

Climate variability and the population dynamics of diarrheal diseases

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and

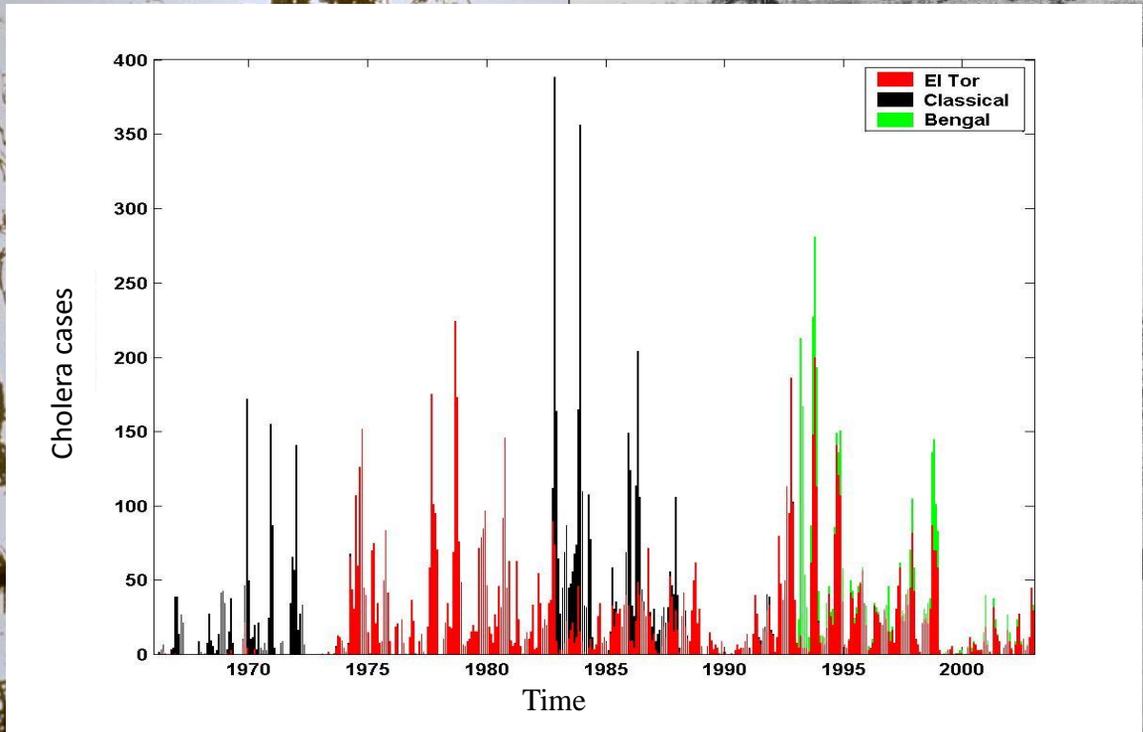
The Santa Fe Institute



London, 1854



Bangladesh, 2000



courtesy ICDDR, B

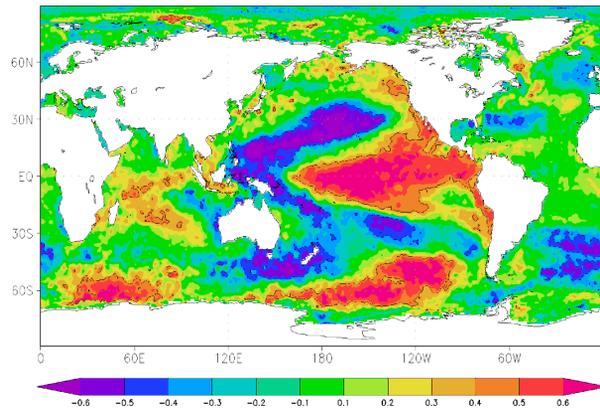






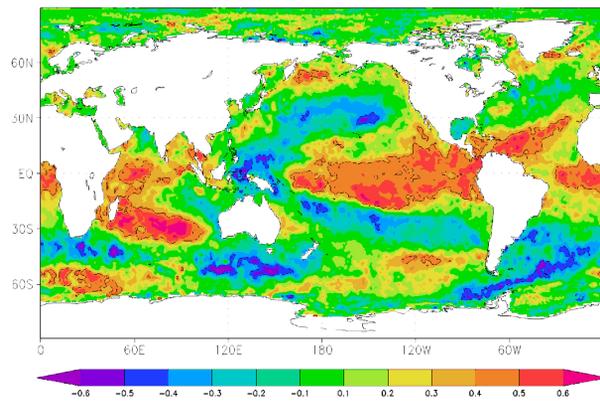
Matlab

Matlab ASOND El Tor Cholera and DJF SST
Rank Correlation 1983–2009



Dhaka

Dhaka ASOND El Tor Cholera and DJF SST
Rank Correlation 1984–2007



SST data: HadSST1:
Rayner et al. 2003

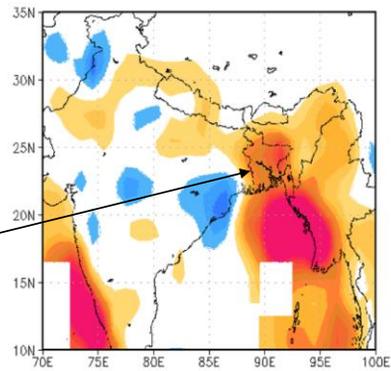
El Tor Cholera

Link between cholera and ENSO

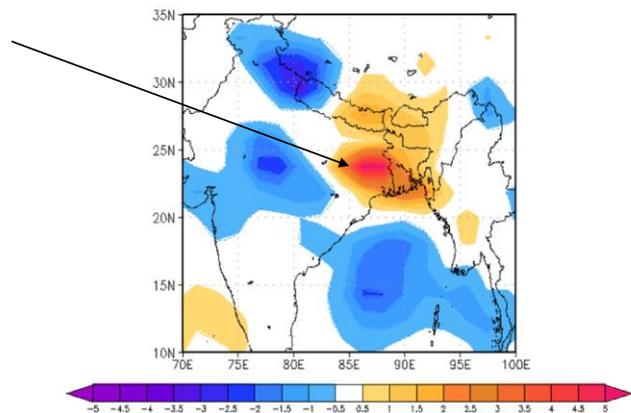
- Observed precipitation enhanced following El Niño
- Model captures much of the observed empirical signal

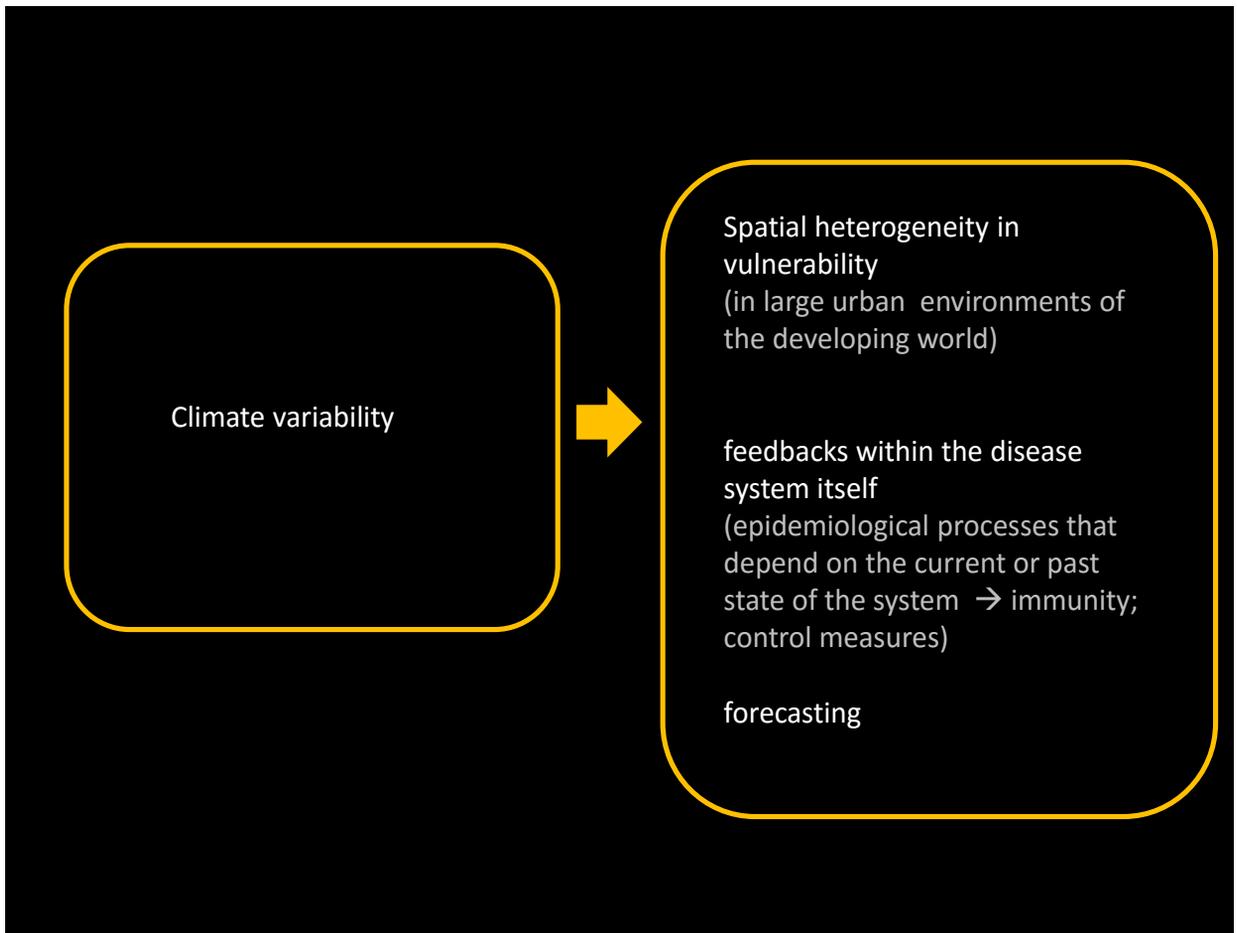
Cash, Rodo and Kinter ,
J. Climate 2008

(a) July–August Observed Precipitation Anomaly



(b) July–August Composite Precipitation Anomaly





Limitation of temporal 'correlative' approaches:

