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**JOINT ICTP-INFM SCHOOL/WORKSHOP ON  
"ENTANGLEMENT AT THE NANOSCALE"**

(28 October – 8 November 2002)

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*" Semiconductor quantum dots : artificial atoms for quantum optics "*

presented by:

**G. M. Gerard**  
DRFMC/CEA, Grenoble  
France



# Semiconductor quantum dots : artificial atoms for quantum optics

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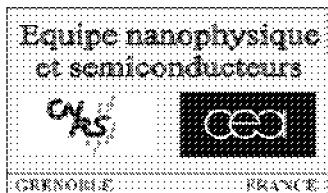
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Work mostly done at CNRS/LPN (Bagneux-> Marcoussis 09/01)  
in collaboration with:

E.Moreau, I. Robert, B. Gayral, I. Abram  
V. Thierry-Mieg (MBE), L. Manin (RIE)

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# Spontaneous emission control in semiconductors

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Many attempts to control SE in semiconductors since ~1975  
by tailoring...

electronic states  
Q wells, Q dots

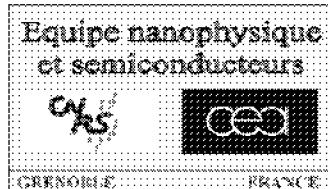
photonic modes  
microcavities, photonic crystals

...for novel/improved optoelectronic devices!

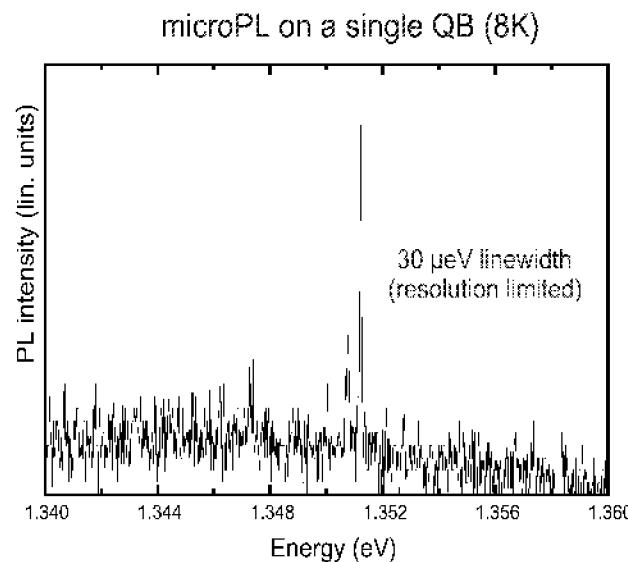
e.g. strained QW lasers (86)

high-efficiency microcavity LEDs (93)  
low-threshold VCSELs ( $30 \mu\text{W}$ ) (95)

strong-coupling regime for QWs (92)



# QDs : artificial atoms for quantum optics



Marzin et al,  
PRL 73, 1138 (1994)

close analogy with single-atom quantum optics

- e.g. coherent control of QD excitons (2001)

New!

- solid-state CQED : Purcell effect (1997)
- generation of quantum states of light (2000)

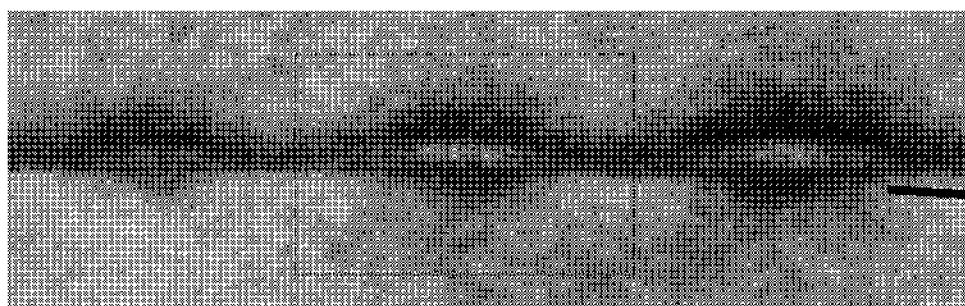
ultimate control on SE, on the single photon level

=> first single-mode single-photon source (2001)

# A single-mode single-photon source

Isolated InAs QD

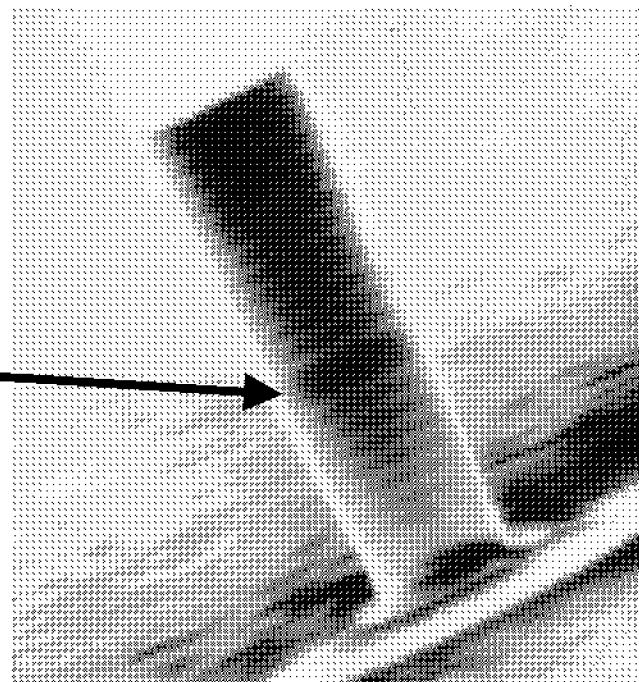
20 nm



=> Single-photon emission

E. Moreau et al,  
Appl. Phys. Lett. 79, 2865 (2001)

GaAs/AlAs micropillar



⇒ Efficient collection  
+  
single-mode behavior

# Outline

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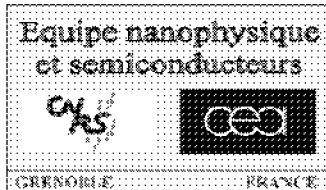
Single photon sources : applications and requirements

Generation of quantum states of light

QDs in microcavities and the photon collection issue

A single-mode single photon source

Prospects



# Single-photon source

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Deterministic emission of light pulses containing  
one and only one photon

Metrology

flux+energy standard

Quantum Key  
Distribution

Polarisation-encoded single photons

Quantum computing

single photons as Q-bits

Equipe nanophysique  
et semiconducteurs



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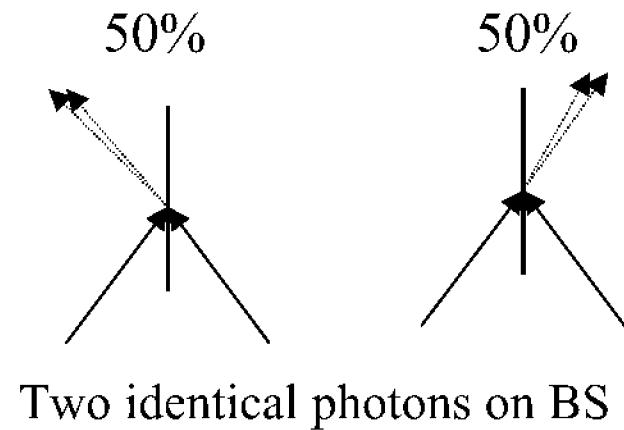
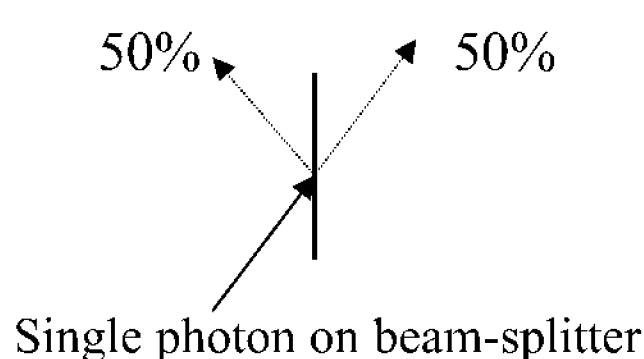


LABORATOIRE DE  
DE PHOTONIQUE  
ET DE NANOSTRUCTURES



# Single photons for quantum computing

Knill et al, Nature 409, 46 (01) « Quantum computing using SPs and linear optics »

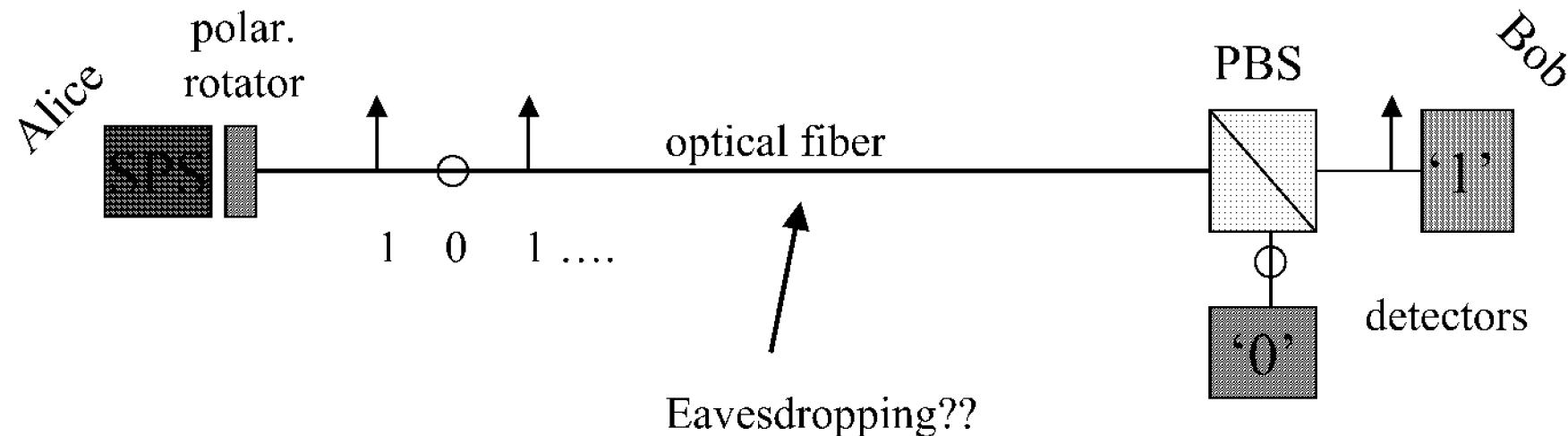


Logical optical gate based on single photons!

Requirements: same mode +polarisation  
SPS efficiency ~1  
Fourier transform limited ( $\Delta v \cdot \Delta \tau = 1/4\pi$ )

Decoherence control !

