



THE AUSTRALIAN NATIONAL UNIVERSITY

# Conversion coefficients and atomic radiations in ENSDF - BrIcc, BrIccMixing and BrIccEmis

Tibor Kibèdi (ANU)

# Heavy Ion Accelerator Facility, ANU Canberra



## ANU HIAS

NEC 14UD tandem electrostatic accelerator commissioned 1975

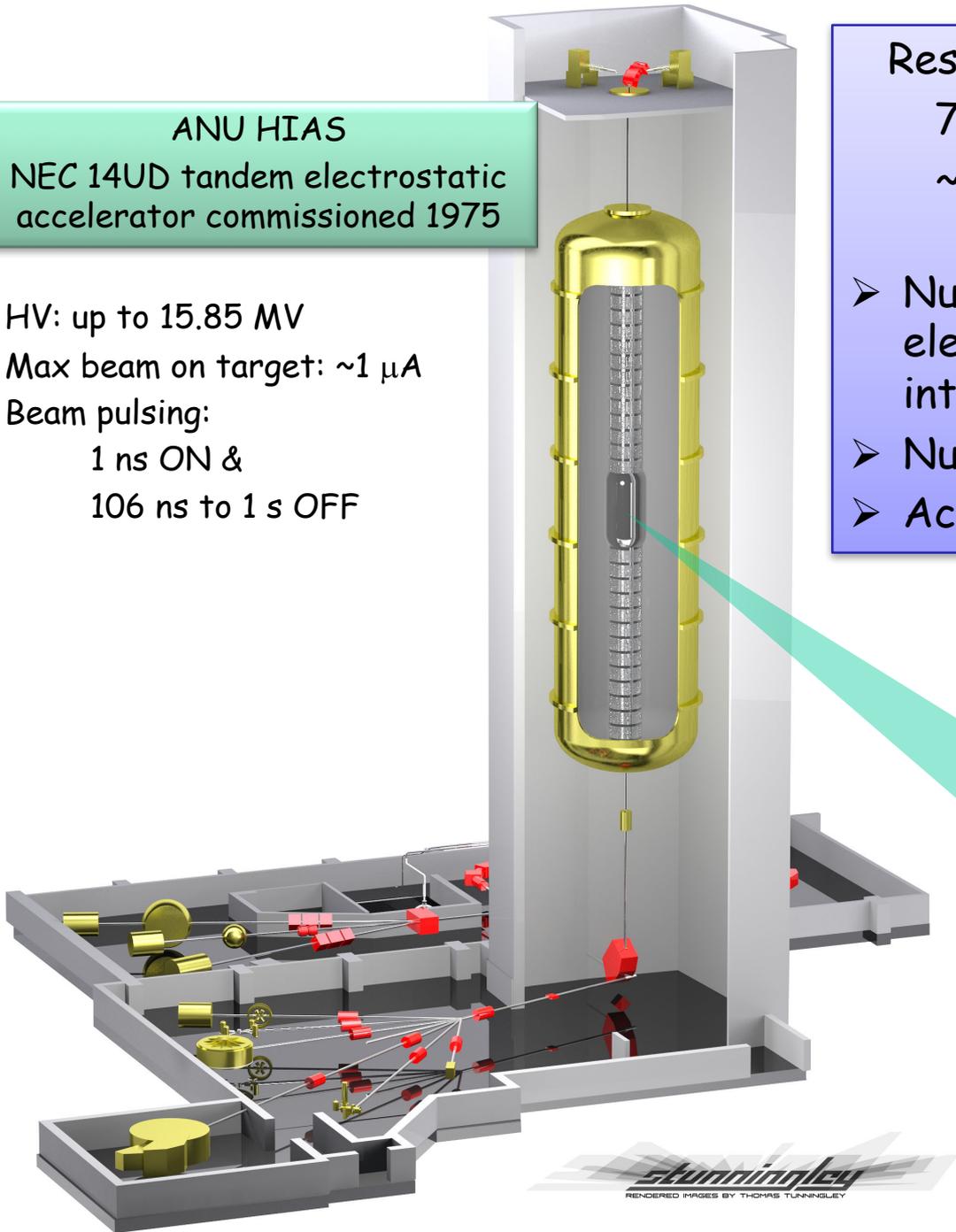
HV: up to 15.85 MV

Max beam on target:  $\sim 1 \mu\text{A}$

Beam pulsing:

1 ns ON &

106 ns to 1 s OFF

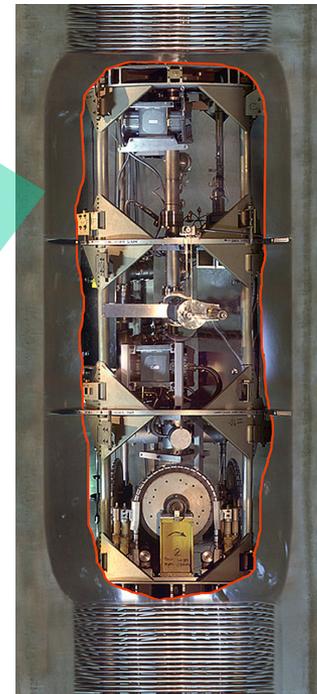


## Research areas

7 continuing / 8 postdocs

$\sim 20$  research students / 60  
outside users)

- Nuclear Structure ( $\gamma$ -ray, conversion electron spectroscopy, hyperfine interactions)
- Nuclear Reaction Dynamics
- Accelerator Mass Spectrometry



- BrIcc**
- BrIcc Home
  - BrIcc Grapher
  - Quick reference
  - Data tables
  - Program manual
  - Obtaining BrIcc
  - Version history
  - Authors

- Nuclear Structure Links**
- ANU Nuclear Physics
  - National Nuclear Data Center
  - IAEA Nuclear Data Centre
  - NSDD network
  - DDEP network

**BrIcc v2.3S**  
**Conversion Coefficient Calculator**

Z (atomic number or symbol)

γ-energy (in keV)  Uncertainty

Enter (optional) uncertainty in energy as **x** or **+x-y**

Multipolarity  δ  Uncertainty

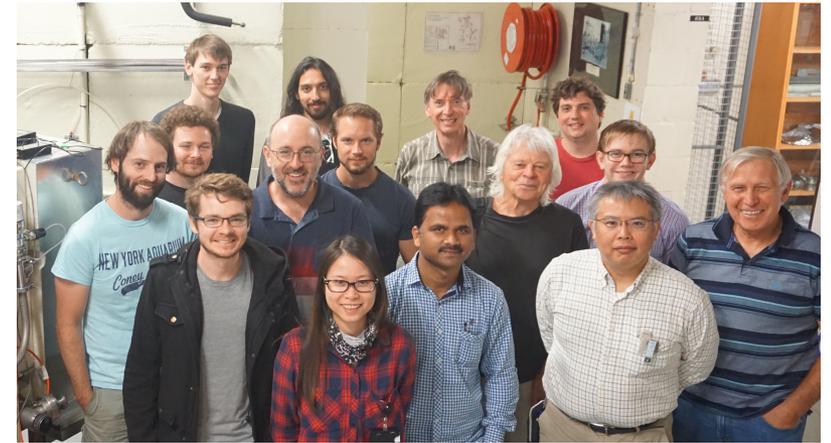
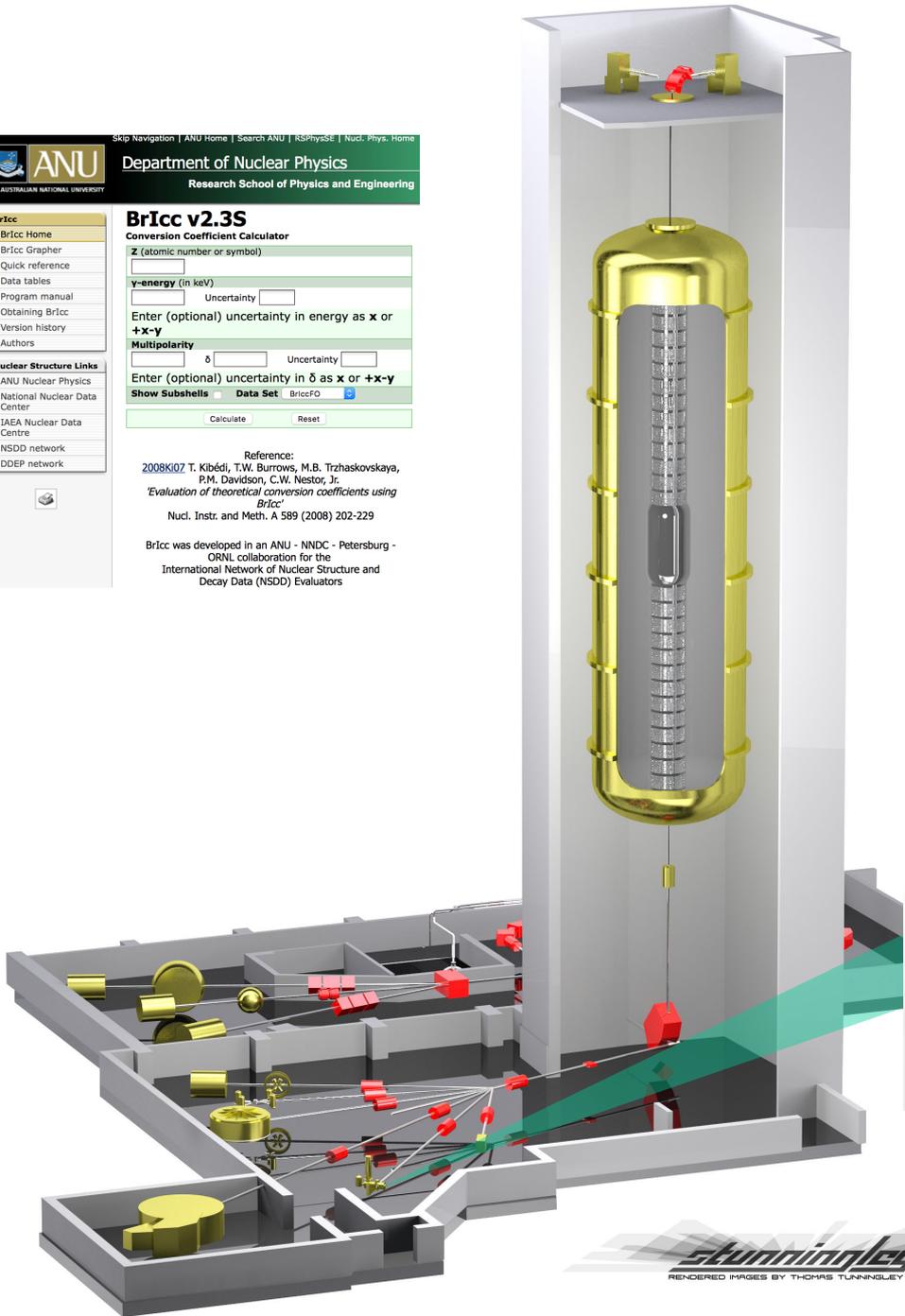
Enter (optional) uncertainty in δ as **x** or **+x-y**

Show Subshells  Data Set

Calculate  Reset

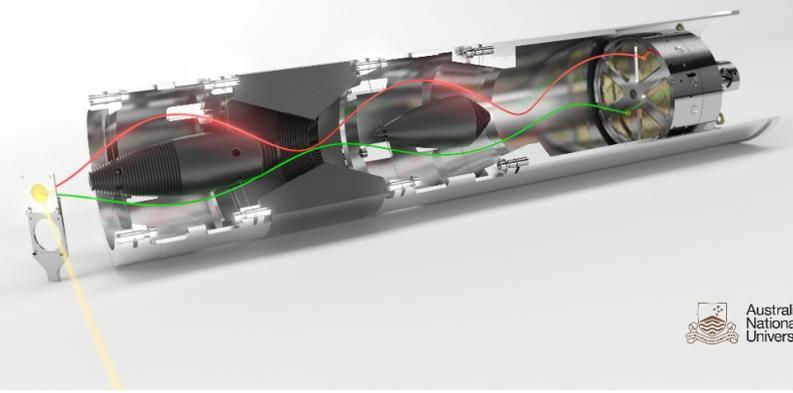
Reference:  
 2008K07 T. Kibédi, T.W. Burrows, M.B. Trzhaskovskaya, P.M. Davidson, C.W. Nestor, Jr.  
*'Evaluation of theoretical conversion coefficients using BrIcc'*  
 Nucl. Instr. and Meth. A 589 (2008) 202-229

BrIcc was developed in an ANU - NNDC - Petersburg - ORNL collaboration for the International Network of Nuclear Structure and Decay Data (NSDD) Evaluators



Looking for E0's with a "pair of glasses" in  $^{12}\text{C}$  to  $^{52}\text{Cr}$  (2018-Apr)

**SUPER-E PAIR SPECTROMETER**



- Calculation of conversion coefficients
- Multipole mixing ratios
- Electric monopole E0 transitions
- Measurements and some aspects of extracting information for ENSDF
- Atomic radiations from nuclear decay

Practice #3:

