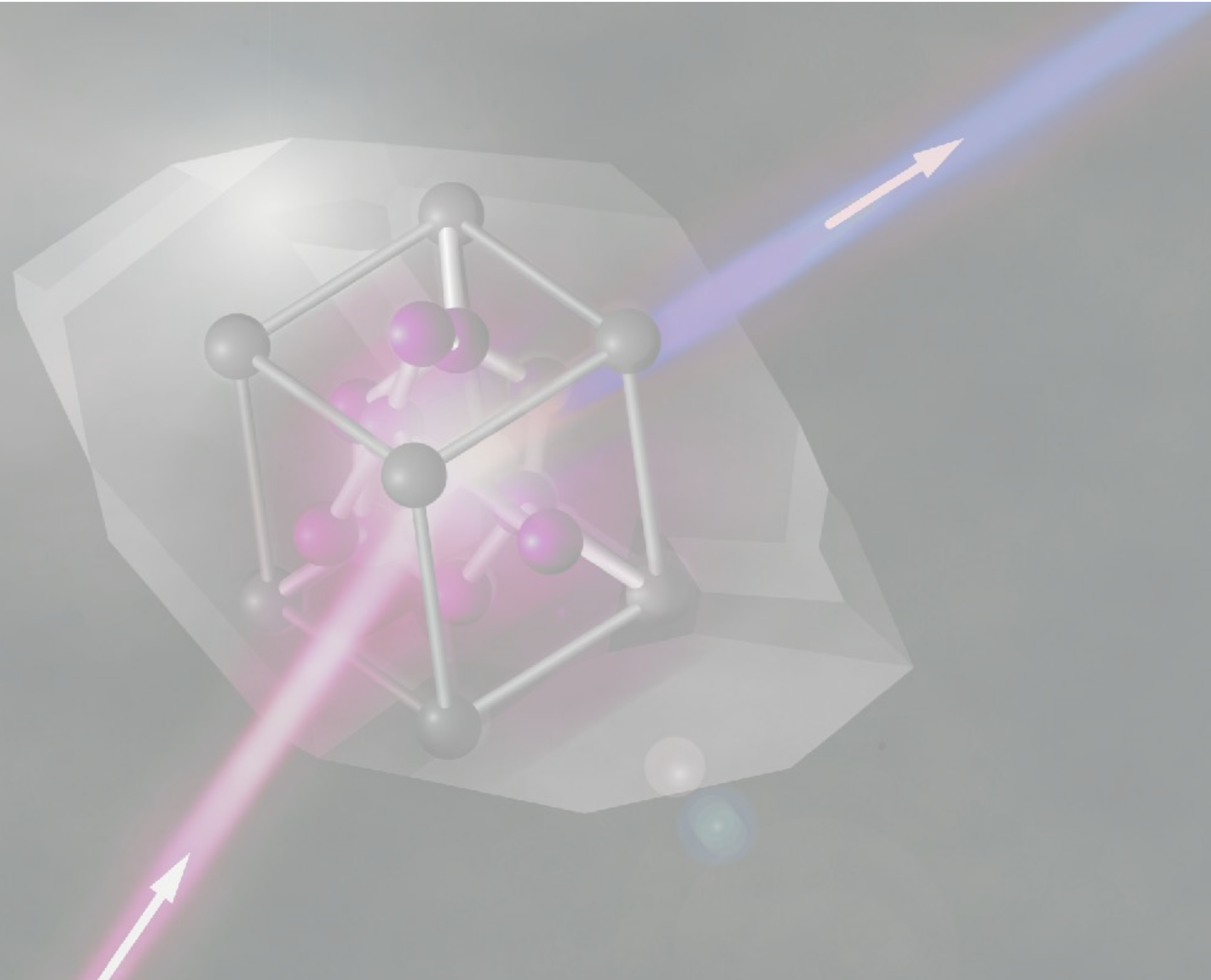


Non-linear processes in X-ray scattering experiments

School on Synchrotron and Free-Electron Laser Methods for Multidisciplinary Applications

Martin Beye,
ICTP Trieste,
May 18, 2018



Outline

From theoretical field interactions to real experiments

Theory

- From Schrödinger to density matrix
- Field interactions vs. photons: coherence
- Fundamental dipole transitions and the vacuum
- Multi-wave mixing schemes

Experiment

- MUSIX
- Heterodyne detection with X-rays
- Amplified spontaneous emission
- Concurrent processes
- Stimulated emission

Concept of field interactions and coherences

Some theory

How does a laser pulse interact with a quantum system?

Time-dependent Schrödinger equation:

$$i\hbar \frac{\partial}{\partial t} |\Psi\rangle = \hat{H} |\Psi\rangle$$

with electric field as perturbation:

$$\hat{H} = \hat{H}_0 + \hat{W}(t)$$

$$\hat{W}(t) = \hat{\mu} \mathcal{E} \cos(\omega t)$$

Assume Eigenstates:

$$\hat{H}_0 |n\rangle = E_n |n\rangle$$

General time-dependent (perturbation) solution:

$$|\Psi(t)\rangle = \sum_n c_n e^{-iE_n t/\hbar} |n\rangle$$

Concept of field interactions and coherences

Laser pulse couples ground state and first excited state

After a (short) pulse coupling the ground and first excited states, the system is in a coherent superposition:

$$|\Psi(t)\rangle = c_0 e^{-iE_0 t/\hbar} |0\rangle + i c_1 e^{-iE_1 t/\hbar} |1\rangle$$

$|0\rangle$ s-orbital

$|1\rangle$ p-orbital



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Concept of field interactions and coherences

Polarisation after such a pulse

$$|\Psi(t)\rangle = c_0 e^{-iE_0 t/\hbar} |0\rangle + i c_1 e^{-iE_1 t/\hbar} |1\rangle$$

$$P(t) = \langle \hat{\mu} \rangle = \langle \Psi(t) | \hat{\mu} | \Psi(t) \rangle$$

$$= \left(c_0 e^{iE_0 t/\hbar} \langle 0| - i c_1 e^{E_1 t/\hbar} \langle 1| \right) \hat{\mu} \left(c_0 e^{-iE_0 t/\hbar} |0\rangle + i c_1 e^{-iE_1 t/\hbar} |1\rangle \right)$$

$$= c_0 c_1 \langle 0 | \hat{\mu} | 1 \rangle \sin(\omega_{01} t) + c_0^2 \langle 0 | \hat{\mu} | 0 \rangle + c_1^2 \langle 1 | \hat{\mu} | 1 \rangle$$

$$\equiv c_0 c_1 \mu_{01} \sin(\omega_{01} t)$$

$$\propto +\mu_{01}^2 \sin(\omega_{01} t)$$

Polarisation oscillates with $\omega_{01} = (E_1 - E_0) / \hbar$

radiates field proportional to $-\mu_{01}^2 \cos(\omega_{01} t)$

Out of phase with exciting field: exciting field is „attenuated“ (destructive interference)

Concept of field interactions and coherences

The radiation from this coherent state is a second interaction with the field and transfers population

$$|\Psi(t)\rangle = c_0 e^{-iE_0 t/\hbar} |0\rangle + i c_1 e^{-iE_1 t/\hbar} |1\rangle$$

This state can be represented in a density matrix.

Directly after the laser pulse, without dephasing or population relaxation, this yields:

$$\rho_{00}(t) = c_0^2 = \text{const.}$$

$$\rho_{11}(t) = c_1^2 = \text{const.}$$

$$\rho_{01}(t) = -i c_0 c_1 e^{+i\omega_{01} t}$$

$$\rho_{10}(t) = i c_0 c_1 e^{-i\omega_{01} t}$$

for maximal pulse strength:

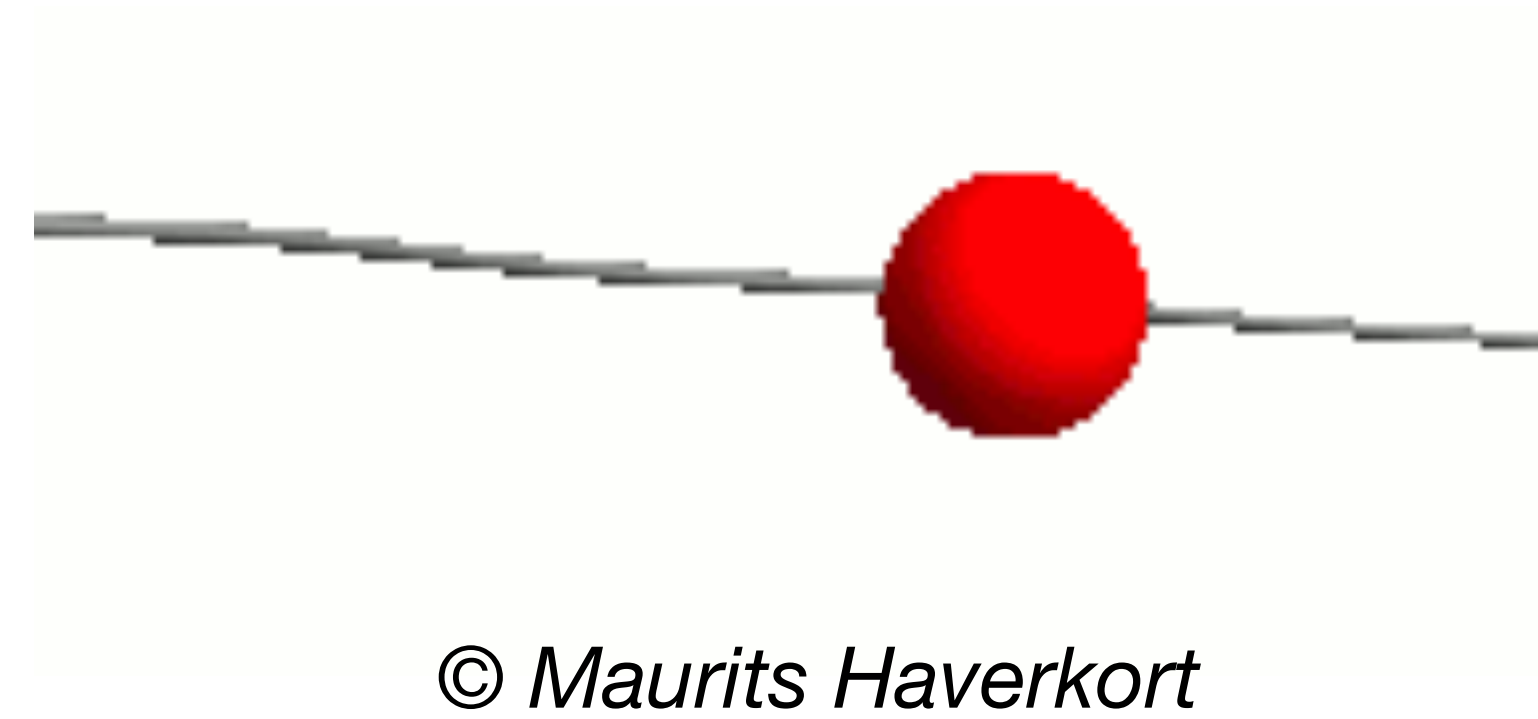
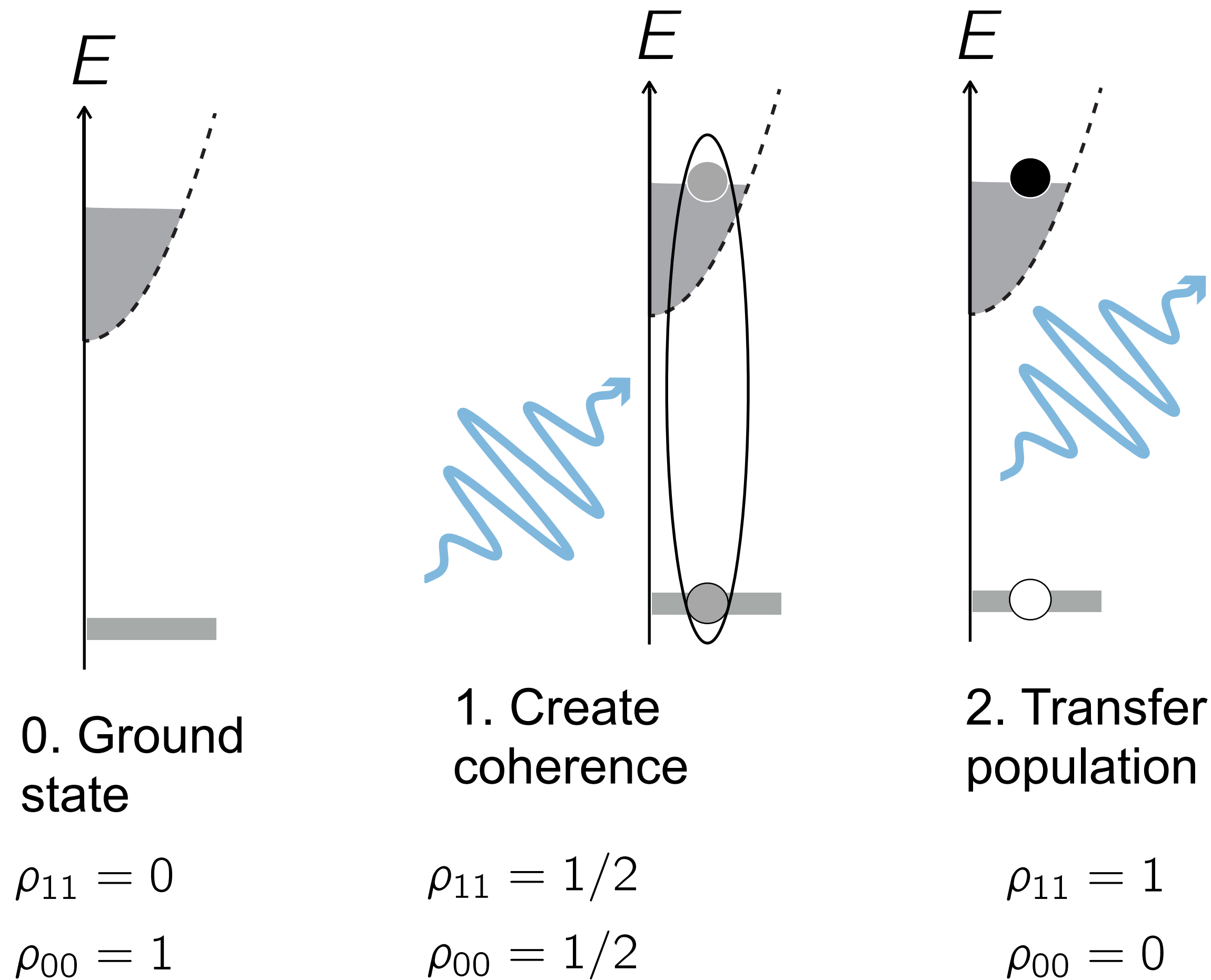
$$\rho(t=0) = \begin{pmatrix} 1/2 & -i/2 \\ +i/2 & 1/2 \end{pmatrix}$$

Diagonal elements are called „populations“.

Off-diagonal elements are „coherences“.

Field interactions and level schemes (population spectroscopies)

Described one field interaction. Absorption becomes real with second field interaction



What is a „coherence“?

From quantum optics to experiment: Sidebands vs streaking

Coherence is a well-defined phase relation.

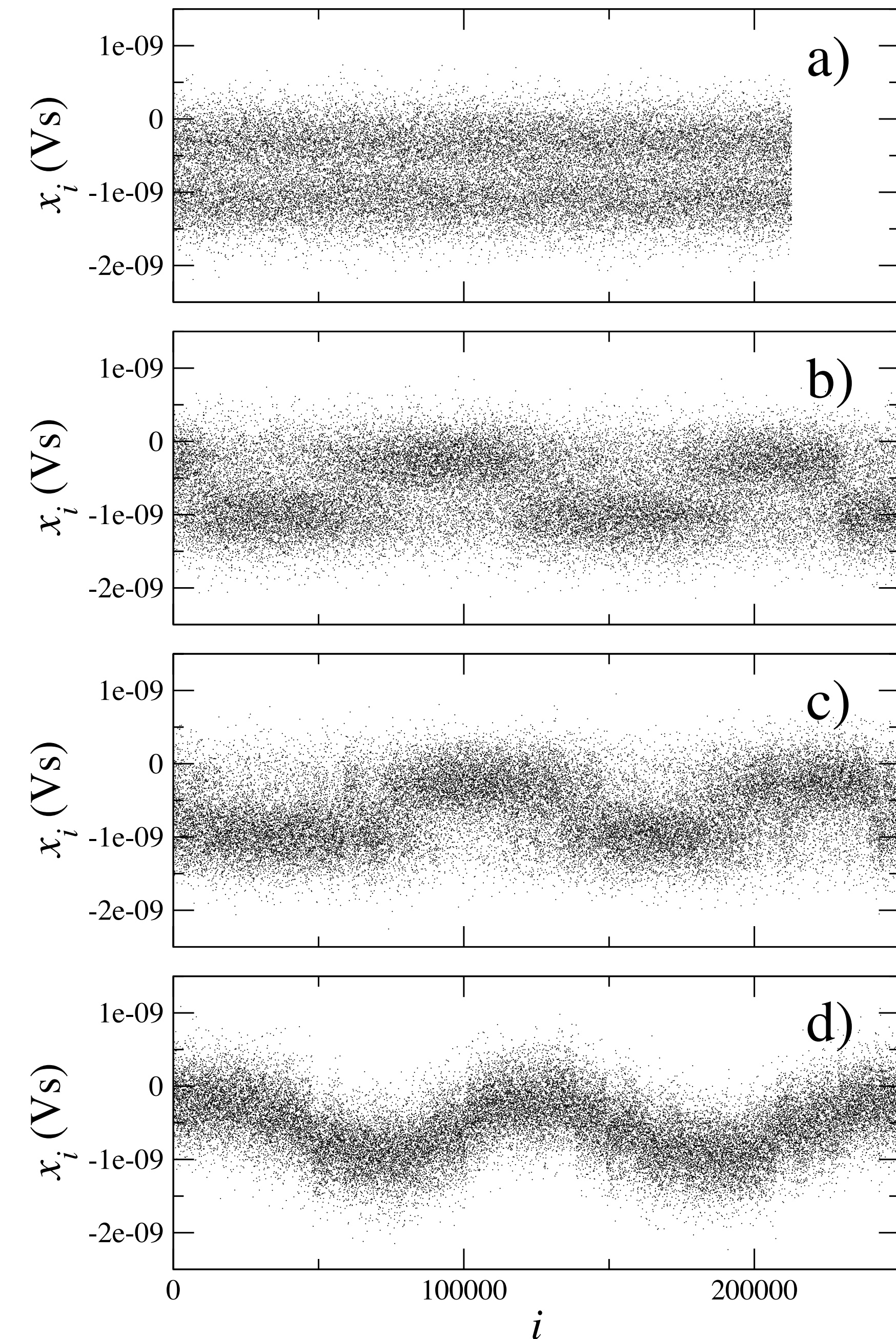
Quantum optics of photon / electric field

Coherent state:

- Well-defined (electric field) phase
- Undefined photon number

Fock state (number state):

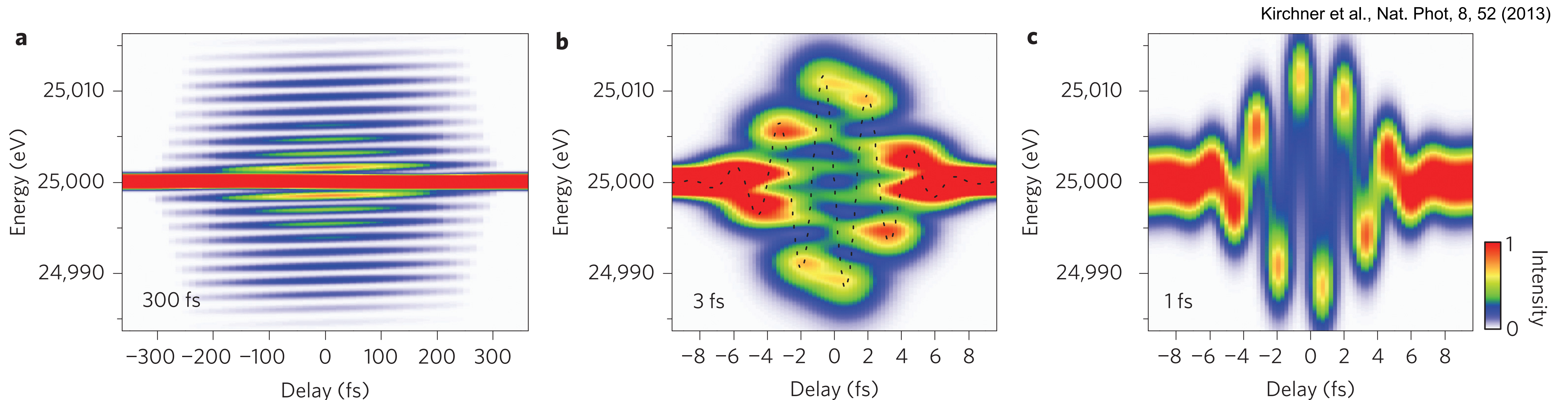
- Undefined phase
- Well-defined photon number



What is a „coherence“?

