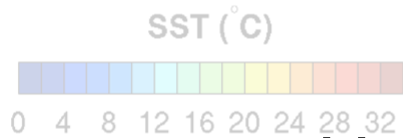


RidgeWorld

Using multiple equilibria to interpret paleoclimate



Sea-Ice thickness (m)

David Ferreira

University of Reading

Collaborators:

John Marshall (MIT)

Brian Rose (Albany)

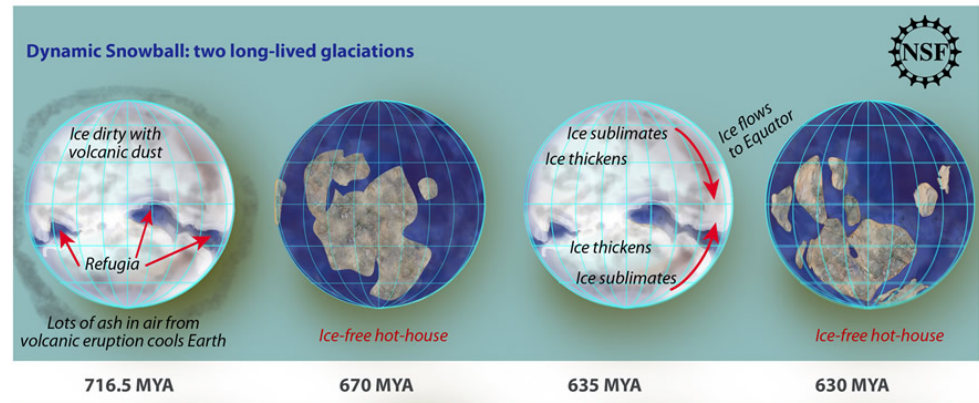
Taka Ito (Georgia Tech)

David McGee (MIT)

Outline

- Paleoclimate context
- Quick summary of multiple state dynamics
- Dynamics of transitions, link with DO events
- Glacial-interglacial states
- Stochastic resonance and GI cycles
- Bonus track

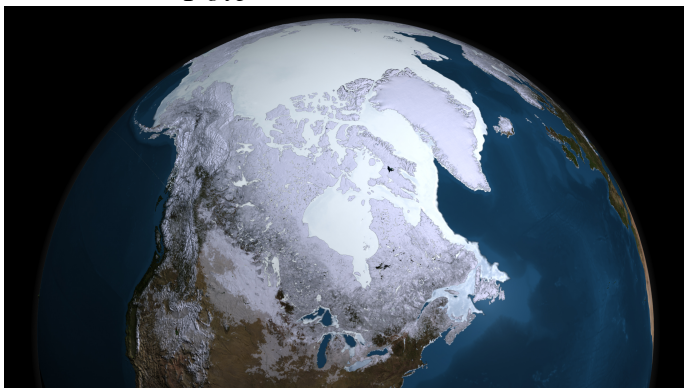
Geology and paleoproxies indicate Earth climate went through very different states



Neoproterozoic Snowball Earth

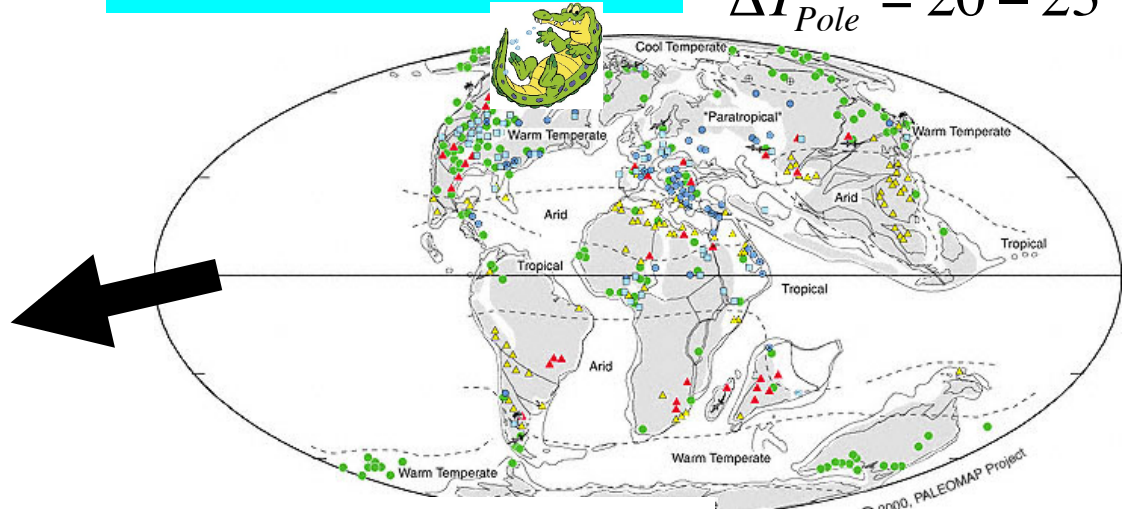
“Moderate” present-day

$$\Delta T_{Pole}^{Eq} = 30 - 35^{\circ}C$$



Ice-free Cretaceous

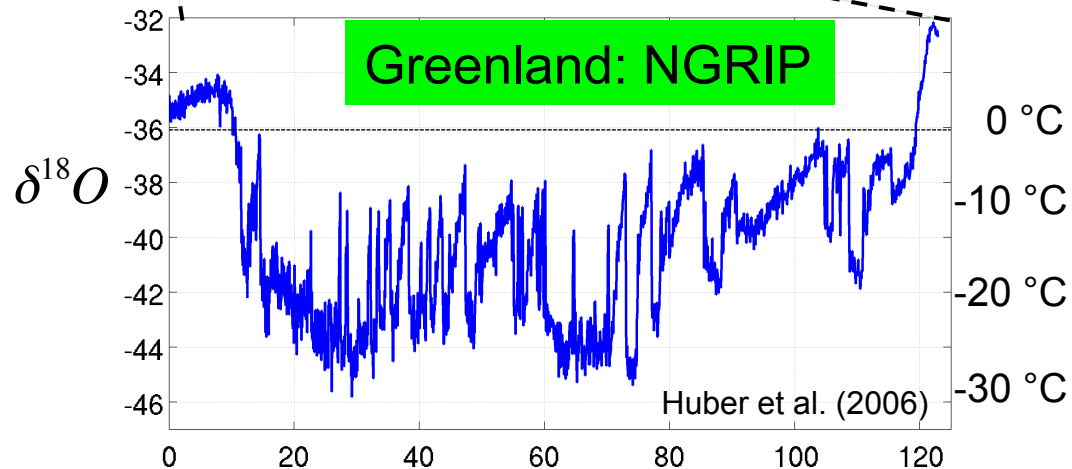
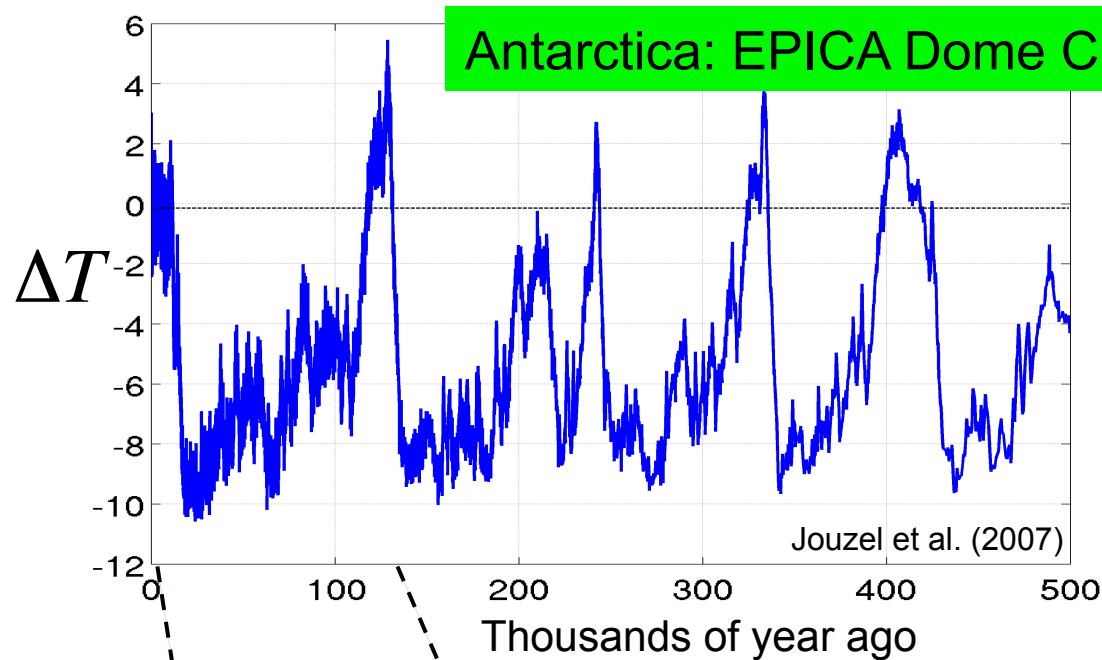
$$\Delta T_{Pole}^{Eq} = 20 - 23^{\circ}C$$



$$T_{Deep} = 10 - 13^{\circ}C_{ous}$$

© 2000, PALEOMAP Project

Glacial-Interglacial cycles



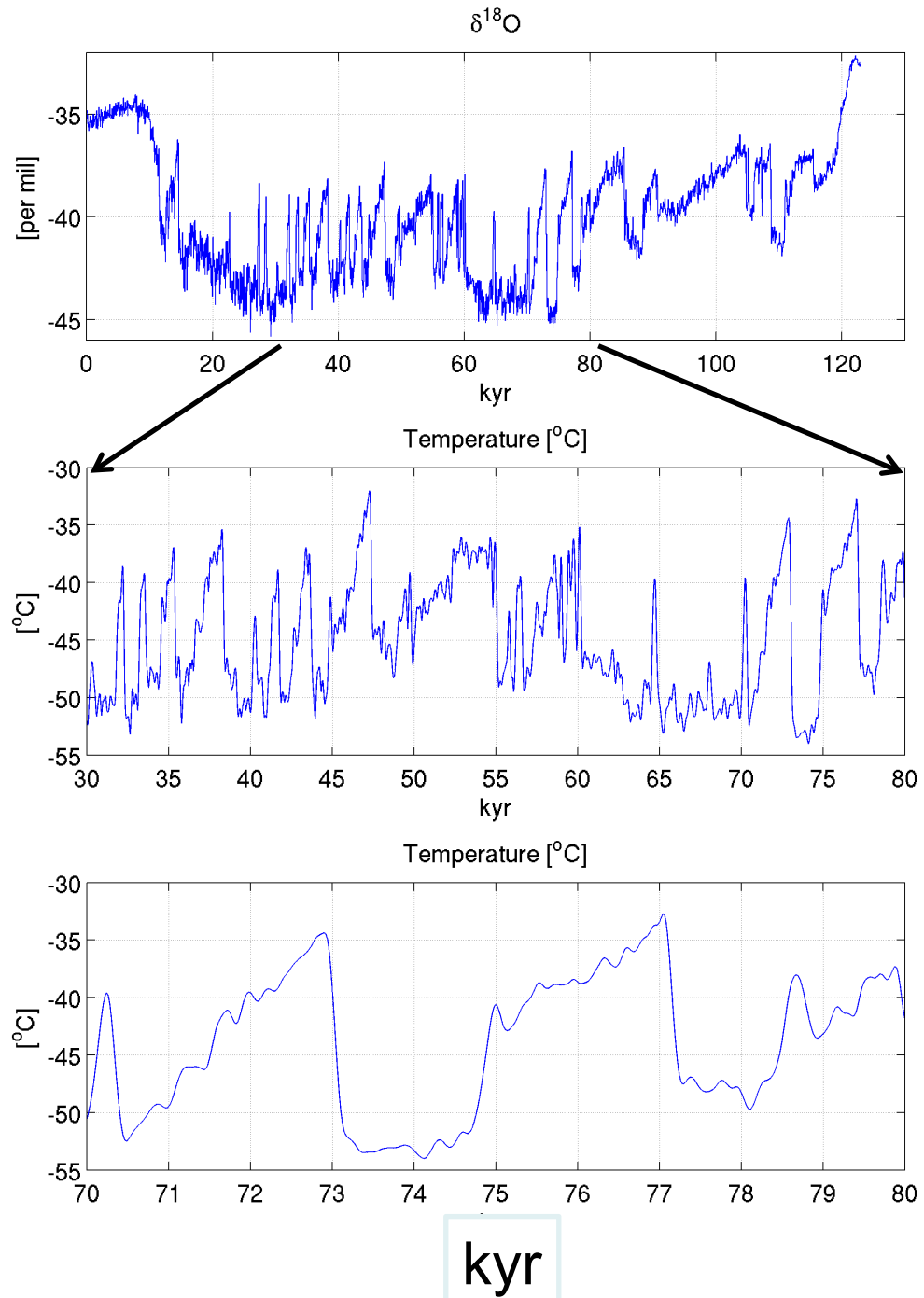
- Massive global climate shifts
→ large ice sheets over Canada/US and Scandinavia (~120 m sea level drop)
→ a few deg. global cooling
- Missing link between forcing (Milankovitch cycles?) and climate response

Millennial timescale fluctuations

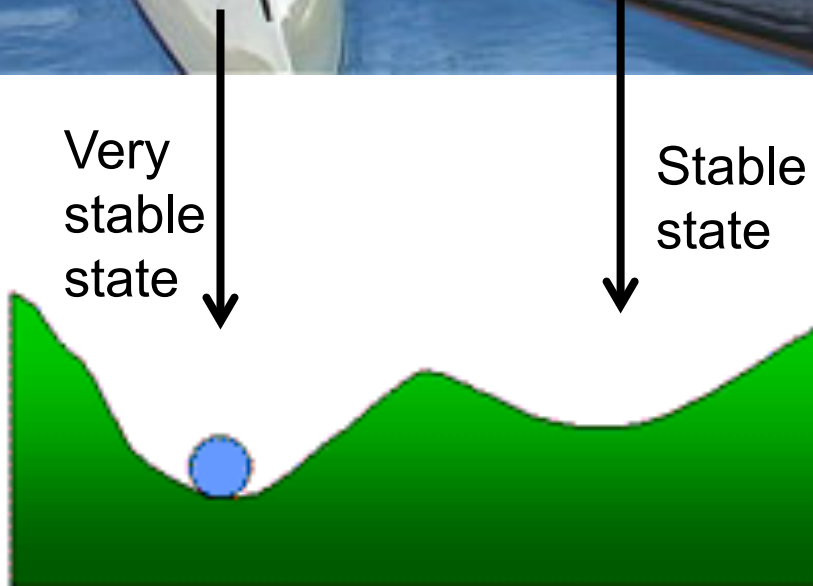
- @ Greenland: amplitude ~ Glacial-Interglacial
- Larger in North Atlantic

Dansgaard-Oeschger events (DO events)

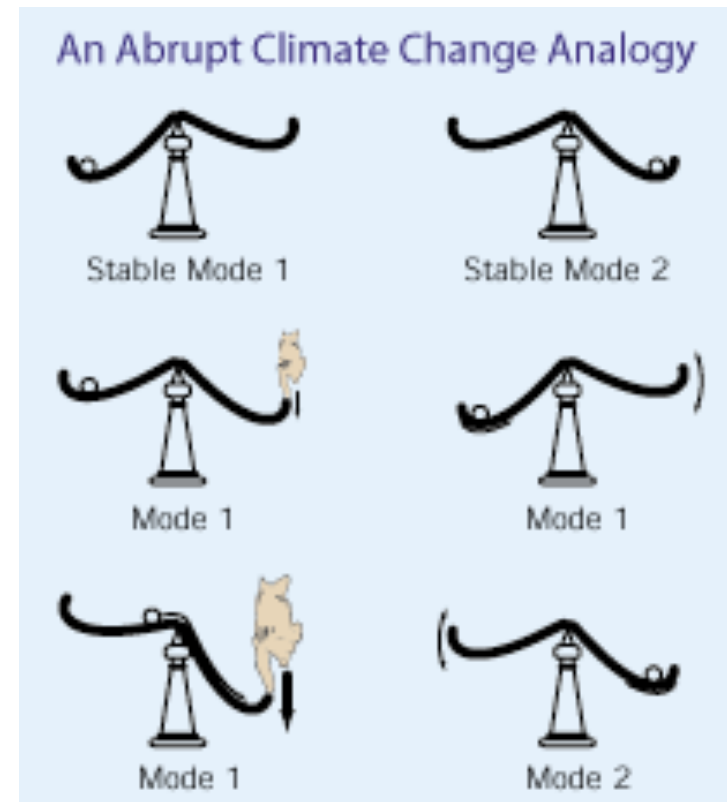
Greenland ice core
record



Multiple equilibrium states and abrupt changes



A small forcing may trigger a large/abrupt change:



Can multiple equilibria play a role in Earth's climate history?

→ There have been many studies in this direction: Benzi et al. (1982) and Paillard (1998), Saltzman et al., Gildor and Tzipermann et al., etc.

Problem: multiple equilibria are commonly found in simple models, but not always/not easily found in complex coupled climate models.

