

# Updated measurement of gamma-ray angular power spectrum of anisotropies

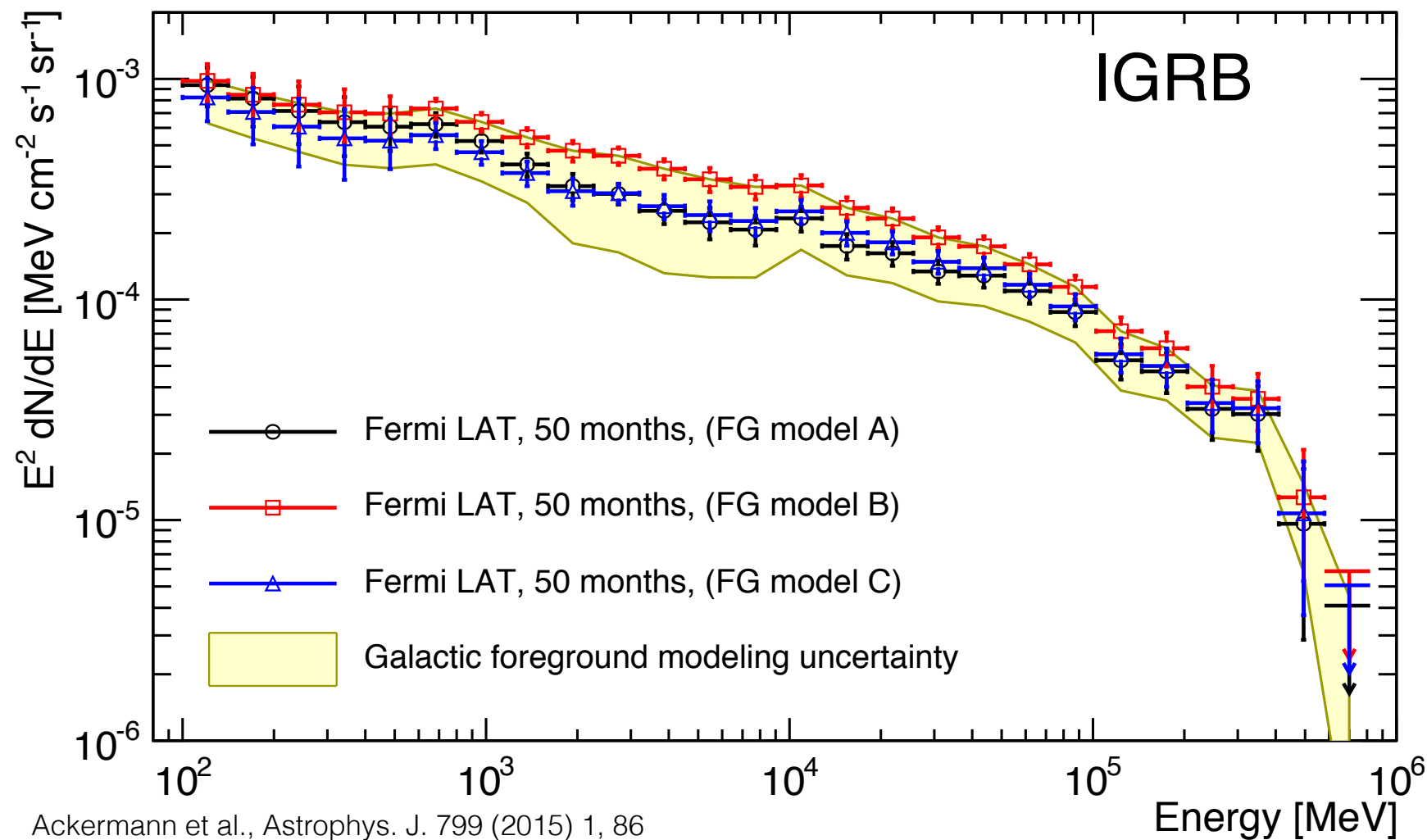
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G. Gomez-Vargas, E. Komatsu, T. Linden, F. Prada, F. Zandanel and A. Morselli



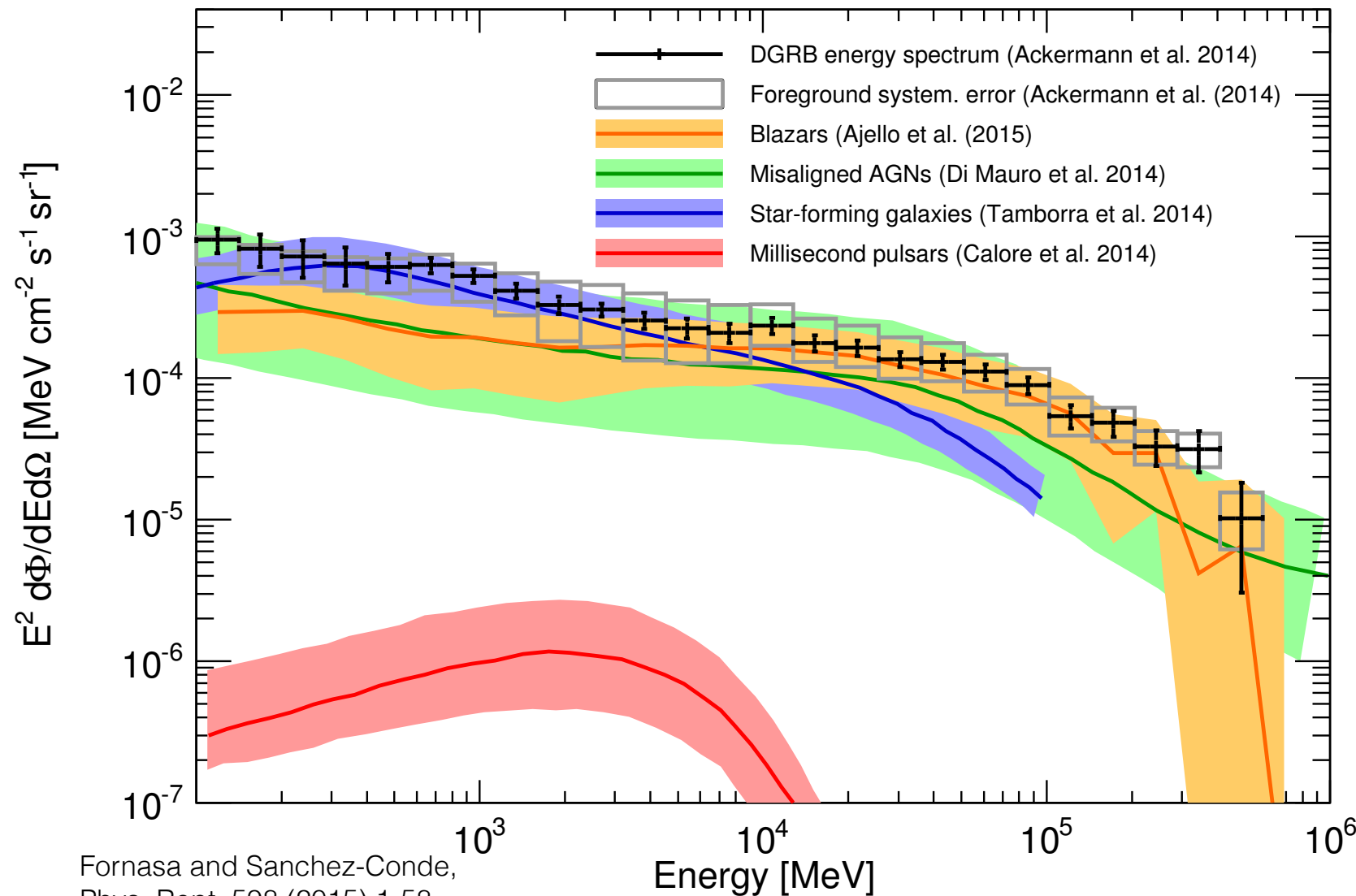
# The Diffuse Gamma-Ray Background (DGRB)



- multi-component fit to Fermi-LAT data
- power-law energy spectrum with a slope of  $2.32 \pm 0.02$  at lower energies and a cut-off at  $279 \pm 52$  GeV
- systematic uncertainty related to the Galactic foreground (15% to 30%)



# Unresolved gamma-ray sources

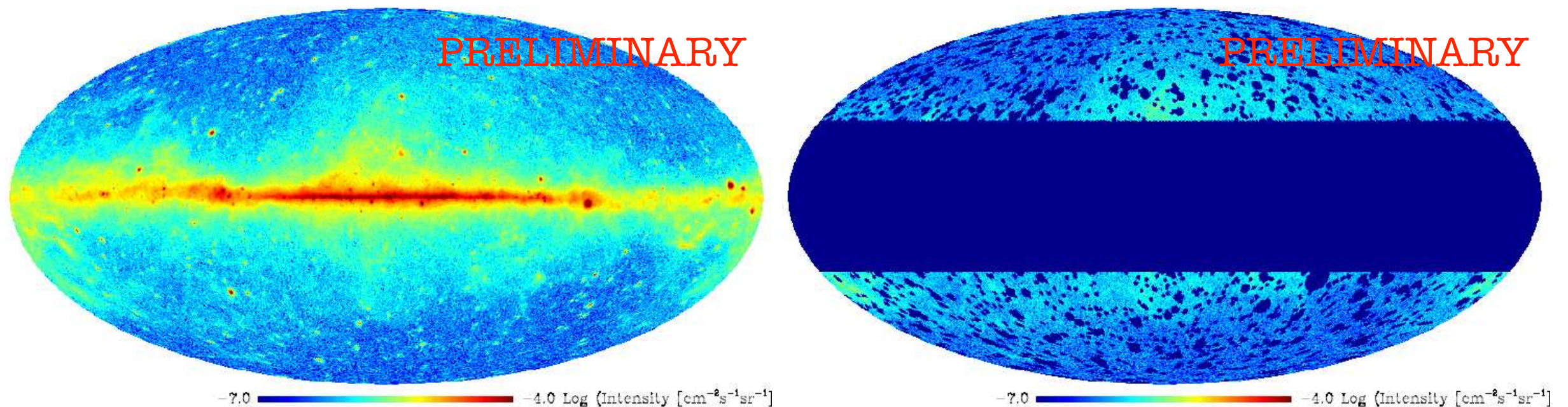


- cumulative emission of unresolved sources
- guaranteed components from unresolved blazars, star-forming galaxies, misaligned AGNs
- build a similar plot for angular power spectrum of anisotropies

$$I(\psi) = \sum_{\ell m} a_{\ell, m} Y_{\ell, m}(\psi)$$

$$C_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$

# New APS measurement



New measurement

81 months

Pass 7 reprocessed  
(ULTRACLEAN\_v15) front

13 energy bins  
between 0.5-500 GeV

masking sources in 3FGL

Ackermann et al. (2012)

22 months

Pass 6 (DIFFUSE\_v3) front and  
back

4 energy bins  
between 1-50 GeV

masking sources in 1FGL



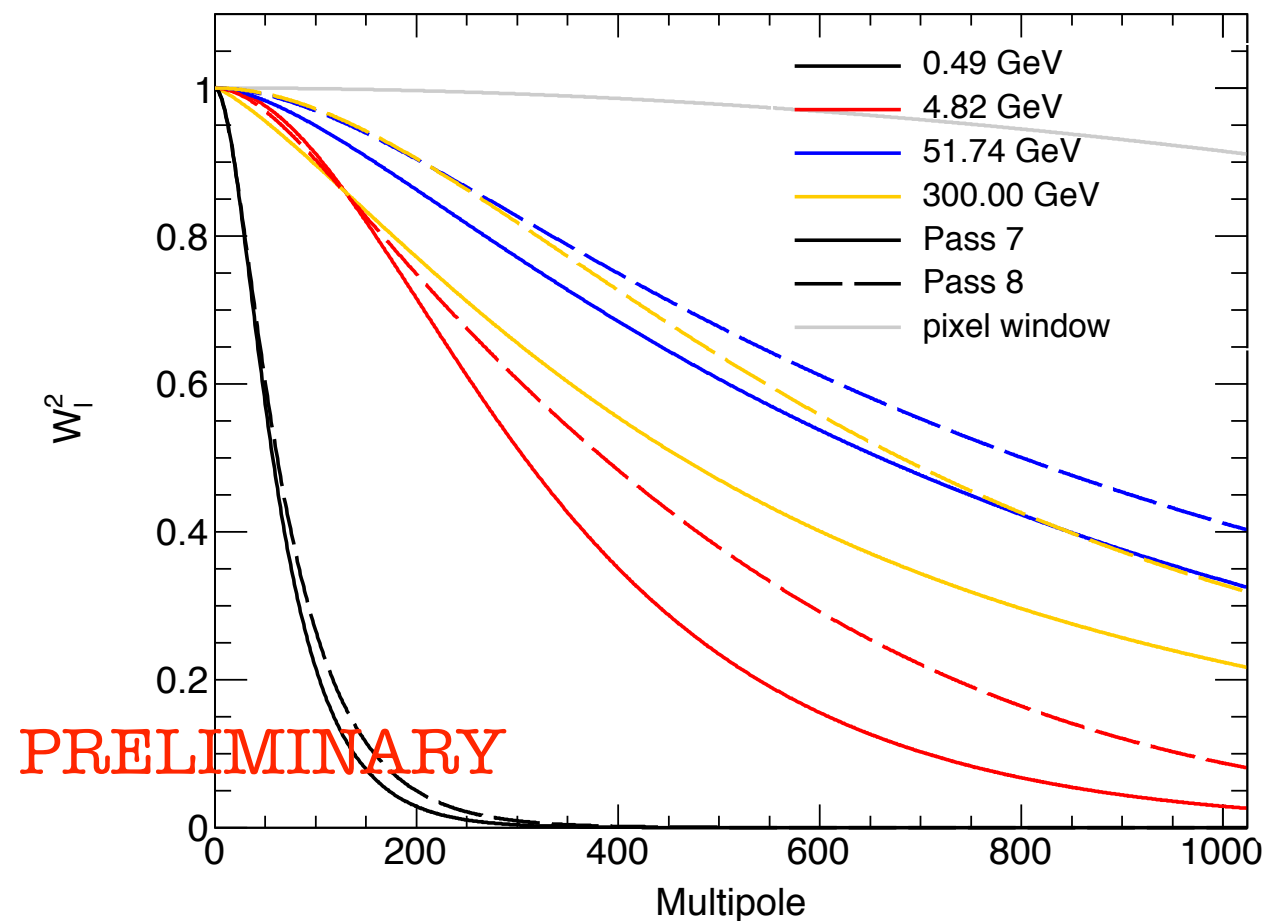
# APS estimator

$$C_{\ell}^{\text{signal},ij} = \frac{C_{\ell}^{\text{Pol},ij} - C_{\text{N}}}{(W_{\ell}^{\text{beam},i} W_{\ell}^{\text{beam},j}) (W_{\ell}^{\text{pix}})^2}$$

photon noise  
(inversely proportional to the  
number of detected photons)

