# Nonadiabatic Dynamics in Nanoscale Materials with Time-Domain DFT



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#### Nonadiabatic Molecular Dynamics

Nonadiabatic coupling between potential energy surfaces opens channels for system to change electronic states.

transition allowed



#### electrons treated quantum-mechanically



nuclei treated classically



## Time-Domain DFT for Nonadiabatic Molecular Dynamics

Craig, Duncan, Prezhdo *Phys. Rev. Lett.* **95,** 163001 (2005)

Electron density derives from Kohn-Sham orbitals  $\rho(x) = \sum_{p} |\varphi_{p}(x)|^{2} \qquad |\Psi\rangle = |\varphi_{p}(x_{1},t)\varphi_{q}(x_{2},t)...\varphi_{v}(x_{N},t)\rangle_{SD}$ DFT functional *H* depends on nuclear evolution *R(t)* Variational principle gives  $i\hbar \frac{\partial \varphi_{p}(x,t)}{\partial t} = H\varphi_{p}(x,t) \quad p = 1,2...$ Orbitals are expanded in adiabatic KS basis  $\varphi_{p}(x,t) = \sum_{\alpha} c_{p}^{\alpha}(t)\chi^{\alpha}(x)$ 

$$i\hbar c^{\alpha} = \sum_{\beta} c^{\beta} \left( \varepsilon^{\beta} \delta_{\alpha\beta} - i\hbar \left\langle \chi^{\alpha} \left| \vec{\nabla}_{R} \right| \chi^{\beta} \right\rangle \cdot \vec{R} \right)$$

non-adiabatic electron-phonón coupling



# **Theoretical Questions**

Perspective: *JPC Lett.* **7** 2100 (2016)

- How to couple quantum and classical dynamics? quantum back-reaction on classical variables
- Can one do better than classical mechanics for nuclear motion? zero-point motion, tunneling, branching, loss of coherence

LS-GFSH

epresentat

Depend

- Decoherence induced surface hopping (DISH) *JCP* **137**, 22A545 (2012) Coherence penalty functional (CPF) *JCP* **140**, 194107 (2014)
- Self-consistent FSSH (SC-FSSH) JPC-L 5, 713 (2014)
- Global flux surface hopping (GFSH) *JCTC* **10**, 3598 (2014) Second quantized surface hopping (SQUASH) *PRL* **113**, 153003 (2014) FSSH in Liouville space *JPCL* **6**, 3827 (2015) GFSH in Liouville space, *JCP-Rapid* **143**, 191102 (2015)



#### **Ehrenfest Dynamics**

Total energy of  
electrons and nuclei 
$$E_{tot} = \frac{MR}{2} + V(R(t)) + Tr_x \rho(x) H(x; R(t))$$
  
is conserved  $\frac{dE_{tot}}{dt} = 0$ 

time-dependent Hellmann-Feynman theorem gives Newton equation





## Why Surface Hopping Needed?



Average surface is not physical



# Fewest Switches Surface Hopping

Tully, JCP 93, 1061 (1990)

Based on probability  $|c_i|^2$ 

(becomes effectively Ehrenfest)

Fewest Switches

based on flux, d  $|c_i|^2/dt$ 





#### Fewest Switches Surface Hopping Tully, JCP 93, 1061 (1990)



a.k.a., quantum-master equationwith time-dependent transition rates:non-perturbative

- correct short time dynamics

Trajectory branching: Tully, JCP 93, 1061 (1990)

Within TDDFT: Craig, Duncan, Prezhdo *PRL* **95**, 163001 (2005)

Detailed balance, due to hop rejection, needed for thermodynamic equilibrium: Parahdekar, Tully *JCP* **122**, 094102 (2005)



#### Super-Exchange Problem

in Tully's surface hopping J. Chem. Phys. 93, 1061 (1990)

Transition probability  $i \rightarrow j$  is proportional to coupling  $V_{ij}$ ,  $d_{ij}$ .

