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SMR.1317 - 19

## *SUMMER SCHOOL ON PARTICLE PHYSICS*

*18 June - 6 July 2001*

### NEUTRINO PHYSICS

#### Lecture III

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Please note: These are preliminary notes intended for internal distribution only.



# Lecture III

# $2\nu$ phenomenology of:

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- Atmospheric  $\nu$

evidence for  $P(\nu_\mu \rightarrow \nu_\mu) < 1$   
 $\rightarrow \nu_\mu$  flavor disappearance

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- Solar  $\nu$

evidence for  $P(\nu_e \rightarrow \nu_e) < 1$   
 $\rightarrow \nu_e$  flavor disappearance

---

- CHOOZ reactor  $\nu$

NO evidence for  $P(\nu_e \rightarrow \nu_e) \neq 1$   
 $\rightarrow$  important constraints

---

- LSND accel.  $\nu$

Controversial evidence for  $P(\nu_\mu \rightarrow \nu_e) > 0$   
(appearance of flavor)

# PHENOMENOLOGY:

COMPARISON OF MODELS WITH DATA  
IS NOT STRAIGHTFORWARD

---

$$\text{MODELS} \equiv P(\nu_\alpha \rightarrow \nu_\beta)$$

$$\text{OBSERVABLES} \equiv \text{lepton rates } R_{\alpha,\beta}$$

$$R_\beta \sim \sum_\alpha \int \phi_\alpha \otimes P_{\alpha\beta} \otimes \sigma_\beta \otimes \epsilon_\beta \pm \delta_\beta$$

↑                      ↑                      ↑                      ↑                      ↑                      ↑  
 lepton.              ν flux              transit.              cross              detector.              uncertainties  
 rate.                probabil.            probab.            sect.            effic.            (theor + expt)  
 ↑                      ↑                      ↑                      ↑                      ↑  
 what                   what                   what  
 we see                we test             we test

---

Constraints on  $P_{\alpha\beta}$  are obtained by comparison of  $R_\beta^{\text{exp}}$  with  $R_\beta^{\text{theo}}$ , typically through a  $\chi^2$  statistics

$$\chi^2 = \sum_{\text{observables}} \frac{(\text{THEORY} - \text{EXPT.})^2}{\text{ERROR}^2} \quad (\text{symbolically})$$

## TWO USES OF $\chi^2$ : (Particle Data Group)

### GOODNESS-OF-FIT

Compare  $\chi^2$  (for a given model) with

$$N_{\text{dof}} = N(\text{DATA}) - N(\text{MODEL FREE PARAMETERS})$$

If  $\chi^2/N_{\text{dof}} \sim 1 \rightarrow \text{MODEL OK}$

### PARAMETER ESTIMATE

If previous model passes goodness-of-fit test, then take best-fit model parameters (minimizing  $\chi^2$ ) as "true" values, and attach them errors by appropriate iso- $\Delta\chi^2$  levels ( $\Delta\chi^2 = \chi^2 - \chi^2_{\text{min}}$ ) for

$$N_{\text{dof}} = N(\text{MODEL FREE PARAMETERS})$$

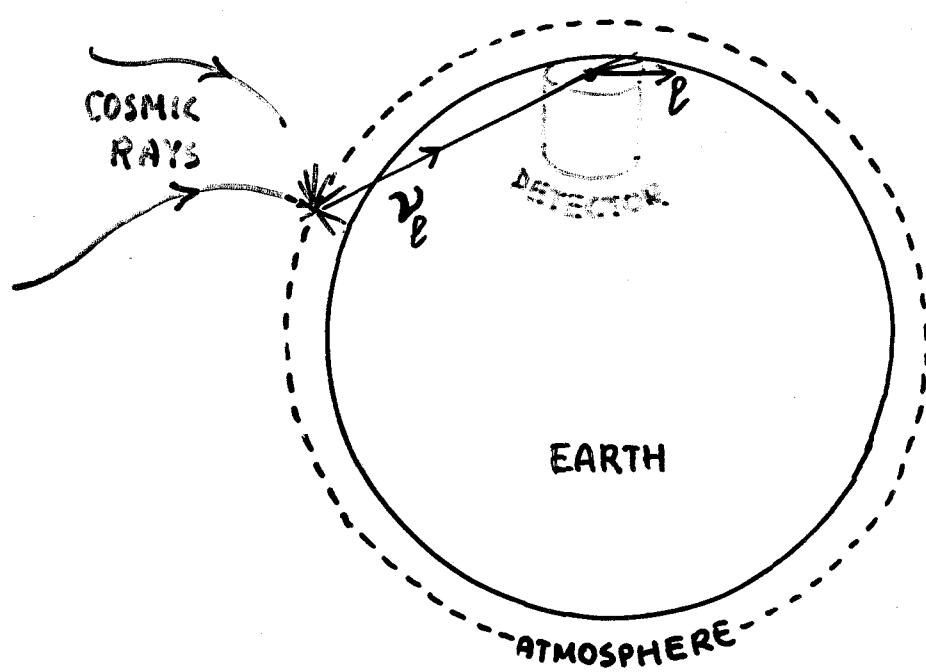
E.g.  $\Delta\chi^2 = 4.61$  gives 30% C.L. errors for  $N_{\text{dof}} < 2$

VAST MAJORITY OF  $\chi^2$ -derived FIGURES  
IN PHENOMENOLOGICAL LITERATURE  
REFERS TO PARAMETER ESTIMATE  
(goodness-of-fit test proven or assumed  
to be satisfied)

# ATMOSPHERIC $\gamma$

Atmospheric  $\bar{\nu}_e$  and  $\bar{\nu}_\mu$  are generated as decay products\* in showers induced by cosmic rays

They can be detected through CC interactions in underground detectors (SuperKamiokande, MACRO, Soudan2,...)



\* mainly from pion decay

$$\begin{aligned}\pi^\pm &\rightarrow \mu^\pm \rightarrow e^\pm \\ &\quad + 2\bar{\nu}_\mu + \bar{\nu}_e\end{aligned}$$

$\gamma$  produce  $e^\pm$ ;  $\gamma$  produce  $\mu^\pm$

## HOW DO THEY LOOK LIKE IN SK?

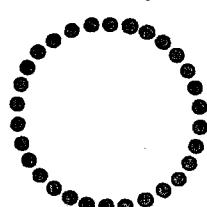
### Particle ID in a Cerenkov Detector:

From side

short track,  
no multiple  
scattering



Ring



Sharp  
Ring

electrons:  
short track,  
mult. scat.,  
brems.

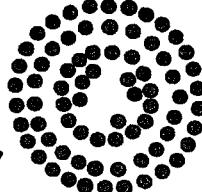


Fuzzy  
Ring

muons:  
long track,  
slows down

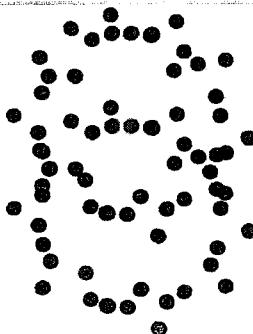
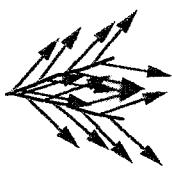


$\mu^\pm$



Sharp Outer  
Ring with  
Fuzzy  
Inner  
Region

neutral pions:  
2 electron-like  
tracks



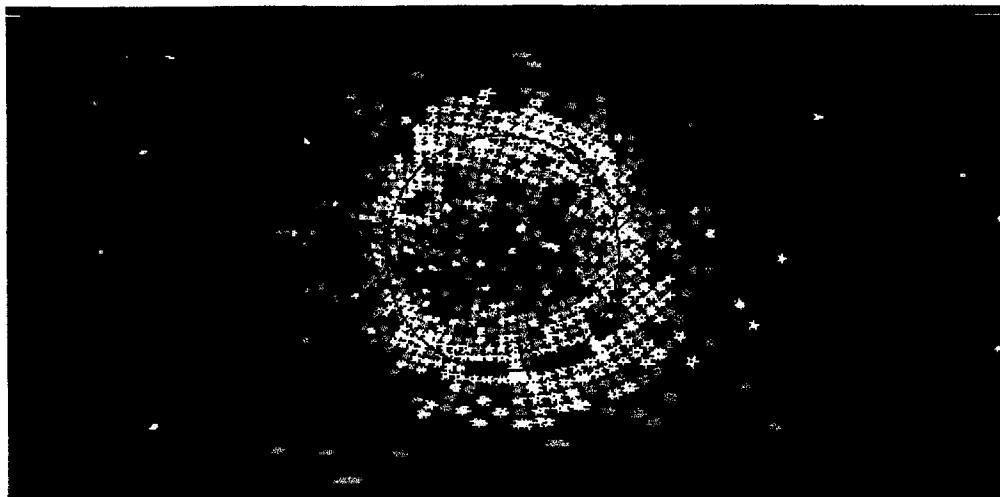
Two  
Fuzzy  
Rings

# Real SK events

## Particle Identification

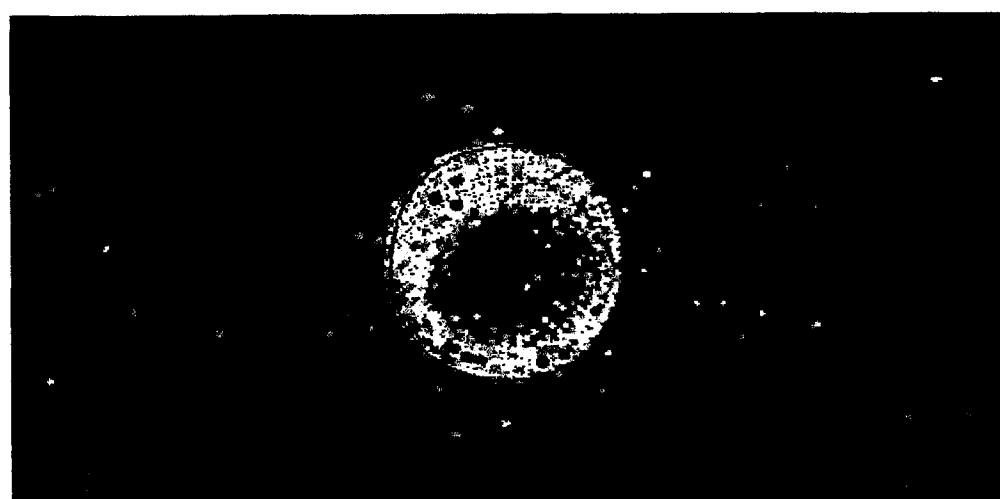
- Must distinguish electrons:

e

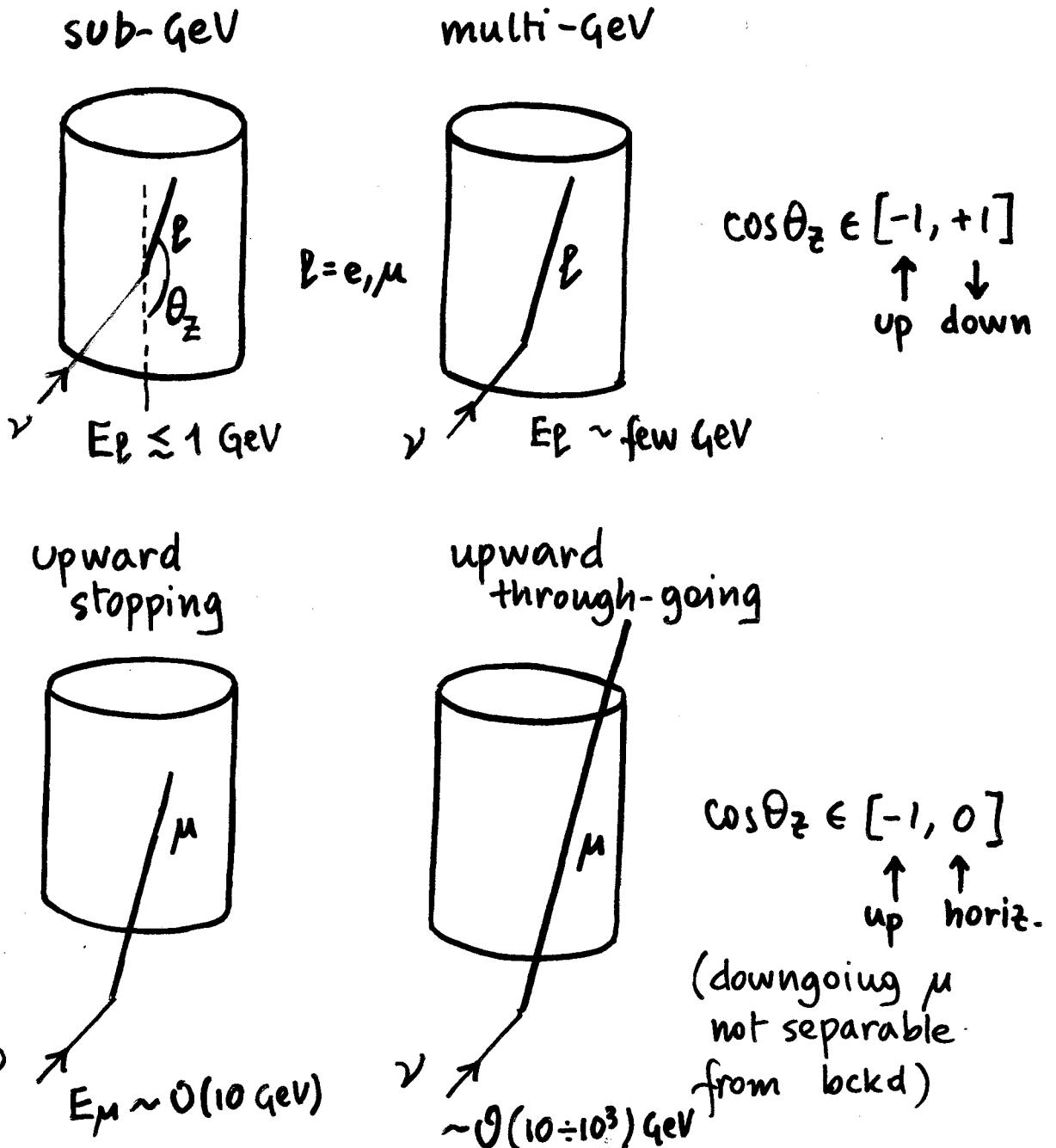


- From muons:

$\mu$



# SuperK. JARGON

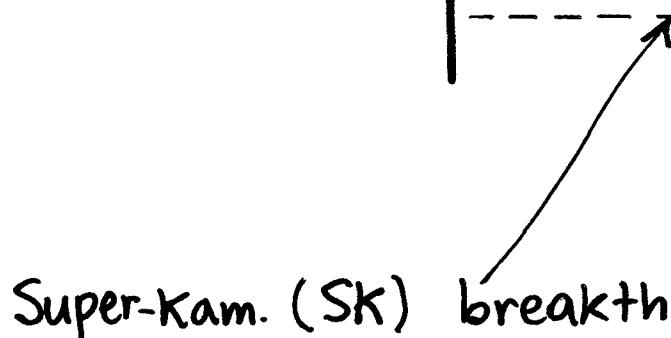


- Range of  $E_\nu$  probed:  $\sim 10^{-1} \div 10^3 \text{ GeV}$
- Range of  $L$  probed:  $\sim 10 \div 10^4 \text{ km}$
- "wide-band" experiment

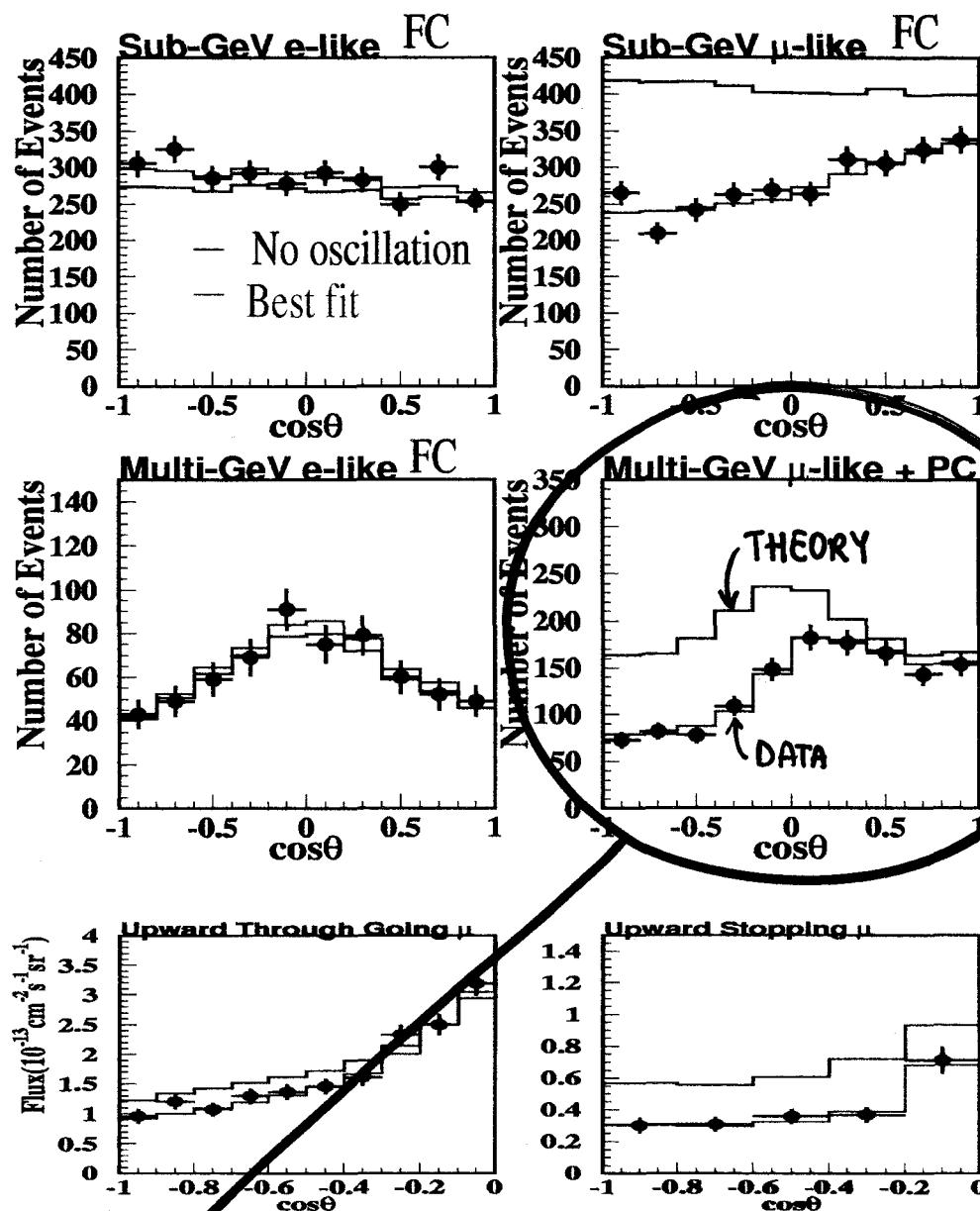
**~ MODEL-INDEPENDENT RESULTS:**  
 (not affected by large normaliz. errors)  
 for no oscillation

PREDICTION	REASON	DATA
$\frac{\Phi(\nu_\mu)}{\Phi(\nu_e)} \sim 2$	$\pi^\pm$ decay	$\frac{\Phi(\nu_\mu)}{\Phi(\nu_e)} \sim 1.2$
$\Phi^\uparrow(\nu_e) \simeq \Phi^\downarrow(\nu_e)$	Spherical source	$\Phi^\uparrow(\nu_e) \simeq \Phi^\downarrow(\nu_e)$
$\Phi^\uparrow(\nu_\mu) \simeq \Phi^\downarrow(\nu_\mu)$	Spherical source	$\Phi^\uparrow(\nu_\mu) < \Phi^\downarrow(\nu_\mu)$

Super-Kam. (SK) breakthrough



# LATEST SK DATA



UP/DOWN ASYMMETRIC DEFICIT OF  
OBSERVED MUONS

3

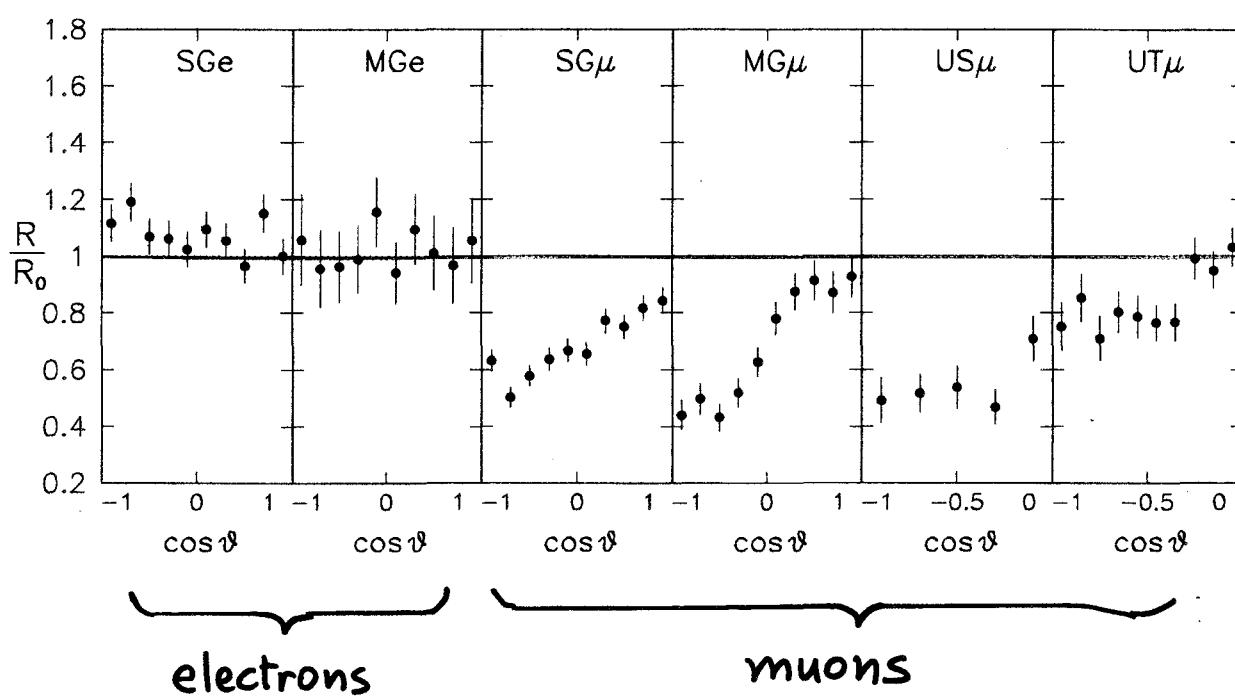
Another represent.  
of the same data:

SG = SubGeV  
MG = MultiGeV  
US = Upward stopping  
UT = " through-going

— Predictions (no osc.)  
• SK data (2001)

Super-Kamiokande (79.5 kTy)  
 $e, \mu$  zenith distributions

Data / MonteCarlo  
( $\pm 1\sigma$  stat. errors)



$\cos \theta = -1$  : upgoing leptons

$\cos \theta = 0$  : horizontal "

$\cos \theta = +1$  : downgoing "

- $e_{\text{observed}} \simeq e_{\text{expected}}$
- $\mu_{\text{observed}} < \mu_{\text{expected}}$



- cannot be  $\nu_\mu \rightarrow \nu_e$
- likely to be  $\nu_\mu \rightarrow \nu_\tau$



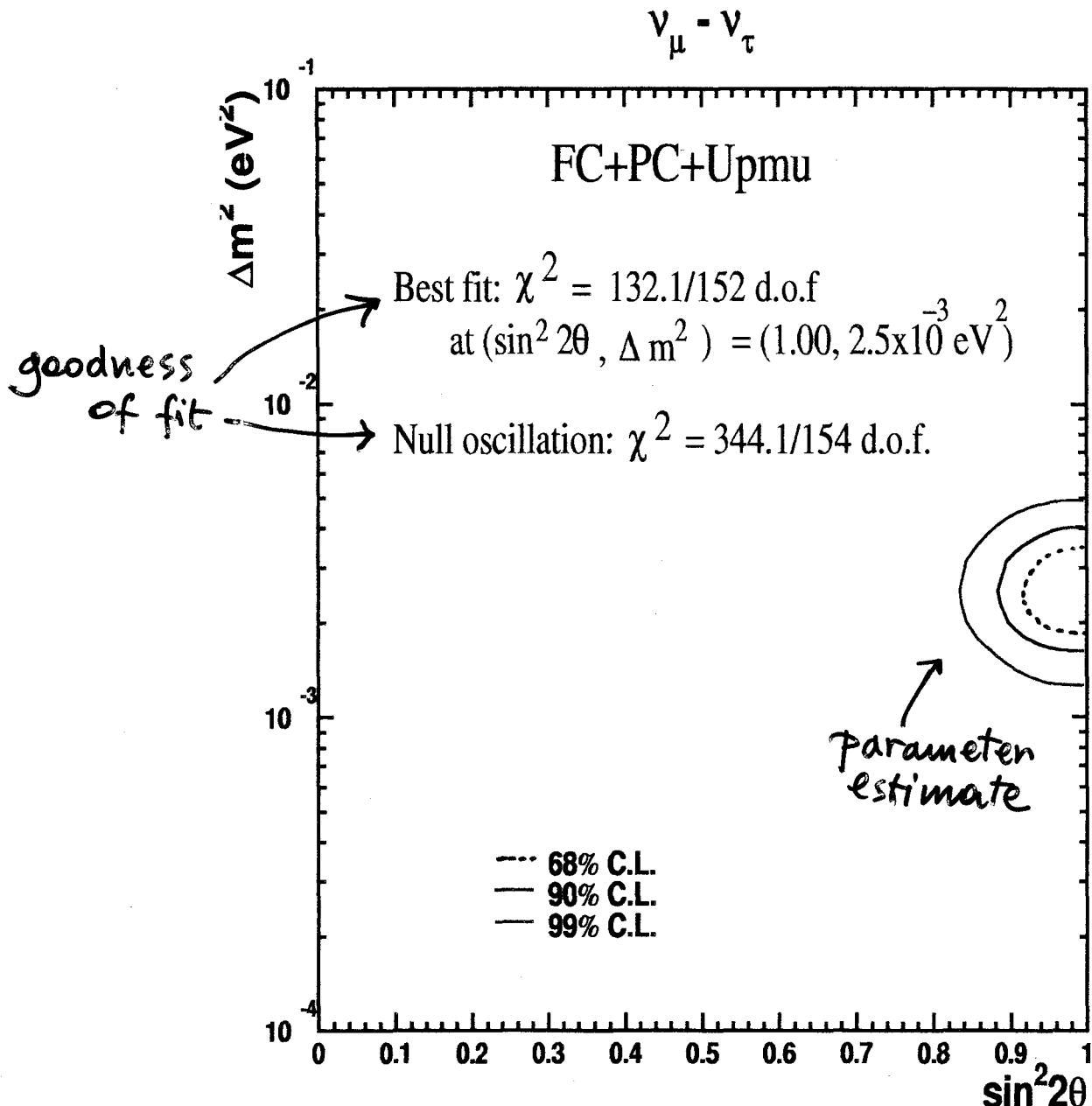
- if  $\nu_\mu \rightarrow \nu_\tau$ , then  $\Delta V_{\mu\tau} = 0$  (vacuum-like)
- lots of spectral data  $(\frac{dR_\mu}{dE}, \frac{dR_\mu}{d\theta_2})$



$\nu_\mu \leftrightarrow \nu_\tau$  analysis expected to select a relatively small spot in mass-mixing param. space

# Official SK analysis

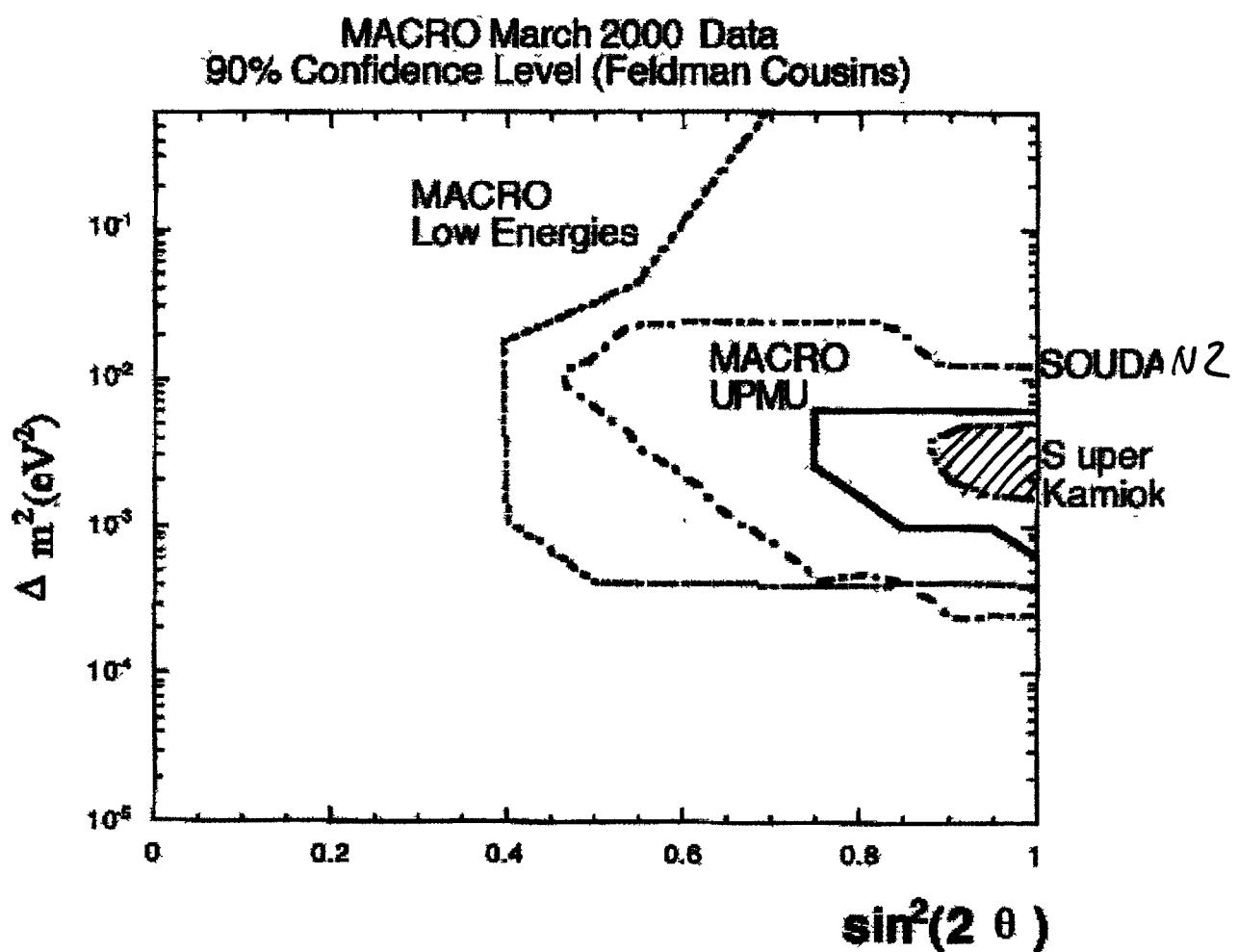
$\nu_\mu \leftrightarrow \nu_\tau$



Best fit:  $\Delta m^2 \simeq 2.5 \times 10^{-3} \text{ eV}^2$

$\sin^2 2\theta \simeq 1$  ("maximal mixing")

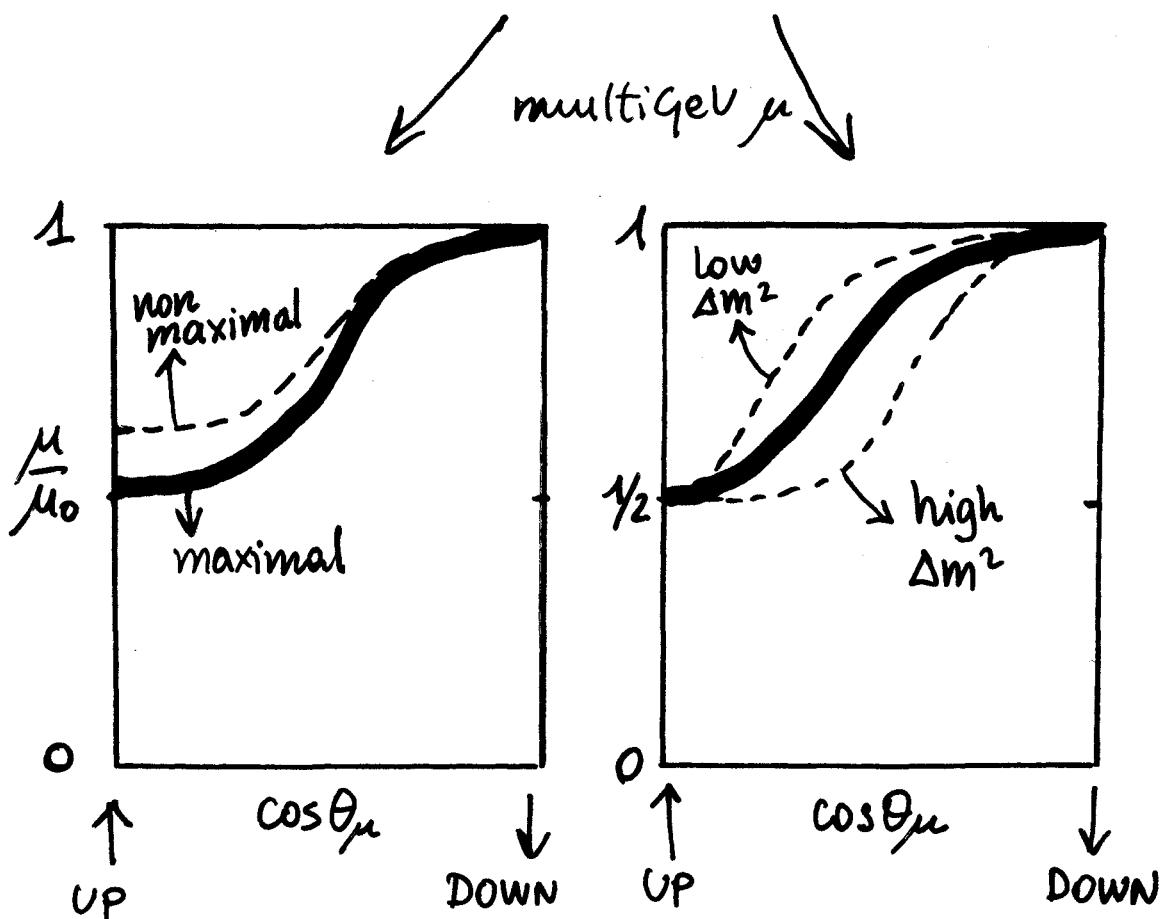
# Confidence level regions ( $\nu_\mu \rightarrow \nu_\tau$ oscillations)



CONSISTENCY AMONG DIFFERENT  
EXPERIMENTS

$\nu_\mu \rightarrow \nu_\tau$   
 $(\Delta m^2, \sin^2 2\theta)$  fit robust because:

- DIFFERENT SK DATA CONSISTENT WITH EACH OTHER
- DIFFERENT EXPERIMENTS CONSISTENT WITH EACH OTHER
- FIT DOMINATED BY A SINGLE, STRIKING EVIDENCE:  
U/D ASYMMETRY OF multi-GeV muons



... CANNOT  
CHANGE  $\sin^2 2\theta$   
TOO MUCH ...

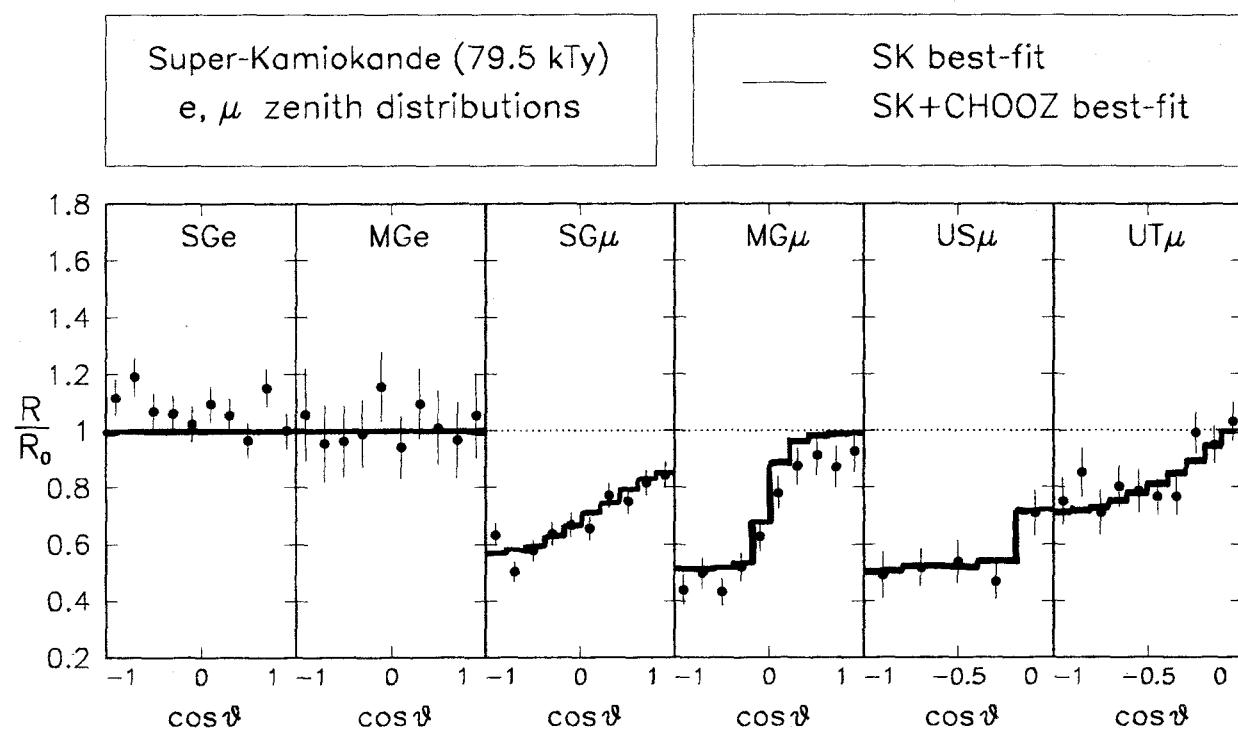
... CANNOT  
CHANGE  $\Delta m^2$   
TOO MUCH ...

At best fit:

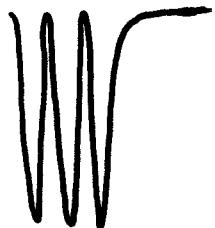
$$P(\nu_\mu \rightarrow \nu_e) = 0 \quad P(\nu_\mu \rightarrow \nu_\tau) \cong \sin^2 \left( 4 \frac{L/km}{E/MeV} \right)$$

shown is  $\int \phi \otimes P \otimes \sigma \otimes \epsilon_{ff}$

Fogli  
E.L.  
Marrone



$\nu_\mu \leftrightarrow \nu_\tau$



### A "MIRACLE" :

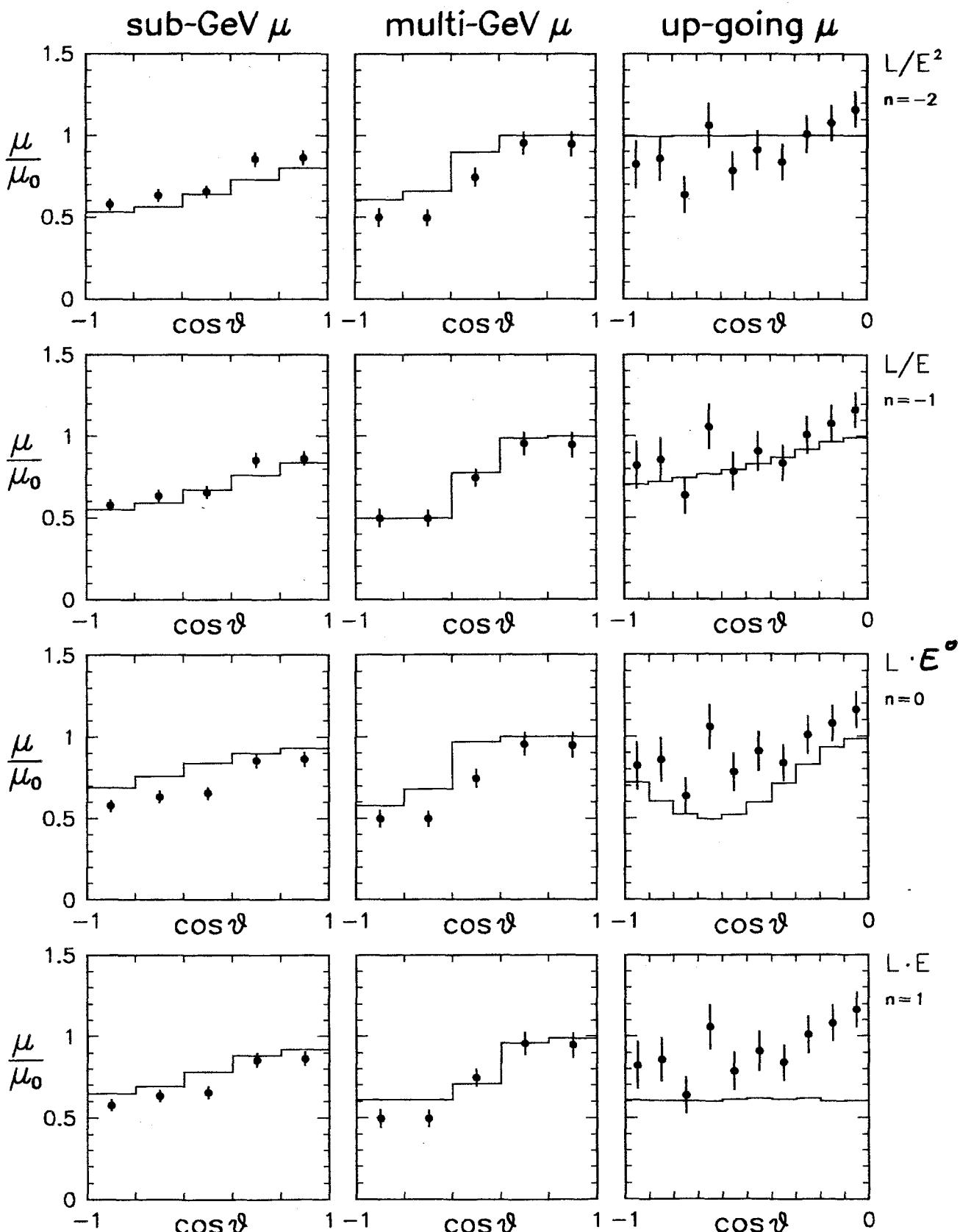
- Exceedingly simple formula for  $P_{\mu\tau}$  works over 3 decades in L and 4 in E
- Nobody could have guessed  $\sin^2$  form from the data without prior theory.