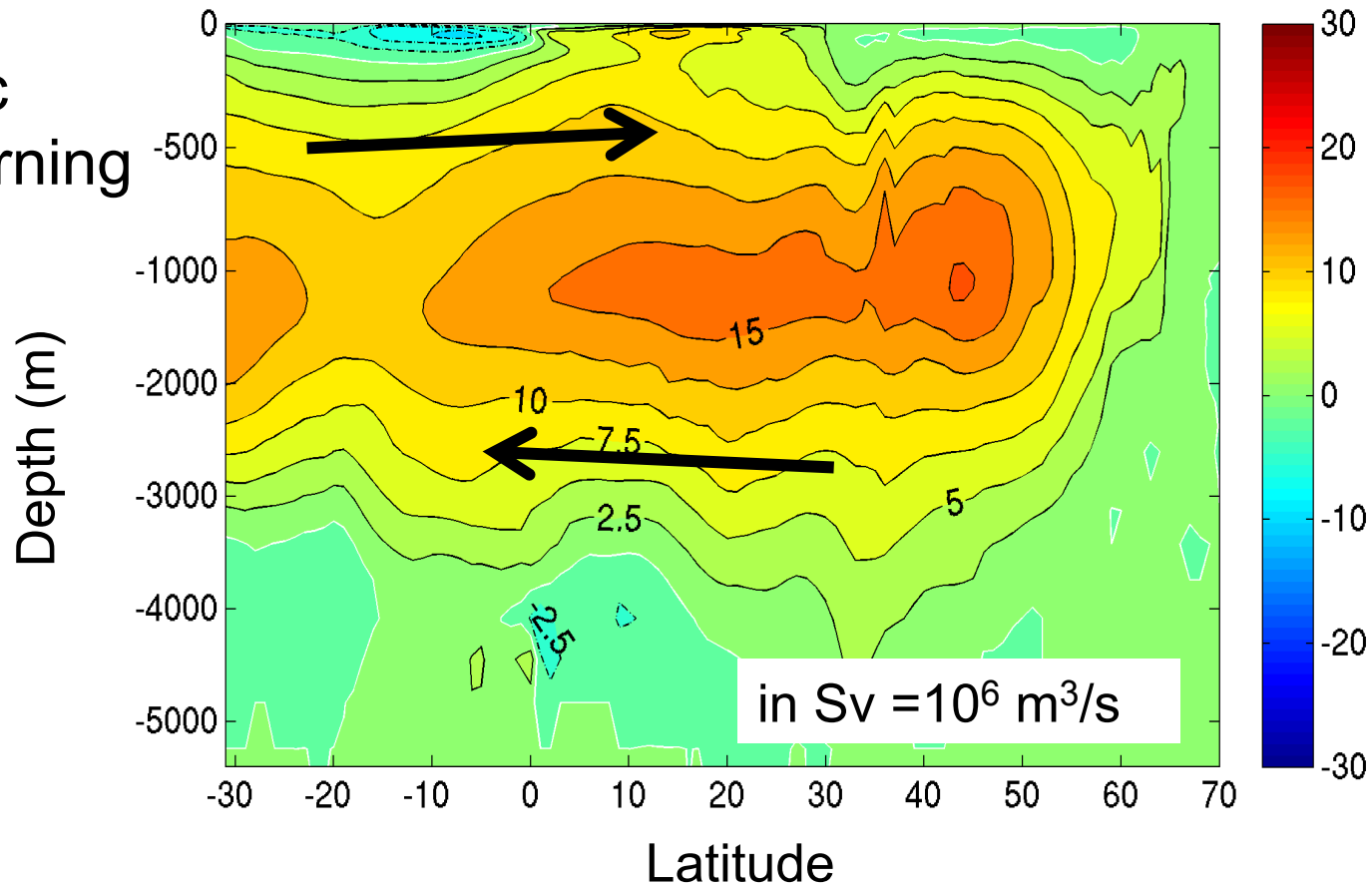
→ simple/low order models: (semi-)analytical models

→ GCMs: from intermediate complexity (e.g. zonally averaged models to state-of-the-art IPCC class models)

Multiple equilibrium states in low-order models

1 Multiple states of the Meridional Overturning Circulation

Atlantic
Overturning



See Ferreira et al. (2018) for why there isn't a Pacific equivalent

OCCA Ocean state estimate (Forget, 2009)

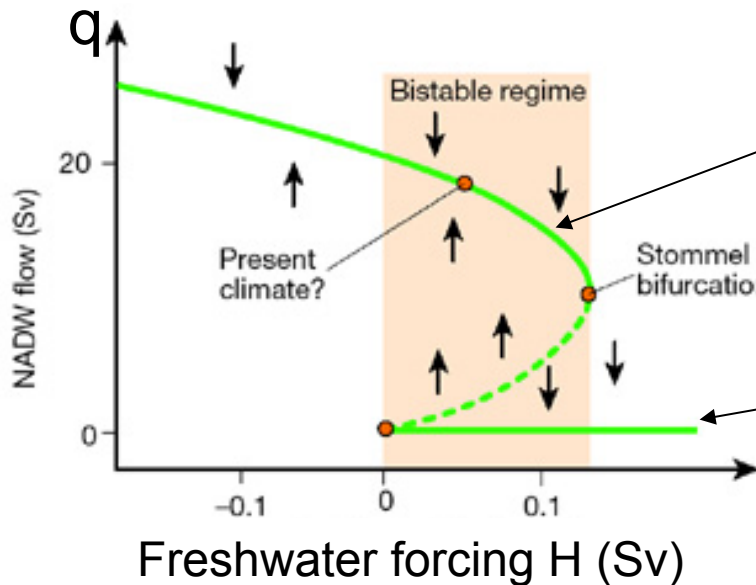
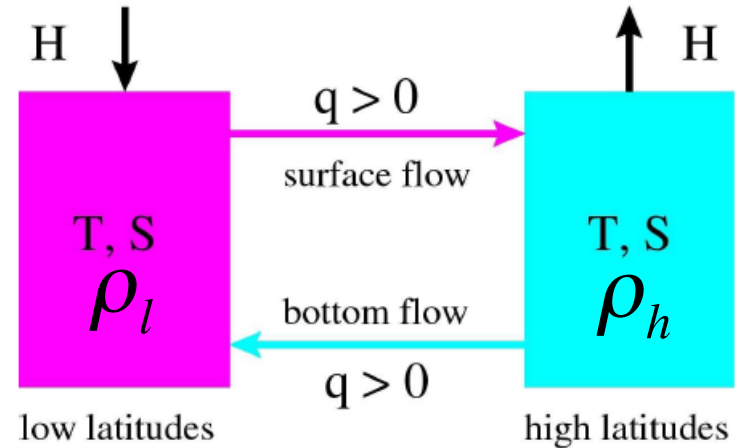
Multiple equilibrium states in low-order models, II

1 Multiple states of the Meridional Overturning Circulation Stommel (1961)

Density-driven flow

$$q = k(\rho_h - \rho_l)$$

$$\rightarrow |q|(1 - q) - H = 0$$



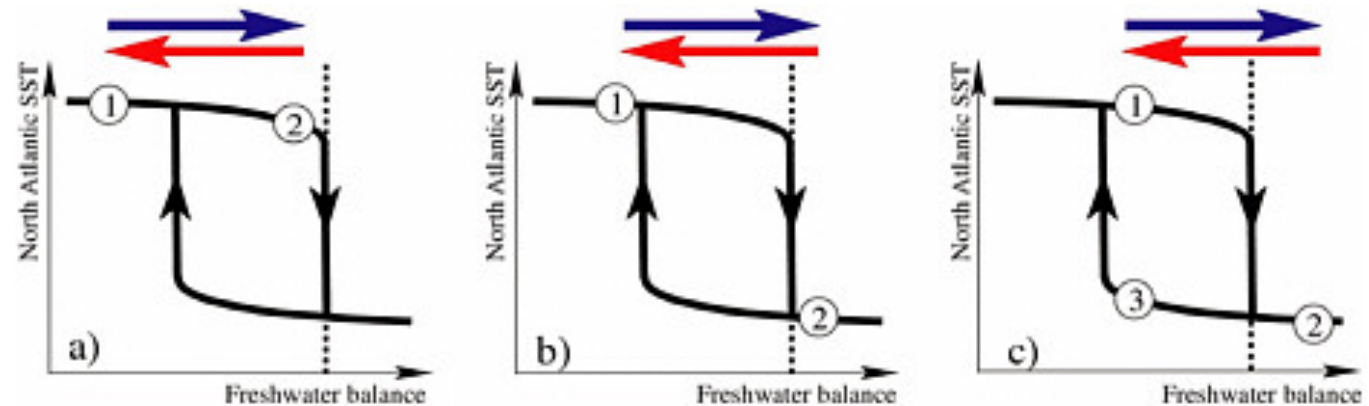
“On” branch: thermal mode

“Off” branch: haline mode

Rahmstorf (2002)

Multiple equilibrium states in low-order models

1 Multiple states of the Meridional Overturning Circulation

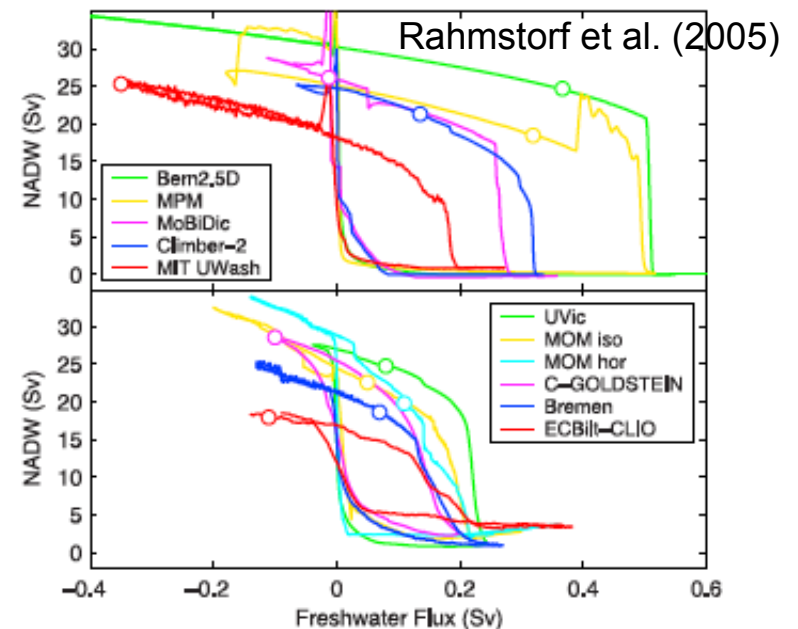


→ Widely used to interpret past abrupt changes (Broecker et al. 1985, Knutti et al, 2004)

→ Easy to find in coupled GCMs of intermediate complexity (Water-hosing experiment,)

→ Less obvious in IPCC-class GCMs (but, see Mecking et al. 2016)

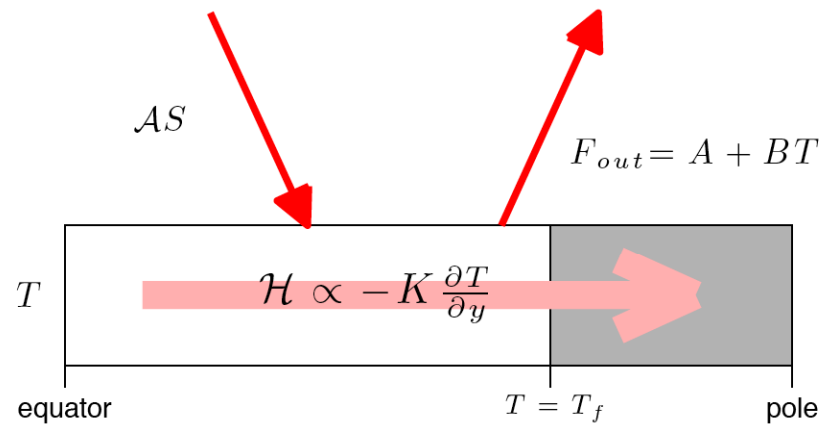
→ Freshwater forcing difficult to reconcile with estimates from paleoproxies (~ 0.1 Sv)



Multiple equilibrium states in low-order models

2

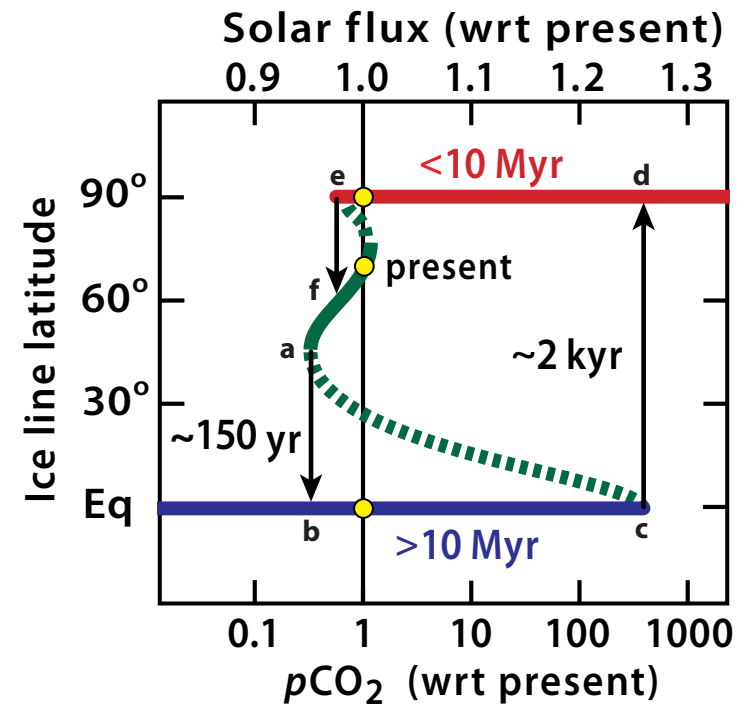
Sea ice-albedo feedback: Budyko-Sellers Energy Balanced Model (EBM)



Simple Energy Balance Model

Rose and Marshall (2009)

Hoffman et al. (2017)

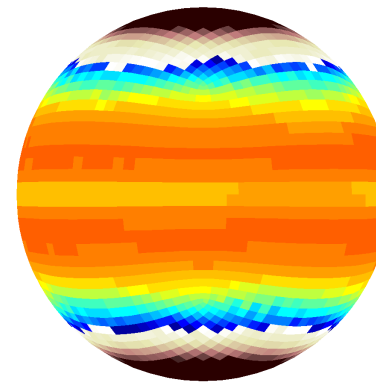
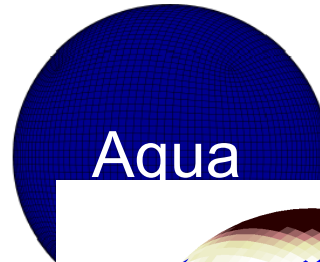
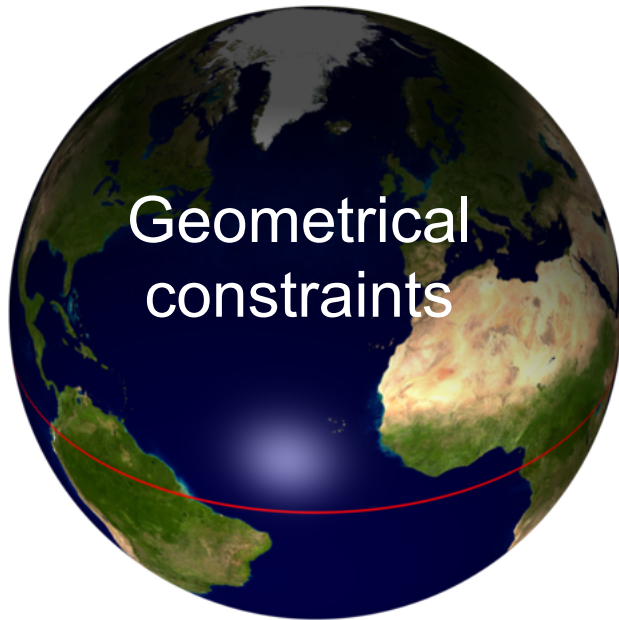


Few examples in GCMs:

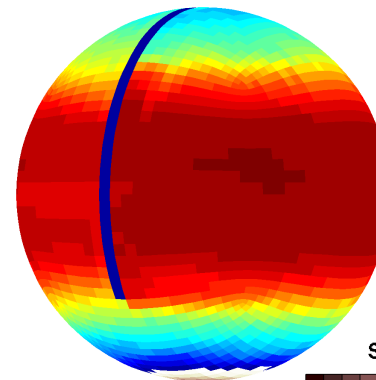
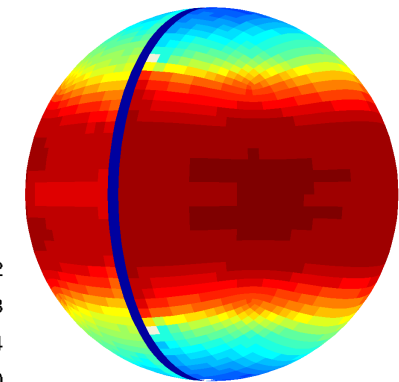
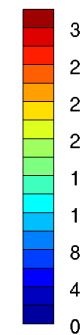
- Langen and Alexev (2004): atmosphere only GMC
- Marotzke and Bozet (2006): a warm state and a Snowball state

Modeling approach

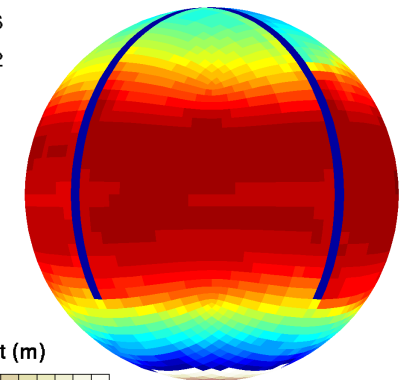
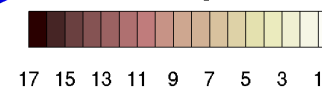
MIT GCM: Ocean-
Atmosphere-Sea ice:



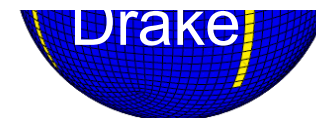
SST (°C)



Sea-Ice height (m)



How much can we explain
with dynamics and simple
geometries ?



