

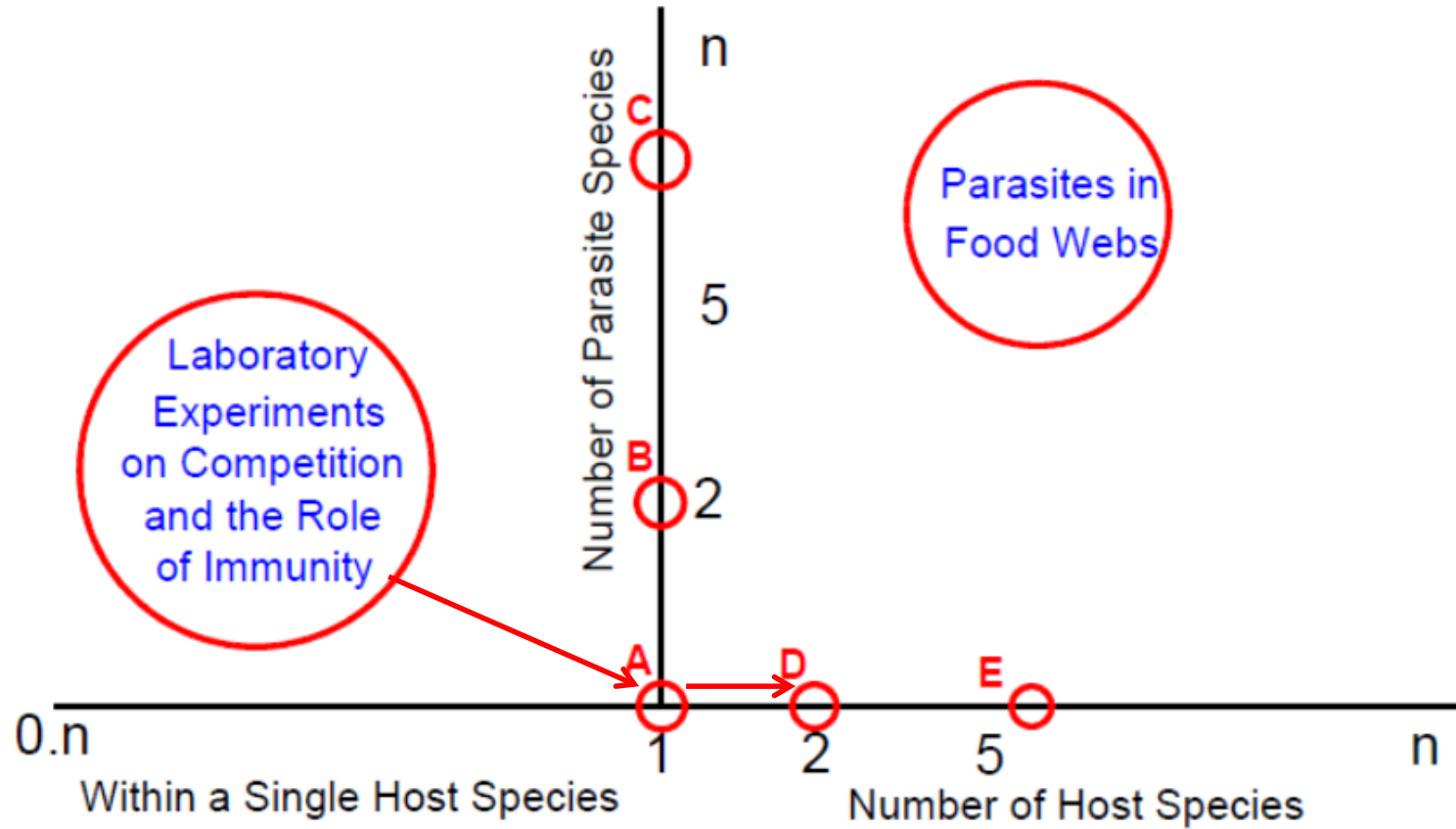
Pathogen with multiple hosts

Andy Dobson

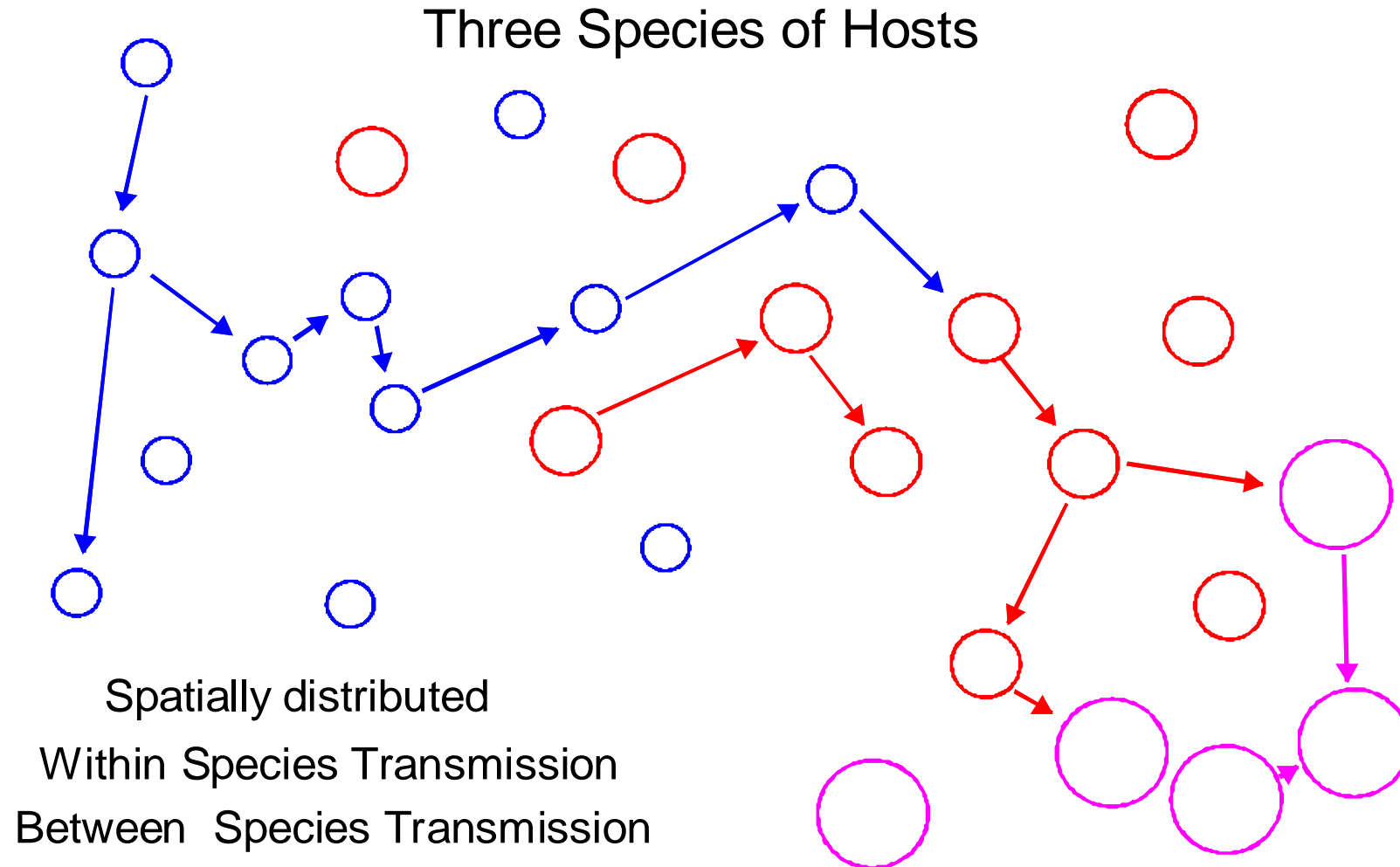
Deconstructing the Serengeti Foodweb:



Mathematical epidemiology has too limited a perspective.....!!



A cartoon of the talk.....



Rinderpest - Serengeti



Basic model structure..

Susceptibles

Allometric scaling of all birth and death rates

$$\frac{dS_i}{dt} = (b_i - d_i - \Delta_i(S_i + I_i))S_i - (\underbrace{\beta_{ii}I_i}_{\text{Within}} + \underbrace{\sum \beta_{ij}I_i}_{\text{Between}})S / (\sum_{j=1,n} N_n)^c$$

Infecteds

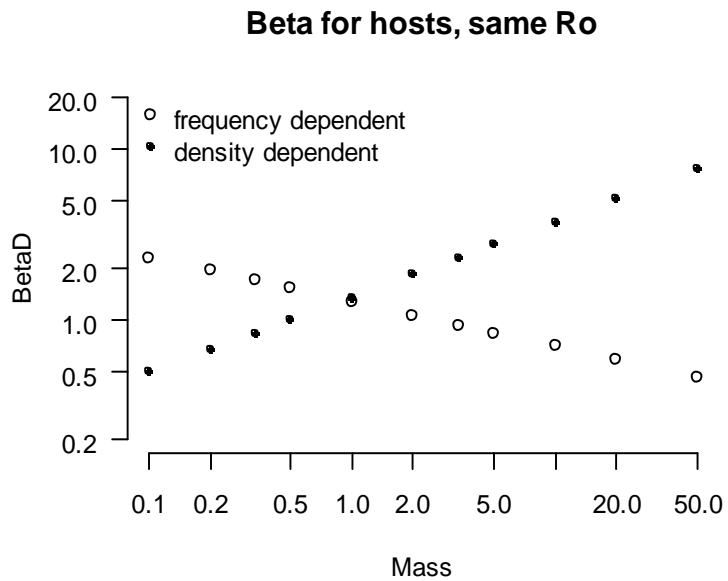
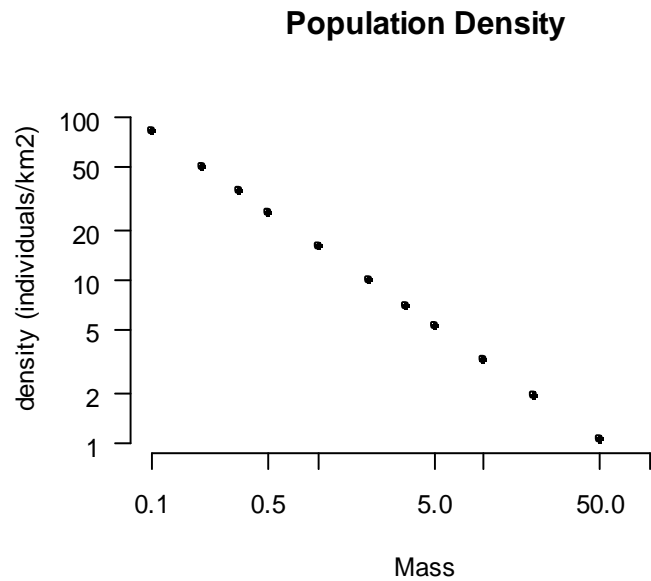
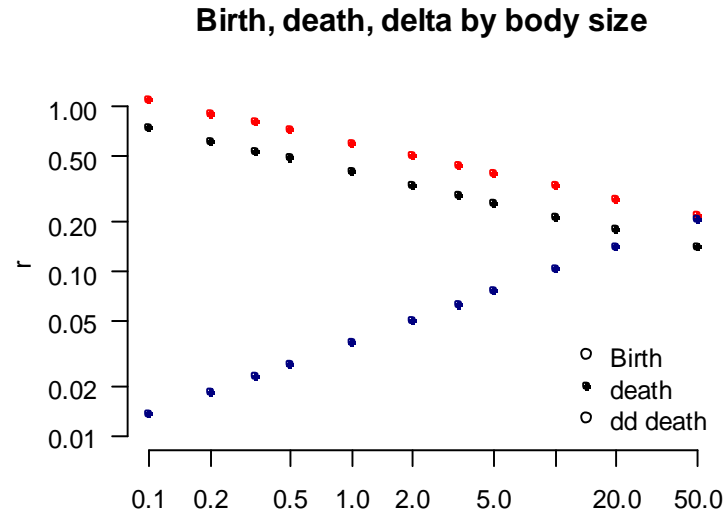
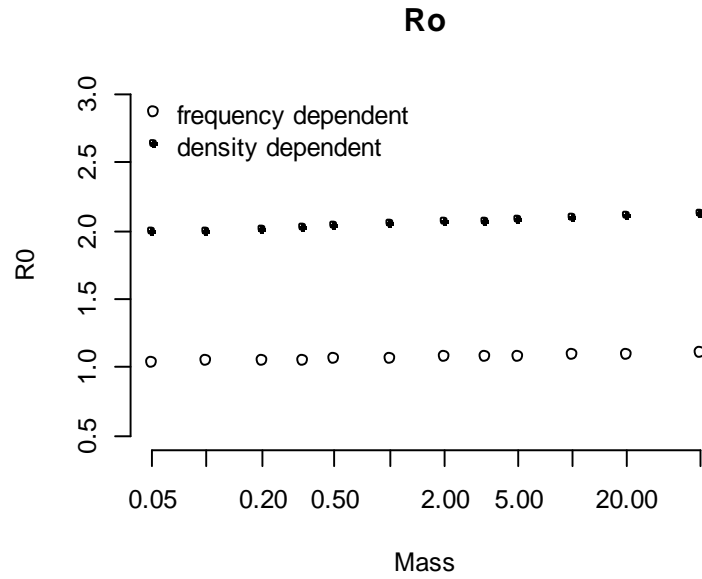
$$dI_i / dt = (\beta_{ii}I_i + \sum \beta_{ij}I_i)S / (\sum_{j=1,n} N_n)^c - d_i(1 + \alpha_i)I_i$$

Between species transmission

$$\beta_{ij} = c\sqrt{\beta_{ii}\beta_{jj}}$$

Scale virulence
as a proportion
of life expectancy

Underlying demography based on allometric scaling with body size (DeLeo and Dobson, Nature 1997)



Basic model structure..

Susceptibles

Allometric scaling of all birth and death rates

$$\frac{dS_i}{dt} = (b_i - d_i - \Delta_i(S_i + I_i))S_i - (\underbrace{\beta_{ii}I_i}_{\text{Within}} + \sum \underbrace{\beta_{ij}I_i}_{\text{Between}})S / (\sum_{j=1,n} N_n)^c$$

Infecteds

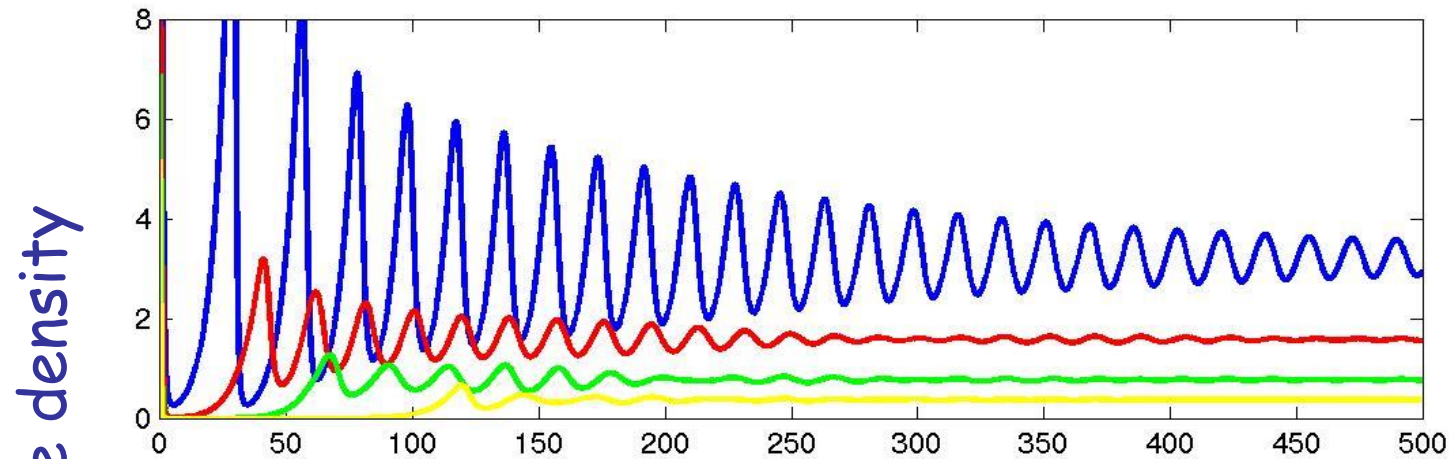
$$dI_i / dt = (\beta_{ii}I_i + \sum \beta_{ij}I_i)S / (\sum_{j=1,n} N_n)^c - d_i(1 + \alpha_i)I_i$$

Between species transmission

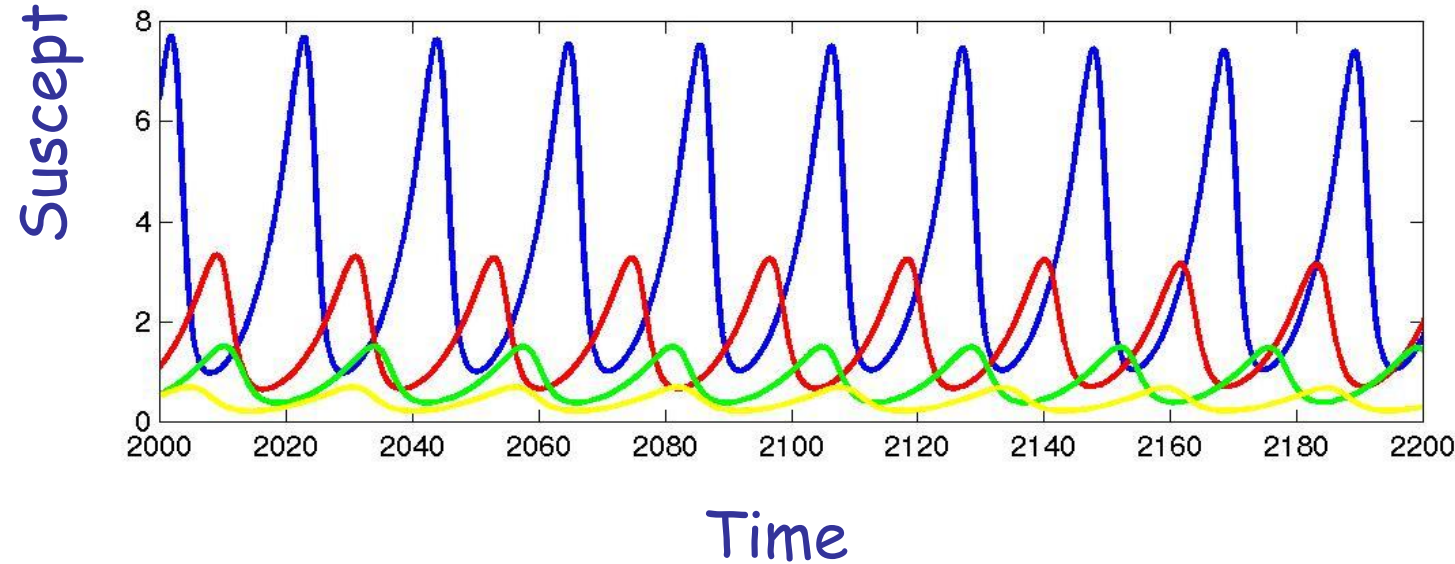
Scale virulence
as a proportion
of life expectancy