This excludes super-exchange: *Kramers 1934, Anderson 1950* 



$$b_{ij} = 2\hbar^{-1} \operatorname{Im}\left(a_{ij}^* V_{ij}\right) - 2\operatorname{Re}\left(a_{ij}^* \dot{\mathbf{R}} \cdot \mathbf{d}_{ij}\right)$$



If state 2 is higher than 1 by more than a few kT and 1 and 3 are not coupled 1->3 is forbidden



# **Global Flux Surface Hopping**

Wang, Trivedi, Prezhdo, J. Theor. Comp. Chem. 10, 3598 (2014)

Superexchange model  $V_{11}(x) = 0$ ,  $V_{22}(x) = 0.01$ ,  $V_{33}(x) = 0.005$   $V_{12}(x) = V_{21}(x) = 0.001e^{-x^2/2}$   $V_{23}(x) = V_{32}(x) = 0.01e^{-x^2/2}$  $V_{13}(x) = V_{31}(x) = 0$ 





k=4-7 superexchange regime



## **FSSH** in Liouville Space

#### L. Wang, A.E. Sifain, O.V.P. J Phys Chem Lett 6, 3827 (2015)

$$\frac{\mathrm{d}|\psi(t)\rangle}{\mathrm{d}t} = \frac{1}{i\hbar}\hat{H}|\psi(t)\rangle \qquad \hat{\rho}(t) = |\psi(t)\rangle\langle\psi(t)|$$
$$\frac{\mathrm{d}\hat{\rho}(t)}{\mathrm{d}t} = \frac{1}{i\hbar}[\hat{H},\hat{\rho}] \qquad |\rho\rangle\rangle = \sum_{ij}\rho_{ij}|ij\rangle\rangle$$
$$\frac{\mathrm{d}}{\mathrm{d}t}|\rho\rangle\rangle = \frac{1}{i\hbar}\hat{L}|\rho\rangle\rangle \qquad \text{One trajectory at a}$$
Normal FSSH

One trajectory at a time Normal FSSH



Questions for coherence states,  $i \neq j$ 

- Energy:  $E_{ii} = (E_{ii} + E_{ij})/2$ , similar to quantum-classical Liouville
- Interpretation of trajectories on ij: assign half to ii, half to jj
- Direction of velocity rescaling for transition  $ij \rightarrow kl$ : add NA coupling vectors NA<sub>ik</sub>+NA<sub>il</sub>

# FSSH & GFSH in Liouville Space

L. Wang, A.E. Sifain, O.V.P. JCP-Rapid 143, 191102 (2015)



Super-exchange is obtained



# USC

#### **Global Flux Surface Hopping**

Wang, Trivedi, Prezhdo, *J.Theor.Comp.Chem.* **10**, 3598 (2014) Trivedi, Wang, Prezhdo, *Nano Lett.* **15**, 2086 (2015)





#### Auger Electron-Hole Relaxation and Hole Trapping in CdSe QD Trivedi, Wang, Prezhdo, *Nano Lett.* **15**, 2086 (2015)



Electron Relaxation without trap 1.3 ps with trap 1.8 ps

Hole trapping 1.2 ps



- Hole is localized on surface, ligand tail not important
- Bottleneck not achieved because hole trapping is too slow, not because hole still couples to electron

Experiment: Sippel et al. Nano Lett. 13 1655 (2013)

#### USC Decoherence & Quantum Zeno Effect



O. V. Prezhdo, P. J. Rossky, *Phys. Rev. Lett.* 81, 5294 (1998)
O. V. Prezhdo, *Phys. Rev. Lett.* 85, 4413 (2000)

With decoherence:  $P_{12} = |T_{12}|^2 + |T_{12}|^2 + ... |^2 T_{12}$ Without decoherence  $P_{12} = |T_{12} + T_{12} + ... |^2 T_{12}$ 

Decoherence makes transitions less likely  $|0.1|^2 + |0.1|^2 < |0.1 + 0.1|^2$ 

• atom



dead



#### Stochastic Mean-Field (decoherence gives branching) Prezhdo J. Chem. Phys. 111, 8366 (1999)

No ad hoc expressions for hopping probability









quantum Brownian motion

$$\frac{d\Psi}{=-iH}\frac{\Psi}{dt}\frac{\gamma}{2}L^{+}L\Psi dt + \sqrt{\gamma}L\Psi dW$$
  
friction noise



# Decoherence Induced Surface Hopping (DISH)

Jaeger, Fisher, Prezhdo J. Chem. Phys. 137, 22A545 (2012)

Evolve in an adiabatic state. Hop when a decoherence event occurs. Rescale velocity as before in SH.