# Single photon sources for quantum key distribution



Alice and Bob share a binary key

This protocol can be made intrinsically secure

(Bennett+Brassard 84 : eavesdropping=> more than 25 % errors)

Secure for present as well as future technology

# Constraints for secure QKD : 1) dark counts

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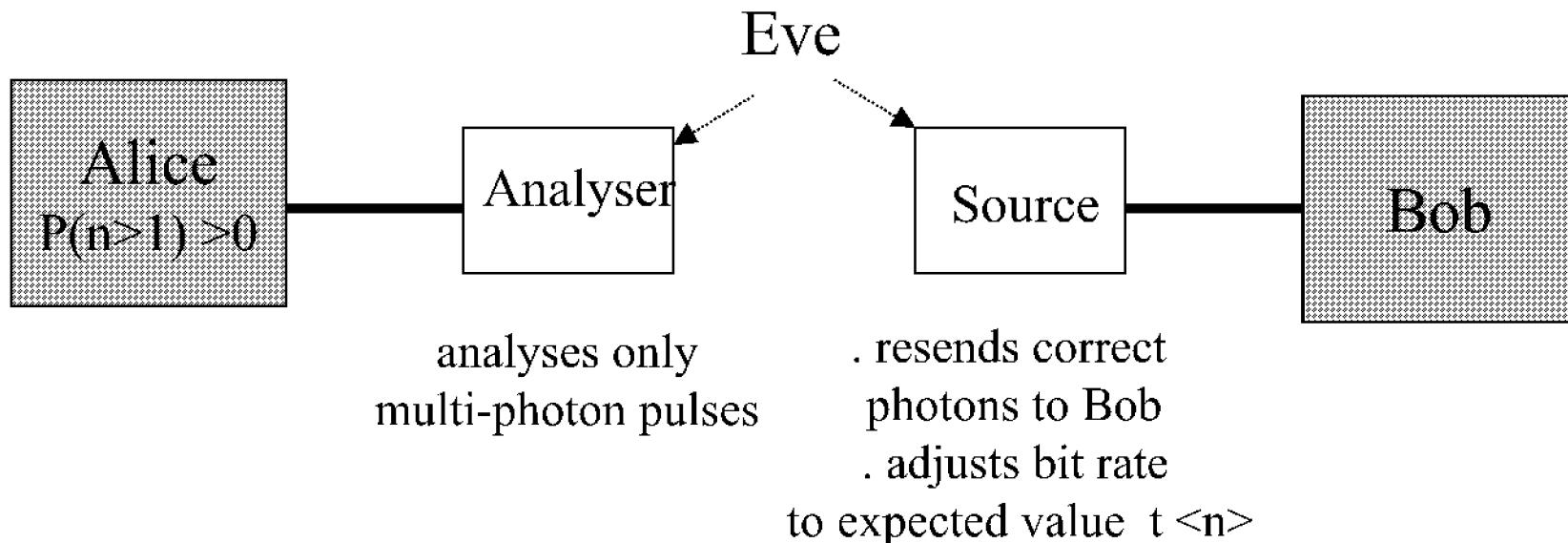


Error correction possible  $\Leftrightarrow < n > t > 10 d$

• limited secure transmission length  
(~100km at most at telecom wavelength)

# Constraints for secure QKD : 2) multi-photon pulses

Lossy channel  $\Rightarrow$  « Photon-Number Splitting » attack



PNS works  $\Leftrightarrow p(n>1) > t \langle n \rangle$

# Secure QKD with weak coherent pulses

$$\langle n \rangle \ll 1$$

$$P(n>1) \sim \frac{\langle n \rangle^2}{2}$$

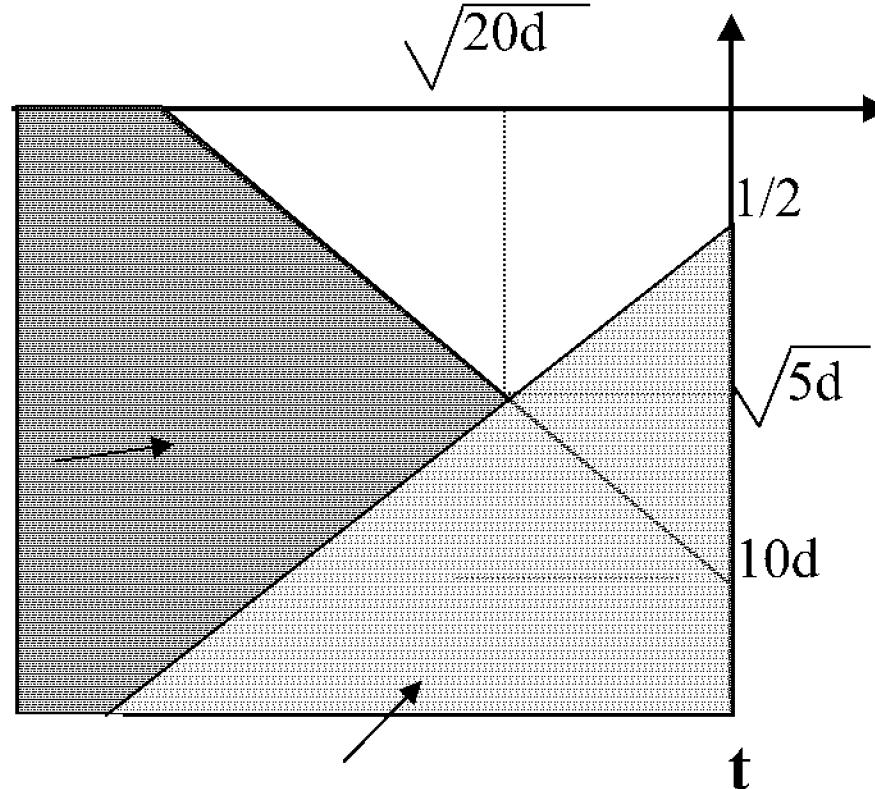
Too many dark counts

$$t \cdot \langle n \rangle < 10 d$$

Too many multi-photon pulses  
 $\langle n \rangle / 2 > t$

$$\langle n \rangle$$

See e.g. Brassard et al  
PRL 85, 1330 (00)

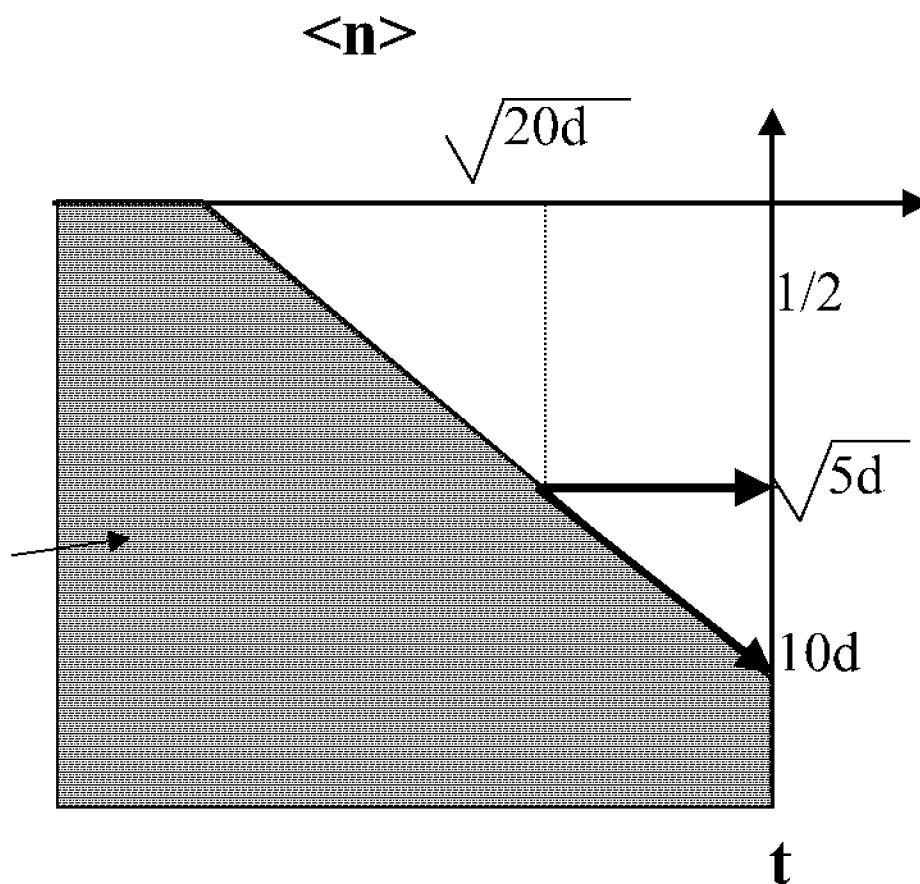


$$\langle n \rangle_{\text{opt}} \sim 4 \cdot 10^{-3} @ 1.3 \mu\text{m}$$

=> low bit rate

# Secure QKD with a perfect SPS

Too many dark counts  
 $t \cdot \langle n \rangle < 10 d$



# SPS vs weak coherent sources

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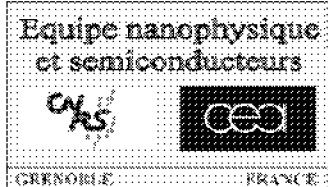
Replacement of attenuated lasers by a perfect SPS (@1.3 μm)

=> secure channel length x 2

=> bit rate x 100

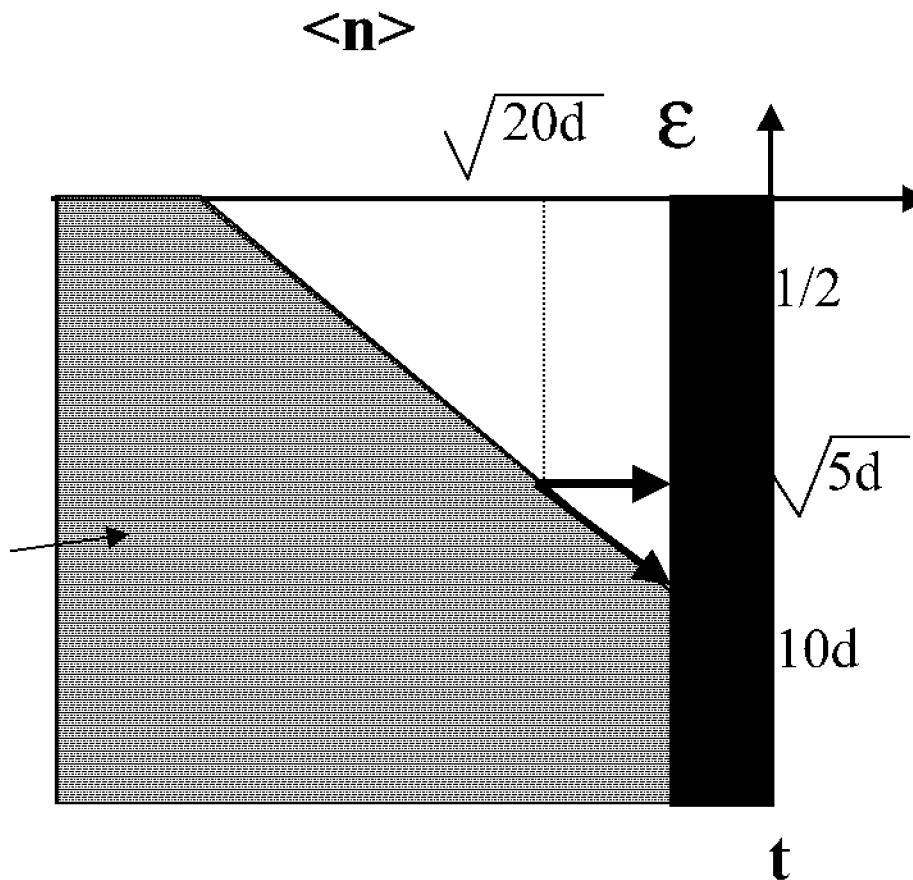
See Brassard et al, PRL 85, 1330 (2000)

What about unperfect single photon sources???



# SPS with limited efficiency ( $\varepsilon < 1$ )

Too many dark counts  
 $t \cdot \langle n \rangle < 10 d$

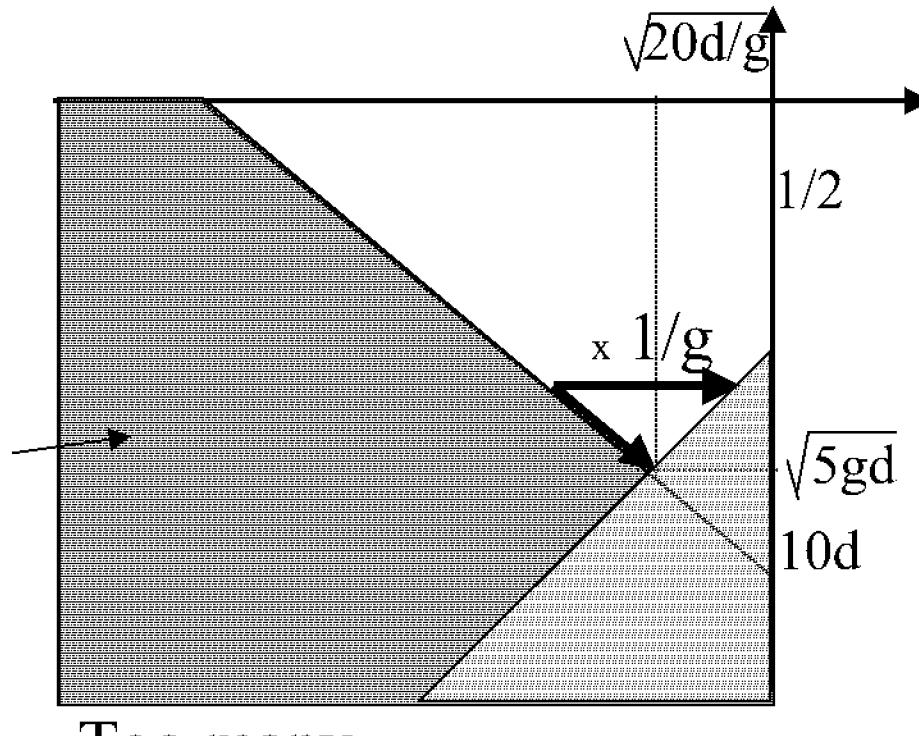


# Unperfect SPS ( $0 < g < 1$ )

$$P(n=2) = g \frac{\langle n \rangle^2}{2}$$

$\langle n \rangle$

Too many dark counts



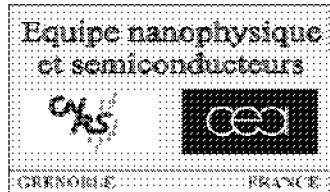
Too many multi-photon pulses  
 $g \langle n \rangle / 2 > t$