$$\beta_{ij} = c\sqrt{\beta_{ii}\beta_{jj}}$$

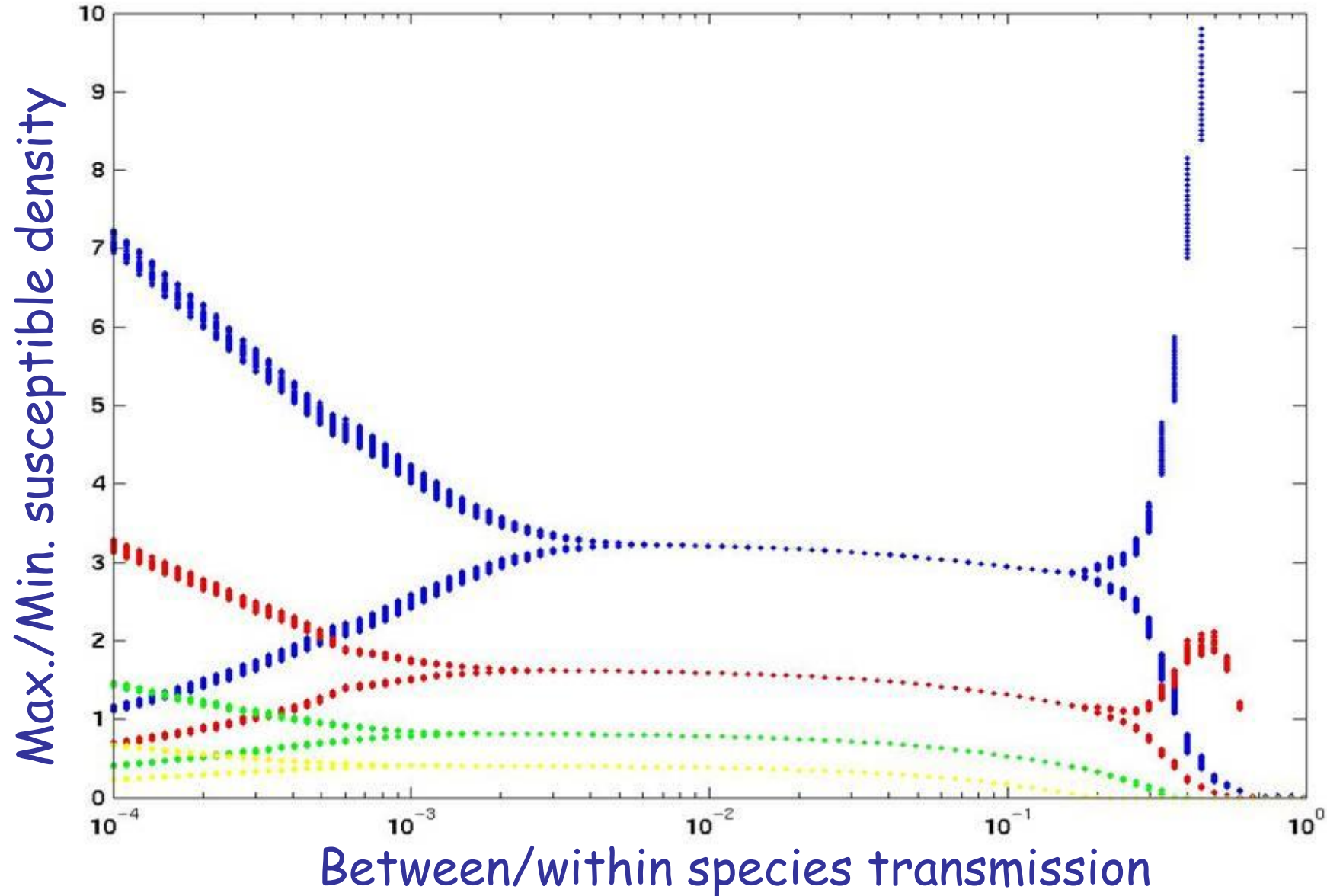
Buffering: dynamics in DD case



Between sps.
transmission

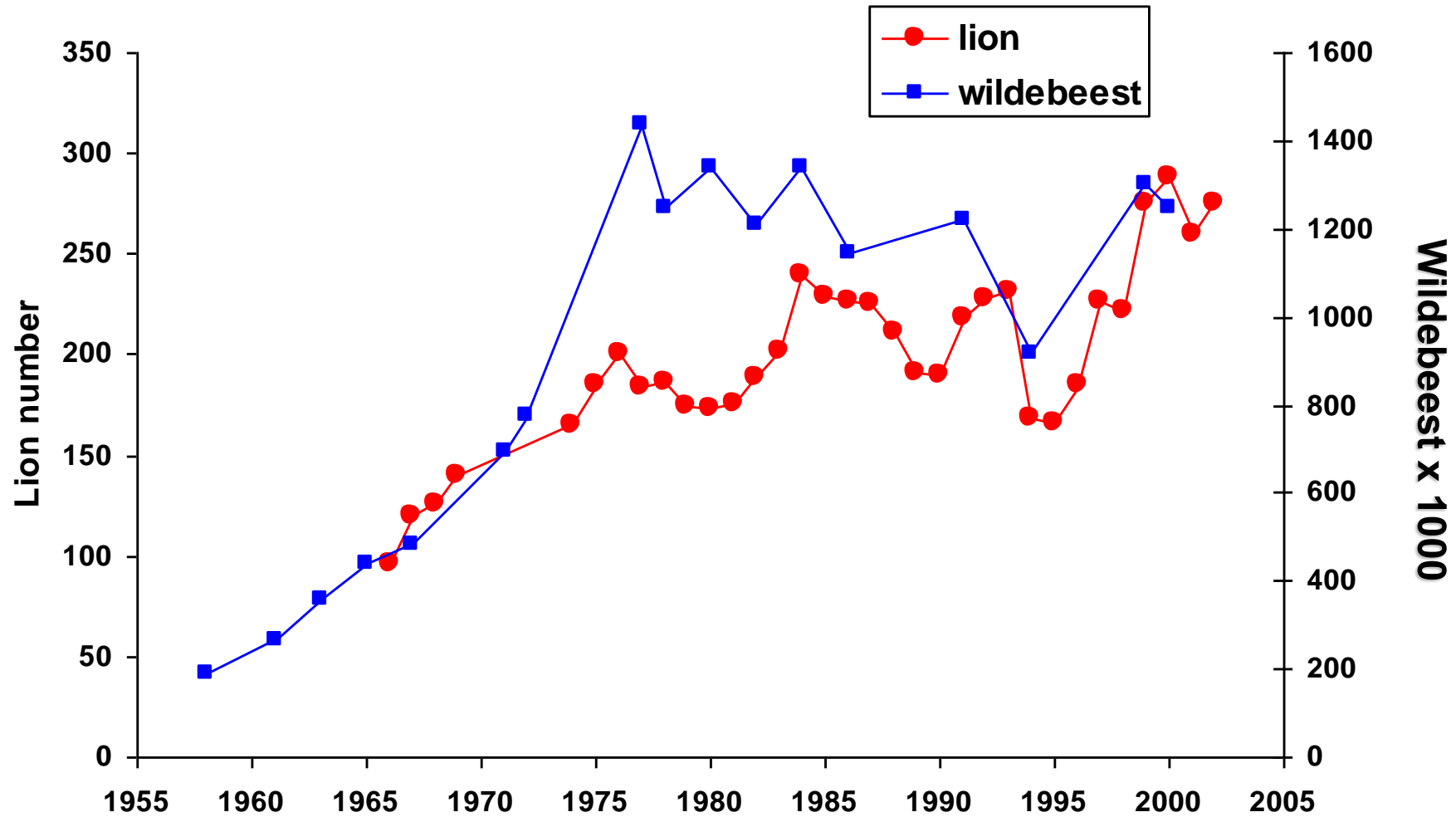


Buffering: dynamics in DD case





Serengeti woodland lion numbers



Lion data from C. Packer

Serengeti secrets : Vaccinating to Control Multiple Pathogens



Dynamics of viral pathogens in Serengeti

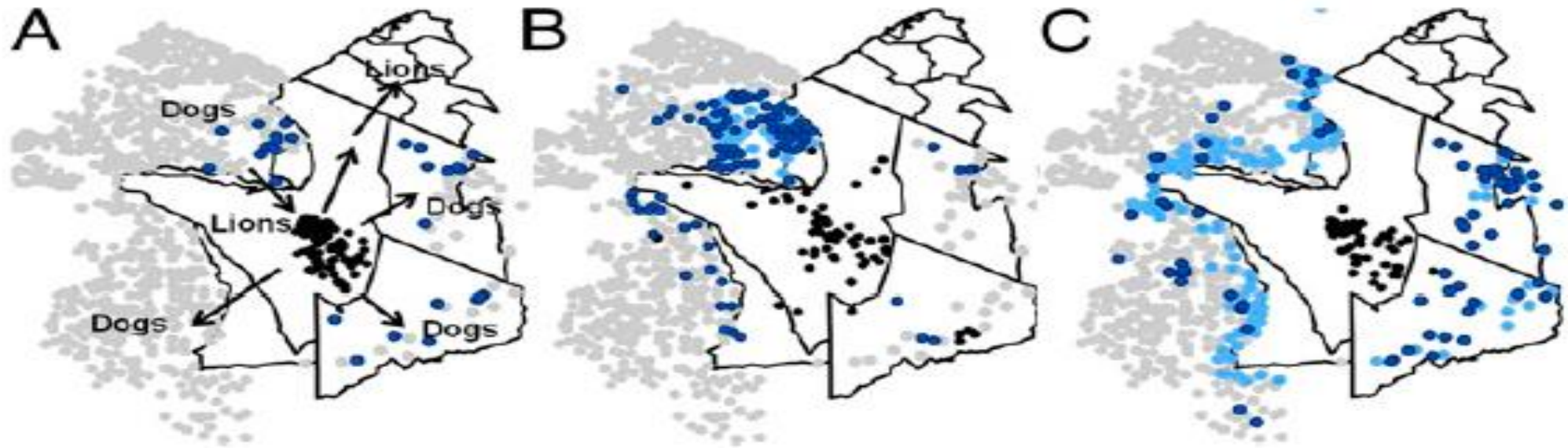
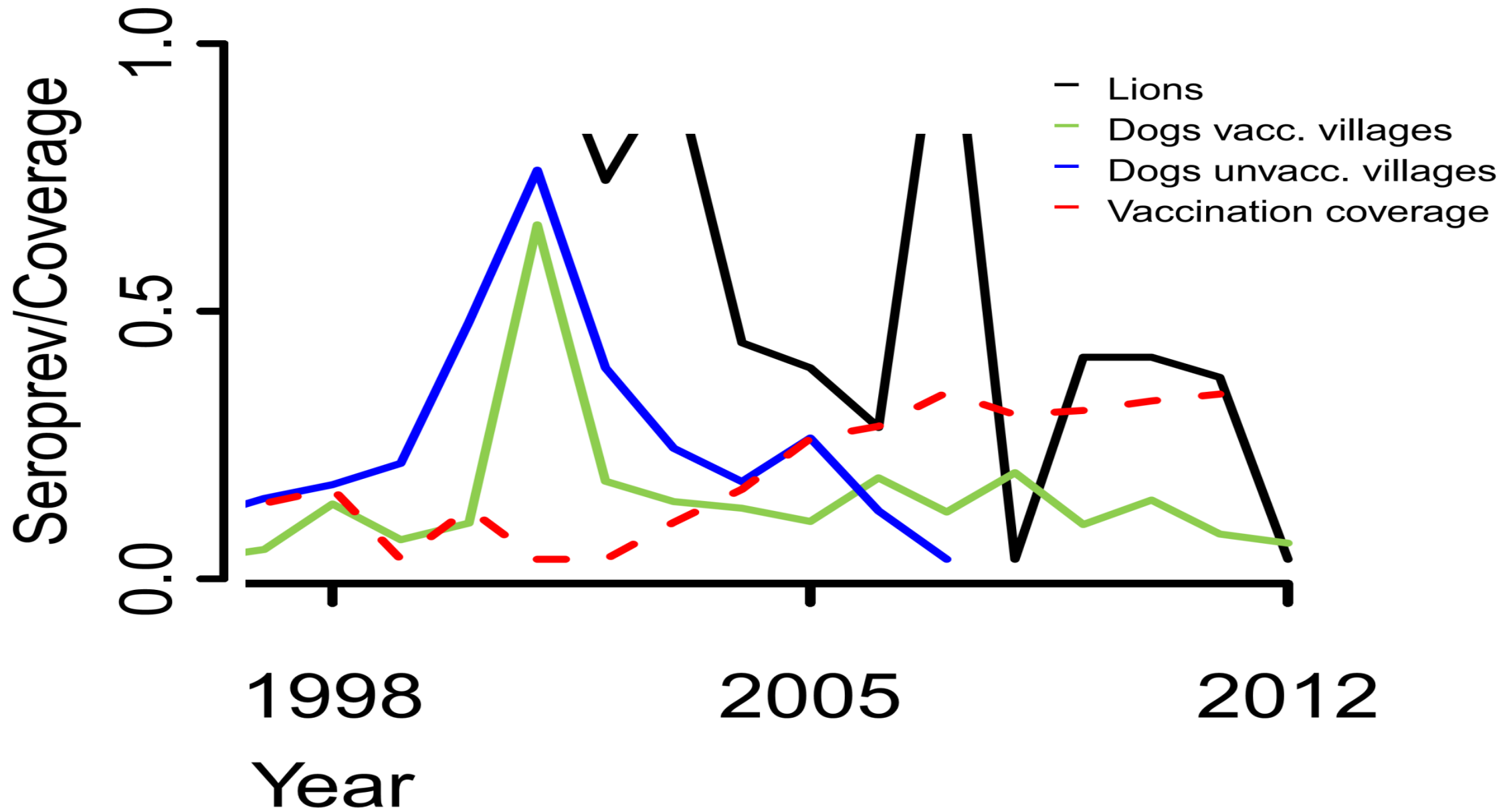
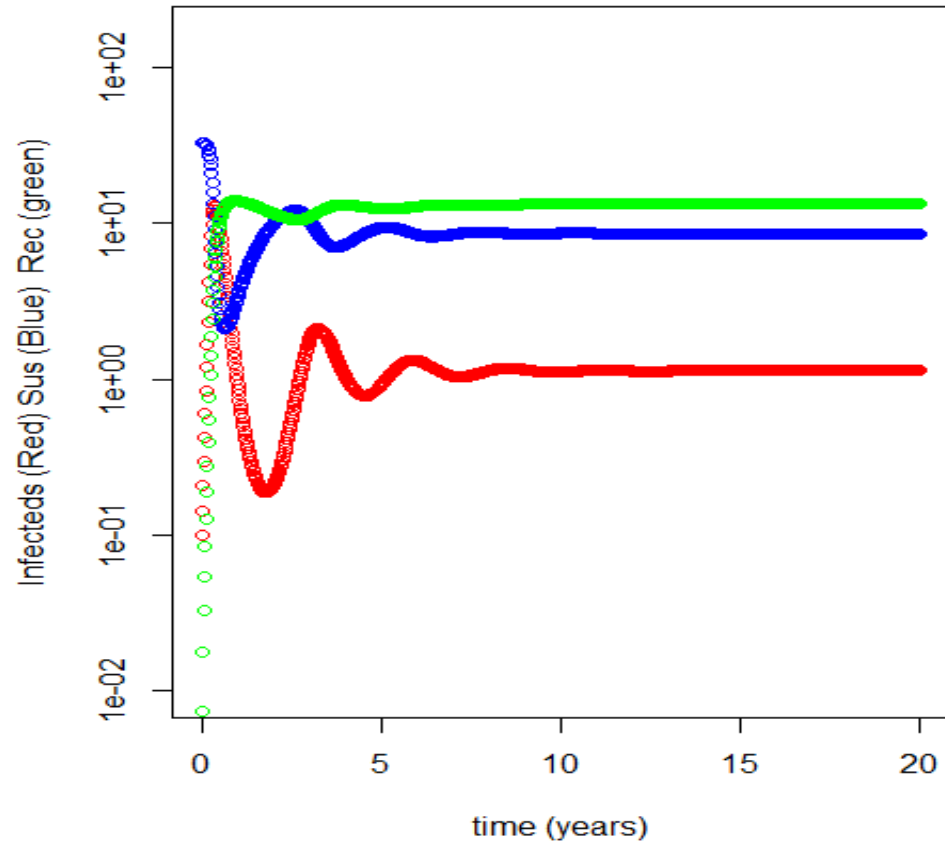


Fig. 1. Map of the Serengeti ecosystem (Tanzania). Circles represent human settlements (gray) surrounding the Serengeti National Park, villages/households from which domestic dogs were sampled (dark blue), locations where lions were sampled (black), and villages included in domestic dog vaccination campaigns that were not sampled (pale blue). (A) Arrows indicate the direction of the spread of CDV during the 1994 epidemic as reconstructed by Cleaveland et al. (16). (B) Small-scale domestic dog vaccination campaigns conducted during 1996–2002. (C) Expanded domestic dog vaccination program implemented during 2003–2012.

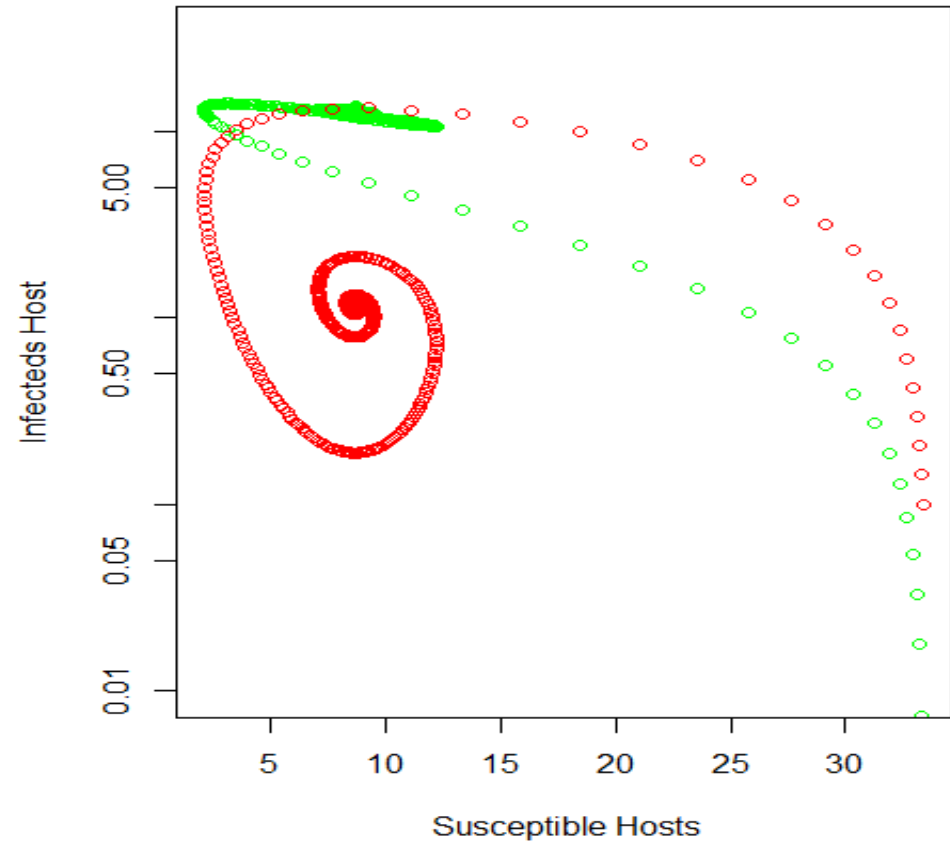
Joint work with Sarah Cleaveland, Katie Hampson, Craig Packer, Tiziana Lembo, Mafalda Viana and many others...



DeLeo and Dobson (1995)

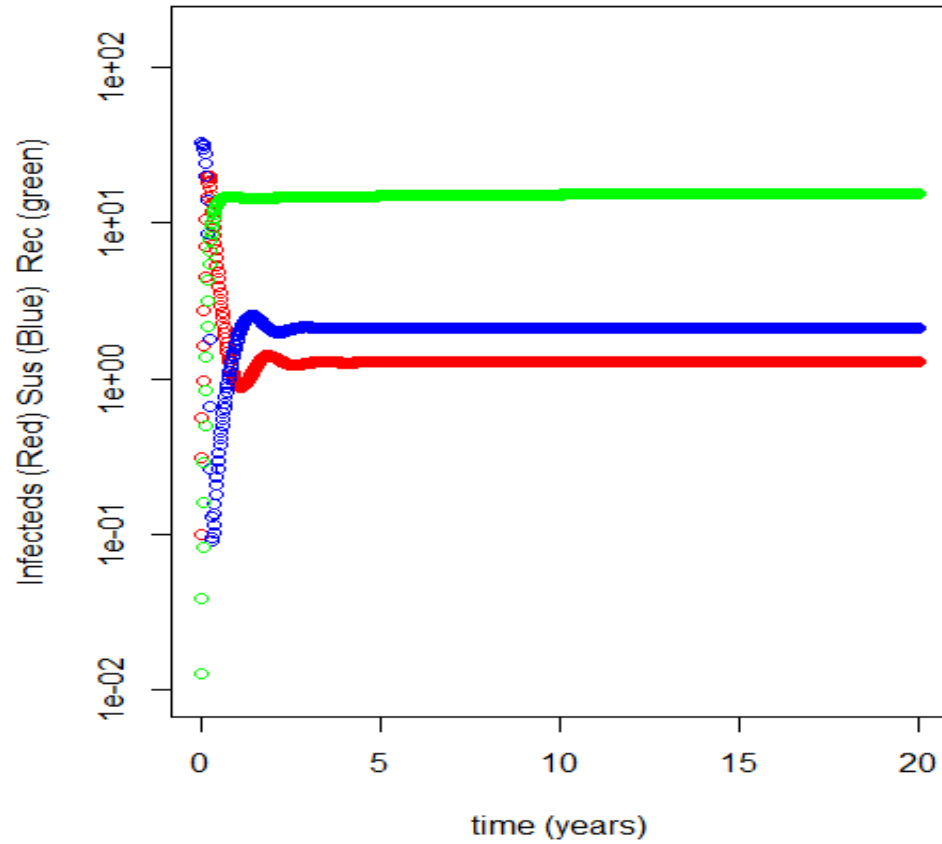


CDV SI model

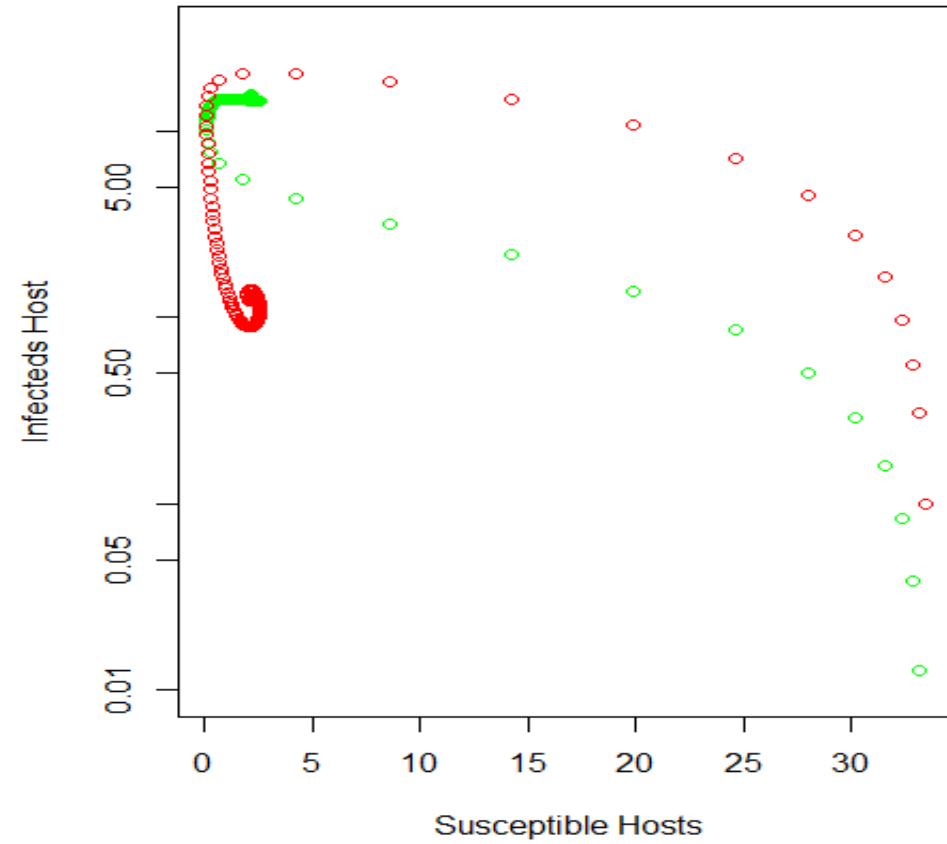


Canine distemper as only pathogen in population

DeLeo and Dobson (1995)

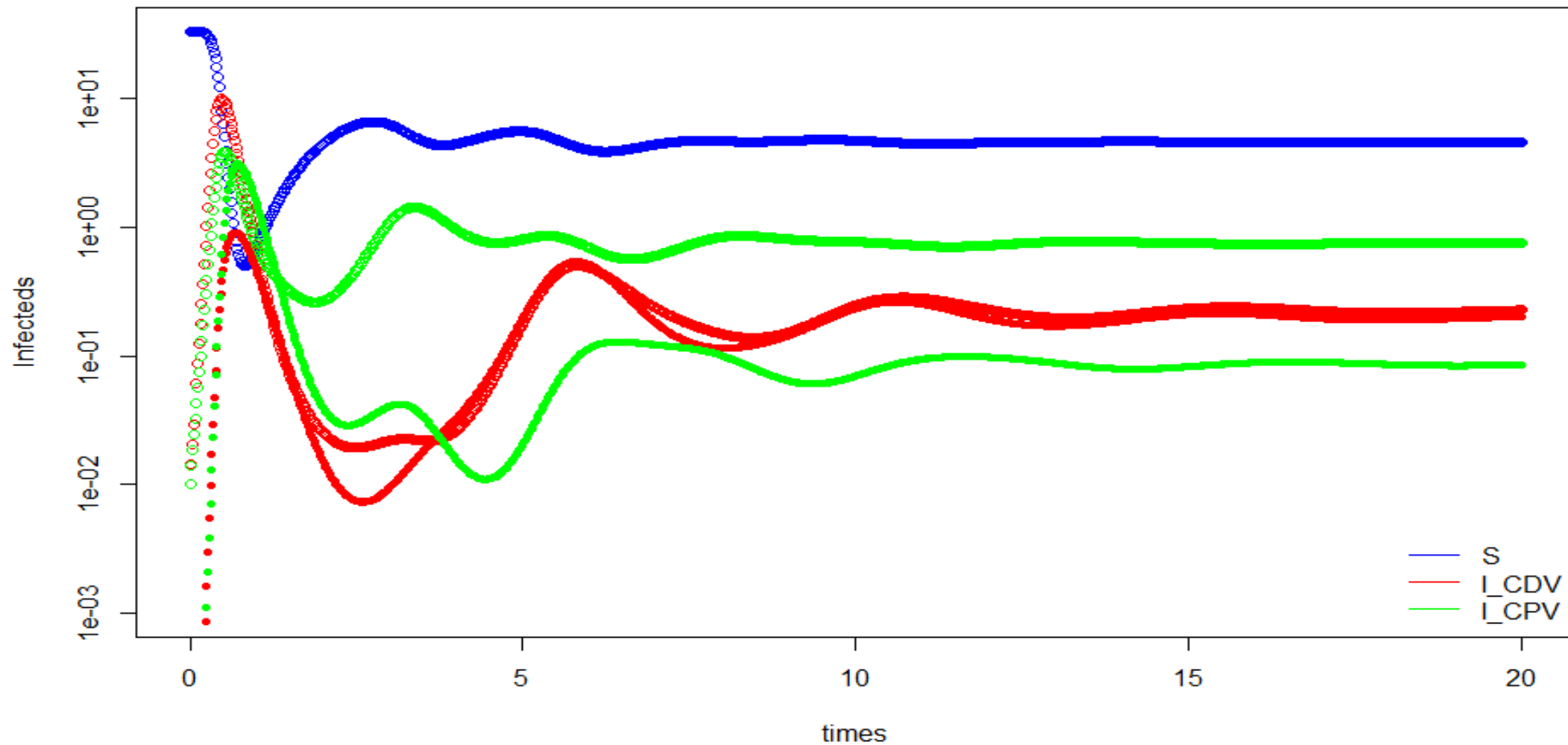


CPV SWIR model

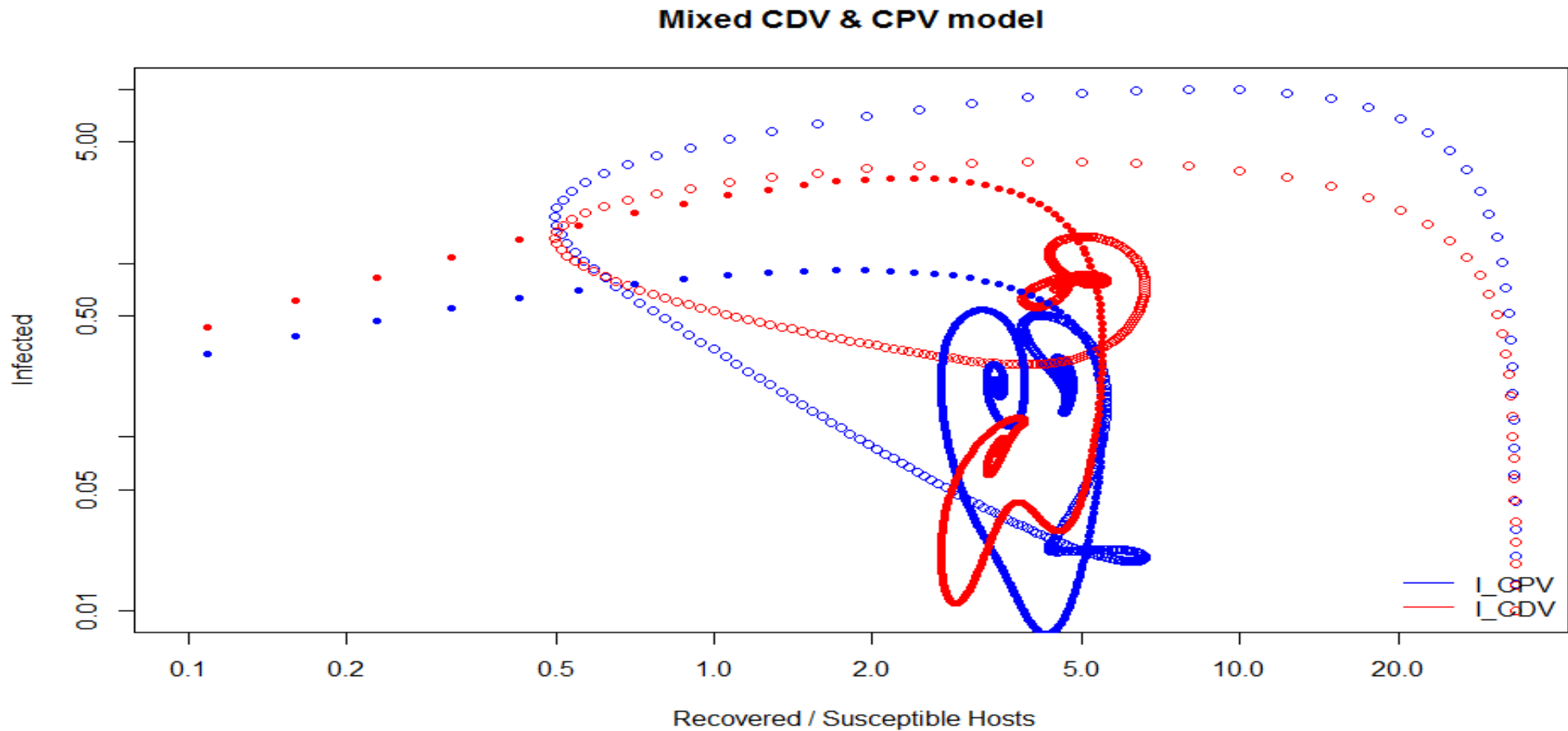


Canine parvovirus as only pathogen present....equally boring..!

Mixed CDV and CPV model

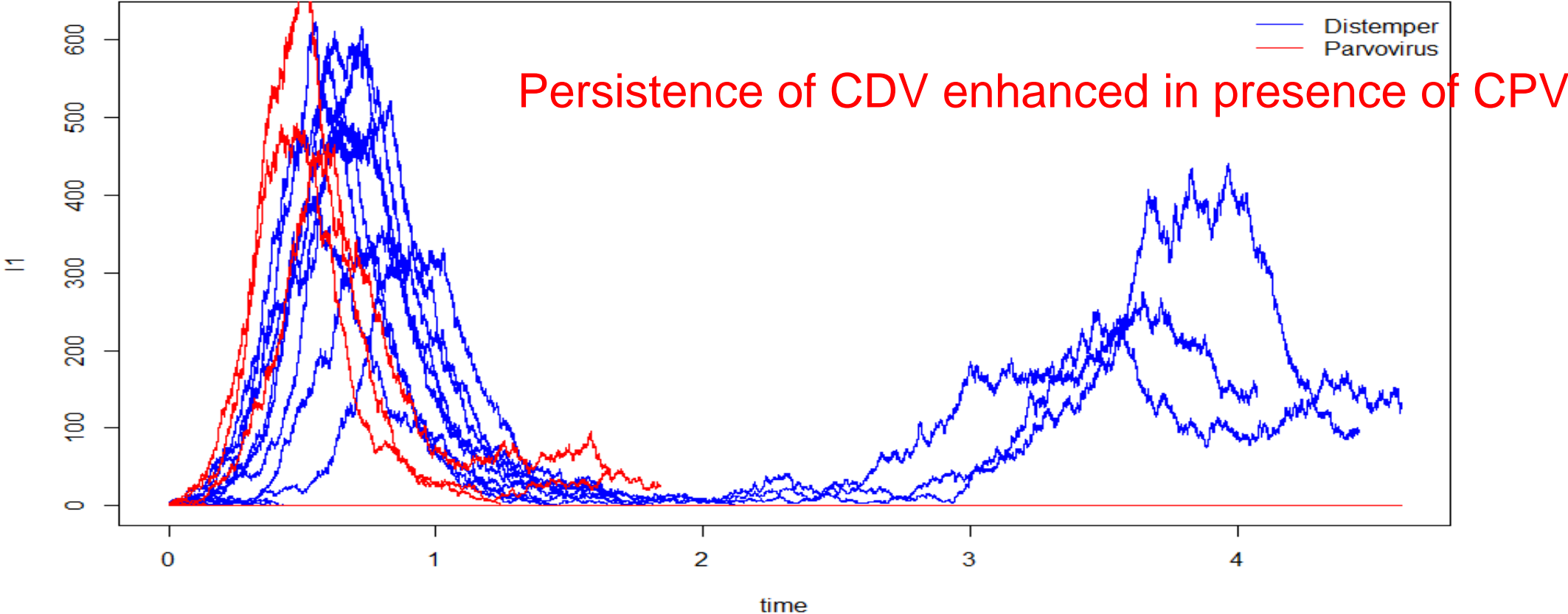


Both CPV and CDV circulating in the host population....!!



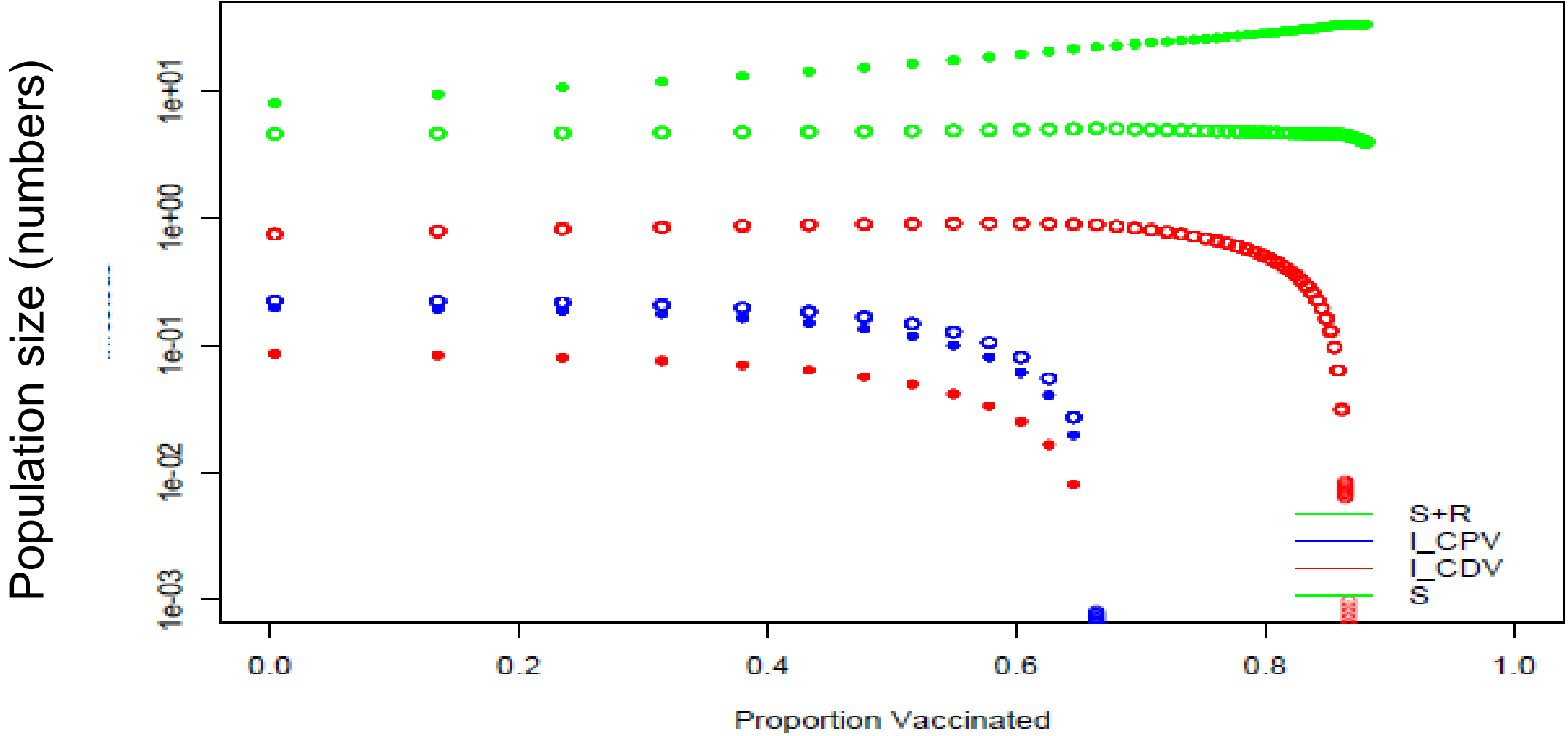
Dynamics are much more interesting although each host is only Ever infected with one virus at any one time...

