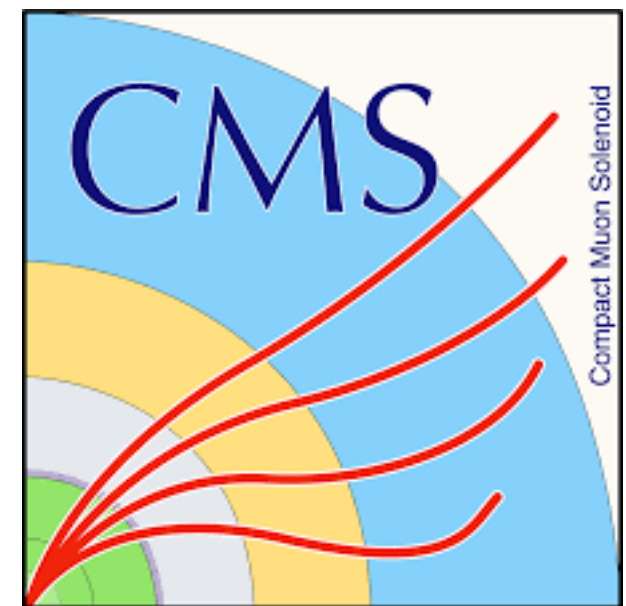
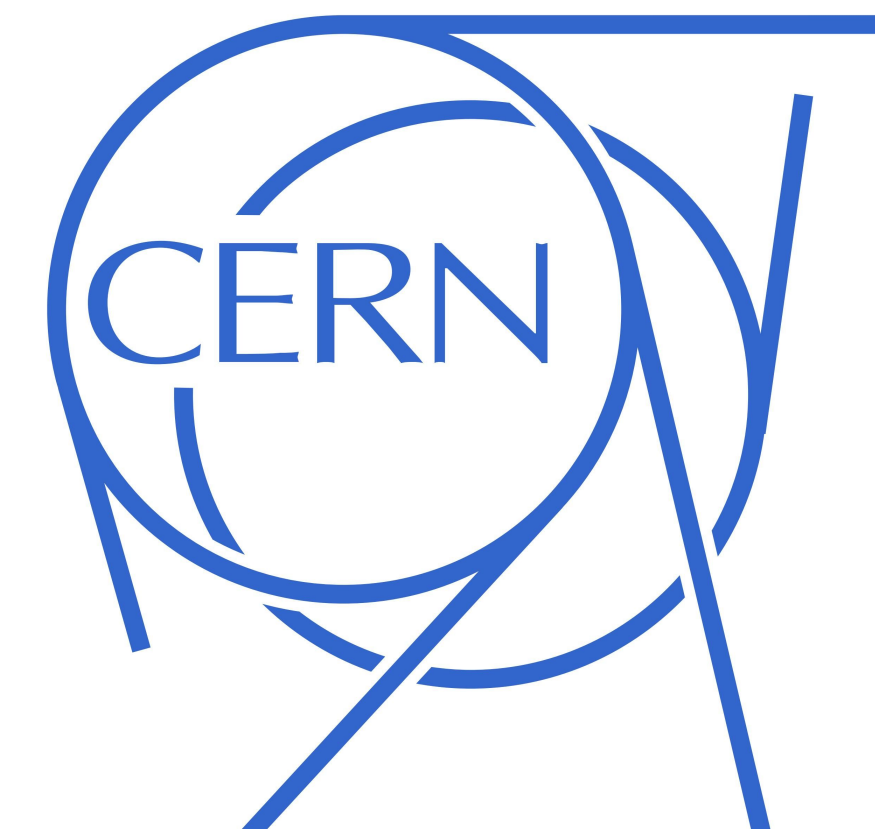


MACHINE LEARNING, NUCLEAR PHYSICS, AND ALGORITHM DEVELOPMENT FOR DATA ANALYSIS IN NUCLEAR RESEARCH

MICHELLE KUCHERA
DAVIDSON COLLEGE

JOINT ICTP-IAEA WORKSHOP ADVANCED SCHOOL ON
COMPUTATIONAL NUCLEAR SCIENCE

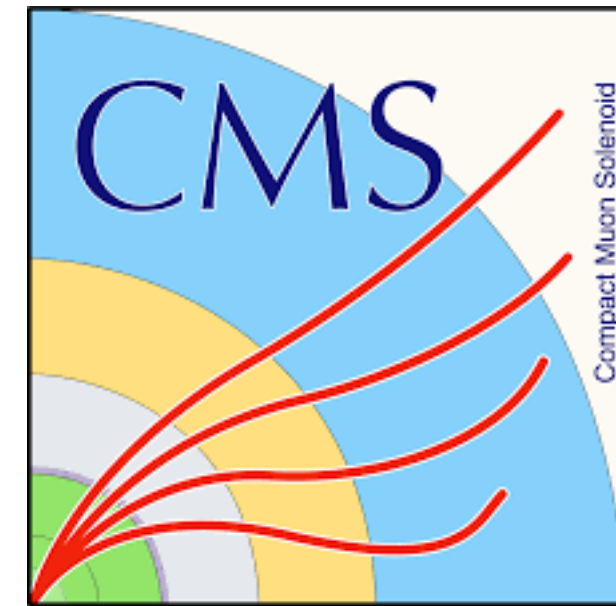
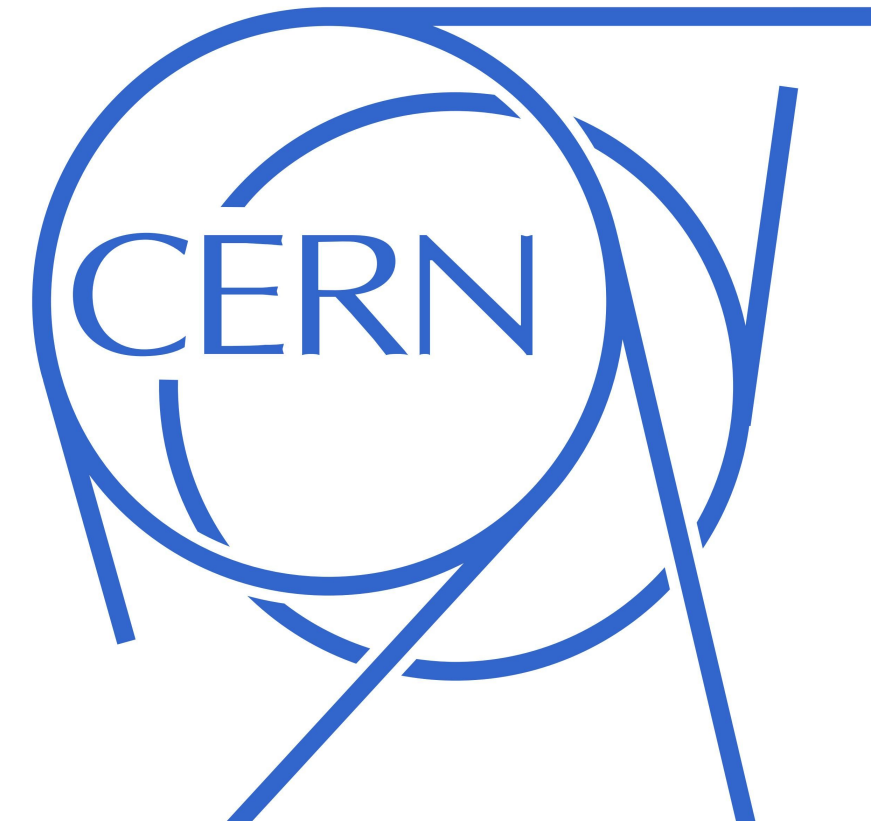
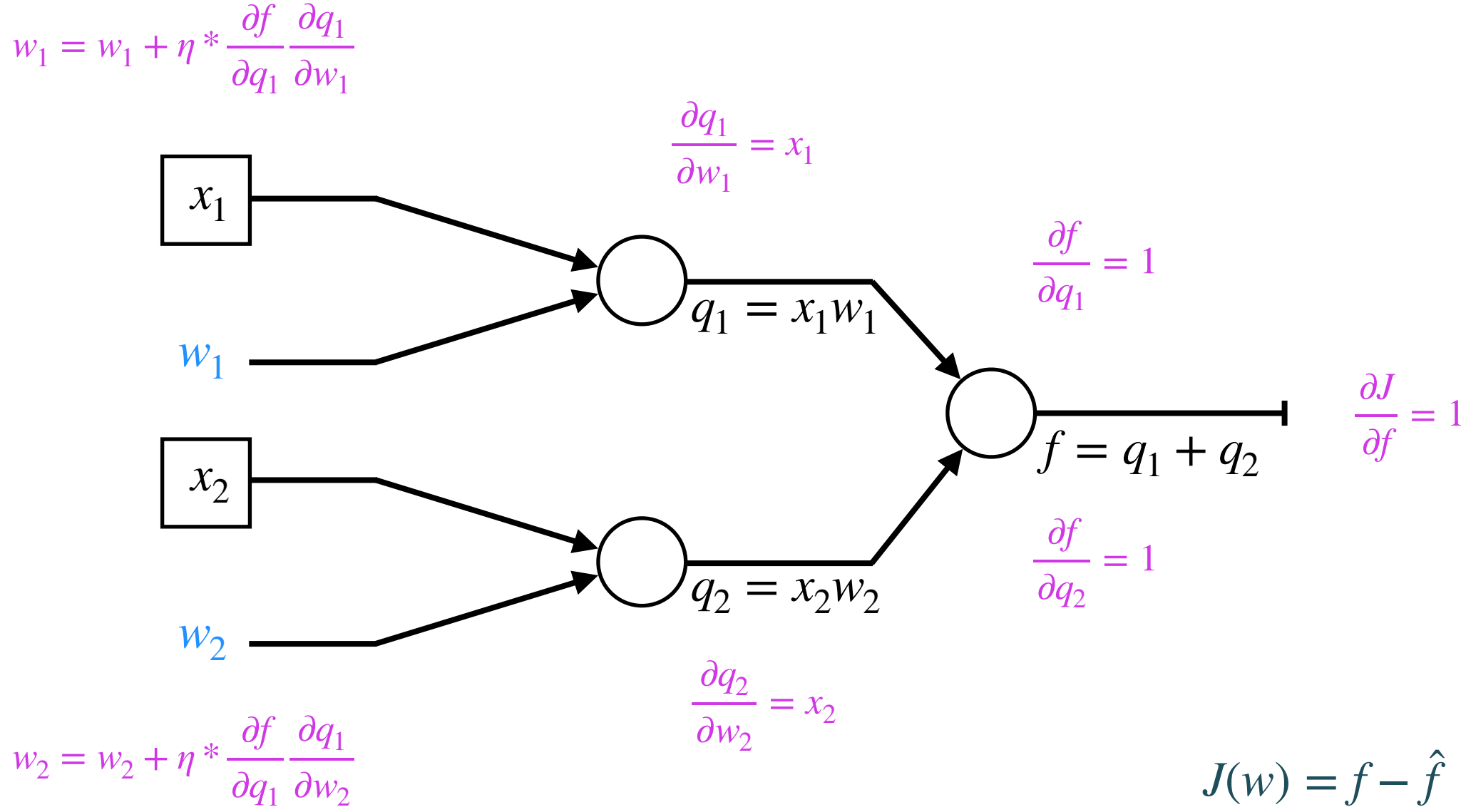
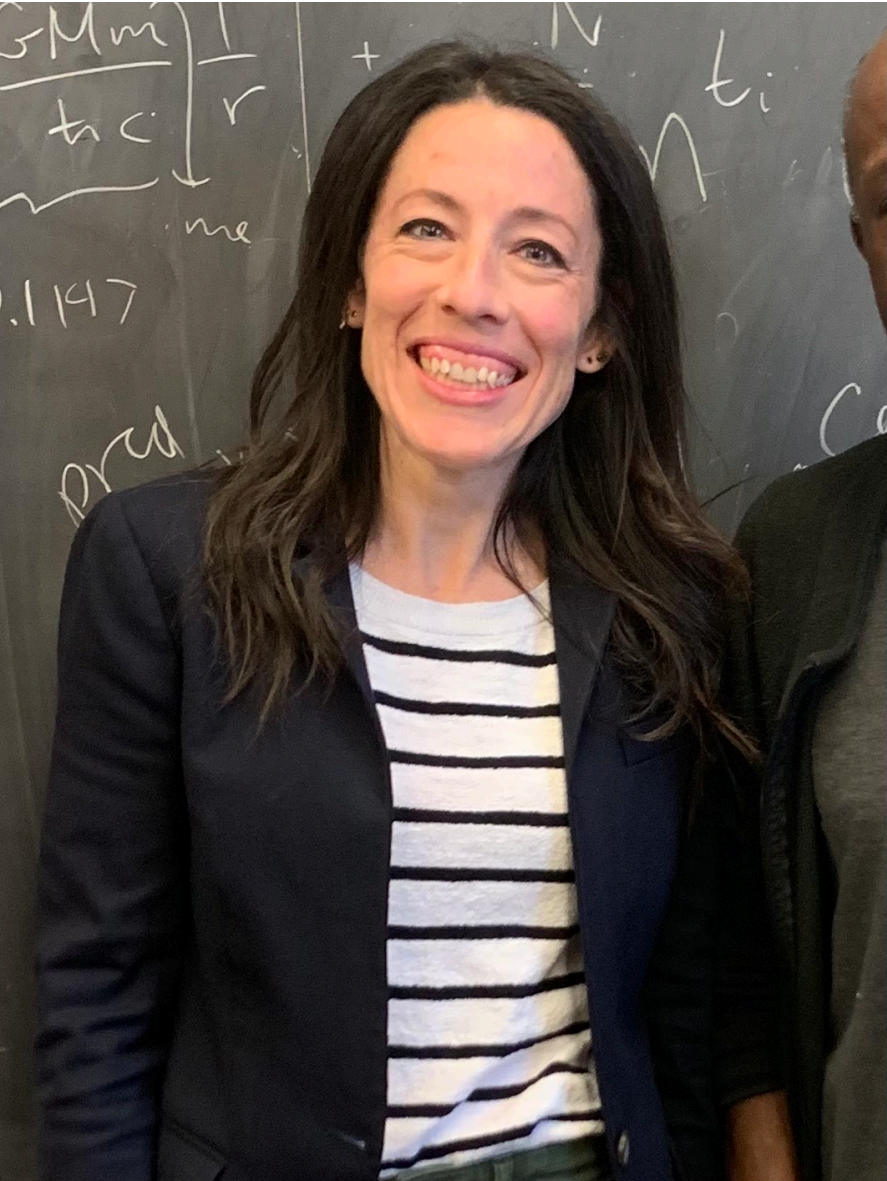
23 MAY 2022



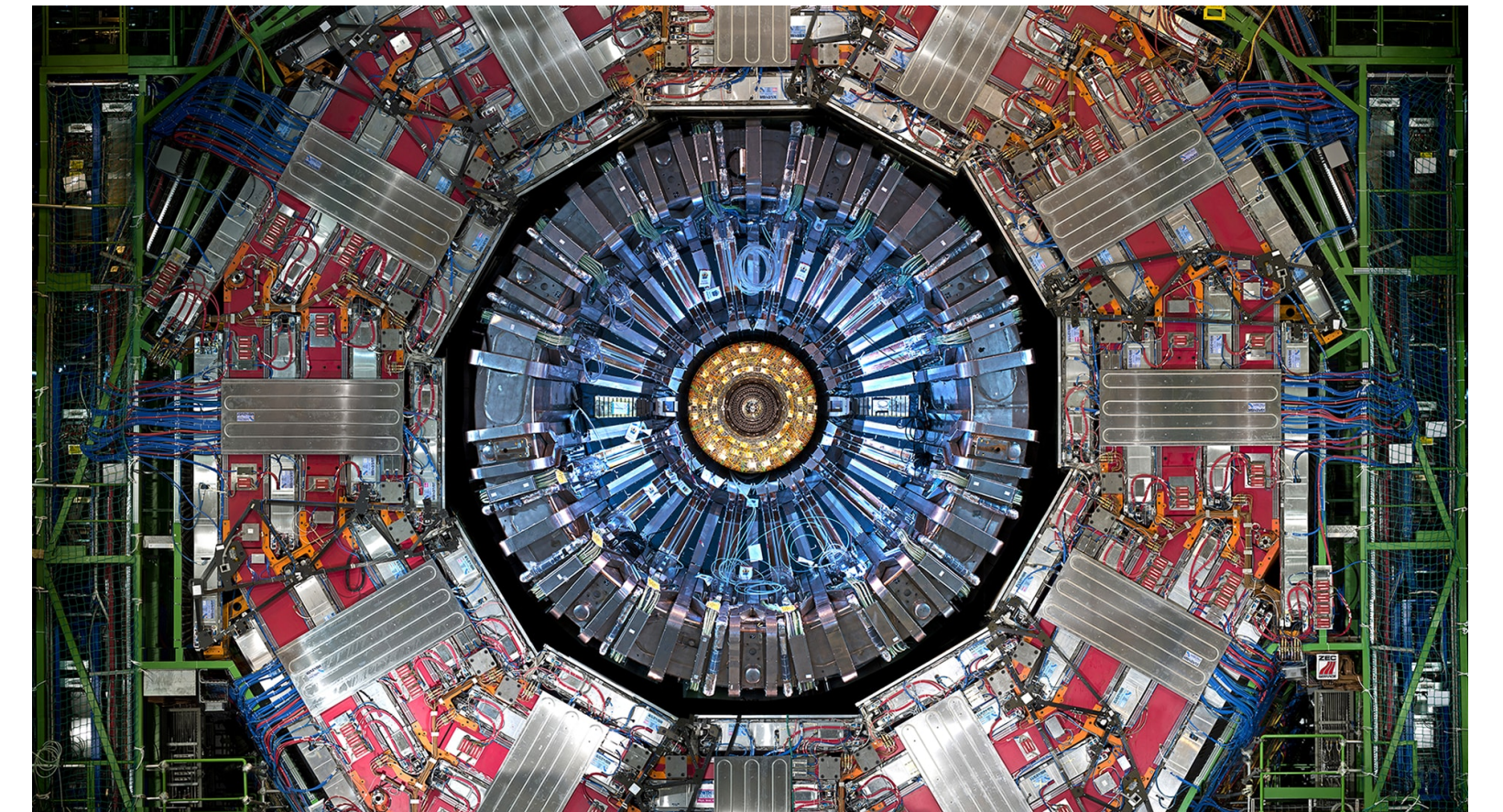
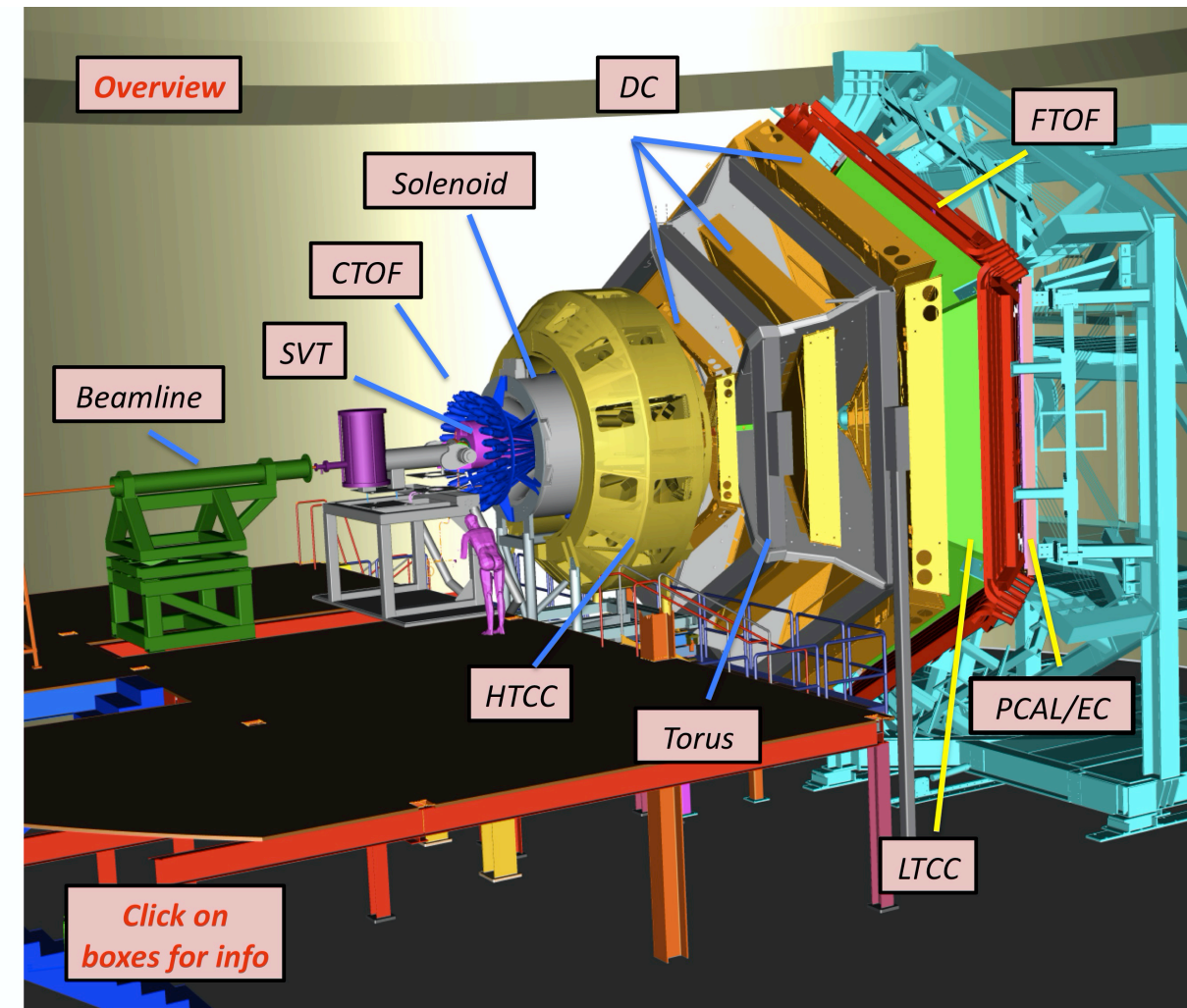
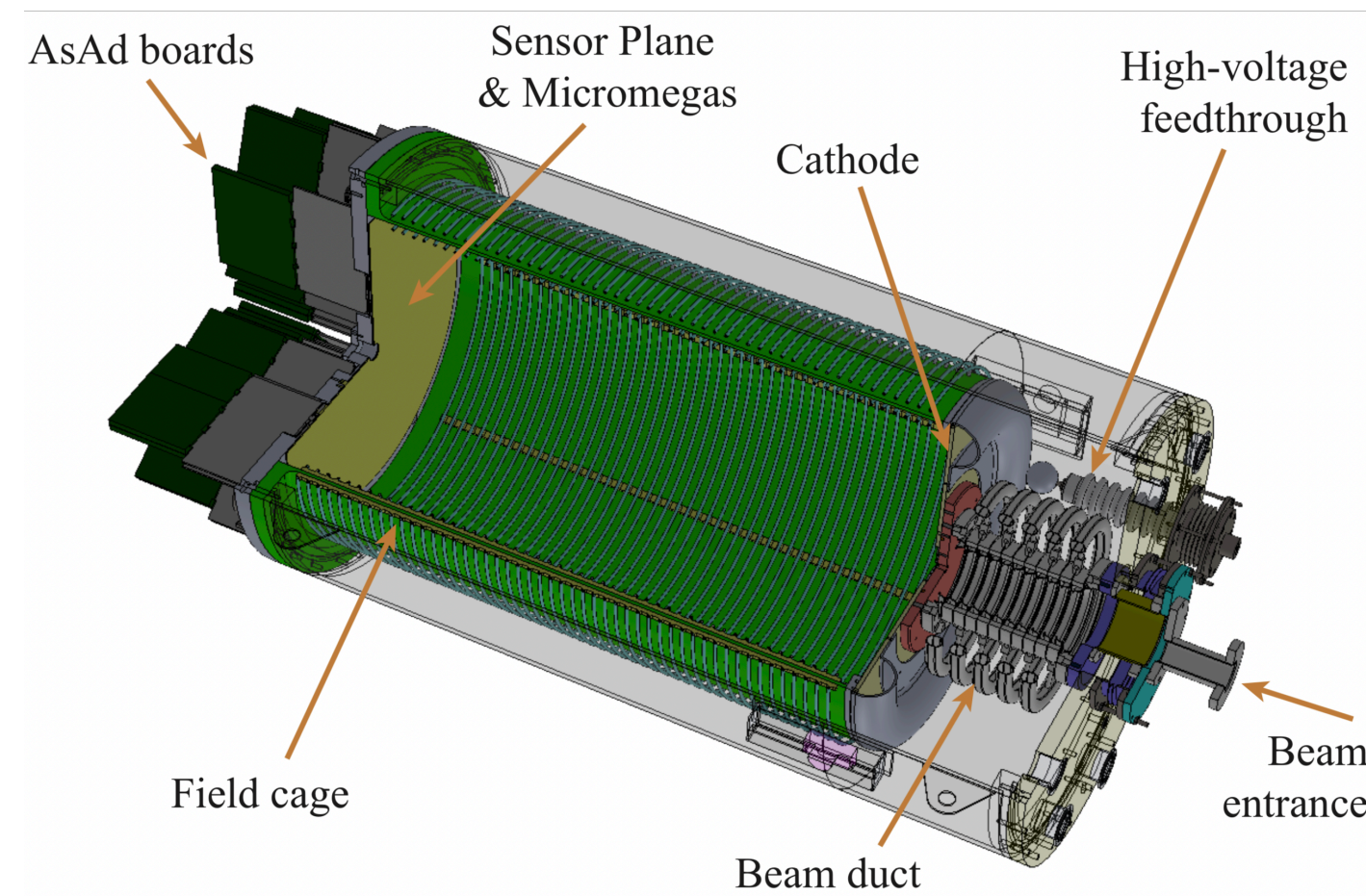
MICHELLE KUCHERA

B.S., M.S. PHYSICS

M.S., PH.D. COMPUTATIONAL SCIENCE



EXPERIMENTAL DATA



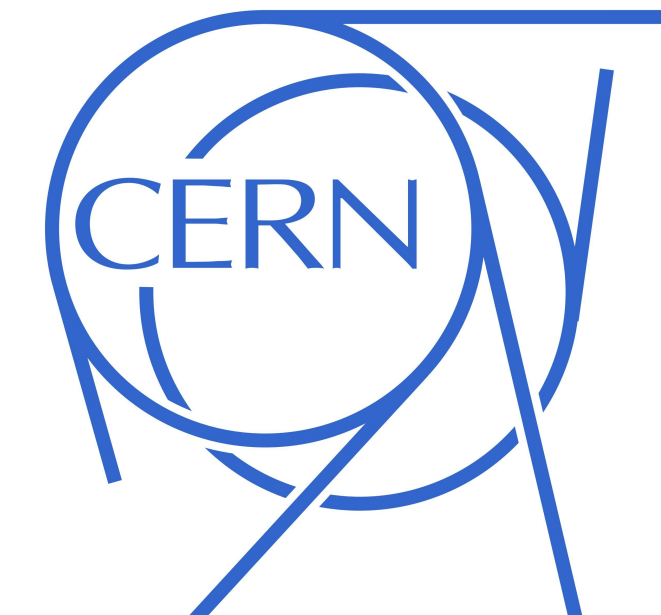
J. BRADT ET. AL., NUCLEAR INSTRUMENTS AND METHODS, 2017.



