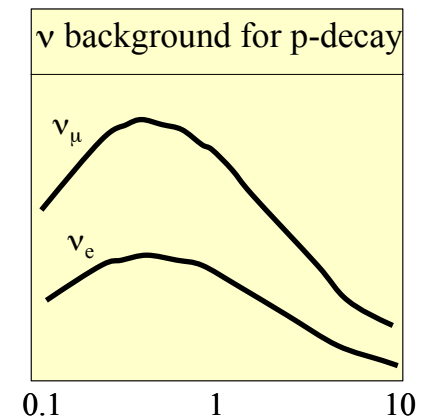


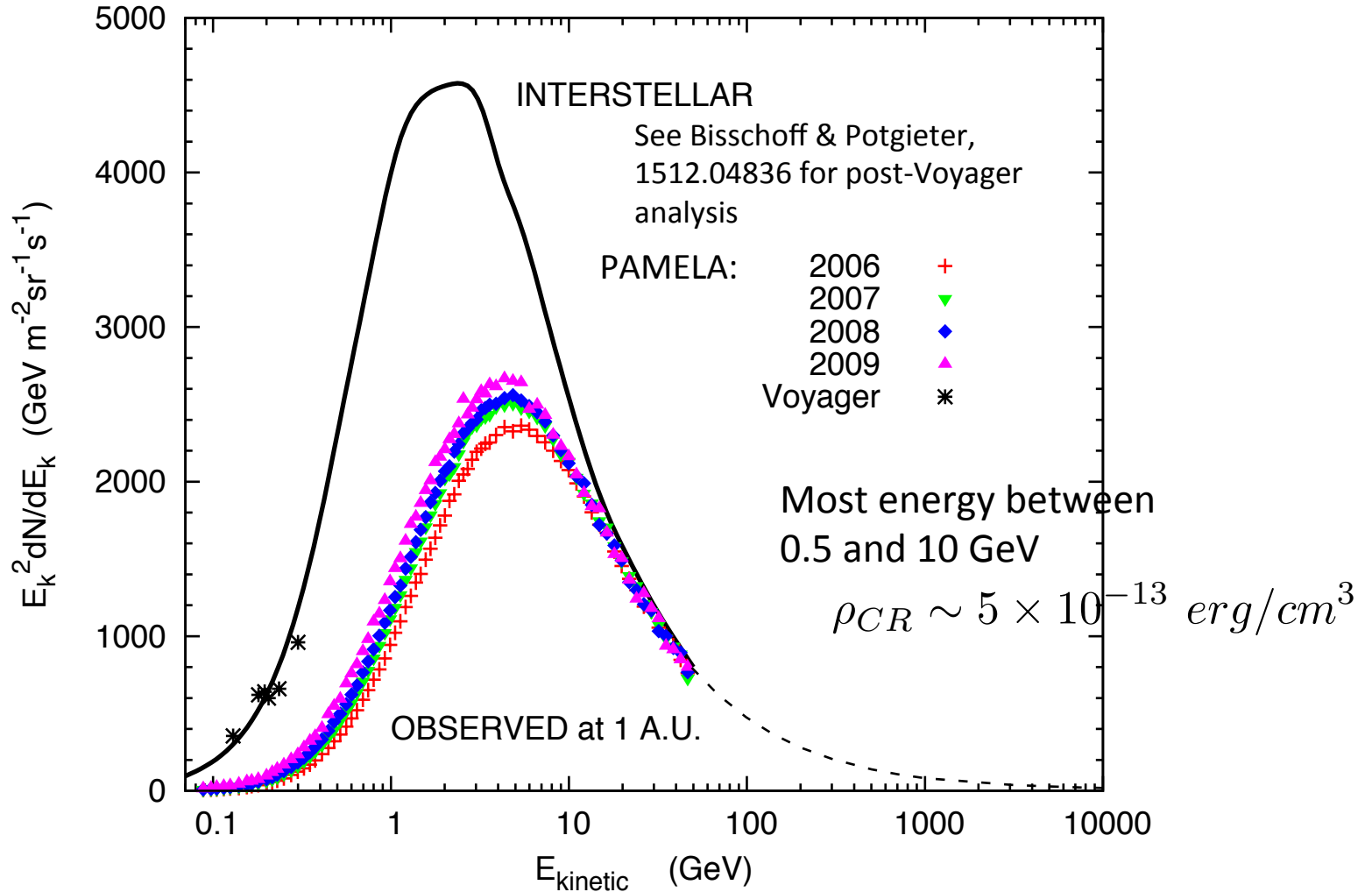
# Cosmic-ray fluxes relevant for Atmospheric Neutrinos

- I.  $\leq \text{TeV}$
- II.  $\text{TeV} \sim \text{PeV}$



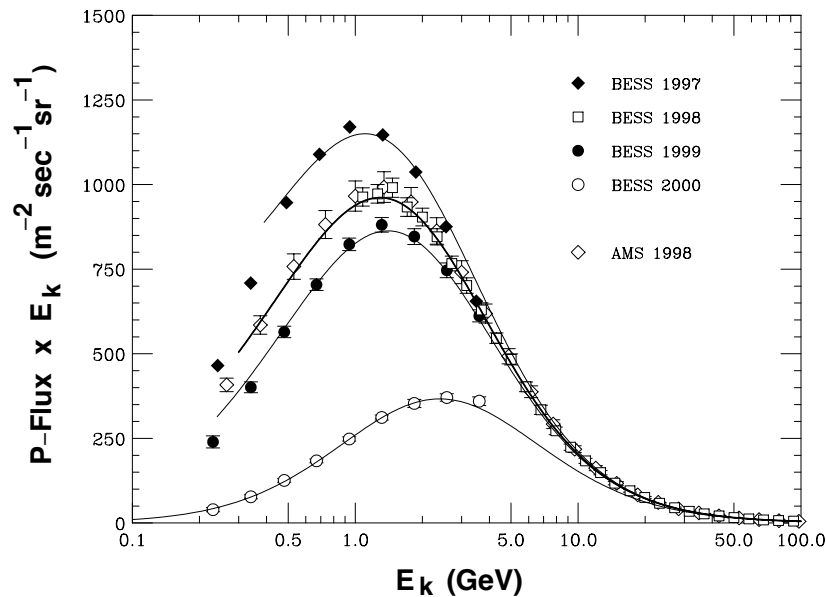
# From the local ISM to 1 AU

Energy Content of Galactic Cosmic-ray Protons

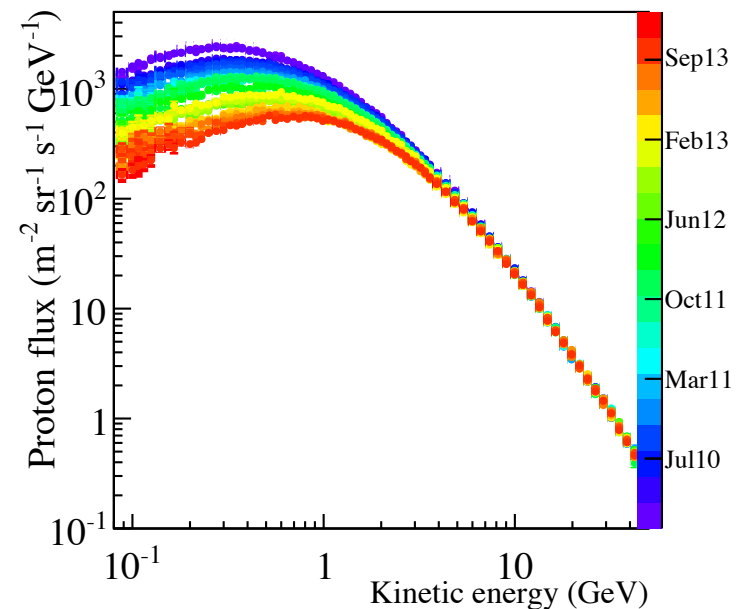


# Solar modulation

BESS, AMS, 1997 - 2000 Cycle 22,  $A > 0$   
Fig. from TG & Honda, 2002



PAMELA, 2010 – 2013  
Martucci et al., 1801.07112



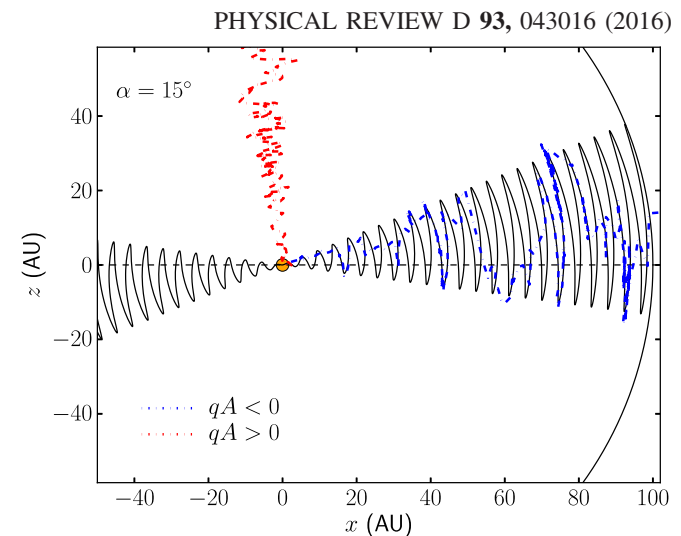
**Figure 9** Proton spectra measured by BESS in 1997, 1998, 1999, and 2000 (70).  
Curves are explained in the text.

See Cholis, Hooper & Linden, PR D 93 (2016) 043016 a full,  
physically motivated parameterization of charge-sign-  
dependent solar modulation

# Charge-sign-dependent solar modulation

- $A$  = polarity of the solar magnetic field
- Changes sign around solar max
- Modulation depends on  $qA$ 
  - Protons, anti-protons are modulated differently
  - Cholis, Hooper, Linden, PR D93 (2016) 043016

\*Gives a detailed parameterization of the force-field parameter as a function of date that accounts for the physical effects of drift and diffusion in the heliospheric magnetic field

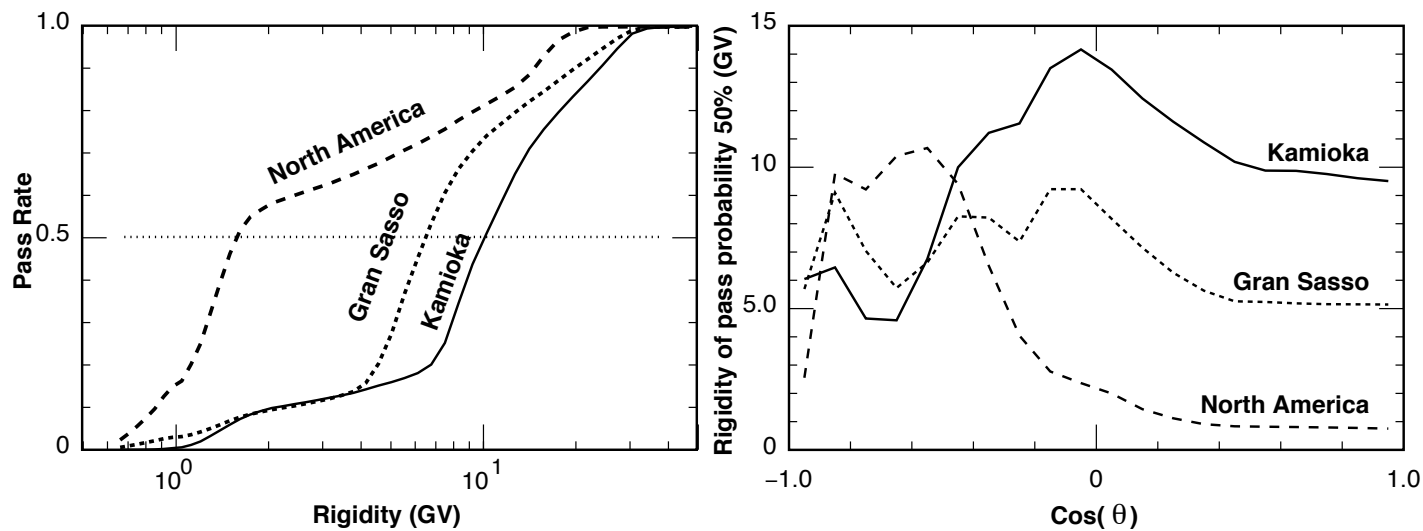
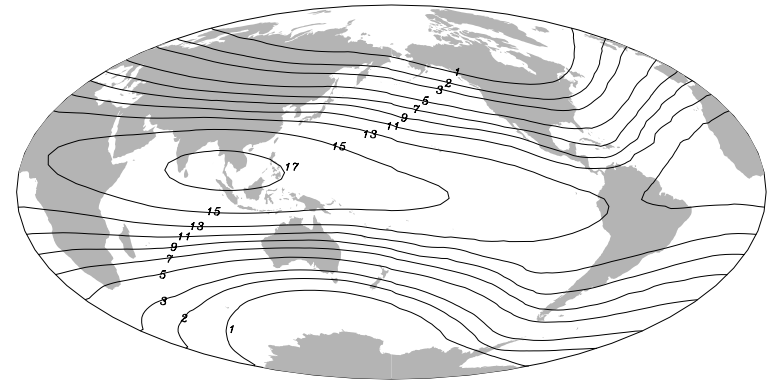


# Next step: getting through the geomagnetic field



Guy Murchie,  
1954

# Geomagnetic cutoffs

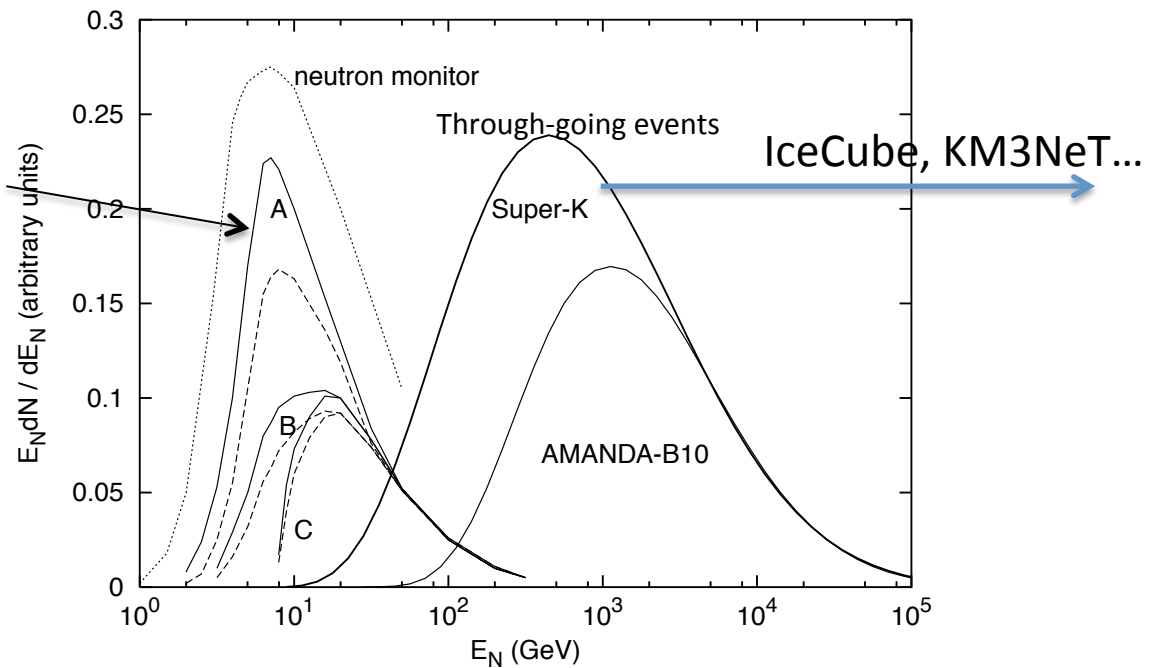


**Figure 11** Cutoffs at three locations: north-central North America (Soudan, Sudbury); Gran Sasso; Kamioka. The left panel shows the passing rate as a function of rigidity integrated over all directions. The right panel shows the rigidity above which half the particles in the azimuthal band at each zenith angle reach the atmosphere. (Positive  $\cos \theta$  refers to downward-moving particles.) TG & Honda, 2002

