Structure data in ENSDF from gamma-ray studies in nuclear reactions

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A bit about gamma rays and nuclear reactions

Gamma rays known since 1900: P. Villard: <u>"Sur la réflexion et la réfraction des rayons cathodiques et des rayons déviables du radium,"</u> *Comptes rendus*, **130**, 1010-12, ibid 1178-79 (1900).

Named as *gamma* (γ) rays by Rutherford in 1903, as continuation of nomenclature for α and β radiation, gamma rays being most penetrating.

An e.m. transition between two levels of a nucleus. Range can be few keV to ~8 MeV in the nuclear context. Can be lower e.g. 7.6 eV in ²²⁹Th. Much higher up to TeV in astronomical context.

Until 1930, about 60 γ rays (emitted by radioactive materials) were known according to:

M. Curie, A. Debierne, A.S. Eve, H. Geiger, O. Hahn, S.C. Lind, S. Meyer, E. Rutherford, E. Schweidler; *The Radioactive Constants as of 1930;* RMP 3, 427 (1931). First compilation of available nuclear data at the time.

Nuclear Reactions have been studied since 1917: ¹⁴N+ $\alpha \rightarrow$ ¹⁷O+p (E. Rutherford)

1942-1943: free neutrons available from reactors

~1950: neutron-capture gamma-ray studies

~1960 and later: neutron scattering, proton, alpha-, and heavy-ion-induced reactions.

Nuclear structure studies using particle beams, and better and bigger gamma-ray detection systems. Why study gamma rays: detailed decay characteristics of mainly bound levels, e-m transition rates for different multipole orders: offers comparison with theoretical model calculations.

Simple undergraduate lab experiment involving reaction gamma rays



 $\alpha + {}^9_4Be \rightarrow {}^{12}_6C^* + n$

 $n + {}^{1}_{1}H \rightarrow {}^{2}_{1}H + \gamma$ (Leads to deuteron binding energy)

 ${}^{12}_{6}C^* \rightarrow {}^{12}_{6}C + \gamma$ (Doppler shifted; leads to lifetime of the first 2+ state)

Detection of 2224.6-keV gamma from n+H and 4438.0-keV from 12C

ENSDF dataset for $1H(n,\gamma)$

2H 1H(N,G) E=THERMAL 1994KI27,1982VA13,1980IS02 ENSDF

- 2H H TYP=FUL\$AUT=J.H. KELLEY, J.L. GODWIN\$CUT=1-May-2003\$
- 2H c Target J|p=1/2+.
- 2H c Measured E|g and I|g, deduced S(n)
- 2H xc (1994Ki27,1982Va13,1980Is02,1980Gr02).
- 2H c Evaluated S(n)=2224.57 keV (1995Au04).
- 2H cL E(A), J(A) \$From (1996FiZY)
- 2H cG RI Intensity per 100 neutron captures
- 2H N 1
- 2H PN
- 2H L 0.0 1+ STABLE

2H 3 L FLAG=A\$

2H L 2224.5725220+,1+

S

- 2H cL J from s-wave neutron capture
- 2H G 2223.245 3 100
- 2H cG E from level-energies difference

Schematics of in-beam gamma-ray data handling



Gamma rays in nuclear reactions

- Bound states: all kinds of reactions leading to structure information for levels populated in these reactions.
- In-beam gamma-ray studies utilizing light-ion, heavy-ion, deep inelastic scattering, fusion-fission reactions, fission induced by light ions, inverse kinematic reactions for one or two nucleon knockouts, etc.: high-spin structures (Also from prompt γ in SF decay e.g. Cf-252, Cm-248 SF decays)
- Neutron, proton or alpha-particle capture followed by gamma emission: low-spin
- Coulomb excitation: light ion or heavy ion: particle and/or gamma detection: low- and high-spin levels.
- Nuclear-resonance fluorescence: low spin

Nuclear Reactions..