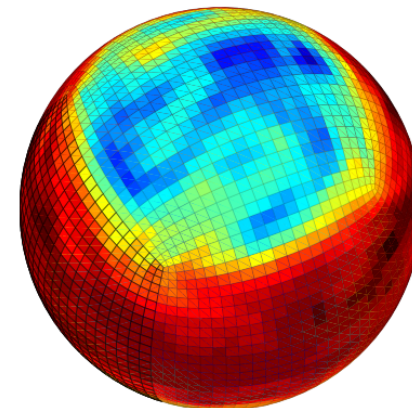
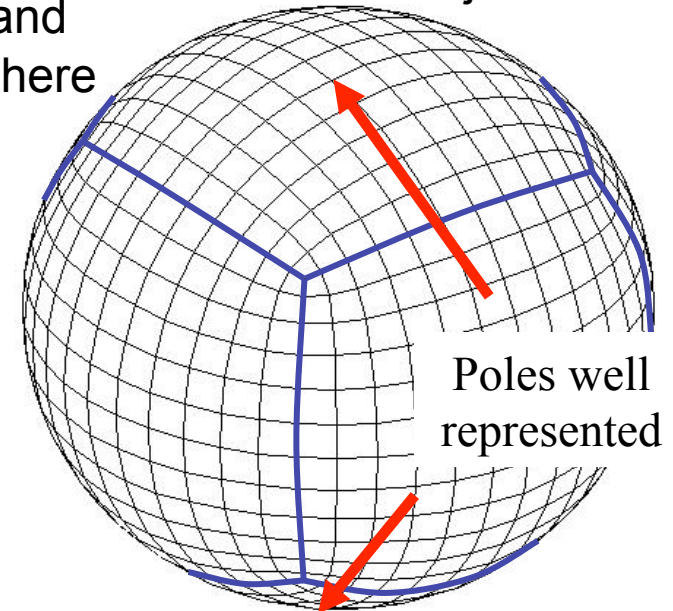
MIT GCM: Coupled Ocean-Atmosphere-Sea ice:

- Primitive equation models,
- Cube-sphere grid: $\sim 3.75^\circ$,
- Synoptic scale eddies in the atmosphere,
- Gent and McWilliams eddy parameterization in the ocean,
- Simplified atmospheric physics (SPEEDY, Molteni 2003),
- Conservation to numerical precision (Campin et al. 2008)

Model complexity: Big step compare to EBM models

Same grid for ocean and atmosphere

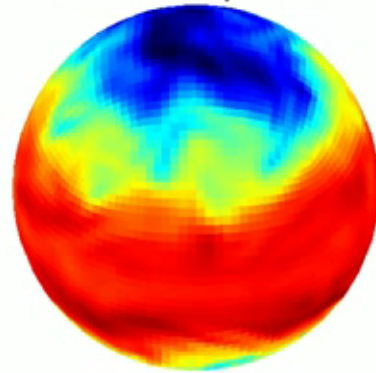
Fully coupled: no adjustments



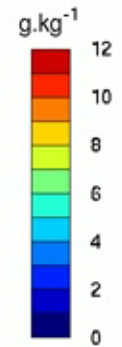
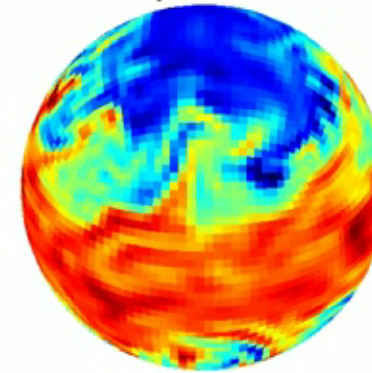
Temperature snap-shot at 500 mb.

Idealized geometries but complex dynamics

500 mb Temperature

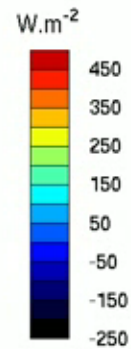
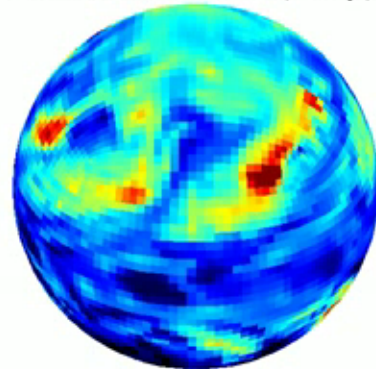


Surface Specific Humidity

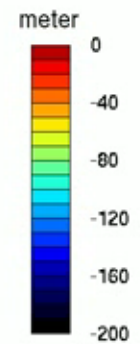
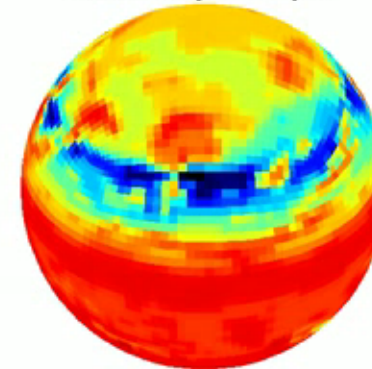


Day 1

Air-sea Heat Flux (+ = up)

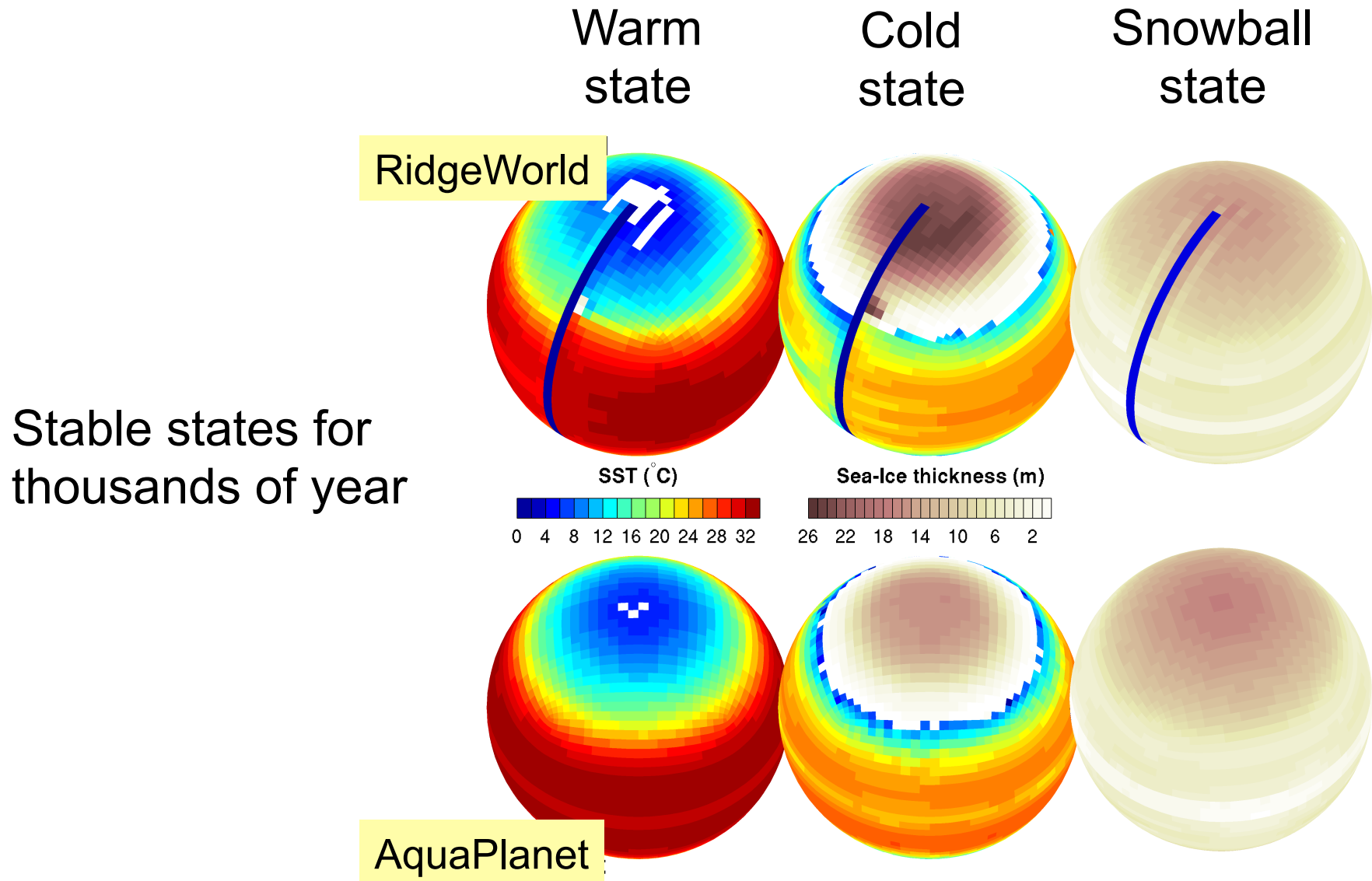


Mixed-layer Depth



→ Not a low order model

Starting with highly idealized configurations

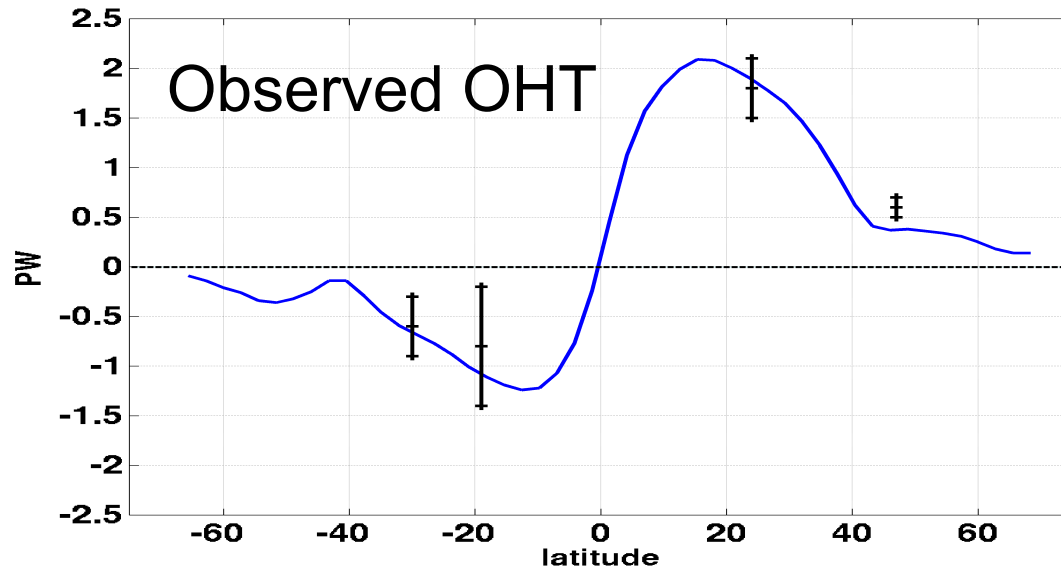


Ferreira et al. 2011

$$\Delta T_{Pole}^{Eq} = 28^{\circ}C \quad \Delta T_{Pole}^{Eq} = 55^{\circ}C$$

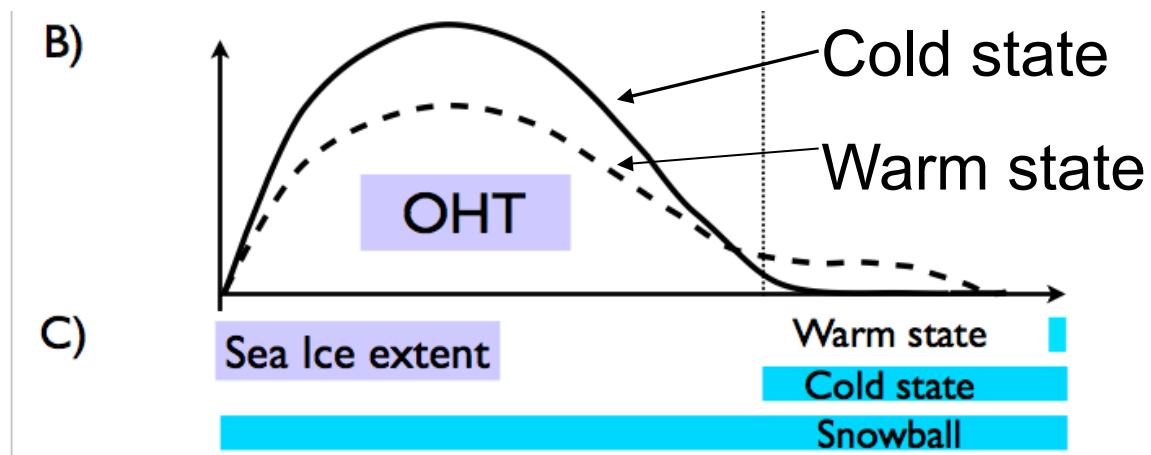
How are the multiple states maintained ?

It's the shape of the OHT !



Cold State: OHT convergence arrests sea-ice expansion

Warm State: OHT heats the poles remotely through enhanced mid-latitudes convection and greenhouse effect



Ocean-Atmosphere EBM

Key differences with the “classical” EBM (Rose and Marshall, 2009):

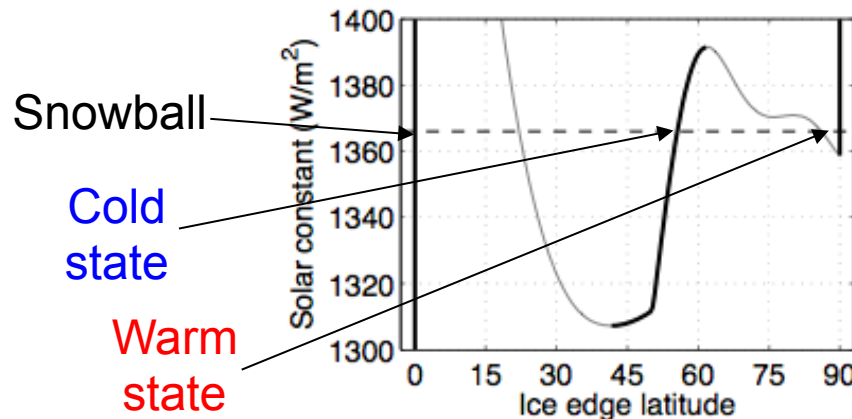
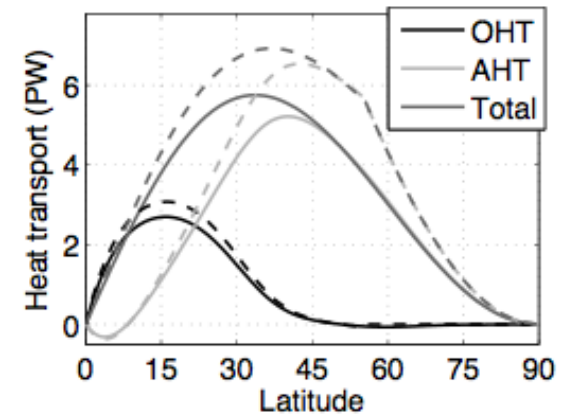
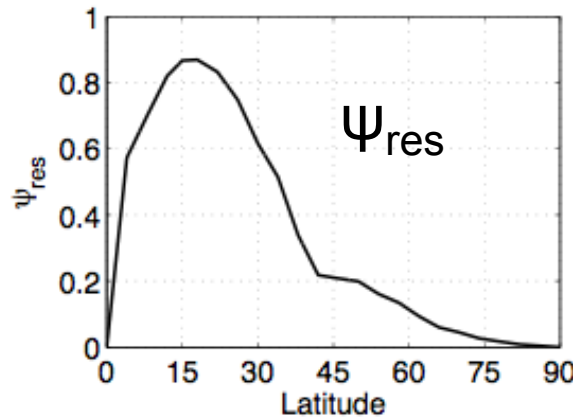
- A coupled ocean-atmosphere EBM,
- OHT has a meridional structure,
- sea ice insulates the ocean.

$$C_a \frac{\partial T_a}{\partial t} = D_y \left(C_a K_a \frac{\partial T}{\partial y} \right) + F_{up} - F_{out}$$

$$C_o \frac{\partial T_o}{\partial t} = D_y (H_o) - F_{up} + \Lambda \times S$$

OHT not diffusive but linked to (effective) MOC:

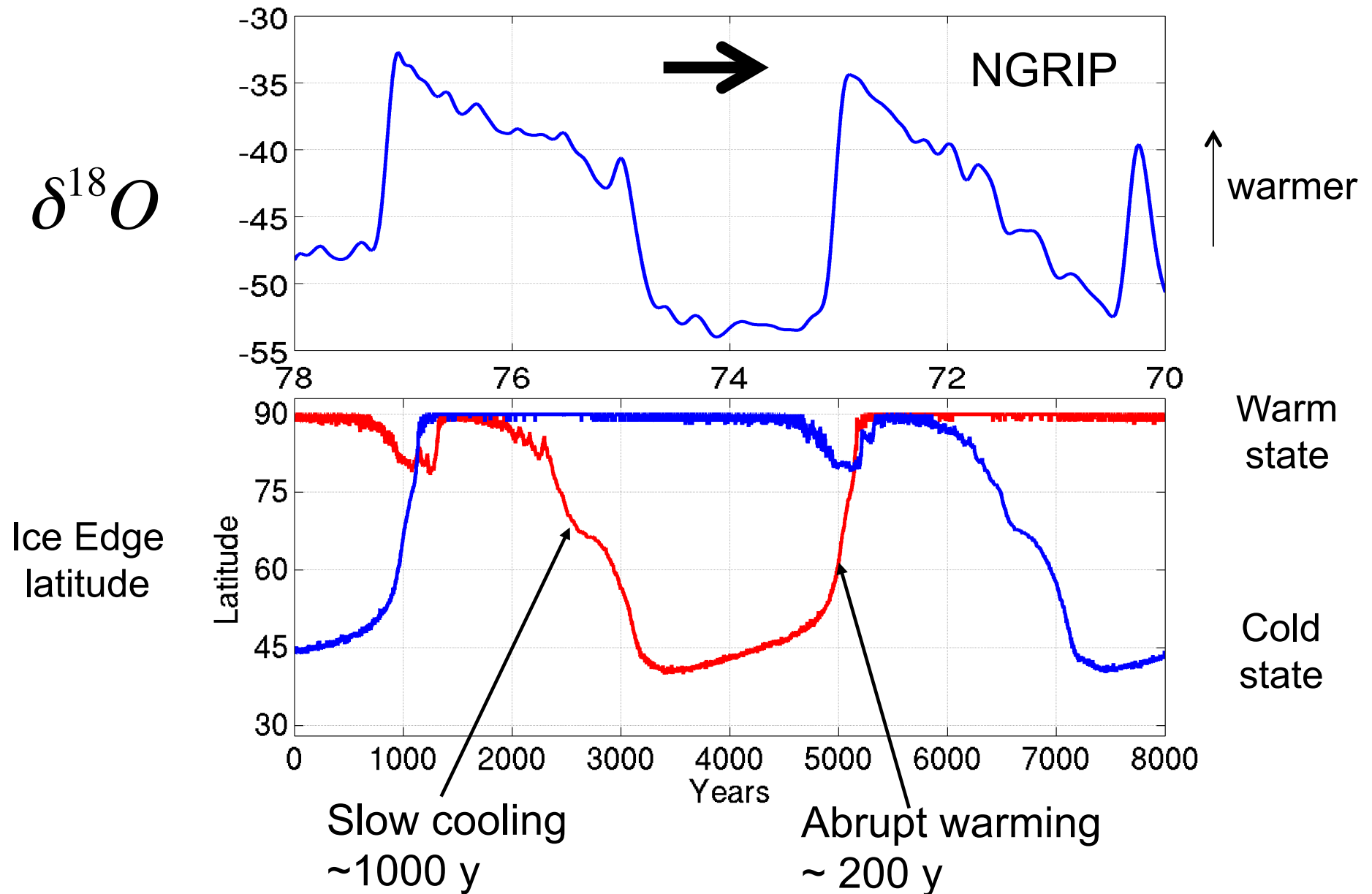
$$H_o \propto \psi_{res} \left(\frac{T_s - T_{deep}}{\Delta z} \right)$$



