

# Small Scale experiments for fundamental physics

ICTP Summer School on Particle  
Physics, June 12-15

Part 2

# Syllabus

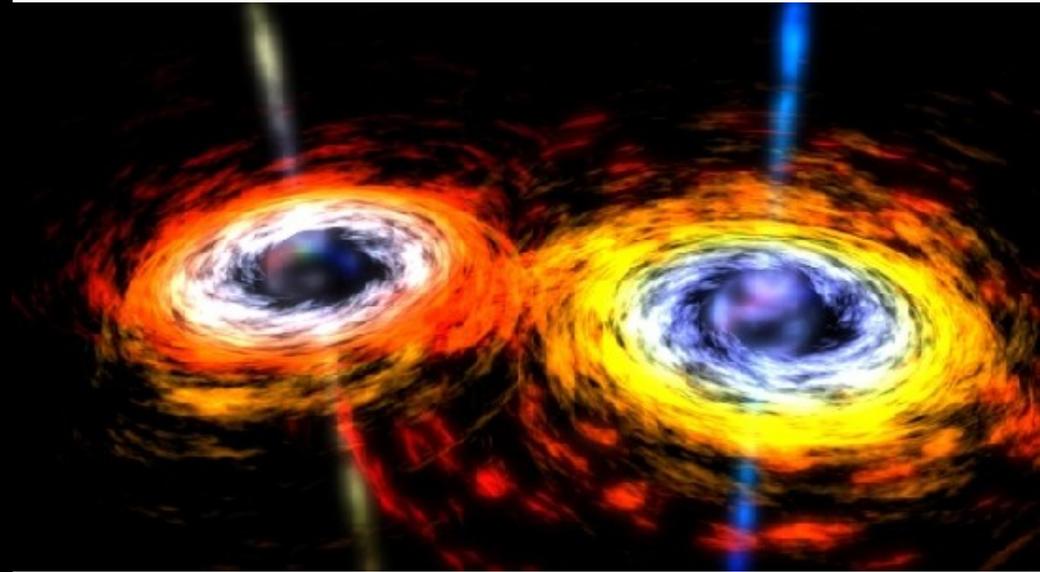
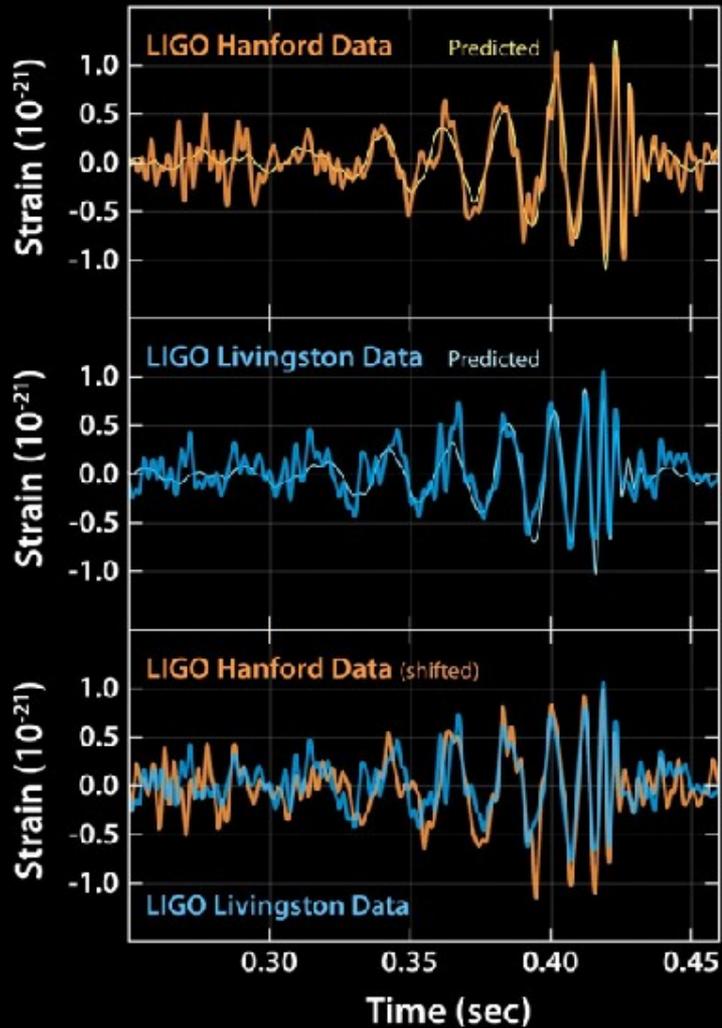
- Introduction
- New (scalar) forces
- Gravitational Waves and Ultralight Dark Matter
- New (spin-dependent) forces  
(relation to axions, EDMS, Cosmic DM experiments)

# Outline for Lectures

- Lecture 2 –
  - Gravitational waves
    - New Techniques:
      - Levitated sensors
      - Atom interferometry
    - Ultralight scalar field dark matter

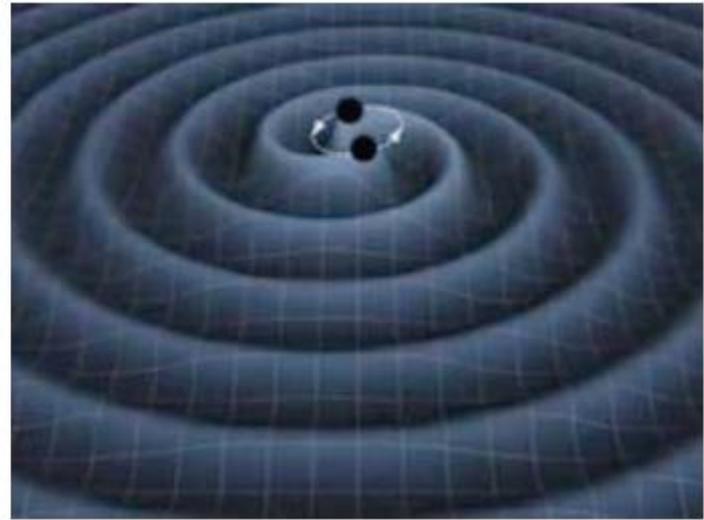
# Gravitational Waves

Sep 14, 2015



B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration)  
Phys. Rev. Lett. **116**, 061102 (2016).

# Gravitational waves



- Several BH events now discovered by Advanced LIGO!
- Sources:
  - Inspirals of astrophysical objects
  - Inflation, Phase transitions, etc.

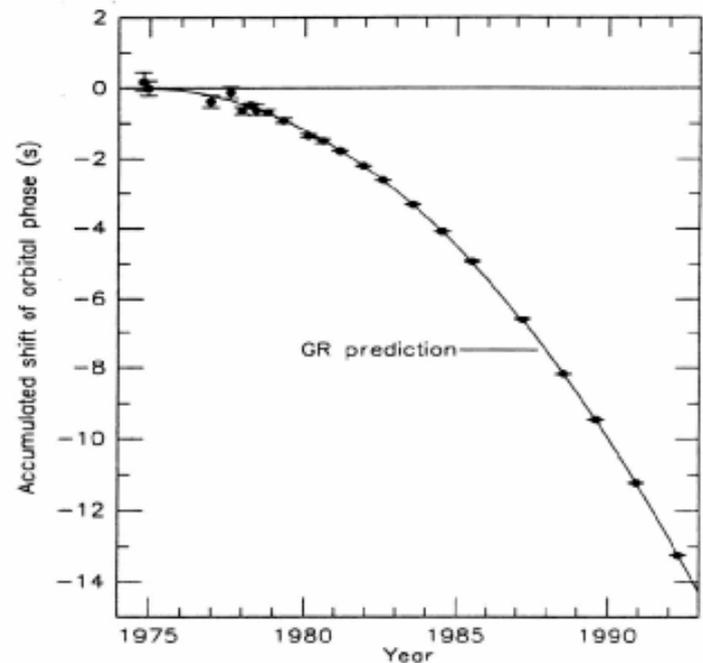
# Indirect evidence: Hulse Taylor Binary

- Binary system of neutron stars emits gravitational waves

Rapidly spinning pulsar (17Hz)  
orbits around another star with 8h period

Period speeds up  $\sim 14$ s over 1975-1993

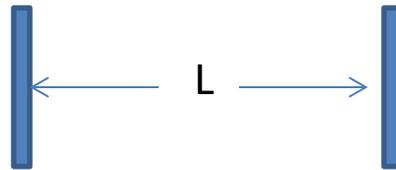
Nobel Prize 1993 (Hulse, Taylor)



J. H. Taylor, L. A. Fowler & P. M. McCulloch  
Nature 277, 437-440 doi:10.1038/277437a0

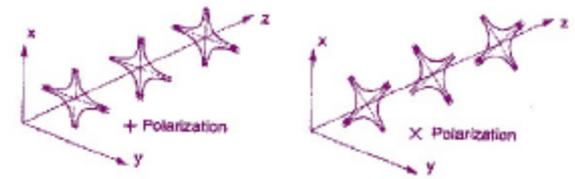
# Gravitational Waves

- Stretch and squeeze the space between test masses



- Strain  $h = \Delta L/L$

- 2 polarizations (+ and x)



Contrast with EM dipole radiation:



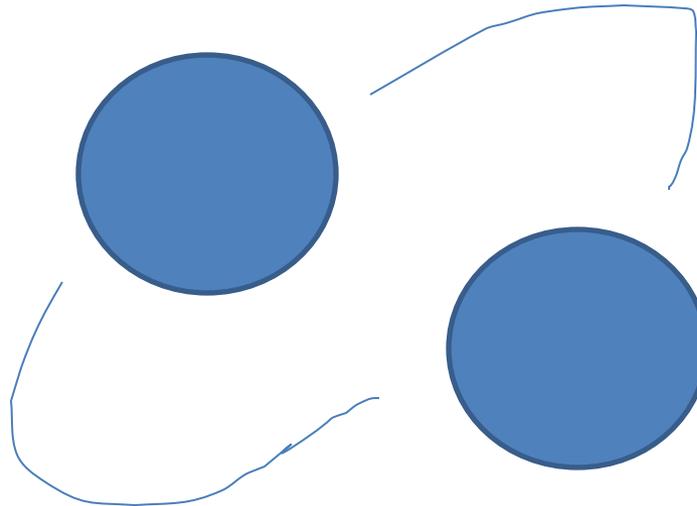
# Sources of Gravitational Radiation

- Example: Neutron star binary

Accelerating charge – EM radiation (dipole)

Accelerating mass – Gravitational radiation (quadrupole)

e.g. rotating dumbbells



e.g.  $h \sim 10^{-21}$

$f \sim 400 \text{ Hz}$

# Resonant bar detectors

Bar driven into resonant oscillation by passing GW

J. Weber ([1969](#))



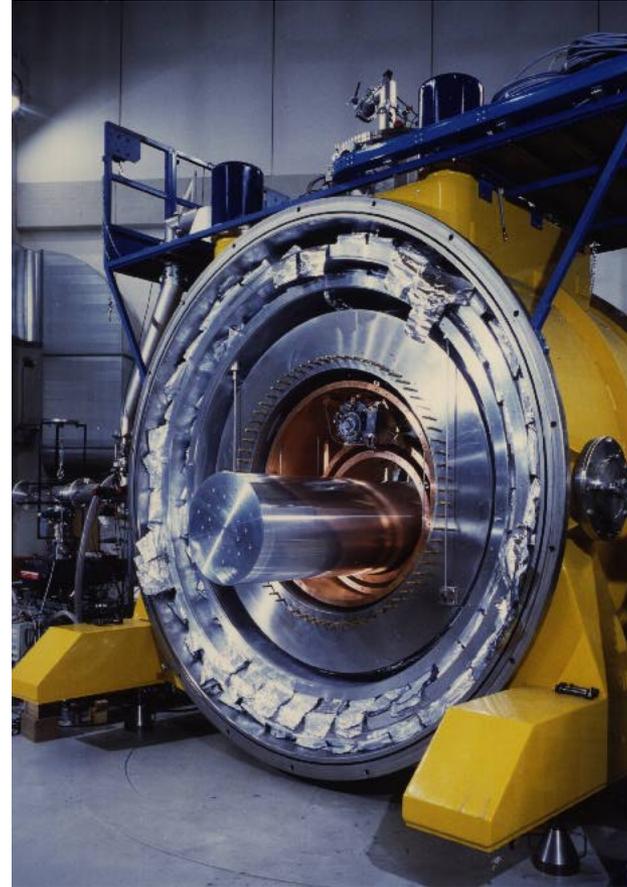
$$\omega_0 = 2\pi(1.6\text{kHz})$$

Aluminum bar

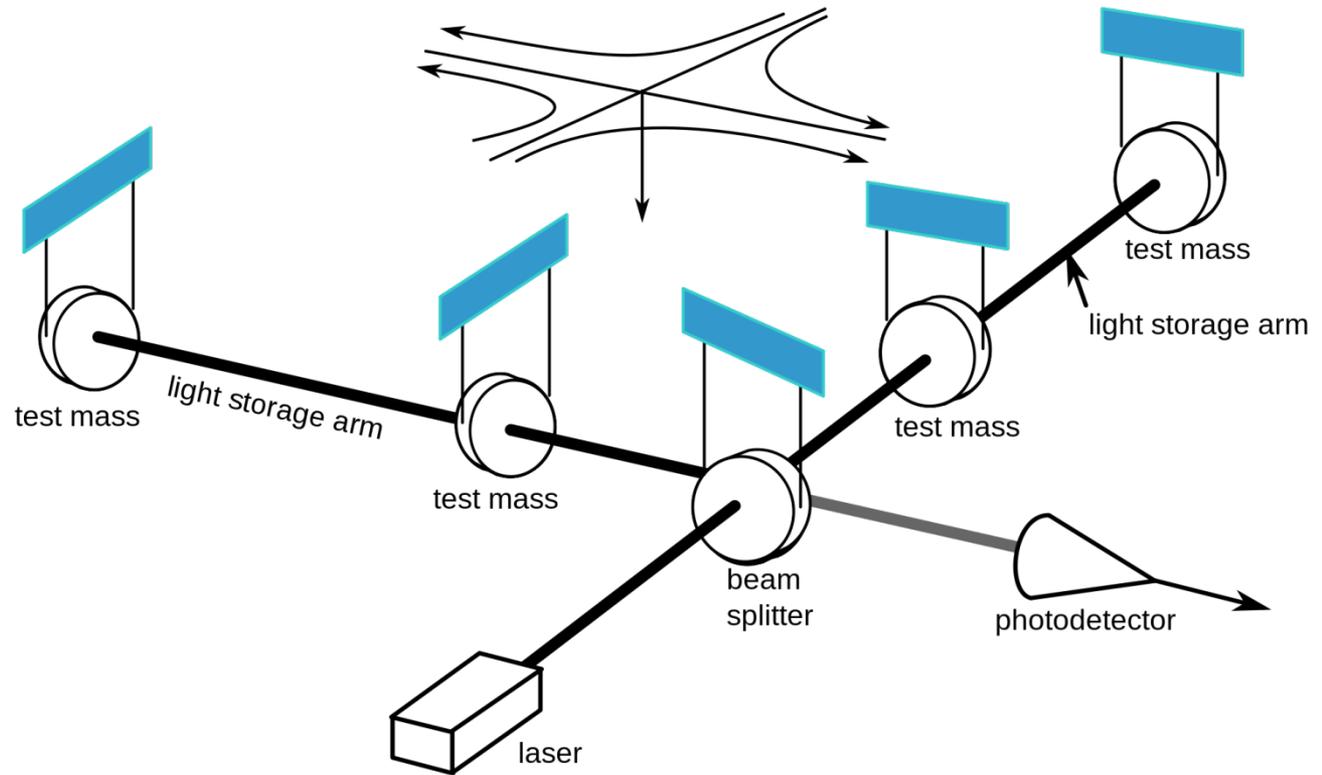
# Resonant bar detectors

AURIGA experiment (Padova, Italy)

- 2.3 tons of Aluminum, 3 m long
- 0.1 K dilution fridge
- $Q=4 \times 10^6$
- Resonant frequency 900 Hz
- Capacitive measurement
- $h \sim 10^{-21} / (\text{Hz})^{1/2}$



