

# Anomalous Excitons in Titanium Dioxide

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# Outline

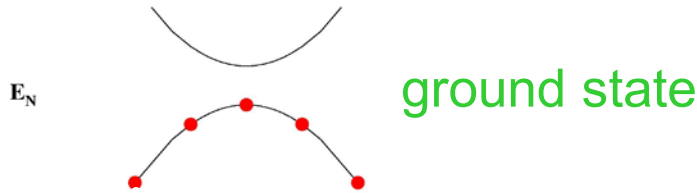


- introduction on  $\text{TiO}_2$
- new data: experiments, theory, the role of doping and temperature on
  - electronic gap
  - optical response
- the nature of excitons in anatase
- further peculiar behaviour of excitons in  $\text{TiO}_2$

# 3-steps theoretical/computational ab initio method for optics: MBPT

Ground State properties (Total energy):

DFT-GGA

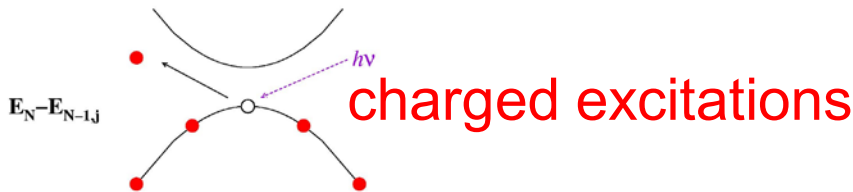


$$\left(-\frac{1}{2}\nabla^2 + V^{ext} + V^H + V_{xc}\right)\phi_j^{KS}(\vec{r}) = \varepsilon_j^{KS}\phi_j^{KS}(\vec{r})$$

G. Onida, L. Reining,  
A. Rubio, Rev. Mod. Phys.  
74 (2002) 601,  
and references therein

1 particle excitations (photoemission)

GW



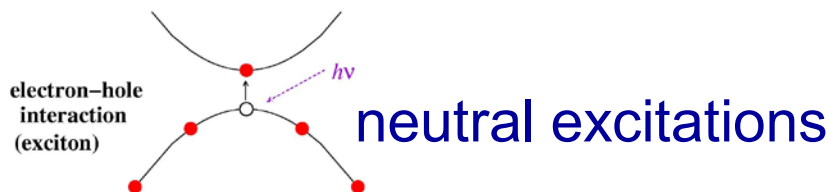
$$\left(-\frac{1}{2}\nabla^2 + V^{ext} + V^H\right)\Psi_j^{QP}(\vec{r}) + \int \Sigma(\vec{r}, \vec{r}', \varepsilon_j^{QP})\Psi_j^{QP}(\vec{r}')d\vec{r}' = \varepsilon_j^{QP}\Psi_j^{QP}(\vec{r})$$

**CODES**

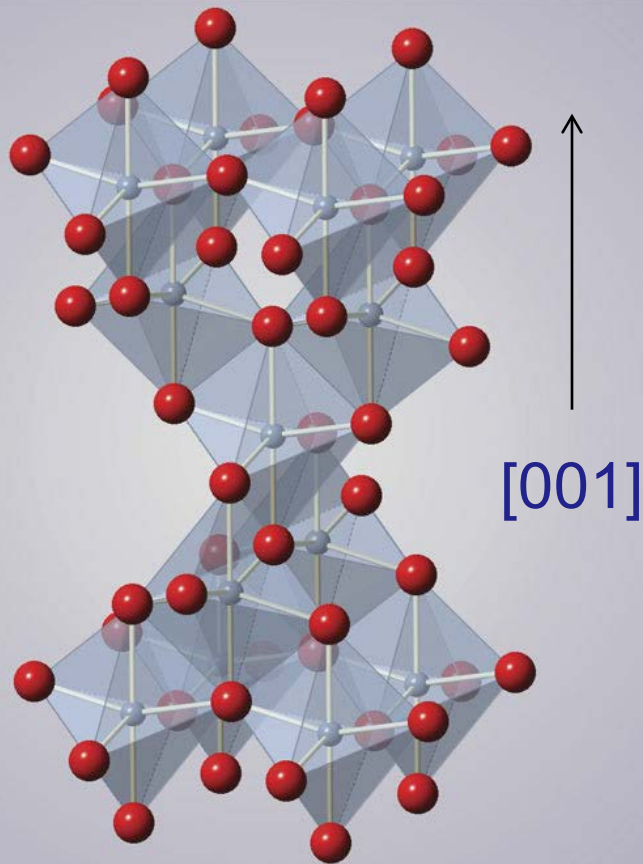
*Quantum Espresso* (DFT)  
*BerkeleyGW*, *Yambo*  
(GW+BSE)

2 particle excitations (absorption)

BSE



# Anatase Crystal Structure



blue atoms: titanium  
red atoms: oxygen  
TiO<sub>6</sub> polyhedra highlighted

tetragonal, anisotropic unit cell  
network of corner-sharing or edge  
sharing TiO<sub>6</sub> octahedra

Ti-3d O-2p orbital interactions run  
mainly in TiO<sub>2</sub> bilayers,  
perpendicular to [001]  
minor contribution along [001]

# ANATASE $\text{TiO}_2$



- material easily fabricated and widely available, useful for energy conversion and transport
- we started working at it in 2008-2009, with GW+BSE
  - GW direct gap at  $\Gamma$ , 4.29 eV (exp. unknown at the time)
  - GW indirect gap at  $X\Gamma$ , 3.83 eV
  - first optical transition at 3.90 eV

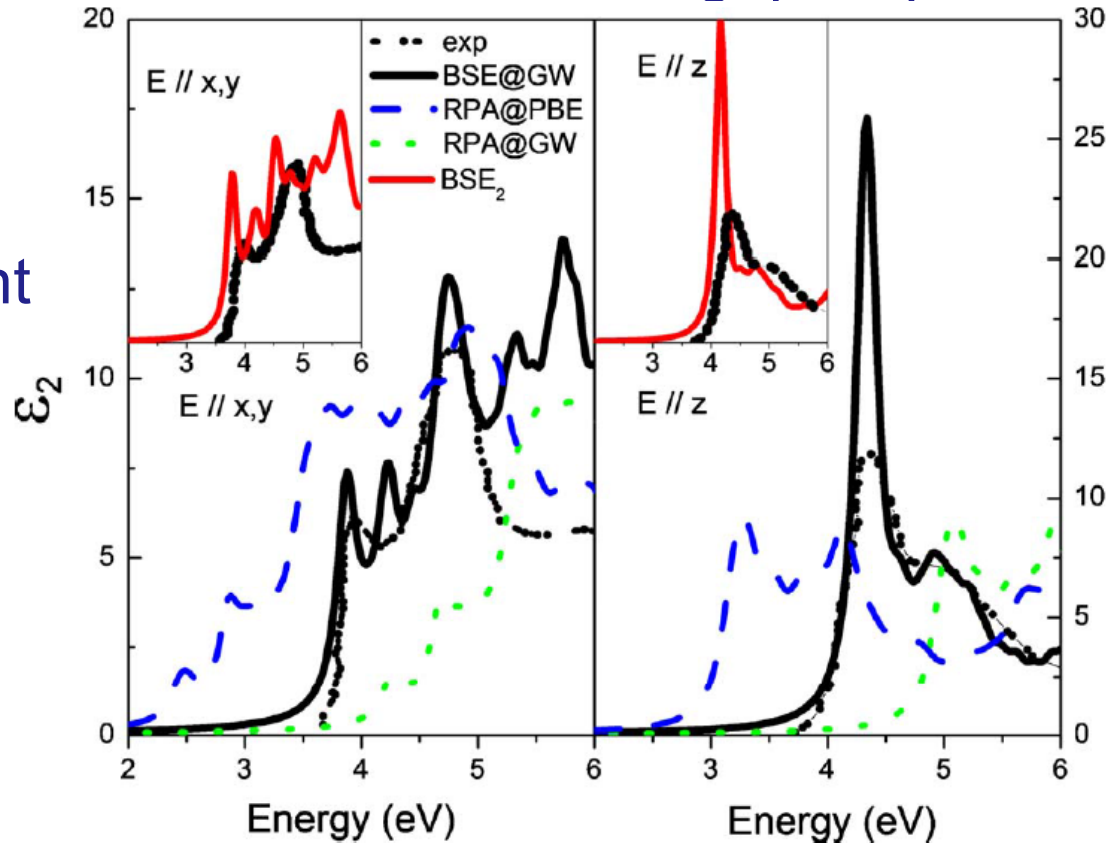
Phys. Rev. B 82, 045207 (2010)

