

Climate change: From basic nonlinear physics to policy-relevant science.

Tim Palmer

Department of Physics

University of Oxford



Suki Manabe: 2021 Nobel Prize for Physics



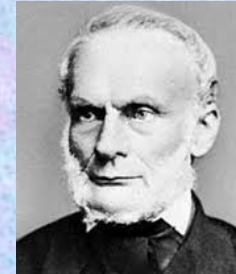
Comprehensive weather and climate models are based on the primitive laws of physics eg



$$\mathbf{F} = ma$$



$$E = \hbar\omega$$



$$\delta Q = TdS$$



We need climate models for:

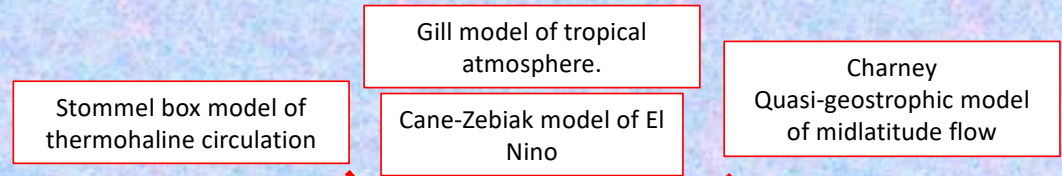
- **Understanding** (Of course!)
- **Mitigation** (How to transition to a decarbonised society.)
- **Adaptation** (How to make society more resilient to changing extremes of weather?)
- **Attribution** (Were observed weather events caused by climate change?)
- **Geoengineering** (Is there a Plan B?)

But is it all just



computing?

Model Hierarchy



Simple

Complex

$$\begin{aligned}\frac{dX}{dt} &= -10X + 10Y \\ \frac{dY}{dt} &= -XZ + 28X - Y \\ \frac{dZ}{dt} &= XY - \frac{8}{3}Z\end{aligned}$$

3-dimensional state space

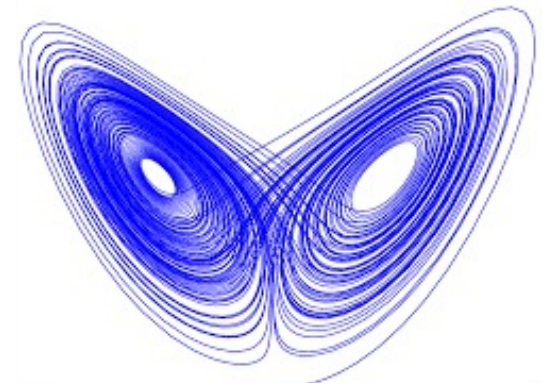
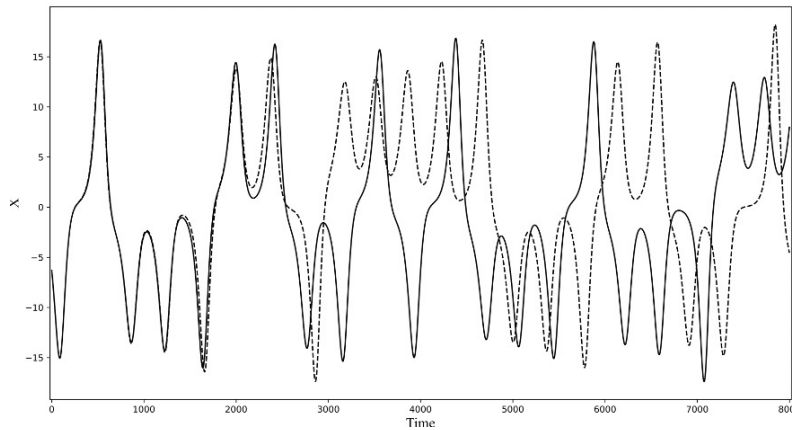
$$\rho \left(\frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) \mathbf{u} = \rho \mathbf{g} - \nabla p + \mu \nabla^2 \mathbf{u}$$

Infinite-dimensional state space.



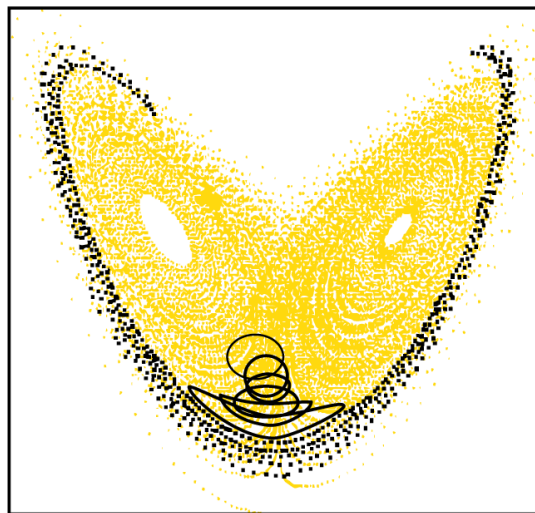
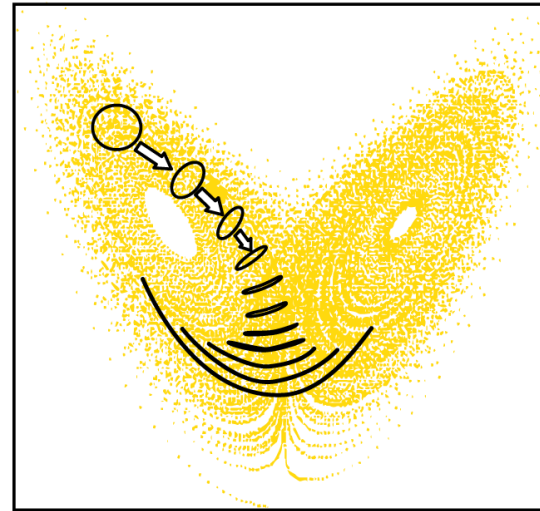
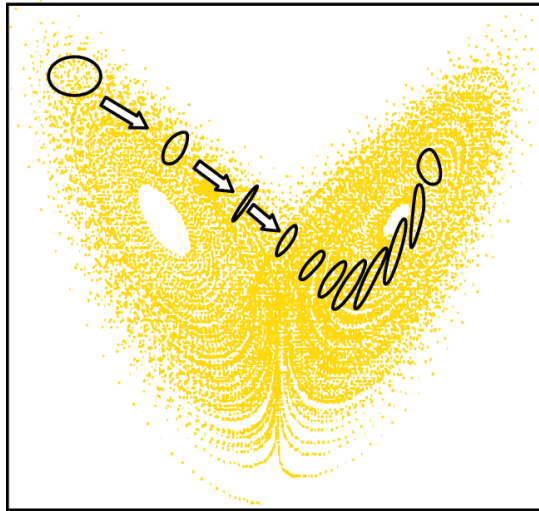


$$\begin{aligned}\frac{dX}{dt} &= -10X + 10Y \\ \frac{dY}{dt} &= -XZ + 28X - Y \\ \frac{dZ}{dt} &= XY - \frac{8}{3}Z\end{aligned}$$



