Infinite variance of U.S. COVID-19 cases and deaths, and Taylor's law of heavy-tailed data

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Over the last century, ecologists, statisticians, physicists, financial quants, and others discovered, in many sets of samples of nonnegative quantities, such as population sizes or stock prices, that the sample variance approximates a power of the sample mean. This power-law relationship of variance to mean is known as a power variance function in statistics, as Taylor's law in ecology, and as fluctuation scaling in physics and financial mathematics. This survey talk will emphasize ideas, motivations, recent theoretical results, applications, and practical implications rather than proofs. Many models of Taylor's law assume the probability distribution underlying each sample has finite mean and variance. Recently, colleagues and I generalized Taylor's law to samples from probability distributions with infinite mean or infinite variance. For such heavy-tailed distributions, we extended Taylor's law to higher moments than the mean and variance and to measures of upside and downside portfolio risk. U.S. COVID-19 cases and deaths illustrate Taylor's law with finite means and infinite variances. This finding has practical implications. Collaborators in this work are Mark Brown, Richard A. Davis, Victor de la Peña, Gennady Samorodnitsky, Chuan-Fa Tang, and Sheung Chi Phillip Yam.

References

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