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**XII WORKSHOP ON  
STRONGLY CORRELATED ELECTRON SYSTEMS**

**17 - 28 July 2000**

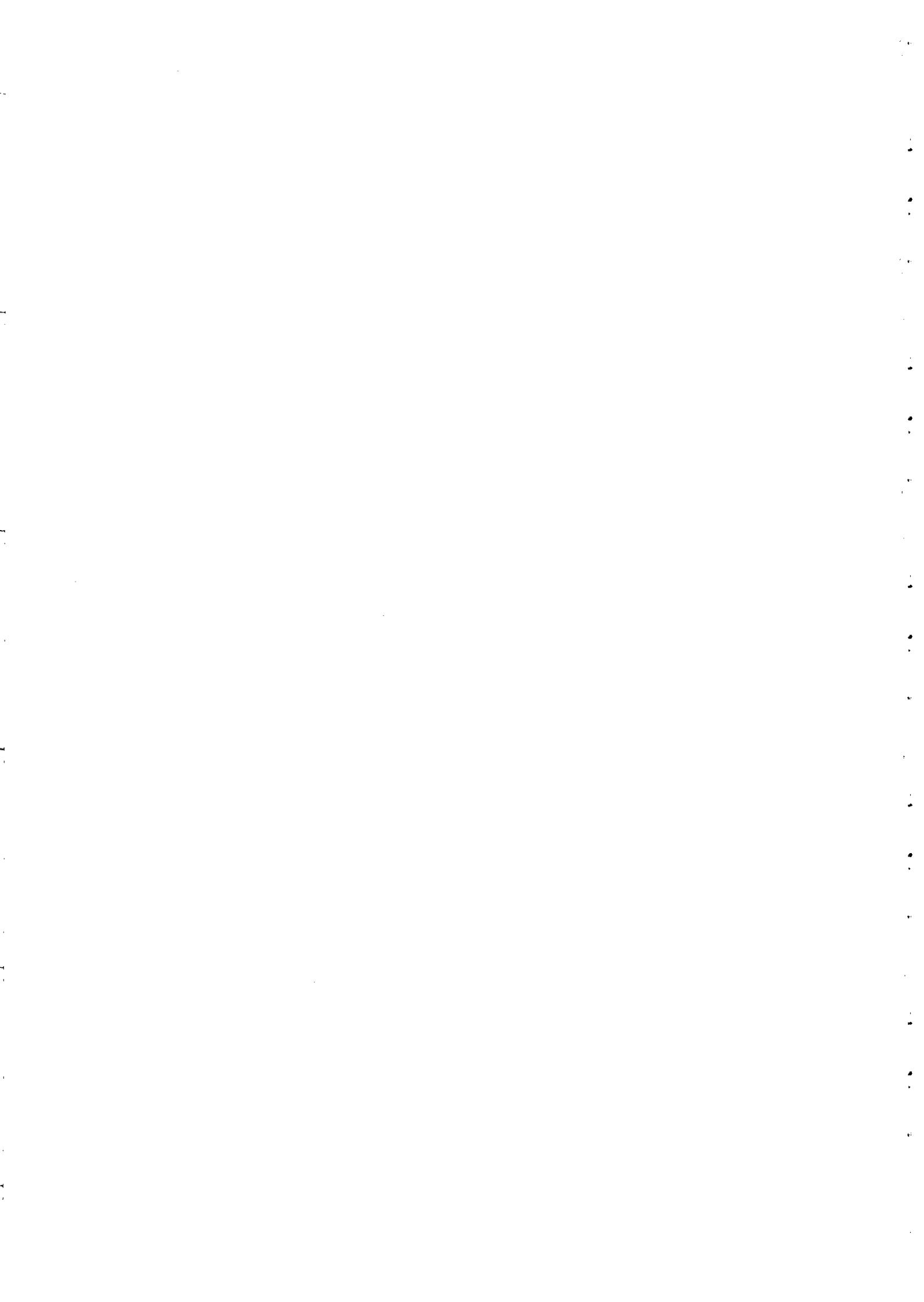
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**UNCONVENTIONAL METALS AND  
SUPERCONDUCTORS IN THE LAYERED RUTHENATES**

**Andy MACKENZIE**  
School of Physics & Astronomy  
University of Birmingham  
U.K.

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*These are preliminary lecture notes, intended only for distribution to participants.*



# Unconventional Metals and Superconductors in the Layered Ruthenates

Talk by Andy Mackenzie

*School of Physics and Astronomy, University of  
Birmingham, UK*

## Collaborators

Robin Perry, Louise Galvin, Lucia Capogna,  
Santiago Grigera, Matthias Hein, Rod  
Ormeno, Andy Sibley, Colin Gough and Ted  
Forgan.

