

Ionosphere Scintillations at low and high latitudes Observations and Modelling



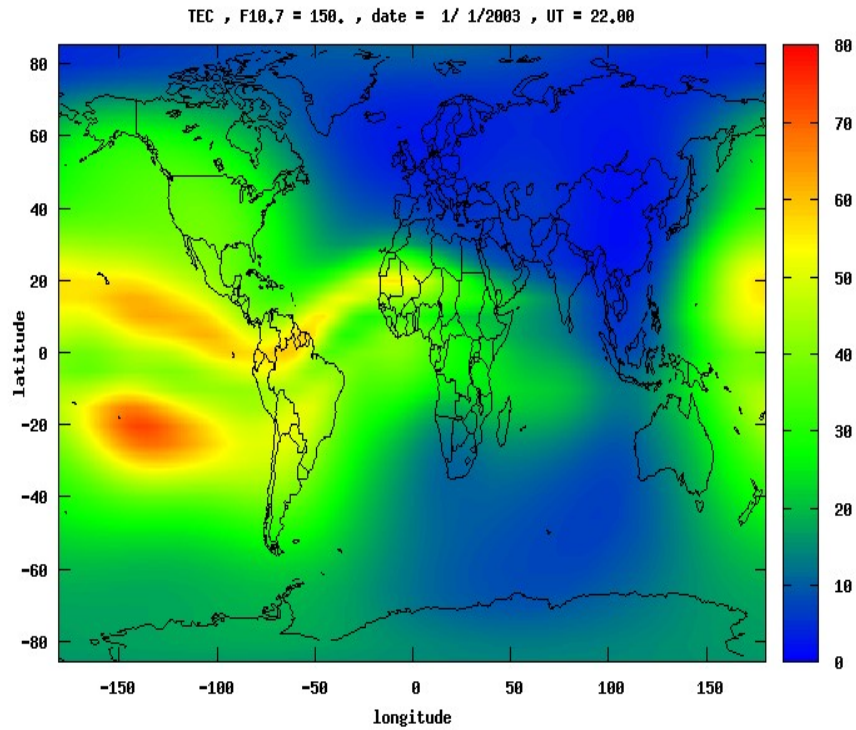
**ESA Monitor network of
receivers**

Y. Béniguel
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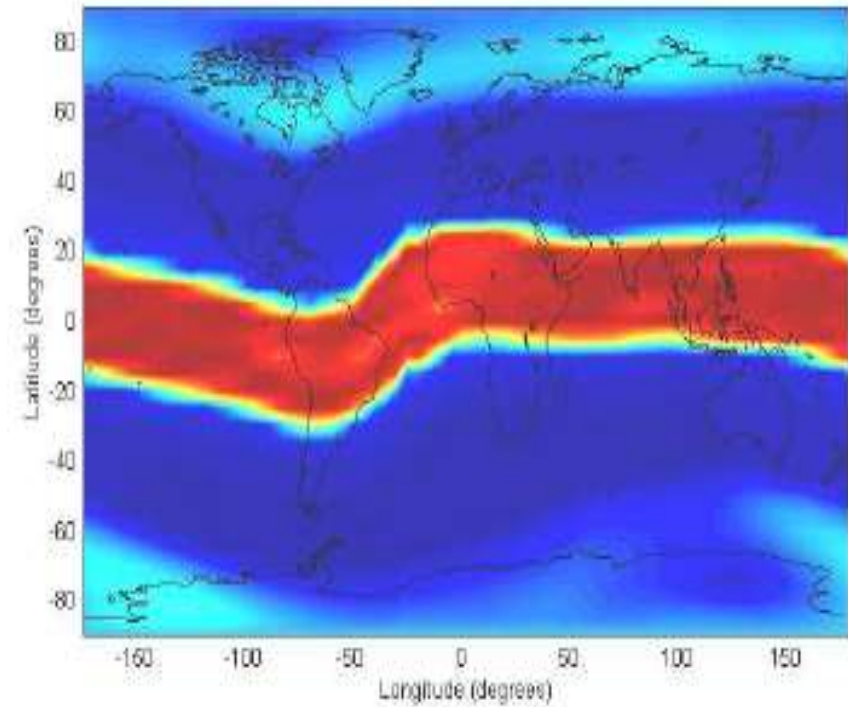
Contents

- **Low Latitudes**
 - Occurrence and probabilities
 - Raw data analysis
- **High Latitudes**
 - Scintillation occurrence dependencies
- **Modelling**
 - GISM
- **Extreme Events**
 - EGNOS

Ionosphere Variability



TEC Map

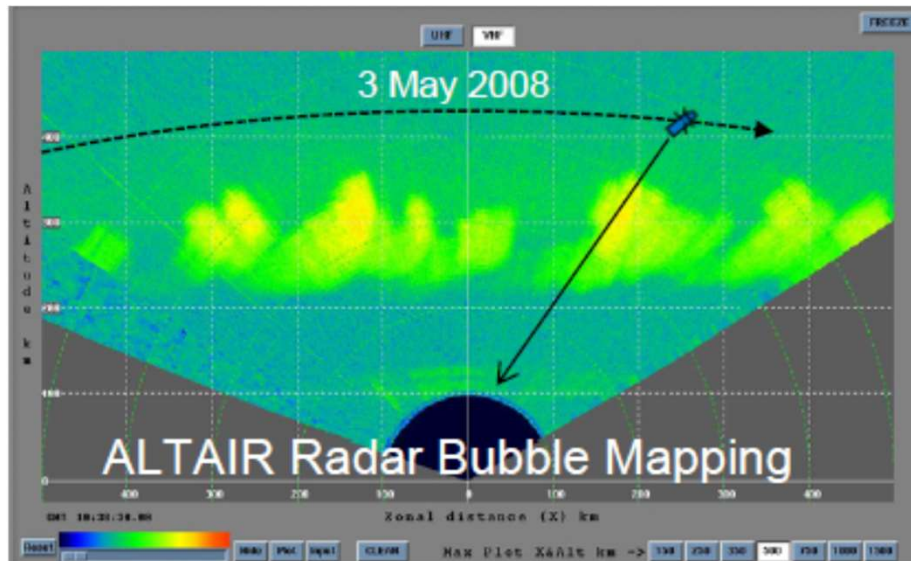


**Location of turbulences
(cumulative map)**

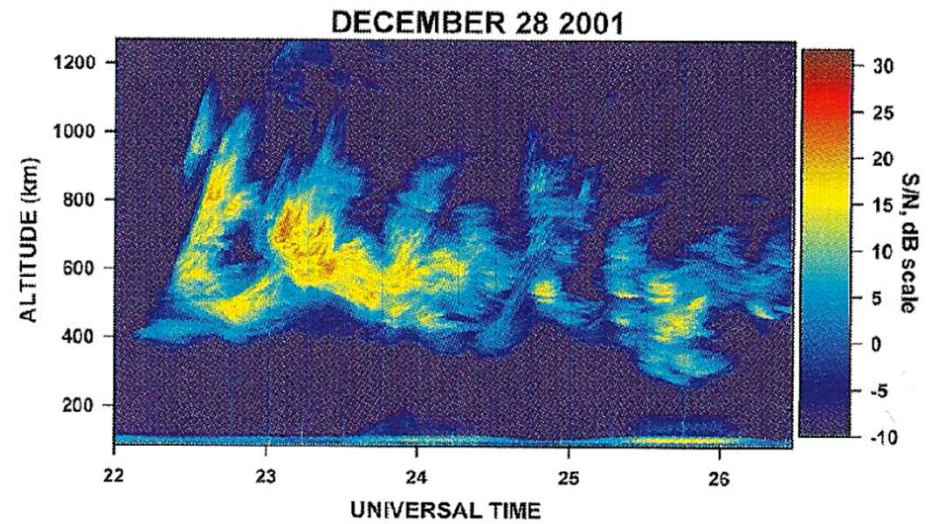
Section 1

Turbulent Ionosphere The Low Latitudes

Medium Radar Observations



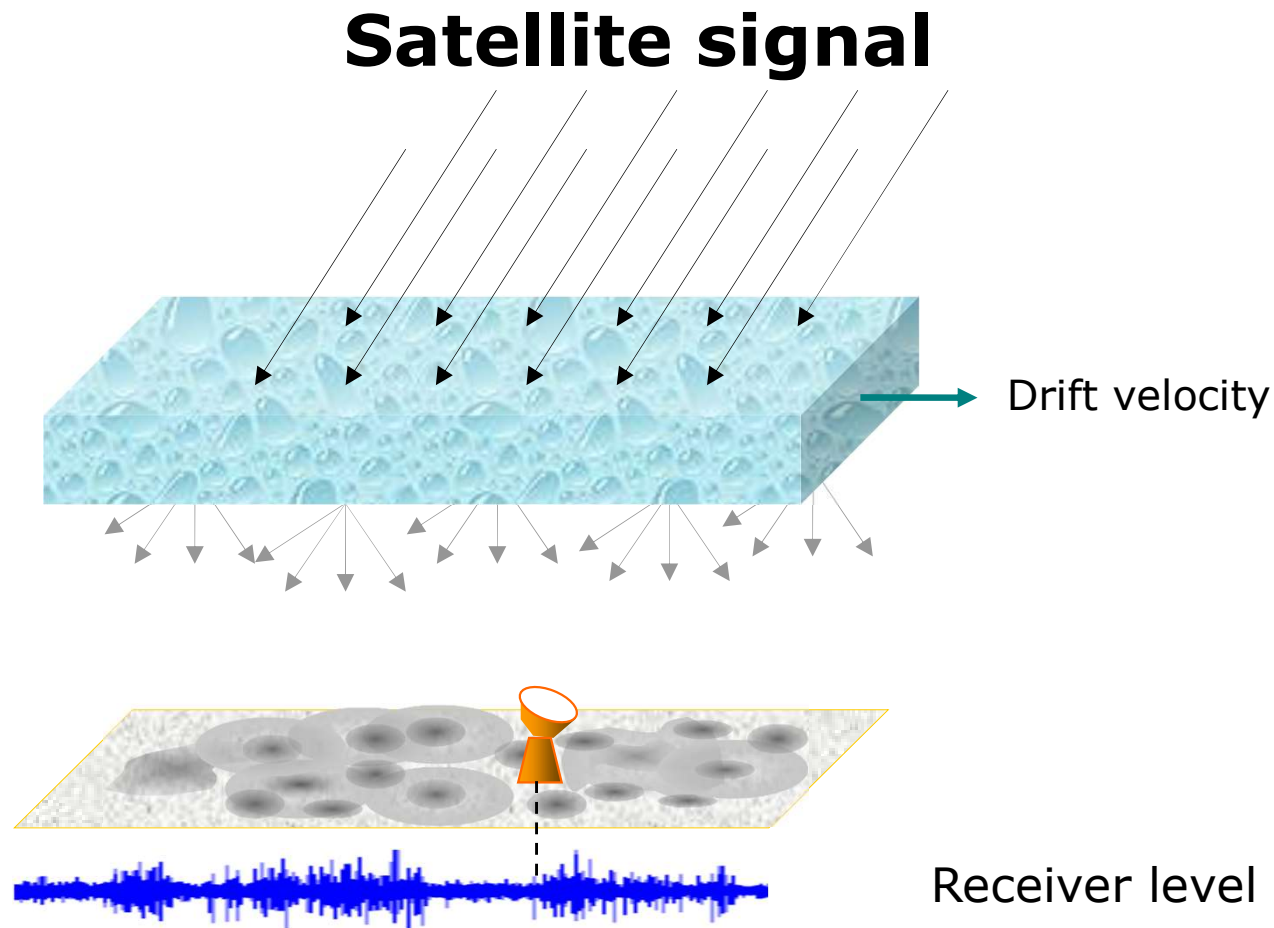
Observations at Kwajalen Islands
Courtesy K. Groves, BC



Observations in Brazil
Courtesy E. de Paula, INPE

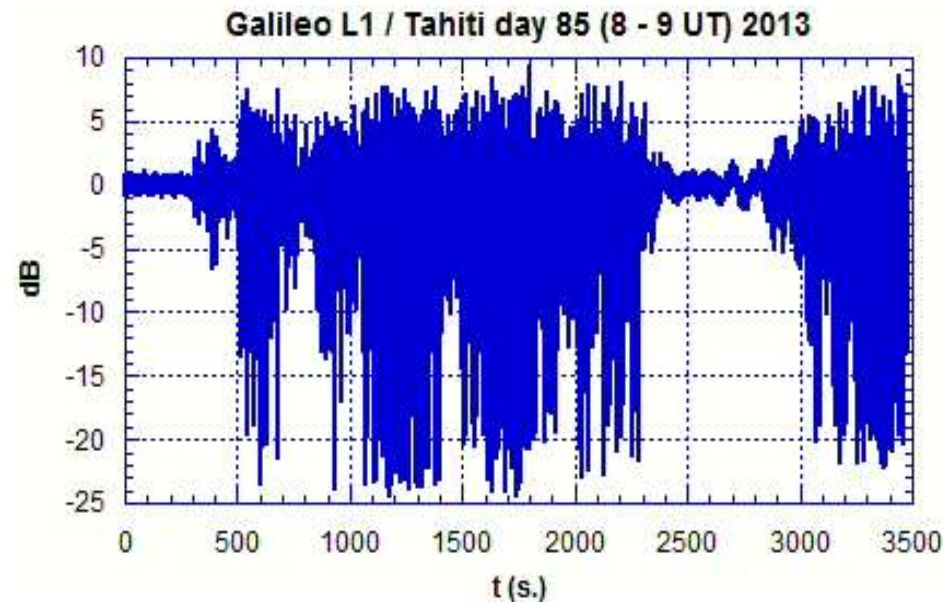
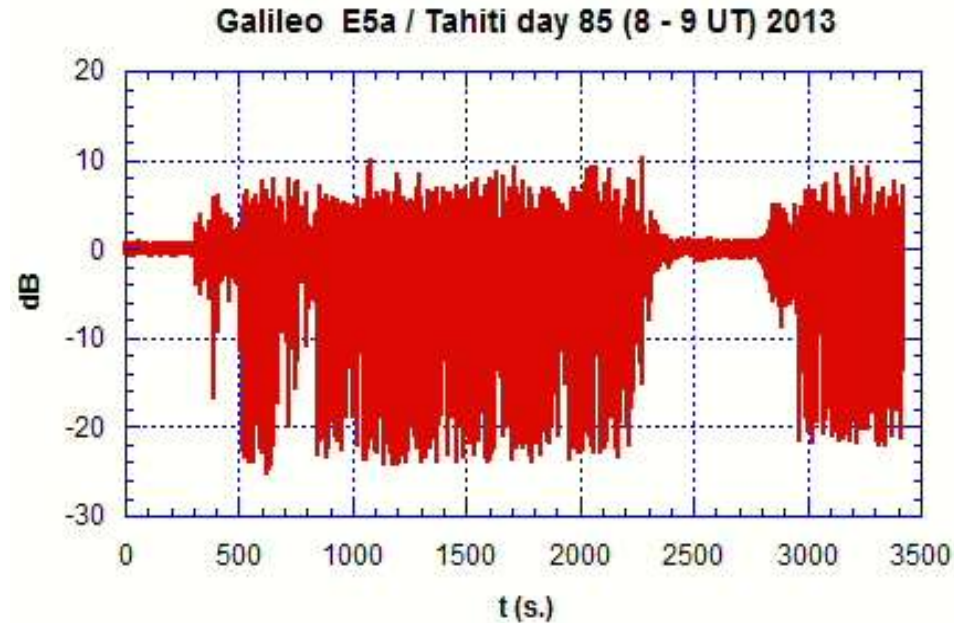
The vertical extent may reach hundreds of kilometers

Physical Mechanism



The scattering pattern changes rapidly in time and space creating fast fluctuations (scintillations) at receiver level

Scintillation on Galileo Satellites L1 vs E5a



Characterisation of Signal Fluctuations

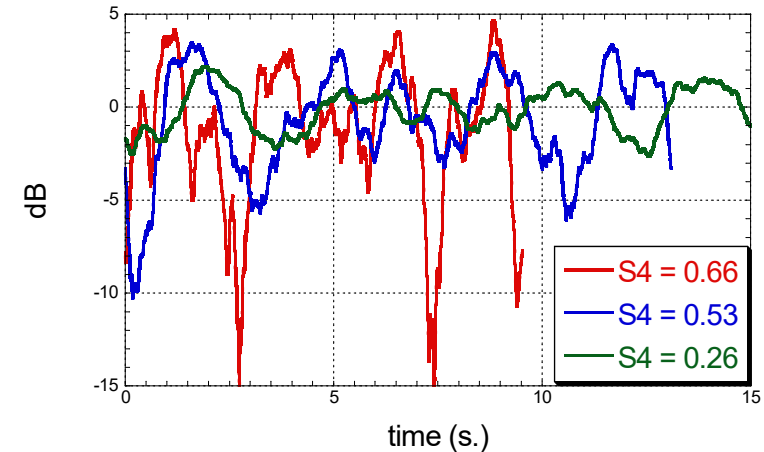
Indices Definition

$$S_4^2 = \frac{\langle I^2 \rangle - \langle I \rangle^2}{\langle I \rangle^2} \quad \text{with} \quad I = |E|^2$$

$$\sigma_\Phi^2 = \langle \Phi^2 \rangle - \langle \Phi \rangle^2$$

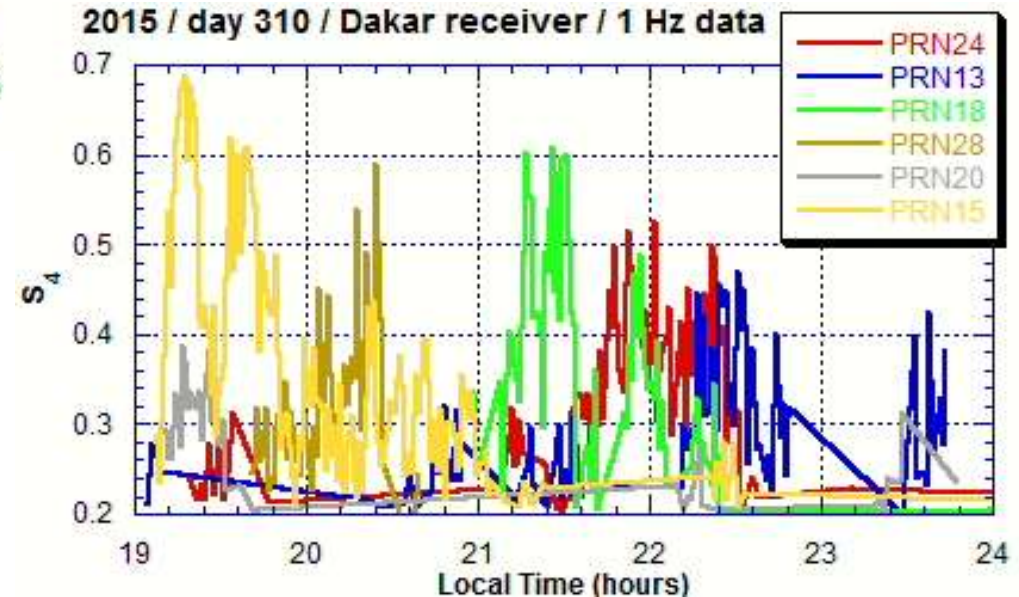
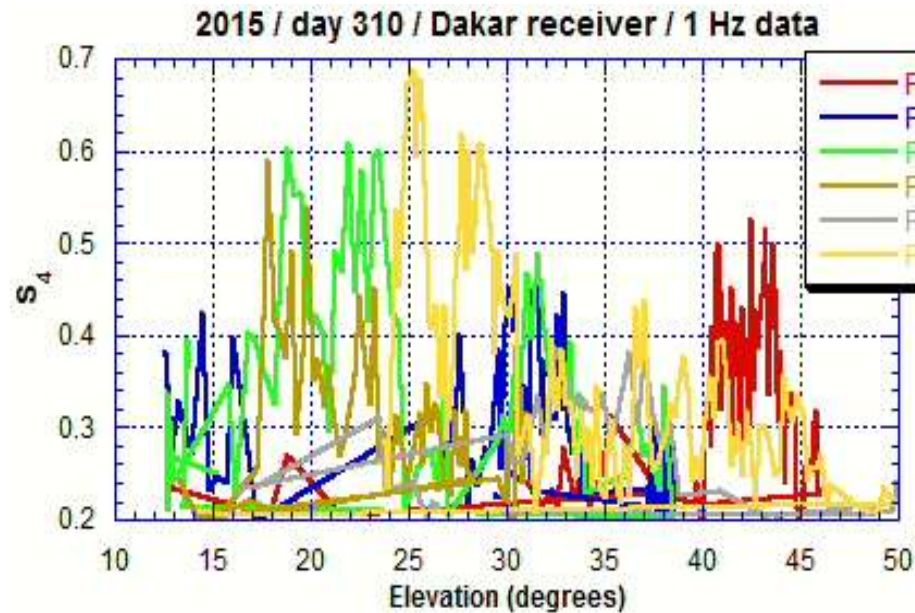
$$\text{ROTI} = \left\langle \left(\frac{\partial \text{TEC}}{\partial t} \right)^2 \right\rangle - \left\langle \frac{\partial \text{TEC}}{\partial t} \right\rangle^2$$

➤ **Decorrelation time**



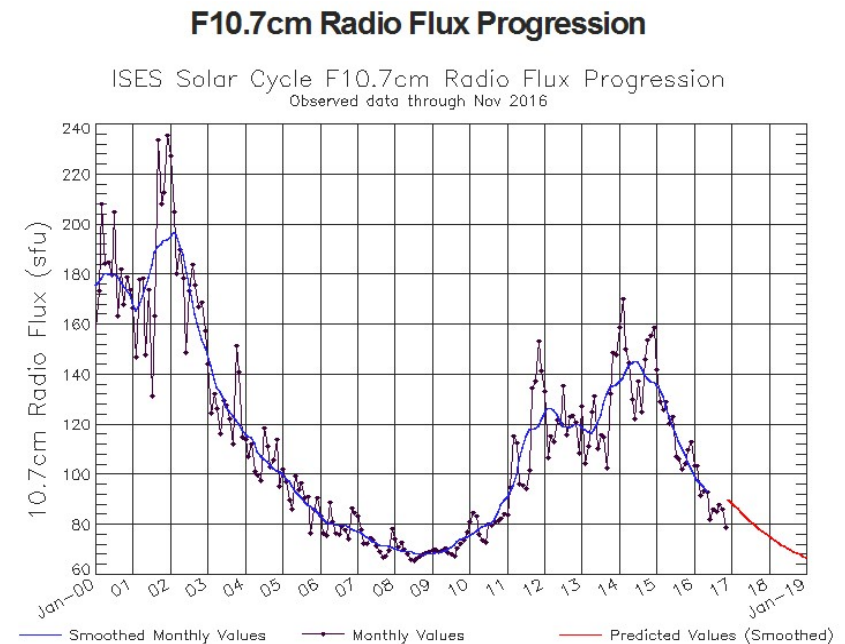
$$0 < S_4 < 1$$

Example: one Day of Scintillation Occurrence Dependency on Local Time and on the Elevation Angle



ESA Measurement Campaigns

- Prediction of Ionospheric scintillations (PRIS) (2006 – 2008) *
- MONitoring of Ionosphere by innovative Techniques coordinated Observations and Resources (MONITOR) (2010– 2014) *
- MONITOR 2 (2014 – 2018) *
- e-MONITOR (2020 –) **



* IEEA + DLR, UPC, QINETIQ, ICTP, TAS, FMI, UWM, ...

