

Thermodiffusion of charged nanoparticles dispersed in Ionic Liquids and in mixtures of molecular solvents

**M. Sarkar¹, J. Riedl¹, G. Demouchy^{1,2}, F. Gélébart¹, F. Cousin³,
G. Mériguet¹, V. Peyre¹, E. Dubois¹ and R. Perzynski¹**

¹ Sorbonne Univ., CNRS, PHENIX, F-75005, Paris, France.

² Univ. Cergy-Pontoise, Dpt. de Phys., F-95011, Cergy-Pontoise, France

³ Lab. Léon Brillouin – CE-Saclay, F-91191 Gif-sur-Yvette cedex, France

Outlook

- Background on Magnetic Fluids / Ferrofluids (FF)
- Synthesis methods for dispersing charged NPs
- SAS determination of interparticle interaction
- Forced Rayleigh Scattering (FRS) technics
- Thermophoretic properties of FF in Molecular Solvents
 - FRS at T=295 K
 - Hydroxyl-coated NPs in water and DMSO
 - Citrate-coated NPs in water
 - FRS at T>295K
 - Hydroxyl-coated NPs in water and DMSO
 - Citrate-coated NPs in water
- Thermophoretic properties of FF in Ionic Liquids at T>295 K
 - Citrate-coated NPs in EAN
 - TFSI-SMIM-coated NPs in EMIM-TFSI
- Summary – Perspectives

Target :

Study of thermophoretic effects
in ionic colloidal dispersions

Systems with big ionic species, and a lot of small ones

$\vec{\nabla}T$ induces $\vec{E}_e = S_e \vec{\nabla}T$ thanks to Seebeck effect

and also $\vec{\nabla}n = -n S_T \vec{\nabla}T$ thanks to Soret effect

n : number of NPs per volume unit

Thermophoretic and thermoelectric properties are interconnected

They both depend on \hat{S}_i of all the ionic species (i) in solution

\hat{S}_i : Eastman entropy of transfer of species (i) in the medium
characteristic of their interaction with the external medium

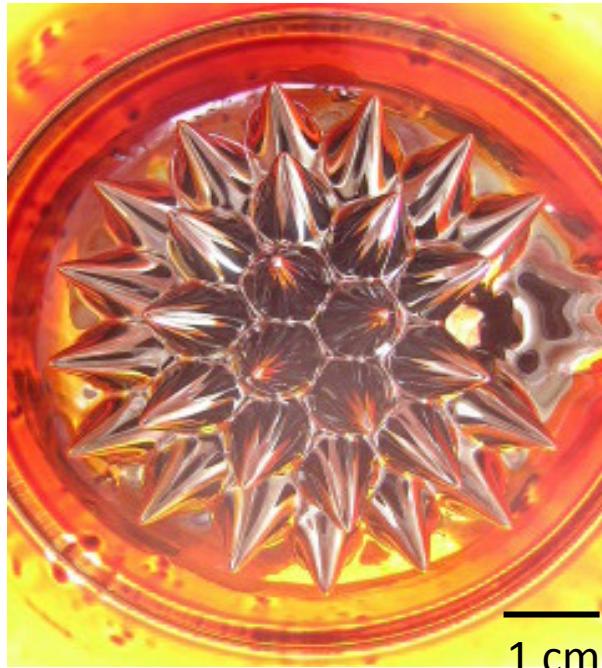
(Heat transport/T)

Thus necessary :

to limit the number of different species, identify them and their n_i ,
to choose media suitable for thermoelectric voltage measurements.

Background on Magnetic Fluids / Ferrofluids (FF)

Colloidal suspensions of magnetic nanoparticles



A material which is fluid and magnetic
with spectacular instabilities and
numerous applications

Automotive : Shock-absorbers (Magnevide®)

Electronic devices : liquid seals for Hard Disks, loudspeakers

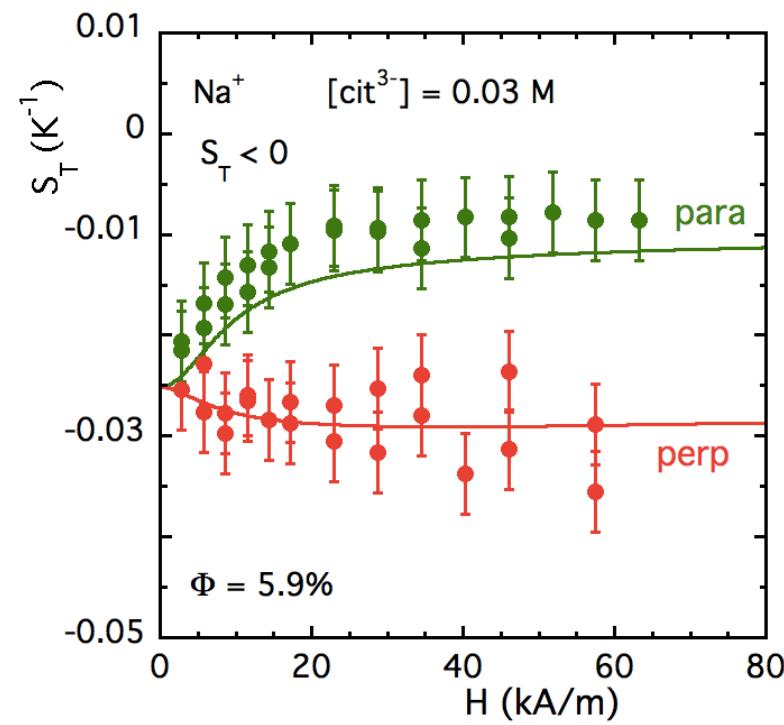
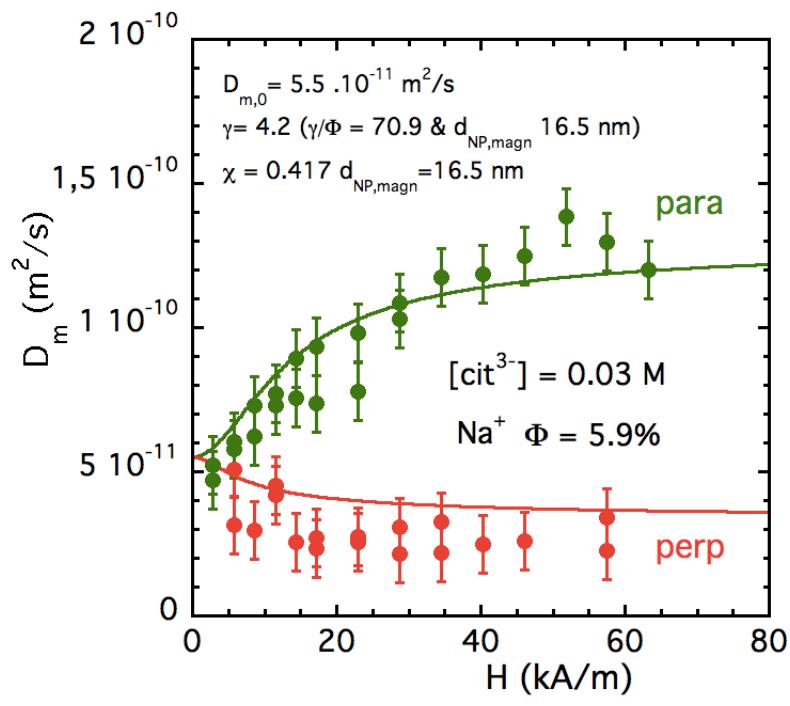
Optics : obturators, modulators

Medecine : MRI contrast agent, antibody titration, cell labelling,

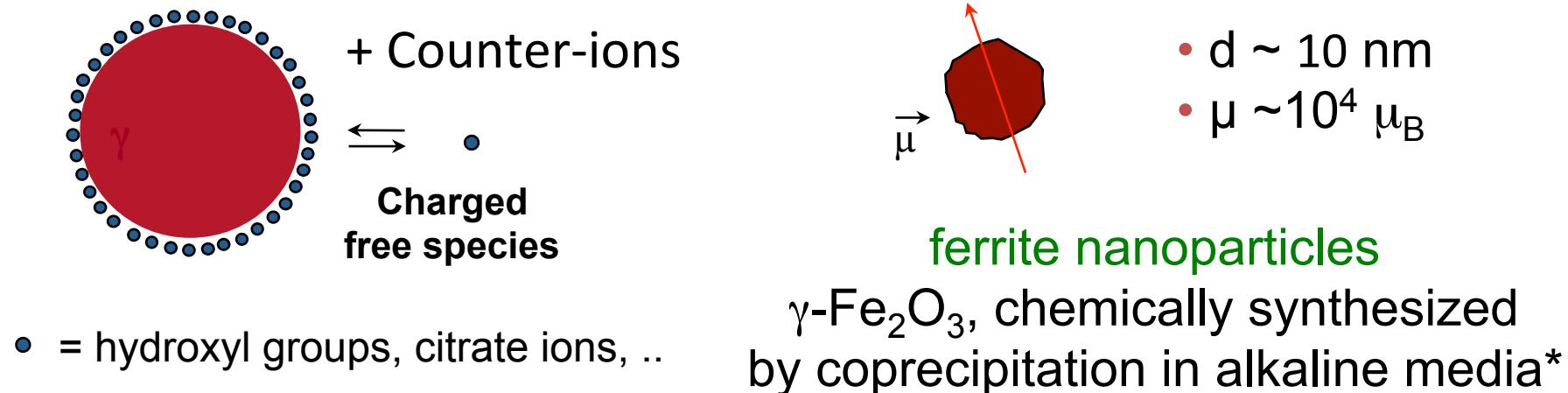
Heat transfer : coolant (Smart-fluids®)

magneto-thermocytolysis, drug delivery

Under-field anisotropy of thermodiffusive and thermophoretic properties



Ionic Magnetic Fluid in water



Ionic stabilization in water:

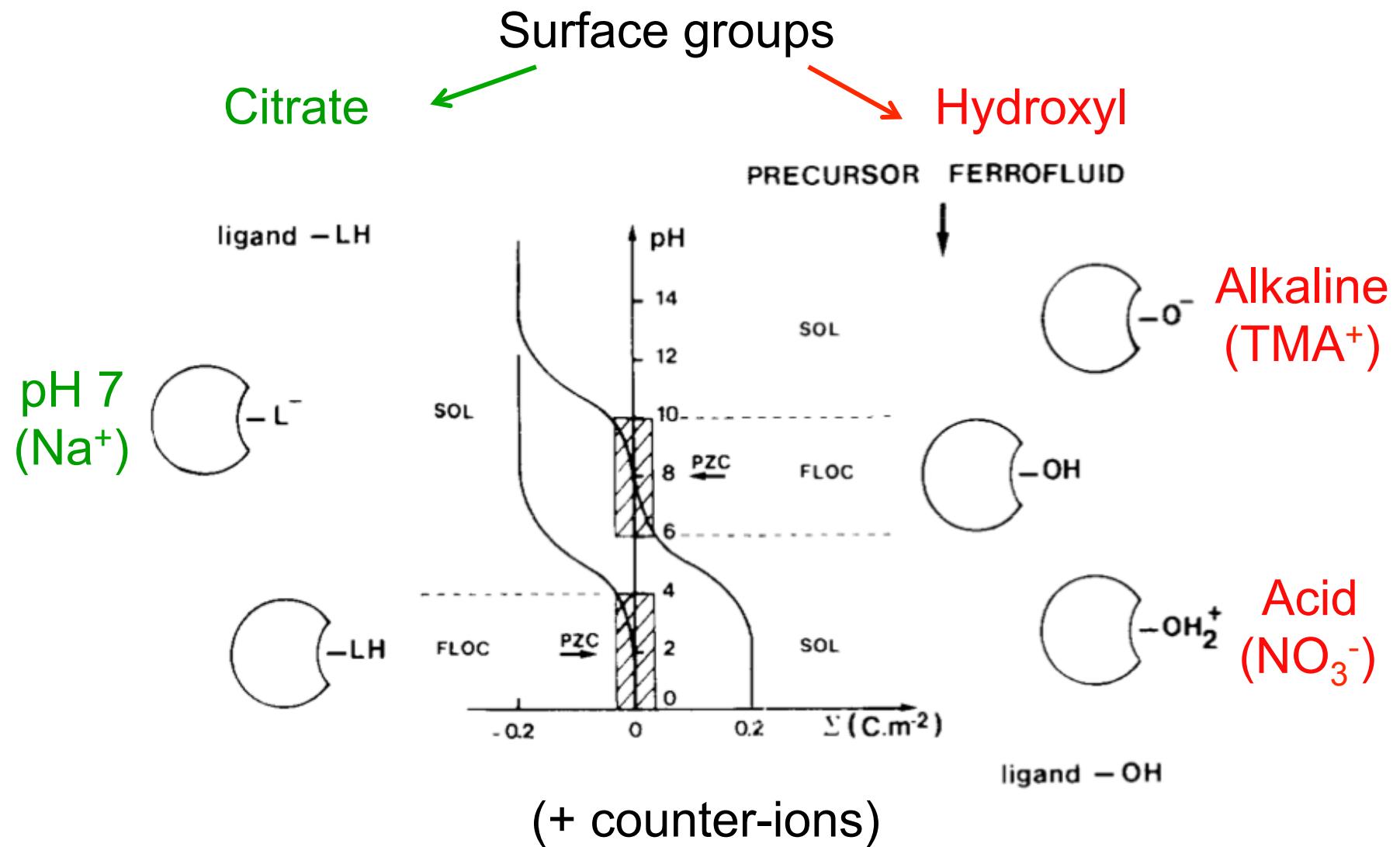
Electrostatic repulsion versus

{ van der Waals attraction
and
magnetic dipolar interaction

R. Massart I.E.E.E. Trans.Mag. Magn. **17** (1981) 1247
F. A. Tourinho et al J. Mat. Sci. **25** (1990) 3249

Aqueous dispersions of ferrite nanoparticles

Evolution of the structural charge with pH and coating



Synthesis method
for dispersing charged NPs
in polar solvents
(Molecular Solvents or Ionic Liquids)

What is needed in this study ?

- (i) Prepare and stabilize FF in a reproducible manner, precisely controlling the nature and the quantity of ions in the solution
- (ii) Prepare them in different media
(DMSO, various Ionic Liquids, ..),
- (iii) Test different types of contreions
(... specific effects of counterions)

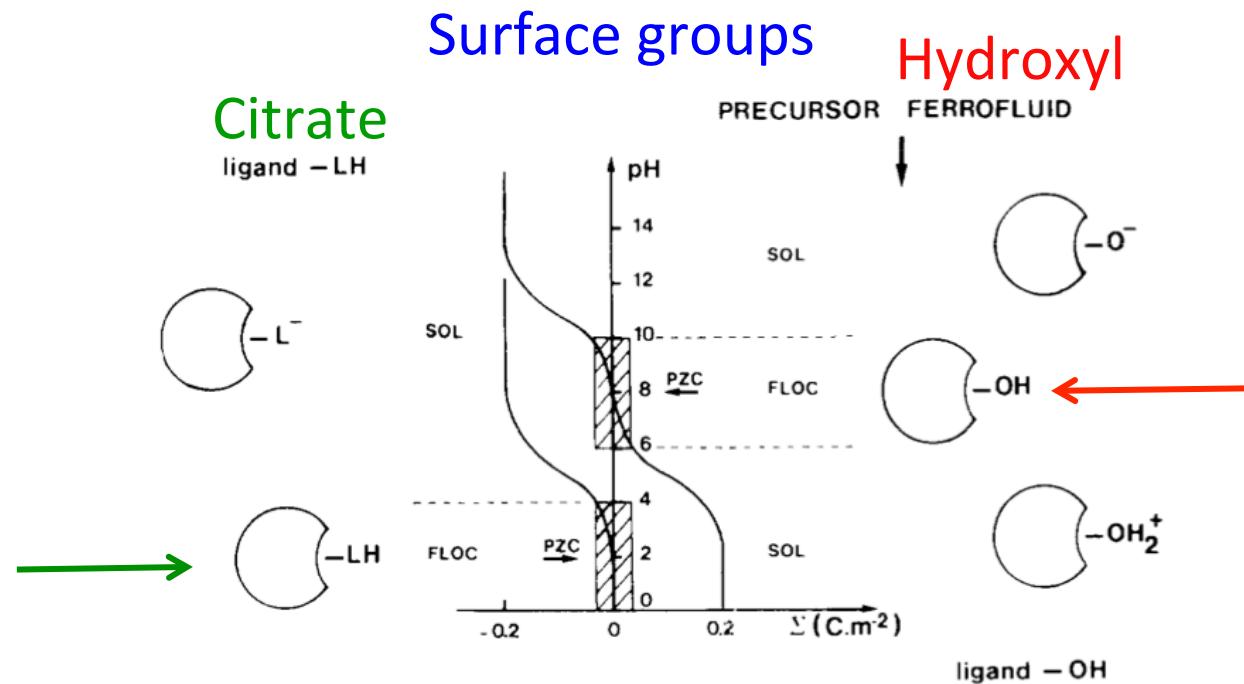
Ex.: in water

- Hofmeister series (protein solubility)
- Jones-Dole coefficients of ionic solution viscosity (ion-solvent interaction, chaotropic & kosmotropic nature of the ions),
- Eastman entropy of transfer of the ions (*)
(ion-solvent interaction)

(*) J. Agar, C. Mou, J. Lin *J.Phys. Chem.* **93** (1989) 2079
N. Takeyama, K. Nakashima *J. Solution Chem.* **17** (1988) 305

Efficient method for exchanging solvent & counter-ions in polar molecular solvents (*)

- Starting from flocculated dispersion at PZC,
- Repeated washing out of free ions and removable water,
- Re-charging of the NPs in the chosen medium with the chosen counter-ions with a controlled and reproducible method



(*) C. L. Filomeno *et al* *J. Phys. Chem. C* **121** (2017) 5539-5550

It allows to change in a controlled way :

- the solvent (water, DMSO, EAN, other ILs)
- the counter-ions (broad spectrum)
- their global quantity

- Concentrated FF obtained by ultracentrifugation

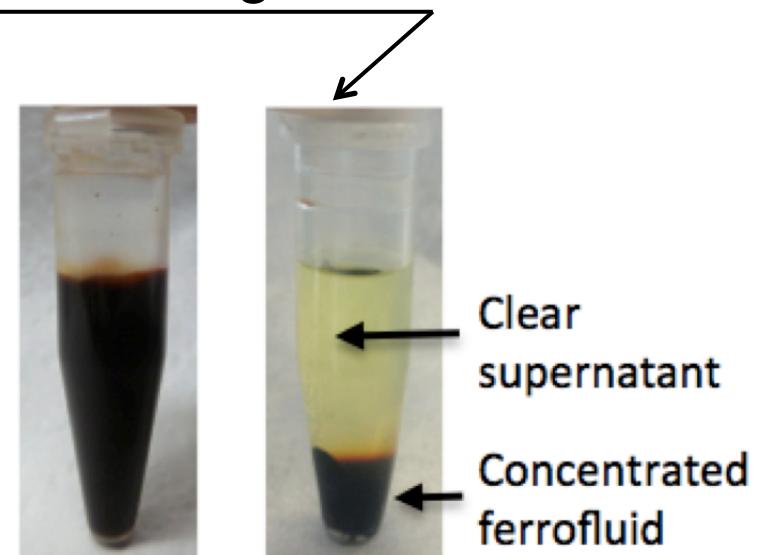
- Conductivity measurements of the supernatant : $[\text{electrolyte}]_{\text{free}}$

- Comparison to the introduced quantity : **structural NP charge**

- Nano-ZS electrophoretic measurements + QELS in dilute

sol : **dynamic effective charge ξ_0 (in molecular solvents)**

- SAXS – RFS



| Coating | Counter-ions | Solvent | Φ -range | $\langle d_{NP} \rangle$ (nm) |
|-----------|---|---------------------------------------|--------------------------------|-------------------------------|
| hydroxide | ClO_4^- | Water | 0.5-2.5% up to 80°C | 9 |
| hydroxide | ClO_4^- | DMSO and mixtures | 0.5-2.5% up to 80°C | 9 |
| hydroxide | ClO_4^- | DMSO | 0.5-3.5% Room T | 6.7 |
| citrate | TBuA^+ TMA^+ Na^+ Li^+ | Water | 0.5-5% Room T 1% up to 80°C | 8.5 |
| citrate | Na^+ Rb^+ Li^+ | EAN | 0.5-4% up to 105°C | 7.4 |
| hydroxide | TFSI^- - $\text{SMIM}^{+/-}$ | $\text{EMIM}^{+/-}$ TFS^- | 1% up to 190°C | 9.2 |

Small Angle Scattering* determination of interparticle interaction

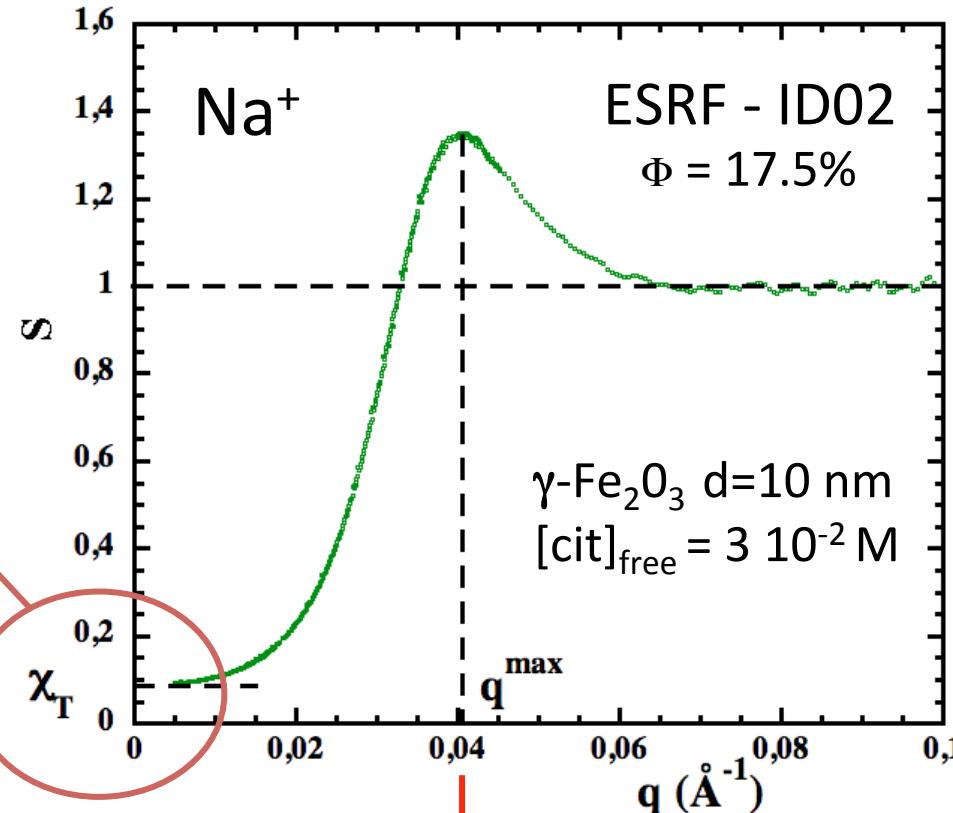
(*) of neutrons SANS or of x-rays SAXS

Typical *structure factor* of an assembly of nanoparticles
with repulsive interparticle interaction, as obtained by SAXS