Stochastic CDV and CPV in population of 10,000 dogs



Vaccination with two pathogens and a single host (CPV, CDV and dogs)

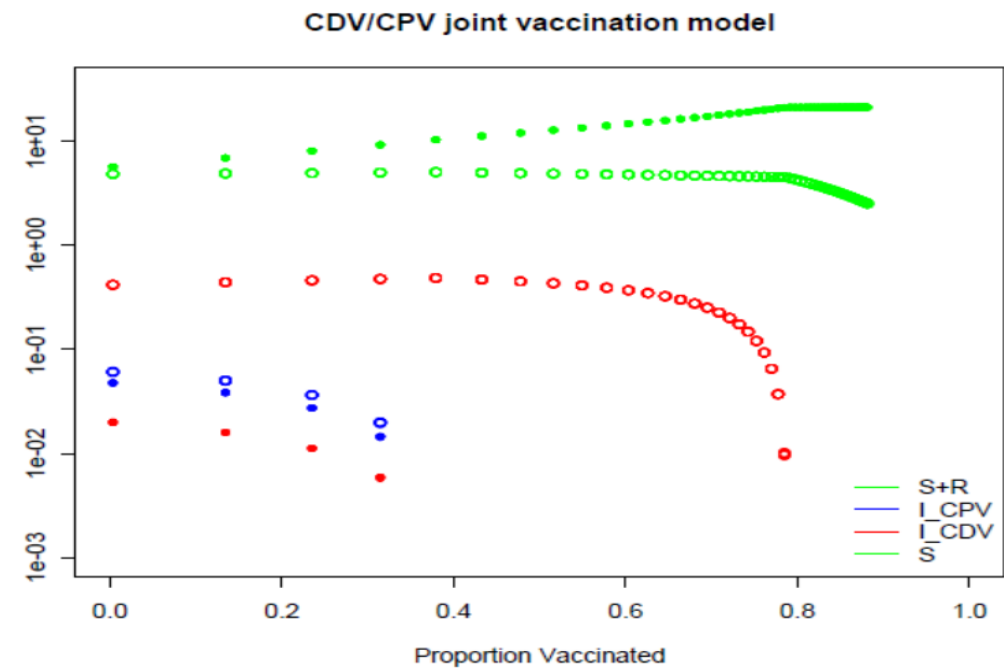
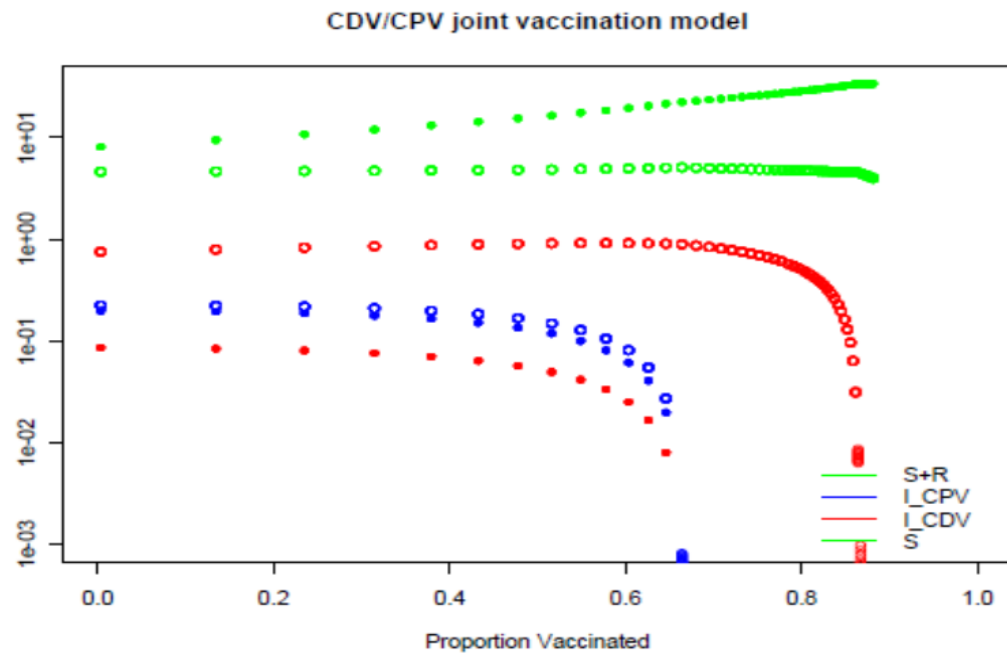
CDV/CPV joint vaccination model



Vaccination interacts with sterilization

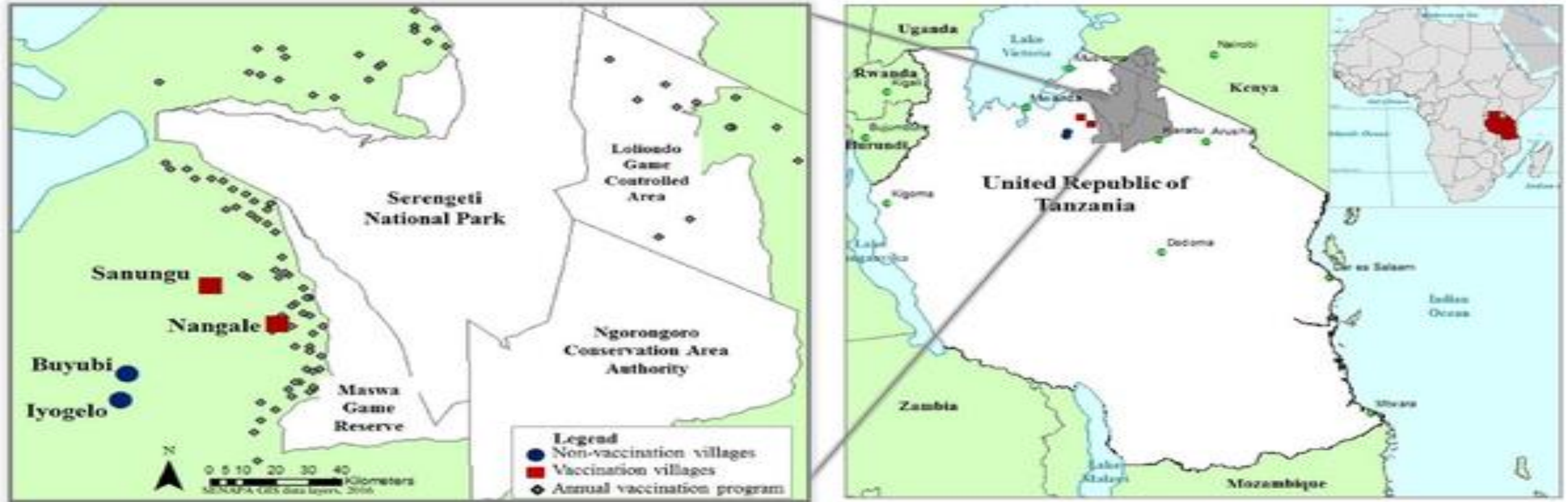
No Sterilization

25% Sterilization



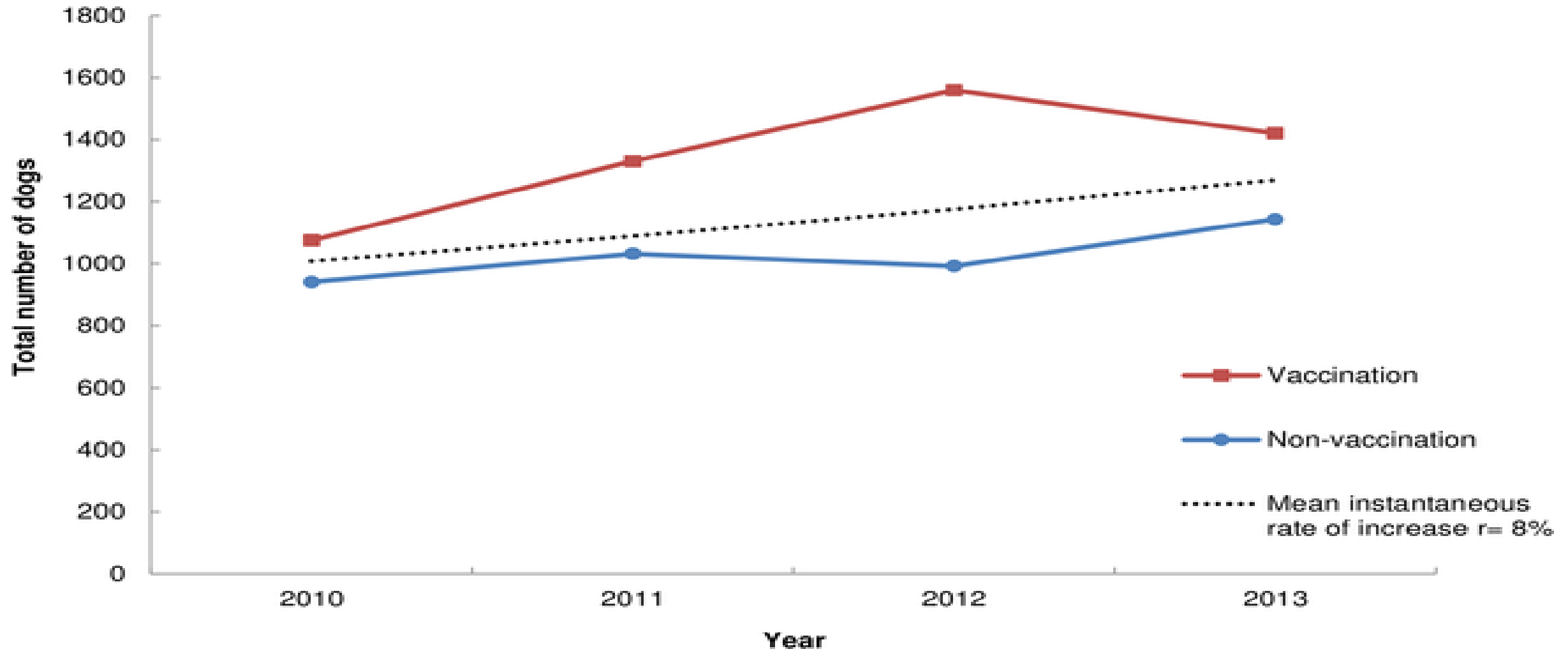
All of this will also apply to attempts to eradicate PPRV by vaccination; much, nu

Fig 1. Location of study villages in relation to Serengeti National Park and existing dog rabies vaccination campaign.



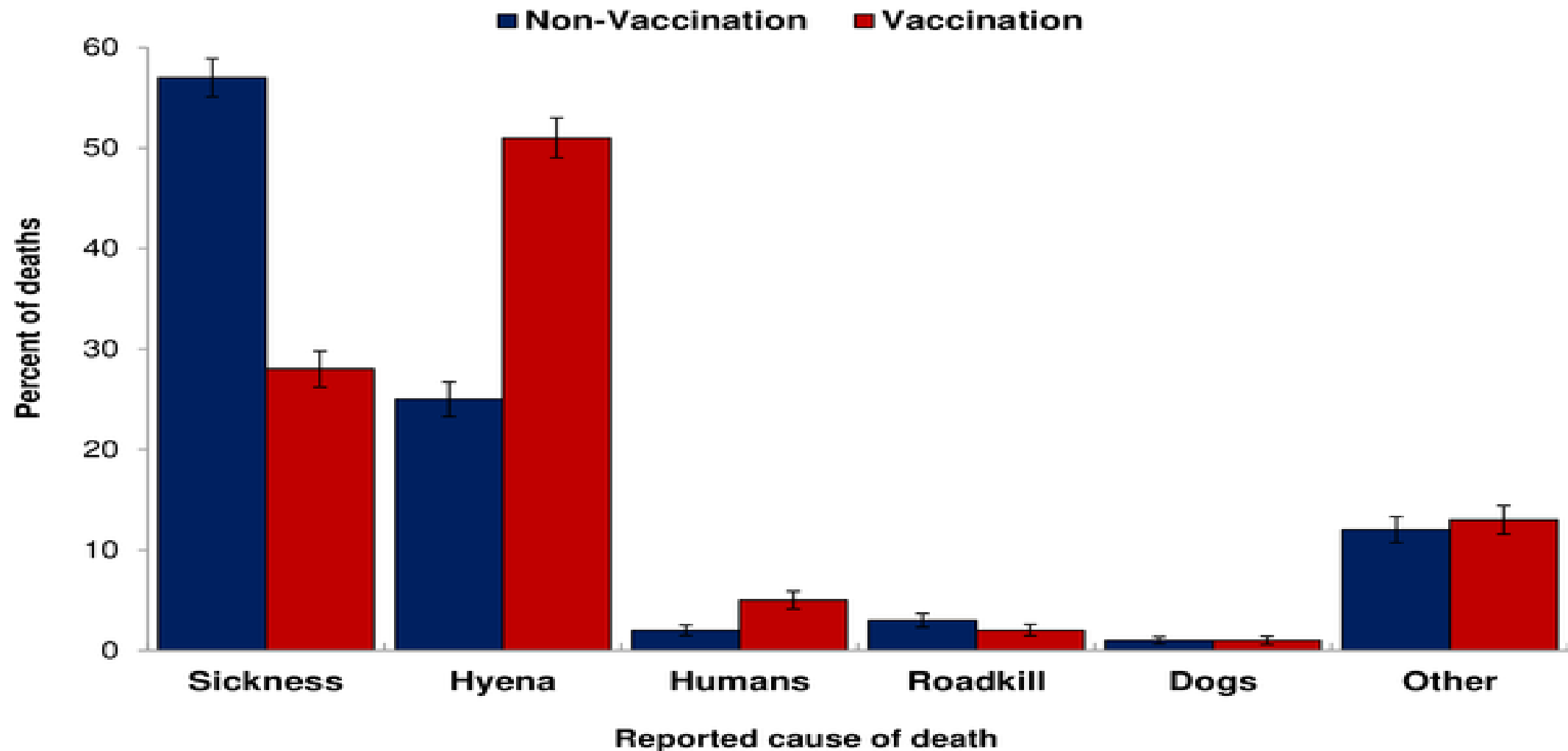
Czupryna AM, Brown JS, Bigambo MA, Whelan CJ, Mehta SD, et al. (2016) Ecology and Demography of Free-Roaming Domestic Dogs in Rural Villages near Serengeti National Park in Tanzania. PLOS ONE 11(11): e0167092. doi:10.1371/journal.pone.0167092
<http://journals.plos.org/plosone/article?id=10.1371/journal.pone.0167092>

Fig 8. Total number of dogs recorded each year of the study in each village census.



Czupryna AM, Brown JS, Bigambo MA, Whelan CJ, Mehta SD, et al. (2016) Ecology and Demography of Free-Roaming Domestic Dogs in Rural Villages near Serengeti National Park in Tanzania. PLOS ONE 11(11): e0167092. doi:10.1371/journal.pone.0167092
<http://journals.plos.org/plosone/article?id=10.1371/journal.pone.0167092>

Fig 7. Percentage of owner-reported causes of death of dogs enrolled in the study.

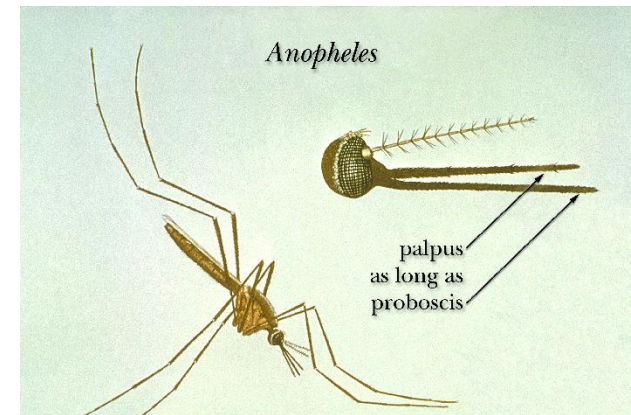
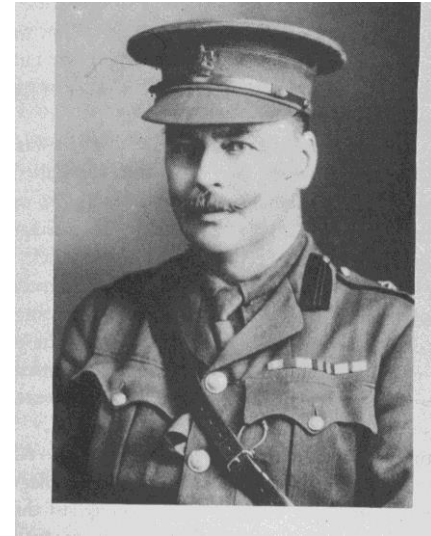


Czupryna AM, Brown JS, Bigambo MA, Whelan CJ, Mehta SD, et al. (2016) Ecology and Demography of Free-Roaming Domestic Dogs in Rural Villages near Serengeti National Park in Tanzania. PLOS ONE 11(11): e0167092. doi:10.1371/journal.pone.0167092
<http://journals.plos.org/plosone/article?id=10.1371/journal.pone.0167092>



Thank you!

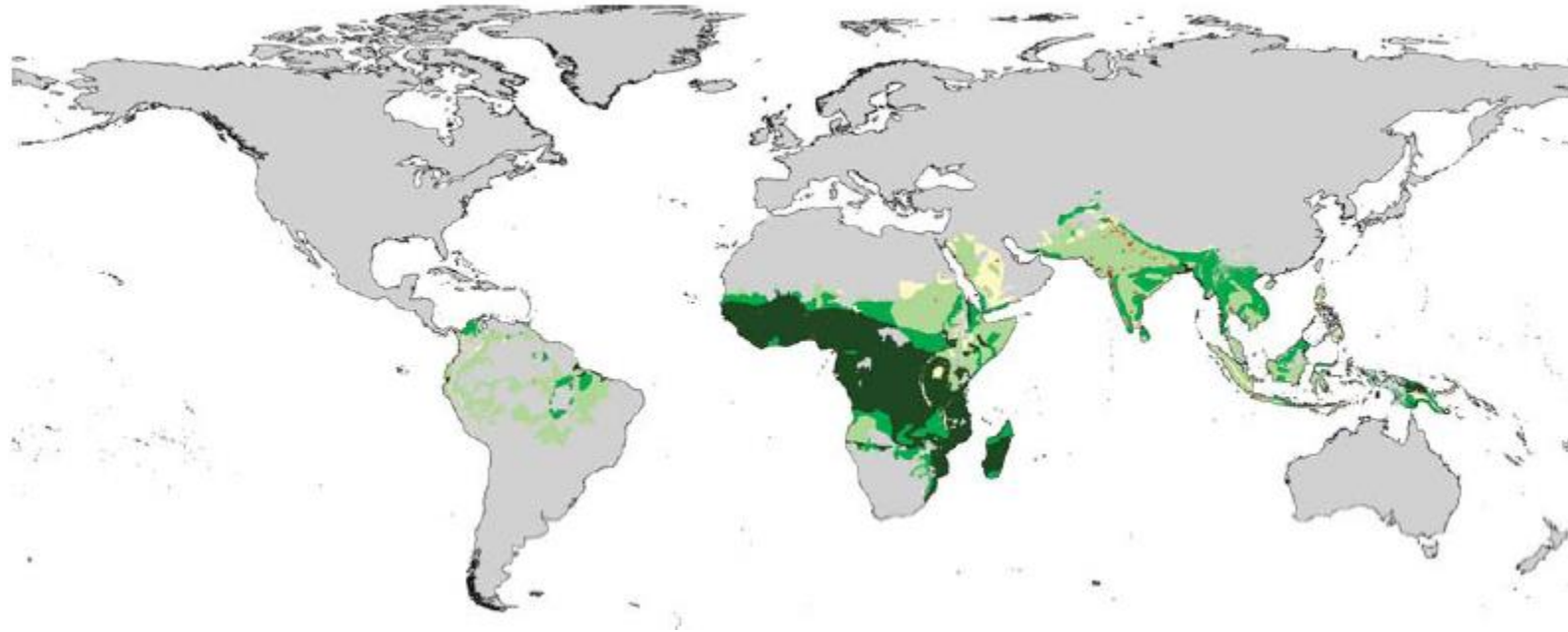
Scarier and scarier, Next we have malaria!



Useful Websites: <http://www.rph.wa.gov.au/labs/haem/malaria/index.html>
<http://www.pitt.edu/~super1/lecture/lec0172/001.htm>

Global burden of malaria

estimated 515 million episodes of clinical *Plasmodium falciparum* malaria in 2002 (Snow *et al* 2005).

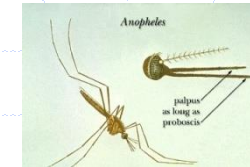


Anopheles gambiae - major vector of malaria in Africa,

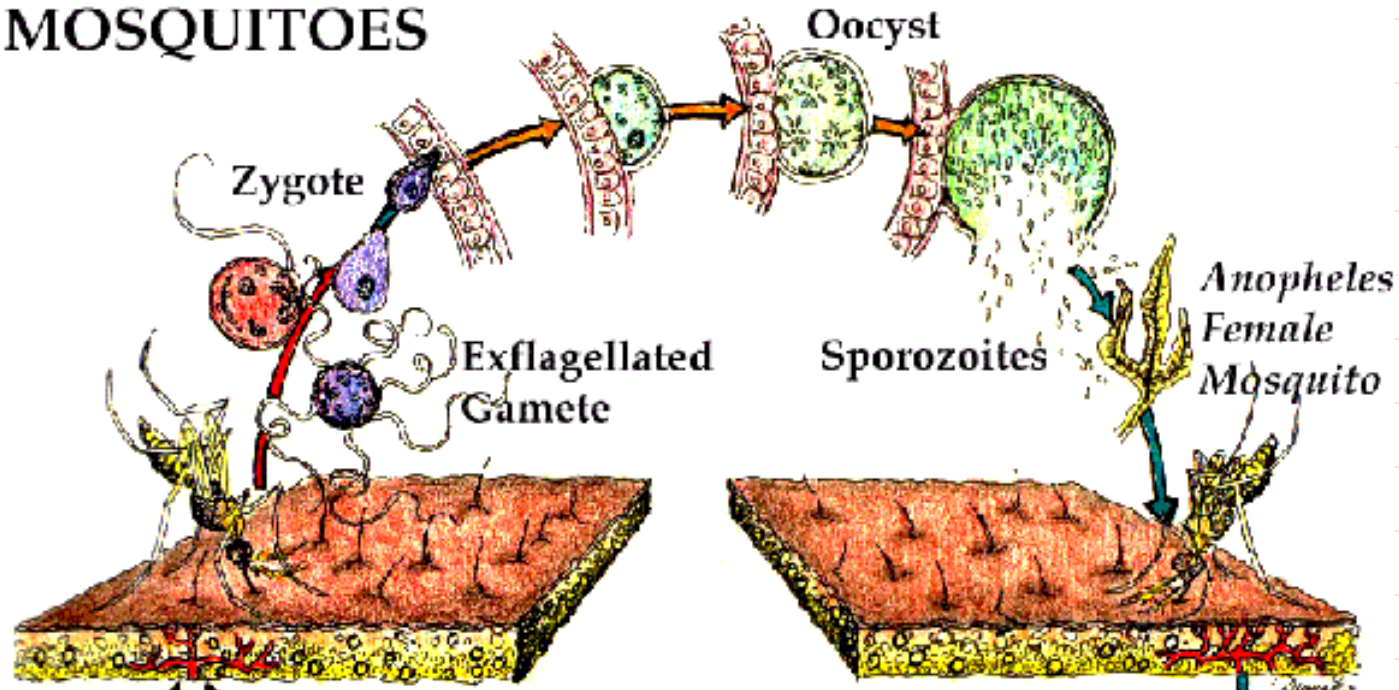
The burden of malaria in Africa

- Africa accounts for approximately 85% of malaria cases in the world
- estimated that African children have between 1.6 and 5.4 episodes of malarial fever each year.
- 3,000 deaths each day
- accounts for 1 in 5 of all childhood deaths in Africa.
- causes low birth weight, anaemia, epilepsy, and learning difficulties.
- imposes huge losses in economic productivity

Ronald Ross



MOSQUITOES

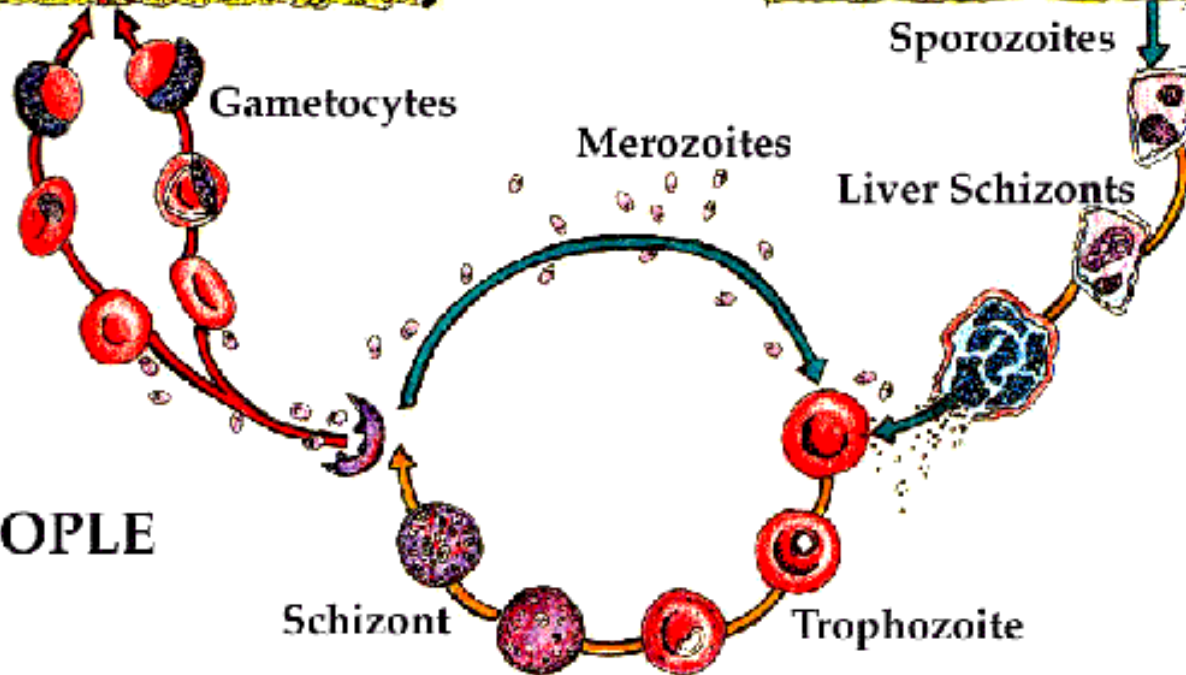


Sexual stages

Protozoan that uses mosquitoes as vectors.

Or is it the other way around?

PEOPLE



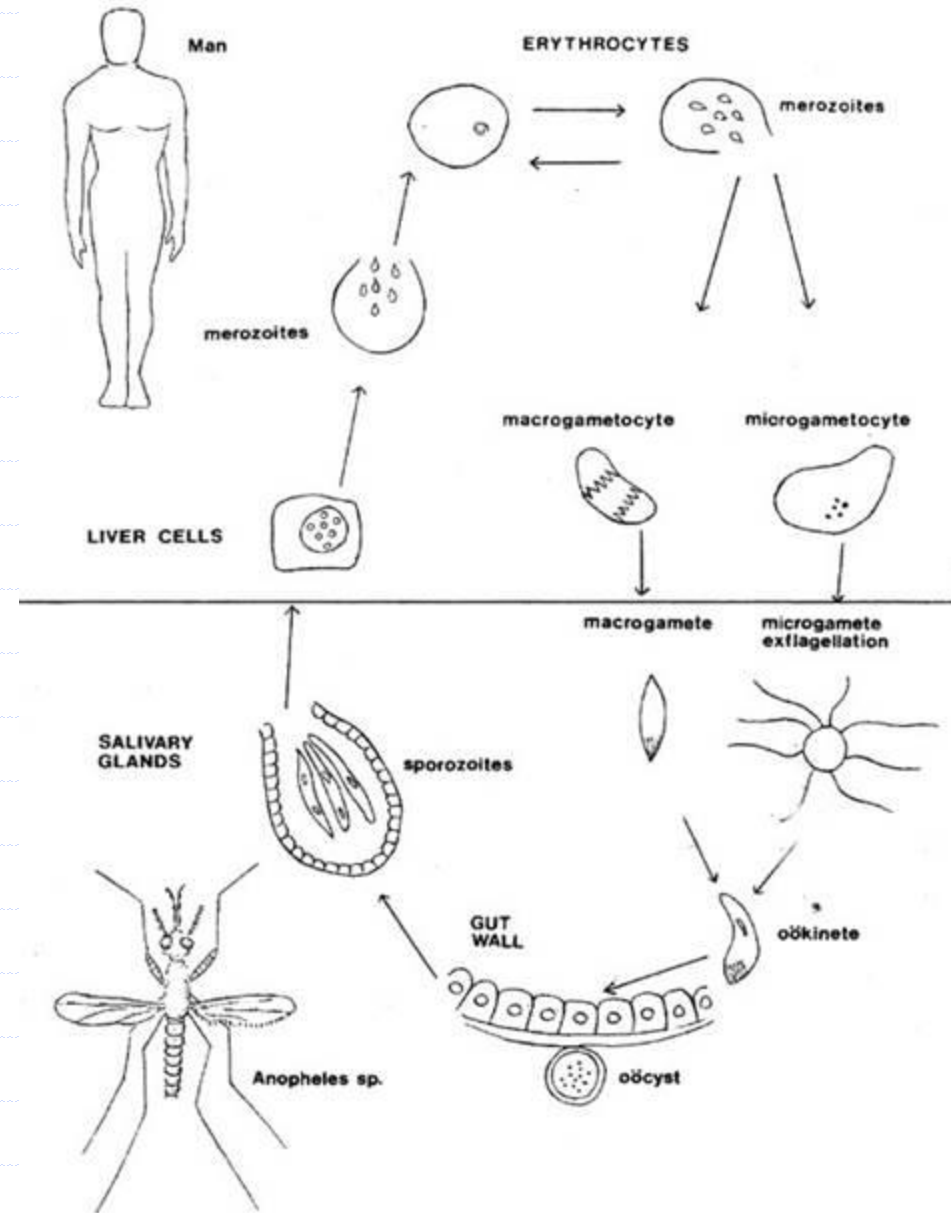
Asexual stages

Back to malaria

Life cycle..

- proportion of the human population infected
- proportion of the female mosquito population infected

Model by Ross and McDonald (1916-1957)



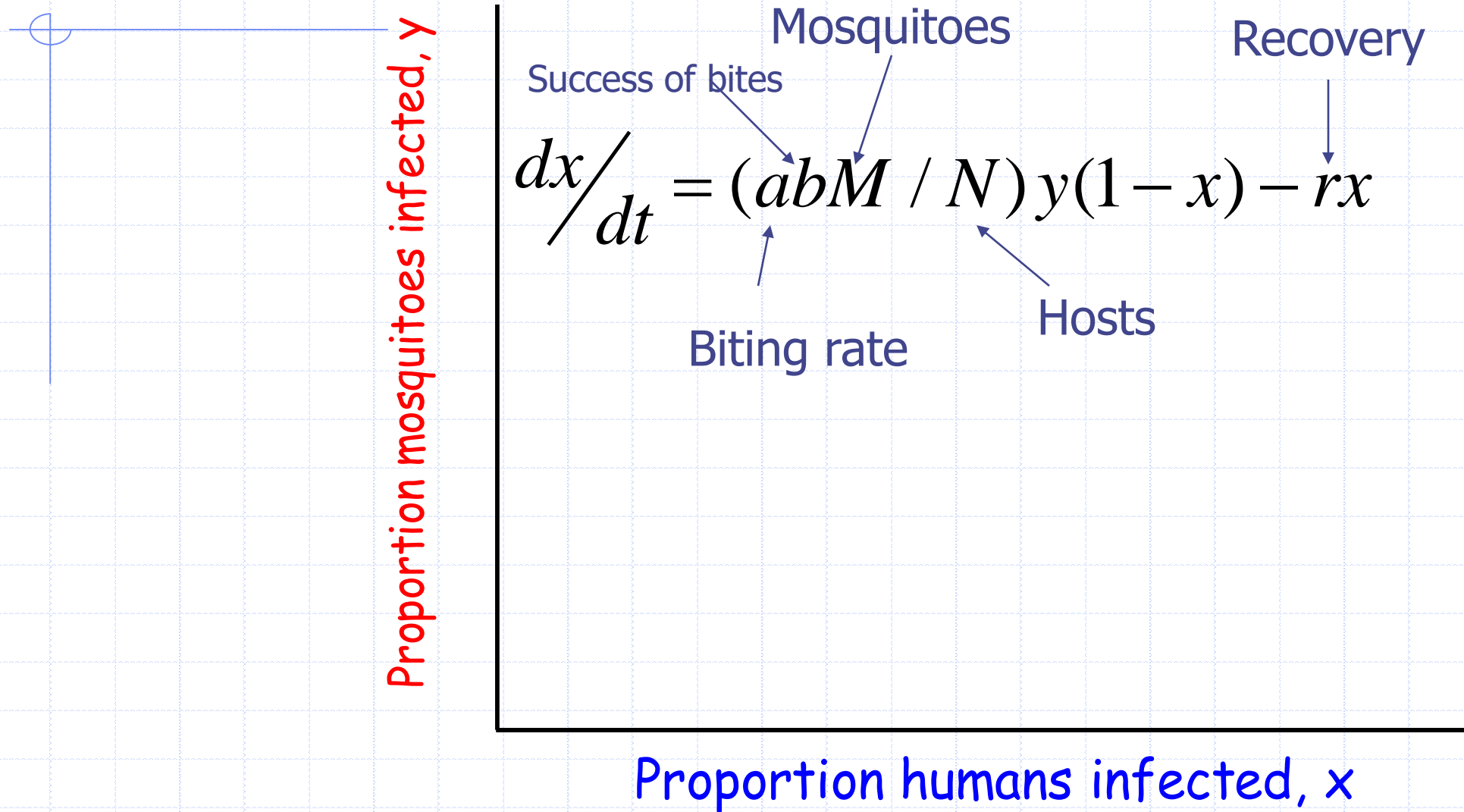
Population dynamics of malaria (Aron & May, 1982).