Christoph Bergemann, Dominic Forsythe,  
Fumihiko Nakamura, May Chiao and  
Stephen Julian.

Satoru Nakatsuji, Shuji NishiZaki and Yoshi  
Maeno.

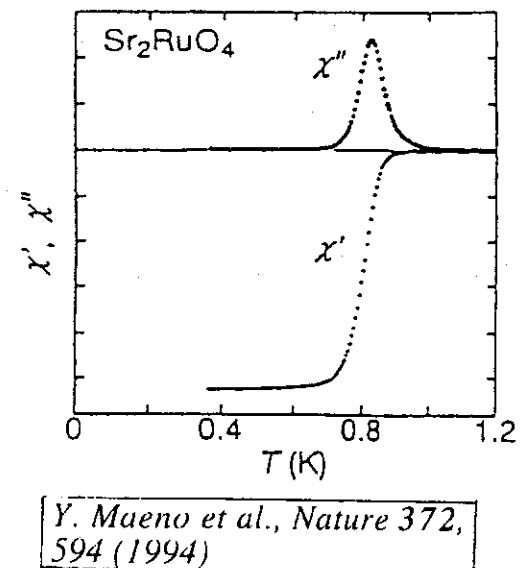
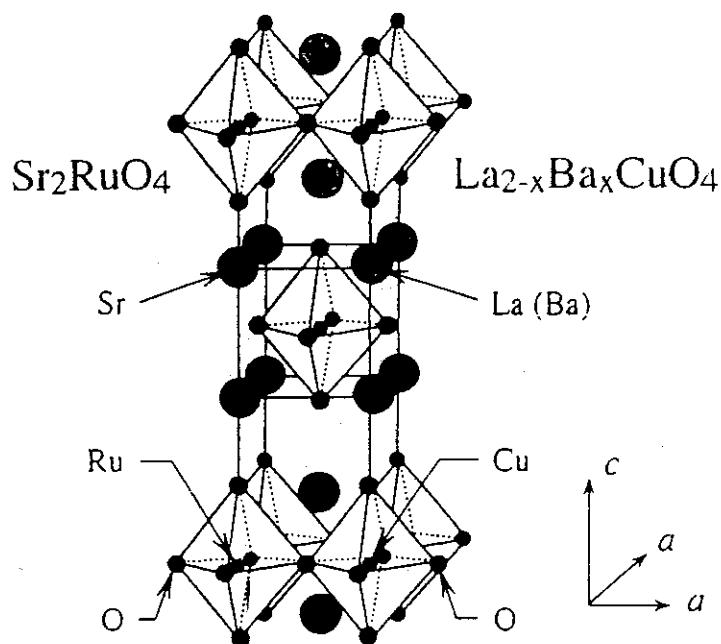
Shin-ichi Ikeda.

Christian Pfleiderer.

## Contents

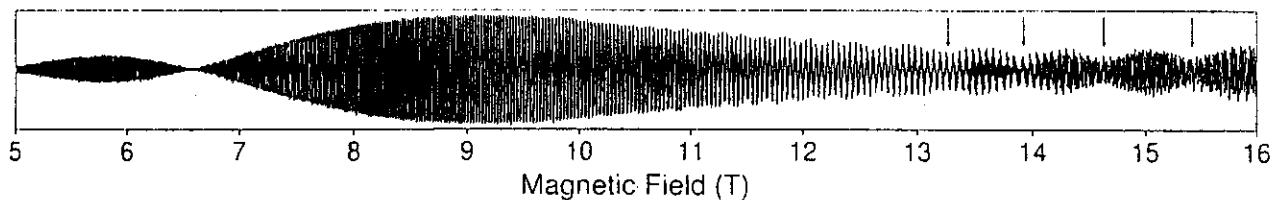
1. Introduction – electronic structure of  $\text{Sr}_2\text{RuO}_4$  and suggestion of triplet superconductivity.
2. Evidence that the superconducting state is not isotropically gapped.
3. Evidence in favour of triplet pairing and time reversal symmetry breaking.
4. Comparison with  $\text{Sr}_3\text{Ru}_2\text{O}_7$ .
5. Summary and conclusions.

## The oxide superconductor $\text{Sr}_2\text{RuO}_4$



Isostructural to  $\text{La}_2\text{CuO}_4$  but a metal in the absence of chemical doping. It is possible to prepare samples of very high purity.