# What primary energies are relevant?

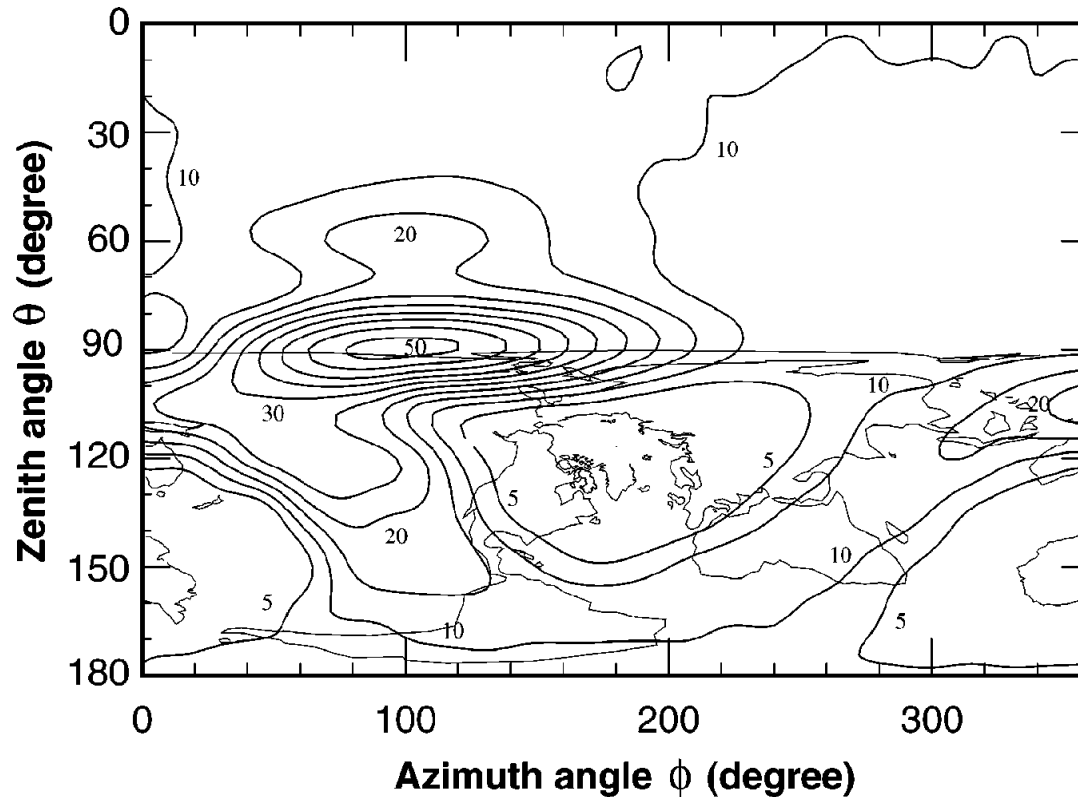
Sub-GeV events at Super-K

- A) Without cutoffs
- B) Upgoing events
- C) Downgoing events



TG, Honda, Ann.Revs. 52 (2002)

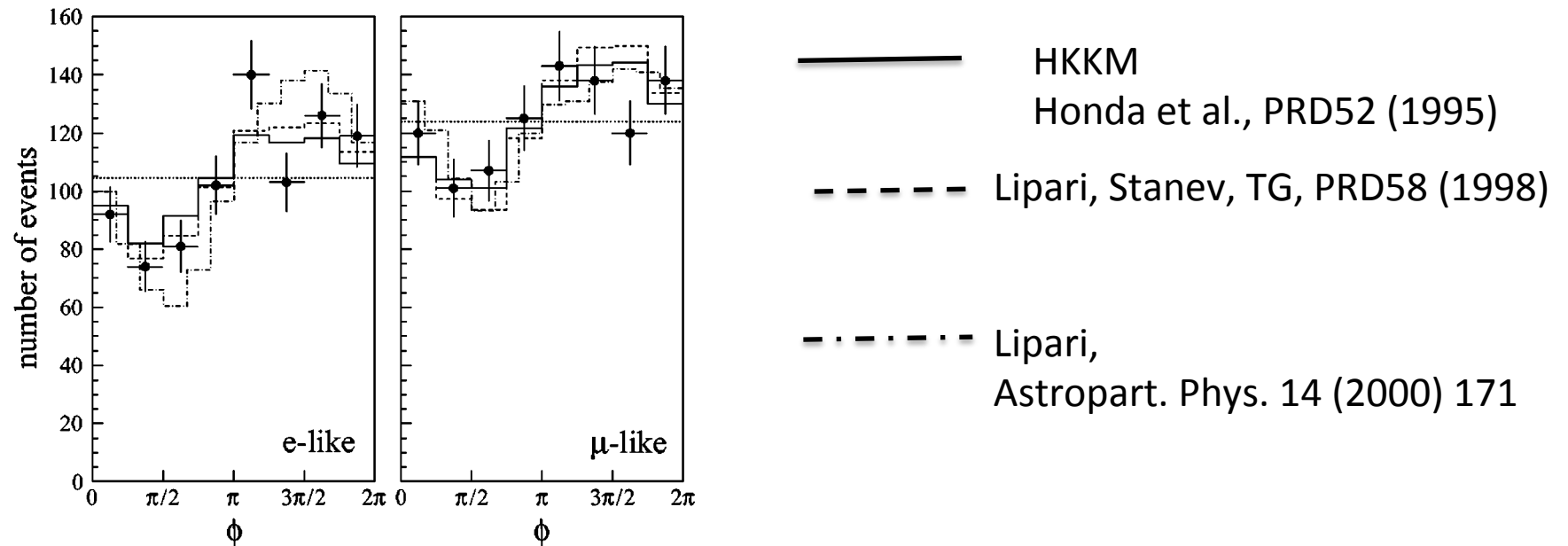
# Strong East-West effect at Super-K



**Figure 10** Contour map of the rigidity cutoff as seen from the Kamioka site. Rigidity cutoffs are shown as a function of arrival direction of the neutrino. (Zenith angle  $>90^\circ$  is for upward-moving particles.) An outline map of the continents is superimposed on the lower hemisphere.



# East-West effect on neutrinos

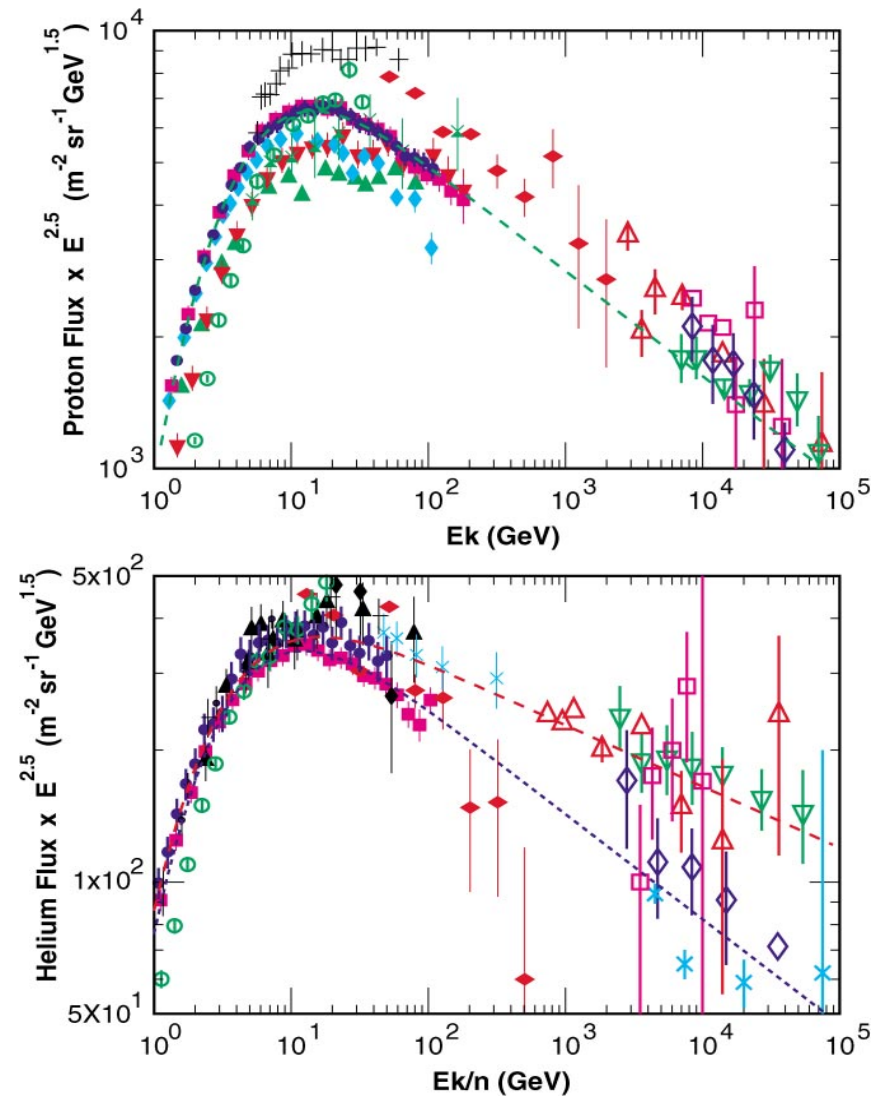


Data from Super-K\* in fixed zenith band compared to calculations.  
Complemented observation of zenith dependence from oscillations.

\*Super-K, (Futagami et al., P.R.L. 82 (1999) 5192

# Spectrum circa 2002

Annu. Rev. Nucl. Part. Sci. 2002.52:153-199. Downloaded from www.annualreviews.org. Access provided by University of Delaware on 04/12/18. For personal use only.



**Figure 6** Observed flux of cosmic-ray protons and helium. The dashed lines show the fits described in the text. The data are: Webber (48), crosses; LEAP (49), upward solid triangles; MASS1 (50), open circles; CAPRICE (52), vertical solid diamonds; IMAX (53), downward solid triangles; BESS98 (54), solid circles; AMS (55, 56), solid squares; Ryan (57), horizontal solid diamonds; JACEE (58), downward open triangles; Ivanenko (59), upward open triangles; Runjob (60), open diamonds; Kawamura (61), open squares. TG & Honda, 2002

Nucleons per GeV/nucleon

# Flux parameterizations

$$\phi(E_k) = K \times \left( E_k + b \exp\left[-c\sqrt{E_k}\right] \right)^{-\alpha}$$

TG, Honda, Lipari, Stanev  
ICRC 27 (Hamburg) 2001  
5(1643)

E in GeV, the b and c factors account for modulation at solar min

**TABLE 2** Parameters for all five components in the fit of Equation 10

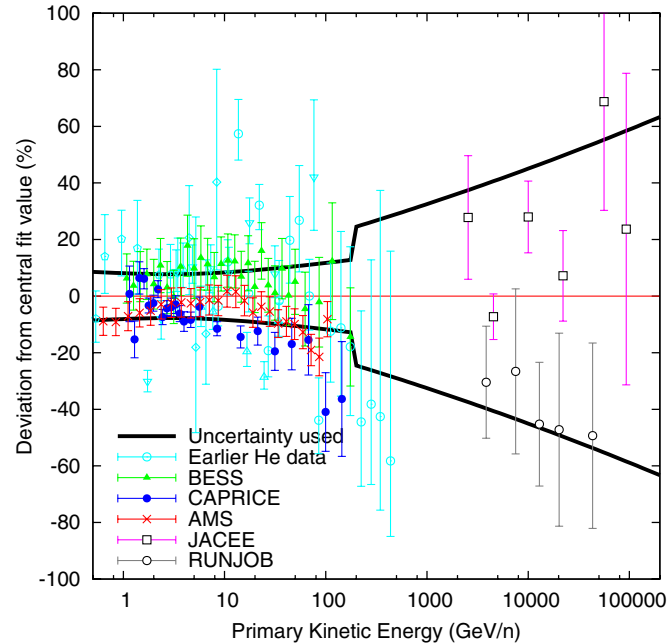
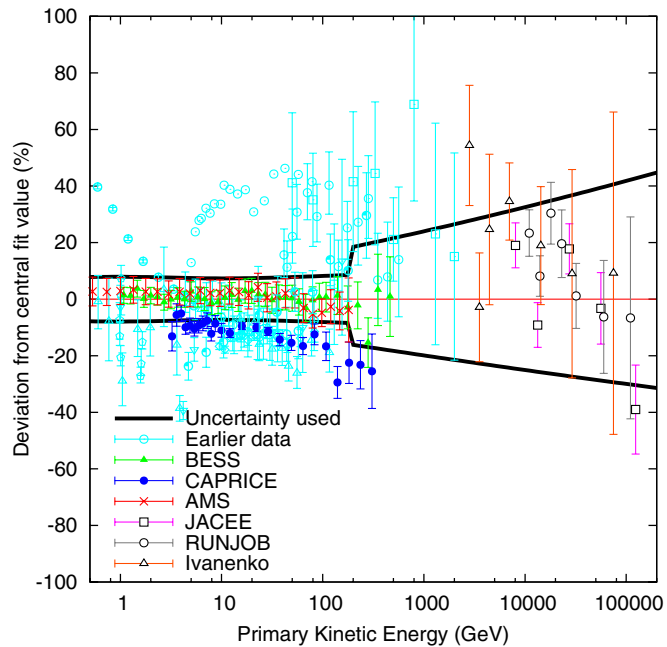
Parameter/component	$\alpha$	$K$	$b$	$c$
Hydrogen ( $A = 1$ )	$2.74 \pm 0.01$	$14900 \pm 600$	2.15	0.21
He ( $A = 4$ , high)	$2.64 \pm 0.01$	$600 \pm 30$	1.25	0.14
He ( $A = 4$ , low)	$2.74 \pm 0.03$	$750 \pm 100$	1.50	0.30
CNO ( $A = 14$ )	$2.60 \pm 0.07$	$33.2 \pm 5$	0.97	0.01
Mg-Si ( $A = 25$ )	$2.79 \pm 0.08$	$34.2 \pm 6$	2.14	0.01
Fe ( $A = 56$ )	$2.68 \pm 0.01$	$4.45 \pm 0.50$	3.07	0.41

Parameter values from  
TG, Honda (Ann.Revs.Nucl.  
Part. Sci. 52, 2002).

In view of more recent data, it is good that we favored the “high” He !