- Inelastic scattering such as (n,n'γ), (p,p'γ), (α,α'γ), etc.: low-spins: gamma and/or particle detection
- Single-particle transfer reactions such as (d,p), (d,t), etc.: low-spins: particle detection; in some of the current experiments, also gamma detection
- Two-particle transfer reactions such as (p,t), (t,p), etc.: low-spins: particle detection; rare gamma detection
- Recoil-decay tagging (RDT), and Isomer spectroscopy: both high- and low-spin levels

Nuclear Reactions

- Unbound states (resonances): according to recently revised ENSDF policies, inclusion of levels, widths and gamma data for charged-particle resonances (proton, alpha, etc.) is required. Reactions: (p,p), (p,γ), (α, γ), etc. : low-spin. Particle and/or gamma detection.
- E(level) deduce from S(P)+E(P)(c.m.), where E(p)(c.m.) is deduced from measured E(P) (lab)
- Neutron resonances: (n,γ), (n,n): low-spin: neutron and/or gamma detection. Requirement when final levels are bound, optional otherwise.

³⁷S structure : 2016Ch14: PRC 93, 044318 PRISMA-CLARA set up at INFN, Legnaro Reaction: 208Pb (36S,37S γ)



¹³³Ce structure: 2016Ay04: PRC 93, 054317 Gammasphere array at ATLAS-ANL. Reaction: 116Cd(22Ne,5n γ)



FIG. 1. Part 1 of the level scheme of 133 Ce. The widths of the arrows are proportional to the relative intensities of the γ rays.

¹³³Ce structure (contd.)



FIG. 2. Part 2 of the level scheme of ¹¹³Ce. The widths of the arrows are proportional to the relative intensities of the γ rays. The intensities of the *O* bands are given as a percentage relative to that of the vrast band *D*2.

Quantities given in ENSDF LEVELS

- Energies: deduced from measured gamma-ray energies, and level scheme based on coincidence data (GTOL code used in ENSDF)
- $J\pi$ and T (or T_z) : spin, parity, isospin
- Half-lives: method cited e.g. delayed-gamma, DSAM, RDDS, etc. (T_{1/2} given not the mean lifetime in ENSDF)
- B(E λ), B(M λ) transition probabilities e.g. from Coulomb Excitation or NRF
- g factor, μ and Q: static magnetic dipole and quadrupole moments: generally for g.s. and isomers. (Transition quadrupole moments in comments)
- Decay modes for g.s. and isomers.
- Γ , Γ_i total or partial widths: generally for resonances (or PDR)
- Resonance energies: generally in lab system
- Configurations and/or band structures, band crossings, etc.:

Quantities given in ENSDF GAMMAS

- Ε_γ measured gamma-ray energy (without recoil correction)
- Iγ measured relative intensity or branching ratio
- Multipolarity (Mult) and multipole mixing ratio (δ) (Krane-Steffen convention)
- Theoretical conversion coefficient (from BrIcc code) for assigned Mult and mixing ratio.

(Transitions with E0 admixture or pure E0 need to be handled with care) Transition intensity: $I(\gamma+ce)$: if available or needed.

 γ - γ coincidence evidence: character "C" in column 78 in data file.

- In support of Mult and δ : (information in comments or data-continuation records)
- Measured internal conversion data such as K-, L-shell conversion coefficients, sub-shell ratios (L1/L2/L3..)

Measured angular distribution/correlation coefficients (A_2 , A_4); DCO ratios, Angular asymmetry ratios, Linear polarization coefficients. B(E λ), B(M λ) – transition probabilities (generally in W.u.)

Nuclear reactions

- To investigate Nuclear shapes, shape co-existence, n-p interaction by experimentally observing nuclear rotational bands with normal deformation, superdeformation and octupole deformation, role of γ deformation and triaxiality, magnetic rotational bands, chirality, signature splitting, backbending, wobbling rotational modes,
- Comparison of observed structures with theoretical calculations based on: Cranked Nilsson-Strutinski shell model; Routhians surface contours, large-scale shell-model for low-mass nuclei.

High-spin studies

Since a paper by Morinaga and Gugelot: NP 46, 210 (1963), such data continue to form a large structure data bank in ENSDF.

