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#### "Application for Retrieval Theory to the EOS Microwave Limb Sounder (MLS)"

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Please note: These are preliminary notes intended for internal distribution only.

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# Application of retrieval theory to the EOS Microwave Limb Sounder (MLS)

Inverse methods in atmospheric science.

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1–12 October 2001 (v1.5)

#### Outline of talk.

- Description of the EOS MLS instrument.
- □ Overview of retrieval problem, construction of vectors etc.
- Issues related to retrieval 'phasing' and constrained quantity error propagation.
- A 'two dimensional' approach to the retrieval problem.
- A discussion of forward model issues.
- Issues related to 'noisy' products (if time).
- □ Implementation of the algorithms in software.
- □ Some initial results from the algorithms.
- □ Plans for future development.

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#### The EOS MLS instrument.

- □ The EOS MLS instrument is a follow on to the successful MLS instrument flown on UARS, launched in 1991.
- □ It is designed to measure aspects of the chemistry and dynamics of the stratosphere and upper troposphere.
- □ It will fly on the EOS Aura platform, along with the HIRDLS, OMI and TES instruments.
- □ The Aura launch is currently scheduled for July 2003.
- EOS MLS is designed, built and calibrated by the Jet Propulsion Laboratory.
- □ The instrument uses the *Microwave Heterodyne* technique (described later) to measure thermal emission from the earth's limb.

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#### Some aspects of microwave limb sounding.

One major difference between microwave sounding and some other techniques (e.g. infrared radiometry) is that spectral lines are easily resolved.

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- □ In the stratosphere and troposphere spectral line shapes are dominated by pressure broadening effects, as opposed to Doppler broadening.
- □ Lines broaden by ~3 MHz per hPa.
- □ Most information comes from observations of *spectral contrast* (the shape of the line), as opposed to absolute radiance (*baseline* effects).
- □ So, for example if we can resolve lines with widths up to 1 GHz, we can sound down to 300 hPa.
- Once the lines get broader than we can resolve issues of absolute radiance come into play, and errors get larger.
- **Q** Radiances described in terms of a *brightness temperature*, in Kelvins.
- □ Observed radiance can thus be a rough indication of the temperature in regions where the radiances saturate (black-out).

#### The microwave heterodyne technique.



# The EOS MLS instrument. GHz module GHz antenna THz module Spectrometer module

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## **EOS MLS Receivers.**

- EOS MLS contains 7 microwave receivers, measuring radiation in the regions around
  - **118 GHz** (two redundant receivers) measuring  $O_2$  emission for temperature/pressure.
  - **190 GHz** measuring some stratospheric species and upper tropospheric water.
  - **240 GHz** mainly intended for measurements of CO and upper tropospheric O<sub>3</sub>.
  - 640 GHz the main stratospheric chemistry 'workhorse'.
  - 2.5 THz (two receivers) for measuring stratospheric OH.
- □ The 118 GHz receiver is a single sideband receiver, all the others are double sideband.

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## **EOS MLS Spectrometers.**

□ The signals from each receiver are sent to several spectrometers.

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- □ These are centered on various spectral lines of interest.
- □ EOS MLS has four different types of spectrometers.
  - **FB25** A filter bank containing 25 discrete channels, with narrow (6 MHz) channels near the line center, broadening to 96 MHz in the at 575 MHz away from line center.
  - **MB11** A filter bank containing only 11 channels, corresponding to the center 11 in the FB25 spectrometers.
  - **DACS** Digital auto-correlating spectrometers, giving  $\sim$ 0.2 MHz resolution over 10 MHz
  - **WF4** These consist of four 500 MHz wide channels judiciously placed within the IF spectrum.



#### Overview of the retrieval process.

Like most instruments the EOS MLS data are divided into 'Levels'.
 Level 0 Raw data from the instrument.

Level 1 Calibrated radiances.

Level 2 Geophysical data along the orbit / tangent point track.

Level 3 Geophysical data mapped onto some regular lat/lon grid.

- □ The rest of this talk concerns the Level 2 processing.
- **D** The method applied is the standard *optimal estimation* approach.
- While we have some new approaches to the problem, the fundamental mathematical approach is standard.

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#### The EOS MLS Orbit and scan.