** DLR + IEEA, UPC, ICTP, NLR, Airbus DE

MONITOR Scintillations Receivers Network

MONITOR Content

- Introduction
- Project partners
- Documentation
- Stations map - data
- Stations map - products
- Search input data
- Search products
- Data policy
- Contact

STATIONS MAP - DATA TYPES



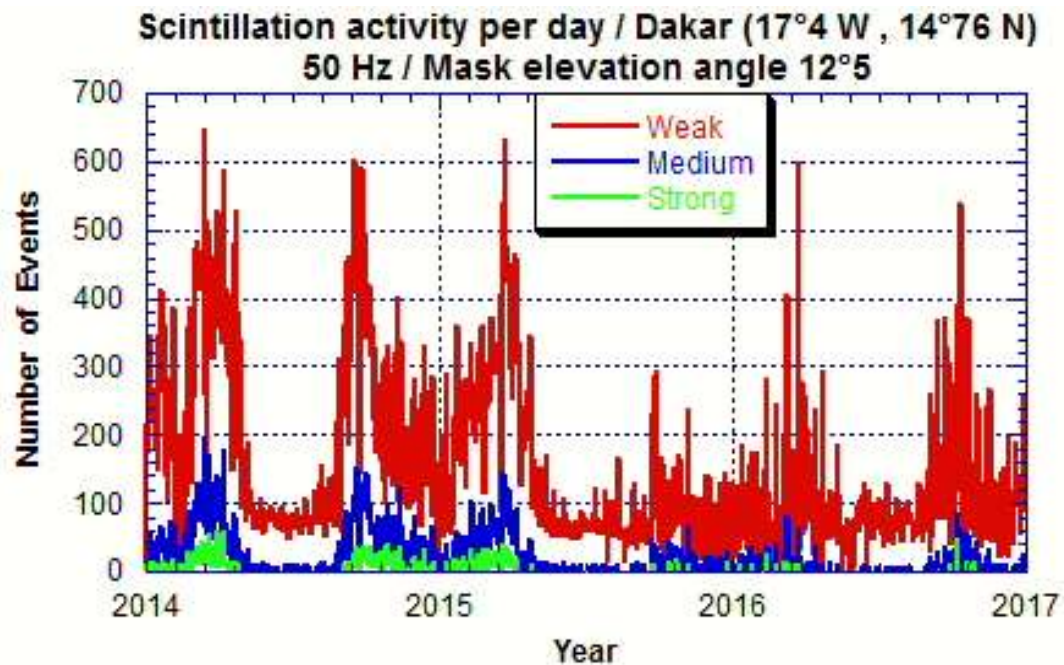
Station Name	Project Operating Period	Latitude	Longitude	Equipment	Sampling frequency
Tahiti (French Polynesia)	Monitor 1 09/2012 – 09/2014	17.55° S	210.39° E	PolaRxS	50 Hz
Lima (Peru)	Monitor 1 09/2011 – 11/2016	12.18° S	282.58° E	GSV4004B	50 Hz
Cayenne (French Guyana)	Monitor 1 05/2006 – 04/2016	4.8° N	307.63° E	GSV4004B	50 Hz
Cape Verde	Monitor 1 12/2012 – 09/2015	16.73° N	337.07° E	GSV4004B + GISMO	50 Hz
Malindi (Kenya)	Monitor 1 04/2013 – 12/2013	3. ° S	40.72° E	PolaRxS	50 Hz
Sodankylä (Finland)	Monitor 1 11/2011 -	67.25° N	26.36° E	GSV4004B	50 Hz
Kevo (Finland)	Monitor 1 03/2013 -	69.75°N	27.019° E	GSV4004B	50 Hz
Dakar (Senegal)	SAGAIE	14.765° N	342.62° E	PolaRxS + Novatel FlexPack 6	50 Hz / 1 Hz
Ouagadougou (Burkina Fasso)	SAGAIE	12.368° N	358.47° E	Novatel FlexPack 6	1 Hz
Lomé (Togo)	SAGAIE	6.132° N	1.223° E	PolaRxS + Novatel FlexPack 6	50 Hz / 1 Hz
Douala (Cameroon)	SAGAIE	4.049° N	9.699° E	Novatel FlexPack 6	1 Hz
N'Djamena (Chad)	SAGAIE	12.113° N	15.048° E	Novatel FlexPack 6	1 Hz
Abidjan (Ivory Coast)	Monitor 2 05/2015 -	5.27° N	356.08 E	PolaRxS	50 Hz
Cotonou (Benin)	Monitor 2 07/2015 -	6.352° N	2°383 E	PolaRxS	50 Hz
Niamtogou (Togo)	Monitor 2 07/2015 -	9.774° N	1.098° E	PolaRxS	50 Hz
Bamako (Mali)	Monitor 2 07/2015 -	12.540° N	7.949 W	PolaRxS	50 Hz
Bahir Dar (Ethiopia)	Monitor 2 07/2014 -	11.598° N	37°396° E	GSV4004B	50 Hz
Kiruna (Sweden)	Monitor 2 04/2015 -	67.743° N	21.06° E	PolaRxS	50 Hz

Low Latitudes Receivers Network

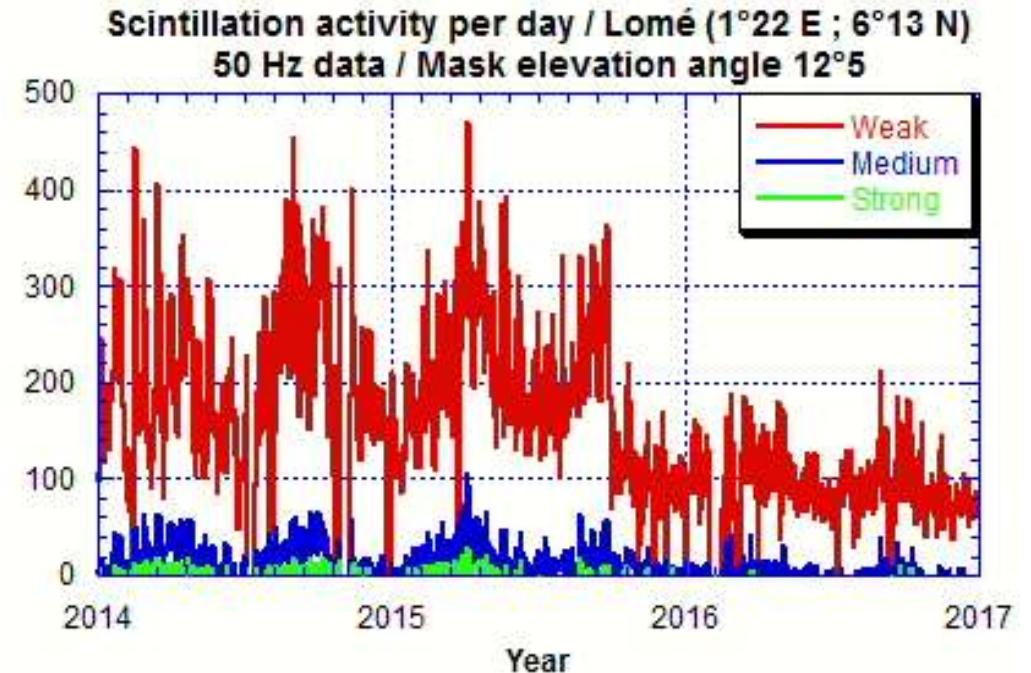


Station Name	Project	Latitude	Longitude	Equipment	Sampling frequency
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Cotonou (Benin)	Monitor 2	6.352° N	2°383 E	PolarXs	50 Hz
Niamtougou (Togo)	Monitor 2	9.774° N	1.098° E	PolarXs	50 Hz
Bamako (Mali)	Monitor 2	12.540° N	7.949 W	PolarXs	50 Hz

Number of Events (> 1 mn) Northern Hemisphere vs Southern Hemisphere



North hemisphere
wrt magnetic equator



South hemisphere
wrt magnetic equator

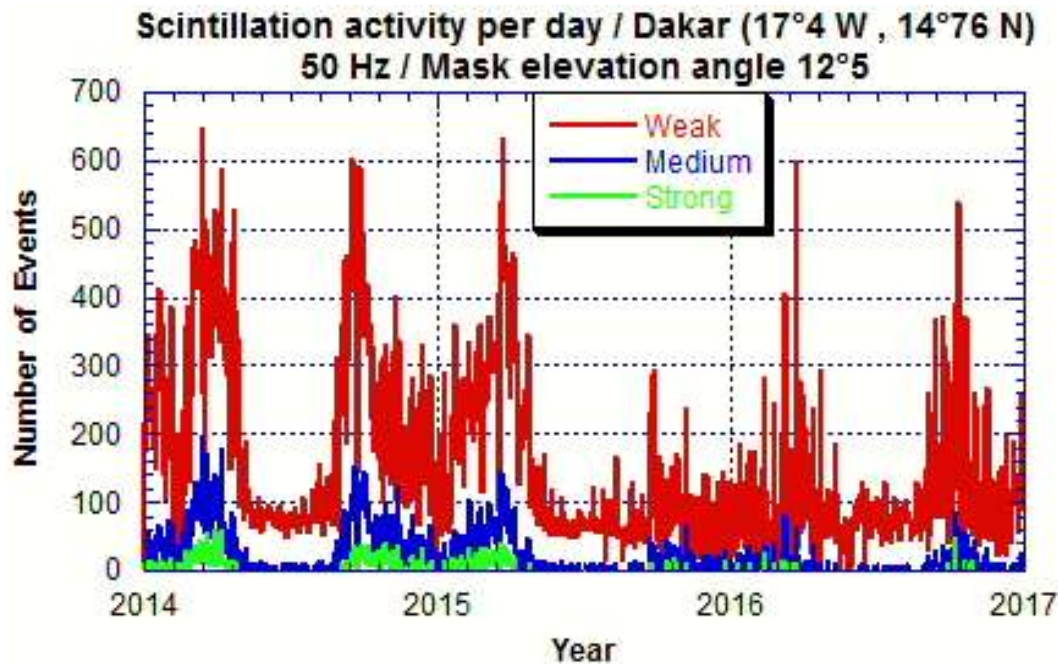
weak : $0.2 < S4 < 0.4$

medium : $0.4 < S4 < 0.6$

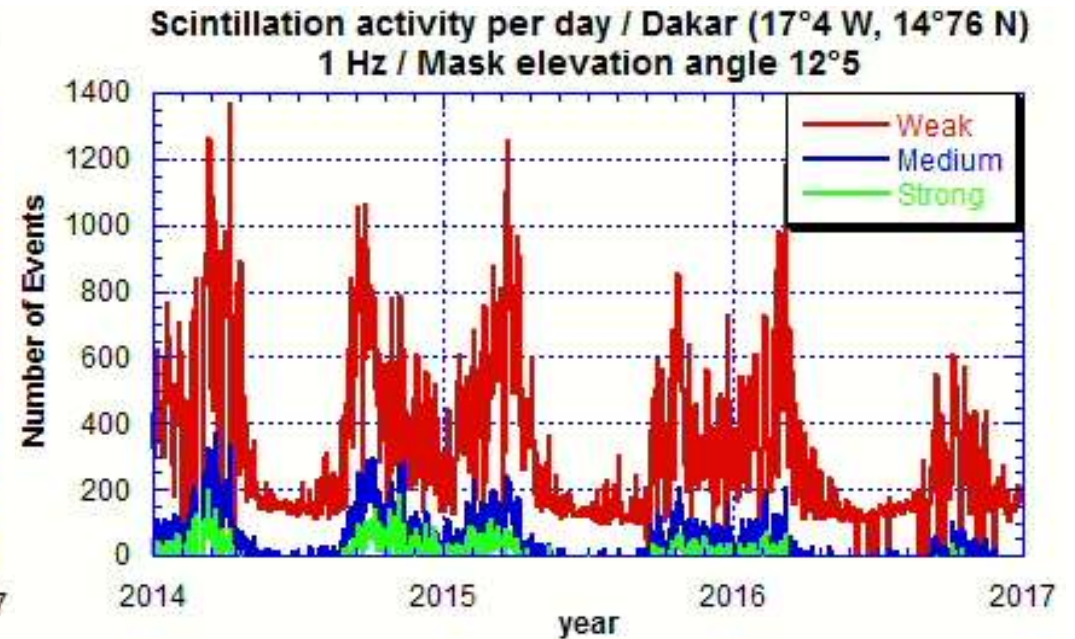
strong : $S4 > 0.6$

Number of Events (1 mn) 1 Hz vs 50 Hz

North hemisphere wrt magnetic equator



50 Hz data

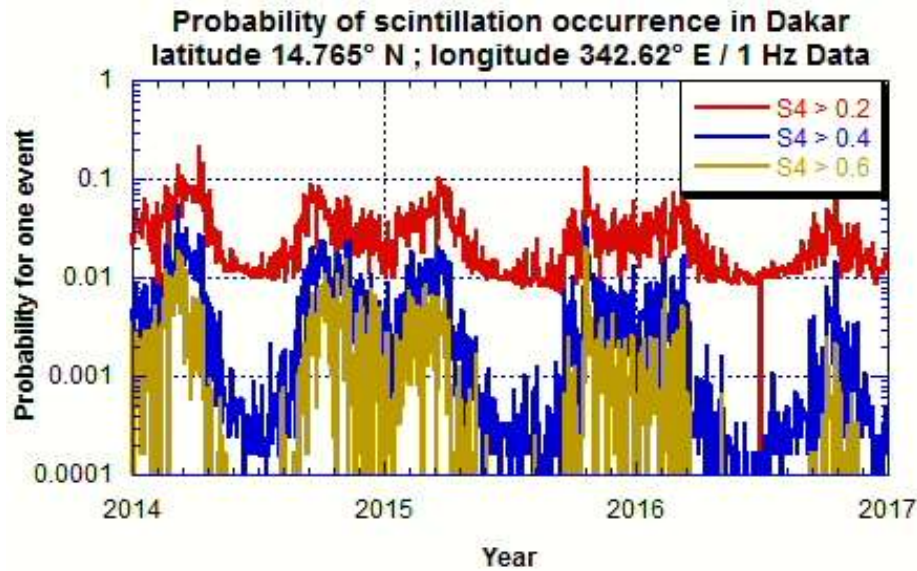


1 Hz data

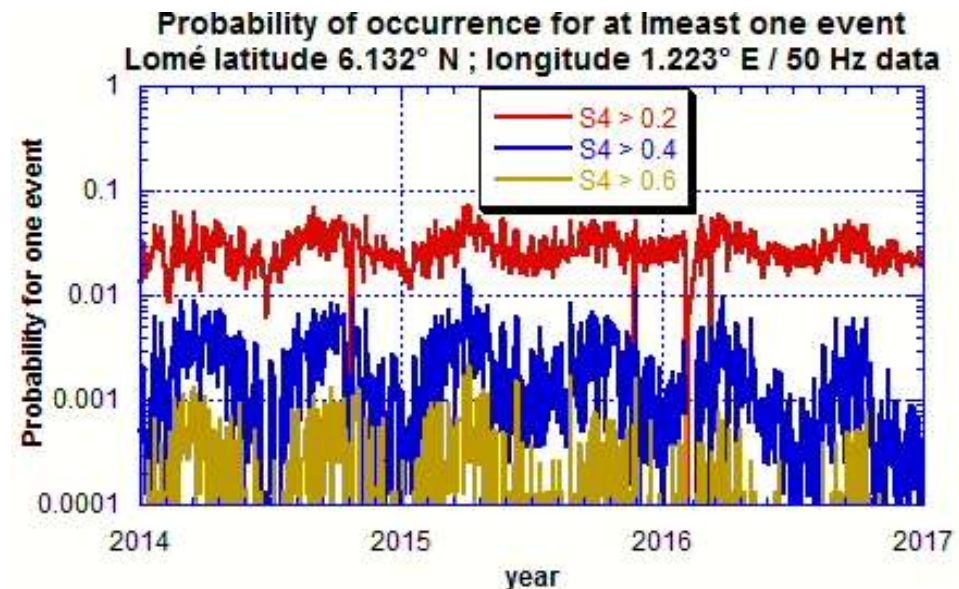
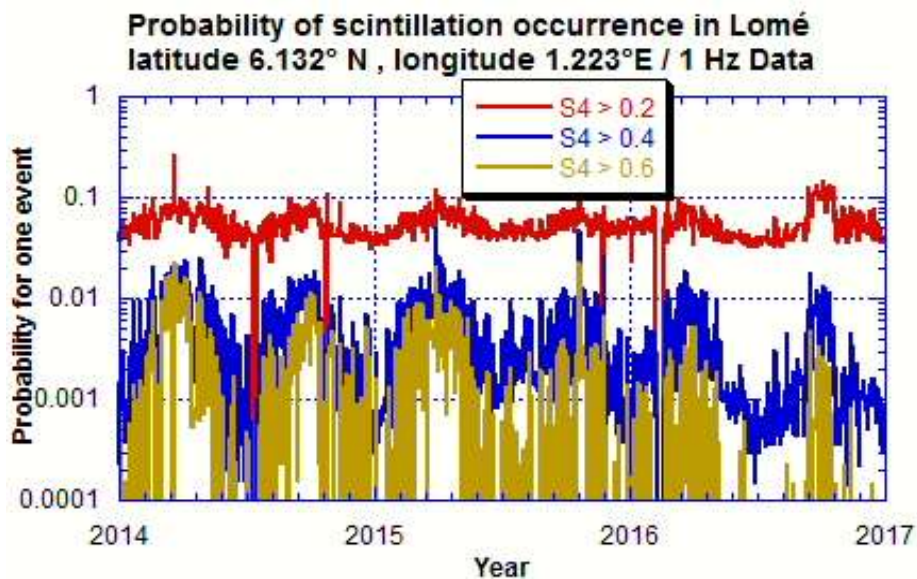
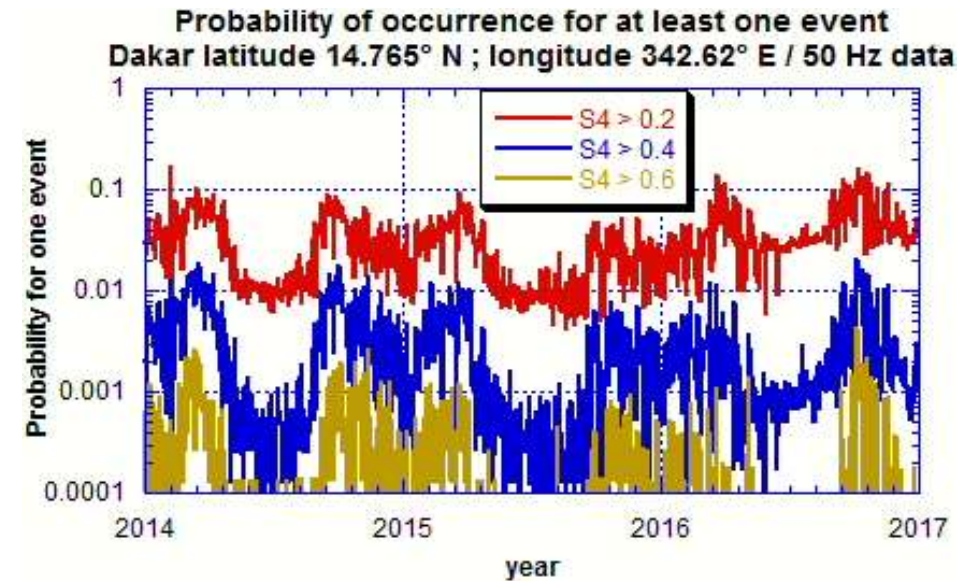
About 2 times more events

Probability of scintillation occurrence 1 Hz vs 50 Hz recording / Comparison of results

1 Hz



50 Hz

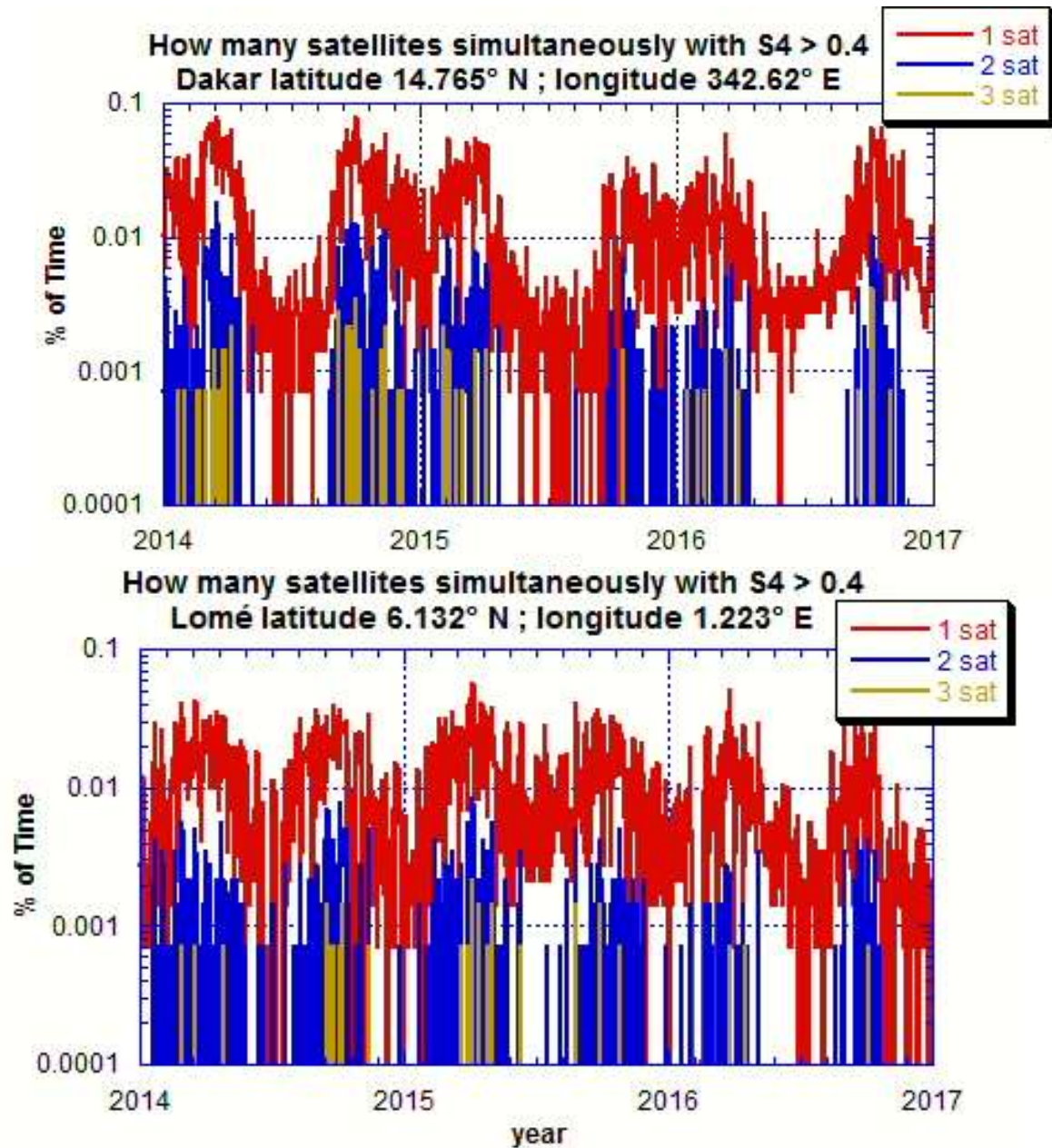


How many links simultaneously affected with scintillations

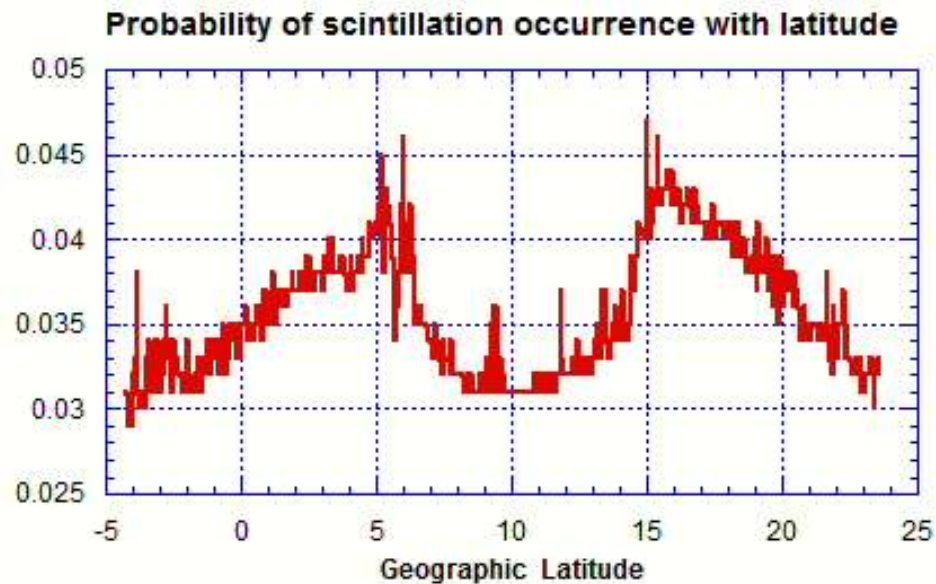
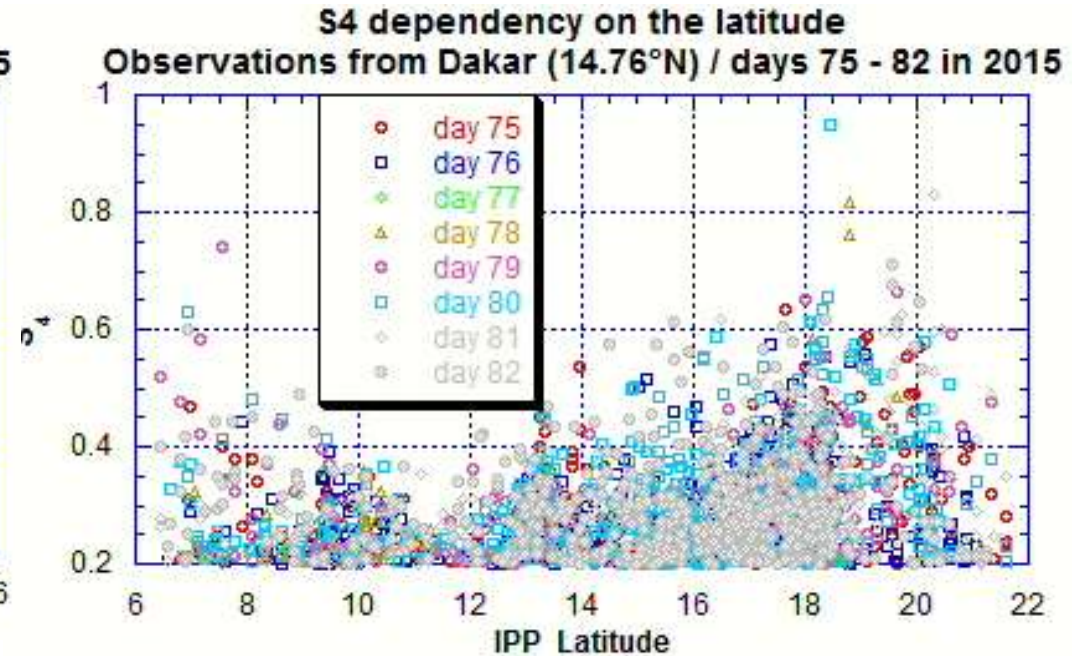
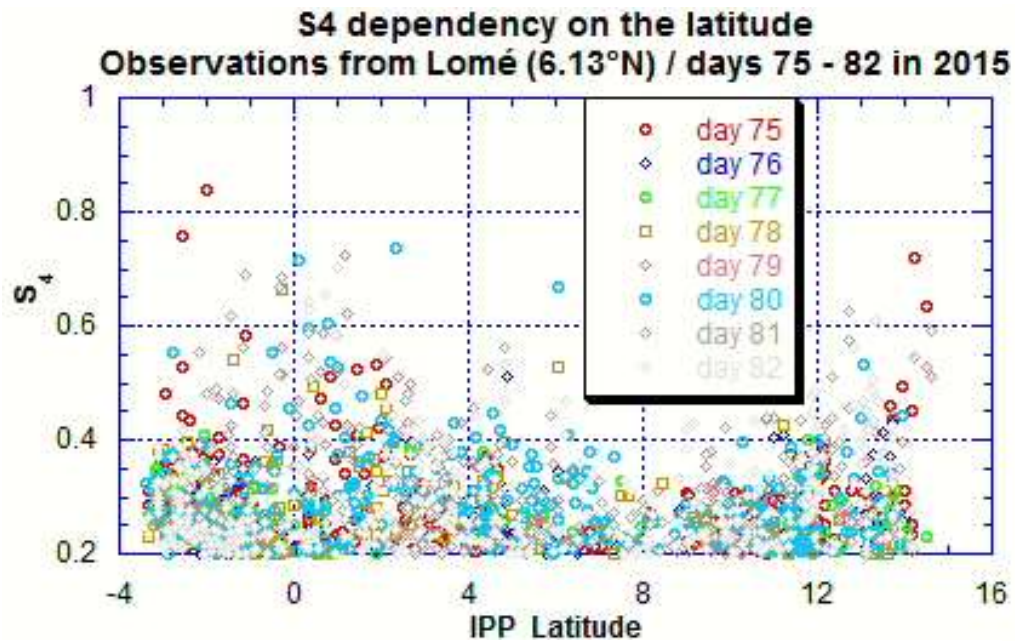
North hemisphere