The fractal Lorenz attractor

Sensitivity of Lorenz 1963 to initial conditions



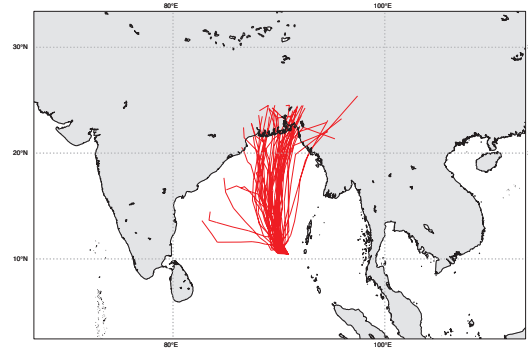
$$\frac{dX}{dt} = F[X]$$

\Rightarrow

$$\frac{d\delta X}{dt} = \frac{dF}{dX} \delta X$$

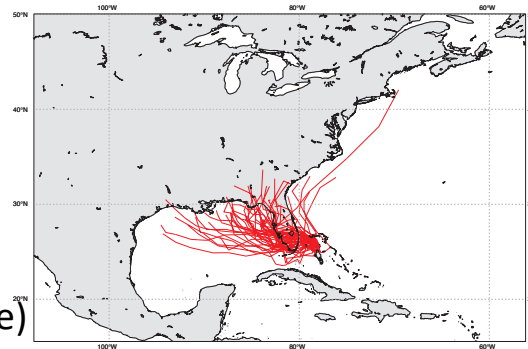
\Rightarrow the growth of
small perturbations
depends on X

Sidr
(predictable)

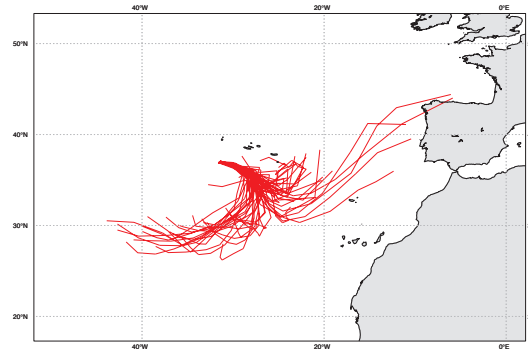


**Week-long
ensemble tropical
cyclone/hurricane
tracks.**

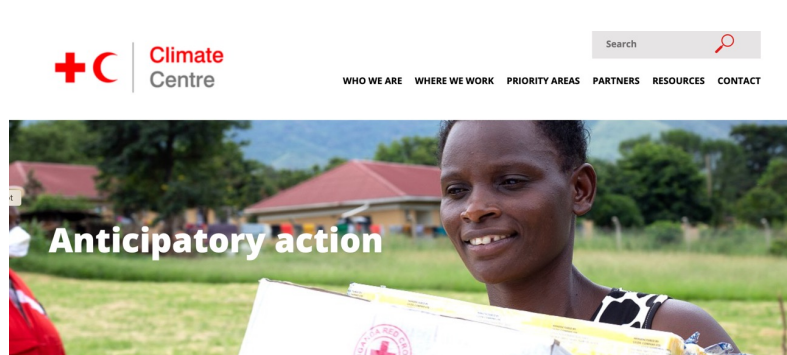
Katrina
(semi-predictable)



Nadine
(unpredictable)



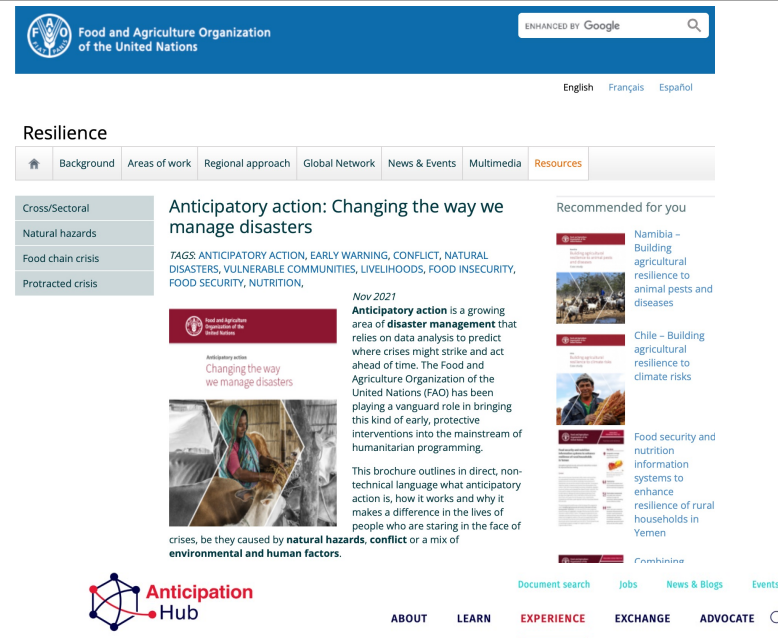
Take anticipatory action when probabilities of extreme weather exceed a predetermined threshold.



Anticipate, prepare, recover



“There’s a real, real change,” Dirk-Jan Omtzigt, chief economist at the UN Office for the Coordination of Humanitarian Affairs (OCHA), told The New Humanitarian in an interview after the conference. “Anticipatory action has always been niche and technical. Now it’s moving into the mainstream... It’s now being embraced by the community at large.”



Anticipatory action in the world

Acting prior to the onset of a predictable hazard to safeguard lives and livelihoods is now becoming increasingly accepted and gradually embedded within the humanitarian system and disaster risk management.

