



“PHOTOTHERMAL DIGITAL LOCK-IN SHADOWGRAPH TECHNIQUE FOR MATERIALS THERMAL CHARACTERIZATION.”

by

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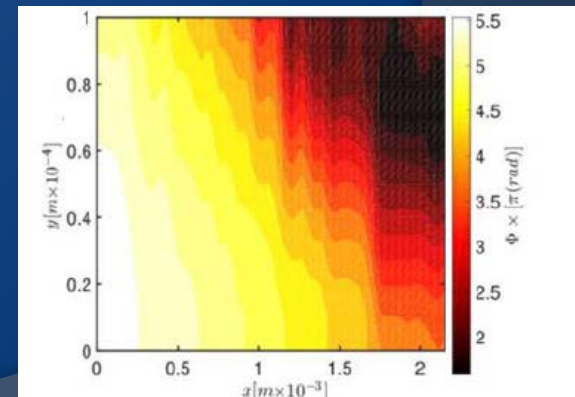
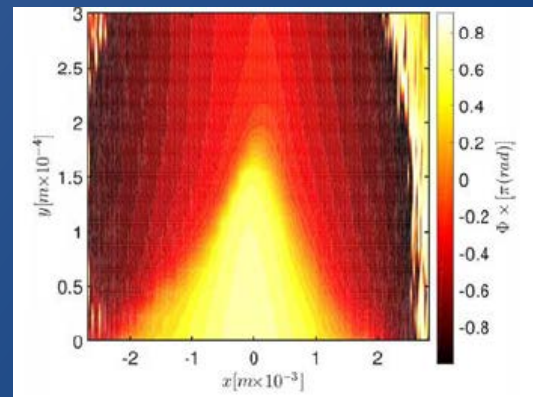
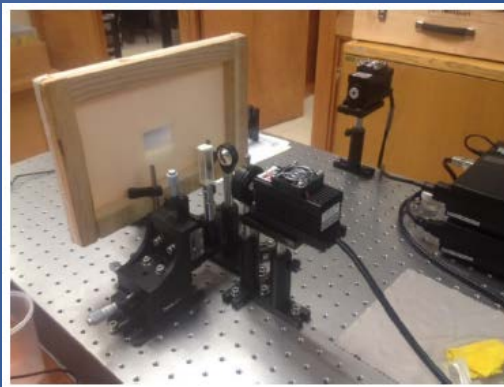


The Abdus Salam
International Centre
for Theoretical Physics

Winter College on Optics: Advanced Optical Techniques for Bio-Imaging
February 13-24, 2017

OUTLINE:

1. THERMAL WAVE PHYSICS. PHOTOTHERMAL TECHNIQUES. THERMAL CHARACTERIZATION OF MATERIALS
2. THE PHOTOTHERMAL BEAM AND MULTIBEAM DEFLECTION TECHNIQUES
3. THE PHOTOTHERMAL SHADOWGRAPH METHOD

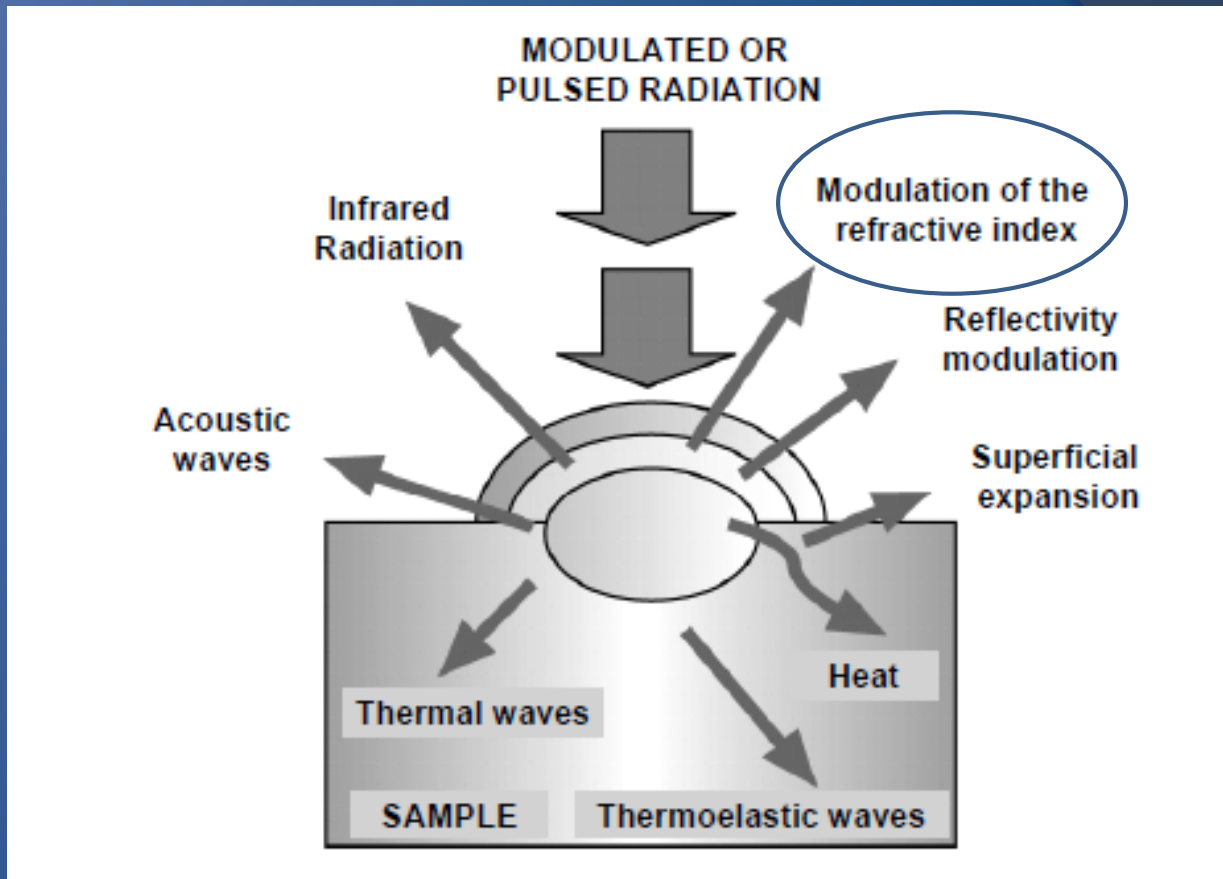


1st PART:

THERMAL WAVE PHYSICS

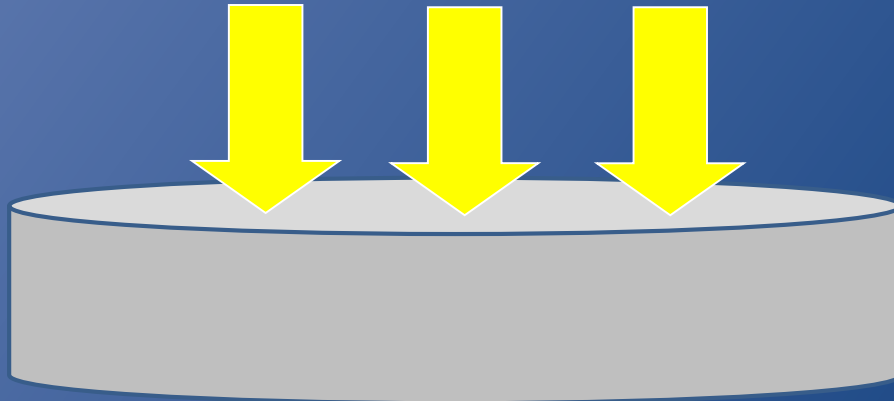
THE PHOTOTHERMAL TECHNIQUES

THERMAL CHARACTERIZATION OF MATERIALS



PRINCIPLES OF PHOTOTHERMAL TECHNIQUES

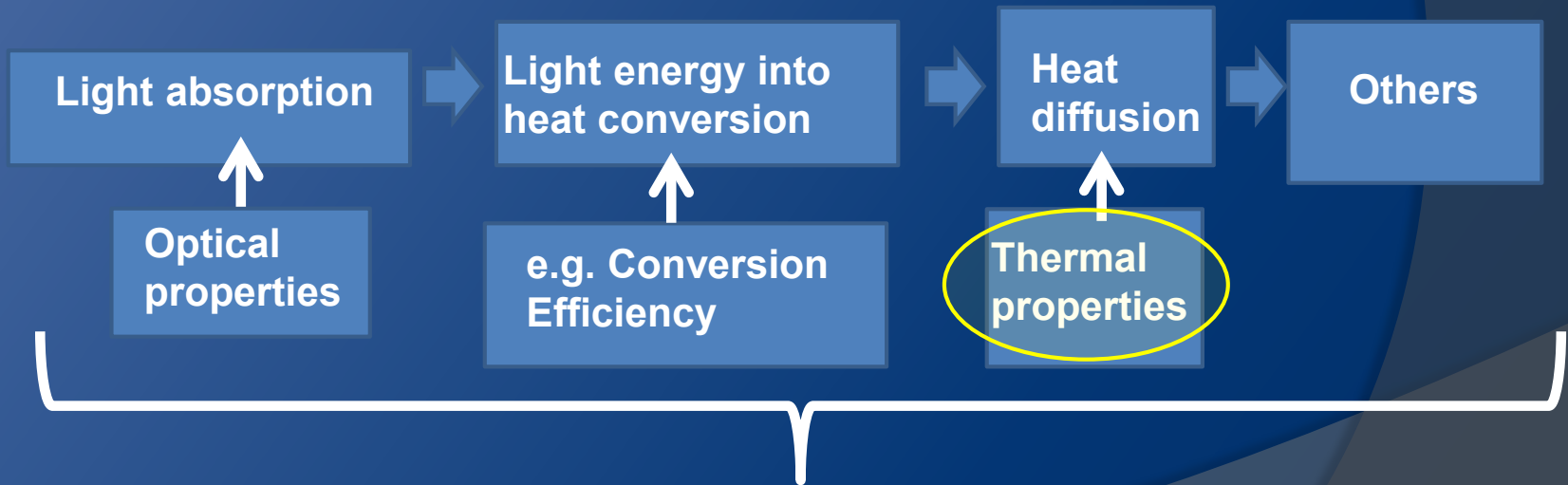
Intensity periodical modulated light beam



DETECTION SYSTEM



Mechanisms involved in the generation of the photothermal signal



MOTIVATION:

WHY TO USE SUCH EFFECT FOR MATERIALS (e.g. thermal) CHARACTERIZATION

Which thermal properties?

Thermal conductivity [W/mK]

Thermal diffusivity [m²/s]

$$\alpha = k / \rho c$$

specific heat [J / kg K]

mass density [kg/m³]

$$C = \rho c$$

Specific (volumen) heat capacity [J / m³ K]

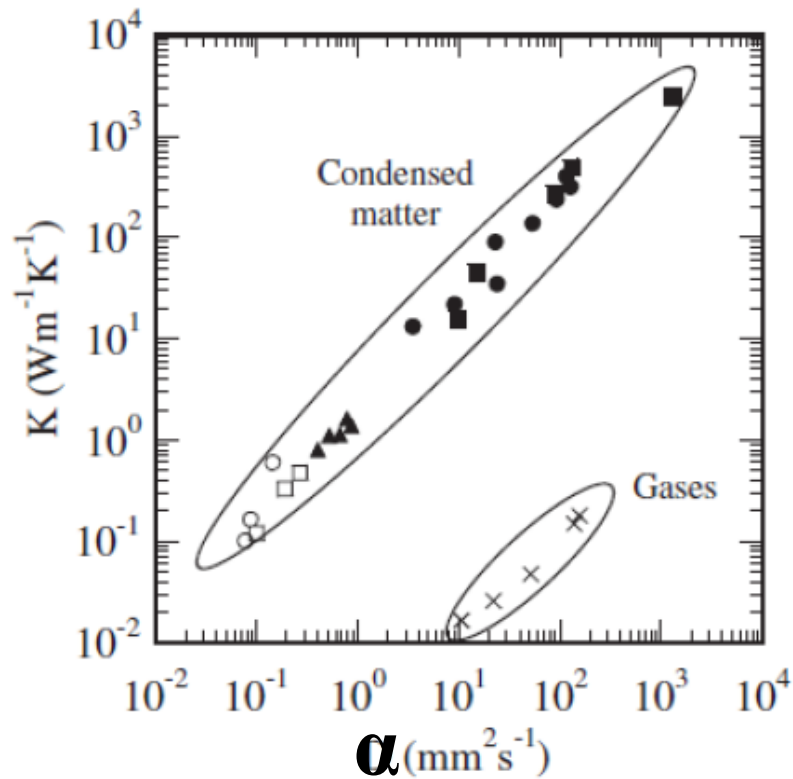
$$\varepsilon = k / \alpha^{1/2} = (Ck)^{1/2}$$

Thermal effusivity [Js^{1/2} m⁻² K⁻¹]

Homogeneous heat diffusion equation

$$\nabla^2 T - \frac{1}{\alpha} \frac{\partial T}{\partial t} = 0$$

Thermal diffusivity becomes the relevant parameter in non-stationary problems



Closed circles: metals; squares: ceramics; triangles: glasses; open squares: polymers; open circles: liquids; crosses: gases

$$\text{Slope} \sim \rho C \sim 3 \times 10^6 \text{ Jm}^{-3} \text{ K}^{-1}$$

Thermal Waves and Their Properties

[Almond and Patel, 1996] Almond, D. P. and Patel, P. M. 1996, "Photothermal Science and Techniques" in "Physics and its Applications, 10", E.R. Dobbsand and S.B. Palmer (Eds), Chapman and Hall, London.