50 Hz data

South hemisphere



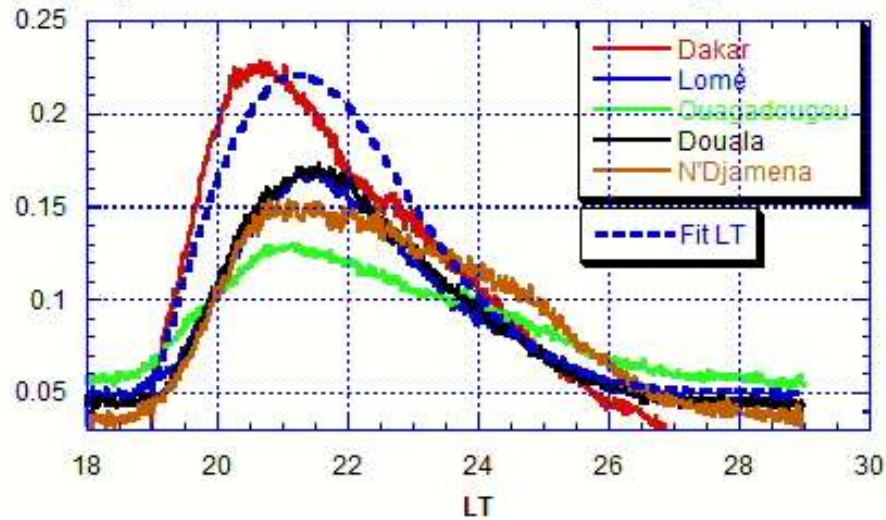
Dependency on the Latitude



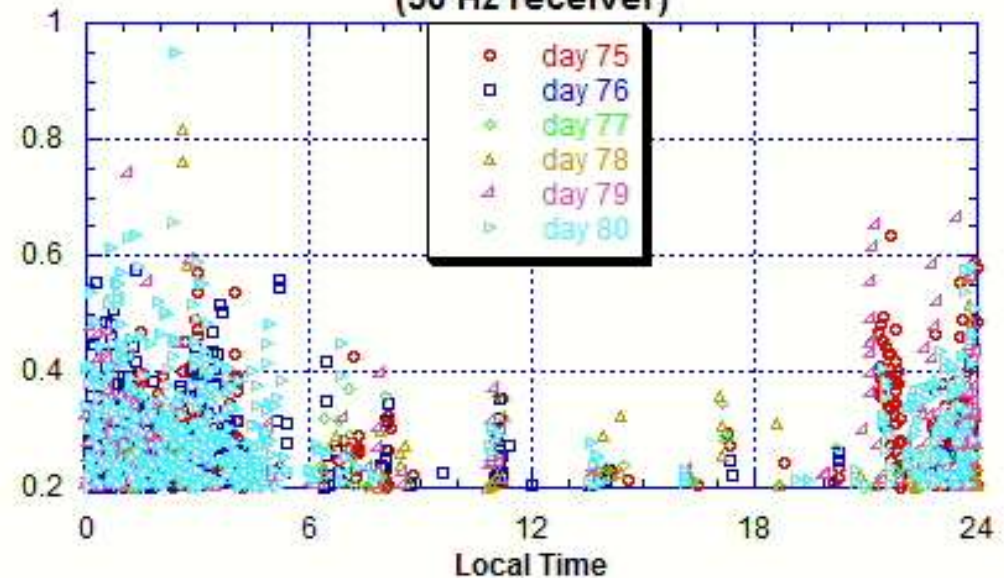
50 Hz receivers
network (3 years
of data)

Dependency on Local Time

Probability of scintillation occurrence depending on the local time



S4 measured during St Patrick storm in Dakar (50 Hz receiver)



$$f(t) = 0.05 + 0.63 \frac{t-19}{\sigma^2} \exp\left(-\frac{(t-19)^2}{2\sigma^2}\right)$$

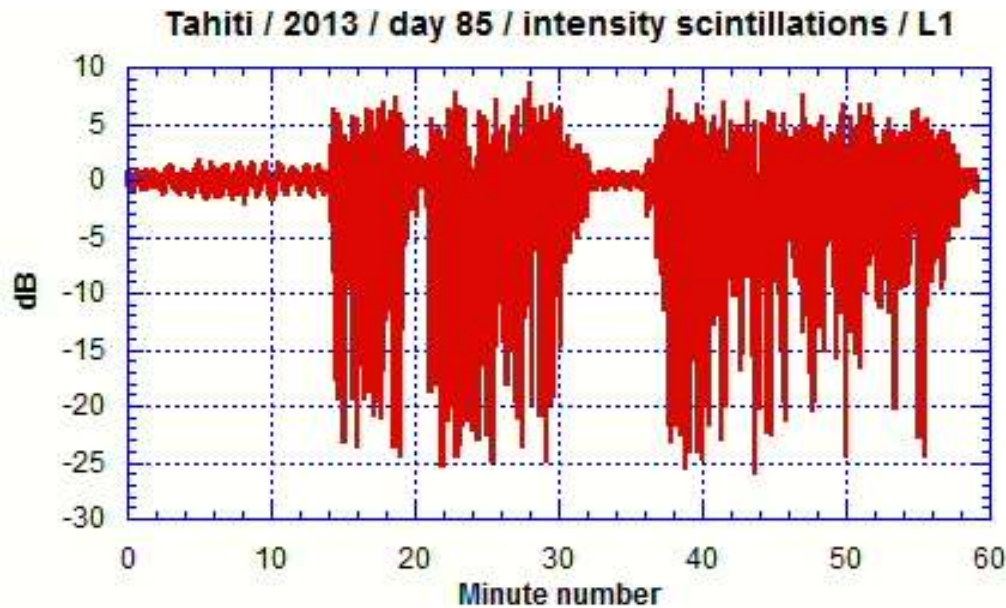
with $\sigma^2 = 5$ and t in hours

$$\int_{19 \text{ pm}}^{2 \text{ am}} f(t) dt = 0.98$$

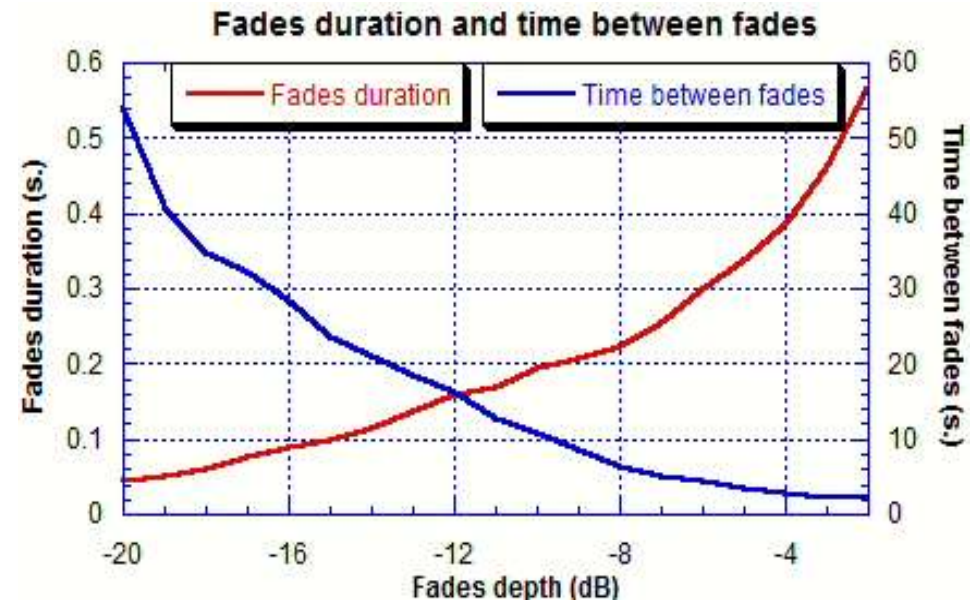
Scintillation also at day time

Raw Data Analysis

Raw Data Analysis

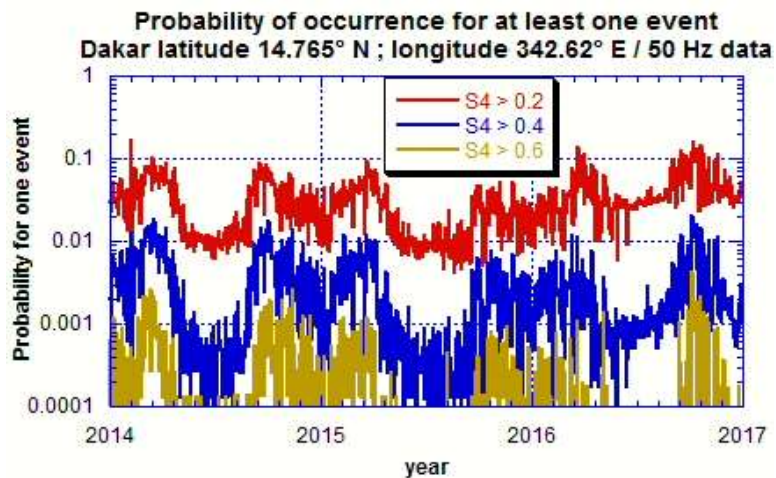
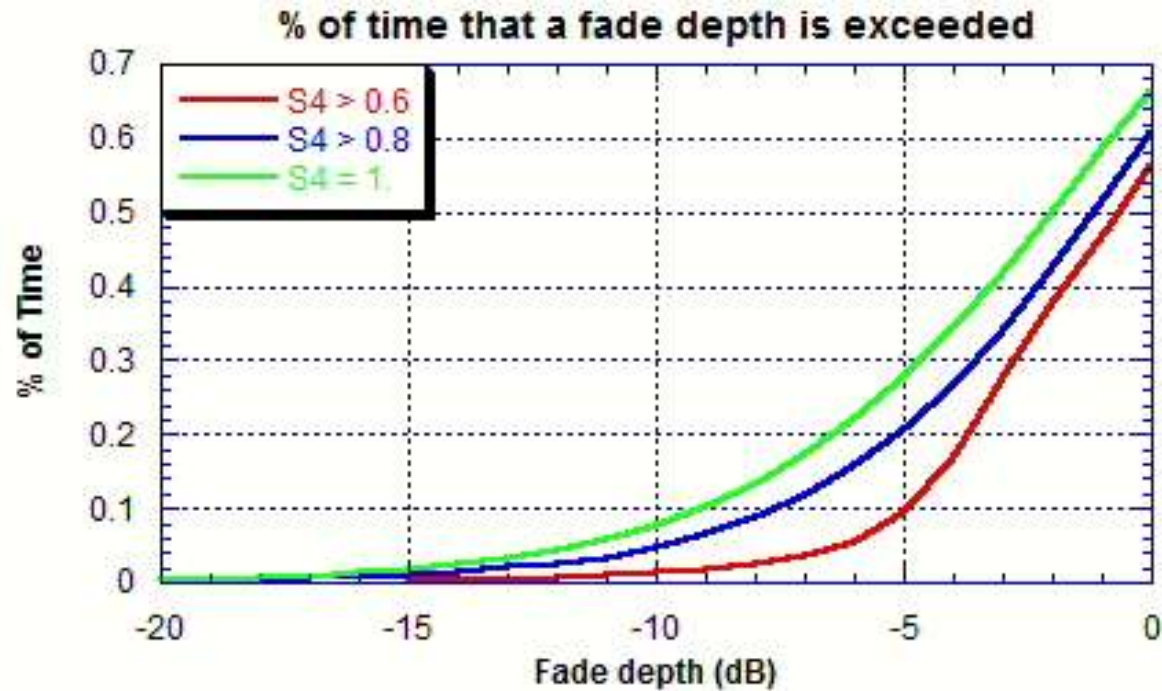


1 hour of data
at a high level of scintillations



Using all data recorded

% of time a fade depth level is exceeded



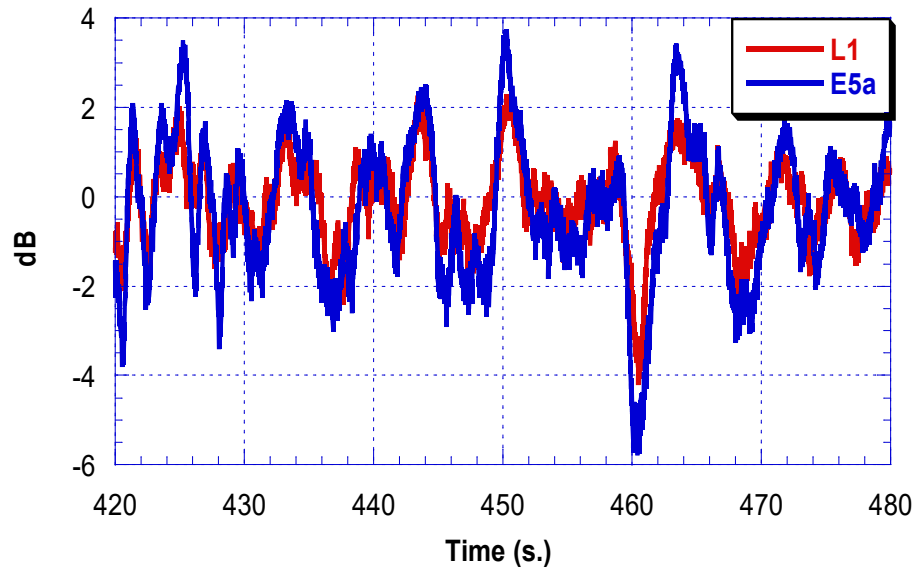
$$P = p(S4) * p(\text{Fade Depth})$$

Time Series

Frequency correlation / Observations

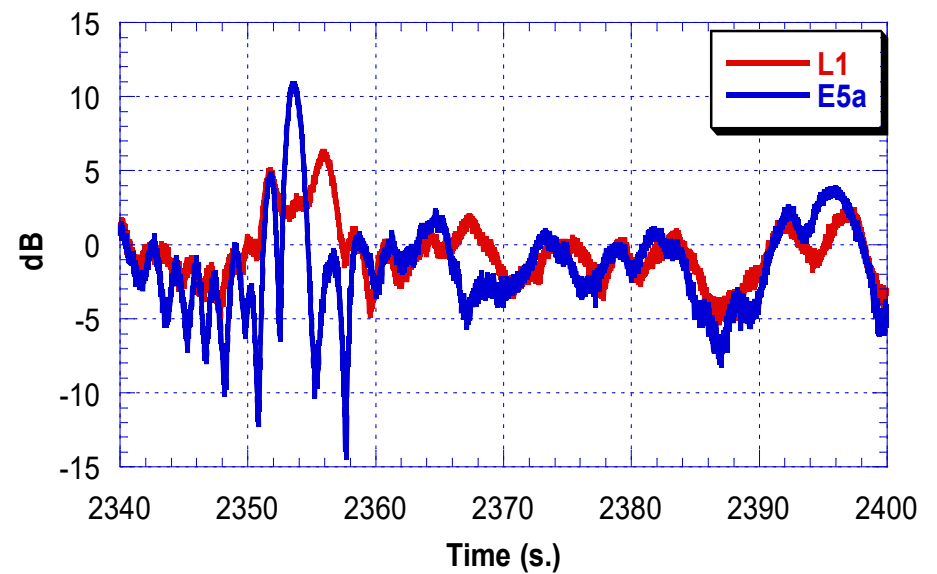
Weak scintillations vs strong scintillations

Tahiti Galileo N° 12 doy 85 / 2013
S4 (L1) = 0.21 ; S4 (E5a) = 0.36



Weak scintillations

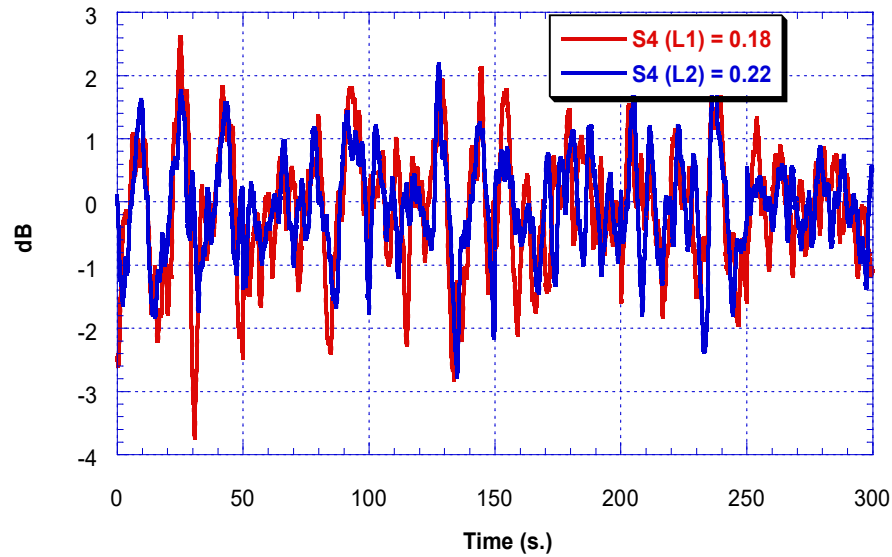
Tahiti Galileo N° 12 doy 85 / 2013
S4(L1) = 0.59 ; S4(E5a) = 1.36



Strong scintillations

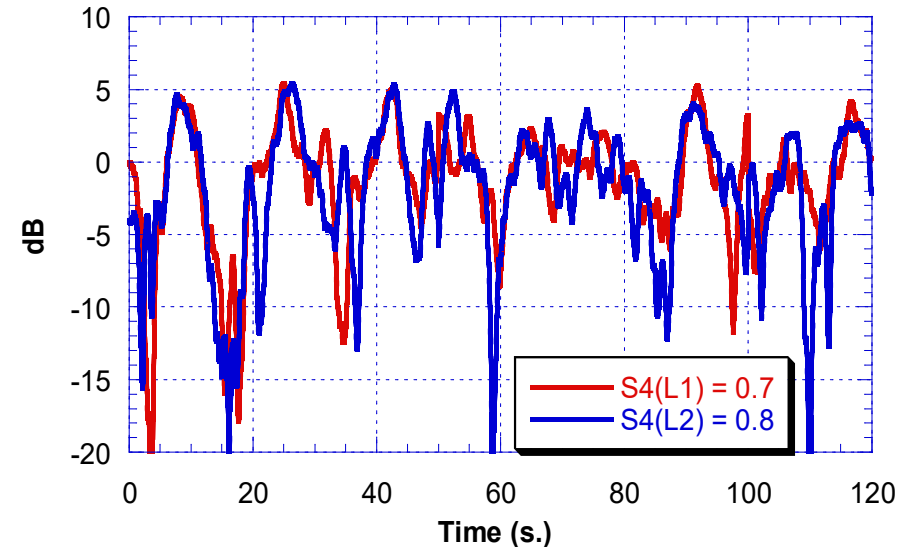
Time Series Frequency Correlation / (Modelling)

Inter Frequency Correlation



Weak scintillations

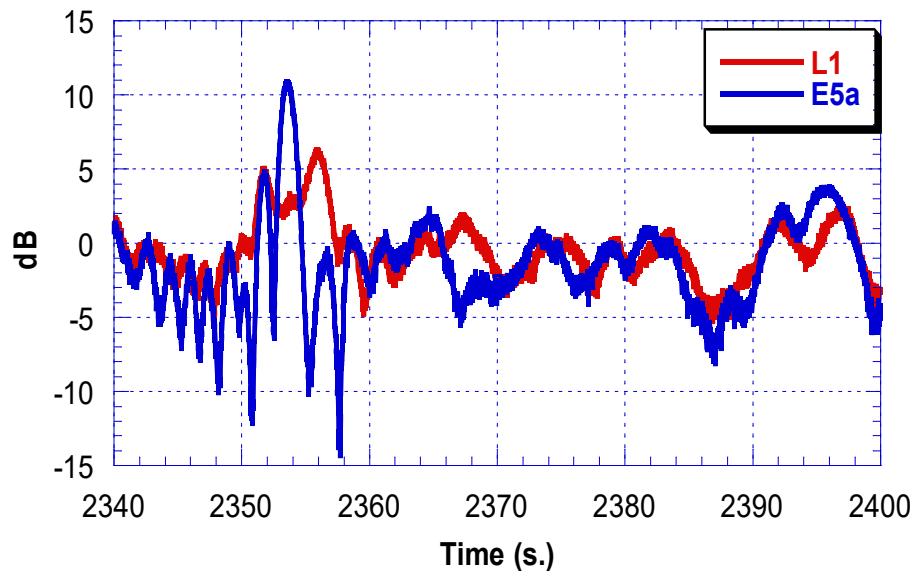
Frequency correlation predicted by GISM



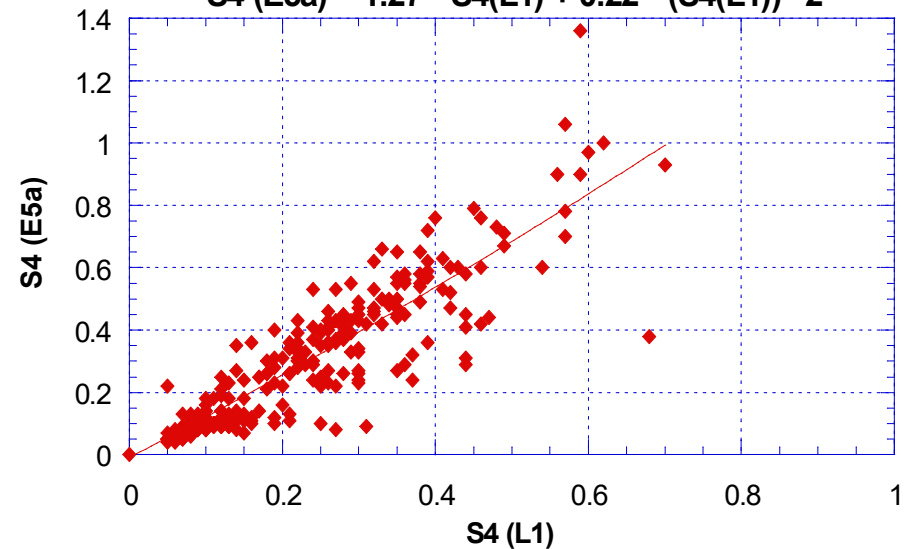
Strong scintillations

Inter Frequency Correlation

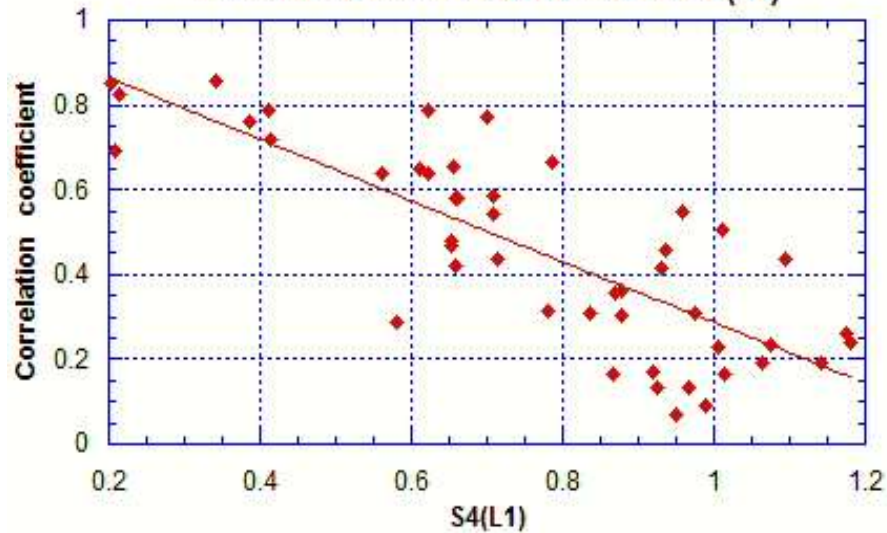
Tahiti Galileo N° 12 doy 85 / 2013
 $S4(L1) = 0.59$; $S4(E5a) = 1.36$