- Reactions with light ions (p, d, t,³He, ⁴He): J<12
- By heavy-ions (A>4): Fusion-evaporation reactions:
 J up to 68 and 141/2. Mostly neutron-deficient nuclei.
- Deep inelastic reactions; one- or two-nucleon knockout reactions in inverse kinematics. (Recent experiments with RI beams). Investigation of *Terra Incognita* (neutron-rich) region
- Since the mid-eighties, large gamma-ray detector arrays: Gammasphere, Eurogam, GASP, SeGA, EXOGAM, MINIBALL, INGA, 8pi, etc. New and more powerful arrays: GRETINA, AGATA. Clovers, Clusters, Segmented HPGe detectors. These are often coupled to particle detection arrays such as MINIBALL, ISIS arrays, etc., and Neutron detectors such as Neutron Wall, MoNA-LISA array, Magnetic spectrometers for conversion electrons

What is measured

- E_{γ} , $I\gamma$, $\gamma\gamma$ -coin, (charged particle, neutrons, ER) γ -coincidences
- α, α_K, ... electron conversion coefficients, usually from I(ce)/Iγ; sometimes from intensity balance (note: this gives α_{exp}).
- K/L, L1/L3 ... ce subshell ratios
- $A_2, A_4 \dots$ Legendre polynomial coefficients characterizing angular distribution ($\gamma(\theta)$) or angular correlation ($\gamma\gamma(\theta)$).
- DCO ratio directional correlation of gammas from oriented nuclei.
- ADO asymmetry ratio *e.g.*, $I_{\gamma}(\theta_1)/I_{\gamma}(\theta_2)$ in $\gamma\gamma$ -coin arrangement
- Linear polarization: polarization asymmetry or IPDCO ratios
- Level T_{1/2} from γ(t), DSAM, RDM, centroid-shift, delayed coincidence, *etc.*, if measured in that reaction (state method used).
- g-factor include if measured in that reaction
- Quite often details of data from high-spin studies are missing in publications; frequent requests to authors.

What quantities are deduced

- Level energy, spin, parity, lifetime, magnetic moment, transition quadrupole moment, B(M1)/B(E2) or some other reduced transition probability ratios.
- Spins and parities deduced from multipolarities and mixing ratios deduced from angular distribution/correlation data. (Krane-Steffen convention in ENSDF for mixing ratio; opposite to Rose-Brink convention)
- Angular Distributions:
- I_{γ} as a function of angle θ with respect to beam direction:

 $W(\theta)=1+A_2P_2(\cos \theta)+A_4P_4(\cos \theta)+\ldots$

A₂, A₄ as signed values included in ENSDF

- $A_2, A_4 \dots$ depend on ΔJ , mixing ratio and degree of alignment σ/J , where σ is halfwidth of Gaussian describing the magnetic substate population.
- For high-spin states, $W(\theta)$ is largely independent of J.
- Alignment is reduced or absent if level lifetime is long e.g. micro-sec isomer.
- W(θ) can determine ΔJ but <u>not</u> $\Delta \pi$. Need other arguments for parity assignment

Angular Distributions

Typical values of A₂, A₄ for θ relative to beam direction if σ /J=0.3

ΔJ	Multipolarity	Sign of A ₂	Sign of A ₄	Typical A ₂	Typical A ₄
2	Q	+	-	+0.3	-0.1
1	D	-		-0.2	0.0
1	Q	-	+	-0.1	+0.2
1	D+Q	+ or -	+	+0.5 to -0.8	0.0 to +0.2
0	D	+		+0.35	0.0
0	Q	-	-	-0.25	-0.25
0	D+Q	+ or -	-	+0.35 to - 0.25	0.0 to -0.25

Quantities deduced: DCO ratios

- <u>D</u>irectional <u>C</u>orrelations of γ-rays from <u>O</u>riented states of Nuclei
- If γ_{K} (known multipolarity) and γ_{U} (unknown multipolarity) are measured in coincidence using detectors at angles θ_{1} and θ_{2} relative to the beam direction:
- DCO=I($\gamma_U(at \theta_1)$ gated by $\gamma_K(at \theta_2)$)/I($\gamma_U(at \theta_2)$ gated by $\gamma_K(at \theta_1)$).
- Sensitive to ΔJ , multipolarity and mixing ratio; independent of $\Delta \pi$.
- Gating transitions are frequently stretched quadrupole, but stretched dipole may also be used. Give the character of gating transition
- Remember that almost similar values are expected for stretched quadrupoles and for ΔJ=0, dipole transitions, although the latter are less common.
- Also ADO ratios are commonly seen when count rates are low.
- Such measurements can determine ΔJ but <u>not</u> $\Delta \pi$. Need other arguments for assignment of parity.