MOREOVER,

$\sin^2$  argument must be  $\propto L/E \rightarrow$

Super-Kamiokande muon  
distributions at best fit

	$L/E^2$	$L/E$	$L$	$L \cdot E$
$\alpha$ $\rightarrow$	1.00	1.00	0.51	0.78
$\beta$ $\rightarrow$	3.00	3.56	0.19	0.27
$\chi^2$ $\rightarrow$	47.7	20.3	62.9	66.0



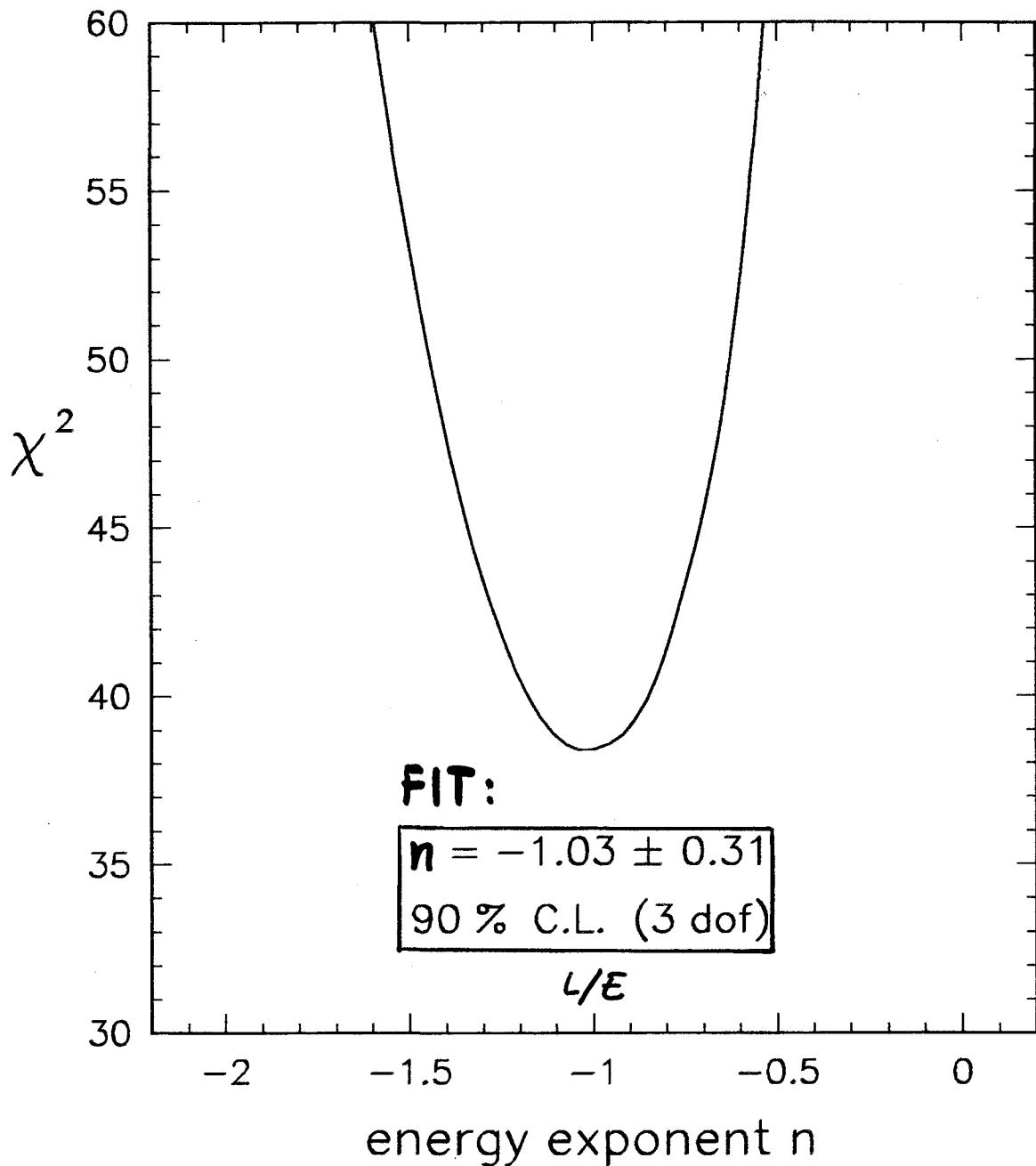
Only  $L/E$  gives good agreement  
at all  $L, E$  probed by SK

$$P_{\text{out}} = \alpha \sin^2(\beta L E^n)$$

$$n = -1 \rightarrow L/E$$

Fit with  $(\alpha, \beta, n)$  free

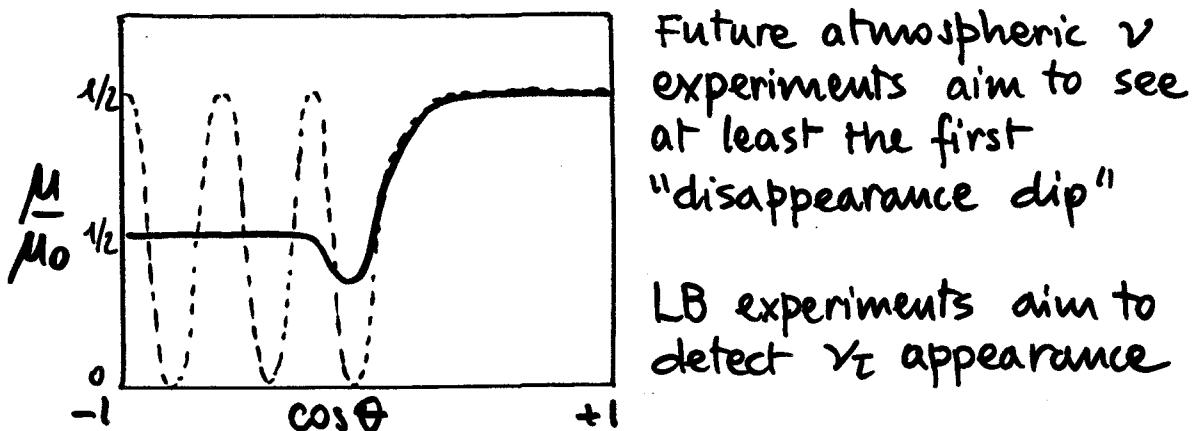
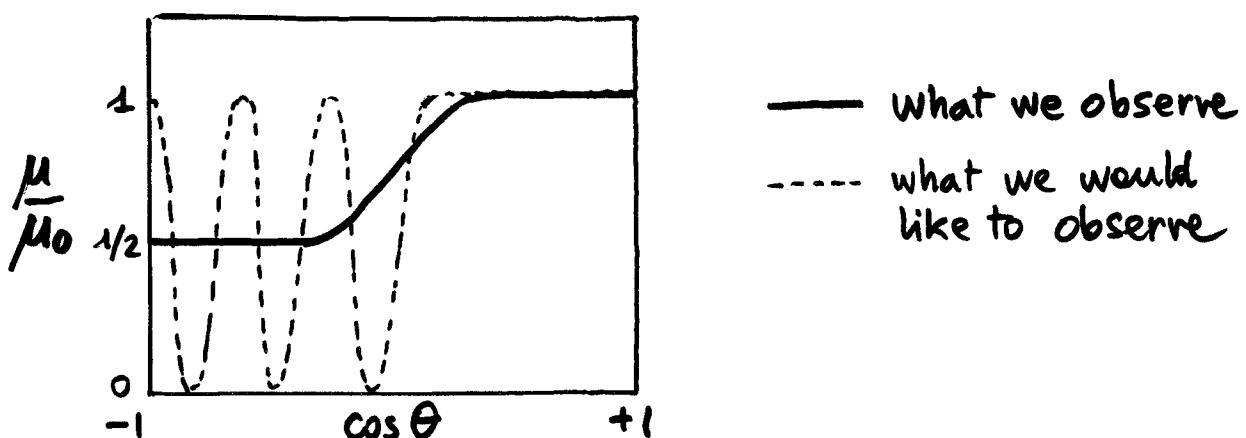
Bounds on nonstandard dynamics



(It was  $n = -0.9 \pm 0.4$  with 45 kTy data)

$\nu_\mu \leftrightarrow \nu_\tau$  EXPLANATION :

- Theoretically SIMPLE
- Experimentally ROBUST
- .... but INDIRECT!



While waiting for future observations ...

... ROOM FOR SKEPTICISM:  
 SCENARIOS WITH NON PERIODIC  $P_{\mu\mu}(L/E)$

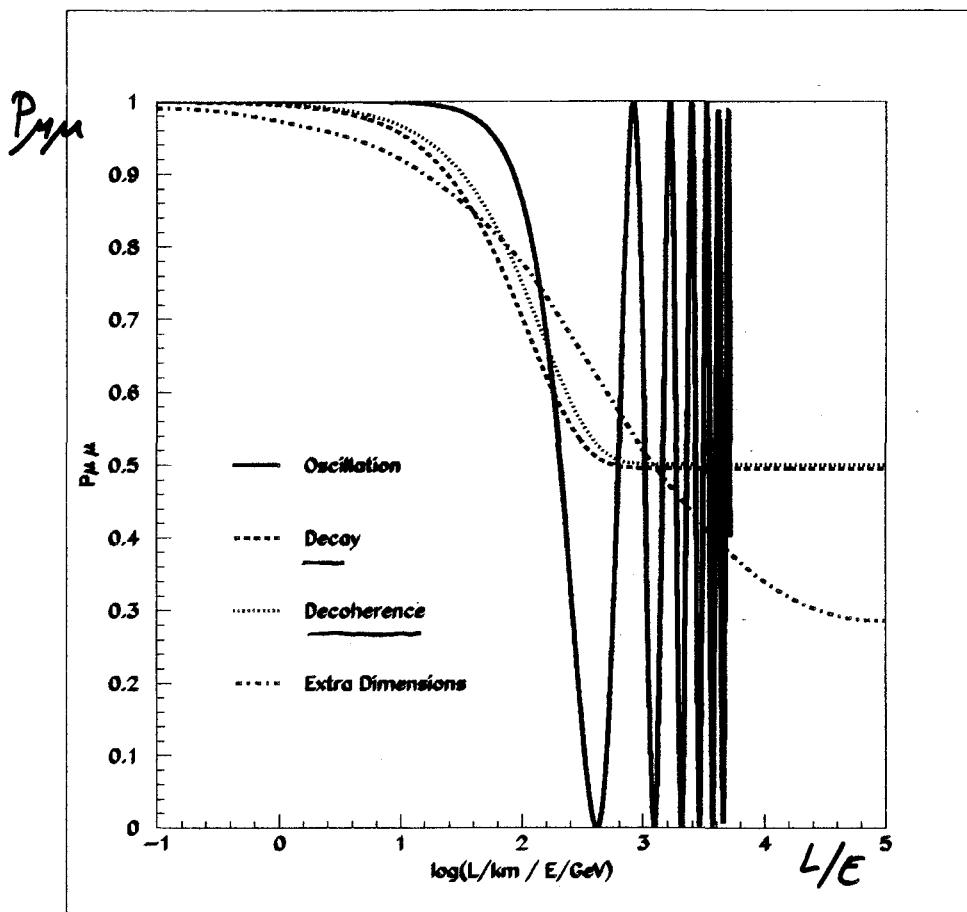


FIGURE 1. Survival probability for  $\nu_\mu$  versus  $\log_{10}(L/E)$  for the decay model, decoherence, extra dimensions and oscillation.

STILL ~ COMPATIBLE WITH DATA  
 BUT PARAMETERS RATHER "AD HOC"

ATMOSPHERIC  $\nu$ :

$\nu_\mu \leftrightarrow \nu_e$  OK

... BUT:

OSCILLATION PATTERN  
NOT YET OBSERVED

---

WE'LL SHOW NOW THAT

$\nu_\mu \leftrightarrow \nu_s$  disfavored

- HERE, MATTER EFFECTS IMPORTANT  
 $(\nu_\mu(x) - \nu_s(x) \neq 0)$  BUT NOT OBSERVED!

## Remember :

For  $\gamma_\mu \leftrightarrow \gamma_e$  :  $\mathcal{H} = \mathcal{H}_{\text{vacuum}} \pmod{1}$

For  $\gamma_\mu \leftrightarrow \nu_s$  :  $\mathcal{H} = \mathcal{H}_{\text{vacuum}} + \begin{pmatrix} \Delta V \\ 0 \\ 0 \end{pmatrix}$   
 $\Delta V = V_\mu - V_s \neq 0$

Effective  
mixing angle  
in matter

$$\sin^2 2\theta_m = \frac{\sin^2 2\theta}{\left(\frac{2\Delta V \cdot E}{\Delta m^2} - \cos 2\theta\right)^2 + \sin^2 2\theta}$$

- MSW effect mostly known for the possible enhancement of small vacuum mixing:

$$\sin^2 2\theta \text{ small} \longrightarrow \sin^2 2\theta_m \sim 1 \text{ for } \Delta V \sim \Delta m^2 / 2E$$

- BUT HERE WE ARE INTERESTED IN THE OPPOSITE FACT:

$$\sin^2 2\theta \simeq 1 \longrightarrow \sin^2 2\theta_m \simeq \frac{1}{1 + \left(\frac{2\Delta V \cdot E}{\Delta m^2}\right)^2} < 1$$

↑  
ESPECIALLY AT HIGH E

→ matter effects inhibit atmospheric  $\gamma_\mu$  disappearance if  $\gamma_\mu \rightarrow \nu_s$

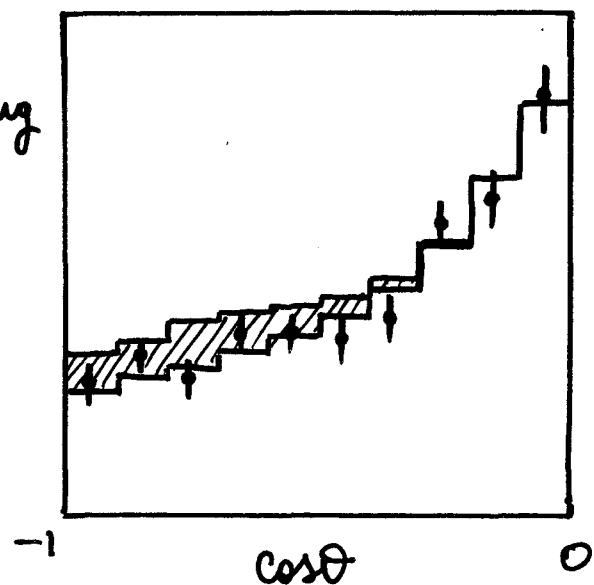
BUT: SK DATA DO NOT SUPPORT  $\sin^2 2\theta_m < 1$

→ High-energy muons in SK

Partially  
Contained  
muons



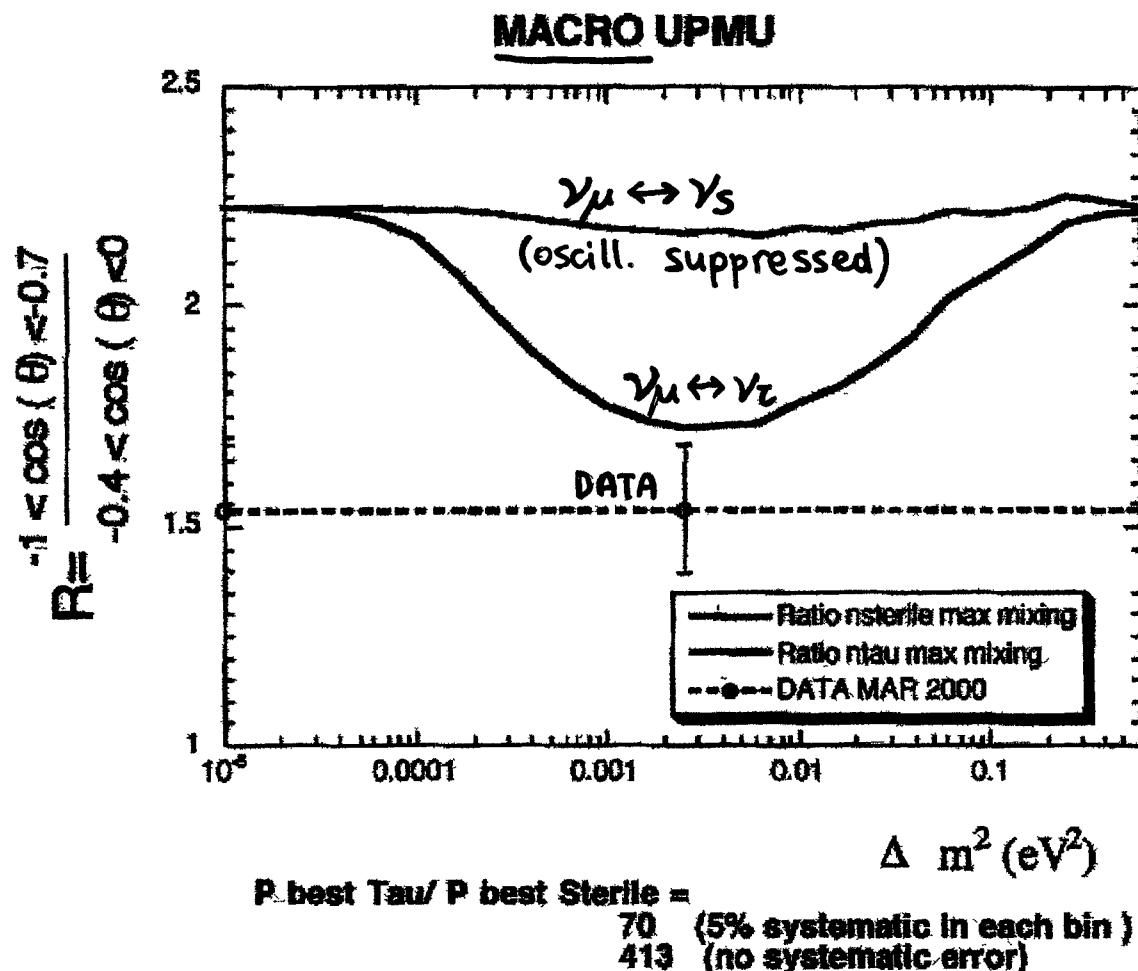
Upward  
through-going  
muons



→ no evidence  
for  $\nu_\mu \leftrightarrow \nu_s$   
"excess"

SK claim:  $\nu_\mu \leftrightarrow \nu_s$  DISFAVORED @>99% C.L.

# Ratio vertical/horizontal Montecarlo Optimized



- The plot is for Maximum mixing.
- Sterile neutrino disfavored respect to tau at **>98%** for any mixing (5% systematic in each bin)

SEVERAL INDEPENDENT DATA SETS  
& ANALYSES DO NOT SUPPORT  
 $\gamma_\mu \rightarrow \nu_s$  AND THE ASSOCIATED  
(MATTER) EFFECTS

E.g. : no observation of reduced  
NC events (statistical) due  
to  $\nu_s$  - non interacting

RECENTLY, SK CLAIMS ISOLATION OF  
"Z-like" "RINGS" AT THE 2 $\sigma$   
LEVEL  $\rightarrow$  FURTHER INDICATION AGAINST  
 $\gamma_\mu \rightarrow \nu_s$

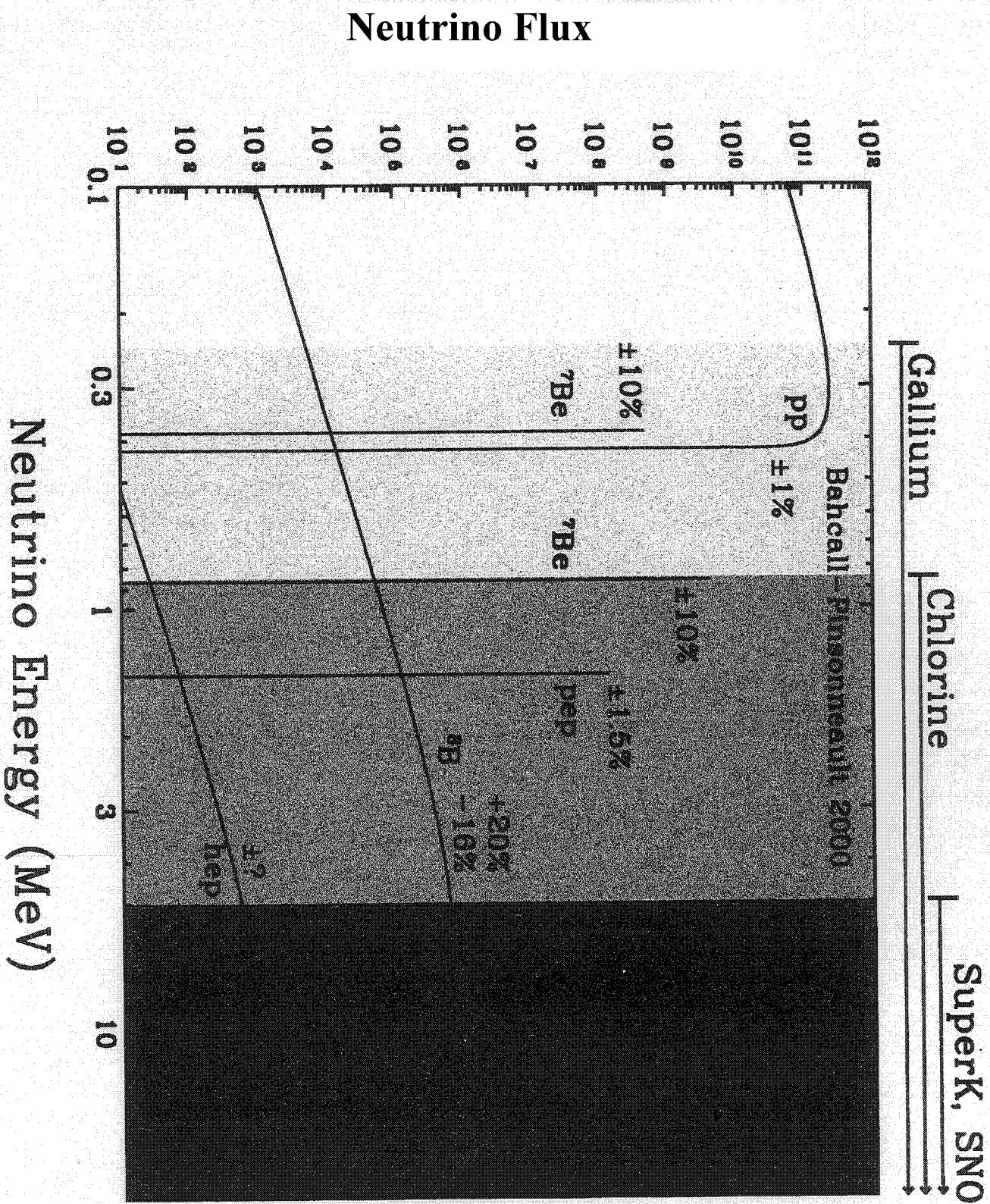


SK data "don't like"  $\nu_s$   
at  $> 99\%$  C.L.  
(assuming PURE  $\gamma_\mu \rightarrow \nu_s$ )

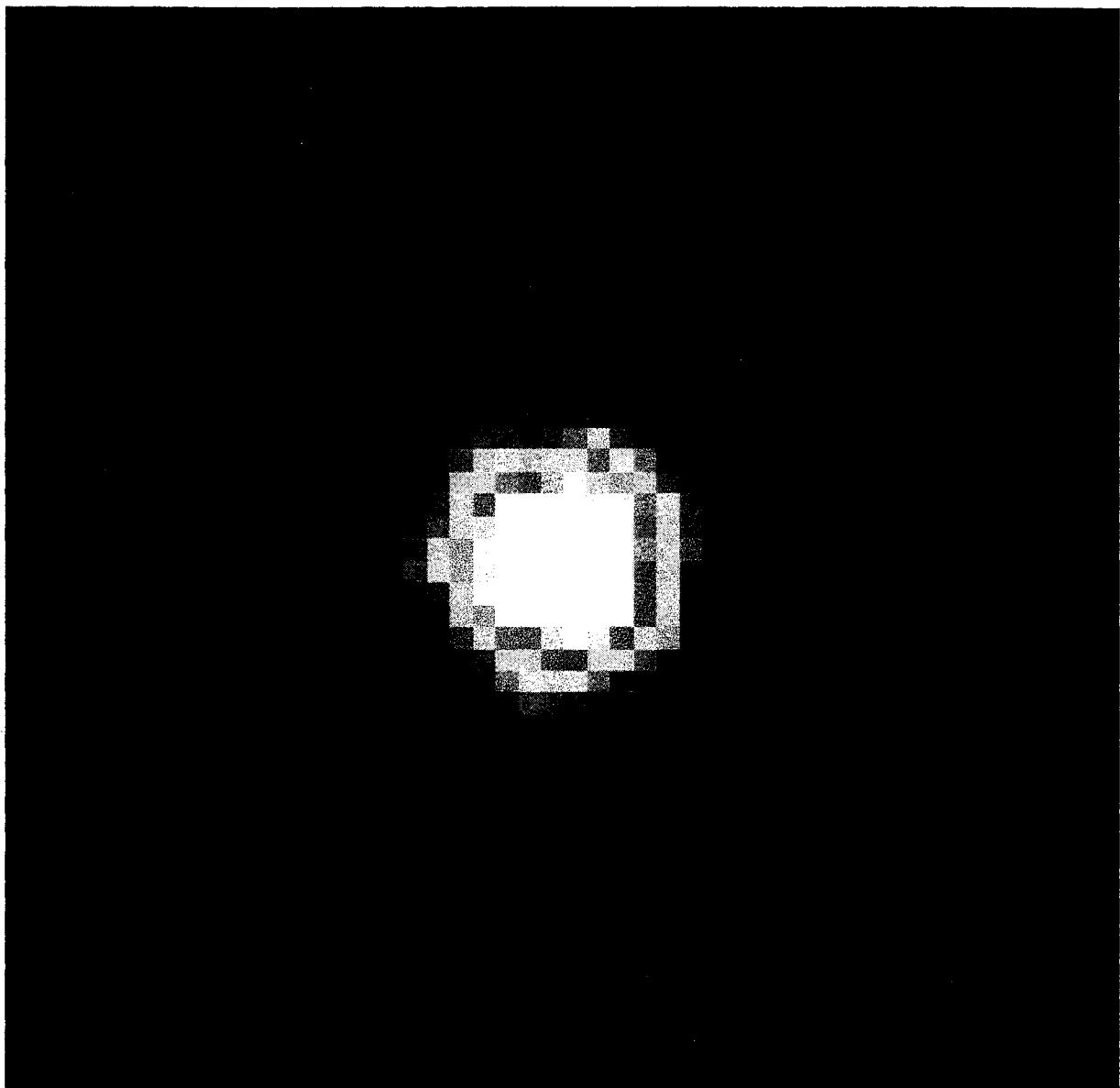
# SOLAR $\nu$ : pre-SNO situation

.... WAIT FOR LECTURE IV  
TO SEE S.N.O. effect....

