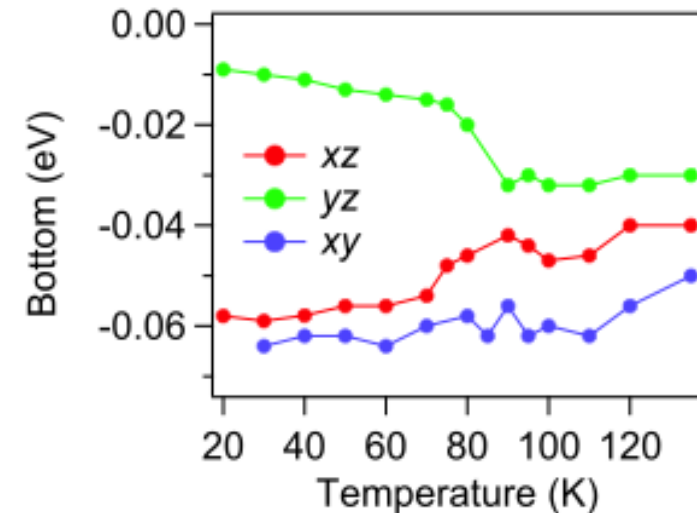
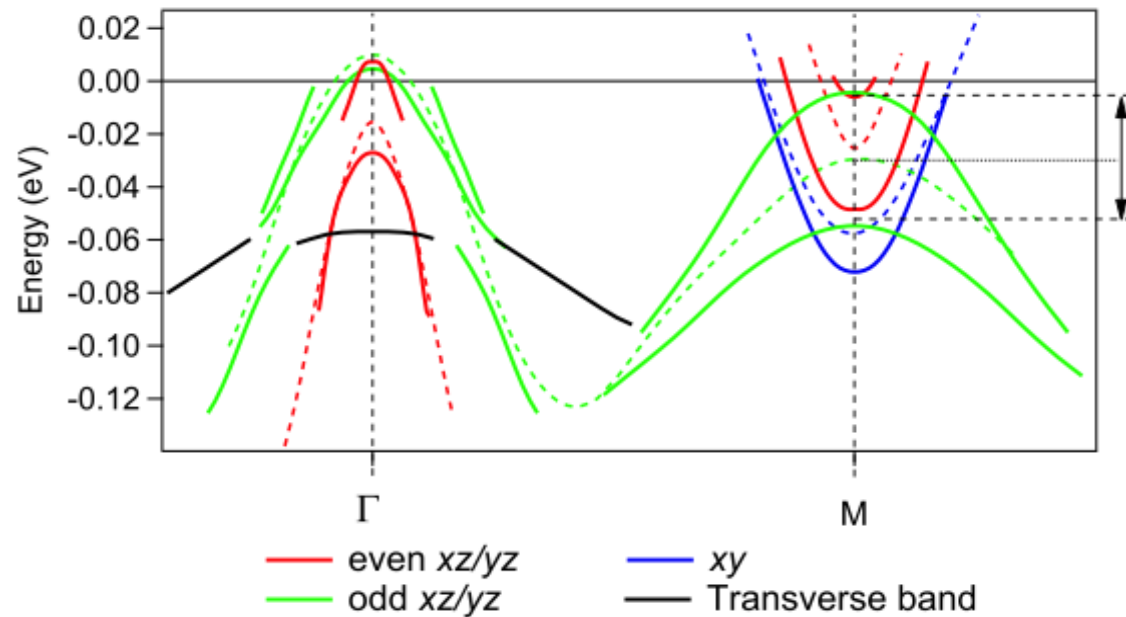
*Enhanced response at the entrance of the Hund  
Metal.*



# EFFECT ON THE BAND STRUCTURE

In the PARAMAGNETIC state  $zx$  and  $yz$  are degenerate = NO splitting at the symmetry points

In the NEMATIC state finite splitting appears between  $zx$  and  $yz$  bands at the symmetry points.



# EFFECT ON THE BAND STRUCTURE

In the PARAMAGNETIC state  $zx$  and  $yz$  are degenerate = NO splitting at the symmetry points

In the NEMATIC state finite splitting appears between  $zx$  and  $yz$  bands at the symmetry points.