# ANATASE TiO<sub>2</sub>



- the optical direct gap is at 3.9 eV (not at 3.2 eV)  
(where an Urbach tail, related to the indirect gap, is present)

reasonable agreement  
with experiments  
*note the anisotropy*



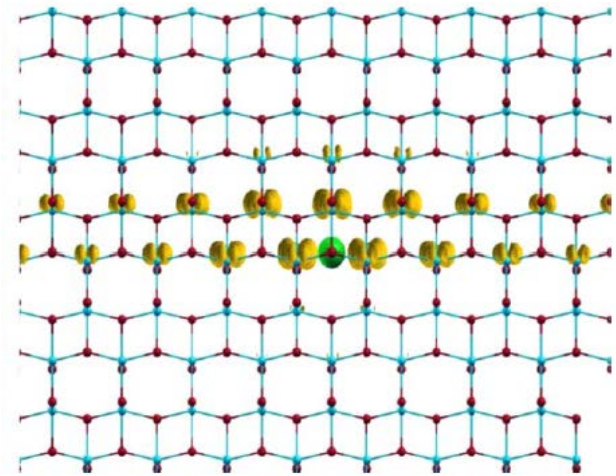
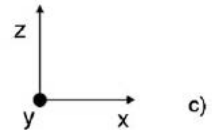
*these were the facts..... BUT*

# ANATASE $\text{TiO}_2$



BUT ..

- first optical transition is ABOVE direct gap at  $\Gamma$
- first optical transition is BELOW indirect gap at X  $\Gamma$
- first optical transition has an associated wavefunction of peculiar shape



so, there were the 'OPEN QUESTIONS':

PRB 82, 045207 (2010)

- is the first optical transition **bound**? why?
- is there a certain degree of **localization**? why?

# Why it is difficult



- difficulty of measuring the exciton binding energy ( $E_B$ ) for an indirect gap material
- perfect, infinite crystal in calculations
- experimental anatase crystals show defects
- nanoparticles (mostly used in applications) are
  - in solvent
  - disordered
  - doped and defected

How to reconcile everything?



# New Experimental and Theoretical Data

collaboration with EPFL experimental group

- steady-state angle-resolved photoemission spectroscopy
- spectroscopic ellipsometry (SE)
- ultrafast two-dimensional deep-ultraviolet spectroscopy

applied to

- pristine TiO<sub>2</sub> anatase crystal of excellent quality
- TiO<sub>2</sub> anatase crystals with various degrees of doping (defects)
- nanoparticles in solvent

combined with

- ab initio many body calculations (GW + BSE), involving also DOPING and TEMPERATURE effects

# Electronic Band Gap

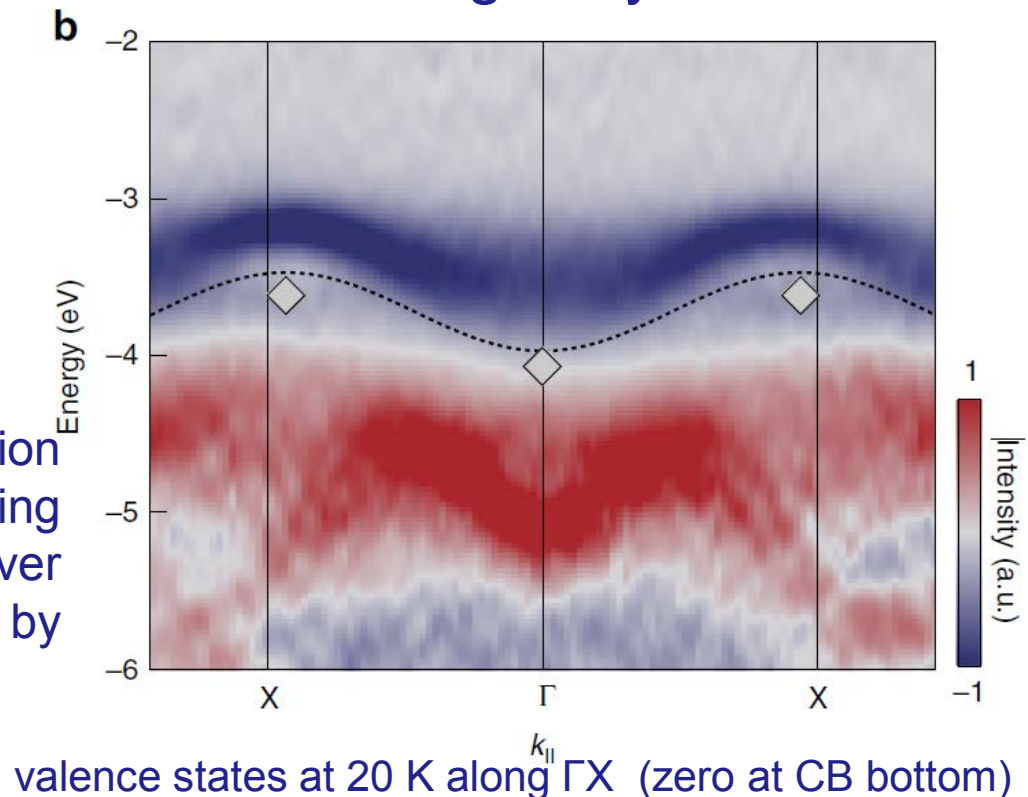


- to reveal a direct exciton, an accurate determination of the **direct electronic bandgap** is needed
- ARPES measurements on anatase TiO<sub>2</sub> single crystal (doped in a controlled manner)

X -3.47 eV

$\Gamma$  -3.97 eV

no measurable bandgap renormalization (BGR) at the  $\Gamma$  point upon doping (increased electron concentration over three orders of magnitude, confirmed by many-body perturbation theory results)