From quantum optics to experiment: Sidebands vs streaking

Interaction of an electric field (photons) with electrons:



Sidebands:

Well-defined photon number

Undefined phase

Streaking:

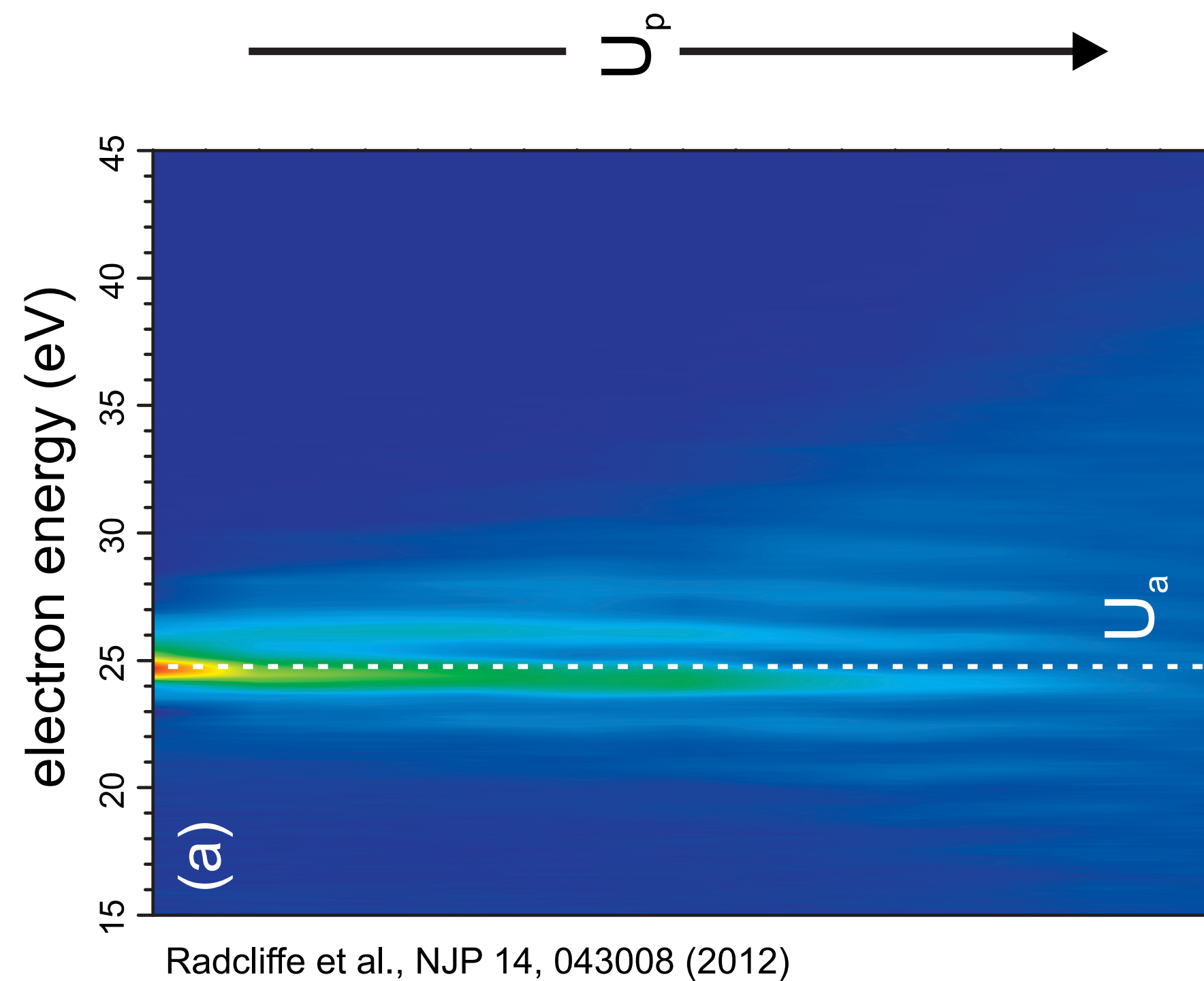
Undefined photon number

Well-defined phase

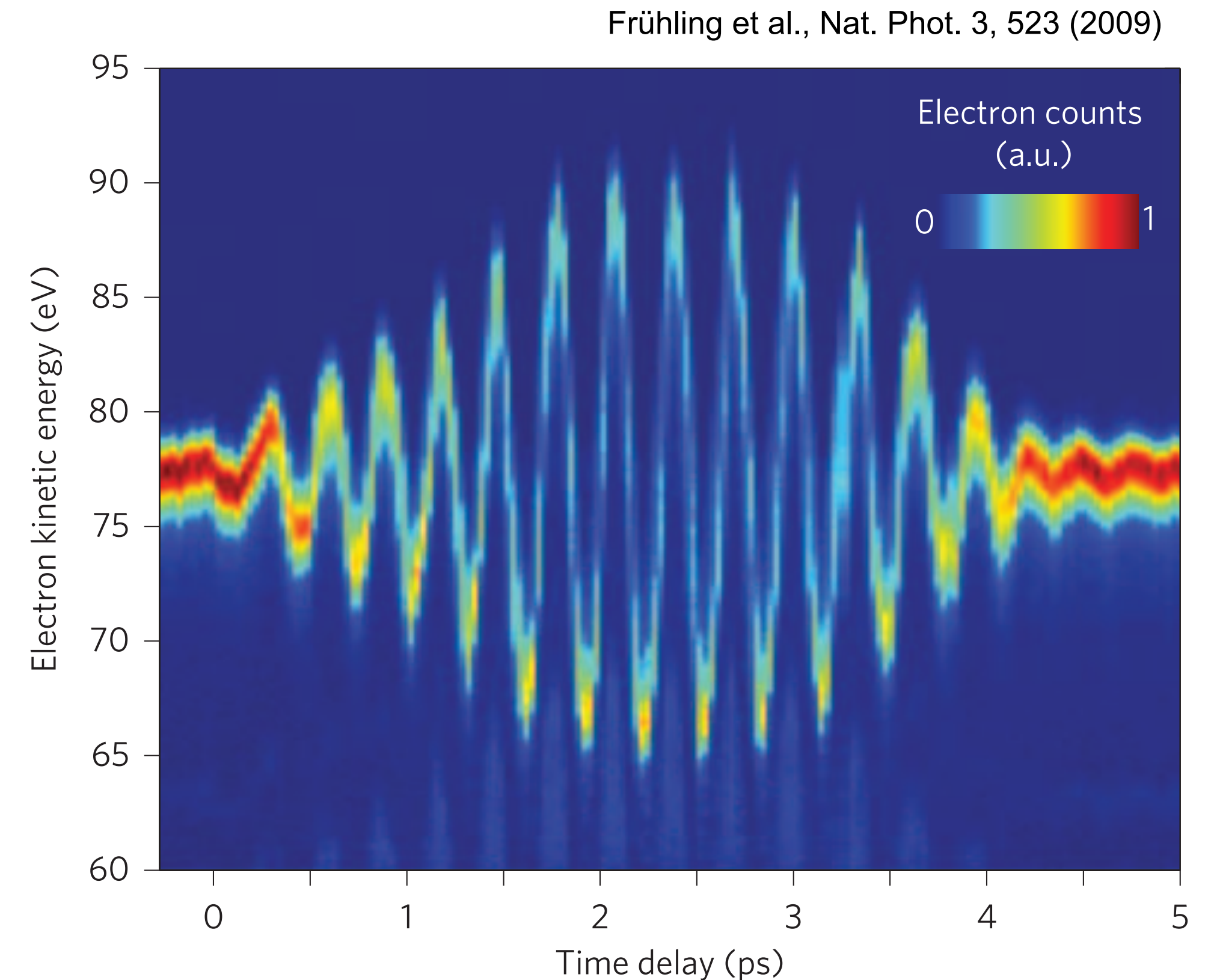
What is a „coherence“?

From quantum optics to experiment: Sidebands vs streaking

Experimental results from FLASH



Sidebands:
Well-defined photon number
Undefined phase



Streaking:
Undefined photon number
Well-defined phase

Field interaction vs. photon interaction

One photon interaction can be regarded as two field interactions ($cc^* = |c|^2$)

In the photon picture the phase is lost.

Population is transferred with two (identical) field interactions.

(Synchrotron spectroscopies are nearly always „population spectroscopies“:

-incoherent (no phase relation)

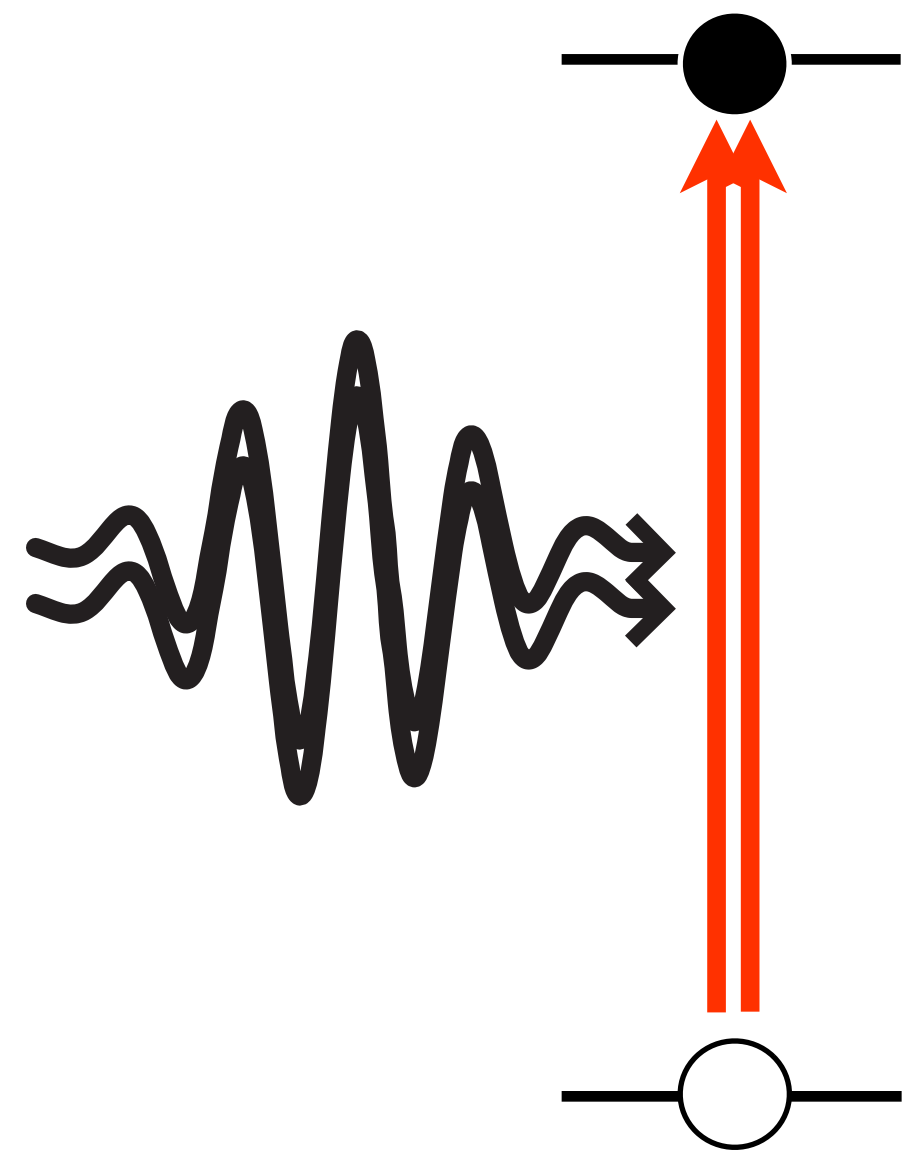
-well-defined number of transitions.

Coherence only becomes relevant at FELs:

-large number of coherent photons)

Fundamental dipole interactions / Photon transitions

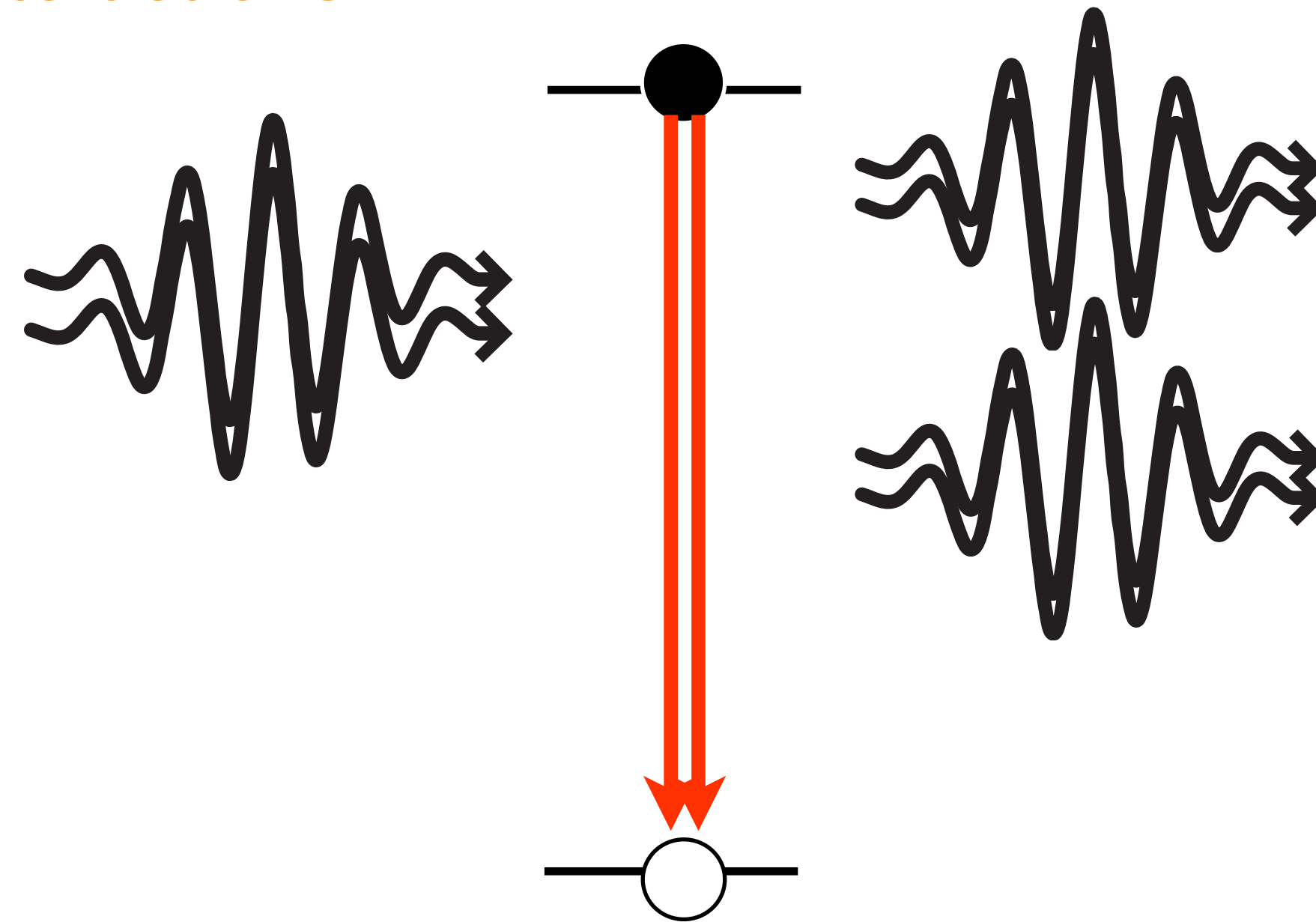
„Two-wave mixing“, two field interactions



Absorption

$$\langle e, N - 1 | \vec{d} | g, N \rangle$$

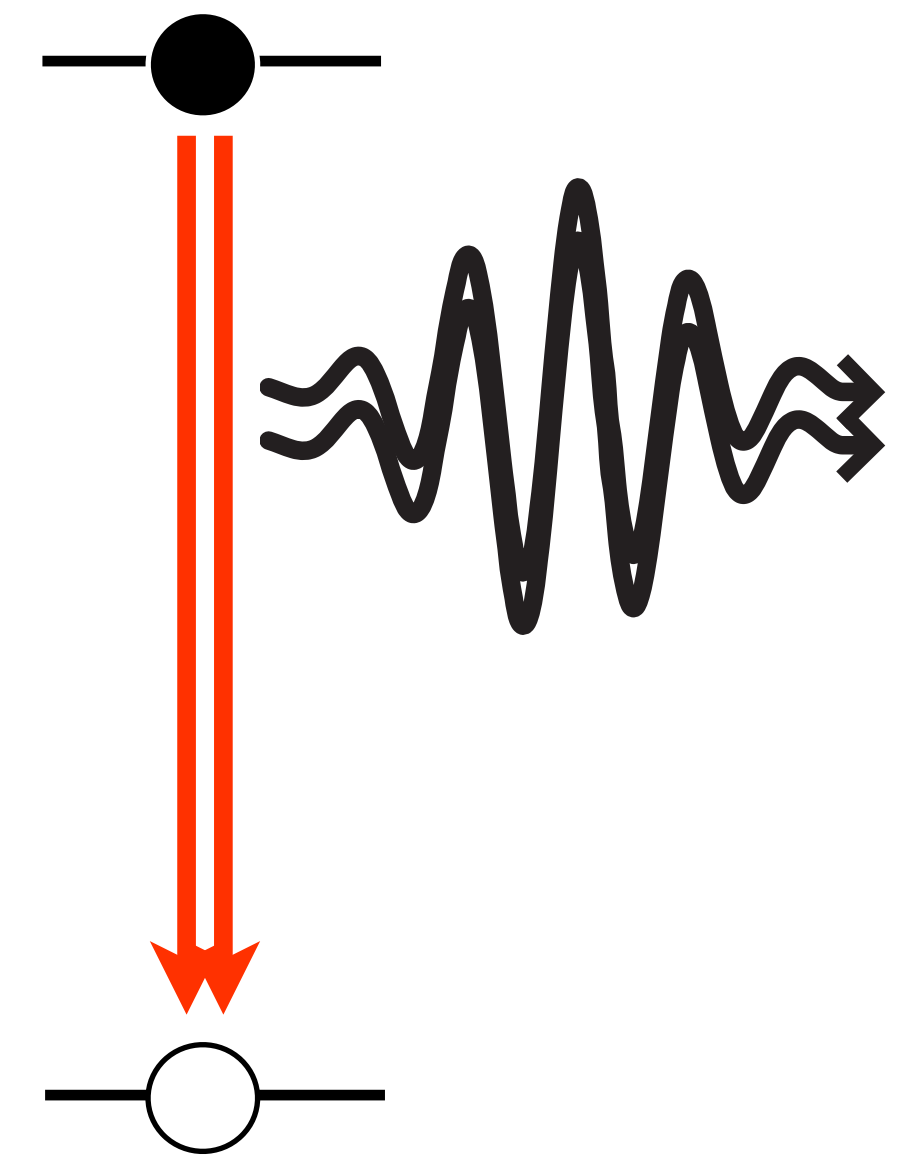
$$P_{abs} = N \sigma \rho_g d$$



Stimulated Emission

$$\langle g, N | \vec{d} | e, N - 1 \rangle$$

$$P_{stim} = N \sigma \rho_e d$$

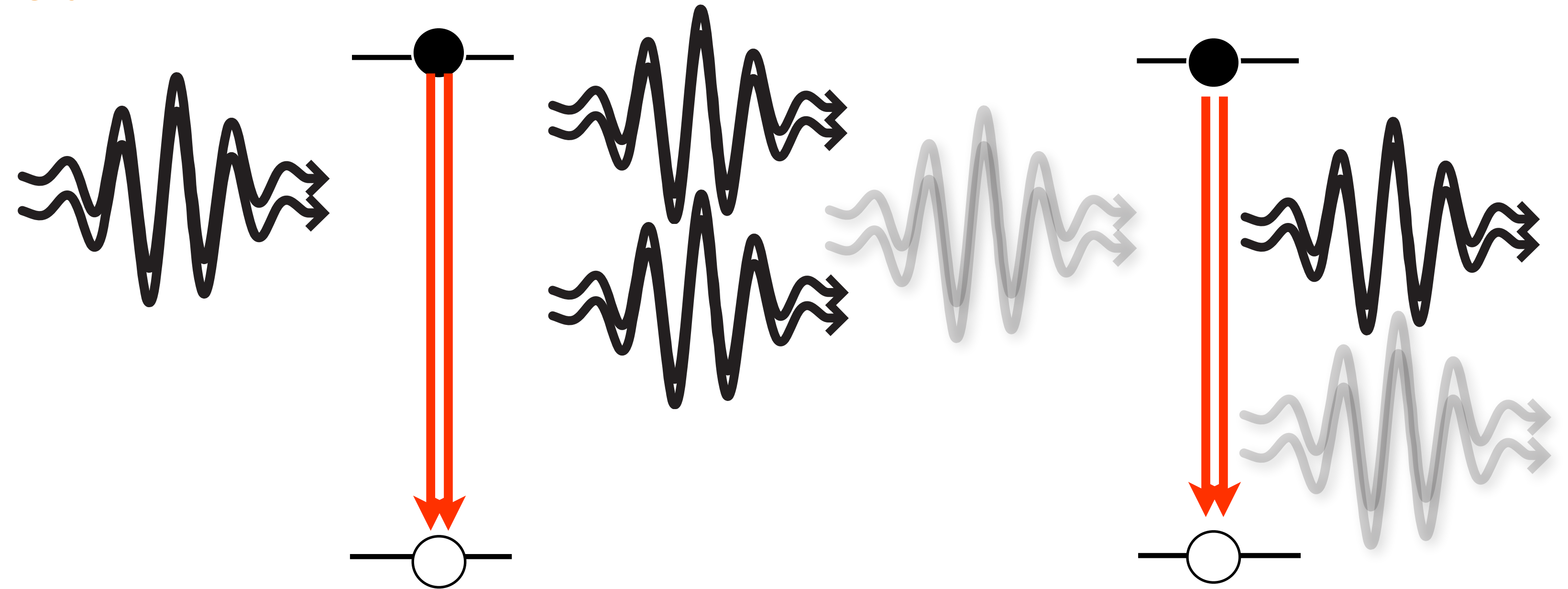
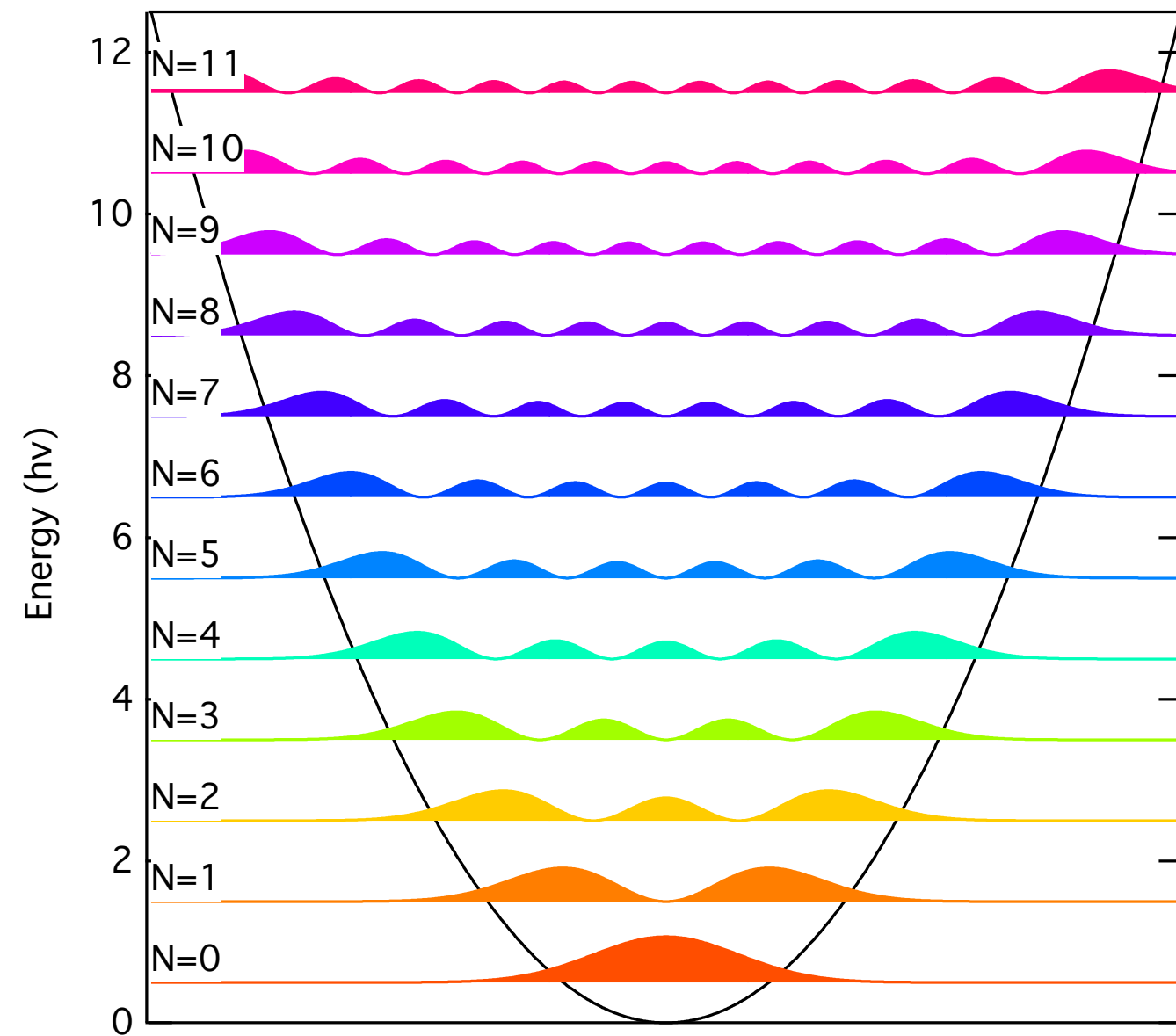