## Quantum oscillations in the magnetisation: the 'dHvA' effect.



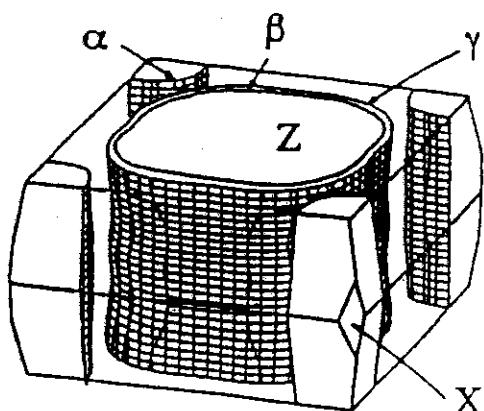
Careful analysis of the temperature, field and angular dependence of the oscillations can be used to obtain a detailed understanding of the Fermi surface topography and low energy excitations.

[A.P. Mackenzie, S.R. Julian, A.J. Diver, G.J. McMullan, M.P. Ray, G.G. Lonzarich, Y. Maeno, S. NishiZaki and T. Fujita, Phys. Rev. Lett. 76, 3786 (1996)].

Resolution in  $\mathbf{k}$  of 1 part in  $10^5$  of the Brillouin zone just demonstrated.

[C. Bergemann, S.R. Julian, A.P. Mackenzie, S. NishiZaki and Y. Maeno, Phys. Rev. Lett. 84, 2662 (2000)].

## The low temperature metallic state of Sr<sub>2</sub>RuO<sub>4</sub>



Very simple electronic structure - nearly two-dimensional, with three Fermi surface sheets.

Fermi liquid,  $m^*$  up to  $15 m_e$ ,  $\langle m^*/m_{\text{band}} \rangle \sim 4$ , accounting fully for electronic specific heat.

Quantitative link with  ${}^3\text{He}$ , a known 'p-wave' superfluid.

Could Sr<sub>2</sub>RuO<sub>4</sub> be a p-wave superconductor?

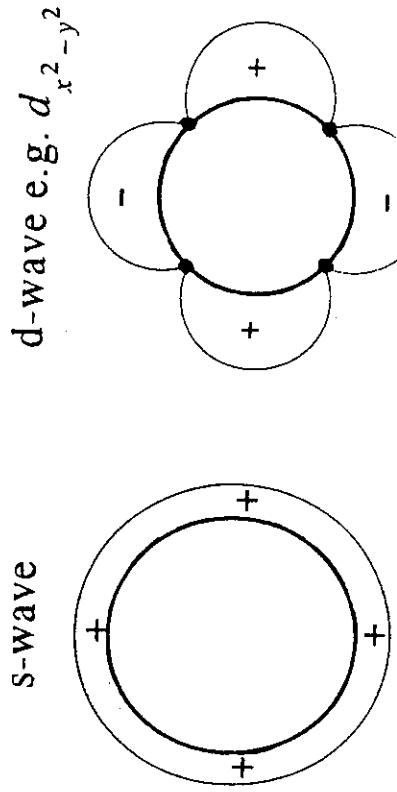
[T.M. Rice and M. Sigrist, *J. Phys.: Cond. Matt.* 7, L643 (1995)  
G. Baskaran, *Physica B* 223 & 224, 490 (1996)]

### Nomenclature of superconducting states

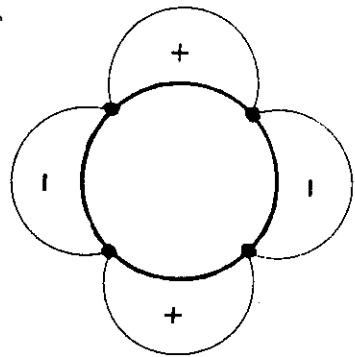
<i>Pair orbital angular momentum, L</i>	<i>Name</i>	<i>Parity of spatial part</i>	<i>Spin state</i>
0	s-wave	even	singlet
1	p-wave	odd	triplet
2	d-wave	even	singlet
.	.	.	.

*For an elementary discussion see J.F. Annett, *Contemp. Phys.* 36, 423 (1995).*

## Singlet superconductors



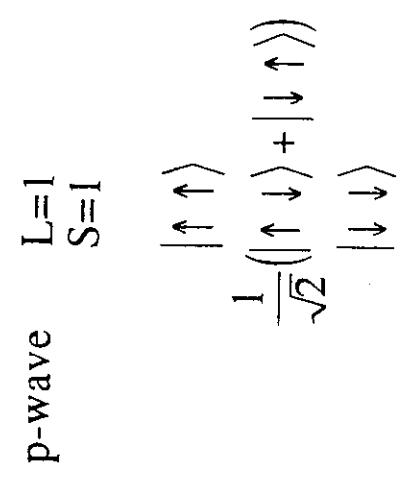
d-wave e.g.  $d_{x^2-y^2}$



$L=0$   
 $S=0$

$$\frac{1}{\sqrt{2}}(|\uparrow \downarrow\rangle - |\downarrow \uparrow\rangle) - \frac{1}{\sqrt{2}}(|\uparrow \downarrow\rangle - |\downarrow \uparrow\rangle)$$

## Triplet superconductors



$$\frac{1}{\sqrt{2}}(|\uparrow \downarrow\rangle + |\downarrow \uparrow\rangle)$$

Order parameter is a three dimensional complex vector  $\mathbf{d}(\mathbf{k})$ , usually 'pinned' in a crystal.