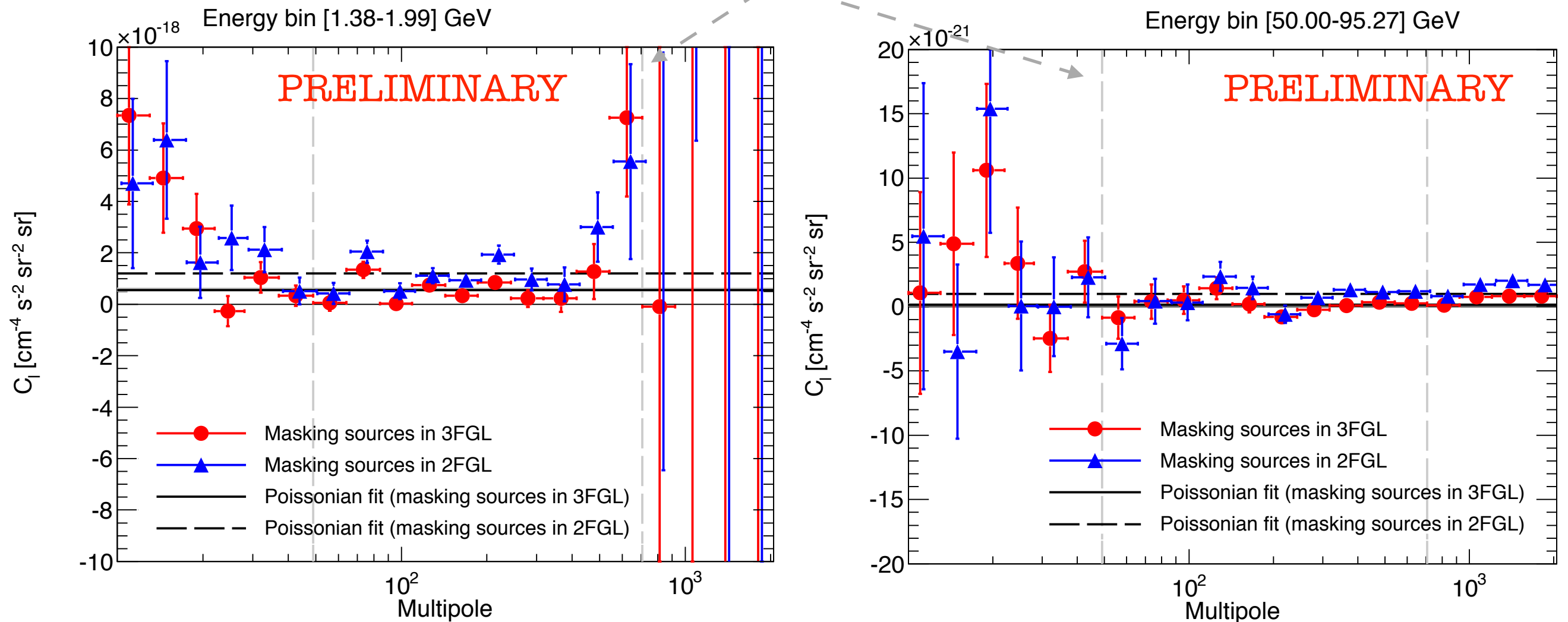
output of the decomposition in  
spherical harmonics (already  
corrected for the effect of the  
mask)

window beam function  
(it corrects for the  
experimental PSF)



# Binned APS measurement

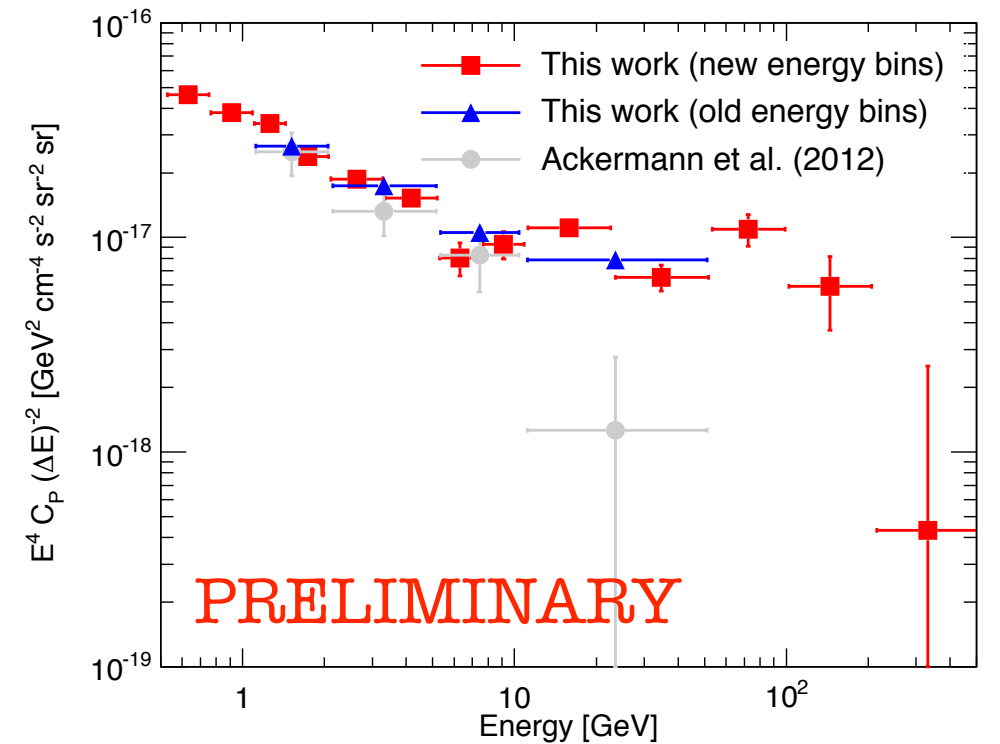
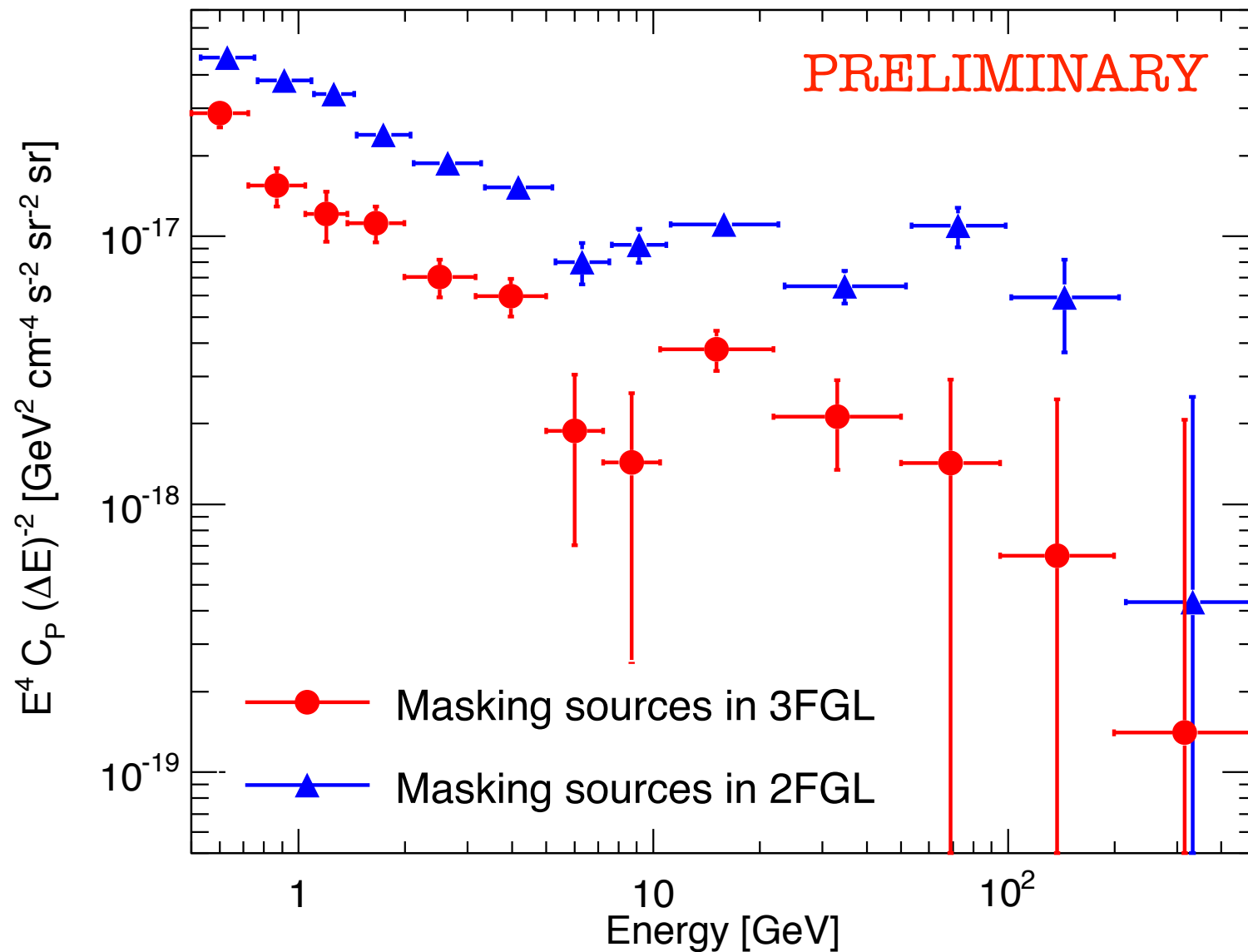
signal region between  $\ell=49$  and 706



- contamination of Galactic foreground at low  $\ell$  and effect of the beam window function at large  $\ell$
- fitting the data with a Poissonian APS:  $\chi^2/\text{dof} = 1.01$ ,  $p\text{-value}=0.61$
- fits with  $A(\ell/\ell_0)^\alpha$  and  $C_P + A(\ell/\ell_0)^\alpha$  have also been considered



# Anisotropy energy spectrum



$$I(\psi, E_i) = \sum_{\ell, m} a_{\ell, m}^i Y_{\ell, m}(\psi)$$

$$C_P^i = \sum_{\alpha} C_{iP, \alpha} = \sum_{\alpha} I_{\alpha}^2(E_i) \tilde{C}_{P, \alpha}$$

- anisotropy energy spectrum traces the intensity energy spectrum of sources
- features in the anisotropy energy spectrum hint at multiple components

# Cross-correlation APS

$$C_{\ell}^{ij} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} a_{\ell m}^i a_{\ell m}^{j*}$$

- 91 independent combination of en. bins: 91 Poissonian  $C_P^{i,j}$

- cross correction coefficients

$$C_P^{i,j} / \sqrt{C_P^{i,i} C_P^{j,j}}$$

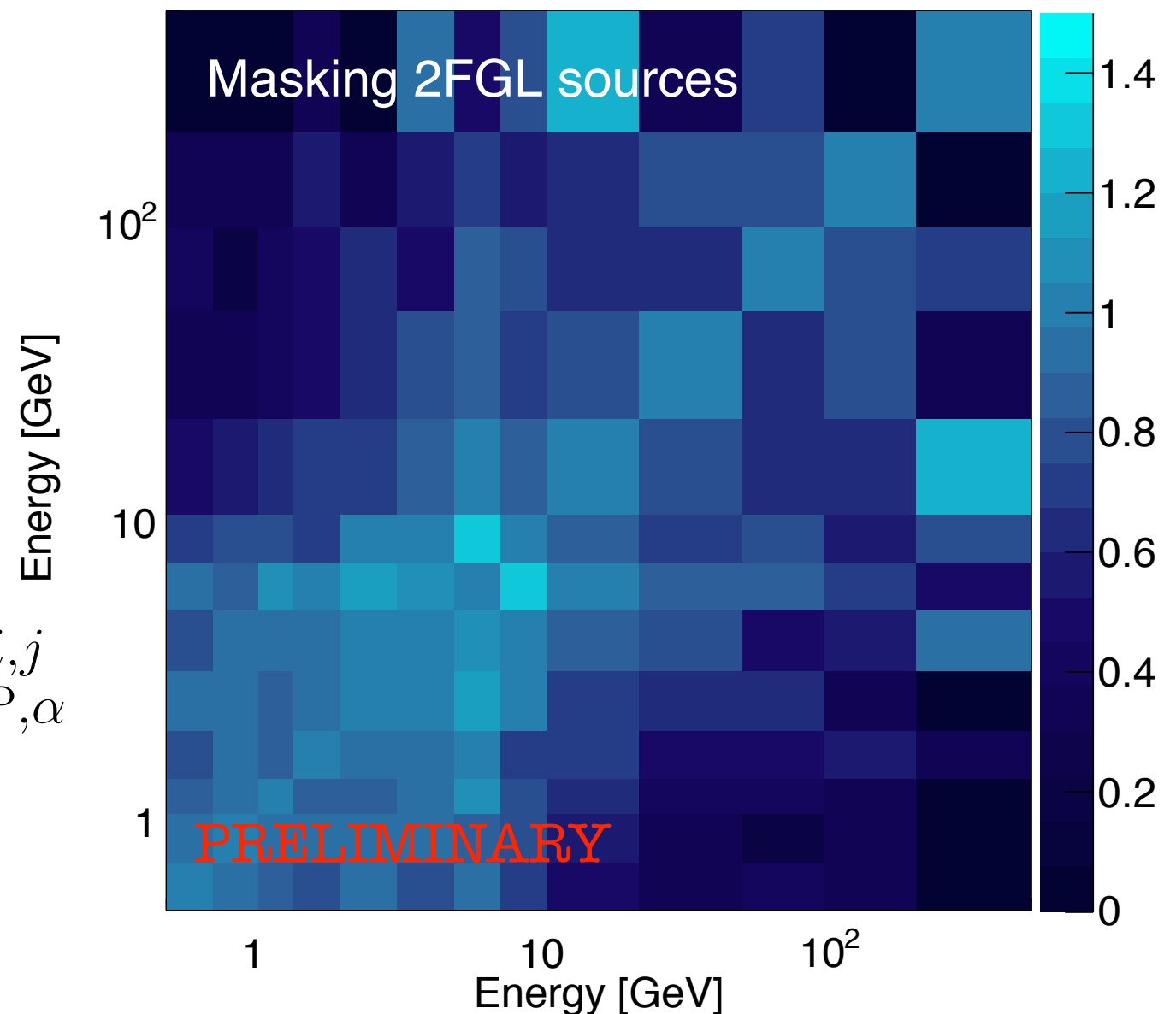
- one source class:

$$C_P^{i,j} = I(E_i) I(E_j) \tilde{C}_P$$

- multiple source classes:

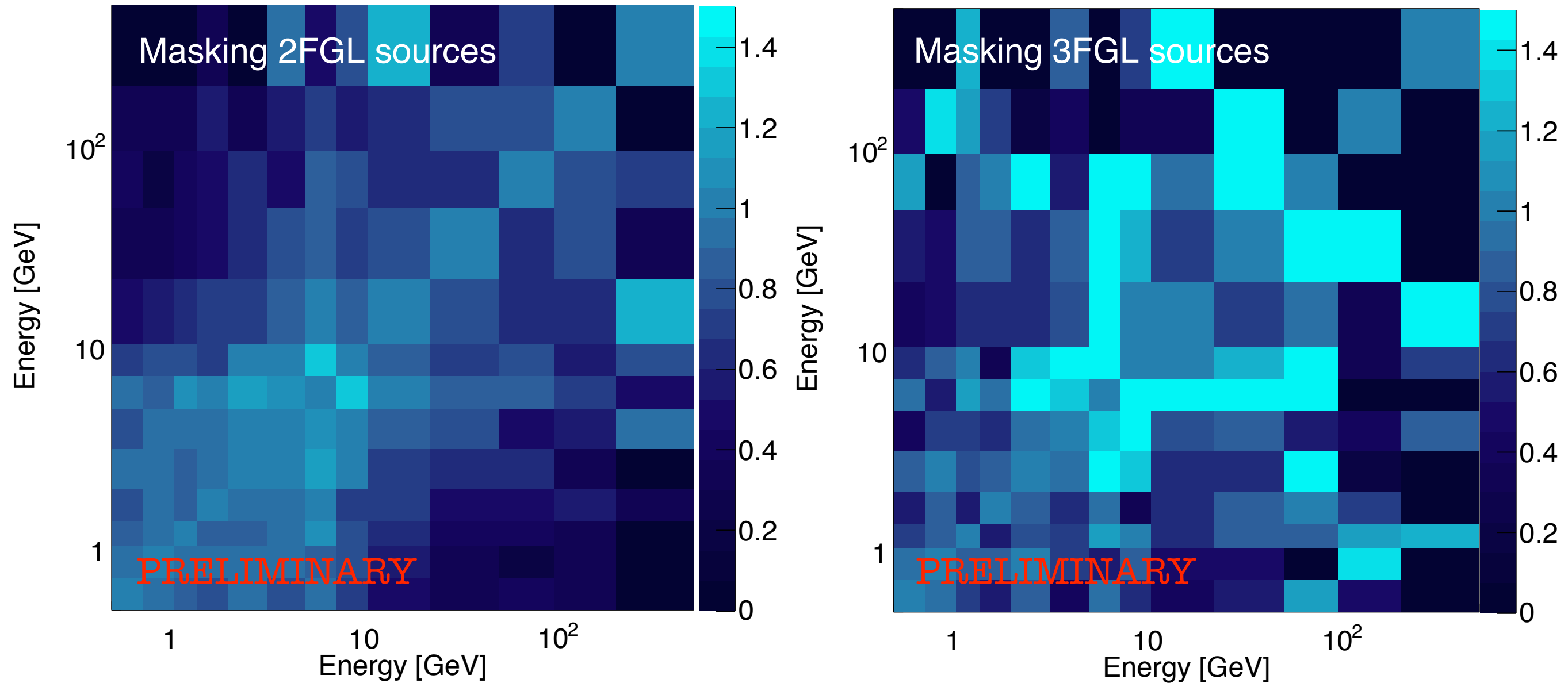
$$C_P^{i,j} = \sum_{\alpha} C_{P,\alpha}^{i,j} = \sum_{\alpha} I(E_i) I(E_j) \tilde{C}_{P,\alpha}^{i,j}$$

- cross-correlation coefficients different than 1.0 hint at multiple components





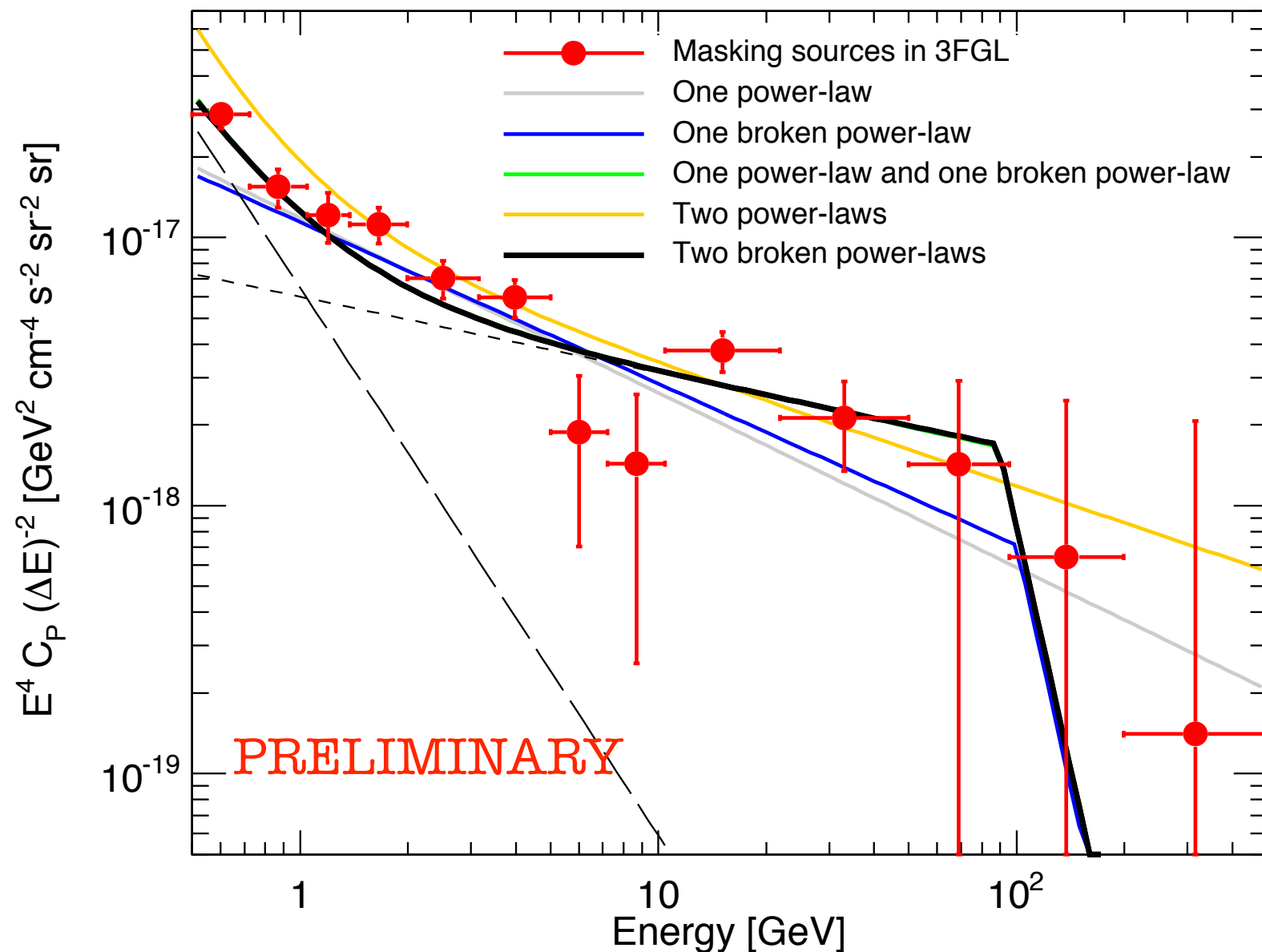
# Cross-correlation APS



# Interpretation in terms of multiple populations

Fitting the data with one or more populations, assuming specific energy spectra:

$$I(E) \propto E^{-\alpha} \quad I(E) \propto \begin{cases} (E/E_0)^{-\alpha} & \text{if } E \leq E_b \\ (E_0/E_b)^{-\alpha+\beta} (E/E_0)^{-\beta} & \text{otherwise} \end{cases}$$



Best-fit model has two contributions both emitting as broken power laws:

- $E_b = (88.9_{-14.4}^{+9.6})$  GeV,  
 $\alpha = 2.15 \pm 0.05$ ,  $\beta > 3.9$
- $E_b > 79$  GeV,  
 $\alpha = 3.0_{-0.2}^{+0.3}$ ,  
 $\beta = 0.88_{-0.15}^{+0.09}$

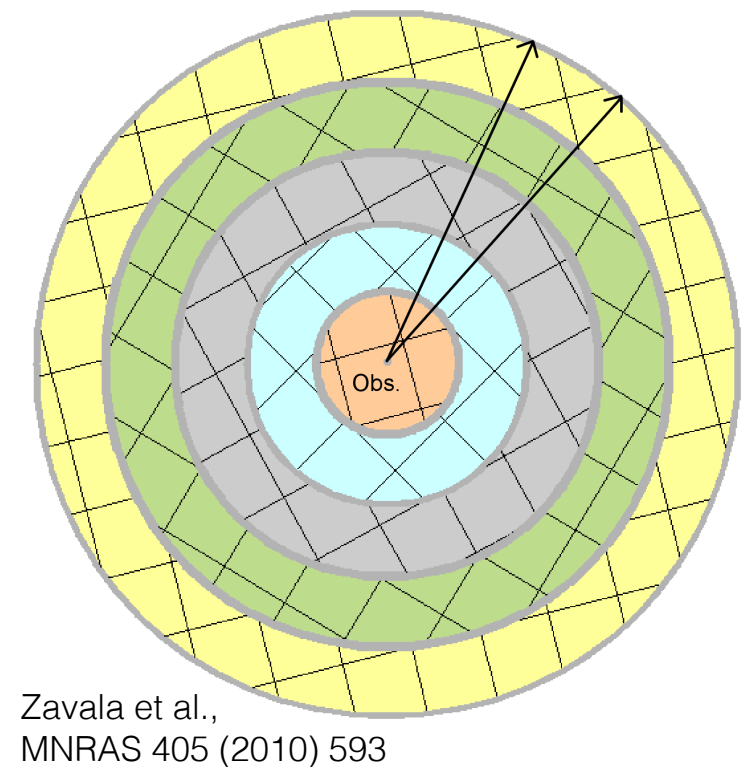
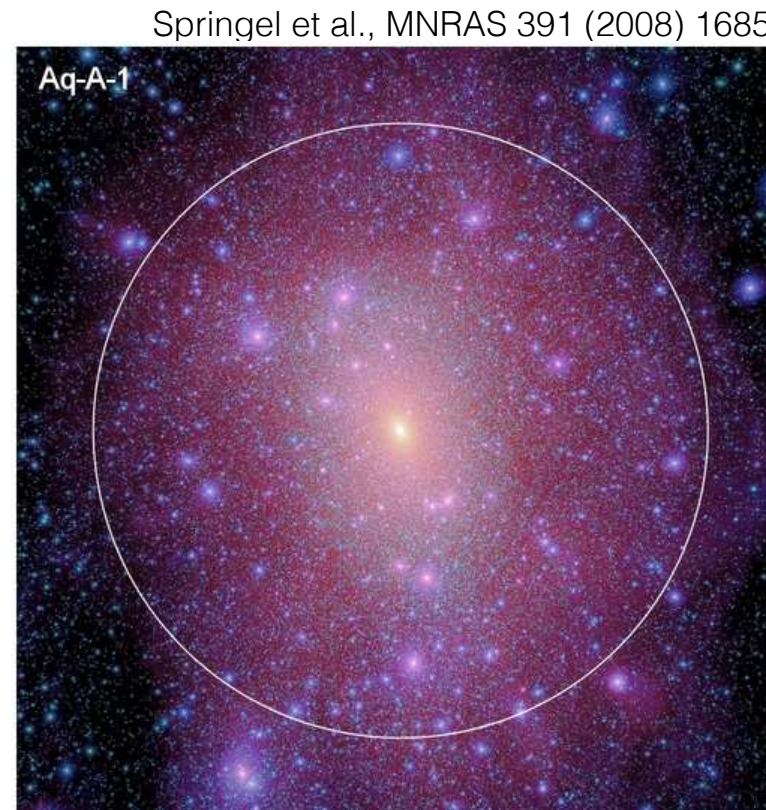
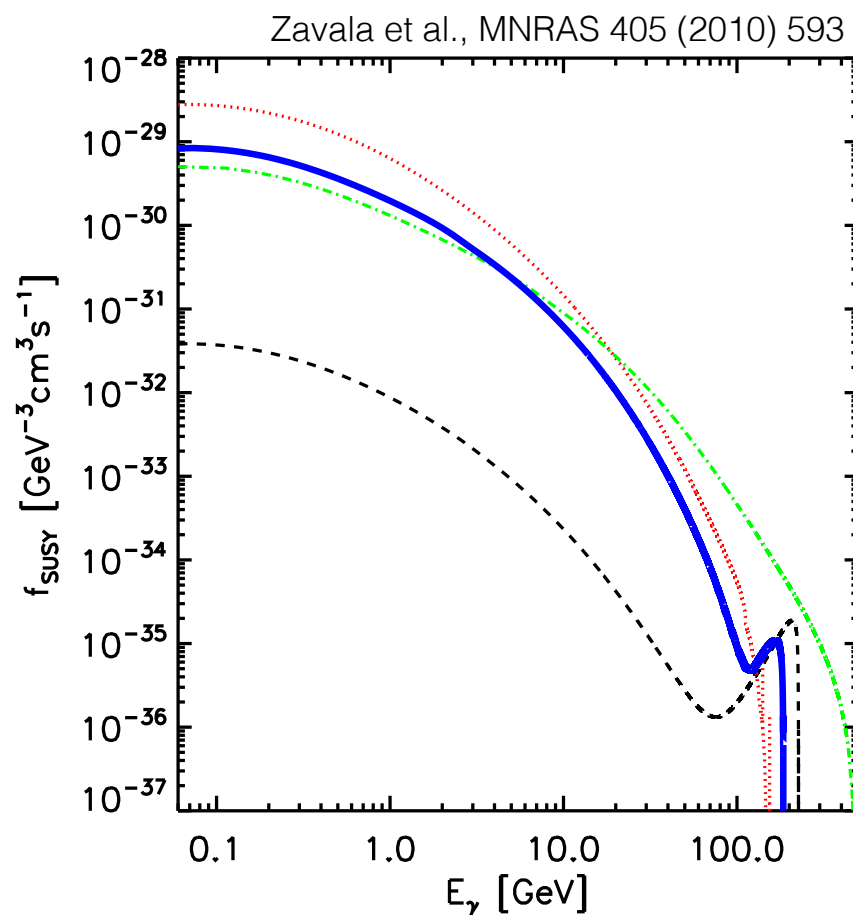
$$\chi^2/\text{dof} = 1.21, \text{ } p\text{-value} = 0.16$$



# Gamma-ray emission induced by Dark Matter (DM)

$$\frac{d\Phi}{dE}(E_\gamma, \Psi) = \frac{(\sigma_{ann} v)}{8\pi m_\chi^2} \int_{l.o.s} d\lambda \sum_i B_i \frac{dN_\gamma^i(E_\gamma(1+z))}{dE} \rho^2(\lambda(z), \Psi) e^{-\tau_{EBL}(z, E_\gamma)}$$

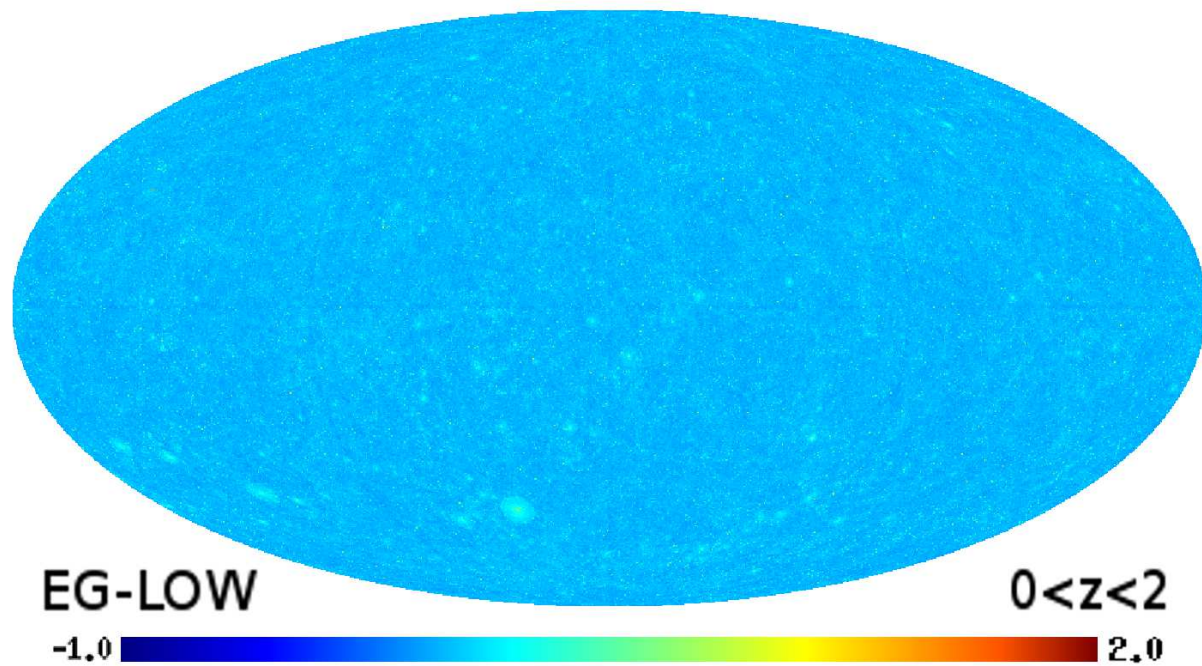
- photon yield: prompt emission, Inverse Compton and hadronic emission
- distribution and shape of DM halos inferred from  $N$ -body simulations
- couple  $N$ -body simulations to analytical recipes in order to estimate emission below their mass resolution (hybrid method)