Spontaneous Emission

$$\langle g, 1 | \vec{d} | e, 0 \rangle$$

Spontaneous emission

Is stimulated by the zero-point field



Stimulated Emission

Spontaneous Emission

$$E_n = \hbar\omega \left(N + \frac{1}{2} \right)$$

$$\langle g, N | \vec{d} | e, N - 1 \rangle$$

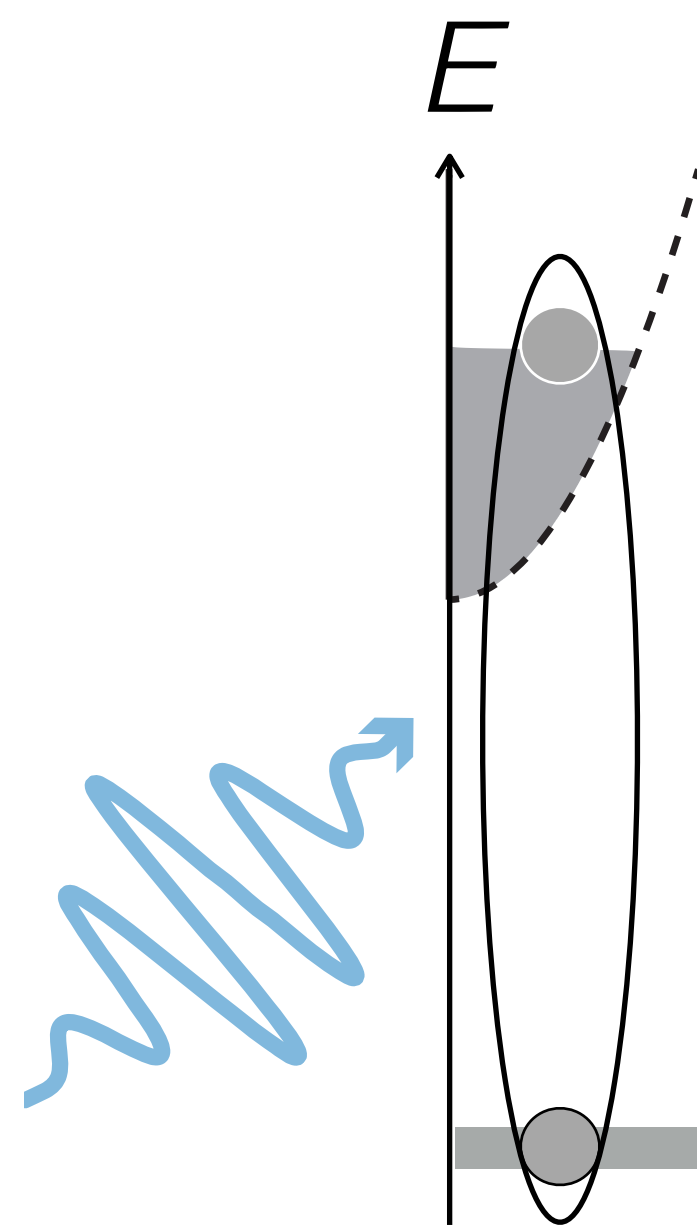
$$\langle g, 1 | \vec{d} | e, 0 \rangle$$

$$P_{stim} = N\sigma\rho_e d > P_{spon} = N_{vac}\sigma\rho_e d$$

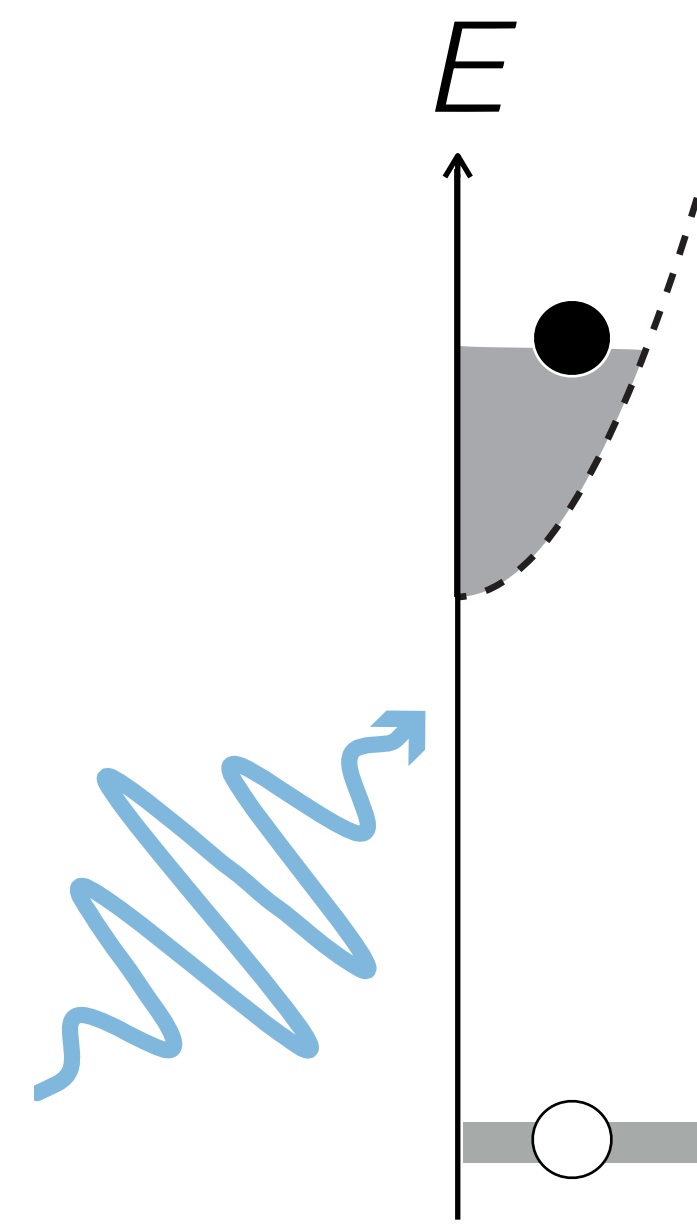
$$N > N_{vac}$$

Everything is four-wave mixing

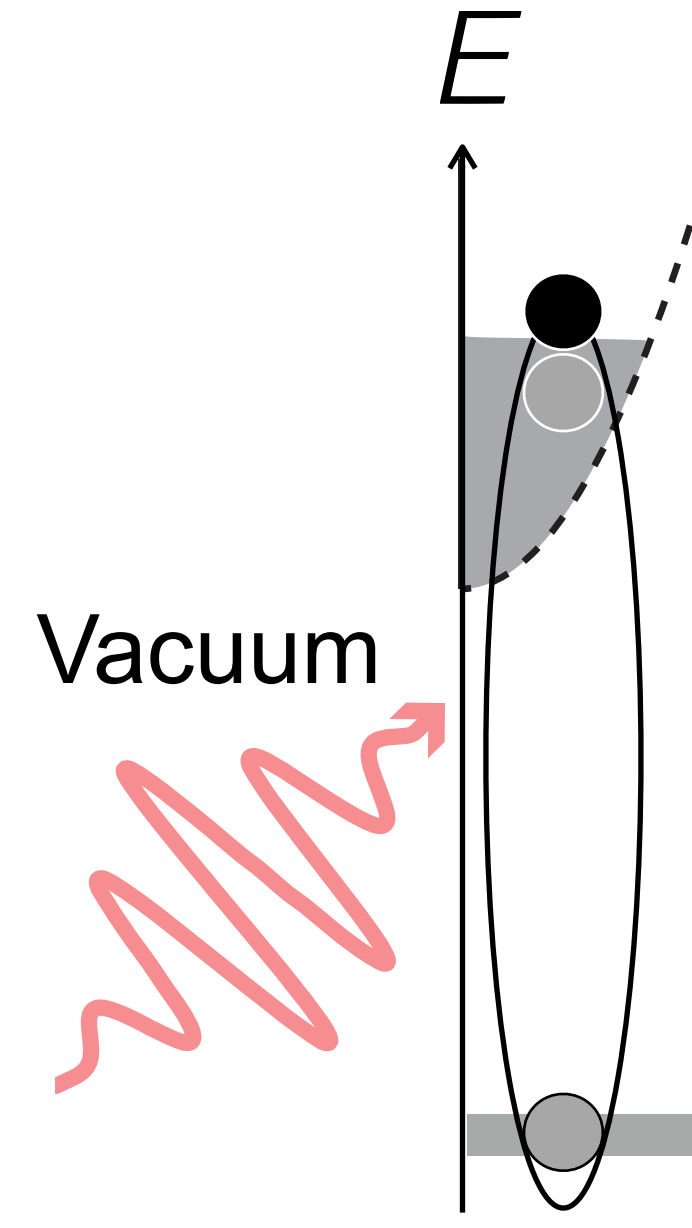
RIXS / XES (population spectroscopies - incoherent, zero-point field)



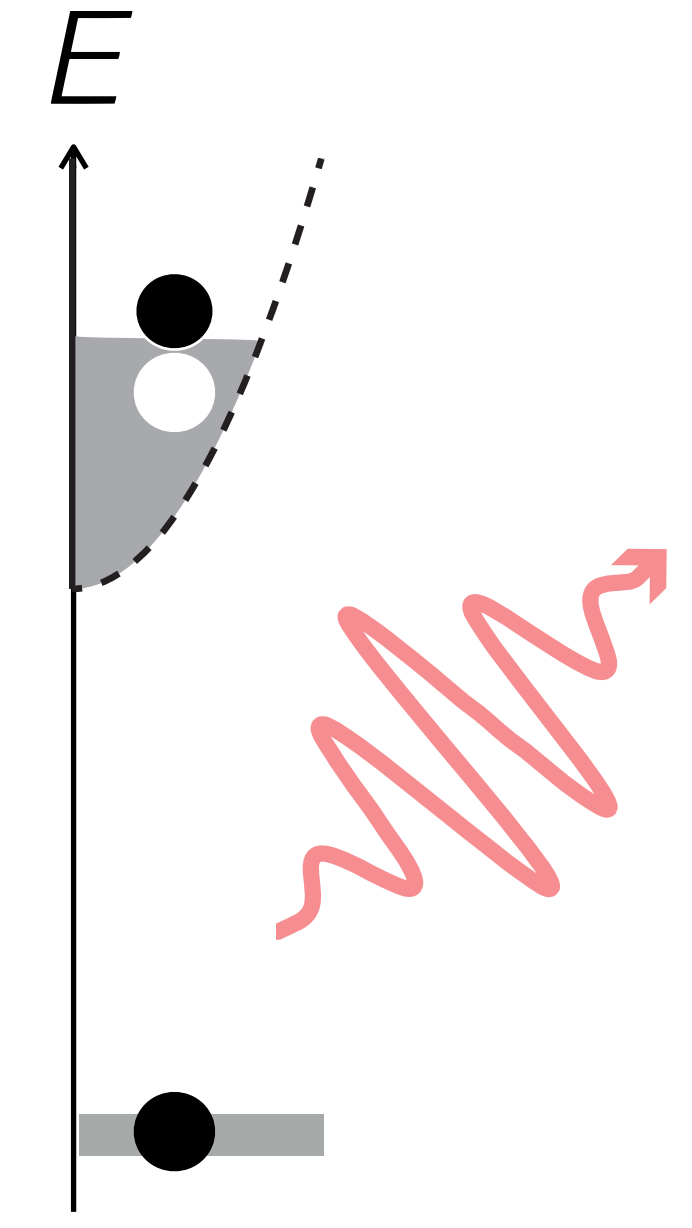
1. Create coherence



2. Transfer population



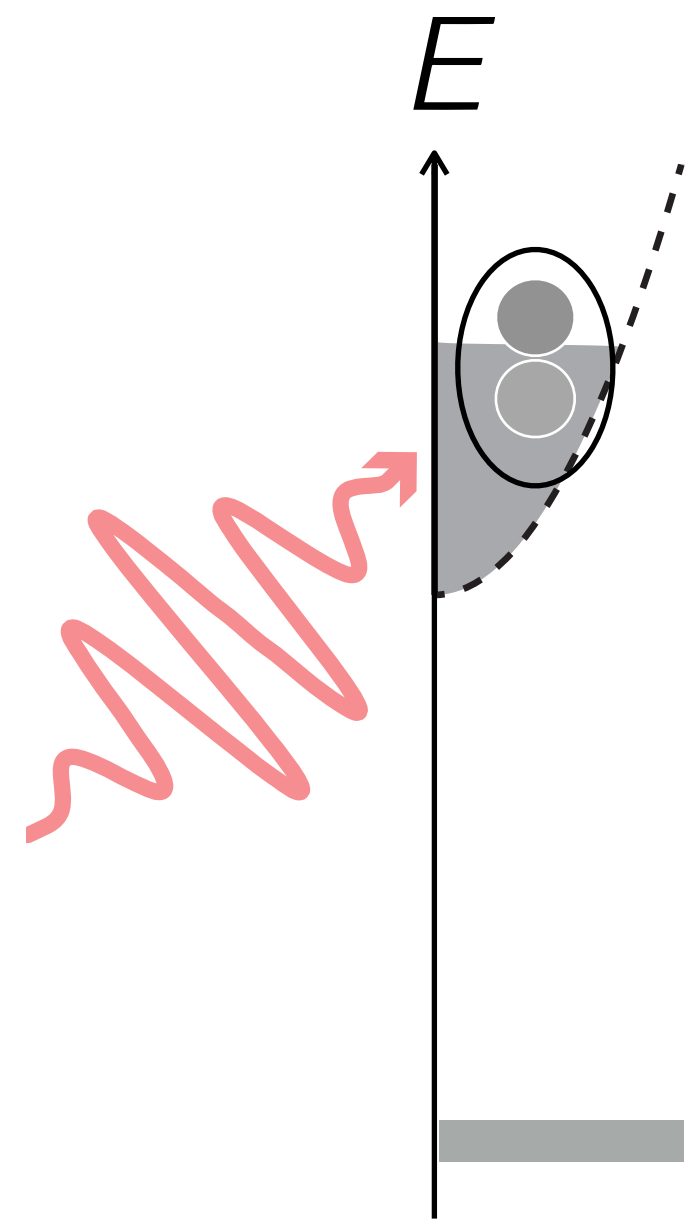
3. Create coherence



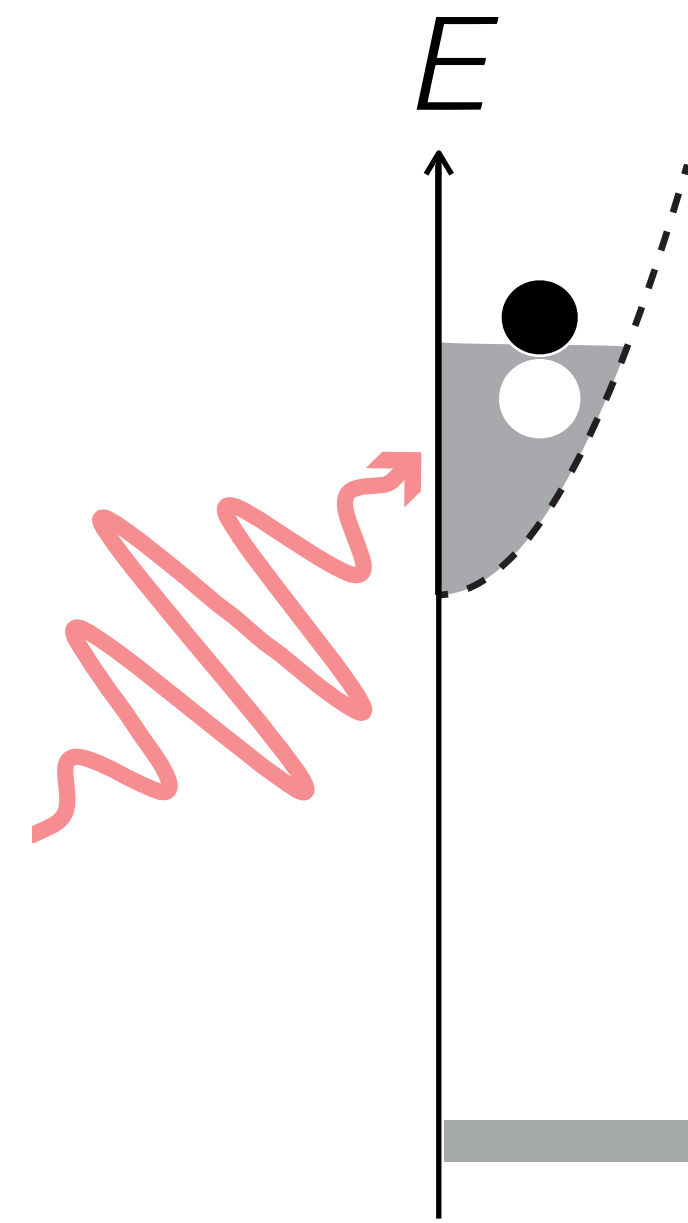
4. Emit photon

Everything is four-wave mixing

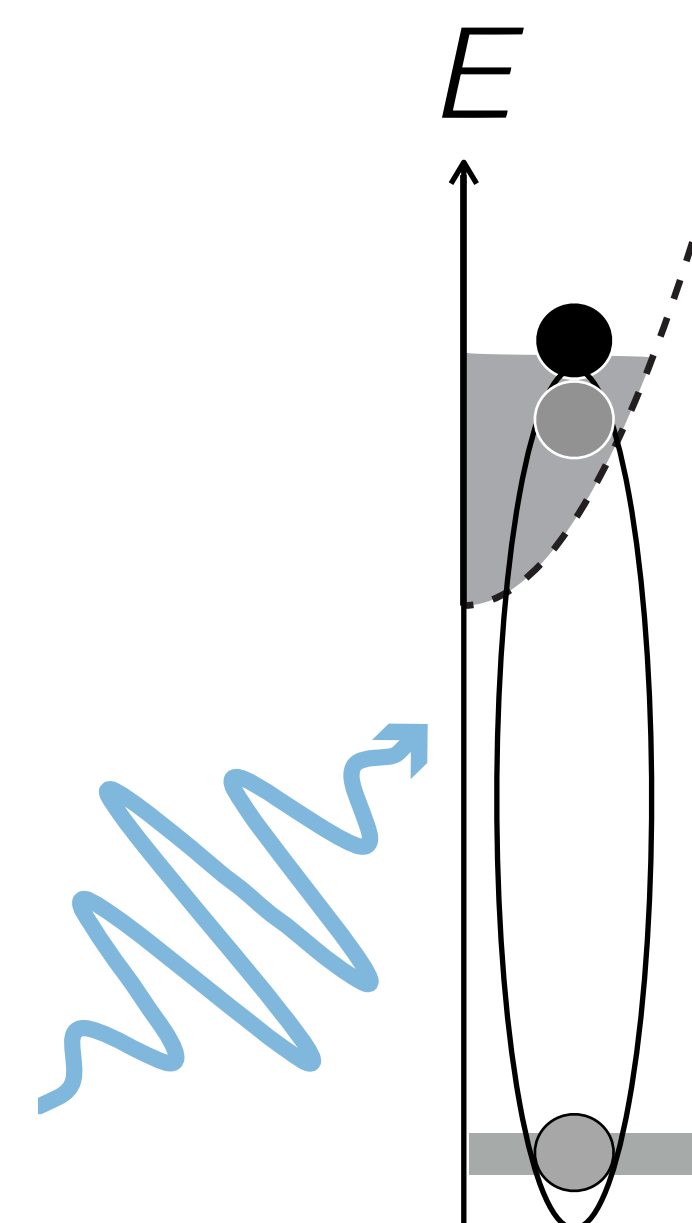
Pump probe—XAS (population spectroscopies - incoherent)