International Journal of Thermal Sciences 98 (2015) 202–207

Isotropic and homogeneous semi-infinite solid + Superficial uniform light absorption (1D) + $\eta = 1$ + $R=0$ + neglecting heat losses (with H)

$$\frac{\partial^2 T(x,t)}{\partial x^2} - \frac{1}{\alpha} \frac{\partial T(x,t)}{\partial t} = 0, \quad x > 0, \quad t > 0$$

HDE

$$-k \left. \frac{\partial T(x,t)}{\partial x} \right|_{x=0} = \frac{I_0}{2} \text{Re}[(1 + \exp(i\omega t))]$$

BC

$$\frac{\partial^2 \theta(x,t)}{\partial x^2} - q^2 \theta(x) = 0$$

$$T(x,t) = \theta(x) \exp(i\omega t) \rightarrow$$

$$q = \sqrt{\frac{i\omega}{\alpha}} = \frac{(1+i)}{\mu}$$

$$\mu = \sqrt{\frac{2\alpha}{\omega}}$$

$$-k \left. \frac{\partial \theta(x,t)}{\partial x} \right|_{x=0} = \text{Re} \left[\frac{I_0}{2} \exp(i\omega t) \right]$$

Wave number Thermal diffusion length

$$T(x,t) = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp(-qx) \exp\left[-i\left(\omega t + \frac{\pi}{4}\right)\right] = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp\left(-\frac{x}{\mu}\right) \exp\left[-i\left(\frac{x}{\mu} + \omega t + \frac{\pi}{4}\right)\right]$$

Thermal Wave Equation

Thermal properties determination is possible !

$$\varepsilon = k/\alpha^{1/2} = (Ck)^{1/2}$$

$$C = \rho c$$

Thermal effusivity $\sim k$ because the almost constancy of C

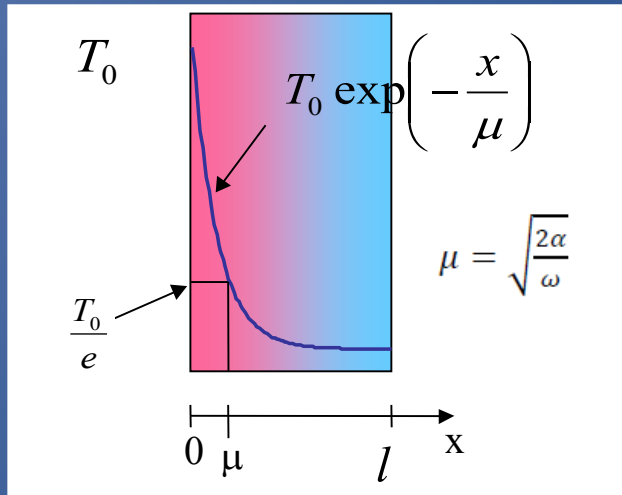
THERMAL WAVES AND THEIR PROPERTIES

$$T(x, t) = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp(-qx) \exp\left[-i\left(\omega t + \frac{\pi}{4}\right)\right] = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp\left(-\frac{x}{\mu}\right) \exp\left[-i\left(\frac{x}{\mu} + \omega t + \frac{\pi}{4}\right)\right]$$

Amplitude

Phase

$$\Delta\phi = x/\mu + \pi/4$$



Thermal diffusion length

$$Z_t = \frac{T(x=0, t) - T_{amb}}{-k \frac{dT(x, t)}{dx} \Big|_{x=0}}$$

$$Z_t = \frac{1-i}{\varepsilon\sqrt{\omega}} = \frac{1}{\varepsilon\sqrt{\omega}} \exp\left(-i\frac{\pi}{4}\right)$$

Thermal impedance

$$T(x, t) = \frac{I_0}{2} Z_t \exp\left(-\frac{x}{\mu}\right) \cos\left(\frac{x}{\mu} + \omega t\right)$$

$$\lambda = 2\pi\mu \quad \text{Wave-length}$$

$$v_f = f\lambda = (\omega/2\pi)(2\pi\mu) = \mu\omega = (2\alpha\omega)^{1/2}$$

Phase velocity

$$v_g = 2v_f$$

Group velocity

THERMAL CHARACTERIZATION BY SLOPE METHOD

$$T(x, t) = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp(-qx) \exp\left[-i\left(\omega t + \frac{\pi}{4}\right)\right] = \frac{I_0}{2\varepsilon\sqrt{\omega}} \exp\left(-\frac{x}{\mu}\right) \exp\left[-i\left(\frac{x}{\mu} + \omega t + \frac{\pi}{4}\right)\right]$$

Amplitude

Phase

$$\mu = \sqrt{\frac{2\alpha}{\omega}}$$

$$\Delta\phi = x/\mu + \pi/4$$

LOG (AMPLITUDE $\times \omega^{1/2}$) VERSUS $\omega^{1/2}$
 PHASE VERSUS $\omega^{1/2}$ } STRAIGHT LINE WITH SLOPE = $L/(2\alpha)^{1/2}$

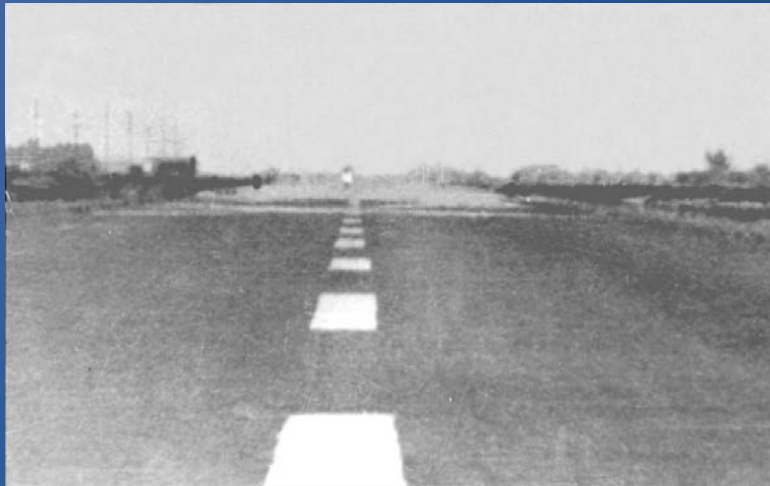
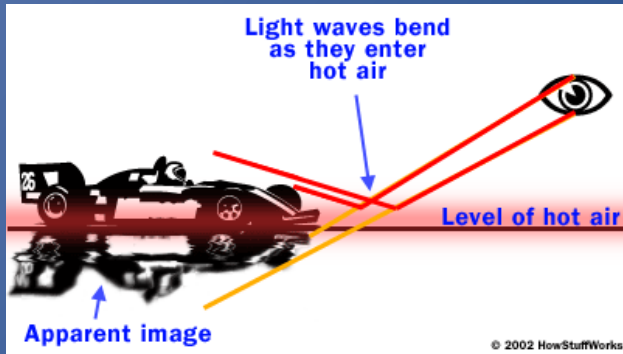
FREQUENCY DEPENDENT INSTRUMENTAL FACTOR
 CAN AFFECT BOTH AMPLITUDE AND PHASE
 → NORMALIZATION PROCEDURES, EXPERIMENTAL ARTIFACTS, ETC