AT-TPC

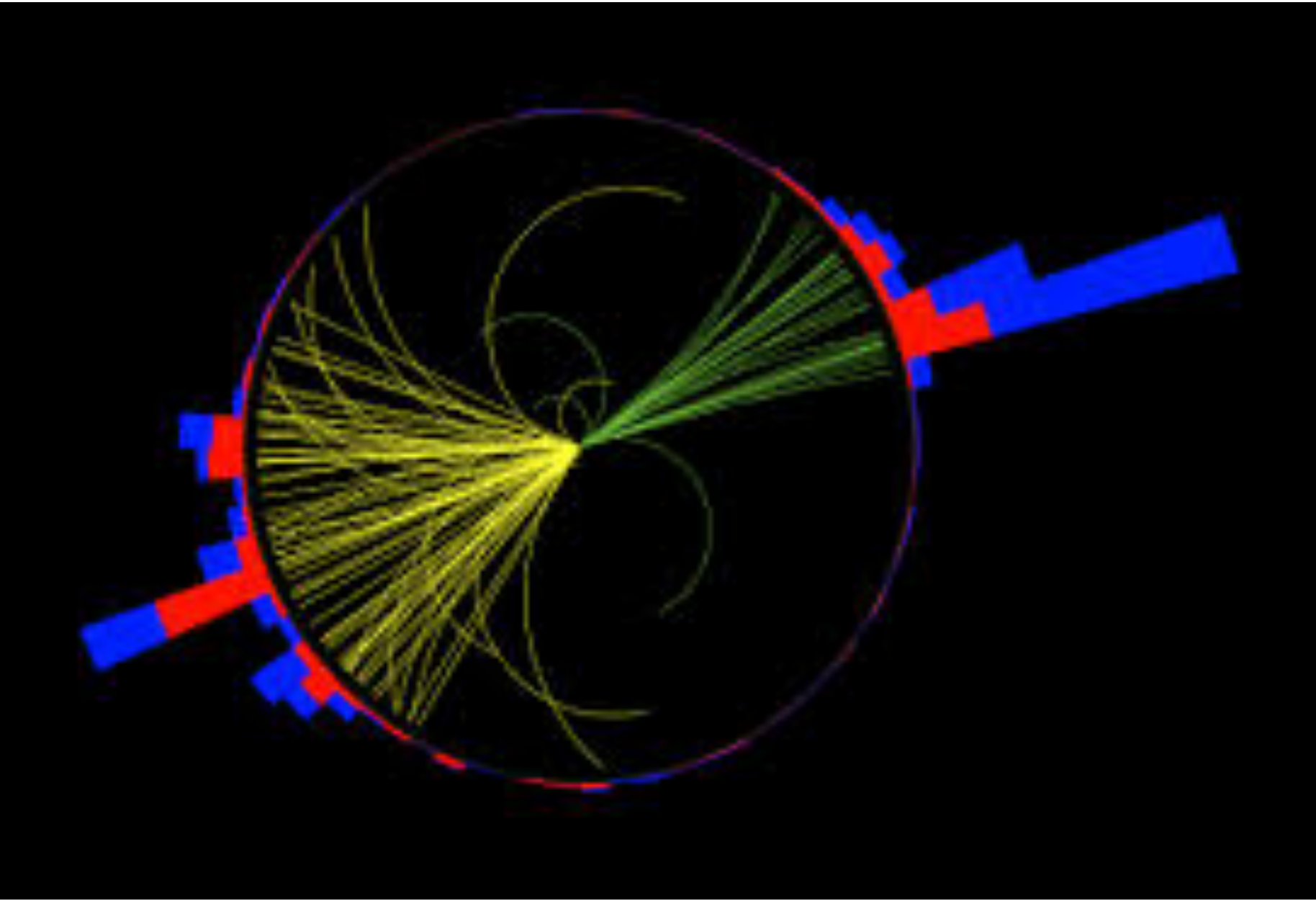
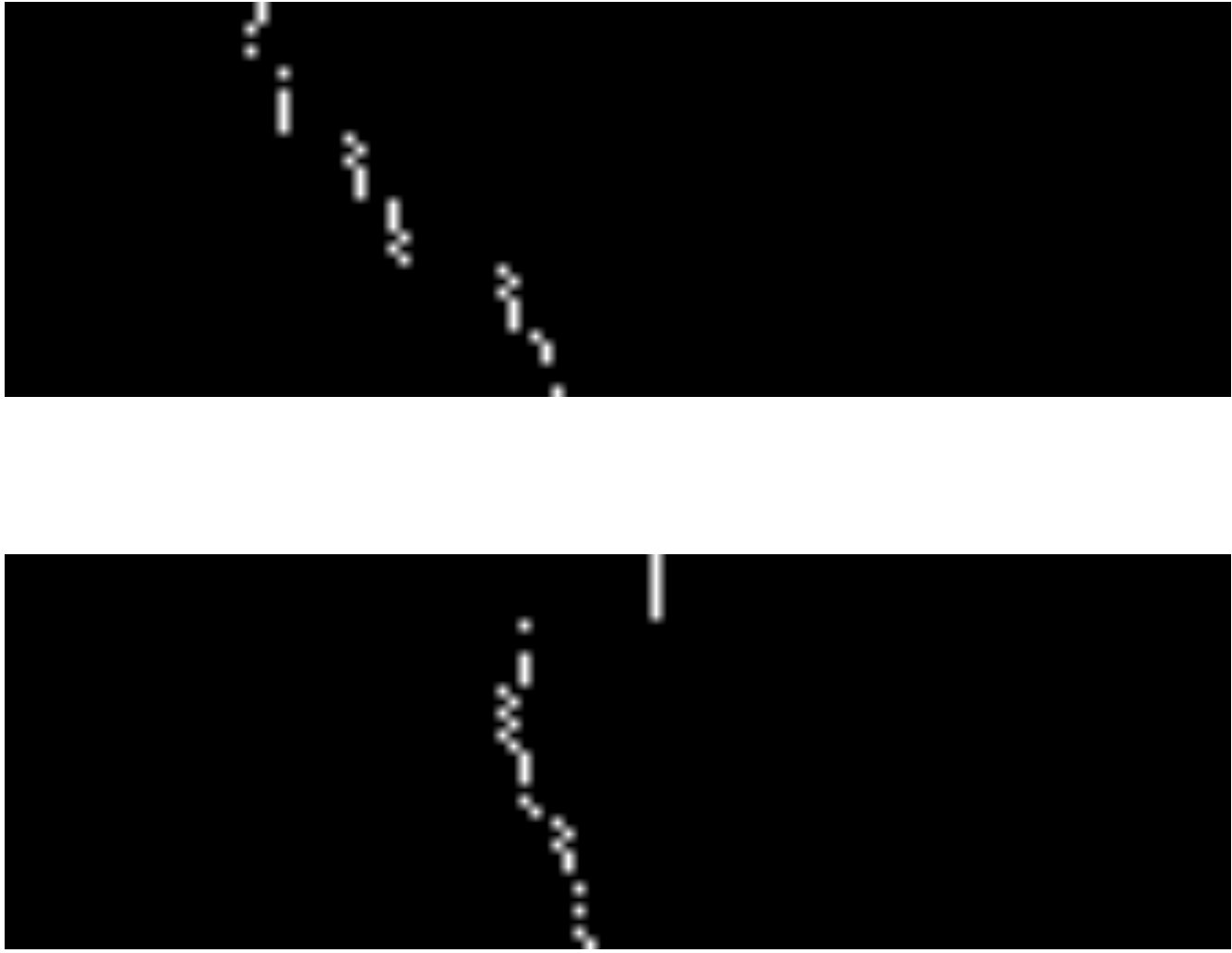
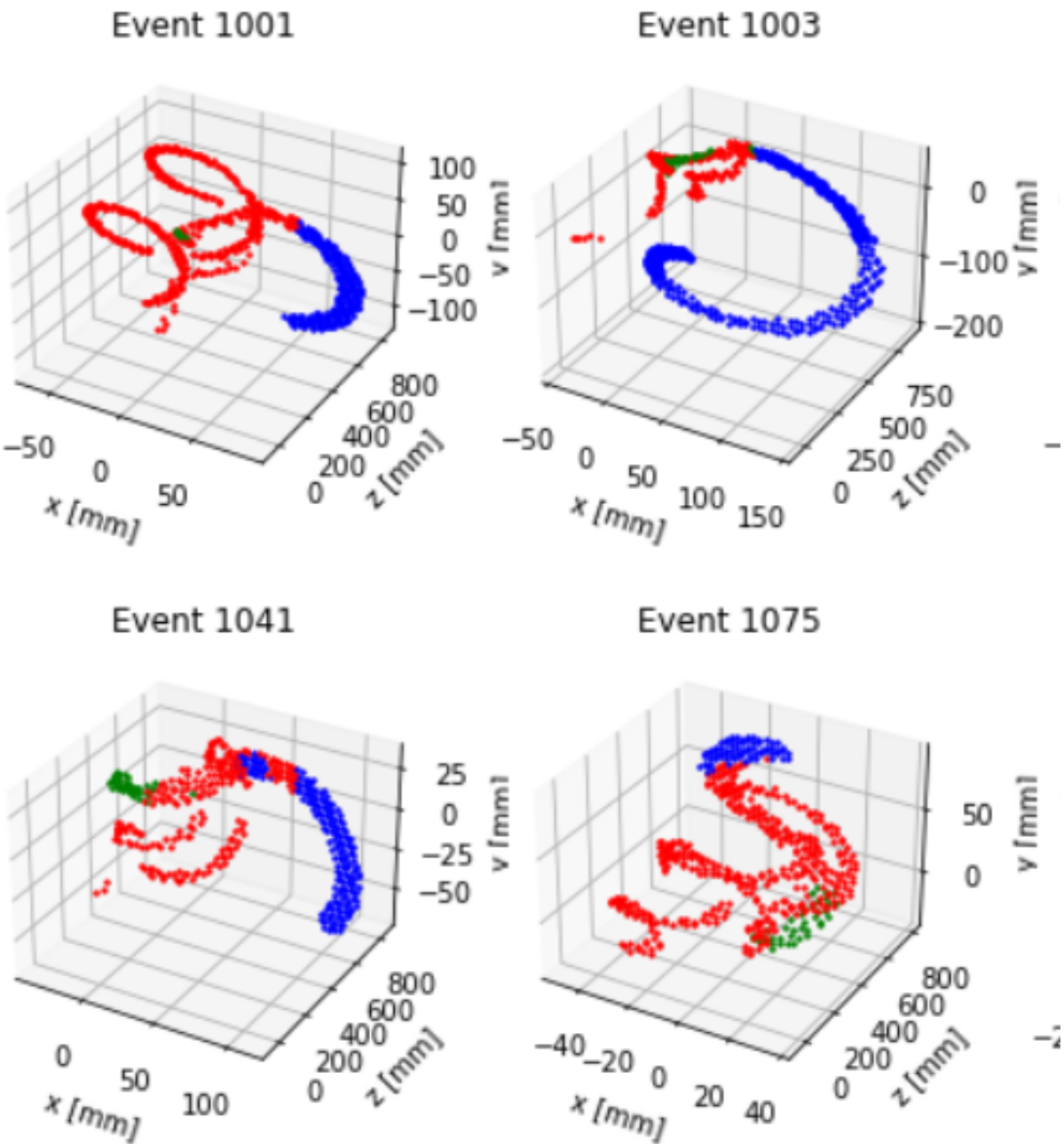


CLAS 12



CMS

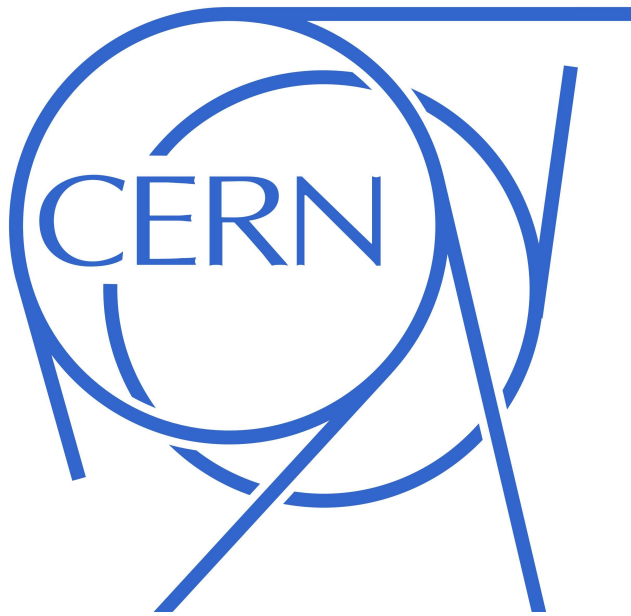
EXPERIMENTAL DATA



AT-TPC

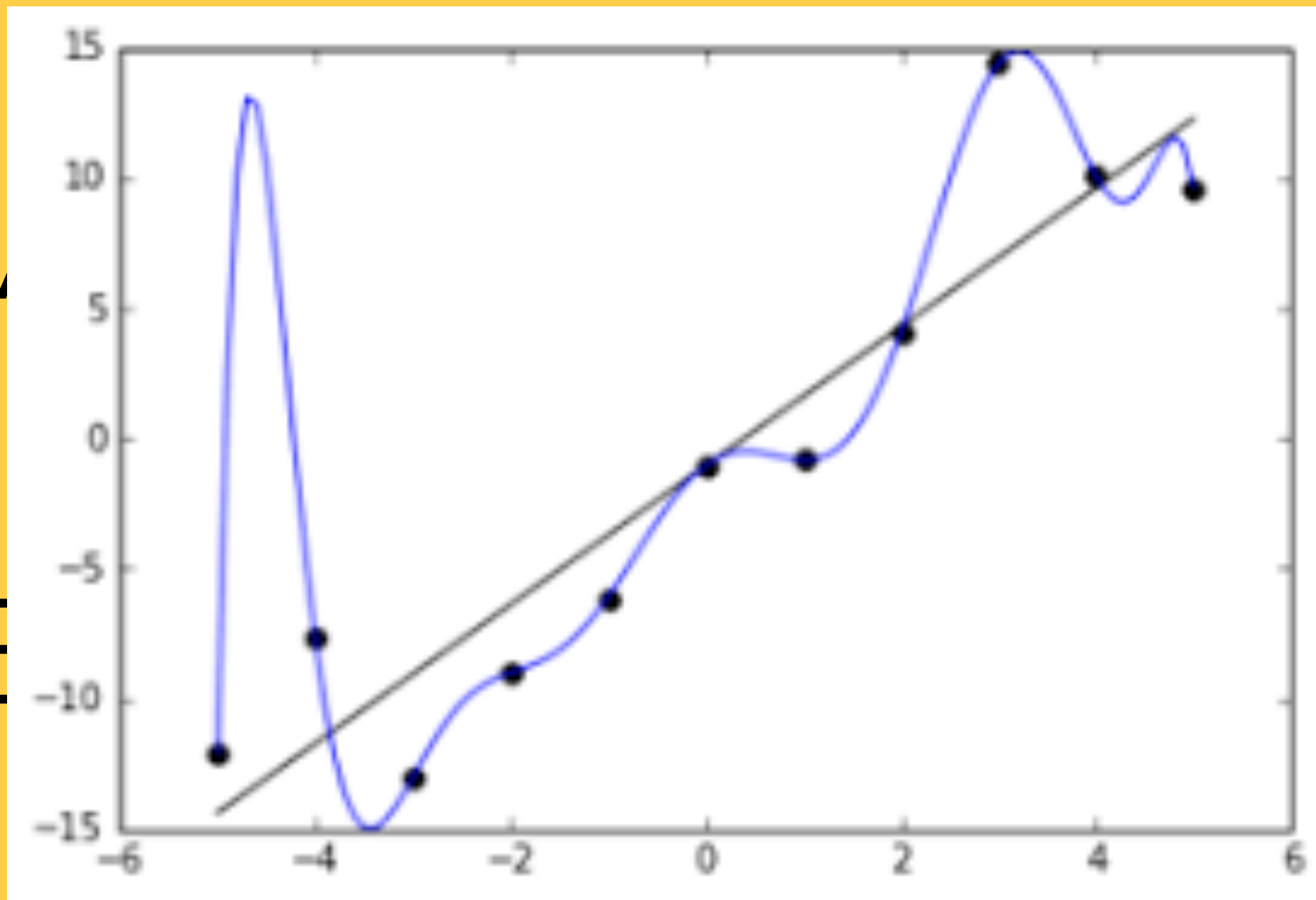


CLAS 12

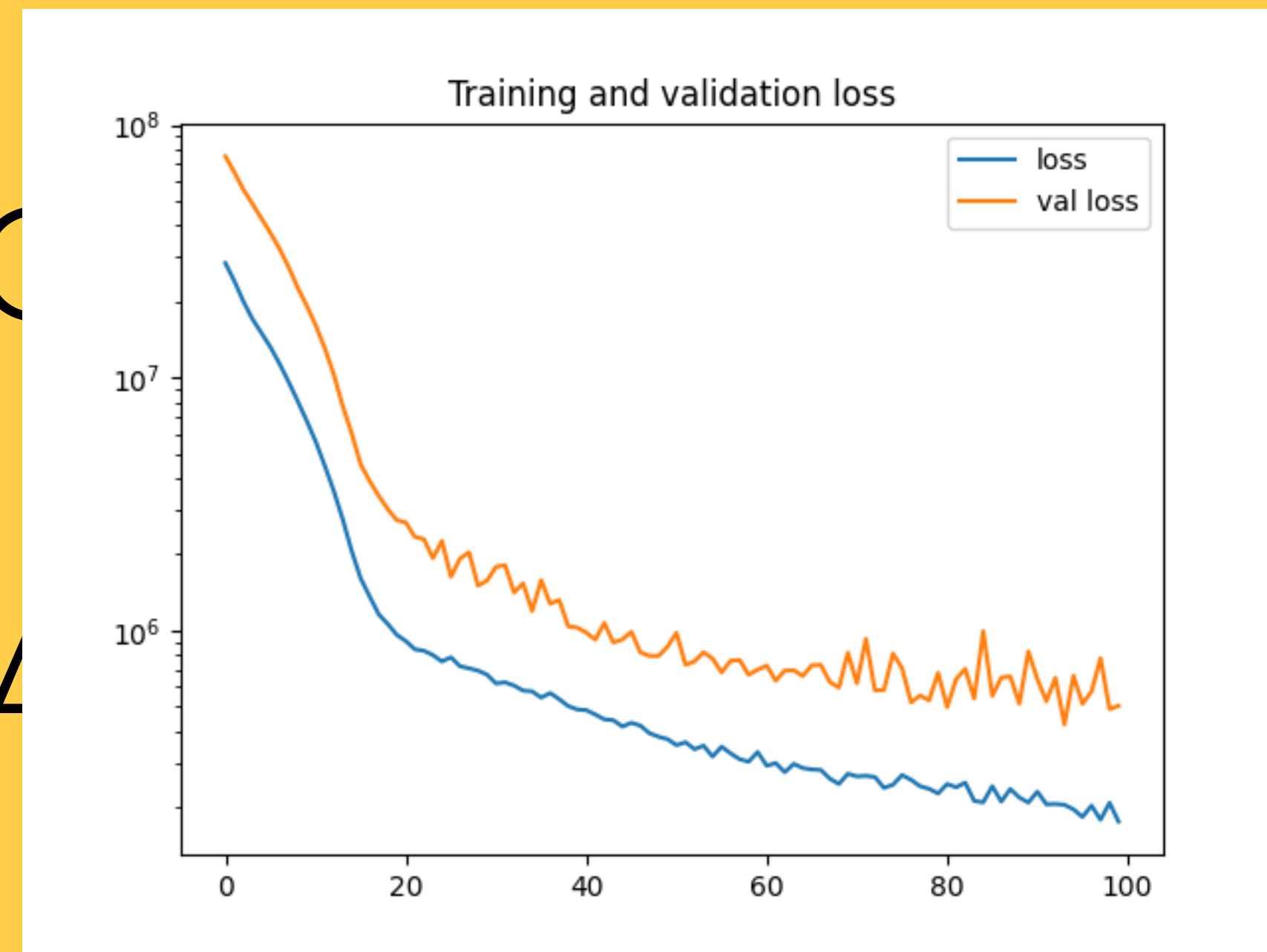


CMS

MA
LE



INC
DA



NEURON

MATHEMATICS



Neural Networks
Volume 4, Issue 2, 1991, Pages 251-257



Approximation capabilities of multilayer feedforward networks

Kurt Hornik

Show more

Share Cite

[https://doi.org/10.1016/0893-6080\(91\)90009-T](https://doi.org/10.1016/0893-6080(91)90009-T)

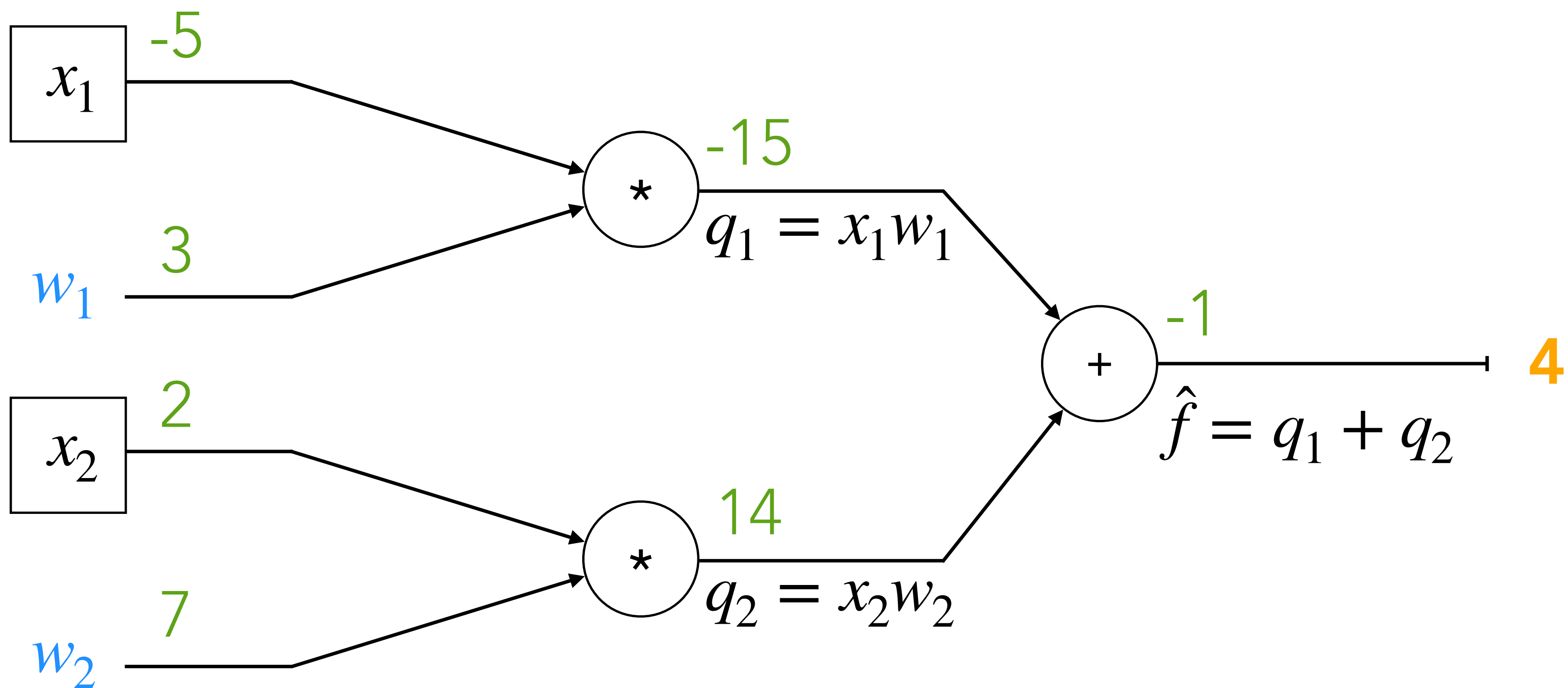
[Get rights and content](#)

Abstract

We show that standard multilayer feedforward networks with as few as a single hidden layer and arbitrary bounded and nonconstant activation function are universal approximators with respect to $L^p(\mu)$ performance criteria, for arbitrary finite input environment measures μ , provided only that sufficiently many hidden units are available. If the activation function is continuous, bounded and nonconstant, then continuous mappings can be learned uniformly over compact input sets. We also give very general conditions ensuring that networks with sufficiently smooth activation functions are capable of arbitrarily accurate approximation to a function and its derivatives.