Given an orbital perturbation the naive splitting expected at the  $\Gamma$  and  $M$  point are:

$$Sp_{\Gamma}^{OFO}(U=0) = 2\delta\epsilon$$

$$Sp_{\Gamma}^{SCO}(U=0) = 2\delta t'$$

$$Sp_{\Gamma}^{DBO}(U=0) = 0$$

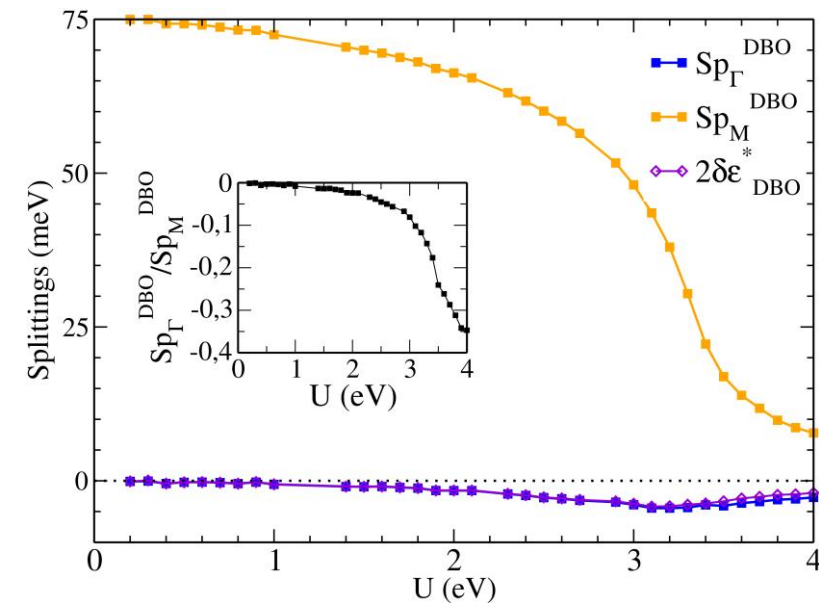
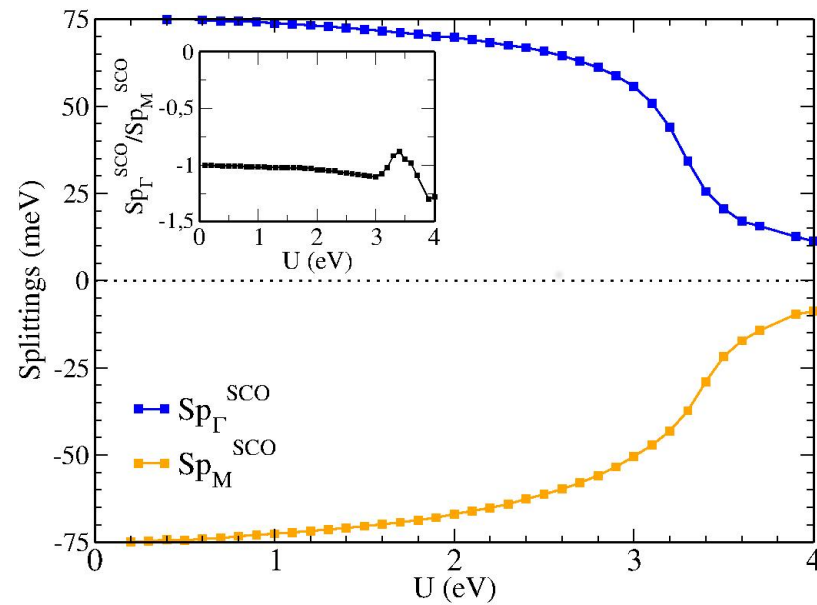
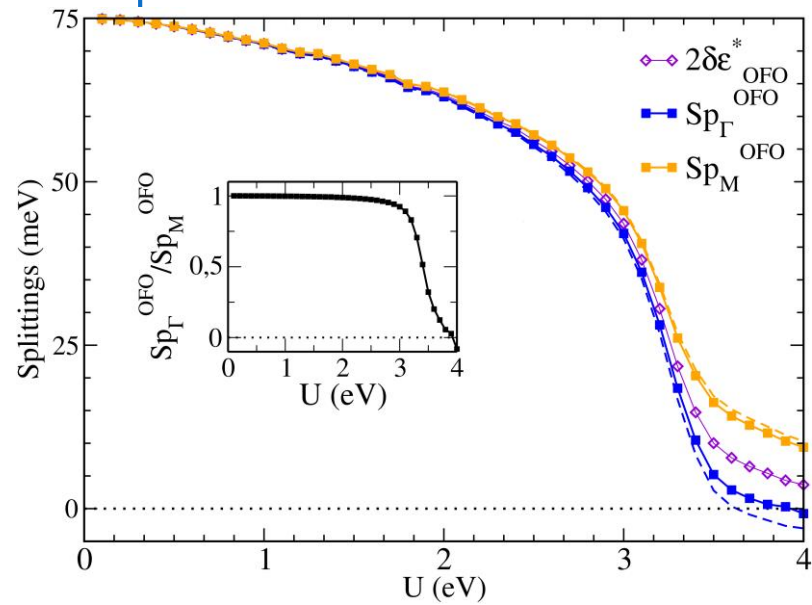
$$Sp_M^{OFO}(U=0) = 2\delta\epsilon$$