# Interferometer detectors



# Global network of GW detectors



# Interferometer detectors

Seismic motion --  
ground motion due to  
natural and  
anthropogenic  
sources

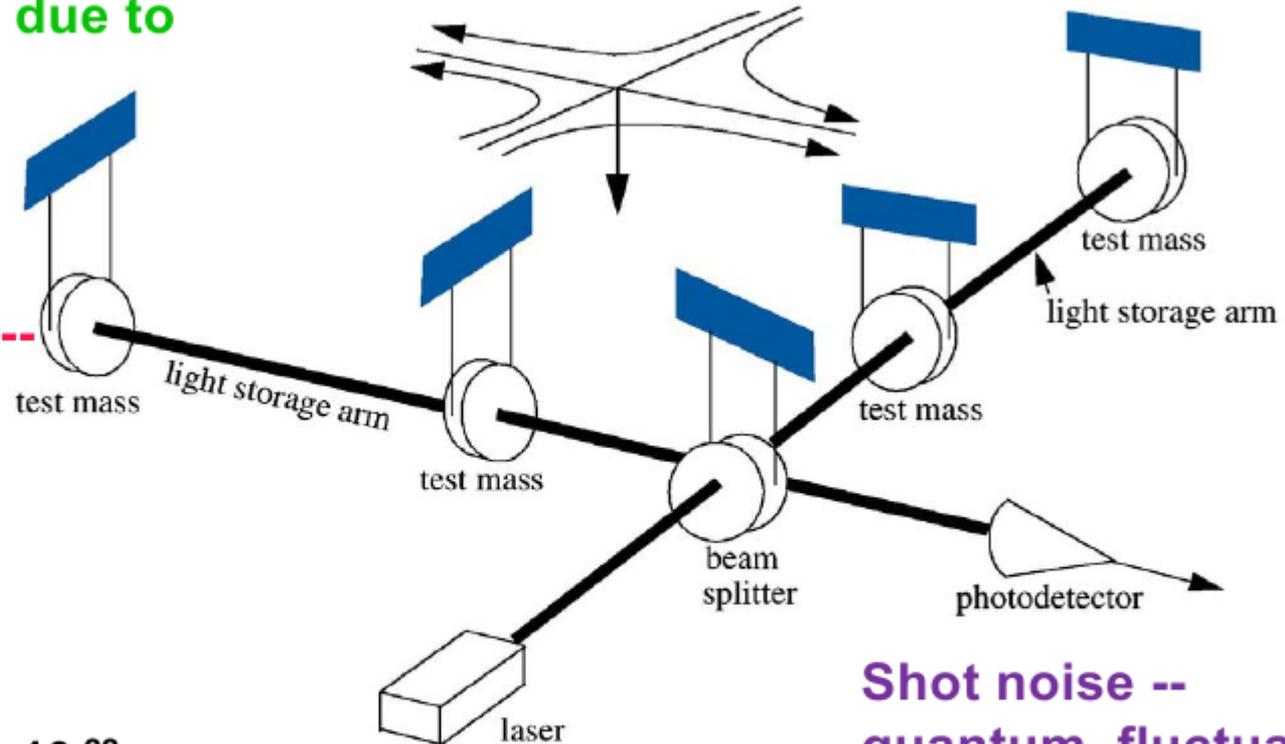
Thermal noise --  
vibrations due  
to finite  
temperature

$$h = \Delta L / L$$

want to get  $h \leq 10^{-22}$ ;  
can build  $L = 4$  km;  
must measure

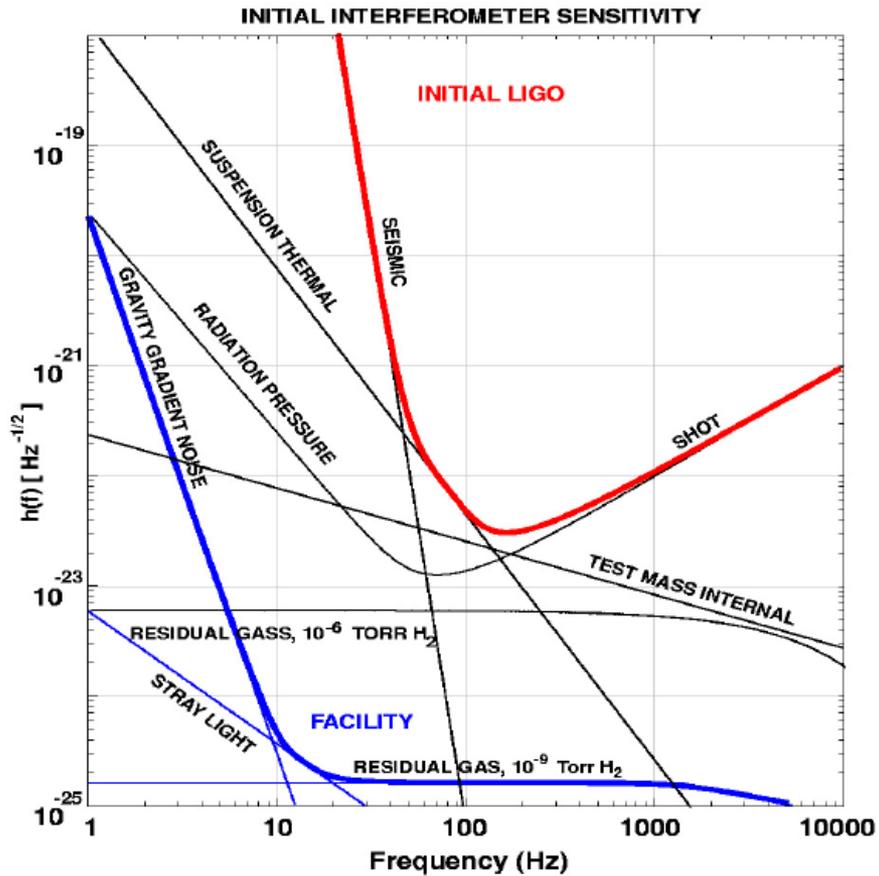
$$\Delta L = h L \leq 4 \times 10^{-19} \text{ m}$$

AJW, LIGO SURF, 6/16/06

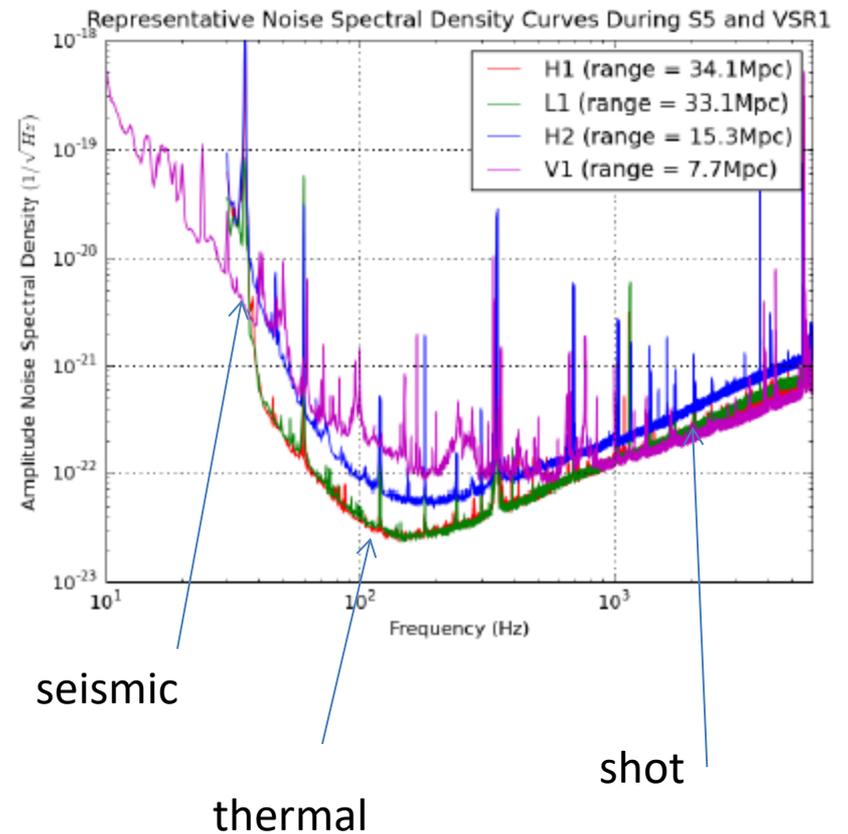
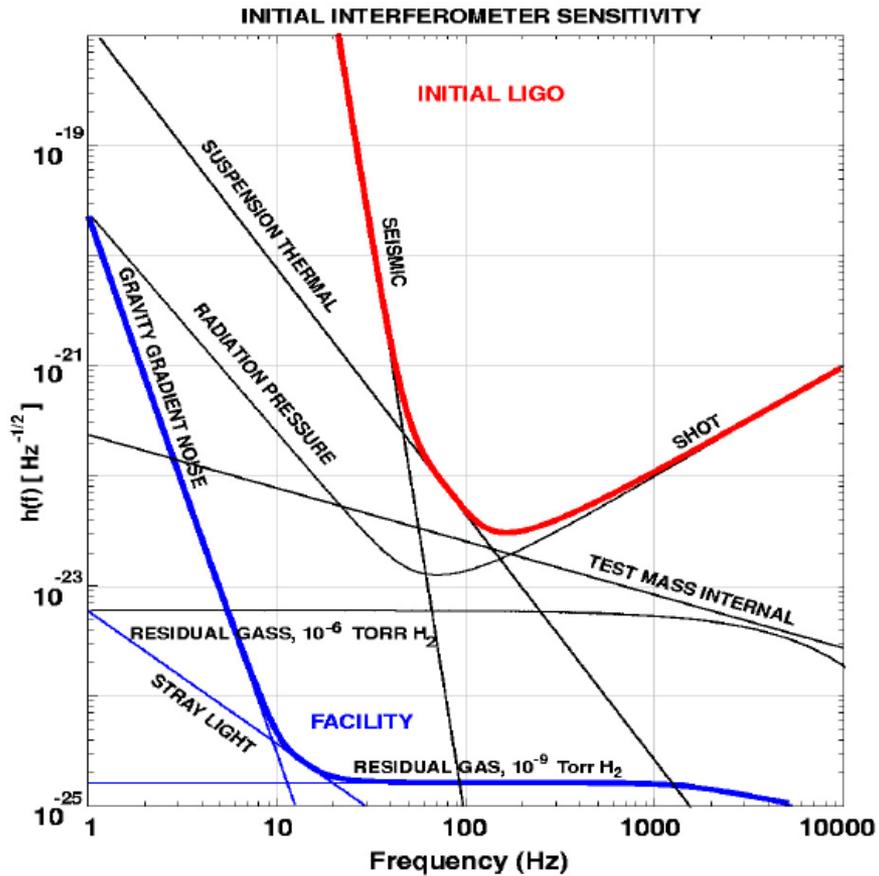


Shot noise --  
quantum fluctuations  
in the number of  
photons detected

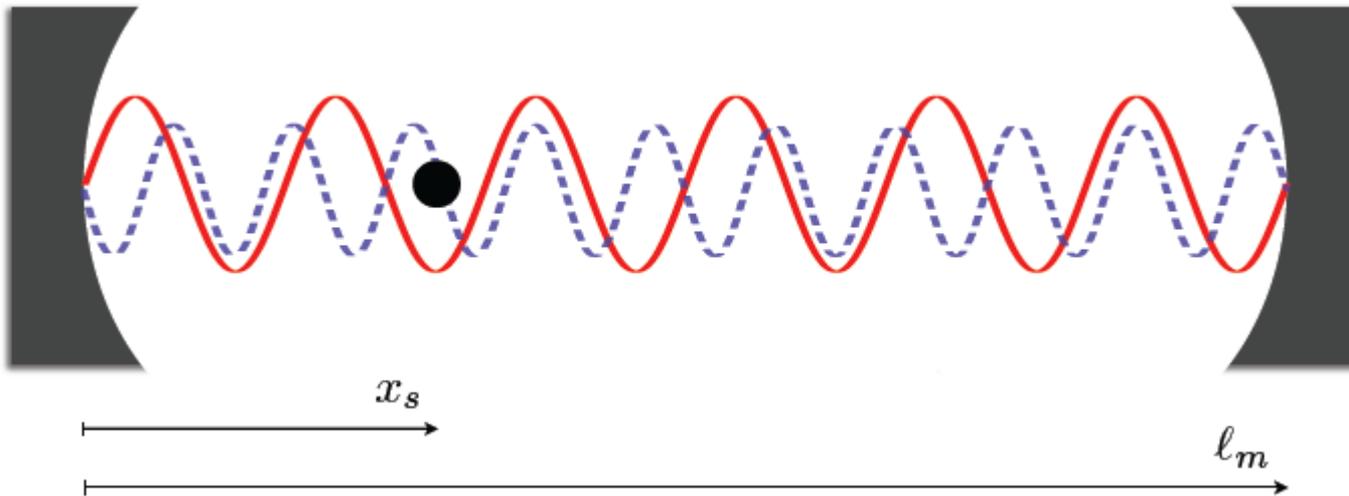
# Sensitivity of LIGO



# Sensitivity of LIGO

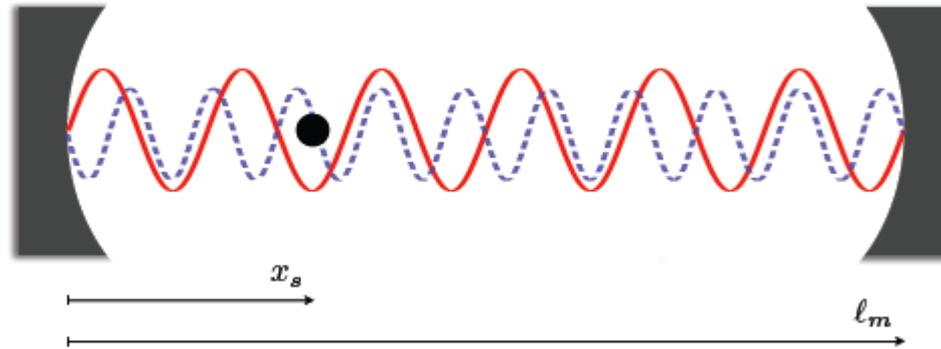


# Gravitational Wave Detection with levitated optomechanics



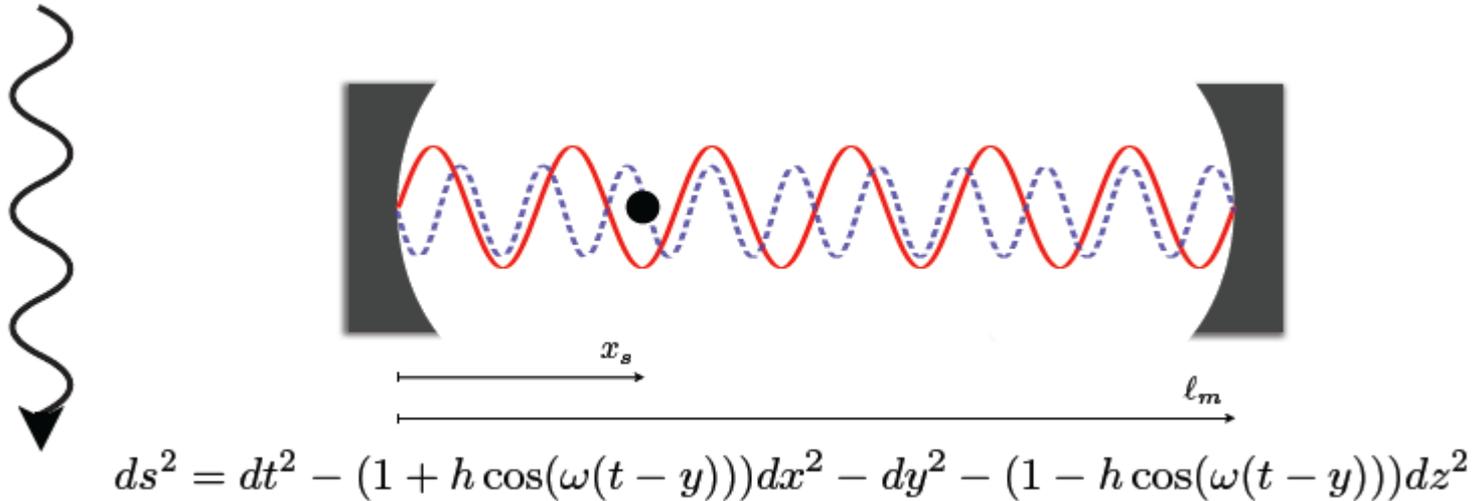
- Fused silica sphere ( $r = 150\text{nm}$ ) or disc ( $t = 500\text{nm}$ ,  $r = 75\ \mu\text{m}$ )  
In an optical cavity of size 10-100 m
- One laser to **trap**, one to **cool** and measure sensor position

# Gravitational Wave Detection



$$ds^2 = dt^2 - (1 + h \cos(\omega(t - y)))dx^2 - dy^2 - (1 - h \cos(\omega(t - y)))dz^2$$