MATHEMATICS

COMPUTATIONAL GRAPH

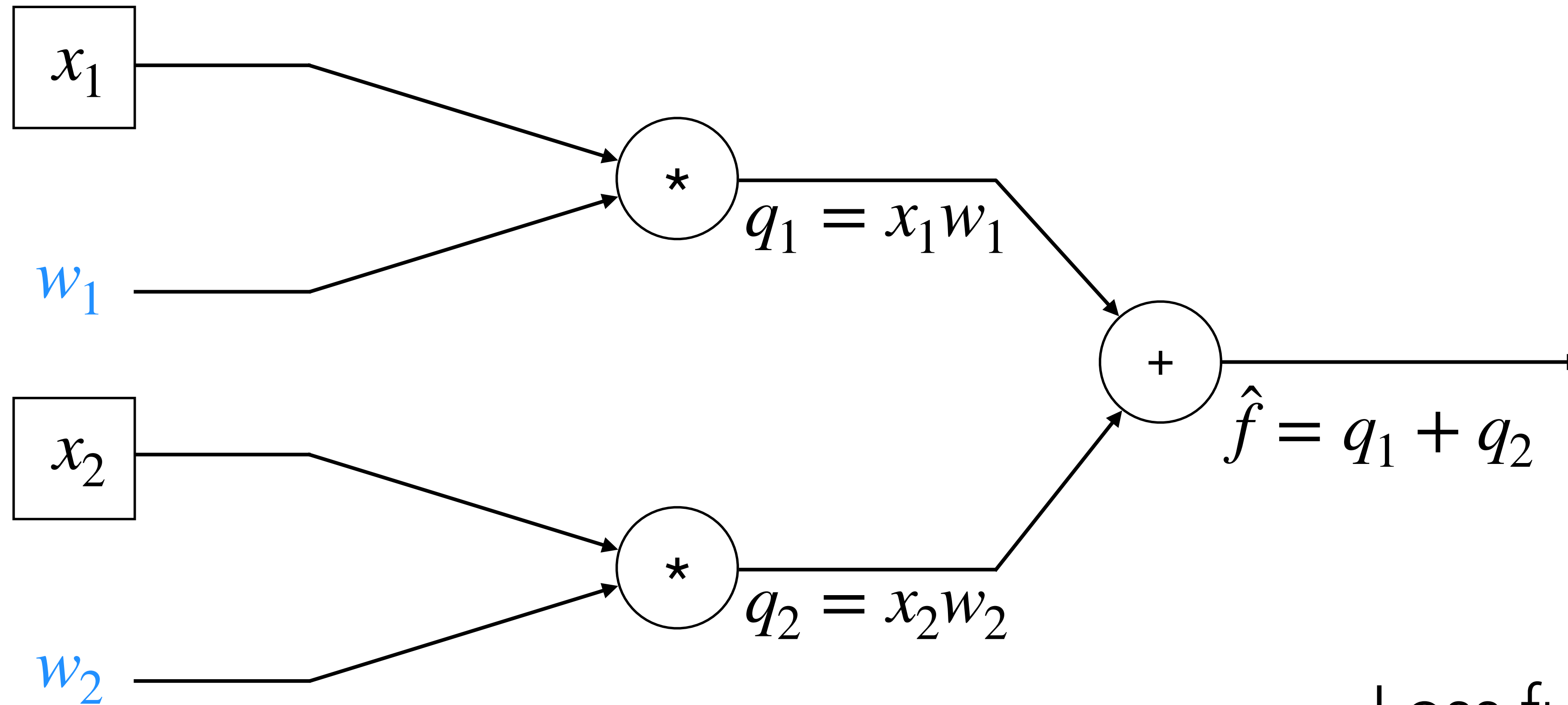


$$\hat{f} = x_1 w_1 + x_2 w_2$$

MACHINE LEARNING

SUPERVISED LEARNING

REGRESSION

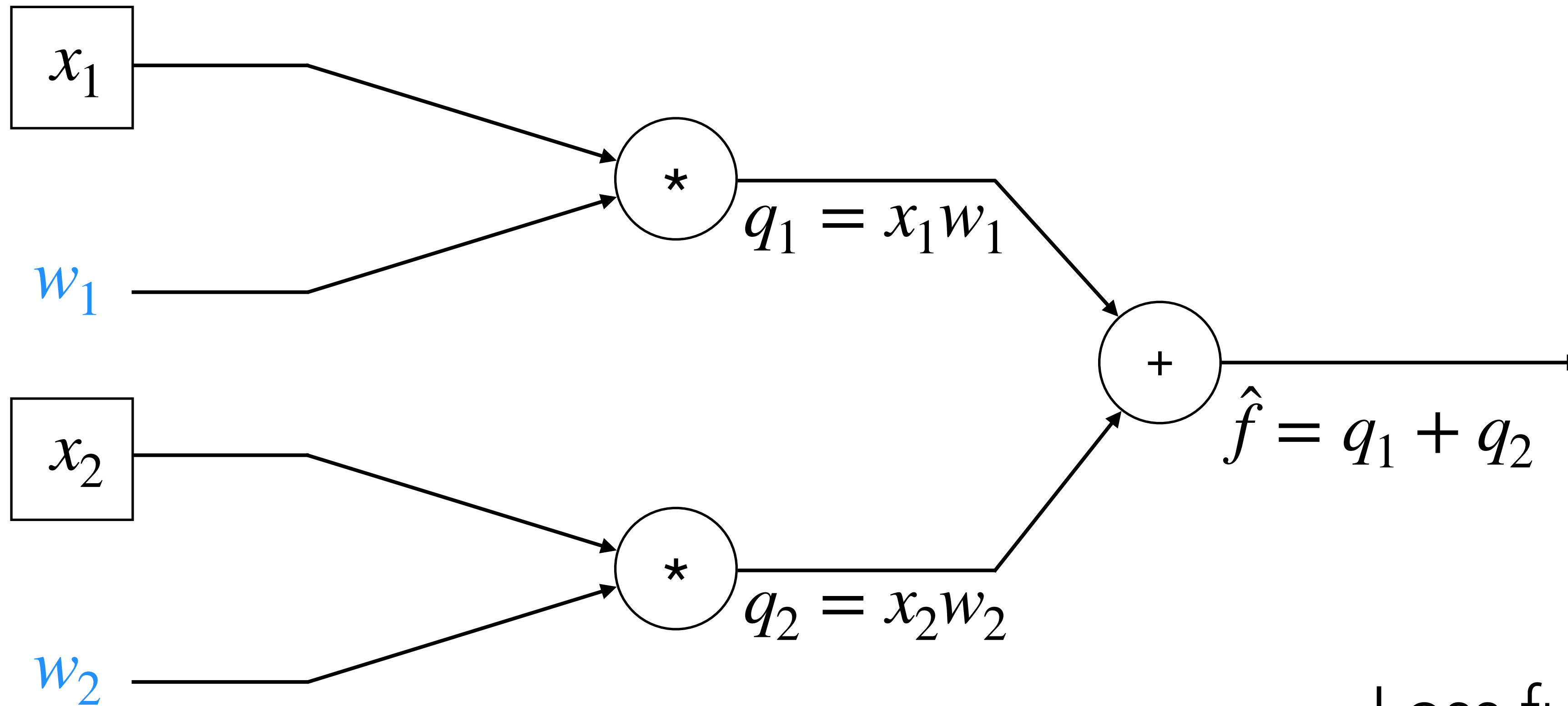


$$\hat{f} = x_1 w_1 + x_2 w_2$$

Loss function

$$J(w) = \hat{f} - f$$

SUPERVISED LEARNING



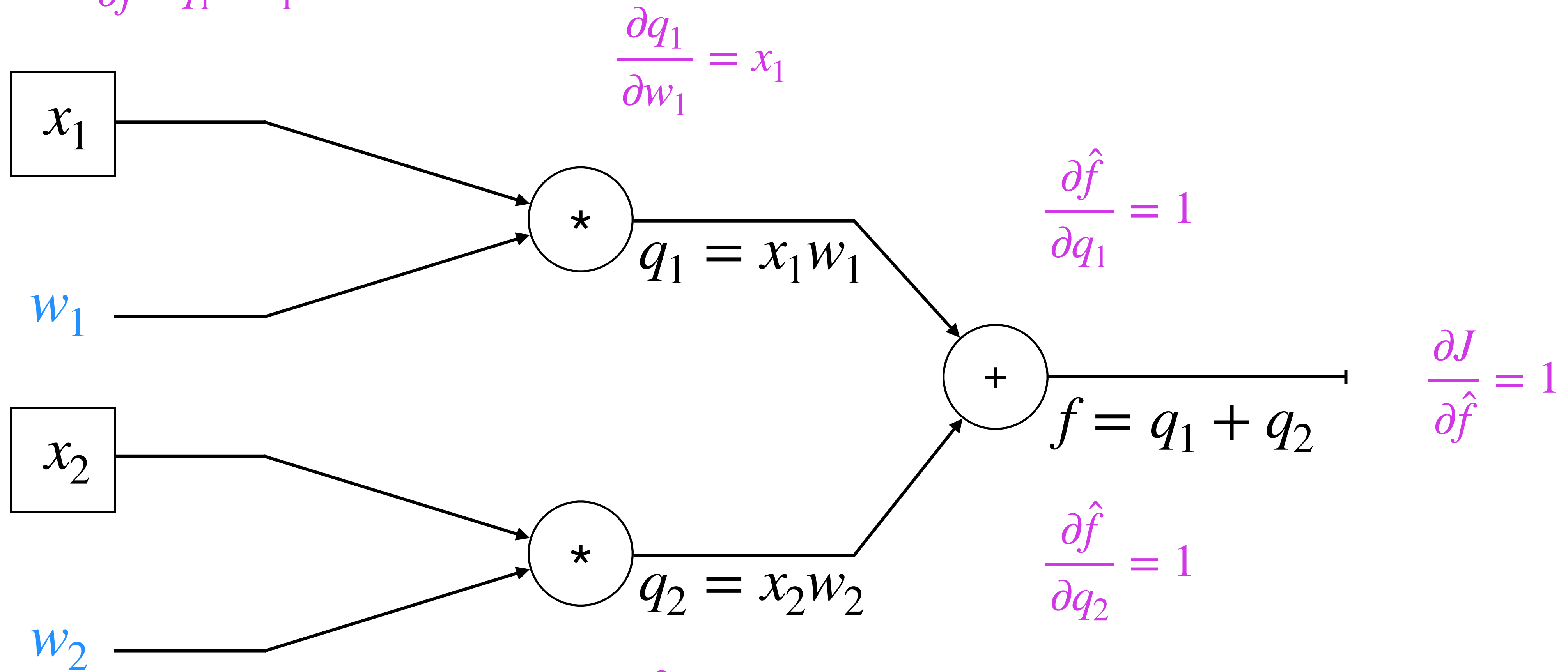
Loss function

$$\hat{f} = x_1 w_1 + x_2 w_2$$

$$J(w) = \hat{f} - f$$

BACKPROPAGATION

$$w_1 = w_1 + \eta * \frac{\partial J}{\partial \hat{f}} \frac{\partial \hat{f}}{\partial q_1} \frac{\partial q_1}{\partial w_1}$$

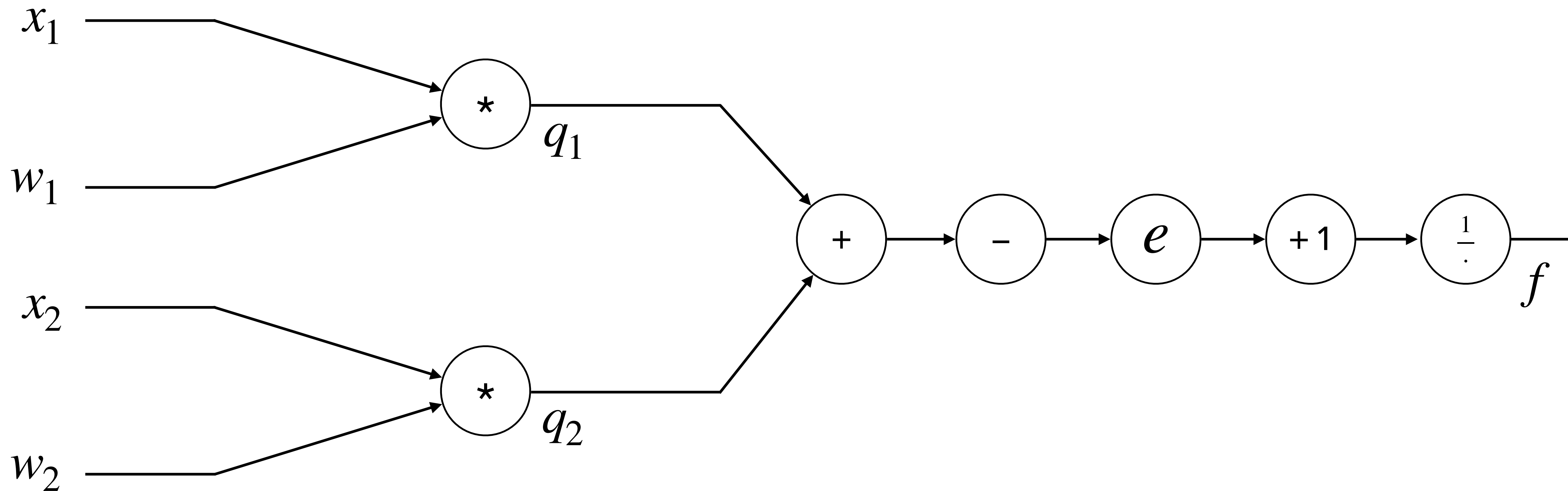


$$w_2 = w_2 + \eta * \frac{\partial J}{\partial \hat{f}} \frac{\partial \hat{f}}{\partial q_2} \frac{\partial q_2}{\partial w_2}$$

Loss function

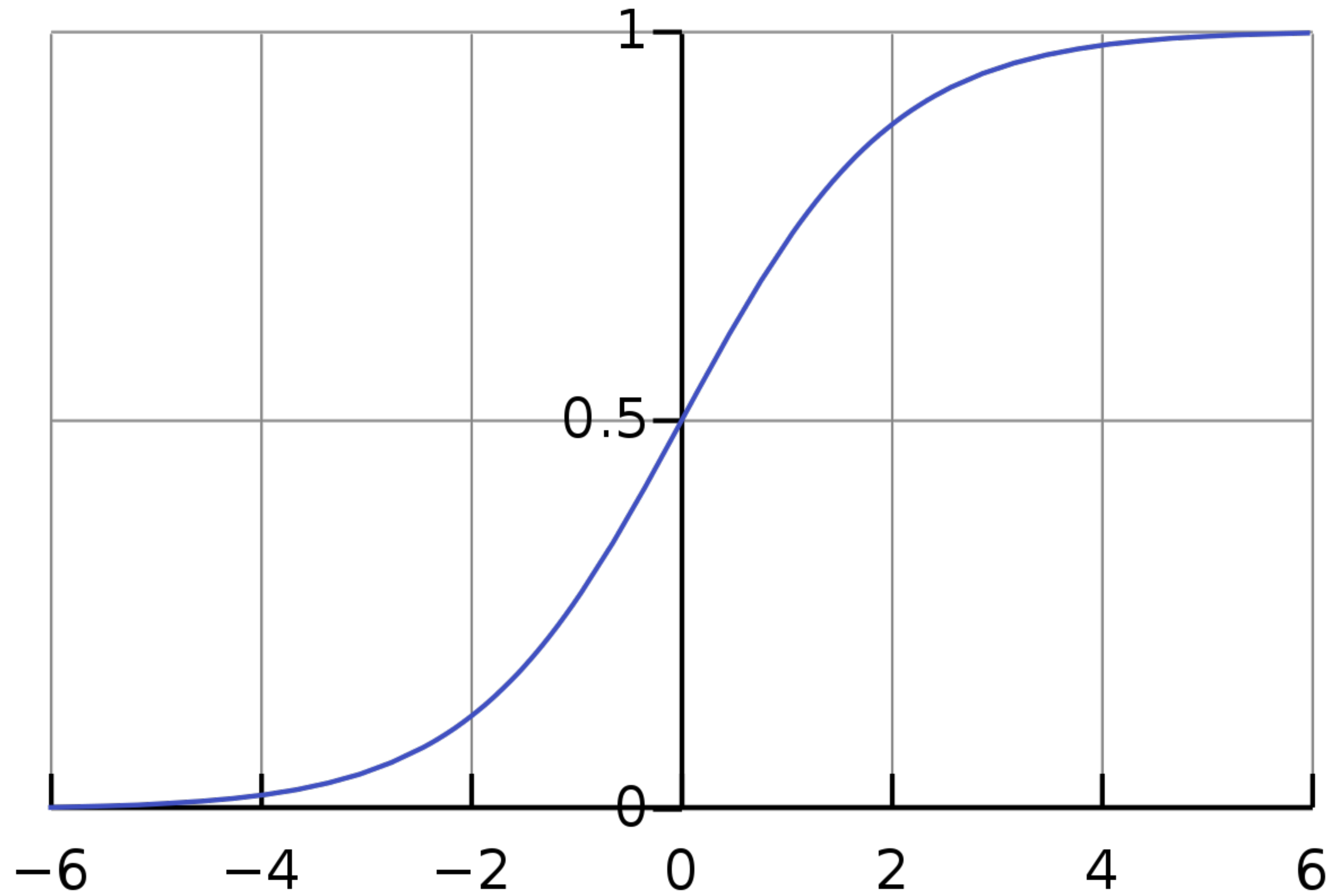
$$J(w) = \hat{f} - f$$

LOGISTIC REGRESSION

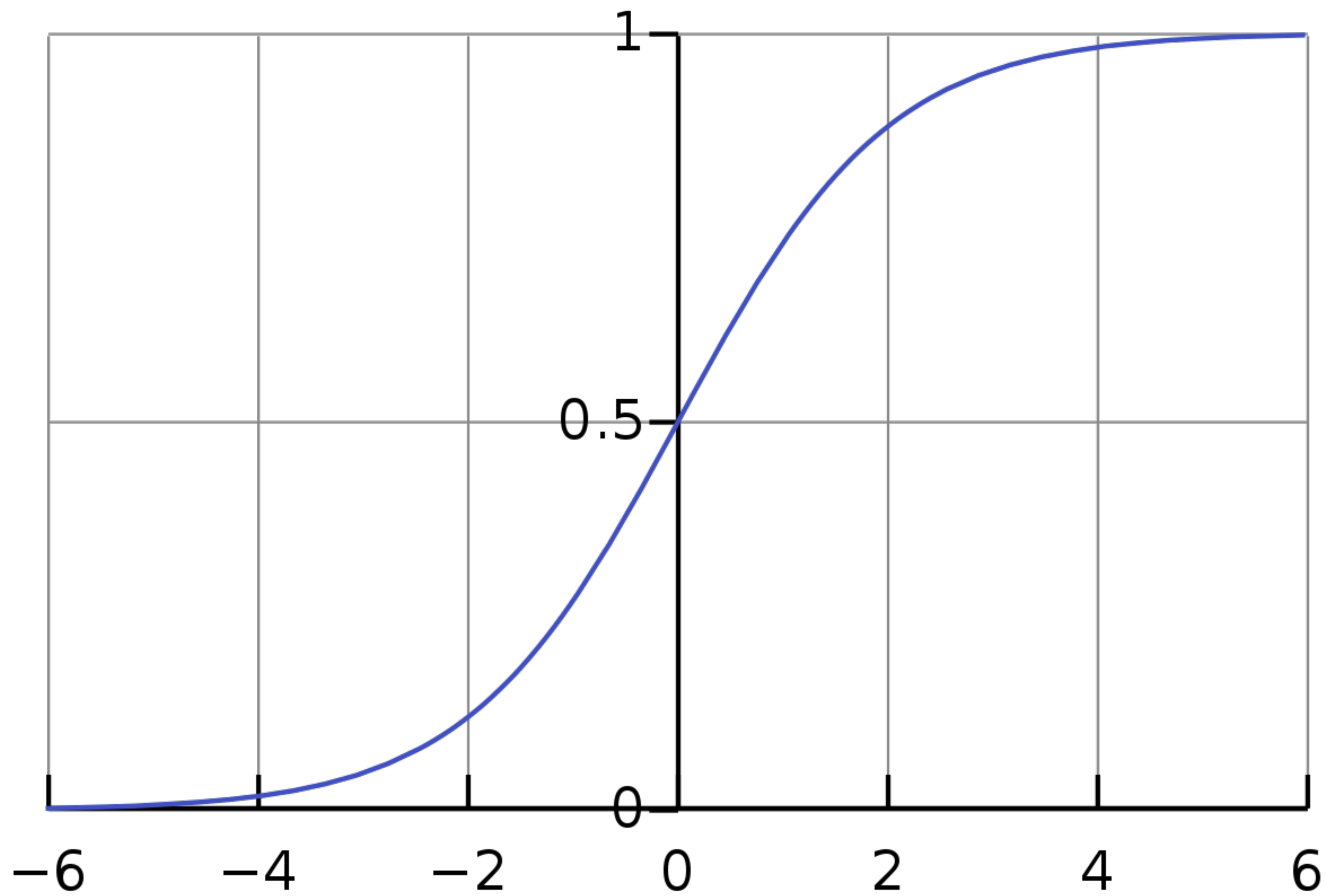


$$f = \frac{1}{1 + e^{-(x_1 w_1 + x_2 w_2)}}$$

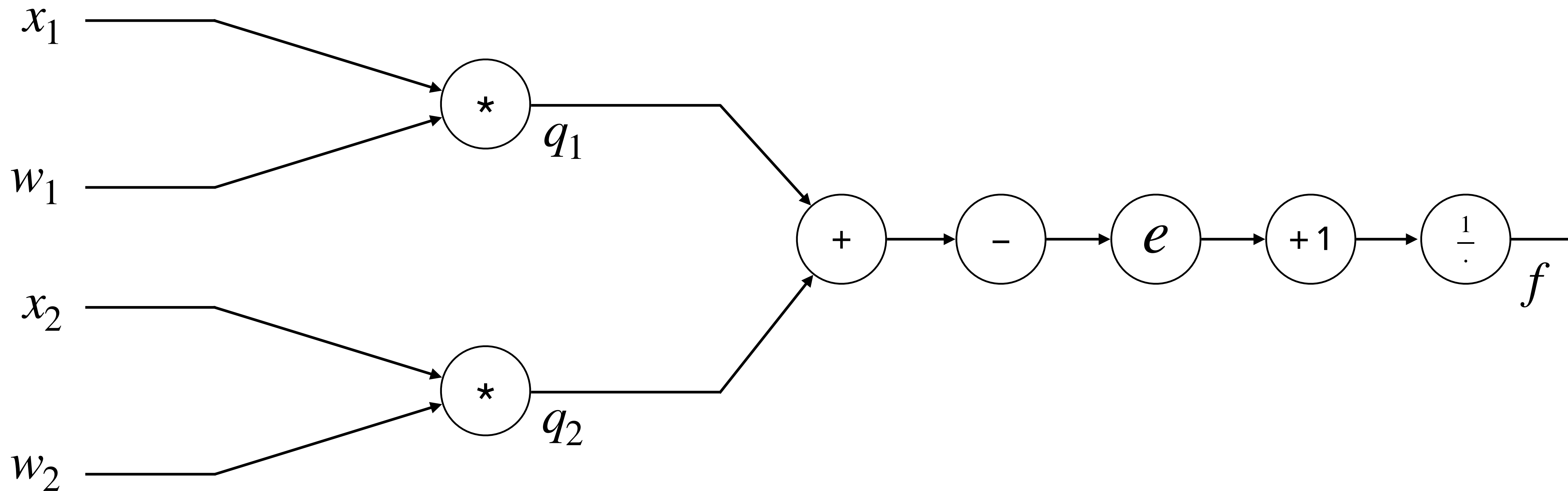
LOGISTIC REGRESSION



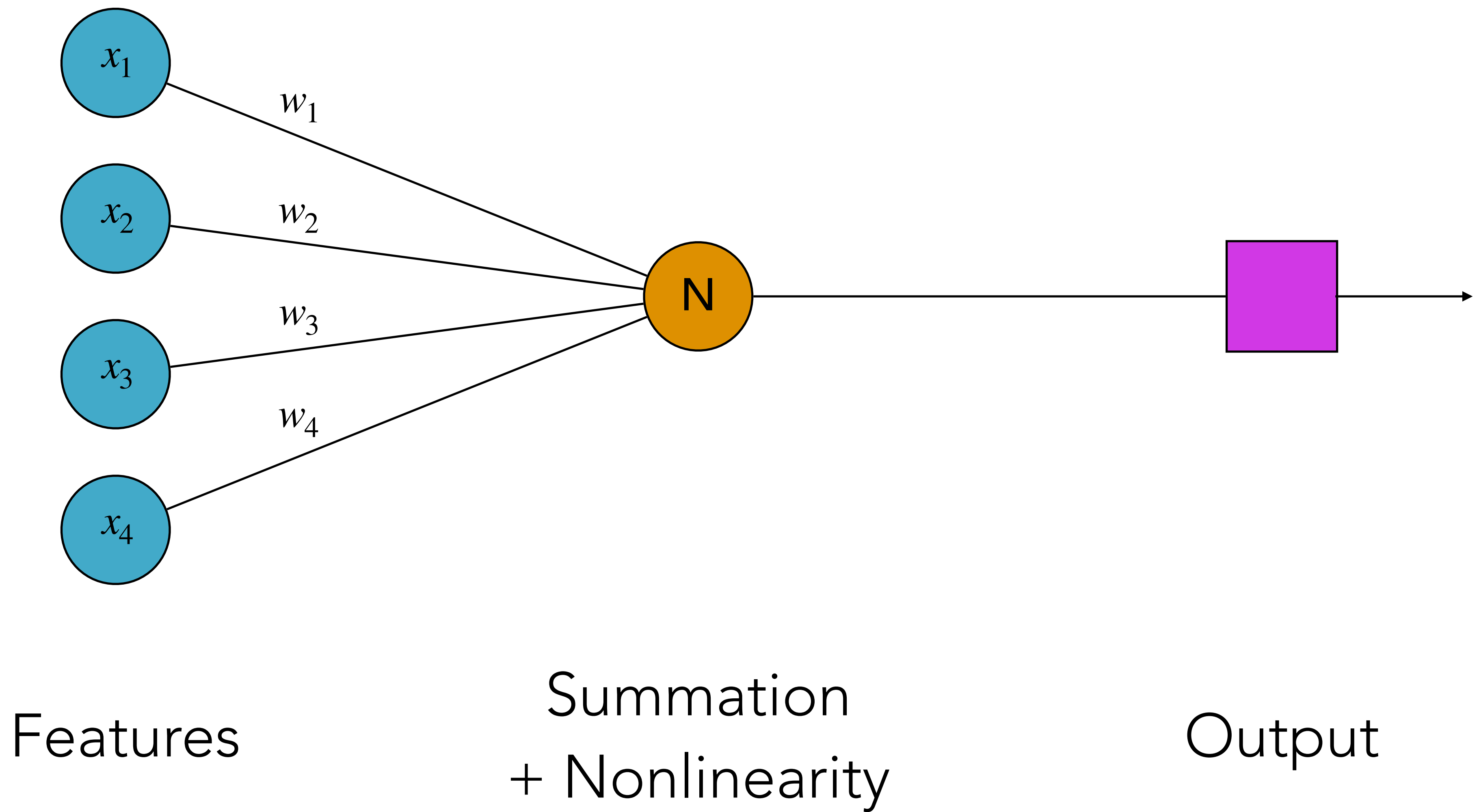
BINARY CLASSIFICATION

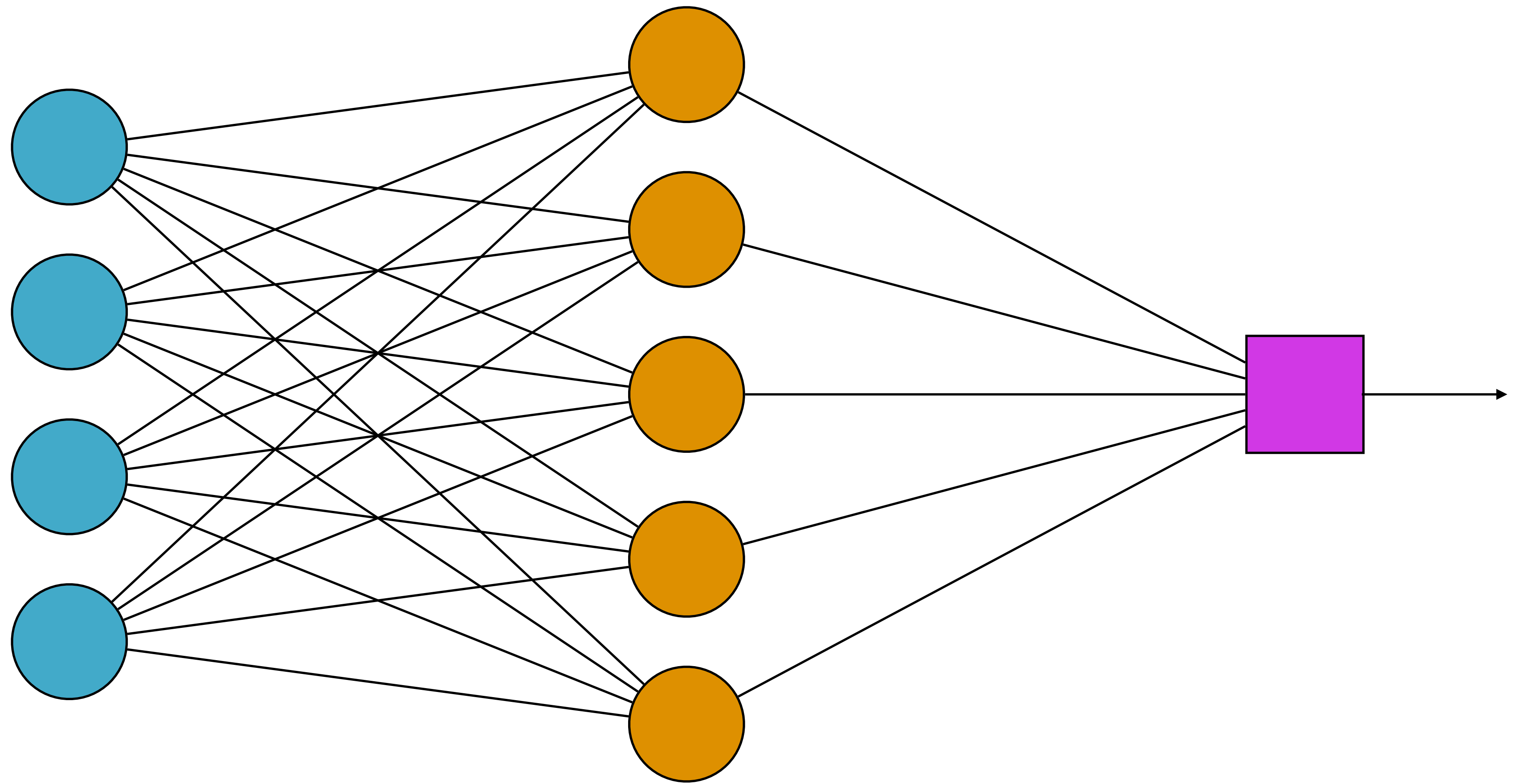


LOGISTIC REGRESSION



$$f = \frac{1}{1 + e^{-(x_1 w_1 + x_2 w_2)}}$$





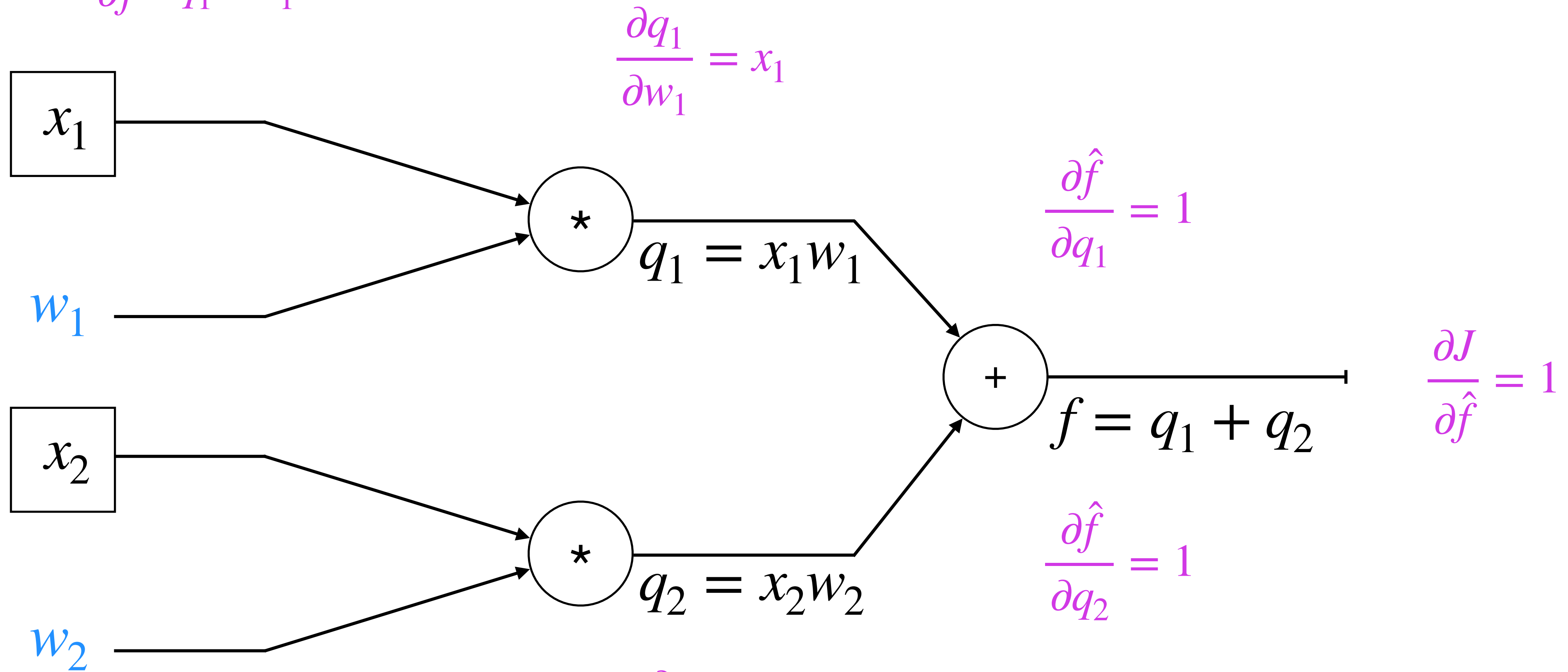
Features

Hidden Layer

Output

BACKPROPAGATION

$$w_1 = w_1 + \eta * \frac{\partial J}{\partial \hat{f}} \frac{\partial \hat{f}}{\partial q_1} \frac{\partial q_1}{\partial w_1}$$



$$w_2 = w_2 + \eta * \frac{\partial J}{\partial \hat{f}} \frac{\partial \hat{f}}{\partial q_2} \frac{\partial q_2}{\partial w_2}$$