Proportion mosquitoes infected, y

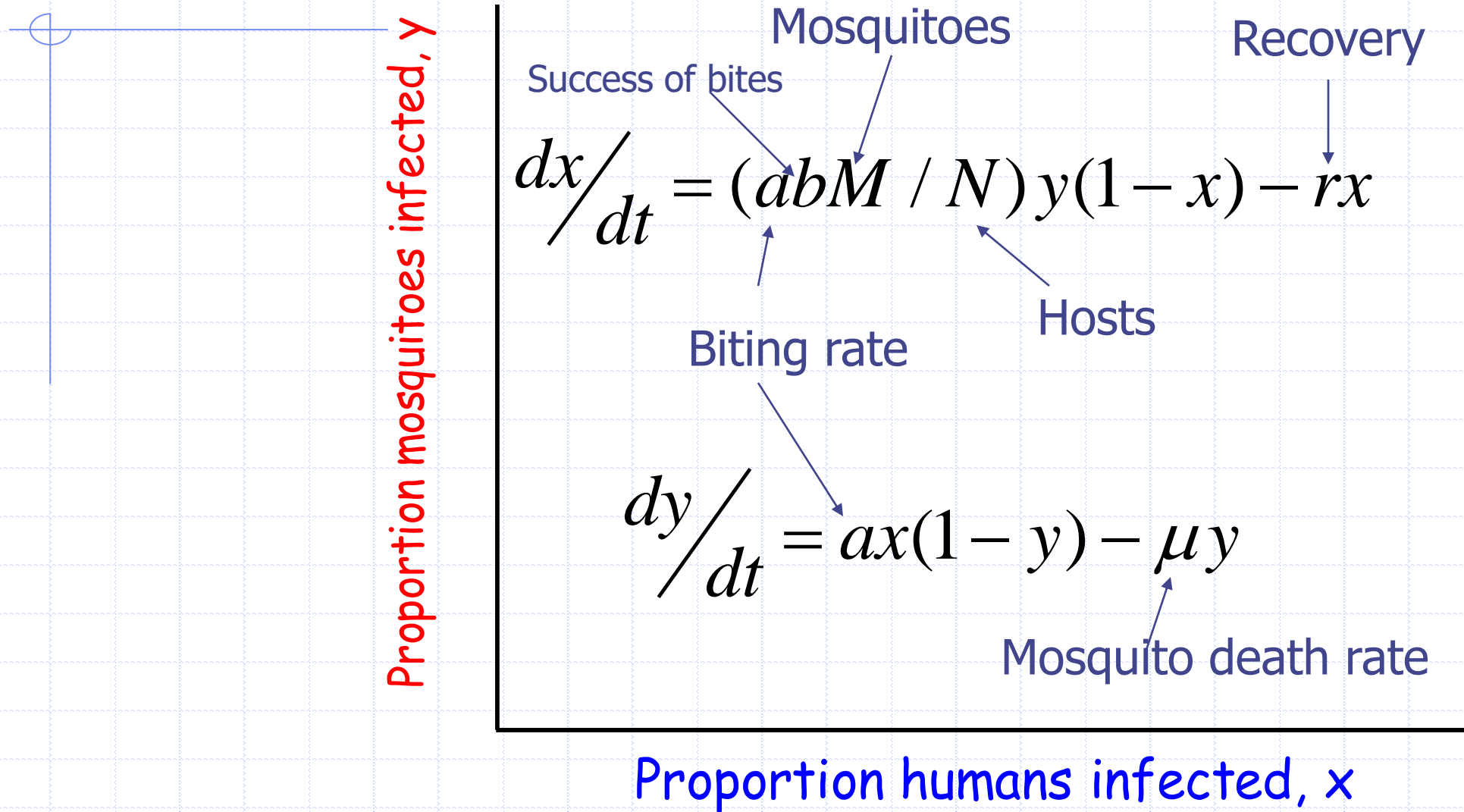
$$\frac{dx}{dt} = (abM / N) y(1 - x) - rx$$

Proportion humans infected, x

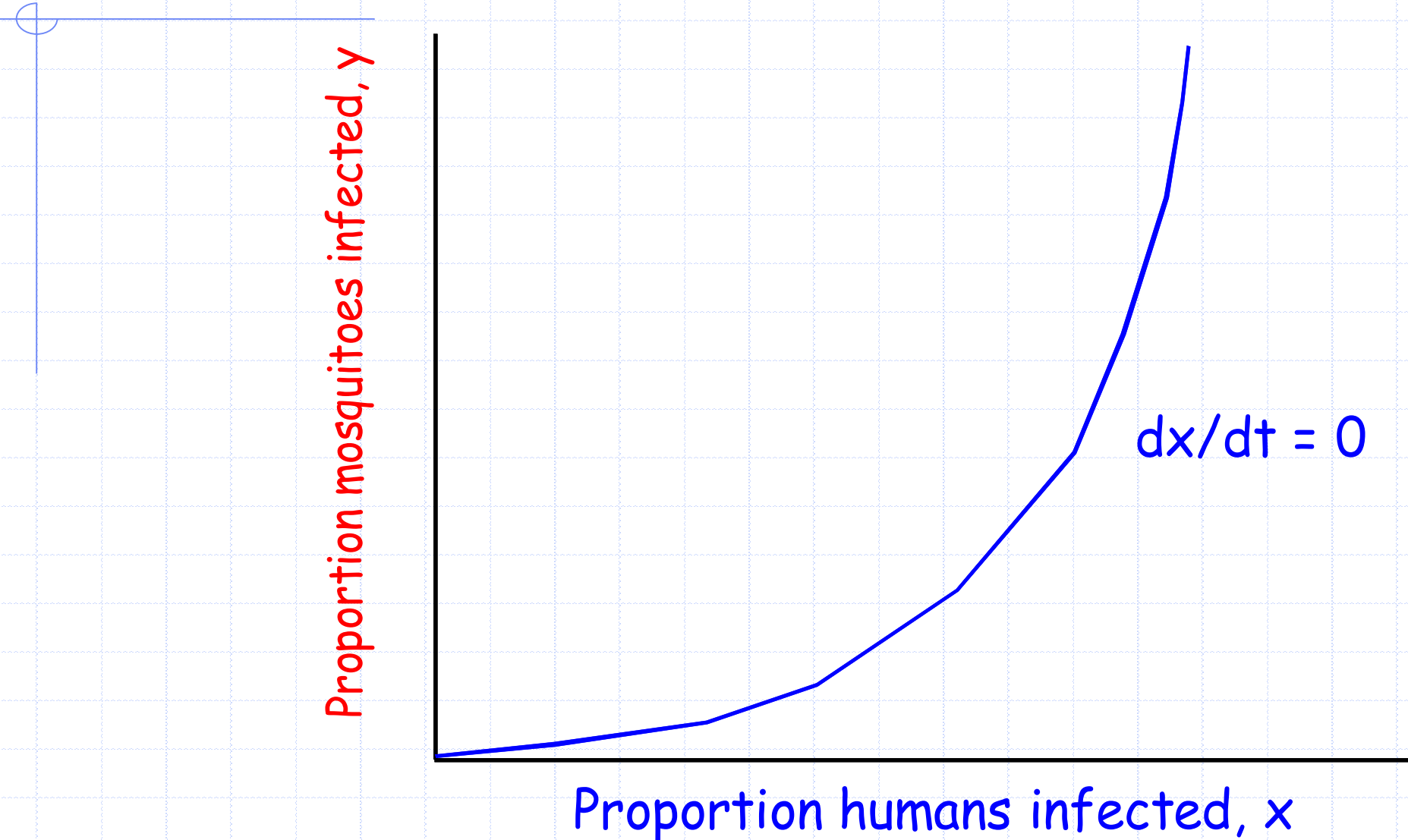
Population dynamics of malaria (Aron & May, 1982).



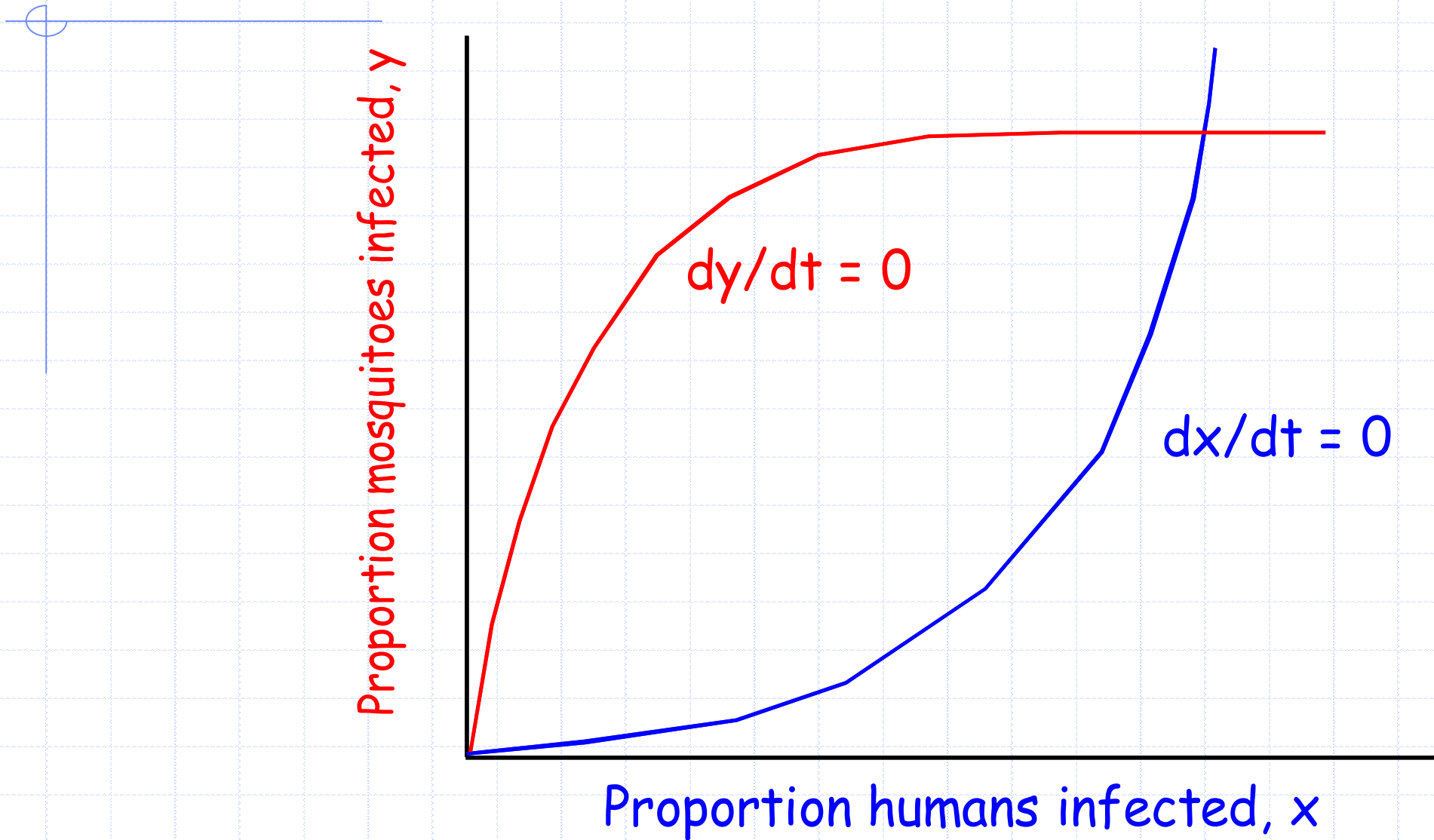
Population dynamics of malaria (Aron & May, 1982).

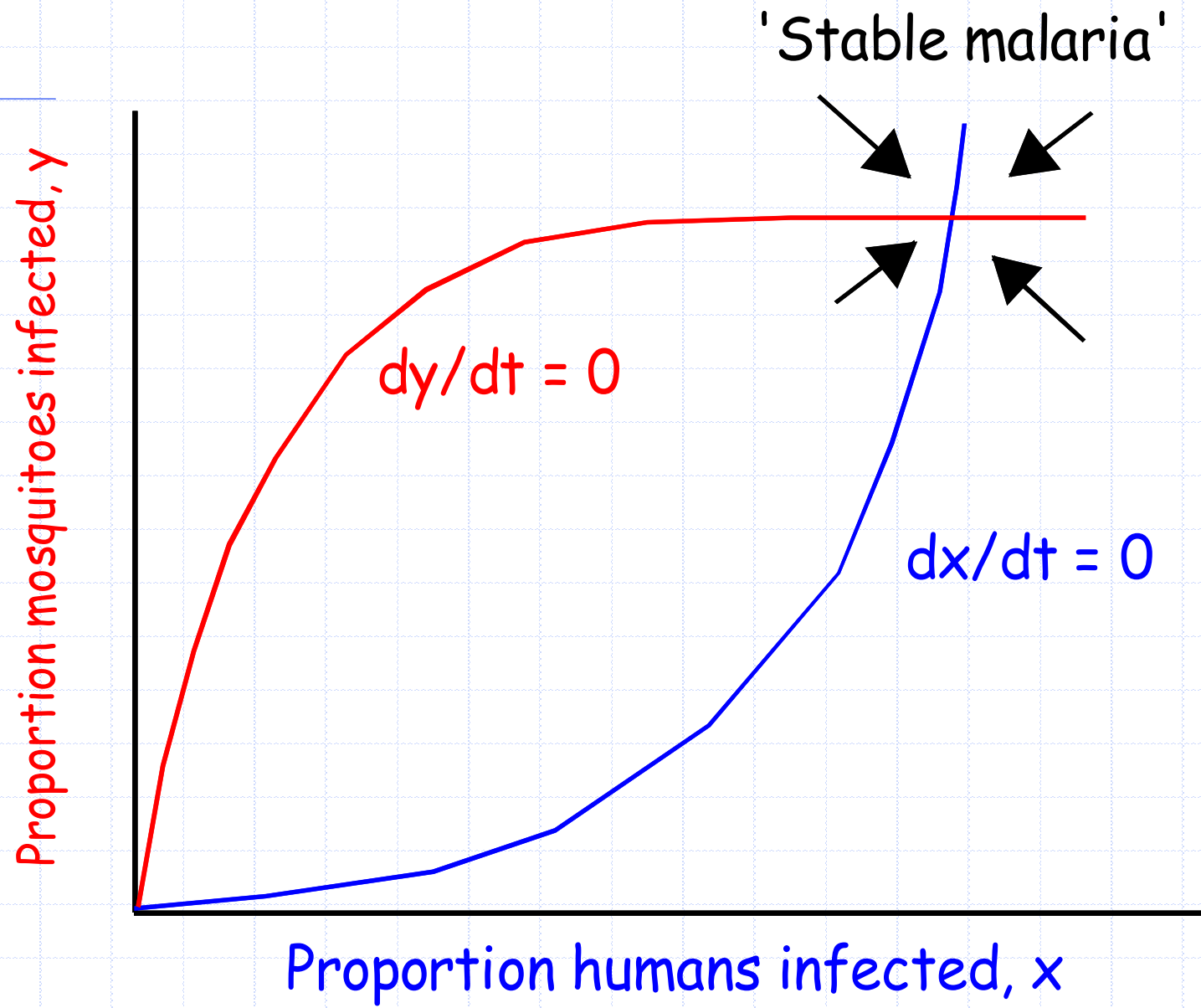


Plot 'zero-growth' isoclines

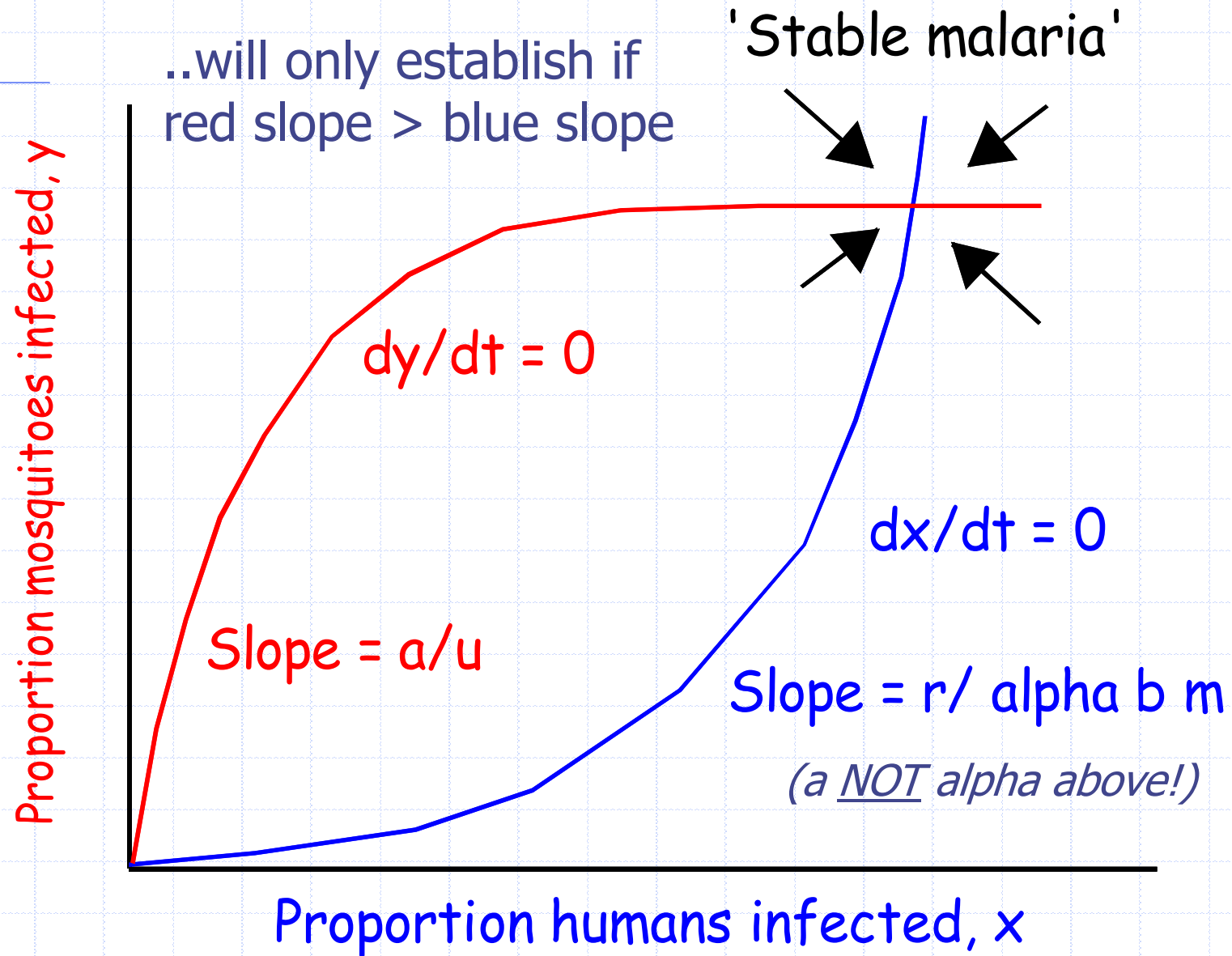


....add the second zero-growth isocline....



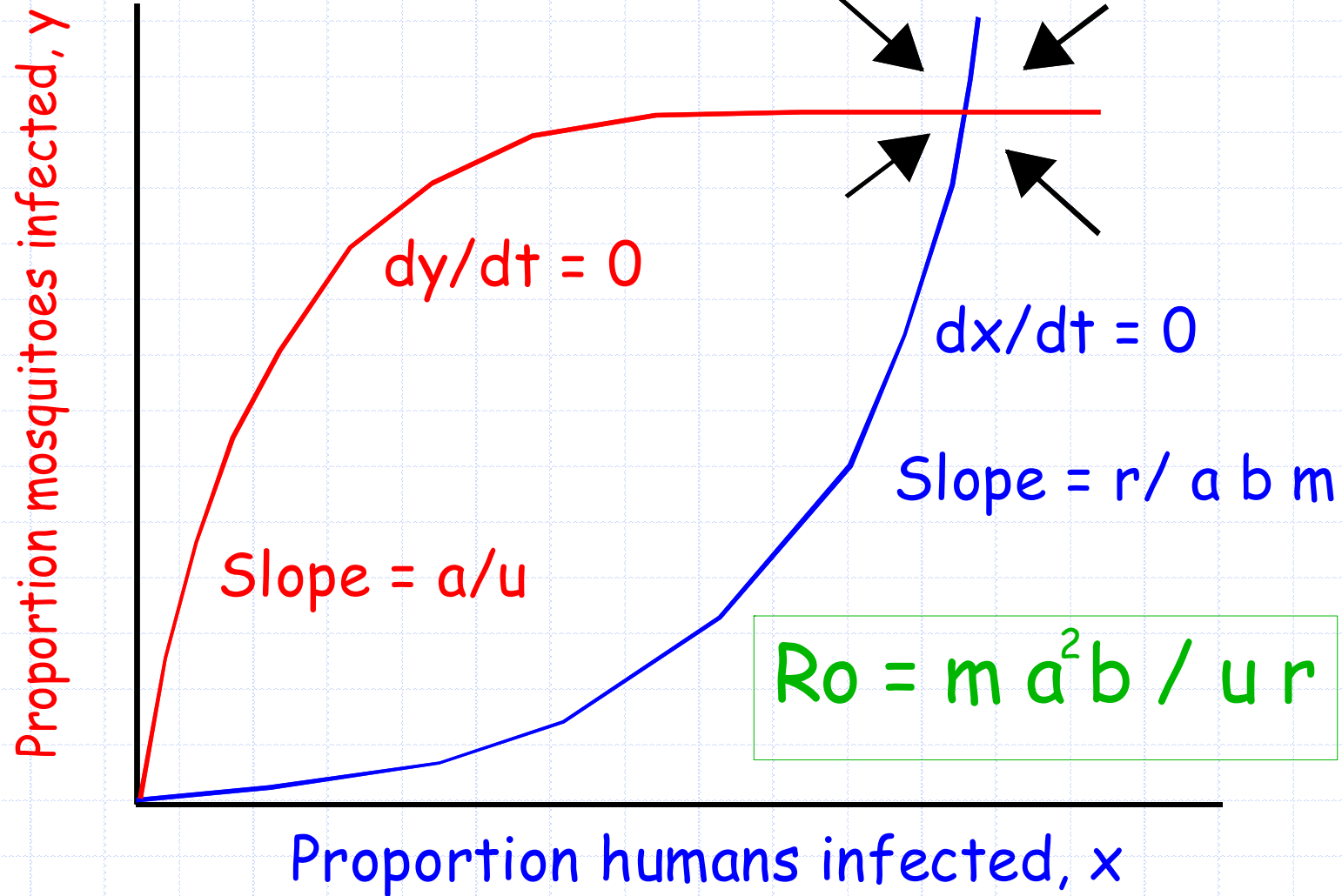


Almost 'Ro'.....!



Wow! Another Ro!

After Aron & May, 1982



Will tend to give epidemic
Cycles as $R_0 \rightarrow 1$!

Proportion mosquitoes infected, y

$$x^* = \frac{R-1}{R + \left(\frac{a}{\mu}\right)}$$

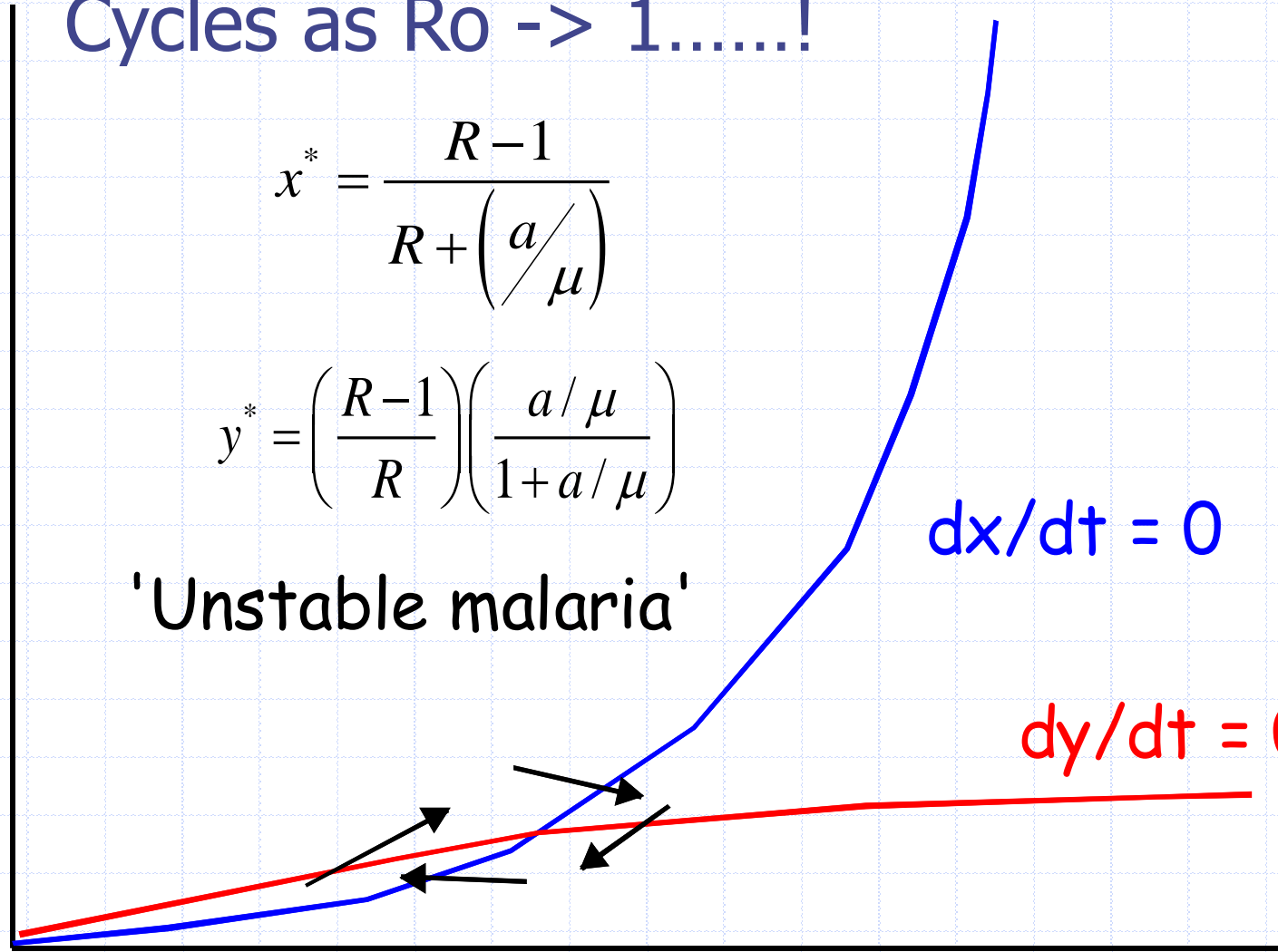
$$y^* = \left(\frac{R-1}{R}\right) \left(\frac{a/\mu}{1+a/\mu}\right)$$

'Unstable malaria'

$dx/dt = 0$

$dy/dt = 0$

Proportion humans infected, x



Could also obtain this by WAIFW - next generation matrix.....

	Human	Mosquito
Human	0	$\frac{a}{\mu}$
Mosquito	$\frac{abm}{r}$	0

Dominant eigenvalue
Gives an expression
for R_0

$$R_0 = \sqrt{\frac{a^2bm}{\mu r}}$$

Could also obtain this by WAIFW - next generation matrix.....

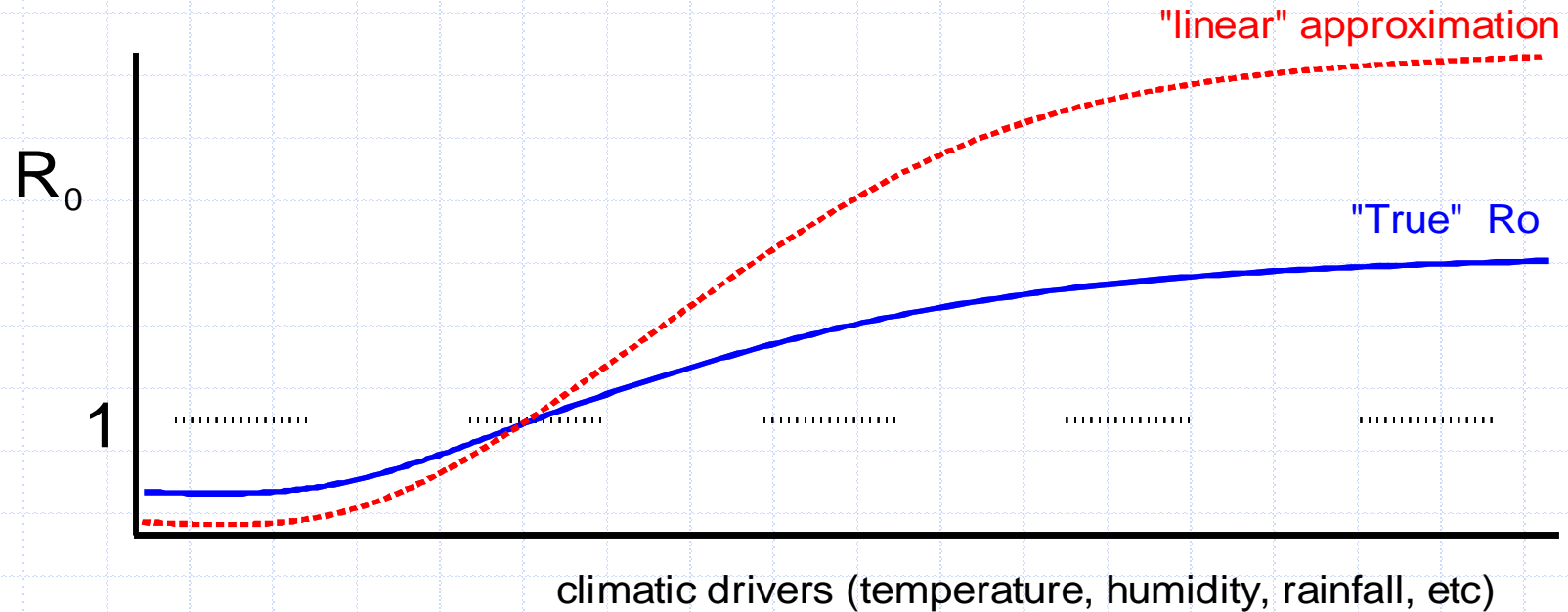
	Human	Mosquito
Human	0	$\frac{a}{\mu}$
Mosquito	$\frac{abm}{r}$	0

Dominant eigenvalue
Gives an expression
for R_0

$$R_0 = \sqrt{\frac{a^2 bm}{\mu r}}$$

The square root term makes a difference -
particularly when $R_0 \gg 1$!