# SOLAR $\nu$ SKY



THE SUN  
AS SEEN WITH V'S



---

(SK)

# SOLAR NEUTRINOS

## EXPERIMENT

## REACTION

- Homestake



- SAGE  
GALLEX + GNO



- Kamiokande

Superkamiokande

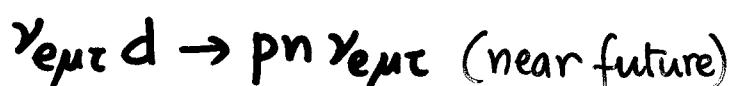


- SNO [CC]



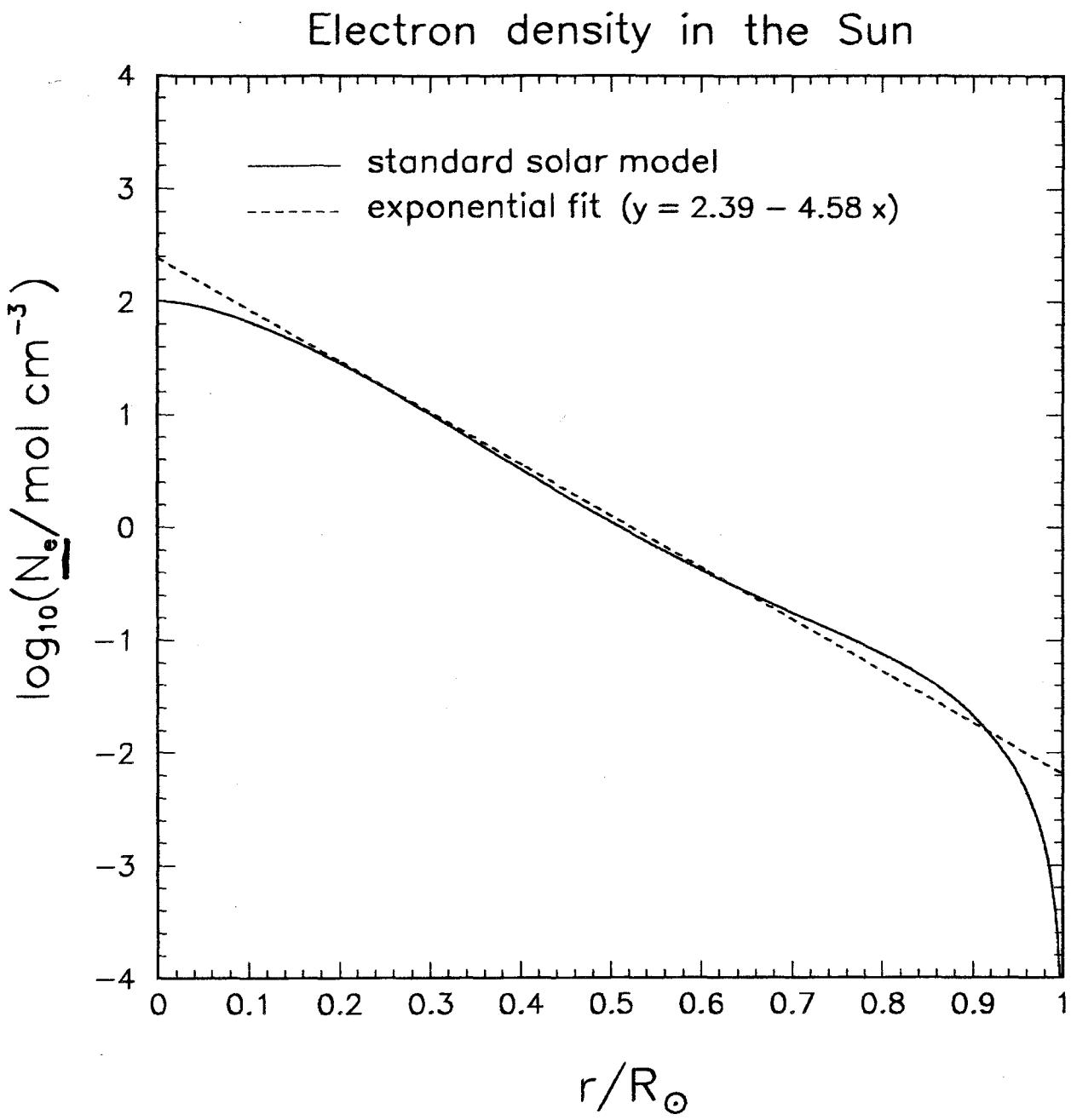
done!

- SNO [NC]



.....

- can probe  $\nu_e$  disappearance over many orders of magnitude
- matter effects important in a large fraction of parameter space

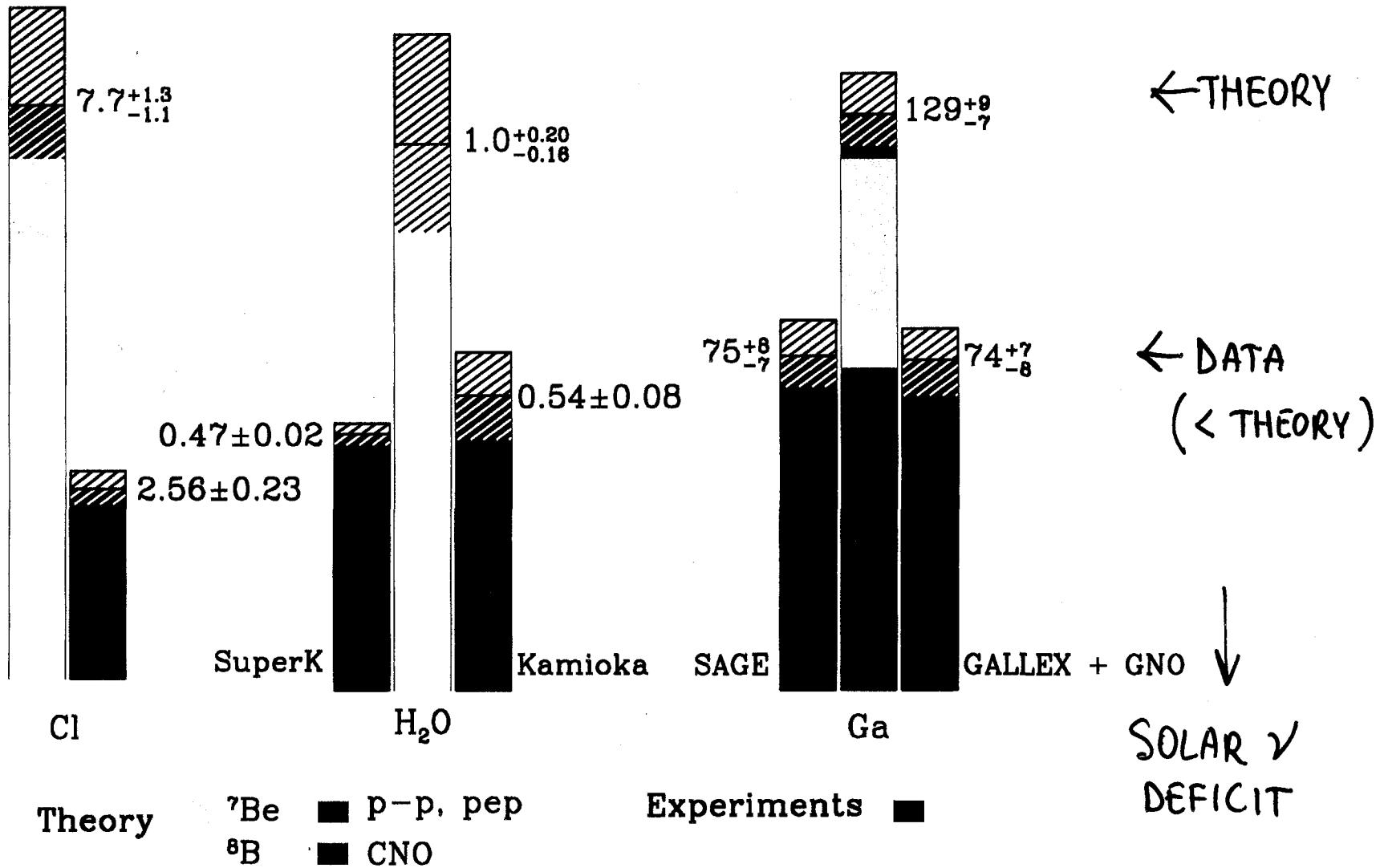


4 orders of magnitude in  $N_e$

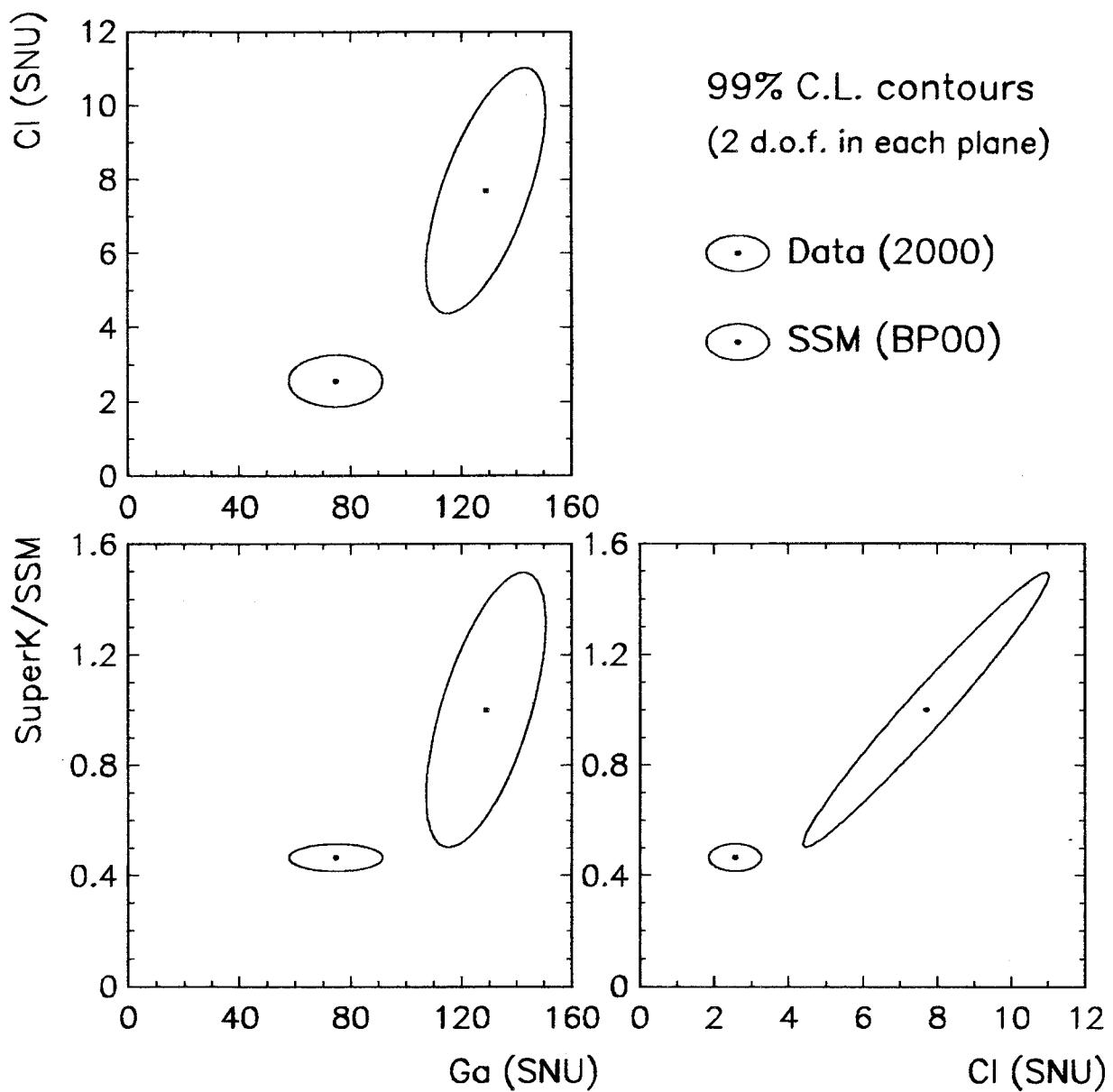
→  $N_e$  relevant for  
 $\Delta m^2 \sim 10^{-8} \div 10^{-4} \text{ eV}^2$