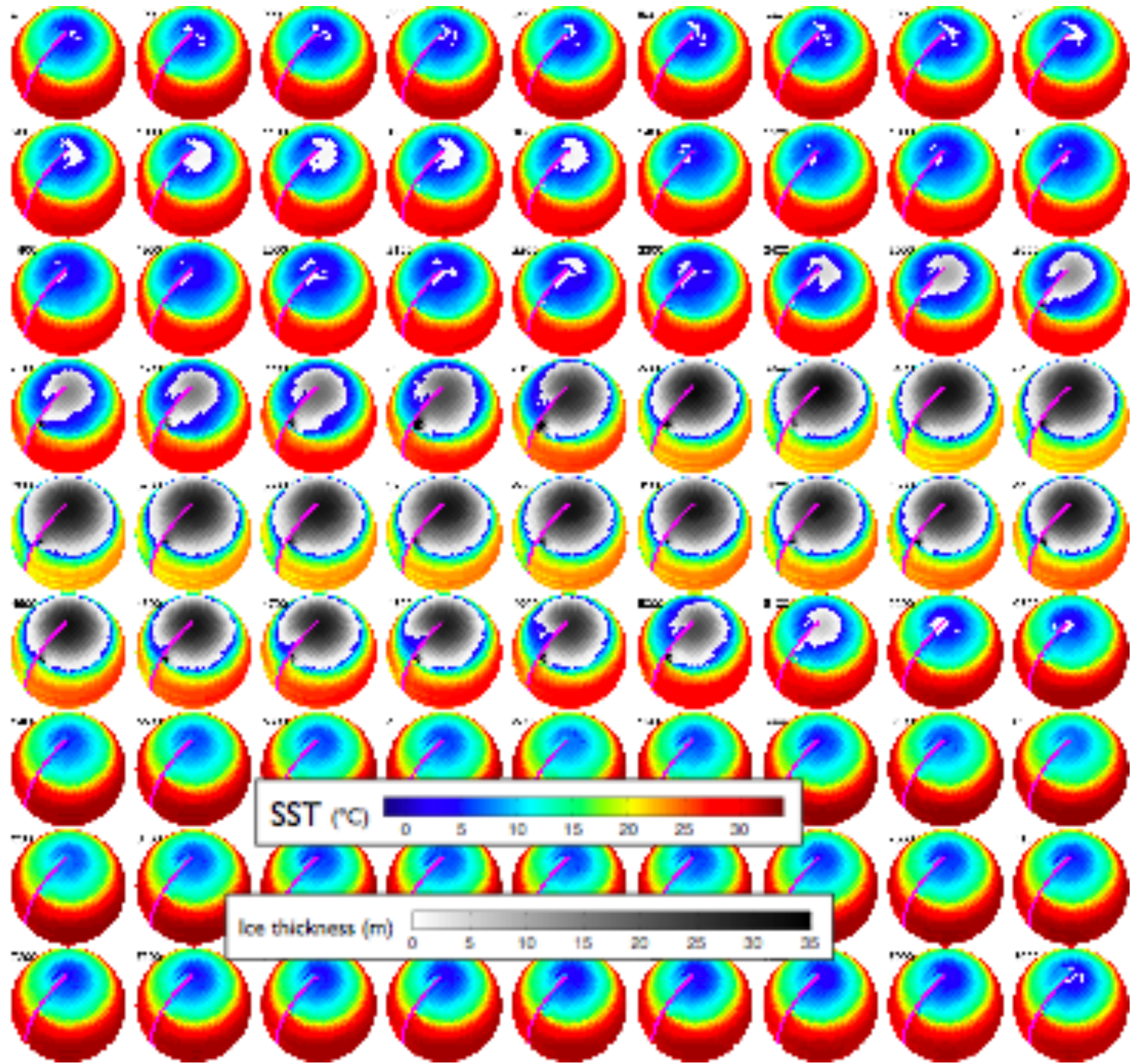
Transition between states

RidgeWorld

Rose et al. 2012



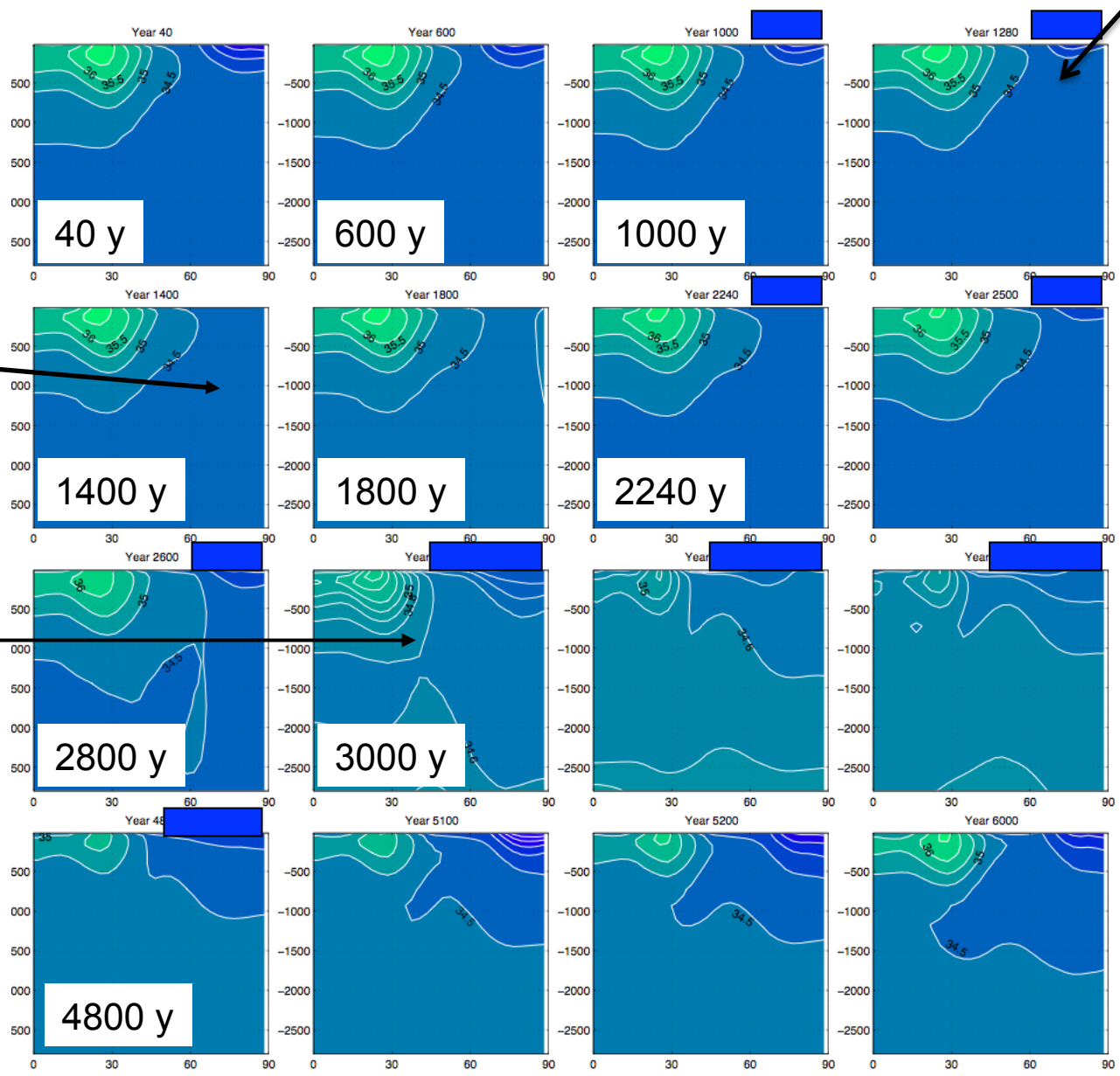
SST and
Sea ice



Evolution of Salt

Ice grows
Brine rejection

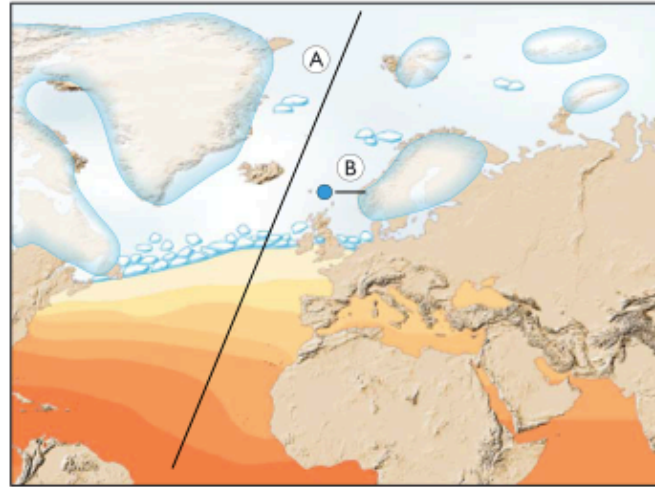
Start from
Warm State



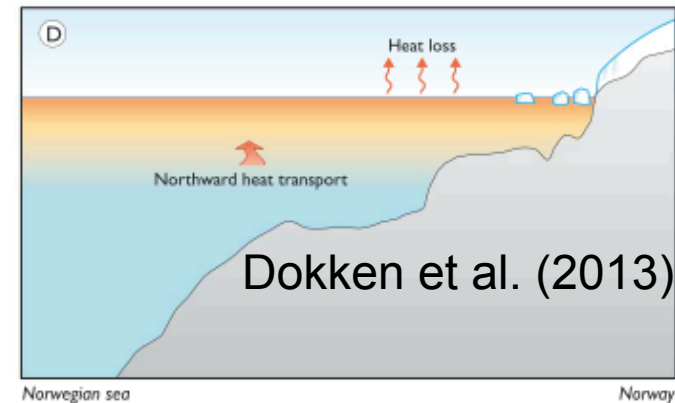
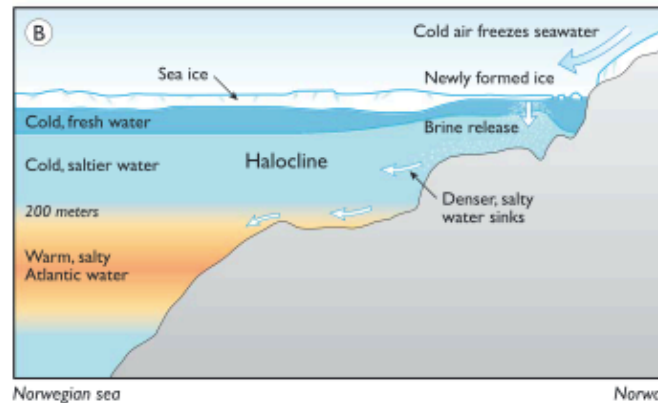
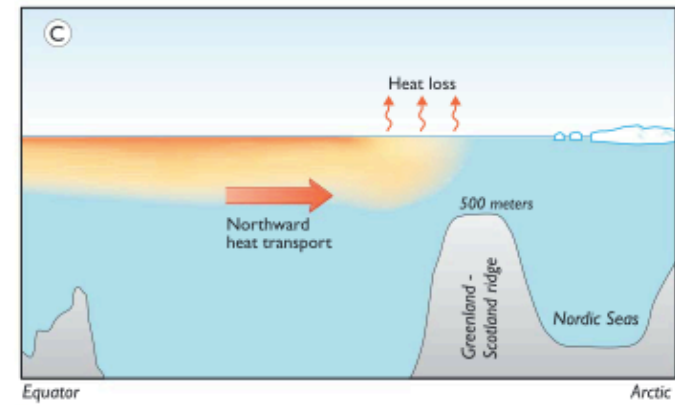
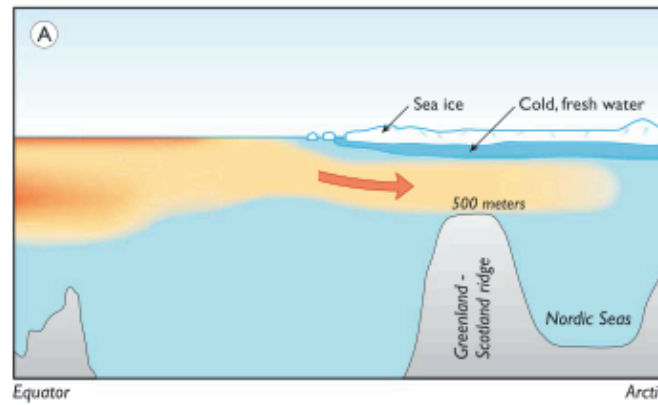
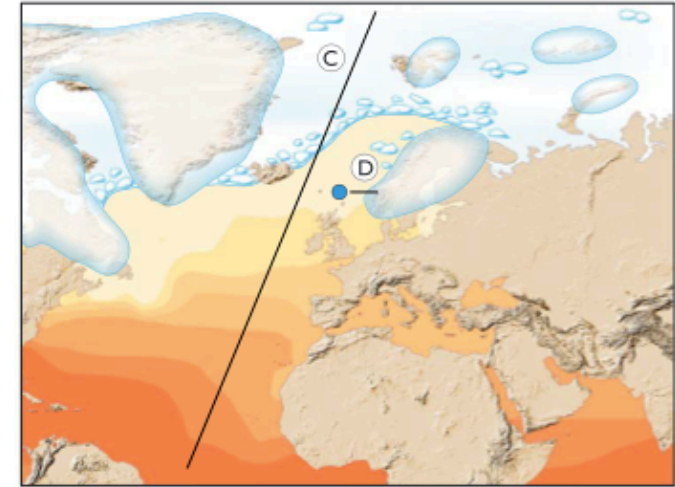
Scenario from paleoproxies

- Suggest an ocean/sea ice instability
- Does rely on AMOC on/off behavior

Stadial conditions



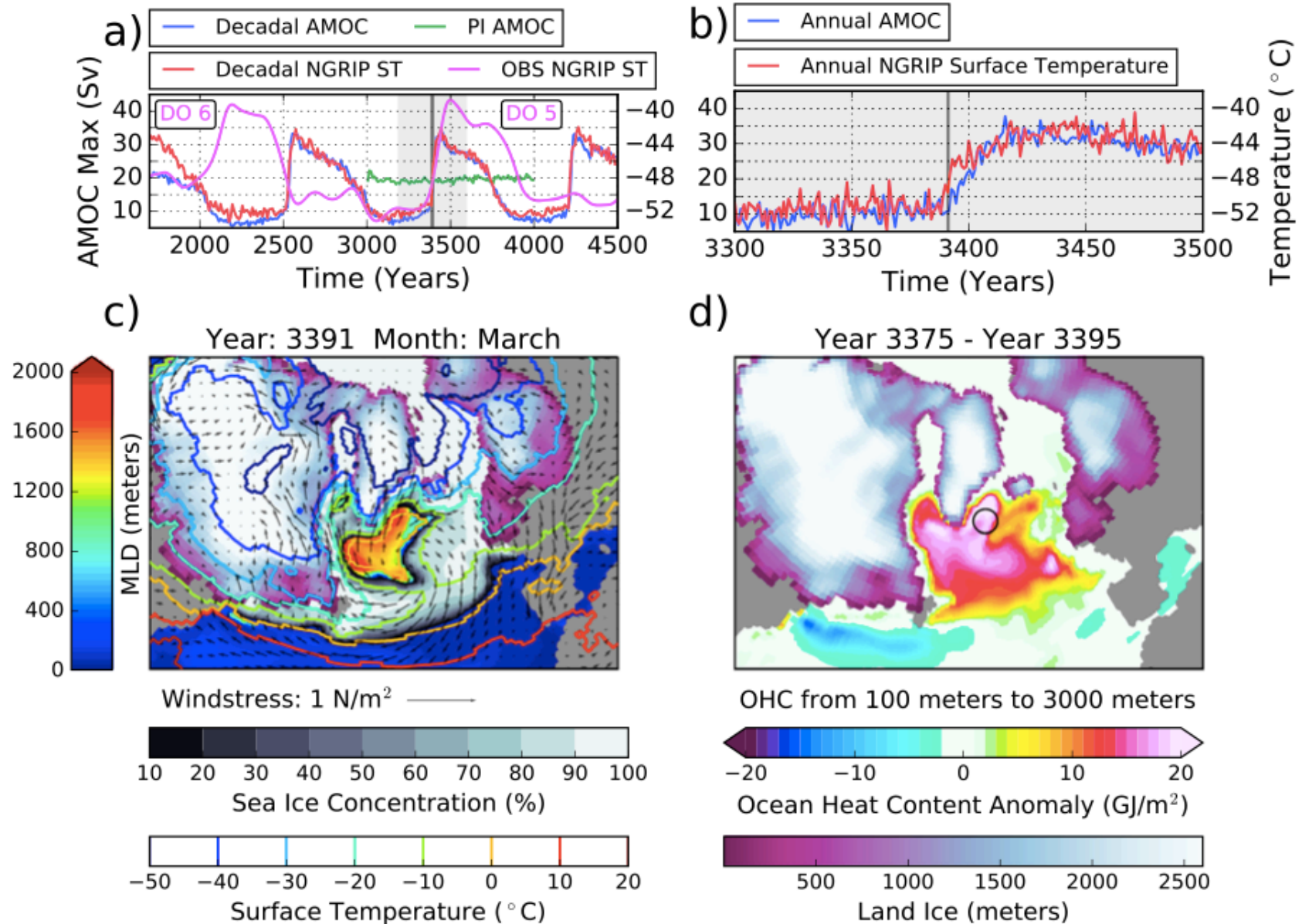
Interstadial conditions



Dokken et al. (2013)

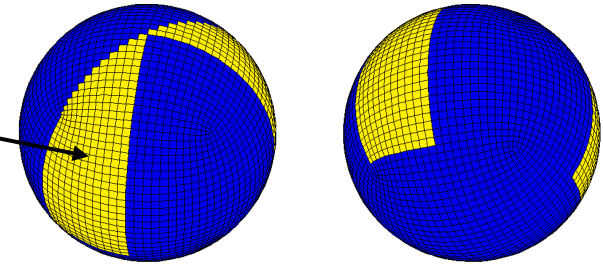
Self-sustained oscillations of ocean/sea ice system

Vettoreti and Peltier (2016)