- □ Aura will fly in a 98° inclined sun-synchronous orbit, performing ~14.5 orbits per day.
- EOS MLS observes the limb directly in front of the spacecraft.
  - ➡ This has interesting and very useful implications to be discussed later in this presentation.
- □ The GHz and THz telescopes make a complete vertical scan of the atmosphere every ~24 seconds.
- □ The scan pattern is designed that the observed latitudes are essentially unchanged from orbit to orbit.
- □ All parts of the globe are measured twice per day.
   ⇒ Once on an ascending orbital node, once descending.
- □ There are plans to have Aqua, Aura, Cloudsat and other platforms fly in formation.

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□ This will allow for near simultaneous observations.

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## The retrieval equation.

- $\Box$  We choose to represent the state of the atmosphere by the vector **x**.
- Radiances from various bands within the instrument are gathered into measurement vectors y<sub>i</sub>, with (typically diagonal) covariances S<sub>i</sub>.
- □ The standard *Gauss Newton* iteration is given by

$$x^{(r+1)} = x^{(r)} + \left[\sum_{i} K_{i}^{T} S_{i}^{-1} K_{i}\right]^{-1} \sum K_{i}^{T} S_{i}^{-1} \left[y_{i} - f_{i}(x^{(r)})\right]$$

where  $f_i$  is the *forward model*, and

$$K_i = \frac{\partial f_i(x)}{\partial x}$$

is the matrix of weighting functions or Jacobians.

□ The solution covariance is given by

$$S_{\textbf{x}} = \left[\sum_{i} K_{i}^{T} S_{i}^{-1} K_{i}\right]^{-1}$$

#### Virtual measurements and a priori.

- □ As it stands, the matrix inversion above is typically not possible.
  - ⇒ There are aspects of the state vector for which the measurements have yielded no information.
- □ We introduce *virtual measurements,* in the form of *a priori* estimates of the state vector values.
- □ It will later prove useful to make these separate measurements, rather than one of the  $y_i$  vectors.
  - $\Rightarrow$  The vector **a** is a *virtual measurement* of **x** with covariance  $S_a$ .
- □ The iteration thus becomes

$$\begin{aligned} \mathbf{x}^{(r+1)} &= \mathbf{x}^{(r)} + \left[ \mathbf{S}_{a}^{-1} + \sum_{i} \mathbf{K}_{i}^{\mathsf{T}} \mathbf{S}_{i}^{-1} \mathbf{K}_{i} \right]^{-1} \\ & \left\{ \mathbf{S}_{a}^{-1} \left[ \mathbf{a} - \mathbf{x}^{(r)} \right] + \sum_{i} \mathbf{K}_{i}^{\mathsf{T}} \mathbf{S}_{i}^{-1} \left[ \mathbf{y}_{i} - \mathbf{f}_{i}(\mathbf{x}^{(r)}) \right] \right. \end{aligned}$$

□ For elements of x that don't need a priori information, the corresponding rows and columns of  $S_{\alpha}$  are set to zero.

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#### Construction of the MLS state vector (cont.)



#### Construction of the MLS state vector.

- The most important components of the MLS state vector are the temperature and composition of the atmosphere, as a function of pressure.
   These are the *standard products* from MLS.
- Note that we use a pressure grid as opposed to a height grid.
- □ In addition, we include the geopotential height of a single pressure surface (e.g. 100 hPa).
  - ➡ To include a complete profile of geopotential height is unnecessary, as the temperature profile already conveys this information.
- □ However, the forward model requires more information in order to model radiances.
- The most important information is the atmospheric pressure at each tangent point.
- □ Also, the angular offset between the various MLS radiometers fields of view is required.

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#### Sizing the MLS retrieval task.

- □ Consider the retrieval of a single MLS ozone profile from one scan's worth of MLS 205 GHz ozone observations.
- □ Retrieve ozone at 12 surfaces per decade from 1000 hPa to 0.1 hPa. □ Length of state vector  $\mathbf{x}$ ,  $\mathbf{n} = 48$
- □ We use 120 minor frames worth of radiances from 25 channels. ⇒ Length of measurement vector  $\mathbf{y}$ ,  $\mathbf{m} = 3000$
- □ The linear form of the optimal estimation equation gives:

$$\mathbf{x} = \mathbf{a} + \begin{bmatrix} \mathbf{S}_{\mathbf{a}}^{-1} + \mathbf{K}^{\mathsf{T}} & \mathbf{S}_{\mathbf{y}}^{-1} \mathbf{K} \end{bmatrix}^{-1} \mathbf{K}^{\mathsf{T}} & \mathbf{S}_{\mathbf{y}}^{-1} (\mathbf{y} - \mathbf{f})$$
$$\mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \begin{bmatrix} \mathbf{f} + \mathbf{f} & \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \mathbf{f} \end{bmatrix}^{-1} \mathbf{f} = \mathbf{f} + \mathbf{f}$$