**Advantages** 

- 1. Includes decoherence
- 2. Gives branching
- 3. Nuclear evolution in pure states

Corresponds to a piece-wise continuous stochastic Schrodinger equation







# **Coherence Penalty Functional**

Akimov, Long, Prezhdo, J. Chem. Phys. 140, 194107 (2014)

- Retain computational efficiency of Ehrenfest no stochastic sampling: 1 trajectory, ordinary differential equations
- Penalize development of coherence

$$i\hbar \frac{\partial c_i(t)}{\partial t} = \sum_i \left[ E_i(R(t)) \delta_{i,j} - i\hbar \frac{P}{M} d_{ij} \right] c_j(t) \qquad \begin{aligned} q_i &= \operatorname{Re}(c_i) \\ p_i &= \operatorname{Im}(c_i) \end{aligned}$$
$$H = \sum_i \frac{E_i}{2\hbar} \left( q_i^2 + p_i^2 \right) - \frac{P}{M} \sum_{i,j} d_{ij} p_i q_j \qquad \dot{p}_i = -\frac{\partial H}{\partial q_i} \quad \dot{q}_i = -\frac{\partial H}{\partial p_i} \end{aligned}$$



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$$H = \sum_i \frac{E_i}{2\hbar} \left( q_i^2 + p_i^2 \right) - \frac{P}{M} \sum_{i,j} d_{ij} p_i q_j \qquad \dot{p}_i = -\frac{\partial H}{\partial q_i} \quad \dot{q}_i = -\frac{\partial H}{\partial p_i}$$

$$\tilde{H} = H + \sum_{\substack{i,j \\ i \neq j}} \lambda_{ij} \left( q_i^2 + p_i^2 \right) \left( q_j^2 + p_j^2 \right) \qquad \text{states with large coherence} \\ \text{are energy maxima} \end{aligned}$$

$$(q_i^2 + p_i^2)(q_j^2 + p_j^2) = |c_i^* c_j|^2 \qquad \begin{array}{c} \operatorname{coherence} \\ \operatorname{measure} \end{array}$$



## Phonon Bottleneck in CdSe QD

Kilina, Neukirch, Habenicht. Kilin, Prezhdo, PRL 110, 180404 (2013)





#### PYXAID: PYthon eXtension of Ab Initio Dynamics

Akimov, Prezhdo, J. Theor. Comp. Chem. 9, 4959 (2013) ibid. 10, 789 (2014)

Python interfaced with Quantum Espresso, VASP

In DFTB+: Pal, Trivedi, Akimov, Aradi, Frauenheim, Prezhdo JCTC 12 1436 (2016) Fragment approach in Gamess: Negben, Prezhdo JPC A 120 7205 (2016)



Overview of new methods Perspective Article in *JPC Lett.* **7** 2100 (2016)





## **Defects Help Charge Separation**

L. Run, N. English, O. V. Prezhdo J. Am. Chem. Soc. 135, 18892 (2013)



Sulfur vacancy lowers donor-acceptor energy gap (20%) and increases NA coupling (factor of 2) ET time (ps)forward backwardExp:0.4T.Lian JACS 133, 9246 (2011)Ideal:3.410Defect:1.0





QD LUMO



# ET between CdSe QD and C<sub>60</sub>

Chaban & Prezhdo, J. Phys. Chem. Lett 4, 1 (2013)

Mechanical mixture: 10ns







Brown & Kamat, JACS 130, 8891 (2008) Bang & Kamat, ACS Nano 12, 9421 (2011)



<= closer contact faster dynamics =>





# ET between CdSe QD and C<sub>60</sub>

Chaban & Prezhdo, J. Phys. Chem. Lett 4, 1 (2013)

system	ET time, ps	dephasing time, fs	NA coupling, meV	binding energy, kJ mol <sup>-1</sup>	
bridge	7.66	15	2.96 (6.85)	4853	
mixture	37.4	11	0.874 (1.29)	19.0	
with Li	27.7	20	1.60 (2.54)	51.3	
Energy (	eV)				
0 — Vacuum			Bridge provides strong		



Bridge provides strong NA electron-phonon coupling needed to remove excess electron energy



#### Auger-assisted ET

Zhu, Yang, Hyeon-Deuk, Califano, Song, Wang, Zhang, Prezhdo, Lian, Nano Lett. 14, 1263 (2014)



Why is there no Marcus inverted region?  $k(r) \propto e$ 





0.7

0.8

0.9

10

∆G. eV

12

Then, hole transfers energy to phonons



Graphene is a metal: electrons and holes can annihilate, not separate *Can electrons transfer into TiO<sub>2</sub> before they relax?* 





- ET consistently faster than energy loss
- Fast ET due to strong donor-acceptor coupling
- NA ET, though coupling is strong; dense state manifold
- 30-60% of direct ET, delocalized excited state





Quantum yield is independent of excitation energy, in contrast to traditional model

 $QY(\omega) = (\hbar\omega - E_{\rm B})^2 / (4E_{\rm F}\hbar\omega)$ 





#### Perovskite/TiO<sub>2</sub> and Doping

Long, Prezhdo *ACS Nano* **9**, 11143 (2015) Liu, Prezhdo *JPC Lett* **6**, 4463 (2015)