- 1 – Spatial (and other forms) of population heterogeneity
- 2 – Nonlinear responses to environmental forcing
- 3 – Everything is seasonal... explanations for seasonality are hard



Highly localized sensitivity to climate forcing drives endemic cholera in a megacity

Robert C. Reiner, Jr.^{a,1}, Aaron A. King^{a,b}, Michael Emch^c, Mohammad Yunus^d, A. S. G. Faruque^d, and Mercedes Pascual^a

^aUniversity of Michigan, Ann Arbor, MI; ^bFogarty International Center, National Institutes of Health, Bethesda, MD 20892; ^cUniversity of North Carolina Chapel Hill, NC; and ^dInternational Centre for Diarrheal Disease Research, Dhaka 1000, Bangladesh

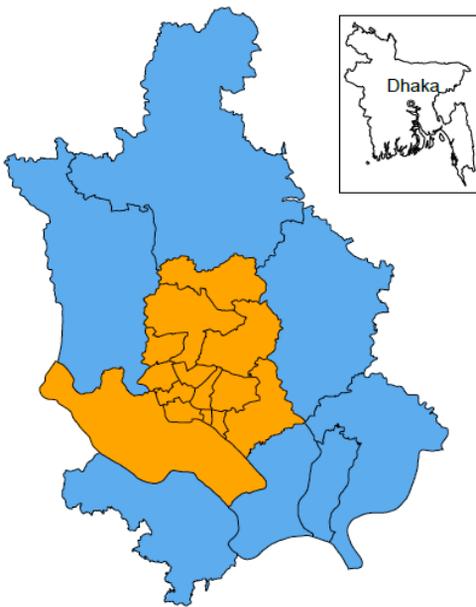


Motivation



- Spatial effects have not been considered before in the response of cholera to climate variability. We may expect global climate drivers such as ENSO to operate at regional scales.
- We still have a poor understanding of proximal mechanisms that mediate the effect of global climate drivers in urban environments
- Statistical models in the literature cannot be used effectively for prediction because of their short lead times (ranging from 0 to 1 months)

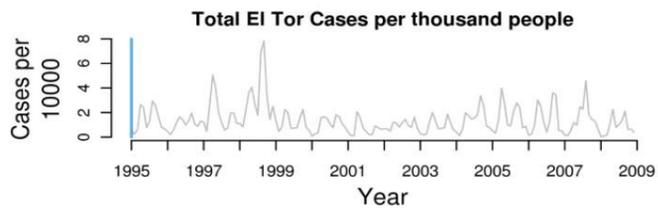
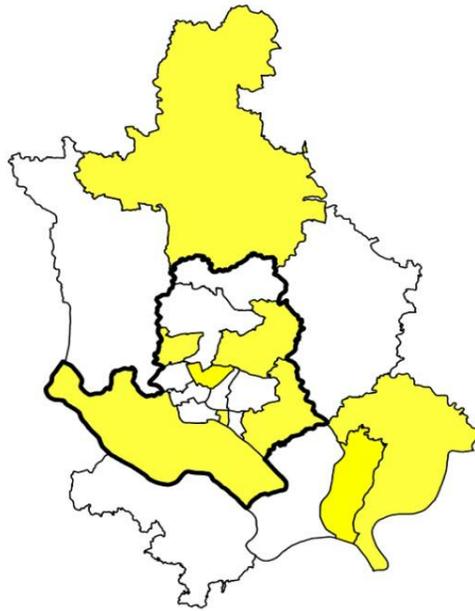
Data Description

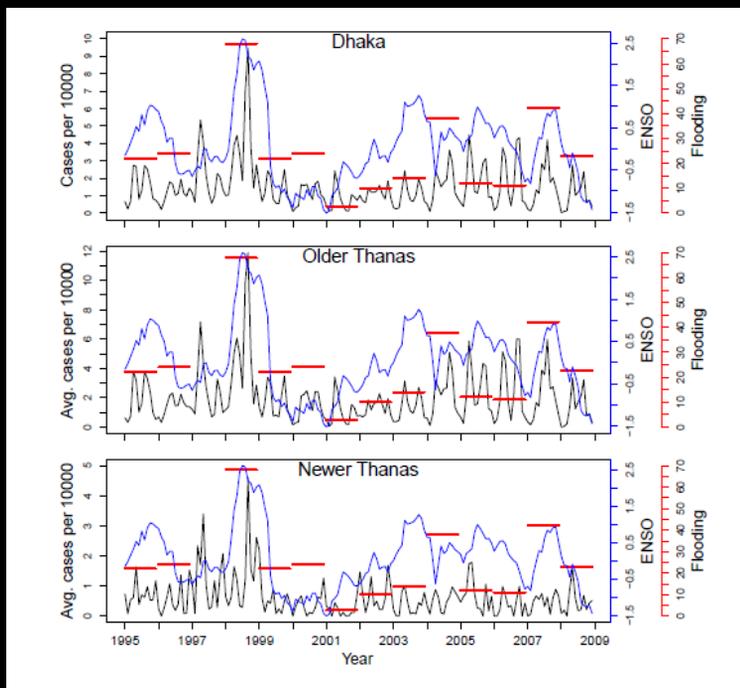


- Dhaka, the capital of Bangladesh, contains more than 14 million people (almost tripled in last 25 years, projected to double in next 25).

- The data we analyze is the number of cases of cholera of the O1 El Tor biotype over 14 years (1995-2008), broken down by thana (i.e. administrative region).

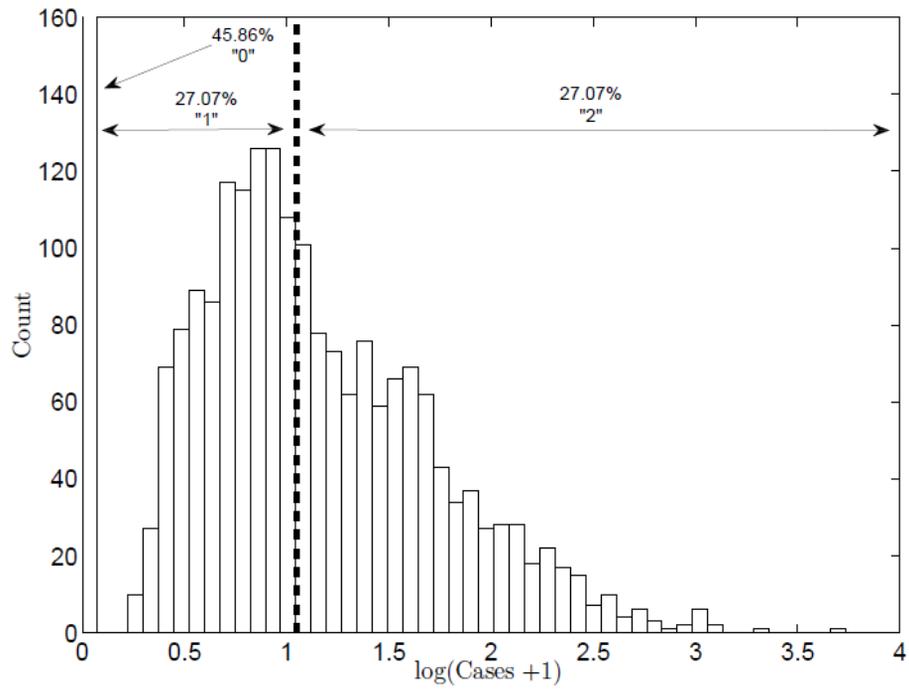
[Movie](#)



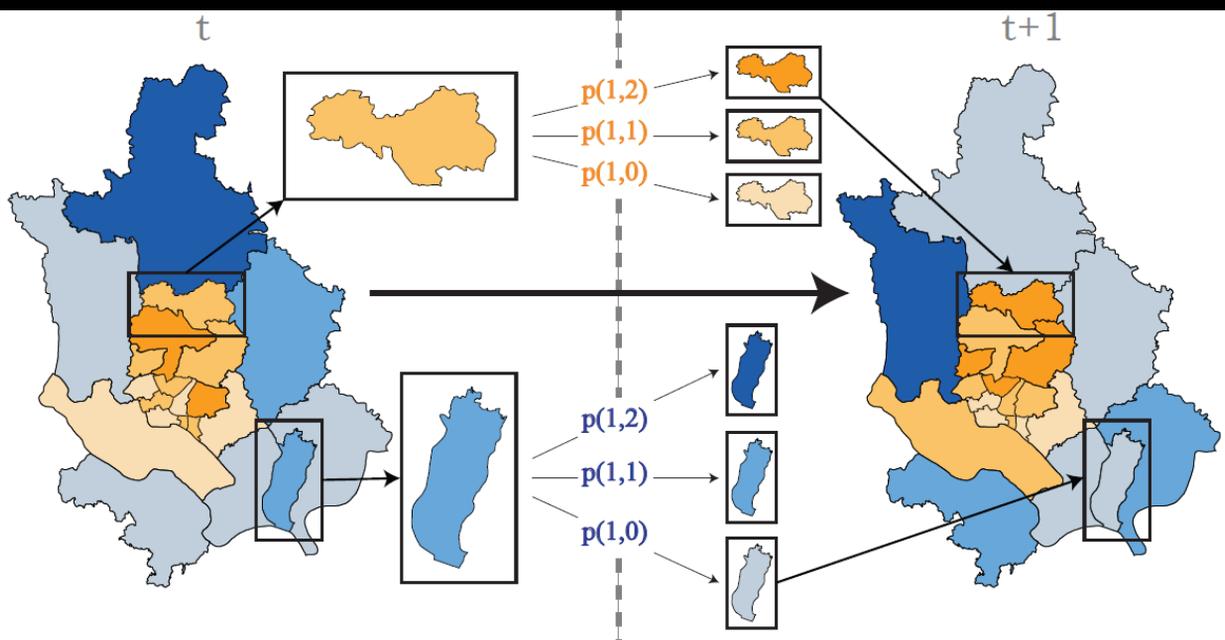


Reiner et al., PNAS 2012

Data Transformation



Probabilistic model (discrete state Markov chain model): probabilities a function of group , season, neighbors' states, and climate covariates.