LOG (AMPLITUDE) VERSUS L
 PHASE VERSUS L } STRAIGHT LINE WITH SLOPE = $(\omega/2\alpha)^{1/2}$

STRAIGHTFORWARD PROCEDURES

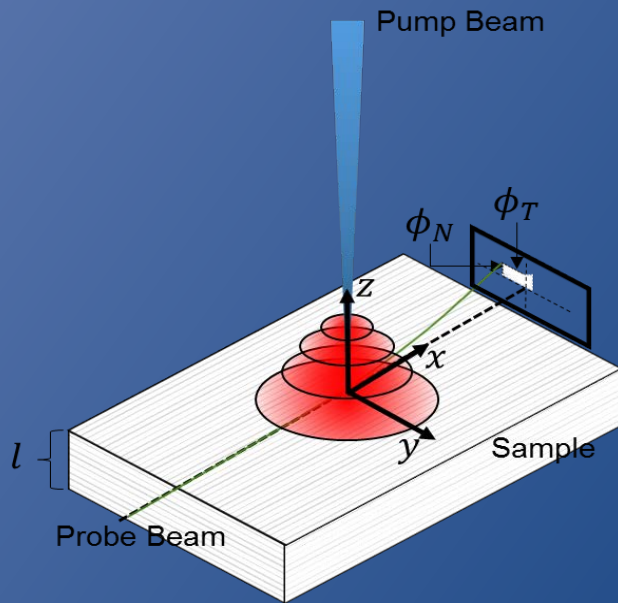
**2ND PART:
THE PHOTOTHERMAL BEAM AND
MULTIBEAM DEFLECTION TECHNIQUES**

MIRAGE EFFECT



BEAM DEFLECTION TECHNIQUE

$$n \propto \frac{dn}{dT} T_\gamma$$



$$\mu_i = \sqrt{\frac{\alpha_i}{\pi f}}$$

$$(\mu_\gamma \ll \mu_s)$$

$$T_\gamma(y) = \frac{P_0}{4\pi k_s} \int_0^\infty \delta J_0(\delta y) \exp\left(-\frac{(\delta a)^2}{4}\right) \frac{1}{\beta_s} \times \Psi \, d\delta$$

$$\Psi = \frac{1 + \exp(-2\beta_s l)}{1 - \exp(-2\beta_s l)} \exp(-z\beta_\gamma)$$

where P_0 is the exciting beam power, a is the beam radius defined at $1/e^2$ of the beam's intensity, k_s is the sample's thermal conductivity, J_0 denotes the Bessel function of zero order, sub-indexes γ and s represent the medium and the sample respectively and $\beta_i = \delta^2 + \frac{i\omega}{\alpha_i}$ ($i = \gamma, s$), with δ as the integration variable

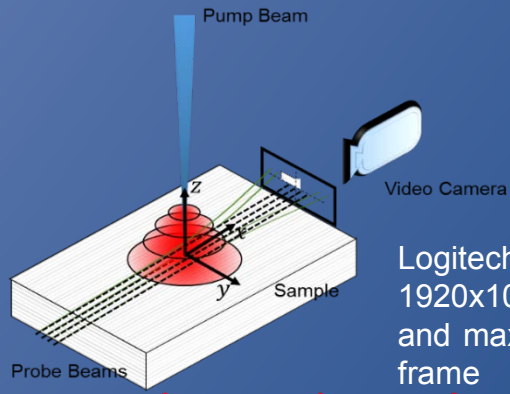
$$\begin{aligned} \phi_T &= -\frac{1}{n} \frac{dn}{dT} \frac{P_0}{2\pi K_s} e^{i\omega t} \int_0^\infty \delta \sin(\delta y) e^{-\frac{(\delta a)^2}{4}} \beta_s^{-1} \Psi d\delta \hat{k} \\ \phi_N &= -\frac{1}{n} \frac{dn}{dT} \frac{P_0}{2\pi K_s} e^{i\omega t} \int_0^\infty \beta_\gamma \cos(\delta y) e^{-\frac{(\delta a)^2}{4}} \beta_s^{-1} \Psi d\delta \hat{j} \end{aligned}$$

where n is the diffraction index and l is the sample's length in the z direction.

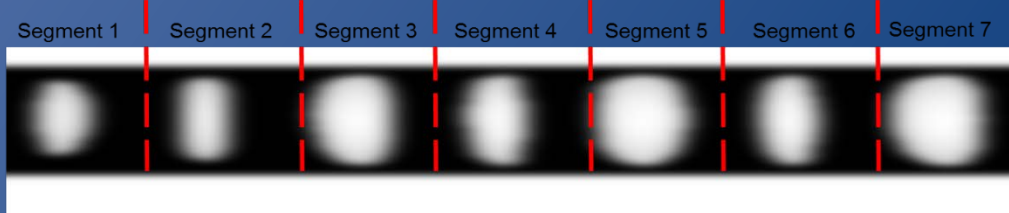
Phase of ϕ_T versus pump to probe offset \rightarrow straightline with slope $m = (\pi f / \alpha_s)^{1/2}$

A. Salazar, A. Sanchez-Lavega, and J. Fernandez, "Theory of thermal diffusivity determination by the mirage technique in solids," *J. Appl. Phys.*, vol. 65, p. 4150, 1989.

