Multi-messenger source models: neutrino-UHECR connections

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Workshop on Perspectives on the Extragalactic Frontier ICTP, Trieste — May 06, 2016





Ultra-high-energy cosmic rays

After 50+ years of UHECR measurements ----



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The electromagnetic sky



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A new player: high-energy astrophysical neutrinos

The era of neutrino astronomy has begun!

IceCube has reported 54 events with 30 TeV - 2 PeV in 4 years



The newest kid on the block: gravitational waves

We have started listening to compact object mergers -



LIGO & VIRGO, PRL 116, 061102 (2016)

What about the sources of HE neutrinos?

Arrival directions compatible with an isotropic distribution -



No association with sources found yet

The multi-messenger picture



We will use gamma-ray bursts (GRBs) as a concrete source example

Why are GRBs interesting as potential ν sources?

- They are the best candidates for detection of coincident high-energy e.m.–neutrino emission at PeV ν energies
- 2 Neutrinos from GRB afterglows are expected to be important at EeV energies (observable by radio neutrino detectors)

[K. MURASE, PRD 76, 123001 (2007)] [S. RAZZAQUE, L. YANG, PRD 91, 043003 (2015)]

Oark, "failed" GRBs might contribute an important part to the diffuse flux seen by IceCube

[P. MÉSZAROS, E. WAXMAN, PRL 87, 171102 (2001)]

Here we will focus on issue **1** and explore the prompt emission of neutrinos in GRBs

Why is *now* a good time to do this?

better, bigger detectors + loads of data + bright future

Neutrinos



- ► IceCube: diffuse flux of HE astrophysical v's
- ► No point sources yet
- GRBs: low bg due to time and direction cuts
- ▶ IceCube-Gen2

GRBs



- ► Fermi: ~ 250 GRBs yr⁻¹ in 8 keV – 40 MeV
- ► ~ 12 GRBs yr⁻¹ in 20 MeV – 300 GeV
- different wavelengths: INTEGRAL, Swift
- ▶ 1000's GRBs detected so far

UHECRs



- Auger: 69 events > 57 EeV
- ► Telescope Array: 72 events
- surface + fluorescence
- ▶ future: LHAASO, JEM-EUSO

GRBs are among the best candidate sources for CRs and ν 's:

- radiated energy of $\sim 10^{52} 10^{53}$ erg
- intense magnetic fields of $\sim 10^5$ G
- magnetically-confined p's shock-accelerated to ~ 10¹² GeV
- plus: low backgrounds (for v's) due to small time window

Problem: experiments (IceCube, ANTARES) are starting to strongly constrain the simplest joint emission models

Solution: we need to build more realistic models!

GRBs – good candidates for UHE CR & ν sources

GRBs are among the best candidate sour

- radiated energy of $\sim 10^{52} 10^{53}$ erg
- intense magnetic fields of $\sim 10^5$ G
- $\begin{array}{cccc} 10^{20} \mbox{ erg } & \mbox{H bo} \\ 10^{26} \mbox{ erg } & \mbox{killer} \\ 10^{40} \mbox{ erg } & \mbox{Deat} \\ 10^{33} \mbox{ erg } s^{-1} & \mbox{Sun} \\ 10^{41} \mbox{ erg } s^{-1} & \mbox{supe} \\ 10^{45} \mbox{ erg } s^{-1} & \mbox{galax} \end{array}$
 - H bomb killer asteroid Death Star Sun supernova galaxy
- magnetically-confined p's shock-accelerated to ~ 10¹² GeV
- > plus: low backgrounds (for ν 's) due to small time window

Problem: experiments (IceCube, ANTARES) are starting to strongly constrain the simplest joint emission models

Solution: we need to build more realistic models!

GRBs - what are they?

GRBs: the most luminous explosions in the Universe

- brief flashes of gamma rays: from 0.1 s to few 100's s
- isotropically distributed in the sky
- ► they are far: most occur at ~ 1 Gpc from us (z ≈ 2)
- they are rare: \sim 0.3 Gpc⁻³ yr⁻¹
- two populations:
 - short-duration (< 2 s): neutron starneutron star or NS-black hole mergers
 - long-duration (> 2 s): associated to hypernovae
- powered by matter accretion onto a black hole



GRBs - a zoo of light curves

GRB light curves come in different shapes:



variability timescale (width of pulses) $\equiv t_v \approx 1 \text{ ms}$

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Neutrino-UHECR connections

GRBs explained - the fireball model

Developed by Mészáros, Reese, Goodman, Pachinsky, et al. in the 1990s



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Internal collisions

Relativistically-expanding blobs of plasma collide with each other, merge, and emit UHE particles —



Producing the UHE ν 's, CRs, γ rays – a first look

Joint production of UHECRs, ν 's, and γ 's:





(Δ^+ : ~50% of all $p\gamma$ interactions)

After propagation, with flavor mixing:

 $u_{oldsymbol{e}}:
u_{\mu}:
u_{ au}:oldsymbol{p}=1:1:1:1$ ("one u_{μ} per cosmic ray")

This neutron model of CR emission is now strongly disfavoured

ICECUBE, *Nature* **484**, 351 (2012) M. AHLERS *et al. Astropart. Phys.* **35**, 87 (2011)

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To calculate the ν flux from a GRB, we need:

