

# BEYOND THE STANDARD MODEL @ THE TEV SCALE

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# *NOT YOUR ADVISOR'S "BEYOND THE STANDARD MODEL"*



BSM IS AS OLD AS THE STANDARD MODEL, GIVING RISE TO DOMINANT PARADIGMS (THE MSSM, WIMPS, ETC.) THAT FILL LECTURES SUCH AS THESE. *BUT WE ARE IN AN ERA RICH WITH DATA THAT IS CHALLENGING THESE PARADIGMS, SO LET'S KEEP AN EYE ON PROMISING ALTERNATIVES.*

# OUTLINE

## PROLOGUE: EFFECTIVE FIELD THEORY

### PART 1: HIERARCHY PROBLEMS

- NATURALNESS
- SCALAR MASSES
- VERSIONS OF THE HIERARCHY PROBLEM

### PART 2: HIERARCHY SOLUTIONS

- MULTIPLE VACUA
- LOW CUTOFFS
- SYMMETRIES

### PART 3: EVERYTHING\* ELSE

- STRONG CP PROBLEM
- UNIFICATION
- BARYOGENESIS

## EPILOGUE: LOOKING TO THE FUTURE





# PROLOGUE: EFFECTIVE FIELD THEORY

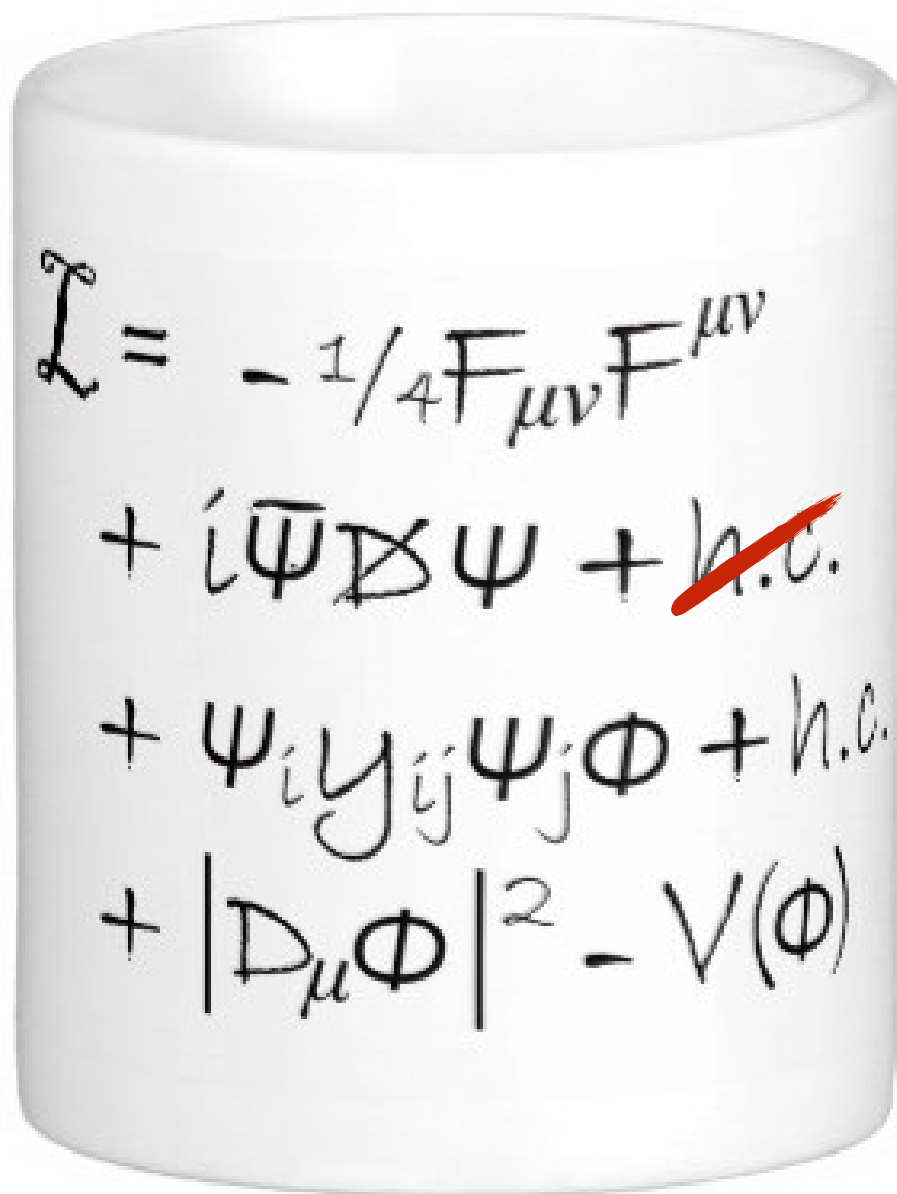


SEE LECTURES  
BY Y. NIR

# BEYOND?

BY *STANDARD MODEL*, LET US TAKE THIS TO MEAN

- (1) THE OBSERVED MATTER (THREE GENERATIONS OF QUARKS & LEPTONS), HIGGS DOUBLET, AND GAUGE FIELDS.
- (2) ALL RENORMALIZABLE (MARGINAL OR RELEVANT) INTERACTIONS ALLOWED BY THE FIELD CONTENT & GAUGE SYMMETRIES ("TOTALITARIAN PRINCIPLE")



The image shows a white ceramic mug with handwritten mathematical formulas in black ink. The formulas represent the Lagrangian of the Standard Model. The first line is  $\mathcal{L} = -1/4 F_{\mu\nu} F^{\mu\nu}$ . The second line is  $+ i \bar{\Psi} \not{D} \Psi + \text{h.c.}$ , where the 'h.c.' is crossed out with a red diagonal line. The third line is  $+ \psi_i y_{ij} \psi_j \Phi + \text{h.c.}$ . The fourth line is  $+ |D_\mu \Phi|^2 - V(\Phi)$ .

$$\begin{aligned} \mathcal{L} = & -1/4 F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\Psi} \not{D} \Psi + \text{h.c.} \\ & + \psi_i y_{ij} \psi_j \Phi + \text{h.c.} \\ & + |D_\mu \Phi|^2 - V(\Phi) \end{aligned}$$

**BSM** ENTAILS ANYTHING BEYOND THIS  
(NEW FIELDS *OR* IRRELEVANT OPERATORS)



# IRRELEVANT?

CONSIDER SCALAR FIELD THEORY IN 4 DIMENSIONS W/ SOME POLYNOMIAL POTENTIAL:

$$S[\phi] = \int d^4x \left[ \frac{1}{2} \partial^\mu \phi \partial_\mu \phi - \frac{1}{2} m^2 \phi^2 - \frac{1}{4!} \lambda \phi^4 - \frac{1}{6!} \tau \phi^6 \right]$$

IN ANY D, MASS DIMENSIONS OF LENGTH & ACTION FIXED,  $[x] = -1, [S] = 0$

$$\text{SO: } [d^4x] = -4 \quad [\phi] = 1 \quad [m^2] = 2 \quad [\lambda] = 0 \quad [\tau] = -2$$

STUDY THEORY AT LONG DISTANCES IN SCALING LIMIT  $x^\mu = s x'^\mu, s \rightarrow \infty, x'^\mu$  fixed

KEEP CANONICAL KINETIC TERM, SO WORK W/  $\phi(x) = s^{(2-d)/2} \phi'(x')$

$$S'[\phi'] = \int d^4x' \left[ \frac{1}{2} \partial^\mu \phi' \partial_\mu \phi' - \frac{1}{2} m^2 s^2 \phi'^2 - \frac{1}{4!} \lambda s^0 \phi'^4 - \frac{1}{6!} \tau s^{-2} \phi'^6 \right]$$

GROWS AT LONG  
DISTANCE (**RELEVANT**)

CONSTANT  
(**MARGINAL**)

SHRINKS  
(**IRRELEVANT**)



# RENORMALIZABLE?

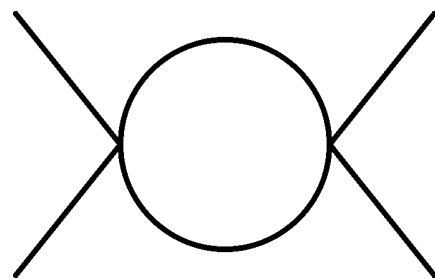
THEORIES WITH ONLY MARGINAL & RELEVANT OPERATORS ARE *RENORMALIZABLE*.  
HISTORICALLY IMPOSE RENORMALIZABILITY IN ORDER TO PRESERVE *PREDICTIVITY*.

LOOPS INTRODUCE DIVERGENCES, REMOVED W/ COUNTERTERMS. FIX COUNTERTERMS WITH DATA.

*RENORMALIZABILITY = FINITE # OF COUNTERTERMS = PREDICTIVE*

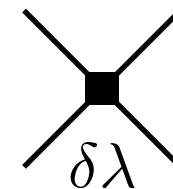
(I.E. USE SOME DATA TO FIX COUNTERTERMS, MAKE PREDICTIONS FOR OTHER MEASUREMENTS)

IN OUR EXAMPLE, ONLY  
DIVERGENCE FROM  
MARGINAL/RELEVANT  
OPERATORS IS



$$\sim \lambda^2 \int \frac{d^4 k}{k^4} \sim \lambda^2 \log \Lambda$$

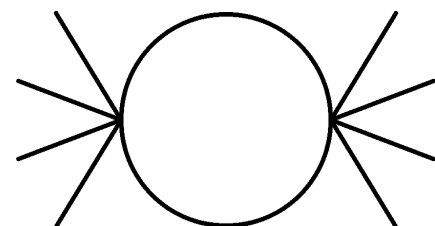
$\Rightarrow$  NEED COUNTERTERM



RENORMALIZES THE  
MARGINAL OPERATOR

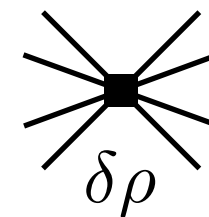
$$\lambda\phi^4$$

BUT IRRELEVANT  
OPERATOR  $\phi^6$   
GENERATES



$$\sim \tau^2 \int \frac{d^4 k}{k^4} \sim \tau^2 \log \Lambda$$

$\Rightarrow$  NEED COUNTERTERM



RENORMALIZES *NEW*  
IRRELEVANT OPERATOR

$$\rho\phi^8$$

ADDING  $\phi^8$  OPERATOR THEN GENERATES  $\phi^{10}$  OPERATOR, AND SO ON *AD INFINITUM*.

NEED INFINITE # OF MEASUREMENTS TO FIX ALL COEFFICIENTS.



# ALL IS NOT LOST

*CAN WE LIVE WITH A NONRENORMALIZABLE THEORY?*

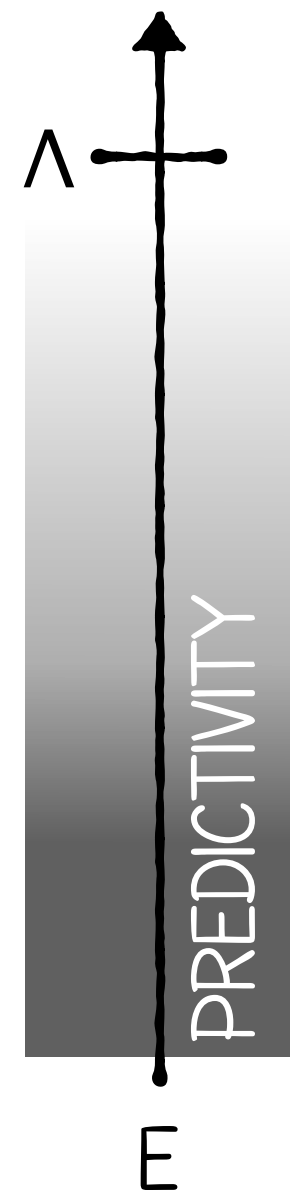
$$[d^4x] = -4 \quad [\phi] = 1 \quad [m^2] = 2 \quad [\lambda] = 0 \quad [\tau] = -2$$

$\tau$  HAS MASS DIMENSION -2. AT SOME SCALE  $\Lambda$ ,  $\tau \sim 1/\Lambda^2$ .

AT ENERGIES  $E \ll \Lambda$ , EFFECTS OF  $\phi^6$  ON  
MARGINAL/RELEVANT PHYSICS ARE  $O(E^2/\Lambda^2)$   
 $\phi^8$  EFFECTS ARE  $O(E^4/\Lambda^4)$ , AND SO ON.

IF WE ONLY STUDY PHYSICS AT  $E \ll \Lambda$ , CAN INCLUDE SOME  
IRRELEVANT OPERATORS & NEGLECT  $\phi^N$  OPERATORS AS  
LONG AS WE ONLY WORK TO  $O(E^N/\Lambda^N)$  PRECISION.  
*FINITE # OF IRRELEVANT OPERATORS =  $O(E^N/\Lambda^N)$  PREDICTIVE*

GOOD FOR  $E \ll \Lambda$ . AS WE APPROACH  $\Lambda$  ALL OPERATORS  
EQUALLY IMPORTANT, NEED UV COMPLETION





# EFFECTIVE FIELD THEORY

DESCRIBING A PHYSICAL SYSTEM REQUIRES SPECIFYING:

- **IMPORTANT DEGREES OF FREEDOM:** *IN QFT, WHAT FIELDS?*
- **IMPORTANT SYMMETRIES:** *IN QFT, WHAT INTERACTIONS?*

THIS + RENORMALIZABILITY GIVES US THE STANDARD MODEL.  
BUT WE CAN RELAX RENORMALIZABILITY IF IN ADDITION WE SPECIFY

- **EXPANSION PARAMETERS:** *IN QFT, WHAT POWER COUNTING?*

THIS LAST INGREDIENT GIVES US **EFFECTIVE FIELD THEORY**.  
POWER COUNTING IS USUALLY IN *DISTANCES/ENERGIES*.



# EFFECTIVE FIELD THEORY

TWO KINDS:

## TOP-DOWN EFT

HIGH ENERGY THEORY IS UNDERSTOOD,  
BUT USEFUL TO HAVE SIMPLER THEORY  
AT LOW ENERGIES.

$$\mathcal{L}_{High} \rightarrow \sum_n \mathcal{L}_{low}^{(n)} \quad \begin{array}{c} \text{Theory 1} \\ \downarrow \\ \text{Theory 2} \end{array}$$

INTEGRATE OUT & MATCH (MATRIX  
ELEMENTS) AT INTERMEDIATE SCALE

E.G. THEORY OF WEAK INTERACTIONS  
(FERMI EFFECTIVE THEORY). WAAAAY  
EASIER TO COMPUTE QCD CORRECTIONS.

## BOTTOM-UP EFT

UNDERLYING THEORY IS UNKNOWN  
OR MATCHING IS TOO DIFFICULT TO  
CARRY OUT

$$\sum_n \mathcal{L}_{low}^{(n)} \quad \begin{array}{c} ??? \\ \downarrow \\ \text{Theory 2} \end{array}$$

WRITE DOWN ALL INTERACTIONS  
CONSISTENT W/ SYMMETRIES.  
COUPLINGS NOT PREDICTED, BUT  
FIT TO DATA.

E.G. CHIRAL LAGRANGIAN, QUANTUM  
EINSTEIN GRAVITY, OR **STANDARD MODEL**

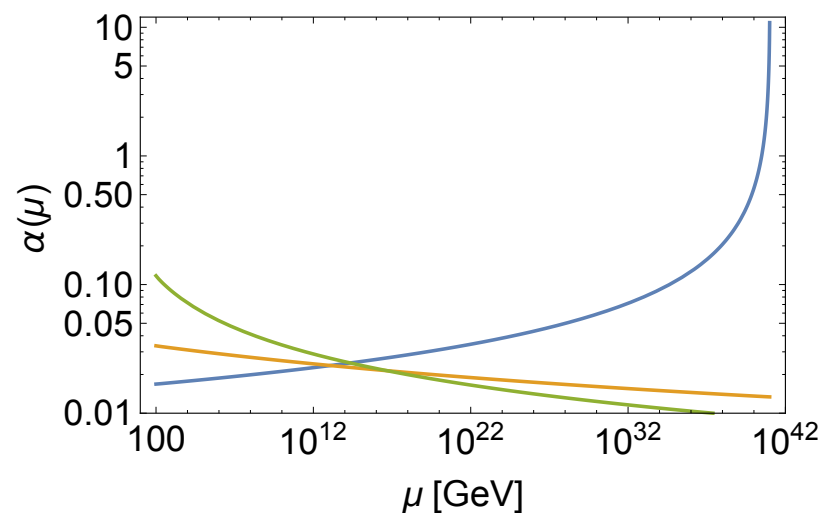


# THE STANDARD MODEL AS EFT

*IF WE LIMIT SM TO ONLY RENORMALIZABLE OPS, WHY WORRY ABOUT ALL THIS?*

THE STANDARD MODEL IS NOT UV COMPLETE.

- (1) “QUANTUM” GRAVITY CONSISTENT BUT NON-RENORMALIZABLE, DEMANDS UV COMPLETION AT THE PLANCK SCALE; PRESUMABLY ALSO INVOLVES SM\*.
- (2) WE HAVE INCONTROVERTIBLE EVIDENCE FOR ADDITIONAL FIELDS AND/OR OPERATORS BEYOND SM.



**\*WHAT IF GRAVITY DECOUPLES FROM SM IN THE UV?**

RUNNING SM GAUGE COUPLINGS INTO FAR UV EVENTUALLY GIVES LANDAU POLE IN  $U(1)_Y$ . WOULD CAUSE FERMIONS TO CONDENSE IN UV. SO UV COMPLETION OF SM IS UNAVOIDABLE!

*NOTE: NOT ALL EVIDENCE FOR BSM COMES FROM HIGH ENERGIES; THE MOST COMPELLING IS FROM SCALES AT OR BELOW THE WEAK SCALE.*



# THE STANDARD MODEL AS EFT

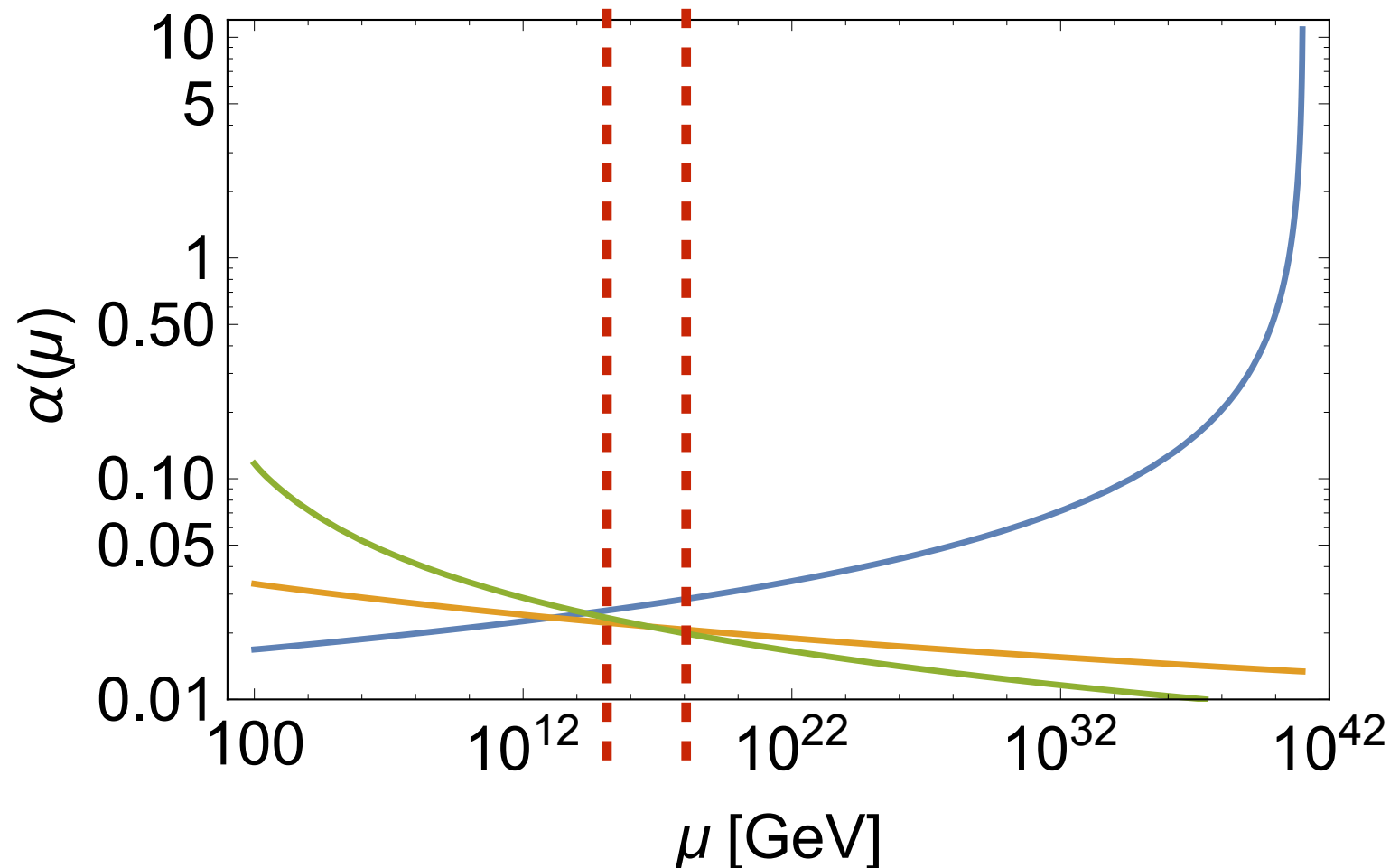
WHAT'S THE MATTER WITH HYPERCHARGE?

$$\frac{\partial \alpha_i}{\partial \ln \mu} = \beta_i = b_i \frac{\alpha_i^2}{2\pi} + \dots \Rightarrow \frac{1}{\alpha_i(\mu)} - \frac{1}{\alpha_i(m_Z)} = -\frac{b_i}{2\pi} \ln \left( \frac{\mu}{m_Z} \right) + \dots \quad \boxed{\alpha_i \equiv \frac{g_i^2}{4\pi}}$$

$$b_1 = 41/10$$

$$b_2 = -19/6$$

$$b_3 = -7$$



SIGN OF U(1) BETA FUNCTION FIXED;  
ADDITIONAL CHARGED STATES ONLY  
INCREASE COEFFICIENT. ALL NON-TRIVIAL  
U(1)'S RUN TO LANDAU POLES IN THE UV.