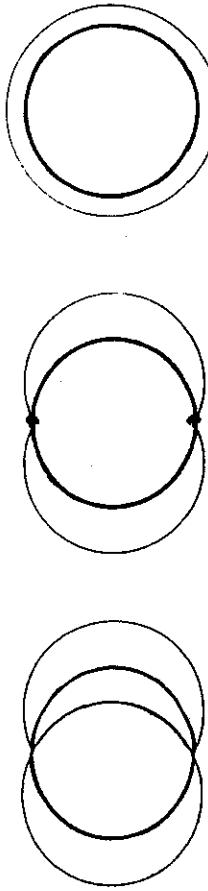
*R. Balian & N.R. Werthamer, Phys. Rev. **131**, 1553 (1963)  
A.J. Leggett, Rev. Mod. Phys. **47**, 331 (1975)*

Cannot suppress  $T_c$  to zero by elastic scattering

$T_c \rightarrow 0$  with strong scattering. Other signatures in thermodynamics, Josephson effects etc.

$$\underline{\Delta = \Delta_o(\mathbf{k})e^{i\phi(\mathbf{k})}}$$

Wide variety of allowed states:



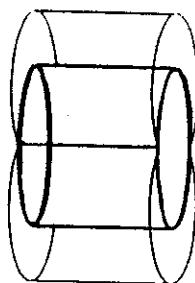
## Some allowed triplet states for Sr<sub>2</sub>RuO<sub>4</sub>:

$d(\mathbf{k})$

Gap structure  
Time reversal  
symmetry?

$$\begin{bmatrix} 0 \\ 0 \\ k_x \end{bmatrix}$$

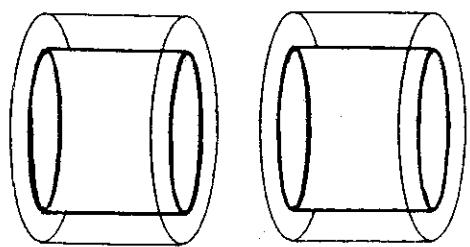
$$\begin{bmatrix} 0 \\ 0 \\ k_x + k_y \end{bmatrix}$$



YES

$$\begin{bmatrix} 0 \\ 0 \\ k_x + ik_y \end{bmatrix}$$

NO

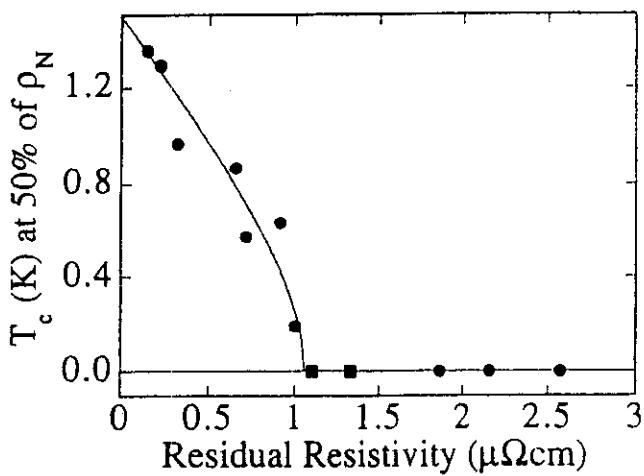


YES

YES

-

## Extremely strong impurity effect in Sr<sub>2</sub>RuO<sub>4</sub>.



$\ell > 900\text{\AA}$  for the observation of superconductivity.

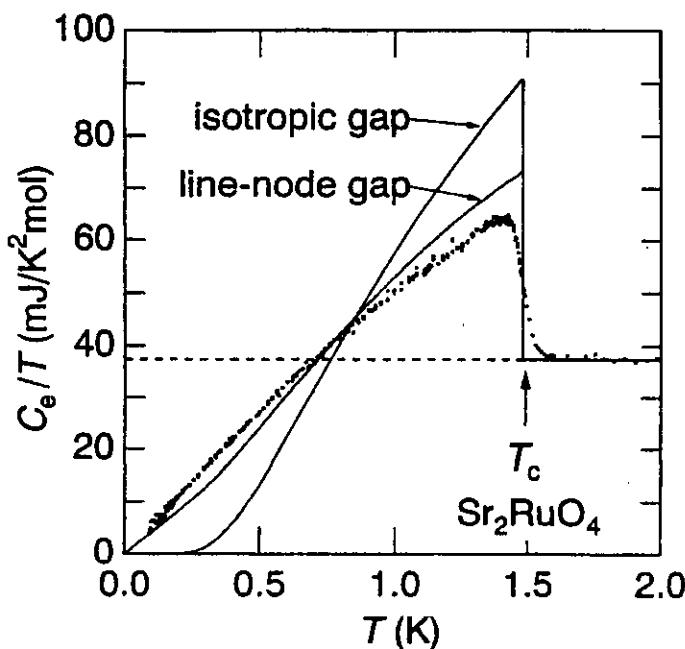
Consistent with known value of  $\xi$ .