Loss function

$$J(w) = \hat{f} - f$$

AUTOMATIC DIFFERENTIATION



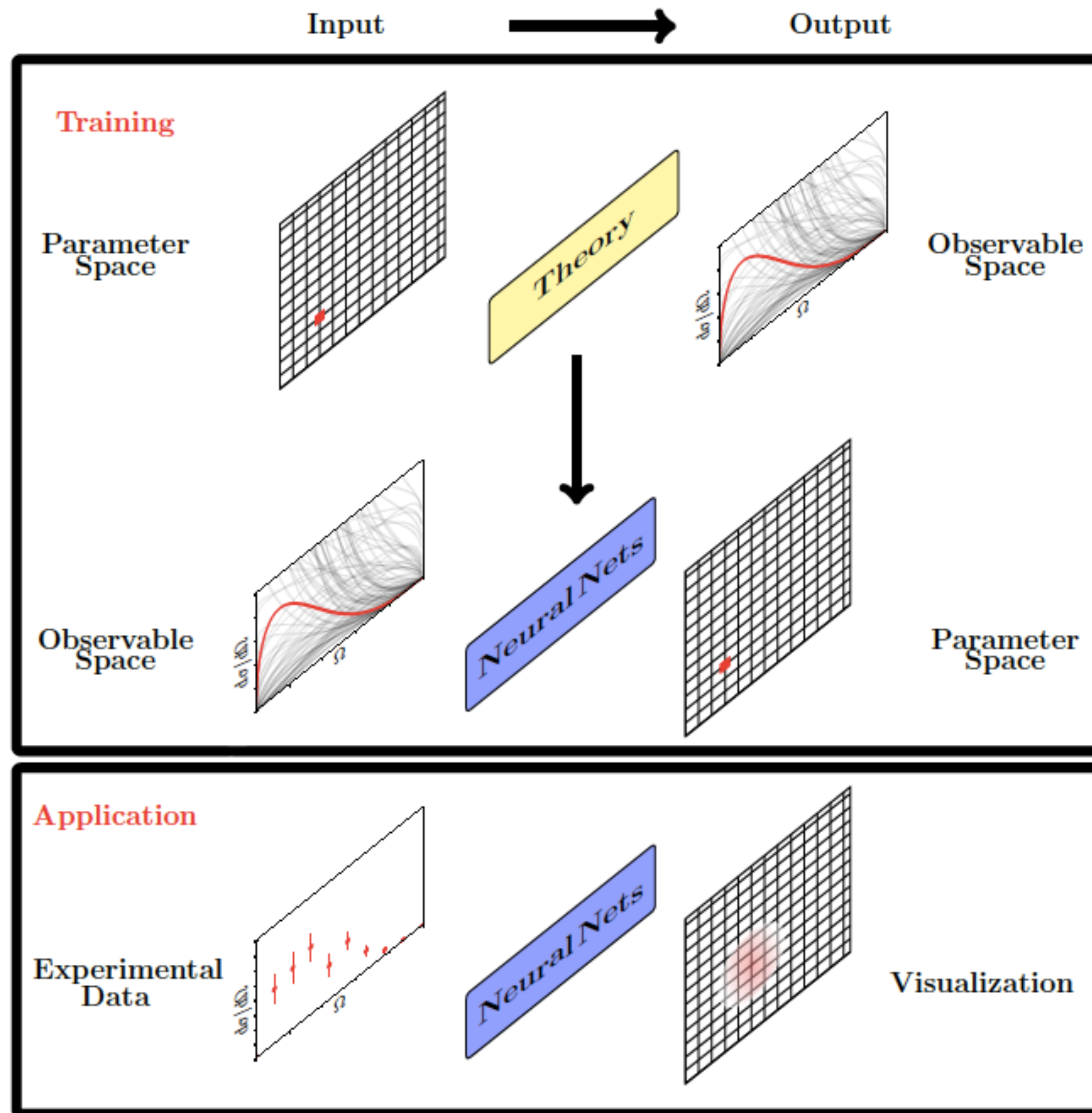
TensorFlow



PyTorch

Application 1: How can experimental observables constrain theoretical models?

THEORY \Leftrightarrow EXPERIMENT

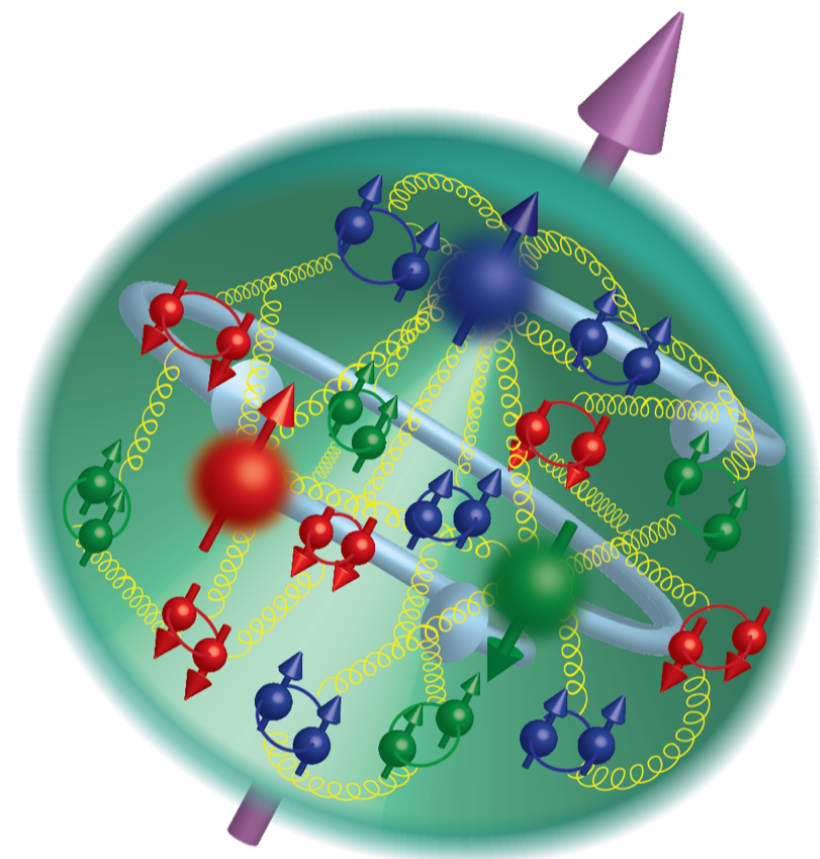
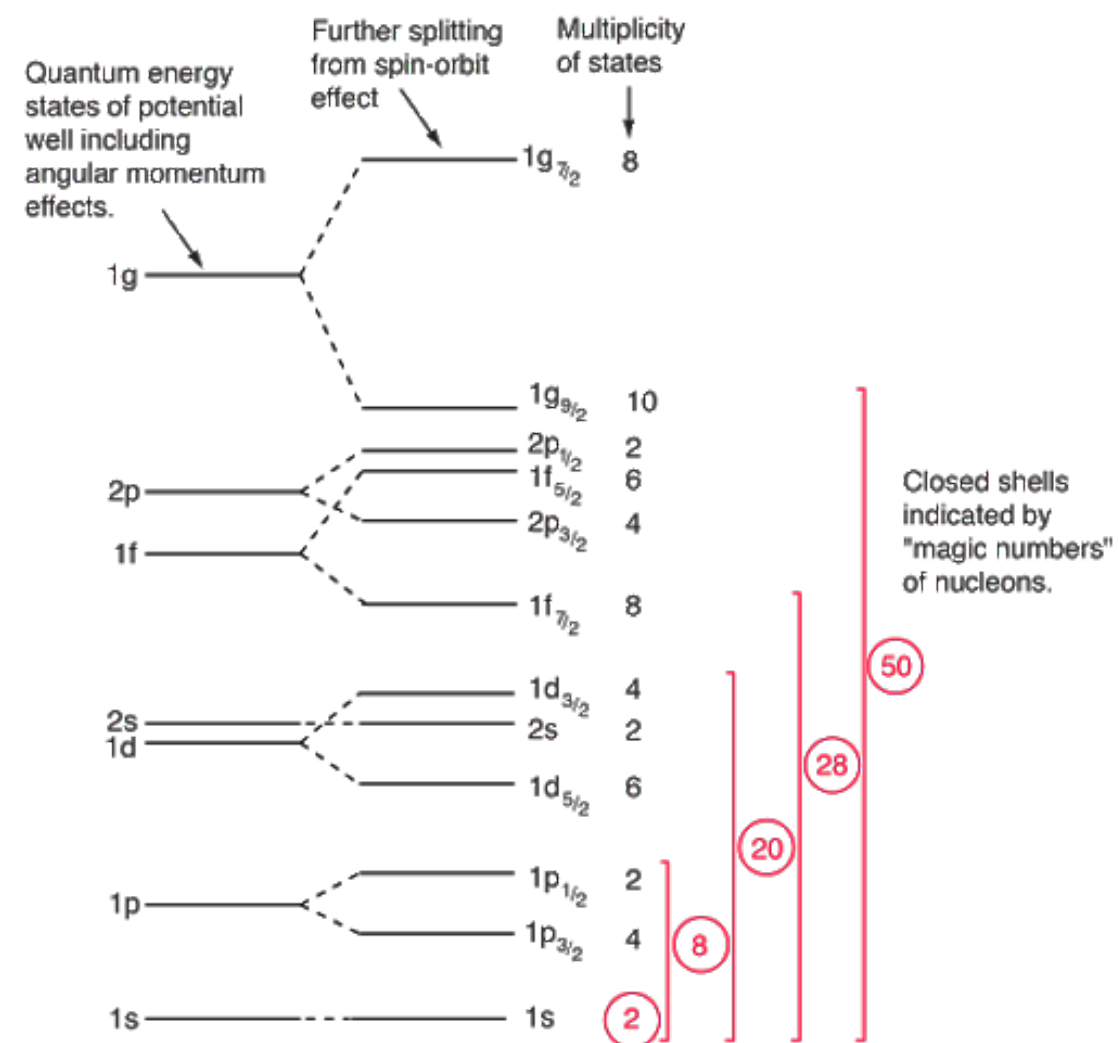
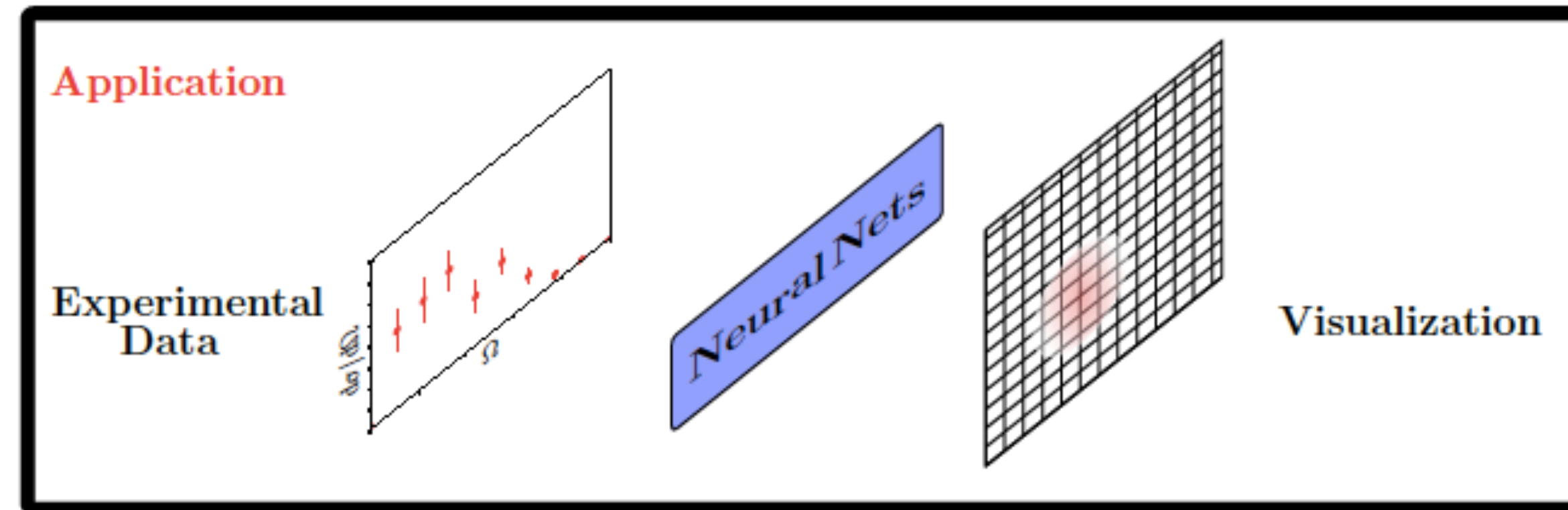
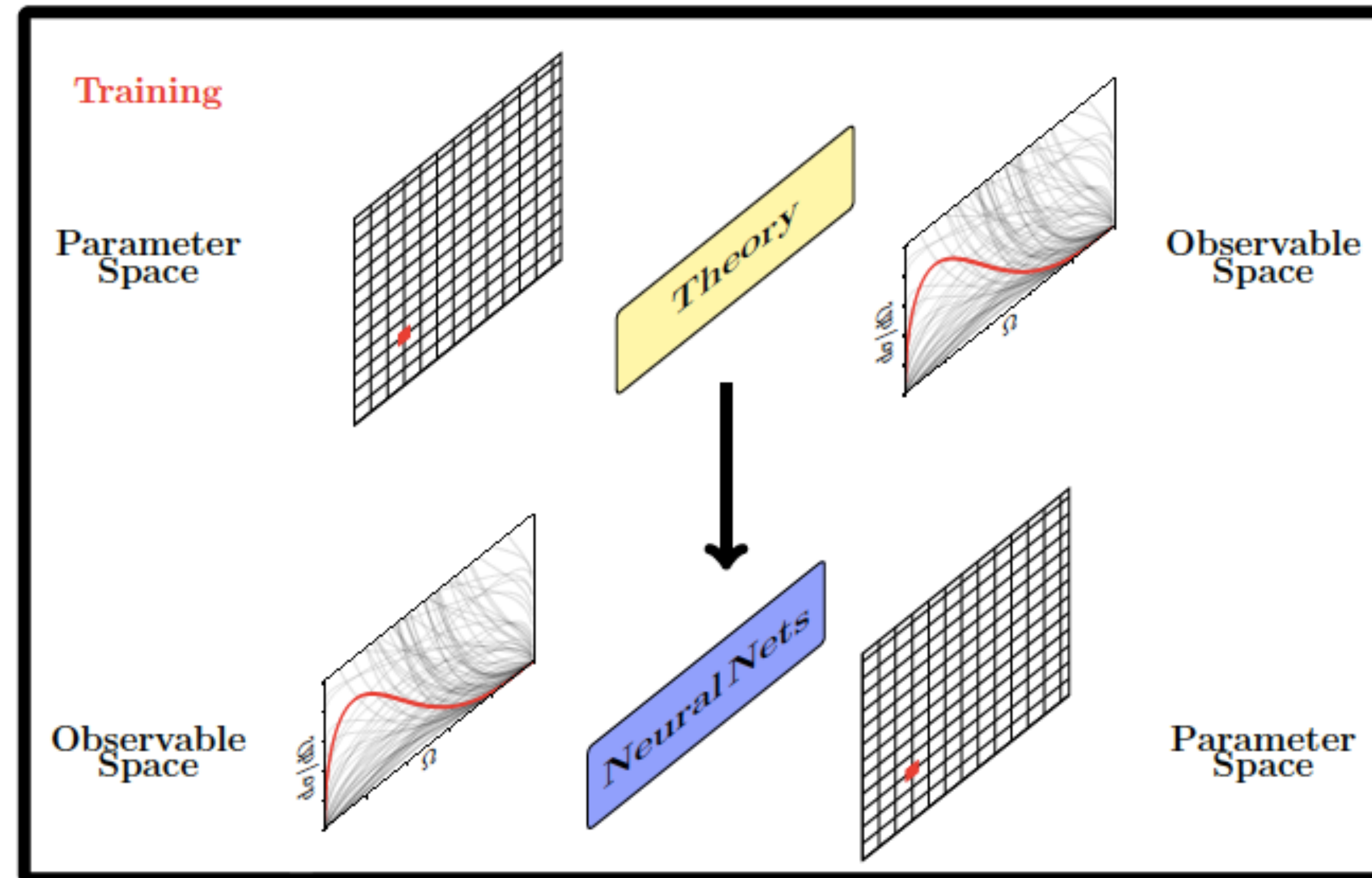


THEORY \rightleftharpoons EXPERIMENT

Input



Output

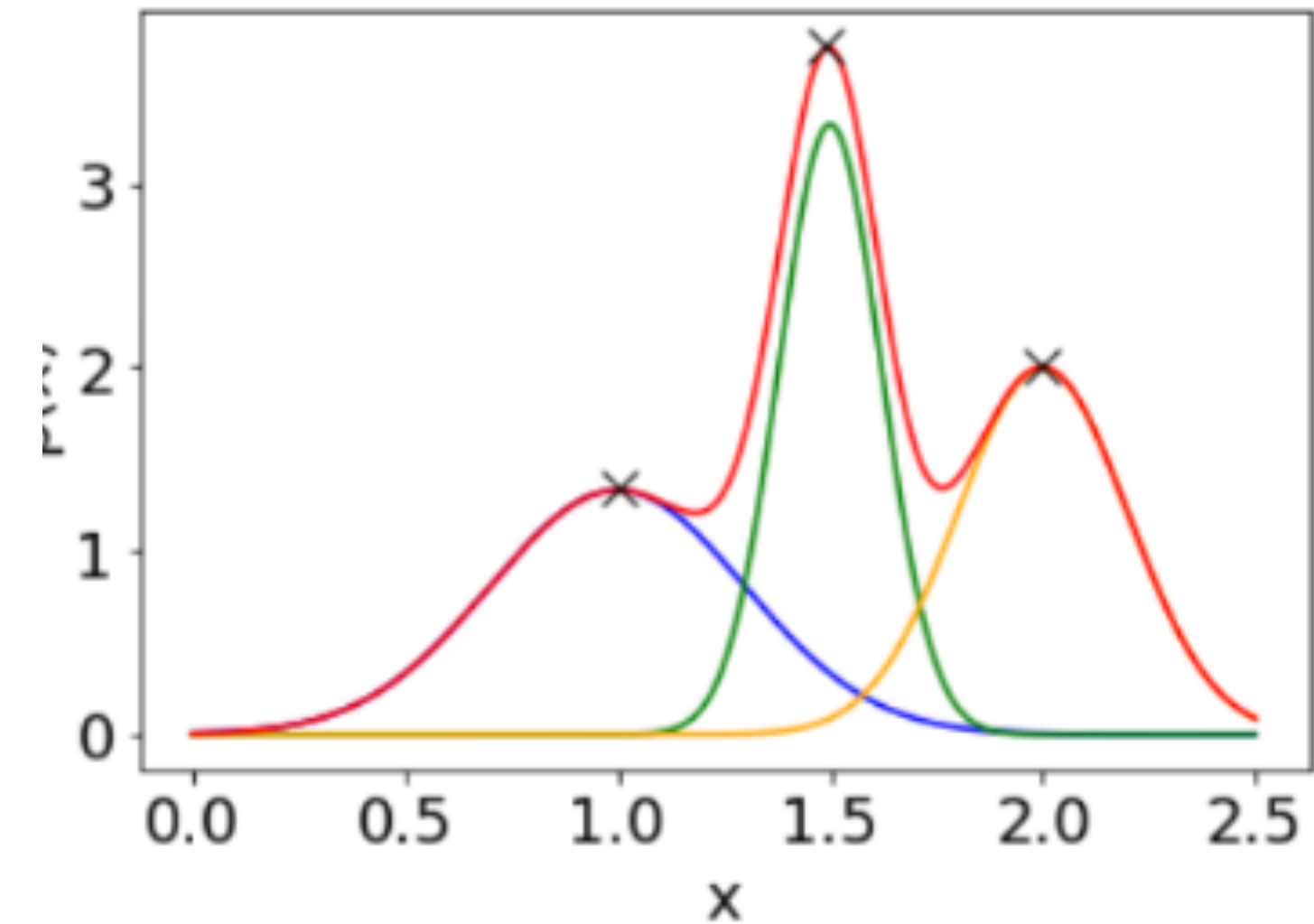
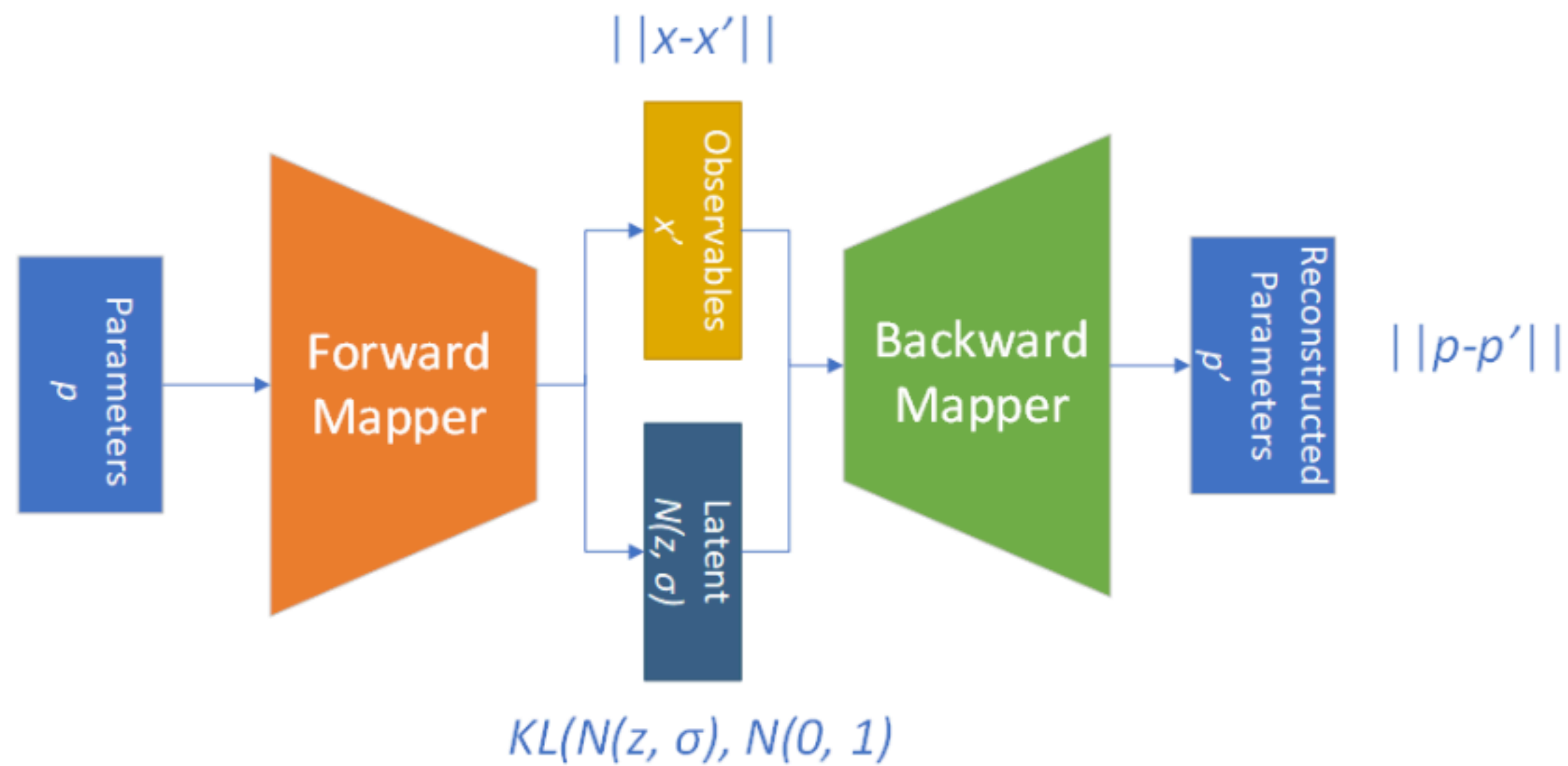


mass \rightarrow	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge \rightarrow	$2/3$	$2/3$	$2/3$	0	0
spin \rightarrow	$1/2$	$1/2$	$1/2$	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS	d down	s strange	b bottom	γ photon	
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$1/2$	$1/2$	$1/2$	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$1/2$	$1/2$	$1/2$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
					GAUGE BOSONS

$\begin{pmatrix} u \\ d \\ u \\ d \end{pmatrix}_L$	$\begin{pmatrix} c \\ s \\ c \\ s \end{pmatrix}_L$	$\begin{pmatrix} t \\ b \\ t \\ b \end{pmatrix}_L$	g	$\begin{pmatrix} \tilde{u} \\ \tilde{d} \\ \tilde{u} \\ \tilde{d} \end{pmatrix}_L$	$\begin{pmatrix} \tilde{c} \\ \tilde{s} \\ \tilde{c} \\ \tilde{s} \end{pmatrix}_L$	$\begin{pmatrix} \tilde{t} \\ \tilde{b} \\ \tilde{t} \\ \tilde{b} \end{pmatrix}_L$	g
$\begin{pmatrix} u \\ d \\ u \\ d \end{pmatrix}_R$	$\begin{pmatrix} c \\ s \\ c \\ s \end{pmatrix}_R$	$\begin{pmatrix} t \\ b \\ t \\ b \end{pmatrix}_R$	γ	$\begin{pmatrix} \tilde{u} \\ \tilde{d} \\ \tilde{u} \\ \tilde{d} \end{pmatrix}_R$	$\begin{pmatrix} \tilde{c} \\ \tilde{s} \\ \tilde{c} \\ \tilde{s} \end{pmatrix}_R$	$\begin{pmatrix} \tilde{t} \\ \tilde{b} \\ \tilde{t} \\ \tilde{b} \end{pmatrix}_R$	$\tilde{\gamma}$
$\begin{pmatrix} \nu_e \\ e \\ e \end{pmatrix}_L$	$\begin{pmatrix} \nu_\mu \\ \mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} \nu_\tau \\ \tau \\ \tau \end{pmatrix}_L$	Z^0	$\begin{pmatrix} \tilde{\nu}_e \\ \tilde{e} \\ \tilde{e} \end{pmatrix}_L$	$\begin{pmatrix} \tilde{\nu}_\mu \\ \tilde{\mu} \\ \tilde{\mu} \end{pmatrix}_L$	$\begin{pmatrix} \tilde{\nu}_\tau \\ \tilde{\tau} \\ \tilde{\tau} \end{pmatrix}_L$	Z^0
$\begin{pmatrix} \nu_e \\ e \\ e \end{pmatrix}_R$	$\begin{pmatrix} \nu_\mu \\ \mu \\ \mu \end{pmatrix}_R$	$\begin{pmatrix} \nu_\tau \\ \tau \\ \tau \end{pmatrix}_R$	W^\pm	$\begin{pmatrix} \tilde{\nu}_e \\ \tilde{e} \\ \tilde{e} \end{pmatrix}_R$	$\begin{pmatrix} \tilde{\nu}_\mu \\ \tilde{\mu} \\ \tilde{\mu} \end{pmatrix}_R$	$\begin{pmatrix} \tilde{\nu}_\tau \\ \tilde{\tau} \\ \tilde{\tau} \end{pmatrix}_R$	W^\pm
			$s = 1$				$s = 1/2$
			$s = 0$				$s = 0$
			$s = 1/2$				$s = 1/2$