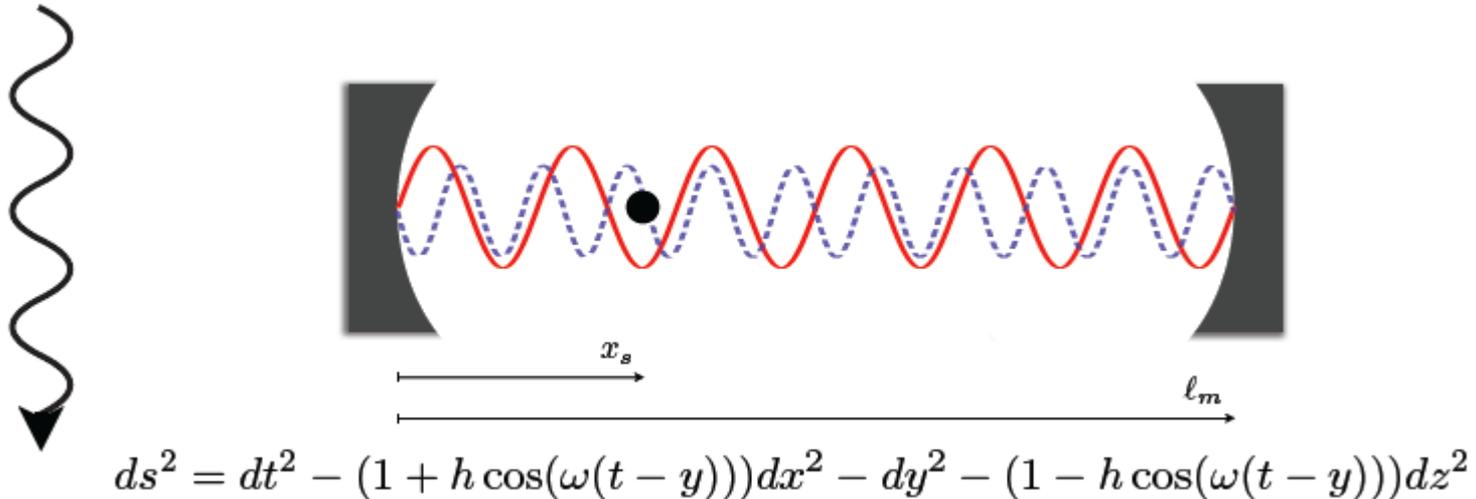
# Gravitational Wave Detection



Gravitational wave changes the physical distance between the end mirrors:

$$L = \ell_m \left[ 1 + \frac{1}{2} h \cos(\omega t) \right]$$

# Gravitational Wave Detection



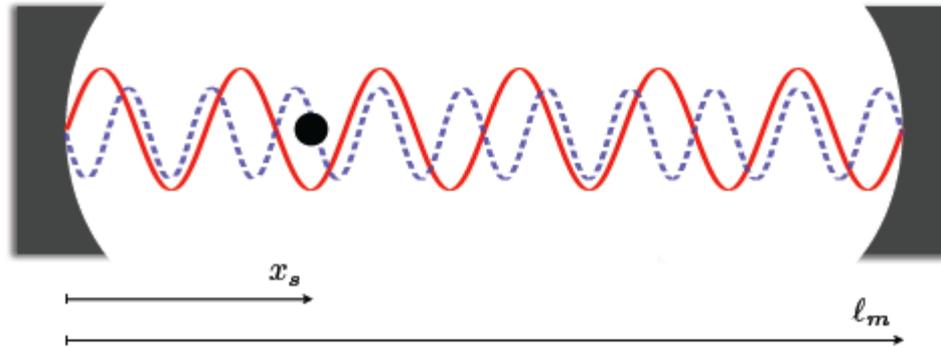
Gravitational wave changes the physical distance between the end mirrors:

$$L = \ell_m \left[ 1 + \frac{1}{2} h \cos(\omega t) \right]$$

and the distance from the input mirror to the sensor

$$X_s = x_s \left[ 1 + \frac{1}{2} h \cos(\omega t) \right]$$

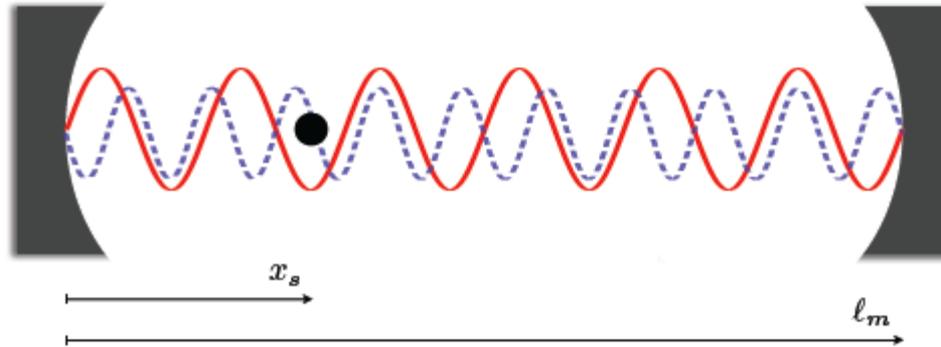
# Gravitational Wave Detection



- Moving end mirror displaces physical position of anti-node relative to sensor

Anti-node shift (LL gauge) : 
$$\delta X_{anti-node} = \frac{1}{2} \ell_m h$$

# Gravitational Wave Detection



- Moving end mirror displaces physical position of anti-node relative to sensor

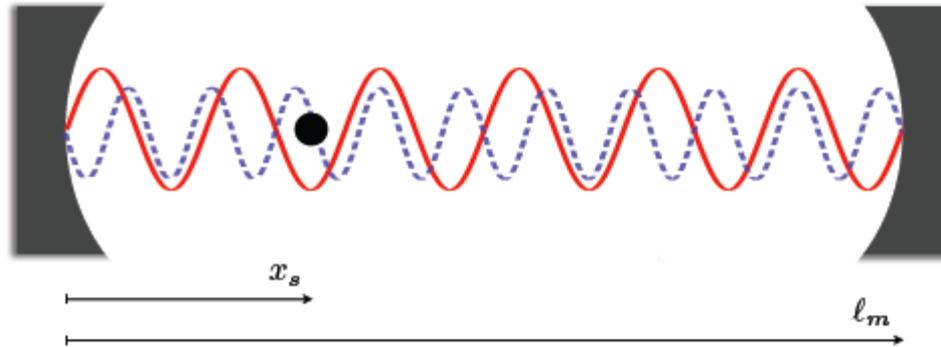
Anti-node shift (LL gauge) : 
$$\delta X_{anti-node} = \frac{1}{2} \ell_m h$$

Sphere shift (LL gauge) : 
$$\delta X_s = \frac{1}{2} x_s h$$

- Sensor position changes with respect to trap minimum:

$$\Delta X = \frac{1}{2} (x_s - \ell_m) h + O(h^2)$$

# Gravitational Wave Detection



$$\Delta X = \frac{1}{2}(x_s - \ell_m)h + O(h^2)$$

$$F_{gw} = -\frac{m\omega_{gw}^2}{2}(x_s - \ell_m)h_0 \cos(\omega_{gw}t + \phi)$$

- Laser intensity changed to match trap frequency to GW frequency
- For a 100m cavity,  $h \sim 10^{-22} \text{ Hz}^{-1/2}$  at high frequency
- Limited by thermal noise in sensor (not laser shot noise)

# Tunable resonant detector

- Like Weber bar detectors with wide tunability

J. Weber ([1969](#))



$$\omega_0 = 2\pi(1.6\text{kHz})$$

Aluminum bar

# Thermal-noise limited strain sensitivity

Gas damping

$$h_{\min} = \frac{4}{\omega_0^2 l_m} \sqrt{\frac{k_B T_{\text{eff}} \gamma_g b}{m}}$$


# Thermal-noise limited strain sensitivity

$$h_{\min} = \frac{4}{\omega_0^2 l_m} \sqrt{\frac{k_B T_{\text{eff}} \gamma_g b}{m} \left( 1 + \frac{\gamma_{sc} + R_+}{n_i \gamma_g} \right)}$$

Gas damping

Photon-recoil heating

Limit from laser cooling

# Thermal-noise limited strain sensitivity

Gas damping

Photon-recoil heating

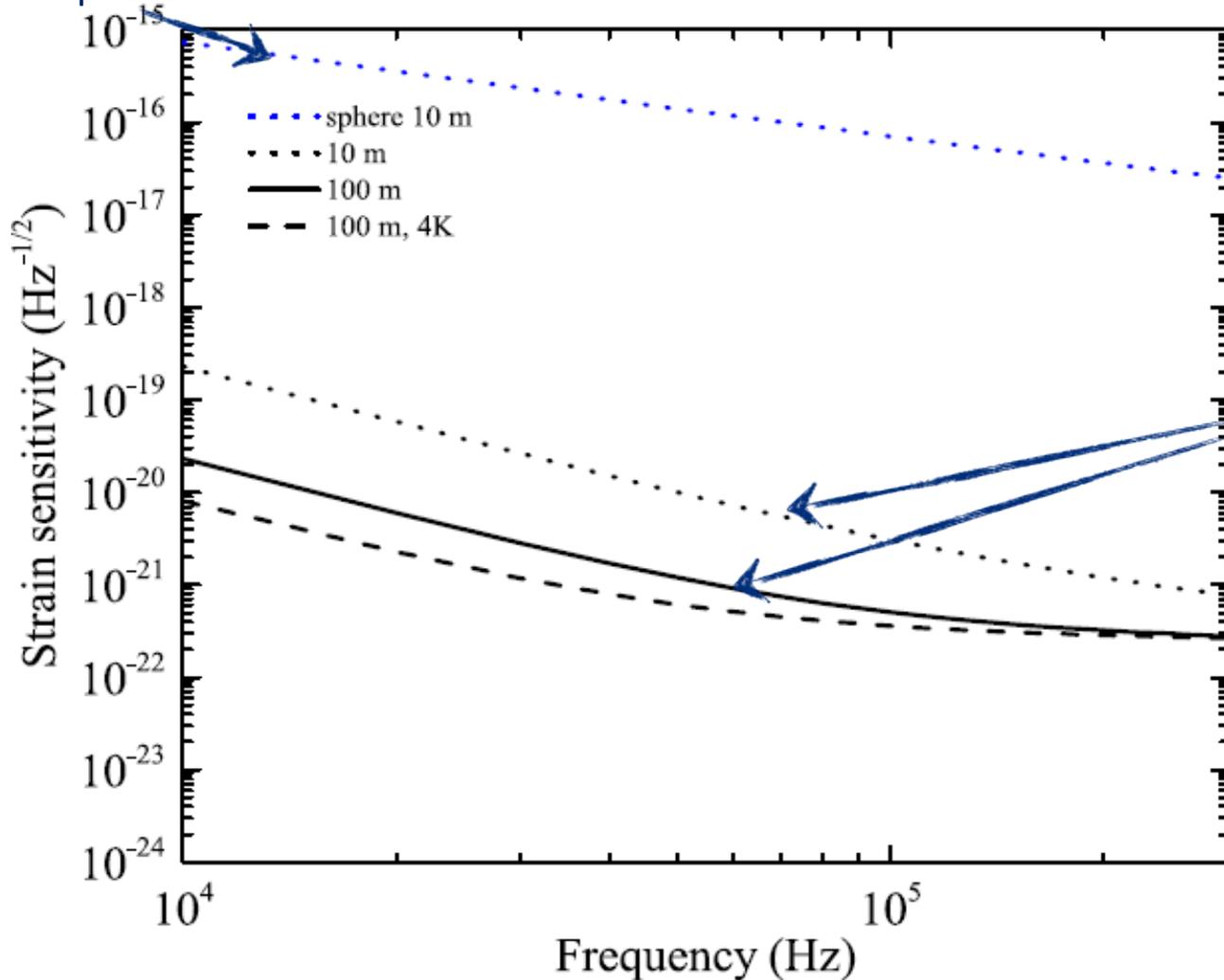
Limit from laser cooling

$$h_{\min} = \frac{4}{\omega_0^2 l_m} \sqrt{\frac{k_B T_{\text{eff}} \gamma_g b}{m} \left( 1 + \frac{\gamma_{sc} + R_+}{n_i \gamma_g} \right) H(\omega_0)}$$
$$H(\omega_0) = \sqrt{1 + \left( \frac{2F}{\pi} \right)^2 \sin^2(\omega_0 l_m / c)}$$

Cavity suppresses response above pole

# GW Strain Sensitivity

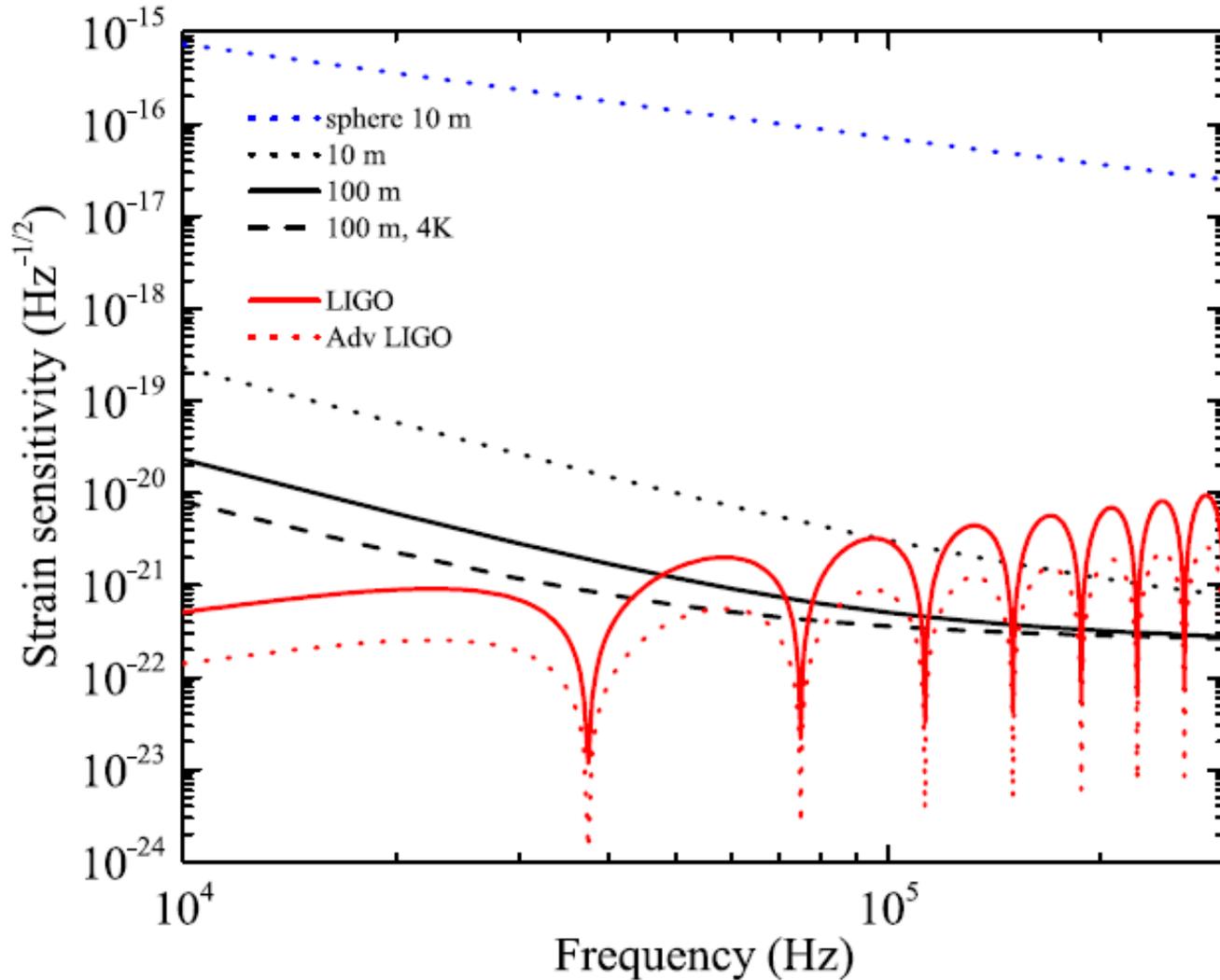
150 nm sphere



500 nm  $\times$  (75  $\mu\text{m}$ )<sup>2</sup>  
disk

Differing sensitivity between the two geometries  
due to difference in mass and in light scattering properties

# GW Strain Sensitivity



— 100 m

Size scale:



LIGO

# GW sources at high-frequency

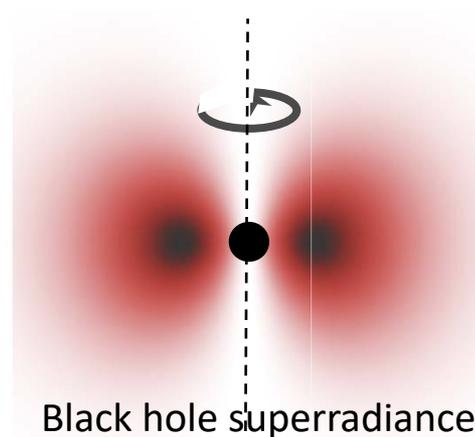
- Astrophysical Sources

Natural upper bound on GW frequency  
inverse BH size  $\sim 30$  kHz

- Beyond standard model physics

- QCD Axion  $\rightarrow$  Annihilation to gravitons in  
cloud around Black holes

A. Arvanitaki et. al, PRD, 81, 123530 (2010)

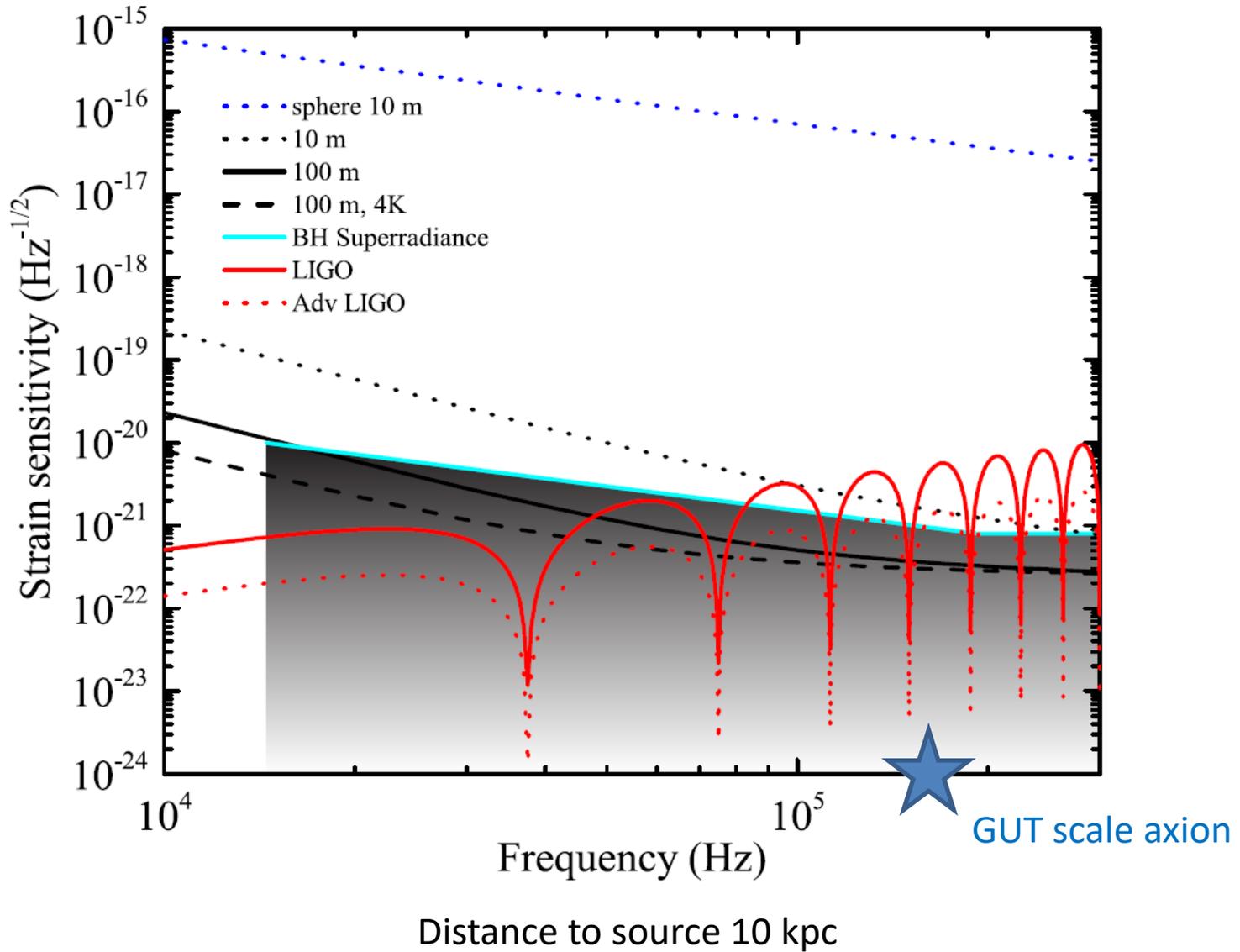


- String cosmology

R. Brustein et. al. Phys. Lett. B, 361, 45 (1995)

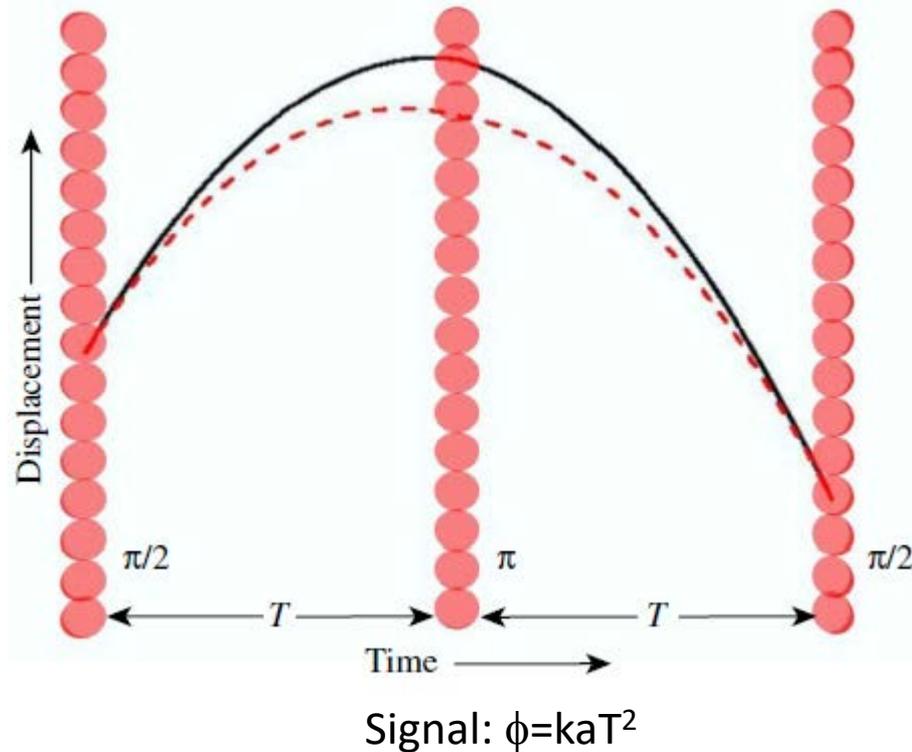
- The unknown?

# GW Strain Sensitivity



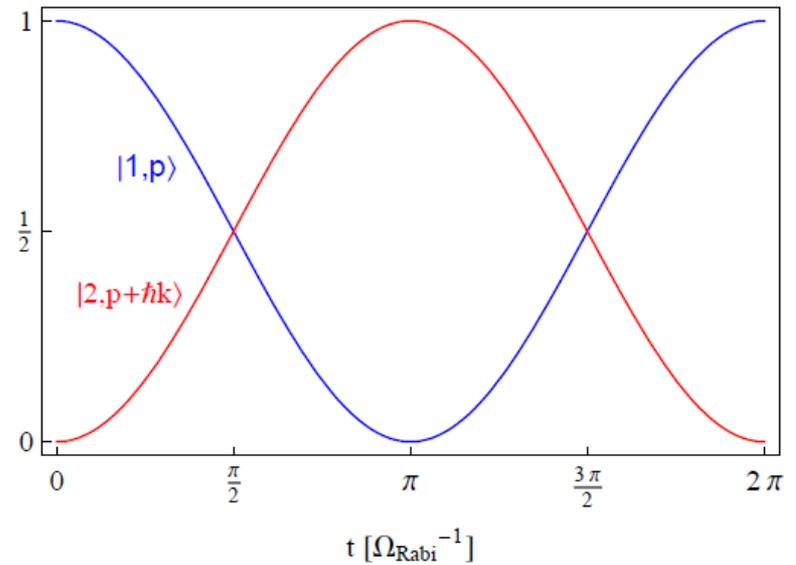
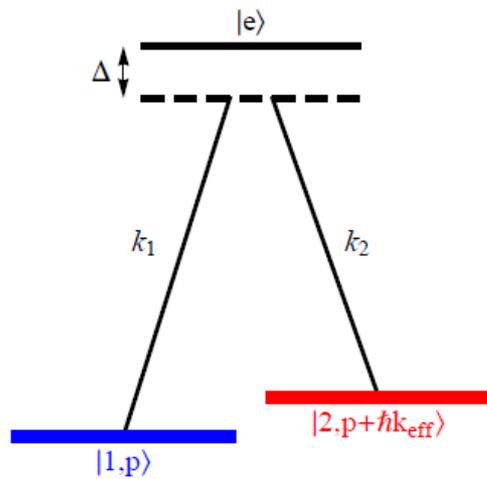
# Matter-wave interferometers

- Excellent for accelerometers, gyroscopes
- Example: atom interferometer



Sensitivity:  $ng/\sqrt{Hz}$  or better

# Atom interferometry with Raman transitions



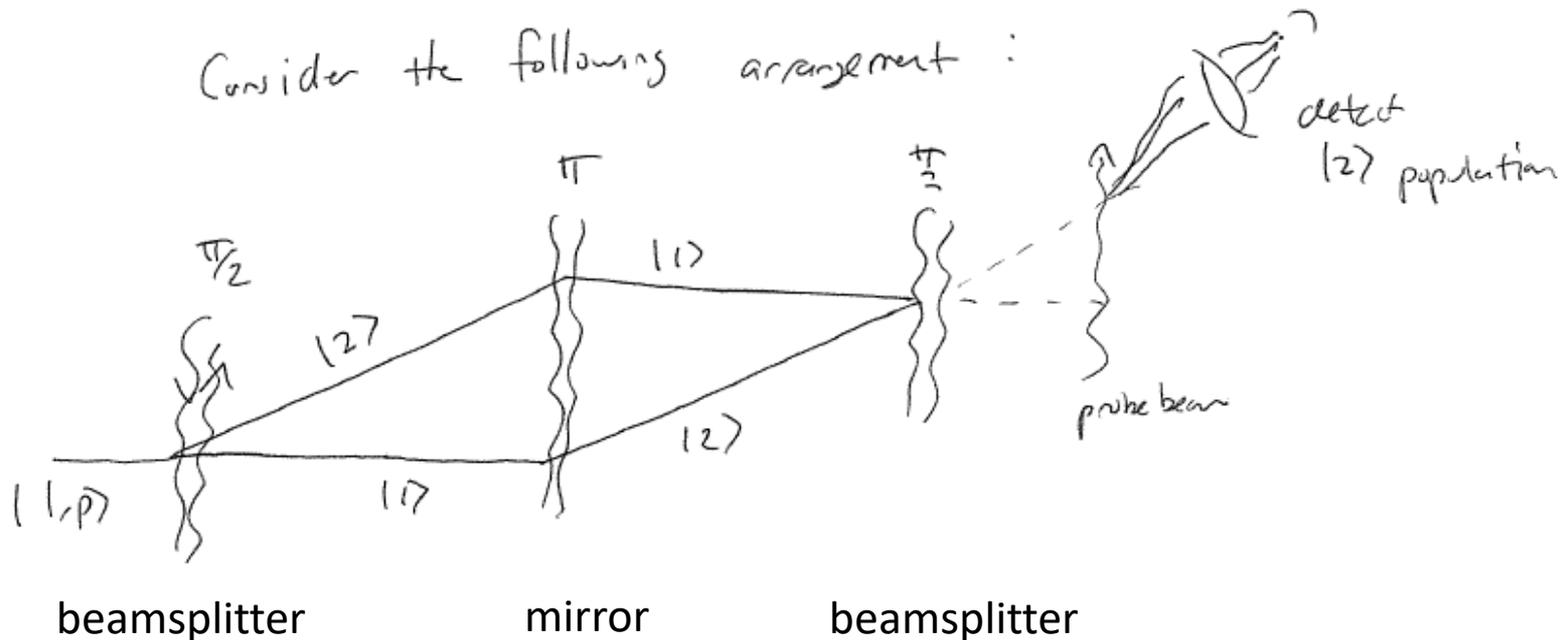
# Beamsplitters and Mirrors

e.g. a  $\frac{\pi}{2}$  pulse will create equal superposition  
 of  $|1\rangle$  &  $|2\rangle$  from initial state  $|1\rangle$ .

$$|\psi_0\rangle = |1, p\rangle$$

$$|\psi\rangle = \{ |1, p\rangle + e^{i\phi_1} |2, p + 2\hbar k\rangle \}$$

Consider the following arrangement:



# Phase shifts in Atom Interferometry

Probability to be in state 1 after 2<sup>nd</sup> beamsplitter pulse:  $[1 + \cos(\Delta\phi)]/2$

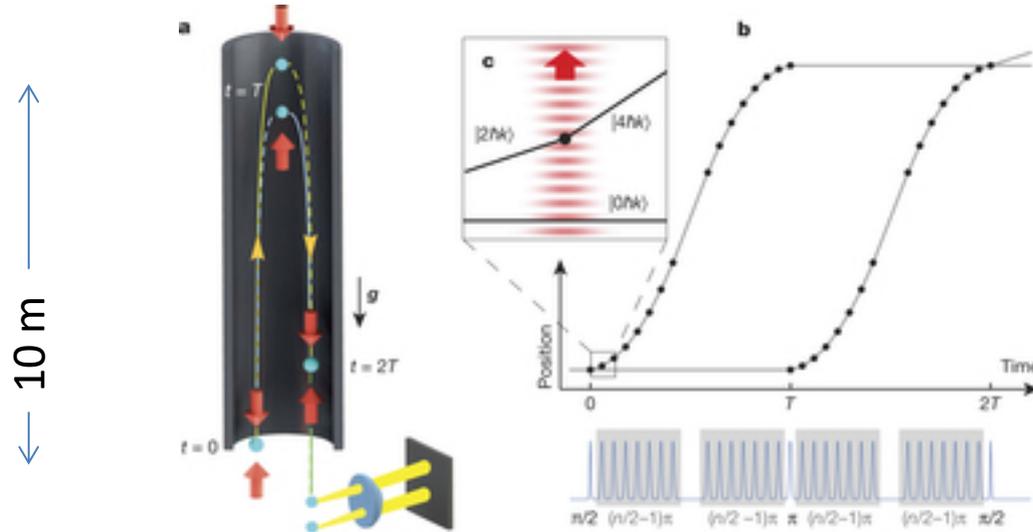
$$\Delta\phi = \Delta\phi_{prop} + \Delta\phi_{laser} + \Delta\phi_{sep}.$$

$$\Delta\phi_{prop} = \frac{1}{\hbar} \int (S_u - S_l) = \frac{1}{\hbar} \int \left( \frac{1}{2}mv_u^2 - mgz_u \right) dt - \frac{1}{\hbar} \int \left( \frac{1}{2}mv_l^2 - mgz_l \right) dt$$

$$\Delta\phi_{laser} = k_{eff}(z_i - z_{1l} - z_{1u} + z_{2l})$$

$$\Delta\phi_{sep} = \frac{m}{2\hbar}(v_{2u} - v_R + v_{2l})(z_{2l} - z_{2u})$$

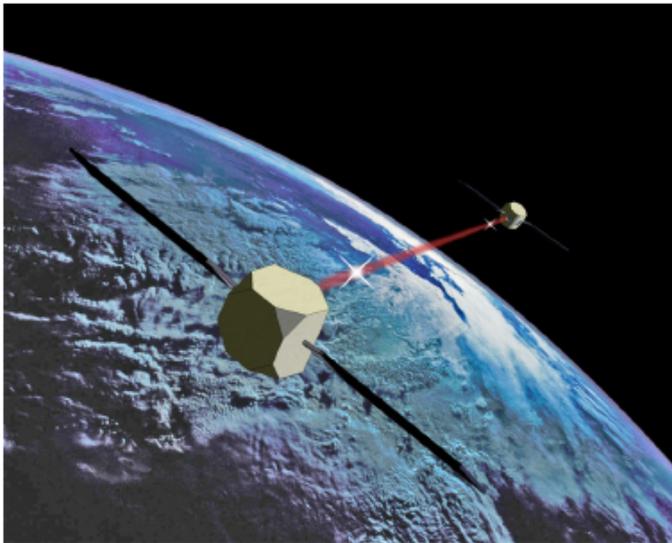
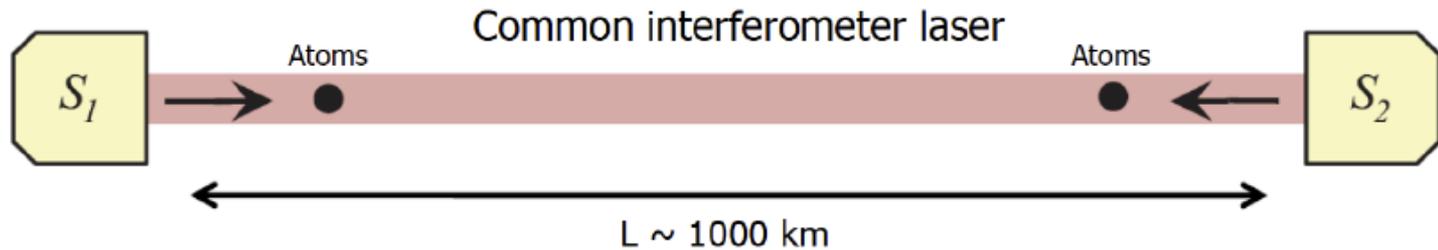
# Quantum superpositions at half-meter scale!



