

SMR/1438 - 12

**JOINT ICTP-INFM SCHOOL/WORKSHOP ON
"ENTANGLEMENT AT THE NANOSCALE"**

(28 October – 8 November 2002)

"A Josephson charge qubit using radio-frequency single-electron-transistor readout"

presented by:

T. Duty
Chalmers University of Technology
Sweden

A Josephson Charge Qubit using Radio-Frequency Single-Electron-Transistor Readout

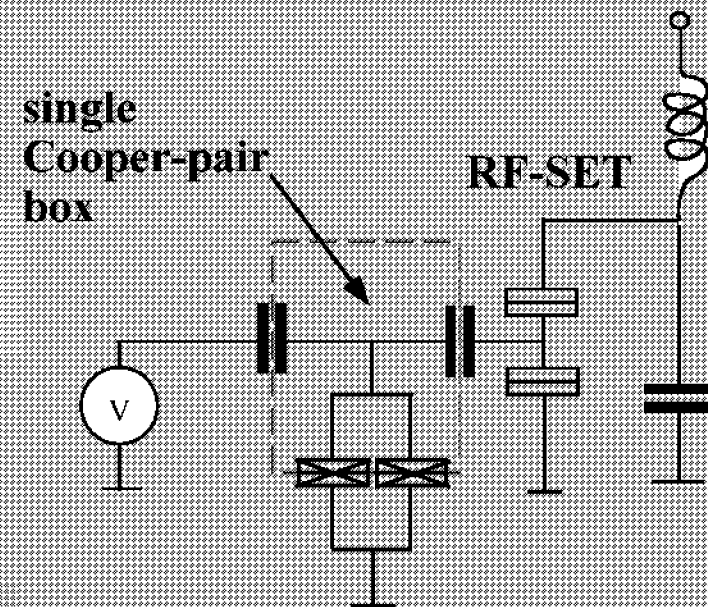
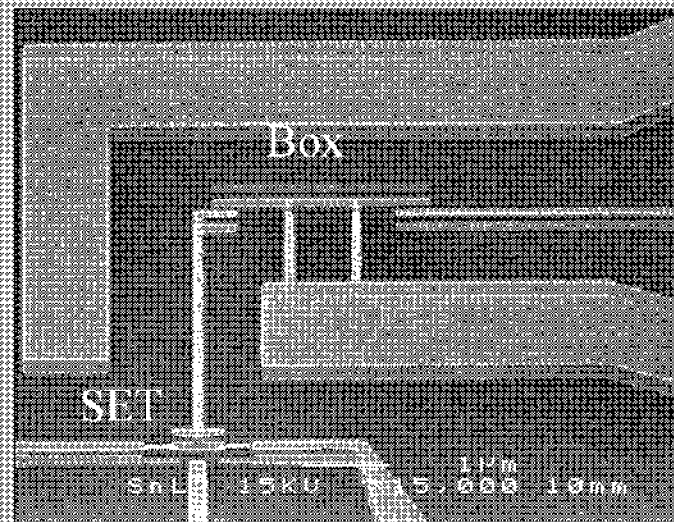
Tim Duty

1. The single-Cooper-pair box
and the single-electron transistor
2. Measuring the box:
quasi-particle states and back-action
3. Spectroscopy
4. Coherent charge oscillations
5. Measuring T_1
6. Pulsed Measurements

D. Gunnarsson
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K. Lehnert

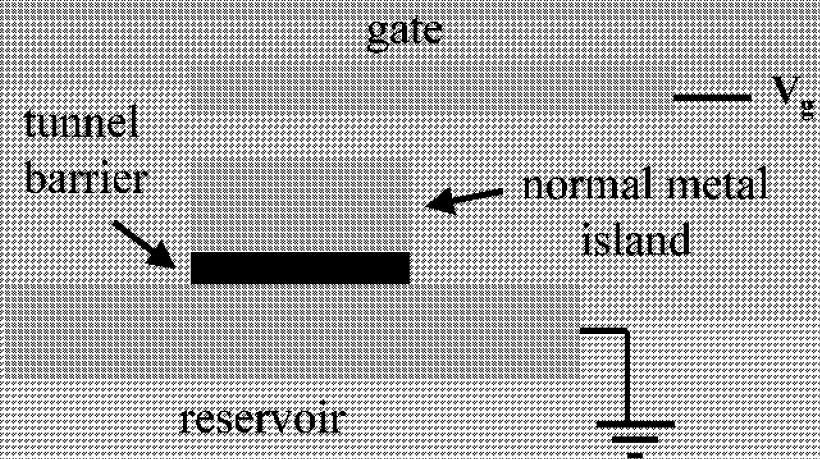
A Single Cooper-pair Box Qubit Integrated with an RF-SET Read-out system



$$\Delta \gg E_C \gg E_J(B) \gg T$$

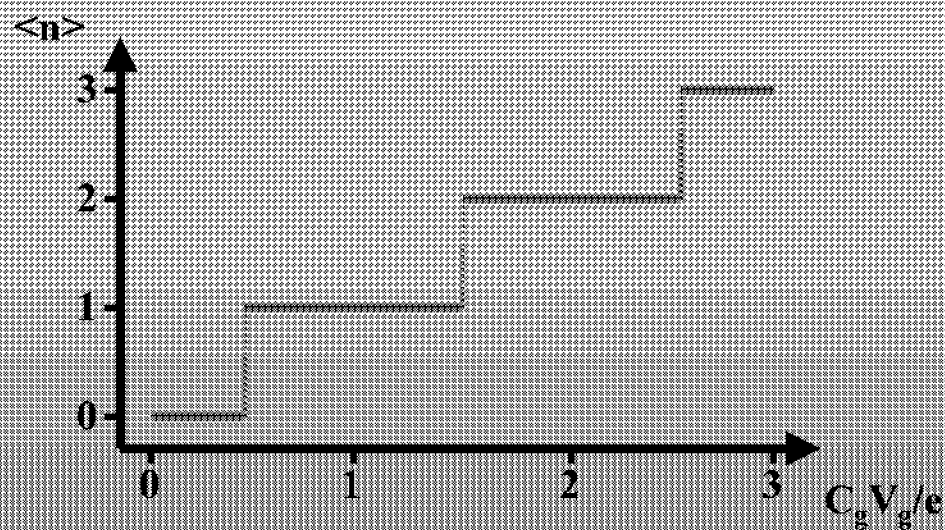
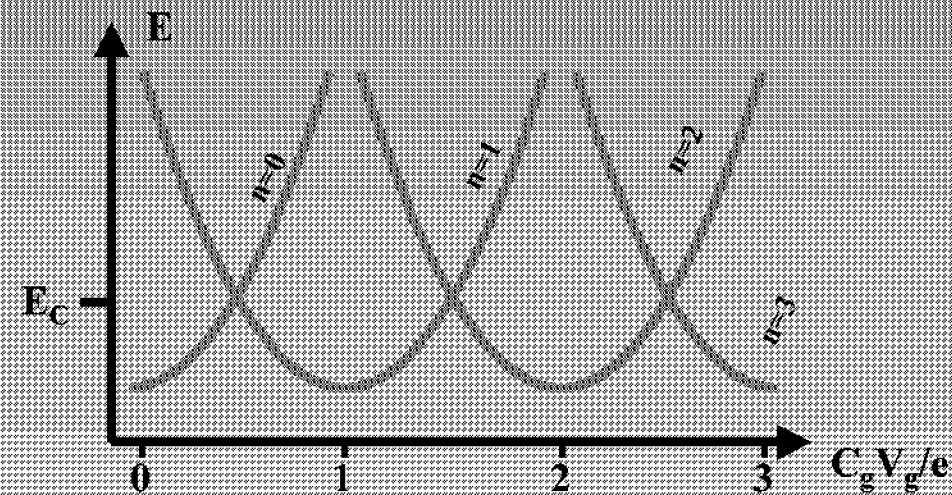
$$2.4\text{K} \quad 1.7\text{K} \quad 0.7-0.05\text{K} \quad 20\text{mK}$$

The Single-Electron Box

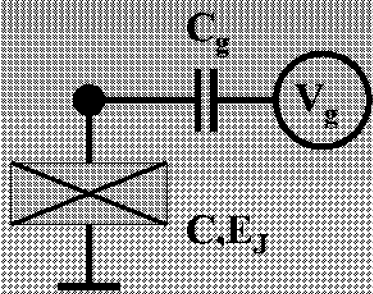


$$E_c = \frac{e^2}{2C_g}$$

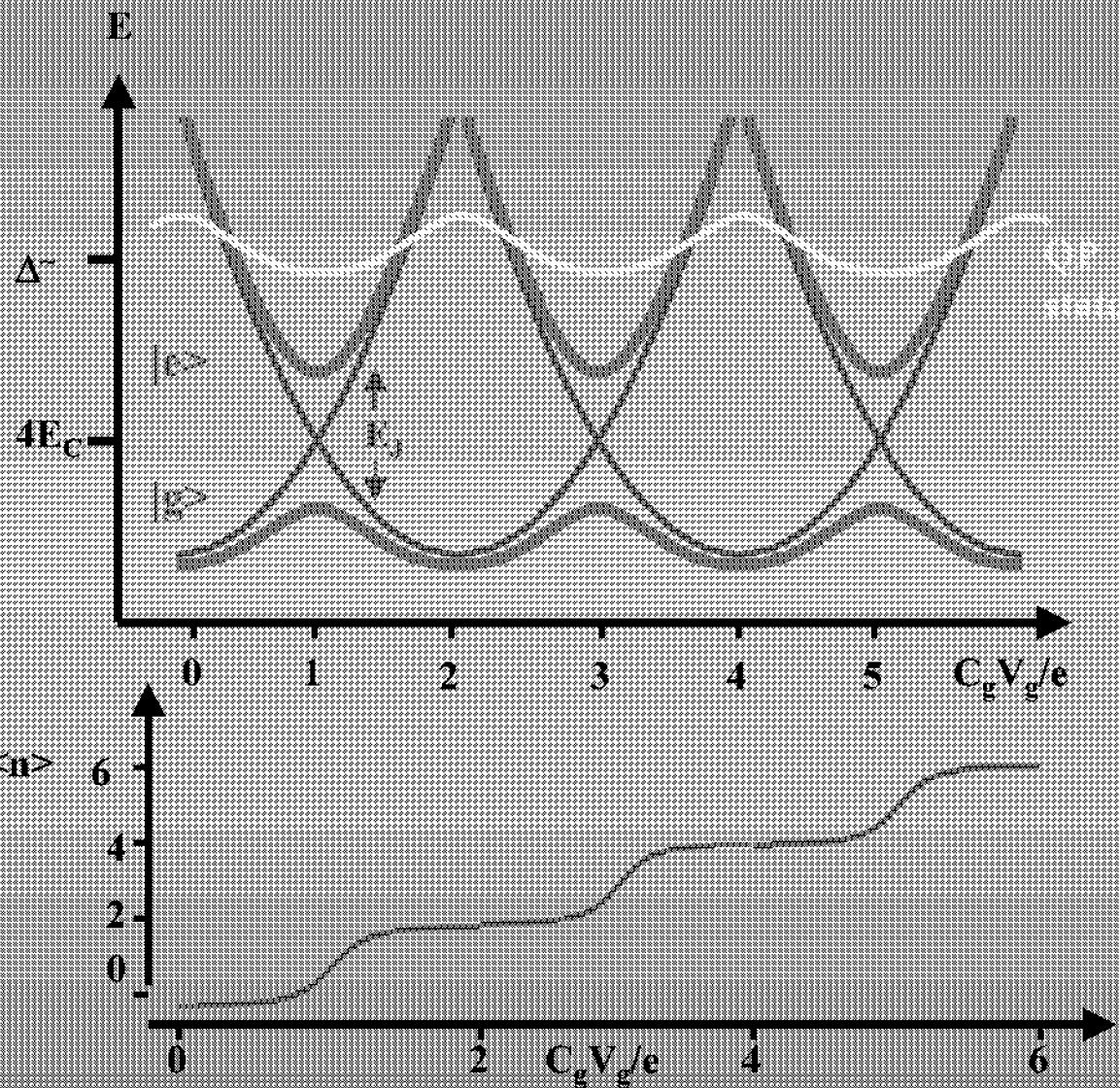
$$k_B T < E_c$$



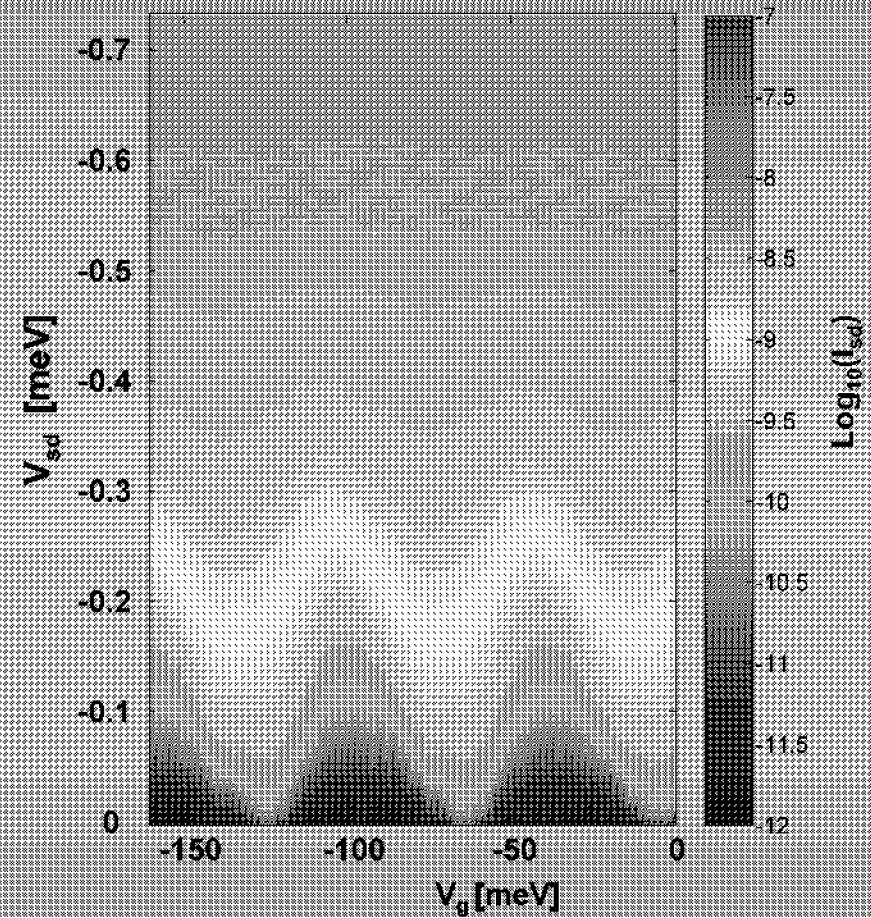
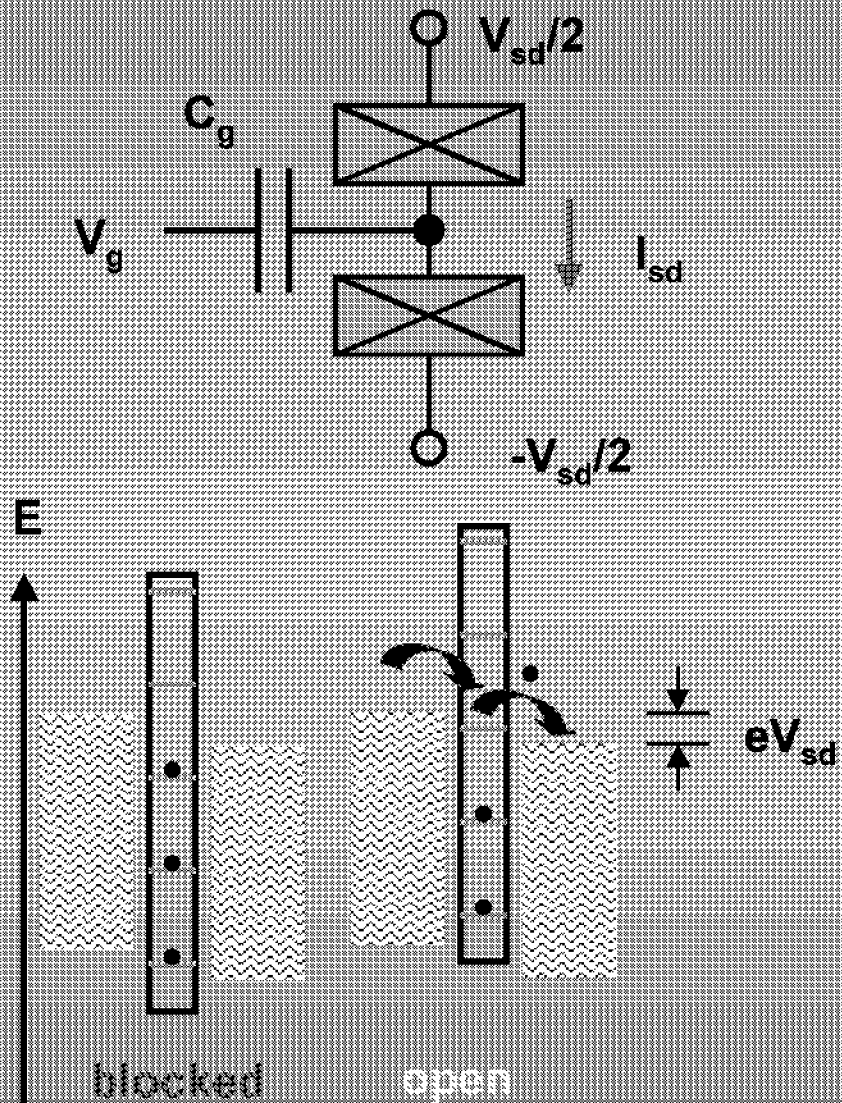
The Single-Cooper-Pair Box