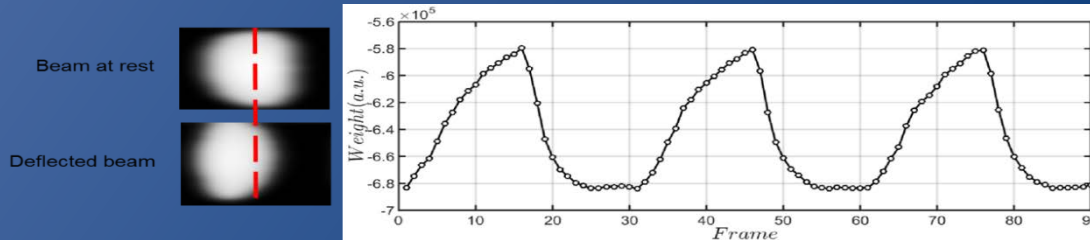
MULTIBEAM DEFLECTION TECHNIQUE



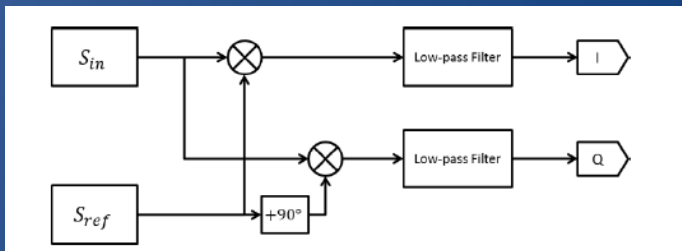
Logitech C920 Webcam
1920x1080 pixels, 8 bit pixel sensitivity
and maximum frame rate of 20 fps at full
frame



Video is segmenting into as many sections as beams there are



Comparison between the weight of pixels values to the right with those to the left of the vertical section midline (software implementation of a QPD)



Lock-in
amplification

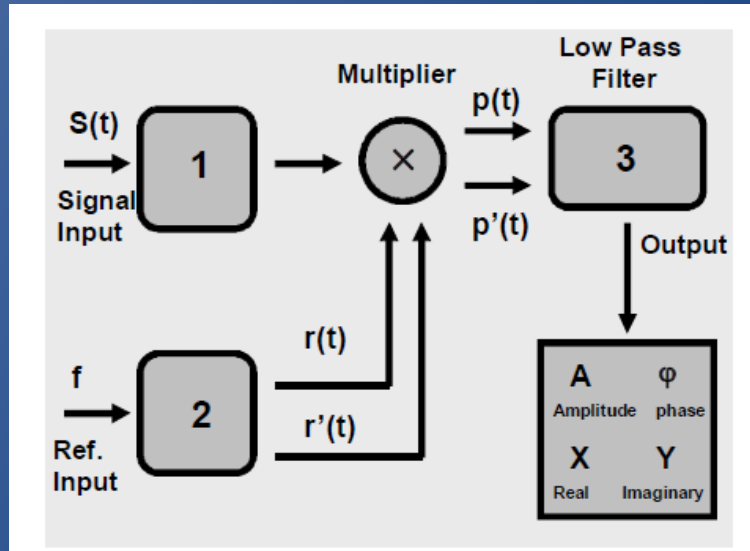
$$\varphi = \tan^{-1} \left(\frac{Q}{I} \right)$$

$$A = \frac{1}{2} \sqrt{I^2 + Q^2}$$

LIA in a Nut Shell

$S = A \cos(\omega t + \varphi) + n$
 signal to be measured

A: signal amplitude;
 φ : signal phase
 $\omega = 2\pi f$: angular frequency
 n: noise at f



$$r = 2 \cos(\omega t)$$

$$r' = 2 \sin(\omega t)$$

$$p = S \times r = A \cos(\varphi) + A \cos(2\omega t + \varphi) + 2n \cos(\omega t)$$

$$p' = S \times r' = A \sin(\varphi) + A \sin(2\omega t + \varphi) + 2n \sin(\omega t)$$

X and Y real (in-phase) and imaginary (quadrature) parts of the complex number $A \exp(i\varphi)$; $i = (-1)^{1/2}$

$$A = (X^2 + Y^2)^{1/2}$$

$$\varphi = \text{atan}(Y/X)$$

$$X = A \cos(\varphi)$$

$$Y = A \sin(\varphi)$$

Lat. Am. J. Phys. Educ. Vol.3, No. 3, Sept. 2009

Examples

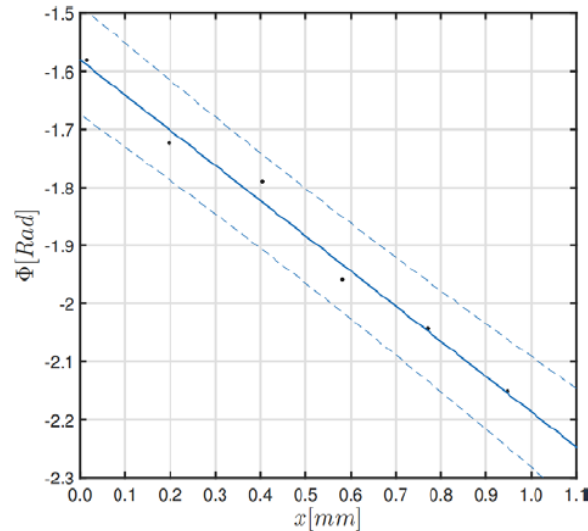
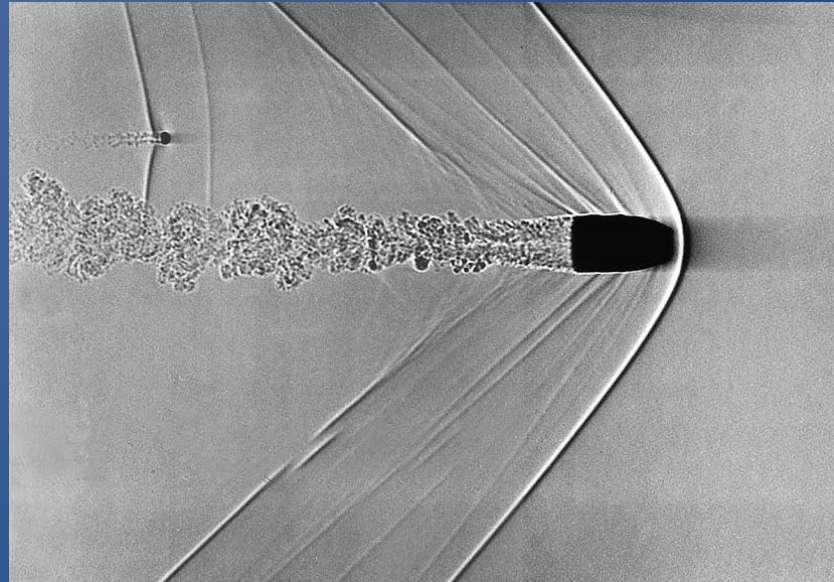


Figure 6 Experimental result for a *CdTe* sample, modulation frequency is 4 Hz. The dots show experimental data, the solid line the best linear fit and the dash lines show the 95% confidence interval for said fit.