# Conclusion

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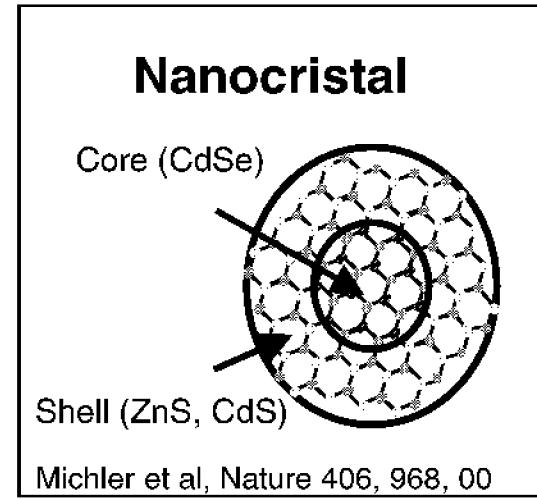
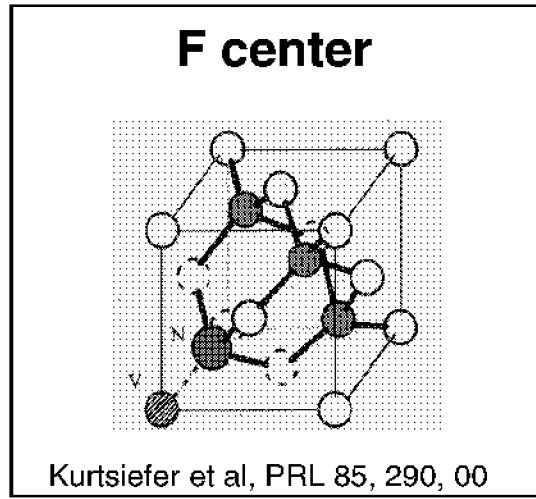
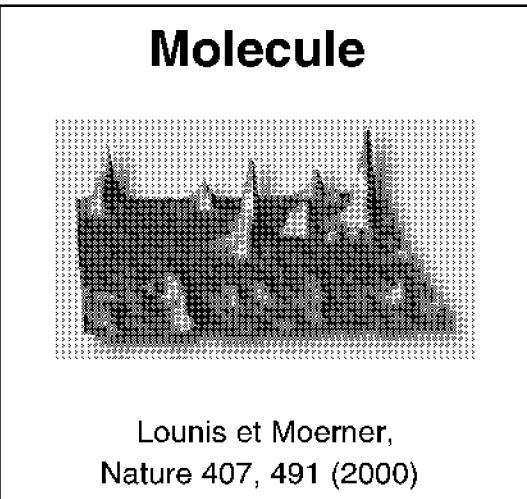
It is essential for a practical Single Photon Source to present both

- . a large efficiency  $p(n=1) = \mathbf{\Sigma} \sim 1$
- . a weak probability to emit multi-photon pulses ( $g \ll 1$ )

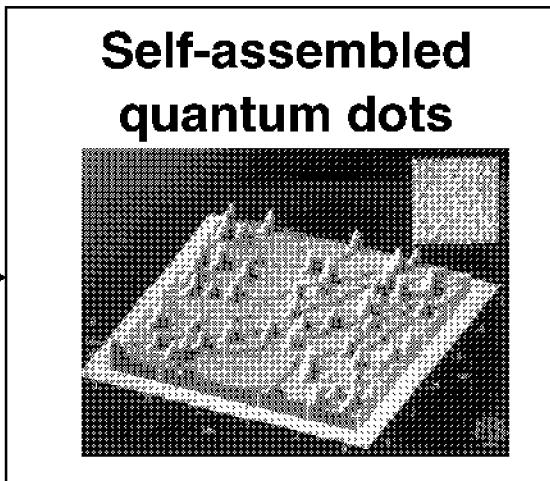


# Solid-state single photon emitters

at 300 K !



$T < 50K$   
until now!

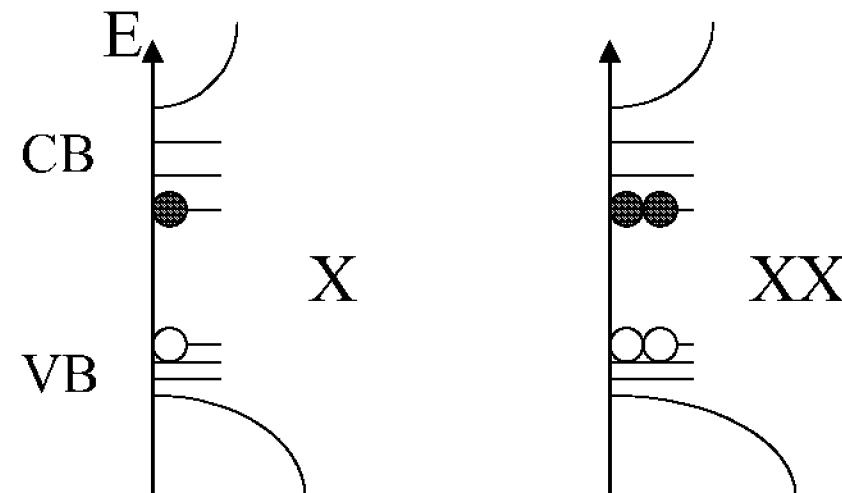


# QD assets for single-photon generation

QDs are      stable      (no blinking, no bleaching)  
                  efficient ( $\eta \sim 1$ )  
                  fast      ( $\tau \sim 1\text{ns}$ )  
                  spectrally narrow at low T

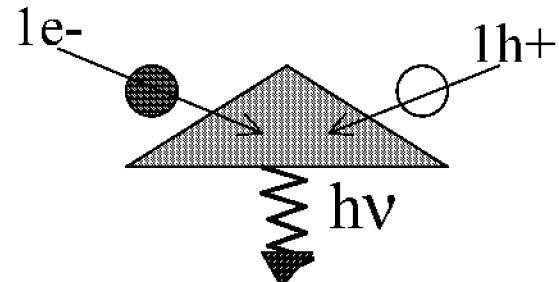
+ adjustable bandgap/non-resonant pumping OK

Pb: a QD is not  
a 2-level system!



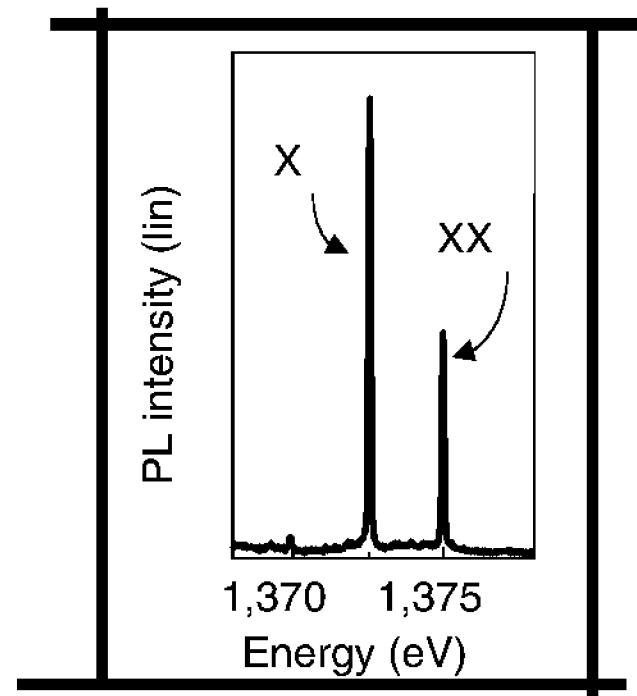
# Strategies for single photon generation

Injection controlled by Coulomb blockade (Yamamoto et al, Nature 99)



$T < 0.1\text{K}$ , no microcavity yet

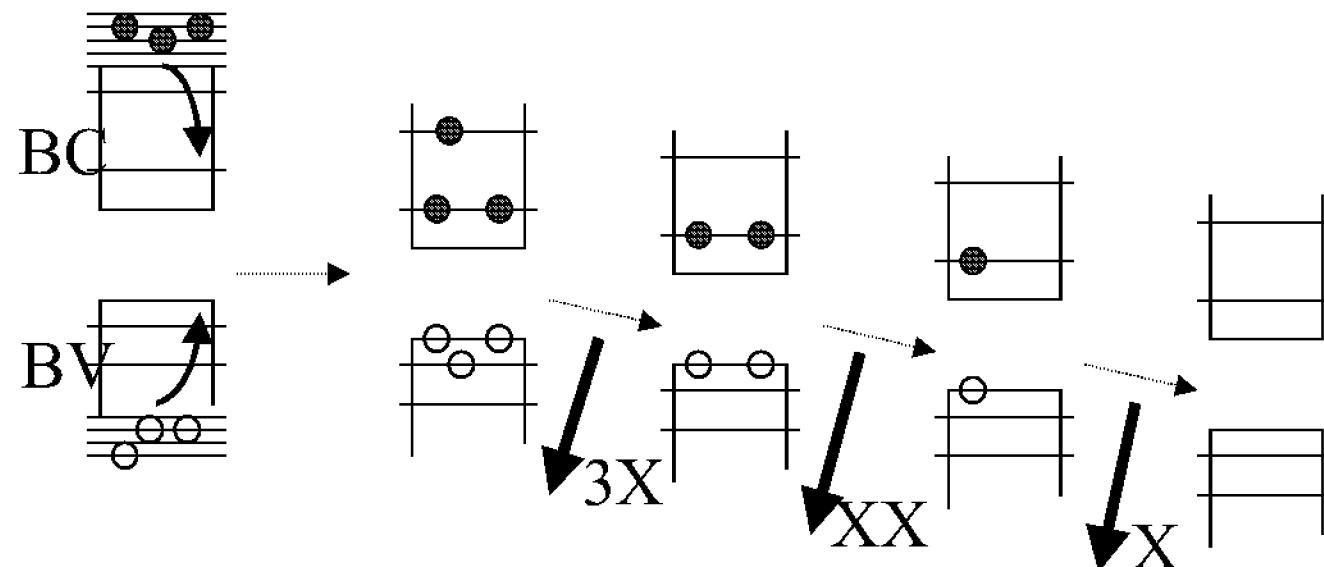
Implement Coulomb interaction between trapped charge carriers