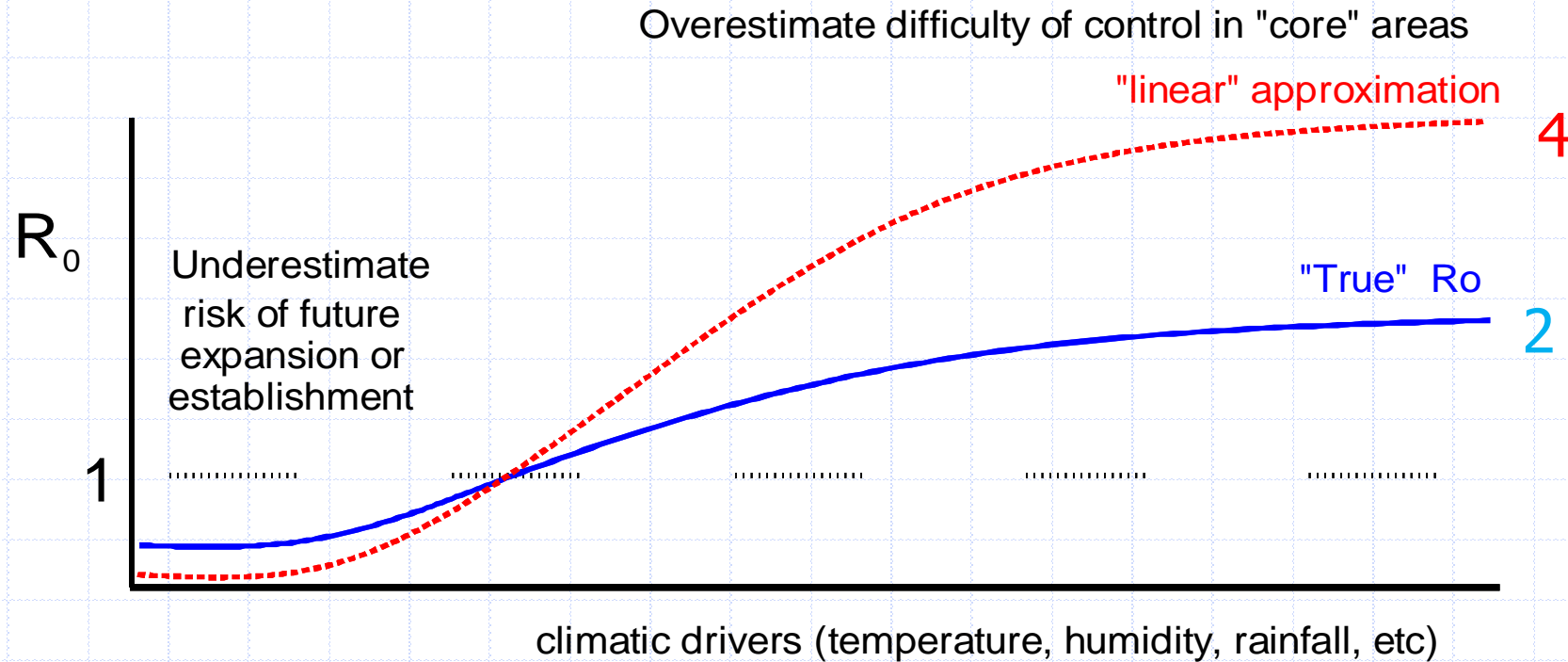
Consider maps of malaria risk.....



Maps of malaria risk will look great because of fancy computer GIS graphics

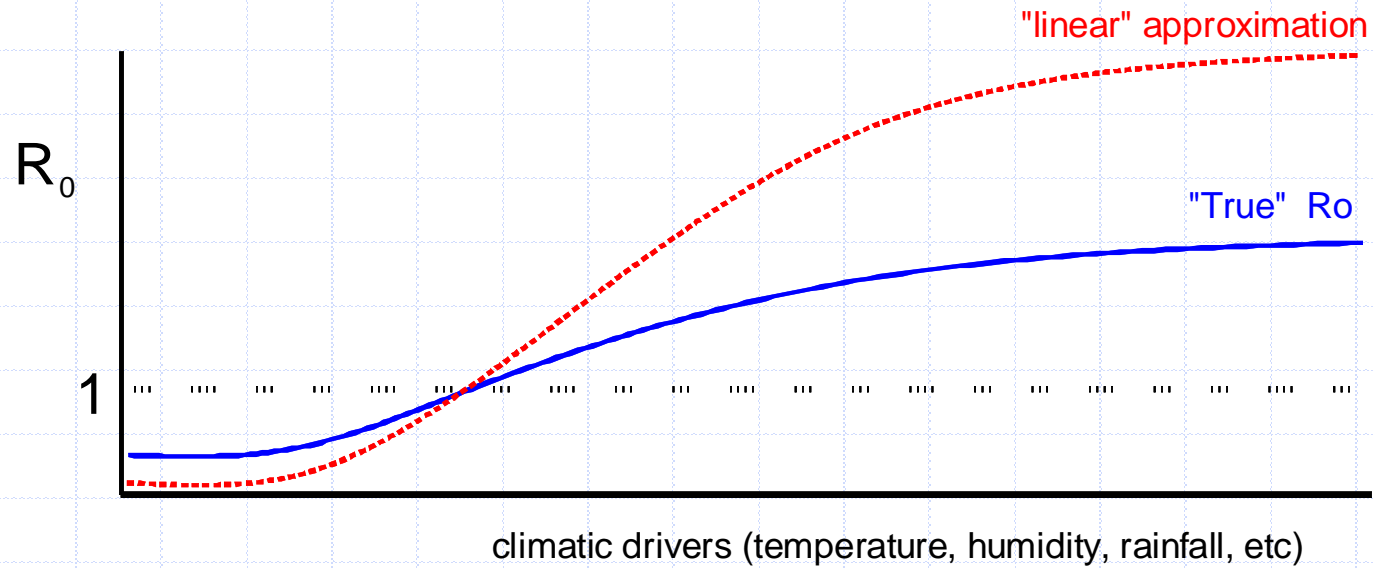
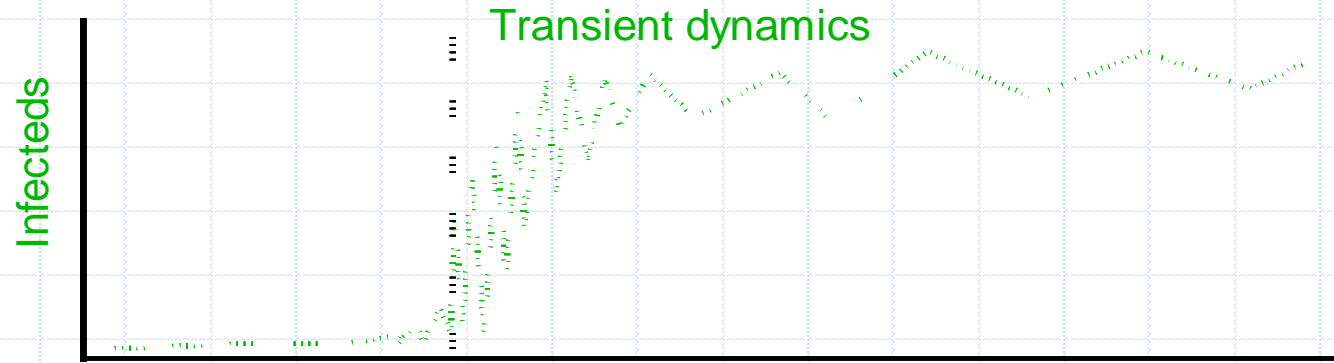
BUT, the linear approximation for R_0 will cause them to distort risk.

Risk maps for vector borne disease



One (of many) problems that underlie these 'risk' maps (many thanks to Jeremy Farrar for discussions about this).

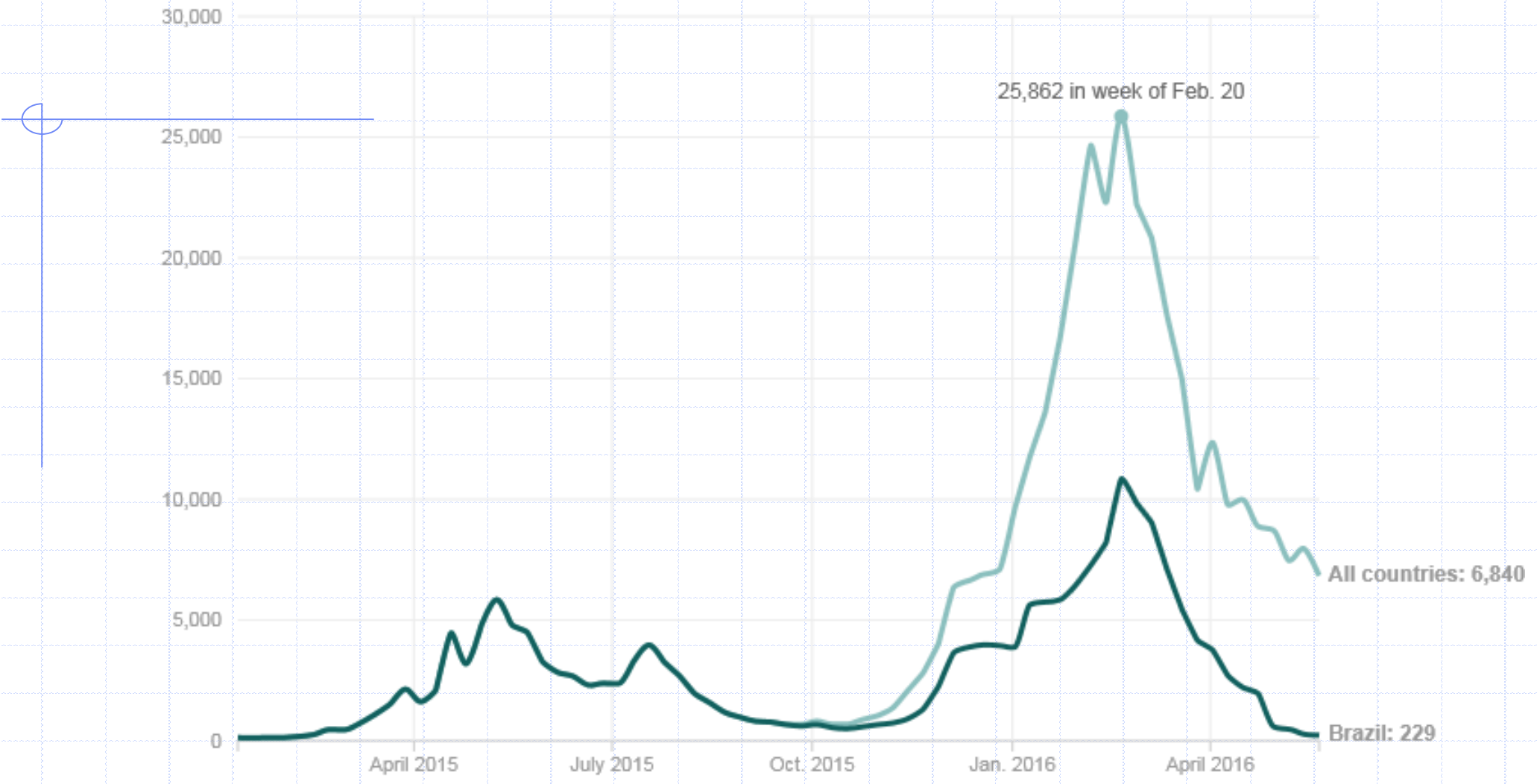
System is most unstable when R_0 close to unity...range boundaries will be fuzzy



Zika virus in Brazil

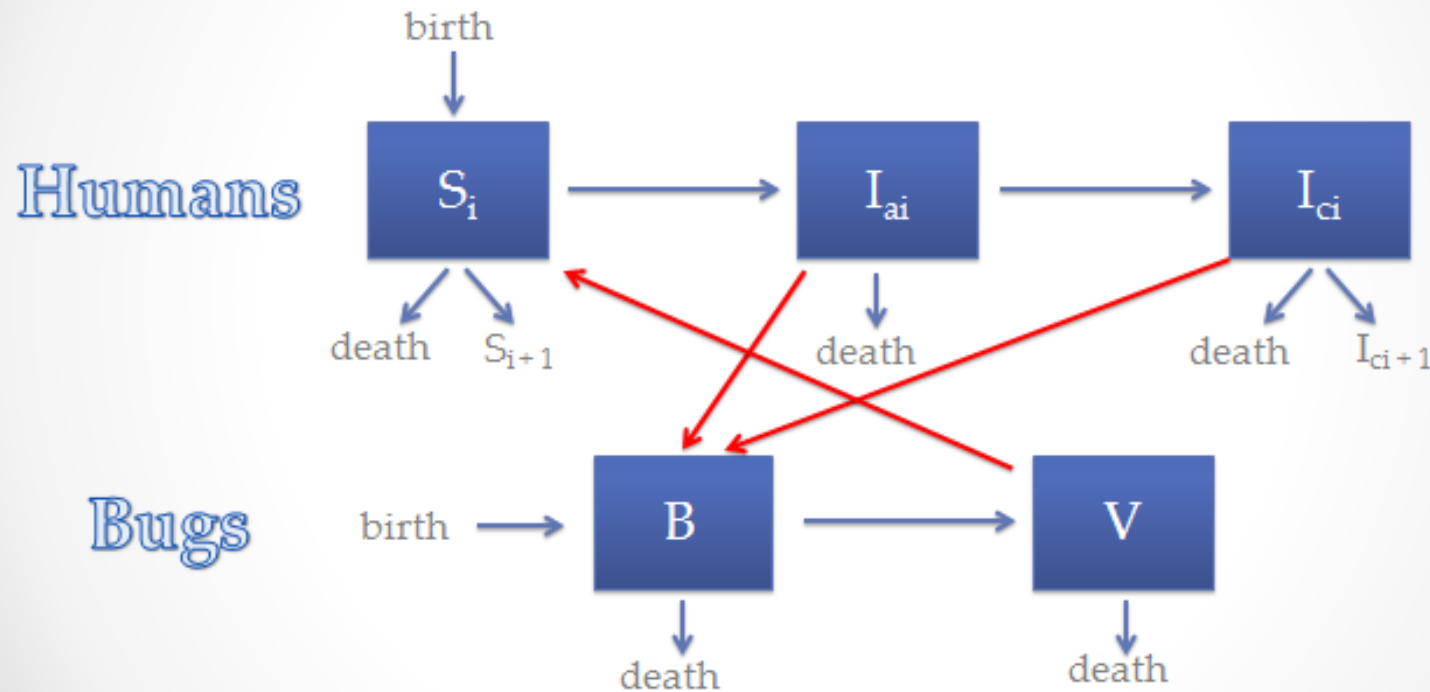


Cases of Zika : Global and in Brazil



Age-structured vector model

Modeling approach

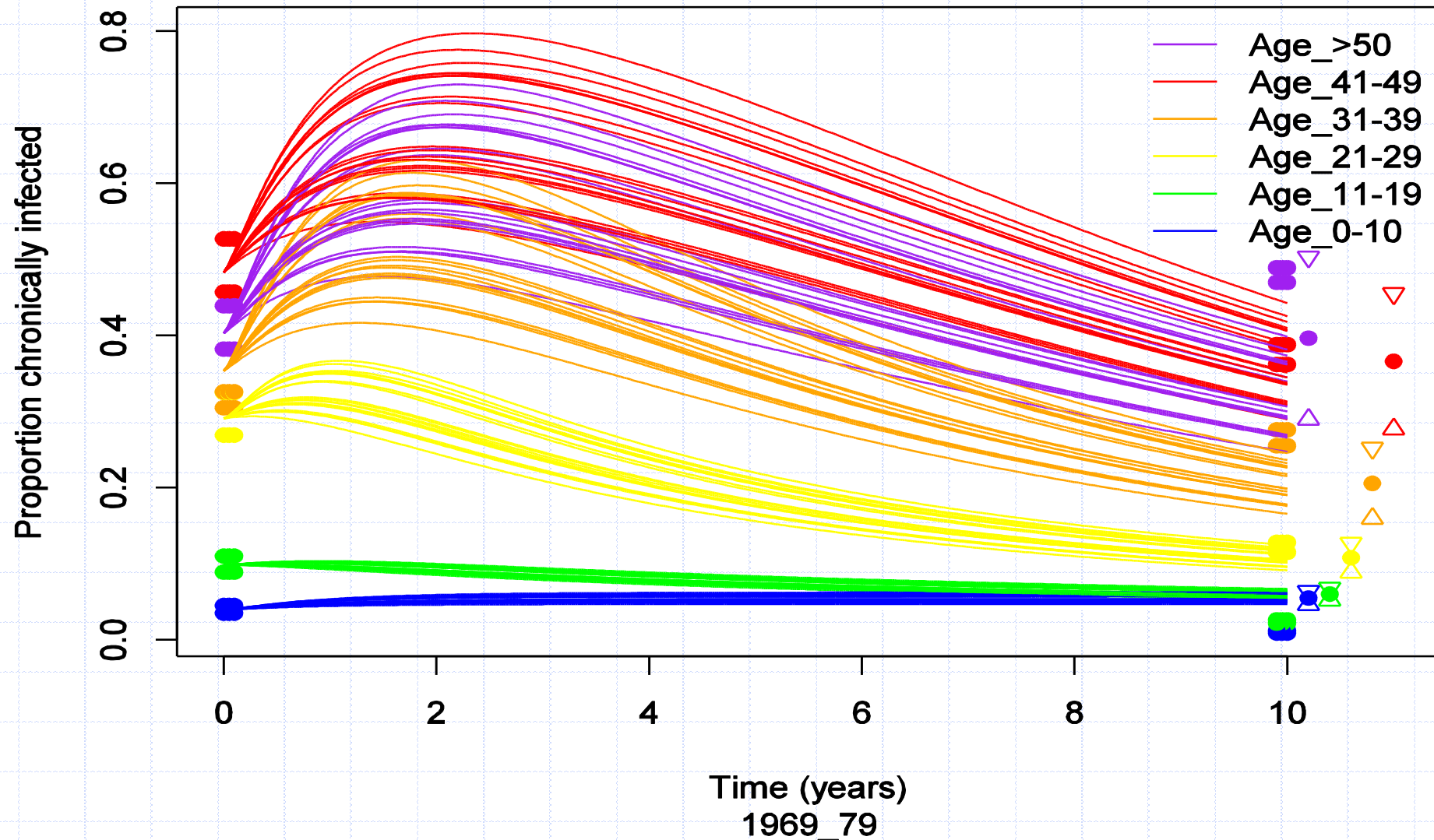


Six age classes and focus on decline in vectors and houses infected over 10

Peterson and Dobson, Vectors and Health; GATES NTD Modelling cons

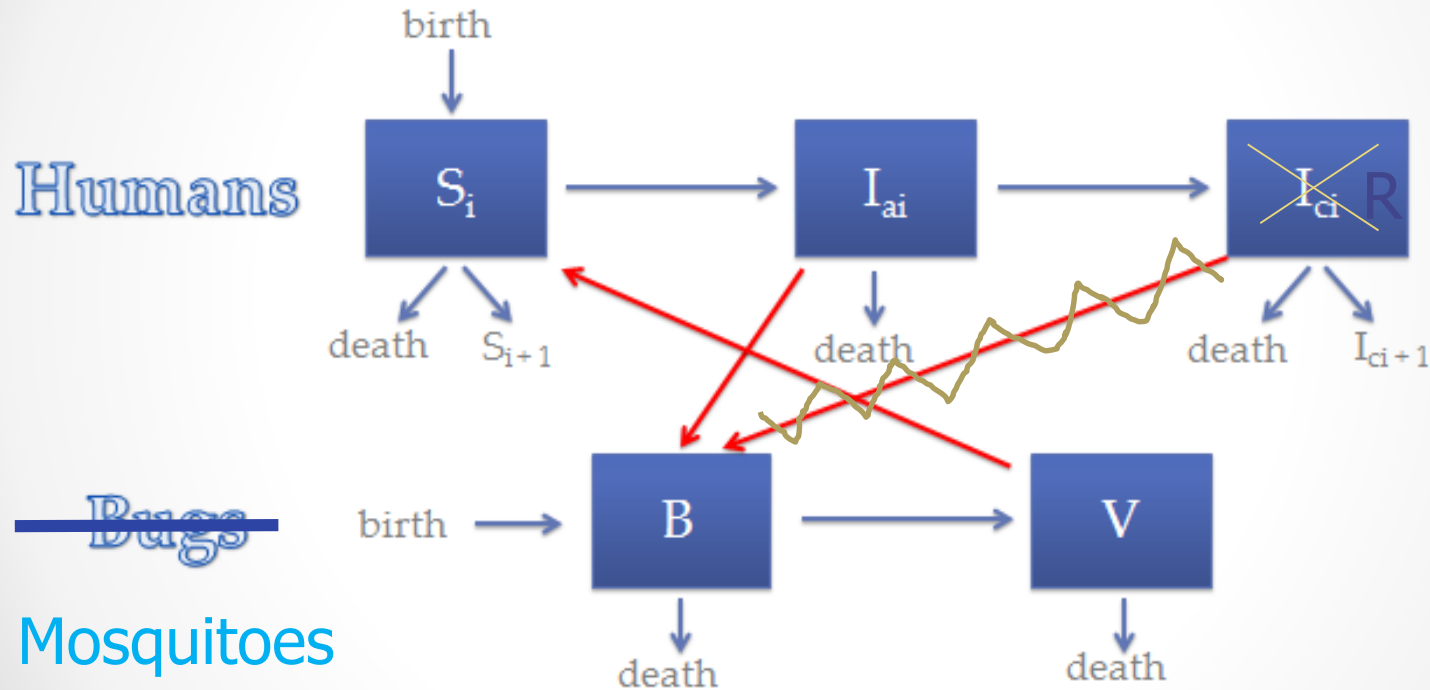
Forward projection 1969 to 1979

Age-Structured model for decadal Chagas prediction in Venezuela



Age-structured vector model

Modeling approach



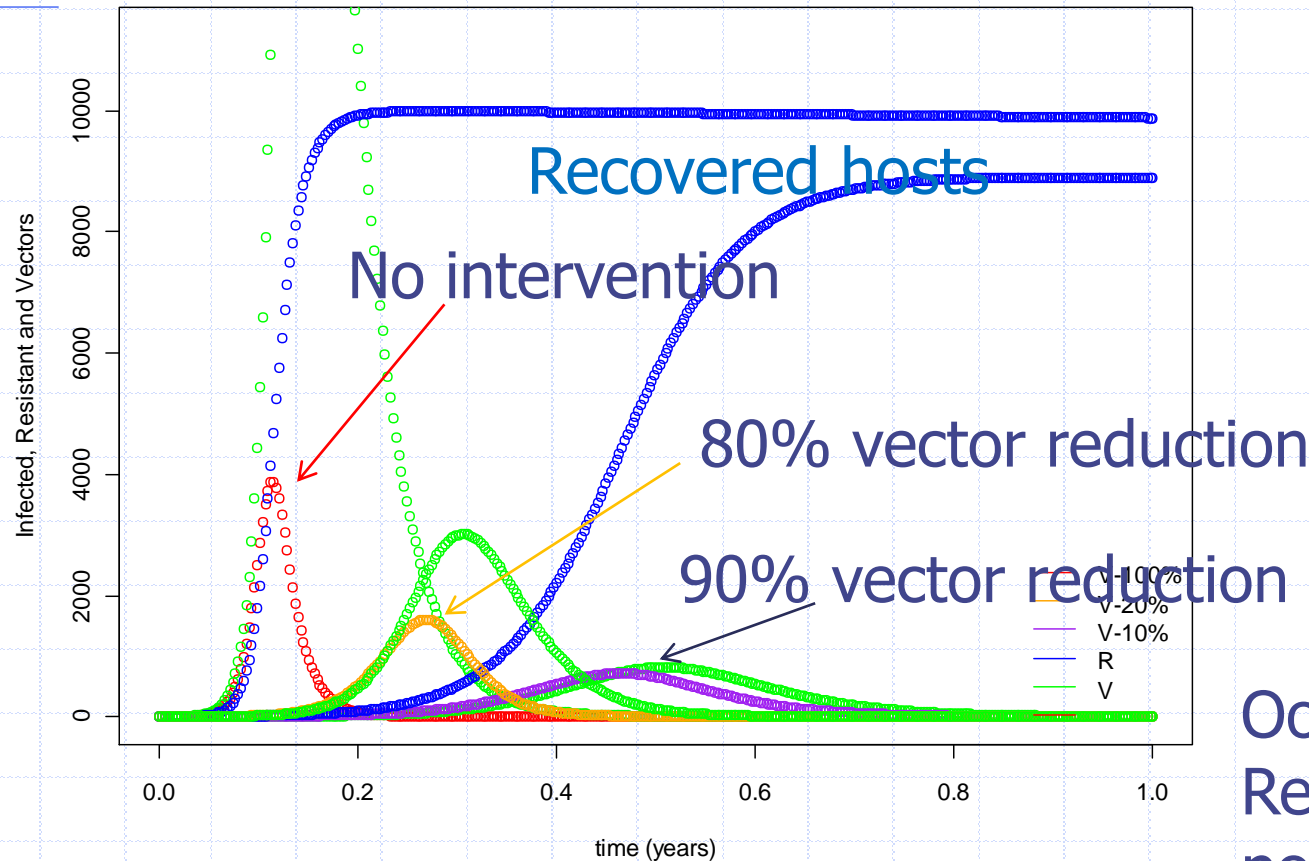
Six age classes and switch bugs to mosquitoes

Change chronics to recovered/resistants and speed up dynamics by around 100x

Infected and recovered and resistant hosts

Dynamics are driven by build up of herd immunity in human population

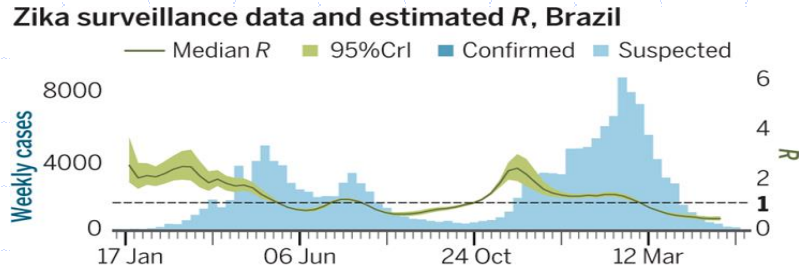
Initial reductions in Vector Abundance



Infected mosquitoes in green

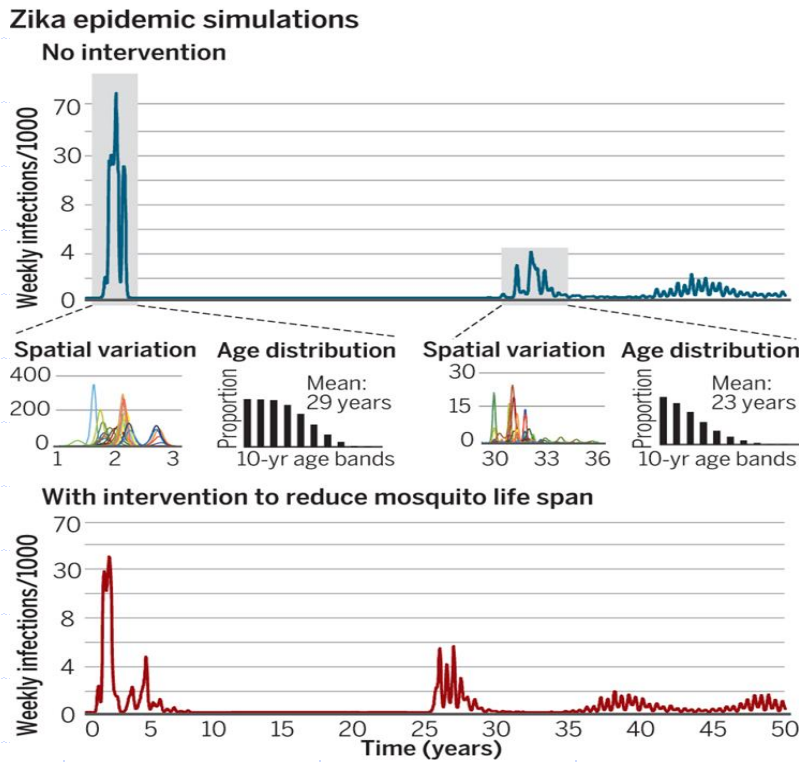
Ooopsss!!
Reduction in vector population has almost no impact on the total number of infected hosts!!

Zika transmission dynamics.



Dam!!

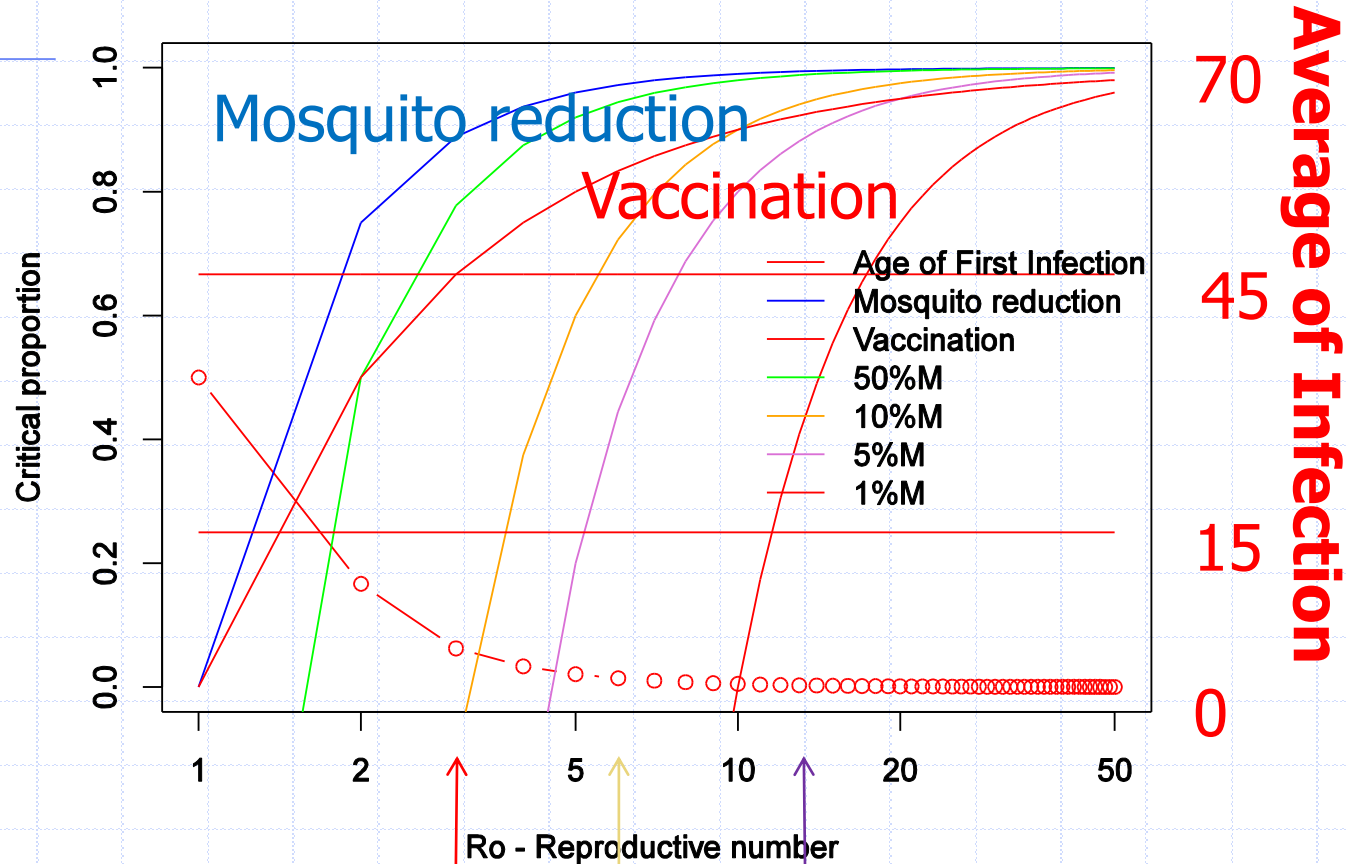
Pipped at the post!!