Model Description

	0	1	2
0	$p(0, 0)$	$p(0, 1)$	$p(0, 2)$
1	$p(1, 0)$	$p(1, 1)$	$p(1, 2)$
2	$p(2, 0)$	$p(2, 1)$	$p(2, 2)$

Markov Chain Model

- We start with a simple Markov Chain model to describe the data.
- This model assumes the only difference between any two observations is what the value of the thanas were the month before.

Model Description

Older

	0	1	2
0	$p(0,0)$	$p(0,1)$	$p(0,2)$
1	$p(1,0)$	$p(1,1)$	$p(1,2)$
2	$p(2,0)$	$p(2,1)$	$p(2,2)$

Newer

	0	1	2
0	$p(0,0)$	$p(0,1)$	$p(0,2)$
1	$p(1,0)$	$p(1,1)$	$p(1,2)$
2	$p(2,0)$	$p(2,1)$	$p(2,2)$

Multiple Markov Chain Model

- We add complexity by allowing the transition matrices to be different depending on the area of the city where the thana is located.

Model Description

		Older		
		0	1	2
N ₁ =0	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

		Newer		
		0	1	2
	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

Multi-Dimensional Markov Chain Model

- To account for local spatial effects, we expand the model to allow for a different transition matrix depending on the maximum state of the nearest neighbors of that thana.

		Older		
		0	1	2
N ₁ =1	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

		Newer		
		0	1	2
	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

		Older		
		0	1	2
N ₁ =2	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

		Newer		
		0	1	2
	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

- All thanas must now be simultaneously tracked, hence we now have a multi-dimensional model (21 dimensions, one for each thana).
-

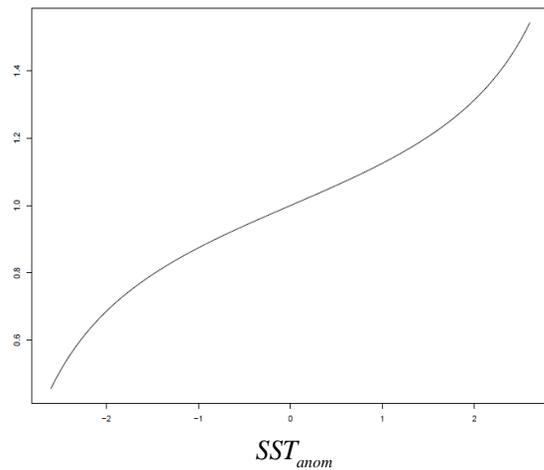
Model Description

Spring				Summer															
		Older			Newer					Older			Newer						
N=2		0	1	2		0	1	2	N=0		0	1	2		0	1	2		
	0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$		0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$		0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$		0	$p_{0,0}$	$p_{0,1}$	$p_{0,2}$
	1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$		1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$		1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$		1	$p_{1,0}$	$p_{1,1}$	$p_{1,2}$
	2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$		2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$		2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$		2	$p_{2,0}$	$p_{2,1}$	$p_{2,2}$

Multi-Dimensional Inhomogeneous Markov Chain (MDIMC) Model

- Allowing the transitions to vary by season, our model is no longer temporally homogeneous, but allows for the known two-peak-per-year dynamics to emerge. Unfortunately there are way too many variables in this model. Only Spring and Summer are shown here in a four season model. One could imagine a different set of matrices for each month.
-

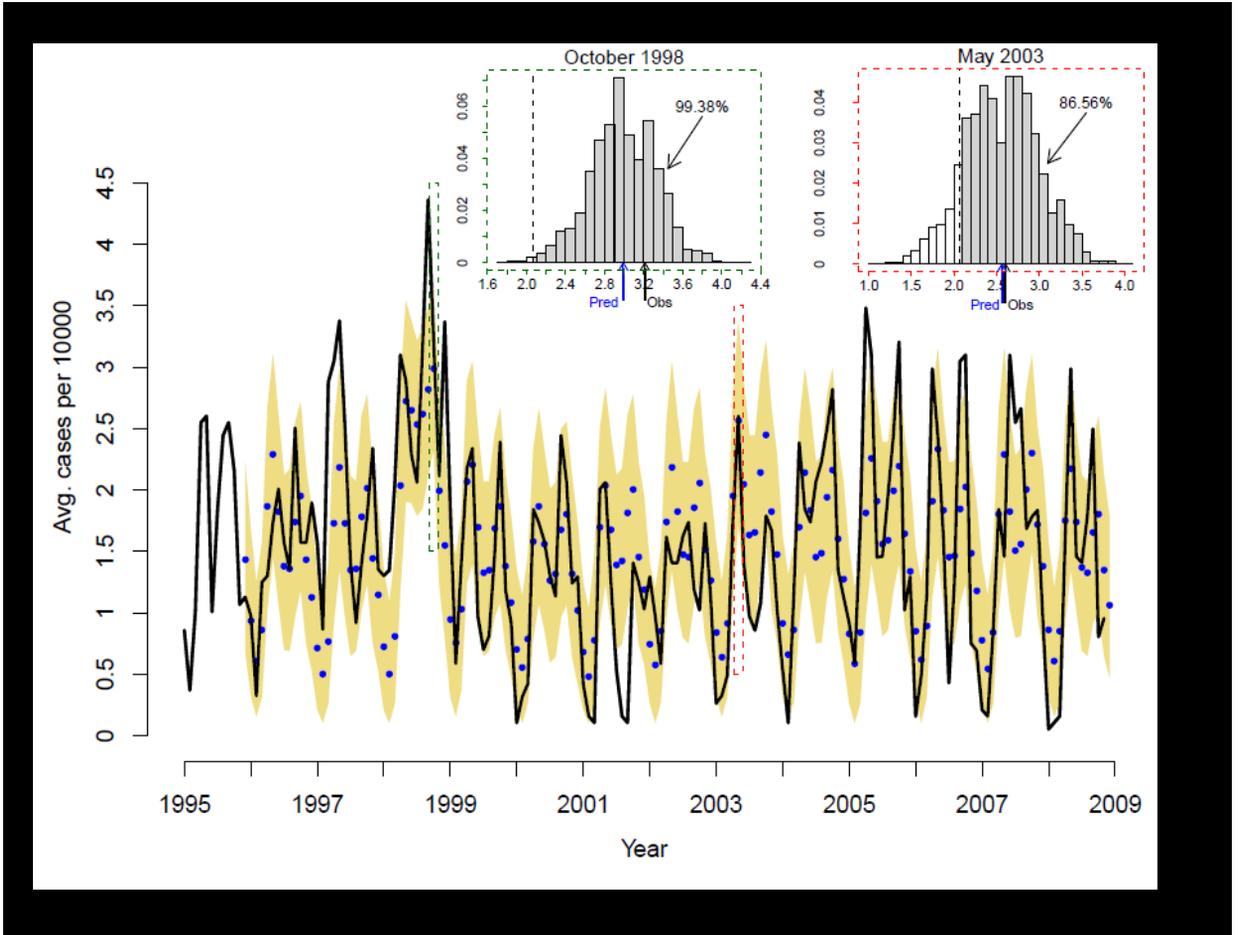
$$P_{ENSO}(i, j) = P(i, j) * [1 + f(SST_{anom})]$$

 $f(SST_{anom})$


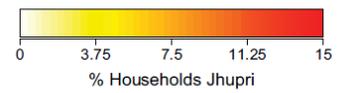
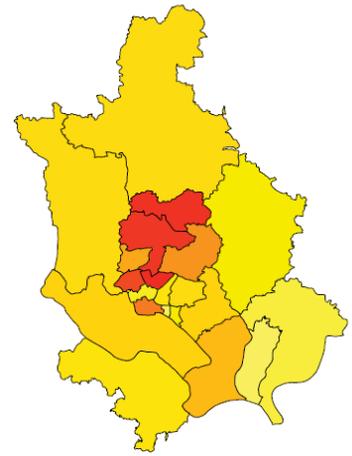
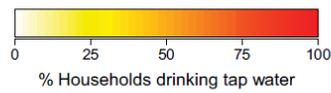
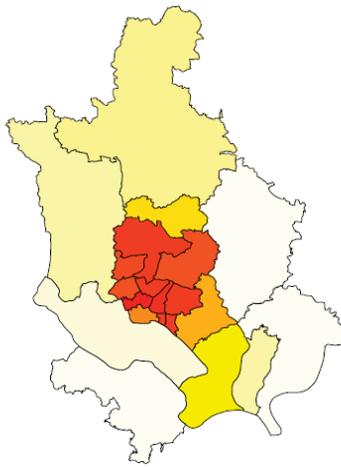
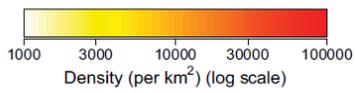
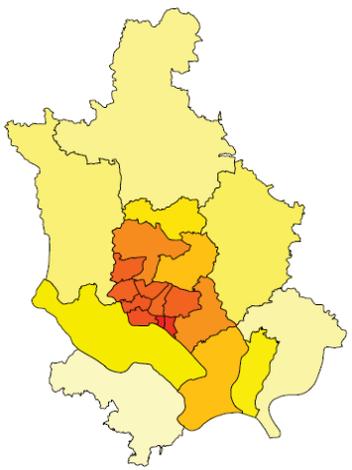
$$\begin{aligned} P\left(X_{k,t} = j | X_{k,t-1} = i, \max_{l \in \mathcal{N}(k)} X_{l,t-1} = v, ENSO = s\right) = \\ = \mathbb{P}_{i,j,\mathcal{D}(k)} \times \text{Neigh}(i, j, v, \mathcal{D}(k)) \times \text{Seas}(i, j, t, \mathcal{D}(k)) \times \text{Nino}(j, s, \mathcal{D}(k)) \end{aligned}$$

