Nonadiabatic Dynamics in Nanoscale Materials with Time-Domain DFT



Oleg Prezhdo U. Southern California



Trieste May 9, 2017











Nonadiabatic Molecular Dynamics

Nonadiabatic coupling between potential energy surfaces opens channels for system to change electronic states.

transition allowed



electrons treated quantum-mechanically



nuclei treated classically



Time-Domain DFT for Nonadiabatic Molecular Dynamics

Craig, Duncan, Prezhdo *Phys. Rev. Lett.* **95,** 163001 (2005)

Electron density derives from Kohn-Sham orbitals $\rho(x) = \sum_{p} |\varphi_{p}(x)|^{2} \qquad |\Psi\rangle = |\varphi_{p}(x_{1},t)\varphi_{q}(x_{2},t)...\varphi_{v}(x_{N},t)\rangle_{SD}$ DFT functional *H* depends on nuclear evolution *R(t)* Variational principle gives $i\hbar \frac{\partial \varphi_{p}(x,t)}{\partial t} = H\varphi_{p}(x,t) \quad p = 1,2...$ Orbitals are expanded in adiabatic KS basis $\varphi_{p}(x,t) = \sum_{\alpha} c_{p}^{\alpha}(t)\chi^{\alpha}(x)$

$$i\hbar c^{\alpha} = \sum_{\beta} c^{\beta} \left(\varepsilon^{\beta} \delta_{\alpha\beta} - i\hbar \left\langle \chi^{\alpha} \left| \vec{\nabla}_{R} \right| \chi^{\beta} \right\rangle \cdot \vec{R} \right)$$

non-adiabatic electron-phonón coupling



Theoretical Questions

Perspective: *JPC Lett.* **7** 2100 (2016)

- How to couple quantum and classical dynamics? quantum back-reaction on classical variables
- Can one do better than classical mechanics for nuclear motion? zero-point motion, tunneling, branching, loss of coherence

LS-GFSH

epresentat

Depend

- Decoherence induced surface hopping (DISH) *JCP* **137**, 22A545 (2012) Coherence penalty functional (CPF) *JCP* **140**, 194107 (2014)
- Self-consistent FSSH (SC-FSSH) JPC-L 5, 713 (2014)
- Global flux surface hopping (GFSH) *JCTC* **10**, 3598 (2014) Second quantized surface hopping (SQUASH) *PRL* **113**, 153003 (2014) FSSH in Liouville space *JPCL* **6**, 3827 (2015) GFSH in Liouville space, *JCP-Rapid* **143**, 191102 (2015)



Ehrenfest Dynamics

Total energy of
electrons and nuclei
$$E_{tot} = \frac{MR}{2} + V(R(t)) + Tr_x \rho(x) H(x; R(t))$$

is conserved $\frac{dE_{tot}}{dt} = 0$

time-dependent Hellmann-Feynman theorem gives Newton equation





Why Surface Hopping Needed?



Average surface is not physical



Fewest Switches Surface Hopping

Tully, JCP 93, 1061 (1990)

Based on probability $|c_i|^2$

(becomes effectively Ehrenfest)

Fewest Switches

based on flux, d $|c_i|^2/dt$





Fewest Switches Surface Hopping Tully, JCP 93, 1061 (1990)



a.k.a., quantum-master equationwith time-dependent transition rates:non-perturbative

- correct short time dynamics

Trajectory branching: Tully, JCP 93, 1061 (1990)

Within TDDFT: Craig, Duncan, Prezhdo *PRL* **95**, 163001 (2005)

Detailed balance, due to hop rejection, needed for thermodynamic equilibrium: Parahdekar, Tully *JCP* **122**, 094102 (2005)



Super-Exchange Problem

in Tully's surface hopping J. Chem. Phys. 93, 1061 (1990)

Transition probability $i \rightarrow j$ is proportional to coupling V_{ij} , d_{ij} .