Neil M. Ferguson et al. Science 2016;353:353-354



Generalized control strategy for any vector borne disease



Average of Infection

70

45

15

0

This is key for Zika!!

Ro - Reproductive number

Zika

Dengue

Malaria

Herd immunity is very different for VBDs!!!

Dobson, Alonso, Peterson and Pascual (in need of a home..)

WAIFW matrices and R_0

Who Acquires Infection From Whom

(Schenzle, 1984; Anderson and May, 1985)

$$W = \begin{bmatrix} \beta_{ii} & \beta_{ij} & \beta_{ik} \\ \beta_{ji} & \beta_{jj} & \beta_{jk} \\ \beta_{ki} & \beta_{kj} & \beta_{kk} \end{bmatrix}$$



R_0 = basic
reproductive
number of the
pathogen

(Diekmann *et al.*, 1990)

Four special cases

1) All2All

$$\begin{bmatrix} \beta_{AA} & \beta_{AB} & \beta_{AC} & \beta_{AD} \\ \beta_{BA} & \beta_{BB} & \beta_{BC} & \beta_{BD} \\ \beta_{CA} & \beta_{CB} & \beta_{CC} & \beta_{CD} \\ \beta_{DA} & \beta_{DB} & \beta_{DC} & \beta_{DD} \end{bmatrix}$$

2) Asym2All

$$\begin{bmatrix} \beta_{AA} & 0 & 0 & 0 \\ \beta_{BA} & \beta_{BB} & 0 & 0 \\ \beta_{CA} & \beta_{CB} & \beta_{CC} & \beta_{CD} \\ \beta_{DA} & \beta_{DB} & \beta_{DC} & \beta_{DD} \end{bmatrix}$$

$$\begin{bmatrix} \beta_{AA} & 0 & 0 & 0 \\ \beta_{BA} & \beta_{BB} & 0 & 0 \\ 0 & \beta_{CB} & \beta_{CC} & 0 \\ 0 & 0 & \beta_{DC} & \beta_{DD} \end{bmatrix}$$

3) SpecChain

$$\begin{bmatrix} 0 & 0 & 0 & \beta_{AV} \\ 0 & 0 & 0 & \beta_{BV} \\ 0 & 0 & 0 & \beta_{CV} \\ \beta_{VA} & \beta_{VB} & \beta_{VC} & v(?) \end{bmatrix}$$

4) All2Vector

Ticks versus mosquitoes I

Basic matrix expression for 'next generation' of infections
whenever an infected host is introduced into the population

$$\begin{array}{c} \text{Transmission vector} \\ \text{To host} \end{array}
 M = \begin{array}{c} \text{Transmission host to vector} \\ \left(\begin{array}{ccc} 0 & \frac{M \beta B}{\mu(B + nC)} & \frac{M \beta nC}{\mu(B + nC)} \\ \frac{bB}{(B + nC)} & 0 & 0 \\ \frac{cnC}{(B + nC)} & 0 & 0 \end{array} \right) \end{array}$$

The basic reproductive number for the pathogen, R_0 , is then given by the dominant eigenvalue of this matrix

Key assumption – M is vector abundance – independent of hosts for mosquitoes, dependent for ticks.

R_0 for insect vectored

This can readily be shown to generalize for n-species of hosts to

$$R_0 = \frac{1}{\sum_{i=1}^n a_i A_i} \sqrt{\frac{M \beta}{\mu} \left(\sum_{i=1}^n v_i (a_i A_i)^2 \right)}$$

Here a_i is the relative attraction of species i to mosquitoes,
 A_i is the abundance of species i and v_i is it's 'viability as a host' ($1/(\alpha_i + d_i + \delta_i)$).

R₀ for tick vectored

This needs to now vary with host abundance...

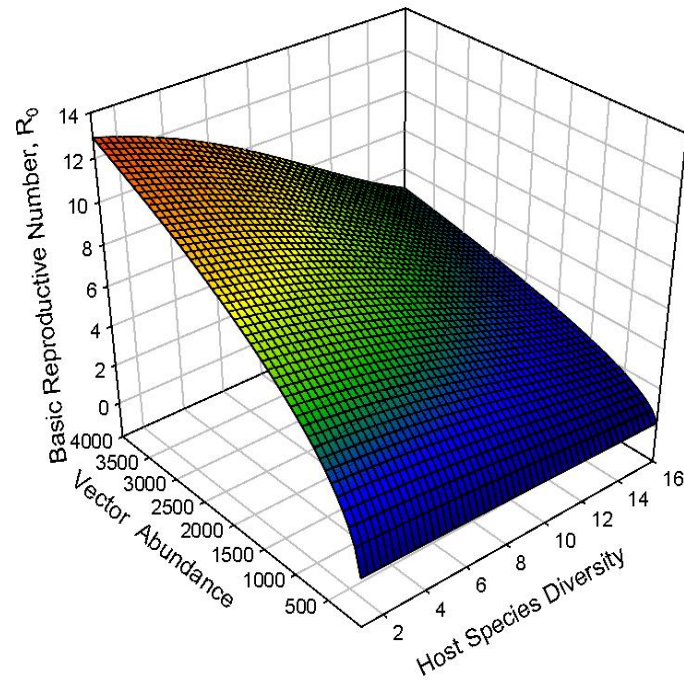
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$$R_0 = \frac{1}{\sum_{i=1}^n a_i A_i} \sqrt{\frac{M\beta}{\mu} \left(\sum_{i=1}^n v_i (a_i A_i)^2 \right)}$$

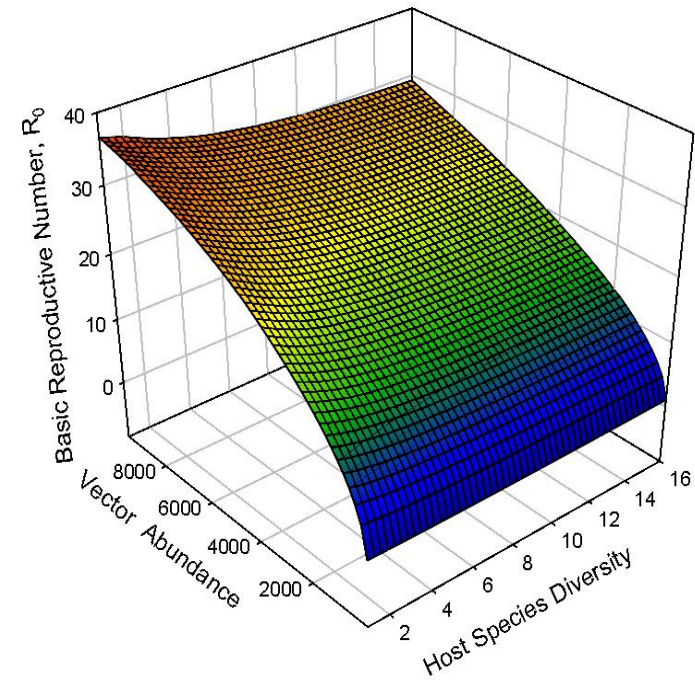
Here a_i is the relative attraction of species i to mosquitoes,
 A_i is the abundance of species i and v_i is its 'viability as a host' ($1/(\alpha_i + d_i + \delta_i)$).

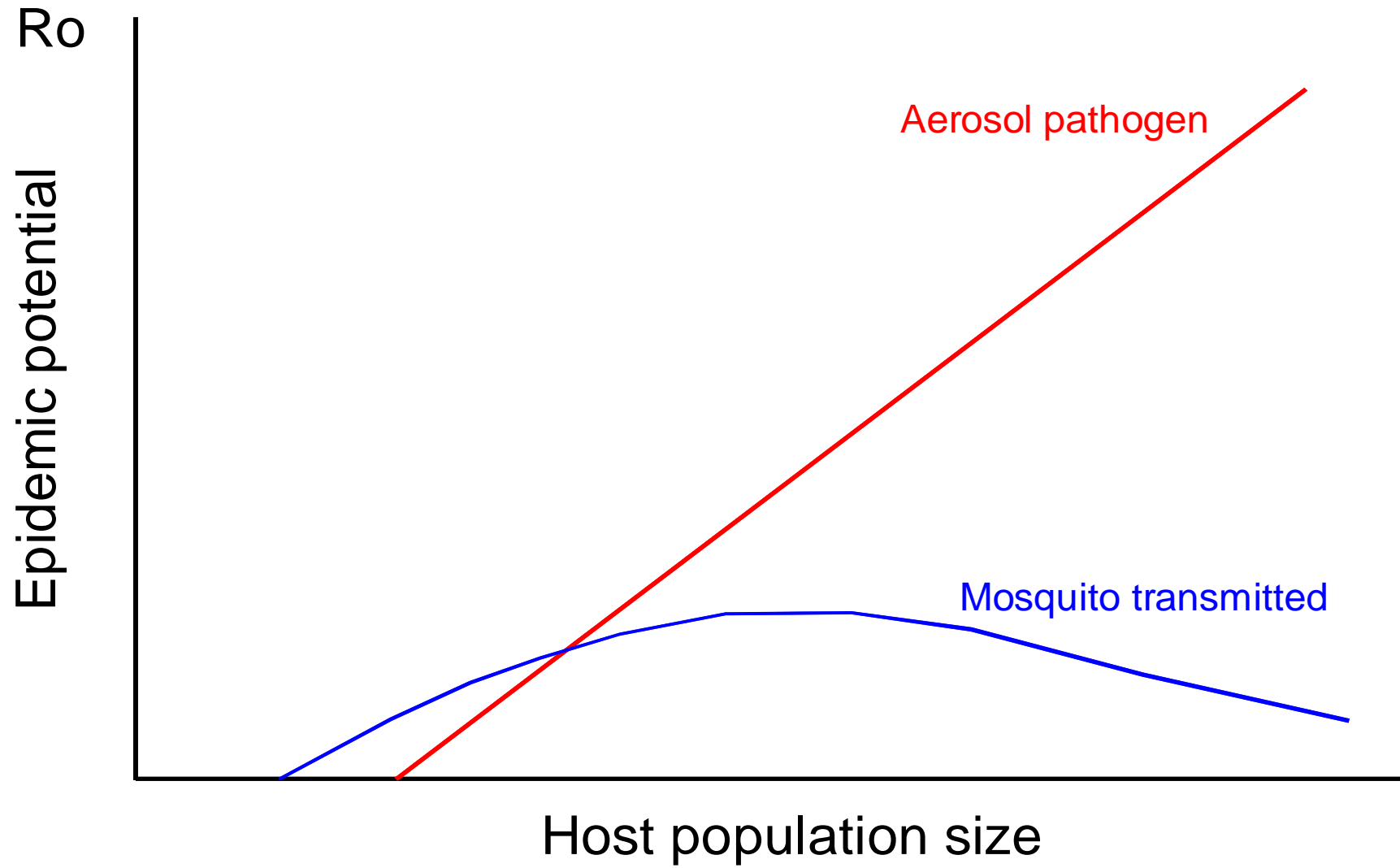
Mosquitoes versus ticks

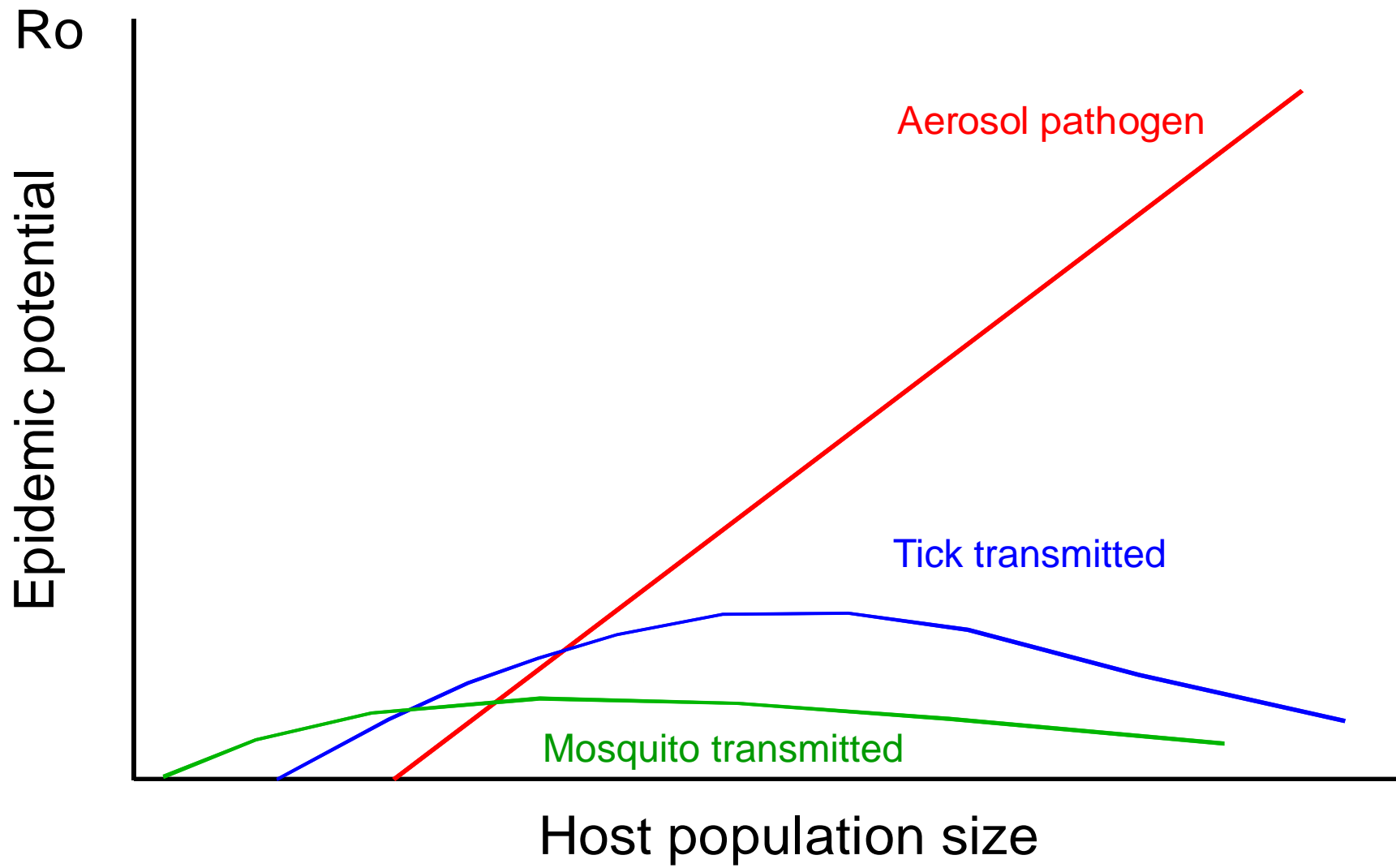
Mosquito Vector Abundance
and Dilution Effects



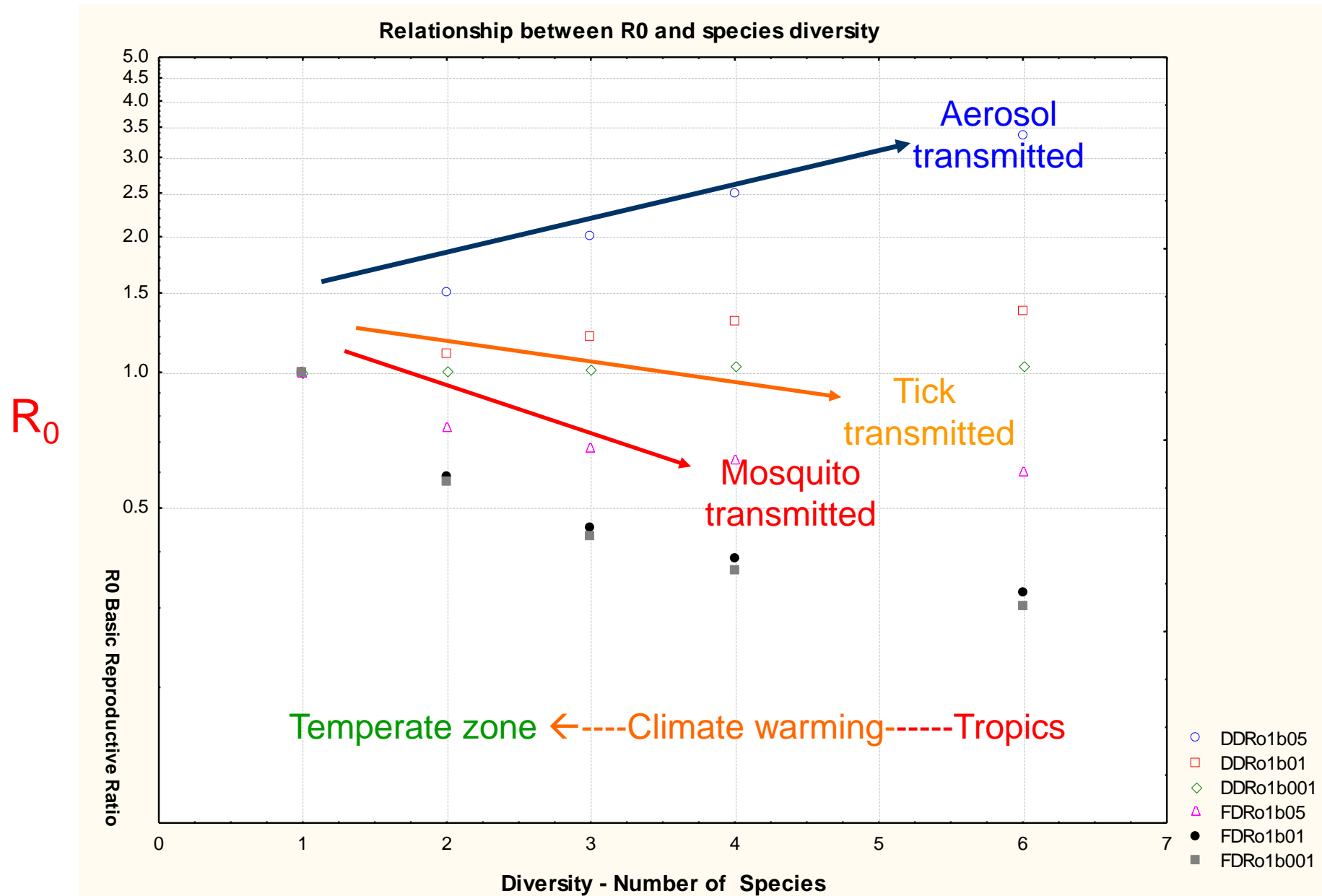
Tick Vector Abundance
and Dilution Effects





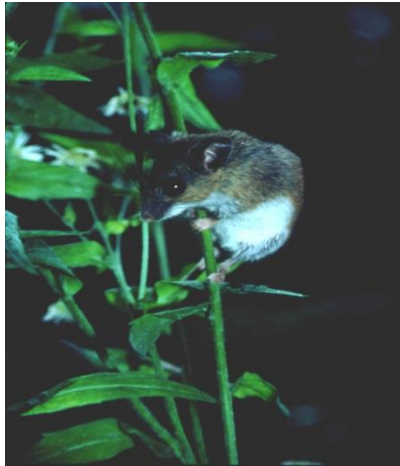


The relationship between biodiversity and potential for disease outbreaks



Lyme disease: the 'dilution effect'

R. Ostfeld *et al.*



Lyme disease

Reservoir host –
white-footed mouse

Vector - ticks



In my back yard in Princeton.....
.....also on campus, in Institute woods

BIODIVERSITY AND THE DILUTION EFFECT IN DISEASE ECOLOGY

KENNETH A. SCHMIDT¹ AND RICHARD S. OSTFELD

Institute of Ecosystem Studies, Box AB, Millbrook, New York 12545 USA

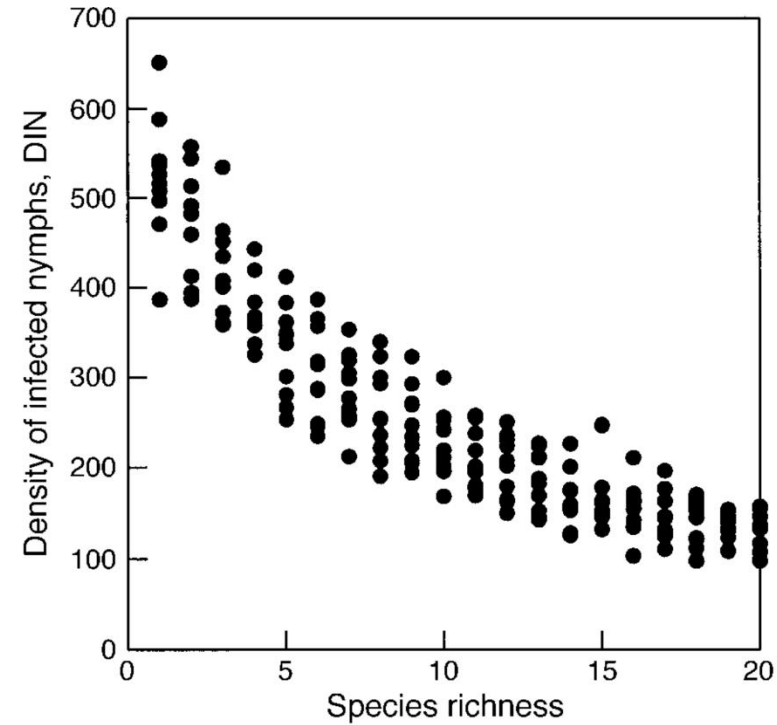
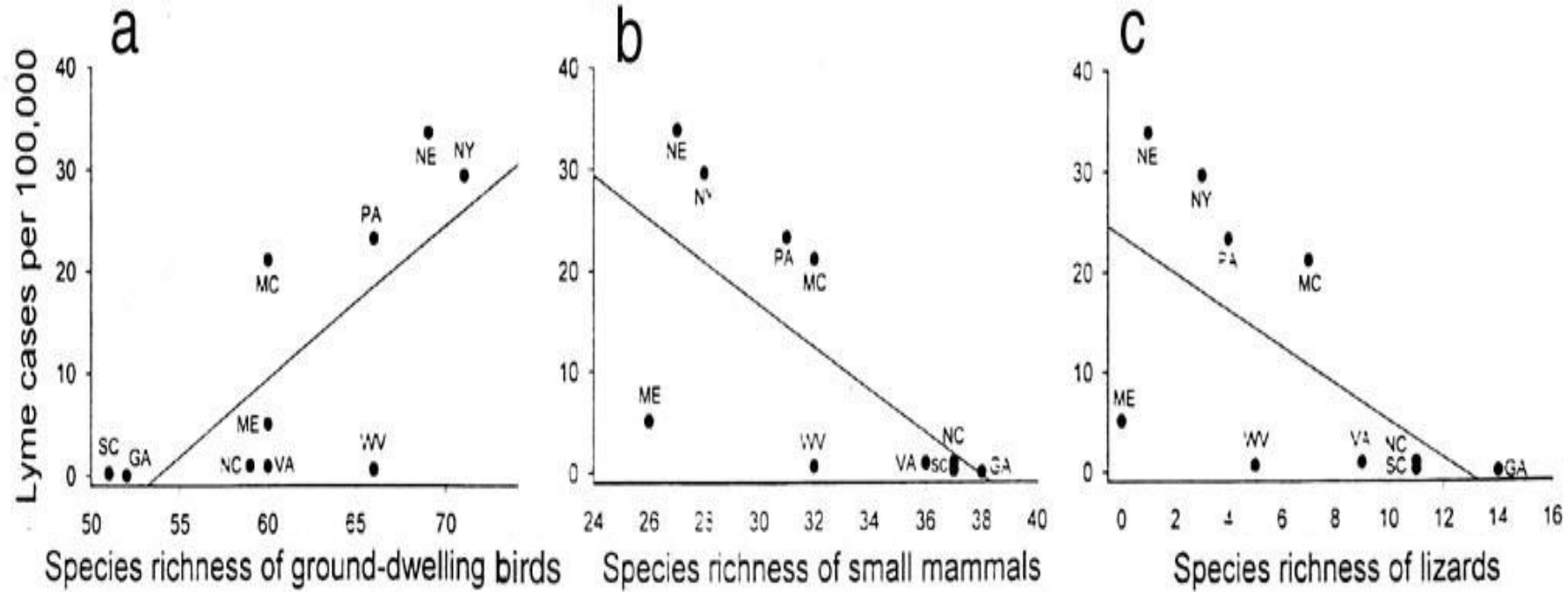


FIG. 2. The density of infected nymphs (DIN) declines with species richness (number of non-mouse, non-chipmunk hosts). Data were generated from 10 simulated host communities at each level of species richness (plus mice and chipmunks). DIN as used in Figs. 2–6 is based on the relative dominance and reservoir competence values assigned to host species in the model simulations and is for comparative purposes.



R. Ostfeld and F. Keesing,
 Conservation Biology 2000.

Host viability for Lyme disease and the ticks that transmit it

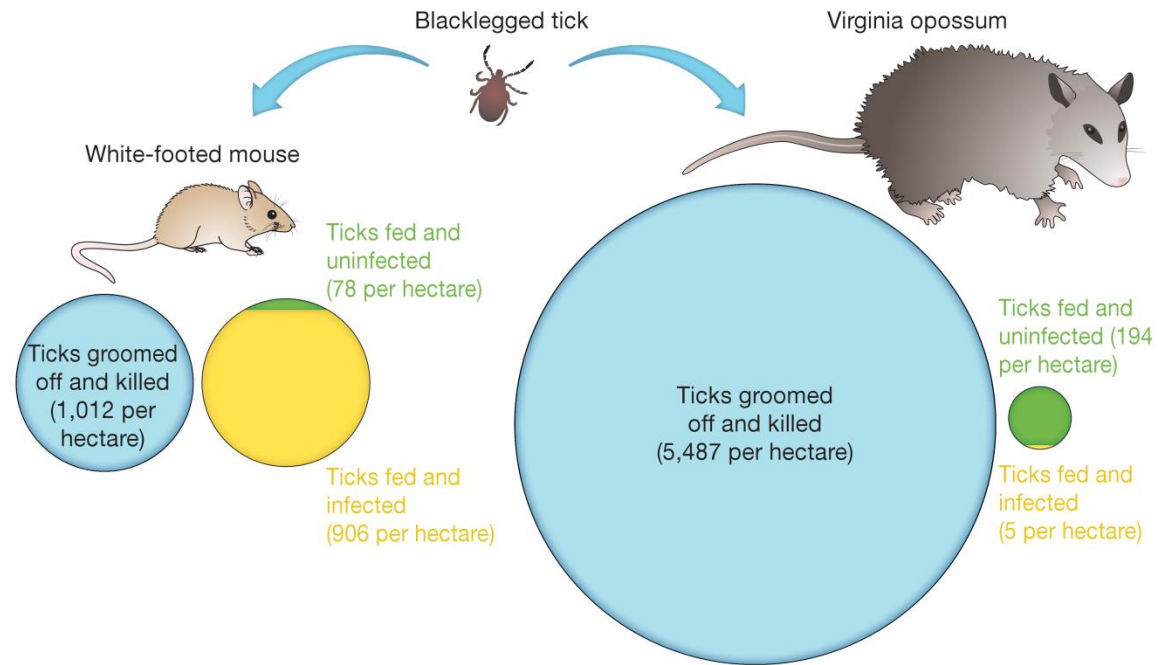
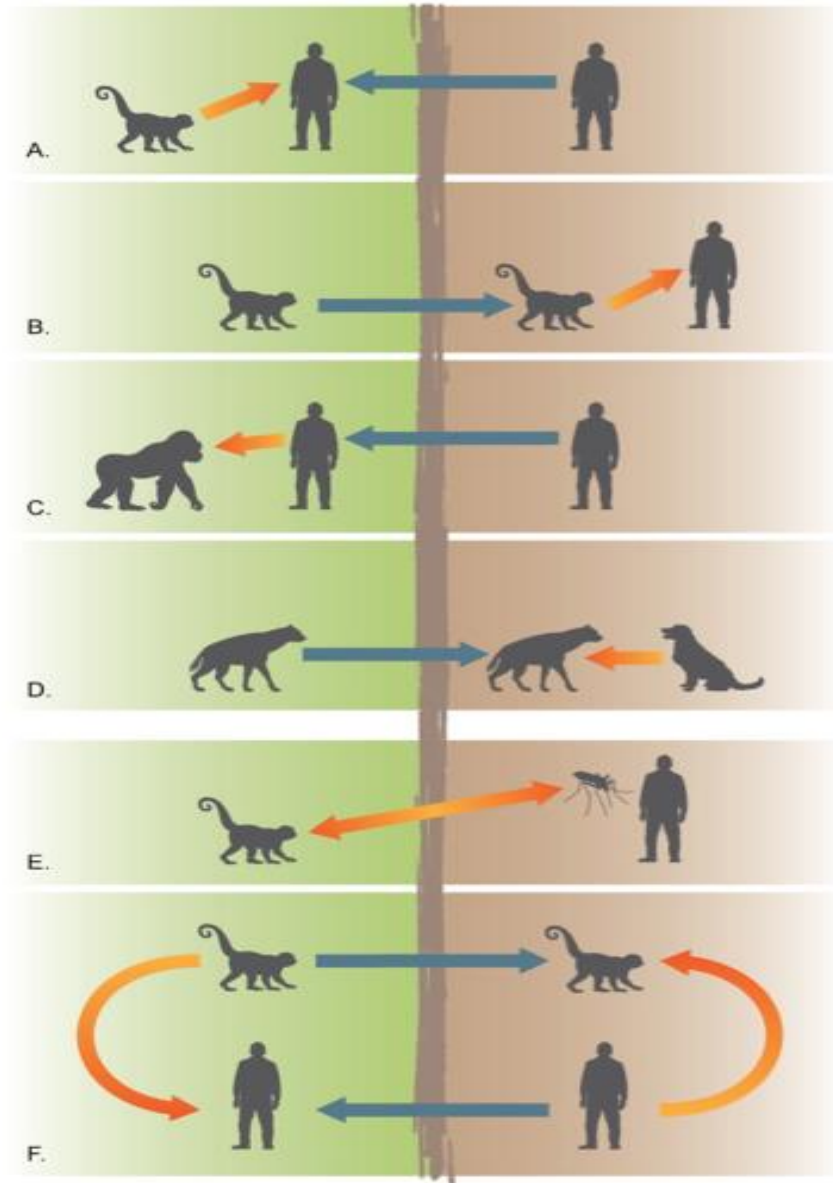


Figure 1 | Roles of host species in the transmission of Lyme disease in the northeastern USA. Lyme disease is transmitted to humans by the bite of an infected blacklegged tick (*Ixodes scapularis*). Immature ticks can acquire the infection if they feed on an infected host and can become infectious to humans if they subsequently survive to the next life stage. White-footed mice are abundant in northeastern forests and feed many ticks¹⁸. Ticks that attempt to

feed on Virginia opossums are likely to be groomed off and killed. Green-and-yellow circles show the mean number of ticks per hectare fed by mice or opossums; yellow shading shows the proportion of ticks infected after feeding. Blue circles show the mean number of ticks per hectare groomed off and killed. Ticks that feed on mice are highly likely to become infected with the bacterium that causes Lyme disease, whereas those that feed on opossums are not.