Maximum  $T_c \sim 1.5\text{K}$  in high purity limit.

## Strong evidence for non-s-wave superconductivity.

A.P. Mackenzie et al., Phys. Rev. Lett 80, 161 (1998)

## Linear temperature dependence of specific heat below $T_c$ .

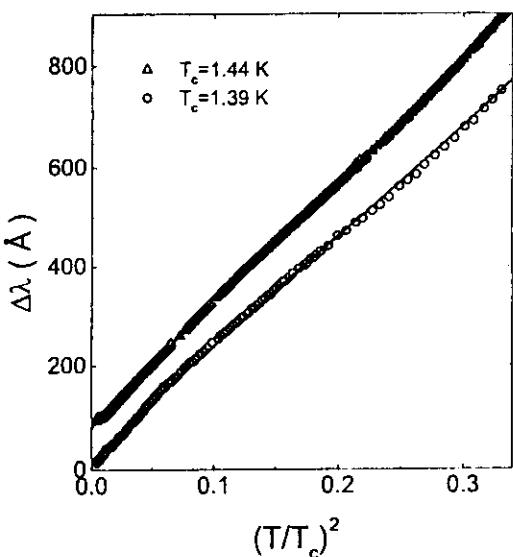


S. NishiZaki, Y. Maeno and Z.Q. Mao,  
J. Low Temp. Phys. 117, 1581 (1999);  
J. Phys. Soc. Jpn. 69, 572 (2000).

Consistent with  $T^3$  variation of  $1/T_1$  in Ru NQR study.  
H. Mukuda, K. Ishida, K. Kitaoka et al., preprint.

POWER LAWS ALSO IN ULTRASOUND, THERMAL COND.

## High frequency measurements of penetration depth show power law behaviour



$T^2$  in pure samples,  $T^3$  in disordered samples at 28 MHz

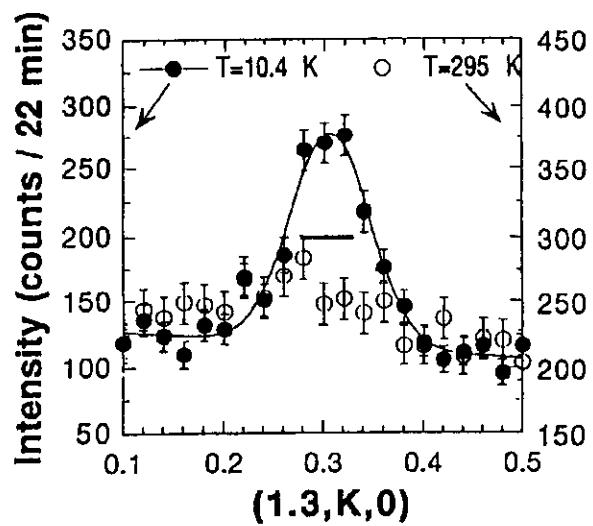
I. Bonalde, B.D. Yanoff, M.B. Salomon, D.J. van Harlingen, E.M.E. Chia, Z.Q. Mao and Y. Maeno, preprint.

$T^2$  in pure samples with interesting  $\omega\tau \sim 1$  behaviour at ~ 10 GHz

R.J. Ormeno, M. Hein, A. Sibley, C.E. Gough and Y. Maeno, preprint.

See also theory for chiral superconductor by T. Morinari and M. Sigrist, preprint

$\chi(q)$  is not as simple as intuitive expectation:



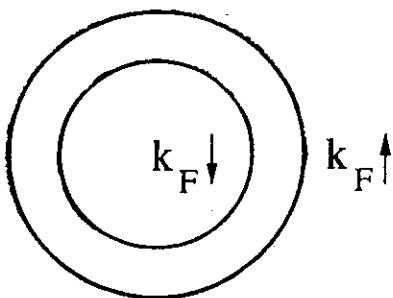
*[Y. Sidis, M. Braden, P. Bourges,  
B. Hennion, S. NishiZaki, Y.  
Maeno and Y. Mori, Phys. Rev.  
Lett. 83, 3320 (1999).]*

*[I.I. Mazin and D.J. Singh, Phys.  
Rev. Lett. 82, 4324 (1999).]*

Tempting to postulate d-wave superconductivity..

However .....