- Spatial heterogeneity: the dynamics between groups are significantly different (p-value=0.0001)
- Local effect: the state of neighboring districts matters (p-value =0.01) but a weaker effect
- Interaction between spatial structure and climate forcing: the parameters governing the effect of ENSO are significantly different between the groups (p-value= 0.03); and similarly for flooding (p-value= 0.015)
 - > ENSO is a significant covariate (p=value < 0.0001); lag of 11 months for the spring months and 9 months for the fall ones.
 - > Flooding is also significant (p-value < 0.0001)
 - > Flooding still significant when tested in the presence of ENSO (p-value = 0.008) and vice-versa (p-value < 0.0001)

Reiner *et al.* (PNAS 2012)



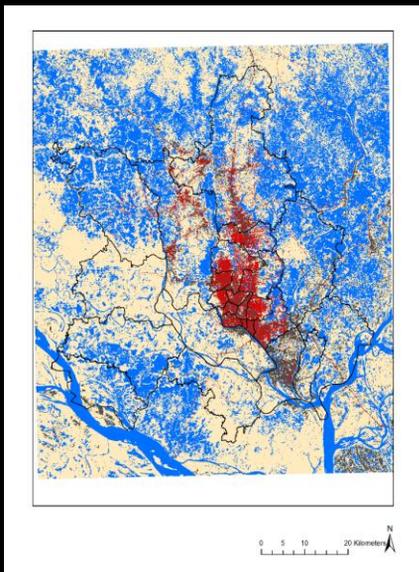
Socio-economic conditions



Summary so far:

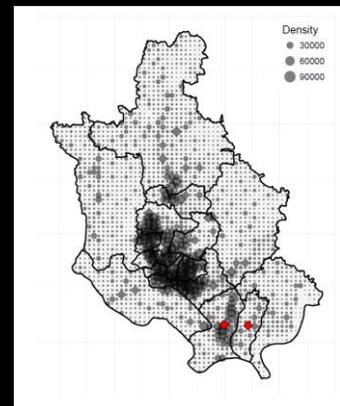
- Cholera outbreaks in Dhaka (and Bangladesh) are driven by climate variability (ENSO and flooding). The effect of El Niño is partly through precipitation and associated flooding.
- Population susceptibility shows pronounced geographic variation within Dhaka, with a part of the city acting as a susceptible core, in a way that highlights the key role of sanitary and associated socio-economic conditions.

A remote-sensing view of the city

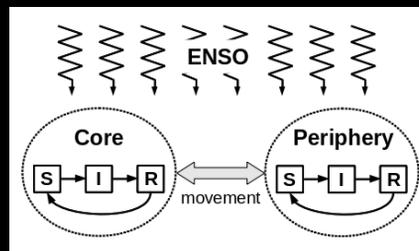


- water
- urban
- rural

Population density

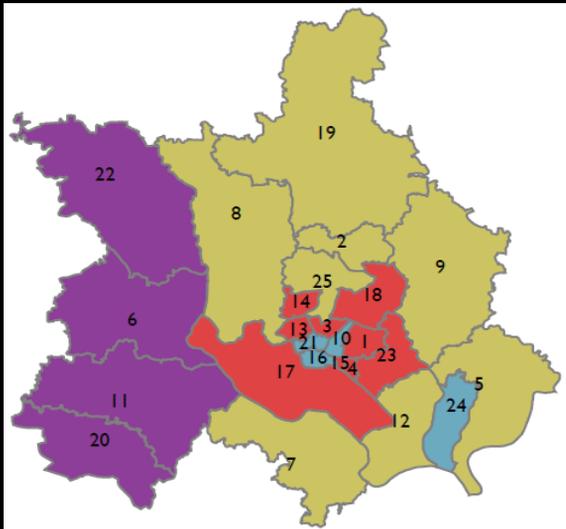


Zooming out



Perez et al. *Advances in Water Resources* 2017

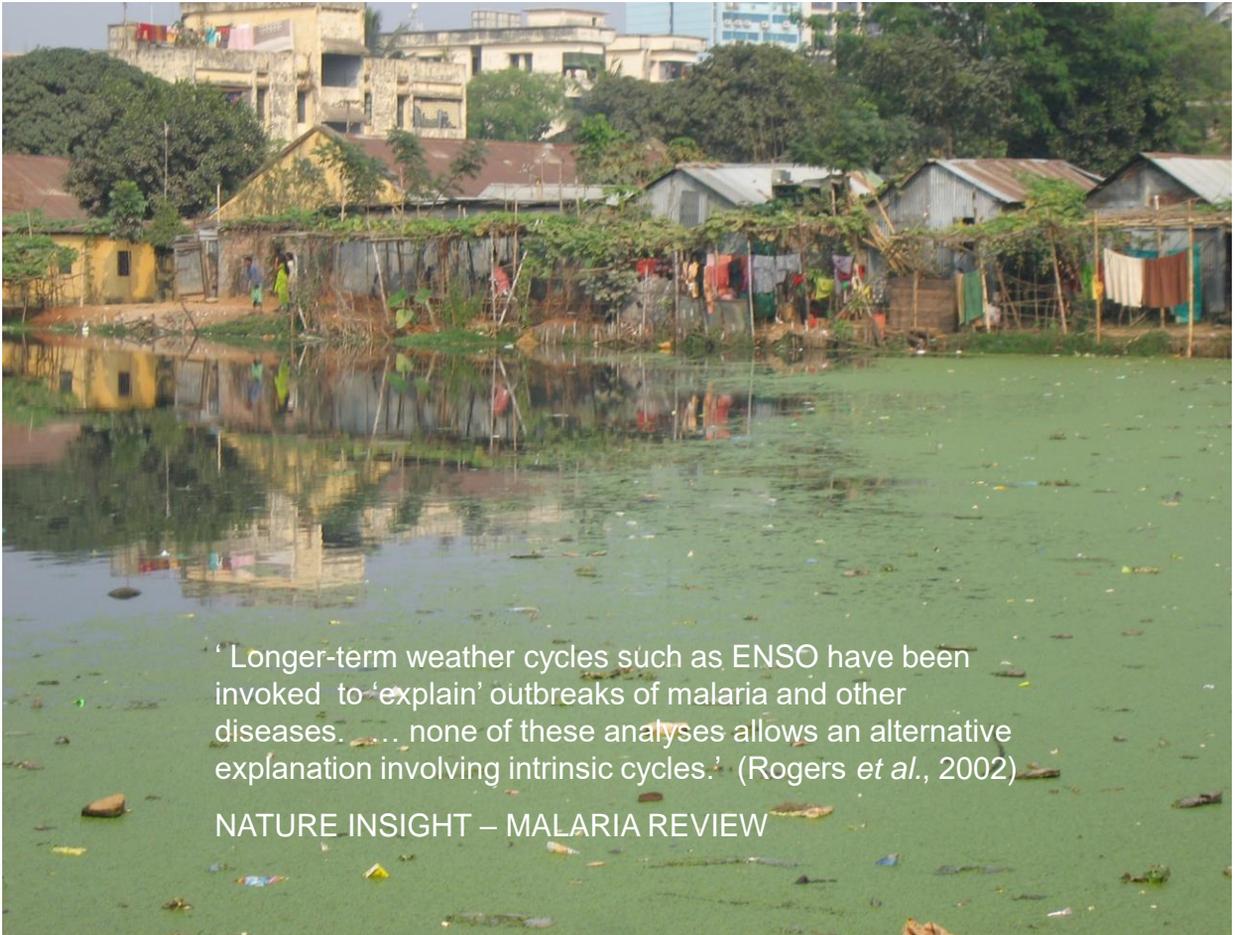
Search algorithms to identify 'groups' of locations with similar dynamics ...



There are $S_{25}^{(2)} = 16,777,215$ distinct groupings.

Bayesian approach to classify districts based on a dynamical model and time series data:

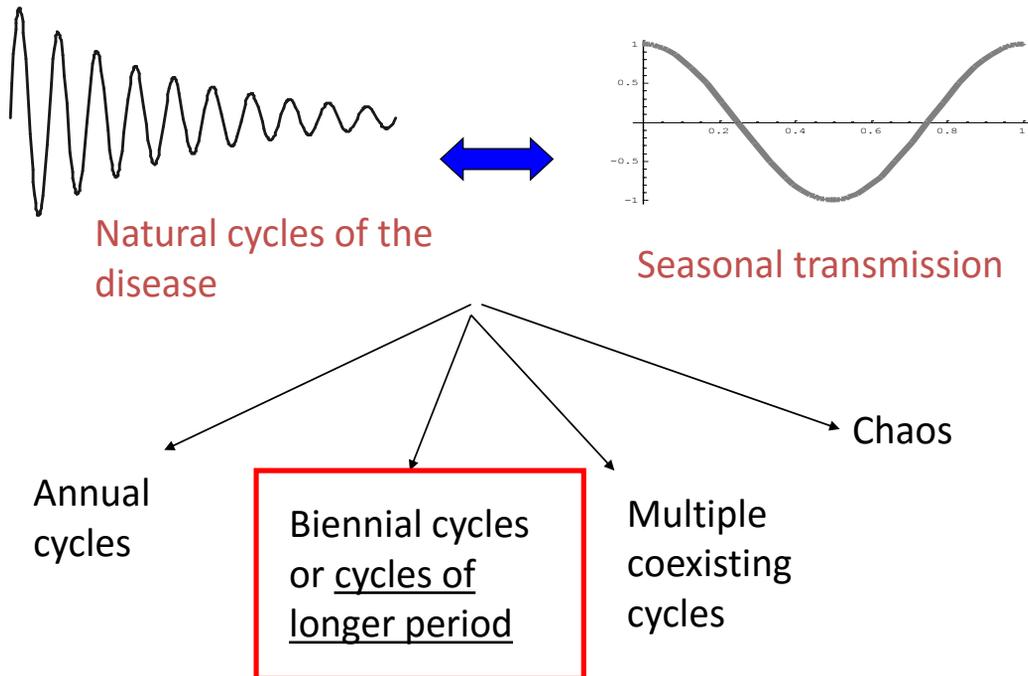
Baskerville EB, Bedford T, Reiner RC, Pascual M (2013) Nonparametric Bayesian grouping methods for spatial time-series data. arXiv:1306.5202.