*More efficient!*

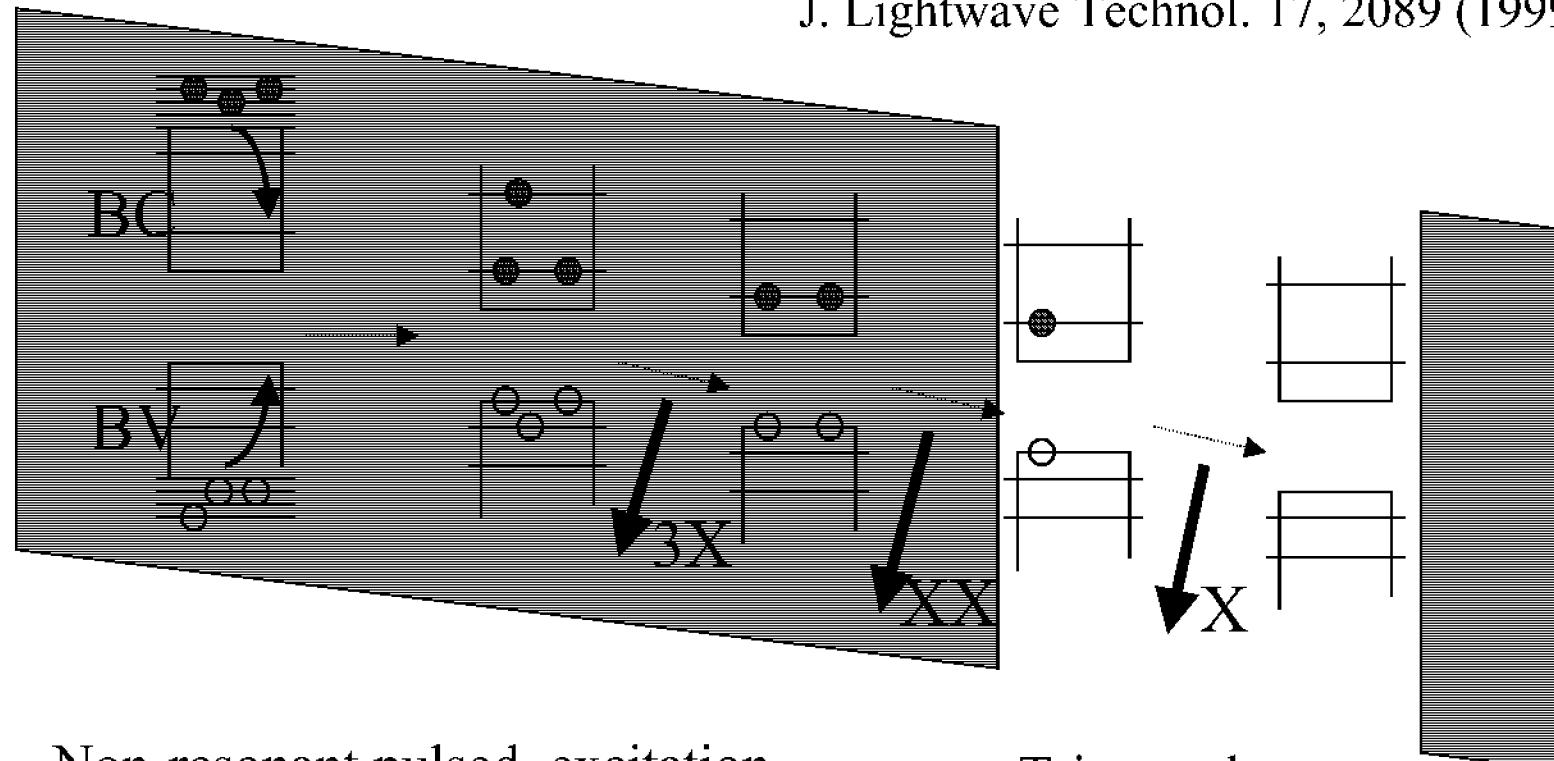
# Single photon generation from a QD

Proposal: J.M. Gérard et B. Gayral,  
J. Lightwave Technol. 17, 2089 (1999)



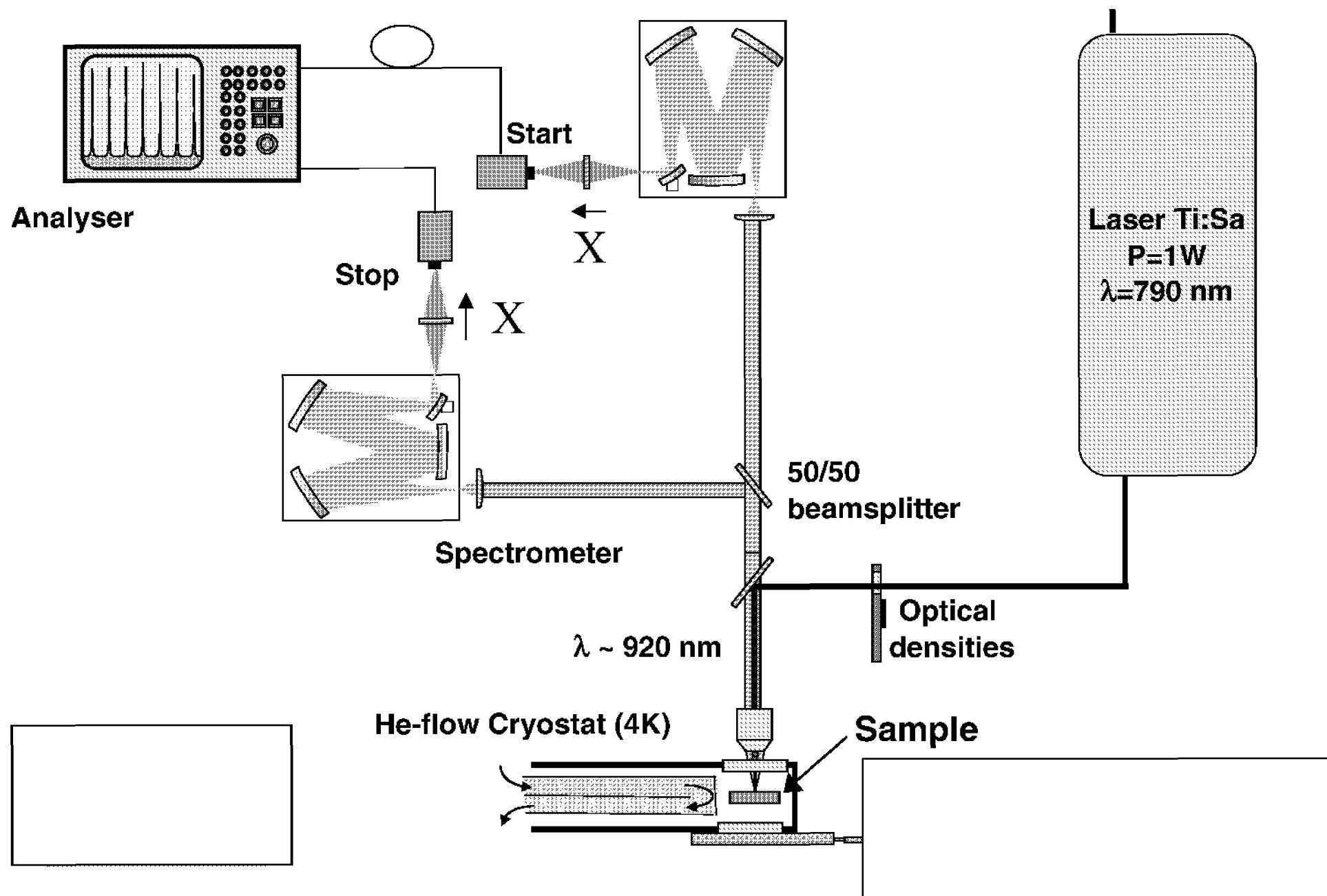
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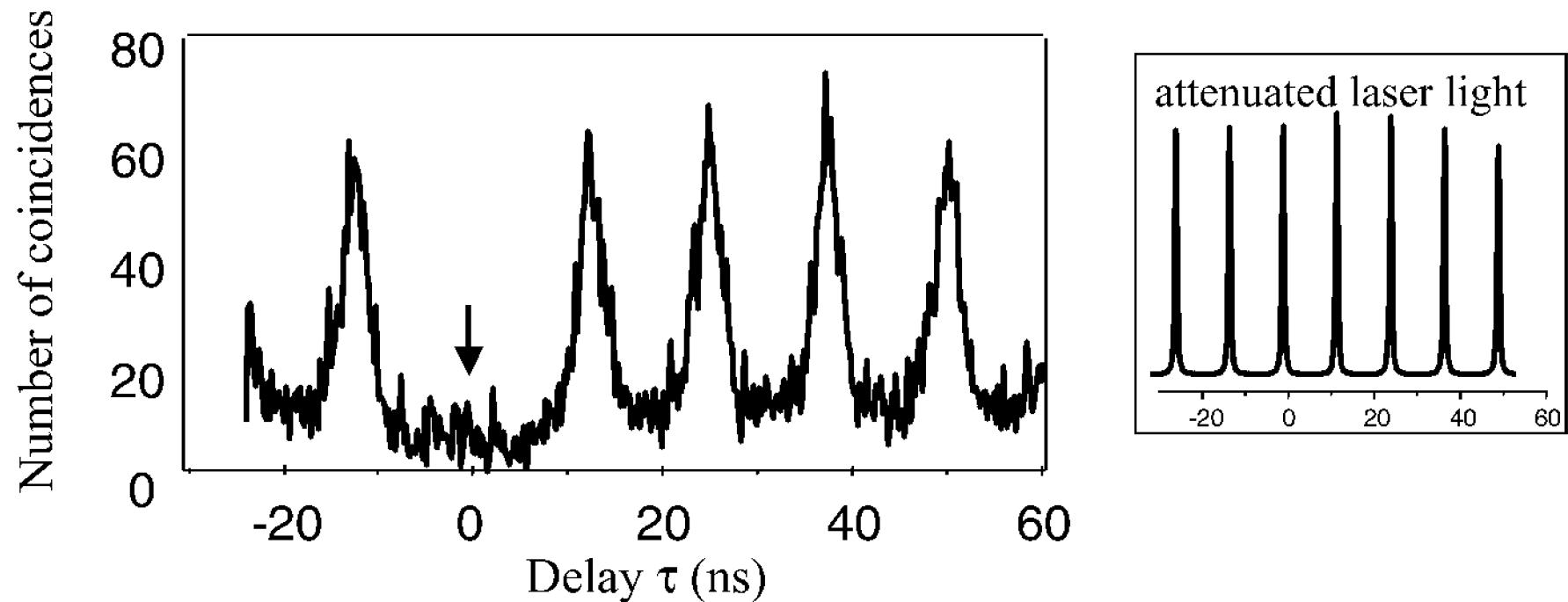
+ Non-resonant pulsed excitation  
+ Spectral filtering  $\Rightarrow$  Triggered Single photon

# Photon correlation setup



# X line correlation histogram

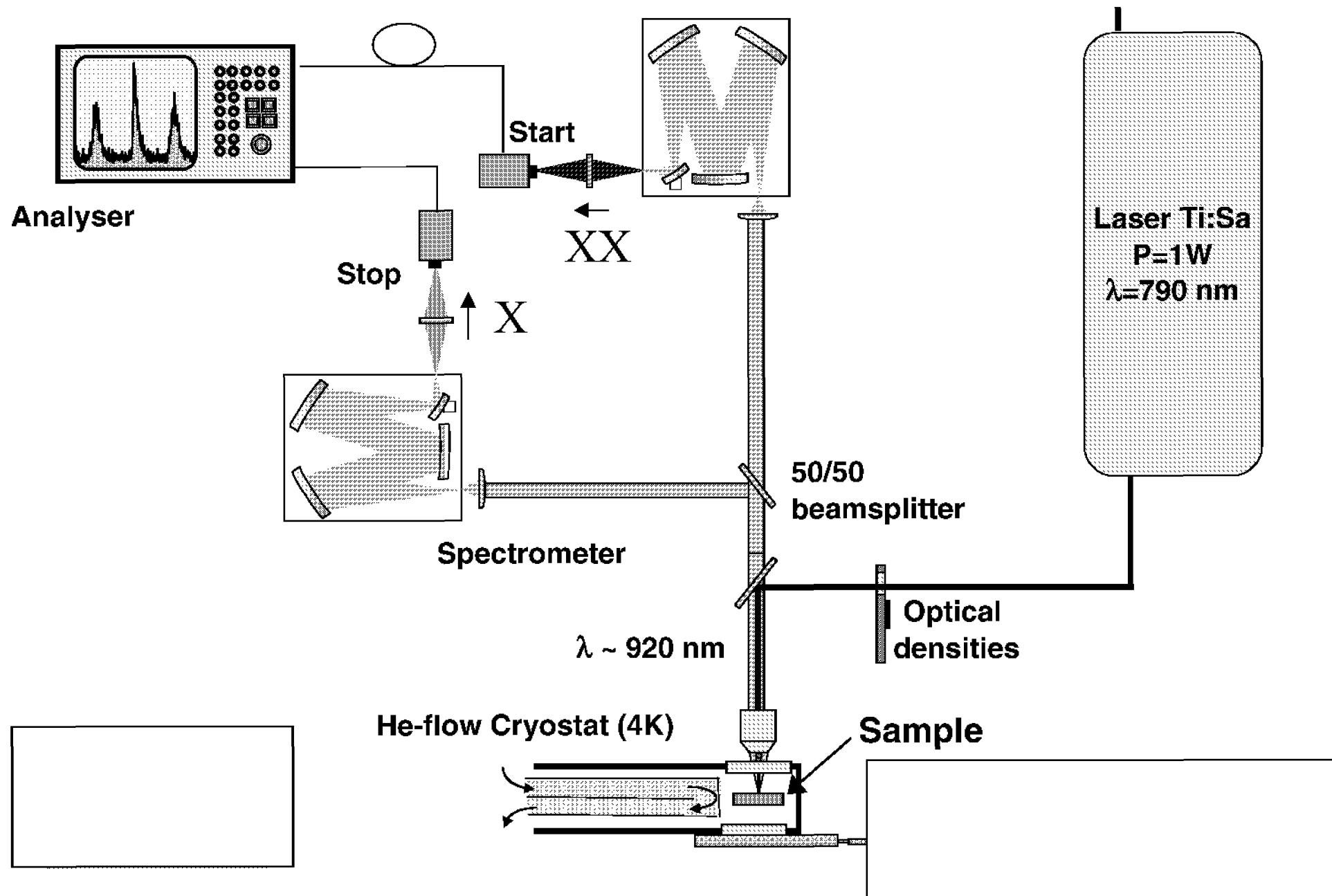
First reports: P. Michler et al, Science 290, 2282 (2000)  
C. Santori et al, PRL 86, 1502 (2000)