DCO Ratios

Typical DCO values for θ_1 =37°, θ_2 =79°, σ /J=0.3

ΔJ _γ ^{gate} , Mult	ΔJ_{γ}	Mult	Typical DCO
2, Q	2	Q	1.0
2, Q	1	D	0.56
2, Q	1	D+Q	0.2 to 1.3
2, Q	0	D	1.0
2, Q	0	D+Q	0.6 to 1.0
1, D	2	Q	1/0.56
1, D	1	D	1.0
1, D	0	D	1/0.56

Parity assignment

- L and $\Delta \pi$: from measured subshell ratios or conversion coefficients.
- $\Delta \pi$ may be determined by γ linear polarization measurements.
- When transition strengths can be deduced from measured level lifetimes (or estimated from coincidence resolving times) and branching, <u>R</u>ecommended <u>Upper L</u>imits (RUL) can be used to rule out some multipolarities (*e.g.*, a stretched Q transition for which B(M2)_W exceeds 1 can be assigned as E2). Similarly, for a D+Q transition with large mixing, RUL may reject E1+M2.
- Assign Mult when measured information indicates a clear preference for that assignment; otherwise, let γ(θ) or DCO data speak for themselves. (Exception: if no measurement exists but mult. is needed for some reason, use notation for assumed value: [M1+E2])
- Notes: many authors in papers assign definite MULT even when there are no data to support. In ENSDF, these should not be given
- Ordering of transitions in cascades often disagree: example Pm-139.

In-beam Gamma-ray data

- One data set for each reaction. Mixing relative intensities from different reactions in a single data set is not advised. Also separate datasets for prompt and delayed gamma data.
- Spin-parities are generally taken from original authors' assignments, but in case of differences, comparison should be made with those in Adopted dataset for a nuclide.
- Special care needed in the assignment of multipolarities. In many cases, these may be differently expressed from those given by the authors, or in some others cases, not given at all.
- For level energies, GTOL code is used for a least-squares fit of the gamma-ray data. If reduced chi-squared is high, try to resolve the situation, sometimes by increasing uncertainties or by omitting some gamma-ray energies. GTOL also points out those gamma-ray energies which deviate from the input values. Values which differ by more than 3σ need special attention.

Coulomb excitation with particle and/or gamma detection

- J π : determined if the excitation probability agrees with that calculated by Alder (1960Al23).
- low energy Coulomb excitation process is expected to be E2
- B(E λ) with level for excitation (*i.e.*, B(E λ) \uparrow)
- E2 (or M1) matrix element should be given in comments
- Deduce $B(E\lambda) = |\langle M(E\lambda) \rangle|^2 / (2J_i+1)$ where J_i is initial spin.
- $B(E\lambda; i \rightarrow f) \uparrow = B(E\lambda; f \rightarrow i) \downarrow x (2J_f+1)/(2J_i+1))$
- In strongly-deformed region, a cascade of E2 transitions with enhanced transition probabilities (B(E2)_W > 10): evidence for a rotational band and for the sequence of Jπ values, provided Jπ of one of the levels is known independently.
- Deduce $T_{1/2}$ from B(E λ) and adopted γ -branching ratios when possible.
- Mixing ratio can sometimes be extracted from M1, E2 matrix elements. Refer to Reorientation method for quadrupole moment.

