

ABSTRACT:

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Exotic compact quotients of $\mathrm{PSL}(2, \mathbb{C})$.

Given a discrete, torsion free subgroup $\Gamma < \mathrm{PSL}(2, \mathbb{C})$, the quotient $\Gamma \backslash \mathrm{PSL}(2, \mathbb{C})$ is an $\mathrm{SO}(3)$ -bundle over the associated hyperbolic 3-manifold $\Gamma \backslash \mathbb{H}^3$, but is also an example of a complete holomorphic Riemannian manifold of constant curvature. Ghys studied deformations of these structures to a more general class of $\mathrm{PSL}(2, \mathbb{C})$ quotients, and this theory was expanded and further studied by Kobayashi and Gueritaud-Kassel. By a result of Tholozan, the volume of compact quotients remains constant under these deformations, and he asked whether there were "exotic" compact quotients, i.e. bundles over compact hyperbolic manifolds with different volume than the standard $\mathrm{SO}(3)$ -bundle. Building on a construction of Agol and the work of Gueritaud-Kassel, we describe an infinite family of such exotic compact quotients, and calculate their volumes using Tholozan's volume formula. This is joint work with Grant Lakeland.