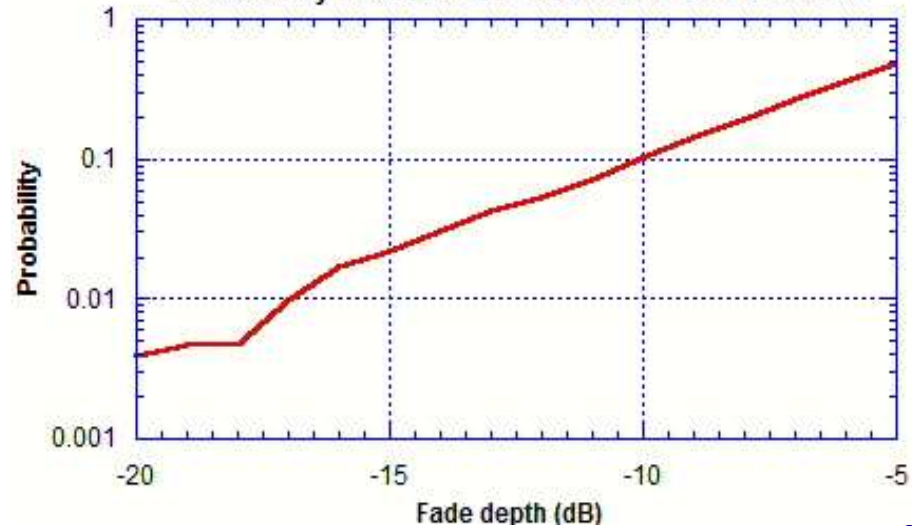
Galileo satellites
 $S4(E5a) = 1.27 * S4(L1) + 0.22 * (S4(L1))^{**2}$



Correlation coefficient L1 - L2 vs $S4(L1)$



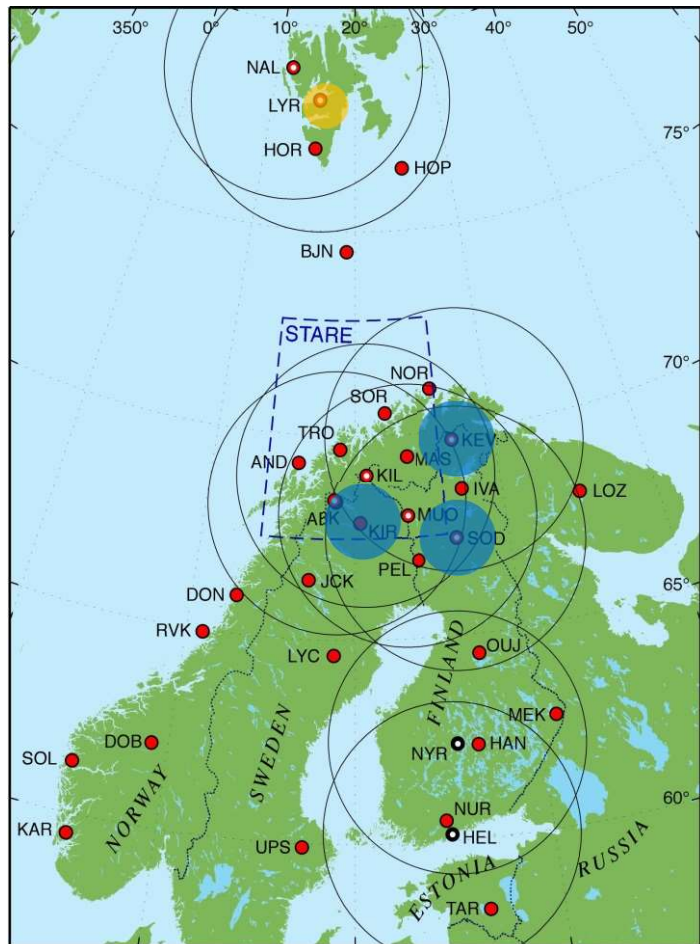
Probability of simultaneous fades on L1 and L2



Section 2

Turbulent Ionosphere The High Latitudes

High Latitude Receivers Network



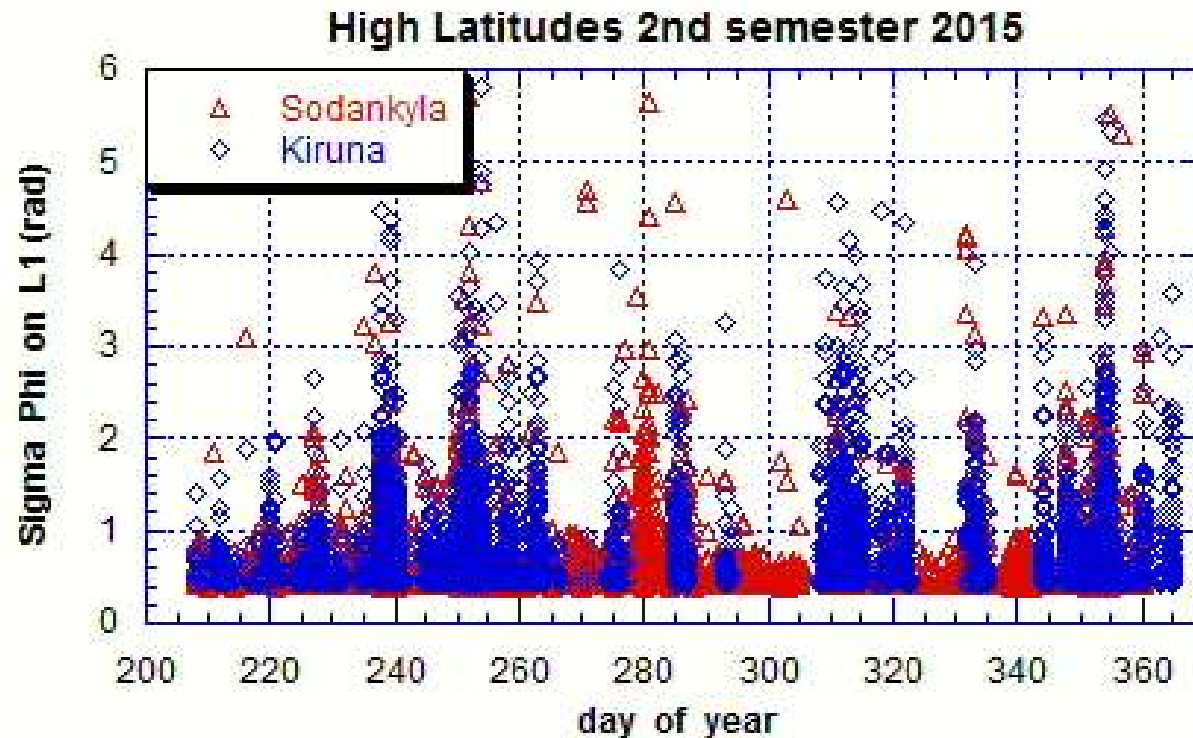
- Magnetometer
- All-sky camera
- Magnetometer and all-sky camera

February 2013

Station Name	Project	Latitude	Longitude	Equipment	Sampling frequency
Sodankylä (Finland)	Monitor	67.25° N	26.36° E	GSV4004B	50 Hz
Kevo (Finland)	Monitor	69.75°N	27.019° E	GSV4004B	50 Hz
Kiruna (Sweden)	Monitor	67.743° N	21.06° E	PolaRxS	50 Hz

MONITOR site

High Latitudes Fluctuations

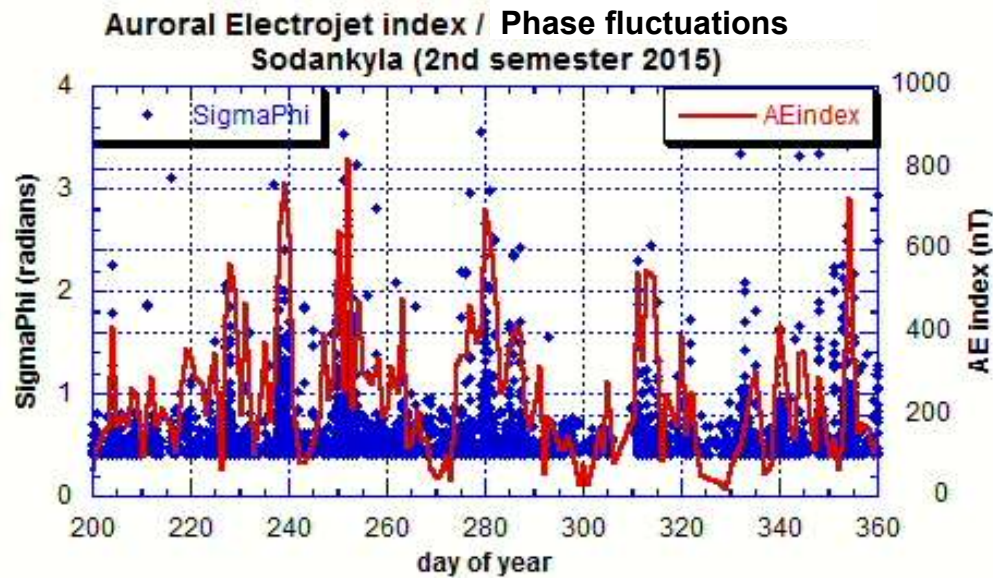


Sodankyla : Novatel GSV 4004B receiver

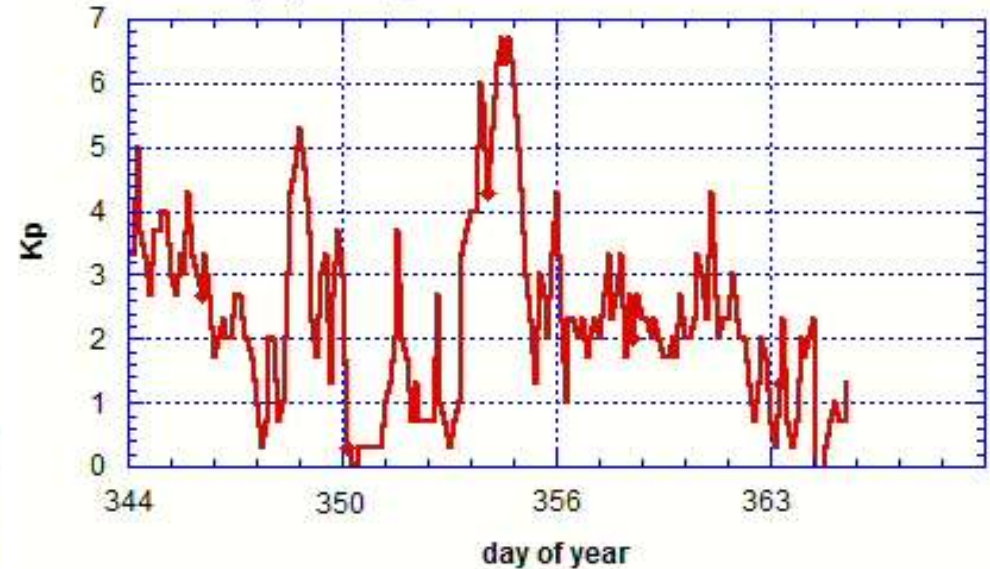
Kiruna : Septentrio PolaRxS receiver

Distance Sodankyla – Kiruna : 280 km

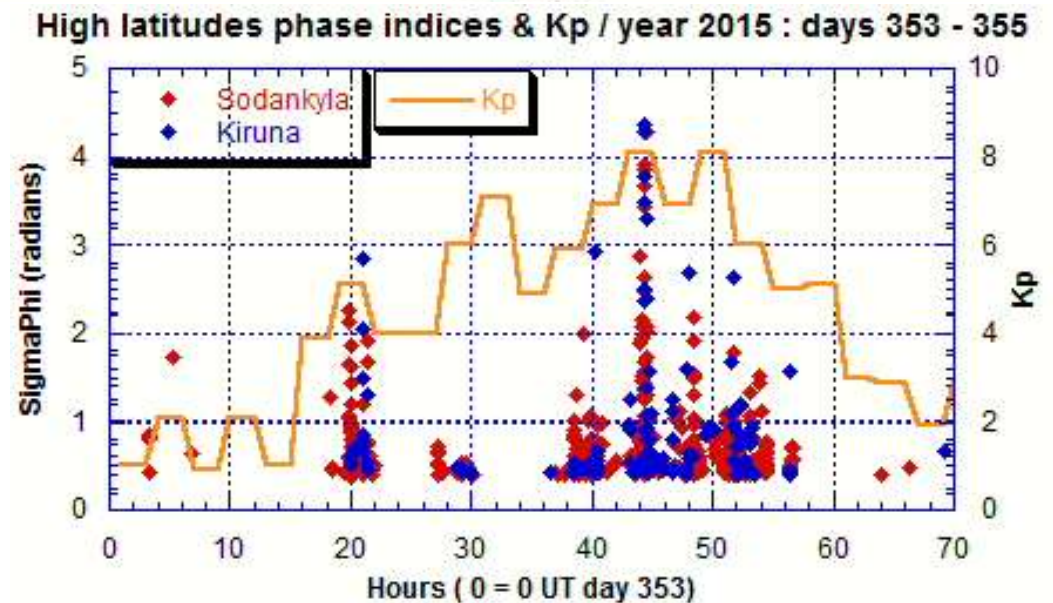
Relationship Phase fluctuation / AE & Kp Indices High Latitudes



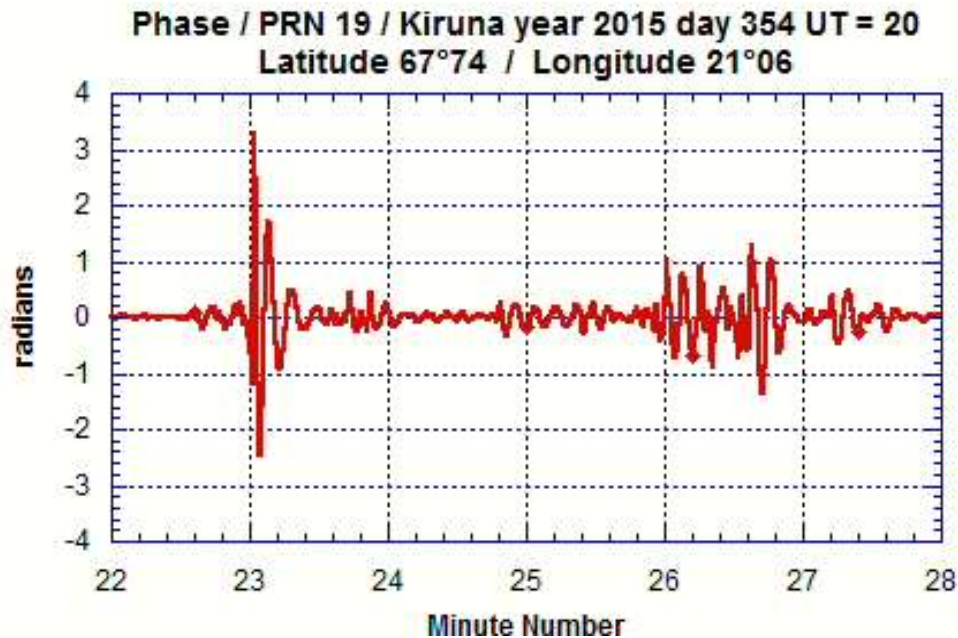
Kp geomagnetic index / december 2015



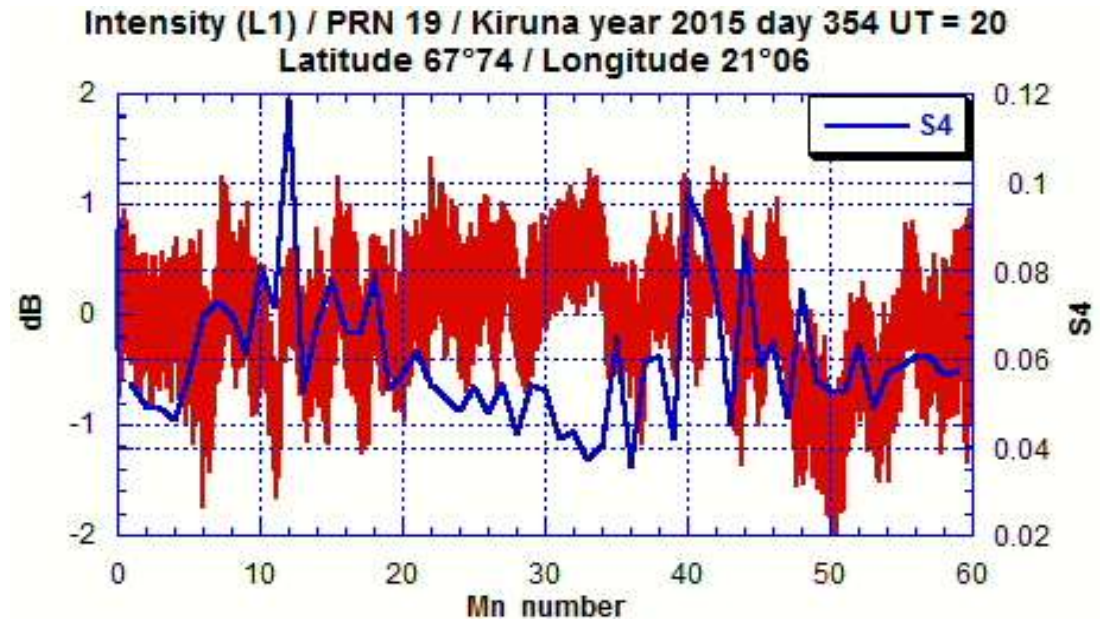
December 2015 magnetic storm



December 2015 Magnetic Storm Phase fluctuation



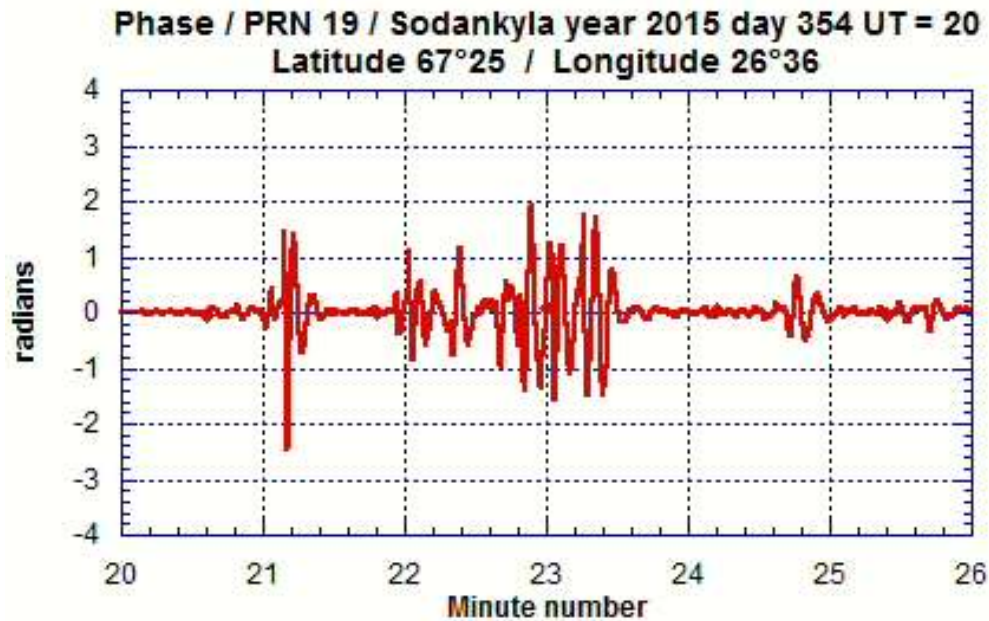
No fluctuations outside
these 6 minutes



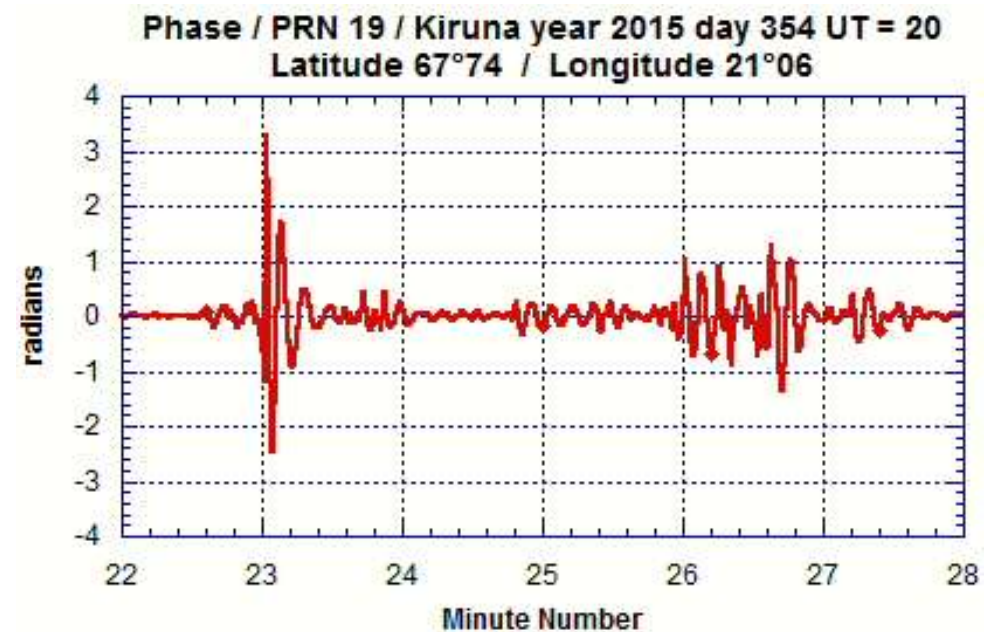
The intensity fluctuation is not an
issue for a GNSS application