Sample	Table 1 Results	
	Measured α_s -value	α_s -literature value
AISI 1018 low carbon steel	$(1.3 \pm 0.3) \times 10^{-5} \text{ m}^2/\text{s}$	$1.33 \times 10^{-5} \text{ m}^2/\text{s}$ [8]
D2 high carbon steel	$(3.9 \pm 0.6) \times 10^{-6} \text{ m}^2/\text{s}$	$4.0 \times 10^{-6} \text{ m}^2/\text{s}$ [9]
CdTe	$(3.4 \pm 1.1) \times 10^{-6} \text{ m}^2/\text{s}$	$3.35 \times 10^{-6} \text{ m}^2/\text{s}$ [10]

**3RD PART:
THE PHOTOTHERMAL SHADOWGRAPH METHOD**



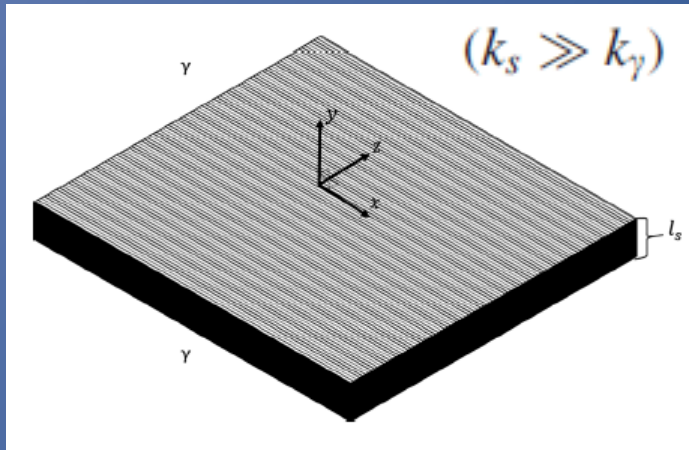
Shadowgraph technique allows to visualize refractive index perturbations in optically transparent or semitransparent media. It is widely used in fluid mechanics, aerodynamics, convection studies, among others

→ Motivation: Can shadowgraph method detect refractive index perturbations in photothermal experiments like beam deflection?

G. S. Settles, *Schlieren and Shadowgraph Techniques* (Springer, Berlin, Heidelberg, 2001).

P. K. Panigrahi and K. Muralidhar, *Schlieren and Shadowgraph Methods in Heat and Mass Transfer* (Springer, 2012).

GOVERNING EQUATIONS



$$T_\gamma(x, y) = \frac{P_0}{4\pi k_s} \int_0^\infty \zeta J_0(\zeta x) \exp\left(-\frac{(\zeta a)^2}{8}\right) \frac{1}{\beta_s} \times \frac{1 + \exp(-2\beta_s l_s)}{1 - \exp(-2\beta_s l_s)} \exp(-y\beta_\gamma) d\zeta,$$

where P_0 is the excitation beam power, a is the beam radius defined at $1/e^2$ of the beam intensity, k_s is the sample's thermal conductivity, J_0 denotes the Bessel function of zero order, sub-indexes γ and s represent the medium and the sample, respectively, $\beta_i = \zeta^2 + \frac{i\omega}{\alpha_i}$ ($i = \gamma, s$), and α is the thermal diffusivity. The thermal diffusion length can be defined as $\mu_i = \sqrt{\frac{\alpha_i}{\pi f}}$.

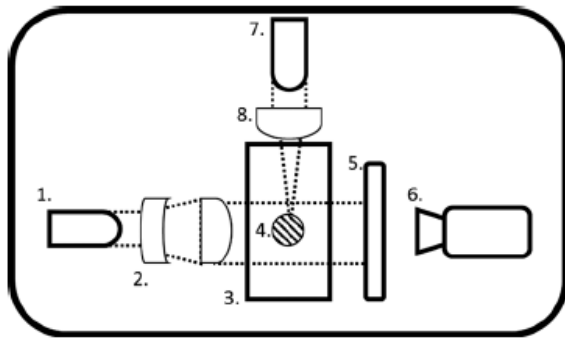


FIG. 4. Experimental configuration. (1) Probe beam, (2) collimating lenses, (3) cell, (4) sample, (5) projection screen, (6) camera, (7) pump beam, (8) focusing lens.

$$n \propto \frac{dn}{dT} T_\gamma$$

$$\frac{I_0 - I_s}{I_s} = (L \times D) \nabla^2 \log(n(x, y))$$

I_0 probe beam intensity; I_s probe beam intensity at projection screen; L distance between sample and screen; D dimension parameter; n refractive index

COMPUTATIONAL SIMULATIONS

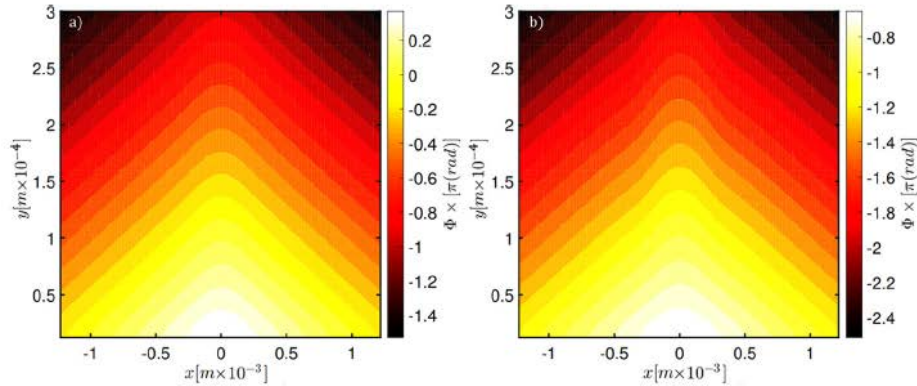


FIG. 2. Simulation results for $\alpha_s = 1.0 \times 10^{-5} \text{ [m}^2/\text{s}]$ and 8 Hz modulation frequency. (a) Thermally thin and (b) thermally thick sample.