- BrIcc, BrIccMixing, Ruler, Gabs



# Electromagnetic Decay Processes

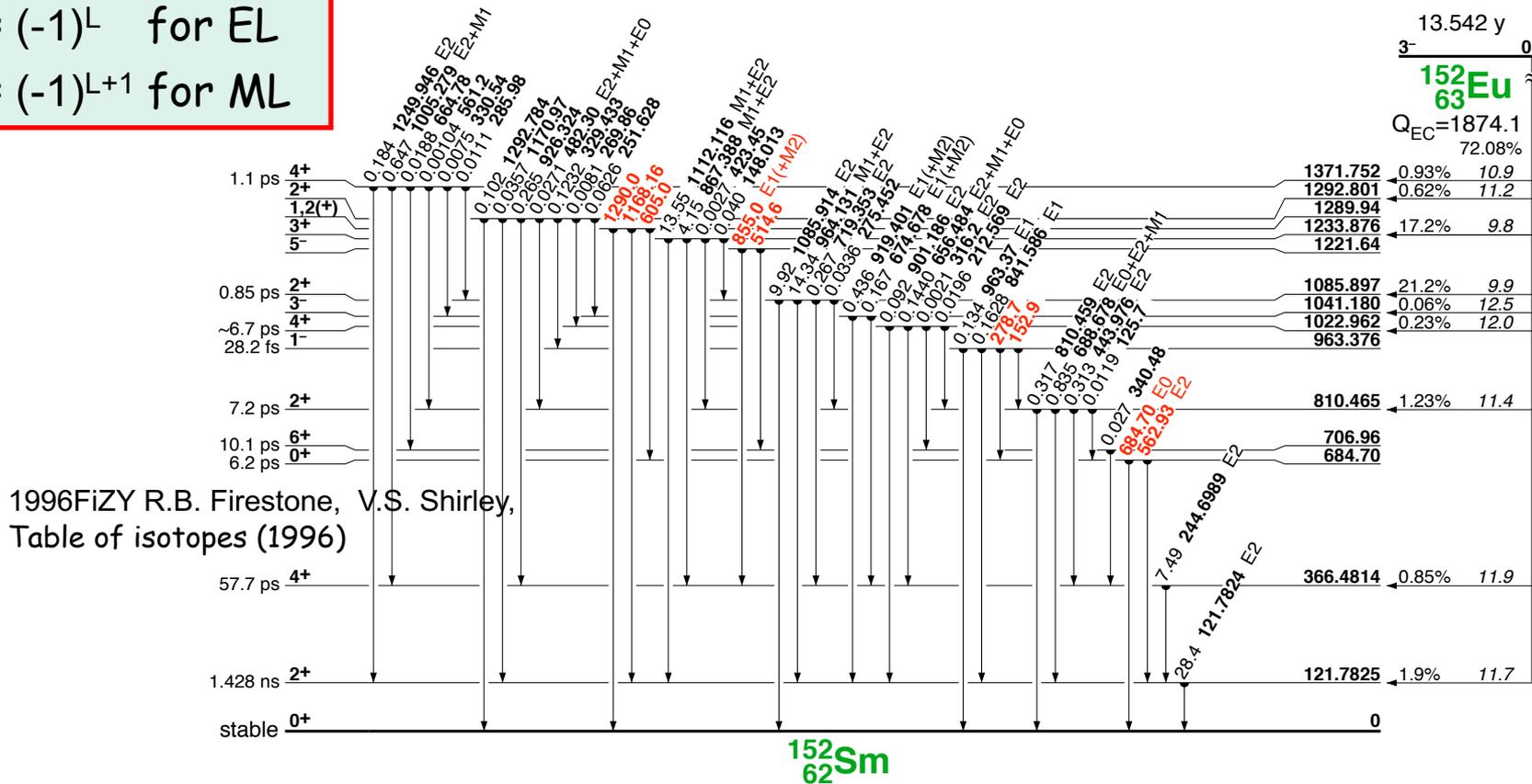
EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

$$\pi = (-1)^{L+1} \text{ for ML}$$



# Electromagnetic Decay Processes

EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

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$$\pi = (-1)^L \text{ for EL}$$

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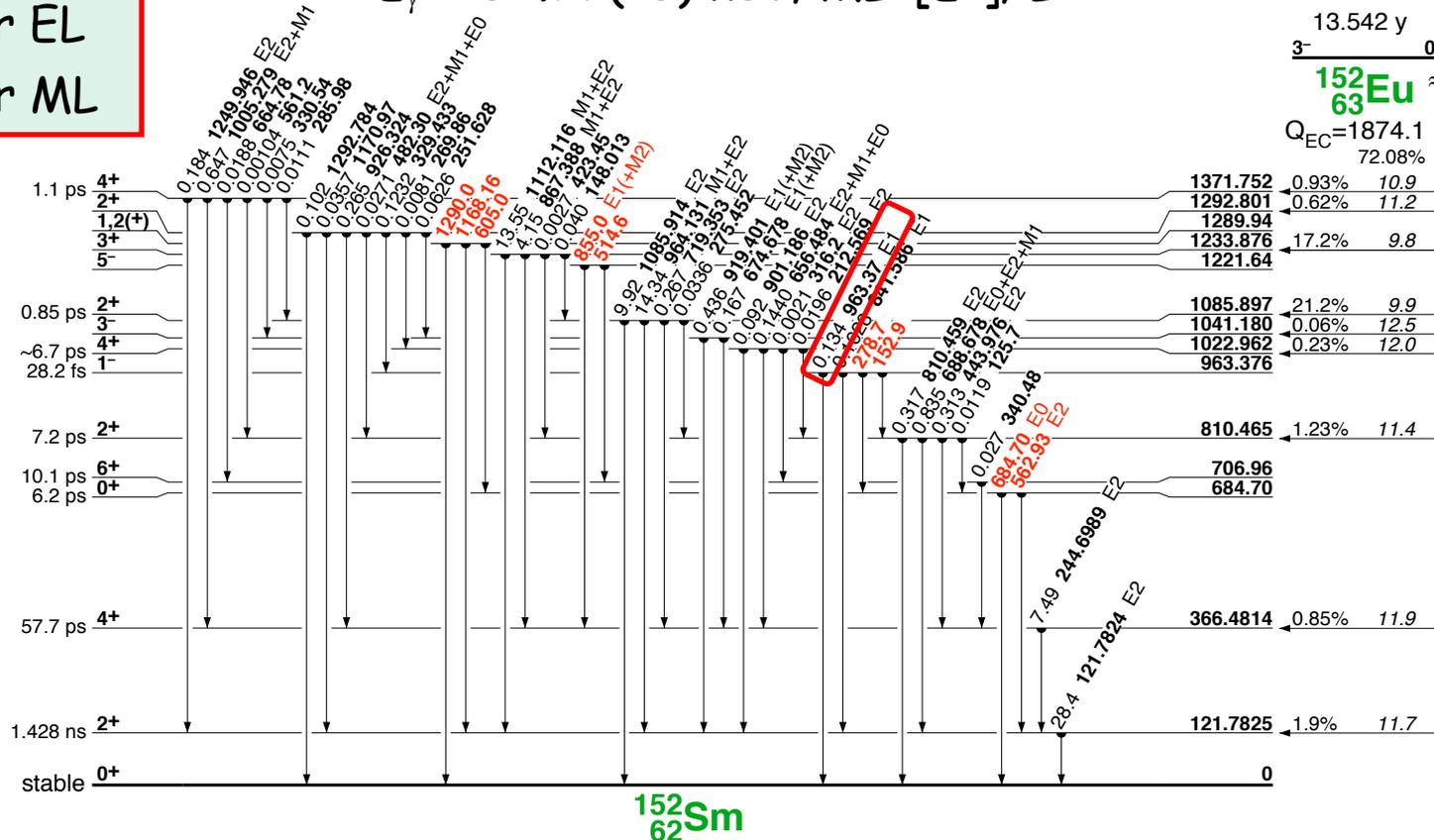
Example (2013Ma77, M.J. Martin, NDSH 114 (2013) 1497):

Initial level: 963.358(3) keV,  $J^\pi=1^-$

Final level: 810.453(5) keV,  $J^\pi=2^+$

$\Delta E=152.905(6)$  keV,  $\Delta J=1$ ,  $\Delta\pi=-1$

$E_\gamma=152.77(16)$  keV;  $ML=[E1]$ ;  $L=1$



# Electromagnetic Decay Processes

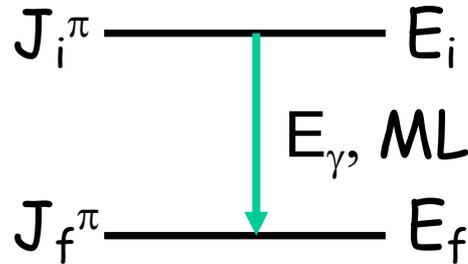
EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

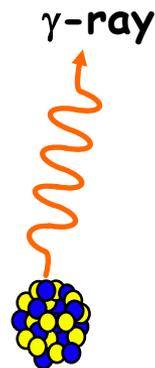
$$\pi = (-1)^L \quad \text{for EL}$$

$$\pi = (-1)^{L+1} \quad \text{for ML}$$



Gamma-rays  
(1<sup>st</sup> order)

$E_\gamma$



Energetics

$$\text{Gamma } E_\gamma = E_i - E_f + T_r$$

# Electromagnetic Decay Processes

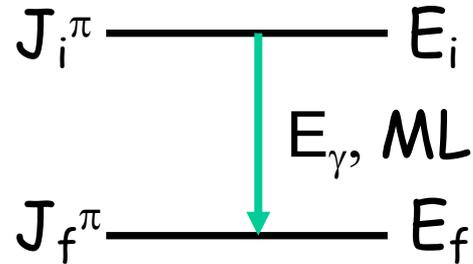
EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

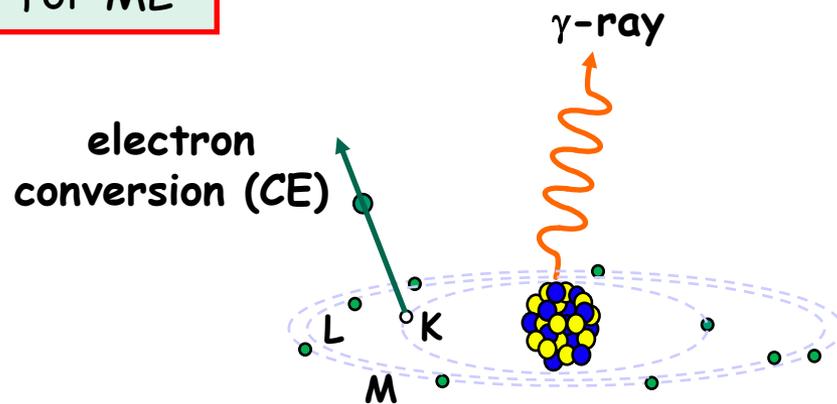
$$\pi = (-1)^{L+1} \text{ for ML}$$



Gamma-rays  
(1<sup>st</sup> order)

$E_\gamma$

Conversion electrons  
(2<sup>nd</sup> order)



Energetics

Gamma  $E_\gamma = E_i - E_f + T_r$

CE  $E_{CE,i} = E_i - E_f - E_{BE,i} + T_r$

# Electromagnetic Decay Processes

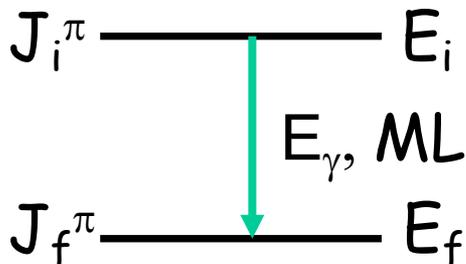
EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

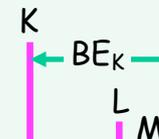
$$\pi = (-1)^{L+1} \text{ for ML}$$



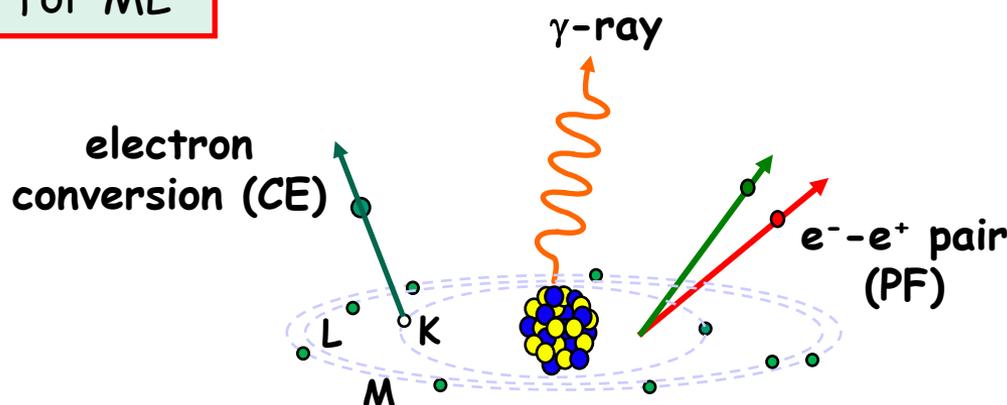
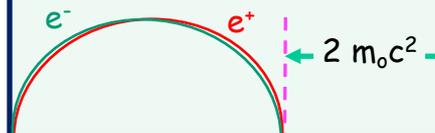
Gamma-rays  
(1<sup>st</sup> order)

$E_\gamma$

Conversion electrons  
(2<sup>nd</sup> order)



Electron-positron pairs  
(3<sup>rd</sup> order)