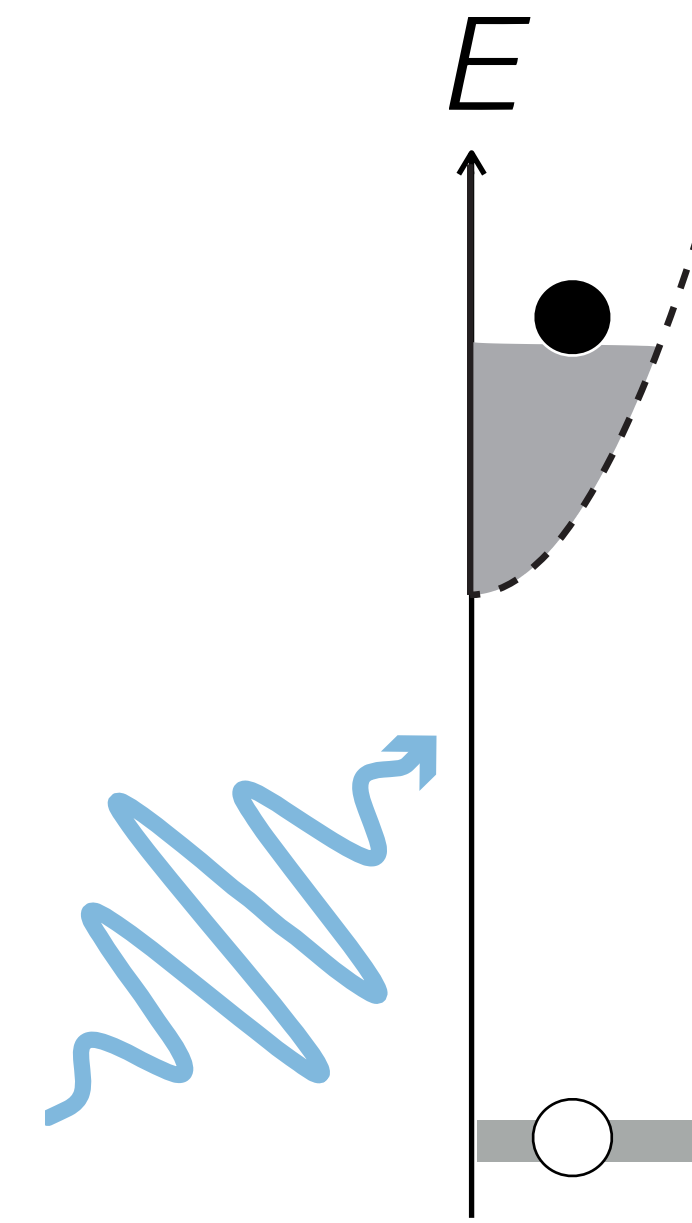
1. Create coherence



2. Transfer population



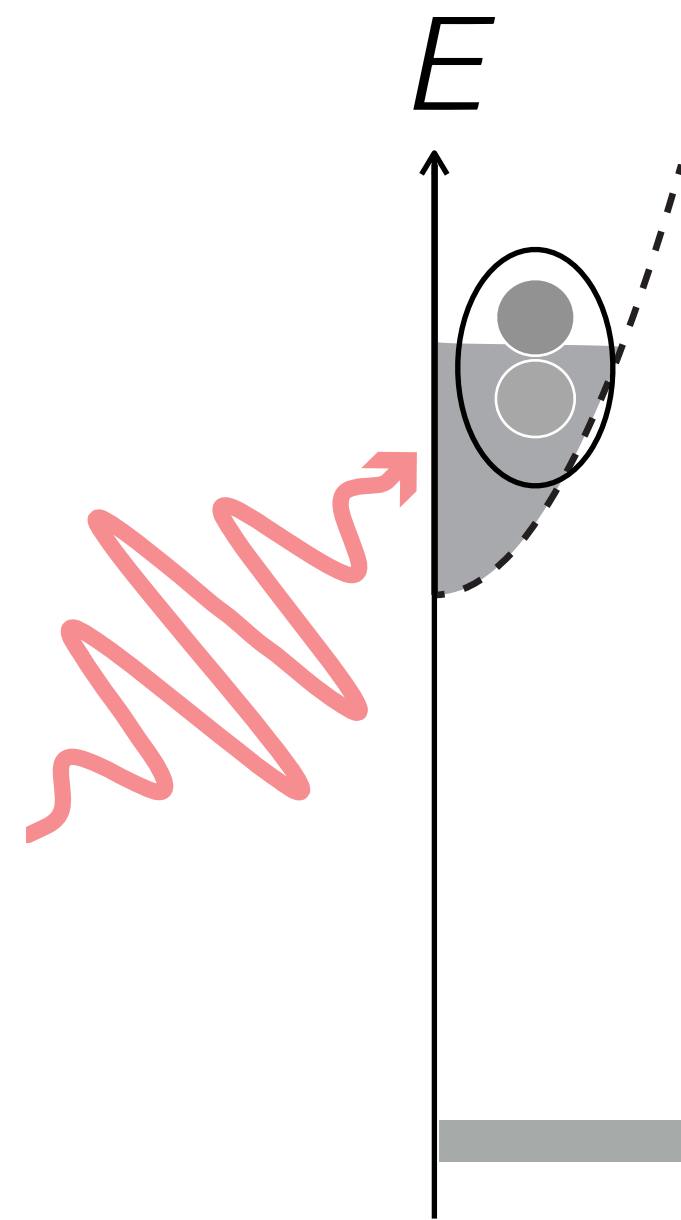
3. Create coherence



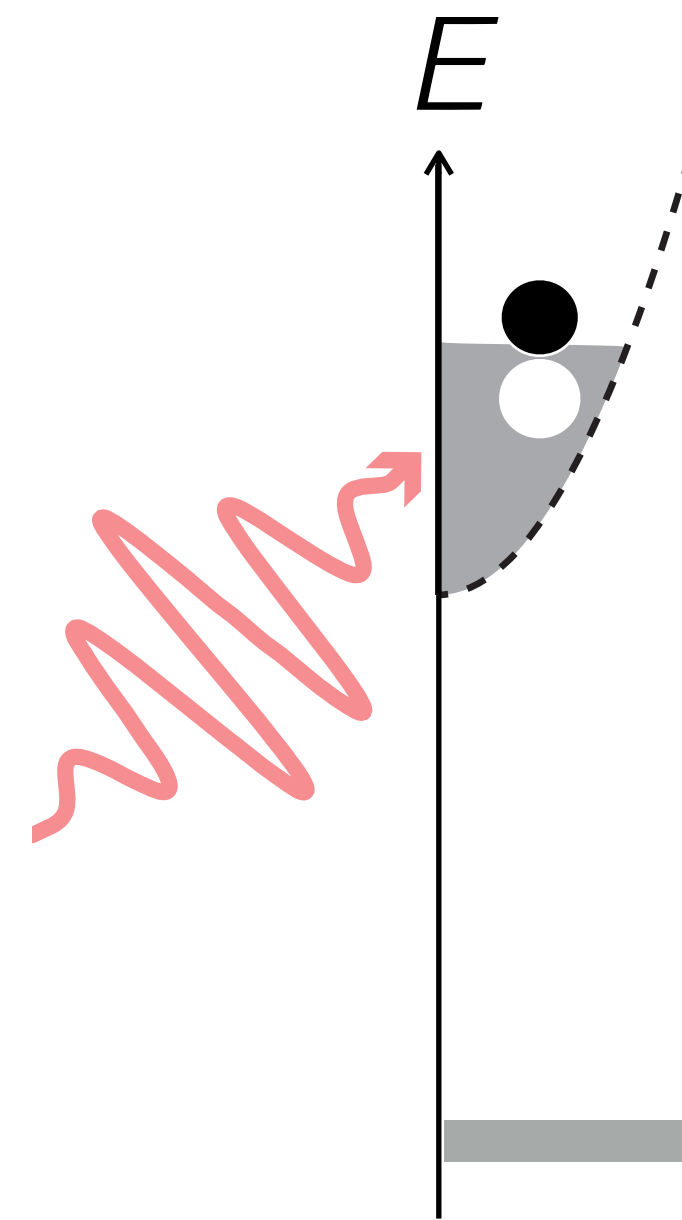
4. Absorb photon

Everything is four-wave mixing

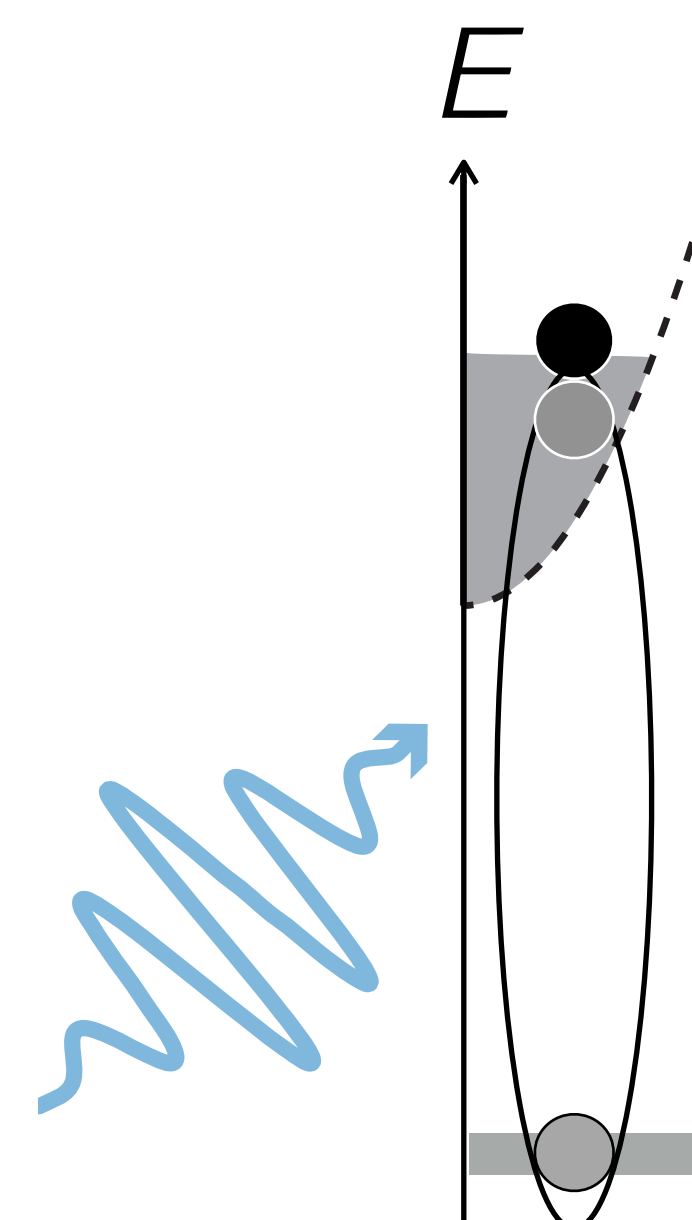
Claudio's transient gratings (but now coherent!)



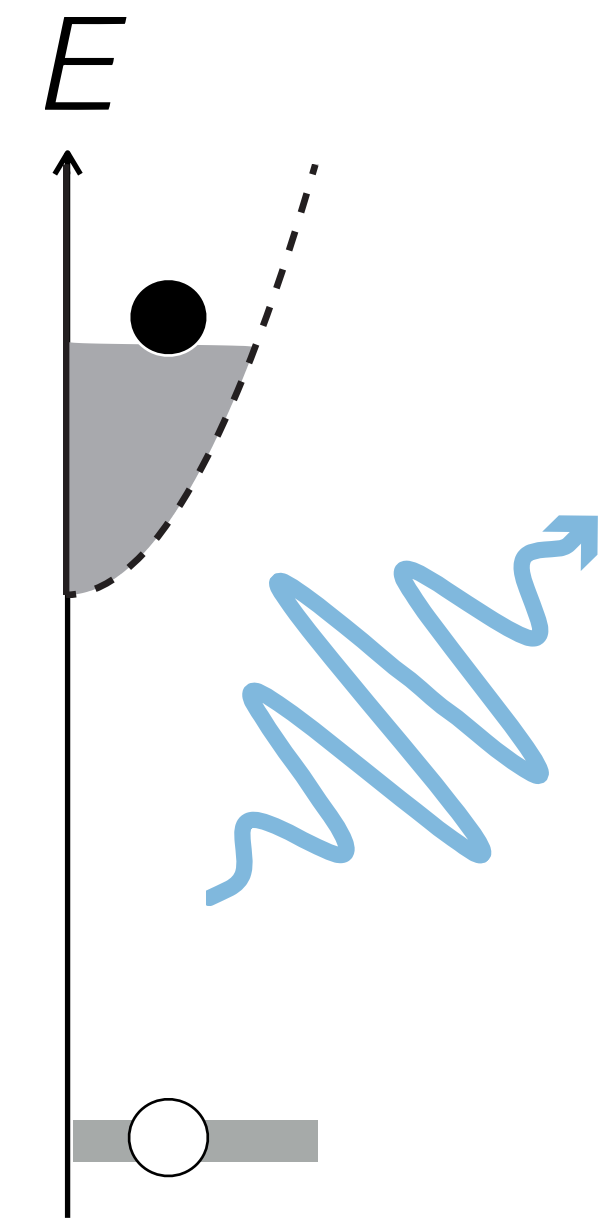
1. Create coherence



2. Transfer population (spatially modulated)



3. Create coherence



4. Scatter photon

Everything is four-wave mixing

Many more:

CARS (coherent anti-Stokes Raman spectroscopy)

CSRS (coherent Stokes Raman spectroscopy)

Stimulated Raman

Inverse Raman

...

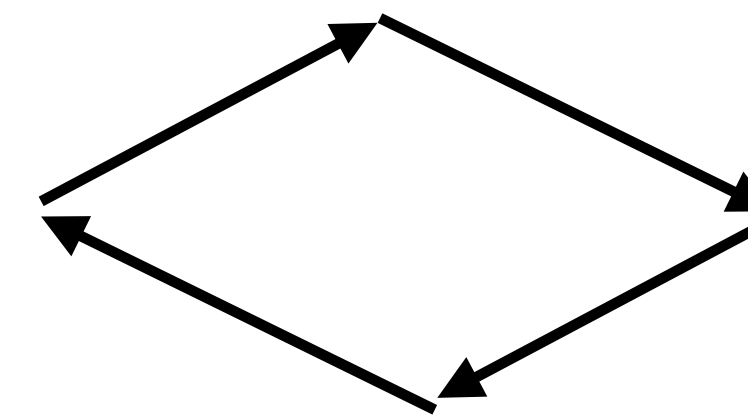
Coherent spectroscopies need phase matching!

k-vectors need to add up

> condition for angles

> angular separation of signal possible

> angular focussing of signal



Everything is four-wave mixing

Polarisation expansion

from Claudio:

$$P = \varepsilon_0 \cdot \left[\left(\sum_i \chi^{(1)} \cdot \mathbf{E}_i \right) + \left(\sum_{ij} \chi^{(2)} \cdot \mathbf{E}_i \cdot \mathbf{E}_j \right) + \left(\sum_{ij,k} \chi^{(3)} \cdot \mathbf{E}_i \cdot \mathbf{E}_j \cdot \mathbf{E}_k \right) + \dots \right]$$

one-wave mixing does not exist... (only a pure coherence cannot be observed)

two-wave mixing is a $\chi^{(1)}$ process

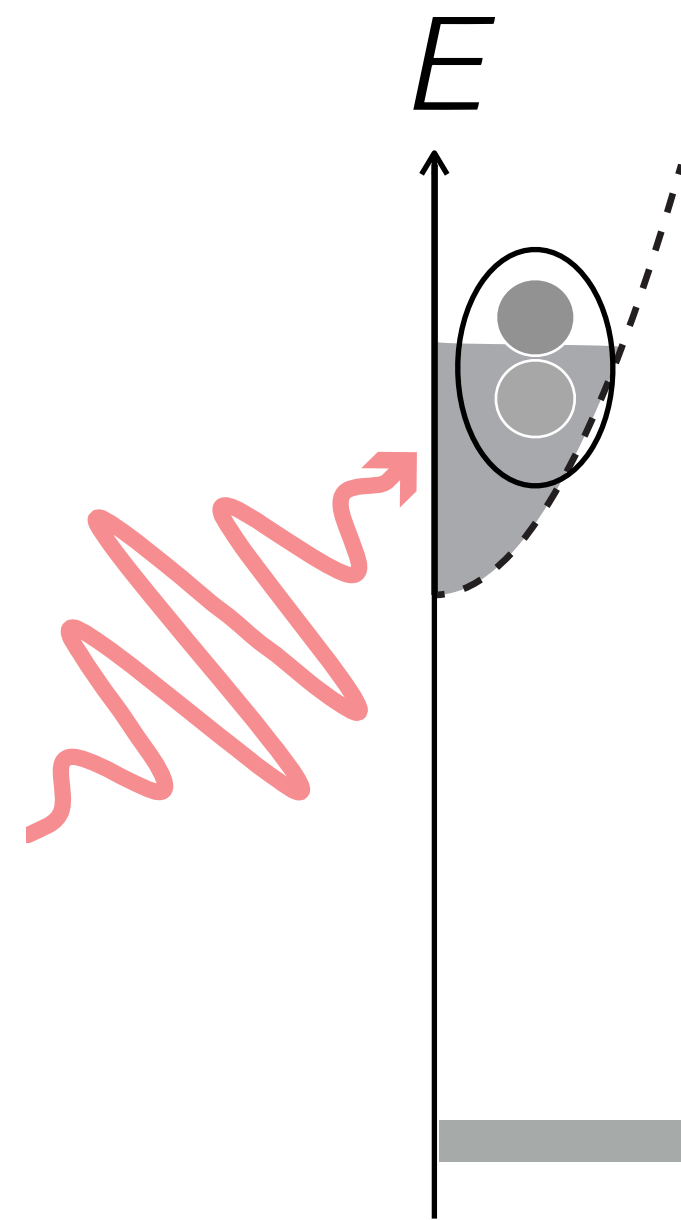
three-wave mixing is a $\chi^{(2)}$ process

four-wave mixing is a $\chi^{(3)}$ process

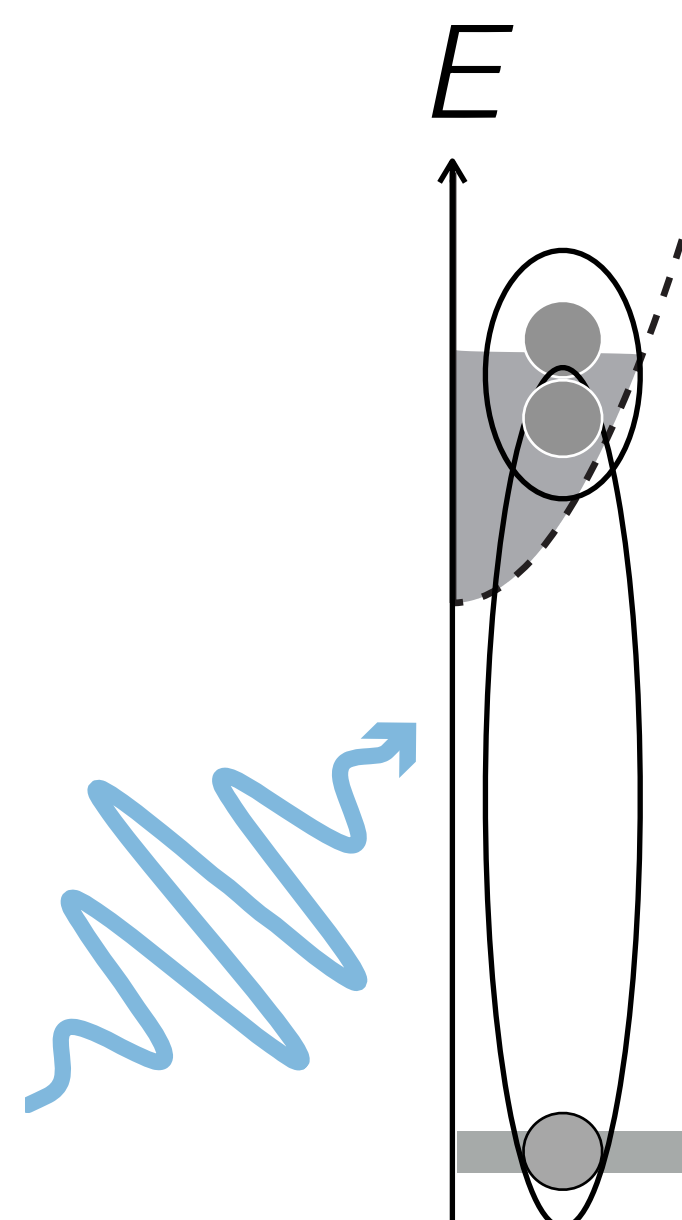
...

Three-wave mixing

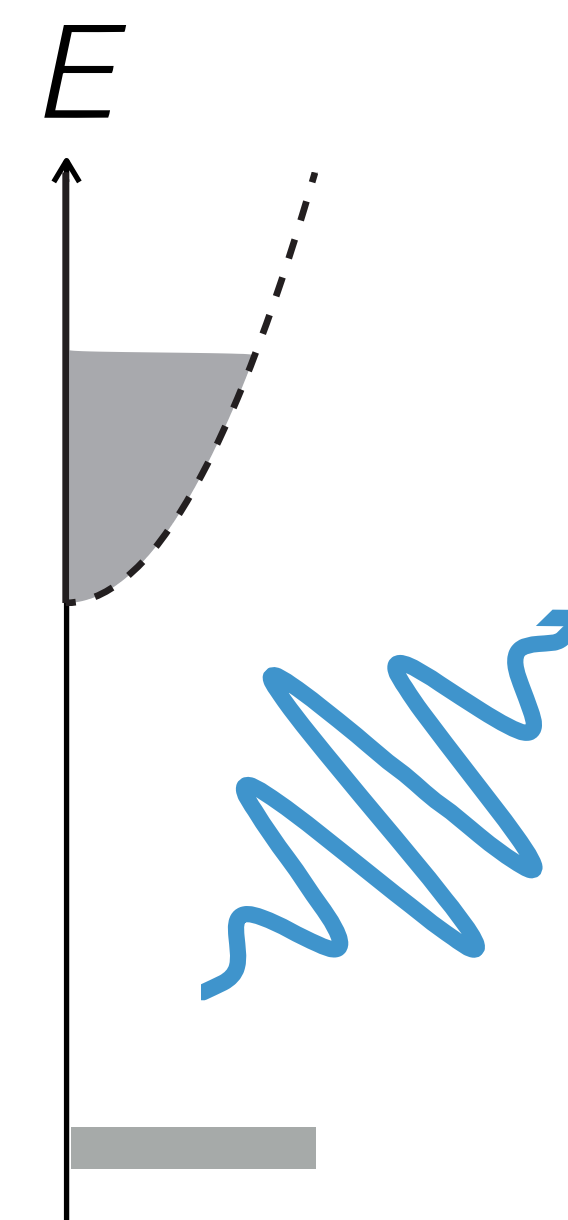
SFG (SHG, DFG)



1. Create coherence



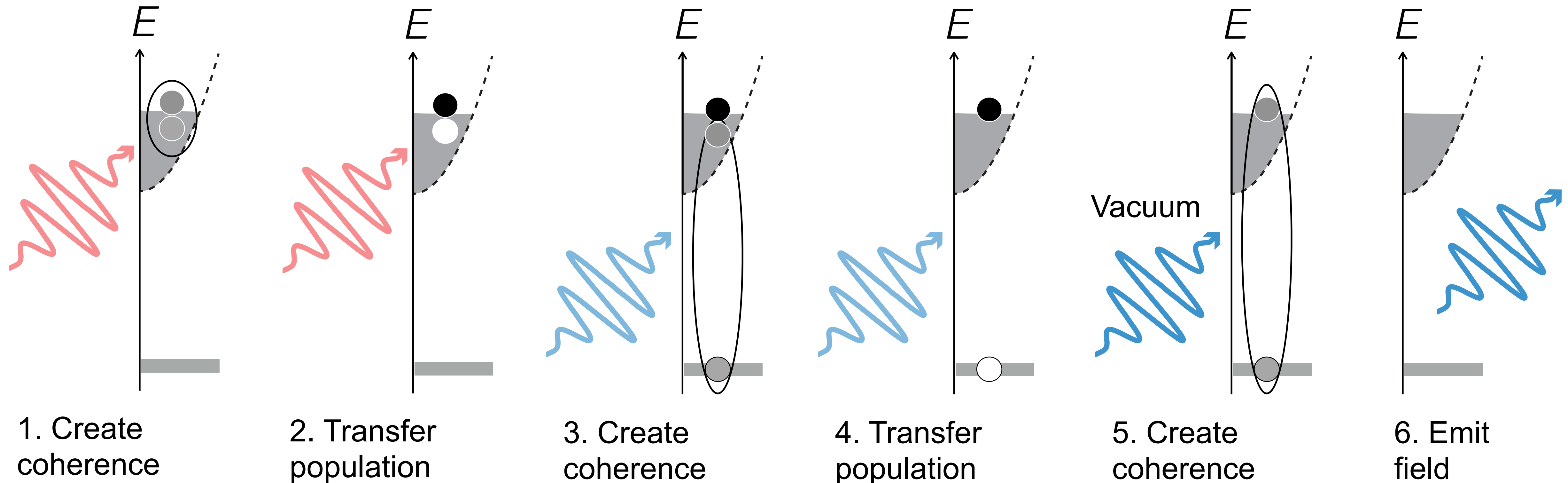
2. Transfer coherence



3. Emit field

Six-wave mixing

Pump-probe (anti-Stokes) RIXS



Experimental designs

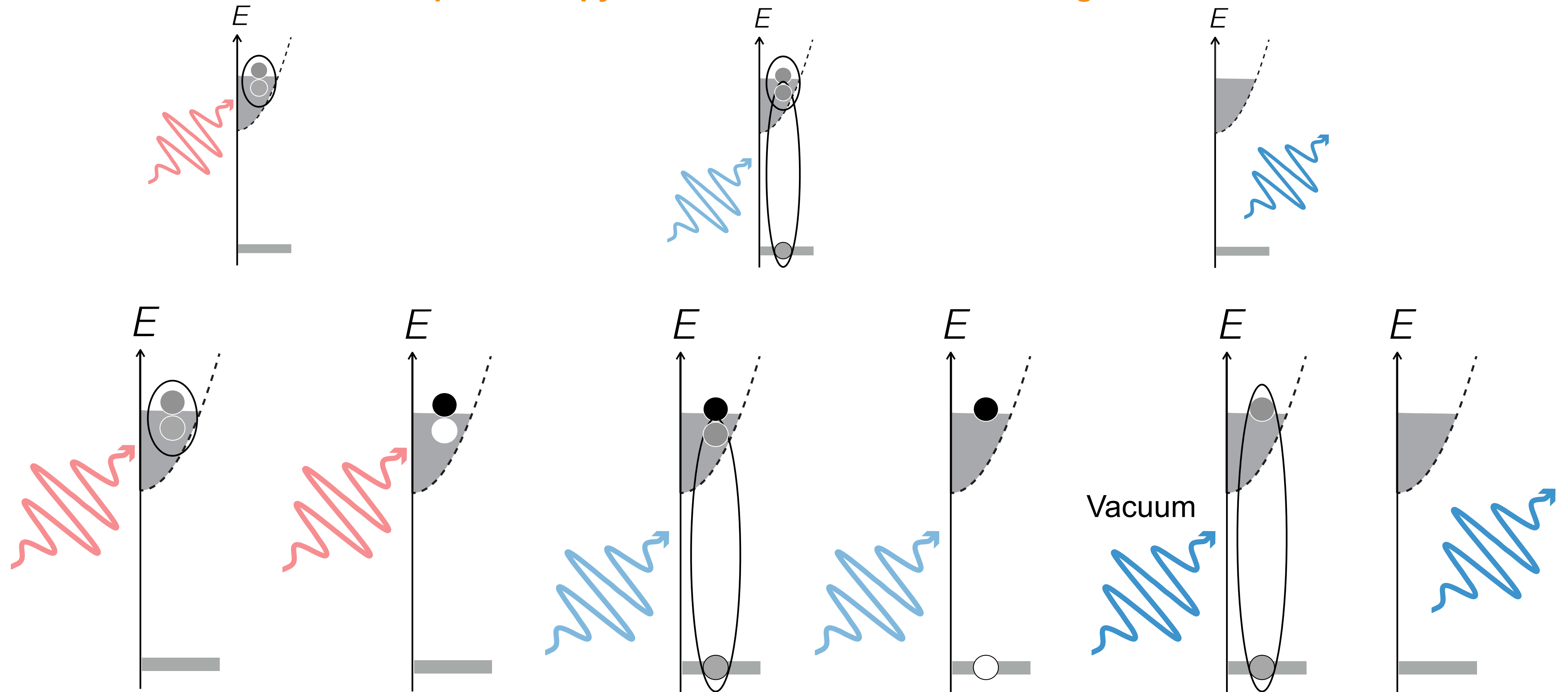
to realise wave-mixing spectroscopies

Things to consider:

- phase matching condition (angles, geometry)
- concurrent processes and their relative strengths