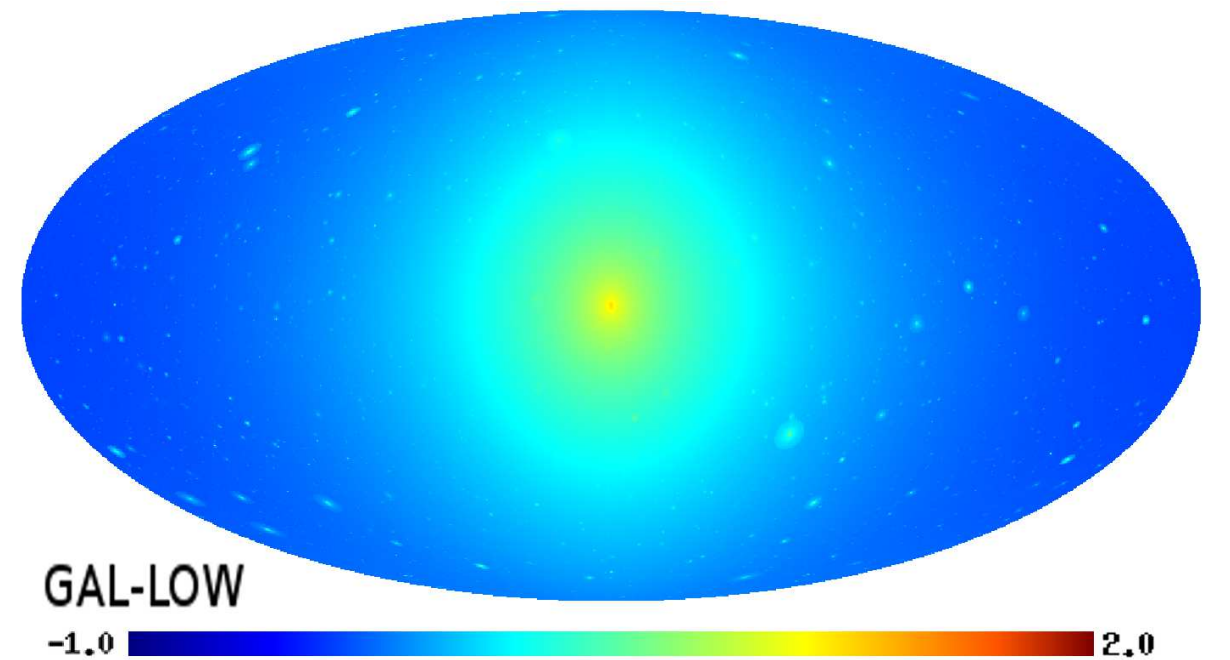
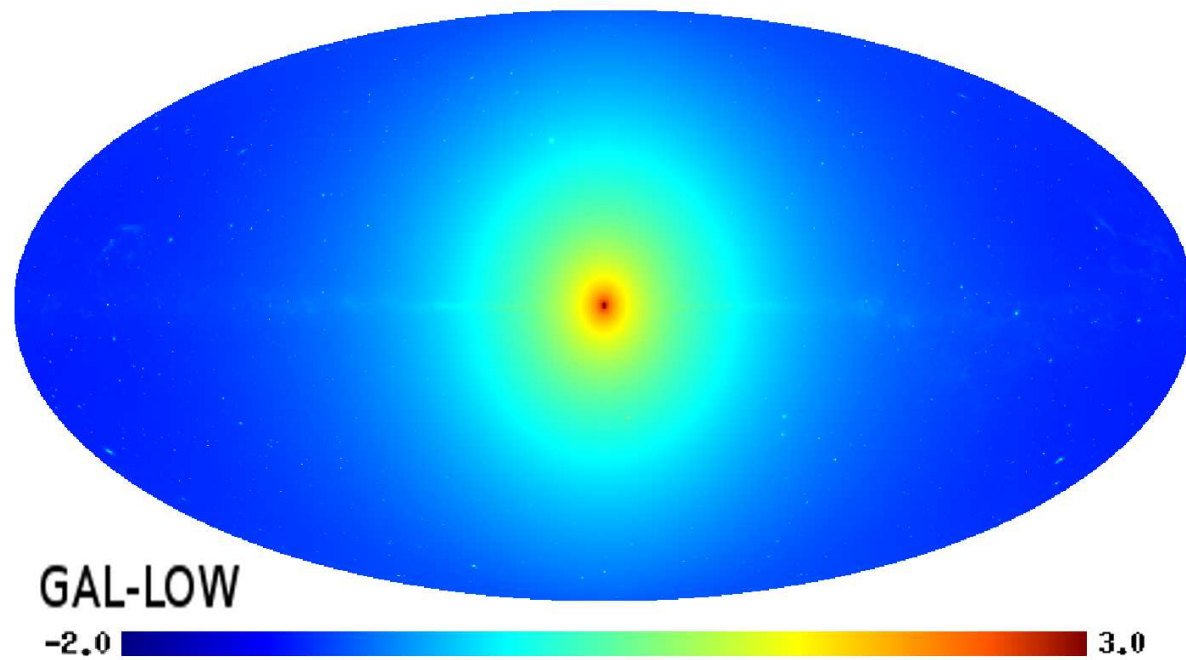
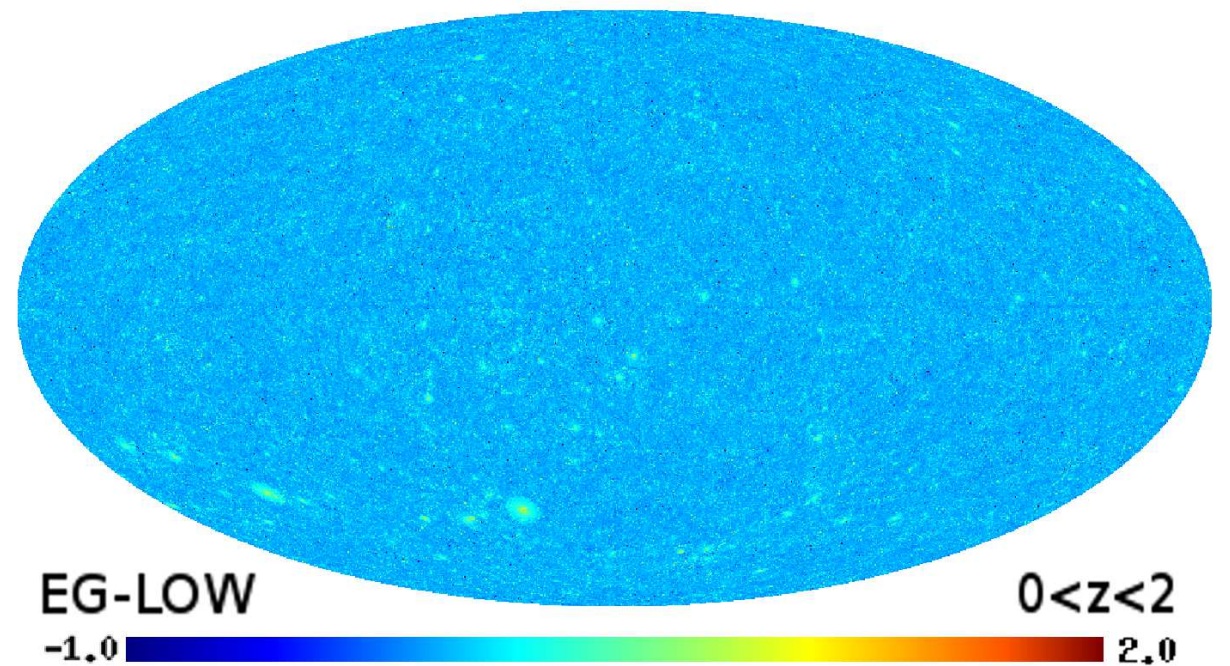


# Gamma-ray anisotropies from Dark Matter

Annihilation



Decay

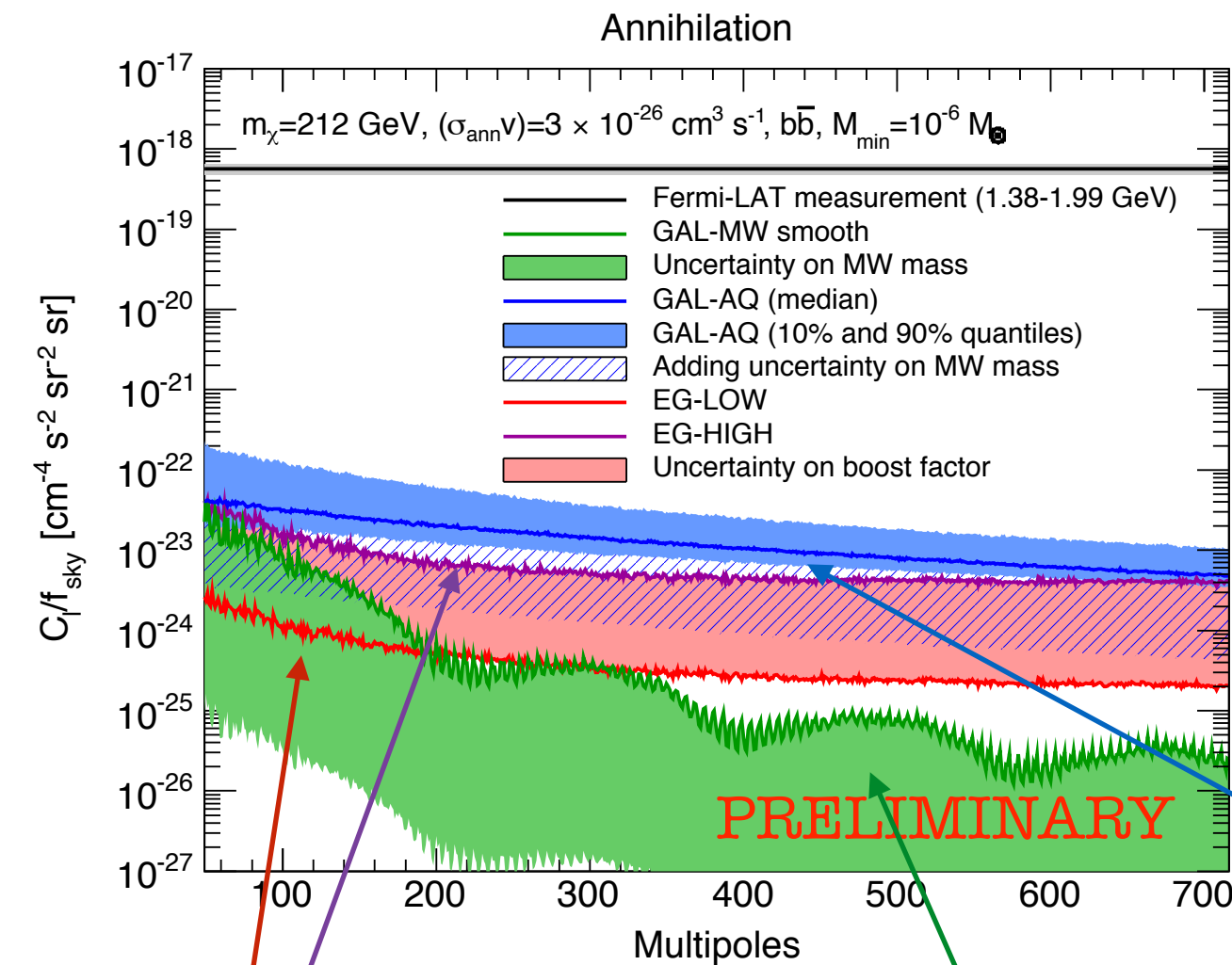


$E=4$  GeV,  $M_{\min}=10^{-6} M_{\odot}$ ,  $b$  quarks

$m_{\chi}=200$  GeV,  $\sigma v=3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$  (annihilation),  $m_{\chi}=2$  TeV,  $\tau=2 \times 10^{27}$  s (decay)

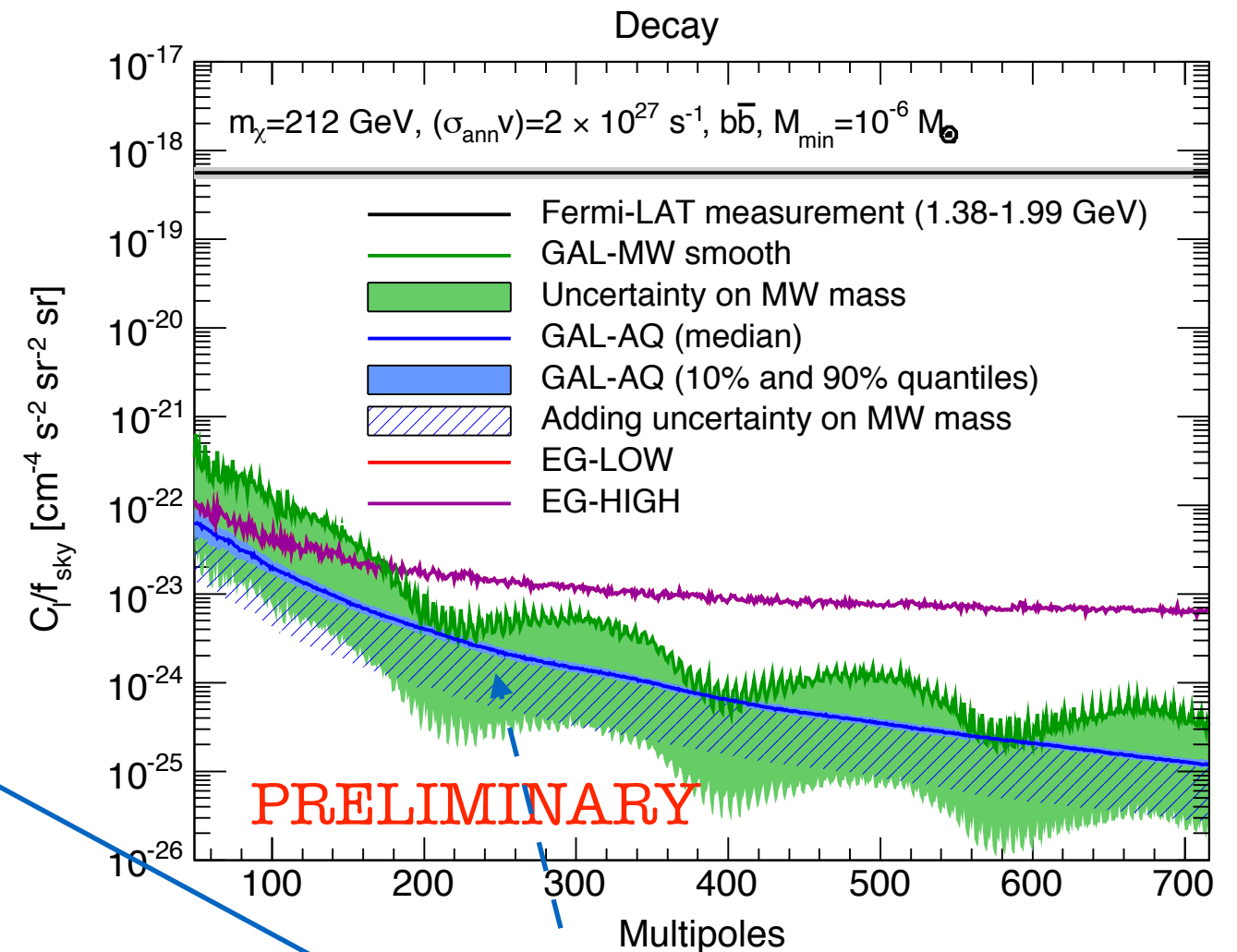


# DM-induced APS



Extragalactic component with different subhalo boost factors

Smooth halo of the Milky Way (outside of the mask) with uncertainty on the total Milky-Way mass