$$k_B T < E_J < E_C < \tilde{\Delta}$$

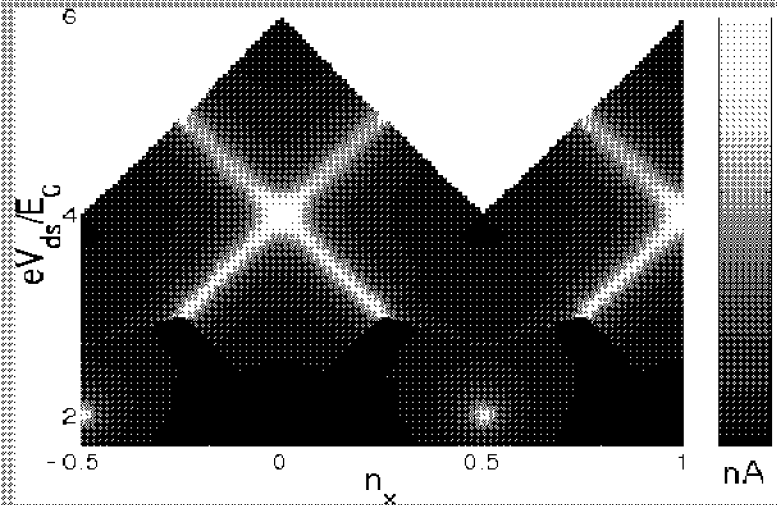


The Single Electron Transistor



Cooper-Pair-Transistor DC Current

Theory



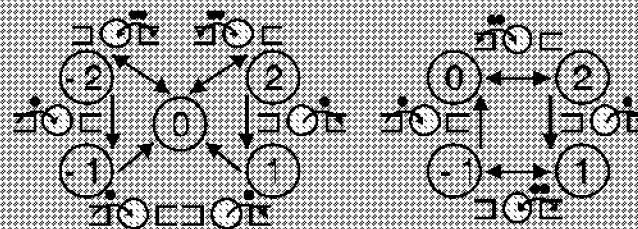
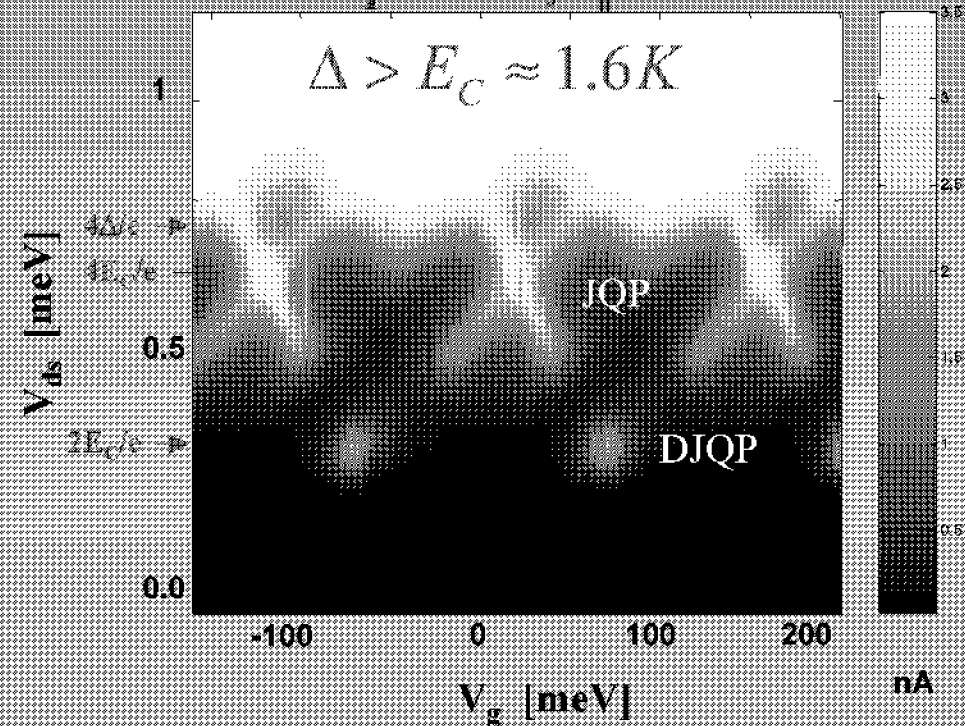
from: Johansson, cond-mat/0210539

Fulton & Dolan (1987)

van den Brink *et al.* (1991)

Hadley *et al.* (1998)

Experiment, $B_{||}=0.4T$



IQP

DJQP

Thesis, 2003/03

The SET as an Electrometer

- Very Sensitive: can detect fractions of an electron charge.
- But it is slow: each junction must be of order of R_Q , leading to a $R_T \sim 100\text{k}\Omega$. For typical lead capacitance, 0.1-1nF, this gives a bandwidth of a few kHz---unacceptable for solid-state QC.
- How can one take advantage of the intrinsic bandwidth, due to capacitance of junctions, which can be as high as 10GHz?
- The 'best' solution is to incorporate the SET into a tank circuit and measure damping.

Figure 1 is a line graph showing the normalized current I/I_0 on the y-axis versus time t in microseconds (μs) on the x-axis. The y-axis ranges from -0.02 to 0.12 with major ticks every 0.02. The x-axis ranges from 0 to 40 with major ticks every 5 units. The plot shows a sharp rise in current at approximately 20 μs , followed by a steady-state oscillation. Text in the plot area indicates $\delta Q = 0.1e$ and $B_w = 1 \text{ MHz}$.

Very high sensitivity: 3.2 $\mu\text{e}/\sqrt{\text{Hz}}$
Aassime et al., APL (01)

Measuring the box

Circuit parameters

$$R_{\text{SET}} \approx 47\text{k}\Omega$$

$$E_{\text{CSET}} \approx 1.51\text{K}$$

$$E_{\text{CBOX}} \approx 1.67\text{K}$$

$$E_J \approx 0.7\text{K}$$

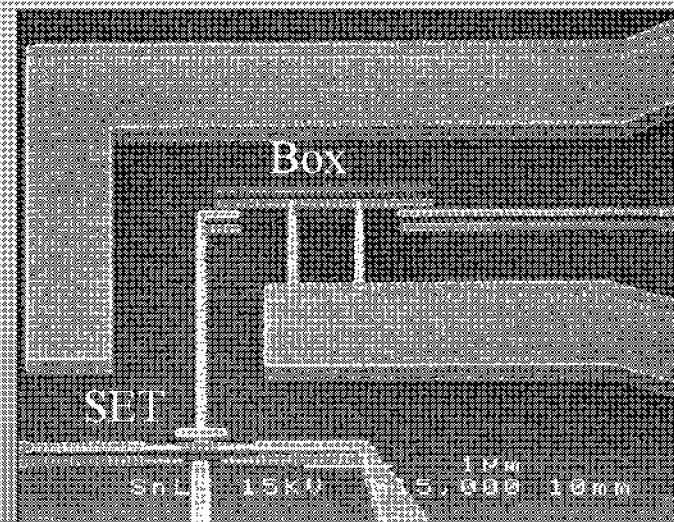
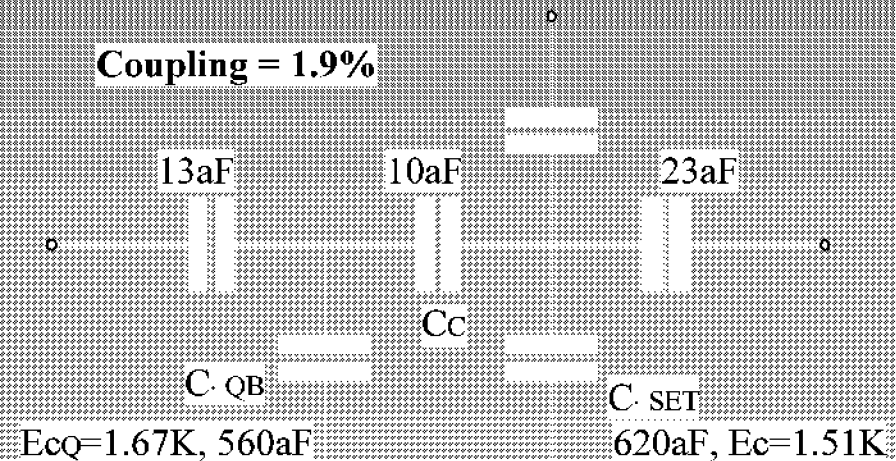
Box to SET coupling = 1.9%

B-field parallel to substrate

$$f_{\text{carrier}} = 380\text{ MHz}$$

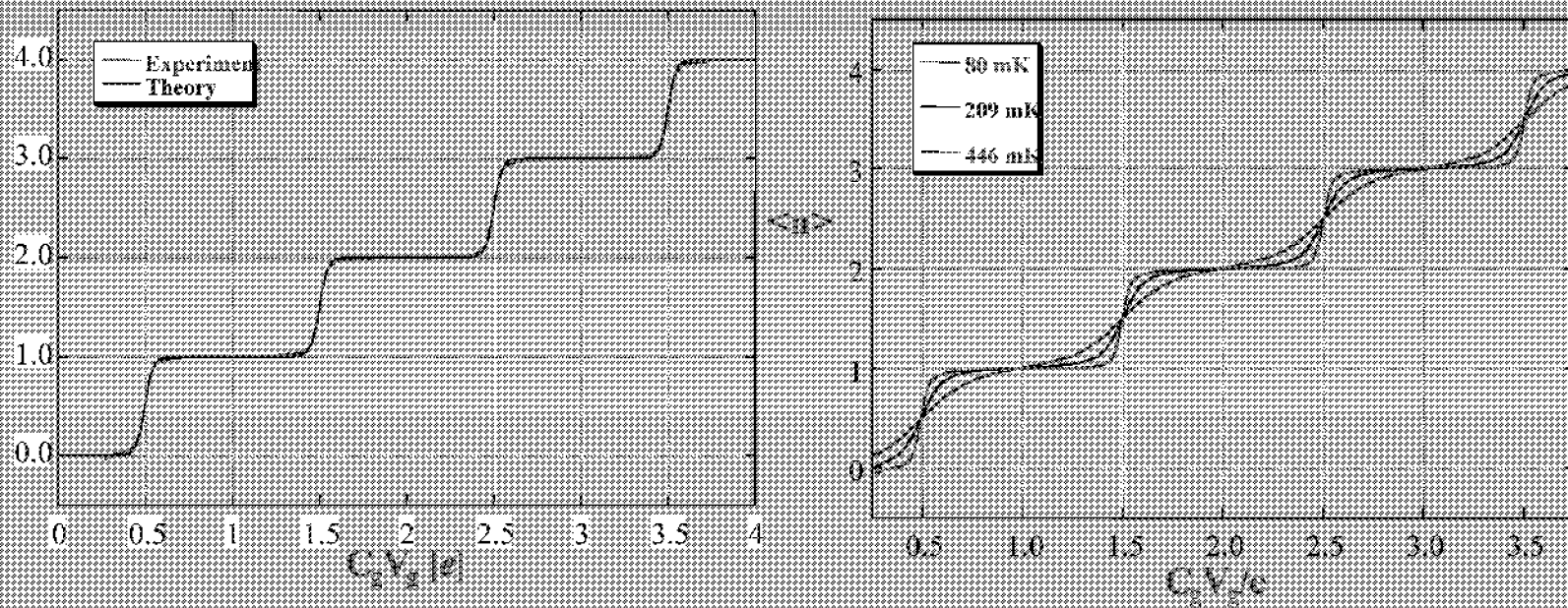
RF-amplitude $\approx -100\text{dBm}$

Staircase sweep frequency
typically 100-300Hz



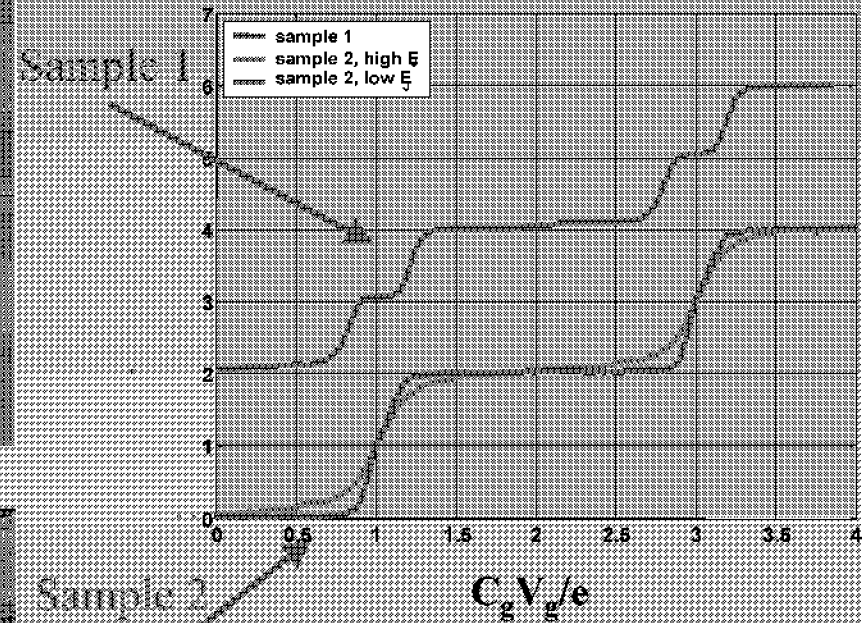
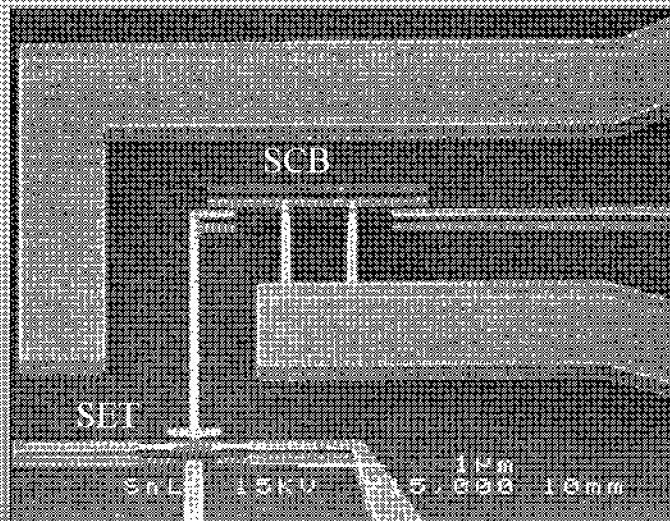
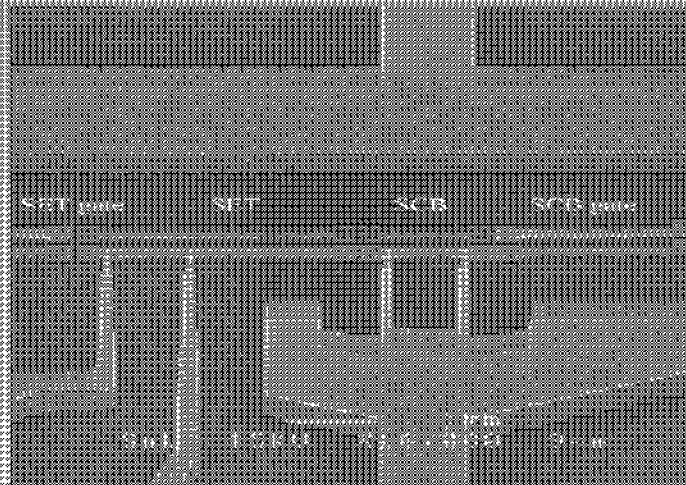
The Coulomb blockade staircase measured in the normal state, $B_{||}=1.25\text{T}$