## Spin susceptibility as a probe for triplet pairing.



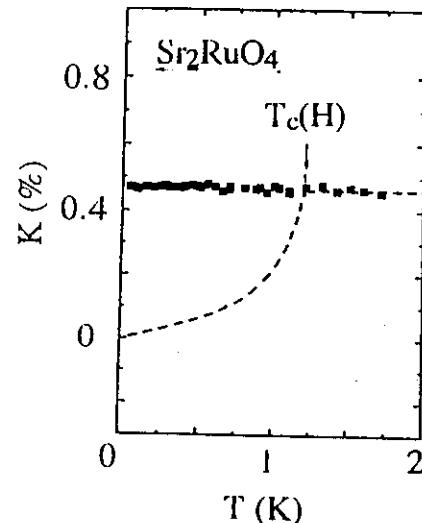
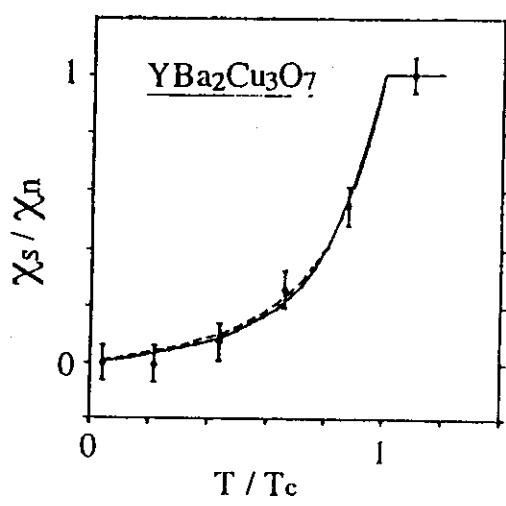
Energy gain for polarisation opposes condensation energy for singlet superconductivity on an unpolarised Fermi surface.

For low applied field, the singlet pairing wins:  
 $\chi_s / \chi_n \rightarrow 0$  as  $T \rightarrow 0$ .

For triplet pairing this is not the case.

Problem: measuring the spin susceptibility in the presence of Meissner diamagnetism.

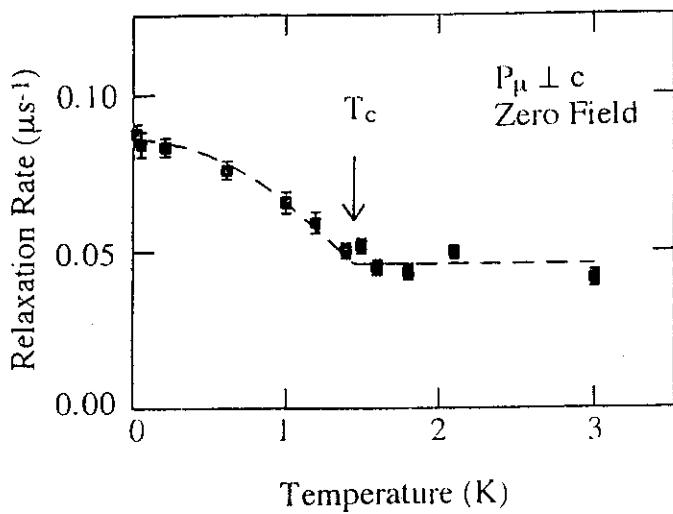
## Spin susceptibility in superconductors by NMR.



[S.E. Barrett, D.J. Durand,  
C.H. Pennington, C.P. Slichter,  
T.A. Friedmann, J.P. Rice and  
D.M. Ginsberg, Phys. Rev. B 41,  
6283 (1990)]

[K. Ishida, H. Mukuda, Y. Kitaoka, K.  
Asayama, Z.Q. Mao, Y. Mori and Y. Maeno,  
Nature 396, 658 (1998)]

## Evidence for breaking of time reversal symmetry at $T_c$ .



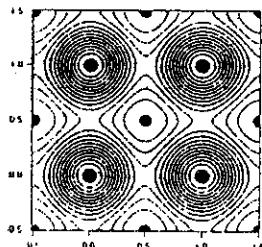
Muon spin rotation gives evidence for a spontaneous magnetic moment at  $T_c$ .

Superconducting state breaks time reversal symmetry.

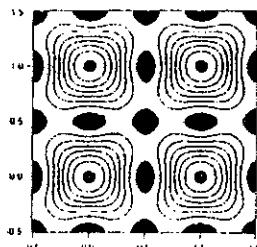
Implication:  $d + id$  or  $\hat{z}(k_x + ik_y)$ , BUT two  $d$  states not expected to be degenerate in a tetragonal system.