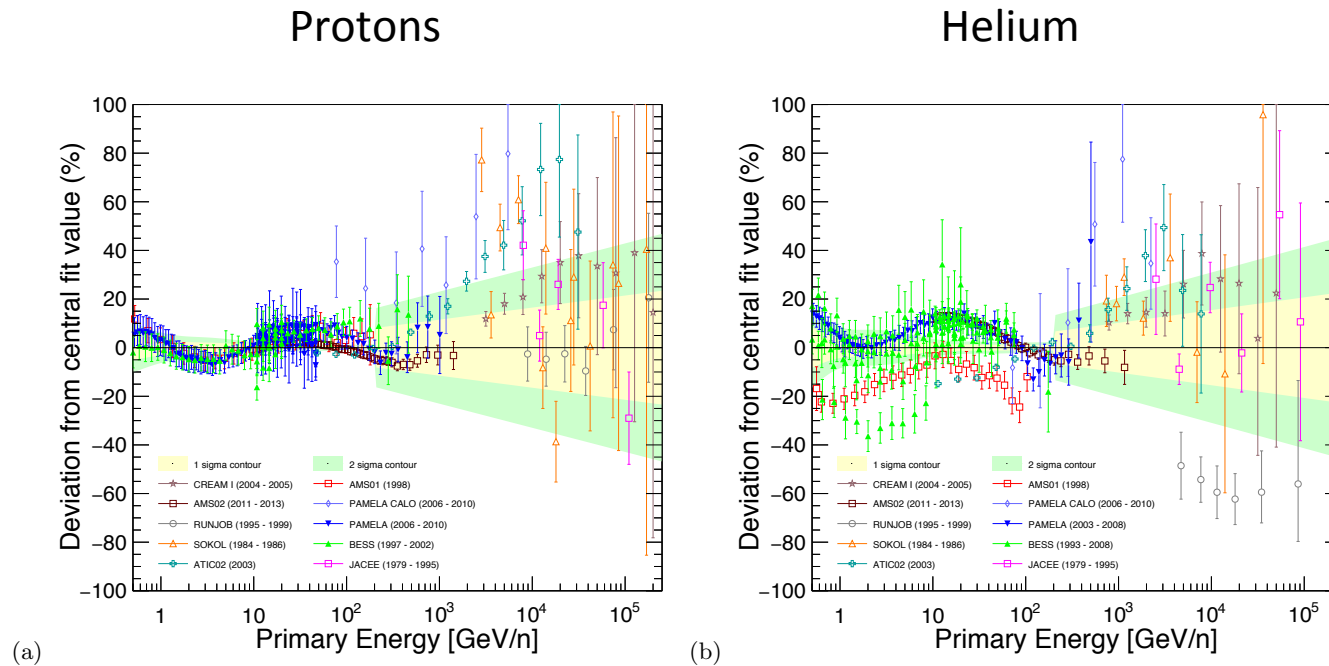
# Data, 2005

Low energy measurements with spectrometers, higher energy with calorimeters



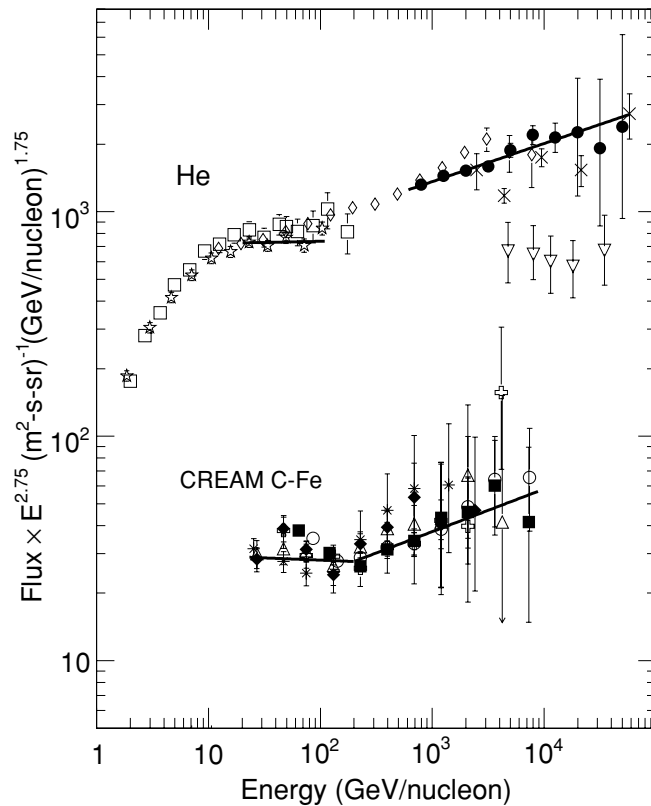
Ratio of data to parameterization for protons and helium from uncertainties paper Barr et al., PR D74 (2006) 094009

# Updated fits include new data: Evans et al., PR D95 (2017) 023012 ( 1612.03219)

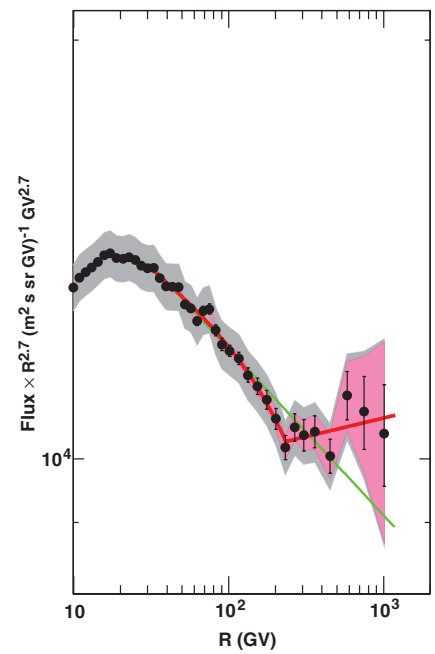


Main new data sets: PAMELA, AMS02, CREAM  
Plots show ratio of data to fits to the GHLS form with new parameter values.  
Uncertainty band is reduced.  
**However: Note systematic difference in shape**

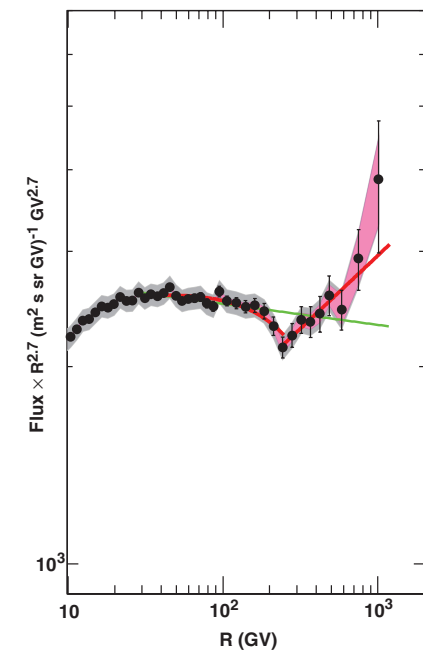
# New observation: Spectral hardening



Proton



Helium

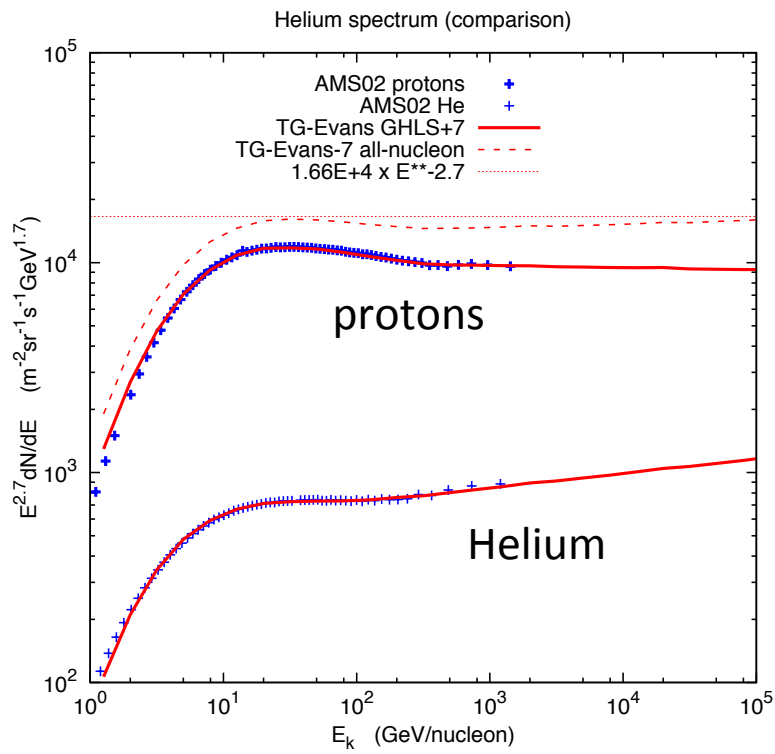


PAMELA, Science 332 (2011) 69

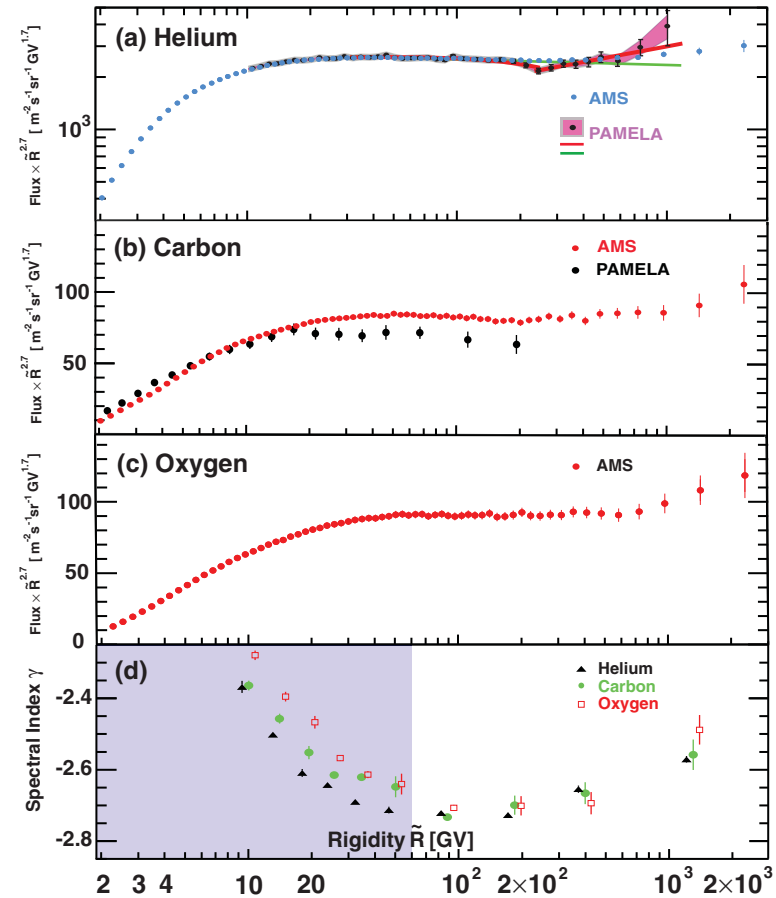
“Discrepant hardening”

CREAM, Ap.J. Letters 714 (2010) L89

# AMS 02



## Rigidity dependent hardening



AMS02, PRL 119 (2017) 251101

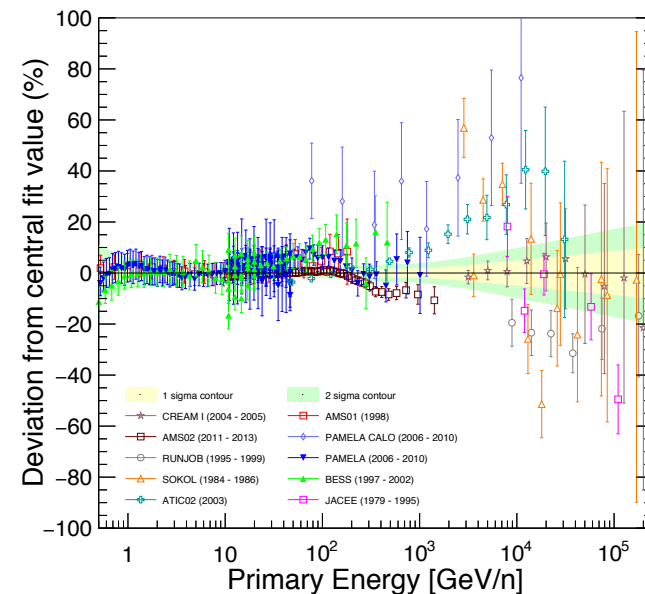
# Evans et al. 7 parameter fit addresses the hardening for protons

$$\phi(E_p) = K \times \left( E_p + b \exp \left[ -c \sqrt{E_p} \right] \right)^{-\alpha} \times \left[ 1 + \left( \frac{E_p}{k} \right)^s \right]^{\frac{\alpha - \alpha'}{s}}$$

3 new parameters:

- $k \approx 150$  GeV,
- $s =$  sharpness,
- $\alpha' < \alpha =$  high energy spectral index

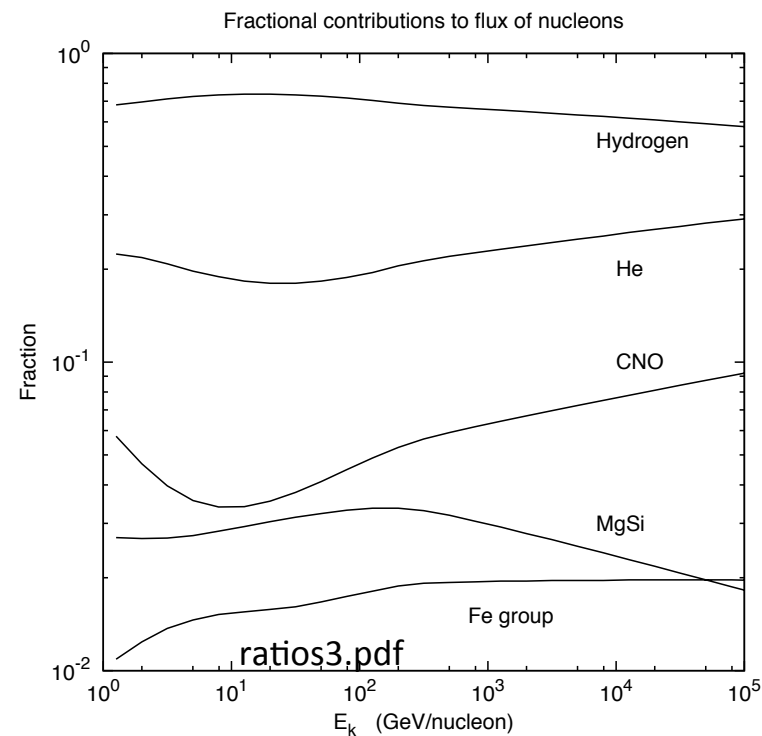
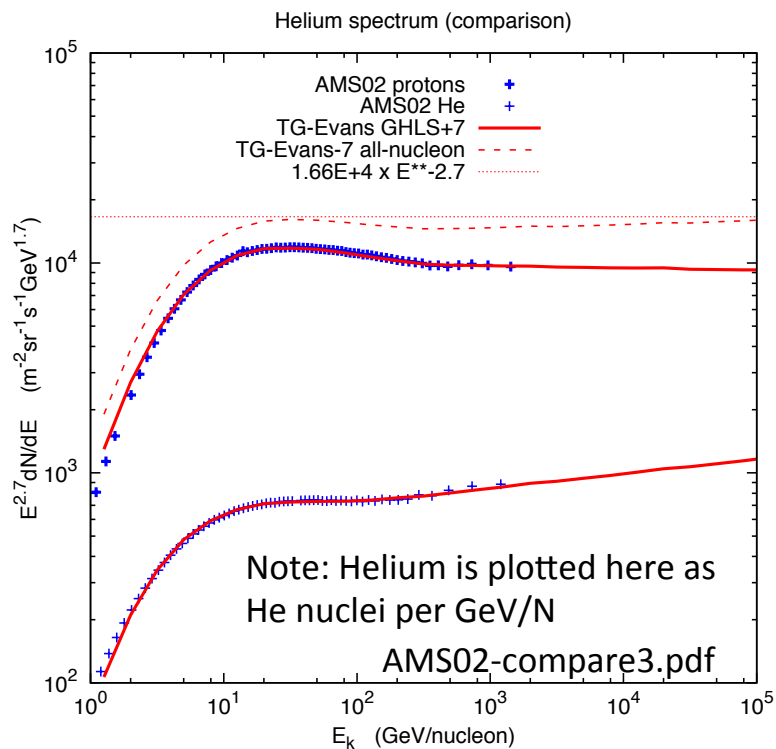
The steepening factor form is from Ter-Antonyan & Haroyan, hep-ex:0003006 (see also Lipari, Astropart. Phys. 97 (2018) 197