$$Sp_M^{SCO}(U=0) = -2\delta t'$$

$$Sp_M^{DBO}(U=0) = 2\delta t \quad (!)$$

Interactions renormalize the band structure (via  $Z$   $xz/yz$  anisotropy) and can modify the bare splitting

# EFFECT ON THE BAND STRUCTURE



*Local Correlations modify the orbital splitting:  
Induce  $k$ -dependence, drive sign change ...*

# MASS ANISOTROPY AND ORBITAL SPLITTING

- ✓ Hund's coupling induces anisotropy in the correlation strength of  $zx$  and  $yz$  orbitals
- ✓ Hund's physics modifies the magnitude of these splittings, their relative value and even their sign.

From ARPES:

Hole/electron sign change orbital polarization observed in FeSe interpreted as a self-energy effect of a low energy orbital selective model

# CONCLUSIONS: HUND PHYSICS IN THE NEMATIC PHASE

- ✓ Only orbital orders that do NOT create large occupation unbalance survive to the correlations
- ✓ Hund's induce **anisotropy in the effective masses of  $zx$  and  $yz$  orbitals**.  
This anisotropy affects the renormalization of the band structure, leading to distinctive signatures in different experimental probes including ARPES.

Important insights for low-energy modeling of IBS



# COLLABORATORS



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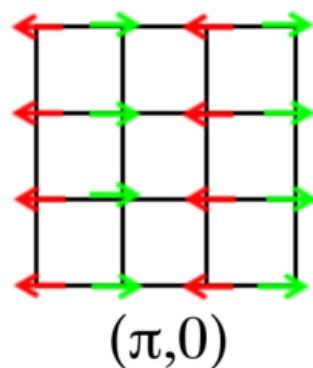
L. Benfatto

Paris-Sud Orsay

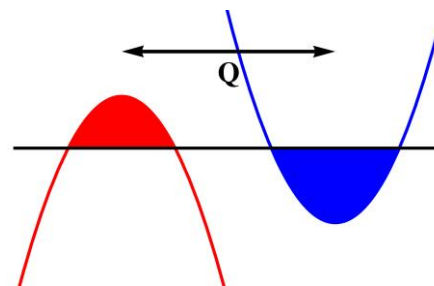
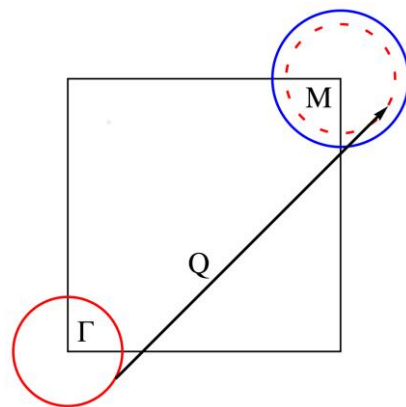
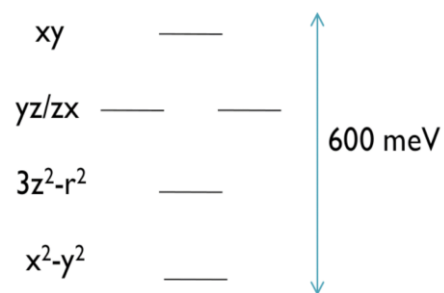
V. Brouet