Temperature dependence of the staircase

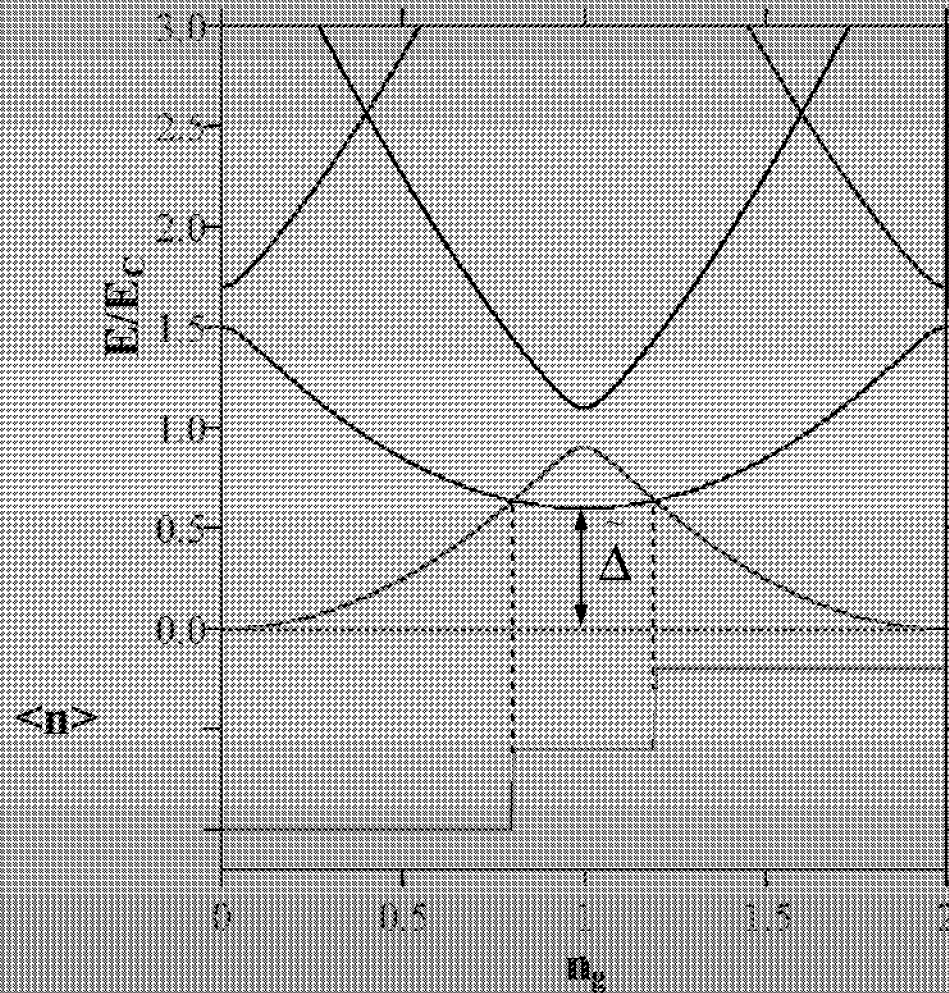


Electron temperature can be estimated from
the rounding and slope of the staircase.

Single-Cooper Pair Boxes



What would you expect in the superconducting state
with Δ not so large?



$$\Delta \approx \Delta_0 - k_B T \ln(N)$$

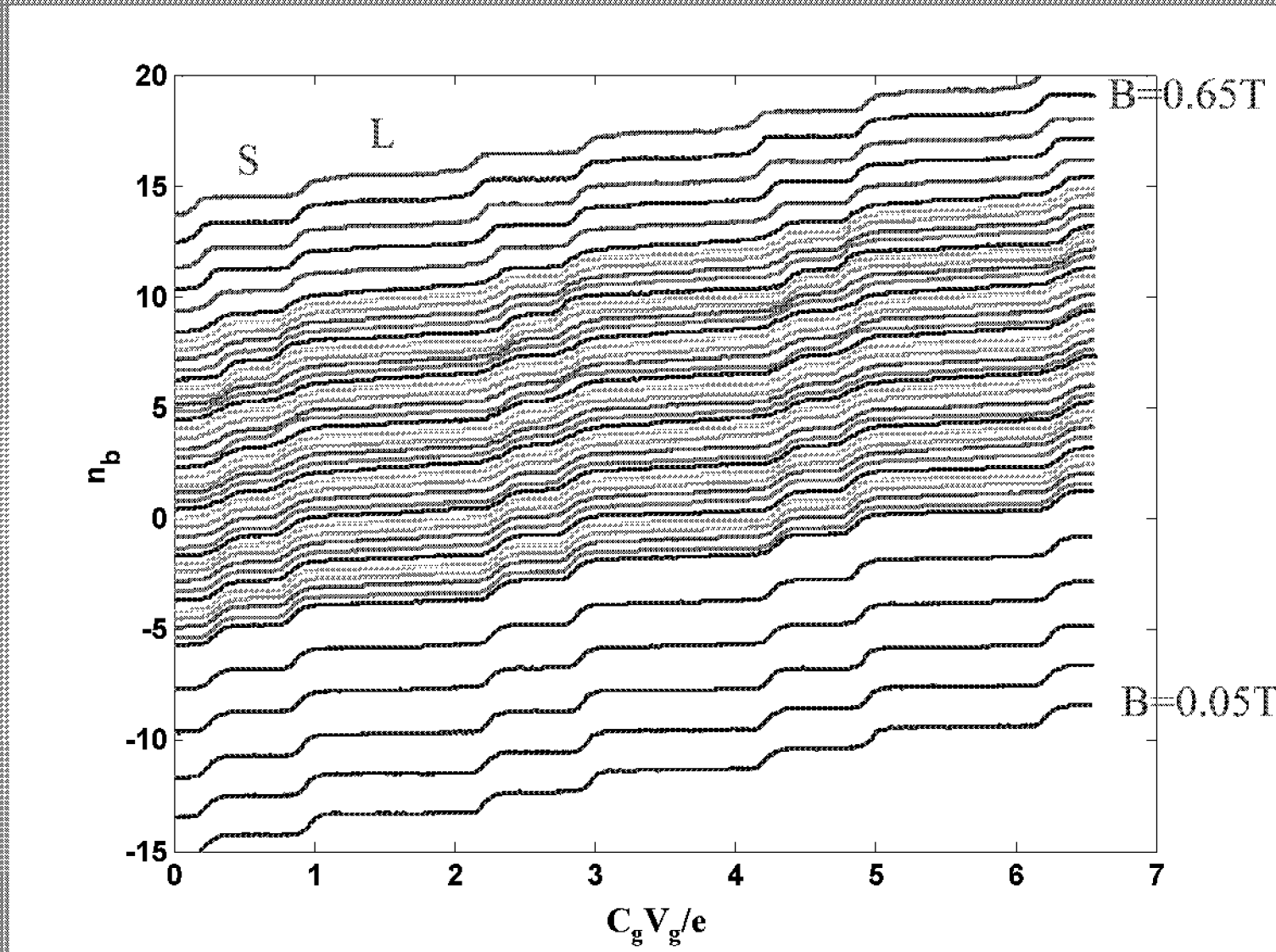
$$\Delta_0 \approx 2.4\text{K for Al}$$

$$\Delta \approx (L-S)/(L+S)$$

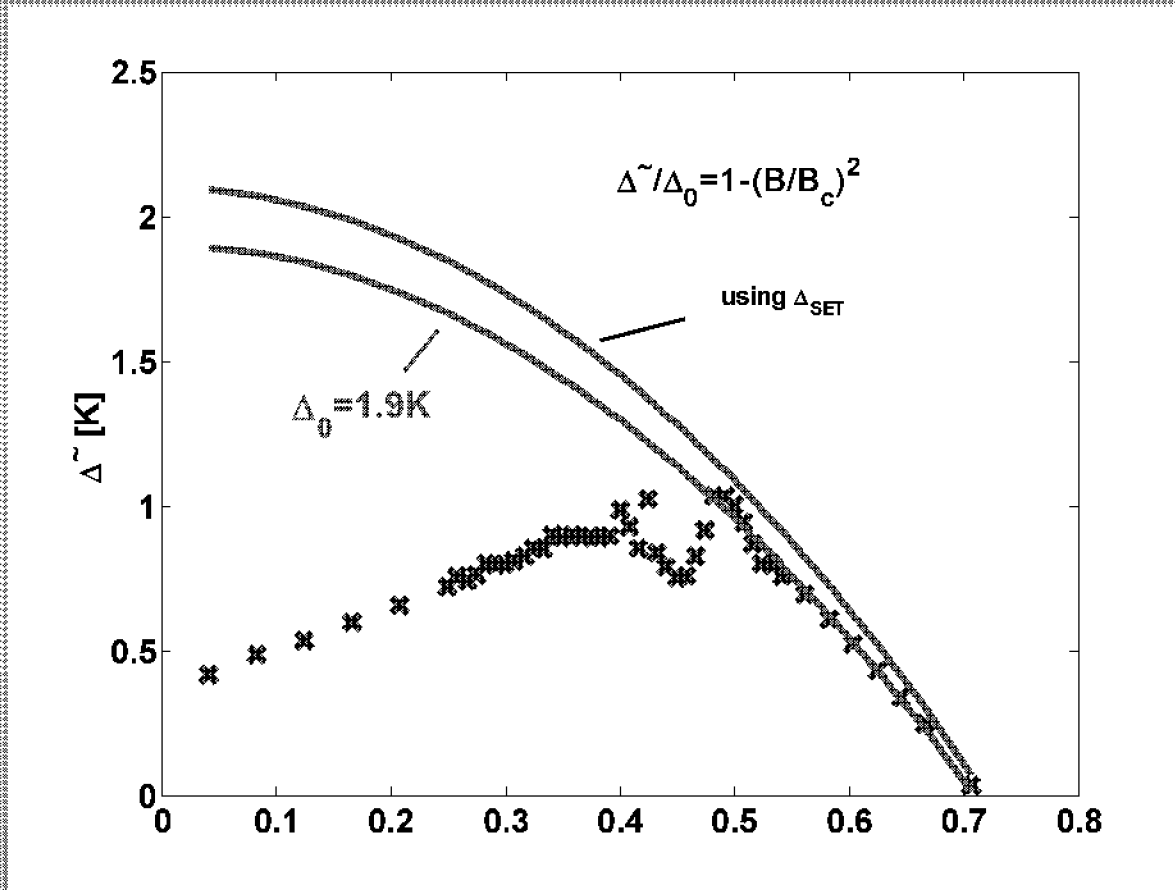
Lafarge et al. Nature (93)

Long Step versus Short Step

Magnetic field dependence of the short step



Extracting $\Delta^{\sim}(B)$



$$\Delta^{\sim} = E_c(L-S)/(L+S)$$

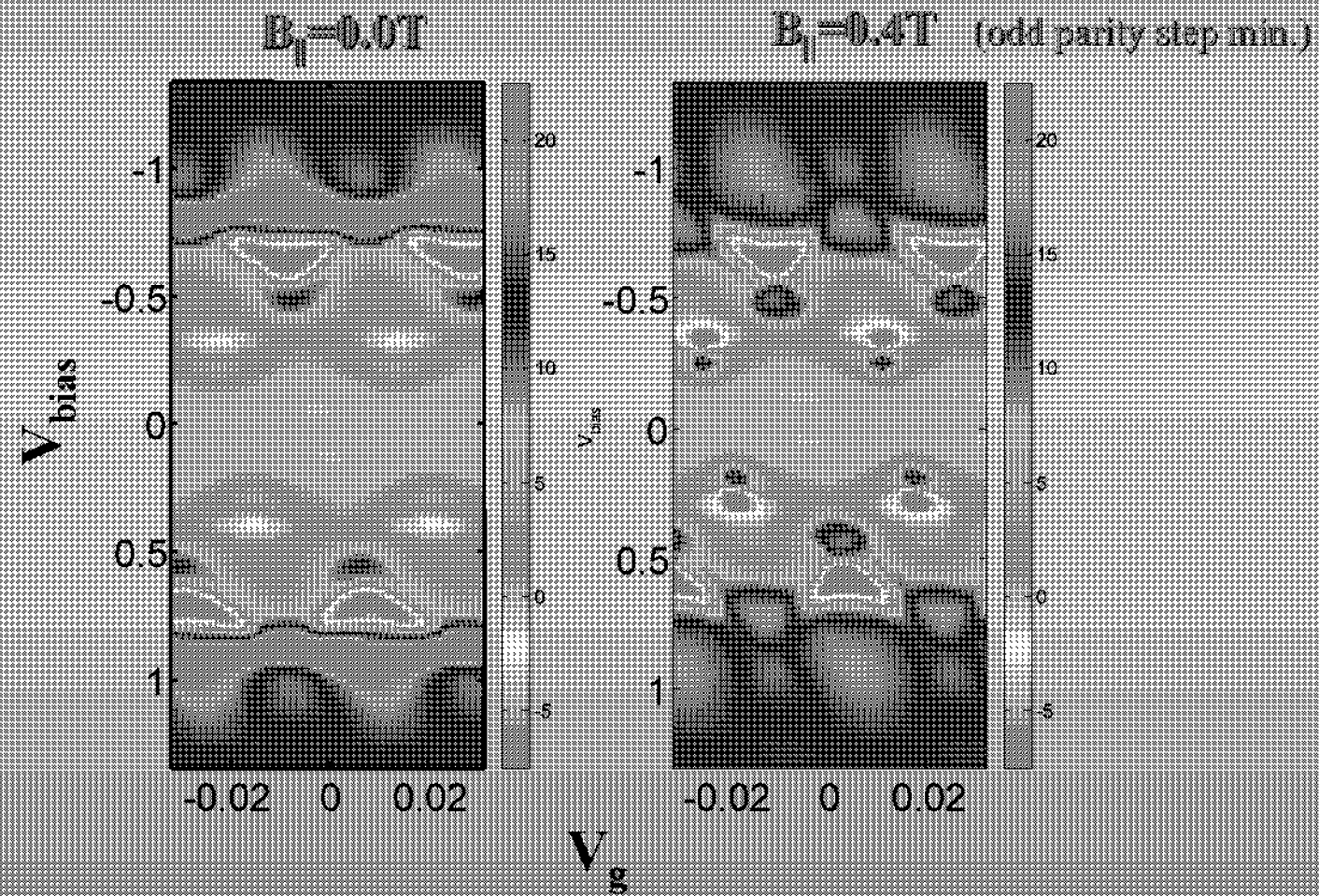
But what is going on for $B < 0.4 T$?

'Field-induced gap engineering' creates QP traps in the leads.