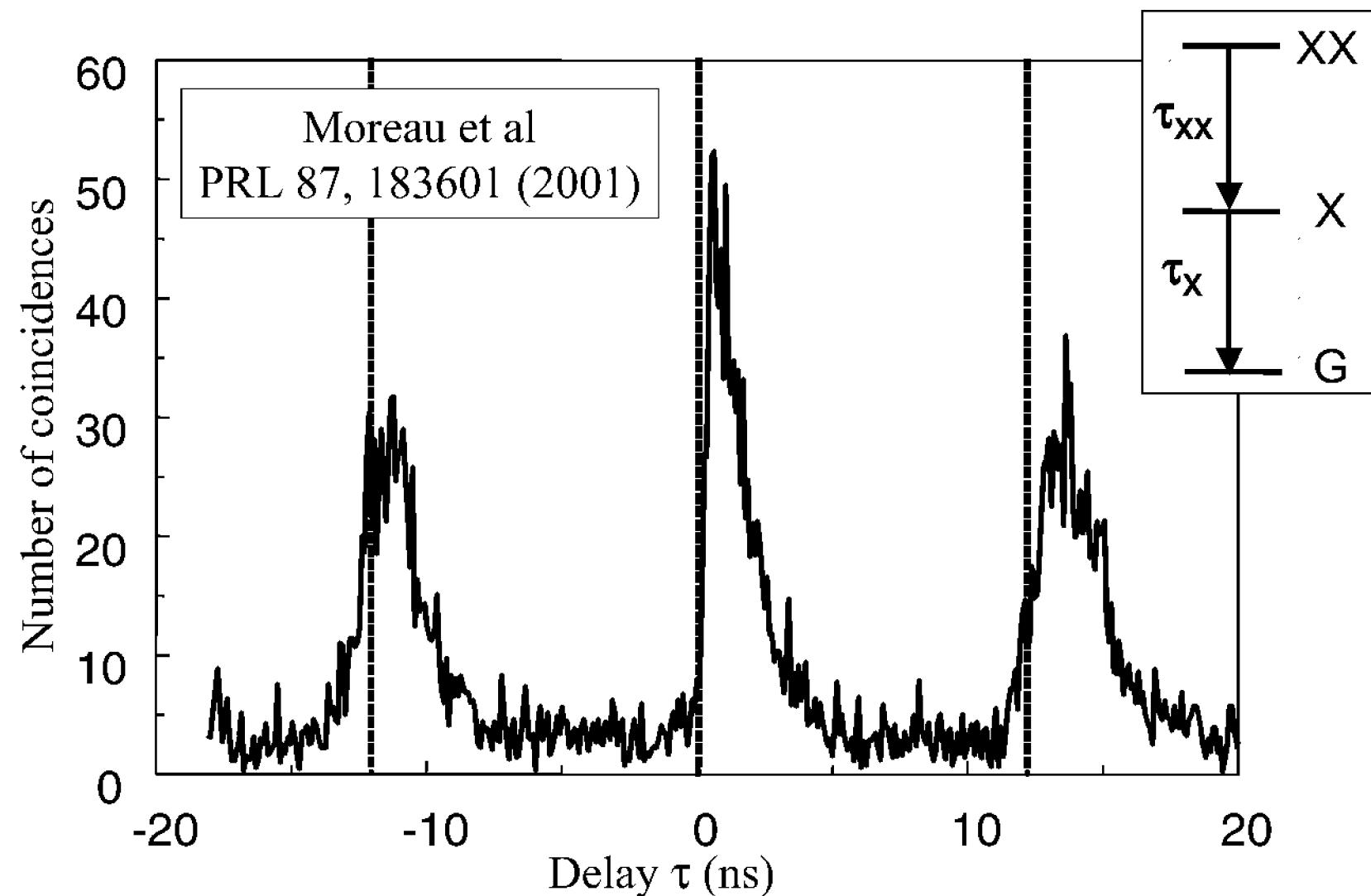
« X » photons are emitted one by one

Protocol works also for electrical pumping (Yuan et al, Science 195, 102, 2002)

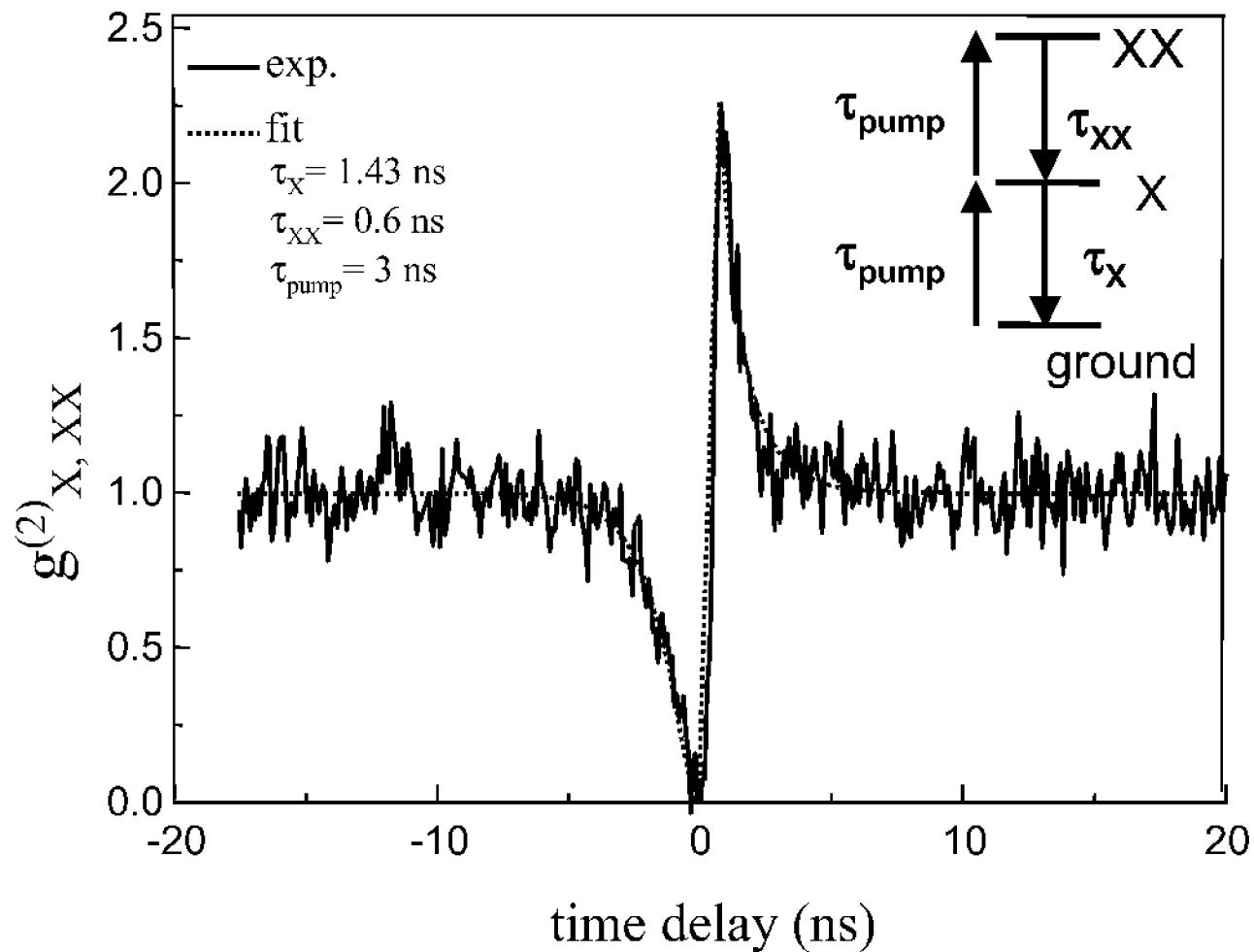
# Photon correlation setup



# Cross-correlations between X and XX photons



# Cross-correlations (cw excitation)



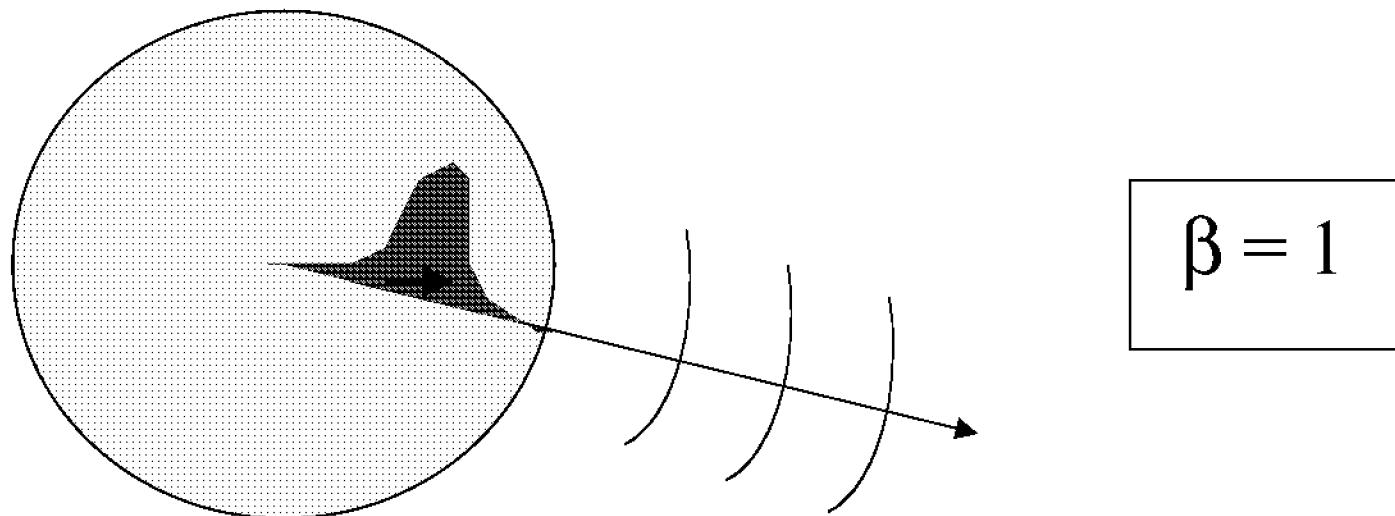
. Both bunching and antibunching

. First observation of a behavior predicted in 1979 !  
(Cohen-Tannoudji et al)