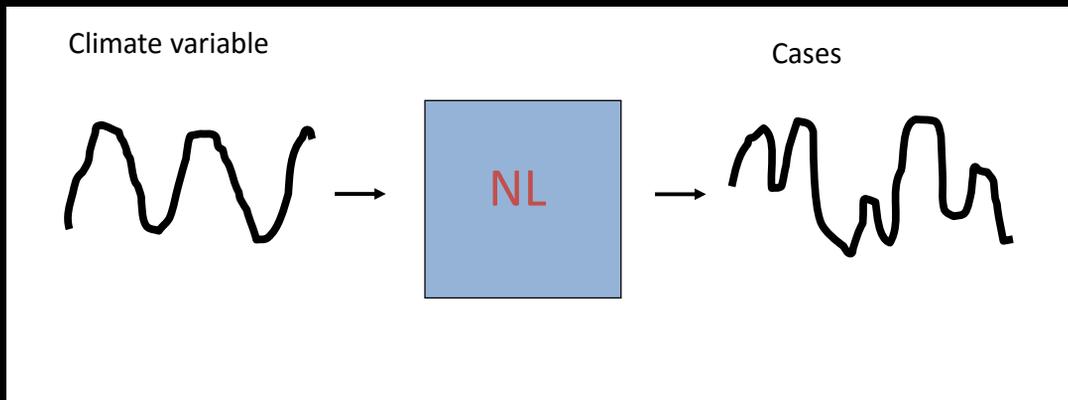


' Longer-term weather cycles such as ENSO have been invoked to 'explain' outbreaks of malaria and other diseases. ... none of these analyses allows an alternative explanation involving intrinsic cycles.' (Rogers *et al.*, 2002)

NATURE INSIGHT – MALARIA REVIEW

when two cycles interact...





Model + statistical inference methods



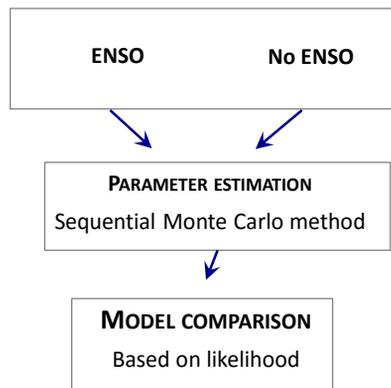
Intrinsic dynamics

Extrinsic drivers

Parameter inference and model comparison



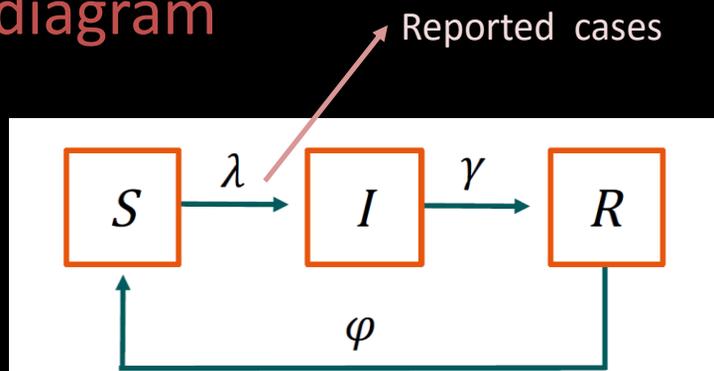
www.keywordpictures.com



Parameters were estimated with a method that **maximizes the likelihood** and allows for the inclusion of both **measurement and process noise**, as well as **hidden variables**

Ionides et al. PNAS 2006, King et al. Statistical inference for partially observed Markov processes (R package) <http://pomp.r-forge.r-project.org>

Model diagram

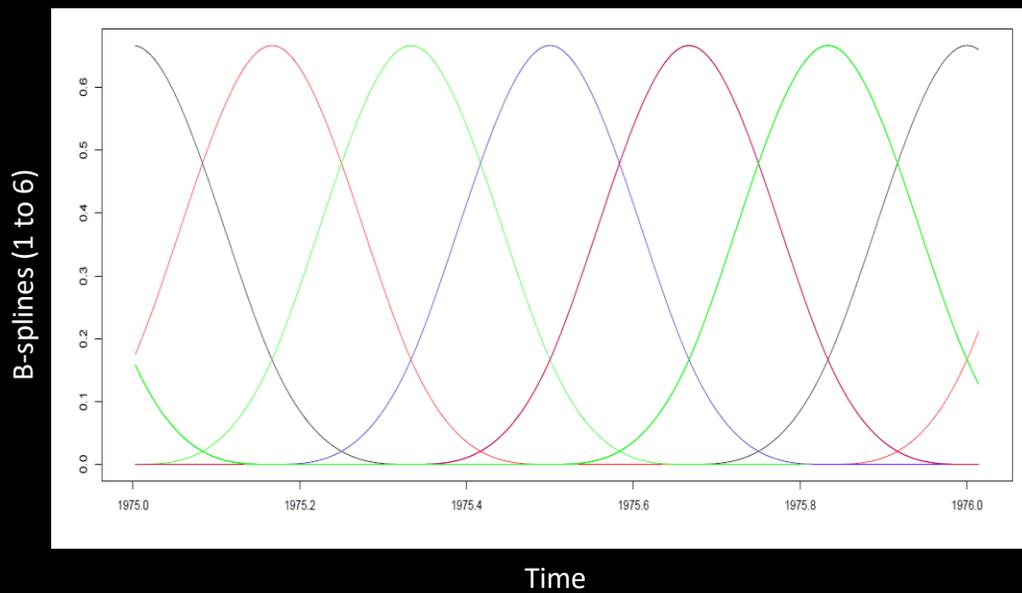


$$\lambda = \text{trend} \left(\begin{array}{c} \text{secondary} \\ \text{transmission} \end{array} + \begin{array}{c} \text{primary} \\ \text{transmission} \end{array} \right)$$

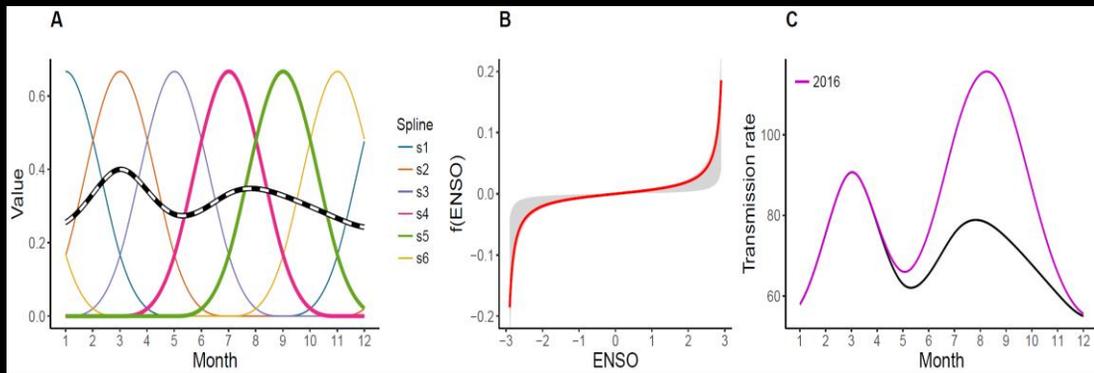
$$\text{secondary transmission} = \beta \frac{I}{N}$$

$$\beta = \text{seasonality} \cdot f(ENSO) \cdot \text{noise}$$

β : seasonality and ENSO



$$\beta = \exp\left[\sum_1^6 a_i \text{season}_i + b \cdot \text{season5} \cdot \text{ENSO}(\text{January})\right]$$



Force of infection

$$\lambda_E(t) = \overbrace{e^{-\eta(t-t_0)}}^{\text{long-term trend}} \left[\beta(t) \left[\frac{I(t)}{N(t)} \right] + \omega \right] \text{ noise}$$

'secondary'
transmission

'primary'
transmission

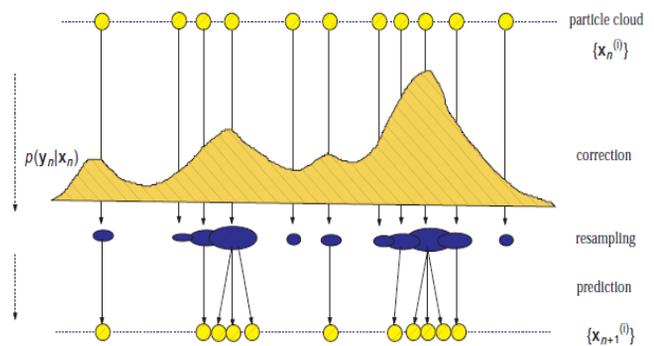
Inference method:

King AA, N D, Ionides EL. Statistical Inference for Partially Observed Markov Processes via the R Package pomp. J Stat Softw. 2016; 69(1): 1–43.