#### Sizing the MLS retrieval task (cont.)

- $\Box$  a is the *a priori* state vector with  $n \times n$  covariance matrix  $S_a$ .
- □ **f** is the forward model measurement vector, (the predicted radiances corresponding to the *a priori* state.
- $\Box$  S<sub>y</sub> is the m  $\times$  m measurement covariance matrix.
- $\Box$  K is the m  $\times$  n matrix of *weighting functions*:

$$\mathbf{K} = \frac{\partial \mathbf{y}}{\partial \mathbf{x}}$$

□ The most time consuming aspects of the calculation are the inversion of  $S_{\mu}$ . (m<sup>3</sup>) and the computation of  $K^T S_{\mu}^{-1} K$  (n<sup>2</sup>m + m<sup>2</sup>n).

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 $\Box$  However, if S<sub>y</sub> is diagonal, we are left with only  $n^2m + nm + m$ .

#### The measurement covariance matrix Sy.

- $\Box$  Clearly, having  $S_y$  as a diagonal matrix would be a real advantage.
- $\Box$  What does is mean if the  $S_y$  matrix is diagonal?
  - $\Rightarrow$  The 'errors' in the radiances are all uncorrelated.
  - ➡ If the radiance in channel 0 is 'too high' that doesn't mean that channel 1 is any more or less likely to also be too high.
- □ What causes non diagonal covariance matrices?
  - ⇒ Certain instrumental effects such as gain variation. These can be taken into account by retrieving quantities such as 'baseline'.
  - ➡ The use of constrained quantity error propagation in multi-phase retrieval processes.

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#### Constrained quantity error propagation.

- □ Many previous retrieval algorithms (e.g. UARS MLS, ISAMS) implemented a multi-phase approach
  - $\Rightarrow$  e.g. a retrieval of temperature/pressure first, from O<sub>2</sub> radiances,
  - ➡ followed by retrievals of various species, using the temperature and pressure data from the earlier phase in the forward model.
- □ The previously retrieved quantities *c* (e.g. temperature and pressure) are *constrained* in the later phases.
- $\Box$  However, our knowledge of these quantities is not perfect, they have a covariance  $S_c$ , estimated by the early phase.
- □ This uncertainty needs to be propagated through the forward model into an additional radiance uncertainty.
- $$\label{eq:should modify our } \begin{split} & \square \mbox{ We should modify our } S_y \mbox{ matrices in the later phases according to } \\ & S_y \mbox{ } \to S_y \mbox{ + } K_c S_c K_c^T \mbox{, where } K_c \mbox{ describes the sensitivity of the radiances to these constrained quantities } \\ & K_c \mbox{ = } \partial y / \partial c. \end{split}$$

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#### Constrained quantity error propagation (cont.)

- $\Box$  This will make  $S_y$  non-diagonal.
  - ➡ If the temperature we are using is too high, then all the forward model radiances will be too large 'in concert'.
- $\hfill\square$  One could choose to ignore the non-diagonal elements of the new  $S_{\psi}$  matrix.
- □ However, previous experience has shown that this can be a poor approximation.
  - ⇒ The retrieval algorithm puts less 'trust' in the measurements than they deserve.
- □ Is there an alternative approach which avoids the costly calculations, and yet retains accuracy?

#### A new approach to multi-phase retrievals.

- $\Box$  Avoiding constrained quantity error propagation makes  $S_{u}$  diagonal.
- Instead we retrieve everything at once from every channel.
- However, as the real MLS system is non linear, we may have to perform several iterations on this 'big' system.
- □ To improve the efficiency, we re-introduce phasing with a new twist.
- □ In the early phases we retrieve the most non-linear quantities (those needing several iterations to converge) from appropriate bands.  $\Rightarrow$  For example, retrieve temperature and pressure from O<sub>2</sub> radiances.
- Once a good estimate is obtained for these quantities, add more linear items to the state and measurement vectors, while still retrieving the earlier quantities.
- □ This larger system will need fewer iterations to converge, as the nonlinear quantities are already close to the solution.
- □ Think of the earlier phases getting 'initial guesses' for the final phase. 20

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## Dividing the data processing into chunks.