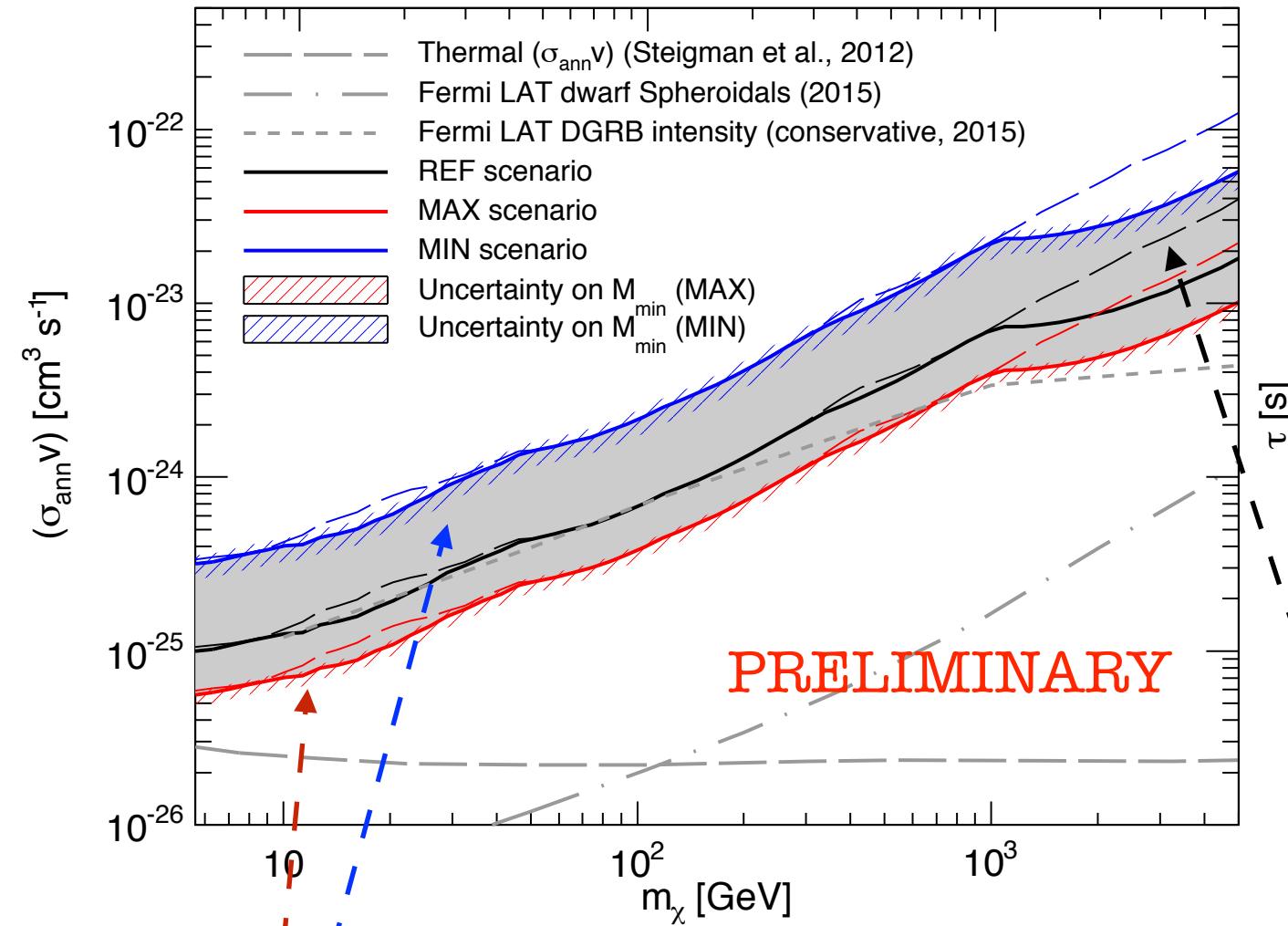
Subhalos of the Milky Way with uncertainty on the position of the Earth

uncertainty on the total mass of the Milky Way

# Conservative exclusion limits

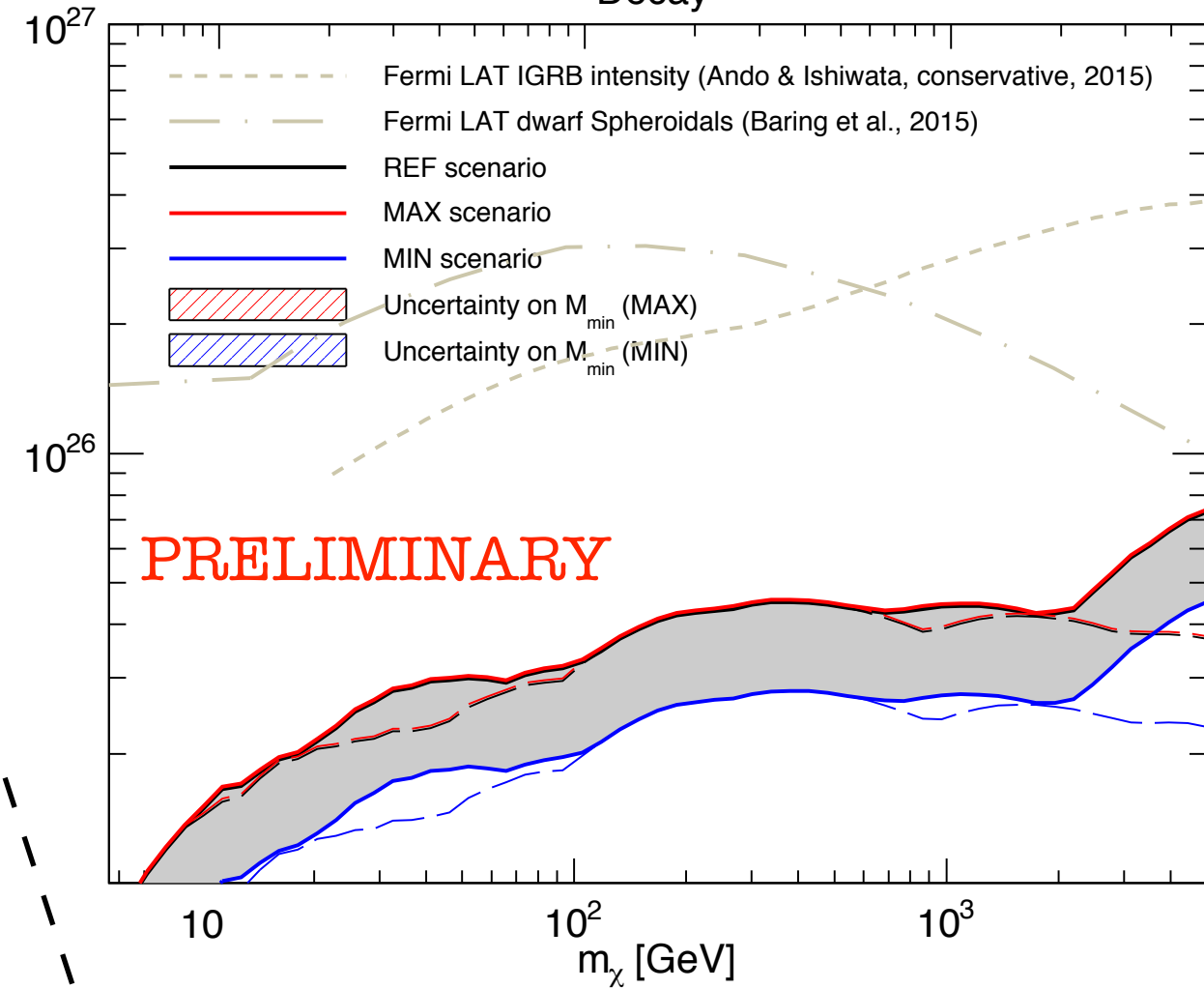
$$\langle C_{\ell, \text{DM}}^{i,j} \rangle < C_P^{i,j} + 1.64 \sigma_{C_P^{i,j}}$$

Annihilation



Uncertainty on the value of  $M_{\text{min}}$

Decay

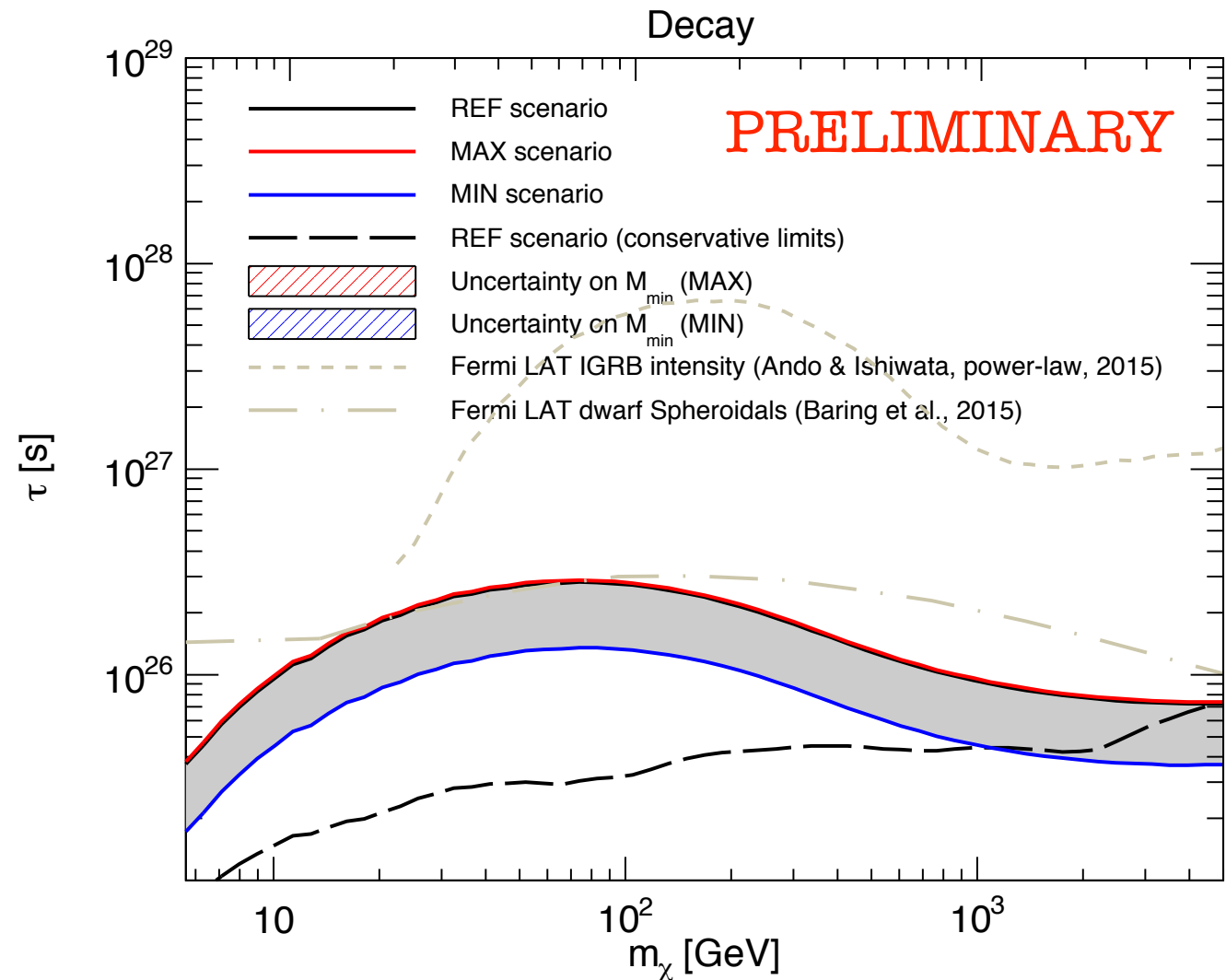
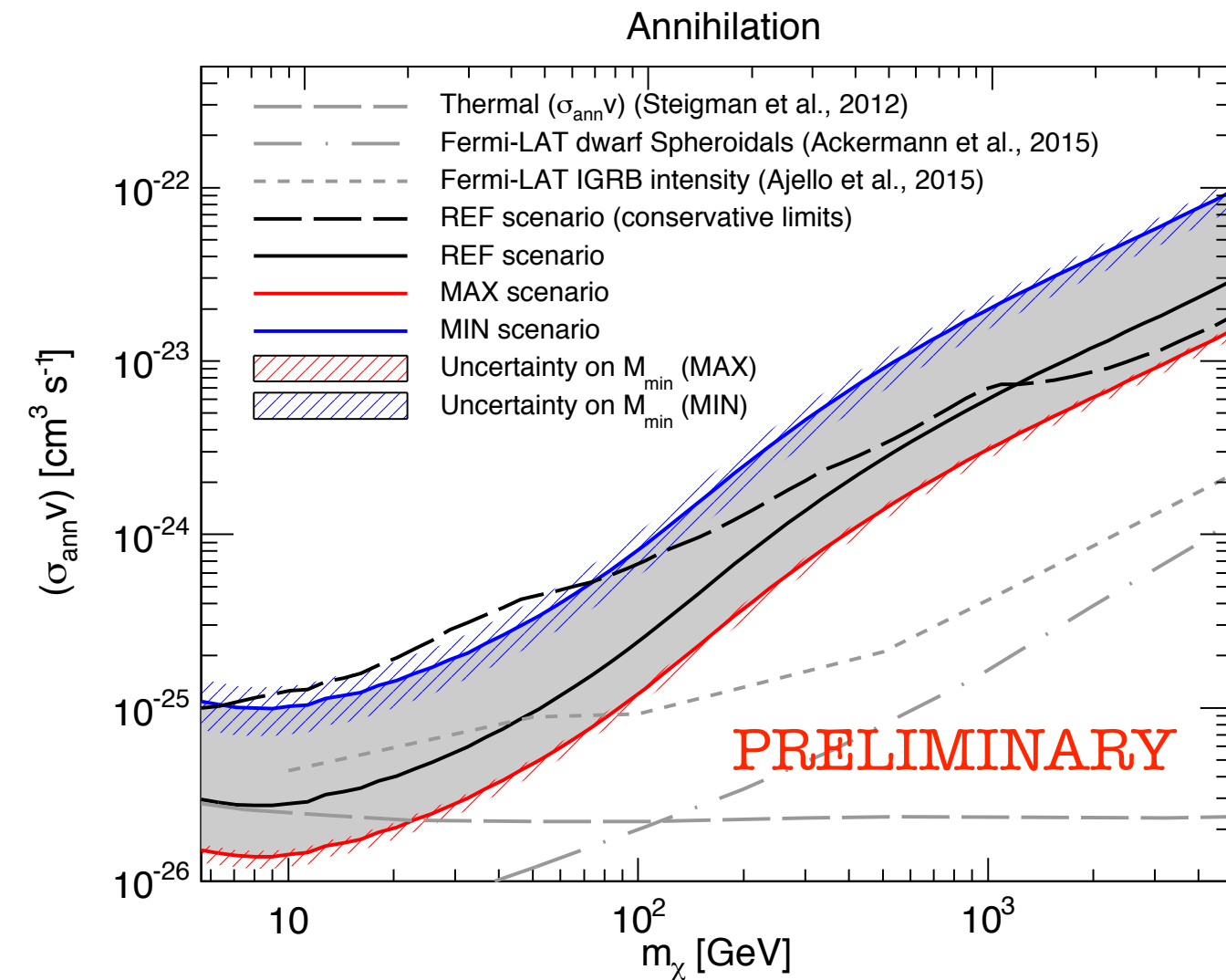