Habitat fragmentation in the Brazilian Amazon over the last 40 years.



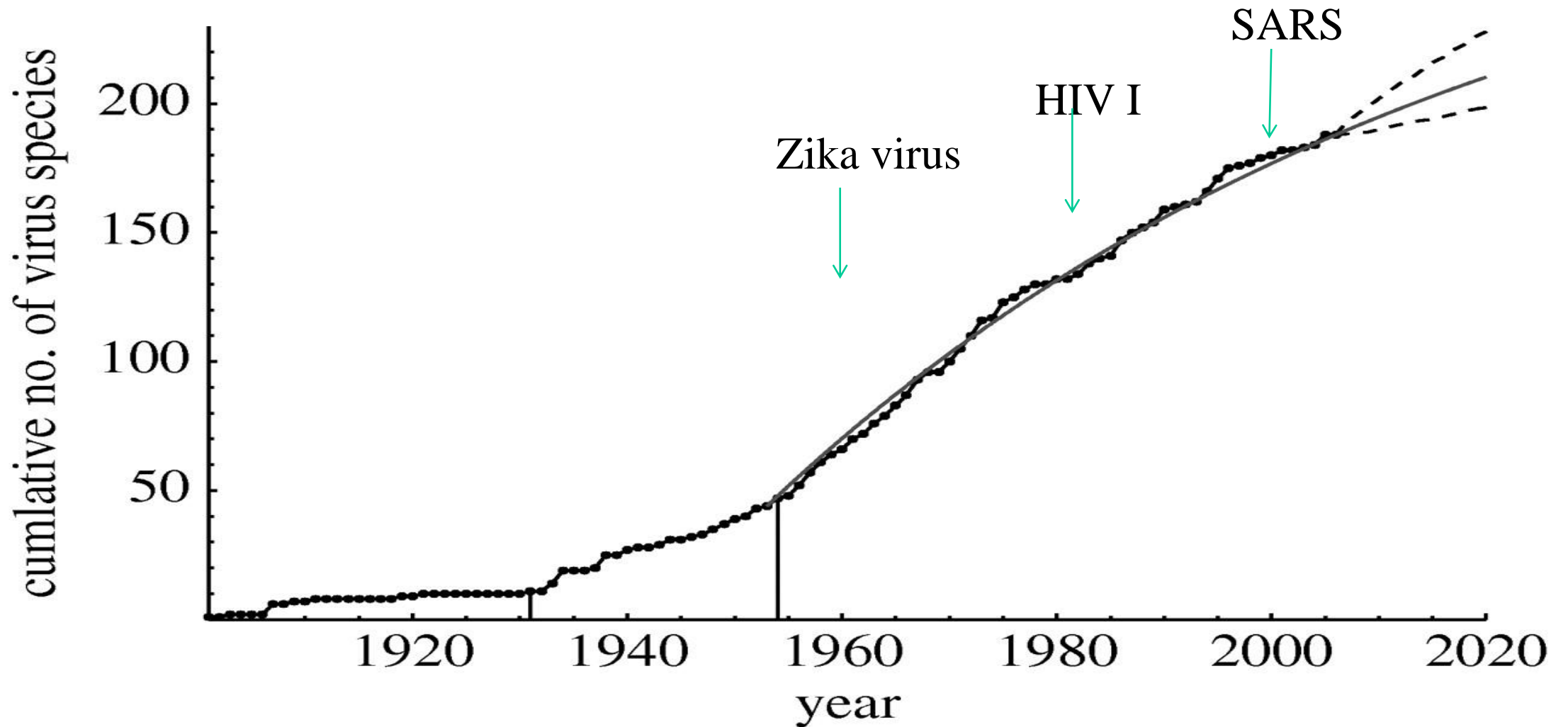


Ways in which pathogens 'jump' the species barrier to establish in new hosts

Core : Matrix

- Habitats

The discovery curve for human virus species.



Mark E.J Woolhouse et al. Proc. R. Soc. B 2008;275:2111-2115

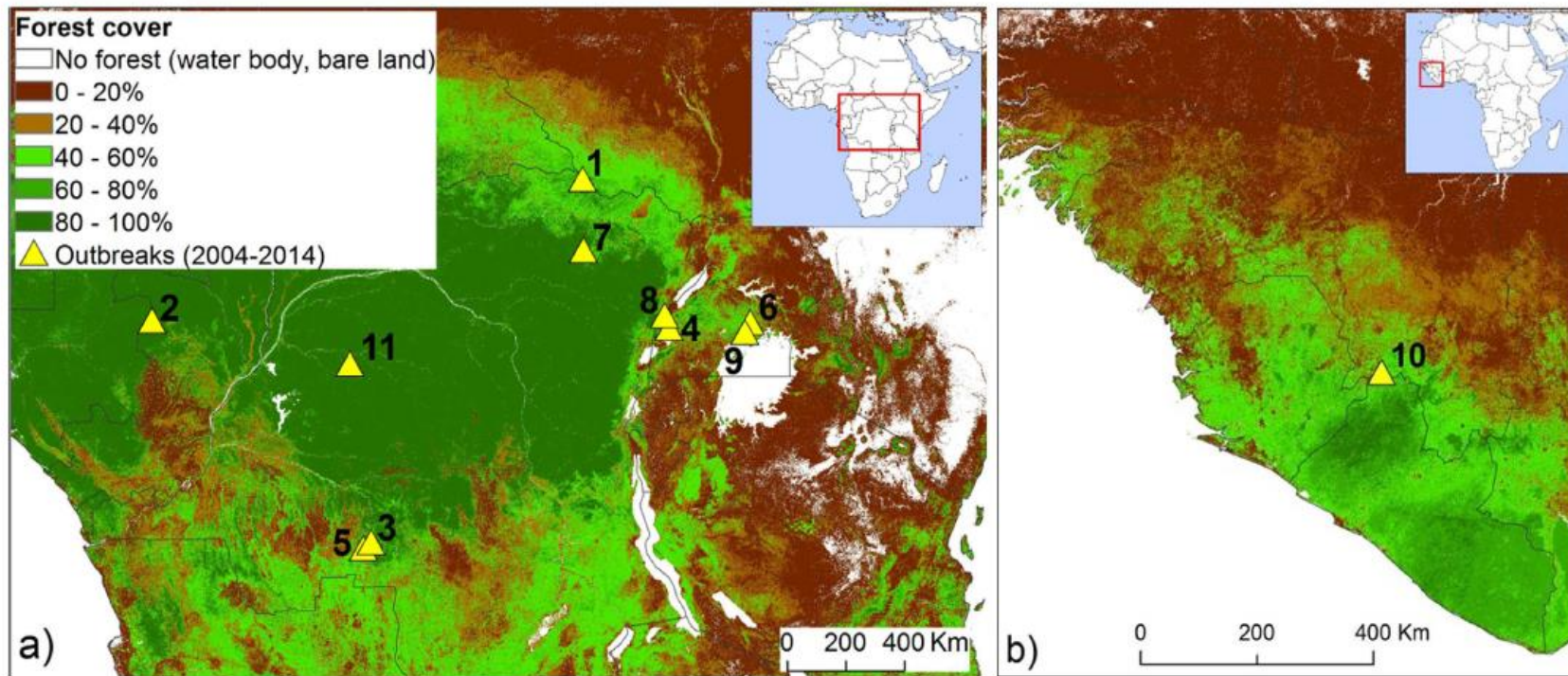


Figure 1. Forest cover maps and locations of first infection events in humans. Forest cover maps and locations of independent first infection events in humans (triangles, see Table 1) in Central (a) and West (b) Africa. The insets indicate the two African regions considered in this study. Legend in (b) is the same than in (a). Maps generated by the authors using ARCGIS 10.2-Version 10.2.0.338, licensed to Politecnico di Milano. The license term can be found on the following link: <http://www.esri.com/legal/software-license>.

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The nexus between forest fragmentation in Africa and Ebola virus disease outbreaks

Received: 17 August 2016
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Maria Cristina Rulli¹, Monia Santini², David T S Hayman³ & Paolo D'Odorico^{4,5,6}

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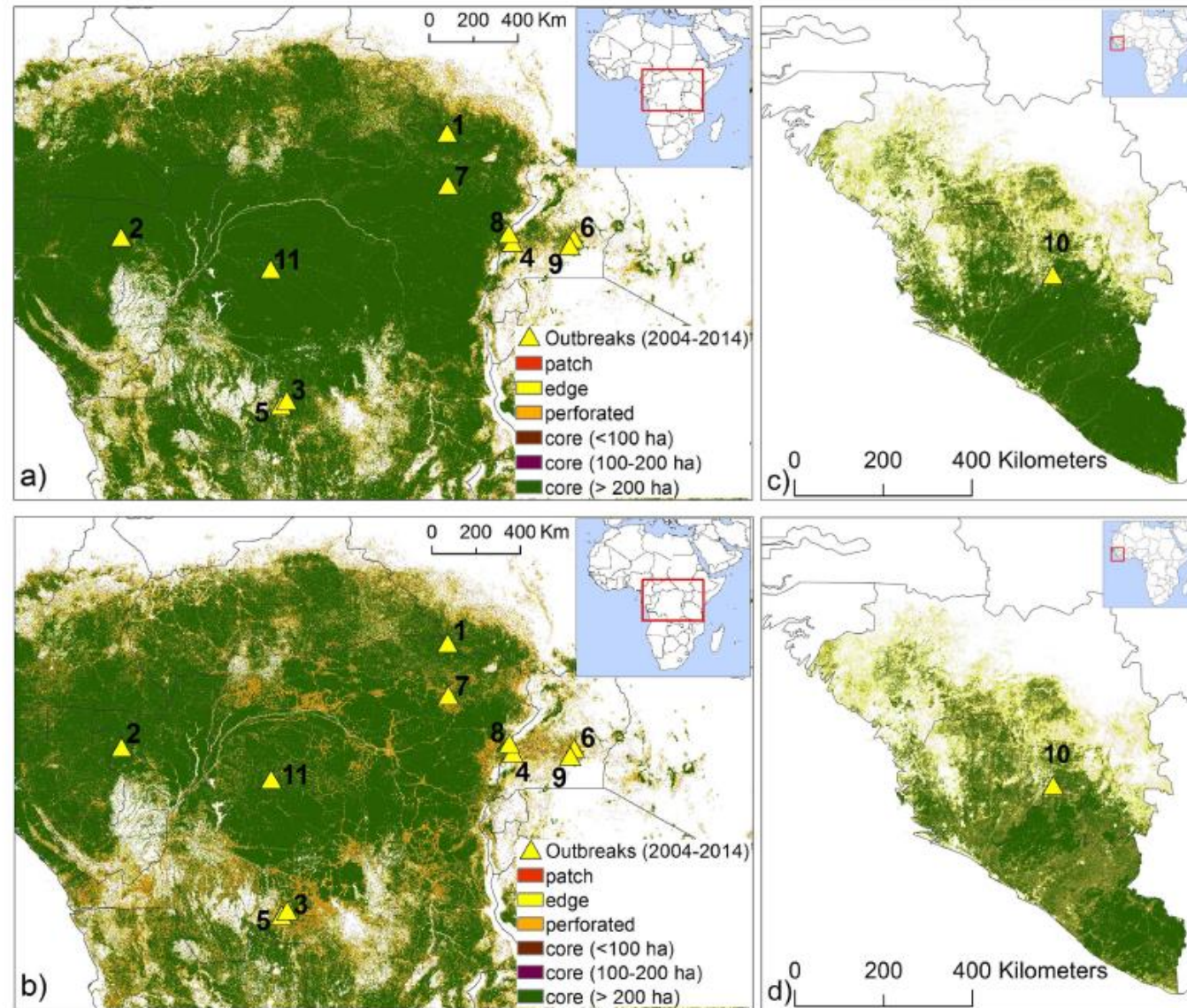
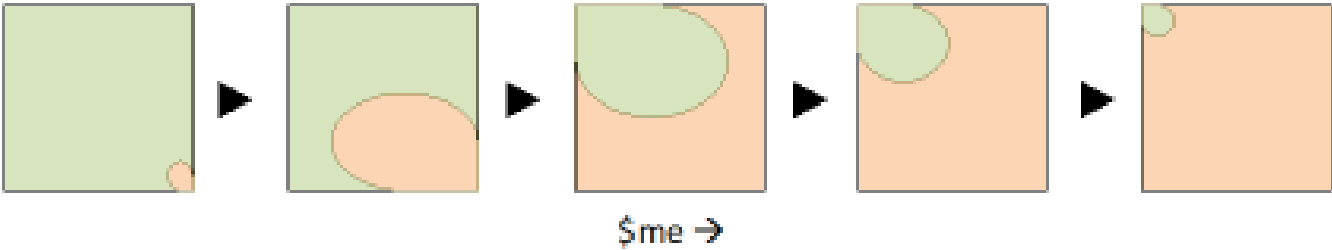
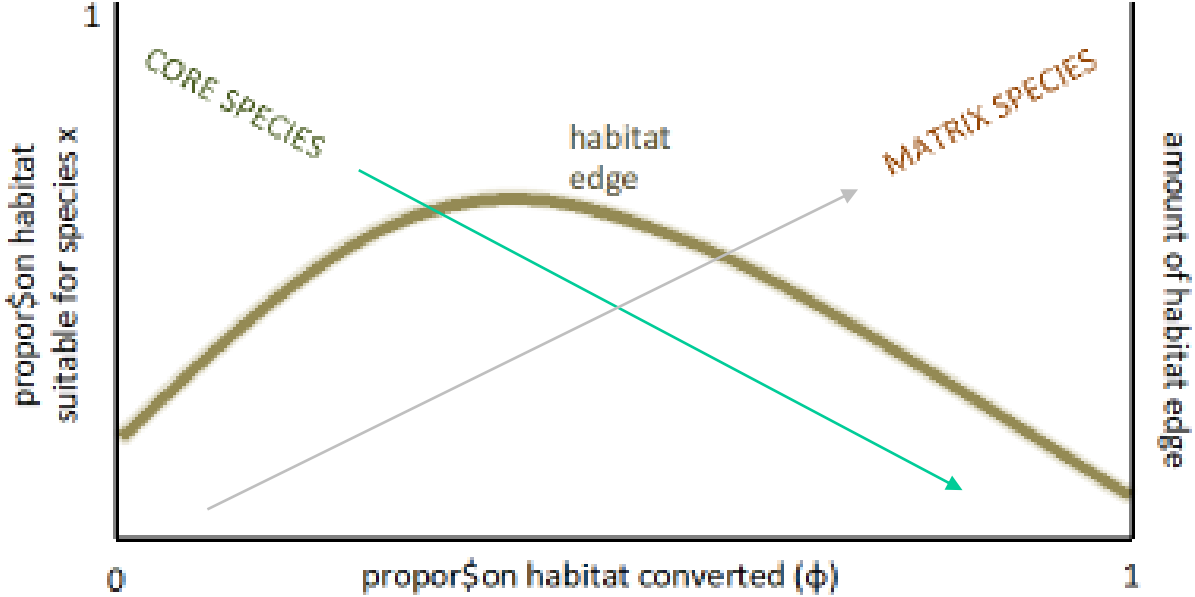


Figure 2. Forest fragmentation in Central and West Africa. Forest fragmentation in Central (panels a, and b)

Faust, McCallum, Bloomfield, Dobson, Plowright et al (in press)



Faust, McCallum, Bloomfield, Dobson , Plowright et al (in press)

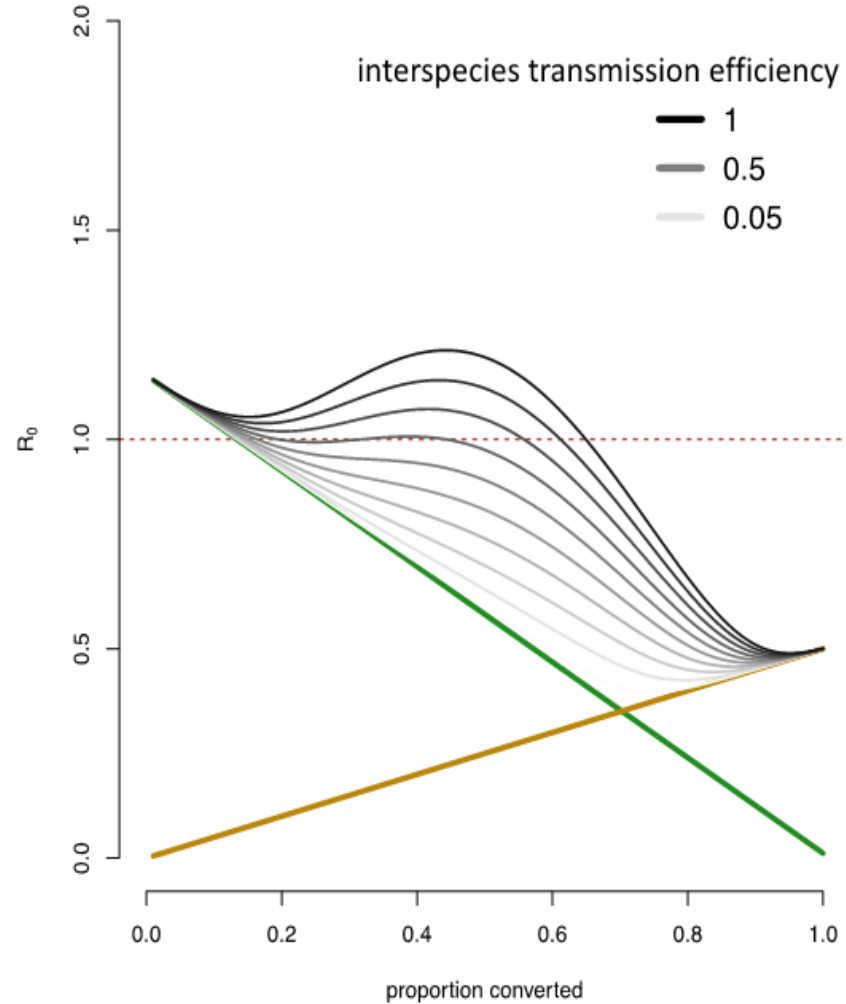
$$\frac{dS_i}{dt} = b_i N_i \left(1 - \frac{N_i}{K_{ia}} \right) - \frac{S_i(\beta_{ii}I_i + \psi \sum_j^n \beta_{ij}I_j)}{a} - d_i S_i, \quad (2.1)$$

$$\frac{dI_i}{dt} = \frac{S_i(\beta_{ii}I_i + \psi \sum_j^n \beta_{ij}I_j)}{a} - I_i(\alpha_i + \gamma_i + d_i) \quad (2.2)$$

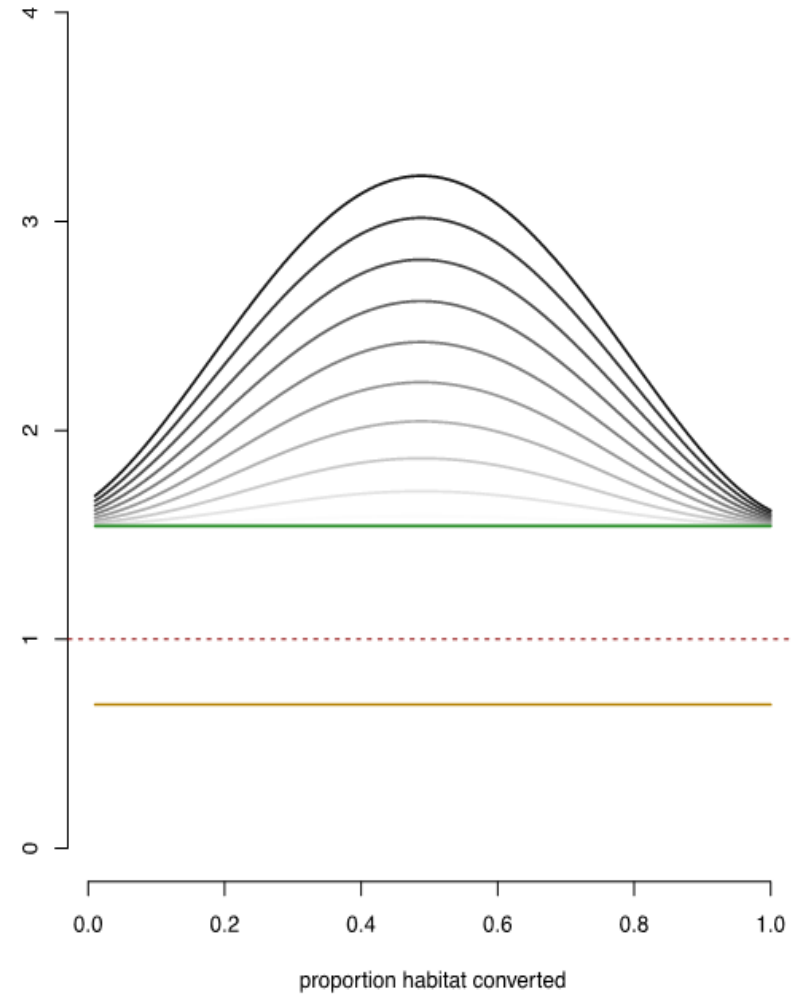
$$\text{and } \frac{dR_i}{dt} = \gamma_i I_i - d_i R_i. \quad (2.3)$$

Faust, McCallum, Bloomfield, Dobson, Plowright et al (in press)

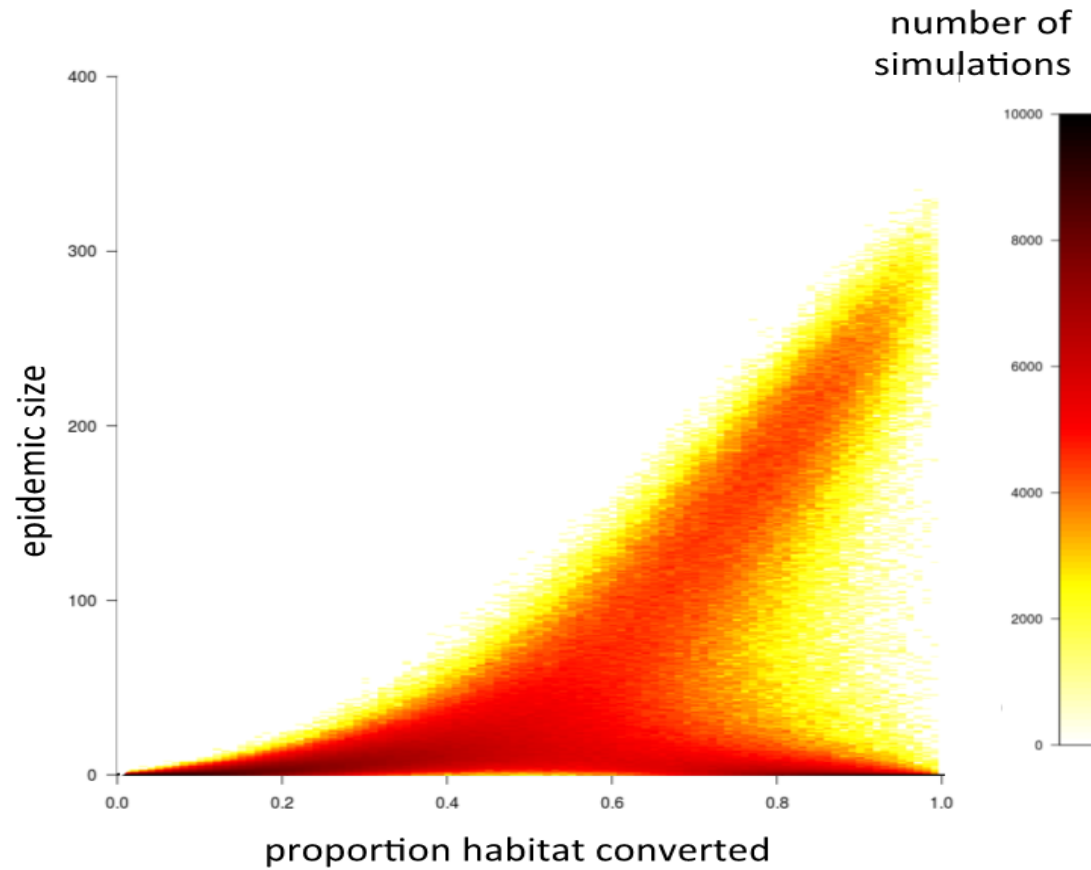
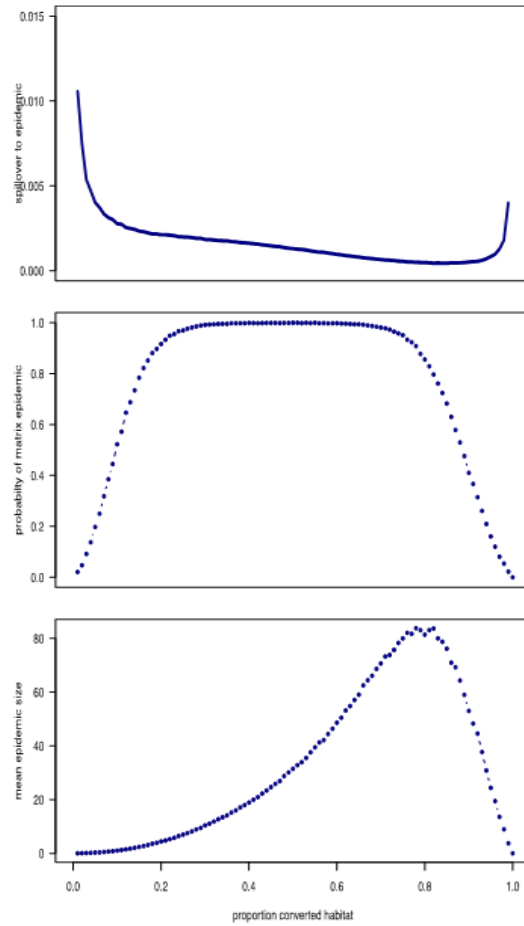
A. density-dependent transmission



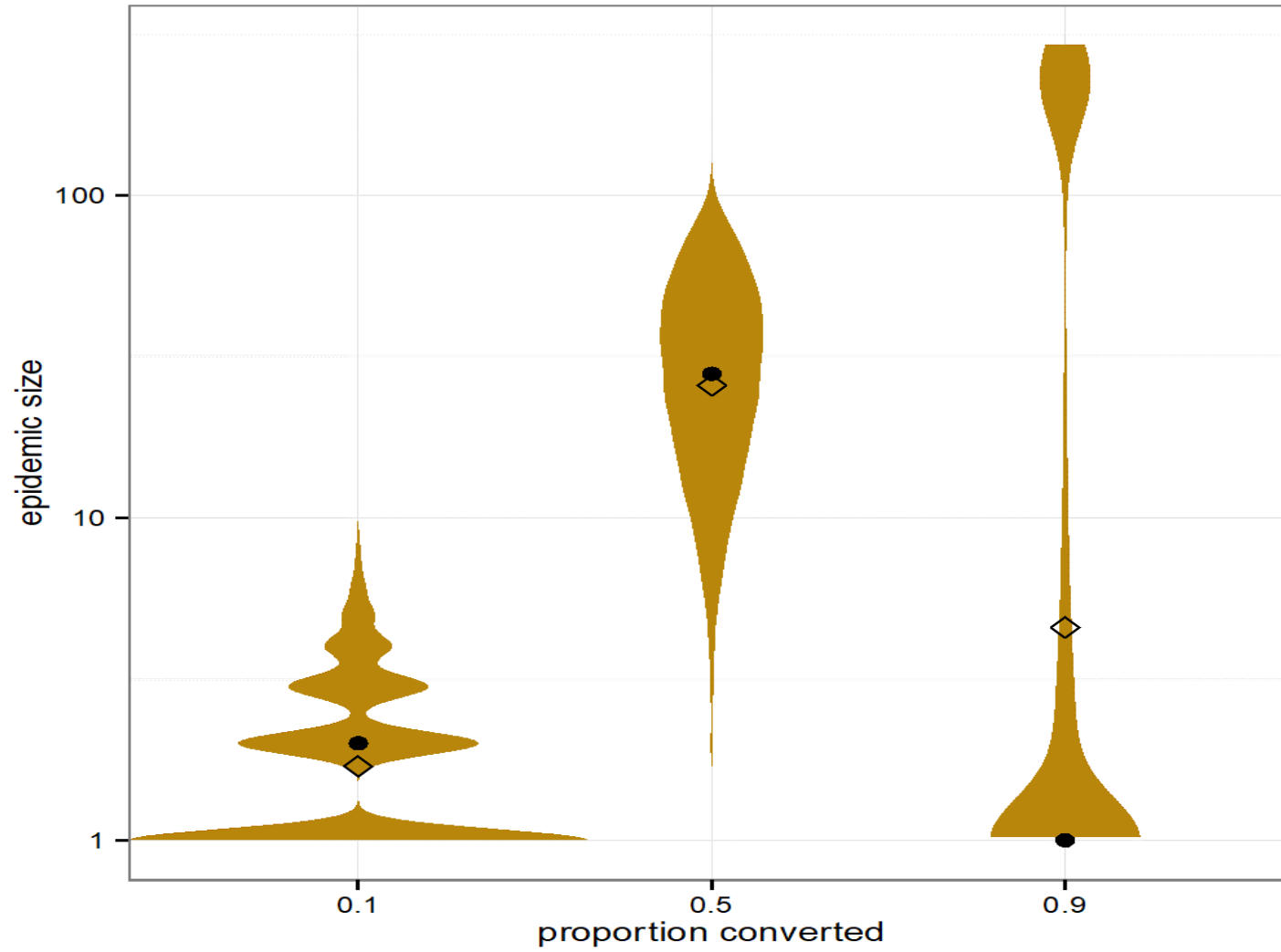
B. frequency-dependent transmission



Faust, McCallum, Bloomfield, Dobson , Plowright et al (in press)