# How to collect/prepare the single photons?

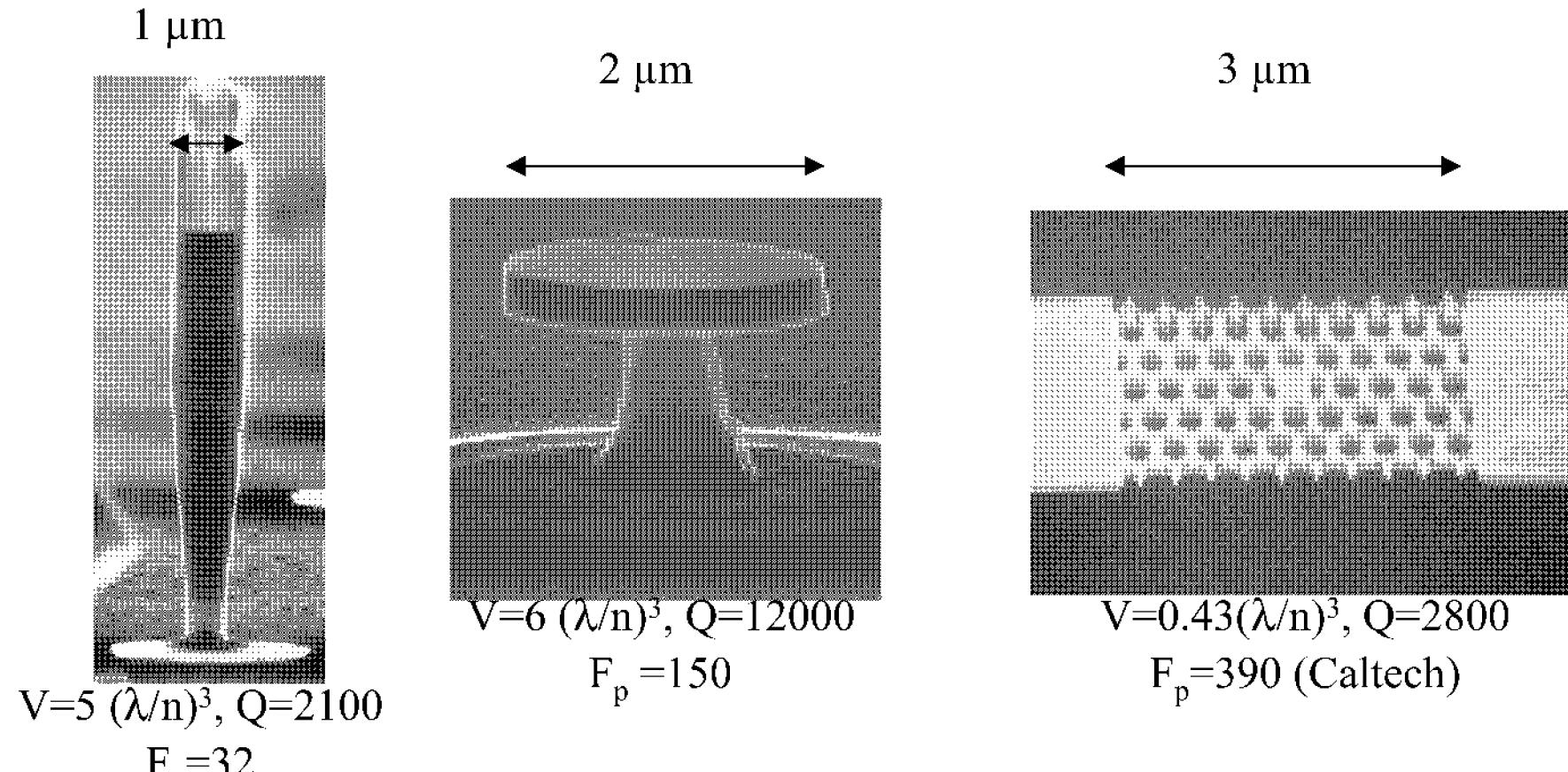
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1) True single-mode cavity = photonic crystal + defect



E. Yablonovitch, PRL, 2238 (1991)

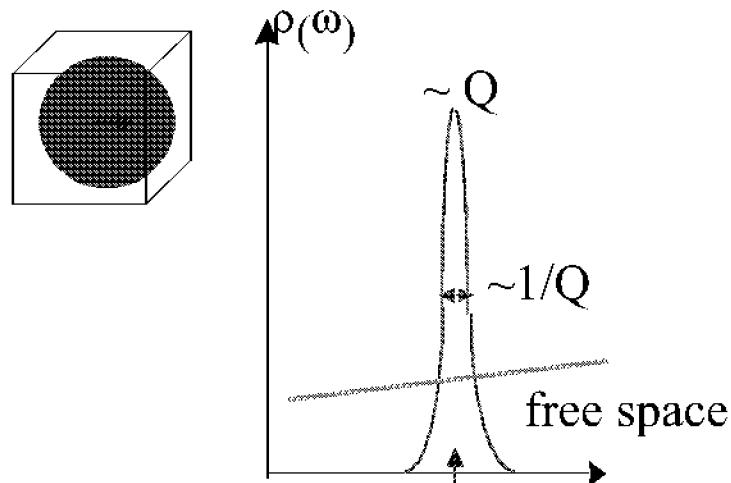
# Some 3D solid-state microcavities



High Q, 3D confined modes  
but not perfect « photonic dots » (leaky modes)!

# The « Purcell effect »

weak coupling  $\rightarrow \frac{1}{\tau} \propto \rho(\omega) \left| \langle i | \vec{d} \cdot \vec{\epsilon} | f \rangle \right|^2$   
regime



$F_p =$  magnitude for an ideal emitter  
. quasi-monochromatic  
. spatial matching  
. spectral matching

Purcell (1946)

$$\frac{T_{free}}{T_{near}} = \frac{3}{4\pi^2} \frac{Q(\lambda/n)^3}{V}$$

$\nwarrow F_p$

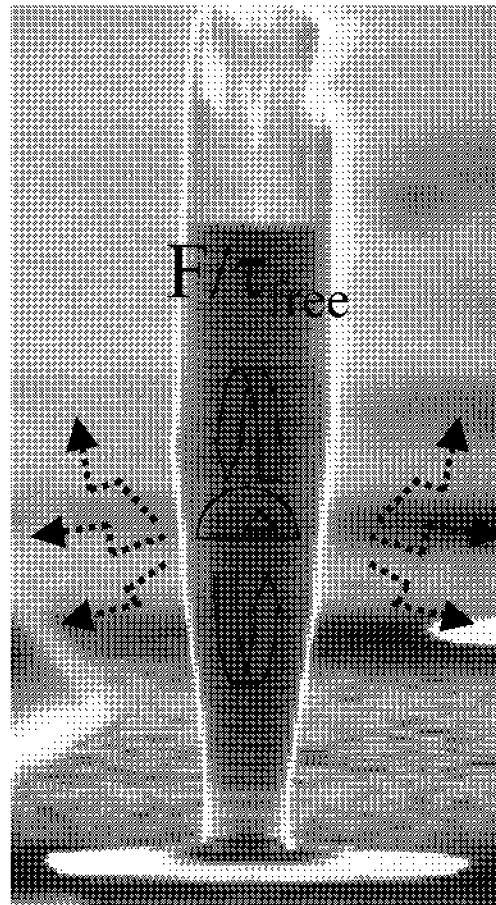
# Purcell effect on InAs QDs

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1997: First observation of the Purcell effect for a solid-state emitter!

QD array in micropillar	x 5	<i>J.M. Gérard et al, PRL 81, 1110 (1998)</i>
QD array in microdisk	x 18	<i>B. Gayral et al, Physica E7, 641(2000)</i>
	x 12	<i>B. Gayral et al, APL 78, 2828 (2001)</i>
single QD in microdisk	x 6	<i>A. Kiraz et al, APL 78, 3932 (2001)</i>
single QD in micropillar	> x 3	<i>E. Moreau et al, APL 79, 2865 (2001)</i> <i>G. Solomon et al, PRL 86, 3903 (2001)</i>

# (Nearly) single-mode spontaneous emission



$\gamma/\tau_{\text{free}}$   
( $\gamma \sim 1$ )

Purcell effect  
=

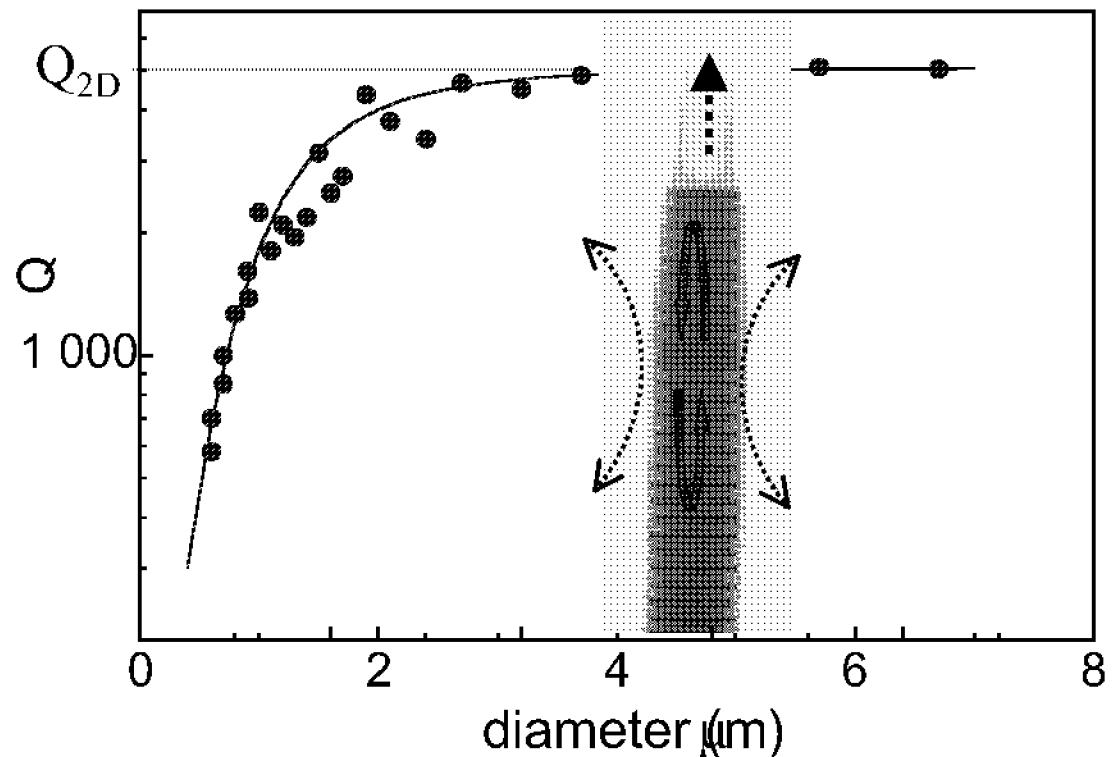
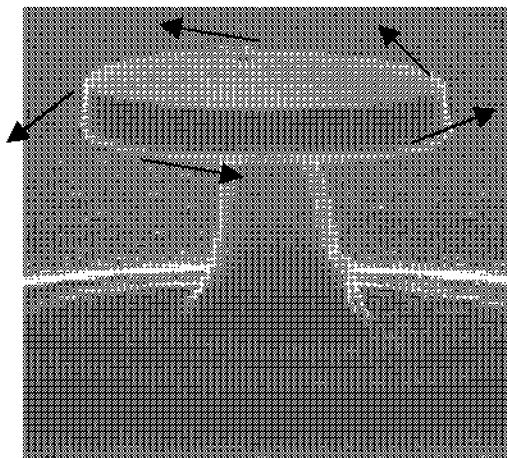
selective enhancement of  
SE into the resonant mode

$$\beta = \frac{F}{F + \gamma} \approx 1$$

*J.M. Gérard et al, PRL 81, 1110 (1998)*

# The photon collection issue

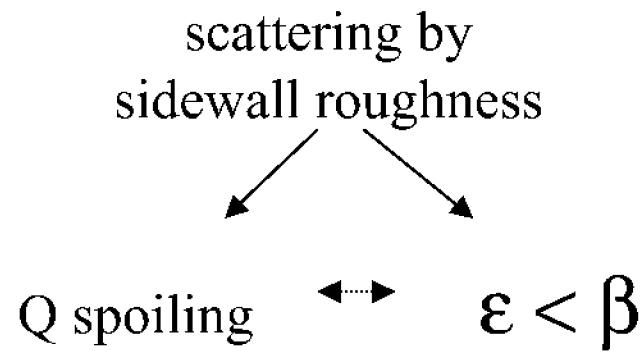
Beware !  
SPS efficiency  $\neq \beta$



scattering by sidewall roughness !

