Development of deformation and "smart" valence spaces

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Shell model and deformation

Can the shell model describe deformed structures?

In the last two decades the improvement in computing power together with the development of powerful shell model methods and codes has allowed to describe well deformed nuclear states, provided the number of degrees of freedom (number of valence particles and the model space are not too large.

For this purpose it is essential to identify the smallest valence space that includes the relevant degrees of freedom

The effective interaction

A multipole expansion

$$V_{eff} = V_m + V_M$$

monopole Multipole





 represents a spherical mean field extracted from the interacting shell model
determines the single particle energies and the shell evolution

- correlations
- energy gains



Deformation

The multipole interaction

The multipole interaction is responsible of the collective behaviour

The main components are: Pairing and Quadrupole

Pairing dominates in semi-magic nuclei \rightarrow superfluidity

When quadrupole correlations dominate \rightarrow deformation

Interplay: Monopole and Multipole

The interplay of the monopole with the multipole terms, like pairing and quadrupole, determines the different phenomena we observe.

In particular, far from stability new magic numbers appear and new regions of deformation develop giving rise to new phenomena such as:

- islands of inversion
- shape phase transitions
- shape coexistence
- haloes, etc.

Quadrupole correlations: Shapes and symmetries

The usual model spaces



One is used to think that light and medium nuclei can be described in a single major HO shell



For heavier nuclei, the spin-orbit (SO) on top of the HO takes over and new boundaries appear



fpg

Quadrupole deformation: a simple model

The spherical nuclear field is close to the harmonic oscillator potential.

In the limit of degeneracy of the single-particle energies of a major harmonic oscillator shell, and in the presence of an attractive Q.Q proton-neutron interaction, the ground state of the many-body nuclear system is maximally deformed Elliott SU(3) in the sd shell

So, at low energy, nuclear states tend to maximize the intrinsic quadrupole moment

The single-particle quadrupole moment is:

$$\mathbf{q}_0 = (2n_{\rm z} - n_{\rm x} - n_{\rm y})$$

where the principal quantum number $N = (n_x + n_y + n_z)$





Example in the sd shell

In the *sd* shell N = 2 $N = (n_x + n_y + nz)$ there are 6 possibilities: (2,0,0) (0,2,0) (0,0,2) (1,1,0)(1,0,1)(0,1,1)

$$q_0 = (2n_z - n_x - n_y)$$

 $q_0 = 4, 1, -2$

Intrinsic states are the Slater "determinants" obtained by filling these fourfold (2p + 2n) degenerate "orbits" along the N=Z line

The "intrinsic orbits" in SU3



> start filling from below → prolate deformation
> start filling from above → oblate deformation

Elliott's SU3 works well in the sd shell but fails for upper shells where the SO interaction introduces large energy shifts

SU3 approximate symmetries

Two variants of SU3 apply in specific spaces

Quasi SU3

applies to the lowest $\Delta j = 2$, $\Delta \ell = 2$ orbits in a major HO shell



N=4

Pseudo SU3

applies to a HO space where the largest *j* orbit has been removed.

A.P. Zuker et al., PRC 52, R1741 (1995). Zuker, Poves, Nowacki, Lenzi, PRC 92, 024320 (2015)



Quadrupole moments in Pseudo SU3



We obtain Q₀ by summing those of the single particles/holes in each "orbit"

Quadrupole moments in Quasi SU3



We obtain Q₀ by summing those of the single particles in each "orbit"

Maximizing quadrupole correlations



K=1/2

K = 3/2

K = 5/2

|quasi |SU3 | pseudo |SU3

Particle-hole excitations in the pseudo + quasi space maximize the quadrupole moment.

The quadrupole correlation energy results much larger than the energy cost to promote the particles

Quadrupole moments in N=Z nuclei

Quadrupole moments can be obtained from this simple schemes for different *np-nh* configurations between pseudo and quasi SU3 spaces.