Total Rates: Standard Model vs. Experiment  
 Bahcall-Pinsonneault 2000

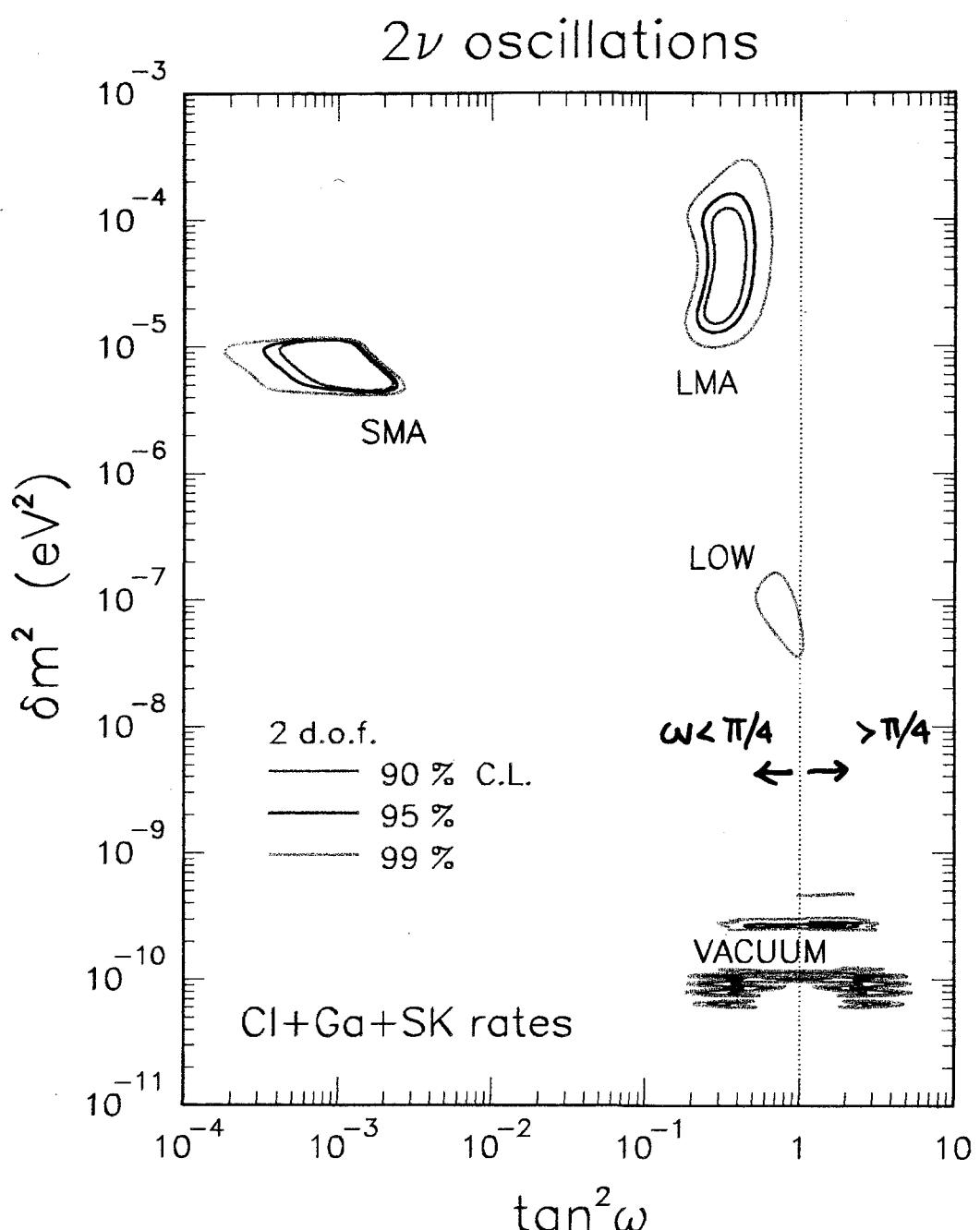
32



## Solar neutrino deficit

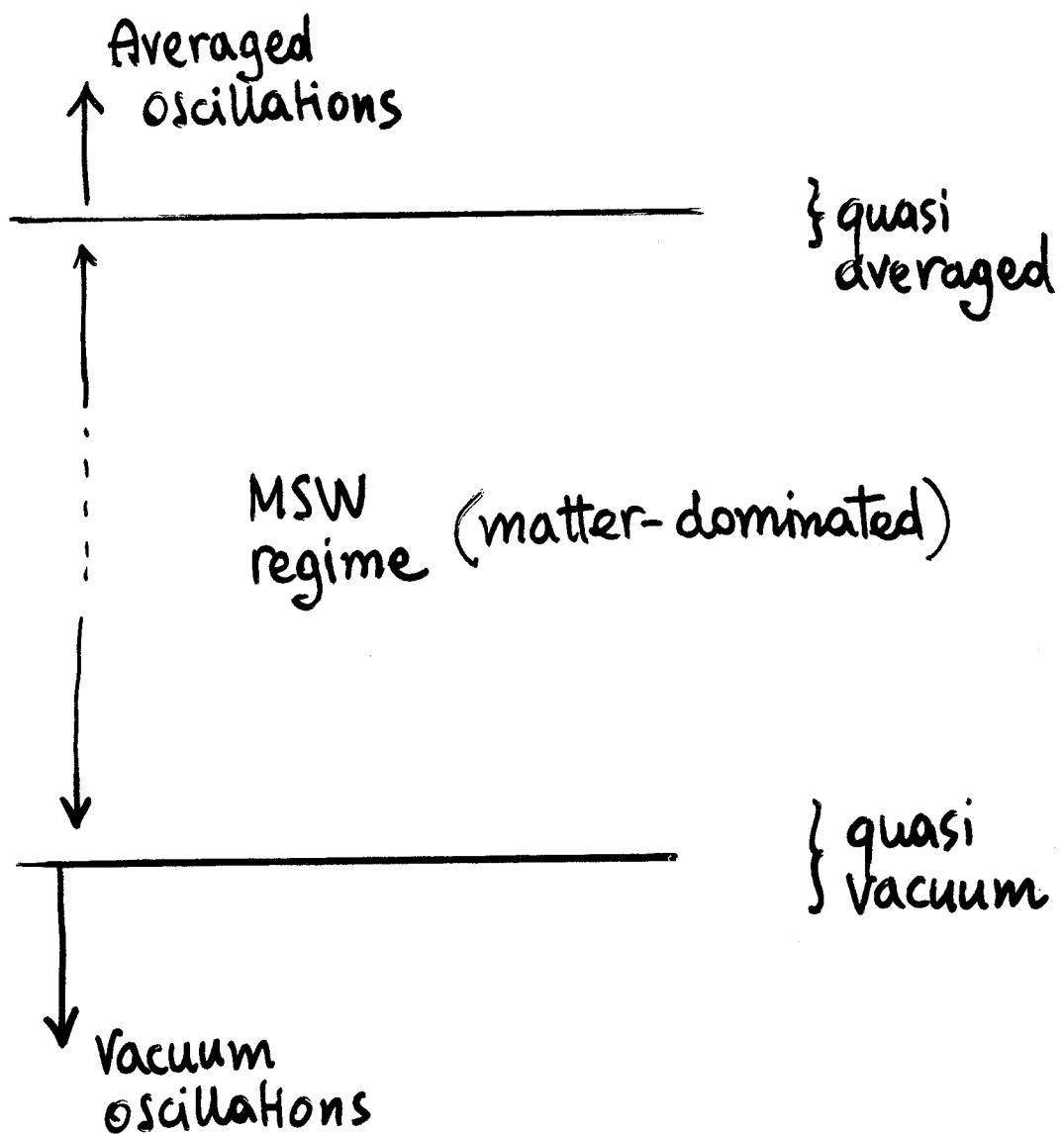


Fogli, E.L.,  
Moutauno, Palazzo



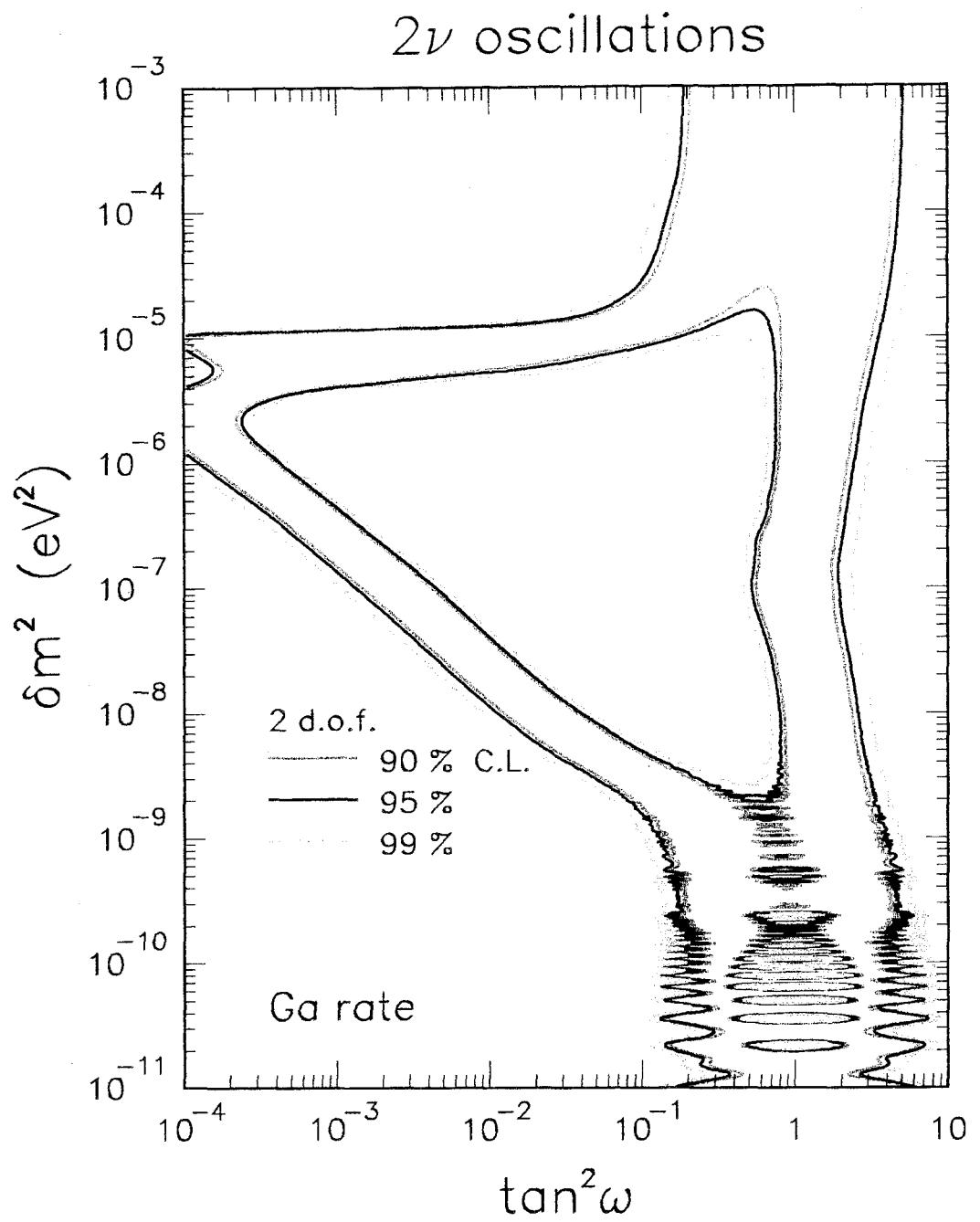
$$\nu_e \rightarrow \nu_{\mu,\tau}$$

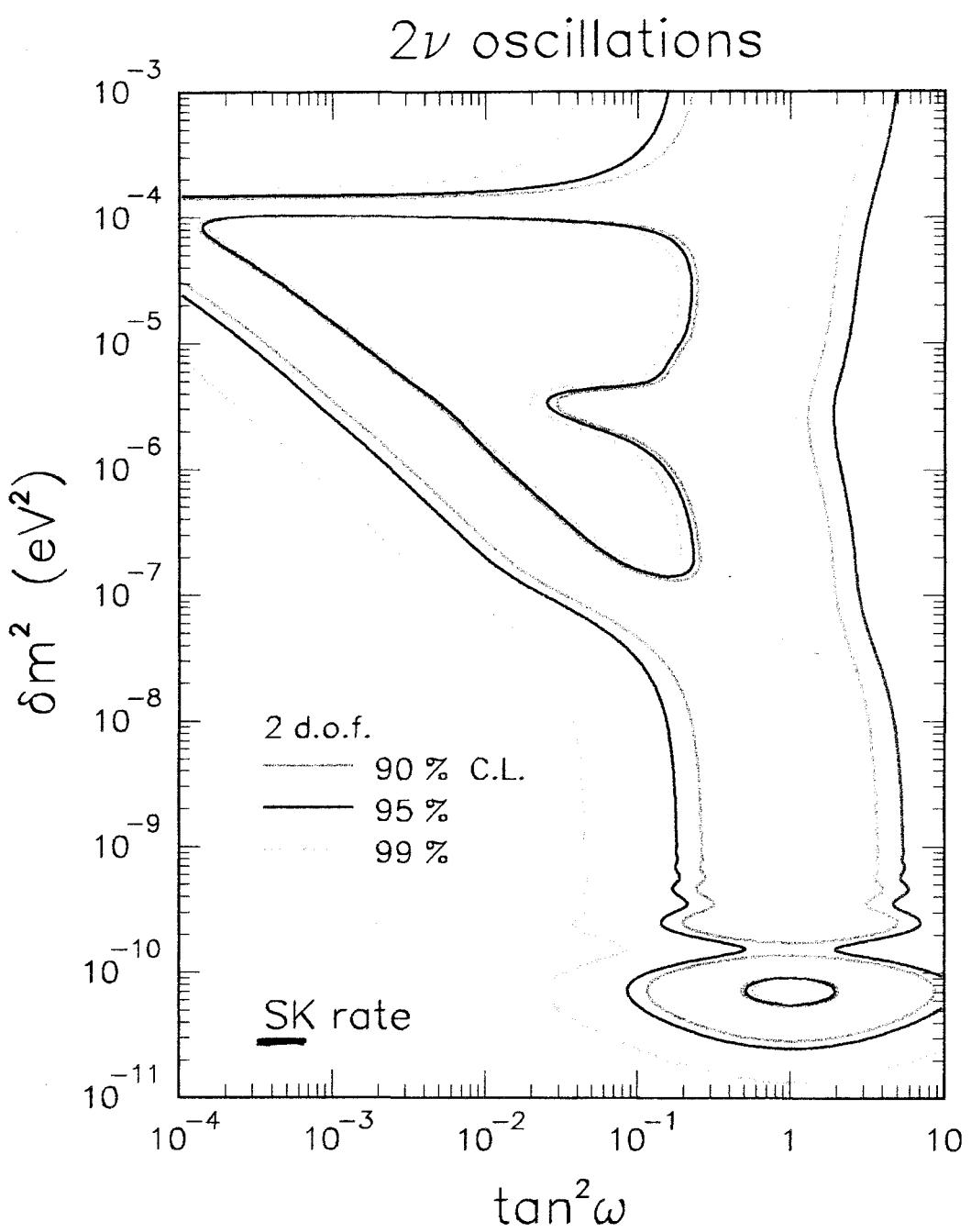
- RATE INFORMATION ONLY
- 2000 DATA + Solar model



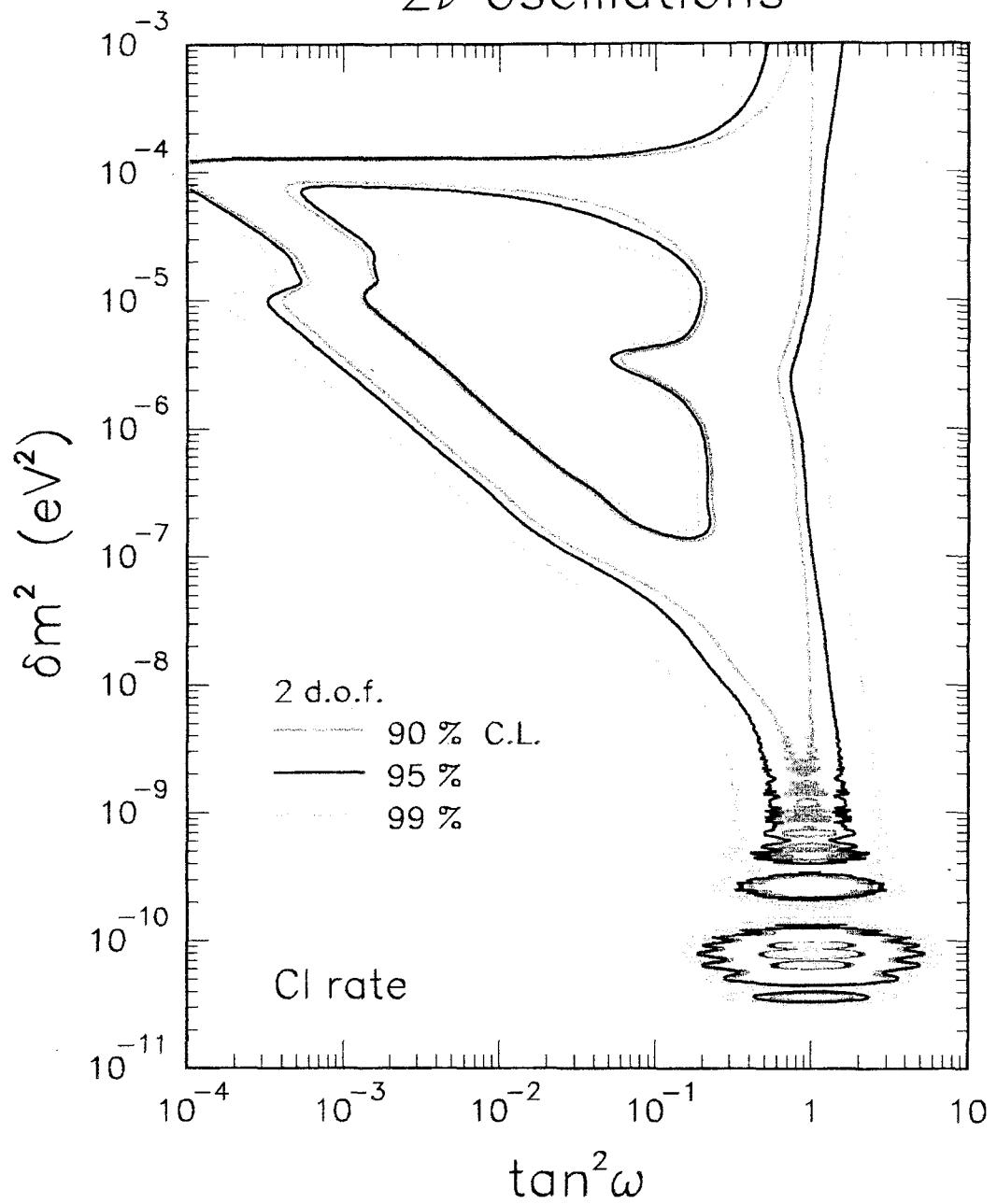
Rather different physics  
in different regimes

→ BREAK DOWN TO SINGLE EXPERIMENTS

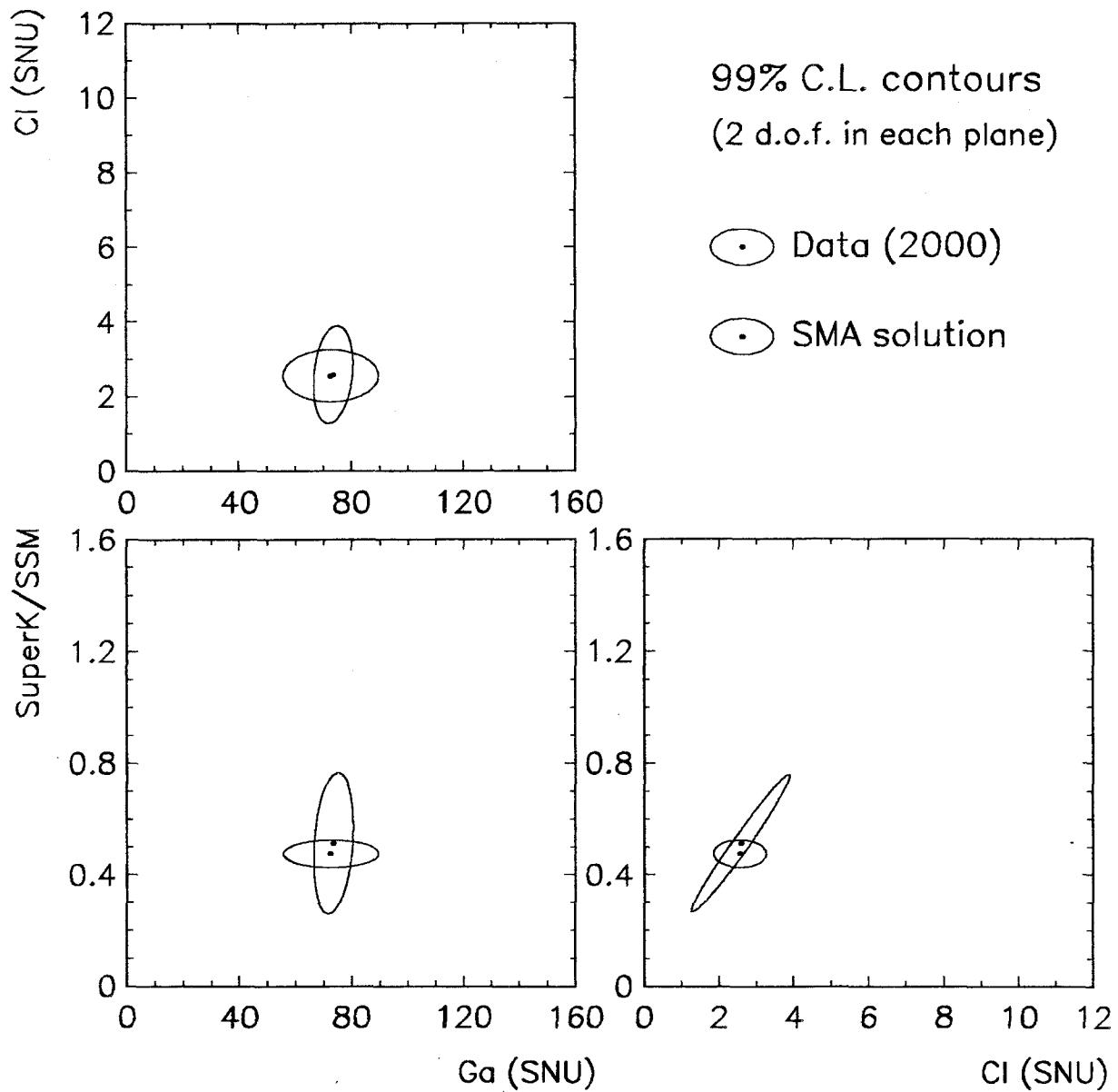




## $2\nu$ oscillations

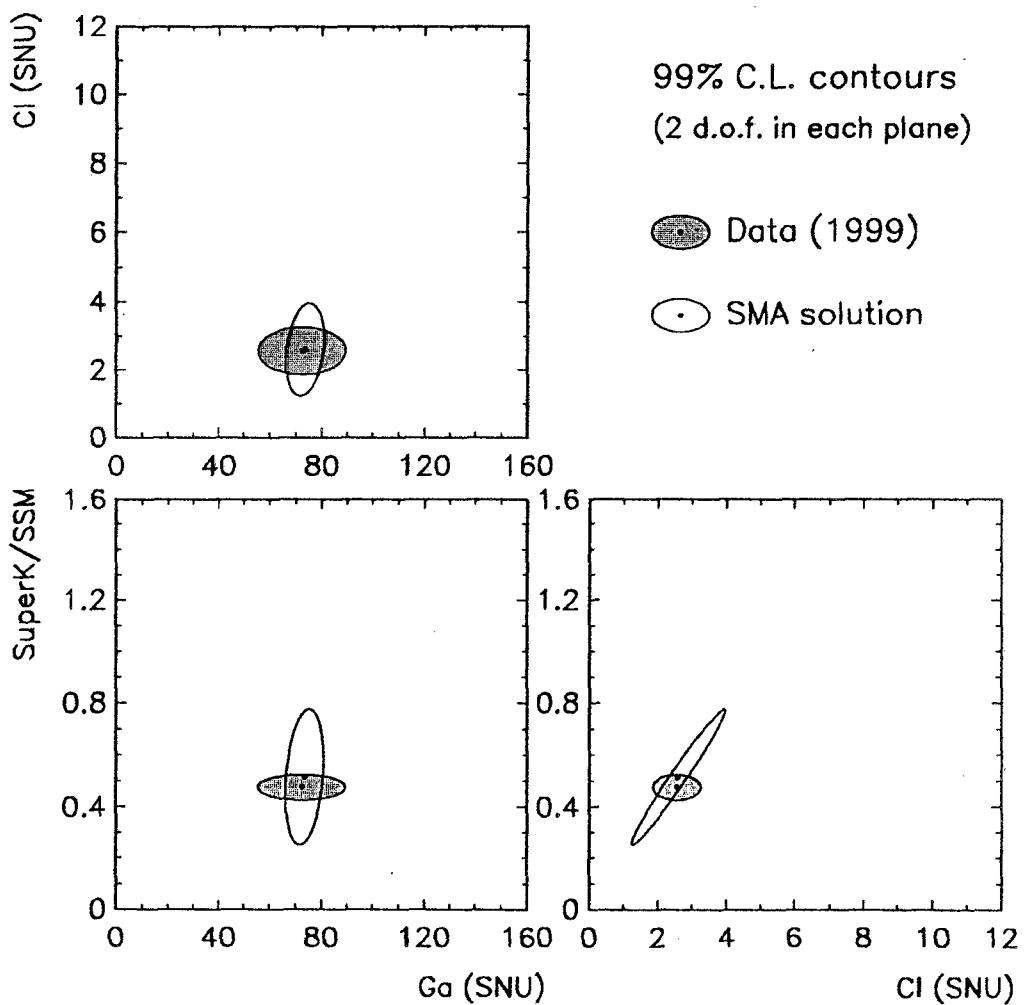


## MSW oscillations, SMA solution



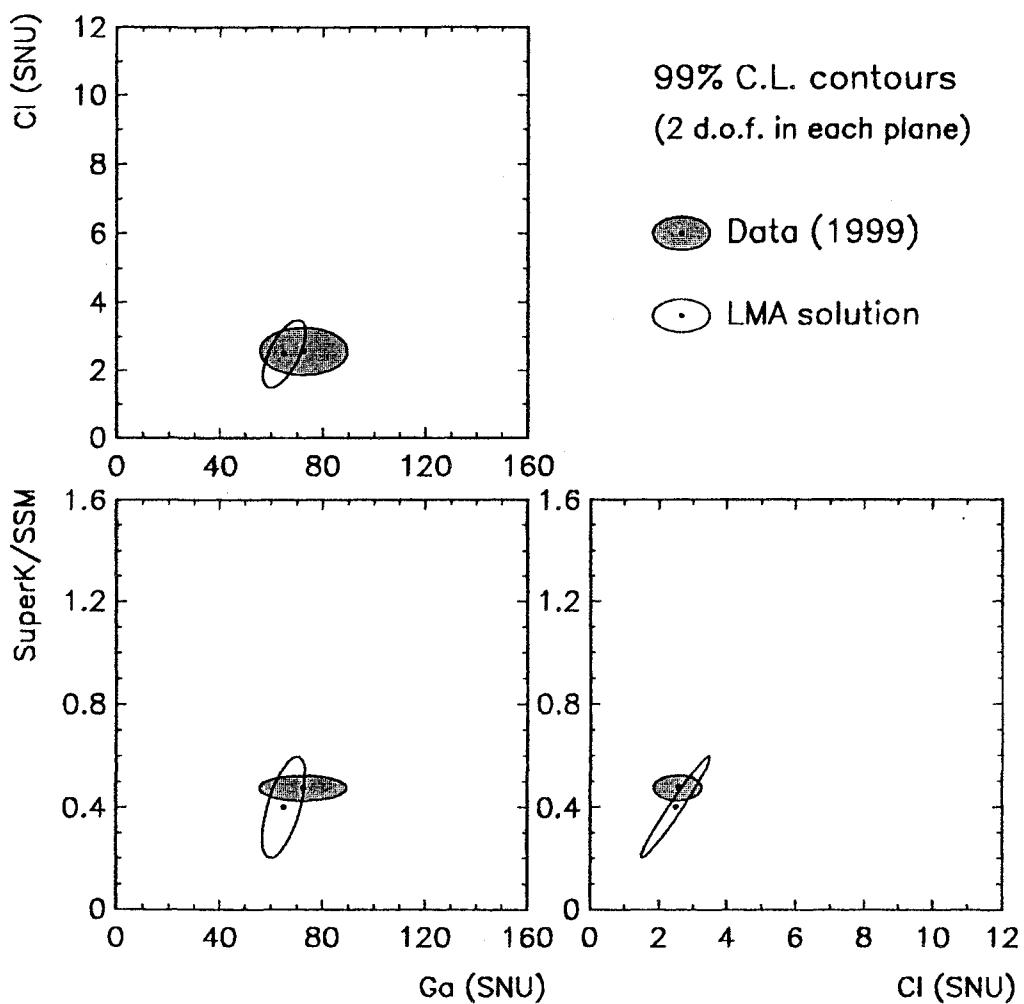
- SMA provides perfect fit to rates
- ... v.v. • Both LMA and LOW underestimate  $G_A$
- ... v.v. • LOW overestimates  $C_L$

MSW oscillations, SMA solution

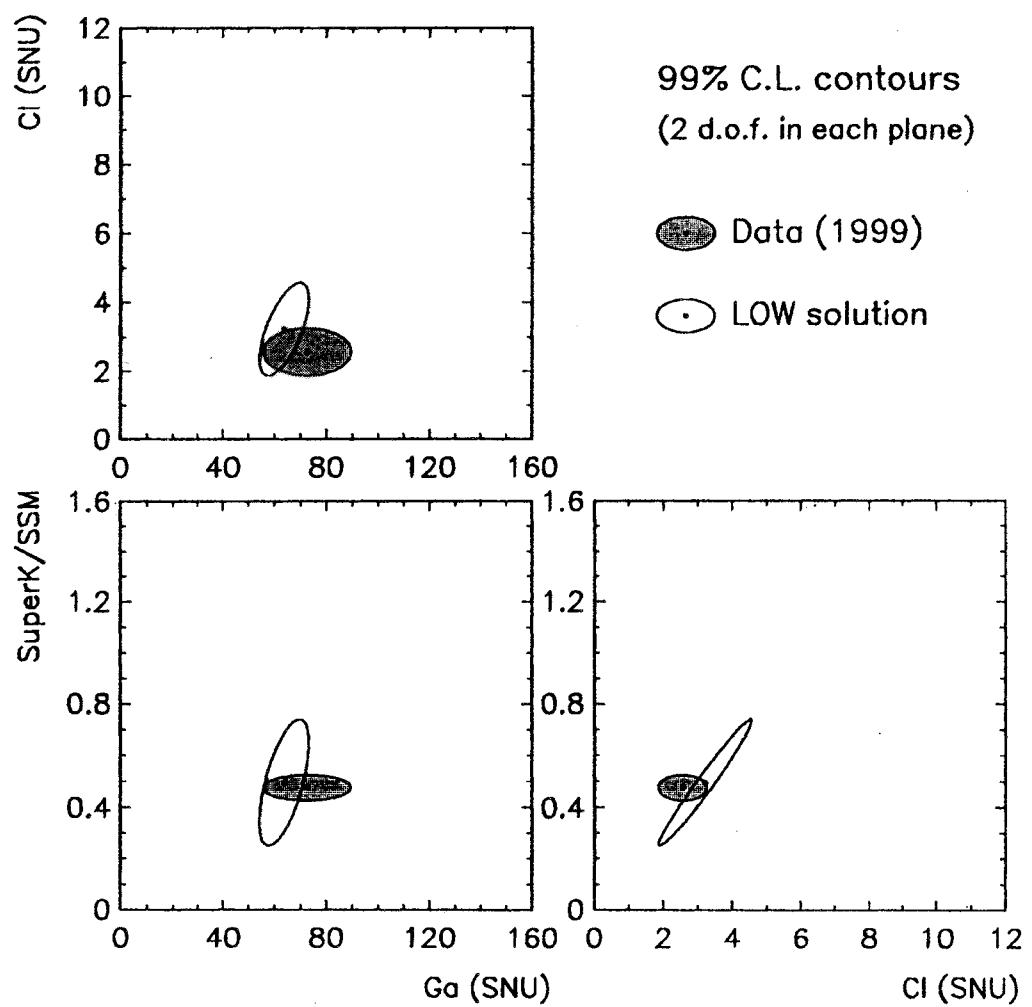


However, bulk of SK/SSM spectrum is flat  
 (as predicted by LOW and LMA solutions)  
 while a "tilt" is expected for the SMA solution  
 (see later.)