- its gamma-ray luminosity L_{γ}^{iso} [erg s⁻¹] [measured]
- its variability timescale t_v [s], from the light curve [measured]
- the bulk Lorentz factor of its jet Γ [estimated]
- the energy in electrons, magnetic field, protons [estimated]

Now let us cook up the neutrinos ►

Normalizing neutrinos with observed gamma rays

energy in neutrinos \propto energy in gamma rays

In detail, for each GRB,

$$\int_{0}^{\infty} dE_{\nu} E_{\nu} F_{\nu} (E_{\nu}) = \frac{1}{8} \underbrace{\left[1 - (1 - \langle x_{\rho \to \pi} \rangle)^{\Delta R/\lambda_{\rho\gamma}}\right]}_{f_{\pi}} \frac{1}{f_{e}} \int_{1 \text{ keV}}^{10 \text{ MeV}} d\epsilon_{\gamma} \epsilon_{\gamma} F_{\gamma} (\epsilon_{\gamma})$$

 $\begin{array}{l} f_{\pi}: \mbox{ fraction of total proton energy transferred to pions} \\ \Delta R: \mbox{ size of the emitting region} \\ \lambda_{p\gamma}: \mbox{ mean free path for } p\gamma \mbox{ interactions} \\ \langle x_{p\rightarrow\pi} \rangle: \mbox{ avg. fraction of } p \mbox{ energy transferred to a } \pi \mbox{ in one interaction} \\ f_e^{-1}: \mbox{ ratio of energy in protons to energy in photons/electrons} \end{array}$

$$\frac{\Delta R}{\lambda_{p\gamma}} = \left(\frac{L_{\gamma}^{\rm iso}}{10^{52}\,{\rm erg\,s^{-1}}}\right) \left(\frac{0.01}{t_{\rm V}}\right) \left(\frac{10^{2.5}}{\Gamma}\right)^4 \left(\frac{{\rm MeV}}{\varepsilon_{\gamma,{\rm break}}}\right)$$

The original recipe: conventional fireball model

Observed gamma-ray fluence [GeV⁻¹ cm⁻²]

$$\mathcal{F}_{\gamma}\left(arepsilon_{\gamma}
ight) \propto \left\{ egin{array}{cc} \left(arepsilon_{\gamma}/arepsilon_{\gamma, ext{break}}
ight)^{-1} &, \ arepsilon_{\gamma} < arepsilon_{\gamma, ext{break}}
ight) = 1 \ ext{MeV} \ \left(arepsilon_{\gamma}/arepsilon_{\gamma, ext{break}}
ight)^{-2.2} &, \ arepsilon_{\gamma} \geq arepsilon_{\gamma, ext{break}}
ight)$$

+

Assumed proton spectrum in the source

$$N_{p}^{\prime}\left(E_{p}
ight) \propto E_{p}^{\prime-2}$$

=

Neutrino spectrum from $p\gamma$, via Δ resonance

$$F_{
u}(E_{
u}) \propto egin{cases} \left(rac{E_{
u}}{E_{
u, ext{break}}}
ight)^{-lpha_{
u}} &, E_{
u} < E_{
u, ext{break}} \ \left(rac{E_{
u}}{E_{
u, ext{break}}}
ight)^{-eta_{
u}} &, E_{
u, ext{break}} \leq E_{
u} < E_{
u,\mu} \ \left(rac{E_{
u}}{E_{
u, ext{break}}}
ight)^{-eta_{
u}} \left(rac{E_{
u}}{E_{
u, ext{break}}}
ight)^{-2} &, E_{
u} \geq E_{
u,\mu} \end{cases}$$

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Neutrino spectrum – conventional fireball



E. WAXMAN, J. N. BAHCALL, *PRL* 78, 2292 (1997)
D. GUETTA *et al.*, *Astropart. Phys.* 20, 429 (2004)

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The static burst assumption

All internal collisions are identical and occur at the same radius -



- Average speed Γ inferred from afterglow observations
- "Variability timescale" t_v measured from the light curve
- Redshift z measured for the host galaxy
- "Isotropically-equivalent volume": $V'_{iso} = 4\pi R_C^2 I'$
- $N_{coll} \approx T_{90}/t_v \sim 100-1000$ identical collisions

Neutron model of UHECR emission under tension?

In 2012, IceCube ruled this analytical version of the fireball model -

- assumed a fixed baryonic loading of 10
- analytical calculation in tension with upper bounds



ICECUBE, *Nature* **484**, 351 (2012) M. AHLERS *et al. Astropart. Phys.* **35**, 87 (2011) D. GUETTA *et al. Astropart. Phys.* **20**, 429 (2004)

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NeuCosmA: (revised) GRB particle emission - I

Two ingredients:



Photons (same shape as observed at Earth):

$$N_{\gamma}'\left(E_{\gamma}'\right) = \begin{cases} \left(\frac{E_{\gamma}'/E_{\gamma,\text{break}}'\right)^{-1}}{\left(\frac{E_{\gamma}'/E_{\gamma,\text{break}}'\right)^{-2.2}}{,} & E_{\gamma}' \ge E_{\gamma,\text{break}}' \\ 0 & , & \text{otherwise} \end{cases} = 1 \text{ keV}$$