It has only been a few years since humanitarian agencies started to develop systems to take action based on forecasts and risk analysis in a small number of pilot countries. Since then this movement has kept on growing: There are now anticipatory action initiatives and projects in more than 60 countries in the world.



$$\rho \left(\frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) \mathbf{u} = \rho \mathbf{g} - \nabla p + \mu \nabla^2 \mathbf{u}$$

Resolved scales
←

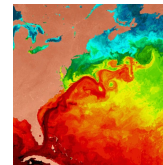
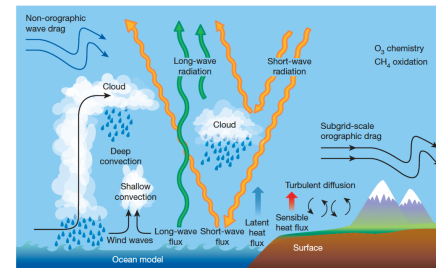
→
Unresolved scales

Dynamical Core



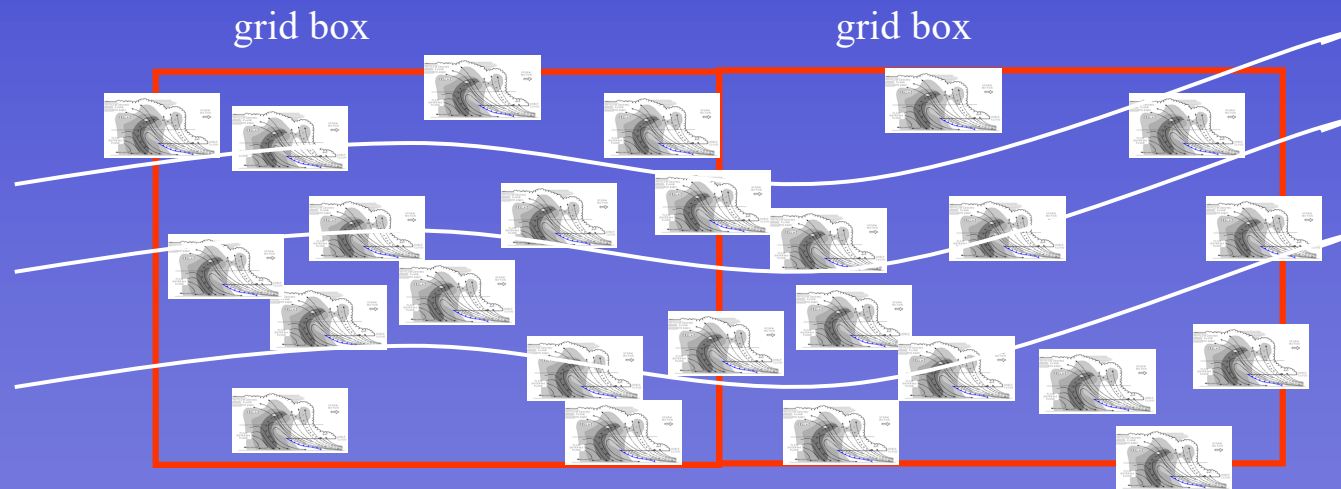
Parametrisations

$$P(X_{Tr}; \alpha)$$



$$D = P$$

Parametrisation based on the assumption that the world looks like this...



C.f. Statistical Mechanics

Navier Stokes

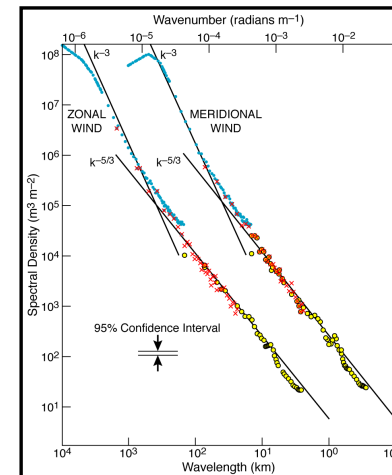
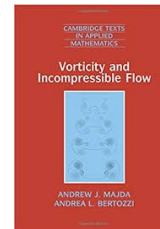
$$\rho \left(\frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) \mathbf{u} = \rho \mathbf{g} - \nabla p + \mu \nabla^2 \mathbf{u}$$

If $u(x,t)$ is the velocity field and $p(x,t)$ is the pressure field associated with a solution to the Navier-Stokes equations, then so is

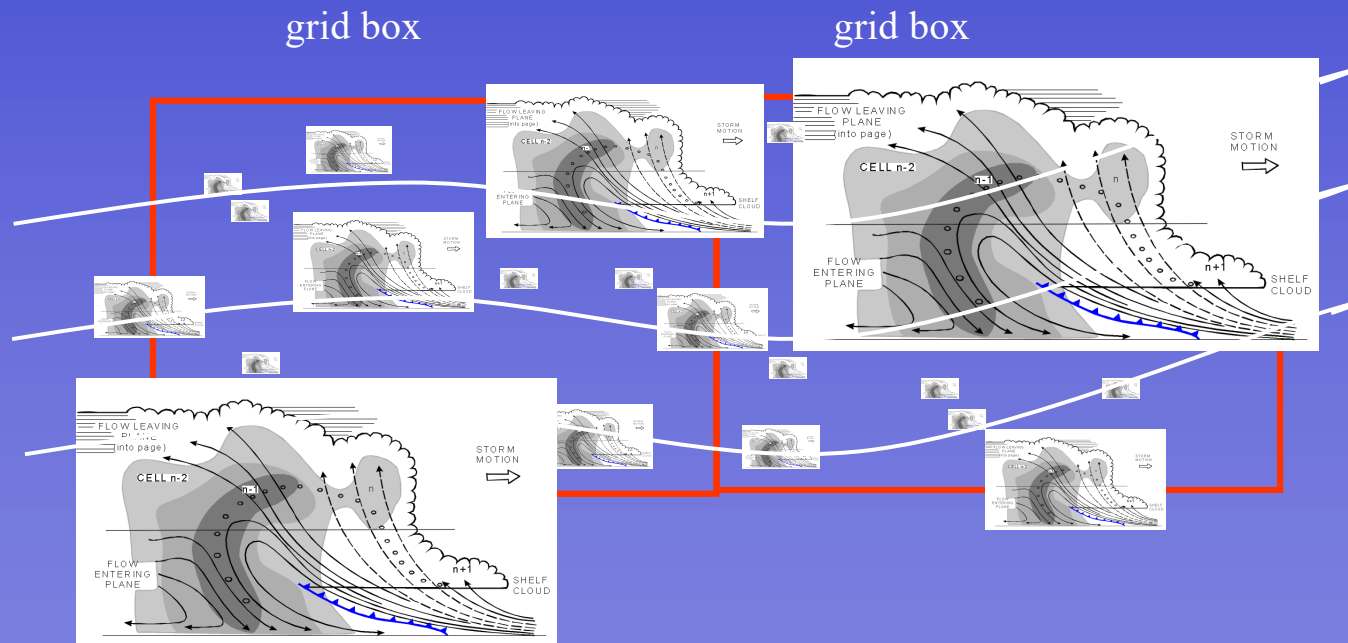
$$u_\tau(x,t) = \tau^{-1/2} u\left(\frac{x}{\tau^{1/2}}, \frac{t}{\tau}\right),$$

$$p_\tau(x,t) = \tau^{-1} p\left(\frac{x}{\tau^{1/2}}, \frac{t}{\tau}\right)$$

where $\tau > 0$ is a dimensionless scaling parameter.