This excludes super-exchange: *Kramers 1934, Anderson 1950*



$$b_{ij} = 2\hbar^{-1} \operatorname{Im}\left(a_{ij}^* V_{ij}\right) - 2\operatorname{Re}\left(a_{ij}^* \dot{\mathbf{R}} \cdot \mathbf{d}_{ij}\right)$$



If state 2 is higher than 1 by more than a few kT and 1 and 3 are not coupled 1->3 is forbidden



Global Flux Surface Hopping

Wang, Trivedi, Prezhdo, J. Theor. Comp. Chem. 10, 3598 (2014)

Superexchange model $V_{11}(x) = 0$, $V_{22}(x) = 0.01$, $V_{33}(x) = 0.005$ $V_{12}(x) = V_{21}(x) = 0.001e^{-x^2/2}$ $V_{23}(x) = V_{32}(x) = 0.01e^{-x^2/2}$ $V_{13}(x) = V_{31}(x) = 0$





k=4-7 superexchange regime



FSSH in Liouville Space

L. Wang, A.E. Sifain, O.V.P. J Phys Chem Lett 6, 3827 (2015)

$$\frac{\mathrm{d}|\psi(t)\rangle}{\mathrm{d}t} = \frac{1}{i\hbar}\hat{H}|\psi(t)\rangle \qquad \hat{\rho}(t) = |\psi(t)\rangle\langle\psi(t)|$$
$$\frac{\mathrm{d}\hat{\rho}(t)}{\mathrm{d}t} = \frac{1}{i\hbar}[\hat{H},\hat{\rho}] \qquad |\rho\rangle\rangle = \sum_{ij}\rho_{ij}|ij\rangle\rangle$$
$$\frac{\mathrm{d}}{\mathrm{d}t}|\rho\rangle\rangle = \frac{1}{i\hbar}\hat{L}|\rho\rangle\rangle \qquad \text{One trajectory at a}$$
Normal FSSH

One trajectory at a time Normal FSSH



Questions for coherence states, $i \neq j$

- Energy: $E_{ii} = (E_{ii} + E_{ij})/2$, similar to quantum-classical Liouville
- Interpretation of trajectories on ij: assign half to ii, half to jj
- Direction of velocity rescaling for transition $ij \rightarrow kl$: add NA coupling vectors NA_{ik}+NA_{il}

FSSH & GFSH in Liouville Space

L. Wang, A.E. Sifain, O.V.P. JCP-Rapid 143, 191102 (2015)



Super-exchange is obtained



USC

Global Flux Surface Hopping

Wang, Trivedi, Prezhdo, *J.Theor.Comp.Chem.* **10**, 3598 (2014) Trivedi, Wang, Prezhdo, *Nano Lett.* **15**, 2086 (2015)





Auger Electron-Hole Relaxation and Hole Trapping in CdSe QD Trivedi, Wang, Prezhdo, *Nano Lett.* **15**, 2086 (2015)



Electron Relaxation without trap 1.3 ps with trap 1.8 ps

Hole trapping 1.2 ps



- Hole is localized on surface, ligand tail not important
- Bottleneck not achieved because hole trapping is too slow, not because hole still couples to electron

Experiment: Sippel et al. Nano Lett. 13 1655 (2013)

USC Decoherence & Quantum Zeno Effect



O. V. Prezhdo, P. J. Rossky, *Phys. Rev. Lett.* 81, 5294 (1998)
O. V. Prezhdo, *Phys. Rev. Lett.* 85, 4413 (2000)

With decoherence: $P_{12} = |T_{12}|^2 + |T_{12}|^2 + ... |^2 T_{12}$ Without decoherence $P_{12} = |T_{12} + T_{12} + ... |^2 T_{12}$

Decoherence makes transitions less likely $|0.1|^2 + |0.1|^2 < |0.1 + 0.1|^2$

• atom



dead



Stochastic Mean-Field (decoherence gives branching) Prezhdo J. Chem. Phys. 111, 8366 (1999)

No ad hoc expressions for hopping probability









quantum Brownian motion

$$\frac{d\Psi}{=-iH}\frac{\Psi}{dt}\frac{\gamma}{2}L^{+}L\Psi dt + \sqrt{\gamma}L\Psi dW$$

friction noise



Decoherence Induced Surface Hopping (DISH)

Jaeger, Fisher, Prezhdo J. Chem. Phys. 137, 22A545 (2012)

Evolve in an adiabatic state. Hop when a decoherence event occurs. Rescale velocity as before in SH.