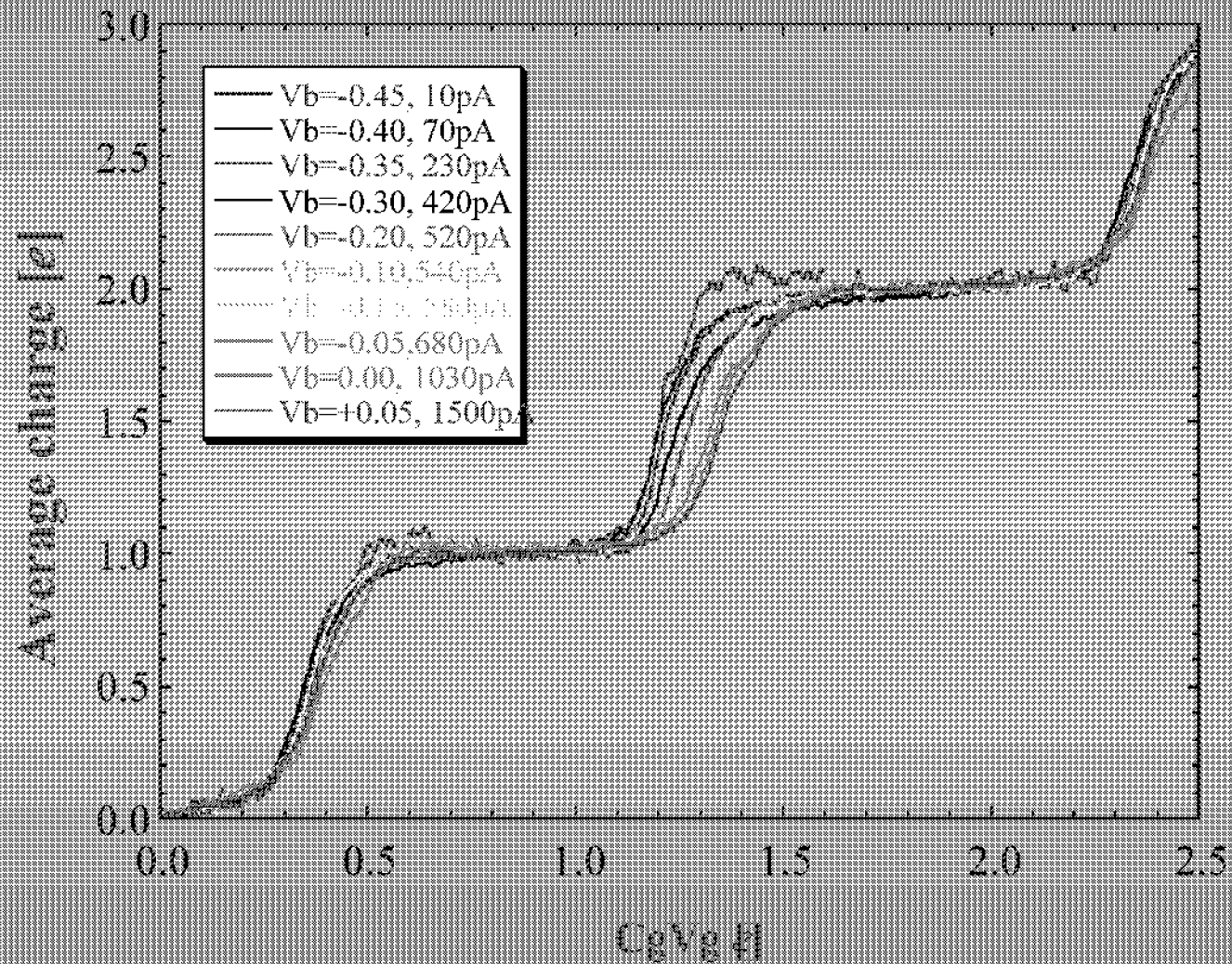
What about BACK ACTION?

How does the SET affect the
staircases?

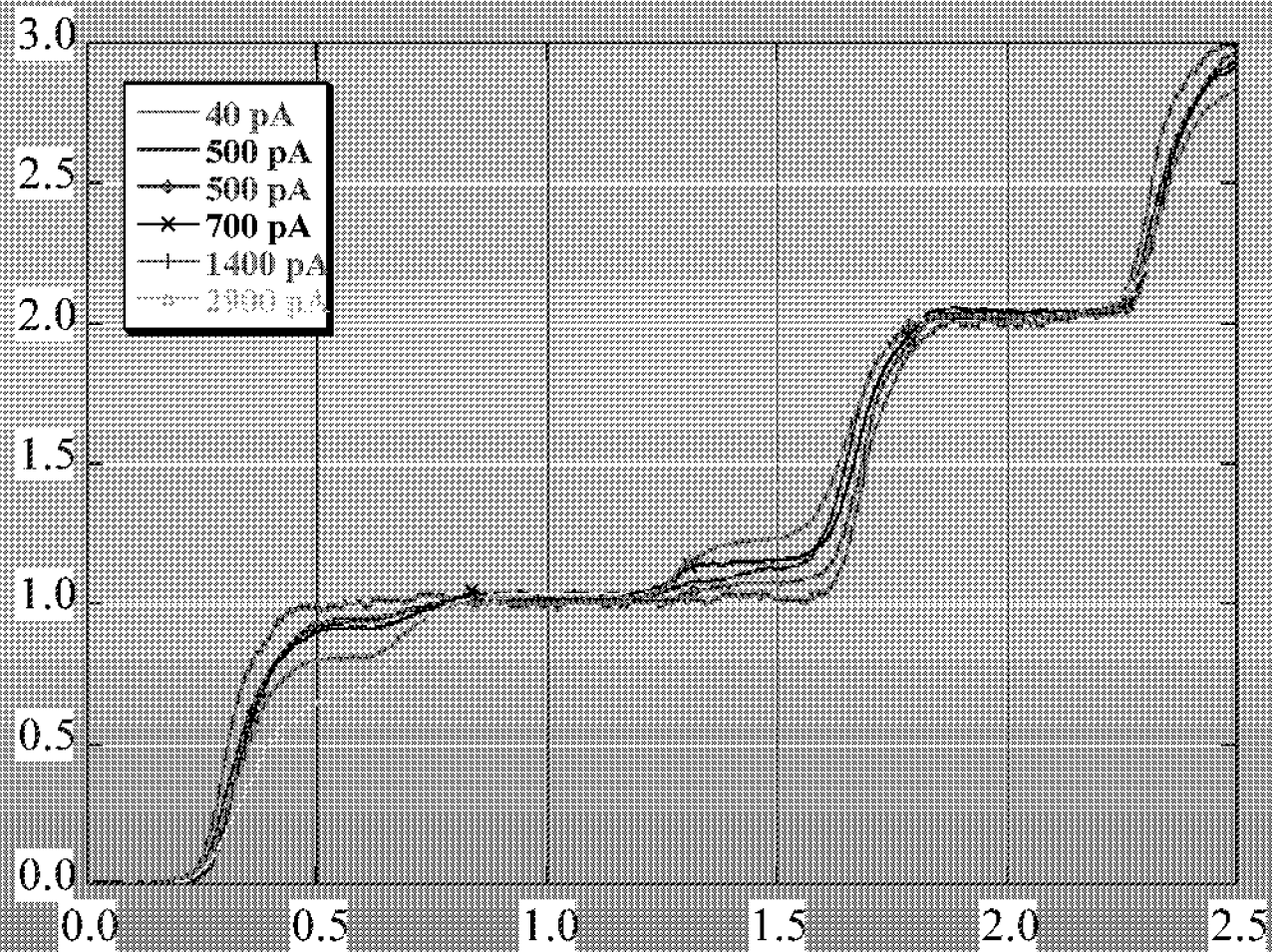
Conductance of SET vs. V_b and V_g



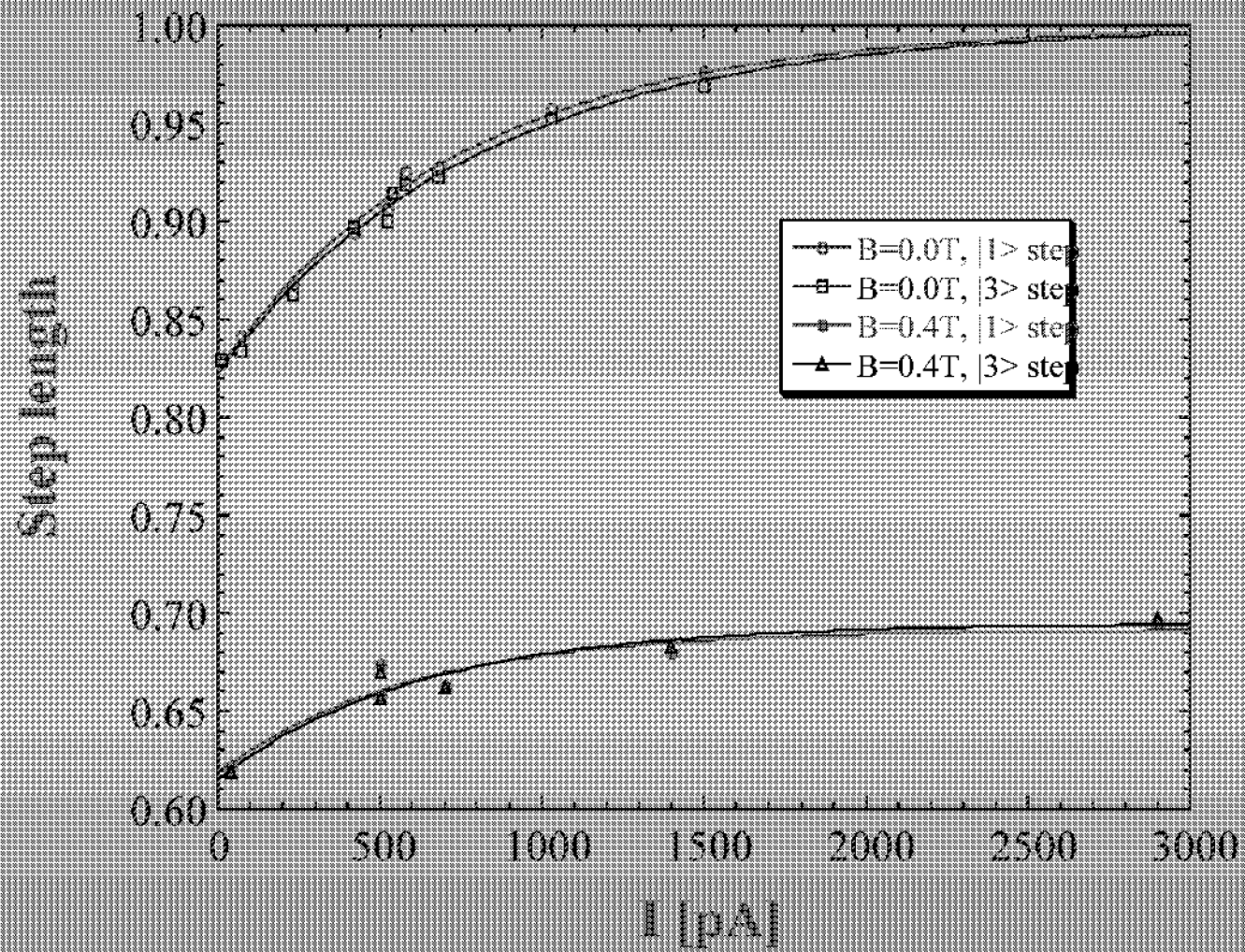
Effect of SET current at zero magnetic field



Effect of SET current at $B=0.20\text{T}$

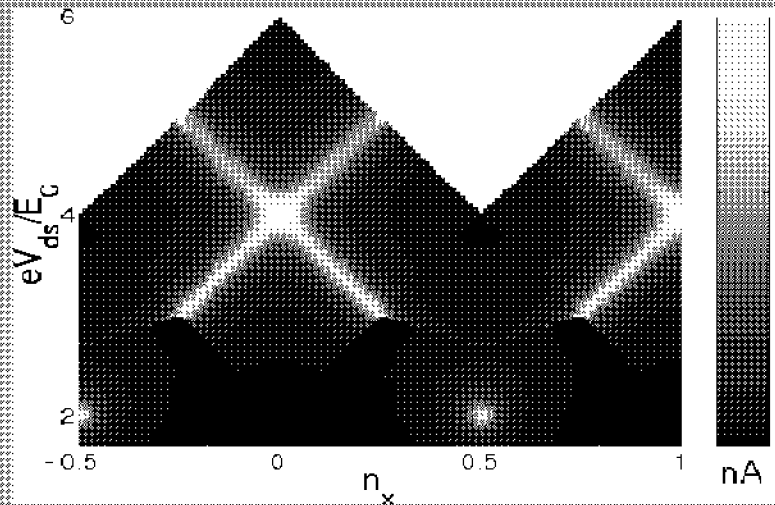


Step width vs. current



Cooper-Pair-Transistor DC Current

Theory



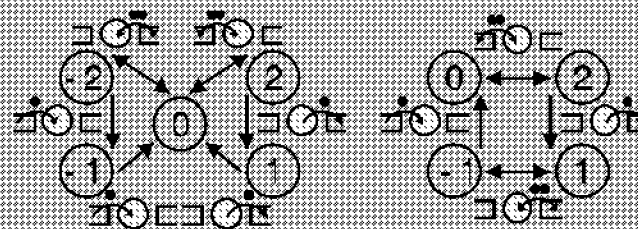
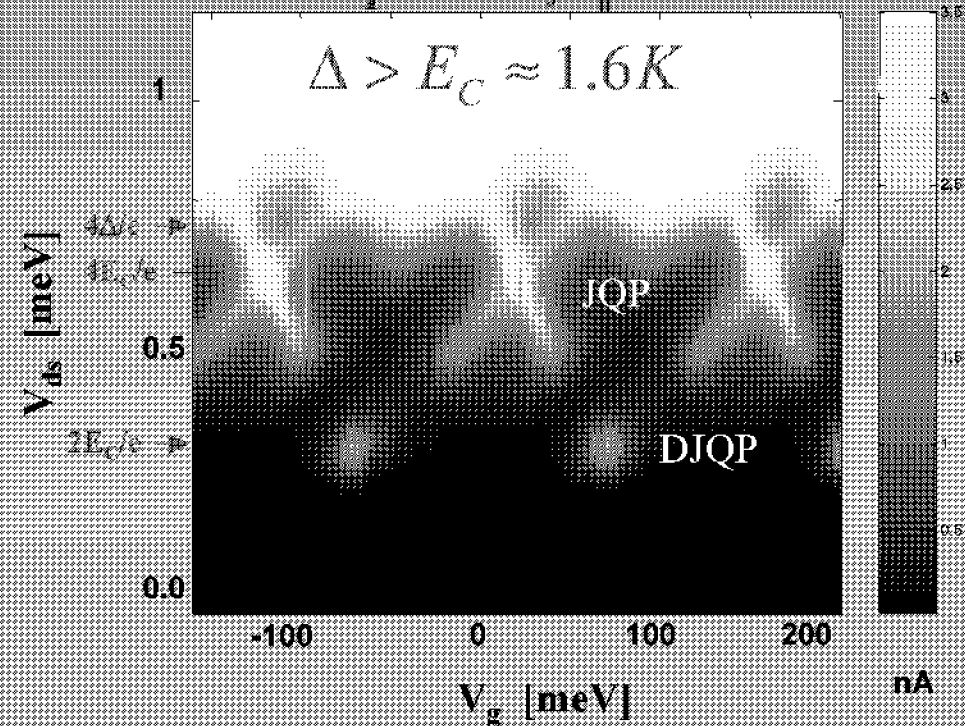
from: Johansson, cond-mat/0210539

Fulton & Dolan (1987)

van den Brink *et al.* (1991)

Hadley *et al.* (1998)