USUAL ASSUMPTION: RUNNING CUT OFF  
BY UNIFICATION AROUND  $10^{15}$  GEV OR  
QUANTUM GRAVITY AROUND  $10^{18}$  GEV

WITHOUT SUCH A CUTOFF, LANDAU  
POLE INEVITABLE.

# THE SMEFT

TREAT SM AS "BOTTOM-UP EFT", WRITE DOWN ALL OPERATORS CONSISTENT WITH SYMMETRIES TO GIVEN ORDER IN POWER COUNTING

**DIM-5: 1 OPERATOR\***

$$\frac{1}{\Lambda} (HL)^2$$

**DIM-6: 59+4 OPERATORS\***

SCHEMATICALLY

GAUGE BOSON OPERATORS

$$\frac{1}{\Lambda^2} |H|^2 V_{\mu\nu} V^{\mu\nu}$$

$$\frac{1}{\Lambda^2} (D^\mu V_{\mu\nu})^2$$

FOUR-FERMI OPERATORS

$$\frac{1}{\Lambda^2} (\bar{\psi} \gamma^\mu \psi) (\bar{\psi} \gamma^\mu \psi)$$

HIGGS OPERATORS

$$\frac{1}{\Lambda^2} (\partial^\mu |H|^2)^2$$

$$\frac{1}{\Lambda^2} |H^\dagger D_\mu H|^2$$

$$\frac{1}{\Lambda^2} |H|^2 |D_\mu H|^2$$

$$\frac{1}{\Lambda^2} |H|^6$$

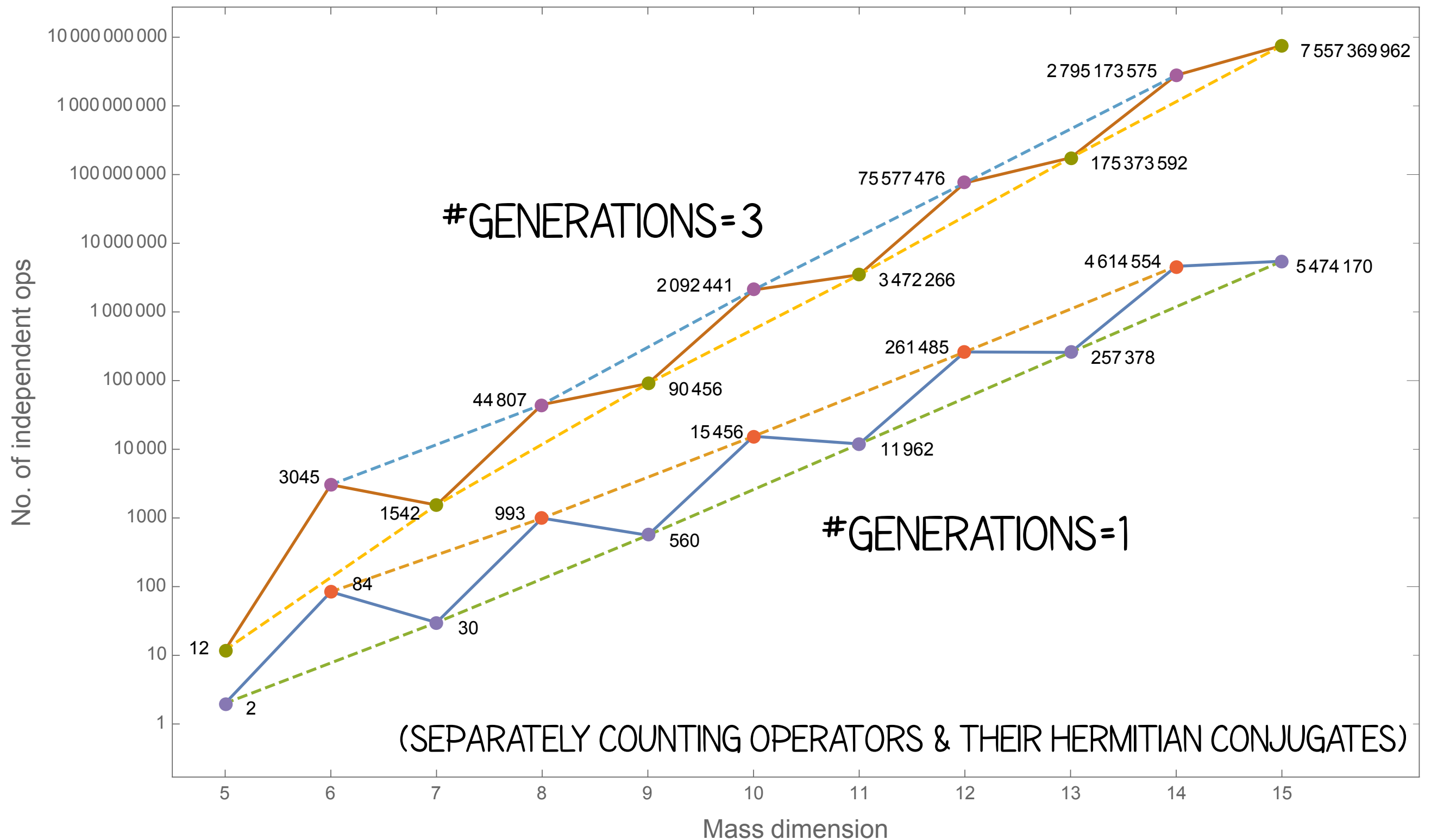
*THE GAME: FIX/CONSTRAIN COEFFICIENTS WITH DATA!*

\*NEGLECTING FLAVOR, I.E. 1 GENERATION AT A TIME.

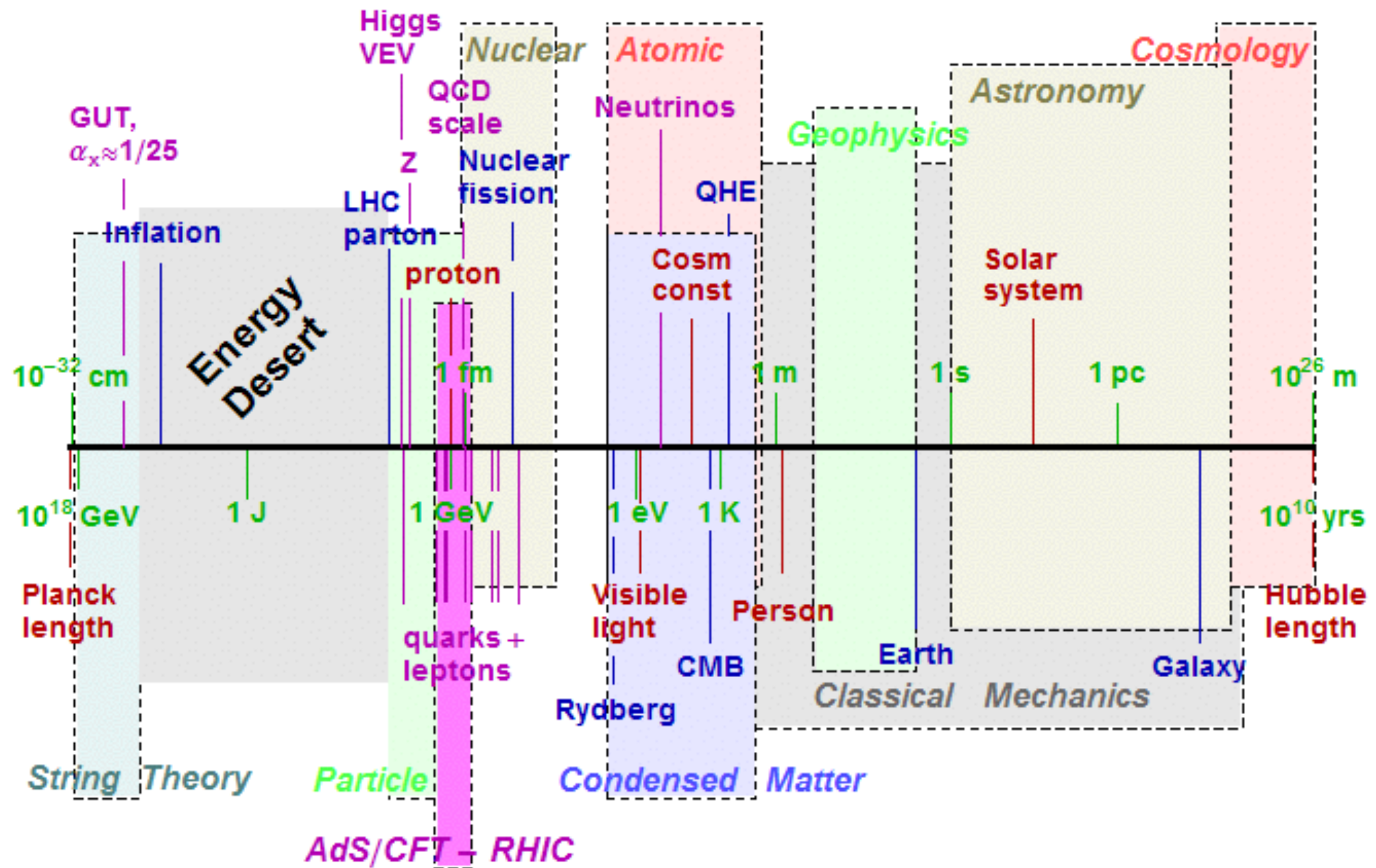


# THE SMEFT

HENNING, LU, MELIA, MURAYAMA '15



# THE DATA

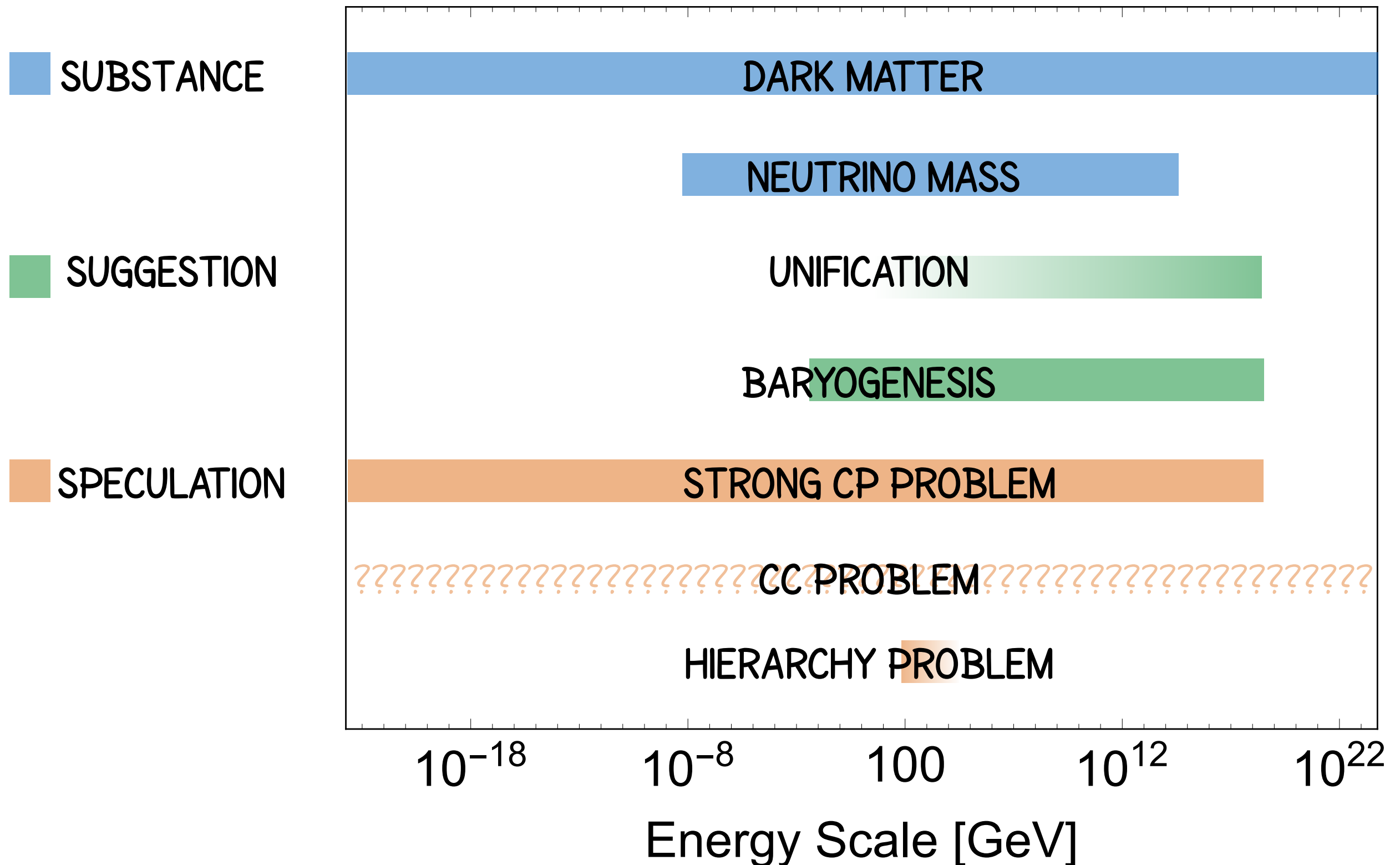


SO FAR, ONLY ONE NONZERO COEFFICIENT. MAJORITY OF BOUNDS ON SMEFT AT OR NEAR TEV SCALE; EXCEPTIONS ARISE IN SOME HIGH-PRECISION SETTINGS (E.G., FLAVOR, EDM)

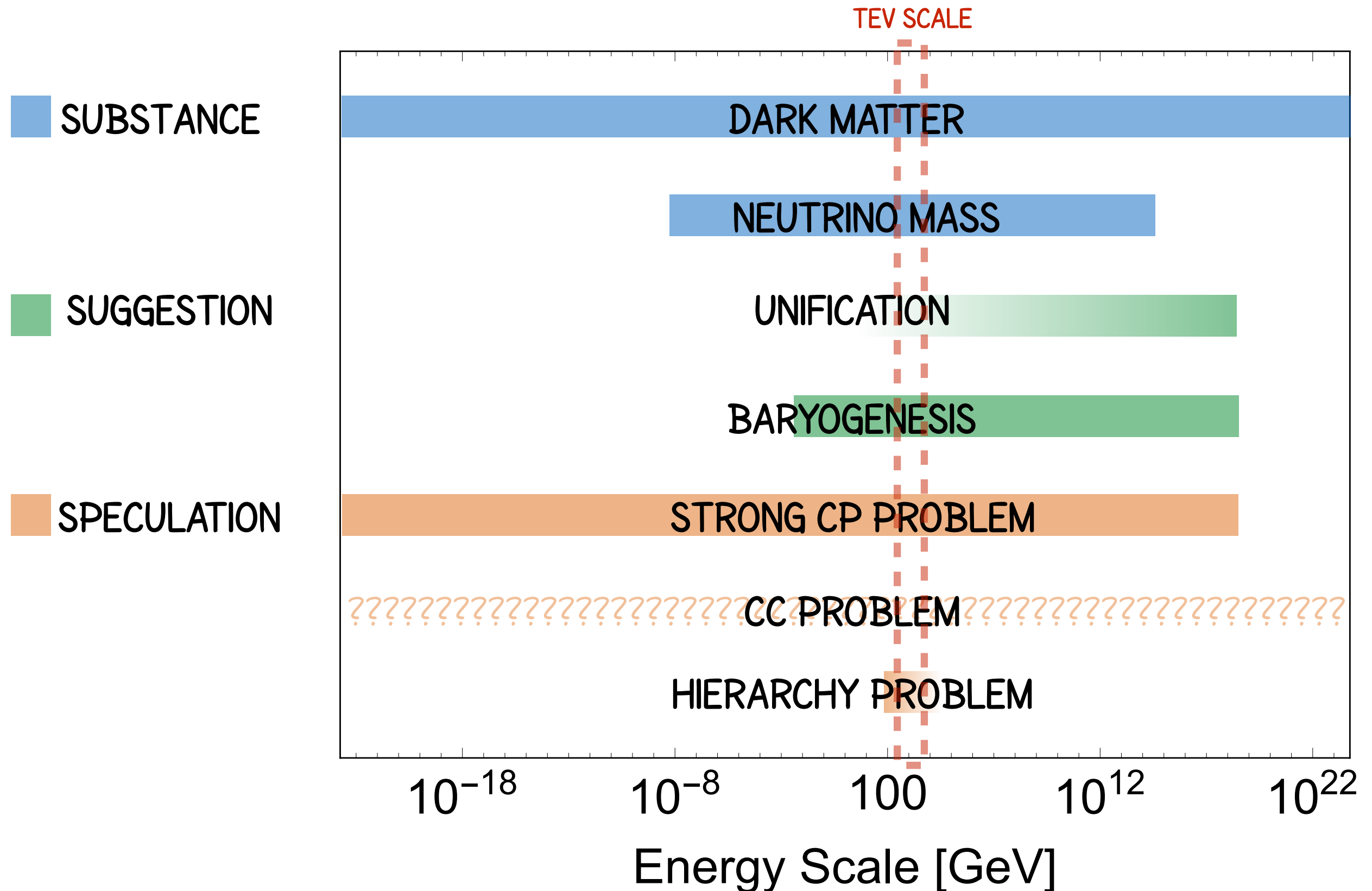


# BEYOND THE STANDARD MODEL

*LOOK FOR SPECIFIC GUIDANCE IN THE SHORTCOMINGS OF THE STANDARD MODEL*



# BEYOND THE STANDARD MODEL





A detailed illustration of a celestial scene. In the upper left, a rainbow arches over a landscape with a large wooden wheel. The sky is filled with numerous yellow stars of various sizes and a crescent moon. In the lower right, a large sun with a human-like face is visible. A large tree stands in the center, and a landscape with rolling hills, a river, and a castle is at the bottom. A figure in a red robe is lying on the ground in the lower left.

# PART 1: THE HIERARCHY PROBLEM



# NATURALNESS CRITERIA

**"DIRAC NATURAL:"** IN THEORY WITH FUNDAMENTAL SCALE  $\Lambda$ ,  
NATURAL SIZE OF OPERATOR COEFFICIENTS IS

$$c_O = \mathcal{O}(1) \times \Lambda^{4-\Delta_O}$$

*BORNE OUT COUNTLESS TIMES IN NATURE & SIMULATION.*

**"TECHNICALLY NATURAL ('T HOOFT):"** COEFFICIENTS CAN BE MUCH SMALLER  
IF THERE IS AN ENHANCED SYMMETRY WHEN THE COEFFICIENT IS ZERO.

$$c_O = \mathcal{S} \times \mathcal{O}(1) \times \Lambda^{4-\Delta_O}$$

WHERE  $\mathcal{S}$  IS A PARAMETER THAT VIOLATES SYMMETRY.

*PHILOSOPHICAL UNDERPINNING: QUANTUM CORRECTIONS RESPECT SYMMETRY; IF SYMMETRY IS BROKEN, QUANTUM CORRECTIONS PROPORTIONAL TO SYMMETRY BREAKING.*



# NATURALNESS IN NATURE

DIRAC'S QUESTION: WHY IS  $m_p \ll M_{Pl}$ ?

18 ORDERS OF MAGNITUDE!

ANSWER: QCD SCALE IS DYNAMICALLY GENERATED BY LOGARITHMIC EVOLUTION OF QCD COUPLING: "DIMENSIONAL TRANSMUTATION"

$$\frac{\partial \alpha_i}{\partial \ln \mu} = \beta_i = b_i \frac{\alpha_i^2}{2\pi} + \dots \Rightarrow \frac{1}{\alpha_3(M_{Pl})} - \frac{1}{\alpha_3(\mu)} = -\frac{b_3}{2\pi} \ln \left( \frac{M_{Pl}}{\mu} \right) + \dots \quad (\mu < M_{Pl})$$

$b_3 = -7$ , SO THERE EXISTS A SCALE WHERE  $\alpha_3 \rightarrow \infty$ : CONFINEMENT

$$\frac{1}{\alpha_3(\Lambda_{QCD})} = 0 \rightarrow \Lambda_{QCD} = M_{Pl} e^{\frac{2\pi}{b_3} \frac{1}{\alpha_s(M_{Pl})}}$$

PROTON ACQUIRES MOST OF ITS MASS FROM CONFINEMENT,  $m_p \sim \Lambda_{QCD}$

*THE DIMENSIONLESS COUPLING IS  $O(1)$ , TOTALLY NATURAL*

# NATURALNESS IN NATURE

SEE LECTURES  
BY Y. NIR

FLAVOR HIERARCHIES: LARGE RANGE OF YUKAWAS,

$$y_e/y_t \sim 10^{-5} \quad y_\nu/y_t \sim 10^{-11}$$

ANSWER: NOT DIRAC NATURAL, BUT TECHNICALLY NATURAL!