At low q 's

$$S(q \rightarrow 0) = \chi = \frac{kT}{\partial \Pi v_{NP}} / \partial \Phi$$

Compressibility
Thermodynamic quantity



$$q^{\max} = \frac{2\pi}{d_0}$$

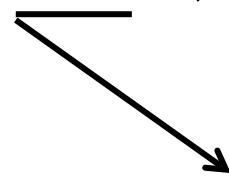
d_0 = most probable interparticle distance

Small Angle X-ray or Neutron scattering

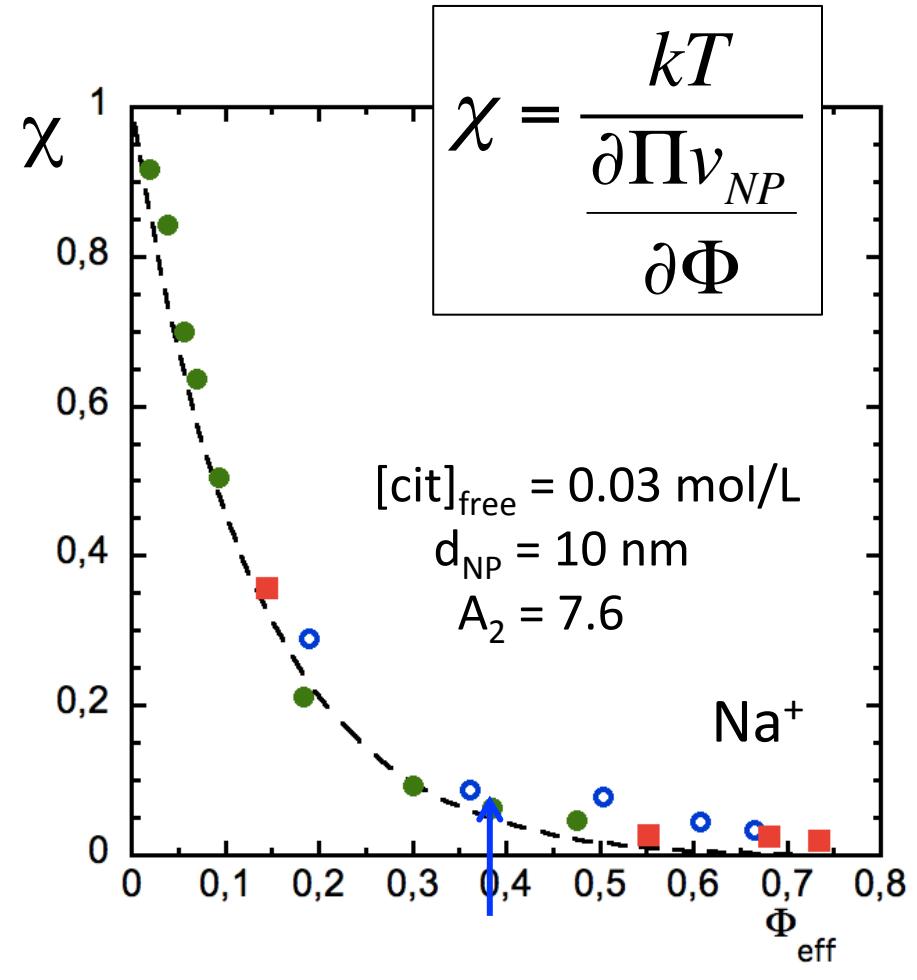
NP's compressibility c
given by the
Carnahan-Starling model of
effective Hard Spheres
(far from the glassy transition)

$$\chi = \frac{(1 - \Phi_{eff})^4}{1 + 4\Phi_{eff} + 4\Phi_{eff}^2 - 4\Phi_{eff}^3 + \Phi_{eff}^4}$$

$$\frac{\Phi_{eff}}{\Phi} = \frac{A_2}{A_{2^{HS}}} = \left(1 + \frac{2\kappa^{-1}}{d_{NP}}\right)^3$$



Two bodies
interaction
coefficient



Limit of validity
of Carnahan-Starling model

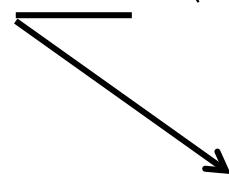
Small Angle X-ray or Neutron scattering

FF in water : citrated NPs with Na^+ counterions at $\neq [\text{cit}]$

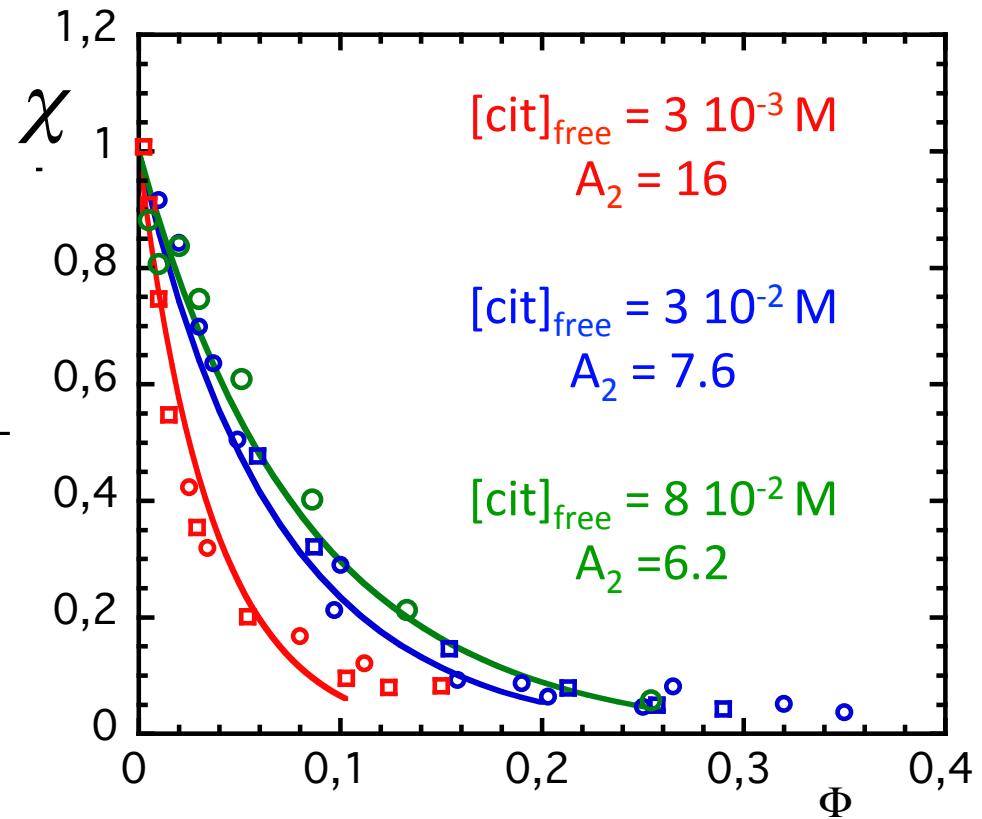
Carnahan-Starling model of
effective Hard Spheres
far from the glassy transition

$$\chi = \frac{(1 - \Phi_{\text{eff}})^4}{1 + 4\Phi_{\text{eff}} + 4\Phi_{\text{eff}}^2 - 4\Phi_{\text{eff}}^3 + \Phi_{\text{eff}}^4}$$

$$\frac{\Phi_{\text{eff}}}{\Phi} = \frac{A_2}{A_2^{\text{HS}}} = \left(1 + \frac{2\kappa^{-1}}{d_{NP}}\right)^3$$



Two bodies
interaction
coefficient



SANS, ILL, Grenoble, France

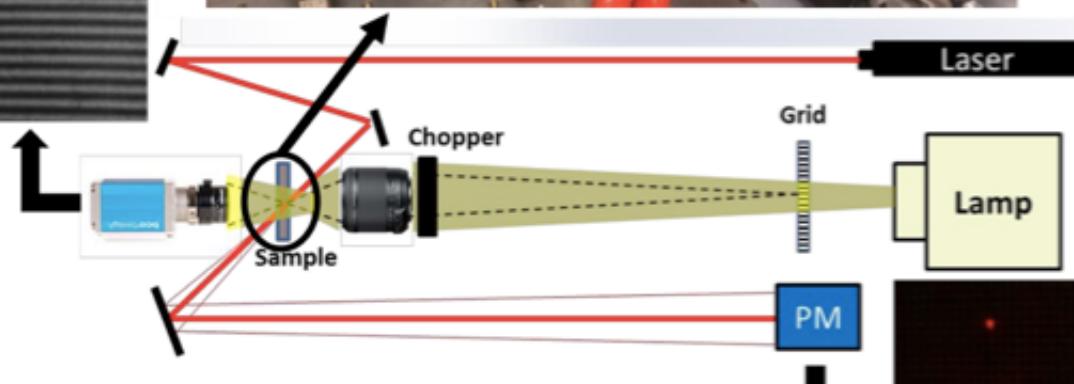
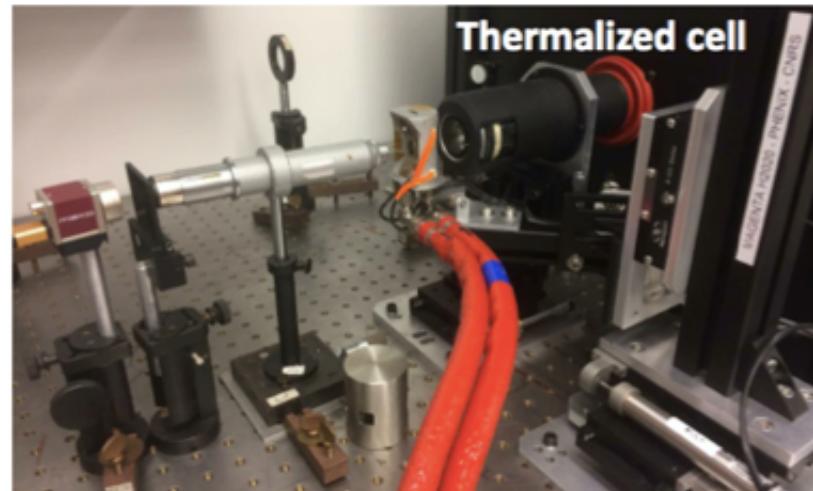
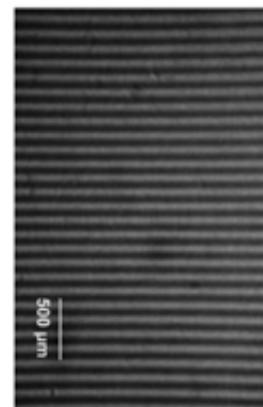
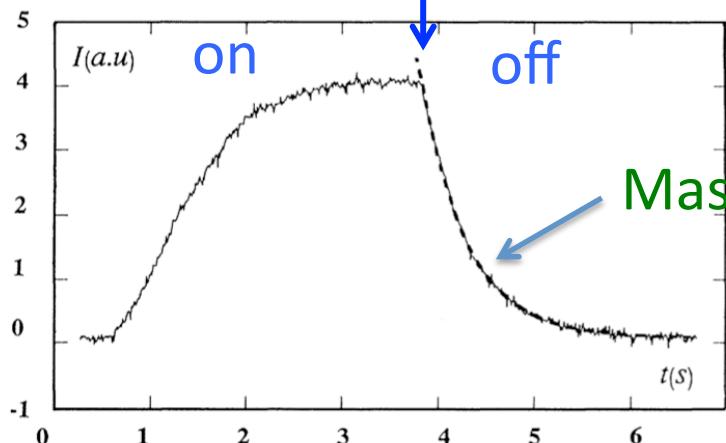
Forced Rayleigh Scattering (FRS)

RFS device

Spatial modulations
of temperature

⇒ Spatial modulations
of concentration
(Soret effect)

Heating
beam

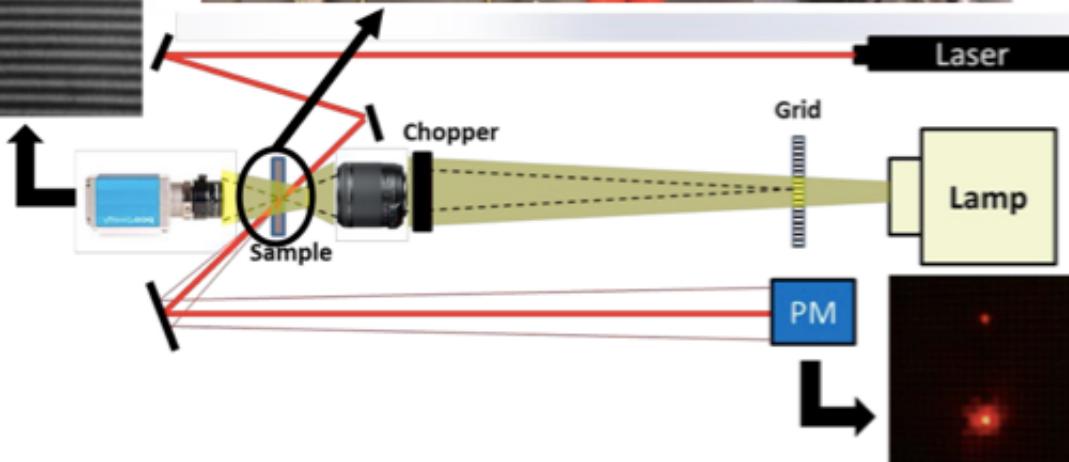
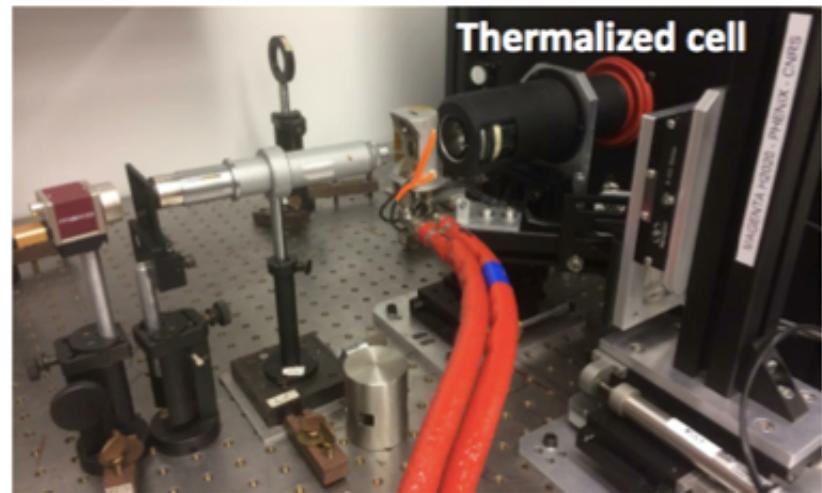
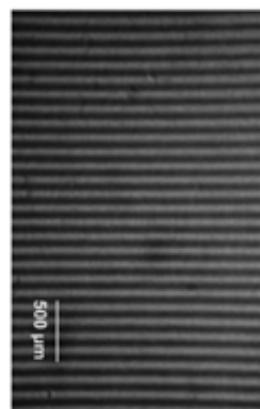
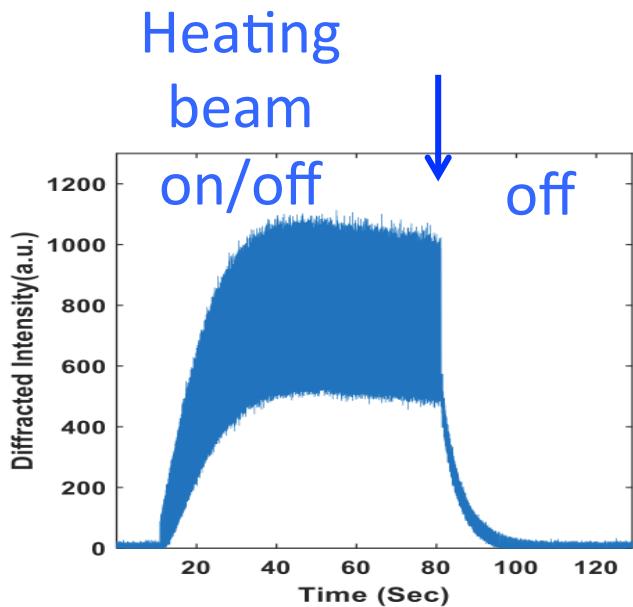


Without chopper

RFS device

Spatial modulations
of temperature

⇒ Spatial modulations
of concentration
(Soret effect)



With the chopper at a few Hz
+ Temporal modulations of
temperature

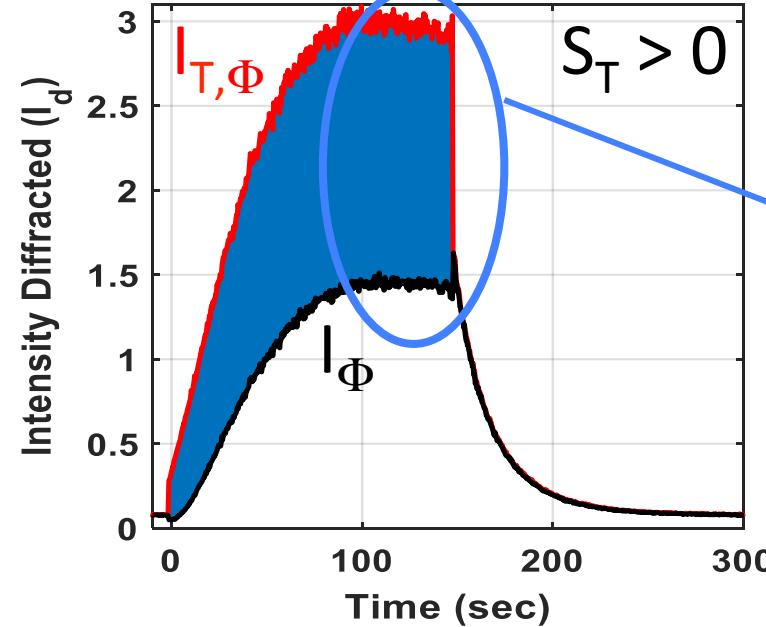
In stationary conditions :

$$\vec{\nabla}\Phi = -\Phi S_T \vec{\nabla}T$$

Soret coefficient

$S_T < 0$: NPs migrate towards hot regions

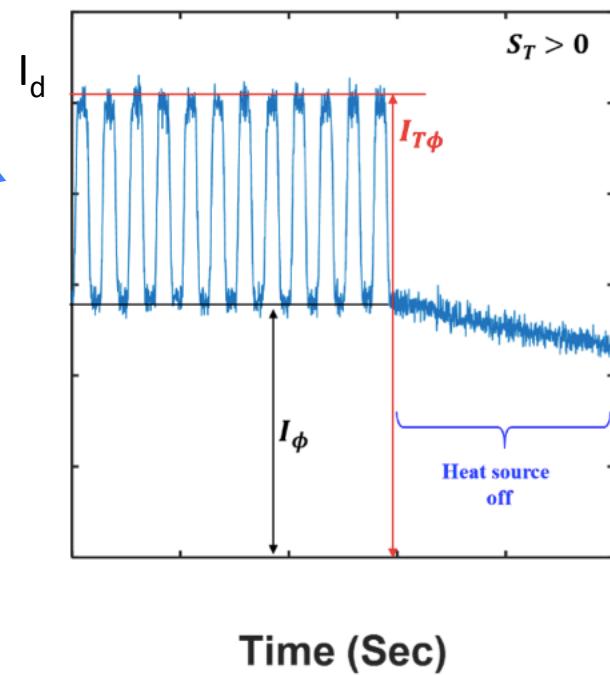
$S_T > 0$: NPs migrate towards cold regions



$$I_\Phi < I_{T,\Phi}$$

$$I_d \propto \Delta n^2$$

$$\Delta n_{T,\Phi} = \Delta n_\Phi + \Delta n_T$$



$$\text{Thermal grating} : \Delta n_T \propto \sqrt{I_{T,\Phi}} - \sqrt{I_\Phi}$$

$$\text{Concentration grating} : \Delta n_\Phi \propto \sqrt{I_\Phi}$$

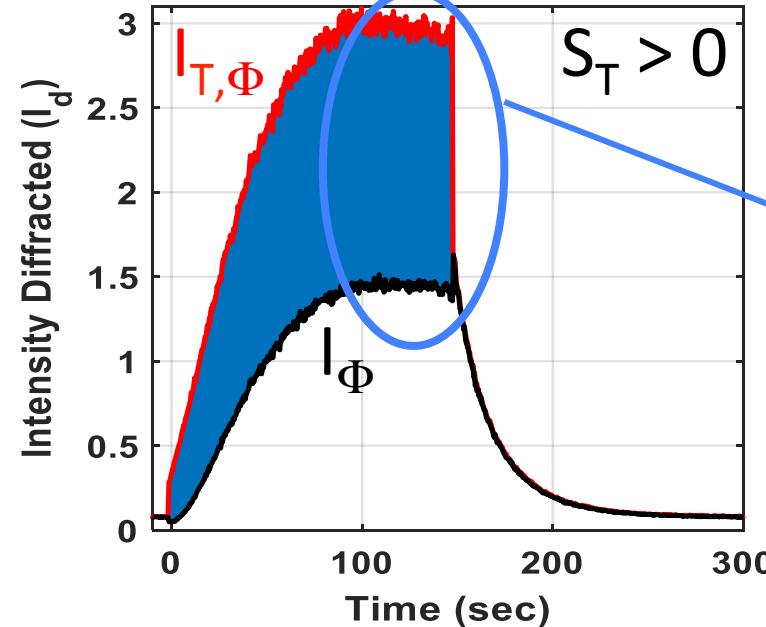
In stationary conditions :