The reality of the situation (consistent with power-law structures)



$$\rho \left(\frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) \mathbf{u} = \rho \mathbf{g} - \nabla p + \mu \nabla^2 \mathbf{u}$$

Resolved scales
←

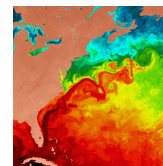
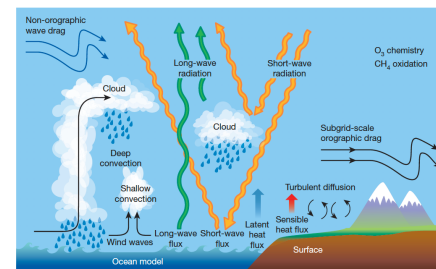
Dynamical Core



Unresolved scales
→


Stochastic
Parametrisations

$$(1 + r)P(X_{tr}; \alpha)$$



$$D = P$$

Stochastic weather and climate models

T. N. Palmer 

Abstract | Although the partial differential equations that describe the physical climate system are deterministic, there is an important reason why the computational representations of these equations should be stochastic: such representations better respect the scaling symmetries of these underlying differential equations, as described in this Perspective. This Perspective also surveys the ways in which introducing stochasticity into the parameterized representations of subgrid processes in comprehensive weather and climate models has improved the skill of forecasts and has reduced systematic model error, notably in simulating persistent flow anomalies. The pertinence of stochasticity is also discussed in the context of the question of how many bits of useful information are contained in the numerical representations of variables, a question that is critical for the design of next-generation climate models. The accuracy of fluid simulation may be further increased if future-generation supercomputer hardware becomes partially stochastic.

Global climate models extend weather forecast models to include a more comprehensive representation of chemical and physical processes, such as those occurring in the cryosphere and biosphere. Such climate models will help society become more resilient to changes in extremes of weather and climate on longer timescales, for several reasons. Through the Intergovernmental Panel on Climate Change Working Group I reports¹, such models will continue to be the primary scientific input for decisions on how fast the world economy must decarbonize to avoid the risk of increased weather and climate extremes caused by ongoing greenhouse gas emissions. In addition, because some level of anthropogenic climate change appears inevitable, climate models will play an important role at the national level in determining infrastructure investments needed to adapt societies to regional climate change as effectively as possible². Doing this requires knowledge, as accurate as possible, on changes to the likelihood of weather and climate extremes on the regional scale. There is also a concern that 'plan B' geoengineering proposals³, such as spraying sulfuric acid droplets into the stratosphere,

could detrimentally affect regional climate features such as monsoon rainfall. This can only be determined using reliable climate models. Furthermore, there is considerable interest in knowing whether specific extreme weather or climatic events can be attributed to human-induced climate change. However, such attributions depend critically on how accurately current-generation climate models simulate the circulation features associated with the types of extreme events under consideration⁴. In addition, irrespective of climate change, climate models play an increasingly important role in the prediction of climate variability on seasonal and decadal timescales⁵. The potential impact of such predictions (the predictability of which derives in large part from ocean–atmosphere coupling) is enormous. An ability to predict drought and flood reliably months or years in advance will be crucial for anticipating and mitigating crop failure⁶ and outbreaks of climate-related diseases, such as epidemic malaria⁷, or anticipating other climate-related impacts.

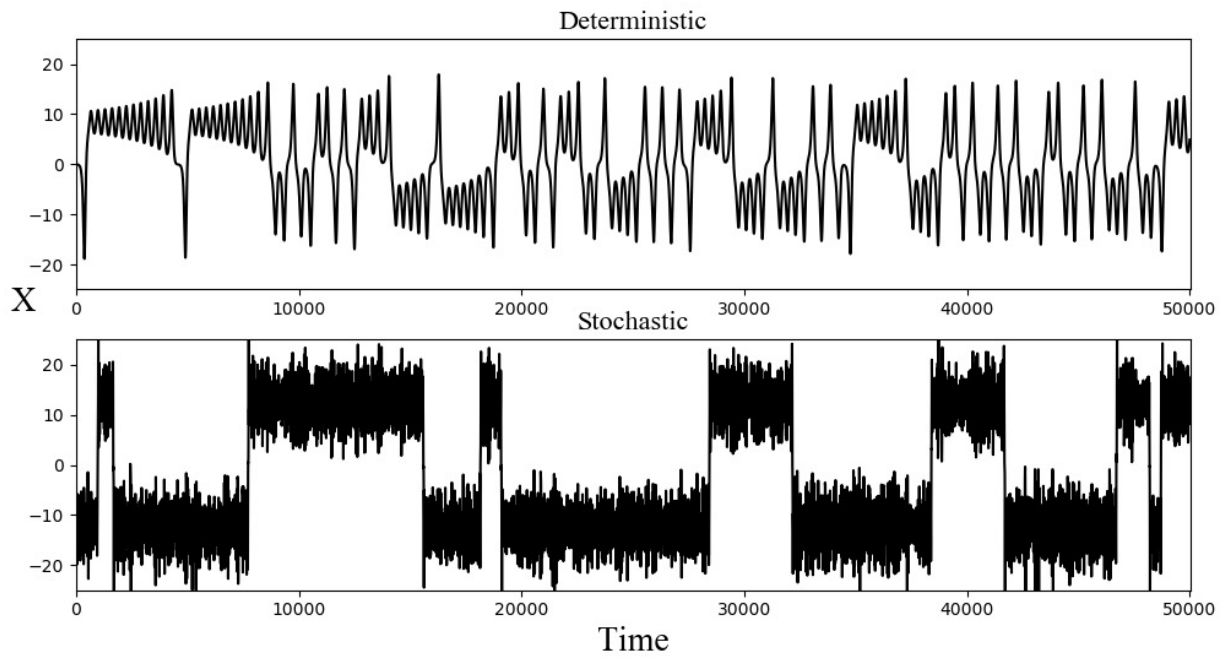
It is worth focusing on the notion of 'reliability'. There will always be uncertainties affecting the accuracy of any prediction

that is made about the weather or climate system, no matter the timescale⁸. The extent to which humankind will cut its greenhouse gas emissions is uncertain, as are the computational representations of the underlying equations of climate and the observations that determine the initial conditions of a prediction. Modern-day weather forecasting uses ensemble prediction methods to estimate the impact of these uncertainties⁹. In an ensemble forecast, typically 50 individual predictions are made from slightly different initial conditions. However, the spread generated in ensembles that only have initial perturbations is typically too small, particularly in the tropics, implying that the observed values fall outside the range of the ensemble too often. This implies that there is a second source of uncertainty, not represented in purely initial-condition ensembles: model uncertainty¹⁰. The representation of such model uncertainty is the topic of this Perspective.