IN LIMIT  $Y \rightarrow 0$ , ENHANCED SYMMETRY OF SM:  $U(3)^5$  FLAVOR SYMMETRY

$$SU(3)_Q \times SU(3)_U \times SU(3)_D \times SU(3)_L \times SU(3)_E \\ \times U(1)_B \times U(1)_L \times U(1)_Y \times U(1)_{PQ} \times U(1)_E$$

YUKAWAS ARE SPURIONS FOR BREAKING THIS SYMMETRY:

$$Y^u \sim (3, \bar{3}, 1)_{SU(3)_q^3} \quad Y^d \sim (3, 1, \bar{3})_{SU(3)_q^3} \quad Y^e \sim (3, \bar{3})_{SU(3)_\ell^2}$$

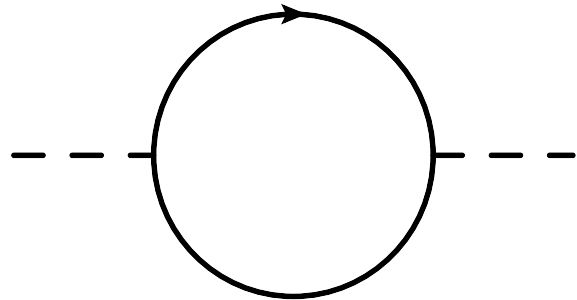
RADIATIVE CORRECTIONS TO YUKAWAS PROPORTIONAL TO YUKAWAS,  
HIERARCHIES ARE RADIATIVELY STABLE

WOULD STILL LIKE AN EXPLANATION FOR YUKAWA HIERARCHIES (E.G. FROGGATT-NIELSEN)

$$\Delta_O = 2$$

natural  $\sim \mathcal{O}(1)\Lambda^2$

# HIERARCHY PROBLEM



*OFTEN HEARD:*

"HIGGS MASS IS QUADRATICALLY DIVERGENT, STANDARD MODEL LOOPS UP TO CUTOFF  $\Lambda$  GIVE CONTRIBUTION:"

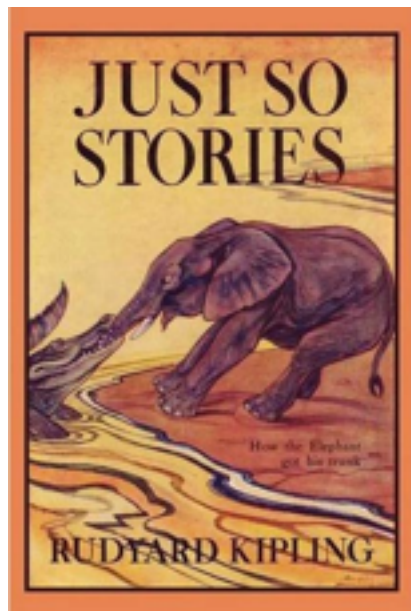
$$\delta m_H^2(\mu) = \frac{\Lambda^2}{16\pi^2} \left[ 6\lambda(\mu) + \frac{9}{4}g_2^2(\mu) + \frac{3}{4}g_Y^2(\mu) - 6\lambda_t^2(\mu) \right]$$

BUT THEN YOU REMEMBER: DIVERGENCES ARE NOT PHYSICAL, WE INTRODUCE COUNTERTERMS TO ABSORB THEM AND USE DATA TO FIX THE COUPLINGS!

WHY NOT CANCEL DIVERGENCE WITH COUNTERTERM? OR BETTER YET, USE A REGULARIZATION & RENORMALIZATION SCHEME WITHOUT DIVERGENCES, E.G. DIMENSIONAL REGULARIZATION WITH MINIMAL SUBTRACTION?

*NOT THE ACTUAL PROBLEM. "QUADRATIC DIVERGENCE" IS AN INDICATION OF THE PROBLEM, BUT NOT THE PROBLEM ITSELF...*





# SCALARS ARE SPECIAL

MASS NEITHER NATURAL NOR TECHNICALLY NATURAL IN SM,  
HIERARCHY PROBLEM IS NOT A "JUST-SO STORY"

FIELD

SYMMETRY AS  $m \rightarrow 0$

IMPLICATION

SPIN-1/2

$$m \Psi \bar{\Psi}$$

$$\Psi \rightarrow e^{i\alpha\gamma_5} \Psi$$

(CHIRAL SYMMETRY)

$$\delta m \propto m$$

NATURAL!

SPIN-1

$$m^2 A_\mu A^\mu$$

$$A_\mu \rightarrow A_\mu + \partial_\mu \alpha$$

(GAUGE INVARIANCE)

$$\delta m \propto m$$

NATURAL!

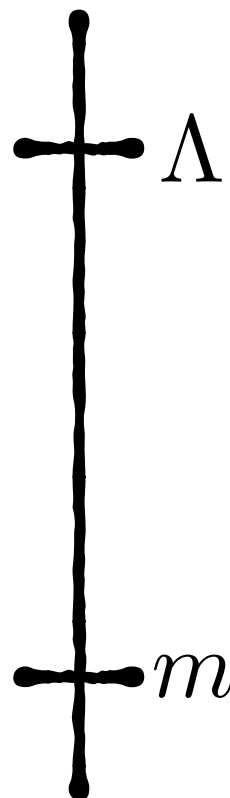
SPIN-0

$$m^2 |H|^2$$

NONE

$$\delta m \propto \Lambda$$

UNNATURAL!



# TWO DEGREES OF DANGER

$$\delta m_H^2(\mu) = \frac{\Lambda^2}{16\pi^2} \left[ 6\lambda(\mu) + \frac{9}{4}g_2^2(\mu) + \frac{3}{4}g_Y^2(\mu) - 6\lambda_t^2(\mu) \right]$$

1. **THE STRONG FORM OF THE HIERARCHY PROBLEM:** FUNDAMENTAL THEORY IS *FINITE*. DIVERGENCES IN AN EFFECTIVE THEORY ARE PHYSICAL (E.G. CUTOFF = LATTICE SPACING), COUNTERTERMS JUST IMPLEMENT TUNING. “QUADRATIC DIVERGENCE” IN SMEFT IS A DIRECT MEASURE OF FINE TUNING.
2. **THE WEAK FORM OF THE HIERARCHY PROBLEM:** LET US ONLY SPEAK OF OBSERVABLE QUANTITIES LIKE POLE MASSES. DIVERGENCES ARE UNPHYSICAL. THE “QUADRATIC DIVERGENCE” IN THE SMEFT IS A STAND-IN FOR FINITE THRESHOLD CORRECTIONS FROM *POSSIBLE* NEW PHYSICS.

STRONG FORM HOLDS TRUE IN ALL KNOWN EXTENSIONS OF THE STANDARD MODEL THAT ARE FINITE (E.G. SUPERSYMMETRY, STRING THEORY), I.E., WHEREVER THE HIGGS MASS CAN BE *PREDICTED*.

*BUT EVEN THE WEAK FORM POSES AN IMMENSE DANGER.*

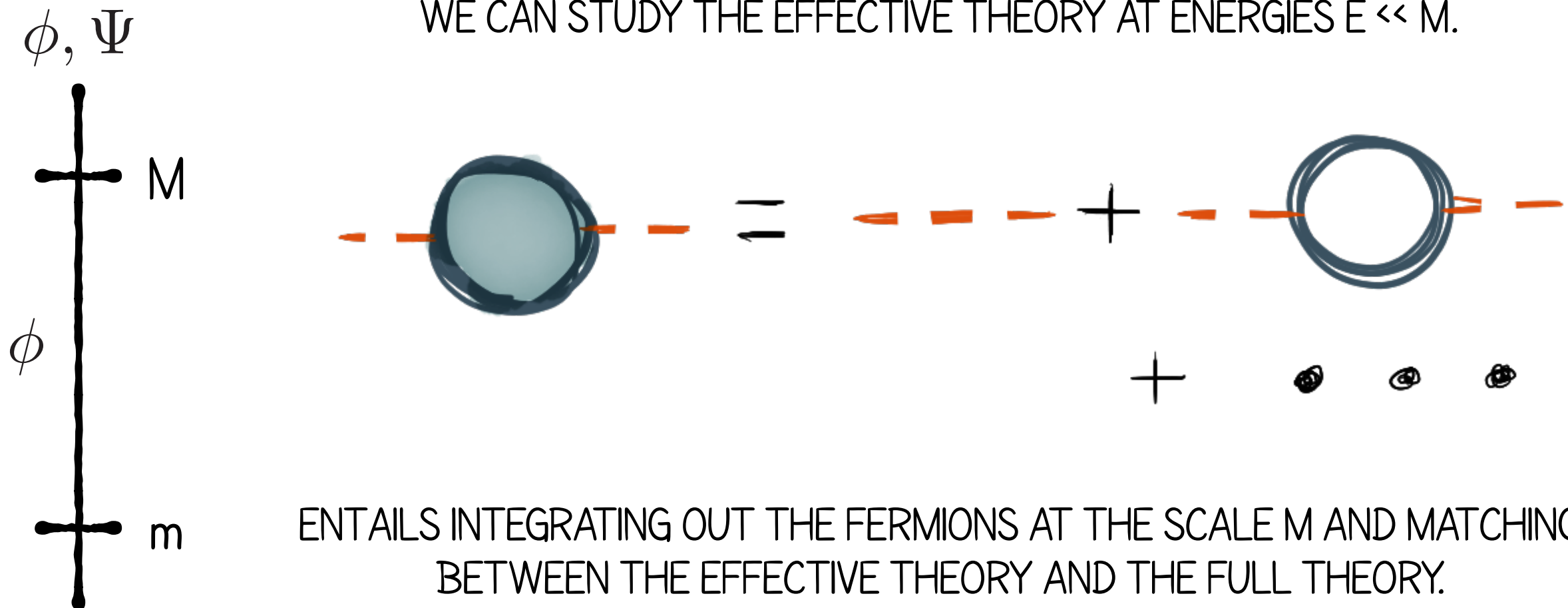
# (WEAK) HIERARCHY PROBLEM

CONSIDER A TOY MODEL WITH A SCALAR AND DIRAC FERMION:

$$\mathcal{L} = \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m^2 \phi^2 - \frac{\lambda}{4!} \phi^4 + \bar{\Psi} i \not{\partial} \Psi - M \bar{\Psi} \Psi + y \phi \bar{\Psi} \Psi$$

IMAGINE WE ARRANGE FOR THE SCALAR TO BE MUCH LIGHTER,  $m \ll M$ .

WE CAN STUDY THE EFFECTIVE THEORY AT ENERGIES  $E \ll M$ .





# (WEAK) HIERARCHY PROBLEM

COMPUTE SCALAR MASS IN THE EFFECTIVE THEORY WITH A HARD MOMENTUM CUTOFF  $\Lambda$ :

$$m_{eff}^2 = m^2 + \frac{y^2}{16\pi^2} \left[ c_1 \Lambda^2 + c_2 m^2 \ln \frac{\Lambda}{\mu} + c_3 M^2 + \mathcal{O}(M^4/\Lambda^2) \right]$$


OR COMPUTED USING DIMENSIONAL REGULARIZATION IN  $4-\epsilon$  DIMENSIONS WITH MINIMAL SUBTRACTION:

$$m_{eff}^2 = m^2 + \frac{y^2}{16\pi^2} \left[ \frac{c_2}{\epsilon} m^2 + c_3 M^2 + \mathcal{O}(\epsilon) \right]$$

IN BOTH CASES, CAN WRITE THE ANSWER IN TERMS OF THE RENORMALIZED MASS  $m^2(\mu=M)$ :

$$m_{eff}^2(\mu = M) = m^2(\mu = M) + \frac{c_3 y^2}{16\pi^2} M^2$$

FINITE THRESHOLD  
CORRECTION



NO DEPENDENCE ON CUTOFF, BUT DEPENDENCE ON  $M$ .

# (WEAK) HIERARCHY PROBLEM

$$m_{eff}^2(\mu = M) = m^2(\mu = M) + \frac{c_3 y^2}{16\pi^2} M^2$$

SCALAR WANTS TO BE WITHIN A LOOP FACTOR OF THE DIRAC FERMION. **TO KEEP SCALAR LIGHTER, NEED TO TUNE RENORMALIZED PARAMETERS OF THE FULL THEORY SO THERE IS A CANCELLATION ON THE RHS.**

THIS REQUIRES A TUNING OF ORDER  $\frac{y^2}{16\pi^2} \frac{M^2}{m^2}$

SEE FINE-TUNING IN TERMS OF RENORMALIZED PARAMETERS, INDEPENDENT OF REGULATOR; APPARENT EVEN IN DIM. REG. WHERE THERE ARE NO QUADRATIC DIVERGENCES.

THE INTUITION ABOUT QUADRATIC DIVERGENCES IS CORRECT IF WE ASSOCIATE  $\Lambda \sim M$ , I.E., CUTOFF  $\sim$  THRESHOLD.

$$\delta m_H^2 \propto \frac{y^2}{16\pi^2} \Lambda^2$$

# (NO FERMIONIC PROBLEM)

IMAGINE WE RAN THE LOGIC IN THE OTHER DIRECTION:  
MAKE THE SCALAR HEAVY, STUDY THE LIGHT FERMION

$$\mathcal{L} = \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}m^2 \phi^2 - \frac{\lambda}{4!} \phi^4 + \bar{\Psi} i \not{\partial} \Psi - M \bar{\Psi} \Psi + y \phi \bar{\Psi} \Psi$$

E.G. DIMENSIONAL REGULARIZATION IN  $4 - \epsilon$  DIMENSIONS WITH MINIMAL SUBTRACTION:

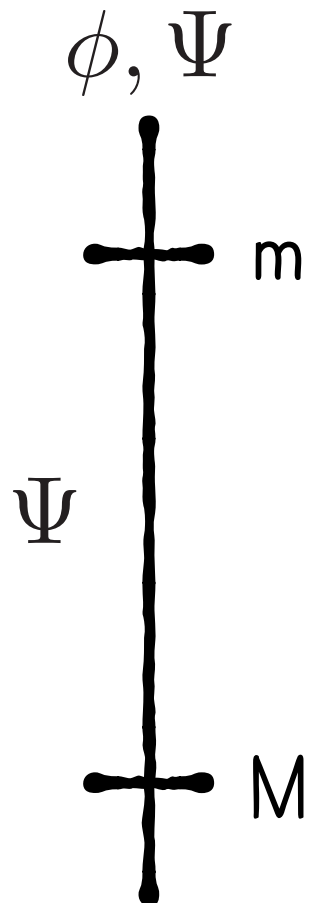
$$M_{eff} = M + \frac{y^2}{16\pi^2} \left[ \frac{c_2}{\epsilon} M + c_3 M + \mathcal{O}(\epsilon, M/m) \right]$$

CORRECTIONS PROPORTIONAL TO FERMION MASS, VANISH  
IN THE LIMIT  $M \rightarrow 0$ . DUE TO THE CHIRAL SYMMETRY

$$\Psi \rightarrow e^{i\alpha\gamma_5} \Psi$$

NO LARGE THRESHOLD CORRECTIONS MATCHING TO UV THEORY W/ SCALAR

NOTE: WORKS ONLY IF  $M$  IS THE ONLY SOURCE OF CHIRAL SYMMETRY BREAKING.



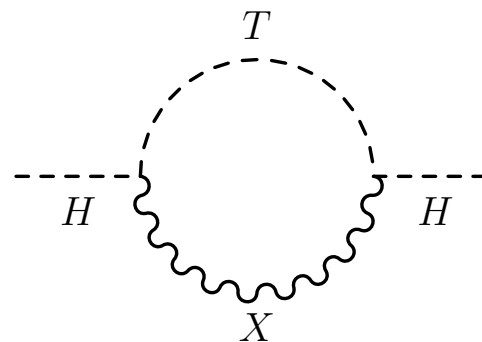


# BSM CREATES A PROBLEM

MOTIVATED BSM THEORY INTRODUCES THESE CORRECTIONS TO THE HIGGS.

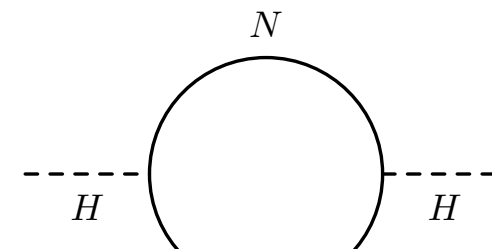
## UNIFICATION

FINITE CORRECTIONS FROM LOOPS OF HEAVY GAUGE BOSONS/HIGGS TRIPLETS.



$$\delta m_H^2 \sim \frac{\alpha_{GUT}}{4\pi} M_{GUT}^2$$

## NEUTRINOS

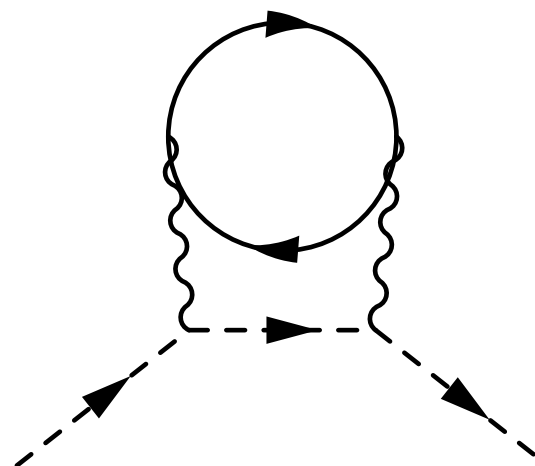


FINITE CORRECTIONS FROM LEPTON + RHN

$$\delta m_H^2 = -\frac{1}{4\pi^2} \sum_{ij} |y_{ij}|^2 M_j^2$$

## DARK MATTER

FINITE CORRECTIONS AT TWO LOOPS FROM WIMP DARK MATTER (I.E. LIVES IN SU(2) MULTIPLET)



$$\delta m_H^2 \sim \left(\frac{\alpha}{4\pi}\right)^2 \times g \left(\frac{m_W^2}{m_\Psi^2}\right) \times m_\Psi^2$$

Quantum numbers SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	Spin	DM could decay into	DM mass in TeV	$m_{DM^\pm} - m_{DM}$ in MeV	Finite naturalness bound in TeV	$\sigma_{SI}$ in $10^{-46} \text{ cm}^2$
2	1/2	0	$EL$	0.54	350	$0.4 \times \sqrt{\Delta}$	$(0.4 \pm 0.6) 10^{-3}$
2	1/2	1/2	$EH$	1.1	341	$1.9 \times \sqrt{\Delta}$	$(0.3 \pm 0.6) 10^{-3}$
3	0	0	$HH^*$	$2.0 \rightarrow 2.5$	166	$0.22 \times \sqrt{\Delta}$	$0.12 \pm 0.03$
3	0	1/2	$LH$	$2.4 \rightarrow 2.7$	166	$1.0 \times \sqrt{\Delta}$	$0.12 \pm 0.03$
3	1	0	$HH, LL$	$1.6 \rightarrow ?$	540	$0.22 \times \sqrt{\Delta}$	$0.001 \pm 0.001$
3	1	1/2	$LH$	$1.9 \rightarrow ?$	526	$1.0 \times \sqrt{\Delta}$	$0.001 \pm 0.001$
4	1/2	0	$HHH^*$	$2.4 \rightarrow ?$	353	$0.14 \times \sqrt{\Delta}$	$0.27 \pm 0.08$
4	1/2	1/2	$(LHH^*)$	$2.4 \rightarrow ?$	347	$0.6 \times \sqrt{\Delta}$	$0.27 \pm 0.08$
4	3/2	0	$HHH$	$2.9 \rightarrow ?$	729	$0.14 \times \sqrt{\Delta}$	$0.15 \pm 0.07$
4	3/2	1/2	$(LHH)$	$2.6 \rightarrow ?$	712	$0.6 \times \sqrt{\Delta}$	$0.15 \pm 0.07$
5	0	0	$(HHH^*H^*)$	$5.0 \rightarrow 9.4$	166	$0.10 \times \sqrt{\Delta}$	$1.0 \pm 0.2$
5	0	1/2	stable	$4.4 \rightarrow 10$	166	$0.4 \times \sqrt{\Delta}$	$1.0 \pm 0.2$
7	0	0	stable	$8 \rightarrow 25$	166	$0.06 \times \sqrt{\Delta}$	$4 \pm 1$

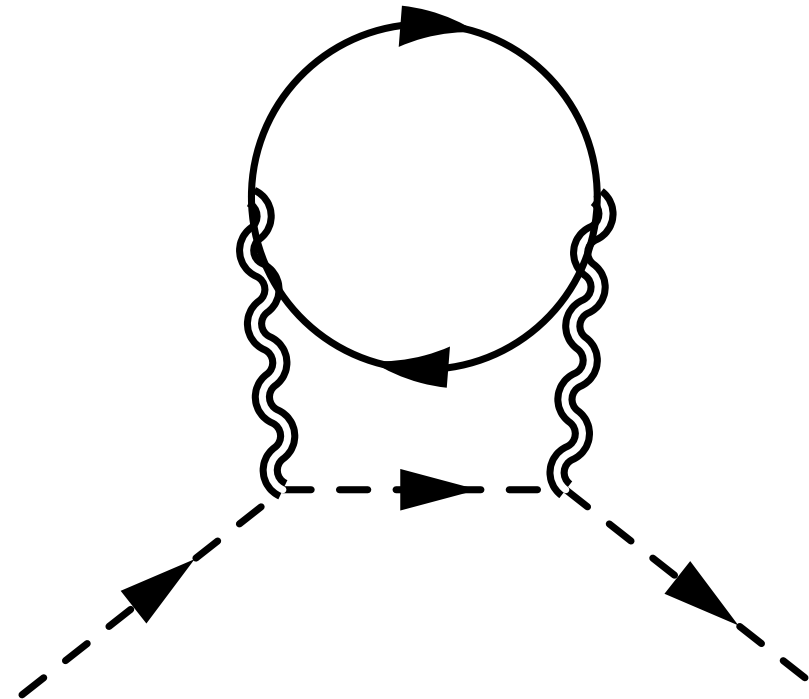
# GRAVITY IS WORSE

DON'T KNOW THE THEORY OF QUANTUM GRAVITY, BUT REASONABLE TO SUPPOSE IT CONTAINS NEW STATES WHOSE MASSES ARE OF ORDER  $M_{Pl}$

CONSIDER E.G. A HEAVY FERMION THAT ONLY COUPLES TO THE HIGGS THROUGH LOOPS OF GRAVITONS.

(CAN COMPUTE THIS USING QUANTUM GRAVITY EFT)

$$\delta m_H^2 \sim \frac{m_H^2}{(16\pi^2)^2} \frac{m_\Psi^4}{M_{Pl}^4}$$



HEY WAIT, THAT'S NOT SO BAD!