$$\vec{\nabla}\Phi = -\Phi S_T \vec{\nabla}T$$

Soret coefficient

$S_T < 0$: NPs migrate towards hot regions

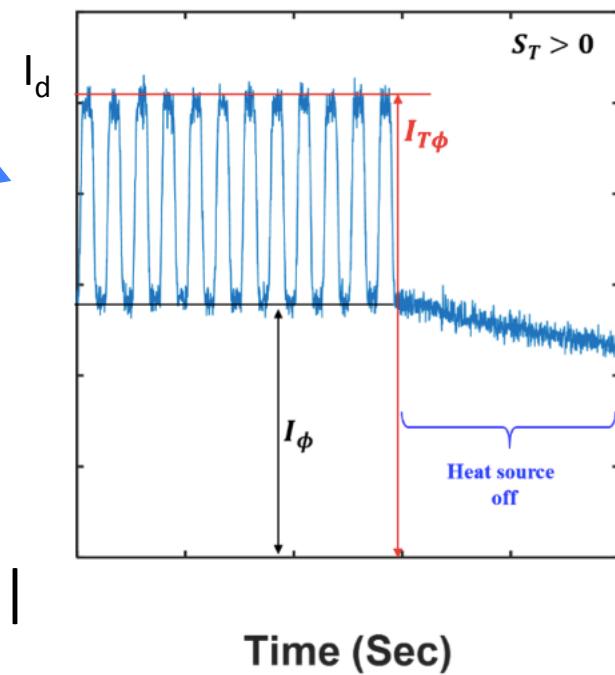
$S_T > 0$: NPs migrate towards cold regions



$$\Rightarrow I_\Phi < I_{T,\Phi}$$

$$I_d \propto \Delta n^2$$

$$\Delta n_{T,\Phi} = \Delta n_\Phi + \Delta n_T$$



Thermal grating : $\Delta T = |\Delta n_T| / |\delta n / \delta T|$

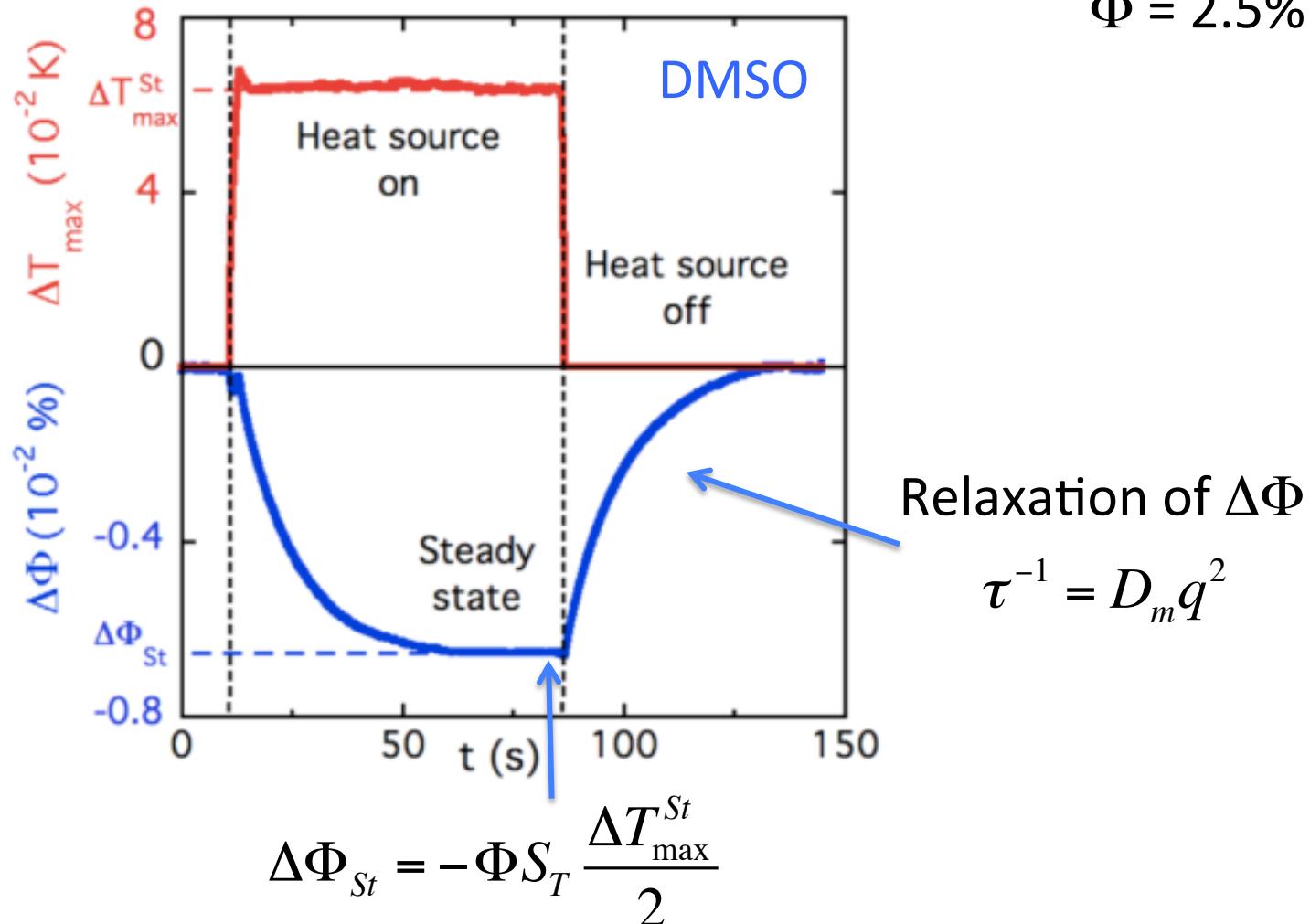
Concentration grating : $|\Delta \Phi| = |\Delta n_\Phi| / |\delta n / \delta \Phi|$

Example : FF in DMSO at T= 295 K

- hydroxyl-coated NPs with $[H^+] \approx 10^{-2} \text{ mole.L}^{-1}$
- ClO_4^- counter-ions

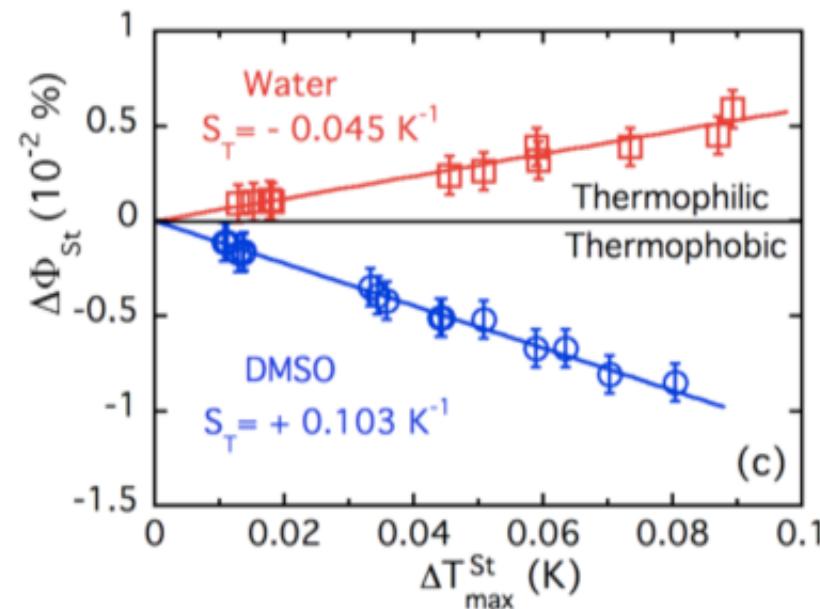
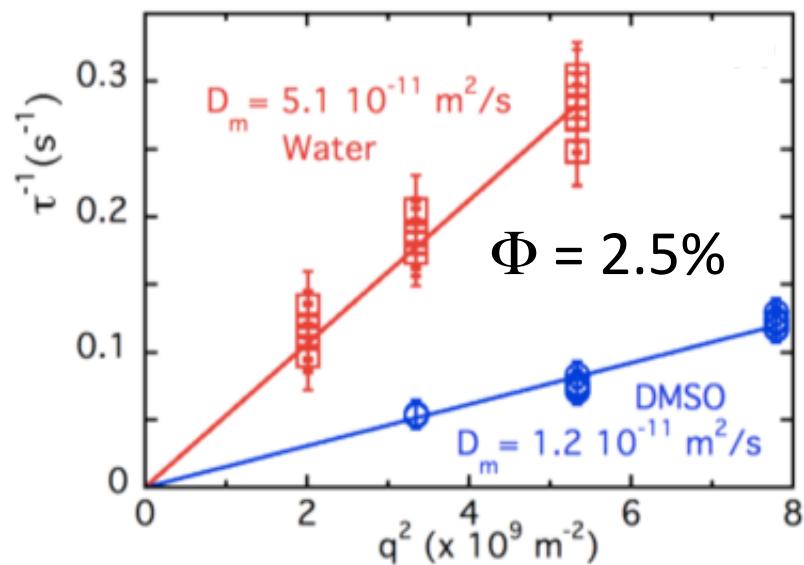
$$\xi_0 > 0$$

$$\Phi = 2.5\%$$



FF in water and in DMSO at T= 295 K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2} \text{ mole.L}^{-1}$ $\xi_0 > 0$
- Same ClO_4^- counter-ions



$$\tau^{-1} = D_m q^2$$

$$\Delta\Phi_{St} = -\Phi S_T \frac{\Delta T_{max}^{St}}{2}$$

Thermodiffusive and thermophoretic properties

FF in molecular solvents*
at room temperature

(*) water, DMSO and their mixtures

FF in water-DMSO mixtures at T = 295 K

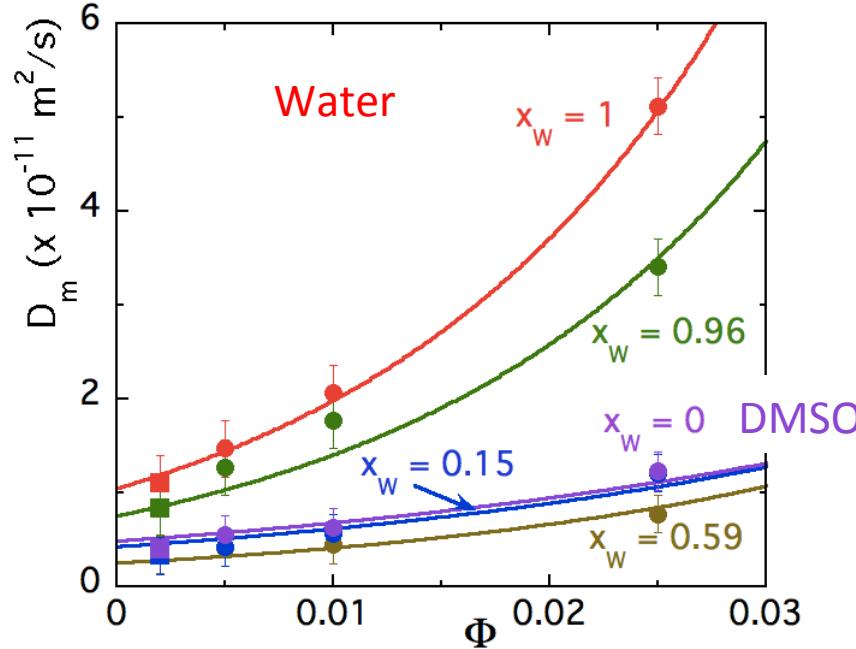
- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹ $\xi_0 > 0$
- Same ClO_4^- counter-ions

FF in water-DMSO mixtures at T = 295 K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2} \text{ mole.L}^{-1}$ $\xi_0 > 0$
- Same ClO_4^- counter-ions

Mass diffusion coefficient

$$D_m = \frac{k_B T}{3\pi\eta d_H \chi}$$

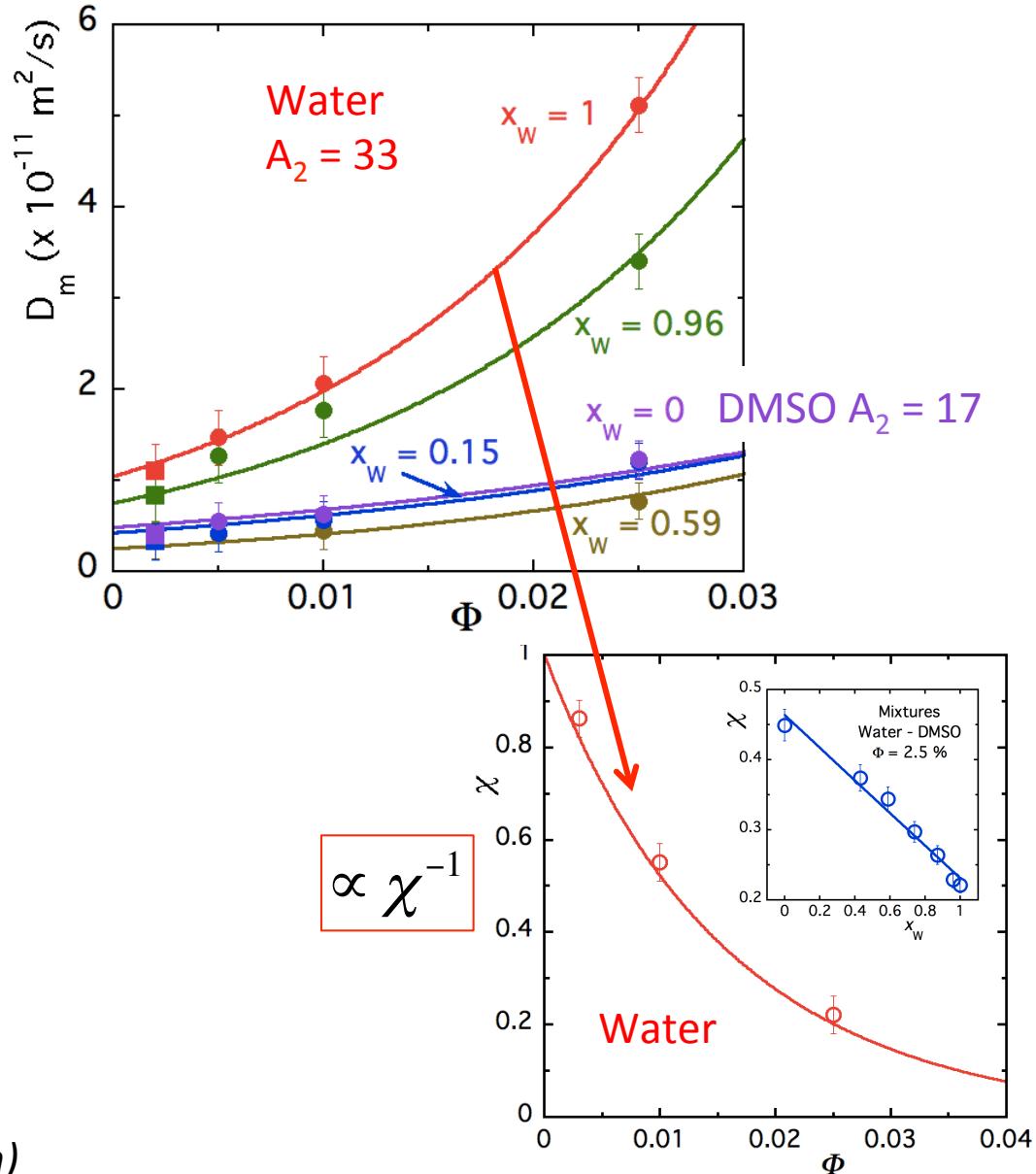


FF in water-DMSO mixtures at T = 295 K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹
- Same ClO_4^- counter-ions

Mass diffusion coefficient

$$D_m = \frac{k_B T}{3\pi\eta d_H \chi}$$

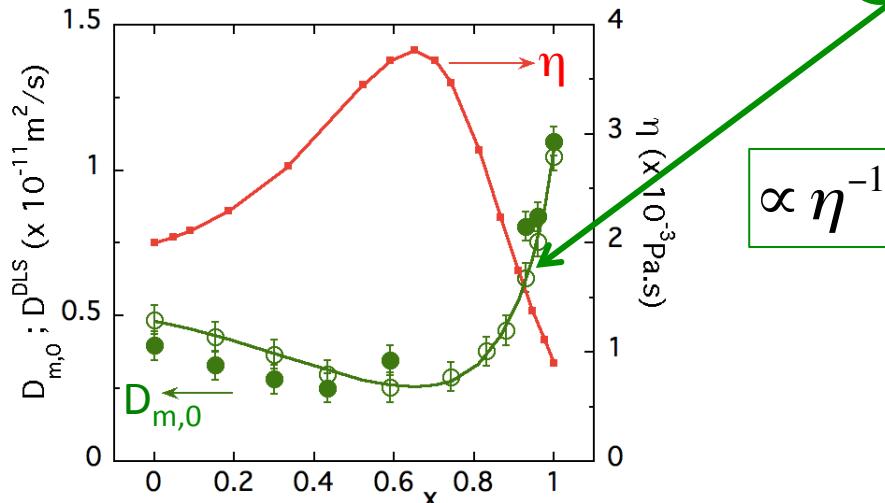


FF in water-DMSO mixtures at T = 295 K

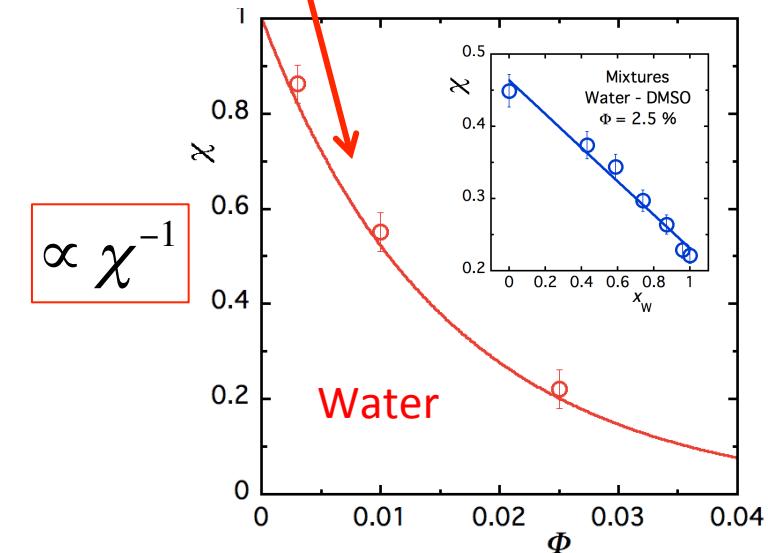
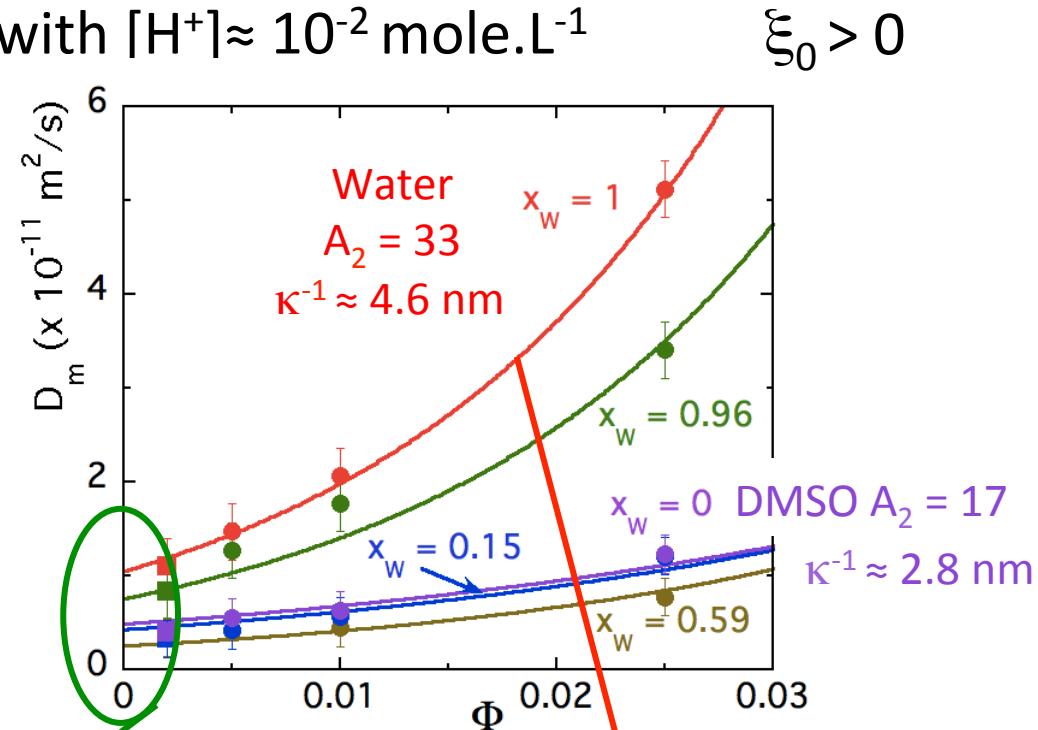
- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹
- Same ClO_4^- counter-ions

Mass diffusion coefficient

$$D_m = \frac{k_B T}{3\pi\eta d_H \chi}$$



M. Sarkar et al (submitted for publication)



FF in water-DMSO mixtures at T = 295 K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2} \text{ mole.L}^{-1}$ $\xi_0 > 0$
- Same ClO_4^- counter-ions

$$S_T = \frac{\chi}{k_B T} \left(\hat{S}_{NP} - e\xi_0 S_e^{st} \right)$$

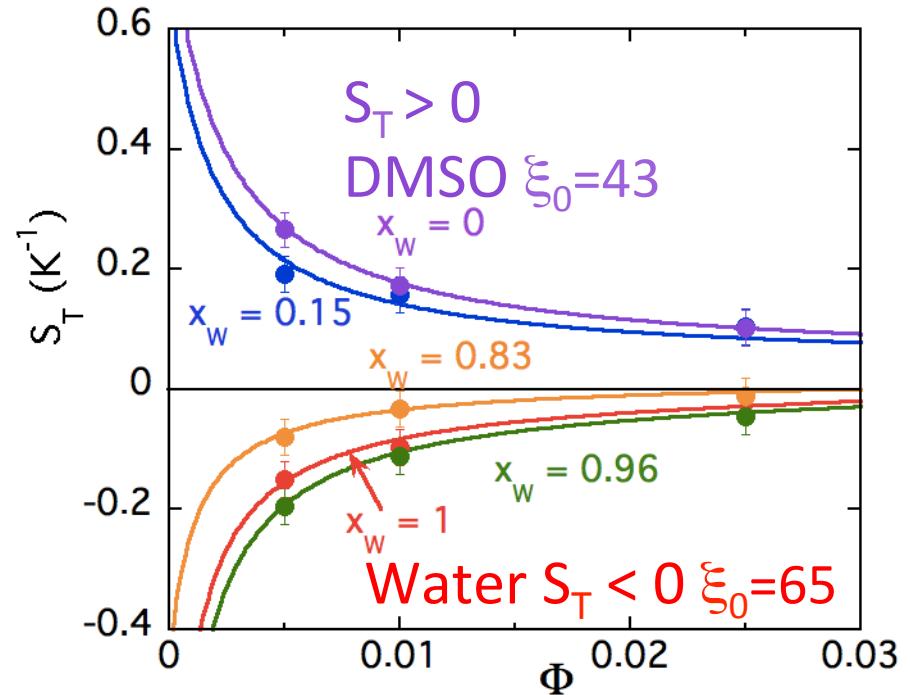
→ Soret coefficient

$$eS_e^{st} = \frac{n_+ \hat{S}_+ - n_- \hat{S}_- + Zn\chi \hat{S}_{NP}}{n_+ + n_- + Zn\chi \xi_0}$$