Experiment, $B_{||}=0.4T$



IQP

DJQP

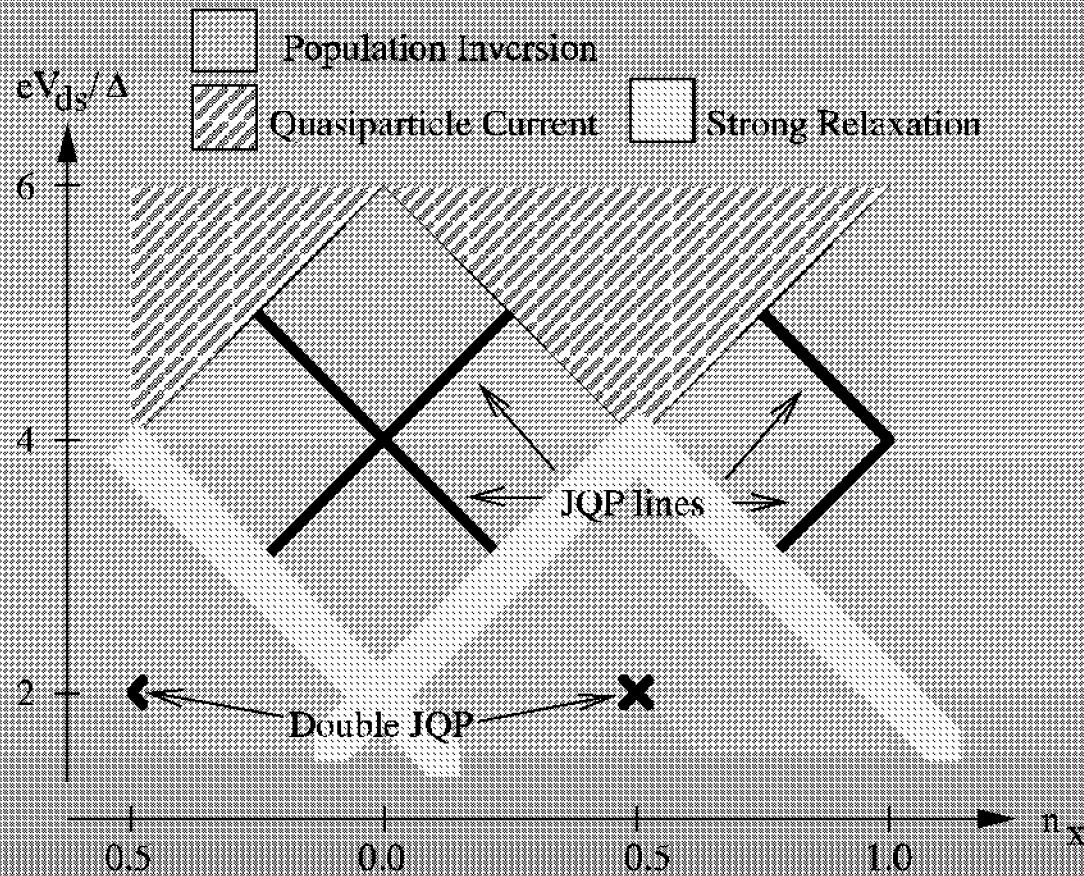
Thesis, 2003/03

Back-action from the SET: Population Inversion and Relaxation

Johansson, cond-mat/0210539

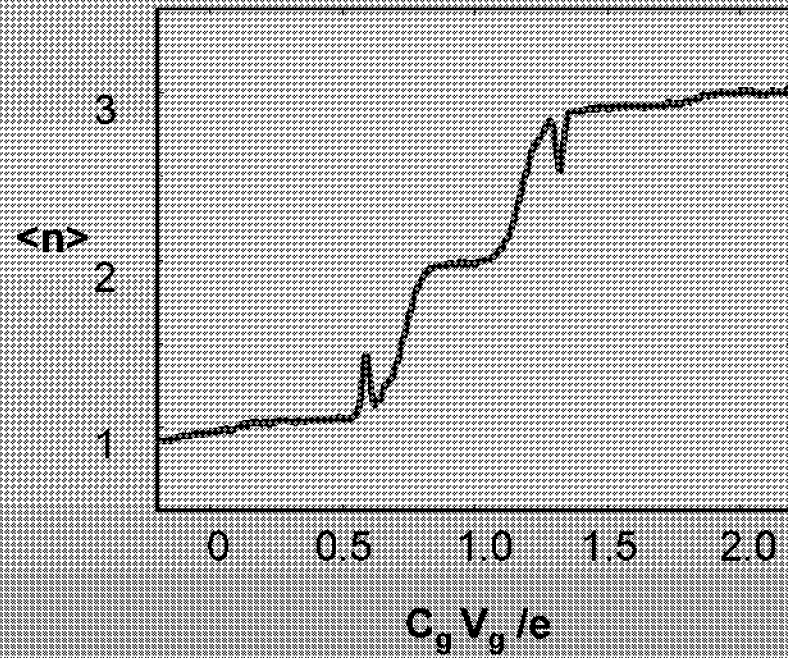
Clerk *et al.* PRL (2002)

Choi *et al.* (2001)

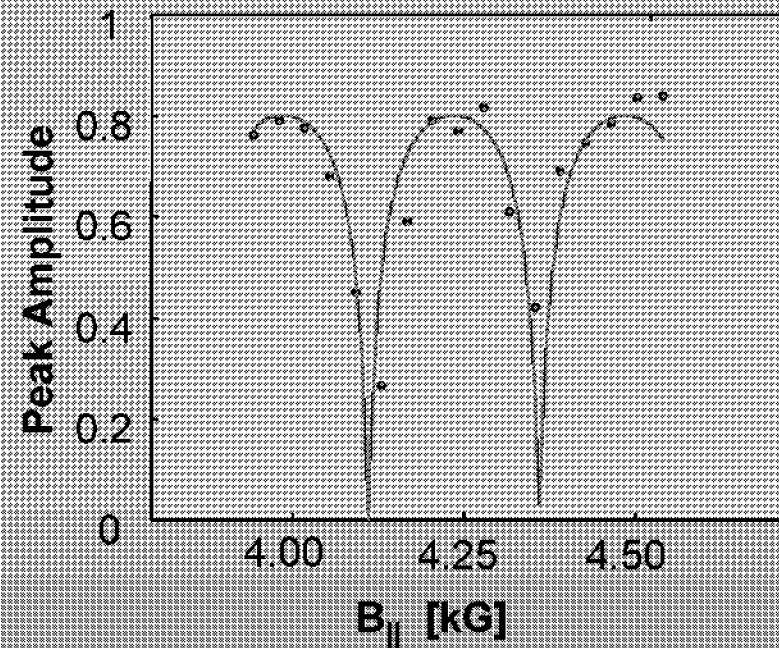


Spectroscopy

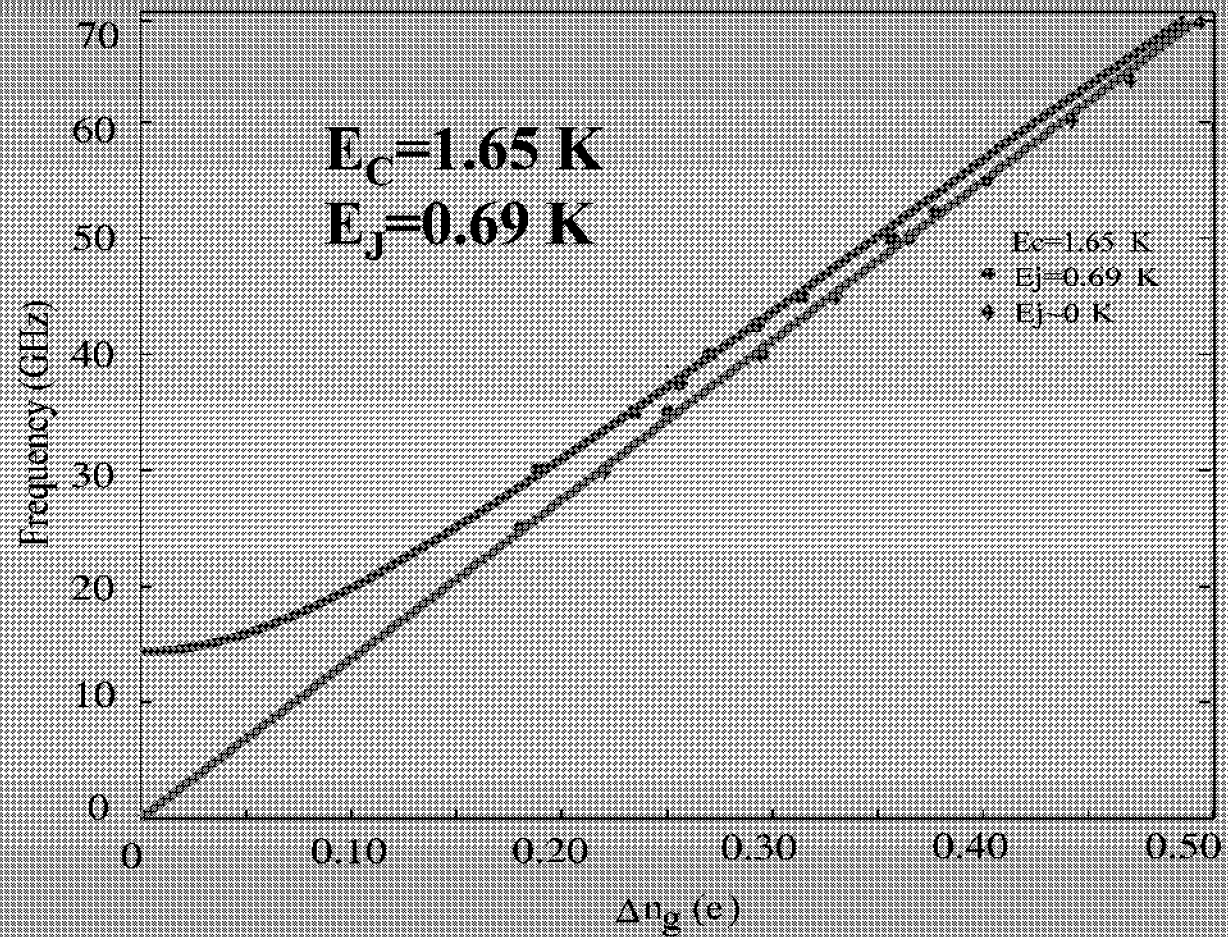
50 GHz peaks



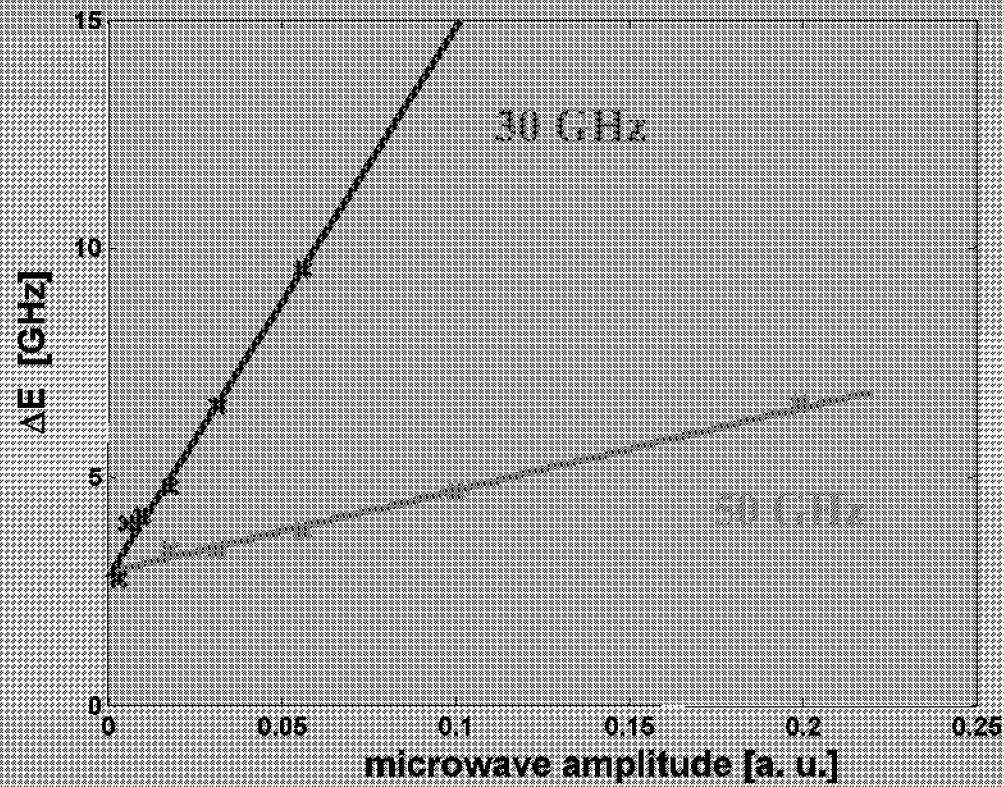
Modulation of E_J with $B_{||}$



Spectroscopic determination of E_J and E_C



Extracting T_2^* from peak width

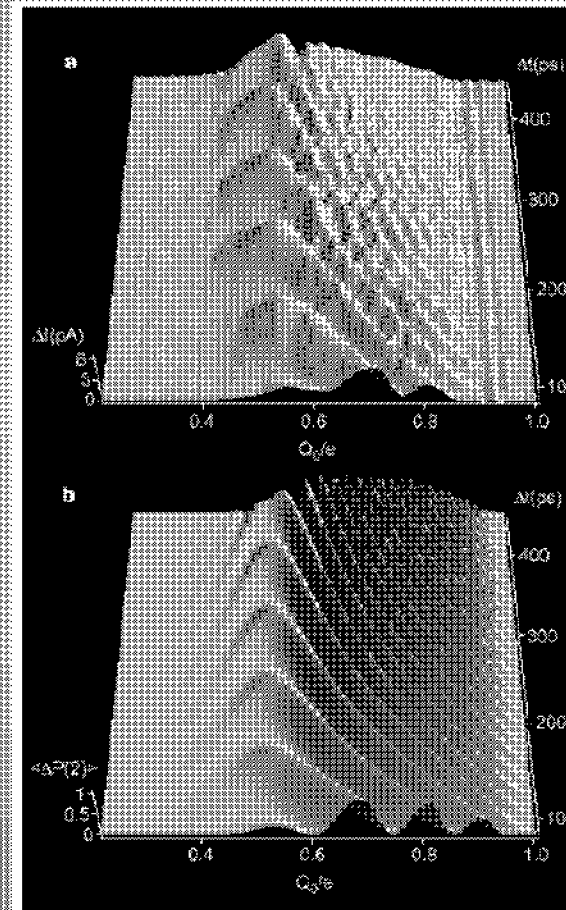
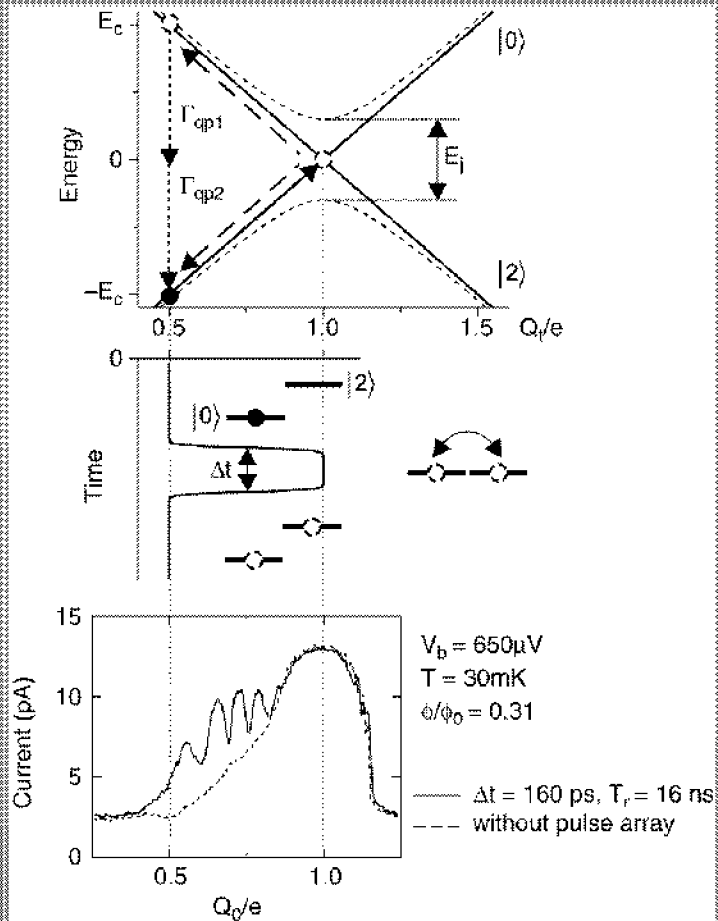


$T_2^* \approx 110$ ps, during
continuous measurement.