B(E2) values can be deduced and compared to experiment. B(E2: $2^+ \rightarrow 0^+$) = $Q_0^2/50.3$ B(E2: $4^+ \rightarrow 2^+$) = $Q_0^2/35.17$

Non-degenerate single-particle energies erode slightly the quadrupole collectivity.

Shape coexistence in ⁸⁰Zr





Islands of inversion and symmetries

Islands of Inversion at the magic numbers can be understood in terms of dynamical symmetries

quasi

SU3

SU3

pseudo

quasi SU3 pseudo SU3

The region south of ⁶⁸Ni

28

π

 $f_{5/2}$

 $p_{1/2}$

 $p_{3/2}$

 $f_{7/2}$

Deformation and SM in the fpgd space

LNPS interaction: renormalized realistic interaction + monopole corrections

quasi

pseudo

SU3

SU3

⁴⁸Ca core protons: full *pf* shell neutrons: $p_{3/2}, f_{5/2}, p_{1/2}, g_{9/2}, d_{5/2}$

 $g_{9/2}$

40

28

Other effective interactions:
V_{low k}: L. Coraggio et al., PRC 89, 024319 (2014).
A3DA: Tsunoda et al., PRC 89, 031301 (2014).

The N=40 isotones

A change of structure is observed along the isotonic chain in good agreement with the available data

Occupation of intruder orbitals and percentage of p-h in g.s. configurations

Nucleus	vg _{9/2}	$vd_{5/2}$	0p0h	2p2h	4p4h	6p6h	Ecorr
⁶⁸ Ni	0.98	0.10	55.5	35.5	8.5	0.5	-9.03
⁶⁶ Fe	3.17	0.46	1	19	72	8	-23.96
⁶⁴ Cr	3.41	0.76	0	9	73	18	-24.83
62Ti	3.17	1.09	1	14	63	22	-19.62
⁶⁰ Ca	2.55	1.52	1	18	59	22	-12.09

LNPS, PRC 82, 054301 (2010)

Measurement of deformation with radioactive beams

Intermediate-energy Coulomb excitation measurements at NSCL-MSU

These data constitute a stringent test for the effective interaction and give direct information on the collectivity and deformation at N=40

H. L. Crawford et al., PRL 110, 242701 (2013) T. Baugher et al., PRC 86, 011305(R) (2012)

Spectroscopy of Mn isotopes

First level schemes from multi-nucleon transfer reactions using CLARA + PRISMA at LNL

Calculations without the quasi-SU3 partners in the *gds* space were unable to reproduce the data for the neutron-rich isotopes

J.J. Valiente-Dobon et al., PRC 78, 024302 (2008)

Spectroscopy with radioactive beams

⁶³Mn

Excitation energy and lifetimes in agreement with data. T. Baugher et al., PRC 93, 014313 (2016)

More data on heavier Mn isotopes coming soon from RIKEN

Shape coexistence in ⁶⁷Co and ⁶⁸Ni

D. Pauwels et al., PRC 78, 041307 (2008) and PRC 79, 044309 (2009)

> The LNPS interaction is able to reproduce these structures

-0.4

-0.2

0.0

Spheroidal Deformation E₂

0.2

0.4

Shape coexistence in ⁶⁷Co

Triple shape coexistence in ⁶⁸Ni

In first approximation, ⁶⁸Ni has a doubly closed shell structure in the g.s.

The first three 0+ states are predicted to have different shapes

Shell model calculations reproduce well all these structures

See also: Y. Tsunoda et al., Phys.Rev.C 89, 024313(R) (2014), for ⁷⁰Ni, ⁷⁰Co: A.I. Morales et al., PLB 765 (2017) 328 and for ⁷²Ni, A.I. Morales et al., PRC 93, 034328 (2016)

More data on heavier Ni isotopes coming soon from RIKEN

F. Nowacki, LNPS calculations