→ Seebeck coefficient for monovalent ions

ξ_0 : Electrophoretic charge

\hat{S}_{NP} , \hat{S}_+ , \hat{S}_- : Eastman entropy of transfer of the charged species



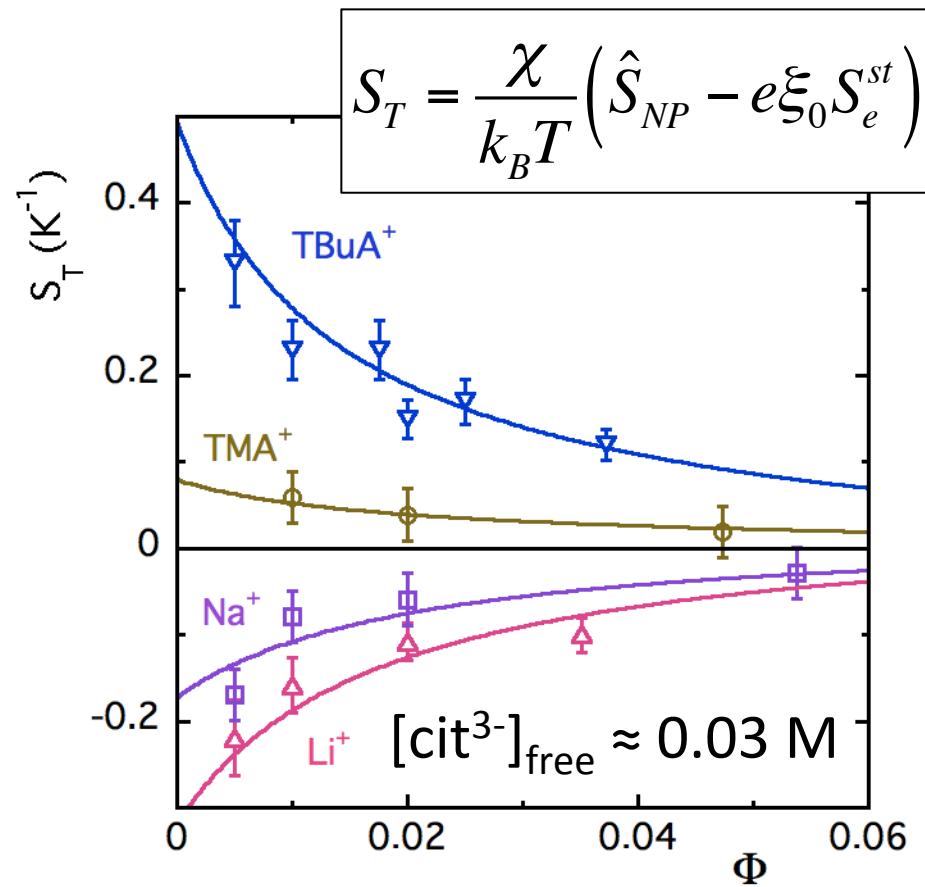
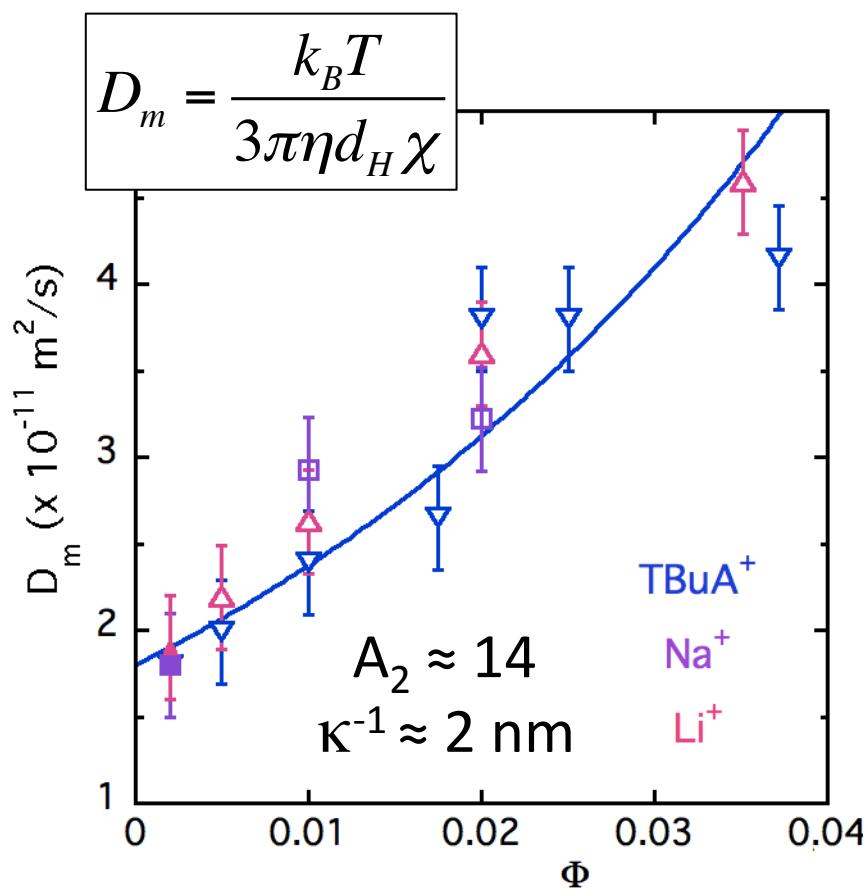
FF in water at pH = 7 and T = 295 K

- Same citrate-coated NPs $\xi_0 < 0$
- Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺

Another method in water to modulate
the sign of Soret coefficient S_T

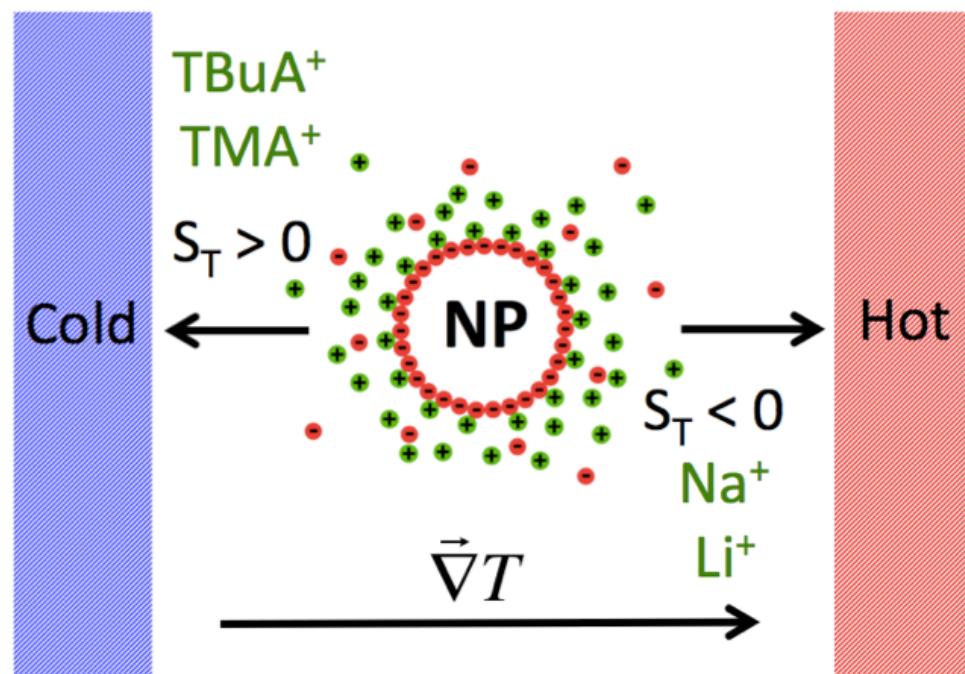
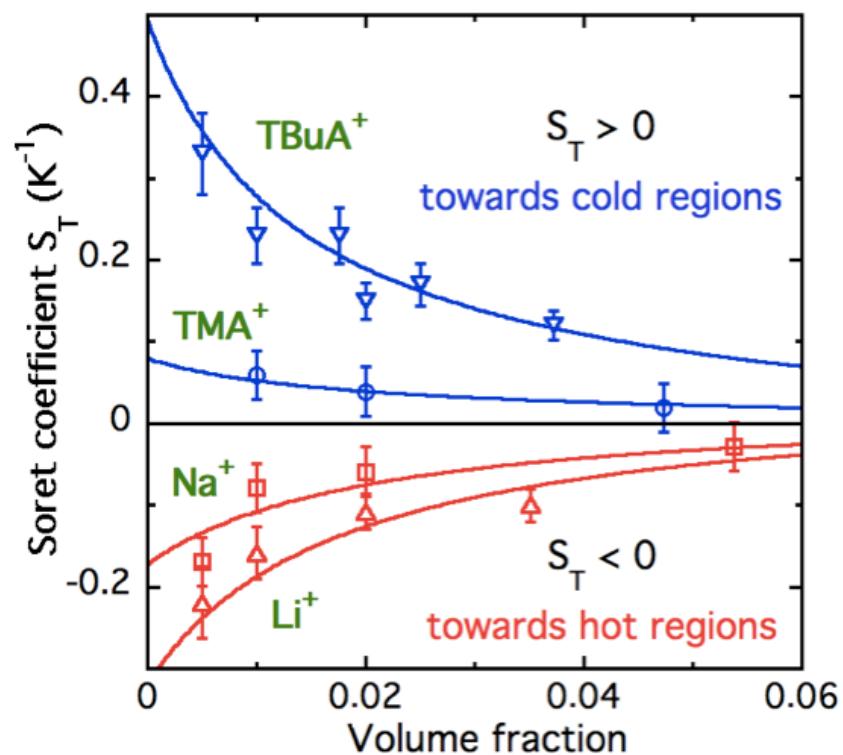
FF in water at pH=7 and T = 295 K

- Same citrate-coated NPs
 - Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺
- $-40 \leq \xi_0 < -28$



FF in water at pH=7 and T = 295 K

- Same citrate-coated NPs
- Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺



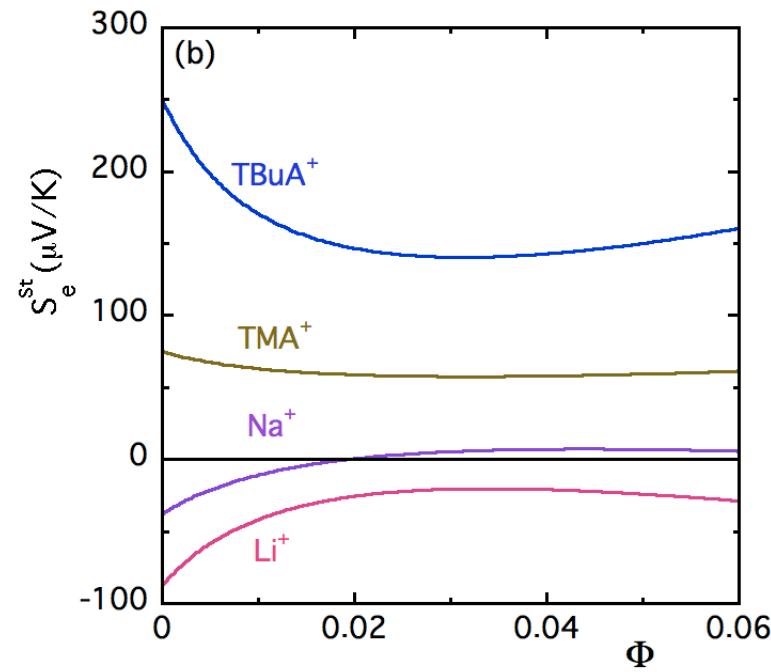
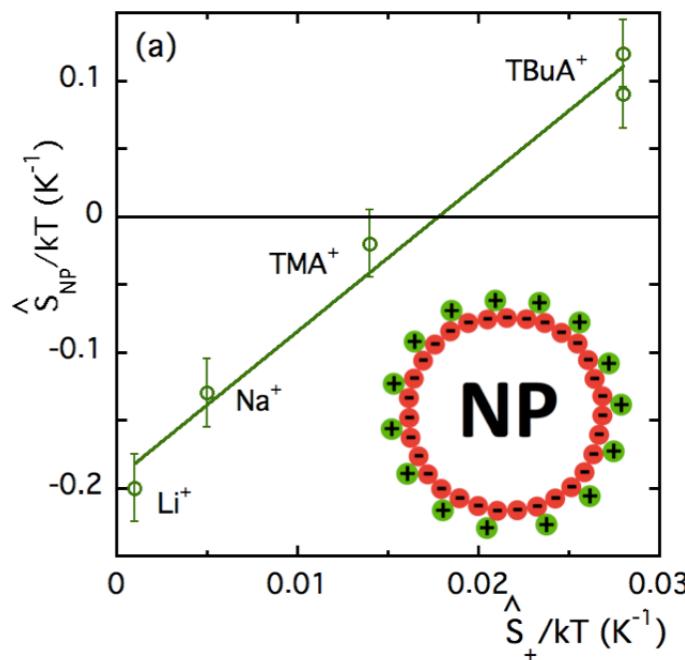
FF in water at pH=7 and T = 295 K

- Same citrate-coated NPs
- Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺ $\xi_0 < 0$

$$S_T = \frac{\chi}{k_B T} \left(\hat{S}_{NP} - e\xi_0 S_e^{st} \right)$$

$$S_e^{st} = \frac{n_+ \hat{S}_+ - n_- \hat{S}_- + Zn\chi \hat{S}_{NP}}{n_+ + n_- + Zn\chi \xi_0}$$

Hyp $Z = \xi_0$ - Here the only unknown parameter is \hat{S}_{NP}



N. Takeyama, K. Nakashima *J. Solution Chem.* **17** (1988) 305

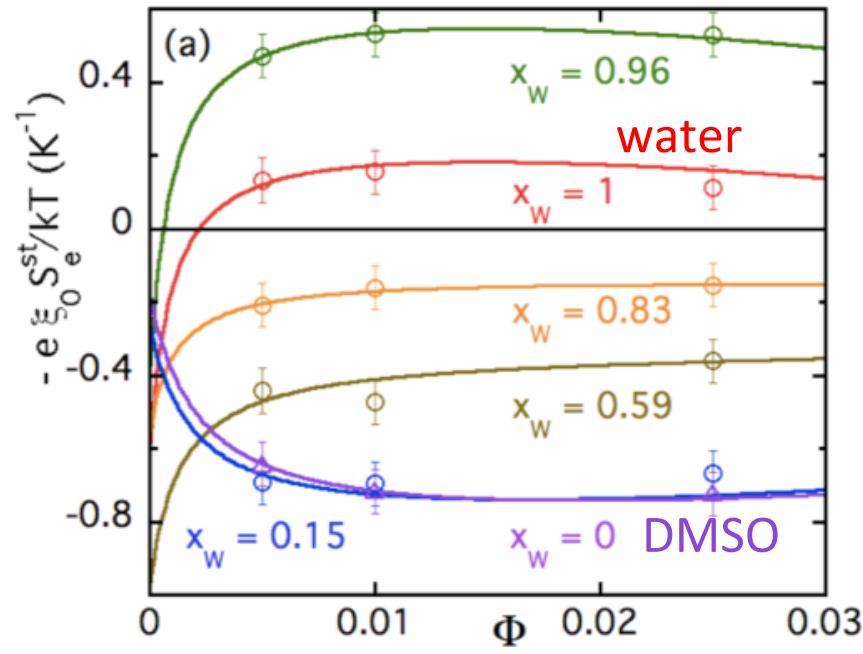
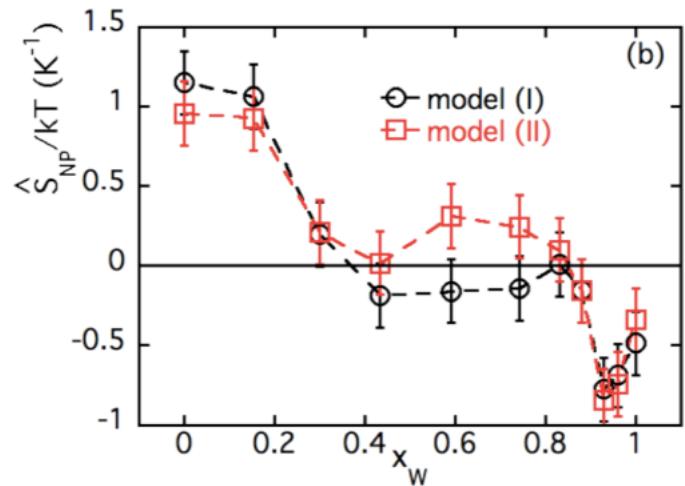
M. Kouyaté *et al* *Phys. Chem. Chem. Phys.* **21** (2019) 1895-1903

Backwards analysis of FF in water-DMSO mixtures

\hat{S}_{ion} deduced from: (I) Born model and (II) Enthalpy transfer model

$$\hat{S}_{ion}(x_w) = \hat{S}_{ion}^{water} - \frac{\Delta_t H_{ion}^o(x_w)}{TN_a}$$

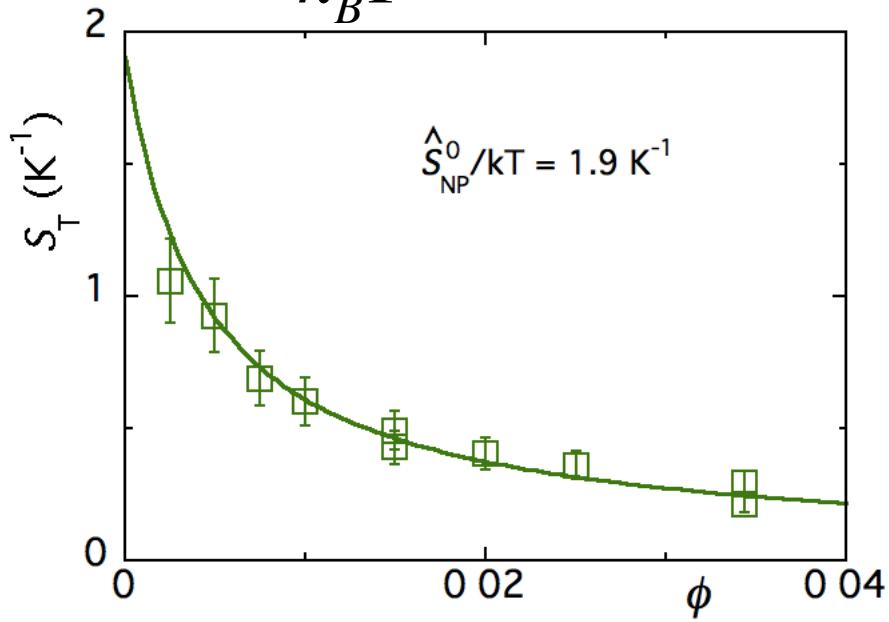
$$S_T = \frac{\chi}{k_B T} \left(\hat{S}_{NP} - e\xi_0 S_e^{st} \right)$$



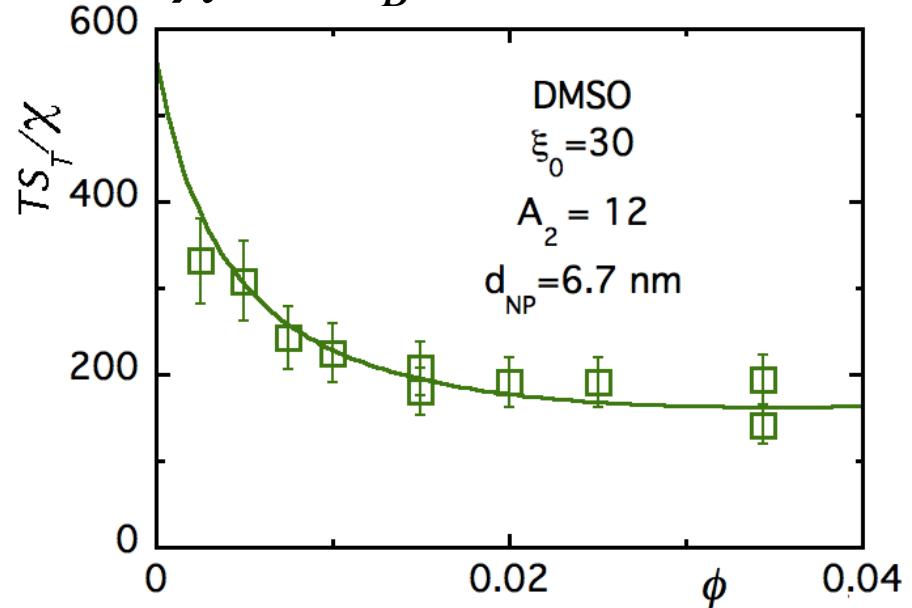
In our range of Φ measurements $-e\xi_0 S_e/kT$ is almost constant but there is a large variation at lower Φ 's