► Protons:
$$N'_{\rho}(E'_{\rho}) \propto E'^{-\alpha_{\rho}}_{\rho}e^{-E'_{\rho}/E'_{
ho,max}}$$
 ($\alpha_{
ho} \gtrsim$ 2)

NeuCosmA: (revised) GRB particle emission - I

Two ingredients:



Photons (same shape as observed at Earth):

$$N_{\gamma}'(E_{\gamma}') = \begin{cases} \left(\frac{E_{\gamma}'/E_{\gamma,\text{break}}'\right)^{-1}}{\left(\frac{E_{\gamma}'/E_{\gamma,\text{break}}'\right)^{-2.2}}{0}}, \frac{E_{\gamma,\text{min}}' = 0.2 \text{ eV} \le E_{\gamma}' < E_{\gamma,\text{break}}' = 1 \text{ keV} \\ \left(\frac{E_{\gamma}'/E_{\gamma,\text{break}}'\right)^{-2.2}}{0}, \frac{E_{\gamma}' \ge E_{\gamma,\text{break}}'}{\rho,\text{max}} \\ \text{, otherwise} \end{cases}$$

$$I_{\text{acc}}'(E_{\rho,\text{max}}) = \min\left[I_{\text{dyn}}', I_{\text{syn}}'(E_{\rho,\text{max}}'), I_{\rho\gamma}'(E_{\rho,\text{max}}')\right]$$

$$\blacktriangleright \text{ Protons: } N_{\rho}'(E_{\rho}') \propto E_{\rho}'^{-\alpha_{\rho}} e^{-E_{\rho}'/E_{\rho,\text{max}}'} \quad (\alpha_{\rho} \gtrsim 2)$$

NeuCosmA: (revised) GRB particle emission - II

Normalize the particle densities at the source —

Photons:



► Protons: baryonic loading (energy in p's / energy in e's + γ 's), e.g., 10 proton energy density per collision $\int E'_p N'_p(E'_p) dE'_p$ • photon energy density per collision

NeuCosmA: (revised) GRB particle emission - III

Injected/ejected spectrum of secondaries $(\pi, K, n, \nu, \text{ etc.})$: $x \equiv E'/E'_{\rho} \quad y \equiv E'_{\rho}E'_{\gamma}/(m_{\rho}c^{2})$ $Q'(E') = \int_{E'}^{\infty} \frac{dE'_{\rho}}{E'_{\rho}}N'_{\rho}(E'_{\rho}) \int_{0}^{\infty} c \ dE'_{\gamma} \ N'_{\gamma}(E'_{\gamma}) \ R(x, y)$ response function

R contains cross sections, multiplicities for different channels



neutrino flavor transitions



NeuCosmA – how the neutrino spectrum changes



S. HÜMMER, P. BAERWALD, W. WINTER, PRL 108, 231101 (2012)

The new prediction of the quasi-diffuse GRB ν flux

Repeat the IceCube GRB neutrino analysis, with NeuCosmA ---

- Same GRB sample and parameters
- Calculate ν fluence for each burst and stacked fluence F_ν (E_ν)

• Quasi-diffuse flux (
$$N_{\text{GRB}} = 117$$
):
 $\phi_{\nu} (E_{\nu}) = F_{\nu} (E_{\nu}) \frac{1}{4\pi} \frac{1}{N_{\text{GRB}}} \frac{667 \text{ bursts}}{\text{yr}}$

Flux \sim 1 order of magnitude lower!



S. HÜMMER, P. BAERWALD, W. WINTER, *PRL* **108**, 231101 (2012)

Improved IceCube limits (2016)

- 3 yr of showers (all flavors) + 4 yr of upgoing tracks with > 1 TeV
- Larger GRB catalogue (807 bursts)
- Six coincident events found (five showers + one track)
- Low statistical significance
- $ho~\lesssim$ 1% of the diffuse flux can be from prompt GRB emission



ICECUBE, 1601.06484

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ICECUBE, 1601.06484

What about low-luminosity and choked GRBs?

- Low-luminosity and choked GRBs might be in the same family as high-luminosity long GRBs
- Due to lower jet speeds (Γ_b), they do not break out
- They might explain the TeV region of the IceCube diffuse ν flux:



The neutron model hinges on:

- 1 p's magnetically confined, only n's escape
- 2 p's interact at most once, n's do not (optically thin source)

However, under the "one ν_{μ} per CR" hypothesis, GRBs are disfavored as the sole sources of UHECRs (AHLERS *et al.*).

M. AHLERS, M. GONZÁLEZ-GARCÍA, F. HALZEN, Astropart. Phys. 35, 87 (2011)

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What if 1 and 2 are violated?