- $\Box$  We process the data in chunks of ~1/8–1/4 orbit in length.
- $\Box$  The measurement vectors  $\mathbf{y}_i$  contain information from M scans.
- $\Box$ . The state vector **x** describes N vertical profiles.
- $\Box$  Typically we choose N = M but this is not a requirement.
- The chunks to overlap slightly, to account for 'edge' effects.
- $\Box$  We have q profiles of overlap (e.g. 3) giving Q = N 2q non overlapped profiles per chunk.



#### A 'two dimensional' approach.

- Unlike UARS MLS, the EOS MLS instrument looks forward from the spacecraft.
- □ This means that all the observations are within the orbital plane. ⇒ Although the rotation of the earth has an impact on this.
- Each limb ray is affected by the state of the atmosphere over a ~1000 km path length.
- □ This corresponds to several adjacent retrieved profiles.
- Note that the scan can be arranged to stack the tangent points in a vertical profile.
  - $\Rightarrow$  As you scan up, the tangent point gets closer to you.
  - $\Rightarrow$  If this happens at the same rate as the spacecraft moves forward, the tangent point locus is vertical.
- □ In the EOS MLS case, we scan slowly through the troposphere and lower stratosphere, then speed up in the upper stratosphere and mesosphere.
- How can we devise an algorithm that takes most advantage of this geometry?

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## Weighting functions for this problem.

- The efficiency gain in this case comes from noting that the weighting function matrices  $K_i$  are very sparse.
- □ For example, the values of temperature for profile 1 have no effect on the radiances for scan 10.
- $\Box$  This gives a block structure for K<sub>i</sub> similar to.

$$\mathbf{K}_{i} = \frac{\partial \mathbf{y}_{i}}{\partial \mathbf{x}} = \bigcup_{i=1}^{N} \begin{bmatrix} Profiles \longrightarrow i \\ \times & \times & 0 & 0 & 0 \\ 0 & \times & \times & 0 & 0 \\ 0 & 0 & \times & \times & 0 \\ 0 & 0 & 0 & \times & \times & 0 \\ 0 & 0 & 0 & 0 & \times & \times \\ 0 & 0 & 0 & 0 & 0 & \times & \times \end{bmatrix}$$

U Where 'profile' is taken to mean the complete state (temperature and composition profiles) for one location.

# $K_i^T S_i^{-1} K_i$ , the 'Normal equations'.

 $\Box$  Given the form for K<sub>i</sub> shown above, and assuming S<sub>i</sub> is diagonal (more on this later), the matrix  $K_i^T S_i^{-1} K_i$ , needed in the retrieval, is of the form:

		Pro	ofile	s —	$\rightarrow$			
	_p[	×	х	х	0	0	0	]
	<u>ਤ</u>	×	х	×	х	0	0	
$\mathbf{K}_{i}^{T}\mathbf{S}_{i}^{-1}\mathbf{K}_{i} =$	les	х	×	х	Х	Х	0 0 × × × ×	
$\mathbf{x}_i \mathbf{s}_i \mathbf{x}_i =$		0	Х	х	х	Х	×	
	$\downarrow$	0	0	Х	×	х	×	
		0	0	0	×	х	×	

- We know that we can ignore any block products involving absent (completely 0) blocks in K<sub>i</sub>
- This matrix is sometimes known as the matrix of normal equations.
- **Given a matrix**  $\mathbf{K}_i$  with block bandwidth p,  $\mathbf{K}_i^T \mathbf{S}_i^{-1} \mathbf{K}_i$  will have a block bandwidth 2p.
- □ Forming this matrix product is the most CPU intensive part of the inverse model calculation, as  $\mathfrak{m} \gg \mathfrak{n}$

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#### A prototype retrieval

- A 'proof of concept' prototype has been designed.
- Forward model and retrieval both written in IDL.
- G Forward model contains all 2D radiative transfer methods required.
- Retrieval linearises this forward model to the form

$$\mathbf{y}^{\star} = \mathbf{y}^{\star} + \mathbf{K}^{\star} \left( \mathbf{x} - \mathbf{x}^{\star} \right)$$

- □ 25 profiles of UARS MLS data have been taken as 'truth'.
  - ⇒ Note that the horizontal resolution of UARS MLS is ~500 km.
  - ⇒ For EOS MLS it is ~150 km.
  - ⇒ Thus the gradients in this model atmosphere are probably a little severe.
- □ A retrieval of Temperature, tangent pressure and ozone was performed.