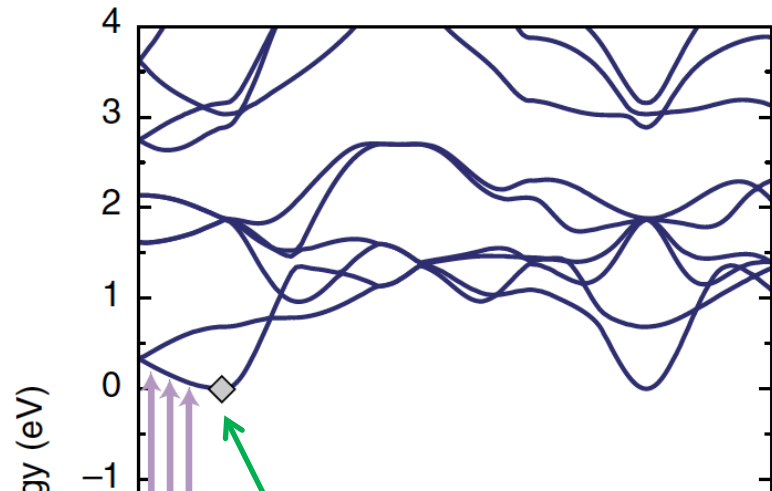
# Electronic Band Gap



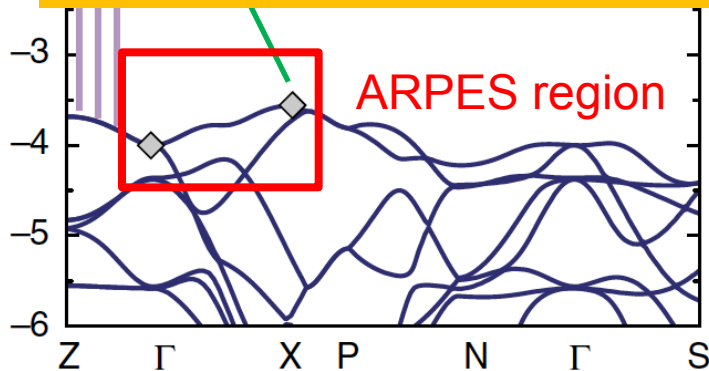
GW electronic structure  
almost **flat bands along  $\Gamma Z$**   
direction of the 3D Brillouin zone

X -3.61 eV

$\Gamma$  -4.07 eV



we got the first ingredient for a bound exciton



sources of differences:

- ~~doping~~ (slight blueshift)
  - temperature ( $E_u$ ,  $A_{2u}$  modes)
- at low T, GW calculations for main modes give negligible blueshift

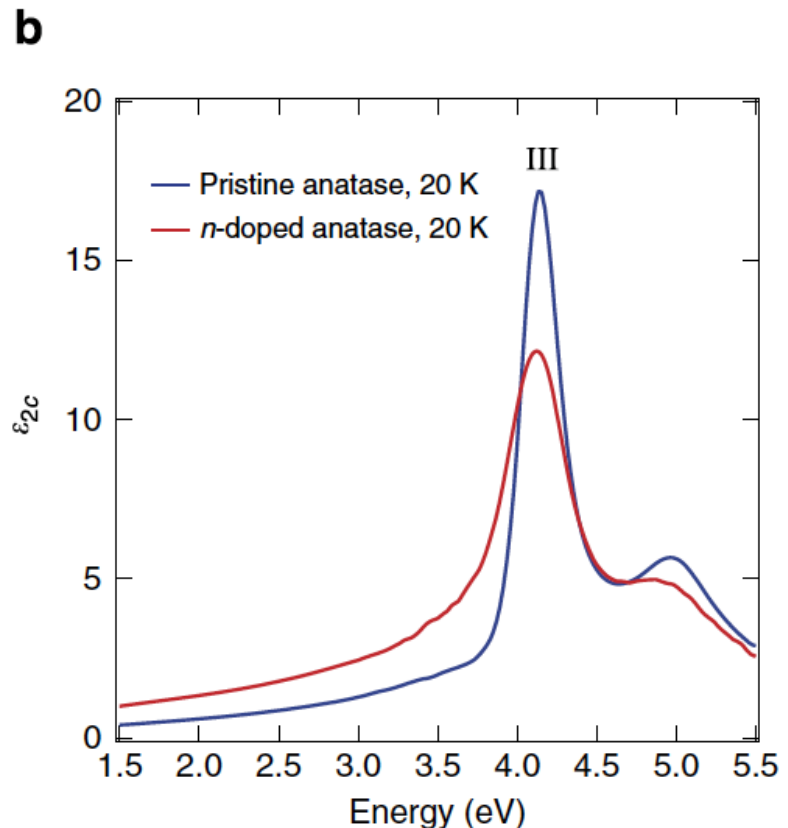
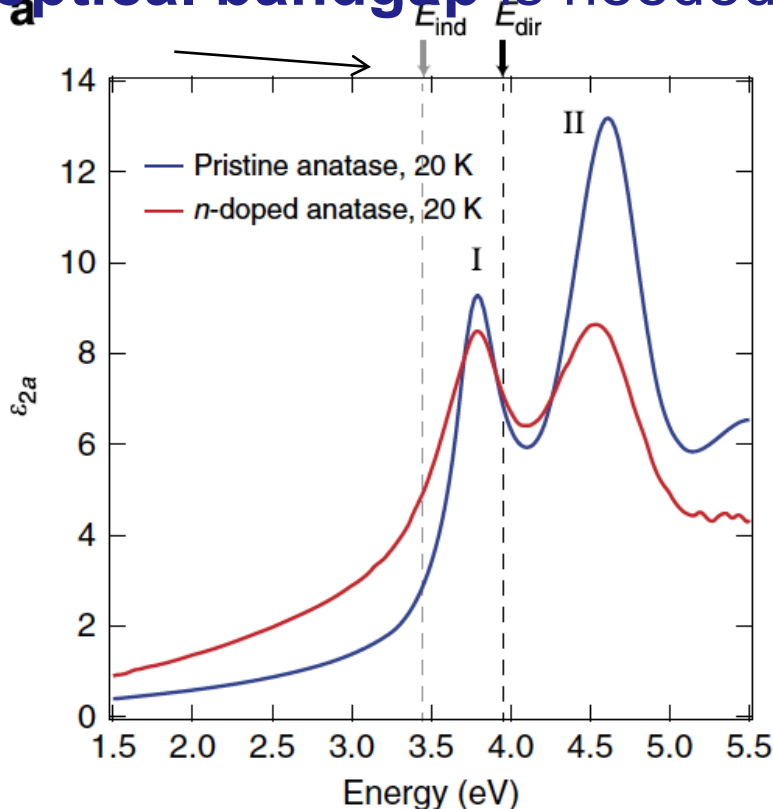
$\Gamma$  **-3.92 eV** (based on ZPR for rutile, PRB 93, 100301 (2013))

*Nat Commun* 8, 13 (2017)

# SE Optical Absorption



- to reveal a direct exciton, an accurate determination of the **optical bandgap** is needed



strong optical anisotropy for light polarised in the (001) plane and perpendicular to it  
high quality sample,  $\epsilon$  direct measure, low T  
→ HIGH QUALITY SPECTRA