Signal:  $\phi = kaT^2$

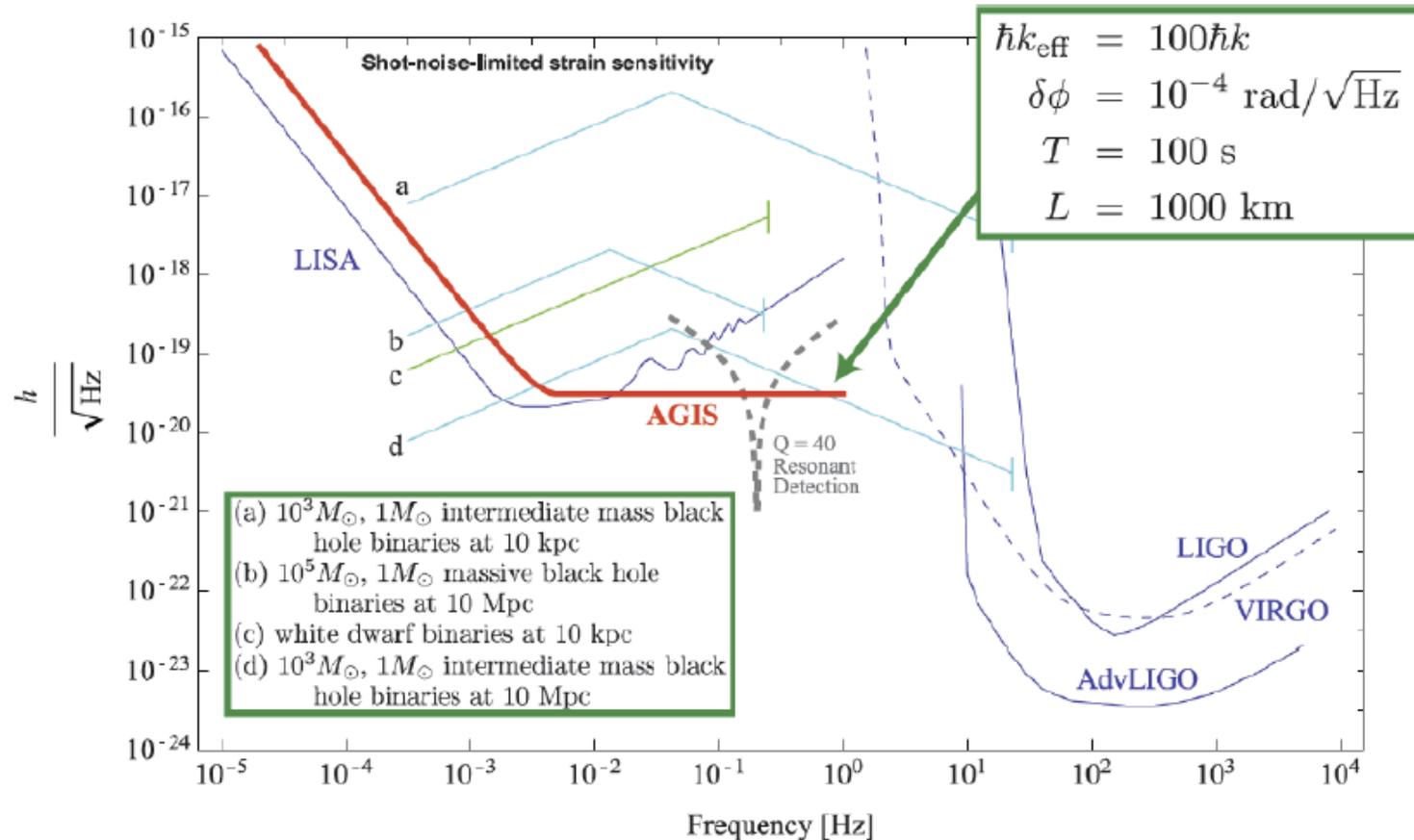
54 cm

- Atom interferometers for gravitational wave detection



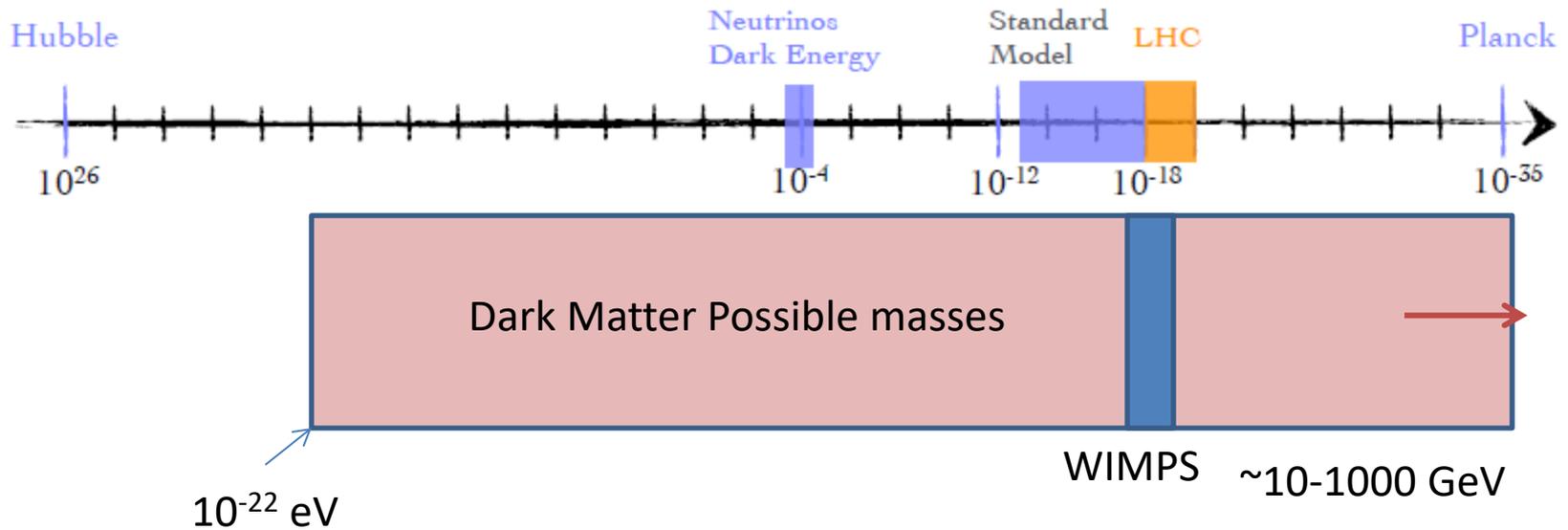
- Atoms are test masses
- Atom is **inertially decoupled** (freely falling); insensitive to vibration
- *However*: Lasers vibrate, are noisy
- **Differential measurement** with common laser helps suppress noise

- Atom interferometers for gravitational wave detection



- Space-based atom GW detector could have science potential comparable to LISA

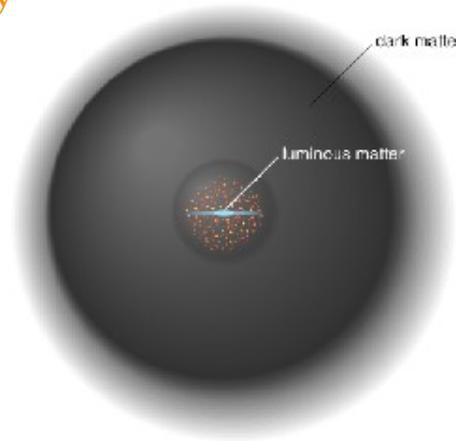
# The length scales of the Universe



80% of the energy scale left to explore

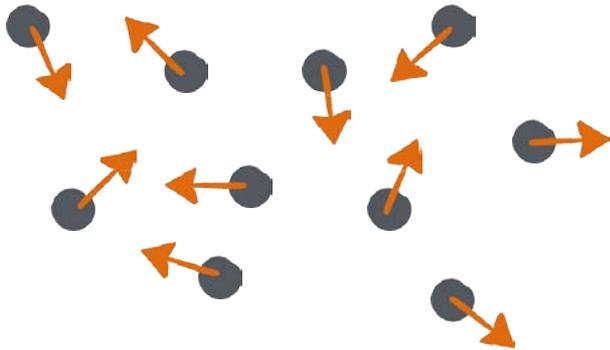
# What If DM Is a Boson and Very Light?

Dark Matter Particles in the Galaxy



Usually we think of

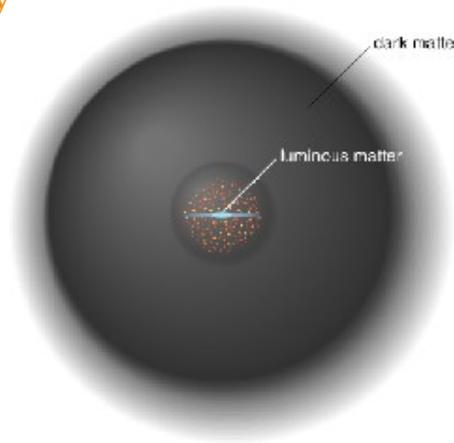
...



like a WIMP

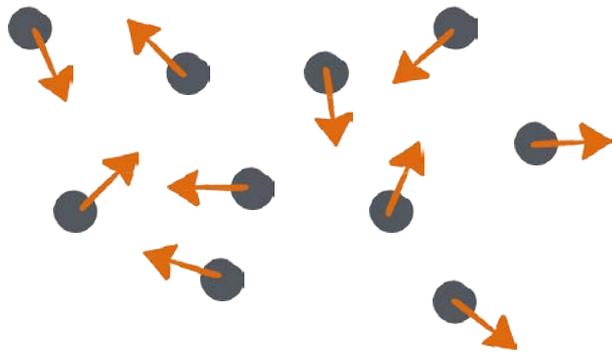
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Dark Matter Particles in the Galaxy



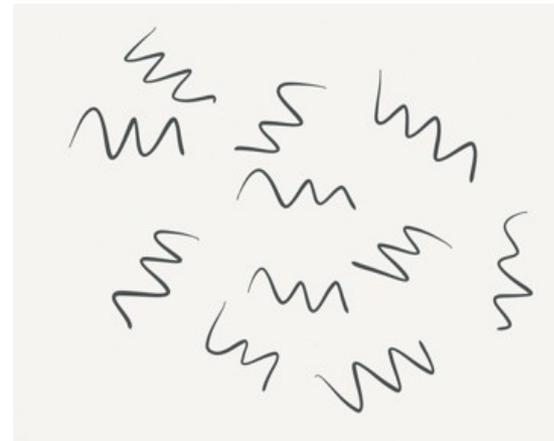
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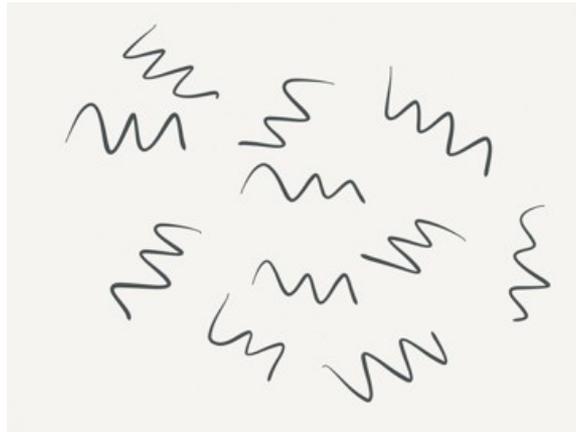
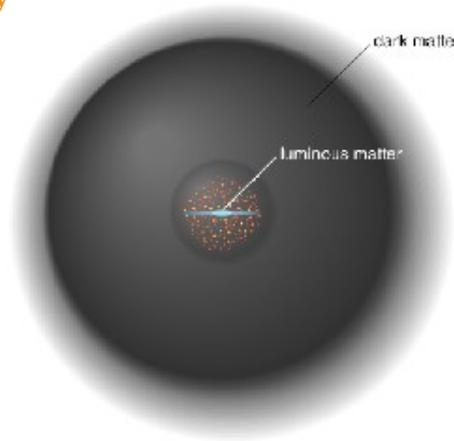
instead of...



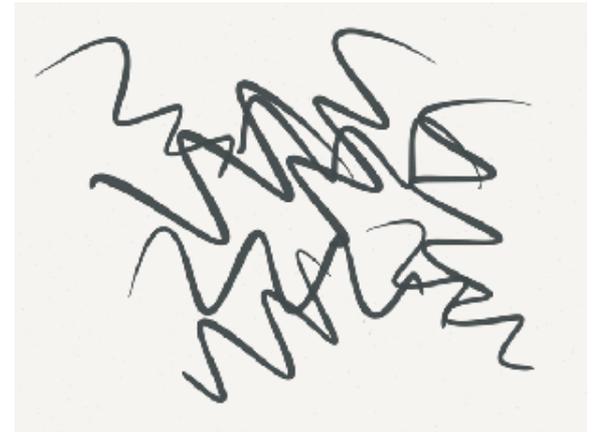
$$\lambda_{DM} = \frac{\hbar}{m_{DM}v}$$

# What If DM Is a Boson and Very Light?

Dark Matter Particles in the Galaxy

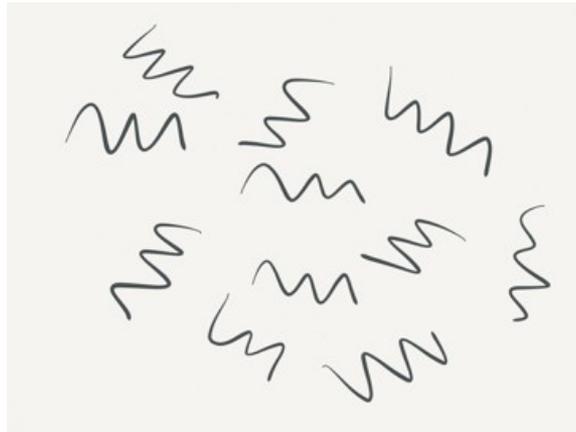
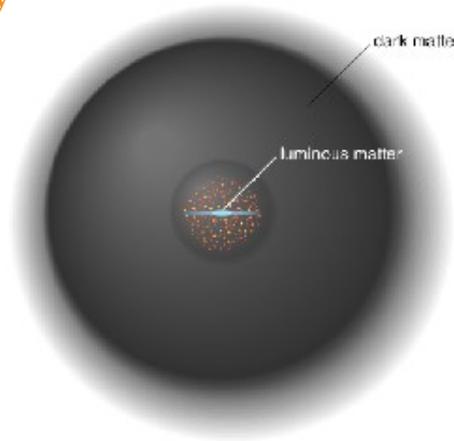