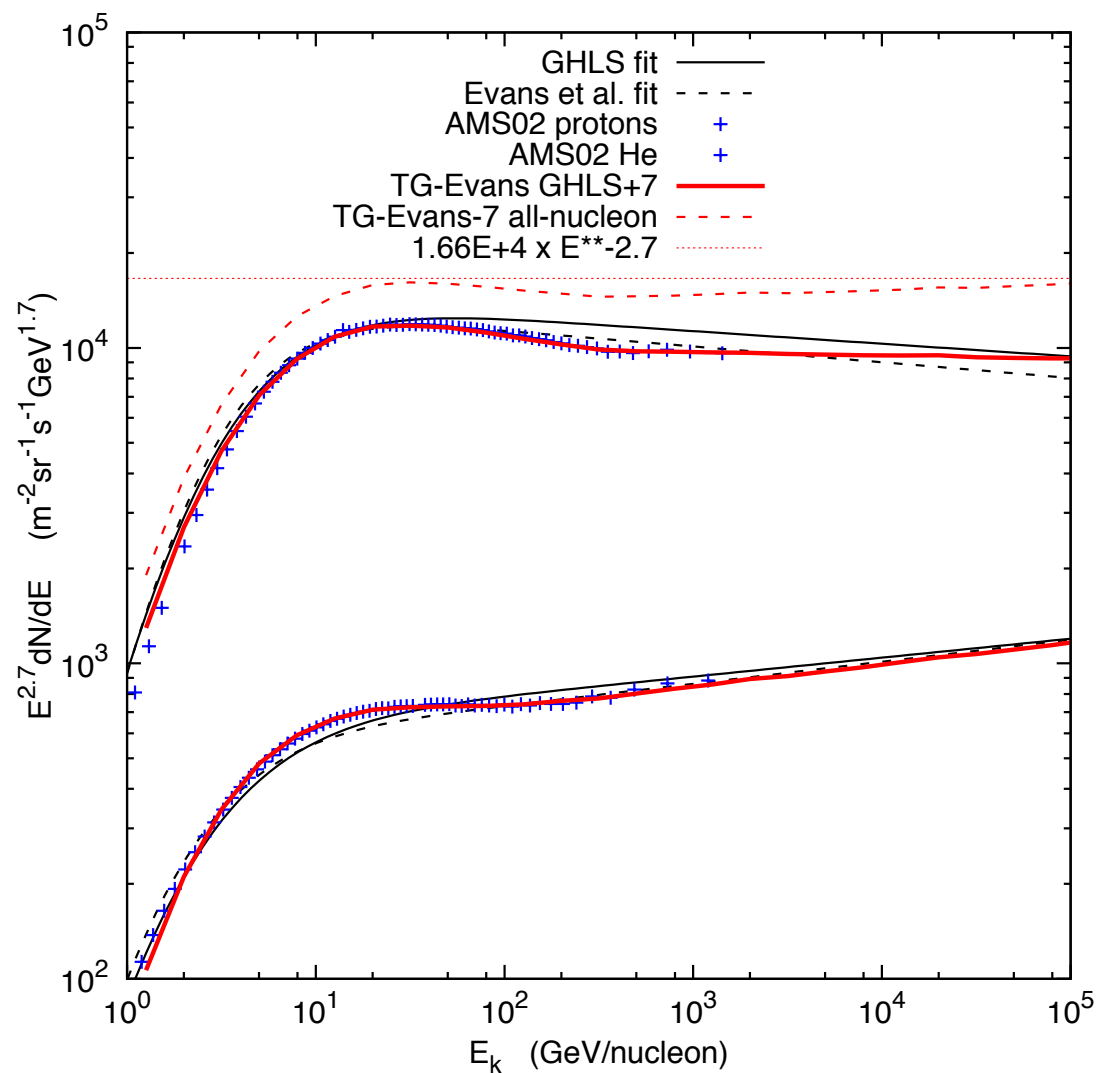


# Modified versions of Evans et al.

Since I want to use these parameterizations specifically for AMS02 antiprotons, I adjusted the fits to give better agreement with AMS02 H and He data. I used the seven-parameter form for He as well as for H. (Evans used it only for H.) Work is in `~/atmosnu/Giles2016/bartol/primary/gbthesisdata/tkg2016/` (11-12 Feb 2017)  
Note: AMS02 data are converted from GV to kinetic energy per nucleon in gnuplot files.

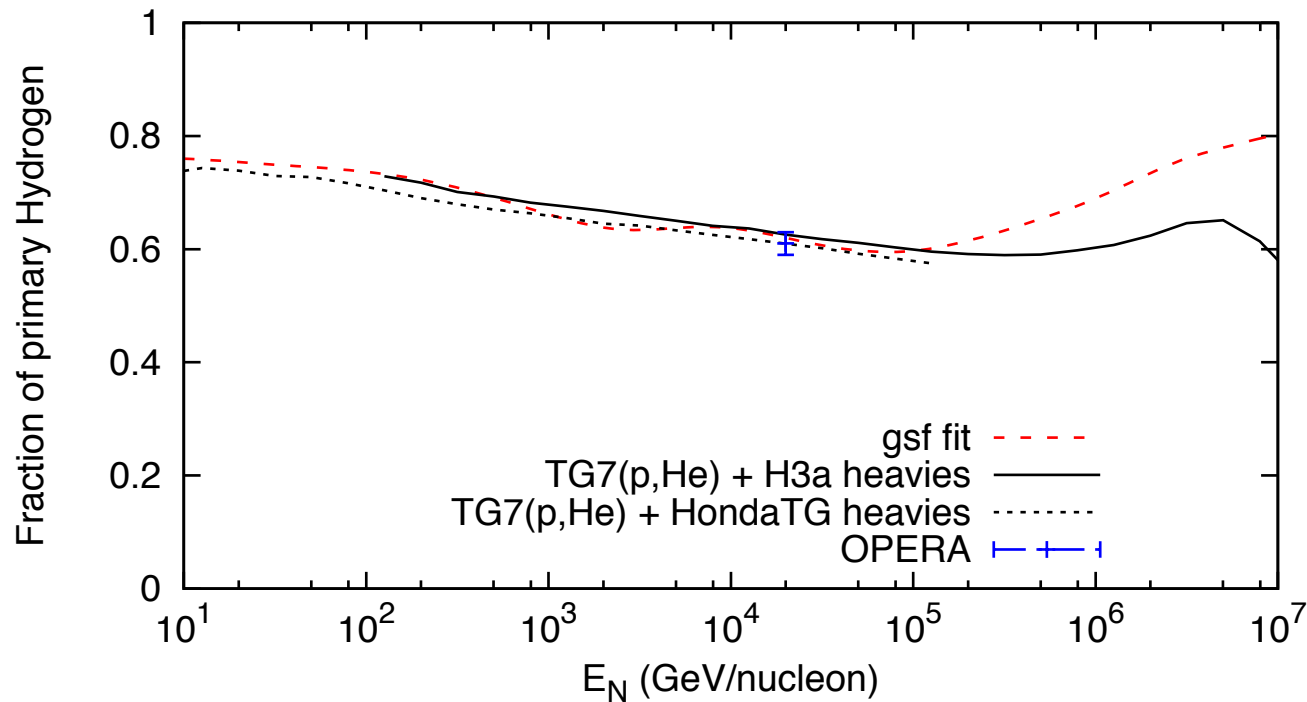


# Compare fits to AMS02



# Hydrogen fraction and $v/\bar{v}$ ratio

To first order depends on  $\delta_0 = \frac{p - n}{p + n} \approx \frac{H}{N}$



# Relation to atmospheric muons

Pions only (Frazer et al., PR D 5 (1972) 1653)

$$\frac{\mu^+}{\mu^-} \approx \frac{1 + \beta\delta_0\alpha_\pi}{1 - \beta\delta_0\alpha_\pi} = \frac{f_{\pi^+}}{1 - f_{\pi^+}},$$

$$\beta = \frac{1 - Z_{pp} - Z_{pn}}{1 - Z_{pp} + Z_{pn}} \approx 0.909;$$

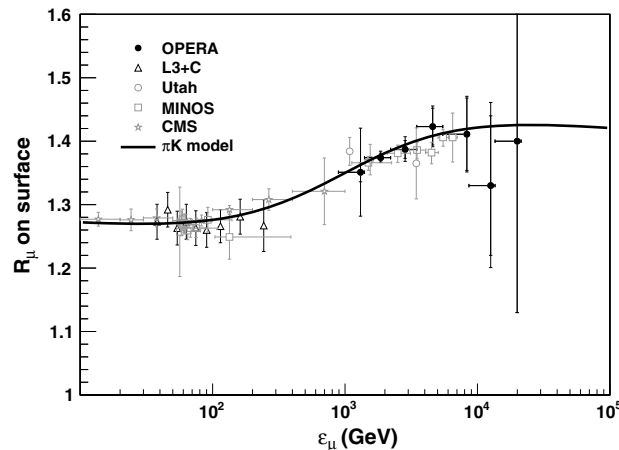
$$\alpha_\pi = \frac{Z_{p\pi^+} - Z_{p\pi^-}}{Z_{v\pi^+} + Z_{v\pi^-}} \approx 0.165$$

Include K  $\rightarrow \mu + \nu_\mu$

TG Astropart. Phys. 35(2012) 801

$$\frac{\mu^+}{\mu^-} = \left[ \frac{f_{\pi^+}}{1 + B_{\pi\mu} \cos(\theta) E_\mu / \epsilon_\pi} + \frac{\frac{1}{2}(1 + \alpha_K \beta \delta_0) A_{K\mu} / A_{\pi\mu}}{1 + B_{K\mu}^+ \cos(\theta) E_\mu / \epsilon_K} \right] \times \left[ \frac{(1 - f_{\pi^+})}{1 + B_{\pi\mu} \cos(\theta) E_\mu / \epsilon_\pi} + \frac{(Z_{NK^-} / Z_{NK}) A_{K\mu} / A_{\pi\mu}}{1 + B_{K\mu} \cos(\theta) E_\mu / \epsilon_K} \right]^{-1}$$

$$\alpha_K = \frac{Z_{pK^+} - Z_{pK^-}}{Z_{pK^+} + Z_{pK^-}}$$

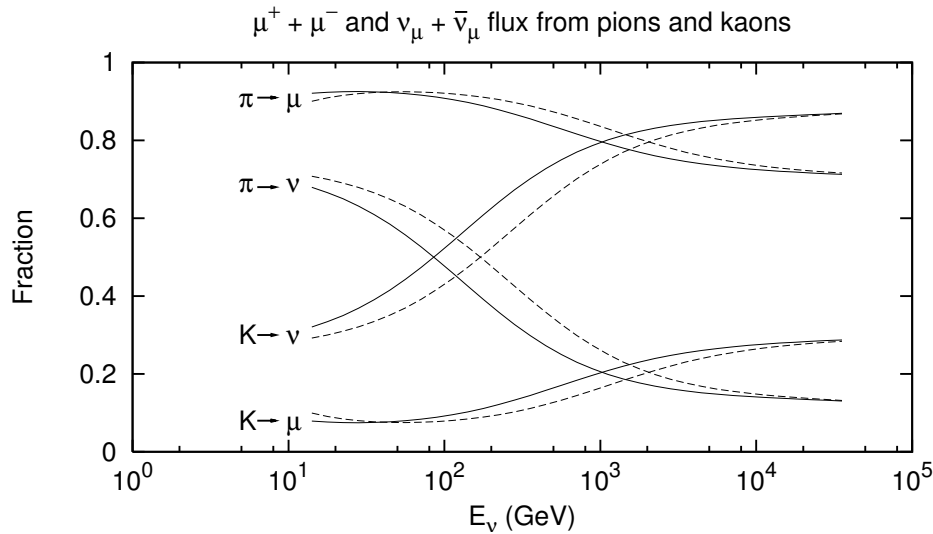


Rise in muon charge ratio reflects higher asymmetry in the charged kaon channel, which becomes more important when

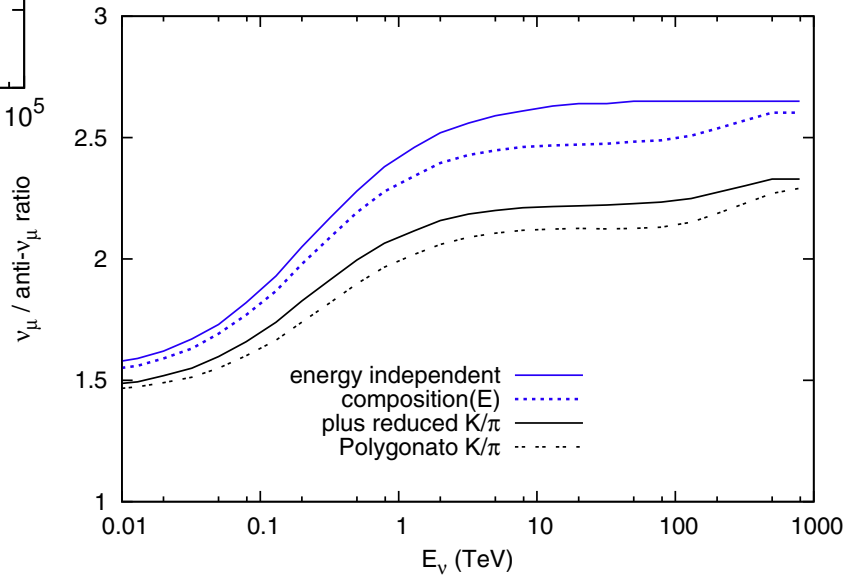
$E_\mu > \epsilon_K \approx 850 \text{ GeV}$ .