Receiver : PolaRxS Septentrio

High latitude fluctuations



Sodankyla

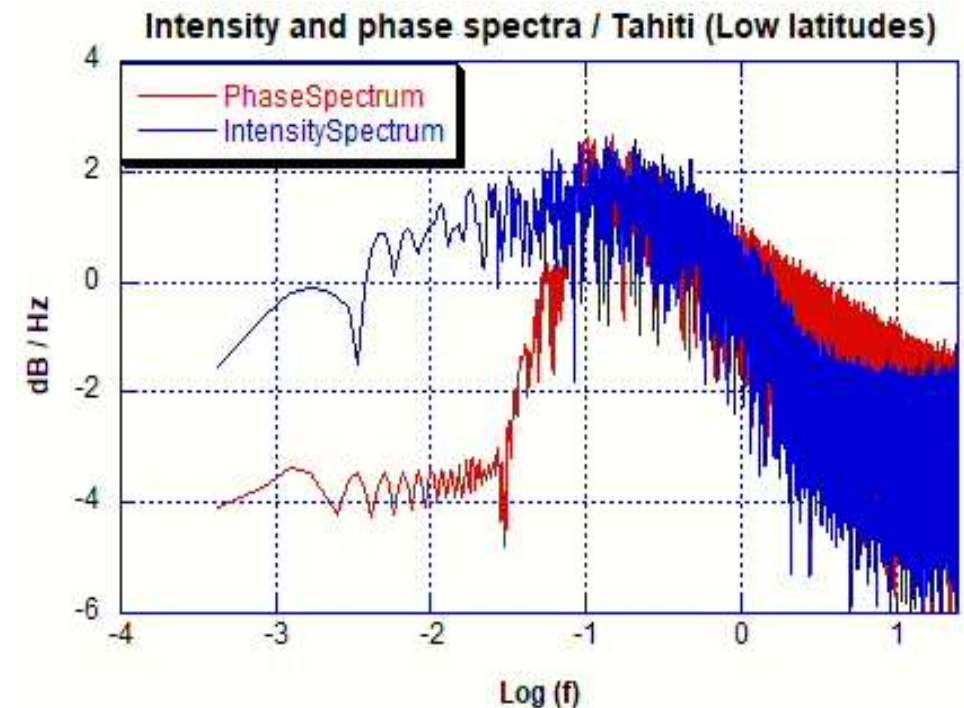
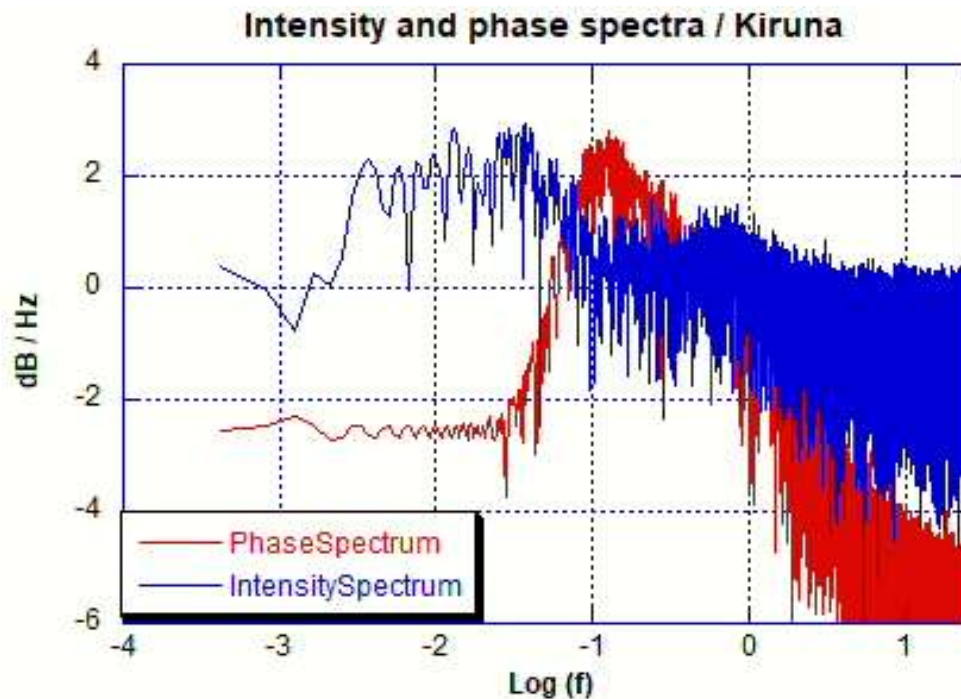


Kiruna

Distance between receivers : 280 km
Drift velocity : around 2 km / s. westward

→ **Refraction rather than diffraction**

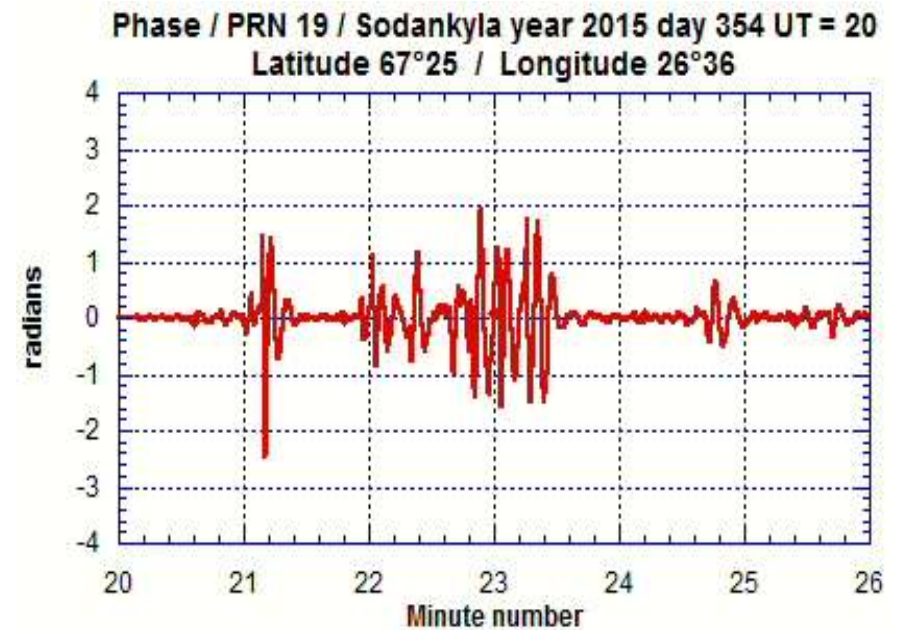
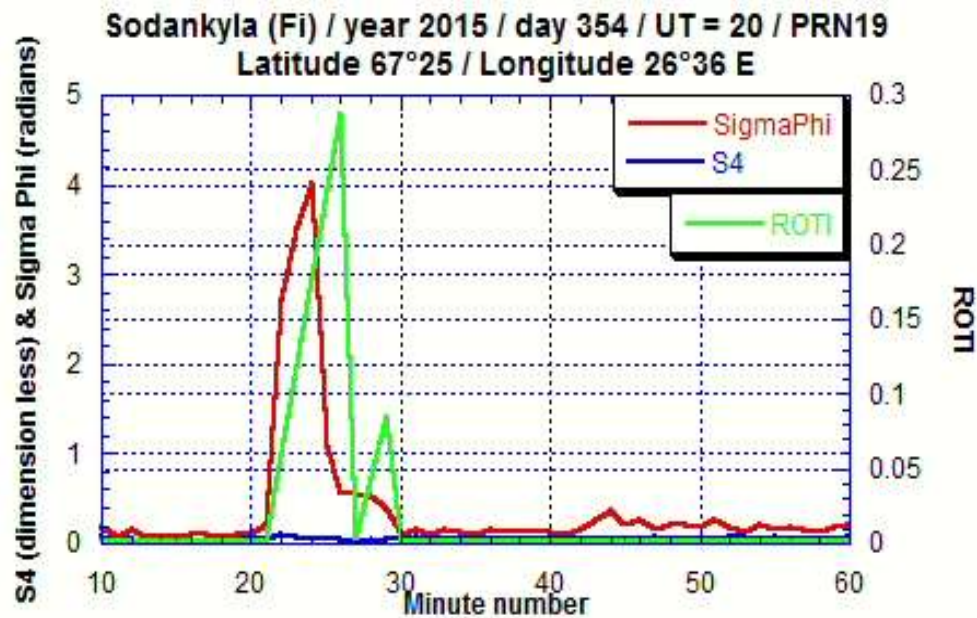
Fluctuations spectra : High Latitudes vs Low Latitudes



High frequencies → Low frequency content

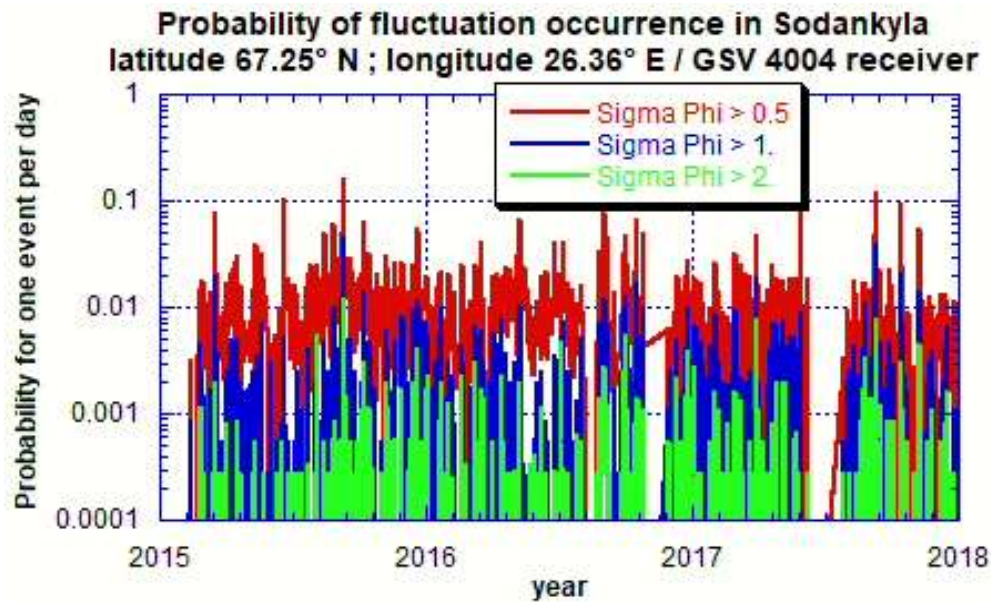
Different parameters for the Fresnel size, the focal scale and the altitude of inhomogeneities

Sigma Phi & ROTI High Lat

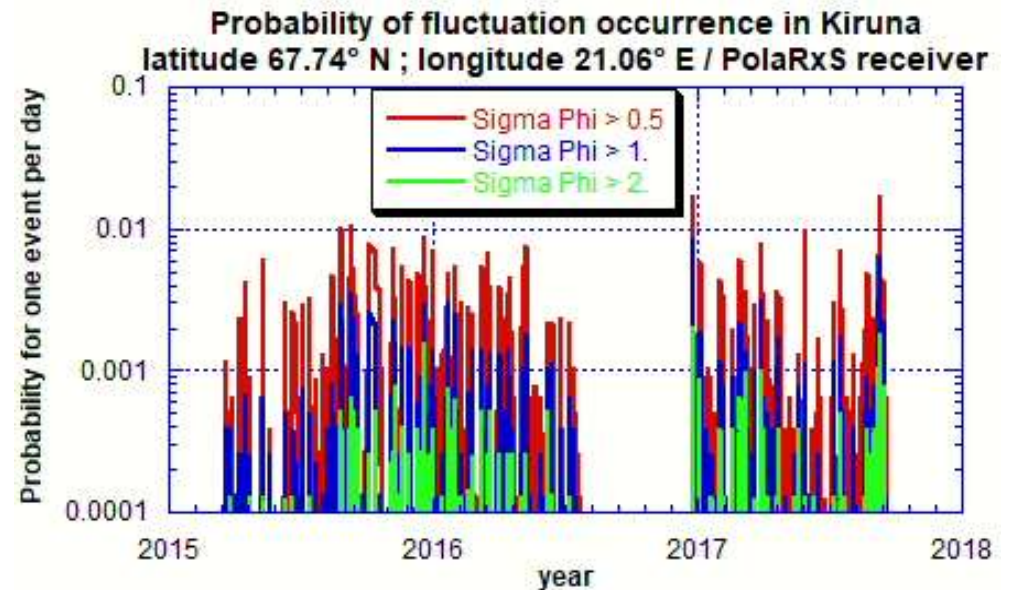


(Relationship of fluctuations to the ROTI index and consequently to TEC gradients)

Probability of occurrence



GSV4004B receiver

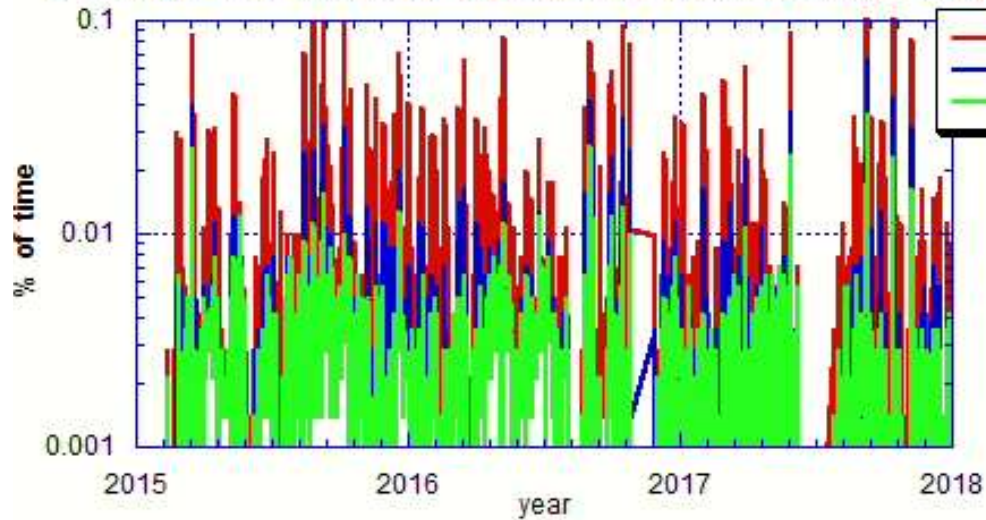


PolaRxS receiver

1 order of magnitude lower with the PolaRxS receiver

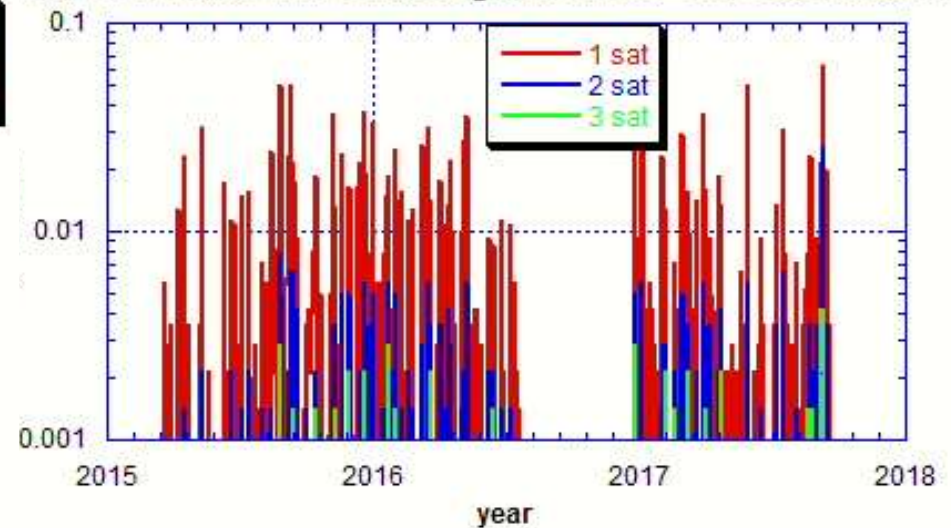
How many links at the same time

How many satellites simultaneously with sigma Phi > 0.5
Sodankyla : latitude 67.25° N ; longitude 26.36° E / GSV 4004 receiver



GSV4004B receiver

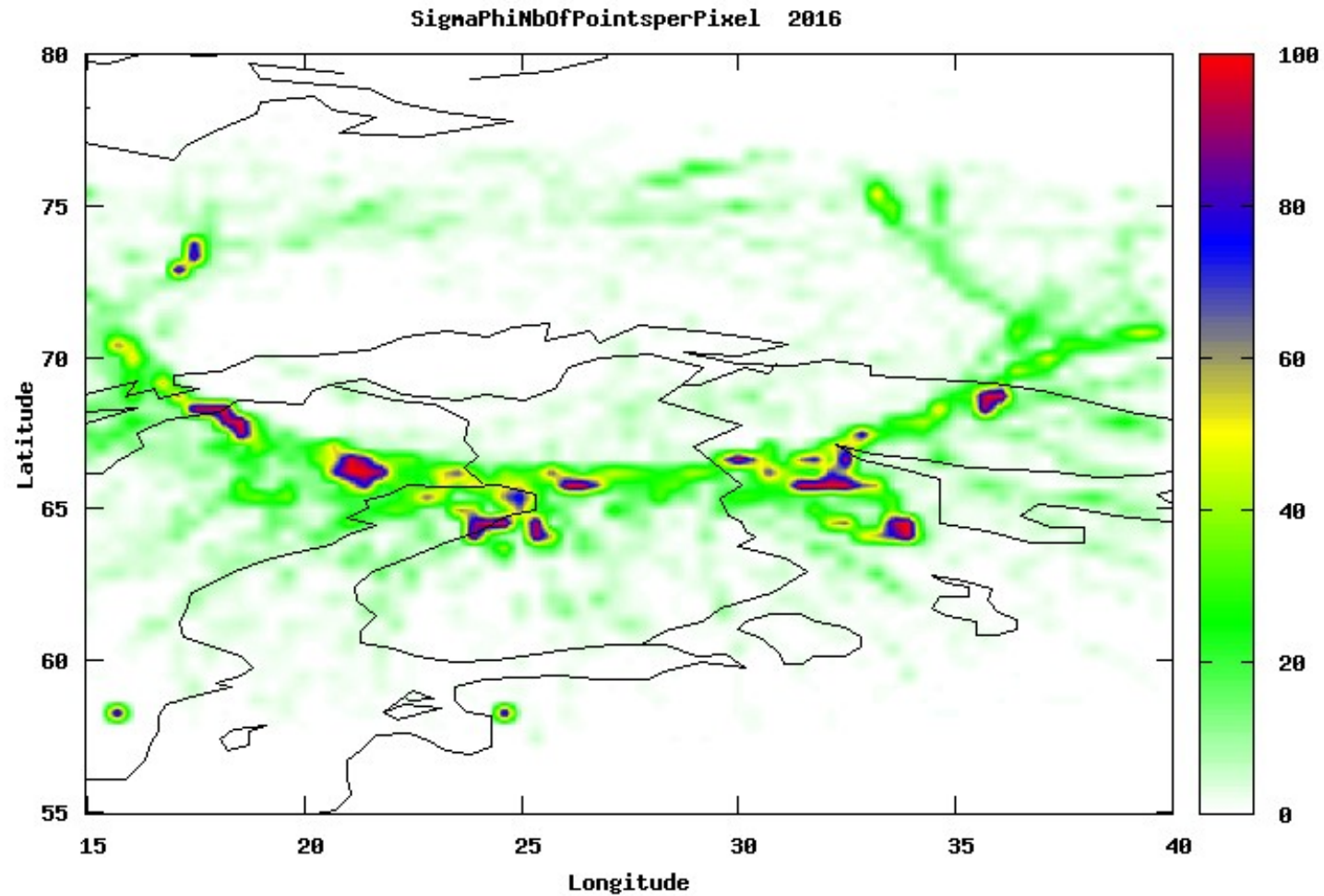
How many satellites simultaneously with sigma Phi > 0.5
Kiruna : latitude 67.74° N ; longitude 21.06° E / PolaRxS receiver



PolaRxS receiver

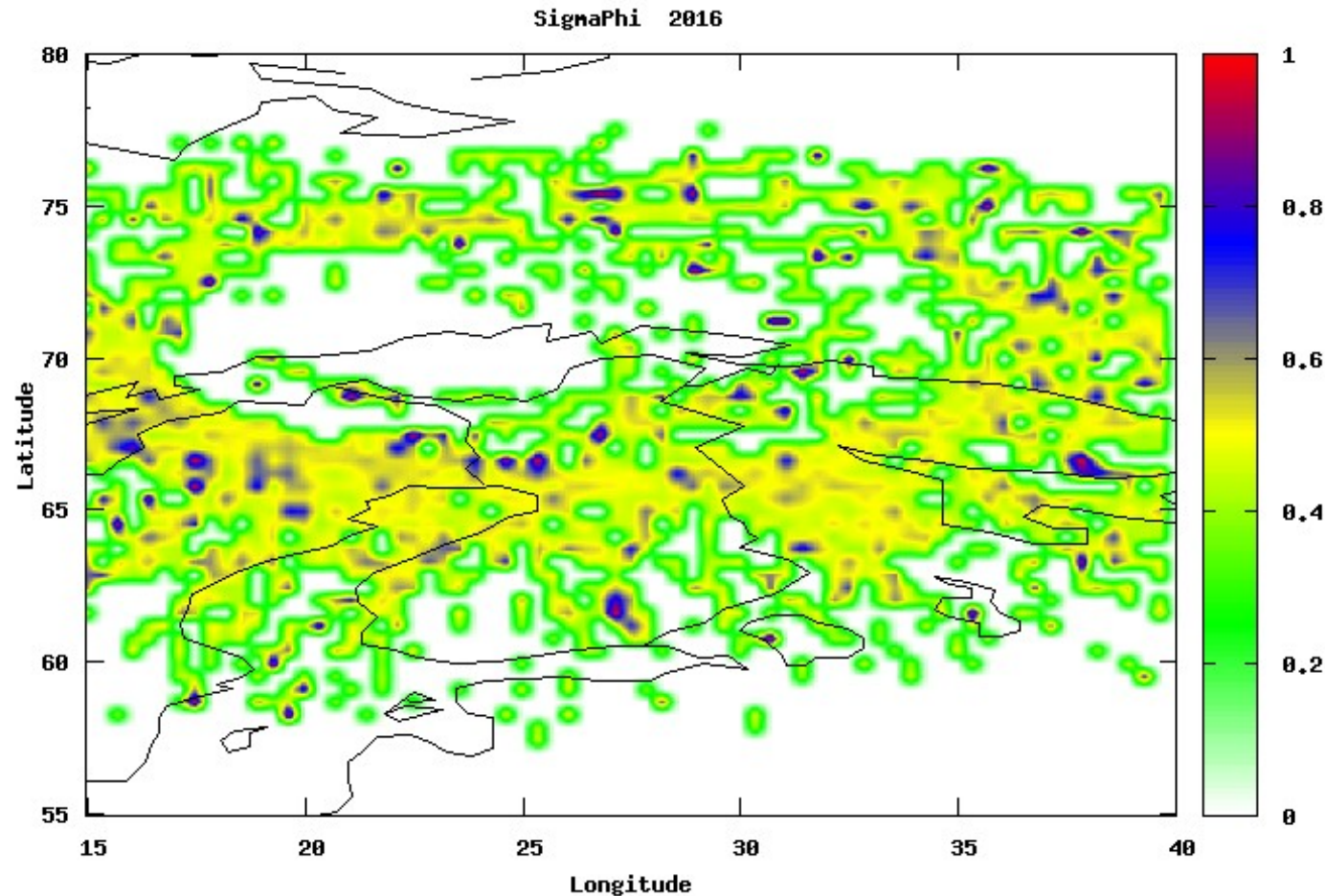
The % of time is lower with the PolaRxS receiver