Energetics

Gamma  $E_\gamma = E_i - E_f + T_r$

CE  $E_{CE,i} = E_i - E_f - E_{BE,i} + T_r$

PF  $E^+ + E^- = E_i - E_f - 2m_0c^2 + T_r$

# Electromagnetic Decay Processes

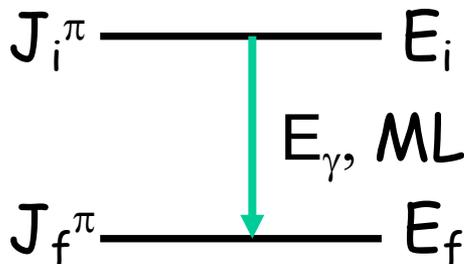
EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

$$\pi = (-1)^{L+1} \text{ for ML}$$



Gamma-rays  
(1<sup>st</sup> order)

$\lambda_\gamma$

$E_\gamma$

Conversion electrons (CE)  
(2<sup>nd</sup> order)

$\lambda_{K,CE}$

K

$BE_K$

L

M

Electron-positron pairs (PF)  
(3<sup>rd</sup> order)

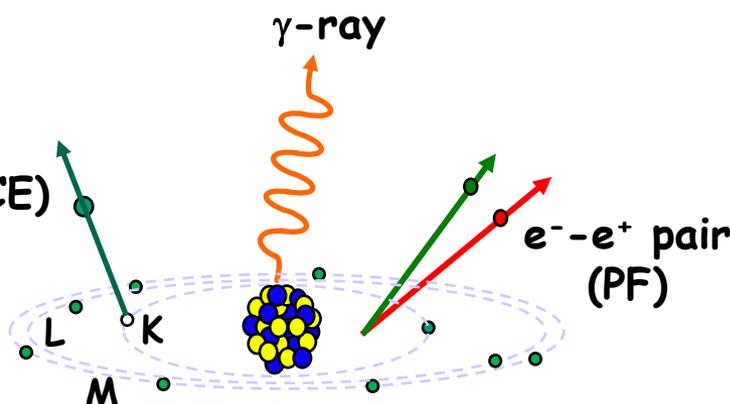
$e^-$

$e^+$

$\lambda_{PF}$

$2 m_0 c^2$

electron  
conversion (CE)



Transition probability

$$\lambda_T = \lambda_\gamma + \lambda_K + \lambda_L + \lambda_M \dots + \lambda_{PF}$$

Conversion coefficient

$$\alpha_{CE,PF} = \lambda_{CE,PF} / \lambda_\gamma$$

$$\lambda_{CE,PF} = \lambda_\gamma \times \alpha_{CE,PF}$$

Energetics

Gamma  $E_\gamma = E_i - E_f + T_r$

CE  $E_{CE,i} = E_i - E_f - E_{BE,i} + T_r$

PF  $E^+ + E^- = E_i - E_f - 2m_0c^2 + T_r$

# Electromagnetic Decay Processes

EM decay: energy and momentum carried away

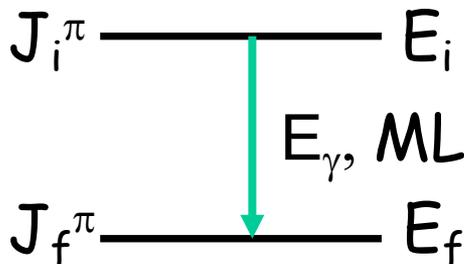
Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

$$\pi = (-1)^{L+1} \text{ for ML}$$

Conversion coefficient:  
relative probability in  
comparison to gamma emission



Gamma-rays  
(1<sup>st</sup> order)

$\lambda_\gamma$

$E_\gamma$

Conversion electrons (CE)  
(2<sup>nd</sup> order)

$\lambda_{K,CE}$

K

$BE_K$

L

M

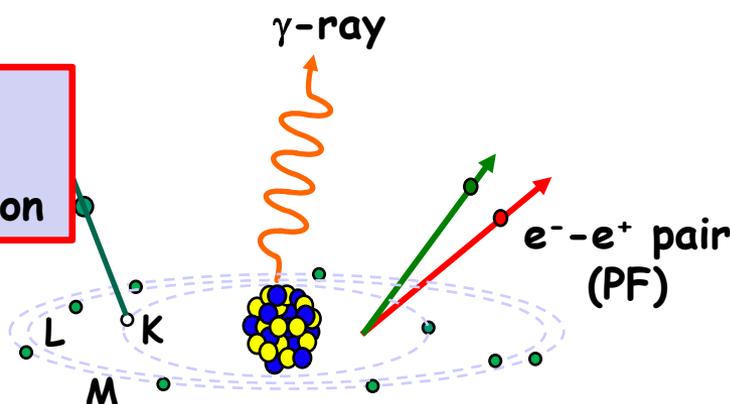
Electron-positron pairs (PF)  
(3<sup>rd</sup> order)

$e^-$

$e^+$

$\lambda_{PF}$

$2 m_0 c^2$



Transition probability

$$\lambda_T = \lambda_\gamma + \lambda_K + \lambda_L + \lambda_M \dots + \lambda_{PF}$$

Conversion coefficient

$$\alpha_{CE,PF} = \lambda_{CE,PF} / \lambda_\gamma$$

$$\lambda_{CE,PF} = \lambda_\gamma \times \alpha_{CE,PF}$$

Energetics

Gamma  $E_\gamma = E_i - E_f + T_r$

CE  $E_{CE,i} = E_i - E_f - E_{BE,i} + T_r$

PF  $E^+ + E^- = E_i - E_f - 2m_0c^2 + T_r$

# Electromagnetic Decay Processes

EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

$$\pi = (-1)^{L+1} \text{ for ML}$$

Conversion coefficient:  
relative probability in  
comparison to gamma emission

Can be calculated - BrIcc  
 $\alpha \sim f(Z, E_\gamma, EML, \text{shell})$

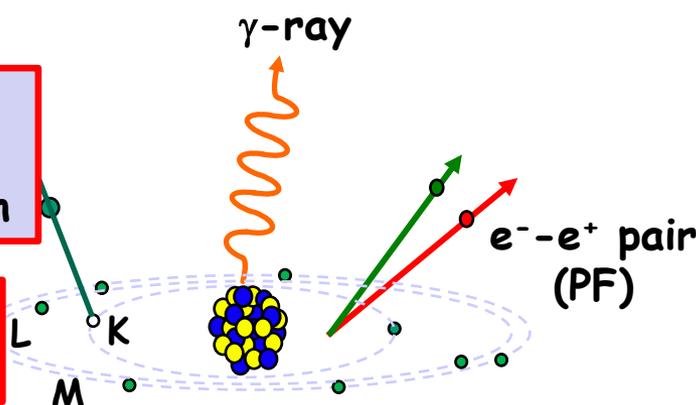
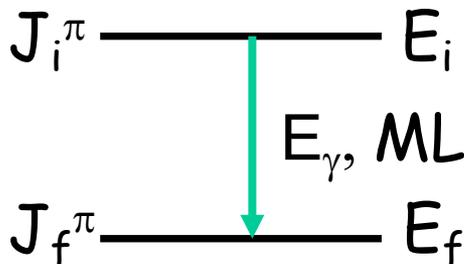
Transition probability

$$\lambda_T = \lambda_\gamma + \lambda_K + \lambda_L + \lambda_M + \dots + \lambda_{PF}$$

Conversion coefficient

$$\alpha_{CE,PF} = \lambda_{CE,PF} / \lambda_\gamma$$

$$\lambda_{CE,PF} = \lambda_\gamma \times \alpha_{CE,PF}$$



Gamma-rays  
(1<sup>st</sup> order)

$\lambda_\gamma$

$E_\gamma$

Conversion electrons (CE)  
(2<sup>nd</sup> order)

$\lambda_{K,CE}$

K

$BE_K$

L

M

Electron-positron pairs (PF)  
(3<sup>rd</sup> order)

$e^-$

$e^+$

$\lambda_{PF}$

$2 m_0 c^2$

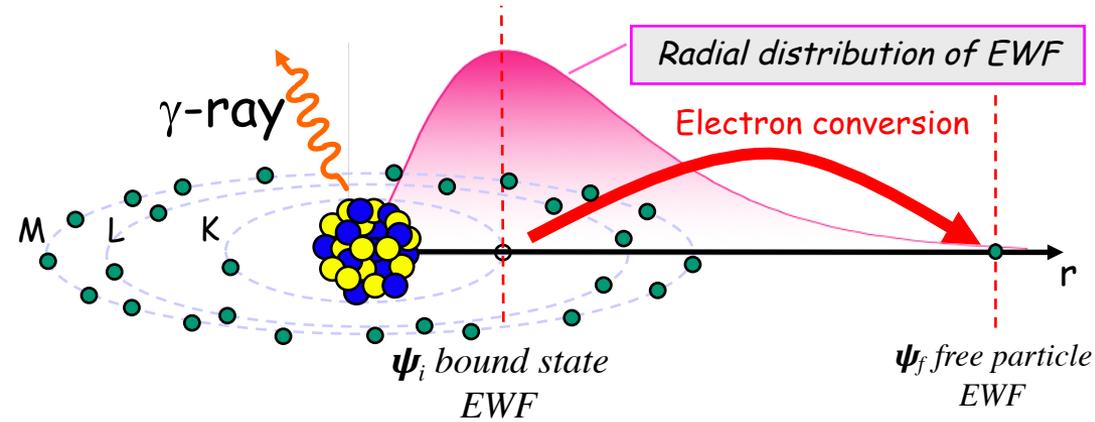
Energetics

Gamma  $E_\gamma = E_i - E_f + T_r$

CE  $E_{CE,i} = E_i - E_f - E_{BE,i} + T_r$

PF  $E^+ + E^- = E_i - E_f - 2m_0c^2 + T_r$

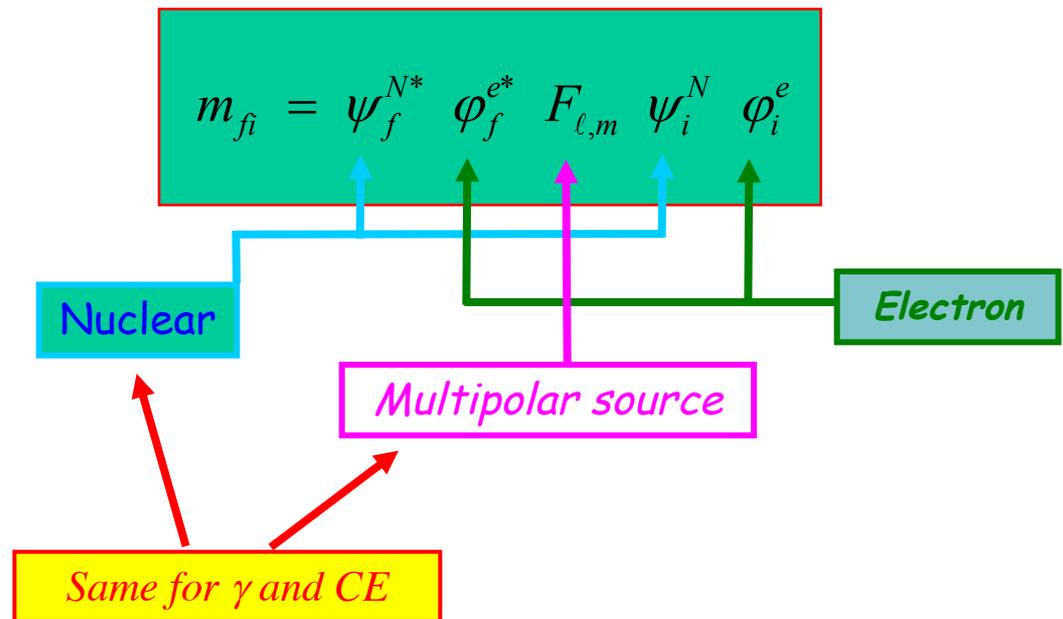
# Conversion electron process and electromagnetic interaction

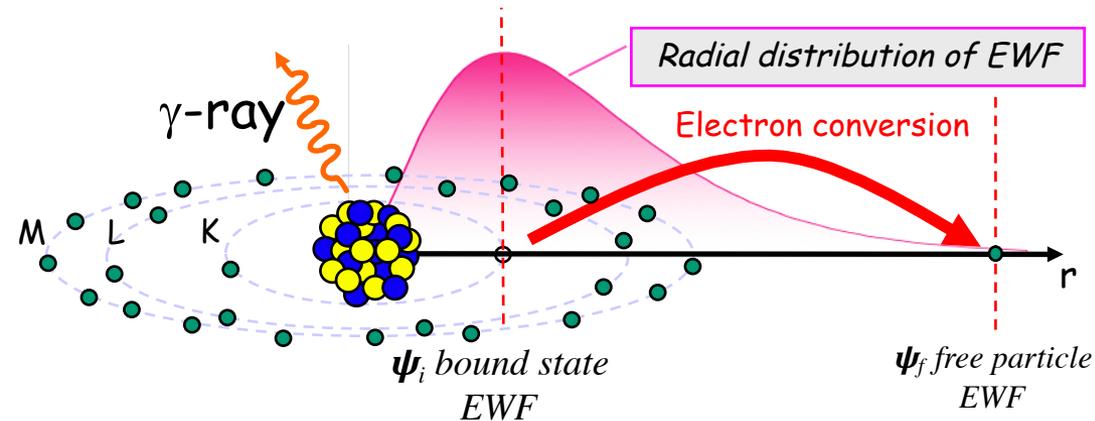


**Fermi's golden rule**

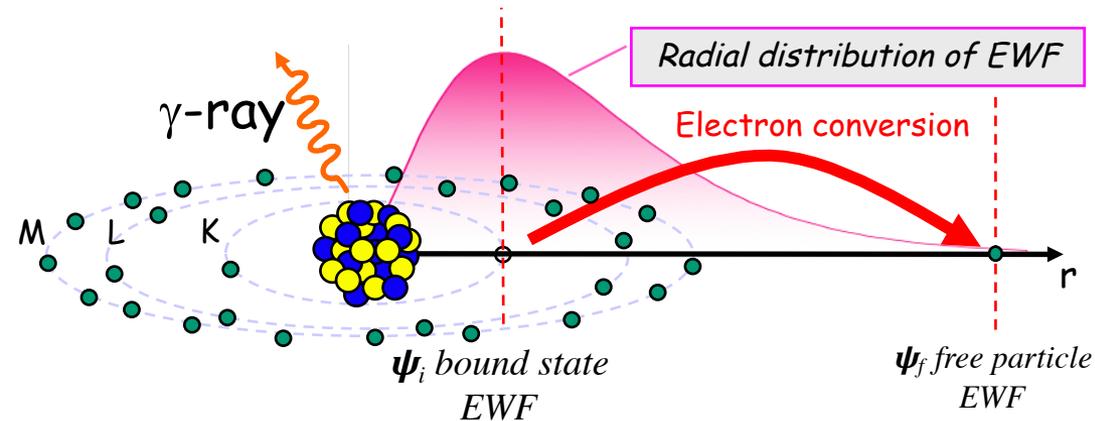
$$\alpha_e = \frac{\lambda_e}{\lambda_\gamma} \Rightarrow \lambda_e = \frac{2\pi}{\hbar} |m_{fi}|^2 \frac{d\rho}{dE}$$