# THE IRON AGE OF SC

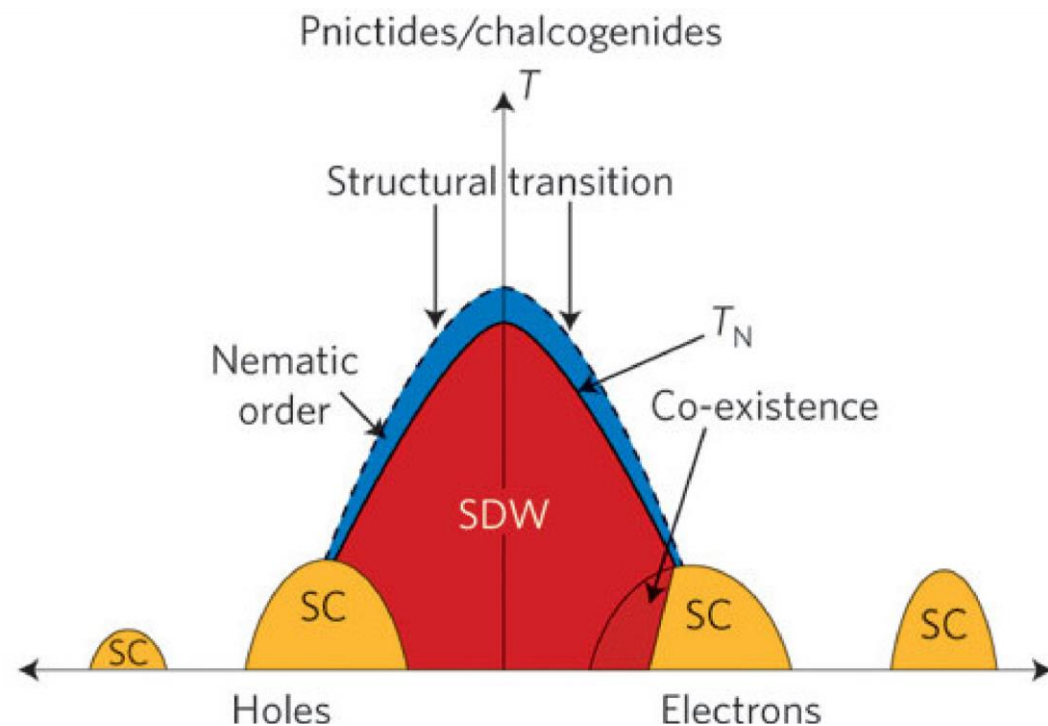
Parent Compound:  
SDW bad metal



Multiband SC System:  
3d Iron orbitals



$Q$  - SDW vector



Nodless gap:  $s_{\pm}$   
symmetry

# IRON-BASED MATERIALS: CORRELATED OR NOT?

## Contrasting evidences for correlation strength

weak

- no Mott insulator in the phase diagram
- hard detection of any Hubbard bands
- moderate correlations from Optics

- Strong mass renormalization from ARPES, Q. Osc. with respect DFT
- bad metallicity
- strong sensitivity to doping