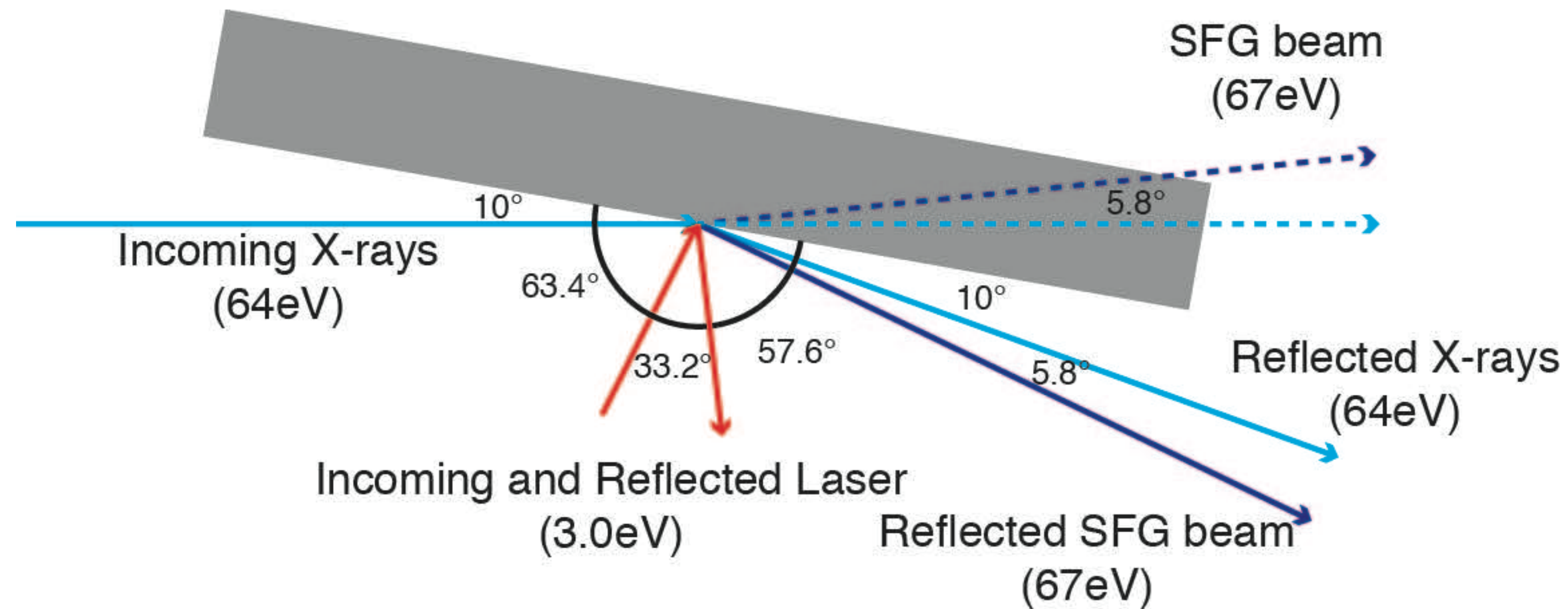
SFG vs. anti-Stokes RIXS

Coherent vs. incoherent spectroscopy / three-wave vs. six-wave mixing



Possible SFG geometry at an M-edge

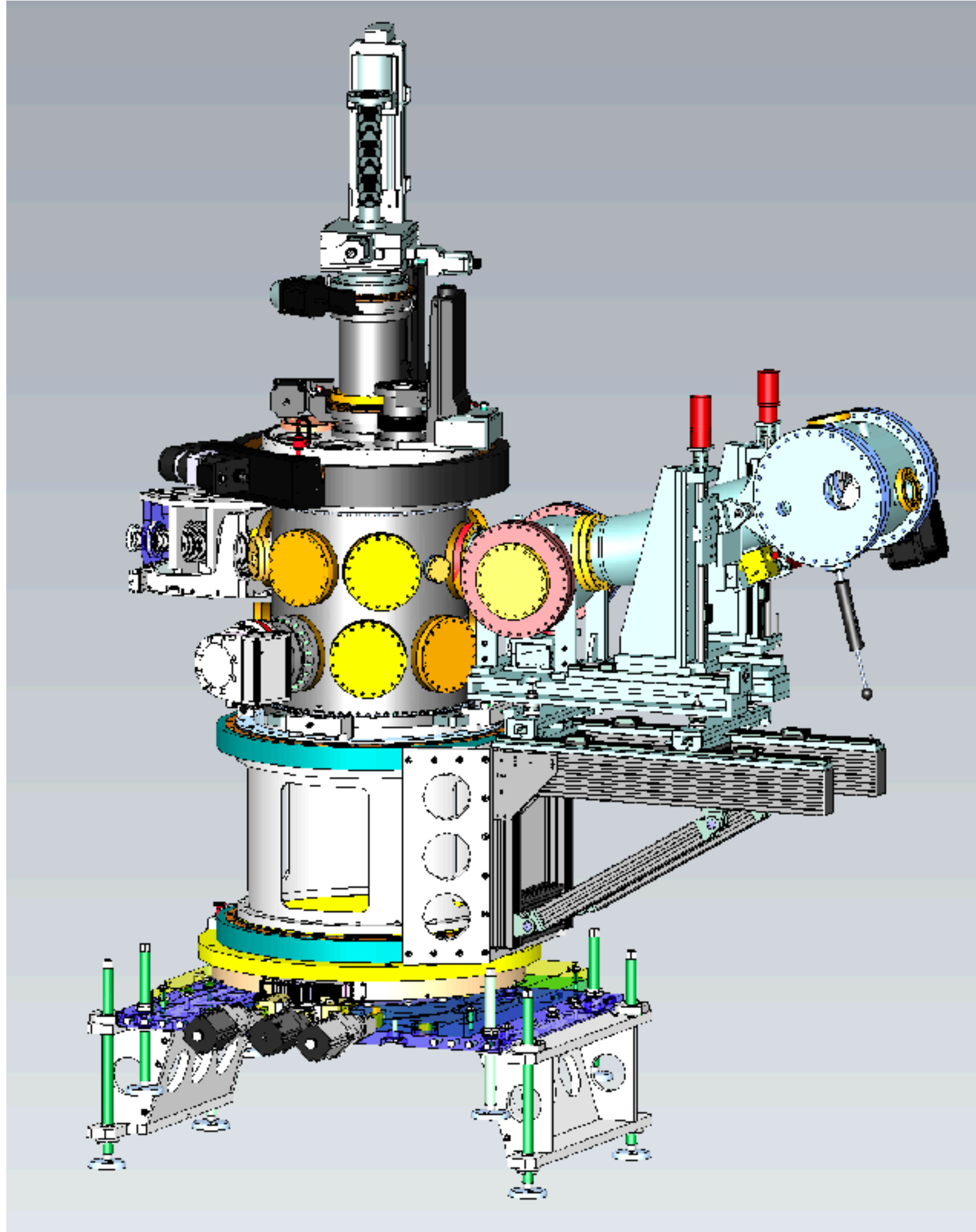
Anti-Stokes RIXS has no phase matching condition



Experiments

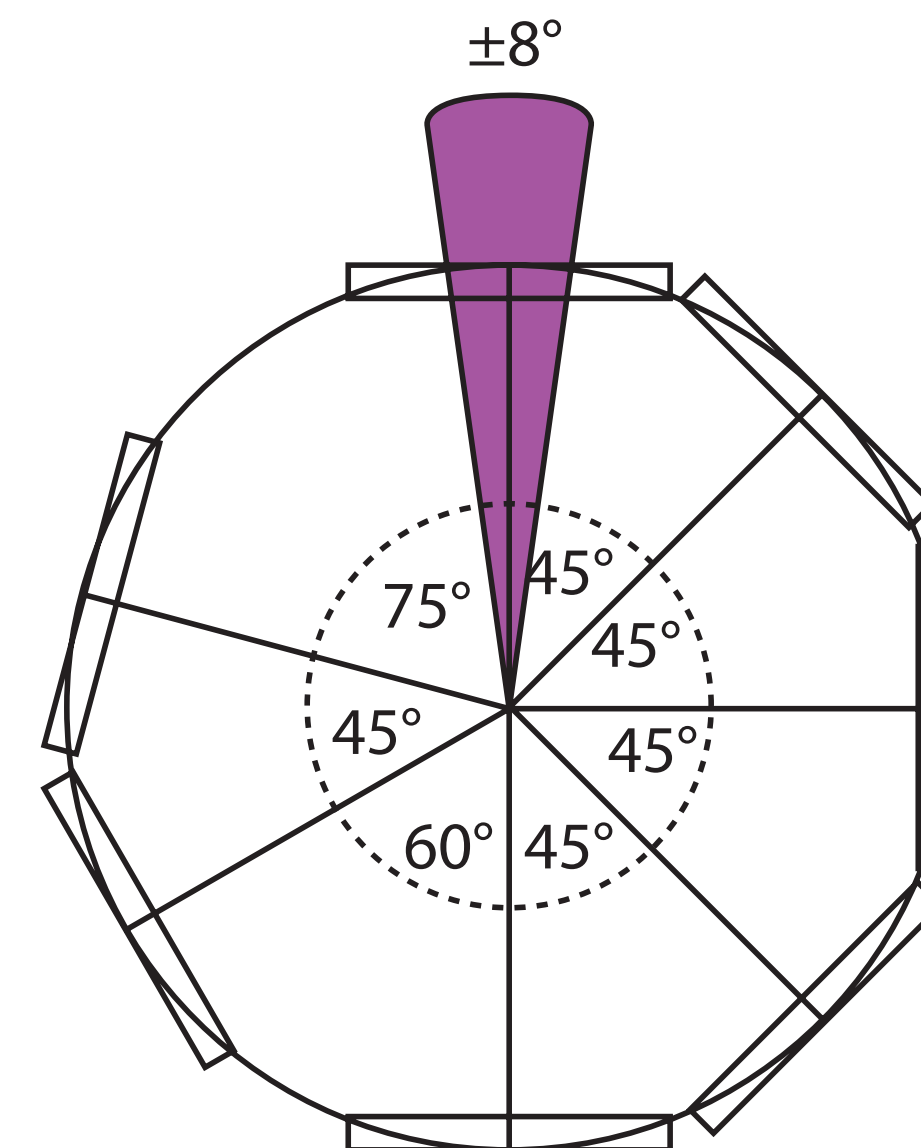
MUSIX

Multi-dimensional spectroscopy and (in-)elastic X-ray scattering instrument



- Designed at DESY
- UHV diffractometer modified from Uni Köln design, in use at BESSY
- spectrometer design in house
- in (full) operation within the next two weeks

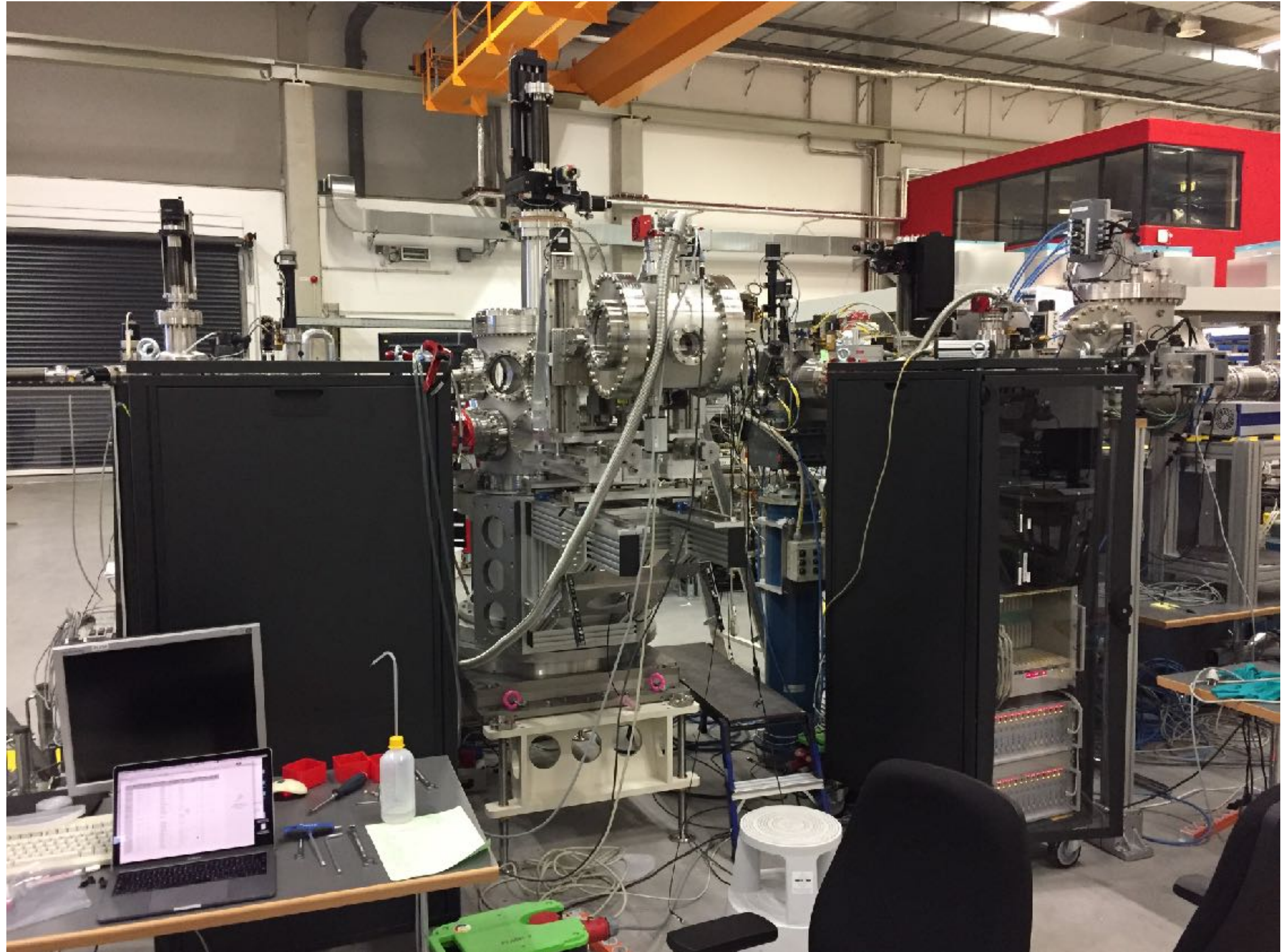
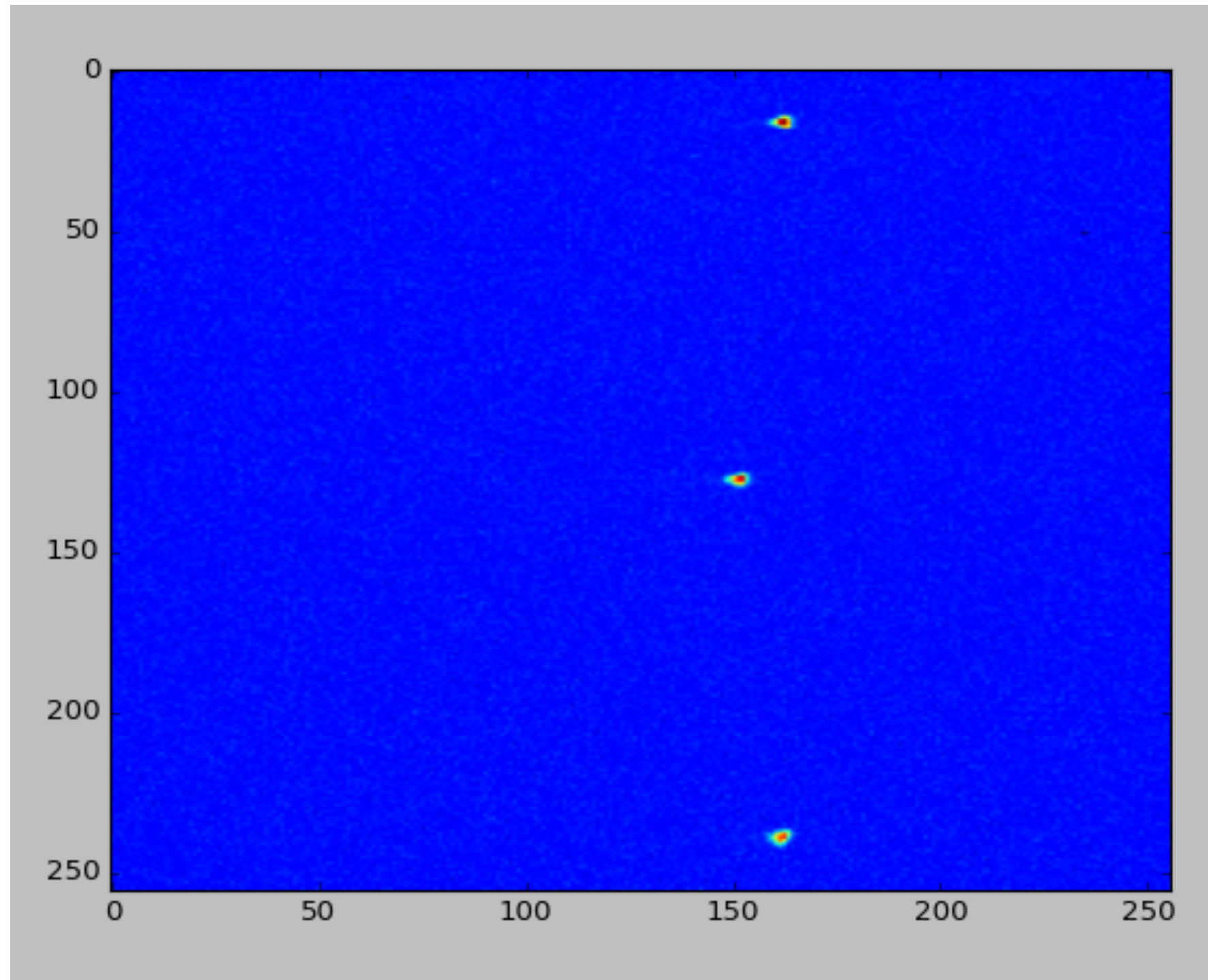
- flexible for various beam lines / light sources
- fulfill phase matching condition
- spectral analysis
- materials' science environment
- open for collaborations @ FLASH / PETRA (P04) or elsewhere



MUSIX in reality

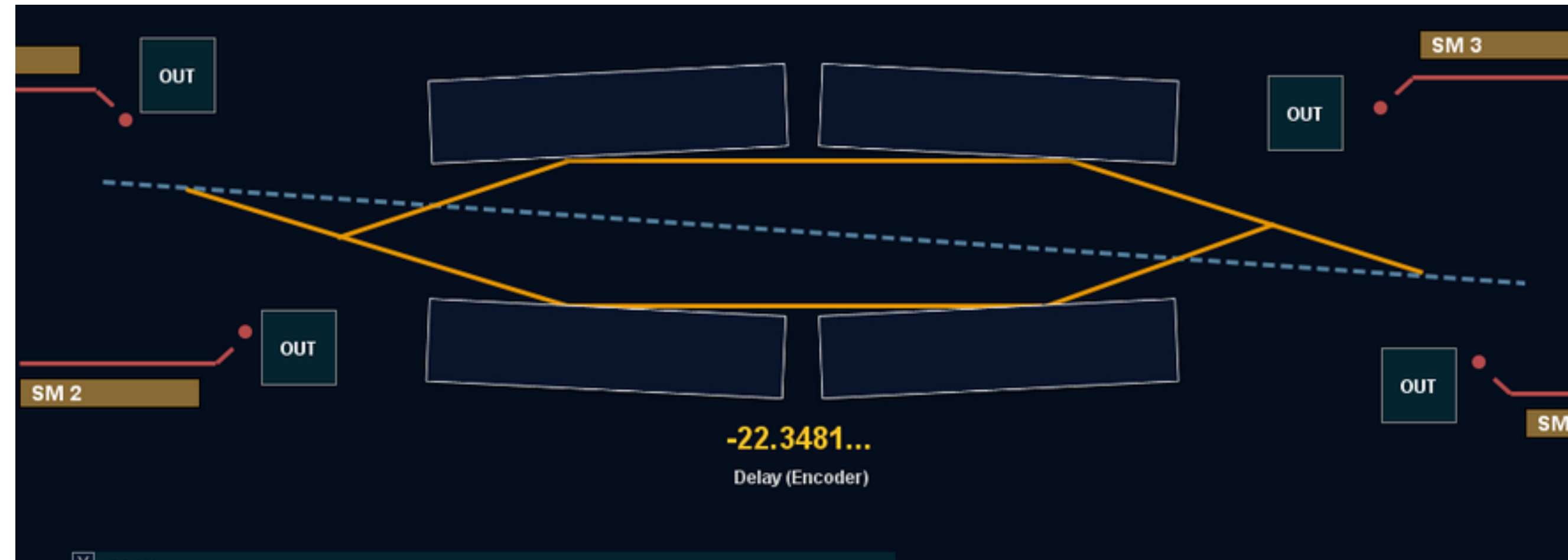
Completed in next two weeks, ideas for future collaborations welcome

- Nitrogen K-edge (400eV) XES
- Triple RZP analyser
- Resonant excitation with third harmonic @ FLASH2