Existing particles SUSY particles (MSSM model)

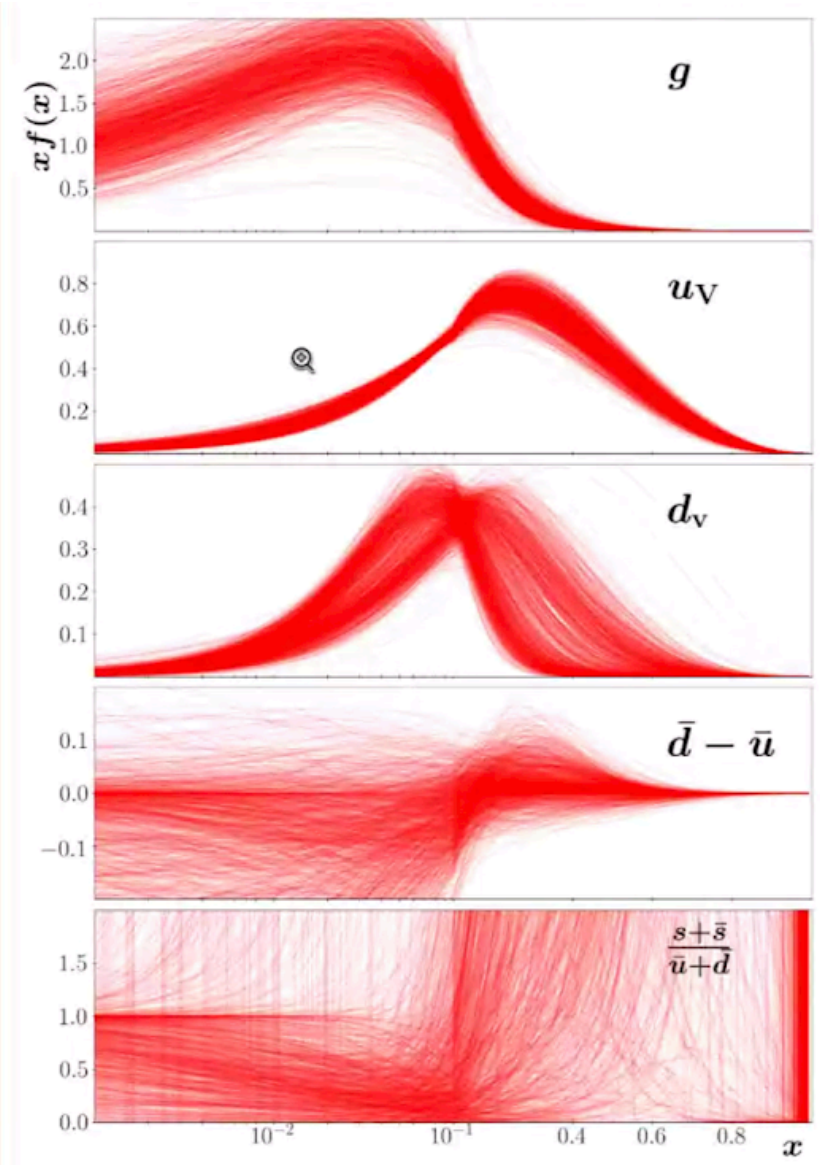
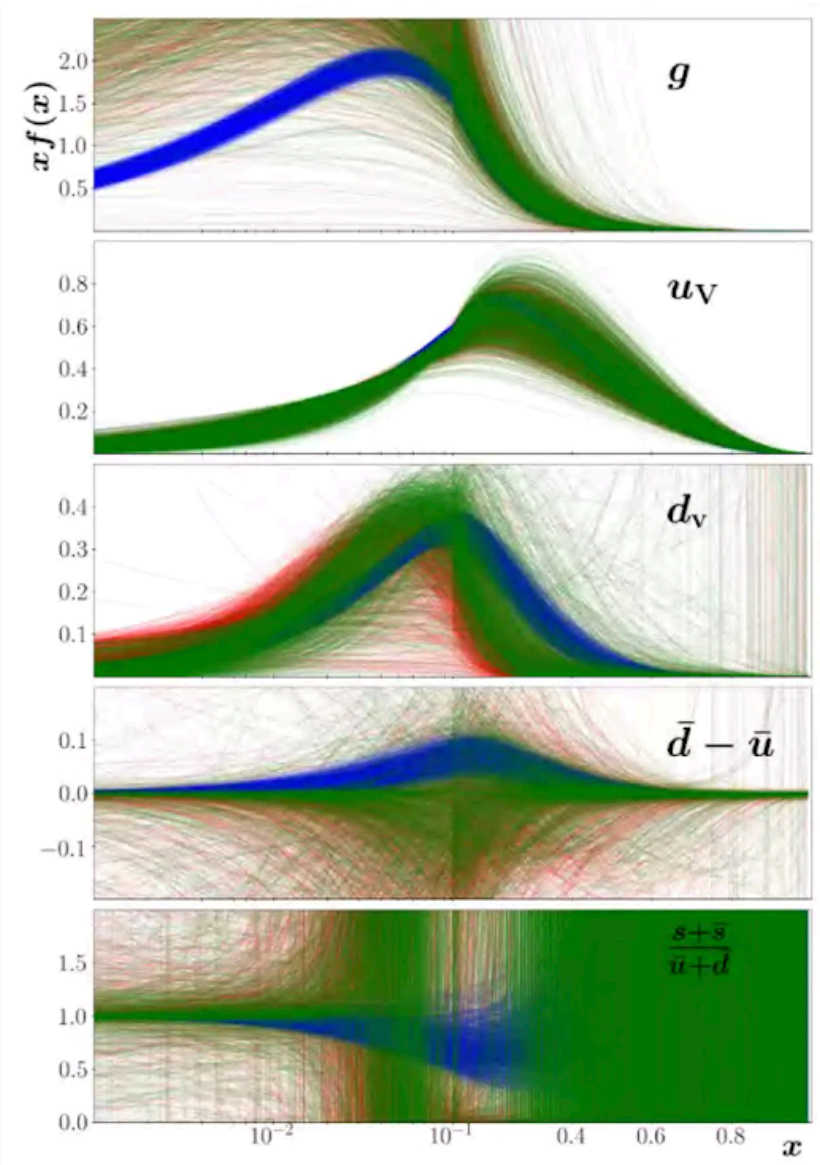
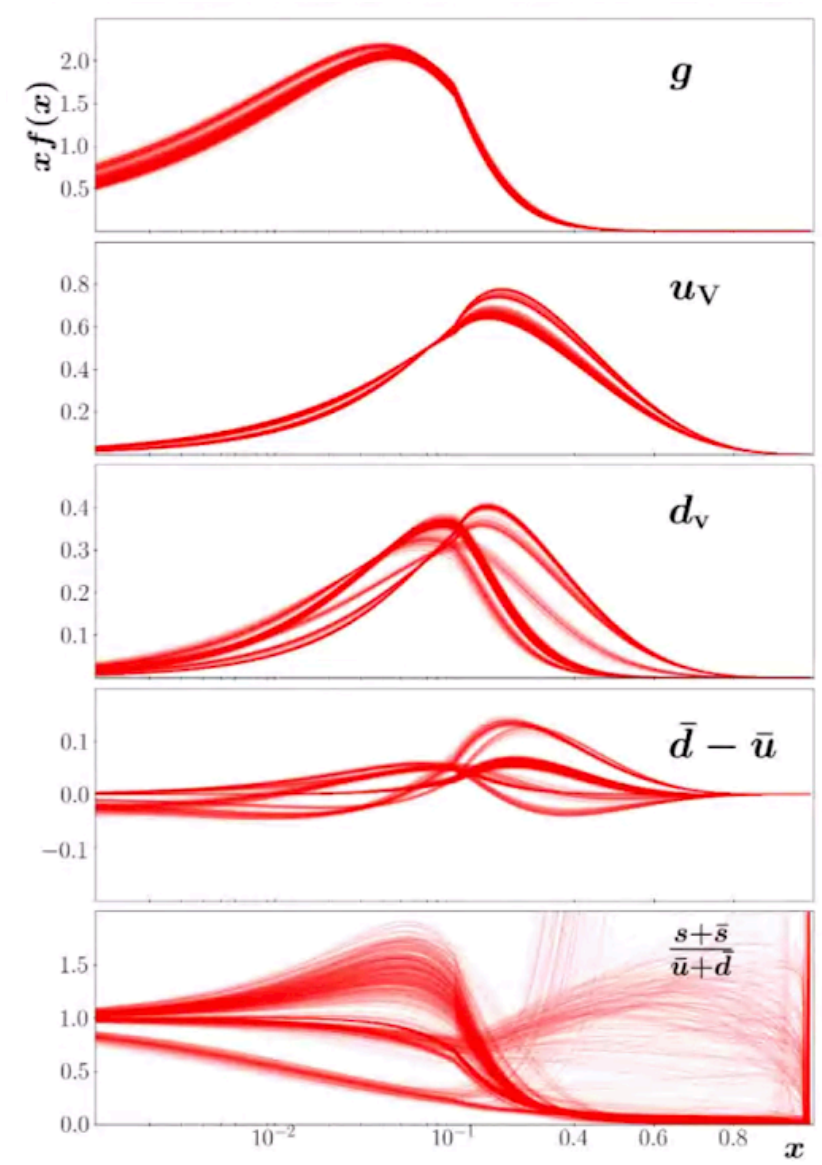
MIXTURE DENSITY NETWORK



Output Layer Interpretation:

$$p(\mathbf{t}|\mathbf{x}) = \sum_{k=1}^K \pi_k(\mathbf{x}) \mathcal{N}(\mathbf{t}|\boldsymbol{\mu}_k(\mathbf{x}), \sigma_k^2(\mathbf{x}))$$

Figure 2: Architecture of the kinematics-independent inverse mapper.



FAST MAPPING TO THEORETICAL PARAMETERS

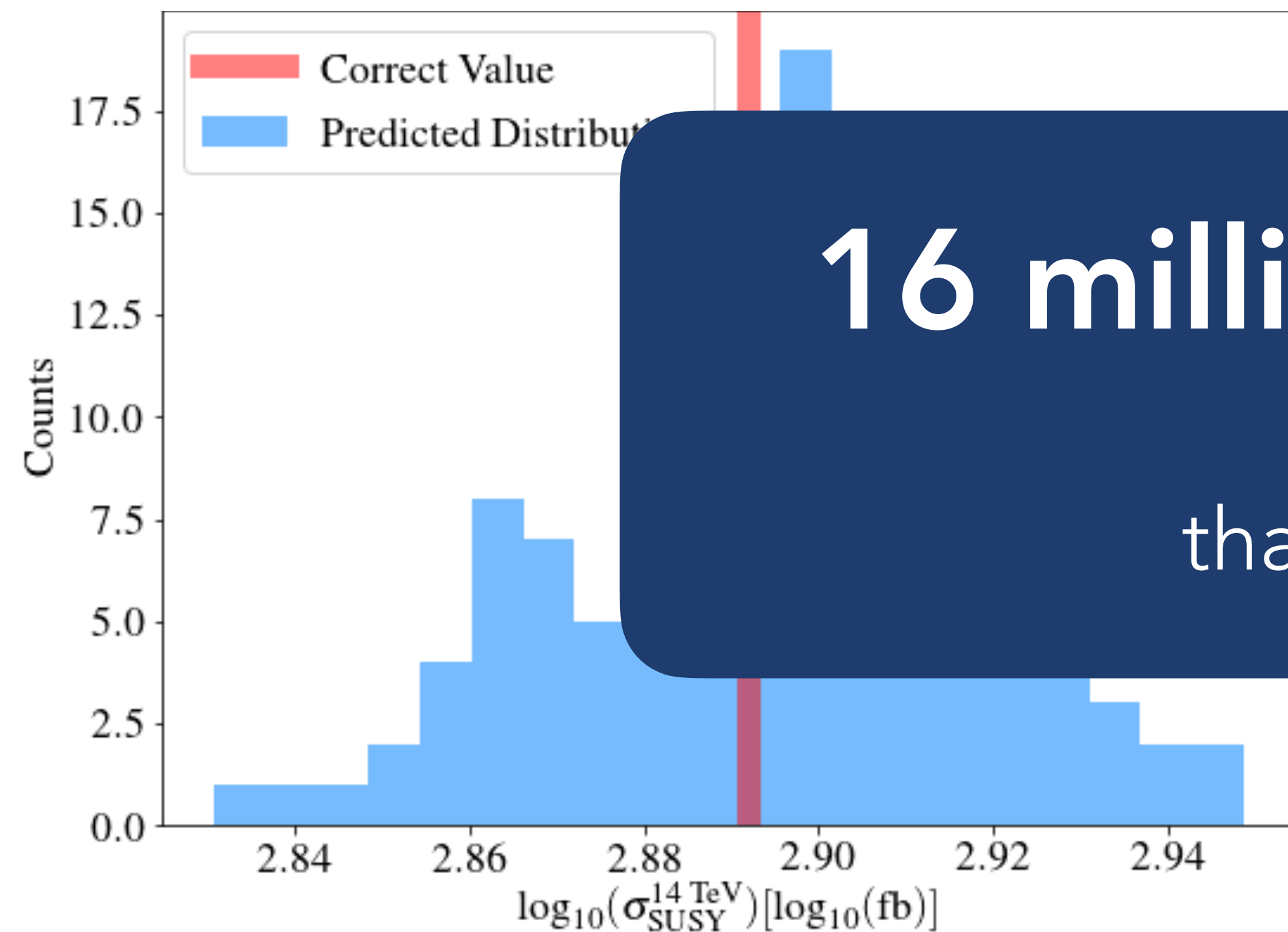
Bayesian Neural Networks

Training — Bayesian inference

Can we make predictions with accurate error estimates?

pMSSM parameters \rightarrow total
SUSY cross section

FAST MAPPING TO THEORETICAL PARAMETERS



16 million times faster

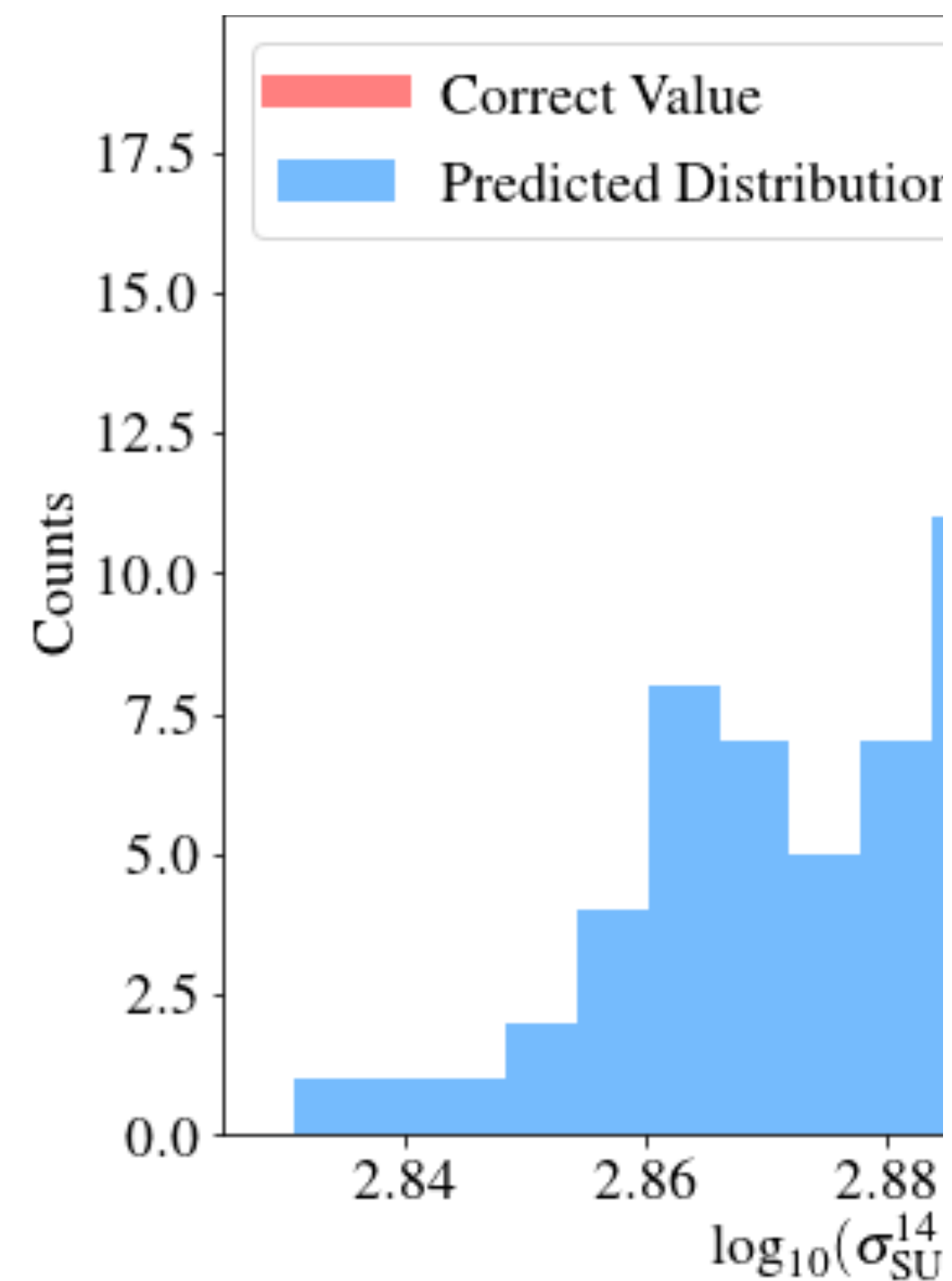
than theory codes!

B.S. Kronheim, M.P. Kuchera, H.B. Prosper, A. Karbo, Bayesian neural networks for fast SUSY predictions, Physics Letters B, Volume 813, 2021, 136041, ISSN 0370-2693, <https://doi.org/10.1016/j.physletb.2020.136041>.

<https://arxiv.org/abs/2009.14393>

<https://alpha-davidson.github.io/TensorBNN>

FAST MAPPING TO THEORETICAL PARAMETERS



B.S. Kronheim, M.P. Kuchera, H.B. Prosper, predictions, Physics Letters B, Volume 813 10.1016/j.physletb.2020.136041.

<https://arxiv.org/abs/2009.14393>

<https://alpha-davidson.github.io/TensorBNN>



Bayesian neural networks for fast SUSY predictions

B.S. Kronheim^{a,*}, M.P. Kuchera^a, H.B. Prosper^b, A. Karbo^a

^a Department of Physics, Davidson College, Davidson, NC 28035, USA

^b Department of Physics, Florida State University, Tallahassee, FL 32306, USA



TensorBNN: Bayesian inference for neural networks using TensorFlow[☆]

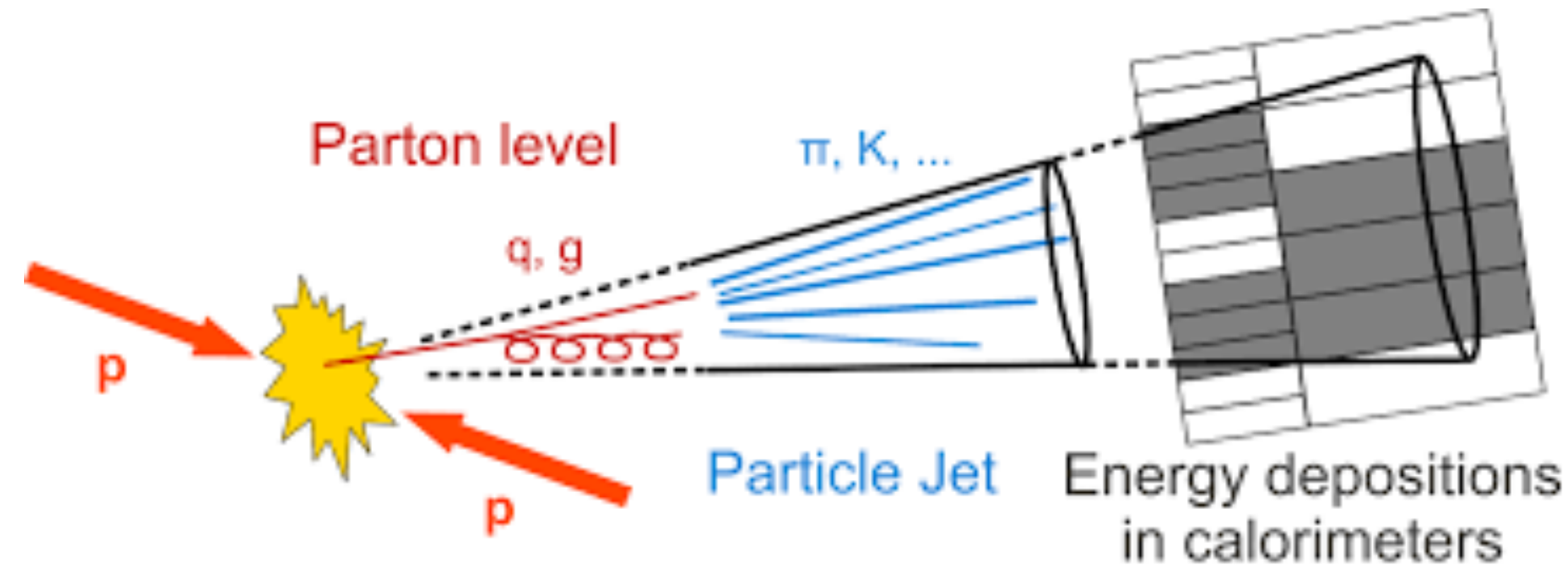
B.S. Kronheim^{a,*}, M.P. Kuchera^a, H.B. Prosper^b

^a Department of Physics, Davidson College, Davidson, NC 28036, United States of America

^b Department of Physics, Florida State University, Tallahassee, FL 32306, United States of America

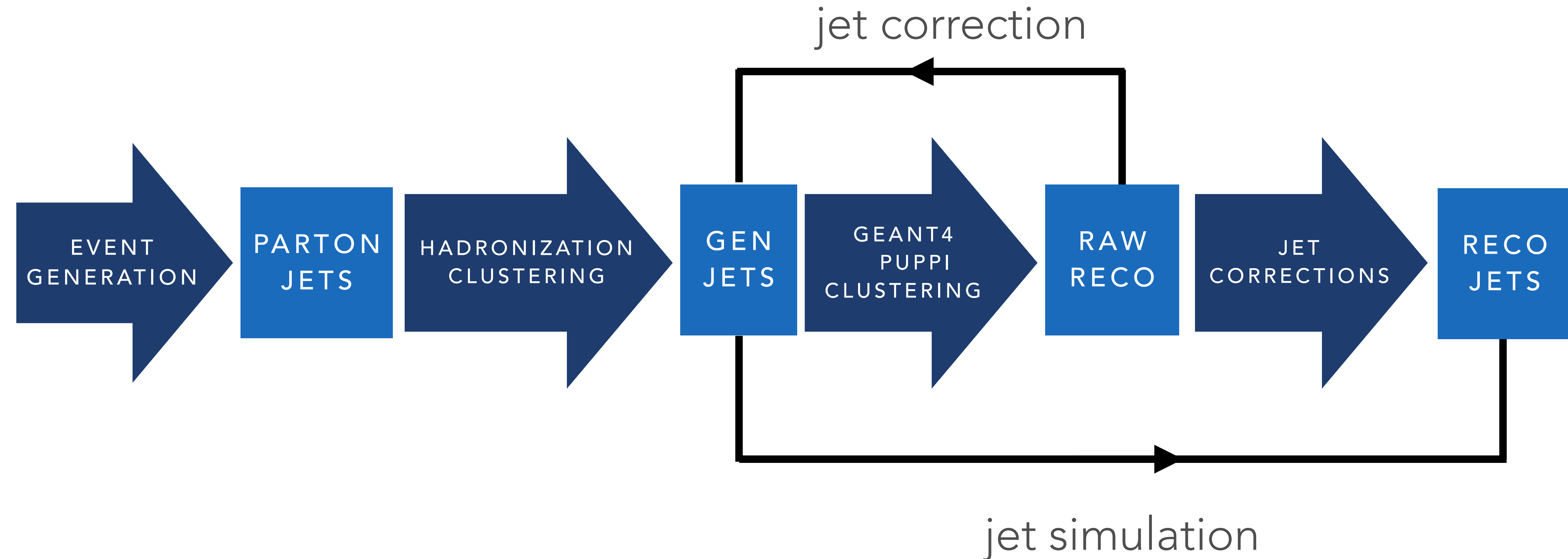
Application 2: How can we make *accurate* predictions for stochastic processes?