Advantages

- 1. Includes decoherence
- 2. Gives branching
- 3. Nuclear evolution in pure states

Corresponds to a piece-wise continuous stochastic Schrodinger equation







Coherence Penalty Functional

Akimov, Long, Prezhdo, J. Chem. Phys. 140, 194107 (2014)

- Retain computational efficiency of Ehrenfest no stochastic sampling: 1 trajectory, ordinary differential equations
- Penalize development of coherence

$$i\hbar \frac{\partial c_i(t)}{\partial t} = \sum_i \left[E_i(R(t)) \delta_{i,j} - i\hbar \frac{P}{M} d_{ij} \right] c_j(t) \qquad \begin{aligned} q_i &= \operatorname{Re}(c_i) \\ p_i &= \operatorname{Im}(c_i) \end{aligned}$$
$$H = \sum_i \frac{E_i}{2\hbar} \left(q_i^2 + p_i^2 \right) - \frac{P}{M} \sum_{i,j} d_{ij} p_i q_j \qquad \dot{p}_i = -\frac{\partial H}{\partial q_i} \quad \dot{q}_i = -\frac{\partial H}{\partial p_i} \end{aligned}$$



Coherence Penalty Functional

Akimov, Long, Prezhdo, J. Chem. Phys. 140, 194107 (2014)

- Retain computational efficiency of Ehrenfest no stochastic sampling: 1 trajectory, ordinary differential equations
- Penalize development of coherence

$$i\hbar \frac{\partial c_i(t)}{\partial t} = \sum_i \left[E_i(R(t)) \delta_{i,j} - i\hbar \frac{P}{M} d_{ij} \right] c_j(t) \qquad \begin{array}{l} q_i = \operatorname{Re}(c_i) \\ p_i = \operatorname{Im}(c_i) \end{array}$$

$$H = \sum_i \frac{E_i}{2\hbar} \left(q_i^2 + p_i^2 \right) - \frac{P}{M} \sum_{i,j} d_{ij} p_i q_j \qquad \dot{p}_i = -\frac{\partial H}{\partial q_i} \quad \dot{q}_i = -\frac{\partial H}{\partial p_i}$$

$$\tilde{H} = H + \sum_{\substack{i,j \\ i \neq j}} \lambda_{ij} \left(q_i^2 + p_i^2 \right) \left(q_j^2 + p_j^2 \right) \qquad \text{states with large coherence} \\ \text{are energy maxima} \end{aligned}$$

$$(q_i^2 + p_i^2)(q_j^2 + p_j^2) = |c_i^* c_j|^2 \qquad \begin{array}{c} \operatorname{coherence} \\ \operatorname{measure} \end{array}$$



Phonon Bottleneck in CdSe QD

Kilina, Neukirch, Habenicht. Kilin, Prezhdo, PRL 110, 180404 (2013)





PYXAID: PYthon eXtension of Ab Initio Dynamics

Akimov, Prezhdo, J. Theor. Comp. Chem. 9, 4959 (2013) ibid. 10, 789 (2014)

Python interfaced with Quantum Espresso, VASP

In DFTB+: Pal, Trivedi, Akimov, Aradi, Frauenheim, Prezhdo JCTC 12 1436 (2016) Fragment approach in Gamess: Negben, Prezhdo JPC A 120 7205 (2016)



Overview of new methods Perspective Article in *JPC Lett.* **7** 2100 (2016)





Defects Help Charge Separation

L. Run, N. English, O. V. Prezhdo J. Am. Chem. Soc. 135, 18892 (2013)



Sulfur vacancy lowers donor-acceptor energy gap (20%) and increases NA coupling (factor of 2) ET time (ps)forward backwardExp:0.4T.Lian JACS 133, 9246 (2011)Ideal:3.410Defect:1.0





QD LUMO



ET between CdSe QD and C₆₀

Chaban & Prezhdo, J. Phys. Chem. Lett 4, 1 (2013)

Mechanical mixture: 10ns







Brown & Kamat, JACS 130, 8891 (2008) Bang & Kamat, ACS Nano 12, 9421 (2011)



<= closer contact faster dynamics =>





ET between CdSe QD and C₆₀

Chaban & Prezhdo, J. Phys. Chem. Lett 4, 1 (2013)

system	ET time, ps	dephasing time, fs	NA coupling, meV	binding energy, kJ mol ⁻¹	
bridge	7.66	15	2.96 (6.85)	4853	
mixture	37.4	11	0.874 (1.29)	19.0	
with Li	27.7	20	1.60 (2.54)	51.3	
Energy (eV)				
0 — Vacuum			Bridge provides strong		



Bridge provides strong NA electron-phonon coupling needed to remove excess electron energy



Auger-assisted ET

Zhu, Yang, Hyeon-Deuk, Califano, Song, Wang, Zhang, Prezhdo, Lian, Nano Lett. 14, 1263 (2014)