Illustrated with another FF sample in pure DMSO
 (smaller NPs, smaller ξ_0)

$$S_T = \frac{\chi}{k_B T} (\hat{S}_{NP} - e\xi_0 S_e^{st})$$

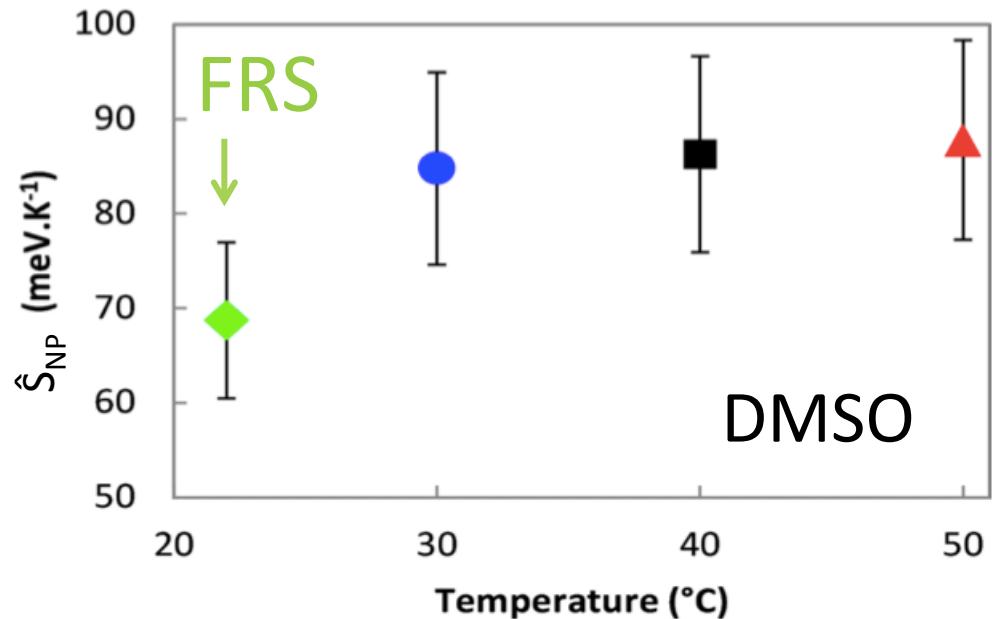
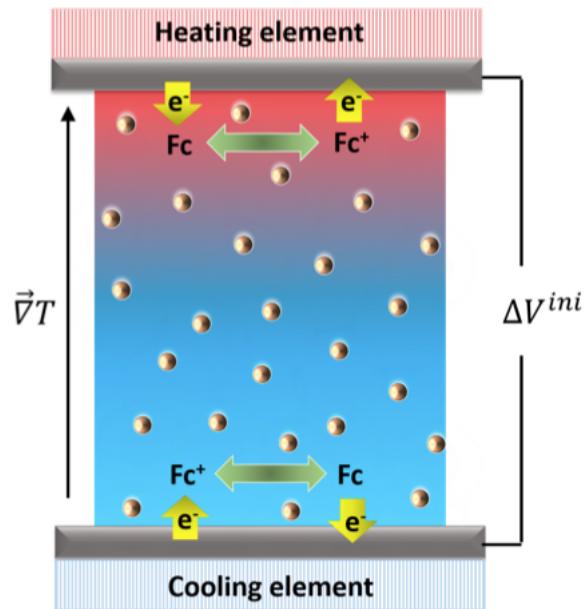


$$\frac{TS_T}{\chi} = \frac{1}{k_B} (\hat{S}_{NP} - e\xi_0 S_e^{st})$$



TS_T/χ is almost constant in the range $1\% \leq \Phi \leq 4\%$
 but there is a large variation at lower Φ 's

Thermoelectric measurements (*) on a similar FF sample in pure DMSO



Same order of magnitude of \hat{S}_{NP}
is found by both determinations :
FRS and thermoelectric measurements in the initial regime

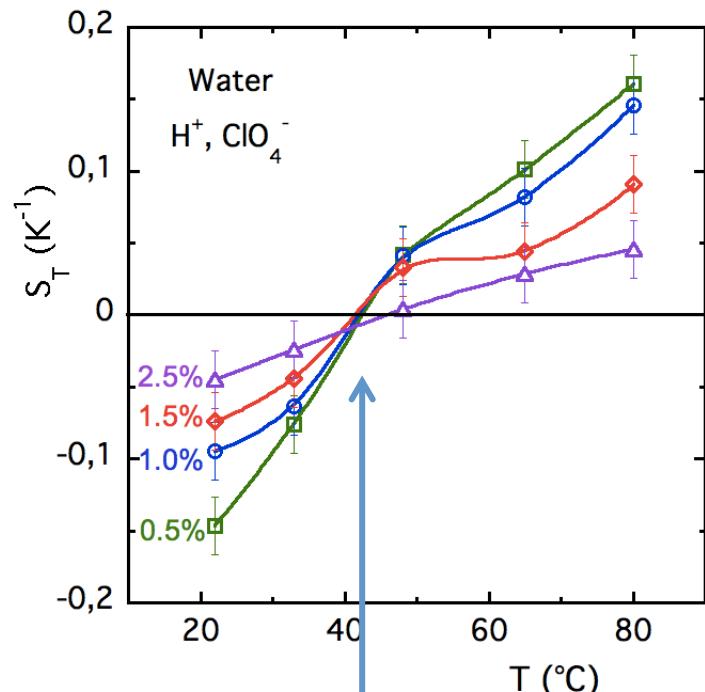
(*) B. Huang *et al* J. Chem. Phys 143 (2015) 054902 – see Sawako Nakamae presentation

Thermodiffusive and thermophoretic
properties
of FF in molecular solvents*
at $T \geq 295K$

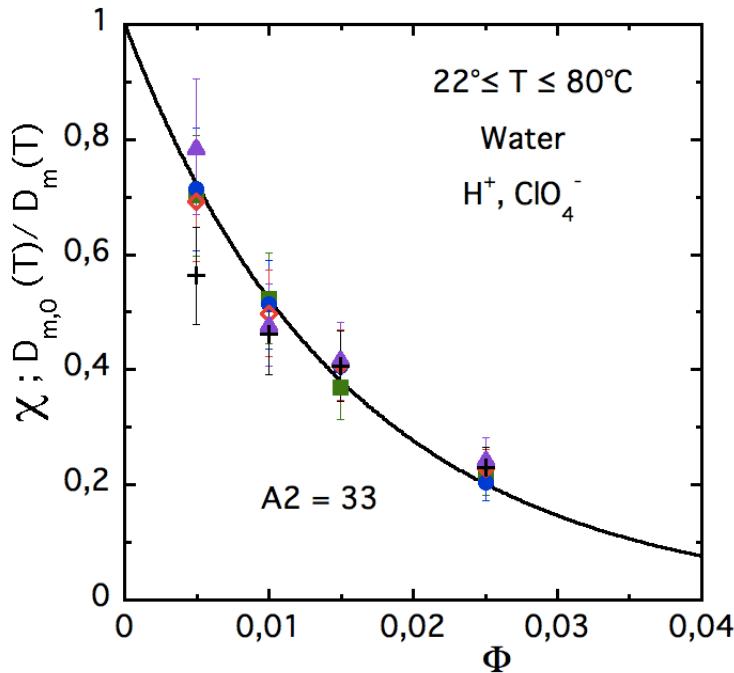
(*) acidic NPs in water and DMSO

Acid FF in water at $T \geq 295$ K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹ $\xi_0 > 0$
- Same ClO_4^- counter-ions



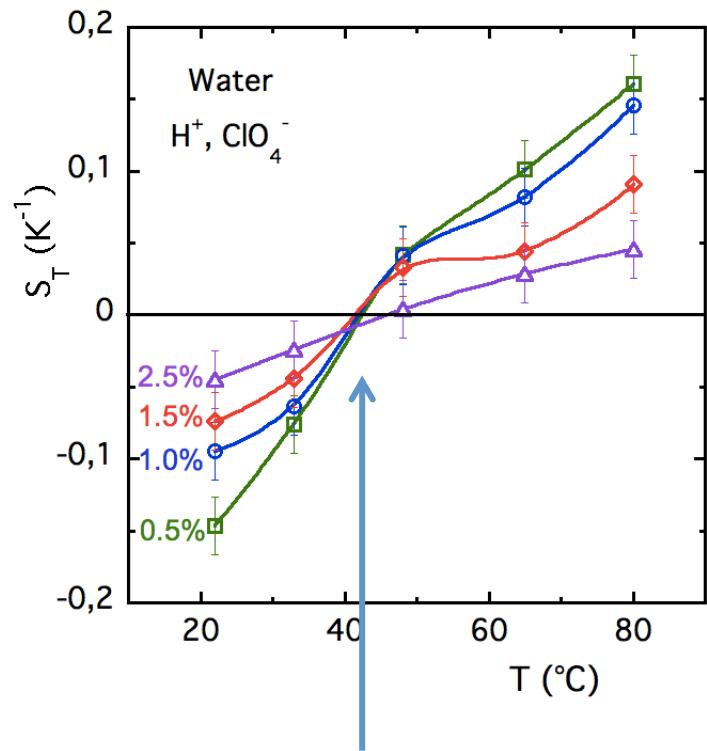
S_T changes its sign
whatever Φ



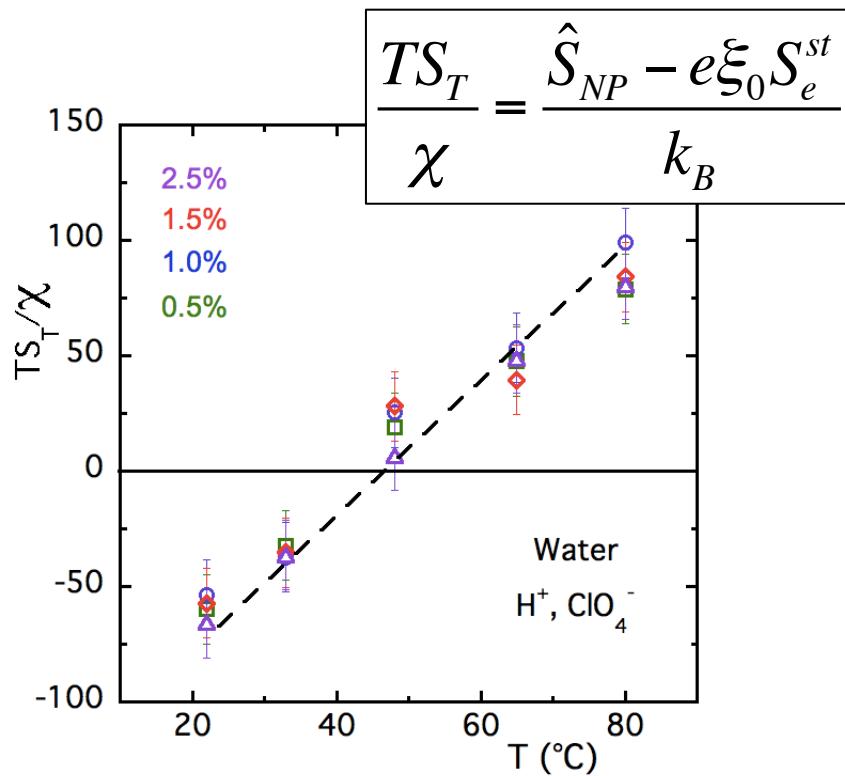
From $D_m(\Phi)$:
 χ indt of T
for $20^\circ C \leq T \leq 80^\circ C$

Acid FF in water at $T \geq 295$ K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹ $\xi_0 > 0$
- Same ClO_4^- counter-ions



S_T changes its sign
whatever Φ



Reference values at 295K :

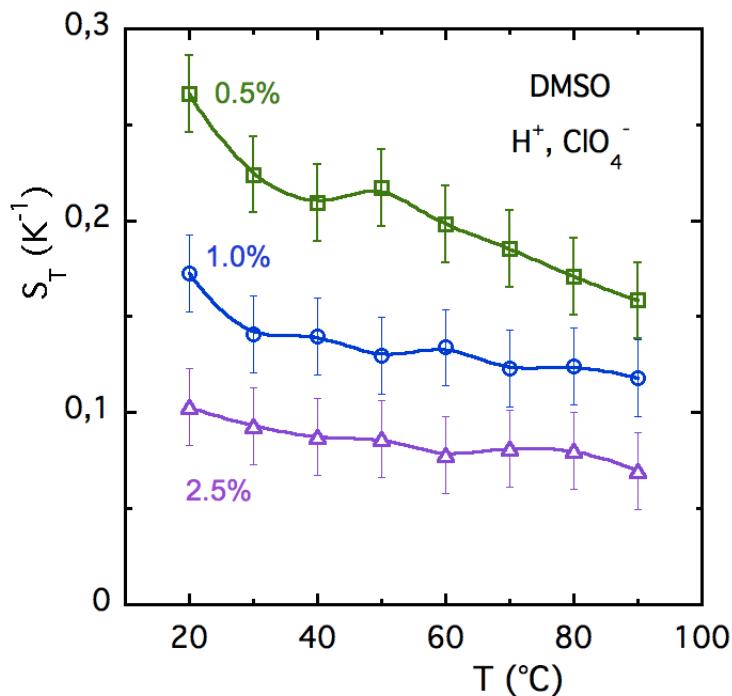
$$\hat{S}_{NP}/k \approx -100$$

$$-e\xi_0 S_e/k \approx +35$$

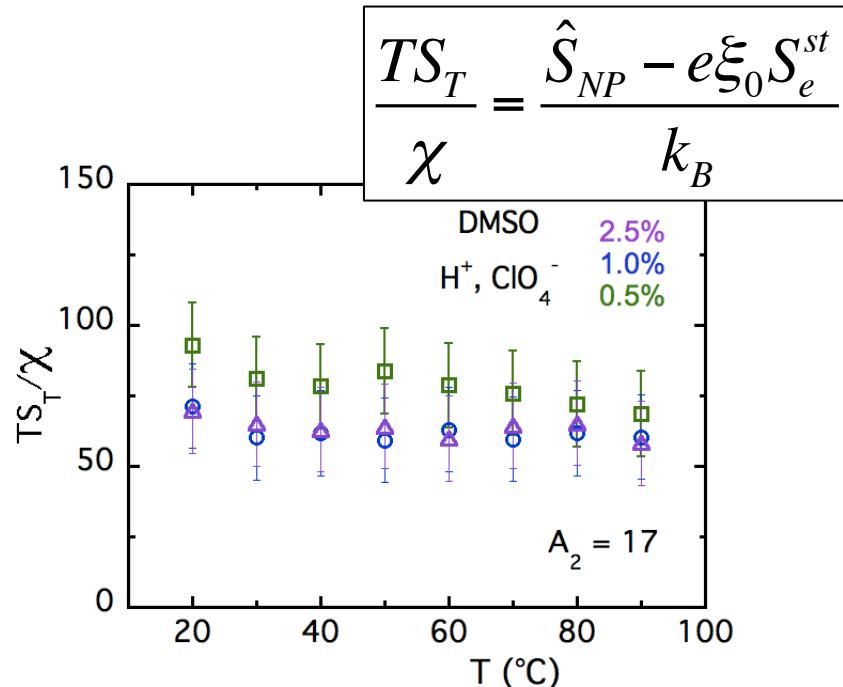
Contr. Ions at $\Phi = 0$: -180

Acid FF in DMSO at $T \geq 295$ K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹ $\xi_0 > 0$
- Same ClO_4^- counter-ions



$S_T > 0$ whatever Φ and T
 $TS_T/\chi \approx cst$ with T



Reference values at 295K :

$$\hat{S}_{NP}/k \approx +280$$

$$-e\xi_0 S_e/k \approx -205$$

Contr. Ions at $\Phi = 0$: - 45

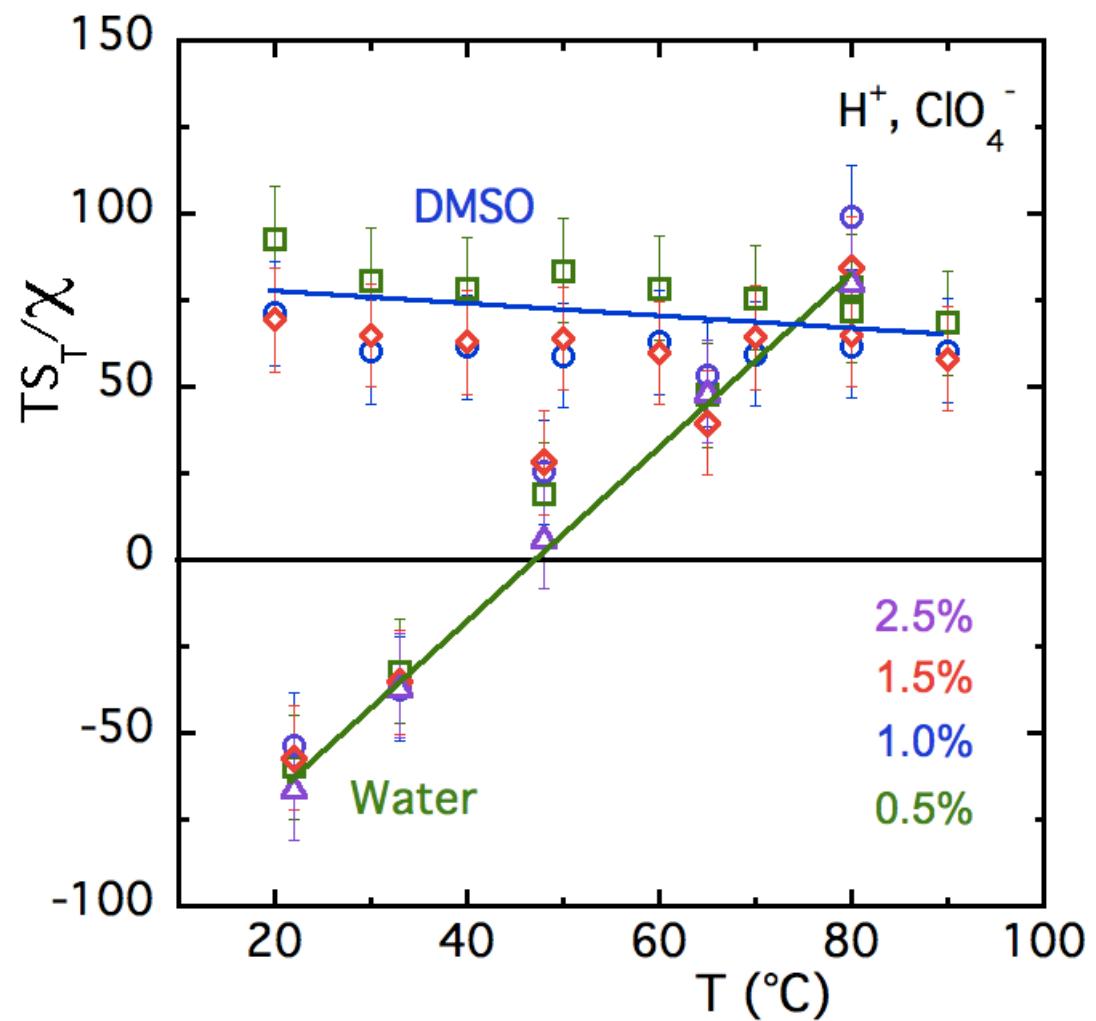
Acid FF in water and DMSO at $T \geq 295$ K

- Same hydroxyl-coated NPs with $[H^+] \approx 10^{-2}$ mole.L⁻¹ $\xi_0 > 0$
- Same ClO_4^- counter-ions

$$\frac{TS_T}{\chi} = \frac{\hat{S}_{NP} - e\xi_0 S_e^{st}}{k_B}$$

At room T,
 TS_T/χ results
from the balance
of two large terms
of opposite sign.

For $\Phi \rightarrow 0$,
 $TS_T/\chi \rightarrow$ larger values
+ 235 in DMSO
-280 in water



FF in water at pH=7 and T ≥ 295 K

- Same citrate-coated NPs

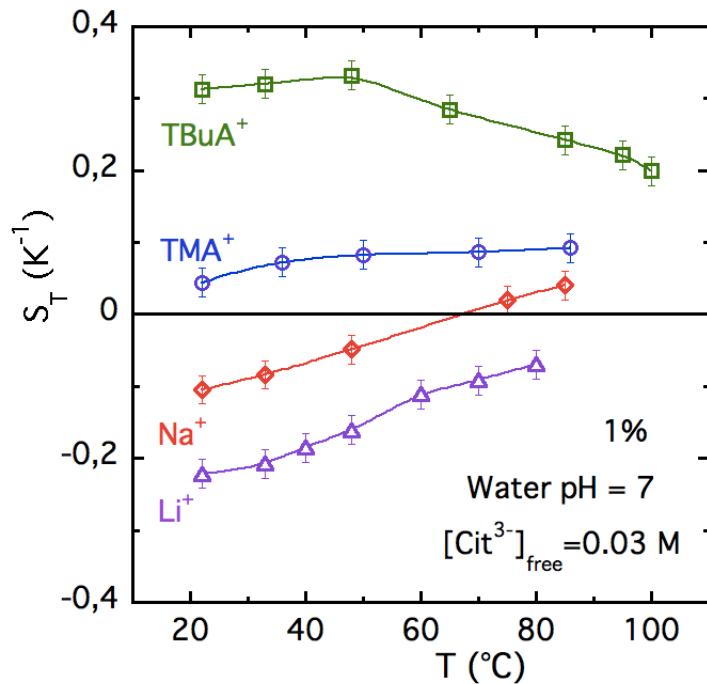
$$\xi_0 < 0$$

- Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺

FF in water at pH=7 and T \geq 295 K

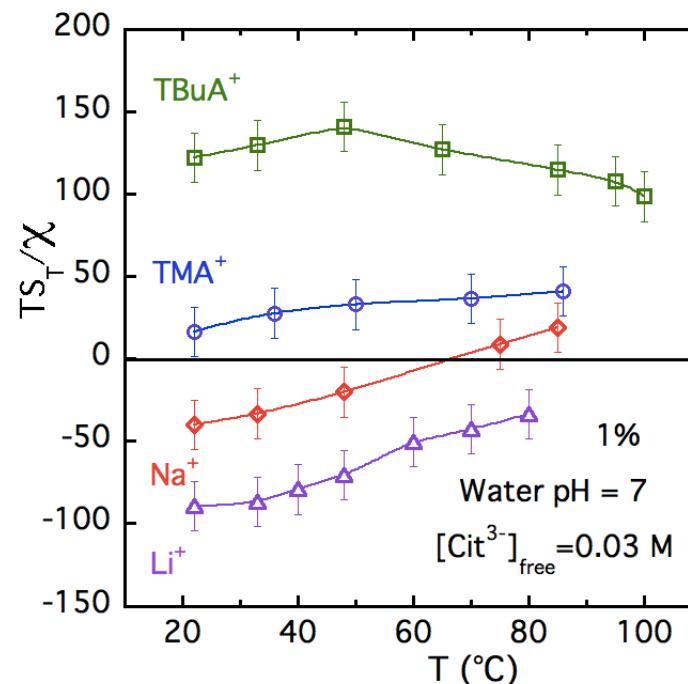
- Same citrate-coated NPs
- Different counter-ions : TBuA⁺, TMA⁺, Na⁺, Li⁺

$$\xi_0 < 0$$



Here also the T-dependence of \hat{S}_+ , \hat{S}_- and ξ_0 are unknown,

Hyp χ indt of T



Reference values at 295K :