JET SIMULATION AND CORRECTION

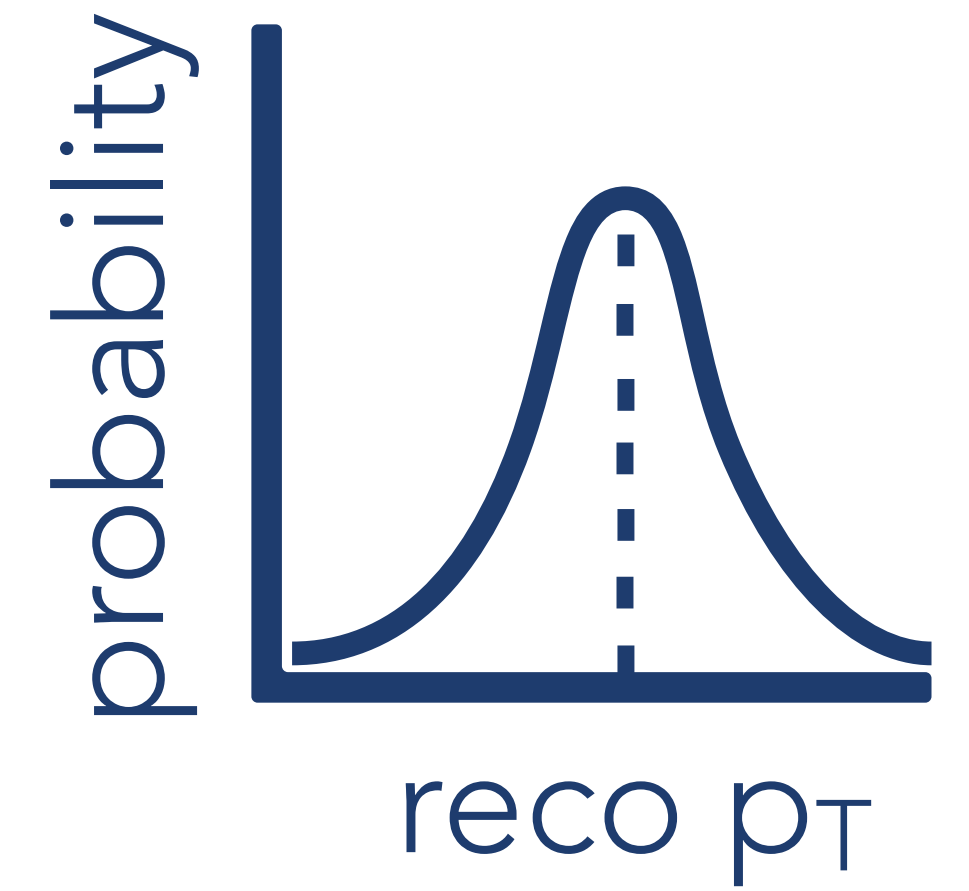
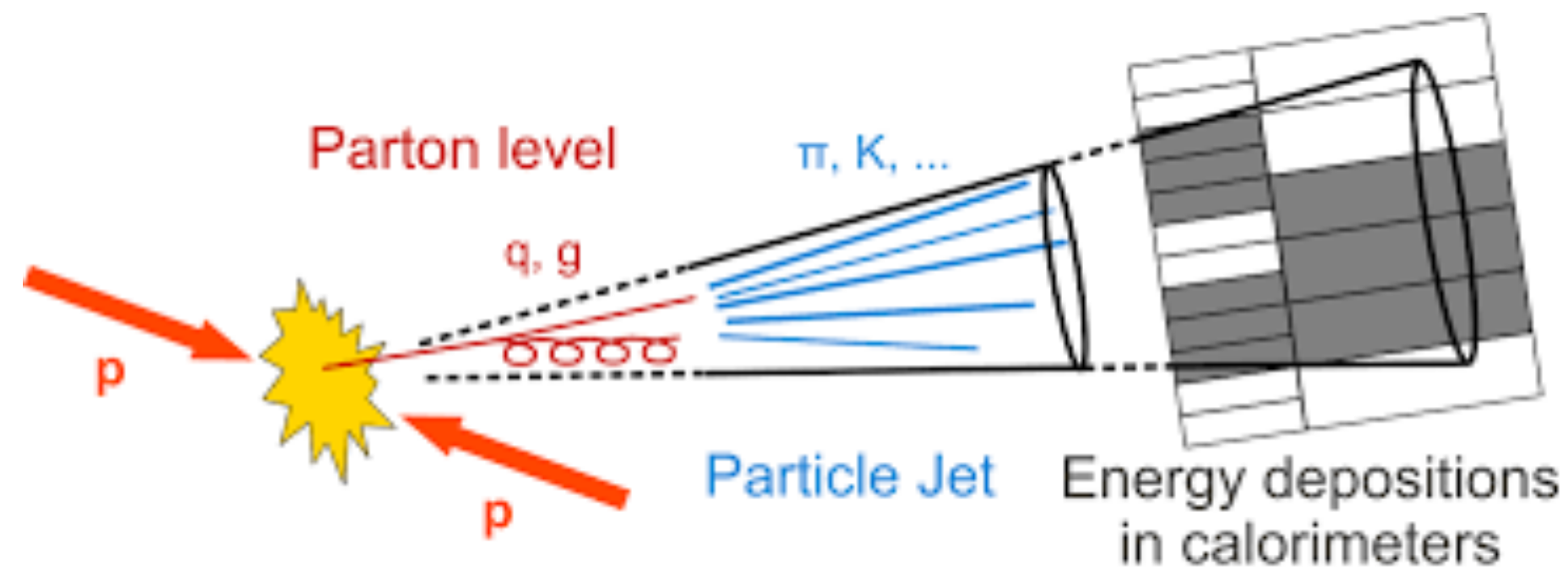


DATASET: CMS Collaboration (2019). Simulated dataset QCD_Pt-15to7000_TuneCUETP8M1_Flat_13TeV_pythia8 in MINIAODSIM format for 2016 collision data. CERN Open Data Portal. DOI:[10.7483/OPENDATA.CMS.J52Q.4T4E](https://doi.org/10.7483/OPENDATA.CMS.J52Q.4T4E)

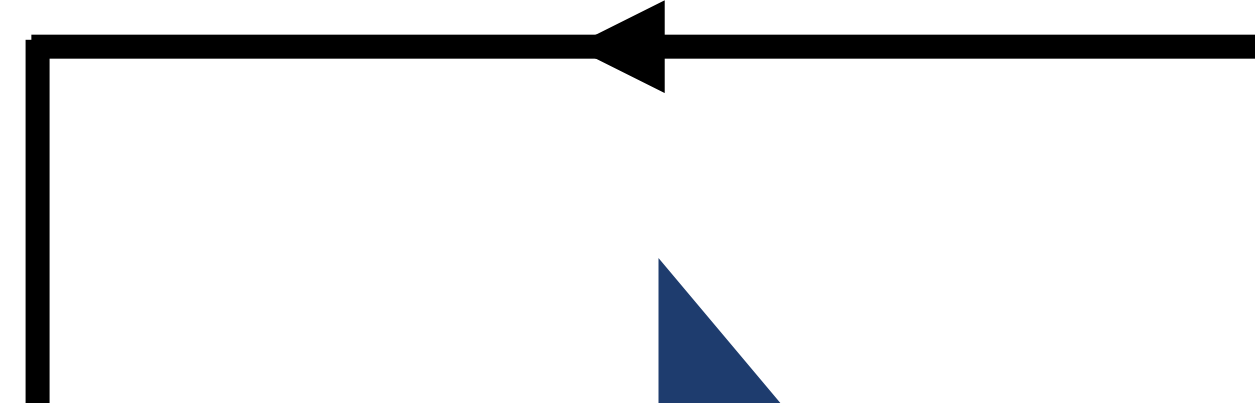
JET SIMULATION AND CORRECTION



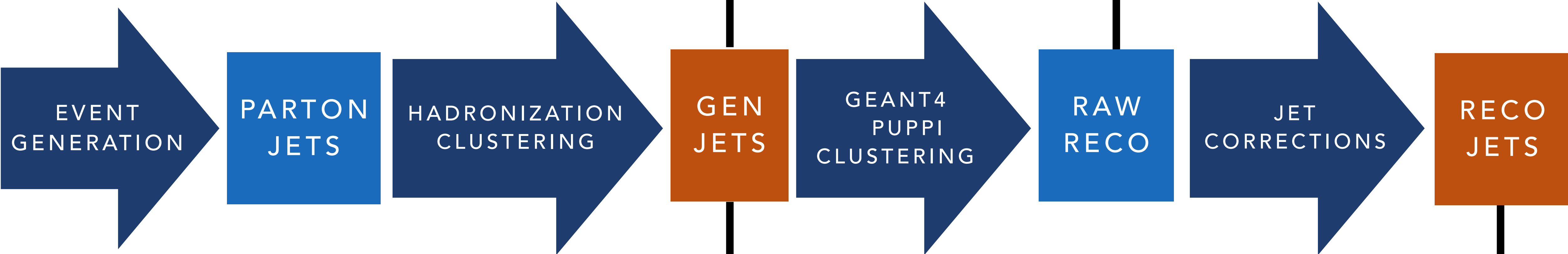
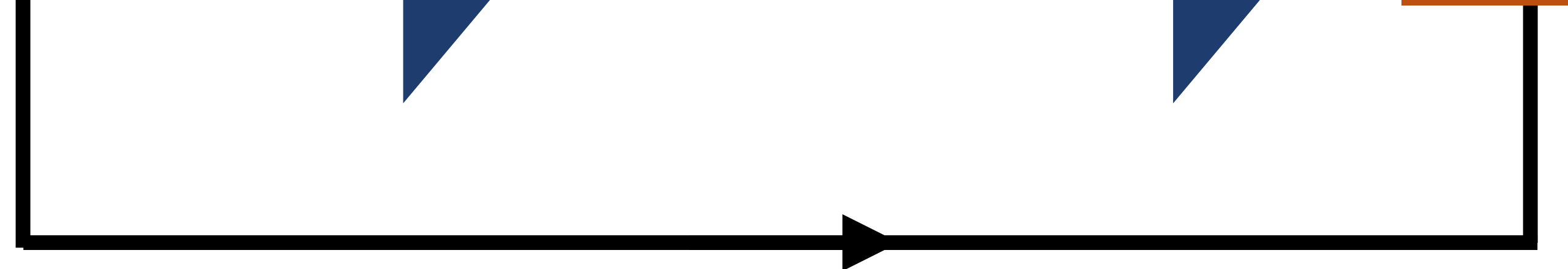
NEED FOR DISTRIBUTION PREDICTIONS



jet correction



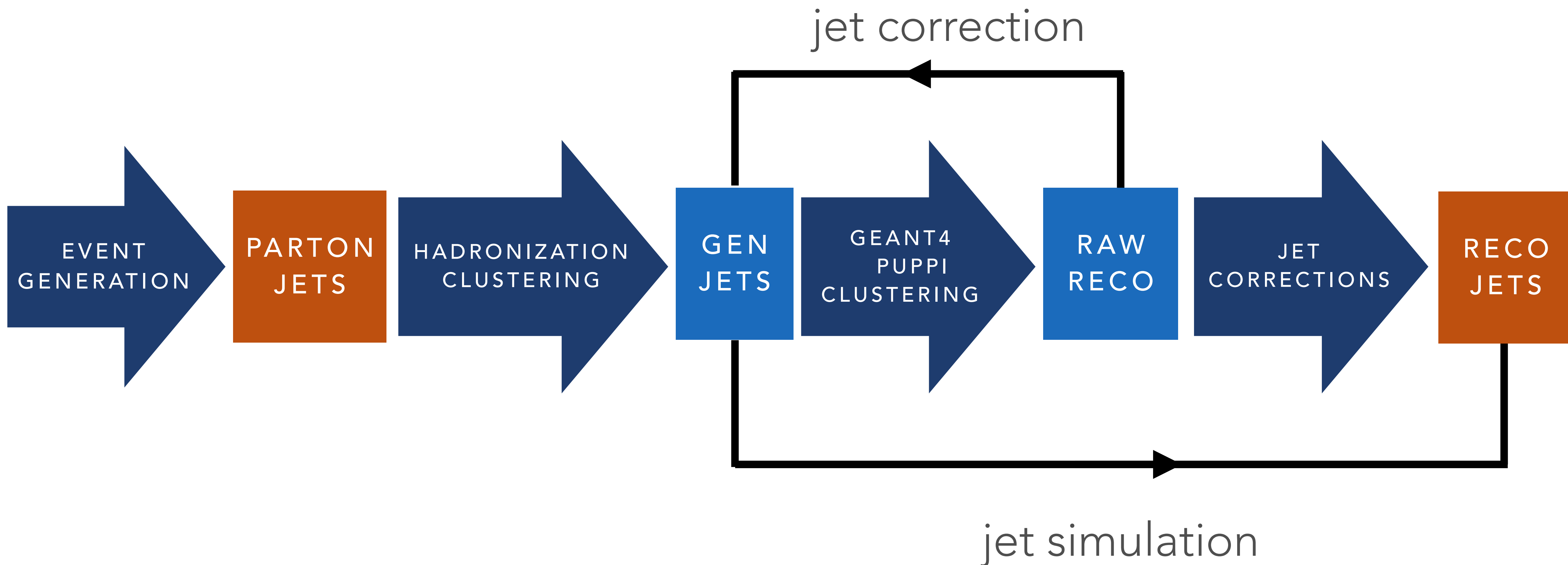
jet simulation



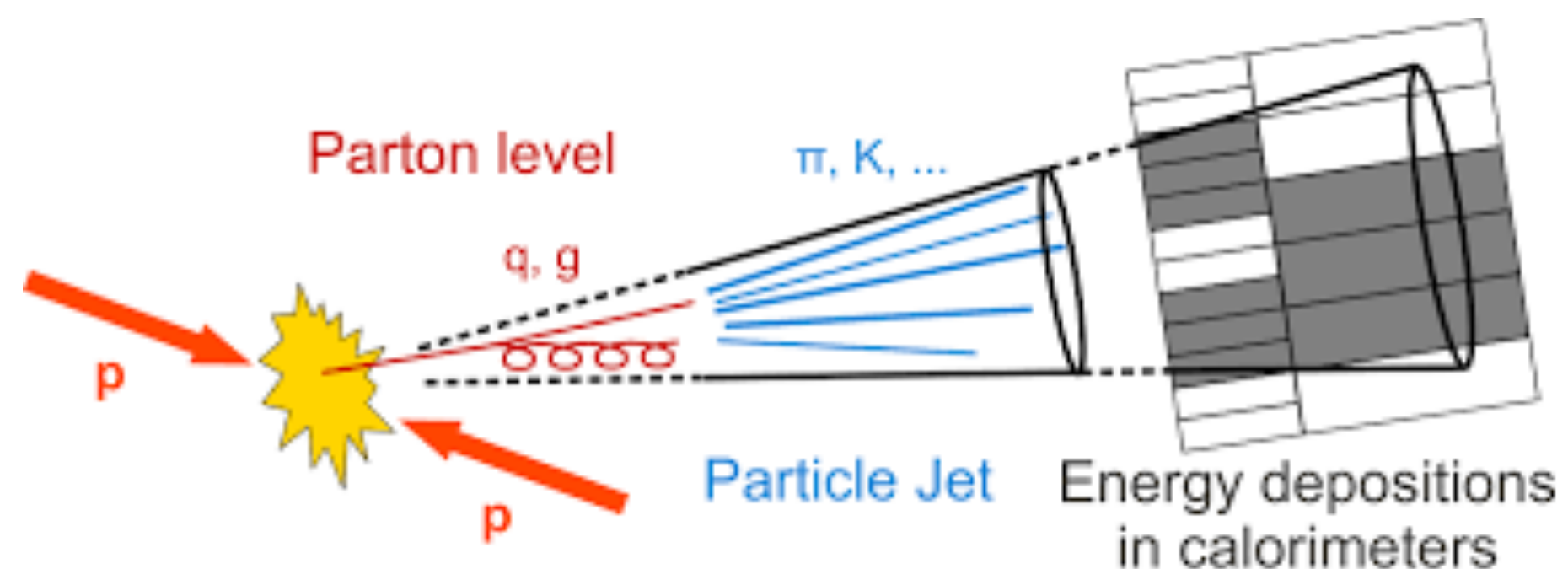
JET SIMULATION AND CORRECTION

J. BLUE, ET.AL., CHEP '21

EPJ WOC 251, 03055 (2021) [HTTPS://DOI.ORG/10.1051/EPJCONF/202125103055](https://doi.org/10.1051/EPJCONF/202125103055)



EXISTING METHODS



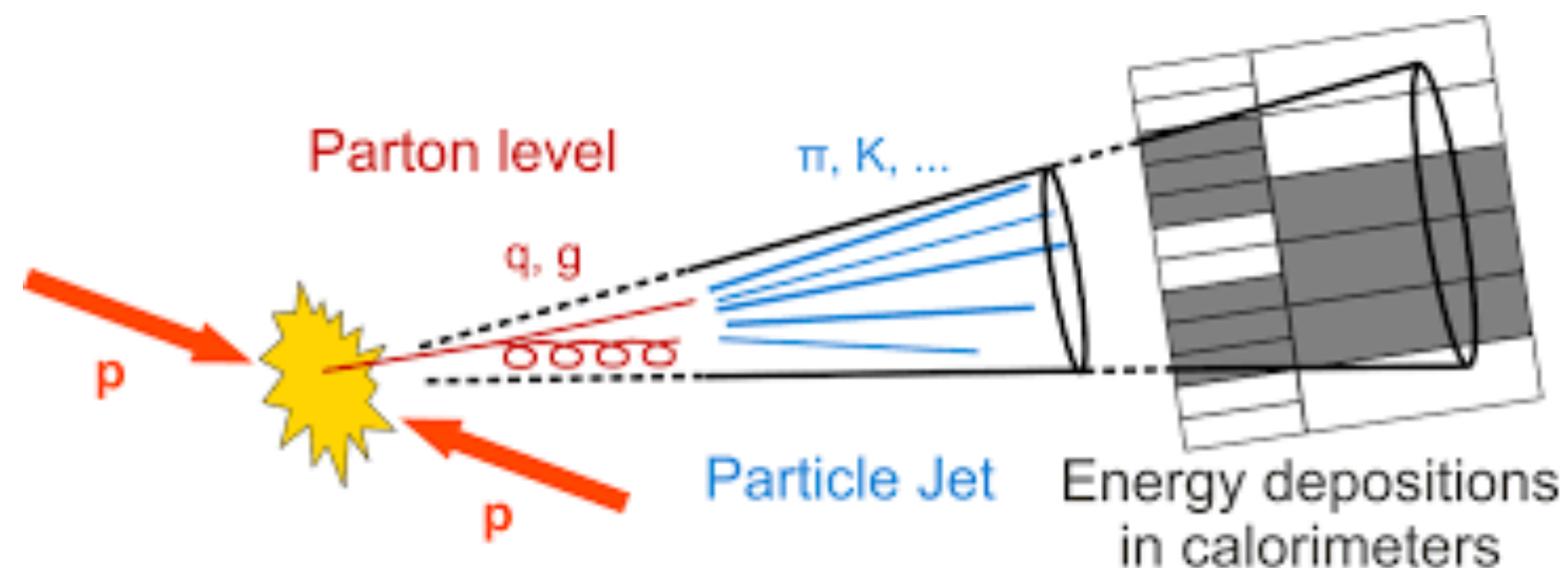
(conditional) generative adversarial networks

arXiv:1912.00477
arXiv:1807.01954
arXiv:1805.00850
arXiv:1712.10321

normalizing flows

arXiv:1904.12072
arXiv:2001.05486
arXiv:2001.10028
arXiv:2012.09873
arXiv:2106.05285

EXISTING METHODS



(conditional) generative adversarial networks

arXiv:1912.00477

arXiv:1807.01954

arXiv:1805.00850

arXiv:1712.10321

How to GAN away Detector Effects

Marco Bellagente¹, Anja Butter¹, Gregor Kasieczka², Tilman Plehn¹, and Ramon Winterhalder¹

¹ Institut für Theoretische Physik, Universität Heidelberg, Germany

² Institut für Experimentalphysik, Universität Hamburg, Germany
bellagente@thphys.uni-heidelberg.de

Precise simulation of electromagnetic calorimeter showers using a Wasserstein Generative Adversarial Network

Martin Erdmann^a Jonas Glombitza^a Thorben Quast^{a,b}

^aIII. Physikalisches Institut A, Rheinisch Westfälische Technische Hochschule, Aachen, Germany

^bEP-LCD, CERN, Geneva, Switzerland

Fast and accurate simulation of particle detectors using generative adversarial networks

Pasquale Musella · Francesco Pandolfi

CALOGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks

Michela Paganini^{1,2,*} Luke de Oliveira^{2,†} and Benjamin Nachman^{2,‡}

¹Department of Physics, Yale University, New Haven, CT 06520, USA

²Lawrence Berkeley National Laboratory, Berkeley, CA, 94720, USA

(Dated: January 1, 2018)

Flow-based generative models for Markov chain Monte Carlo in lattice field theory

M. S. Albergo,^{1,2,3} G. Kanwar,⁴ and P. E. Shanahan^{4,1}

¹Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada

²Cavendish Laboratories, University of Cambridge, Cambridge CB3 0HE, U.K.

³University of Waterloo, Waterloo, Ontario N2L 3G1, Canada

⁴Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, U.S.A.

i-flow: High-dimensional Integration and Sampling with Normalizing Flows

CHRISTINA GAO¹, JOSHUA ISAACSON¹, AND CLAUDIUS KRAUSE¹

¹Theoretical Physics Department, Fermi National Accelerator Laboratory, Batavia, IL, 60510, USA

Event Generation with Normalizing Flows

Christina Gao,¹ Stefan Höche,¹ Joshua Isaacson,¹ Claudius Krause,¹ and Holger Schulz²

¹Fermi National Accelerator Laboratory, Batavia, IL, 60510, USA

²Department of Physics, University of Cincinnati, Cincinnati, OH 45219, USA

Measuring QCD Splittings with Invertible Networks

Sebastian Bieringer¹, Anja Butter¹, Theo Heimel¹, Stefan Höche², Ullrich Köthe³, Tilman Plehn¹, and Stefan T. Radev⁴

¹Institut für Theoretische Physik, Universität Heidelberg, Germany

²Fermi National Accelerator Laboratory, Batavia, IL, USA

³Heidelberg Collaboratory for Image Processing, Universität Heidelberg, Germany

⁴Psychologisches Institut, Universität Heidelberg, Germany

heimel@thphys.uni-heidelberg.de

CaloFlow: Fast and Accurate Generation of Calorimeter Showers with Normalizing Flows

Claudius Krause and David Shih

NHETC, Dept. of Physics and Astronomy, Rutgers University, Piscataway, NJ 08854, USA

E-mail: Claudius.Krause@rutgers.edu, shih@physics.rutgers.edu



normalizing flows

[arXiv:1904.12072](https://arxiv.org/abs/1904.12072)

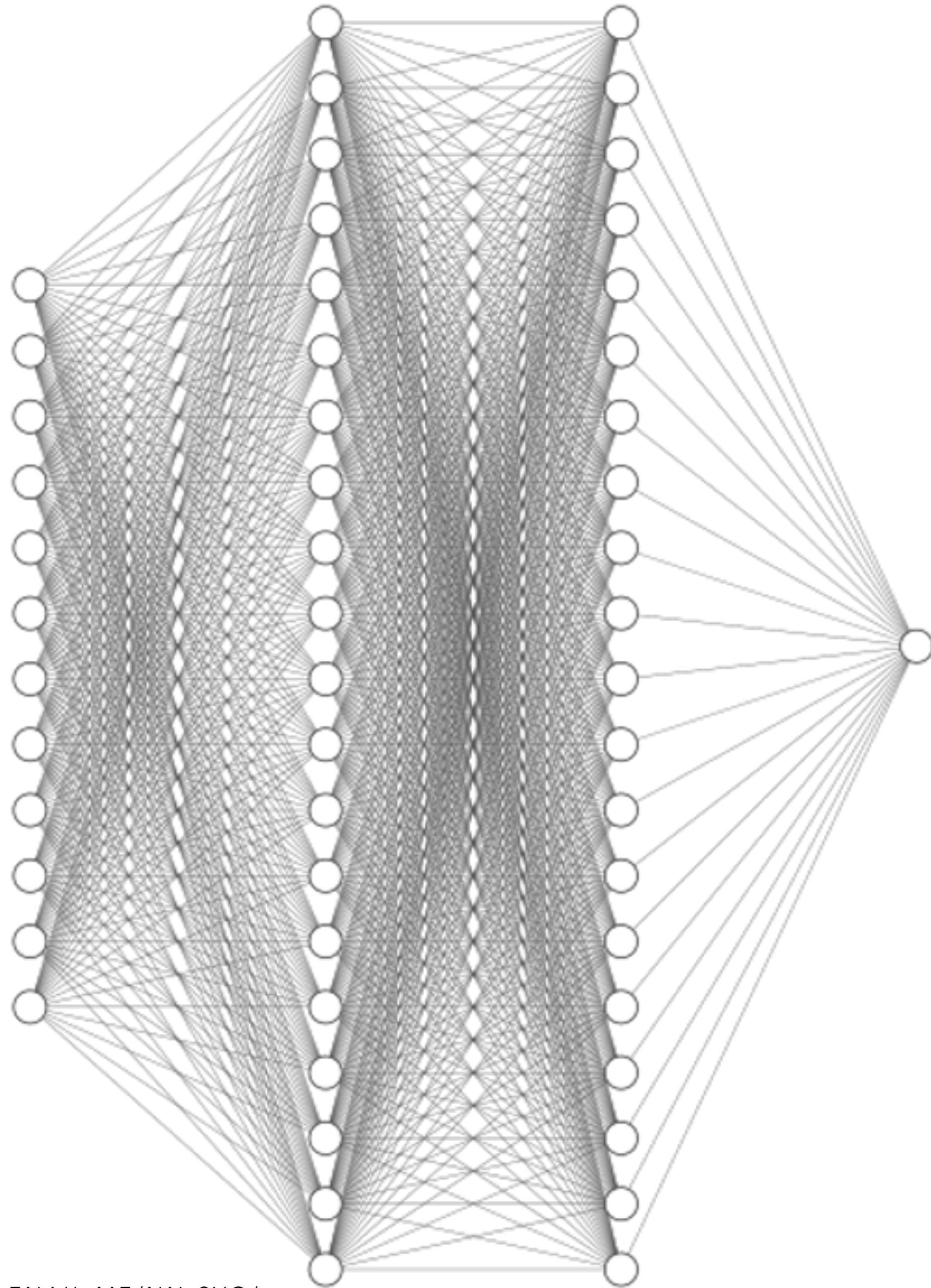
[arXiv:2001.05486](https://arxiv.org/abs/2001.05486)

[arXiv:2001.10028](https://arxiv.org/abs/2001.10028)

[arXiv:2012.09873](https://arxiv.org/abs/2012.09873)

[arXiv:2106.05285](https://arxiv.org/abs/2106.05285)

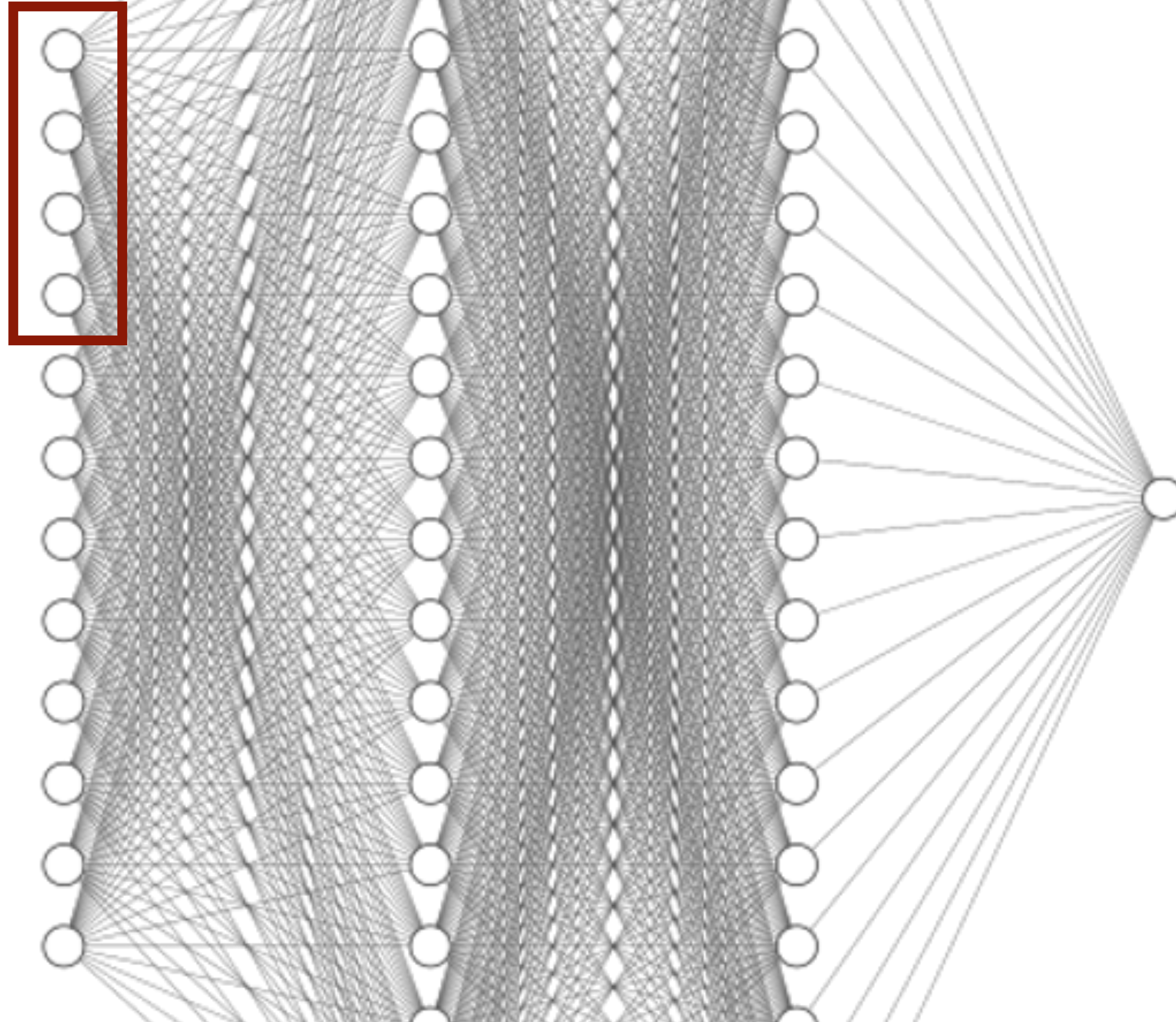
IMPLICIT QUANTILE NETWORKS ARCHITECTURE



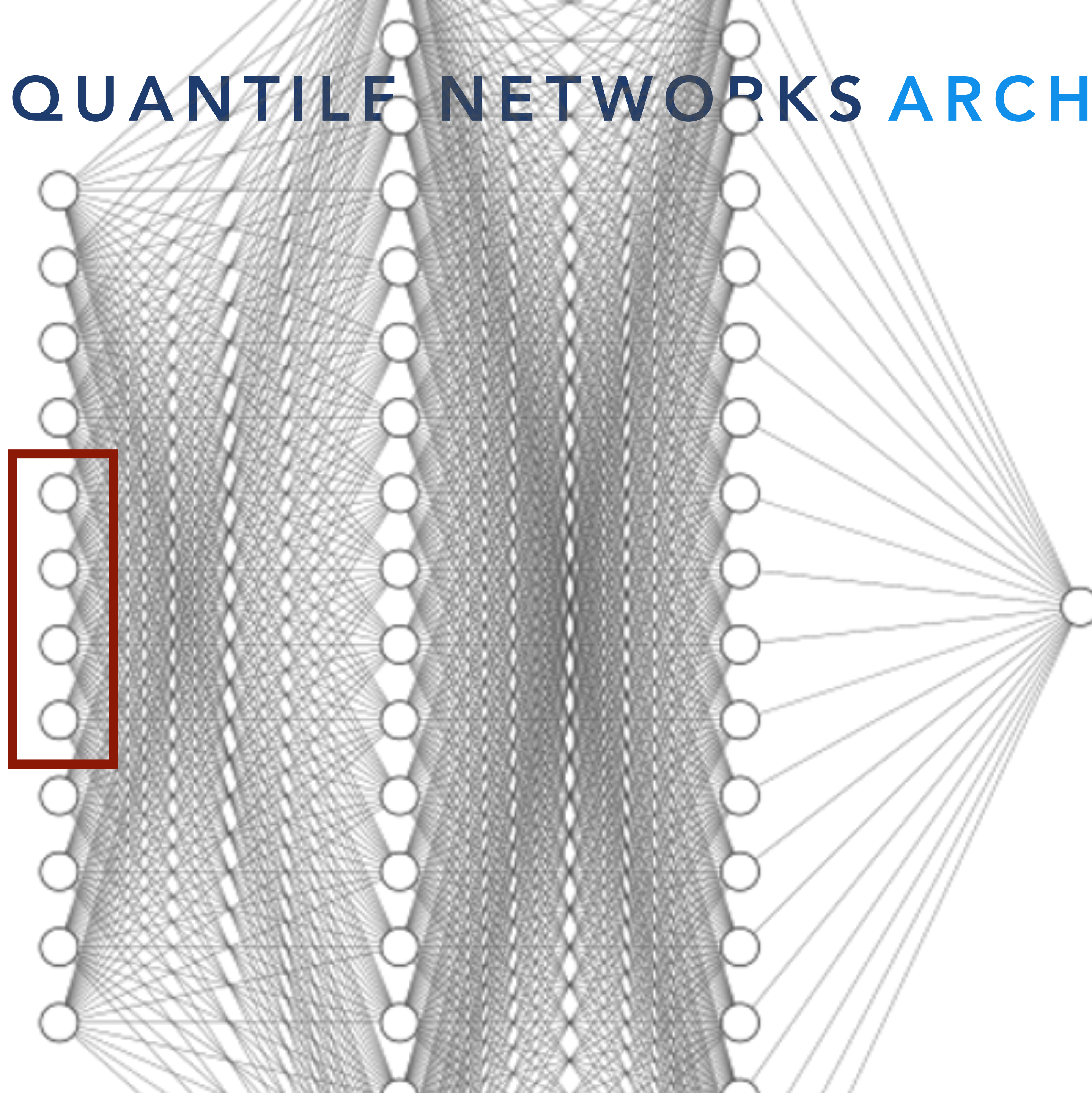
$$(p_T, \eta, \phi, m) \rightarrow (p'_T, \eta', \phi', m')$$