Why is there no Marcus inverted region? $k(r) \propto e$





0.7

0.8

0.9

10

∆G. eV

12

Then, hole transfers energy to phonons



Graphene is a metal: electrons and holes can annihilate, not separate *Can electrons transfer into TiO₂ before they relax?*





- ET consistently faster than energy loss
- Fast ET due to strong donor-acceptor coupling
- NA ET, though coupling is strong; dense state manifold
- 30-60% of direct ET, delocalized excited state





Quantum yield is independent of excitation energy, in contrast to traditional model

 $QY(\omega) = (\hbar\omega - E_{\rm B})^2 / (4E_{\rm F}\hbar\omega)$





Perovskite/TiO₂ and Doping

Long, Prezhdo *ACS Nano* **9**, 11143 (2015) Liu, Prezhdo *JPC Lett* **6**, 4463 (2015)



- Electron-hole recombination limits photovoltaic efficiency
- Cl and Br doping increase efficiency: Nano Lett. 13, 1764 (2013); Science 345, 542 (2014)
- Sn doping decreases efficiency: J. Phys. Chem. Lett. 5, 1004 (2014)



Perovskite/TiO₂ and Doping

Long, Prezhdo *ACS Nano* **9**, 11143 (2015) Liu, Prezhdo *JPC Lett* **6**, 4463 (2015)



- Cl, Br are smaller than I; poorer contact with TiO₂
- Cl, Br do not contribute to HOMO; NA coupling decreases
- Sn contributes to HOMO, is lighter than Pb; NA coupling increases
- Lighter Cl, Br shorten quantum coherence; reduce rate



Perovskite Grain Boundary

Long, Liu, Prezhdo, JACS 138 3884 (2016); JACS spotlight





- By creating localized states, gap and increases coupling
- Cl-doping pushes e-h states • away from boundary, reduces coupling



Perovskite Iodine Interstitial Defect

Li, Liu, Bai, Zhang, Prezhdo, ACS Energ. Lett. in press



- Hole trapping is fast, but recombination of trapped hole with electron is very slow because electron and hole are separated
- Hole can be trapped and de-trapped multiple times before recombining, increasing free carrier lifetimes





Moisture and e-h Recombination

Long, Fang, Prezhdo, J Phys Chem Lett 7 3215 (2016)



- Small amount of water localizes electron, distances it from hole
- Water film increases phonon coupling, accelerates e-h recombination
- Electron trap is not deep, next to conduction band edge

Some moisture is good: *Science* 542 **345** (2014); *ACS Nano* **9** 9380 (2015) A lot of moisture is bad: *ACS Nano* **9** 9380 (2015); *J Am Chem Soc* **137** 1530 (2015)



Local Order in Perovskites

Jankowska, Prezhdo, J. Phys. Chem. Lett. 8, 812 (2017)



Table 1. Canonically Averaged Bandgap and Its Standard Deviation (σ_{BG}), Absolute Value of NAC, Pure-Dephasing Time, and Nonradiative Electron-Hole Recombination Time (τ) for Studied Perovskite Forms

form	bandgap/eV	$\sigma_{ m BG}/ m meV$	NAC /meV	dephasing/fs	τ/ps
ferro	3.56	0.13	0.658	7.5	800
anti-ferro	3.37	0.11	0.849	8.0	559
mixed	3.41	0.10	0.768	10.0	612

Ferro-electric order decreases NA coupling, shortens coherence, and hence, increases lifetime

> There is no NA coupling tail in ferro phase



Local Order in Perovskites

Jankowska, Prezhdo, J. Phys. Chem. Lett. 8, 812 (2017)



Singlet Fission

Akimov, Prezhdo JACS, 2014, 136, 1599



Experiment: Chan et al. Science **2011**, 334, 1541

observation of ME

ME does not originate from S1

initial state is a superposition of S1 and ME



1 photon = 2 electrons: $max \sim 44\%$

Comprehensive Kinetics

Akimov, Prezhdo JACS, 2014, 136, 1599



) Reproduce experimental timescales

- 2) CT competes with SF, reducing efficiency
- 3) Intermediate ME and CT states are important
- S₁ to ME transition is slow
- 5) Resolved inconsistency in energy alignment, CT₀