High Latitudes Number of Links



Peak value at about 65° of latitude

Fluctuations Map / High Latitudes

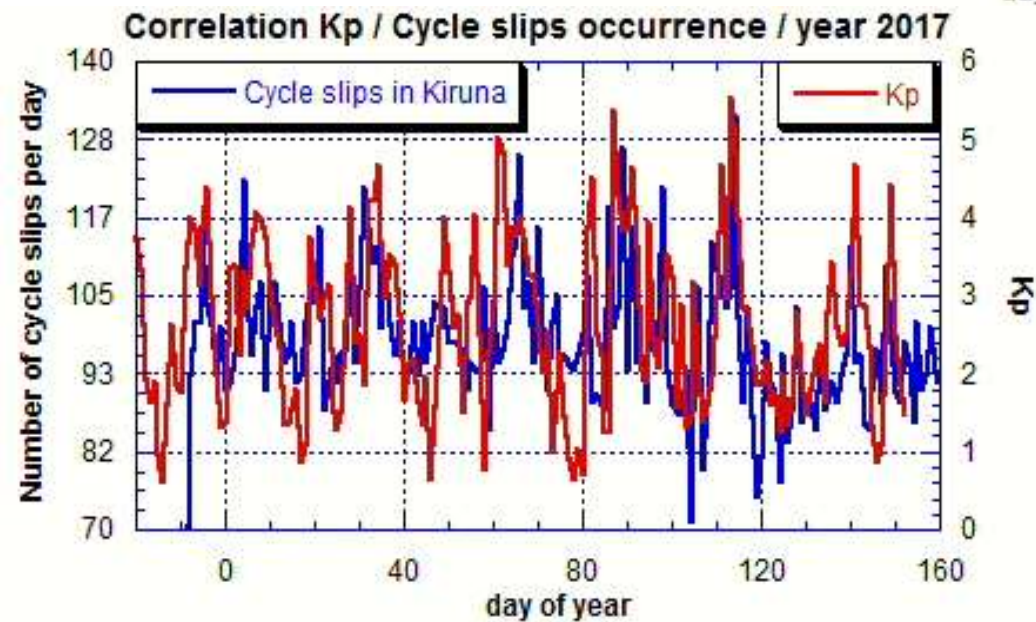
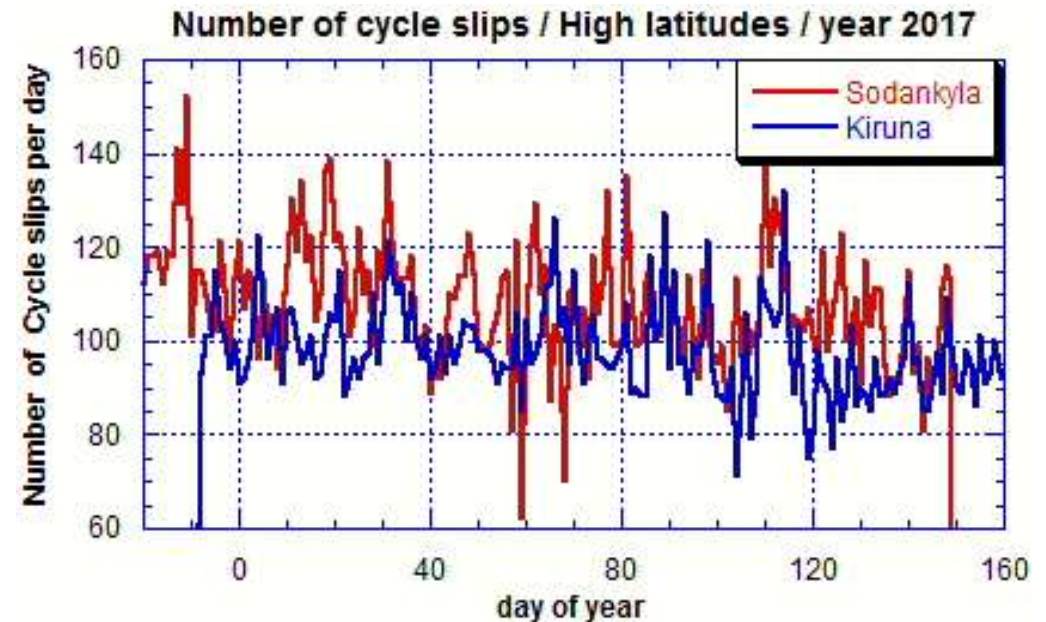
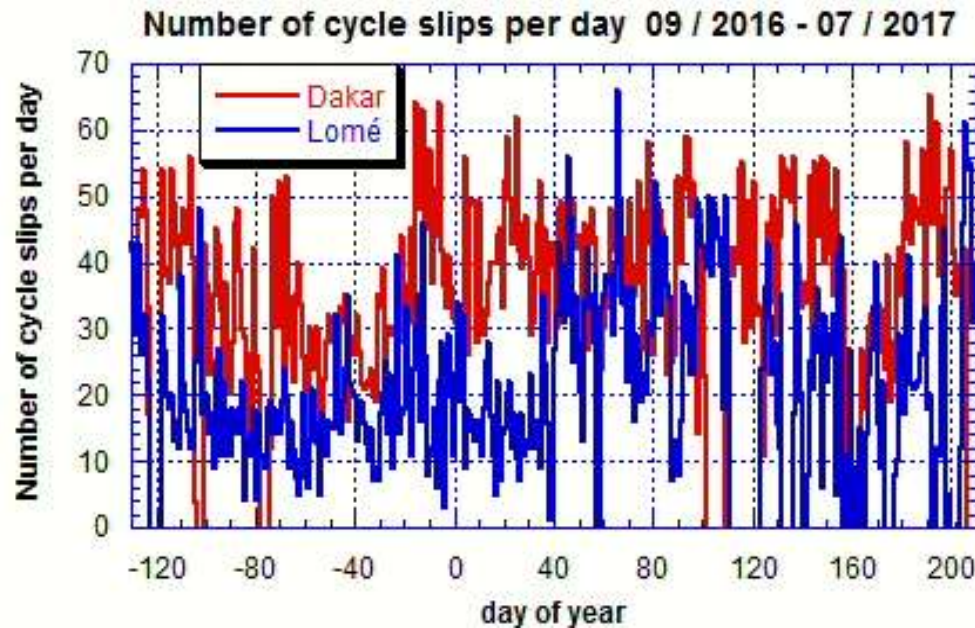


Scandinavian sector

sigma phi median values at IPPs cumulated over the year

Cycle Slips

Low Latitudes vs High Latitudes



Rinex input data files
(1 Hz)

Blewit algorithm

Section 3

Modelling

Multiple Phase screens technique GISM*

* developed under ESA / ESTEC contract

Béniguel Y., P. Hamel, “A Global Ionosphere Scintillation Propagation Model for Equatorial Regions”,
Journal of Space Weather Space Climate, 1, (2011), doi: 10.1051/swsc/2011004

Ray Technique

Appleton Hartree formula

$$n^2 = 1 - \frac{X}{U - \frac{Y^2 \sin^2 \theta}{2(U - X)} \pm \left[\frac{Y^4 \sin^4 \theta}{4(U - X)^2} + Y^2 \cos^2 \theta \right]^{1/2}} \approx 1 - X$$

$$\begin{aligned} X &= (f_p / f)^2 & \text{and} & \quad f_p = 9 \sqrt{N_e} & \text{is the plasma frequency} \\ Y &= f_b / f & \text{and} & \quad \omega_b = eB/m & f_b \text{ is the gyro frequency} \\ U &= 1 - jZ & \text{and} & \quad Z = \nu / \omega & \text{is the collision frequency} \end{aligned}$$

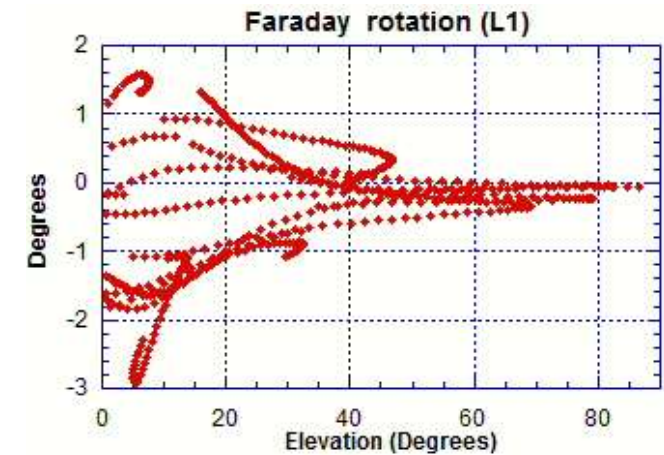
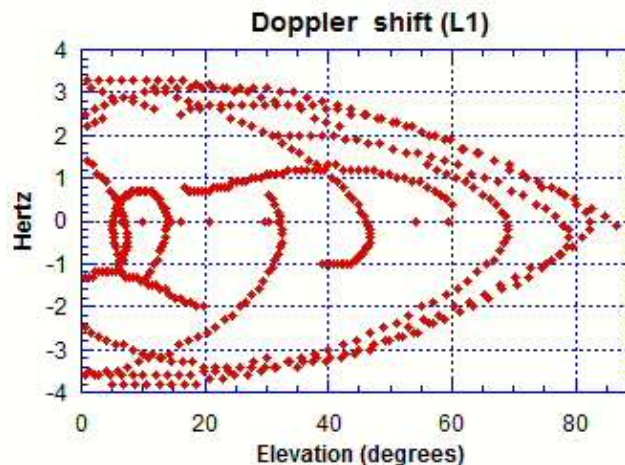
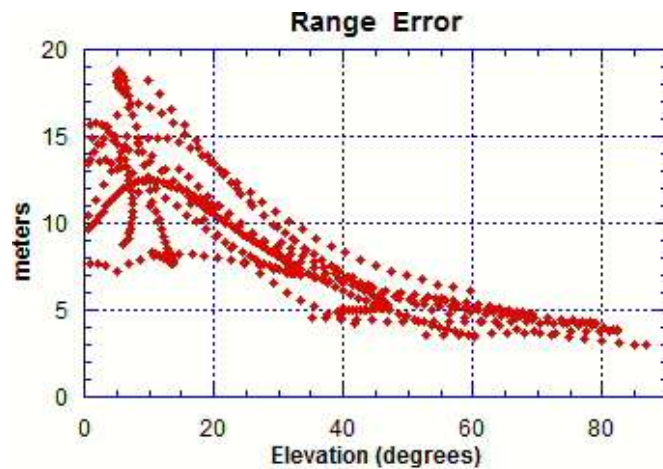
Line of sight calculation

$$\frac{d x_i}{d t} = \frac{c^2 k_i}{\omega} \qquad \frac{d k_j}{d t} = - \frac{\omega_p}{\omega}$$

Runge Kutta algorithm ; NeQuick model for Ne

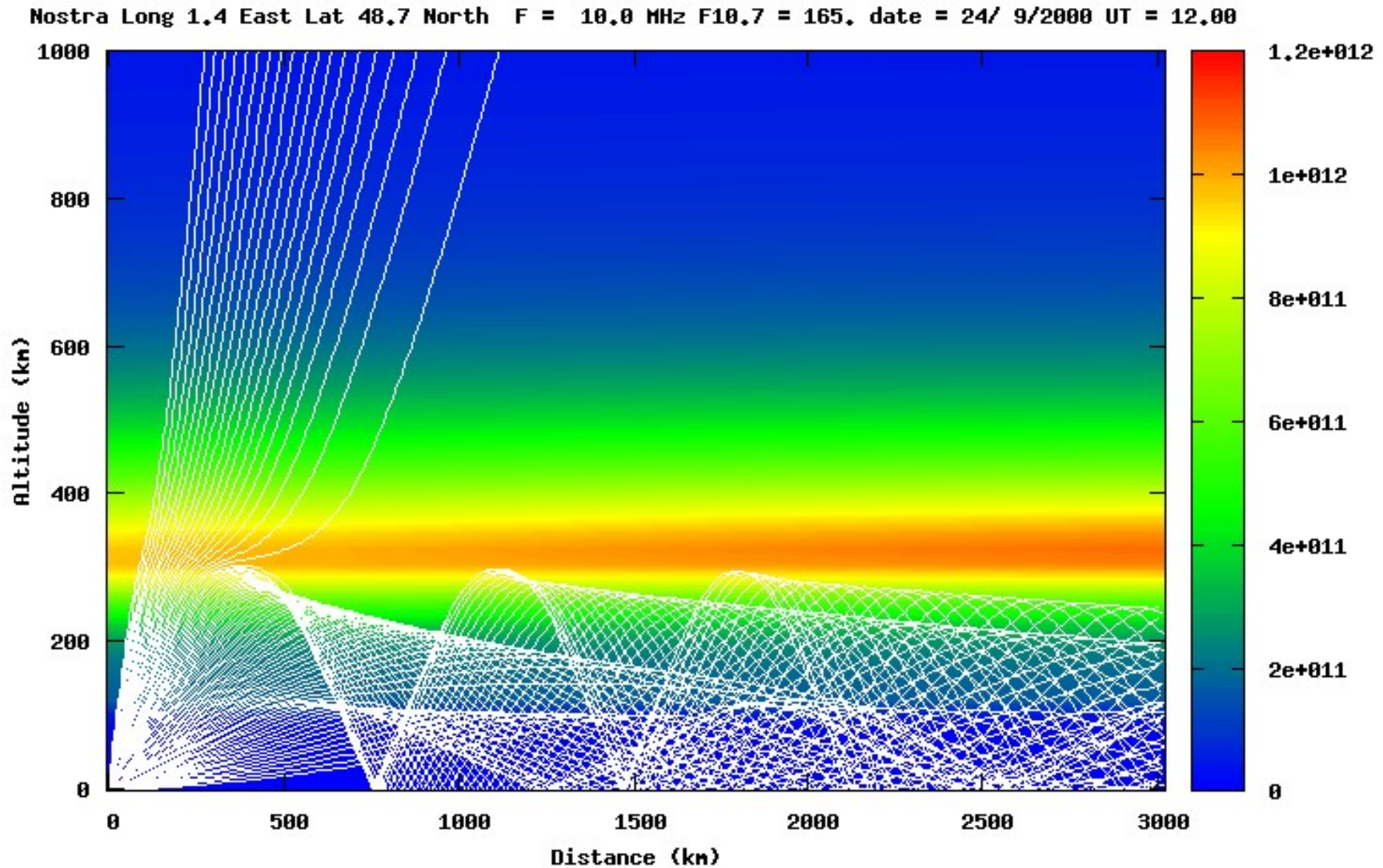
Mean Errors

distance	phase	Faraday rotation
$\Delta L = \frac{40.3 N_T}{f^2} \quad \text{with} \quad N_T = \int_0^z N_e ds$	$\Delta \Phi = k \int_0^{\Delta z} \Delta n(\rho, z) dz = \lambda r_e N_T$	$\Psi = \frac{e^3}{2 \epsilon_0 c m^2 \omega^2} \int_0^z N_e B \cos \theta ds$



Mid latitudes / solar flux 150

HF Propagation



2 reflexion heights (caustics of reflected rays) at D & E layers

Field Propagation Equation

$$E(\rho, z, \omega, t) = U(\rho, z, \omega) \exp \left\{ j \left(\omega t - \int \langle k(z') \rangle dz' \right) \right\}$$

The field amplitude value U is a solution of the parabolic equation (paraxial approximation)

$$2jk \frac{\partial U(\rho)}{\partial z} + \nabla_t^2 U(\rho) + k^2 \varepsilon_1(\rho) U(\rho) = 0$$

Method of solution : phase screen technique

Field Propagation Equation

Solution of the parabolic equation

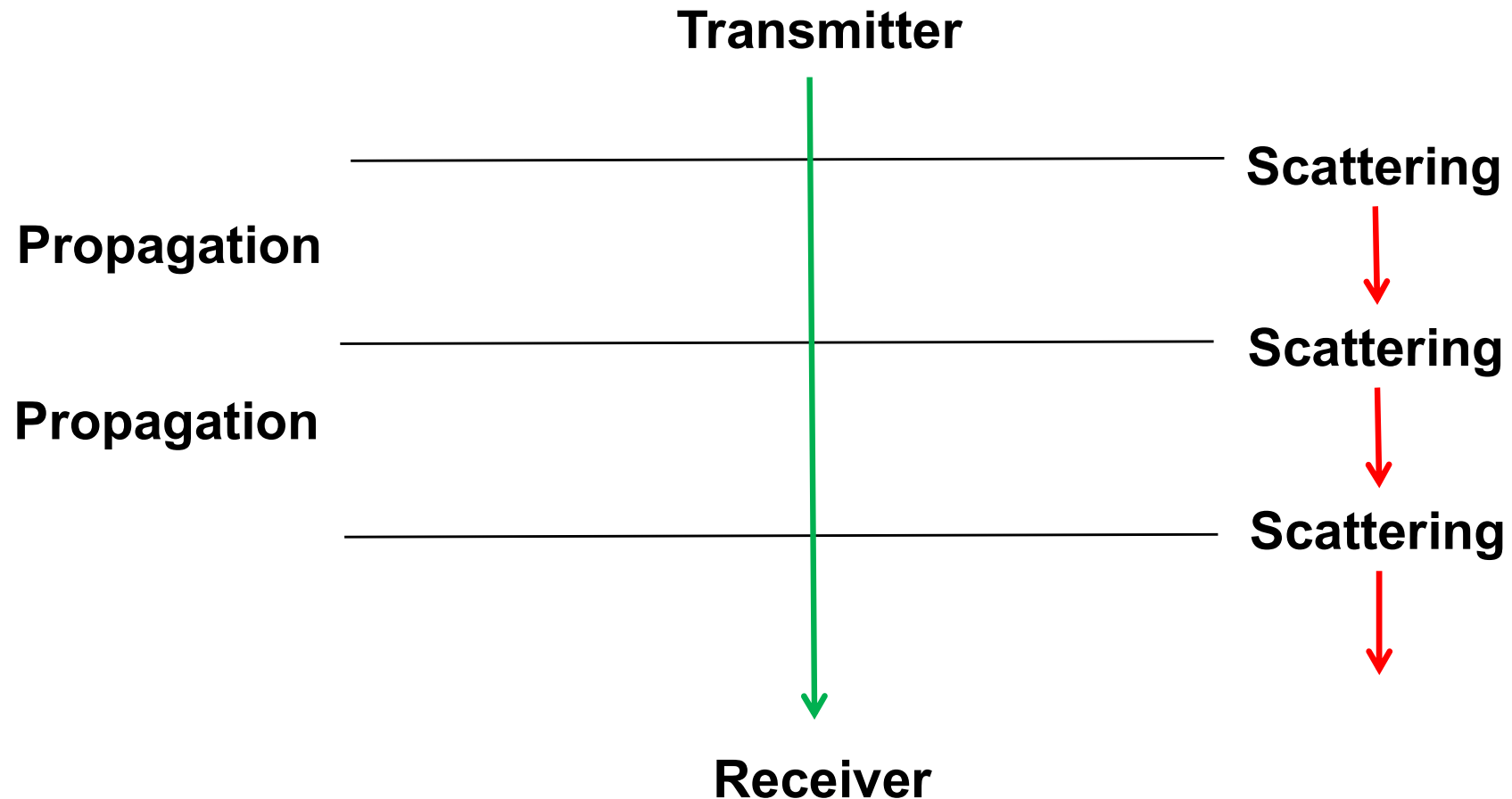
$$2jk \frac{\partial}{\partial z} \langle U(\mathbf{r}) \rangle + \nabla_{\perp}^2 \langle U(\mathbf{r}) \rangle + k^2 \langle \varepsilon(\mathbf{r}) U(\mathbf{r}) \rangle = 0$$

$$2jk \frac{\partial}{\partial z} \langle U(\mathbf{r}) \rangle + \nabla_{\perp}^2 \langle U(\mathbf{r}) \rangle + j \frac{k^3}{4} A(0) \langle U(\mathbf{r}) \rangle = 0$$

Using the medium index autocorrelation function

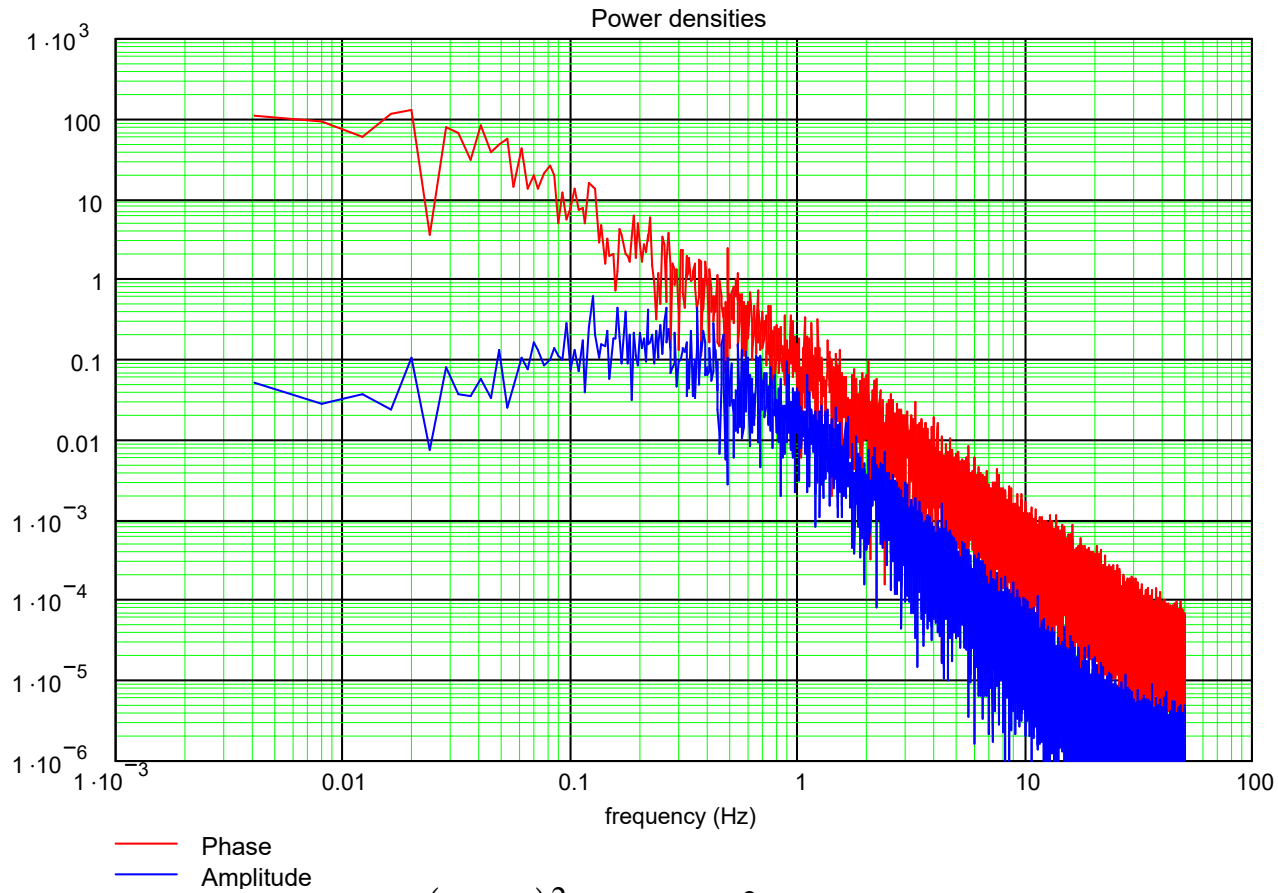
$$B(z, \rho) = \langle \varepsilon(\rho_1) \varepsilon(\rho_2) \rangle \quad A(\rho) = \int B(z, \rho) dz$$

Phase Screen Technique



Propagation : 1st & 3rd terms ; scattering : 2nd & 3rd terms

Phase & Intensity Spectra



$$\gamma_{\Phi}(\mathbf{K}) = \frac{(\lambda r_e)^2 L C_S \sigma_{Ne}^2}{(\mathbf{K}^2 + q_0^2)^{p/2}} = \frac{C_P}{(\mathbf{K}^2 + q_0^2)^{p/2}}$$

3 parameters : σ_{Ne} ; q_0 ; p

Phase Synthesis (1D)

$$\Phi(\rho) = \text{FFT}^{-1}(\text{FFT}(u) * \gamma_{\Phi}(k))$$

u random number with a uniform spectral density

Done at each successive layer

1D Analysis Isotropic Medium

LOS



$$B_{\Phi}(\rho) = \frac{C_P}{2\pi} \int \gamma_{\Phi}(k) \exp(-jk\rho) dk$$

$$[B_{\Phi}(\rho)]_{1D} = \frac{C_P}{2\pi} \frac{\sqrt{\pi}}{2^{(p-3)/2} \Gamma(p/2)} q_0^{1-p} (\rho q_0)^{(p-1)/2} K_{(p-1)/2}(\rho q_0)$$

Anisotropic vs Isotropic



$$\gamma_{\Phi} (K) = \frac{(\lambda r_e)^2 L C_s \sigma_{Ne}^2 a b}{(q^2 + q_0^2)^{p/2}}$$

$$\gamma_{\Phi} (K) = \frac{a b C_p}{\left((AK_{x\perp}^2 + BK_{x\perp} q_{y\perp} + CK_{y\perp}^2)^2 + q_0^2 \right)^{p/2}}$$