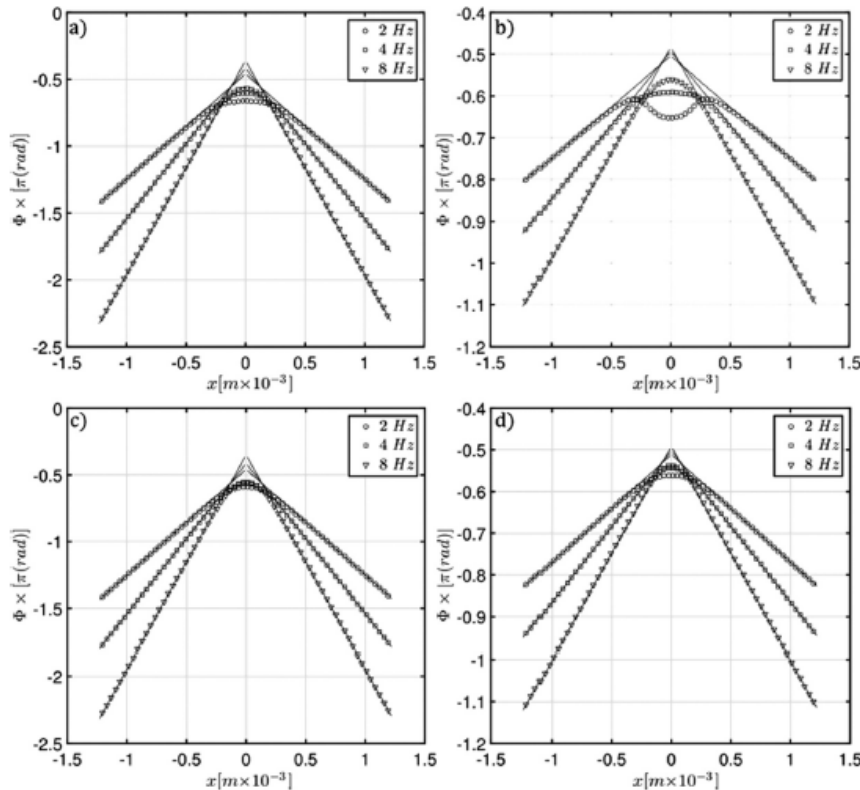
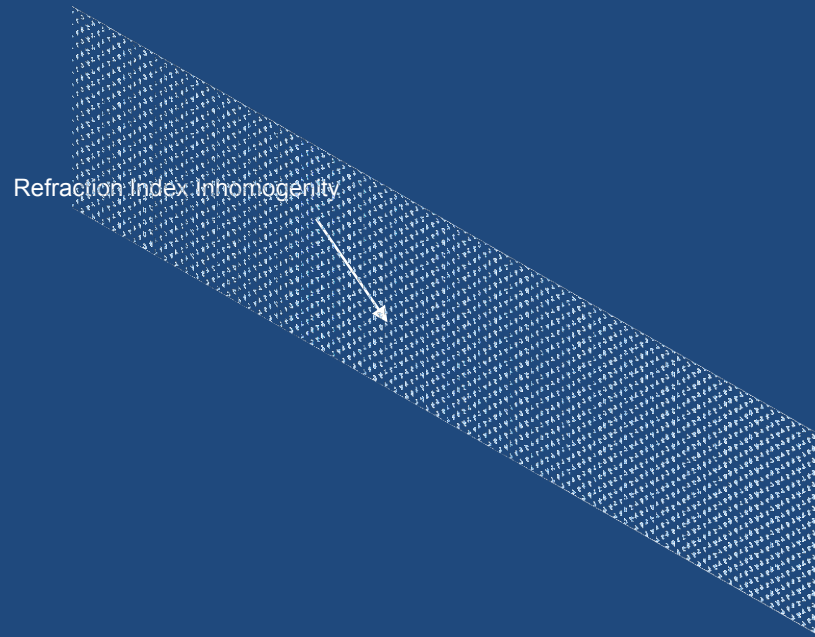


TABLE II. Simulation results.

	$\alpha_s \left(\frac{\text{m}^2}{\text{s}} \right)$	f (Hz)	$m \left(\frac{\text{rad}}{\text{m}} \right)$	R^2	$\hat{\alpha}_s \left(\frac{\text{m}^2}{\text{s}} \right)$	ϵ (%)
Thermally thin	1.00×10^{-6}	2	2500	1	1.00×10^{-6}	0.5
		4	3542	1	1.00×10^{-6}	0.1
		8	5012	1	1.00×10^{-6}	<0.1
	1.00×10^{-5}	2	810	1	0.96×10^{-5}	4.0
		4	1137	1	0.97×10^{-5}	3.1
		8	15848	1	0.98×10^{-5}	2.0
Thermally thick	1.00×10^{-6}	2	2484	1	1.02×10^{-6}	1.8
		4	3538	1	1.00×10^{-6}	0.4
		8	5019	1	9.97×10^{-7}	0.3
	1.00×10^{-5}	2	776	1	1.04×10^{-5}	4.3
		4	1114	1	1.01×10^{-5}	1.3
		8	1585	1	1.00×10^{-5}	0.1

Objective: to estimate thermal diffusivity from slope and to obtain the estimation error by comparing it with the actual value used for the simulation



EQUIPMENT

NIR



THERMOGRAPHIC CAMERA FLIR SC2500 NIR
(0.9 – 1.7) μm 320x256 pixel InGaSb, frame rate 340 Hz
(WITH LOCK-IN ON BOARD FACILITIES)

PROBE LASER : 905 nm DIODE LASER

PUMP LASER : 445 nm 250 mW (nominal) DL

SAMPLE PLACED WITHIN A 1 cm^3 CELL AND INMERSED IN ACETONITRILE (HIGH $d\eta/Dt$)

VISIBLE



WEB CAM LOGITECH C920 FULL HS CMOS

PROBE LASER : 630 nm DIODE LASER

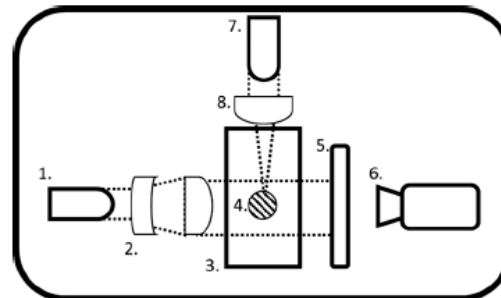


FIG. 4. Experimental configuration. (1) Probe beam, (2) collimating lenses, (3) cell, (4) sample, (5) projection screen, (6) camera, (7) pump beam, (8) focusing lens.