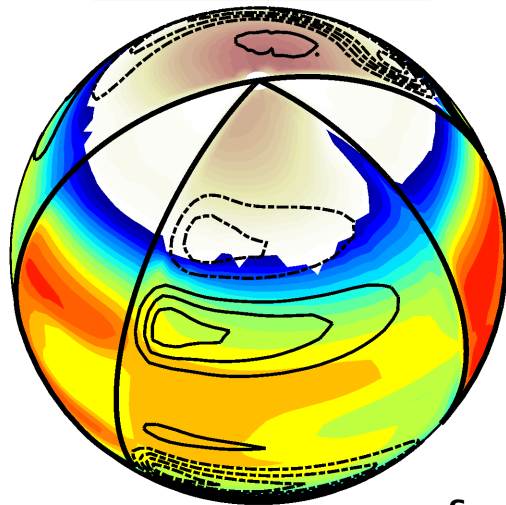


Boomerang

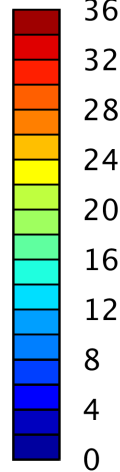
Continents



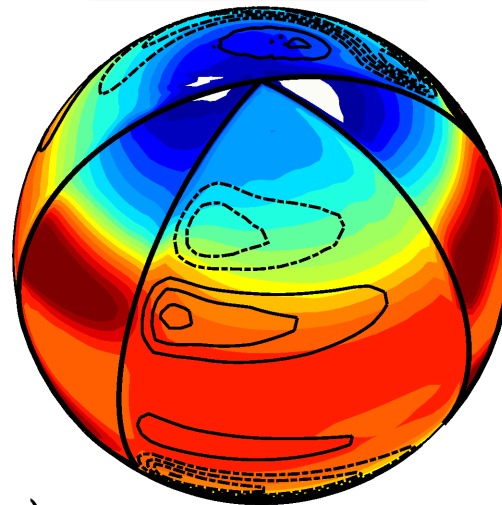
Cold state



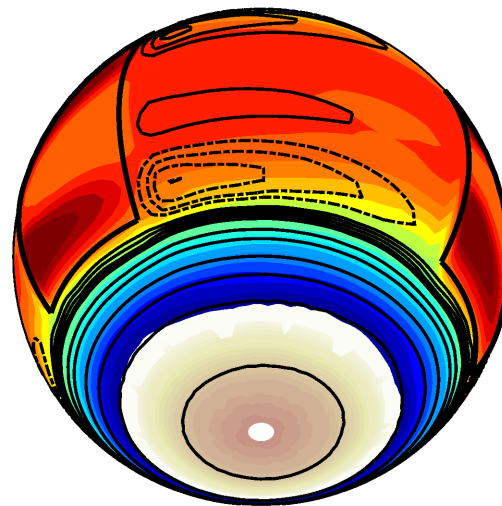
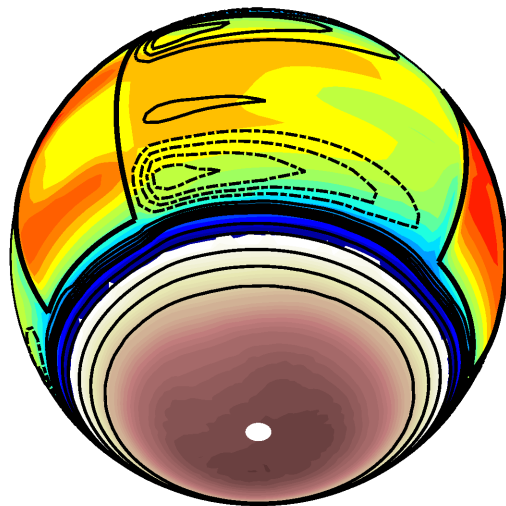
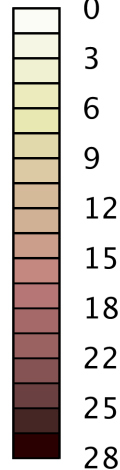
SST (°C)



Warm state



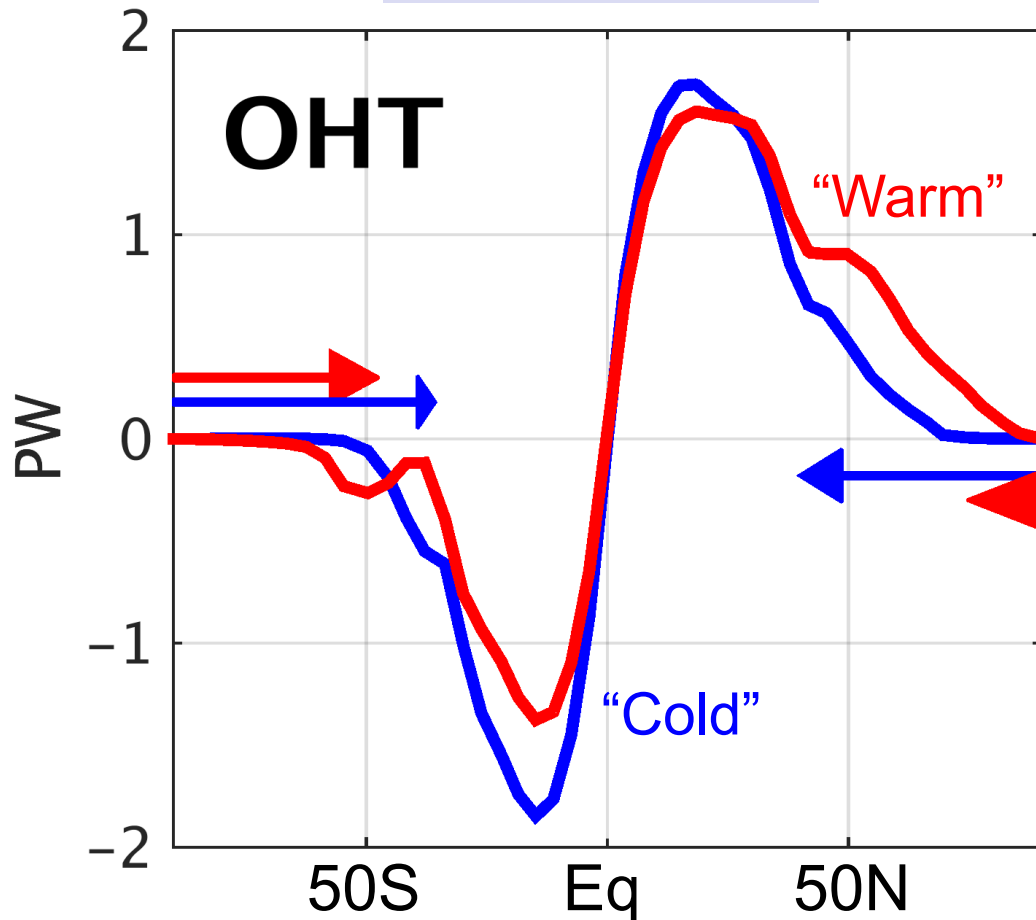
Sea-Ice thickness (m)



- $\Delta\text{SST} = 8.2\text{ }^{\circ}\text{C}$
- $\Delta\text{SAT} = 13.5\text{ }^{\circ}\text{C}$
- SH sea ice: $+14^{\circ}$ in Winter
- NH sea ice cap grows to $\sim 45^{\circ}\text{N}$
- Atm. pCO_2 : -108 ppm
(from 265 to 157 ppm).

OHT/sea ice edge relationship in “Boomerang”

Global OHT



→ Ice edges rest poleward of the large mid-latitudes OHT convergences

→ Multiple states emerge from Northern Hemisphere

Global MOC and Temperature

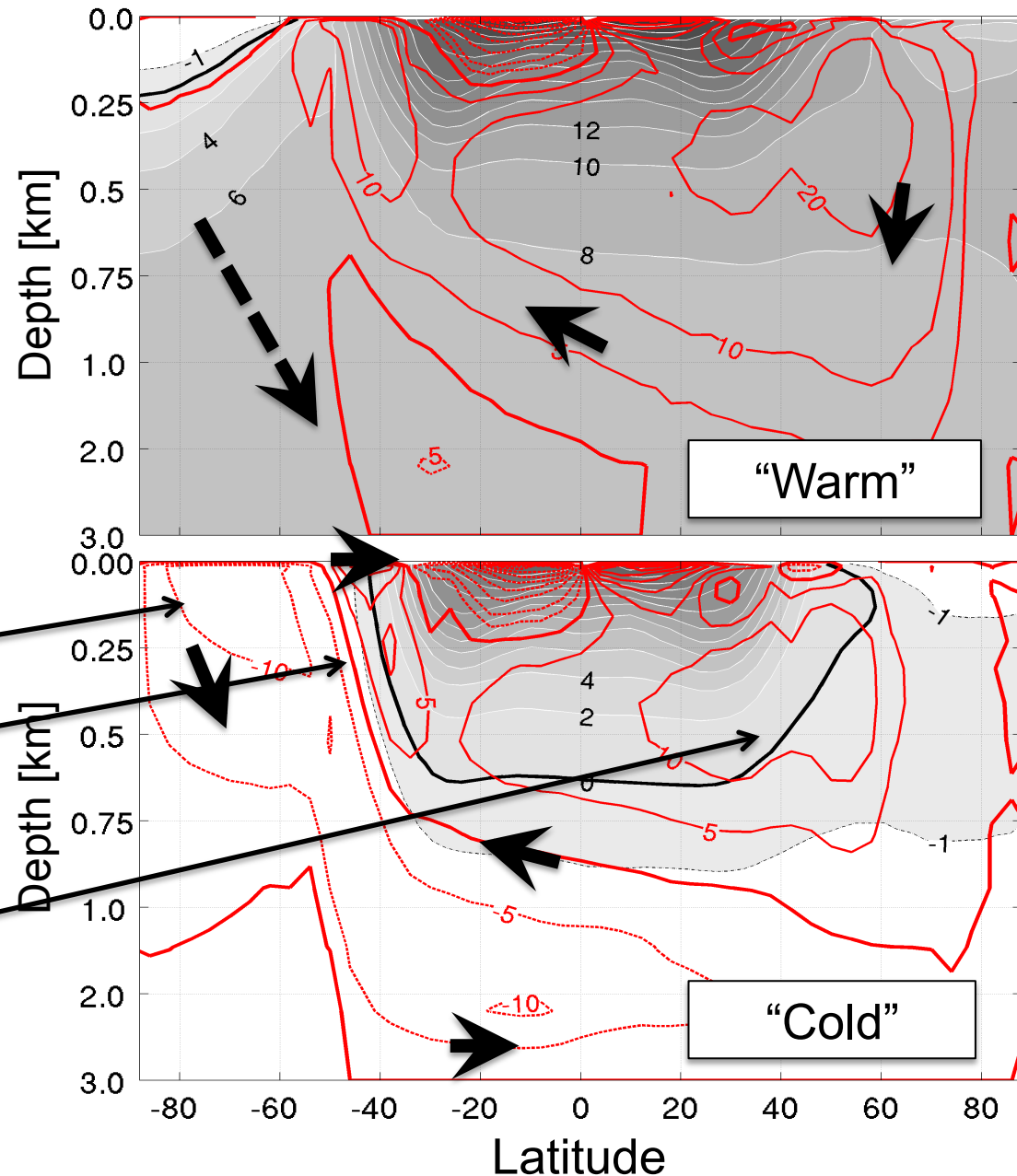
Ventilation of deep ocean shifts to the southern ocean:

“Cold” state bottom waters:

- colder: -1.5°C , \sim freezing point
- saltier (+0.5 psu)
- See Adkins et al. (2002)

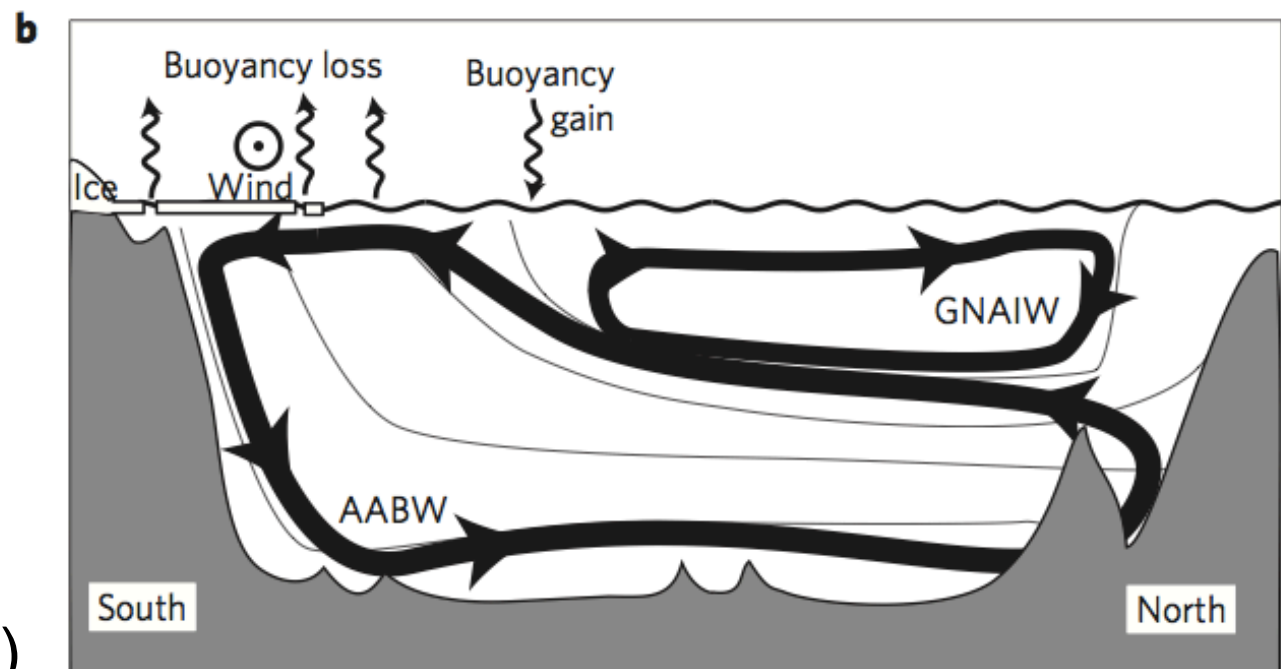
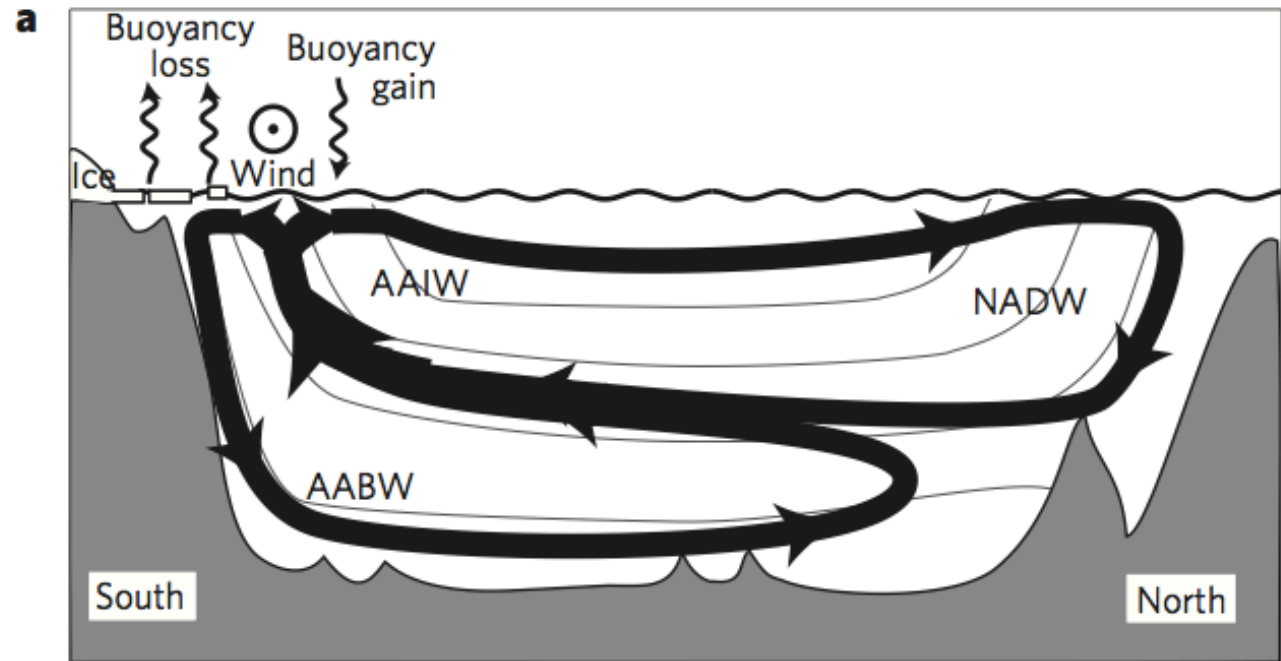
- Brine rejection drives AABW-like cell
- Net SO upwelling rate unchanged
- NH cell shoals and weakens

(see Watson et al. 2015, Ferrari et al. 2014)