The key parameter is  $\alpha_K$

# The effect is more important for $\nu_\mu$



2-body decay kinematics favors  
K over  $\pi$  for neutrinos

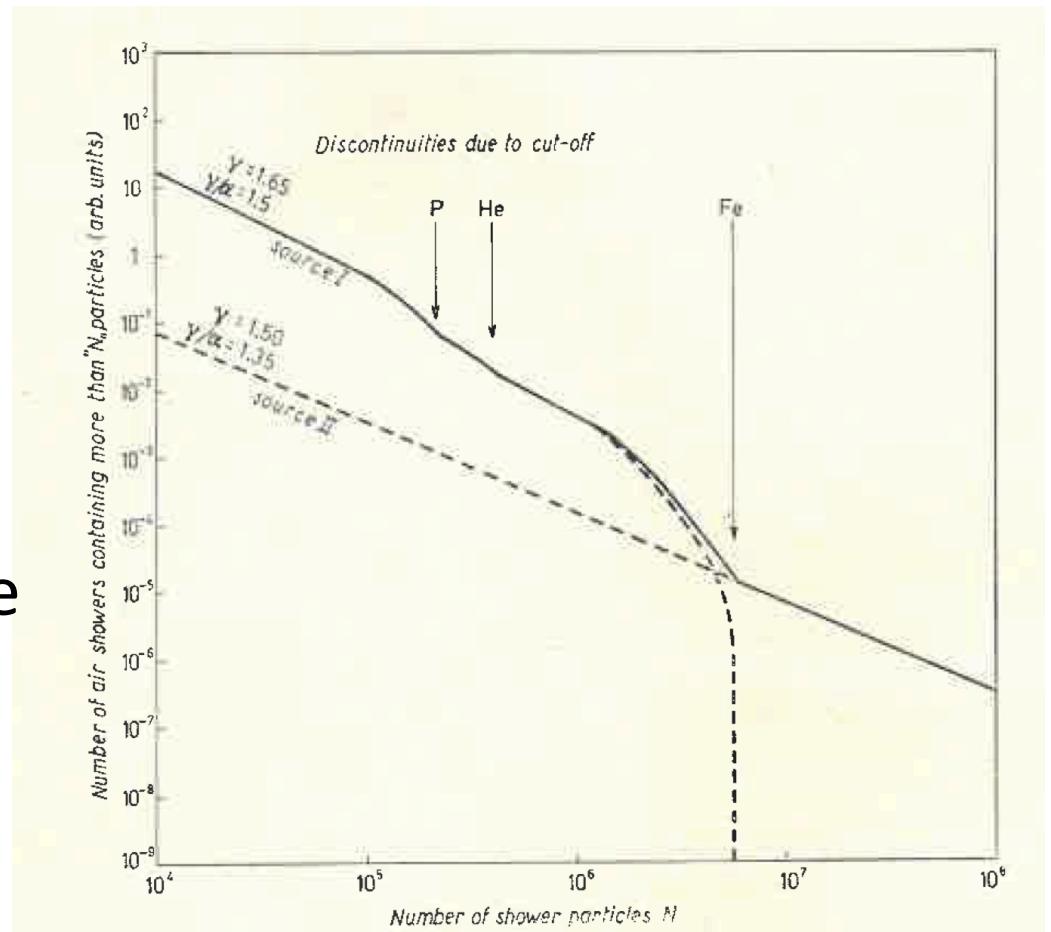


# $E \gg 100 \text{ TeV}$

- Flux too low for direct measurements
- Ground-base EAS experiments
  - Large aperture x exposure provides data to  $\gg \text{EeV}$
  - All-particle spectrum depends on  $E$  per nucleus
  - Composition measurements at best resolve groups of nuclei, e.g. (p, He, CNO, Mg-Si, Fe)
- We need the spectrum of nucleons (in  $E$  per nucleon) to calculate fluxes of leptons
- Physics-based models give useful guidance

# Peters cycles and particle populations

- Rigidity dependence
  - $R = P_{\text{tot}} c / Z e$
  - Implies sequence: p, He, C, ... Fe
- Spectral hardening
  - Suggests new particle population
- Galactic and extra-galactic populations

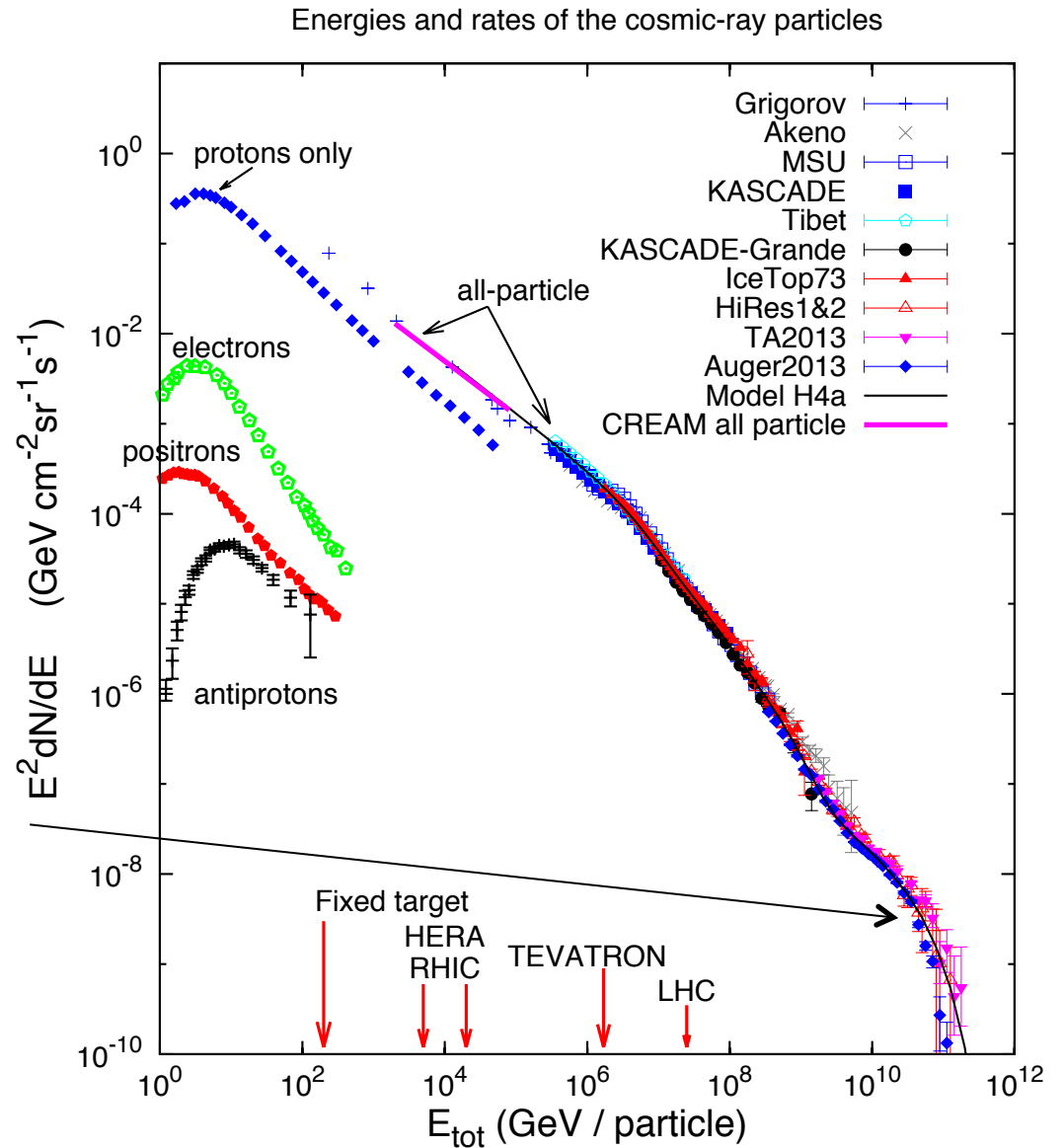


B. Peters, Il Nuovo Cimento 22 (1961) 800

# Spectrum

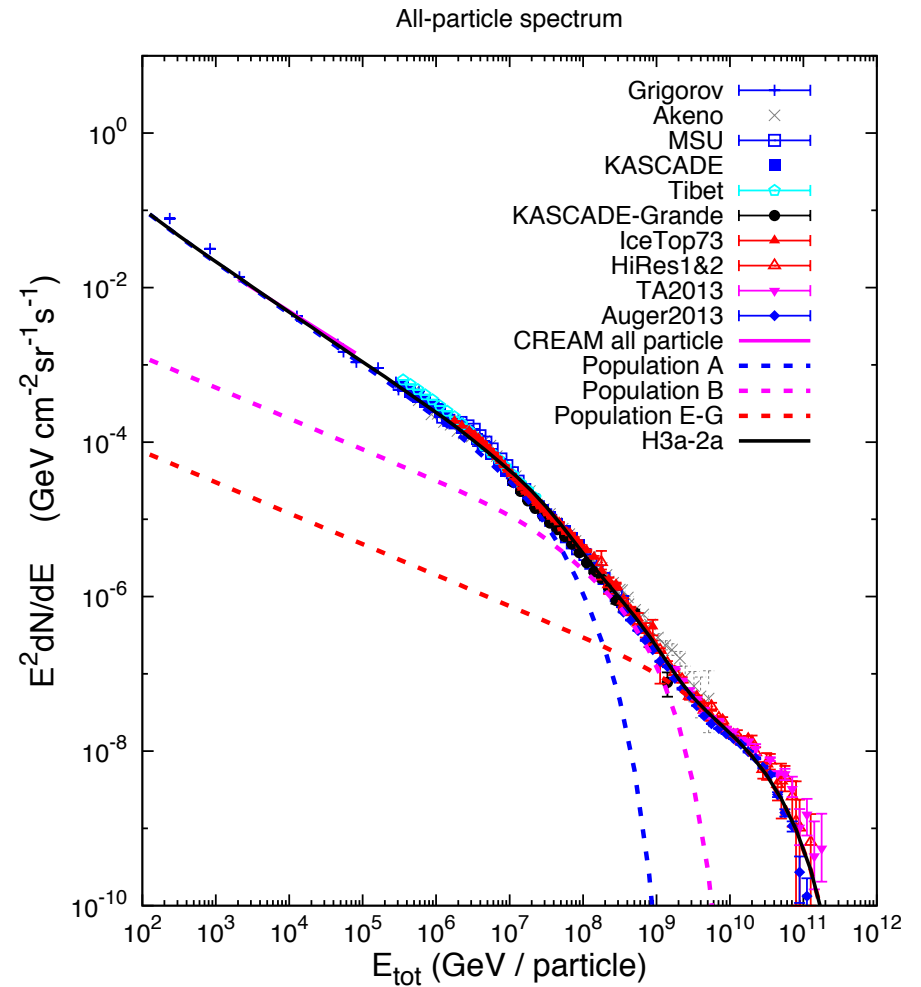
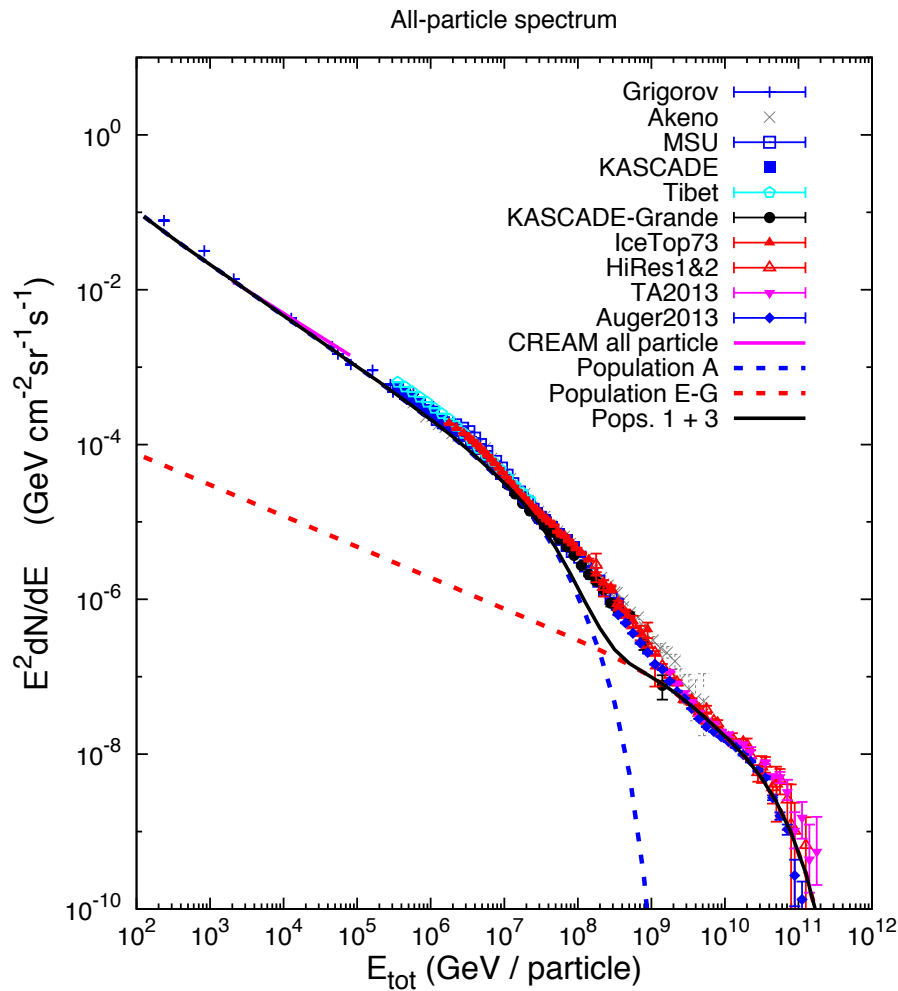
-- a global view

Cutoff ? .... or  
Maximum energy  
of acceleration?