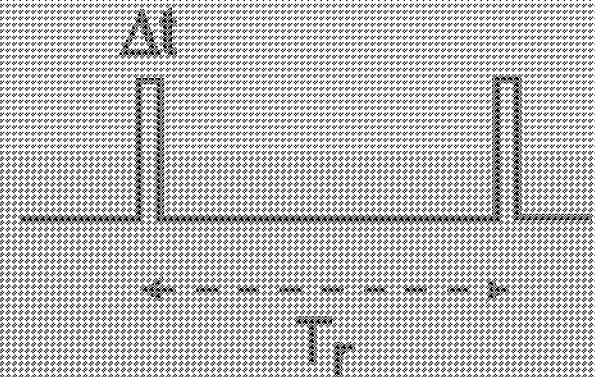
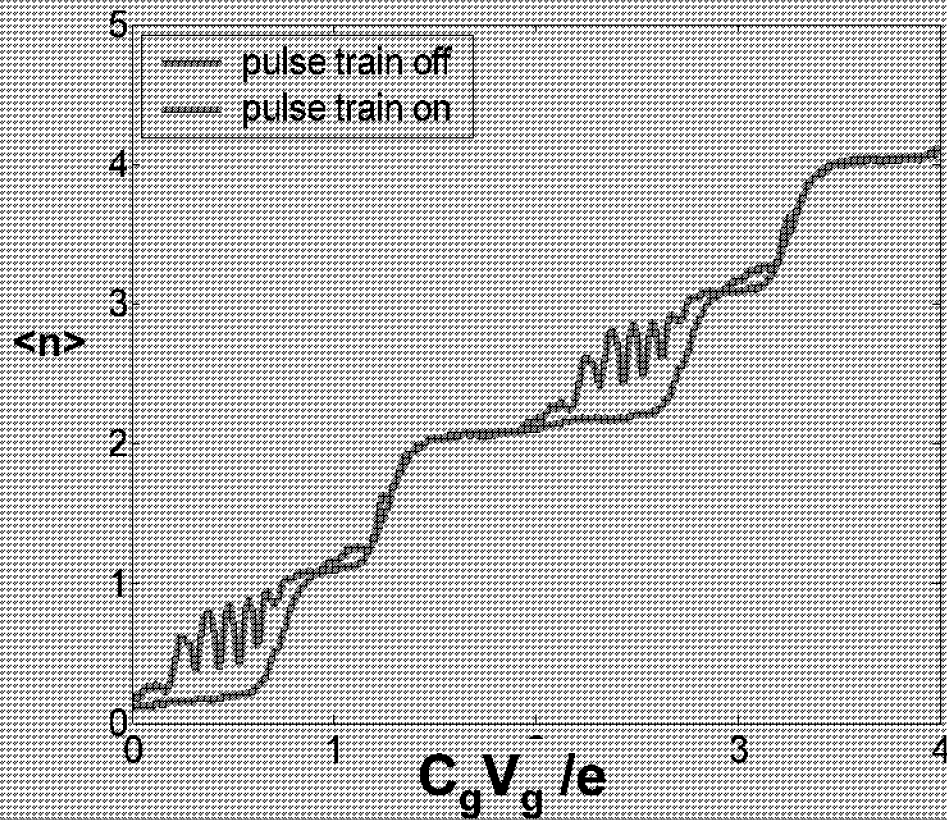
Coherent Charge Oscillations

Observed by continuous measurement with the RF-SET,
while applying fast pulses to the box gate.

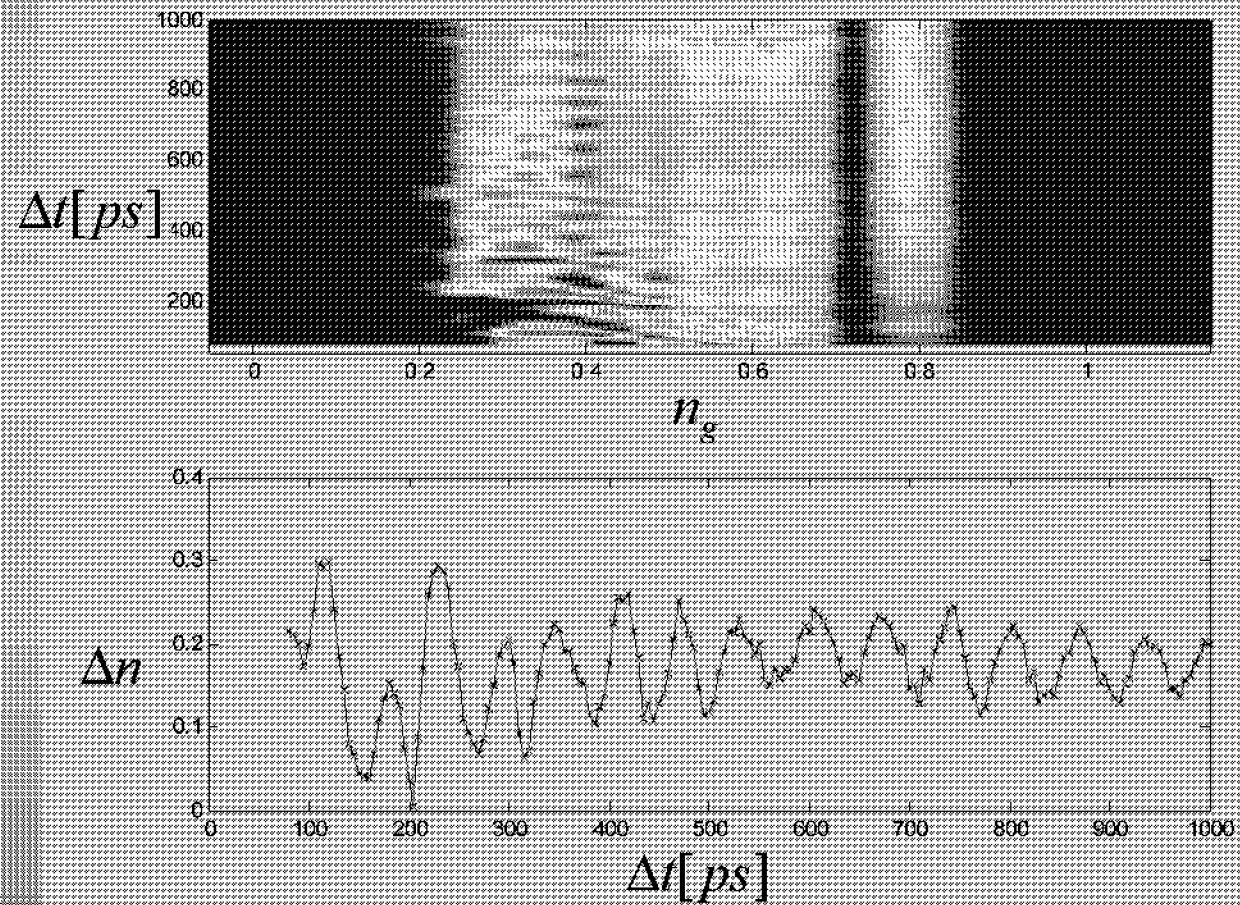
Makamura, Pashkin and Tsai (1999)



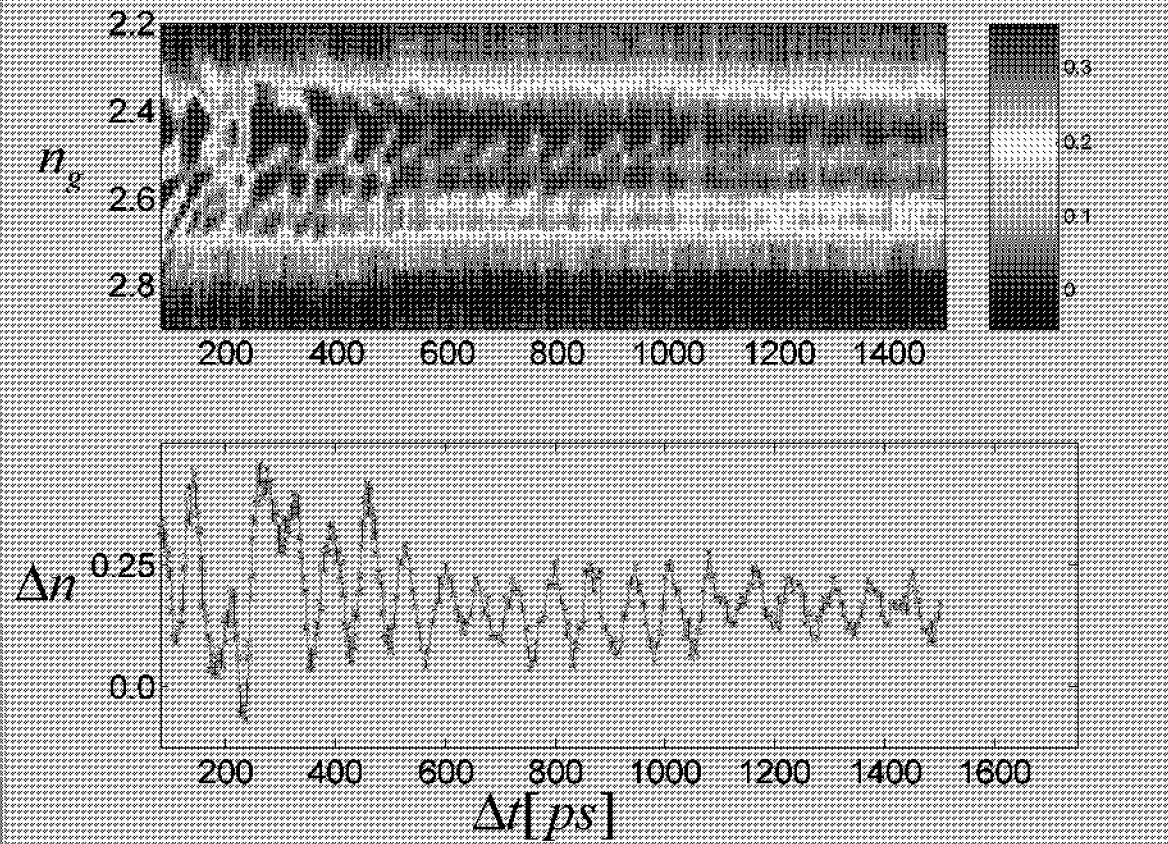
Continuous measurement with $T_r = 59\text{ns}$, amplitude $1e$ pulse train



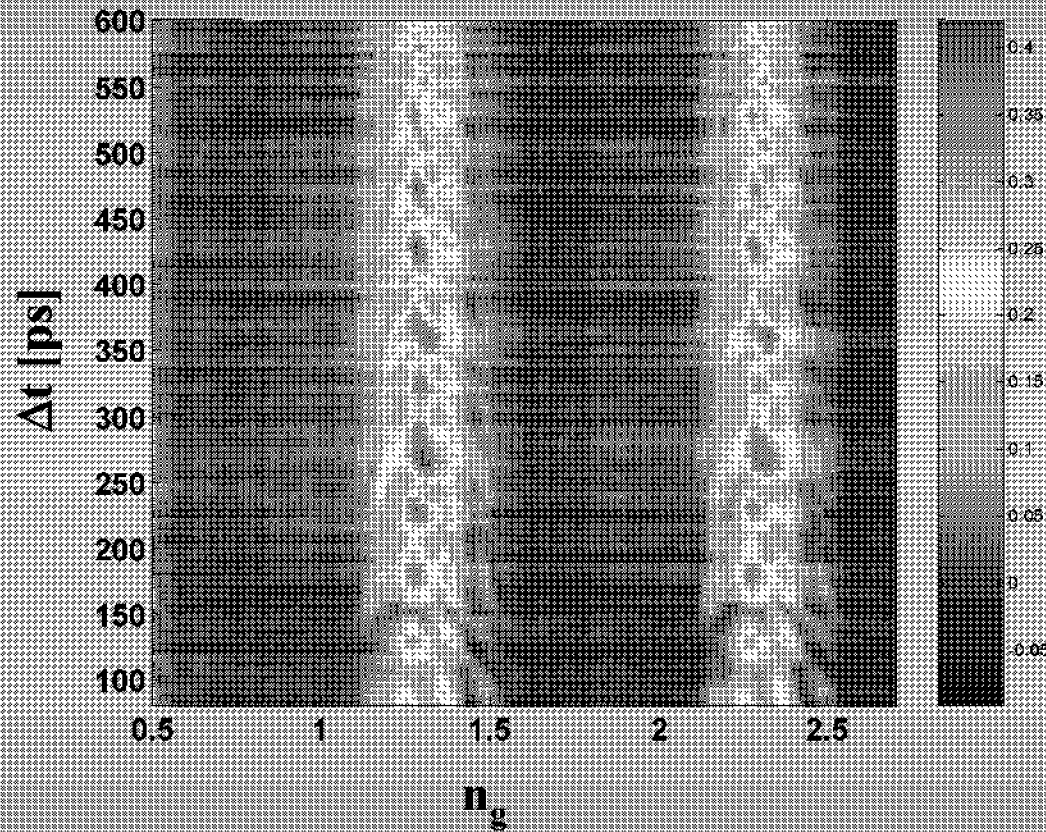
Coherent Oscillations



$B_1=0.30$ T, $E_J=0.67$ K



Oscillations of even AND odd parity states!

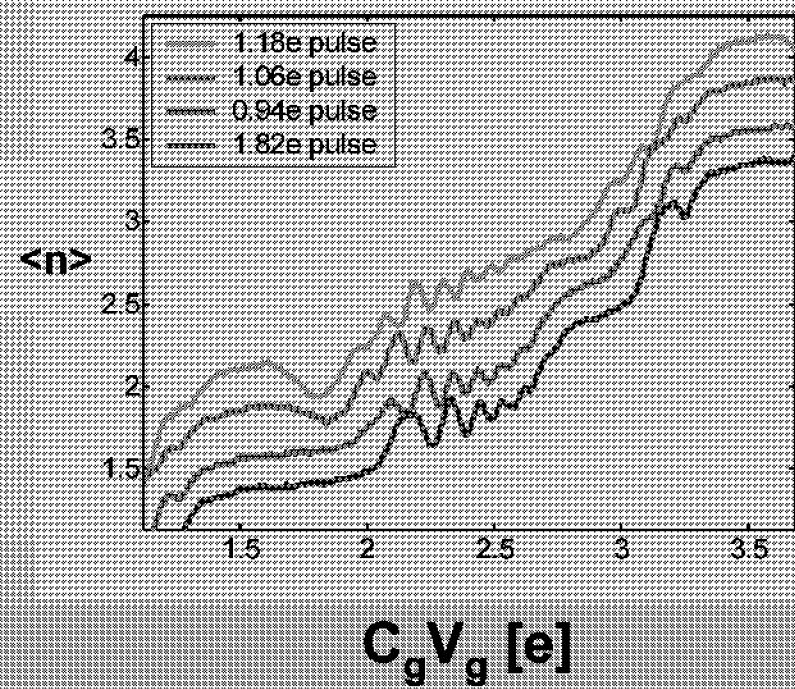
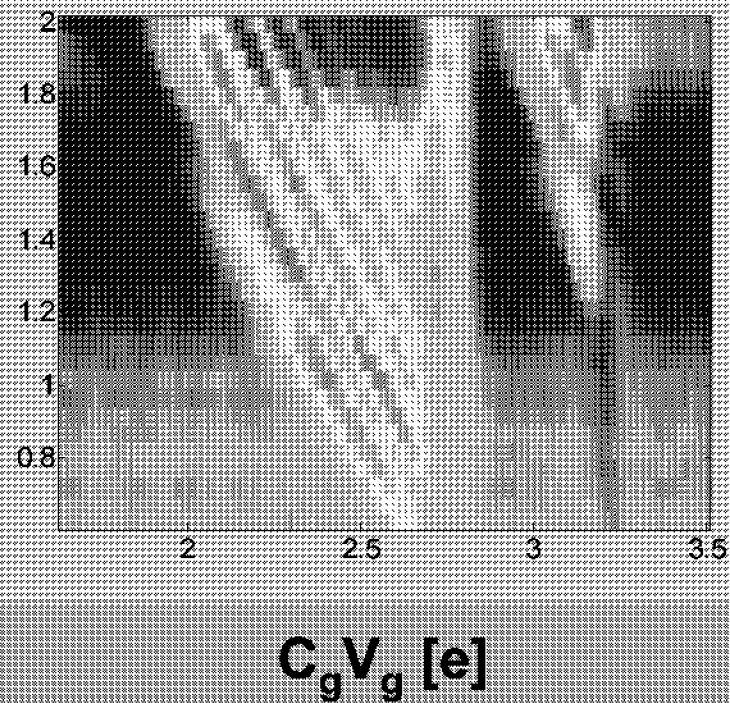


$B_{||}=0T$, bias at JQP where staircases are e-periodic.