An ensemble can be interpreted probabilistically using simple frequentism: if 40% of ensemble members predict a dry season over some region of interest, then, in the absence of model biases, the probability forecast of a dry season can be assumed to be 40%. If the a priori climatological probability of a dry season is, for instance, only 10%, then there may be some merit in farmers taking precautionary action by planting drought-resistant crops at the start of a growing season. However, the value to the farmer of such a decision — the seeds for which may be more expensive and produce smaller yields — depends critically on whether such probability forecasts are reliable. In this context, reliability¹¹ requires that, over a subsample of previous ensemble forecasts in each of which the probability of a dry season is 40%, then a dry season should have occurred 40% of the time. Because of model error, climate-timescale forecasts are not yet fully reliable¹².

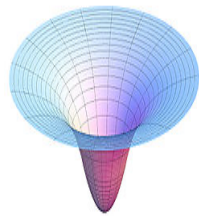
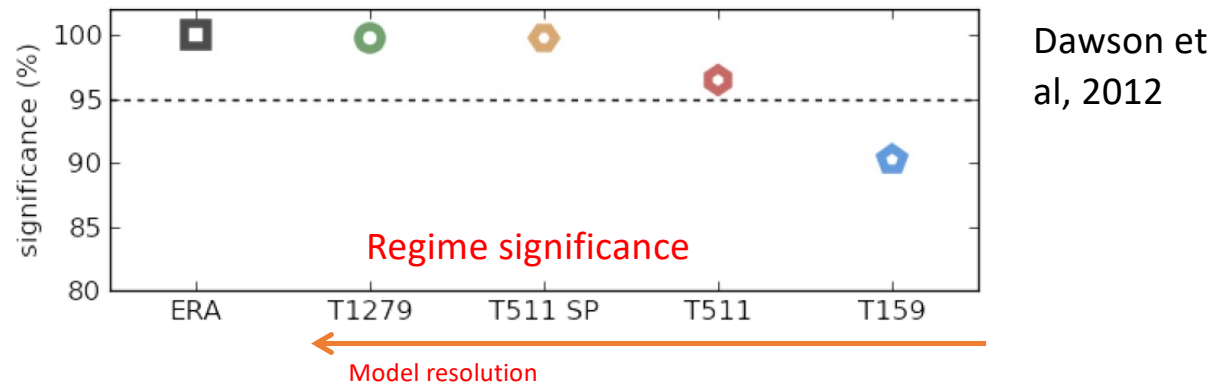
Of course, understanding how our climate system works is of great interest for its own sake, and comprehensive climate models are vital for scientific understanding. If reality can be simulated accurately with a fully comprehensive model, the essential ingredients needed to explain a particular climatic phenomenon can be discovered by removing inessential ingredients one

$$\begin{aligned}\frac{dX}{dt} &= -10X + 10Y + \eta_1 \\ \frac{dY}{dt} &= -XZ + 28X - Y + \eta_2 \\ \frac{dZ}{dt} &= XY - \frac{8}{3}Z + \eta_3\end{aligned}$$

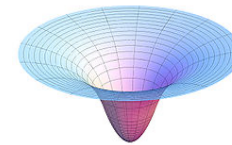


Adding noise to Lorenz 63 equations helps stabilize the regimes

Simulating Regimes in Comprehensive Climate Models



Both enhanced resolution topography and stochastic parametrisations help improve regime significance.



As potential wells, the regimes in contemporary climate models are too shallow.



Unusually calm and cloudy weather led to resurgence in fossil fuel use in 2021

Published: January 14, 2022 3.28pm GMT

2021 was an unusually calm year in British waters. Kaisn / shutterstock

✉ Email

Great Britain's wind turbines and solar panels both saw a drop in

Authors

Policy-relevant climate modelling is computationally expensive

- High-resolution stochastic atmosphere-ocean dynamical cores
- Ensembles
- Representations of cryosphere, biosphere, chemical cycles

Currently available HPC constrains what is possible



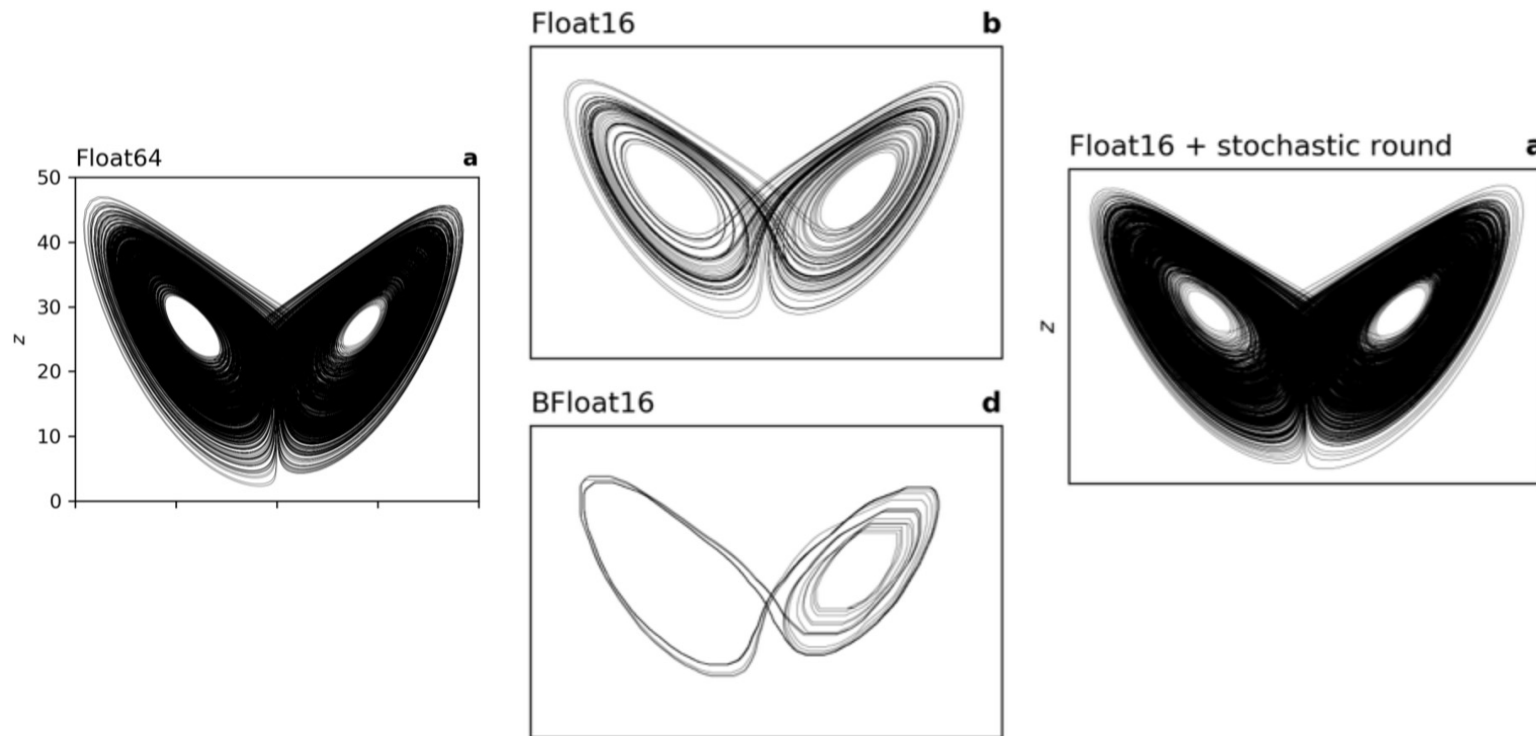
How can we make models cheaper?