# Support for time reversal symmetry breaking from small angle neutron scattering (SANS).

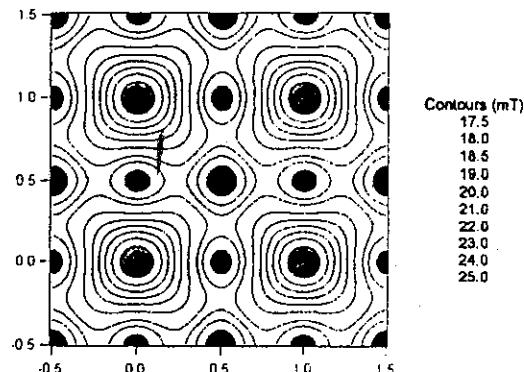
Single component  
Ginzburg-Landau



Two component  
Ginzburg-Landau

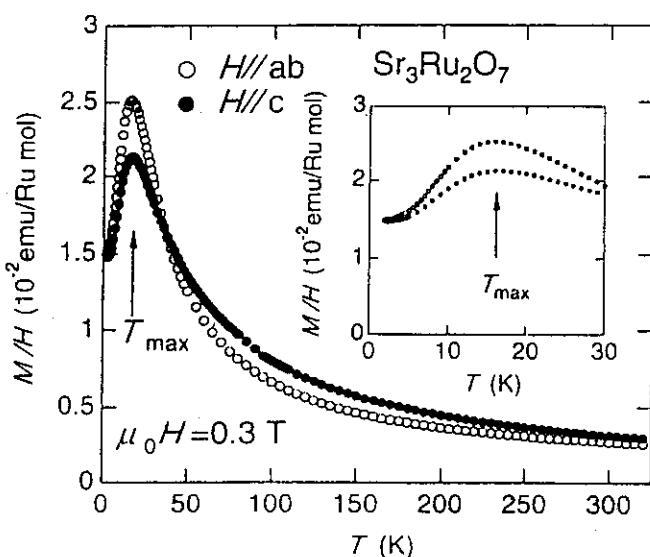


Experimental



P.G. Kealey, T.M. Riseman, E.M. Forgan, L.M. Galvin, A.P. Mackenzie, S.L. Lee, D. M'K. Paul, R. Cubitt, D.F. Agterberg, R. Heeb, Z.Q. Mao and Y. Maeno,  
*Phys. Rev. Lett.* **84**, 6094 (2000)

## Magnetic susceptibility of $\text{Sr}_3\text{Ru}_2\text{O}_7$

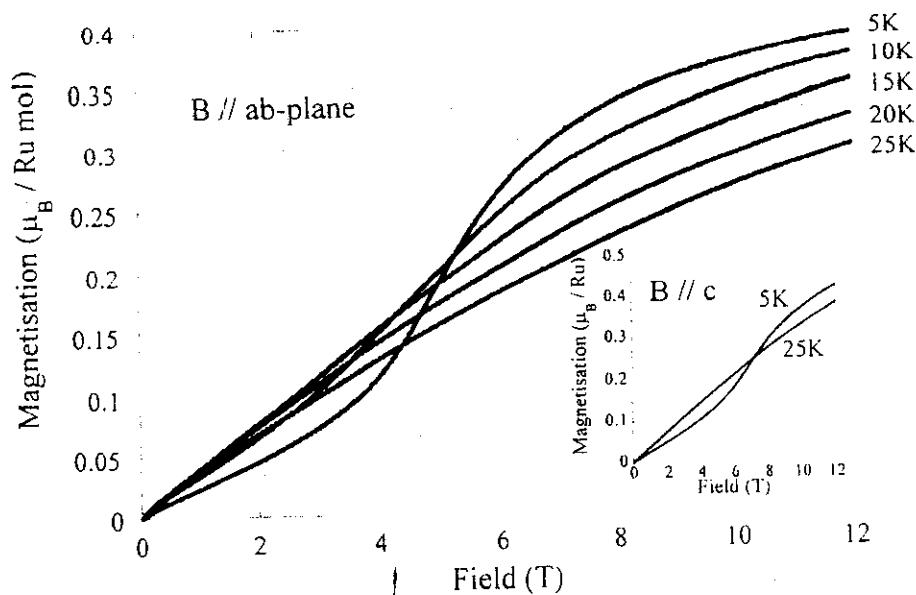


Large susceptibility enhancement in  $\text{Sr}_3\text{Ru}_2\text{O}_7$ .  $\chi$  is over an order of magnitude bigger than  $\text{Sr}_2\text{RuO}_4$ . Cleanest crystals are *paramagnetic*,

Specific heat shows broad feature near maximum in  $\chi$ , and a large  $\gamma$  of up to  $100 \text{ mJ/mol-RuK}^2$ .