(SMALL BECAUSE THE GRAVITON COUPLING TO A MASSLESS, ON-SHELL PARTICLE AT ZERO MOMENTUM VANISHES, SO RESULT IS PROPORTIONAL TO  $M_H$ )

# GRAVITY IS WORSE

LET'S GO TO THREE LOOPS, SO THE GRAVITON COUPLES VIA A LOOP OF TOP QUARKS. TOP QUARKS ARE OFF SHELL, SO COUPLING NOT SUPPRESSED

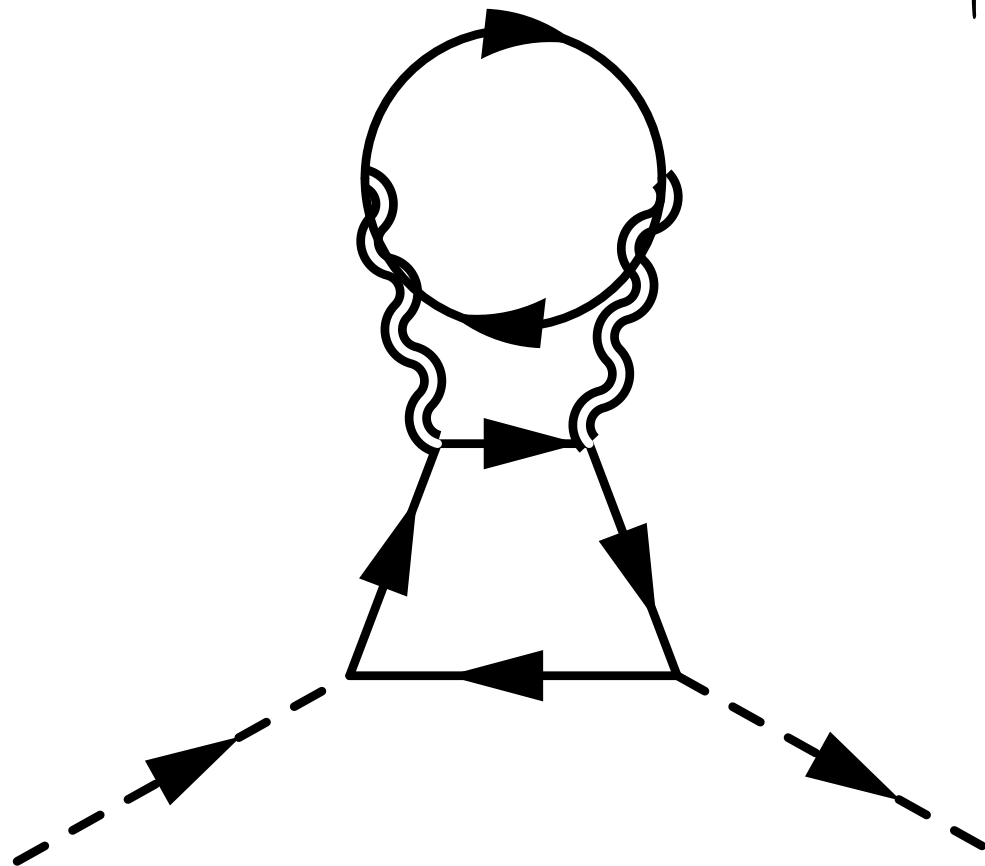
NOW WE FIND A CORRECTION PROPORTIONAL TO MASS OF THE HEAVY FERMION,

$$\delta m_H^2 \sim \frac{6y_t^2}{(16\pi^2)^3} \frac{m_\Psi^6}{M_{Pl}^4}$$

SUMMING OVER ALL SM PARTICLES IN THE LOOP, THIS LOOKS LIKE OUR NAIVE ONE-LOOP QUADRATIC DIVERGENCE CALCULATION WITH

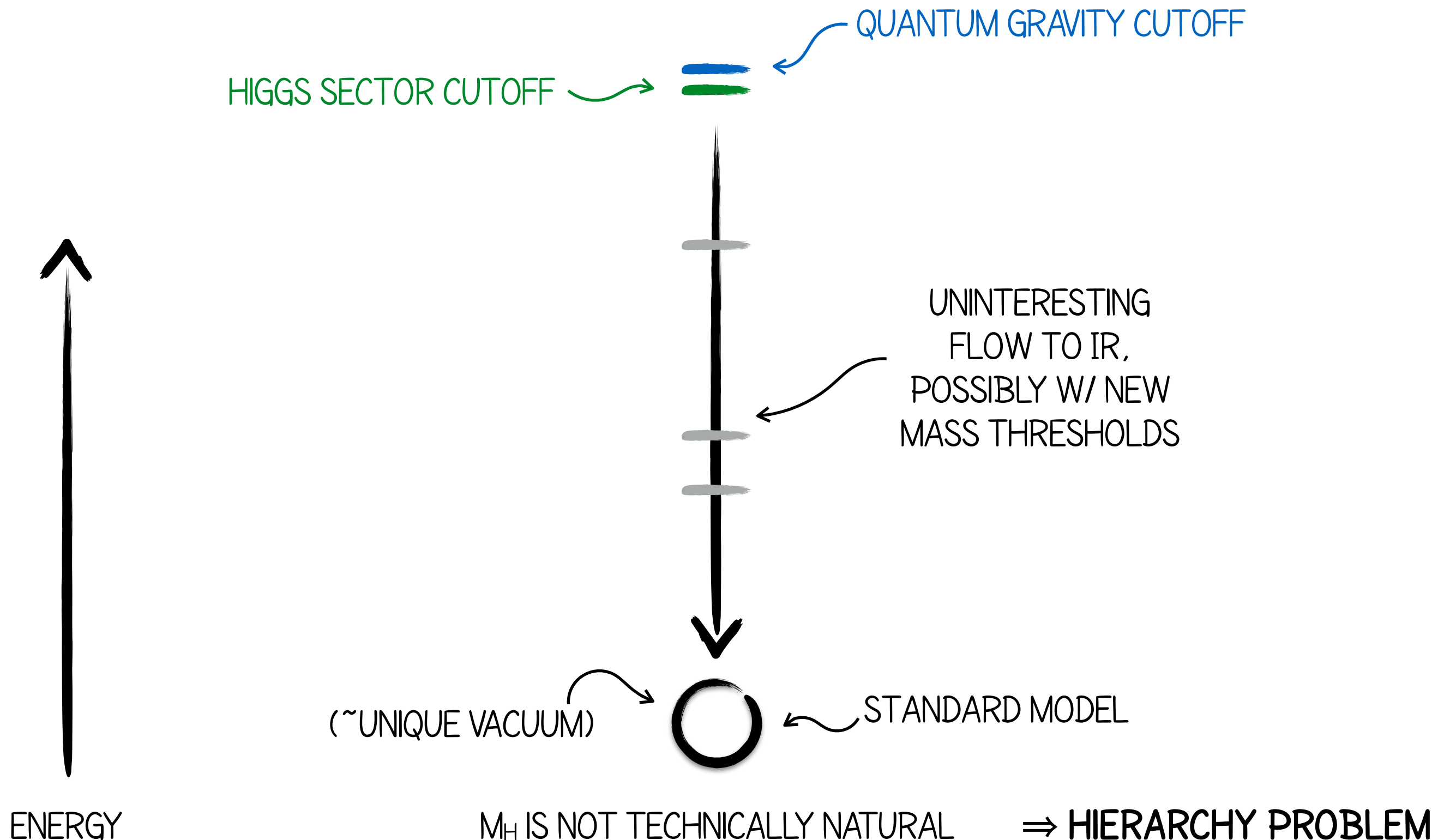
$$\Lambda \sim M_{Pl}/16\pi^2$$

SO EVEN HEAVY STUFF WITH PURELY GRAVITATIONAL COUPLINGS TO SM GIVES LARGE FINITE CORRECTIONS.





# THE HIERARCHY PROBLEM



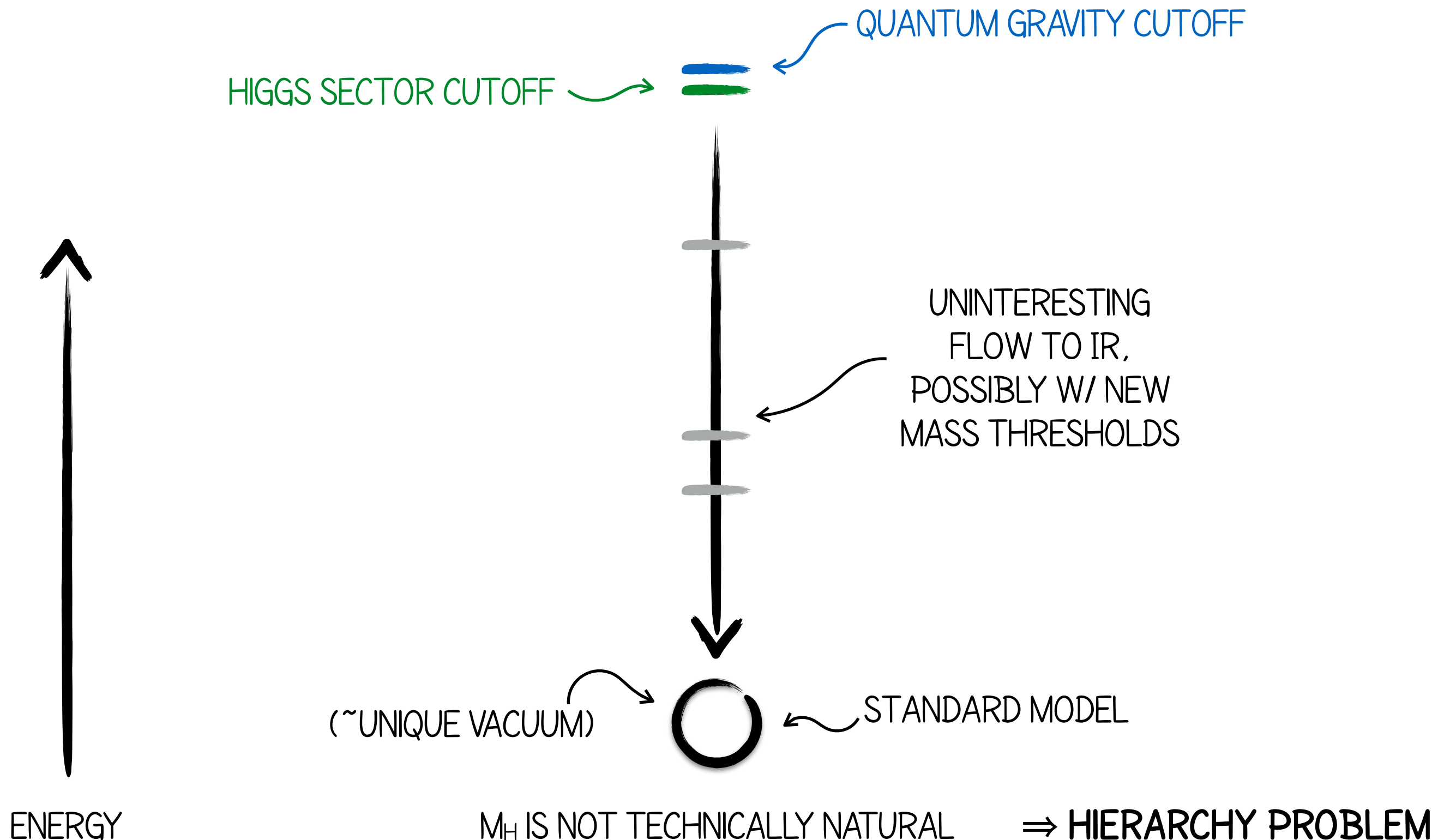




# PART 2: HIERARCHY SOLUTIONS



# THE HIERARCHY PROBLEM



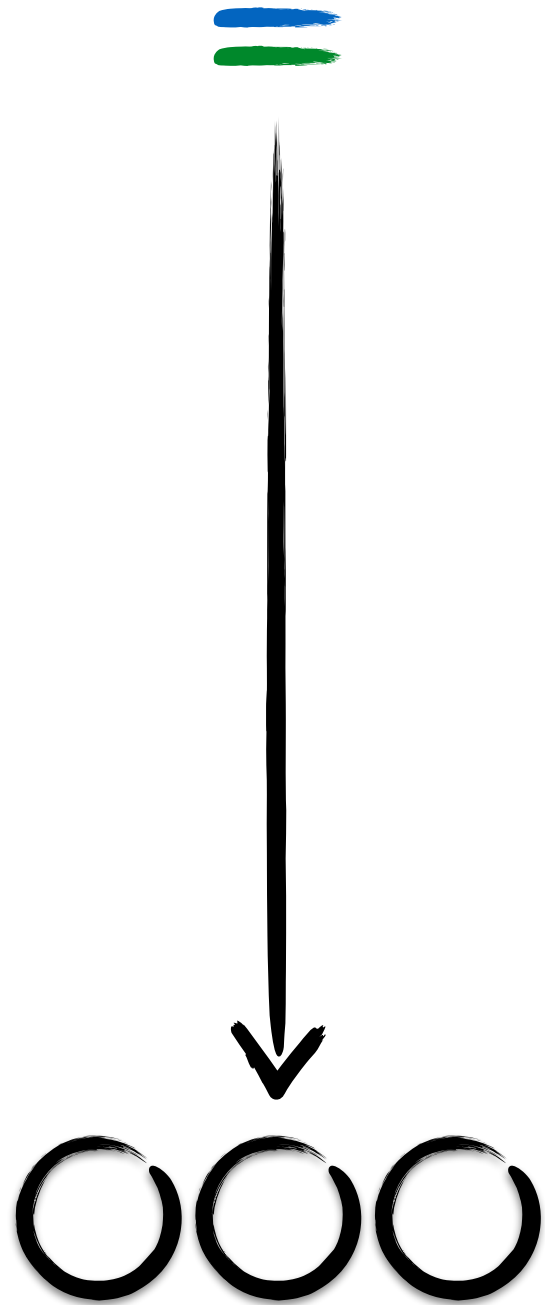


# SELECTING A VACUUM

VACUUM IS ONE OF MANY; END UP IN OBSERVED VACUUM THROUGH SOME CONSTRAINT.

## 1. ANTHROPICS

- LIGHTNESS OF THE HIGGS RESULTS FROM FINELY TUNED CANCELLATION.
- EXPLICABLE W/ ANTHROPIC REASONING: THERE IS A LANDSCAPE OF VACUA ACROSS WHICH THE HIGGS MASS VARIES, BUT ONLY LOW/ TUNED HIGGS MASSES ARE COMPATIBLE WITH OBSERVERS.
- PLAUSIBILITY DEPENDS STRONGLY ON WHAT QUANTITIES YOU ASSUME ARE ALLOWED TO VARY OVER THE LANDSCAPE!
- EVEN IF THERE IS A MULTIVERSE & ANTHROPIC PRESSURE, WHY SHOULD THE UNIVERSE BOTHER WITH AN ELEMENTARY SCALAR? TECHNICOLOR WOULD HAVE WORKED JUST FINE.



# (ANTHROPIC ASIDE)

- FOR EXAMPLE, YOU CAN IMAGINE AN ANTHROPIC PRESSURE IN A MULTIVERSE WHERE THE HIGGS MASS/VEV VARIES BUT DIMENSIONLESS COUPLINGS (YUKAWAS) ARE HELD FIXED.

- WHEN  $V \ll V_{SM}$ , **PROTONS DECAY INTO NEUTRONS** SINCE

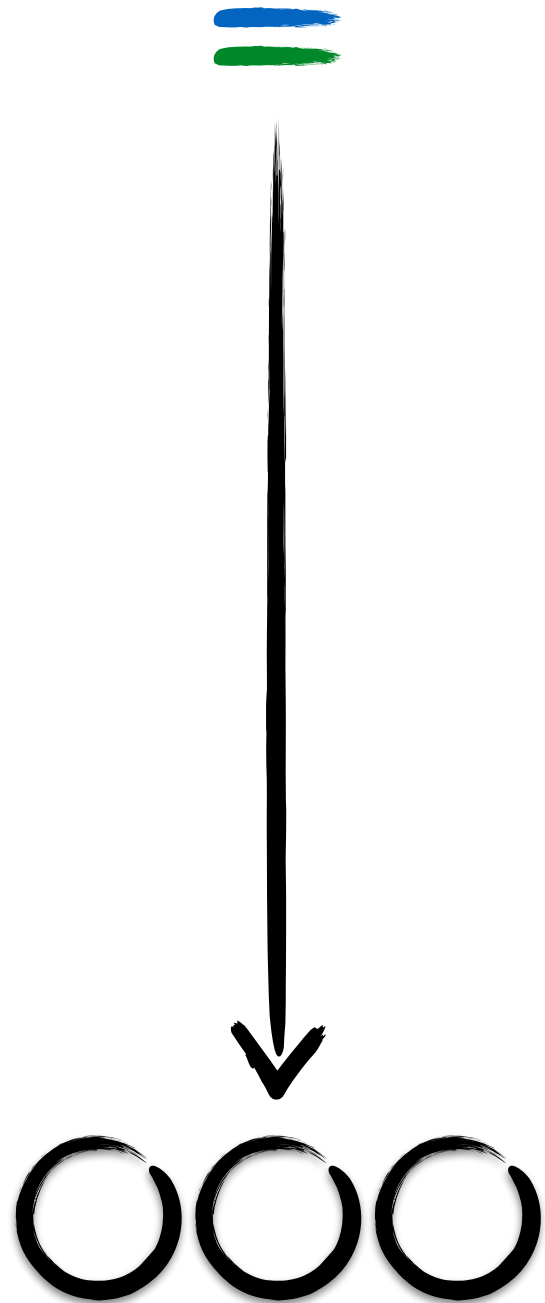
$$m_n - m_p = (3v/v_{SM} - 1.7) \text{ MeV}$$

- WHEN  $V \gg V_{SM}$ , **THE NEUTRON IS NO LONGER STABLE** WITHIN NUCLEI BECAUSE THE NEUTRON-PROTON MASS SPLITTING EXCEEDS THE NUCLEAR BINDING ENERGY:

$$m_n - m_p > B_d$$


- PROVIDES AN ANTHROPIC PRESSURE FOR  $V \sim V_{SM}$ , UNDER THE ASSUMPTION THAT ONLY THE VEV VARIES.

- BUT **NOT AN EXPLANATION** IF YUKAWAS CAN VARY, OR IF THERE CAN BE EXTRA GAUGE GROUPS.

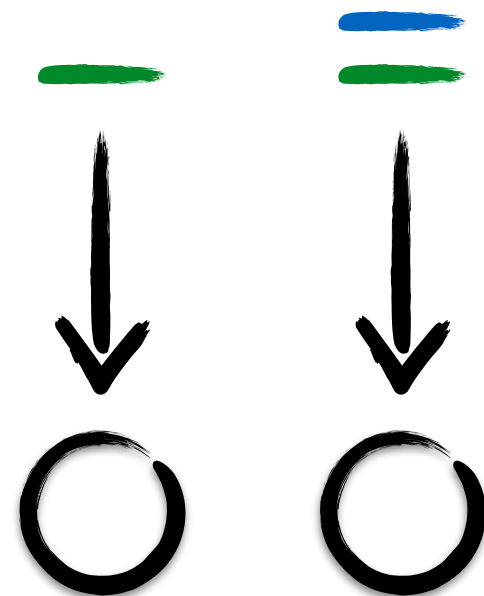


# LOWERING THE CUTOFF

...IN DIVERSE DIMENSIONS

- 
1. RANDALL-SUNDRUM / TECHNICOLOR
  2. LARGE EXTRA DIMENSIONS /  $10^{32} \times \text{SM}$
  3. LITTLE STRING THEORY

- THE 4D UV CUTOFF (HIGGS ALONE, OR WHOLE SM) IS EXTREMELY LOW, AROUND 1 TEV



- FLAVOR PHYSICS HAPPENS HERE (HIGGS OR WHOLE SM CUTOFF), ALSO QUANTUM GRAVITY & ALL OTHER UV PHYSICS (SM CUTOFF)
- PROBLEM: SEEN A HIGGS + MASS GAP (LIMITS IN THE FEW TEV RANGE FROM DIRECT SEARCHES, MUCH HIGHER FOR FLAVOR/PRECISION ELECTROWEAK). NO INDICATION THE SM OR EVEN JUST HIGGS HAS CUTOFF AT THE TEV SCALE.

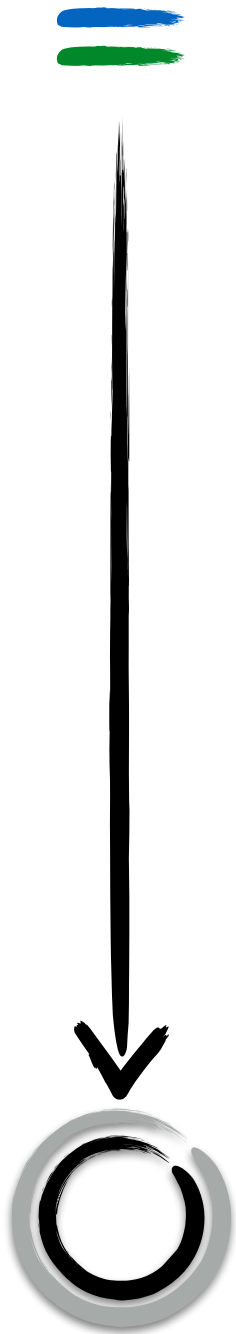


# ADDING A SYMMETRY

EXTEND THE SM WITH A SYMMETRY THAT  
MAKES HIGGS MASS TECHNICALLY NATURAL

1. SUPERSYMMETRY
2. GLOBAL SYMMETRY

- THE 4D UV CUTOFF (HIGGS ALONE, OR WHOLE SM) CAN BE HIGH, BUT SYMMETRY MUST BE VALID DOWN TO LOW SCALES
- SYMMETRY MUST BE BROKEN IN A WAY THAT DOESN'T REINTRODUCE UV SENSITIVITY; PREDICTS NEW PARTICLES
- WEAKLY COUPLED REALIZATIONS ALLOW A FINITE MASS GAP BETWEEN HIGGS AND NEW STATES.



# WHAT'S THE SCALE?

IF HIERARCHY PROBLEM IS SOLVED, WHERE DOES A NEW SYMMETRY OR CUTOFF ENTER?

QUANTIFY SENSITIVITY OF HIGGS MASS TO NEW PHYSICS VIA RATIO

$$\Delta \equiv \frac{2\delta m_H^2}{m_h^2}$$

A *GUIDEPOST* TO WHERE NEW PHYSICS SHOULD ENTER; IN THE SM WITH A UNIFORM CUTOFF  $\Lambda$ , SM LOOPS UP TO  $\Lambda$  GIVE

$$\delta m_H^2(\mu) = \frac{\Lambda^2}{16\pi^2} \left[ 6\lambda(\mu) + \frac{9}{4}g_2^2(\mu) + \frac{3}{4}g_Y^2(\mu) - 6\lambda_t^2(\mu) \right]$$

EXPECT NEW PHYSICS TO ENTER AND ALTER SM AT SOME SCALE\*

$\Delta \lesssim 1$  (NO TUNING) REQUIRES  $\Lambda \lesssim 500$  GEV;

$\Delta \lesssim 10$  (10%-LEVEL TUNING) REQUIRES  $\Lambda \lesssim 1.6$  TEV;

$\Delta \lesssim 100$  (1%-LEVEL TUNING) REQUIRES  $\Lambda \lesssim 5$  TEV.