Density of the final electron state (continuum)

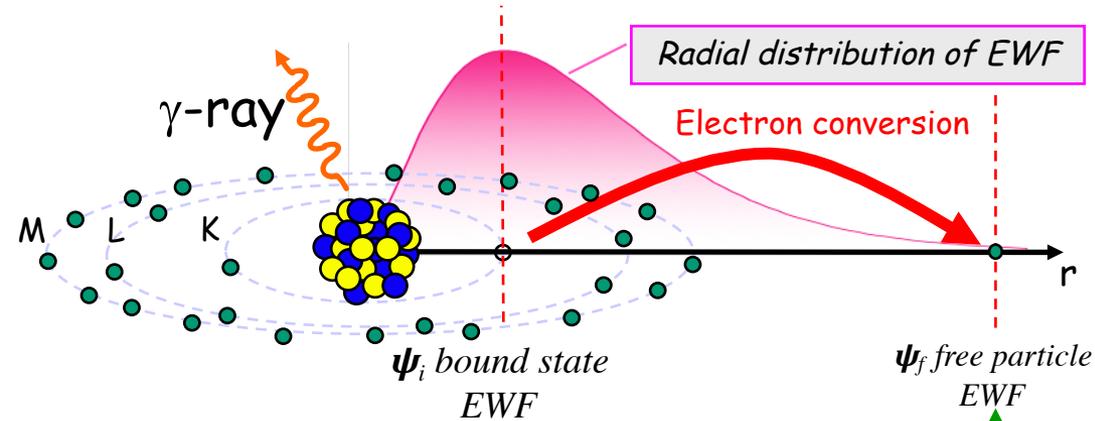




- Relativistic Dirac-Fock method
- One-electron approximation
- Free neutral atom
- Screening of the nuclear field by the atomic electrons
- Spherically symmetric atomic potential
- Relativistic electron wave functions
- Experimental electron binding energies
- Finite nuclear size
- Dynamic (penetration) effects incorporated using the Surface Current model
- Spherically symmetric nucleus; calculations for the most abundant isotope



- Atomic many body correlations: factor  $\sim 2$  for  $E_{\text{kin}}(\text{ce}) < 1 \text{ keV}$
- Partially filled valence shell: non-spherical atomic field
- Binding energy uncertainty:  $< 0.5\%$  for  $E_{\text{kin}}(\text{ce}) > 10 \text{ keV}$
- Chemical effects:  $\ll 1\%$



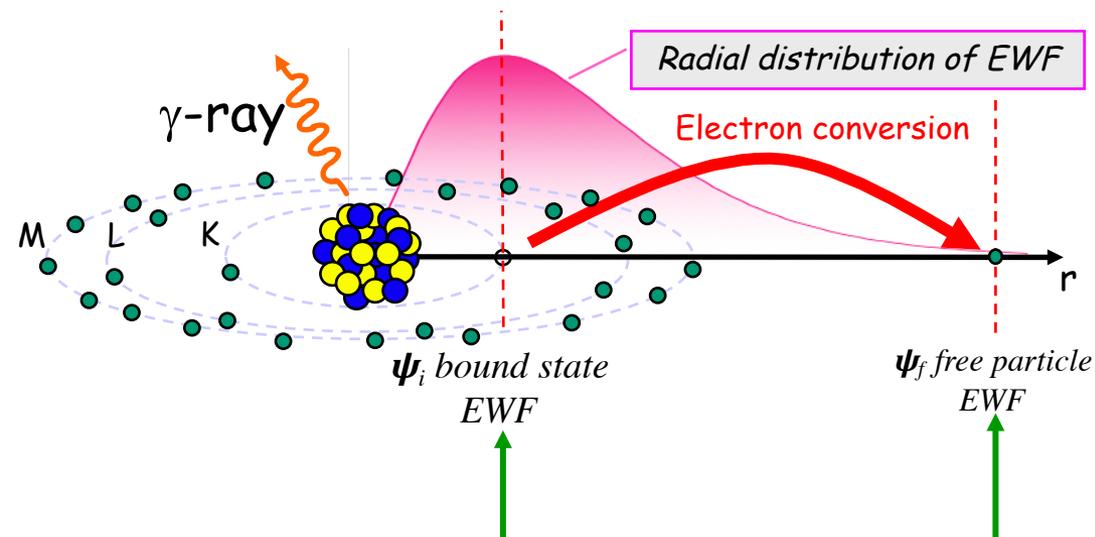
**"No Hole" - BTNTR: SCF of a neutral atom**

*Vacancy disregarded*

*2002Ba85 numerical tables  
(Band et al., ADNDT 81 (2002) 1)*

*BrIccNH table - extended and revised  
calculations*

# ICC calculations - Atomic vacancies



BrIccFO Accuracy:

- 188  $\alpha_{tot}, \alpha_K, \alpha_L$  ICC
- Pure E2, E3, M3 M4 multipolarities (no penetration effect)
- max 10% uncertainty

(Exp-Theor)/Exp  $\sim +0.8\%$

SCF of a neutral atom

Constructed from the WF of a neutral atom, not SCF

**"Frozen Orbitals" - RNIT(2)**

ENSDF pre 2005

Hager and Seltzer

- Hatree-Fock
- Different physical assumptions
- $\sim 4\%$  accuracy

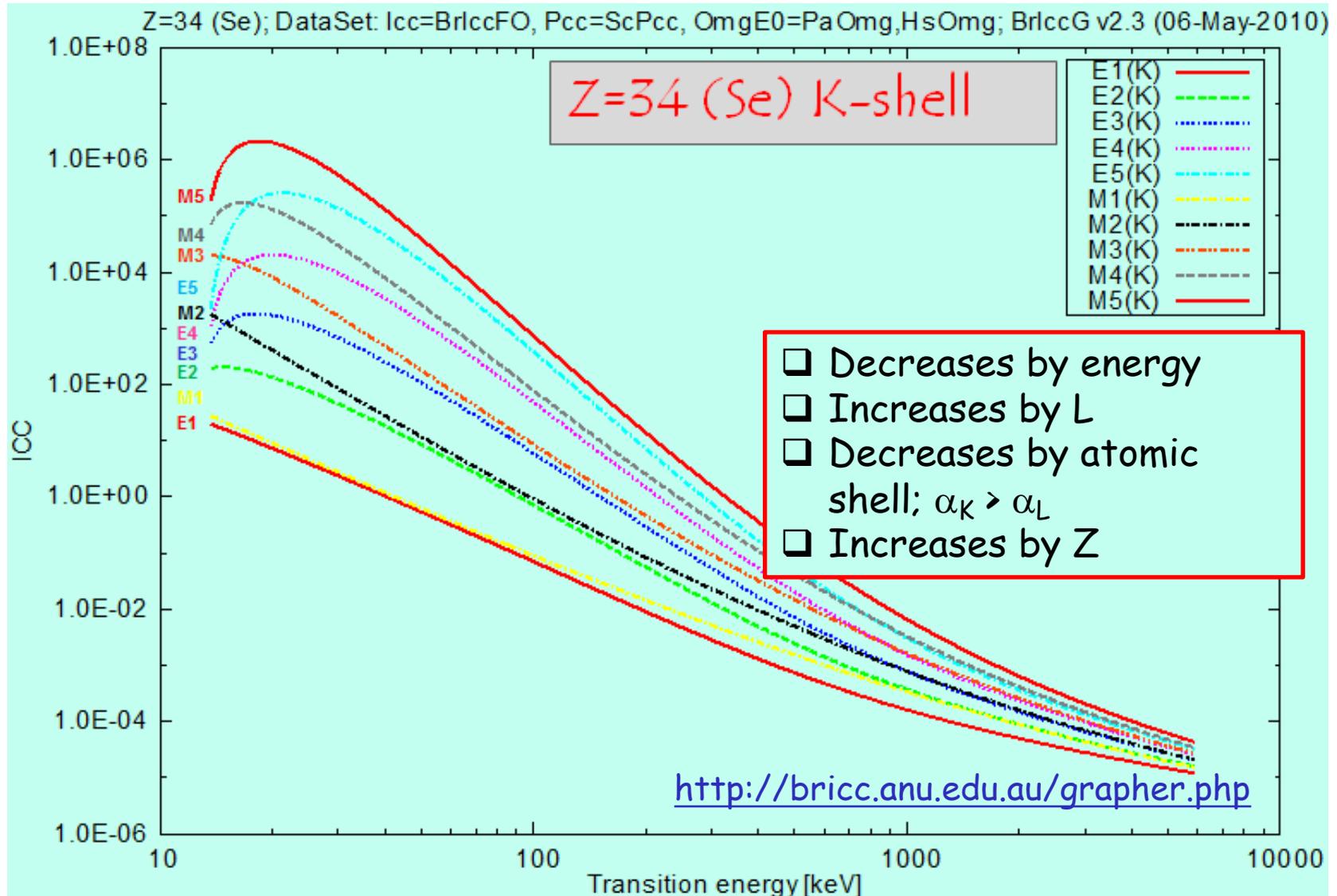
**Vacancy incorporated**

2008Ki07 T. Kibèdi et al., Nucl. Instr. and Meth.

A 589 (2008) 202

**BrIccFO - data table**

# Theoretical conversion coefficients



- ❑ Total transition probability (intensity):  $\lambda_{\text{total}} = I_{\gamma} \times (1 + \alpha_{\text{total}})$
- ❑  $\alpha_i(Z, E_{\gamma}, \pi L, \delta, \lambda)$  function of
  - $i$  - atomic shell / electron-positron pair
  - $Z$  - atomic number
  - $E_{\gamma}$  - transition energy
  - $\pi L$  - multipolarity
  - $\delta$  - mixing ratio
  - $\lambda$  - nuclear penetration parameter (not many cases: E1, M1)
- ❑ Comparing experimental and theoretical conversion coefficients
  - Transition multipolarity (pure/mixed), magnetic or electric character
  - Normalised Peak to Gamma (NPG) method:
 
$$\alpha_{\text{exp}} = N * [A_{\text{CE}}/A_{\gamma}] * [\epsilon_{\gamma}/\epsilon_{\text{CE}}]$$
  - Further details: J.H. Hamilton, *The Electromagnetic Interaction in Nuclear Spectroscopy*, Ch 11, North Holland (1975)
- ❑ E0 transitions - collective excitations and shape co-existence

EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$|L-j_i| \lesssim j_f \lesssim L+j_i$$

$$\pi = (-1)^L \text{ for EL}$$

$$\pi = (-1)^{L+1} \text{ for ML}$$

	$\Delta\pi=+1$		$\Delta\pi=-1$	
$\pi L$	M1	M3	E1	E3
$\pi' L'$	E2	E4	M2	M4

Special case: mixed transitions with 3 multipolarities:

$^{184}\text{W}$  536.674(15) keV

E1+M2+E3,

ME(M2/E1)=+0.070(6),

MR(E3/M2)=-0.025(4)

$\lambda=-2.1(2)$ ;

Example:  $2^+$  to  $1^+$  transition,  $\Delta J=-1$

- pure M1( $\Delta J=-1,0,+1$ )
- pure E2( $\Delta J=-2,-1,0,+1,+2$ )
- mixed M1+E2( $\Delta J=-1,0,+1$ )

$\gamma$ -ray transition probability:

$$\lambda_\gamma(\pi' L' / \pi L) = \lambda_\gamma(\pi' L') + \lambda_\gamma(\pi, L)$$

Mixing ratio (MR)

$$\delta^2(\pi' L' / \pi L) = \frac{\lambda_\gamma(\pi' L')}{\lambda_\gamma(\pi L)}$$

Conversion coefficient for CE and PF

$$\alpha(\pi' L' / \pi L) = \frac{\alpha(\pi L) + \delta^2 \alpha(\pi' L')}{1 + \delta^2}$$

# E0 - electric monopole transitions

EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$j_i = j_f$$

$$\Delta\pi = 0$$

Pure E0

- NO gamma-ray
- Only CE or PF

References:

1997Wo07

J.L. Wood et al.,  
NP **A651** (1999) 323

2005Ki02

T. Kibèdi, R.H. Spear,  
At. Data Nucl. Data Tabl.  
**89** (2005) 77

E0 conversion coefficient NOT DEFINED

$$\alpha(E0) = \lambda_{CE,PF}(E0) / \cancel{\lambda_\gamma(E0)}$$

E0 transition rate

$$\lambda_{CE,PF}(E0) = \rho^2(E0) \Omega_{CE,PF}(E0)$$

$\rho(E0)$  - monopole strength parameter, contains all nuclear structure information

$\Omega_{CE,PF}(E0)$  - theoretical E0 electronic factor (BrIcc)

E0 reduced transition rate

$$B(E0) = \rho^2(E0) e^2 R_0^4$$

Experimental determination

$$\rho^2(E0) = 1 / [\Omega_{CE}(E0) + \Omega_{PF}(E0)] \times \tau(E0)$$

# E0+E2+M1 - mixed transitions

EM decay: energy and momentum carried away

Selection rules ( $\pi L$ )

$$j_i = j_f$$

$$\Delta\pi = 0$$

2+ to 2+ transition

- Can proceed with E0 in competition with E2+M1

Transition probability:

$$\lambda(E0+E2+M1) = \lambda_{CE}(E0) + \lambda_{PF}(E0) + \lambda_{\gamma}(E2) + \lambda_{CE}(E2) + \lambda_{PF}(E2) + \lambda_{\gamma}(M1) + \lambda_{CE}(M1) + \lambda_{PF}(M1)$$

MR(E2/M1) mixing ratio

$$\delta^2(E2/M1) = \frac{\lambda_{\gamma}(E2)}{\lambda_{\gamma}(M1)}$$

MR(E0/E2) mixing ratio

$$q_K^2(E0/E2) = \frac{\lambda_K(E0)}{\lambda_K(E2)}$$

Conversion coefficient (K-shell)

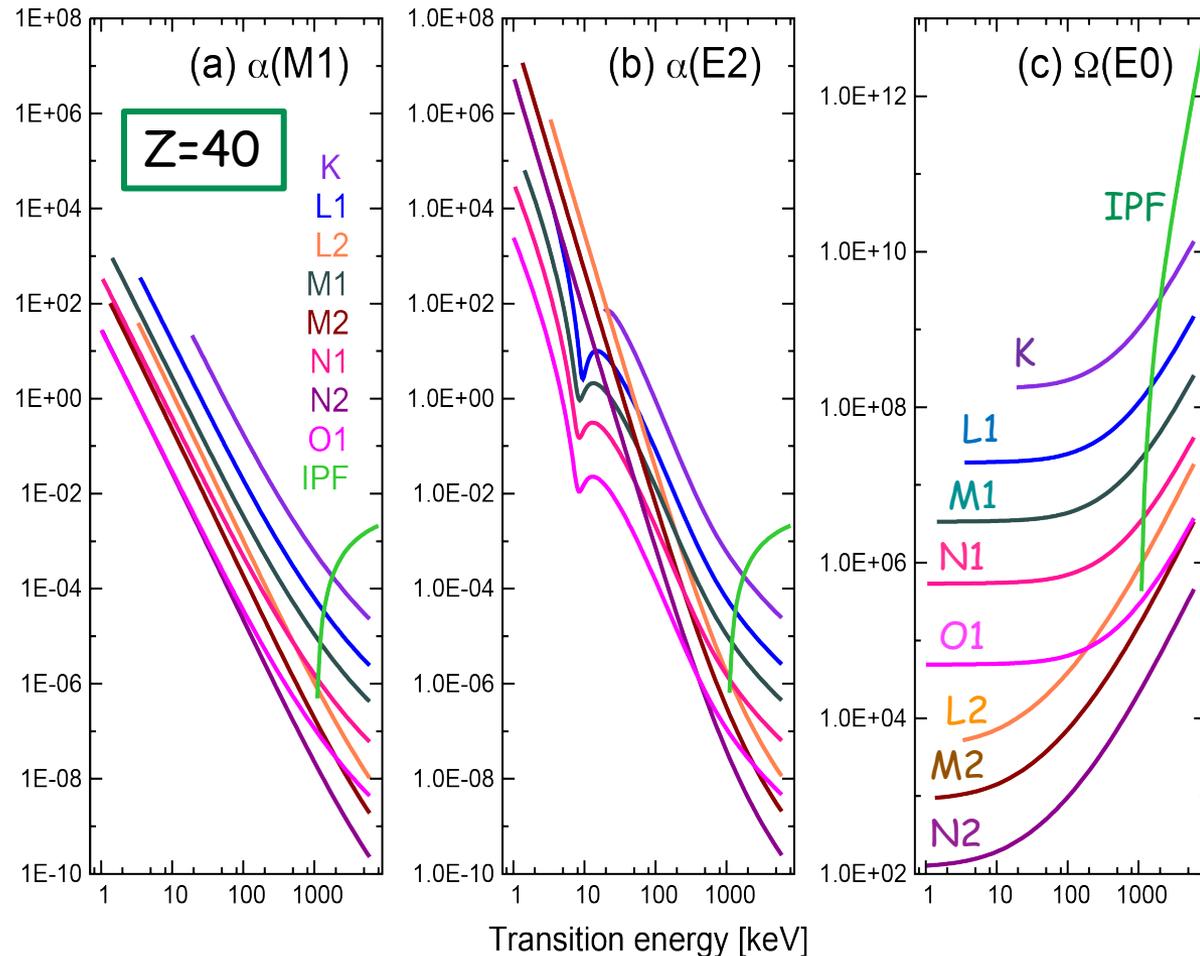
$$\alpha_K(E0 + E2 + M1) = \frac{\alpha_K(M1) + \delta^2 \times [1 + q_K^2] \times \alpha_K(E2)}{1 + \delta^2}$$

$\rho^2(E0)$  can be determined if both E2/M1 and E0/E2 mixing ratios and level half life are known (E0/E2 mixing ratio from  $\alpha_K$ )

# Conversion coefficients and E0 electronic factors using BrIcc

$\alpha(M1,E2)$ : from BrIcc (2008Ki07);  
 $W_{CE,PF}(E0)$ : J. Dowie and T. Eriksen (2018 ANU)

- E0 conversion on  $nS_{1/2}$  and  $nP_{1/2}$  shells only
- Energy dependence
  - $\alpha_{CE}(M1,E2)$ : ↓ up 14 orders of magnitude
  - $\Omega_{CE}(E0)$ : ↑ 2-3 orders of magnitude
  - Opposite trend for pair conversion
- Atomic shells (K, L, M): Always decreasing
- Accuracy of the ICC tables:
  - $\alpha_{CE} \sim 1.4\%$
  - $\alpha_{PF}$  - not evaluated,  $\sim 3\%$
  - $\Omega(E0) \sim 5\%$



# Conversion coefficients and E0 electronic factors using BrIcc

```

125TE G 35.4925 5 6.68 13M1+E2 0.029 +3-2 13.68
125TES G KC=11.69 17$LC=1.596 25$MC=0.319 5$NC+=0.0697 11
125TES G NC=0.0630 10$OC=0.00674 10
125TE cG E$ From wavelength of 349.328 {I5} m~' (1976Mi18) and
125TE2cG conversion factor of 12398.520 keV|m~' from 2000He14
125TE cG RI$ From CC deduced by the evaluator from MR and LAMBDA=0.9 {I8}.
125TE2CG Others: 6.68 {I3} (1990Iw04),
125TE3CG 6.8 {I3} (1969Ka08),
125TE4CG 6.51 {I13} (1983De11)
125TE cG M,MR,LAMBDA,CC$ From
125TE2CG EKC/(1+ECC)=0.80 {I5}, ELC/(1+ECC)=0.11 {I2},
125TE3CG EMC/(1+ECC)=0.020 {I4} (1952Bo16);
125TE4CG CEL2/CEL1=0.089 {I4}, CEL3/CEL1=0.024 {I2} (1965Ge04);
125TE5CG CEK/CEL=12.3 {I25}, CEL2/CEL1=0.106 {I20} (1969Ca01);
125TE6CG EKC=11.78 {I18}, ECC=12.95 {I28} (1969Ka08);
125TE7CG EKC/(1+ECC)=0.804 {I10} (1970Ma51);
125TE8CG ECC=14.25 {I64}, EKC=11.90 {I31}, EM2C/EM1C=0.092 {I5},
125TE9CG EL2C/EL1C=0.082 {I4}, EL3C/EL1C=0.019 {I3} (1979CoZG);125TEaCG
ELC/EMC=5.21 {I26}, EMC/ENC=4.87 {I20}, EM1C/EM3C=33.6 {I55},
125TEbCG EM1C/EN1C=4.68 {I14}, EL1C/EL3C=43.7 {I94} (1982Br16);
125TEcCG ELC=1.4 {I1} (1998Sa55);
125TEdCG EL2C/EL1C=0.083 {I3}, EL3C/EL1C=0.018 {I4}, EM1C/EL1C=0.20{I11},
125TEeCG EM2C/EM1C=0.077 {I20}, EN1C/EM1C=0.20 {I1} (2017TeZW).

```

# Conversion coefficients and E0 electronic factors using BrIcc

## Wednesday Practice #3

- ☐ Gamma records and conversion coefficients in ENSDF
- ☐ How to use BrIcc & BrIccMixing

Skip Navigation | ANU Home | Search ANU | RSPHysSE | Nucl. Phys. Home



**Department of Nuclear Physics**

Research School of Physics and Engineering

**BrIcc**

- BrIcc Home
- BrIcc Grapher
- Quick reference
- Data tables
- Program manual
- Obtaining BrIcc
- Version history
- Authors

**Nuclear Structure Links**

- ANU Nuclear Physics
- National Nuclear Data Center
- IAEA Nuclear Data Centre
- NSDD network
- DDEP network

### BrIcc v2.3S

**Conversion Coefficient Calculator**

Z (atomic number or symbol)

γ-energy (in keV)  
 Uncertainty

Enter (optional) uncertainty in energy as **x** or **+x-y**

**Multipolarity**  
 δ  Uncertainty

Enter (optional) uncertainty in δ as **x** or **+x-y**

Show Subshells  Data Set

---

**BrIccS v2.3 (9-Dec-2011)**  
**Z=62 (Sm, Samarium)**  
**γ-energy: 1005.27 (+5 -5) keV**  
**Mixing Ratio δ: -3.2 (+3 -2)**  
**Data Sets: BrIccFO**

**Warning**

- ICC could not be calculated for EG+DEGH above 398.000 keV

Shell	E(ce)	M1	E2	Mixed ICC
Tot		3.888E-03	2.459E-03	0.00259 (5)
K	958.44	3.326E-03	2.085E-03	0.00220 (4)
L-tot	997.61	4.423E-04	2.938E-04	0.000307 (5)
K/L		7.521E+00	7.099E+00	7.15 (17)
M-tot	1003.58	9.440E-05	6.306E-05	6.59E-5 (11)
L/M		4.685E+00	4.659E+00	4.66 (11)
N6	1005.26			
N-tot	1004.94	2.141E-05	1.425E-05	1.488E-5 (25)
L/N		2.066E+01	2.062E+01	20.6 (5)
O-tot	1005.23	3.227E-06	2.111E-06	2.21E-6 (4)
L/O		1.371E+02	1.392E+02	139 (4)
P-tot	1005.27	2.058E-07	1.239E-07	1.312E-7 (24)
L/P		2.150E+03	2.370E+03	2.34E3 (6)

Reference:  
[2008KI07](#) T. Kibédi, T.W. Burrows, M.B. Trzhaskovskaya, P.M. Davidson, C.W. Nestor, Jr.  
*'Evaluation of theoretical conversion coefficients using BrIcc'*  
Nucl. Instr. and Meth. A 589 (2008) 202-229

# Atomic radiations from nuclear decay

$\varepsilon$  radiations

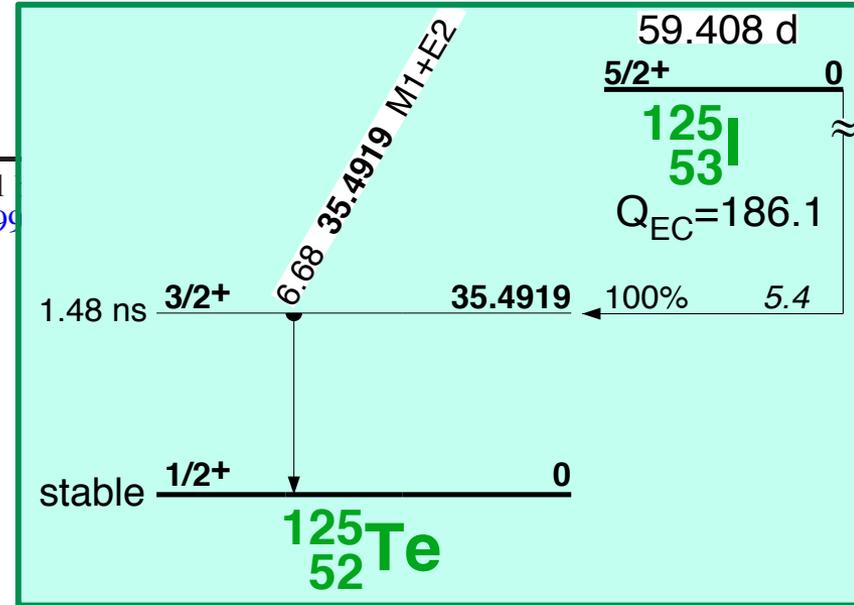
$E(\text{decay})$	$E(\text{level})$	$I\varepsilon^\dagger$	$\text{Log } ft$
150.27 6	35.4925	100	5.4171 5

$E(\text{decay})$ : Deduced from internal  
(1986Bo46), 143.8 keV 20 (199  
 $\varepsilon K(\text{exp})=0.83 4$  (1996Ka48).