Decreasing DM Mass

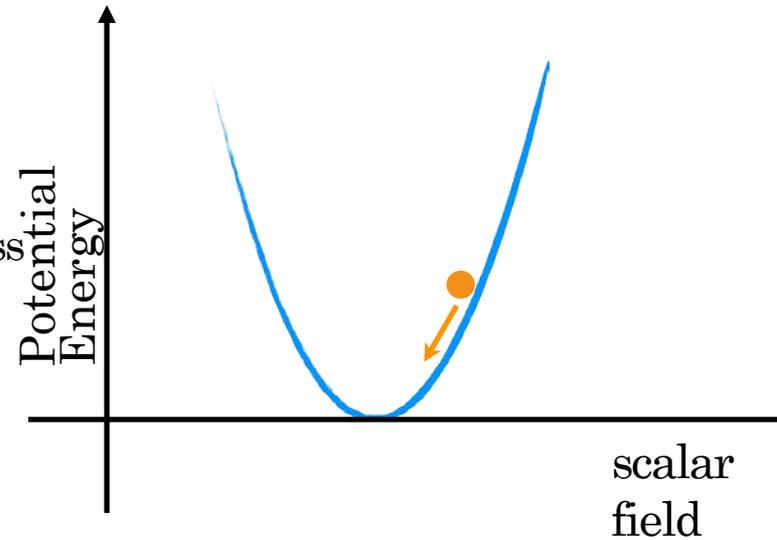


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Dark Matter Particles in the Galaxy

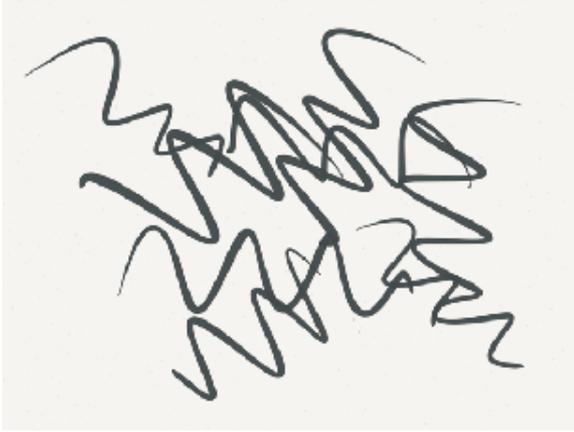


Decreasing DM Mass



Equivalent to a Scalar Wave

# Going from DM particles to a DM “wave”



$$\text{When } n_{DM} > \frac{1}{\lambda_{DM}^3}$$

In our galaxy this happens when  $m_{DM} < 1 \text{ eV}/c^2$

we can talk about DM  $\phi(x,t)$  and locally

$$\phi(t) \approx \phi_0 \cos \omega_{DM} t$$

with amplitude

$$\phi_0 \propto \frac{\sqrt{\text{DM density}}}{\text{DM mass}}$$

with frequency

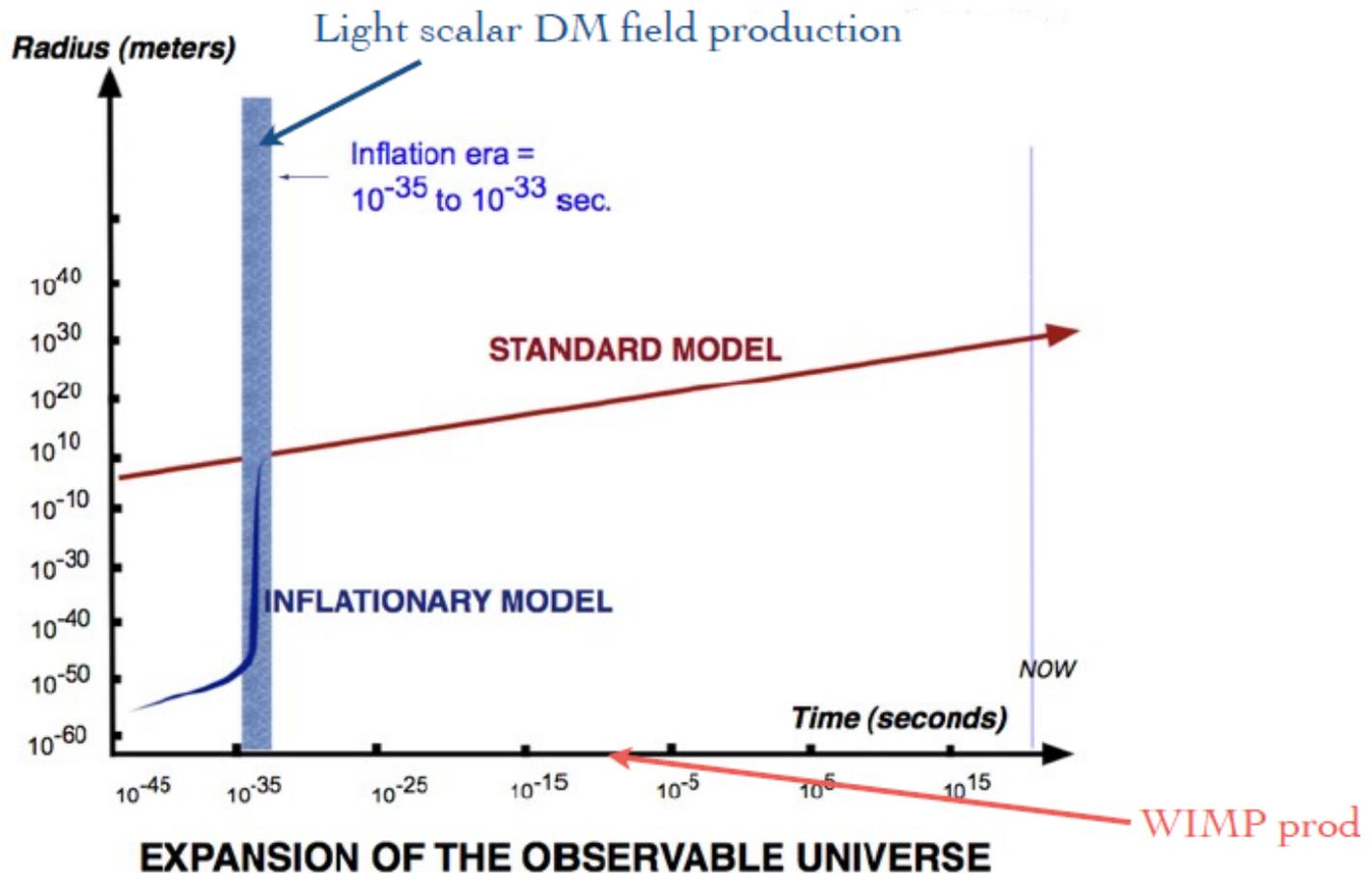
$$\omega_{DM} \approx \frac{m_{DM} c^2}{\hbar}$$

and finite coherence

$$\delta\omega_{DM} \approx \frac{m_{DM} v^2}{\hbar} = 10^{-6} \omega_{DM}$$

# Scalar DM field production

- The “misalignment mechanism” during inflation

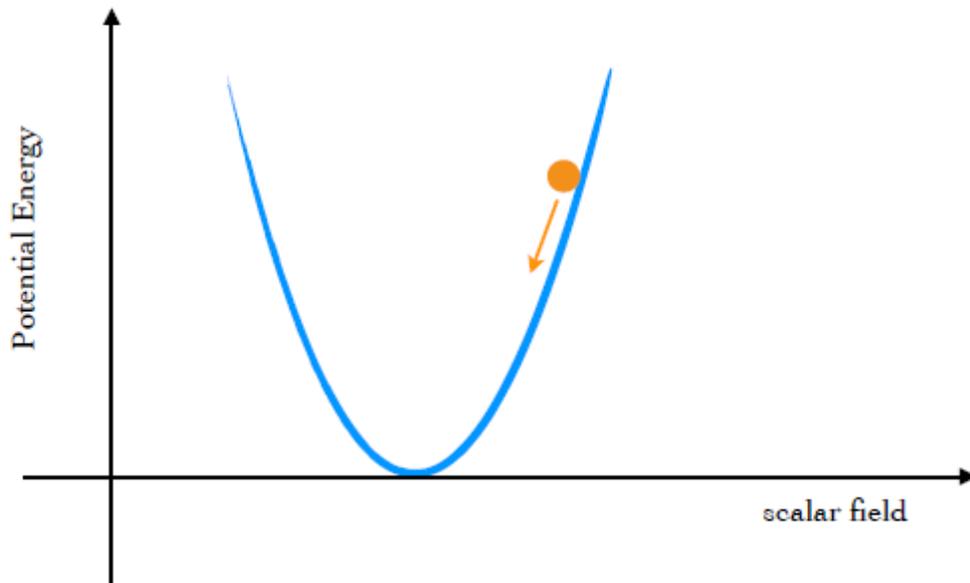


# Light scalar Dark Matter

- Just like a harmonic oscillator

$$\ddot{\phi} + 3 H \dot{\phi} + m_{\phi}^2 \phi = 0$$

$$\ddot{x} + \gamma \dot{x} + \omega^2 x = 0$$



Frozen when:  
Hubble  $>$   $m_{\phi}$

Oscillates when:  
Hubble  $<$   $m_{\phi}$

$\rho_{\phi}$  scales as  $a^{-3}$   
just like **Dark Matter**

Initial conditions set by inflation

# Light scalar Dark Matter

- Dark Matter can exist at a variety of mass scales:

$>10^{-22}$  eV (size of dwarf galaxies)

- Ultralight DM looks like coherent field rather than particle

$$\phi(\mathbf{r}, t) = \phi_0 \cos(\omega_\phi t - \mathbf{k}_\phi \cdot \mathbf{r} + \dots).$$

$$\phi_0 = \hbar \sqrt{2\rho_{\text{DM}}} / (m_\phi c)$$

# Spatial and time variations of masses and fundamental constants

$$-\mathcal{L}_n^{\text{int}} = (\sqrt{\hbar c \phi})^n \times \left( \frac{m_e \bar{\psi}_e \psi_e}{\Lambda_{n,e}^n} + \frac{m_p \bar{\psi}_p \psi_p}{\Lambda_{n,p}^n} - \frac{1}{4\Lambda_{n,\gamma}^n} F_{\mu\nu}^2 + \dots \right).$$

$$\frac{m_f^{\text{eff}}}{m_f} = 1 + \frac{(\sqrt{\hbar c \phi(\mathbf{r}, t)})^n}{\Lambda_{n,f}^n},$$

$$\frac{\alpha^{\text{eff}}}{\alpha} \approx 1 + \frac{(\sqrt{\hbar c \phi(\mathbf{r}, t)})^n}{\Lambda_{n,\gamma}^n}.$$

$$\phi(\mathbf{r}, t) = \phi_0 \cos(\omega_\phi t - \mathbf{k}_\phi \cdot \mathbf{r} + \dots).$$

$$\phi_0 = \hbar \sqrt{2\rho_{\text{DM}}} / (m_\phi c)$$

# Other properties of ultralight scalars

- Mediates new interactions in matter

- Generates a fifth force in matter



$$F \sim \frac{(d_i Q_i)^2}{4\pi M_{Pl}^2} \frac{M_1 M_2}{r^2} e^{-m_\phi r}$$

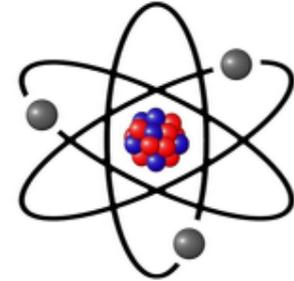
- Generates Equivalence Principle violation



# Techniques for sensing oscillating scalar DM

- Atomic clocks
- Bar detectors
- Torsion Balances
- Atom Interferometers

# Oscillating Atomic and Nuclear Energy Splittings



- Optical Splittings

$$\Delta E_{\text{optical}} \propto \alpha_{EM}^2 m_e \sim \text{eV}$$

- Hyperfine Splittings

$$\Delta E_{\text{hyperfine}} \propto \Delta E_{\text{optical}} \alpha_{EM}^2 \left( \frac{m_e}{m_p} \right) \sim 10^{-6} \text{ eV}$$

- Nuclear Splittings

$$\Delta E (m_p, \alpha_s, \alpha_{EM}) \sim 1 \text{ MeV}$$

DM appears as a signature in atomic (or nuclear) clocks

# Oscillating Atomic and Nuclear Energy Splittings

- Optical Splittings



$$\Delta E_{\text{optical}} \propto \alpha_{EM}^2 m_e \sim \text{eV}$$

- Hyperfine Splittings

$$\Delta E_{\text{hyperfine}} \propto \Delta E_{\text{optical}} \alpha_{EM}^2 \left( \frac{m_e}{m_p} \right) \sim 10^{-6} \text{ eV}$$

- Nuclear Splittings

$$\Delta E (m_p, \alpha_s, \alpha_{EM}) \sim 1 \text{ MeV}$$

DM appears as a signature in atomic (or nuclear) clocks

# Atomic Clocks

- Kept tuned to an atomic energy level splitting

**Current definition of a second:**

the duration of 9192631770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium 133 atom

- Have shown stability of 1 part in  $10^{18}$

Compared to 1 part in  $10^{13}$  expected by DM

- Have won several Nobel prizes in the past 20 years

# How does and Atomic Clock Work?

Keep a laser tuned to a long-lived (> minutes) atomic transition



How well can I measure the frequency of the laser when tuned to the atom?

$$\frac{\delta f}{f} \sim \frac{\Gamma_{\text{atom}}}{f} \frac{1}{\sqrt{N_{\text{atoms}}}} \sqrt{\frac{\tau_{\text{cycling}}}{t_{\text{experiment}}}}$$

# How do you take the measurements?

- Observe two clocks every  $\tau_{\text{cyclin}}g$  to remove systematics
- Calculate ratio of frequencies which depends on Dark Matter
- Take Fourier transform to look for oscillations with period longer than  $\tau_{\text{cyclin}}g$

Atomic Clock DM searches are broadband searches

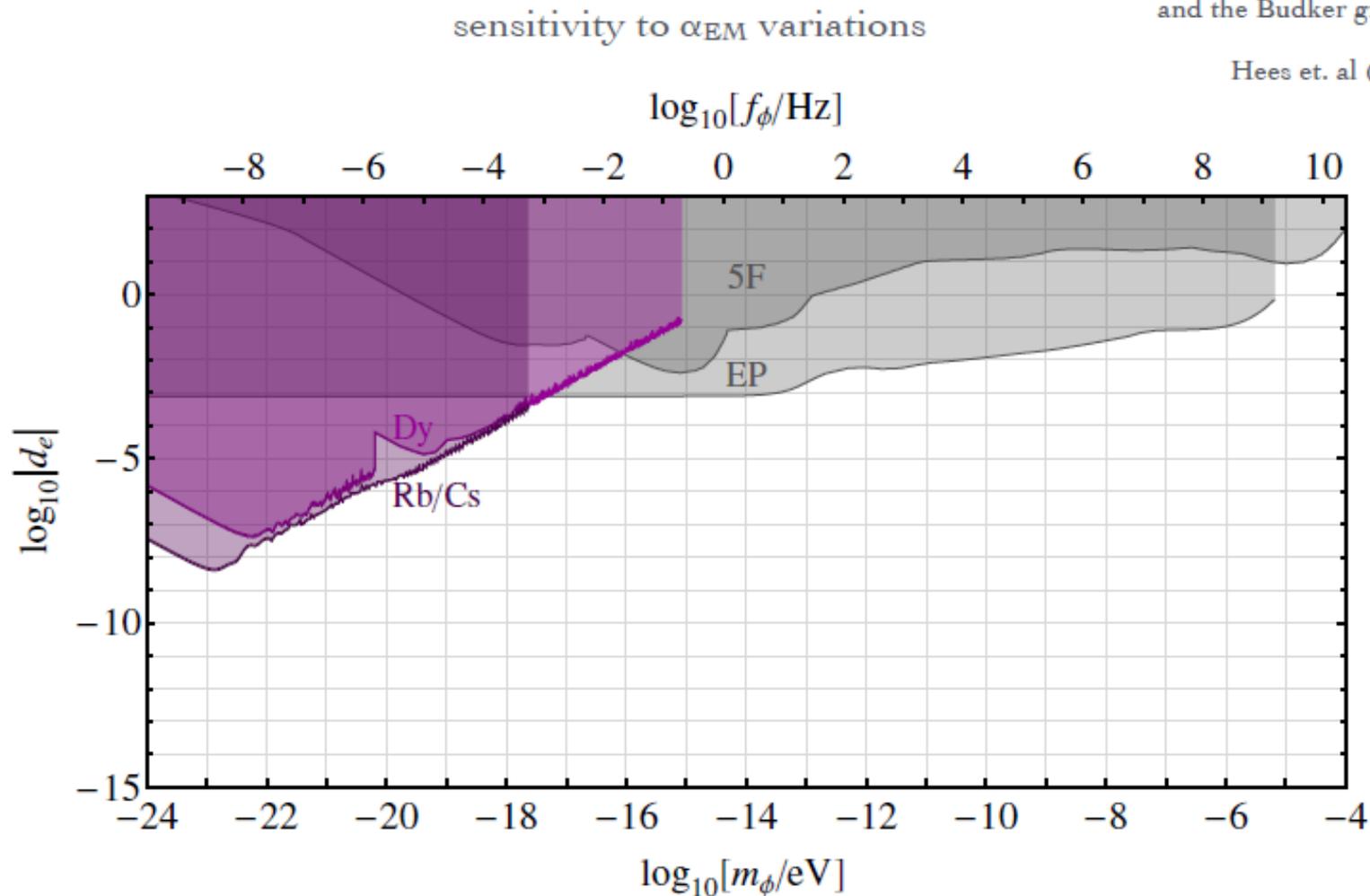
# What type of comparisons can we do?