Likelihood maximization
by iterated filtering (based
on sequential Monte Carlo
methods --- particle filters)
can accommodate:

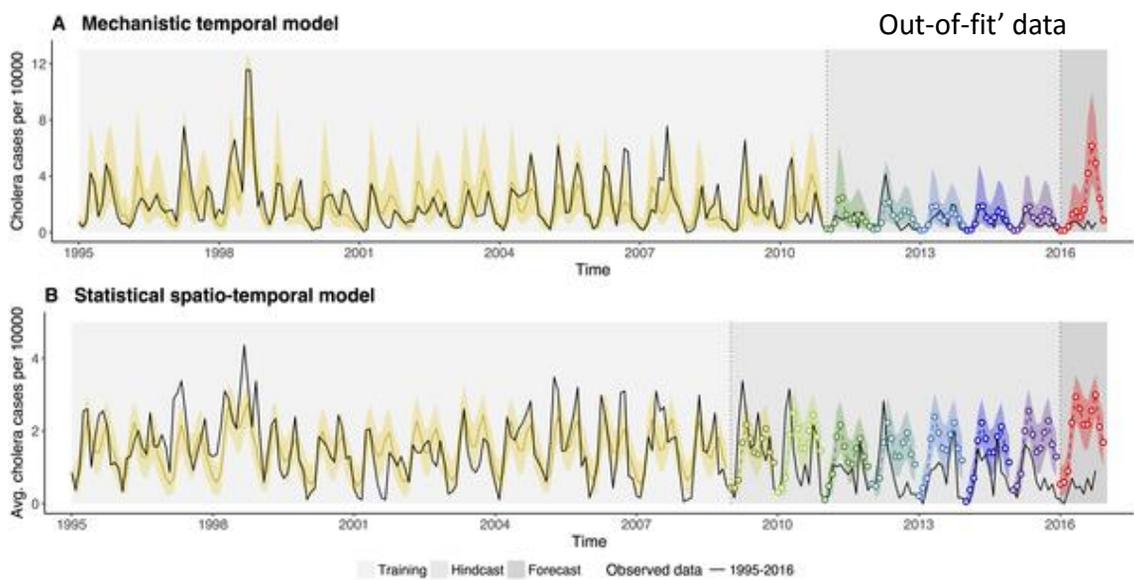
- flexible model formulations ; continuous time
- unobserved variables (e.g. susceptibles)
- stochasticity , trends
- measurement error (under-reporting)

See Laneri et al (PloS Comp. Biol. 2010)
for inclusion of covariates
and
pseudo-code
in a malaria example



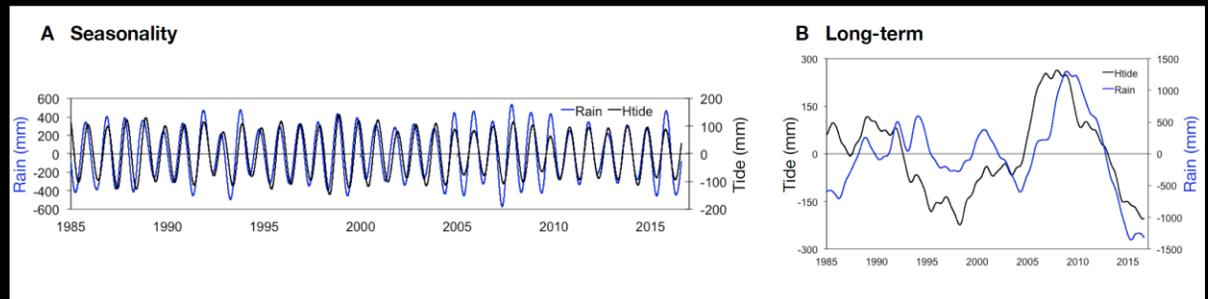
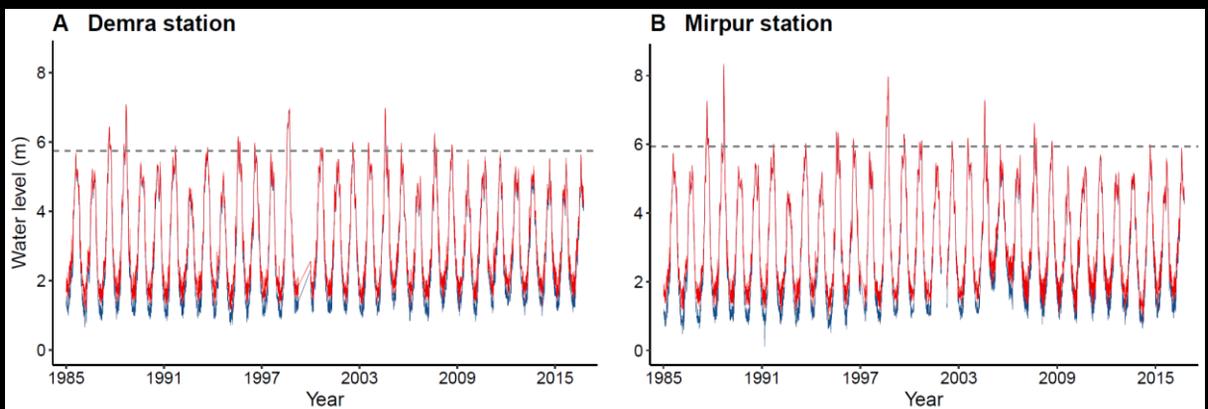
From Z. Chen 2009

Fig 2. Comparison of simulated and predicted monthly cases with those reported for Dhaka, Bangladesh.



Martinez PP, Reiner RC Jr, Cash BA, Rodó X, Shahjahan Mondal M, et al. (2017) Cholera forecast for Dhaka, Bangladesh, with the 2015-2016 El Niño: Lessons learned. PLOS ONE 12(3): e0172355. <https://doi.org/10.1371/journal.pone.0172355>
<http://journals.plos.org/plosone/article?id=10.1371/journal.pone.0172355>

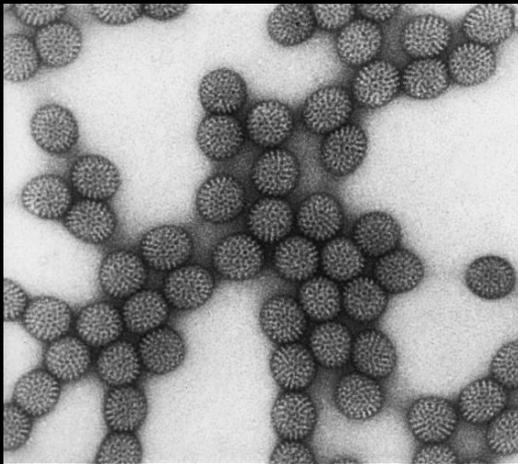
Water level and rainfall in Dhaka



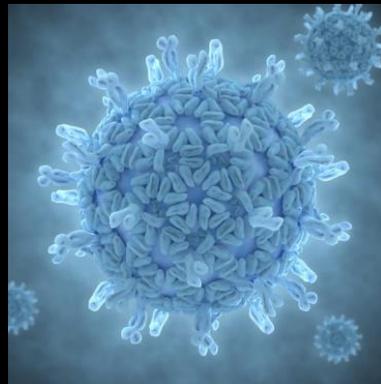
Some conclusions

- Model with ENSO better explains the retrospective data including the large epidemic of 1998
- It also predicts the low incidence of 'out-of-fit' data during non-EL Nino years
- It overpredicts the response to the 2015-16 event.
- This appears to reflect a decrease susceptibility to flooding in the city, and perhaps a decadal change in rainfall conditions

Rotavirus: segmented RNA virus

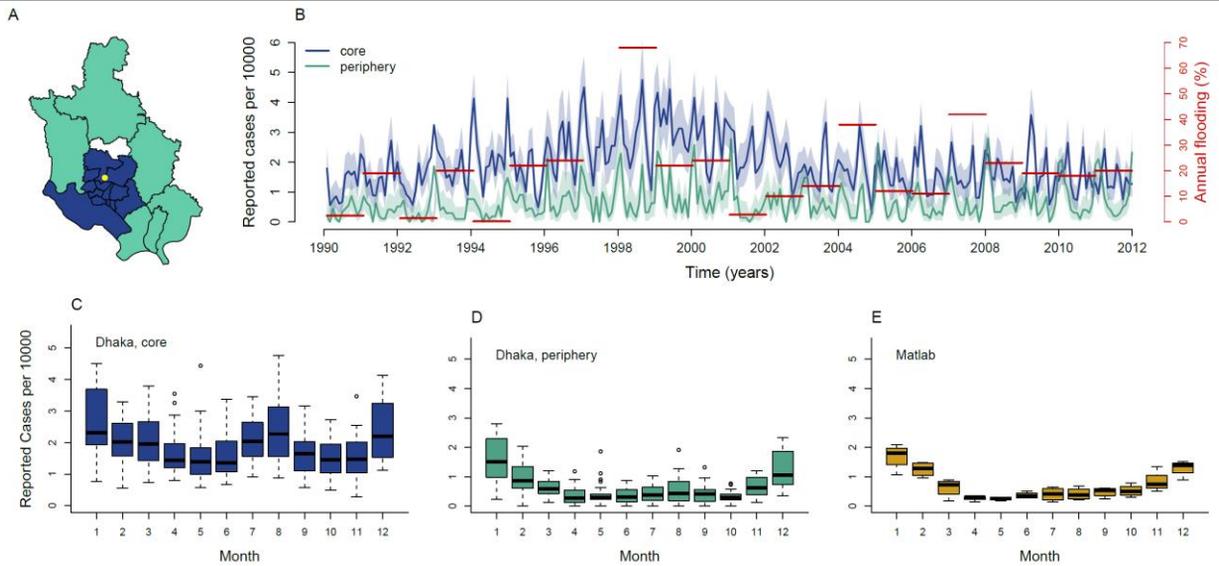


Transmission electron micrograph of rotavirus particles
<http://pathmicro.med.sc.edu/virol/rotaviruses.htm>