NIR RESULTS

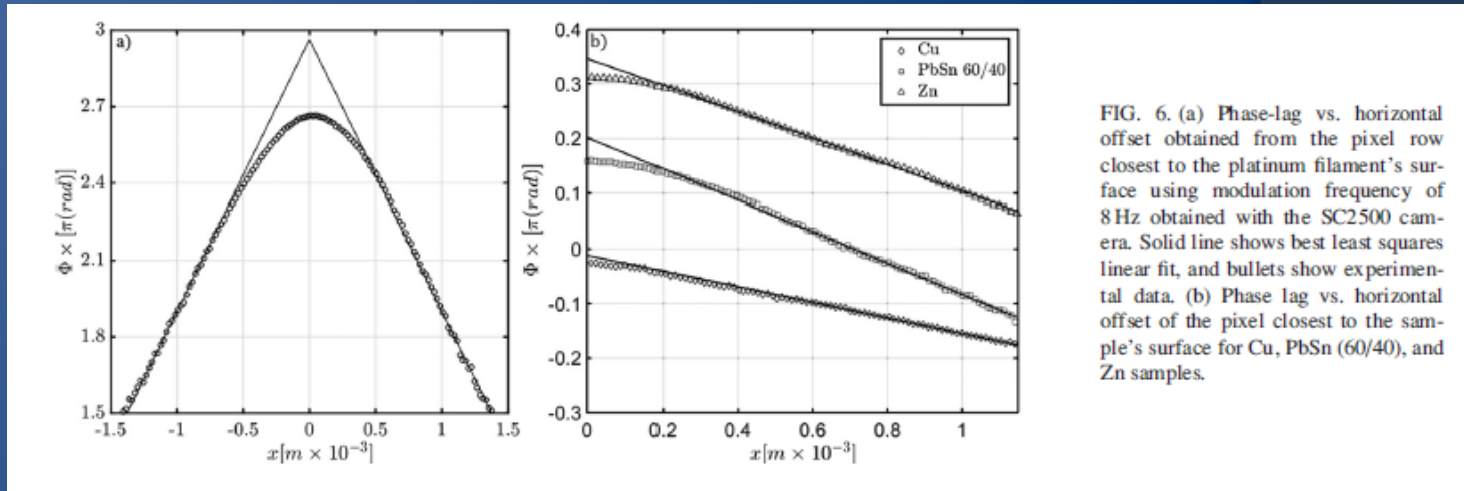
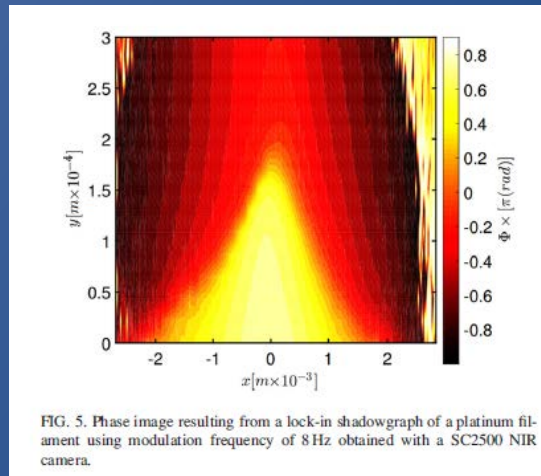


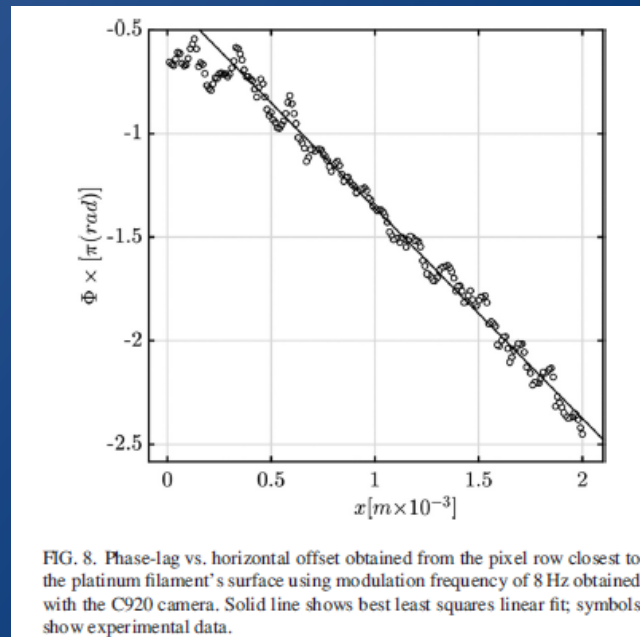
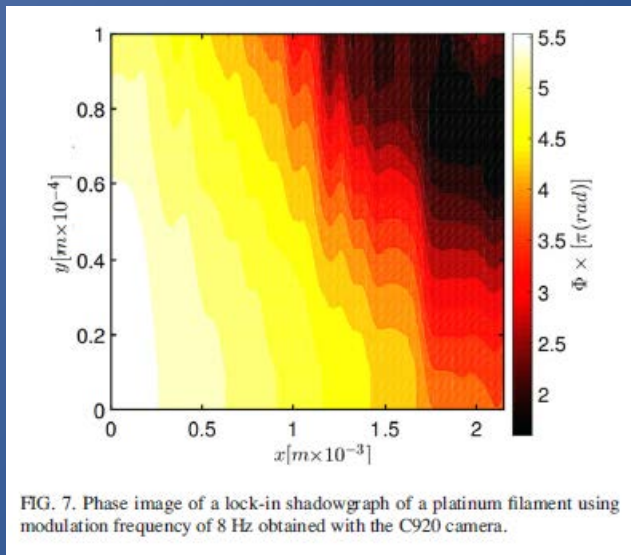
TABLE III. Results.

Material	$\alpha_s \left(\frac{\text{m}^2}{\text{s}} \right)$ measured by shadowgraph	$\alpha_s \left(\frac{\text{m}^2}{\text{s}} \right)$ literature
Copper	$(1.18 \pm 0.11) \times 10^{-4}$	1.17×10^{-4} (Ref. 21)
Platinum	$(2.36 \pm 0.10) \times 10^{-5}$	2.52×10^{-5} (Ref. 21)
Zinc	$(4.24 \pm 0.16) \times 10^{-5}$	4.16×10^{-5} (Ref. 21)
PbSn	$(3.03 \pm 0.10) \times 10^{-5}$	3.34×10^{-5} (Ref. 22)
Solder (40/60)		

J. Appl. Phys. 119, 164902 (2016)

VISIBLE RESULTS

C920-WEBCAM + DIGITAL LOCK-IN PIXEL BY PIXEL DATA PROCESSING



$$\alpha = (2.44 \pm 0.1) \times 10^{-5} \text{ m}^2/\text{s}$$

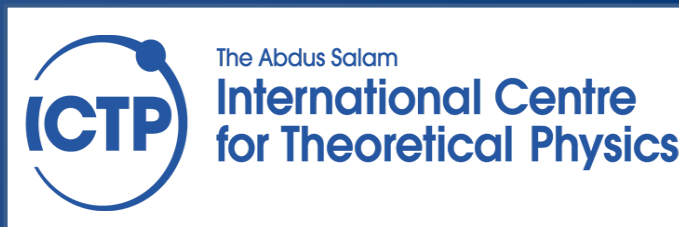
CONCLUSIONS:

THE PHOTOTHERMAL LOCK-IN SHADOWGRAPH METHOD WAS IMPLEMENTED FOR THE FIRST TIME AND VALIDATED BY THEORETICAL AND EXPERIMENTAL RESULTS.

HIGHLY SPECIALIZED HARDWARE IS NOT REQUIRED FOR THE TECHNIQUE TO WORK; A SIMPLE WEBCAM CAN BE USED AS A SENSING ELEMENT → TECHNIQUE HIGHLY ACCESSIBLE, FOR EXAMPLE FOR TEACHING THERMAL WAVE PHYSICS

ACKNOWLEDGEMENTS

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Thank you!