# SE Optical Absorption



## pristine crystal, at 20 K

direct absorption for  $E \perp [001]$

- sharp peak at **3.79 eV (I)**
- long Urbach tail at lower energies
- broader charge excitation at 4.61 eV (II) (up to 5.00 eV)

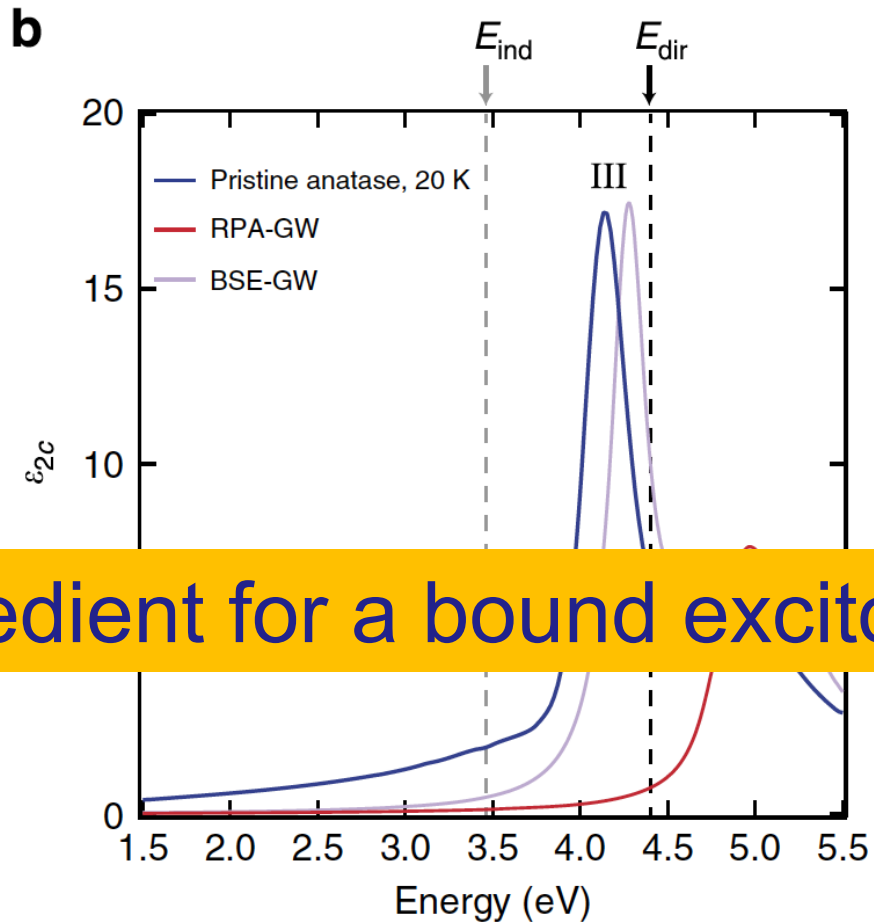
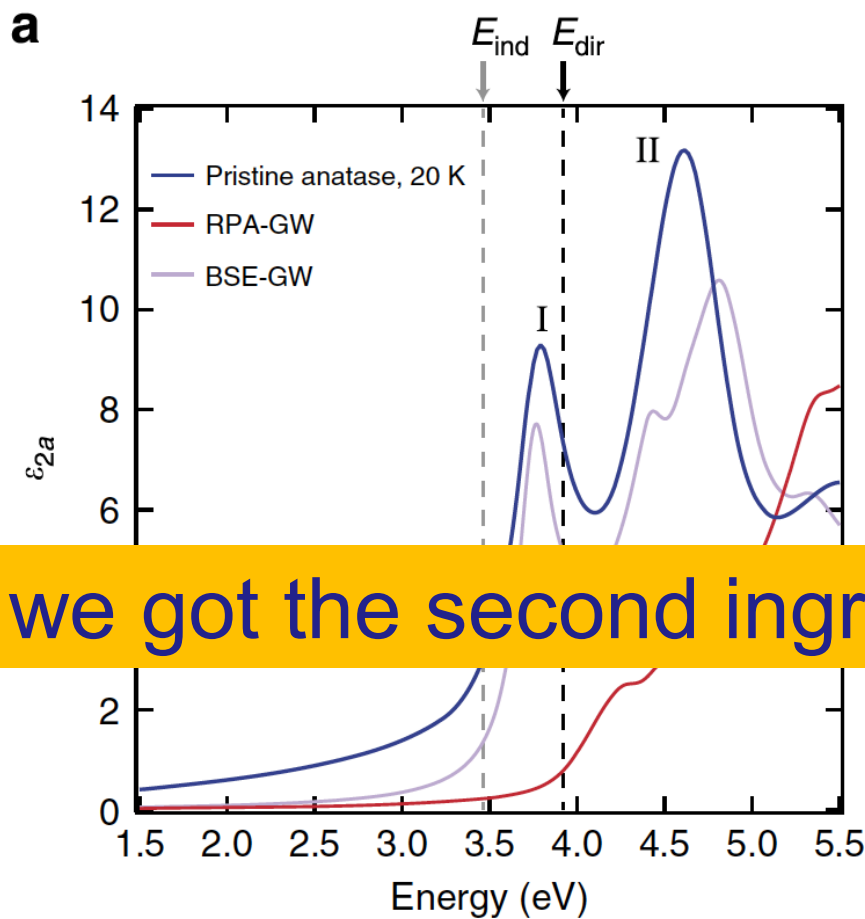
direct absorption for  $E \parallel [001]$

- peak at 4.13 eV (III) (with a shoulder at 5.00 eV)

all these excitations are still clear-cut in the **n-doped sample**

→ doping does not affect the peak (I) position (verified by GW-BSE calculations)

# Ab Initio Optical Absorption



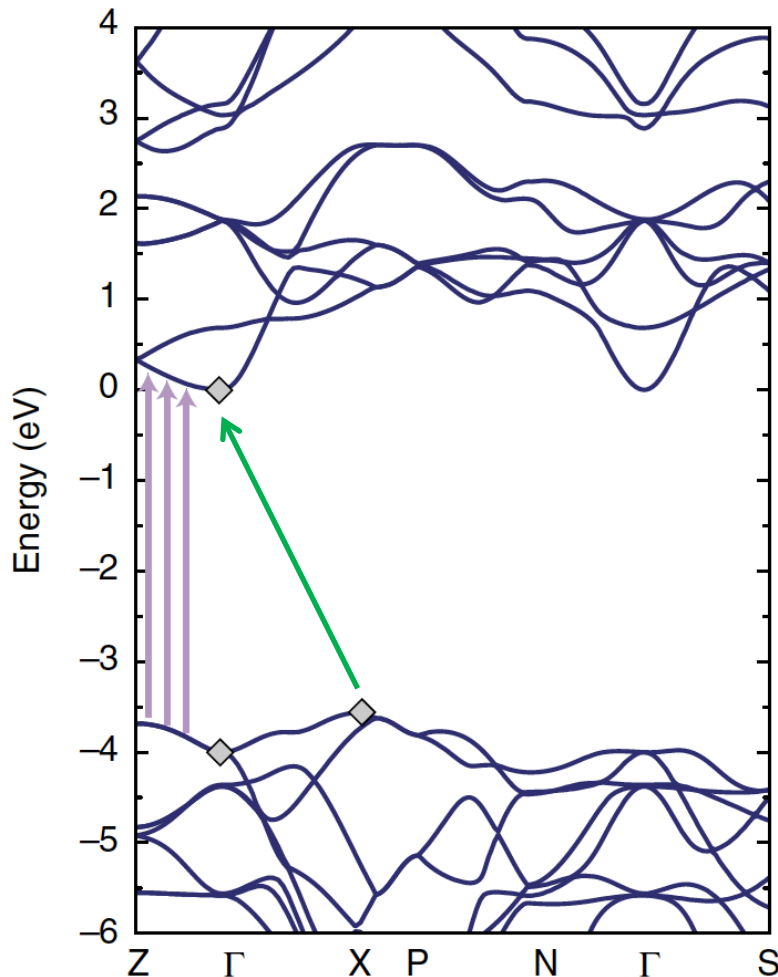
we got the second ingredient for a bound exciton