strong

Itinerant electron vs Localized electrons picture

# OFO PERTURBATION: $J_H$ ANALYSIS

→ **Onsite perturbation**

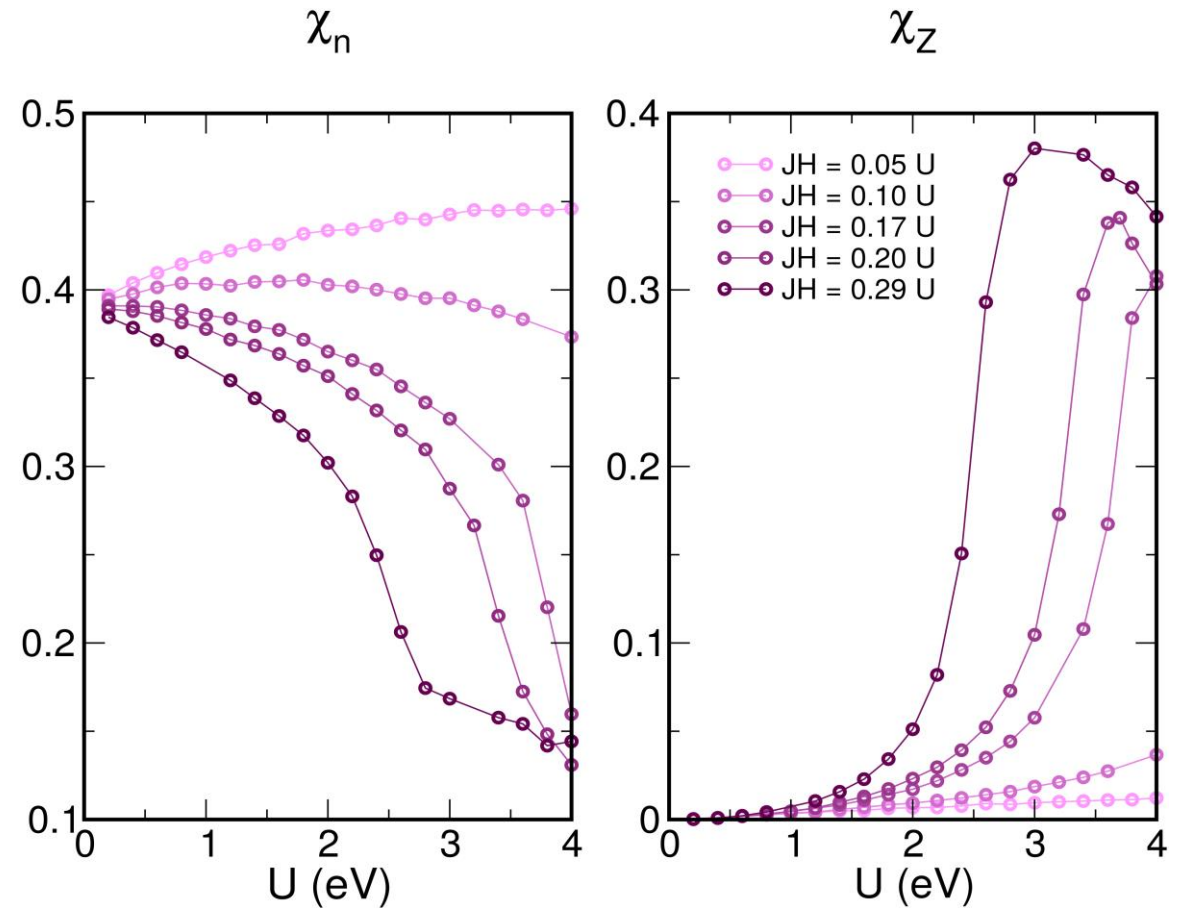
Onsite splitting  $\delta\epsilon = \epsilon_{xz} - \epsilon_{yz}$

$$\begin{array}{c} \epsilon_{zx} \\ \epsilon_{yz} \end{array} \begin{array}{c} \text{---} \\ \text{---} \end{array} \updownarrow \delta\epsilon$$

→ **Susceptibility**

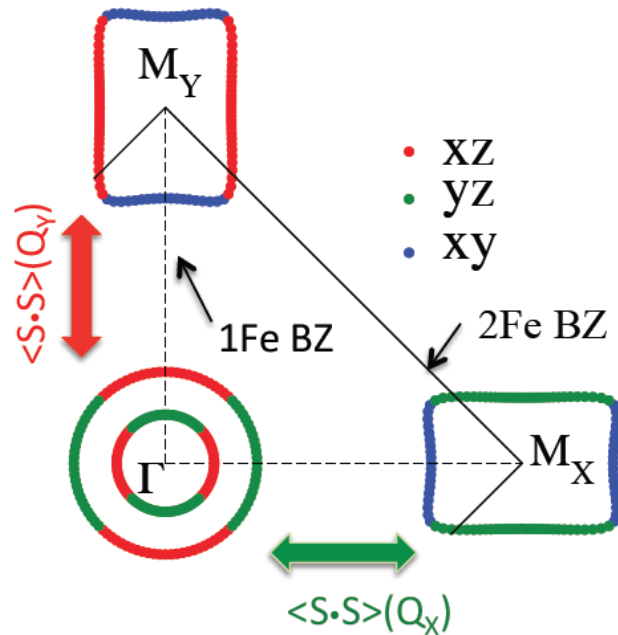
$$\chi_n = \frac{n_{yz} - n_{xz}}{\delta\epsilon}$$

$$\chi_Z = \frac{Z_{yz} - Z_{xz}}{\delta\epsilon}$$



# ORBITAL SELECTIVITY IN LOW ENERGY MODEL

Project interacting multiorbital Hamiltonian into low-energy model for IBS



- Nematicity follows from the yz/xz orbital
- Spin fluctuations are orbital selective
- Self-energy corrections orbital dependent shrinking of the Fermi Surfaces