





# GPU acceleration of plane-wave codes using SIRIUS library

Materials Design Ecosystem at the Exascale: High-Performance and High-Throughput Computing Anton Kozhevnikov, CSCS January 29, 2018





# Introduction

#### **Piz Daint: #3 supercomputer in the world**



Cray XC50, 5320 nodes

Intel Xeon E5-2690v3 12C, 2.6GHz, 64GB + NVIDIA Tesla P100 16GB 4.761 Teraflops / node





# **Piz Daint node layout**







No magic "silver bullet" exists!





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Usual steps in porting codes to GPUs





# No magic "silver bullet" exists!

Usual steps in porting codes to GPUs

- cleanup and refactor the code
- (possibly) change the data layout
- fully utilize CPU threads and prepare code for node-level parallelization
- move compute-intensive kernels to GPUs





#### CUDA (C / C++ / Fortran) OpenCL \_global\_\_ void add\_pw\_ekin\_gpu\_kernel(int num\_gvec\_\_, double alpha , 13 \_\_kernel void vector\_add(const int n, \_\_global float \*a, \_\_global float \*b, \_\_global float \*c) { 10 double const\* pw\_ekin\_, 14 const int i = get global id(0); 11 cuDoubleComplex const\* phi\_\_, if (i < n) { 15 12 cuDoubleComplex const\* vphi\_\_, 16 c[i] = a[i] + b[i];13 cuDoubleComplex\* hphi ) 17 } 14 18 } 15 int ig = blockIdx.x \* blockDim.x + threadIdx.x; 16 if (ig < num\_gvec\_\_) {</pre> 17 cuDoubleComplex z1 = cuCadd(vphi\_[ig], make\_cuDoubleComplex(alpha\_ \* pw\_ekin\_[ig] \* phi\_[ig].x, 18 alpha\_ \* pw\_ekin\_[ig] \* phi\_[ig].y)); 19 hphi\_\_[ig] = cuCadd(hphi\_\_[ig], z1); 20 } 21 }

#### OpenACC

- 76 acc = 0
  77 !\$acc parallel present(x)
- 78 !\$acc loop reduction(+:acc)
- 79 do i = 1, N
- 80 acc = acc + x(i) \* x(i)
- 81 enddo
- 82 **!\$acc end parallel**
- 83 call mpi\_allreduce(acc, accglobal, 1, MPI\_DOUBLE, MPI\_SUM, MPI\_COMM\_WORLD, err)

#### OpenMP 4.0

```
#pragma omp target data map(tofrom: x[0:n],y[0:n])
{
    #pragma omp target
    #pragma omp for
    for (int i = 0; i < n; i++)
        y[i] += a * x[i];
}</pre>
```















Computational scientists









Computational scientists



Supercomputer

CSCS





















**Electronic-structure codes** 

#### **Electronic structure codes**

Basis functions for KS states Atomic potential treatment	Periodic Bloch functions (plane-waves or similar)	Localized orbitals
Full-potential	FLEUR Wien2K Exciting Elk	FHI-aims FPLO
Pseudo-potential	VASP CPMD Quantum ESPRESSO Abinit Qbox	CP2K SIESTA OpenMX



## **Delta DFT codes effort**

• CSCS

Code	Version	Basis	Electron treatment	∆-value	Authors
WIEN2k	13.1	LAPW/APW+lo	all-electron	0 meV/atom	S. Cottenier [16] <mark></mark>
FHI-aims	081213	tier2 numerical orbitals	all-electron (relativistic atomic_zora scalar)	0.2 meV/atom	ASE [2,16] <mark></mark>
Exciting	development version	LAPW+xlo	all-electron	0.2 meV/atom	Exciting [10,16] <mark></mark>
Elk	3.1.5	APW+lo	all-electron	0.3 meV/atom	Elk [14,16] <mark>片</mark>
Quantum ESPRESSO	5.1	plane waves	SSSP Accuracy (mixed NC/US/PAW potential library)	0.3 meV/atom	QuantumESPRESSO [12,16]
FHI-aims	081213	tier2 numerical orbitals	all-electron (relativistic zora scalar 1e- 12)	0.3 meV/atom	ASE [2] 皆
VASP	5.2.12	plane waves	PAW 2015 GW-ready (5.4)	0.3 meV/atom	K. Lejaeghere [16] <mark></mark>
ABINIT	7.8.2	plane waves	PAW JTH v1.0	0.4 meV/atom	F. Jollet and M. Torrent Ѐ
FLEUR	0.26	LAPW (+lo)	all-electron	0.4 meV/atom	FLEUR [9,16] <mark></mark>