excellent agreement with exp SE

univocal assignment of peaks → exc (I) is the FIRST direct transition

→ exc (I) is used as optical gap

# what about the indirect gap?



exc (I) comes from  $\Gamma$ Z region  
VB and CB are almost parallel

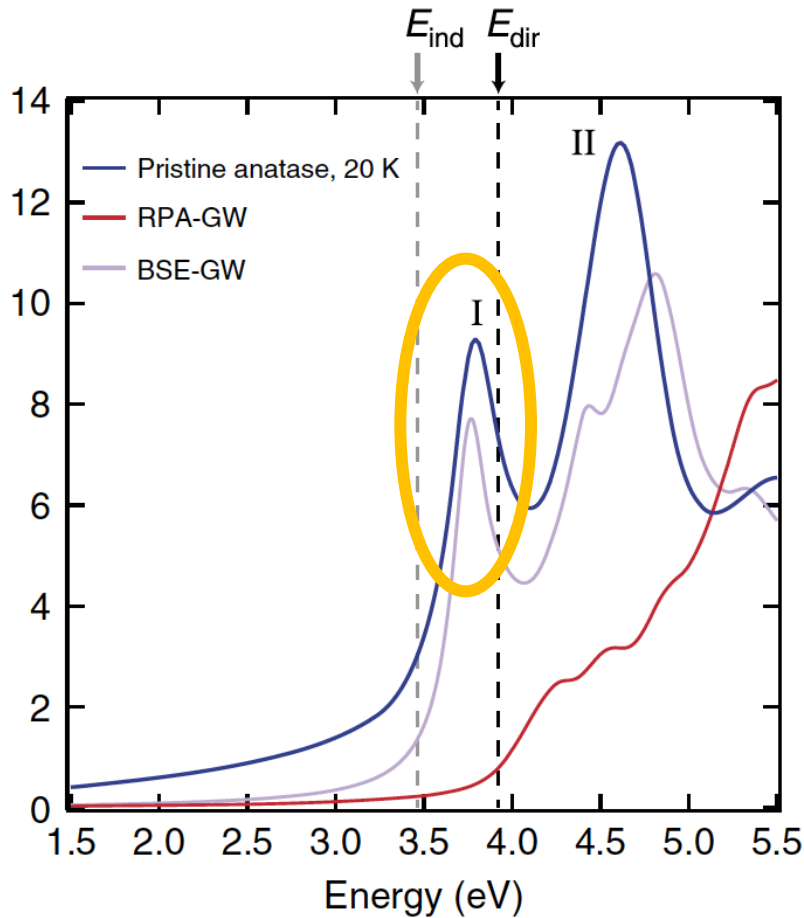
indirect gap is at X $\Gamma$

supercell calculations exclude  
contributions to exc (I) from  
indirect transitions (no resonant)

# PES + SE + (GW-BSE) =



**a**



EB exp. (20 K) = 180 meV

EB th. (frozen atoms) = 160 meV

*again, more questions than answers....*

**is exciton (I) stable at RT?  
why it is so strongly bound?**

is the exciton (I) delocalized, or not,  
in the crystal? why?

is the exciton (I) present, and how, in  
real samples (e.g. NPs)?

what to do with this 'bound' exciton?

**bound exciton in anatase  
EB surprisingly large!**



## is exciton (I) stable at RT?

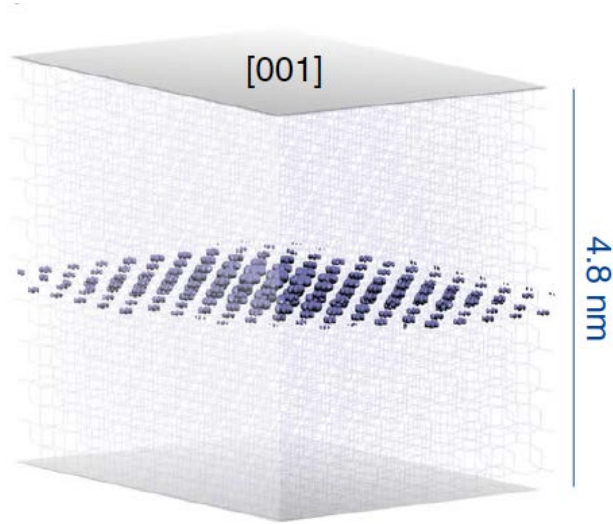
el-ph coupling effects on electronic and optical gap:  
an overall blueshift is observed (experimental - computational)  
→ at RT the exciton(I) is still bound

## why it is so strongly bound?

- $\epsilon$  (anisotropic, depending on both energy and momentum) and **electronic structure** (parallel bands along  $\Gamma Z$ ) give the overall behaviour of excitons binding
- intermediate binding energy: Wannier-Mott / Frenkel exciton

SrTiO<sub>3</sub>: EB 220 meV (Phys B 407, 2632 (2012), PRB 87, 235102 (2013))