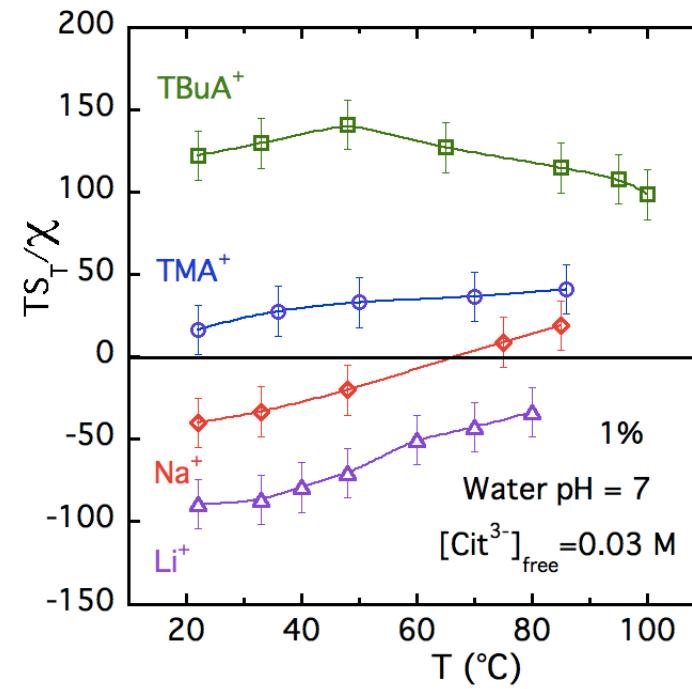
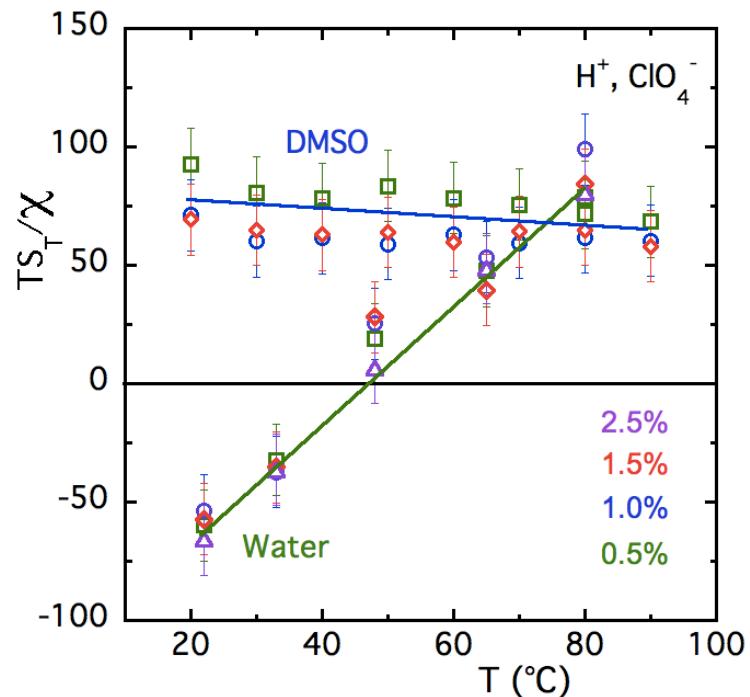
TBuA⁺ : $\hat{S}_{NP}/k \approx +30$, $-e\xi_0 S_e/k \approx +80$

TMA⁺ : $\hat{S}_{NP}/k \approx -6$, $-e\xi_0 S_e/k \approx +25$

Na⁺ : $\hat{S}_{NP}/k \approx -40$, $-e\xi_0 S_e/k \approx -5$

Li⁺ : $\hat{S}_{NP}/k \approx -60$, $-e\xi_0 S_e/k \approx -20$

Summary of FRS results in molecular solvents at $T \geq 295$ K



$$\frac{TS_T}{\chi} = \frac{\hat{S}_{NP} - e\xi_0 S_e^{st}}{k_B}$$

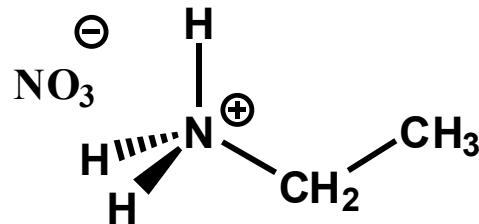
At room T, TS_T/χ results from the balance of two large terms either in competition of sign or with the same sign

Thermodiffusive and thermophoretic properties of FF in Ionic Liquids* at $T \geq 295K$

(*) Two examples in EAN (several counter-ions)
and in EMIM-TFSI

FF based on EAN

Ethyl ammonium nitrate EAN

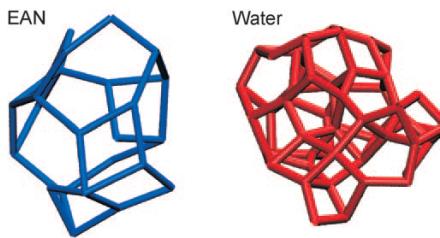


Home
made

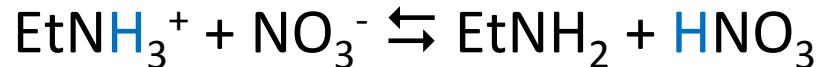
Melting Point = 14 °C $\eta = 35 \text{ cP}$
at 300K

Similar to water

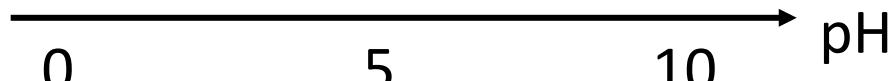
H-bonded
network



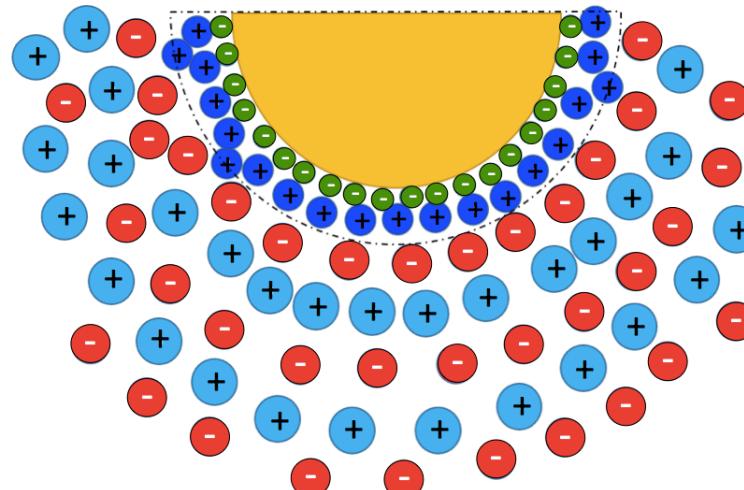
Protic Ionic Liquid



acidic neutral basic

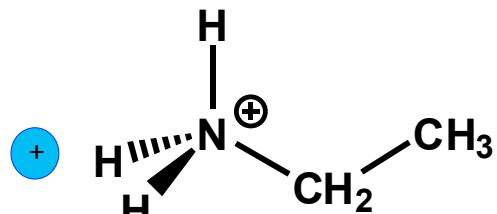


Water content < 0.3% w/w



- Negative citrate surface species

- various counterions



Ethylammonium +

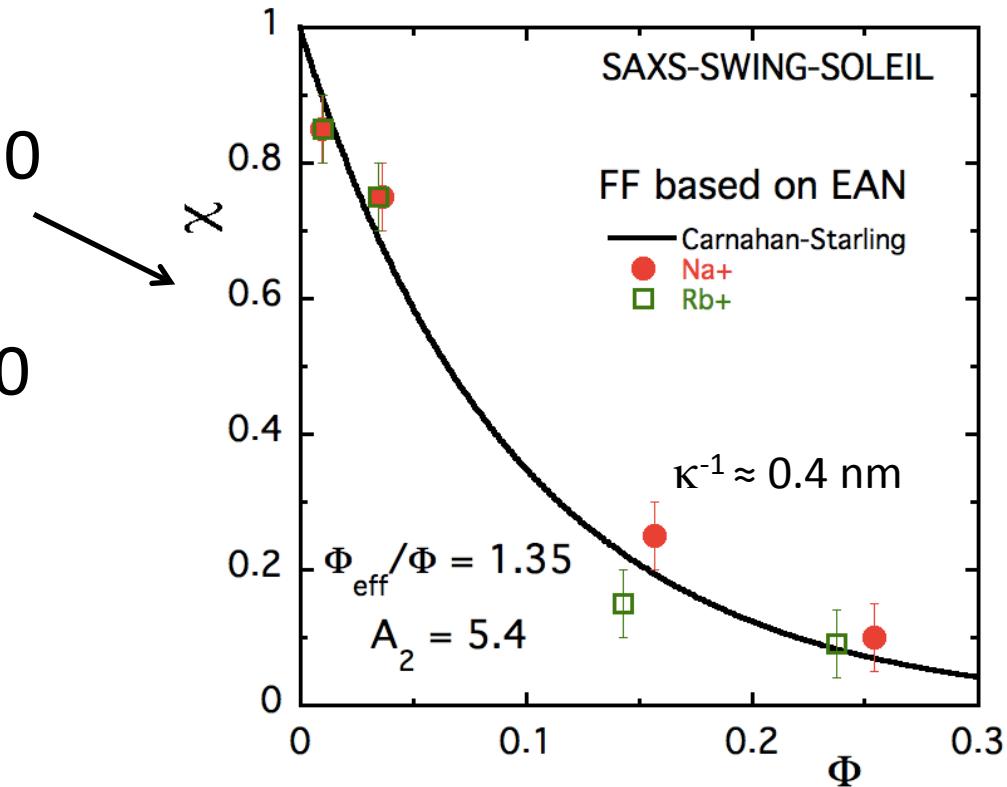
FF based on EAN at 295K – SAXS measurements

Nature of the counter-ions in the mother-solution influence

- the colloidal stability of the dispersion
- the interparticle interaction

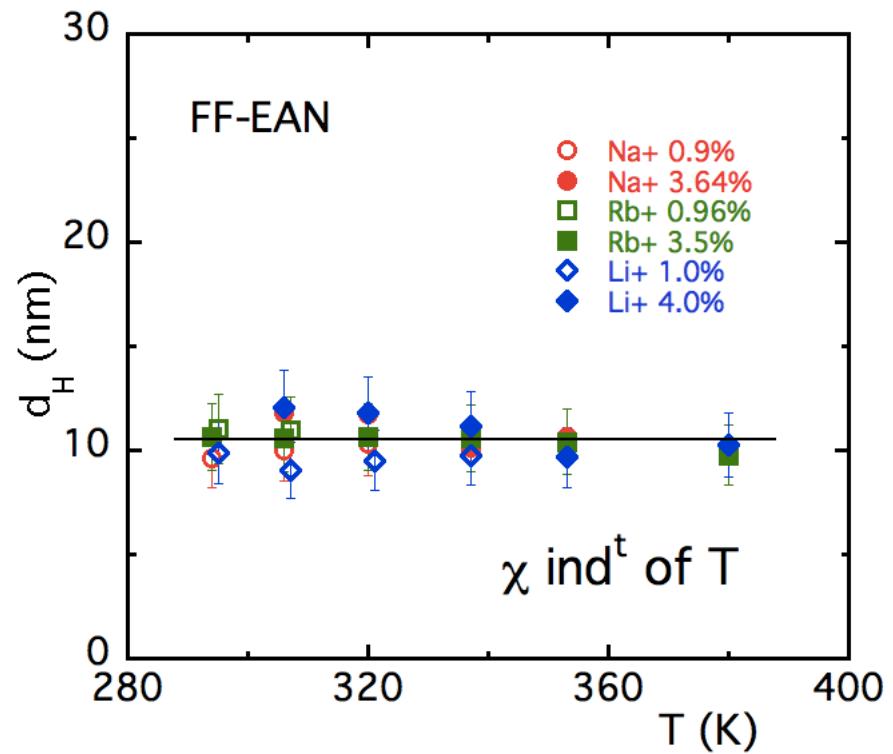
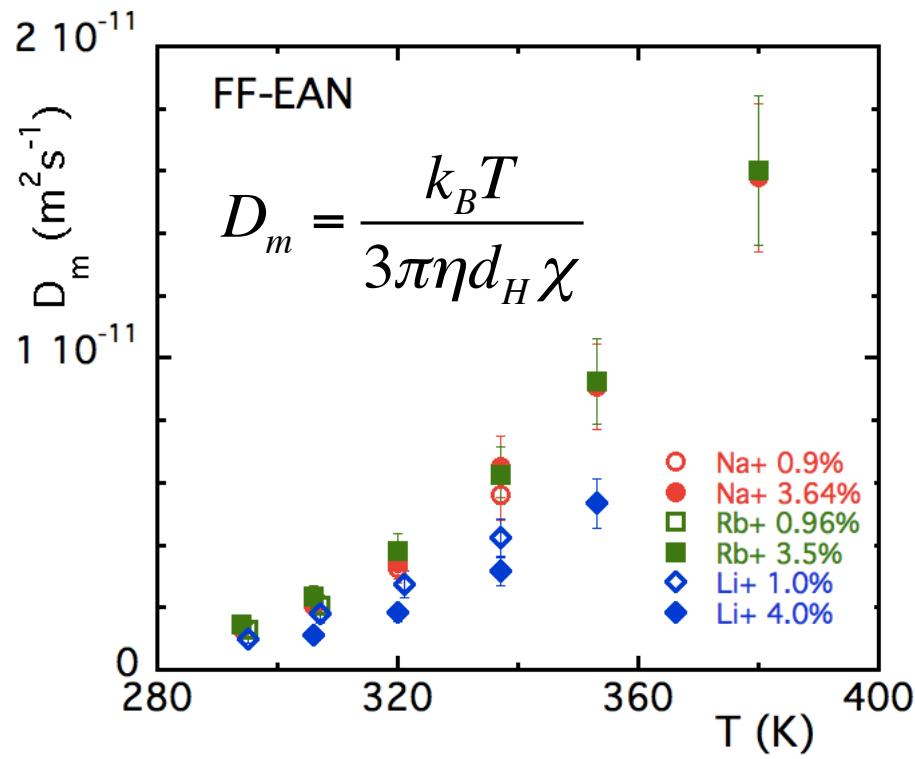
Na^+
 Rb^+ } Repulsion $A_2 > 0$

Li^+ Attraction $A_2 < 0$
 $S(q=0) > 1$



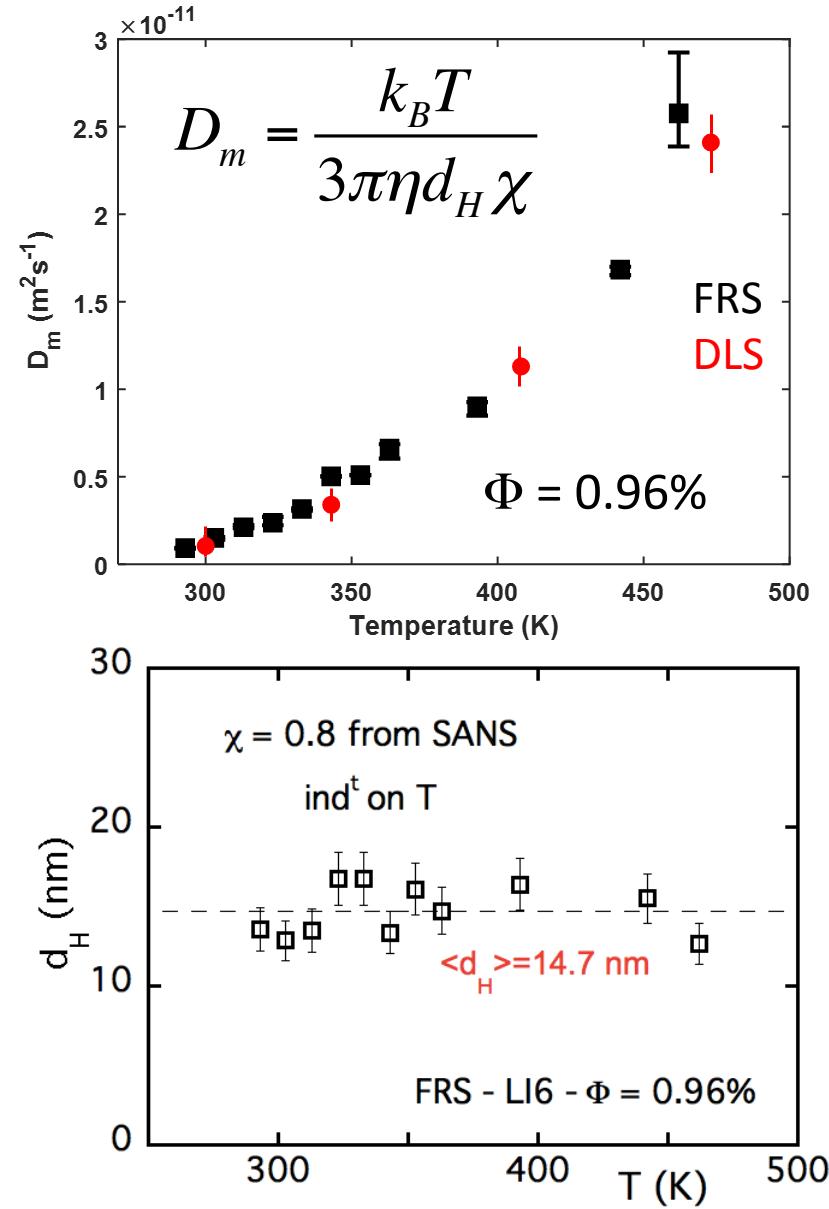
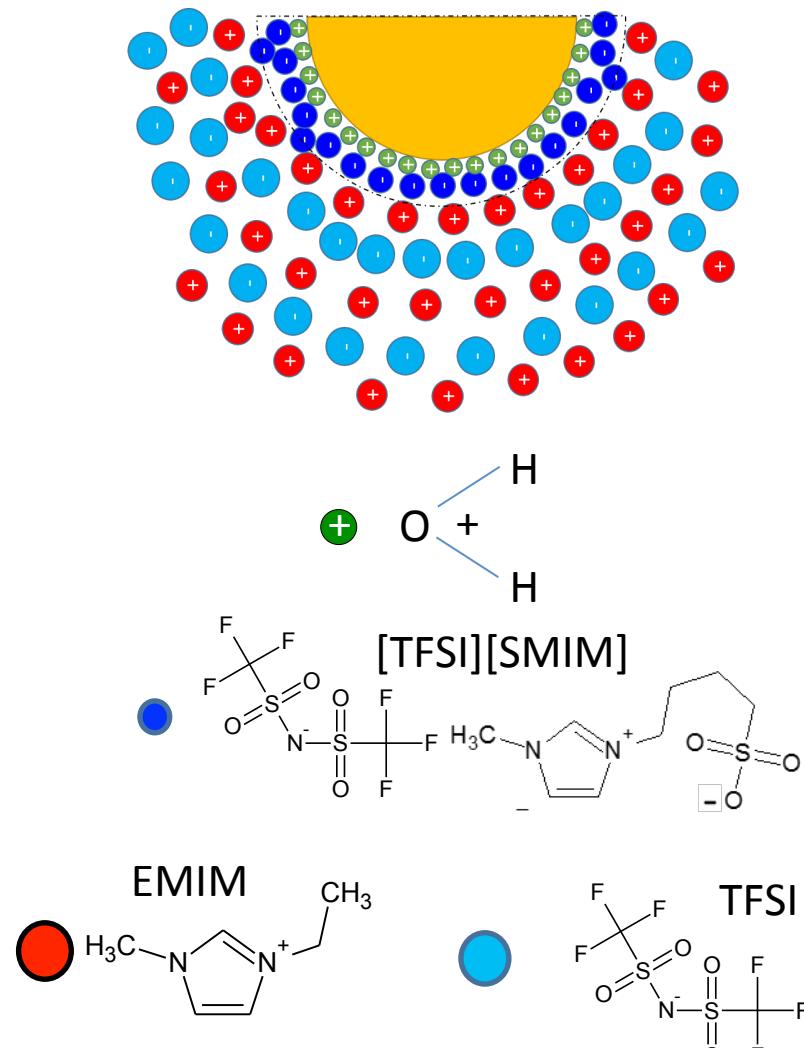
In case of repulsion: some counter-ions remain close to the NPs surface
(chemical titration, ASAXS)

FF based on EAN at T≥ 295K



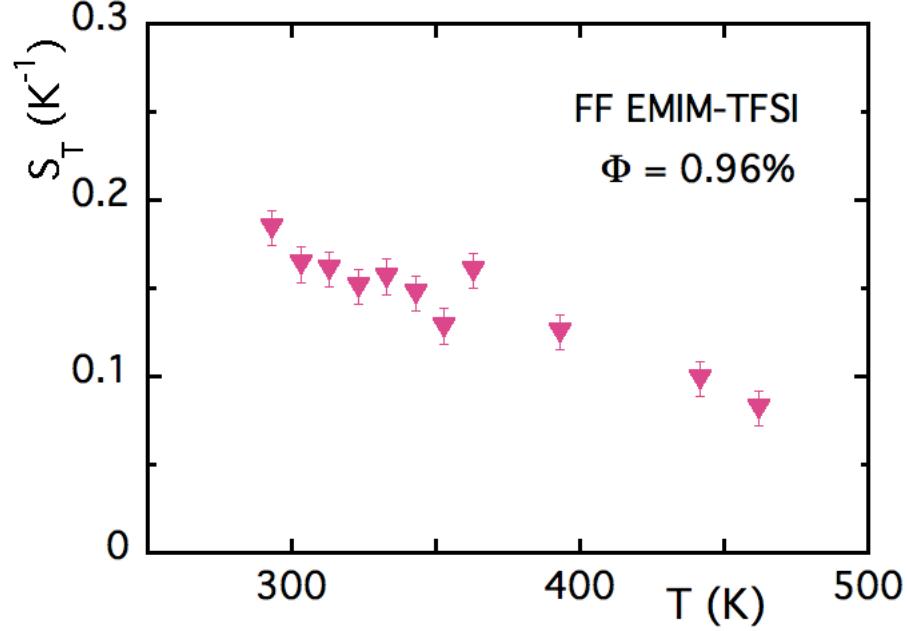
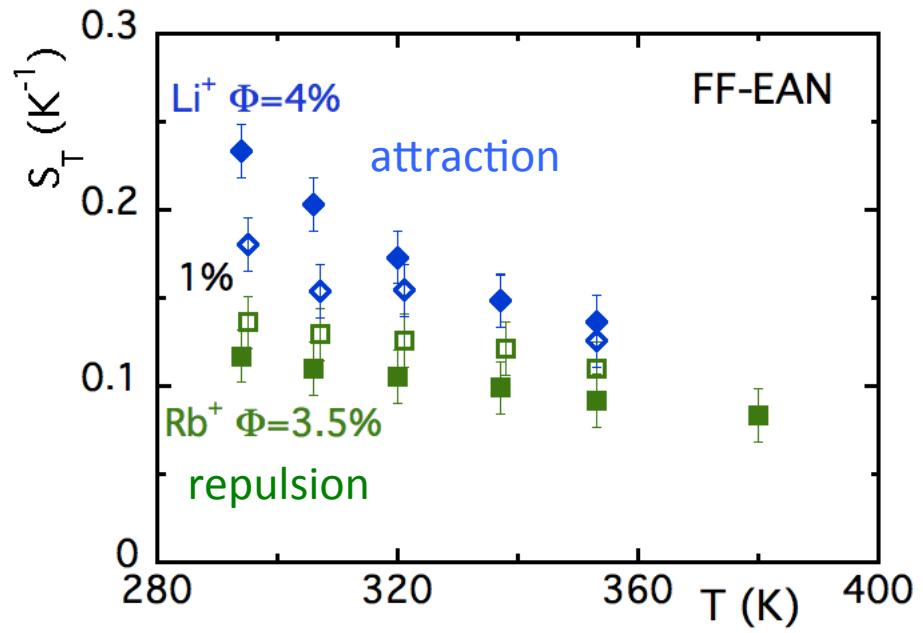
In the Φ -range 1-4%, diffusion coefficient D_m is ruled by viscosity $\eta(T)$ and interparticle interaction $\chi(\Phi)$ at 295K