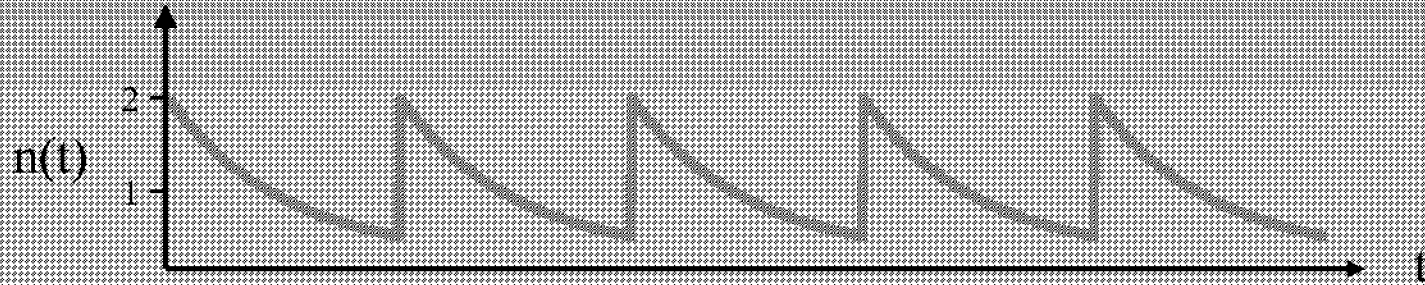
Quasi-particles not always 'bad'?

Pulse Amplitude Dependence

Pulse Amplitude

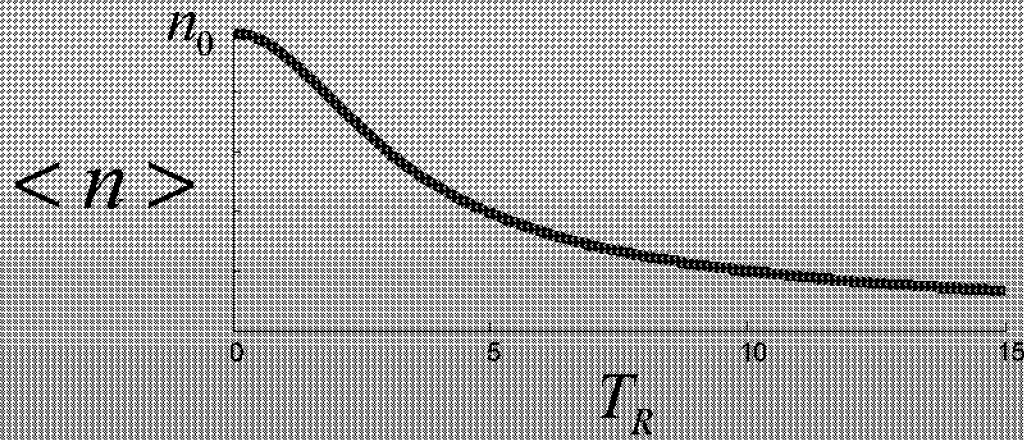


Dependence of Amplitude on T_1 and T_R

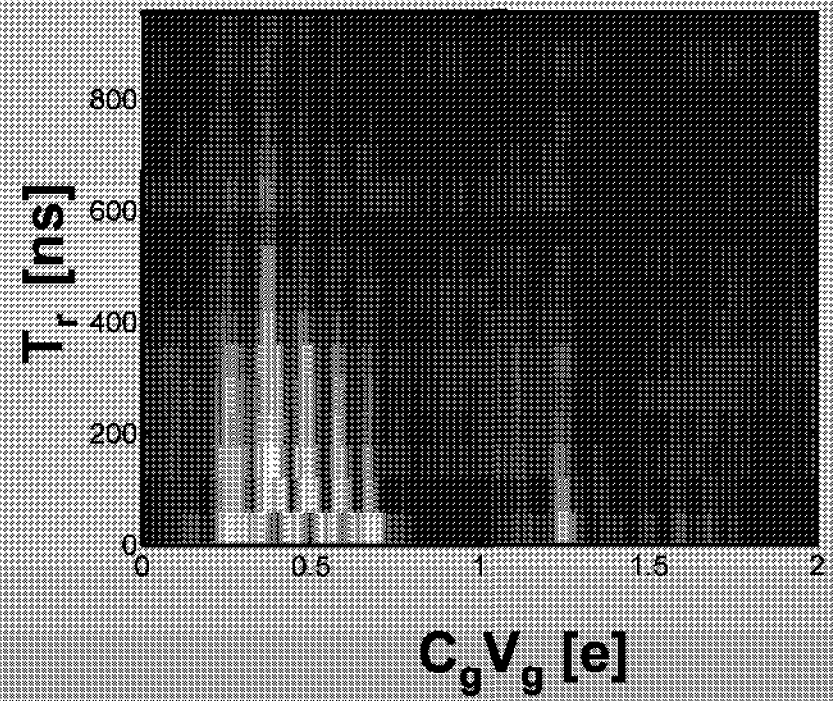
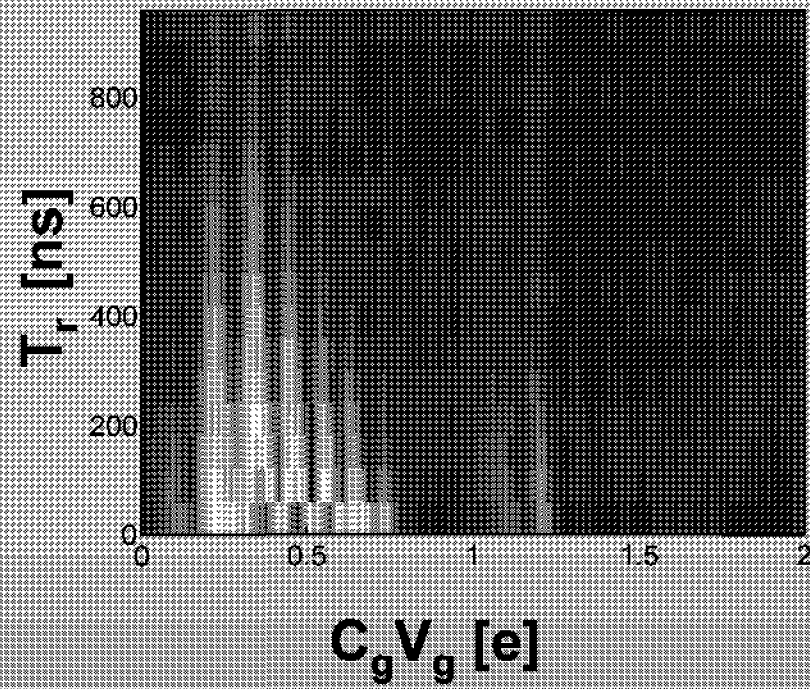


$$\langle n \rangle (T_R) = 2n_0 \frac{T_1}{T_R} \frac{1 - e^{-T_R/T_1}}{1 + e^{-T_R/T_1}}$$

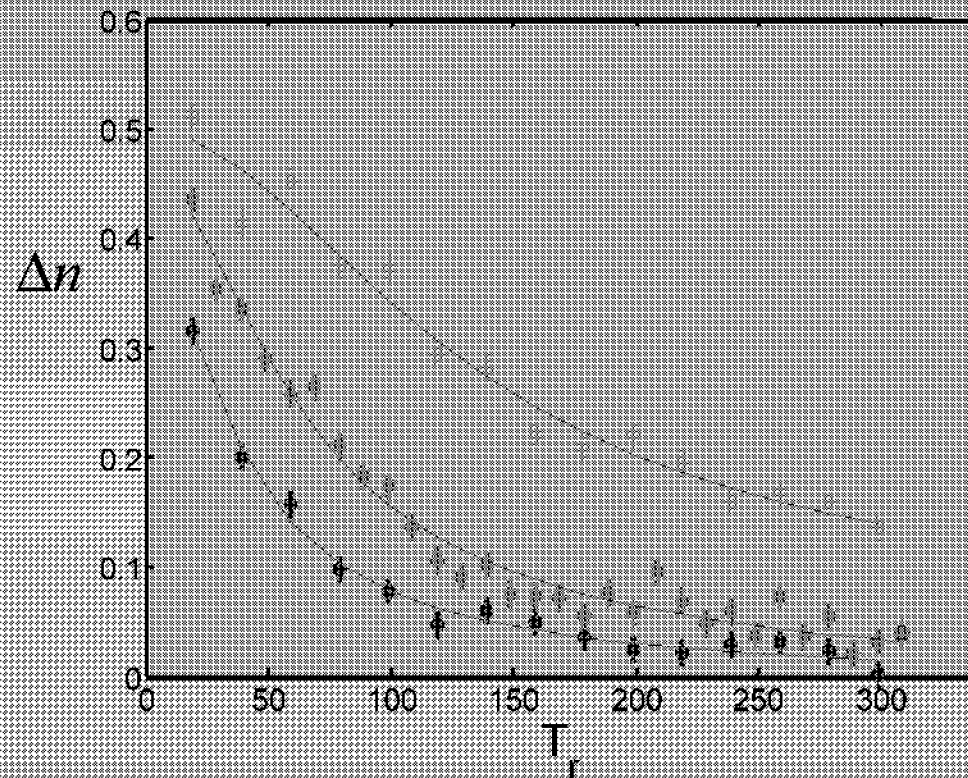
$$\sim 2n_0 \frac{T_1}{T_R}$$



T_r Measurements at $B_r=0.30T$



T_1 measurements at $B_z=0.0T$



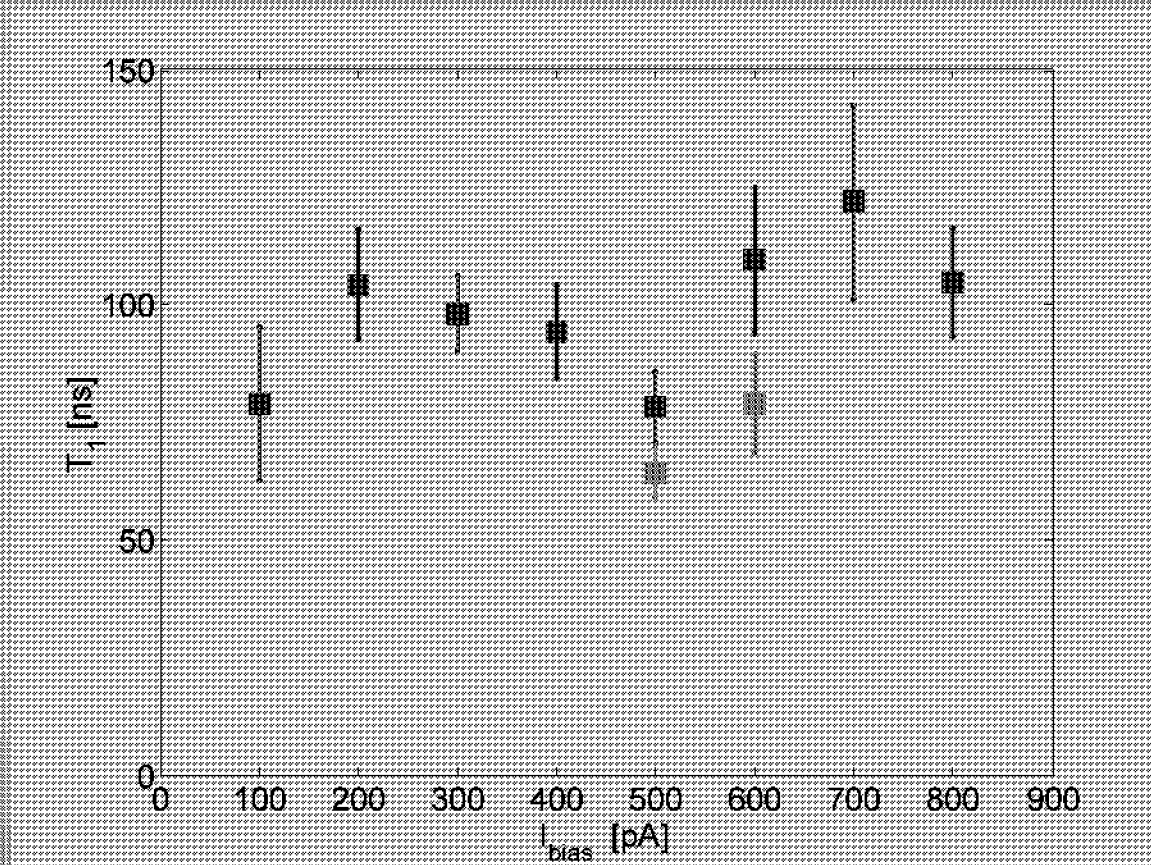
DJQP: $I_b=300\text{pA}$, $T_1=40\text{ns}$

JQP: $I_b=1300\text{pA}$, $T_1=19\text{ns}$

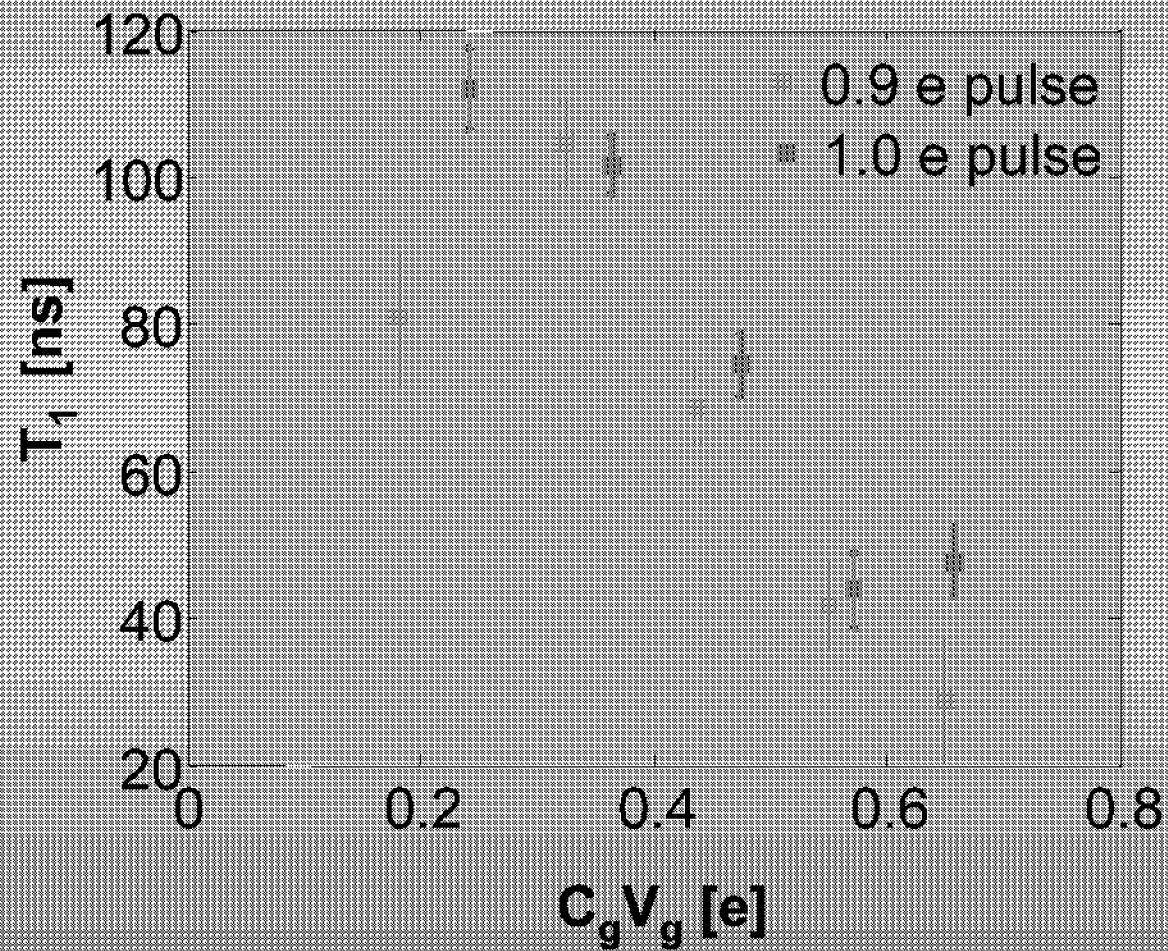
JQP: $I_b=2300\text{pA}$, $T_1=12\text{ns}$

Note that measurement fidelity
is $> 50\%$.