Additional geometric factor* with respect to the 2D case

$$G = \frac{ab}{(AC - B^2/4)^{1/2}}$$

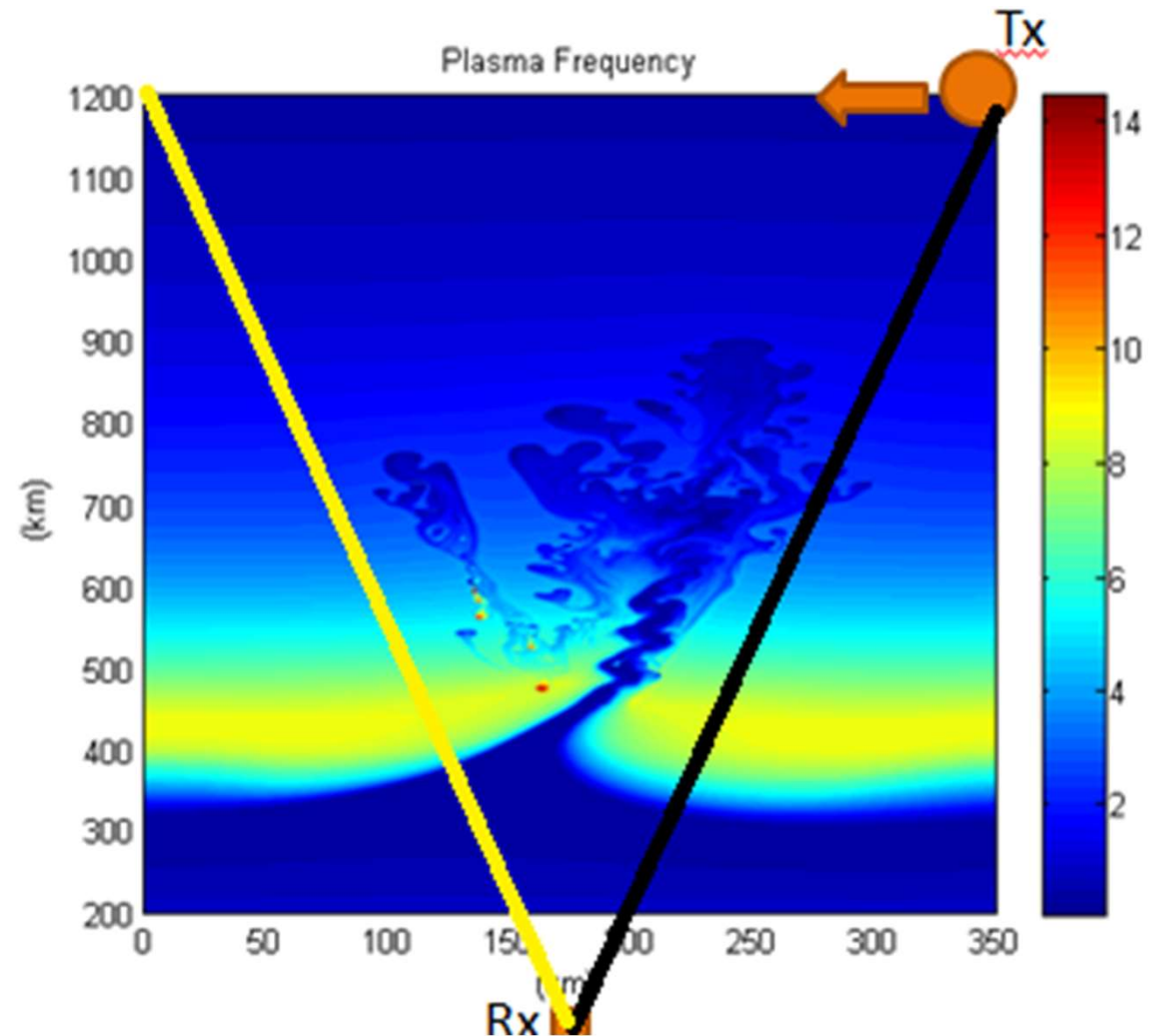
a, b ellipses axes

A, B, C trigonometric terms resulting from rotations related to variable changes

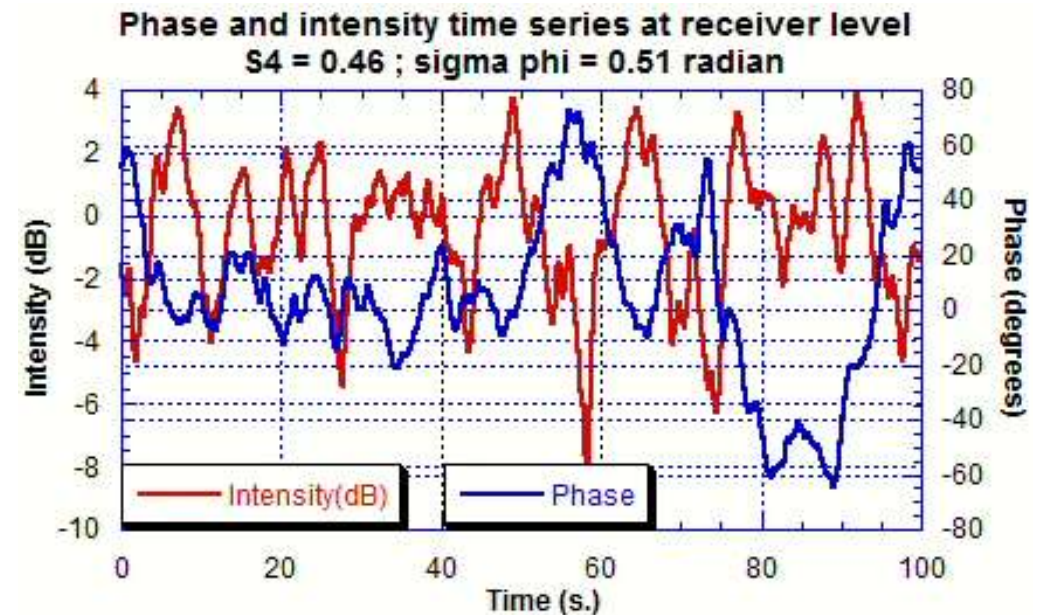
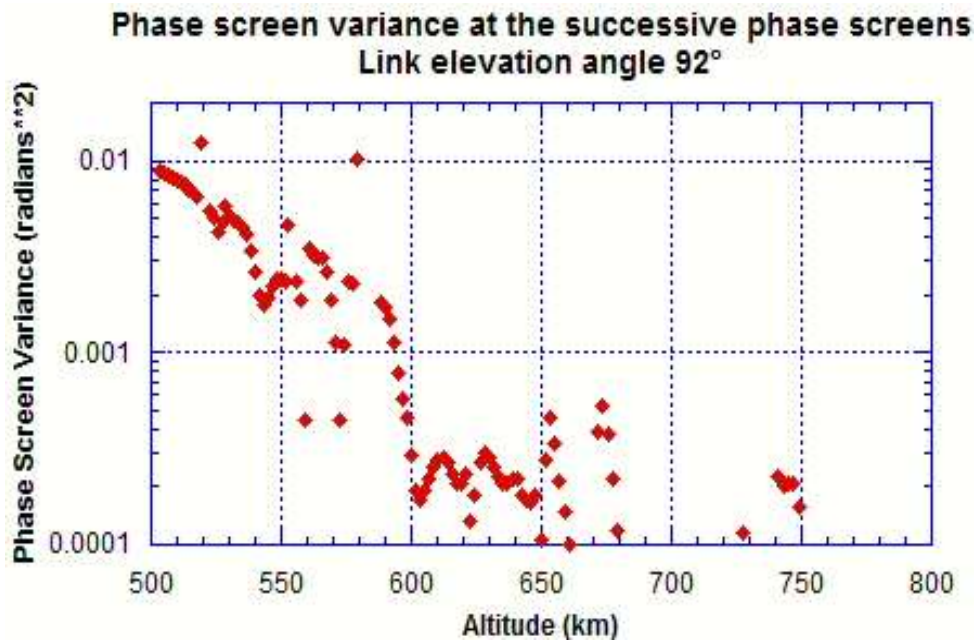
* Rino CL. 2011. The theory of scintillation with applications in remote sensing. Wiley, New Jersey.

NICT Model : Bubbles Development

- Receiver at $d = 180$ km
- Satellite at $h = 1200$ km from $d = 350$ km to 0 km



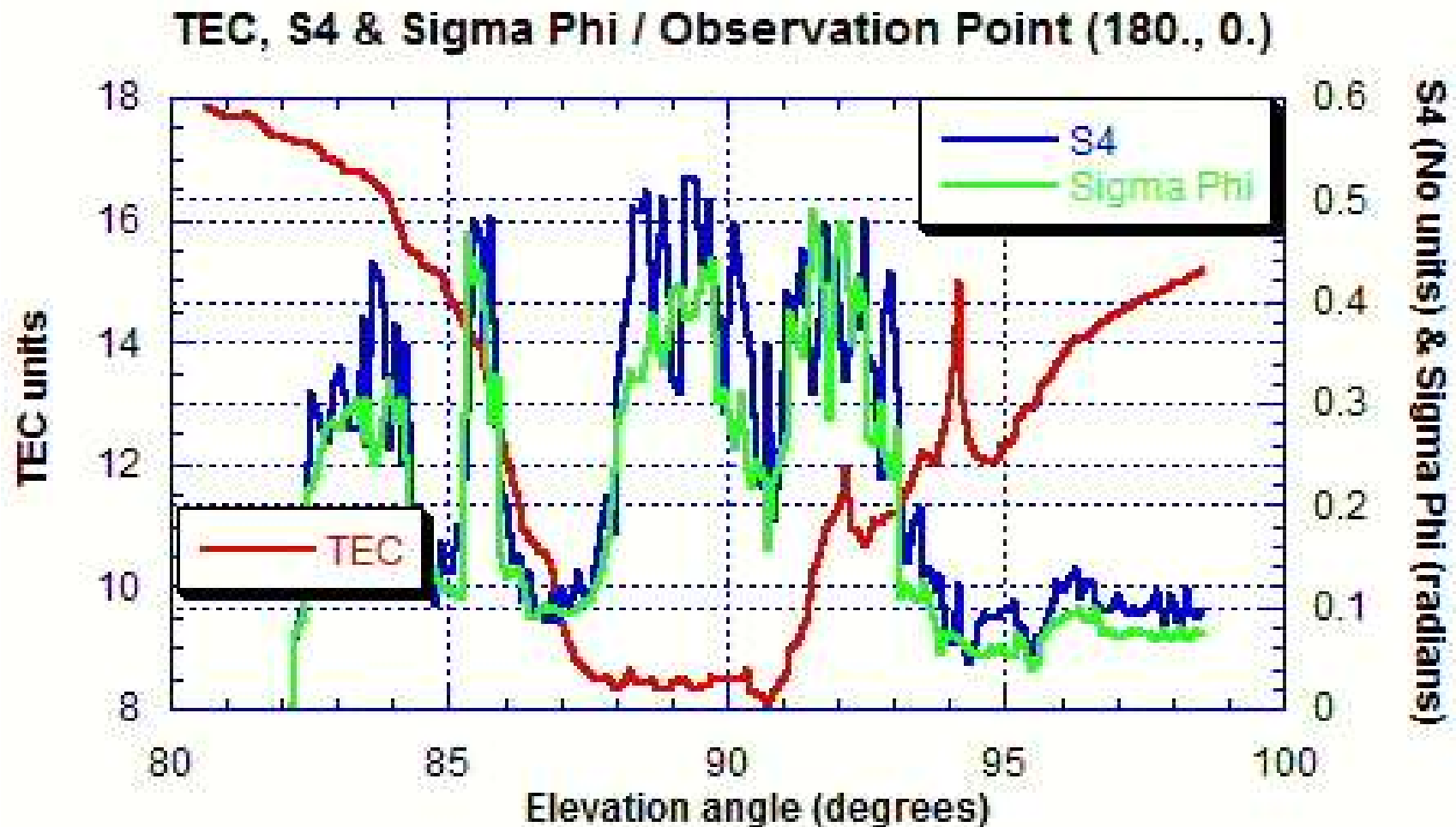
Crossing Bubbles for one Particular Elevation Angle



143 phase screens

TEC, S4 and σ_ϕ Time series

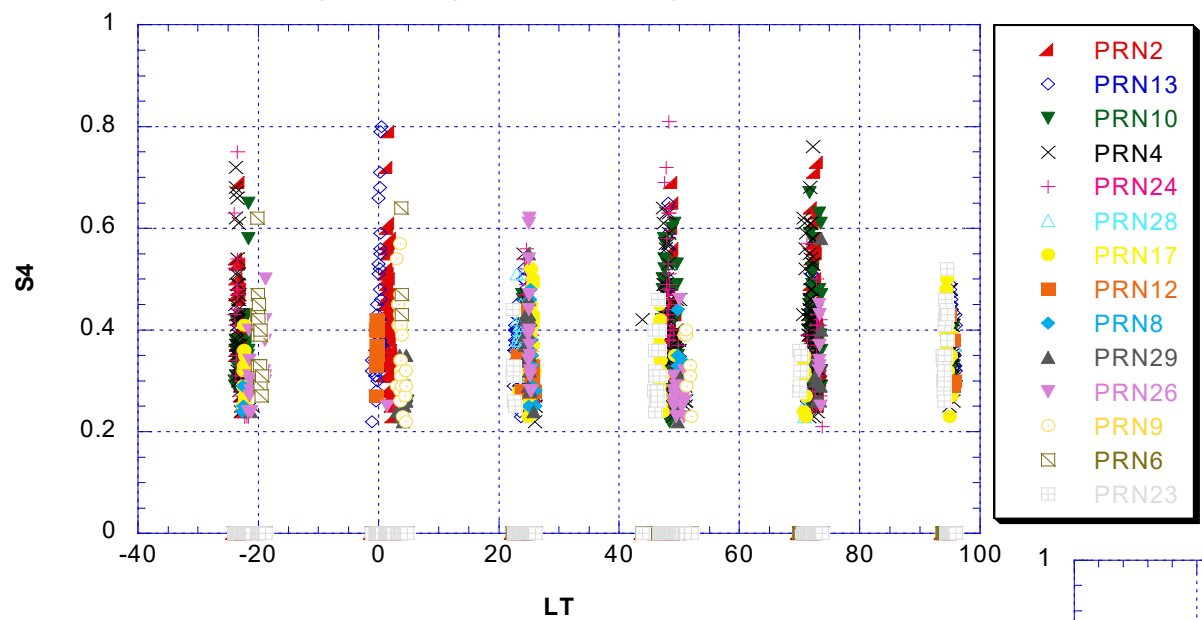
Scanning the medium



Modelling vs Measurements

Modelling vs Measurements (Intensity of received signal)

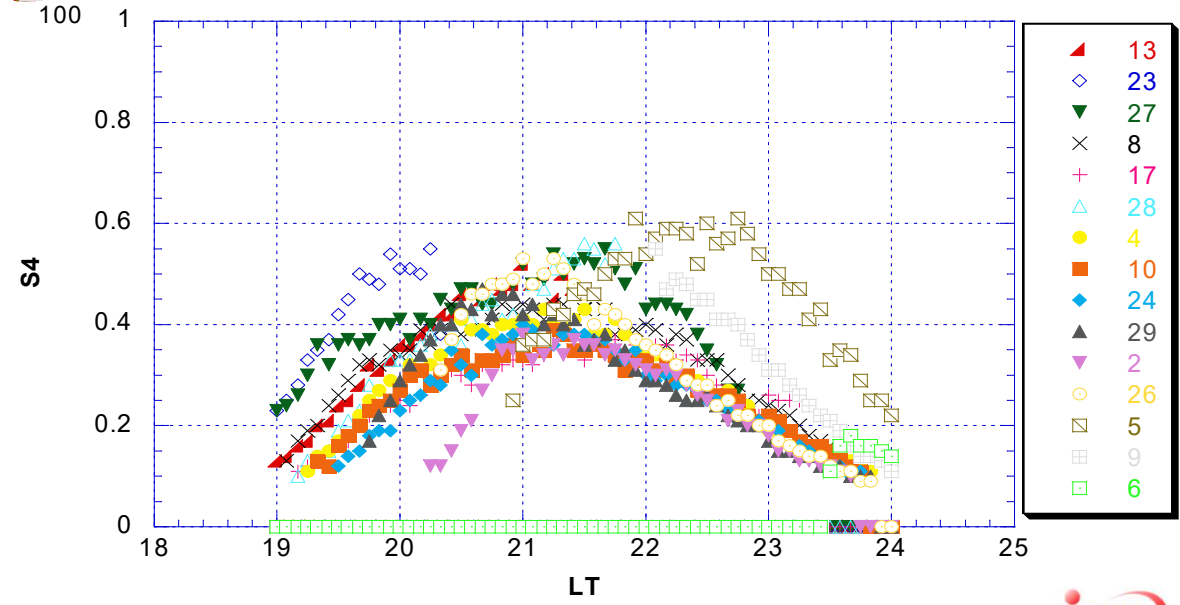
S4 all satellites
Cayenne days 314 to 319 : year 2006



← **Measurements**

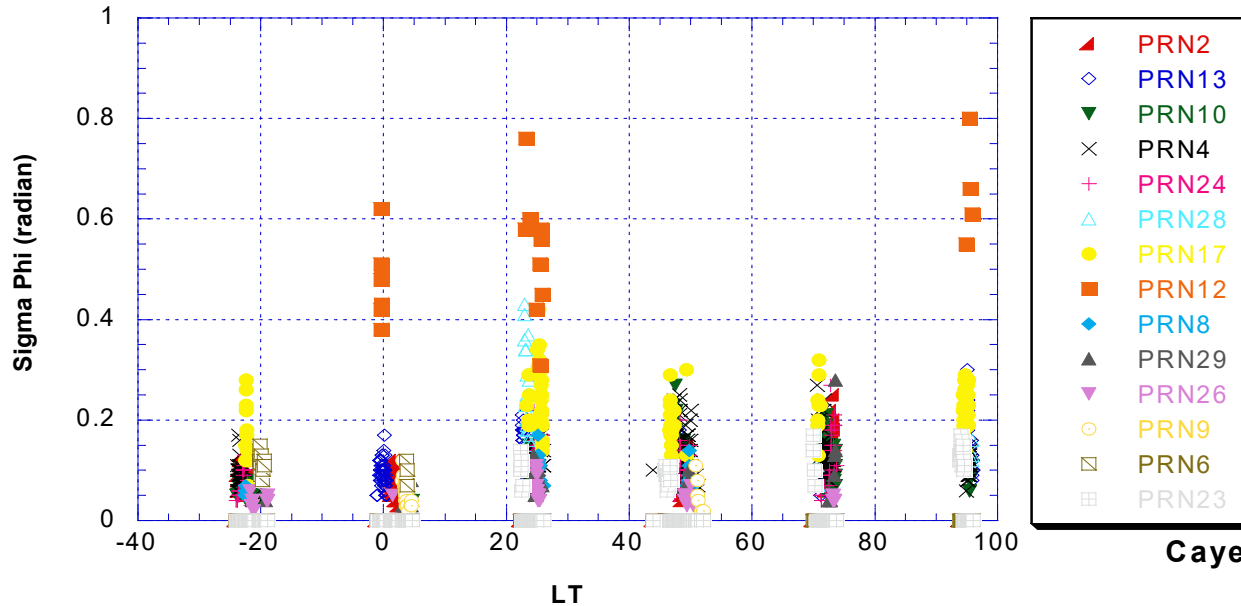
Modelling →

Cayenne day 314 / 2006
GISM



Modelling vs Measurements (Phase of received signal)

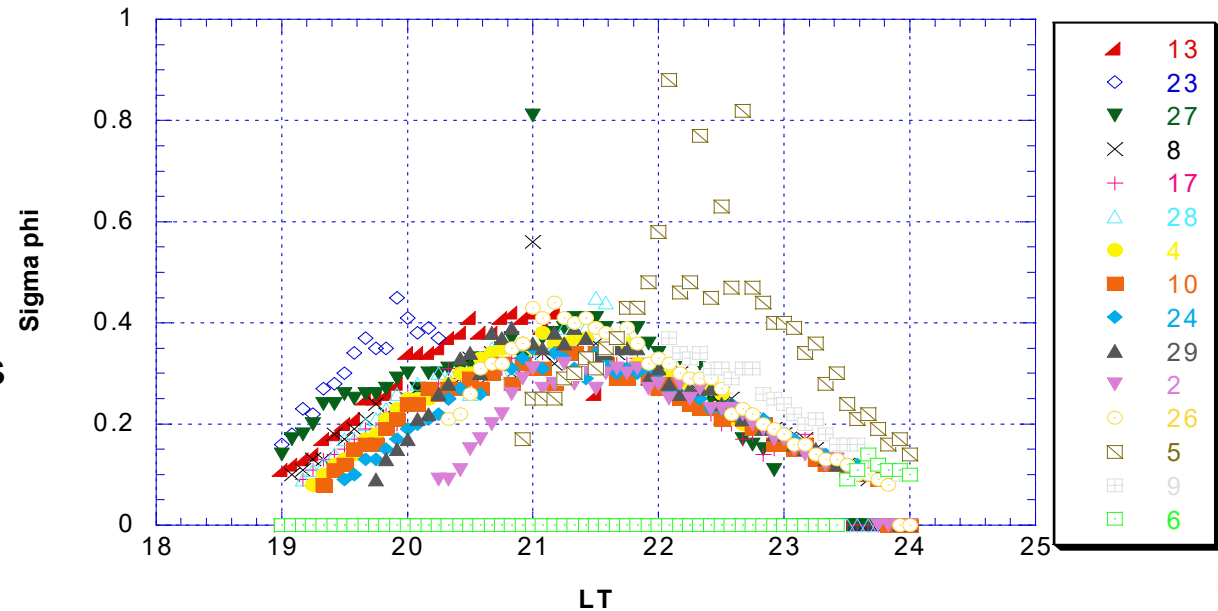
Sigma Phi all satellites
Cayenne, days 314 to 319 / year 2006



The phase RMS value is slightly lower than the S4 value

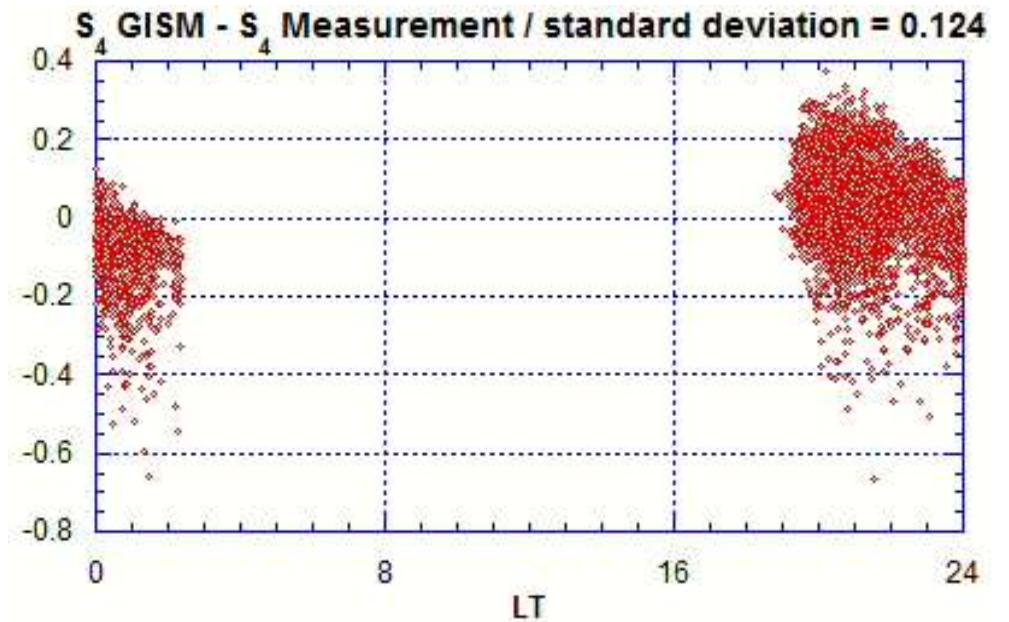
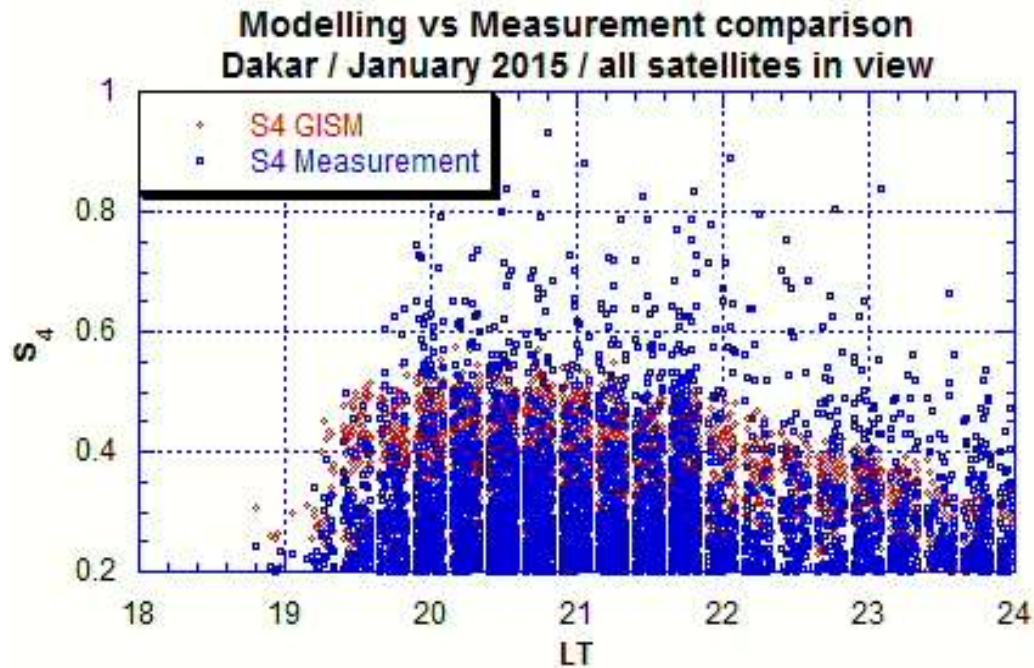
← **Measurements**

Modelling →



Some samples exhibit high values (both measurements and modelling) due to the cycle slips

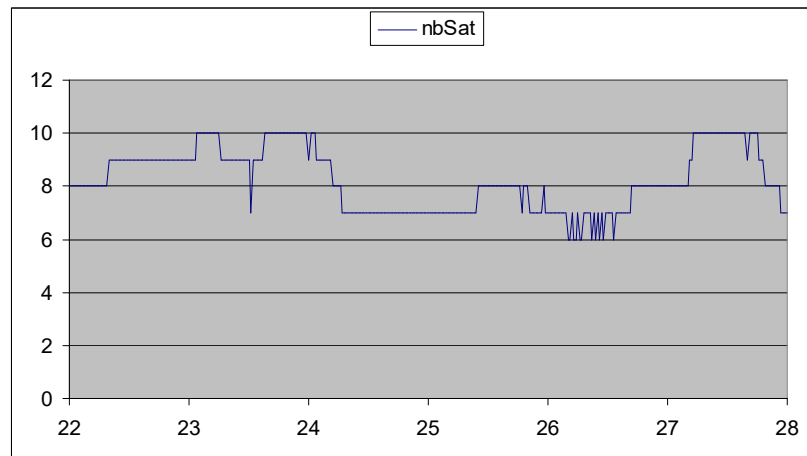
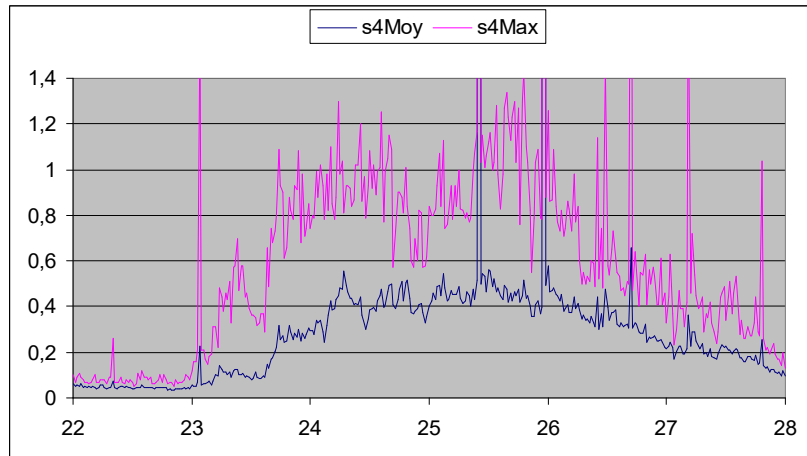
Modelling vs Measurements one month of measurements