\*BEST-CASE SCENARIO, NO LARGE LOGS

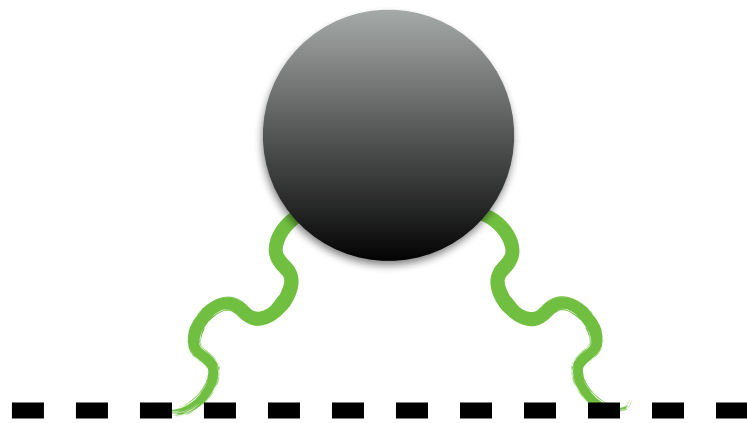
# THE NATURALNESS STRATEGY

THIS IS A *STRATEGY* FOR NEW PHYSICS NEAR  $M_H$ , NOT A *NO-LOSE THEOREM*,  
BECAUSE THE THEORY DOES NOT BREAK DOWN IF IT IS UNNATURAL.

BUT NATURALNESS HAS OFTEN BEEN A VERY *SUCCESSFUL* STRATEGY.  
WE HAVE OTHER SCALARS IN NATURE, THANKS TO QCD.

*E.G. CHARGED PIONS*

PIONS ARE GOLDSTONES, BUT ELECTROMAGNETISM EXPLICITLY  
BREAKS GLOBAL SYMMETRY.



ELECTROMAGNETIC CONTRIBUTION TO THE CHARGED PION MASS  
SENSITIVE TO THE CUTOFF OF THE PION EFT.

$$m_{\pi^\pm}^2 - m_{\pi^0}^2 = \frac{3\alpha}{4\pi} \Lambda^2$$

$$m_{\pi^\pm}^2 - m_{\pi^0}^2 = (35.5 \text{ MeV})^2 \Rightarrow \Lambda < 850 \text{ MeV}$$

RHO MESON (NEW PHYSICS!) ENTERS AT 770 MEV:  $\Delta \sim 1$



# POSSIBLE SYMMETRIES

WHAT SYMMETRIES MIGHT WE EMPLOY?

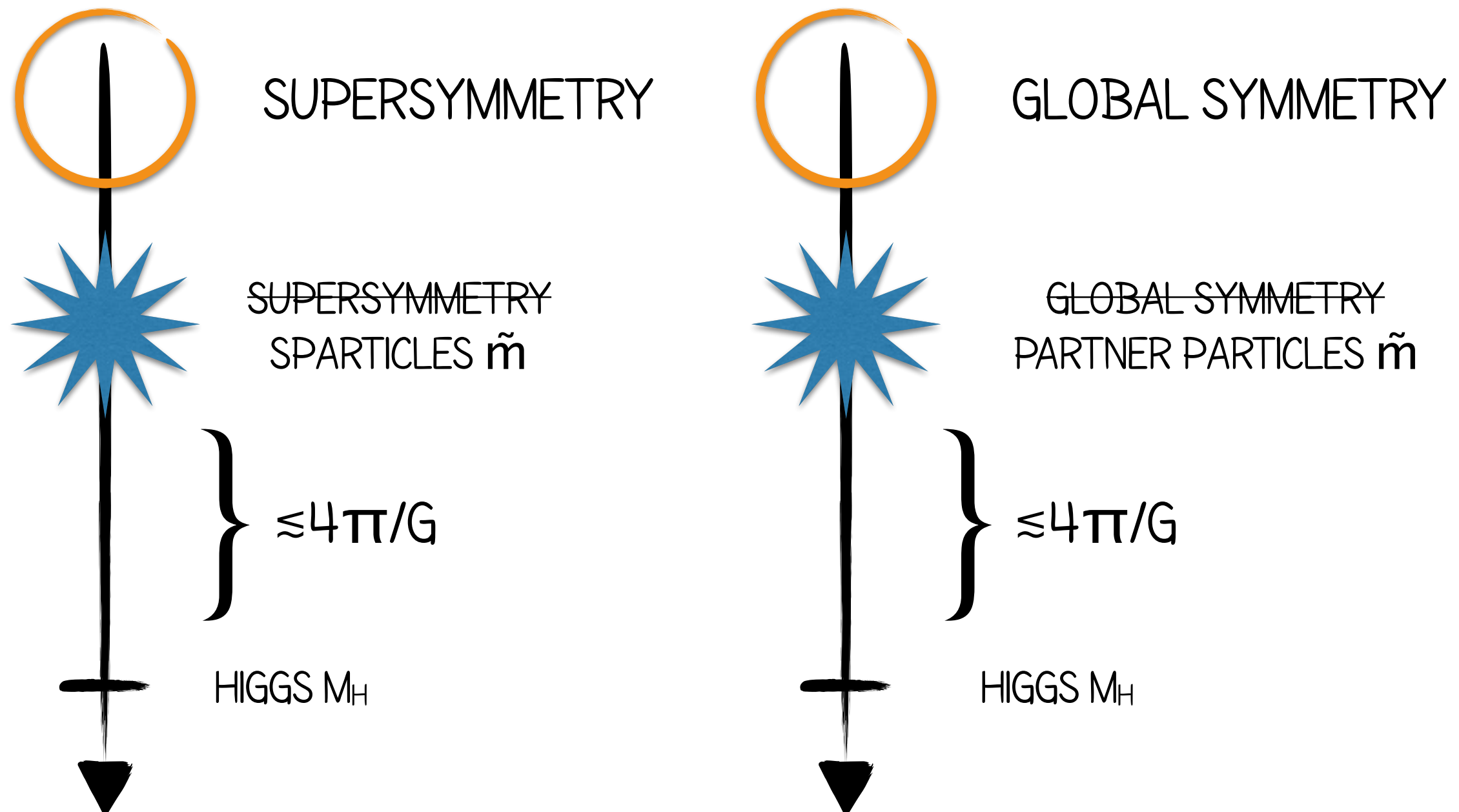
**The Coleman-Mandula theorem (1967):** *in a theory with non-trivial interactions (scattering) in more than 1+1 dimensions, the only possible conserved quantities that transform as tensors under the Lorentz group are the energy-momentum vector  $P_\mu$ , the generators of Lorentz transformations  $M_{\mu\nu}$ , and possible scalar symmetry charges  $Z_i$  corresponding to internal symmetries, which commute with both  $P_\mu$  and  $M_{\mu\nu}$ .*

*EXTENSION TO SPINOR SYMMETRY CHARGES BY HAAG, LOPUSZANSKI, SOHNIUS*

SO THE OPTIONS ARE: **GLOBAL SYMMETRY OR SUPERSYMMETRY**  
(CAN FANCY THE THEORY UP IN EXTRA DIMENSIONS, ETC., BUT 4D EFFECTIVE THEORY STILL USES ONE OF THESE SYMMETRIES)

# POSSIBLE SYMMETRIES

*EXTEND THE SM WITH A SYMMETRY ACTING ON THE HIGGS*



# NEW PARTICLES

CONTINUOUS SYMMETRIES COMMUTING W/ SM  $\rightarrow$   
PARTNER STATES W/ SM QUANTUM NUMBERS

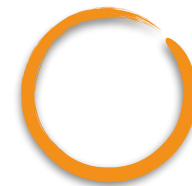


## SUPERSYMMETRY

$$\begin{aligned}\phi &\rightarrow \phi + \epsilon\psi \\ \psi &\rightarrow \psi + c^\mu \partial_\mu \phi\end{aligned}$$

OPPOSITE-STATISTICS PARTNER  
FOR EVERY SM PARTICLE

CONTRIBUTE TO THE HIGGS MASS:



## GLOBAL SYMMETRY

$$\Phi \rightarrow (1 + i\alpha T)\Phi$$

SAME-STATISTICS PARTNER  
FOR EVERY SM PARTICLE

$$m_h^2 \sim \frac{3y_t^2}{4\pi^2} \tilde{m}^2 \log(\Lambda^2 / \tilde{m}^2)$$

# SUPERSYMMETRY

EXTENDED SPACETIME SYMMETRY

EXTEND POINCARÉ SYMMETRY W/ SPINORIAL CHARGES  $Q_\alpha, \tilde{Q}_{\dot{\alpha}}$

(MINIMAL N=1 SUPERSYMMETRY IN D=4)

SUPER-EXTENSION OF POINCARÉ ALGEBRA:

$$[P_\mu, Q_\alpha] = [P_\mu, \tilde{Q}^{\dot{\alpha}}] = 0$$

$$[M^{\mu\nu}, Q_\alpha] = i(\sigma^{\mu\nu})_\alpha^\beta Q_\beta$$

$$[M^{\mu\nu}, \tilde{Q}^{\dot{\alpha}}] = i(\bar{\sigma}^{\mu\nu})^{\dot{\alpha}}_{\dot{\beta}} \tilde{Q}^{\dot{\beta}}$$

ALONG WITH  $\{Q_\alpha, \tilde{Q}_{\dot{\beta}}\} = 2P_\mu(\sigma^\mu)_{\alpha\dot{\beta}}$  AND  $\{Q_\alpha, Q_\beta\} = 0$



# SUPERFIELDS

ORGANIZE FIELDS INTO IRREPS OF SUPER-POINCARÉ SYMMETRY

SUPERFIELDS CONTAIN BOTH BOSONS AND FERMIONS

$$Q|\text{Boson}\rangle = |\text{Fermion}\rangle$$

$$Q|\text{Fermion}\rangle = |\text{Boson}\rangle$$

$$\text{tr}[(-1)^{N_f}] = 0 \rightarrow n_F = n_B \Rightarrow \text{SAME \# OF BOSONIC \& FERMIONIC D.O.F.}$$

$$[P^2, Q_\alpha] = [P^2, \tilde{Q}_{\dot{\alpha}}] = 0 \Rightarrow \text{COMPONENTS HAVE SAME MASS}$$

AT MOST ONE U(1) GLOBAL SYMMETRY DOES NOT COMMUTE W/ SUPERCHARGES

$$[R, Q_\alpha] = -Q_\alpha \quad [R, Q_{\dot{\alpha}}^\dagger] = Q_{\dot{\alpha}}^\dagger$$

$\Rightarrow$  COMPONENTS HAVE SAME QUANTUM #'S APART FROM U(1)<sub>R</sub>

TRANSFORMATIONS ACTING ON FIELDS

$$\delta\phi = \epsilon^\alpha \psi_\alpha$$

$$\phi \rightarrow \phi + \delta\phi$$

$$\psi \rightarrow \psi + \delta\psi$$

$$\delta\psi_\alpha = -i(\sigma^\nu \epsilon^\dagger)_\alpha \partial_\nu \phi$$

# THE MSSM

ONE SUPERMULTIPLY FOR EACH SM FIELD + SECOND HIGGS DOUBLET

Names		spin 0	spin 1/2	$SU(3)_C, SU(2)_L, U(1)_Y$
squarks, quarks ( $\times 3$ families)	$Q$	$(\tilde{u}_L \ \tilde{d}_L)$	$(u_L \ d_L)$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$
	$\bar{u}$	$\tilde{u}_R^*$	$u_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$
	$\bar{d}$	$\tilde{d}_R^*$	$d_R^\dagger$	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons, leptons ( $\times 3$ families)	$L$	$(\tilde{\nu} \ \tilde{e}_L)$	$(\nu \ e_L)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
	$\bar{e}$	$\tilde{e}_R^*$	$e_R^\dagger$	$(\mathbf{1}, \mathbf{1}, 1)$
Higgs, higgsinos	$H_u$	$(H_u^+ \ H_u^0)$	$(\tilde{H}_u^+ \ \tilde{H}_u^0)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$
	$H_d$	$(H_d^0 \ H_d^-)$	$(\tilde{H}_d^0 \ \tilde{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

Names	spin 1/2	spin 1	$SU(3)_C, SU(2)_L, U(1)_Y$
gluino, gluon	$\tilde{g}$	$g$	$(\mathbf{8}, \mathbf{1}, 0)$
winos, W bosons	$\tilde{W}^\pm \ \tilde{W}^0$	$W^\pm \ W^0$	$(\mathbf{1}, \mathbf{3}, 0)$
bingo, B boson	$\tilde{B}^0$	$B^0$	$(\mathbf{1}, \mathbf{1}, 0)$

# SOFTLY BROKEN SUPERSYMMETRY

SUPERSYMMETRY MUST BE BROKEN; BREAKING WITH RELEVANT OPERATORS  
GUARANTEES IT REMAINS A GOOD SYMMETRY IN THE UV

$$\begin{aligned}\mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{h.c.} \right) \\ & - \left( \tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\ & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\ & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.})\end{aligned}$$

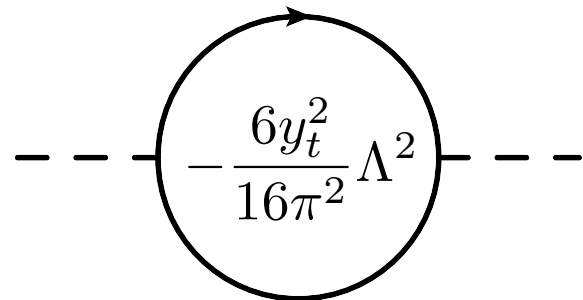
INCREASES MASSES OF NEW SUPERPARTNERS RELATIVE TO SM COUNTERPARTS

# SUSY & THE HIERARCHY PROBLEM

SUPERSYMMETRY RELATES SCALARS TO FERMIONS, SO CHIRAL SYMMETRY MAKES HIGGS MASS TECHNICALLY NATURAL.

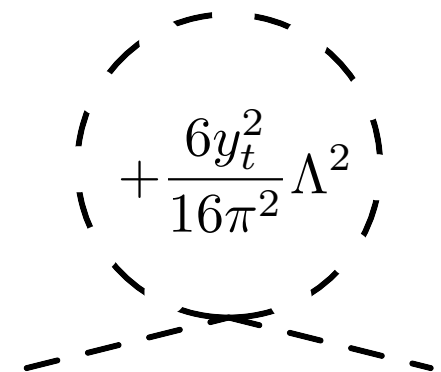
NEW INTERACTIONS RELATED BY SUPERSYMMETRY TO SM INTERACTIONS. E.G. IN TOP-STOP SECTOR,

$$\mathcal{L} \supset y_t H Q_3 t_R^\dagger + |y_t|^2 |H \cdot \tilde{Q}_3|^2 + |y_t|^2 |H|^2 |\tilde{t}_R|^2$$



A Feynman diagram showing a top quark loop. It consists of a solid circle with an arrow indicating a fermion loop. Inside the circle is the expression  $-\frac{6y_t^2}{16\pi^2}\Lambda^2$ . Two dashed lines extend from the left and right sides of the circle, representing external Higgs lines.

ELIMINATION OF UV SENSITIVITY APPARENT IN "QUADRATIC DIVERGENCE", WHICH CANCELS BETWEEN TOP & STOP LOOPS



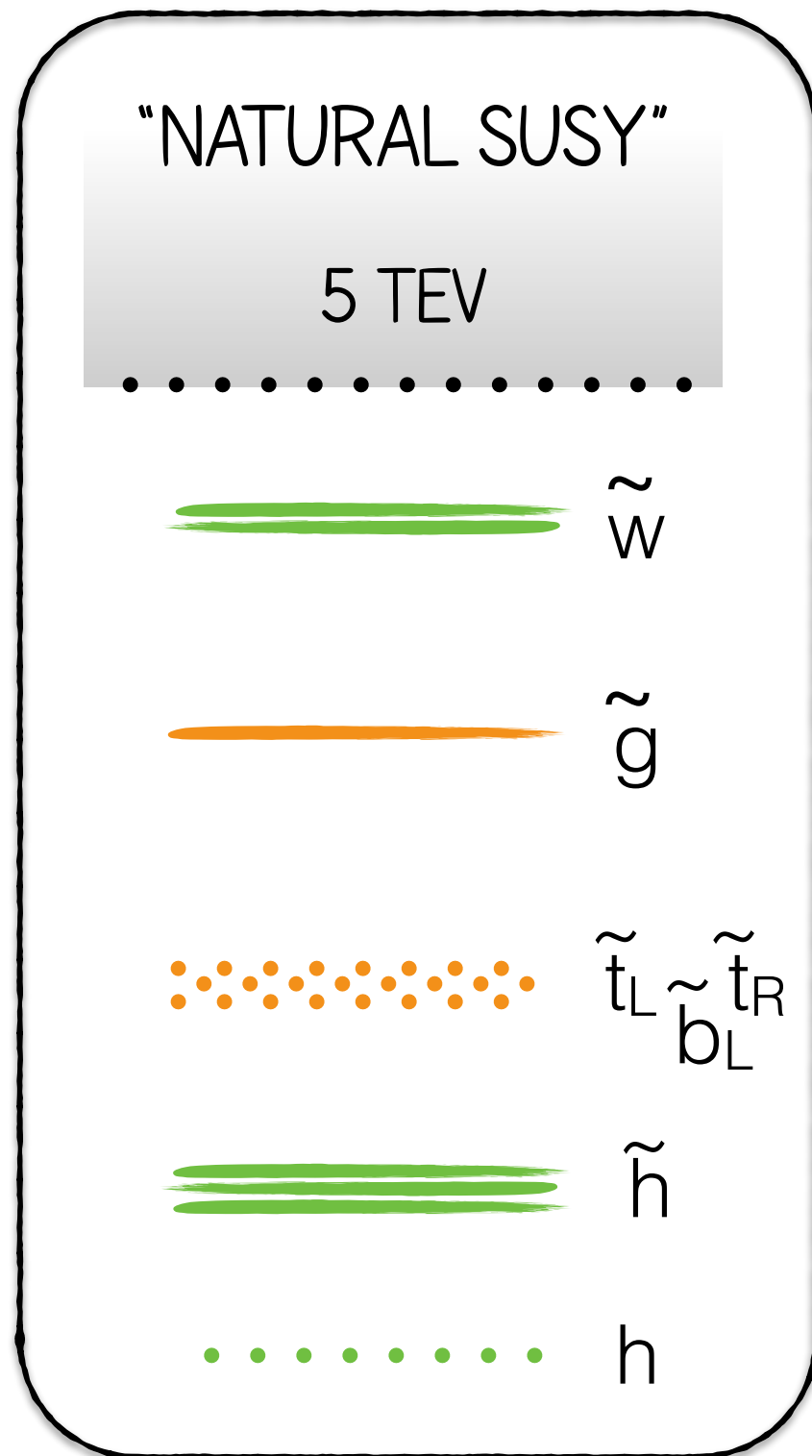
A Feynman diagram showing a stop squark loop. It consists of a dashed circle. Inside the circle is the expression  $+\frac{6y_t^2}{16\pi^2}\Lambda^2$ . Two dashed lines extend from the left and right sides of the circle, representing external Higgs lines.

LEAVES ONLY FINITE THRESHOLD CORRECTION  $m_H^2 \sim -\frac{6y_t^2}{16\pi^2}\tilde{m}_t^2$

*SUPERSYMMETRY PROTECTS AGAINST ARBITRARY PHYSICS AT HIGH SCALES, BUT SUPERPARTNERS MUST ENTER NEAR WEAK SCALE.*



# SUSY EXPECTATIONS



BEST CASE SCENARIO GIVEN NULL RESULTS:  
SUPERPARTNER MASS HIERARCHY INVERSELY  
PROPORTIONAL TO CONTRIBUTION TO HIGGS MASS

$$\delta m_h^2 \propto \mu^2 \quad (\text{"HIGGSINOS"})$$

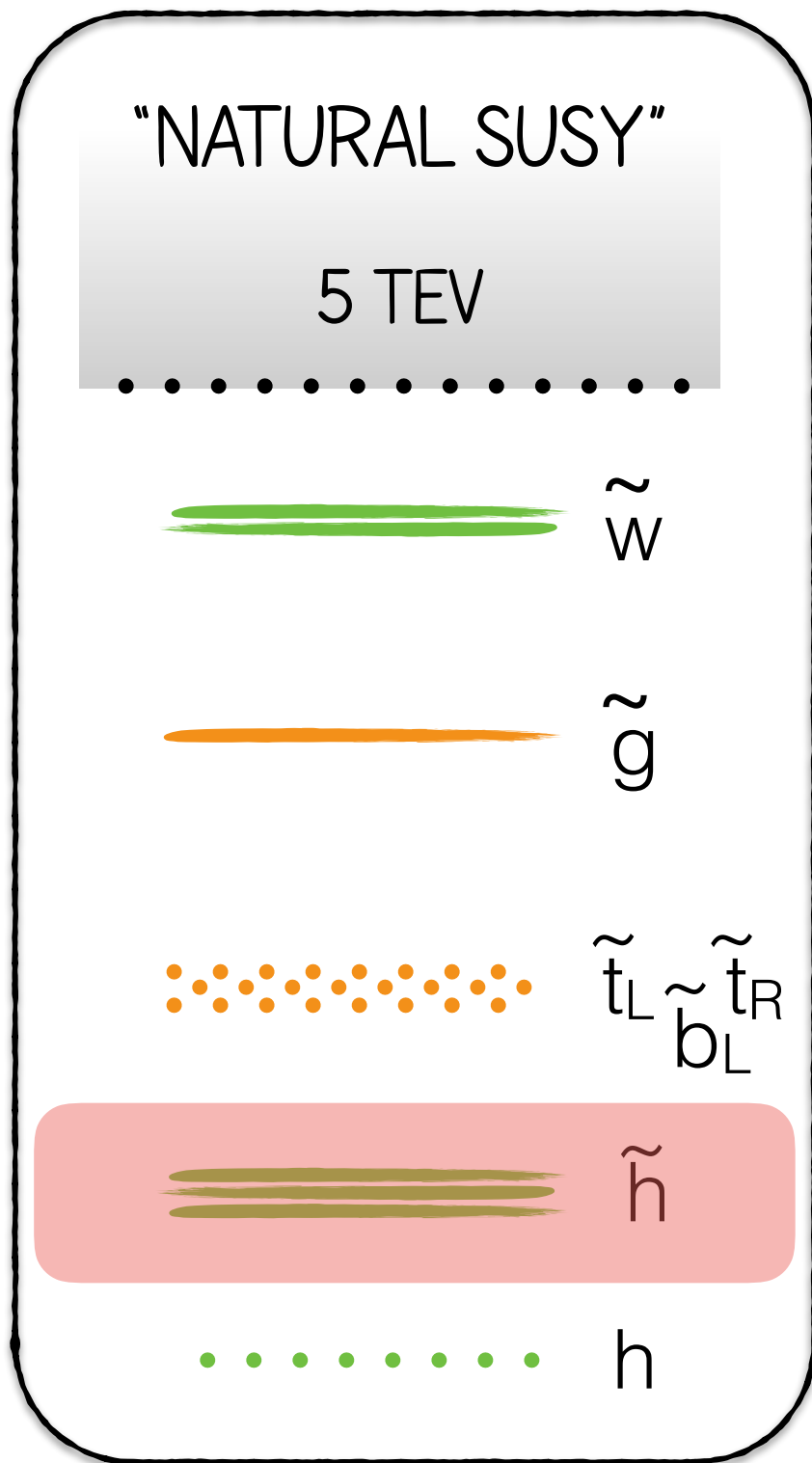
$$m_h^2 \sim \frac{3y_t^2}{4\pi^2} \tilde{m}^2 \log(\Lambda^2 / \tilde{m}^2) \quad (\text{STOPS})$$

ETC...