$^\dagger$  Absolute intensity per 100 decays.

$\gamma(^{125}\text{Te})$

$I_\gamma$  normalization: From  $I_\gamma(35\gamma)=6.68 13$  per decay, no  $\varepsilon$  feeding to g.s.



$E_\gamma$	$I_\gamma^\dagger$	$E_i(\text{level})$	$J_i^\pi$	$E_f$	$J_f^\pi$	Mult.	$\delta$	$\alpha^\ddagger$	Comments
35.4925 5	6.68 13	35.4925	$3/2^+$	0.0	$1/2^+$	M1+E2	0.029 +3-2	13.68	$E_\gamma$ : From wavelength of 349.328 5 mÅ (1976Mi18) and conversion factor of 12398.520 keV×mÅ from 2000He14. $I_\gamma$ : From 1990Iw04. Others: 6.8 3 (1969Ka08), 6.51 13 (1983De11). $\delta$ : Recommended values from 1977Kr13; $\delta=0.029 3$ (1982Br16). Mult.: From $\alpha(K)\text{exp}=12.0 4$ , $\alpha(\text{exp})=13.7 6$ (1969Ka08); L1:L2:L3=100 1:9.54 18:2.3 5 (1982Br16); see also 1982Br16 for other subshell $\alpha$ .

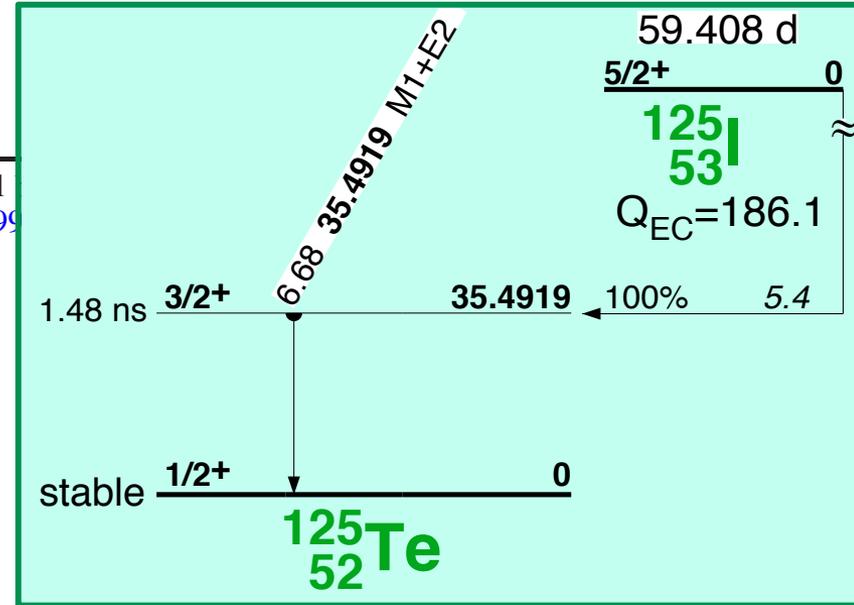
# Atomic radiations from nuclear decay

$\varepsilon$  radiations

$E(\text{decay})$	$E(\text{level})$	$I\varepsilon^\dagger$	$\text{Log } ft$	
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35.4925 5	6.68 13	35.4925	3/2 <sup>+</sup>	0.0	1/2 <sup>+</sup>	M1+E2	0.029 +3-2	13.68	<p><math>E_\gamma</math>: From wavelength of 349.328 5 mÅ (1976Mi18) and conversion factor of 12398.520 keV×mÅ from 2000He14.</p> <p><math>I_\gamma</math>: From 1990Iw04. Others: 6.8 3 (1969Ka08), 6.51 13 (1983De11).</p> <p><math>\delta</math>: Recommended values from 1977Kr13; <math>\delta=0.029 3</math> (1982Br16).</p> <p>Mult.: From <math>\alpha(K)\text{exp}=12.0 4</math>, <math>\alpha(\text{exp})=13.7 6</math> (1969Ka08); L1:L2:L3=100 1:9.54 18:2.3 5 (1982Br16); see also 1982Br16 for other subshell <math>\alpha</math>.</p>

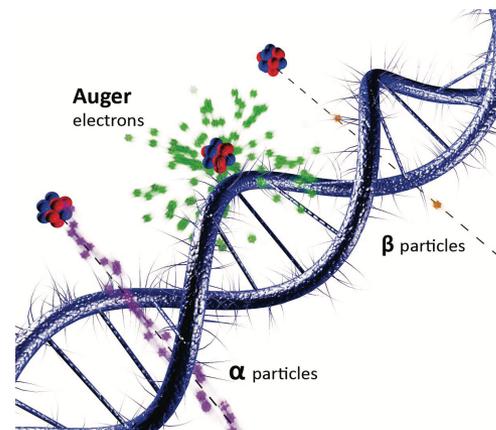
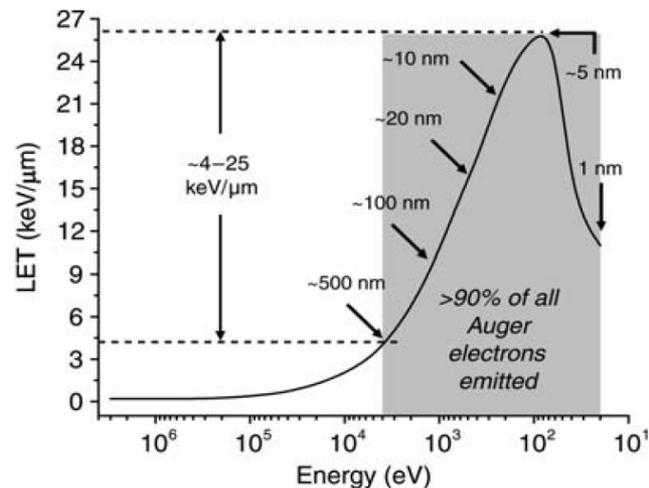
- EC decay of  $^{125}\text{I}$ : 1.0 atomic vacancy/decay
- CE decay of the 35.5 keV decay: 0.93 atomic vacancy/decay

X-rays & Auger electrons from the atomic relaxation process are NOT (yet) in ENSDF

# The biological effect of Auger electrons

Interaction of ionizing radiation:

- ❑ Spectrum of energy loss
- ❑ Generation of secondary electrons
- ❑ Low energy electrons are the ideal tool
- ❑ Auger electrons from radioisotopes - decay at close proximity to the DNA



# The biological effect of Auger electrons

Interaction of ionizing radiation:

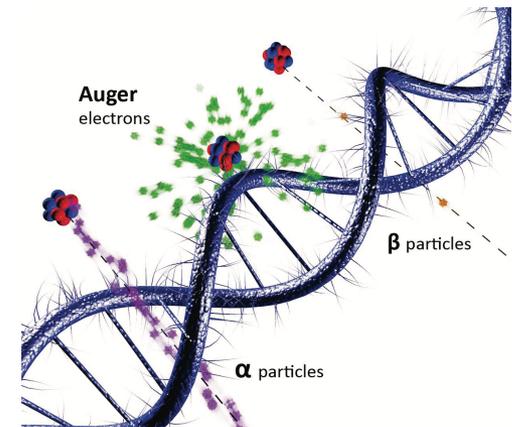
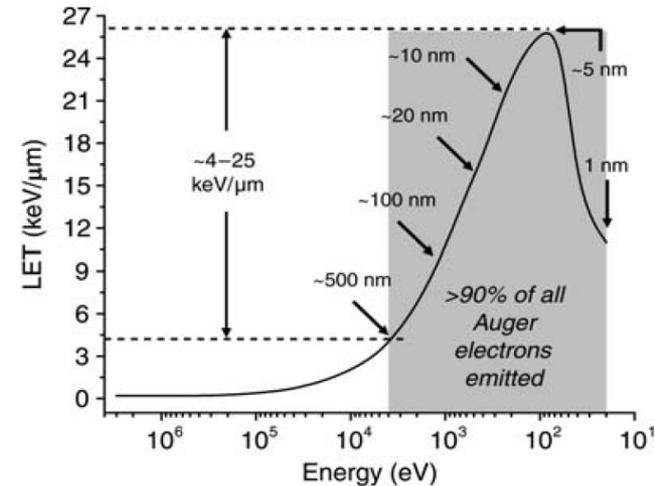
- Spectrum of energy loss
- Generation of secondary electrons
- Low energy electrons are the ideal tool
- Auger electrons from radioisotopes - decay at close proximity to the DNA

## Which Isotope?

- Number of electrons per decay
- Ratio of X &  $\gamma$  vs.  $e^-$  &  $\beta$
- Physical vs. effective half life
- Suitable radiochemistry

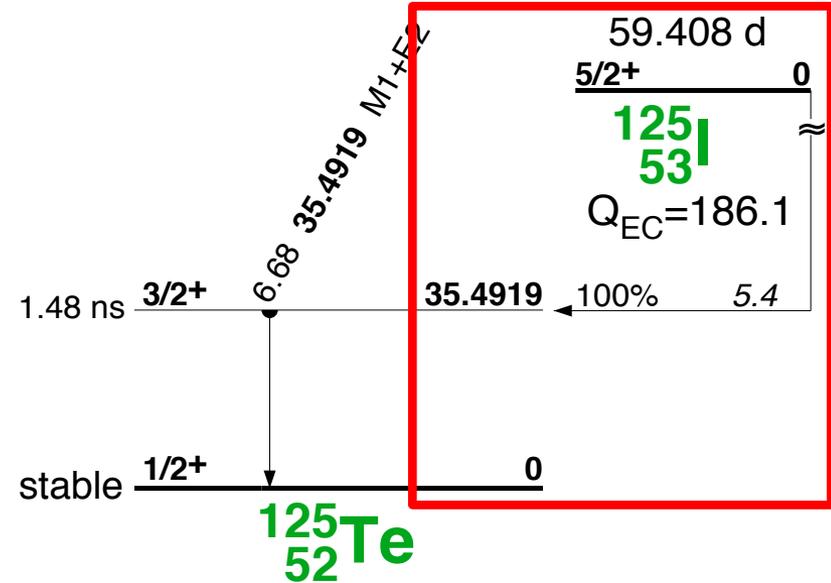
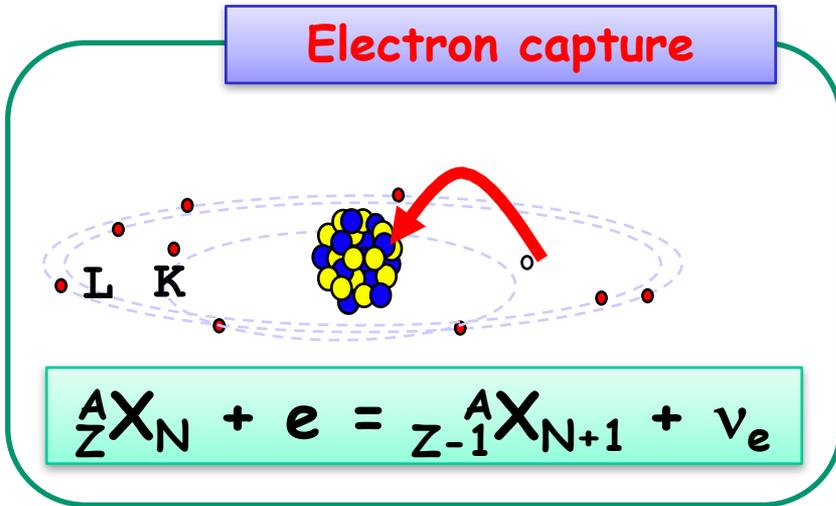
## Physics input to dose calculations:

- Radiation spectra
- Energy loss



# Auger electron yields - how well are known?

	RADAR	DDEP	Eckerman & Endo (2007)	Howell (1992)	Stepanek (2000)	Pomplun (2012)
$^{99m}\text{Tc}$ (6.007 h)	0.869	0.13	4.363	4.0		2.5
$^{111}\text{In}$ (2.805 d)	1.136	1.16	7.215	14.7	6.05	
$^{123}\text{I}$ (13.22 h)	1.064	1.08	13.71	14.9		6.4
$^{125}\text{I}$ (59.4 d)	1.77	1.78	23.0	24.9	15.3	12.2
$^{201}\text{Tl}$ (3.04 d)	0.773	0.614	20.9	36.9		
<b>Vacancy propagation</b>	<b>Deterministic</b>	<b>Deterministic</b>	<b>Deterministic (+++)</b>	<b>Monte Carlo with charge neutralization</b>	<b>Monte Carlo</b>	<b>Monte Carlo</b>



Electron capture rates:

$$P_K + P_L + P_M + P_N + P_O + P_{\beta^+} = 1$$

Tables:  $3 \leq Z \leq 103$ ; E. Schönfeld, PTB-6.33-95-2 (1995)