S. Ikeda et al., *cond-mat '99* & to appear in *Phys. Rev. B*

## Metamagnetism of $\text{Sr}_3\text{Ru}_2\text{O}_7$

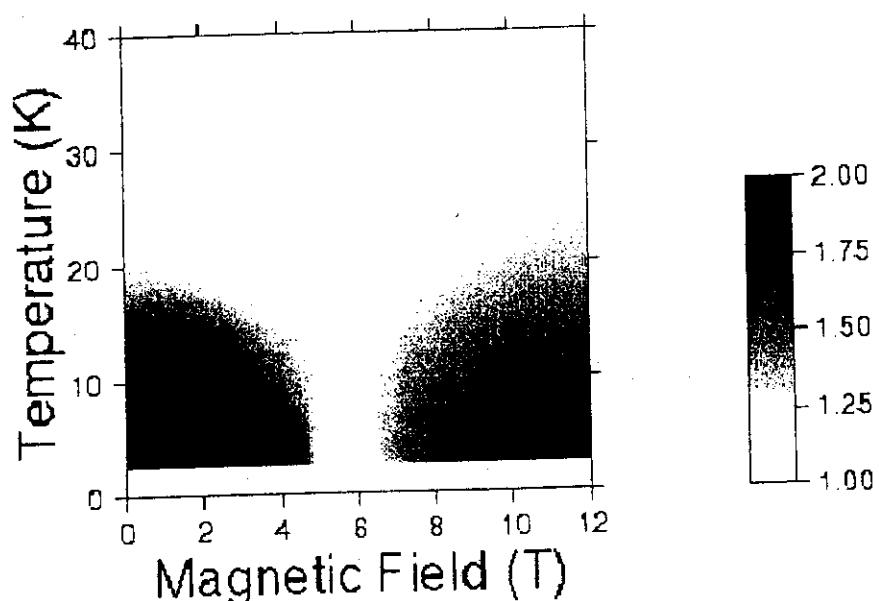


Metamagnetism seen below 10K.

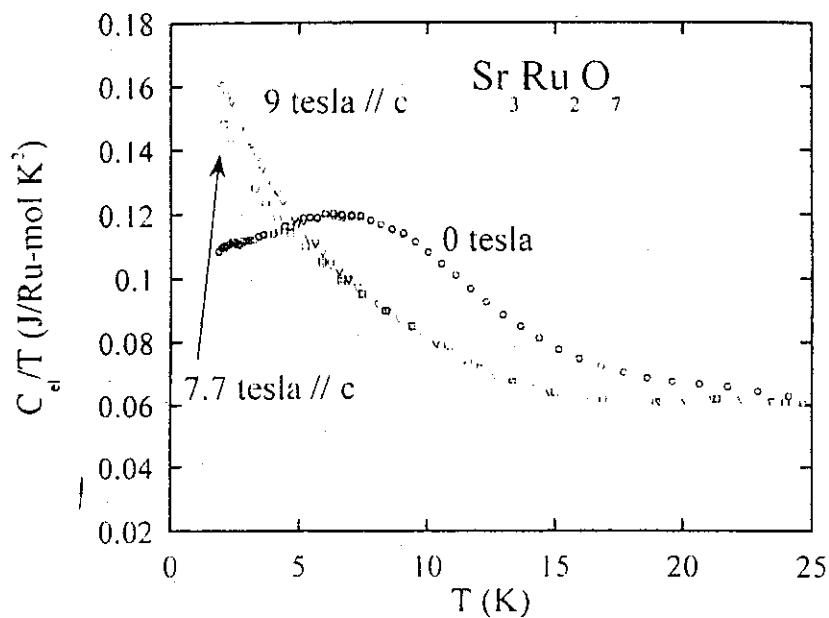
Isotropic for in-plane fields, and only a mild anisotropy for  $B // c$ .

These vibrating sample magnetometer measurements have low T limit of 5K.

Empirical phase diagram for  $\text{Sr}_3\text{Ru}_2\text{O}_7$  based on measurement of resistivity with  $B // ab$



# Diverging specific heat $\gamma$ at the metamagnetic field in $\text{Sr}_3\text{Ru}_2\text{O}_7$



R.S. Perry, L.M. Galvin, S. Grigera, L. Capogna, A.J. Schofield, A.P. Mackenzie, M. Chiao, S.R. Julian, S. Ikeda, S. Nakatsuji, Y. Maeno and C. Pfleiderer, cond-mat '00

## Summary and conclusions

Measurements sensitive to the density of states below  $T_c$  give good evidence that it is not isotropically gapped.

However, there is also good evidence that the superconducting state is spin triplet, and breaks time reversal symmetry at  $T_c$ .

Possibilities for understanding these results are

- a) P-wave superconductivity with  $\mathbf{d} = \hat{z}(k_x + ik_y)$  and a pairing interaction that has a strong dependence on Fermi surface sheet and  $\mathbf{k}$ .
- b) More exotic triplet states.