How the exclusion limits would look like if only the auto-correlation were used

# 2-component fit to the binned APS

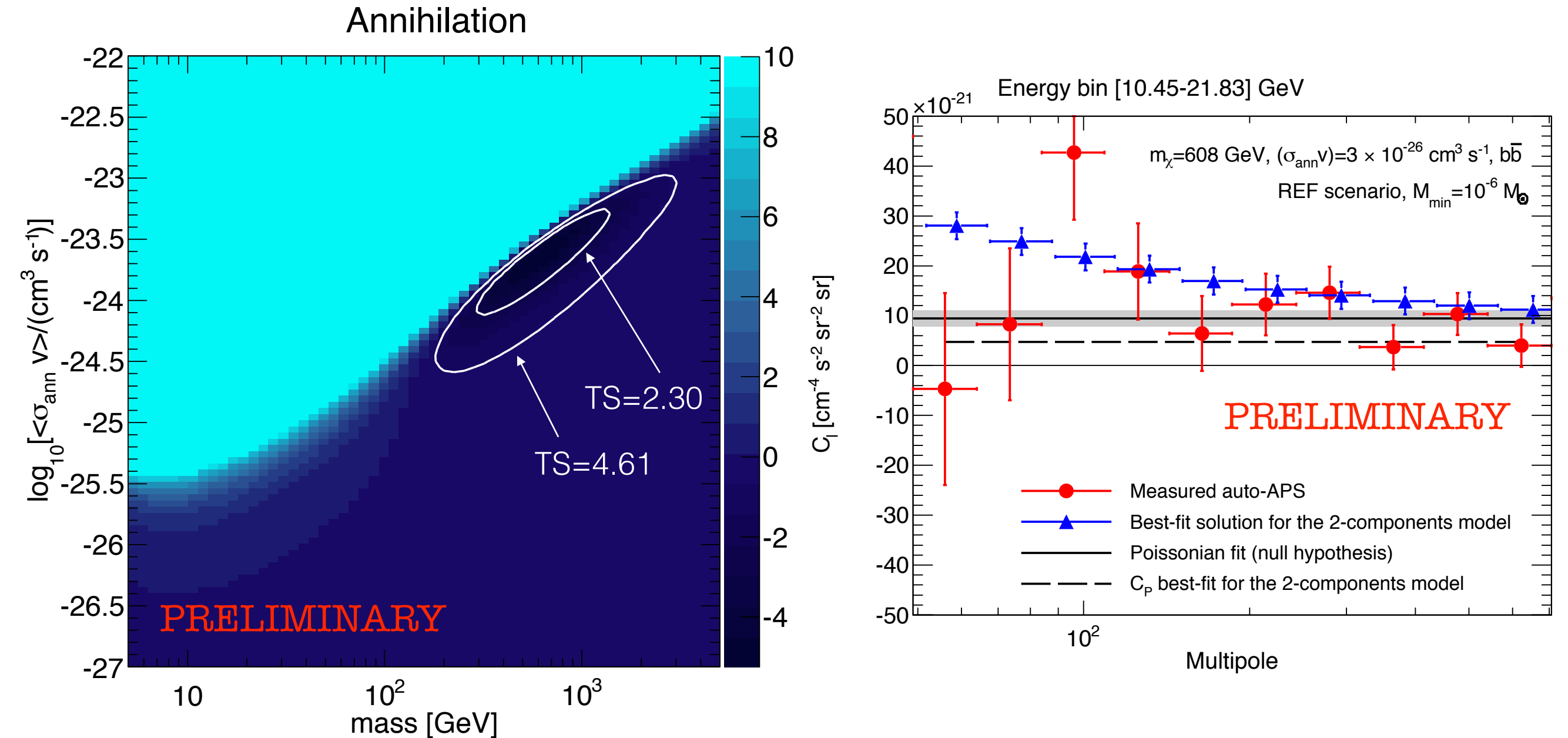
$$\chi^2 = - \sum_{i,j,\ell} \frac{[C_\ell^{i,j} - C_{\ell,\text{DM}}^{i,j} - C_{\text{P}}^{i,j}]^2}{\sigma_{C_\ell^{i,j}}^2}$$

95% CL exclusion limit when Test Statistics  $\Delta\chi^2=3.84$



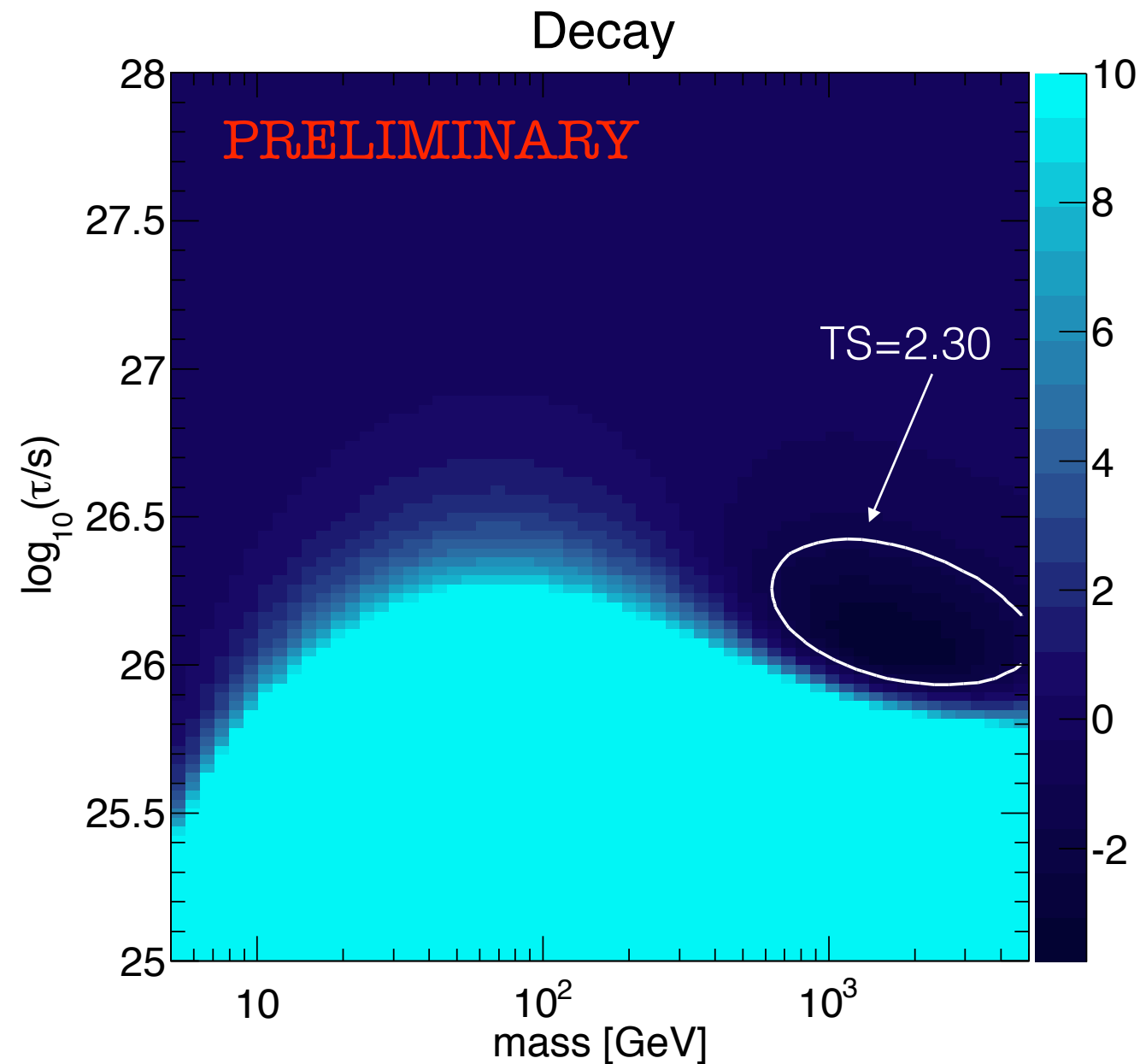


# 2-component fit to the binned APS



- $\text{TS} = -2 \ln[\chi^2(\text{no DM})] + 2 \ln[\chi^2(m_\chi, \sigma v)]$
- best-fit solution has  $\text{TS}=-4.5$ ,  $m_\chi=607$  GeV,  $(\sigma_{\text{ann}} v)=2.2 \times 10^{-24} \text{ cm}^3 \text{s}^{-1}$

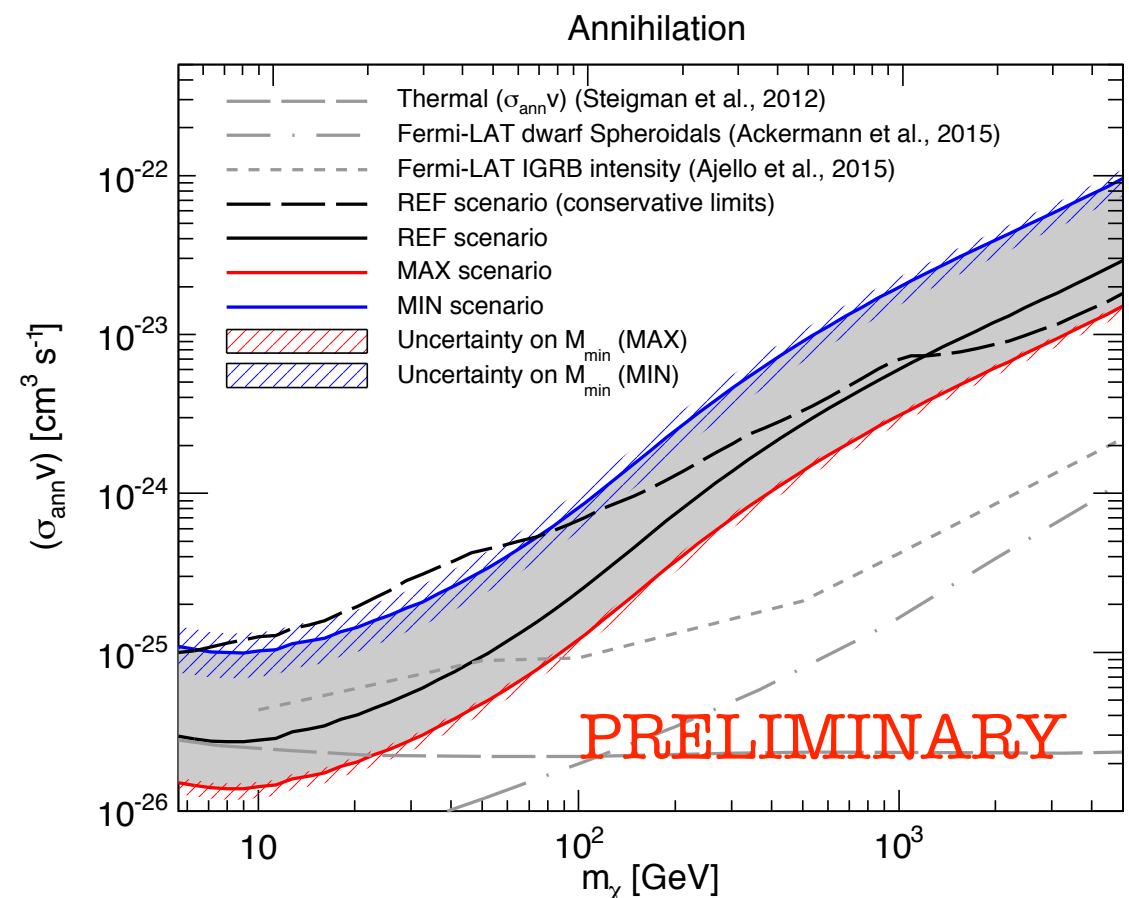
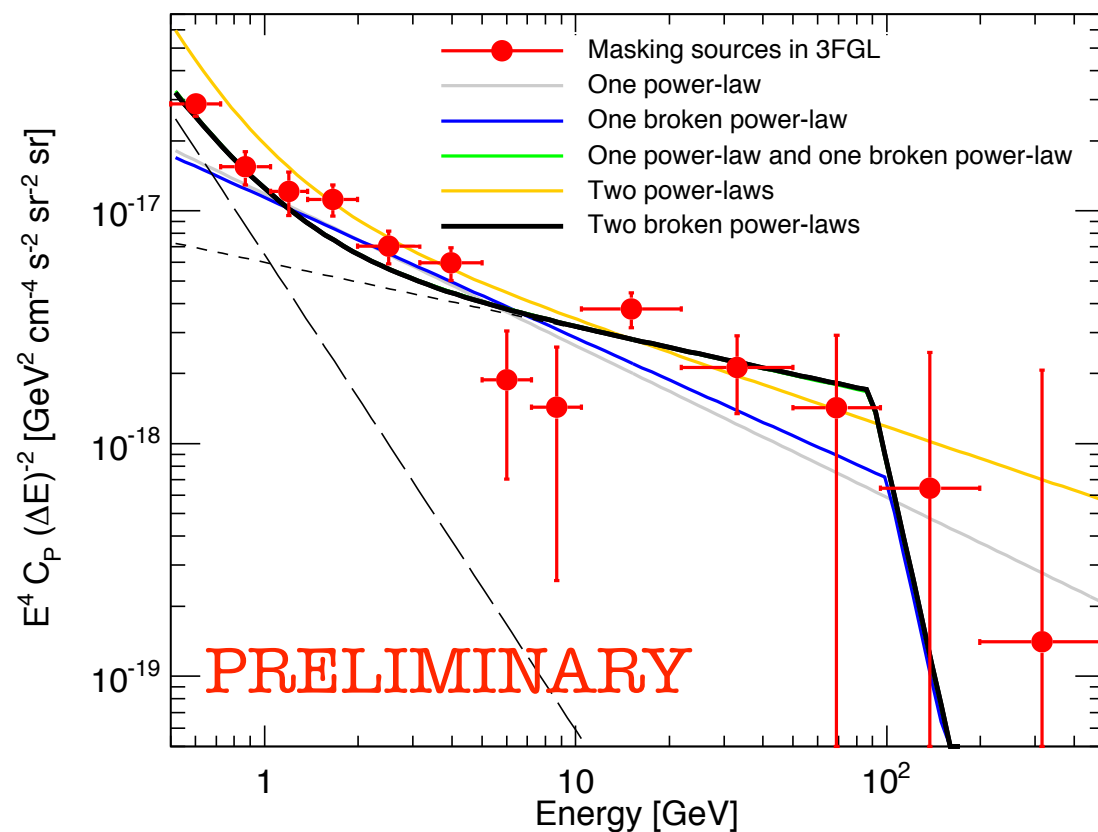
# 2-component fit to the binned APS