- Unit cell is mapped to a regular grid
- All functions are expanded in plane-waves
- All functions are expanded in plane trace. Atomic potential is replaced by a pseudopotential  $\hat{V}_{PS} = V_{loc}(\mathbf{r}) + \sum \sum |\beta_{\xi}^{\alpha}\rangle D_{\xi\xi'}^{\alpha}\langle \beta_{\xi'}^{\alpha}|$





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$$\varphi_{\mathbf{G}+\mathbf{k}}(\mathbf{r}) = \frac{1}{\sqrt{\Omega}} e^{i(\mathbf{G}+\mathbf{k})\mathbf{r}}$$





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Potential and density:

$$V(\mathbf{r}) = \sum_{\mathbf{G}} V(\mathbf{G}) e^{i\mathbf{G}\mathbf{r}} \qquad \rho(\mathbf{r}) = \sum_{\mathbf{G}} \rho(\mathbf{G}) e^{i\mathbf{G}\mathbf{r}}$$





- Approximation to atomic potential
- Core states are excluded
- Number of basis functions: ~1000 / atom
- Number of valence states: ~0.001 0.01% of the total basis size
- Efficient iterative subspace diagonalization schemes exist
- Atomic forces can be easily computed
- Stress tensor can be easily computed



- Unit cell is partitioned into "muffin-tin" spheres and interstitial region
- Inside MT spheres spherical harmonic expansion is used
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Basis functions:

$$\varphi_{\mathbf{G}+\mathbf{k}}(\mathbf{r}) = \begin{cases} \sum_{\ell m} \sum_{\nu=1}^{O_{\ell}^{\alpha}} A_{\ell m \nu}^{\alpha}(\mathbf{G}+\mathbf{k}) u_{\ell \nu}^{\alpha}(r) Y_{\ell m}(\hat{\mathbf{r}}) & \mathbf{r} \in \mathrm{MT}\alpha \\ \frac{1}{\sqrt{\Omega}} e^{i(\mathbf{G}+\mathbf{k})\mathbf{r}} & \mathbf{r} \in \mathrm{I} \end{cases}$$







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$$V(\mathbf{r}) = \begin{cases} \sum_{\ell m} V_{\ell m}^{\alpha}(r) Y_{\ell m}(\hat{\mathbf{r}}) & \mathbf{r} \in \mathrm{MT}\alpha \\ \sum_{\mathbf{G}} \ell m & V(\mathbf{G}) e^{i\mathbf{G}\mathbf{r}} & \mathbf{r} \in \mathrm{I} \end{cases} \qquad \rho(\mathbf{r}) = \begin{cases} \sum_{\ell m} \rho_{\ell m}^{\alpha}(r) Y_{\ell m}(\hat{\mathbf{r}}) & \mathbf{r} \in \mathrm{MT}\alpha \\ \sum_{\mathbf{G}} \ell m & \rho(\mathbf{G}) e^{i\mathbf{G}\mathbf{r}} & \mathbf{r} \in \mathrm{I} \end{cases}$$





- No approximation to atomic potential
- Core states are included
- Number of basis functions: ~100 / atom
- Number of valence states: ~15-20% of the total basis size
- Large condition number of the overlap matrix
- Full diagonalization of dense matrix is required (iterative subspace diagonalization schemes are not efficient)
- Atomic forces can be easily computed
- Stress tensor can't be easily computed (N-point numerical scheme is often required)





# Common features of the FP-LAPW and PP-PW methods

- Definition of the unit cell (atoms, atom types, lattice vectors, symmetry operations, etc.)
- Definition of the reciprocal lattice, plane-wave cutoffs, **G** vectors, **G+k** vectors
- Definition of the wave-functions
- FFT driver
- Generation of the charge density on the regular grid
- Generation of the XC-potential
- Symmetrization of the density, potential and occupancy matrices
- Low-level numerics (spherical harmonics, Bessel functions, Gaunt coefficients, spline interpolation, Wigner D-matrix, linear algebra wrappers, etc.)







# **SIRIUS** library

# Motivation for a common domain specific library

Extend the legacy Fortran codes with the API calls to a domain-specific library which runs on GPUs and other novel architectures.







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#### Where to draw the line?