- Electron-hole recombination limits photovoltaic efficiency
- Cl and Br doping increase efficiency: Nano Lett. 13, 1764 (2013); Science 345, 542 (2014)
- Sn doping decreases efficiency: J. Phys. Chem. Lett. 5, 1004 (2014)



#### Perovskite/TiO<sub>2</sub> and Doping

Long, Prezhdo *ACS Nano* **9**, 11143 (2015) Liu, Prezhdo *JPC Lett* **6**, 4463 (2015)



- Cl, Br are smaller than I; poorer contact with TiO<sub>2</sub>
- Cl, Br do not contribute to HOMO; NA coupling decreases
- Sn contributes to HOMO, is lighter than Pb; NA coupling increases
- Lighter Cl, Br shorten quantum coherence; reduce rate



# **Perovskite Grain Boundary**

Long, Liu, Prezhdo, JACS 138 3884 (2016); JACS spotlight





- By creating localized states, gap and increases coupling
- Cl-doping pushes e-h states • away from boundary, reduces coupling



#### Perovskite Iodine Interstitial Defect

Li, Liu, Bai, Zhang, Prezhdo, ACS Energ. Lett. in press



- Hole trapping is fast, but recombination of trapped hole with electron is very slow because electron and hole are separated
- Hole can be trapped and de-trapped multiple times before recombining, increasing free carrier lifetimes





#### Moisture and e-h Recombination

Long, Fang, Prezhdo, J Phys Chem Lett 7 3215 (2016)



- Small amount of water localizes electron, distances it from hole
- Water film increases phonon coupling, accelerates e-h recombination
- Electron trap is not deep, next to conduction band edge

Some moisture is good: *Science* 542 **345** (2014); *ACS Nano* **9** 9380 (2015) A lot of moisture is bad: *ACS Nano* **9** 9380 (2015); *J Am Chem Soc* **137** 1530 (2015)



# Local Order in Perovskites

Jankowska, Prezhdo, J. Phys. Chem. Lett. 8, 812 (2017)



Table 1. Canonically Averaged Bandgap and Its Standard Deviation ( $\sigma_{BG}$ ), Absolute Value of NAC, Pure-Dephasing Time, and Nonradiative Electron-Hole Recombination Time ( $\tau$ ) for Studied Perovskite Forms

form	bandgap/eV	$\sigma_{ m BG}/ m meV$	NAC /meV	dephasing/fs	$\tau/\mathrm{ps}$
ferro	3.56	0.13	0.658	7.5	800
anti-ferro	3.37	0.11	0.849	8.0	559
mixed	3.41	0.10	0.768	10.0	612

Ferro-electric order decreases NA coupling, shortens coherence, and hence, increases lifetime

> There is no NA coupling tail in ferro phase



## Local Order in Perovskites

Jankowska, Prezhdo, J. Phys. Chem. Lett. 8, 812 (2017)



# **Singlet Fission**

#### Akimov, Prezhdo JACS, 2014, 136, 1599



Experiment: Chan et al. Science **2011**, 334, 1541

observation of ME

ME does not originate from S1

initial state is a superposition of S1 and ME



1 photon = 2 electrons:  $max \sim 44\%$ 

# **Comprehensive Kinetics**

Akimov, Prezhdo JACS, 2014, 136, 1599



) Reproduce experimental timescales

- 2) CT competes with SF, reducing efficiency
- 3) Intermediate ME and CT states are important
- S<sub>1</sub> to ME transition is slow
- 5) Resolved inconsistency in energy alignment, CT<sub>0</sub>

#### SF photovoltaic design principles

S<sub>1</sub> and ME should be coupled during photoexcitation

Thick pentacene layer slows down CT, allowing SF to happen



# **2D Mapping of Pentacene**

Yost et al. Nat. Chem. 6, 492 (2014)





2D mappings of inter-chromophore structure suggest how to maximize singlet fission through molecular packing



Standard structures are not optimal

**Optimal conformations are slipped in transverse direction by one ring** 





#### Dimensionality and ET Mechanism



Tafen, Long, Prezhdo Nano Lett. 14, 1790 (2014)





# **CNT/Polymer Asymmetry**

Long, Prezhdo Nano Lett, 14, 3335 (2014)





*More CNT*: harvest broader light spectrum; reduce energy/voltage losses *More P3HT*: better charge separation and higher current