IMPLICIT QUANTILE NETWORKS ARCHITECTURE

(p_T, η, ϕ, m)

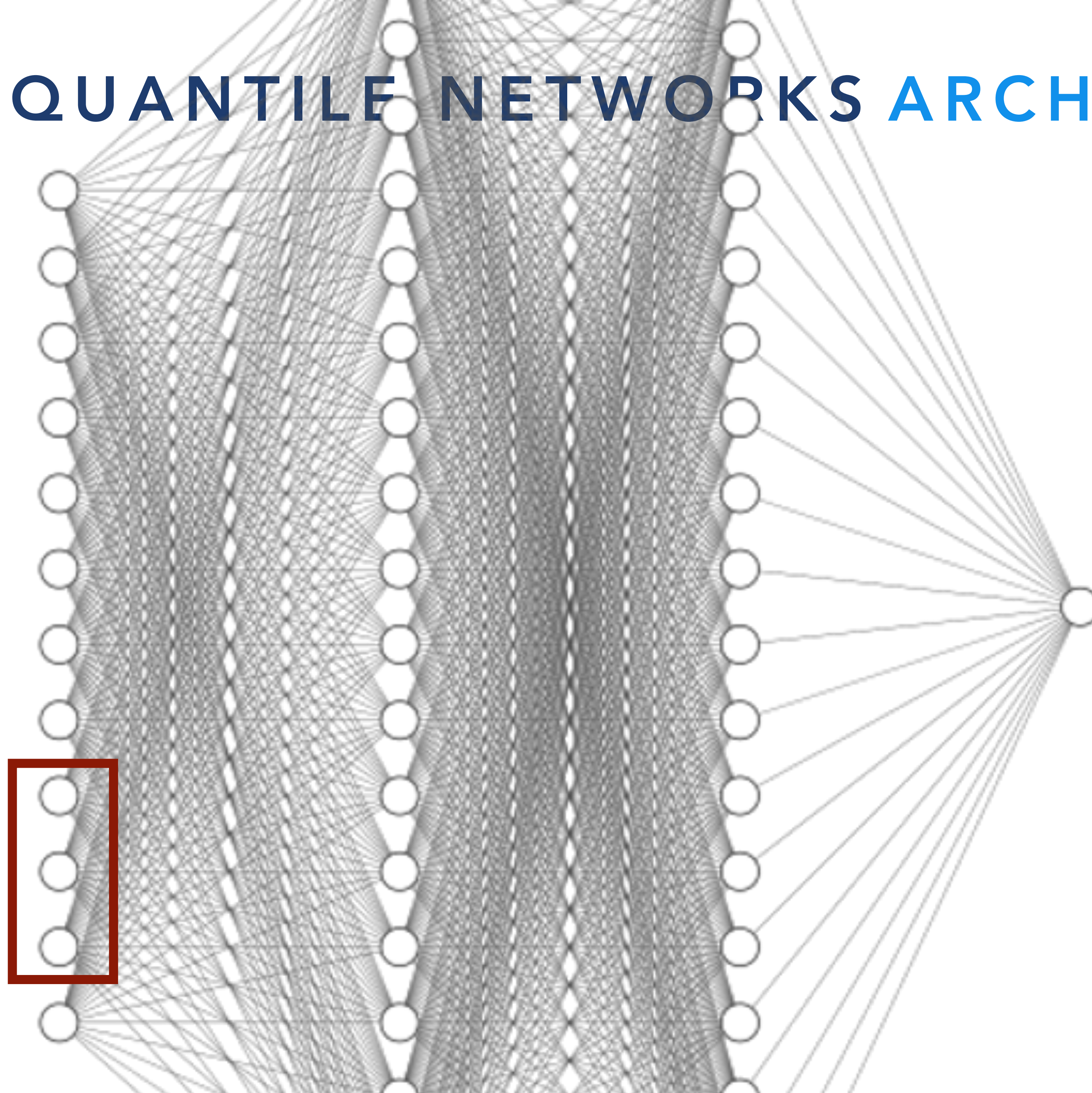


IMPLICIT QUANTILE NETWORKS ARCHITECTURE



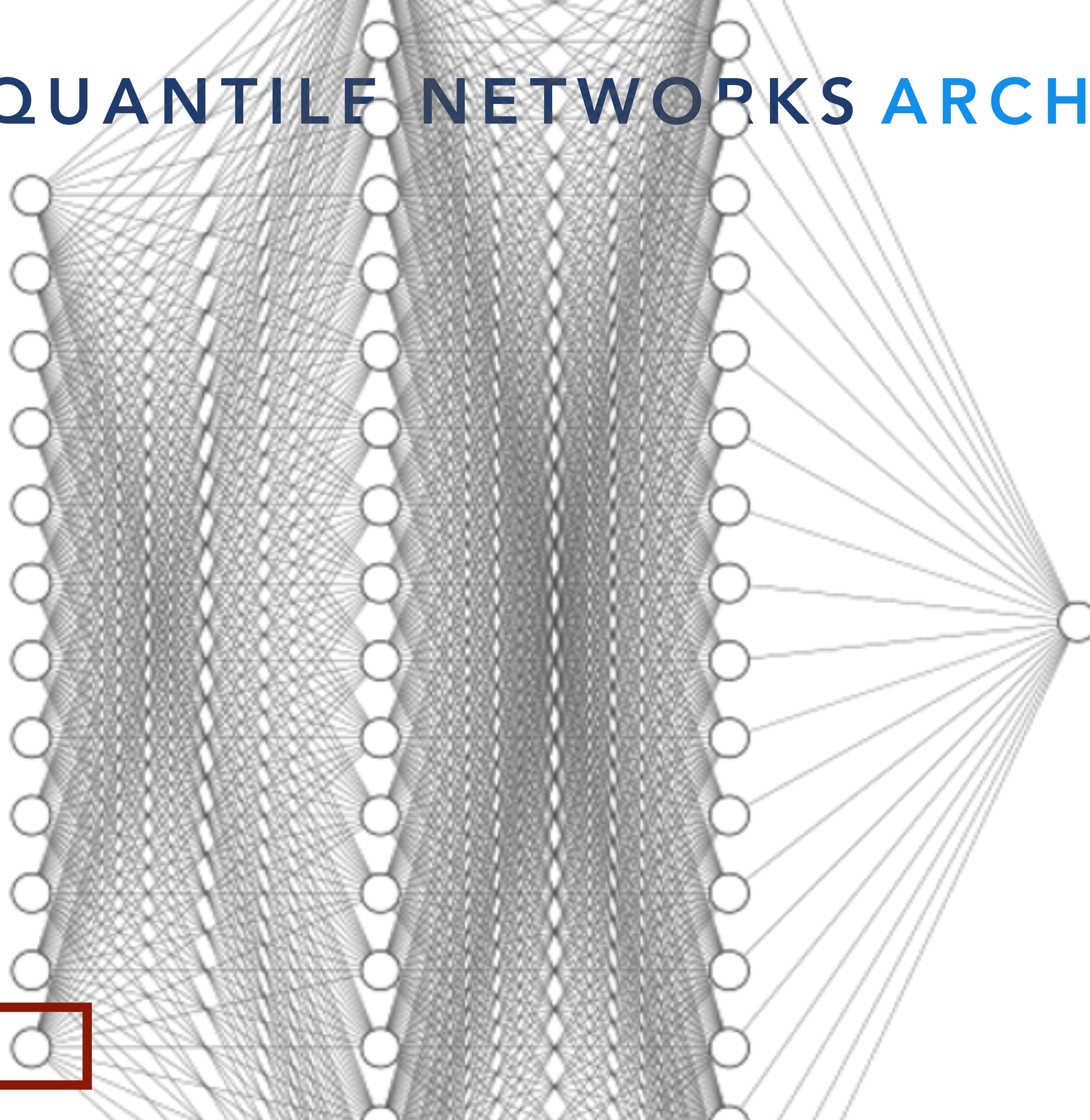
(p_T, η, ϕ, m)
[0,0,1,0]

IMPLICIT QUANTILE NETWORKS ARCHITECTURE



(p'_T, η', ϕ')

IMPLICIT QUANTILE NETWORKS ARCHITECTURE



$\tau \sim U(0,1)$



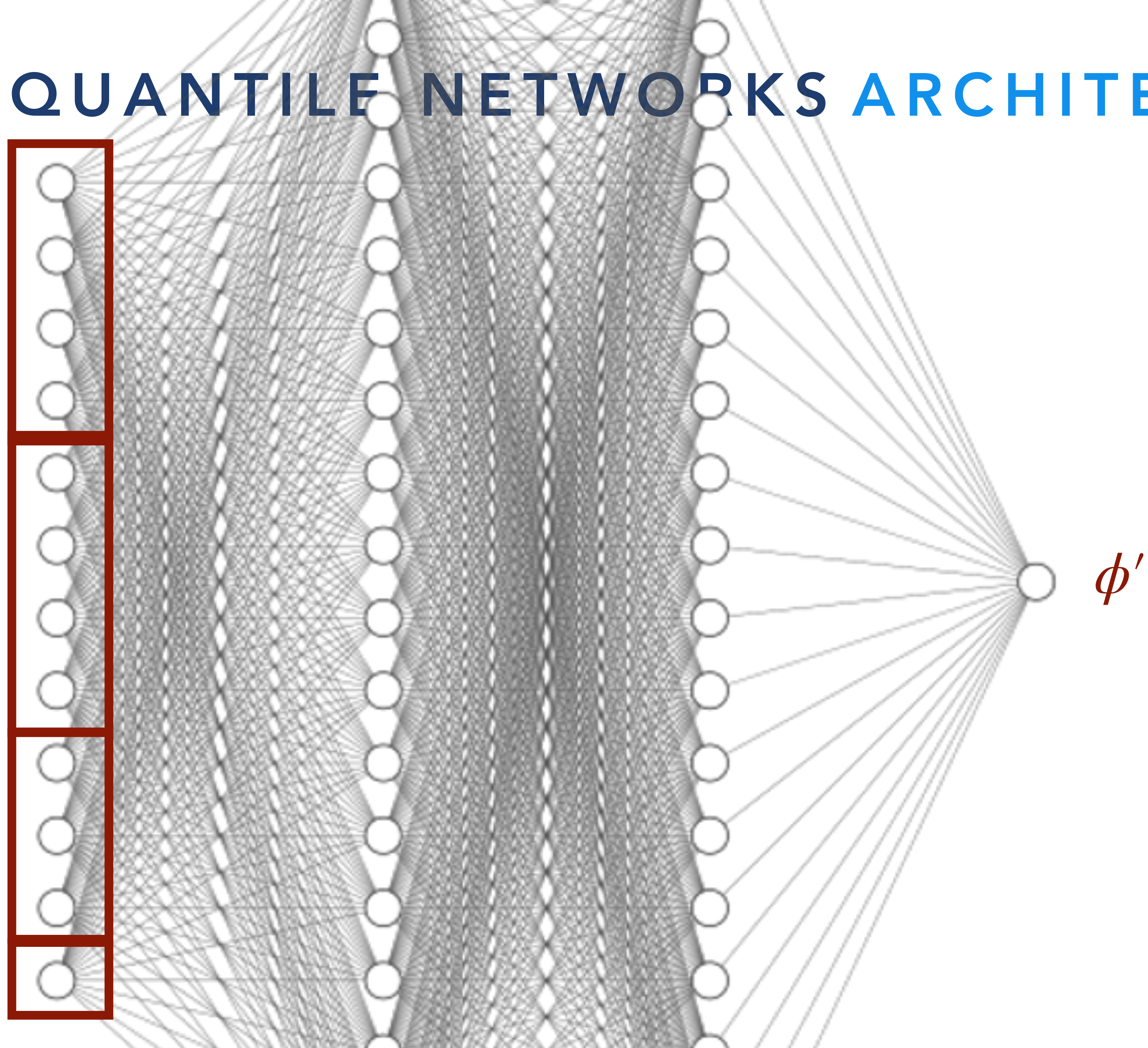
IMPLICIT QUANTILE NETWORKS ARCHITECTURE

(p_T, η, ϕ, m)

(p_T, η, ϕ, m)
 $[0,0,1,0]$

(p'_T, η', ϕ')

$\tau \sim U(0,1)$



IMPLICIT QUANTILE NETWORKS ARCHITECTURE

(p_T, η, ϕ, m)

(p_T, η, ϕ, m)
[0,0,1,0]

(p'_T, η', ϕ')

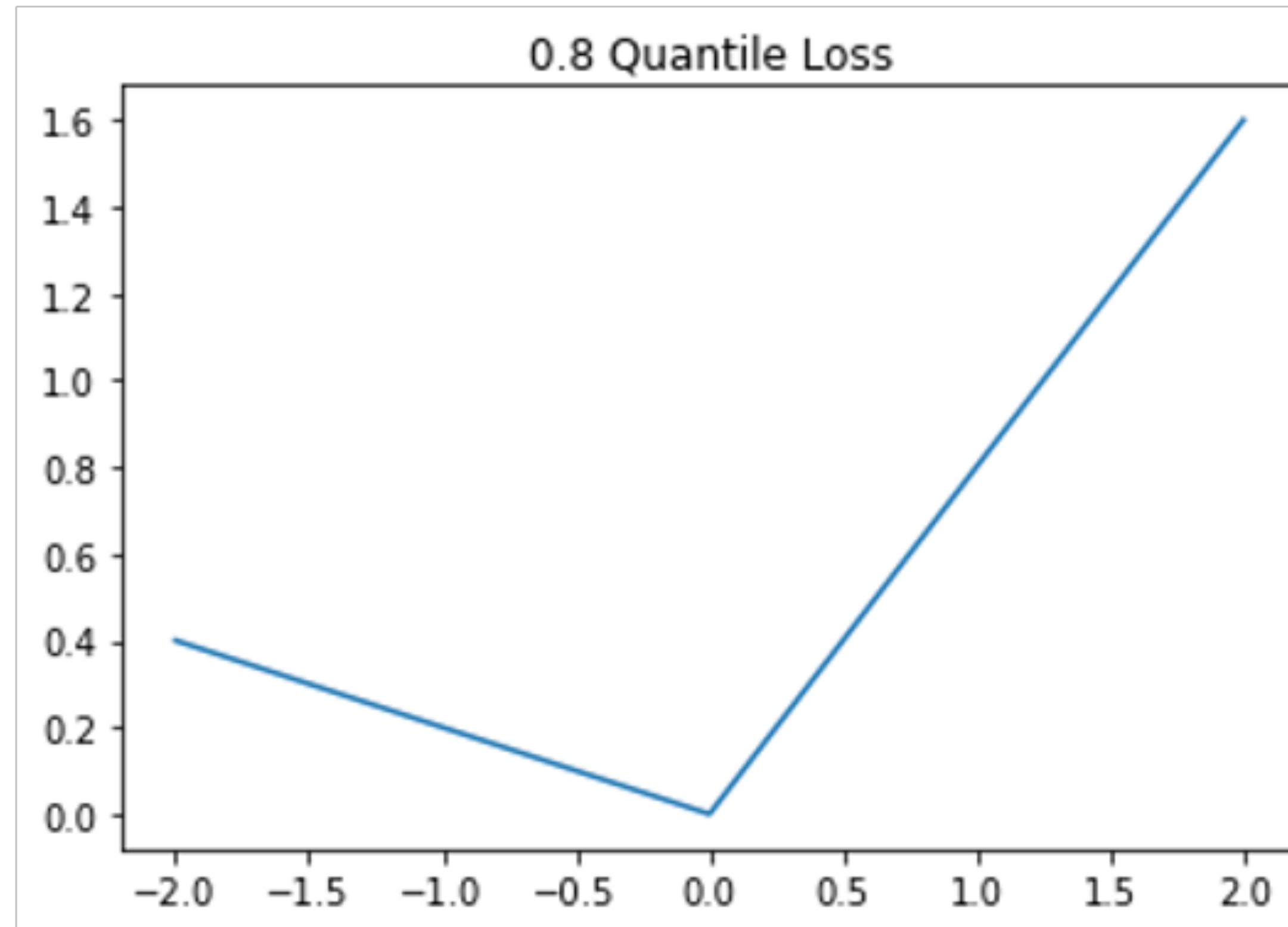
$\tau \sim U(0,1)$

$$\begin{aligned} (p_T, \eta, \phi, m, 1, 0, 0, 0, 0, 0) &\rightarrow (p'_T), \\ (p_T, \eta, \phi, m, 0, 1, 0, 0, p'_T, 0, 0) &\rightarrow (\eta'), \\ (p_T, \eta, \phi, m, 0, 0, 1, 0, p'_T, \eta', 0) &\rightarrow (\phi'), \\ (p_T, \eta, \phi, m, 0, 0, 0, 1, p'_T, \eta', \phi') &\rightarrow (m'), \end{aligned}$$

$$p(A, B, C, D) = p(A | D)p(B | A, D)p(C | A, B, D)$$

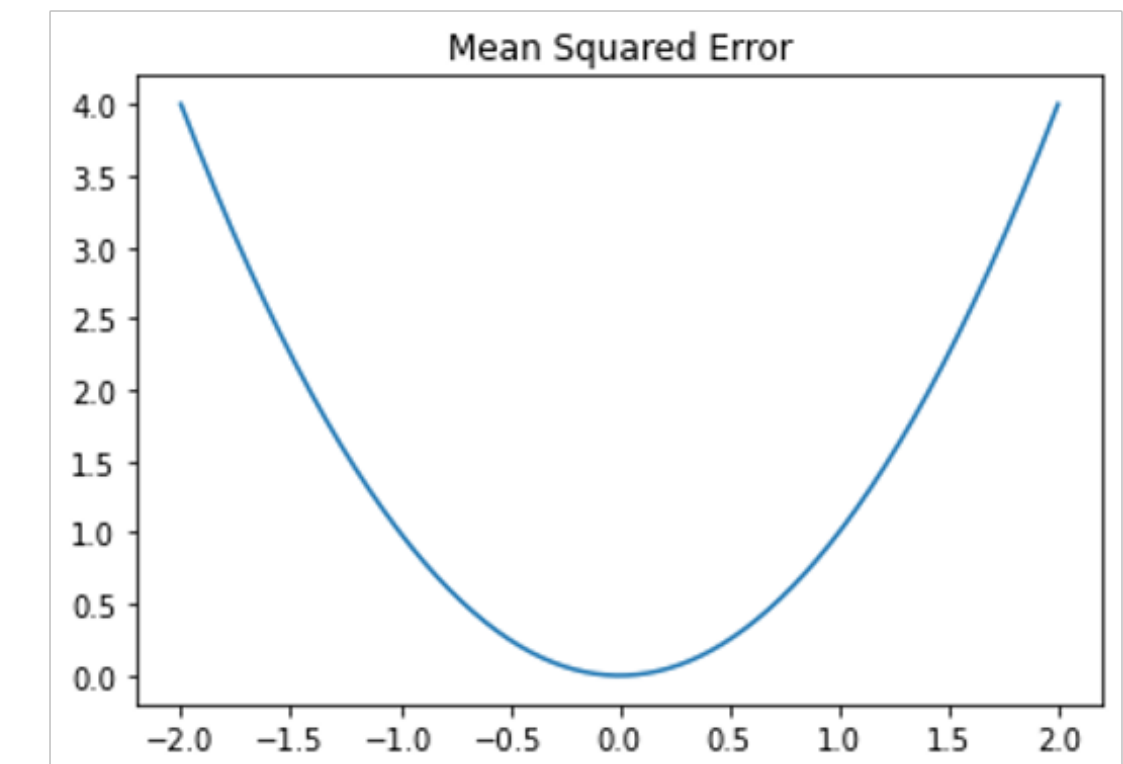
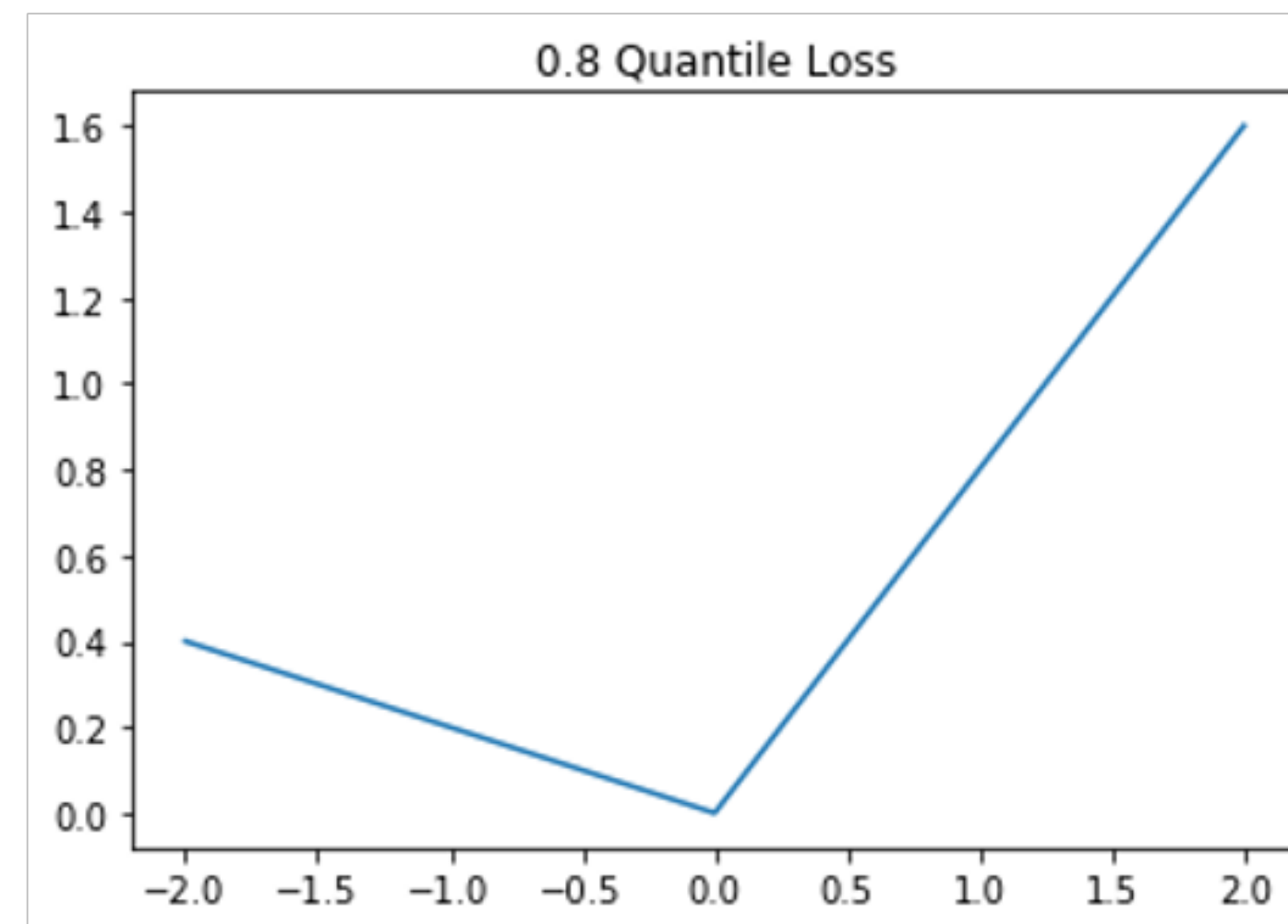
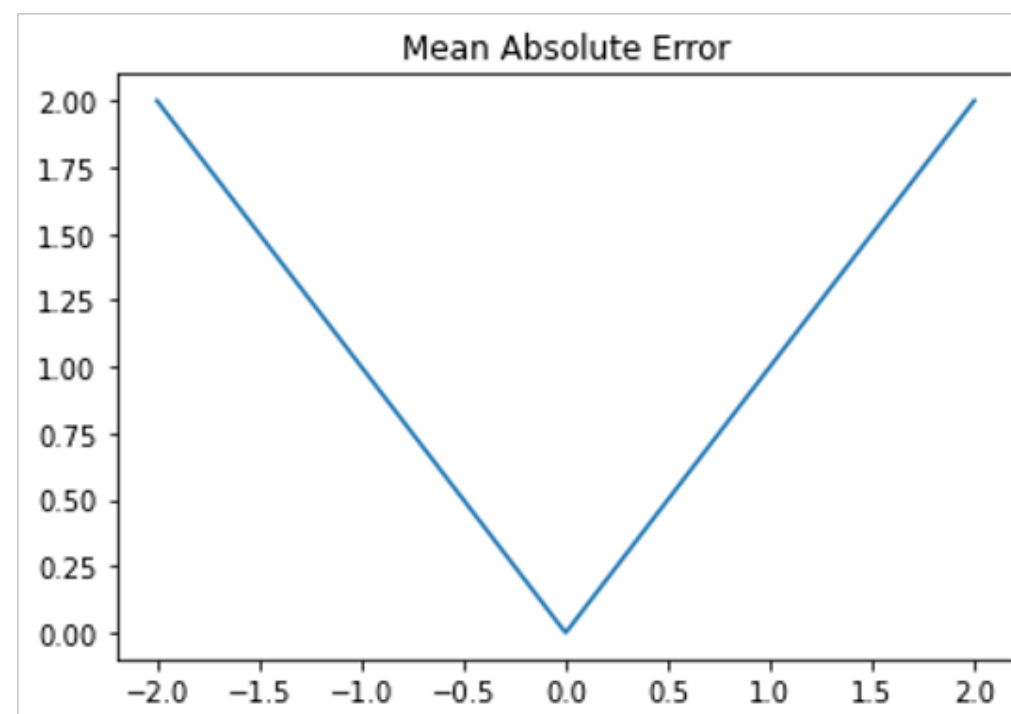
ϕ'