- > p's "leak out", not accompanied by (direct) ν production
- multiple p interactions enhance the ν flux
- ▶ in optically thick sources, only n's at the borders escape

M. AHLERS, M. GONZÁLEZ-GARCÍA, F. HALZEN, Astropart. Phys. 35, 87 (2011)

Going beyond the neutron model

We have improved the model - now UHECRs escape as either:

- neutrons, which decay into protons outside the source; or
- protons that leak out without interacting inside the source

Relative contributions determined by $\tau_n \equiv \left(t_{\rho\gamma}^{-1} / t_{dyn}^{-1} \right) \Big|_{E'_{\rho,max}}$



A two-component model of UHECR emission

Sample neutrino fluences -

Optically thin source



Optically thick source

P. BAERWALD, MB, W. WINTER, ApJ 768, 186 (2013)

From the sources to us






Because of the cosmological expansion:



Cosmological photon backgrounds:





 γ 's and e^{\pm} 's dump energy into e.m. cascades through

- ▶ pair production, $\gamma + \gamma_b \rightarrow e^+ + e^-$
- ▶ inverse Compton scattering, $e^{\pm} + \gamma_b \rightarrow e^{\pm} + \gamma$

Lower-energy (GeV-TeV) gamma-rays detected by Fermi-LAT



p's are deflected by extragalactic magnetic fields

⇒ except for the most energetic ones, they are Pierre Auger found weak correlation not expected to point back to the sources

with known AGN positions

They lose energy through:

▶ pair production, $p + \gamma_b \rightarrow p + e^+ + e^-$ depend on the redshift evolution

> photohadronic interactions, $p\gamma_b$

of the cosmological γ backgrounds





Initial UHE ν flavor fluxes: $\nu_e : \nu_\mu : \nu_\tau = 1 : 2 : 0$

Probability of $\nu_{\alpha} \rightarrow \nu_{\beta}$ transition: $P_{\alpha\beta}(E_0, z)$

Flavor oscillations redistribute the fluxes — at Earth: $\nu_e : \nu_\mu : \nu_\tau \approx 1 : 1 : 1$ (might be changed by exotic physics!)

What do the diffuse fluxes look at Earth, then?

Neutron model vs. two-component model: prompt and cosmogenic *v*'s

UHECRs

Neutrinos



Constraints from experimental data

Fit the UHECR flux to Telescope Array data & enforce the IceCube GRB ν and cosmogenic ν upper limits —



More relativistic (higher Γ) GRBs are needed

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Neutrino-UHECR connections

Going further: an evolving burst

Consider an evolving fireball -

- the fireball expands with time
- ~ 1000 shells propagate with different speeds
- they have different masses
- they collide at different radii (collisions no longer identical)

What is different?

The particle (γ , p) densities fall as the fireball expands – particle production conditions change with time/radius

S. Kobayashi, T. Piran, R. Sari, *ApJ* **490**, 92 (1997) F. Daigne, R. Mochkovitch, *MNRAS* **296**, 275 (1998)



Initial distribution of shell speeds

Distribution of initial shell speeds (Lorentz factors):

$$\ln\left(\frac{\Gamma_{k,0}-1}{\Gamma_0-1}\right) = A_{\Gamma} \cdot x$$

x follows a Gaussian distribution, $P(x) dx = dx e^{-x^2/2}/\sqrt{2\pi}$



Each collision occurs in a different emission regime -



MB, P. BAERWALD, K. MURASE, W. WINTER, Nat. Commun. 6, 6783 (2015)

Synthetic light curves

An emission pulse is assigned to each collision – their superposition yields a synthetic light curve:



MB, P. BAERWALD, K. MURASE, W. WINTER *Nature Commun.* 6, 6783 (2015)

Synthetic light curves

An emission pulse is assigned to each collision

- their superposition yields a synthetic light curve:



Different particles come from different jet regions

Emission of different species peaks at different collision radii -



Why?

As the fireball expands, photon and proton densities fall

Why does it matter?

GRB parameters derived from gamma-ray observations might not be adequate to describe ν and UHECR emission

MB, P. BAERWALD, K. MURASE, W. WINTER, Nat. Commun. 6, 6783 (2015)

A robust minimal diffuse ν flux from GRBs

Take the simulated burst as stereotypical

Quasi-diffuse neutrino flux, assuming 667 identical GRBs per year:



What makes a GRB bright in neutrinos? (Preliminary)

- Goal: to use the morphology of the GRB gamma-ray light curve to assess whether the burst is neutrino-bright
- The central engine determines the features of the light curve

Undisciplined GRB engine

 Engine emits shells with log-normal distribution of Γ

Broad C distribution

Disciplined GRB engine

Engine emits shells with oscillating Γ





Light curves

Undisciplined GRB engine

- Fast variability dominates
- No broad pulses

Disciplined GRB engine

- Broad pulses dominate
- Fast variability on top



So which burst is neutrino-bright?

Compare the quasi-diffuse neutrino fluxes:



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Time delays in gamma-ray light curves

Neutrino-weak bursts show time delays in different energy bands -



MB, MURASE, WINTER, IN PREP.

- ► GRBs *are* good UHECR and *ν* source candidates
- **But** the CR- ν - γ connection is trickier than originally thought
- Contribute to the diffuse HE astrophysical ν flux at the few % level
- Likely to be the first point neutrino sources to be resolved
- Need next-gen neutrino telescopes (IceCube-Gen2, KM3NeT) ...
- ... while Auger, Telescope Array, CTA, etc. gather extensive UHECR statistics
- Based on gamma-ray light curve morphology, we can build better GRB catalogues for v searches

Backup slides

GRBs - an accidental discovery

After the 1963 Nuclear Test Ban Treaty, the U.S. launched six pairs of *Vela* satellites:

- They carried X-ray, gamma-ray, and neutron detectors
- Vela 5a-b had enough spatial resolution to pinpoint the direction of events
- Intense gamma-ray emission from a nuclear explosion lasts $\lesssim 10^{-6} \ s \ldots$
- ... however, longer-lasting emissions were detected



VELA 5A/B SATELLITES (NASA)

GRBs - the first one detected

First GRB detected: July 2, 1967, 14:19 UTC



Detected by Vela 3, 4a, 4b (found on archival data)

What do they look like?

e.g., GRB060218 seen by Swift



SDSS, SWIFT COLLAB., SLOAN FOUNDATION, NSF, NASA

GRBs - two populations

Two populations of GRBs:



 T_{90} : time during which 90% of gamma-ray energy is recorded

Improved IceCube bounds (2014)

- Only upgoing ν_{μ} 's with > 1 TeV used
- Four years of data (IC-40, -59, -79, -86)
- Larger GRB catalogue (506 bursts)
- One coincident event found, with low statistical significance
- $\blacktriangleright\,\lesssim$ 1% of the diffuse flux can be from prompt GRB emission



[[]ICECUBE, ApJ 805, L5 (2015)]

Optical depth:

$$\tau_n = \left. \frac{t_{p\gamma}^{-1}}{t_{dyn}^{-1}} \right|_{E_{p,max}} = \begin{cases} \lesssim 1 , & \text{optically thin source} \\ > 1 , & \text{optically thick source} \end{cases}$$

Particles can escape from within a shell of thickness λ'_{mfp} :

$$\lambda_{\rho,\mathsf{mfp}}^{\prime}\left(E^{\prime}\right) = \min\left[\Delta r^{\prime}, R_{L}^{\prime}\left(E^{\prime}\right), ct_{\rho\gamma}^{\prime}\left(E^{\prime}\right)\right] \\ \lambda_{n,\mathsf{mfp}}^{\prime}\left(E^{\prime}\right) = \min\left[\Delta r^{\prime}, ct_{\rho\gamma}^{\prime}\left(E^{\prime}\right)\right] \right\} f_{\mathsf{esc}} = \frac{\lambda_{\mathsf{mfp}}^{\prime}}{\Delta r^{\prime}}$$

fraction of escaping particles

We need direct proton escape

Scan of the GRB emission parameter space -

 $\begin{array}{ccc} \text{acceleration} & \longrightarrow & \eta = 0.1 \\ \text{efficiency} & \longrightarrow & \eta = 1.0 \end{array}$



P. BAERWALD, INB, AND W. WINTER, ApJ 700, 186 (2013)

we need high efficiencies \Rightarrow direct proton escape *is* required

Star-formation-rate vs. GRB redshift evolution

The exclusion from cosmogenic ν 's grows if the number of GRBs evolves more strongly with redshift:



direct p escape, n = 1.0

 $n_{\rm GRB}(z) \propto \rho_{\rm SFR}(z)$ (star formation rate)











Especially "Multi π " contribution leads to change of flux shape; neutrino flux higher by up to a factor of 3 compared to WB treatment
NeuCosmA – further particle decays

$$\begin{array}{rcl} \pi^+ & \rightarrow & \mu^+ + \nu_\mu \\ & \mu^+ \rightarrow {\pmb e}^+ + \nu_{\pmb e} + \bar{\nu}_\mu \end{array}$$

$$\begin{array}{rccc} \pi^- & \rightarrow & \mu^- + \bar{\nu}_\mu \\ & \mu^- \rightarrow {\pmb e}^- + \bar{\nu}_{\pmb e} + \nu_\mu \end{array}$$

$$K^+ \rightarrow \mu^+ + \nu_\mu$$

$$n \rightarrow p + e^- + ar{
u}_e$$

NeuCosmA – further particle decays



Resulting ν_e flux (at the observer)

P. BAERWALD, S. HÜMMER, AND W. WINTER, Phys. Rev. D83, 067303 (2011)

NeuCosmA – further particle decays



Resulting ν_{μ} flux (at the observer)

P. BAERWALD, S. HÜMMER, AND W. WINTER, Phys. Rev. D83, 067303 (2011)

NeuCosmA - how the neutrino spectrum changes - I



S. HÜMMER, P. BAERWALD, W. WINTER, *Phys. Rev. Lett.* **108**, 231101 (2012)

Corrections to the analytical model:

- ► shape revised:
 - shift of first break (correction of photohadronic threshold)
 - different cooling breaks for μ 's and π 's
 - (1 + z) correction on the variability scale of the GRB
- Correction cf_{π} to π prod. efficiency:
 - $f_{C_{\gamma}}$: full spectral shape of photons
 - $f_{\approx} = 0.69$: rounding error in analytical calculation
 - $f_{\sigma} \simeq 2/3$: from neglecting the width of the Δ -resonance
- ► Correction *c*_S:
 - energy losses of secondaries
 - energy dependence of the mean free path of protons

NeuCosmA - neutrino spectra including flavor mixing



P. BAERWALD, S. HÜMMER, W. WINTER, Phys. Rev. D83, 067303 (2011)

Characteristic double peak structure from μ and π decay in both flavors, additional peak from K^+ decay at 10⁸ to 10⁹ GeV