$$\varepsilon < \beta$$

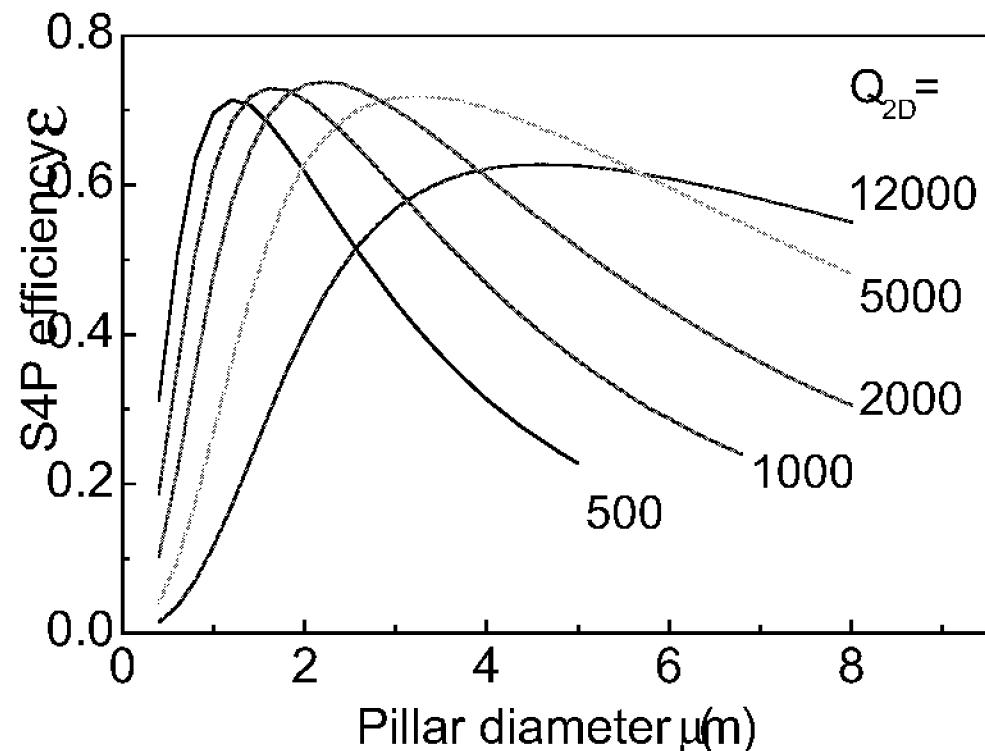
# SPS efficiency for GaAs/AlAs micropillars



$$\frac{1}{Q} = \frac{1}{Q_{2D}} + \frac{1}{Q_{scat}}$$

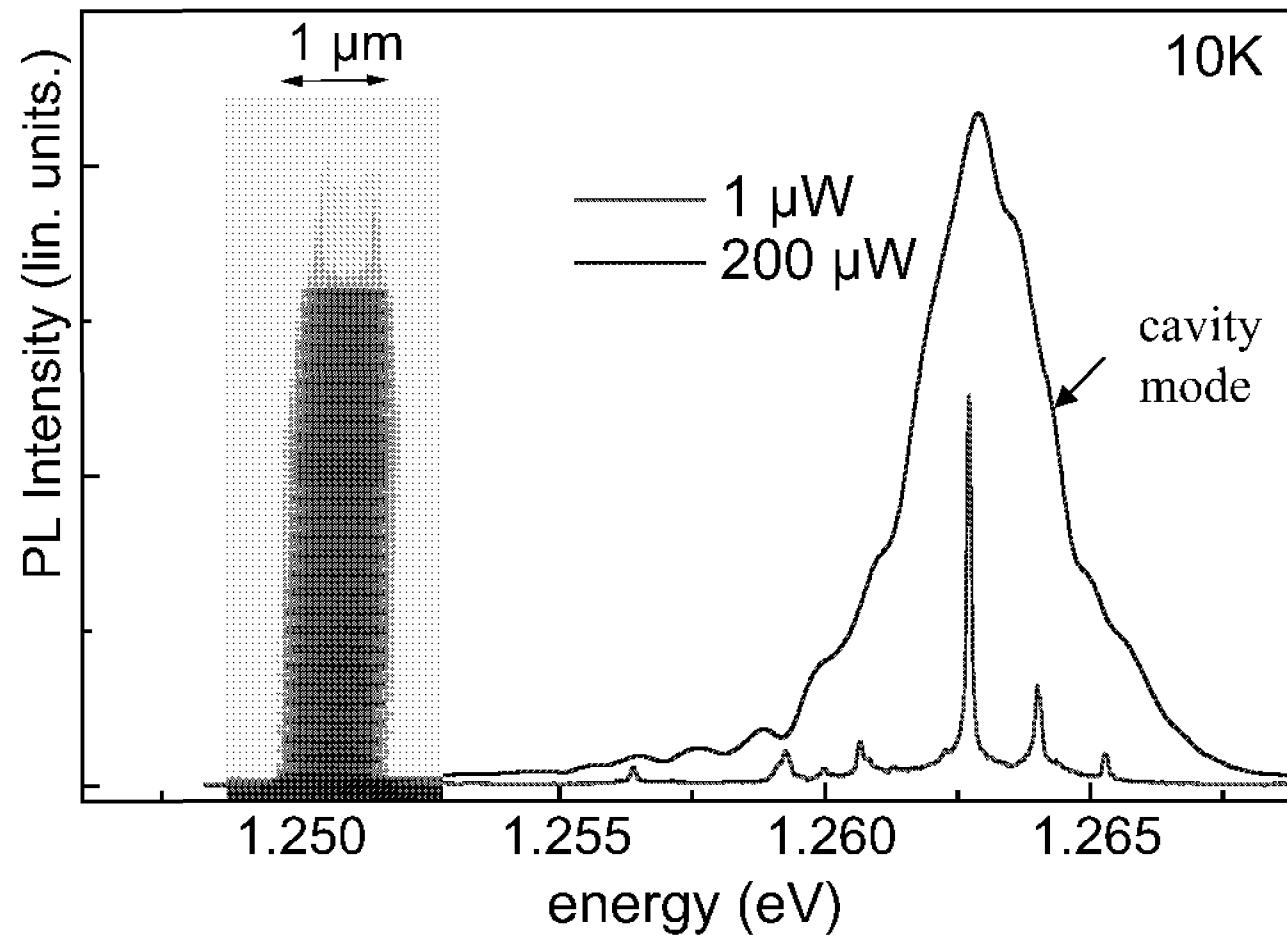


$$\varepsilon = \beta \frac{Q}{Q_{2D}}$$

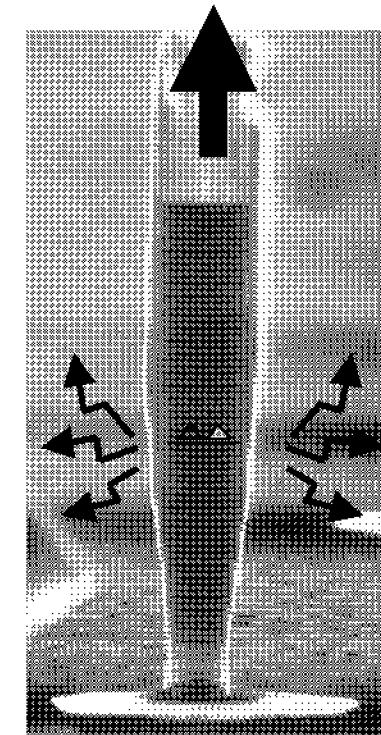
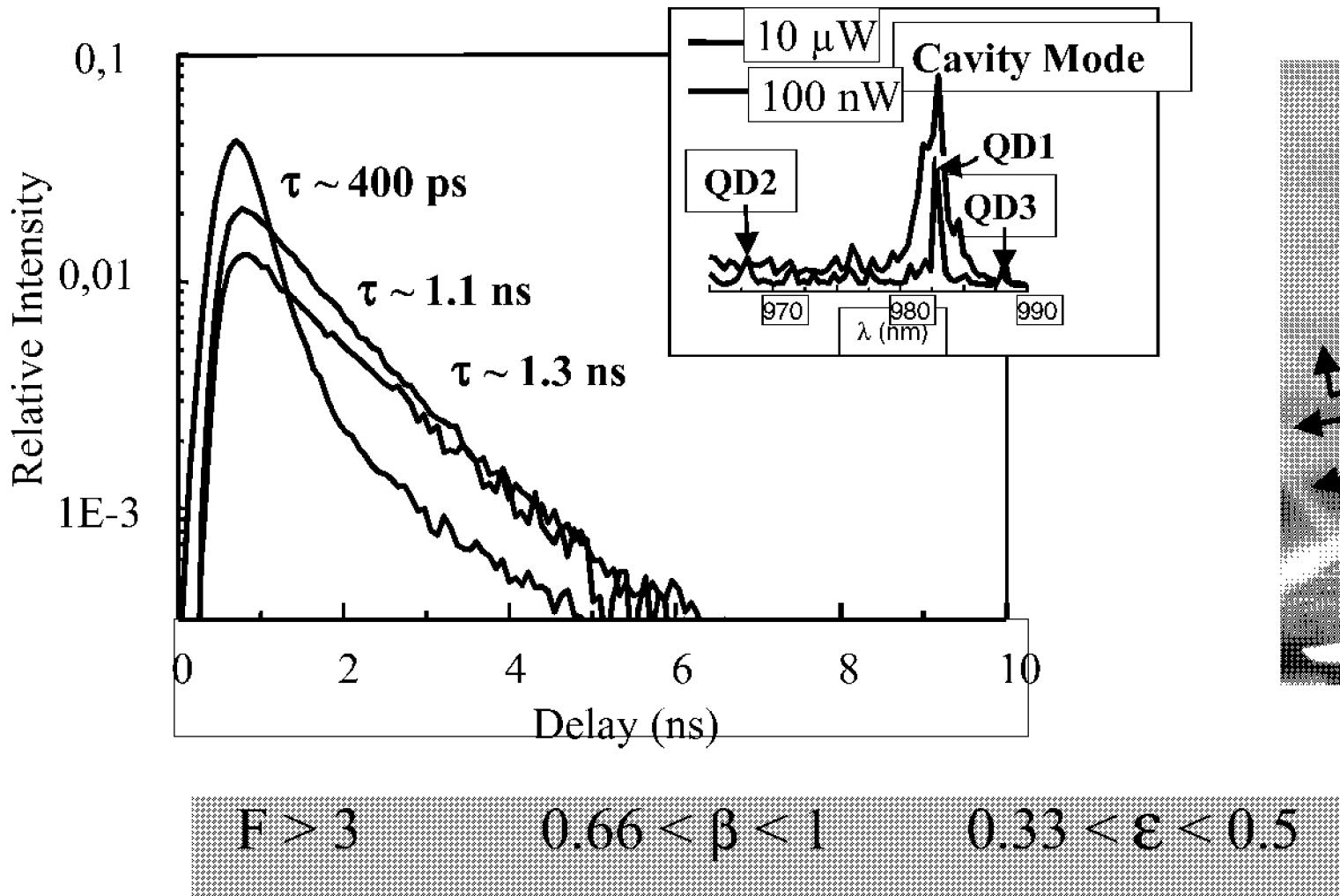