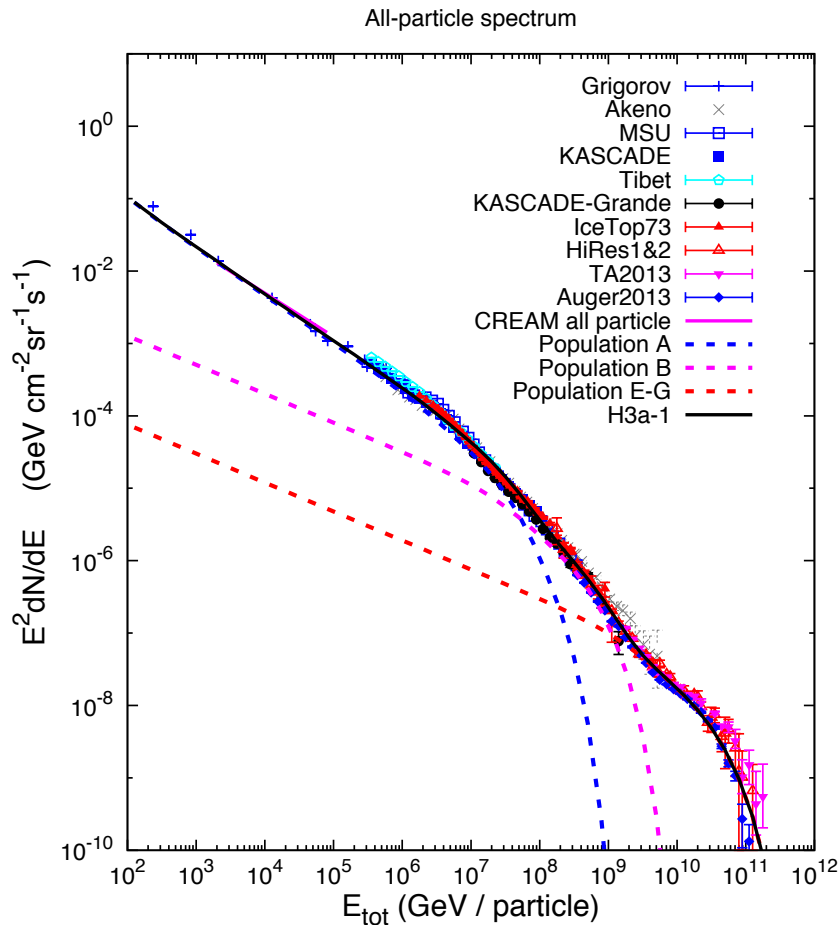




# 2 components is not enough



# 3 population model



## Pop. 1: Galactic I

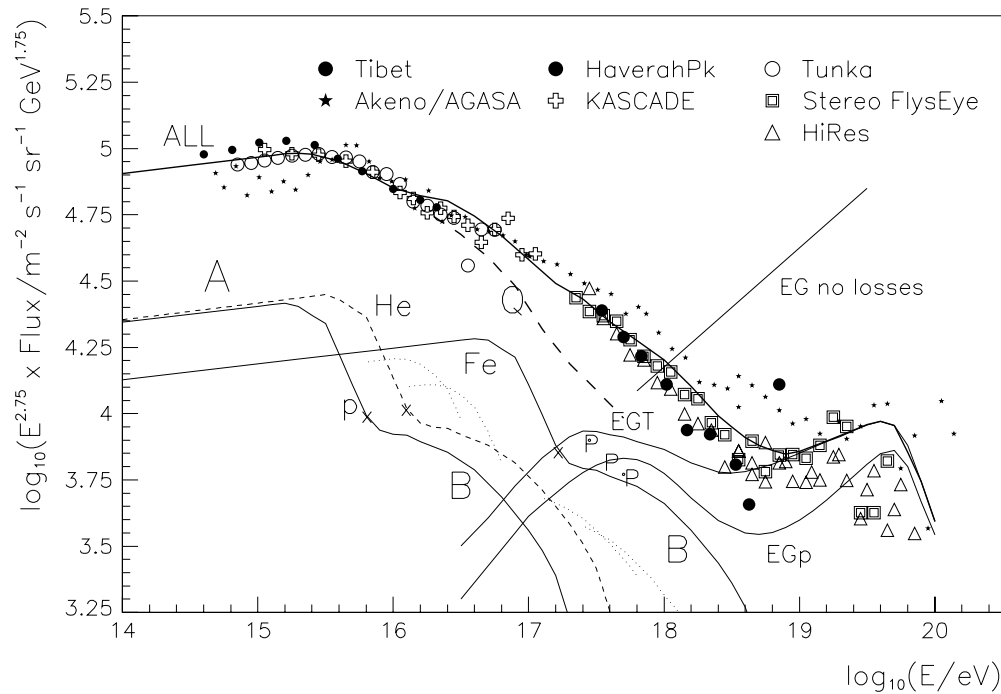
- Assume power-law extrapolation of each group from direct measurements
- Assume rigidity-dependent cutoff at the knee

## Pop. 2: Galactic II

- Needed to fill in before extragalactic component
- Assume rigidity-dependent cutoff

## Pop. 3: Extragalactic

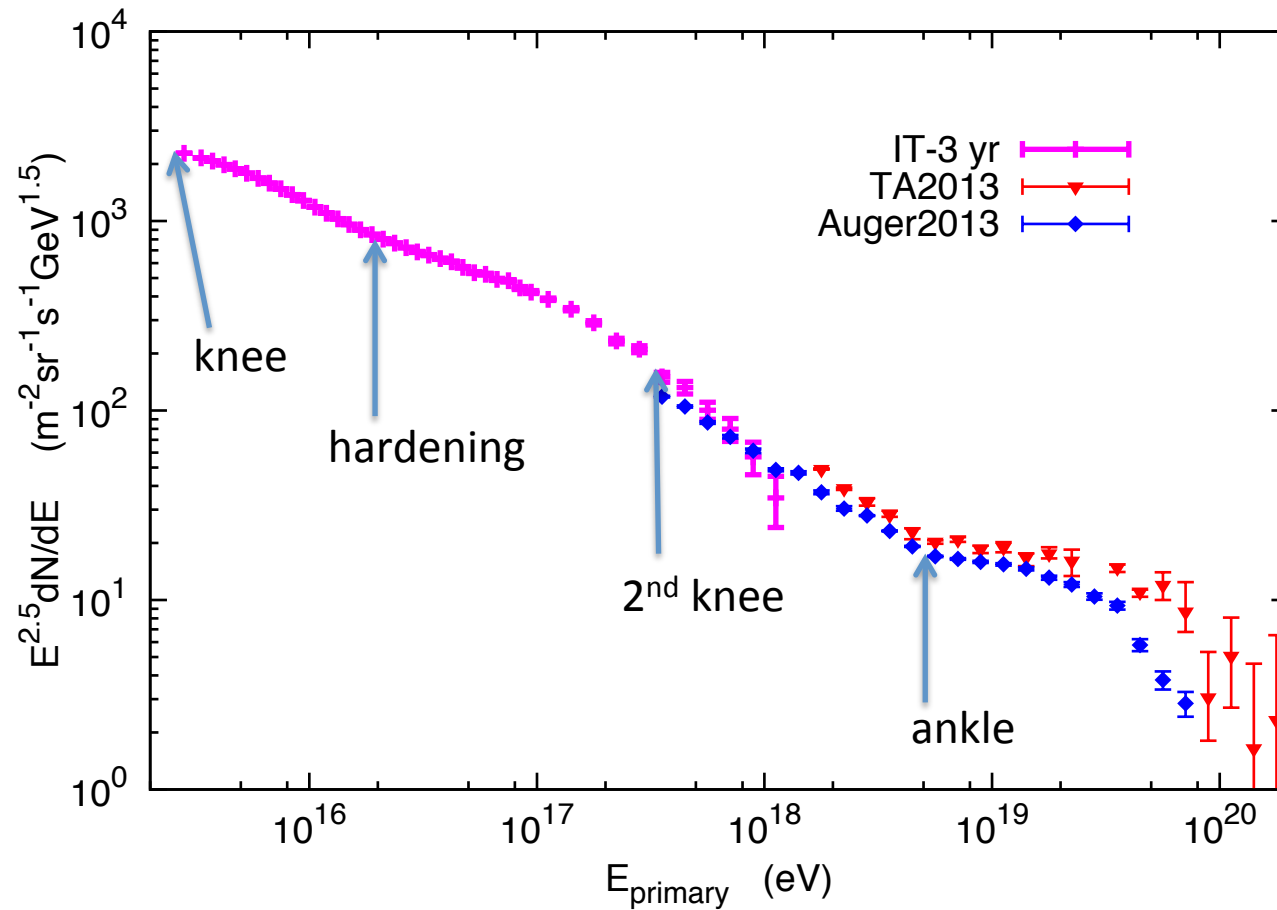
# Hillas' Galactic population B



**Figure 2.** The cosmic ray spectrum as the sum of galactic H, He, CNO, Ne-S and Fe components with the same rigidity dependence, and extragalactic H + He (total EGT) having a spectrum  $\propto E^{-2.3}$  before suffering losses by CMBR and starlight interactions. The galactic components were given a turn-down shape based on KAS CADE knee shape as far as the point marked x. The dashed line Q is the total if the extended tail B of the galactic flux is omitted.

A.M. Hillas, J. Phys. G: Nucl. Part. Phys. **31** (2005) R95–R131

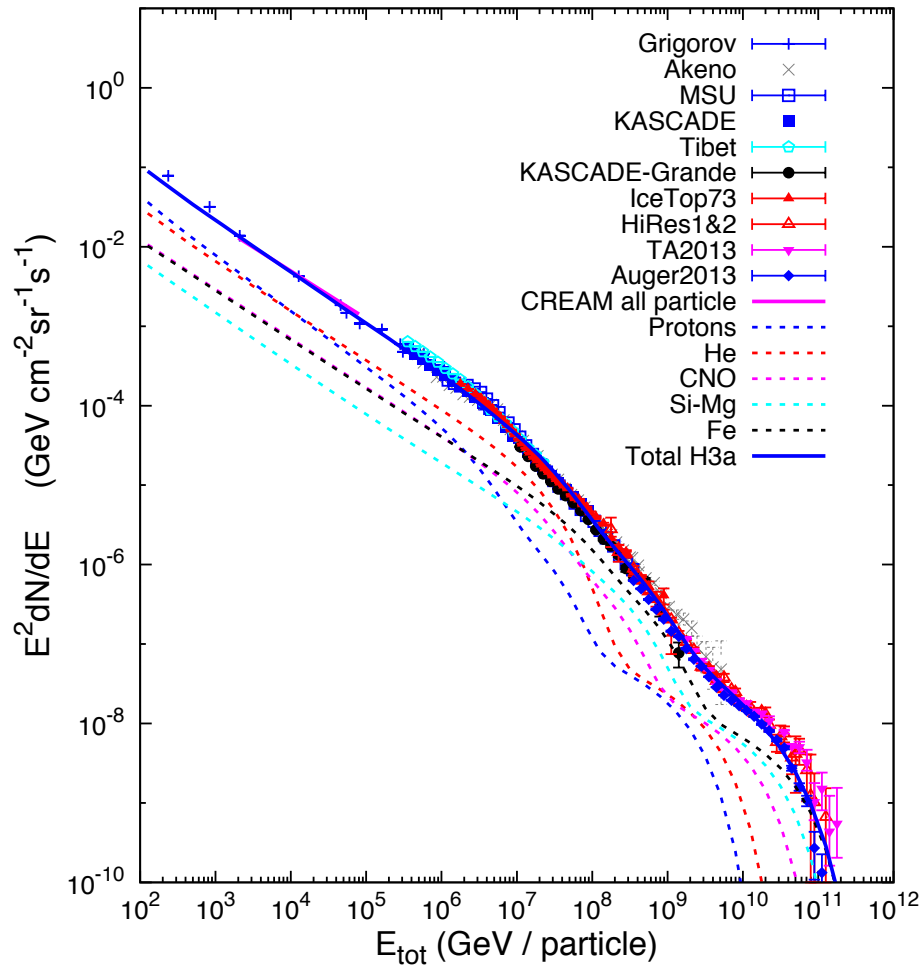
# Features in all-particle spectrum



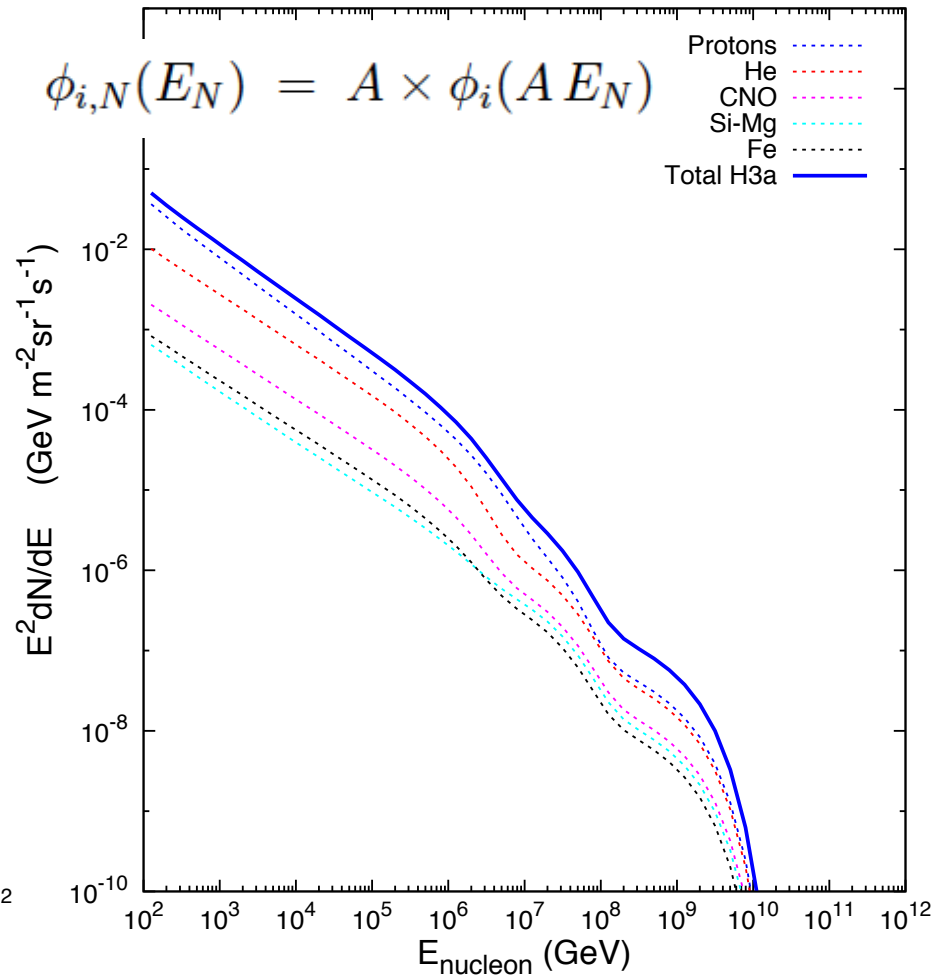
# All-particle spectrum to nucleon spectrum

$$\phi_i(E) \equiv E \frac{dN_i}{dE} = \sum_{j=1}^3 a_{i,j} E^{-\gamma_{i,j}} \times \exp \left[ -\frac{E}{Z_i R_{c,j}} \right]$$