Thermal and resonance (ARC) neutron capture studies: (n,γ) E=thermal, (n,γ) E=res

- Use separate datasets for thermal and resonance n-capture data.
- Primary and secondary transitions usually appear in the same dataset even if their intensities require different normalizations.
- The J π of the thermal neutron capture state(s) is J π (target)±1/2 (*i.e.*, s-wave capture is assumed).
- In thermal neutron capture, the multipolarity of a primary γ is E1 or M1 for strong gamma rays; M1+E2 or E2 possible for weaker ones.
- For resonance n capture, it is optional to include the resonances and their properties; it is required to give the bound states fed, their interconnecting gammas and any conclusions concerning level Jπ.
- In average resonance n capture (ARC), include primary and secondary gamma-ray data, and reduced intensities (which carry information on final state Jπ); final bound level energies and deduced Jπ. Also consider authors' statistical analysis using DICEBOX code

Nuclear Resonance Fluorescence: Pygmy dipole resonances and scissors mode excitations: current interest

- (γ,γ) , (γ,γ') , (pol γ,γ') measurements with bremsstrahlung spectrum; low momentum transfer so mainly E1 and M1, but some E2 excitation.
- γ spectrum measured; areas of γ peaks at Ex₀ and Ex₁, combined with knowledge of N γ (Ex₀), yields scattering cross sections, from which width and branching information may be obtained.
- γ asymmetry differentiates D and Q excitation
- γ linear polarization differentiates M and E
- Integrated) scattering cross section I_s (eV b) is often given as:

 $I_s = g(\Gamma \gamma_0 \Gamma \gamma_f / \Gamma) (\pi \hbar c / E \gamma)^2$, where $g = (2J+1)/(2J_0+1)$, $E \gamma$ in MeV

- where J₀ is g.s. spin, J is spin of excited level, Γ is its total width and Γ_0 , Γ_f partial decay widths for γ decay to the g.s. and the final state f, respectively; for elastic scattering, $\Gamma\gamma_0 = \Gamma\gamma_f = \Gamma$. From g($\Gamma\gamma_0^2 / \Gamma$) and $\Gamma\gamma_0 / \Gamma$ (or $I\gamma_0 / \Sigma I(\gamma)$), deduce Γ or level half-life. T_{1/2} (ps)= 0.456 / Γ (meV)
- B(E1) \uparrow =0.955(g $\Gamma\gamma_0$ /E γ^3) [10⁻⁵e²b].
- $B(M1) \uparrow = 0.0864(g\Gamma\gamma_0/E\gamma^3) [\mu^2_N]$

Inelastic Scattering: (n,n'γ)

- Gamma-ray energies and intensities
- Angular distributions
- Excitation functions and absolute gamma-ray cross sections
- Level lifetimes using Doppler-shift attenuation method.
- Comparison of measured cross sections with theoretical cross sections from EMPIRE or TALYS codes; can lead to spin-parity assignments.

RDT, Isomer spectroscopy: ¹⁵⁸Ta: 2016Ca15: PRC 93, 034307 JUROGAM array at University of Jyvaskyla. 102Pd(58Ni,pn γ) reaction



FIG. 3. Proposed level scheme of ¹⁵⁸Ta. The widths of the arrows are proportional to the measured intensities in JUROGAM, except for transitions seen only at the focal plane, for which the arrow widths are proportional to intensities measured in the clover detector. Tentative transitions are indicated with dashed arrows with energies in parentheses, while tentative levels are indicated by dashed lines and level energies in parentheses. The α -decay energy of the 9⁺ state is taken from Ref. [18]. The spin and parity assignments have been adopted from Ref. [16].

Example of an ENSDF-formatted dataset: ⁴⁵S (Z=16, N=29) single-particle level structure A. Gade et al. PRC 93, 054315 (May 11, 2016): first study of levels in ⁴⁵S