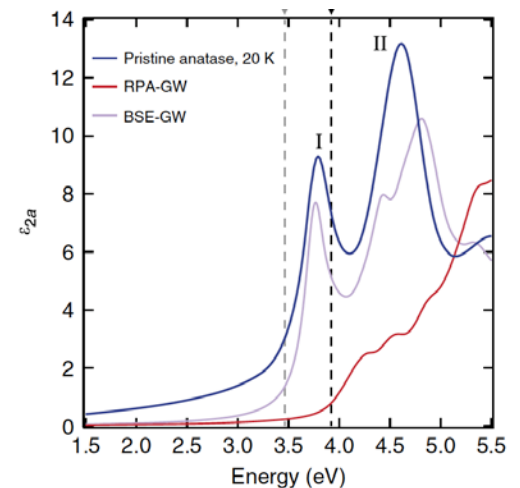
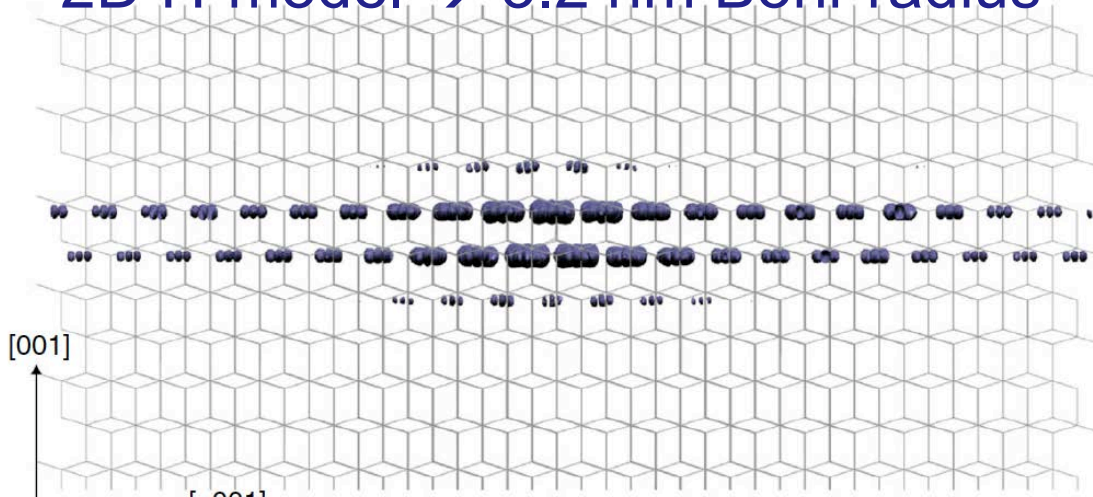
# Localized Exciton (I)



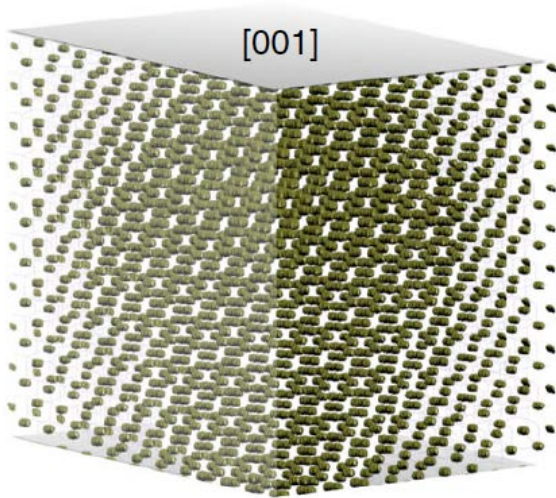
2D exciton in a 3D crystal:  
 similar to 2D materials!  
 (MoS<sub>2</sub> ML, PRL 111, 216805 (2013))  
 not observed in rutile TiO<sub>2</sub> and SrTiO<sub>3</sub>

due to crystal & wavefunction symmetries (octahedra packing → along  $\Gamma Z$ , VB and CB are almost flat)

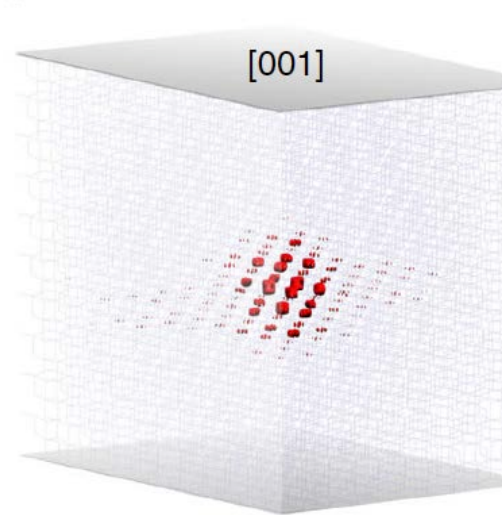
2D H-model → 3.2 nm Bohr radius



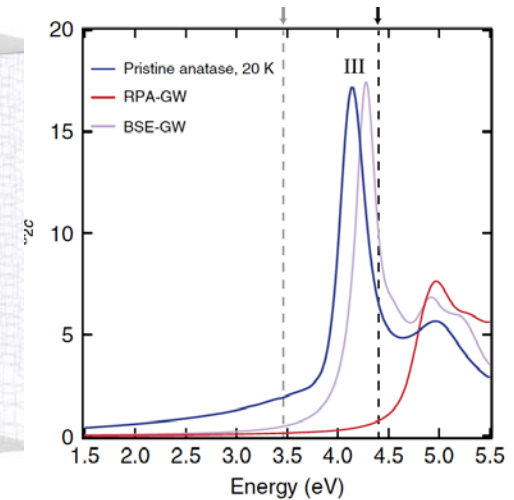
# Resonant and Mixed Excitons



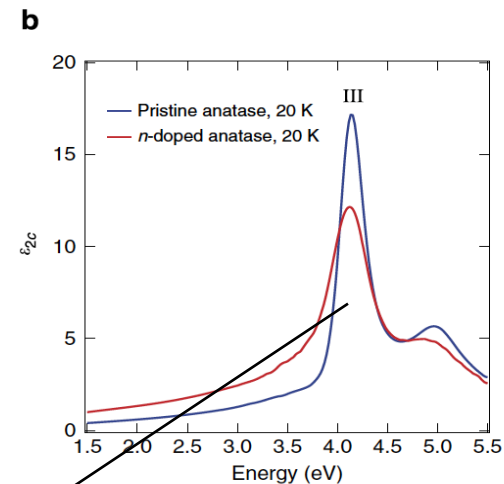
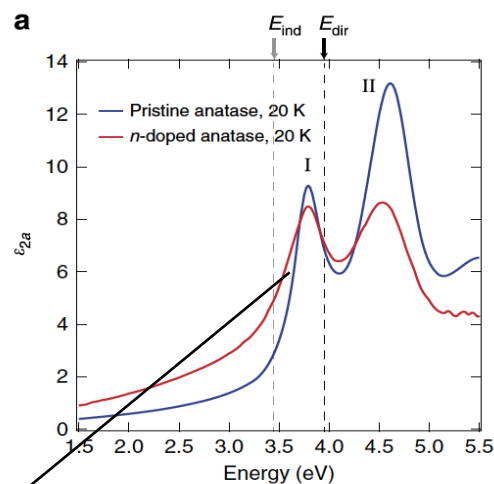
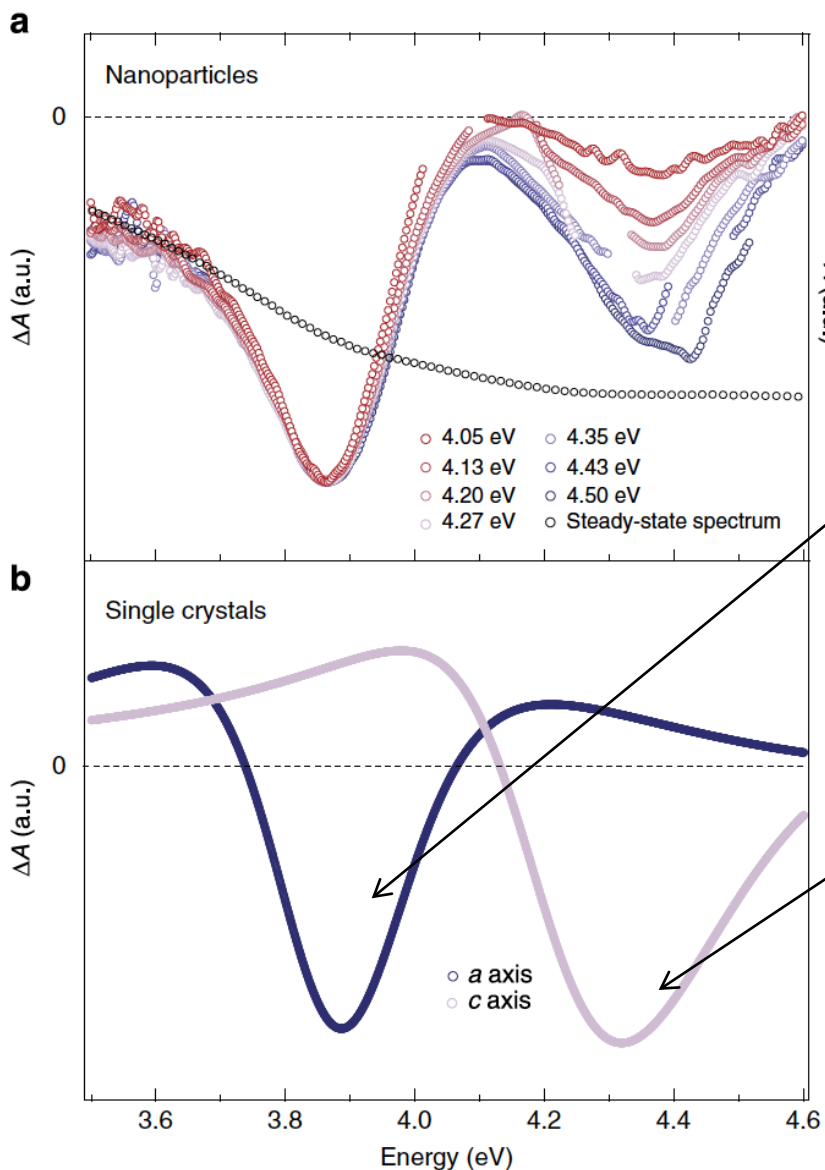
exciton (II):  
resonant  
onset at the GW  
continuum rise