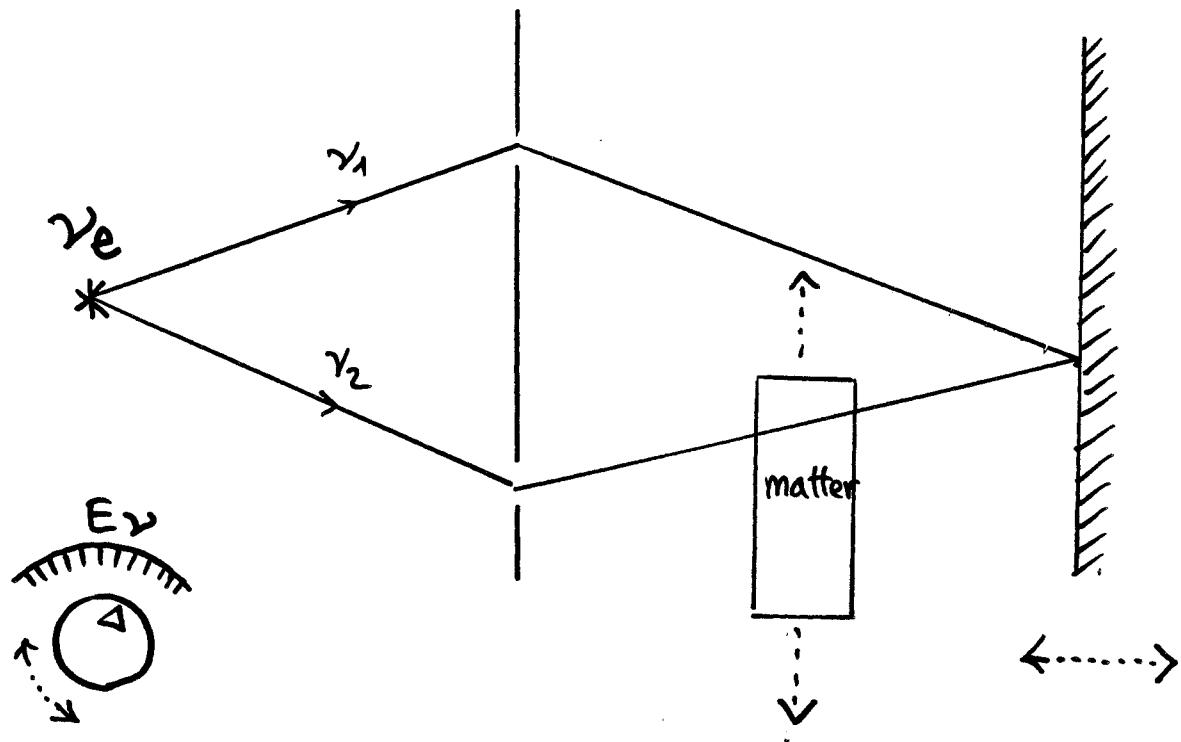
## MSW oscillations, LMA solution



## MSW oscillations, LOW solution



AVERAGE DEFICIT  $\leftrightarrow$  "GREY SCREEN"  
 HOW TO GET MORE INFORMATION?



"TUNE"  
ENERGY

↓  
energy  
spectrum

"MOVE"  
MATTER  
IN AND OUT

↓  
day-night  
earth effect

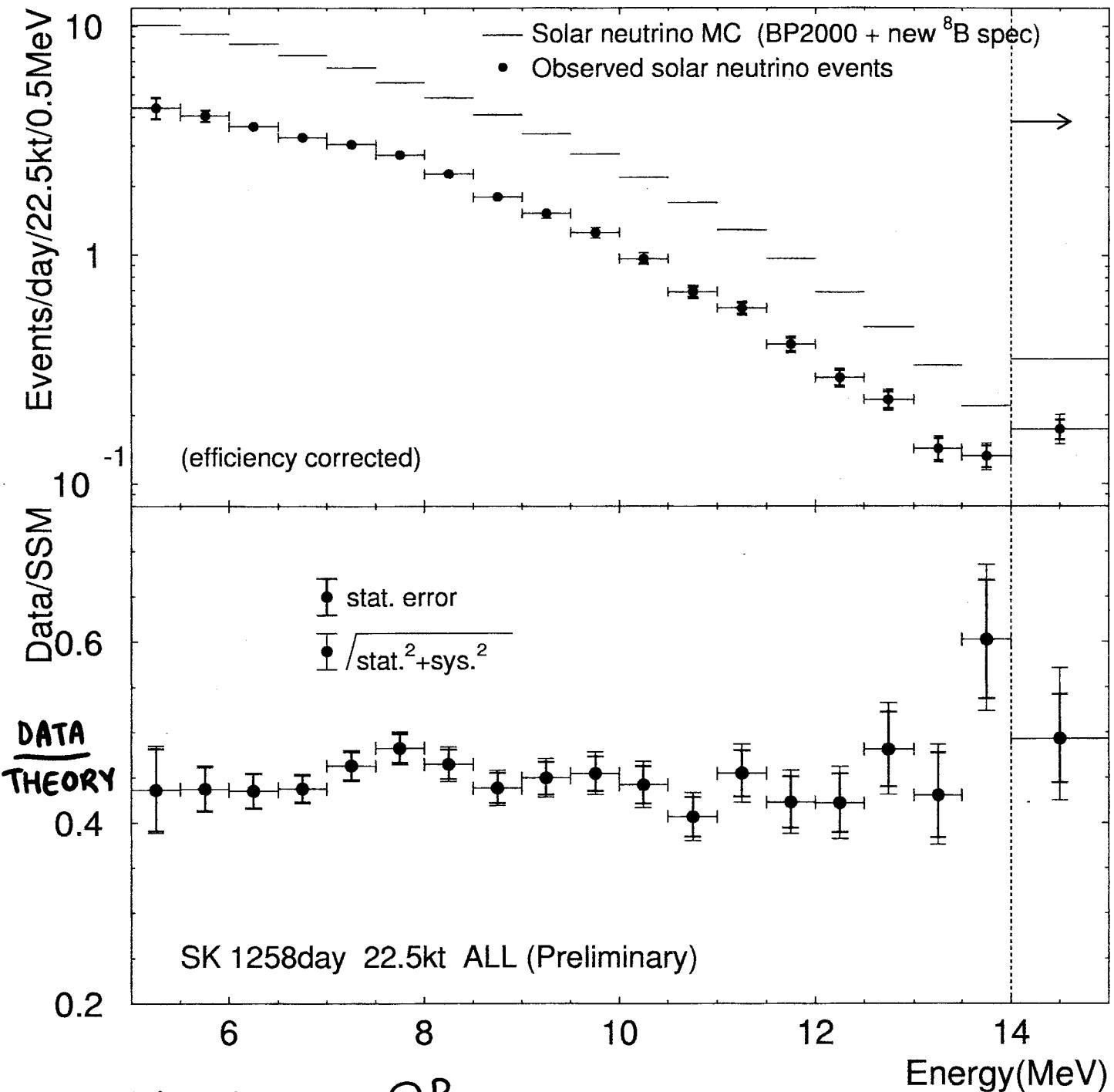
"MOVE"  
SCREEN  
BACK  
AND  
FORTH

↓  
eccentricity  
variations  
of L

→ HOPE TO "ENHANCE" INTERFERENCE PATTERN

# The Recoil Spectrum

$\nu + e \rightarrow \nu + [e]$ -spectrum



Distortion if  $\frac{\partial P_{ee}}{\partial E_\nu} \neq 0$

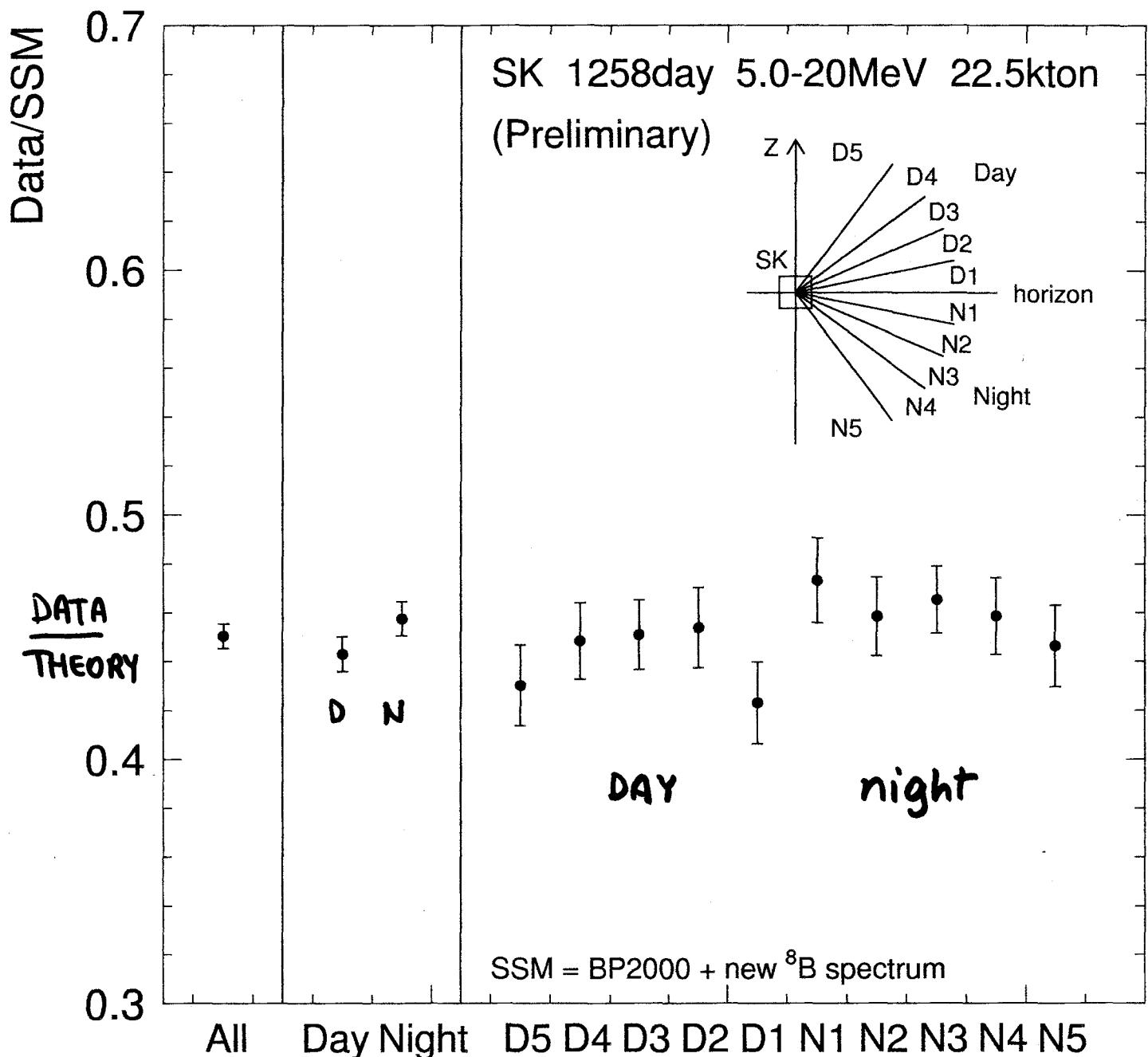
→ NOTHING SEEN

Michael B. Smy, UC Irvine

SK 2001

# Day/Night

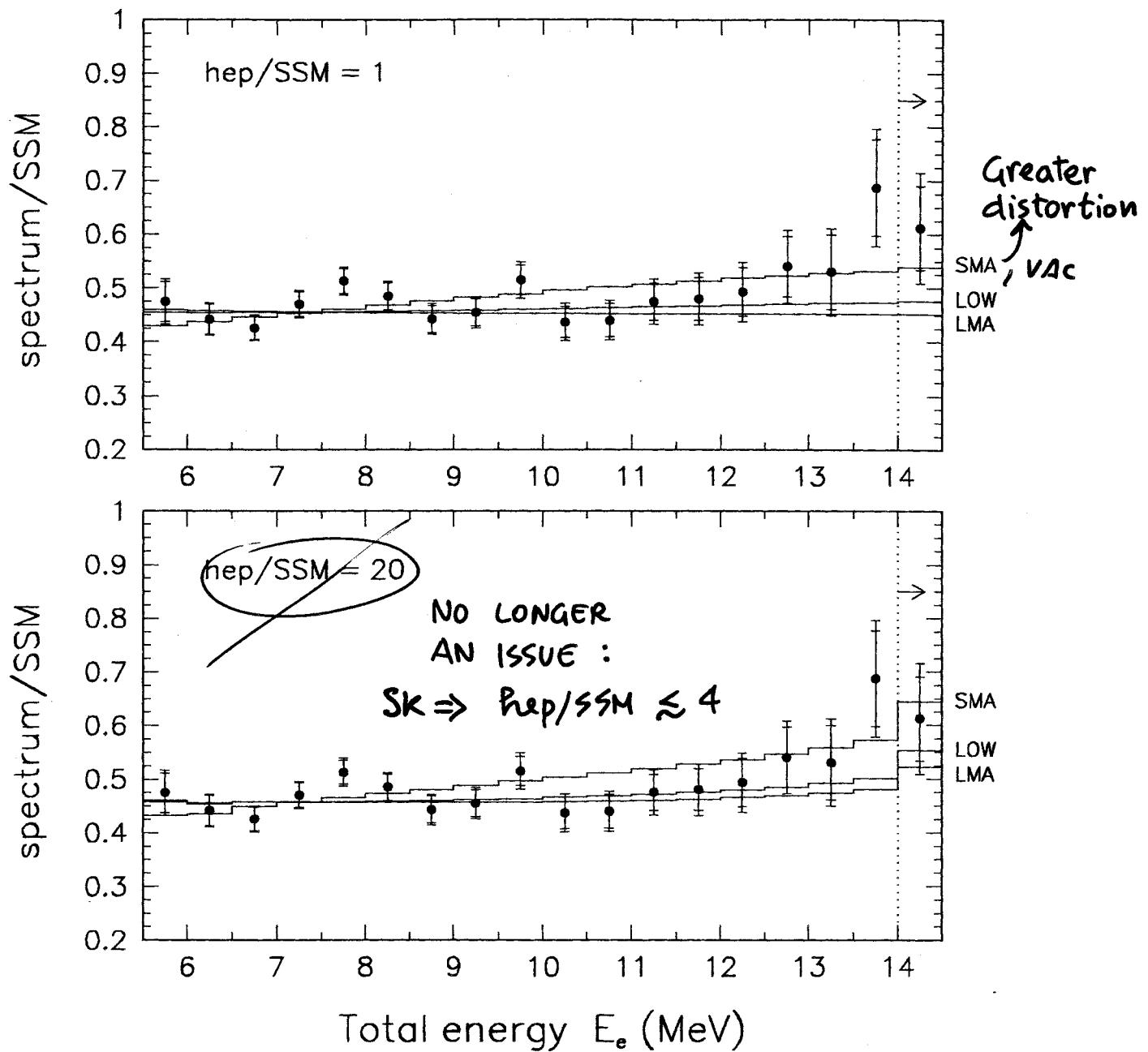
→ EARTH MATTER EFFECTS



Distortion if  $\frac{\partial \text{Pee}}{\partial N_e^{\text{Earth}}} \neq 0 \rightarrow \text{NOT SEEN}$

Michael b. Smy, UC Irvine

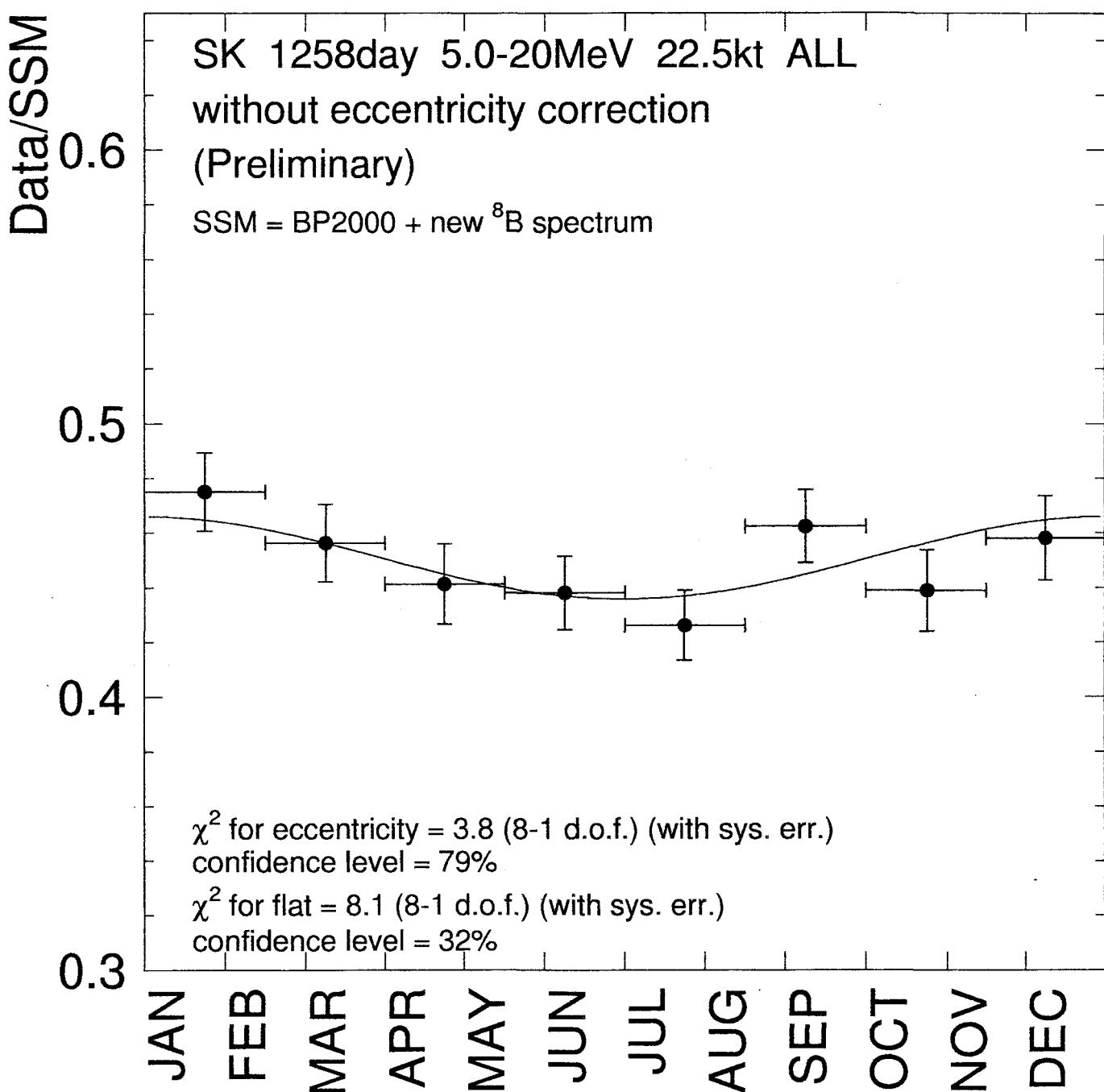
## Super-Kamiokande electron energy spectrum



SK 2001

# Seas. Variation

$$= \text{BASELINE VARIATIONS } L(t) \approx L_0 \left(1 - \epsilon \cos \frac{2\pi t}{T}\right)$$