FF based on EMIM-TFSI at $T \geq 295\text{K}$



IL-FF based on
NEA or EMIM-TFSI

$$S_T = \frac{\chi}{k_B T} \left(\hat{S}_{NP} - e\xi_0 S_e^{st} \right)$$

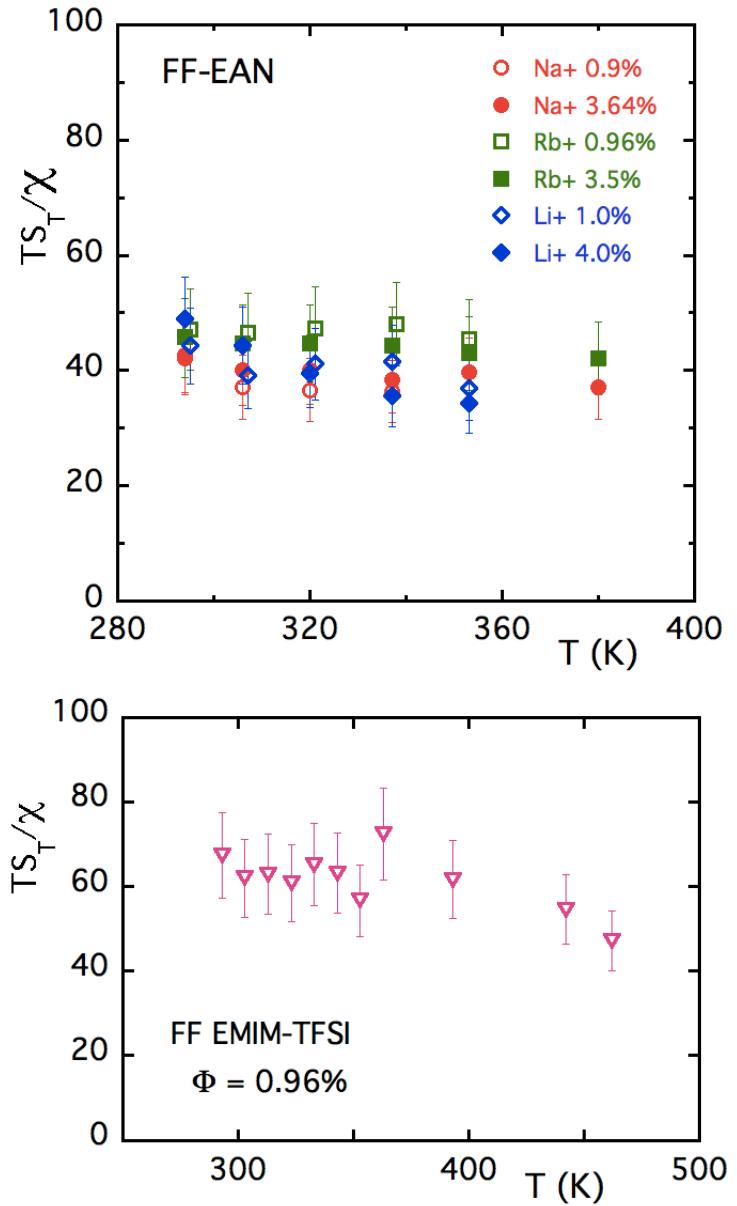


IL-FF based on NEA or EMIM-TFSI

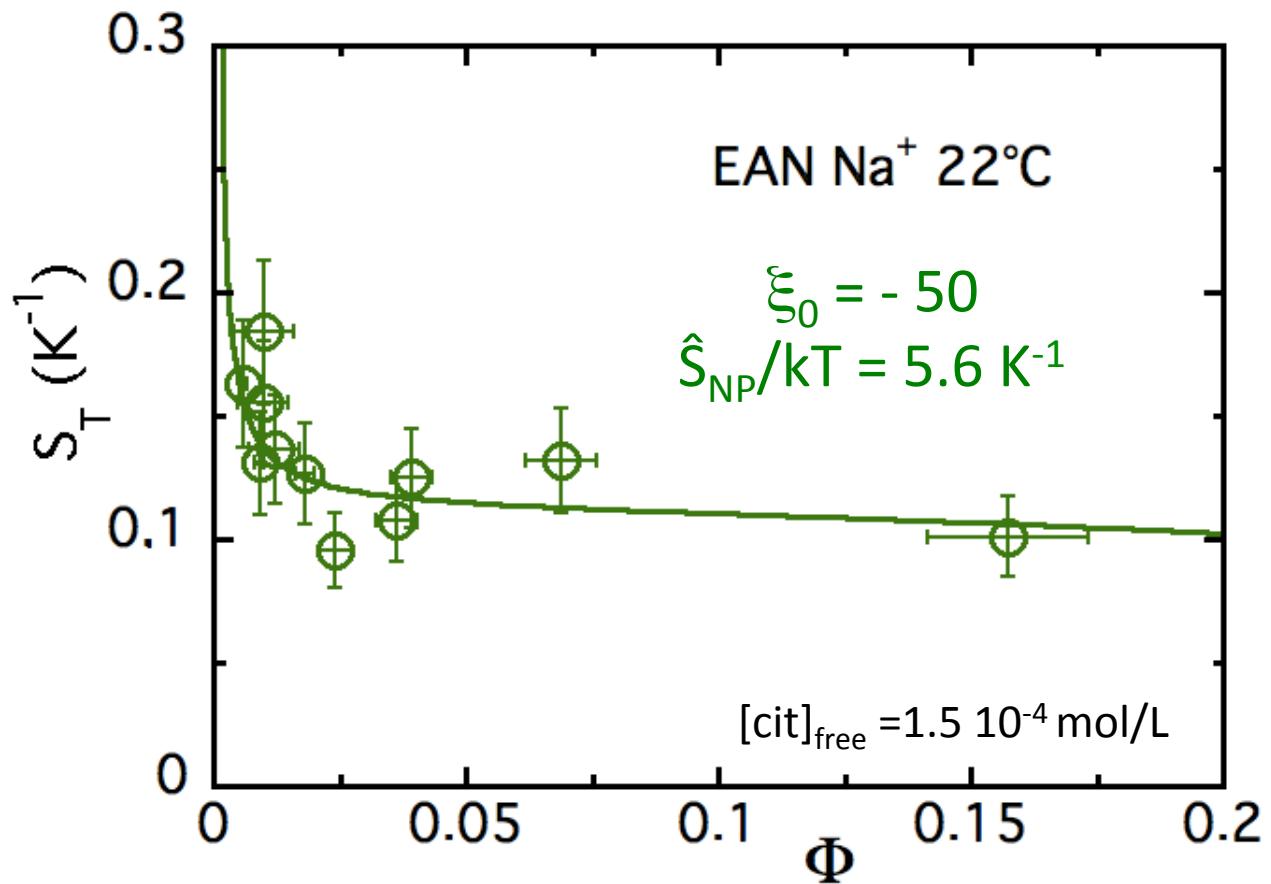
$$\frac{TS_T}{\chi} = \frac{\hat{S}_{NP} - e\xi_0 S_e^{st}}{k_B}$$

$$S_e^{st} = \frac{n_+ \hat{S}_+ - n_- \hat{S}_- + Z n \chi \hat{S}_{NP}}{n_+ + n_- + Z n \chi \xi_0}$$

To go further
we need measurements
at larger concentrations
.. They are in progress

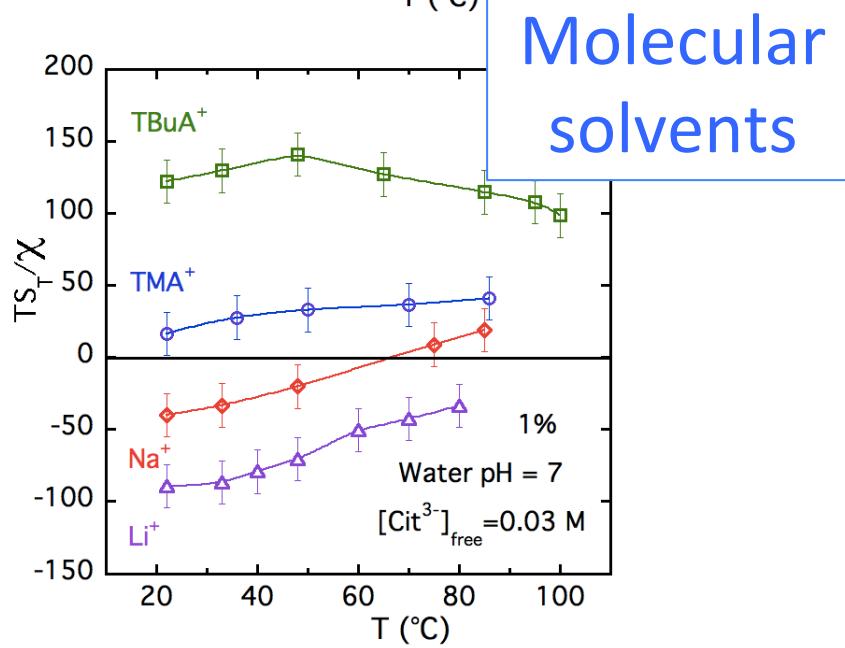
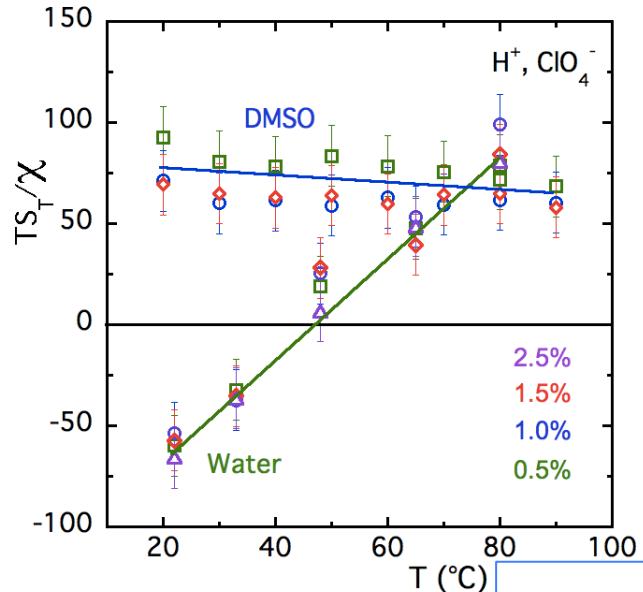


An example of Φ -dependence at room temperature for FF based on EAN with Na^+ counterions



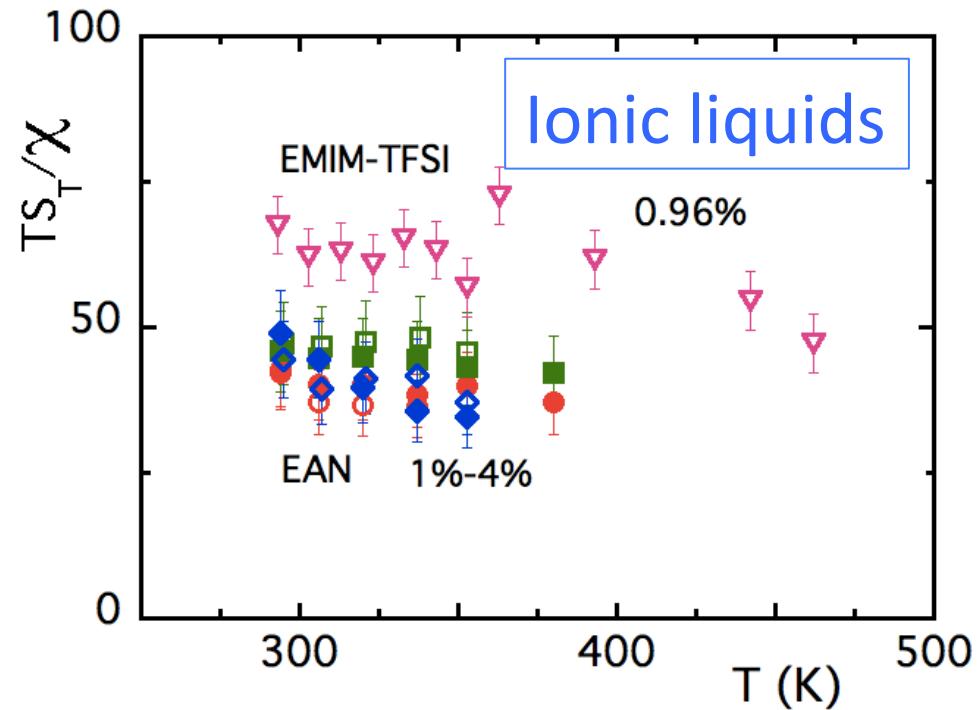
Tentative adjustment neglecting \hat{S}_+ and \hat{S}_- in front of \hat{S}_{NP}

Summary



T-dependences of

$$\frac{TS_T}{\chi} = \frac{\hat{S}_{NP} - e\xi_0 S_e^{st}}{k_B}$$



Thank you for your attention

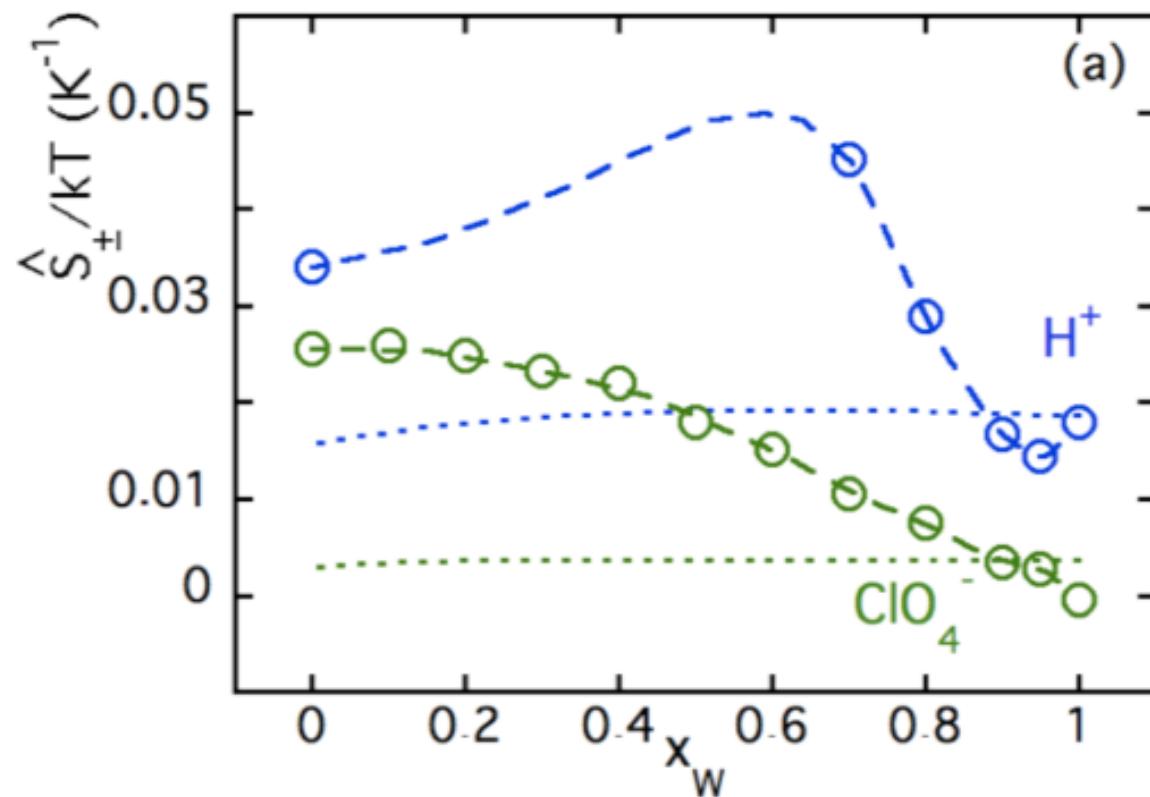
We acknowledge :

- Synchrotron SOLEIL for time-allocation at the SWING beam-line,
- Horizon 2020 FET-PROACTIVE project, MAGENTA, associated with the Grant n° 731976,



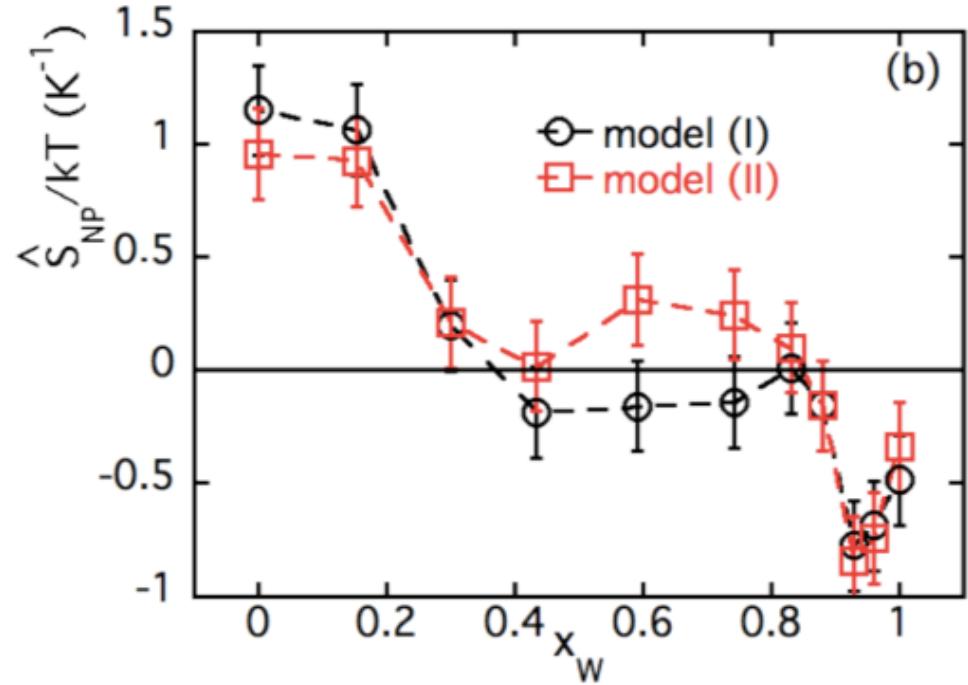
Contributions \hat{S}^+ and \hat{S}^- (of ions H⁺ and ClO₄⁻) in mixtures of water and DMSO deduced from:

- Born model (dotted lines)
- Enthalpy transfer model (dashed lines) $\hat{S}_{ion}(x_w) = \hat{S}_{ion}^{water} - \frac{\Delta_t H_{ion}^o(x_w)}{TN_a}$