IMPLICIT QUANTILE NETWORKS LOSS FUNCTION



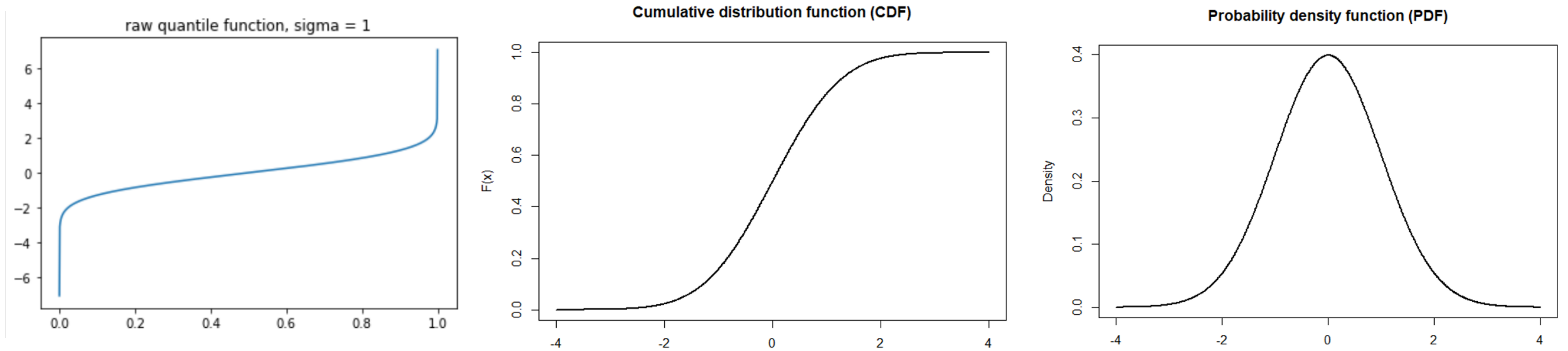
$$\mathcal{L}(f, x, y, \tau) = \begin{cases} \tau(y - f(x, \tau)) & y \geq f(x, \tau) \\ (\tau - 1)(y - f(x, \tau)) & y < f(x, \tau) \end{cases}$$

IMPLICIT QUANTILE NETWORKS LOSS FUNCTION



$$\mathcal{L}(f, x, y, \tau) = \begin{cases} \tau(y - f(x, \tau)) & y \geq f(x, \tau) \\ (\tau - 1)(y - f(x, \tau)) & y < f(x, \tau) \end{cases}$$

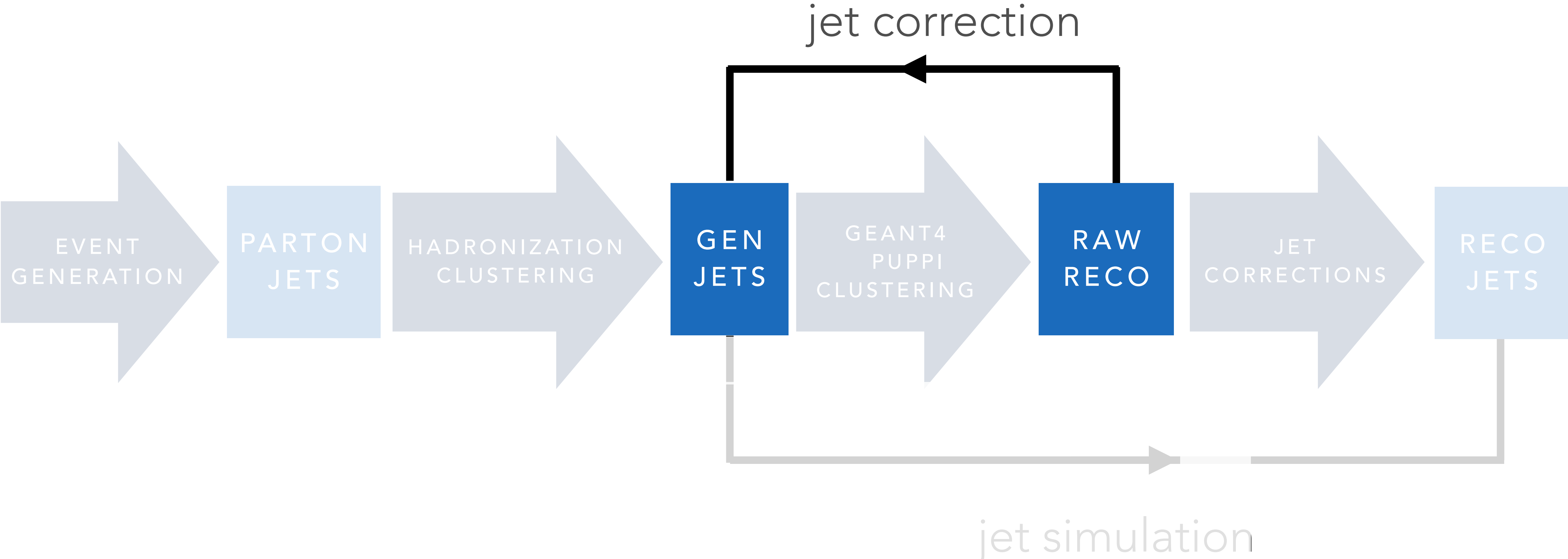
IMPLICIT QUANTILE NETWORKS LOSS FUNCTION



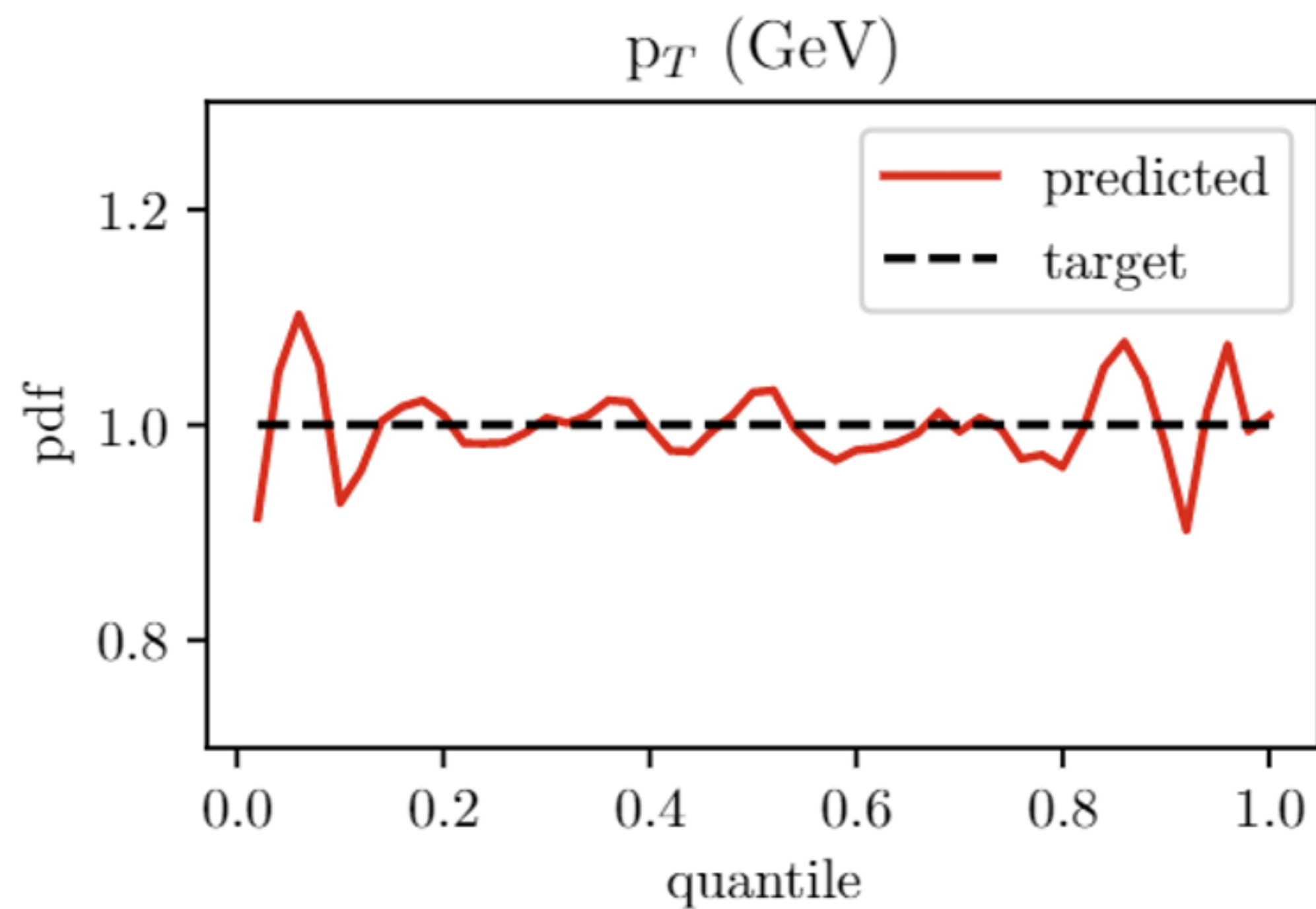
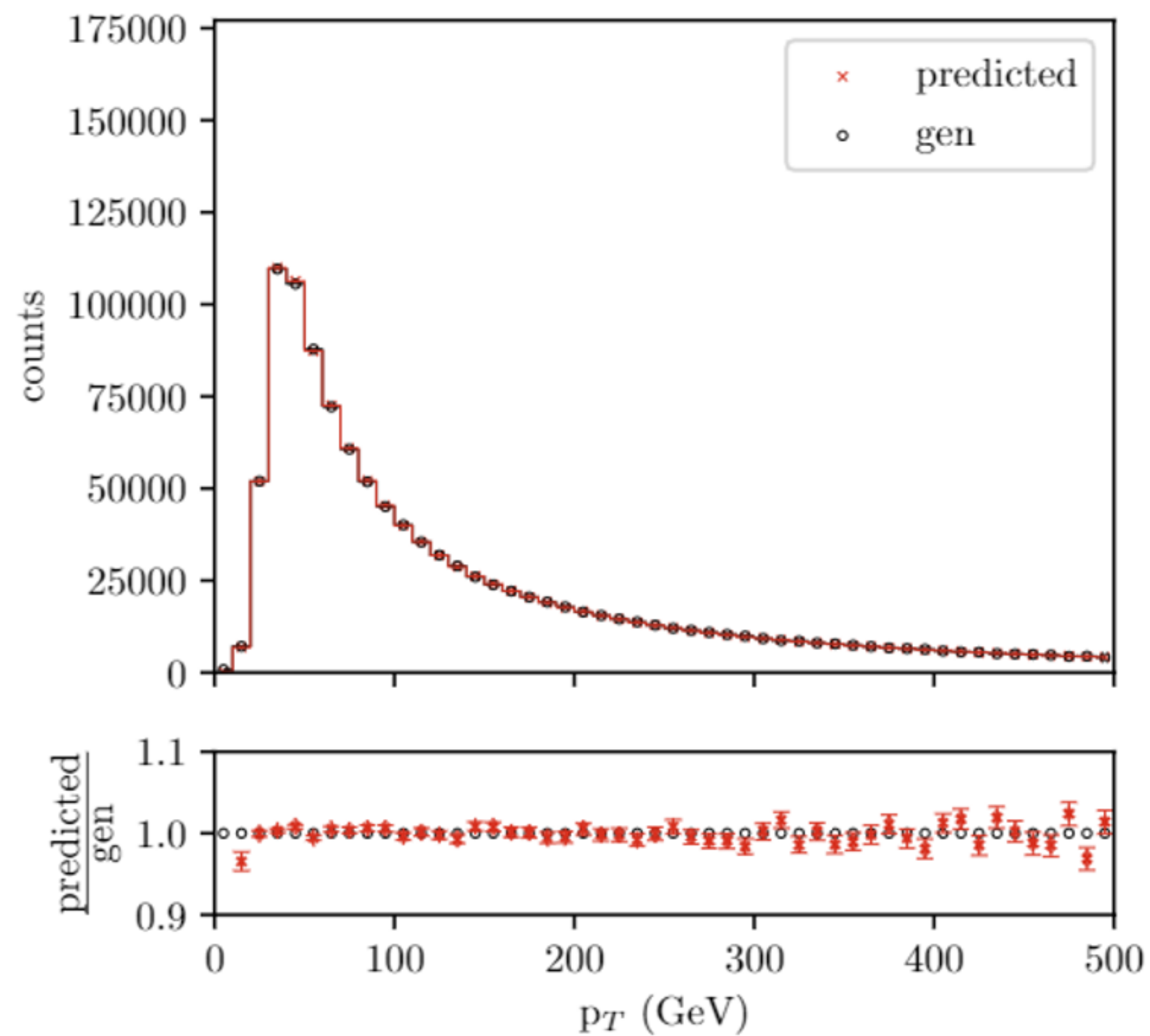
$$\mathcal{L}(f, x, y, \tau) = \begin{cases} \tau(y - f(x, \tau)) & y \geq f(x, \tau) \\ (\tau - 1)(y - f(x, \tau)) & y < f(x, \tau) \end{cases}$$

regularization
$$\begin{cases} \left(\frac{dy}{d\tau}\right)^2 & \frac{dy}{d\tau} < 0 \\ 0 & \frac{dy}{d\tau} \geq 0 \end{cases}$$

RESULTS JET CORRECTION



RESULTS JET CORRECTION

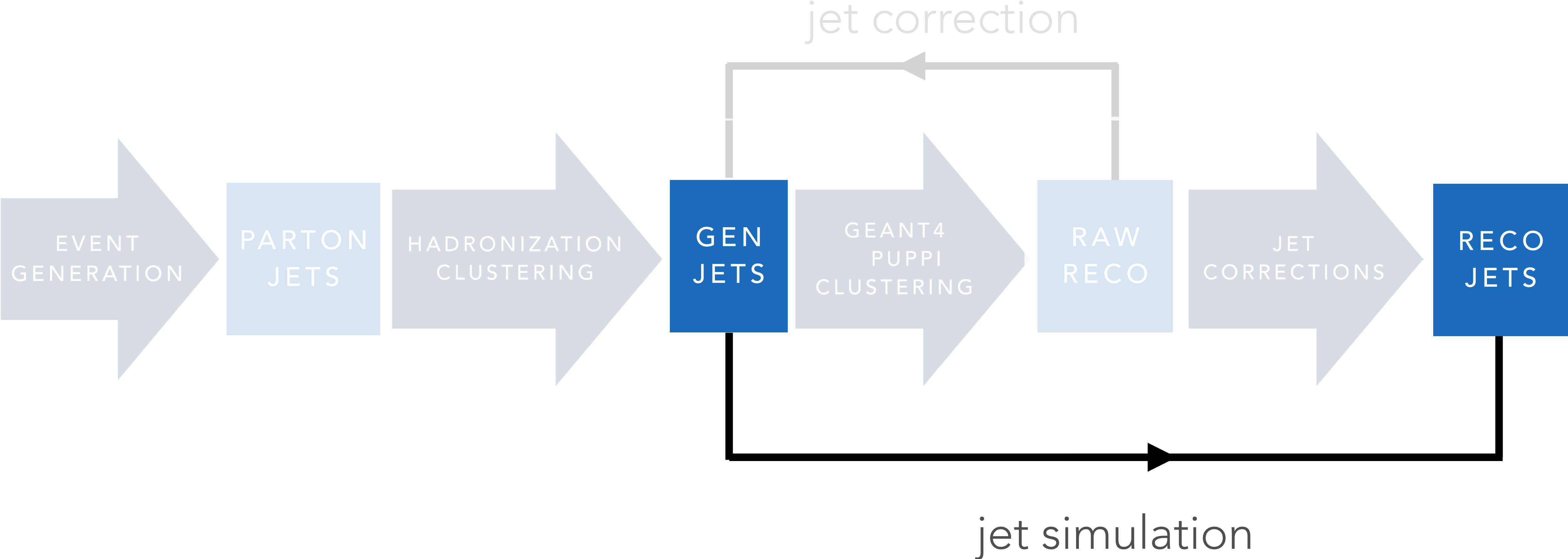


EV
GENE

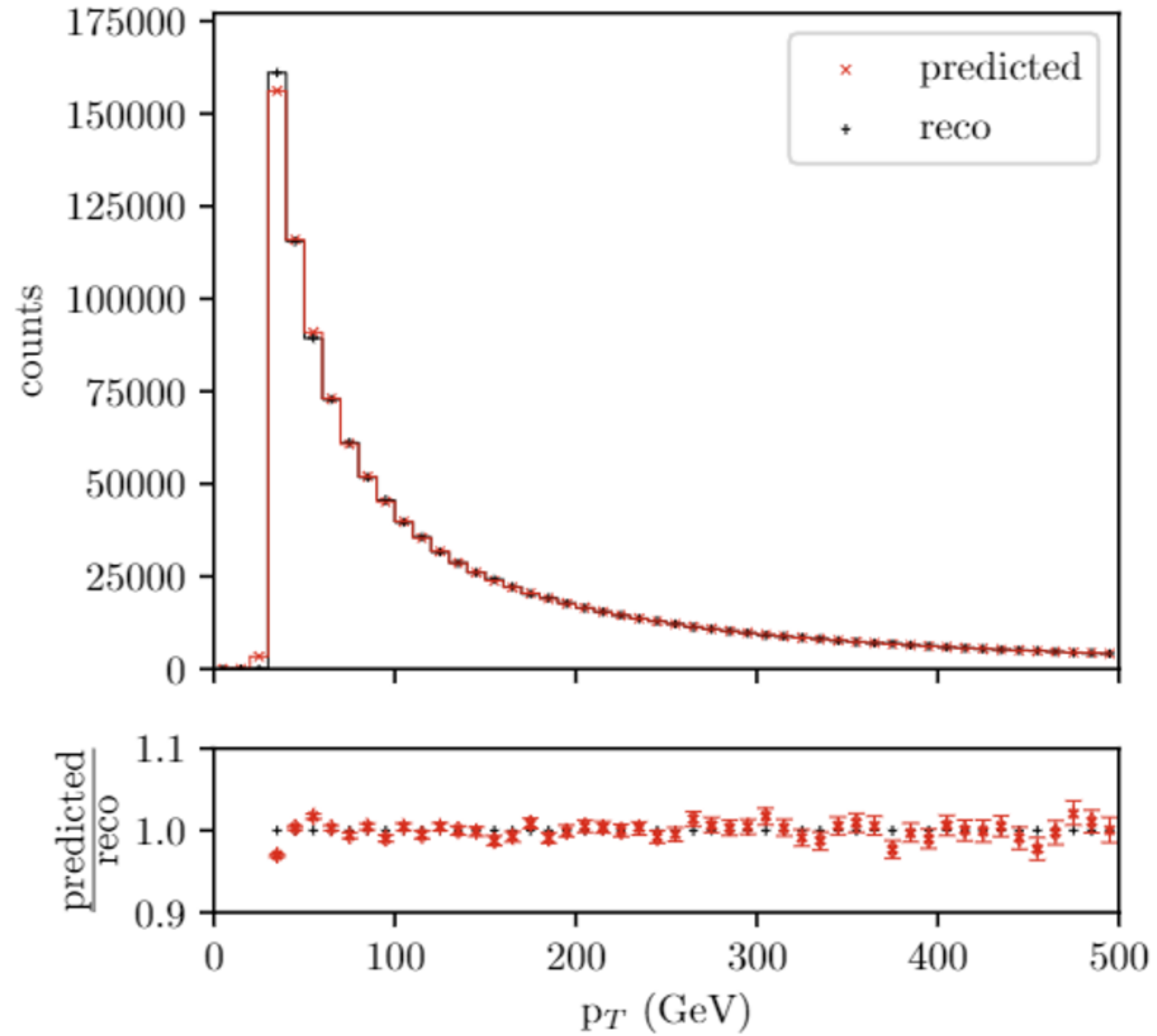
RECO
JETS

jet simulation

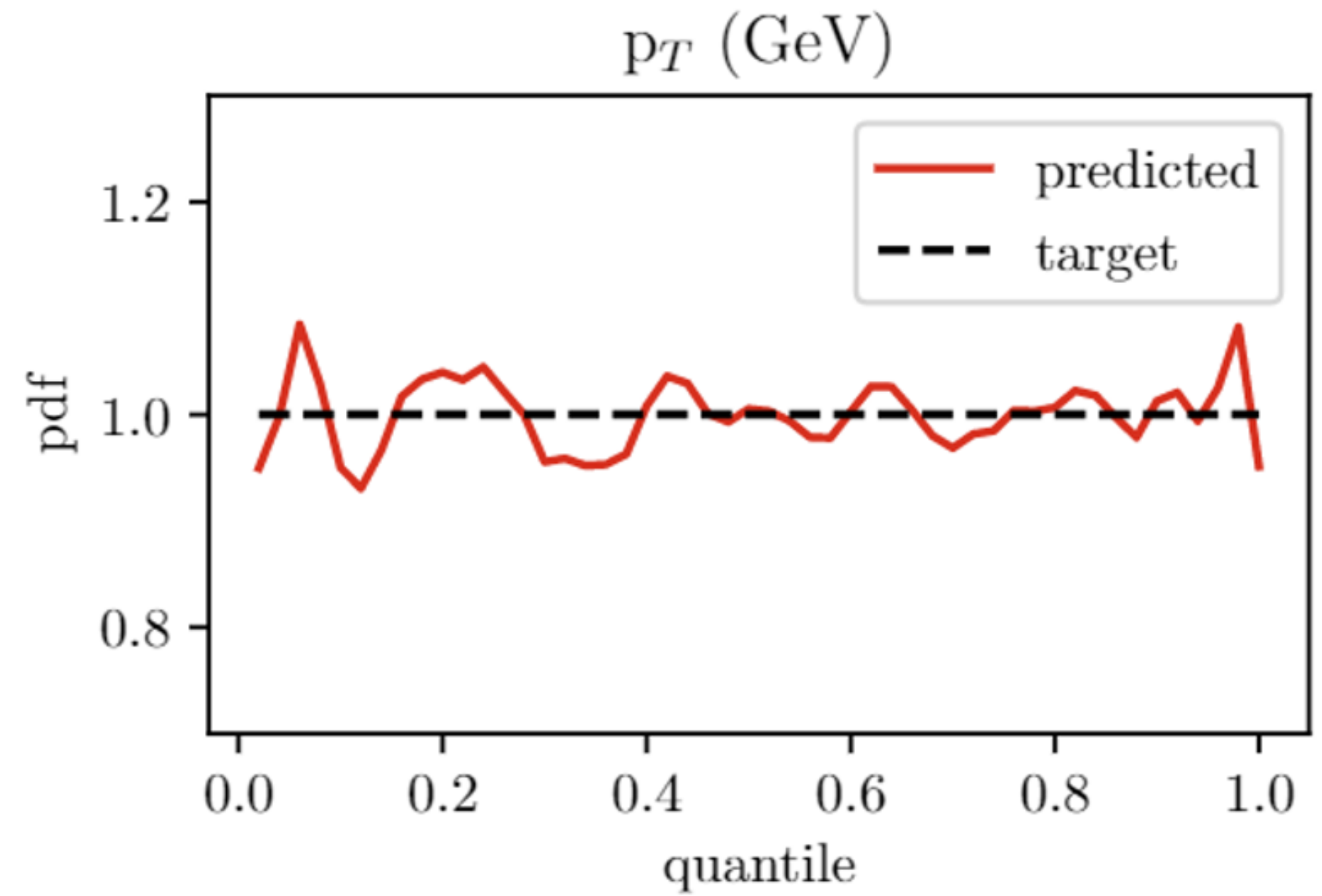
RESULTS JET SIMULATION



RESULTS JET SIMULATION



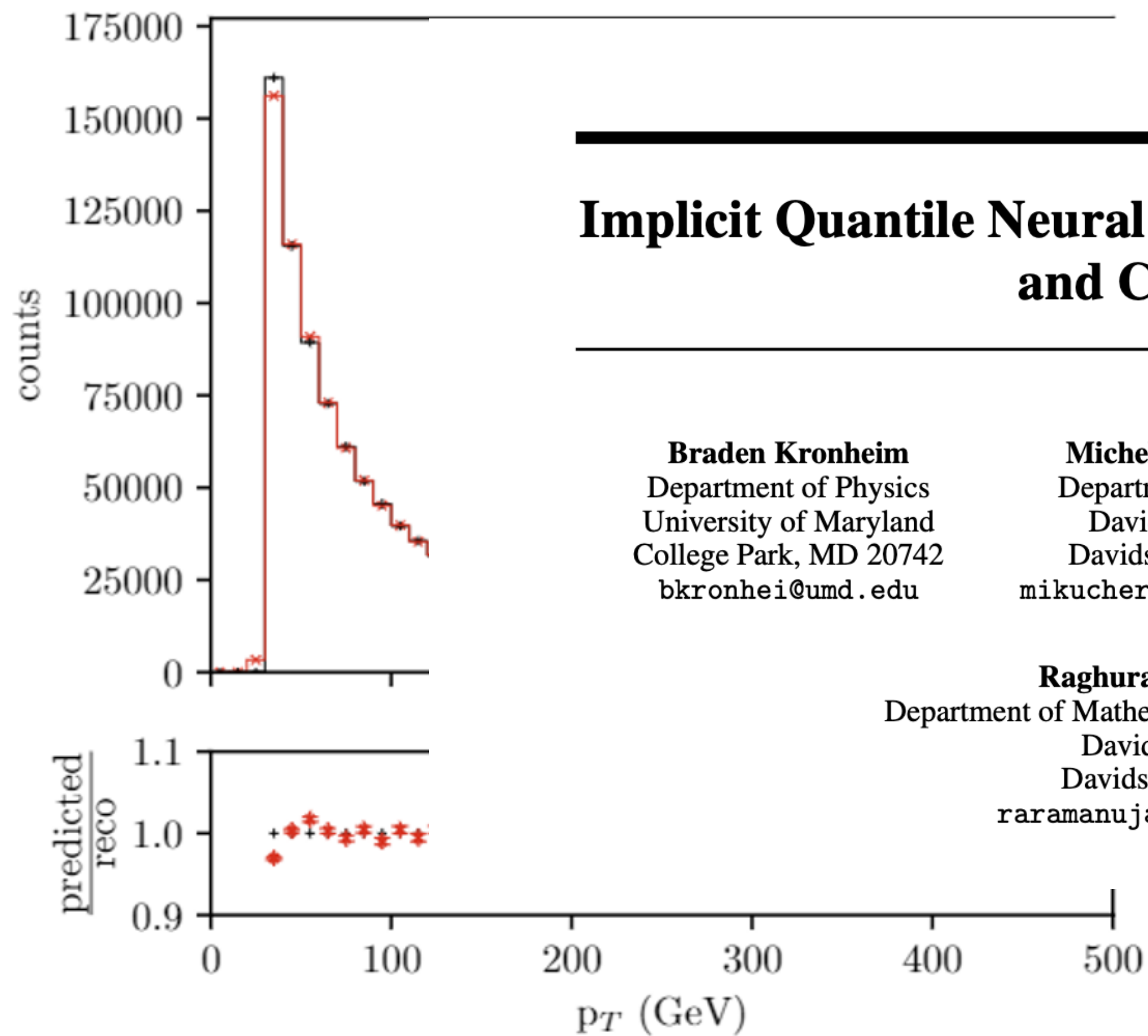
EVEN
GENERA



RECO
JETS

jet simulation

RESULTS JET SIMULATION



Implicit Quantile Neural Networks for Jet Simulation and Correction

Braden Kronheim
Department of Physics
University of Maryland
College Park, MD 20742
bkronhei@umd.edu

Michelle P. Kuchera
Department of Physics
Davidson College
Davidson, NC 28035
mikuchera@davidson.edu

Harrison B. Prosper
Department of Physics
Florida State University
Tallahassee, FL 32306
hprosper@fsu.edu

Raghuram Ramanujan
Department of Mathematics & Computer Science
Davidson College
Davidson, NC 28035
raramanujan@davidson.edu



EVEN
GENERA

RECO
JETS

jet simulation