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□ Radiances from R1:118.B1F:PT and R2:190.B6F:03 were used.

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#### Computational effort in the retrieval

- $\Box$  The formation of the normal equations scales according to Npn<sup>2</sup>m.
- $\Box$  The key point is that this operation scales as N, not N<sup>2</sup>. Therefore.
- □ It takes the same time to retrieve one 200 profile chunk as to retrieve two 100 profile chunks!
- □ The limitation on the size of N becomes the memory capacity of the computer.
- □ Solving this matirx with a 'sparsity aware' Cholesky decomposition scales as  $N^2 pn^3$ .
- $\Box$  Thus, the matrix solver will typically be faster than the  $K^T S_u^{-1} K$  by a factor of  $\sim m/Nn$ .
- Of course, in real situations we have more complex state and measurement vectors, introducing more sparsity.
  - ⇒ For example, very few MLS bands have sensitivity to minor species such as ClO.

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#### Weighting functions for the prototype



#### The 'full' MLS forward model.

- □ The forward model is similar to that developed for UARS MLS, extended to two dimensions.
- □ It is a microwave line by line model, using pressure as the independent vertical coordinate.
- □ Radiances are computed for a set of fixed tangent pressures.
  - $\Rightarrow$  A different fixed frequency mesh is used for each tangent pressure.
  - ⇒ Typically covering one or more 25 channel filter bank.
  - ➡ The radiances at these frequencies are then convolved with the individual MLS channel responses.
- These profiles are then convolved with the MLS field of view (FOV) response, and interpolated to the required tangent pressure.

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⇒ This interpolation yields the derivative of radiance wrt. tangent pressure virtually for free.

#### **Results from a prototype — Ozone**



#### The 'full' MLS forward model (cont.)

- □ The state vector profiles are taken to represent tie points in a 'linear spline' interpolation.
- **D** Note that the state vector contains vmr not log vmr (except for  $H_2O$  in the troposphere).
- The forward model accounts for the linear variations in temperature and composition accross it's integration layers.
- □ A Gauss-Legendre quadrature (3–6 point) integration scheme is applied.
- □ Radiance derivatives with respect to composition, temperature, and some spectroscopic parameters can be computed analytically.
- □ The mixing ratio derivatives are cheap to compute.
- □ Temperature derivatives are somewhat more expensive.
  - ➡ It transpires that the most significant terms are those due to the effects of the FOV.
  - ➡ Changes in temperature affect the shape of the FOV when viewed in pressure space.

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#### The linear MLS forward model

□ For many of the MLS spectral bands, the system is highly linear.

Given this, it is possible to construct a simple linear forward model as

$$y = y^* + K^* [x - x^*]$$
 (1)

- $\square$  y<sup>\*</sup> and K<sup>\*</sup> are pre-tabulated radiances and derivatives for state x<sup>\*</sup>.
- $\Box$  In UARS MLS the  $x^*$  linearisation states were divided up according to latitude band and month.
- $\Box$  For EOS we intend a more dynamic scheme, tabulating standard cases (e.g. inside polar vortex, tropical spring,...), and choosing the most appropriate given the value of x.
- □ The radiances and derivatives are tabulated for fixed tangent pressures.
- These are then interpolated to the tangent pressures in the state vector. The interpolation yielding the derivative with respect to tangent pressure as an added bonus.

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#### Approach for 'noisy' products.

- □ Many of the MLS data products will be 'noisy'
- Products such as BrO with very low concentrations and/or signal strengths.
- □ Some form of averaging (e.g. weekly zonal mean, monthly map) will be needed to yield Level 2 data with useful signal to noise.

#### Forward model implementation

- We plan to use the linear forward model for most channels.
- □ As each channel becomes optically thick, the linear forward model becomes a poorer approximation.
- Optical depth increases with decreasing tangent height and increasing proximity to the line center.
- □ We use each channel down to the tangent heights where it is too optically thick, and then ignore it.
- Information will still be obtained from the channels further from the line center at these heights.
- □ For the 'wing' channels (furthest from line center), we'll have to use the full non-linear forward model if we wish to get useful information.
- □ We may still take the derivatives from the linear model for speed.