Do we need 64-bit precision (default for traditional scientific computation) if the computational equations are stochastic?

Explosion of AI has seen development of 16-bit chips

Can we run high resolution climate models with 16-bit floating-point numbers?

Potential for a substantial (32 times) speed up?



Too periodic!

3-bit
deterministic 1-bit
deterministic 1-bit
stochastic

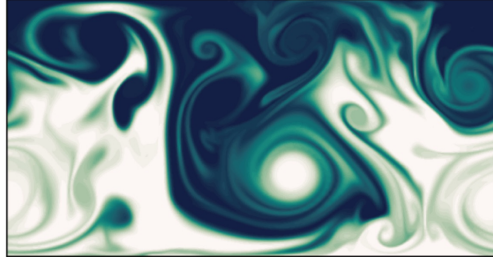
85%	85%	85%
70%	70%	70%
55%	55%	55%
45%		45%
30%		30%
15%		15%
	Deterministic rounding	Stochastic rounding

Noise can be a positive resource!

Integration of Shallow-Water Equations

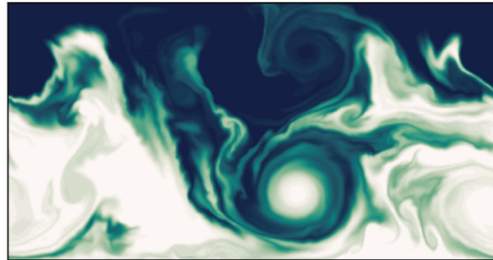
64 bit floats

Float64



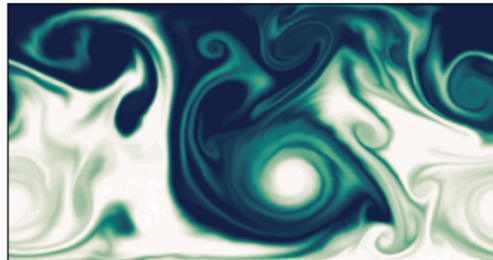
16 bit floats

Float16



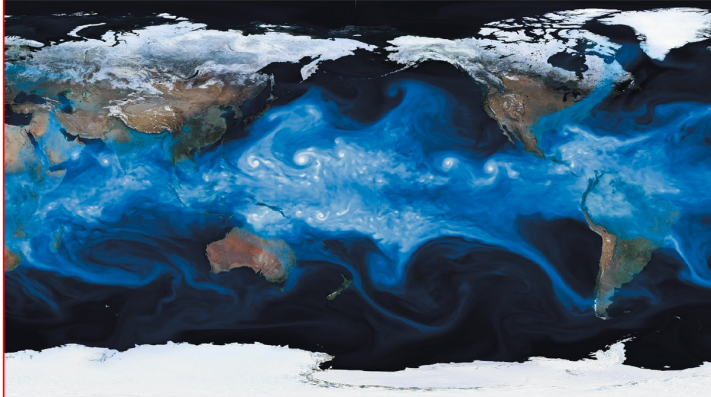
16 bit floats with
stochastic rounding

Float16 + stochastic rounding



Milan Klouwer

COMMENT



A simulation of Earth's atmosphere generated by the Community Atmosphere Model.

Build imprecise supercomputers

Energy-optimized hybrid computers with a range of processor accuracies will advance modelling in fields from climate change to neuroscience, says **Tim Palmer**.

Today's supercomputers lack the power to model accurately many aspects of the real world, from the impact of cloud systems on Earth's climate to the processing ability of the human brain. Rather than wait decades for sufficiently powerful supercomputers — with their potentially unsustainable energy demands — it is time for researchers to reconsider the basic concept of the computer. We must move beyond the idea of a computer as a fast but otherwise traditional Turing machine, churning through calculations bit by bit in a sequential, precise and reproducible manner.

In particular, we should question whether

input — and with the same high level of precision. I argue that for many applications they do not.

Energy-efficient hybrid supercomputers with a range of processor accuracies need to be developed. These would combine conventional energy-intensive processors with low-energy, non-deterministic processors, able to analyse data at variable levels of precision. The demand for such machines could be substantial, across diverse sectors of the scientific community.

MORE WITH LESS

Take climate change, for example. Estimates of Earth's future climate are based on solve

grid cells of 100 kilometres in width — can resolve the large, low-pressure weather systems typical of mid-latitudes, but not individual clouds. Yet modelling cloud systems accurately is crucial for reliable estimates of the impact of anthropogenic emissions on global temperature.