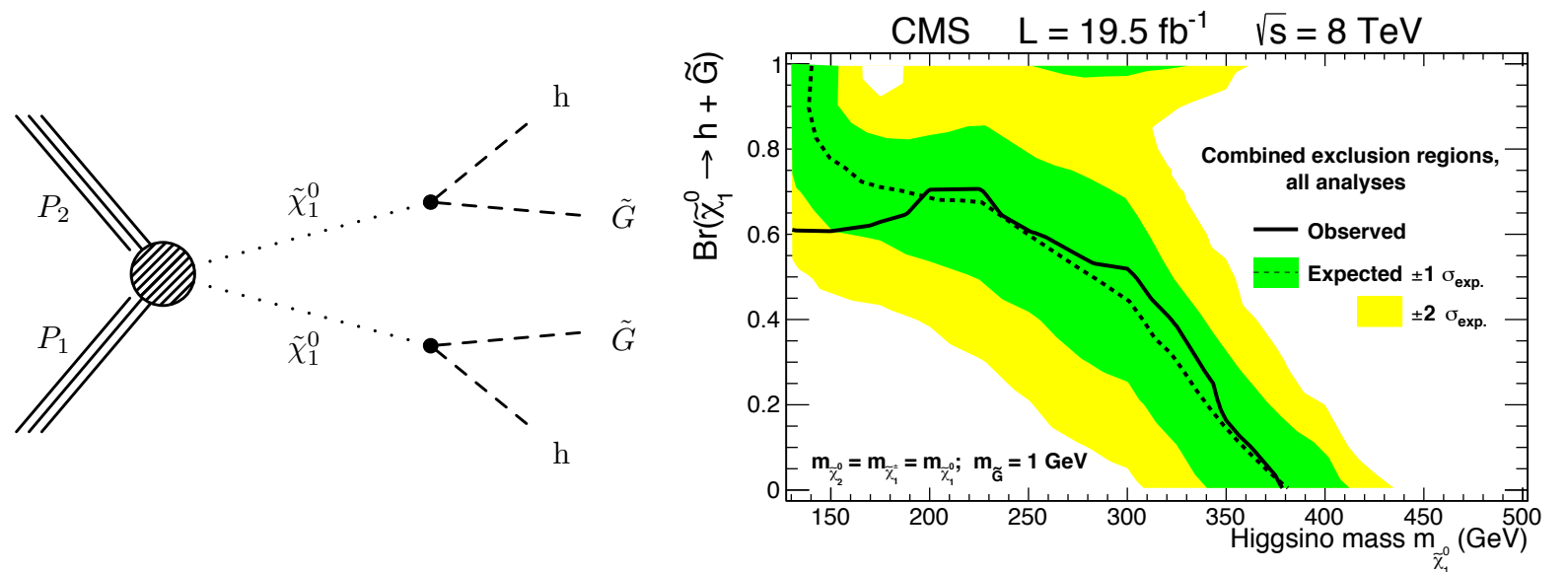
QCD PRODUCTION OF STOPS, GLUINOS  
LEADS TO STRONGEST CONSTRAINTS

[DIMOPOULOS, GIUDICE '95; COHEN, KAPLAN, NELSON '96; PAPUCCI,  
RUDERMAN, WEILER '11; BRUST, KATZ, LAWRENCE, SUNDRUM '11]

# HIGGSINO SIGNALS

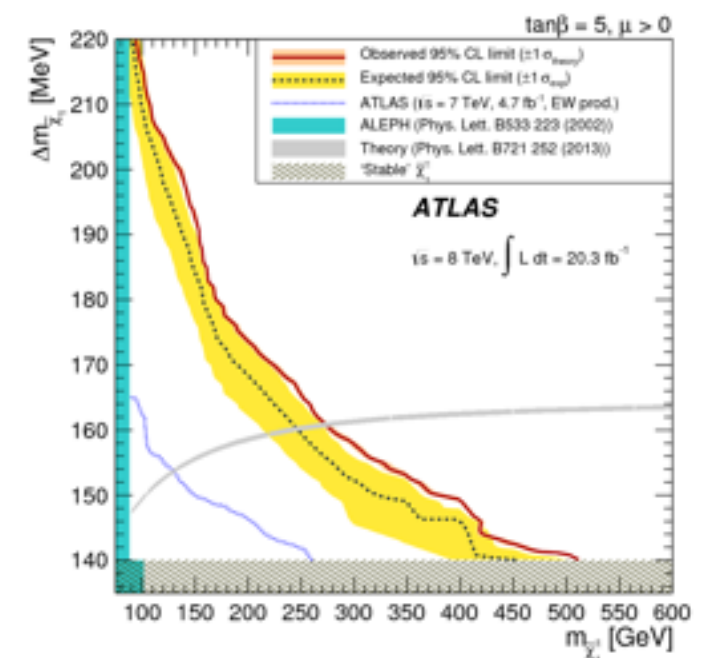
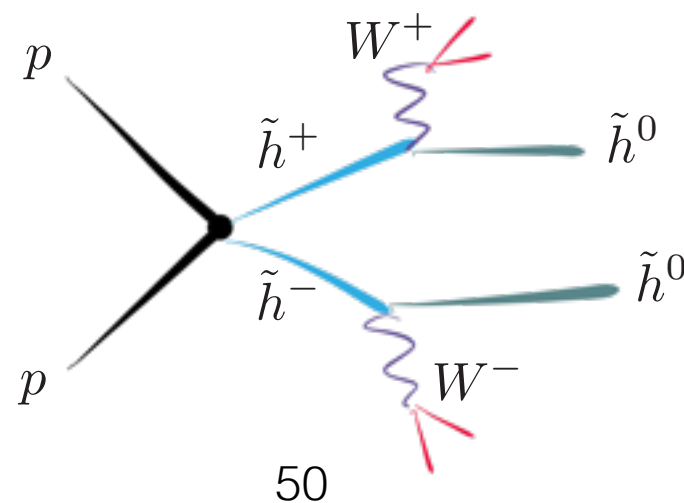


LOTS OF SEARCHES...

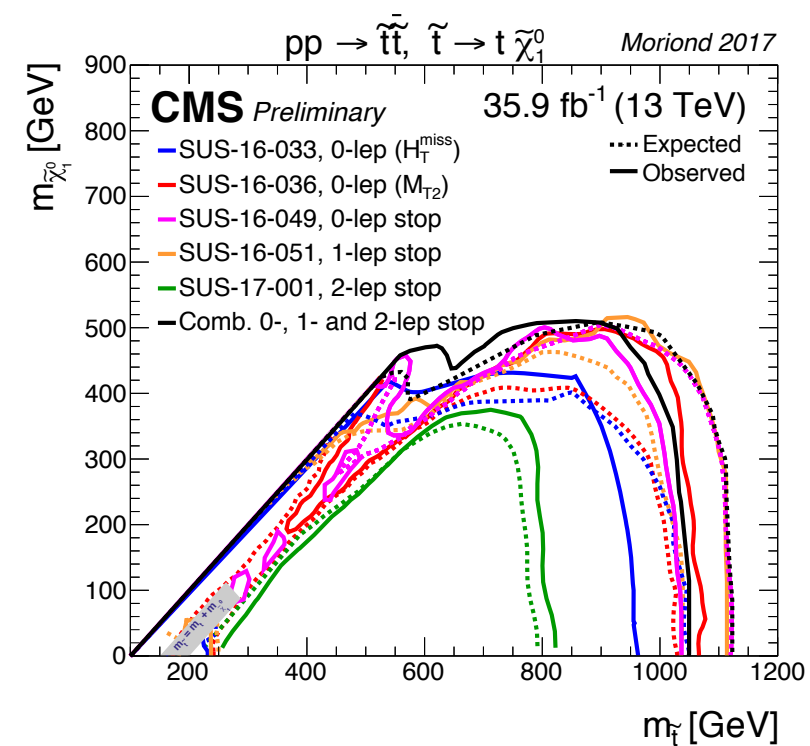
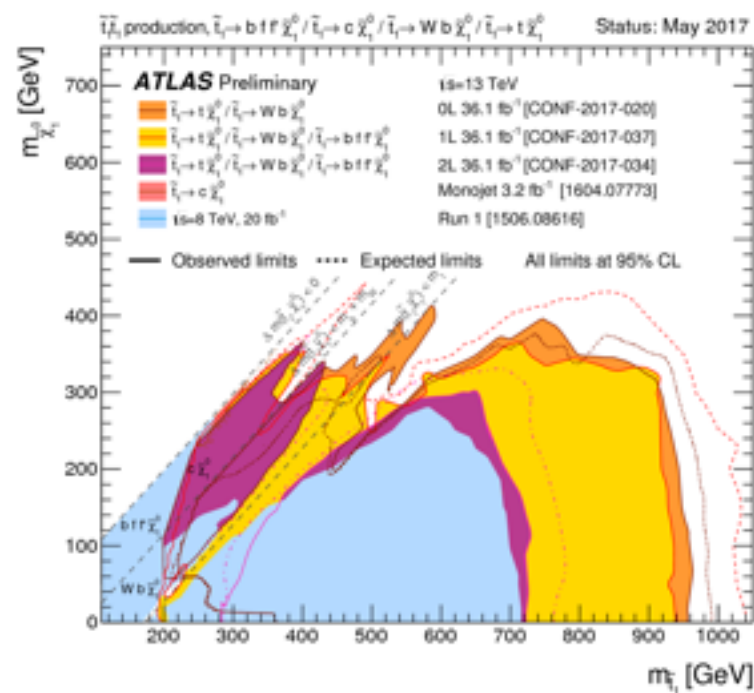
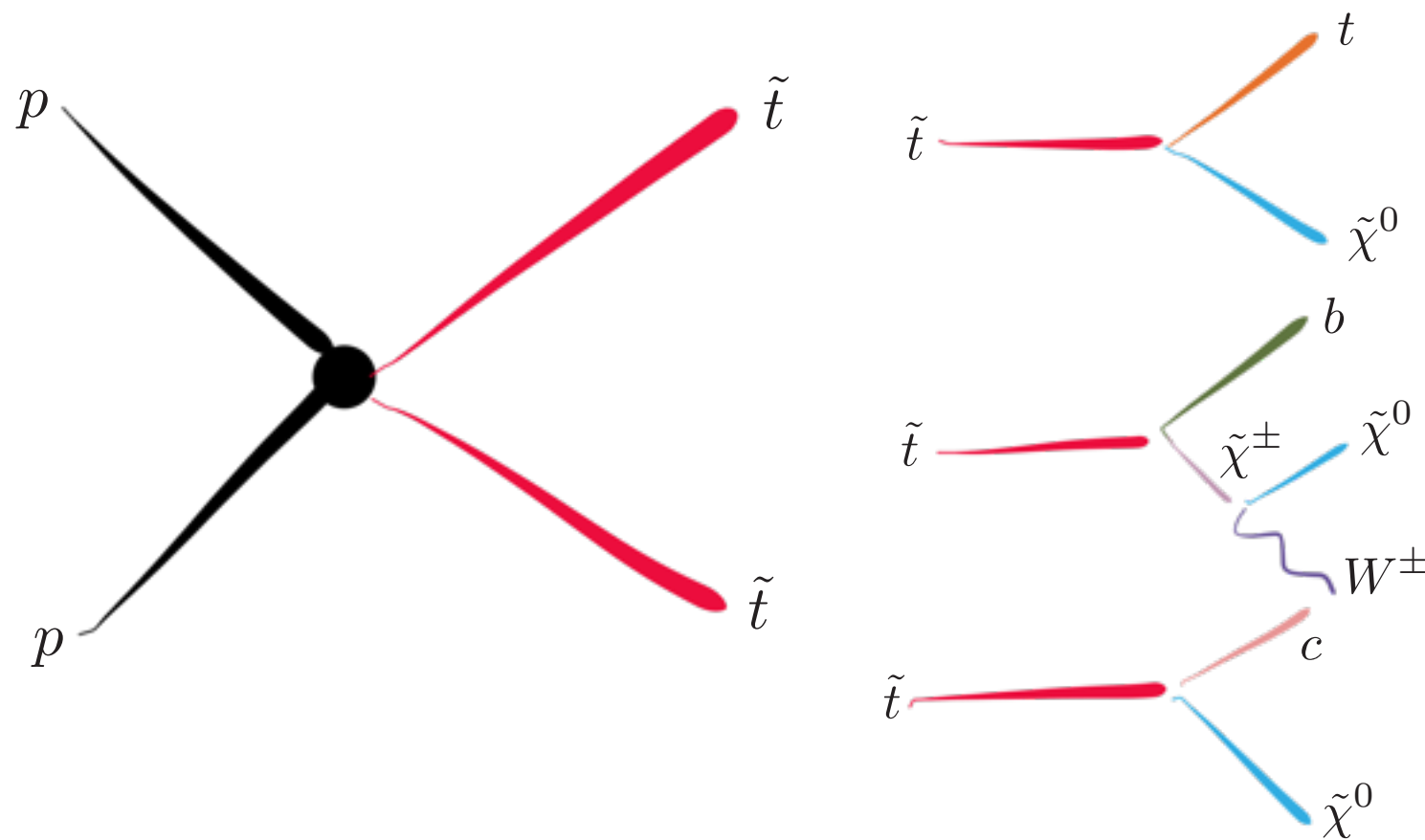
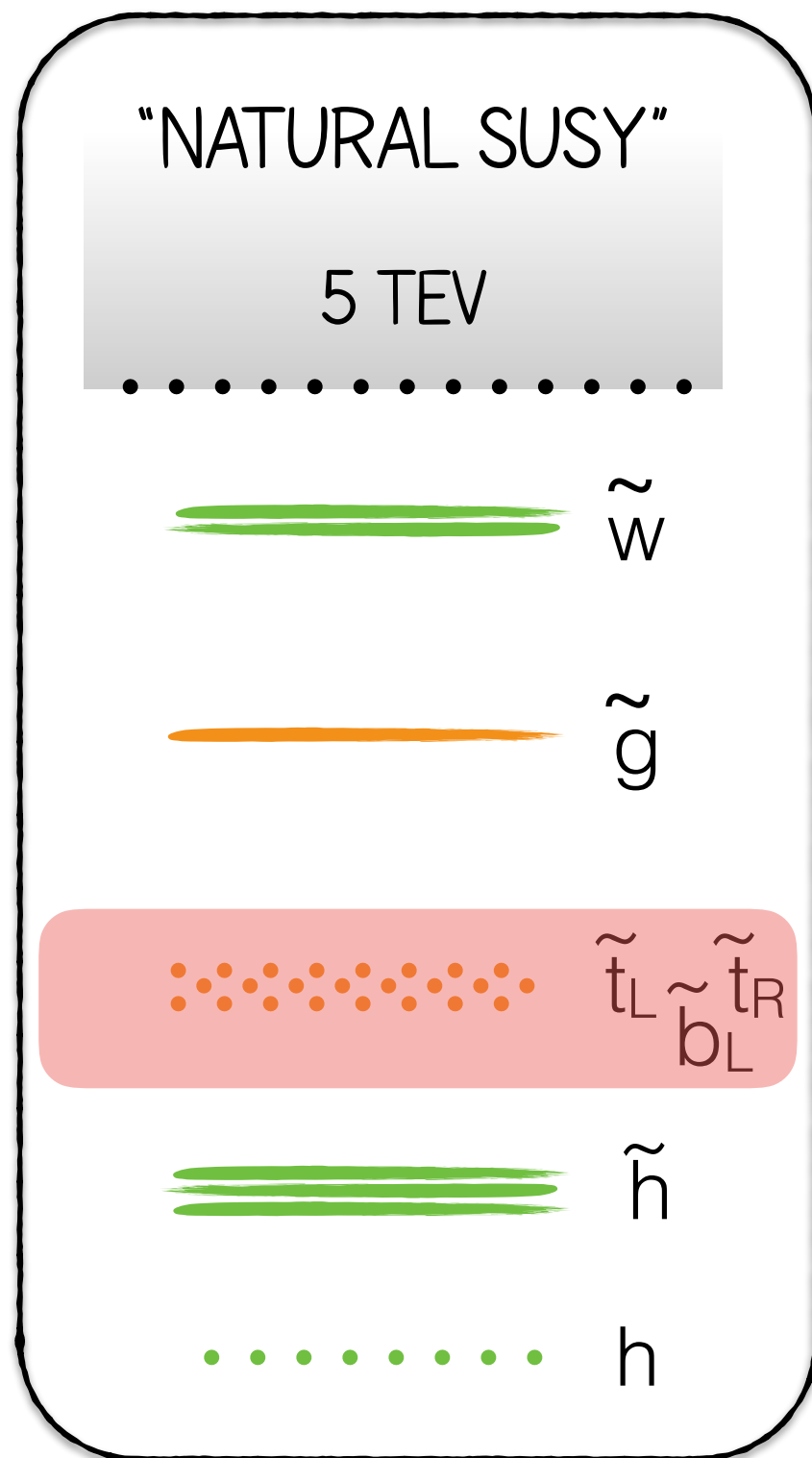


...BUT NO IRREDUCIBLE LIMITS

CHARGINO-NEUTRALINO SPLITTING IN  
PURE HIGGSINO MULTIPLET: 355 MEV  
[THOMAS, WELLS '98]



# STOP SIGNALS



# GLUINO SIGNALS

"NATURAL SUSY"