#### Output:

wave-functions  $\psi_j(\mathbf{r})$  and eigen energies  $\varepsilon_j$ charge density  $\rho(\mathbf{r})$  and magnetization  $\mathbf{m}(\mathbf{r})$ total energy  $E_{tot}$ , atomic forces  $\mathbf{F}_{\alpha}$  and stress tensor  $\sigma_{\alpha\beta}$ 





# **SIRIUS** library

- full-potential (L)APW+lo
  - non-magnetic, collinear and non-collinear magnetic ground states
  - non-relativistic, ZORA and IORA valence solvers
  - Dirac solver for core states
- norm-conserving, ultrasoft and PAW pseudopotentials
  - non-magnetic, collinear and non-collinear magnetic ground states
  - spin-orbit correction
  - atomic forces
  - stress tensor
  - Gamma-point case



#### **SIRIUS** library

CSCS

# https://github.com/electronic-structure/SIRIUS

**SIRIUS** is a collection of classes that abstract away the different building blocks of PW and LAPW codes. The class composition hierarchy starts from the most primitive classes (**Communicator**, **mdarray**, etc.) and progresses towards several high-level classes (**DFT\_ground\_state**, **Band**, **Potential**, etc.). The code is written in C++11 with MPI, OpenMP and CUDA programming models.

		DFT_grou	nd_state				
Band							
	Local_operator						
	Potential					_	
	Densit	У					
K_poin	it_set						
К_рс	pint	_					
Non_local_	operator						
Beta_pro	jectors	Periodi	c_function	Matc	hing_coefficients		
Simulation_context							
Unit_cell	Radial_integ	grals	Au	ugmentation_operator		Step	_function
Atom_type	Radial_	grid					
Atom	Spline	)					
Eigensolver Wave functions				;			
dmatrix							
BLACS_grid	FFT3D						
MPI_grid	Gvec						
Communicat	ndarray	splind	lex	matrix3d	veo	ctor3d	



#### **Doxygen documentation**

#### https://electronic-structure.github.io/SIRIUS-doc/



Do[Print[FullSimplify[D[Rlm[1, m, theta, phi], theta]]], {1, 0, 4}, {m, -1, 1}]

Do[Print[FullSimplify[TrigExpand[D[Rlm[1, m, theta, phi], phi]/Sin[theta]]]], {1, 0, 4}, {m, -1, 1}]



pw ekin



#### **Development cycle**

## https://github.com/electronic-structure/q-e



# Example of QE/SIRIUS interoperability

QE	Initialization	phase	SIRIUS		
read input file, read pseudopotentials, create a list of k-points, initialize data structures, communicators, etc.					
set unit cell parameters (lattice vectors, atom types, atomic positions, etc.), cutoffs and other parameters					
		initialize s	simulation context		
	set k-p	oints			
initialize			<_point_set class		
		initialize Density class			
		initiali	ze Potential class		
	initialize DFT_ground_state class				
		gene	rate initial density		
	get rho( <b>G</b> )	and mag(	G)		



# Example of QE/SIRIUS interoperability



**ETH** zürich





🀼 cscs		Number	of nodes	<b>ETH</b> zürich
0 —	1	2	5	10
-				
500 <u> </u>				
to solutio				
ົດອີ່ 1500				
2000				
	QE (CPU)	QE+SIRIUS (CPU)	QE+SIRIUS (KNL)	QE+SIRIUS (GPU)





Performance benchmark of the QE and SIRIUS-enabled QE codes for the 64-atom unit cell of Si<sub>1-x</sub>Ge<sub>x</sub> The runs we performed on hybrid nodes with 12-core Intel Haswell @2.5GHz + NVIDIA Tesla P100 card (GPU), on dual socket 18-core Intel Broadwell @2.1GHz nodes (CPU) and on nodes with 64-core Intel Xeon Phi processor @1.3 GHz (KNL). Time for the full 'vc-relax' calculation is reported.



ETH zürich

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ETH zürich



	QE (CPU)	QE+SIRIUS (CPU)	QE+SIRIUS (KNL)	QE+SIRIUS (GPU)	
400 —					
(;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;					
to solution					
Line 100					
0 —	18		32	50	
CSCS		Nur	nber of nodes		<b>ETH</b> zürich









Performance benchmark of the QE and SIRIUS-enabled Exciting codes for the 96-atom unit cell of Mn metalorganic framework. The runs we performed on dual socket 18-core Intel Broadwell @2.1GHz nodes (CPU) and on hybrid nodes with 12-core Intel Haswell @2.5GHz + NVIDIA Tesla P100 card (GPU).



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Exciting (CPU, sequential diagonalization with MKL)

Exciting+SIRIUS (CPU, sequential diagonalization with MKL) Exciting+SIRIUS (CPU, parallel diagonalization with ELPA) Exciting+SIRIUS (GPU, sequential diagonalization with MAGMA)

	-		Number	of nodes		
CSCS	0	12	24	96	216	<b>FTH</b> züric
Tim	75					
le to so	150					
olution	225					
(minutes) 300 (minutes)	300					
	375					
Z	450					

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# Thank you for your attention.