The resolution of this computational grid is determined by the available computing power. Current petaflop computers can perform up to 10^{15} additions or multiplications — floating-point operations — per second (flops). By the early 2020s, next-generation exaflop supercomputers, capable of 10^{16} operations per second, will be able to resolve the largest and most vic-

ILLUSTRATION BY JAMES HAMILTON FOR NATURE

Nature 2015

GRAPHCORE

Home About Products Industries Developer Blog Careers Get Started →

Designed for AI

INTELLIGENCE PROCESSING UNIT

The world's most complex processor, co-designed with Poplar software, so it's easy to deploy



10. HALF-PRECISION FLOATING POINT AND STOCHASTIC ROUNDING

The IPU supports IEEE half-precision floating-point numbers, and supports stochastic rounding in hardware. The IPU extensions to TensorFlow expose this floating point functionality through the functions described below. See the [Python API](#) for more details.

$$\rho \left(\frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \right) \mathbf{u} = \rho \mathbf{g} - \nabla p + \mu \nabla^2 \mathbf{u}$$

Resolved scales
←

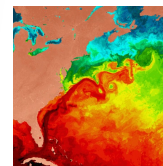
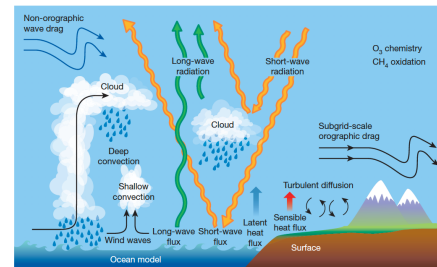
Dynamical Core



Unresolved scales
→

Stochastic
Parametrisations

$$(1 + r)P(X_{tr}; \alpha)$$



$$D = P$$

Replace
RHS
with 16-
bit AI.

Could Quantum Computers Help? Maybe.

arXiv > quant-ph > arXiv:2011.06571

Quantum algorithm for nonlinear differential equations

Seth Lloyd,^{1,2} Giacomo De Palma,^{1,2} Can Gokler,³ Bobak Kiani,^{2,4}
Zi-Wen Liu,⁵ Milad Marvian,⁶ Felix Tennie,⁷ Tim Palmer,⁷

1. Department of Mechanical Engineering, MIT, 2. Research Lab for Electronics, MIT,

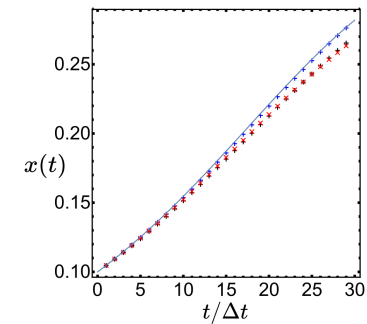
3. Engineering And Applied Sciences, Harvard University, 4. Department of Electrical Engineering and Computer Science, MIT,

5. Perimeter Institute, 6. Department of Electrical and Computer Engineering, Department of Physics, UNM

7. Department of Physics, University of Oxford

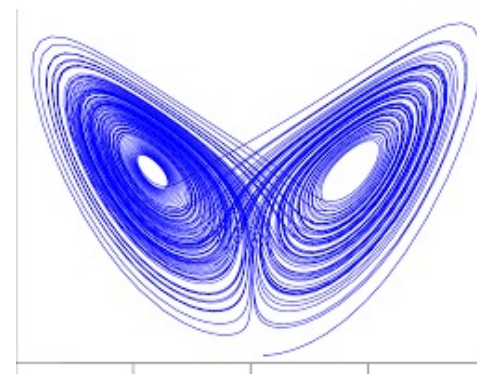
* to whom correspondence should be addressed: slloyd@mit.edu

Abstract: Quantum computers are known to provide an exponential advantage over classical computers for the solution of linear differential equations in high-dimensional spaces. Here, we present a quantum algorithm for the solution of *nonlinear* differential equations.



155 FIG. 3. Integration of $\dot{x} = x - 8x^3$. Comparison of a classical forward Euler solution (blue horizontal/vertical
156 crosses) with an ensemble-averaged solution (black horizontal/vertical crosses) and the quantum solver output
157 (red diagonal crosses). The solid blue line represents a Runge-Kutta method based solution. The step size was
158 chosen as $\Delta t = 0.05$ and the quantum solver was initialised with $N = 10$ identical copies.

Work in progress:

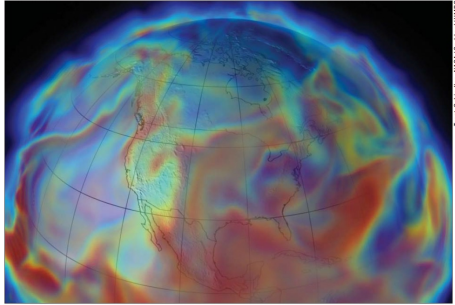


A CERN for climate change

Providing reliable predictions of the climate requires substantial increases in computing power. **Tim Palmer** argues that it is time for a multinational facility fit for studying climate change

This winter has seen unprecedented levels of travel chaos across Europe and the US. In particular, the UK experienced some of the coldest December temperatures on record, with snow and ice causing many airports to close. Indeed, George Osborne, the UK's Chancellor of the Exchequer, attributed the country's declining economy in the last quarter of 2010 to this bad weather. A perfectly sensible question to ask is whether this type of weather will become more likely under climate change? Good question, but the trouble is we do not know the answer with any great confidence.

The key point is that the cold weather was not associated with some "global cooling" but with an anomalous circulation pattern that brought Arctic air to the UK and other parts of Europe. This very same circulation pattern also brought warm temperatures to parts of Canada and south-east Europe. Global mean temperatures were barely affected. Weather-forecast models, which only have to predict a few days ahead at a time, are able to represent this level of detail very well. Global climate models, however, such



A global approach to a global problem Modelling the climate may require a unified strategy for computing.

to be able to resolve deep convective cloud systems, known to be crucial in transporting heat moisture and momentum from the planet's surface into the high troposphere, a climate simulator needs to have a grid-point spacing of at least 1 km. But we cannot say, short of actually doing the numerical experiments with such a grid, how much more accurate a climate simulator would be if these deep convective clouds could be properly represented by the laws of physics, rather

than by parameterizations. The technical challenges will be great, requiring dedicated supercomputers faster than the best today. Greater international collaboration will be needed to pool skills and funds. Against the cost of mitigating climate change — conceivably trillions of dollars — investing, say, one quarter of the cost of the Large Hadron Collider (whose annual budget is just under US\$1 billion) to reduce uncertainty in climate-change projections is surely warranted. Such an investment will also improve regional estimates of climate change — needed for adaptation strategies — and our ability to forecast extreme weather.

Physics World



Local effects such as thunderstorms, crucial for predicting global warming, could be simulated by fine-scale global climate models.

Build high-resolution global climate models

International supercomputing centres dedicated to climate prediction are needed to reduce uncertainties in global warming, says Tim Palmer.