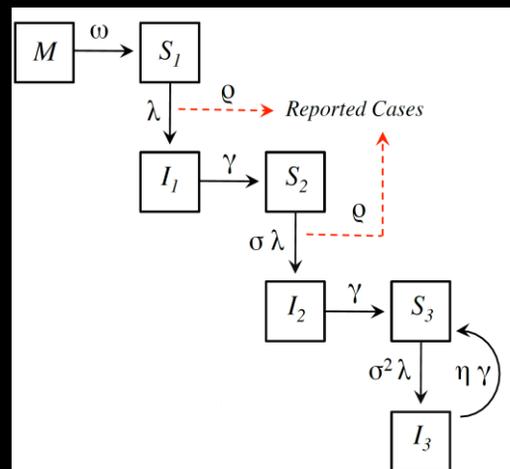
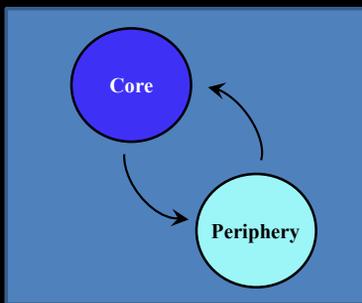


<http://www.babymed.com/infections/rotavirus>

Rotavirus: empirical patterns



Transmission model



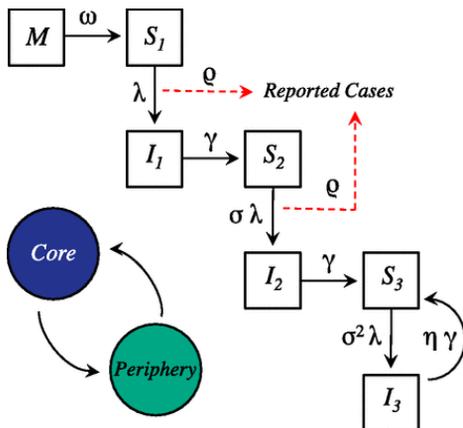
Martinez *et al.*, PNAS 2016

Transmission model

Force of Infection

α = coupling ($0 \leq \alpha \leq 1$)

$$\lambda_i = \beta_i \left[\alpha_i \frac{(I_{1i} + I_{2i} + I_{3i})}{P_i} + (1 - \alpha_j) \frac{(I_{1j} + I_{2j} + I_{3j})}{P_i} \right]$$



Transmission rate

$$\beta_i = \exp \left[\sum_{k=1}^6 b_{ki} s_k + b_{fi} s_4 F \right] \left[\frac{d\Gamma}{dt} \right]$$

seasonality (interannual variation) *flooding* *process noise*

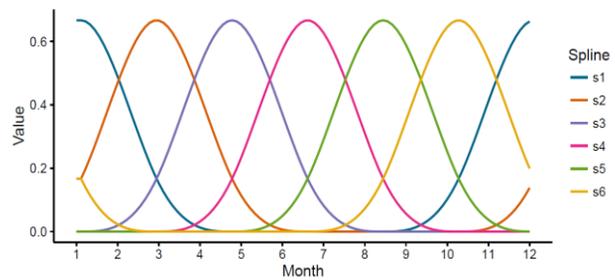
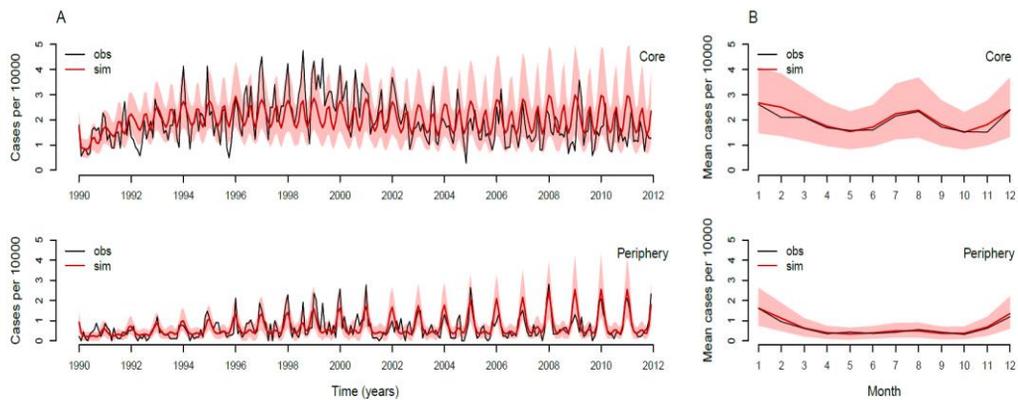
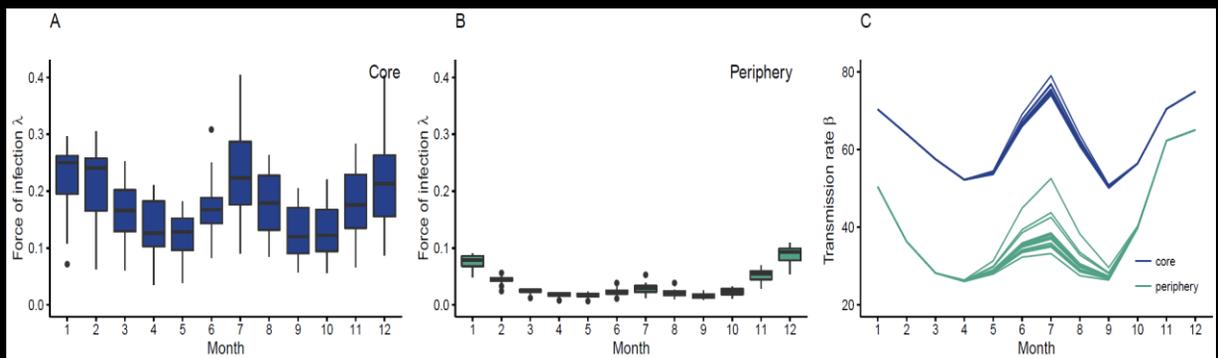


Table 1. A likelihood-based comparison of the different models

Model	log-likelihood	SE	no. param	AIC	LR Test
With flooding effect	-1577.6	0.33	25	3205.2	
Without flooding effect	-1582.2	0.35	23	3210.4	$p\text{-value} = 0.01$



Martinez *et al.*, PNAS 2016.



>> Higher force of infection in the core

>> Especially, during the monsoons

>> Transmission in the core continues outside the two main seasons (no deep troughs)

Some general implications

- Dense urban areas can enhance transmission and facilitate more endemic dynamics
- In these areas, enhanced responses to climate forcing may be seen even in infections that are not considered climate sensitive to begin with
- These responses are reflected primarily in changes to the seasonality
- More epidemic behavior, in areas where disease persistence throughout the year is more marginal, will exhibit responses to climate forcing at multiannual rather than seasonal scales



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journal homepage: www.elsevier.com



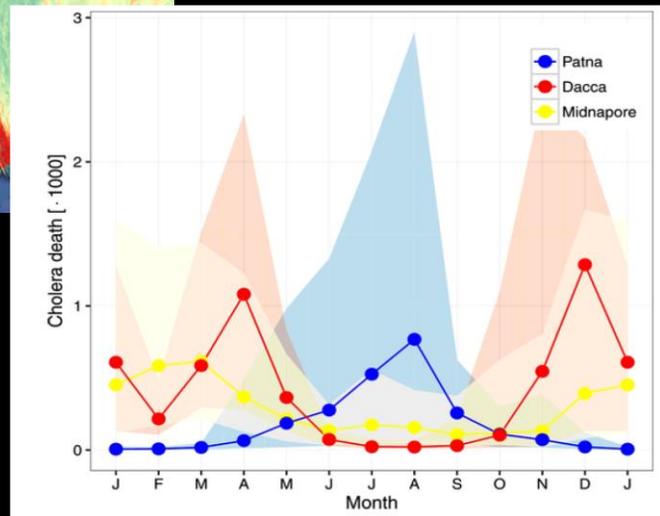
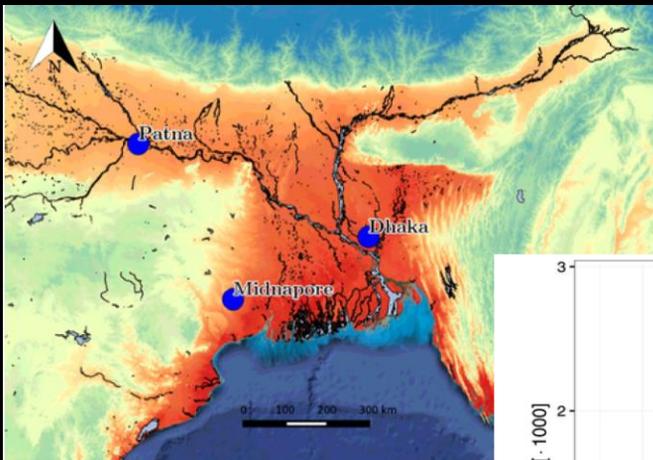
Seasonality in cholera dynamics: A rainfall-driven model explains the wide range of patterns in endemic areas

Theo Baracchini^a, Aaron A. King^b, Menno J. Bouma^{c, d}, Xavier Rodó^d, Enrico Bertuzzo^e, Mercedes Pascual^{*, f}