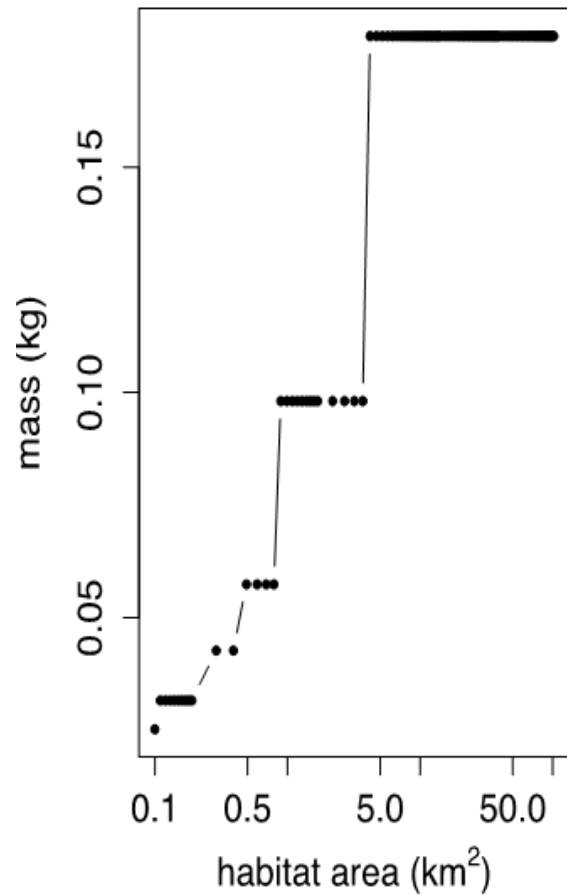


Faust, McCallum, Bloomfield, Dobson , Plowright et al (in press)

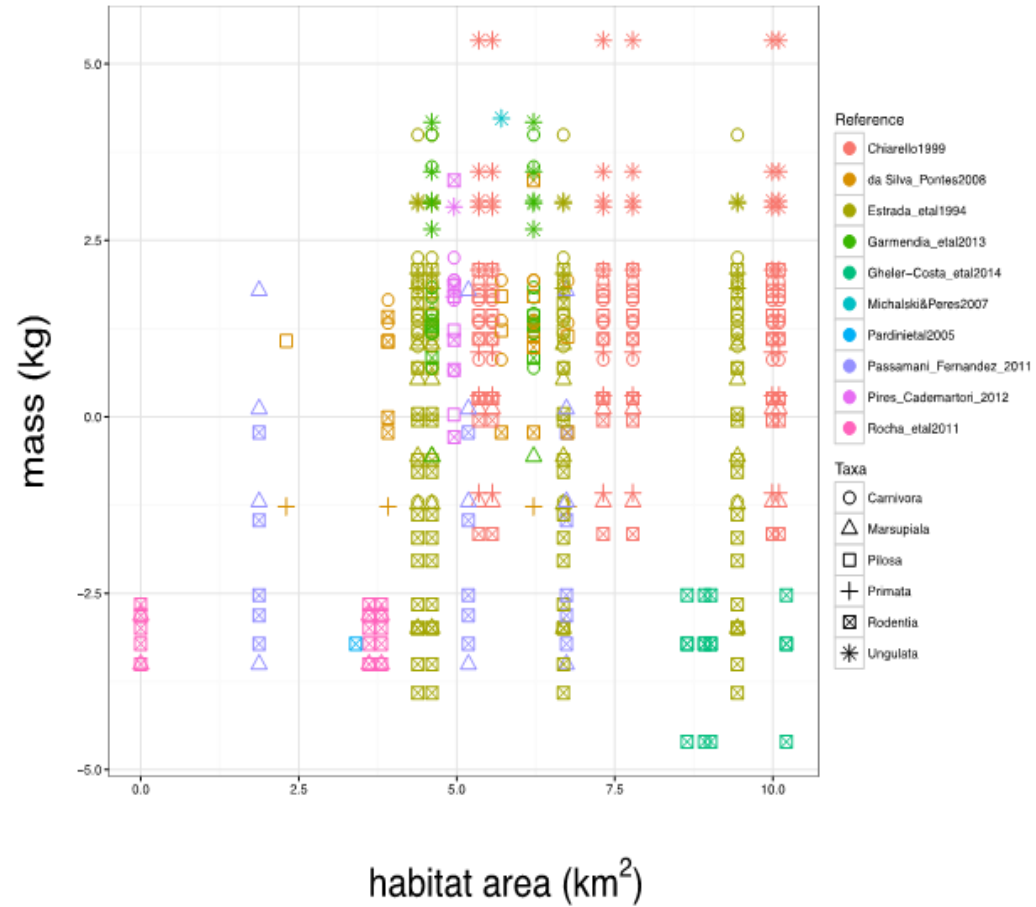


What happens in any individual patch as it erodes?

A. Simulated body size



B. Empirical data

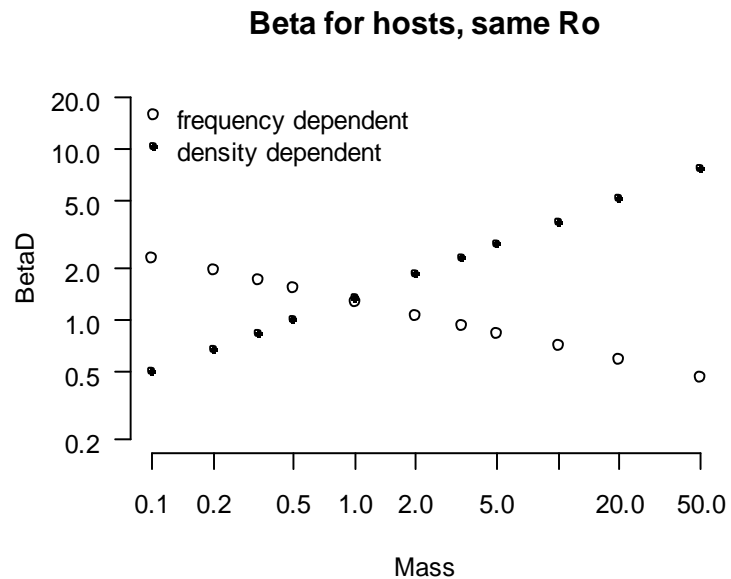
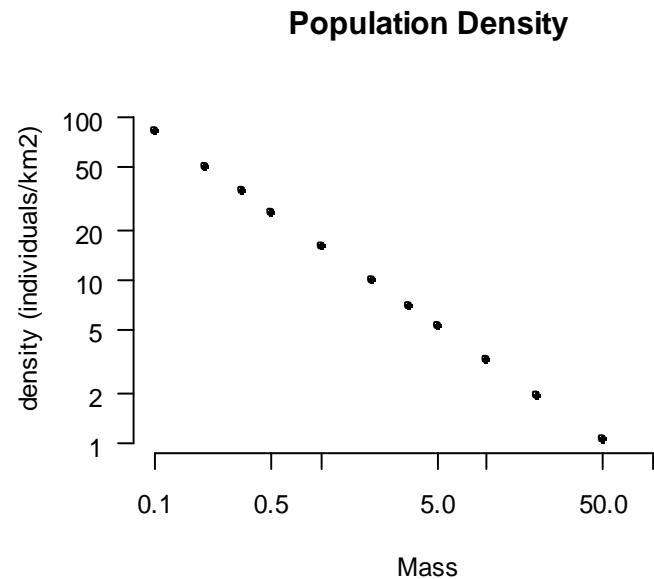
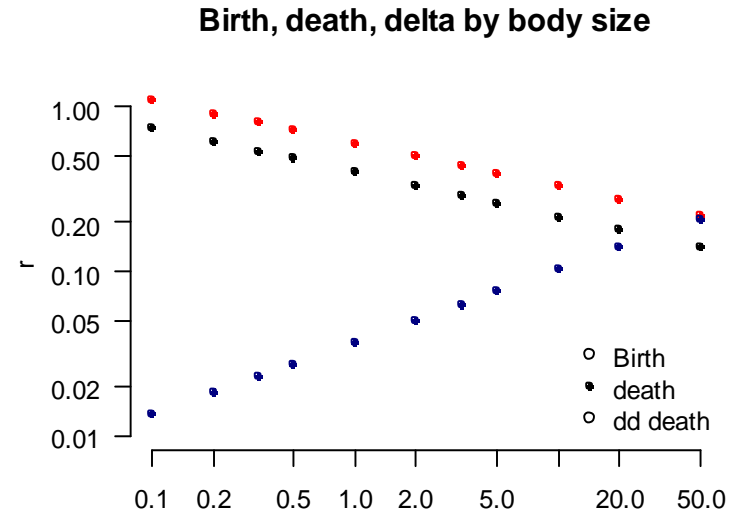
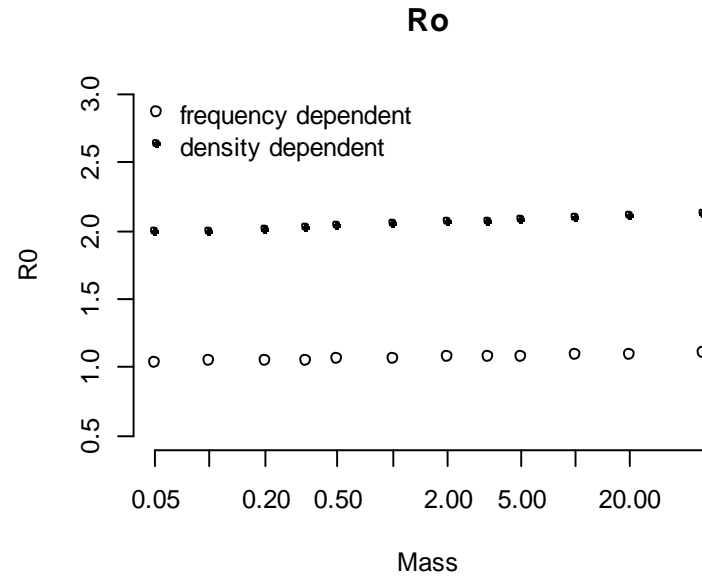


Habitat patch occupancy by body size. A) The simulated average body size in a patch at disease free equilibrium.

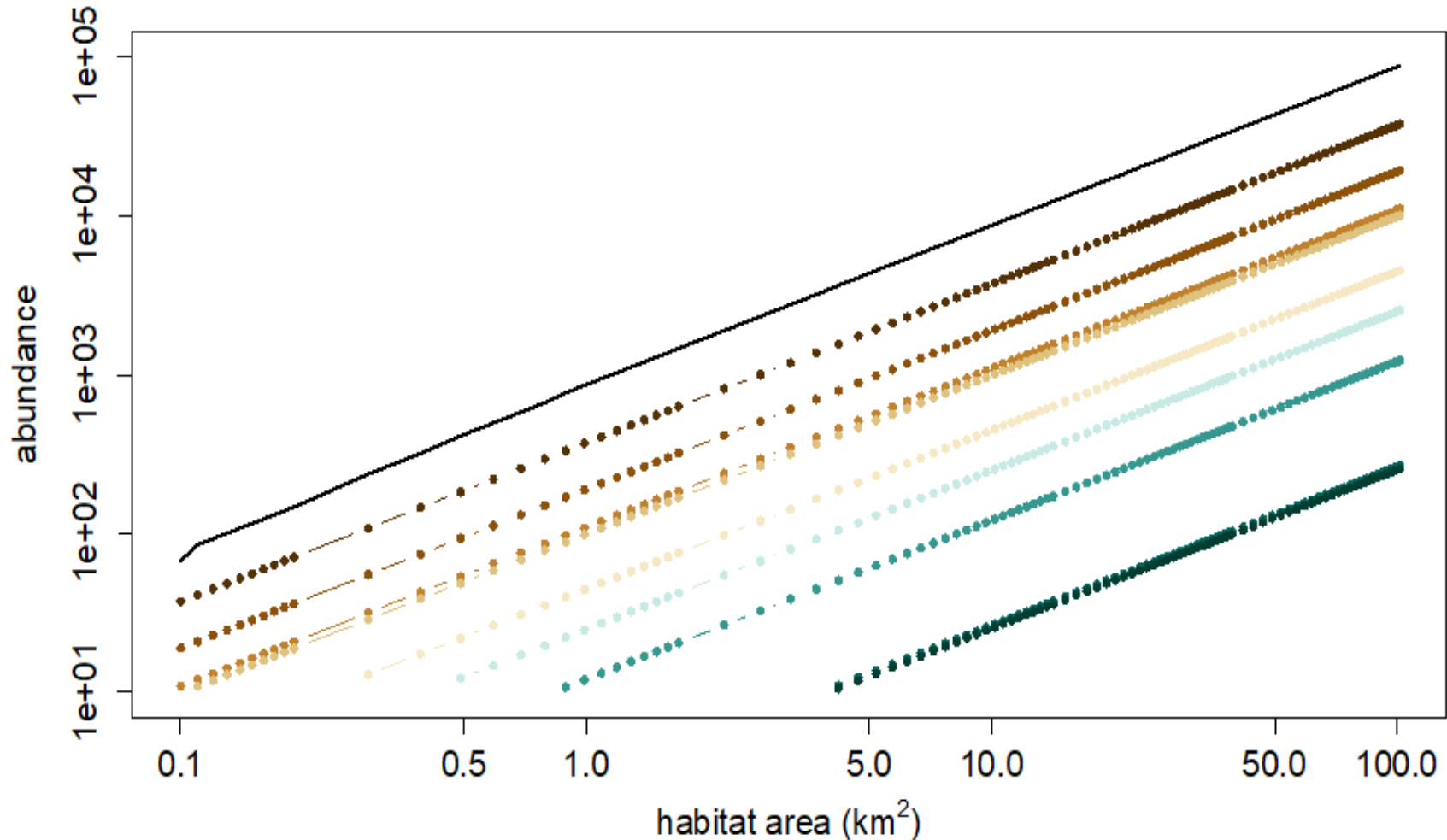
B) Empirical data from all studies that we could find showing that smaller bodied species are present in smaller patch sizes and persist in the larger patches when larger species are added (data from [10-20], listed in supplementary text information).

Faust, Dobson, Bloomfield, Gottdecker, McCallum, Gillespie, Plowright (2017)

Underlying demography based on allometric scaling with body size (DeLeo and Dobson, Nature 1997)

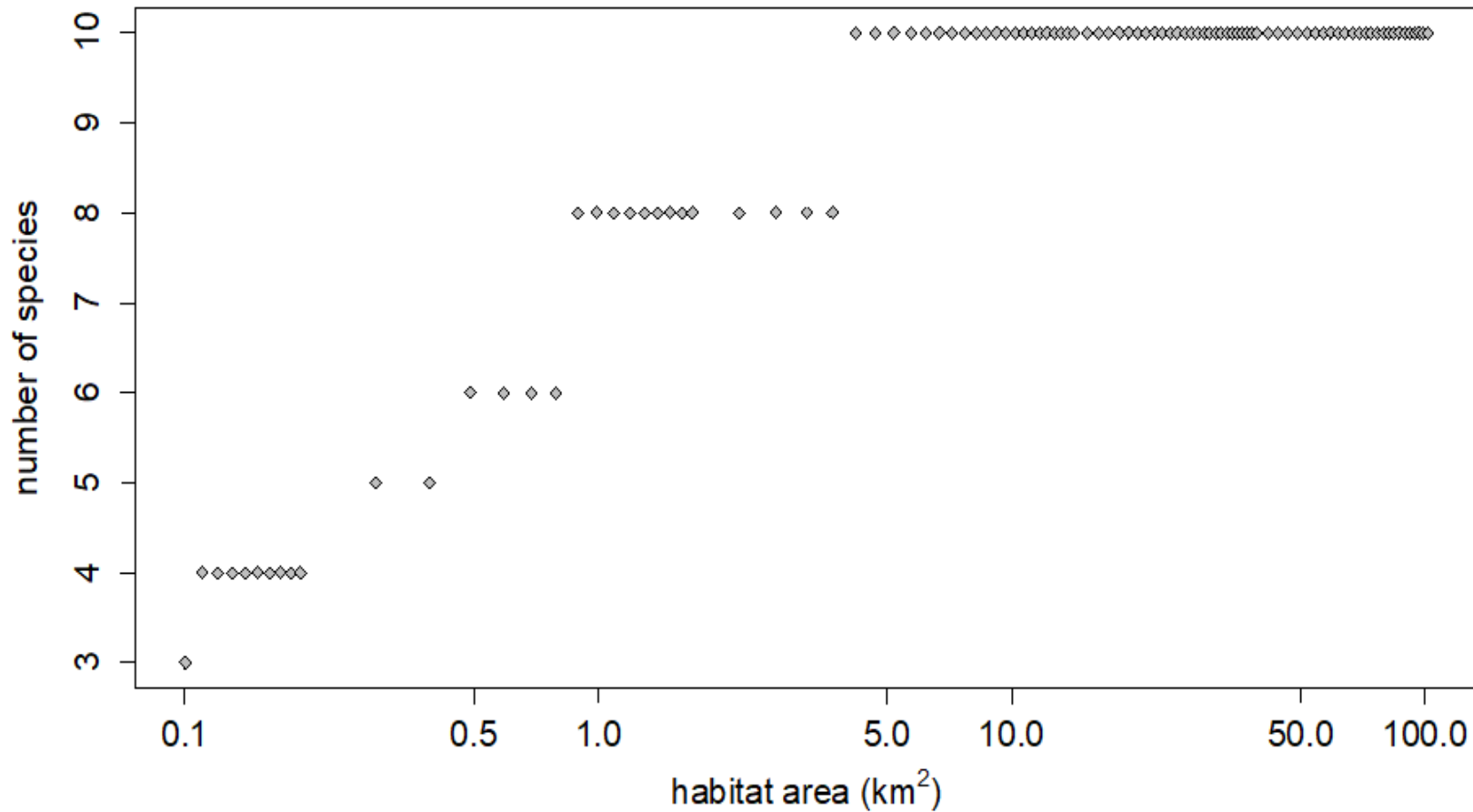


Abundance of species in a disease free equilibrium. The abundance of each species and total abundance in each habitat for example community (mean body size of 10 species = 0.011, 0.030, 0.065, 0.075, 0.23, 0.537, 1.505, 1.515, 13.333, and 14.201 kg).



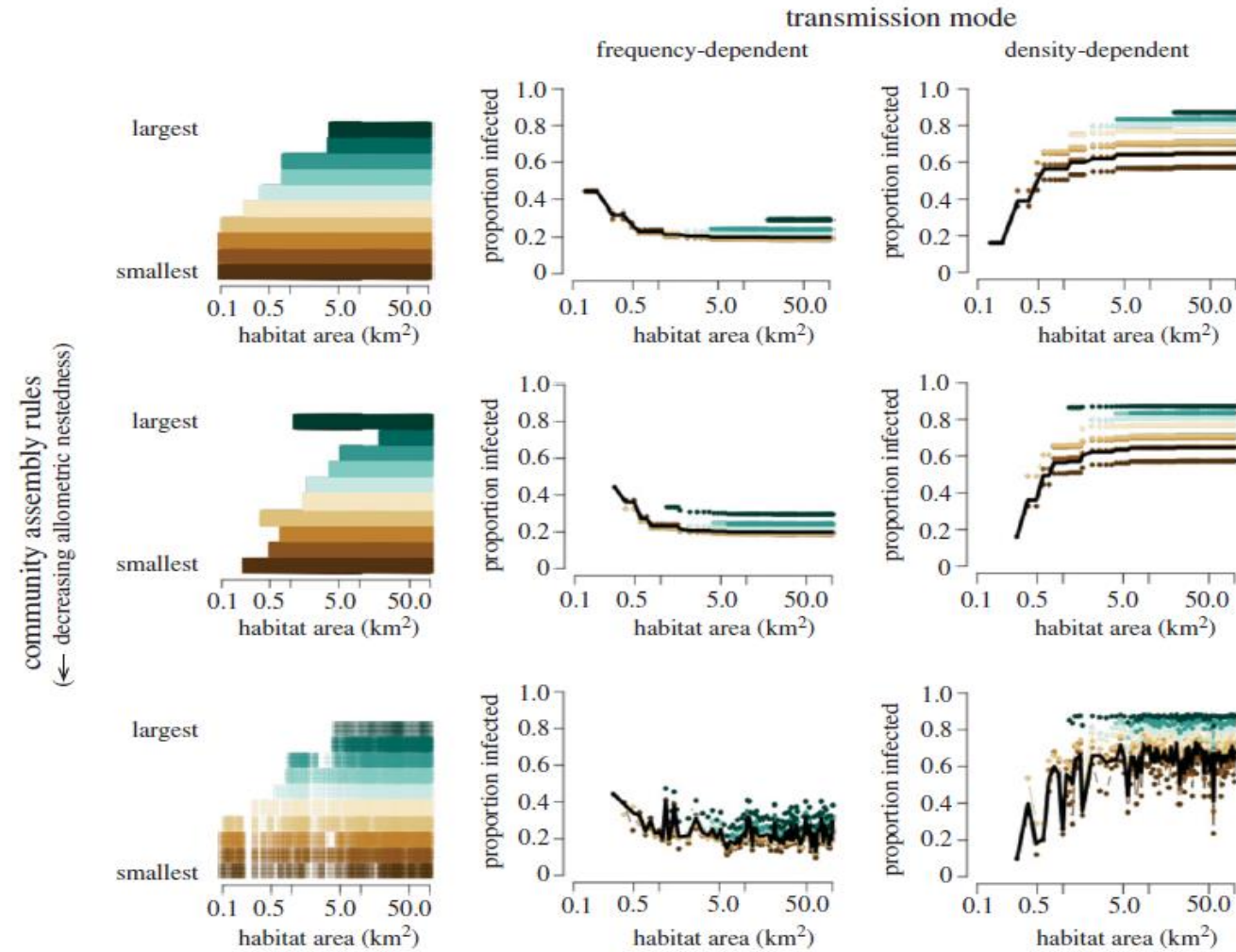
Faust, Dobson, Bloomfield, Gottdecker, McCallum, Gillespie, Plowright (2017)

Species accumulation curve for disease free equilibrium. The number of species in each habitat patch for a community with a ten host species pool with an average body size of 0.011, 0.030, 0.065, 0.075, 0.23, 0.537, 1.505, 1.515, 13.333, and 14.201 kg.



Faust, Dobson, Bloomfield, Gottdecker, McCallum, Gillespie, Plowright (2017)

Risk of exposure to different pathogens will vary between larger and smaller patches



Relatively robust result even when hosts of different competency are added in

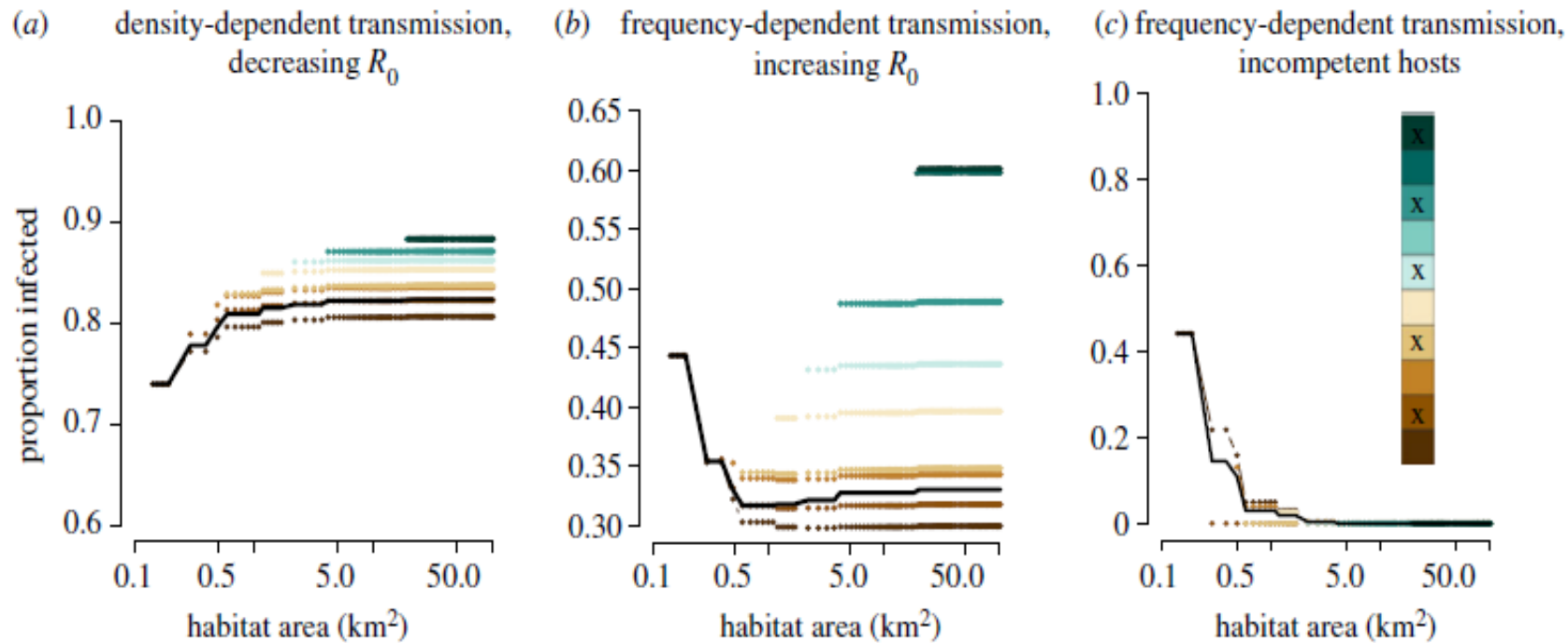


Figure 2. Variation in host competence and underlying assumptions impact diversity–disease relationships. (a) Even if the smallest hosts are the most competent [61] and there are extreme differences in R_0 between body sizes (electronic supplementary material, figure S5), only the amplification effect is observed for density-dependent pathogens. (b) If behavioural allometry leads to an increase in R_0 across body size, this can lead to an amplification effect for frequency-dependent pathogens at larger patch sizes, but a dilution effect for small to intermediate patches. (c) When species that can become infected but are in turn not infectious (incompetent hosts, denoted by x) are randomly assembled along the distribution of body sizes, then dilution effects can be exacerbated for frequency-dependent pathogens, but this depends on the order of community introduction of these incompetent hosts.

Subtle effects of host territoriality - within-species between territories, etc

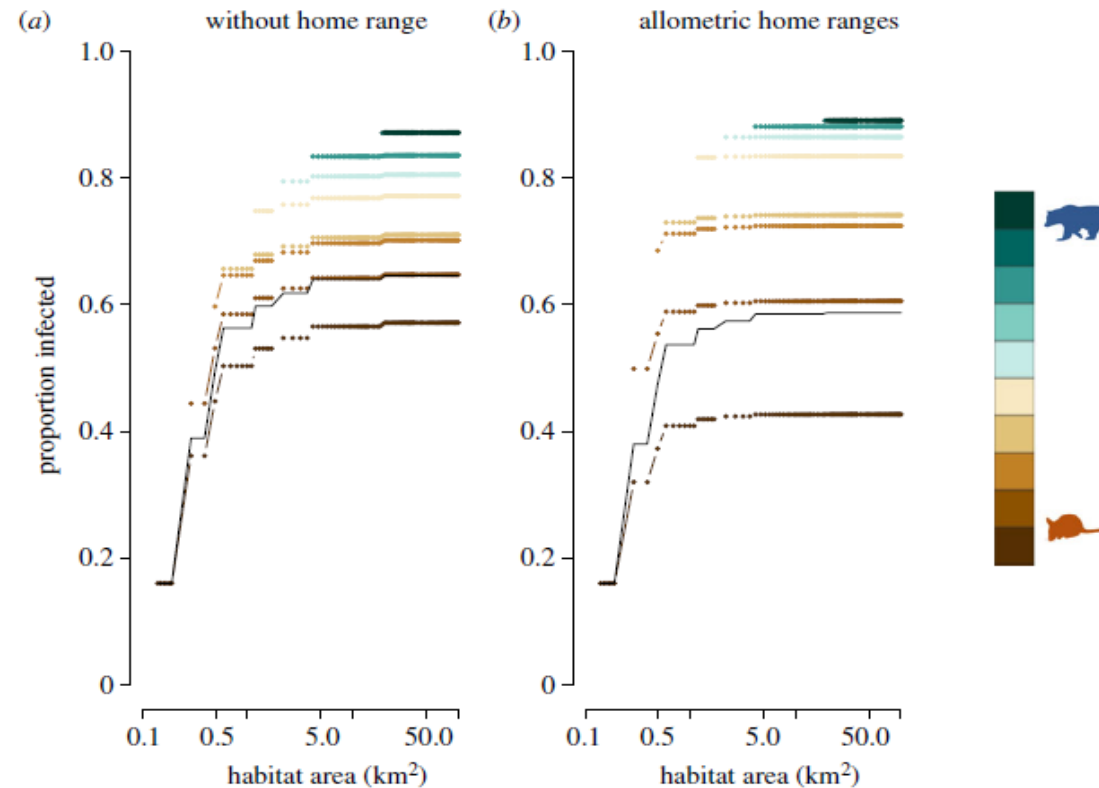


Figure 3. Impact of heterogeneous contacts on density-dependent pathogen transmission. Using identical disease parameters, endemic prevalence was observed for a host system that assumed contacts were determined by density of hosts (a) and compared with a system in which home range determined the average contacts of an individual from a given species (b). When home range is not taken into account, overall prevalence is higher, but when home range is considered, larger-bodied species that have larger home ranges have higher within-species infection prevalence.

Faust, Dobson, Bloomfield, Gottdecker, McCallum, Gillespie, Plowright (2017)

The dynamics of multi-host, multi parasite systems are more subtle than those of single pathogen, single hosts.

- Basic models can be scaled up – key parameter is relative rate of transmission between versus within species.
- Allometric scaling of demographic and epidemiological parameters allows generalization to n-species of hosts
 - This can also be done for macroparasites – DeLei, Dobson and Gatto, 2016.
- Frequency-dependent transmission can give rise to a dilution effect, density dependent usually gives an amplification of epidemic size.