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Neutrino-UHECR connections

The need for km-scale neutrino telescopes

Expected ν flux from cosmological accelerators (Waxman & Bahcall 1997 & 1998):

$$E^2 \Phi_{
u} \sim 10^{-8} rac{f_{\pi}}{0.2} \left(rac{\dot{arepsilon}^{[10^{10},10^{12}]}}{10^{44} \ ext{erg Mpc}^{-3} \ ext{yr}^{-1}}
ight) \ ext{GeV cm}^{-2} \ ext{s}^{-1} \ ext{sr}^{-1}$$

Integrated flux above 1 PeV:

$$\Phi_{
u} \, (> 1 \; \text{PeV}) \sim \int_{1 \; \text{PeV}}^{\infty} \, rac{10^{-8}}{E^2} \; dE \sim 10^{-20} \; ext{cm}^{-2} \; ext{s}^{-1} \; ext{sr}^{-1}$$

Number of events from half of the sky (2π):

$$\mathit{N}_{\!
u} \simeq 2 \pi \cdot \Phi_{\!
u} \left(> 1 \ \text{PeV}
ight) \cdot 1 \ \text{yr} \cdot \mathit{A}_{\text{eff}} pprox \left(2.4 imes 10^{-10} \ \text{cm}^{-2}
ight) \mathit{A}_{ ext{eff}} \; ,$$

where $A_{\rm eff}$ is the effective area of the detector

To detect $N_{\nu} > 1$ events per year, we need an area of

$$A_{\rm eff}\gtrsim 0.4~{\rm km}^2$$

Therefore, we need km-scale detectors, like IceCube

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We have seen that protons interact with the cosmological photon fields (CMB, etc.), *e.g.*,

$$p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + n$$
,

and neutrinos are created in the decays of the secondaries:

$$\pi^{+} \rightarrow \mu^{+} + \nu_{\mu}$$

$$\mu^{+} \rightarrow \overline{\nu}_{\mu} + \nu_{e} + e^{+}$$

$$n \rightarrow p + e^{-} + \overline{\nu}_{e}$$

These are called *cosmogenic neutrinos*

Cosmogenic neutrinos



Interaction with the photon backgrounds - I

Energy loss rate (GeV s⁻¹):

$$b(E) \equiv \frac{dE}{dt}$$

• For pair production $p\gamma \longrightarrow pe^+e^-$:

$$b_{e^+e^-}(E,z) = -\alpha r_0^2 \left(m_e c^2\right)^2 c \int_2^\infty d\xi n_\gamma \left(\frac{\xi m_e c^2}{2\gamma}, z\right) \frac{\phi(\xi)}{\xi^2}$$

• n_{γ} : isotropic photon background (GeV⁻¹ cm⁻³)

• ξ : photon energy in units of $m_e c^2$

- proton energy: $E = \gamma m_p c^2 \ (\gamma \gg 1)$
- $\phi(\xi)$: (tabulated) integral in energy of outgoing e^-

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G. BLUMENTHAL, Phys. Rev. D 1, 1596 (1970)
H. BETHE, W. HEITLER, Proc. Roy. Soc. A146, 83 (1934)
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Interaction with the photon backgrounds - II

Photohadronic interactions – $p\gamma$ interaction rate (s⁻¹ per particle):

$$\Gamma_{\rho\gamma\to\rho'b}(E,z) = \frac{1}{2} \frac{m_{\rho}^2}{E^2} \int_{\frac{\epsilon_{\rm th}m_{\rho}}{2E}}^{\infty} d\epsilon \frac{n_{\gamma}(\epsilon,z)}{\epsilon^2} \int_{\epsilon_{\rm th}}^{2E\epsilon/m_{\rho}} d\epsilon_r \epsilon_r \sigma_{\rho\gamma\to\rho'b}^{\rm tot}(\epsilon_r)$$

1 For given values of *E* and *z*, NeuCosmA calculates the cooling rate $t_{\rho\gamma}^{-1} \equiv -(1/E) b_{\rho\gamma}$ (s⁻¹) as

$$t_{
ho\gamma}^{-1}\left(E,z
ight) = \sum_{i}^{ ext{all channels}} \Gamma_{
ho
ightarrow
ho}^{i}\left(E,z
ight) {\cal K}^{i} \; ,$$

with $K^i E$ the loss of energy per interaction

- 2 From this, we calculate back $b_{p\gamma}$ (GeV s⁻¹) ...
- 3 ... and the corresponding energy-loss term in the transport equation, $\partial_E (b_{p\gamma} Y_p)$.

S. HÜMMER, M. RÜGER, F. SPANIER, W. WINTER, Astrophys. J. 721, 630 (2010) [1002.1310]

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Neutrino-UHECR connections

Interaction lengths

Note that $L_{CIB} \gg L_{CMB}$:



Matches, e.g., H. TAKAMI, K. MURASE, S. NAGATAKI, K. SATO, Astropart. Phys. 31, 201 (2009) [0704.0979]

Secondary injection of neutrons, neutrinos (GeV⁻¹ cm⁻³ s⁻¹)

$$Q'(E') = \int_{E'}^{\infty} \frac{dE'_{\rho}}{E'_{\rho}} N'_{\rho} \left(E'_{\rho}\right) \int_{0}^{\infty} cd\varepsilon' N'_{\gamma} \left(\varepsilon'\right) R\left(E', E'_{\rho}, \varepsilon'\right)$$