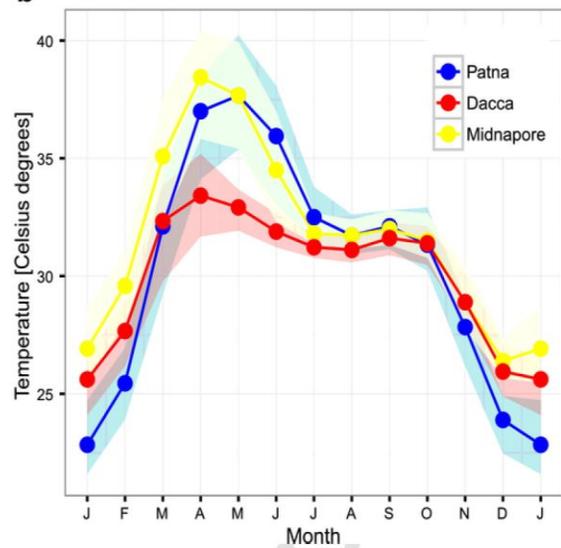
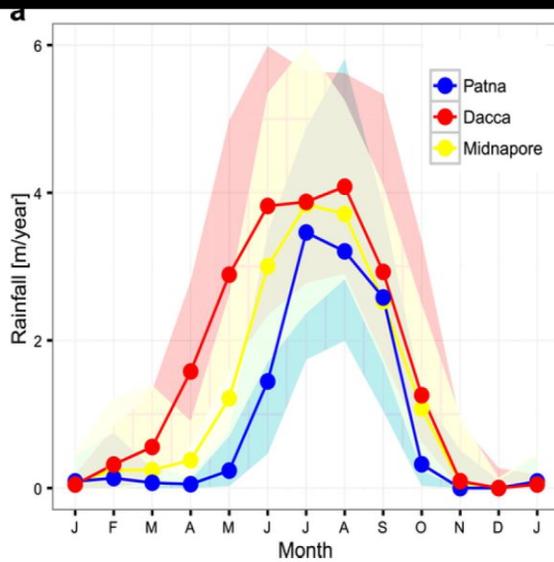
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Climate variables and seasonality



Seasonality of rainfall and temp

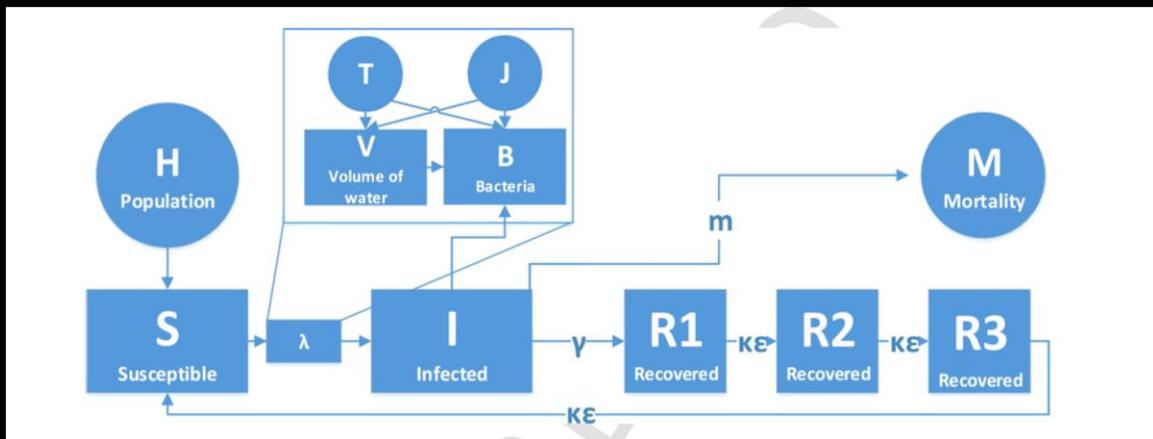


The model

$$\frac{dV}{dt} = J(t) - ET(T, V) - f(V) \cdot V$$

$$\lambda(t) = \beta \frac{\frac{B(t)}{V(t)A}}{\frac{B(t)}{V(t)A} + K},$$

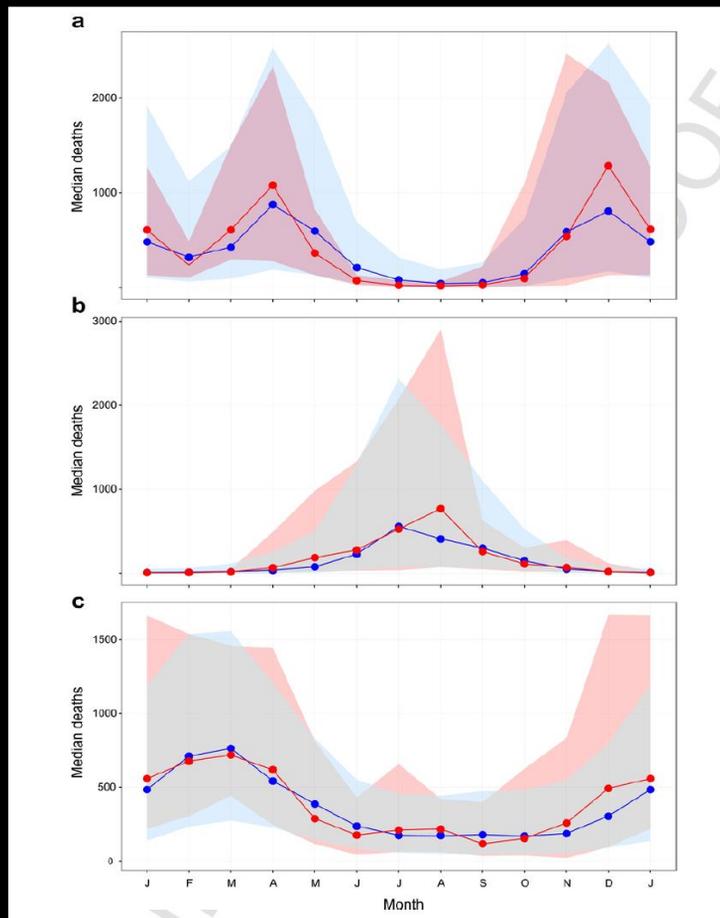
$$\frac{dB}{dt} = -\mu_B(T) B + p(t) [1 + \phi \cdot J(t)] I \cdot \xi(t) - f(V) B$$



Seasonality: Model and data

The historical Bengal region encompasses all the seasonal patterns observed worldwide

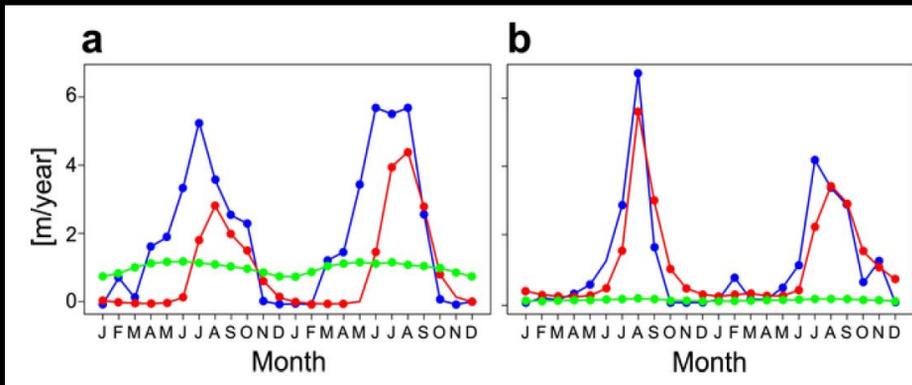
Monthly data:
1891-1941



Rainfall and 'hydrology'

Dhaka

Patna

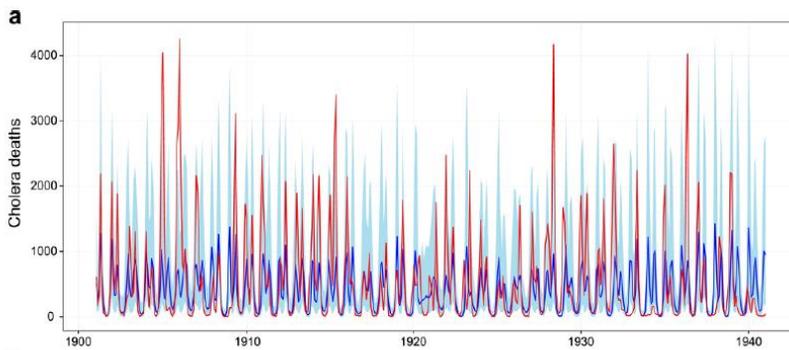


— drainage

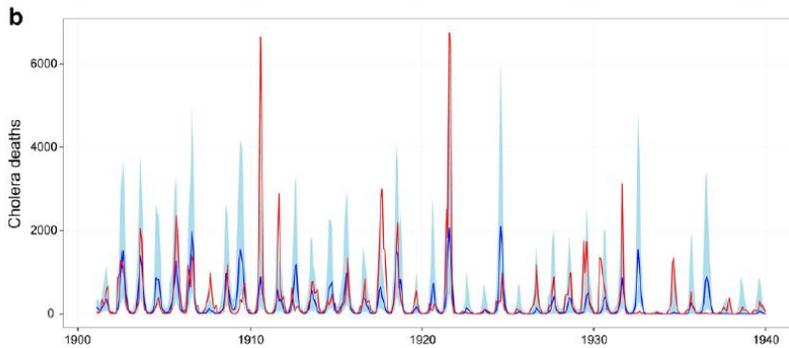
— rainfall

Interannual variability

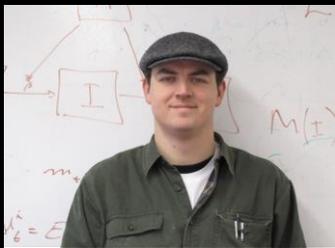
Dhaka



Patna

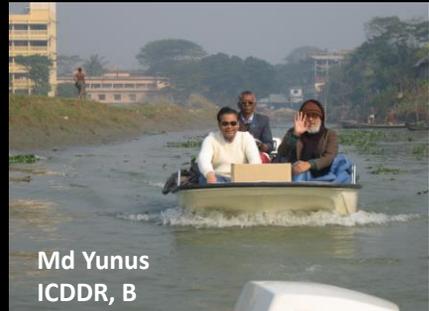


Gracias



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Conclusions and Implications

- Cholera epidemics appear primarily limited by the local depletion of susceptibles
- Explicit 'space' matters (the dynamics are distributed in space or in a network)
- **Stochasticity (demographic noise) might be essential to the epidemic dynamics of infectious diseases, beyond the recognized effect of small population size on extinction.**



NOAA, Oceans and Health
Howard Hughes Medical Institute
Graham Environmental Sustainability Institute (GESI, UM)