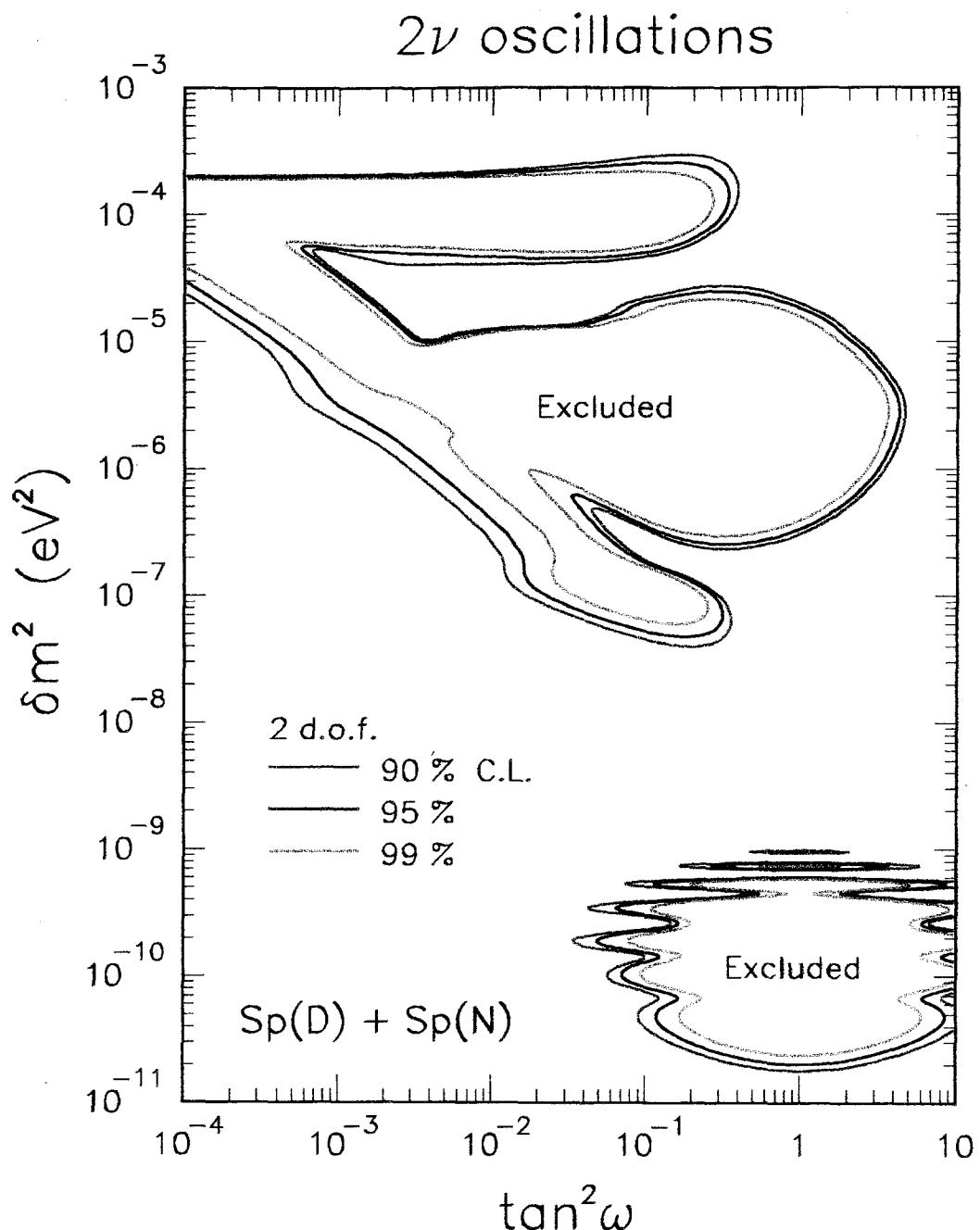


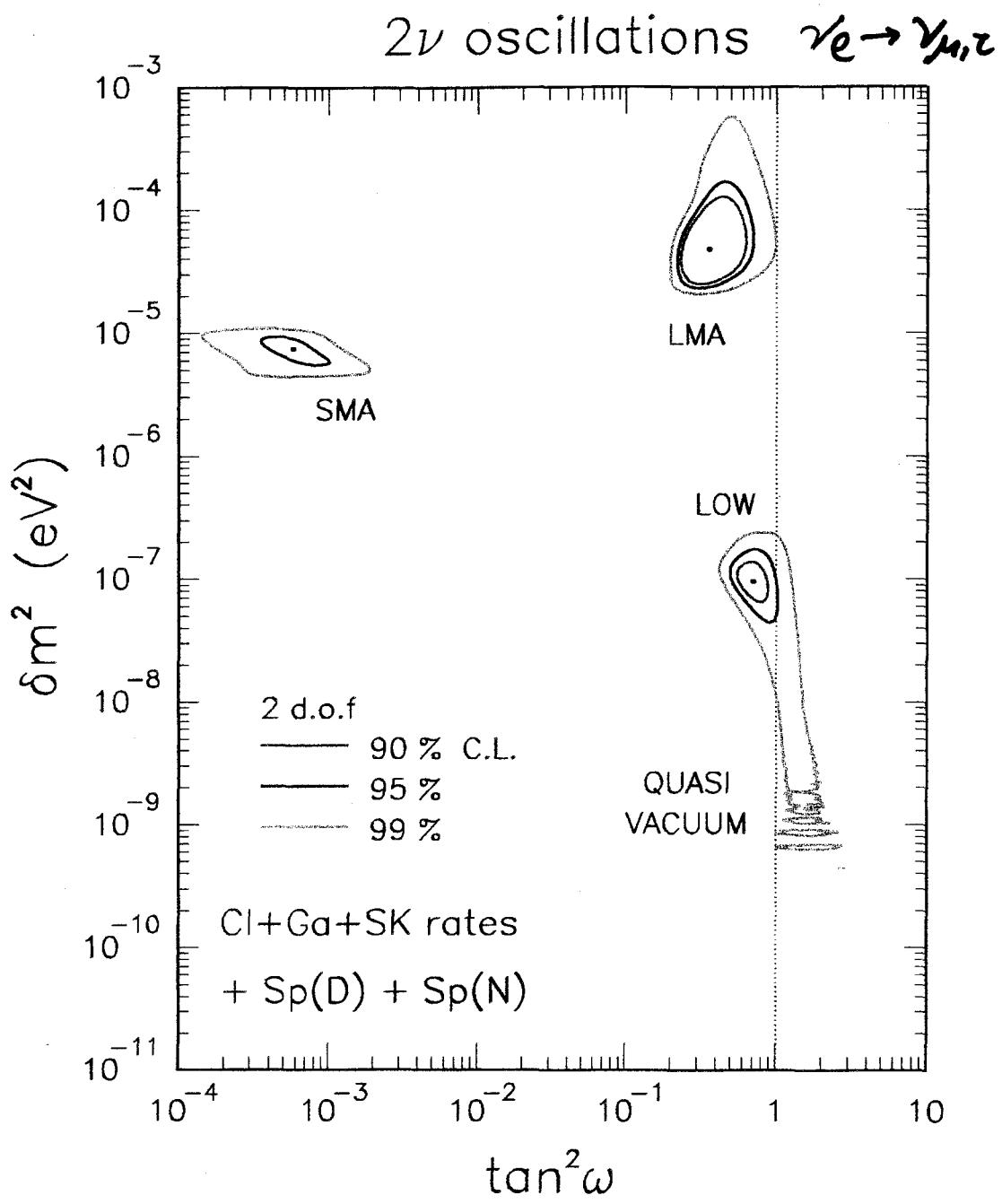
$1/r^2$  Slightly Favoured over Flat

Distortion if  $\frac{\partial P_{ee}}{\partial L} \neq 0 \rightarrow \text{NOT SEEN}$

Michael b. Smy, UC Irvine

Nonobservation of model-independent signals excludes some regions...

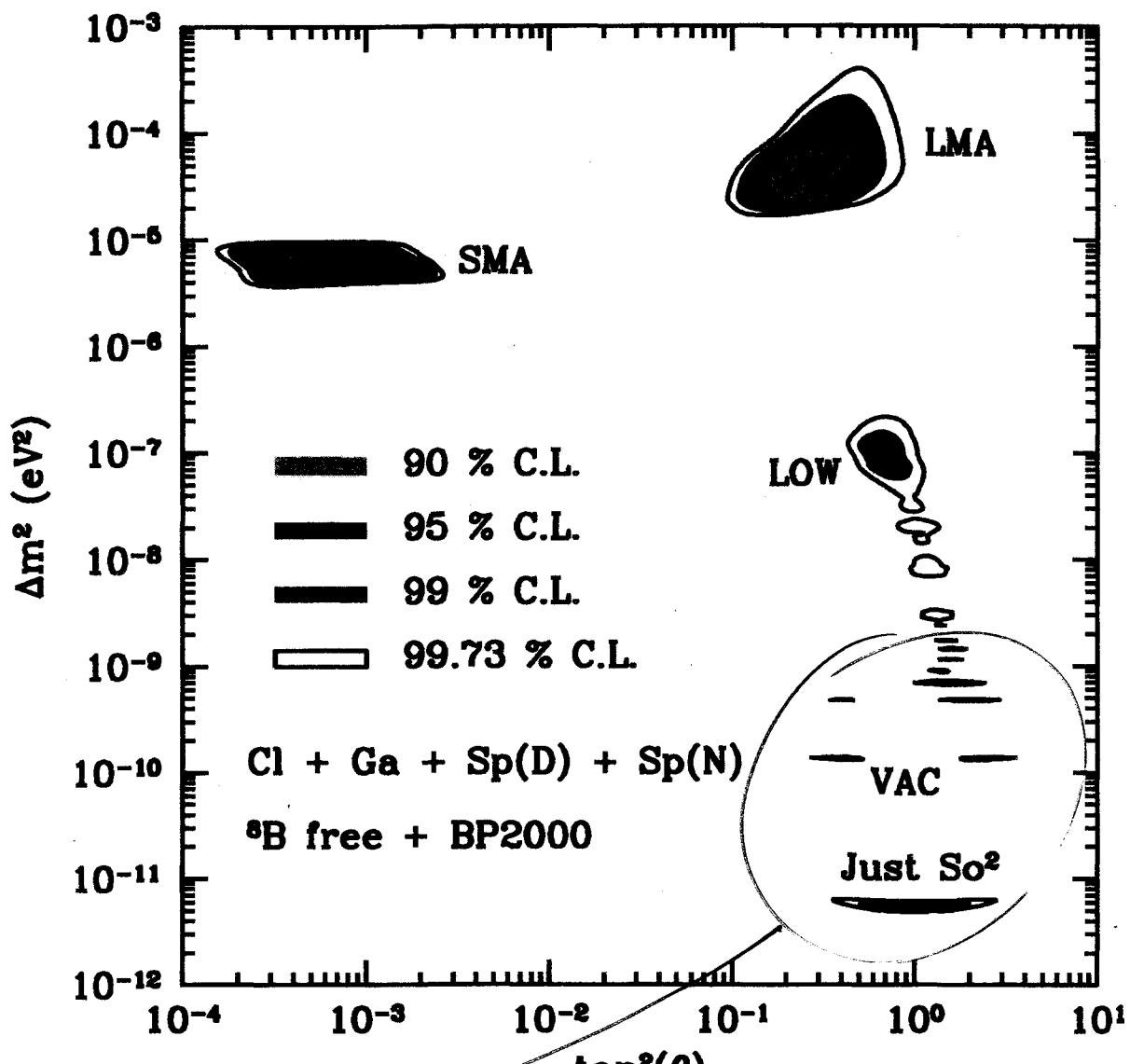




... and changes the likelihood of all solutions

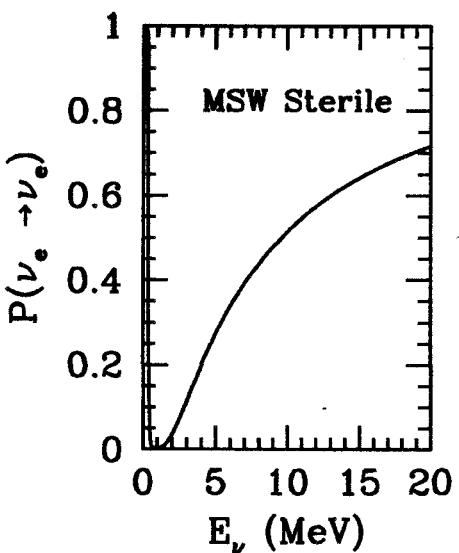
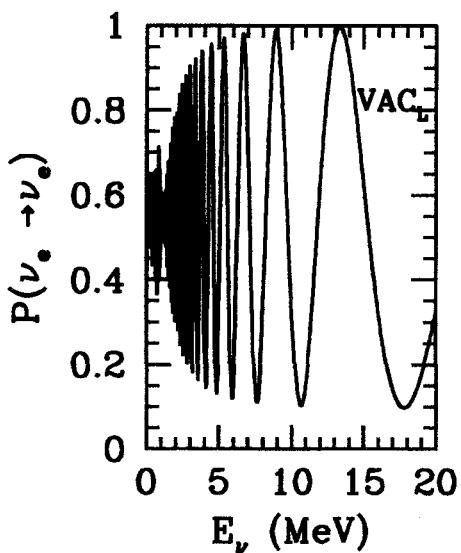
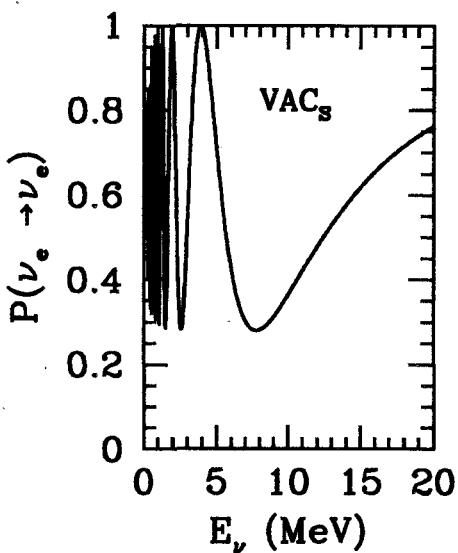
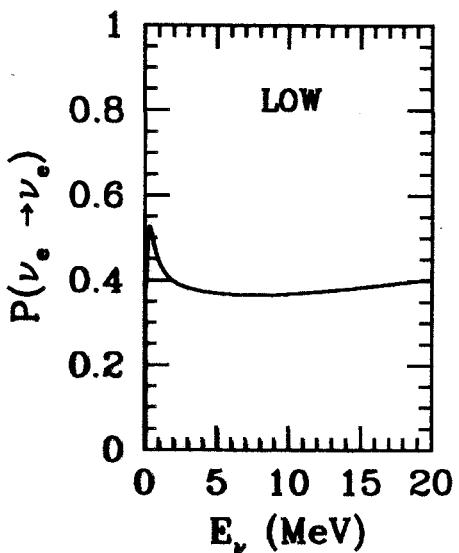
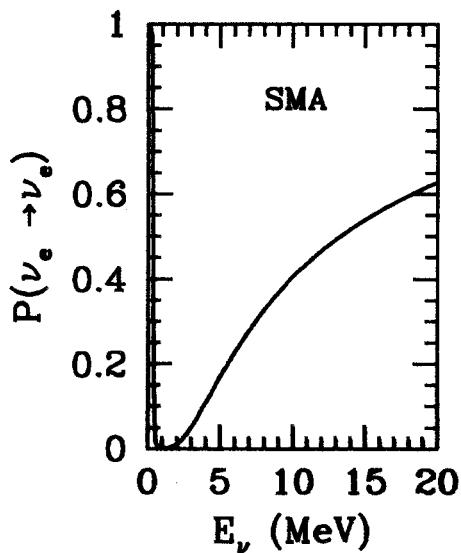
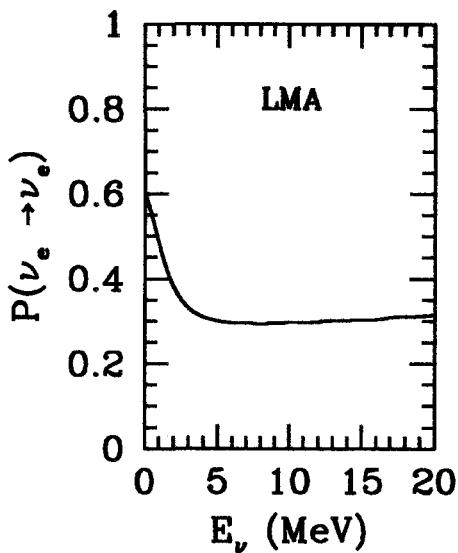
LMA favored  $\rightarrow$  ENORMOUS INTEREST  
 FOR FUTURE  $\gamma$  FACT PROJECTS, WHICH  
 CAN MEASURE (OR BE SENSITIVE) TO  $\Delta m^2_{\text{solar}}$   
 ONLY IF NOT TOO SMALL WITH RESPECT TO  $\Delta m^2_{\text{atm}}$

Similar analysis with larger uncertainties (\*B flux free) ....



Bahcall  
Krauss  
Smirnov

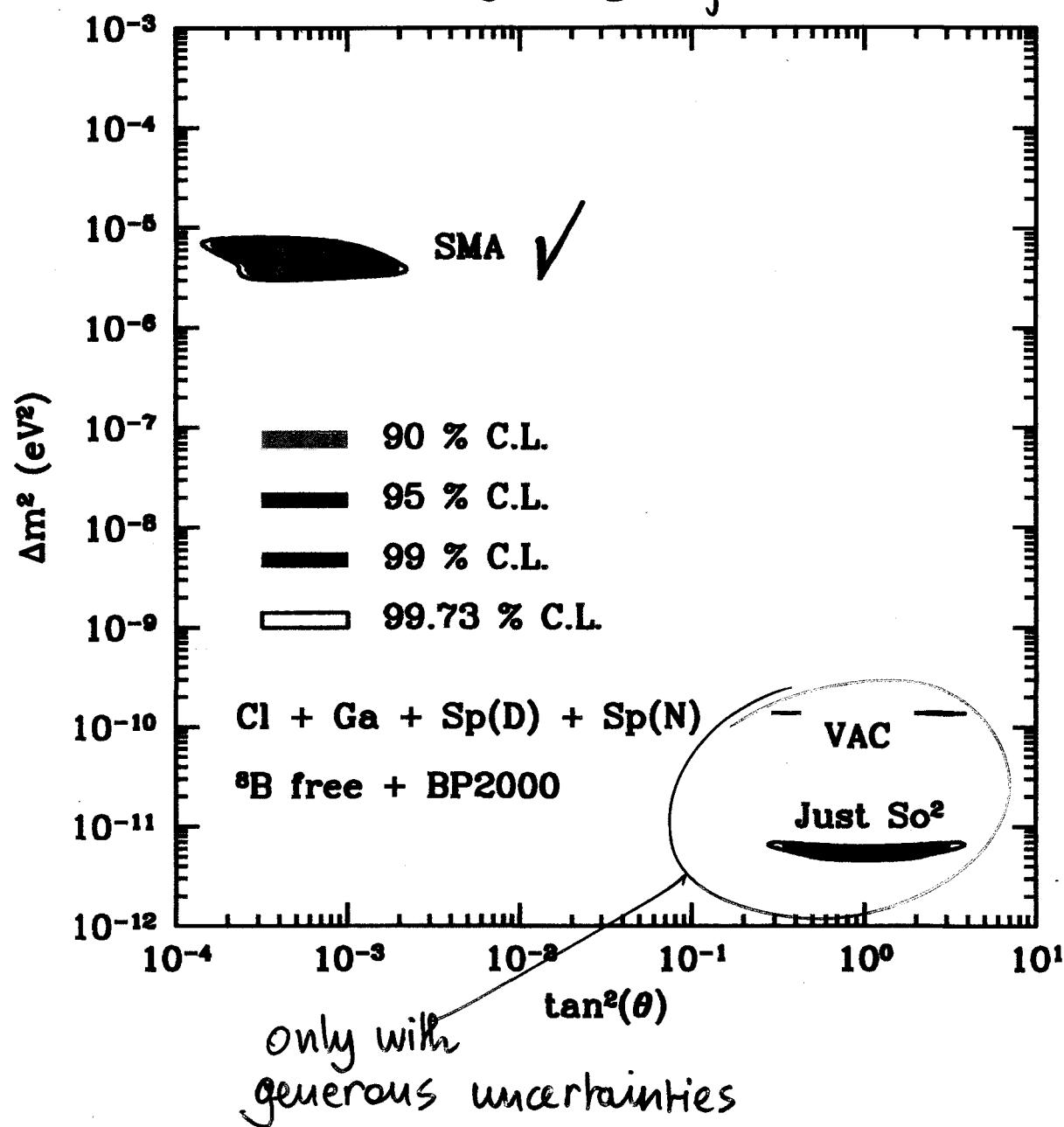
As for atm.  $\nu$ 's, oscillation pattern is "hidden" in the data. Here, however, range of possibility is even larger



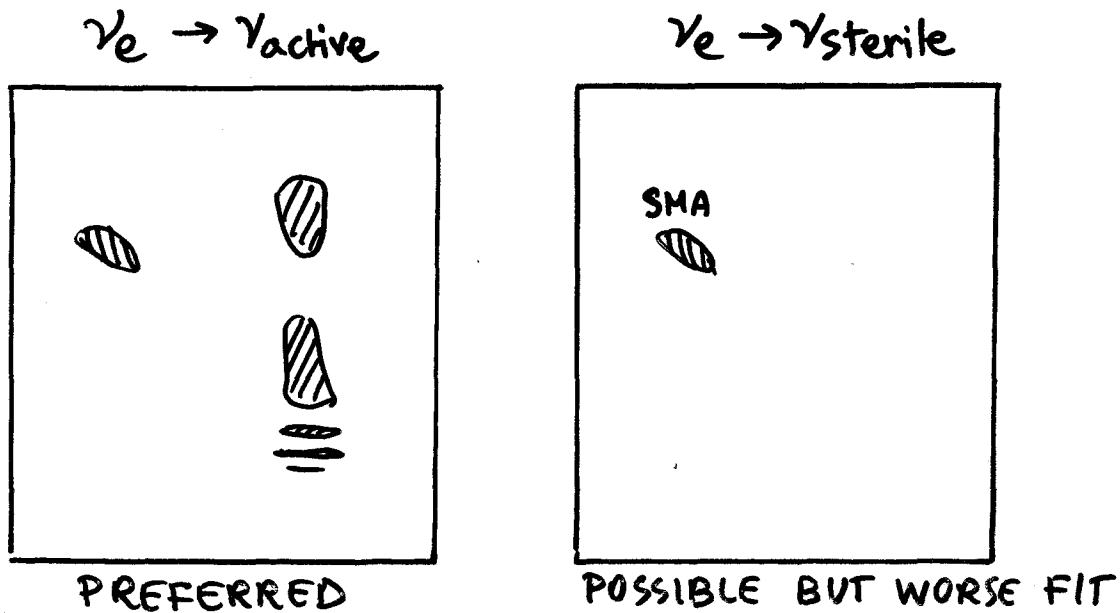
Bahcall & Krastev

for  $\gamma_e \rightarrow \gamma_S$ :  
only SMA  
Survives

$\nu_e \rightarrow \gamma_S$  fit



## TYPICALLY:



- $\nu_e \rightarrow \nu_{\text{sterile}}$  does not produce NC events in SK  $\rightarrow$  underestimates SK rate and predicts too strong VAC distortions
- PERTURBING SMA parameters can "adjust" SK without destroying agreement with other data, due to large  $dPee/dE_\nu$  in SMA region for  $E_\nu$  in SK range
- THIS IS NOT POSSIBLE FOR LMA, LOW (rather flat Pee anyway)
- In any case,  $\nu_e \rightarrow \nu_{\text{sterile}}$  fit worse than  $\nu_e \rightarrow \nu_{\text{active}}$