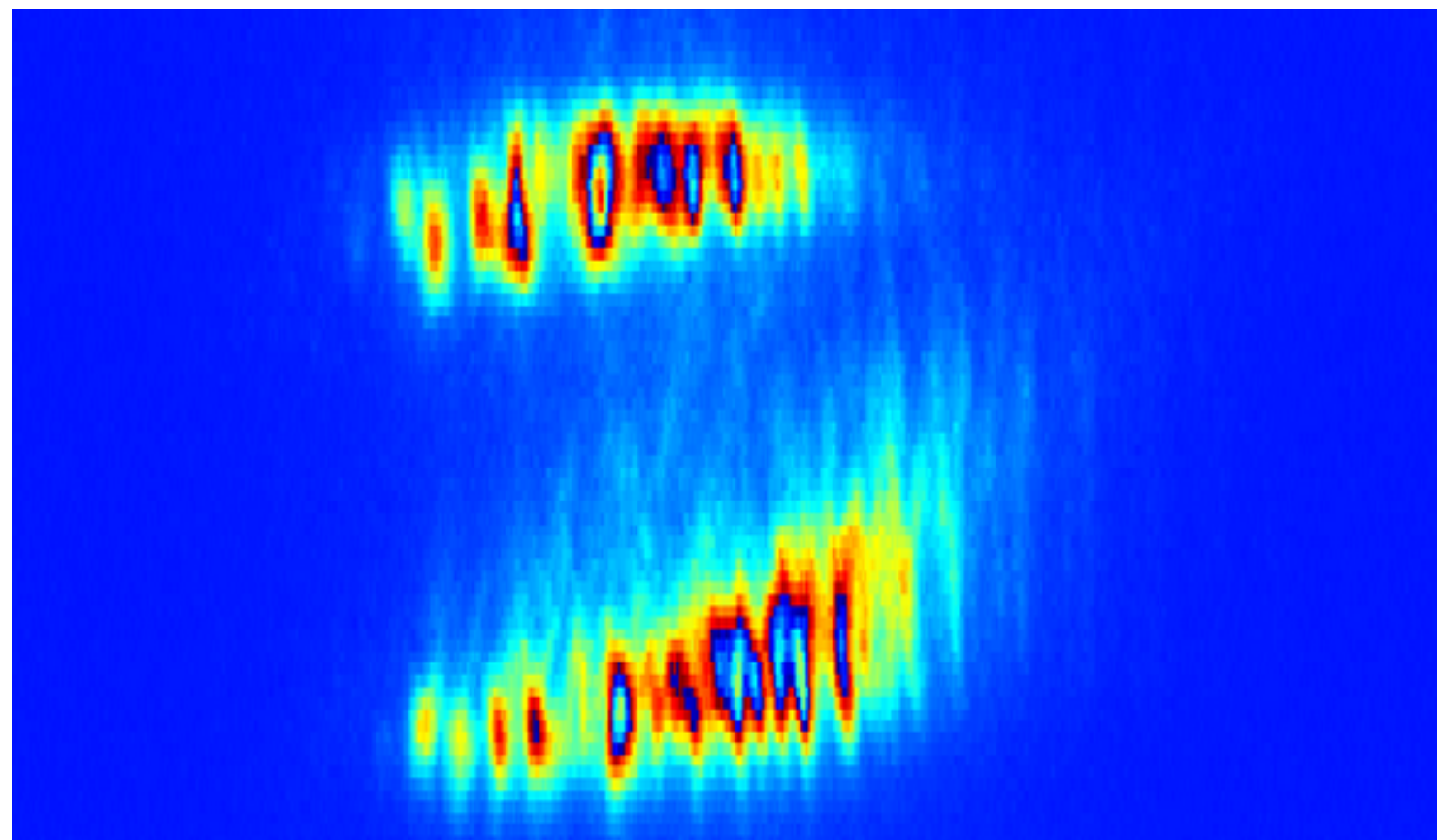


Heterodyne detection: Coherent reference beams

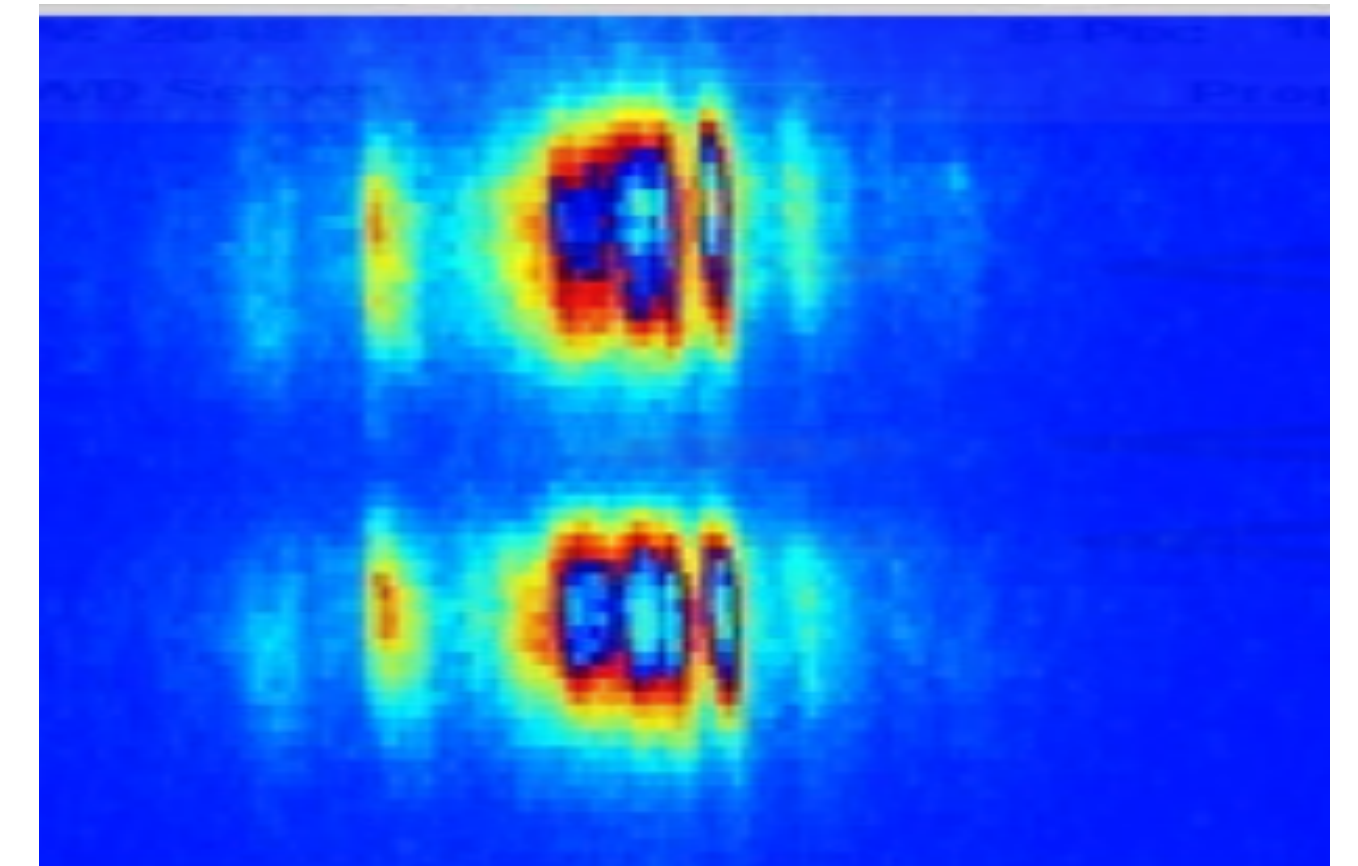
Optimised split and delay units



Standard scheme:
Split with edge of mirror



New scheme:
Split with transmission grating

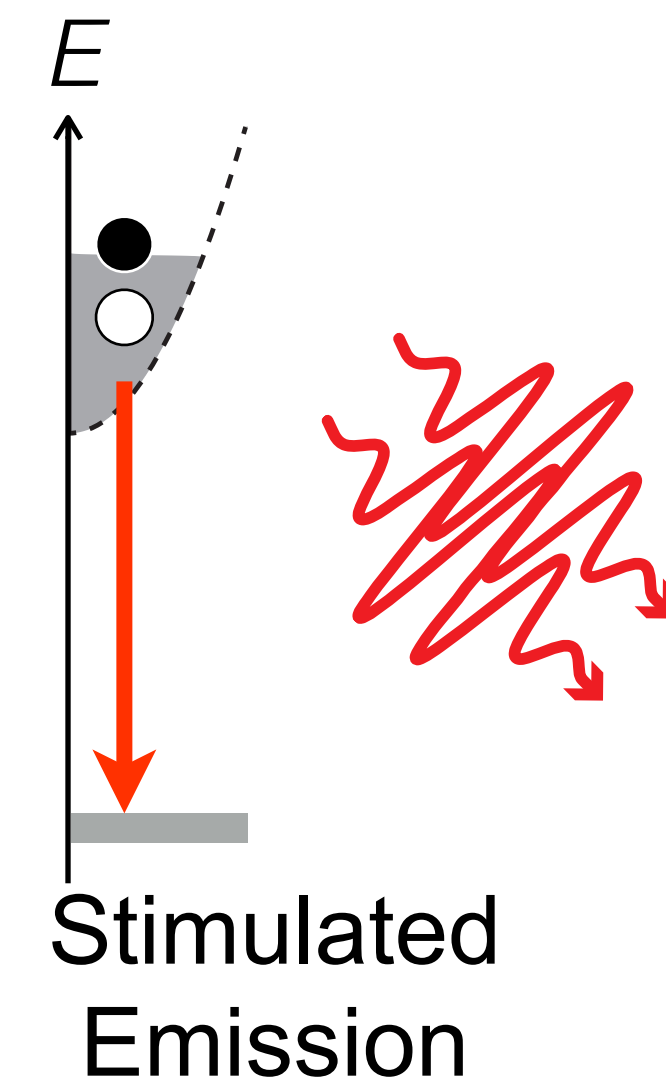
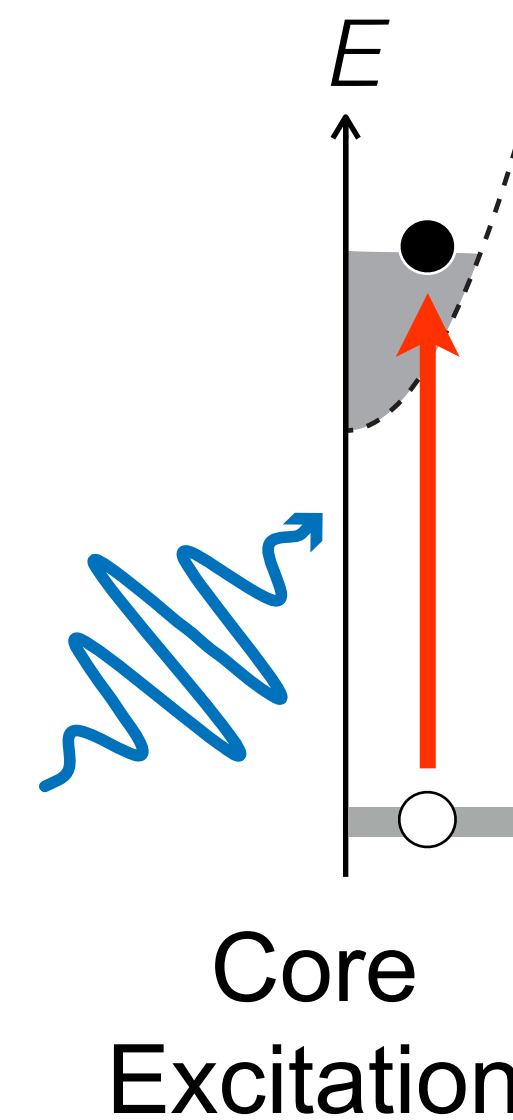
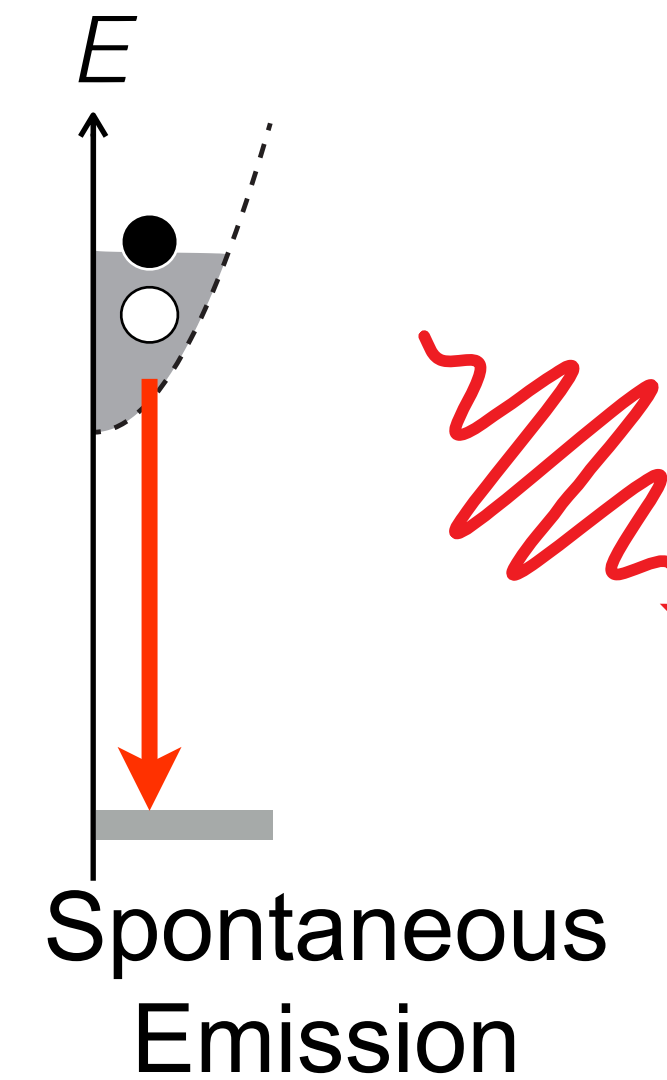
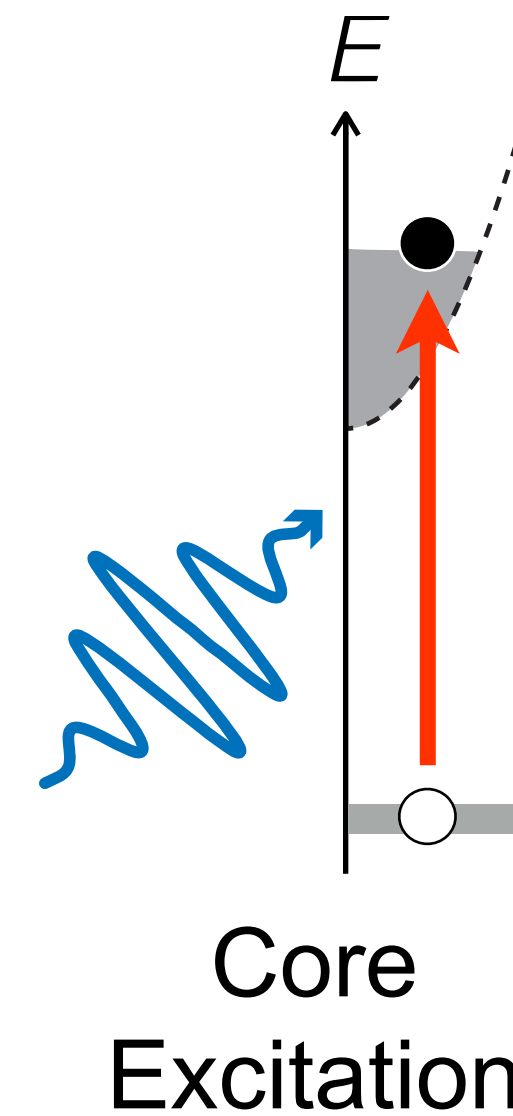


Collaboration with G. Brenner (FLASH) et al. + C. David (PSI) et al.

Amplified spontaneous emission @ FLASH

Silicon at high intensities

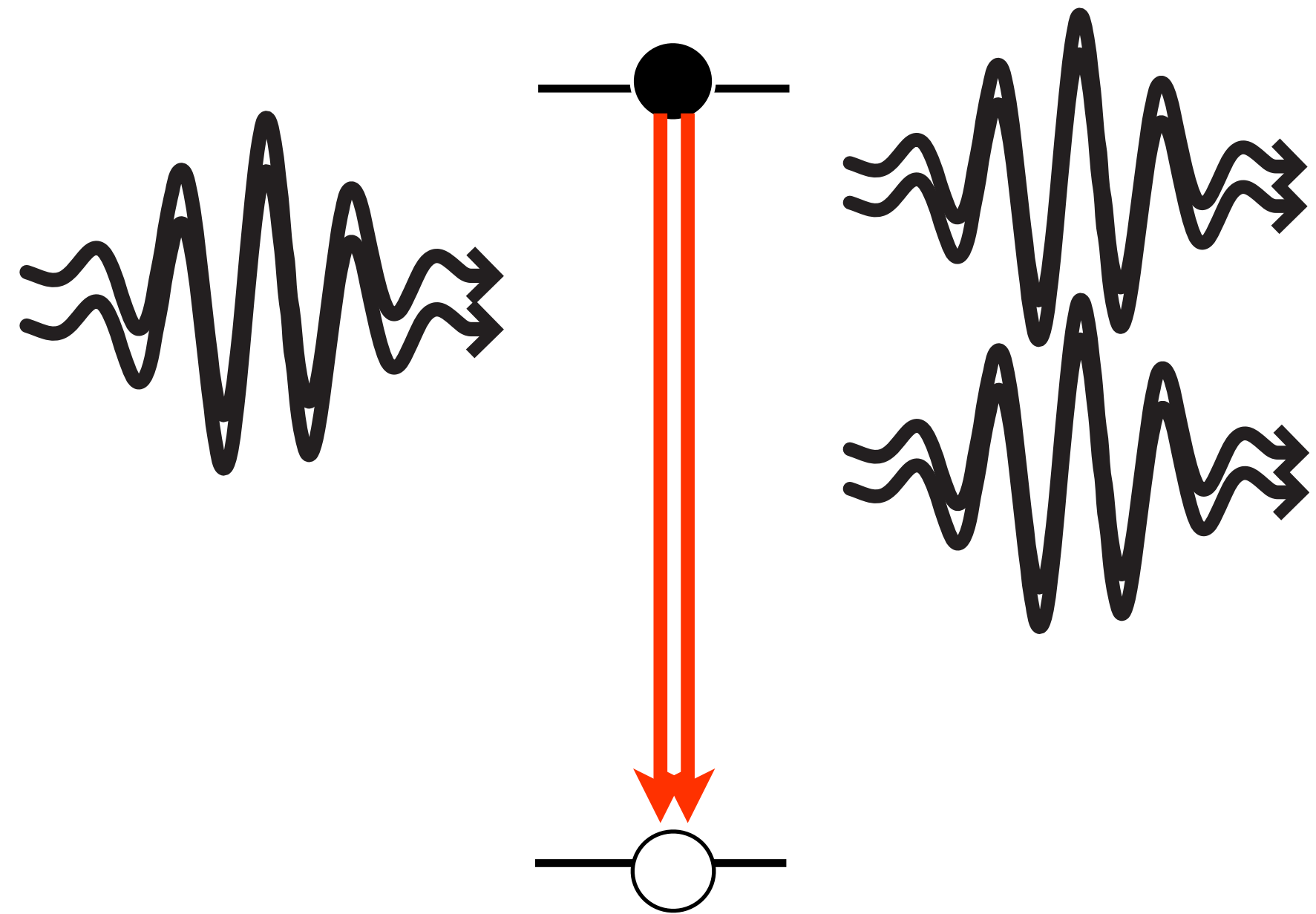
Martin Beye
Simon Schreck
Florian Sorgenfrei
Christoph Trabant
Niko Pontius
Christian Schüssler-
Langeheine
Wilfried Wurth
Alexander Föhlisch



Beye et al., Nature 501, 191 (2013)

Geometry optimisation

Maximise interaction length with core-excited volume



Stimulated Emission

$$P_{stim} = \sigma_{stim} \rho_{ch} d \stackrel{!}{=} 1$$

$$\sigma_{stim} \approx \sigma_{abs}$$

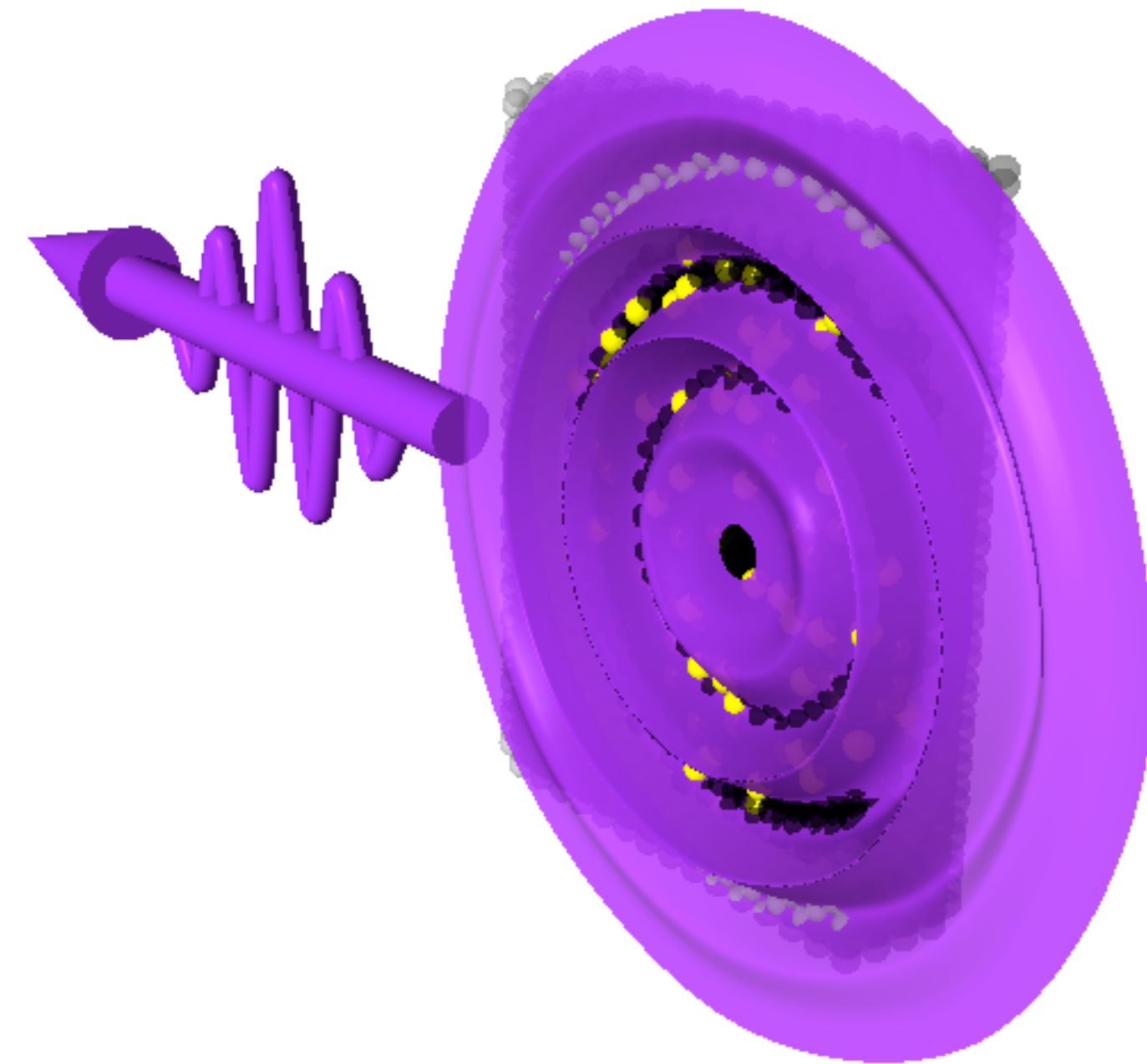
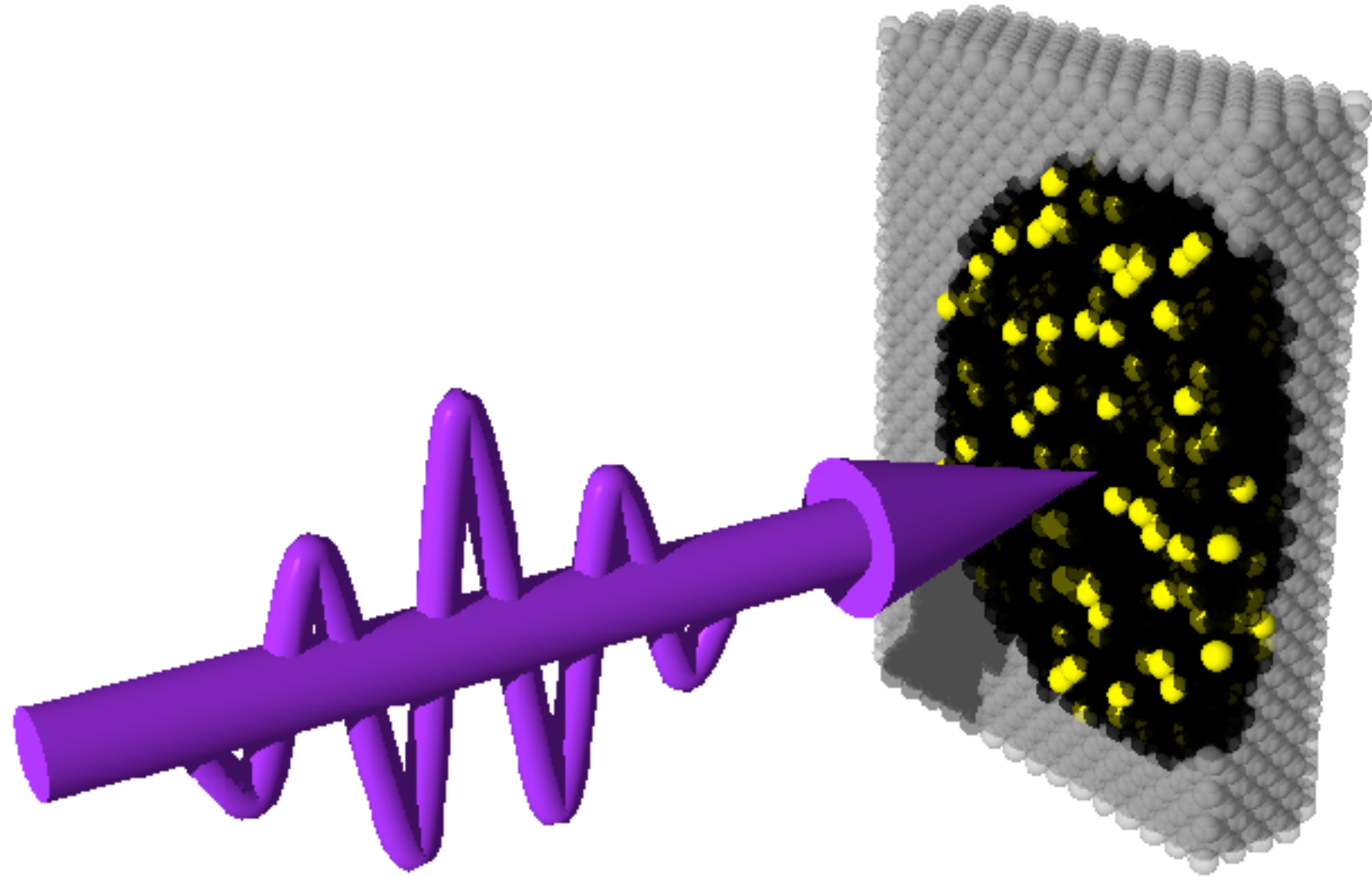
$$\sigma_{abs} = \frac{1}{\lambda_{abs} \rho_{atom}}$$