Normalisation to the observed GRB photon flux F_γ

$$\int arepsilon' N_{\gamma}'\left(arepsilon'
ight) darepsilon' = rac{E_{
m iso}'^{
m sh}}{V_{
m iso}'} \propto F_{\gamma} \;, \;\; \int E_{
ho}' N_{
ho}'\left(E_{
ho}'
ight) dE_{
ho}' = rac{1}{f_e} rac{E_{
m iso}'^{
m sh}}{V_{
m iso}'} \propto rac{F_{\gamma}}{f_e}$$

Fluence per shell, at Earth (GeV $^{-1}$ cm $^{-2}$)

$$\mathcal{F}^{\mathrm{sh}} = t_{\mathrm{v}} V_{\mathrm{iso}}^{\prime} rac{\left(1+z
ight)^2}{4\pi d_L^2} Q^{\prime}$$

Secondary injection of neutrons, neutrinos (GeV⁻¹ cm⁻³ s⁻¹)

$$Q'(E') = \int_{E'}^{\infty} \frac{dE'_{\rho}}{E'_{\rho}} N'_{\rho} \left(\frac{E'_{\rho}}{\rho} \right) \int_{0}^{\infty} cd\varepsilon' N'_{\gamma} \left(\varepsilon' \right) R\left(E', E'_{\rho}, \varepsilon' \right)$$

▶ Photon density, shock rest frame (GeV⁻¹ cm⁻³):

$$\begin{split} \textbf{\textit{N}}_{\gamma}'\left(\varepsilon'\right) &\propto \left\{ \begin{array}{ll} \left(\varepsilon'\right)^{-\alpha_{\gamma}}, & \varepsilon'_{\gamma,\text{min}} = \textbf{0.2 eV} \leq \varepsilon' \leq \varepsilon'_{\gamma,\text{break}} \\ \left(\varepsilon'\right)^{-\beta_{\gamma}}, & \varepsilon'_{\gamma,\text{break}} \leq \varepsilon' \leq \varepsilon'_{\gamma,\text{max}} = \textbf{300} \times \varepsilon'_{\gamma,\text{min}} \\ \varepsilon'_{\gamma,\text{break}} = \mathcal{O}\left(\text{keV}\right), \alpha_{\gamma} \approx \textbf{1}, \beta_{\gamma} \approx \textbf{2} \end{split} \right. \end{split}$$

Proton density:

$$N_{\rho}^{\prime}\left(E_{\rho}^{\prime}
ight)\propto\left(E_{\rho}^{\prime}
ight)^{-lpha_{
ho}} imes\exp\left[-\left(E_{
ho}^{\prime}/E_{
ho,\max}^{\prime}
ight)^{2}
ight]~(lpha_{
ho}pprox2)$$

Maximum proton energy limited by energy losses:

$$t_{
m acc}^{\prime}\left(\mathcal{E}_{
m
ho,max}^{\prime}
ight) = \min\left[t_{
m dyn}^{\prime},t_{
m syn}^{\prime}\left(\mathcal{E}_{
m
ho,max}^{\prime}
ight) ,t_{
m
ho\gamma}^{\prime}\left(\mathcal{E}_{
m
ho,max}^{\prime}
ight)
ight]$$

Secondary injection of neutrons, neutrinos (GeV⁻¹ cm⁻³ s⁻¹)

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– Normalisation to the observed GRB photon flux ${\it F_{\gamma}}$ –

$$\int \varepsilon' N_{\gamma}' \left(\varepsilon' \right) d\varepsilon' = \frac{E_{\rm iso}'^{\rm sh}}{V_{\rm iso}'} \propto F_{\gamma} \;, \;\; \int E_{\rho}' N_{\rho}' \left(E_{\rho}' \right) dE_{\rho}' = \frac{1}{f_e} \frac{E_{\rm iso}'^{\rm sh}}{V_{\rm iso}'} \propto \frac{F_{\gamma}}{f_e} \;\;$$

Secondary injection of neutrons, neutrinos (GeV⁻¹ cm⁻³ s⁻¹)

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Normalisation to the observed GRB photon flux
$$F_{\gamma}$$

$$\int \varepsilon' N'_{\gamma} (\varepsilon') d\varepsilon' = \frac{E'^{\text{sh}}_{\text{iso}}}{V'_{\text{iso}}} \propto F_{\gamma} , \quad \int E'_{\rho} N'_{\rho} (E'_{\rho}) dE'_{\rho} = \frac{1}{f_e} \frac{E'^{\text{sh}}_{\text{iso}}}{V'_{\text{iso}}} \propto \frac{F_{\gamma}}{f_e}$$

Fluence per shell, at Earth (GeV⁻¹ cm⁻²)

$$\mathcal{F}^{\rm sh} = t_{\rm v} V_{\rm iso}^{\prime} \frac{\left(1+z\right)^2}{4\pi d_L^2} Q^{\prime}$$

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A fast-rise-exponential-decay (FRED) gamma-ray pulse is emitted in every collision:



The prediction is robust

Simulations show only weak dependence of the flux on the boost Γ ...