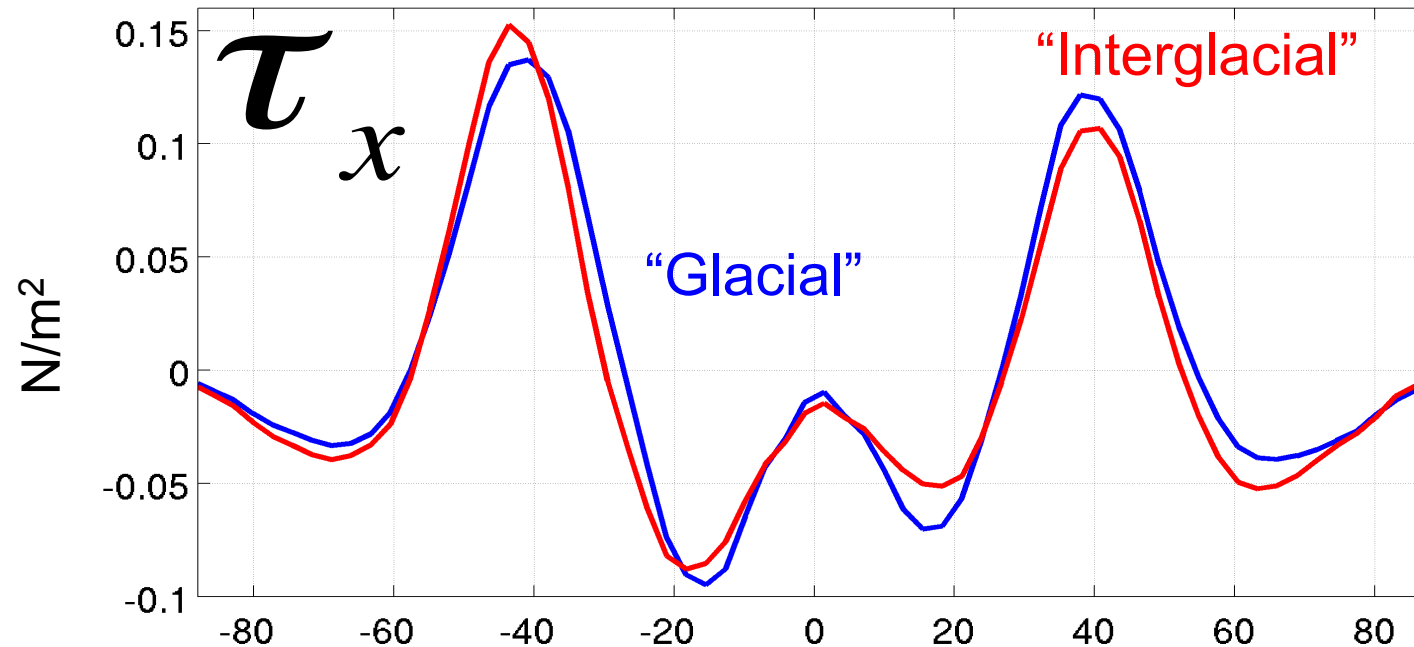
In steady state,
Water coming to the surface:

- Moves south for a buoyancy loss
- Moves to the North for a buoyancy gain



Watson et al. (2015)

Surface Winds



In glacial climate:

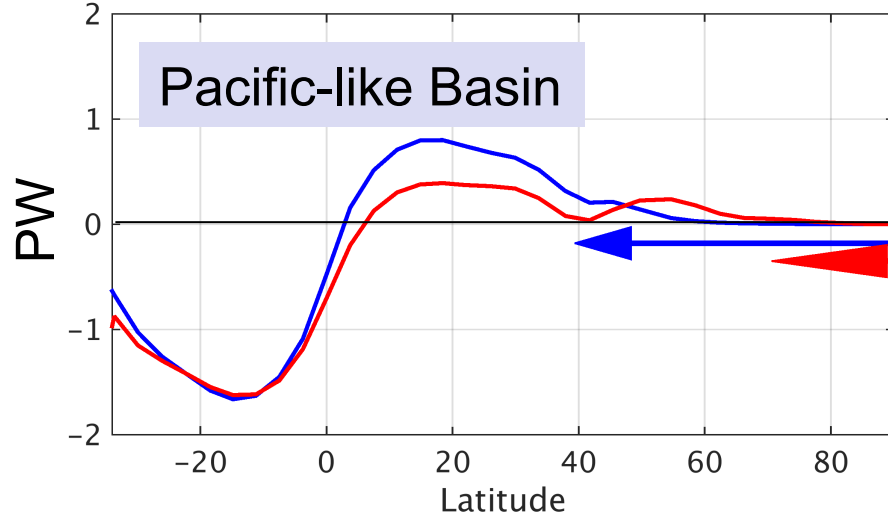
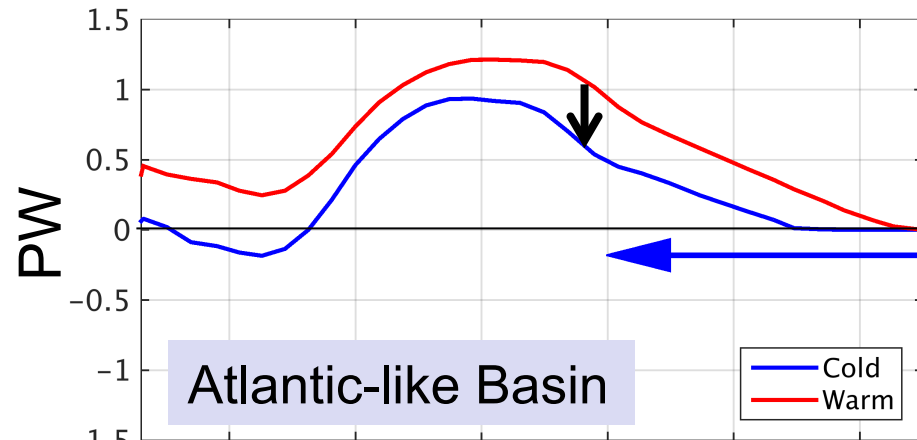
- Trade winds strengthen (as do the Hadley circulation)
- SH westerly winds shift equatorward ~ 1.5 deg
- and weaken $\sim 10\%$

→ Driven by equatorward expansion of sea ice

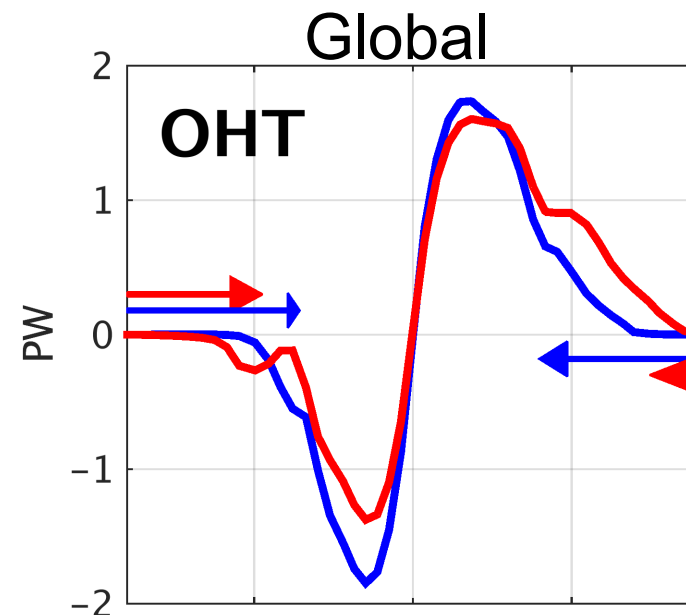
Paleoproxy: no consensus (Shulmeister et al. 2004, Kohfeld et al. 2016)

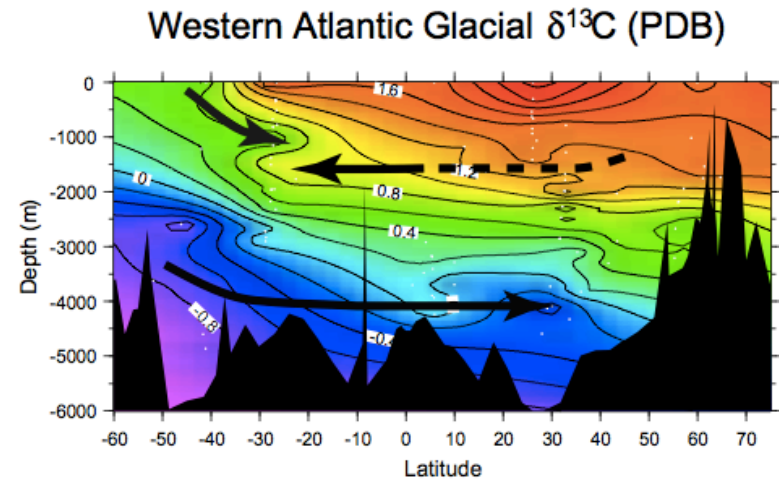
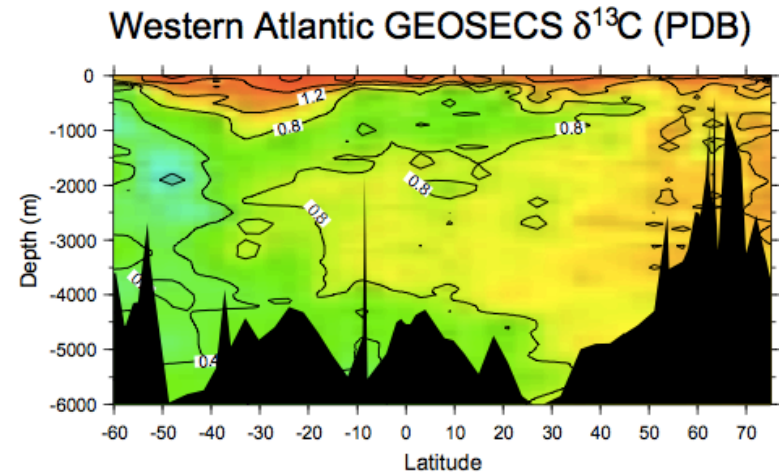
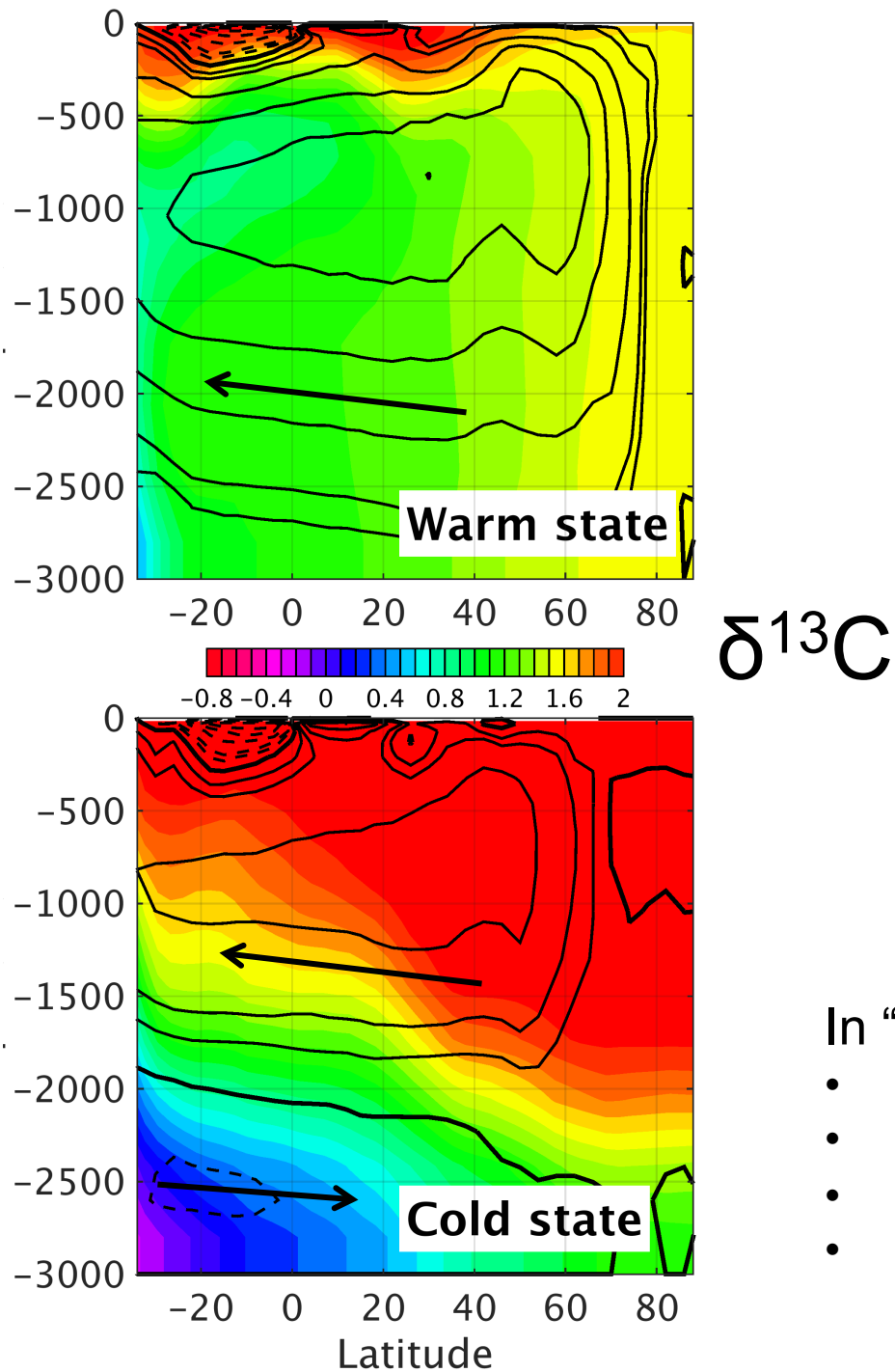
PMIP simulation: no consensus (Sime et al. 2016)

Ocean Heat transports



- “AMOC” decreases
- Decreased OHT in Small basins
- Over compensated by increase in Large basin





In “Cold” state: Curry and Oppo 2005

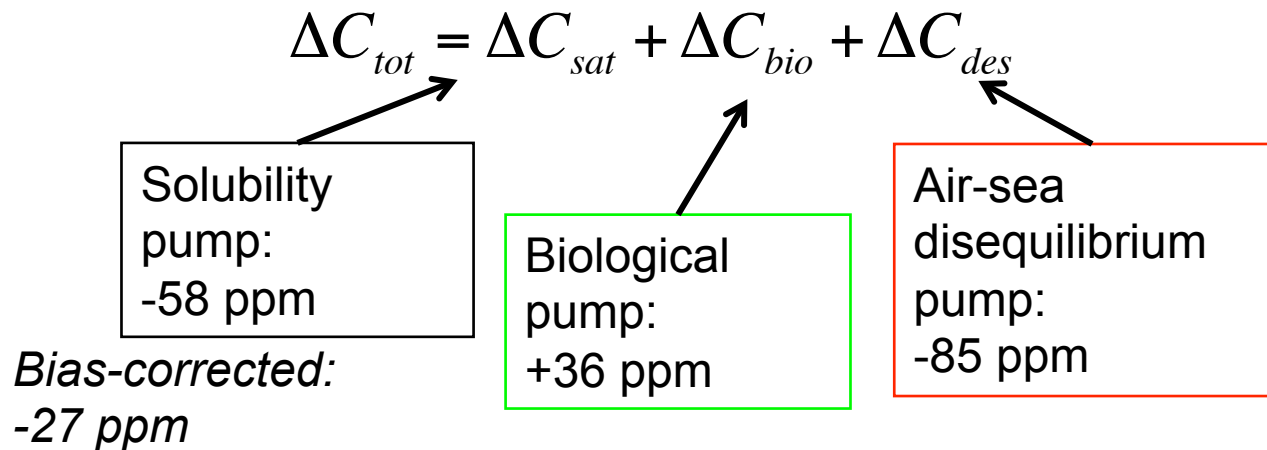
- Shallower, weaker “NADW”,
- Deep convection shifted by 15° southward
- Nutrient-rich AABW-like water
- Depleted upper ocean,

See also Lynch-Stieglitz et al. 2007

How is carbon stored in the “Glacial” ocean?

- ocean carbon-cycle model coupled to atmospheric CO₂,
- inventories of carbon, alkalinity, and phosphate are identical in the 2 solutions.
- the atmospheric CO₂ is *not radiatively active*.

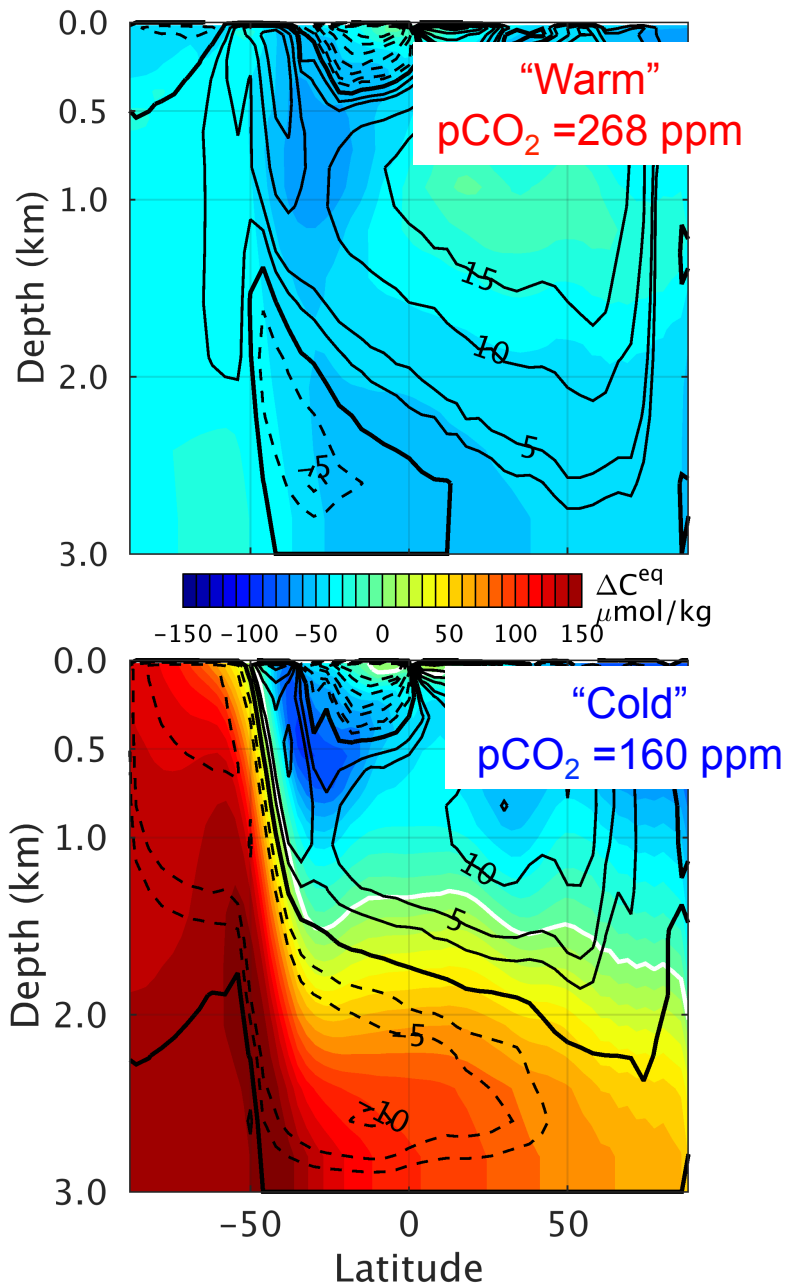
Change (“Warm” → “Cold”) in 3 carbon reservoirs:



- Solubility pump: Temperature dominated (but include salt)
- Net Biological pump: organic + carbonate (CaCO₃ + Alkalinity)

Disequilibrium pump

Global MOC and ΔC^{eq}



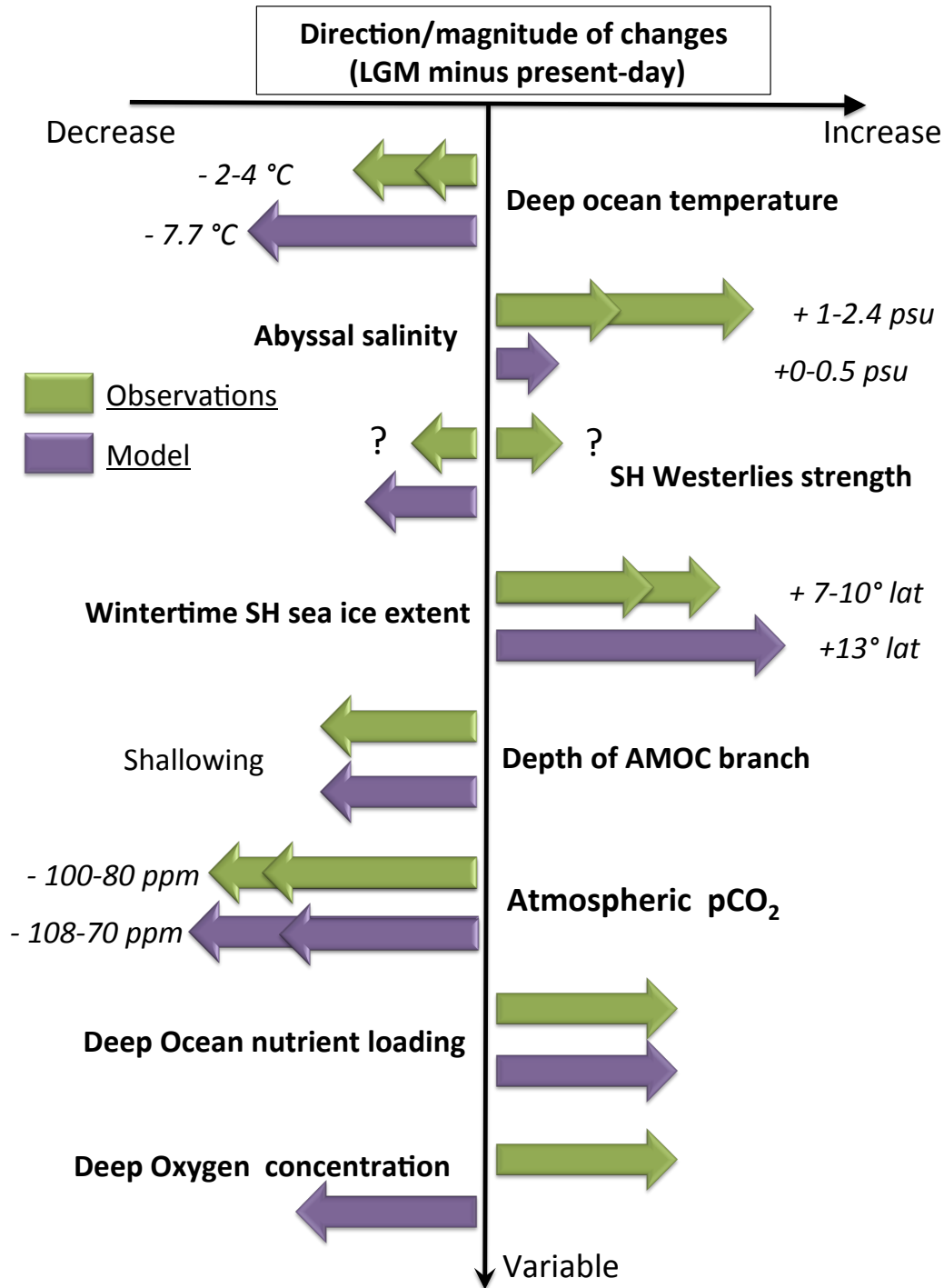
How is carbon stored in the “Glacial” ocean?

→ Increased sea-ice cover reduces the ventilation of upwelled deep waters: DIC accumulates in the deep ocean (Stephens and Keeling, 2000).

Caveats:

- Solubility is overestimated
- Biological pump decreases everywhere in Cold state; Oxygen content also increase in deep ocean (Jaccard and Galbraith 2011, Kohfel et al. 2005)

→ lack of iron cycle? More complex ecosystem

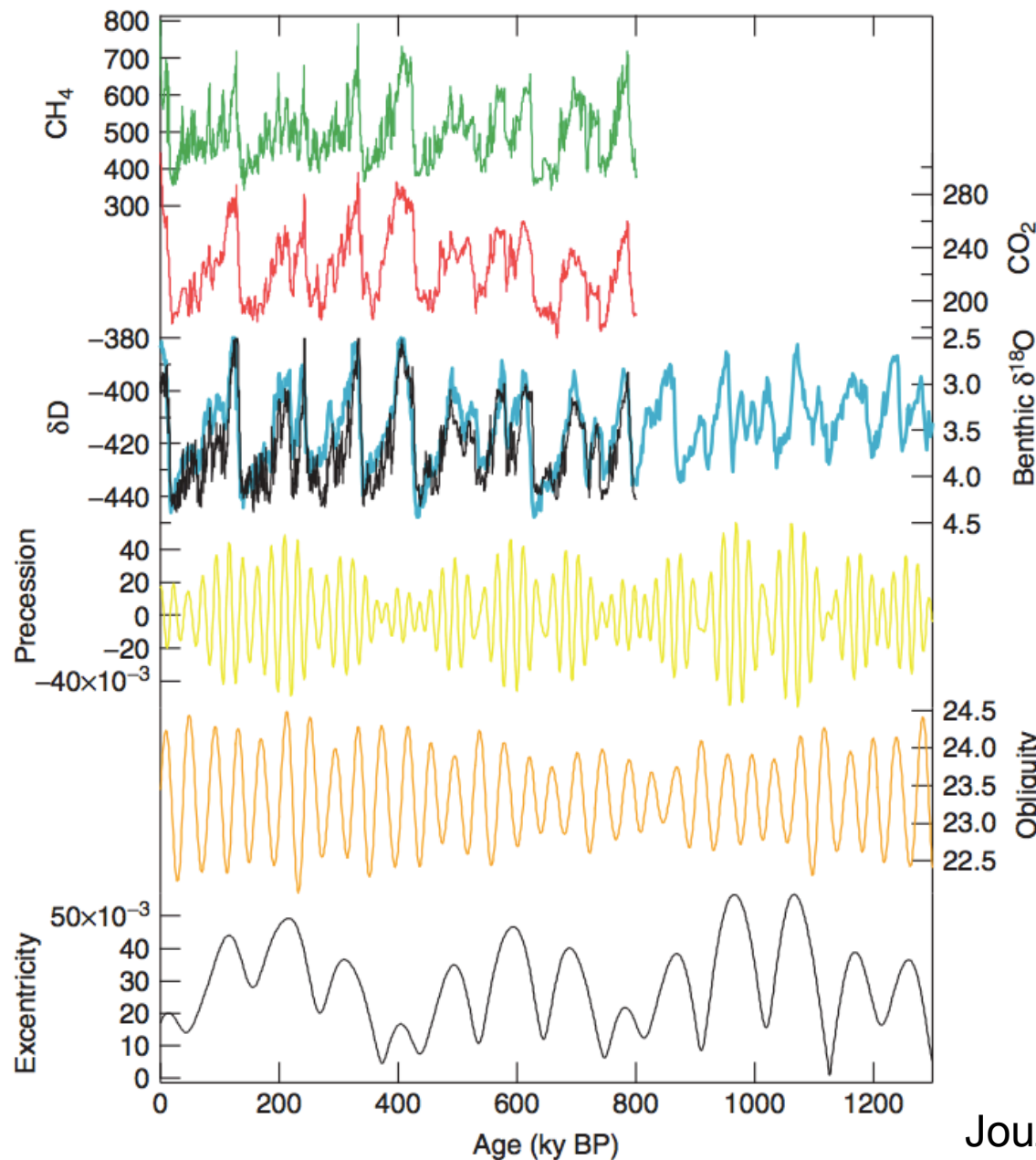


Summary of the
changes:
Simulation versus
Paleoproxy

NH large sea expansion : consistent with paleproxies (de Vernal et al. 00)

Curry and Oppo 05, Lynch-Stieglitz et al. 07, but Gebbie 14

Stochastic resonance



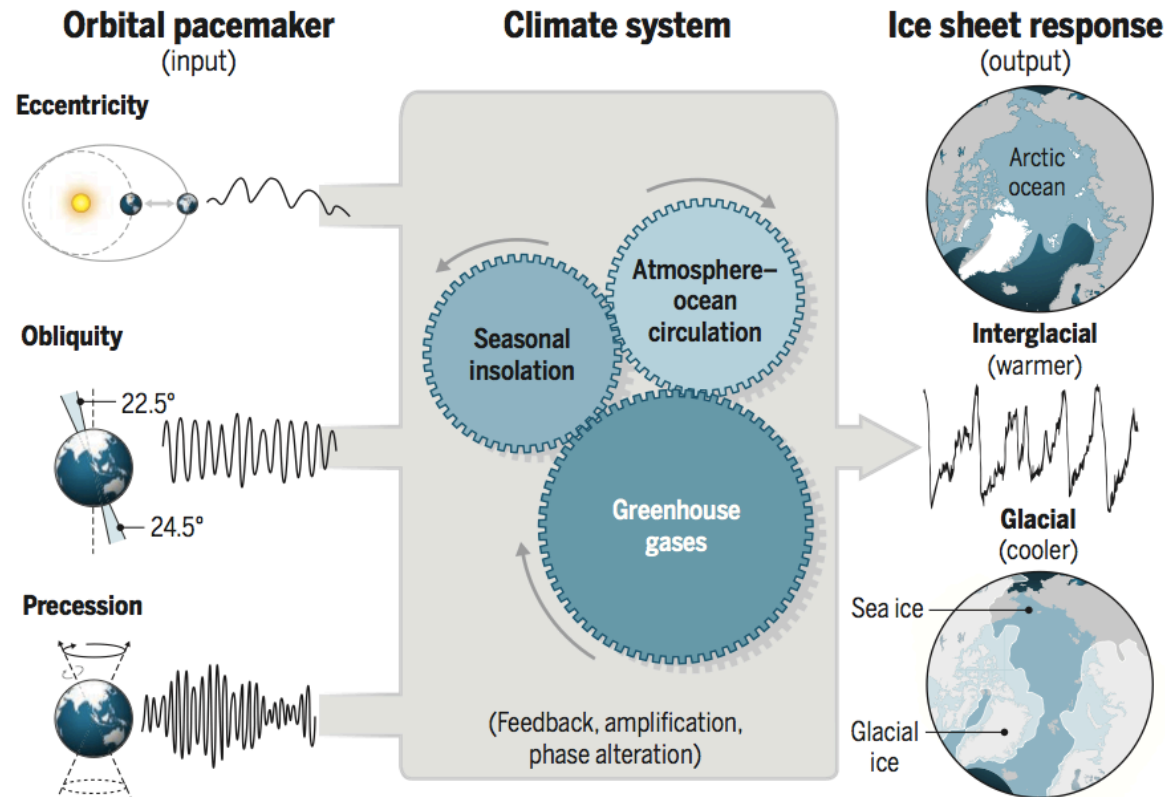
- Periodicity of orbital parameters found in paleoproxy record (Hays et al. 1976)

~20 kyr

~40 kyr

~100 kyr

Problem remains: we don't know the link between input and output

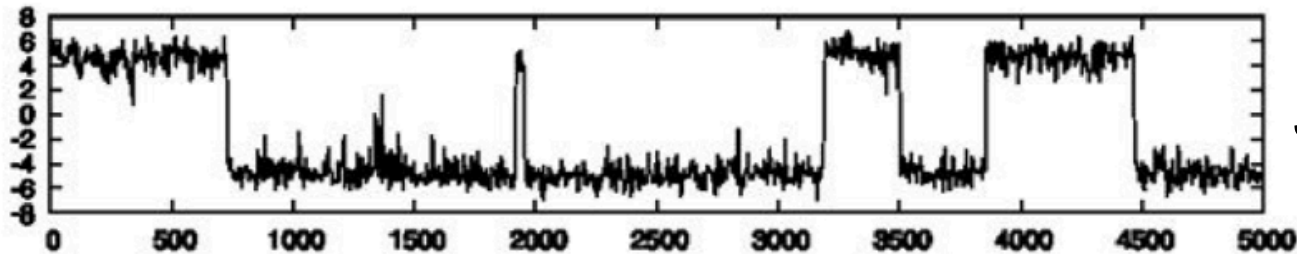
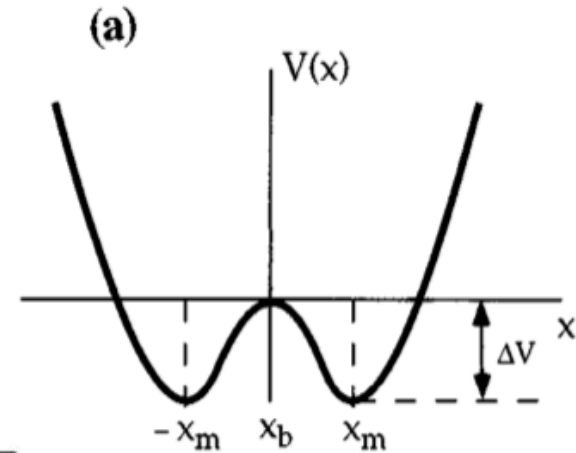


Hodell (2016)

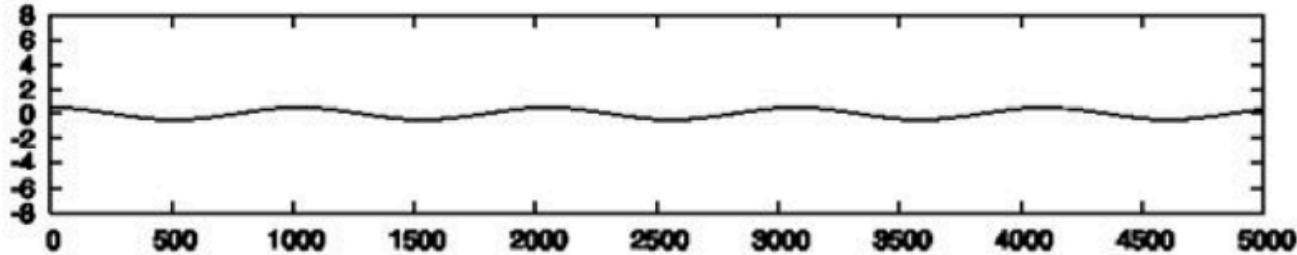
Two families of mechanisms:

- “linear” view: forcing is amplified by strong feedbacks (CO₂, ice-sheet, sea ice)
- “non-linear” view: free oscillations of the climate system, paced or phased-locked by the Milankovitch forcing (Saltzman et al., Tziperman et al., etc.) or multiple states

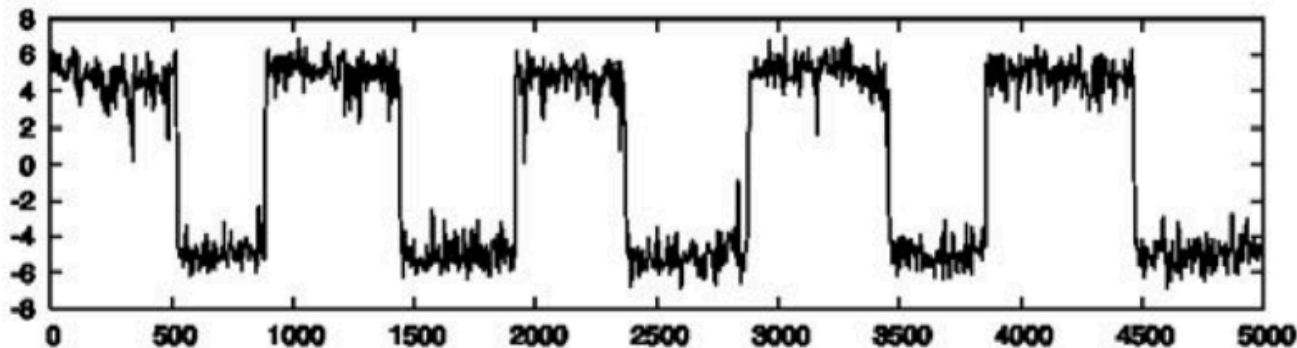
The basics of stochastic resonance



Just forced with noise



Small forcing that does not trigger transition



Forced with noise + small forcing

The basics of stochastic resonance

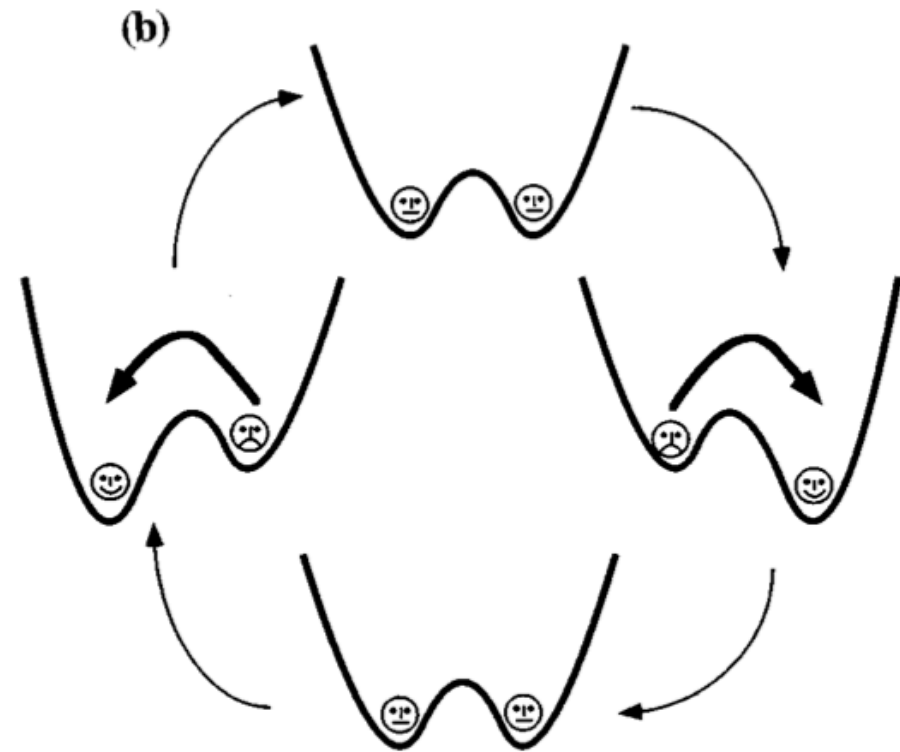
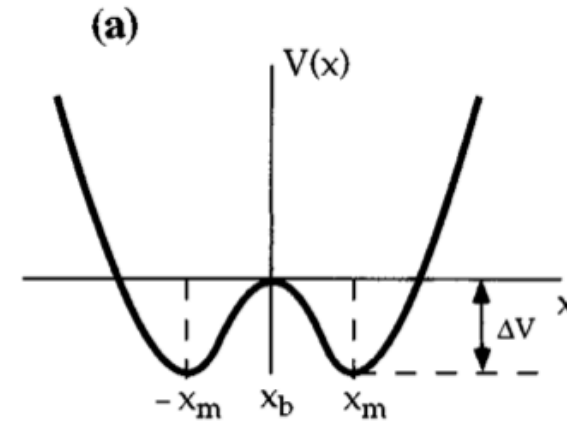
Kramers transition rate, i.e. expected time between transition in the presence of noise:

$$T_n \propto \exp\left(\frac{\Delta V}{\sigma^2}\right)$$

Noise variance

Add a forcing with period T_f :