All-particle spectrum



Spectrum of nucleons



# Three-population models

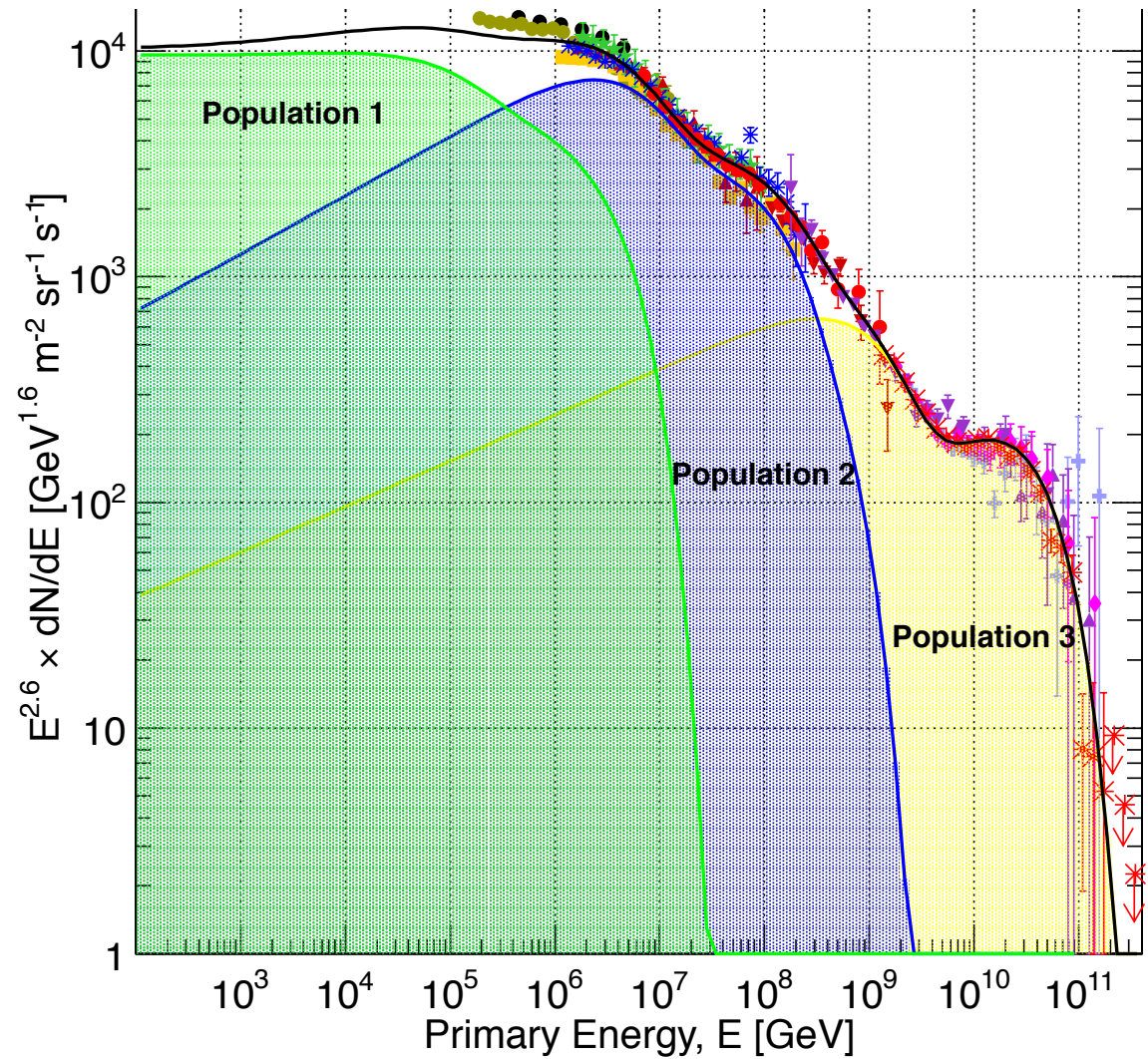
		p	He	CNO	Mg-Si	Fe
Galactic A	Pop. 1:	7860	3550	2200	1430	2120
	$R_c = 4$ PV	1.66	1.58	1.63	1.67	1.63
Galactic B	Pop. 2:	20	20	13.4	13.4	13.4
	$R_c = 30$ PV	1.4	1.4	1.4	1.4	1.4
Extragalactic { H3a →	Pop. 3:	1.7	1.7	1.14	1.14	1.14
	$R_c = 2$ EV	1.4	1.4	1.4	1.4	1.4
H4a →	Pop. 3(*):	200	0.0	0.0	0.0	0.0
	$R_c = 60$ EV	1.6				

TG Astropart. Phys. 35 (2012) 801

		p	He	C	O	Fe	$50 < Z < 56$	$78 < Z < 82$
GST	Pop. 1:	7000	3200	100	130	60		
	$R_c = 120$ TV	1.66	1.58	1.4	1.4	1.3		
	Pop. 2:	150	65	6	7	2.3	0.1	0.4
	$R_c = 4$ PV	1.4	1.3	1.3	1.3	1.2	1.2	1.2
	Pop. 3:	14				0.025		
	$R_c = 1.3$ EV	1.4				1.2		

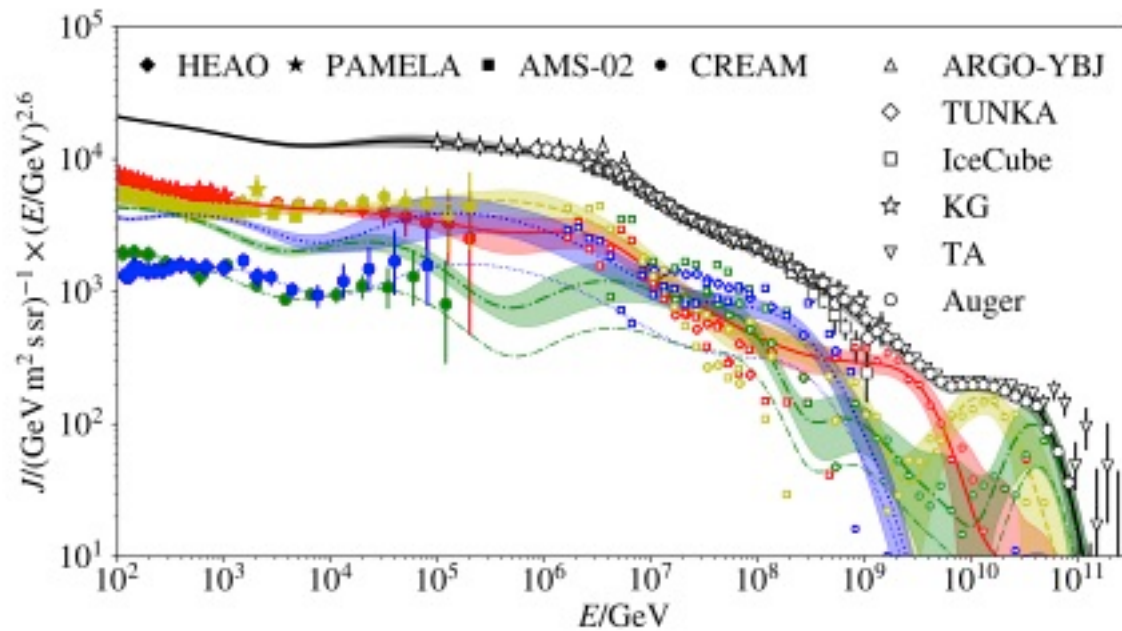
TG, Stanev, Tilav, Front. Phys. (Beijing) 8 (2013) 748 (arXiv:1303.3565)

# GST 3 population model



# GSF (Global Spline Fit)

“Data-driven”, no input model (H. Dembinski et al., 1711.11432)

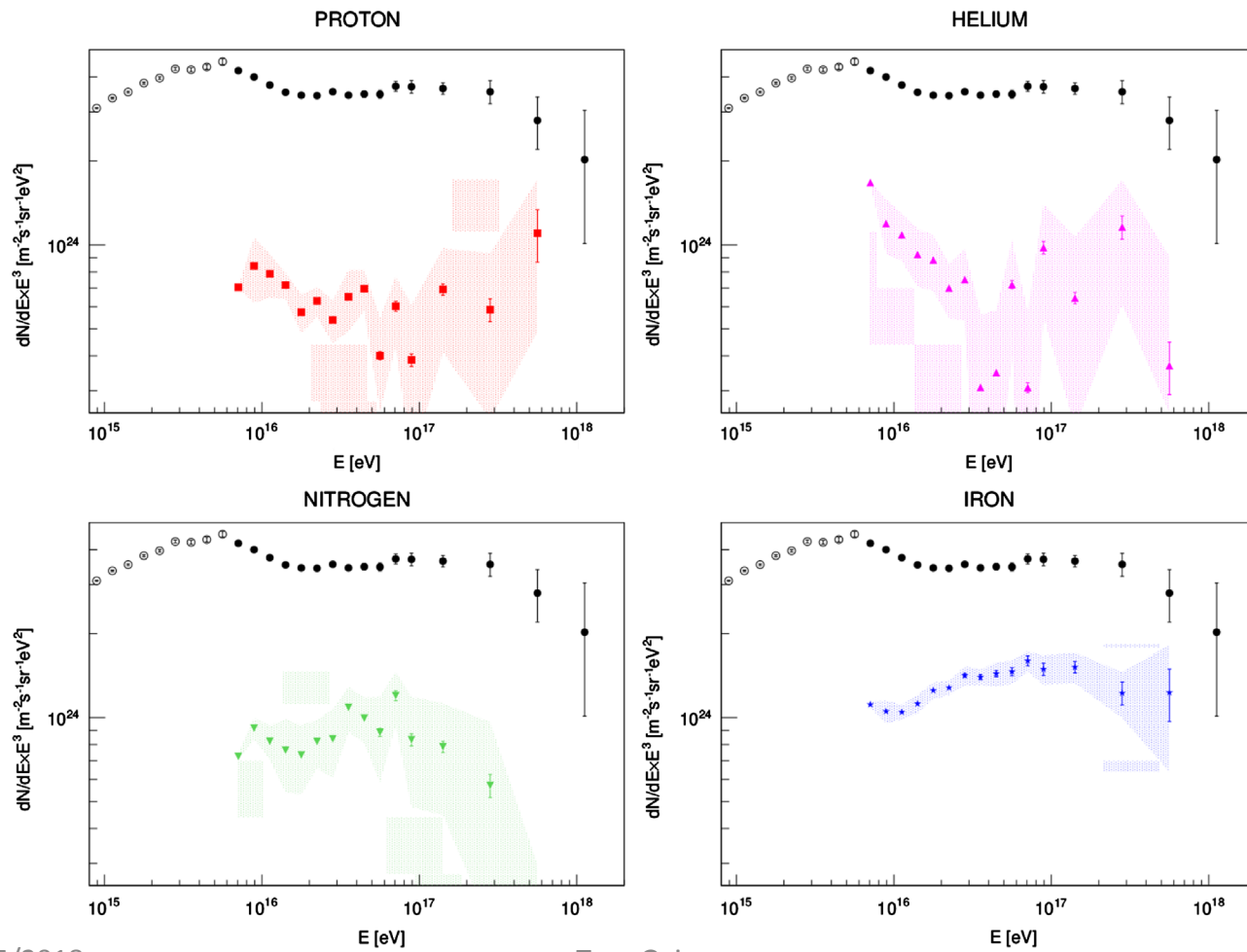




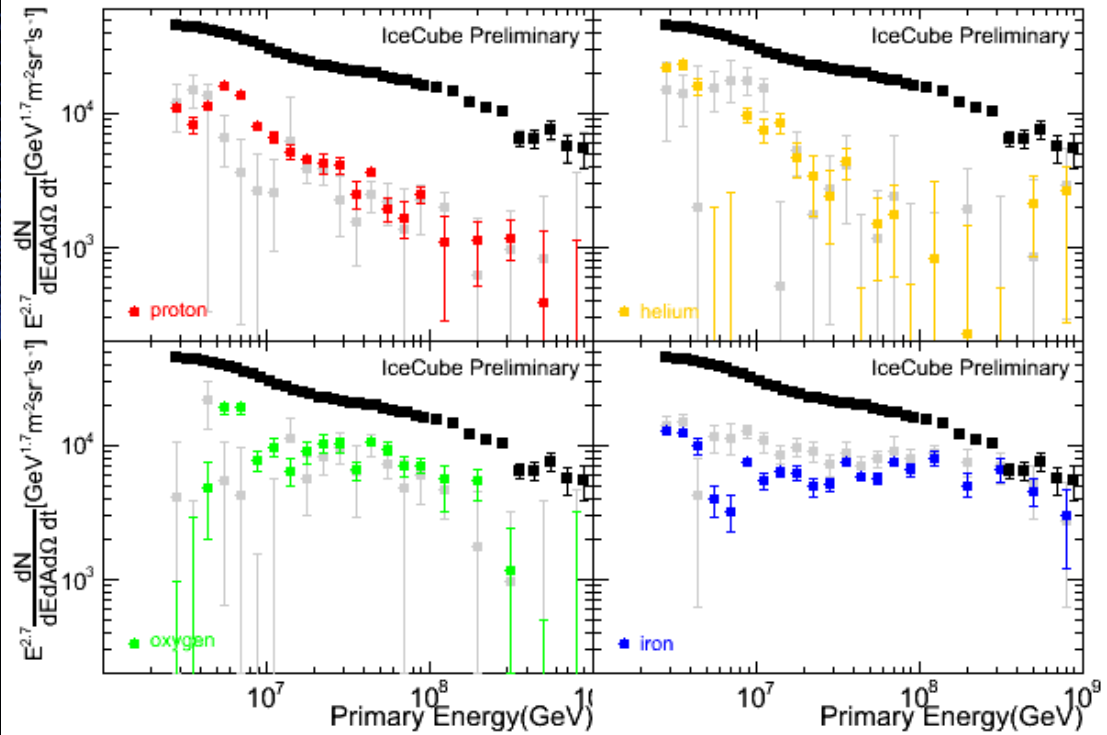
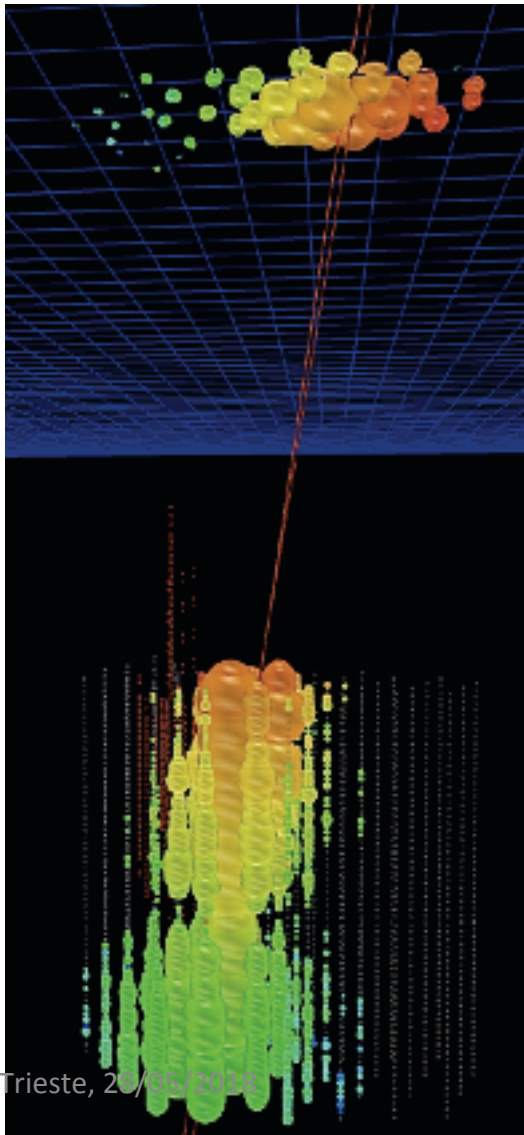
# TUNKA

V.V. Prosin et al. / Nuclear Instruments and Methods in Physics Research A 756 (2014) 94–101