$$\frac{\rho_{ch} d}{\lambda_{abs} \rho_{atom}} = 1$$

$$\frac{\rho_{ch}}{\rho_{atom}} = \frac{\lambda_{abs}}{d}$$

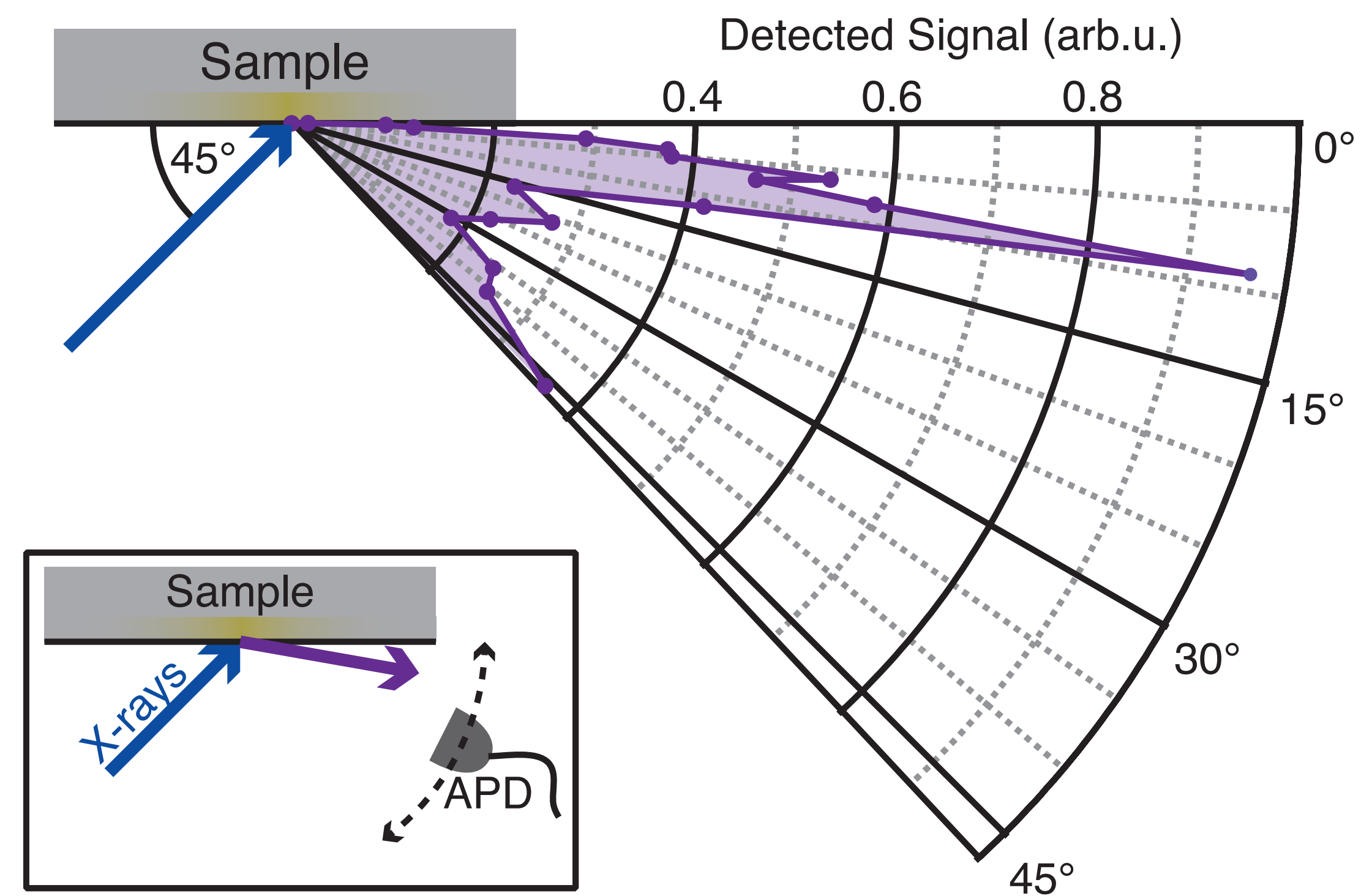
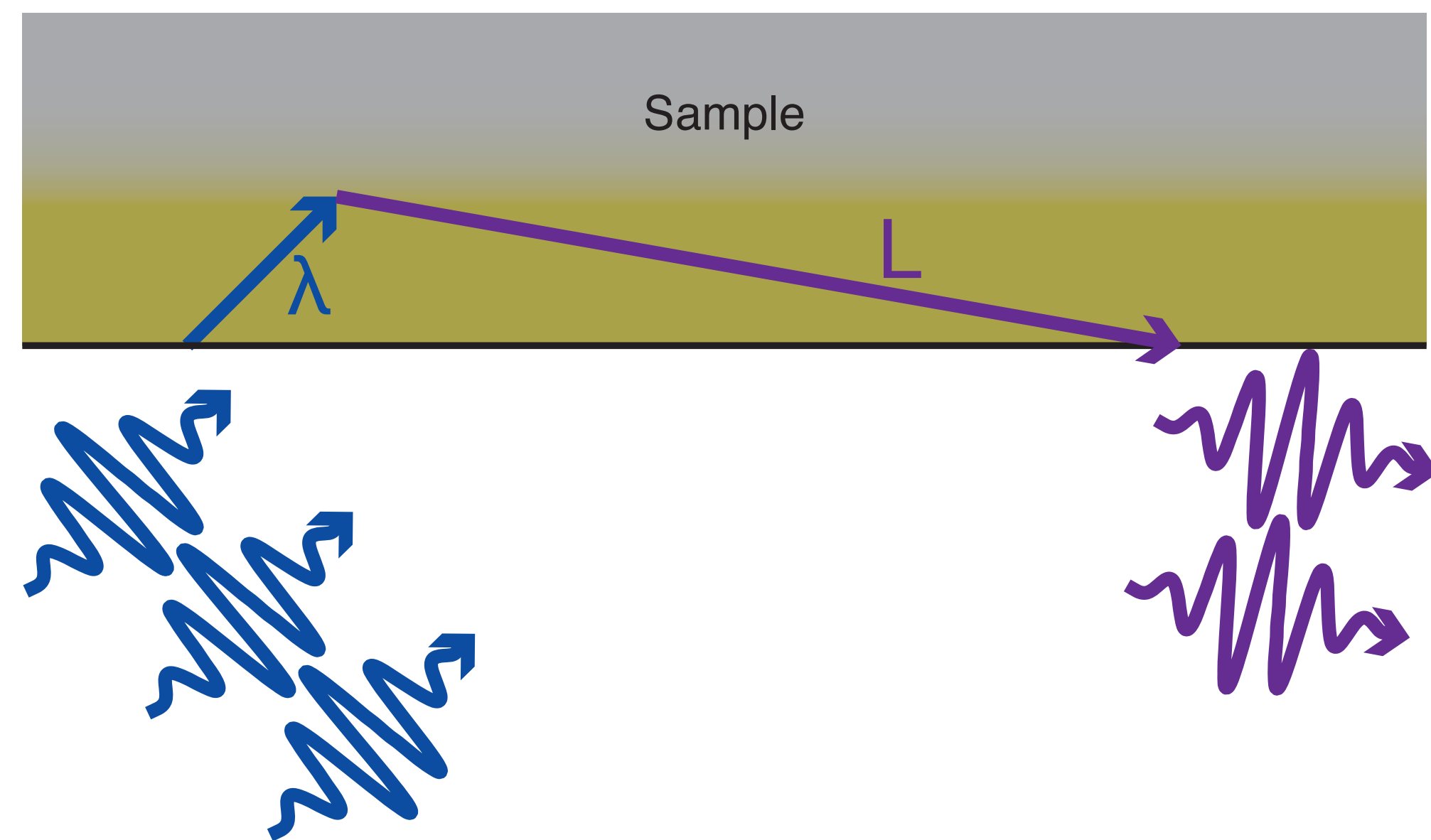
Stimulation front

Primarily along the surface for soft X-rays on solids

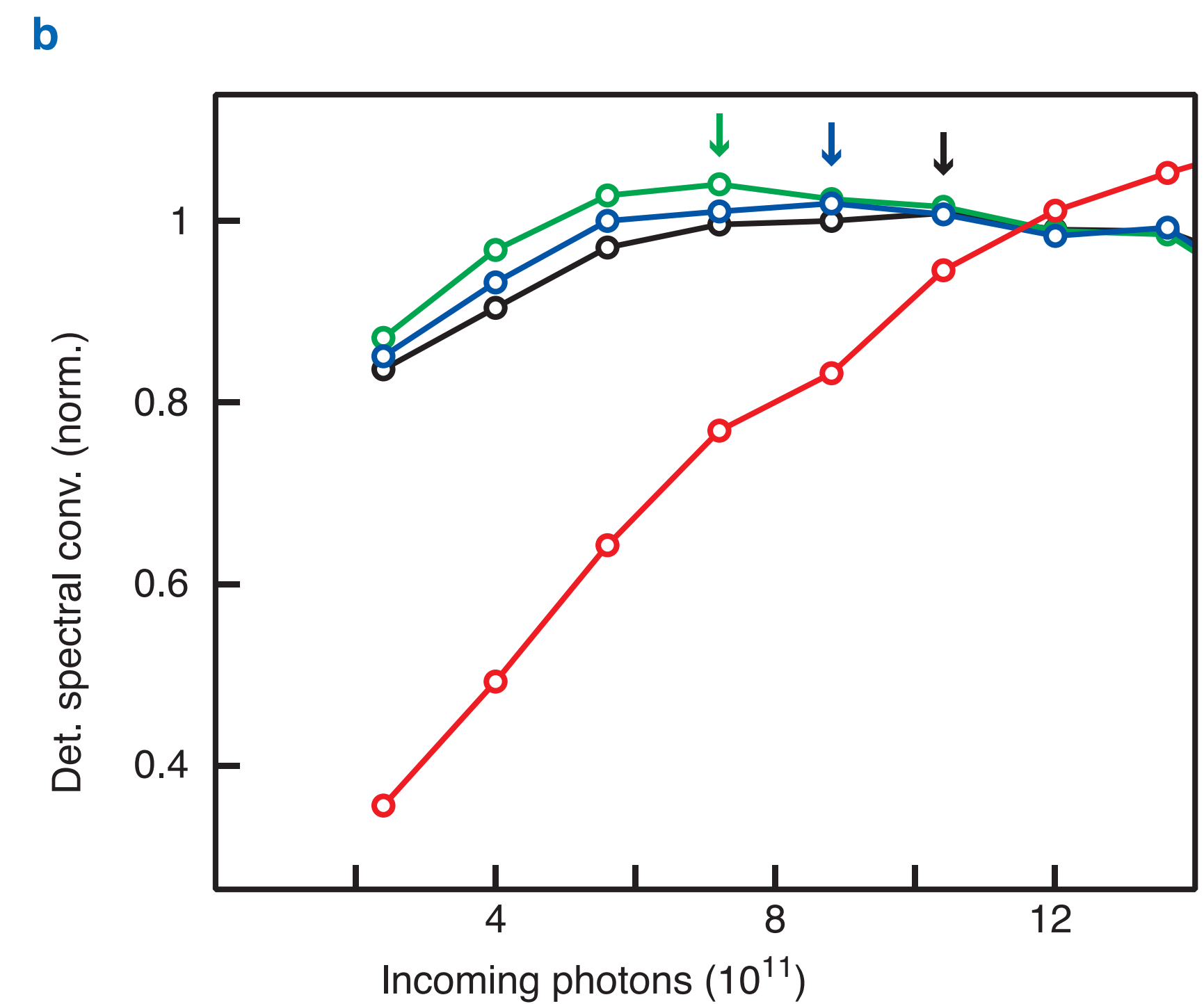
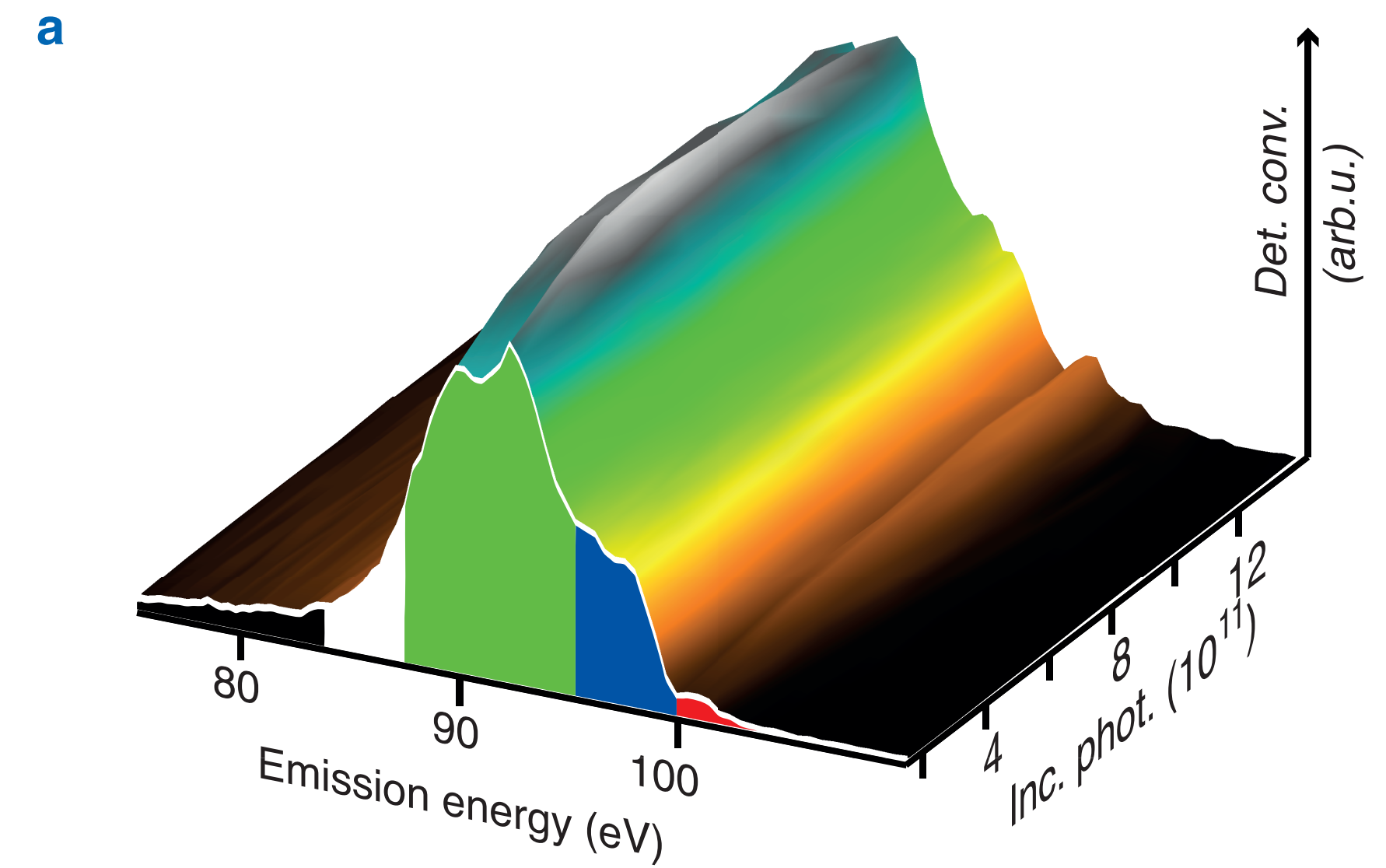
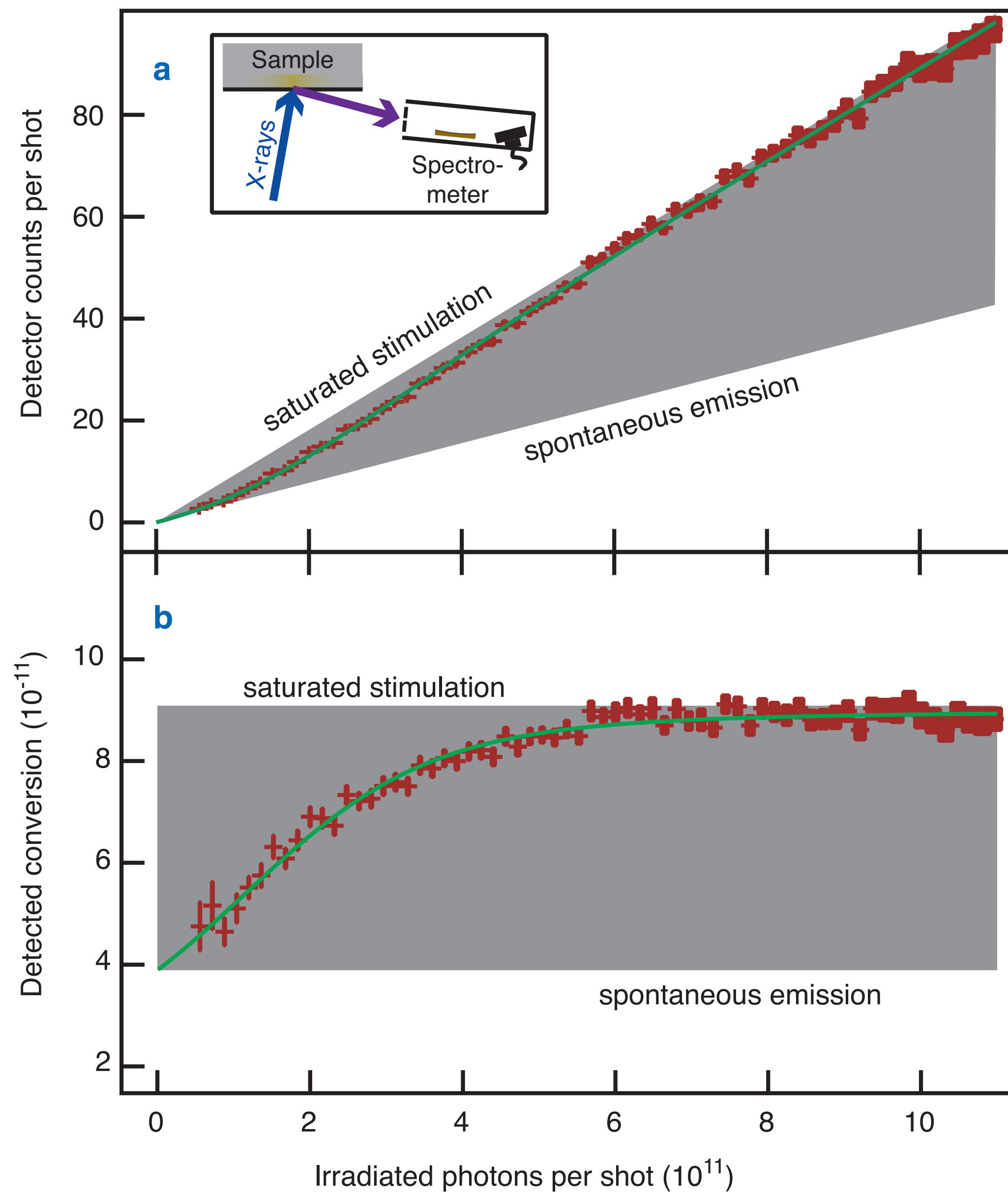


Angular dependence

Si (100), 115eV, 1J/cm², 30 fs

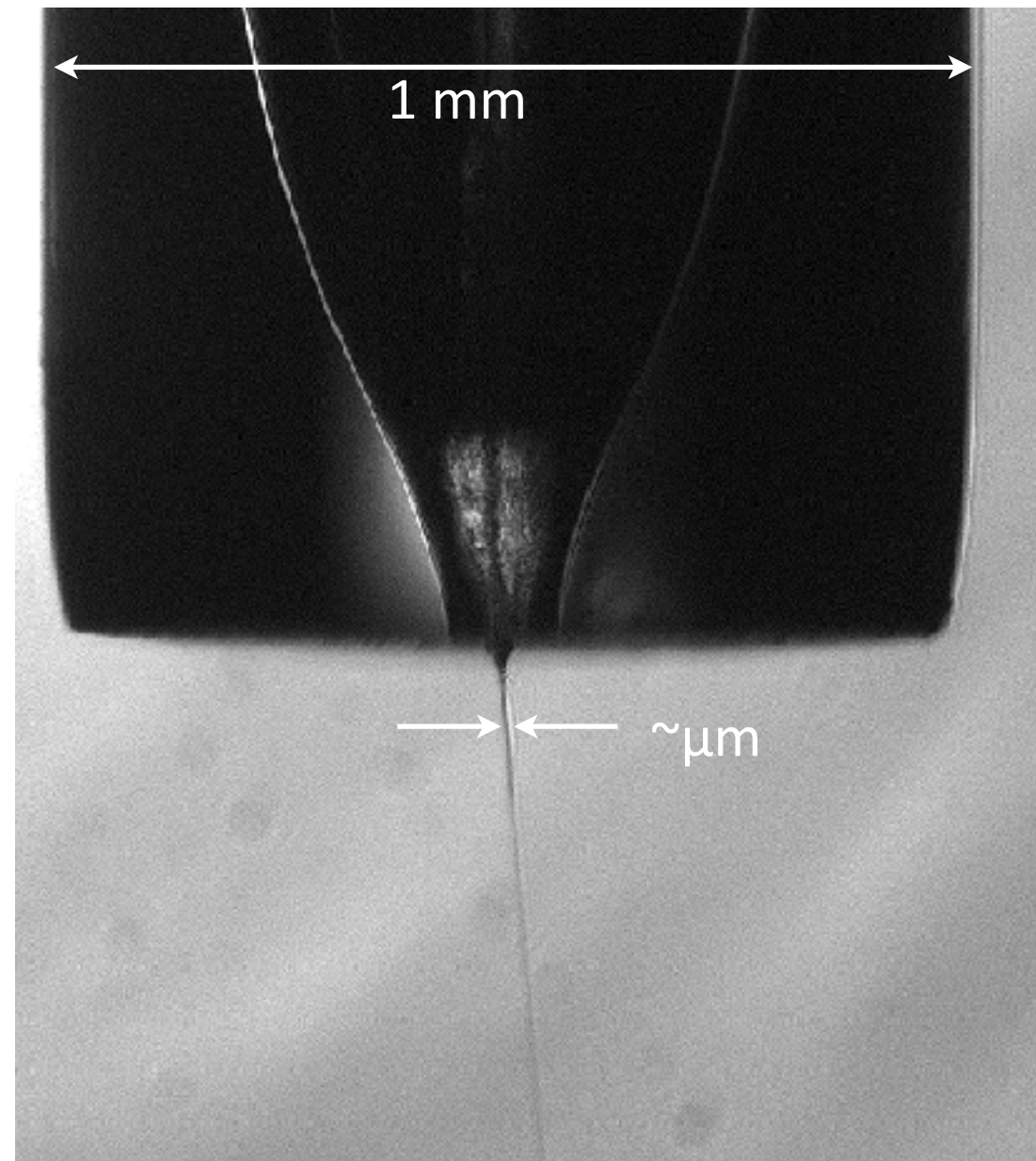


Fluence and spectral dependence



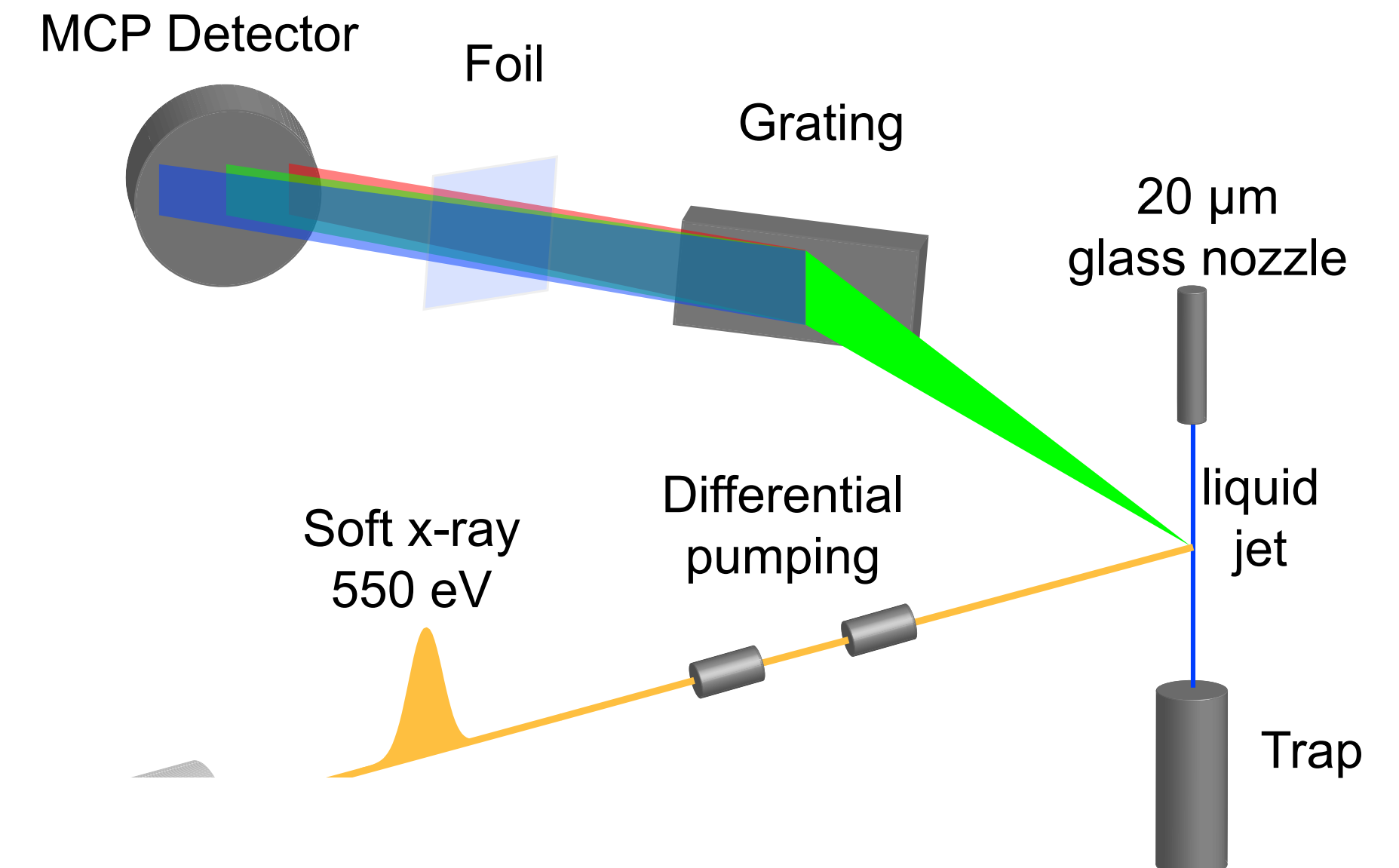
Amplified spontaneous emission from water?