Efficiencies around 70% can be reached for state of the art pillars

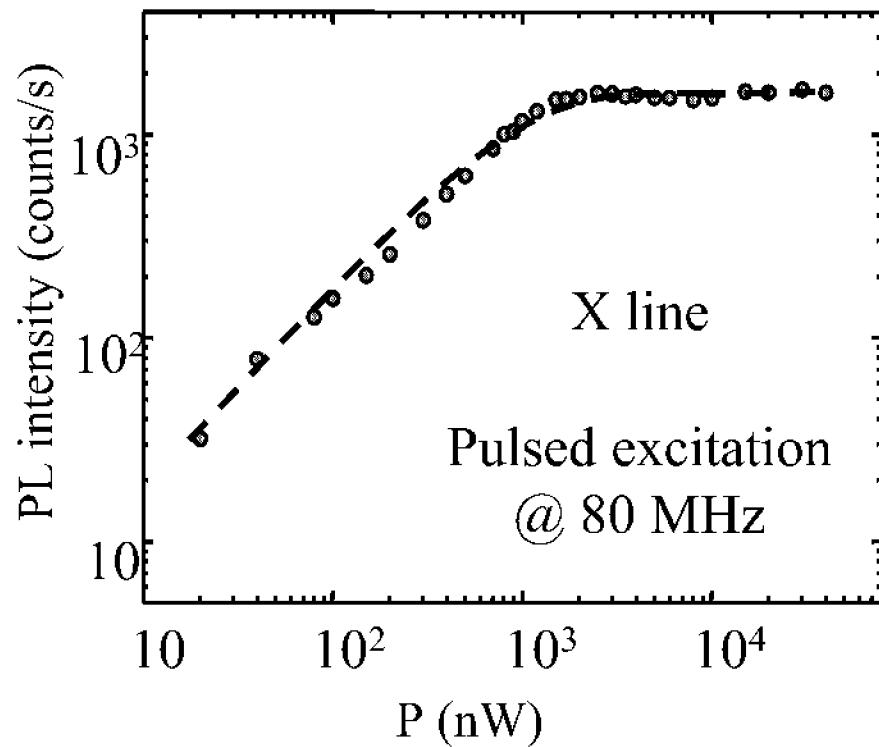
# Few QDs in a micropillar



# Purcell effect on isolated QDs in a micropillar ( $Q_{2D}=1000$ , $Q=500$ , $F_p=7$ )



# Experimental estimate of the SPS efficiency $\mathcal{E}$



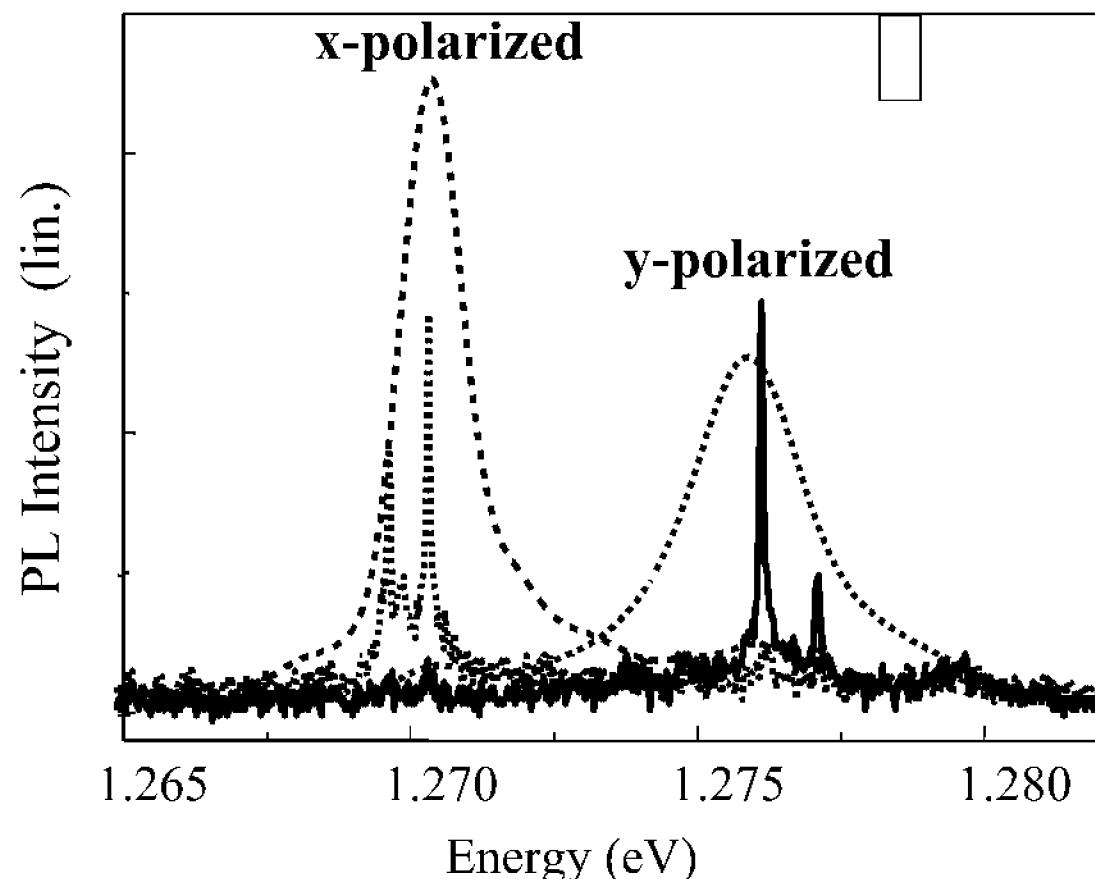
. Saturation of the X line  
=>1 photon emitted per period

. Signal:  
4.8 10<sup>-4</sup> counts per period

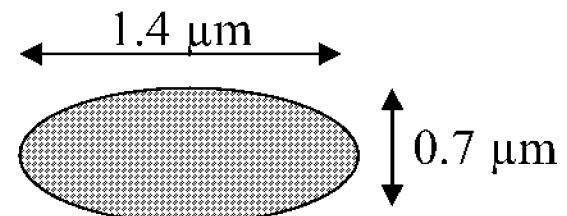
. collection/detection  
efficiency of the set-up  
~ 1.1 10<sup>-3</sup>

$$\mathcal{E} \sim 0.44$$

# Polarization control in single-mode micropillars



Elliptical cross section



Non degenerate fundamental mode  
*Gayral et al, APL 72, 1421, 1998*

~ 90% linear polarisation degree  
of single QD emission  
*Moreau et al, APL 79, 2865, 2001*

# Conclusion

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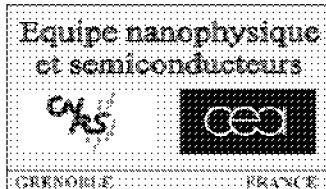
Single QD in a micropillar:

- > first single-mode single-photon source
- > first optoelectronic device based on a CQED effect

Already much better for QKD than attenuated laser diodes

- > efficiency > 40% demonstrated (70% within reach)
- > 5-fold reduction of two-or-more-photons pulses
- => secure transmission length $\uparrow$ , bit rate $\uparrow$

But T<50K,  $\lambda \sim 1 \mu\text{m}$ ...



# Prospects for QD-SPS

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Extension at 1.3  $\mu\text{m}$  (good InAs/GaAs QDs are available)

Electrical pumping of single QDs in VCSEL like structures

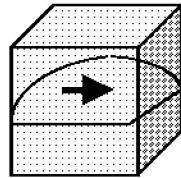
High temperature operation:

- . T~77K achievable for truly single InAs QDs
- . T~ 300K likely for II-VI single QDs with giant X-XX splitting

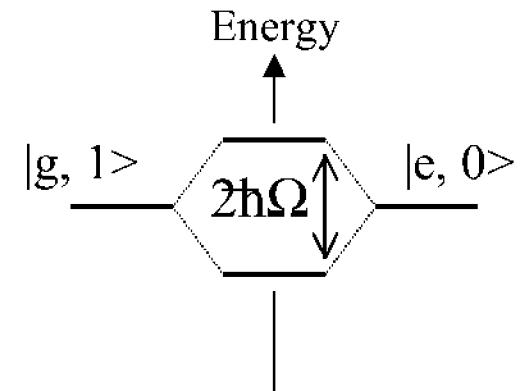
Fourier-transform-limited single photons for quantum computing

- . Requires  $T_2 = T_1/2$  !
- . Control of decoherence processes  $T_2 \uparrow$  (see invited talk by G. Cassabois)
- .  $T_1 \downarrow$  through the Purcell effect

# CQED : strong coupling for single QDs?



|ground, 1 photon>  
↓  $\Omega_{\text{rabi}}$   
|excited, 0 photon>



InAs QD in  
solid-state cavity :

$$\hbar\Omega = |\vec{d} \cdot \vec{\epsilon}_{\max}|$$

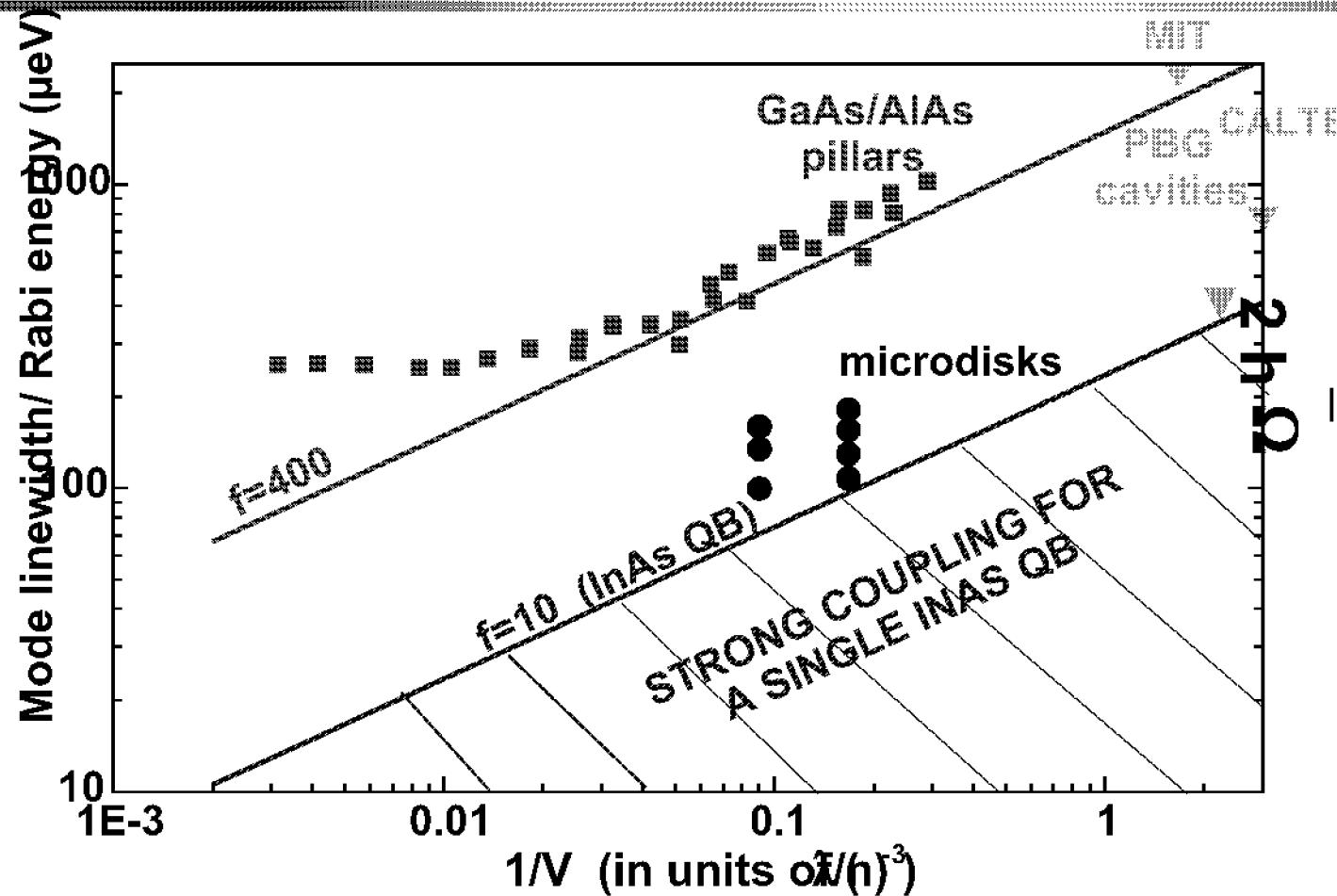
large dipole (0.6 e.nm)

huge vacuum field ( $10^5$  V/cm)

vacuum Rabi splitting observable  $\Leftrightarrow 2\hbar\Omega > \Delta E_{\text{emitter}} + \Delta E_{\text{cavity}}$

# Strong coupling for single QDs ?

Gérard et al, Physica E9, 131 (2001)  
Andreani et al, PRB 60, 13276 (1999)



Microdisks are the best candidates for InAs QDs

Interest of QD with larger oscillator strength (QW interface fluctuations)