- Hyperfine to Optical transitions
  - Sensitive to  $m_e$ ,  $m_q$ , and  $\alpha_s$  (less to  $\alpha_{EM}$ )
- Optical to Optical transitions
  - Sensitive to  $\alpha_{EM}$
- Nuclear to Optical transitions
  - Sensitive to  $m_e$ ,  $\alpha_{EM}$ ,  $m_q$ , and  $\alpha_s$

# The Dy isotope and Rb/Cs Clock Comparison

Ken Van Tilburg  
and the Budker group (2015)

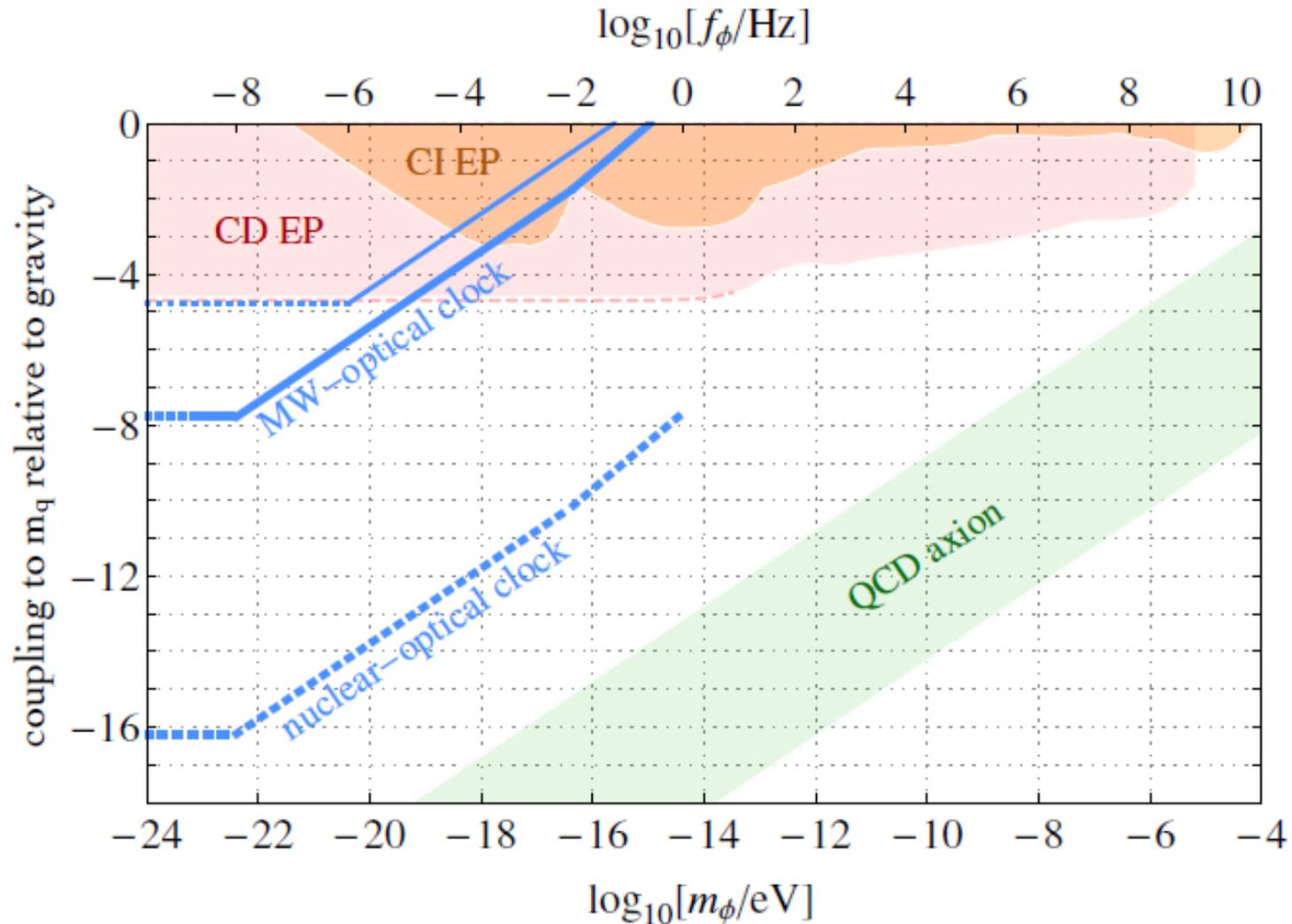
Hees et. al (2016)



Analysis performed with existing  
data

# Projected - Future Clock Comparisons

Future Sensitivity of a  $^{229}\text{Th}$  clock with  $10^{-15}/\text{Hz}^{-1/2}$  noise



# Detecting oscillating interatomic distances

- The Bohr radius changes with DM

- $r_B \sim (\alpha m_e)^{-1}$

$$\frac{\delta r_B}{r_B} = - \left( \frac{\delta \alpha_{EM}}{\alpha_{EM}} + \frac{\delta m_e}{m_e} \right)$$

- The size of solids changes with DM

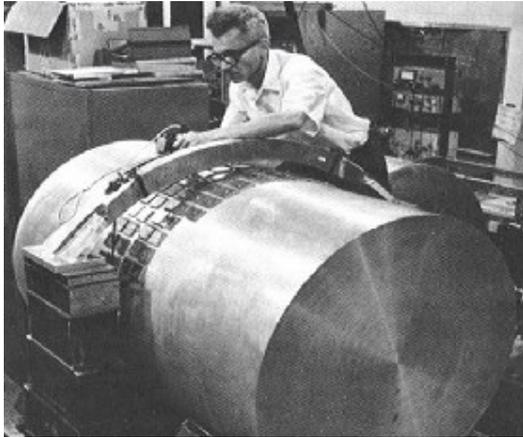
- $L \sim N (\alpha m_e)^{-1}$

$$\frac{\delta L}{L} = - \left( \frac{\delta \alpha_{EM}}{\alpha_{EM}} + \frac{\delta m_e}{m_e} \right)$$

Need macroscopic objects to get a detectable signal

# Resonant-Mass Detectors

- In the 1960's: **The Weber Bar**



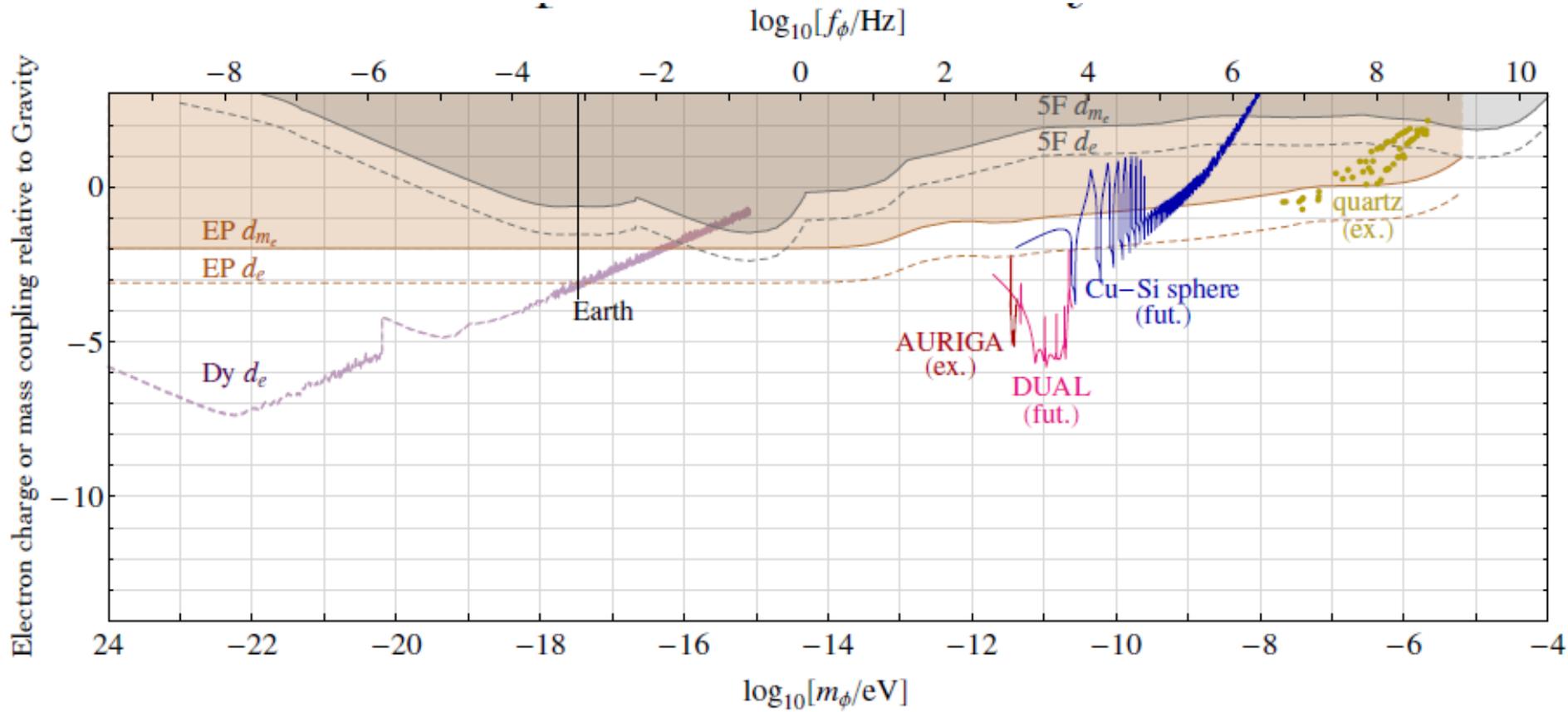
Strain sensitivity  $h \sim 10^{-17}$

- Today: AURIGA, NAUTILUS, MiniGrail

Strain sensitivity  $h \sim 10^{-23}$



# Experimental Sensitivity



# Ultralight DM with accelerometers

## Dark Matter Direct Detection with Accelerometers

Peter W. Graham,<sup>1</sup> David E. Kaplan,<sup>1,2,3,4</sup> Jeremy Mardon,<sup>1</sup> Surjeet Rajendran,<sup>3</sup> and William A. Terrano<sup>5,6</sup>

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<sup>3</sup>*Berkeley Center for Theoretical Physics, Department of Physics, University of California, Berkeley, CA 94720*

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<sup>5</sup>*Center for Experimental Nuclear Physics and Astrophysics,*

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Spin	Type	Operator	Interaction	Oscillating DM Effects	Searches
0	scalar	$\phi h^\dagger h, \phi \mathcal{O}_{\text{SM}}$	Higgs portal / dilaton	$m_e, m_p, \alpha$ variation	Atomic clocks [51]
				acceleration	*
	pseudo-scalar	$a G^{\mu\nu} \tilde{G}_{\mu\nu}$	axion-QCD	nucleon EDM	CASPER [18]
		$a F^{\mu\nu} \tilde{F}_{\mu\nu}$	axion-E&M	EMF along $B$ field	ADMX [13]
		$(\partial_\mu a) \bar{\psi} \gamma^\mu \gamma_5 \psi$	axion-fermion	spin torque	CASPER [18]
1	vector	$A'_\mu \bar{\psi} \gamma^\mu \psi$	minimally coupled	acceleration	*
		$F'_{\mu\nu} F^{\mu\nu}$	vector-photon mixing	EMF in vacuum	DM Radio [32], ADMX
		$F'_{\mu\nu} \bar{\psi} \sigma^{\mu\nu} \psi$	dipole operator	spin torque	CASPER [18]
	axial-vector	$A'_\mu \bar{\psi} \gamma^\mu \gamma_5 \psi$	minimally coupled	spin torque	CASPER [18]
2 (?)	tensor	$h'_{\mu\nu} T^{\mu\nu}$ (?)	gravity-like	grav. wave-like	grav. wave detectors?

# Dark Matter induced acceleration

Consider Higgs portal DM:

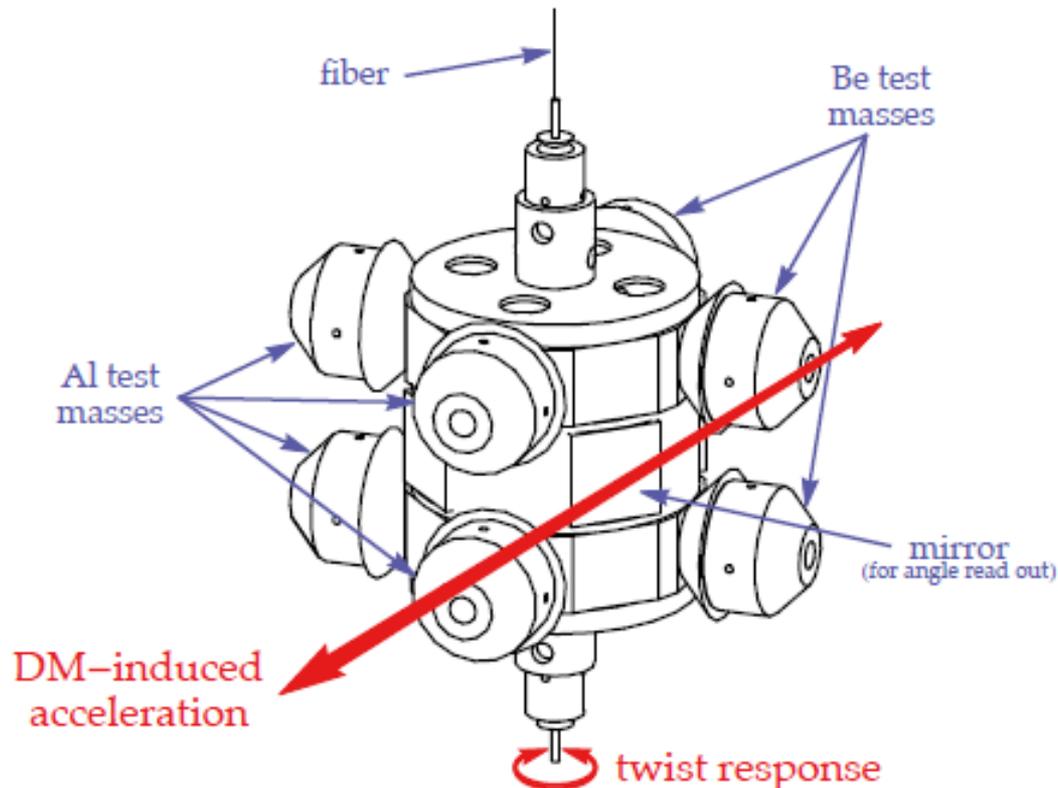
$$\mathcal{L} \supset \frac{b\phi}{m_h^2} \langle h \rangle g_{h\psi\psi} \bar{\psi}\psi$$

Force on matter due to:  $\nabla\phi$

- Different materials with different composition, different binding energies etc. experience relative accelerations due to DM field
- Violates EP
- In direction of grad phi (changes over times longer than coherence time)