Reabsorption of emission for long pulses and short core hole lifetimes



Liquid jet speed ~ 20 m/s
 \sim kHz to MHz rep. rate

The LJE/FlexRIXS endstation



Kunnus, K. *et al. Rev. Sci. Instrum.* **83**, 123109 (2012)

PRL **113**, 153002 (2014)

PHYSICAL REVIEW LETTERS

10 OCTOBER 2014

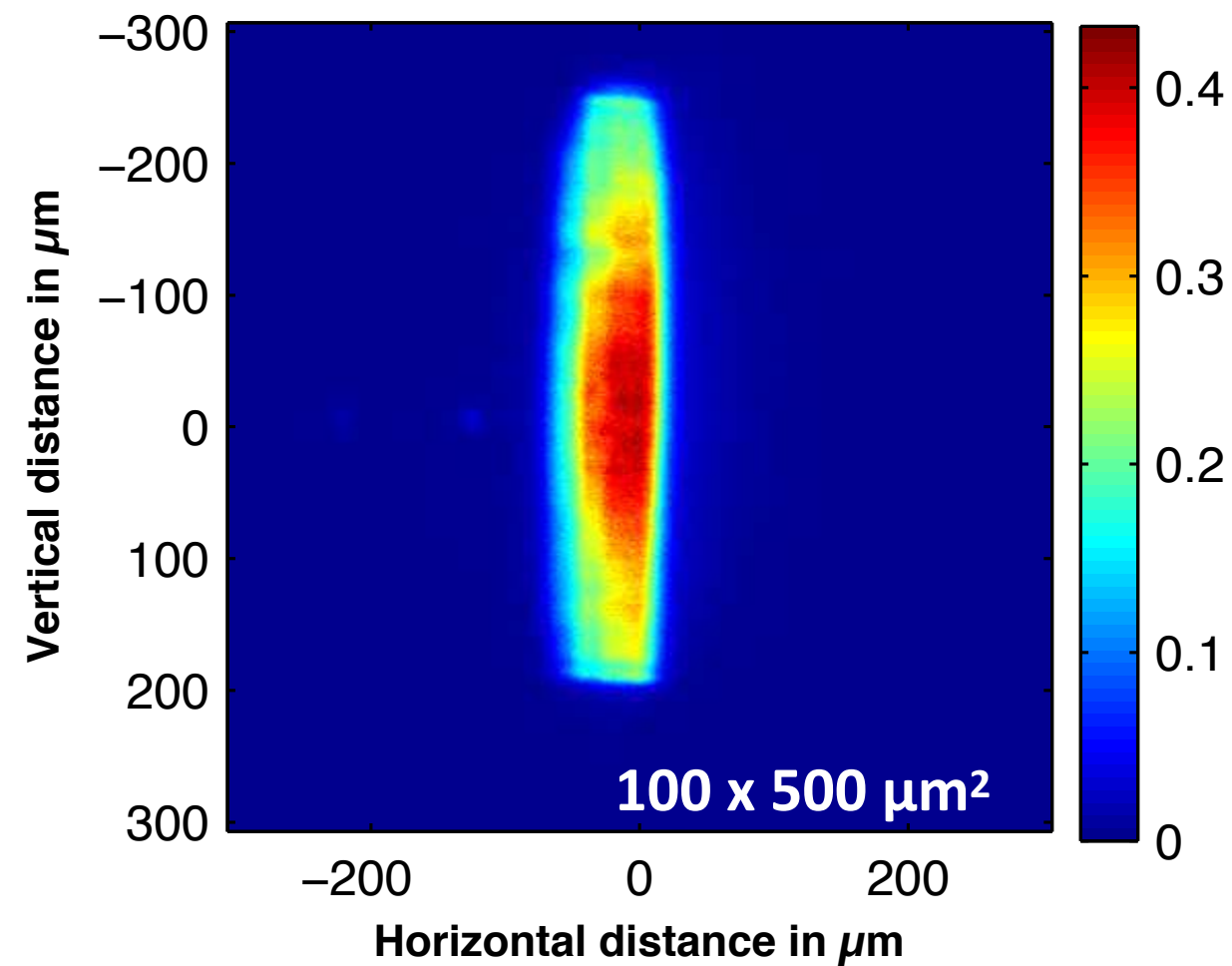
Reabsorption of Soft X-Ray Emission at High X-Ray Free-Electron Laser Fluences

Simon Schreck,^{1,2,*} Martin Beye,^{1,†} Jonas A. Sellberg,^{3,4} Trevor McQueen,^{4,5} Hartawan Laksmono,⁶ Brian Kennedy,¹ Sebastian Eckert,¹ Daniel Schlesinger,³ Dennis Nordlund,⁷ Hirohito Ogasawara,⁷ Raymond G. Sierra,⁶ Vegard H. Segtnan,^{4,8} Katharina Kubicek,^{9,10} William F. Schlotter,¹¹ Georgi L. Dakovski,¹¹ Stefan P. Moeller,¹¹ Uwe Bergmann,¹¹ Simone Techert,^{9,10,12} Lars G. M. Pettersson,³ Philippe Wernet,¹ Michael J. Bogan,⁶ Yoshihisa Harada,^{13,14} Anders Nilsson,^{3,4,7} and Alexander Föhlisch^{1,2}

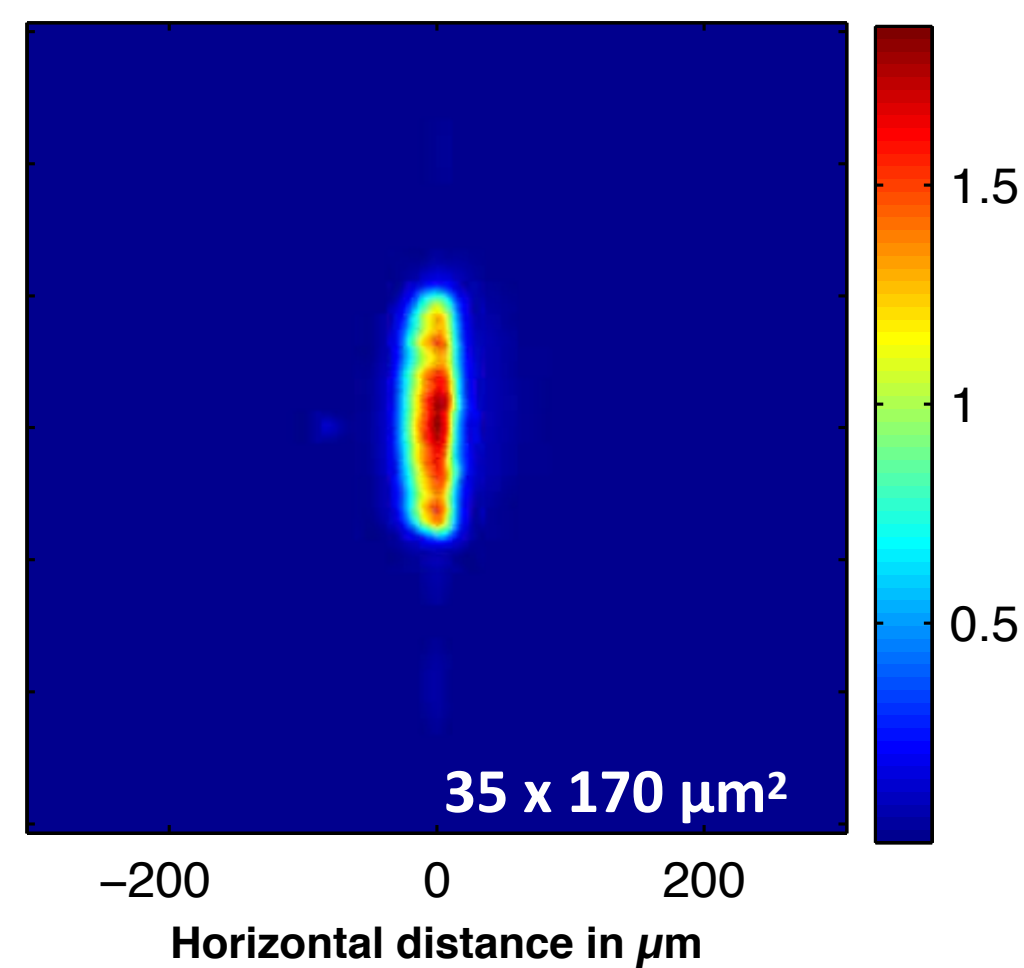
Continuous fluence variation by orders of magnitude

LCLS SXR has bendable KB-mirrors

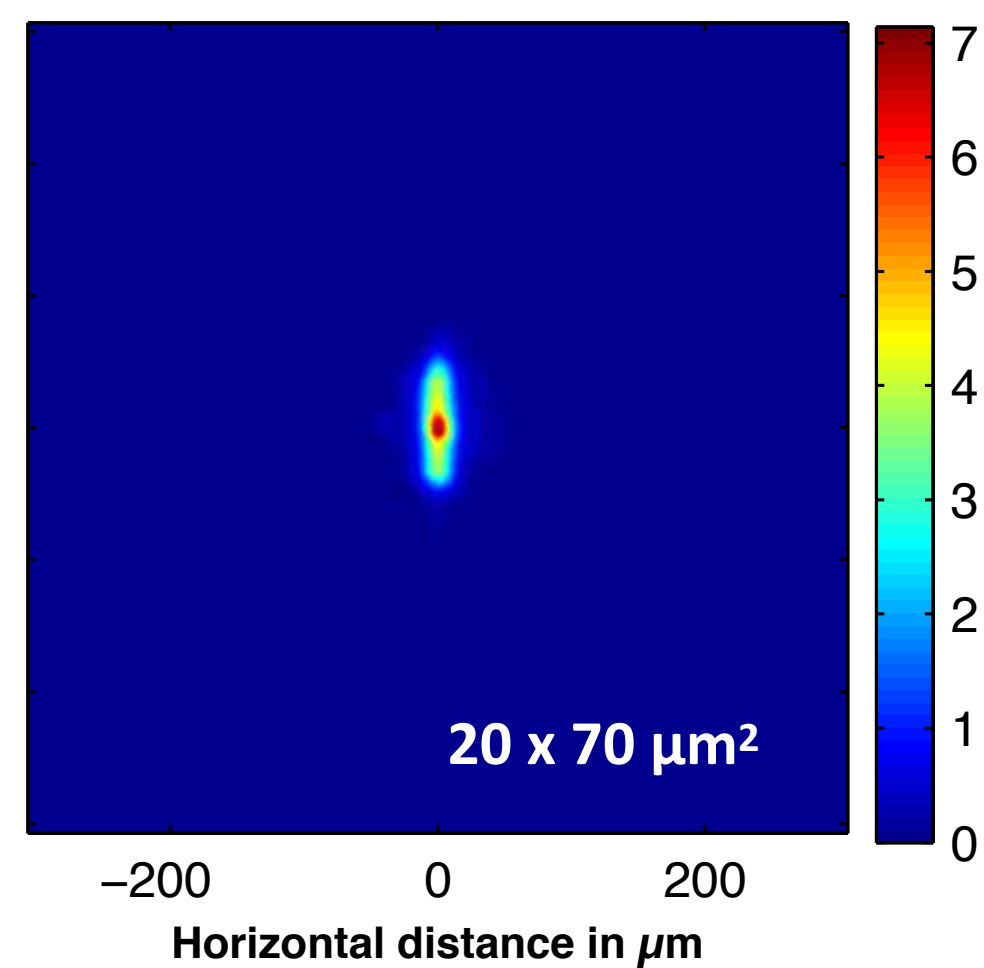
XL



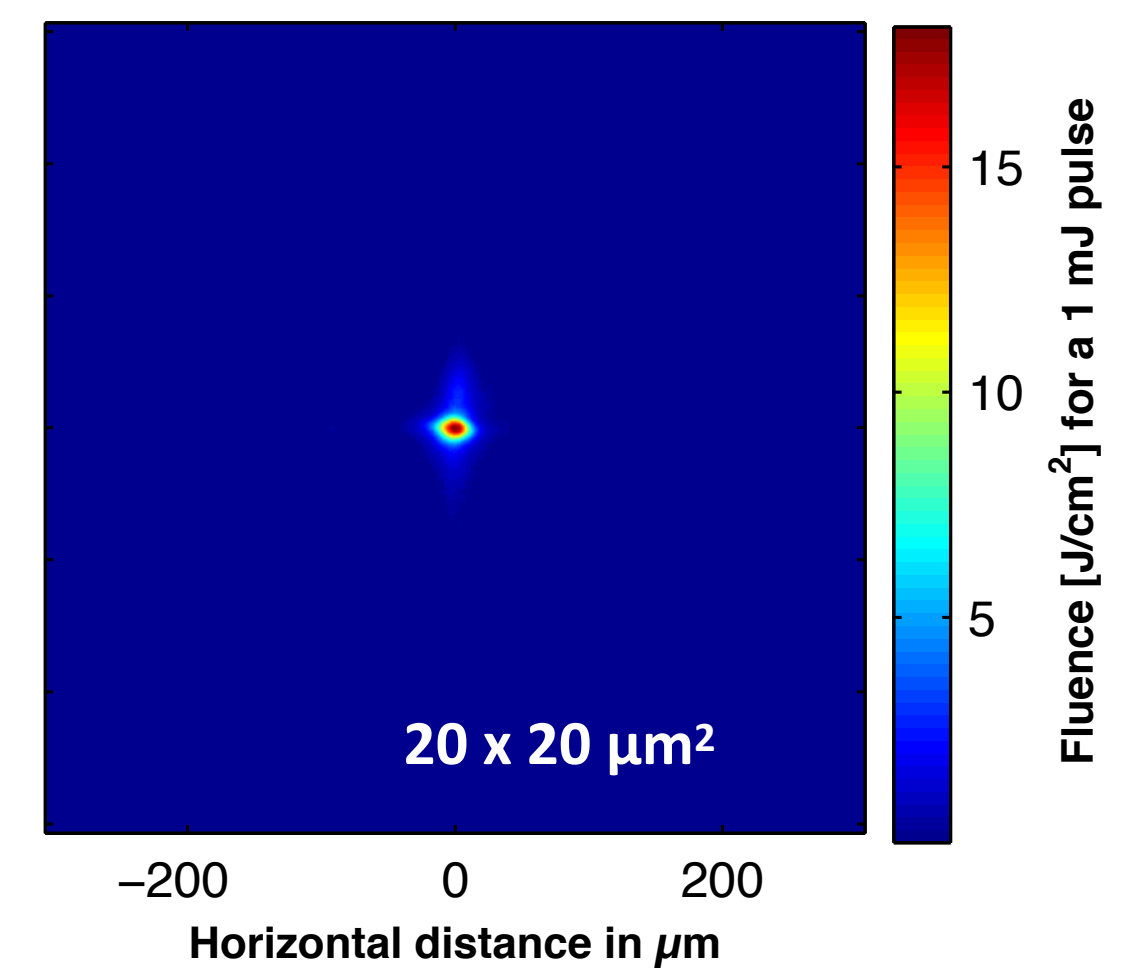
L



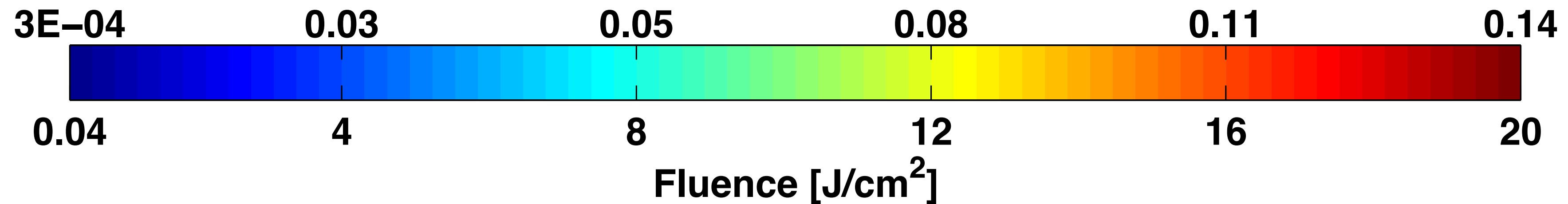
M



S

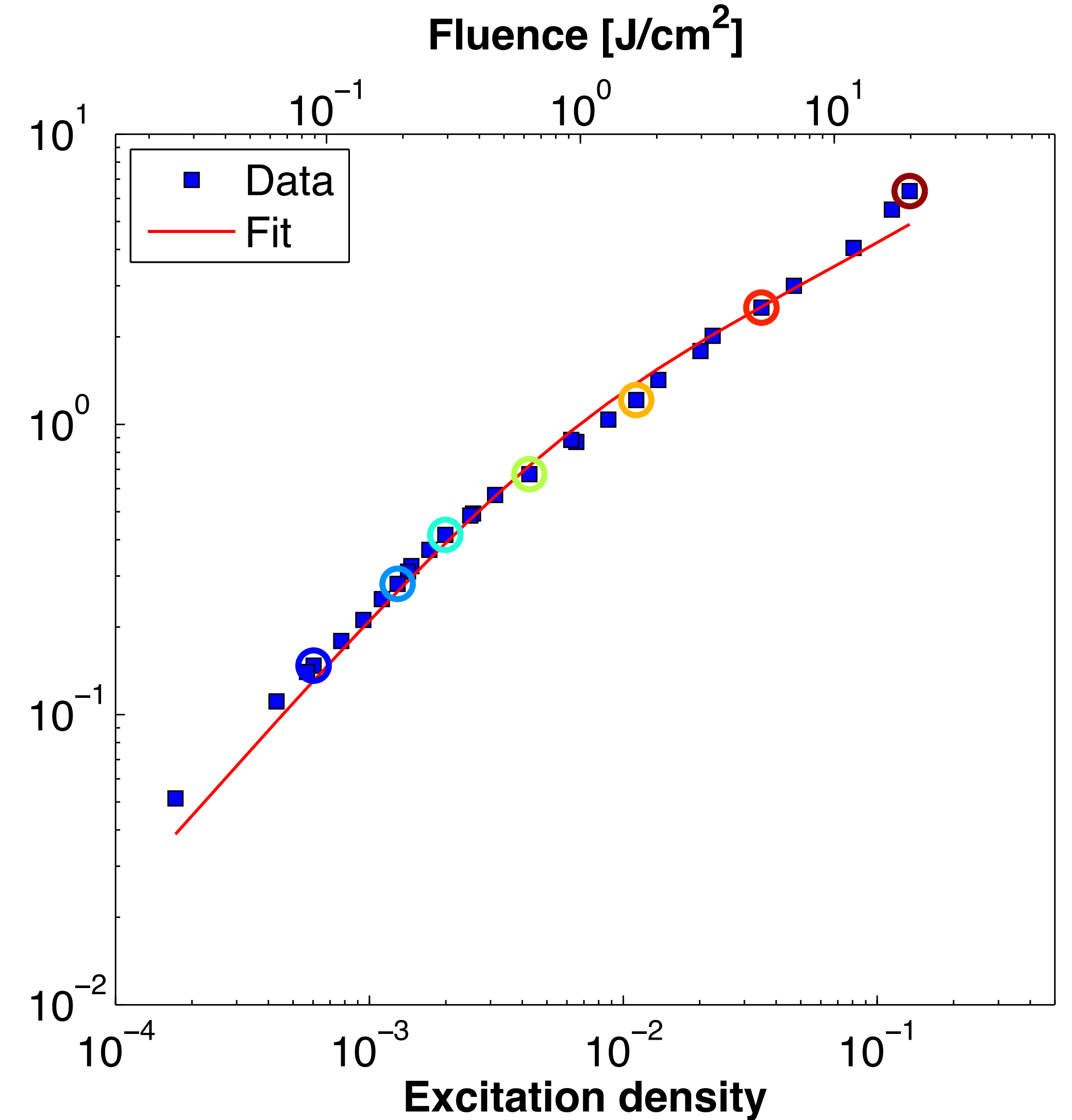
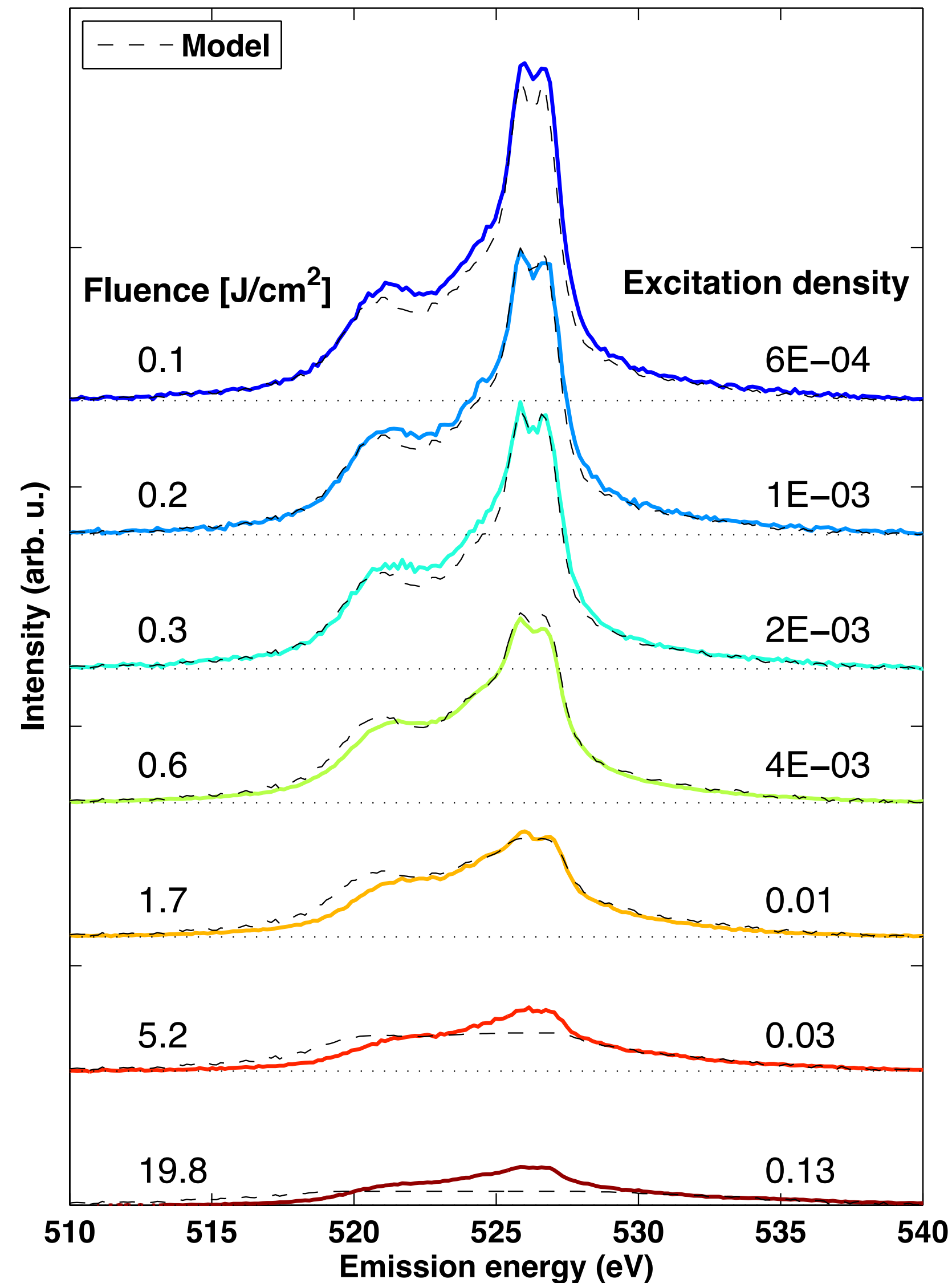


Excitation density [Photons/Molecule]



Saturation in spectra and count rate

Simple model taking Auger cascade into account, models dependences quantitatively



Summary

From theoretical field interactions to real experiments

- **Some non-linear processes have been observed**
- **Mostly population spectroscopy**
- **Electronic coherences in the X-ray regime still await discovery**
- **Potential to circumvent Auger cascade, if no population transfer**
- **Coherence lifetime undetermined, potentially very short**
- **WE NEED SHORTER PULSES!!!!**

**THANK YOU FOR YOUR
ATTENTION.**