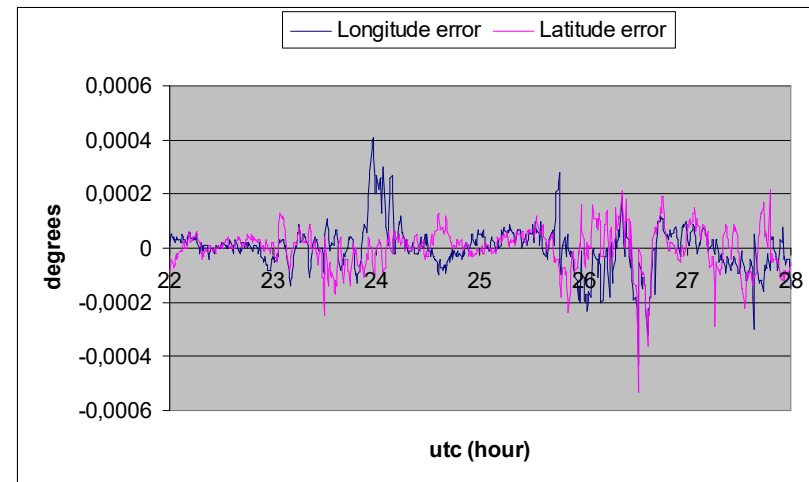
All links considered: input data from the 1 mn pre processed file of recorded data

Positioning Errors Related to scintillations

Positioning errors from Measurements in Brazil in 2001



- Solving the navigation equation
- Satellite trajectories obtained from the Yuma files



0.0001 degree → 10 meters

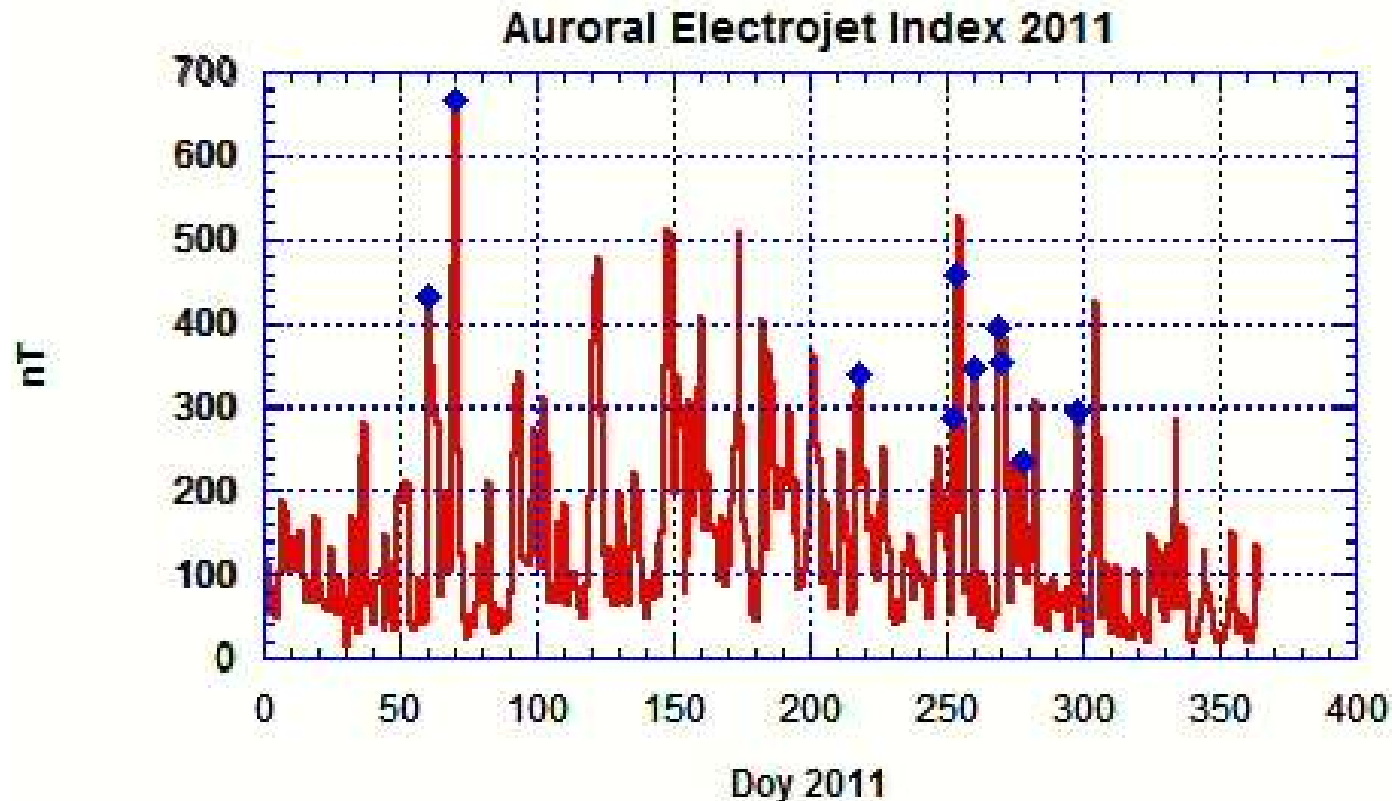
Section 4

Extreme events

Storms list

Month with Dst values < -100 nT													
1	2	3	4	5	6	7	8	9	10	11	12	Month	Count
J	F	M	A	M	J	J	A	S	O	N	D	Year	per Year
		X						XX	X			2011	4
		X	X			X			XX	X		2012	6
		X			XX	X						2013	4
	XX		XX									2014	4
		X			X						X	2015	3
XX					X				X			2016	4
				X				X				2017	2
							X					2018	1
2	2	4	3	1	4	2	1	3	4	1	1	Sum:	28

EGNOS Days of Decrease Performance

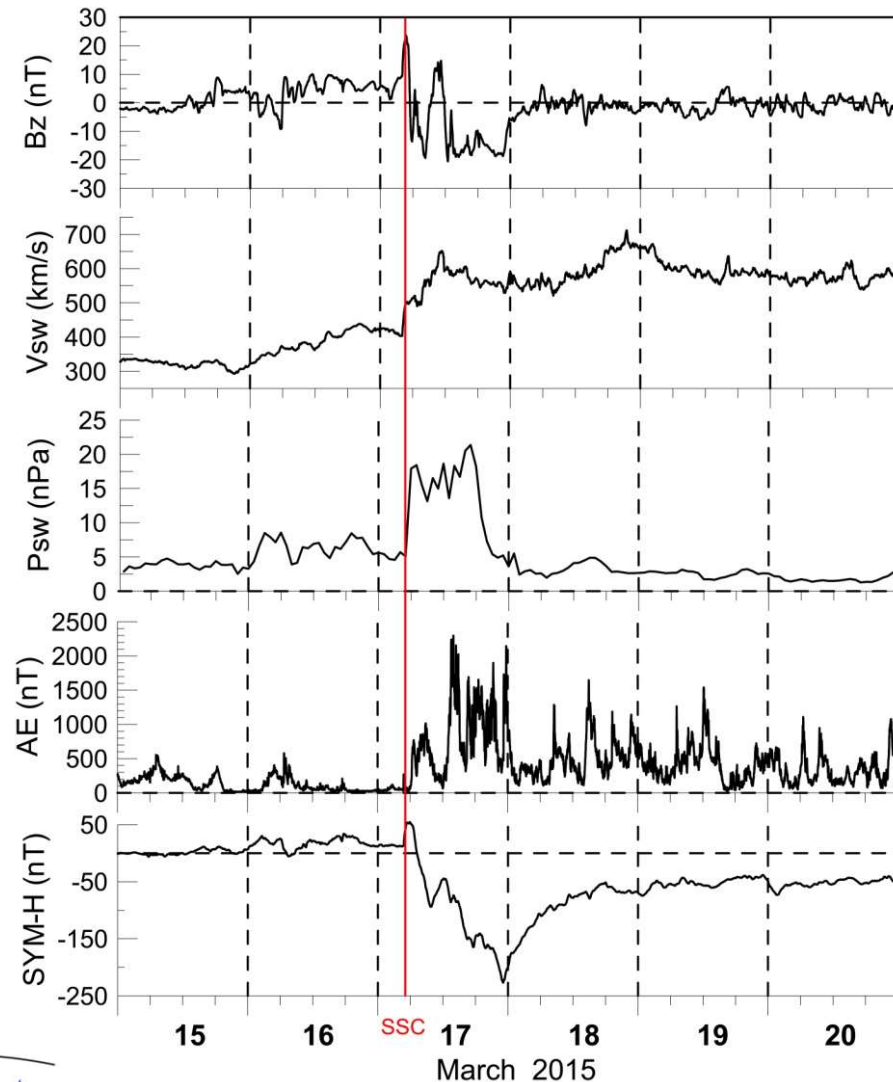


The EGNOS days of decrease of performance were all corresponding to a peak of the magnetic activity

Study Case

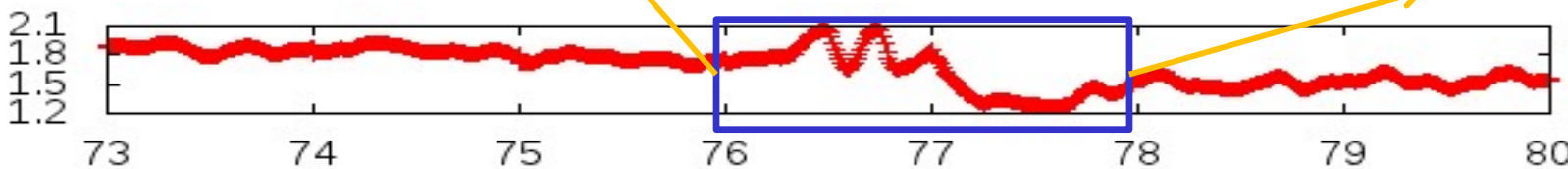
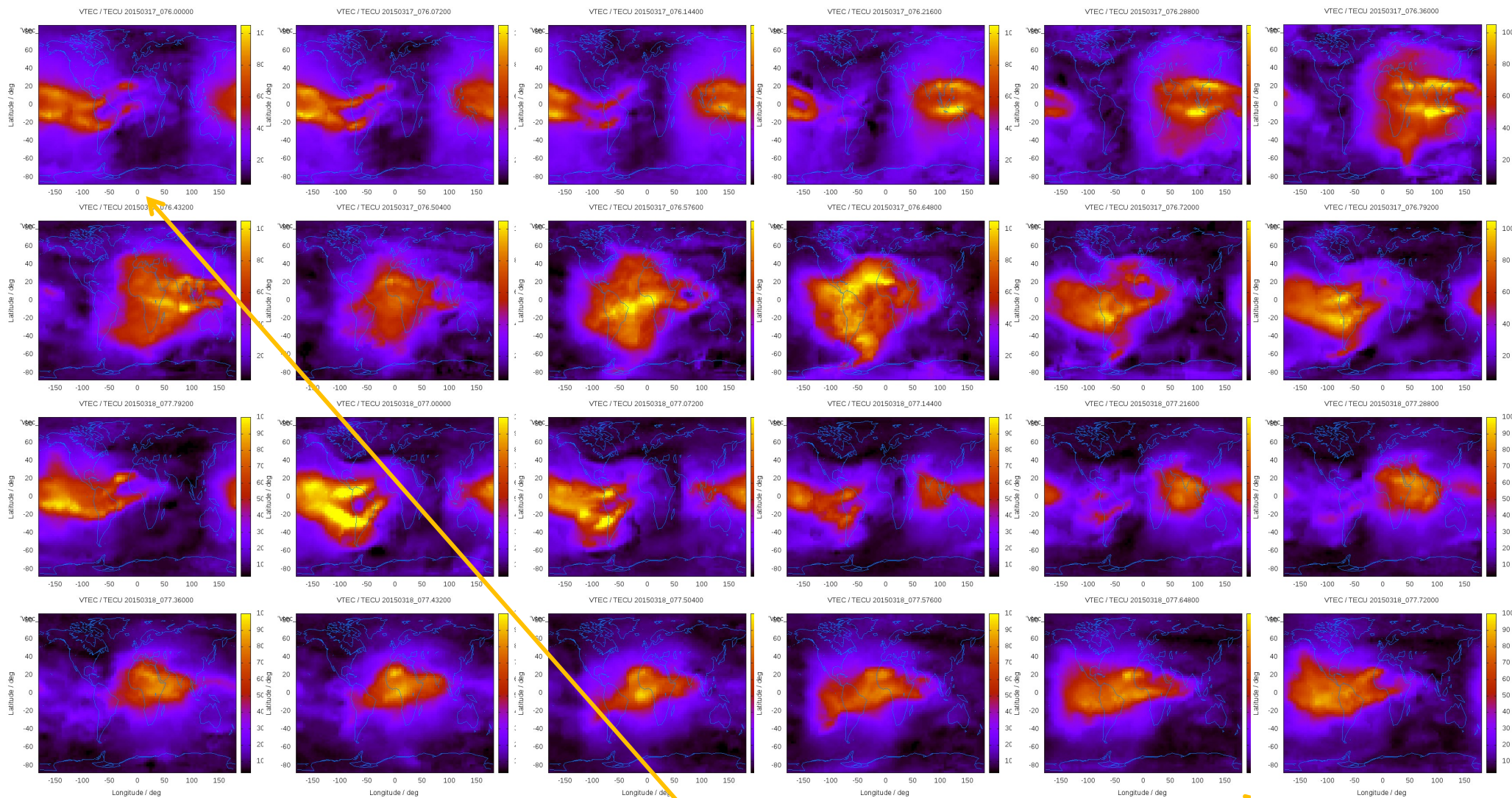
**St Patrick magnetic storm
17 – 22 march 2015**

Index detection of the 2015 St Patrick geomagnetic storm



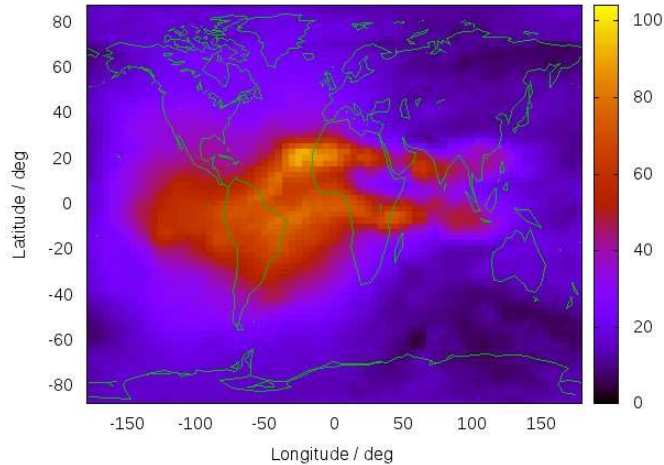
- Largest storm for the last 10 years
- Intense particle precipitation
- Aurora was recorded at mid-latitudes

VTEC snapshots @ 2h from 17/03/2015 (doy 76) 00h to 19/03/2015 (doy 77) 24h



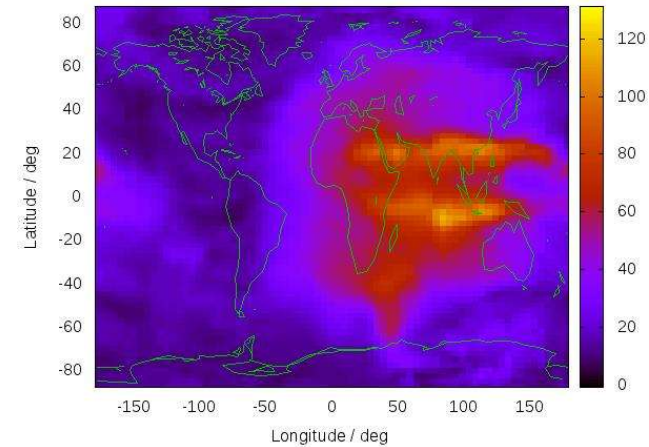
Maps of the Peak Activity

VTEC / TECU 20150316_075.64800



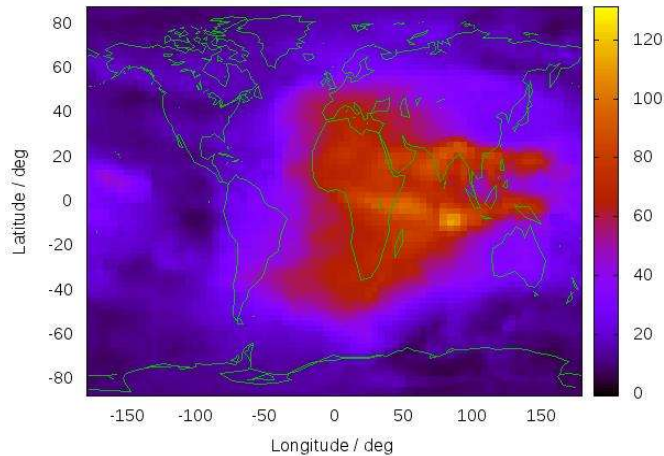
day 75 : 18 h

VTEC / TECU 20150317_076.36000



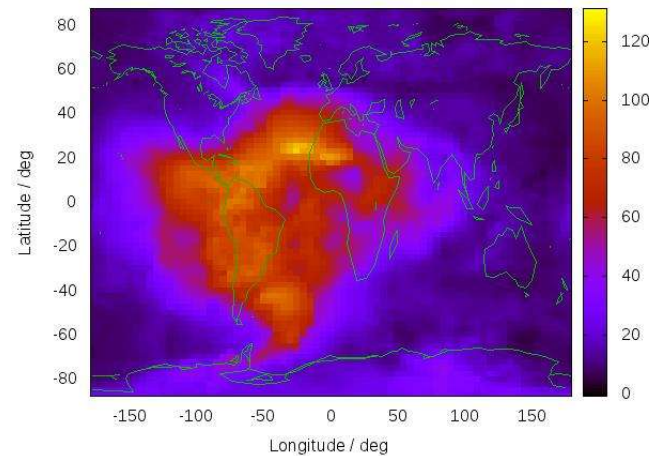
day 76 : 10 h

VTEC / TECU 20150317_076.43200



day 76 : 12 h

VTEC / TECU 20150317_076.64800



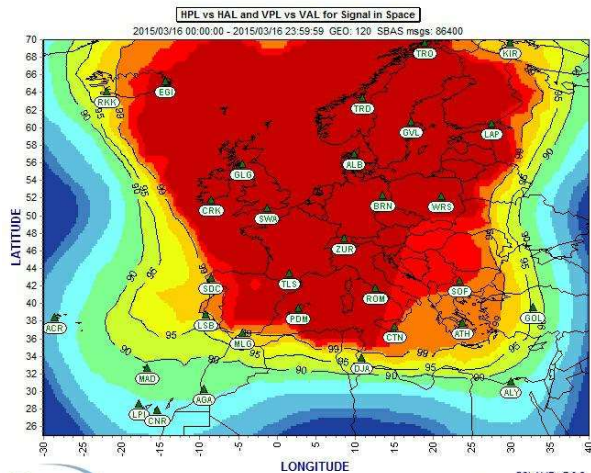
day 76 : 18 h



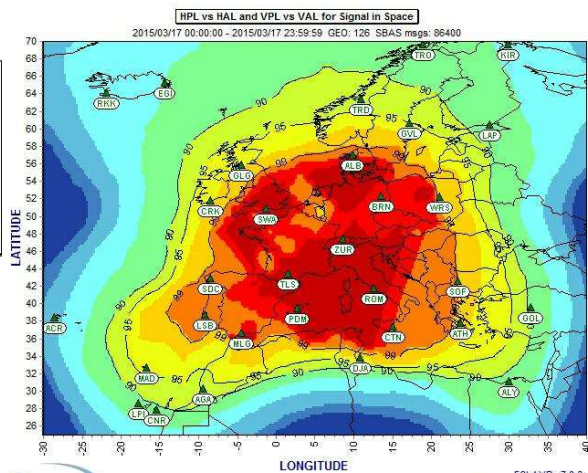
17/03/2015 (doy 76), to 21/03/2015 (day 80)

Availability maps

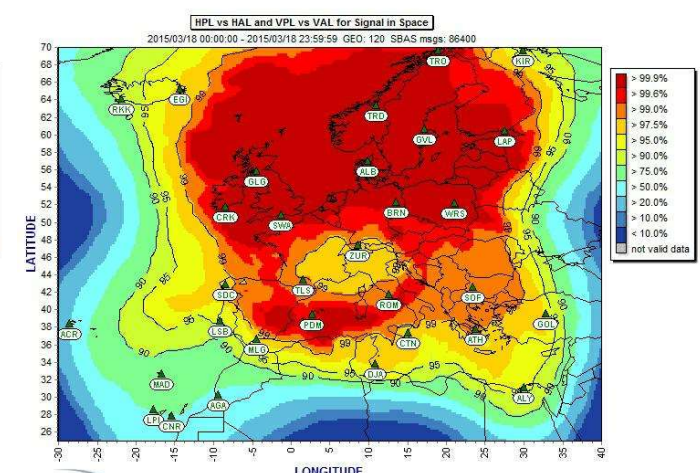
(from https://egnos-user-support.essp-sas.eu/new_egnos_ops/?q=apv1_availability)



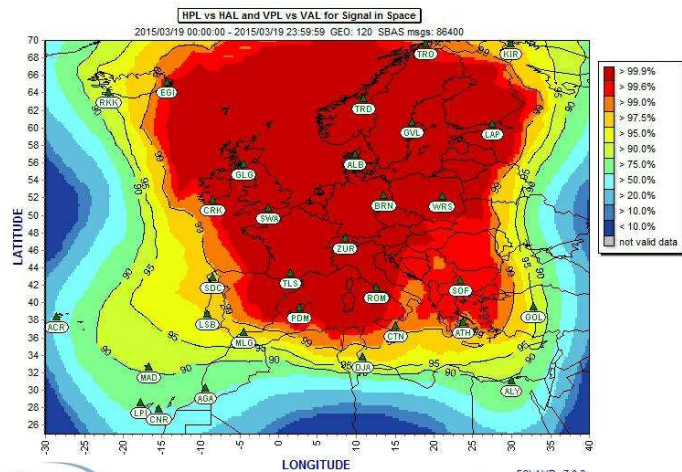
16 march



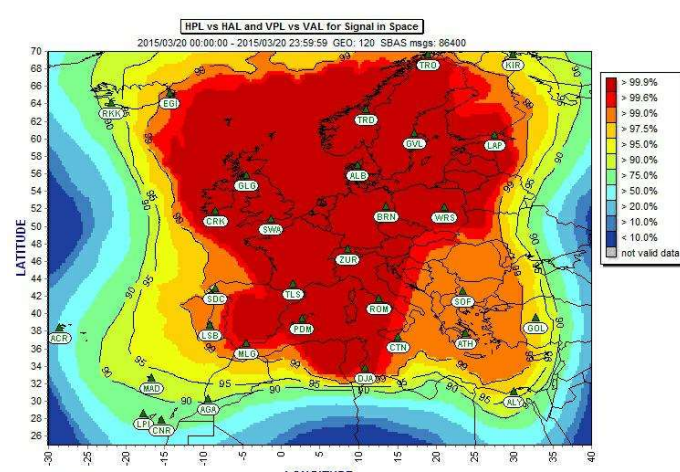
17 march



18 march



19 march



20 march

Conclusion

➤ **Scintillation occurrence & Probabilities**

- Low latitudes : The probability of scintillation events was derived depending on the season, latitude and local time for one and several satellites
- High latitudes : relationship to the magnetic activity

➤ **Raw data analysis**

- Fade and inter fades durations & probabilities were given, depending on the S4 value.
- Signal Correlation characteristics

➤ **Modelling : GISM (phase screen model)**

➤ **Extreme events (EGNOS performance loss)**

References

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- JP Adam, Y. Béniguel, N. Jakowski, T. Noack, V. Wilken, M. Cueto, A. Bourdillon, JJ. Valette, P. Lassudrie – Duchesne, B. Arbesser Rastburg, “Analysis of scintillations recorded during the PRIS measurement campaign”, *Ionospheric Effects Symposium, IES 2008*, 13 – 15 mai 2008, Alexandria, Va, USA
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