5 TEV



$\tilde{W}$



$\tilde{g}$



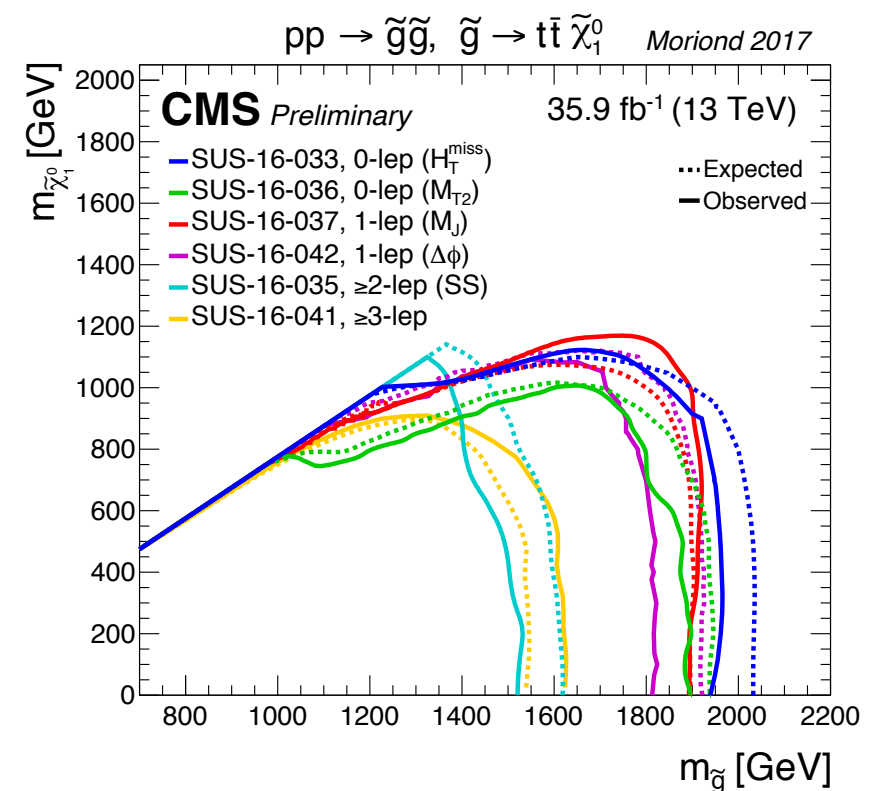
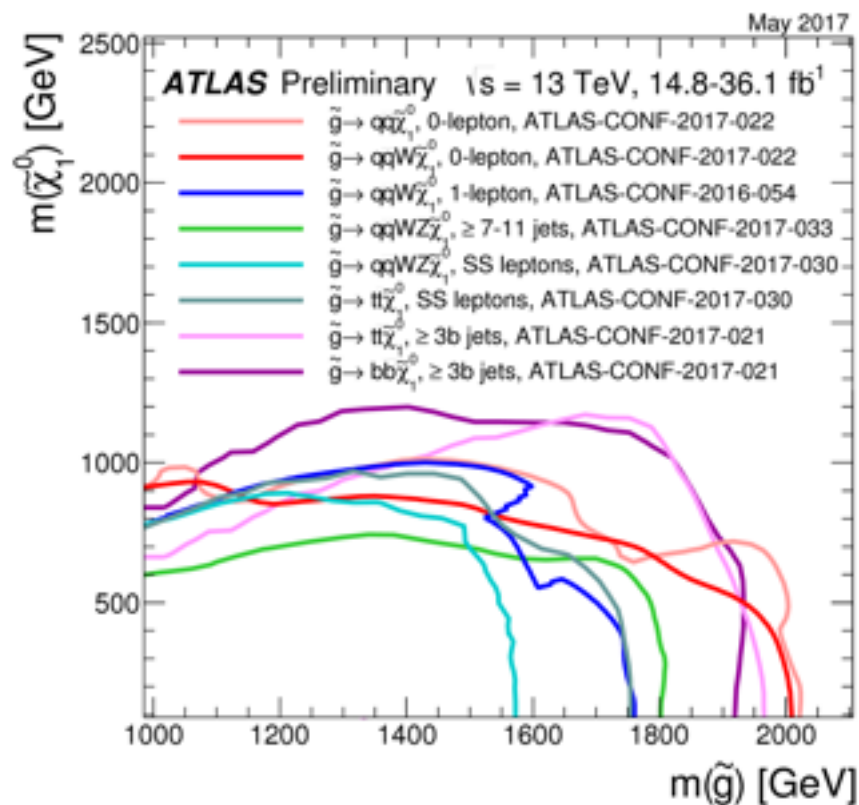
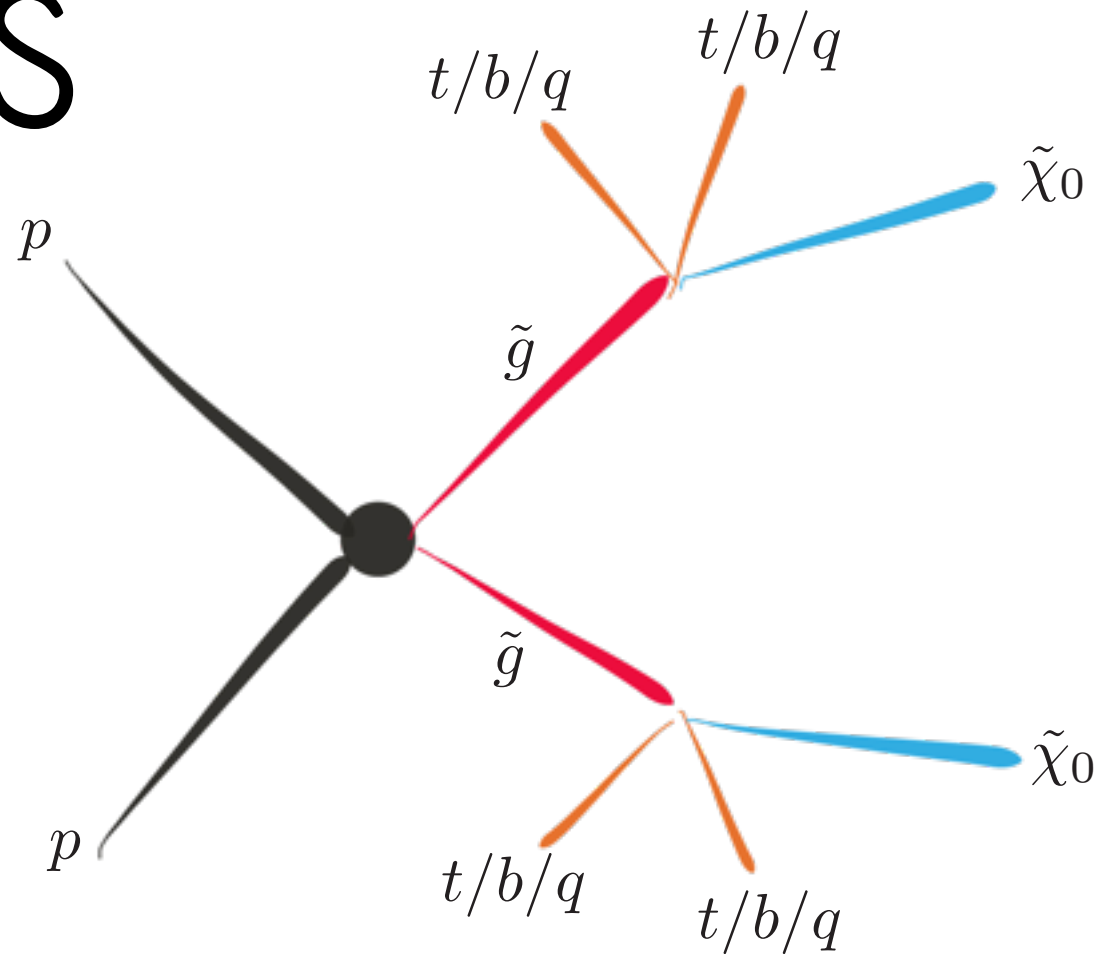
$\tilde{t}_L \tilde{t}_R$   
 $\tilde{b}_L$



$\tilde{h}$



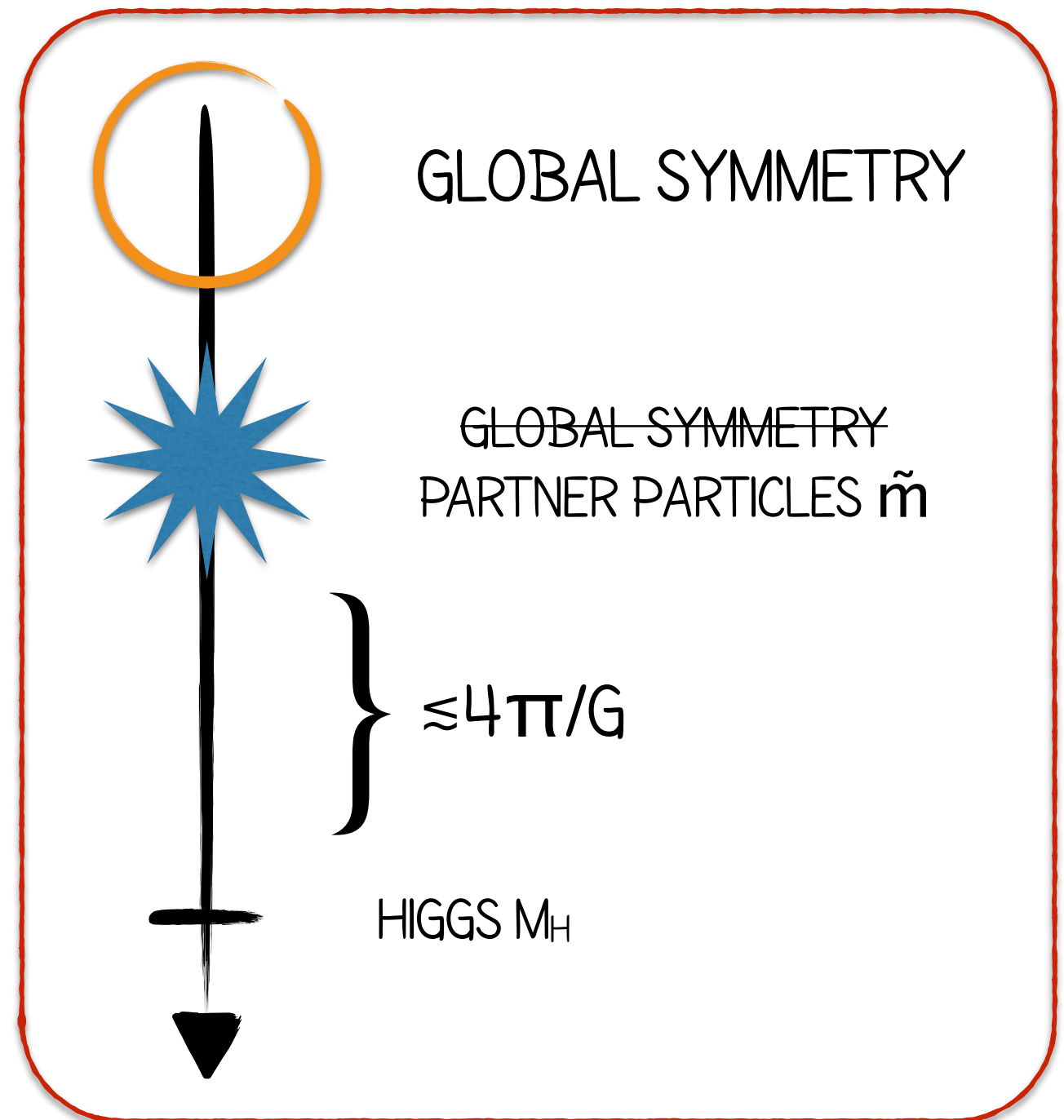
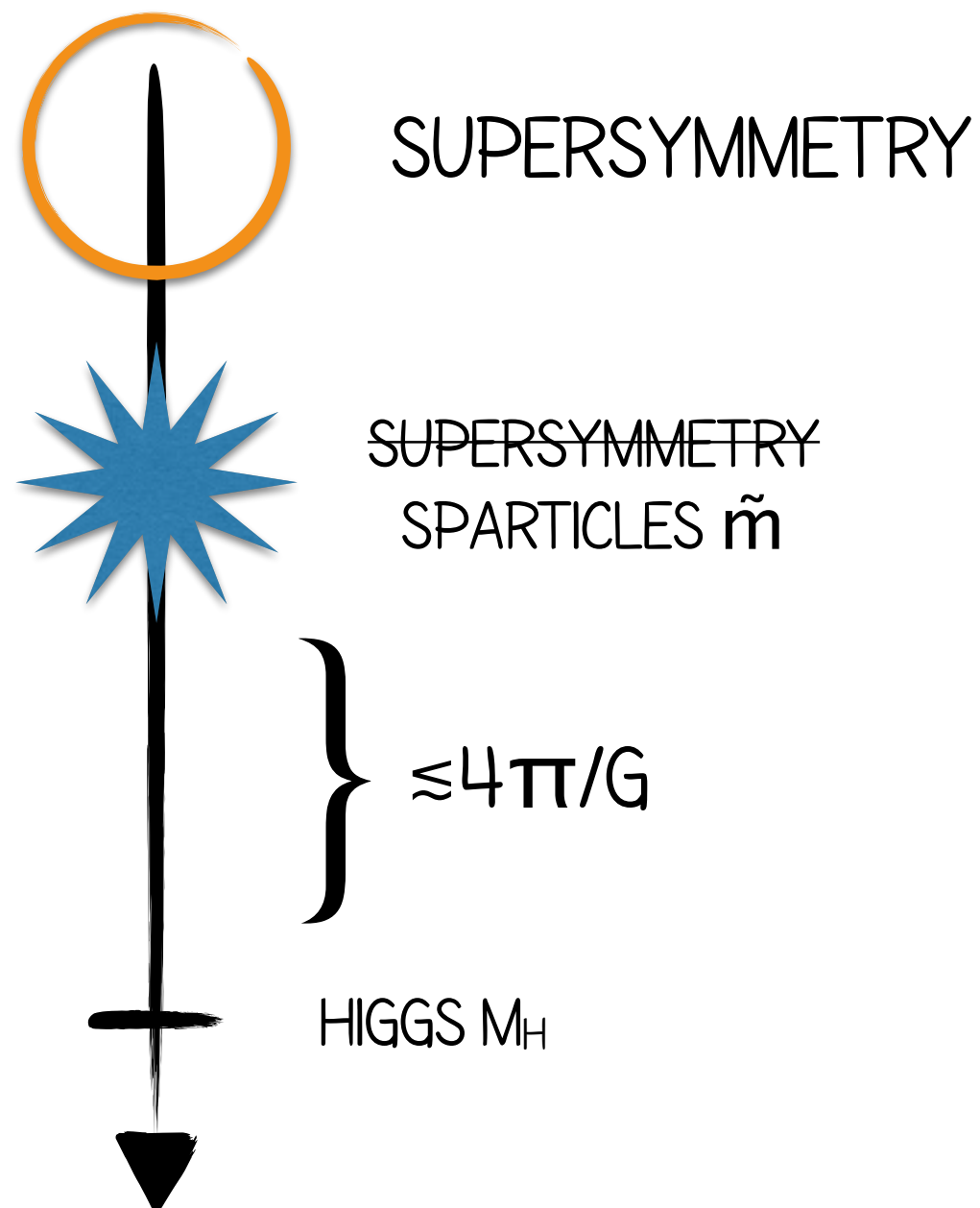
$h$





# POSSIBLE SYMMETRIES

*EXTEND THE SM WITH A SYMMETRY ACTING ON THE HIGGS*



# GLOBAL SYMMETRY: AN EXAMPLE

CONSIDER AN  $SU(N)$  GLOBAL SYMMETRY, SPONTANEOUSLY  
BROKEN BY VEV OF A FUNDAMENTAL SCALAR  $\phi$

$$SU(N) \rightarrow SU(N-1)$$

GOLDSTONE COUNTING:  $[N^2 - 1] - [(N-1)^2 - 1] = 2N - 1$

ORGANIZE INTO  $N-1$  COMPLEX SCALARS + ONE REAL

EXPAND  $\phi$  IN TERMS OF GOLDSTONES  $\boldsymbol{\pi}$ :

$$\phi = \exp \left[ \frac{i}{f} \left( \begin{array}{c|c} & \begin{matrix} \pi_1 \\ \vdots \\ \pi_{N-1} \end{matrix} \\ \hline \begin{matrix} \pi_1^* & \cdots & \pi_{N-1}^* \end{matrix} & \pi_0/\sqrt{2} \end{array} \right) \right] \begin{pmatrix} 0 \\ \vdots \\ 0 \\ f \end{pmatrix} \equiv e^{i\pi/f} \phi_0$$

LOW-ENERGY THEORY OF  $\boldsymbol{\pi}$  INDEPENDENT OF DETAILS OF SYMMETRY BREAKING

# GLOBAL SYMMETRY: AN EXAMPLE

UNBROKEN SU(N-1)  
GENERATORS:

$$U_{N-1} = \begin{pmatrix} \hat{U}_{N-1} & 0 \\ 0 & 1 \end{pmatrix}$$

$\phi$  TRANSFORMS AS A FUNDAMENTAL, SO

$$\phi \rightarrow U_{N-1} \phi = (U_{N-1} e^{i\pi/f} U_{N-1}^\dagger) U_{N-1} \phi_0 = e^{\frac{i}{f} (U_{N-1} \pi U_{N-1}^\dagger)} \phi_0$$

THE  $\pi$  TRANSFORM AS

$$\left( \begin{array}{c|c} & \vec{\pi} \\ \hline \vec{\pi}^\dagger & \pi_0/\sqrt{2} \end{array} \right) \rightarrow U_{N-1} \left( \begin{array}{c|c} & \vec{\pi} \\ \hline \vec{\pi}^\dagger & \pi_0/\sqrt{2} \end{array} \right) U_{N-1}^\dagger = \left( \begin{array}{c|c} & \hat{U}_{N-1} \vec{\pi} \\ \hline \vec{\pi}^\dagger \hat{U}_{N-1}^\dagger & \pi_0/\sqrt{2} \end{array} \right)$$

I.E., THE  $\vec{\pi}$  TRANSFORM AS FUNDAMENTALS UNDER UNBROKEN SU(N-1)

TRANSFORMATION UNDER BROKEN GENERATORS MORE COMPLICATED, BUT AT LINEAR ORDER TRANSFORM BY A SHIFT:  $\vec{\pi} \rightarrow \vec{\pi} - \vec{\alpha} + \dots$

THE USUAL SHIFT SYMMETRY OF GOLDSTONES. A SYMMETRY TO PROTECT SCALARS...

# GLOBAL SYMMETRY: AN EXAMPLE

LET'S NOW CONSTRUCT A TOY MODEL FOR THE HIGGS

CONSIDER  $SU(3) \rightarrow SU(2)$

CONVENIENT TO  
PARAMETERIZE  
GOLDSTONES AS

$$\pi = \left( \begin{array}{cc|c} -\eta/2 & 0 & H_1 \\ 0 & -\eta/2 & H_2 \\ \hline H_1^* & H_2^* & \eta \end{array} \right)$$

SUGGESTIVE: H TRANSFORMS AS A COMPLEX DOUBLET  
OF UNBROKEN  $SU(2)$  & ENJOYS A SHIFT SYMMETRY

LOW-ENERGY THEORY FOR H INHERITS NON-RENORMALIZABLE INTERACTIONS

$$f^2 |\partial_\mu \phi|^2 = |\partial_\mu H|^2 + \frac{H^\dagger H |\partial_\mu H|^2}{f^2} + \dots$$

LOOPS IN THIS EFT  
ARE OF ORDER  $\frac{1}{f^2} \frac{\Lambda^2}{16\pi^2}$

SO CONSISTENT POWER  
COUNTING IMPLIES

$$\Lambda \lesssim 4\pi f$$

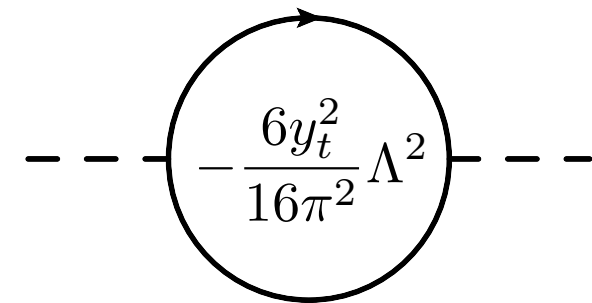


# GLOBAL SYMMETRY: AN EXAMPLE

OF COURSE, HIGGS MUST COUPLE TO SM FIELDS; COUPLINGS  
BREAK SU(3) AND HENCE VIOLATE SHIFT SYMMETRY

$$\mathcal{L} \supset -\lambda_t t_R^\dagger \tilde{H} Q_3 \quad \text{WHERE} \quad \tilde{H} = (i\sigma_2 H)^\dagger \text{ AND } Q_3 = (t_L, b_L)$$

GIVES THE USUAL QUADRATIC DIVERGENCE,  
NOT PROTECTED BY SHIFT SYMMETRY



$$-- \left( -\frac{6y_t^2}{16\pi^2} \Lambda^2 \right) --$$

MIGHT AS WELL HAVE NEVER INTRODUCED GLOBAL SYMMETRY...

SOLUTION: EXTEND TOP  
MULTIPLY TO SU(3):

$$\begin{aligned} Q_3 &\rightarrow \hat{Q}_3 \\ t_R &\rightarrow \hat{t}_R + \hat{T}_R \end{aligned} \quad \hat{Q}_3 = (\sigma_2 Q_3, T_L)$$

+ ADD SU(3) SYMMETRIC TOP YUKAWA,

$$\mathcal{L} \supset -(\lambda_1 \hat{t}_R^\dagger + \lambda_2 \hat{T}_R^\dagger) \phi^\dagger \hat{Q}_3 + \text{h.c.}$$

# GLOBAL SYMMETRY: AN EXAMPLE

BELOW SCALE OF SPONTANEOUS SU(3) BREAKING, INTERACTIONS ARE

$$\mathcal{L} = -f(\lambda_1 \hat{t}_R^\dagger + \lambda_2 \hat{T}_R^\dagger) T_L - \lambda_1 \hat{t}_R^\dagger \tilde{H} Q_3 + \frac{\lambda_1}{2f} (H^\dagger H) \hat{t}_R^\dagger T_L + \text{h.c.} + \dots$$

MASS EIGENSTATES	$T_L, t_L$	$t_R = \frac{\lambda_2 \hat{t}_R - \lambda_1 \hat{T}_R}{\sqrt{\lambda_1^2 + \lambda_2^2}}$	$T_R = \frac{\lambda_1 \hat{t}_R + \lambda_2 \hat{T}_R}{\sqrt{\lambda_1^2 + \lambda_2^2}}$
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IN TERMS OF THE MASS EIGENSTATES, INTERACTIONS ARE

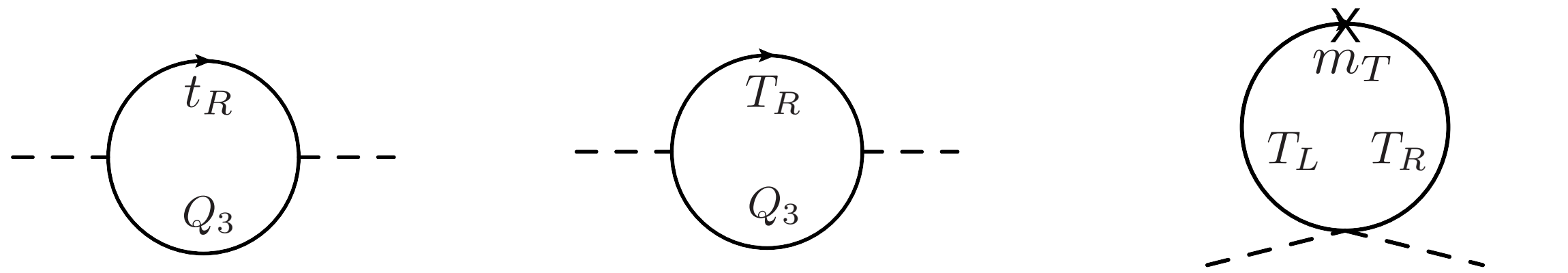
$$\mathcal{L} = -\lambda_t t_R^\dagger \tilde{H} Q_3 - \lambda_T T_R^\dagger \tilde{H} Q_3 + \frac{\lambda_1^2}{m_T} (H^\dagger H) T_R^\dagger T_L + \text{h.c.} + \dots$$

WHERE	$m_T = \sqrt{\lambda_1^2 + \lambda_2^2} f$	$\lambda_t = \frac{\lambda_1 \lambda_2}{\sqrt{\lambda_1^2 + \lambda_2^2}}$	$\lambda_T = \frac{\lambda_1^2}{\sqrt{\lambda_1^2 + \lambda_2^2}}$
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# GLOBAL SYMMETRY & THE HIERARCHY PROBLEM

TOP YUKAWA NOW ARISES FROM SU(3) SYMMETRIC INTERACTION,  
SO SHIFT SYMMETRY IS PRESERVED

IN TERMS OF THE LOW-ENERGY THEORY, STUDY QUADRATIC DIVERGENCE:



$$\begin{aligned}
 & -\frac{6\lambda_t^2}{16\pi^2}\Lambda^2 & -\frac{6\lambda_T^2}{16\pi^2}\Lambda^2 & +\frac{6(\lambda_t^2 + \lambda_T^2)}{16\pi^2}\Lambda^2
 \end{aligned}$$

COUPLINGS EXACTLY SO THAT TOP PARTNER CANCELS RADIATIVE CONTRIBUTIONS  
FROM HIGHER SCALES. LOOKS MAGICAL, BUT GUARANTEED BY SYMMETRY STRUCTURE

REMAINING CONTRIBUTION IS FINITE THRESHOLD  
CORRECTION DUE TO SPLITTING IN MULTIPLET

$$m_H^2 \sim -\frac{6y_t^2}{16\pi^2}m_T^2 \log(\Lambda^2/m_T^2)$$

# GLOBAL EXPECTATIONS

GLOBAL

5 TEV



$W', Z'$



$t'_L, t'_R$   
 $b'_L$



$h$

STORY BASICALLY THE SAME AS SUSY, BUT NOW W/  
LIGHT FERMIONIC TOP PARTNERS & HIGGS TUNING

$$m_H^2 \sim -\frac{6y_t^2}{16\pi^2} m_T^2 \log(\Lambda^2/m_T^2) \quad (\text{TOP PARTNERS})$$

RADIATIVE HIGGS POTENTIAL FROM PARTNERS

$$V(h) \sim \frac{N_c}{16\pi^2} m_\psi^4 \epsilon^2 \left[ c_1 \frac{h^2}{f^2} + c_2 \frac{h^4}{f^4} \right]$$

QUARTIC &  $M^2$  AT SAME LOOP ORDER, EXPECT  $V \sim F$

*I.E., NO SEPARATION BETWEEN WEAK SCALE & GLOBAL BREAKING*

MAKING  $V < F$  REQUIRES TREE-LEVEL TUNING  
OF TERMS IN THE POTENTIAL

$$\Delta \sim f^2/v^2$$

LIMITS NOW FROM QCD-CHARGED STATES &  
HIGGS MIXING.



