Ahmed El Alaoui: Optimization of mean-field spin glasses

We consider the question of computing an approximate ground state configuration of an Ising (mixed) p-spin Hamiltonian H_N from a bounded number of gradient evaluations.

I will present an efficient algorithm which exploits the ultra-metric structure of the superlevel sets of H_N in order to achieve an energy E_* characterized via an extended Parisi variational principle. Time permitting, I will discuss the following points:

- If H_N has no overlap gap, then E_* is the ground state energy.

- E_* is the best energy achievable by a class of message passing algorithms.

- In the case of the 3-spin model, which is known to exhibit overlap gap, preliminary numerical evaluations suggest that E_* is strictly lower than the so-called "threshold" energy, which is thought to lower-bound Glauber-type dynamics.

This is joint work with Andrea Montanari and Mark Sellke.