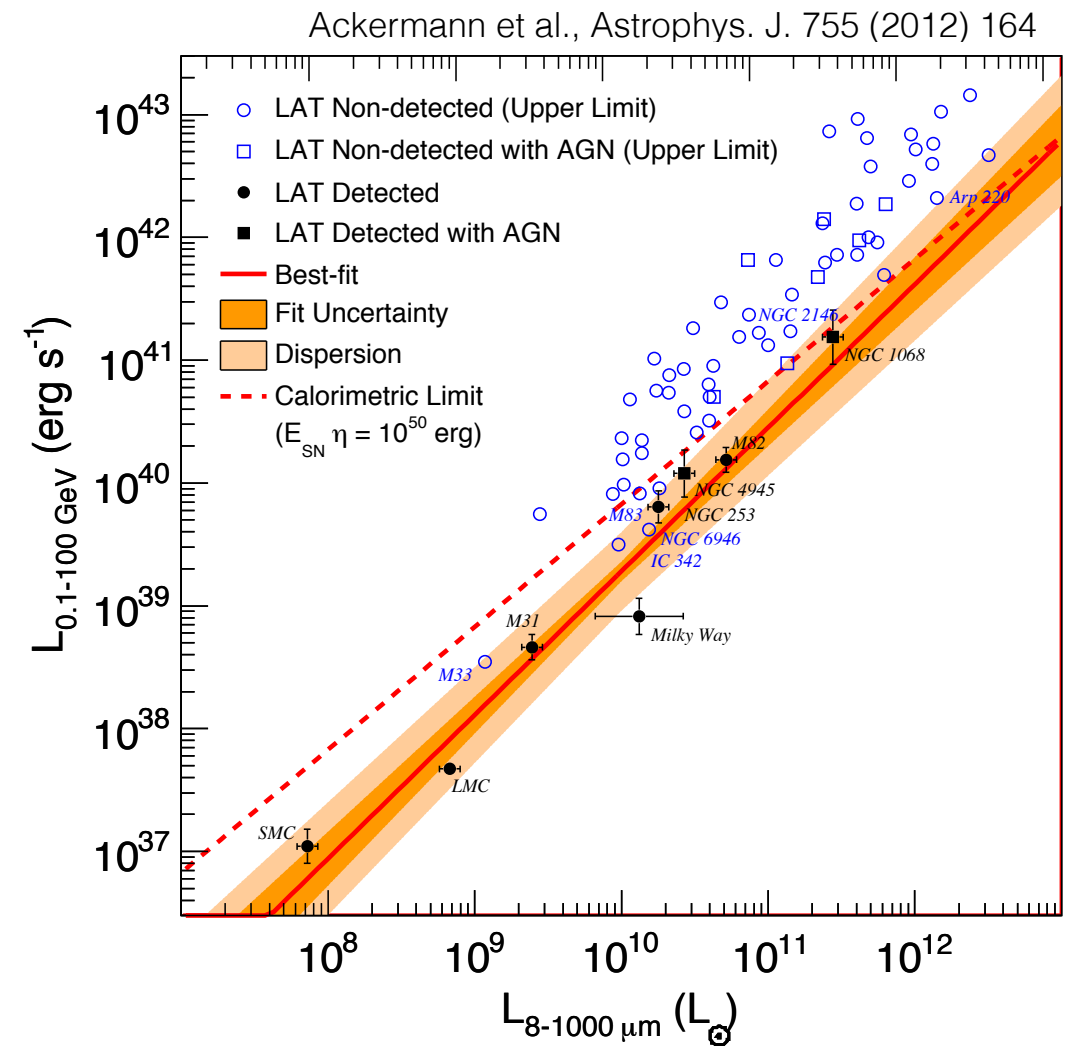
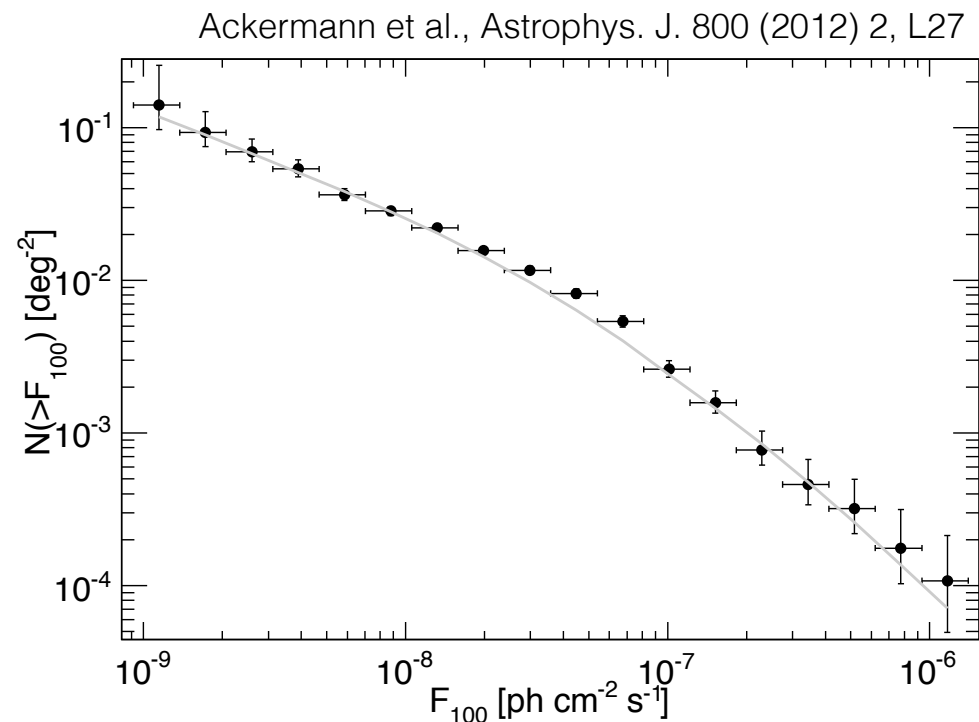
best-fit solution has  $m_\chi = 1743$  GeV,  $\tau = 1.2 \times 10^{26}$  s

# Conclusions

- new measurement of anisotropy angular power spectrum
- possibly two distinct population of sources are responsible for the signal
- constraints on additional components can be derived
- combination with cross-correlation with other tracers of Large Scale Structures and with other messengers (neutrinos)



# Estimating the emission of unresolved sources



- abundant sources: number of detected objects as a function of their flux
- rare sources (in gamma rays): measure correlation with other frequencies (IR for star-forming galaxies, radio for misaligned AGNs)



# How to bin the APS

- produce 100 Monte Carlo realisations of the gamma-ray sky with a fixed nominal  $C_P$
- PolSpice computes  $C_\ell$  and estimates errors and covariances
- analytical expression for the error is

$$\sigma_\ell = \sqrt{2/(2\ell + 1)} \left( C_\ell + \frac{C_N}{W_\ell^2} \right)$$

- to bin  $C_\ell$  in one multipole bin, you can compute:
  - A. unweighted average**
  - B. weighted average with weight =  $1/\sigma_\ell$
  - C. weighted average with weight =  $1/\sigma_\ell$  and only photon noise
- Monte Carlo simulations prove that method B underestimates the APS
- method B was used in Ackermann et al. (2012)

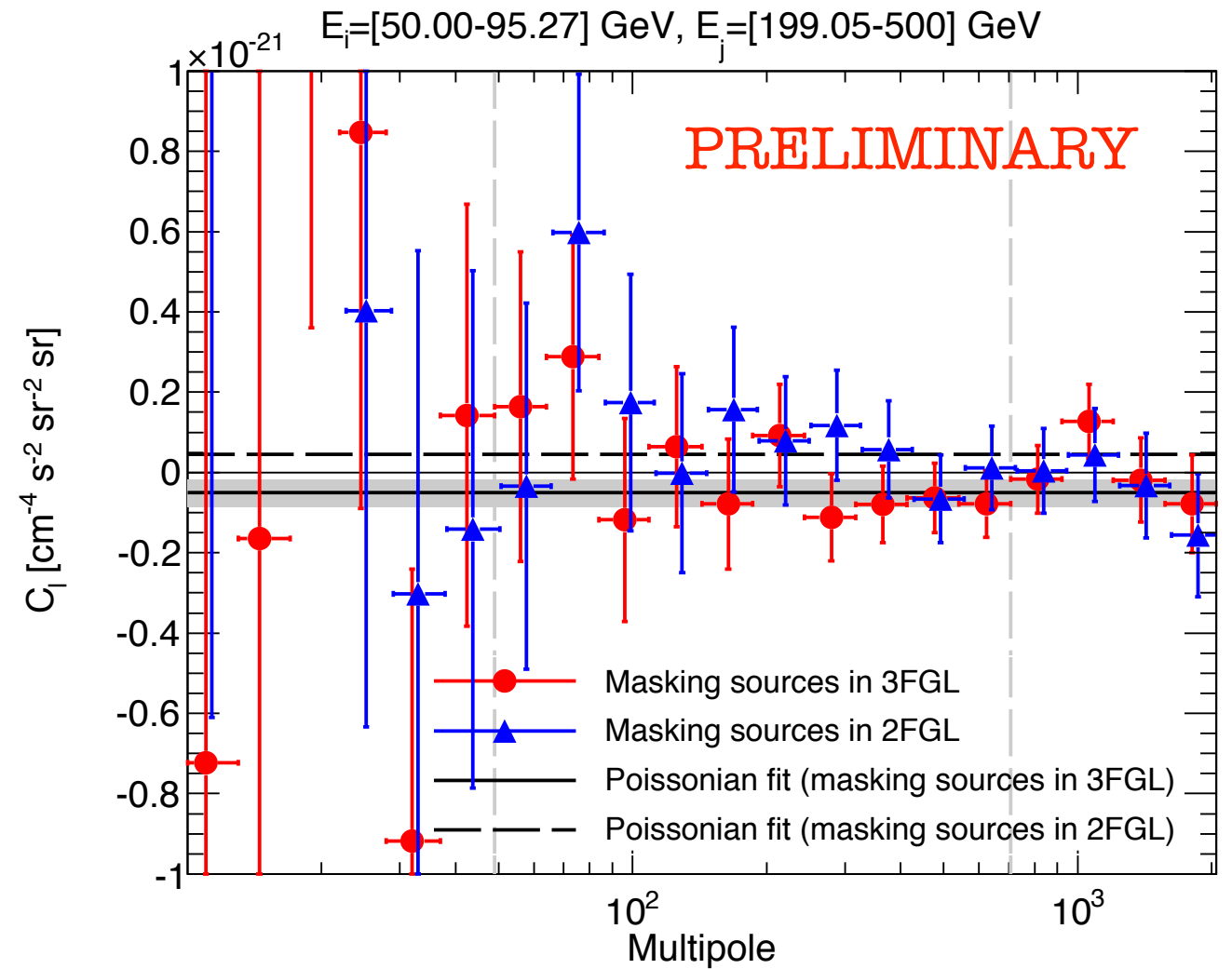
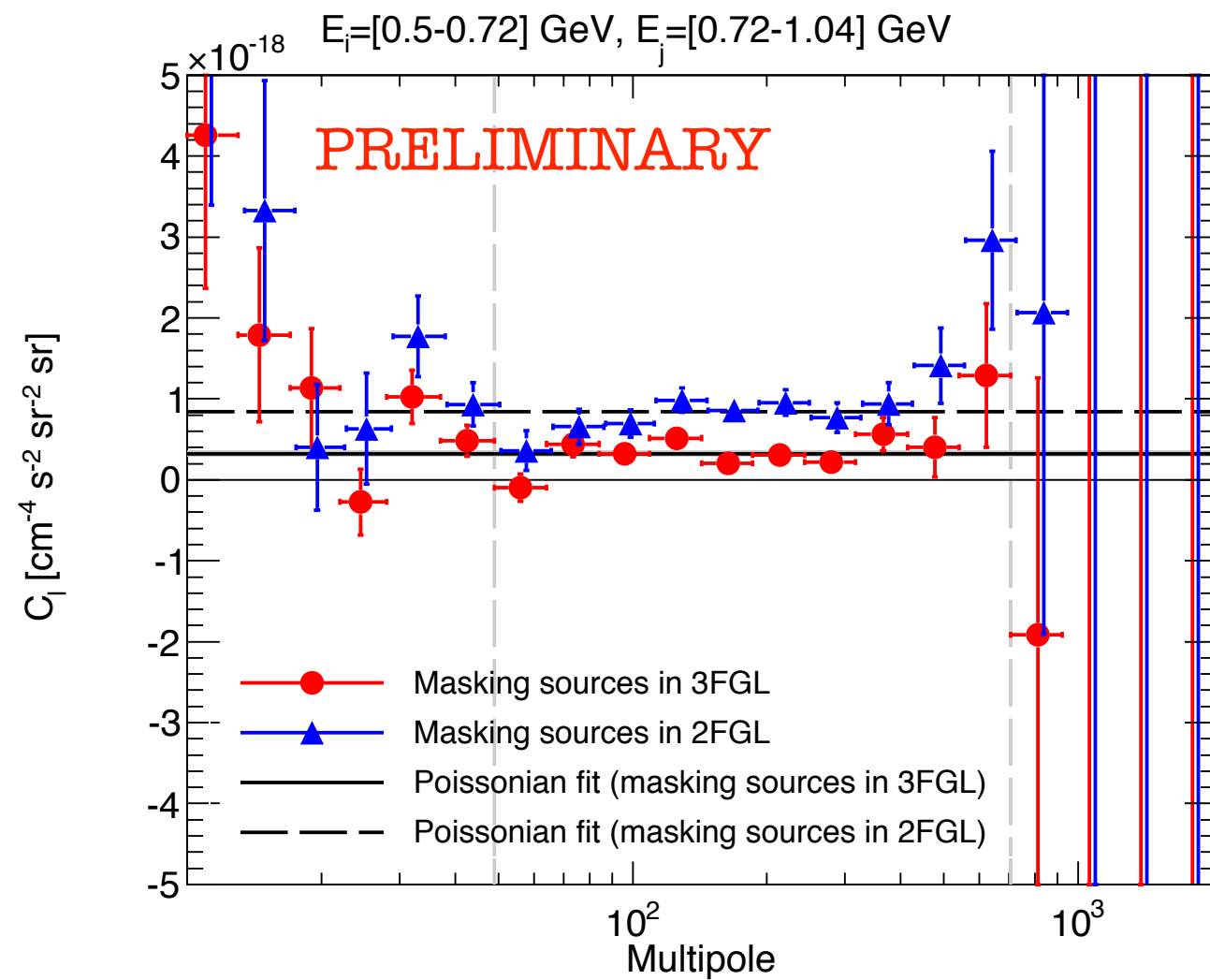
# How to estimated the error of the binned APS