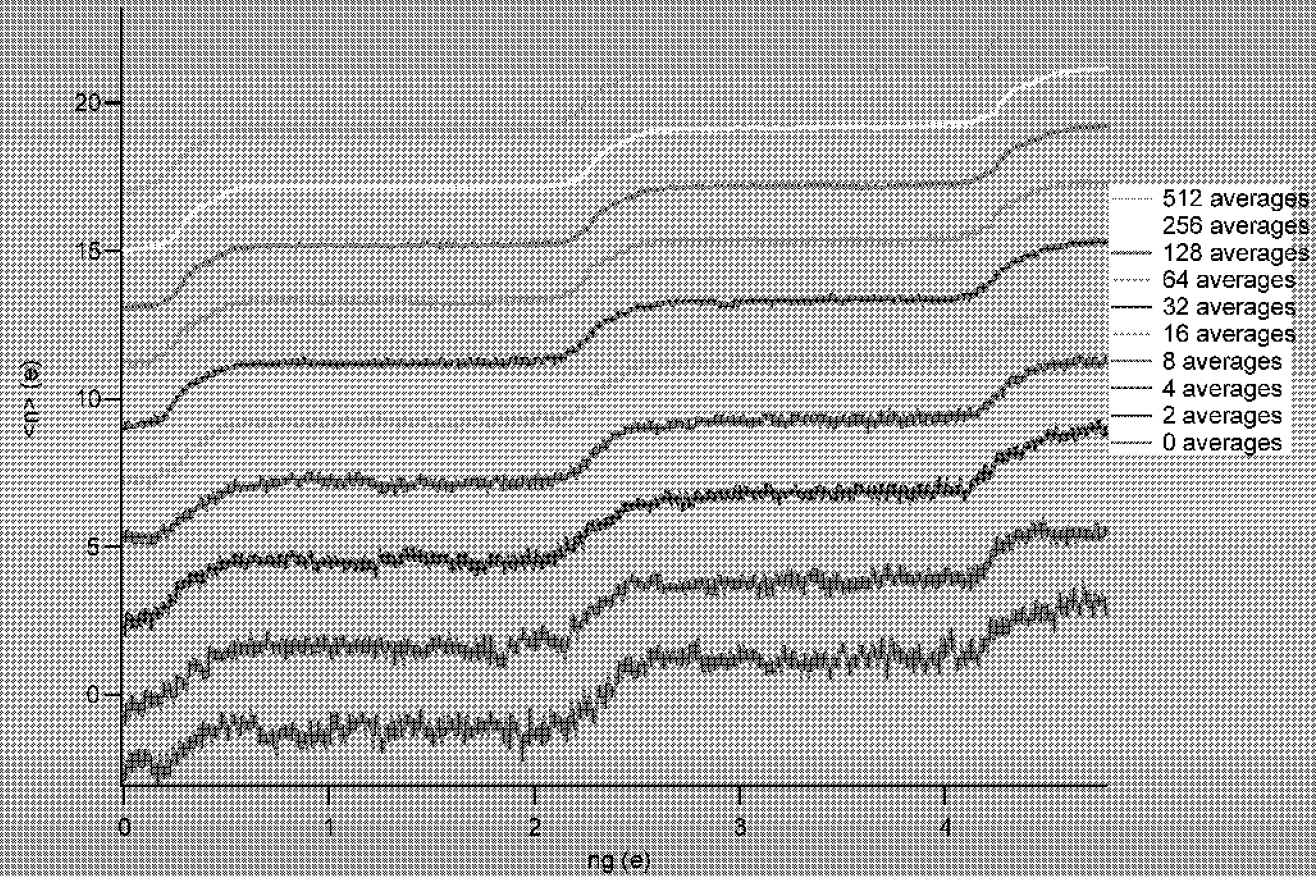
T_1 measurements at $B_{||}=0.30\text{T}$



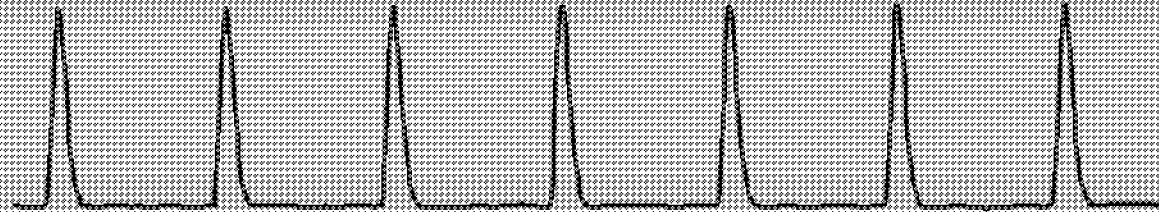
Dependence of T_1 on ΔE at $B_f=0.30\text{T}$



Approaching Single-Shot Sensitivity

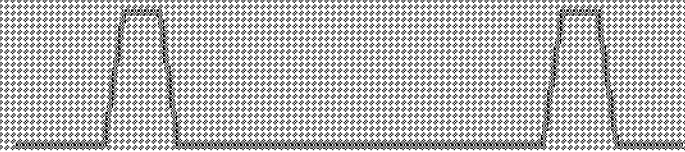


Pulsed Mode Measurements

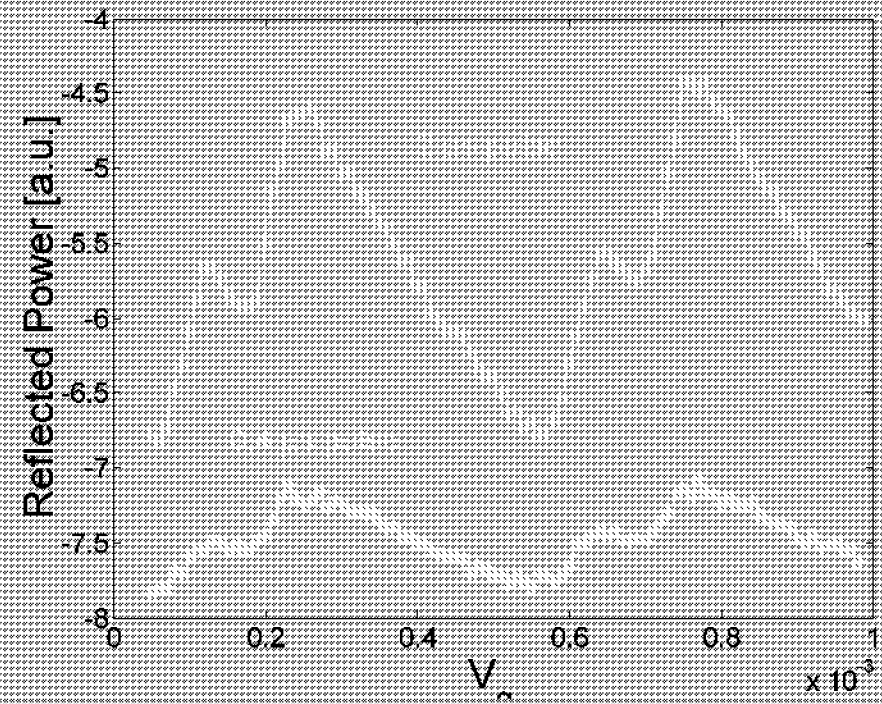


Pulsed RF Read-out

width: 0.3-2.0 μs
 T_F : 10 μs

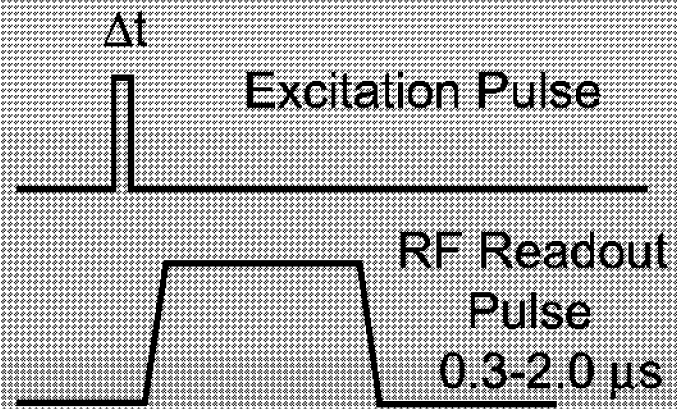


Low RF power, 3e DC bias
and
High power, mid-gap DC bias

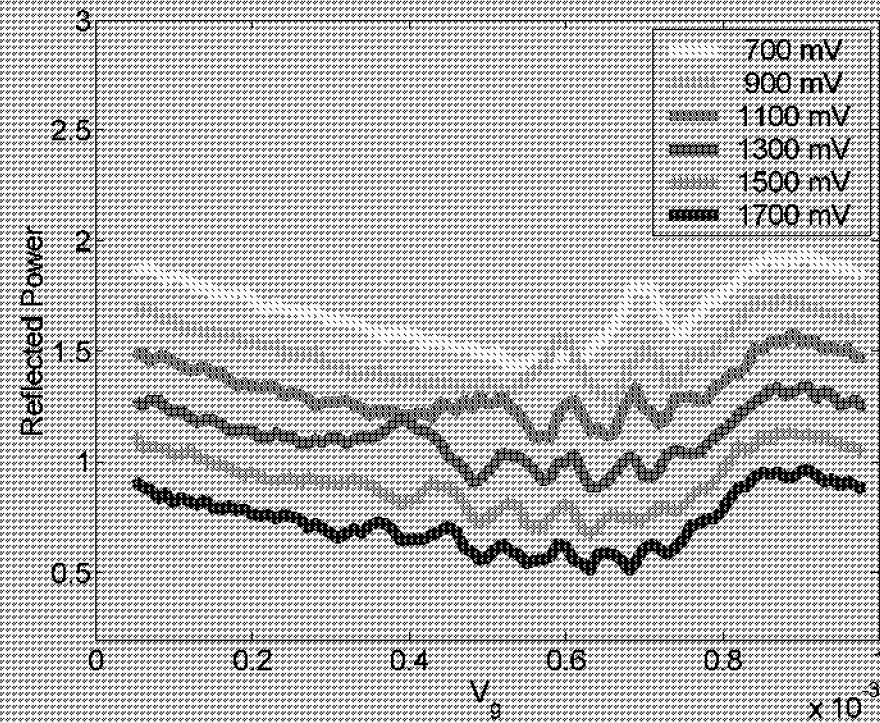


512 repetitions / pt.

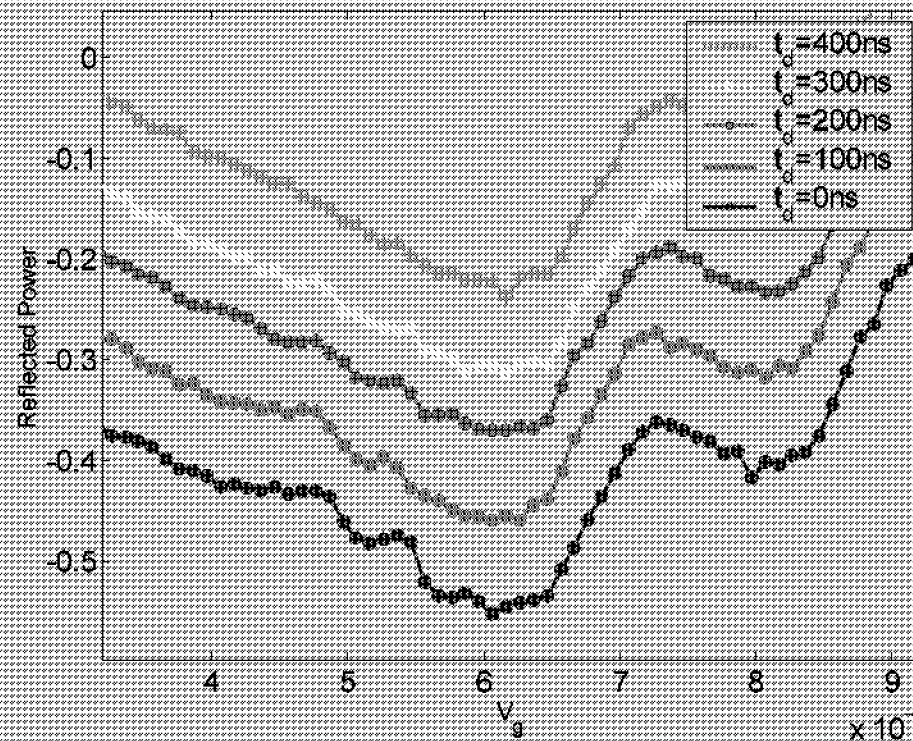
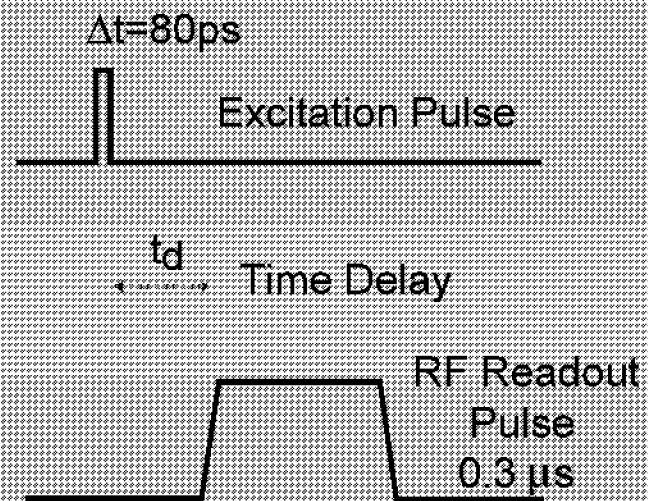
Pulsed Read-out of Excited State



0.3 μs read-out pulse, $B=0.72\text{T}$



Probing T_1 with Pulsed Measurement



Conclusions

- Demonstrated continuous and pulsed read-out of box charge.
- Observed coherent free-precession of charge (reproduced Nakamura's results using fast pulses and RF-SET read-out).
- RF-SET coupled to a single-Cooper-pair box is a very unique system: a ~~macroscopic~~, er, mesoscopic quantum device measuring mesoscopic quantum coherence.
- T_1 measurements show effects of 'back-action', although T_1 saturates at ~ 100 ns, even with pulsed measurement.
- Improvements needed and planned:
 - Quasi-particle traps, lower E_C , better microwave engineering.
 - SQUID amplifier
 - Coplanar waveguides
 - Better control of E_J
 - Capability of fast pulsing on SET gate and bias.