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#### Obvious approaches for 'noisy' products

- □ There are two obvious approaches for dealing with 'noisy' products.
- □ Average in measurement space:
  - ⇒ Average together many radiance observations and perform retrievals on the averaged radiances.
  - ⇒ This works, provided the signal of interest is not affected by a varying contaminant who's effect on the radiances is non-linear.

#### □ Average in state space:

- ➡ Perform single profile retrievals as with the 'standard' products and average the results appropriately.
- $\Rightarrow$  This solves the problem with non linear contaminants.
- ➡ However, the *a priori* information is introduced in *each* profile retrieval and will thus strongly bias an average.
- ⇒ But one can't make the individual profile *a priori* too loose without risking instability in the individual retrievals.

#### A new approach: Average in 'information' space.

- ❑ Construct a state vector which is the desired result.
   ⇒ For example a monthly zonal mean BrO field.
- □ Then we consider each relevant set of radiance observations as an individual measure of this quantity.
- □ We use the previously retrieved quantities such as temperature, pressure, ozone etc. as constrained quantities in the forward model for these retrievals.
  - $\Rightarrow$  This deals with the issues of having non linear contaminants.
  - $\Rightarrow$  Error propagation for these quantities is tbd.
  - $\Rightarrow$  We include the *a priori* in the retrieval *once only*.
- □ Mathematically this comes down to:

$$\mathbf{x} = \left[ S_{a}^{-1} + \sum_{i} K_{i}^{\mathsf{T}} S_{i}^{-1} K_{i} \right]^{-1} \sum_{i} K_{i}^{\mathsf{T}} S_{i}^{-1} \left[ y_{i} - f_{i} \left( a \right) \right],$$

where the summation is over all the relevant sets of radiance profiles.

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## Implementation of the algorithms in software.

- □ We want to process one days worth of data in less than one day.
   ⇒ We're aiming for 6 hours, to allow for parallel reprocessing streams.
- □ The software is written at JPL, and will be run at a Raytheon facility in Pasadena under contract to JPL.
- □ The data will then be sent to the Goddard DAAC (EOS data repository) for archive and distribution.
- We're anticipating running the code on Beowulf style cluster.
- □ Having divide the data into the chunks described earlier, we have the nodes work on them independently.
- □ If the nodes themselves have multiple (e.g. 2) processors, either: □ give them each two chunks (may take too much memory).
  - ➡ write the chunk processing code in a parallel manner (a little harder to implement).

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□ We currently have a 64 node, 128 processor IBM linux cluster.

# Making it even easier

- □ It is possible to improve on the efficiency of this algorithm further,
- □ if the routine (i.e. daily) processing outputs forward model radiances or the radiance residuals.
- **D** These are equivalent to the y f terms in the retrieval equation.
- □ As the signal of interest is small, weighting functions can be pretabulated.
- □ The daily processing can even retrieve its own estimates of the 'noisy' species.

⇒ These can be useful in spotting 'freak' events.

- □ Again, as the signals are small, a linear correction can be made for the amount inferred by the daily processing.
- □ The UARS MLS instrument has a filter bank centered on a spectral line from H<sub>2</sub>O<sub>2</sub>.

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□ This will be an ideal test case for the algorithm.

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# Implemetation in software (cont.)

- □ Software written in Fortran 95.
  - ⇒ F95 has many powerful features that Fortran 77 really lacks.
  - ➡ Higher level languages such as IDL and Matlab lack the speed, also cost too much in cluster environment.
  - $\Rightarrow$  C does not handle arrays as well, and is typically harder to optimize.
- □ We implemented a somewhat object orientated approach.
  - ➡ Defining 'vector' and 'matrix' types and overloading some appropriate operators.
- The code is driven by the 'Level 2 Configuration File' (l2cf).
- ➡ This is essentially a language devised to describe retrievals, forward model calculations and related activities.

#### Vectors, quantities and matrices in the software

□ At the heart of the software is the concept of a 'quantity'.

- $\Rightarrow$  This is a collection of data for a chunk.
- ➡ For example, a set of temperature profiles, or ozone profiles, tangent pressures or radiances.
- ⇒ Simpler items such as instrument calibration parameters, isotope ratios etc. are also stored as 'quantities'.
- Quantities are collected together to make 'vectors'.
  - ⇒ For example the state vector, and measurement vectors.
  - ➡ For efficiency we divorce the vector 'template' (quantity geolocation information etc.) from the 'value'.
- U We also define the concept of a matrix.
  - ⇒ These have attached vectors describing their rows and columns.