# CHOOZ

REACTOR EXPERIMENT

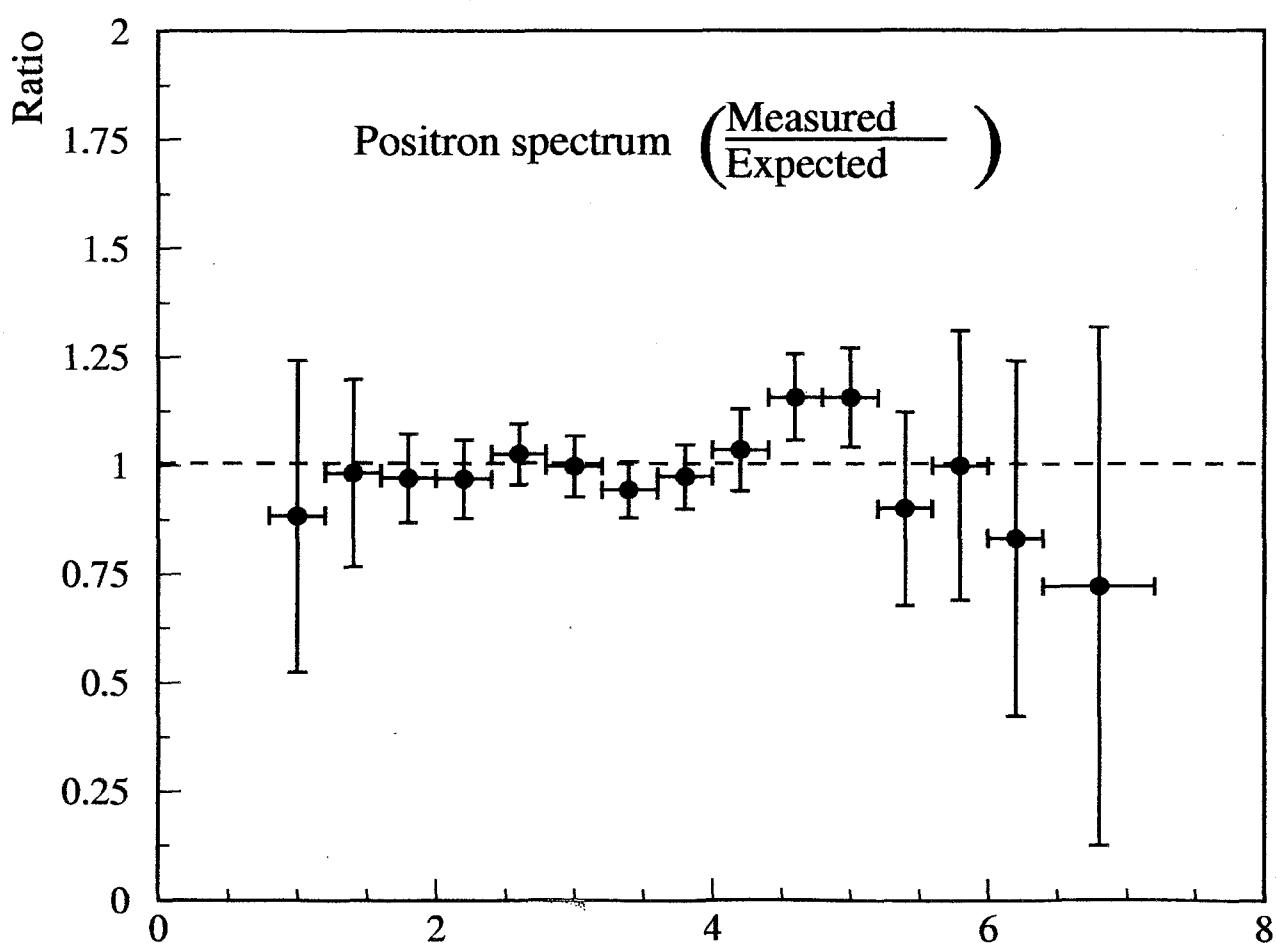
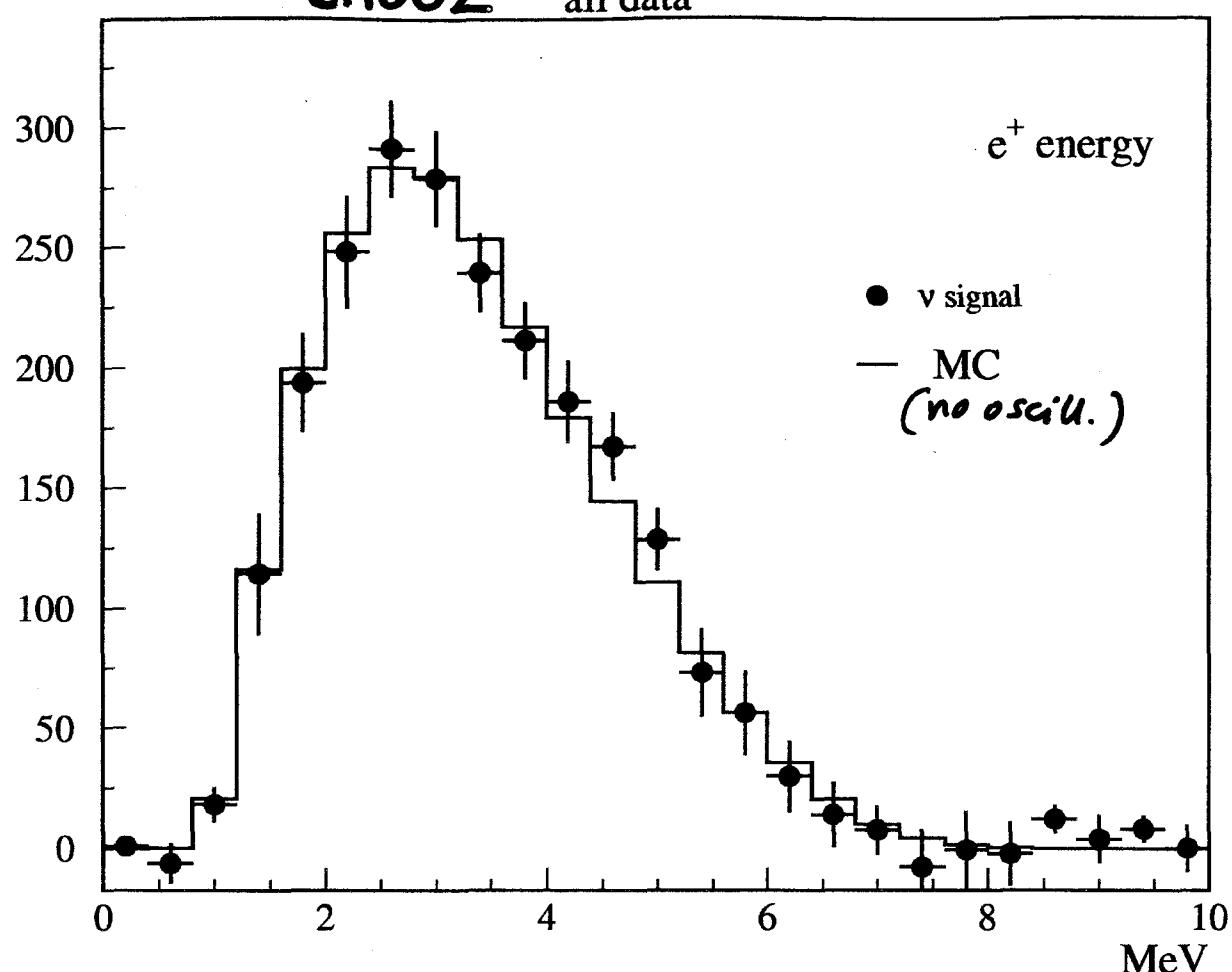
$\langle E \rangle \sim \text{few MeV}$

$L \sim 1 \text{ km}$

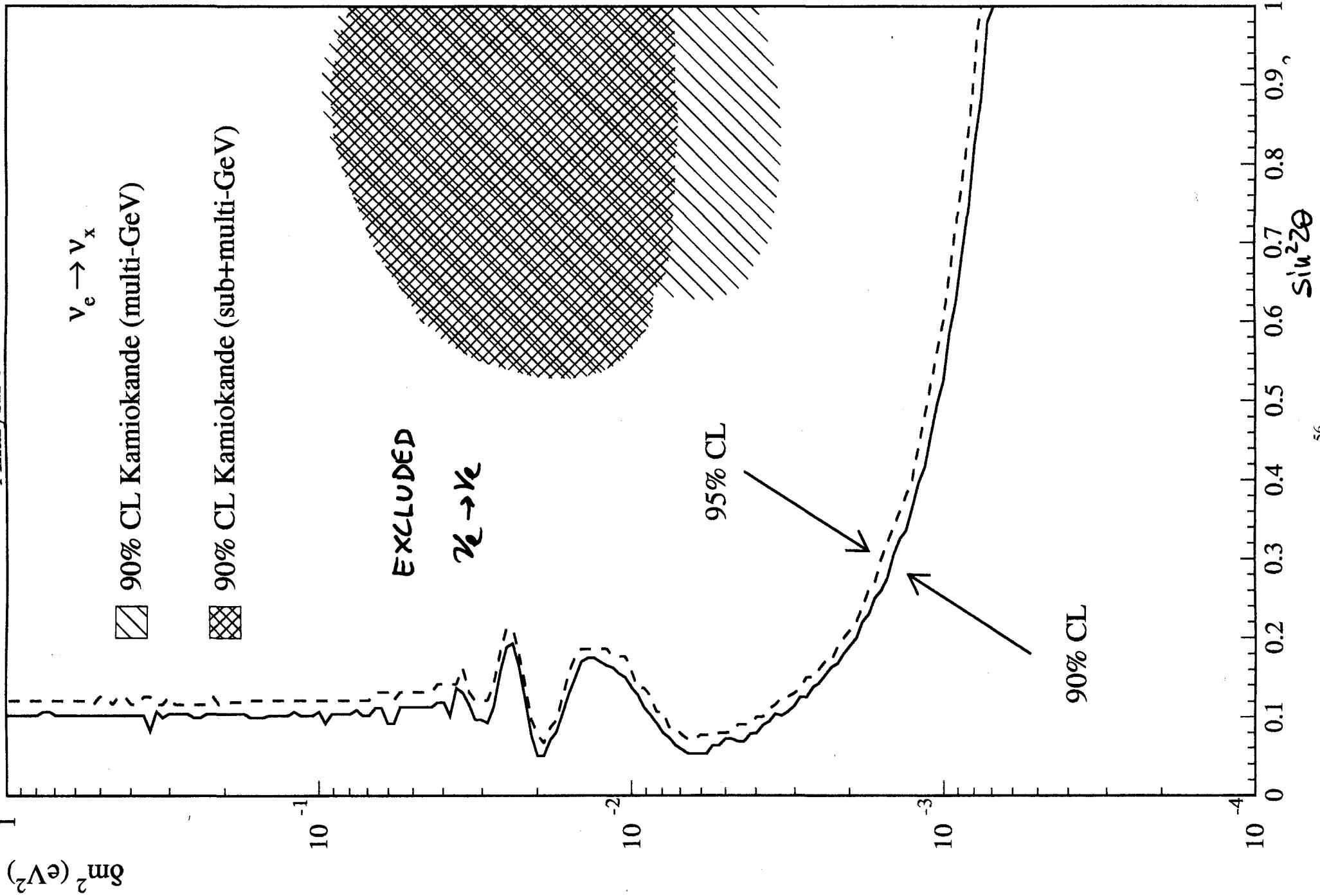
CRUCIAL BOUNDS ON  $\bar{\nu}_e \rightarrow \bar{\nu}_e$   
DISAPPEARANCE IN  
 $\Delta m^2$  RANGE PROBED BY ATM.  $\nu$

- NO SIGNAL FOUND
- REINFORCES EXCLUSION OF  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  AS EXPLANATION OF ATM  $\nu$  DATA
- FORBIDS LARGE  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  TRANSITIONS FOR  $\Delta m^2 \gtrsim 0.7 \times 10^{-3} \text{ eV}^2$

**CHOOZ** all data



Analysis A



# Schematic View of $\nu$ -beam and LSND

$$\tilde{\nu}_\mu \rightarrow \tilde{\nu}_e$$

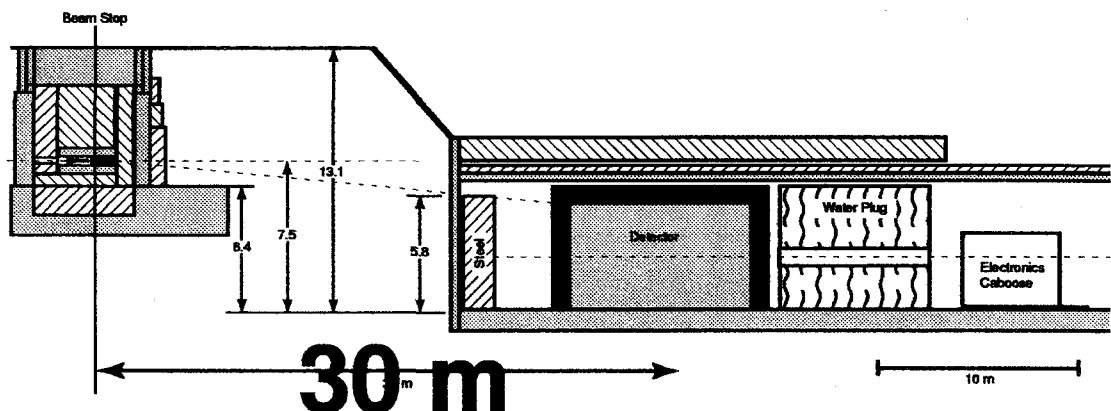


Figure 2: The LSND target/detector geometry.

**Detector:**

**1220 8-inch PMTs  
167 tons of Mineral Oil**

**Veto Shield:**

**292 5-inch PMTs  
Active + Passive Shielding**

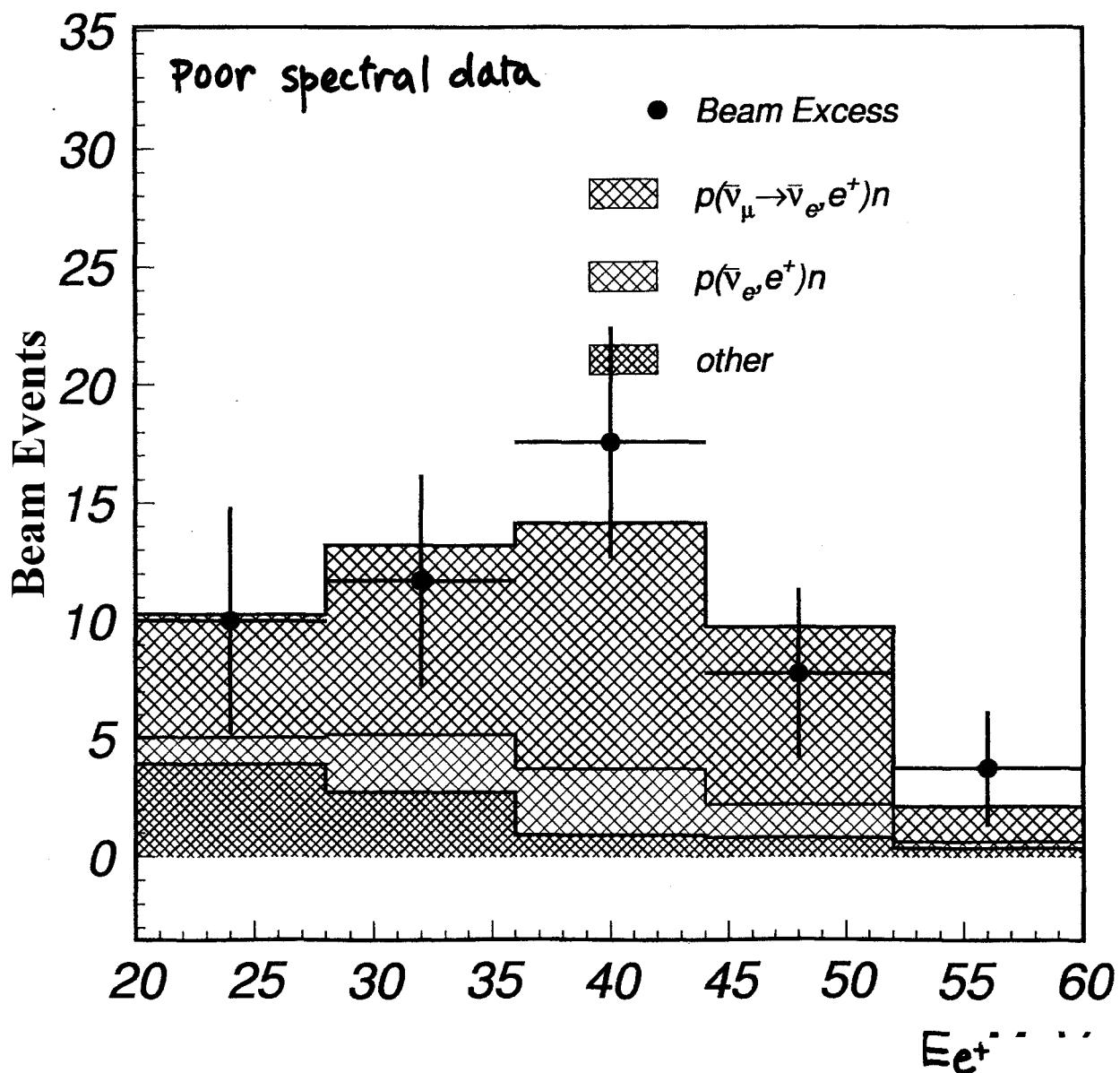
**Duty Ratio:**

**~6%**

EXPERIMENTAL EVIDENCE  
IS CONTROVERSIAL

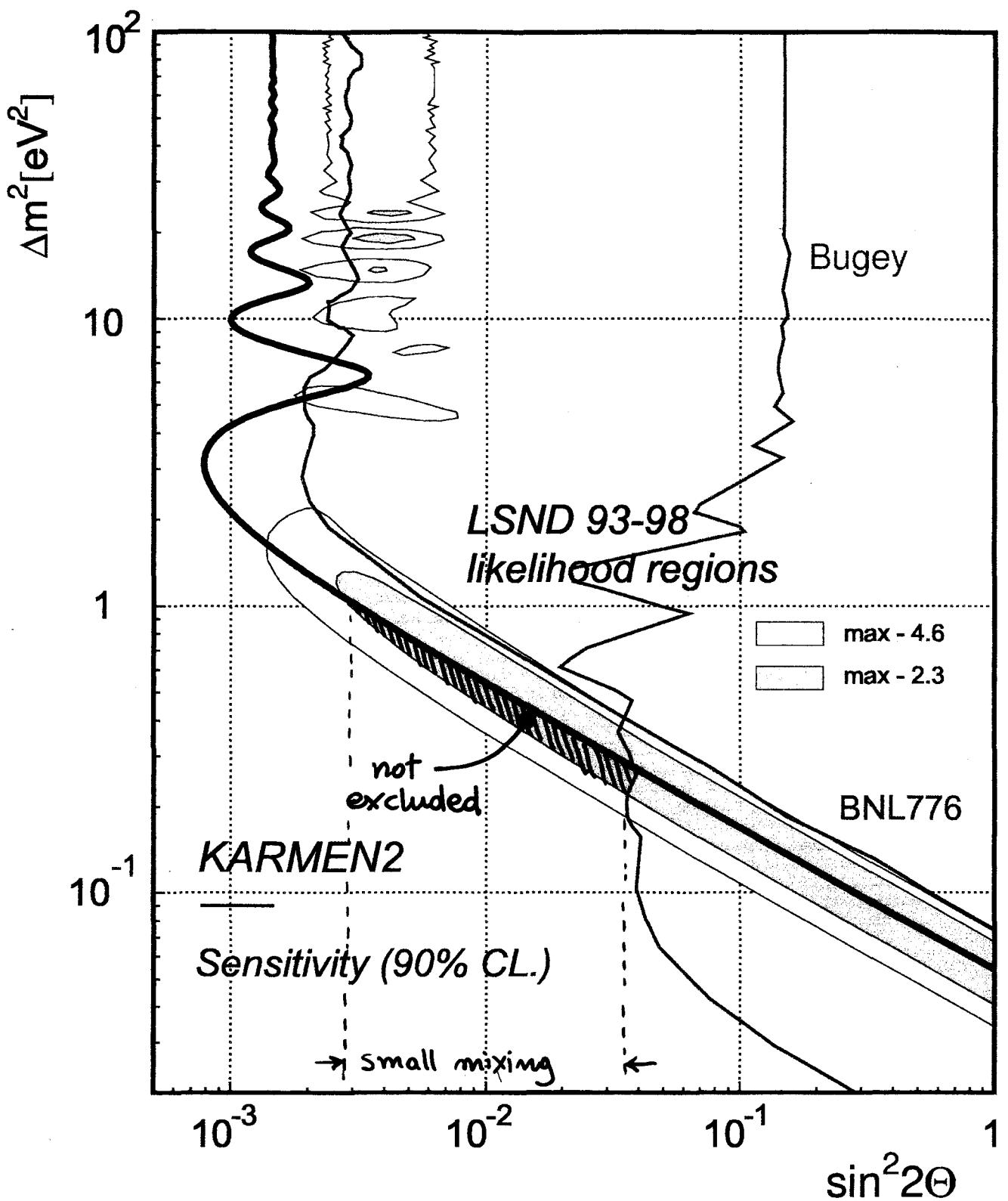
BUT IMPLICATIONS ARE  
INTERESTING ( $m_\nu \sim O(1\text{eV})$ )

NOTE :  $P_{\mu e} \sim \text{few \%}$  (small)



# EXPECTED KARMEN2 SENSITIVITY

4 years of data taking 2/97-2/01



$$\sin^2 2\theta < 1.4 \times 10^{-3} \text{ (90% CL.)}$$

Sensitivity = 'average' oscillation-limit (MC Basis)

# RECAP. (2v)

● ATMOSPHERIC $\nu$ :	$\nu_\mu \rightarrow \nu_e$	NO
$\Delta m^2 \sim 3 \times 10^{-3} \text{ eV}^2$	$\nu_\mu \rightarrow \nu_\tau$	OK
	$\nu_\mu \rightarrow \nu_s$	Strongly disfavored
● SOLAR $\nu$ :	$\nu_e \rightarrow \nu_{\mu, \tau}$	OK
$\Delta m^2 \lesssim 10^{-3} \text{ eV}^2$	$\nu_e \rightarrow \nu_s$	possible but worse fit
● CHOOZ :	NO $\nu_e$ disappearance for $\Delta m^2 \gtrsim 10^{-3} \text{ eV}^2$	
● LSND :	$\nu_\mu \rightarrow \nu_e$ (?)	
	$\Delta m^2 \sim \Theta(1 \text{ eV}^2)$	

NEXT: • COMBINATIONS  
IN 3V, 4V SCHEMES