exciton (III):  
resonant & localized  
3D H-model (localized part)  
→ 0.27 nm Bohr radius  
 $E_B = 150$  meV



# Excitons in NanoParticles

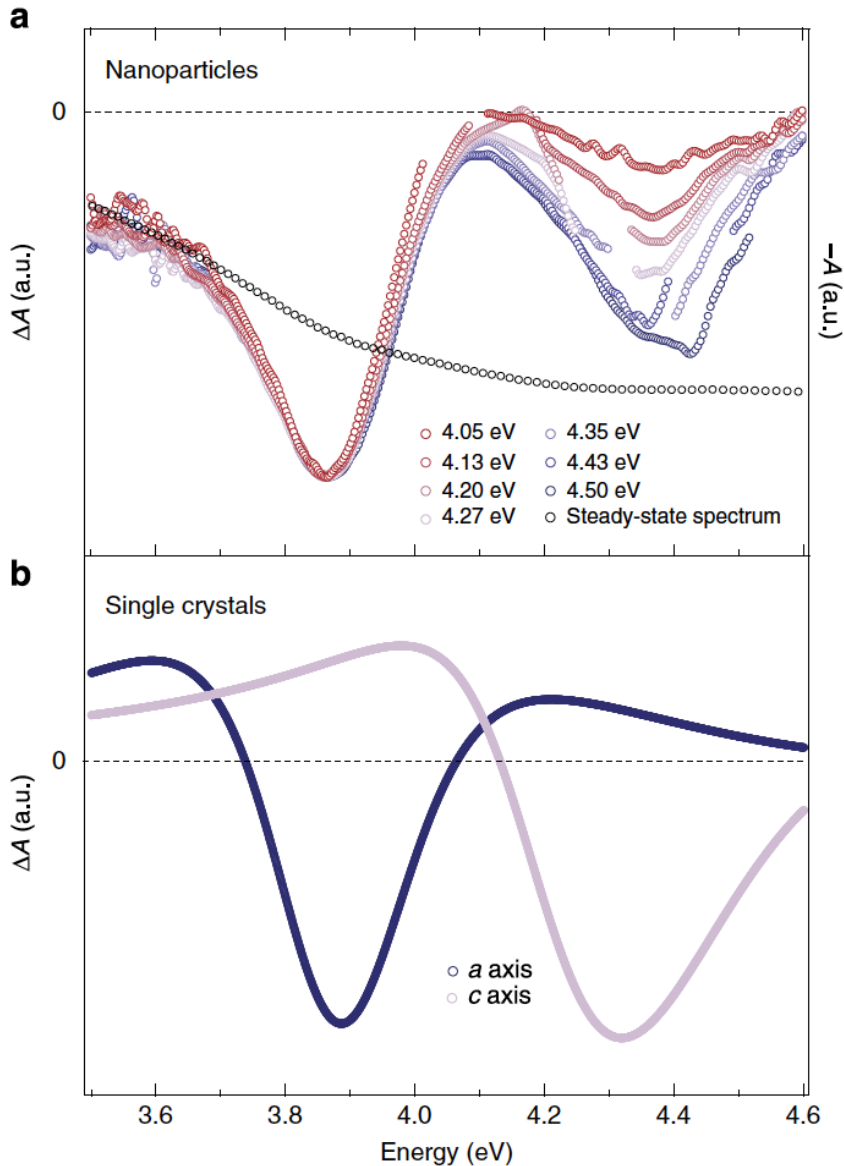


colloidal NPs (25 nm radius)  
doped single crystal

ultrafast two-dimensional  
deep-ultraviolet spectroscopy

only localized excitons appear

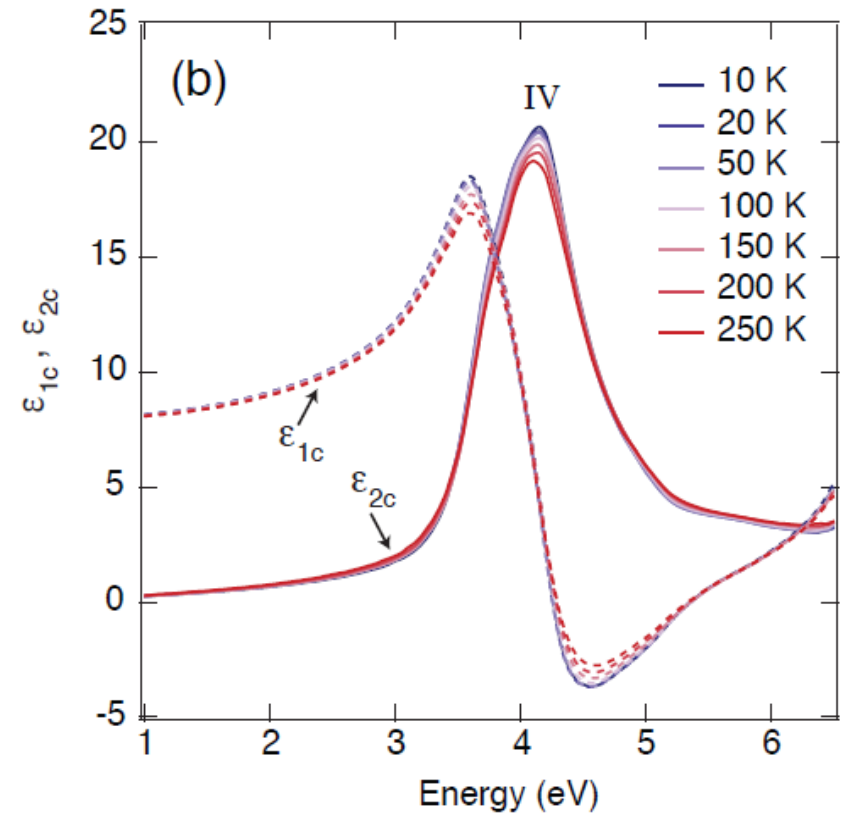
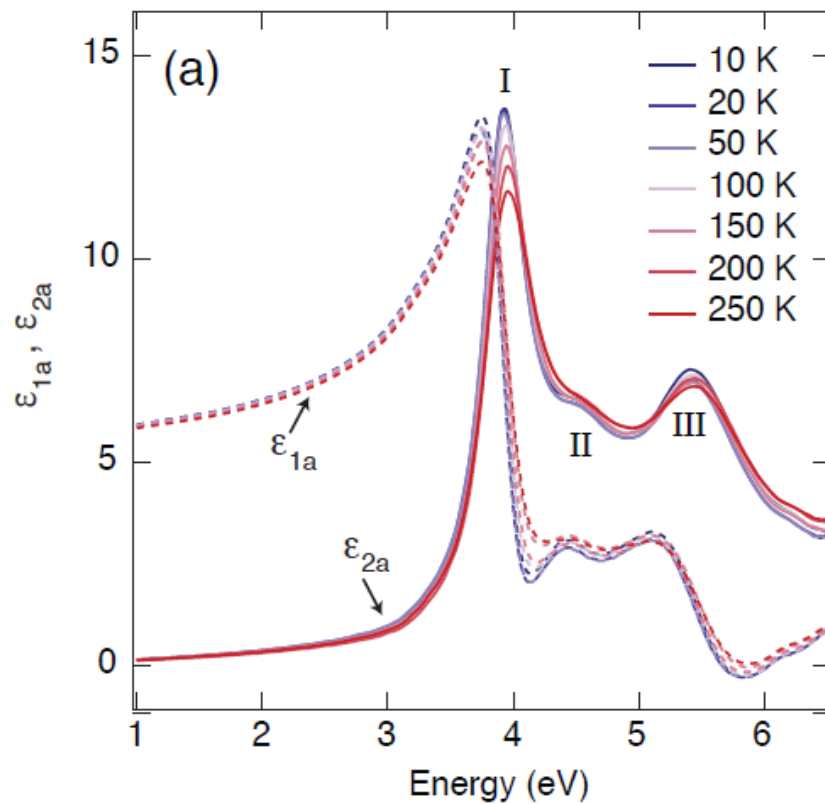
# Excitons in NanoParticles



same elementary localized and bound excitations are observed in pure crystals and in defect-rich samples (doped single crystals and nanoparticles)

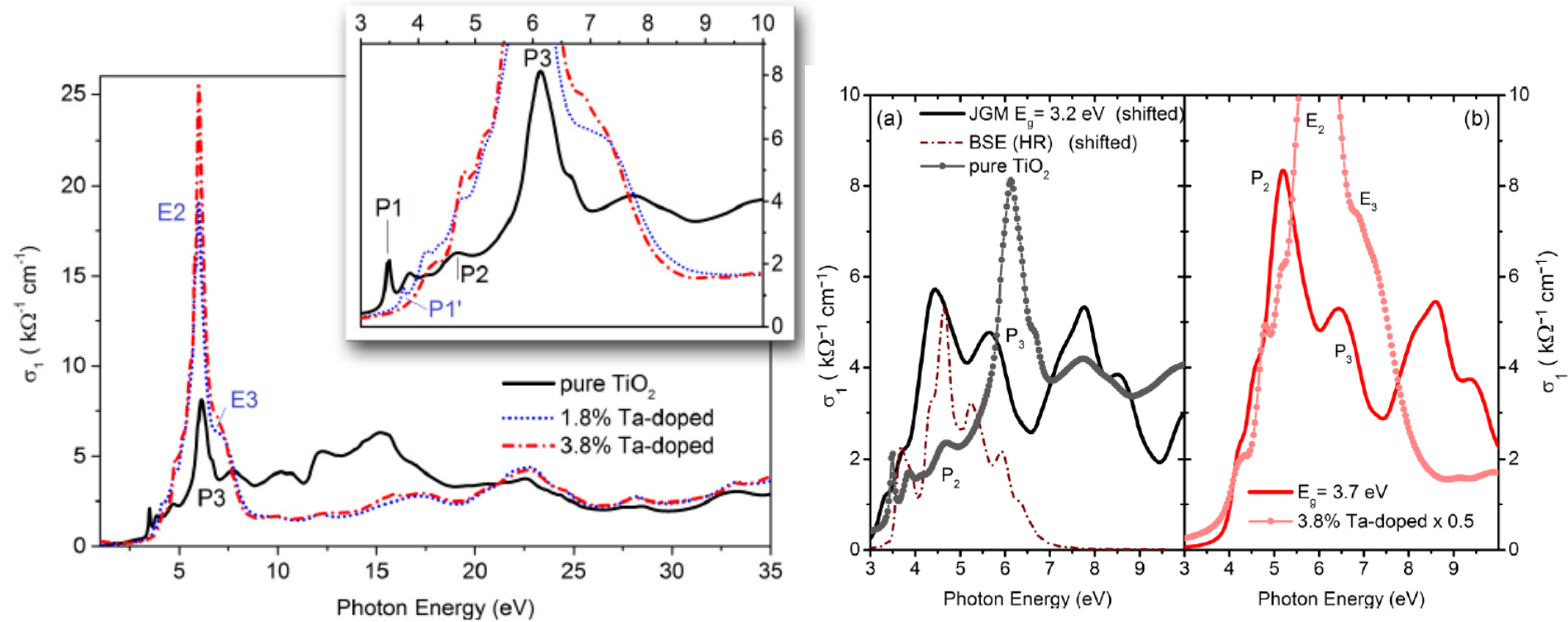
# Excitons in Rutile

anomalous blueshift in rutile optical spectra with temperature  
el-ph coupling at work



# Strong Correlation in Doped Anatase

anomalous resonant excitonic absorption induced by Ta doping



Ta-f electrons induce a transition, with a band gap opening, similar to strongly correlated materials (cuprates)

# Conclusions



- TiO<sub>2</sub> is not a 'simple' materials: it hides peculiar properties
- advanced experimental and theoretical techniques provide a unified and coherent description of a **bound localized 2D** exciton in anatase single **crystals**, pure and defected, and in more applicative samples as **colloidal NPs**
- a **3D localized** exciton is also observed at higher energies and different polarization
- anomalous T-effects in both rutile and anatase excitons
- anomalous doping-effects in anatase
- doping, defects, el-ph may alter the optical response
- how to tune and optimize excitons behaviour via doping, strain, .



# Aknowledgments



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