The drive to decarbonize the global economy is usually justified by appealing to the precautionary principle: reducing emissions is warranted because the risk of doing nothing is unacceptably high. By emphasizing the idea of risk, this framing recognizes uncertainty in the magnitude and timing of global warming. This uncertainty is substantial. If warming occurs at the upper end of the range projected in the Intergovernmental Panel on Climate Change (IPCC) Fifth Assessment Report¹, then unmitigated climate change will probably prove disastrous worldwide, and rapid global decarbonization is paramount. If warming occurs at the lower end of this range, then decarbonization could proceed more slowly and some societies' resources may be better focused on local adaptation measures. Reducing these uncertainties substantially will take a new generation of global climate simulators capable of resolving finer details,

including cloud systems and ocean eddies. The technical challenges will be great, requiring dedicated supercomputers faster than the best today. Greater international collaboration will be needed to pool skills and funds. Against the cost of mitigating climate change — conceivably trillions of dollars — investing, say, one quarter of the cost of the Large Hadron Collider (whose annual budget is just under US\$1 billion) to reduce uncertainty in climate-change projections is surely warranted. Such an investment will also improve regional estimates of climate change — needed for adaptation strategies — and our ability to forecast extreme weather.

GRAND CHALLENGES
The greatest uncertainty in climate projections is the role of the water cycle — cloud formation in particular — in amplifying or damping the warming effect of CO₂ in the atmosphere. Clouds are influenced strongly

by two types of circulation in the atmosphere: mid-latitude, low-pressure weather systems that transport heat from the tropics to the poles, and convection, which conveys heat and moisture vertically. Global climate simulators calculate the evolution of variables such as temperature, humidity, wind and ocean currents over a grid of cells. The horizontal size of cells in current global climate models is roughly 100 kilometres. This resolution is fine enough to simulate mid-latitude weather systems, which stretch for thousands of kilometres. But it is insufficiently fine to describe convective cloud systems that rarely extend beyond a few tens of kilometres. Simplified formulae known as 'parameterizations' are used to approximate the average effects of convective clouds or other small-scale processes within a cell. These approximations are the main source of errors and uncertainties in climate

Elena Cornelli

La tragedia della Marmola da il Nòva 24, ma anche le inondazioni in Bangladesh che hanno distrutto il villaggio Ilmescoro, dipendono dalla crisi del clima dovuta alle emissioni delle relative emissioni di gas a effetto serra. «Quello che sta succedendo in questo periodo è perfettamente coerente con le previsioni dei modelli climatici che abbiamo a disposizione: la situazione è destinata a peggiorare nei prossimi anni, se non si prendono drastiche provvedimenti per fermare le emissioni», spiega Tim Palmer, fisico dell'Università di Oxford, che sarà domani in Italia per intervenire al colloquio di Trieste per il centenario dell'Unione internazionale di Fisica Pura ed Applicata.

Palmer è un pioniere della modellistica climatica: è stato fra i primi a sviluppare la previsione pro-

ca climatica potrà produrre previsioni abbastanza accurate da mettere a disposizione degli Stati, per prendere le decisioni giuste nella gestione del territorio davanti a questa crisi epocale.

«Per fare un esempio pratico, tanti modelli concordano sul futuro del clima in Italia: sappiamo che nei prossimi anni il clima del Sud Europa è in particolare quello che ha lo scenario più preoccupante, perché più caldo e secco, con le conseguenze di cui vediamo le premesse già oggi. Di conseguenza, il governo italiano su quali misure andrebbero prese per affrontare la crisi del clima deve basarsi sui dati dei suoi supercomputer e i modelli.

«Questo problema non interessa solo l'Italia, ma molte altre del mondo, che saranno anche le più colpite dalla crisi. «Se le temperature si comportano come si comportano a vivere. Nelle zone tropicali e subtropicali, comprese alcune zone del Medio Oriente, le ondate di caldo invece porteranno un esodo di massa probabilmente già a metà di questo secolo. Solo preparando i questi eventi con modelli accurati abbiamo una possibilità di evitare l'irrimediabile di massa del rifugiato climatico», sottolinea Palmer. La crisi climatica impedisce di vedere le possibilità, per questo ne sappiamo oggi, sono coerenti con la

crisi del clima. «Questo diventa un problema per le misure di adattamento, perché i governi non capiscono quali infrastrutture costruiranno, non sappiamo se si devono difendere dalla siccità o dalle inondazioni», fa notare Palmer.

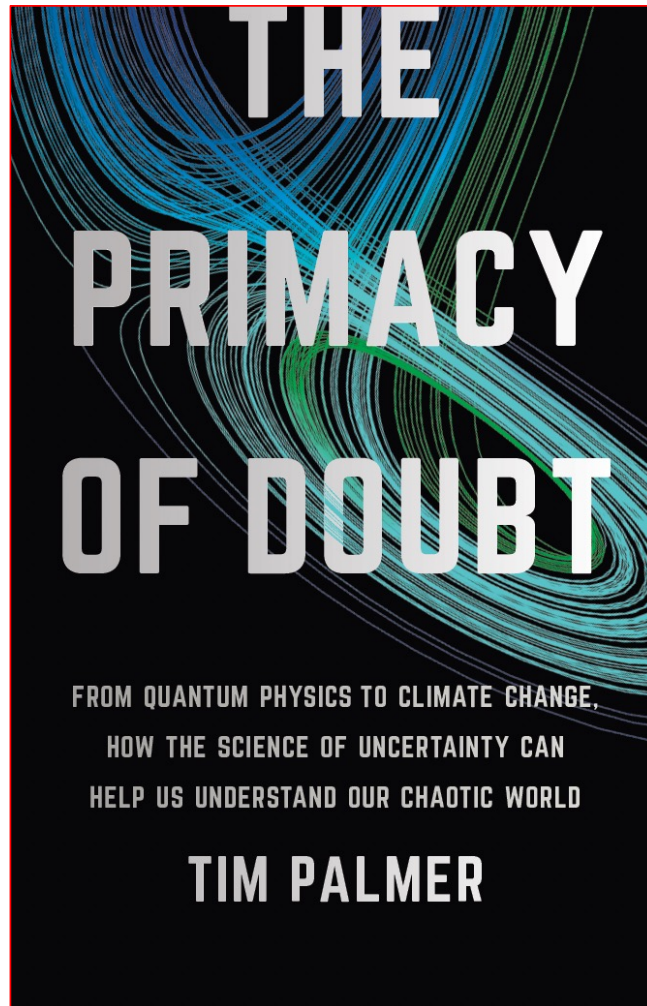
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TIM PALMER
Fisico dell'Università di Oxford, è uno dei pioniere della modellistica climatica: è stato fra i primi a sviluppare la previsione pro-

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