→ resonance (synchronization)
for $T_n \sim T_f$

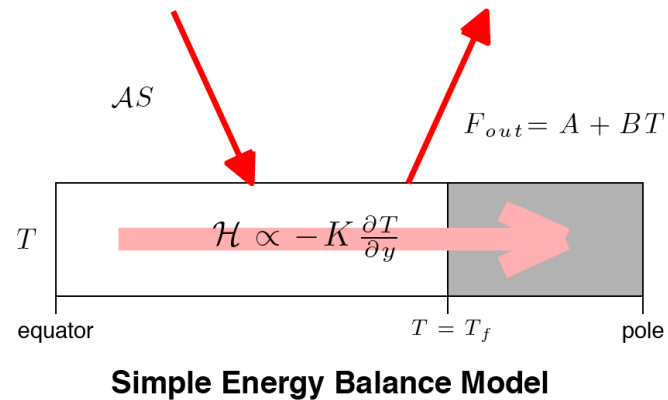


Gammaitoni et al. 1998

SR was born with glacial-Interglacial cycles in mind, but:

- ad-hoc/oversimplified models (0D)
- need multiple states

→ Time to revise

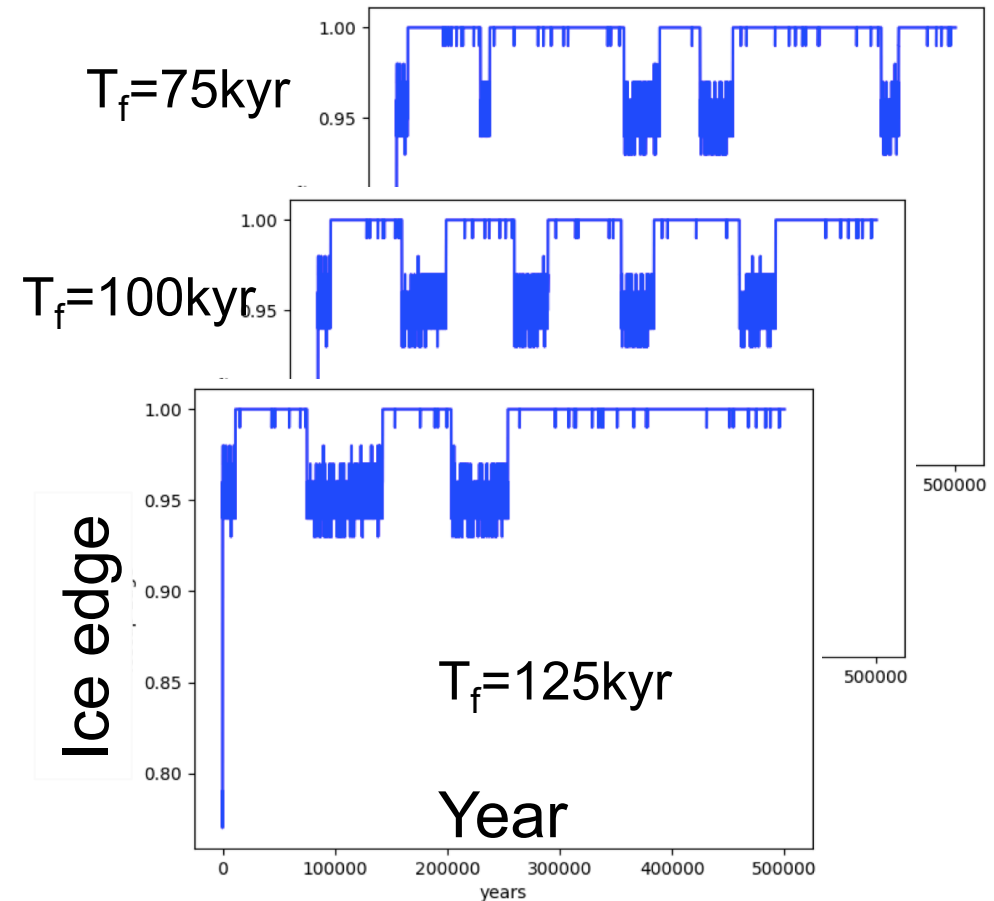


→ Use simple classic EBM = 1D

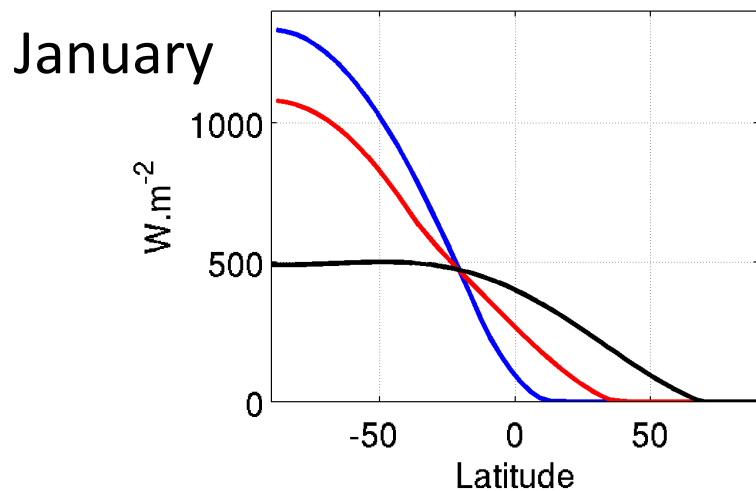
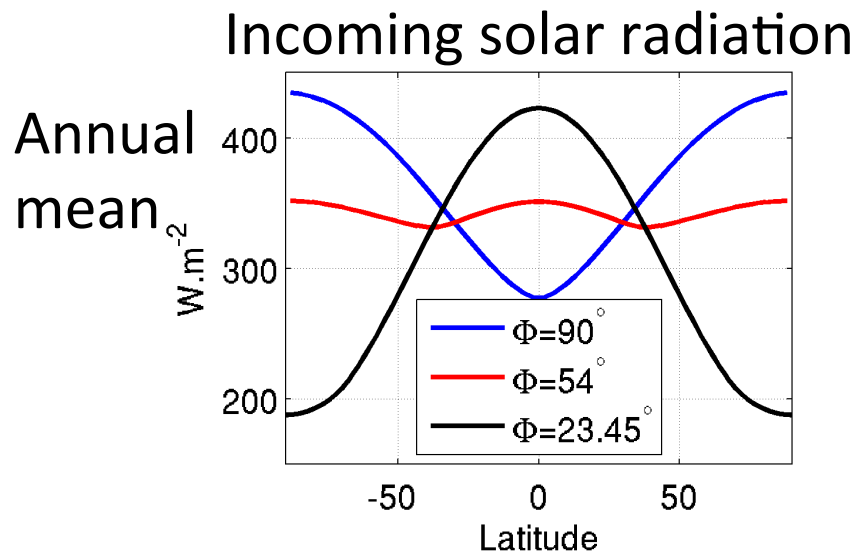
→ Tune noise so Kramers rate
~100 kyr

→ Forcing amplitude $Q/2000$ with
 $Q=340 \text{ W/m}^2$

Ioannis Katharopoulos



1 High-obliquity aquaplanet



SCIENCE

Summer Solstice 2018: The Search for Life in the Galaxy

As you mark the longest day of the year, consider the debate among astronomers over whether Earth's tilt toward the sun helps make life on our world and others possible.

At h
war
Expe
temp

in NYT

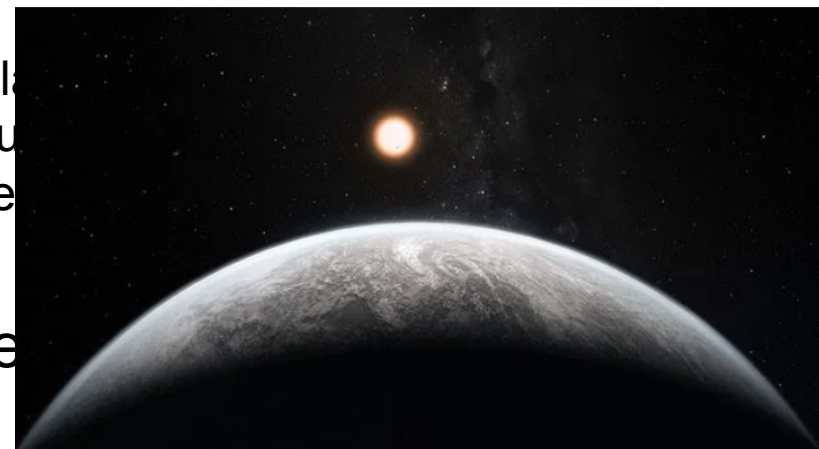
By Shannon Hall

June 20, 2018

Extr

If pol
fluctu
there

Like

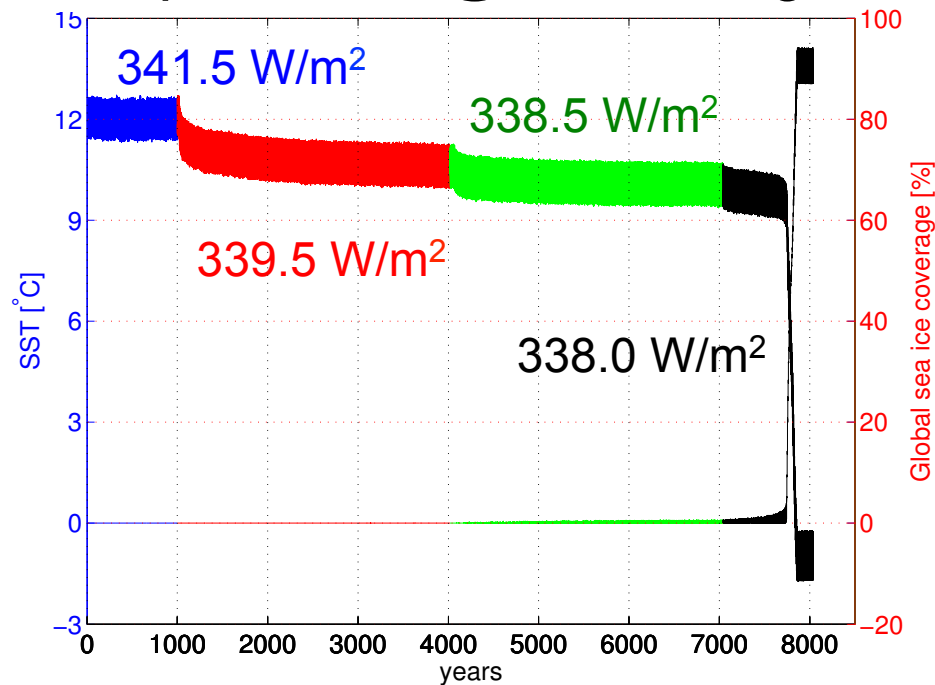


Habitability

Median+min/max
over 90-55°S

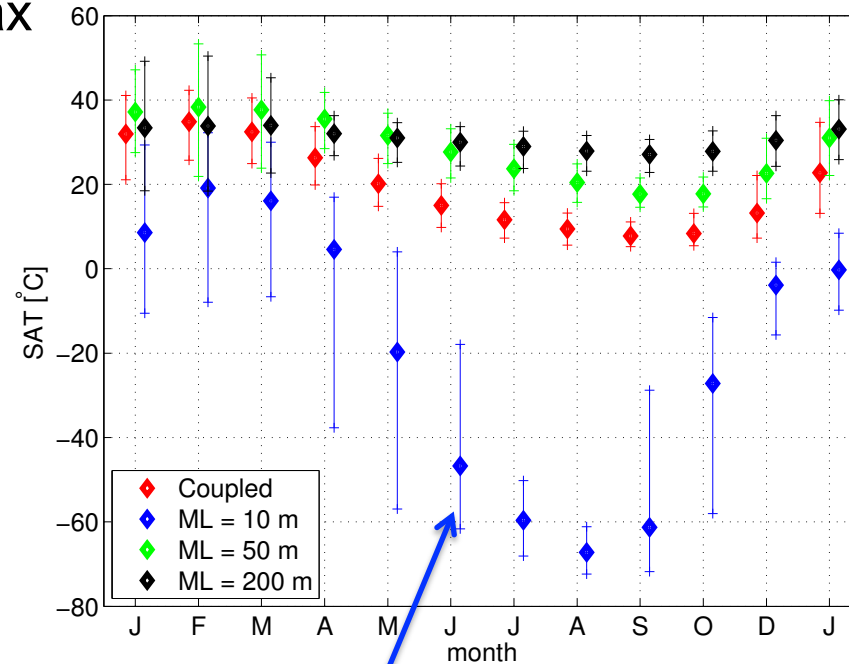
- “Deep” ocean stabilizes climate
- Too shallow ocean → global glaciation

Coupled runs @ $\Phi=90$ deg



Surface Air Temperature

$\phi=90^\circ$

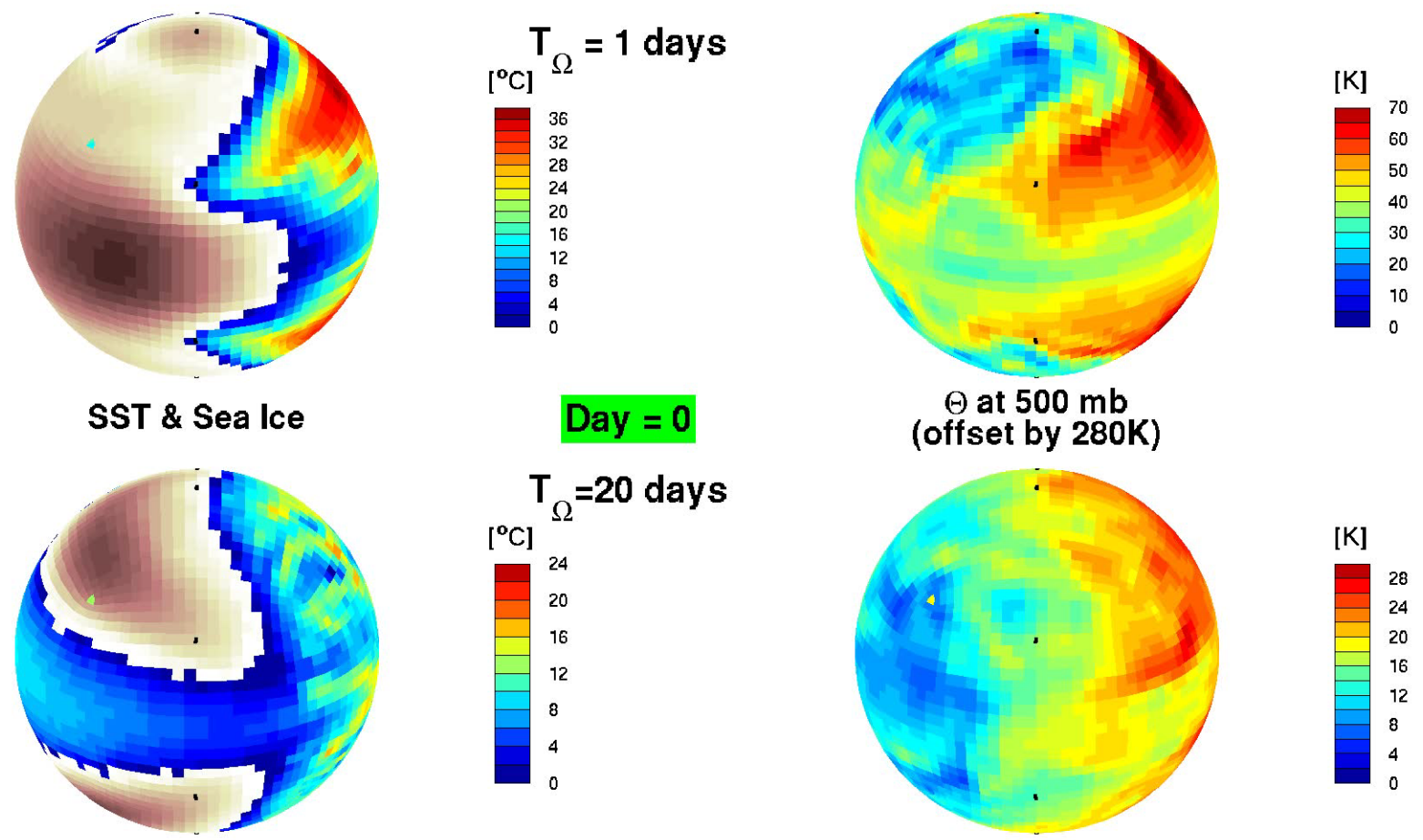


Snowball collapse

Climate system unstable
to small sea ice covers

Ferreira et al. (2014)

2 Tidally-locked aquaplanet



Summary

- Multiple equilibrium states can exist in a complex fully dynamical 3d climate GCM
- Meridional structure of the OHT is key: a large mid-latitude convergence (as observed, wind-driven)
- Think less about AMOC bi-stability (fundamentally an ocean-only process)
- Think more ocean/sea ice multiple states/instability
- Need a more systematic search for this type of equilibria (as was done for the MOC bi-stability)