- method A: average of the analytical expression for the error  $\sigma_\ell$

$$\sigma_\ell = \sqrt{2/(2\ell + 1)} \left( C_\ell + \frac{C_N}{W_\ell^2} \right)$$

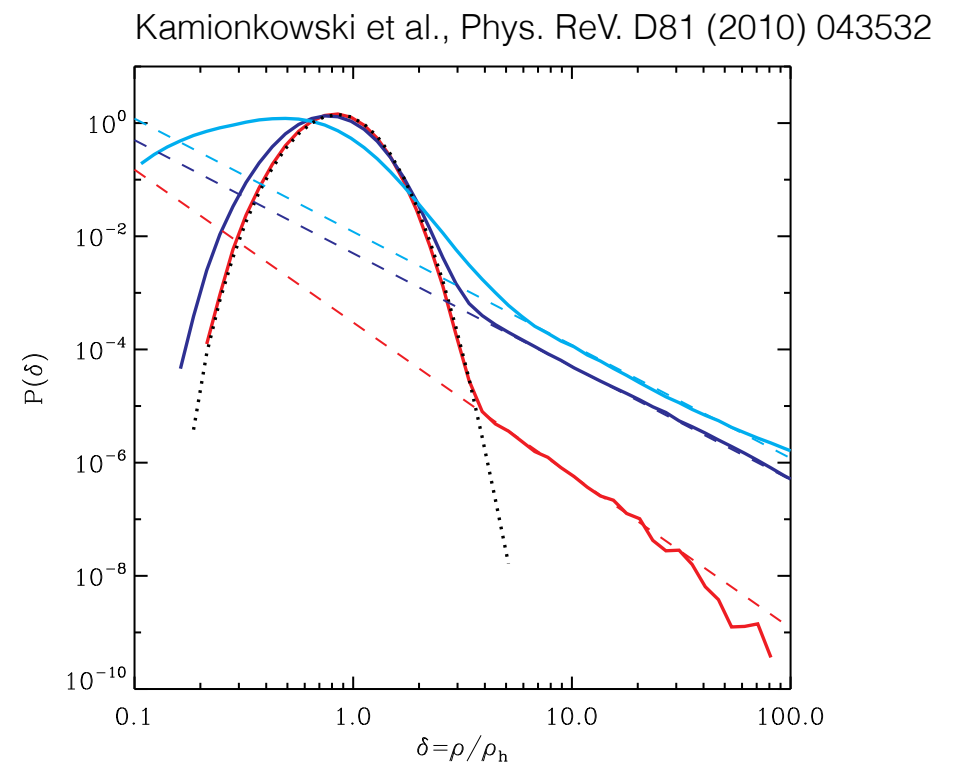
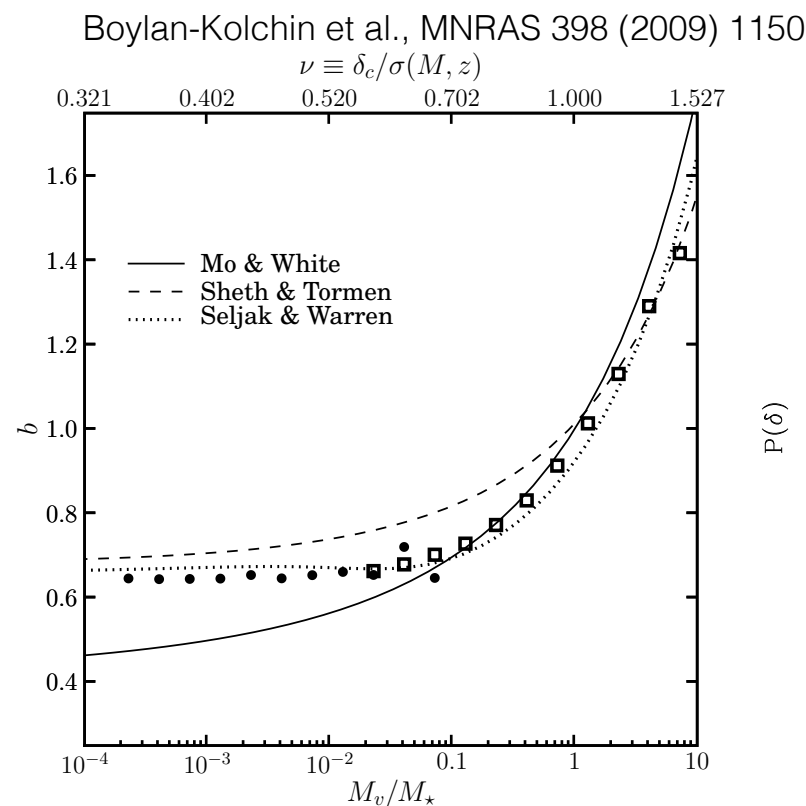
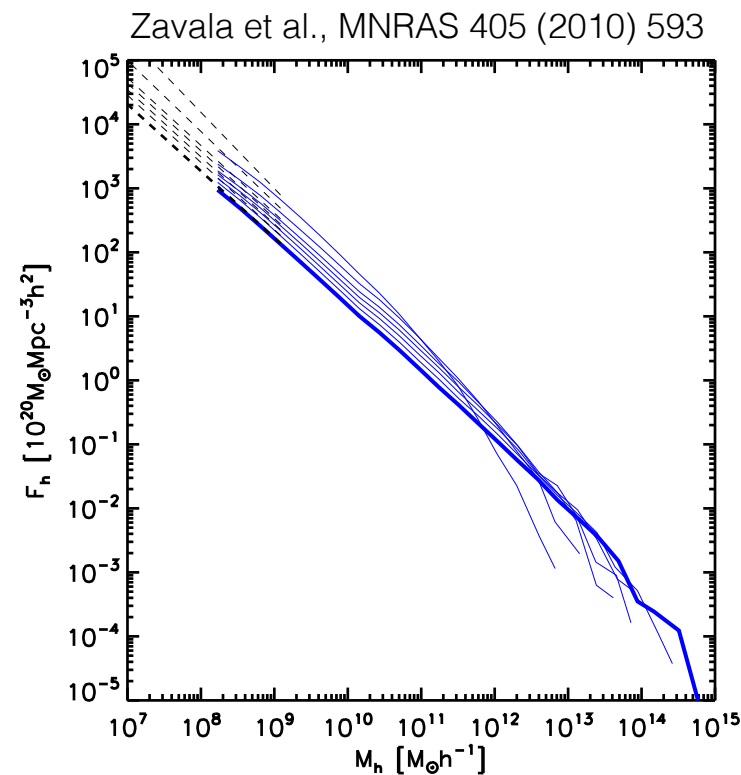
- method B: average of the variances and covariances computed by PolSpice
- the two methods agree
- the estimated error describes well the distribution of the binned  $C_\ell$  from the 100 Monte Carlo realisations

# Cross-correlation



# DM-induced emission

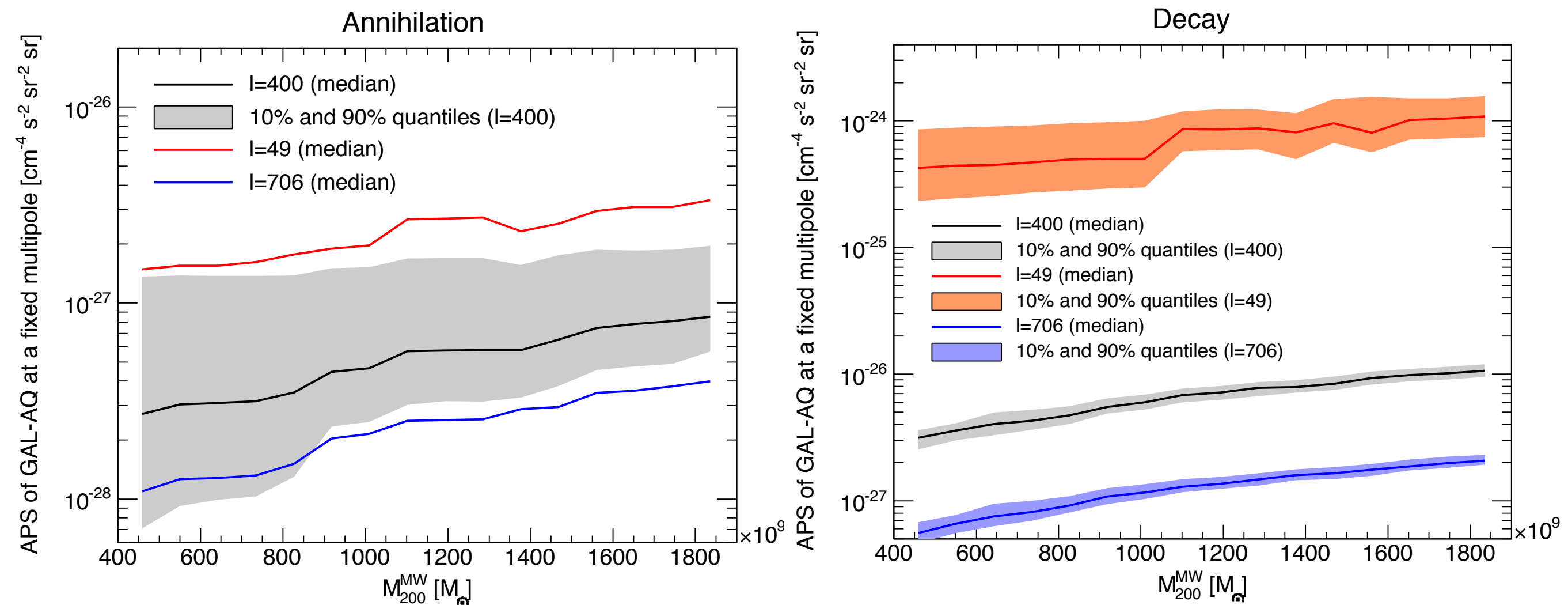
- repetition of the Millennium-II simulation box to cover a large portion of the Universe
- extrapolation below the mass resolution of the Millennium-II (assuming low-mass halos trace the smallest halos in Millennium-II)
- unresolved subhalos accounted for through an analytic fit to  $P(\rho, r)$
- Milky Way smooth halo and Galactic subhalos from Aquarius (carved in the centre)





# Effect of an uncertain MW mass on GAL-AQ

- uncertainty of a factor 4 on the mass of the Milky Way (MW)
- 16 bins in  $M_{\text{MW}}$  accounting for a correspondent depletion in the amount of Galactic subhalos
- including uncertainty on the position of the observer

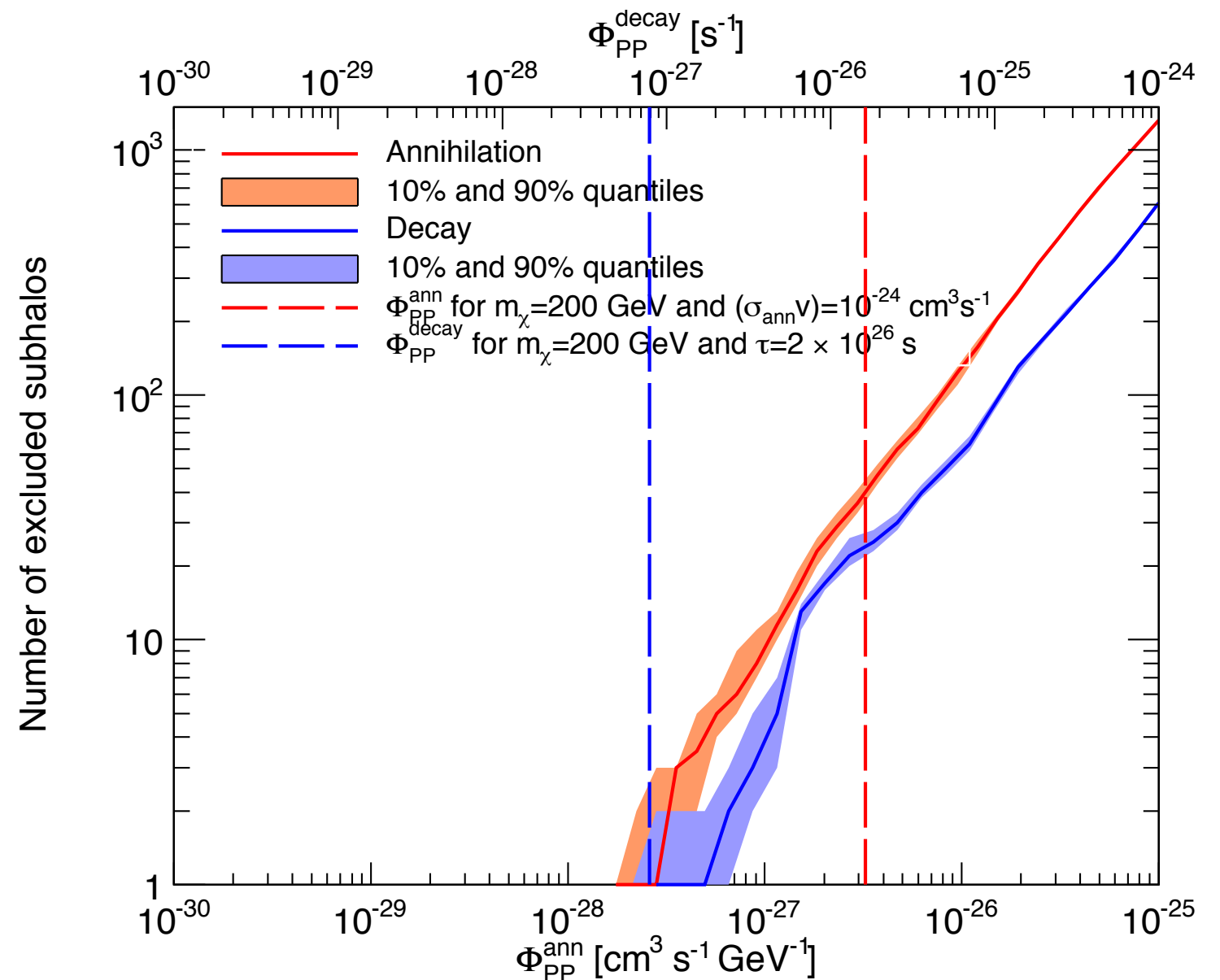


# Effect of an too-bright subhalos on GAL-AQ

- for certain combination of  $(m_\chi, \sigma_{\text{ann}}v)$  and  $(m_\chi, \tau)$ , some subhalos are brighter than the 3FGL sensitivity
- those structures should be masked

$$\Phi_{\text{PP}}^{\text{ann}} = \frac{(\sigma_{\text{ann}}v)}{2m_\chi^2} \int_{\bar{E}} E \frac{dN_\gamma^{\text{ann}}}{dE} dE$$

$$\Phi_{\text{PP}}^{\text{decay}} = \frac{1}{m_\chi \tau} \int_{\bar{E}} E \frac{dN_\gamma^{\text{decay}}}{dE} dE$$



# Effect of an too-bright subhalos on GAL-AQ