SF photovoltaic design principles

S₁ and ME should be coupled during photoexcitation

Thick pentacene layer slows down CT, allowing SF to happen



2D Mapping of Pentacene

Yost et al. Nat. Chem. 6, 492 (2014)





2D mappings of inter-chromophore structure suggest how to maximize singlet fission through molecular packing



Standard structures are not optimal

Optimal conformations are slipped in transverse direction by one ring





Dimensionality and ET Mechanism



Tafen, Long, Prezhdo Nano Lett. 14, 1790 (2014)





CNT/Polymer Asymmetry

Long, Prezhdo Nano Lett, 14, 3335 (2014)





More CNT: harvest broader light spectrum; reduce energy/voltage losses *More P3HT*: better charge separation and higher current



Superconductors

Long, Prezhdo, J. Phys. Chem. Lett. 8, 193 (2017)

- Electron-phonon coupling leads to Cooper pairing
- Measuring electron-phonon relaxation time gives experimental estimate of coupling (earlier from Raman or neutron scattering)

 $\lambda \langle \omega^2 \rangle = \frac{2\pi}{3} \frac{k_B T_l}{\hbar \tau_{e-ph}}$ electron-phonon coupling (2nd moment of Eliashberg function) Eliashberg theory generalizes Bardeen-Cooper-Schriffer theory $T_c = \omega_D \lambda/2$ critical temperature for superconductivity in strong coupling limit



Faster, 100 fs component is associated with electron-phonon interactions

PRL 105 257001 (2010)



- Reproduced dynamics in YBCO; considered 3 derivatives
- YBCS shows stronger electron-phonon coupling, possibly higher T_c
- Though S is heavier that O, but stronger bonding interaction
- Higher valence band density of states



Decomposition of Nitro-Fullerene

Chaban, Prezhdo J. Phys. Chem. Lett 6 913 (2015)





After 100 ps

 $C_{60} [NO_2]_{12}$

(a) Initial configuration
(b) C-NO₂ => C-O-N-O
(c) CO, NO on C₆₀ surface
(d) Explosion, CO=>CO₂ NO=>NO₂





Explosion of Nitro-Fullerene Chaban, Prezhdo JPC Lett 6 913 (2015)



 $C_{60} [NO_2]_{12}$

(a) Initial configuration
(b) C-NO₂ => C-O-N-O
(c) CO, NO on C₆₀ surface
(d) Explosion, CO=>CO₂ NO=>NO₂

NewScientist

Tiny buckybombs could make bacteria explode



03 September 2014



Photo-Initiated Explosion of Polynitro-CNT

Chaban, Pal, Prezhdo, JACS 138, 15927 (2016)



- NO₂ groups contribute to DOS at all energies; hence, immediately activated by electron-phonon relaxation after IR absorption
- Electron-phonon energy redistribution within 0.1-1ps
- Explosion within 10ps
- Chemistry continues past 100ps



- Explosion is possible both with and without oxygen
- About twice more energy is released if oxygen is present



In Lieu of Conclusions

Nonadiabatic Molecular Dynamics with Time-Dependent Density Functional Theory

Applications

- Auger assisted ET; lack of Marcus inverted regime
- Why graphene (metal!) can be used as light-harvester?
- Instantaneous plasmon-driven ET
- Perovskites, role of boundaries, dopants, humidity, order
- Singlet fission vs. charge transfer?
- Dimensionality and ET mechanism
- Exploiting asymmetry of ET in CNT/polymer systems
- Measure of el-ph coupling in superconductors
- Photo-induced explosion of nitro-CNTs







SC Why Surface Hopping in Kohn-Sham Representation Works

S. Fischer, B. Habenicht, A. Madrid, W. Duncan, O. V. Prezhdo, J. Chem. Phys. **134**, 024102 (2011)

- KS close to LR/TDDFT (in contrast to HF and CIS)
- No bond-breaking, conformational changes.
- Many-electrons, single excitation small perturbation
- Averaging over many initial conditions and pathways



1580

1600



Additional Approximations Useful for Nanoscale Systems

- 1. DFT functional (Hamiltonian) depends on ground state density, even though the true density does evolve
- 2. Ground and excited state nuclear trajectories are similar

Justification:

- 1. Excitation of 1 or 2 electrons out of hundreds does not change density and forces much
- 2. Thermal fluctuations are often larger than differences in the equilibrium geometries of ground and excited electronic states

<u>Key Advantage</u> – allows use of ground state trajectory, while still performing TDKS & SH for electronic state populations