9BE(46CL,45SG):XUNDL-1 2016GA14 201607 45S 45S c Compiled (unevaluated) dataset from 2016Ga14: 45S 2c Phys Rev C 93, 054315 (2016) 45S c Compiled by B. Singh (McMaster), July 25, 2016 45S c One-proton removal reaction from the ground state of {+46}Cl projectile 45S c 2016Ga14: E({+46}Cl)=86.6 MeV/nucleon produced in 45S 2c {+9}Be({+48}Ca,X),E=140 MeV/nucleon primary reaction, using A1900 45S 3c fragment separator at NSCL-MSU facility. Reaction target=376 45S 4c mg/cm{+2} {+9}Be. The products were identified using S800 45S 5c spectrograph based on energy loss and time-of-flight information. 45S 6c Measured particle identification spectra, Elg, Ilg using SeGA array of 45S 7c 36-fold segmented HPGe detectors. Deduced levels, J, |p, |s. Detailed 45S 8c reaction-model, cross sections and spectroscopic factor calculations 45S 9c for proton-removal reactions using DWBA and SDPF-U and SDPF-MU 45S Ac shell-model interactions. Calculations assumed J|p=1- for the ground 45S Bc state of {+46}Cl 45S cL J\$From 2016Ga14, based on shell-model calculations 45S G 1445 8 45S cG E\$this |g ray is not discussed by 2016Ga14 45S L 0 (3/2-)45S cL \$Inclusive |s=2.6 mb {I1} for one-proton removal, derived from 45S 2cL yield of {+45}S reaction products and number of incoming {+46}Cl 45S 3cL projectiles, 5% systematic uncertainty has been added in guadrature 45S L 506 6 (1/2-) 45S G 506 6 45S L 1299 7 (3/2-) 45S G 1299 7 45S L 1360 7 (5/2-) 45S G 1360 7 45S L 2111 11 (3/2-) 45S G 751 8

45S G 809

9



FIG. 6. Event-by-event Doppler-reconstructed γ -ray spectrum of ⁴⁵S following population of the nucleus in the ⁹Be(⁴⁶Cl, ⁴⁵S + γ)X one-proton-removal reaction (v/c = 0.393). The inset shows a tentative level scheme based on energy sums, intensity arguments, and comparison with shell-model calculations (see text)

Tables, drawing and reference list from the ENSDFformatted file: using JAVA-NDS code

29-1	NUCLEAR DATA SHEETS	⁴⁵ ₁₆ S ₂₉ -1			
	⁹ Be(⁴⁶ Cl,45 ₅ γ):XUNDL-1 2016Ga14				
npiled (unevaluated) dataset from 2016Ga14: npiled by B. Singh (McMaster), July 25, 201	Phys Rev C 93, 054315 (2016). 5.				
→proton removal reaction from the ground sta 6Ga14: E(⁴⁶ C1)=86.6 MeV/nucleon produced separator at NSCL-MSU facility. Reaction tt energy loss and time-of-flight information. M segmented HPGe detectors. Deduced levels, for proton-removal reactions using DWBA at the ground state of ⁴⁶ C1.	te of ⁴⁶ Cl projectile. in ⁹ Be(⁴⁶ Ca,X),E=140 MeV/nucleon primary reaction, using A19 rget=376 mg/cm ² ⁹ Be. The products were identified using S800 sp leasured particle identification spectra, $E\gamma$, $I\gamma$ using SeGA array of J, π , σ . Detailed reaction-model, cross sections and spectroscopic : ad SDPF-U and SDPF-MU shell-model interactions. Calculations a	00 fragment ectrograph based on 36-fold factor calculations ssumed Jπ=1- for			
	⁴⁵ S Levels				
(level) Jπ [†]	T Comments				
0 (3/2-) Inclusive σ=2.6 mb I for 6 incoming ⁴⁶ Cl projectile 506 6 (1/2-) 199 7 (3/2-) 360 7 (5/2-) (111 11 (3/2-)	Inclusive σ=2.6 mb l for one-proton removal, derived from yield of ⁴⁵ S reaction products and number of incoming ⁴⁶ Cl projectiles, 5% systematic uncertainty has been added in quadrature.				
[†] From 2016Ga14, based on shell-model cal	rulations.				
	<u>γ(⁴⁵S)</u>				
(level) $J_{l}\pi$ E_{γ} E_{f} $J_{f}\pi$	Comments				
$ \begin{array}{lllllllllllllllllllllllll$					
-1445 8	E _γ , this γ ray is not discussed by 2010Ga14.				
[†] Placement of transition in the level scheme ^x γ ray not placed in level scheme.	is uncertain.				

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Tables, drawing and reference list