99

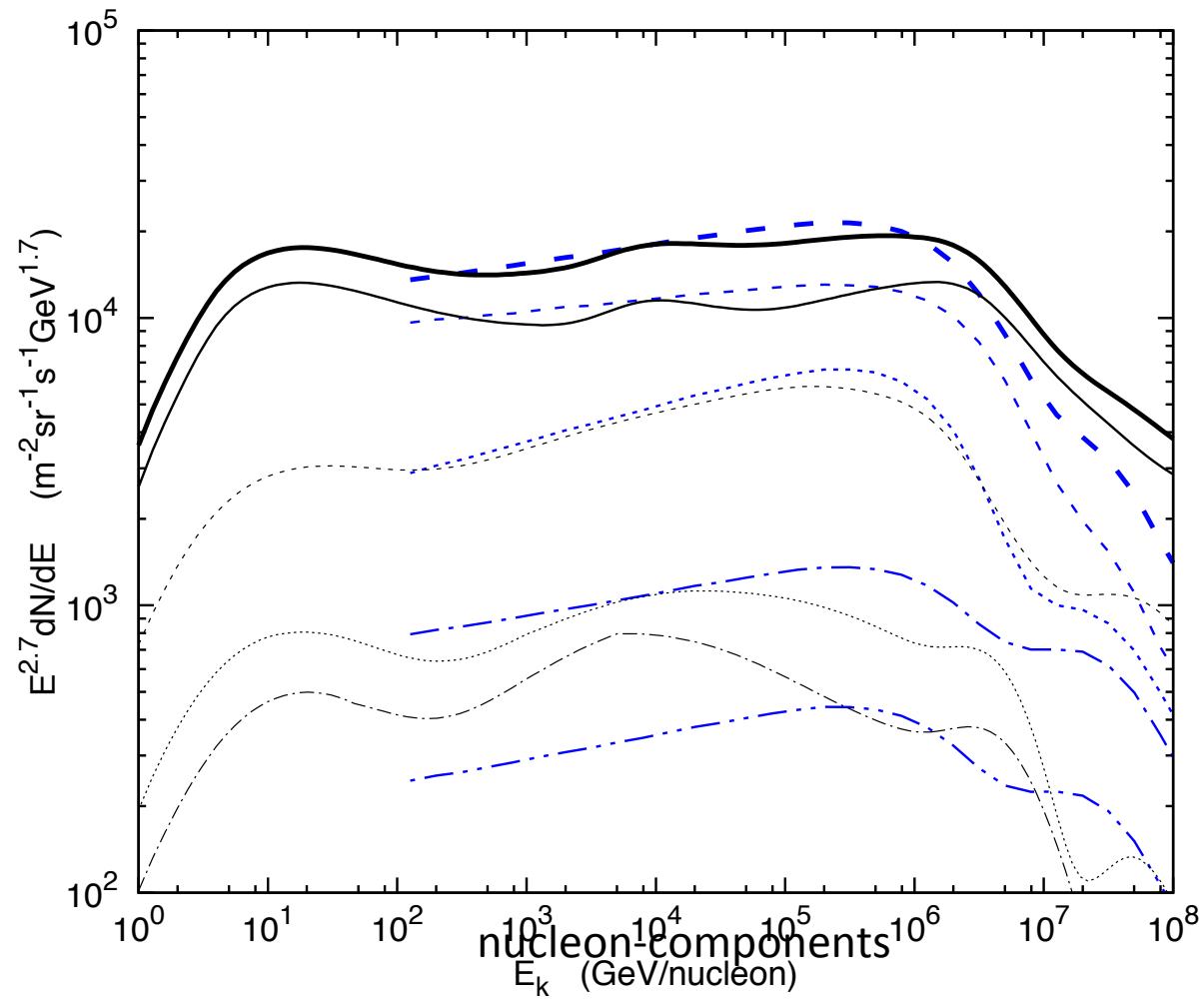


# IceCube/IceTop coincident events

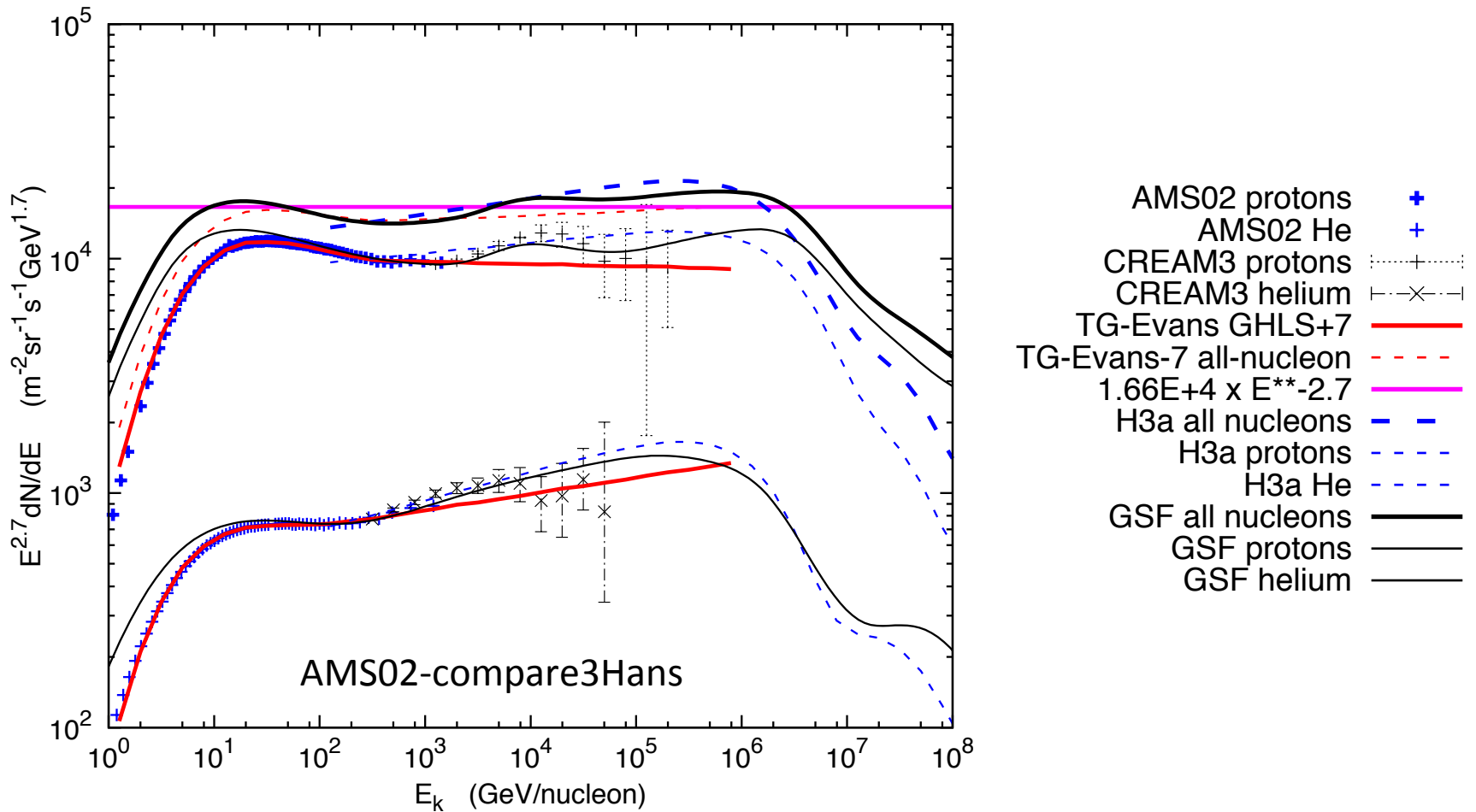


IceCube, ICRC 2015, arXiv:1510.05225

# Nucleon spectra: compare H3a, GSF

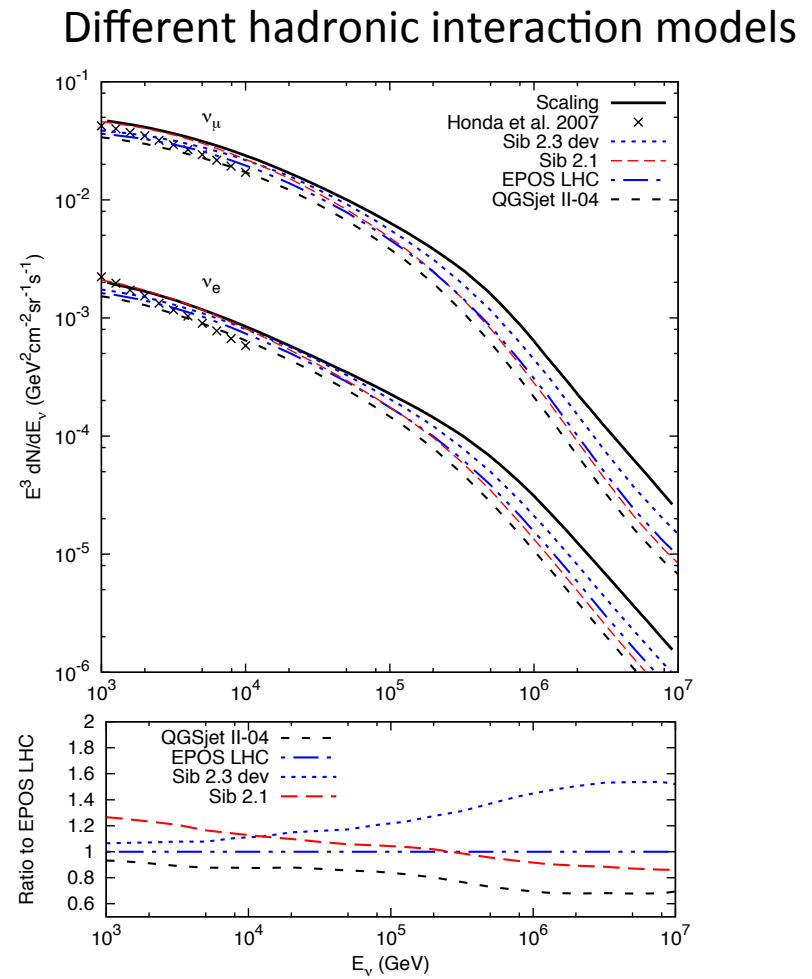
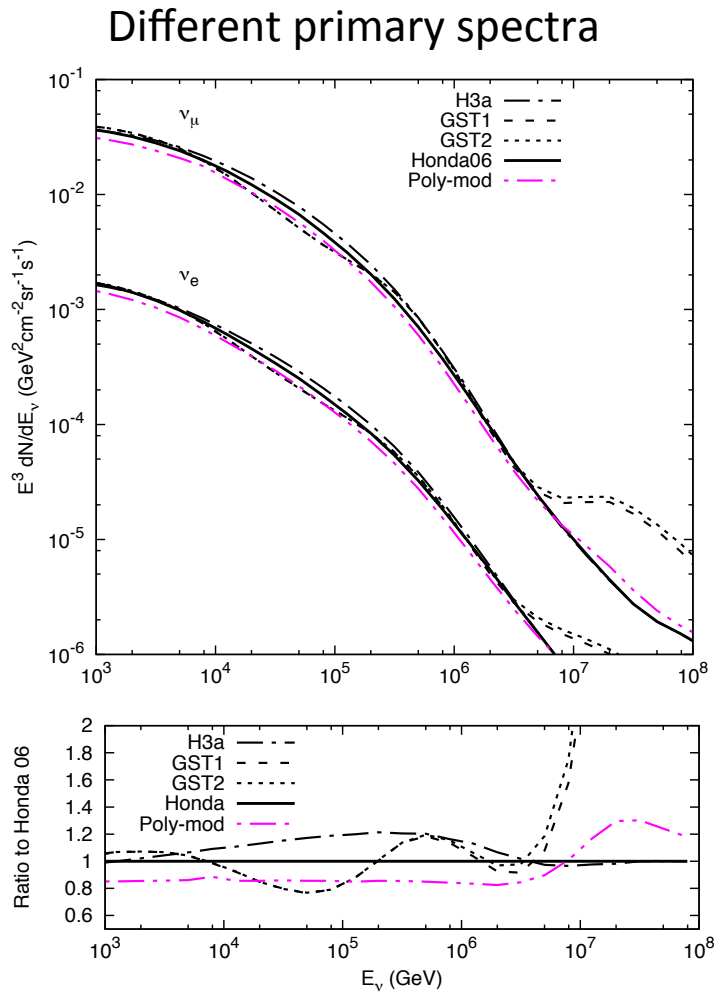


# Compare p and He (incl. data)

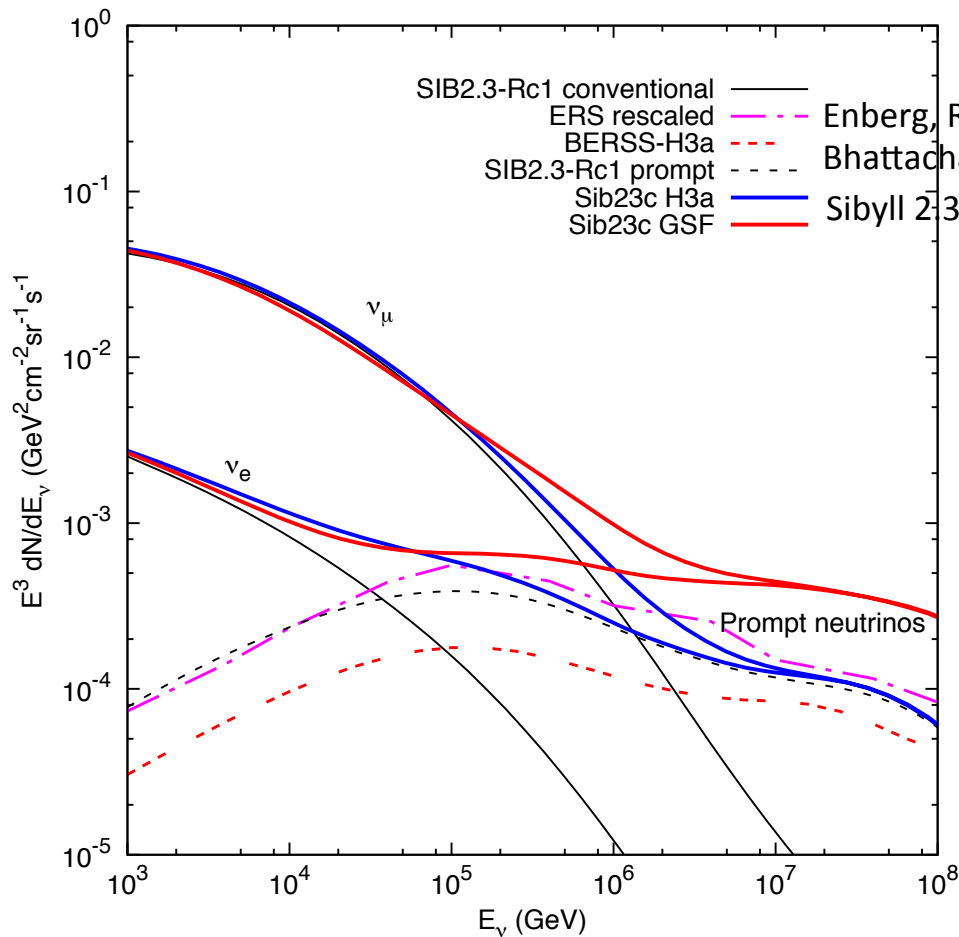


# Uncertainties in conventional $\nu$ fluxes:

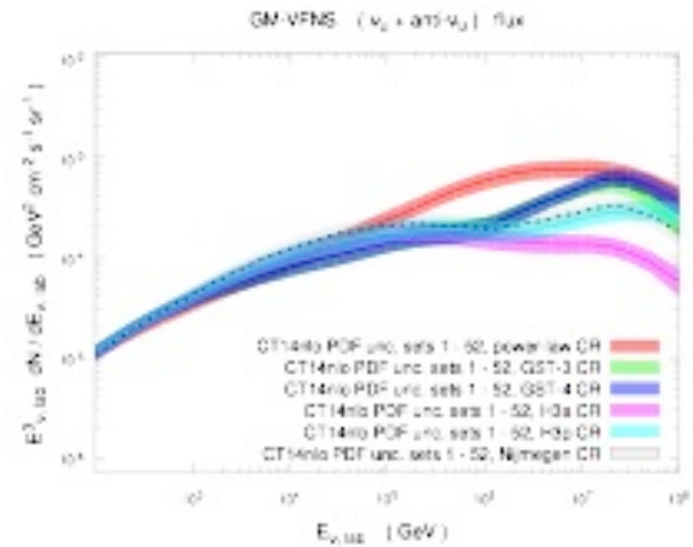
TG: 1605.03073



# Uncertainties in prompt $\nu$



Note lower crossover for electron neutrinos



Benzke Garzelli, et al., arXiv: 1705.10386