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➡ Typically describe derivative of one vector with respect to another (e.g. weighting functions), or the covariance of a single vector.

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#### Storage and manipulation of matrices

- $\hfill\square$  The quantities in a vector a themeselves divided into 'instances'.
  - $\Rightarrow$  These are horizontal realizations of the quantity.
  - ⇒ Individual temperature profiles, separate radiance scans etc.
- □ The matrices are divided up into blocks by quantity and index.
  - ⇒ The derivative of band 1, scan 10 radiance with respect to temperature profile 11 etc.
- □ The blocks in the matrices can be of four types: **Absent** All zeros, nothing stored.

Full A 'full' block.

Banded A block with a few clustered non-zero elements per column.

- Sparse A block with a few non-zero elements in random locations.
- □ The banded and sparse representations are only typically worthwhile for blocks with <~20% non-zero elements.

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**□** The matrix algebra in the code effitiently deals with all of these.

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## A flexible Level 2 program.

- □ The Level 2 software is very flexible:
  - $\Rightarrow$  Can read and write to/from both Level 1 and Level 2.
  - ⇒ Manipulates gridded data from climatological sources.
  - ➡ Can perform stand alone forward model calculations, in addition to retrievals.
- **□** This means that the one program can do:
  - ⇒ Standard retrievals.
  - $\Rightarrow$  Simulations of radiance fields.
  - $\Rightarrow$  Pre-computation of the tables for the linear forward model.
  - $\Rightarrow$  Or even all three together!
- □ This is much easier than writing three separate programs, each using slightly different I/O and initialisation code.

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Clearly, the configuration needs to be described in a clear manner.

## The Level 2 Configuration File (l2cf)

- □ The l2cf is in many ways a computer language for describing retrievals.
- Can define quantities, vectors, matrices etc. in a very similar manner to the definitions of types and variables in other languages.

The syntax is somewhat reminiscent of IDL.

- ; Define a vertical coordinate system in -log10(pressure/hPa),
- ; with 25 surfaces at 12 per decade starting at 1000mb, followed ; by 24 surfaces at 6 per decade.
- standardSurfaces: vGrid, coordinate=Zeta, type=Logarithmic, \$
   start=1000mb, formula=[25:12, 24:6]

; Place profiles where GHz tangent point height first crosses ; 15km each scan.

standardProfiles: hGrid, type=height, height=15km, module=GHz

; Define a template for temperature, GHz tangent pressure, ; ozone and band 6 radiances. temperature: Quantity, vGrid=standardSurfaces, hGrid=standardProfiles, \$

temperature: Quantity, vGrid=standardSurfaces, hGrid=standardProfiles, \$
type=temperature
ptahGHz: Quantity, type=ptan, module=GHz

canGHZ: Quantity, type=ptan, module=GHZ

ozone: Quantity, type=vmr, molecule=03, vGrid=standardSurfaces, \$
hGrid=standardProfiles
band6: Quantity, type=radiance, signal='R2:190.B6:03'

#### The Level 2 Configuration File (cont.)

#### The Level 2 Configuration File (cont.)



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#### **Production code.**

- □ The production code is still under development and testing.
- **G** Essential functionality in place.
- □ What remains are many 'small but vital' features that will be needed.

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- □ Also need to ensure code is 'bomb proof'.
  - Aust be able to cope with missing data, broken radiometers etc.
- □ Hoping to add an 'on-line diagnostic' capability.
  - A separate IDL task that can communicate with the fortran code during testing display results etc.
- Note that the software is flexible enough that it can easily be modified to process data from UARS MLS.
  - ➡ No code changes required, just some changes to the l2cf and new calibration files.
- □ Some results from a simple retrieval, similar to the 'prototype' follow.

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#### Results from production code.



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#### Summary.

- □ MLS is a passive microwave instrument designed to measure the chemistry and dynamics of earth's atmosphere from 5–80 km.
- **u** The retrieval algorithms use the standard *optimal estimation* approach.
- One new aspect is a two dimensional 'tomographic' approach to the problem.
- □ Avoid error propagation problems by doing simultaneous retrievals.

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- □ Implemented in a very flexible software setup.
- U Work proceeding well.

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