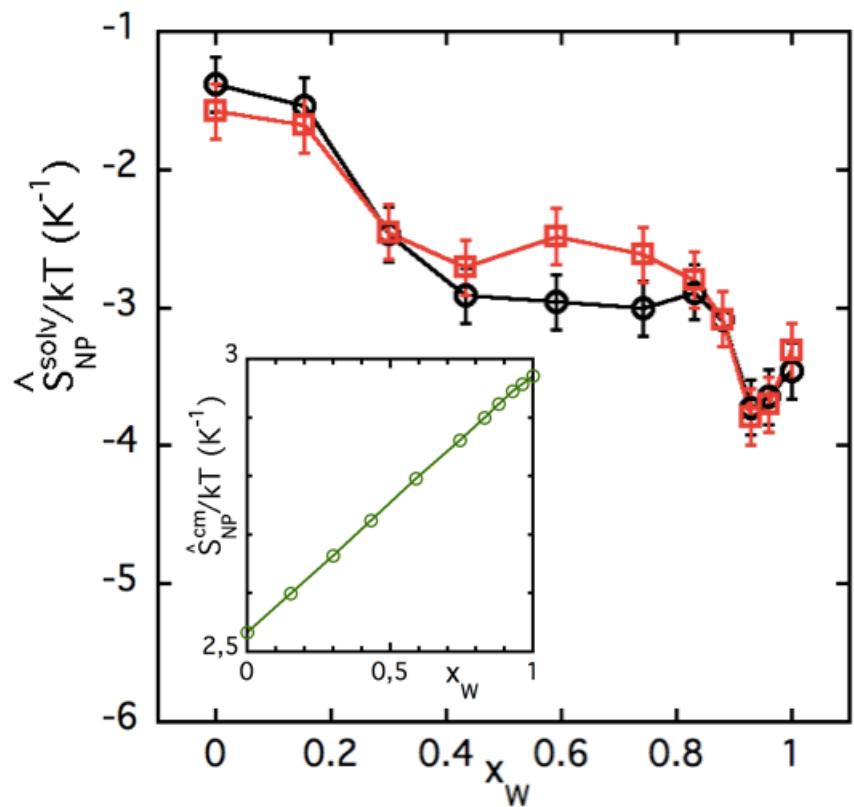


N. Takeyama, K. Nakashima *J. Solution Chem.* **17** (1988) 305

Y. Marcus, *Ion properties* (Marcel Dekker, New York 1997).

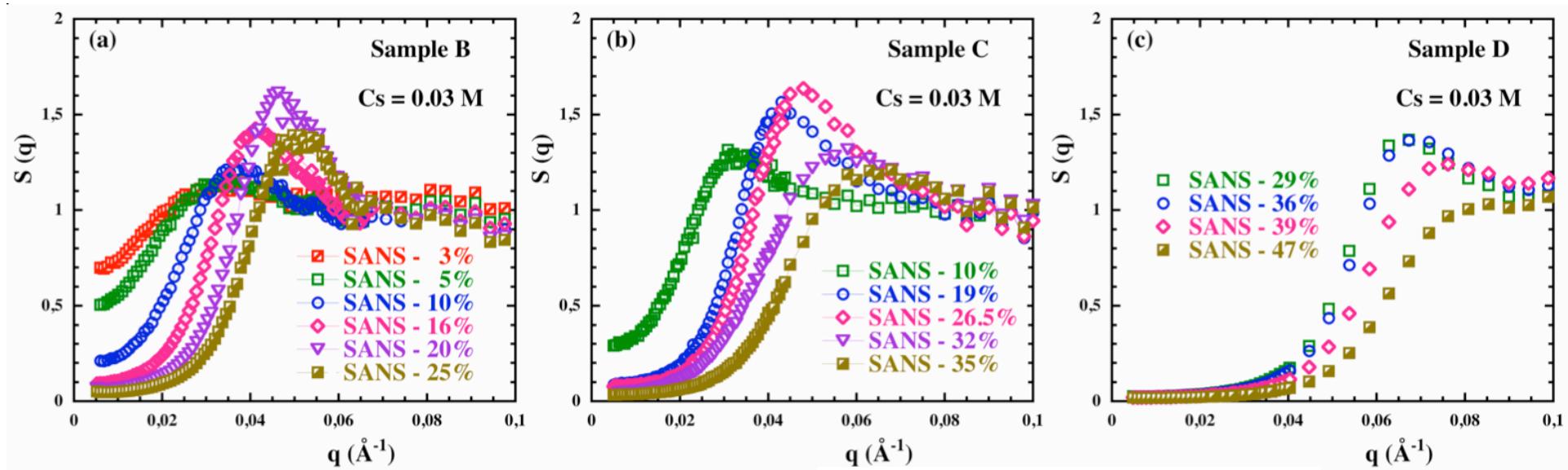


$$\hat{S}_{NP} = \hat{S}_{NP}^{cm} + \hat{S}_{NP}^{solv}$$



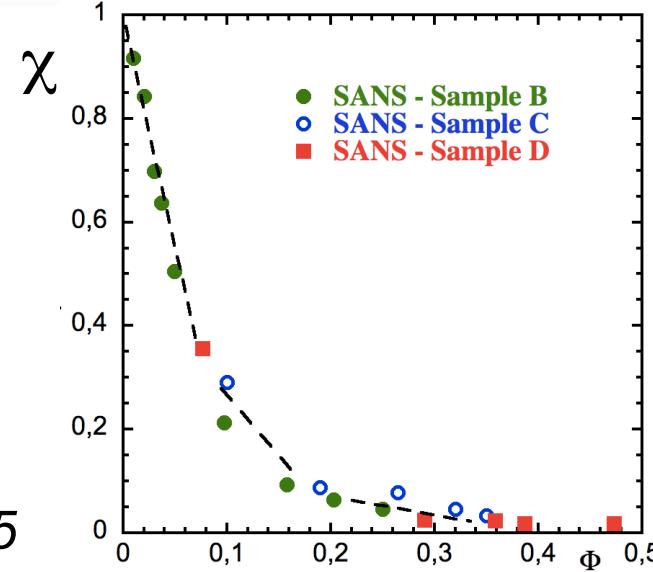
Influence of volume fraction Φ on the structure factor

SANS (LLB – ILL) $d_{NP} \sim 10$ nm $[cit]_{free} = 0.03$ mol/L



and on the
compressibility

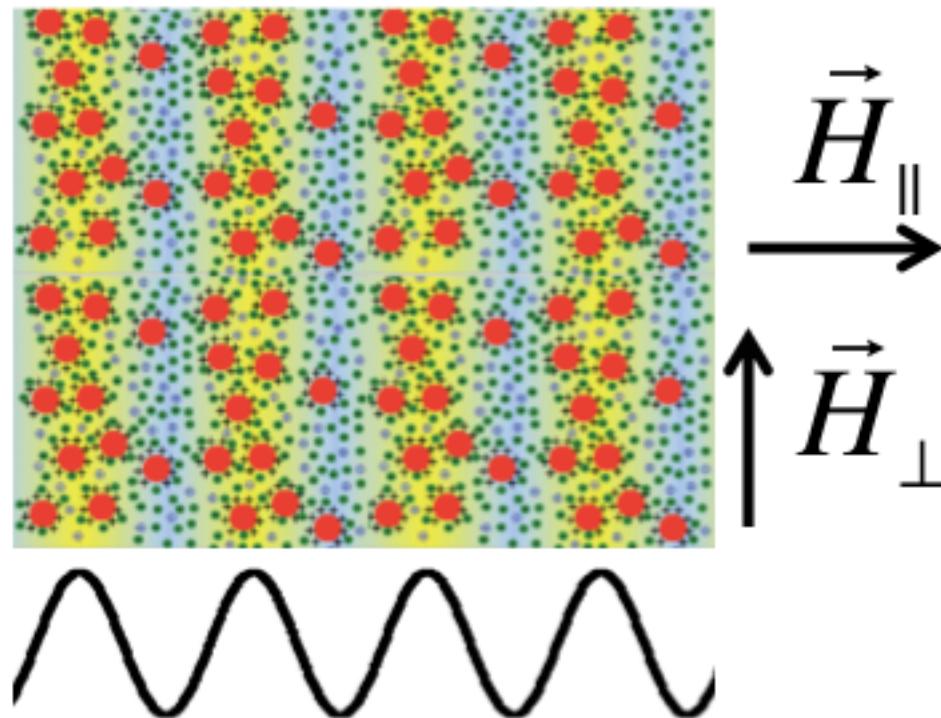
G. Mériguet et al
Magnetohydrodynamics 48 (2012) 415



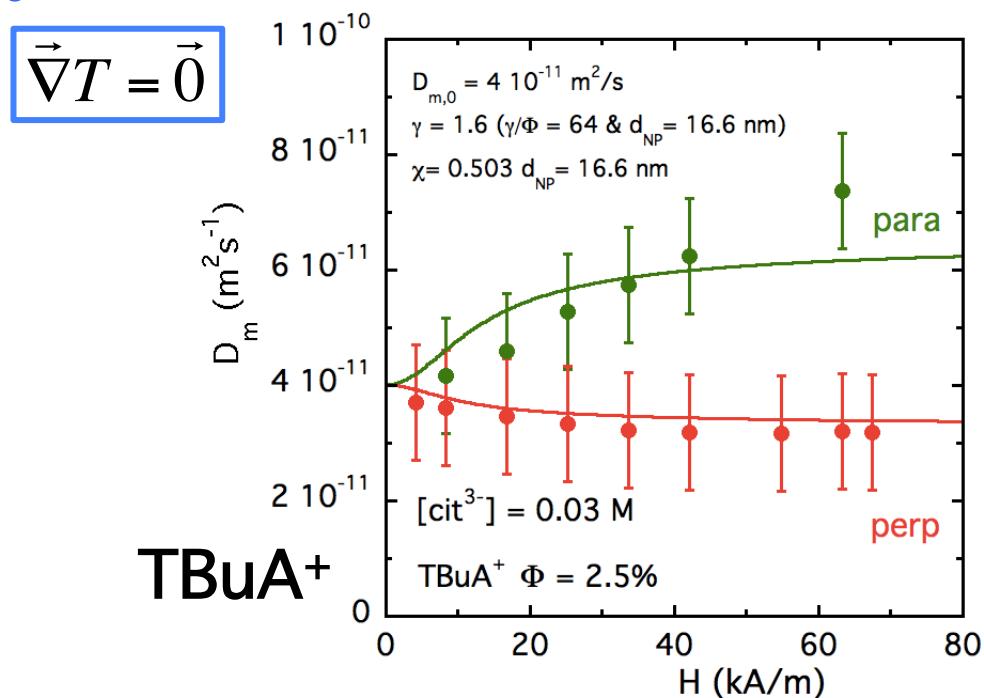
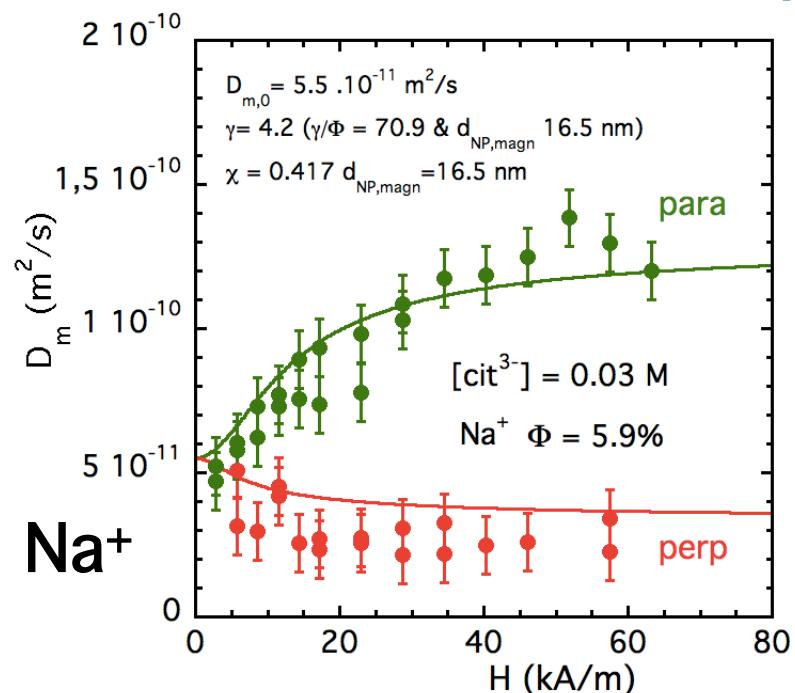
Na^+

Relaxation of the concentration grating under magnetic field

$$\vec{\nabla}T = \vec{0}$$



Under-field anisotropy of the diffusion coefficient



$$D_m^{\vec{H}_{\perp}} = \frac{kT}{\xi} \left(\frac{1}{\chi} - \alpha_{\lambda} \right)$$

with

$$D_m^{\vec{H}_{\parallel}} = \frac{kT}{\xi} \left(\frac{1}{\chi} + \beta_{\lambda} - \alpha_{\lambda} \right)$$

$$\xi_e = \xi + \lambda \gamma L(\xi_e) \quad \xi = \mu_0 \frac{m_S v_{NP} H}{kT}$$

$$\alpha_{\lambda} = \frac{\lambda \gamma L^2(\xi_e)}{1 - \lambda \gamma L'(\xi_e)}$$

$$\beta_{\lambda} = \frac{\gamma L^2(\xi_e)}{(1 - \lambda \gamma L'(\xi_e))(1 + (1 - \lambda) \gamma L'(\xi_e))}$$

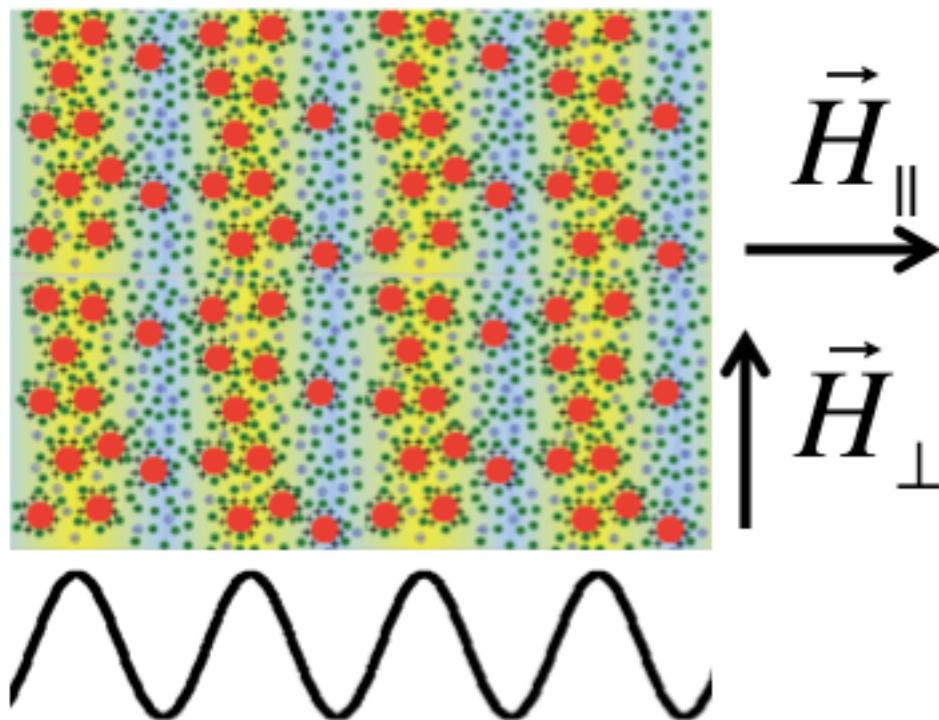
$$L(\xi) = \coth \xi - 1 / \xi$$

$$\gamma = \mu_0 \frac{m_S^2 v_{NP} \Phi}{kT}$$

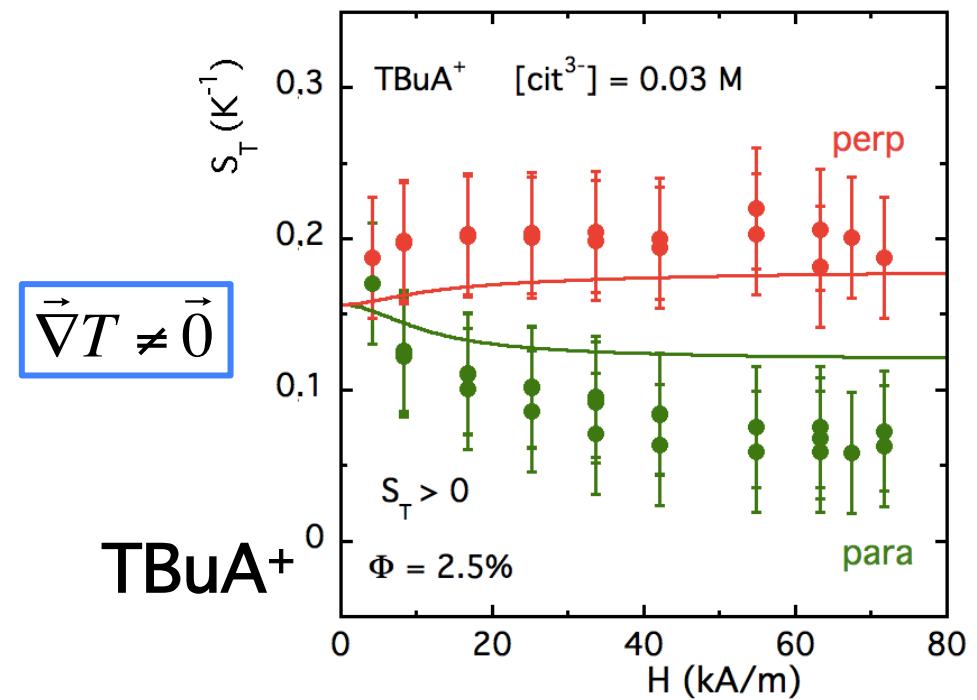
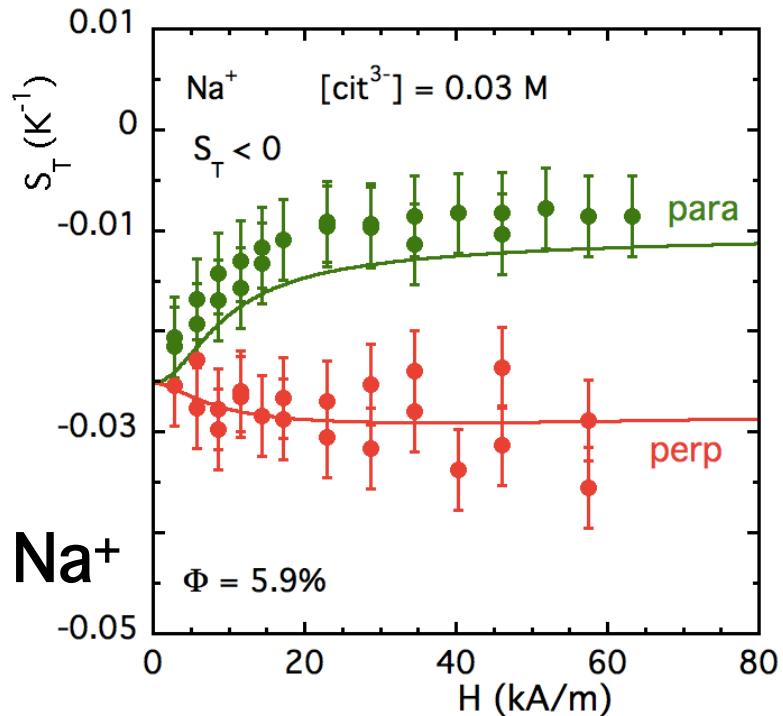
Soret coefficient measurements under magnetic field (in stationary conditions)

Local $\vec{\nabla}T$ either in phase or out-of-phase
with respect to $\vec{\nabla}\Phi$ depending on S_T sign

$$\vec{\nabla}T \neq \vec{0}$$



Under-field anisotropy of the Soret coefficient



$$S_T^{\vec{H}_{\perp}} = \frac{1}{kT \left(\frac{1}{\chi} - \alpha_{\lambda} \right)} \left[\frac{1}{n} \frac{\partial \Pi_{H=0}}{\partial T} + \hat{S}_{NP} - e\xi_0 S_e^{st} + k S_1 \right]$$

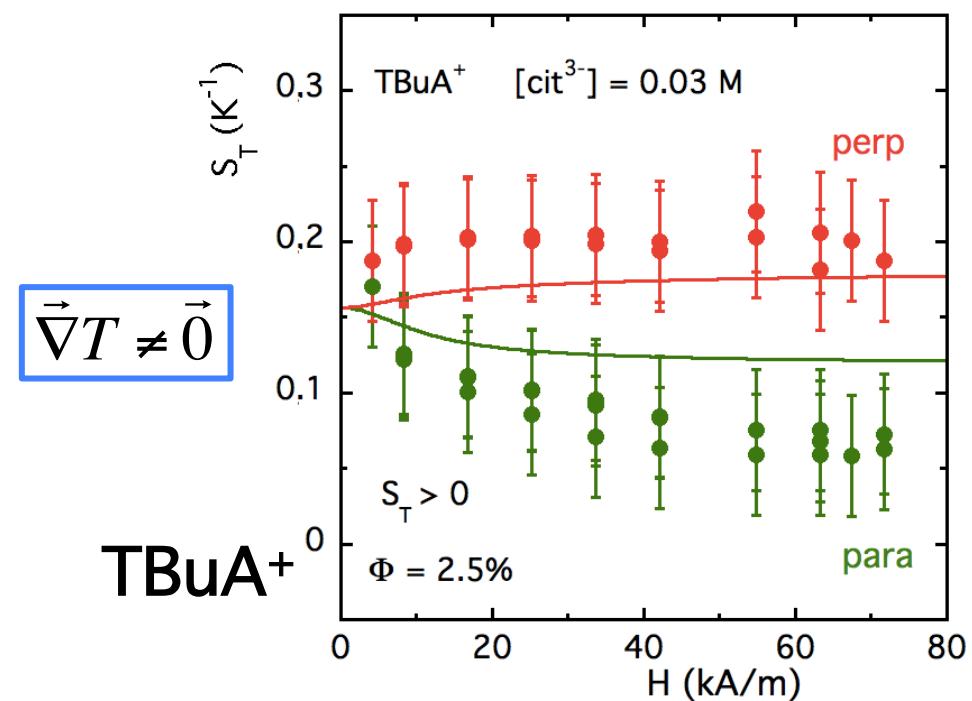
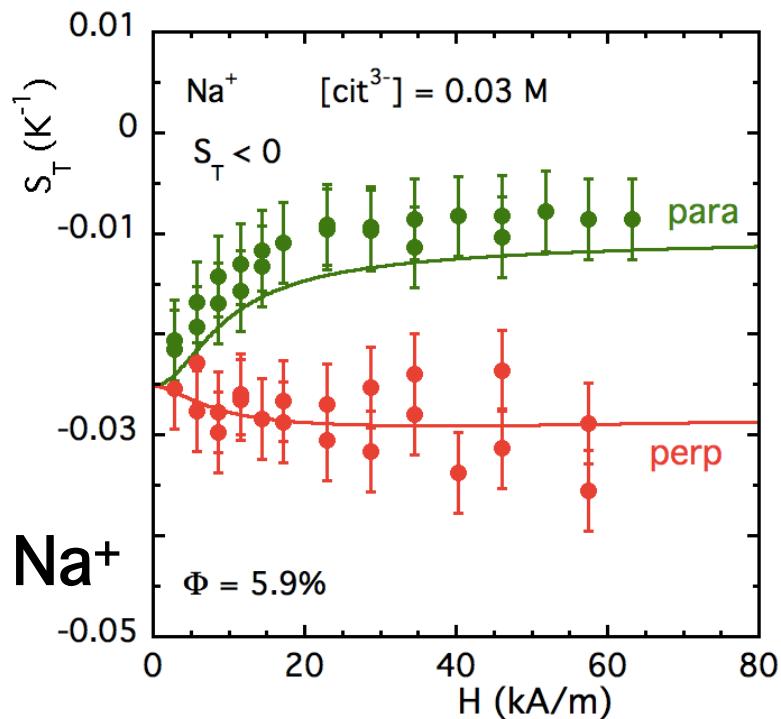
$$S_T^{\vec{H}_{\parallel}} = \frac{1}{kT \left(\frac{1}{\chi} + \beta_{\lambda} - \alpha_{\lambda} \right)} \left[\frac{1}{n} \frac{\partial \Pi_{H=0}}{\partial T} + \hat{S}_{NP} - e\xi_0 S_e^{st} + k(S_1 - S_2) \right]$$

$$S_1 = \frac{\xi_e L(\xi_e)}{1 - \lambda \gamma L'(\xi_e)} - \ln \frac{sh \xi_e}{\xi_e}$$

with

$$S_2 = \beta_{\lambda} \frac{\xi_e L'(\xi_e)}{L(\xi_e)}$$

Under-field anisotropy of the Soret coefficient



The ordering between $S_T^{H\perp}$ and $S_T^{H\parallel}$ depends on the sign of $S_T^{H=0}$ thus on the nature of the counterions

Increasing Soret coefficient by field application may allows increasing thermoelectric energy conversion in thermocells (*).

(*) T. Salez et al *Phys. Chem. Chem. Phys.* **19** (2017) 9409