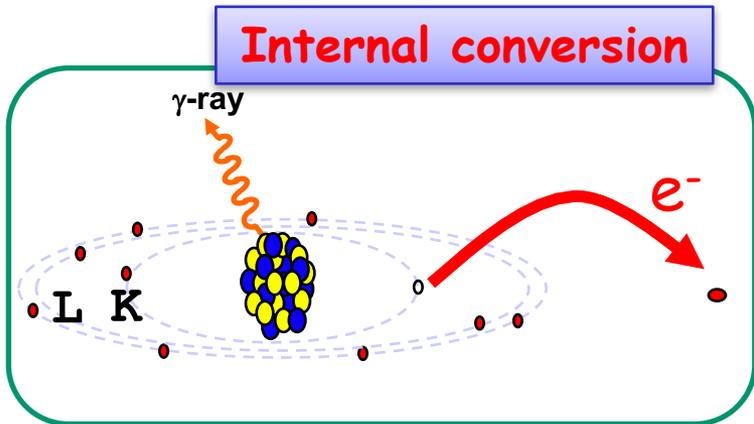
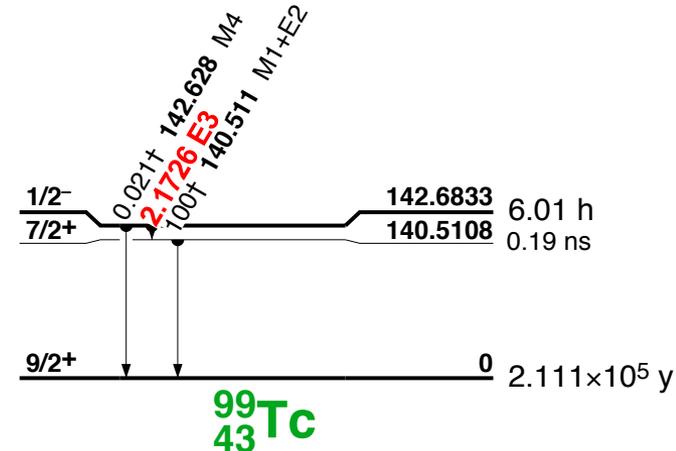
Calculation of subshell ratios: E. Schönfeld,  
Appl. Rad. And Isot. 49 (1998) 1353

Accuracy:  $P_K$ : 0.3%,  $P_L$ : 3%, subshell ratios: up to 25%

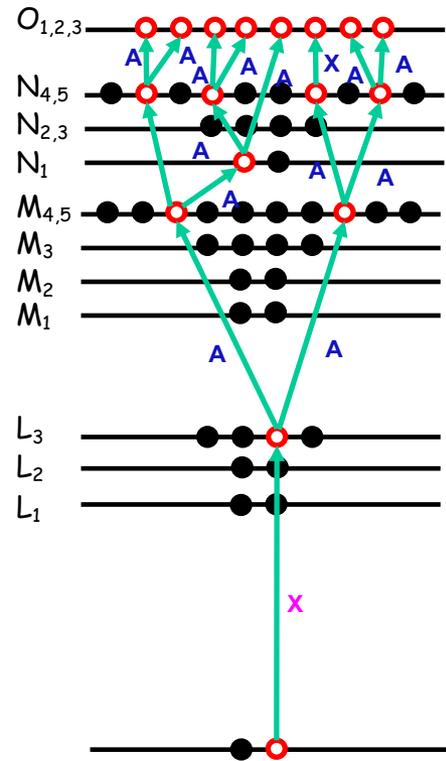
# BrIcc - Internal conversion coefficients

Shell	E(ce)	E3
Tot		1.370E10 (20)
M1	1.63	2.26E6 (4)
M2	1.73	3.37E9 (5)
M3	1.75	5.98E9 (9)
M4	1.92	1.100E9 (16)
M5	1.92	1.655E9 (24)
M-tot	1.78	1.211E10 (17)
N1	2.10	5.00E5 (7)
N2	2.13	4.92E8 (7)
N3	2.14	8.77E8 (13)
N4	2.17	9.11E7 (13)
N5	2.17	1.350E8 (19)
N-tot	2.14	1.596E9 (23)
O1	2.17	3.49E4 (5)
O-tot	2.17	3.49E4 (5)

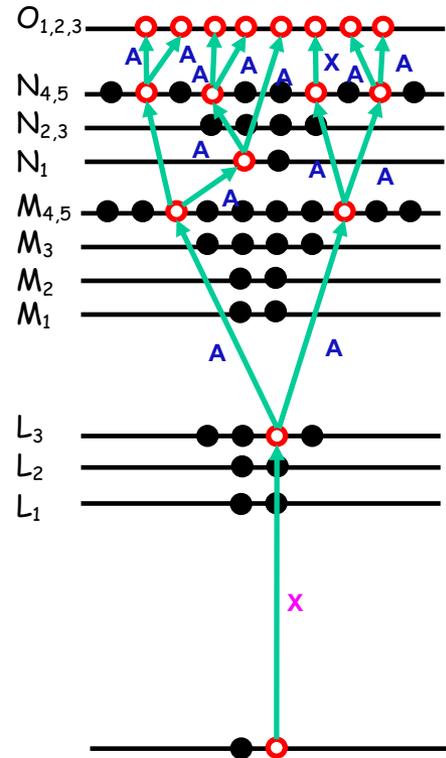
Conversion coefficient  
=  $N(e^-)/N(\gamma)$



- Relativistic Dirac-Fock atomic model;  
Band et al. ADNDT 81 (2002) 1
- Frozen orbital approximation
- ICC ~1.3% accurate
- Z=5-110; 1-6000 keV; E1-E5, M1-M5, All subshells; Electron/Pair ICC, E0
- Tabulations:  
Z=5-110: T. Kibedi, et al, NIM A589 (2008) 202  
Z=111-126: T. Kibedi, et al, ADNDT 98 (2012) 313



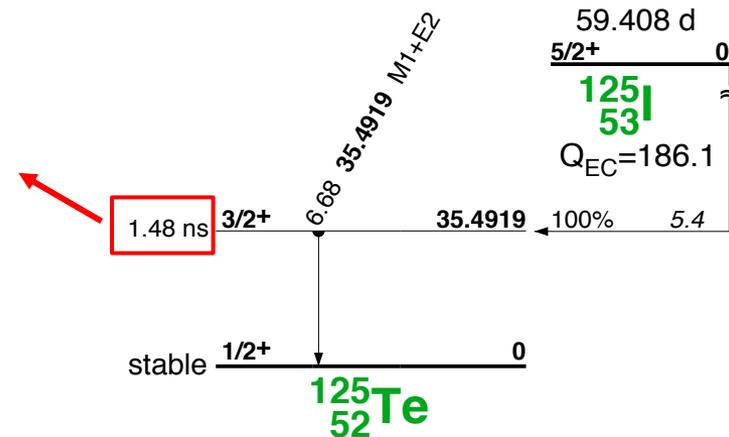
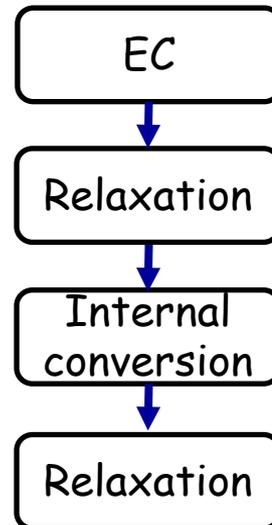
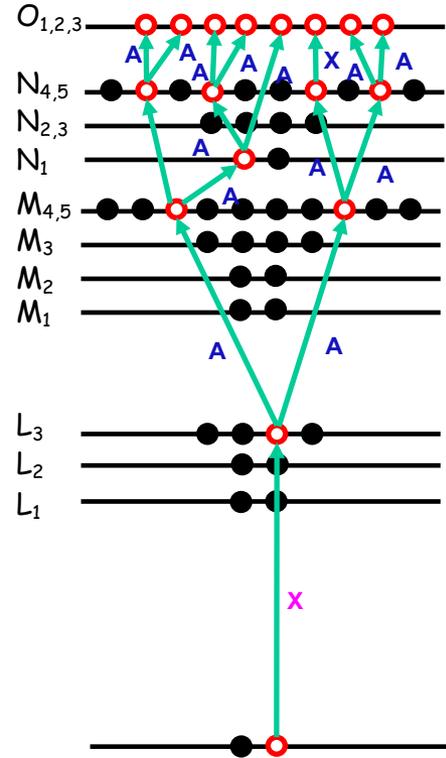
- ❑ Transition energies from Dirac-Fock atomic model
  - ❖ RAINE code (Band 2002)
  - ❖ No QED or Breit corrections; energies overestimated
- ❑ Transition rates from EADL (Perkins 1991)
  - ❖ Calculated for single initial vacancies
  - ❖ Krause-Carlson statistical correction, PR 158 (1967) 18
  - ❖ No shaking or double Auger process



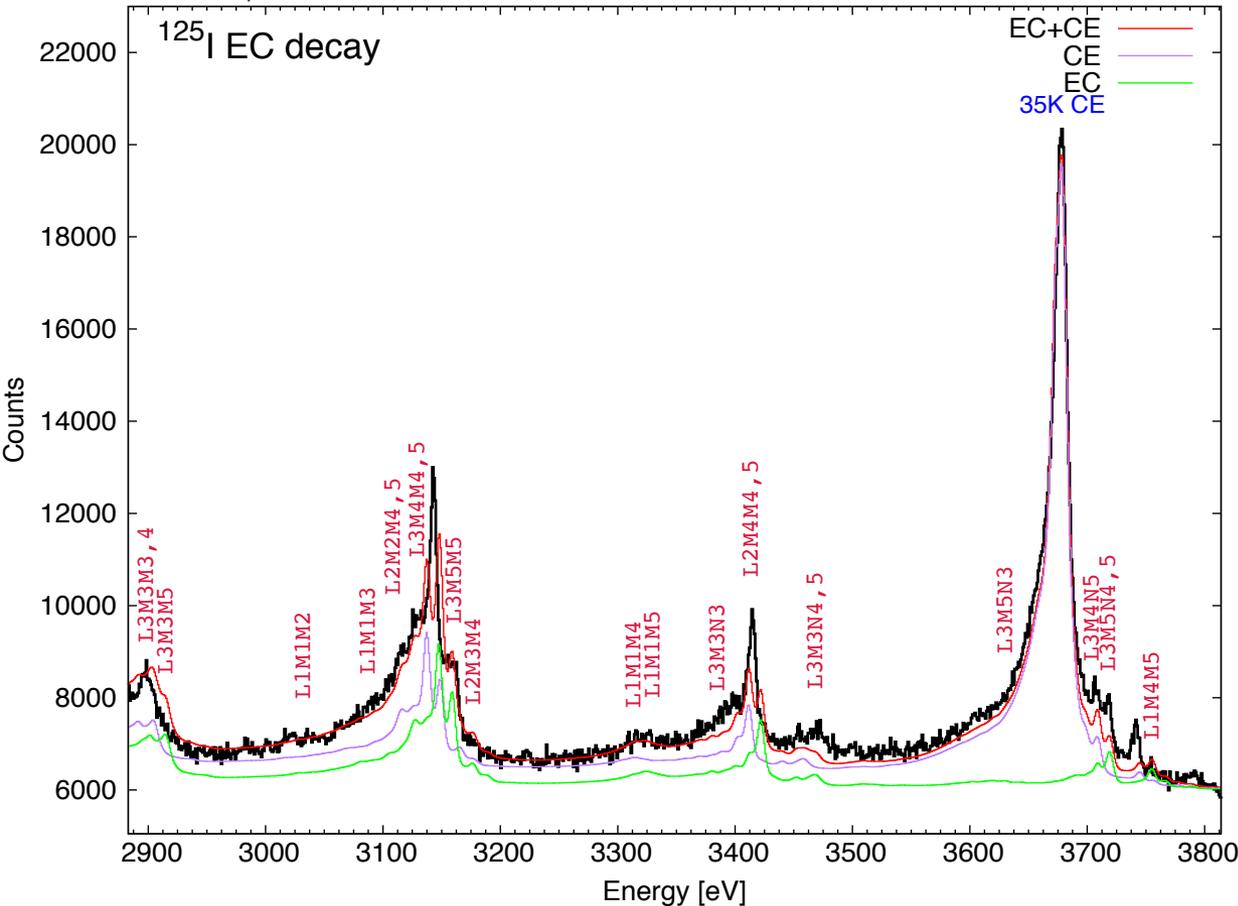
- X-ray or Auger electron emission to fill vacancy
- Multi step, stochastic process; Monte Carlo
- Transition energies and transition probabilities are needed for every propagation step
- Transition energies from Dirac-Fock atomic model
- Transition rates from EADL (Perkins 1991)
- Krause-Carlson correction to transition rates to take into account multiple vacancies
- STOP: Vacancy in valence shell / no transition is possible