... and on the GRB engine variability time δt_{eng}



Neutrino-UHECR connections

Accelerating iron

- Photodisintegration destroys nuclei close to the center (~ 10⁸ km) e.g., ANCHORDOQUI et al., Astropart. Phys. 29, 1 (2008)
- However, they can survive at large radii:



Propagating the UHECRs to Earth

We use a Boltzmann equation to transport protons to Earth:

Comoving number density of protons (GeV⁻¹ cm⁻³):

$$Y_{p}\left(E,z\right)=n_{p}\left(E,z\right)/\left(1+z\right)^{3},$$

with n_p the real number density

Transport equation (comoving source frame):



Contribution of GRBs to the diffuse ν flux

- Three populations: high-luminosity long GRBs (HL-GRB), low-luminosity long GRBs (LL-GRB), short GRBs (sGRB)
- Sub-PeV: GRBs contribute a few % to the IceCube diffuse flux
- PeV: contribution could be higher



We can already limit the parameter space by using the UHECR observations and ν upper bounds:

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P. BAERWALD, MB, W. WINTER, Astropart. Phys. 62, 66 (2015)

 10^{53}

We can already limit the parameter space by using the UHECR observations and ν upper bounds:

- Generate the UHECR spectrum at every point in parameter space (*e.g.*, in Γ vs. L_{iso})
- Pit each spectrum to UHECR data (TA, PAO, HiRes)
- Find the best-fit point (diamond), and the 90% (red), 95% (yellow), and 99% (blue) C.L. regions

direct *p* escape, $\alpha_p = 2$, $\eta = 1$



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direct *p* escape, $\alpha_p = 2$, $\eta = 1.0$



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 - 7 After 15 yr of exposure and no detection, cosmogenic neutrinos also exclude

direct *p* escape, $\alpha_p = 2$, $\eta = 1.0$



Initialising the burst simulation

Initial number of plasma shells in the jet: $\gtrsim 1000$



Initial values of shell parameters:

- Width of shells and separation between them: $I = d = c \cdot \delta t_{eng}$
- Equal kinetic energy for all shells ($\sim 10^{52}$ erg)
- Shell speeds Γ_{k,0} follow a distribution (log-normal or other)

Propagating and colliding the shells



During propagation:

- speeds, masses, widths do not change (only in collisions)
- the new, merged shells continue propagating and can collide again

Evolution stops when either:

- a single shell is left; or
- $\blacktriangleright\,$ all remaining shells have reached the circumburst medium ($\gtrsim 6\times 10^{11}$ km)

final number of collisions

 \approx number of initial shells (\gtrsim 1000)

S. Kobayashi, T. Piran, R. Sari, *ApJ* **490**, 92 (1997) F. Daigne, R. Mochkovitch, *MNRAS* **296**, 275 (1998)

Anatomy of an internal collision

1 Propagation



Anatomy of an internal collision



Anatomy of an internal collision



Part of the initial kinetic energy radiated as γ 's, ν 's, p's, and n's:



How is the new prediction different?

- The top-contributing collisions are at the photosphere
- Pion production efficiency there is independent of Γ:

$$f_{
ho\gamma}^{
m ph}\sim 5\cdot rac{arepsilon}{0.25}\cdot rac{\epsilon_e}{0.1}\cdot rac{1\ {
m keV}}{\epsilon_{\gamma,{
m break}}'}$$

- $\varepsilon :$ energy dissipation efficiency
- ϵ_e : fraction of dissipated energy as e.m. output (photons)
- \blacktriangleright \Rightarrow Time-integrated neutrino fluence dominated is independent of Γ :

$$\mathcal{F}_{
u} \propto rac{N_{ ext{coll}}\left(f_{\mathcal{P}\gamma} \gtrsim 1
ight)}{N_{ ext{coll}}^{ ext{tot}}} imes \min\left[1, f_{\mathcal{P}\gamma}^{ ext{ph}}
ight] imes rac{\epsilon_{\mathcal{P}}}{\epsilon_{e}} imes E_{\gamma- ext{tot}}^{ ext{iso}}$$

- Compare to standard predictions, which have a $\langle \Gamma \rangle^{-4}$ dependence
- Raising \(\epsilon_\rho\) automatically decreases \(\epsilon_\epsilon\), so the photosphere grows, but still \(\phi\) 10 photospheric collisions dominate
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$$\mathcal{F}_{\nu} \propto \frac{\frac{\sim 10}{N_{\text{coll}}(f_{\rho\gamma} \gtrsim 1)}}{\frac{N_{\text{tot}}}{N_{\text{coll}}^{\text{tot}}} \times \min\left[1, f_{\rho\gamma}^{\text{ph}}\right] \times \underbrace{\frac{10}{\epsilon_{\rho}}}_{\gamma-\text{tot}} \times \frac{10^{53} \text{ erg}}{E_{\gamma-\text{tot}}}$$

- Compare to standard predictions, which have a $\langle \Gamma \rangle^{-4}$ dependence
- Raising \(\epsilon_\rho\) automatically decreases \(\epsilon_\epsilon\), so the photosphere grows, but still \(\phi\) 10 photospheric collisions dominate

Undisciplined GRB engine

- Shells have very different speeds
- Collide quickly, close to engine
- High p and γ densities
- ~ 10 optically-thick bursts near the photosphere

Disciplined GRB engine

- Shells have similar speeds
- Collide far from engine
- Low p and γ densities
- All (superphotospheric) collisions are optically thin





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