#### Superconductors

#### Long, Prezhdo, J. Phys. Chem. Lett. 8, 193 (2017)

- Electron-phonon coupling leads to Cooper pairing
- Measuring electron-phonon relaxation time gives experimental estimate of coupling (earlier from Raman or neutron scattering)

 $\lambda \langle \omega^2 \rangle = \frac{2\pi}{3} \frac{k_B T_l}{\hbar \tau_{e-ph}}$  electron-phonon coupling (2<sup>nd</sup> moment of Eliashberg function) Eliashberg theory generalizes Bardeen-Cooper-Schriffer theory  $T_c = \omega_D \lambda/2$  critical temperature for superconductivity in strong coupling limit



Faster, 100 fs component is associated with electron-phonon interactions

PRL 105 257001 (2010)

![](_page_49_Figure_0.jpeg)

- Reproduced dynamics in YBCO; considered 3 derivatives
- YBCS shows stronger electron-phonon coupling, possibly higher  $T_c$
- Though S is heavier that O, but stronger bonding interaction
- Higher valence band density of states

![](_page_50_Picture_0.jpeg)

## **Decomposition of Nitro-Fullerene**

Chaban, Prezhdo J. Phys. Chem. Lett 6 913 (2015)

![](_page_50_Figure_3.jpeg)

![](_page_50_Picture_4.jpeg)

#### After 100 ps

 $C_{60} [NO_2]_{12}$ 

(a) Initial configuration
(b) C-NO<sub>2</sub> => C-O-N-O
(c) CO, NO on C<sub>60</sub> surface
(d) Explosion, CO=>CO<sub>2</sub> NO=>NO<sub>2</sub>

![](_page_50_Figure_8.jpeg)

![](_page_51_Picture_0.jpeg)

#### Explosion of Nitro-Fullerene Chaban, Prezhdo JPC Lett 6 913 (2015)

![](_page_51_Figure_2.jpeg)

 $C_{60} [NO_2]_{12}$ 

(a) Initial configuration
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(c) CO, NO on C<sub>60</sub> surface
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# NewScientist

Tiny buckybombs could make bacteria explode

![](_page_51_Picture_7.jpeg)

03 September 2014

![](_page_52_Picture_0.jpeg)

## Photo-Initiated Explosion of Polynitro-CNT

Chaban, Pal, Prezhdo, JACS 138, 15927 (2016)

![](_page_52_Figure_3.jpeg)

- NO<sub>2</sub> groups contribute to DOS at all energies; hence, immediately activated by electron-phonon relaxation after IR absorption
- Electron-phonon energy redistribution within 0.1-1ps
- Explosion within 10ps
- Chemistry continues past 100ps

![](_page_53_Figure_0.jpeg)

- Explosion is possible both with and without oxygen
- About twice more energy is released if oxygen is present

![](_page_54_Picture_0.jpeg)

# In Lieu of Conclusions

Nonadiabatic Molecular Dynamics with Time-Dependent Density Functional Theory

#### Applications

- Auger assisted ET; lack of Marcus inverted regime
- Why graphene (metal!) can be used as light-harvester?
- Instantaneous plasmon-driven ET
- Perovskites, role of boundaries, dopants, humidity, order
- Singlet fission vs. charge transfer?
- Dimensionality and ET mechanism
- Exploiting asymmetry of ET in CNT/polymer systems
- Measure of el-ph coupling in superconductors
- Photo-induced explosion of nitro-CNTs

![](_page_54_Picture_13.jpeg)

![](_page_54_Picture_14.jpeg)

![](_page_55_Picture_0.jpeg)

#### SC Why Surface Hopping in Kohn-Sham Representation Works

S. Fischer, B. Habenicht, A. Madrid, W. Duncan, O. V. Prezhdo, J. Chem. Phys. **134**, 024102 (2011)

- KS close to LR/TDDFT (in contrast to HF and CIS)
- No bond-breaking, conformational changes.
- Many-electrons, single excitation small perturbation
- Averaging over many initial conditions and pathways

![](_page_56_Figure_6.jpeg)

1580

1600

![](_page_57_Figure_0.jpeg)

# Additional Approximations Useful for Nanoscale Systems

- 1. DFT functional (Hamiltonian) depends on ground state density, even though the true density does evolve
- 2. Ground and excited state nuclear trajectories are similar

#### Justification:

- 1. Excitation of 1 or 2 electrons out of hundreds does not change density and forces much
- 2. Thermal fluctuations are often larger than differences in the equilibrium geometries of ground and excited electronic states

<u>Key Advantage</u> – allows use of ground state trajectory, while still performing TDKS & SH for electronic state populations