# BrIccEmis - Fast vs. Slow neutralisation

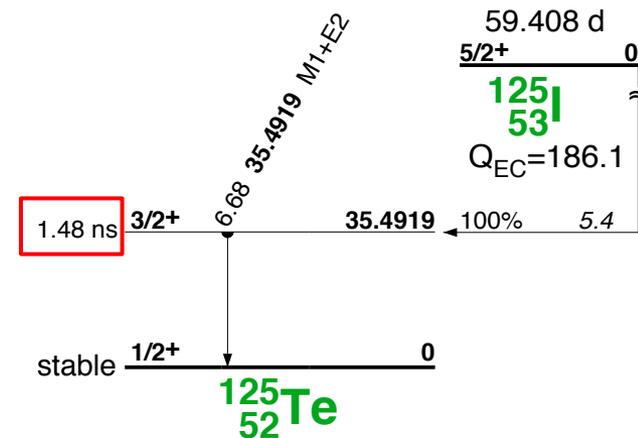
- ❑ Is the atom ISOLATED or in CONDENSED PHASE?
- ❑ Auger cascade very fast:  $10^{-14}$  to  $10^{-16}$  s
- ❑ Condensed phase: vacancies filled from environment (Charlton and Booz 1981, Humm 1984, Howell 1992)
- ❑ Neutralization is a slow process (Pomplun 2012)
- ❑ BrIccEmis: fast or slow neutralization option  
Correct treatment: condensed physics model



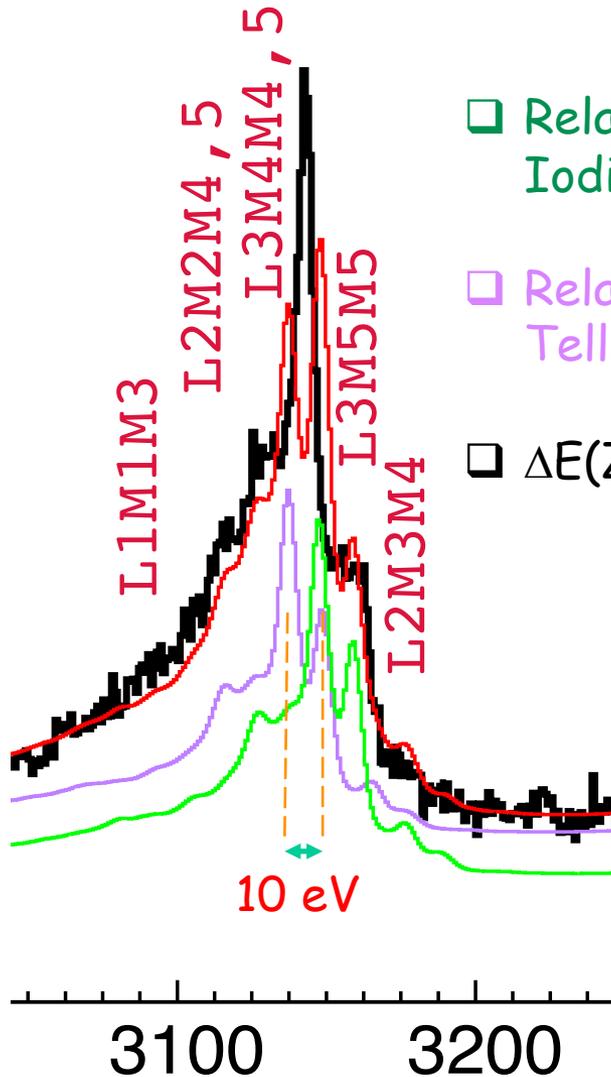
# Benchmarking BrIccEmis using low energy electron measurements



- ❑ Monolayer source, FWHM=7 eV! (with M. Vos, ANU 2018)
- ❑ See Bryan Tee's talk on Friday



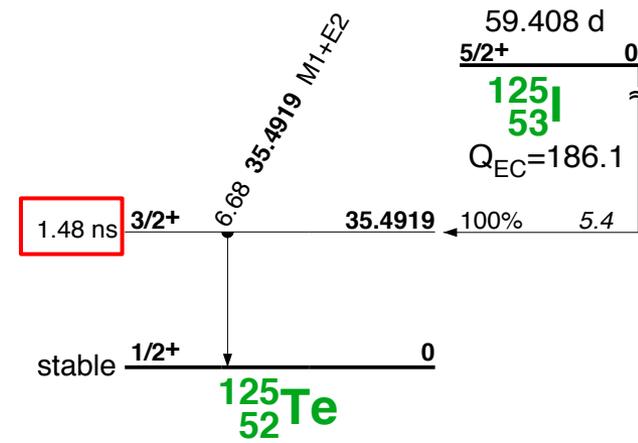
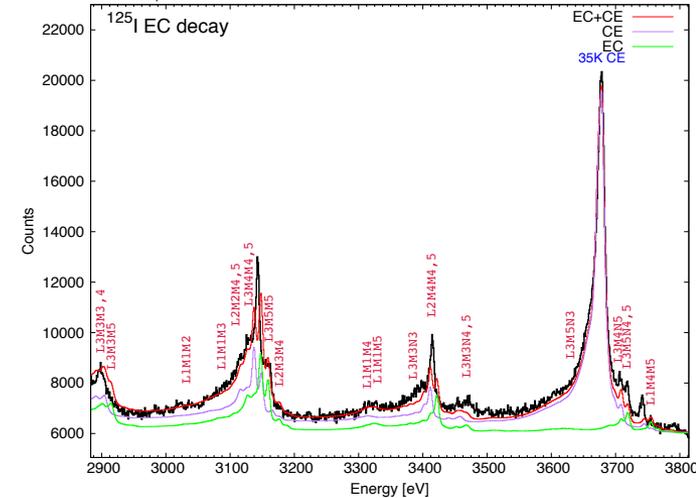
# Benchmarking BrIccEmis using low energy electron measurements



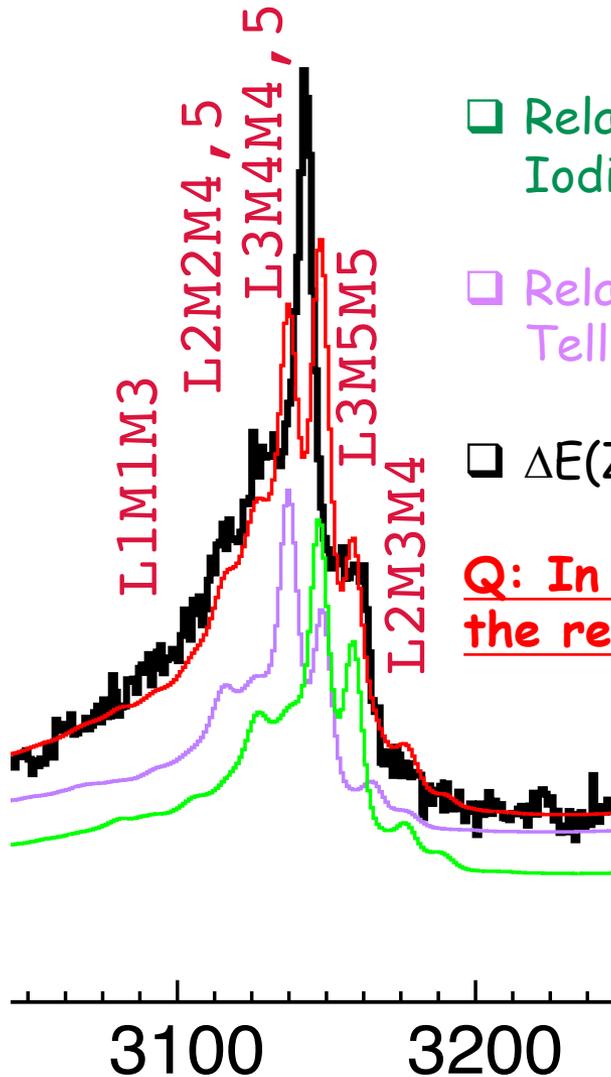
□ Relaxation following EC in Iodine (Z=53)

□ Relaxation following CE in Tellurium (Z=52)

□  $\Delta E(Z=53 \text{ vs } Z=52) \sim 10 \text{ eV}$



# Benchmarking BrIccEmis using low energy electron measurements

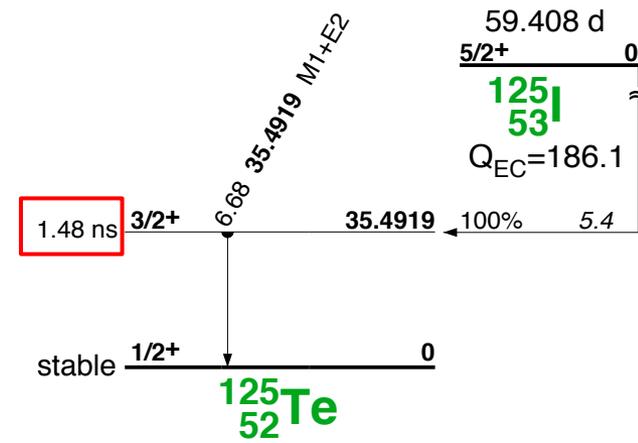
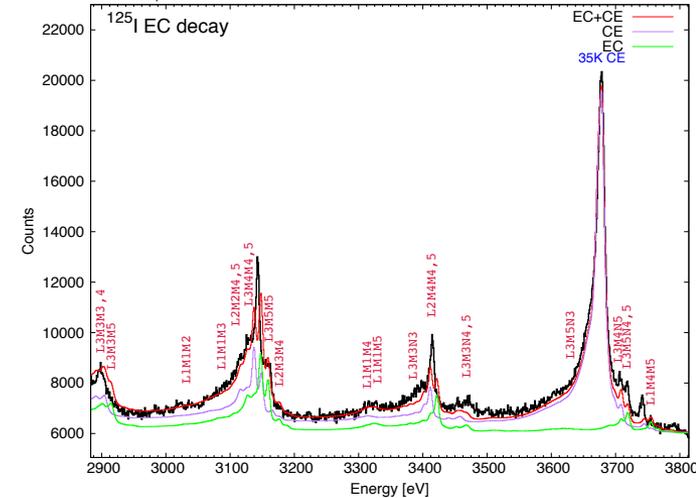


□ Relaxation following EC in Iodine (Z=53)

□ Relaxation following CE in Tellurium (Z=52)

□  $\Delta E(Z=53 \text{ vs } Z=52) \sim 10 \text{ eV}$

Q: In which atomic field the relaxation take place



- ❑ BrIccEmis atomic radiations data base and programs - under development
- ❑ NSDD 2017: new ENSDF record types adopted
- ❑  $^{125}\text{I}$ : Energy release keV) per decay:
  - Gamma-Rays: 2.3806
  - CE electrons: 7.0253
  - X-rays: 39.6999
  - Auger electrons: 11.4230

```
# AUGER electrons =====
AUGER transition types:      703
#
# Trans      Mean[eV]      95% Conf. range      Prob. [per decay]
Auger_Tot      575.67      [0.67 : 3549.10]      1.984E+01
Auger_Ktot     24012.13     [21862.97 : 30041.68]  1.919E-01
Auger_KLL      22601.02     [21862.97 : 23073.01]  1.291E-01
Auger_KLX      26542.05     [25891.68 : 27430.52]  5.678E-02
Auger_KXY      30408.86     [29843.69 : 31587.48]  6.024E-03
Auger_Ltot     2779.82      [122.27 : 3992.71]    1.842E+00
CK_LLX         289.40      [65.01 : 549.65]      2.688E-01
Auger_LMM      3050.80     [2480.27 : 3744.61]    1.210E+00
Auger_LMX      3678.37     [3314.78 : 4270.55]    3.395E-01
Auger_LXY      4311.28     [4026.15 : 4851.10]    2.389E-02
Auger_Mtot     328.61      [21.81 : 632.80]      4.507E+00
CK_MMX         100.06      [8.36 : 246.72]       1.310E+00
Auger_MXY      422.29     [263.30 : 648.98]     3.197E+00
Auger_Ntot     16.01      [0.41 : 73.45]        1.330E+01
SCK_NNN        16.25     [0.52 : 55.53]        2.244E+00
CK_NNX         35.73     [0.97 : 108.81]       9.260E-01
Auger_NXY      14.15     [0.40 : 66.52]        1.013E+01

# X-rays =====
X-ray transition types:      73
#
# Trans      Mean[eV]      95% Conf. range      Prob. [per decay]
X-ray tot     25571.24     [3777.51 : 31791.82]  1.553E+00
X-ray Ktot    28138.08     [27297.22 : 31791.86]  1.390E+00
X-ray KL2     27297.23     [27297.22 : 27297.24]  3.998E-01
X-ray KL3     27571.64     [27571.62 : 27571.66]  7.438E-01
X-ray KM      31083.12     [31046.62 : 31099.03]  2.021E-01
X-ray KM2     31046.64     [31046.62 : 31046.65]  6.798E-02
X-ray KM3     31098.99     [31098.95 : 31099.03]  1.327E-01
X-ray KM4     31338.46     [31338.44 : 31338.49]  5.930E-04
X-ray KM5     31349.15     [31349.13 : 31349.18]  8.410E-04
X-ray KN      31798.94     [31791.82 : 31801.93]  4.199E-02
X-ray KN2     31791.84     [31791.82 : 31791.86]  1.410E-02
X-ray KN3     31801.85     [31801.78 : 31801.93]  2.766E-02
X-ray K0      31921.01     [31919.97 : 31921.84]  2.270E-03
X-ray K02     31920.61     [31919.97 : 31921.31]  7.880E-04
X-ray K03     31921.22     [31920.57 : 31921.84]  1.482E-03
X-ray Ltot    3933.22     [3338.04 : 4583.98]    1.480E-01
X-ray Mtot    557.26     [249.90 : 882.17]      7.812E-03
X-ray Ntot    100.36     [76.62 : 166.99]       6.722E-03

# SIMULATED TOTAL ENERGY RELEASED PER DECAY=====
# Trans      Energy [keV]
Gamma-Rays:      2.3806
CE electrons:    7.0253
X-rays:          39.6999
Auger electrons: 11.4230
```