# HIGGS SIGNALS

GLOBAL

5 TEV

$W', Z'$

$t'_L, t'_R, b'_L$

$h$

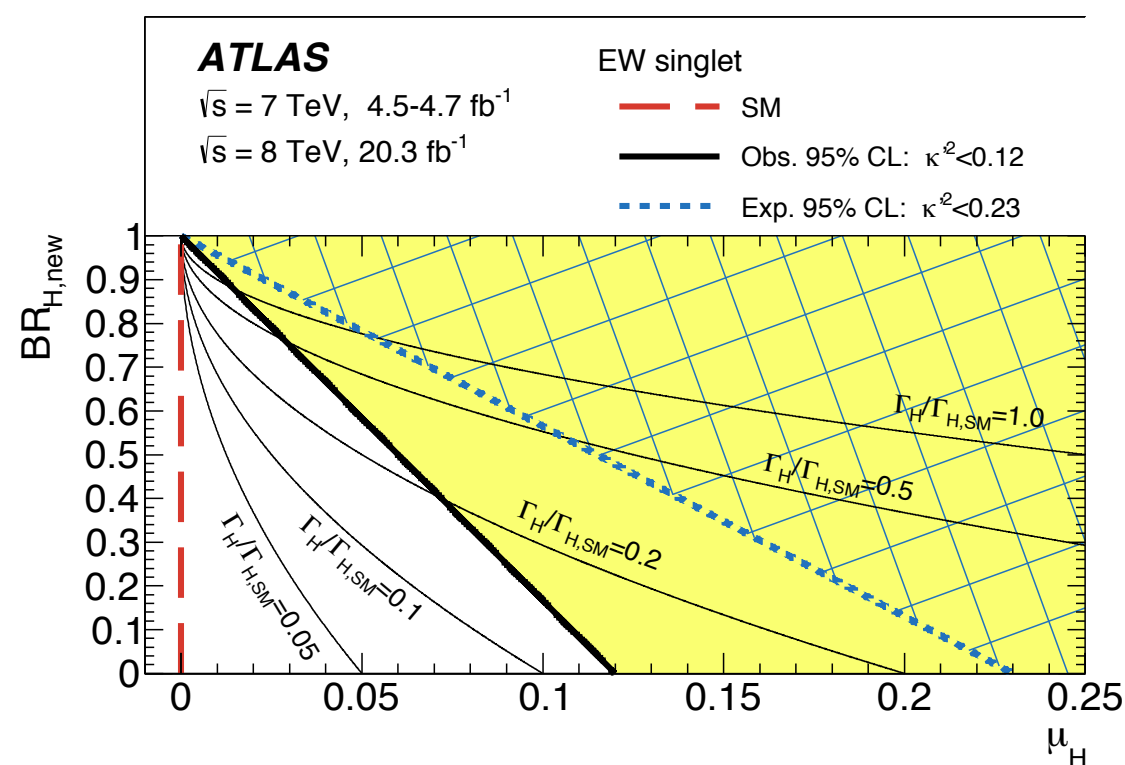
$$|\partial_\mu H|^2 + \frac{H^\dagger H}{f^2} |\partial_\mu H|^2 \rightarrow \left(1 + \frac{v^2}{f^2}\right) \frac{1}{2} (\partial_\mu h)^2$$

CANONICALLY  
NORMALIZE

$$h \rightarrow \left(1 - \frac{v^2}{2f^2}\right) h$$

SHIFTS HIGGS COUPLINGS UNIFORMLY, E.G.

$$\frac{m_Z^2}{v} h Z_\mu Z^\mu \rightarrow \frac{m_Z^2}{v} \left(1 - \frac{v^2}{2f^2}\right) h Z_\mu Z^\mu$$



LIMIT  
 $v^2/f^2 < 0.1$   
 UNLIKELY TO  
 IMPROVE  
 MUCH IN  
 FUTURE OF  
 LHC

# TOP PARTNER SIGNALS

3RD-GENERATION VECTOR-LIKE QUARKS.  
EASIER THAN SUSY: LARGER XSEC, NO MET

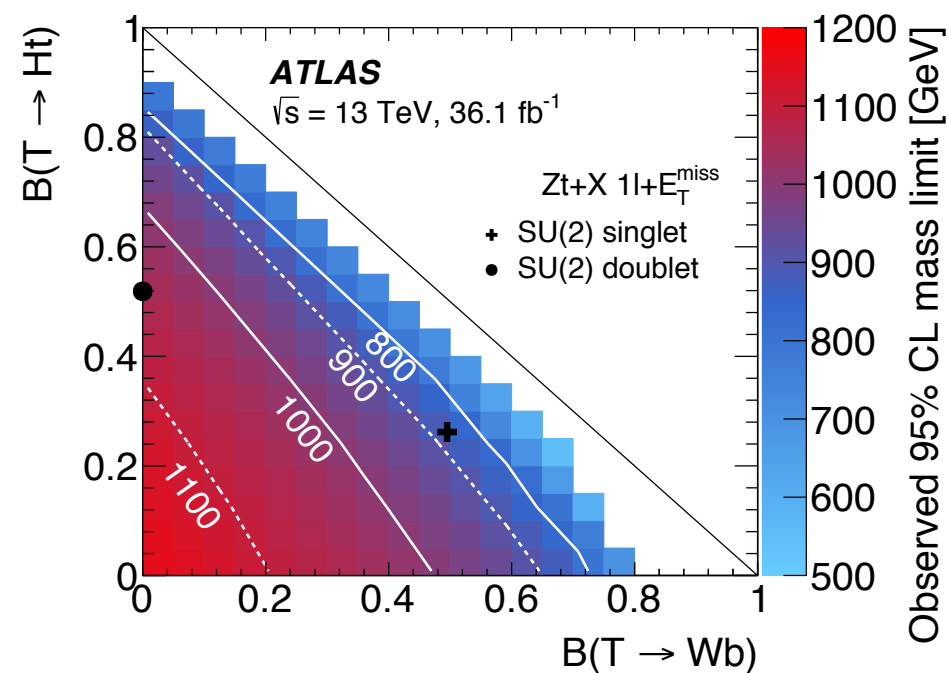
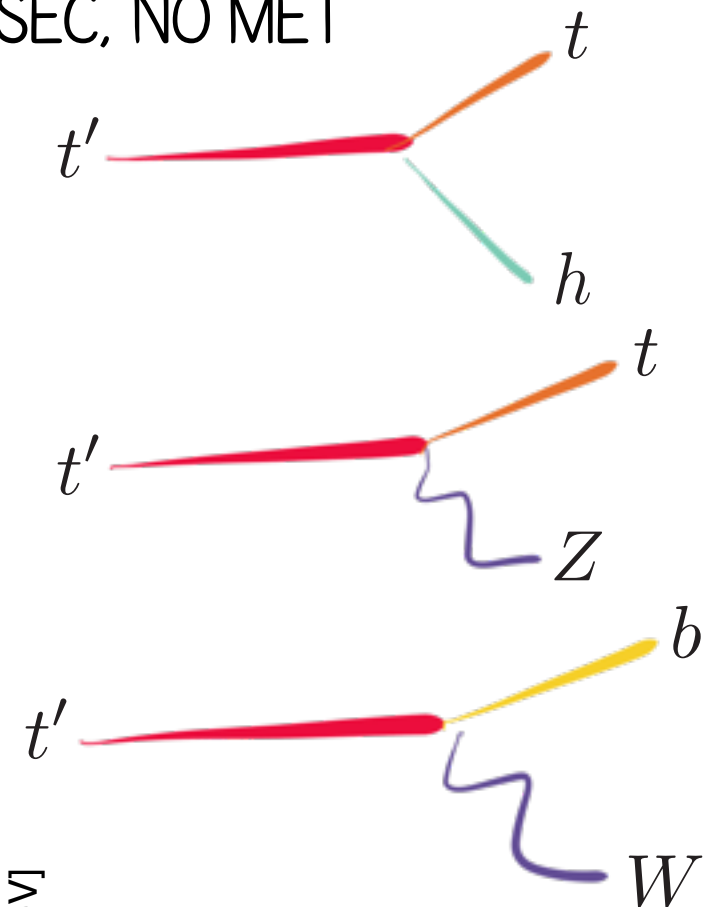
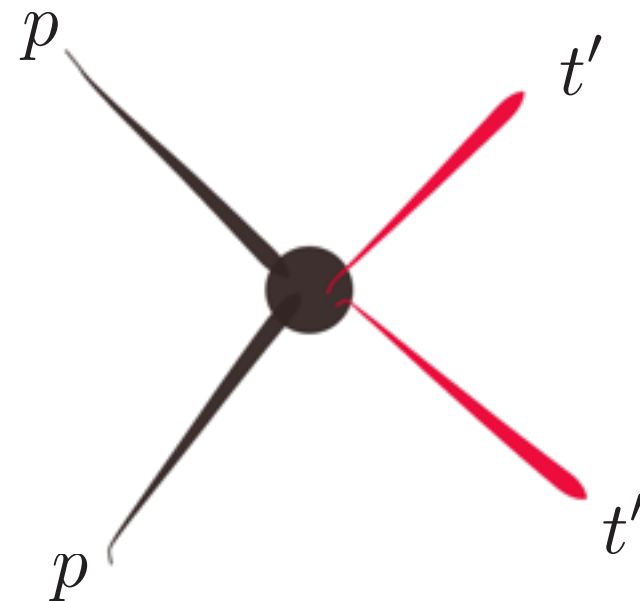
GLOBAL

5 TEV

$W', Z'$

$t'_L, t'_R, b'_L$

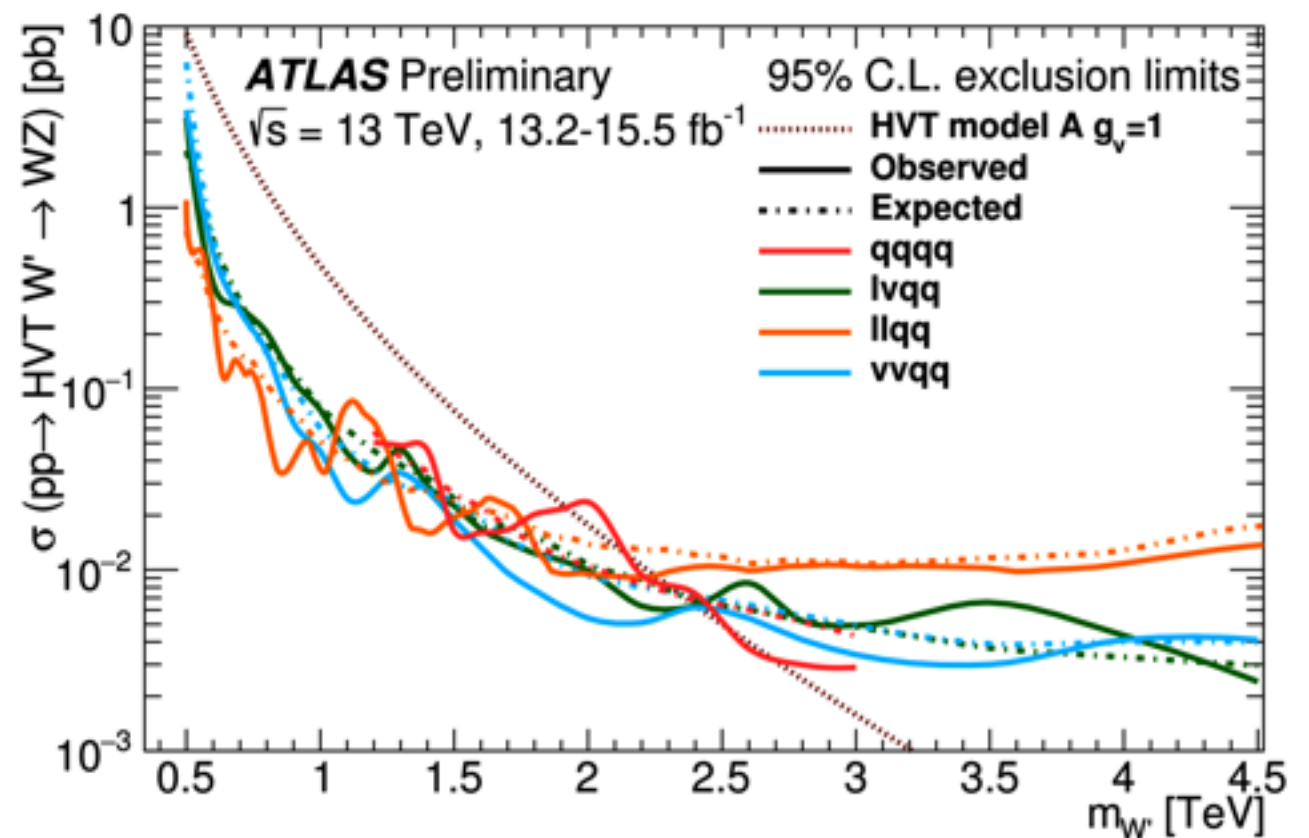
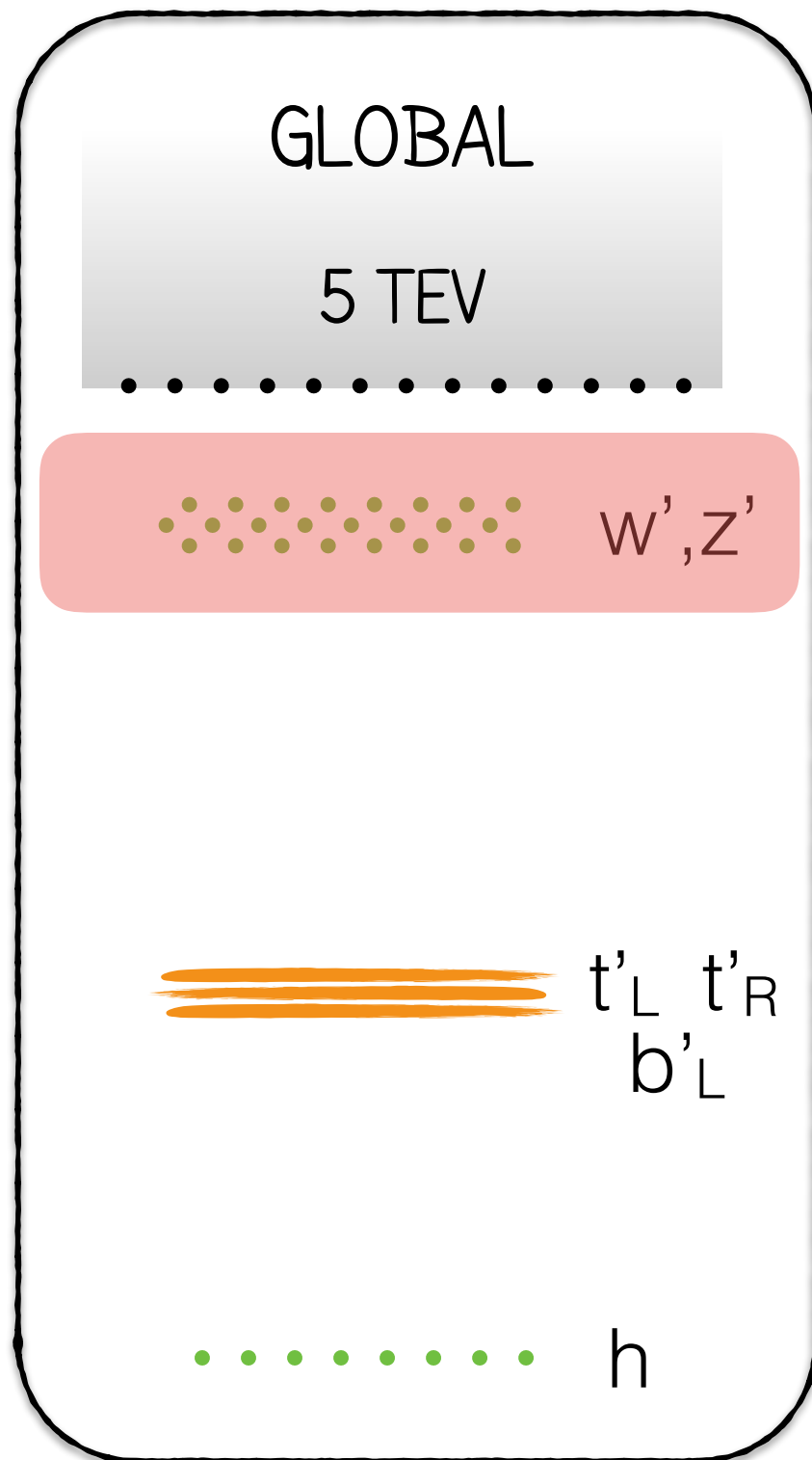
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VARIOUS  
FINAL  
STATES

# RESONANCE SIGNALS

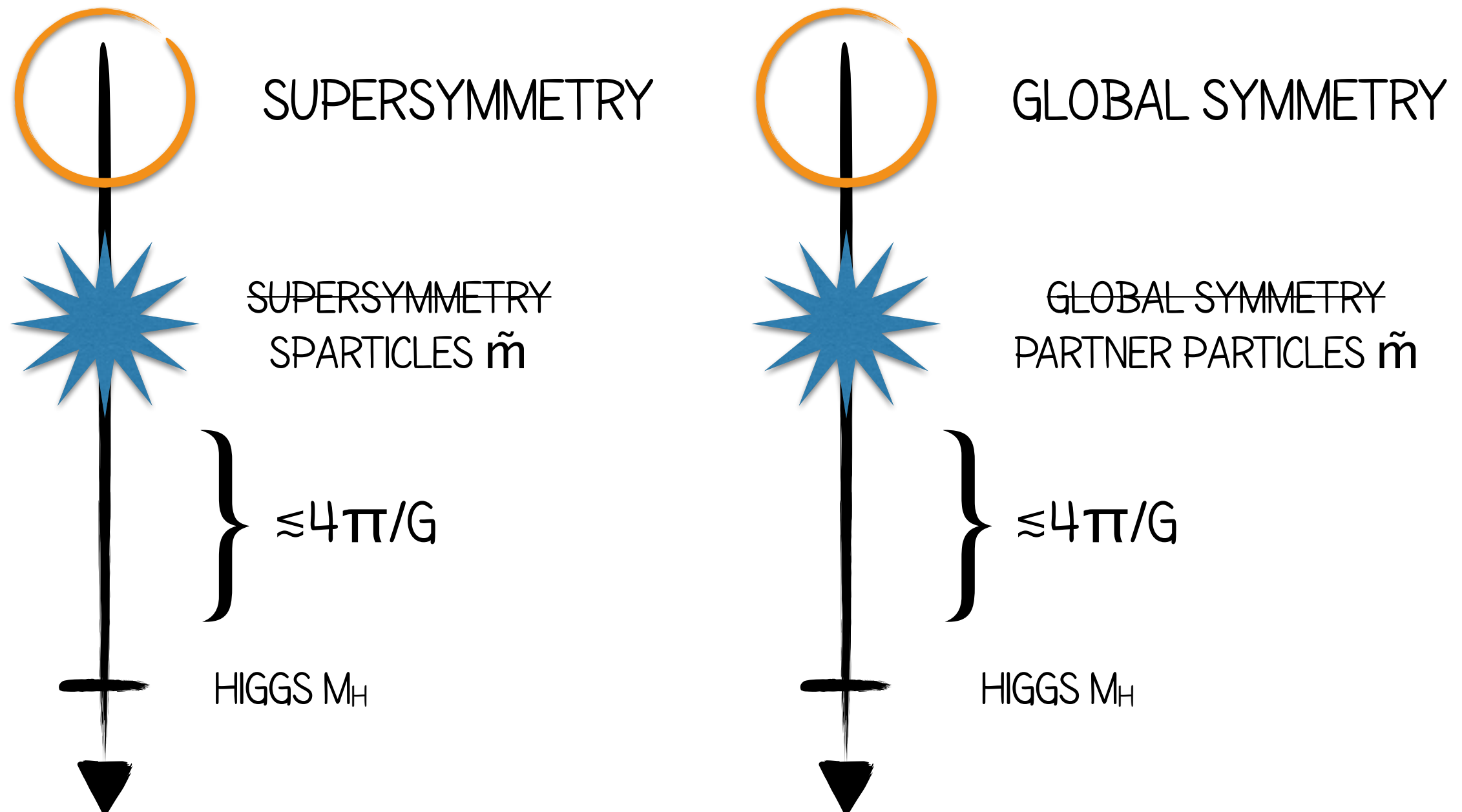
WIDE VARIETY OF POSSIBLE RESONANCES & SIGNALS



COMPARABLE TO PRECISION ELECTROWEAK LIMITS

$$S = 4\pi(1.36) \left( \frac{v}{m_\rho} \right)^2 \rightarrow m_\rho \gtrsim 3 \text{ TeV}$$

# SYMMETRY SUMMARY



SYMMETRY SOLUTIONS TO THE HIERARCHY PROBLEM PREDICT A SYSTEMATIC SET OF SIGNALS.  
NO EVIDENCE SO FAR. COULD STILL BE AROUND THE CORNER, BUT WORTH ASKING...



# IS THIS ALL THERE IS?