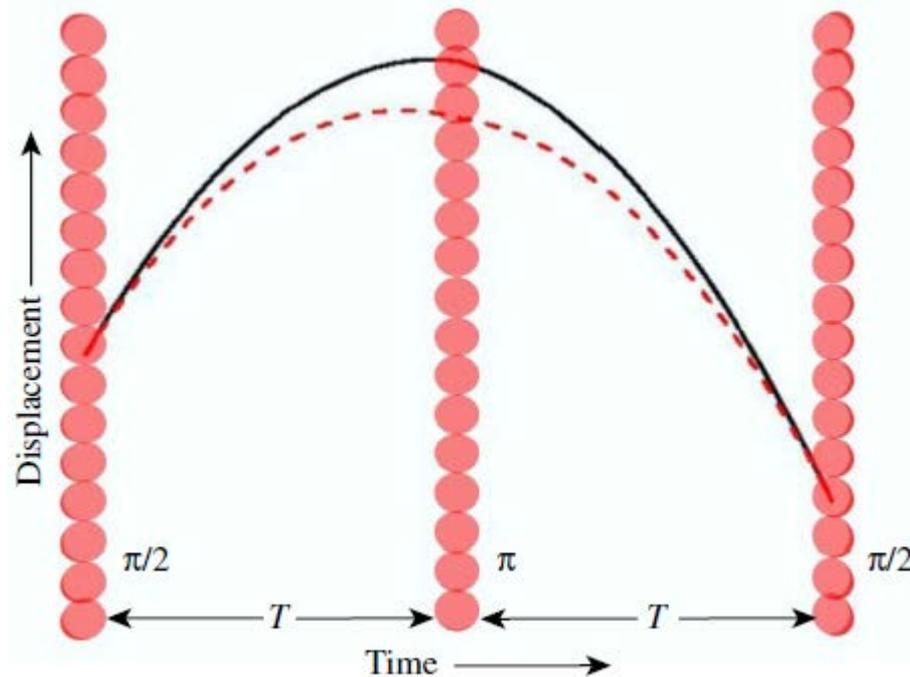
# Torsion balance tests

- Tests of Equivalence principle

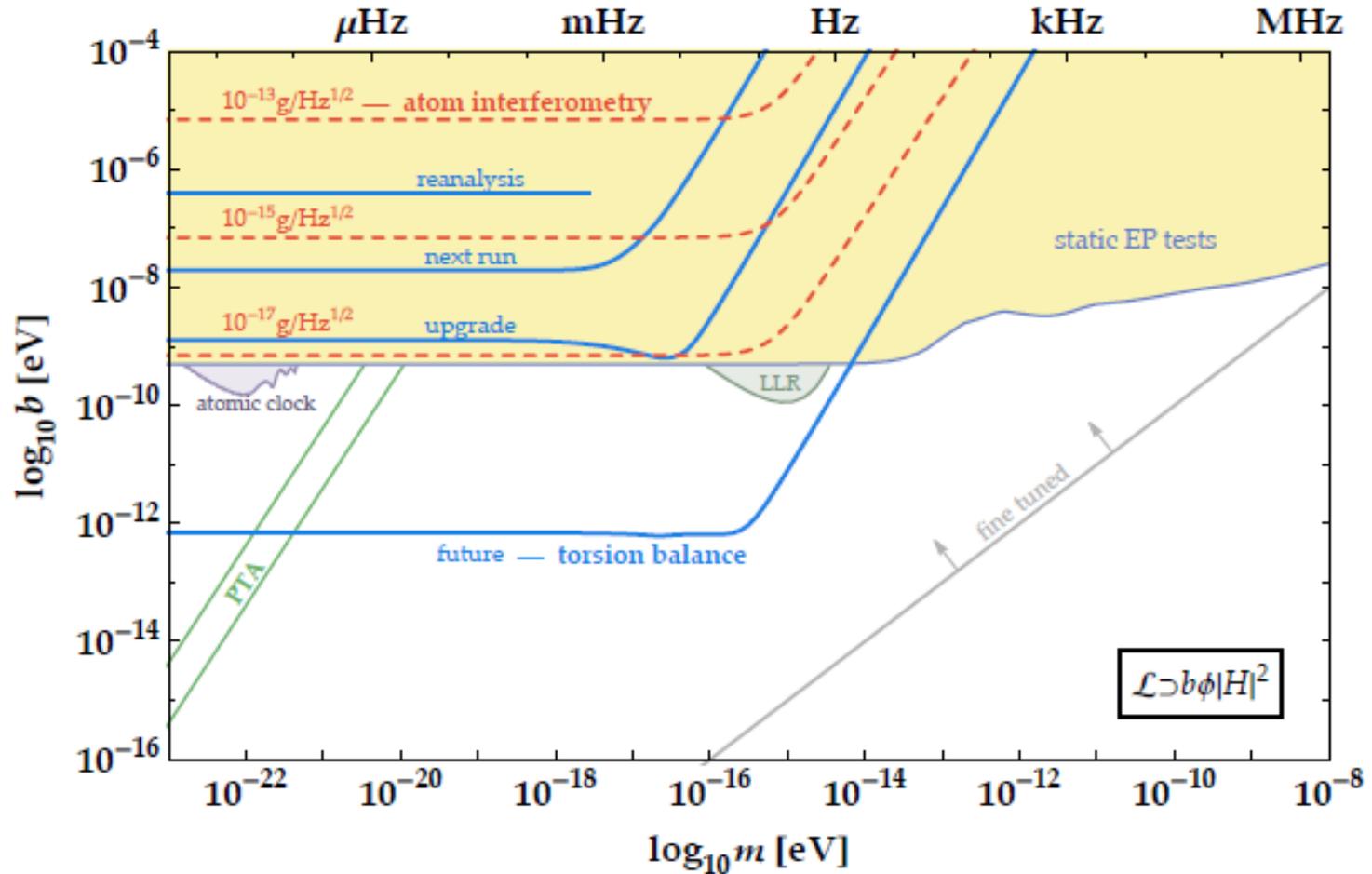


# Atomic Interferometers

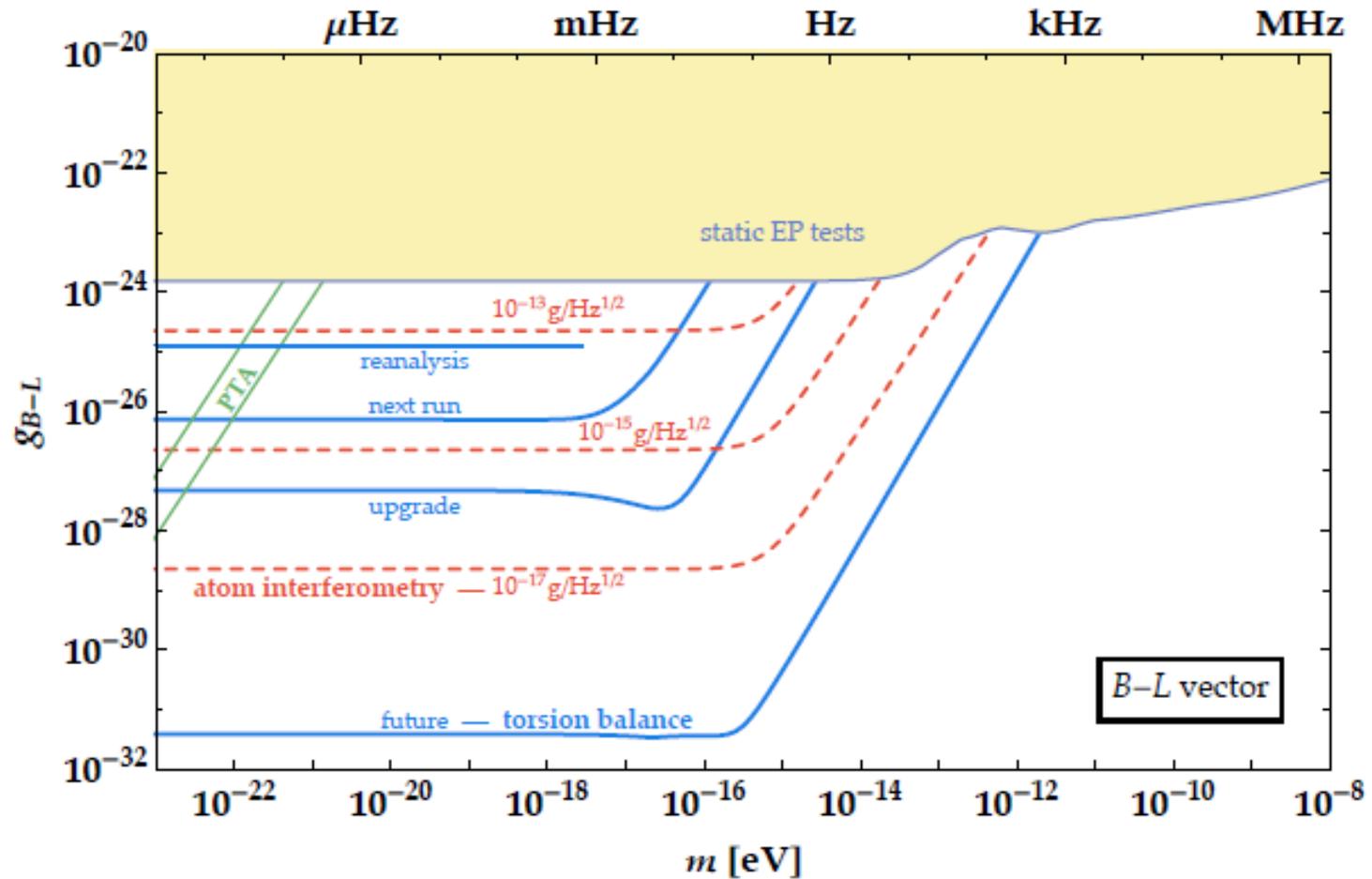
- Also can measure force due to  $\nabla\phi$   
e.g. for different atomic isotopes



# Higgs portal



# Vector (B-L) portal



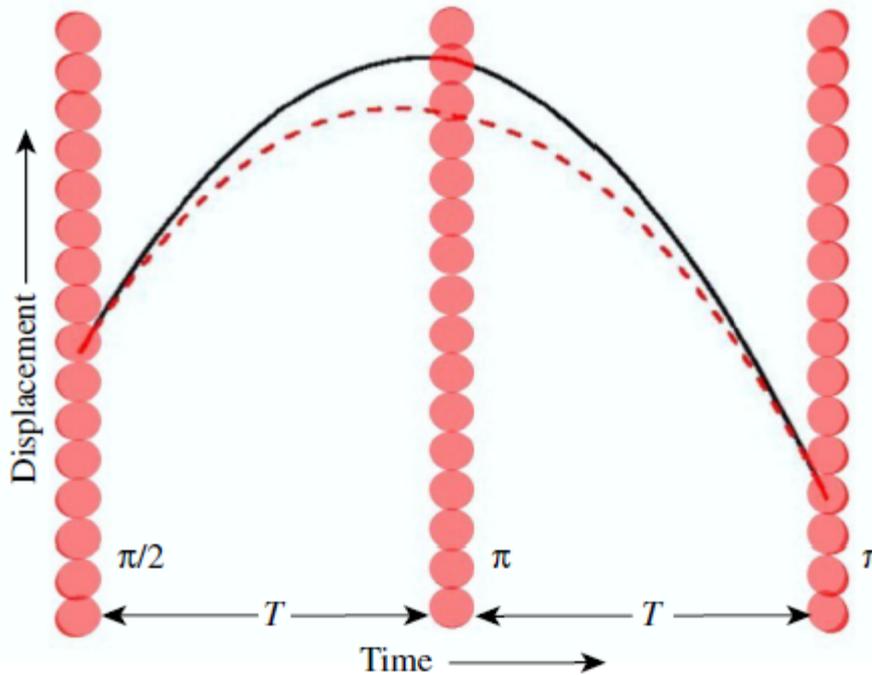
# Time-varying acceleration of earth and masses of atoms

$$\begin{aligned}\frac{\Delta g_n}{g} &= \frac{\Delta M_\oplus}{M_\oplus} \\ &= \left( \frac{2\rho_{\text{DM}}\hbar^3}{m_\phi^2 c \Lambda_n^2} \right)^{n/2} \times \frac{1}{2^{(n-1)}} \cos(n\omega_\phi t - nk_\phi \cdot \mathbf{r} + \dots)\end{aligned}$$

$$g(t) = g_0[1 + \delta_g \cos(\omega t + \theta_0)],$$

$$m(t) = m_0[1 + \delta_m \cos(\omega t + \theta_0)].$$

# Mach-Zehnder Atom interferometer

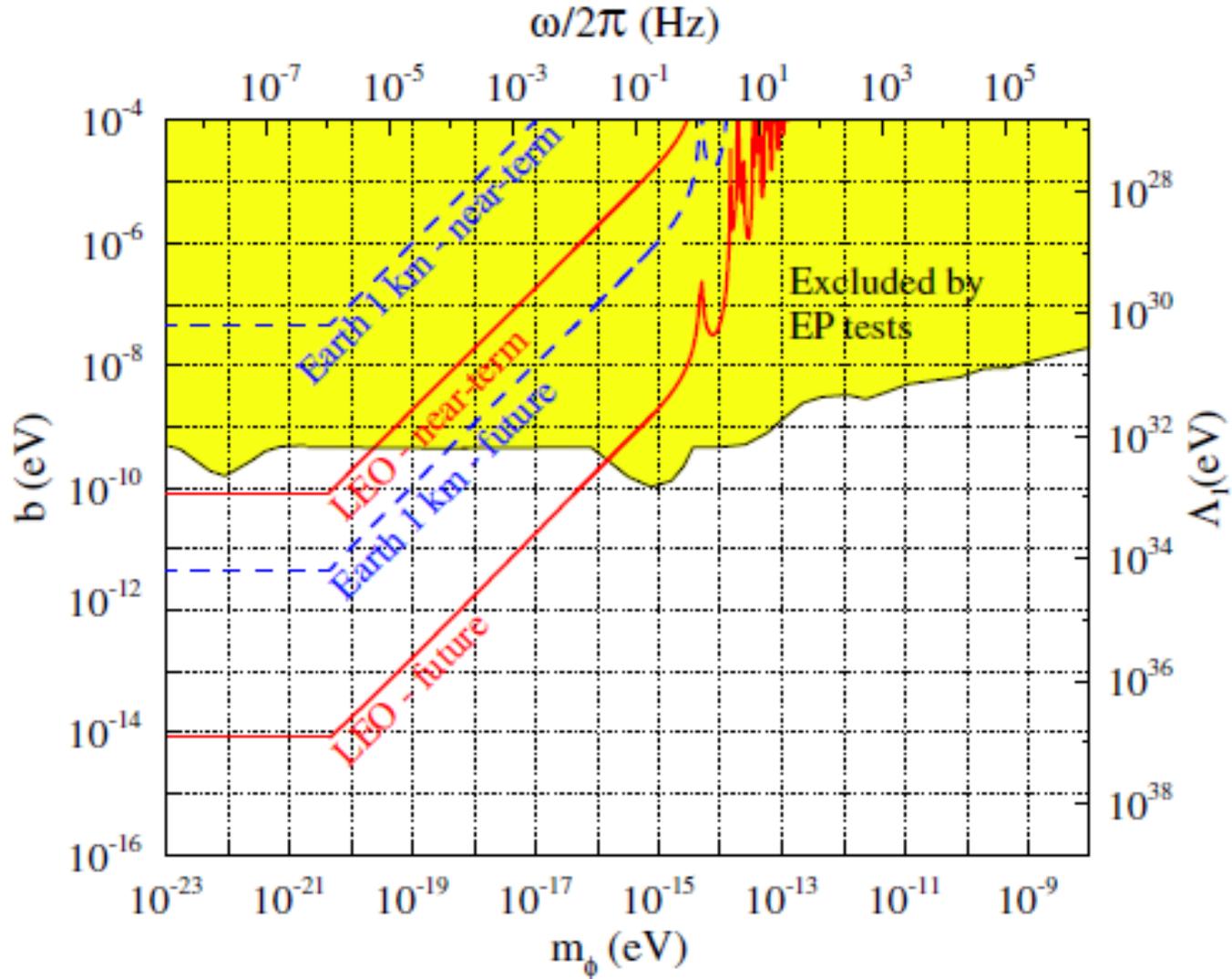


$$v_R(t) = \hbar k_{\text{eff}}/m(t) \approx \frac{\hbar k_{\text{eff}}}{m_0} [1 - \delta_m \cos(\omega t + \theta_0)].$$

$$\begin{aligned} \Delta\phi = & -k_{\text{eff}}g_0T^2 - \delta_m \frac{2g_0k_{\text{eff}}T}{\omega} (\sin \omega T - \sin 2\omega T) \\ & + [\delta_g + 2\delta_m] \frac{g_0k_{\text{eff}}}{\omega^2} (1 - 2\cos \omega T + \cos 2\omega T) \\ & + \delta_m \left( \frac{k_{\text{eff}}(v_L + v_R/2)}{\omega} \right) (2\sin \omega T - \sin 2\omega T) \end{aligned}$$

FIG. 1. Spacetime diagram for the Mach-Zehnder atom interferometer. Atomic wave packets are split into a superposition state with differing momenta, reflected with a mirror ( $\pi$ ) pulse, and recombined with a final beam splitter pulse. The final population in state  $|1\rangle$  is given by  $[1 + \cos(\Delta\phi)]/2$ .

# Higgs portal search



# Summary

- New AMO techniques (levitated particles, atom interferometers) could enable search for GWs at higher (and lower) frequency
  - Variety of methods to search for oscillating ultralight dark matter
    - time variation of constants (clocks)
    - length changes in materials (resonant bars)
    - accelerometers (torsion balances, atomic interferometers)
- (next lectures) Axions, spin-dependent new forces